

Study of exclusive decays of $B_s \rightarrow \psi(1S,2S)K_s$ and $B_s \rightarrow \eta_c(1S,2S)K_s$ in the framework of Relativistic Independent Quark Model

(Based on- arXiv:2404.14267v2 [hep-ph])

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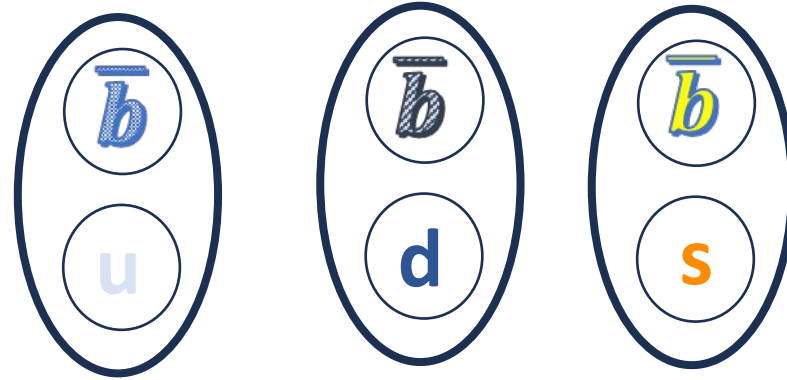
భారతీయ సాంకేతిక విజ్ఞాన సంస్థ హైదరాబాద్
भारतीय प्रौद्योगिकी संस्थान हैदराबाद
Indian Institute of Technology Hyderabad



Outline

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Introduction



- Heavy $\sim (5-6)$ GeV
- Long lifetime ~ 1.5 ps.
- B mesons decay via weak interactions
- Involve in flavor changing processes
- CP violating effects

Motivation

- B_s meson is involved in rare decay processes.
- The B_s mesons show the effect of mixing.
- This oscillation from matter to antimatter can be used to measure fundamental parameters of the Standard Model.
- In addition, it is closely related to CP violation and might have far reaching effects, such as the matter-antimatter asymmetry observed in the universe.
- $B_s \rightarrow J/\psi K_s$ is used as the control channel to handle phase shift $\Delta\phi_d$.
- The decay $B_d \rightarrow J/\psi K_s$ is considered as the "golden mode" for measuring the CKM angle $\sin 2\beta$.
- The decay $B_s \rightarrow J/\psi K_s$ is related to $B_d \rightarrow J/\psi K_s$ through the U-spin symmetry of strong interaction.

Literature

Extracting γ from $B(s/d) \rightarrow J/\psi K_S$ and $B(d/s) \rightarrow D^+(d/s)D^-(d/s)$

#6

Robert Fleischer (CERN) (Mar, 1999)

Published in: *Eur.Phys.J.C* 10 (1999) 299-306 • e-Print: [hep-ph/9903455](#) [hep-ph]

Penguin Effects in $\phi_{d,s}$ Determinations

#1 citations

Robert Fleischer (NIKHEF, Amsterdam and Vrije U., Amsterdam) (Dec, 2012)

Contribution to: CKM 2012 • e-Print: [1212.2792](#) [hep-ph]

A Roadmap to Control Penguin Effects in $B_d^0 \rightarrow J/\psi K_S^0$ and $B_s^0 \rightarrow J/\psi \phi$

#1

Full text search

↻ 8 citations

Kristof De Bruyn (NIKHEF, Amsterdam), Robert Fleischer (NIKHEF, Amsterdam and Vrije U., Amsterdam) (Dec 21, 2014)

Published in: *JHEP* 03 (2015) 145 • e-Print: [1412.6834](#) [hep-ph]

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↻ 93 citations

Literature

Observation of $B_s^0 \rightarrow J/\psi K^{*0}(892)$ and $B_s^0 \rightarrow J/\psi K_S^0$ Decays

CDF Collaboration • T. Aaltonen (Helsinki Inst. of Phys.) [Show All\(514\)](#)

Feb. 2011

Measurement of the $B_s^0 \rightarrow J/\psi K_S^0$ branching fraction

LHCb Collaboration • R Aaij (NIKHEF, Amsterdam) [Show All\(596\)](#)

Measurement of the time-dependent CP asymmetries in $B_s^0 \rightarrow J/\psi K_S^0$

LHCb Collaboration • Roel Aaij (NIKHEF, Amsterdam) [Show All\(703\)](#)

Measurement of the effective $B_s^0 \rightarrow J/\psi K_S^0$ lifetime

LHCb Collaboration • R Aaij (NIKHEF, Amsterdam) [Show All\(632\)](#)

Apr 16, 2013

arXiv:2201.04499 [hep-ex] (2022) 82:499

<https://doi.org/10.1140/epjc/s10052-022-10315-y>

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PHYSICAL JOURNAL C

Regular Article - Experimental Physics

Observation of $B^0 \rightarrow \psi(2S)K_S^0 \pi^+ \pi^-$ and $B_s^0 \rightarrow \psi(2S)K_S^0$ decays

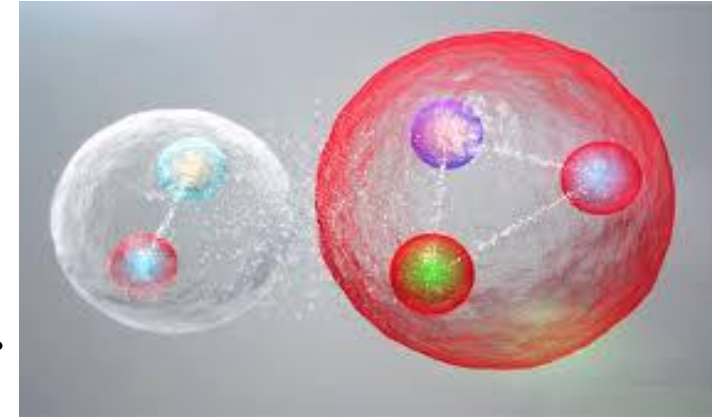
CMS Collaboration*

CERN, 1211 Geneva 23, Switzerland

Relativistic Independent Quark(RIQ) Model

- ❑ *In this model a hadron is considered as a colour singlet core of relativistic independent quark and antiquark, surrounded by cloud of pions.*
- ❑ *The quark constituents in this model are believed to interact with the potential in the form :*

$$U(r) = \frac{1}{2} (1 + \gamma_0)(ar^2 + V_0)$$



- ❑ *The potential represents phenomenologically the confining interaction expected in QCD to be generated by non-perturbative multigluon mechanism.*

We incorporate this interaction potential in the lagrangian density to obtain in the form :

$$\mathcal{L} = \overline{\psi}_q \left[\frac{1}{2} i \gamma^\mu \partial_\mu - U(r) - m_q \right] \psi_q(r)$$

The Dirac Equation:

$$(\boldsymbol{\alpha} \cdot \mathbf{p} + \beta m_q + U(r)) \psi_q(\mathbf{r}) = E \psi_q(\mathbf{r})$$

where, $\boldsymbol{\alpha} = \frac{\gamma_i}{\gamma_0}$ and $\beta = \gamma_0$

Solving the Dirac equations we get positive and negative energy solutions known as quark and antiquark orbitals respectively in the general form:

$$\psi_{nlj}^+(\vec{r}) = \begin{pmatrix} \frac{ig_{nlj}(r)}{r} \\ (\vec{\sigma} \cdot \hat{r}) \frac{f_{nlj}(r)}{r} \end{pmatrix} \varphi_{ljm_j}(\hat{r}) \quad \psi_{nlj}^-(\vec{r}) = \begin{pmatrix} i\vec{\sigma} \cdot \hat{r} \frac{f_{nlj}(r)}{r} \\ g_{nlj}(r)/r \end{pmatrix} (-1)^{j+m_j-l} \varphi_{ljm_j}(\hat{r})$$

Where ,

$$g_{nlj}(r) = N_q \left(\frac{r}{r_{nl}} \right)^{l+1} e^{-r^2/2r_{nl}^2} L_{n-1}^{l+1/2} \left(\frac{r^2}{r_{nl}^2} \right)$$

$$\text{and } f_{nlj}(r) = -N_q \frac{1}{r_{nl}\lambda_{nl}} \left(\frac{r}{r_{nl}} \right)^{l+2} e^{-r^2/2r_{nl}^2} \left[L_{n-2}^{l+3/2} \left(\frac{r^2}{r_{nl}^2} \right) + L_{n-1}^{l+3/2} \left(\frac{r^2}{r_{nl}^2} \right) \right]$$

MOMENTUM PROBABILITY AMPLITUDE

- For $n=1$ and $l=0$ (ground state)

$$G_s(\vec{p}_s) = \frac{i\pi N_s}{2\alpha_s \lambda_s} \sqrt{\frac{(E_{p_s} + m_s)}{E_{p_s}}} (E_{p_s} + E_s) \exp\left(-\frac{\vec{p}_s^2}{4\alpha_s}\right)$$

$$\tilde{G}_b(\vec{p}_b) = \frac{i\pi N_b}{2\alpha_b \lambda_b} \sqrt{\frac{(E_{p_b} + m_b)}{E_{p_b}}} (E_{p_b} + E_b) \exp\left(-\frac{\vec{p}_b^2}{4\alpha_b}\right)$$

Using the momentum probability amplitudes for quarks and antiquarks we construct the momentum profile function for the meson state as:

$$\mathcal{G}_{B_s}(\vec{p}_b, \vec{p}_s) = \sqrt{\tilde{G}_b(\vec{p}_b) G_s(\vec{p}_s)}$$

MOMENTUM DISTRIBUTION
FUNCTION

MESON STATE AND MESON NORMALIZATION

The meson state at definite momentum \vec{P} and spin projection S_{B_s} is taken as:

$$|B_s(\vec{P}, S_{B_s})\rangle = \hat{\Lambda}_{B_s}(\vec{P}, S_{B_s}) |(\vec{p}_b, \lambda_b); (\vec{p}_s, \lambda_s)\rangle$$

$$\text{where } |(\vec{p}_b, \lambda_b); (\vec{p}_s, \lambda_s)\rangle = \tilde{b}_b^\dagger(\vec{p}_b, \lambda_b) \hat{b}_s^\dagger(\vec{p}_s, \lambda_s) |0\rangle$$

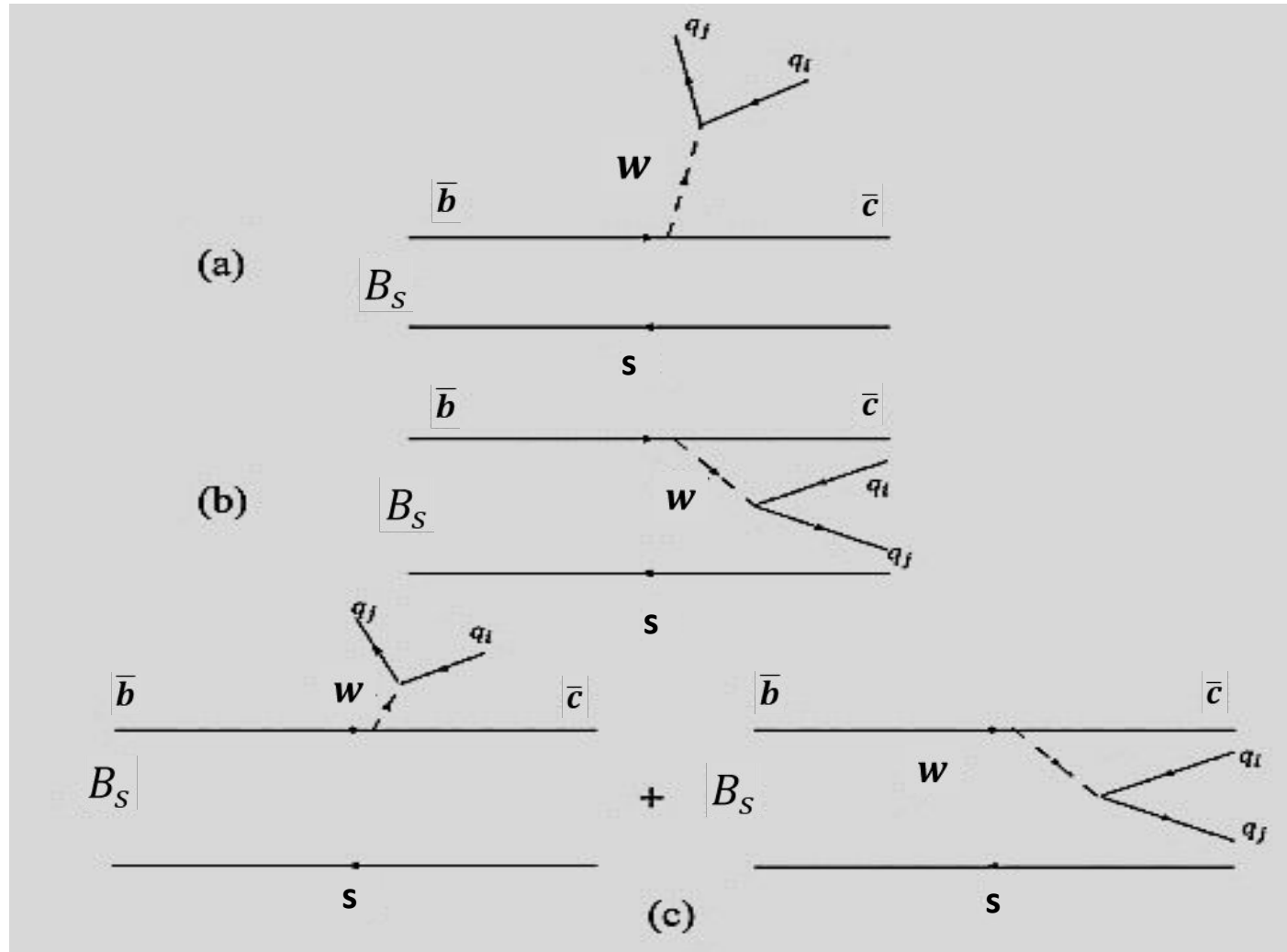
$$\hat{\Lambda}_{B_s}(\vec{P}, S_{B_s}) = \frac{\sqrt{3}}{\sqrt{N_{B_s}(\vec{P})}} \sum_{\delta_b, \delta_s} \zeta_{b,s}^{B_s}(\lambda_b, \lambda_s) \int d^3\vec{p}_b d^3\vec{p}_s \delta^{(3)}(\vec{p}_b + \vec{p}_s - \vec{P}) \mathcal{G}_{B_s}(\vec{p}_b, \vec{p}_s)$$

Imposing Normalisation condition

$$\langle B_s(\vec{P}') | B_s(\vec{P}) \rangle = \delta^3(\vec{P} - \vec{P}')$$

$$\text{Where } N(\vec{P}) = \int d^3\vec{p}_b |G(\vec{p}_b, \vec{P} - \vec{p}_b)|^2$$

FEYNMAN DIAGRAM



Class I

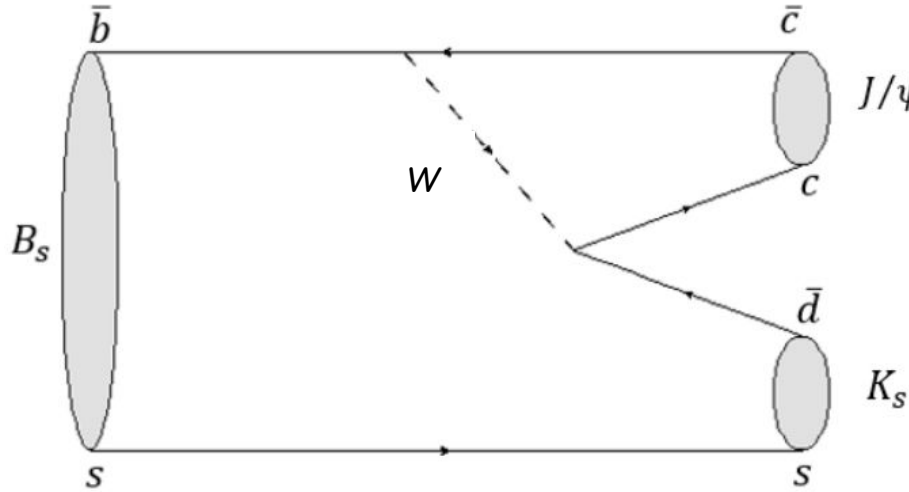


Class II



Class III

$B_s \rightarrow \psi(1S, 2S) K_s$ and $B_s \rightarrow \eta_c(1S, 2S) K_s$



$$\langle m_1 m_2 | \mathcal{H}_{\text{eff}} | M \rangle$$

$$= \frac{G_F}{\sqrt{2}} V_{q_1(2)q'_1(2)} V_{q_3q'_3} [a_1(\mu) \langle m_2 | J^\mu | 0 \rangle \langle m_1 | J_\mu | M \rangle + a_2(\mu) \langle m_1 | J^\mu | 0 \rangle \langle m_2 | J_\mu | M \rangle],$$

The nonvanishing part of the matrix elements of the current J^μ between the vacuum and final meson states in covariant form are parameterized by meson decay constants $f_{P,V}$

$$\langle P | \bar{q}'_i \gamma^\mu \gamma_5 q_j | 0 \rangle = i f_P p_P^\mu$$

$$\langle V | \bar{q}'_i \gamma^\mu q_j | 0 \rangle = e^{*\mu} f_V m_V$$

$$\langle P(p_P) | \bar{q}_c \gamma_\mu q_b | B_s(p) \rangle$$

$$= [(p + p_P)_\mu - \frac{M^2 - m_P^2}{q^2} q_\mu] F_1(q^2) + \frac{M^2 - m_P^2}{q^2} q_\mu F_0(q^2)$$

$$= (p + p_P)_\mu f_+(q^2) + (p - p_P)_\mu f_-(q^2),$$

FORM FACTOR EXPRESSION

$$f_{\pm}(q^2) = \frac{1}{2} \int d\vec{p}_b C(\vec{p}_b) \left\{ [E_b(\vec{p}_b) + m_b] [E_d(\vec{p}_b + \vec{k}) + m_d] + \vec{p}_b^2 \pm [E_b(\vec{p}_b) + m_b] [M \mp E_{P_1}] \right\}$$

$$C(\vec{p}_b) = \frac{\mathcal{G}_{B_s}(\vec{p}_b, -\vec{p}_b) \mathcal{G}_{K_s}(\vec{p}_b + \vec{k}, -\vec{p}_b)}{\sqrt{N_{B_s}(0) N_{K_s}(\vec{k})}}$$

$$\sqrt{\frac{[E_b(\vec{p}_b) + E_s(-\vec{p}_b)] [E_d(\vec{p}_b + \vec{k}) + E_s(-\vec{p}_b)]}{E_b(\vec{p}_b) E_d(\vec{p}_b + \vec{k}) [E_b(\vec{p}_b) + m_b] [E_d(\vec{p}_b + \vec{k}) + m_d]}}$$

DECAY WIDTH

$$B_s \rightarrow \eta_c K_s$$

$$\Gamma(B_s \rightarrow \eta_c K_s) = \frac{|\vec{k}|}{8\pi M^2} |A_1|^2 |F_0(q^2)|^2$$

$$|A_1| = \frac{G_F}{\sqrt{2}} V_{bc} V_{cd} a_2 (M^2 - m_{K_s}^2) f_{\eta_c}$$

$$F_0(q^2) = \left[\frac{q^2}{(M^2 - m_{K_s}^2)} \right] f_-(q^2) + f_+(q^2)$$

$$B_s \rightarrow J/\psi K_s$$

$$\Gamma(B_s \rightarrow J/\psi K_s) = \frac{|\vec{k}|^3}{8\pi m_{J/\psi}^2} |A_2|^2 |F_1(q^2)|^2$$

$$|A_2| = \frac{G_F}{\sqrt{2}} V_{bc} V_{cd} 2a_2 m_{J/\psi} f_{J/\psi}$$

$$F_1(q^2) = f_+(q^2) = \frac{1}{2} \int d\vec{p}_b C(\vec{p}_b)$$

$$\left\{ [E_b(\vec{p}_b) + m_b] [E_d(\vec{p}_b + \vec{k}) + m_d] + \vec{p}_b^2 + [E_b(\vec{p}_b) + m_b] [M - E_P] \right\}$$

Numerical Analysis

INPUT PARAMETERS

For ground state we take the quark masses, corresponding binding energies and potential parameters:

$$(a, V_0) \equiv (0.017166 \text{ GeV}^3, -0.1375 \text{ GeV})$$

$$m_d = 0.07875$$

$$E_d = 0.47125$$

$$m_s = 0.31575$$

$$E_s = 0.591$$

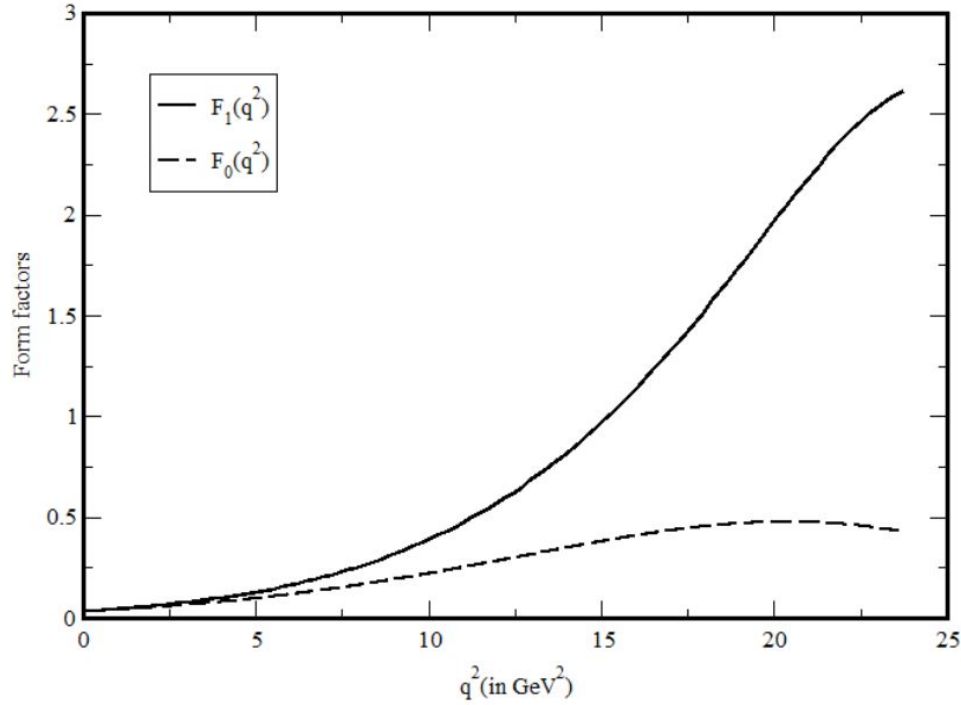
$$m_c = 1.49275$$

$$E_c = 1.57951$$

$$m_b = 4.77659$$

$$E_b = 4.76633$$

RESULTS



Decays	Our work	Exp. results
$B_s \rightarrow J/\psi K_s$	$2.023^{+0.325}_{-0.295}$	1.92 ± 0.14 [PDG]
$B_s \rightarrow \eta_c K_s$	$1.192^{+0.184}_{-0.162}$	-
$B_s \rightarrow \psi(2S) K_s$	$0.515^{+0.89}_{-0.506}$	$0.97 \pm 0.20(stat) \pm 0.03(syst)$ $\pm 0.22(\frac{f_s}{f_d})$ [CMS2022]
$B_s \rightarrow \eta_c(2S)$	$0.0573^{+0.0638}_{-0.0375}$	-

(BF in 10^{-5})

\mathcal{R}	Our Result	Exp. Result
$\frac{B(B_s \rightarrow J/\psi K_s)}{B(B_d \rightarrow J/\psi K_s)}$	$0.0454^{+0.006}_{-0.0057}$	$0.0431 \pm 0.0017(stat) \pm 0.0012(syst) \pm 0.0025$ [LHCb2015]
$\frac{B(B_s \rightarrow \psi(2S) K_s)}{B(B_d \rightarrow \psi(2S) K_s)}$	$0.0177^{+0.0269}_{-0.0173}$	$0.033 \pm 0.0069(stat) \pm 0.0011(syst)$ [CMS2022]

Summary

- The resulting BF's of $B_s \rightarrow \psi(1S,2S)K_s$ obtained from our work align with experimental results, as reported by the LHCb and CMS Collaboration.
- Our predictions for $B_s \rightarrow \eta_c(1S,2S)K_s$ will become a key reference for both experimentalists and theorists.
- To ensure thoroughness, additionally, we compute the ratio of BF of B_s to B_d for the same final states, $\psi(nS)$ with K_s .
- Our predictions in this analysis, achieved through a parameter-free unification within our model framework, aim to strengthen confidence in SM predictions and contribute to valuable discussions on the crucial B_s sector in flavor physics.

Thank You!

$$\begin{aligned} & \langle P(p_P) | \bar{q}_c \gamma_\mu q_b | B_s(p) \rangle \\ &= \left[(p + p_P)_\mu - \frac{M^2 - m_P^2}{q^2} q_\mu \right] F_1(q^2) + \frac{M^2 - m_P^2}{q^2} q_\mu F_0(q^2) \\ &= (p + p_P)_\mu f_+(q^2) + (p - p_P)_\mu f_-(q^2), \end{aligned}$$

$$f_+(q^2) = F_1(q^2)$$

$$f_-(q^2) = \frac{M^2 - m_P^2}{q^2} [F_0(q^2) - F_1(q^2)]$$

Numerical Analysis

INPUTS

Mesons	Mass(in MeV) ★	Decay constant (in MeV)
B_s	5366.92 ± 0.10	-
K_s	497.61 ± 0.013	-
J/ψ	3096.9 ± 0.006	$418 \pm 8 \pm 5$
η_c	2983.9 ± 0.04	$387 \pm 7 \pm 2$
$\psi(2S)$	3686.1 ± 0.06	143 ± 81
$\eta_c(2S)$	3637.7 ± 1.1	$56 \pm 21 \pm 3$

★ PDG 2022

★ "Radiative transitions in charmonium from lattice QCD," Phys. Rev. D 73 (2006) 074507, arXiv:hep-ph/0601137.

★ "Charmonia decay constants from the QCD lattice and QCD sum rules," Nucl. Part. Phys. Proc. 273-275 (2016) 1611–1617

MESON	MESON MASS (GeV)	
	<u>Prediction</u>	<u>Experiment</u>
$D^{\pm*}$	2.0149	2.0101
D^{\pm}	1.8538	1.8694
$D_S^{\pm*}$	2.0731	2.1103
D_S^{\pm}	1.9149	1.9690
$B^{\pm*}$	5.3292	5.3246
B^{\pm}	5.2643	5.2786
B_S^{0*}	5.3720	5.4256
B_S^0	5.3055	5.3786
$B_c^{\pm*}$	6.3142	-
B_c^{\pm}	6.2707	6.2749

Published by Barik and Dash
(i) *Phys.Rev.D* 33, 1925 (1986a)
(ii) *Pramana-J. Phys.*29(6), 543-557 (1987)