



# Hadronic B decays at Belle and Belle II

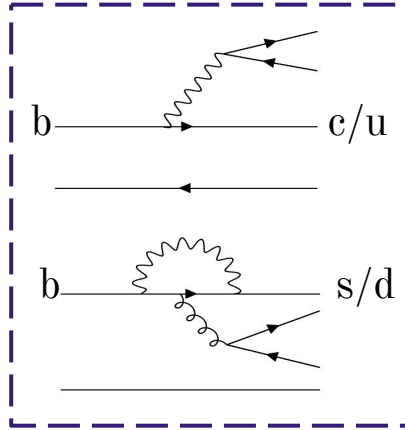
Swarna Prabha Maharana (IIT Hyderabad)  
on behalf of the Belle II collaboration

PPC 2024, Parallel Session



# B → Hadronic

- Dominated by the  $b \rightarrow c$  trees.
- Hadronic decays of B-mesons account for  $\sim 75\%$  of the total branching fraction.

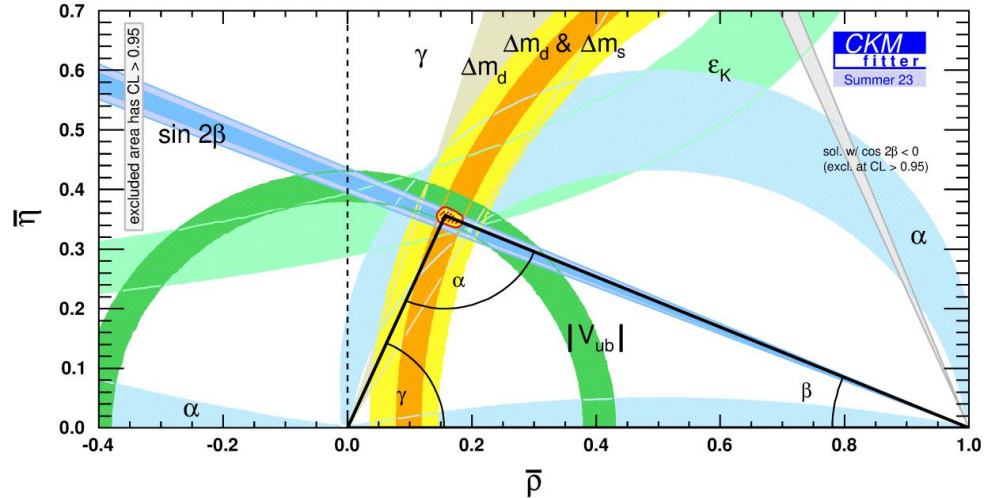


For today:

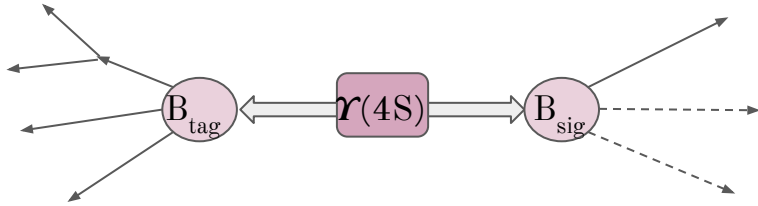
- $B^- \rightarrow D^0 \rho(770)^-$
- $B \rightarrow D^{(*)} K K_S$
- Belle + Belle II combined measurement of  $\phi_3$
- $B \rightarrow \pi^0 \pi^0$ : towards  $\phi_2$

Probe the SM:

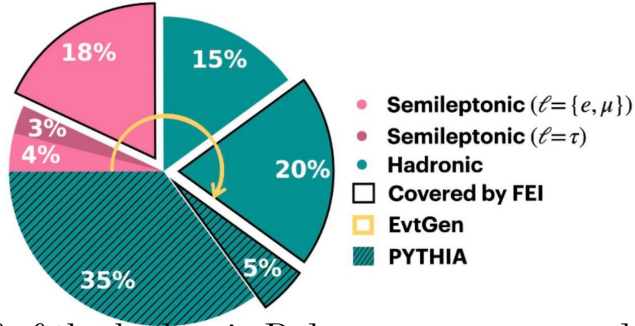
- over-constrain CKM triangle
  - $\phi_1/\beta$ : via time-dependent analysis of e.g.  $J/\psi K_S$
  - $\phi_2/\alpha$ : via isospin analysis of  $B \rightarrow \rho\rho$ ,  $B \rightarrow \pi\pi$
  - $\phi_3/\gamma$ : via  $B^- \rightarrow Dh^-$ ,  $B^- \rightarrow D^* K^-$
- via isospin sum rules



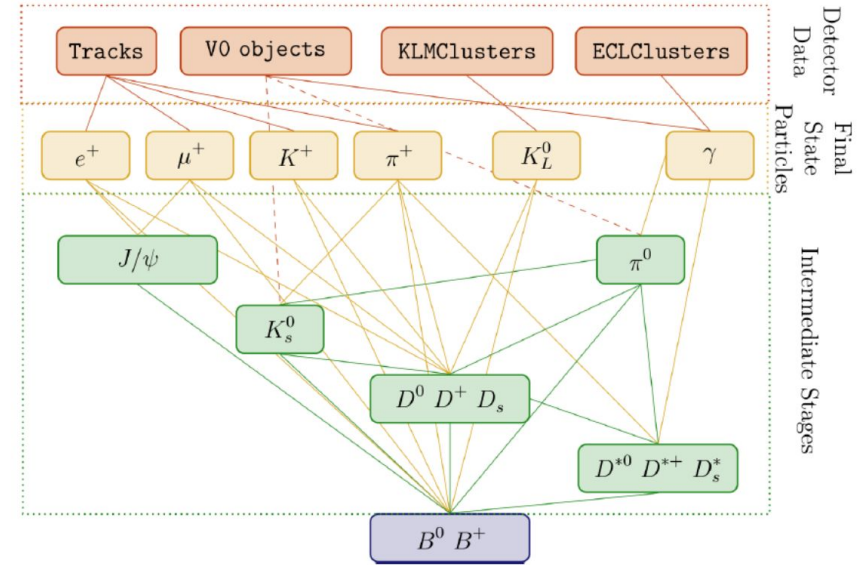
# Hadronic Tagging



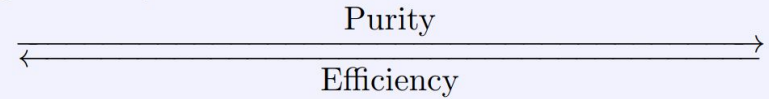
- Missing energy modes need tagging.
- Hadronic tagging has high purity as well as gives direction of B.
- But large data-MC discrepancy in several channels



- Only half of the hadronic B decays are measured.
- PYTHIA generates the other half in MC.
- Most measurements are performed with small data sets.



## Tagging techniques



**Inclusive**  
 $B \rightarrow \text{anything}$   
 $\epsilon \approx \mathcal{O}(100\%)$

**Semileptonic**  
 $B \rightarrow D^{(*)} \ell \nu \ell$   
 $\epsilon \approx \mathcal{O}(1\%)$

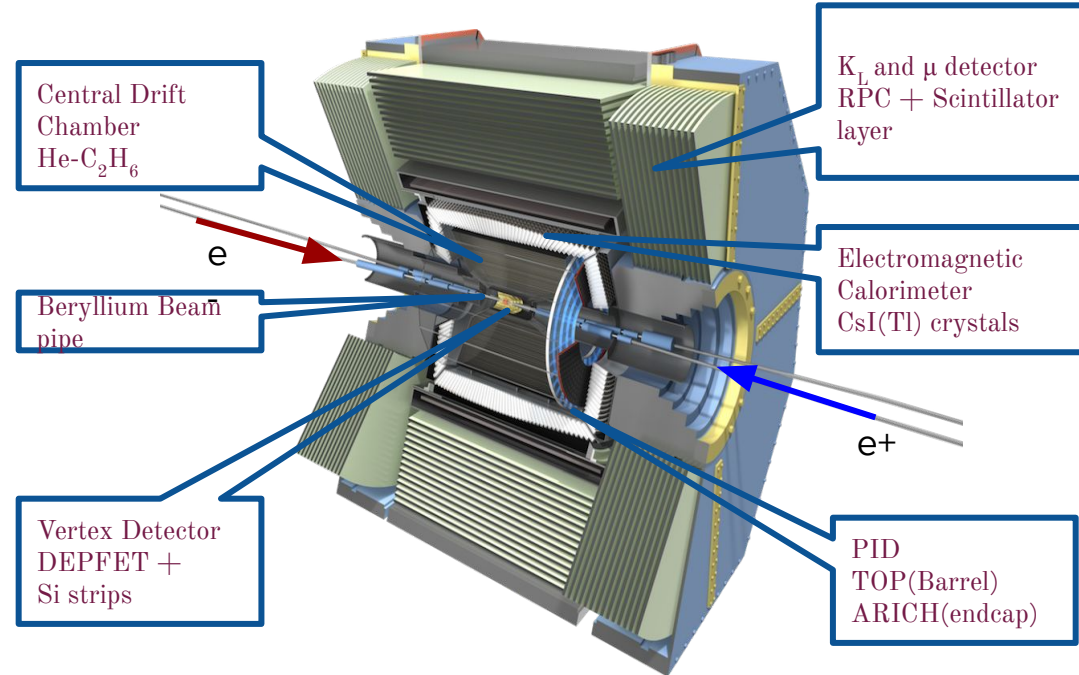
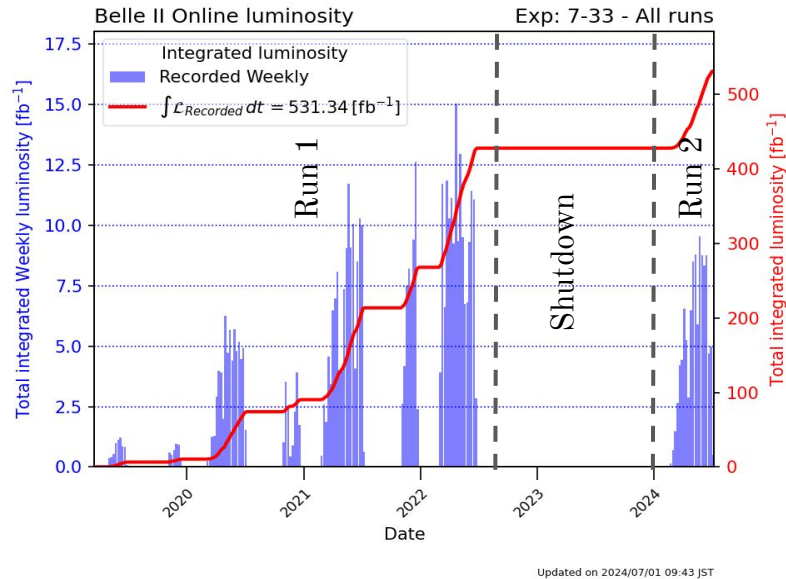
**Hadronic**  
 $B \rightarrow \text{hadrons}$   
 $\epsilon \approx \mathcal{O}(0.1\%)$

Improving FEI efficiency  $\rightarrow$  More DATA in hand

# Belle II

- Asymmetric  $e^-e^+$  collisions at  $\Upsilon(4S)$  resonance.
- $\Upsilon(4S) \rightarrow BB$  : 2B's and nothing else.
- $1.1 \times 10^9 B\bar{B}$  pairs per  $ab^{-1}$

- clean environment
- excellent neutral reconstruction



# Analysis

## 1. Reconstruction

- Start with final state particles
- Form a B candidate

## 2. Selection

- Background suppression
- Mostly continuum background

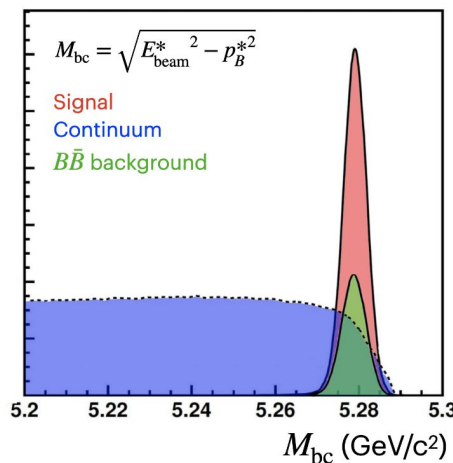
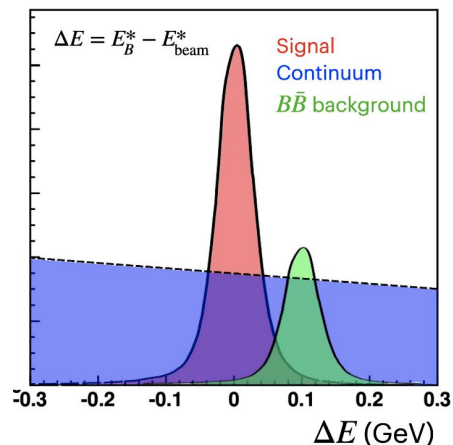
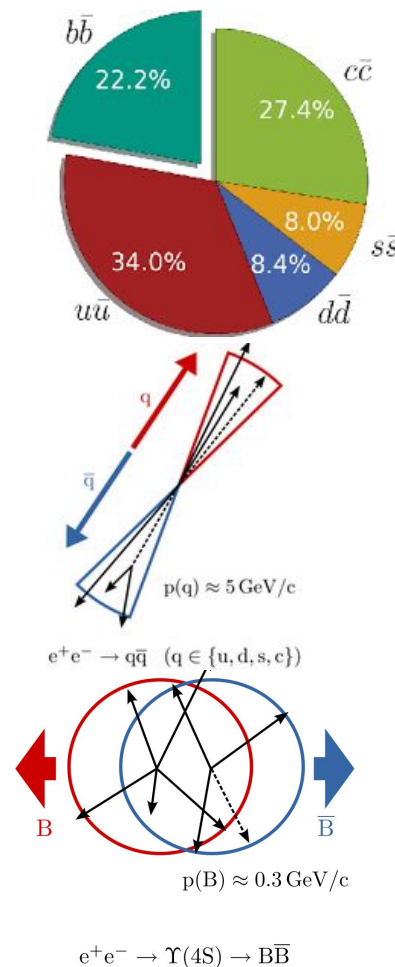
## 3. Modelling + Fit

- Model using simulation
- fit to data to extract physics quantities

## 4. Systematic uncertainties

- toy studies + control modes

Challenges: small BR, high backgrounds, neutrals



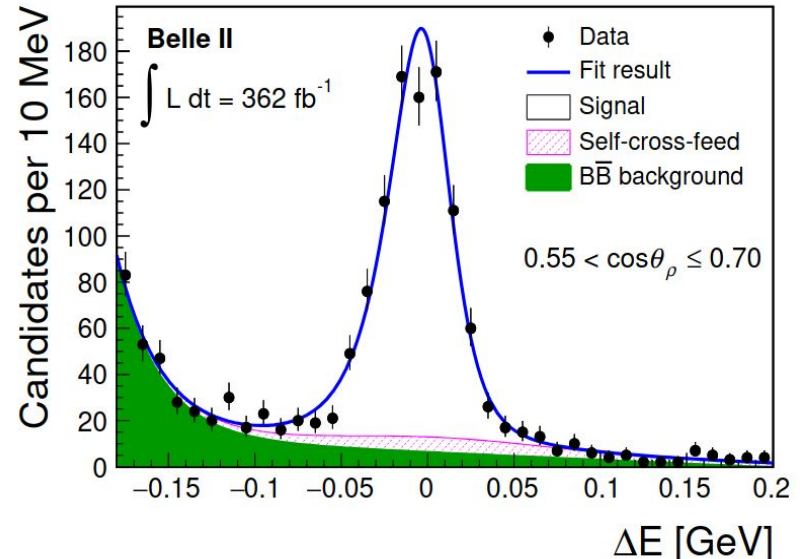
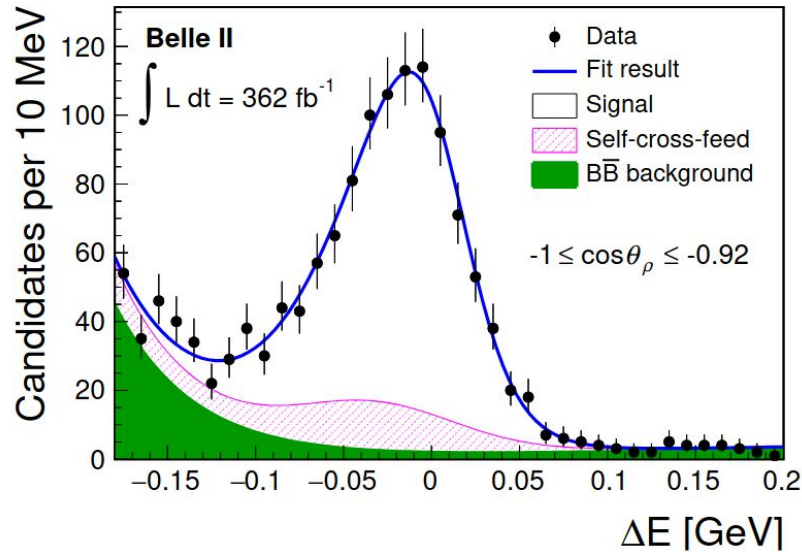
Improving knowledge on B decays

# $B^- \rightarrow D^0 \rho(770)^-$

[Phys. Rev. D 109, L111103]

- PDG measurement-  $(1.35 \pm 0.18)\%$  by CLEO(1994) with  $0.9\text{fb}^{-1}$ , which includes large uncertainty
- $B^- \rightarrow D^0 \rho^-$ ,  $B^0 \rightarrow D^+ \rho^-$ , and  $B^0 \rightarrow D^0 \rho^0$  provides tests of calculations of hadronic decay rates based on the heavy-quark limit and factorization models.

Needs to account: Contamination from non-resonant component  $B^- \rightarrow D^0 \pi \pi^0$  contribution in  $\Delta E$ .



- Signal Extraction- unbinned maximum likelihood fit to  $\Delta E$  distribution

Solution: Perform fit in bins of  $\cos \theta_\rho$  ( $\theta_\rho$  the angle between the  $\pi^-$  momentum and the direction opposite to the  $B^-$  momentum in the  $\rho^-$  rest frame)

# $B^- \rightarrow D^0 \rho(770)^-$

[Phys. Rev. D 109, L111103]

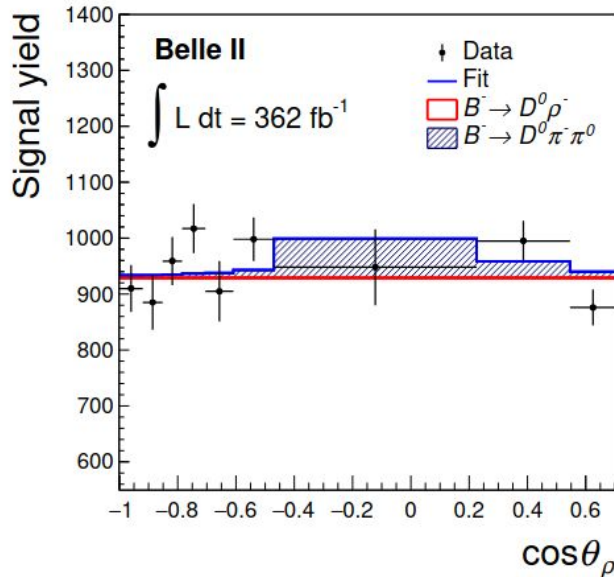
Template fit to distribution  $\cos\theta_\rho$ :

- non-uniform binning: flat distribution for  $B^- \rightarrow D^0 \rho^-$
- $\cos\theta_\rho < 0.7$ : to suppress decays  $B^- \rightarrow D^{**} \pi$
- $\sim (1.9 \pm 1.8)\%$  contribution of  $B^- \rightarrow D^0 \pi^- \pi^0$

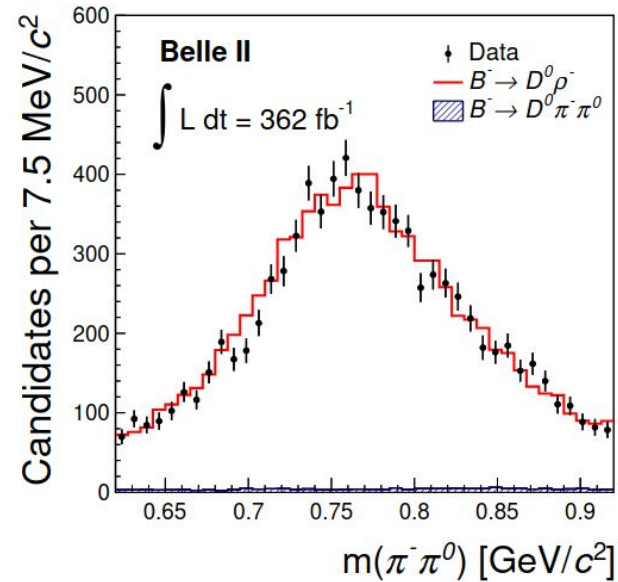
$$\mathcal{B}(B^- \rightarrow D^0 \rho^-) = (0.939 \pm 0.021 \pm 0.050)\%$$

2× better precision!!

Systematically limited by  $\pi^0$  reconstruction efficiency



Factorization test : In agreement with prediction





# $B \rightarrow D^{(*)} K K_{(S)}^{(*)0}$ and $B \rightarrow D^{(*)} D_s^-$

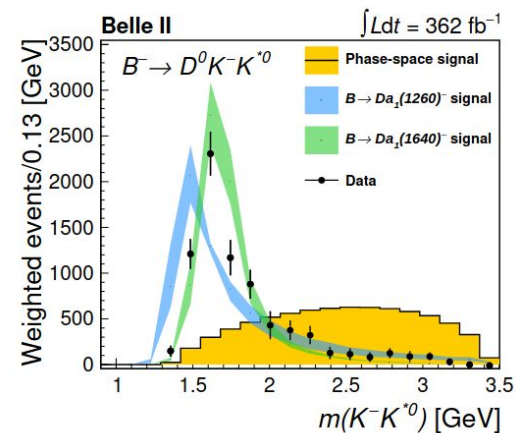
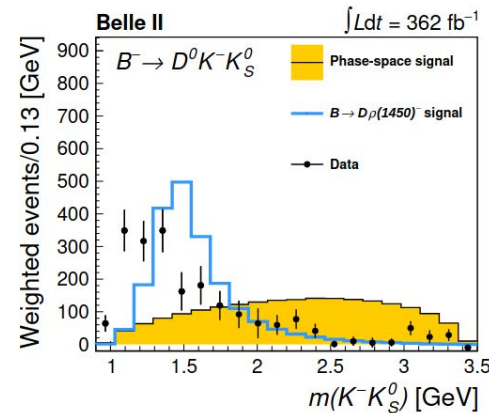
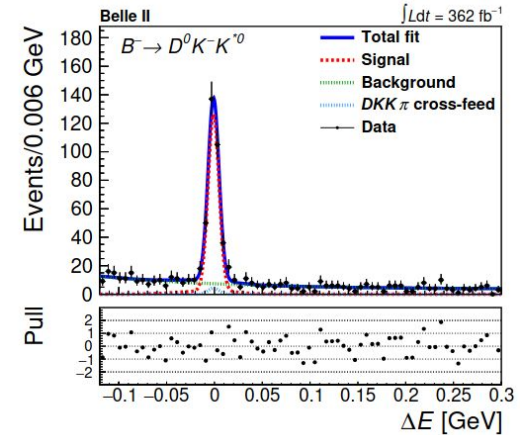
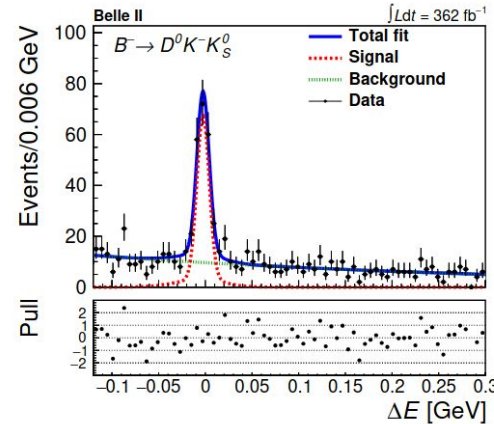
[J. High Energy. Phys. **2024**, 206]

$B \rightarrow DK^- K$  decays make up a few percent of the overall hadronic branching fraction

- Only a small amount of them are well measured.
- Serves as inputs for simulations and tagging techniques.
- Possibility of  $B \rightarrow DX^- (\rightarrow K^- K)$ , with an intermediate resonance  $X^-$  that decays strongly,

Challenge: bkg from non-resonant  $B \rightarrow DK^- K\pi$   
 Modes in  $K^*$  modes  $\rightarrow$  fit to  $M(K\pi)$

- Signal Extraction: fit  $\Delta E$  distribution
- BF's extracted applying an efficiency correction in the plane  $M(D^{(*)} K_S^{(*)0}, M(K^- K_S^{(*)0}))$
- Extraction of bkg-subtracted and efficiency-corrected invariant mass and helicity angles.
- $J^P = 1^{-/+}$  dominant transitions

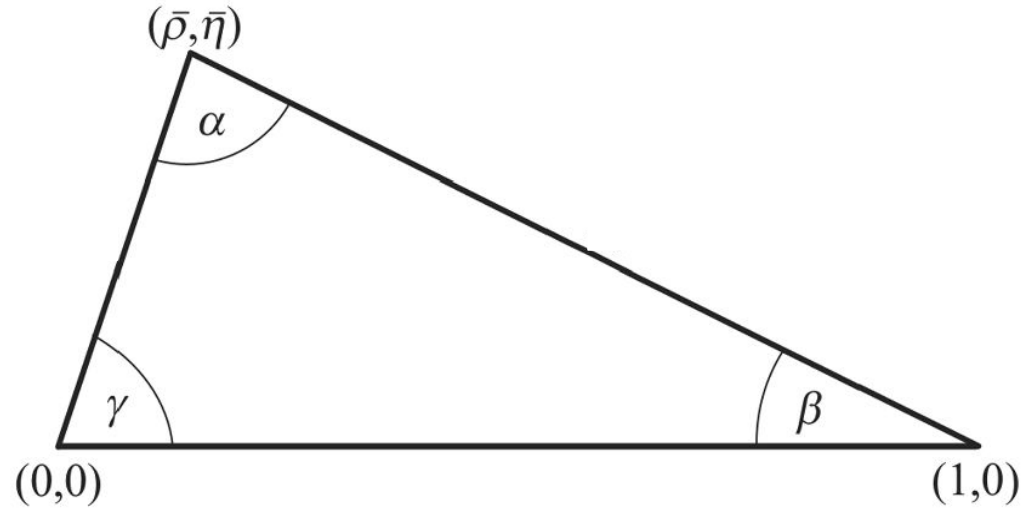


# $B \rightarrow D^{(*)} K K_{(S)}^{(*)0}$ and $B \rightarrow D^{(*)} D_s^-$

[J. High Energ. Phys. **2024**, 206]

Channel	Yield ( $K_S^0 / K^{*0}$ )	Average $\varepsilon$ ( $K_S^0 / K^{*0}$ )	$\mathcal{B}$ [ $10^{-4}$ ]	
$B^- \rightarrow D^0 K^- K_S^0$	$209 \pm 17$	0.098	$1.82 \pm 0.16 \pm 0.08$	
$\bar{B}^0 \rightarrow \bar{D}^+ \bar{K}^- \bar{K}_S^0$	$105 \pm 14$	0.048	$0.82 \pm 0.12 \pm 0.05$	First observation
$B^- \rightarrow D^{*0} K^- K_S^0$	$51 \pm 9$	0.044	$1.47 \pm 0.27 \pm 0.10$	
$\bar{B}^0 \rightarrow D^{*+} \bar{K}^- \bar{K}_S^0$	$36 \pm 7$	0.046	$0.91 \pm 0.19 \pm 0.05$	
$B^- \rightarrow D^0 K^- K^{*0}$	$325 \pm 19$	0.043	$7.19 \pm 0.45 \pm 0.33$	
$\bar{B}^0 \rightarrow D^+ K^- K^{*0}$	$385 \pm 22$	0.021	$7.56 \pm 0.45 \pm 0.38$	3× better precision
$B^- \rightarrow D^{*0} K^- K^{*0}$	$160 \pm 15$	0.019	$11.93 \pm 1.14 \pm 0.93$	
$\bar{B}^0 \rightarrow D^{*+} \bar{K}^- \bar{K}^{*0}$	$193 \pm 14$	0.020	$13.12 \pm 1.21 \pm 0.71$	
$B^- \rightarrow D^0 D_s^-$	$144 \pm 12 / 153 \pm 13$	0.04 / 0.09	$95 \pm 6 \pm 5$	World's best
$\bar{B}^0 \rightarrow D^+ D_s^-$	$145 \pm 12 / 159 \pm 13$	0.02 / 0.05	$89 \pm 5 \pm 5$	
$B^- \rightarrow D^{*0} D_s^-$	$30 \pm 6 / 29 \pm 7$	0.02 / 0.04	$65 \pm 10 \pm 6$	
$\bar{B}^0 \rightarrow D^{*+} D_s^-$	$43 \pm 7 / 37 \pm 7$	0.02 / 0.04	$83 \pm 10 \pm 6$	

# CPV via CKM



# $\phi_3/\gamma$ measurement: Belle + Belle II combination

$$\phi_3 \equiv \arg(-V_{ud}V_{ub}^*/V_{cd}V_{cb}^*)$$

$$\frac{\mathcal{A}^{\text{suppr.}}(B^- \rightarrow \bar{D}^0 K^-)}{\mathcal{A}^{\text{favor.}}(B^- \rightarrow D^0 K^-)} = r_B e^{i(\delta_B - \phi_3)}$$

[arXiv:2404.12817v2]  
Accepted by JHEP

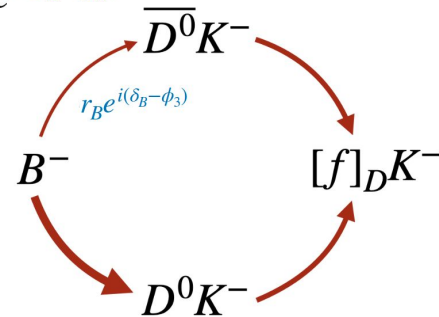
- Tree level decays — no (large) BSM
- Strong constraint on SM

various approaches — different final states:

- Self-conjugate final states
- Cabibbo-suppressed decays ,
- eigenstates

First combination of all Belle and Belle II measurements:

59 input observables, 18 free parameters.

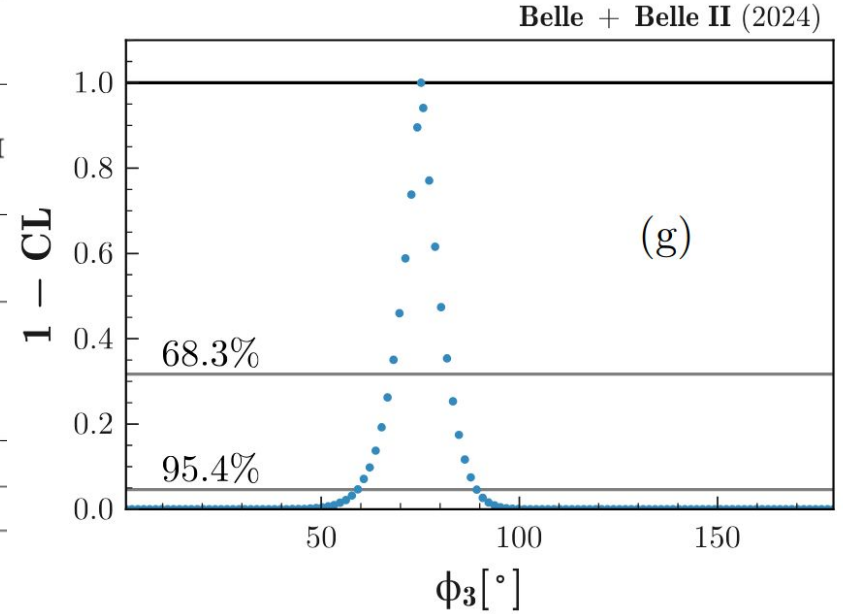


$B$ decay	$D$ decay	Method	Data set (Belle + Belle II)[fb <sup>-1</sup> ]	
$B^+ \rightarrow Dh^+$	$D \rightarrow K_S^0 \pi^0, K^- K^+$	GLW	711 + 189	[JHEP 05 212 (2024)]
$B^+ \rightarrow Dh^+$	$D \rightarrow K^+ \pi^-, K^+ \pi^- \pi^0$	ADS	711 + 0	[PRL 106 231803 (2011), PRD 88 091104(2013)]
$B^+ \rightarrow Dh^+$	$D \rightarrow K_S^0 K^- \pi^+$	GLS	711 + 362	[JHEP 09 146 (2023)]
$B^+ \rightarrow Dh^+$	$D \rightarrow K_S^0 h^- h^+$	BPGGSZ (m.i.)	711 + 128	[JHEP 02 063 (2022)]
$B^+ \rightarrow Dh^+$	$D \rightarrow K_S^0 \pi^- \pi^+ \pi^0$	BPGGSZ (m.i.)	711 + 0	[JHEP 10 178 (2019)]
$B^+ \rightarrow D^* K^+$	$D^* \rightarrow D \pi^0, D \rightarrow K_S^0 \pi^0, K_S^0 \phi, K_S^0 \omega,$ $K^- K^+, \pi^- \pi^+$	GLW	210+0	[PRD 73 051106 (2006)]
$B^+ \rightarrow D^* K^+$	$D^* \rightarrow D \pi^0, D \gamma, D \rightarrow K_S^0 \pi^- \pi^+$	BPGGSZ (m.d.)	605 + 0	[PRD 81 112002 (2010)]

# $\phi_3/\gamma$ measurement: Belle + Belle II combination

[arXiv:2404.12817v2]  
Accepted by JHEP

Decay	Observable	Value	Source
$D \rightarrow K^+\pi^-$	$R_D^{K\pi}$	$(3.44 \pm 0.02) \times 10^{-3}$	HFLAV
	$\delta_D^{K\pi}$	$(191.7 \pm 3.7)^\circ$	
	$r_D^{K\pi} \cos(\delta_D^{K\pi})$	$-0.0562 \pm 0.0081$	BESIII
	$r_D^{K\pi} \sin(\delta_D^{K\pi})$	$-0.011 \pm 0.012$	
$D \rightarrow K^+\pi^-\pi^0$	$r_D^{K\pi\pi^0}$	$0.0441 \pm 0.0011$	CLEO + LHCb + BESIII
	$\kappa_D^{K\pi\pi^0}$	$0.79 \pm 0.04$	
	$\delta_D^{K\pi\pi^0}$	$(196 \pm 11)^\circ$	
$D^0 - \bar{D}^0$ mixing	$x_D$	$(0.407 \pm 0.044)\%$	HFLAV
	$y_D$	$(0.647 \pm 0.024)\%$	
$D \rightarrow K_S^0 K^- \pi^+$	$(r_D^{K_S^0 K^- \pi^+})^2$	$0.356 \pm 0.034$	CLEO
	$\kappa_D^{K_S^0 K^- \pi^+}$	$0.94 \pm 0.12$	
	$\delta_D^{K_S^0 K^- \pi^+}$	$(-16.6 \pm 18.4)^\circ$	
	$(r_D^{K_S^0 \bar{K}^- \pi^+})^2$	$0.370 \pm 0.003$	
$B^+ \rightarrow Dh^+$	$R_{\text{GLS}}$	$0.0789 \pm 0.0027$	PDG



$$\phi_3 = (75.2 \pm 7.6)^\circ$$

[HFLAV]  
 $\phi_3^{\text{WA}}(^\circ) = 66.2_{-3.6}^{+3.4}$

# $B^0 \rightarrow \pi^0 \pi^0$ : towards $\phi_2$

Tree-level  $b \rightarrow uud$  processes allow extraction of  $\phi_2$

- Interference with penguin amplitudes
- Statistical limitation due to color suppression in tree diagram

## First measurement of $B^0 \rightarrow \pi^0 \pi^0$ at Belle II

- 4 photons in final state
- Suffers from large background

Update on  $BF$  and  $A_{CP}$  using full Run-1 statistics with

- new GNN-based flavor tagger
- BDT dedicated for photon selection and  $qq$  suppression
- reduction of systematic uncertainties

## Signal extraction by simultaneous fit

- $\Delta E$ ,  $M_{bc}$ , BDT output (C), transformed wrong tag probability

$$\mathcal{B}(B^0 \rightarrow \pi^0 \pi^0) = (1.26 \pm 0.20 \pm 0.11) \times 10^{-6}$$

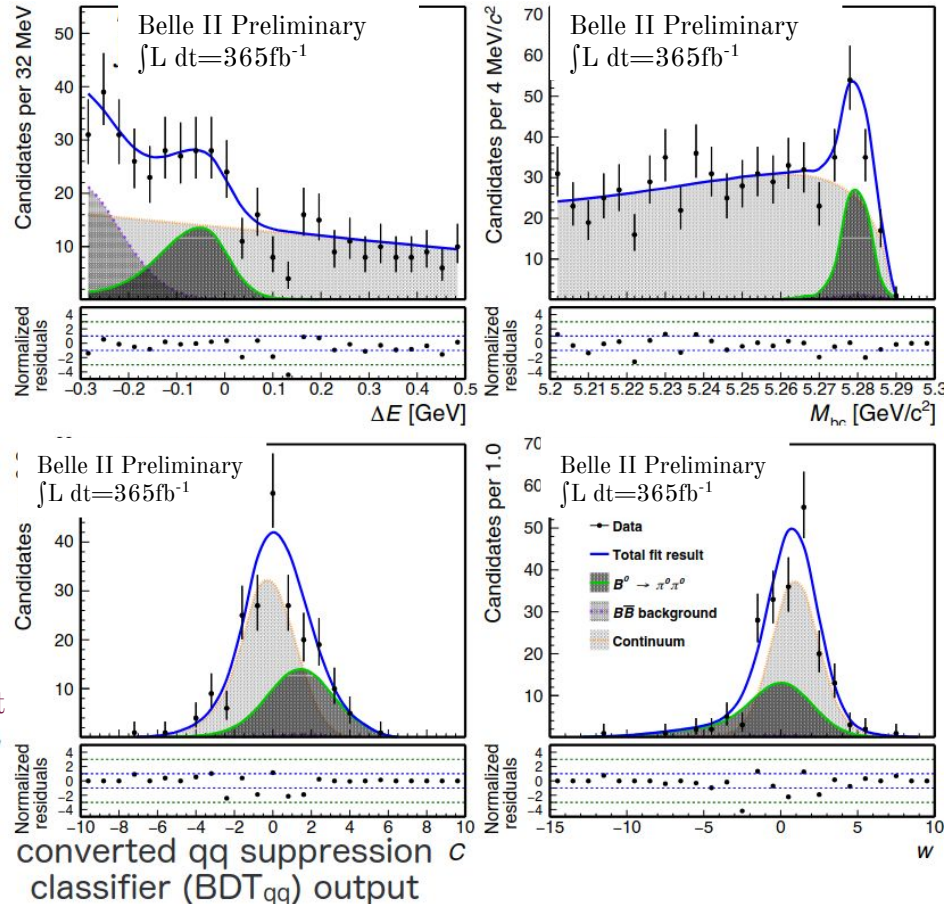
$$A_{CP}(B^0 \rightarrow \pi^0 \pi^0) = 0.06 \pm 0.30 \pm 0.06$$

World's best

Compatible with world averages despite smaller data sample

paper in preparation

189fb<sup>-1</sup> [Phys. Rev. D 107, 112009]



# Summary

- Improve B decay knowledge  $B^- \rightarrow D^0 \rho^-$ ,  $B \rightarrow DD_S$
- New decay modes observed  $B \rightarrow D^{(*)} K^- K_S^{(*)0}$ .
- Combining Belle and Belle II measurements to precisely measure  $\phi_3$
- Progress towards measurement of  $\phi_2$

**Run 2 started, more luminosity on it's way!**

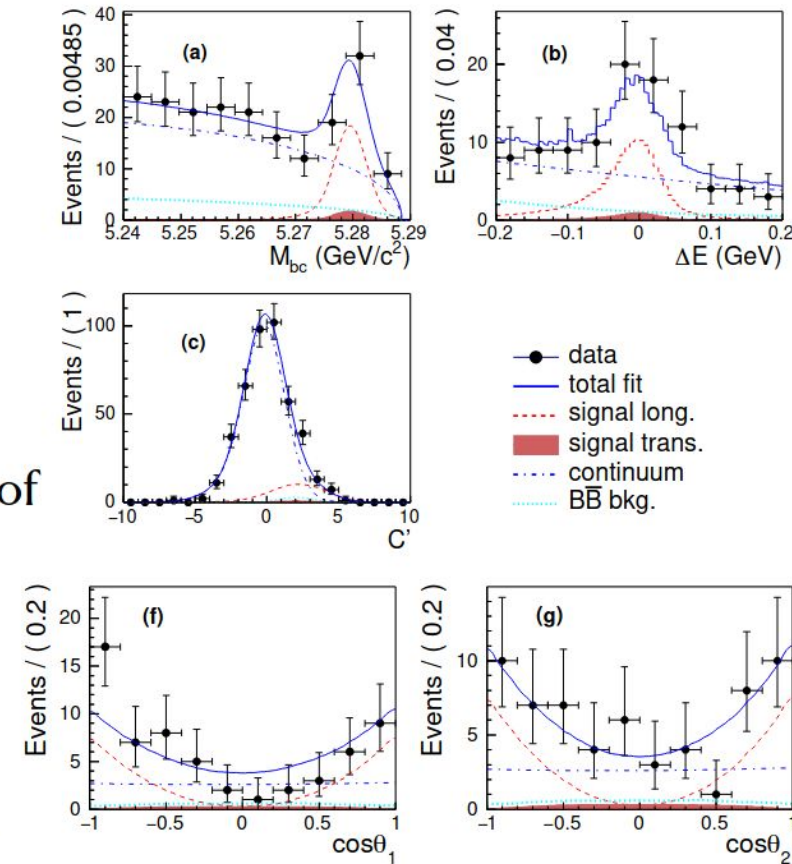


# $B^0 \rightarrow \omega\omega$

[Phys. Rev. Lett. 133, 081801]

- Rare and never observed decay
- Polarisation ( $f_L$ ) and direct-CPV parameter  $A_{CP}$  useful for  $B \rightarrow VV$  decays
- BF,  $f_L$  and  $A_{CP}$  extraction in full Belle dataset
- Bkg suppressed using event-topology information
- Signal extraction from fit to:  $\Delta E$ ,  $M_{bc}$ , continuum suppression output,  $\omega$  invariant masses and cosine of helicity angles of both the  $\omega$ 's

$$\mathcal{B} = (1.53 \pm 0.29 \pm 0.17) \times 10^{-6}$$
$$f_L = 0.87 \pm 0.13 \pm 0.13$$
$$A_{CP} = -0.44 \pm 0.43 \pm 0.11,$$





$$B \rightarrow D^{(*)} K K_{(S)}^{(*)0} \text{ and } B \rightarrow D^{(*)} D_s^-$$

## bkg-subtracted and efficiency corrected $m(K^- K)$ distributions

