



Anisotropy and the missing rest frame of the Universe

Falsify the standard dark cosmological model

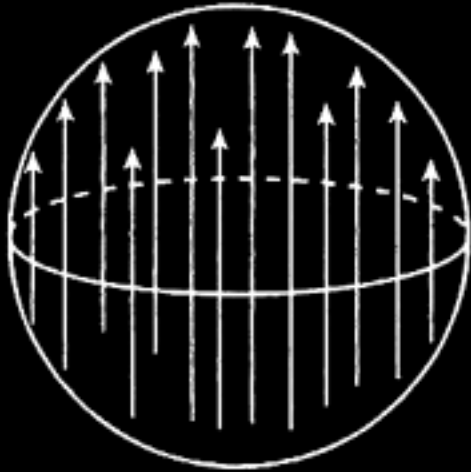
M. Rameez

work in coll with:

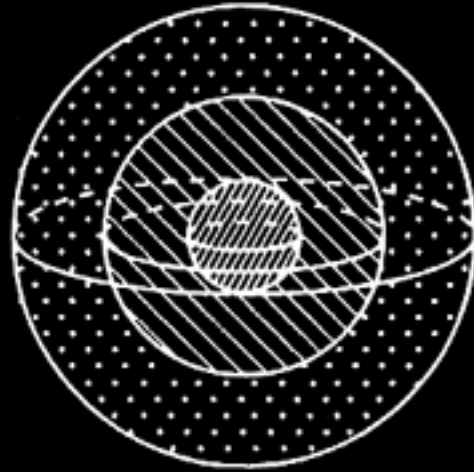
Secrest, von Hausegger, Colin, Mohayaee, Sarkar

# The cosmological principle

The Universe is (statistically) **isotropic** and **homogenous** (on large scales).



Homogeneous  
Not isotropic



Isotropic  
Not homogeneous

No special positions or directions in the Universe.  
“The universe presents the same general aspect at every point”  
Edward Arthur Milne  
Also the Copernican principle : we are ‘typical’ observers.

The ‘Perfect’ version was abandoned following the discovery of the CMB in 1964 and the realization that the universe *does* have a beginning ... but the cosmological principle lived on

Enables an enormous simplification in the equations

Einstein Field Equations - > Friedmann Equations

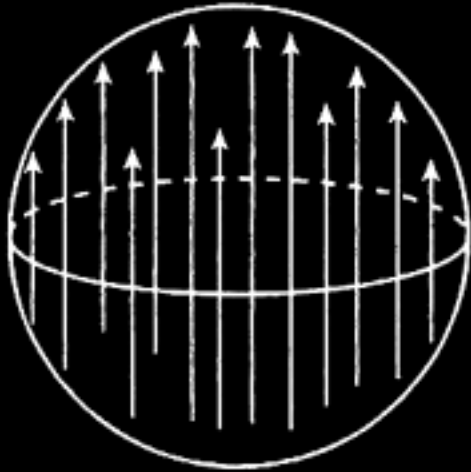
Scale factor  $a(t)$

$$\Omega_M + \Omega_K + \Omega_\Lambda = 1$$

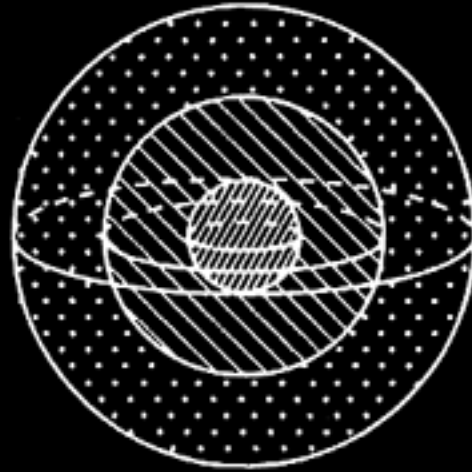
The cosmic sum rule

# The cosmological principle

The Universe is sensibly **isotropic** and homogenous when **averaged** on large scales



Homogeneous  
Not isotropic



Isotropic  
Not homogeneous

No special positions or directions in the Universe.  
“The universe presents the same general aspect at every point”

Edward Arthur Milne

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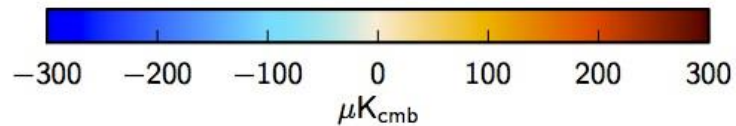
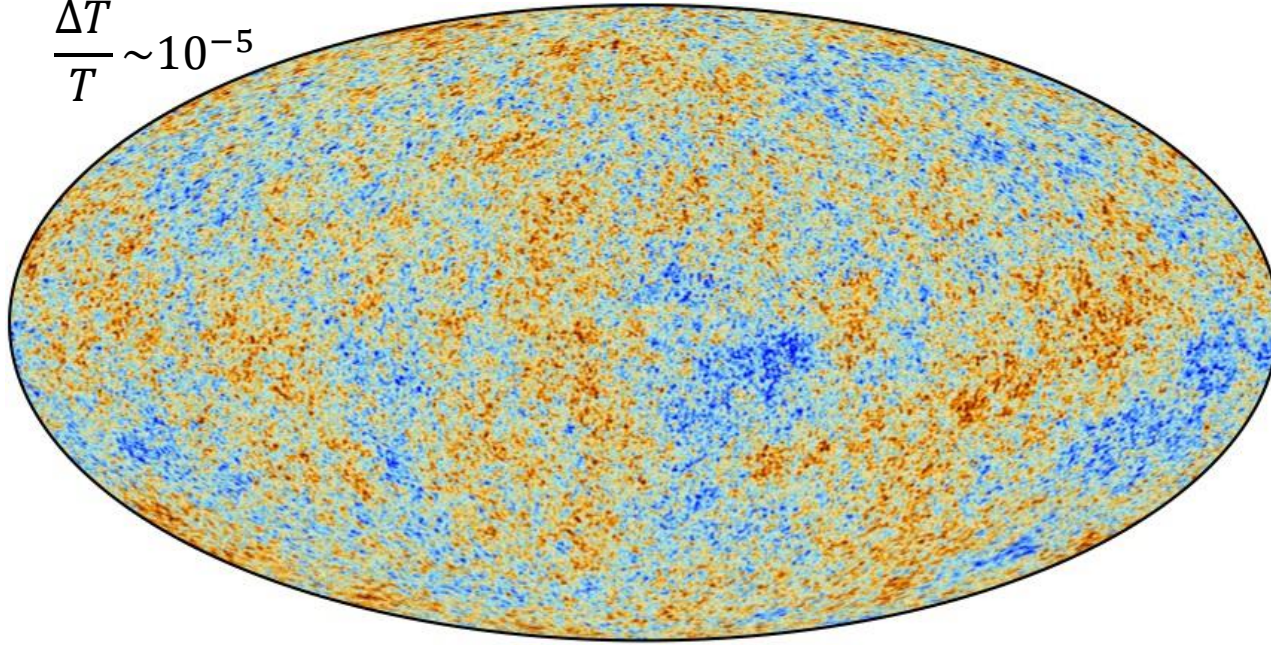
The real reason, though, for our adherence here to the Cosmological Principle is not that it is surely correct, but rather, that it allows us to make use of the extremely limited data provided to cosmology by observational astronomy. ...

... If the data will not fit into this framework, we shall be able to conclude that either the Cosmological Principle or the Principle of Equivalence is wrong. Nothing could be more interesting.

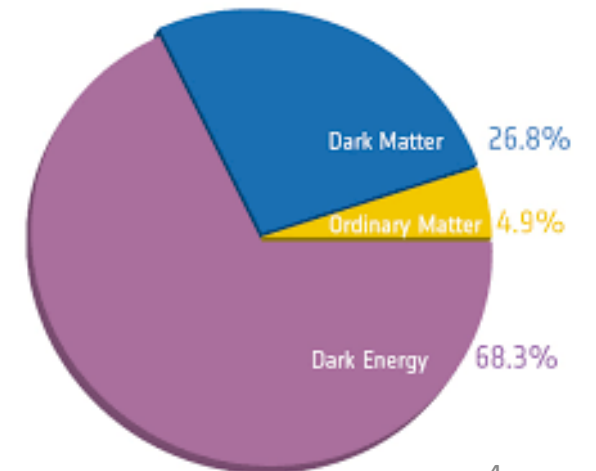
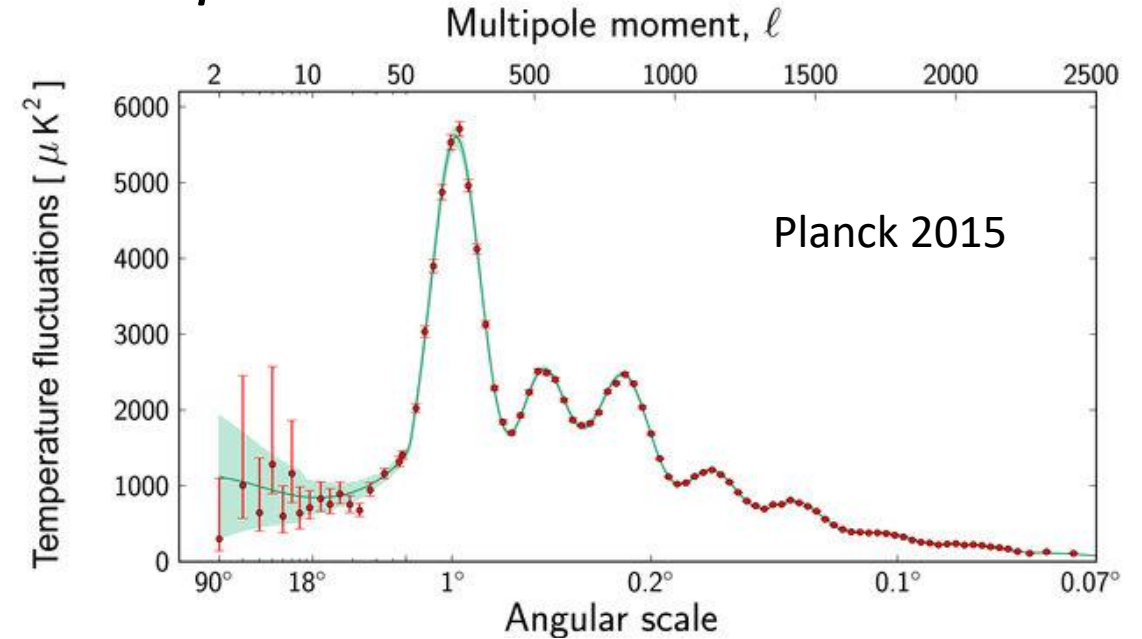
Steven Weinberg, *Gravitation and Cosmology* (1972)

*“Data from the Planck satellite show the Universe to be highly isotropic”*

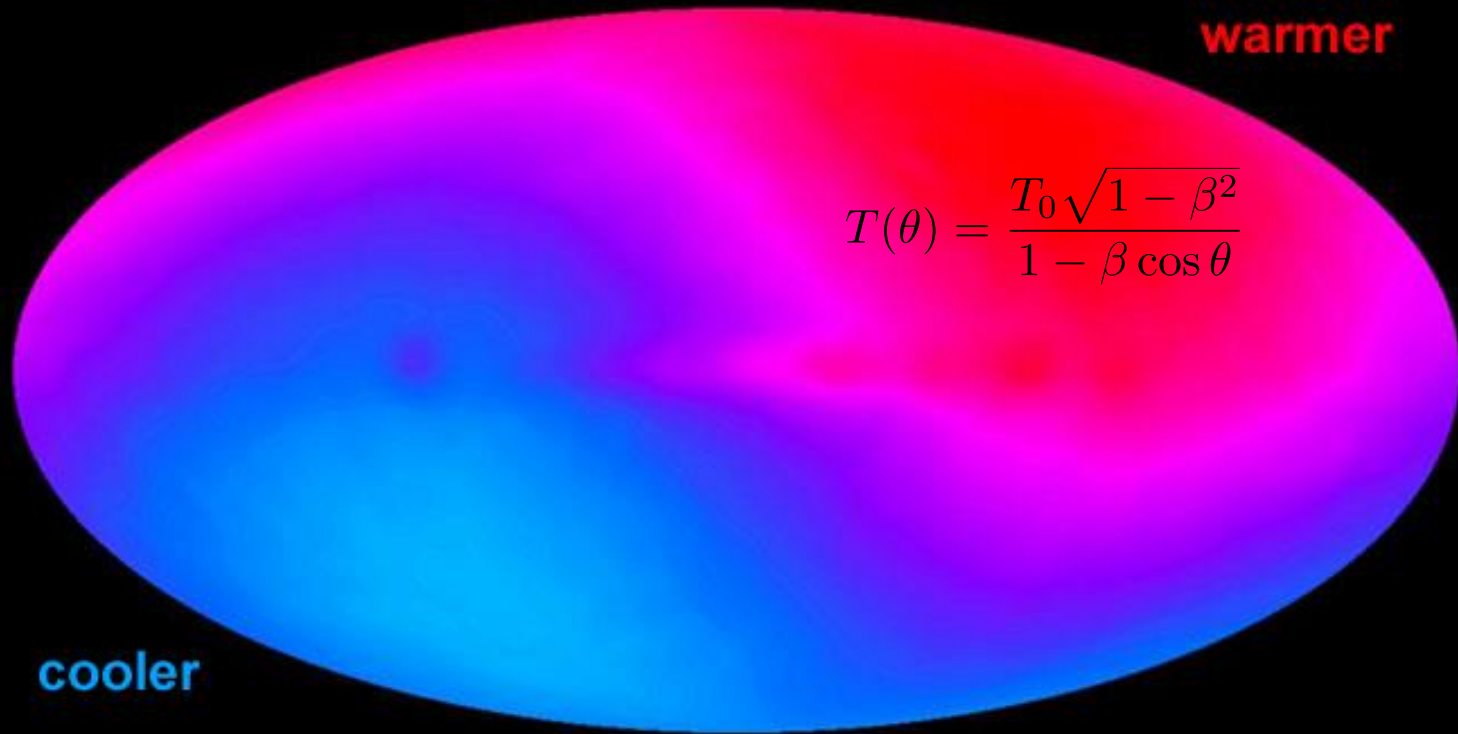
$$T = 2.725 \text{ K}$$
$$\frac{\Delta T}{T} \sim 10^{-5}$$



We observe a **statistically isotropic** Gaussian random field of small temperature fluctuations (fully quantified by the 2-point correlations  $\rightarrow$  angular power spectrum)



# The CMB Dipole : Purely Kinematic?



Net motion of the Solar System barycentre:  
369 +/- 2 km/s w.r.t 'CMB rest frame'  
towards

R.A = 168.0, DEC = -7.0

Is this 'Purely Kinematic'?

What is the origin of this motion?

COBE Experiment, 1996

Planck 2015

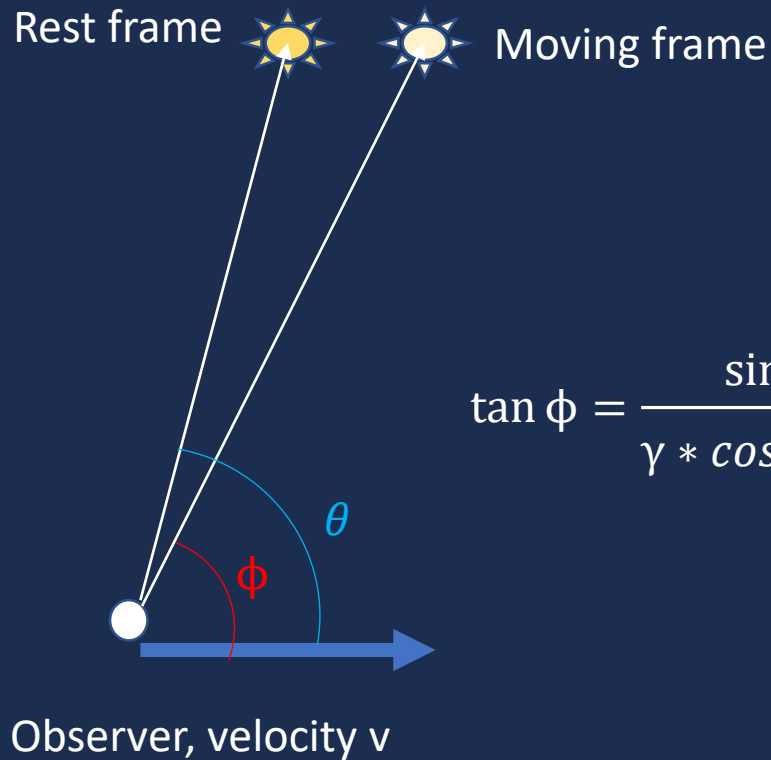
$$\frac{\Delta T}{T} \sim 10^{-3}$$

# A moving observer - Kinematic Dipole

$$\sigma(\theta)_{obs} = \sigma_{rest} \left[ 1 + \left[ 2 + x(1 + \alpha) \right] \frac{v}{c} \cos(\theta) \right]$$

Ellis & Baldwin (1984)

## Aberration



$$\tan \phi = \frac{\sin \theta}{\gamma * \cos \theta - \frac{v}{c}}$$

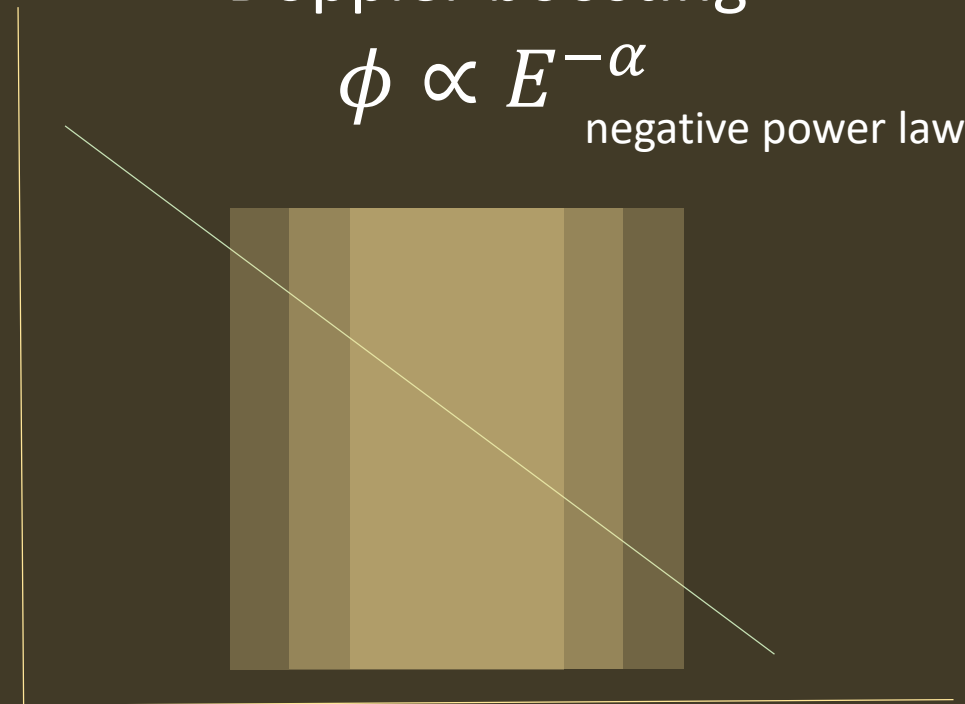
+

## Doppler boosting

$$\phi \propto E^{-\alpha}$$

negative power law

Differential flux



Energy

Flux limited catalog -> more sources in direction of motion

# On the expected anisotropy of radio source counts

G. F. R. Ellis<sup>\*</sup> and J. E. Baldwin<sup>†</sup> *Orthodox Academy of Crete, Kolymbari, Crete*

Received 1983 May 31; in original form 1983 March 31

**Summary.** If the standard interpretation of the dipole anisotropy in the microwave background radiation as being due to our peculiar velocity in a homogeneous isotropic universe is correct, then radio-source number counts must show a similar anisotropy. Conversely, determination of a dipole anisotropy in those counts determines our velocity relative to their rest frame;

Needs a million sources to detect the CMB dipole velocity



380 *G. F. R. Ellis and J. E. Baldwin*

amplitude  $D$  of the quasi-sinusoidal output of the interferometer provides information on the source population at flux densities where there is approximately one source per beam area,  $S \approx 0.2$  Jy, about 10 times deeper than the catalogue for the 4C data. It is the large number of beam areas in the survey, about  $9.5 \times 10^4$ , which provides the good statistical accuracy which is necessary for our purposes. Hughes & Longair (1967) analysed these data for evidence of anisotropy in the source population. They found none, but again did not set a numerical limit on any dipole anisotropy present. Analysis of the data in their table 1 on the median values of  $D$  in areas  $2^h$  in RA by  $10^\circ$  in Dec, for a dipole term aligned with a maximum at Dec  $0^\circ$ , gives an amplitude of the dipole anisotropy of  $(6.9 \pm 5.6) \times 10^{-3}$  in a direction towards RA  $01^h.7$ . The quoted error is again the statistical error arising from the finite number of independent values of  $D$ . In practice the uncertainty in the constancy of the calibration of sensitivity throughout the  $24^h$  of RA is of comparable magnitude. The effects of motion of the observer relative to the source population discussed above are

# On the expected anisotropy of radio source counts

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380 *G. F. R. Ellis and J. E. Baldwin*

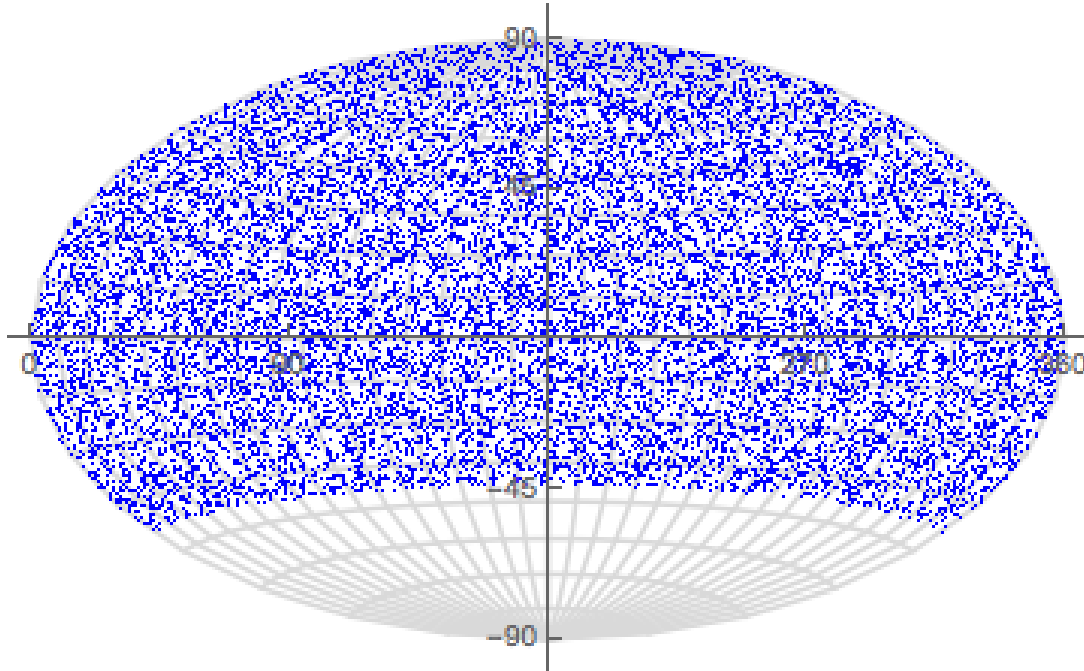
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The situation anticipated by Ellis and Baldwin in 1984 now confronts us!



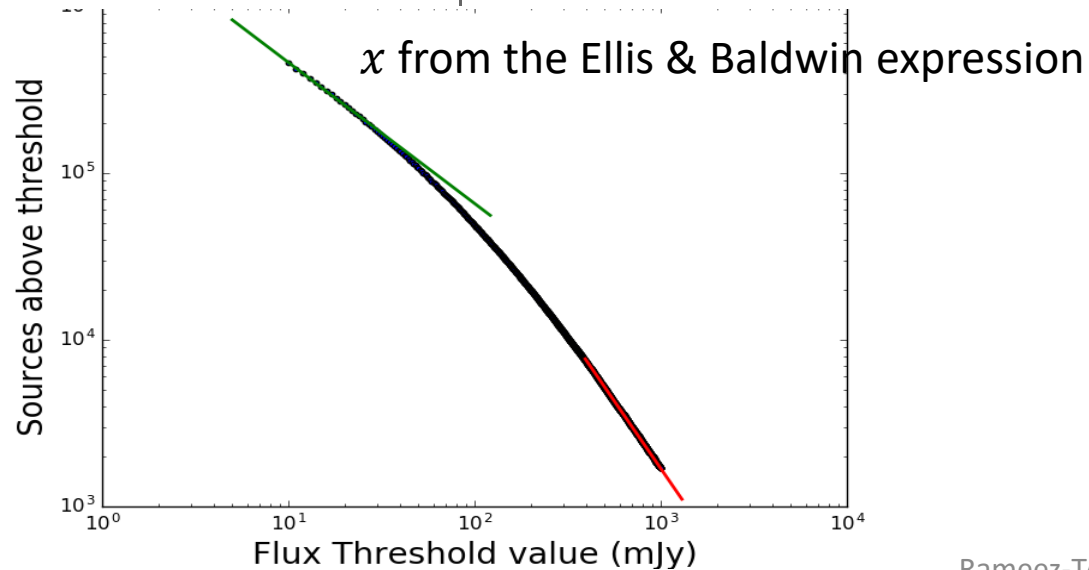
# Ellis & Baldwin tests : The Cosmic Dipole Anomaly

# The NRAO VLA Sky Survey (NVSS)



1.4 GHz survey of the Northern sky, by the National Radio Astronomy Observatory. Down to dec =  $-40.4^\circ$

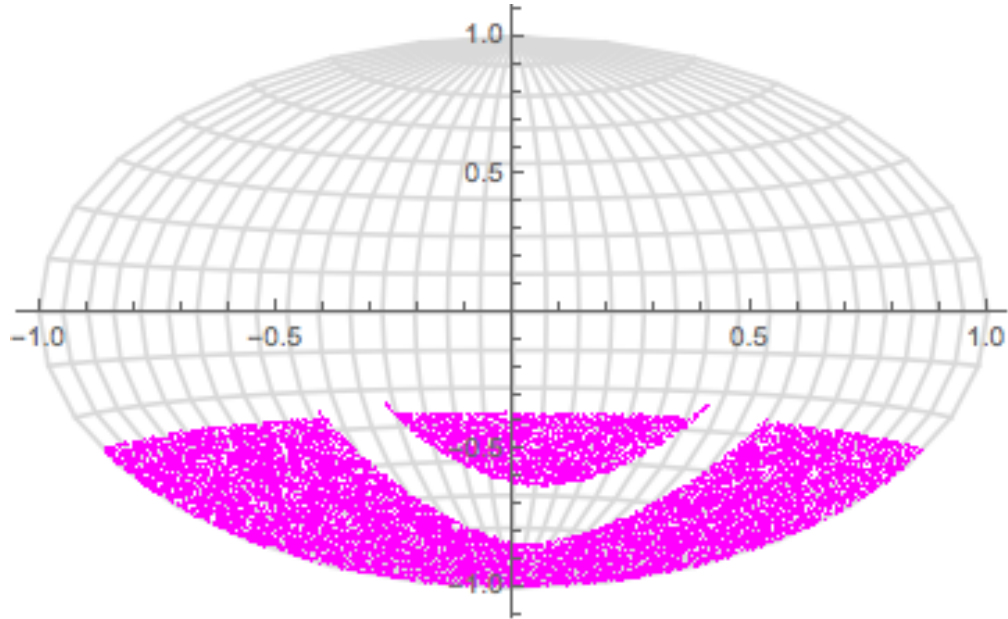
1,773,488 sources above 2.5 mJy. But 'complete' with uniform sky exposure only above 10 mJy



Phys. Rev. D, 78, 043519

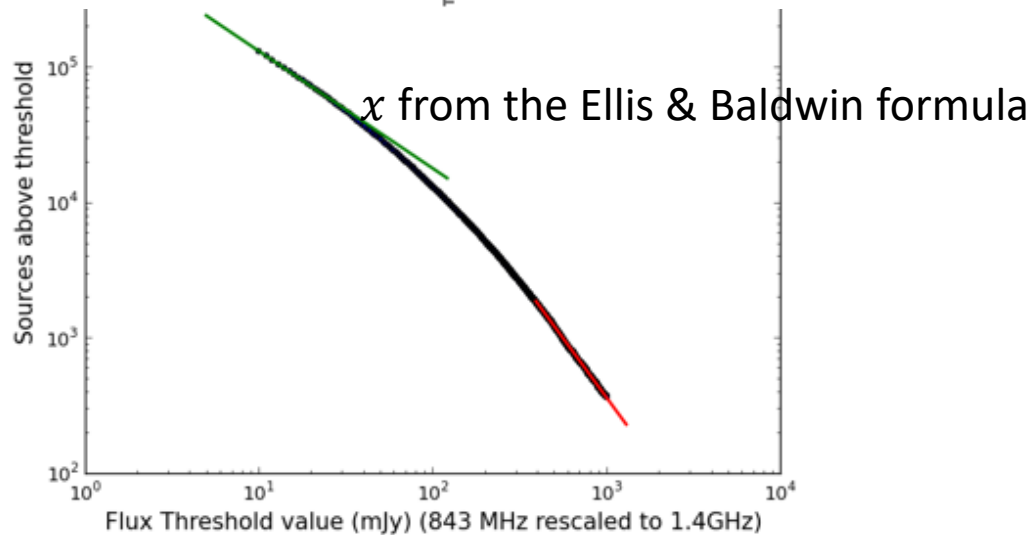
First seen by Singal, A. K. 2011, ApJL, 742, L23,

# Sydney University Molonglo Sky Survey (SUMSS)

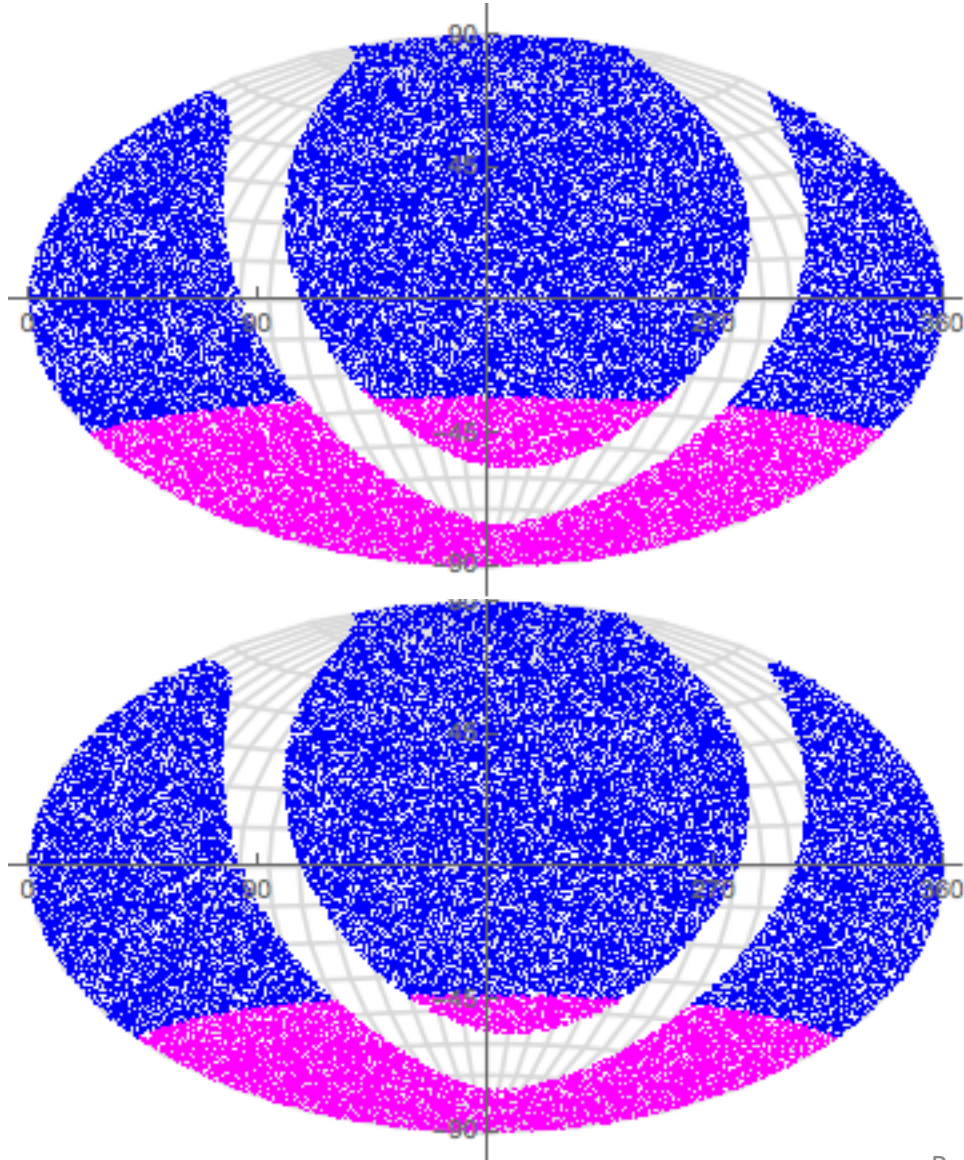


843 MHz survey of the Southern sky, by the Molonglo Observatory Synthesis telescope. Dec  $< -30.0^\circ$

211050 radio sources. Similar sensitivity and resolution to NVSS

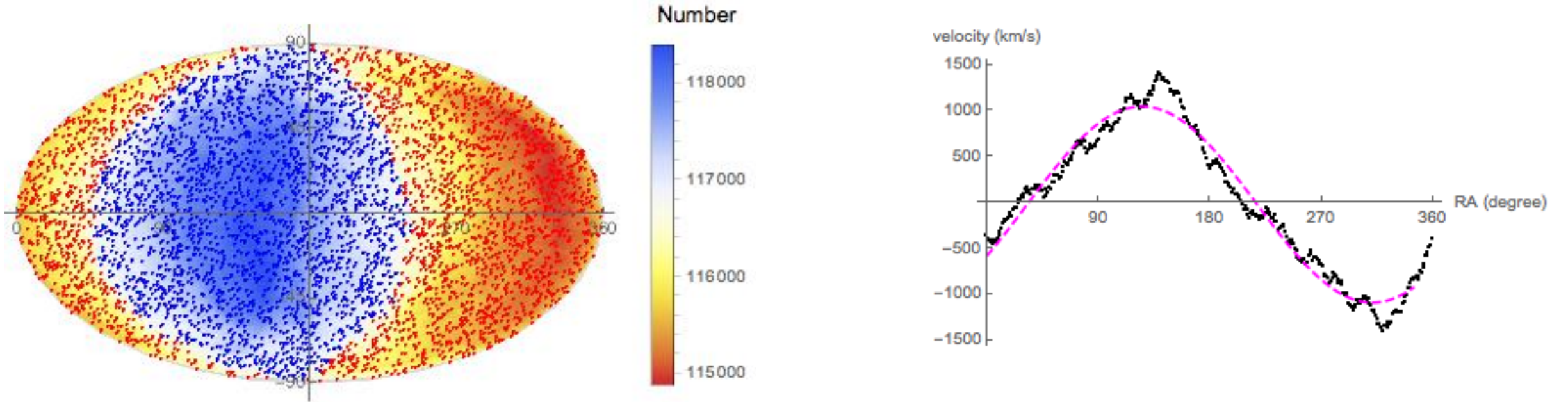


# The NVSUMSS-Combined All Sky catalog



- Rescale SUMSS fluxes by  $(843/1400)^{-0.75}$
- Remove Galactic Plane at  $\pm 10$  degree in NVSS
- Remove NVSS sources below and SUMSS sources above dec -30 (or -40)
- Apply common threshold flux cut on both samples
- $z \sim 1$

# Results



Velocity  $\sim 1355 \pm 351$  km/s, Dir within  $10^\circ$  of CMB dipole direction.

Statistical significance,  $\sim 2.81$  Sigma, with the 3D linear estimator, constrained mainly by the catalogue size

**Bengaly et al 2018 JCAP 1804 (2018) no.04, 031 find a 5.1 sigma excess in TGSS !**

**SKA phase 1 measurement  $\sim 10\%$**

**Bengaly (et al) 2018 MNRAS, 486, Issue 1 (2019) 1350-1357**

*“We conclude that for all analysed surveys, the observed Cosmic Radio Dipole amplitudes **exceed the expectation, derived from the CMB dipole.**”*

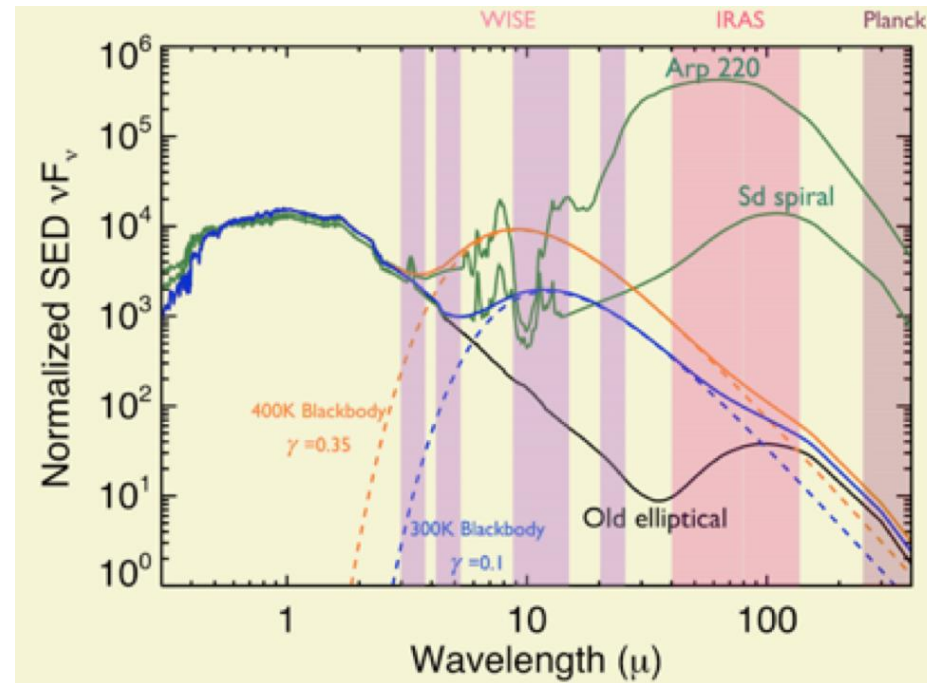
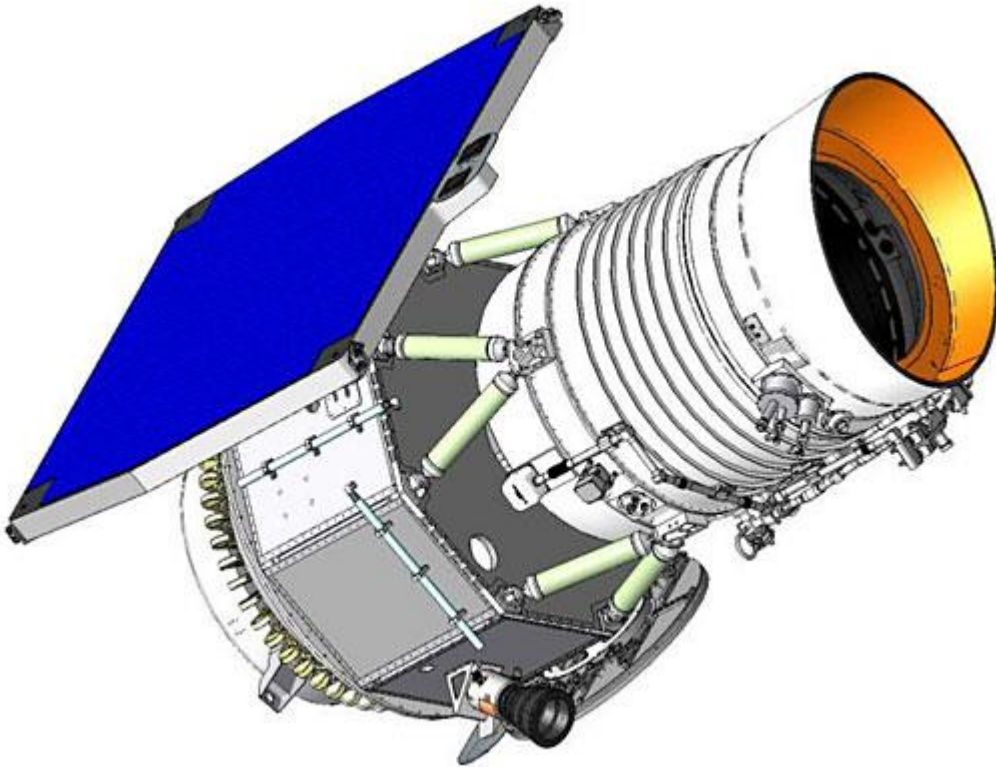
**Siewert et al 2020, Astron.Astrophys. 653 (2021) A9**

# The Widefield Infrared Survey Explorer

All sky infrared survey over 10 months, in the bands 3.4, 4.6, 12 and 22  $\mu\text{m}$  using a 40 cm diameter telescope







Generated a catalog of 746 million+ objects, most of which are stars.

Directionally unbiased survey strategy, arc second angular resolution, multi band photometry.



## OPEN ACCESS

## A Test of the Cosmological Principle with Quasars

Nathan J. Secrest<sup>1</sup> , Sebastian von Hausegger<sup>2,3,4</sup> , Mohamed Rameez<sup>5</sup> ,  
Roya Mohayaee<sup>3</sup> , Subir Sarkar<sup>4</sup> , and Jacques Colin<sup>3</sup> 

Published 2021 February 25 • © 2021. The Author(s). Published by the American Astronomical Society.

[The Astrophysical Journal Letters](#), [Volume 908](#), [Number 2](#)

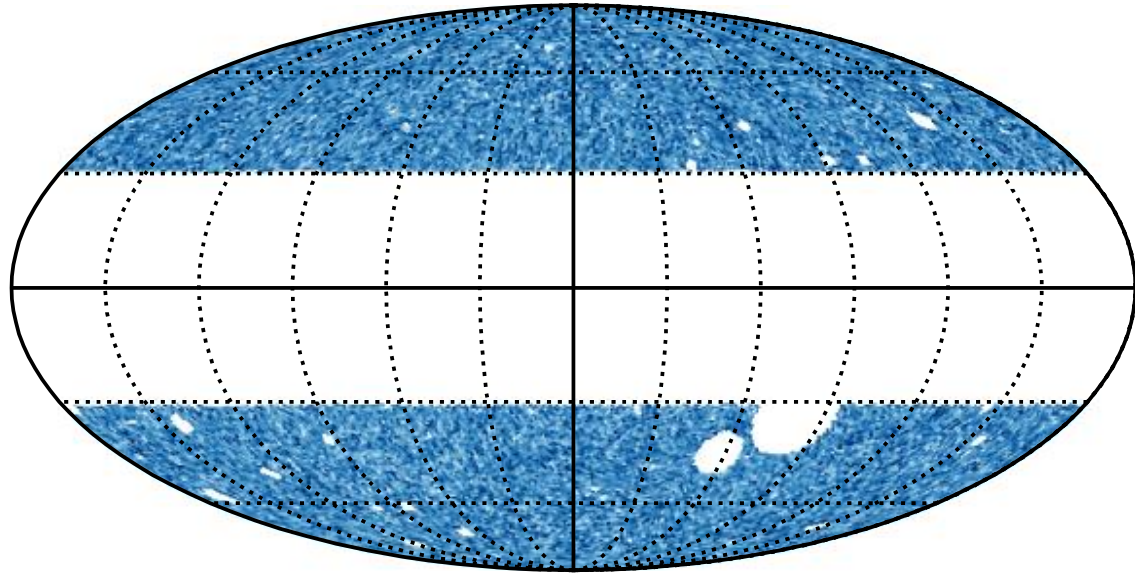
**Citation** Nathan J. Secrest *et al* 2021 *ApJL* **908** L51

**DOI** 10.3847/2041-8213/abdd40

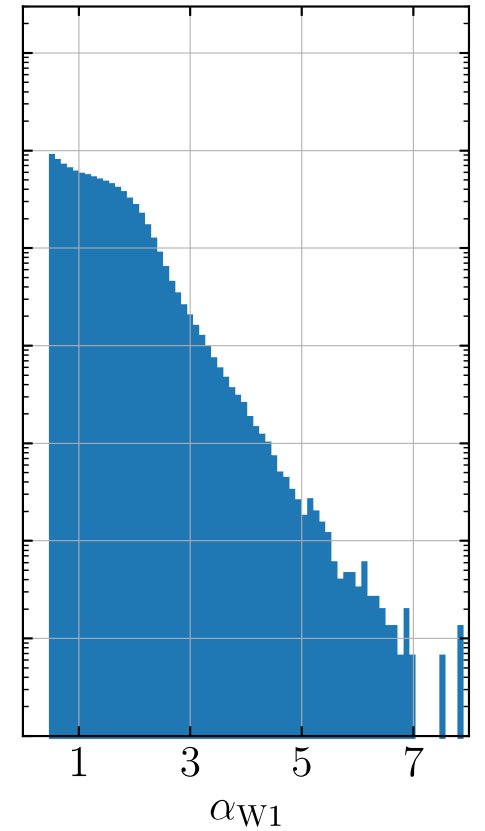
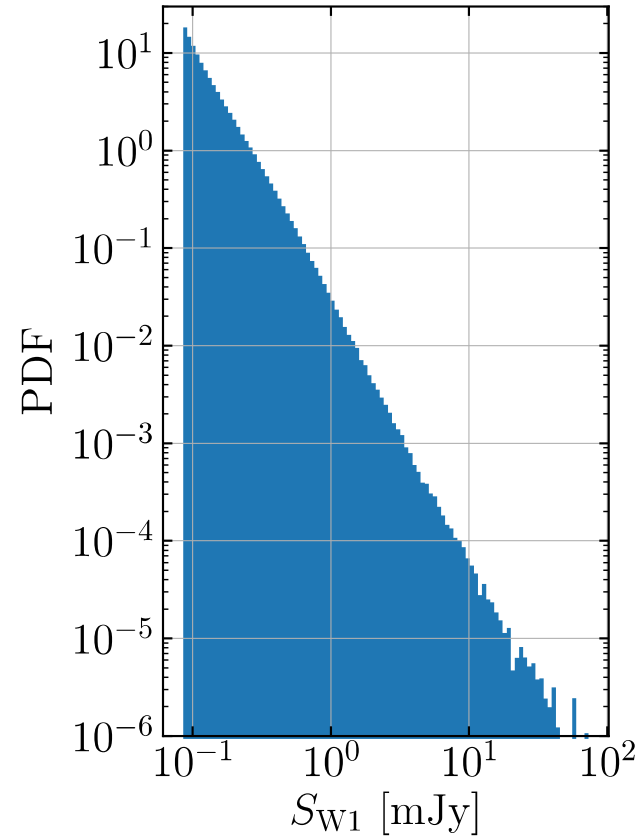
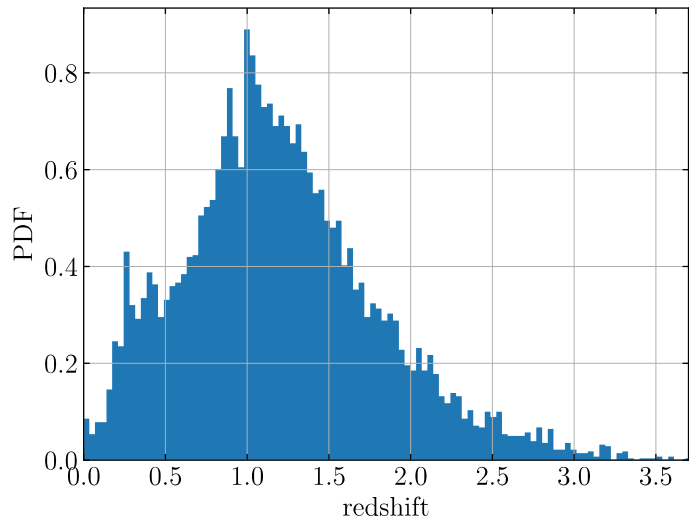
### ABSTRACT

We study the large-scale anisotropy of the Universe by measuring the dipole in the angular distribution of a flux-limited, all-sky sample of 1.36 million quasars observed by the Wide-field Infrared Survey Explorer (WISE). This sample is derived from the new CatWISE2020 catalog, which contains deep photometric measurements at 3.4 and 4.6  $\mu\text{m}$  from the cryogenic, post-cryogenic, and reactivation phases of the WISE mission. While the direction of the dipole in the quasar sky is similar to that of the cosmic microwave background (CMB), its amplitude is over twice as large as expected, rejecting the canonical, exclusively kinematic interpretation of the CMB dipole with a p-value of  $5 \rightarrow 10^{-7}$  ( $4.9\sigma$  for a normal distribution, one-sided), the highest significance achieved to date in such studies. Our results are in conflict with the cosmological principle, a foundational assumption of the concordance  $\Lambda$ -CDM model.

# CatWISE AGN 1355352 sources



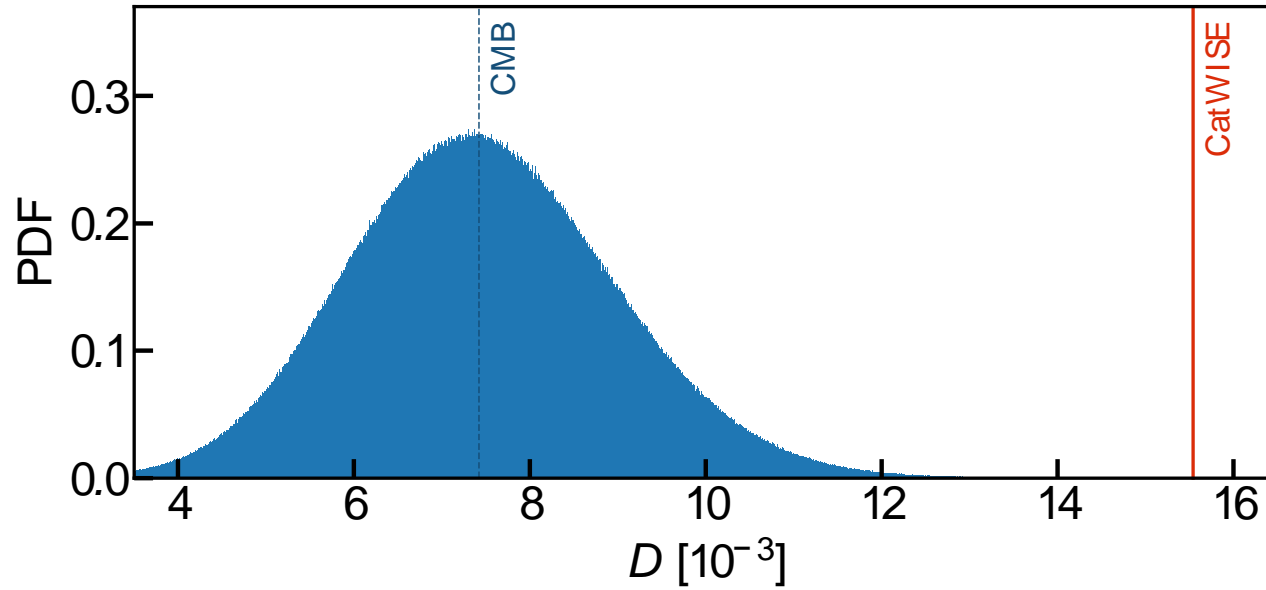
30 source  $\text{deg}^{-2}$  90



*Astrophys.J.Lett.* 908 (2021) 2, L51

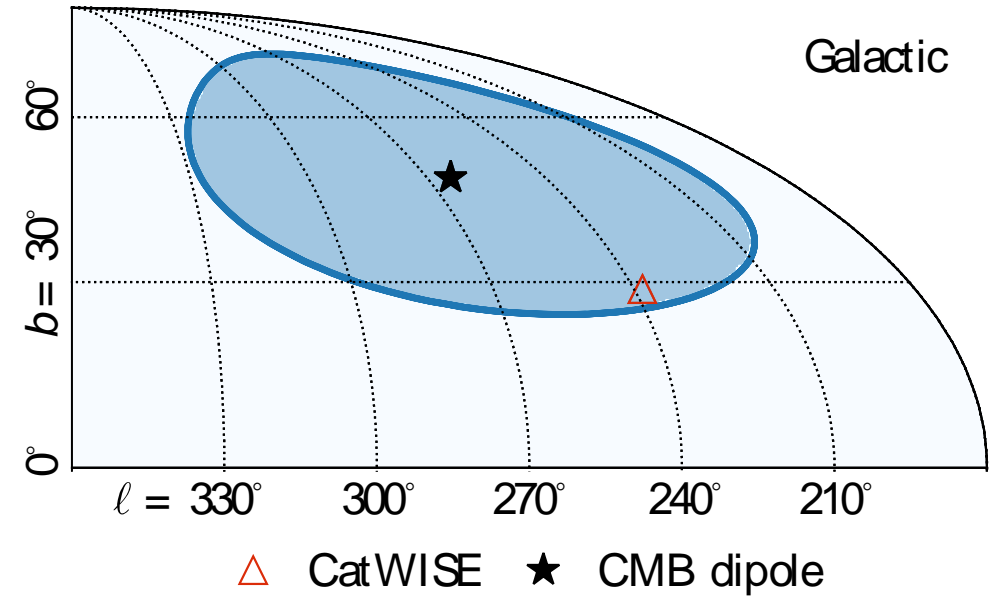


# Results

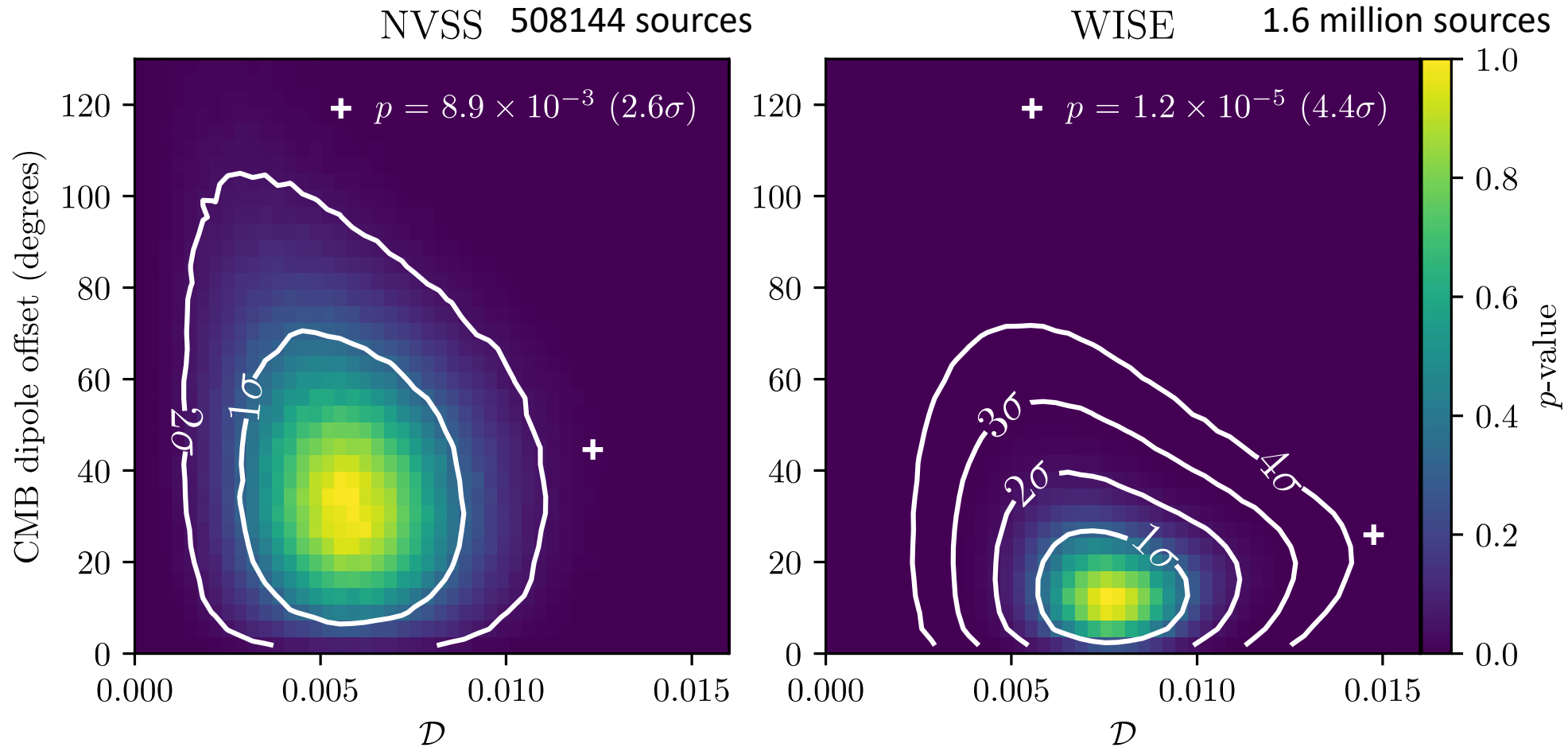


$$p = 5 \times 10^{-7} (4.9 \sigma)$$

Obtained by scrambling the data itself,  
frequentist null hypothesis testing,



Open Science <https://zenodo.org/record/4448512>



Conservative Sample size weighted Z-scores :  $5.1 \sigma$

*Astrophys.J.Lett.* 937 (2022) L31  
<https://zenodo.org/record/6784602>

Also in a sample of  $z \sim 0.2$  galaxies  
*Mon.Not.Roy.Astron.Soc.* 477 (2018) 2, 1772-1781 (backup slides)

# Testing the Cosmological Principle with CatWISE Quasars: A Bayesian Analysis of the Number-Count Dipole

Lawrence Dam<sup>1,2,\*</sup>, Geraint F. Lewis<sup>1,†</sup> & Brendon J. Brewer<sup>3</sup>

<sup>1</sup>*Sydney Institute for Astronomy, School of Physics, A28, The University of Sydney, NSW 2006, Australia*

<sup>2</sup>*Département de Physique Théorique and Center for Astroparticle Physics, Université de Genève, 24 quai Ernest-Ansermet, 1211 Genève 4, Switzerland*

<sup>3</sup>*Department of Statistics, The University of Auckland, Private Bag 92019, Auckland 1142, New Zealand*

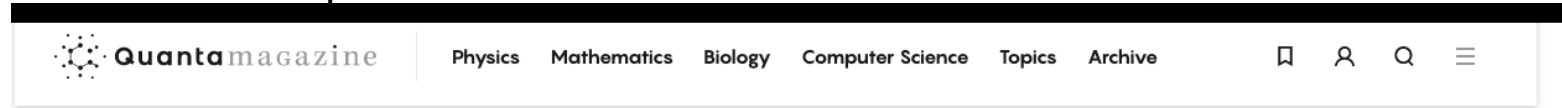
Accepted XXX. Received YYY; in original form ZZZ

## ABSTRACT

The Cosmological Principle, that the Universe is homogeneous and isotropic on sufficiently large scales, underpins the standard model of cosmology. However, a recent analysis of 1.36 million infrared-selected quasars has identified a significant tension in the amplitude of the number-count dipole compared to that derived from the CMB, thus challenging the Cosmological Principle. Here we present a Bayesian analysis of the same quasar sample, testing various hypotheses using the Bayesian evidence. We find unambiguous evidence for the presence of a dipole in the distribution of quasars with a direction that is consistent with the dipole identified in the CMB. However, the amplitude of the dipole is found to be 2.7 times larger than that expected from the conventional kinematic explanation of the CMB dipole, with a statistical significance of  $5.7\sigma$ . To compare these results with theoretical expectations, we sharpen the  $\Lambda$ CDM predictions for the probability distribution of the amplitude, taking into account a number of observational and theoretical systematics. In particular, we show that the presence of the galactic plane mask causes a considerable loss of dipole signal due to a leakage of power into higher multipoles, exacerbating the discrepancy in the amplitude. By contrast, we estimate using probabilistic arguments that the source evolution of quasars improves the discrepancy, but only mildly so. These results support the original findings of an anomalously large quasar dipole, independent of the statistical methodology used.



## The response

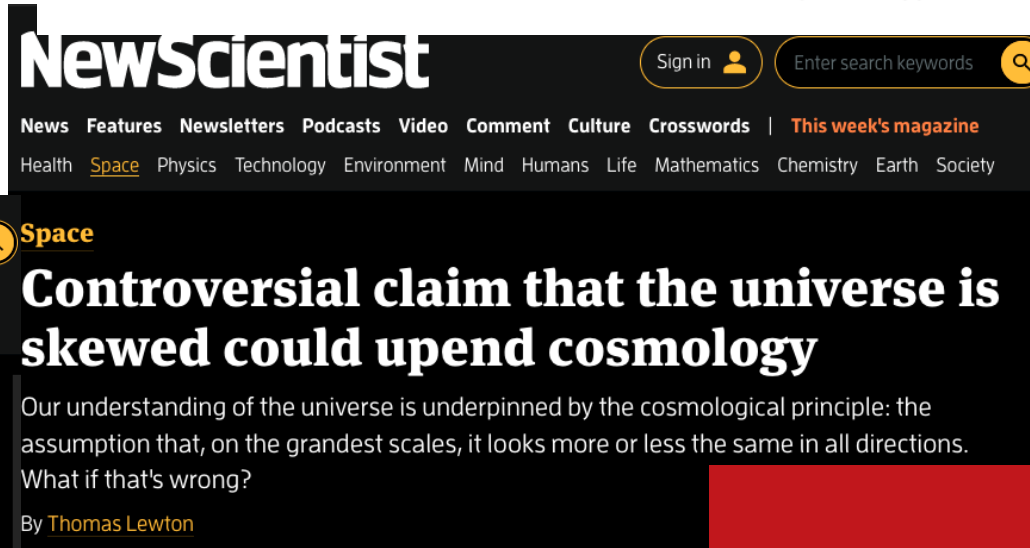
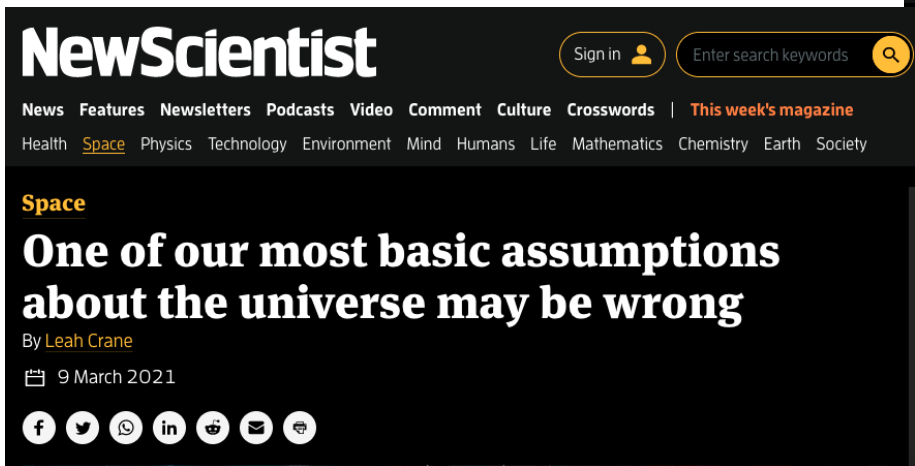


COSMOLOGY

### Cosmologists Parry Attacks on the Vaunted Cosmological Principle

27

A central pillar of cosmology — the universe is the same everywhere and in all directions — is surviving a storm of possible evidence against it.



THE SCIENCES

### Is the Universe Different In Different Directions?

29/04/2021

Now known by the community as the “Cosmic Dipole Anomaly”

# Dipole Cosmology: The Copernican Paradigm Beyond FLRW

Chethan KRISHNAN<sup>a\*</sup>, Ranjini MONDOL<sup>a†</sup>, M. M. SHEIKH-JABBARI<sup>b‡</sup>

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Indian Institute of Science, Bangalore 560012, India

<sup>b</sup> School of Physics, Institute for Research in Fundamental Sciences (IPM),  
P. O. Box 19395-5531, Tehran, Iran

## SO(3) → U(1), tilted Bianchi V/VII<sub>h</sub> - 4 Friedmann like equations

### Large-scale geometry of the Universe

Yassir Awwad<sup>◆</sup> and Tomislav Prokopec<sup>◇</sup>

<sup>◇</sup> Institute for Theoretical Physics, Spinoza Institute & EMMEΦ  
Utrecht University, Princetonplein 5, 3584 CC Utrecht, The Netherlands

## Thursten Perelman theorem -> anisotropic Thursten geometries should be considered on par with Friedmann geometry

### Spatially Homogeneous Universes with Late-Time Anisotropy

Andrei Constantin<sup>Ⓞ,1,\*</sup> Thomas R. Harvey<sup>Ⓞ,1,†</sup> Sebastian von Hausegger<sup>Ⓞ,2,‡</sup> and Andre Lukas<sup>Ⓞ,1,§</sup>

<sup>1</sup>Rudolf Peierls Centre for Theoretical Physics, University of Oxford, Parks Road, Oxford, UK

<sup>2</sup>Astrophysics, University of Oxford, Denys Wilkinson Building, Keble Road, Oxford, UK

"Standard cosmology would then need a drastic revision, with implications for DM."  
Cirelli, Strumia and Zupan 2024

# QCD axion dark matter and the cosmic dipole anomaly

Chengcheng Han<sup>1,\*</sup>

<sup>1</sup>School of Physics, Sun Yat-Sen University, Guangzhou 510275, China  
(Dated: November 29, 2022)

Highlighted by PDG 2022 as one of the principal anomalies in Cosmology.



Journal of High Energy Astrophysics

Volume 34, June 2022, Pages 49-211



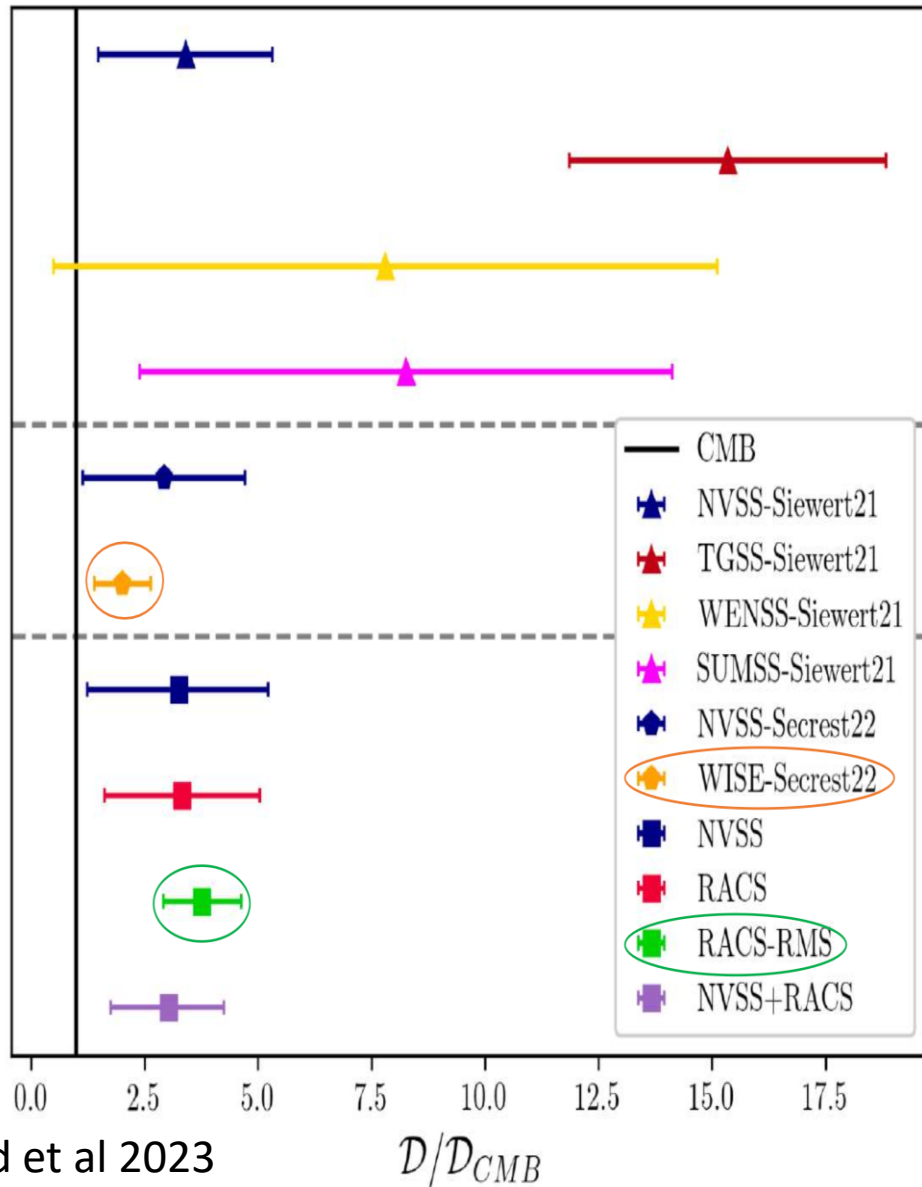
Review

## Cosmology intertwined: A review of the particle physics, astrophysics, and cosmology associated with the cosmological tensions and anomalies

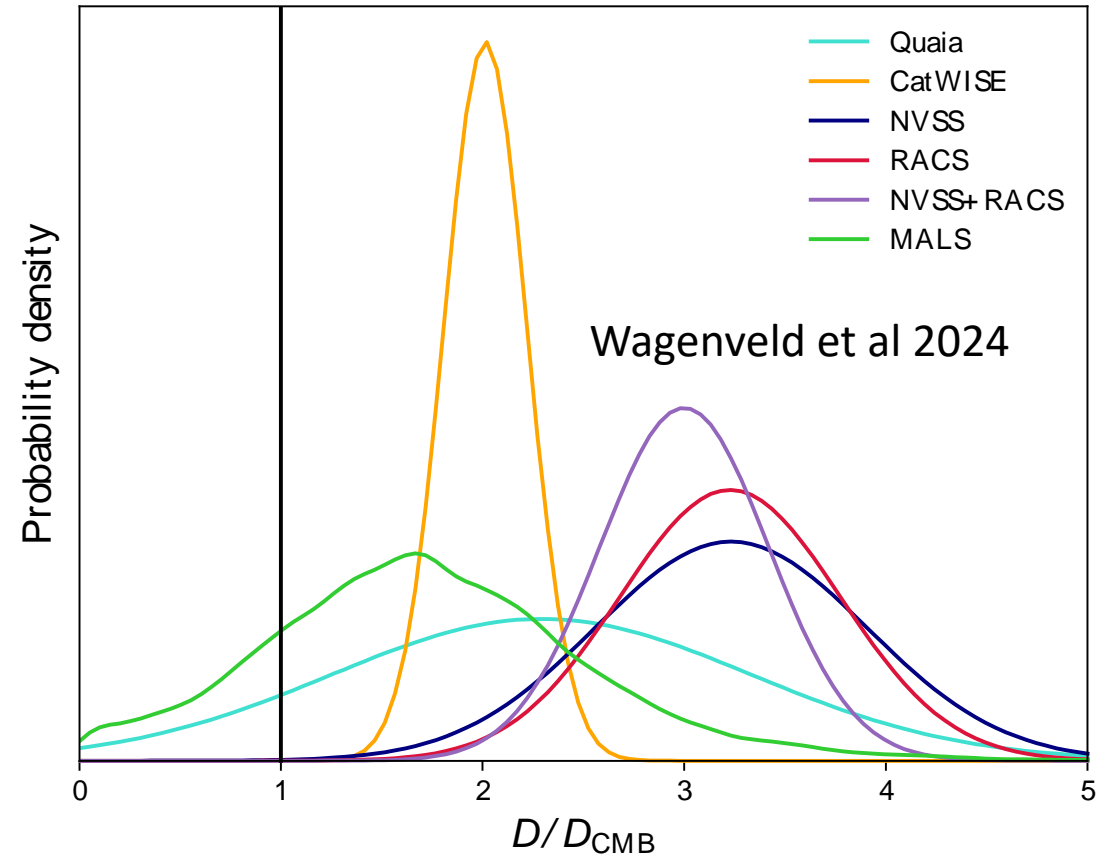
[Elcio Abdalla](#)<sup>a</sup>, [Guillermo Franco Abellán](#)<sup>b</sup>, [Amin Aboubrahim](#)<sup>c</sup>, [Adriano Agnello](#)<sup>d</sup>, [Özgür Akarsu](#)<sup>e</sup>, [Yashar Akrami](#)<sup>f g h i</sup>, [George Alestas](#)<sup>j</sup>, [Daniel Aloni](#)<sup>k</sup>, [Luca Amendola](#)<sup>l</sup>, [Luis A. Anchordoqui](#)<sup>m n o</sup>, [Richard I. Anderson](#)<sup>p</sup>, [Nikki Arendse](#)<sup>q</sup>, [Marika Asgari](#)<sup>r s</sup>, [Mario Ballardini](#)<sup>t u v w</sup>, [Vernon Barger](#)<sup>x</sup>, [Spyros Basilakos](#)<sup>y z</sup>, [Ronaldo C. Batista](#)<sup>aa</sup>, [Elia S. Battistelli](#)<sup>ab ac</sup>, [Richard Battye](#)<sup>ad</sup>, [Micol Benetti](#)<sup>ae af</sup> ... [Miguel Zumalacárregui](#)<sup>aw</sup>

Cosmic Dipole Anomaly, right beside the Hubble tension  
Peebles 2022, 2024

THE COSMIC RADIO DIPOLE: BAYESIAN ESTIMATORS ON NEW AND OLD RADIO SURVEYS



Wagenveld, Klöckner, Schwarz, A&A 675:A72, 2023



10+ papers that claim consistency with the kinematic expectation in **other** datasets.

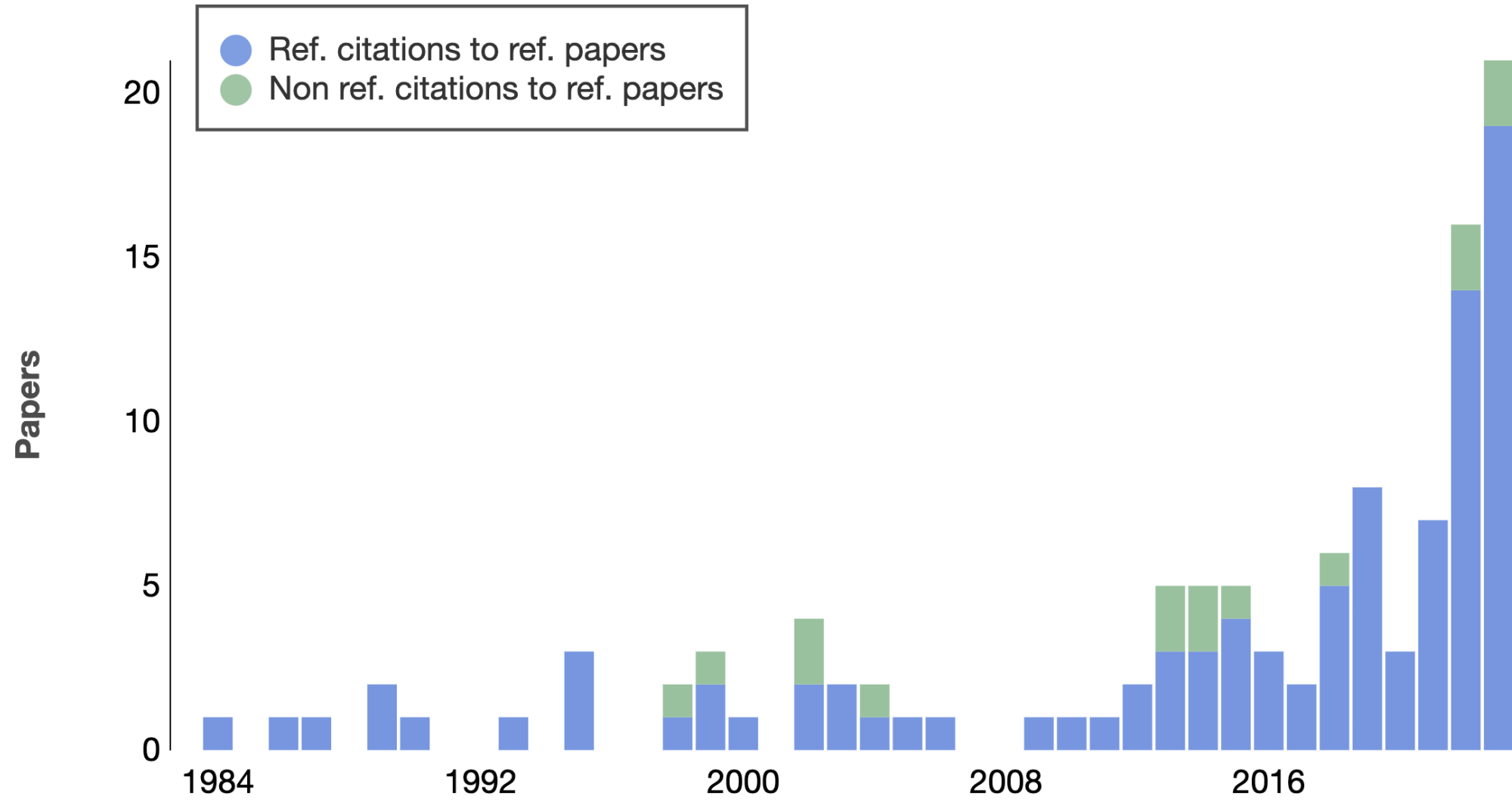
Watch out for upcoming RevModPhys review.

SKA, Euclid, SphereX

Dipole amplitudes with **3 $\sigma$**  uncertainties compared to the amplitude expected from the CMB

# Citations to Ellis & Baldwin 1984

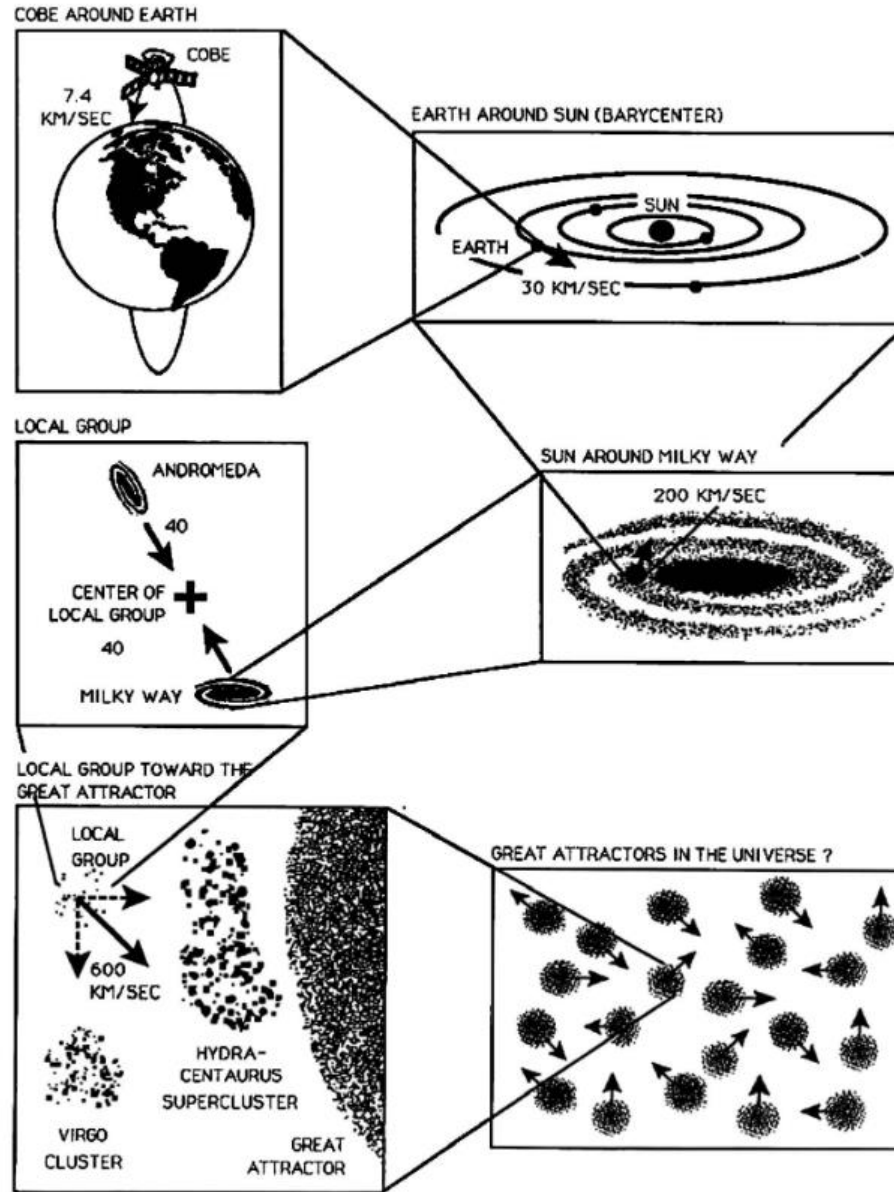
stacked  grouped



# Bulk flows and a tilted Universe in SNe 1a

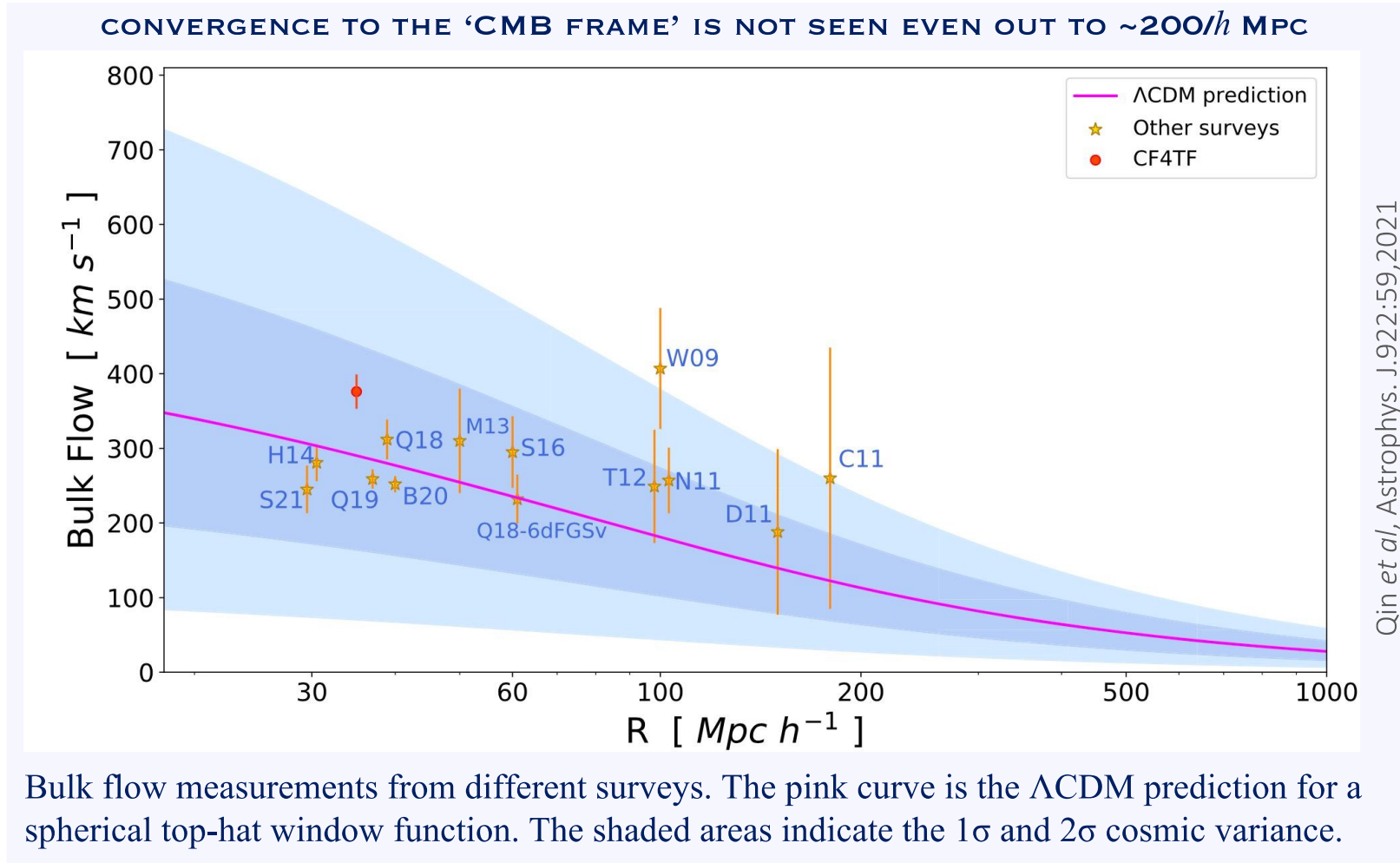
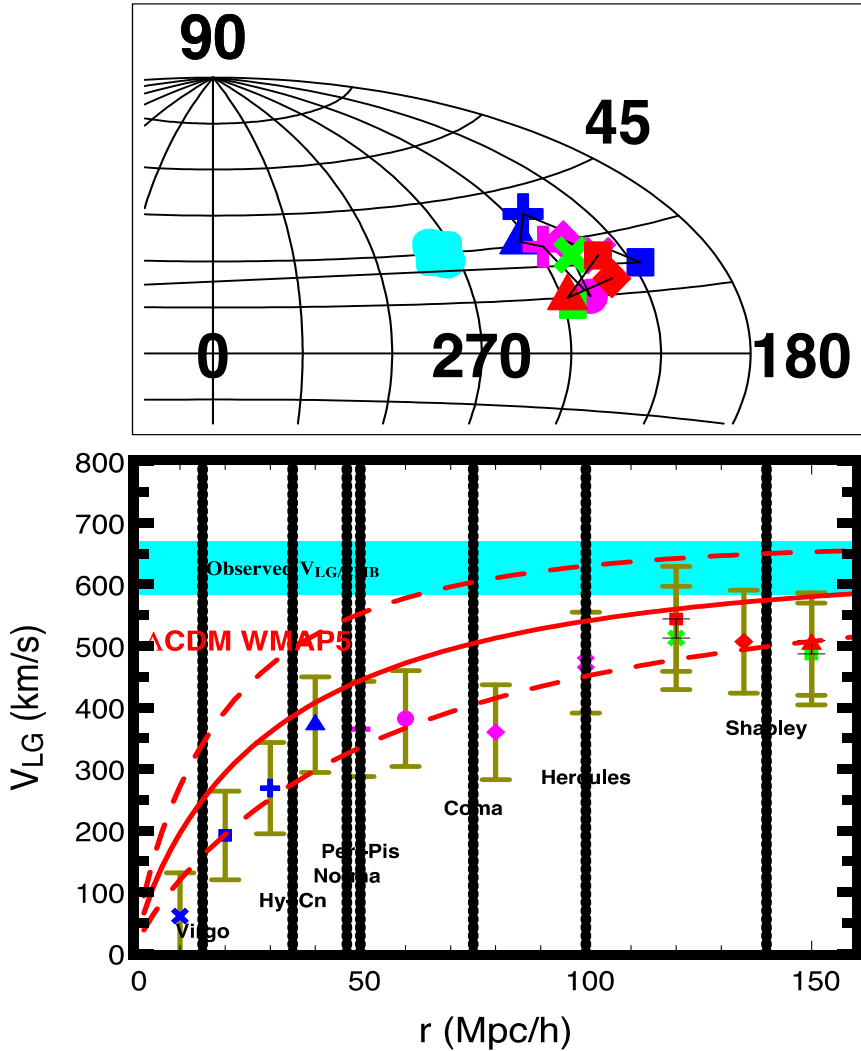


# VELOCITY COMPONENTS OF THE OBSERVED CMB DIPOLE



George Smoot, Nobel Lecture, 8 Dec 2006

# Where is the cosmic 'rest frame'?



G. Lavaux, R. Brent Tully, R. Mohayaee, S. Colombi

• *Astrophys.J.* 709 (2010) 483-498

LETTER TO THE EDITOR

# Gravity in the Local Universe: density and velocity fields using CosmicFlows-4

H.M. Courtois<sup>\*1</sup>, A. Dupuy<sup>2</sup>, D. Guinet<sup>1</sup>, G. Baulieu<sup>1</sup>, and F. Ruppin<sup>1</sup>

<sup>1</sup> Université Claude Bernard Lyon 1, IUF, IP2I Lyon, 69622 Villeurbanne, France

<sup>2</sup> Korea Institute for Advanced Study, 85, Hoegi-ro, Dongdaemun-gu, Seoul 02455, Republic of Korea

Received A&A Oct 31, 2022 - AA/2022/45331; Accepted date

## ABSTRACT

This article publicly releases three-dimensional reconstructions of the local Universe gravitational field below  $z=0.8$  that were computed using the full catalogue CosmicFlows-4 of 56,000 galaxy distances and its sub-sample of 1,008 type Ia supernovae distances. The article also provides some first CF4 measurements of the growth rate of structure using the pairwise correlation of peculiar velocities  $f\sigma_8 = 0.44(\pm 0.01)$  and of the bulk flow in the Local Universe of  $200 \pm 88 \text{ km s}^{-1}$  at distance  $300 h_{100}^{-1} \text{ Mpc}$ .

**Key words.** Cosmology: large-scale structure of Universe

# Analyzing the Large-Scale Bulk Flow using CosmicFlows4: Increasing Tension with the Standard Cosmological Model

Richard Watkins<sup>†,1</sup>, Trey Allen<sup>†</sup>, Collin James Bradford<sup>†</sup>, Albert Ramon Jr.<sup>†</sup>,  
Alexandra Walker<sup>†</sup>, Hume A. Feldman<sup>\*,2</sup>, Rachel Cionitti<sup>\*</sup>, Yara Al-Shorman  
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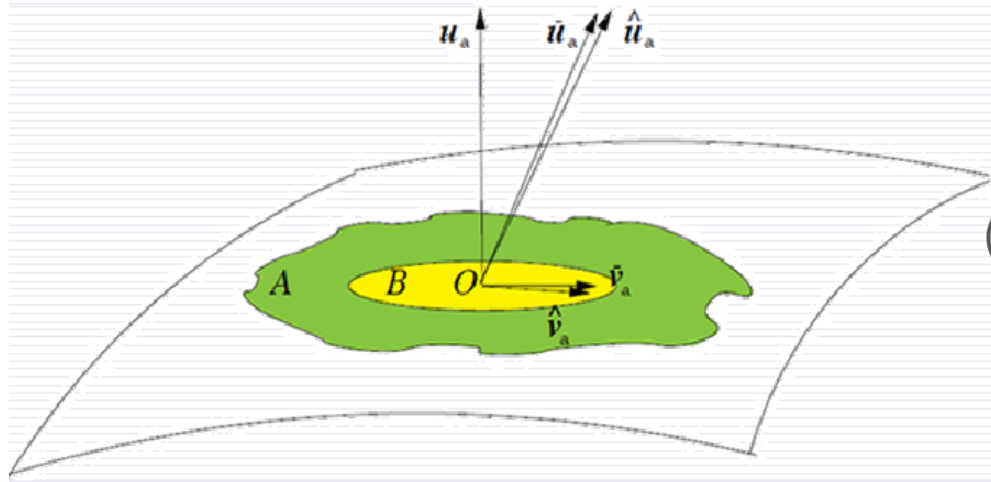
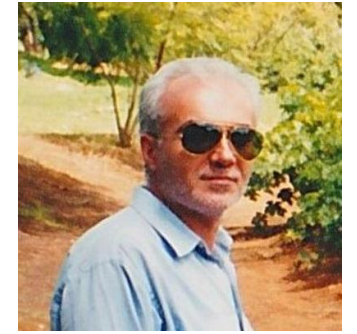
emails: <sup>1</sup>rwatkins@willamette.edu; <sup>2</sup>feldman@ku.edu

7 February 2023

## ABSTRACT

We present an estimate of the bulk flow in a volume of radii  $150-200h^{-1}\text{Mpc}$  using the minimum variance (MV) method with data from the *CosmicFlows-4* (CF4) catalog. The addition of new data in the CF4 has resulted in an increase in the estimate of the bulk flow in a sphere of radius  $150h^{-1}\text{Mpc}$  relative to the *CosmicFlows-3* (CF3). This bulk flow has less than a 0.03% chance of occurring in the Standard Cosmological Model ( $\Lambda\text{CDM}$ ) with cosmic microwave background derived parameters. Given that the CF4 is deeper than the CF3, we were able to use the CF4 to accurately estimate the bulk flow on scales of  $200h^{-1}\text{Mpc}$  (equivalent to 266 Mpc for Hubble constant  $H_o = 75 \text{ km/s/Mpc}$ ) for the first time. This bulk flow is in even greater tension with the Standard Model, having less than 0.003% probability of occurring. To estimate the bulk flow accurately, we introduce a novel method to calculate distances and velocities from distance moduli that is unbiased and accurate at all distances. Our results are completely independent of the value of  $H_o$ .

# The tilted Friedmann Universe



**If we are inside a large local ‘bulk flow’.**

(Tsagas 2010, 2011, 2012; Tsagas & Kadiltzoglou 2015, Tsagas 2019, 2021)

The patch A has mean peculiar velocity  $\tilde{v}_a$  with  $\vartheta = \tilde{D}^a v_a \gtrless 0$  and  $\dot{\vartheta} \gtrless 0$  (the sign depending on whether the bulk flow is accelerating or decelerating)

Inside region B, the r.h.s. of the expression

$$1 + \tilde{q} = (1 + q) \left(1 + \frac{\vartheta}{\Theta}\right)^{-2} - \frac{3\dot{\vartheta}}{\Theta^2} \left(1 + \frac{\vartheta}{\Theta}\right)^{-2}, \quad \tilde{\Theta} = \Theta + \vartheta,$$

drops below 1 and the observer ‘measures’ *negative* deceleration parameter in one direction of the sky – i.e. towards the CMB dipole

This implies that **observers** experiencing locally accelerated expansion, as a result of their own drift motion, may also find that the acceleration is maximised in one direction and minimised in the opposite. We argue that, typically, such a dipole anisotropy should be relatively small and the axis should probably **lie fairly close to the one seen in the spectrum of the Cosmic Microwave Background.**

LETTER TO THE EDITOR

# Evidence for anisotropy of cosmic acceleration★

Jacques Colin<sup>1</sup>, Roya Mohayaee<sup>1</sup>, Mohamed Rameez<sup>2</sup>, and Subir Sarkar<sup>3</sup><sup>1</sup> CNRS, UPMC, Institut d'Astrophysique de Paris, 98 bis Bld Arago, Paris, France<sup>2</sup> Niels Bohr Institute, University of Copenhagen, Blegdamsvej 17, 2100 Copenhagen, Denmark<sup>3</sup> Rudolf Peierls Centre for Theoretical Physics, University of Oxford, Parks Road, Oxford OX1 3PU, UK  
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## ABSTRACT

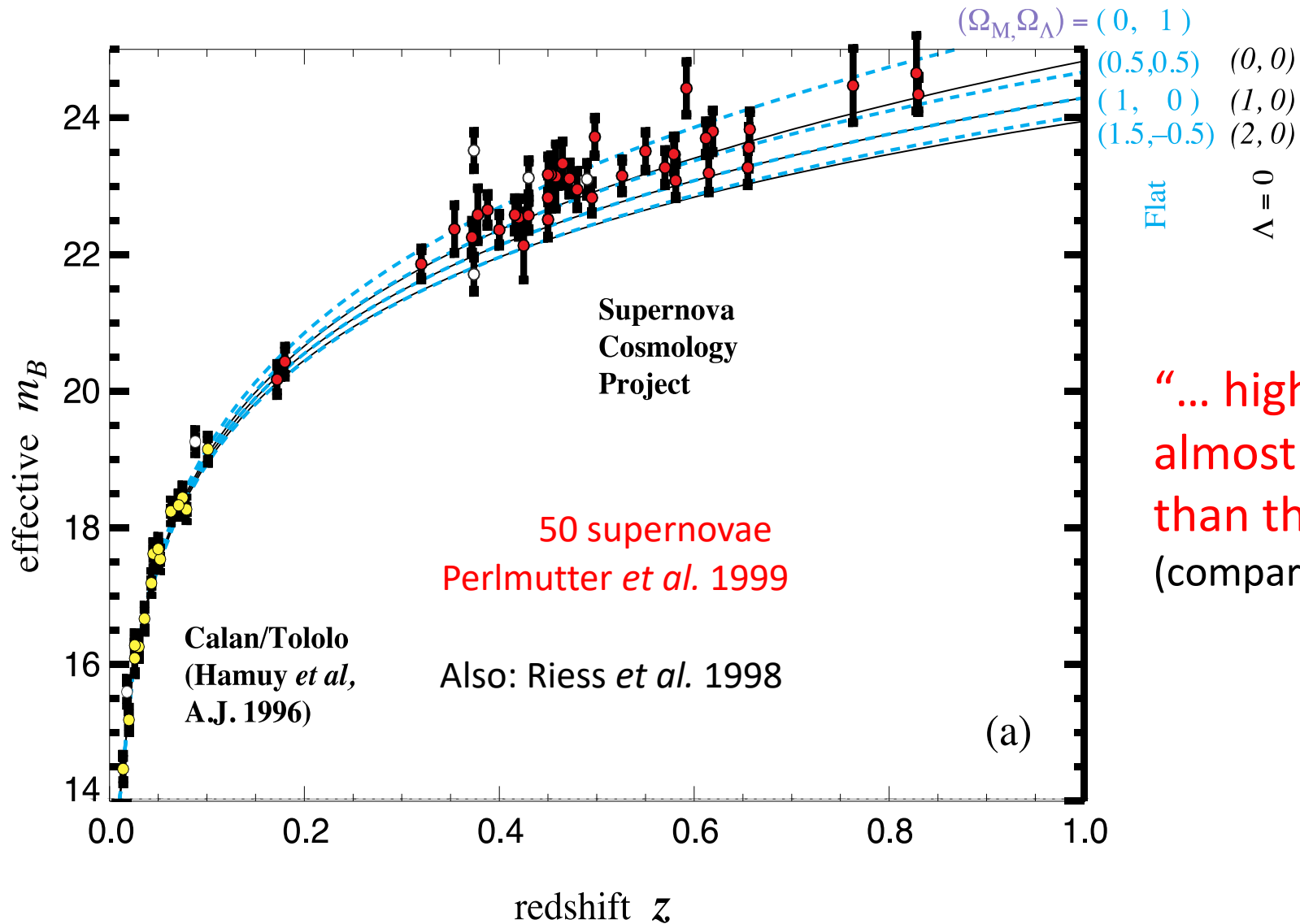
Observations reveal a “bulk flow” in the local Universe which is faster and extends to much larger scales than are expected around a typical observer in the standard  $\Lambda$ CDM cosmology. This is expected to result in a scale-dependent dipolar modulation of the acceleration of the expansion rate inferred from observations of objects within the bulk flow. From a maximum-likelihood analysis of the Joint Light-curve Analysis catalogue of Type Ia supernovae, we find that the deceleration parameter, in addition to a small monopole, indeed has a much bigger dipole component aligned with the cosmic microwave background dipole, which falls exponentially with redshift  $z$ :  $q_0 = q_m + \mathbf{q}_d \cdot \hat{n} \exp(-z/S)$ . The best fit to data yields  $q_d = -8.03$  and  $S = 0.0262$  ( $\Rightarrow d \sim 100$  Mpc), rejecting isotropy ( $q_d = 0$ ) with  $3.9\sigma$  statistical significance, while  $q_m = -0.157$  and consistent with no acceleration ( $q_m = 0$ ) at  $1.4\sigma$ . Thus the cosmic acceleration deduced from supernovae may be an artefact of our being non-Copernican observers, rather than evidence for a dominant component of “dark energy” in the Universe.

Using the SDSS-II/SNLS-3  
Joint Lightcurve Analysis  
(JLA) compilation of 740 SNe

Ensuing debate

Rubin & Heitlauf 2019  
Rahman et al 2021

# The discovery of dark energy



“... high redshift supernovae appear almost 0.15 mag (~15% in flux) fainter than the low redshift supernovae”  
(compared to expectation for  $\Lambda = 0$  universe)

(a)

# SDSS-II/SNLS 3 Joint Lightcurve Analysis, 2014

(SALT 2 For making 'stretch' and 'colour' corrections to the observed lightcurves)

B-band  $\rightarrow$  
$$\mu_B = m_B^* - M + \alpha X_1 - \beta C$$

SALT 2 parameters Betoule *et al.*, A&A **568**:A22,2014

Name	$z_{\text{cmb}}$	$m_B^*$	$X_1$	$C$	$M_{\text{stellar}}$
03D1ar	0.002	$23.941 \pm 0.033$	$-0.945 \pm 0.209$	$0.266 \pm 0.035$	$10.1 \pm 0.5$
03D1au	0.503	$23.002 \pm 0.088$	$1.273 \pm 0.150$	$-0.012 \pm 0.030$	$9.5 \pm 0.1$
03D1aw	0.581	$23.574 \pm 0.090$	$0.974 \pm 0.274$	$-0.025 \pm 0.037$	$9.2 \pm 0.1$
03D1ax	0.495	$22.960 \pm 0.088$	$-0.729 \pm 0.102$	$-0.100 \pm 0.030$	$11.6 \pm 0.1$
03D1bp	0.346	$22.398 \pm 0.087$	$-1.155 \pm 0.113$	$-0.041 \pm 0.027$	$10.8 \pm 0.1$
03D1co	0.678	$24.078 \pm 0.098$	$0.619 \pm 0.404$	$-0.039 \pm 0.067$	$8.6 \pm 0.3$
03D1dt	0.611	$23.285 \pm 0.093$	$-1.162 \pm 1.641$	$-0.095 \pm 0.050$	$9.7 \pm 0.1$
03D1ew	0.866	$24.354 \pm 0.106$	$0.376 \pm 0.348$	$-0.063 \pm 0.068$	$8.5 \pm 0.8$
03D1fc	0.331	$21.861 \pm 0.086$	$0.650 \pm 0.119$	$-0.018 \pm 0.024$	$10.4 \pm 0.0$
03D1fq	0.799	$24.510 \pm 0.102$	$-1.057 \pm 0.407$	$-0.056 \pm 0.065$	$10.7 \pm 0.1$
03D3aw	0.450	$22.667 \pm 0.092$	$0.810 \pm 0.232$	$-0.086 \pm 0.038$	$10.7 \pm 0.0$
03D3ay	0.371	$22.273 \pm 0.091$	$0.570 \pm 0.198$	$-0.054 \pm 0.033$	$10.2 \pm 0.1$
03D3ba	0.292	$21.961 \pm 0.093$	$0.761 \pm 0.173$	$0.116 \pm 0.035$	$10.2 \pm 0.1$
03D3bl	0.356	$22.927 \pm 0.087$	$0.056 \pm 0.193$	$0.205 \pm 0.030$	$10.8 \pm 0.1$

There may well be other variables that the magnitude correlates with ...

# The ingredients of the fit

$$\mu_B = m_B^* - M + \alpha X_1 - \beta C$$

$$= 25 + 5 \log_{10} \frac{d_L}{\text{Mpc}}$$

$$-c^2 d\tau^2 = c^2 dt^2 + a(t)^2 d\Sigma^2$$

- $H = \frac{\dot{a}}{a}$
  - $q \stackrel{\text{def}}{=} -\frac{\ddot{a}a}{a^2}$  (defined with a minus to be positive for a decelerating universe)
  - $j = \frac{\ddot{a}}{aH^3}$
- $$d_L(z) = \frac{cz}{H_0} \left\{ 1 + \frac{1}{2}[1 - q_0]z - \frac{1}{6} \left[ 1 - q_0 - 3q_0^2 + j_0 + \frac{kc^2}{H_0^2 a_0^2} \right] z^2 + O(z^3) \right\}^{\text{Kinematic}}$$

Visser 2004

Exact

$$d_L = (1+z) \frac{d_H}{\sqrt{\Omega_k}} \sinh \left( \sqrt{\Omega_k} \int_0^z \frac{H_0 dz'}{H(z')} \right),$$

$$d_H = c/H_0, \quad H_0 \equiv 100h \text{ km s}^{-1} \text{ Mpc}^{-1},$$

$$H = H_0 \sqrt{\Omega_m (1+z)^3 + \Omega_k (1+z)^2 + \Omega_\Lambda},$$

$$q = \frac{\Omega_M}{2} - \Omega_\Lambda \text{ (in } \Lambda\text{CDM)}$$

Concordance cosmology is given by

$$\Omega_M \sim 0.3, \quad \Omega_\Lambda \sim 0.7$$

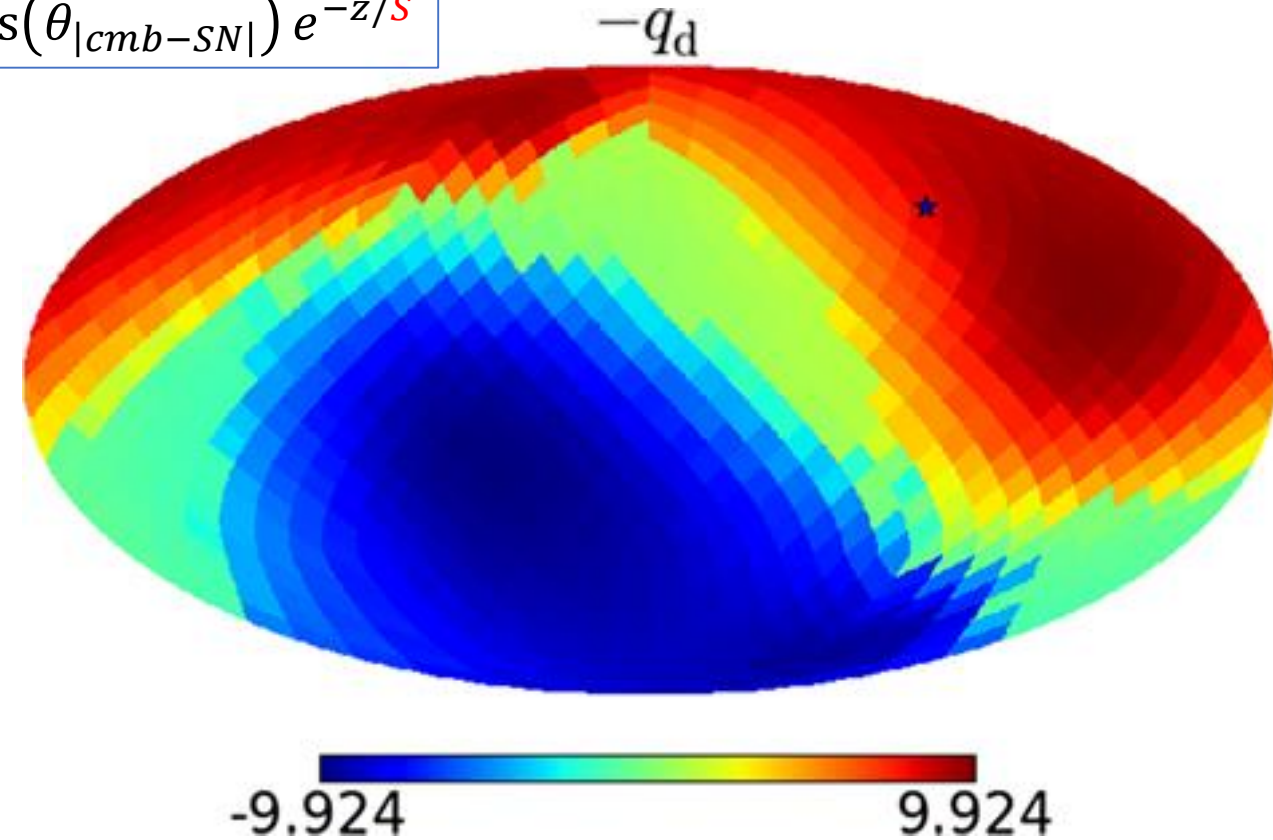
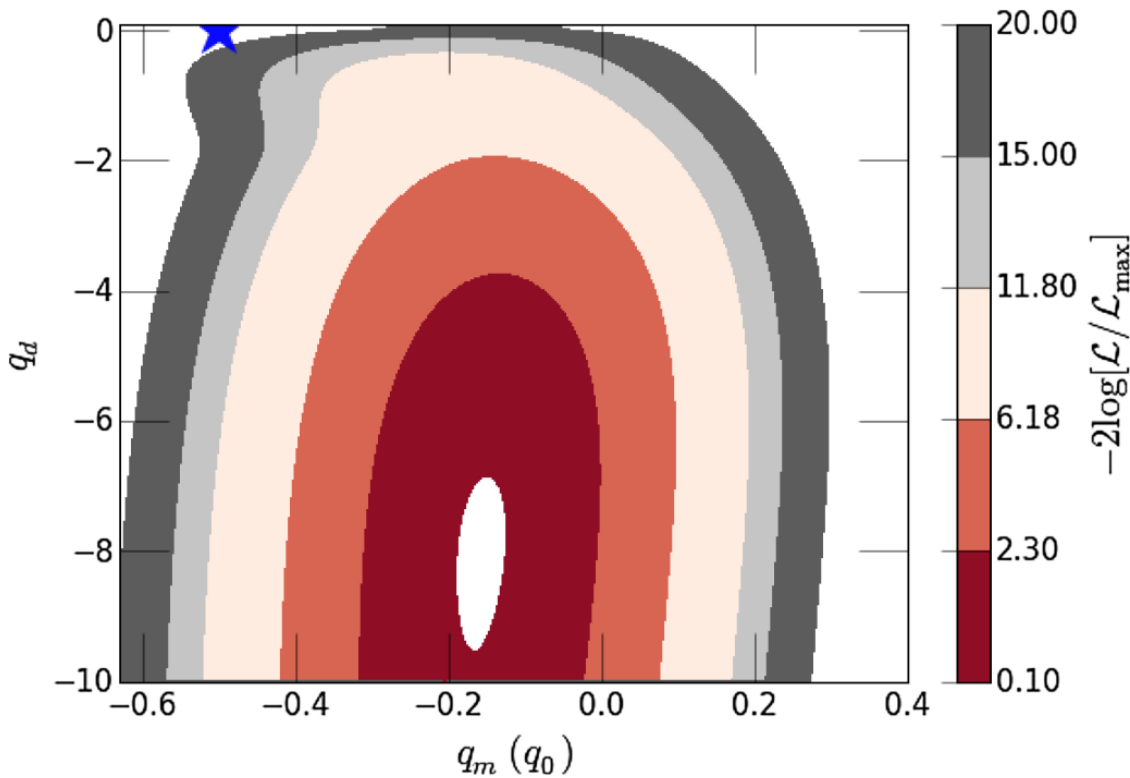
$$\Omega_k \sim 0$$

$$H \sim 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$$



# Scale dependent Dipole in the deceleration parameter

$$\text{Tilt: } q_0 \rightarrow q_m + q_d \cos(\theta_{|cmb-SN|}) e^{-z/S}$$



The dipolar component of acceleration is larger than the monopole, and dominates out to  $z \sim 0.1$ . Statistically significant @  $3.9 \sigma$

$$q_d \gg q_m$$

The statistical significance of the Universe accelerating isotropically is  $< 1.4 \sigma$ !

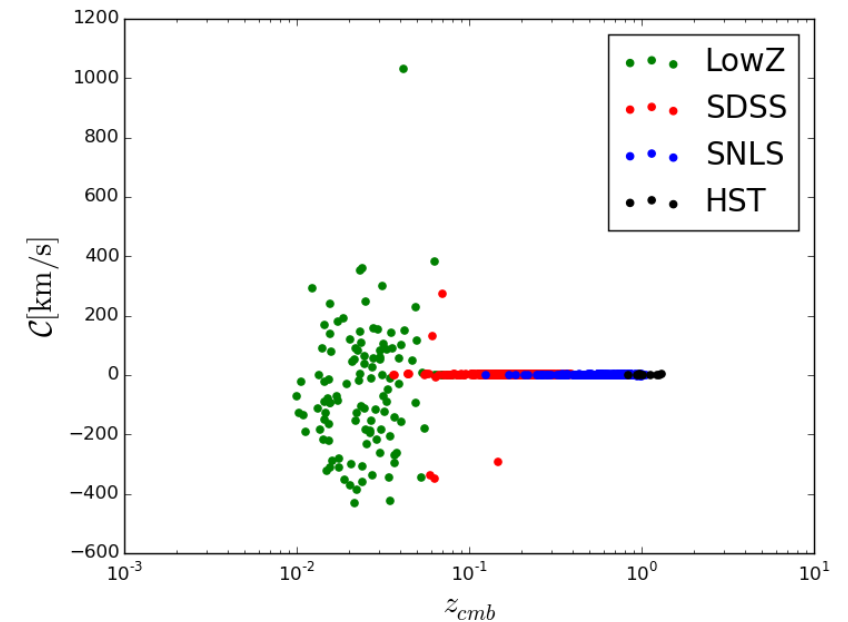
Cosmic acceleration, (and dark energy) may simply be an artefact of our being located inside a 'bulk flow' ... in accordance with the prediction of Tsagas (2011)

# Contentious Issue : We used the heliocentric redshifts.

#name	zcmb	zhel	dz	mb	dmb	x1	dx1	color	dcolor
03D1au	0.503084	0.504300	0	23.001698	0.088031				
03D1aw	0.580724	0.582000	0	23.573937	0.090132				
03D1ax	0.494795	0.496000	0	22.960139	0.088110				
03D1bp	0.345928	0.347000	0	22.398137	0.087263				
03D1co	0.677662	0.679000	0	24.078115	0.098356				
03D1dt	0.610712	0.612000	0	23.285241	0.092877				
03D1ew	0.866494	0.868000	0	24.353678	0.106037				
03D1fc	0.330932	0.332000	0	21.861412	0.086437				
03D1fa	0.798566	0.800000	0	24.510389	0.101777				

A choice described as  
'shocking' by Rubin &  
Heitlauf 2019

$$C = [(1 + z_{hel}) - (1 + z_{cmb})(1 + z_{pec}^{hel})] \times c$$



$$1 + z_{hel} = (1 + z_{pec}^{hel}) \times (1 + \bar{z}) \times (1 + z_{pec}^{SN})$$

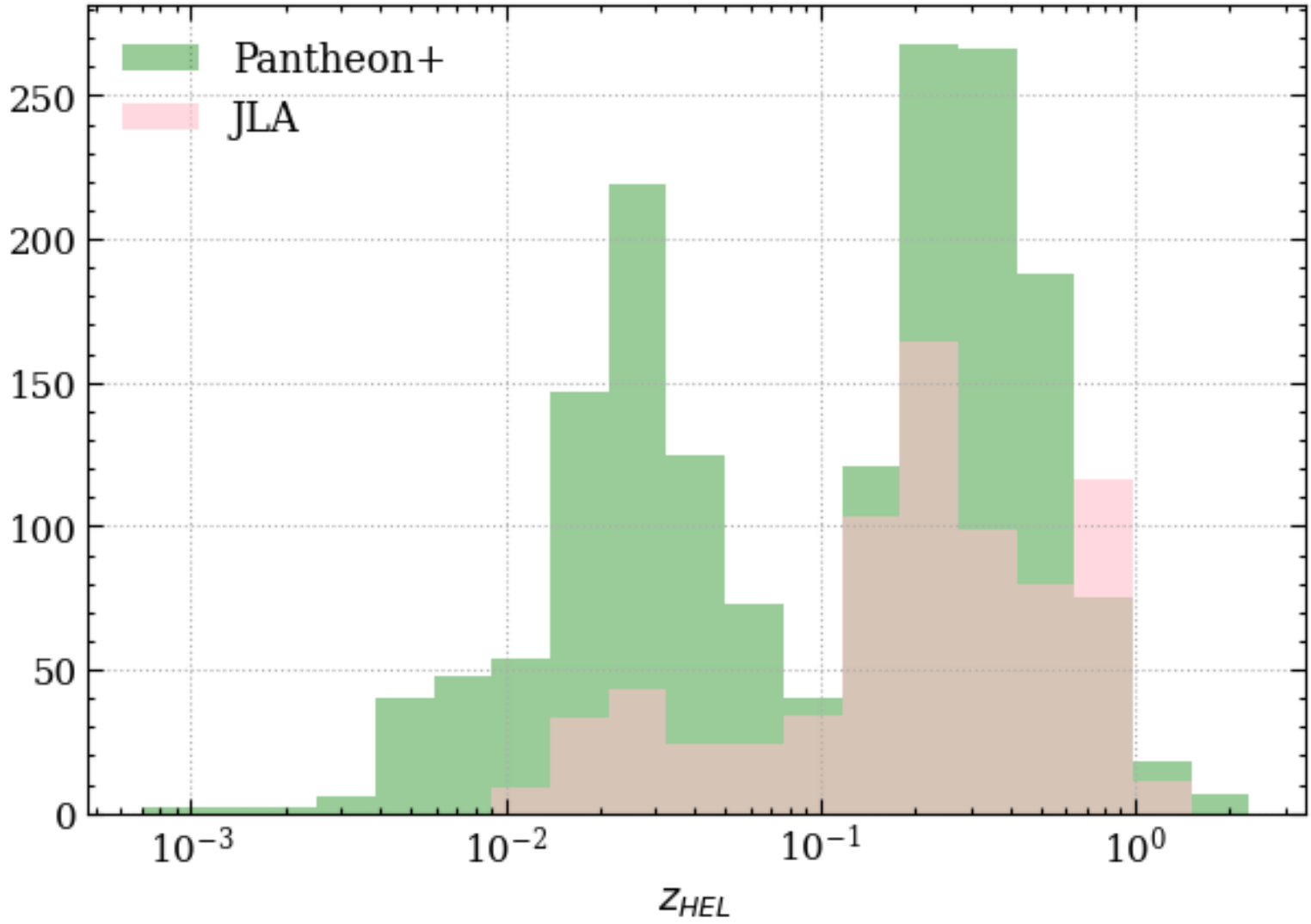
$z_{hel} \rightarrow$  measured

$z_{cmb} (\bar{z}) \rightarrow$  inferred using a flow model

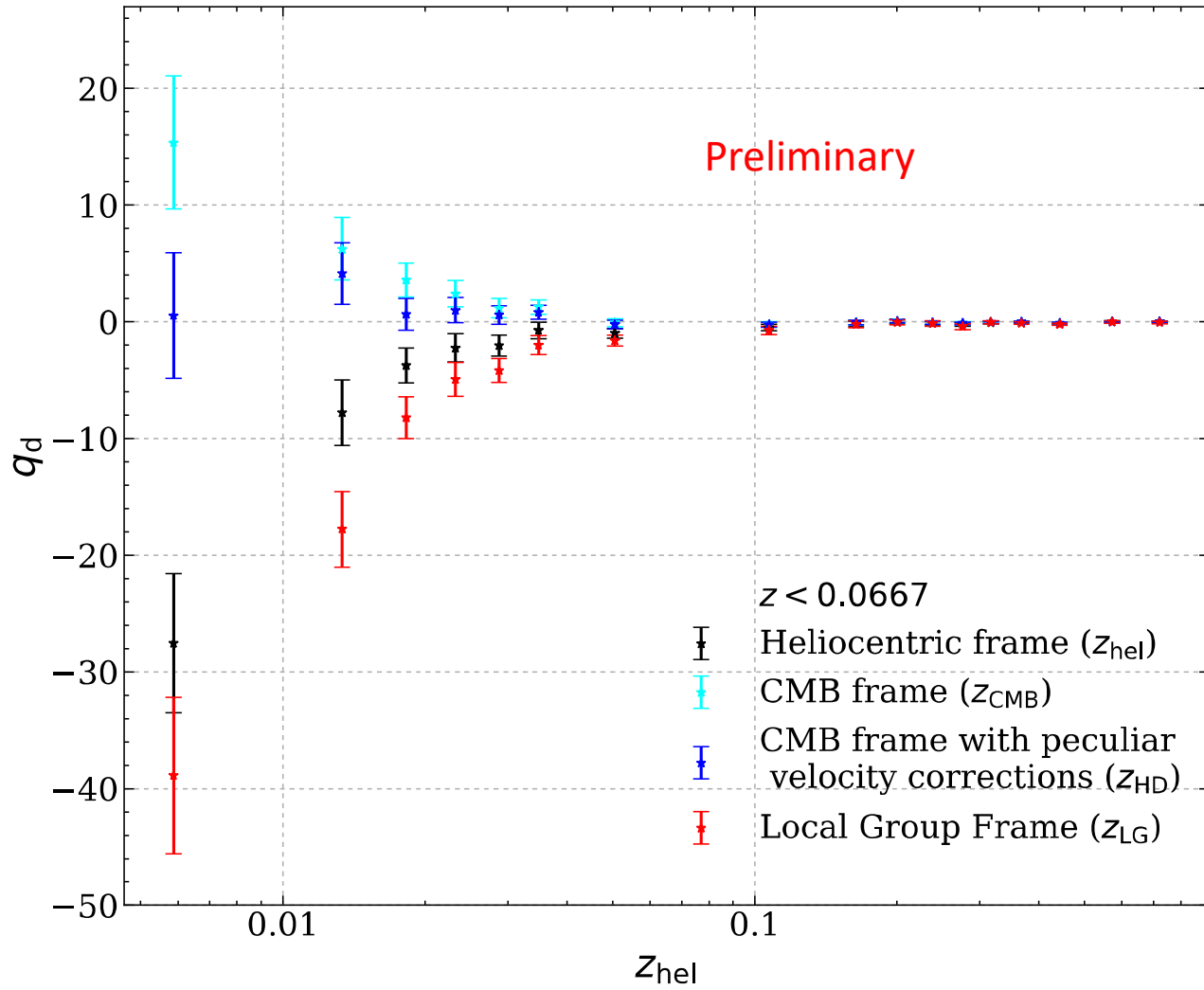
Davis *et al.* Astrophys.J. 741 (2011) 67

Ellis & Stoeger (1987)

“The fitting problem in cosmology”

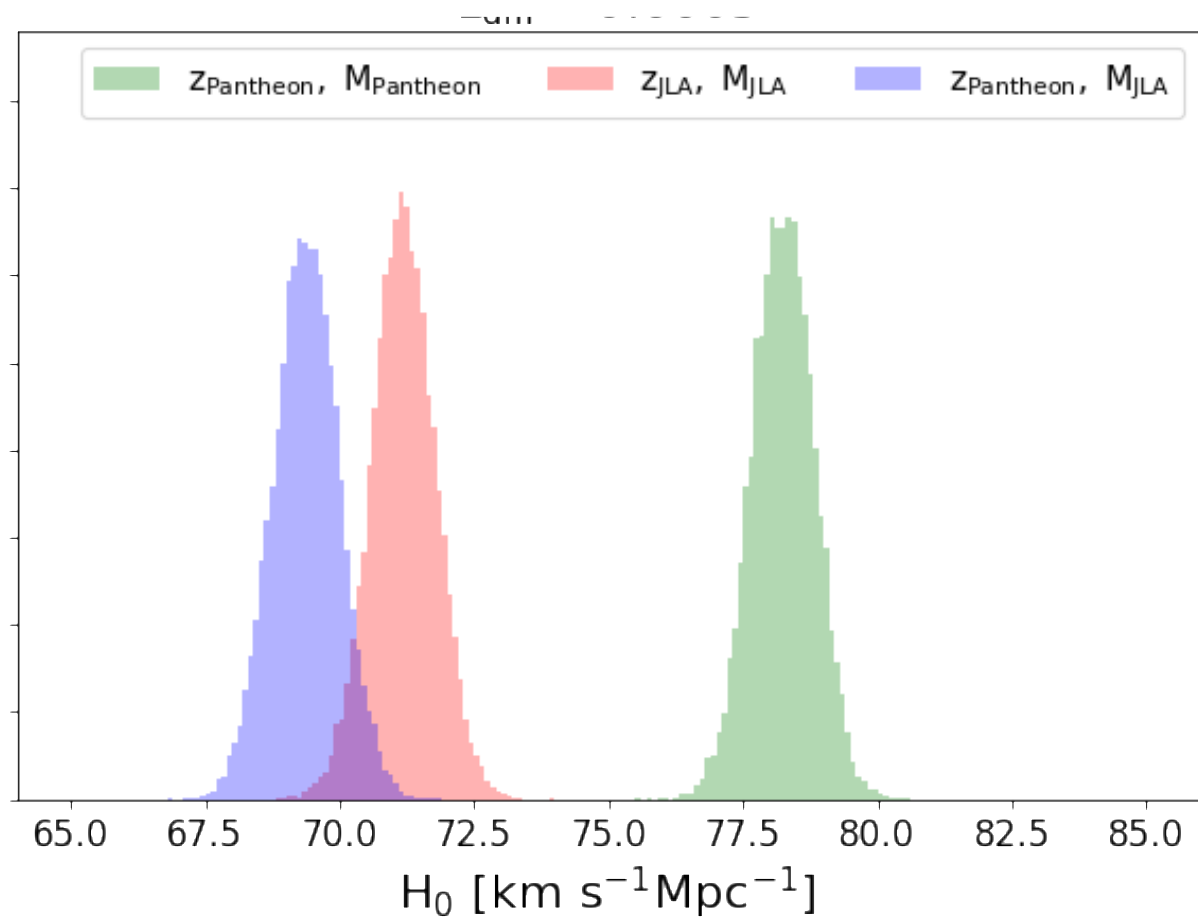
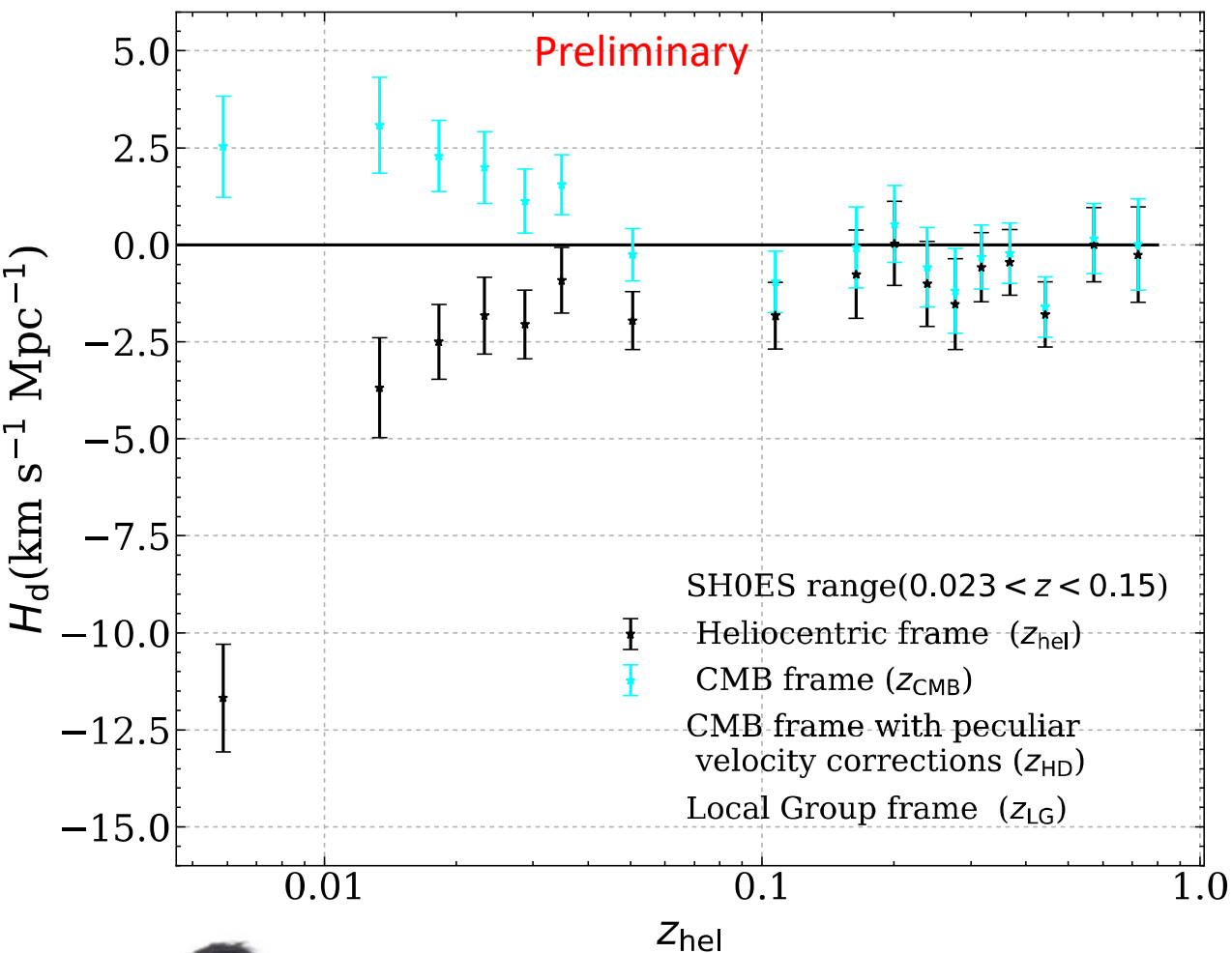


Various changes in terminology



In preparation, Sah et. al. 2024

# The Anisotropy on H is greater than the SHOES claimed uncertainty on H



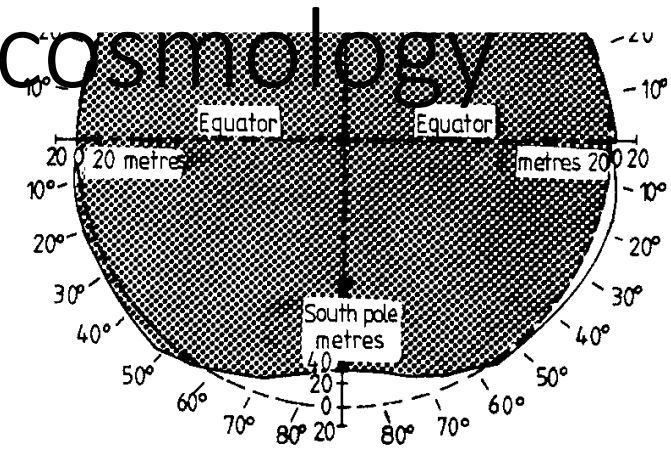
Rameez and Sarkar 2021 *Class. Quantum Grav.* **38** 154005

In preparation, Sah et. al. 2024



# The 'fitting problem' in cosmology

**Abstract.** This paper considers the best way to fit an idealised exactly homogeneous and isotropic universe model to a realistic ('lumpy') universe; whether made explicit or not, some such approach of necessity underlies the use of the standard Robertson-Walker models as models of the real universe. Approaches based on averaging, normal coordinates and null data are presented, the latter offering the best opportunity to relate the fitting procedure to data obtainable by astronomical observations.



**Figure 1.** (a) An exactly uniform and spherically symmetrical FLRW universe  $U'$  mapped into the lumpy universe  $U$  so as to give the best fit possible. (b) An exactly spherical sphere fitted to the lumpy world to give the best fit possible.

ion

cosmology aims at finding the large-scale matter distribution and spacetime the universe from astronomical observations. There are broadly speaking approaches that have been applied to this problem.

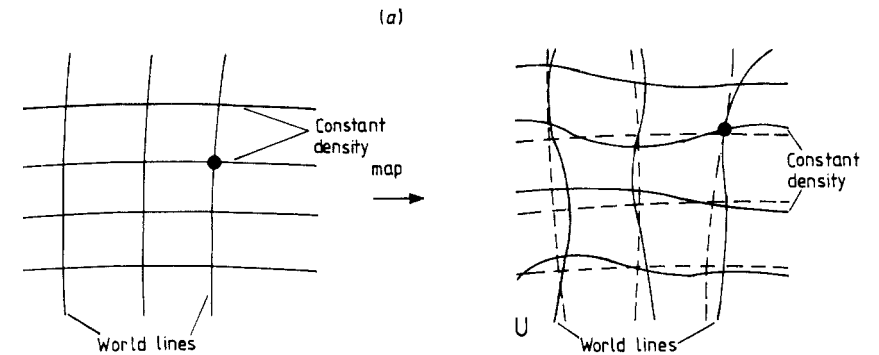
The Earth is a Sphere to a precision of 50 kms on the radius, but not to a precision of 5 kms

Similarly the Universe is FLRW to a precision of  $10 \text{ km s}^{-1} \text{ Mpc}^{-1}$  but not to a precision of  $1 \text{ km s}^{-1} \text{ Mpc}^{-1}$

It is tilted

The 'fitting problem' in cosmology

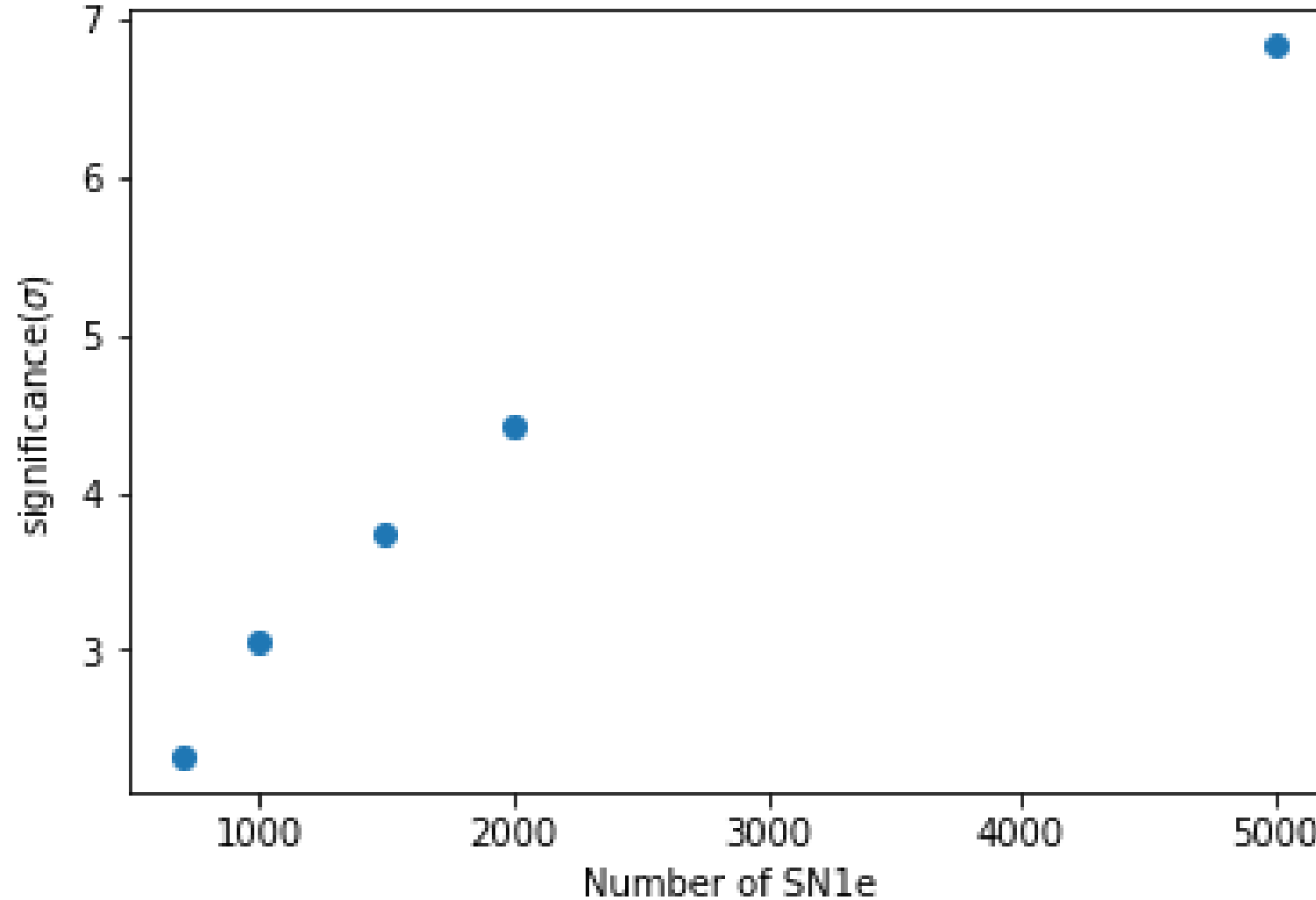
1699



# $\sigma$ vs N

LSST DESC Project No 254  
“testing tilted cosmology”  
Modelling and Combined  
Probes working group

Ongoing : Develop rest  
frame independent  
template fitting and  
calibration pipelines



Median significance at which  $q_d = 0$  can be rejected, from 100 simulations of N SNe, using the method of CMRS19

With ~5000 SNe, the null hypothesis can be rejected at more than 6 sigma

# Conclusion

## The Universe is anisotropic and the Cosmic Rest Frame is a myth

- Ellis & Baldwin tests performed on 4 independent Radio galaxy catalogues and CatWISE Quasars conclusively reject the exclusively kinematic interpretation of the CMB dipole at  $> 5 \sigma$ . **CMB rest frame and matter rest frame are different. Cosmological principle stands falsified.**
- SN1a data are better fit by a “tilted Friedmann model”. Ensuing debate stultifies dark energy evidence.
- Strong hint towards the inhomogeneous cosmological models.

A new cosmological tension!

Three projects in LSST DESC

All who have data access are welcome to join

### Reviews

Mohayaee, Rameez & Sarkar

*Eur.Phys.J.ST* 230 (2021) 9, 2067-2076

Subir Sarkar

“Heart of Darkness”

*Inference: International Review of Science* 6 (2022) 4



**Heart of Darkness**  
Subir Sarkar

*Cosmologists are often in error, but never in doubt.*  
—Lev Landau<sup>1</sup>

**I**N THE STANDARD MODEL of cosmology, about seventy percent of the energy density of the universe—the dark energy driving its accelerating rate of expansion—is described by Albert Einstein’s cosmological constant.<sup>2</sup> In this essay, I argue that the standard model of cosmology is wrong. This should come as no surprise. “The history of science,” Georges Lemaitre remarked, “provides many instances of discoveries which have been made for reasons which are no longer considered satisfactory.” It may be, he added suggestively, “that the discovery of the cosmological constant is such a case.”<sup>3</sup>

Einstein published the general theory of relativity in 1915; and in 1917, he attempted to apply his theory to the cosmos as a whole. The result was a universe that was

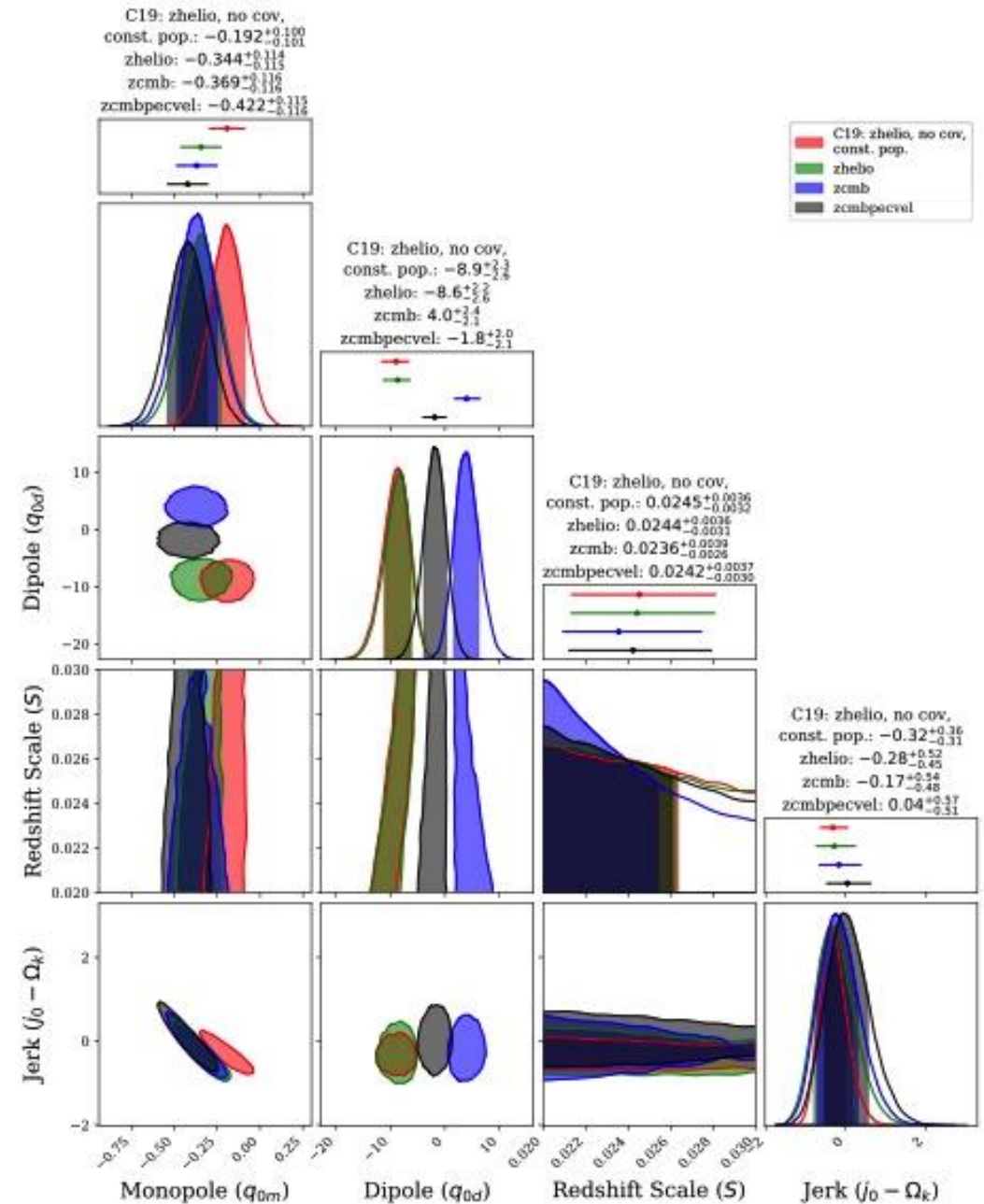
Subir Sarkar is Emeritus Professor at the Rudolf Peierls Centre for Theoretical Physics, University of Oxford.



# The peculiar velocities question

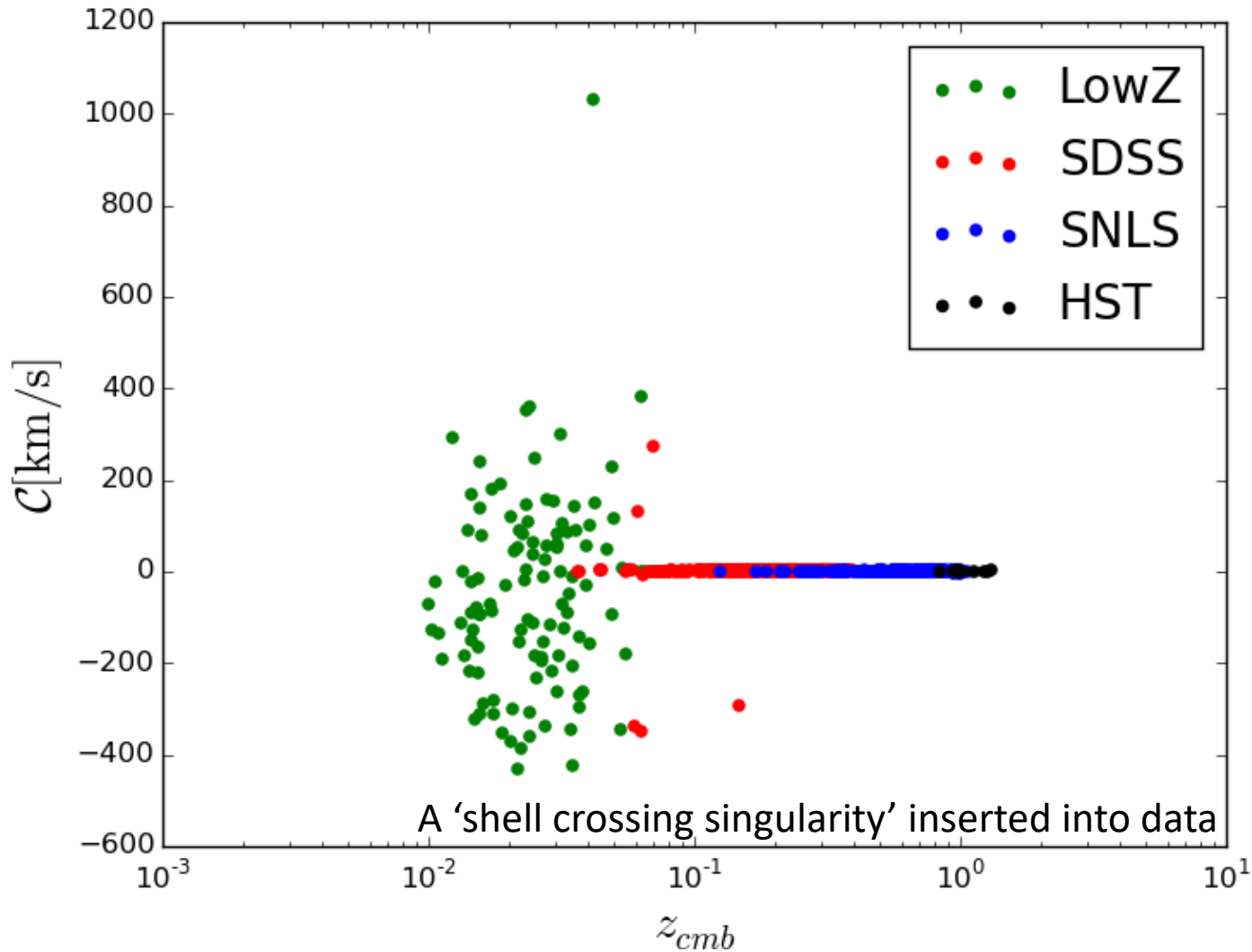
- **Rubin & Heitlauf (2019)** demonstrate that

- If the correction for the motion of the observer w.r.t. the CMB rest frame is introduced, the direction of the dipole in  $q$  reverses
- Only when further correction for peculiar velocities is introduced, does the dipole in  $q$  effectively disappear



# 'Untilting' the Universe

$$C = [(1 + z_{hel}) - (1 + z_{cmb})(1 + z_{pec}^{hel})] \times c$$



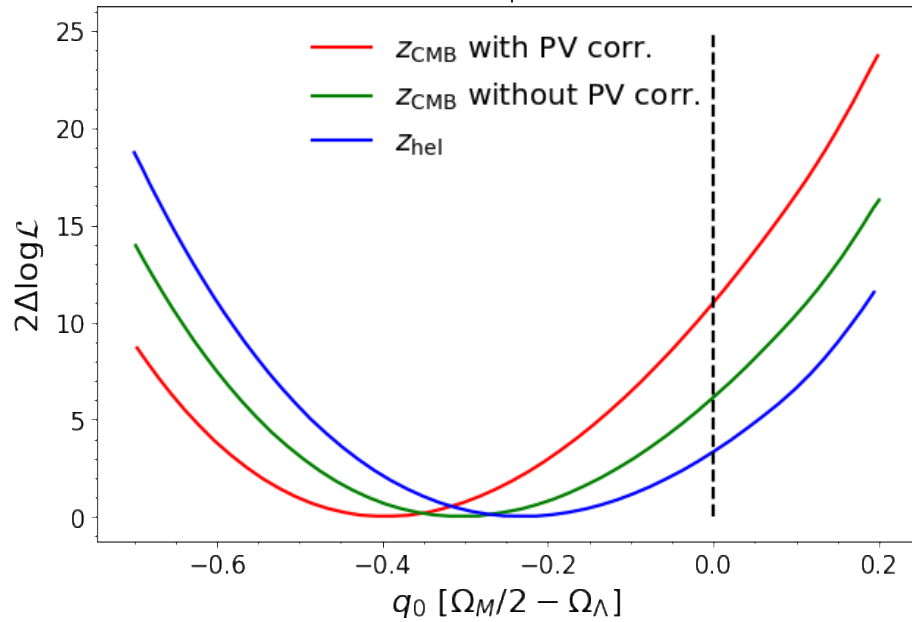
SNe Ia at  $z > 0.06$  are assumed (arbitrarily) to be in the CMB rest frame (only uncorrelated 150 km/s in error budget)

Flow model (Streaming Motions of Abell Clusters, Hudson 2004) has a  $\sim 687 \pm 203$  km/s residual bulk flow

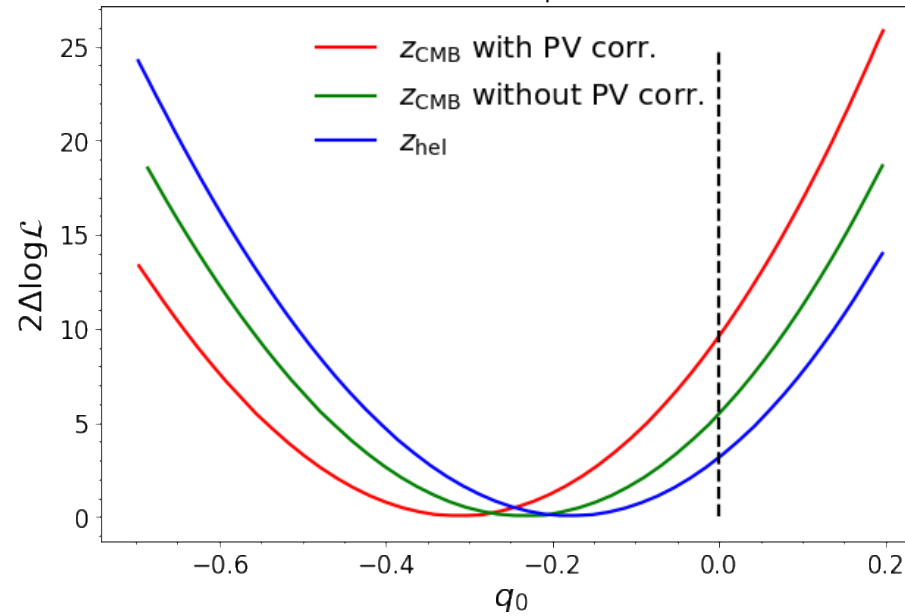
About ~half the evidence (relative dimming of high- $z$  SNe has to be put into the data), in the process introducing an arbitrary discontinuity!

$$\begin{aligned} \Delta\mu_{pv} &= \frac{5}{\log(10)} \frac{v}{zc} \\ &= \frac{5}{\log(10)} \frac{687}{0.067 \times c} = \mathbf{0.074} \end{aligned}$$

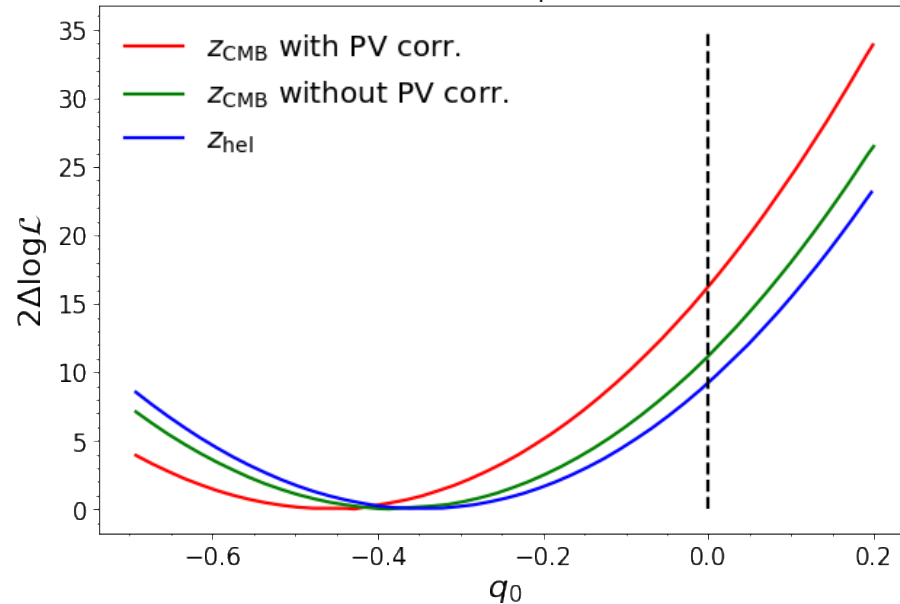
FLRW - 10 parameter



kinematic - 10 parameter



kinematic - 22 parameter



About ~half the evidence (relative dimming of high-z SNe has to be put into the data), in the process introducing an arbitrary discontinuity!

“... high redshift supernovae appear almost 0.15 mag (~15% in flux) fainter than the low redshift supernovae” (compared to expectation in a  $\Lambda = 0$  universe)

$$\Delta\mu_{pv} = \frac{5}{\log(10)} \frac{v}{zc}$$

Mohayaee et al 2021 *Eur.Phys.J.ST* 230 (2021) 9

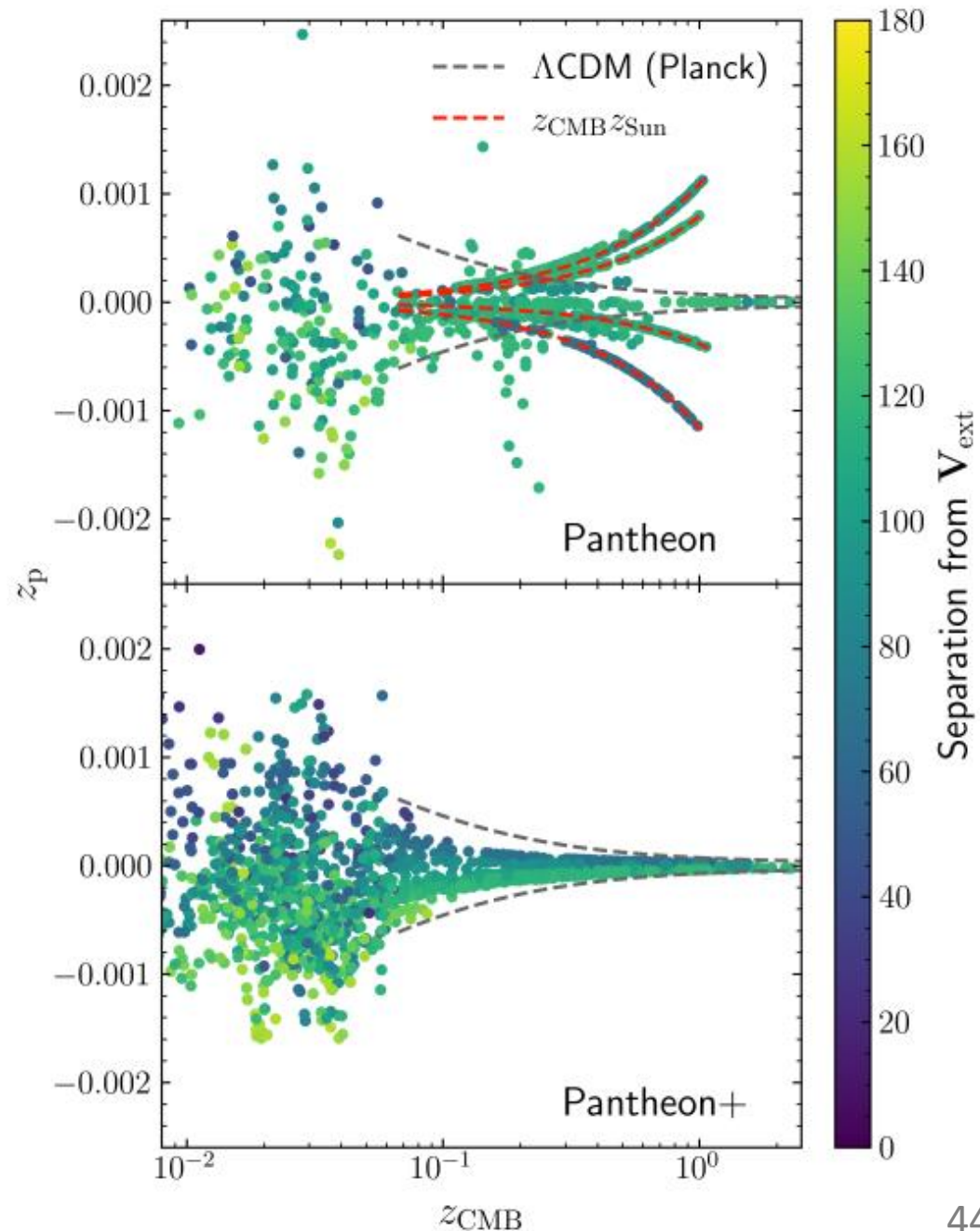
# Things get weirder in later SNe Ia datasets

E.g. Carr et al 2022 on Pantheon+ peculiar velocities

## 6.3. Velocities beyond $r_{\max}$

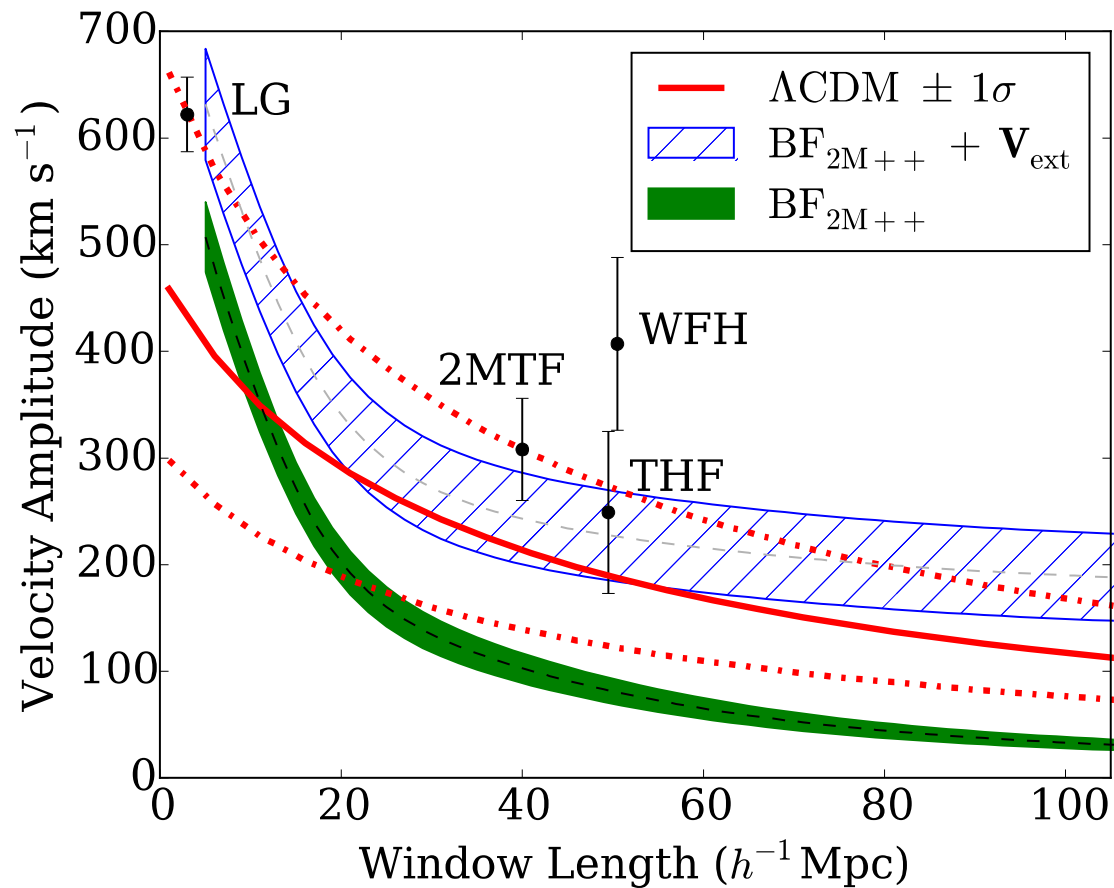
It is difficult to properly account for velocities outside  $r_{\max}$  because we do not have an adequate measurement of the density field to predict individual velocities precisely. However, we expect velocities to continue to behave largely according to the bulk flow trend beyond  $r_{\max}$  as a consequence of  $\Lambda$ CDM large scale structure. In standard  $\Lambda$ CDM a theoretical bulk flow magnitude of  $\sim 20 \text{ km s}^{-1}$  is expected even for a sphere with radius  $z \sim 1$  (gray dashed lines in Figure 9). Accordingly, peculiar velocities of galaxies outside  $r_{\max}$  should not be set to zero.

To ensure a smooth transition across  $r_{\max}$  we have chosen to model the bulk flow as a decaying function consistent with  $\Lambda$ CDM expectations, and in the direction of the bulk flow of the  $200 h^{-1} \text{ Mpc}$  sphere. While there is a  $\Lambda$ CDM model dependence, the impact of this high- $z$  correction on cosmological inferences is small both because the corrections are small (at most  $\sim 5 \times 10^{-4}$  when in the direction of the bulk flow), and



# Circular reasoning in search of the cosmic rest frame?

This is the model using which Pantheon and Pantheon+ compilations correct for peculiar velocities

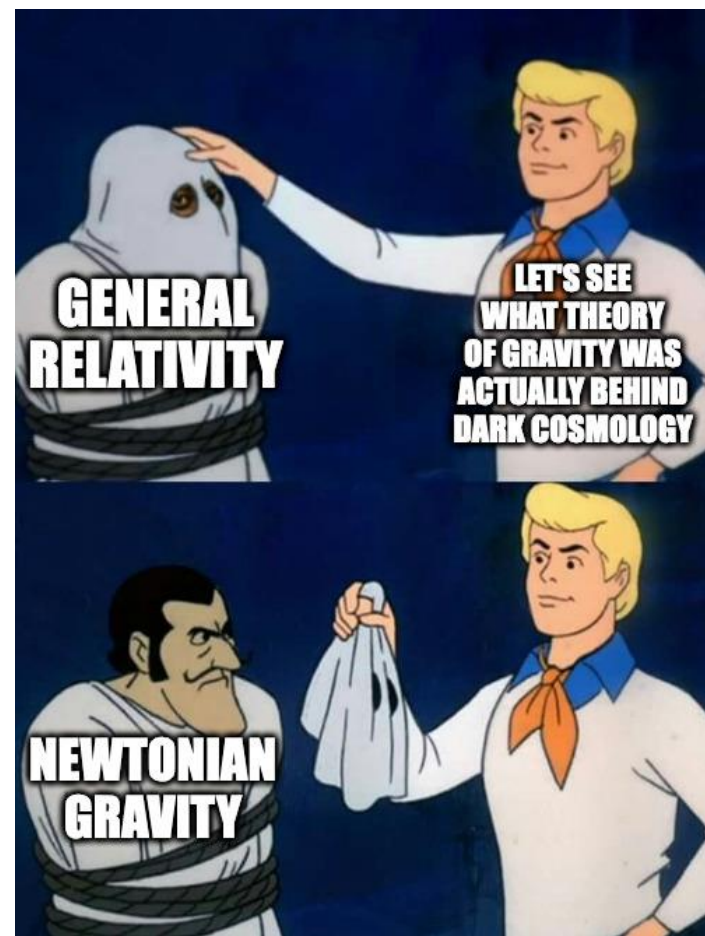


Infers the peculiar velocity field from a density contrast field derived from data (2M++ compilation) using linear Newtonian perturbation theory.

$$v(\mathbf{r}) = \frac{H_0 f(\Omega_m)}{4\pi b_g} \int \delta_g(\mathbf{r}') \frac{(\mathbf{r}' - \mathbf{r})}{|\mathbf{r}' - \mathbf{r}|^3} d^3 \mathbf{r}'.$$

Carrick, Turnbull, Lavaux, Hudson *MNRAS*, 450 (2015) 317

“We find that an external bulk flow is preferred at the **5.1σ** level, and the best fit has a velocity of **159 ± 23 km s<sup>-1</sup>** towards  $l = 304^\circ \pm 11^\circ$ ,  $b = 6^\circ \pm 13''$  [beyond 200  $h^{-1}$  Mpc radius]





dscolnic commented on Nov 28, 2018

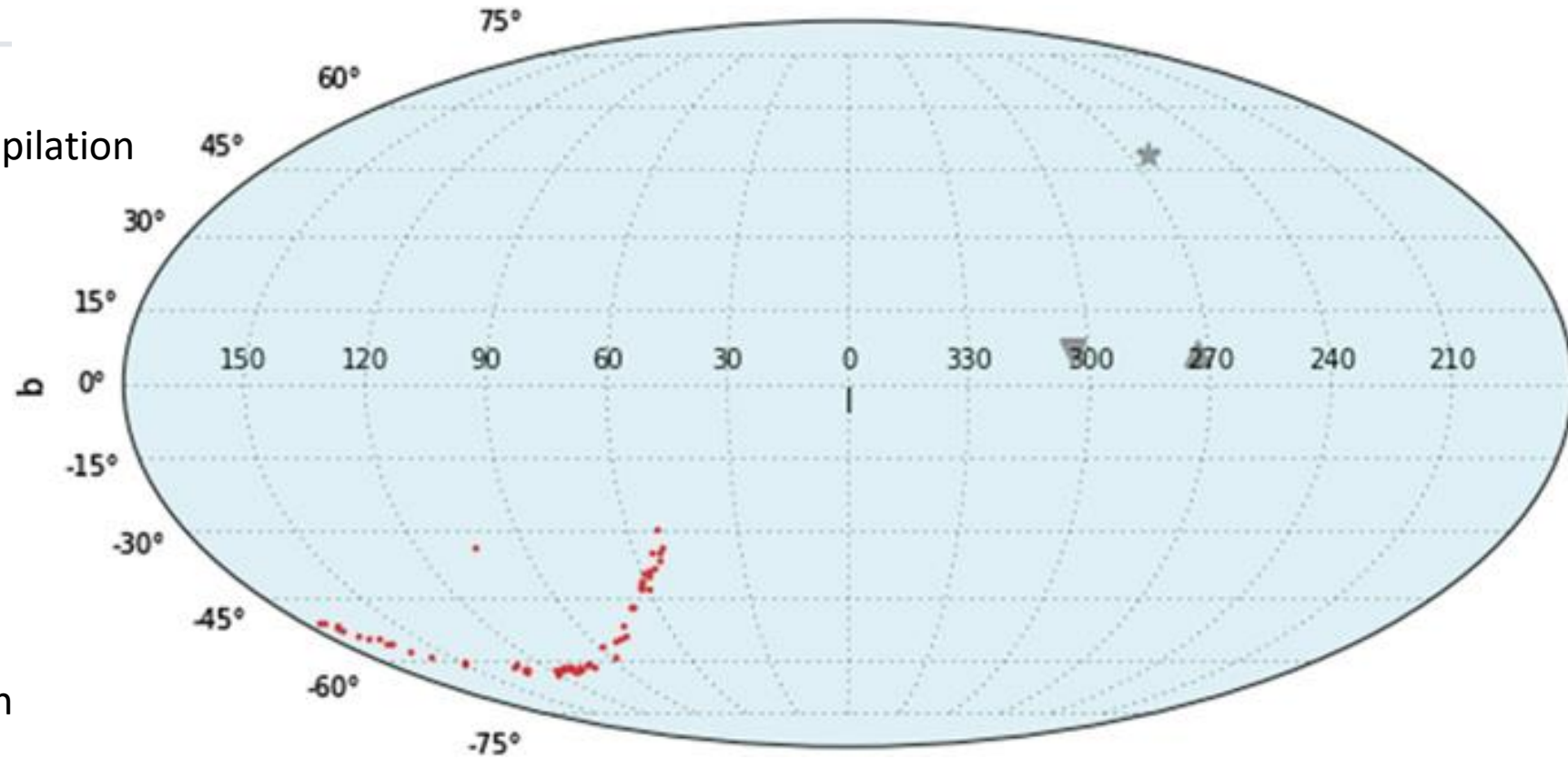
Owner ...

Hi - I have posted a new file that has no peculiar velocity corrections for  $z > 0.08$ .



dscolnic closed this on Nov 28, 2018

Also in the intermediate Pantheon compilation



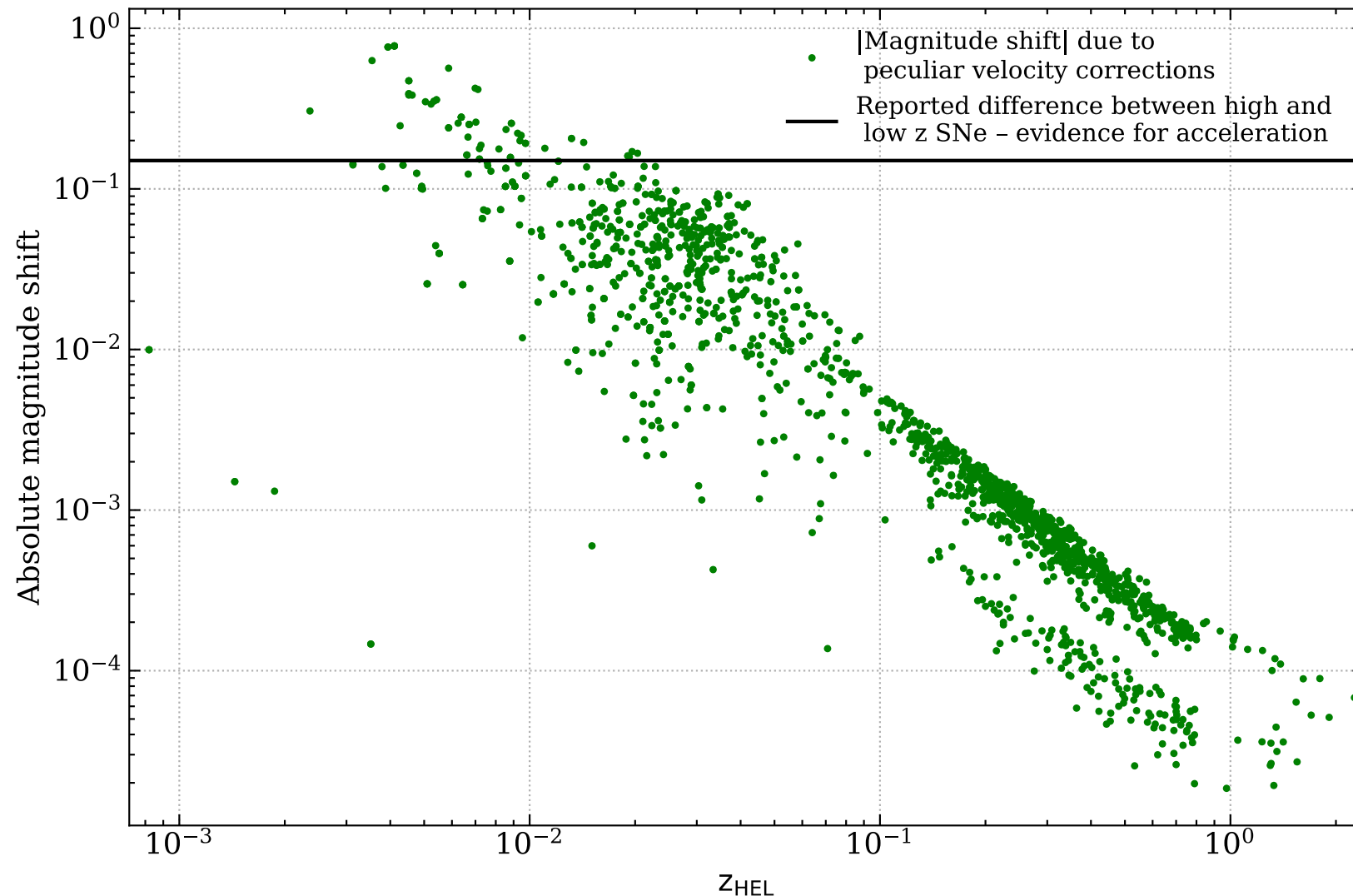
<https://github.com/dscolnic/Pantheon>

1905.00221

$$\Delta\mu_{pv} = \frac{5}{\log(10)} \frac{v}{zc}$$

Each one of the supernovae now has to be corrected

The corrections applied to the low z ones are far larger than the 0.15 mag relative dimming between low z and high z SNe



How to sculpt an elephant?

Chethan KRISHNAN<sup>a\*</sup>, Ranjini MONDOL<sup>a†</sup>, M. M. SHEIKH-JABBARI<sup>b‡</sup>

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Indian Institute of Science, Bangalore 560012, India

<sup>b</sup> School of Physics, Institute for Research in Fundamental Sciences (IPM),  
P. O. Box 19395-5531, Tehran, Iran

## SO(3) → U(1), tilted Bianchi V/VII<sub>h</sub> - 4 Friedmann equations

### Large-scale geometry of the Universe

Yassir Awwad<sup>♠</sup> and Tomislav Prokopec<sup>◇</sup>

<sup>◇</sup> Institute for Theoretical Physics, Spinoza Institute & EMMEΦ  
Utrecht University, Princetonplein 5, 3584 CC Utrecht, The Netherlands

Thursten Perelman theorem -> anisotropic Thursten geometries  
should be considered on par with Friedmann geometry

### Spatially Homogeneous Universes with Late-Time Anisotropy

Andrei Constantin<sup>⊕,1,\*</sup> Thomas R. Harvey<sup>⊕,1,†</sup> Sebastian von Hausegger<sup>⊕,2,‡</sup> and Andre Lukas<sup>⊕,1,§</sup>

<sup>1</sup>Rudolf Peierls Centre for Theoretical Physics, University of Oxford, Parks Road, Oxford, UK

<sup>2</sup>Astrophysics, University of Oxford, Denys Wilkinson Building, Keble Road, Oxford, UK

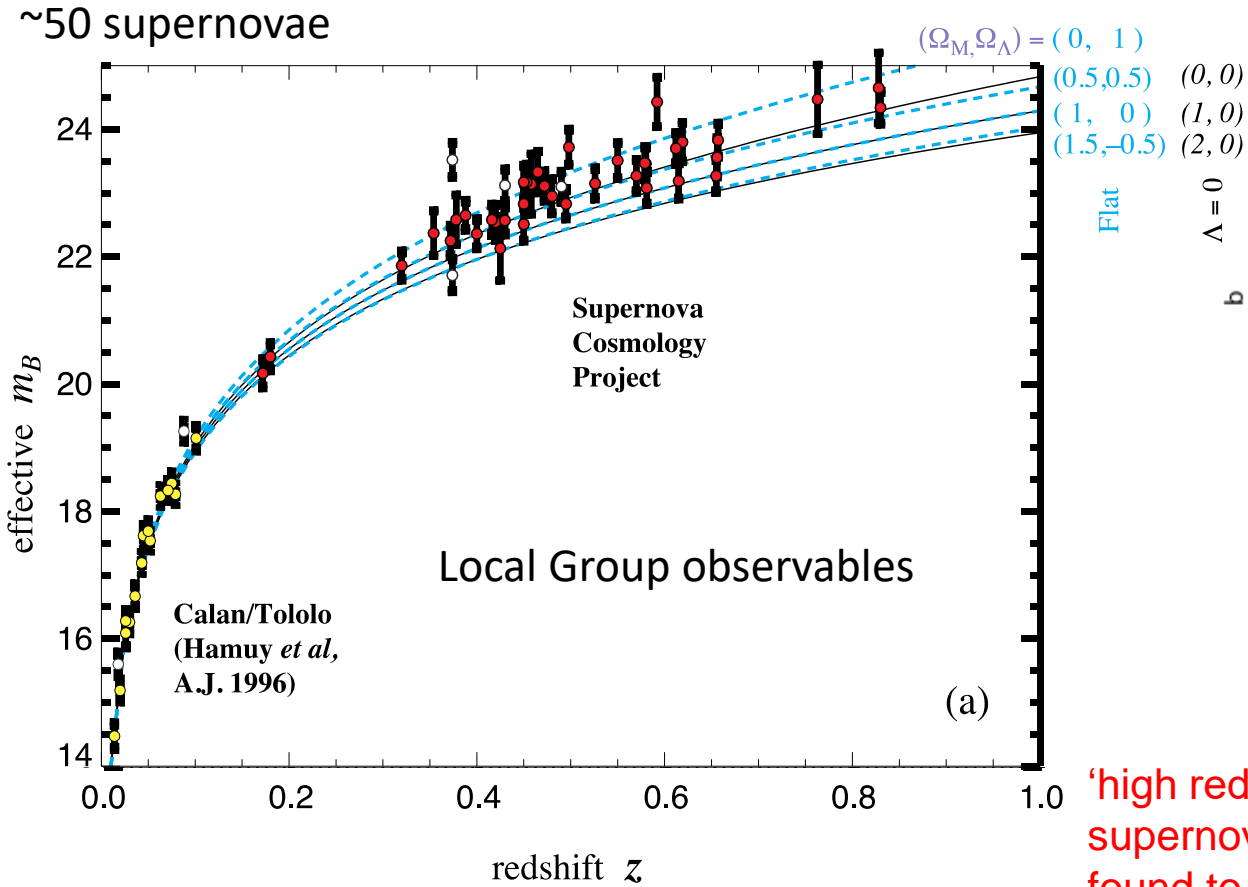
Chengcheng Han<sup>1,\*</sup>

<sup>1</sup>School of Physics, Sun Yat-Sen University, Guangzhou 510275, China

(Dated: November 29, 2022)



# The discovery of dark energy



'high redshift supernovae were found to be dimmer (15% in flux) than the low redshift supernovae (compared to what would be expected in a  $\Lambda = 0$  universe)'

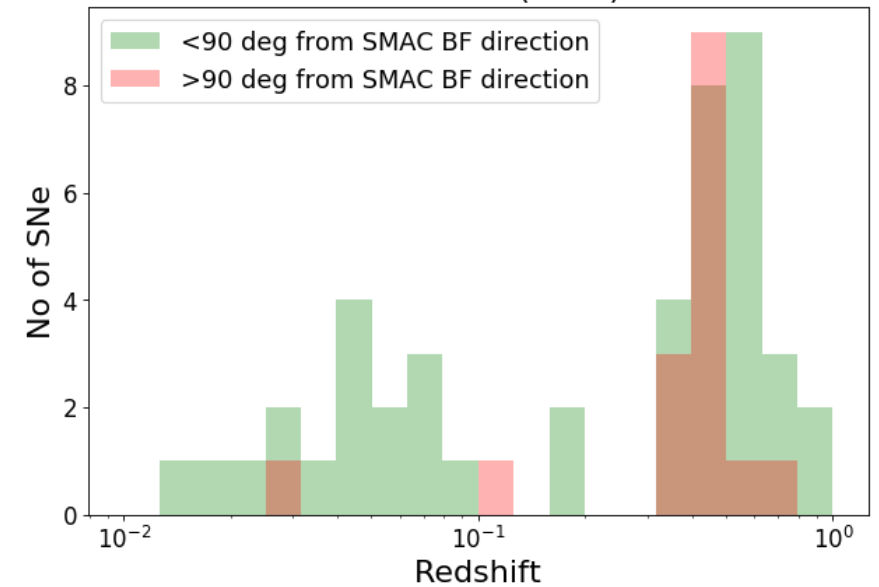
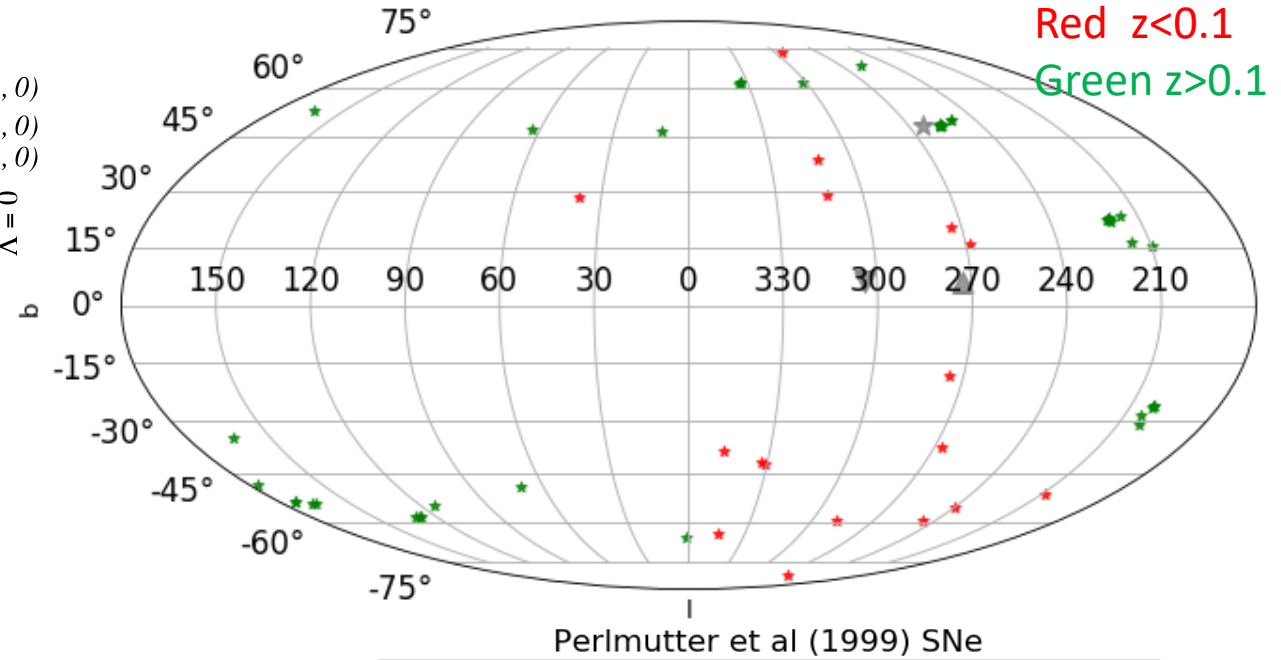
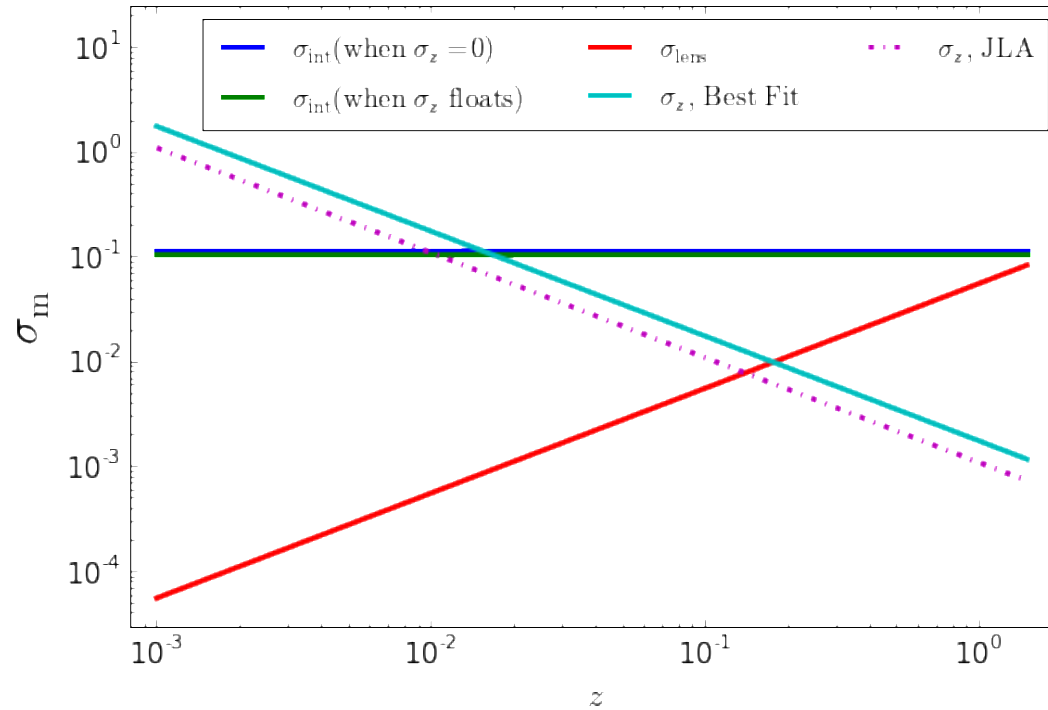


FIG. 2

Collaboration	Number of SNe Ia	$N_{\text{out}}$	Lightcurve	CRF	Treatment of peculiar velocities	Lensing
SCP [9]	60 (18+42)	4	“stretch”	LG	$\sigma_v = 300 \text{ km s}^{-1}$	
HZT [10]	50 (34+16)	-	MLCS, template	CMB	$\sigma_v = 200 \text{ km s}^{-1}, 2500 \text{ km s}^{-1}$ at high $z$	
SNLS [68]	117 (44+73)	2 <sup>a</sup>	SALT	CMB+helio	$z_{\text{min}} = 0.015$	
SCP (Union) [69]	307	8 <sup>a</sup>	SALT	CMB+helio	$z_{\text{min}} = 0.015, \sigma_v = 300 \text{ km s}^{-1}$	$\sigma^l = 0.093z$
Union2 [70]	557	12 <sup>a</sup>	SALT2	CMB+helio	$z_{\text{min}} = 0.015, \sigma_v = 300 \text{ km s}^{-1}$	$\sigma^l = 0.093z$
SCP [72]	580	0	SALT2	CMB+helio	not available	corrections
SNLS [71]	472	6 <sup>a</sup>	SALT2 & SiFTO	CMB	$\sigma_v = 150 \text{ km s}^{-1}$ + SN-by-SN corrections	$\sigma^l = 0.055z$
JLA [11]	740	0	SALT2	CMB	$\sigma_v = 150 \text{ km s}^{-1}$ + SN-by-SN corrections	$\sigma^l = 0.055z$
Pantheon [62]	1048	86	SALT2	CMB	$\sigma_v = 250 \text{ km s}^{-1}$ + SN-by-SN corrections	$\sigma^l = 0.055z$



Newest : Union 3, data not properly public yet

Mohayaee et al 2021 *Eur.Phys.J.ST* 230 (2021) 9

# Some worry about the scale of $\Lambda$

## General Relativity

$$R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} + \Lambda g_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

*“Space tells matter how to move  
Matter tells space how to curve”*: Wheeler

*No special (inertial or accelerating) frames*

A problem in Riemannian geometry.

## FLRW Exact Solution

Exact isotropy and homogeneity **at all scales**:

$$-c^2 d\tau^2 = c^2 dt^2 + a(t)^2 d\Sigma^2$$

**Synchronized clocks, a constant time hypersurface**

$$H^2 = \left(\frac{\dot{a}}{a}\right)^2$$

$$H^2 = H_0^2 [\Omega_M(1+z)^3 + \Omega_K(1+z)^2 + \Omega_\Lambda]$$

$$\Omega_M + \Omega_K + \Omega_\Lambda = 1$$

The cosmic sum rule

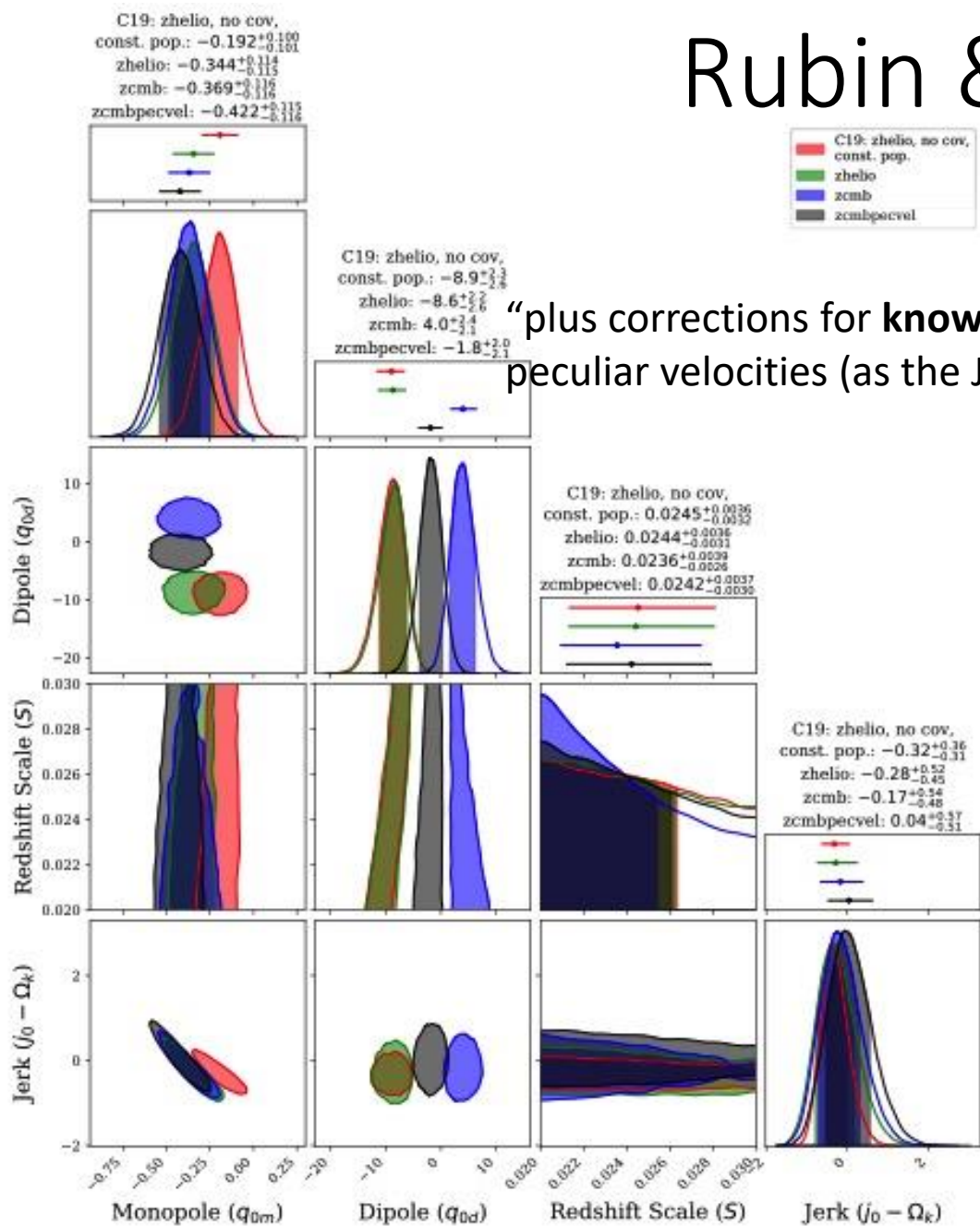
$\Lambda$ , if it's a vacuum energy appears to be about  $10^{120}$  below its 'natural' value from QFT

*“there is nonzero vacuum energy of just the right order of magnitude to be detectable today”*

Is the evidence for dark energy secure?

Sarkar, Gen.Rel.Grav.40:269-284,2008

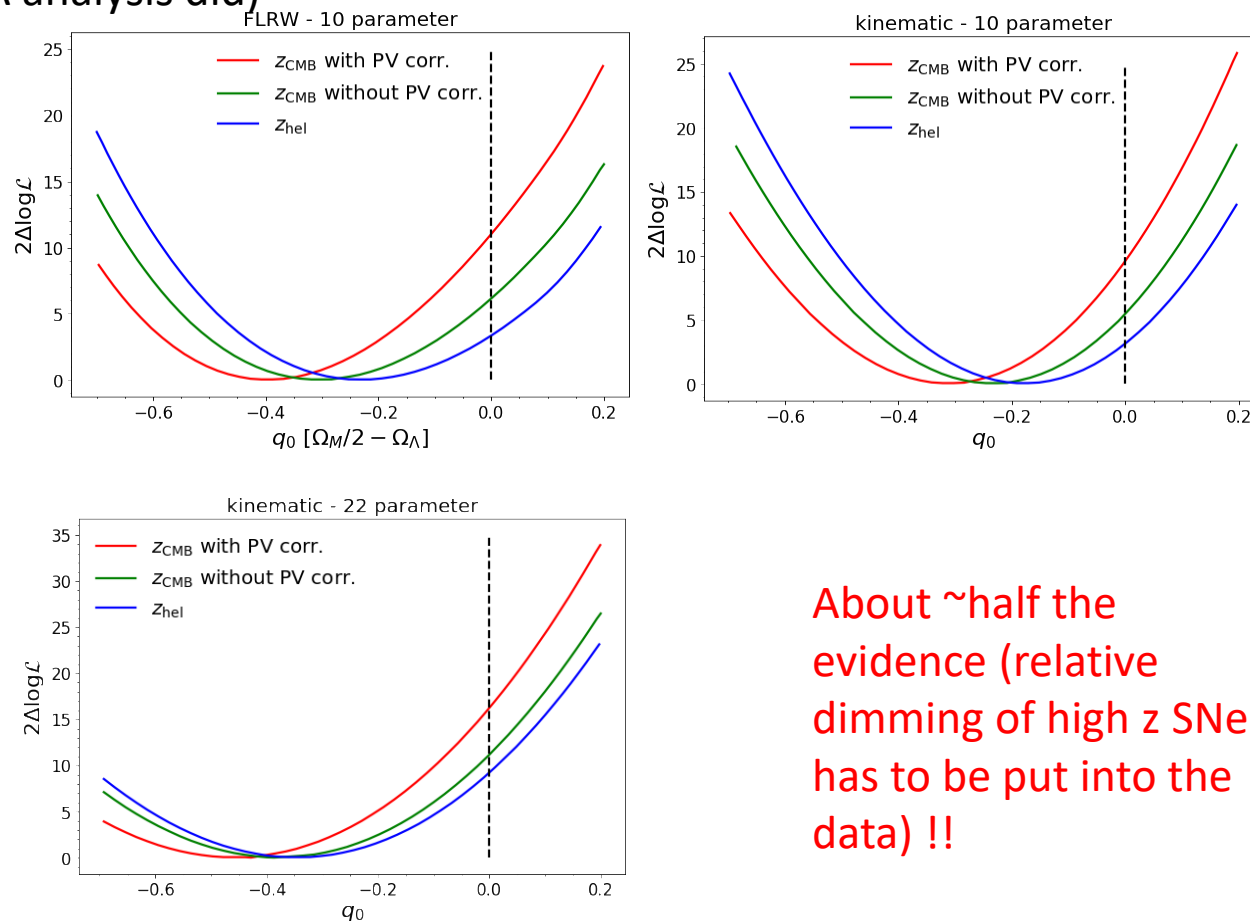
# Rubin & Heitlauf 2019



“plus corrections for known peculiar velocities (as the JLA analysis did)”

$$\Delta\mu_{pv} = \frac{5}{\log(10)} \frac{v}{z_c}$$

Our Response



About ~half the evidence (relative dimming of high z SNe has to be put into the data) !!

# Peculiar velocity impact on SN1a magnitude

$$1 + z = (1 + \bar{z})(1 + z_{pec}^{hel})(1 + z_{pec}^{SN})$$

$$d_L(z) = \bar{d}_L(\bar{z}) (1 + z_{pec}^{hel})(1 + z_{pec}^{SN})^2$$

Davis et. al. *Astrophys.J.* 741 (2011) 67

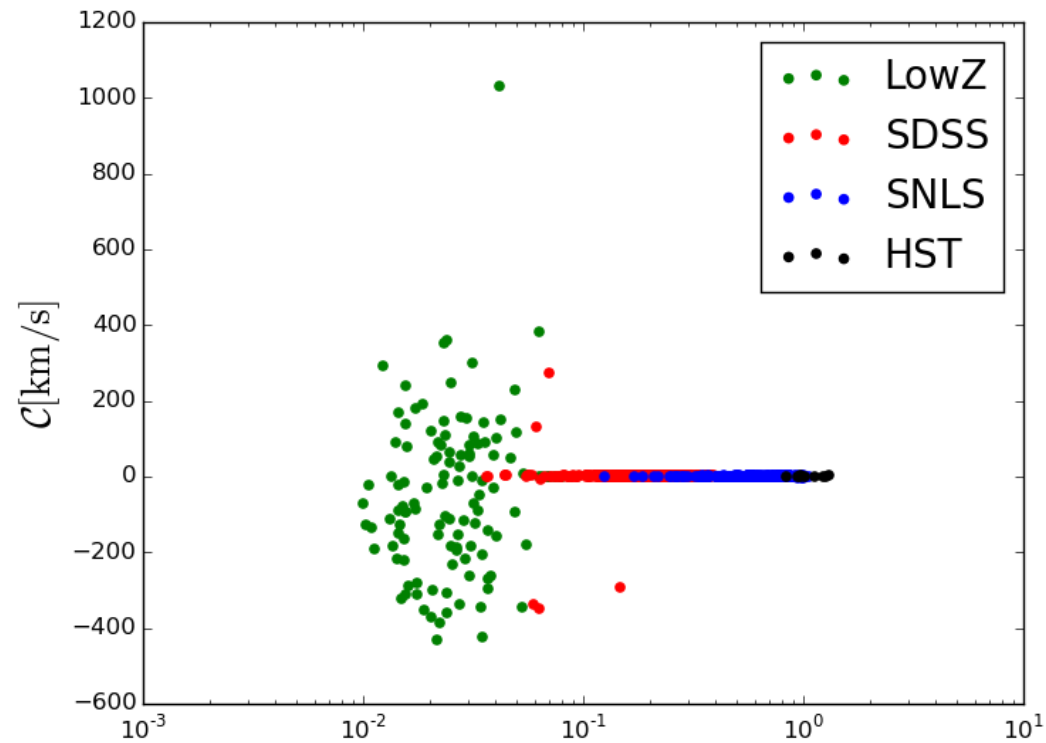
JLA (and Pantheon) redshifts and magnitudes have been 'corrected' to account for the local bulk flow.

#name	zcmb	zhel	dz	mb	dmb	x1	dx1	color	dcolor
03D1au	0.503084	0.504300	0	23.001698	0.088031				
03D1aw	0.580724	0.582000	0	23.573937	0.090132				
03D1ax	0.494795	0.496000	0	22.960139	0.088110				
03D1bp	0.345928	0.347000	0	22.398137	0.087263				
03D1co	0.677662	0.679000	0	24.078115	0.098356				
03D1dt	0.610712	0.612000	0	23.285241	0.092877				
03D1ew	0.866494	0.868000	0	24.353678	0.106037				
03D1fc	0.330932	0.332000	0	21.861412	0.086437				
03D1fg	0.798566	0.800000	0	24.510389	0.101777				

$z_{hel} \rightarrow$  measured

$z_{cmb} \rightarrow$  inferred using a flow model

$$C = [(1 + z_{hel}) - (1 + z_{cmb})(1 + z_d)] \times c$$



SN1a at  $z > 0.06$  are assumed (arbitrarily) to be in the CMB rest frame. (only uncorrelated 150 km/s in error budget)

Flow model – SMAC has a  $\sim 600$  km/s residual bulk flow

Consequently, we use only  $z_{hel}$  and subtract out the corrections to  $m_B$

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Davis et. al. *Astrophys.J.* 741 (2011) 67

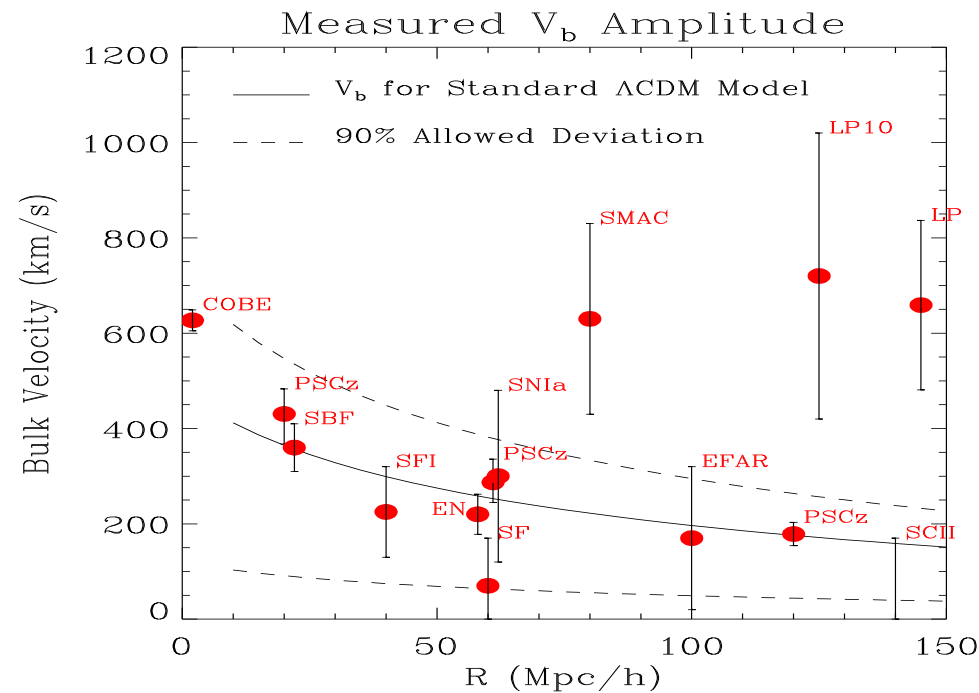
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#name	z <sub>cmb</sub>	z <sub>hel</sub>	dz	mb	dmb	x1	dx1	color	dcolor
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03D1fn	0.798566	0.800000	0	24.510389	0.101777				

$z_{hel} \rightarrow$  measured

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$$C = [(1 + z_{hel}) - (1 + z_{cmb})(1 + z_d)] \times c$$



SN1a at  $z > 0.06$  are assumed (arbitrarily) to be in the CMB rest frame. (only uncorrelated 150 km/s in error budget)  
 Wrong 'correction' to SDSS2308 in JLA. Many such mistakes in Pantheon (eg : SN2246).

Flow model – SMAC has a  $\sim 600$  km/s residual bulk flow

Consequently, we use only  $z_{hel}$  and subtract out the corrections to  $m_B$

# There is an arbitrary discontinuity within the data.

Also in the subsequent Pantheon compilation



dscolnic commented on Nov 28, 2018

Owner ...

Hi - I have posted a new file that has no peculiar velocity corrections for  $z > 0.08$ .

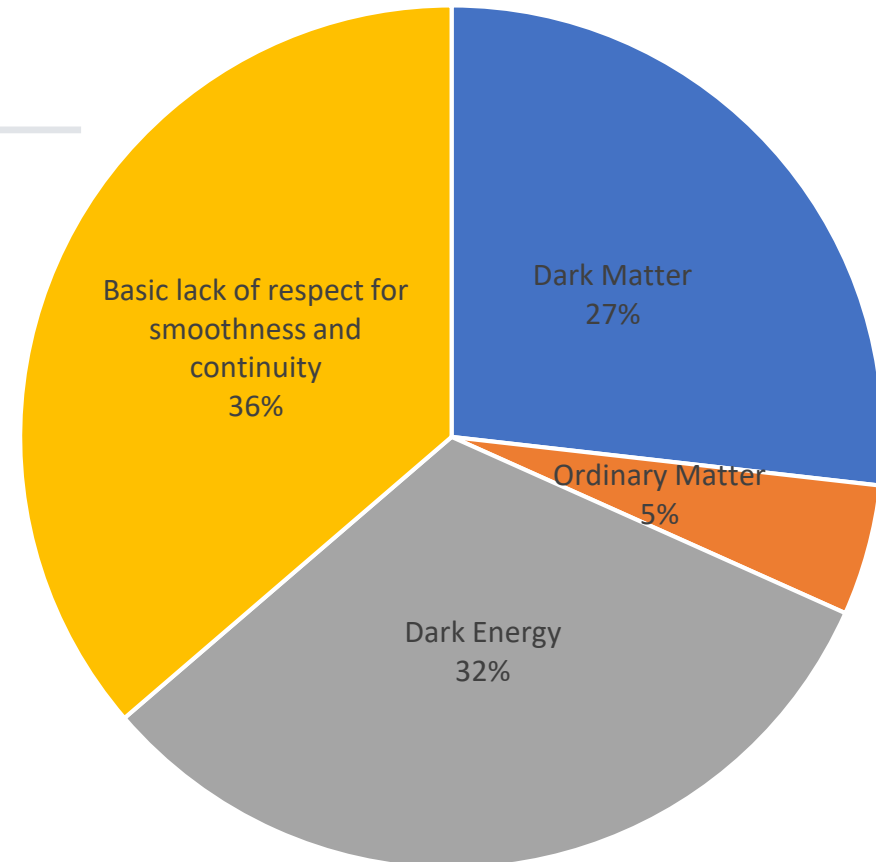


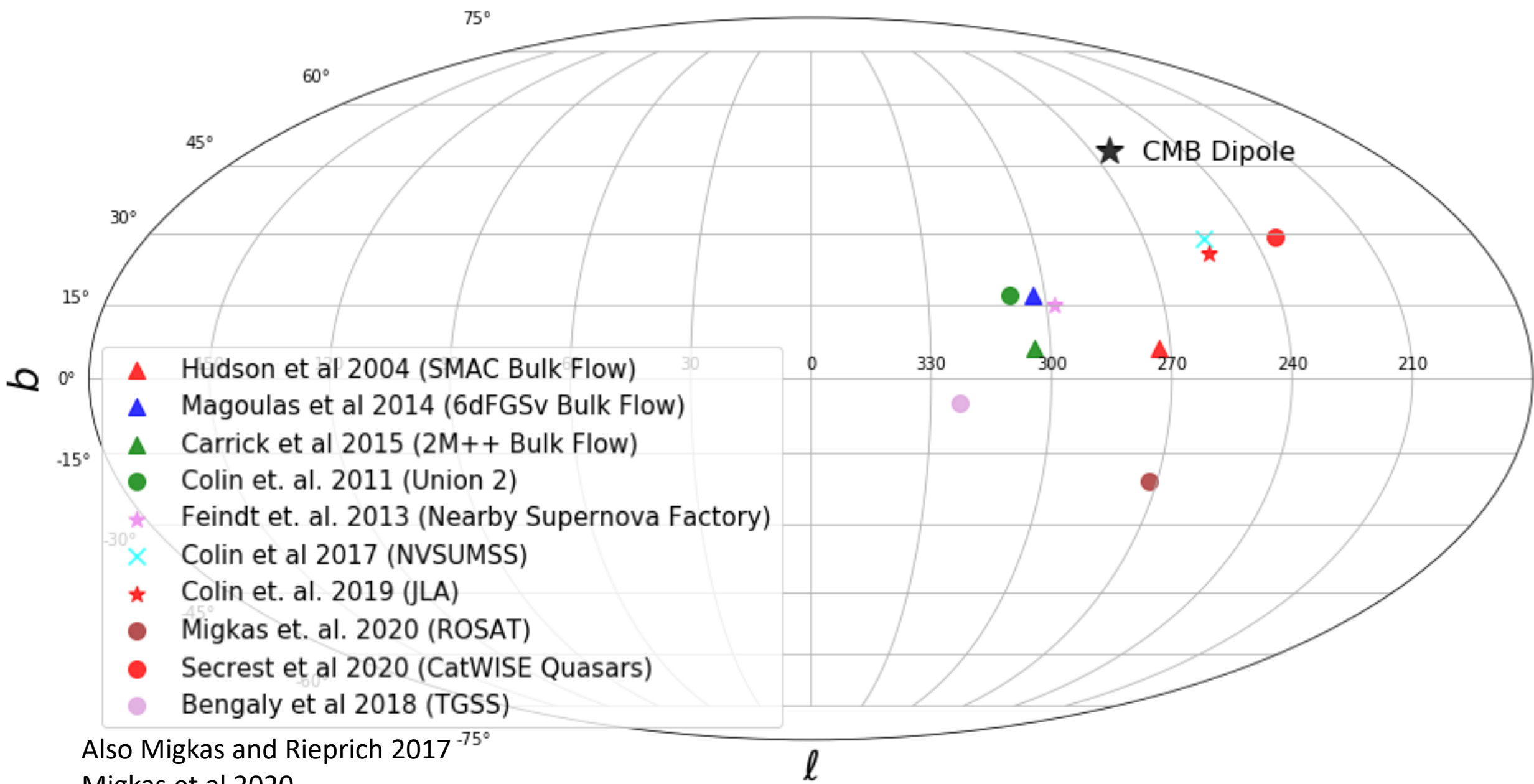
dscolnic closed this on Nov 28, 2018

<https://github.com/dscolnic/Pantheon/issues/2>

This is because in the absence of demonstrable convergence between the bulk flow of the local Universe and the 'CMB rest frame', there is no way to correct for it completely (one could fit it as a nuisance parameter).

Key Hubble tension papers rely on these corrections or directly on the Pantheon compilation (for eg Kenworthy et al 2019)





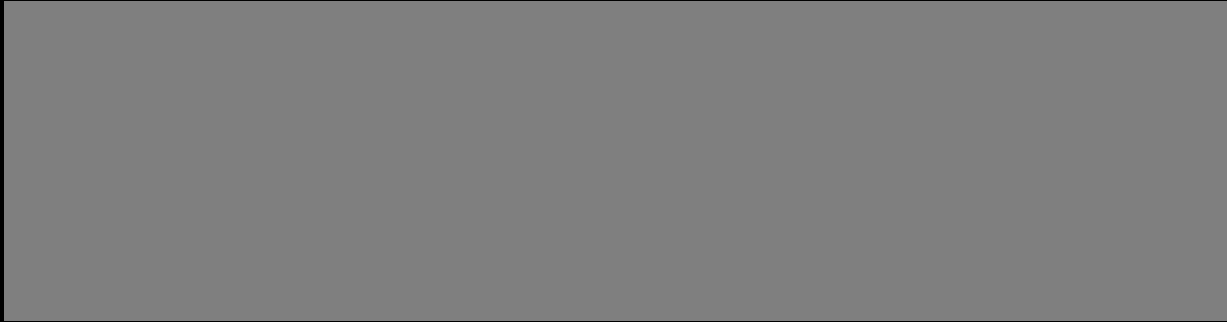
Also Migkas and Rieprich 2017  
Migkas et al 2020.



# What we mean by 'non Copernican observers'

$$R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} + \Lambda g_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

## The FLRW universe



Can be described by one scale factor  $a(t)$  and Friedmann equations exactly.

$$\Omega_M + \Omega_K + \Omega_\Lambda = 1$$

The cosmic sum rule

Maximal symmetry forbids peculiar velocities

Some existing debates in literature (inhomogeneous cosmology/backreactions) suggest that problems such as Dark Matter and Dark Energy can also be tackled by critically examining the tools and framework with which we do cosmology.

## The Real Universe



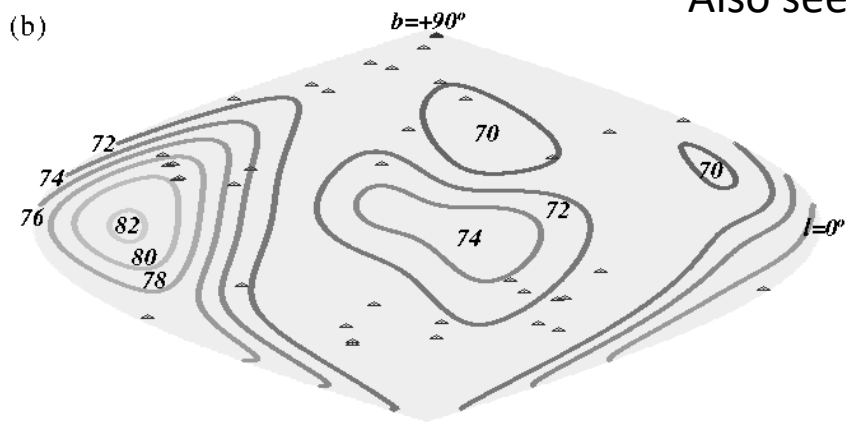
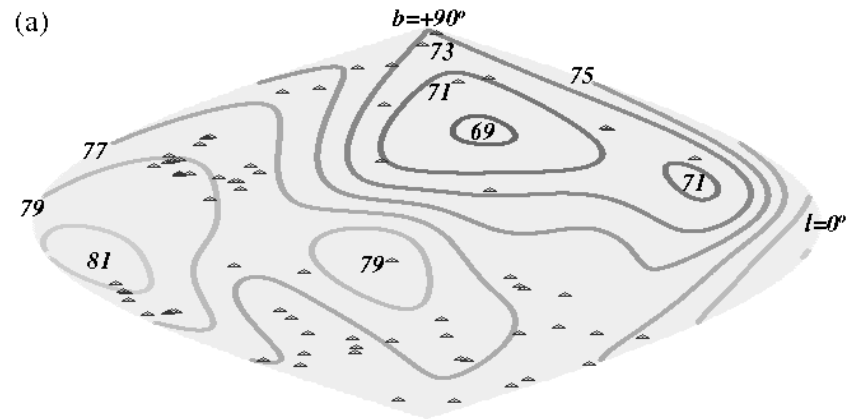
$$\dot{\Theta} = -\frac{\theta^2}{3} - 2\sigma^2 + 2\omega^2 - E[\vec{X}]^a_a + \dot{X}^a_{;a} + \Lambda$$

Ellis, "On the Raychaudhuri Equation"  
Pramana-J.Phys., Vol. 69, No. 1, July 2007

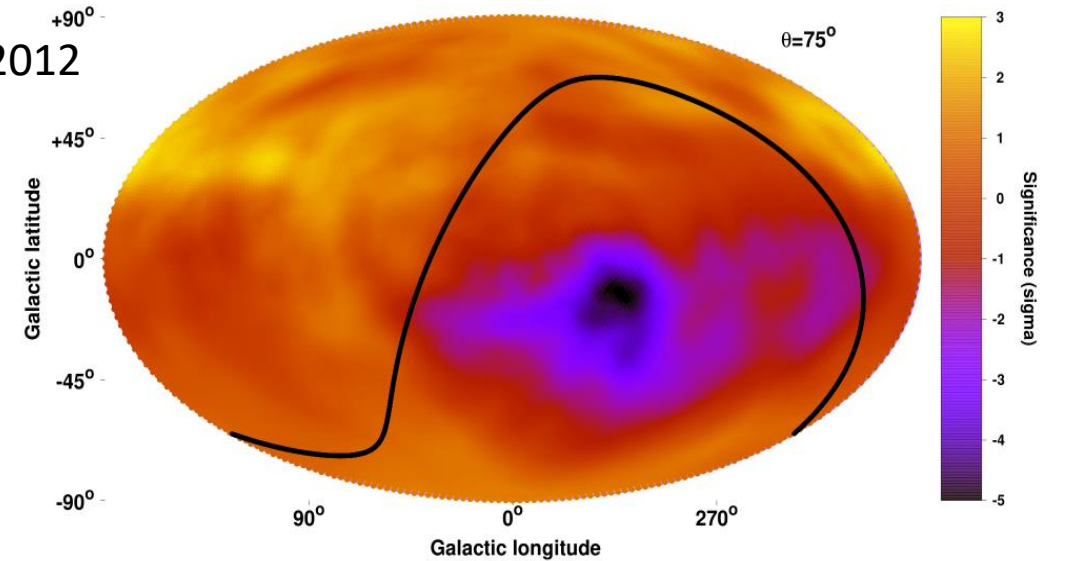
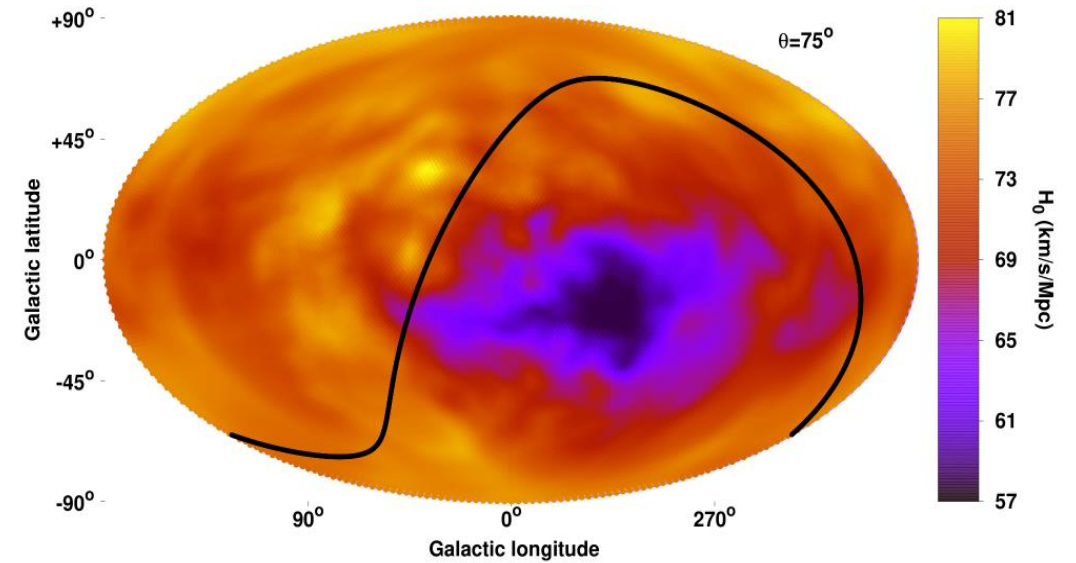
Everything has a peculiar velocity of  $\sim 10^{-3}$ , they should be viewed as differences in the expansion rate of the Universe

# There is no Hubble constant, let alone a tension

McClure and Dyer 2007, motivated by the Raychoudhury Equation



Also see Wiltshire et al 2012



A statistically significant difference in expansion rate of  $9 \text{ km s}^{-1} \text{ Mpc}^{-1}$  is found to occur across the sky.

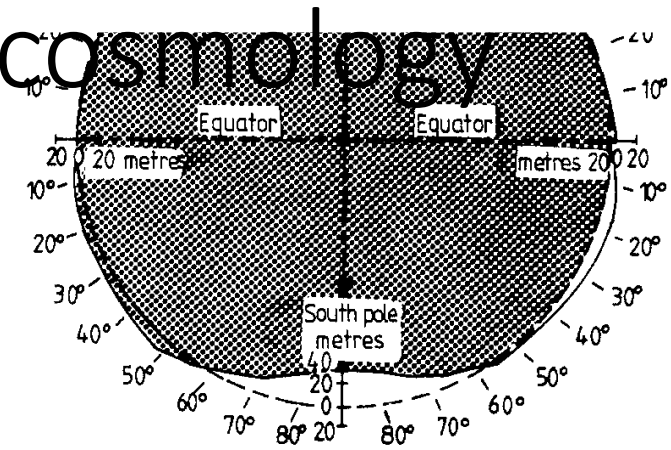
Migkas et al 2020

# Conclusions

- Number counts of flux limited catalogues in radio and infrared all indicate somewhat significant (up to  $\sim 3.9\sigma$ ) tensions with the 'purely kinematic' interpretation of the CMB dipole.
  - Hopeful that SKA and EUCLID can set this to rest by testing.
- Convergence to the CMB rest frame has not been demonstrated.
  - There is a case for precision testing the CMB dipole.
  - The local Universe has a bulk flow out to  $\sim 400$  Mpc.  
McClure and Dyer 2007  
The CMB rest frame does not exist
- SN1a data pre ship with 'corrections' and are being continuously adjusted. The Hubble tension is manufactured using these corrections.
- Evidence  $3.9 \sigma$  for a tilt in the local Universe. Isotropic acceleration compatible with 0 at  $< 1.4$  sigma
- Since  $\Lambda$ CDM cosmology is dying, time to move to an anisotropic cosmology.

# The 'fitting problem' in cosmology

**Abstract.** This paper considers the best way to fit an idealised exactly homogeneous and isotropic universe model to a realistic ('lumpy') universe; whether made explicit or not, some such approach of necessity underlies the use of the standard Robertson-Walker models as models of the real universe. Approaches based on averaging, normal coordinates and null data are presented, the latter offering the best opportunity to relate the fitting procedure to data obtainable by astronomical observations.



**Figure 1.** (a) An exactly uniform and spherically symmetrical FLRW universe  $U'$  mapped into the lumpy universe  $U$  so as to give the best fit possible. (b) An exactly spherical sphere fitted to the lumpy world to give the best fit possible.

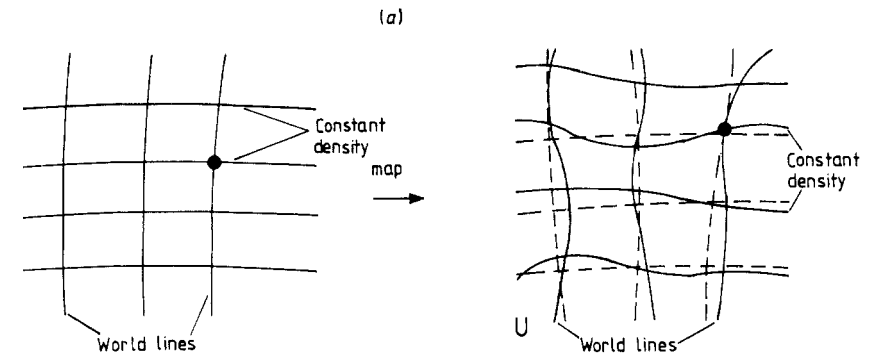
ion

cosmology aims at finding the large-scale matter distribution and spacetime the universe from astronomical observations. There are broadly speaking approaches that have been applied to this problem.

Section 4.3 and 4.4 give a detailed discussion of how to correct for peculiar velocities, isotropize data, fit it to an idealized model, judge goodness of fit and what it means for fundamental physics. Read this along with Conley et al 2011, Rubin & Heitlauf 2019 and Davis et al 2011

The 'fitting problem' in cosmology

1699



# Results

**Table 2.** Tilted local universe, with  $\sigma_z$  set to zero, fitted to data with the MLE.

	$-2 \log \mathcal{L}_{\max}$	$q_m$	$q_d$	$S$	$j_0 - \Omega_k$	$\alpha$	$x_{1,0}$	$\sigma_{x_{1,0}}$	$\beta$	$c_0$	$\sigma_{c_0}$	$M_0$	$\sigma_{M_0}$
Tilted universe	-208.28	-0.157	-8.03	0.0262	-0.489	0.135	0.0394	0.931	3.00	-0.0155	0.071	-19.027	0.114
No tilt ( $q_d = 0$ )	-189.52	-0.166	0	-	-0.460	0.133	0.0396	0.931	2.99	-0.014	0.071	-19.028	0.117
No accn. ( $q_m = 0$ )	-205.98	0	-6.84	0.0384	-0.836	0.134	0.0365	0.931	2.99	-0.014	0.071	-19.002	0.115

**Notes.** The BIC for the models above is -129.00, -123.45, and -133.31, providing strong evidence for the last model.

**Table 3.** Tilted local universe, with  $\sigma_z$  left floating, fitted to data with the MLE.

	$-2 \log \mathcal{L}_{\max}$	$q_m$	$q_d$	$S$	$j_0 - \Omega_k$	$\alpha$	$x_{1,0}$	$\sigma_{x_{1,0}}$	$\beta$	$c_0$	$\sigma_{c_0}$	$M_0$	$\sigma_{M_0}$	$c\sigma_z$ [km s <sup>-1</sup> ]
Tilted universe	-216.90	-0.154	-6.33	0.0305	-0.497	0.134	0.0395	0.932	3.04	-0.0158	0.071	-19.022	0.106	241
No tilt ( $q_d = 0$ )	-203.23	-0.187	0	-	-0.425	0.133	0.0398	0.932	3.05	-0.0151	0.071	-19.032	0.106	274
No accn. ( $q_m = 0$ )	-214.74	0	-5.60	0.0350	-0.833	0.133	0.0368	0.932	3.04	-0.0145	0.071	-19.000	0.106	243

**Notes.** The BIC for the models above is -131.01, -130.55, and -135.46, providing positive evidence for the last model.

The dipolar component of  $q$  is larger than the monopole, and dominates out to  $z > 0.1$

The significance of  $q_o$  being negative is  $< 1.4\sigma$ !

Cosmic acceleration may simply be an artefact of our being located inside a 'bulk flow'!

# Results

$q_d \gg q_m$

**Table 2.** Tilted local universe, with  $\sigma_z$  set to zero, fitted to data with the MLE.

	$-2 \log \mathcal{L}_{\max}$	$q_m$	$q_d$	$S$	$j_0 - \Omega_k$	$\alpha$	$x_{1,0}$	$\sigma_{x_{1,0}}$	$\beta$	$c_0$
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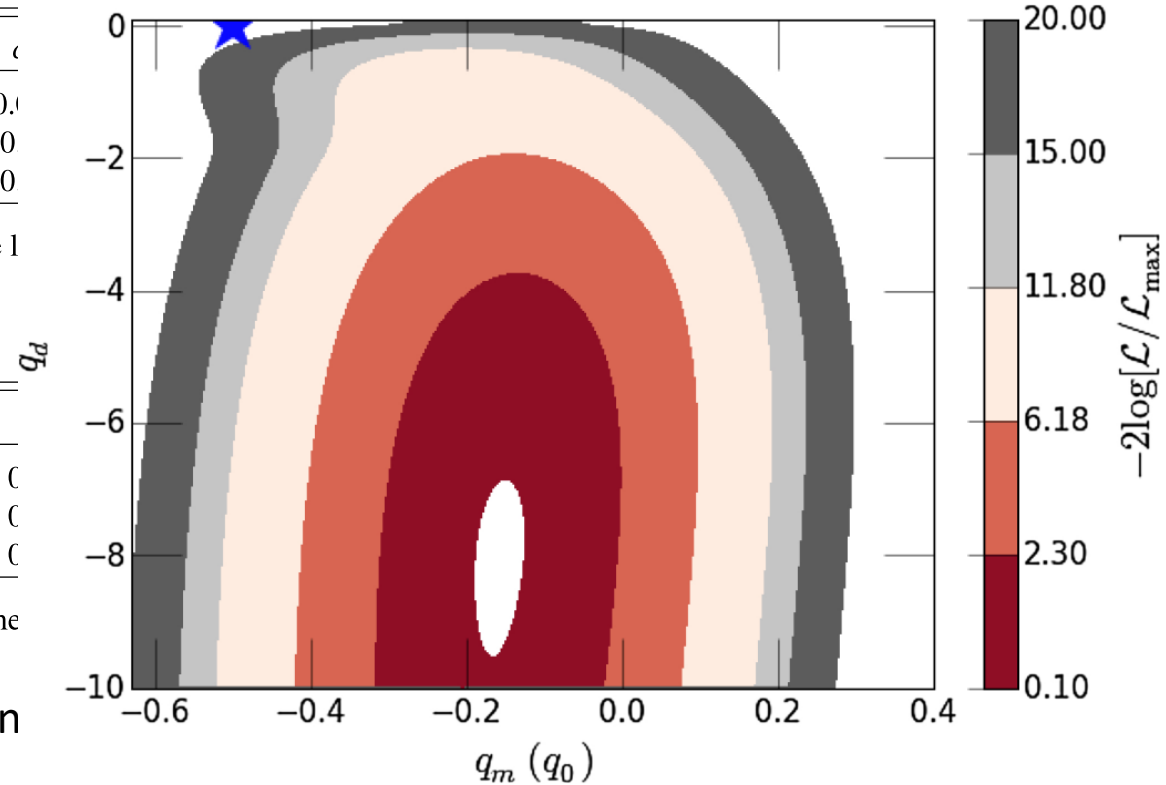
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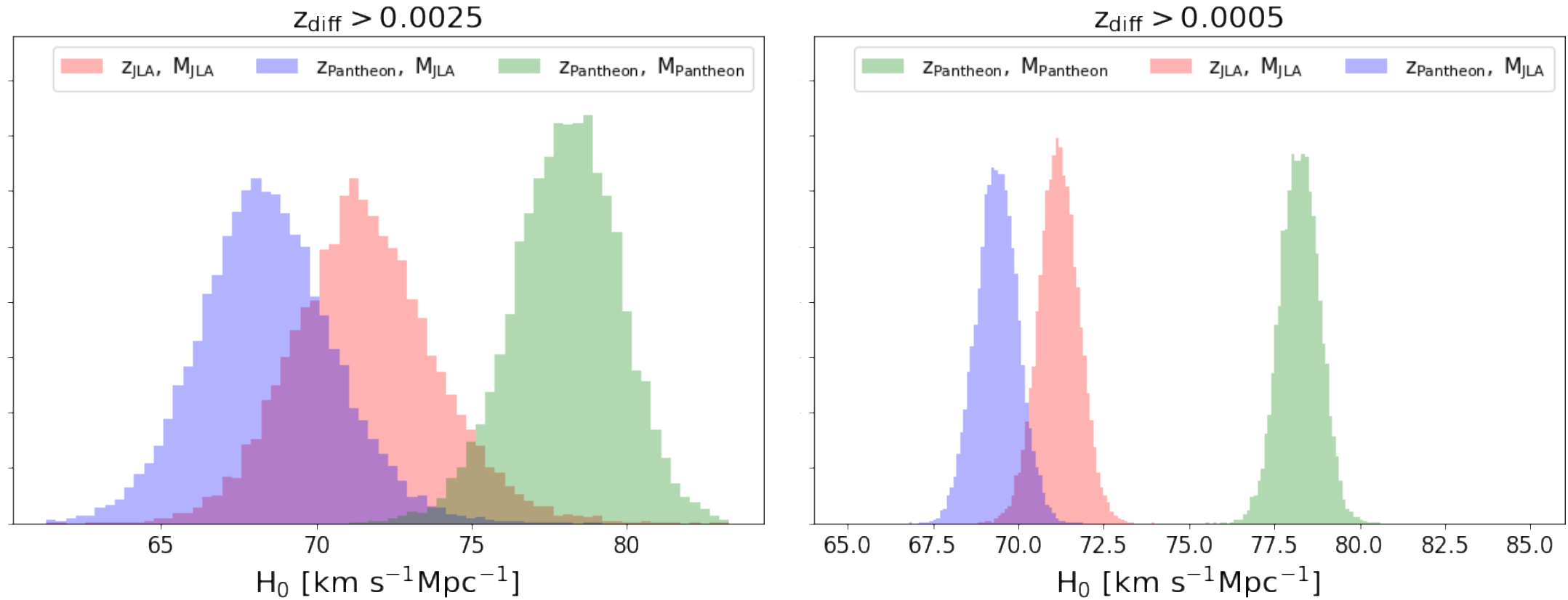
The dipolar component of  $q$  is larger than the monopole, and dominant



The significance of  $q_0$  being negative is  $<1.4\sigma$ !

Cosmic acceleration may simply be an artefact of our being located inside a 'bulk flow'!

# A trivial solution to the Hubble tension?

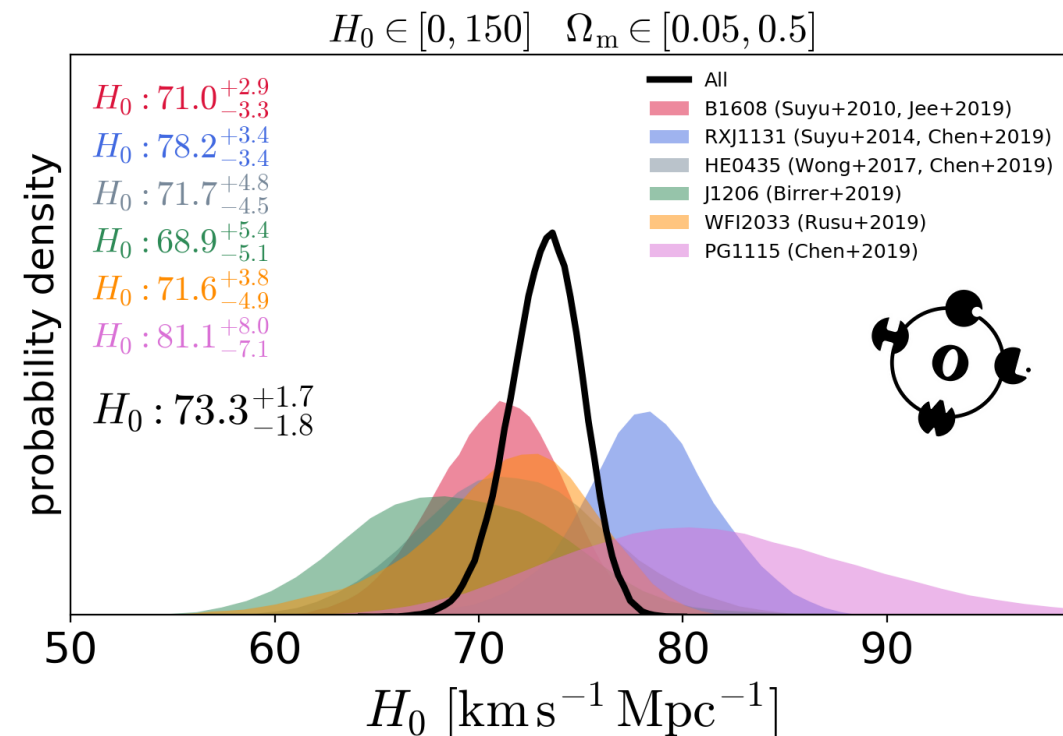


The shifts in redshift and magnitude appear to be sufficient to lower the Hubble 'constant' from  $\sim 72$  to 68, keeping many other parameters fixed to that of Riess et al 2016

# What is $\Lambda$ CDM cosmology?

The naive fitting of data from the real Lumpy Universe, to a smooth toy model, treating all scatter as statistical, when it could be cosmological

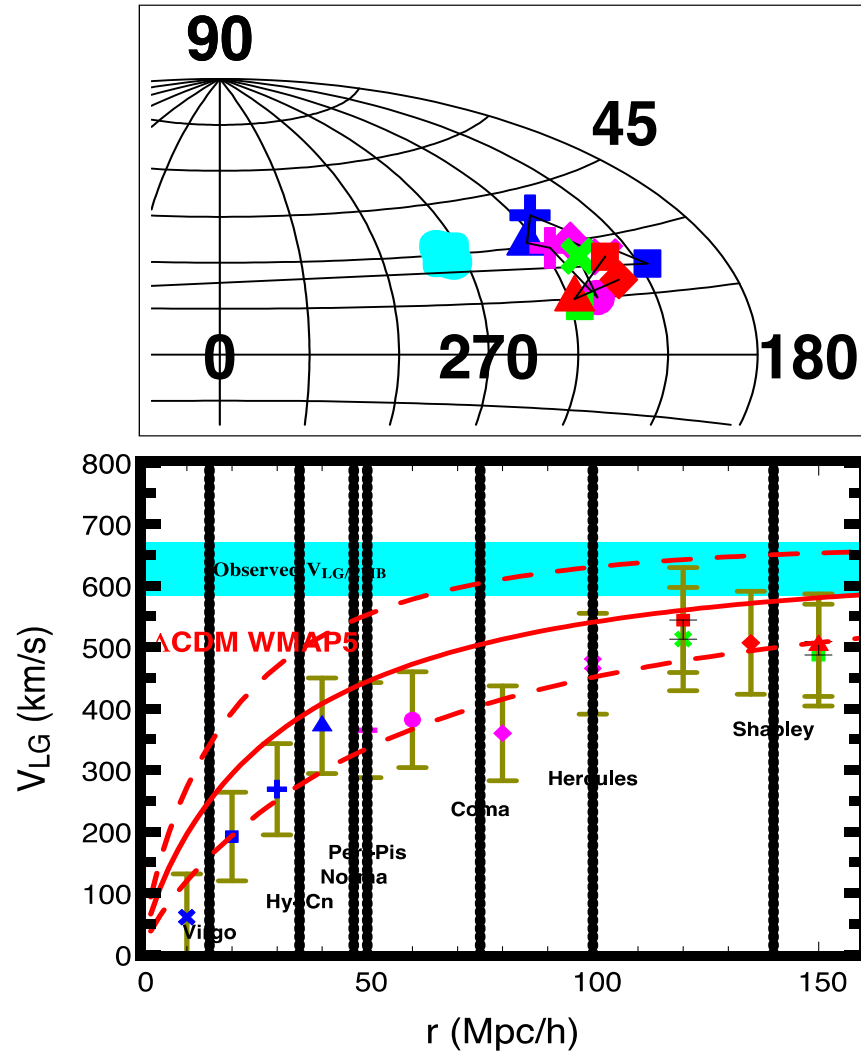
Such as this H0licow measurement



Note : This is very honestly communicated

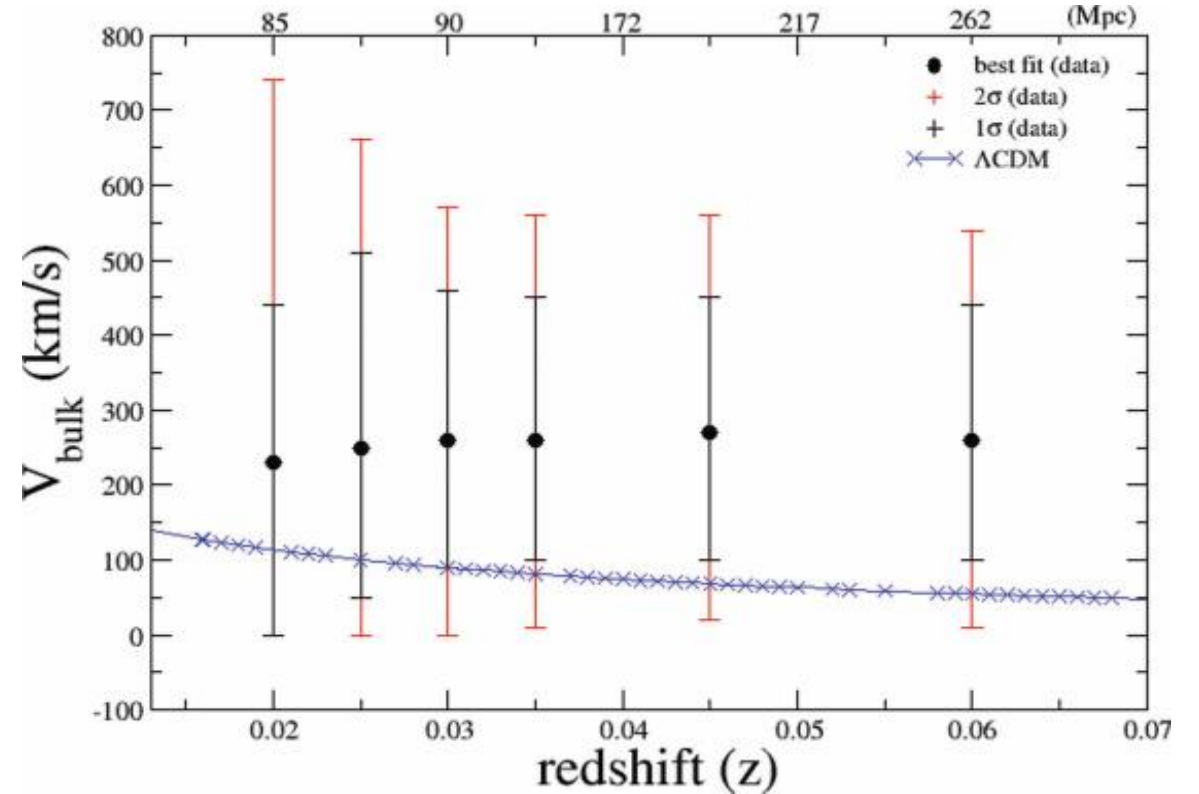


# Where is the cosmic 'rest frame'?



G. Lavaux, R. Brent Tully, R. Mohayaee, S. Colombi

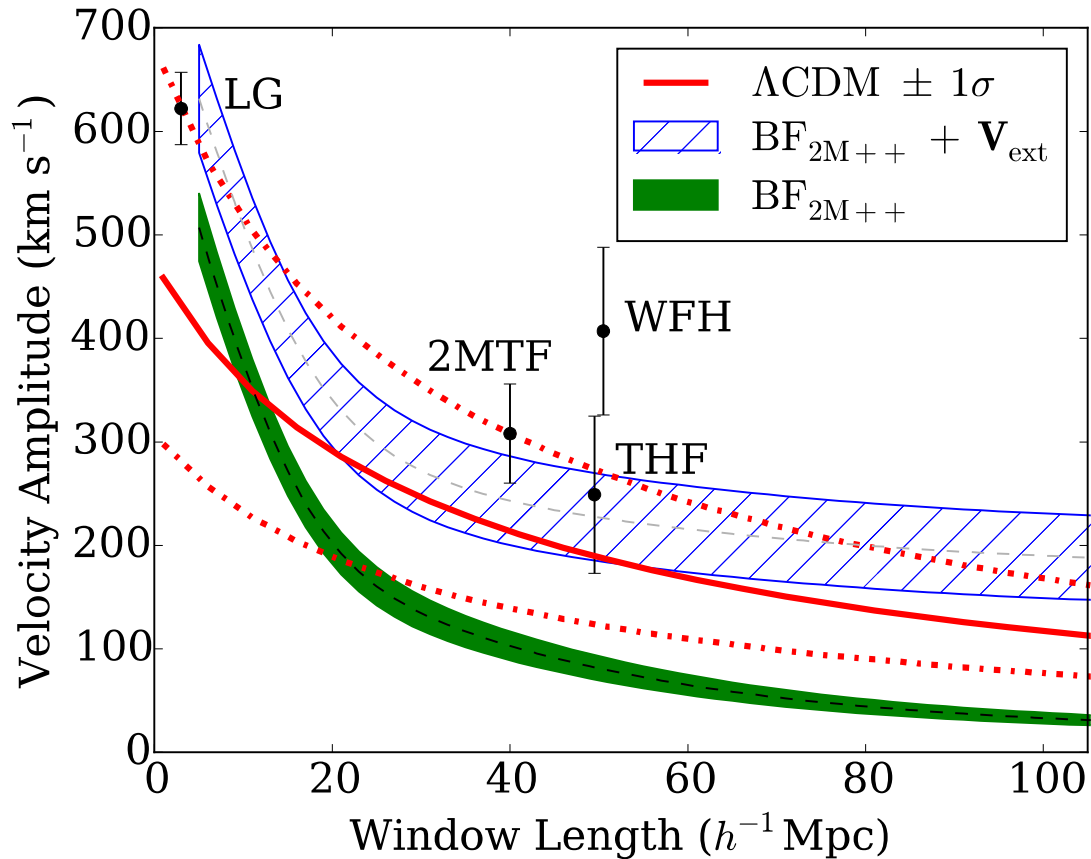
• *Astrophys.J.* 709 (2010) 483-498



Colin J., Mohayaee R., Sarkar S. & Shafieloo A.,  
2011, *MNRAS*, 414, 264

Confirmed by Feindt et al

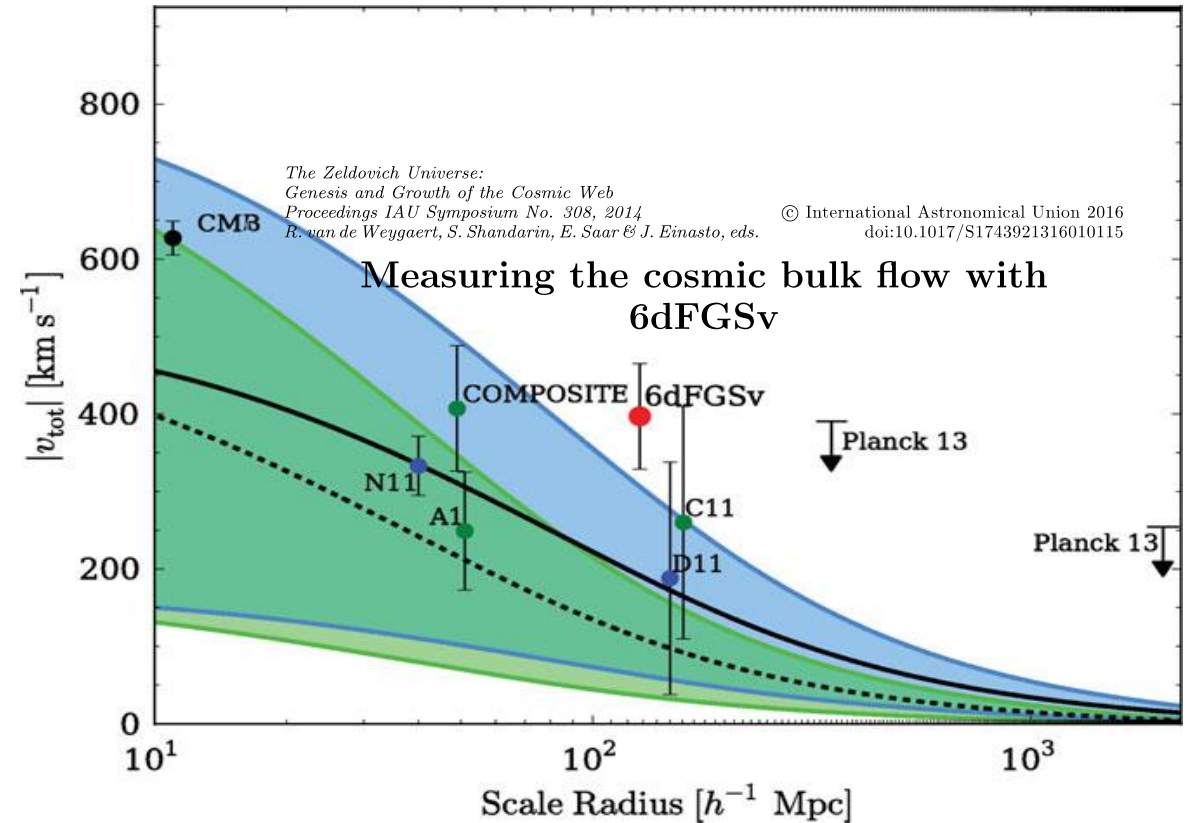
# Where is the cosmic 'rest frame'?



Carrick, Turnbull, Lavaux, Hudson *MNRAS*, 450, 1, 11 2015, 317–332

“We find that an external bulk flow is preferred at the  $5.1\sigma$  level, and the best fit has a velocity of  $159 \pm 23 \text{ km s}^{-1}$  towards  $l = 304^\circ \pm 11^\circ$ ,  $b = 6^\circ \pm 13^\circ$  [beyond 300 Mpc radius]

Measuring the cosmic bulk flow with 6dFGSv



Magoulas et al, 2014

Springbob et al 2014

# But the real Universe has structure on all scales

## The FLRW universe



Can be described by one scale factor  $a(t)$  and Friedmann equations exactly.

Maximal symmetry forbids peculiar velocities

## The Real Universe



$$\dot{\Theta} = -\frac{\theta^2}{3} - 2\sigma^2 + 2\omega^2 - E[\vec{X}]^a_a + \dot{X}^a_{;a} + \Lambda$$

Ellis, "On the Raychaudhuri Equation"  
Pramana–J.Phys., Vol. 69, No. 1, July 2007

Everything has a peculiar velocity of  $10^{-3}$

We can observe only one.

The Real Universe has structure on much smaller scales than our representations of it

# Standard Cosmology

N body simulations assume the existence of a background FLRW metric and use Newtonian gravity (which is the zero velocity weak field of GR).

Linearizations, perturbation theory, initial conditions from inflation

Peculiar velocities are things moving w.r.t. a FLRW background

Defended by authors of GR textbooks such as Robert Wald, using heuristic arguments.

# Inhomogeneous Cosmology

Real Universe can only be represented by an FLRW metric. Large scale dynamics obtained from the 'coarse graining' of small scale dynamics.

Is a complex system with nonlinear dynamics.

Peculiar velocities are differences in the expansion rate of the Universe

Has a true metric that is everywhere far from FLRW

Talks about almost flat, almost isotropic, almost FLRW cosmologies

Leading cosmologists, authors of textbooks such as Ellis and Kolb take this view.

There is an averaging problem, a fitting problem and backreactions. Clarkson et al 2011 Rept.Prog.Phys. 74 (2011) 112901

# The 'fitting problem' in cosmology

**Abstract.** This paper considers the best way to fit an idealised exactly homogeneous and isotropic universe model to a realistic ('lumpy') universe; whether made explicit or not, some such approach of necessity underlies the use of the standard Robertson-Walker models as models of the real universe. Approaches based on averaging, normal coordinates and null data are presented, the latter offering the best opportunity to relate the fitting procedure to data obtainable by astronomical observations.

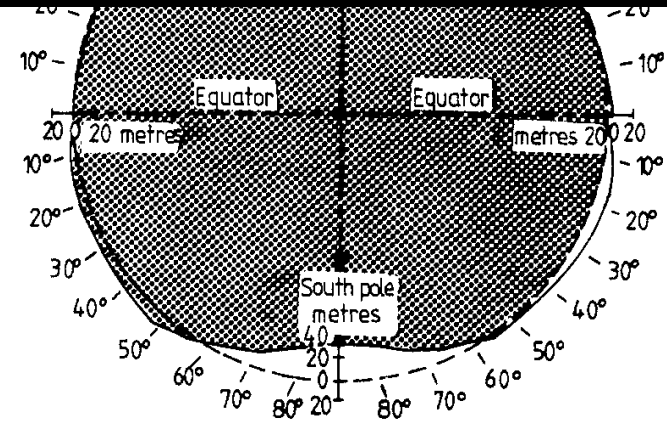


Figure 1. (a) An exactly uniform and spherically symmetrical FLRW universe  $U'$  mapped to the lumpy universe  $U$  so as to give the best fit possible. (b) An exactly spherical universe fitted to the lumpy world to give the best fit possible.

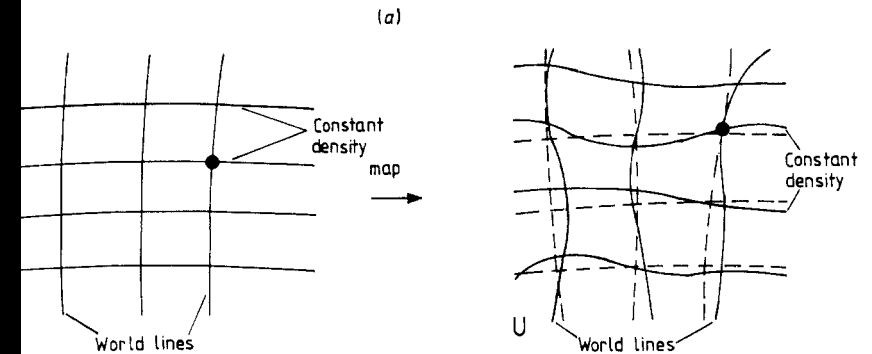
on

cosmology aims at finding the large-scale matter distribution and spacetime geometry of the universe from astronomical observations. There are broadly speaking several approaches that have been applied to this problem.

Section 4.3 and 4.4 give a detailed discussion of how to correct for peculiar velocities, isotropize data, fit it to an idealized model, judge goodness of fit and what it means for fundamental physics

The 'fitting problem' in cosmology

1699



# Test this with a sample of 740 Type 1a Supernovae

**Table 2.** Tilted local universe, with  $\sigma_z$  set to zero, fitted to data with the MLE.

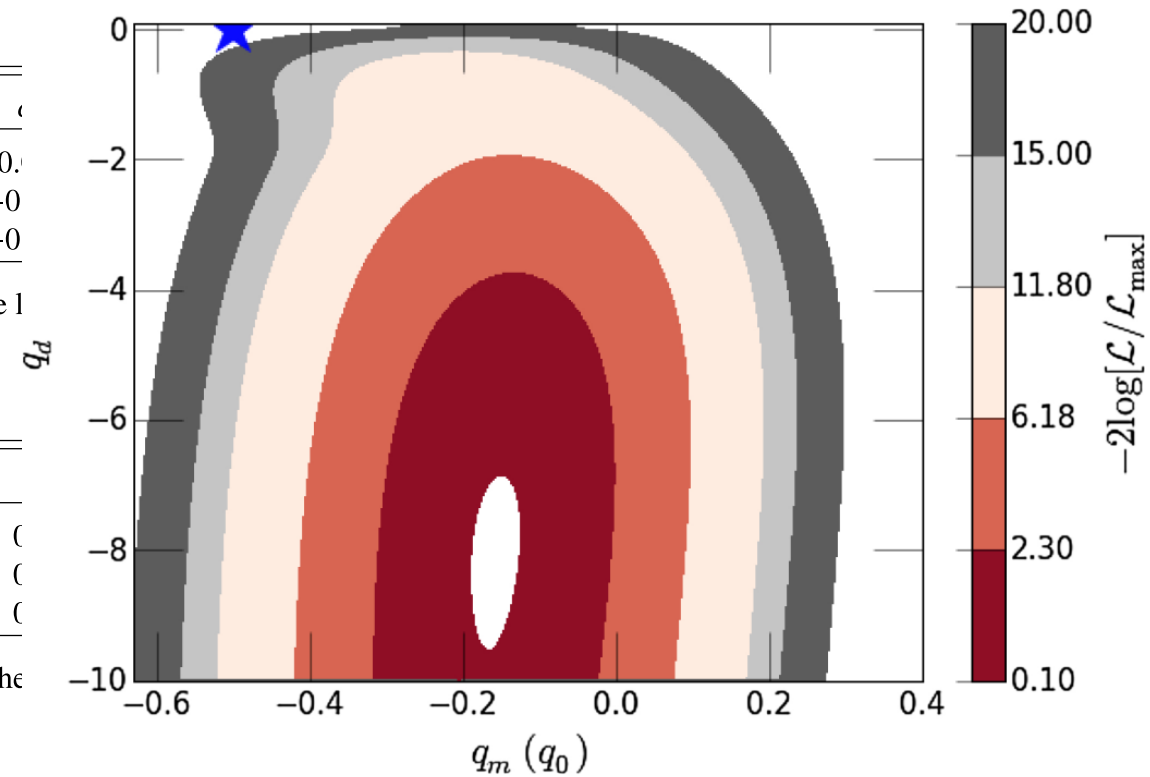
	$-2 \log \mathcal{L}_{\max}$	$q_m$	$q_d$	$S$	$j_0 - \Omega_k$	$\alpha$	$x_{1,0}$	$\sigma_{x_{1,0}}$	$\beta$	$c_0$
Tilted universe	-208.28	-0.157	-8.03	0.0262	-0.489	0.135	0.0394	0.931	3.00	-0.0158
No tilt ( $q_d = 0$ )	-189.52	-0.166	0	-	-0.460	0.133	0.0396	0.931	2.99	-0.0151
No accn. ( $q_m = 0$ )	-205.98	0	-6.84	0.0384	-0.836	0.134	0.0365	0.931	2.99	-0.0145

**Notes.** The BIC for the models above is -129.00, -123.45, and -133.31, providing strong evidence for the tilted universe.

**Table 3.** Tilted local universe, with  $\sigma_z$  left floating, fitted to data with the MLE.

	$-2 \log \mathcal{L}_{\max}$	$q_m$	$q_d$	$S$	$j_0 - \Omega_k$	$\alpha$	$x_{1,0}$	$\sigma_{x_{1,0}}$	$\beta$	$c_0$
Tilted universe	-216.90	-0.154	-6.33	0.0305	-0.497	0.134	0.0395	0.932	3.04	-0.0158
No tilt ( $q_d = 0$ )	-203.23	-0.187	0	-	-0.425	0.133	0.0398	0.932	3.05	-0.0151
No accn. ( $q_m = 0$ )	-214.74	0	-5.60	0.0350	-0.833	0.133	0.0368	0.932	3.04	-0.0145

**Notes.** The BIC for the models above is -131.01, -130.55, and -135.46, providing positive evidence for the tilted universe.



The dipolar component of  $q$  is larger than the monopole, and dominates out to  $z \sim 0.1$

$$q_d \gg q_m$$

The significance of  $q_0$  being negative is  $< 1.4\sigma$ !

Cosmic acceleration may simply be an artefact of our being located inside a 'bulk flow'! : Non Copernican observers

Rubin & Hayden (ApJ 833:L30,2016) verify the results of Nielsen et al  
 but then argue that the light-curve fit parameters may be redshift-dependent

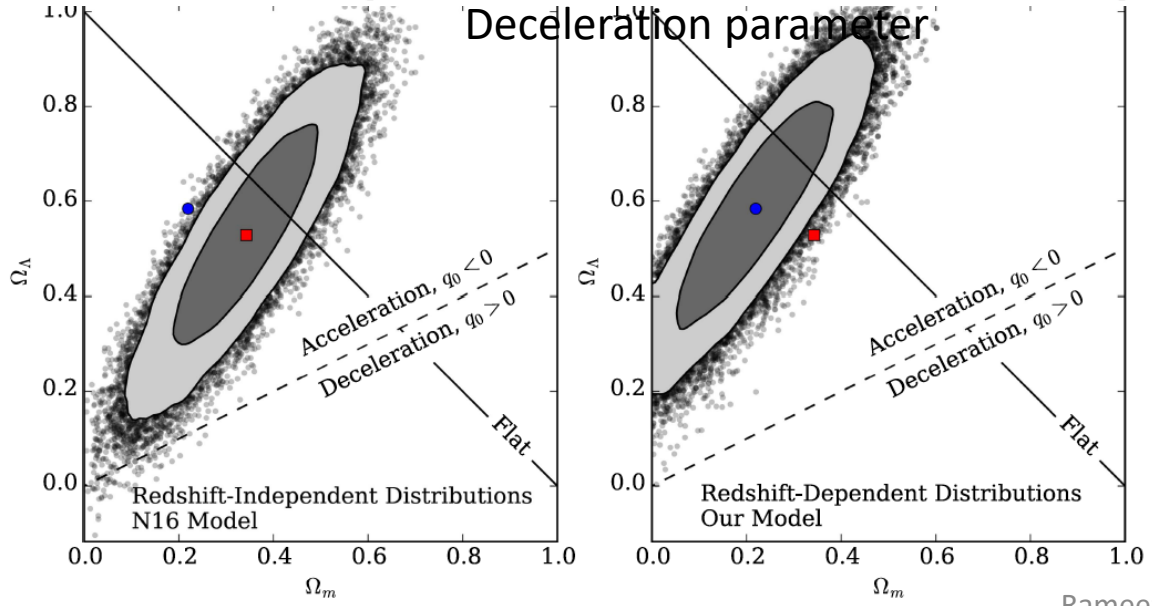
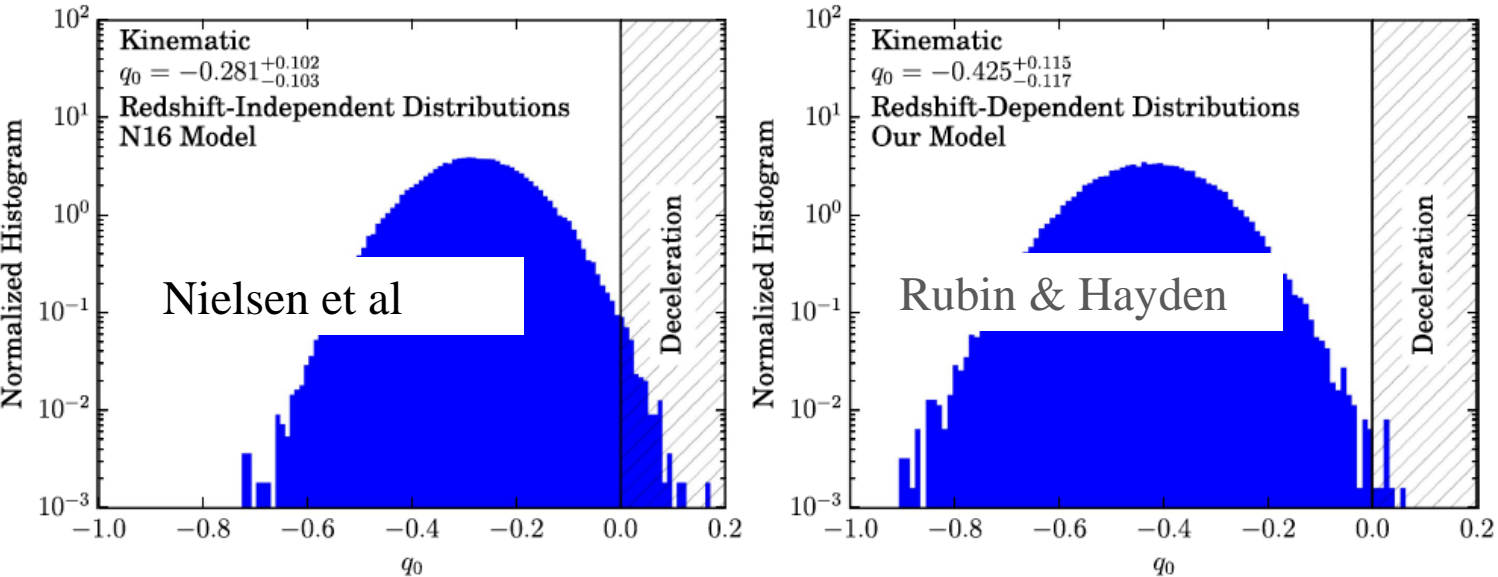


Figure 2.  $\Omega_m$ - $\Omega_\Lambda$  constraints enclosing 68.3% and 95.4% of the samples from the posterior. Underneath, we plot all samples. The left panel shows the constraints obtained with  $x_1$  and  $c$  distributions that are constant in redshift, as in the N16 analysis; the right panel shows the constraints from our model. The red square and blue circle show the location of the median of the respective posteriors.

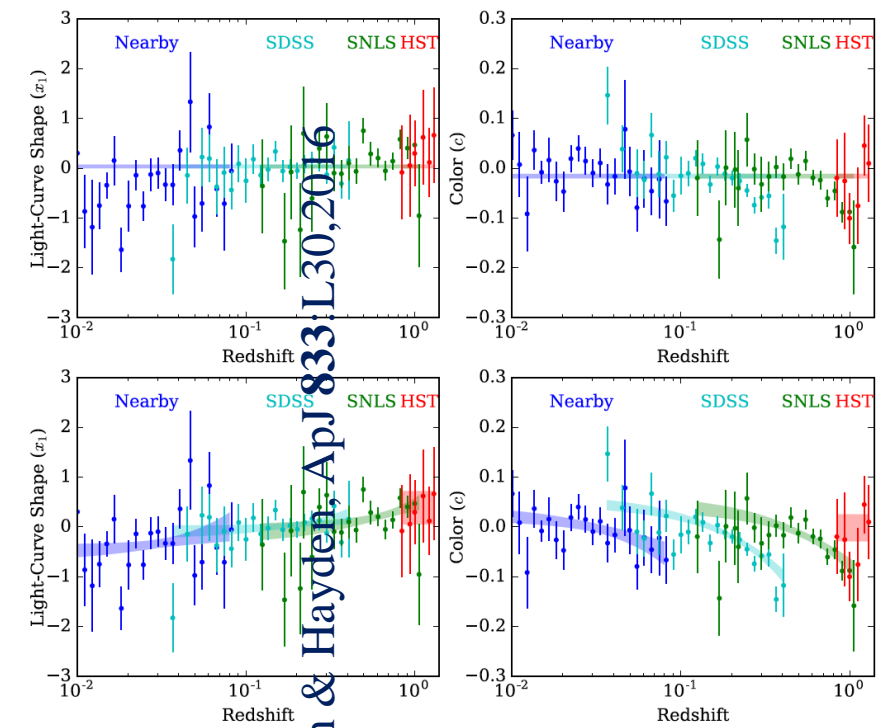
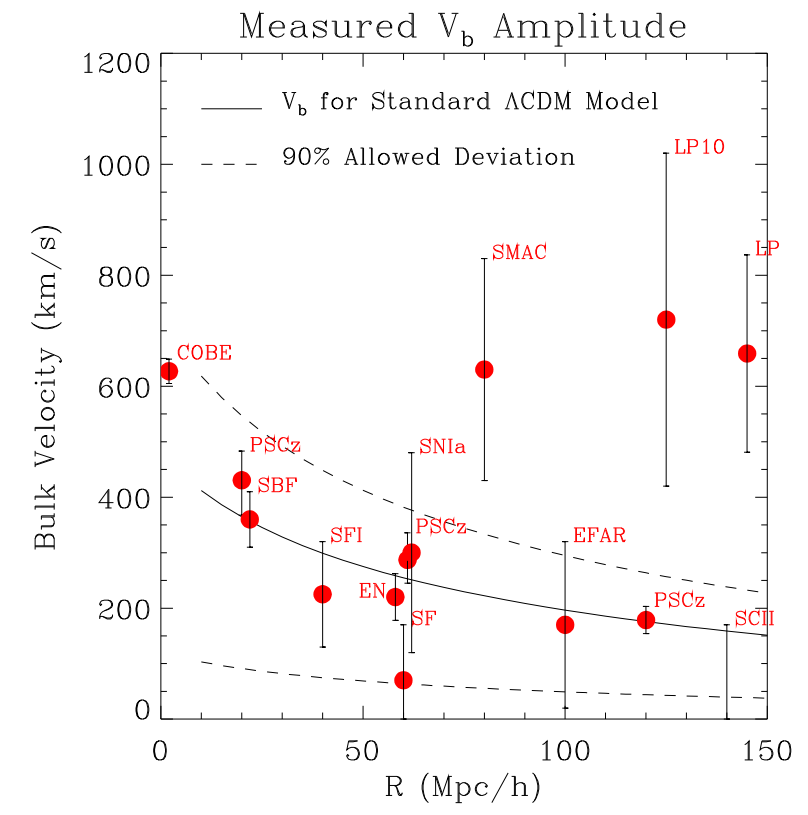
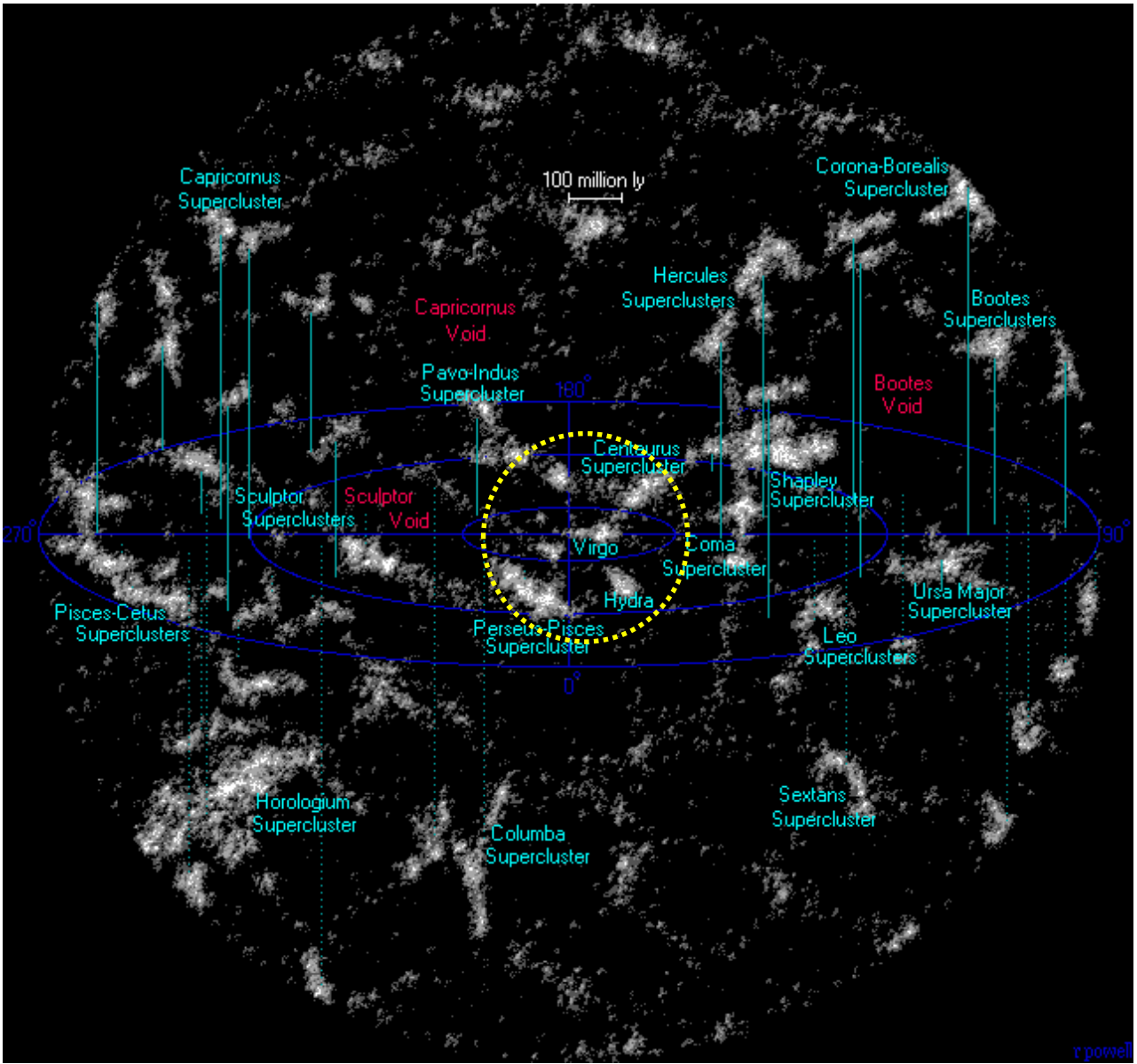


Figure 1. Binned  $x_1$  (left panels) and  $c$  (right panels) light-curve parameters as a function of redshift for the JLA sample. The trend of color with redshift within each ground-based sample is expected due to the combination of the color-luminosity relation combined with redshift-dependent luminosity detection limits. The top panels show the 68% credible constraints on a constant-in-redshift model, as was used in N16. The bottom panels show our proposed revision. Failing to model the drift in the mean observed distributions demonstrated by the bottom panels will tend to cause high-redshift SNe to appear brighter on average, therefore reducing the significance of accelerating expansion.

Two out of 3 parameters that go into the distance modulus have been examined by eye and made sample and redshift dependent.  
 Against the principles of blinded data analysis.  
 20 hyperparameters to standardize 740 SN1e

Even if this is justified, the significance with which a non-accelerating universe is rejected rises only to  $\lesssim 4\sigma$  — still inadequate to claim a ‘discovery’ (even though the dataset has increased from ~50 to 740 SNe Ia in 20 yrs)!

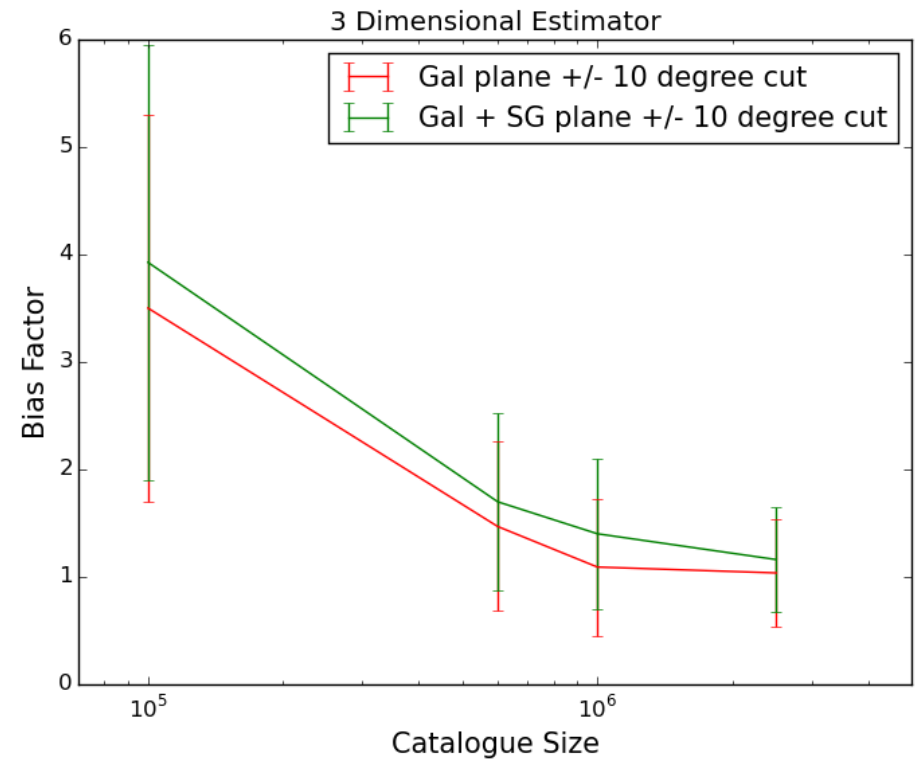
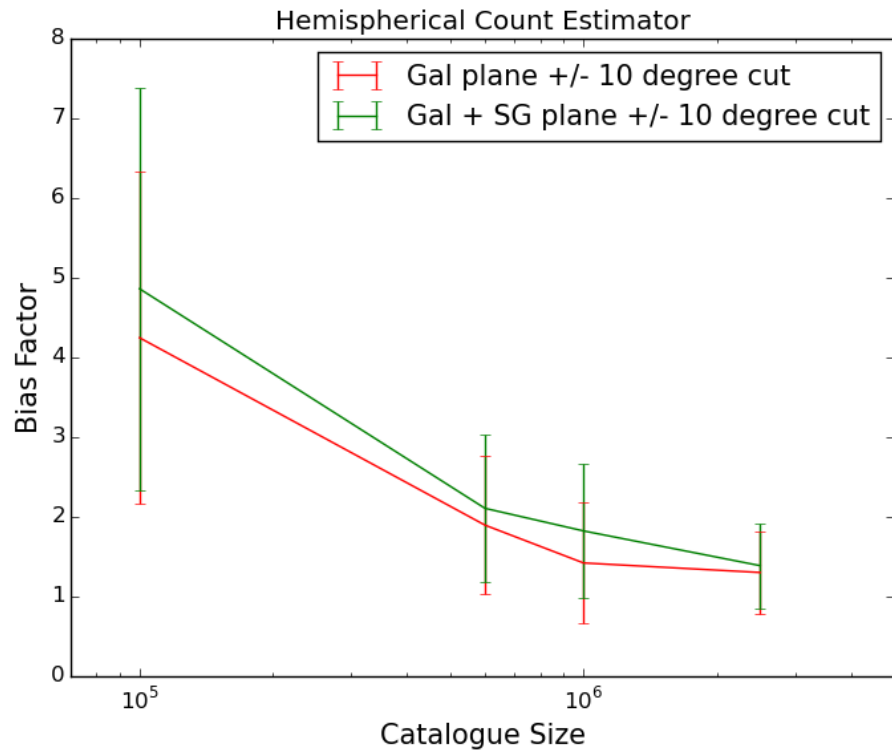




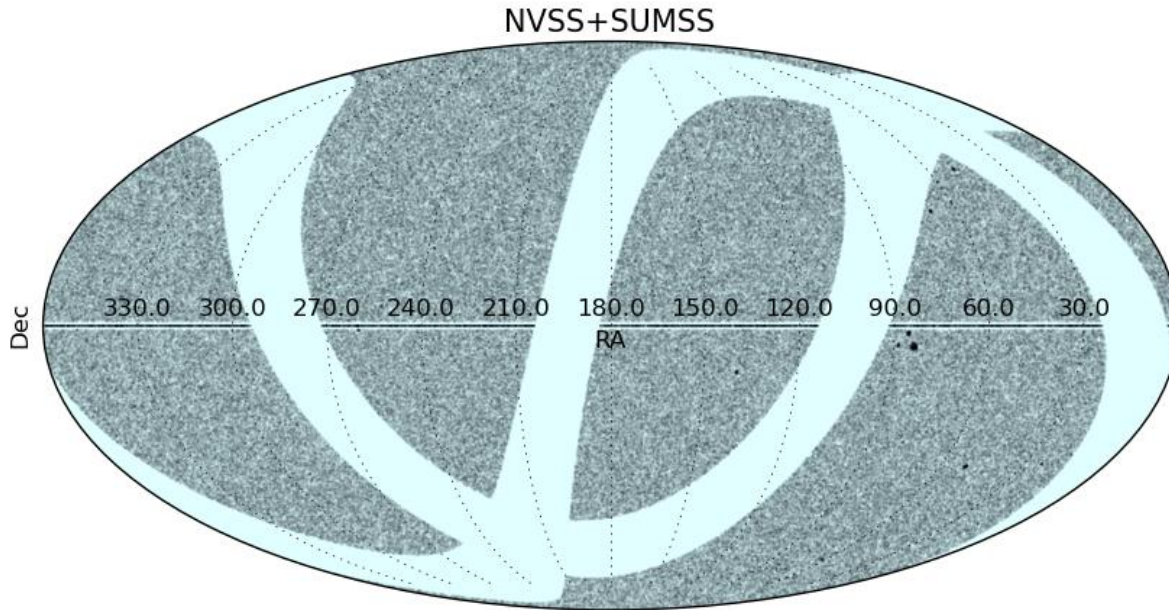
# Estimators for the Dipole

$$\vec{D}_H = \hat{z} * \frac{N_{UH} - N_{LH}}{N_{UH} + N_{LH}}$$

$$\vec{D}_{3D} = \frac{1}{N} \sum_{i=1}^N \hat{r}_i$$



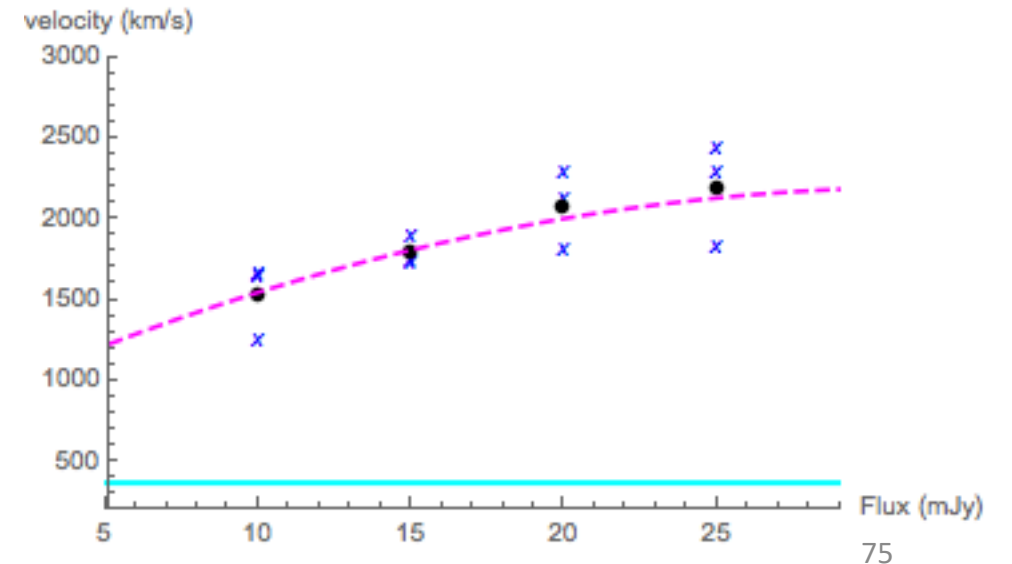
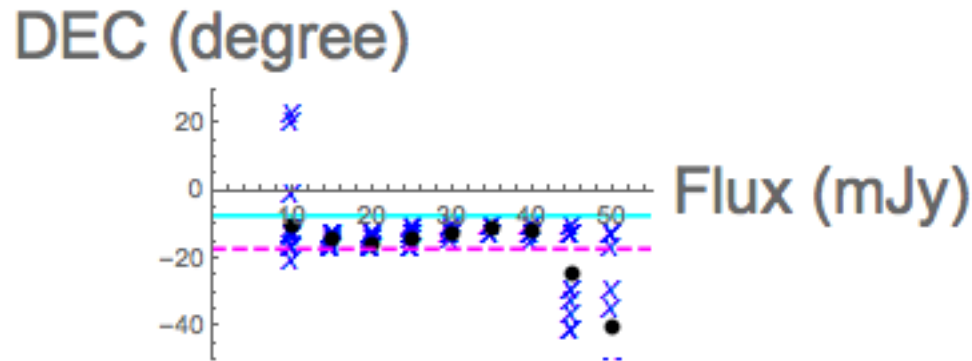
# Local Sources contamination?



Remove the Supergalactic plane. Disk like structure containing the majority of clusters at  $z < 0.03$

Remove sources within 1 arcsecond of 2MRS  $z < 0.03$  sources

No significant impact on the velocity/direction of the dipole



	$-2 \log \mathcal{L}_{\max}$	$q_m$	$q_d$	$S$	$j_0 - \Omega_k$	$\alpha$	$\beta$	$M_0$	$\sigma_{M_0}$
Rubin & Hayden (22 param.) with no dipole	-331.6	-0.4574	–	–	0.1458	0.1345	3.067	-19.07	0.1074
As above with no acceleration ( $q_m = 0$ )	-315.6	0	–	–	-1.351	0.1323	3.048	-19.01	0.1088
Rubin & Hayden (22 param.) with dipole $\propto e^{-z/S}$	-335.9	-0.3867	-0.2325	0.1825	-0.1779	0.1337	3.028	-19.06	0.1076
As above with no acceleration ( $q_m = 0$ )	-326.9	0	-2.186	0.05034	-1.333	0.1325	3.02	-19.01	0.1087
Rubin & Hayden (16 param.) with no dipole	-242.4	-0.3873	–	–	0.2937	0.1345	3.063	-19.05	0.1080
As above with no acceleration ( $q_m = 0$ )	-229.9	0	–	–	-0.8444	0.1325	3.051	-19.00	0.1094
Rubin & Hayden (16 param.) with dipole $\propto e^{-z/S}$	-250.2	-0.3329	-0.2091	0.2726	0.04258	0.1336	3.021	-19.04	0.1081
As above with no acceleration ( $q_m = 0$ )	-241.2	0	-0.3585	0.1794	-0.8645	0.132	3.009	-19.00	0.1093
Rubin & Hayden (16 + 3 param.) with no dipole	-253.4	-0.09894	–	–	-0.102	0.1346	3.023	-19.07, -19.00, -18.94, -18.78	0.1082
As above with no acceleration ( $q_m = 0$ )	-253	0	–	–	-0.2661	0.1344	3.016	-19.06, -18.99, -18.92, -18.77	0.1084

Even with the sample and redshift dependent treatment for  $x_{1,0}$  and  $c_0$  proposed by R&H,  $q_m=0$  is disfavoured only at 2.4 sigma and allows for a large  $q_d$  extending to  $z \sim 0.18$

If  $x_{1,0}$  and  $c_0$  can be sample or redshift dependent, why not  $M_0$ ? Undermines the use of SN1a as standard candles but justified by AIC.

# Planck 2015

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Parameter	<i>Planck</i> TT+lowP+lensing
$\Omega_b h^2$ . . . . .	$0.02226 \pm 0.00023$
$\Omega_c h^2$ . . . . .	$0.1186 \pm 0.0020$
$100\theta_{MC}$ . . . . .	$1.04103 \pm 0.00046$
$\tau$ . . . . .	$0.066 \pm 0.016$
$\ln(10^{10} A_s)$ . . . . .	$3.062 \pm 0.029$
$n_s$ . . . . .	$0.9677 \pm 0.0060$
$H_0$ . . . . .	$67.8 \pm 0.9$
$\Omega_m$ . . . . .	$0.308 \pm 0.012$
$\Omega_m h^2$ . . . . .	$0.1415 \pm 0.0019$
$\Omega_m h^3$ . . . . .	$0.09591 \pm 0.00045$
$\sigma_8$ . . . . .	$0.815 \pm 0.009$
$\sigma_8 \Omega_m^{0.5}$ . . . . .	$0.4521 \pm 0.0088$
Age/Gyr . . . . .	$13.799 \pm 0.038$
$r_{drag}$ . . . . .	$147.60 \pm 0.43$
$k_{eq}$ . . . . .	$0.01027 \pm 0.00014$

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<https://arxiv.org/pdf/1706.09309.pdf>

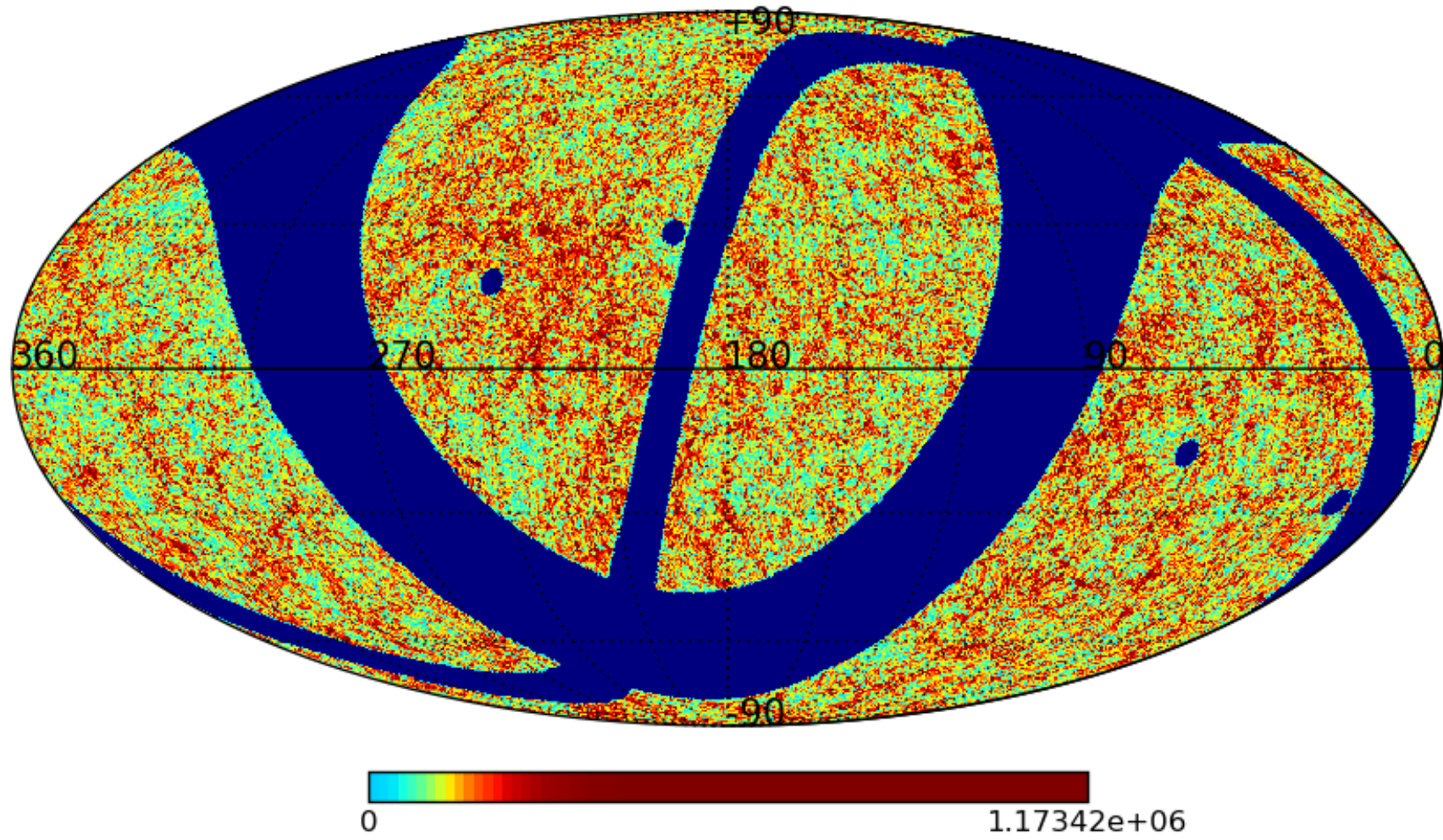
<https://arxiv.org/pdf/1505.07800.pdf>

# On the measurement of cosmological parameters

Rupert A. C. Croft, Matthew Dailey (CMU)

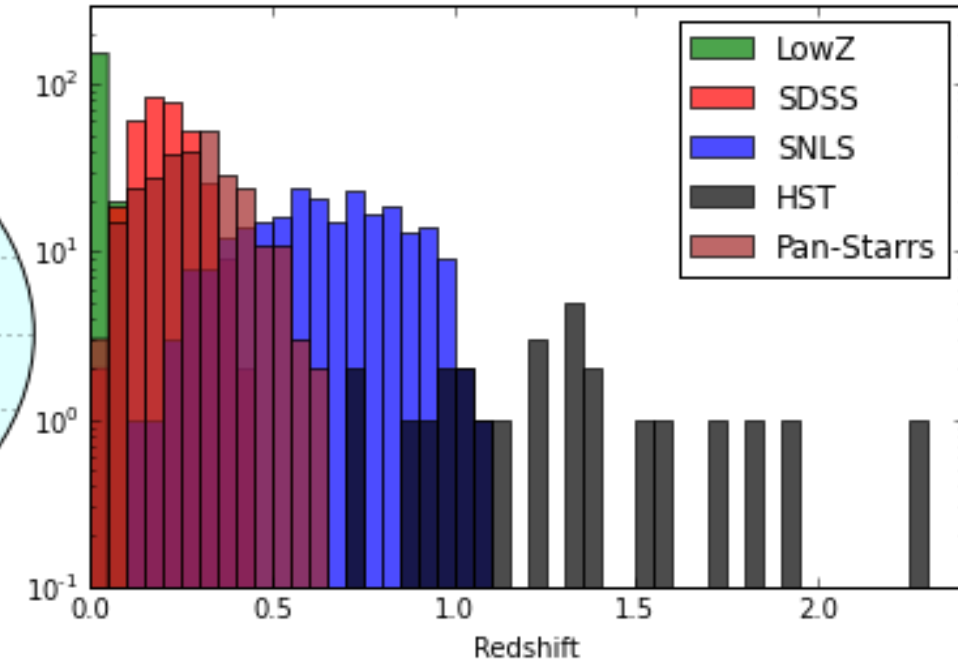
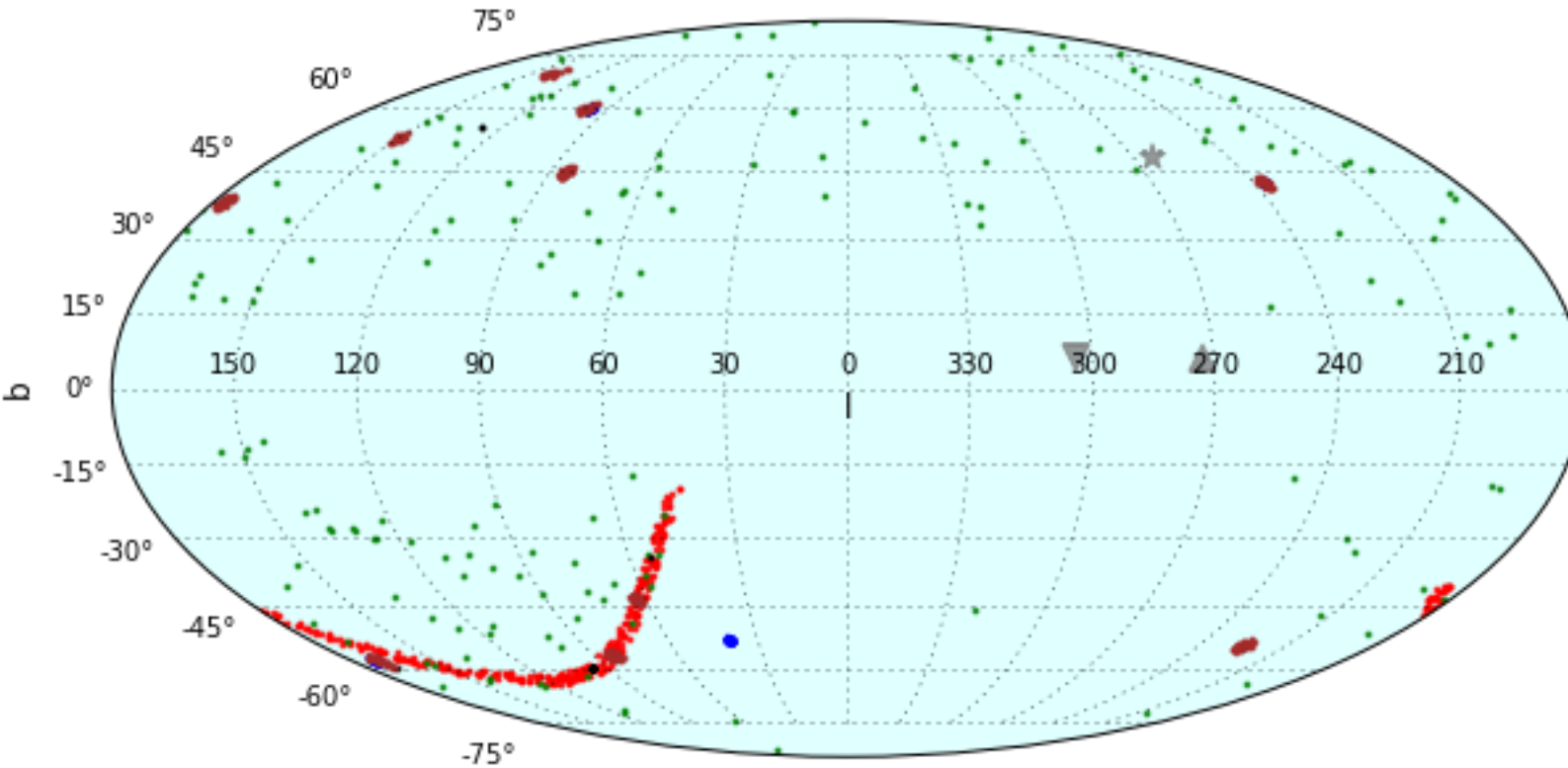
*(Submitted on 14 Dec 2011 (v1), last revised 21 Jul 2015 (this version, v2))*

We have catalogued and analysed cosmological parameter determinations and their error bars published between the years 1990 and 2010. Our study focuses on the number of measurements, their precision and their accuracy. The accuracy of past measurements is gauged by comparison with the WMAP7 results. The 637 measurements in our study are of 12 different parameters and we place the techniques used to carry them out into 12 different categories. We find that the number of published measurements per year in all 12 cases except for the dark energy equation of state parameter  $w_0$  peaked between 1995 and 2004. Of the individual techniques, only BAO measurements were still rising in popularity at the end of the studied time period. The fractional error associated with most measurements has been declining relatively slowly, with several parameters, such as the amplitude of mass fluctuations  $\sigma_8$  and the Hubble constant  $H_0$  remaining close to the 10% precision level for a 10–15 year period. The accuracy of recent parameter measurements is generally what would be expected given the quoted error bars, although before the year 2000, the accuracy was significantly worse, consistent with an average underestimate of the error bars by a factor of  $\sim 2$ . When used as complement to traditional forecasting techniques, our results suggest that future measurements of parameters such as  $fNL$ , and  $w_a$  will have been informed by the gradual improvement in understanding and treatment of systematic errors and are likely to be accurate. However, care must be taken to avoid the effects of confirmation bias, which may be affecting recent measurements of dark energy parameters. For example, of the 28 measurements of  $\Omega_{\Lambda}$  in our sample published since 2003, only 2 are more than 1  $\sigma$  from the WMAP results. Wider use of blind analyses in cosmology could help to avoid this.



# The Pantheon compilation

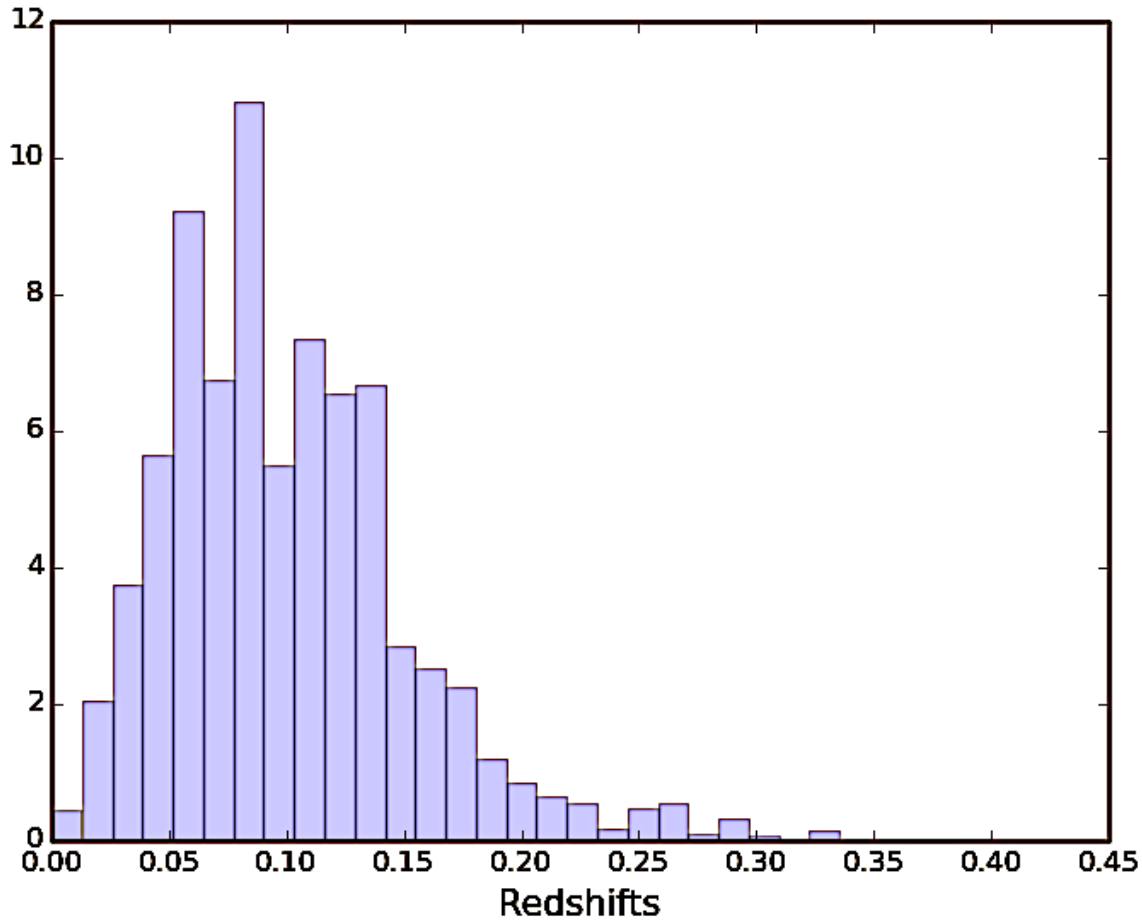
Scolnic et al. *Astrophys.J.* 859 (2018) no.2, 101



JLA + additional SN1a from Pan Starrs and HST  
1048 SN1a, redshifts corrected for peculiar velocities using the 2M++  
flow field  
890 are in the hemisphere opposite the 2M++ bulk flow

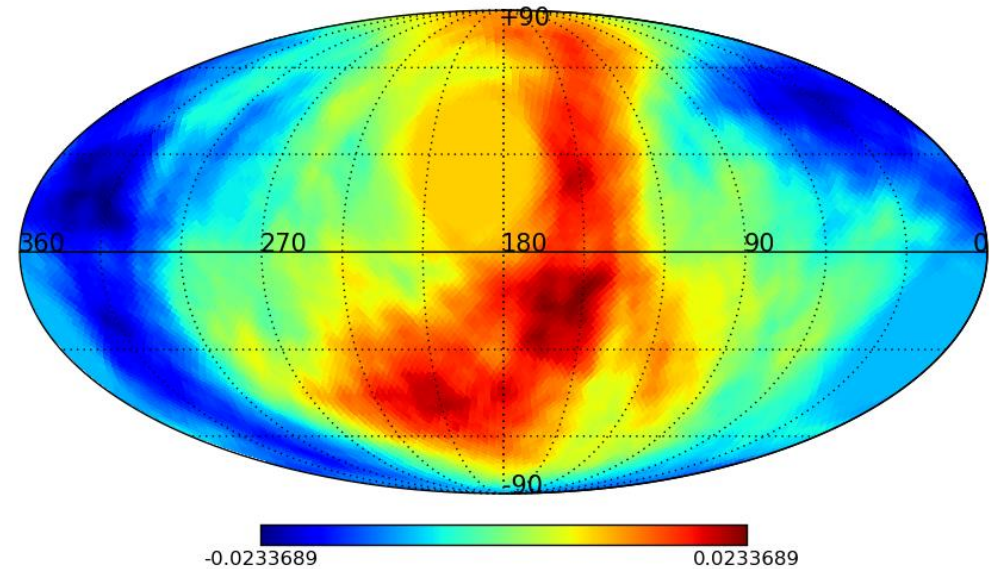
However, we use only JLA!

# Redshift distribution of the removed sources



$d = 0.0124 > 1200$  km/s if fully kinematic  
 $172.6^\circ$  RA,  $-6.6^\circ$  Dec ( $\sim 4.5^\circ$  from CMB)

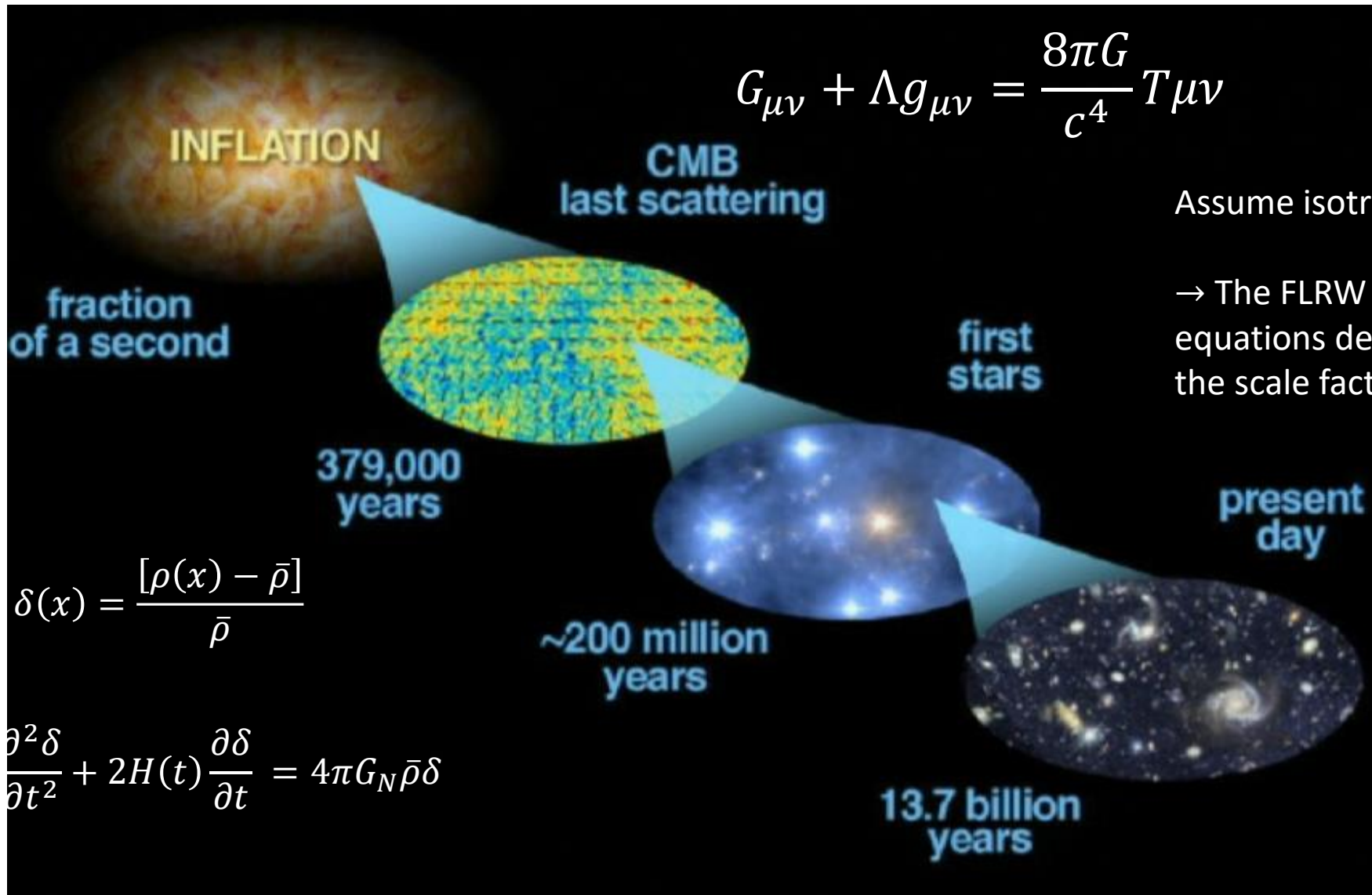
Total dipole is at least  $4.2\sigma$  statistically significant.



By cross correlating with Galaxy and Mass Assembly

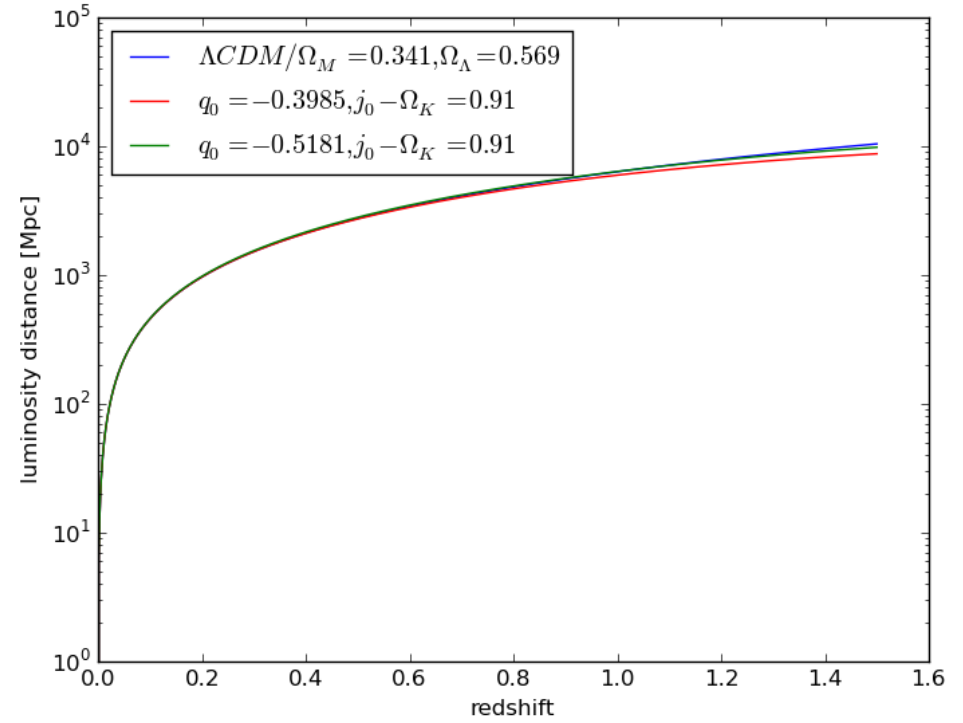
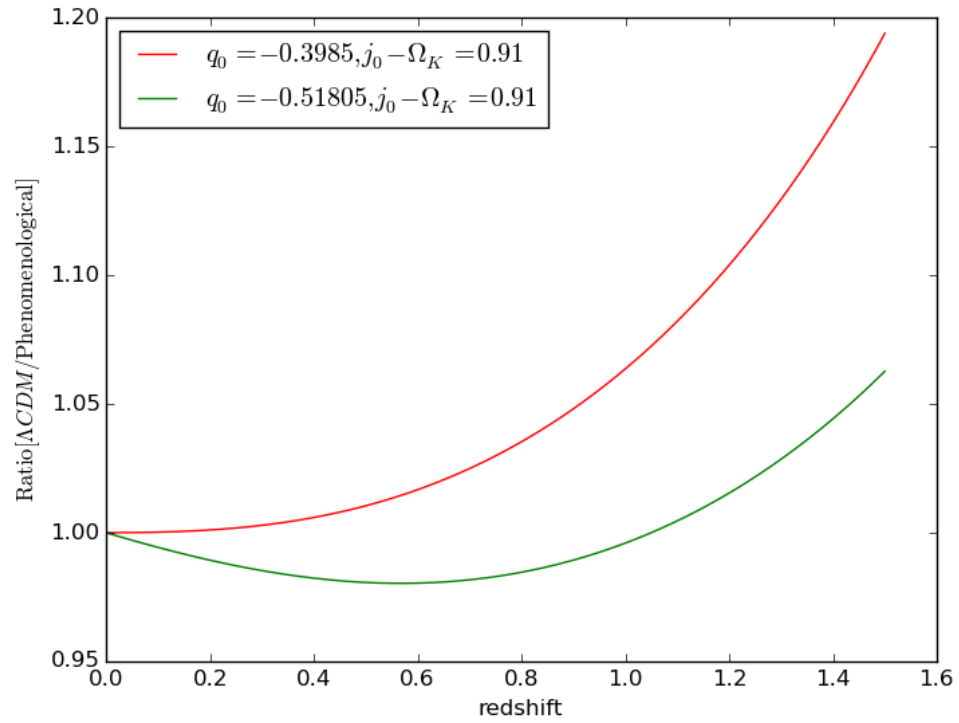


$$G_{\mu\nu} + \Lambda g_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$



$$\delta(x) = \frac{[\rho(x) - \bar{\rho}]}{\bar{\rho}}$$

$$\frac{\partial^2 \delta}{\partial t^2} + 2H(t) \frac{\partial \delta}{\partial t} = 4\pi G_N \bar{\rho} \delta$$



# Residual clustering dipole

- For a Copernican observer:

$$\langle D_{cls} \rangle = \sqrt{\frac{9}{4\pi} C_1}$$

$$C_l = b^2 \frac{2}{\pi} \int_0^\infty f_l(k)^2 P(k) k^2 dk$$

$$f_l(k) = \int_0^\infty j_l(kr) f(r) dr$$

$$f(r) = \frac{H(z)}{H_0 r_0} \frac{dN}{dz}$$

Using Planck 2015 cosmological parameters and astropy, using the the redshift distribution as  $dN/dz$

$$\langle D_{cls} \rangle < 0.0018$$

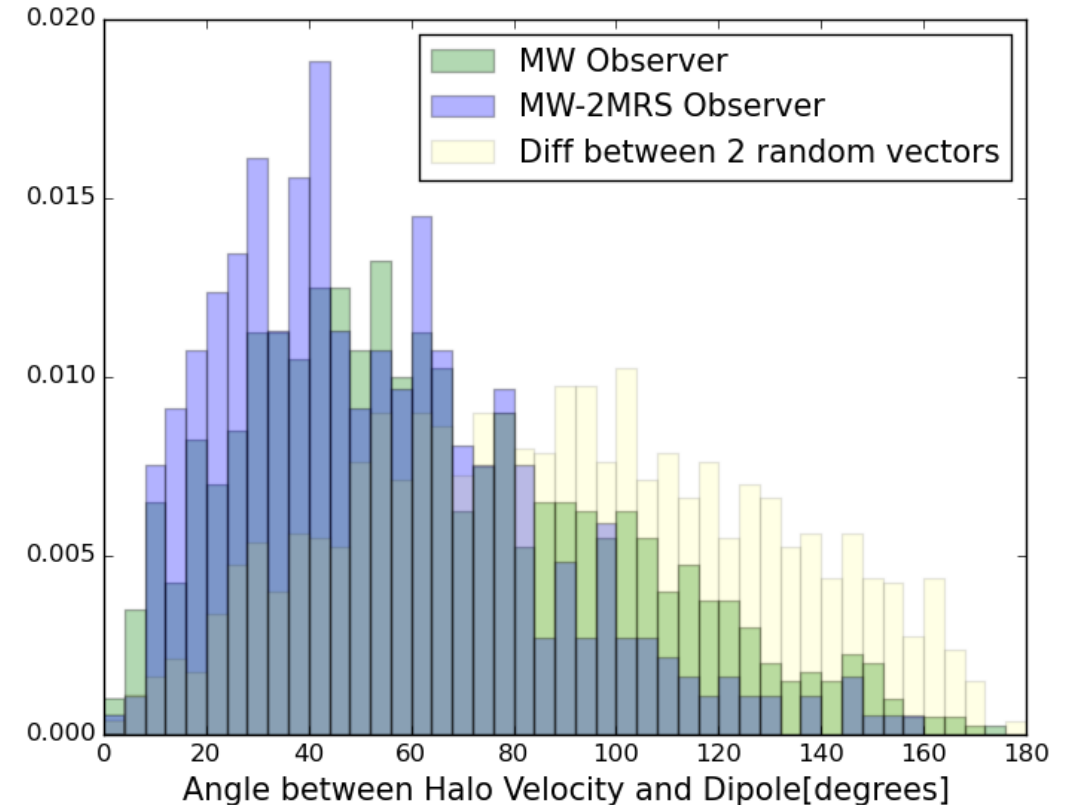
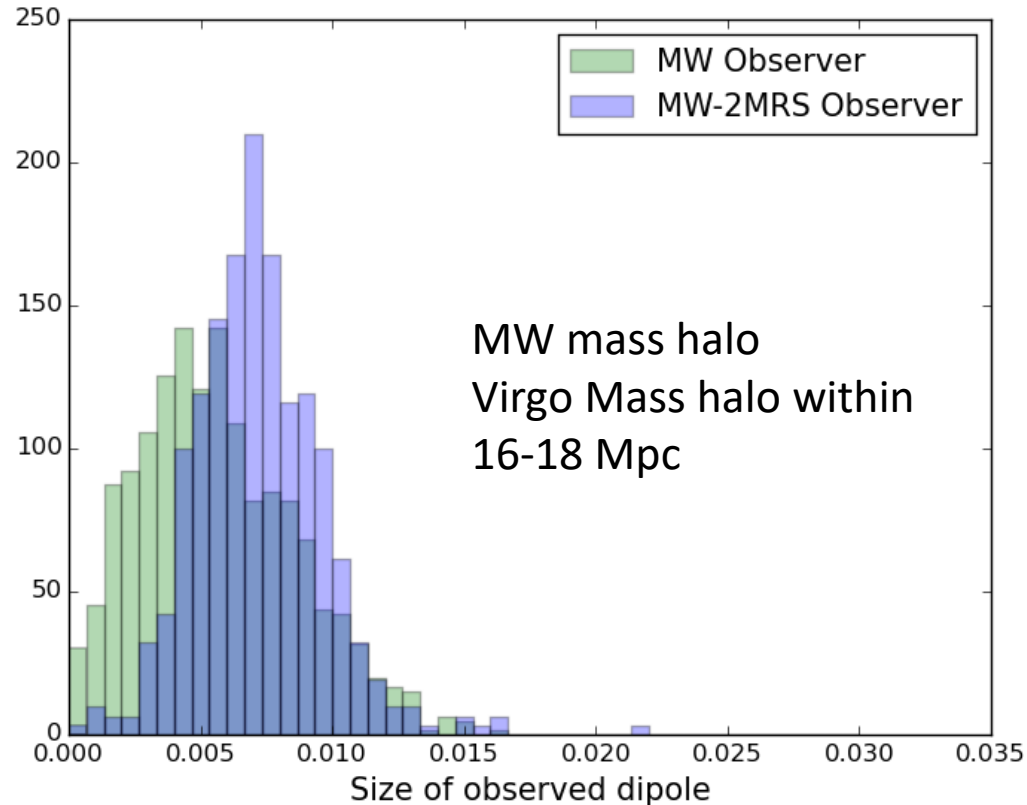
In the final sample

$$D_{kin} = 0.0106$$

Velocity of  $\sim 3000$  km/s

# Dark Sky N Body Simulations

First trillion particle simulation of the  $\Lambda$ CDM universe.



Only  $\sim <1\%$  of halos with MW-like mass and velocity are inside bulk flows  $> 240$  km/s on scales exceeding 260 Mpc

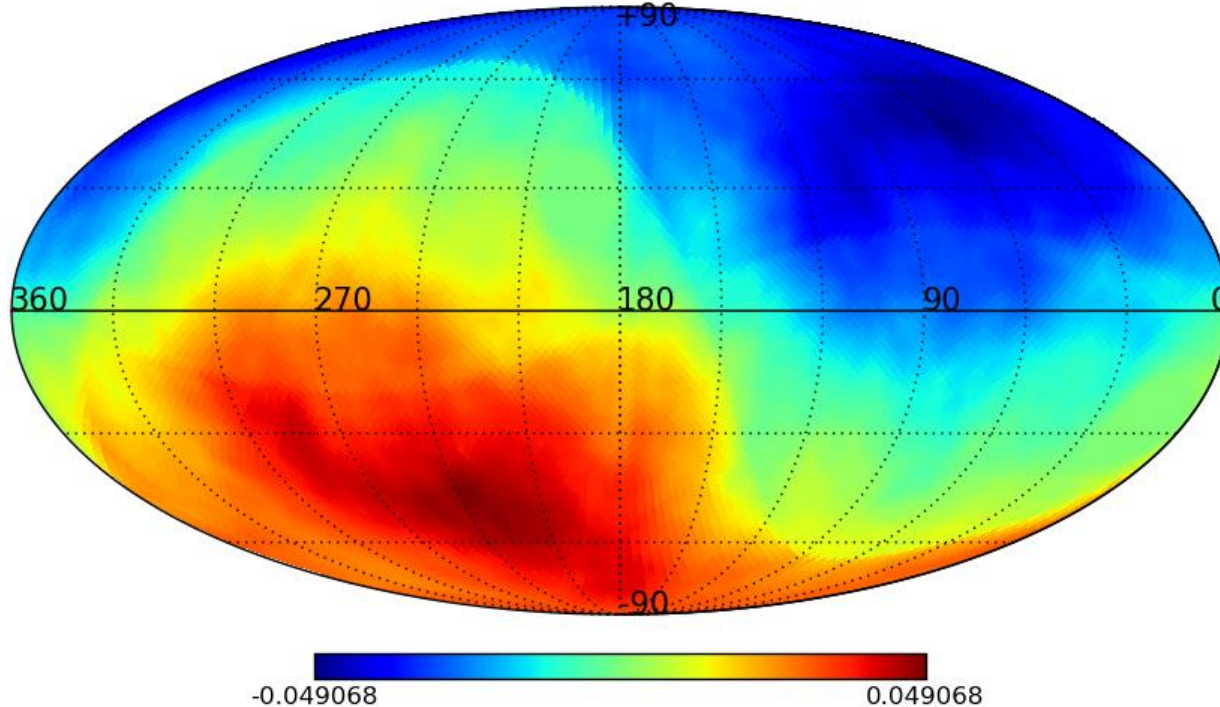
$$\langle D_{cls} \rangle = 0.0076 \pm 0.0022$$

$$\langle D_{kin} \rangle = 0.0048 \pm 0.0024$$

# Getting rid of the stars

following from MNRAS448,1305–1313 (2015)

- Magnitude cuts in different bands, Galactic plane cut at +/-15 degrees
  - Sample of 2.46 million Galaxies, 76% complete, with 1.8% star contamination



Cross correlate with deep surveys over a very narrow sky (SDSS, GAMA) to determine how many are stars and how many are Galaxies

The maximum is in the direction (AllWISE)  
237.4° RA, -46.6 ° Dec  
331.9° l 6.02° b

110 degrees from the CMB direction

Dipole magnitude  $\sim 0.049$

Fully kinematic interpretation  $\sim 6000$  km/s

in agreement with MNRAS 445 (2014) L60-L64

# How approximate? Cosmological Backreaction

Is there proof that backreaction of inhomogeneities is irrelevant in cosmology?

T Buchert<sup>1</sup>, M Carfora<sup>2</sup>, G F R Ellis<sup>3</sup>, E W Kolb<sup>4</sup>, M A H MacCallum<sup>5</sup>, J J Ostrowski<sup>6,1,†</sup>, S Räsänen<sup>7</sup>, B F Roukema<sup>6,1,†</sup>, L Andersson<sup>8</sup>, A A Coley<sup>9</sup>, and D L Wiltshire<sup>10</sup>

<sup>1</sup>Université de Lyon, Observatoire de Lyon, Centre de Recherche Astrophysique de Lyon, CNRS UMR 5574: Université Lyon 1 and École Normale Supérieure de Lyon, 9 avenue Charles André, F-69230 Saint-Genis-Laval, France

<sup>2</sup>Dipartimento di Fisica, Università degli Studi di Pavia, via A. Bassi 6, I-27100 Pavia, Italy, and Istituto Nazionale di Fisica Nucleare, Sezione di Pavia, via A. Bassi

Exact but closer to reality than FLRW -> Swiss Cheese Universes.

Underdensities always expand a little faster than overdensities.

They come to dominate the volume

Thus any inhomogeneity should lead to faster expansion.

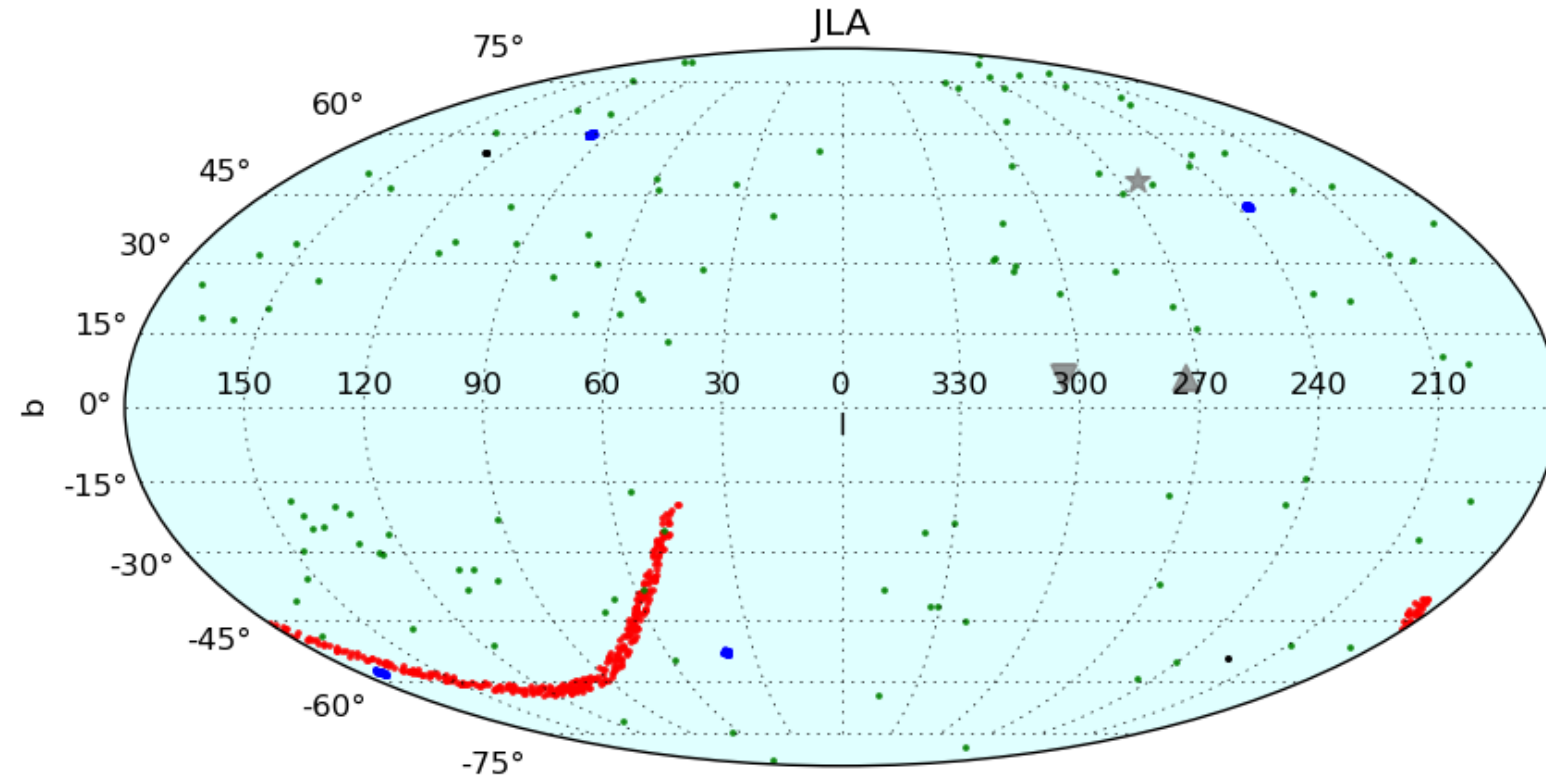
Marra, Kolb, Matarrese 2007 , Rasanen 2012, Rasanen 2015

Can explain most of of observed dark energy

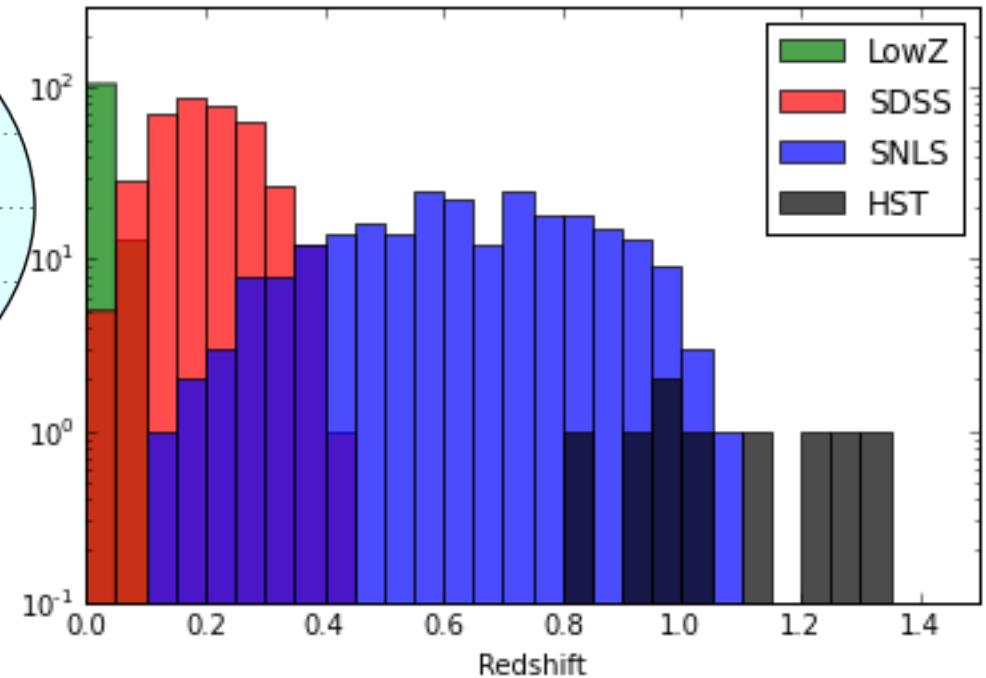
Backreaction even within perturbative gravity : Adamek, Class. Quantum Grav. 36, 014001 (2019)

15 Oct 2015

# 2014 : The Joint Lightcurve Analysis ( JLA ) Sample



Betoule et. al. *Astron.Astrophys.* 568 (2014) A22



The SDSSII/SNLSIII Joint Lightcurve Analysis (JLA) catalogue of SN1a  
 740 SN1a , 551 of which are in the hemisphere opp to the CMB motion  
 Redshifts corrected using SMAC, which has a bulk flow (gray triangle)  
 631 are in the opp hemisphere to SMAC BF

SNe down to  $z=0.01$  reintroduced  
 CMB frame observables:

# Spectral Adaptive Lightcurve Template

(For making 'stretch' and 'colour' corrections to the observed lightcurves)

$$\mu_B = m_B^* - M + \alpha X_1 - \beta C$$

B-band

SALT 2 parameters

Betoule *et al.*, A&A 568:A22,2014

Name	$z_{\text{cmb}}$	$m_B^*$	$X_1$	$C$	$M_{\text{stellar}}$
03D1ar	0.002	$23.941 \pm 0.033$	$-0.945 \pm 0.209$	$0.266 \pm 0.035$	$10.1 \pm 0.5$
03D1au	0.503	$23.002 \pm 0.088$	$1.273 \pm 0.150$	$-0.012 \pm 0.030$	$9.5 \pm 0.1$
03D1aw	0.581	$23.574 \pm 0.090$	$0.974 \pm 0.274$	$-0.025 \pm 0.037$	$9.2 \pm 0.1$
03D1ax	0.495	$22.960 \pm 0.088$	$-0.729 \pm 0.102$	$-0.100 \pm 0.030$	$11.6 \pm 0.1$
03D1bp	0.346	$22.398 \pm 0.087$	$-1.155 \pm 0.113$	$-0.041 \pm 0.027$	$10.8 \pm 0.1$
03D1co	0.678	$24.078 \pm 0.098$	$0.619 \pm 0.404$	$-0.039 \pm 0.067$	$8.6 \pm 0.3$
03D1dt	0.611	$23.285 \pm 0.093$	$-1.162 \pm 1.641$	$-0.095 \pm 0.050$	$9.7 \pm 0.1$
03D1ew	0.866	$24.354 \pm 0.106$	$0.376 \pm 0.348$	$-0.063 \pm 0.068$	$8.5 \pm 0.8$
03D1fc	0.331	$21.861 \pm 0.086$	$0.650 \pm 0.119$	$-0.018 \pm 0.024$	$10.4 \pm 0.0$
03D1fq	0.799	$24.510 \pm 0.102$	$-1.057 \pm 0.407$	$-0.056 \pm 0.065$	$10.7 \pm 0.1$
03D3aw	0.450	$22.667 \pm 0.092$	$0.810 \pm 0.232$	$-0.086 \pm 0.038$	$10.7 \pm 0.0$
03D3ay	0.371	$22.273 \pm 0.091$	$0.570 \pm 0.198$	$-0.054 \pm 0.033$	$10.2 \pm 0.1$
03D3ba	0.292	$21.961 \pm 0.093$	$0.761 \pm 0.173$	$0.116 \pm 0.035$	$10.2 \pm 0.1$
03D3bl	0.356	$22.927 \pm 0.087$	$0.056 \pm 0.193$	$0.205 \pm 0.030$	$10.8 \pm 0.1$

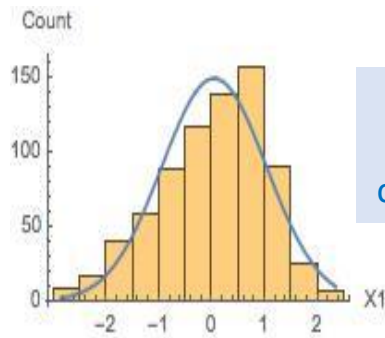
There may well be other variables that the magnitude correlates with ...



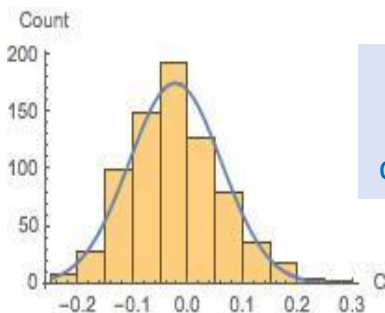
$\mathcal{L}$  = probability density(data|model)

$$\begin{aligned} \mathcal{L} &= p[(\hat{m}_B^*, \hat{x}_1, \hat{c}) | \theta] \\ &= \int p[(\hat{m}_B^*, \hat{x}_1, \hat{c}) | (M, x_1, c), \theta_{\text{cosmo}}] \\ &\quad \times p[(M, x_1, c) | \theta_{\text{SN}}] dM dx_1 dc \end{aligned}$$

Well-approximated as Gaussian



JLA data  
'Stretch'  
corrections



JLA data  
'Colour'  
corrections

$$p[(M, x_1, c) | \theta] = p(M | \theta) p(x_1 | \theta) p(c | \theta),$$

$$p(M | \theta) = \frac{1}{\sqrt{2\pi\sigma_M^2}} \exp\left(-\left[\frac{M - M_0}{\sigma_{M0}}\right]^2 / 2\right)$$

$$p(x_1 | \theta) = \frac{1}{\sqrt{2\pi\sigma_{x0}^2}} \exp\left(-\left[\frac{x_1 - x_{10}}{\sigma_{x0}}\right]^2 / 2\right)$$

$$p(c | \theta) = \frac{1}{\sqrt{2\pi\sigma_{c0}^2}} \exp\left(-\left[\frac{c - c_0}{\sigma_{c0}}\right]^2 / 2\right)$$

# Likelihood

$$p(Y|\theta) = \frac{1}{\sqrt{|2\pi\Sigma_l|}} \exp \left[ -\frac{1}{2}(Y - Y_0)\Sigma_l^{-1}(Y - Y_0)^T \right]$$

$$p(\hat{X}|X, \theta) = \frac{1}{\sqrt{|2\pi\Sigma_d|}} \exp \left[ -\frac{1}{2}(\hat{X} - X)\Sigma_d^{-1}(\hat{X} - X)^T \right]$$

$$\mathcal{L} = \frac{1}{\sqrt{|2\pi(\Sigma_d + A^T\Sigma_l A)|}} \times \exp \left( -\frac{1}{2}(\hat{Z} - Y_0 A)(\Sigma_d + A^T\Sigma_l A)^{-1}(\hat{Z} - Y_0 A)^T \right)$$

cosmology

intrinsic distributions

SALT2

Simultaneously fit for

- $\Omega_M$
- $\Omega_\Lambda$
- $q_d$
- $S$
- $\alpha$
- $x_{1,0}$
- $\sigma_{x_{1,0}}$
- $\beta$
- $c_0$
- $\sigma_{c_0}$
- $M_0$
- $\sigma_{M_0}$

## Confidence regions

$$p_{\text{cov}} = \int_0^{-2 \log \mathcal{L} / \mathcal{L}_{\text{max}}} \chi^2(x; \nu) dx$$

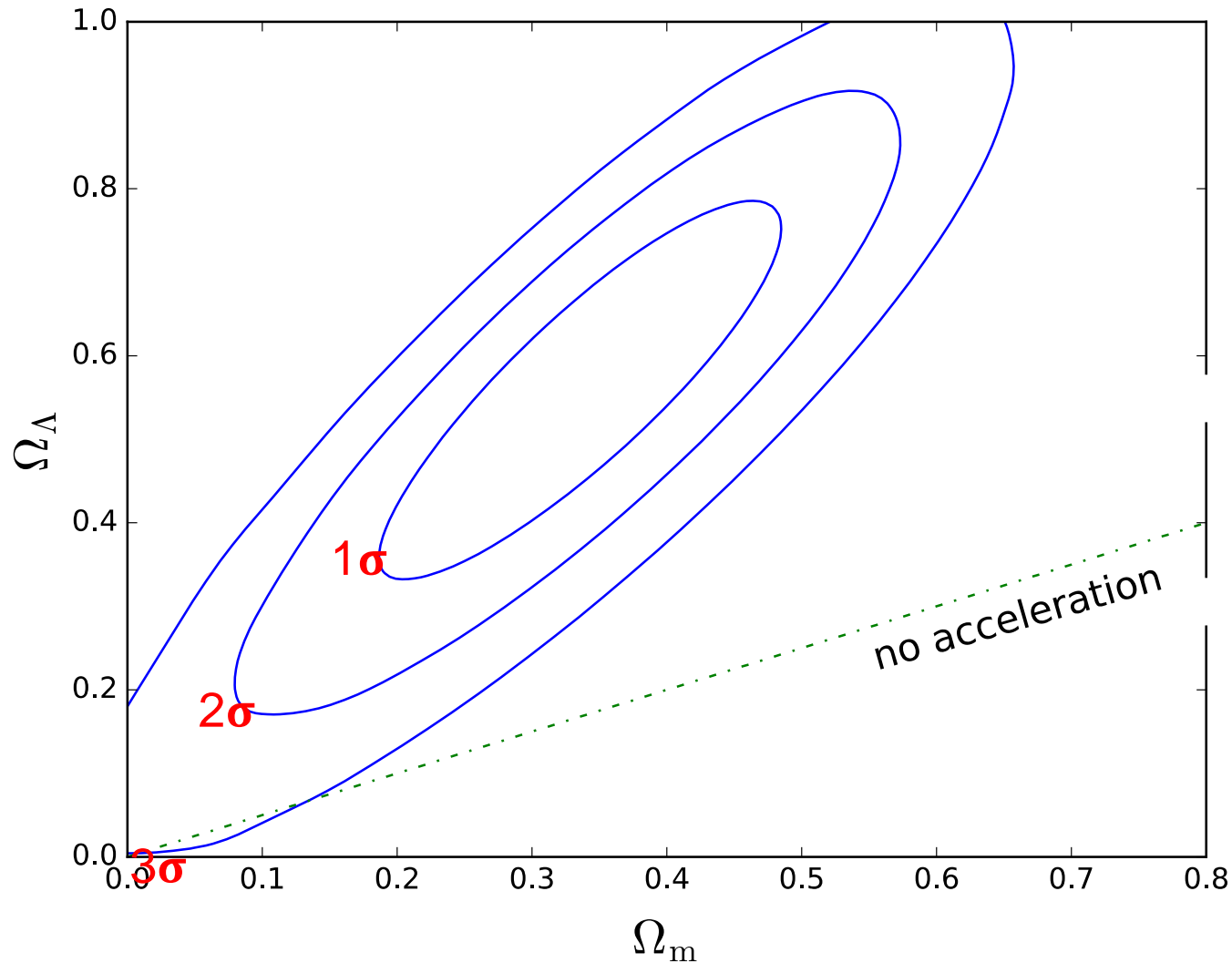
$$\mathcal{L}_p(\theta) = \max_{\phi} \mathcal{L}(\theta, \phi)$$

1,2,3-sigma

solve for Likelihood value

# Data consistent with uniform expansion @<3 $\sigma$ !

profile likelihood



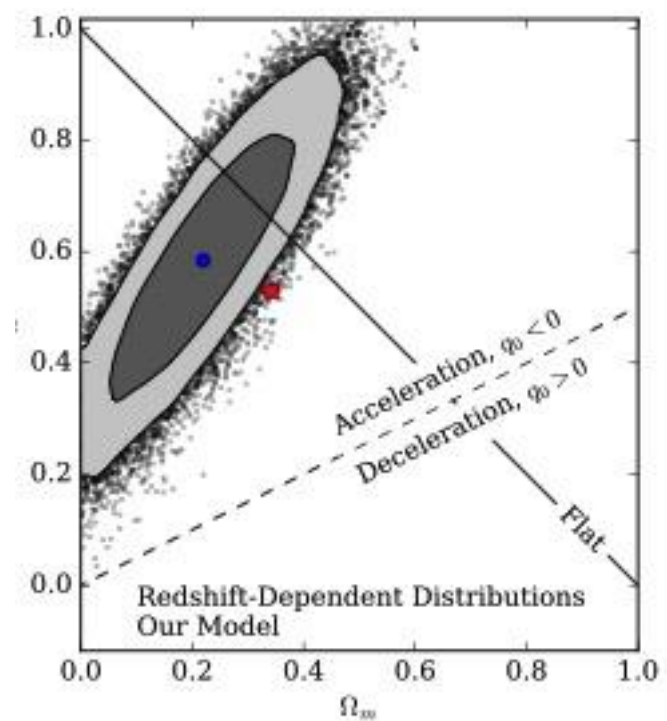
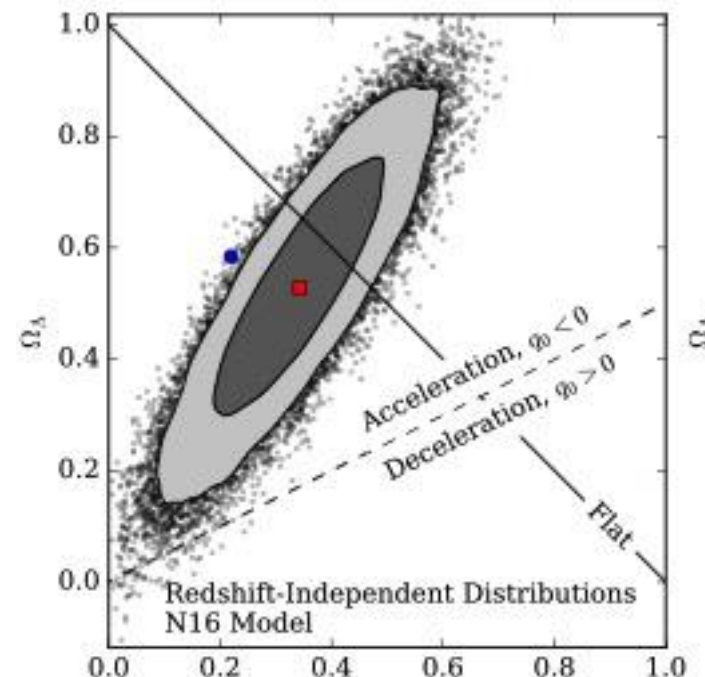
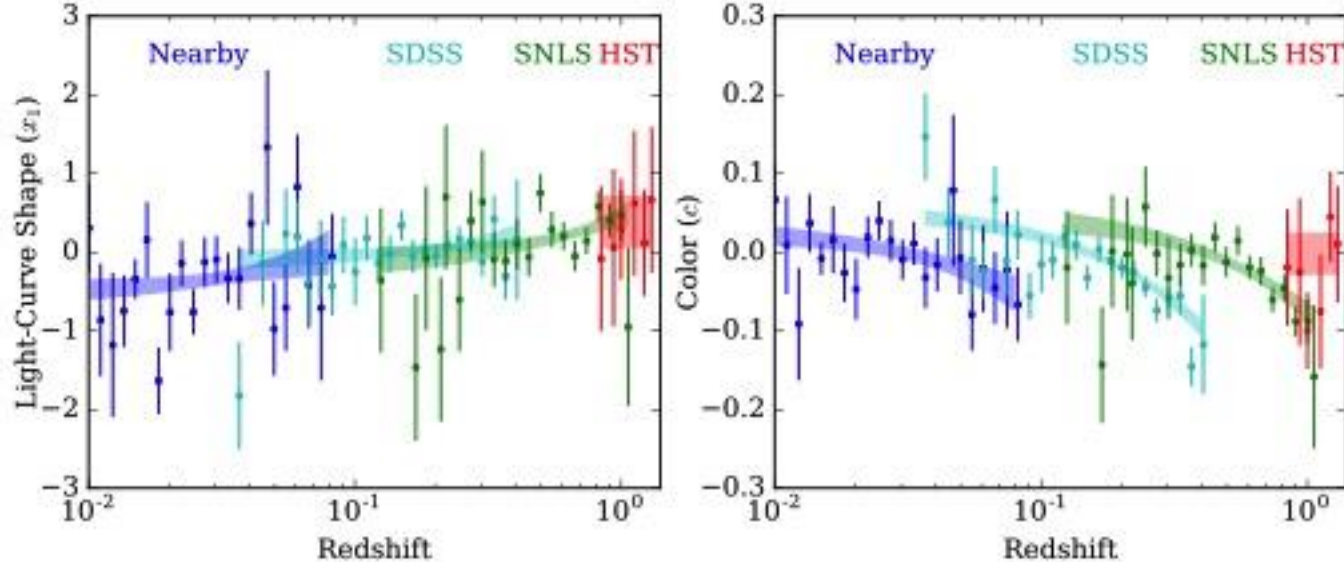
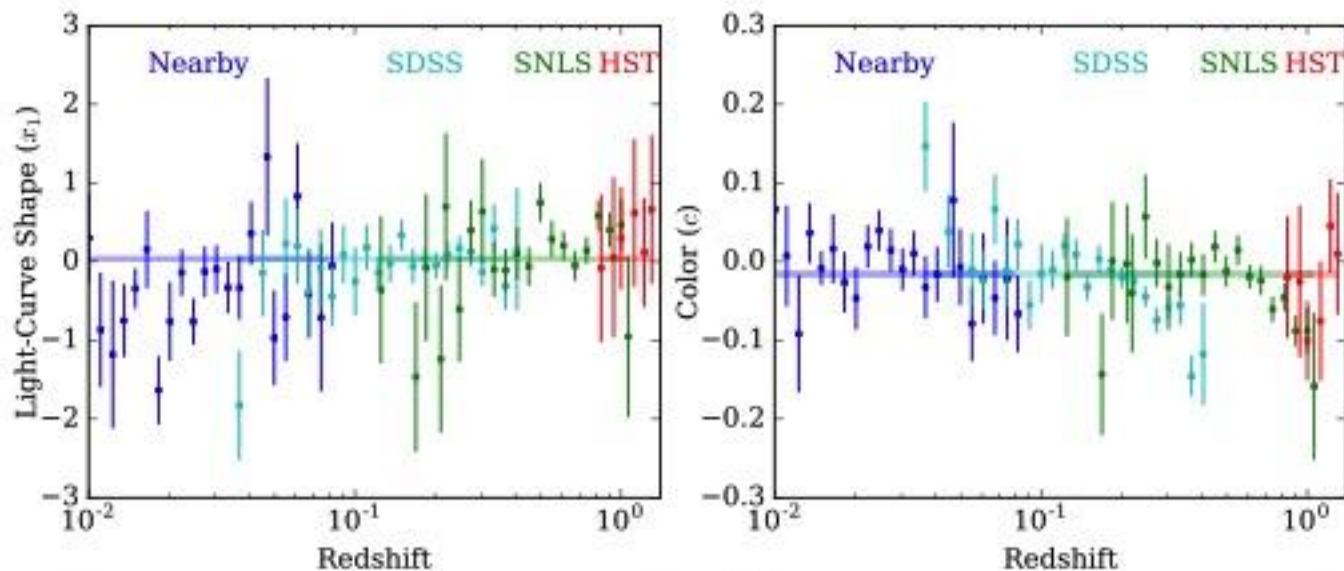
MLE, best fit

$\Omega_M$	0.341
$\Omega_\Lambda$	0.569
$\alpha$	0.134
$x_0$	0.038
$\sigma_{x_0}^2$	0.931
$\beta$	3.058
$c_0$	-0.016
$\sigma_{c_0}^2$	0.071
$M_0$	-19.05
$\sigma_{M_0}^2$	0.108

Nielsen, Guffanti  
& Sarkar.,  
Sci.Rep.6:35596,2  
016

Rubin & Hayden 2016  
Added 12 parameters to this  
10 parameter fit, to claim  
significance > 4sigma

# Rubin & Hayden 2016



# Peculiar velocity impact on SN1a magnitude

$$1 + z = (1 + \bar{z})(1 + z_{pec}^{hel})(1 + z_{pec}^{SN})$$

$$d_L(z) = \bar{d}_L(\bar{z}) (1 + z_{pec}^{hel})(1 + z_{pec}^{SN})^2$$

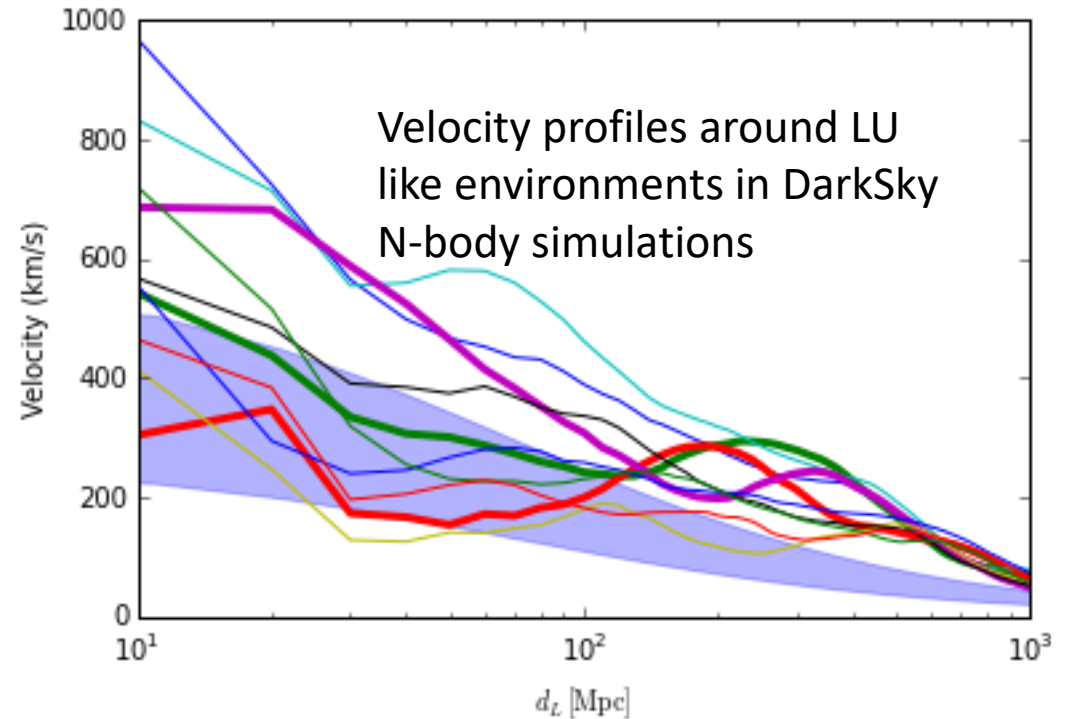
Davis et. al. *Astrophys.J.* 741 (2011) 67

JLA (and Pantheon) redshifts and magnitudes have been corrected to account for the local bulk flow.

#name	zcmb	zhel	dz	mb	dmb	x1	dx1	color	dcolor
03D1au	0.503084	0.504300	0	23.001698	0.088031				
03D1aw	0.580724	0.582000	0	23.573937	0.090132				
03D1ax	0.494795	0.496000	0	22.960139	0.088110				
03D1bp	0.345928	0.347000	0	22.398137	0.087263				
03D1co	0.677662	0.679000	0	24.078115	0.098356				
03D1dt	0.610712	0.612000	0	23.285241	0.092877				
03D1ew	0.866494	0.868000	0	24.353678	0.106037				
03D1fc	0.330932	0.332000	0	21.861412	0.086437				
03D1fn	0.798566	0.800000	0	24.510389	0.101777				

$z_{hel} \rightarrow$  measured

$z_{cmb} \rightarrow$  inferred using a flow model



SN1a at  $z > 0.06$  are assumed (arbitrarily) to be in the CMB rest frame. (only uncorrelated 150 km/s in error budget)  
 Wrong 'correction' to SDSS2308 in JLA. Many such mistakes in Pantheon (eg : SN2246).

Consequently, we use only  $z_{hel}$  and subtract out the corrections to  $m_B$

# Luminosity distance in the FLRW Universe

Exact

$$d_L = (1+z) \frac{d_H}{\sqrt{\Omega_k}} \sinh \left( \sqrt{\Omega_k} \int_0^z \frac{H_0 dz'}{H(z')} \right),$$

$$d_H = c/H_0, \quad H_0 \equiv 100h \text{ km s}^{-1} \text{ Mpc}^{-1},$$

$$H = H_0 \sqrt{\Omega_m(1+z)^3 + \Omega_k(1+z)^2 + \Omega_\Lambda},$$

Kinematic

- $H = \frac{\dot{a}}{a}$
- $q \stackrel{\text{def}}{=} -\frac{\ddot{a}a}{\dot{a}^2}$  (defined with a minus to be positive for a decelerating universe)

$$q = \frac{\Omega_M}{2} - \Omega_\Lambda \text{ (in } \Lambda\text{CDM)}$$

- $j = \frac{\ddot{a}}{aH^3}$  **Matt Visser 2004**

$$d_L(z) = \frac{cz}{H_0} \left\{ 1 + \frac{1}{2}[1 - q_0]z - \frac{1}{6} \left[ 1 - q_0 - 3q_0^2 + j_0 + \frac{kc^2}{H_0^2 a_0^2} \right] z^2 + O(z^3) \right\}$$

What we mean by tilt :  $q_0 \rightarrow q_m + q_d \cos(\theta_{|cmb-SN|}) e^{-z/S}$

# A study of Dipolar Signal in distant Quasars with various observables

Rahul Kothari,<sup>a</sup> Mohit Panwar,<sup>b</sup> Gurmeet Singh,<sup>b</sup> Prabhakar Tiwari,<sup>c</sup> Pankaj Jain<sup>d</sup>

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<sup>b</sup>Department of Physics, Indian Institute of Technology, Kanpur 208016, India

<sup>c</sup>National Astronomical Observatories, Chinese Academy of Science, Beijing, 100101, P.R.China

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E-mail: [quantummechanickothari@gmail.com](mailto:quantummechanickothari@gmail.com)

**Abstract.** We study the signal of anisotropy in AGNs/quasars of CatWISE2020 catalogue using different observables. It has been reported earlier that this data shows a strong signal of dipole anisotropy in the source number counts. We test this claim using two independent data analysis procedures and find our number count dipole consistent with the earlier results. In addition to number counts, we test for the anisotropy signal in two other observables — mean spectral index  $\bar{\alpha}$  and mean flux density  $\bar{B}$ . We find a dipole signal of considerable strength both in the mean spectral index and the mean flux density. The dipole in mean flux density points towards the galactic center and becomes very weak after imposing a flux cut to remove sources with flux greater than 1 mJy. This can be attributed to the presence of some bright sources. The signal in mean spectral index, however, is relatively stable as a function of both flux and galactic cuts. The dipole in this observable points roughly opposite to the galactic center and hence most likely arises due to galactic bias. Hence, the signal in both the mean spectral index and mean flux density appears to be consistent with isotropy.

# AllWISE-Galaxies

Star galaxy separation following from MNRAS448,1305–1313 (2015)

- Magnitude cuts in different bands, Galactic plane cut at +/-15 degrees
  - Sample of 2.46 million Galaxies, 76% complete, with 1.8% star contamination

Cross correlate with deep surveys over a very narrow sky (SDSS, GAMA) to determine how many are stars and how many are Galaxies

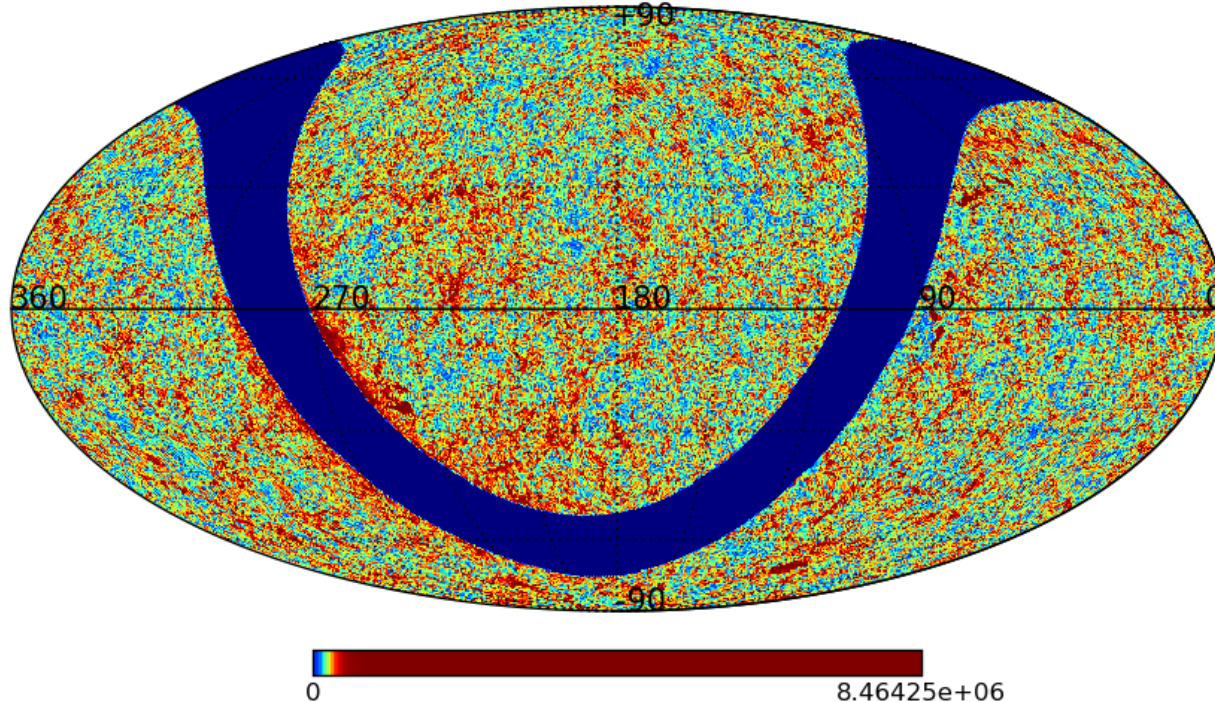
The maximum is in the direction (AllWISE)  
237.4° RA, -46.6° Dec  
331.9° l 6.02° b

110 degrees from the CMB direction

Dipole magnitude  $\sim 0.049$

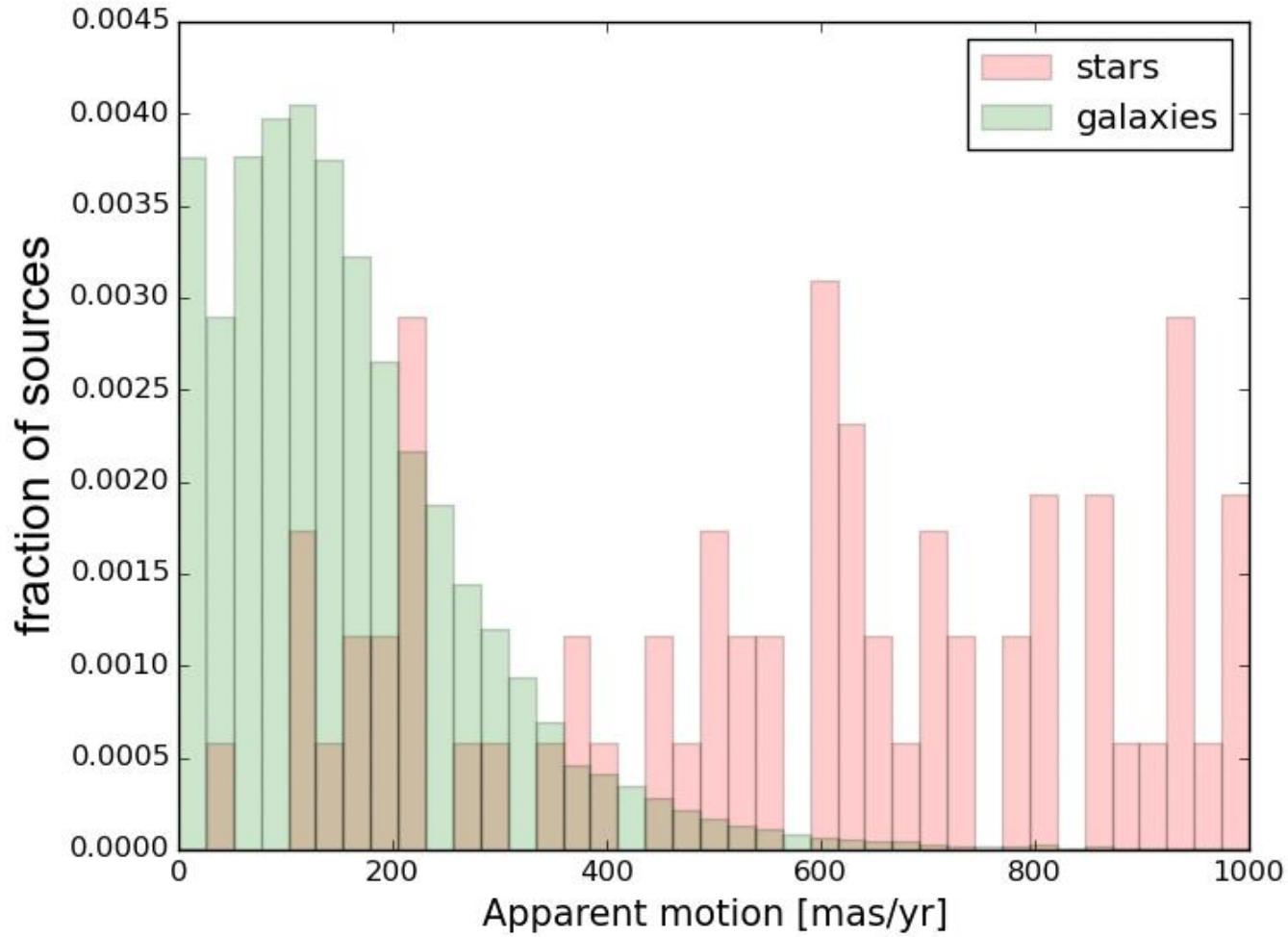
Fully kinematic interpretation  $\sim 6000$  km/s

in agreement with MNRAS 445 (2014) L60-L64





# Getting rid of the stars



Apparent motion = parallax + proper motion

Stars in the Galaxy have higher apparent motions 400 mas/yr up to many arc seconds/year

Cuts on apparent motion can bring star contamination down to 0.1%, while still keeping ~1.8 million galaxies.

182.9° RA, -55.6° DEC, 50.1° from the CMB

Dipole magnitude reduces to 0.014

Star galaxy identification by cross correlating with SDSS

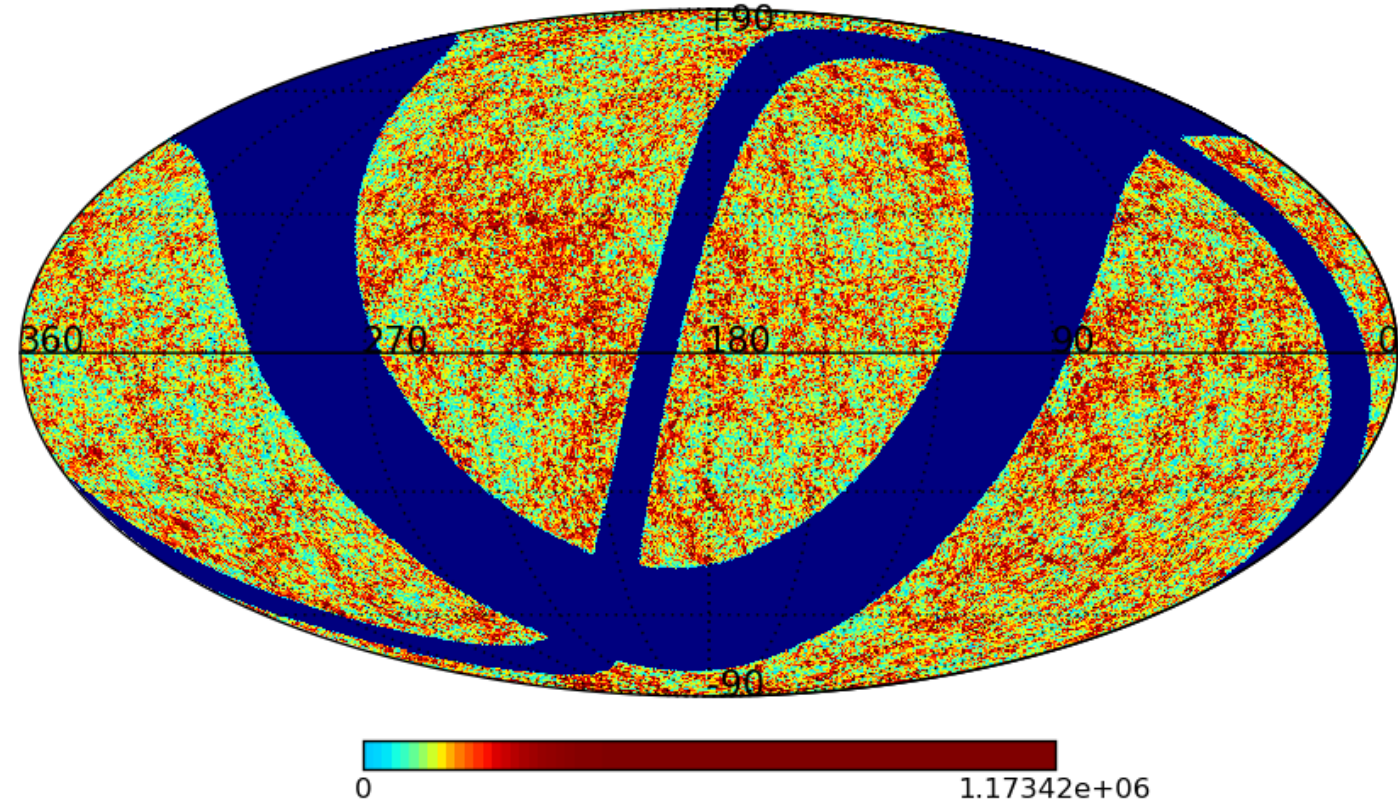
# Suppressing local anisotropies

~200 Mpc

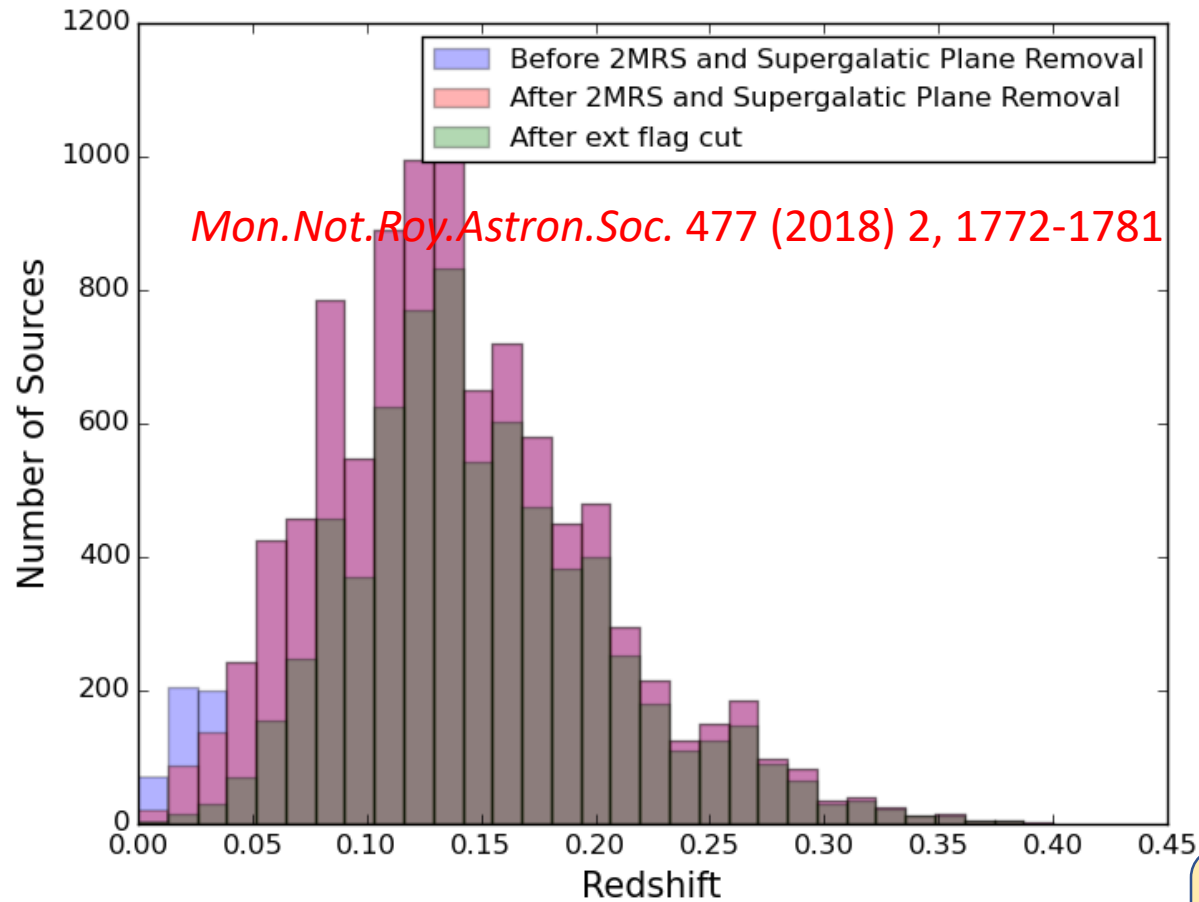
Remove extended sources and the supergalactic plane.

Further reduce  $z < 0.03$  sources by cross correlating with 2MRS and removing the correlated sources.

6.1'' PSF



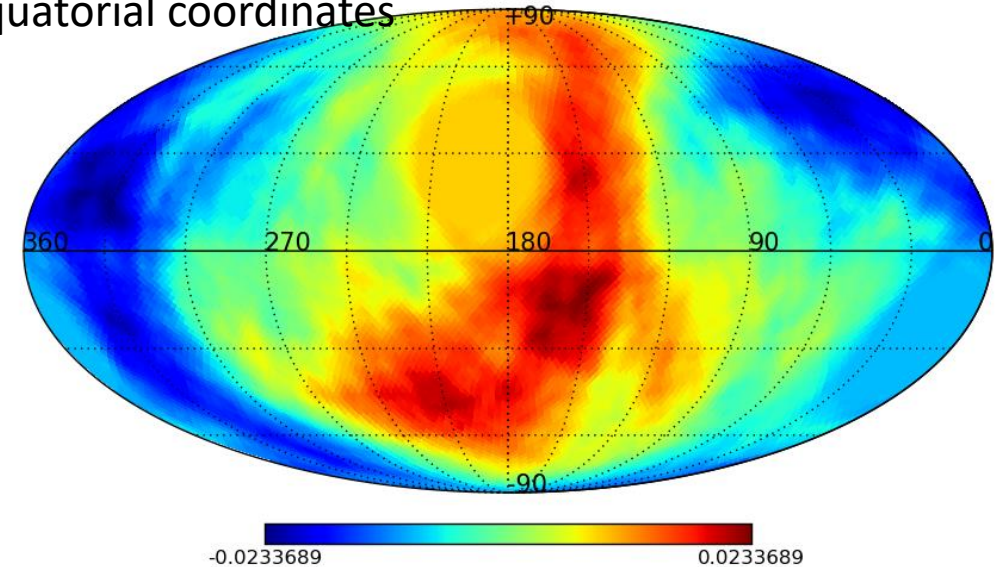
# 1192182 - AllWISE Galaxies



By cross correlating with Galaxy and Mass Assembly

$d = 0.0124 > 3600$  km/s if fully kinematic  
 $172.6^\circ$  RA,  $-6.6^\circ$  Dec ( $\sim 4.5^\circ$  from CMB dipole)  
 $4.6\sigma$  statistically significant.

Equatorial coordinates



**$V = 1260 \pm 629$  km/s within 6 degrees of CMB dipole**  
**Low redshift**

# Dipoles in a catalogue of galaxies

In an all-sky catalogue with sources of redshift distribution  $D(z)$  from directionally unbiased survey with  $N$  sources

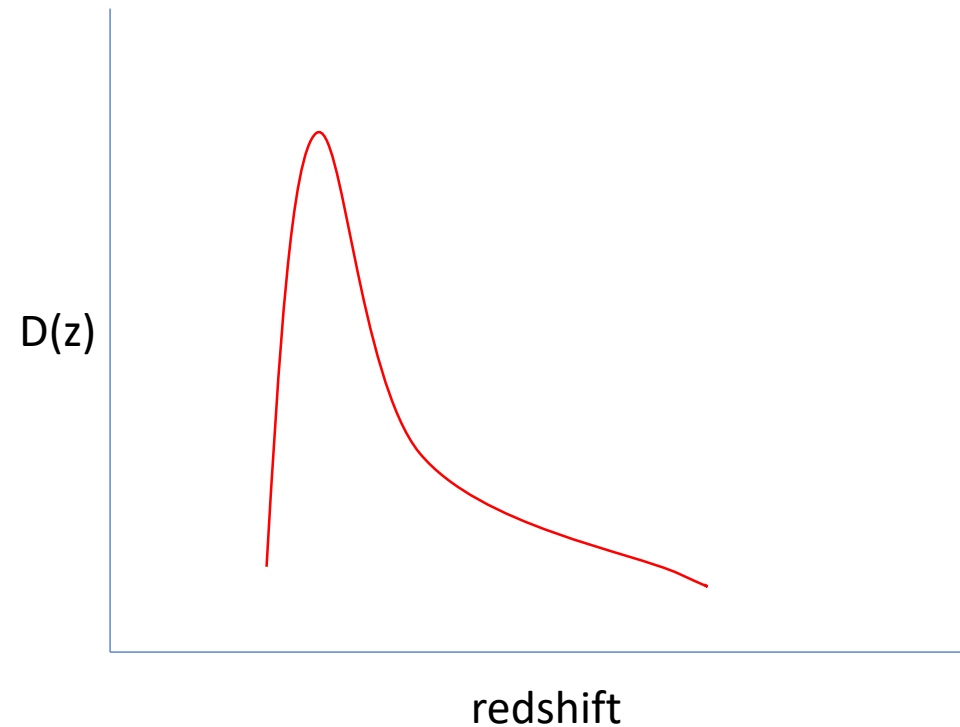
$$\vec{\delta} = \vec{\mathcal{K}} (\vec{v}_{obs}, x, \alpha) + \vec{\mathcal{R}} (N) + \vec{D}_{cls} (D(z)) + \vec{\mathcal{F}}$$

$\vec{\mathcal{K}}$  → **The Kinematic dipole**, depends on source spectrum, source flux function, observer velocity

$\vec{\mathcal{R}}$  → **The shot noise dipole**,  $\propto 1/\sqrt{N}$ , isotropic

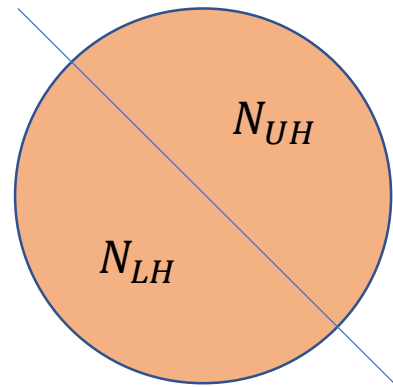
$\vec{D}_{cls}$  → **The clustering dipole**, local anisotropy due to structure

$\vec{\mathcal{F}}$  → **Foregrounds**, mainly stars and other Galactic contamination



# Estimators for the Dipole

$$\vec{D}_H = \hat{z} * \frac{N_{UH} - N_{LH}}{N_{UH} + N_{LH}}$$



Vary the direction of the hemispheres until maximum asymmetry is observed

Easy visualization

High Bias and statistical error  $2.6/\sqrt{N}$

$$\vec{D}_{3D} = \frac{1}{N} \sum_{i=1}^N \hat{r}_i$$

Add up unit vectors corresponding to directions in the sky for every source

Relatively lower bias and statistical error  $1/\sqrt{N}$

Rubart and Schwarz 2013

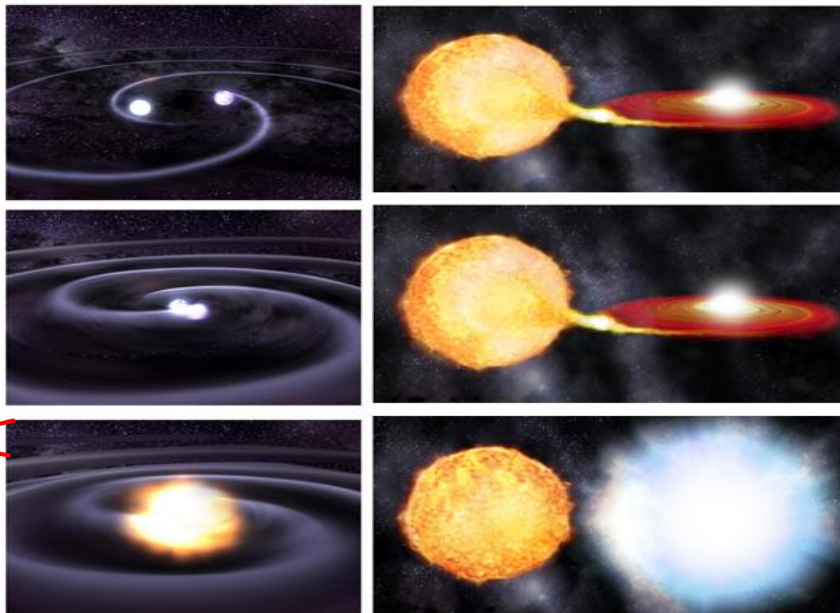
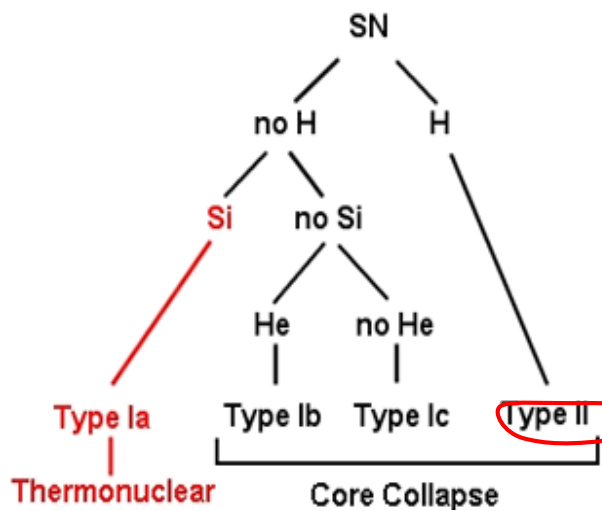
$$\frac{[n_p - \bar{n}(1 + \vec{D}_q \cdot \hat{r}_p)]^2}{\bar{n}(1 + \vec{D}_q \cdot \hat{r}_p)}$$

Minimize the above term, even less bias than the linear estimator

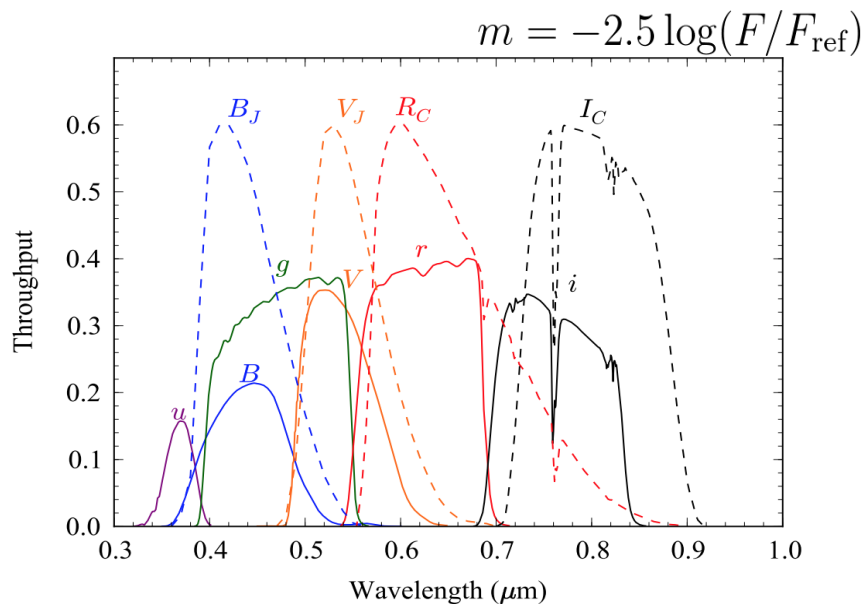
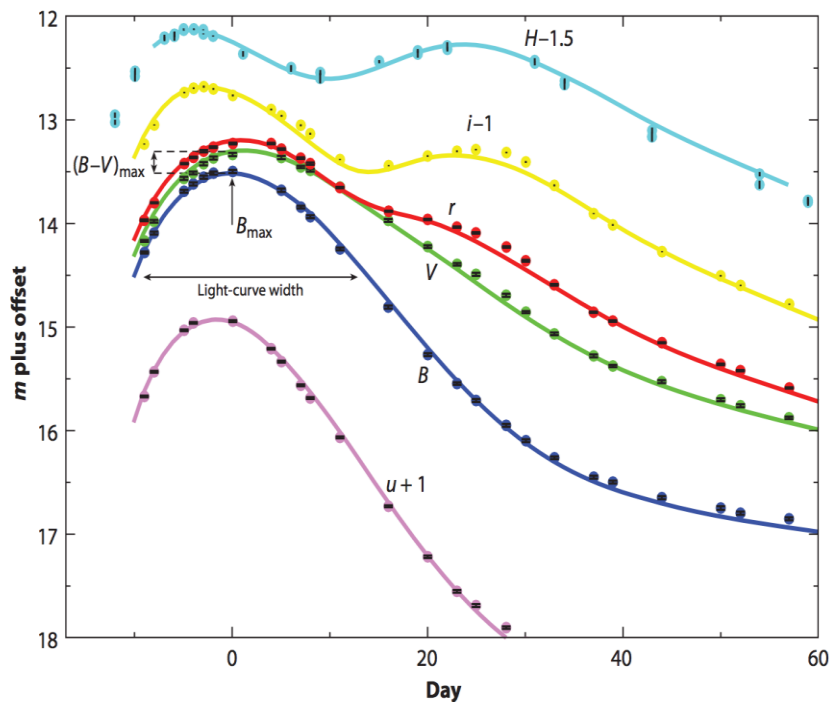
$$\vec{D}_H = \frac{\hat{z}}{N} \int_{\phi=0}^{\phi=2\pi} \int_{\theta=0}^{\theta=\pi} \sigma(\theta) \frac{|\cos\theta|}{\cos\theta} \sin\theta d\theta d\phi$$

$$\vec{D}_C = \frac{\hat{z}}{N} \int_{\phi=0}^{\phi=2\pi} \int_{\theta=0}^{\theta=\pi} \sigma(\theta) \cos\theta \sin\theta d\theta d\phi$$

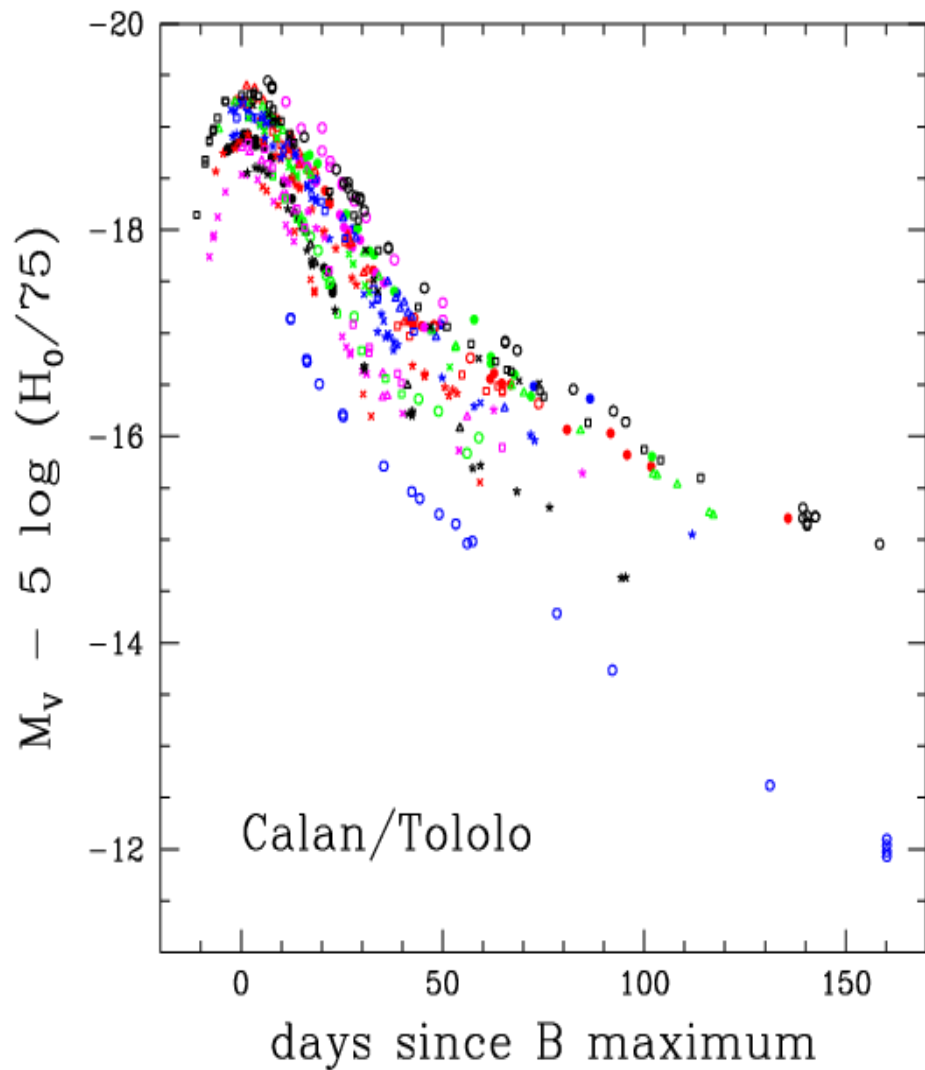
# What are Type Ia supernovae?



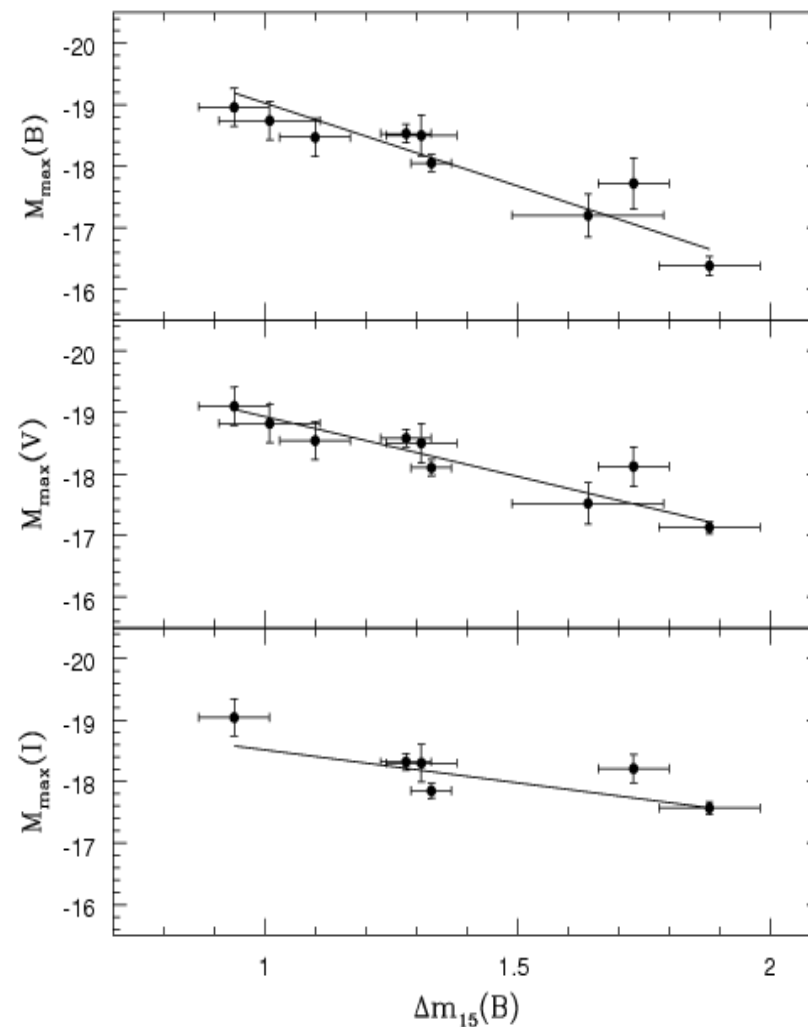
A white dwarf accreting matter from a binary companion, reignites when crossing  $\sim 1.44$  Solar Masses



# They are certainly *not* 'standard candles'



Hamuy, arXiv:311.5099

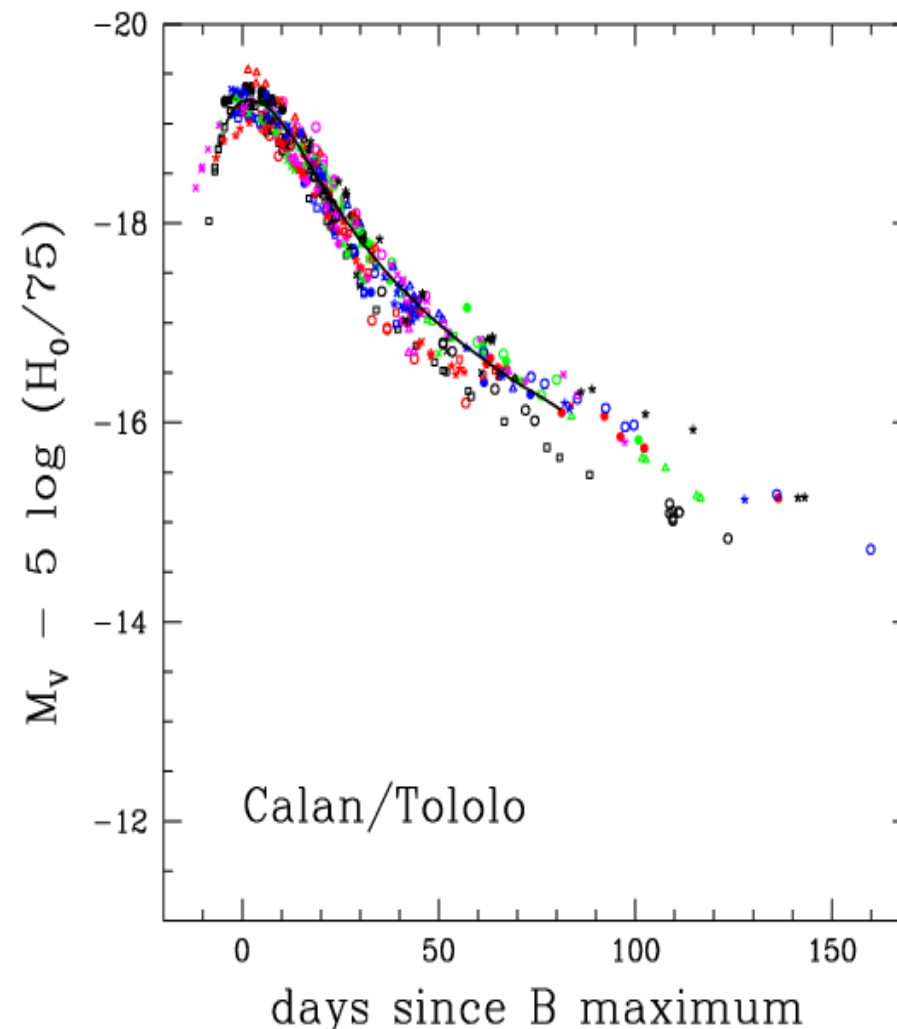
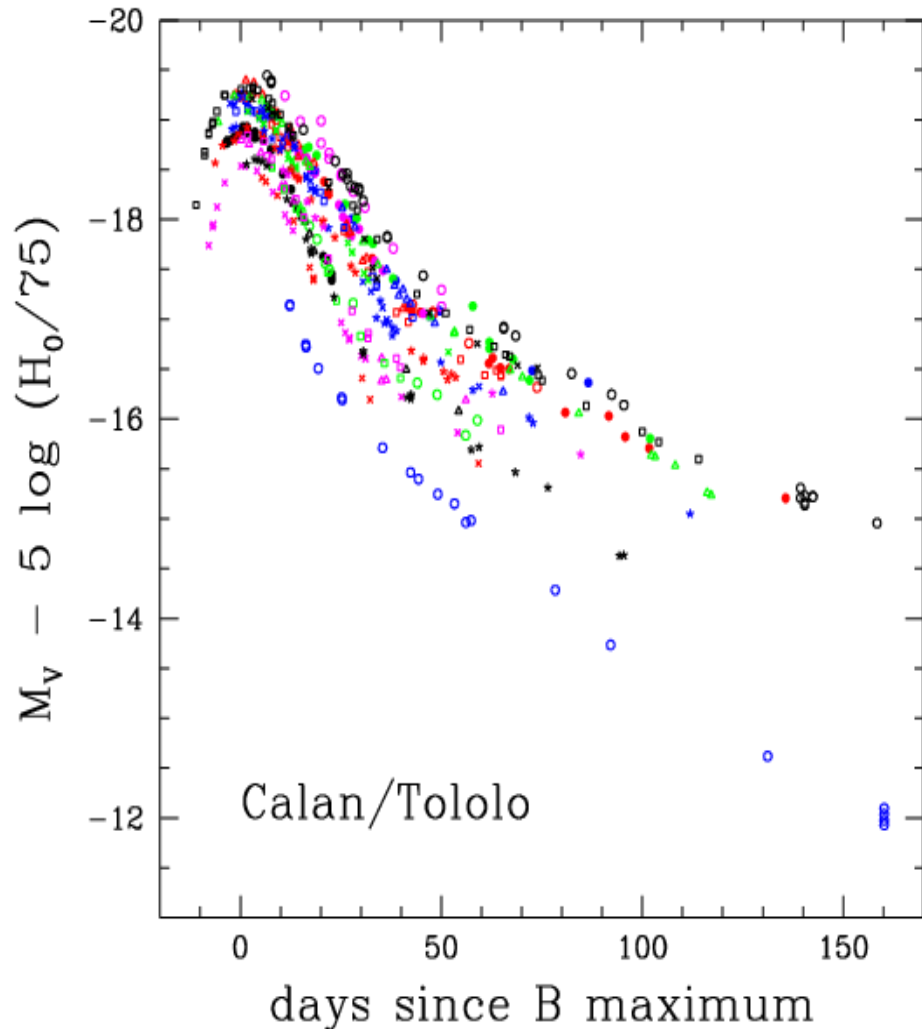


Phillips, ApJ 413:L105, 1993

But they can be 'standardised' using the observed correlation between their peak magnitude and light-curve width (NB: this is *not* understood theoretically)

# Type Ia supernovae as 'standardisable candles'

Corrected  
data



Hamuy, 1311.5099

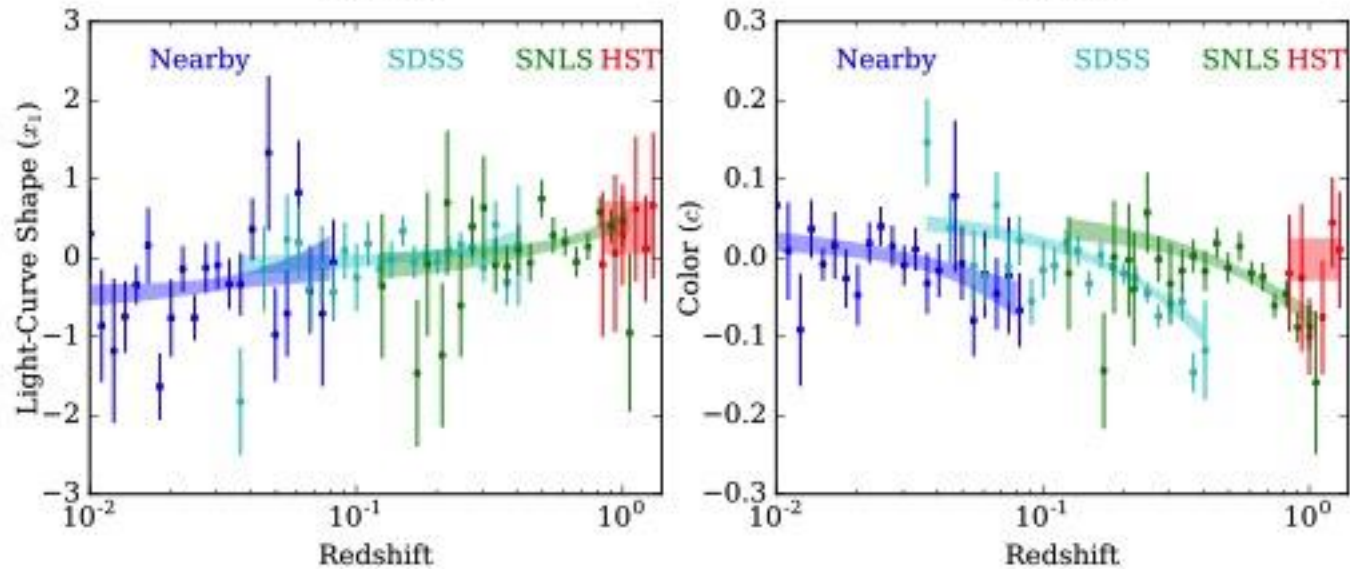
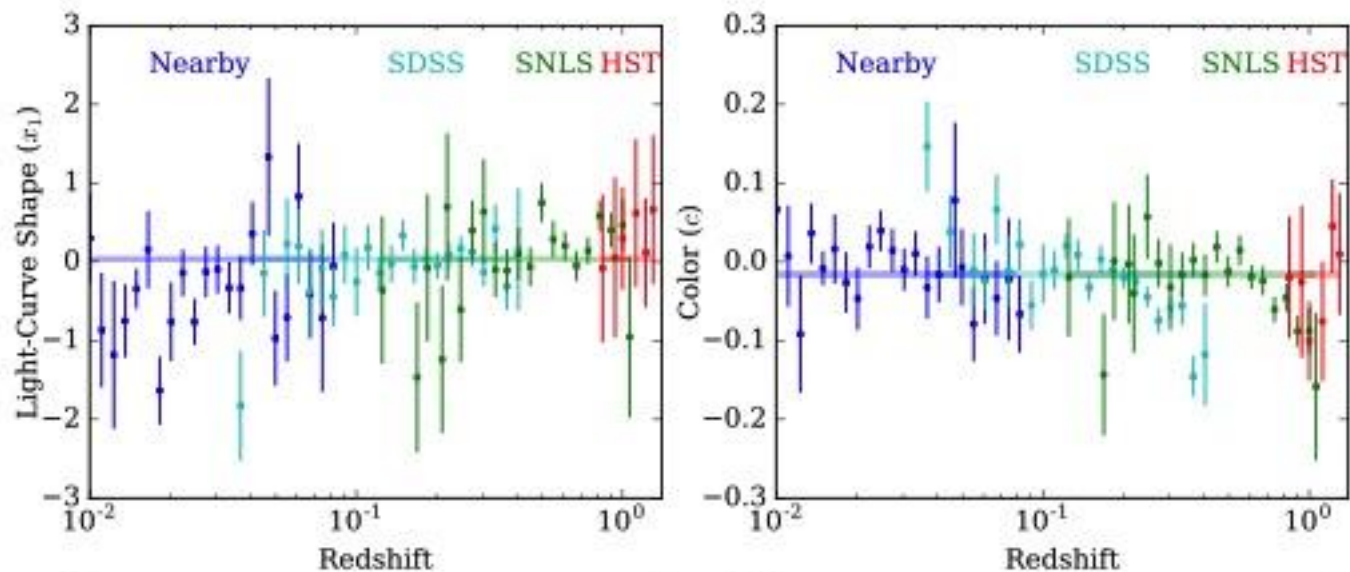
Distance modulus

$$\mu_B = m_B^* - M + \alpha X_1 - \beta C$$

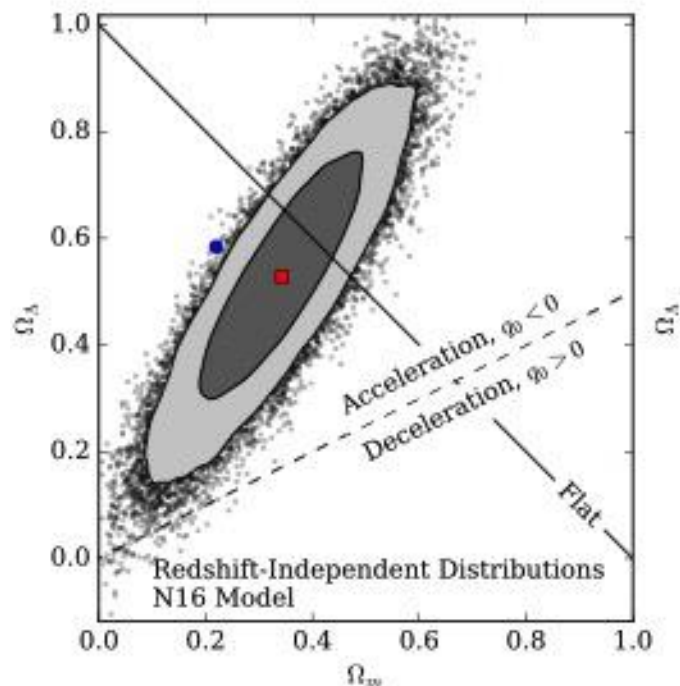
$$= 25 + 5 \log_{10} \frac{d_L}{\text{Mpc}}$$

Use a standard template (e.g. SALT 2) to make 'stretch' and 'colour' corrections ...



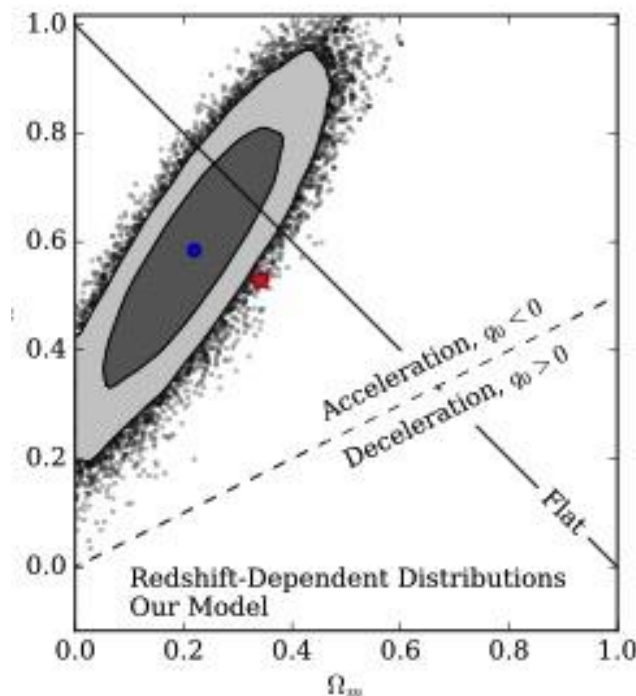


$$\mu_B = m_B^* - M + \alpha X_1 - \beta C$$



Dam *et al*

Rahman *et al*



But if  $x_1$  and  $c$  are z-dependent, SNe Ia are not standardizeable

See also works by Young-Wook Lee