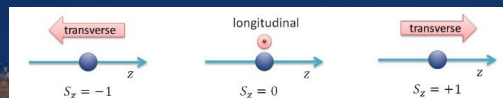


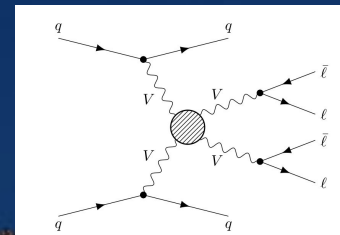
Mareen Hoppe<sup>1</sup>, Marek Schönherr<sup>2</sup>, Frank Siegert<sup>1</sup>

<sup>1</sup>Institute of Nuclear and Particle Physics, Technische Universität Dresden

<sup>2</sup>Institute for Particle Physics Phenomenology, Durham University



Dr. Z. Zinanos: Tests of the Standard Model of Particles. <https://www.mpp.mpg.de/~zinanos/material/lecture10.pdf>



# Polarized cross sections for vector boson production with Sherpa



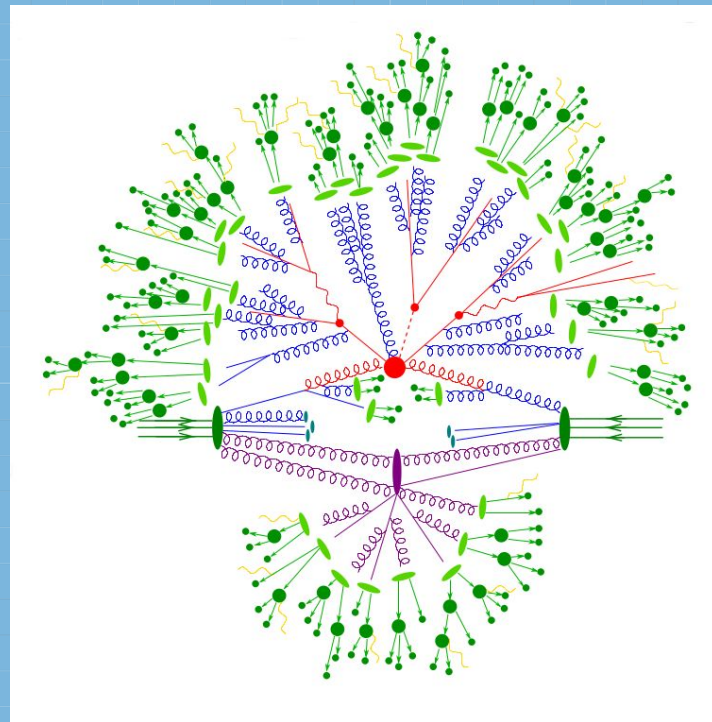
COMETA polarisation workshop Toulouse, September 23, 2024

# The SHERPA event generator

New major release SHERPA 3.0.0 since July!

[E. Bothmann et al. 2019]

- two tree-level built-in **matrix element generators**: COMIX, AMEGIC
- **higher order QCD effects**: matching via S-MC@NLO, multi-jet merging via CKKW-L algorithm
- **approximate NLO EW effects**: EWvirt & EW Sudakov
- two **parton showers**: CSS, DIRE
- **cluster fragmentation** model
- **hadron- and tau-decay** module
- **multiple interaction** simulation á la PYTHIA
- **higher-order QED effects** via YFS resummation
- interfaces to
  - OpenLoops
  - Recola
  - GoSam
  - MCFM
  - BlackHat
  - MadLoop
  - RIVET 3 & 4
  - UFO
  - PYTHIA 8



Hard process  
Parton shower  
QED radiation

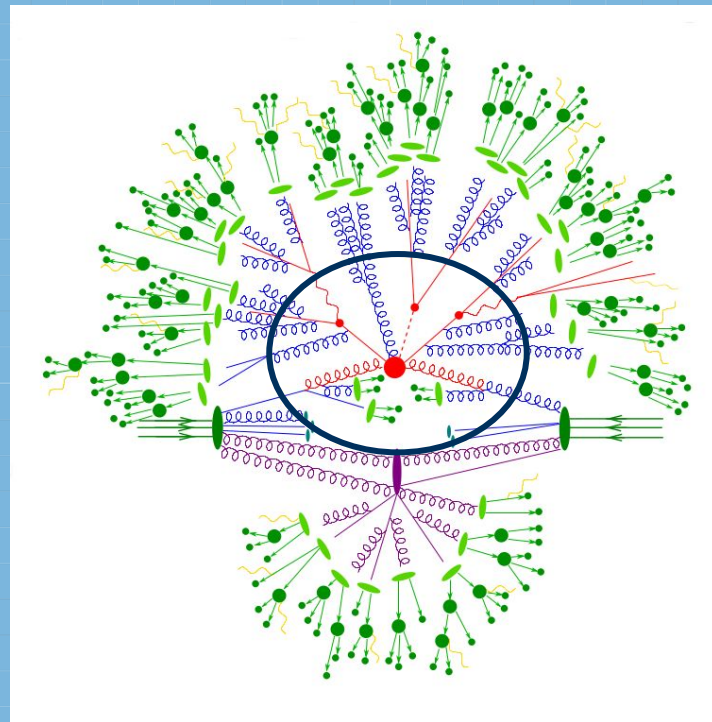
Hadronization  
Hadron decays  
Multiple interactions

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Hard process  
Parton shower  
QED radiation

Hadronization  
Hadron decays  
Multiple interactions

# *SHERPA's polarization framework*

## **Design principles & features**

# Polarized cross sections for intermediate particles

$$\frac{d\sigma}{dX} = f_L \frac{d\sigma_L}{dX} + f_R \frac{d\sigma_R}{dX} + f_0 \frac{d\sigma_0}{dX} \left( + f_{int.} \frac{d\sigma_{int.}}{dX} \right)$$

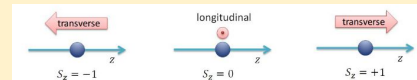
## Polarization for intermediate particles

- completeness relation

$$\left( -g^{\mu\nu} + \frac{q^\mu q^\nu}{m_V^2} \right) = \sum_{\lambda=1}^4 \varepsilon^\mu(q, \lambda) \varepsilon^{*\nu}(q, \lambda)$$

- lead to interferences between different polarisations

## Polarization Basis



Dr. Z. Zinonos: Tests of the Standard Model of Particles. <https://www.mpp.mpg.de/~zinonos/material/lecture10.pdf>

- helicity basis

$$\varepsilon_{\pm}^{\mu}(q) = \frac{e^{\mp i\phi}}{\sqrt{2}} (0, -\cos\theta \cos\phi \pm i\sin\phi, -\cos\theta \sin\phi \mp i\cos\phi, \sin\theta)$$

$$\varepsilon_0^{\mu}(q) = \frac{q^0}{m} \left( \frac{|\vec{q}|}{q^0}, \cos\phi \sin\theta, \sin\phi \sin\theta, \cos\theta \right)$$

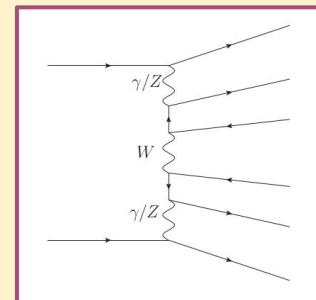
- frame dependent!

## Separation of polarization

- amplitude needs to factorize: production  $\otimes$  propagator  $\otimes$  decay
- problem: non-resonant diagrams  
→ no polarisation definition, but necessary for gauge invariance
- **solution:** appropriate approximations - gauge invariant options:

- Pole Approximation ((D)PA)
- Narrow-Width Approximation (NWA)

$$\frac{1}{(q^2 - m_V^2)^2 + \Gamma_V^2 m_V^2} \rightarrow \frac{\pi \delta(q^2 - m_V^2)}{\Gamma_V m_V}$$





# The narrow-width approximation

$$\mathcal{M} = \mathcal{M}_\mu^{\text{prod}} \left( \frac{i(-g^{\mu\nu} + \frac{q^\mu q^\nu}{m_V^2})}{q^2 - m_V^2 + i\Gamma_V m_V} \right) \mathcal{M}_\nu^{\text{decay}}$$

$$\left(-g^{\mu\nu} + \frac{q^\mu q^\nu}{m_V^2}\right) = \sum_{\lambda=1}^4 \varepsilon^\mu(q, \lambda) \varepsilon^{*\nu}(q, \lambda) \quad \text{Completeness relation}$$

$$\frac{1}{(q^2 - m_V^2)^2 + \Gamma_V^2 m_V^2} \rightarrow \frac{\pi \delta(q^2 - m_V^2)}{\Gamma_V m_V} \quad \text{Narrow width approximation}$$

$$|\mathcal{M}|^2 \propto \sum_{\lambda_1 \dots \lambda_n; \lambda'_1 \dots \lambda'_n} \mathcal{M}_{\lambda_1 \dots \lambda_n}^{\text{P}} \mathcal{M}_{\lambda'_1 \dots \lambda'_n}^{*\text{P}} \mathcal{M}_{\lambda_1 \dots \lambda_n}^{\text{D}} \mathcal{M}_{\lambda'_1 \dots \lambda'_n}^{*\text{D}}$$

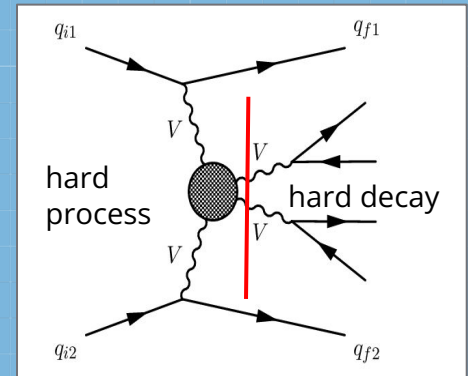
hard process

$$|\mathcal{M}^{\text{P}}|^2 = \sum_{\lambda_1 \dots \lambda_n} \mathcal{M}_{\lambda_1 \dots \lambda_n}^{\text{P}} \mathcal{M}_{\lambda_1 \dots \lambda_n}^{*\text{P}}$$



hard decay

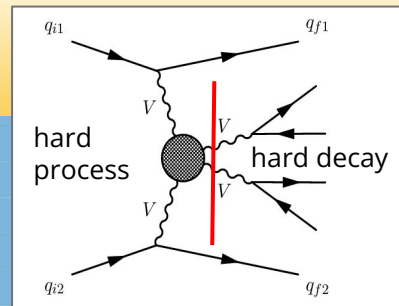
$$|\mathcal{M}^{\text{D}}|^2 = \sum_{\lambda_1 \dots \lambda_n} \mathcal{M}_{\lambda_1 \dots \lambda_n}^{\text{D}} \mathcal{M}_{\lambda_1 \dots \lambda_n}^{*\text{D}}$$



- **PROBLEM: spin correlations**
- ➔ **solution: spin-correlation algorithm** [P. Richardson 2001]

# On-shell Approximation in SHERPA

[S. Höche et al. 2014]



- **extended narrow-width approximation:**
  - spin correlations preserved
  - off-shell effects via mass smearing of on-shell vector boson states

01

Simulation of unpolarized production process

$$|\mathcal{M}^P|^2 = \sum_{\lambda_1 \dots \lambda_n} \mathcal{M}_{\lambda_1 \dots \lambda_n}^P \mathcal{M}_{\lambda_1 \dots \lambda_n}^{*P}$$

02

Recalculation of the production amplitude tensor

$$|\mathcal{M}^P|^2_{\lambda_1 \dots \lambda_n; \lambda'_1 \dots \lambda'_n} = \mathcal{M}_{\lambda_1 \dots \lambda_n}^P \mathcal{M}_{\lambda'_1 \dots \lambda'_n}^{*P}$$

03

Spin correlation algorithm generates decay chain, LO decay matrices [P. Richardson 2001]

$$\mathcal{D}_{\lambda_A \lambda'_A} = \frac{1}{\mathcal{N}_D} \mathcal{M}_{\lambda_A}^D \mathcal{M}_{\lambda'_A}^{D*}$$

04

Mass Smearing of the intermediate vector bosons according to Breit-Wigner distribution

$$\text{BW} \sim \frac{1}{(p^2 - M^2)^2 + \Gamma^2 M^2}$$

E, |p| adjusted while preserving direction of flight in FS COM to account for new virtuality

05

Reweighting of production cross section with decay branching ratio

$$|\mathcal{M}^{\text{NWA}}|^2 = |\mathcal{M}^P|^2 \times \text{BR}$$

- algorithm for polarized cross sections:
  - simulation essentially unpolarized
  - polarization fractions calculated on top
  - starting point: production amplitude tensor & decay matrices from spin correlation algorithm

1. Separated amplitudes from unpolarized simulation

2. Transformation to desired spin basis

3. Multiplication of production & decay

4. Calculation of polarization fractions & labeling

5. Multiplication with event XS & output as event weights

$$\begin{matrix} \tilde{\mathcal{M}}_{\kappa_1 \dots \kappa_n}^{\mathcal{P}} & \tilde{\mathcal{M}}_{\kappa'_1 \dots \kappa'_n}^{*\mathcal{P}} \\ \tilde{\mathcal{M}}_{\kappa_1 \dots \kappa_n}^{\mathcal{D}} & \tilde{\mathcal{M}}_{\kappa'_1 \dots \kappa'_n}^{*\mathcal{D}} \end{matrix}$$

$$|\mathcal{M}|_{\lambda_1 \dots \lambda_n; \lambda'_1 \dots \lambda'_n}^2 = \sum_{\kappa_1 \kappa'_1 \dots \kappa_n \kappa'_n} a_{\lambda_1 \kappa_1}^{\text{part1}} a_{\lambda'_1 \kappa'_1}^{\text{part1}*} \dots \dots a_{\lambda_n \kappa_n}^{\text{partn}} a_{\lambda'_n \kappa'_n}^{\text{partn}*} |\tilde{\mathcal{M}}|_{\kappa_1 \dots \kappa_n; \kappa'_1 \dots \kappa'_n}^2$$

$$|\mathcal{M}^{\text{pol}}|_{\lambda_1 \dots \lambda_n; \lambda'_1 \dots \lambda'_n}^2 \propto \mathcal{M}_{\lambda_1 \dots \lambda_n}^{\mathcal{P}} \mathcal{M}_{\lambda'_1 \dots \lambda'_n}^{*\mathcal{P}} \mathcal{M}_{\lambda_1 \dots \lambda_n}^{\mathcal{D}} \mathcal{M}_{\lambda'_1 \dots \lambda'_n}^{*\mathcal{D}}$$

$$\text{Frac}_{\lambda_1 \dots \lambda_n; \lambda'_1 \dots \lambda'_n} = \frac{|\mathcal{M}^{\text{pol}}|_{\lambda_1 \dots \lambda_n; \lambda'_1 \dots \lambda'_n}^2}{\sum_{\lambda_1 \dots \lambda_n; \lambda'_1 \dots \lambda'_n} |\mathcal{M}^{\text{pol}}|_{\lambda_1 \dots \lambda_n; \lambda'_1 \dots \lambda'_n}^2}$$

Nominal or variation name	XS [pb]
Nominal	0.00636840738801
PolWeight_COM.W+.W+.+	0.00606858451764
PolWeight_COM.W+.W+.-	0.00078445056672
PolWeight_COM.W+.W+.0	0.00037696877407
PolWeight_COM.W+.-W+.+	0.00077432059972
PolWeight_COM.W+.-W+.-	0.00140317472405
PolWeight_COM.W+.-W+.0	0.00063431615306
PolWeight_COM.W+.0W+.+	0.00037938319197
PolWeight_COM.W+.0W+.-	0.00063363366425
PolWeight_COM.W+.0W+.0	0.00065521961374
PolWeight_COM.W+.0W+.T	0.00101508799740
PolWeight_COM.W+.0W+.t	0.00101301683622
PolWeight_COM.W+.TW+.0	0.00101353727376
PolWeight_COM.W+.TW+.T	0.00364953844553
PolWeight_COM.W+.tW+.0	0.00101110492712
PolWeight_COM.W+.tW+.t	0.00365053040852



# Key part of the polarization framework: Transformation of the matrix elements

- two ways to change polarization definition in matrix elements:
  - a priori: change polarization definition directly in matrix element generator
  - **a posteriori: transformation of calculated production tensor, decay matrices**
- change of basis = basis transformation of polarization vectors

$$\begin{pmatrix} \tilde{\epsilon}_+^0 & \tilde{\epsilon}_-^0 & \tilde{\epsilon}_0^0 \\ \tilde{\epsilon}_+^1 & \tilde{\epsilon}_-^1 & \tilde{\epsilon}_0^1 \\ \tilde{\epsilon}_+^2 & \tilde{\epsilon}_-^2 & \tilde{\epsilon}_0^2 \\ \tilde{\epsilon}_+^3 & \tilde{\epsilon}_-^3 & \tilde{\epsilon}_0^3 \end{pmatrix} = \begin{pmatrix} \epsilon_+^0 & \epsilon_-^0 & \epsilon_0^0 \\ \epsilon_+^1 & \epsilon_-^1 & \epsilon_0^1 \\ \epsilon_+^2 & \epsilon_-^2 & \epsilon_0^2 \\ \epsilon_+^3 & \epsilon_-^3 & \epsilon_0^3 \end{pmatrix} \begin{pmatrix} a_{++} & a_{-+} & a_{0+} \\ a_{+-} & a_{--} & a_{0-} \\ a_{+0} & a_{-0} & a_{00} \end{pmatrix}$$

matrix of new polarization vectors

matrix of default polarization vectors

transformation coefficients

- transformation of matrix elements

$$|\mathcal{M}|_{\lambda_1 \lambda'_1 \dots \lambda_n \lambda'_n}^2 = \sum_{\kappa_1 \kappa'_1 \dots \kappa_n \kappa'_n} a_{\lambda_1 \kappa_1}^{\text{part1}} a_{\lambda'_1 \kappa'_1}^{\text{part1}*} \dots a_{\lambda_n \kappa_n}^{\text{partn}} a_{\lambda'_n \kappa'_n}^{\text{partn}*} |\mathcal{M}|_{\kappa_1 \kappa'_1 \dots \kappa_n \kappa'_n}^2$$

matrix element in new basis

linear combination coefficients

matrix element in default basis

- algorithm for polarized cross sections:
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PolWeight_COM.W+.0W+.0	0.00065521961374
PolWeight_COM.W+.0W+.T	0.00101508799740
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PolWeight_COM.W+.TW+.0	0.00101353727376
PolWeight_COM.W+.TW+.T	0.00364953844553
PolWeight_COM.W+.tW+.0	0.00101110492712
PolWeight_COM.W+.tW+.t	0.00365053040852

# Advantages



bluemoji.io

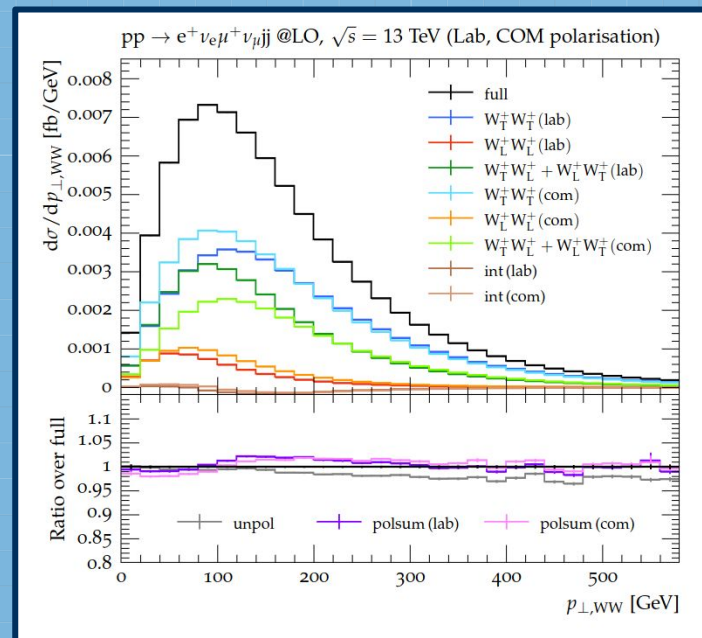
- + fully differential (per event) polarization fractions for all polarization combinations & interference

$$\underbrace{|\mathcal{M}|^2}_{\text{coherent sum}} = \underbrace{\sum_{\lambda} |\mathcal{M}_{\lambda}^{\mathcal{F}}|^2}_{\text{polarised contributions, incoherent sum}} + \underbrace{\sum_{\lambda \neq \lambda'} \mathcal{M}_{\lambda}^{\mathcal{F}} \mathcal{M}_{\lambda'}^{*\mathcal{F}}}_{\text{interference}},$$

- + different polarization definitions in one simulation run

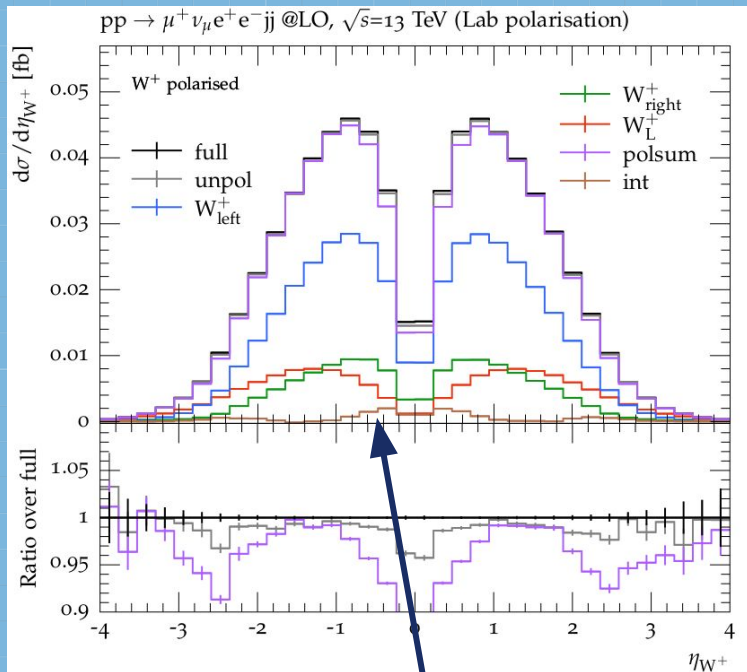
- ✓ laboratory frame
- ✓ center of mass frame of arbitrary combination of initial- / final state particles
- ✓ parton-parton frame
- ✓ easily extendable, if necessary

W<sup>+</sup>W<sup>+</sup>-scattering

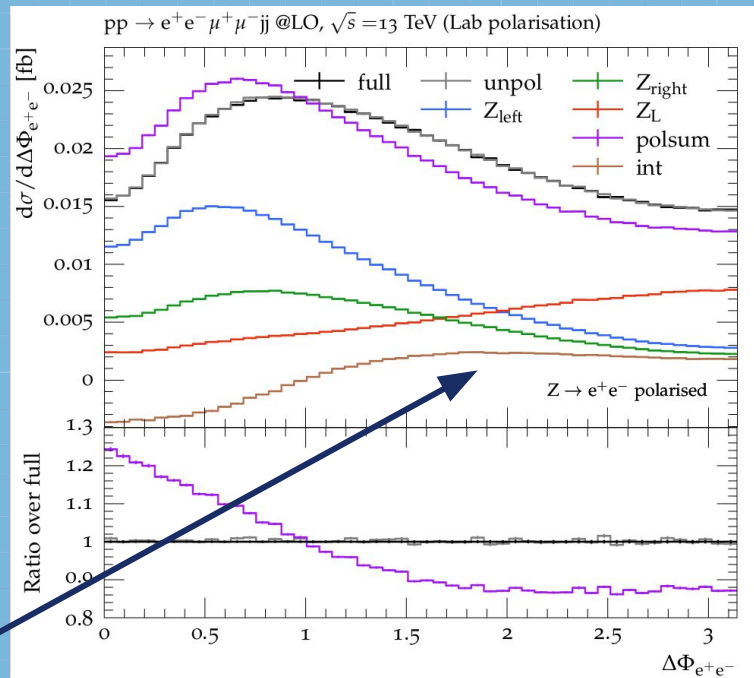


# Interference templates

$W^+Z$ -scattering



$ZZ$ -scattering



➤ interference not always negligible

# *SHERPA's polarization framework*

## **Higher order effects & BSM**

# Polarized cross sections matched to PS - MC@NLO

[S. Höche et al. 2012]

idea MC@NLO: double counting eliminated by subtraction of the shower contribution at fixed order from contributions of the hard process at higher orders

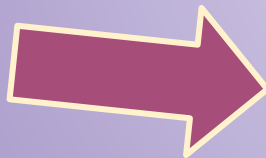
$$\sigma_{\text{MC@NLO}}^{\text{NLO}} = \underbrace{\int d\tilde{\Phi}_n \bar{B}_n^A(\tilde{\Phi}_n) \left[ \bar{\Delta}^A(t_0) + \int_{t_0} d\tilde{\Phi}_1 \frac{D_n^A(\tilde{\Phi}_{n+1})}{B_n(\tilde{\Phi}_n)} \bar{\Delta}^A(t) \right]}_{=:\sigma_{\text{S}}} + \underbrace{\int d\tilde{\Phi}_{n+1} H_n^A(\tilde{\Phi}_{n+1})}_{=:\sigma_{\text{H}}}$$

## Resolved S-events

- universal-soft-collinear radiation pattern in PS approximation above PS IR cutoff

- construction from complete real emission amplitude

virtual, ultra-soft & ultra-collinear emission effects neglected for polarization fractions



## Recalculation of the amplitude tensor in dependency of event type

### Unresolved S-events

- emissions below PS IR cutoff
- virtual corrections

- construction from Born amplitude

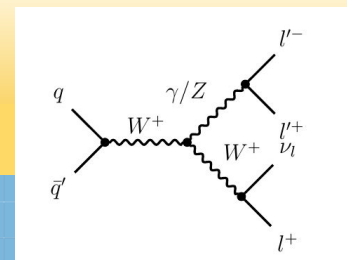
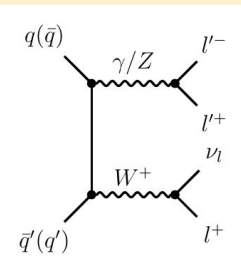
### H-events

- hard, well-separated emissions beyond PS starting scale
- process-specific corrections to universal soft-collinear emission pattern

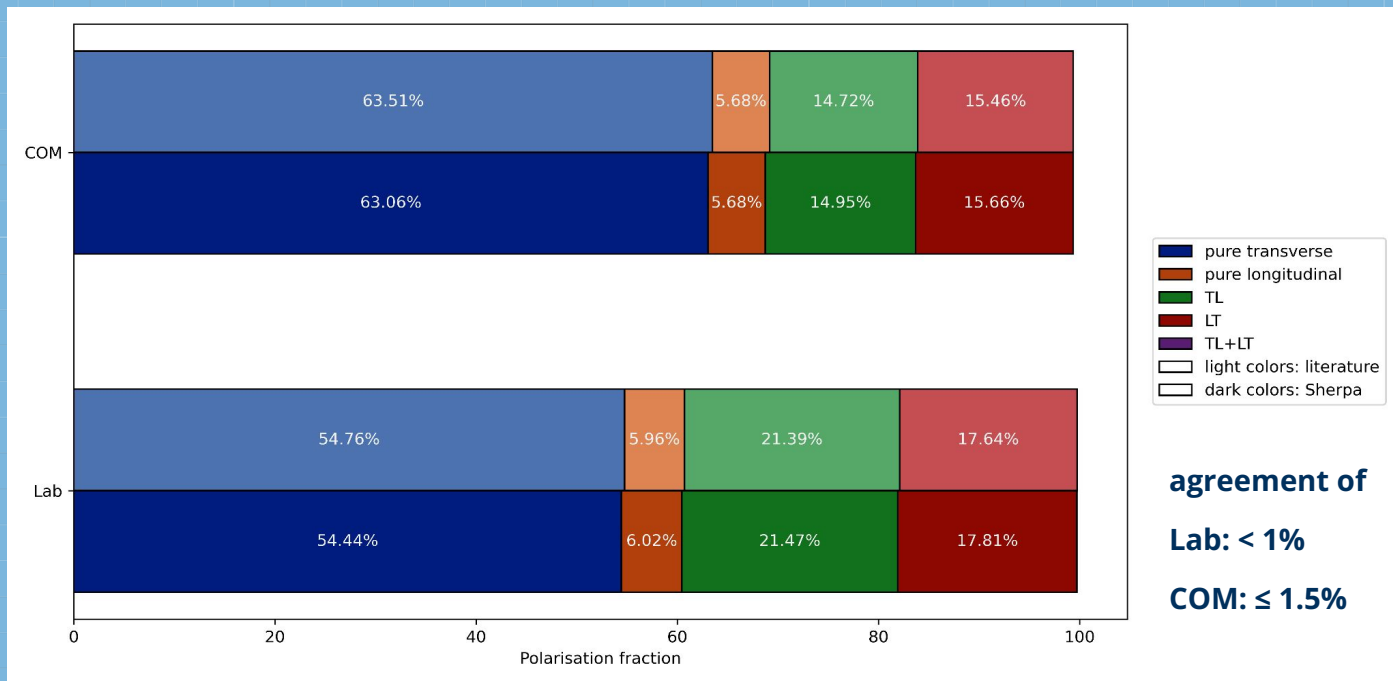
- construction from complete real emission amplitude



# nLO+PS vs. full fixed NLO - WZ-Diboson production



Comparison with NLO QCD fixed order calculation [[A. Denner & G. Pelliccioli 2021](#)]

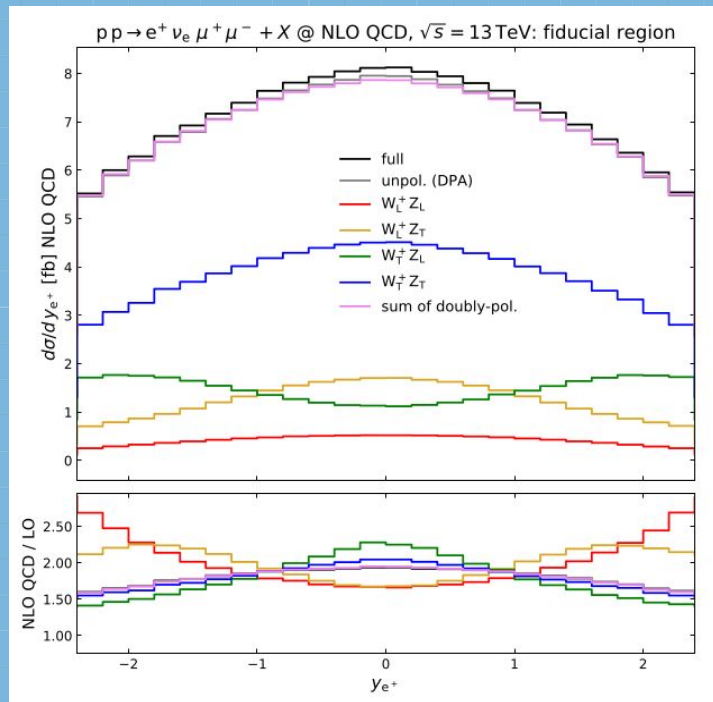


# *WZ* Diboson production - Rapidity of the *W*-lepton

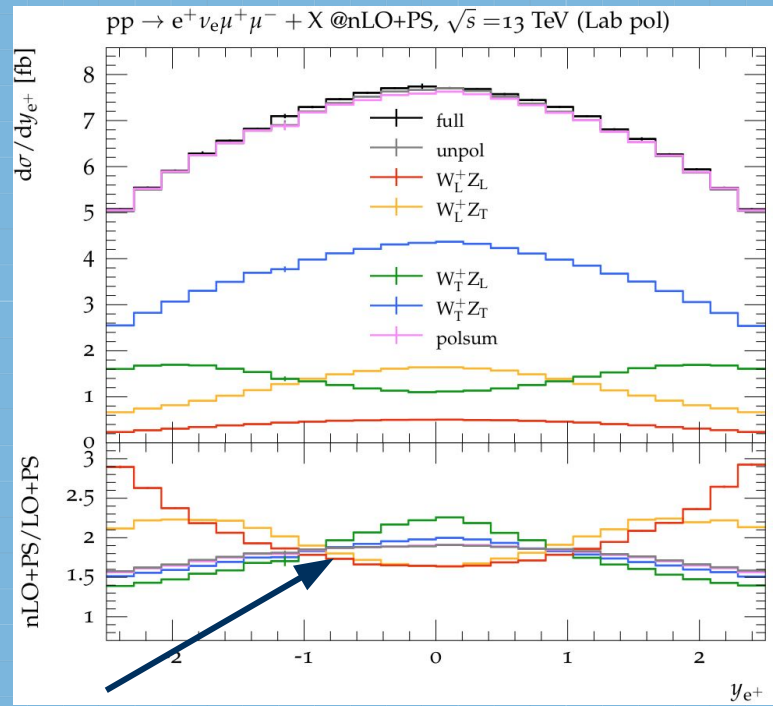
(Lab)

NLO QCD calculation fixed order

[A. Denner & G. Pelliccioli 2021]



Sherpa nLO+PS



Reproduces even non-trivial NLO effects!

# nLO+PS (Sherpa) vs. full NLO+PS (POWHEG+PYTHIA)

Literature: [\[G. Pelliccioli, G. Zanderighi 2023\]](#)

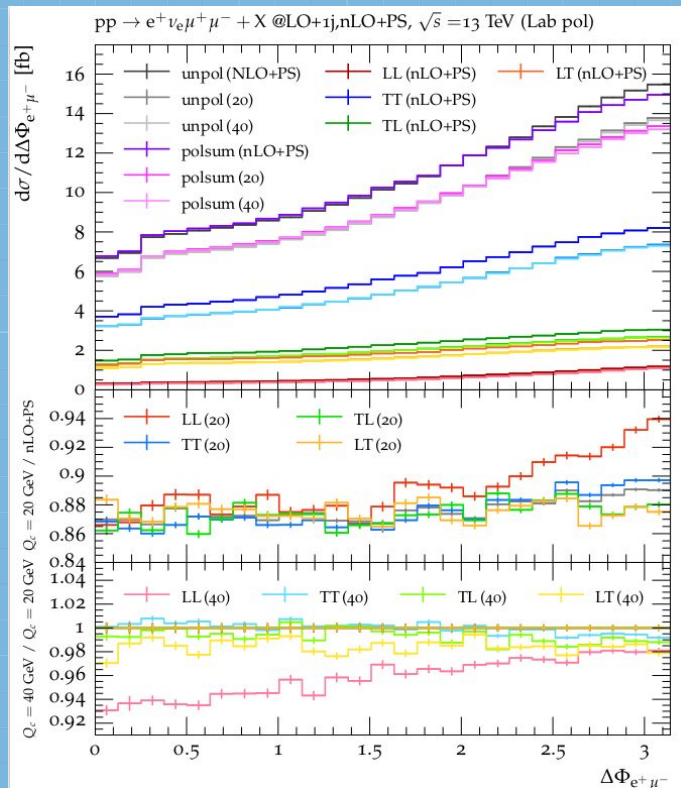
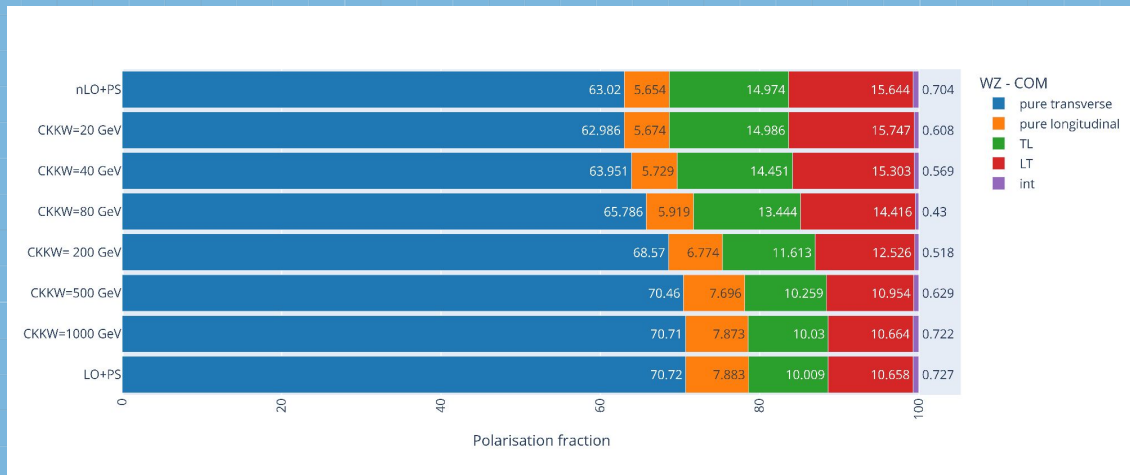
WZ production [\[G. Pelliccioli, G. Zanderighi 2023\]](#): similar agreement compared to NLO QCD+PS

## ZZ-Production

	$\sigma_{\text{NLO+PS}}$ [fb]	Fraction [%]	$\sigma_{\text{nLO+PS}}$ [fb]	Fraction [%]	$\frac{\text{nLOPS}}{\text{NLOPS}} - 1$ [%]	
					XS	Frac
<i>unpol</i>	14.02(1)	100	14.017(17)	100	-0.0	
<i>LL</i>	0.819(1)	5.84	0.8404(12)	5.996(11)	+2.6	+2.7
<i>LT + TL</i>	3.565(3)	25.43	3.6177(39)	25.81(4)	+1.5	+1.5
<i>TT</i>	9.47(1)	67.52	9.370(14)	66.85(13)	-1.1	-1.0
<i>int</i>	0.171	1.28	0.1886(24)	1.345(17)	+10.3	+5.1

# Multi-leg merging

## WZ-Diboson production

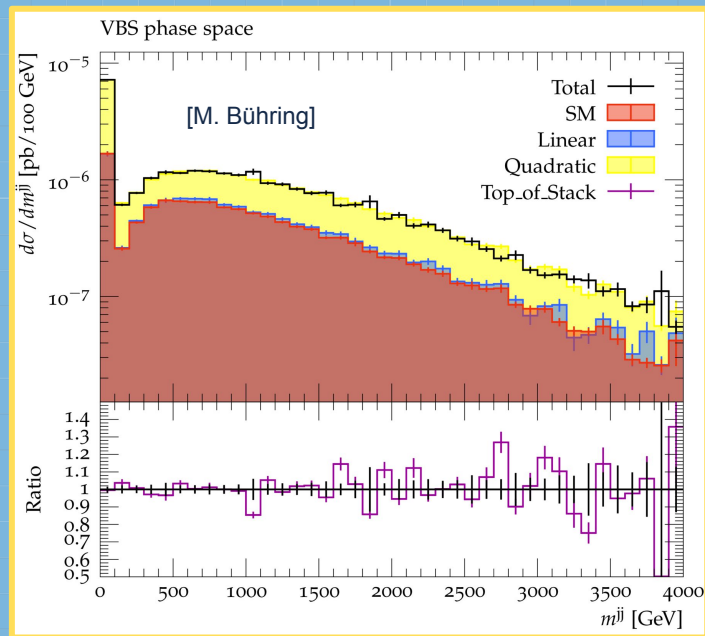


- based on CKKW merging
- LO & N(n)LO QCD accuracy
- small merging scale crucial
- no limitation in combination with polarization framework

# UB polarization beyond the Standard Model

- **UFO format:** standardized format for BSM models for simple import in event generators
- **SHERPA UFO interface:** [\[S. Höche et al. 2014\]](#)
  - Lorentz & color structures built automatically
  - automatic decay tables / chains
  - handling of intermediate resonances
  - spin correlations
  - effective field theories
  - form factors
- **combination with polarization framework via intermediate resonances suite**

W+W+jj SMEFT dim-6

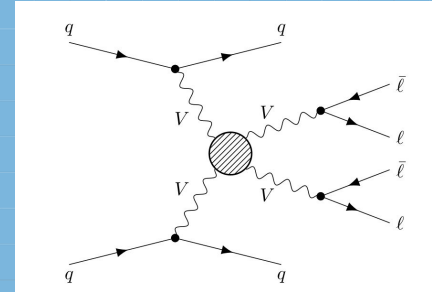
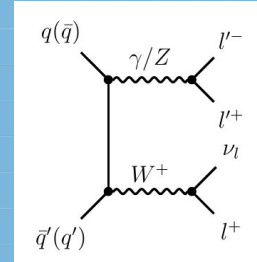


# *Polarization framework in real life*



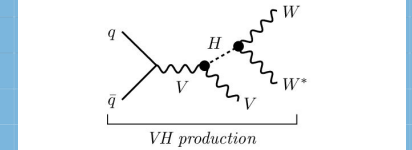
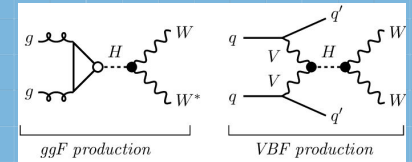
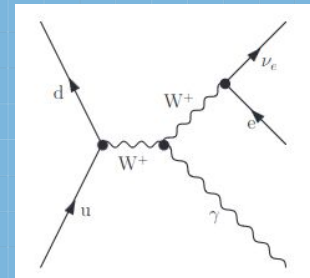
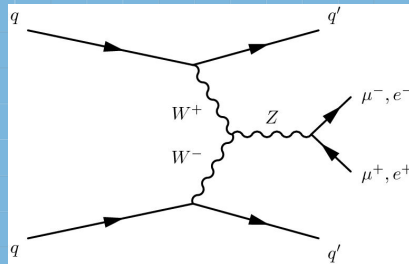
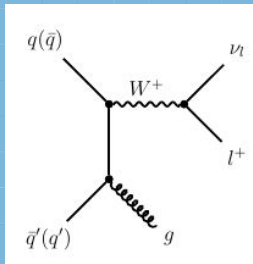
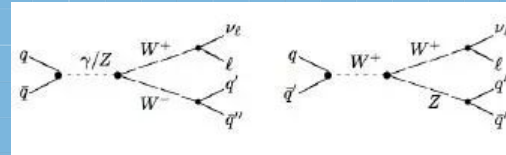
# Available processes & current limitations

- all processes with intermediate vector bosons that are possible with SHERPA's tree-level matrix element generators
- up to nLO QCD in production process
- leptonic- as well as hadronic decays
- extension to spin- $\frac{1}{2}$  particles easily possible

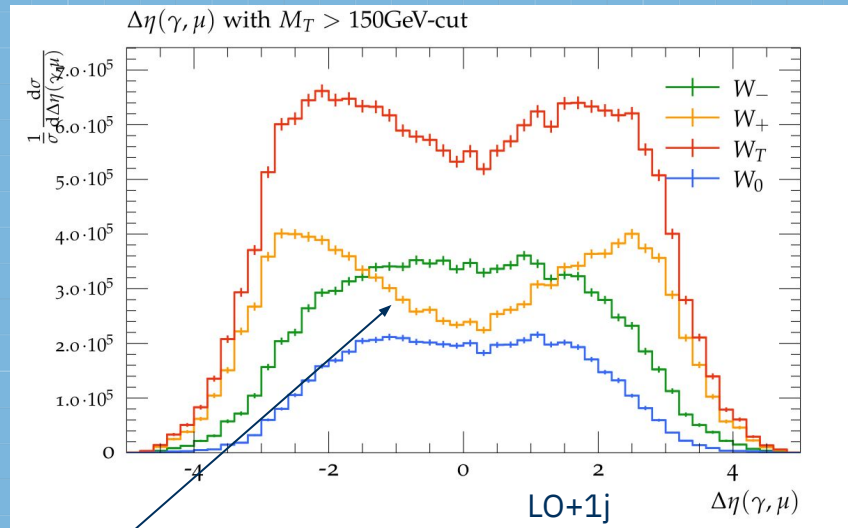
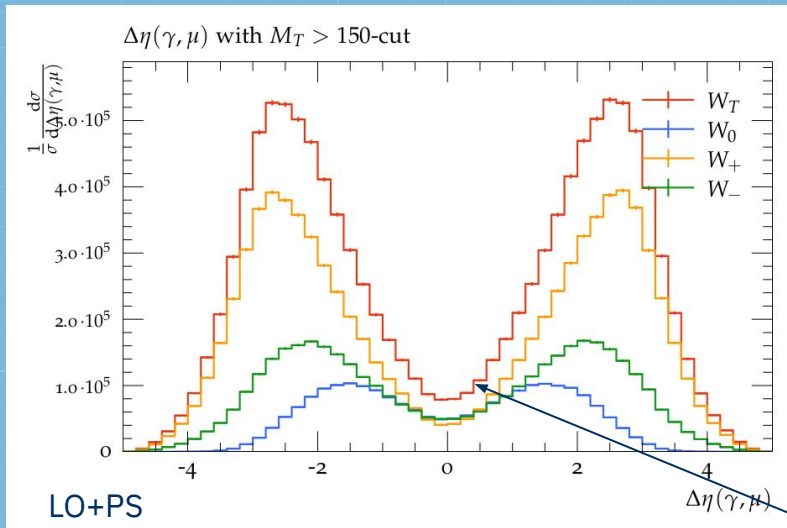


## Limitations

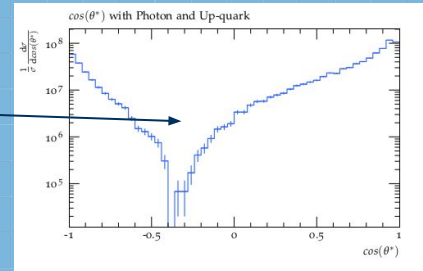
- no loop-induced processes
- no higher order effects on decays



# Polarized $W\gamma$ production



sums up to dip in unpolarized result due to radiation amplitude zero effect in  $\cos\Theta$  with  $\Theta = \angle$  between  $\gamma$  &  $u$  in  $W\gamma$  rest frame



Huge impact from higher order QCD corrections!

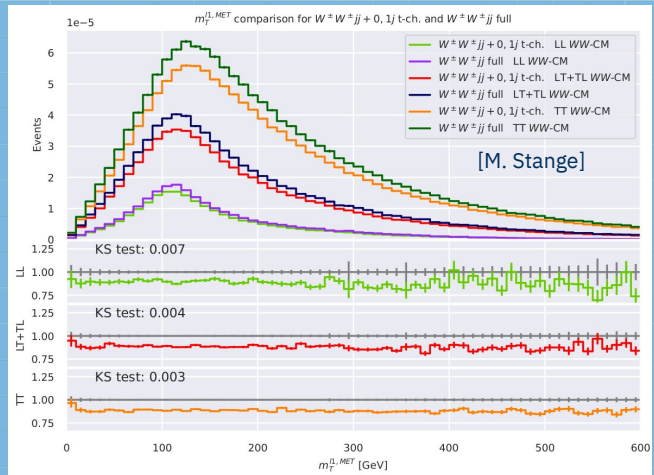
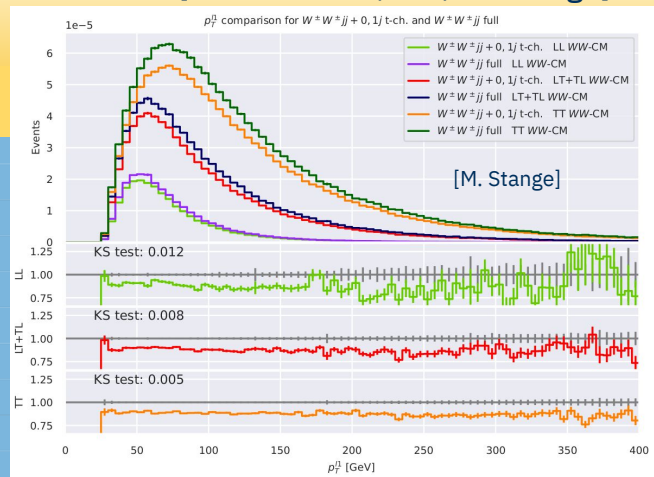
	LO+PS	LO+1j
$f_0$	0.1556	0.2196
$f_+$	0.4277	0.3454
$f_-$	0.4166	0.4349

# First higher order QCD predictions for VBS $W^+W^+jj$ matched to PS

[E. Bachmann, MH, M. Stange]

	$\mathcal{L}O+PS$	$\mathcal{L}O+1j$ VBS approx
unpol [fb]	2.459	2.302
LL [fb]	0.237	0.224
Fraction [%]	9.63	9.73
LT+TL [fb]	0.765	0.716
Fraction [%]	31.12	31.10
TT [fb]	1.497	1.399
Fraction [%]	60.88	60.77

... and differential polarization fractions!



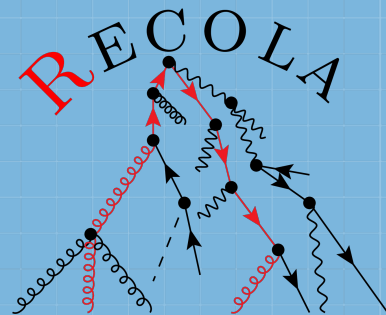
**Recently:**  
 First NLO QCD + NLO EW fixed order results available  
[\[A. Denner, C. Haitz, G. Pelliccioli 2024\]](#)

Only sub-percent level effect on integrated...

# *Current projects*

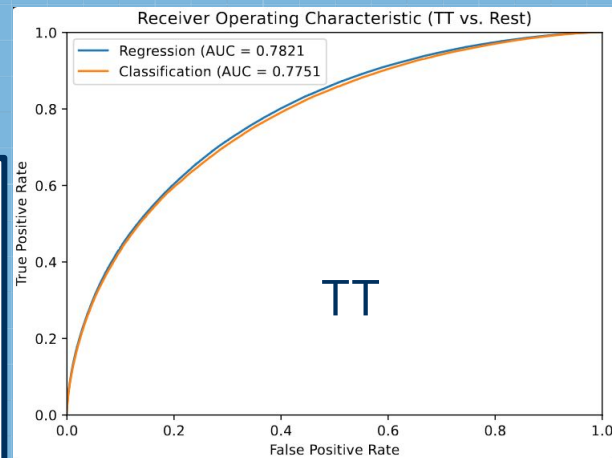
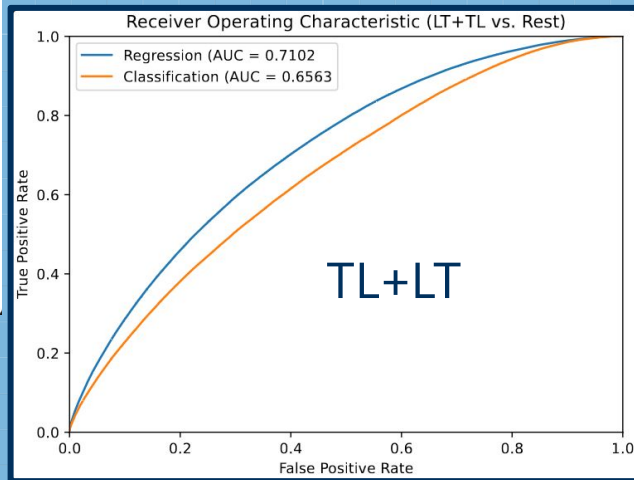
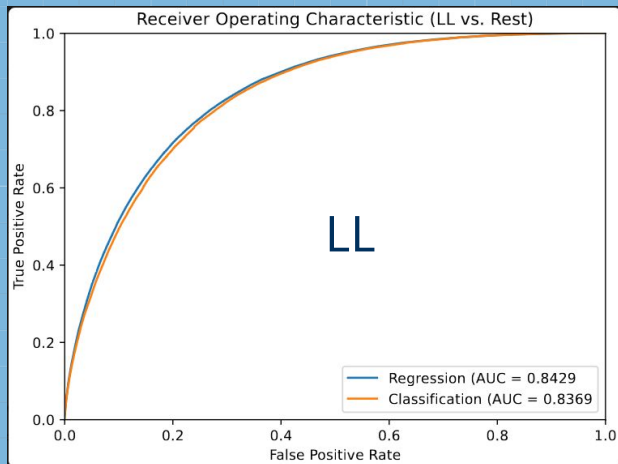
# Ongoing: Extension to complete NLO QCD / NLO EW

- **first step: Extension of SHERPA's Recola interface to get polarized loop-amplitudes**
  - transformation to SHERPA's spin basis to use it together with COMIX decay amplitudes
  - implemented spin trafo used
- **currently testing first implementation**
- **first application: loop-induced processes**



# Ongoing: Usage as polarization tagger

- first proof of concept study: recursion NN trained on polarization fractions in VBS  $W^+W^+jj$  @LO outperforms classification net [[J. A. Neumann CERN-THESIS-2023-346](#)]



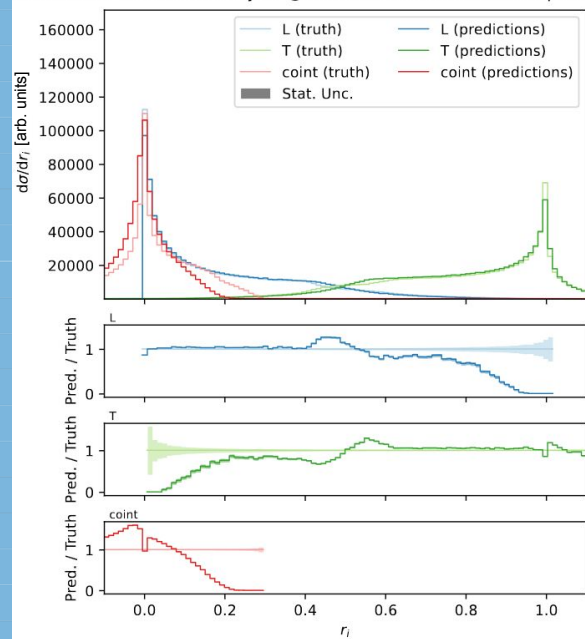


# Ongoing: Usage as polarization tagger

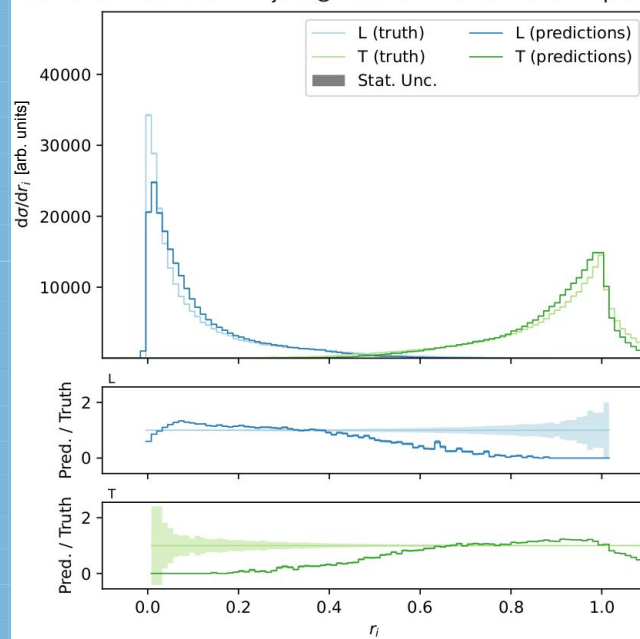
[E. Bachmann, MH]

- now: working on proper polarization tagger trained on polarization weights:
  - starting with Z+jets example like in [M. Grossi et al. 2023] & multi-layer perceptrons in LAB

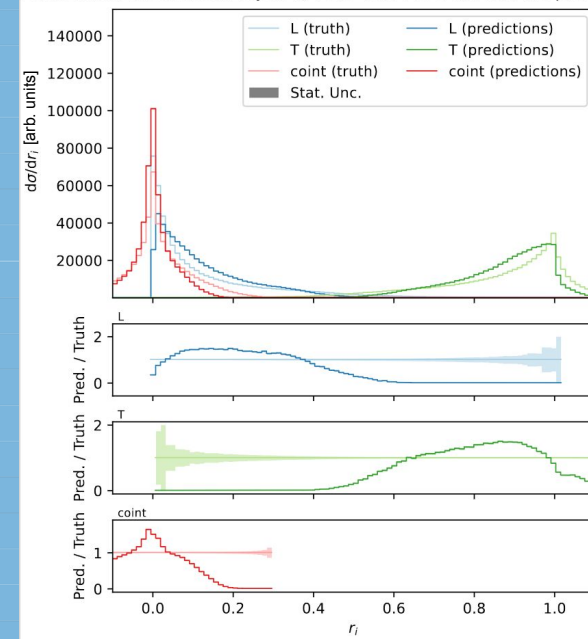
Polarization fractions in Z+jets @ 13.6 TeV: MC truth and NN pred.



Polarization fractions in Z+jets @ 13.6 TeV: MC truth and NN pred.



Polarization fractions in Z+jets @ 13.6 TeV: MC truth and NN pred.



## 1. fixed order LO

agreement true vs. NN:



## 2. LO+PS restricted on events with 1 jet



## 3. LO+PS all jets

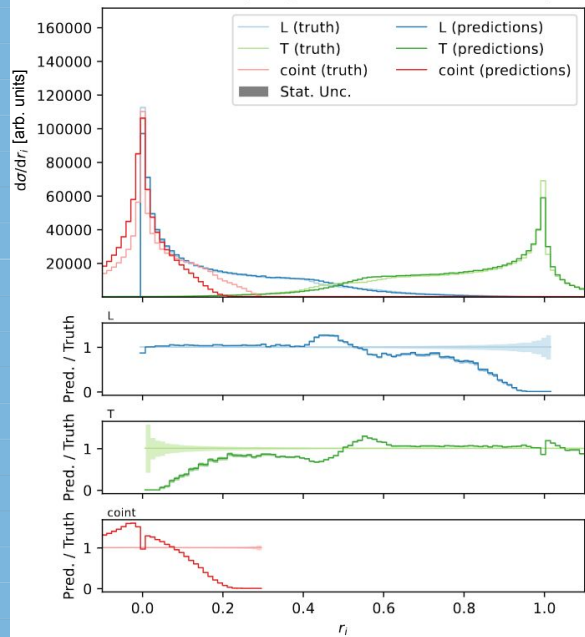


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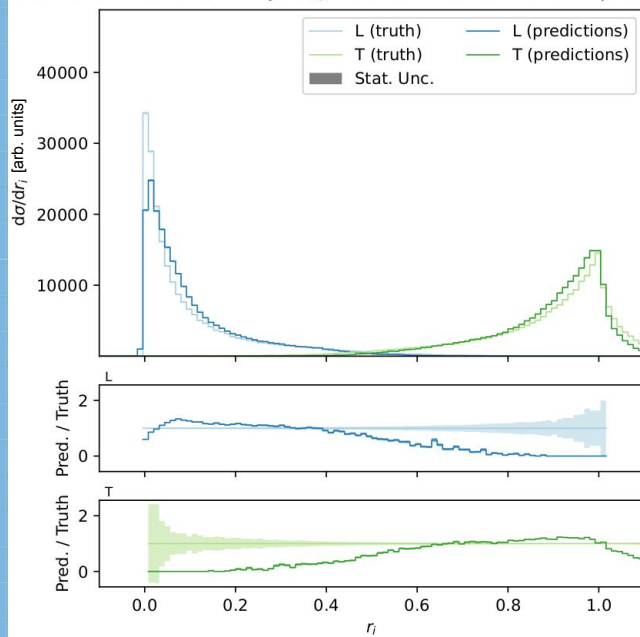
**Next step:**  
Trying different network architecture (GNNs) in order to include all jets as training inputs

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  - starting with Z+jets example like in [M. Grossi et al. 2023] & multi-layer perceptron

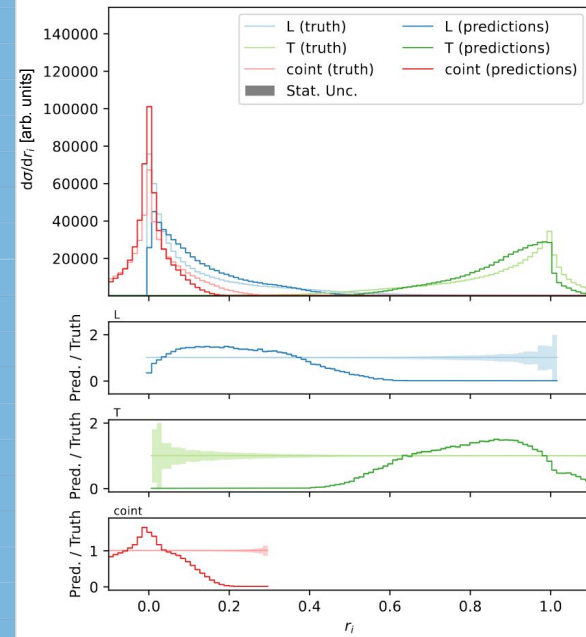
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# Summary and Outlook



- ✓ **Overview over SHERPA's polarization framework**
  - publicly available since SHERPA 3.0.0beta
- ✓ **Key features:**
  - all polarized cross sections in one simulation run
  - direct calculation of interference between different polarizations
  - provide several reference frames
  - accuracy up to nLO+PS, multi-leg merging
  - no process limitation ( for intermediate VBs ) beside loop-induced processes
  - usable for SM and BSM physics

## What comes next ...

- ❑ Extension to loop-induced processes
- ❑ Extension to NLO QCD and approximate NLO EW
- ❑ Application for polarization tagging
- ❑ Applications in phenomenological studies: NLO effects to VBS processes, BSM studies, hadronic decays

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*Thank you for  
your attention!*

# *Backup*

# Spin-Correlation Algorithm

[P. Richardson 2001]

- here only for VB decaying into stable leptons

hard process final state particles & production (2→n) matrix element tensor  $|\mathcal{M}^{\mathcal{P}}|_{\lambda_1 \dots \lambda_n \lambda'_1 \dots \lambda'_n}^2$

choose one outgoing particle A  
randomly

$$\text{Spin density matrix } \rho_{\lambda_j \lambda'_j}(A) = \frac{1}{N_\rho} \mathcal{M}^{\mathcal{P}}_{\kappa_1 \kappa_2; \lambda_1 \dots \lambda_j \dots \lambda_n} \mathcal{M}^{\mathcal{P}*}_{\kappa_1 \kappa_2; \lambda'_1 \dots \lambda'_j \dots \lambda'_n} \prod_{i \neq j} \mathcal{D}_{\lambda_i \lambda'_i}^i$$

with  $\mathcal{D}_{\lambda_i \lambda'_i}^i = \frac{1}{n_{hel}} \delta_{\lambda_i \lambda'_i}$  if particle not chosen yet

choose decay channel of A according to branching  
ratios

Generate momenta of A's decay products according to  $\rho_{\lambda_A \lambda'_A} \mathcal{M}^{\mathcal{D}}_{\lambda_A; \lambda_1 \dots \lambda_n} \mathcal{M}^{\mathcal{D}*}_{\lambda'_A; \lambda_1 \dots \lambda_n}$

all decay products stable

Calculate A's decay matrix  $\mathcal{D}_{\lambda_A \lambda'_A} = \frac{1}{\mathcal{N}_{\mathcal{D}}} \mathcal{M}^{\mathcal{D}}_{\lambda_A; \lambda_1 \dots \lambda_n} \mathcal{M}^{\mathcal{D}*}_{\lambda'_A; \lambda_1 \dots \lambda_n}$



# Mass Smearing Algorithm

- **spin correlation algorithm runs on on-shell momenta**
  - **mass smearing performed afterwards**
- 1. Generate off-shell masses for VBs**
    - a. determine max. available mass = invariant mass of total mom of VB production FS
    - b. starting with VB with smallest decay width
    - c. dice mass according to Breit-Wigner distribution from [0, totmass]
  - 2. Boost final state momenta of production process accordingly**
  - 3. Boost final state momenta of decay particles accordingly**

Guiding principles for 2.+3.

- **redistribute  $E$ ,  $|p|$  of the particles while preserving direction of flight in CMS of the FS particles**

# Basic Usage - ZZ production example

```
BEAMS: 2212
BEAM_ENERGIES: 6500

WIDTH_SCHEME: Fixed

COMIX_DEFAULT_GAUGE: 0

PARTICLE_DATA:
  24: {Width: 0}
  23: {Width: 0}
```

Real masses, couplings  
→ no complex mass scheme

VB decay process

Polarised cross sections  
with ZZ COM reference  
frame enabled

VB production  
process @nLO + PS

Spinor gauge such that  
polarization vectors have  
the typical form

VB width zero to fulfill  
SU(2) Ward identities

VB production process  
multi-leg merging (LO+1j)

```
HARD_DECAYS:
  Enabled: true
  Channels:
    23,11,-11: {Status: 2}
    23,13,-13: {Status: 2}
  Pol_Cross_Section:
    Enabled: true
    Reference_System: COM

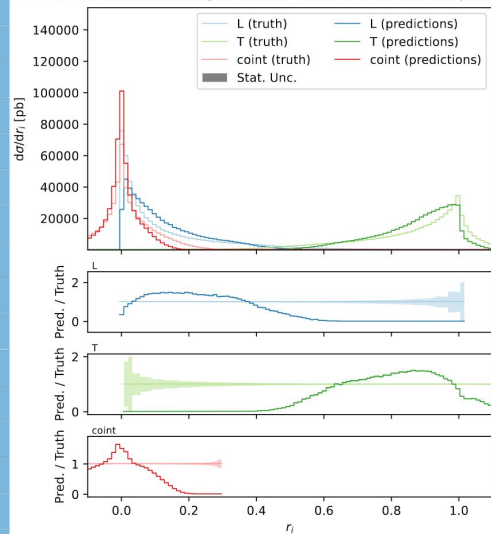
# production process: (jj -> ZZ)
PROCESSES:
- 93 93 -> 23 23:
  Order: {QCD: 0, EW: 2}
  NLO_Mode: MC@NLO
  NLO_Order: {QCD: 1, EW: 0}
  ME_Generator: Amegic
  RS_ME_Generator: Comix
  Loop_Generator: OpenLoops

ANALYSIS: Rivet
RIVET:
  --analyses:
    - COMETA_ZZ_production_analysis|
```

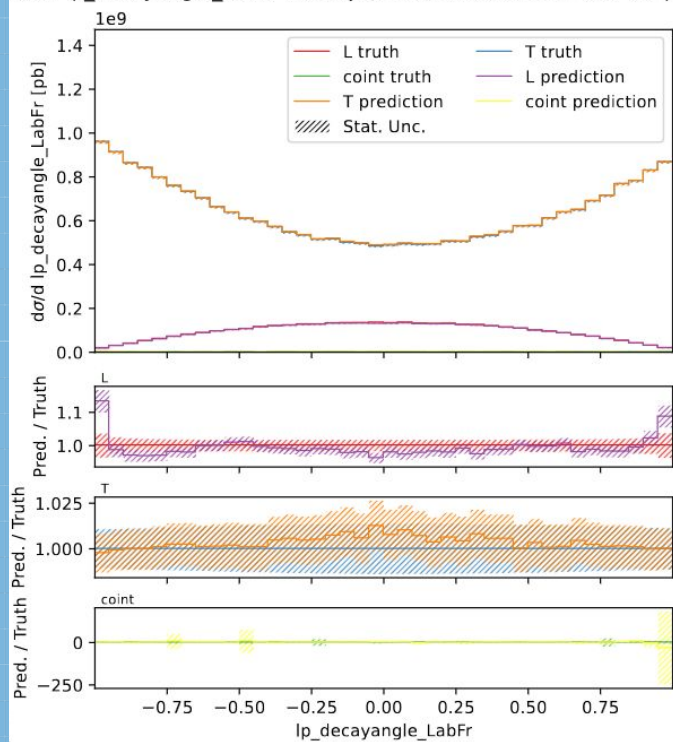
```
# production process: (jj -> ZZ)
PROCESSES:
- 93 93 -> 23 23 93{1}:
  Order: {QCD: 0, EW: 2}
  CKKW: 20
```

# Ongoing: Usage as polarization tagger

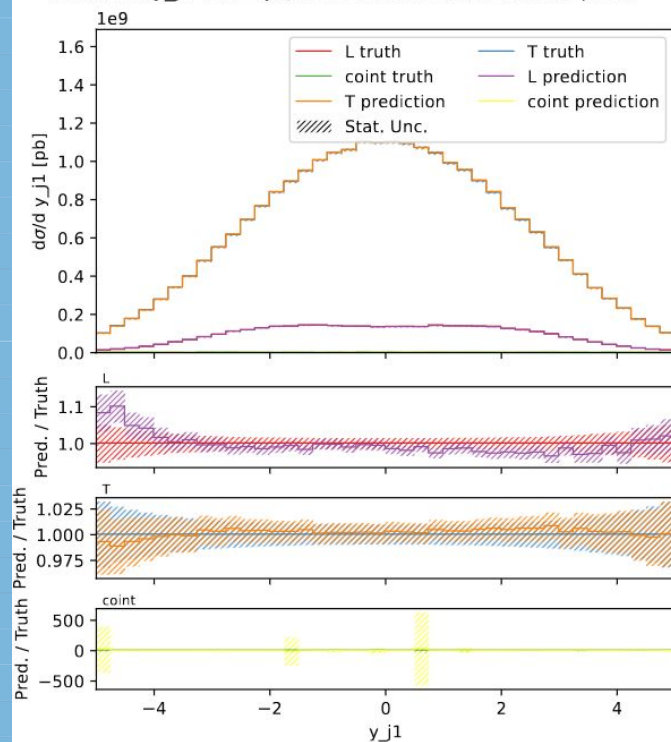
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Polarized  $l_p$  decayangle\_LabFr for Z+j @ 13.6 TeV: MC truth and NN pred.



Polarized  $y_{j1}$  for Z+j @ 13.6 TeV: MC truth and NN pred.



Z+jets @ LOPS,  
Laboratory frame