

New Physics effects in semileptonic $\bar{B}_s \rightarrow K^{*+} (\rightarrow K\pi) l^- \bar{\nu}_l$ decays

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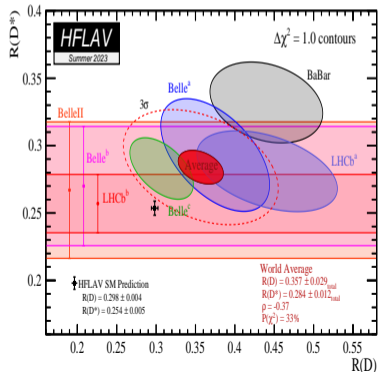
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Introduction

The semileptonic decays are interesting avenue to look for the New Physics beyond the Standard Model.

- Several analysis with New Physics have performed which can explain the observed discrepancy. (Very recent [arXiv 2405.06062](https://arxiv.org/abs/2405.06062))
- We analyzed the allowed New Physics constrained by the available $b \rightarrow ul\nu$ data.
- We aim to provide a comprehensive analysis of the $\bar{B}_s \rightarrow K^{*+} (\rightarrow K\pi) l^- \bar{\nu}_l$ decays process, focusing particularly on its sensitivity to NP effects.



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Effective Field Theory

The effective Hamiltonian for the transition governed by $b \rightarrow ul\nu$ is given by:

$$H_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{ub} \left[(1 + C_{V_L}) O_{V_L} + C_{V_R} O_{V_R} + C_{S_L} O_{S_L} + C_{S_R} O_{S_R} + C_T O_T \right],$$

where the operators are:

$$\begin{aligned} O_{V_L} &= (\bar{u}\gamma_\mu P_L b) (\bar{l}\gamma^\mu P_L \nu) \\ O_{V_R} &= (\bar{u}\gamma_\mu P_R b) (\bar{l}\gamma^\mu P_L \nu), \\ O_{S_R} &= (\bar{u}P_R b) (\bar{l}P_L \nu), \\ O_{S_L} &= (\bar{u}P_L b) (\bar{l}P_L \nu), \\ O_T &= (\bar{u}\sigma^{\mu\nu} P_L b) (\bar{l}\sigma_{\mu\nu} P_L \nu). \end{aligned}$$

We assume the lepton flavour universal NP couplings for light leptons ($l = \mu$ or e):

$$C_i^l = \frac{(C_i^e + C_i^\mu)}{2}.$$

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New Physics Constraints

We constraint the New Physics by the available $b \rightarrow ul\nu$ data :

- For the decay mode $\bar{B}^0 \rightarrow \pi^+ l^- \bar{\nu}$, we have utilized the globally averaged q^2 - binned branching ratio spectrum published by the HFLAV collaboration. [arXiv:2206.07501](https://arxiv.org/abs/2206.07501)
- We use the world average of the differential branching fractions in different q^2 bins for the decay $B \rightarrow \rho l\nu$ published by the HFLAV collaboration. [arXiv:2206.07501](https://arxiv.org/abs/2206.07501)
- We use the world average of the differential branching fractions in different q^2 bins for the decay $B \rightarrow \omega l\nu$ published by the HFLAV collaboration. [arXiv:2206.07501](https://arxiv.org/abs/2206.07501)
- The measurement of leptonic decay $B \rightarrow \mu\nu$ from Belle is also used to constraint the NP parameters. [arXiv:1911.03186](https://arxiv.org/abs/1911.03186)

New Physics contribution in $B \rightarrow Pl\nu$

The differential decay rate of semileptonic decay of $B \rightarrow P$ can be written in term of NP WCs as:

$$\begin{aligned} \frac{d\Gamma(B \rightarrow Pl\nu)/dq^2}{d\Gamma(B \rightarrow Pl\nu)^{SM}/dq^2} &= \left| 1 + C_{V_L}^l + C_{V_R}^l \right|^2 \left[\left(1 + \frac{m_l^2}{2q^2} \right) H_{V,0}^s + \frac{3}{2} \frac{m_l^2}{q^2} H_{V,t}^s \right] \\ &+ \frac{3}{2} |C_{S_L}^l + C_{S_R}^l|^2 H_S^s + 8 |C_T^l| \left(1 + \frac{2m_l^2}{q^2} \right) H_T^s \\ &+ 3 \operatorname{Re}[(1 + C_{V_L}^l + C_{V_R}^l) (C_{S_L}^{l*} + C_{S_R}^{l*})] \frac{m_l}{\sqrt{q^2}} H_S^s H_{V,t}^s \\ &- 12 \operatorname{Re}[(1 + C_{V_L}^l + C_{V_R}^l) C_T^{l*}] \frac{m_l}{\sqrt{q^2}} H_T^s H_{V,0}^s \end{aligned}$$

Hadronic matrix elements can be written in terms of Form Factors which have been determined by using combined LCSR + Lattice fit. [[arXiv:1205.6245](https://arxiv.org/abs/1205.6245), [1911.03186](https://arxiv.org/abs/1911.03186)]

New Physics contribution in $B \rightarrow V l \nu$

Similarly for $B \rightarrow V$ can be written in terms of NP WCs as :

$$\begin{aligned}
 \frac{d\Gamma(B \rightarrow V l \nu)/dq^2}{d\Gamma(B \rightarrow V l \nu)^{SM}/dq^2} = & \left(|1 + C_{V_L}^l|^2 + |C_{V_R}^l|^2 \right) \left[\left(1 + \frac{m_l^2}{2q^2} \right) (H_{V,+}^2 + H_{V,-}^2 + H_{V,0}^2) + \frac{3}{2} \frac{m_l^2}{q^2} H_{V,t}^2 \right] \\
 & - 2 \operatorname{Re} \left[(1 + C_{V_L}^l) C_{V_R}^{l*} \right] \left[\left(1 + \frac{m_l^2}{2q^2} \right) (H_{V,0}^2 + 2H_{V,+} H_{V,-}) + \frac{3}{2} \frac{m_l^2}{q^2} H_{V,t}^2 \right] \\
 & + \frac{3}{2} |C_{S_R}^l - C_{S_L}^l|^2 H_S^2 + 8 |C_T^l| \left(1 + \frac{2m_l^2}{q^2} \right) (H_{T,+}^2 + H_{T,-}^2 + H_{T,0}^2) \\
 & + 3 \operatorname{Re} \left[(1 - C_{V_R}^l + C_{V_L}^l) (C_{S_R}^{l*} - C_{S_L}^{l*}) \right] \frac{m_l}{\sqrt{q^2}} H_S H_{V,t} \\
 & - 12 \operatorname{Re} \left[(1 + C_{V_L}^l) C_T^{l*} \right] \frac{m_l}{\sqrt{q^2}} (H_{T,0} H_{V,0} + H_{T,+} H_{V,+} - H_{T,-} H_{V,-}) \\
 & - 12 \operatorname{Re} \left[C_{V_R}^l C_T^{l*} \right] \frac{m_l}{\sqrt{q^2}} (H_{T,0} H_{V,0} + H_{T,+} H_{V,+} - H_{T,-} H_{V,-})
 \end{aligned}$$

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Methodology

- We perform the χ^2 analysis to constraints the NP parameter space and use MINUIT for the χ^2 analysis.

The χ^2 in our analysis is defined as :

$$\chi^2(C_i) = \sum_{m,n} \left(O^{th}(C_i) - O^{exp} \right)_m C_{mn}^{-1} \left(O^{th}(C_i) - O^{exp} \right)_n$$

where C_{mn}^{-1} is the covariance matrix which includes both experimental and theoretical uncertainties. O^{exp} and O^{th} are the experimental measurement and theoretical predictions, respectively.

- We consider the NP in 1D and 2D scenarios. The best fit values for the NP parameters are obtained by minimizing the χ^2 .
- We also get the allowed parameter space of new physics Wilson coefficients for 2-D scenarios based on $\Delta\chi^2$ values. ($\Delta\chi^2 = \chi^2 - \chi_{min}^2$)

Best fit of 1D New Physics Scenario

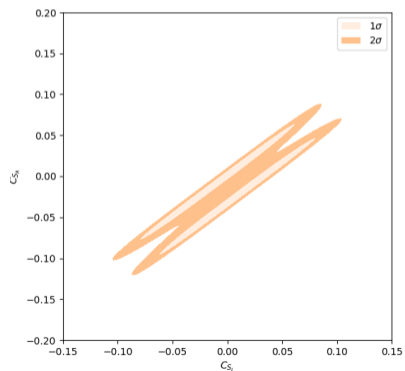
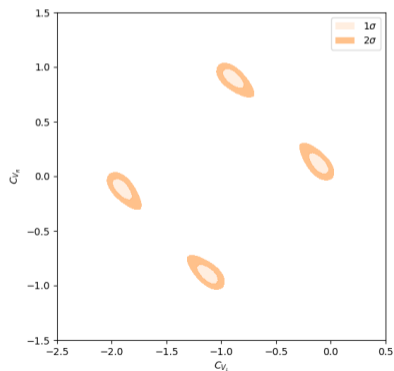
Scenarios	best fit point	χ^2_{min}
SM	-	24.34
S1 : C_{V_L}	-0.032(47)	23.87
S2 : C_{V_R}	0.069(47)	22.31
S3 : C_{S_L}	-0.003(4)	23.85
S4 : C_{S_R}	0.003(4)	23.85
S5 : C_T	0.005(49)	24.33
S6 : $C_{V_L} = -C_{V_R}$	-0.093(54)	20.61

Best fit of 2D New Physics Scenario

Scenarios	best fit point	χ^2_{min}
$S7 : (C_{V_L}, C_{V_R})$	S7a: $[-0.079(56), 0.115(62)]$	20.21
	S7b: $[-0.892(60), 0.928(56)]$	20.21
	S7c: $[-1.122(63), -0.928(57)]$	20.21
	S7d: $[-1.934(58), -0.115(62)]$	20.21
$S8 : (C_{V_L}, C_{S_L})$	$[-0.038(48), -0.003(4)]$	23.22
$S9 : (C_{V_L}, C_{S_R})$	$[-0.038(48), 0.004(4)]$	23,21
$S10 : (C_{V_L}, C_T)$	$[-0.032(47), 0.006(57)]$	23.85
$S11 : (C_{V_R}, C_{S_L})$	$[0.075(48), -0.004(4)]$	21.44
$S12 : (C_{V_R}, C_{S_R})$	$[0.075(48), 0.004(4)]$	21.46
$S13 : (C_{V_R}, C_T)$	$[0.068(48), 0.0007(50)]$	22.31
$S14 : (C_{S_L}, C_{S_R})$	$[0.008(121), 0.011(120)]$	23.85
$S15 : (C_{S_L}, C_T)$	$[-0.003(4), 0.005(49)]$	23.85
$S16 : (C_{S_R}, C_T)$	$[0.003(4), 0.005(49)]$	23.85
$S17 : (C_{V_L} = -C_{V_R}, C_{S_L} = -C_{S_R})$	$[-0.116(59), 0.015(2)]$	18.84

ALLOWED NEW PHYSICS PARAMETER SPACE

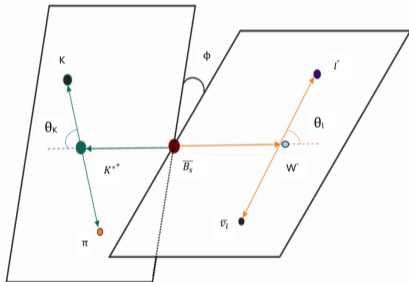
We plot the 1σ and 2σ contours in the 2-D WC's plane.



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Kinematics of $\bar{B}_s \rightarrow K^{*+}(\rightarrow K\pi)l^- \bar{\nu}_l$ decay

- In our work we provide comprehensive analysis of the $\bar{B}_s \rightarrow K^{*+}(\rightarrow K\pi)l^- \bar{\nu}_l$ decay.



The four body decays distribution for $\bar{B}_s \rightarrow K^{*+}(\rightarrow K\pi)l^- \bar{\nu}_l$ decay can be characterized by four kinematic variables : q^2 , θ_l , θ_{K^*} and ϕ .

Angular Distribution for $\bar{B}_s \rightarrow K^{*+} (\rightarrow K\pi) l^- \bar{\nu}_l$ decay

The four fold differential distribution for this decay is given by [arXiv: 1212.2231](https://arxiv.org/abs/1212.2231) :

$$\frac{d^4\Gamma}{dq^2 d\cos\theta_l d\cos\theta_{K^*} d\phi} = \frac{8\pi}{3} \left[(J_{1s} + J_{2s} + J_3 \cos 2\phi + J_{6s} \cos\theta_l + J_9 \sin 2\phi) + (J_{1c} + J_{2c}) + (J_4 \cos\phi + J_5 \sin\theta_l \cos\phi + J_7 \sin\theta_l \sin\phi + J_8 \sin\phi) J_{6c} \cos\theta_l \right]$$

Here $J_i(q^2)$ are the angular coefficient . These coefficients contains the form factors and are sensitive to different new physics.

- The angular coefficients can be written as:

$$J_{1s} = \frac{3}{16} \left[3|\mathcal{A}_\perp^L|^2 + 3|\mathcal{A}_\parallel^L|^2 + 16|\mathcal{A}_{0\parallel}|^2 + 16|\mathcal{A}_{t\perp}|^2 \right]$$

$$J_{1c} = \frac{3}{4} \left[|\mathcal{A}_0^L|^2 + 2|\mathcal{A}_t^L|^2 + 8|\mathcal{A}_{\parallel\perp}|^2 \right]$$

$$J_{2s} = \frac{3}{16} \left[|\mathcal{A}_\perp^L|^2 + |\mathcal{A}_\parallel^L|^2 - 16|\mathcal{A}_{0\parallel}|^2 - 16|\mathcal{A}_{t\perp}|^2 \right]$$

$$J_{2c} = -\frac{3}{4} \left[|\mathcal{A}_0^L|^2 - 8|\mathcal{A}_{\parallel\perp}|^2 \right]$$

$$J_3 = \frac{3}{8} \left[|\mathcal{A}_\perp^L|^2 - |\mathcal{A}_\parallel^L|^2 + 16|\mathcal{A}_{0\parallel}|^2 - 16|\mathcal{A}_{t\perp}|^2 \right]$$

$$J_4 = \frac{3}{4\sqrt{2}} \left[|\mathcal{A}_0^L| |\mathcal{A}_\parallel^L|^* - 8\sqrt{2} |\mathcal{A}_{\parallel\perp}| |\mathcal{A}_{0\parallel}|^* \right]$$

$$J_5 = \frac{3}{2\sqrt{2}} \text{Re} \left[|\mathcal{A}_0^L| |\mathcal{A}_\perp^L| + 2\sqrt{2} |\mathcal{A}_{0\parallel}| |\mathcal{A}_t^L|^* \right]$$

$$J_{6s} = \frac{3}{2} \text{Re} \left[|\mathcal{A}_\parallel^L| |\mathcal{A}_\perp^L|^* \right]$$

$$J_{6c} = -6 \text{Re} \left[|\mathcal{A}_{\parallel\perp}| |\mathcal{A}_t^L|^* \right]$$

$$J_7 = \frac{3}{2\sqrt{2}} \text{Im} \left[|\mathcal{A}_0^L| |\mathcal{A}_\parallel^L|^* - 2\sqrt{2} |\mathcal{A}_{t\perp}| |\mathcal{A}_t^L|^* \right]$$

$$J_8 = \frac{3}{4\sqrt{2}} \text{Im} \left[|\mathcal{A}_0^L| |\mathcal{A}_\perp^L|^* \right]$$

$$J_9 = \frac{3}{4} \text{Im} \left[|\mathcal{A}_\perp^L| |\mathcal{A}_\parallel^L|^* \right]$$

Observables in $\bar{B}_s \rightarrow K^{*+} (\rightarrow K\pi) l^- \bar{\nu}_l$ decay

The differential decay rate :

$$\frac{d\Gamma}{dq^2} = \left[2J_{1s} + J_{1c} - \frac{1}{3} (2J_{2s} + J_{2c}) \right]$$

The forward-backward asymmetry for lepton can be written in terms of the angular coefficients as :

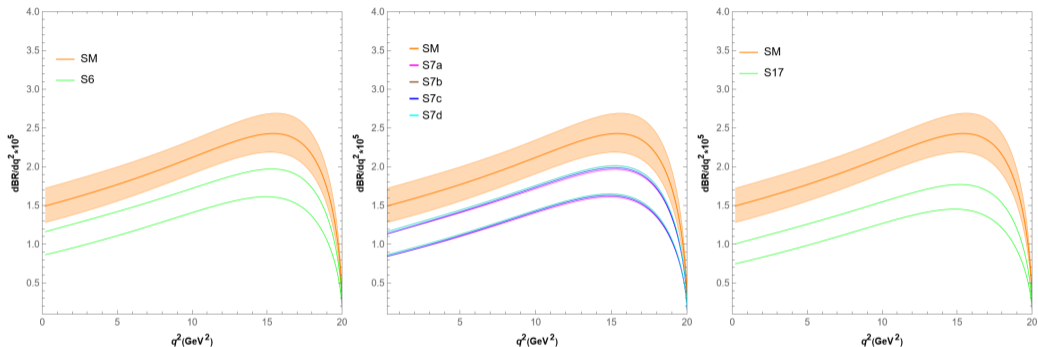
$$A_{FB} = \frac{J_{6s} + \frac{1}{2}J_{6c}}{\left[2J_{1s} + J_{1c} - \frac{1}{3} (2J_{2s} + J_{2c}) \right]}$$

The Longitudinal Polarization of K^* meson can be written as :

$$F_L = \frac{J_{1c} - \frac{1}{3}J_{2c}}{J_{tot}}, \quad J_{tot} = \frac{(2J_{1s} + J_{1c}) - (2J_{2s} + J_{2c})}{3}$$

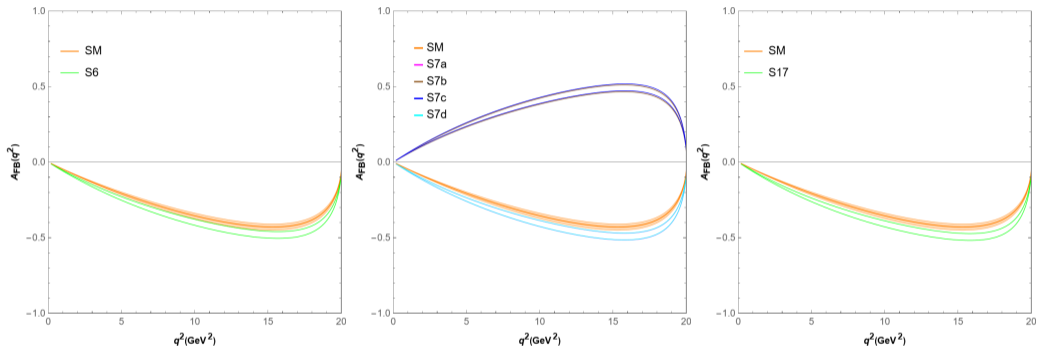
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Predictions for the Differential Branching Fraction



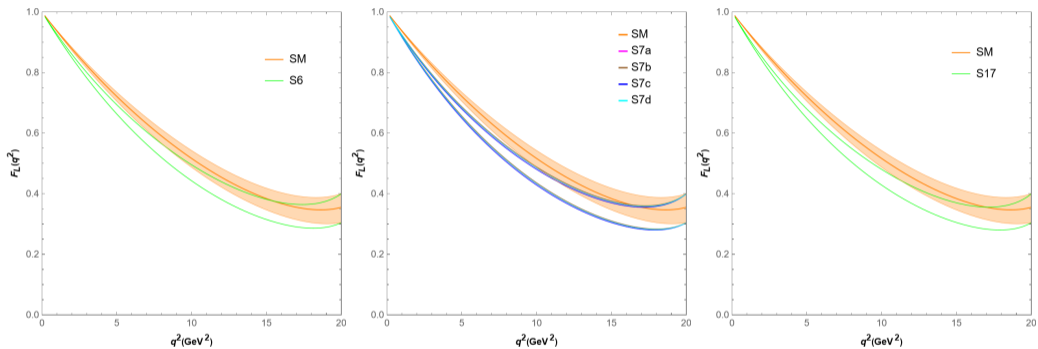
- Scenarios S6, S7 and S17 show the deviation from SM in the Branching fraction.
- The four different cases in S7 scenario can not be distinguished based on the Branching fraction.

Predictions for the Forward-Backward Asymmetry



- In AFB S6,S7 and S17 show the deviation from SM.
- S7b and S7c Scenarios can be distinguish from S7a and S7d Scenarios.

Predictions for the Logitudnal Polarization of K^* meson



- Longitudinal polarization of K^* meson shows the similar kind of deviation as in Branching Fraction.

Prediction for the INTEGRATED ANGULAR OBSERVABLES

Normalized angular observables defined as :

$$\tilde{J}_i = \frac{\int_{q_{min}^2}^{q_{max}^2} J_i(q^2) dq^2}{\int_{q_{min}^2}^{q_{max}^2} \frac{d\Gamma}{dq^2} dq^2}$$

Scenario	\tilde{J}_{1s}	\tilde{J}_{1c}	\tilde{J}_{2s}	\tilde{J}_{2c}	\tilde{J}_3	\tilde{J}_4	\tilde{J}_5	\tilde{J}_{6s}
SM	0.255(35)	0.409(47)	0.085(12)	-0.409(47)	-0.059(23)	0.194(7)	-0.283(23)	-0.311(40)
S1	0.247(36)	0.420(48)	0.082(12)	-0.420(48)	-0.071(23)	0.199(7)	-0.266(22)	-0.286(38)
S2	0.258(37)	0.405(49)	0.086(12)	-0.405(49)	-0.055(26)	0.192(10)	-0.292(30)	-0.314(45)
S3	0.247(36)	0.420(48)	0.082(12)	-0.420(48)	-0.071(23)	0.199(7)	-0.266(22)	-0.286(38)
S4	0.247(36)	0.420(48)	0.082(12)	-0.420(48)	-0.071(23)	0.199(7)	-0.266(22)	-0.286(38)
S5	0.247(36)	0.420(48)	0.082(13)	-0.420(49)	-0.070(23)	0.199(11)	-0.266(23)	-0.286(38)
S6	0.267(38)	0.395(50)	0.089(13)	-0.395(50)	-0.043(30)	0.187(12)	-0.308(34)	-0.331(49)

Scenario	\tilde{J}_{1s}	\tilde{J}_{1c}	\tilde{J}_{2s}	\tilde{J}_{2c}	\tilde{J}_3	\tilde{J}_4	\tilde{J}_5	\tilde{J}_{6s}
<i>S7a</i>	0.270(38)	0.390(51)	0.090(13)	-0.390(51)	-0.039(31)	0.185(12)	-0.314(35)	-0.338(50)
<i>S7b</i>	0.270(39)	0.390(51)	0.090(13)	-0.390(52)	-0.039(33)	0.185(13)	0.313(38)	-0.337(52)
<i>S7c</i>	0.272(39)	0.387(52)	0.091(13)	-0.387(52)	-0.035(34)	0.184(14)	0.318(38)	0.342(52)
<i>S7d</i>	0.270(38)	0.390(52)	0.090(13)	-0.390(52)	-0.039(33)	0.185(14)	-0.313(38)	-0.337(52)
S8	0.247(36)	0.420(48)	0.082(12)	-0.420(48)	-0.071(23)	0.199(07)	-0.266(22)	-0.286(38)
S9	0.247(36)	0.420(48)	0.082(12)	-0.420(48)	-0.071(23)	0.199(07)	-0.266(22)	-0.286(38)
S10	0.248(36)	0.419(48)	0.081(15)	-0.418(51)	-0.070(23)	0.198(16)	-0.265(23)	-0.285(38)
S11	0.260(37)	0.404(49)	0.087(12)	-0.404(47)	-0.053(27)	0.191(10)	-0.294(30)	-0.317(45)
S12	0.260(37)	0.404(49)	0.087(12)	-0.404(47)	-0.053(27)	0.191(10)	-0.294(30)	-0.317(45)
S13	0.258(36)	0.405(49)	0.086(12)	-0.405(49)	-0.055(26)	0.192(10)	-0.292(30)	-0.314(45)
S14	0.247(36)	0.420(48)	0.082(12)	-0.420(48)	-0.071(23)	0.199(07)	-0.266(22)	-0.286(38)
S15	0.247(36)	0.420(48)	0.082(13)	-0.419(49)	-0.070(23)	0.199(11)	-0.266(23)	-0.286(38)
S16	0.247(36)	0.420(48)	0.081(13)	-0.419(49)	-0.070(23)	0.199(11)	-0.267(23)	-0.286(38)
S17	0.273(39)	0.386(52)	0.091(13)	-0.385(52)	-0.033(34)	0.183(14)	-0.329(37)	-0.344(52)

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Conclusion

- We investigated the New Physics in the semileptonic decay $\bar{B}_s \rightarrow K^{*+} (\rightarrow K\pi) l^- \bar{\nu}_l$ induced by the quark level transition $b \rightarrow ul\nu$.
- We considered the most general effective Hamiltonian with the different possible Lorentz structures.
- The different NP wilson coefficients are constrained by the available measurements of branching ratios of $\bar{B}^0 \rightarrow \pi^+ l^- \bar{\nu}$, $B \rightarrow \rho l\nu$, $B \rightarrow \omega l\nu$ and $B \rightarrow \mu\nu$ decays.
- We investigated the NP effects in $\bar{B}_s \rightarrow K^{*+} (\rightarrow K\pi) l^- \bar{\nu}_l$ by predicting the q^2 spectrum of Branching Ratio, Forward-Backward asymmetry and polarization fraction of K^* meson F_L . And also provide predictions for the Integrated Angular Observables.

Thank you for listening !

Appendix

The hadronic matrix elements for $B_s \rightarrow K^*$ can be written in terms of seven form factors namely $V, A_0, A_1, A_{12}, T_1, T_2$ and T_{23} . The form factors are defined by simplified series expansion in z given by Bharucha-Straub-Zwicky as

$$f_i(q^2) = \frac{1}{(1 - q^2/m_{R,i}^2)} \sum_k \alpha_k^i [z(q^2) - z(0)]^k, \quad \text{Where } z(t) = \frac{\sqrt{t_+ - t} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - t} + \sqrt{t_+ - t_0}}$$

with $t_{\pm} = (m_{B_s} \pm m_{K^*})$ and $t_0 = (m_{B_s} + m_{K^*})(\sqrt{m_{B_s}} - \sqrt{m_{K^*}})^2$.

f_i	J^P	$m_{R,i}/\text{GeV}$
A_0	0^-	5.279
V, T_1	1^-	5.325
A_1, T_2, A_{12}, T_{23}	1^+	5.724

Table 1: Masses of resonances required for form factor parameterizations

f_i	α_0^i	α_1^i	α_2^i
V	0.28 ± 0.02	-0.82 ± 0.19	5.08 ± 1.42
A_0	0.36 ± 0.02	-0.36 ± 0.20	8.03 ± 2.07
A_1	0.22 ± 0.01	0.24 ± 0.16	1.77 ± 0.85
A_{12}	0.27 ± 0.02	1.12 ± 0.11	3.43 ± 0.78
T_1	0.24 ± 0.01	-0.75 ± 0.15	2.49 ± 1.37
T_2	0.24 ± 0.01	0.31 ± 0.15	1.58 ± 0.93
T_{23}	0.60 ± 0.04	2.40 ± 0.27	9.64 ± 2.03

Table 2: Simplified series expansion coefficients α_k^i for parameterising the $B_s \rightarrow K^*$ form factors using the combined LCSR + Lattice fit

Appendix

The form factors for vector currents, axial vector currents and tensor currents in the helicity basis can be written as :

- Vector current

$$\mathcal{F}_\perp(q^2) = \frac{\sqrt{2\lambda}}{M_{B_s}(M_{B_s} + M_{K^*})} V(q^2)$$

- Axial vector current

$$\mathcal{F}_t(q^2) = \frac{\sqrt{\lambda}}{M_{B_s}^2} A_0(q^2)$$

$$\mathcal{F}_\parallel(q^2) = \sqrt{2} \frac{M_{B_s} + M_{K^*}}{M_{B_s}} A_1(q^2)$$

$$\mathcal{F}_0(q^2) = \frac{8M_{K^*} A_{12}(q^2)}{M_{B_s}}$$

- Tensor current

$$\mathcal{F}_\perp^T(q^2) = \frac{\sqrt{2\lambda}}{M_{B_s}^2} T_1(q^2)$$

$$\mathcal{F}_\parallel^T(q^2) = \frac{\sqrt{2}(M_{B_s}^2 - M_{K^*}^2)}{M_{B_s}^2} T_2(q^2)$$

$$\mathcal{F}_0^T(q^2) = \frac{4M_{K^*} T_{23}(q^2)}{M_{B_s} + M_{K^*}}$$

Appendix

The contribution from helicity amplitudes can be given as

$$\mathcal{A}_0^L = -4 \frac{M_{B_s}^2 (1 + C_{V_L} - C_{V_R}) \mathcal{F}_0(q^2)}{\sqrt{q^2}}$$

$$\mathcal{A}_\perp^L = 4M_{B_s} (1 + C_{V_L} + C_{V_R}) \mathcal{F}_\perp(q^2)$$

$$\mathcal{A}_\parallel^L = -4M_{B_s} (1 + C_{V_L} - C_{V_R}) \mathcal{F}_\parallel(q^2)$$

$$\mathcal{A}_t^L = -4 \left[\frac{m_l M_{B_s}^2}{\sqrt{q^2}} (1 + C_{V_L} - C_{V_R}) + \frac{M_{B_s}^2}{m_b} (C_{S_L} - C_{S_R}) \right] \mathcal{F}_t(q^2)$$

$$\mathcal{A}_{\parallel\perp} = +8M_{B_s} C_T \mathcal{F}_0^T(q^2)$$

$$\mathcal{A}_{t\perp} = 4\sqrt{2} \frac{M_{B_s}^2}{\sqrt{q^2}} C_T \mathcal{F}_\perp^T(q^2)$$

$$\mathcal{A}_{0\parallel} = 4\sqrt{2} \frac{M_{B_s}^2}{\sqrt{q^2}} C_T \mathcal{F}_\parallel^T(q^2)$$