

PPC 2024

Breaking into the window of primordial black hole dark matter with x-ray microlensing

Based on arXiv: 2405.20365 (Submitted to Phys. Rev. Lett. [PRL])



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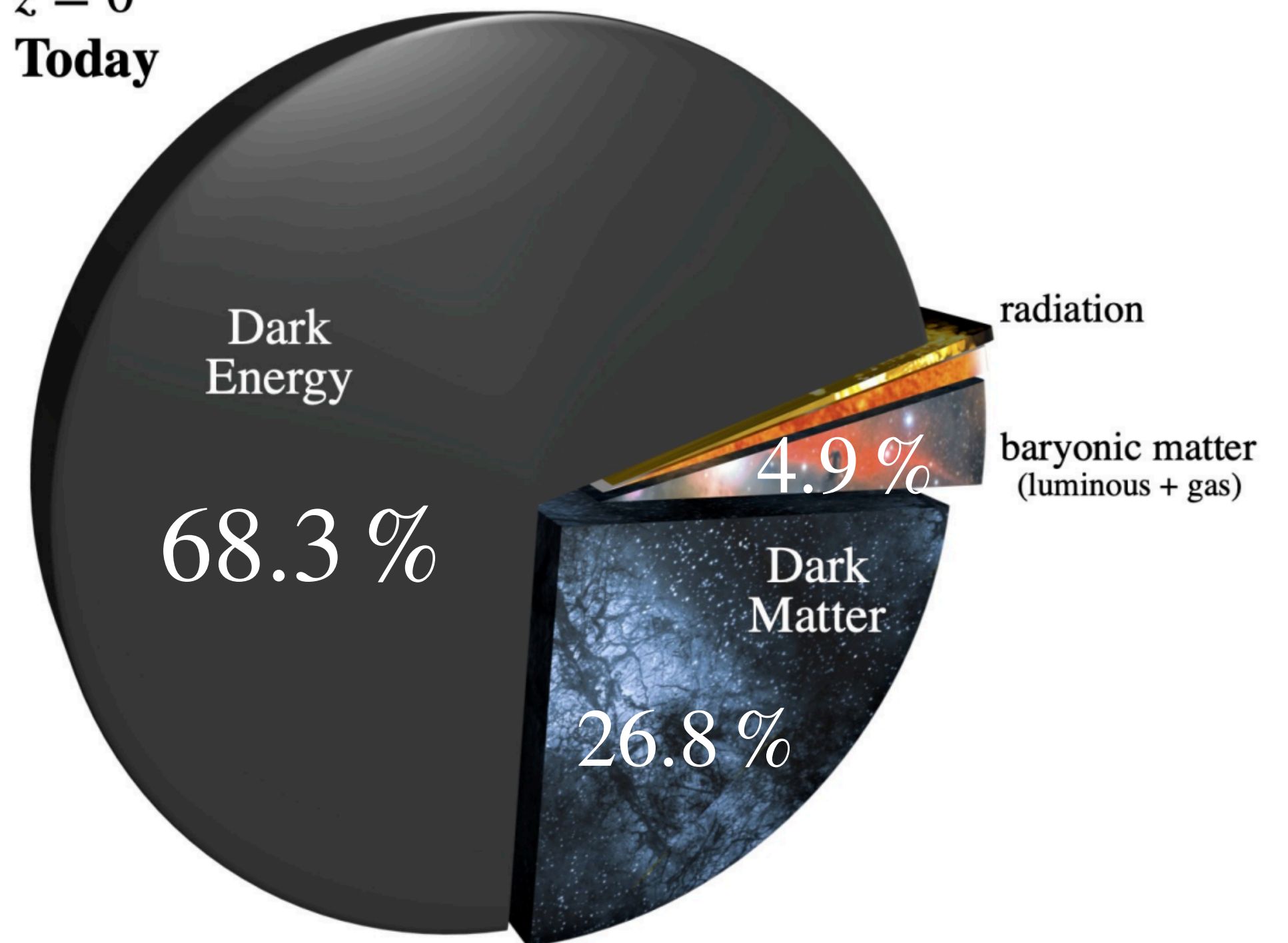
Ingredients of our universe

What our universe is made up of?

This is what CMB tells
about the universe we
live in



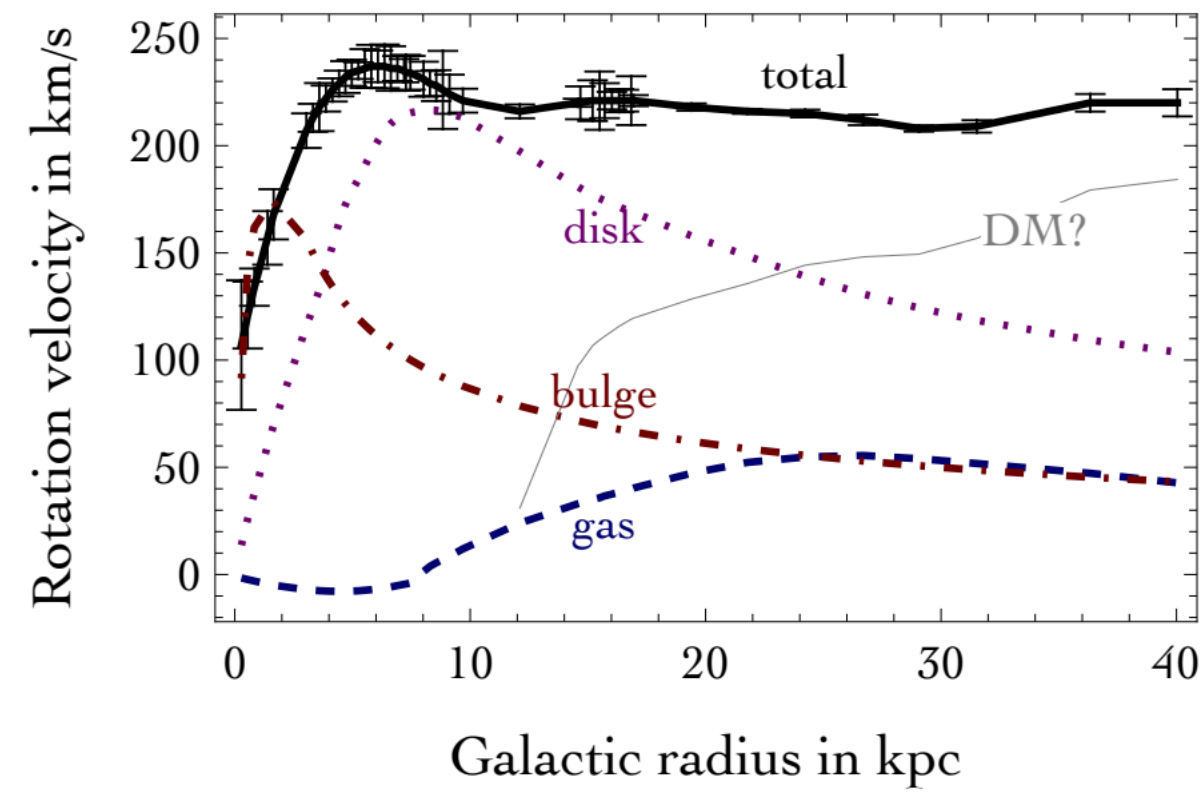
$z = 0$
Today



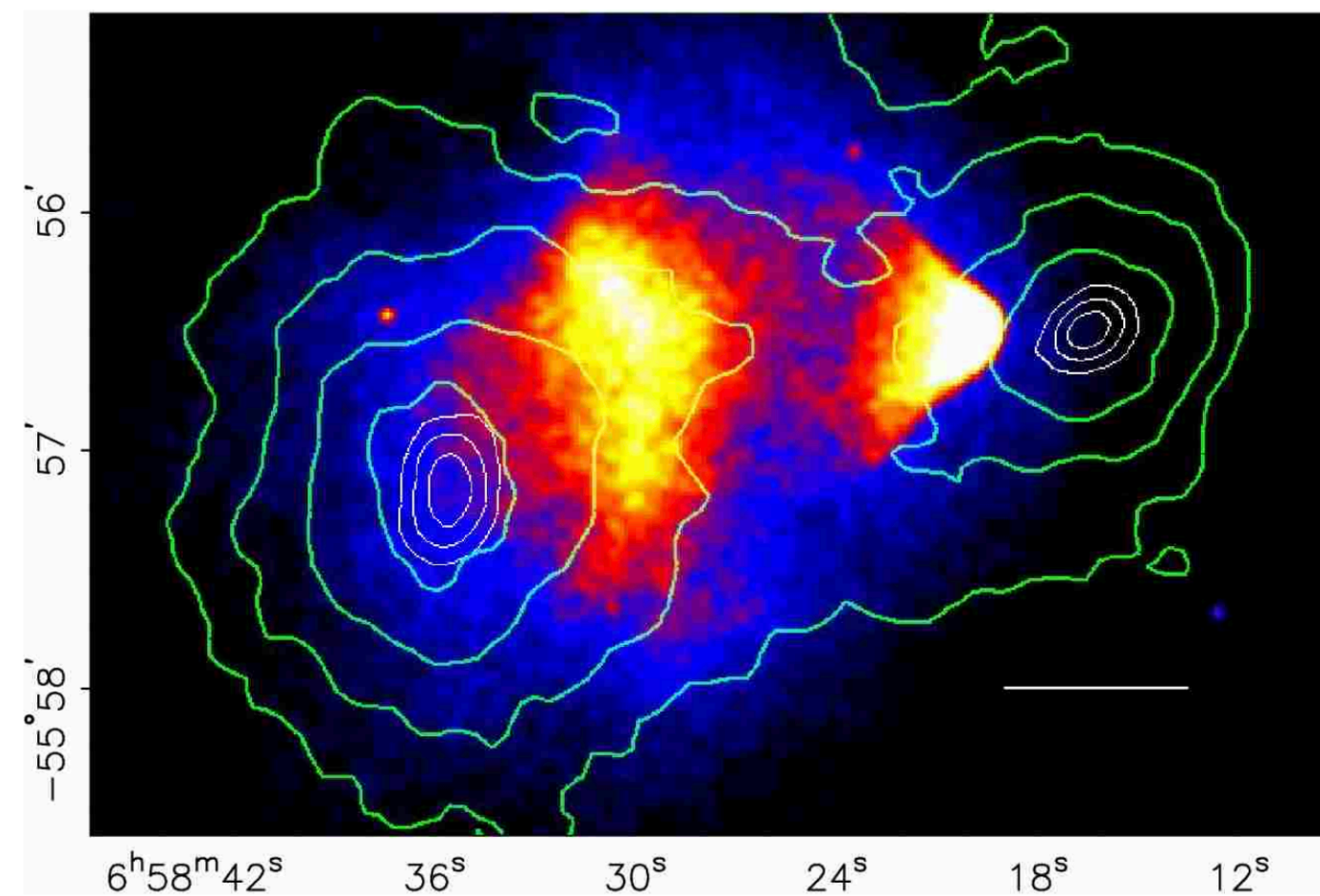
Cirelli et. al. [arXiv: 2406.01705]

Dark matter comprises ~85% of total matter in the universe!

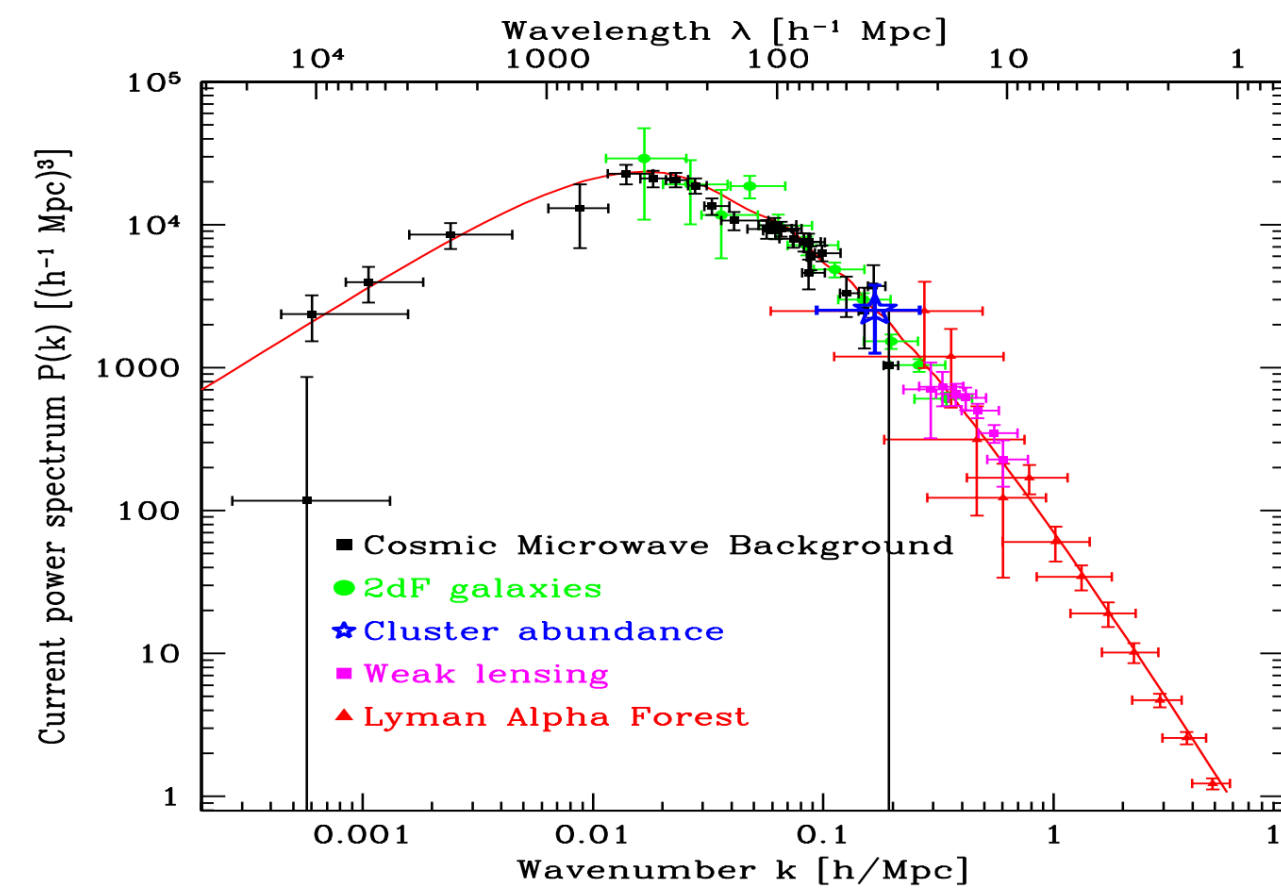
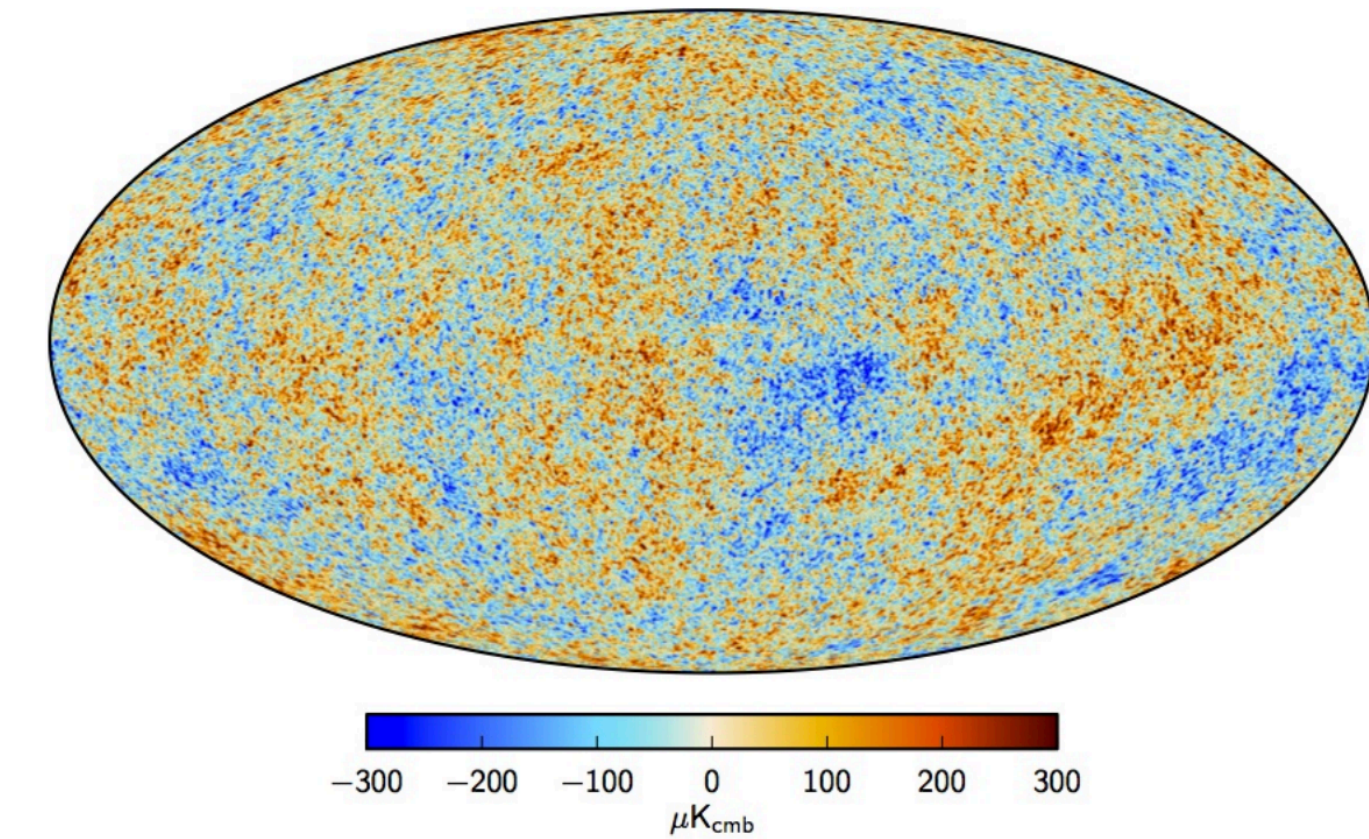
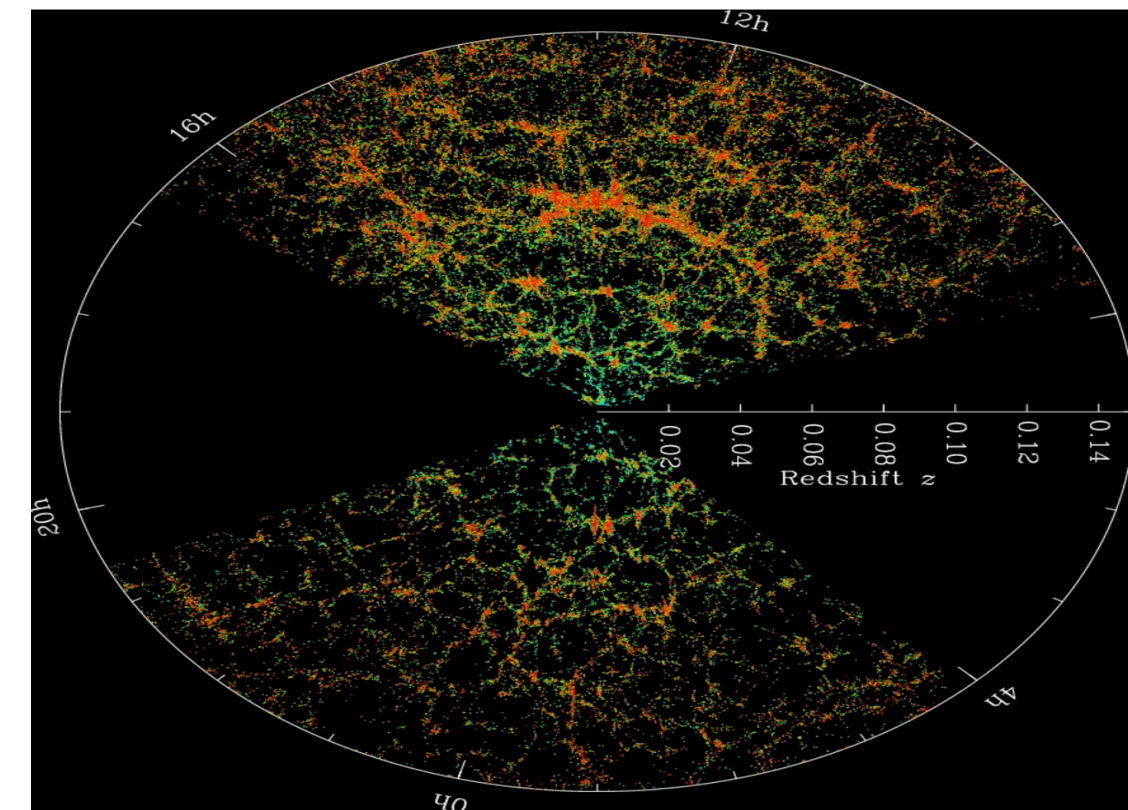
Evidences of dark matter in the universe



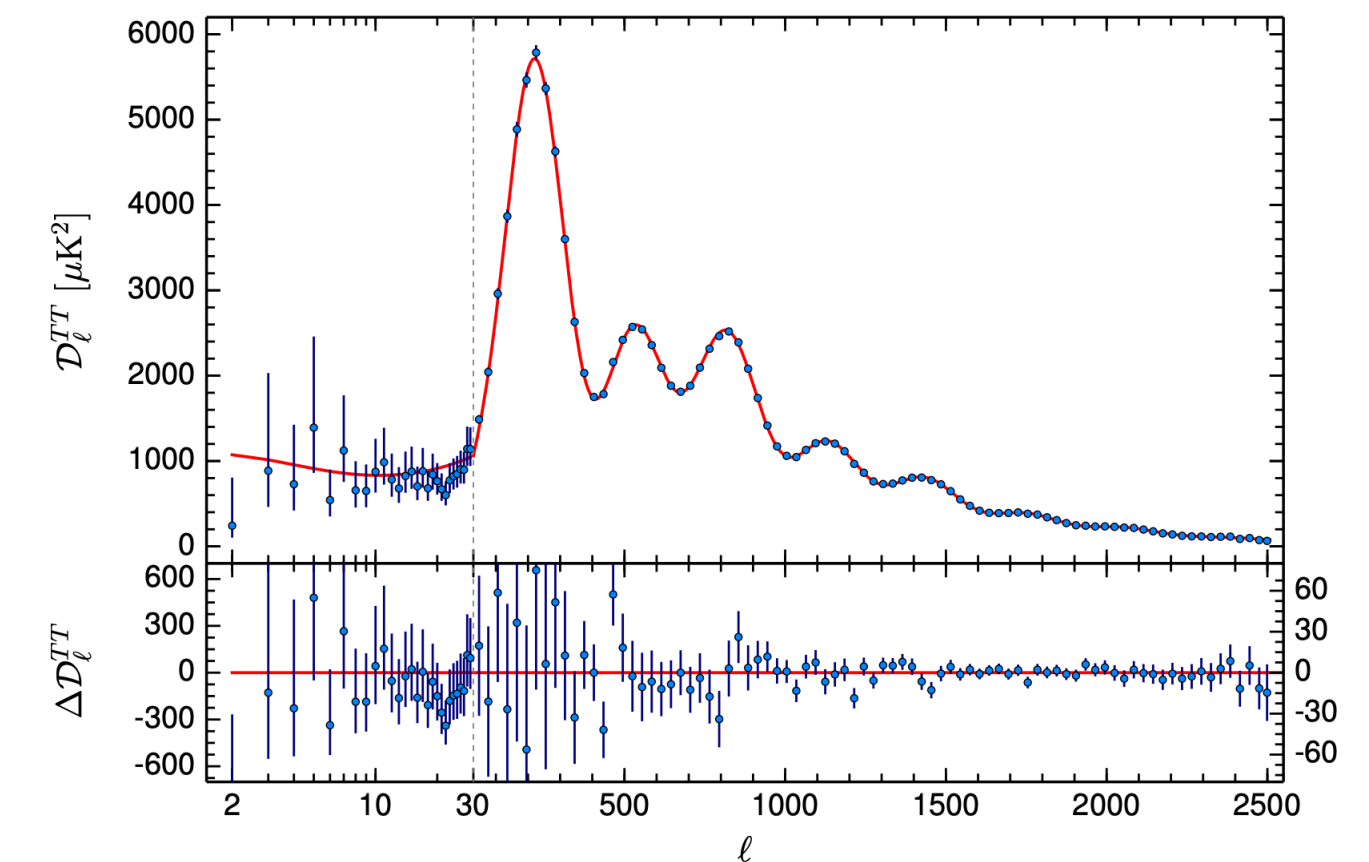
Smoking gun...Bullet cluster



Clowe et al., The Astrophysical Journal + 2006



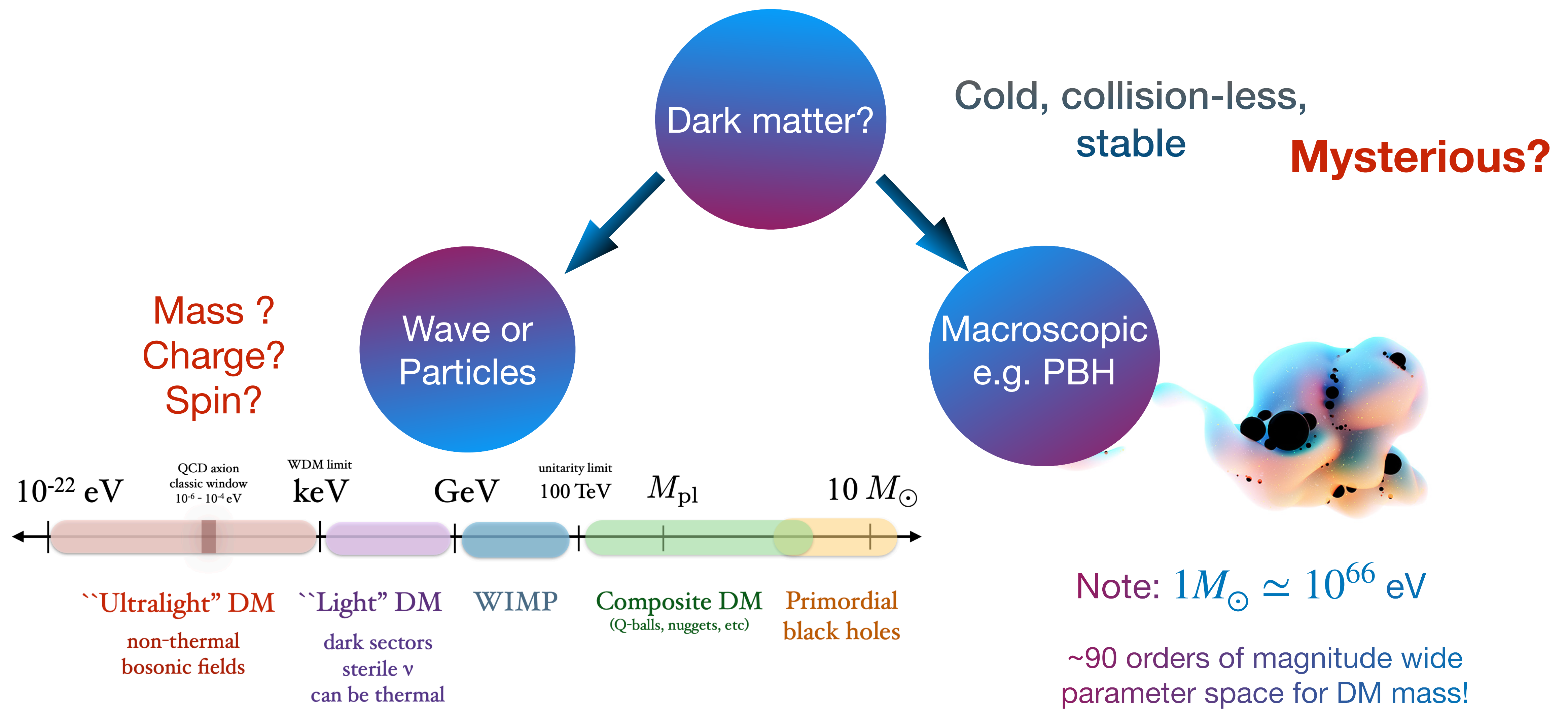
Cirelli et. al. [arXiv: 2406.01705]



Small scale

Large scale

What is Dark Matter after all?



[Image: Tongyan Lin + 2019]

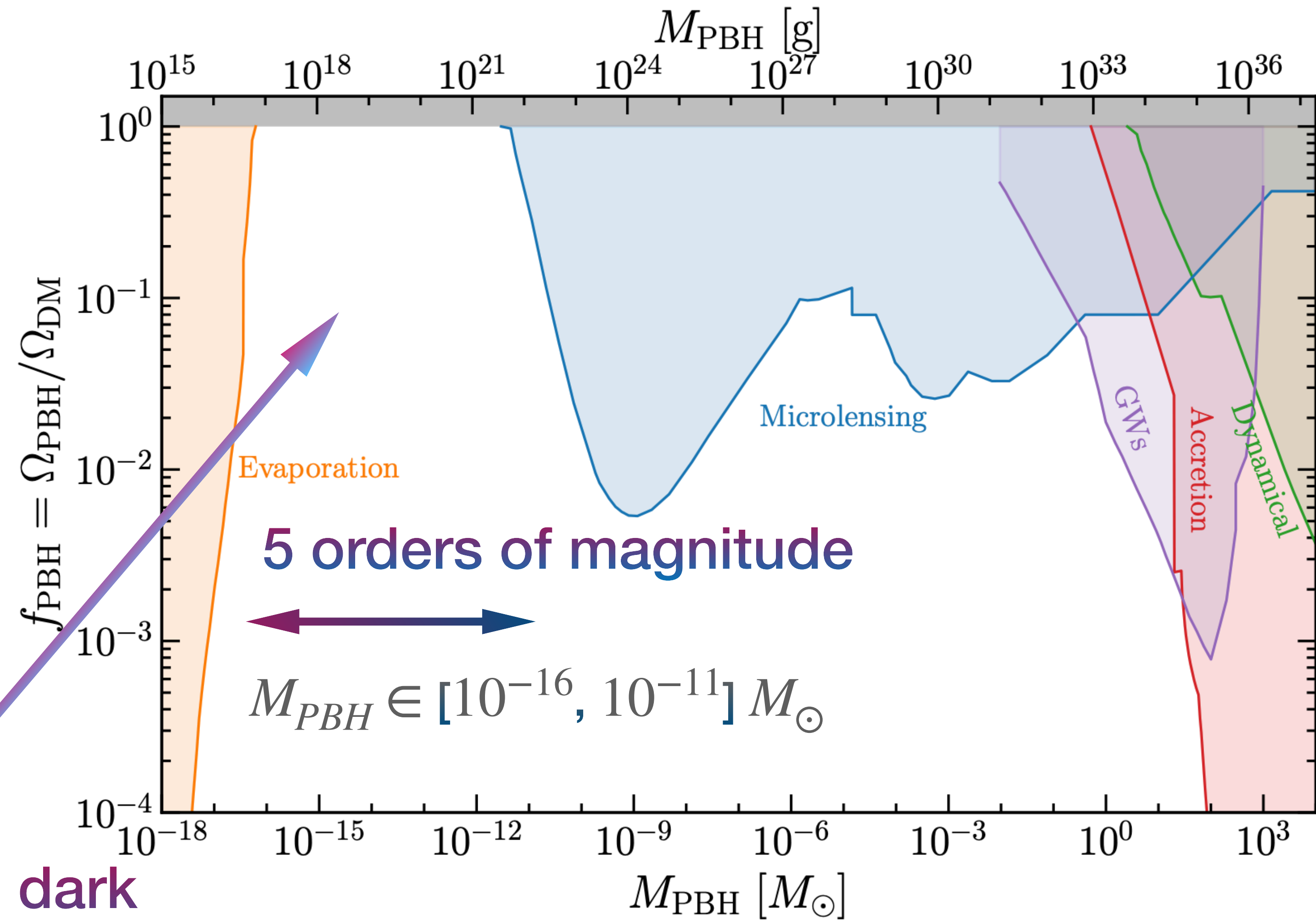
The primordial black hole dark matter window

PBHs may form due to density perturbations generated during the inflationary epoch!



1974

PBH as 100 % dark matter!?

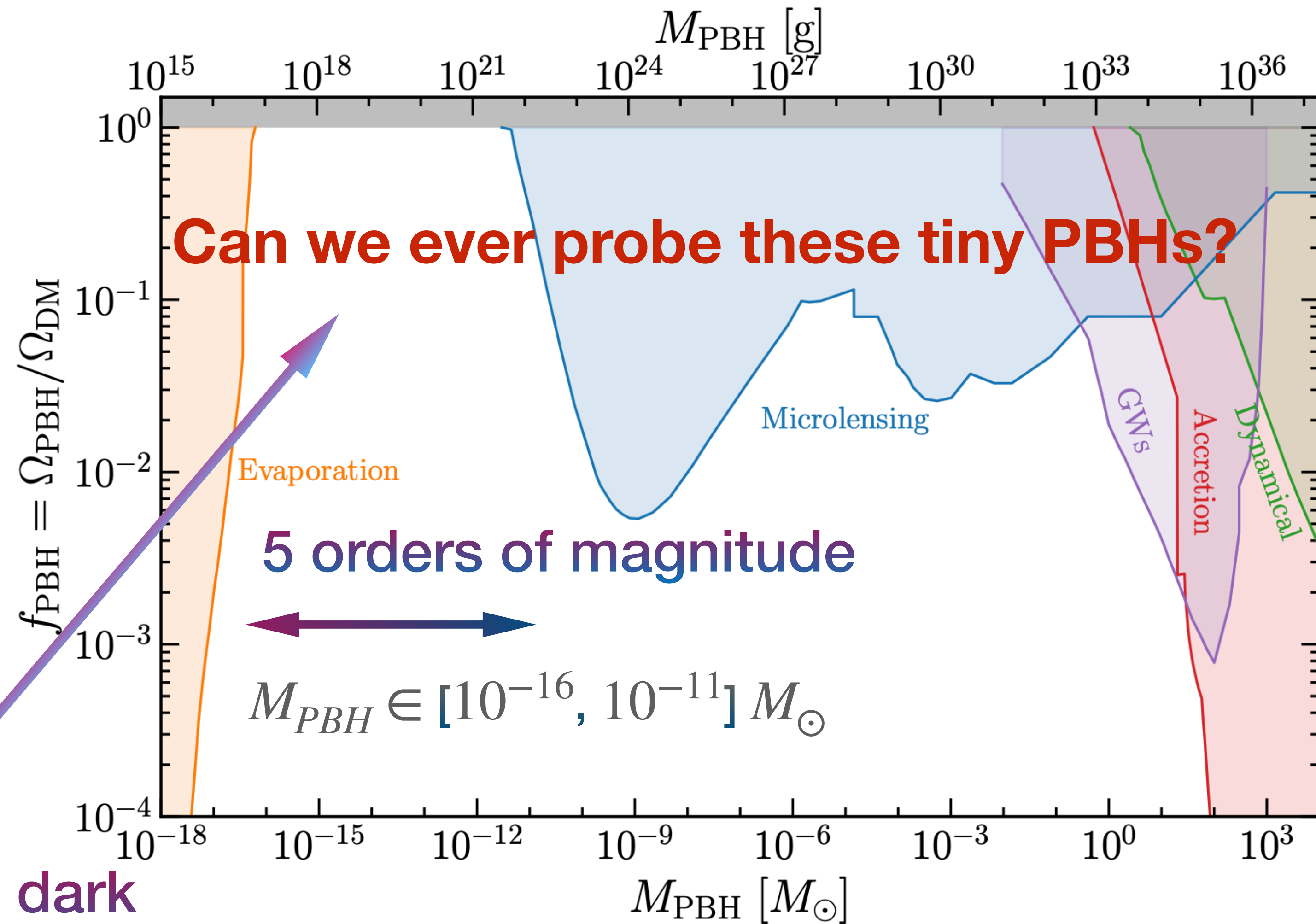


[Oncins + 2022, arXiv:2205.14722]

The primordial black hole dark matter window

PBHs may form due to density perturbations generated during the inflationary epoch!

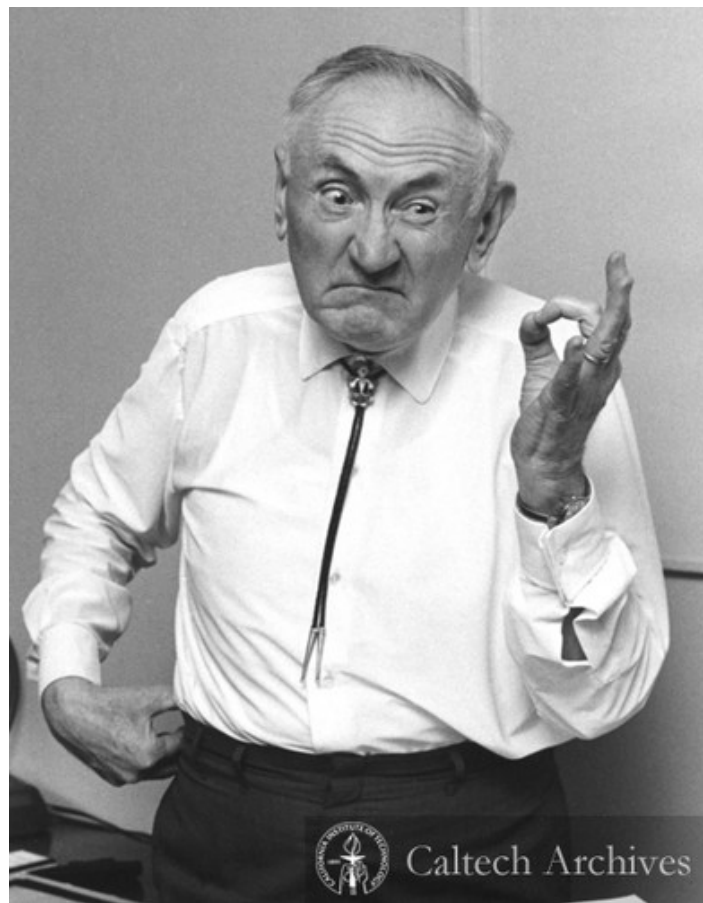
PBH as 100 % dark matter!?



[Oncins + 2022, arXiv:2205.14722]

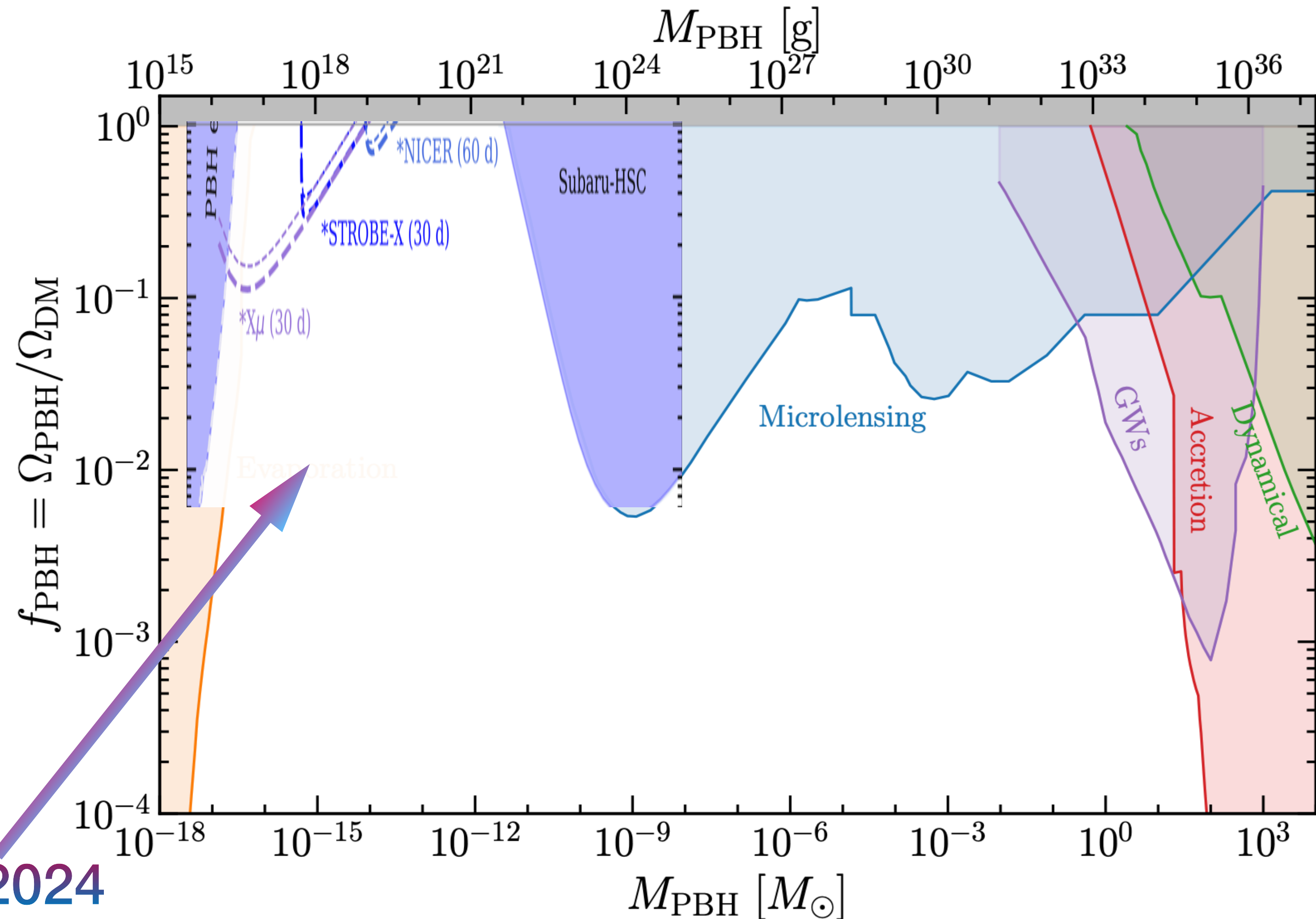
The primordial black hole dark matter window

Current and future x-ray telescopes can probe this window!

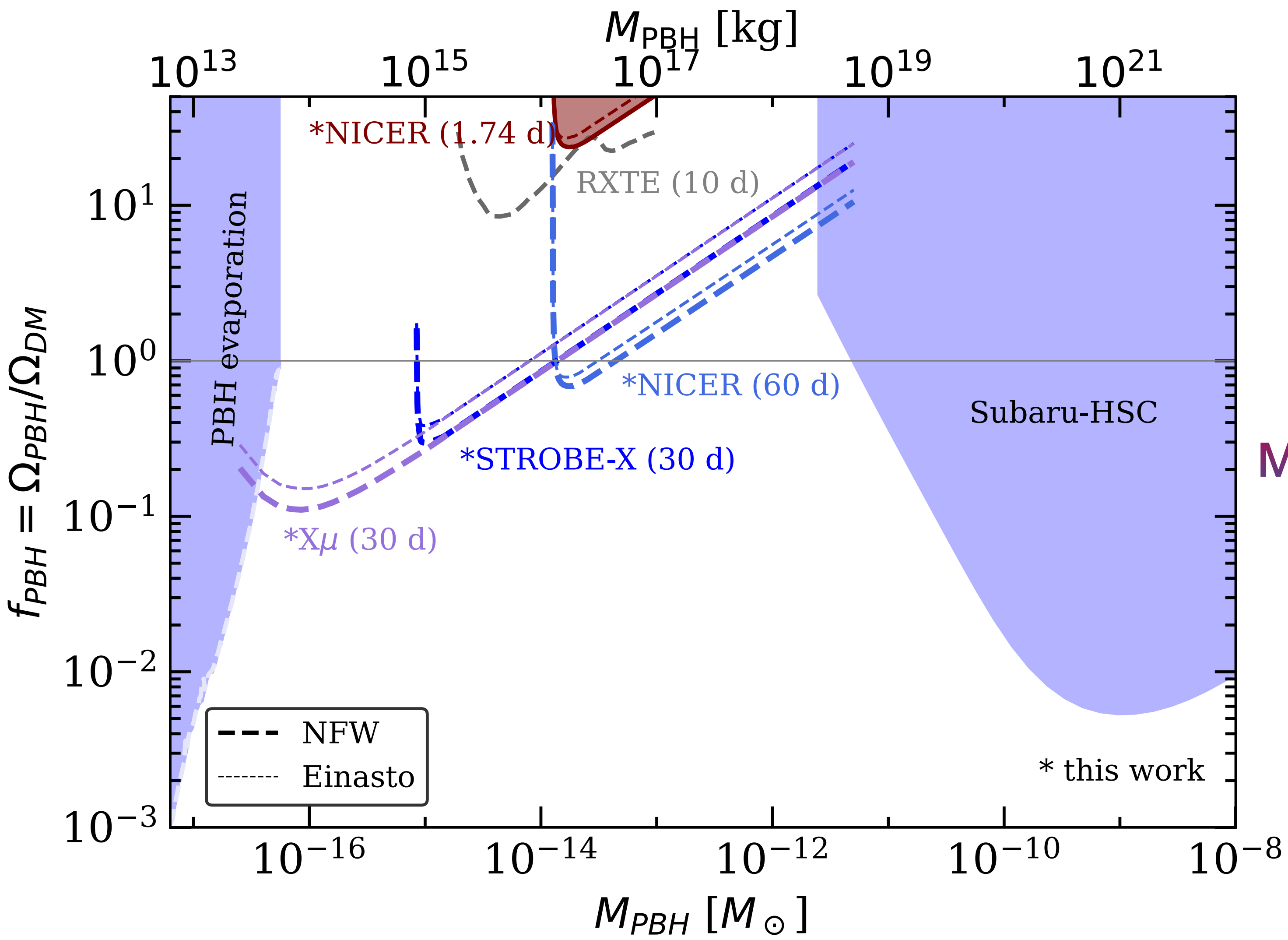


Manish Tamta et. al. + 2024

arXiv:2405.20365

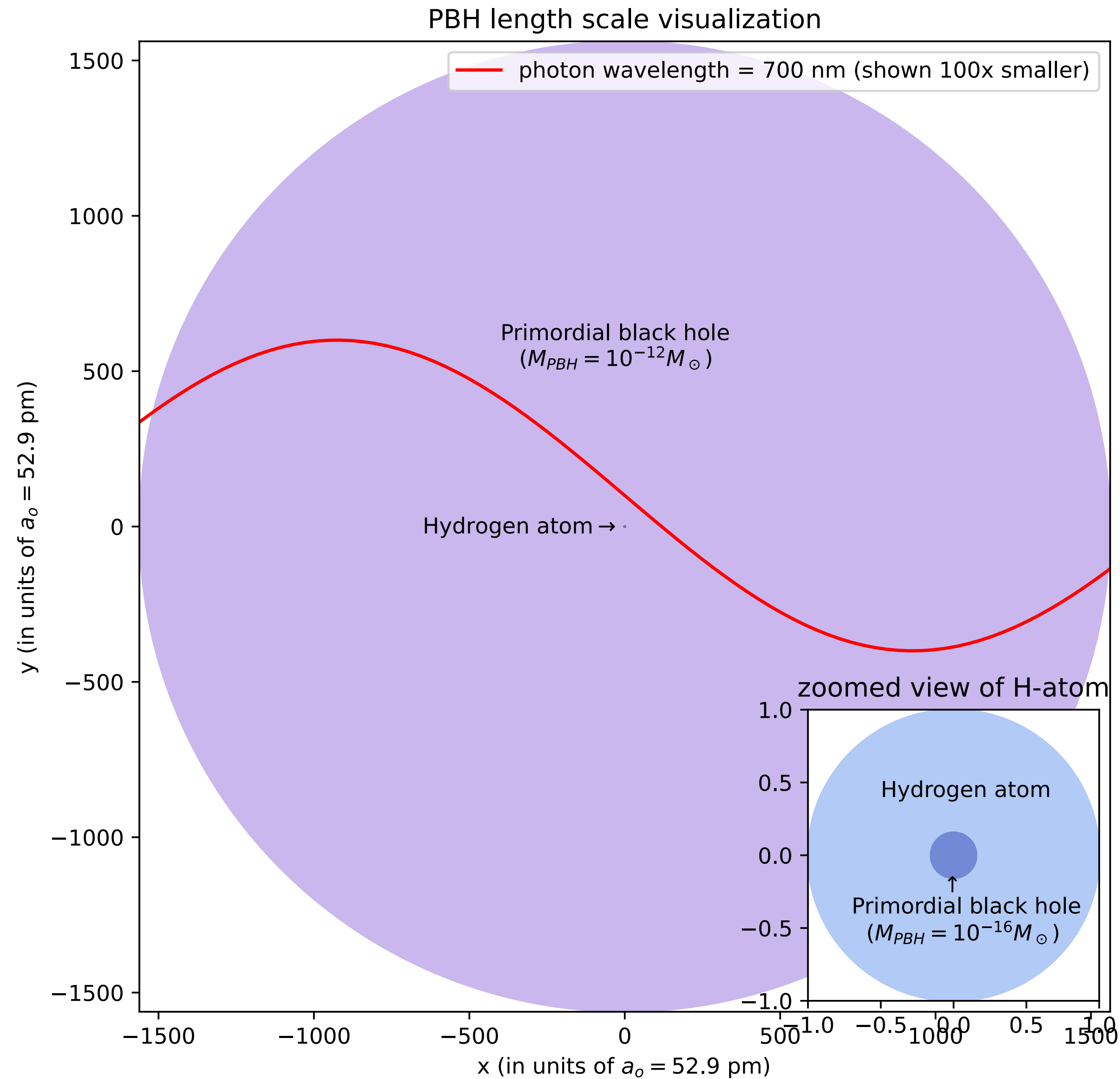


X-ray telescope sensitivities for PBH dark matter detection/exclusion



X μ : used the SED of Crab-like pulsar in SMC

Manish Tamta et. al.
+ 2024

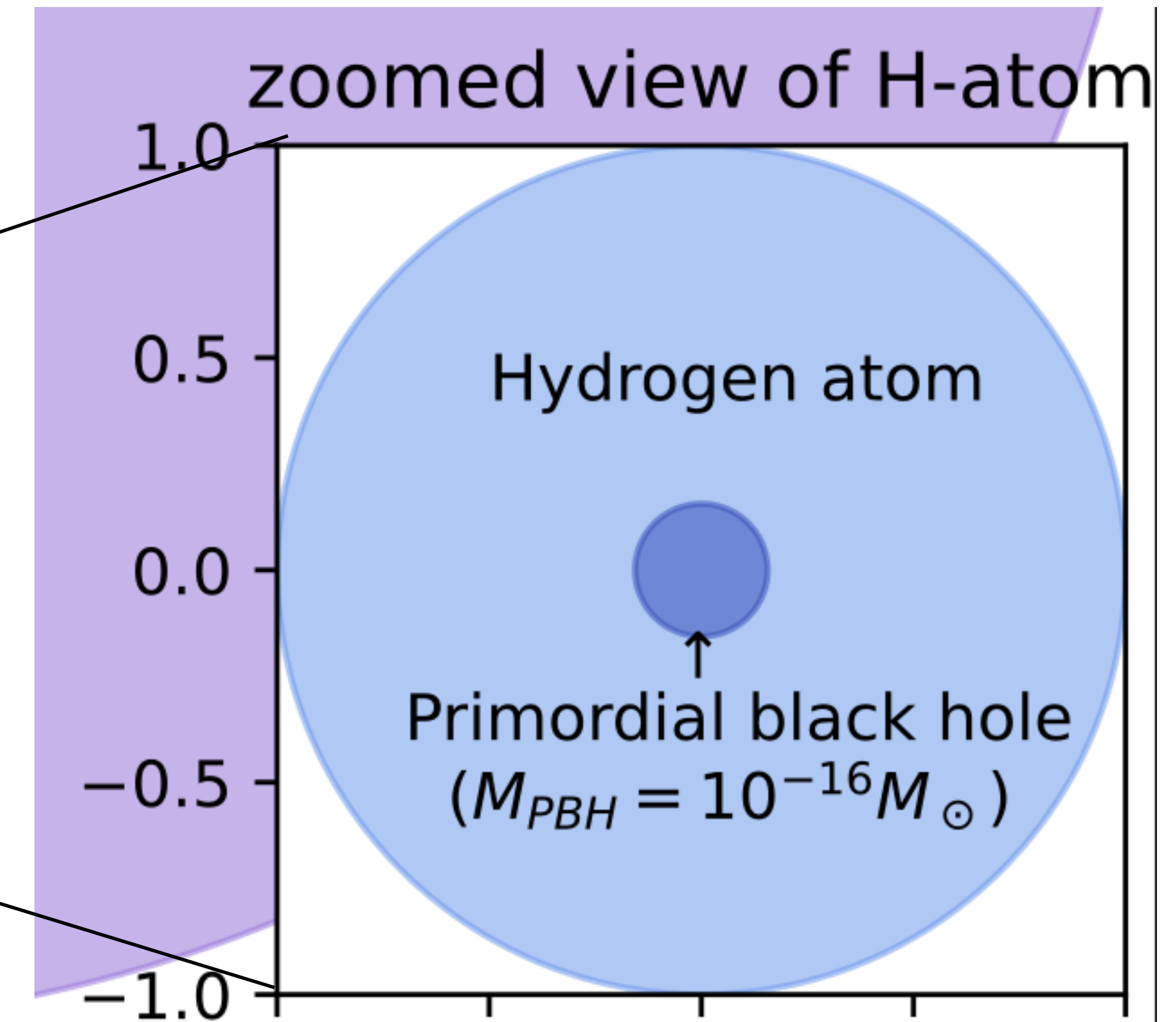
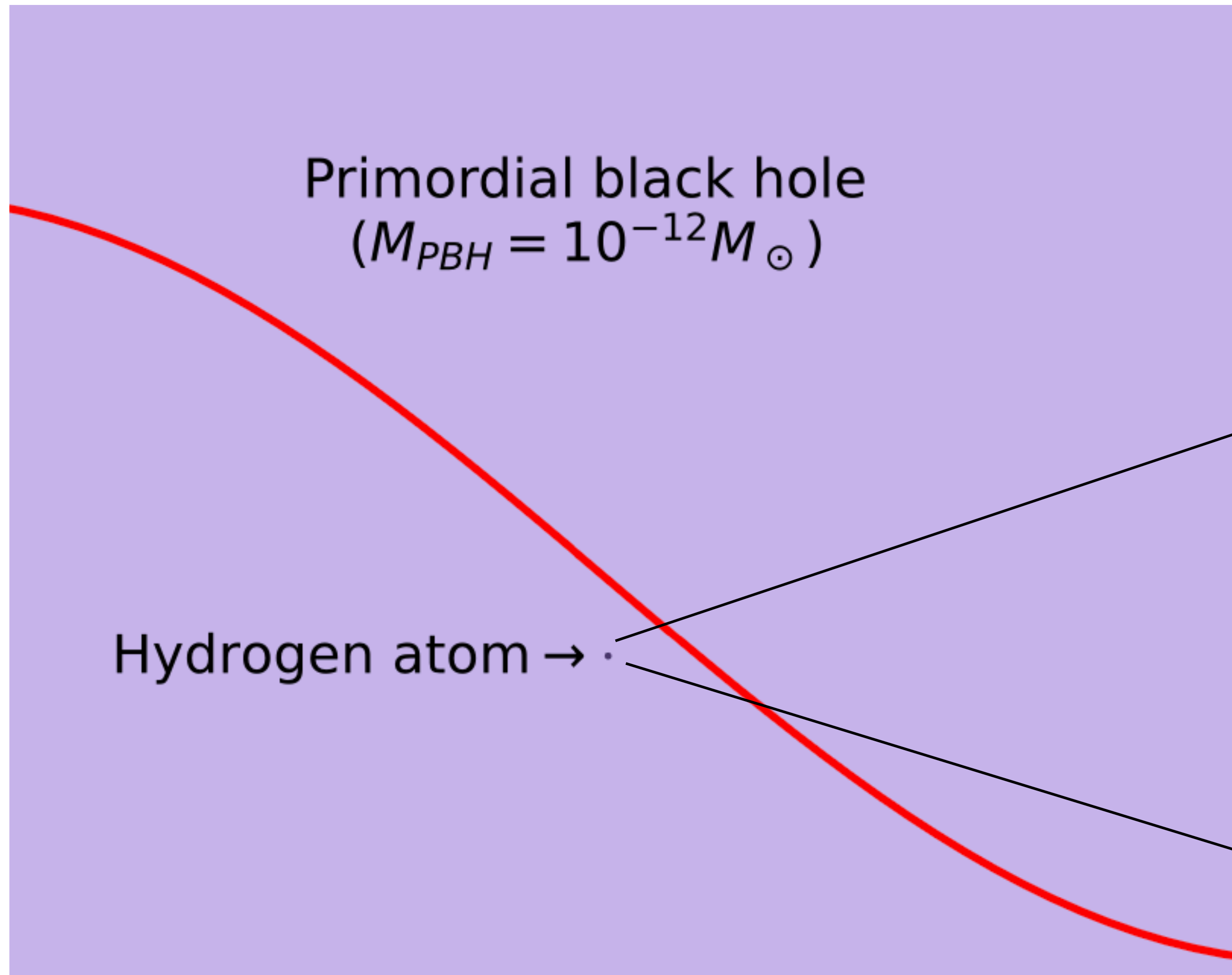


Mass/length scales involved

$$M_{PBH} \in [10^{-16}, 10^{-11}] M_{\odot}$$

$$R_{Schw} \in [2.9 \times 10^{-13}, 2.9 \times 10^{-8}] m$$

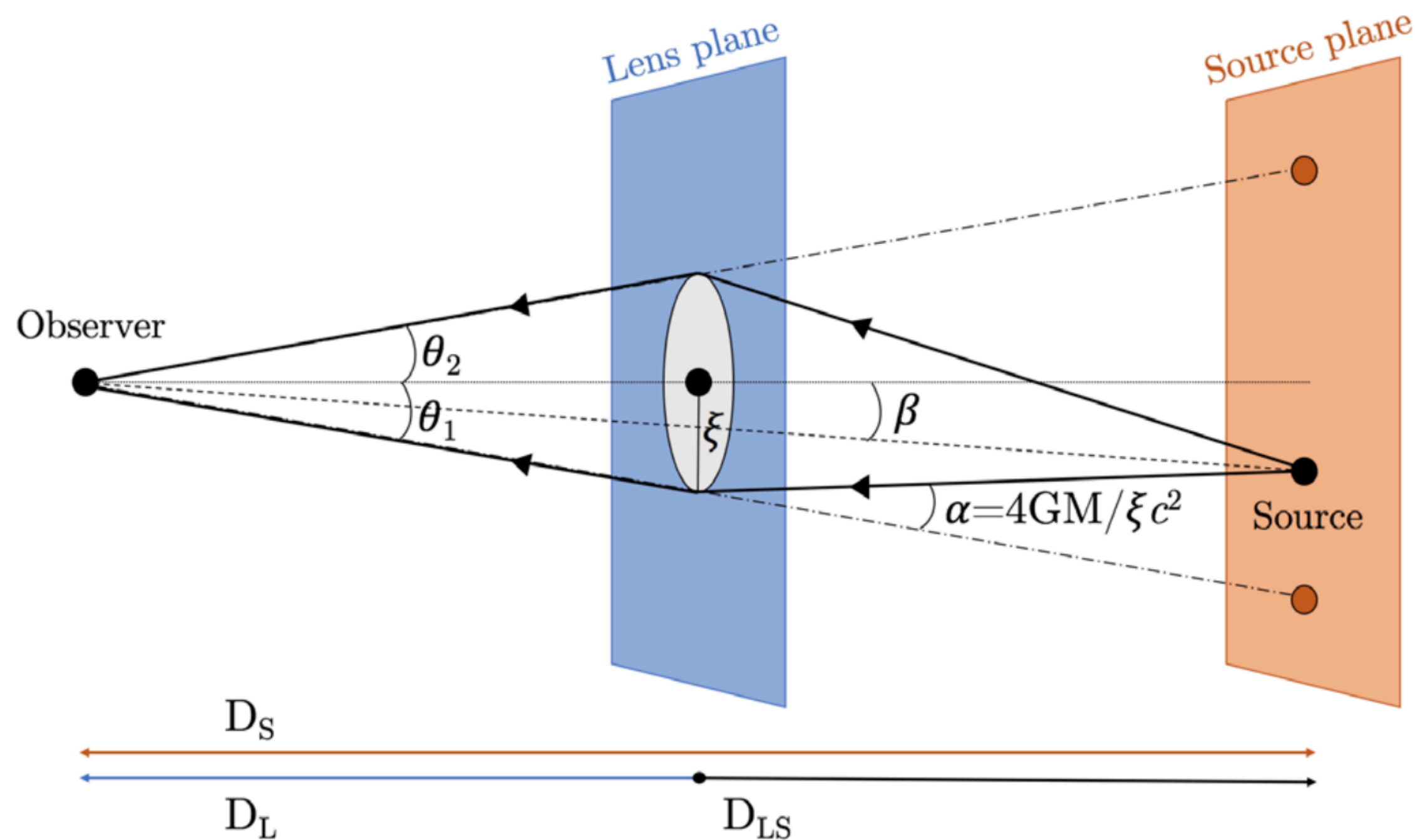
X-ray photons can probe these subatomic size PBHs



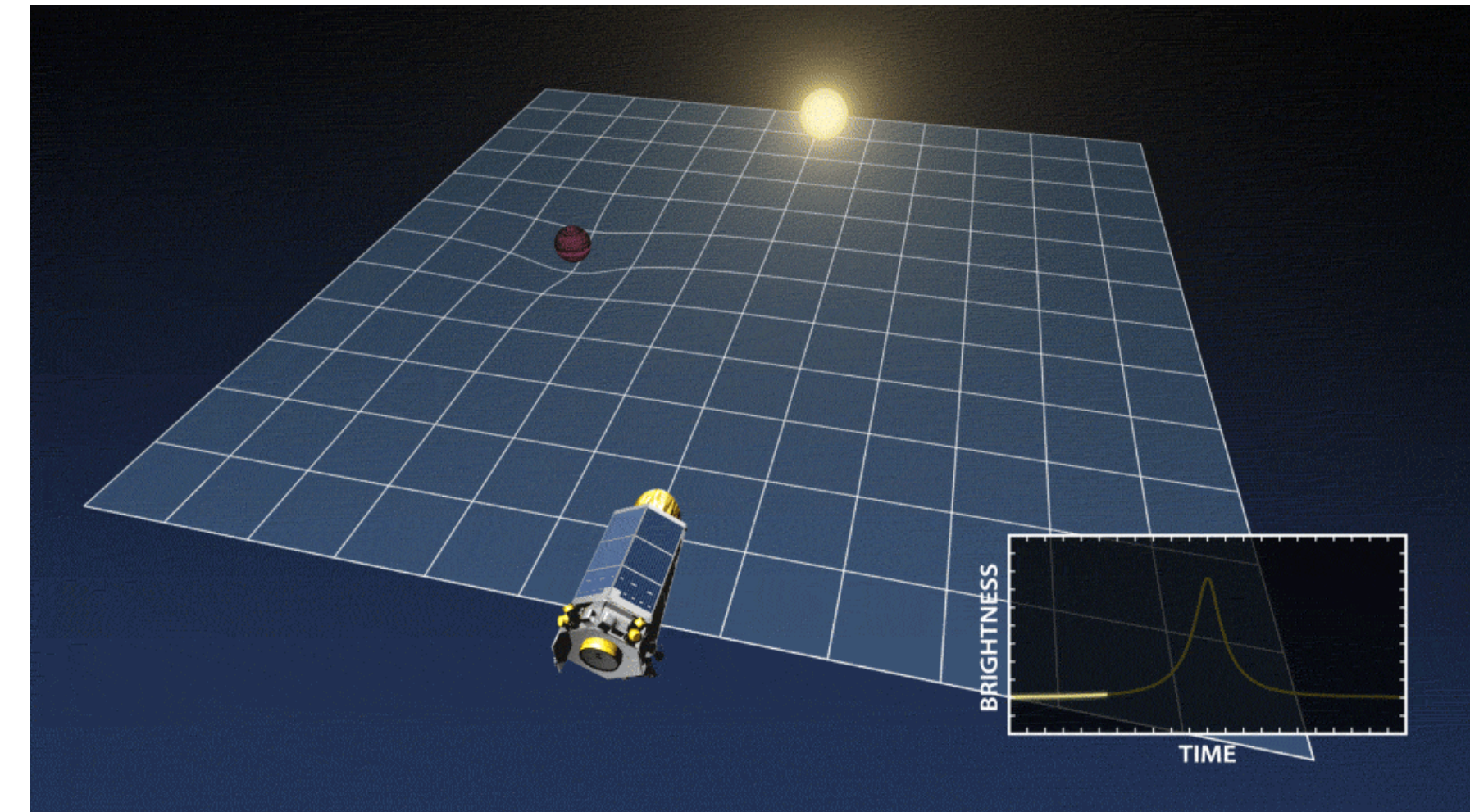
52.9 pm

What is gravitational microlensing

Lens equation: $\vec{\beta} = \vec{\theta} - \vec{\alpha}$



Croon, McKeen, Raj + 2020



$$\hat{\alpha} = \frac{4GM}{c^2 \xi} = \frac{2R_{Schw}}{\xi}$$

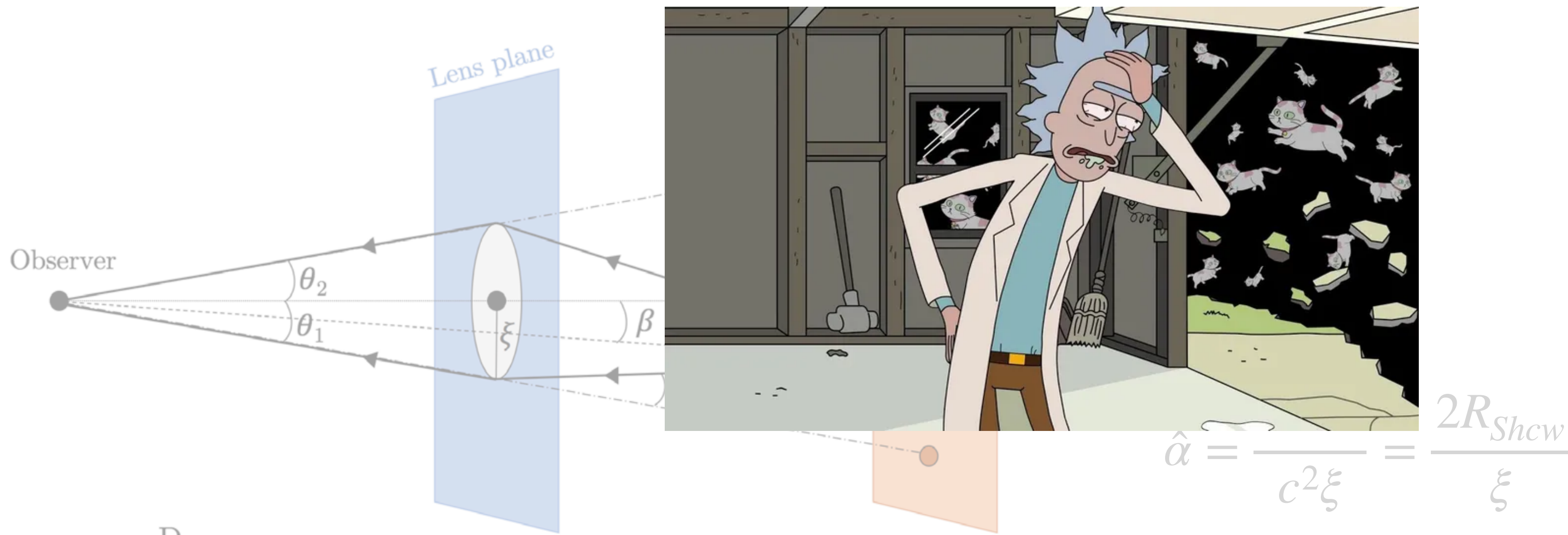
Magnification due to a point lens

$$\mu = \frac{\theta}{\beta} \frac{d\theta}{d\beta} = \frac{y^2 + 2}{y\sqrt{y^2 + 4}}$$

$$y \equiv \frac{\beta}{\theta_E}$$

Need for wave optics microlensing

Lens equation: $\vec{\beta} = \vec{\theta} - \vec{\alpha}$



$$\hat{\alpha} = \frac{2R_{Shcw}}{c^2 \xi} = \frac{2R_{Shcw}}{\xi}$$

Lens equation breaks down when microlensing happens in the wave regime!

Croon, McKeen, Raj + 2020

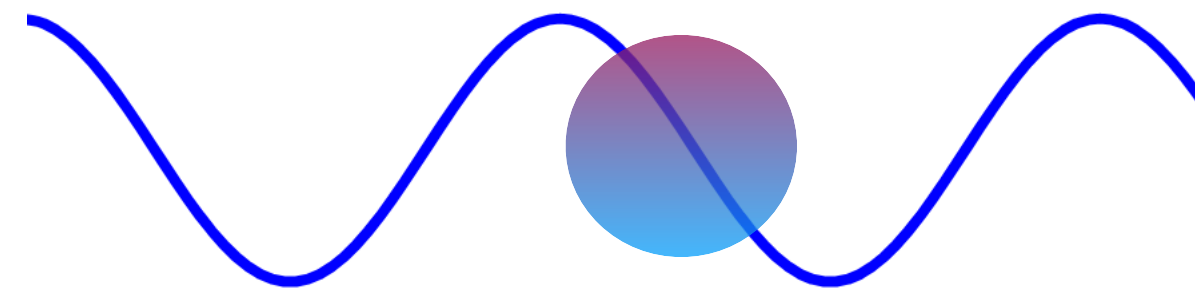
$$\mu = \frac{v \, dv}{\beta \, d\beta} = \frac{y^2 + 2}{y\sqrt{y^2 + 4}}$$

Wave regime lensing and Parameter w

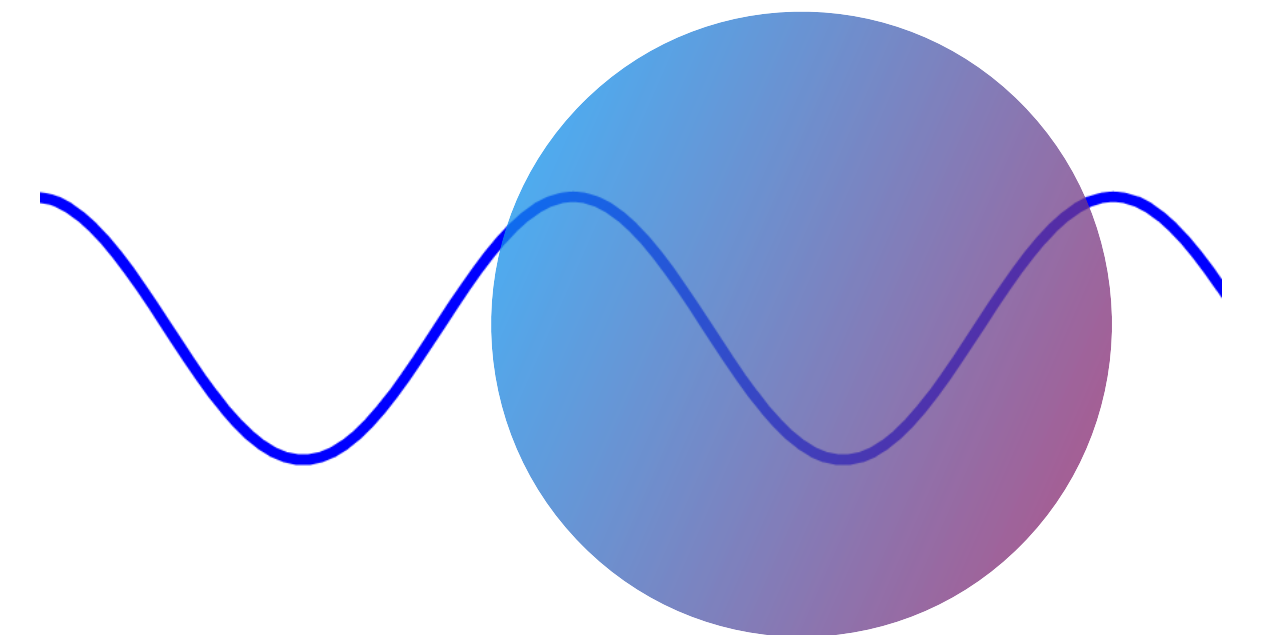
$$w \equiv \frac{4GM E_\gamma}{\hbar c^3} = \frac{2R_{schw} E_\gamma}{\hbar c}$$

← Dimensionless frequency

Wave regime: if $w \lesssim y^{-1}$



Geometric optics regime: when $w \gg y^{-1}$



Note that y is impact parameter!

Theory of gravitational microlensing in the wave regime+FSE

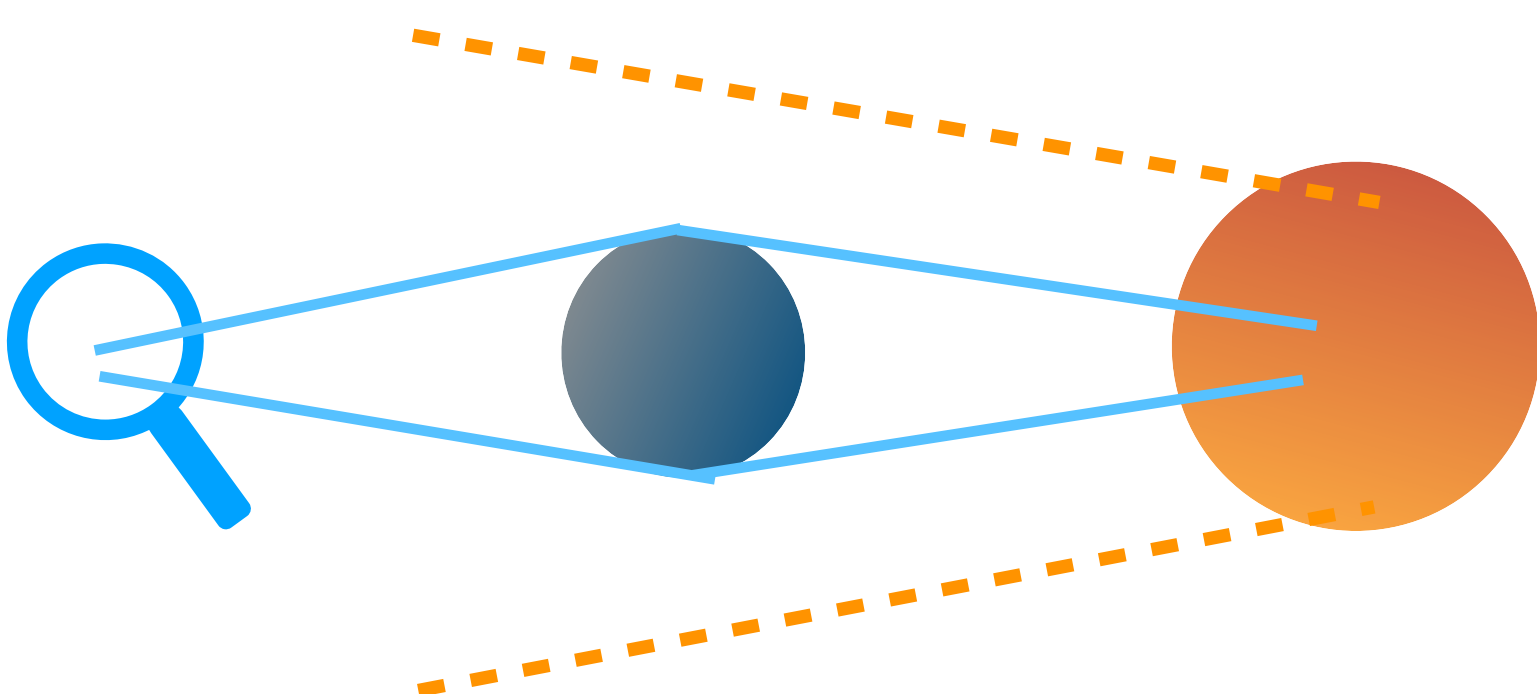
$$\bar{\mu}_E(y, a_s(x)) = \frac{1}{\mathcal{N}} \int_{E_{min}}^{E_{max}} dE \mathcal{A}(E) \mathcal{F}(E) a_s^{-2} e^{-\frac{y^2}{2a_s^2}} \frac{\pi w}{1 - e^{-\pi w}} \int_0^\infty r e^{\frac{-r^2}{2a_s^2}} I_0(yr/a_s^2) \left| {}_1F_1\left(\frac{iw}{2}, 1; \frac{iwr^2}{2}\right) \right|^2 dr$$

Pulsar
Wave-effects

Detector
Finite extent of the source

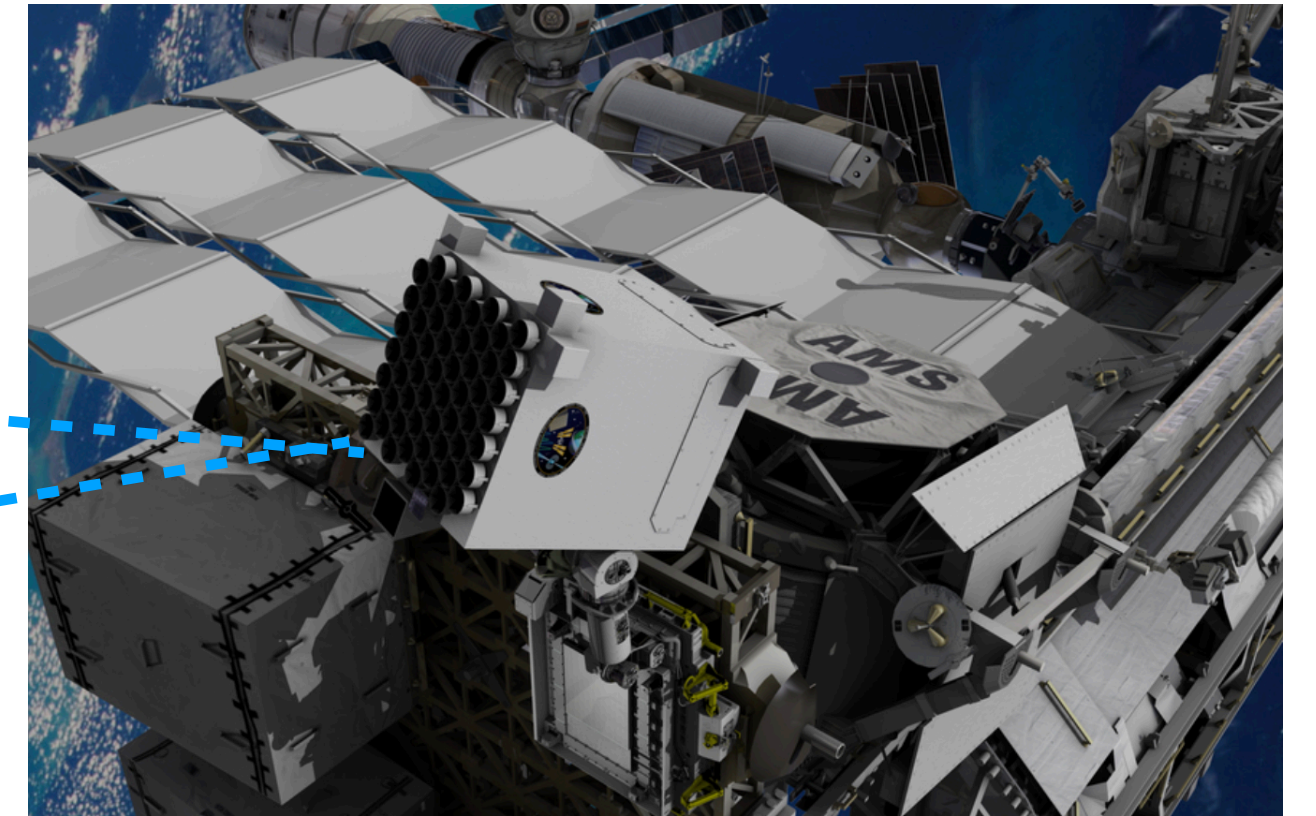
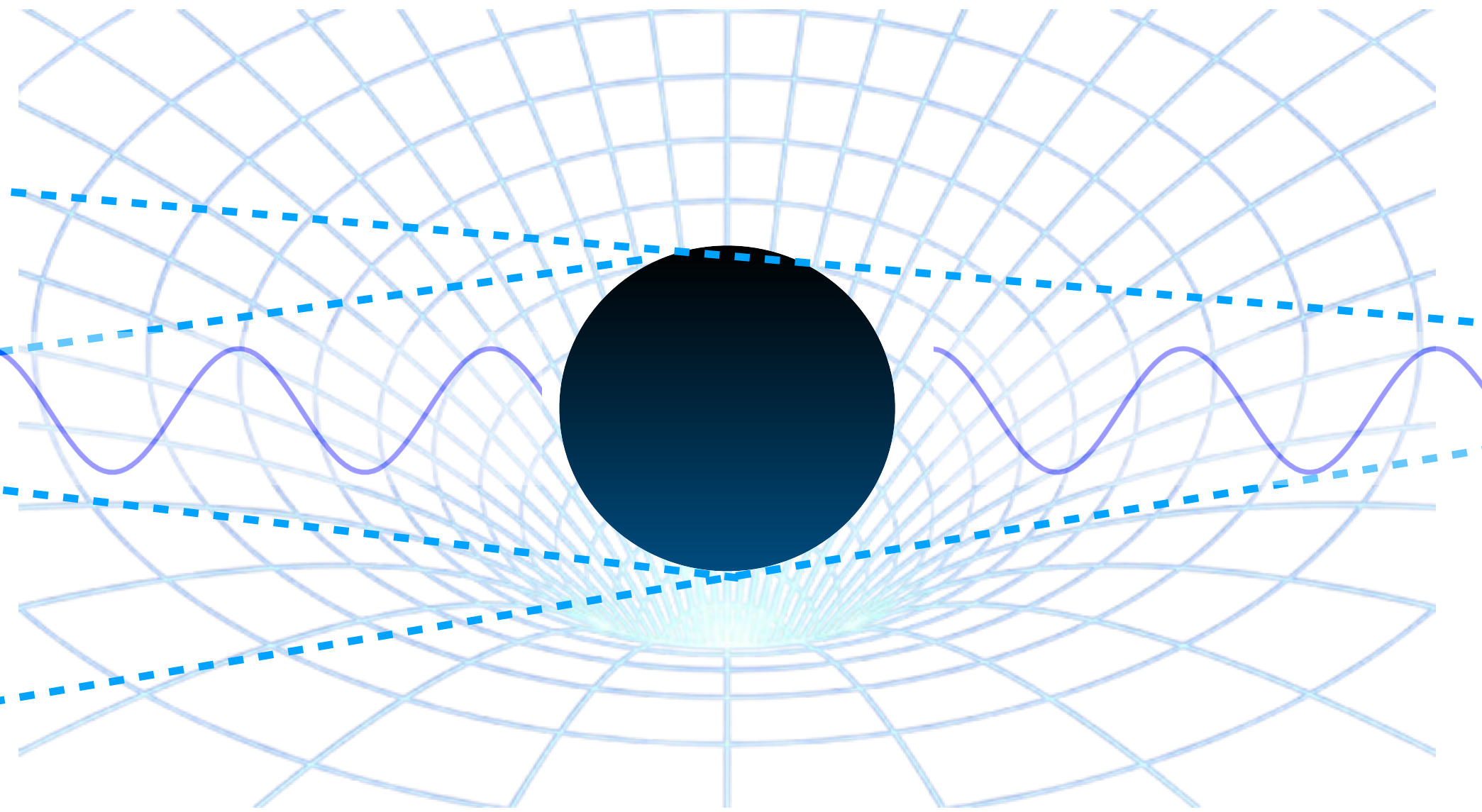
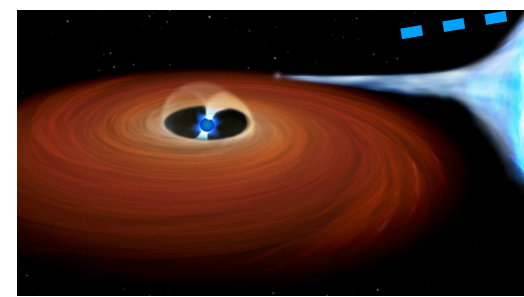
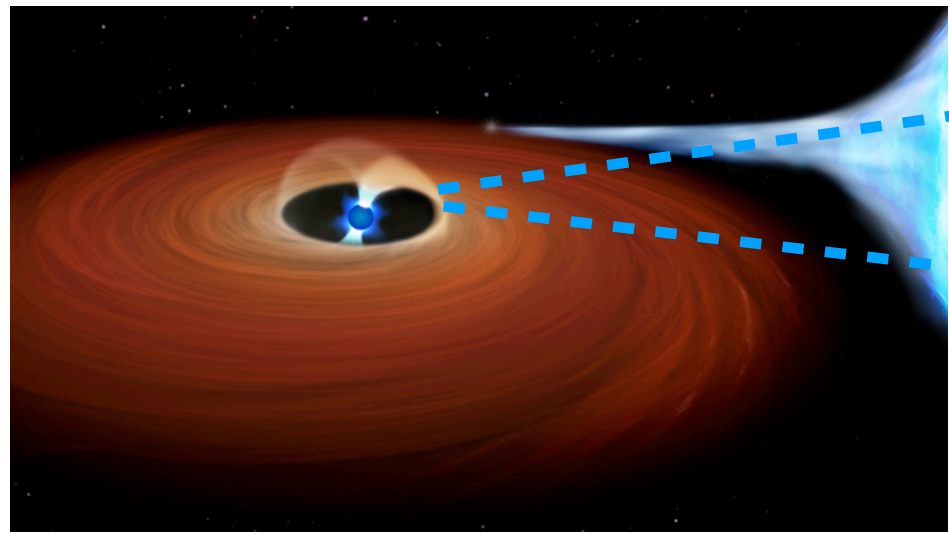
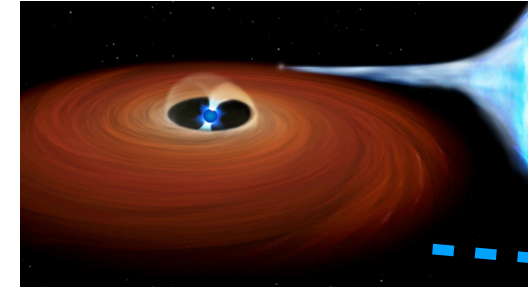
$$a_s = \frac{xR_s}{r_E}$$

where $\mathcal{N} = \int_{E_{min}}^{E_{max}} dE \mathcal{A}(E) \mathcal{F}(E)$



Frequency dependent magnification!

X-ray microlensing can probe subatomic size PBHs

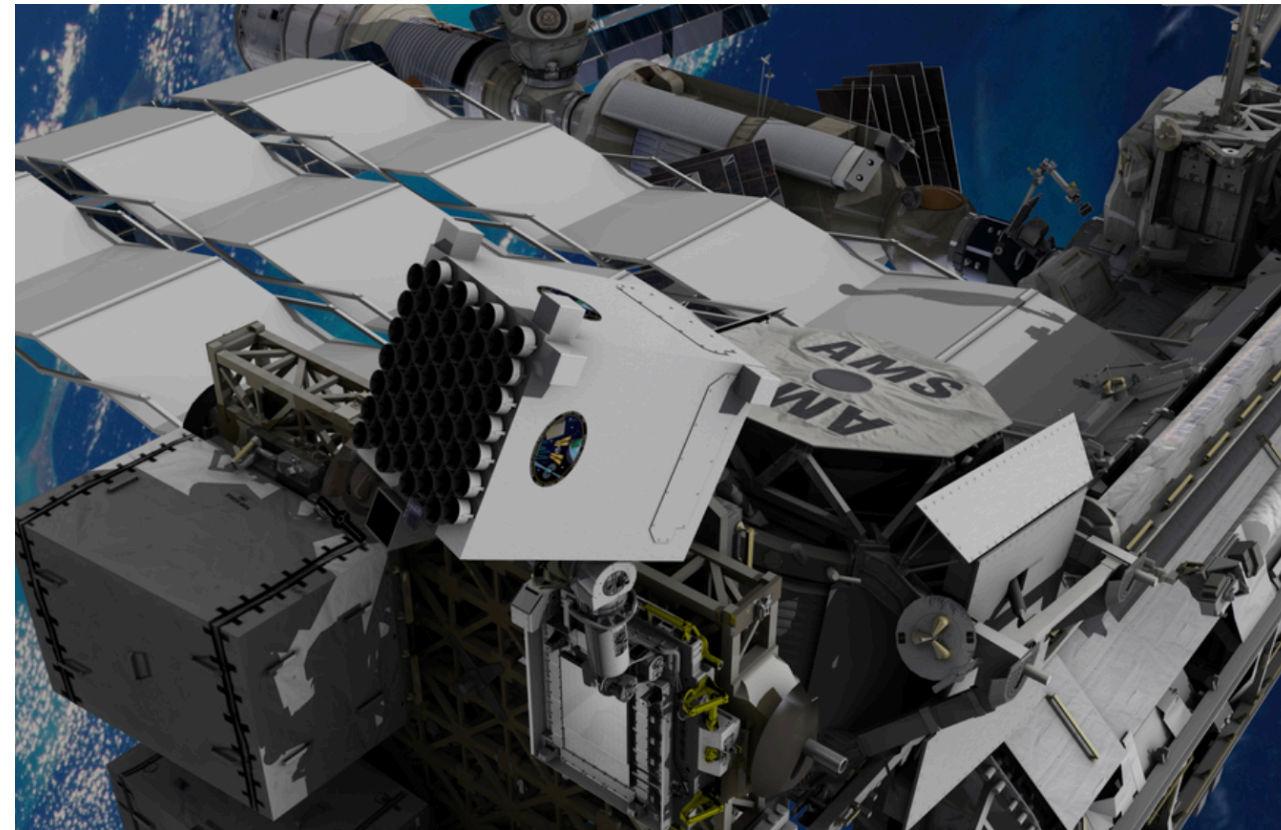


Yang Bai et. al. + 2019

Why X-ray pulsars?

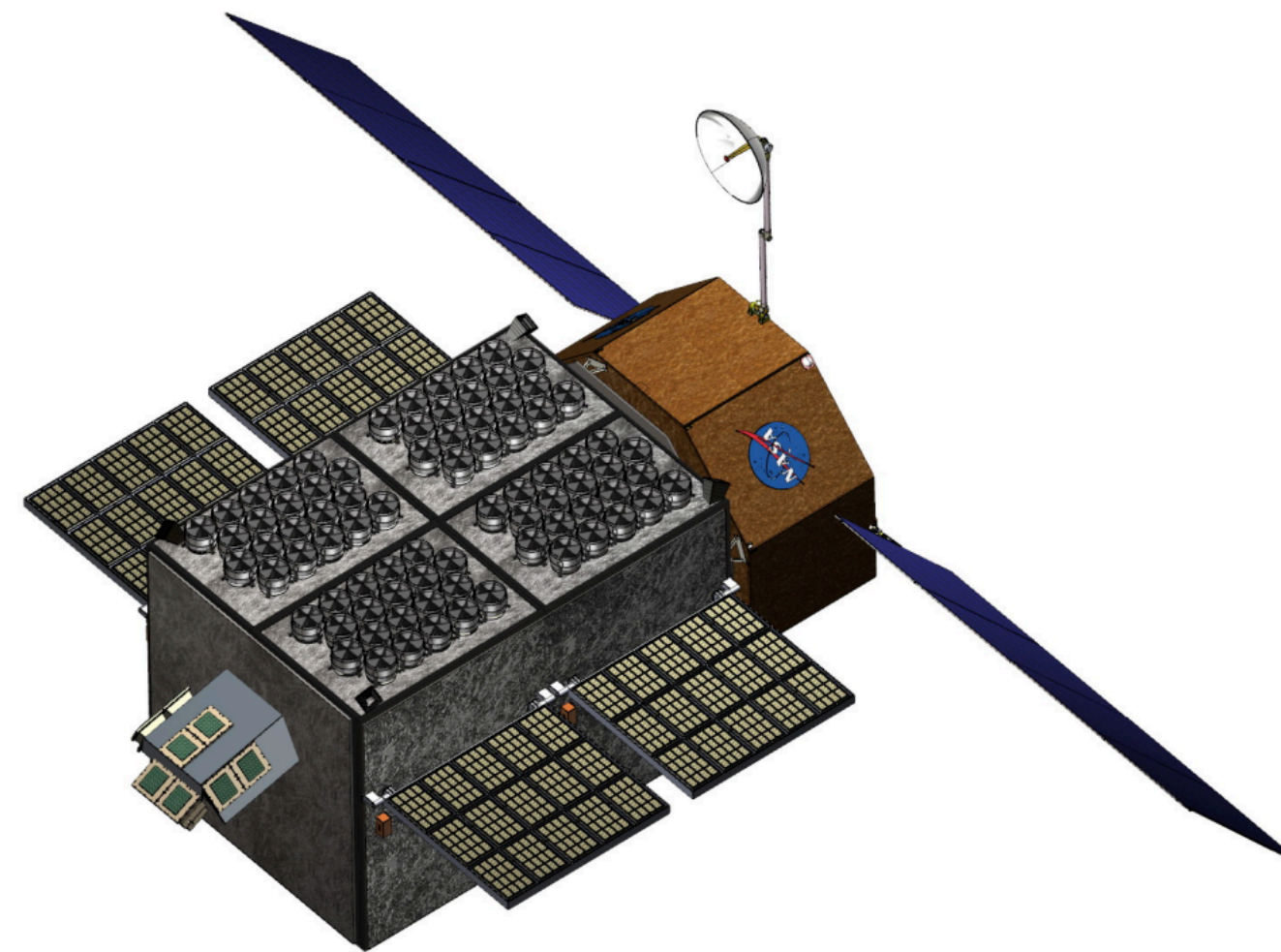
- Less variability and persistent x-ray emission
- Higher photon counts

Telescopes and pulsars for x-ray microlensing



NASA's NICER

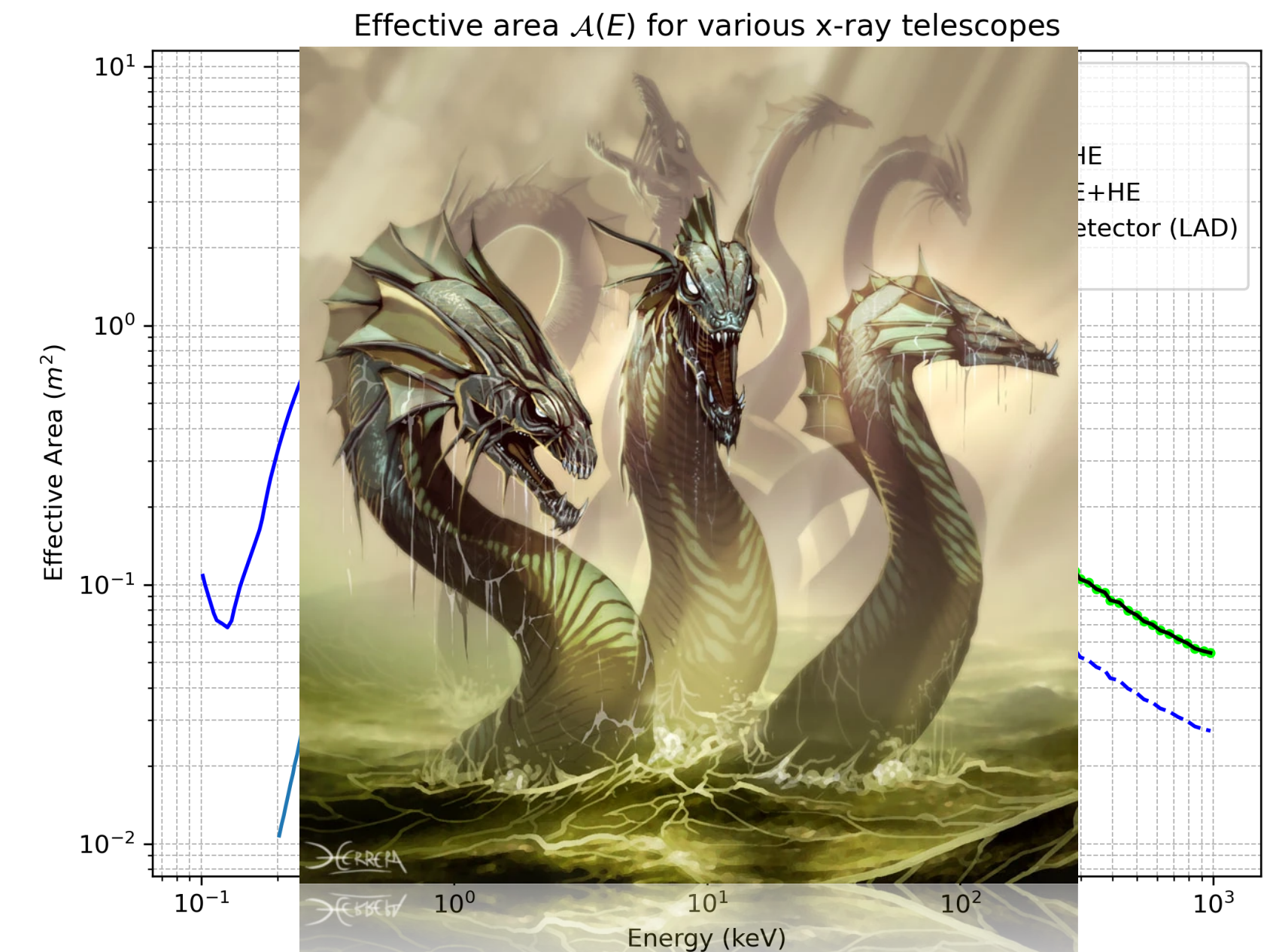
<https://svs.gsfc.nasa.gov/>



STROBE-X

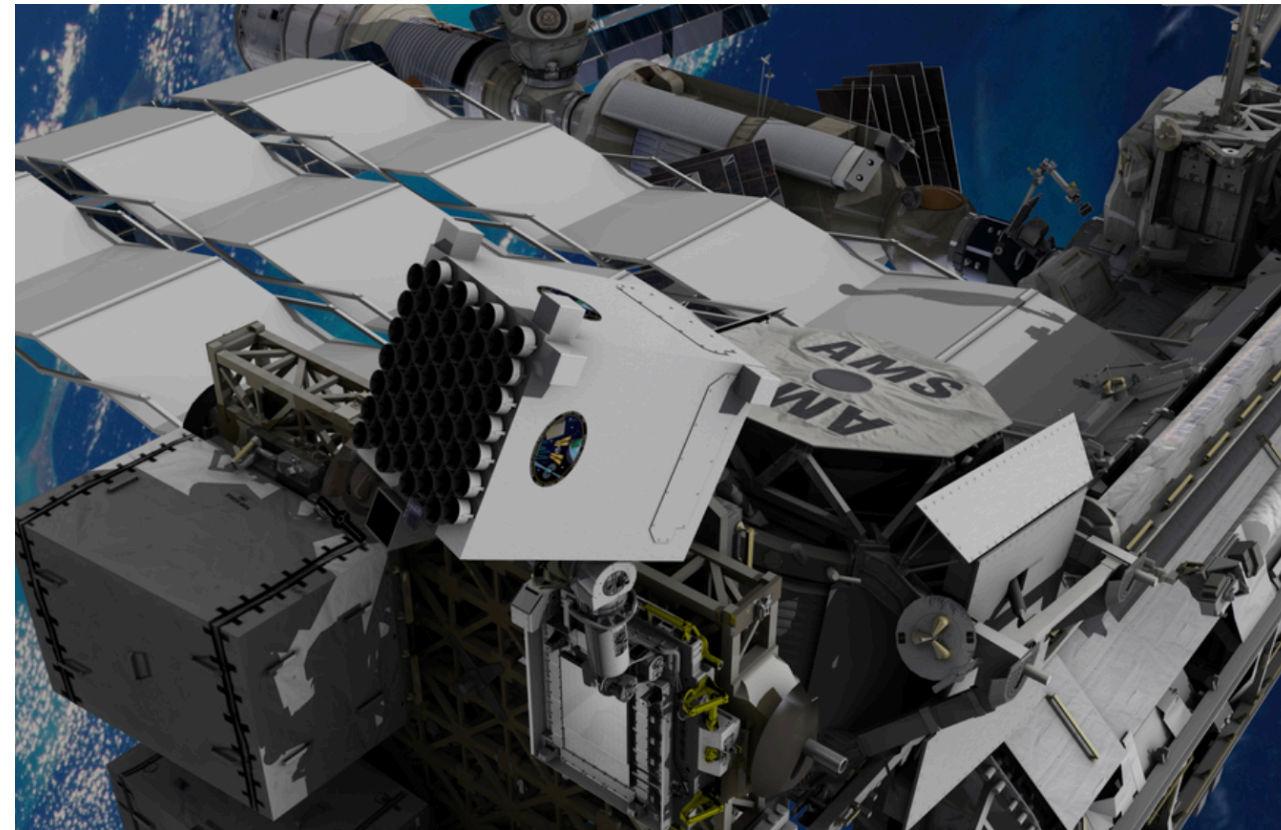
arXiv:1903.03035

Expected launch: 2031



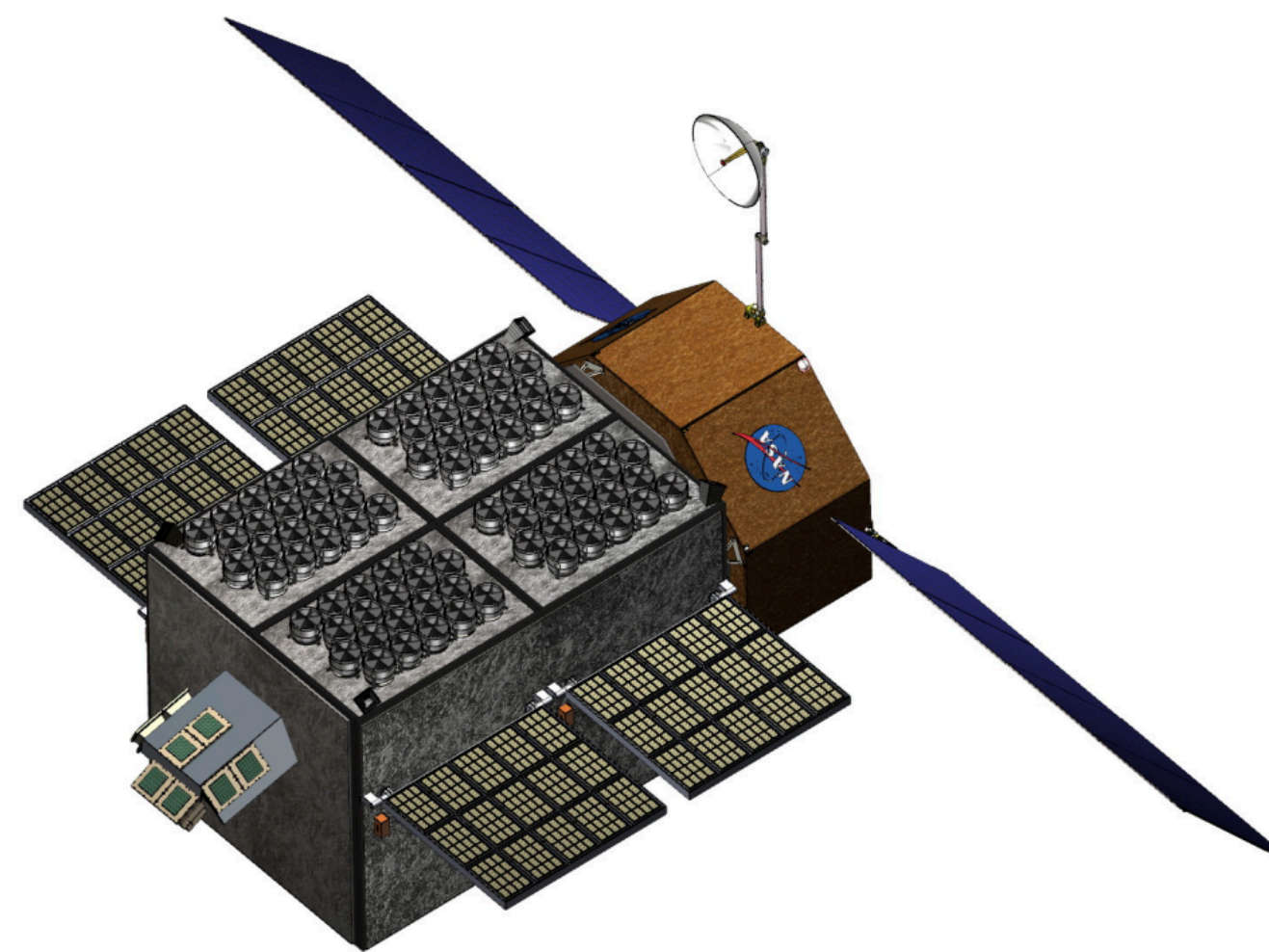
**Let's hope for such
telescopes in the near future :)**

Telescopes and pulsars for x-ray microlensing



NASA's NICER

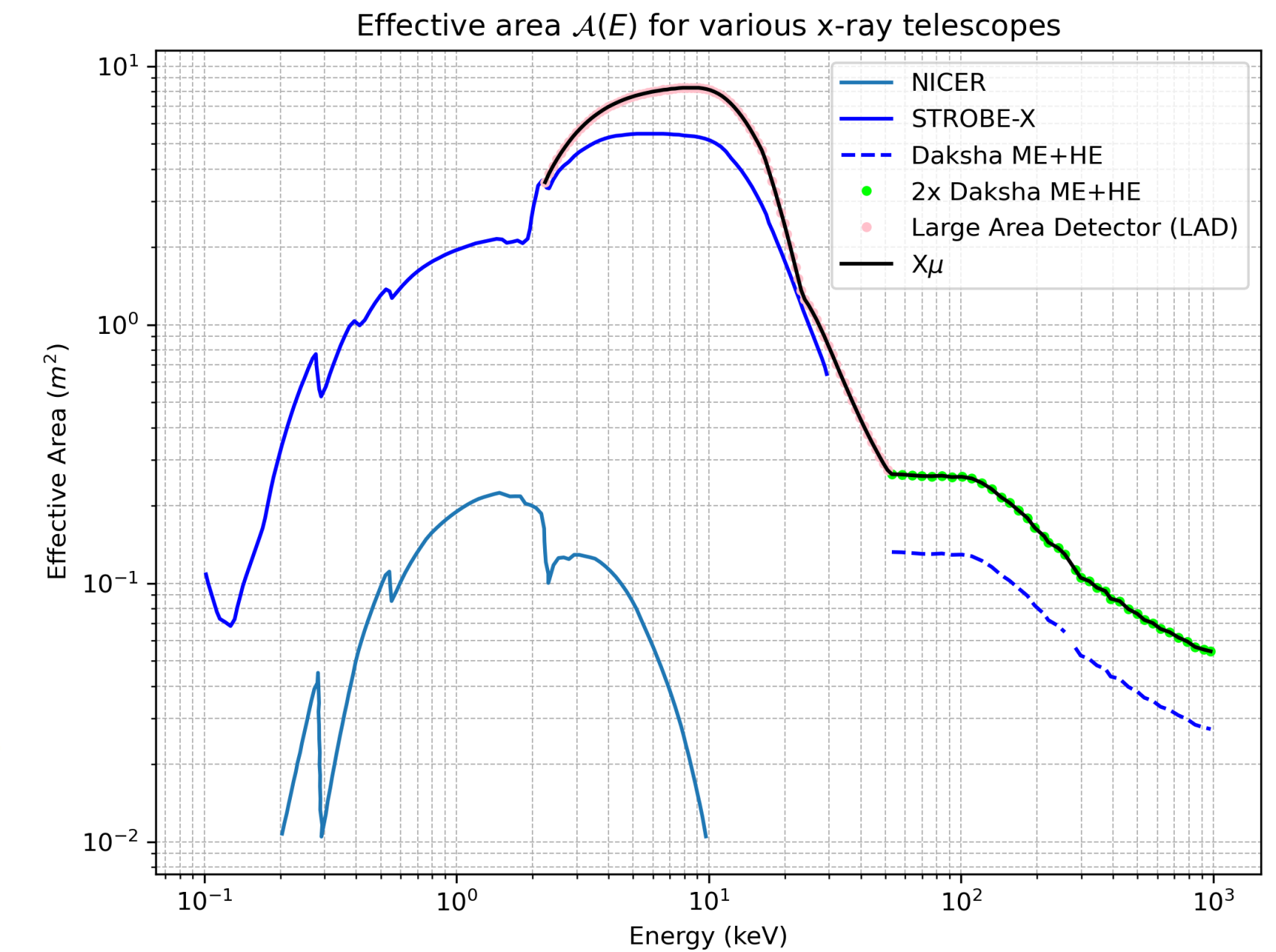
<https://svs.gsfc.nasa.gov/>



STROBE-X

arXiv:1903.03035

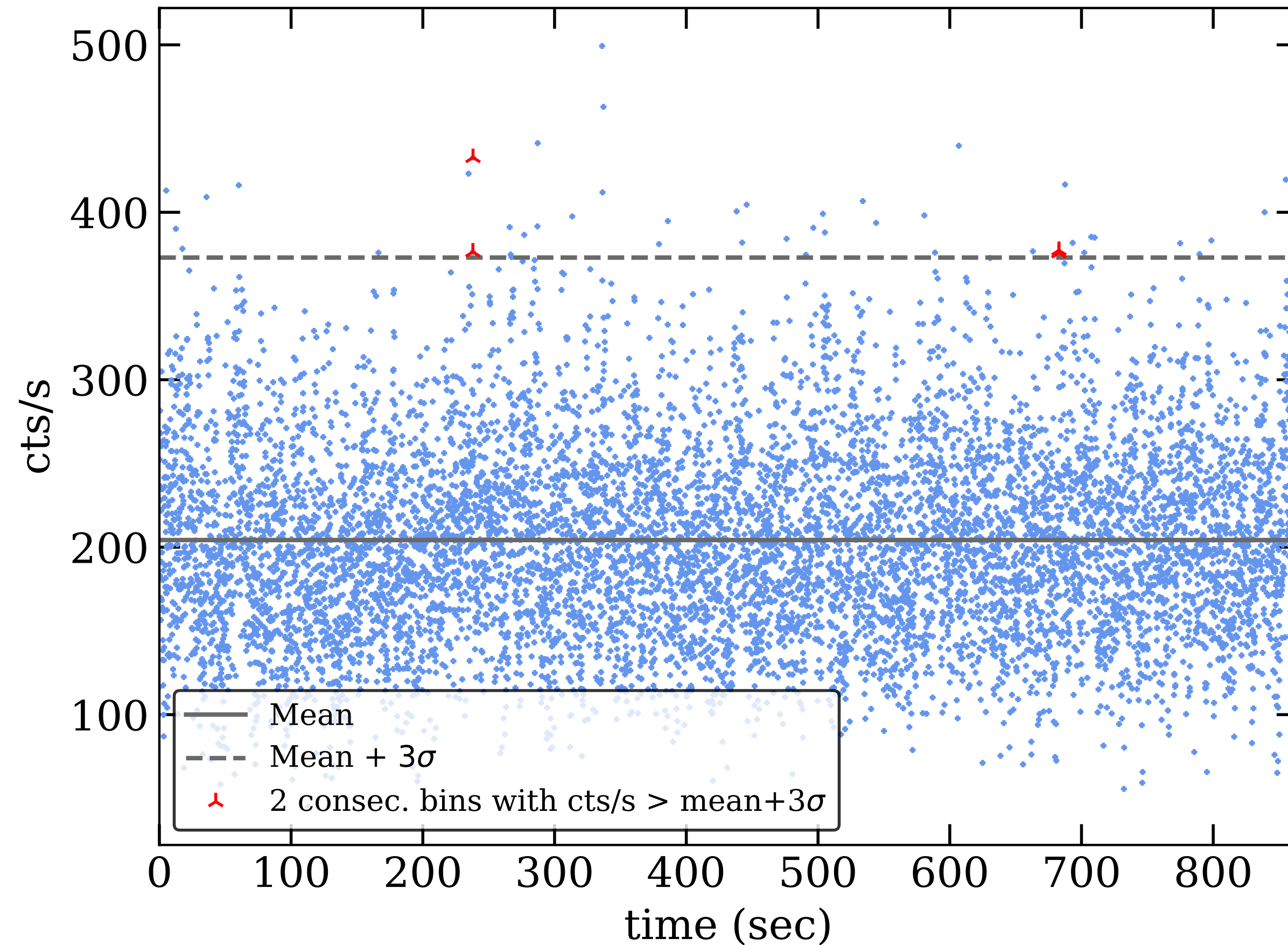
Expected launch: 2031



$X\mu$

x-ray pulsar	net exposure (days)	D_S (kpc)	(ℓ, b)	σ_B/B
SMC X-1	1.74	64 [28]	$(300.41^\circ, -43.56^\circ)$	0.28
Cyg X-2	5.47	11 [29]	$(87.33^\circ, -11.32^\circ)$	0.02
Vela X-1	4.46	2 [30]	$(263.06^\circ, 3.93^\circ)$	0.25
Crab pulsar	4.76	2 [31]	$(184.56^\circ, -5.78^\circ)$	0.01

Statistical way of interpreting X-ray pulsar light curve



How to identify a true microlensing event in the light curve?

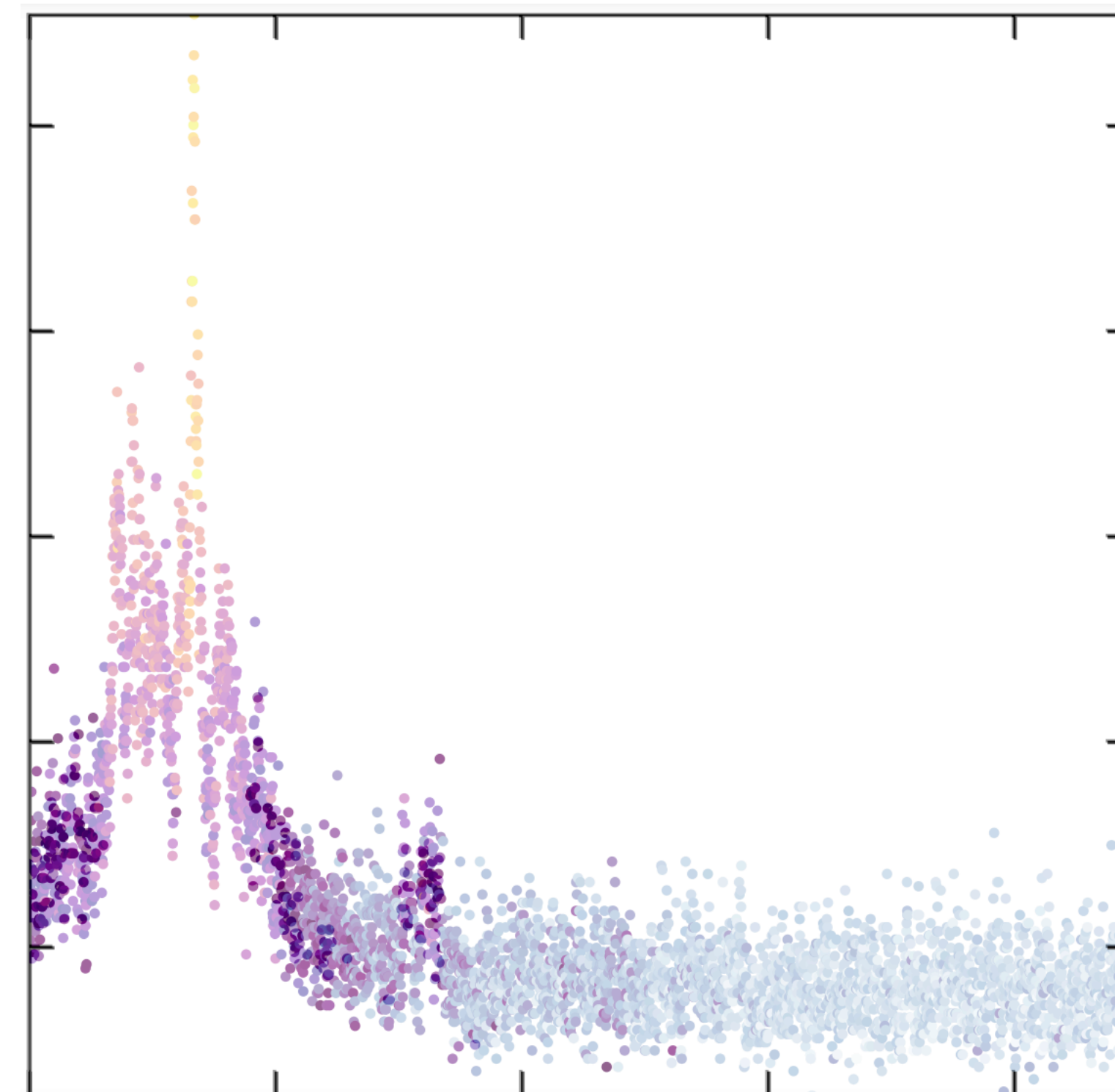
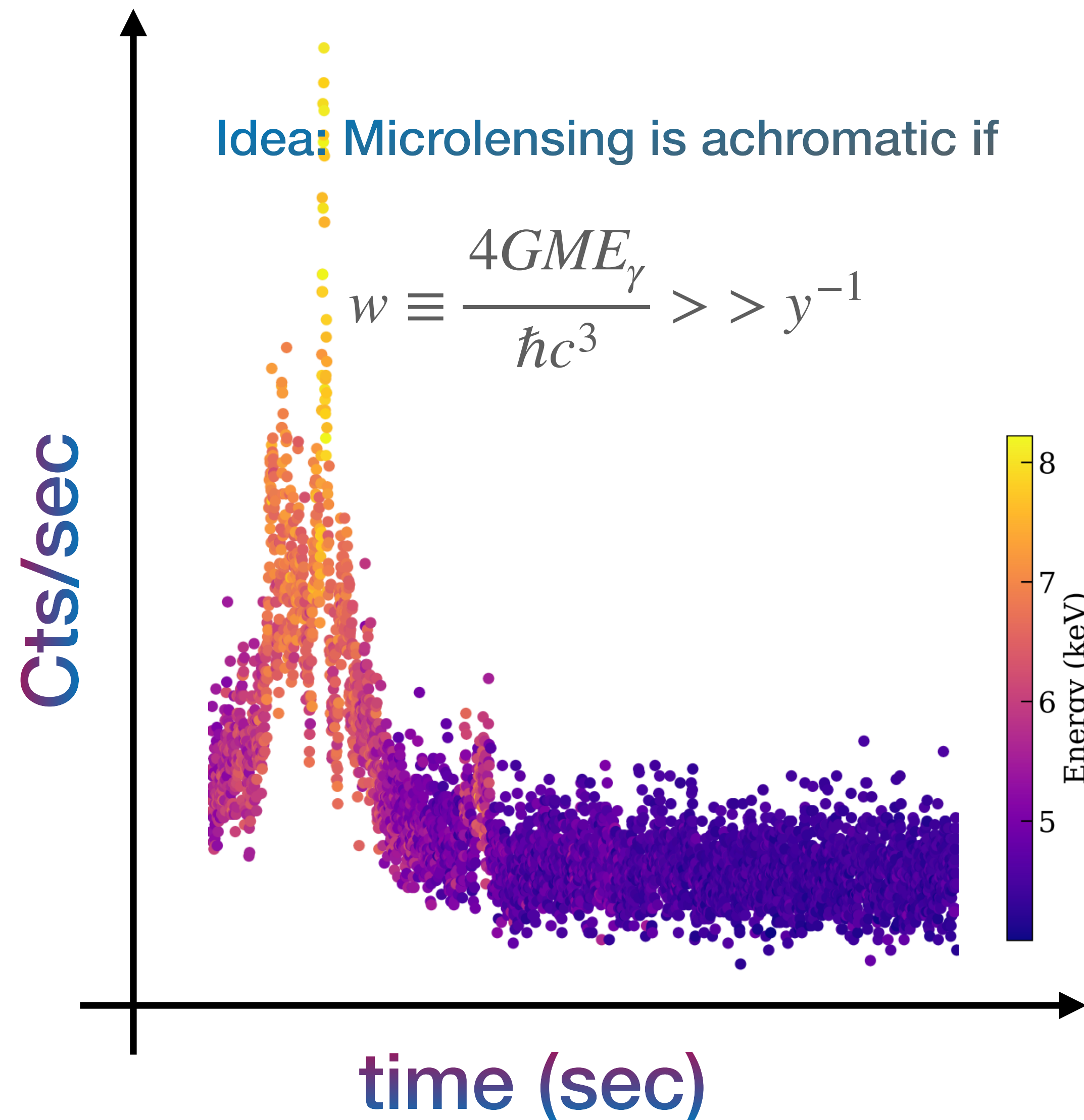
Excess x-ray photon counts at 3σ level for 3 consecutive time bins is a detection!

+

Achromaticity ($w \gtrsim y^{-1}$)

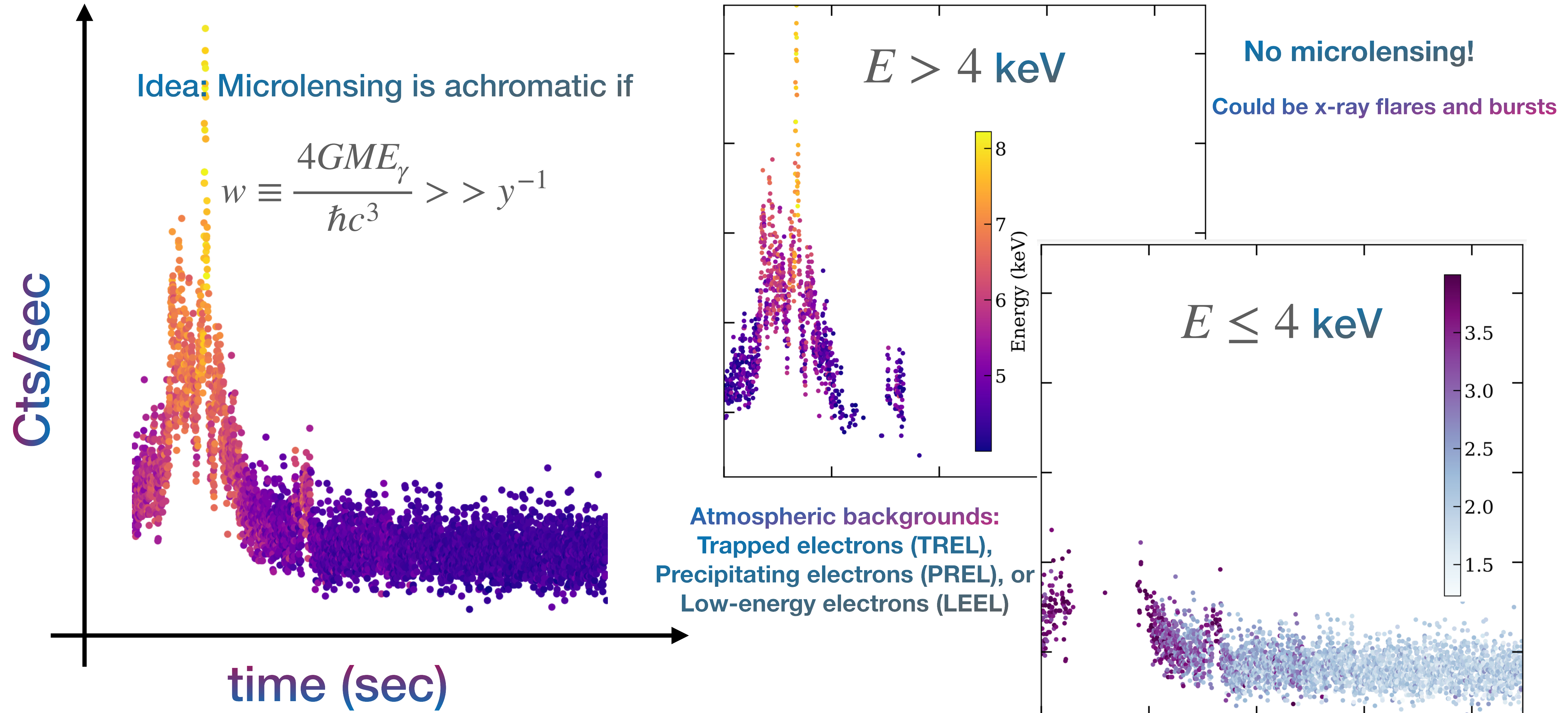
$$\mathbb{P}(N_\sigma) = [1 - \Phi(N_\sigma = 3)]^{N_{consec}=3} = 2.5 \times 10^{-9}$$

A new diagnostic for x-ray microlensing



Split the light
curve into
multiple energy
windows

A new diagnostic for x-ray microlensing



Microlensing Event Rate

$$\frac{d\Gamma}{dt_E} = f_{PBH} \frac{2D_s}{Mv_0^2} \int_0^1 dx \rho_{dm}(x) v_E^4(x) e^{-v_E^2/v_0^2} \times \int_0^{y_T(x)} \frac{dy}{\sqrt{y_T^2 - y^2}} \times \mathbb{P}(n_\sigma)$$

Local DM
density

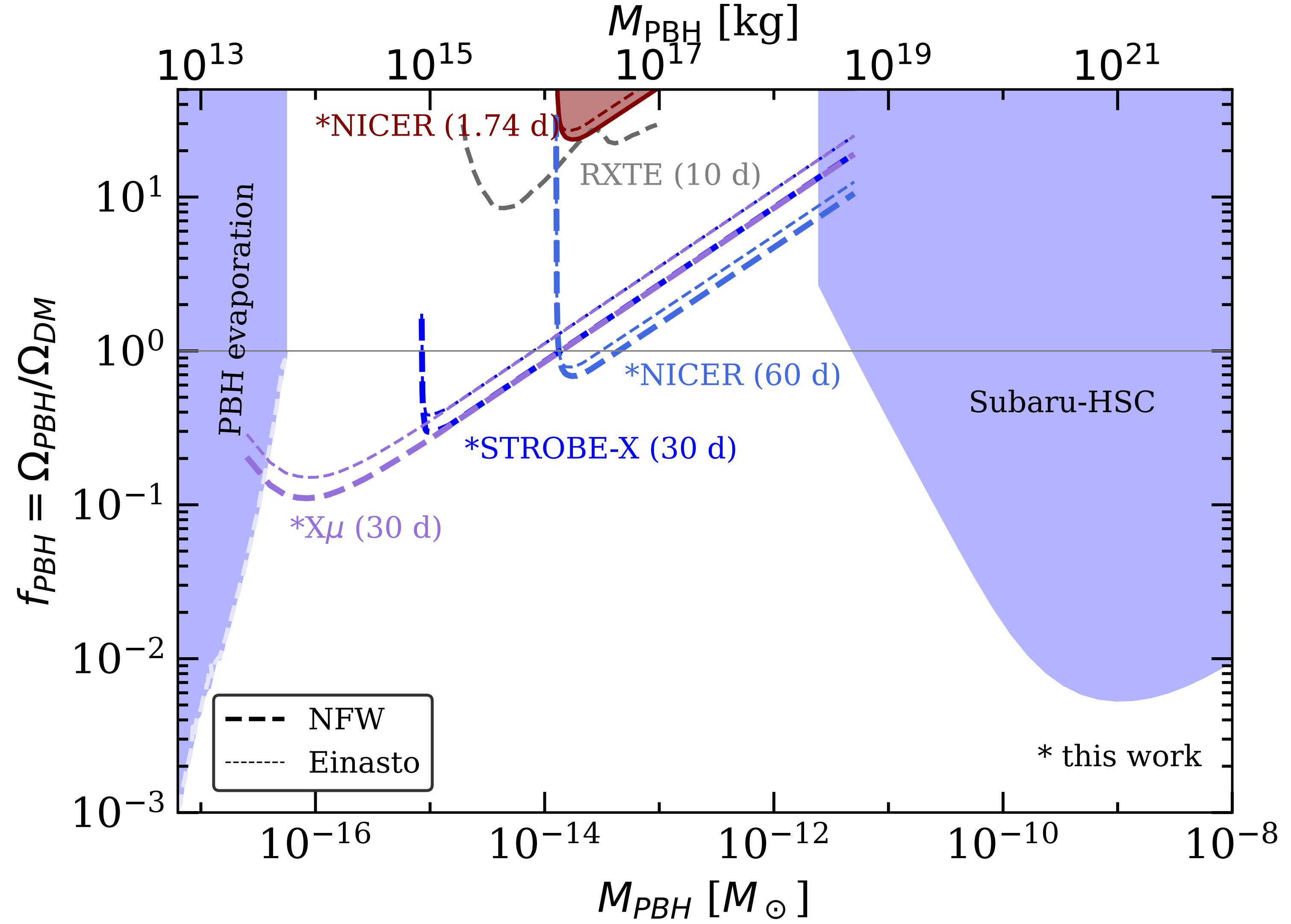
Remember

$$d\Gamma \sim 1/\sqrt{M}$$

$$v_E \equiv 2r_E \sqrt{y_T^2 - y^2} / t_E$$

Total # of microlensing events: $N_{ev} = f_{PBH} \sum_i T_{obs}^i \int_{t_{min,i}}^{t_{max,i}} dt_E \frac{d\Gamma_i}{dt_E}$

X-ray telescope sensitivities for PBH dark matter detection/exclusion



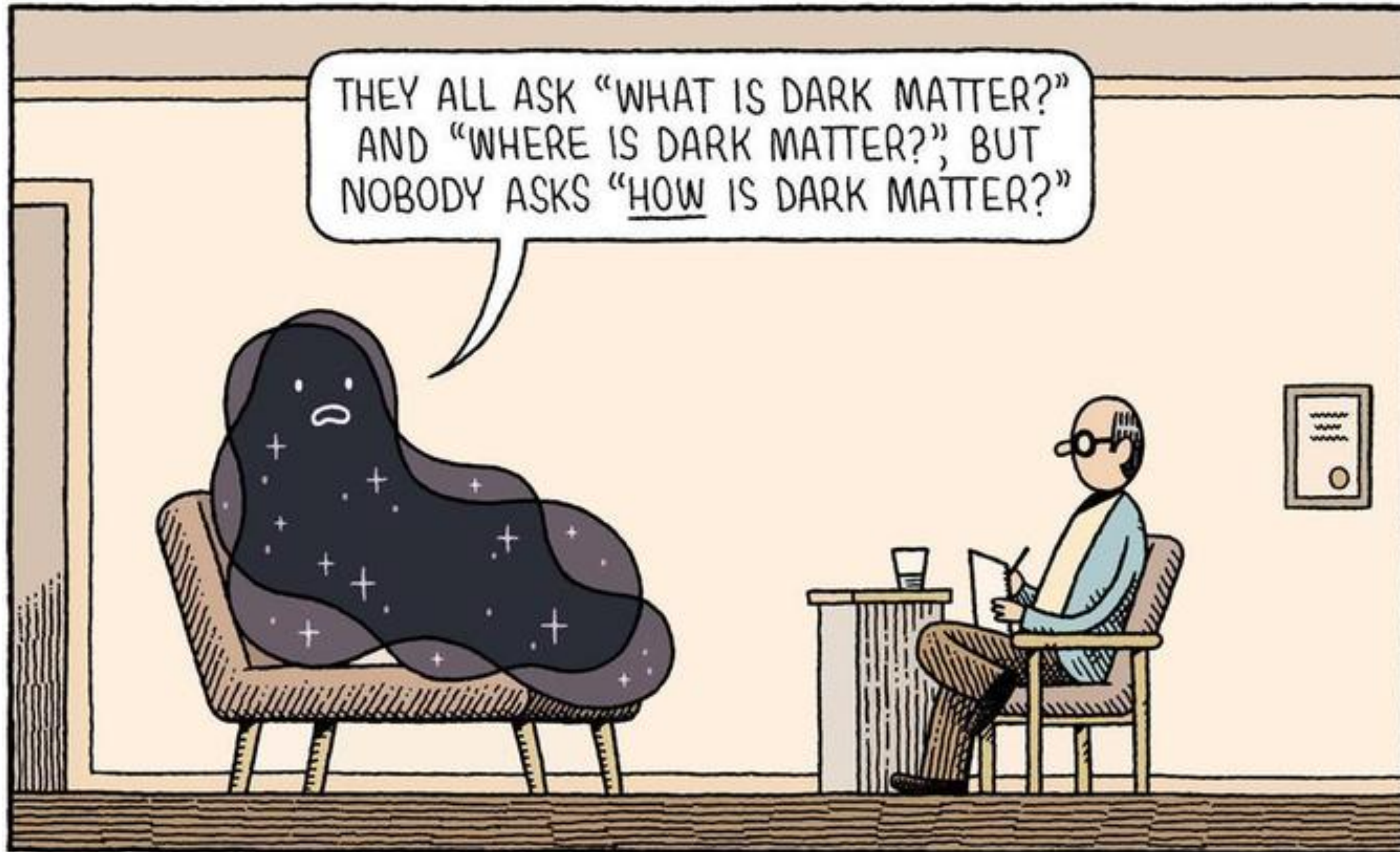
X μ : used the SED of Crab-like pulsar in SMC

Take Home

- Primordial black holes (PBHs) in the mass range $10^{-16} - 10^{-11} M_{\odot}$ may constitute 100% dark matter.
- **WO microlensing of bright x-ray pulsars provide the most robust and immediately implementable opportunity to uncover PBH dark matter.**

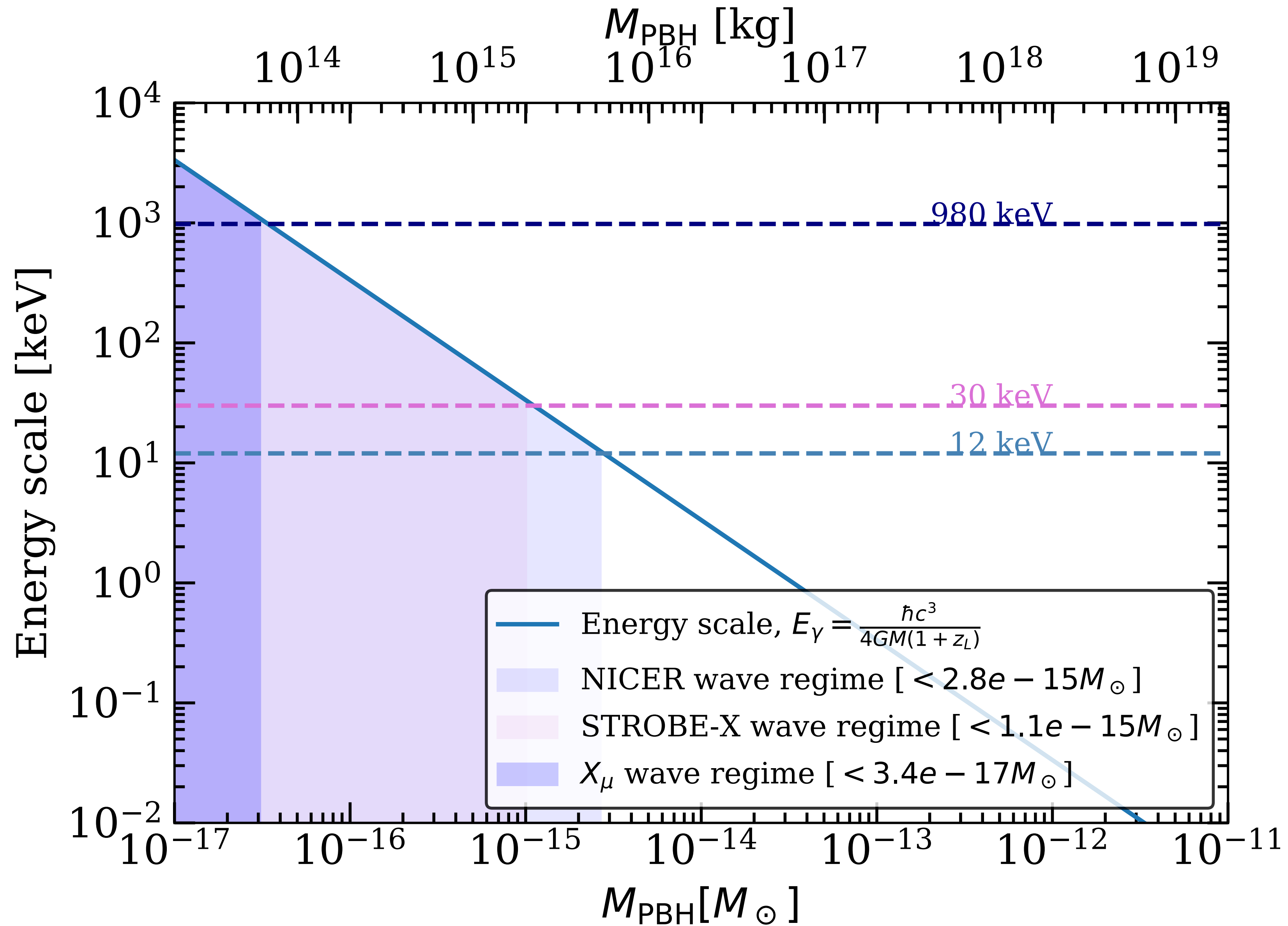
Take Home

- Primordial black holes (PBHs) in the mass range $10^{-16} - 10^{-11}M_{\odot}$ may constitute 100% dark matter.
- **WO microlensing of bright x-ray pulsars provide the most robust and immediately implementable opportunity to uncover PBH dark matter.**
- **NICER telescope can probe this window near $10^{-14}M_{\odot}$ with just two months of exposure on the x-ray pulsar SMC-X1!**
- **PBH evaporation limit at around $10^{-16}M_{\odot}$, may be probed with a minimal microlensing setup involving hard x-ray pulsars!**



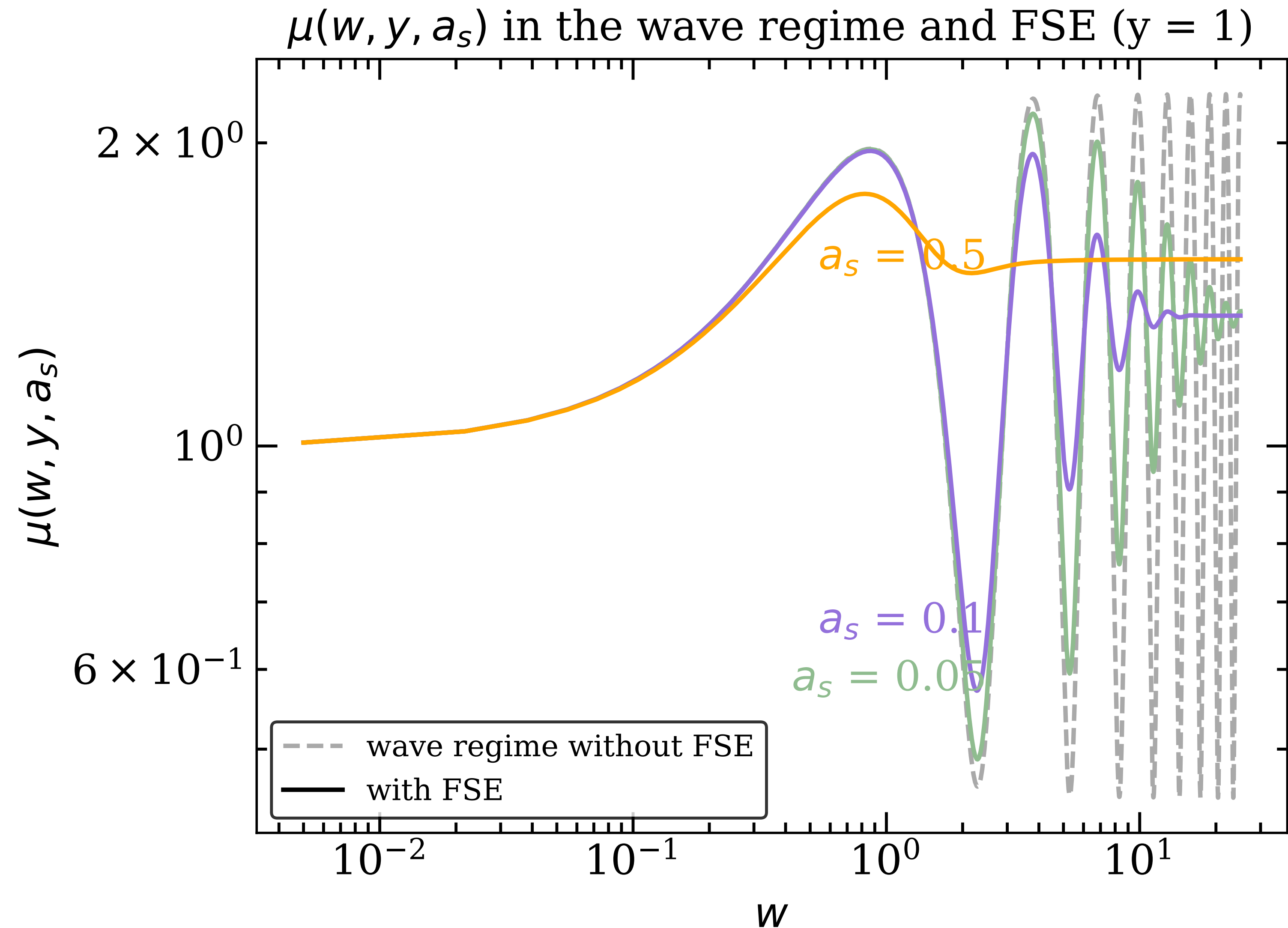
TOM GAULD for NEW SCIENTIST

Thank you for listening :)



**PBH masses
that can be
probed**

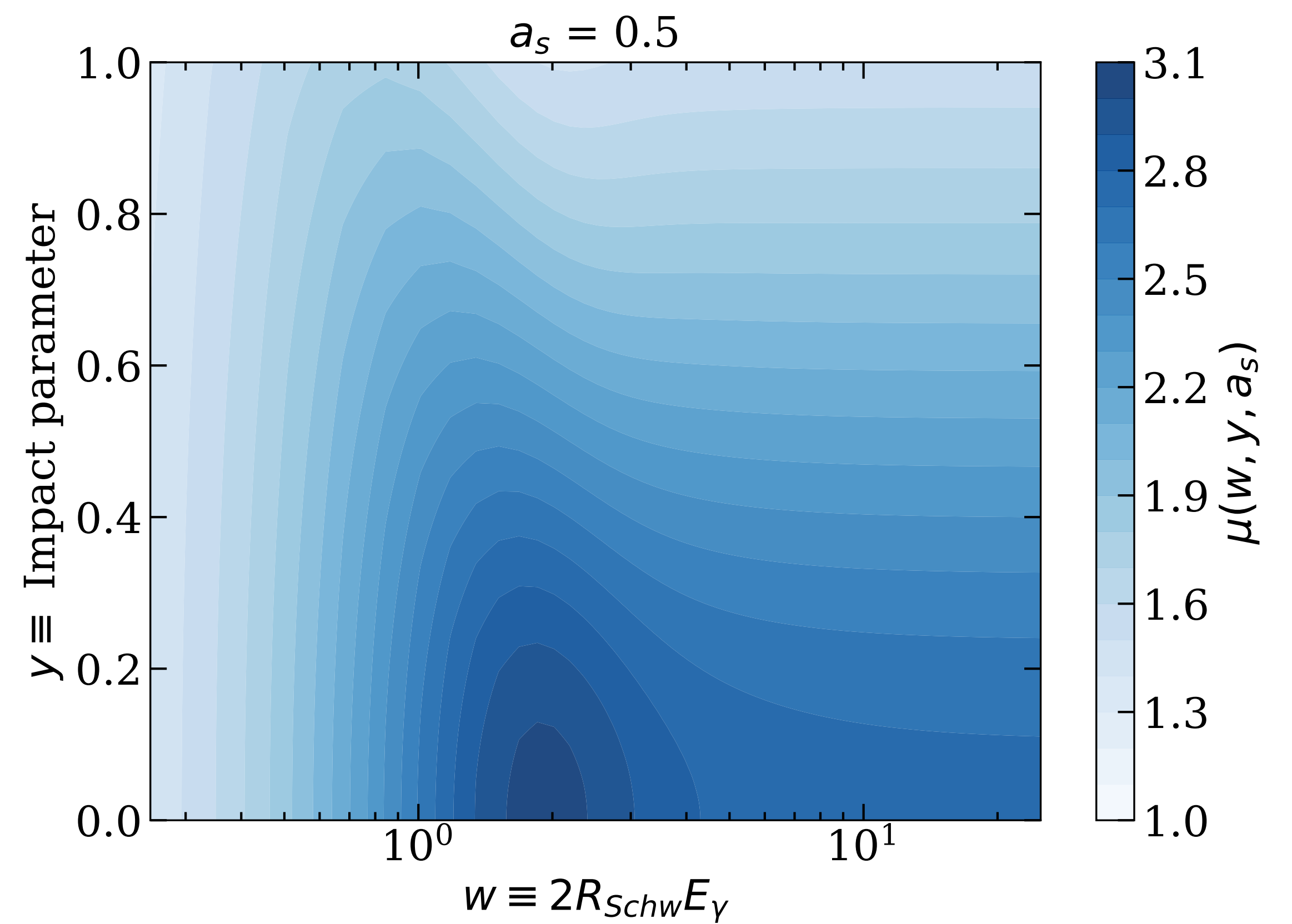
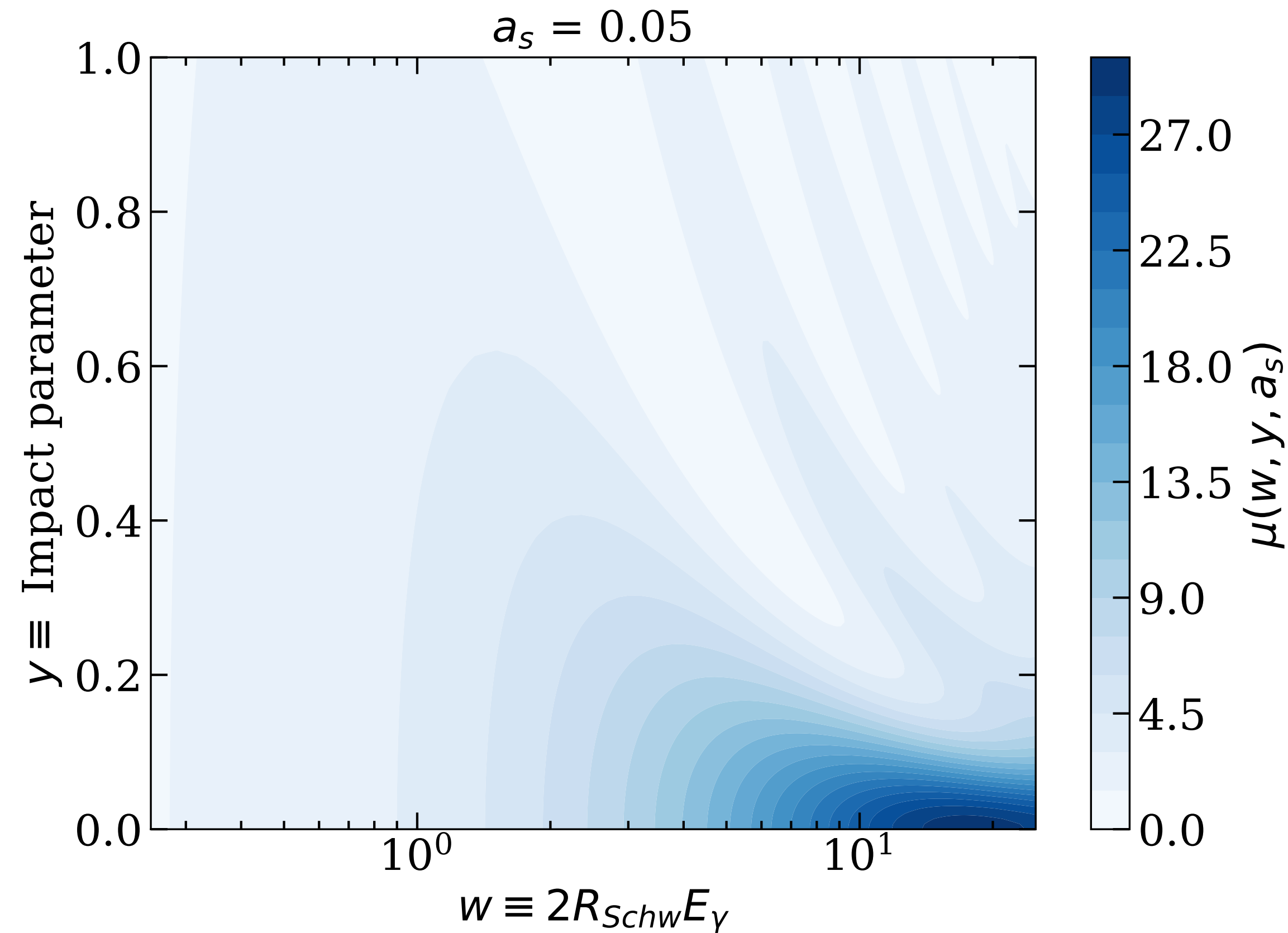
Buffer slides: Frequency dependent magnification



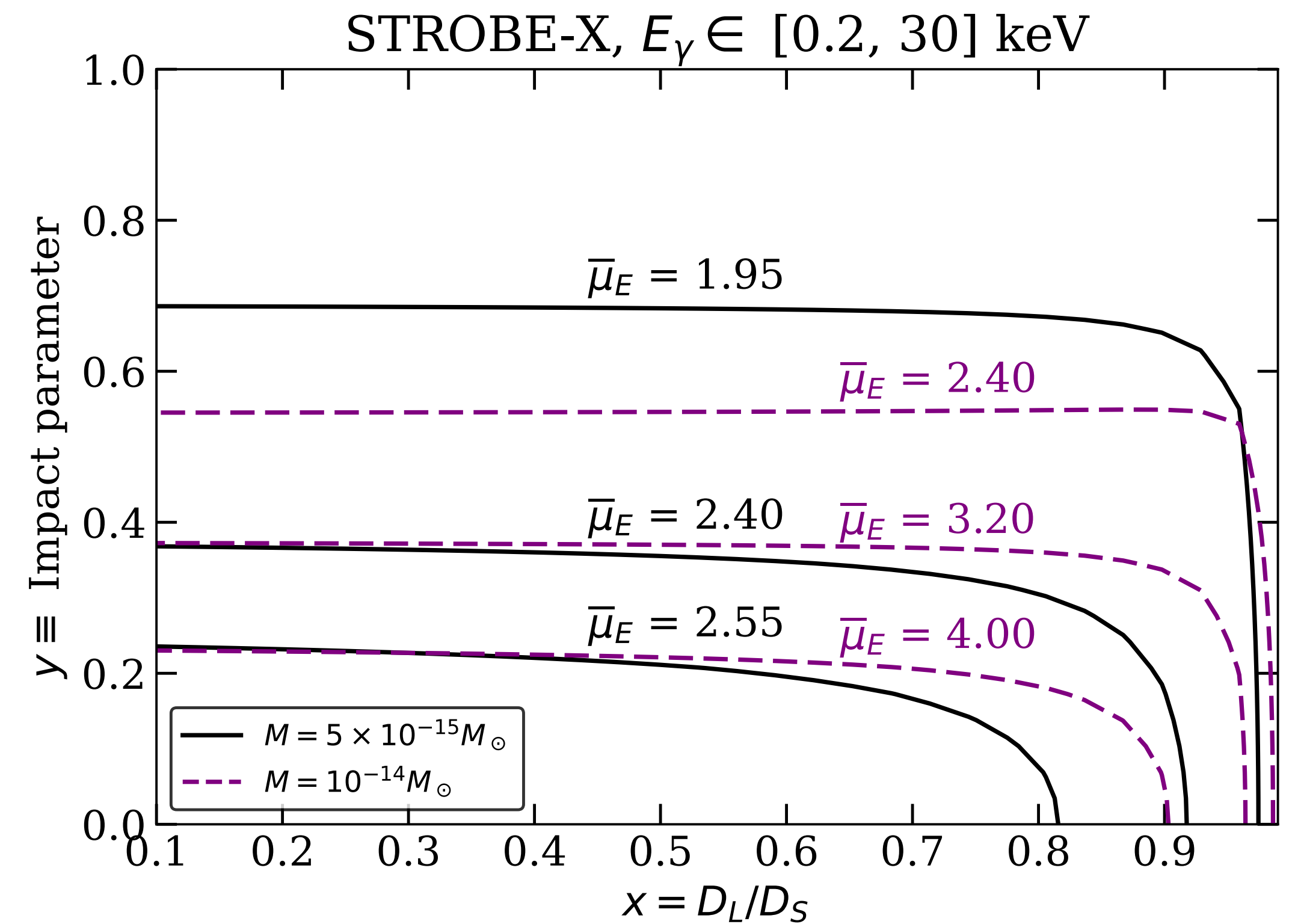
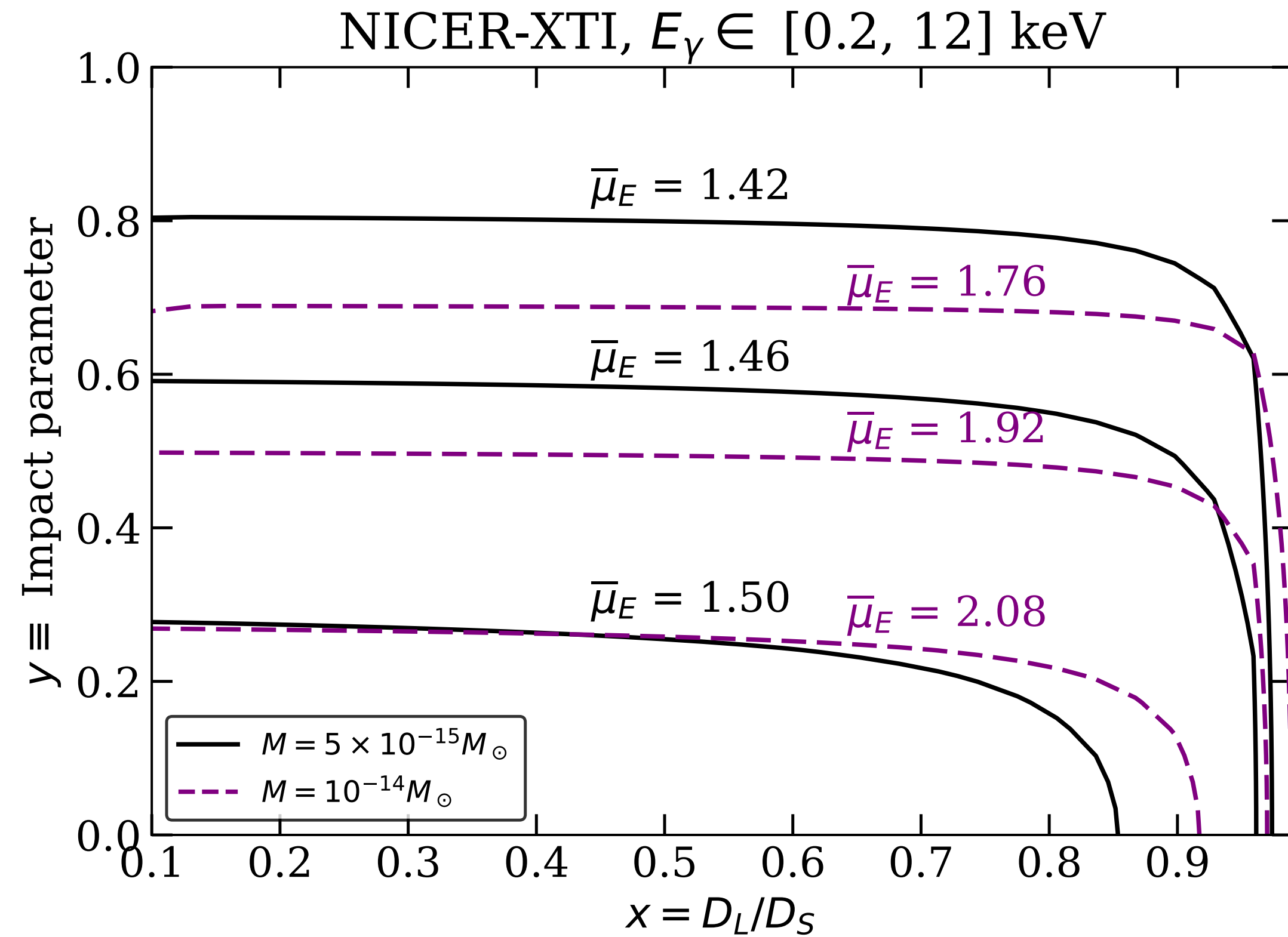
Microlensing magnification
in the wave regime
+
finite extent of the source

$$a_s = \frac{xR_s}{r_E}$$

Buffer slides: Magnification factor $\mu(w, y, a_s(x))$ in w-y space



Buffer slides: Detector and pulsar specific energy averaged magnification



Buffer slides: Statistical way of interpreting X-ray pulsar light curve

Threshold magnification:

$$\mu_{thresh} = \frac{1 + N_{\sigma}\sigma_B/B}{1 + n_{\sigma}\sigma_B/B}$$

Detection criterion:

$$\bar{\mu}_E \gtrsim \mu_{thresh}$$

$N_{\sigma} - N_{consec}$ criterion:

$N_{\sigma} = 3$ and $N_{consec} = 3$ with $n_{\sigma} = -1$ are optimal choices.

- Remark: $\mathbb{P}(n_{\sigma} = 0) = 0.13$; low event acceptance
- $\mathbb{P}(n_{\sigma} = -1) = 0.596$; optimal yet significant choice
- $\mathbb{P}(n_{\sigma} = -2) = 0.93$; too aggressive choice

Buffer slides: Condition for time binning of light curve

- Killing the Look elsewhere effect

$$\mathbb{P}(N_\sigma) < \frac{t_{\text{bin}}}{t_{\text{exp}}}$$

$$\mathbb{P}(N_\sigma) = [1 - \Phi(N_\sigma = 3)]^{N_{\text{consec}}=3} = 2.5 \times 10^{-9}$$

$$\frac{t_{\text{bin}}}{t_{\text{exp}}} = 1.9 \times 10^{-8} \left(\frac{t_{\text{bin}}}{0.1 \text{ s}} \right) \left(\frac{60 \text{ days}}{t_{\text{exp}}} \right)$$