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(Assisted) baryon number violation

$$
\Gamma(p \to e^+ \pi^0) \simeq \frac{1}{2 \times 10^{34} \, {\rm yr}} \left| \frac{y_{1111}^j}{(3 \times 10^{15} \, {\rm GeV})^{-2}} \right|^2
$$

Assuming perturbative couplings to 'X' particle Quark level dim-6

$$
s_{6} = y_{abcd}^{1} \epsilon^{\alpha\beta\gamma} (\overline{d}_{a,\alpha}^{C} u_{b,\beta}) (\overline{Q}_{i,c,\gamma}^{C} \epsilon_{ij} L_{j,d}) + y_{abcd}^{2} \epsilon^{\alpha\beta\gamma} (\overline{Q}_{i,a,\alpha}^{C} \epsilon_{ij} Q_{j,b,\beta}) (\overline{u}_{c,\gamma}^{C} \ell_{d}) + y_{abcd}^{3} \epsilon^{\alpha\beta\gamma} \epsilon_{il} \epsilon_{jk} (\overline{Q}_{i,a,\alpha}^{C} Q_{j,b,\beta}) (\overline{Q}_{k,c,\gamma}^{C} L_{l,d}) + y_{abcd}^{4} \epsilon^{\alpha\beta\gamma} (\overline{d}_{a,\alpha}^{C} u_{b,\beta}) (\overline{u}_{c,\gamma}^{C} \ell_{d}) + \text{h.c.} ,
$$

Effective operators: quark level….assuming perturbative new physics

Neutron-Antineutron Oscillation Search using a 0.37 Megaton Year Exposure of Super-Kamiokande

- As a BNV process that violate both B and B-L, neutron-antineutron oscillation provides a unique probe of baryon number violation
- Most of the models predicting $n \bar{n}$ correspond to energy scales of $10^2 - 10^3$ TeV, well above the scales that can be probed by accelerators

$$
\mathcal{L}=i\bar{n}\gamma^{\mu}\partial_{\mu}n-\frac{m_{n}}{2}\Big[\bar{n}\langle
$$

K. Abe et al. (Super-Kamiokande Collaboration) Phys. Rev. D 103, 012008 - Published 21 January 2021

BNV with suppressed proton decay in 4 dimensions : at high scale

The only leptoquark and diquark models with a triplet or sextet color structure that do not suffer from tree-level proton decay. The primes indicate the existence of dim 5 proton decay channels.

Phys. Rev. D 87, 075004 Jonathan M. Arnold, Bartosz Fornal and Mark B. Wise Physics Letters B 777 (2018) 324-331 Nima Assad, Bartosz Fornal*, Benjamín Grinstein

Possible interaction terms between the scalars

Possible vector color triplet and sextet representations.

• In the light of null results from $\Delta B=1$ searches, the possibility of discovering *neutron-antineutron* oscillations has recently gained increased interest

$$
2.5 \text{ TeV} \left(\frac{10^8 \text{ TeV}}{\Lambda} \right)^{1/4} \gtrsim 90 \text{ TeV}
$$

• Though tree-level proton decay is absent, there q could be dim-5 operator that leads to protondecay.

vector leptoquark representations $(3, 1)_{\frac{2}{3}}$ and $(3, 3)_{\frac{2}{3}}$

$$
\frac{1}{\Lambda} \, (\overline{Q_L^c} H^{\dagger}) \gamma^{\mu} d_R V_{\mu} \, , \quad \frac{1}{\Lambda} \, (\overline{Q_L^c} \tau^A H^{\dagger}) \gamma^{\mu} d_R V_{\mu}^A \, , \qquad \qquad \text{Pro}
$$

Process mediating $n - \bar{n}$ oscillations via the vector diquark (6, 2) $\frac{1}{\epsilon}$

Physics Letters B 777 (2018) 324–331 Nima Assad, Bartosz Fornal*, Benjamín Grinstein

$$
\left\{\begin{array}{c}\n\star^{(H)} \\
\hline\nV\n\end{array}\right\}
$$
\n
$$
\tau_p \approx (2.5 \times 10^{32} \text{ years}) \left(\frac{M}{10^4 \text{ TeV}}\right)^4
$$

ton decay through a dimension five interaction

• This operator does not exist if we gauge $U(1)_{B-L}$.

BNV with suppressed proton decay in 4 dimensions : at high scale

Vectors:

KEK Preprint 2016-21 (HYPER-KAMIOKANDE design report)

- With the next generation of experiments with higher sensitivity probing even further, the New Physics models would require further complicated structures.
- There exists two phenomena that lack clear evidence in terrestrial experiments
	- A. Baryon number violation
	- B. Dark Matter
- Its curious to wonder whether both are connected. Does Dark Matter act as a catalyst for BNV ?

PHYSICAL REVIEW D 84, 096008 (2011) Hooman Davoudiasl,^{1,*} David E. Morrissey,^{2,†} Kris Sigurdson,^{3,‡} and Sean Tulin^{2,§} **(Assisted/induced) baryon number violation**

as
$$
\tau^{-1} = n_{DM}(\sigma v)_{IND}
$$
 where $n_{DM} = \rho_{DM}/(m_{\psi} + m_{\psi})$

$$
\tau_N^{-1} \approx (10^{32} \text{ yrs})^{-1} \times \left(\frac{\rho_{DM}}{0.3 \text{ GeV/cm}^3}\right) \left(\frac{(\sigma v)_{IND}}{10^{-39} \text{ cm}^3/\text{s}}\right)
$$

$$
(\sigma v)_{IND} \approx 10^{-39} \text{ cm}^3/\text{s} \times \left(\frac{\Lambda_{IND}}{1 \text{ TeV}}\right)^{-6}
$$

Asymmetric Dark Matter

• Effective induced BNV lifetime can be defined

$$
\mathscr{L}_{\rm eff}\sim \frac{1}{\Lambda^3}\,u_R^i d_R^j d_R^k \Psi_R \Phi
$$

(Assisted) baryon number violation from 4k+2 dimensions

• Clifford Algebra in 4k+2 dimensions

- This is unlike in 4k dimensions.
- Thus the fermion representation and its charge conjugate must satisfy the same Weyl condition

Phys. Rev. D 109 (2024) 9, 095039 Akshay and **MTA**

$$
\{\Gamma_M, \Gamma_N\} = 2\eta_{MN}
$$

\n
$$
\Gamma^{4k+3} = \alpha \Gamma^0 \Gamma^1 \Gamma^2\Gamma^{4k+1}
$$

\n
$$
P_{\pm} = \frac{1}{2} (1 \pm \Gamma^{4k+3}) \qquad \psi_{\pm} = P_{\pm} \psi
$$

\n
$$
\psi^c = C\psi \equiv (C\Gamma^0)\psi^*
$$

\n
$$
\Gamma^M = -(C\Gamma^0)\Gamma^{M*}(C\Gamma^0)^{-1}
$$

\n
$$
= -C(\Gamma^M)^T C^{-1}.
$$

\n
$$
\sqrt{[C\Gamma^0, \Gamma^{4k+3}]} = 0 \text{ in } 4k+2-\text{dimension}
$$

- Witten anomaly constrains the number of $SU(2)_W$ doublets to appear in multiples of 3
- Although non-vanishing reducible anomalies like $[SU(2)_W]$ ⁴, $[SU(3)_c]$ ² $[SU(2)_W]$ ²,
- candidate

Phys. Rev. D 109 (2024) 9, 095039 Akshay and **MTA**

 $[SU(2)_W]^{2}[U(1)_Y]^{2},...$ are manageable via Green-Schwarz mechanism, irreducible anomalies like $[SU(3)_c]^3[U(1)_Y]$ require the chiral assignment $Q_+, \mathcal{U}_-, \mathcal{D}_-$ for quarks and $L_\pm, \mathscr{E}_\mp, \mathscr{N}_\mp$ for leptons

• A combination of 5th and 6th component of the Hypercharge gauge boson becomes the Dark Matter

Some properties of six dimensions

Some properties of six dimensions

- $\Psi_{\pm} = \psi_{\pm l} f_l + \psi_{\pm r} f_r$
- This residual Σ^{45} generates a rotational invariance $U(1)_{45}$
- Interestingly, on orbifolding, the square T^2/Z_2 would break this $U(1)_{45}$ down to a Z_4 symmetry since its invariant under $\pi/2$ rotations.
- Under this generator, the fermions $\,\psi_{\pm l}$ are charged $\pm\,1/2$ and $\psi_{\pm r}$ are charged $\mp\,1/2$
- All the operators in this geometry should keep this symmetry preserved.
- Thus, on a square T^2/Z_2 the baryon and lepton number violating operators should satisfy the selection rule $\frac{3}{4}$ A $\frac{1}{4}$ A $\frac{1}{4}$ 2 $\Delta B \pm$ 2 $\Delta L = 0$ *mod* 4
- Other orbifolds like T^2/Z_3 , makes sure that proton decay along with other $\Delta B=2, \ \Delta L=2$ processes are also suppressed. Except for neutron-antineutron oscillation

Phys. Rev. D 109 (2024) 9, 095039 Akshay and **MTA**

• On compactifying on T^2 the Lorentz generators break to $\Sigma^{MN}\to \Sigma^{\mu\nu}$ and Σ^{45} and the fermions become

(Assisted) baryon number violation 6 dimensions

- operators are allowed.
- The gamma matrices are

$$
\Gamma^{\mu} = \gamma^{\mu} \otimes \sigma^{1} , \ \Gamma^{4} = \gamma^{5} \otimes \sigma^{1} , \ \Gamma^{4}
$$

$$
C = i\Gamma^{4}\Gamma^{2}\Gamma^{0}
$$

$$
= \gamma^{5}\gamma^{2}\gamma^{0} \otimes \sigma^{1}
$$

Phys.Rev.D 109 (2024) 9, 095039 Akshay and **MTA**

• Thus geometry plays a crucial role. But for generality, lets assume a simple T^2/Z_2 , in which all the

$\Gamma^5={\rm 1}\otimes\sigma^2\hspace{0.5cm} \Gamma^7=\Gamma^0\Gamma^1\Gamma^2\Gamma^3\Gamma^4\Gamma^5={\rm 1}\otimes\sigma^3\,.$ $[C\Gamma^0,\Gamma^7]=0$

(Assisted) baryon number violation 6 dimensions

• Model independent baryon number and lepton number violating operators in six-

dimensions are,

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(Assisted) baryon number violation on orbifolding to 4 dimensions

• After orbifolding, the operators with least number of KK-modes are $\Psi_{\pm}(x^\mu,x^4,x^5) = \frac{1}{R}\sum \left(\psi_{\pm l}^{(n,m)}(x^\mu) f_{\pm l}(x_4,x_5)\right)$

 $+ \; \psi_{\pm r}^{(n,m)}(x^\mu) f_{\pm r}(x_4,x_5) \Big) \; ,$

$$
\Delta B = 2 = \Delta L
$$
\n
$$
q_{+l}^{(0,0)}
$$
\n
$$
\frac{C_2^S}{\Lambda_4^8} (q_{+l}^{(0,0)T} \gamma^2 \gamma^0 \mathcal{U}_{-l}^{(1,0)})^2 (\mathcal{E}_{-l}^{T(1,0)} \gamma^2 \gamma^0 q_{+l}^{(0,0)})^2
$$
\n
$$
q_{\mu} \mathcal{E}_{-l}^{(1,0)}
$$
\n
$$
\frac{C_2^V}{\Lambda_4^8} (u_{-r}^{(0,0)T} \gamma^2 \gamma^0 \gamma^{\mu} \mathcal{D}_{-l}^{(1,0)})^2 (u_{-r}^{(0,0)T} \gamma^2 \gamma^0 \gamma_{\mu} \mathcal{E}_{-l}^{(1,0)}
$$

Phys.Rev.D 109 (2024) 9, 095039 Akshay and MTA

(Assisted) $\Delta B = 1$, $\Delta L = 1$ process

$$
\mathcal{O}_1 = \frac{C_1^S}{\Lambda_4^2} \left(q_{+l}^{(0,0)T} \gamma^2 \gamma^0 \mathcal{U}_{-l}^{(1,0)} \right) \left(\mathcal{E}_{-l}^{T(1,0)} \gamma^2 \gamma^0 q_{+l}^{(0,0)} \right) \n+ \frac{C_1^V}{\Lambda_4^2} \left(u_{-r}^{(0,0)T} \gamma^2 \gamma^0 \gamma^\mu \mathcal{D}_{-l}^{(1,0)} \right) \left(u_{-r}^{(0,0)T} \gamma^2 \gamma^0 \gamma_\mu \mathcal{E}_{-l}^{(0,0)T} \right)
$$

$$
C_{\text{AND}}O_{\text{AND}} = y_u y_e g_Y^2 \frac{C_1^S}{\Lambda_4^2} \frac{1}{M_{KK}^2} (q_{+l}^{T(0,0)} \gamma^2 \gamma^0 u_-^{(0)})
$$

$$
\times (e_{-r}^{T(0,0)} \gamma^2 \gamma^0 q_{+l}^{(0,0)}) V_B^{(1,0)} V_B^{(1,0)}
$$

$$
C_{p\rightarrow e} = y_u y_e g_Y^2 \frac{C_1^S}{16\pi^2 \Lambda_4^2} \left(\frac{M_s}{M_{KK}}\right)^4
$$

 $\mathcal{L}^{(1,0)}_{-l})$

 $\overline{}$

$$
\Gamma_{p\to e} = \frac{1}{2 \times 10^{34}} \left| \frac{C_{p\to e}}{(3 \times 10^{15} \text{ GeV})^{-2}} \right|^2
$$

Phys.Rev.D 109 (2024) 9, 095039 Akshay and MTA

$(A$ ssisted) $\Delta B = 2$, $\Delta L = 2$ process

$$
\mathcal{O}_2 = \frac{C_2^S}{\Lambda_4^8} (q_{+l}^{(0,0)T} \gamma^2 \gamma^0 \mathcal{U}_{-l}^{(1,0)})^2 (\mathcal{E}_{-l}^{T(1,0)} \gamma^2 \gamma^0 q_{+l}^{(0,0)})^2
$$

$$
+\frac{\mathcal{C}_2^{\gamma}}{\Lambda_4^8} (u_{-r}^{(0,0)T}\gamma^2\gamma^0\gamma^{\mu}\mathcal{D}_{-l}^{(1,0)})^2 (u_{-r}^{(0,0)T}\gamma^2\gamma^0\gamma_{\mu}\mathcal{E}_{-l}^{(1,0)})^2
$$

$$
C_{\text{ANNA}} \mathcal{O}_{\text{ANNA}} = y_u^2 y_e^2 g_Y^4 \frac{C_2^S}{\Lambda_4^8 M_{KK}^4} (q_{+l}^{(0,0)T} \gamma^2 \gamma^0 u_{-r}^{(0,0)})^2
$$

$$
\times (e_{-r}^{T(0,0)} \gamma^2 \gamma^0 q_{+l}^{(0,0)})^2 V_B^{(1,0)} V_B^{(1,0)} V_B^{(1,0)} V_B^{(1,0)}
$$

$DM + p \rightarrow DM + \bar{p} + e^+ + e^+$

$$
\mathcal{O}_{VVppee} = \frac{1}{(\Lambda_{VVppee})^4} (\bar{p}^c p)(\bar{e}^c e) V_B^{(1,0)} V_B^{(1,0)}
$$

$$
\tau_{\text{ANNA}} = 5 \times 10^{33} \text{years} \left(\frac{\Lambda_{VVppee}}{300 \text{ GeV}}\right)^8
$$

Summary:

- Dark Matter being a catalyst to baryon number violation can be the reason for the rarity of events
- baryon number violation
- Interesting signatures would be positron fluxes from DM spikes

• Other places in the galaxy with higher Dark Matter density would be efficient regions to generate the required

Thank you

Dinucleon and Nucleon Decay to Two-Body Final States with no Hadrons in Super-Kamiokande

Super-Kamiokande Collaboration arXiv:1811.12430

The Super-Kamiokande (SK) water Cherenkov detector, with a fiducial volume of 22.5 kilotons, contains 1.2×10^{34} nucleons. SK lies one kilometer under Mt. Ikenoyama in Japan's Kamioka Observatory. The detector is cylindrical with a diameter of 39.3 meters and a height of 41.4 meters, optically separated into an inner and an outer region. Eight-inch photomultiplier tubes (PMTs) line the outer detector facing outwards and serve primarily as a veto for cosmic ray muons, and 20-inch PMTs face inwards to measure Cherenkov light in the inner detector $[12]$.

FIG. 1. (color online) An SK event display of a typical $pp \rightarrow$ $e^+ \mu^+$ event shown in θ - ϕ view. The non-showering ring (from the μ^+) is on the left and the showering ring (from the e^+) is on the right. The energy of each ring is approximately 900 MeV.

The following selection criteria are applied to signal MC, atmospheric ν MC, and data:

- $(A1)$ Events must be fully contained in the inner detector with the event vertex within the fiducial volume (two meters inward from the detector walls),
- $(A2)$ There must be two Cherenkov rings,
- (A3) Both rings must be showering for the $pp \rightarrow e^+e^+$, $nn \rightarrow e^+e^-, nn \rightarrow \gamma\gamma$ and $p \rightarrow e^+\gamma$ modes; one ring must be showering and one ring must be nonshowering for the $pp \to e^+\mu^+, nn \to e^+\mu^-, nn \to$ $e^{-}\mu^{+}$ and $p \to \mu^{+}\gamma$ modes; both rings must be non-showering for the $pp \rightarrow \mu^+\mu^+, nn \rightarrow \mu^+\mu^$ modes (see note in $[19]$),
- (A4) There must be zero Michel electrons for the $pp \rightarrow$ e^+e^+ , $nn \rightarrow e^+e^-$, $nn \rightarrow \gamma\gamma$ and $p \rightarrow e^+\gamma$ modes; there must be less than or equal to one Michel electron for the $pp \to e^+\mu^+, nn \to e^+\mu^-, nn \to e^-\mu^+$ and $p \to \mu^+ \gamma$ modes; there is no Michel electron cut for the $pp \to \mu^+\mu^+, nn \to \mu^+\mu^-$ modes (see note in $[20]$,
- $(A5)$ The reconstructed total mass, M_{tot} , should be $1600 \leq M_{tot} \leq 2050$ MeV/c² for the dinucleon decay modes; the reconstructed total mass should be 800 $\leq M_{tot} \leq 1050$ MeV/c² for the nucleon decay modes,
- $(A6)$ The reconstructed total momentum, P_{tot} , should be $0 \leq P_{tot} \leq 550$ MeV/c for the dinucleon decay modes; for the nucleon decay modes, it should be $100 \le P_{tot} \le 250$ MeV/c for the event to be in the "High P_{tot} " signal box and $0 \leq P_{tot} \leq 100 \text{ MeV/c}$ for the event to be in the "Low P_{tot} " signal box,
- (A7) [SK-IV nucleon decay searches only] There must be zero tagged neutrons.

	Lifetime limit	
Decay mode	per oxygen nucleus per nucleon	
	$(\times 10^{33} \text{ years})$ $(\times 10^{34} \text{ years})$	
$pp \rightarrow e^+e^+$	4.2	
$nn \rightarrow e^+e^-$	4.2	
$nn \rightarrow \gamma\gamma$	4.1	
$pp \rightarrow e^+ \mu^+$	4.4	
$nn \rightarrow e^+ \mu^-$	4.4	
$nn \rightarrow e^- \mu^+$	4.4	
$pp \rightarrow \mu^+\mu^+$	4.4	
$nn \rightarrow \mu^+ \mu^-$	4.4	
$p \rightarrow e^+ \gamma$		4.1
$p \rightarrow \mu^+ \gamma$		$2.1\,$

arXiv:1811.12430 (Dinucleon and Nucleon Decay to Two-Body Final States with no Hadrons in Super-Kamiokande)

KEK Preprint 2016-21
(HYPER-KAMIOKANDE design report)

TABLE IV. Parameters of past (KAM [114, 115]), running (SK [116, 117]), and future (HK-3TankLD and HK-1TankHD) water Cherenkov detectors. The KAM and SK have undergone several configuration changes and parameters for KAM-II and SK-IV are referred in the table. The single-photon detection efficiencies are products of the quantum efficiency at peak (\sim 400 nm), photo-electron collection efficiency, and threshold efficiency. Most right column (HK-1TankHD) shows another design under study which consist of one tank instrumented with high density PMTs.

fermions given by,

$$
\mathcal{L}_S = y^{(+-)} \bar{\mathcal{Q}}^C{}_+ S_2 \mathcal{E}_- + z^{(-+)} \bar{\mathcal{U}}^C{}_-(DQ_2) \mathcal{Q}_+ + h.c., \tag{38}
$$

where $y^{(+-)}$ and $z^{(-+)}$ are complex 3 × 3 Yukawa coupling matrices.

Vector LeptoQuark and Scalar Diquark

The interaction of the vector LeptoQuark and scalar Diquark with the fermions given as,

$$
\mathcal{L}_{SV} = z^{(-+)}U^{C}{}_{-}(DQ_{2})\mathcal{Q}_{+} + w^{(++)}\bar{\mathcal{Q}}^{C}{}_{+}\Gamma^{M}V_{3M}L_{+} + h.c., \qquad (39)
$$

where the V_{3M} is the vector triplet LeptoQuark and the DQ_2 is the scalar Diquark doublet.

Scalar LeptoQuark and Vector Diquark

The coupling of the scalar LeptoQuark and vector Diquark with the fermions is:

$$
\mathcal{L}_{VS} = y^{(+-)} \bar{\mathcal{Q}}^C{}_+ S_2 \mathcal{E}_- + x^{(++)} \bar{\mathcal{Q}}^{C}{}^a{}_+ \Gamma^M \epsilon^{ab} D Q_{3M} \mathcal{Q}^b_+ + h.c., \tag{40}
$$

Vector LeptoQuark and Vector Diquark

The interaction becomes,

$$
\mathcal{L}_{VV} = x^{(++)} \bar{\mathcal{Q}}^{C}{}_{+}^{a} \Gamma^{M} \epsilon^{ab} DQ_{3M} \mathcal{Q}_{+}^{b} + w^{(++)} \bar{\mathcal{Q}}^{C}{}_{+} \Gamma^{M} V_{3M} L_{+} + h.c., \tag{41}
$$

where the V_{3M} , DQ_{3M} are the triplet vector Leptoquark and Diquark.

Scalar LeptoQuark and Scalar Diquark

The Lagrangian for the singlet LeptoQuark S_2 $(\bar{3}, 2, \frac{5}{3})$ and singlet Diquark $DQ_2(\bar{3}, 2, -\frac{5}{3})$ interactions with the