

Dark Matter Heating vs. Vortex Creep Heating of Old Neutron Stars

Maura E. Ramirez Quezada (JGU Mainz)

Based on

arXiv: [2309.02633](#), [2308.16066](#), [2204.02413](#),

In collaboration with/

Motoko Fujiwara, Koichi Hamaguchi & Natsumi Nagata

PPC 2024



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भारतीय प्रौद्योगिकी संस्थान हैदराबाद
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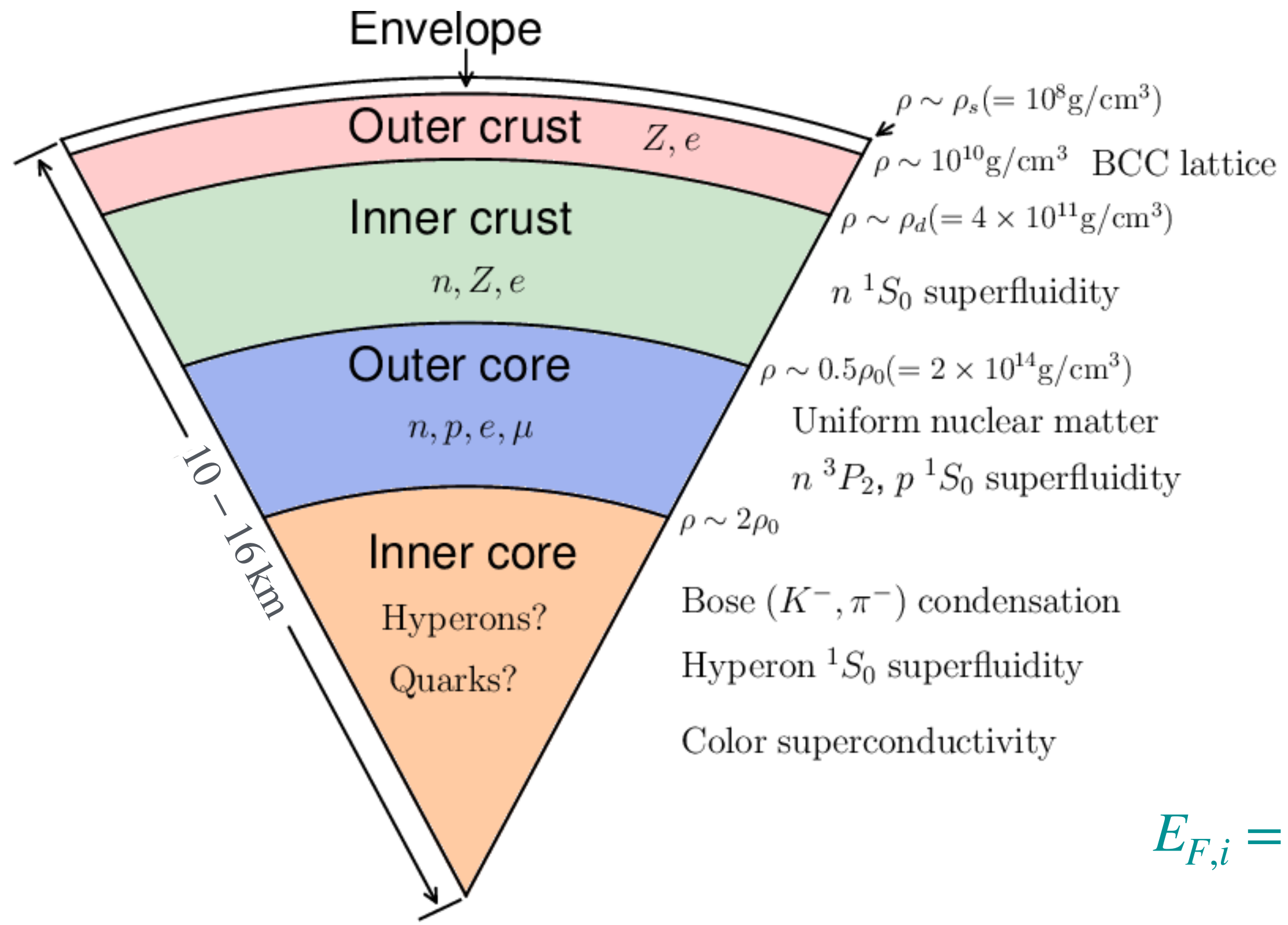
Outline

- ▶ Neutron Stars
 - ▶ Structure
 - ▶ Cooling process
- ▶ NS as DM laboratories
 - ▶ DM heating of NS
 - ▶ Vortex creep
- ▶ Summary



Neutron Stars: Structure

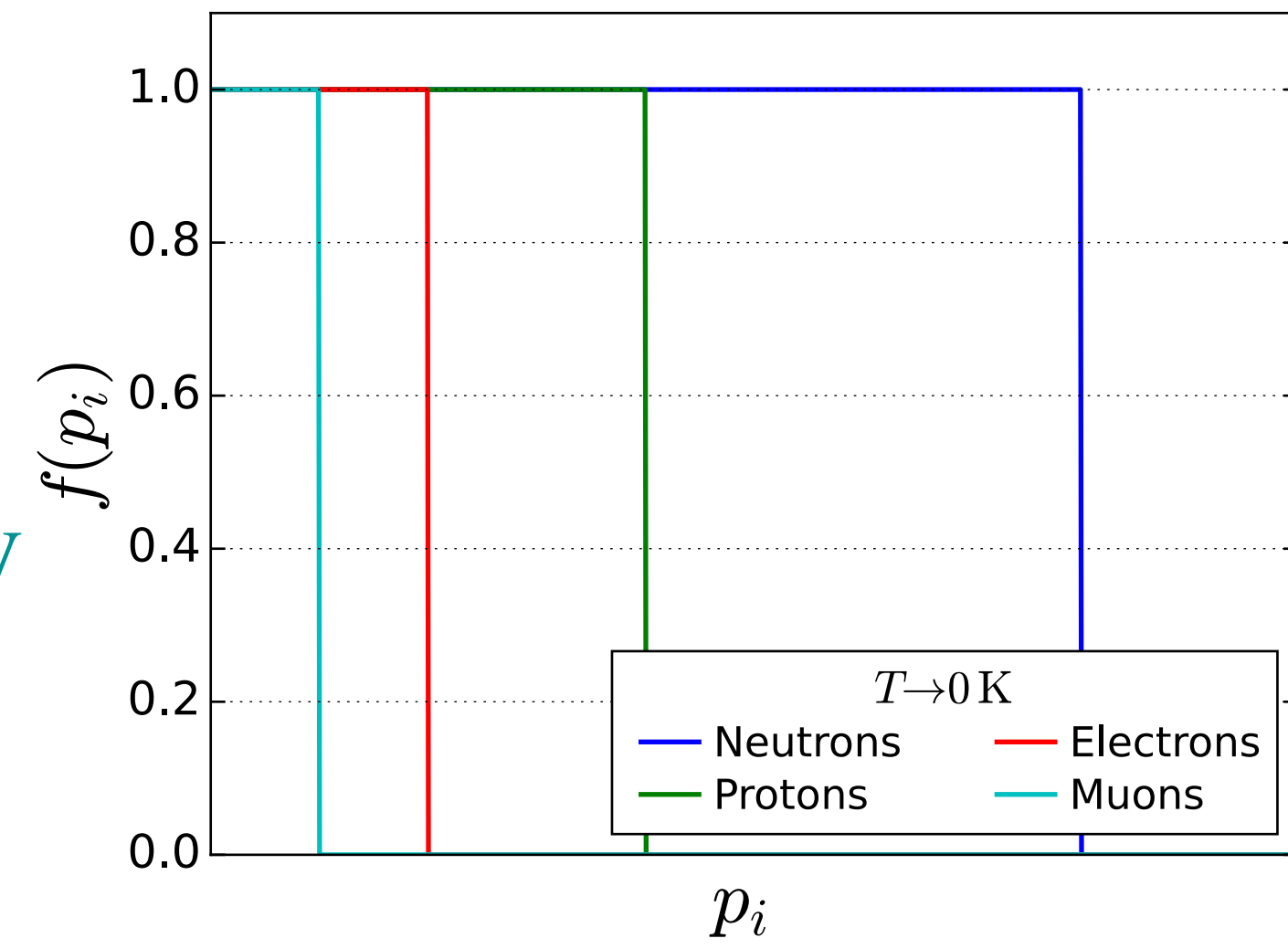
The upper mass limit depends on the uncertain EOS



- Extremely compact objects:
 $M_\star \sim (1 - 2) M_\odot, R_\star \sim (10 - 16) \text{ km}, \bar{\rho} \sim \mathcal{O}(10^{14}) \text{ g/cm}^3$
- Their exact composition is still unknown.
- The core accounts for 99% of the mass of the NS
- Mostly composed of neutrons + admixture of protons and electrons + muons (when $E_{F,e} > m_\mu$)
- Neutron, protons and electrons are degenerate

$$E_{F,i} = \frac{\hbar^2 p_{F,i}^2}{2m_i}$$

$$p_{F,n} \sim 300 - 500 \text{ MeV}$$



Lim, Y., Hyun, C.H., & Lee, C. (2015). Nuclear Equation of State and Neutron Star Cooling. *arXiv: Nuclear Theory*.

Neutron Stars: Standard Cooling Theory

$$C \frac{dT}{dt} = -L_\nu - L_\gamma$$

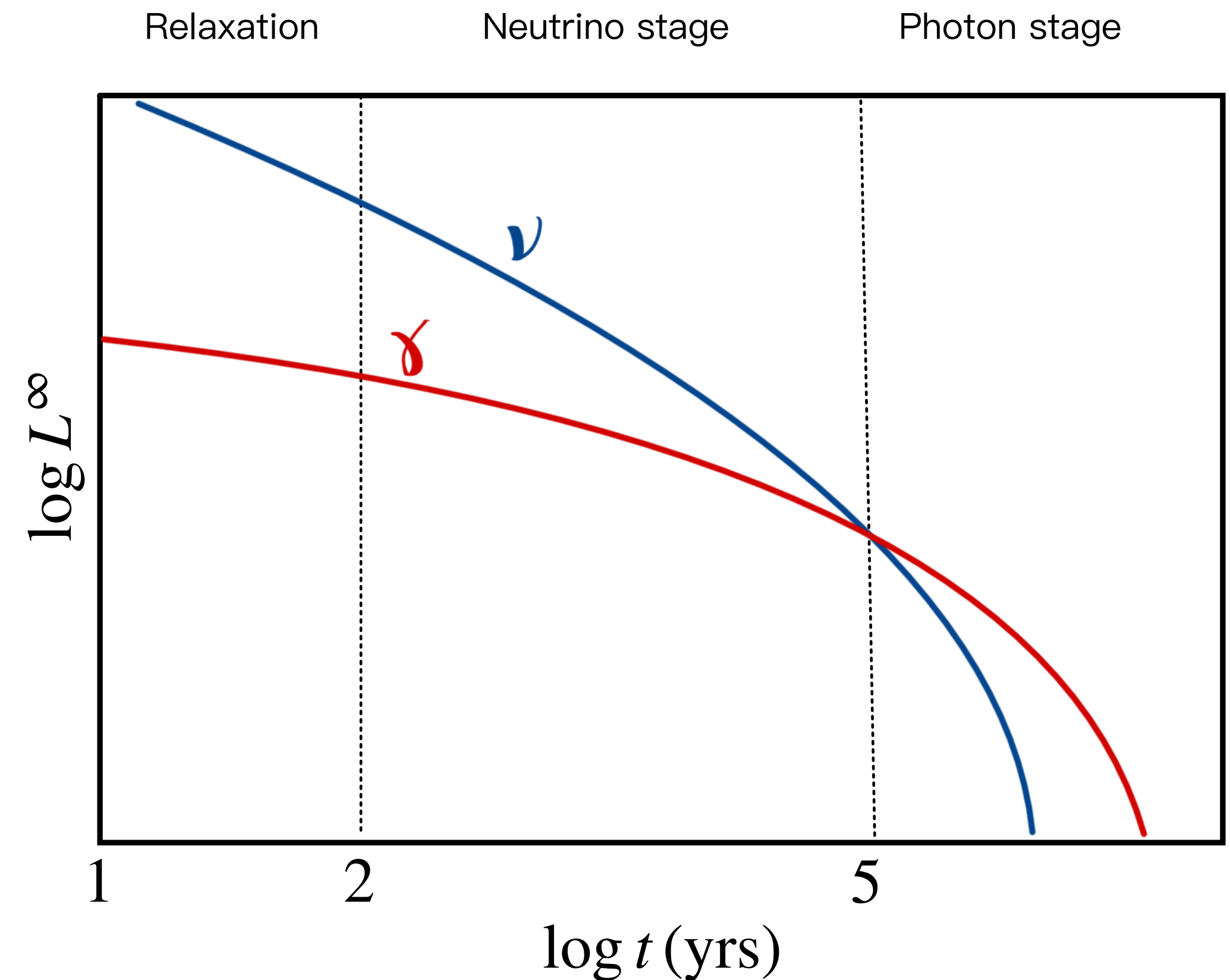
► Young NS ($t \lesssim 10^5$ yr)

Neutrino emission is the predominant process

► Old NS ($t > 10^5$ yr)

Photon emission is the predominant process

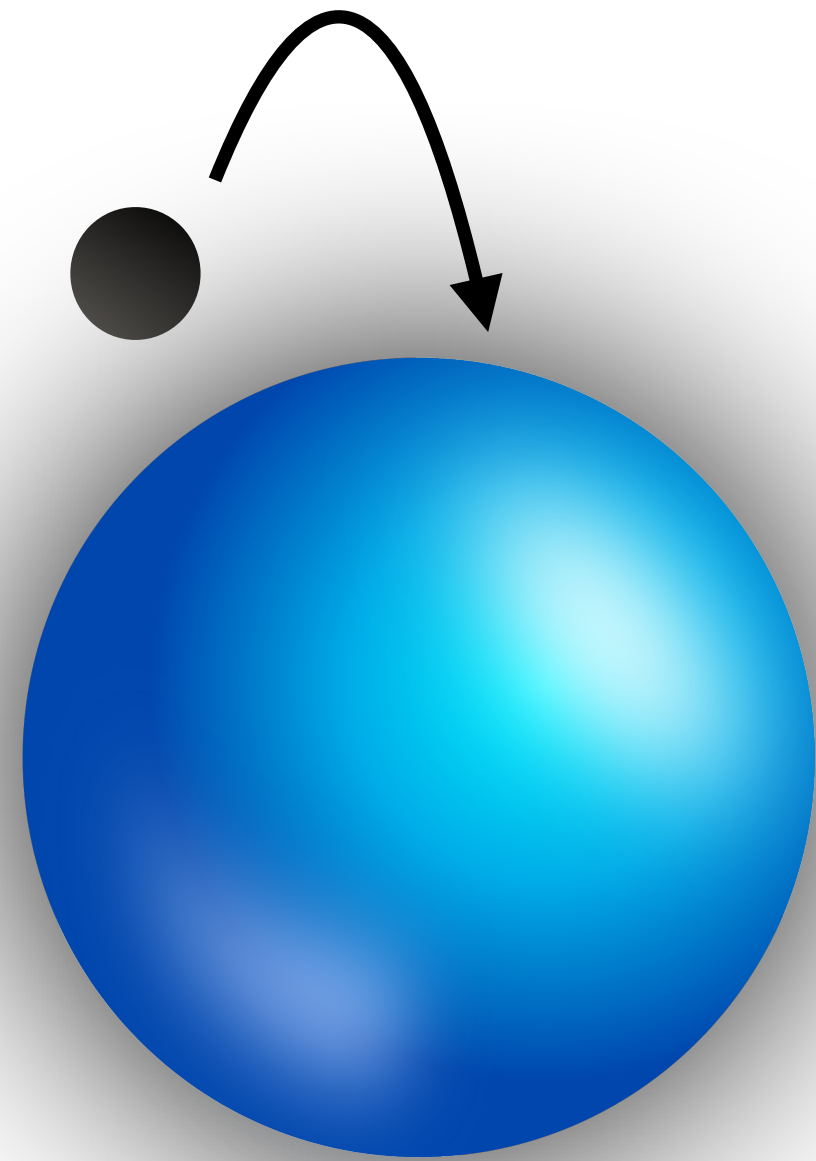
$$L_\gamma = 4\pi R_\star^2 \sigma_{\text{SB}} T_s^4$$



DM heating of NS

$$C \frac{dT}{dt} = -L_\nu - L_\gamma + L_{\text{DM}}$$

DM heating of NS

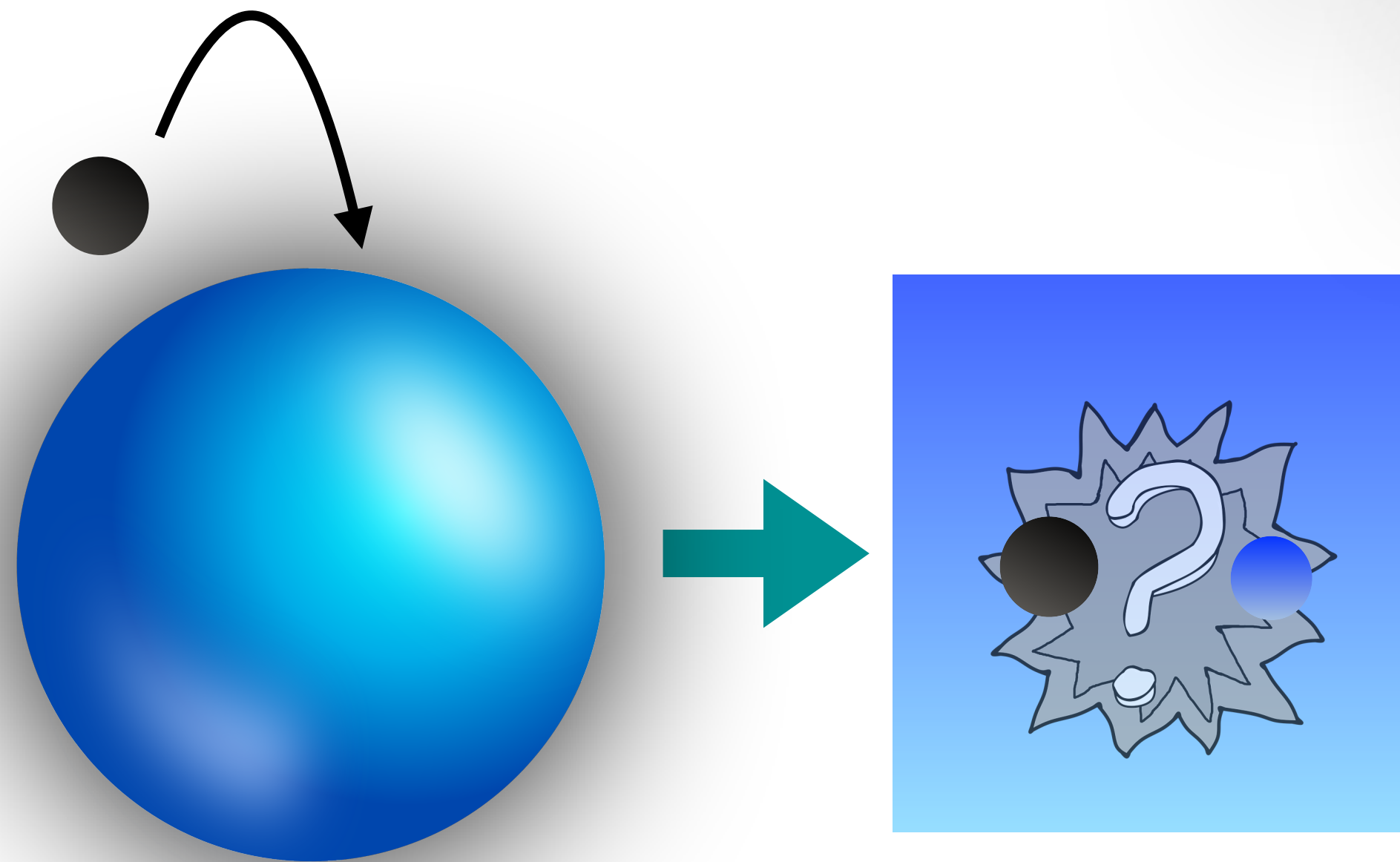


Neutron Stars

$$C \frac{dT}{dt} = -L_\nu - L_\gamma + L_{\text{DM}}$$

DM heating of NS

$$C \frac{dT}{dt} = -L_\nu - L_\gamma + L_{\text{DM}}$$

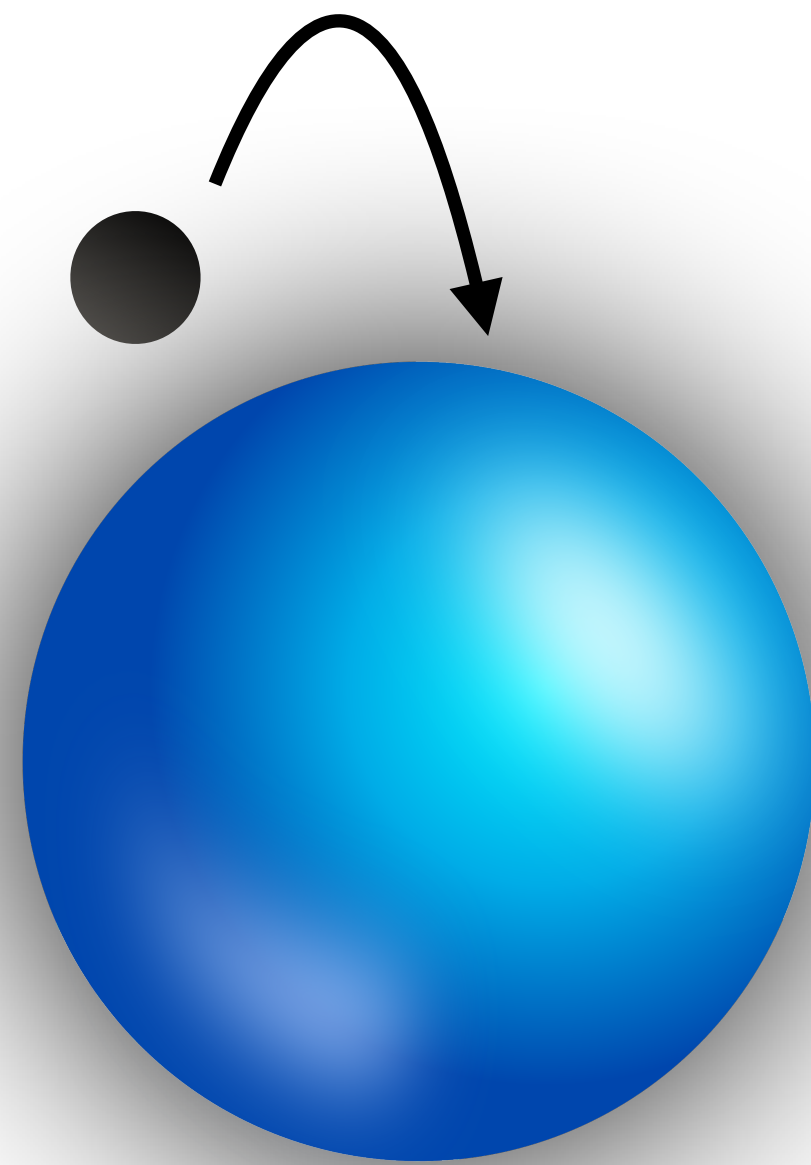


Neutron Stars

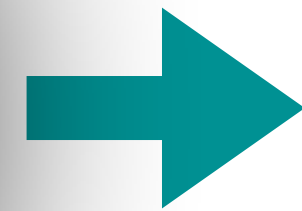
Stellar matter

DM heating of NS

$$C \frac{dT}{dt} = -L_\nu - L_\gamma + L_{\text{DM}}$$

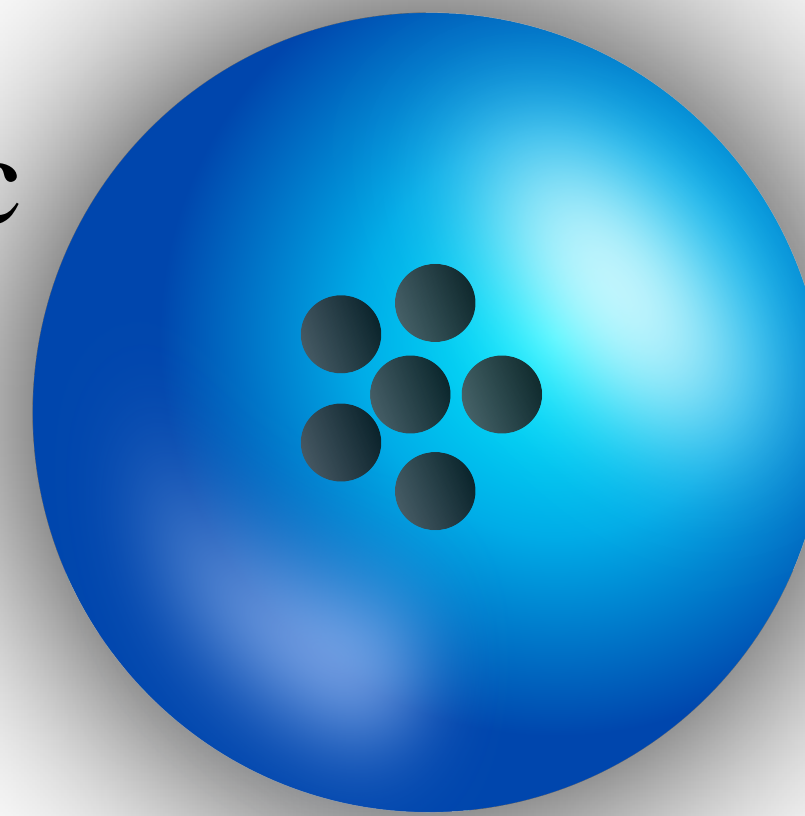
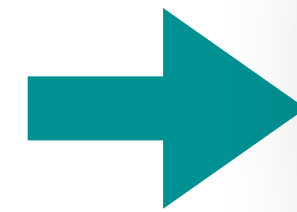


Neutron Stars



Stellar matter

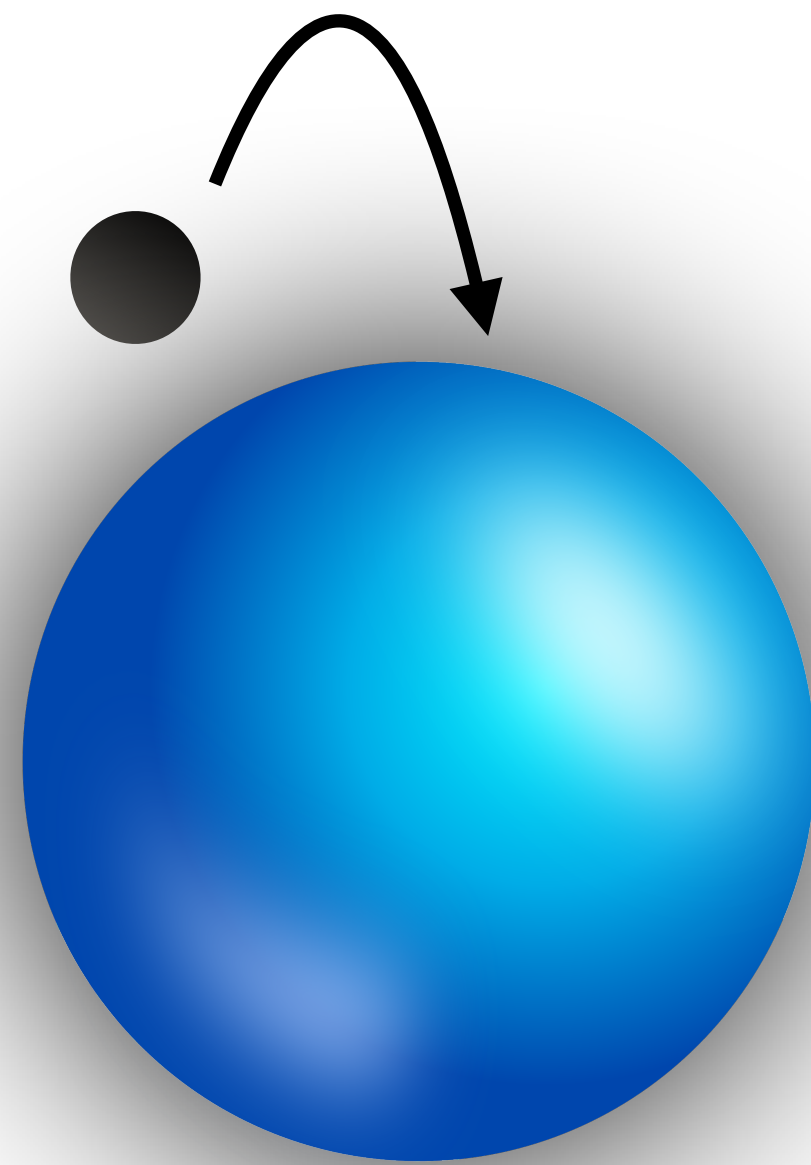
$$v < v_{\text{esc}}$$



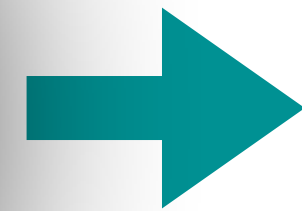
DM accumulates
in the core

DM heating of NS

$$C \frac{dT}{dt} = -L_\nu - L_\gamma + L_{\text{DM}}$$

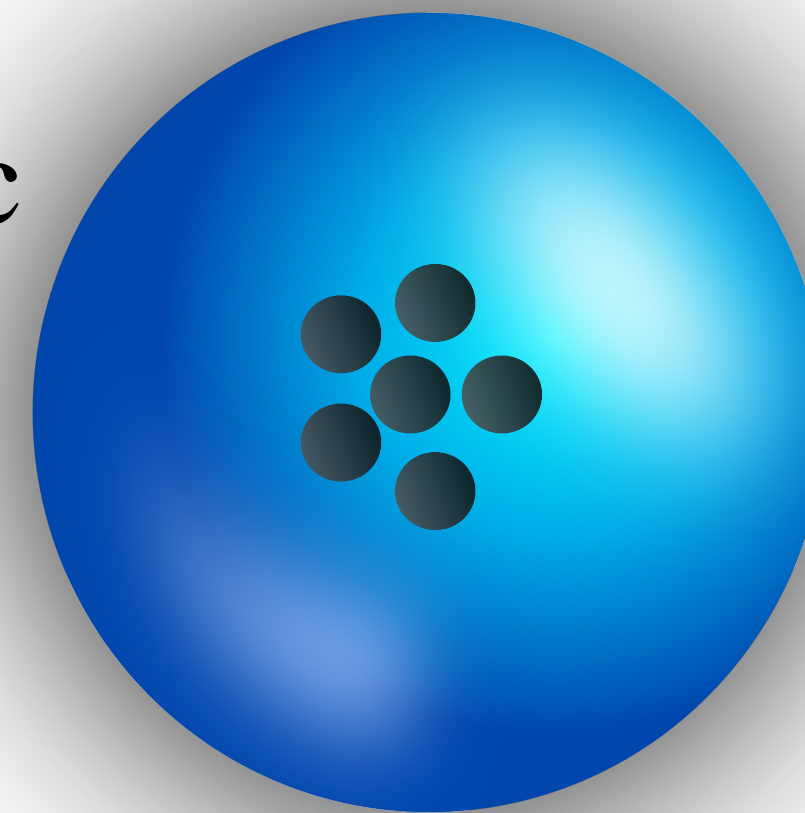
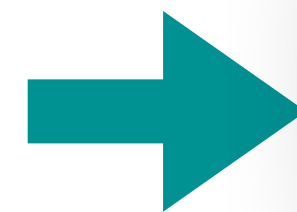


Neutron Stars

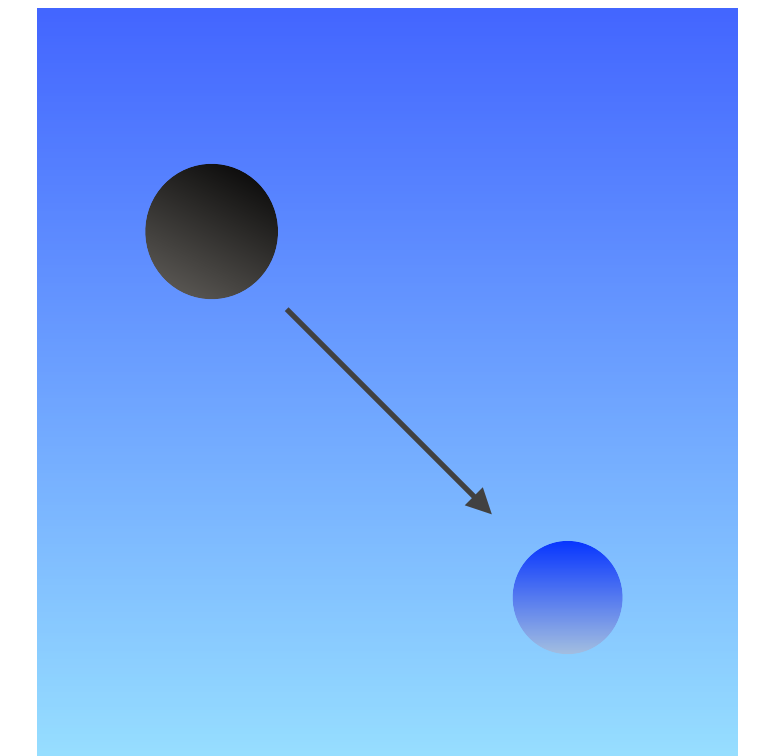
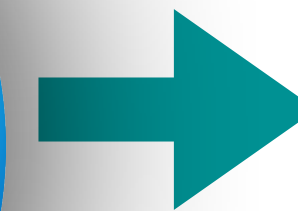


Stellar matter

$v < v_{\text{esc}}$



DM accumulates
in the core

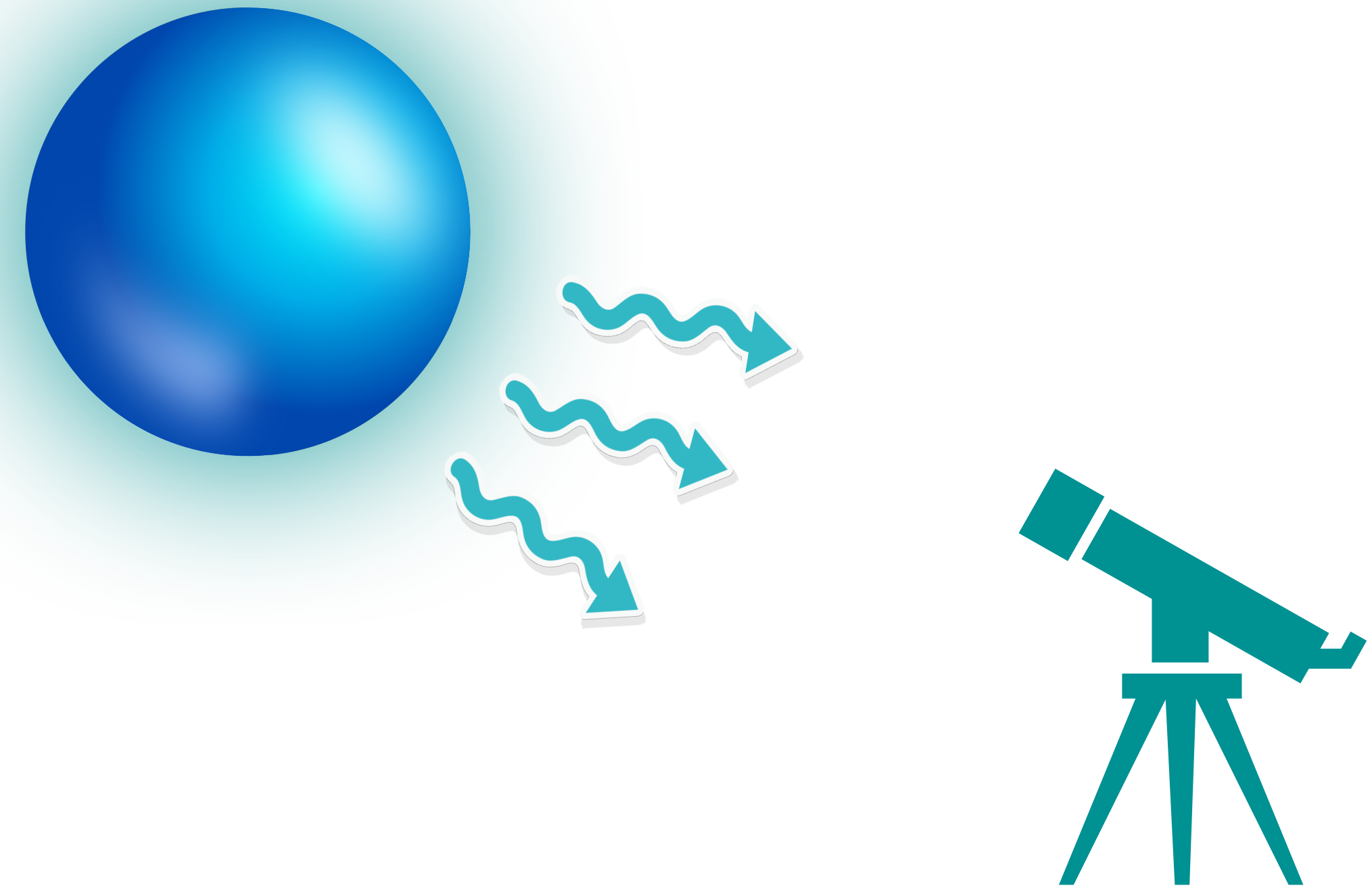
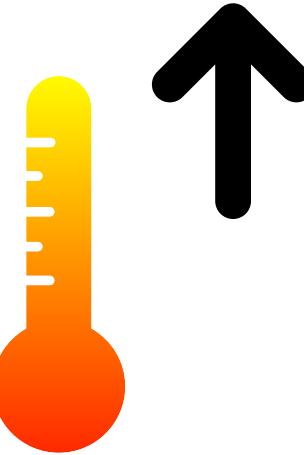


DM annihilates to
SM particles

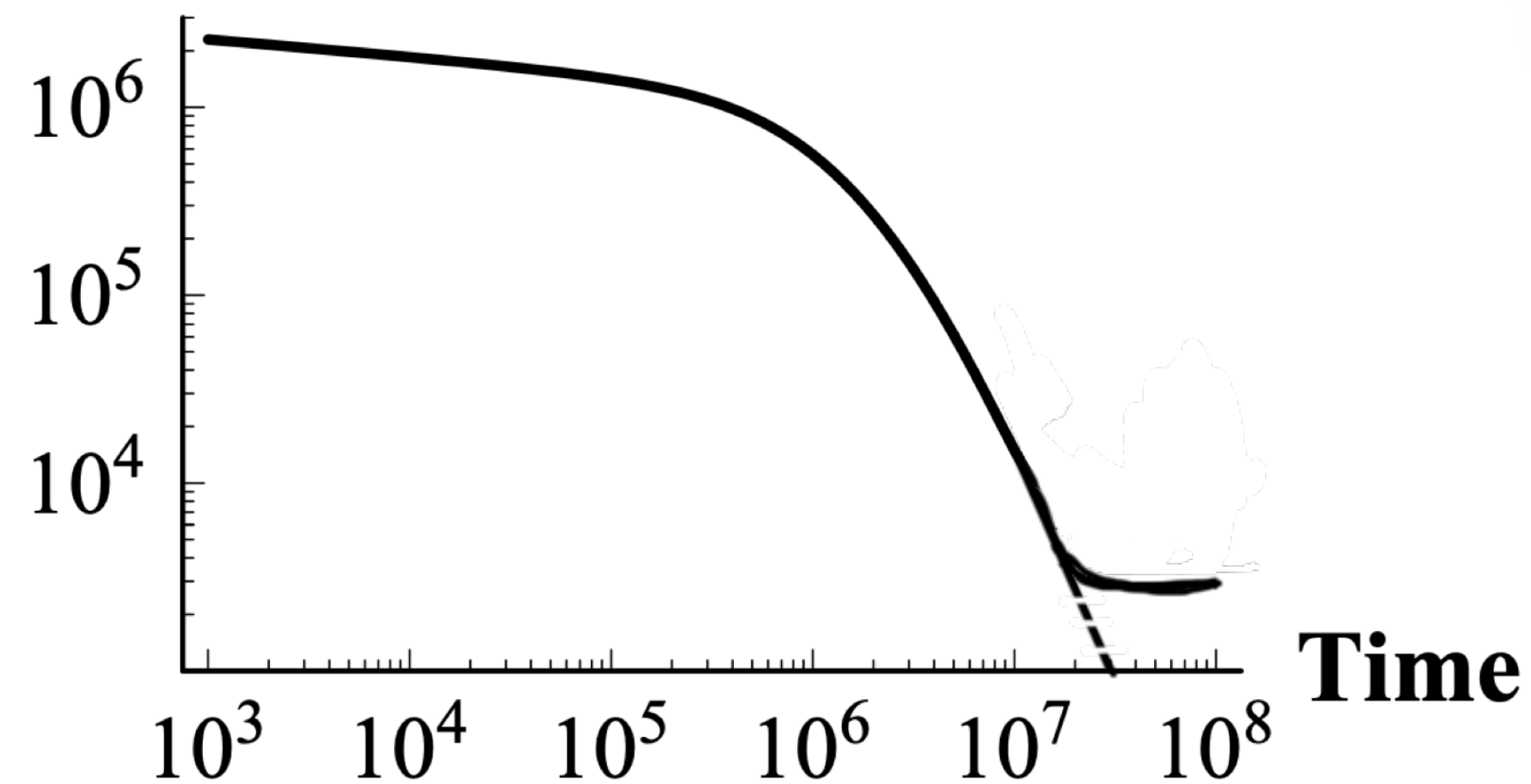
DM heating of NS

$$C \frac{dT}{dt} = -L_\nu - L_\gamma + L_{\text{DM}}$$

Heating of the star to temperatures of the order of ~ 2000 K



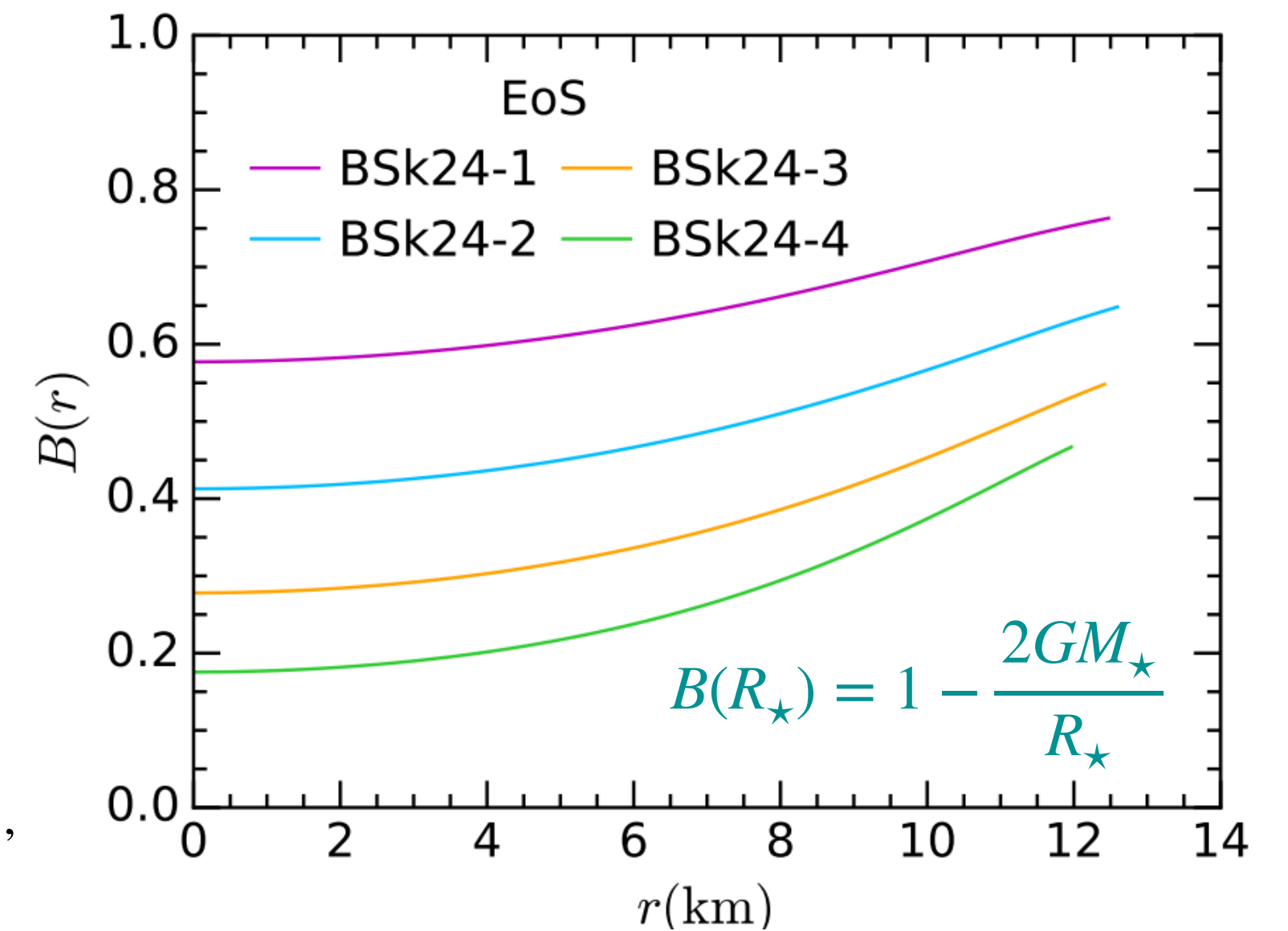
Surface Temperature



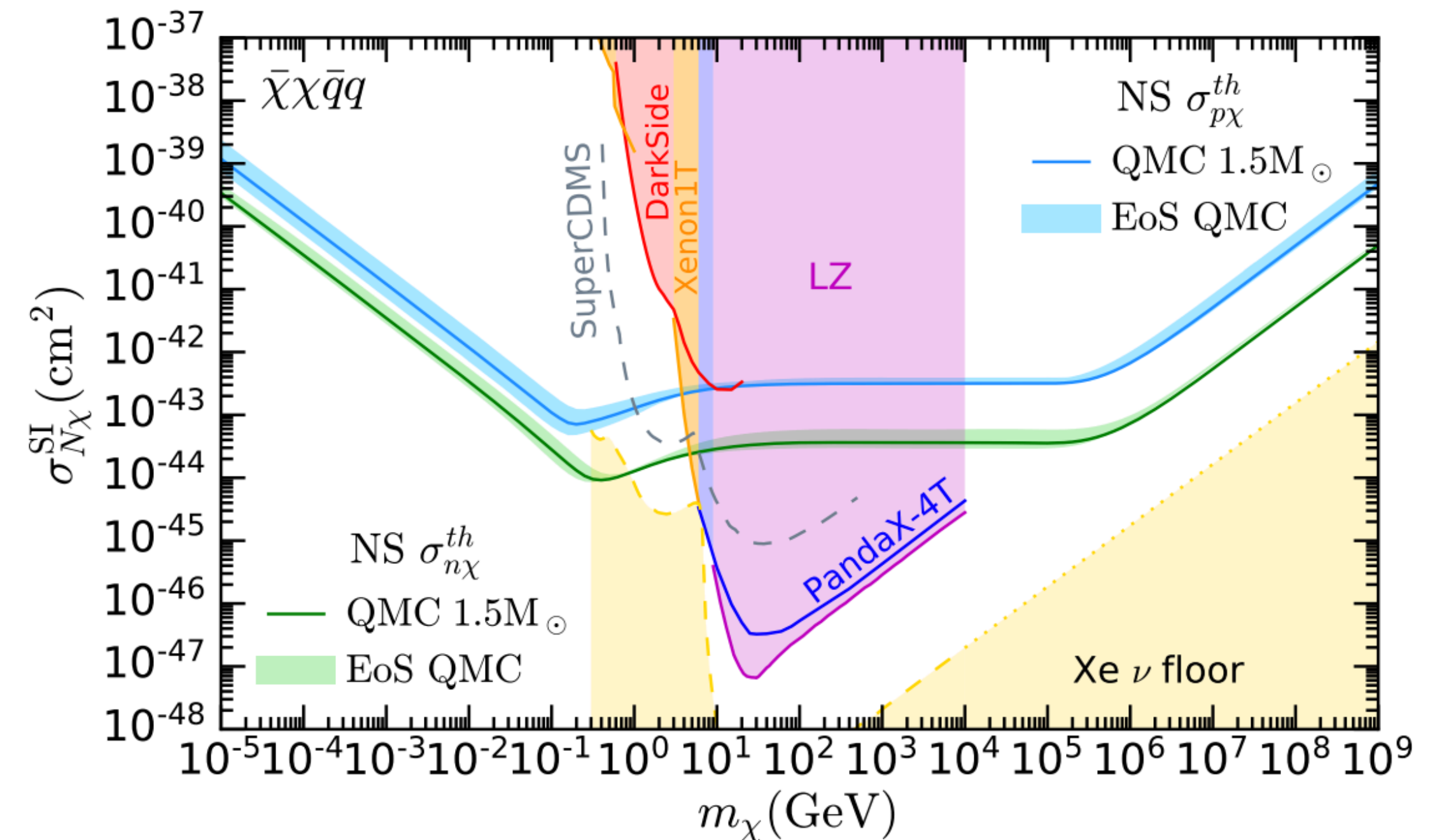
► **Observations of an old/cold NS potentially leads to a DM signal.**

NS as DM laboratories

- ▶ No detector threshold for light DM: Sub-GeV regime, down to $\mathcal{O}(10)$ keV
- ▶ DM particles become mildly relativistic when approaching the NS
 - ▶ $v_{esc}^2(r) = 1 - B(r)$ ($v \sim (0.5 - 0.7) c$ at the NS surface)
 - ▶ Velocity/momentum suppressed scattering
- ▶ Threshold cross sections:
 - ▶ Nucleons: $\sigma_{th}^N \sim [10^{-45} - 10^{-44}] \text{ cm}^2$
 - ▶ Leptons: $\sigma_{th}^\mu \sim 8 \times 10^{-44} \text{ cm}^2$
- ▶ No limitation from neutrino floor



Anzuini, Bell, Busoni, Motta, Robles, Thomas and Virgato 2108.02525



NS as DM laboratories

► Multiple targets: e, μ, p, n

► **DM coupled only to muon**

K. Hamaguchi, N. Nagata, MRQ [2204.02413]

A large parameter space will remain **unexplored** in the LHC and DM **direct searches**.

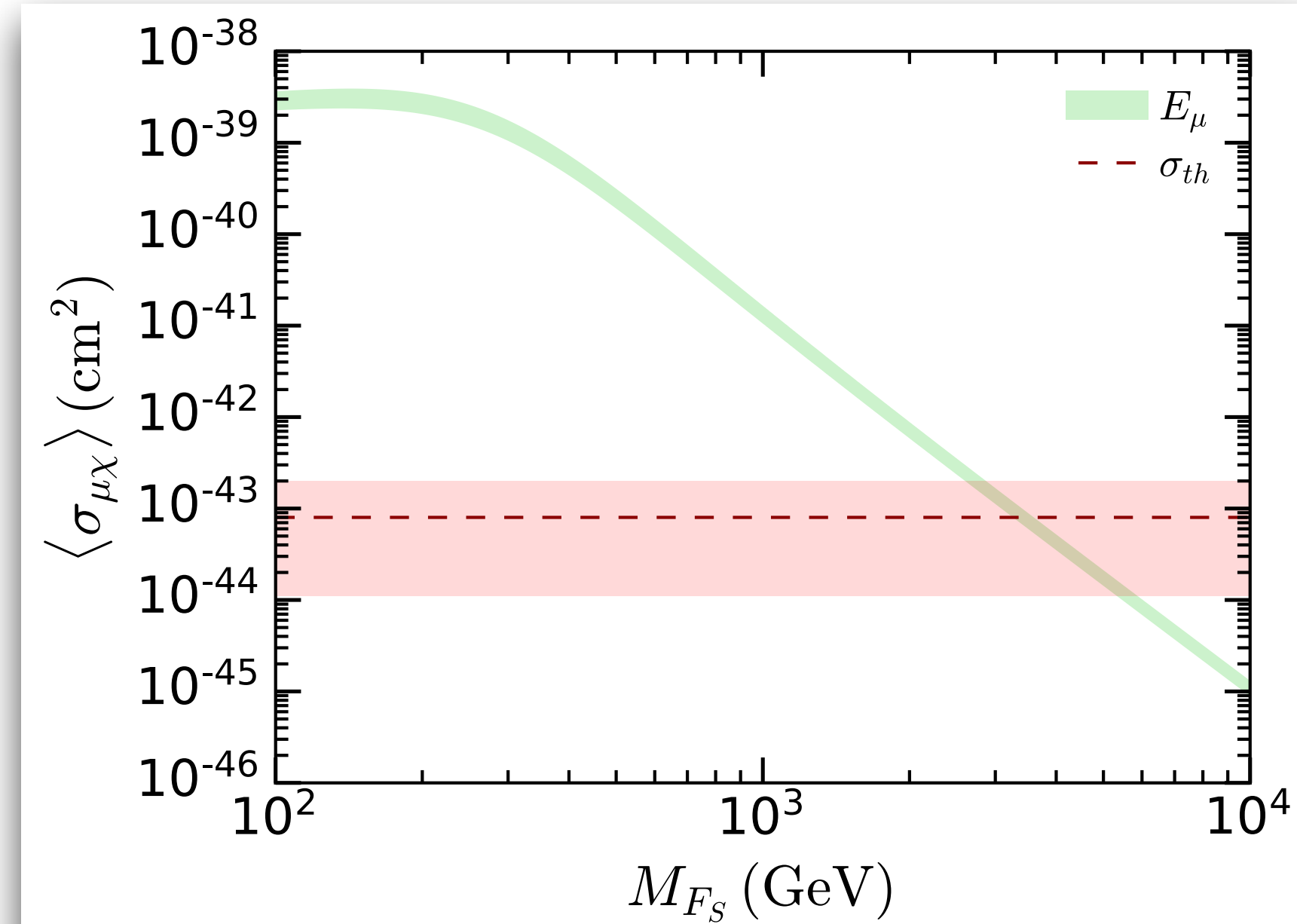
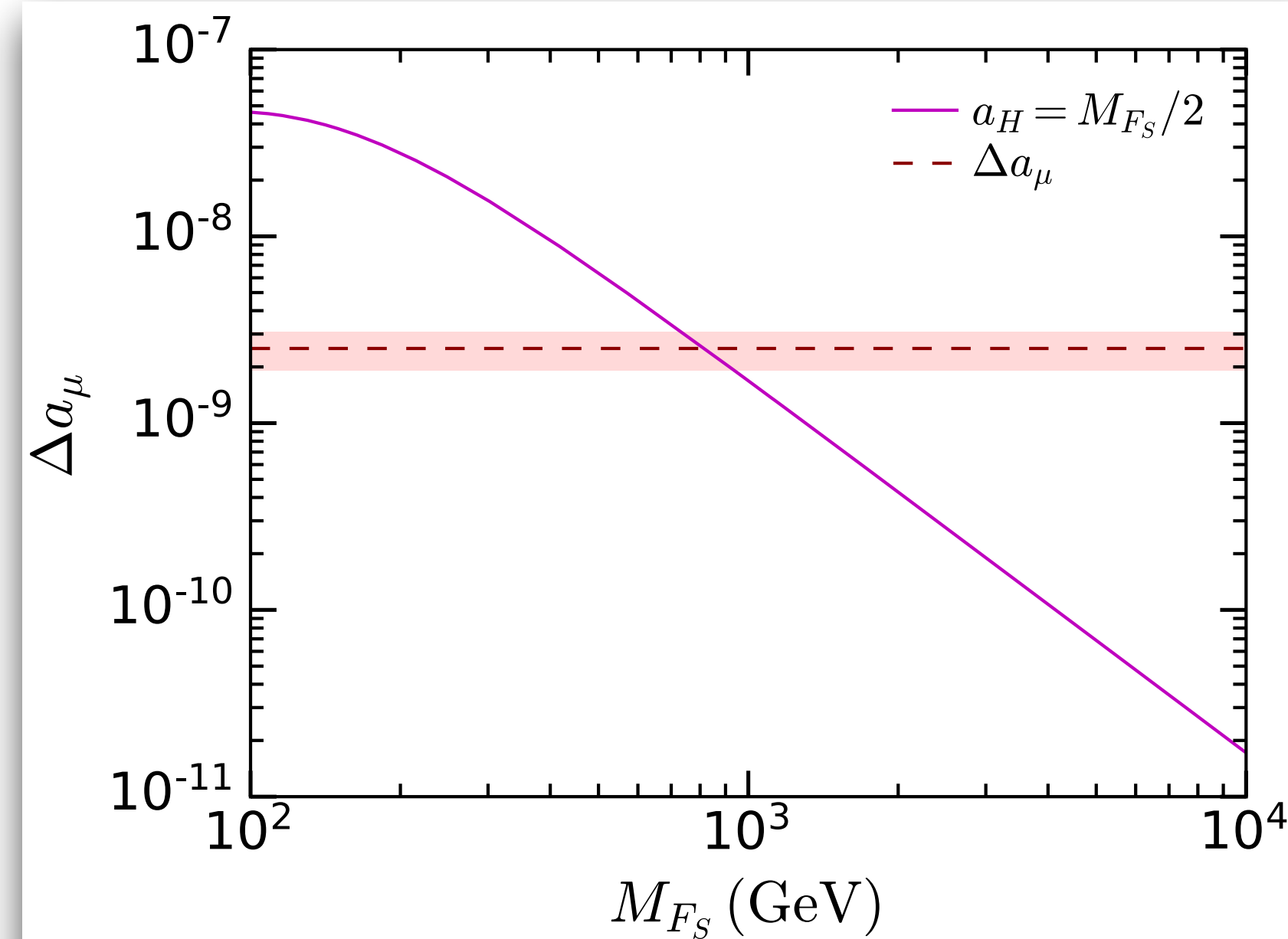
Field	Spin	SU(3) _C	SU(2) _L	U(1) _Y	Z ₂
χ_S	1/2	1	1	0	–
\tilde{L}	0	1	2	–1/2	–
\tilde{e}	0	1	1	1	–

$$\mathcal{L}_{\text{mass}} = - \left(\frac{1}{2} M_{F_S} \chi_S \chi_S + \text{h.c.} \right) - M_{\tilde{L}}^2 |\tilde{L}|^2 - M_{\tilde{e}}^2 |\tilde{e}|^2,$$

$$\mathcal{L}_{\text{Yukawa}} = -y_1 \chi_S L_\mu \tilde{L}^\dagger - y_2 \chi_S \mu_R^c \tilde{e}^\dagger + \text{h.c.},$$

$$\mathcal{L}_{\text{tri}} = -a_H \tilde{e} \tilde{L} H^\dagger + \text{h.c.},$$

$$\mathcal{L}_{\text{quart}} = - \sum_{f=L, \tilde{e}} \lambda_f |\tilde{f}|^2 |H|^2 - \lambda'_L \tilde{L}^\dagger \tau_a \tilde{L} H^\dagger \tau_a H + \dots$$



NS as DM laboratories

Internal heating: **Vortex creep**

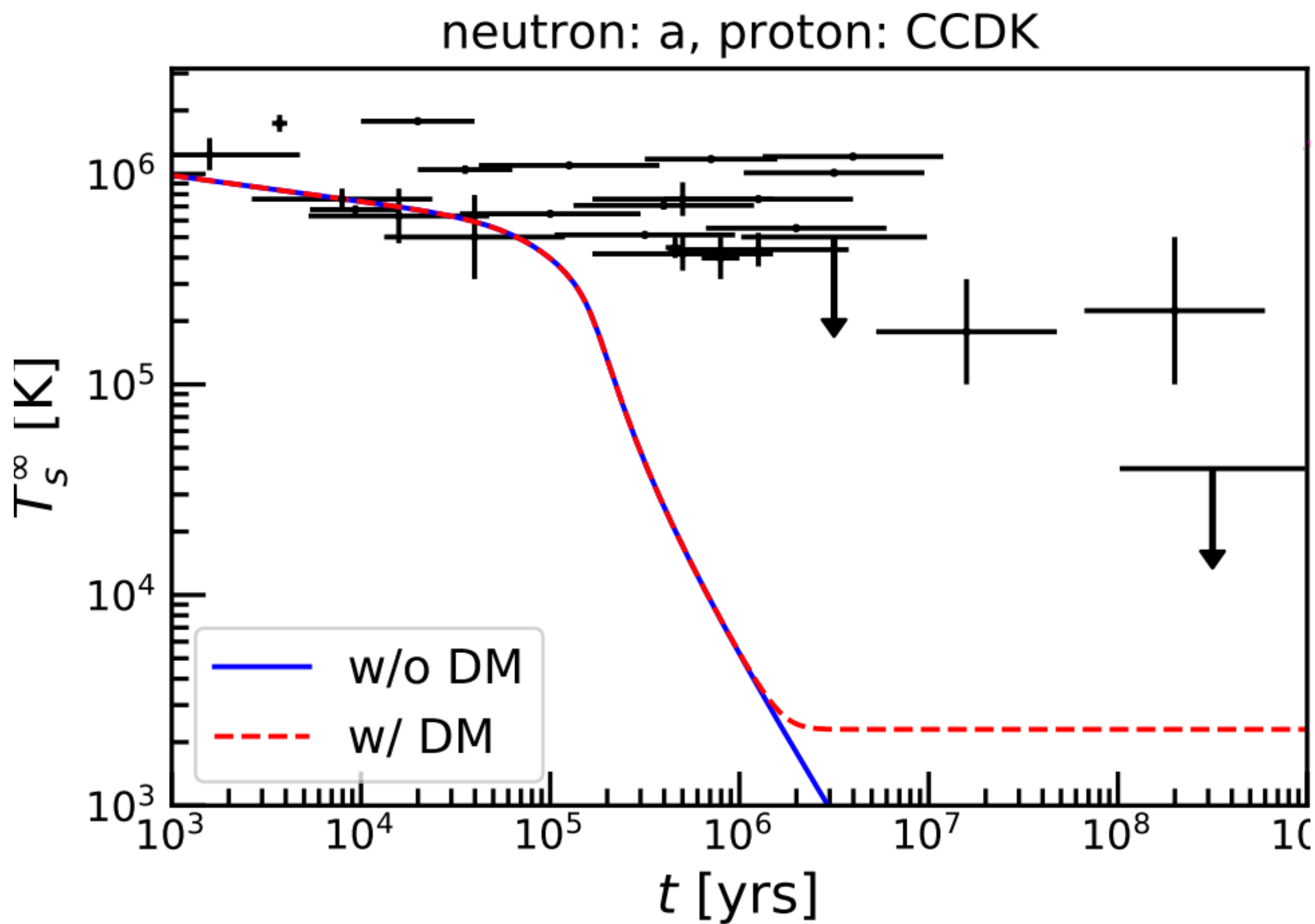


Figure taken from [K. Yanagi's](#)

► Some **old** and **warmer** NSs have been observed ($T \gg 2000$ K)

► Neither standard cooling nor DM heating **can** explain those old warm NSs.

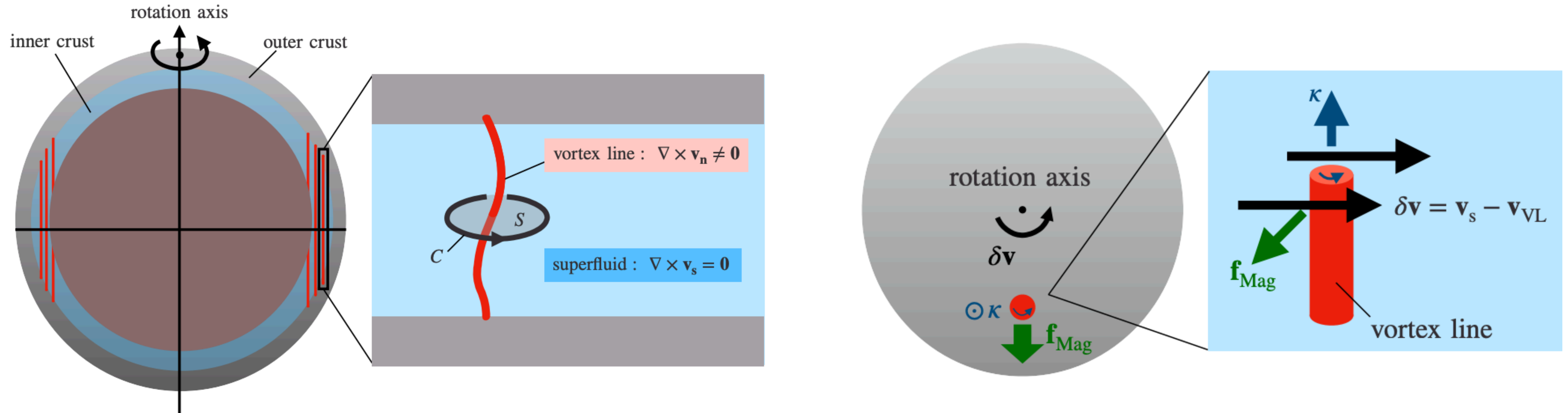
► Some internal heating could be the reason/explanation for such NS temperatures:

► **Vortex creep Heating.**

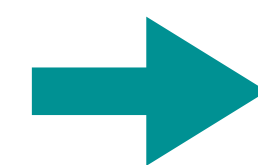
[M. Fujiwara, K. Hamaguchi, N. Nagata, MRQ \[arXiv: 2308.16066, 2309.02633\]](#)

NS as DM laboratories

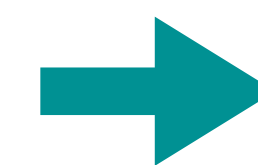
Internal heating: Vortex creep



Vortex lines are formed in a rotating NS



Vortex creep: Vortex lines start to move outwards



Vortex creep heating: total energy stored in the superfluid component is dissipated as heat

NS as DM laboratories

Internal heating: **Vortex creep**

$$C \frac{dT}{dt} = -L_\nu - L_\gamma + L_{\text{VC}}$$

Phenomenological approach of J

$$L_{\text{VC}} = J |\dot{\Omega}|$$

$$T_s^{\text{eq}} = \left(\frac{J |\dot{\Omega}|}{4\pi R_\star^2 \sigma_{\text{SB}}} \right)^{1/4}$$

Steady vortex creep scenario: The crust and superfluid component decelerate at the same time

VC heating mechanism balanced with the photon luminosity $L_\gamma = L_{\text{VC}}$

NS as DM laboratories

Internal heating: Vortex creep

$$J_{\text{obs}} = \frac{4\pi R_{\star}^2 \sigma_{\text{SB}} T_s^4}{|\dot{\Omega}|}$$

Young pulsars

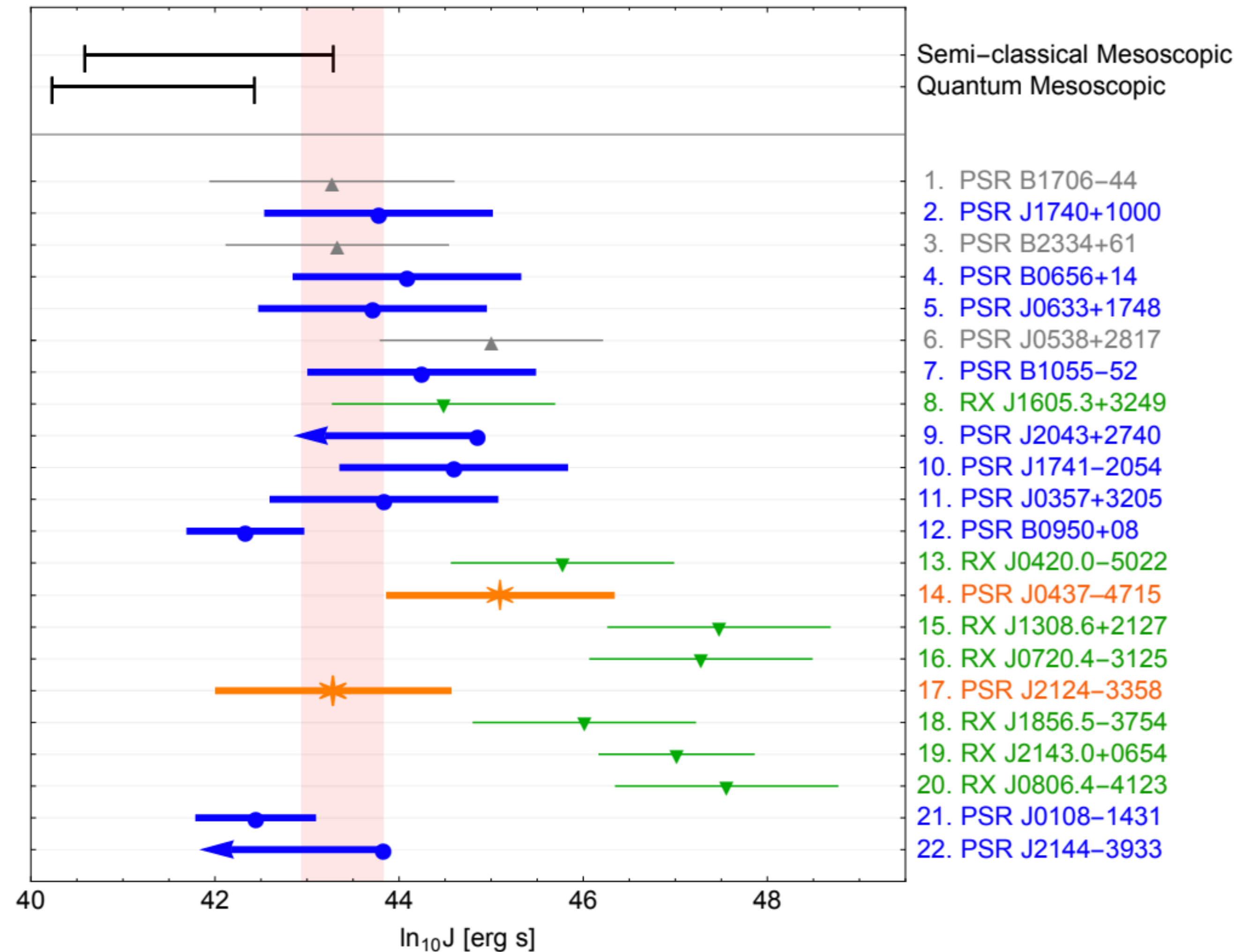
XDINS (strong magnetic fields)

Ordinary pulsars

Millisecond pulsars

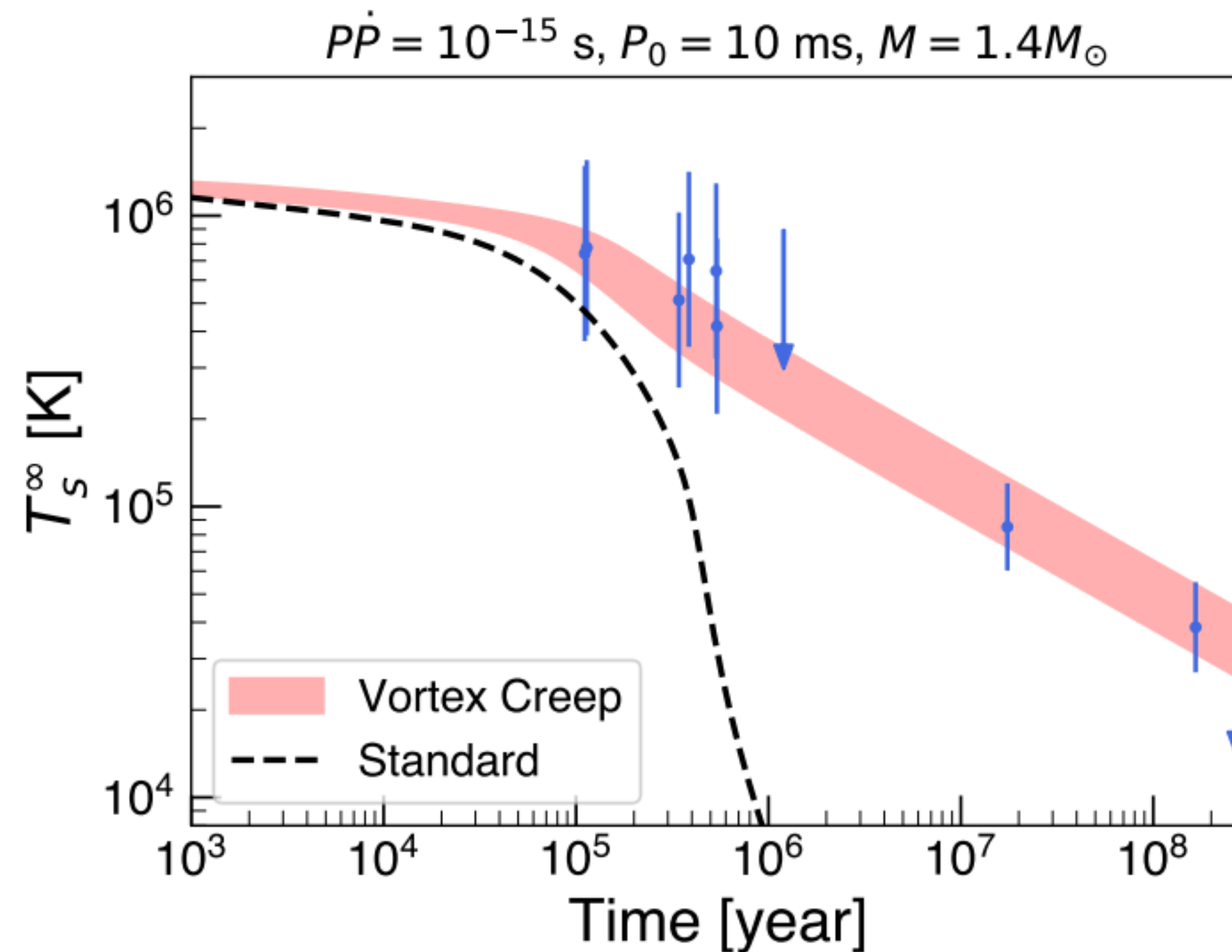
$$J_{\text{obs}} \sim 10^{43} - 10^{44} \text{ erg} \cdot \text{s}$$

$$\text{For } |\dot{\Omega}| = [10^{-16}, 10^{-10}] \text{ s}^{-2}$$

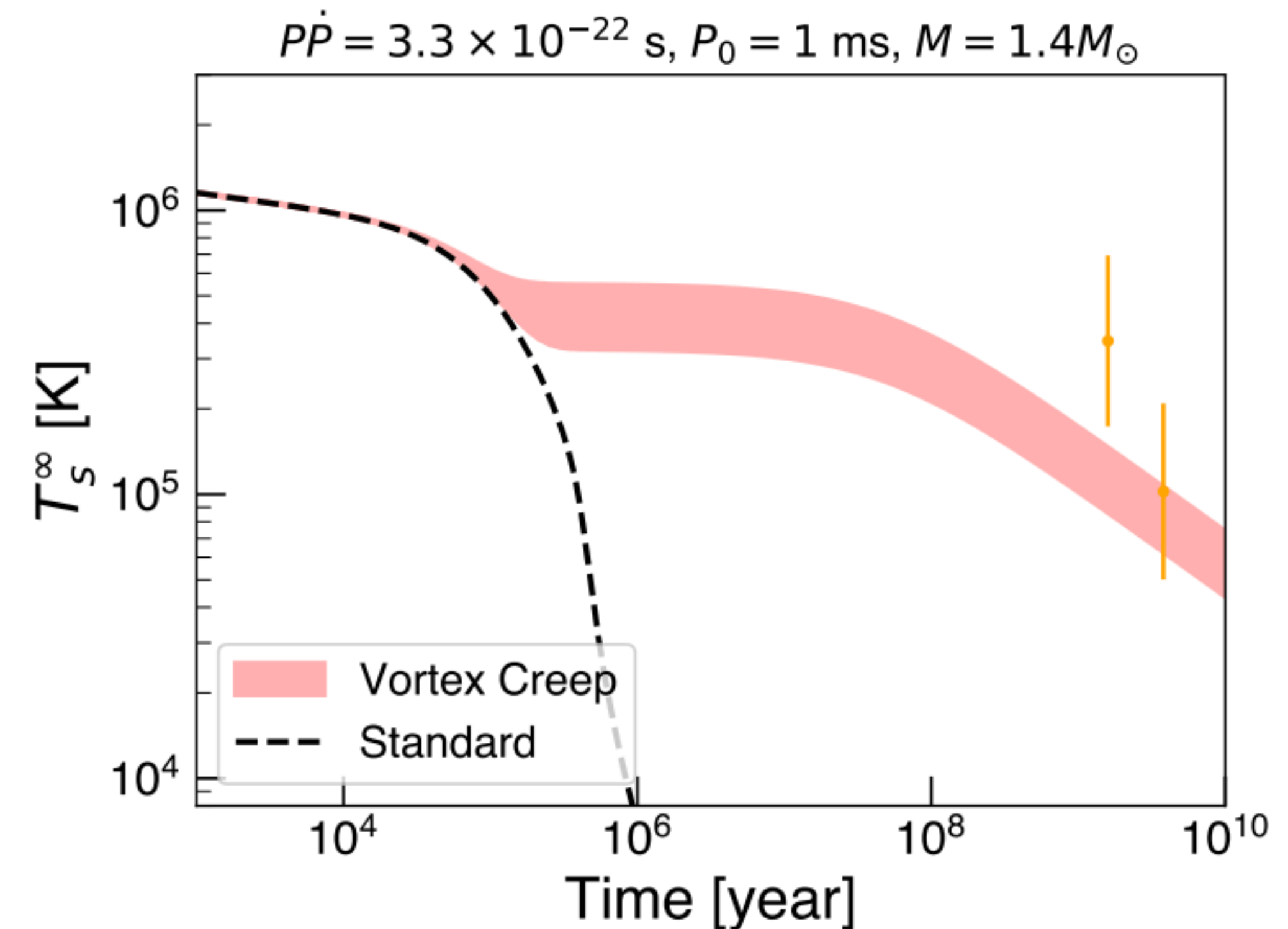


NS as DM laboratories

Internal heating: Vortex creep



(a) Ordinary pulsars



(b) Millisecond pulsars

NS as DM laboratories

Vortex creep heating + DM heating

$$C \frac{dT}{dt} = -L_\nu - L_\gamma + L_{\text{heat}}$$

Assuming the heating luminosity is dominated by the DM effects:

$$T_{s|\text{DM}} = \left(\frac{[X + (B(R_\star)^{-1/2} - 1)] m_\chi C(m_\chi)}{4\pi R_\star^2 \sigma_{\text{SB}}} \right)^{1/4}$$

$$L_{\text{heat}} \simeq L_\gamma = B(R_\star) \times 4\pi R_\star^2 \sigma_{\text{SB}} T_s^4$$

$$T_s^{\text{Max}} = 2600 \text{ K}$$

After capture and annihilation of DM

$$L_{\text{DM}} \simeq B(R_\star) \times [X + (B(R_\star)^{-1/2} - 1)] m_\chi C(m_\chi)$$

- The predicted surface temperature dominated by DM effects is quite universal for a wide range of DM mass

$$1 \text{ GeV} \lesssim m_\chi \lesssim 1 \text{ PeV}$$

NS as DM laboratories

Vortex creep heating + DM heating

$$C \frac{dT}{dt} = -L_\nu - L_\gamma + L_{\text{heat}}$$

↓

$$L_{\text{VC}} + L_{\text{DM}}$$

$$L_{\text{heat}} \simeq L_\gamma = B(R_\star) \times 4\pi R_\star^2 \sigma_{\text{SB}} T_s^4$$

After capture and annihilation of DM

$$L_{\text{DM}} \simeq B(R_\star) \times [X + (B(R_\star))^{-1/2} - 1] m_\chi C(m_\chi)$$

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$$T_{s|\text{DM}} = \left(\frac{[X + (B(R_\star))^{-1/2} - 1] m_\chi C(m_\chi)}{4\pi R_\star^2 \sigma_{\text{SB}}} \right)^{1/4}$$

$$T_s^{\text{Max}} = 2600 \text{ K}$$

- The predicted surface temperature dominated by DM effects is quite universal for a wide range of DM mass

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NS as DM laboratories

Vortex creep heating + DM heating

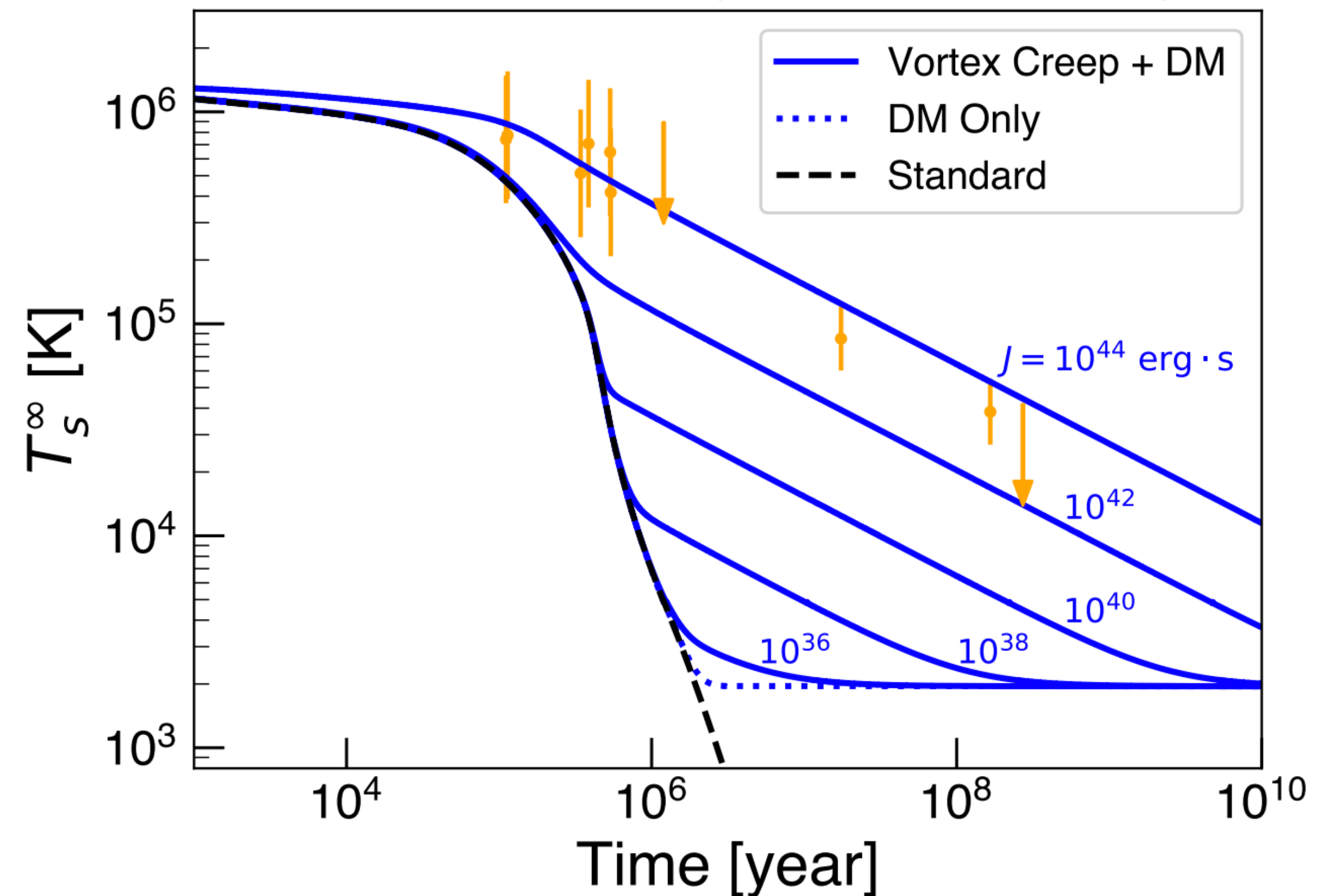
To observe DM heating effects:

$$L_{VC} \ll L_{DM}$$

The DM heating is concealed by the vortex creep heating unless $J \lesssim 10^{38} \text{ erg} \cdot \text{s}$

- ▶ Akmal-Pandaharipande-Ravenhall (APR) EOS. [arXiv:nucl-th/9804027]
- ▶ $M_{\star} = 1.4 M_{\odot}$
- ▶ $R_{\star} = 12 \text{ km}$

$$P = 1 \text{ s}, \dot{P} = 10^{-15}, P_0 = 10 \text{ ms}, M = 1.4 M_{\odot}$$



NS as DM laboratories

Vortex creep heating + DM heating

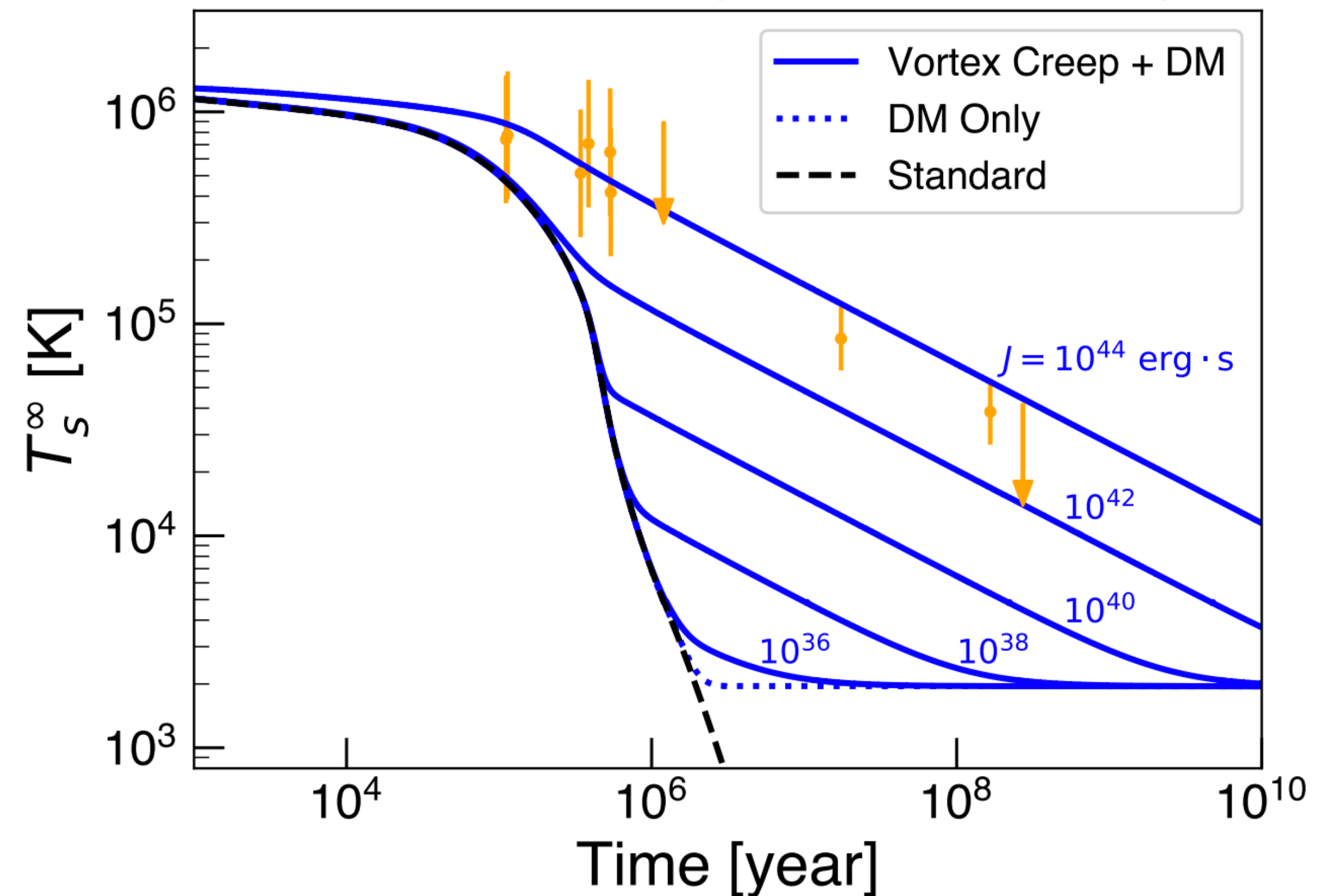
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NS as DM laboratories

Vortex creep heating + DM heating

To observe DM heating effects:

$$L_{VC} \ll L_{DM} \quad \times$$

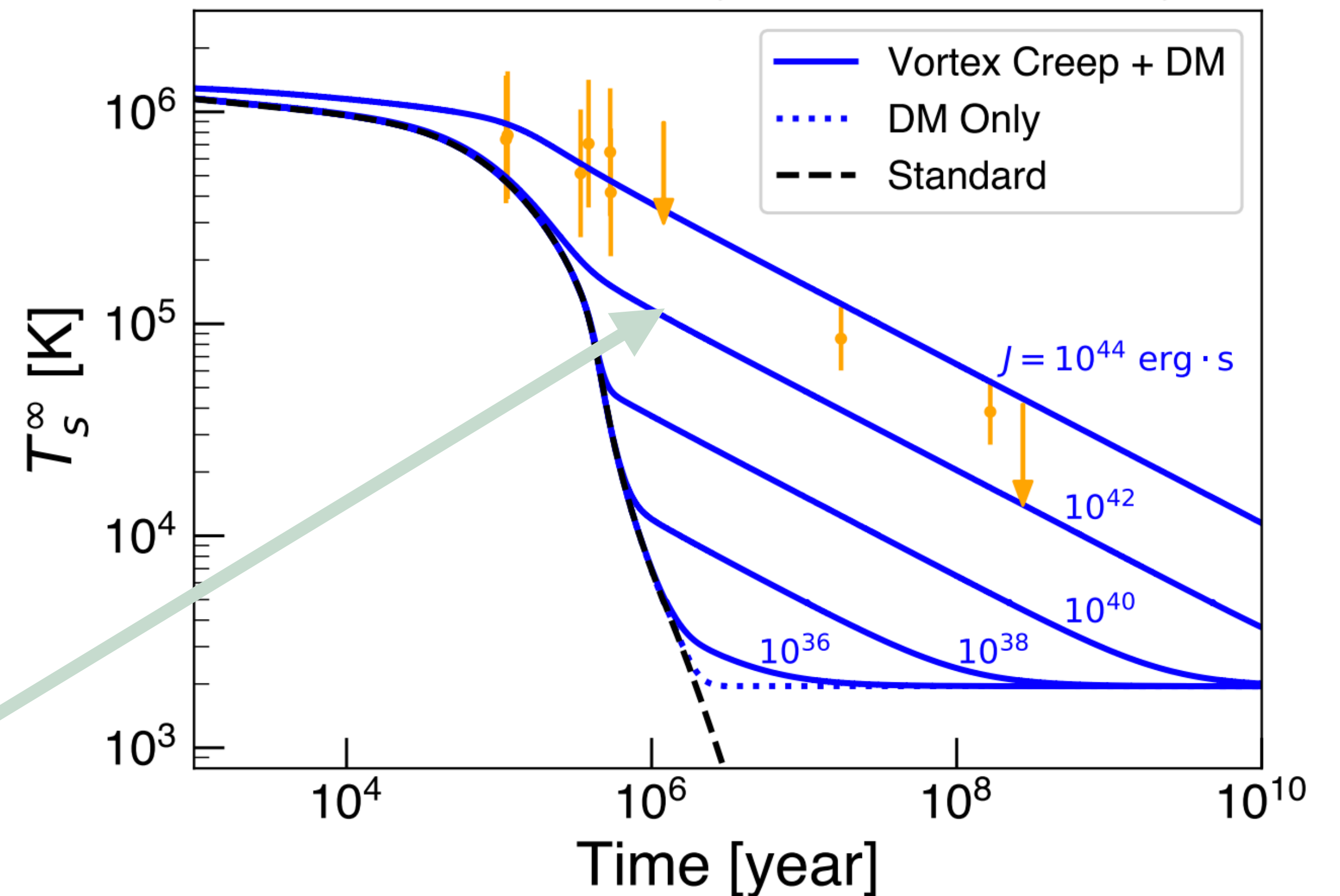
The DM heating is concealed by the vortex creep heating unless $J \lesssim 10^{38} \text{ erg} \cdot \text{s}$

Seems to be challenging

$J \sim 10^{44} \text{ erg} \cdot \text{s}$ can explain old & warm NS

- ▶ Akmal-Pandaharipande-Ravenhall (APR) EOS. [arXiv:nucl-th/9804027]
- ▶ $M_{\star} = 1.4 M_{\odot}$
- ▶ $R_{\star} = 12 \text{ km}$

$$P = 1 \text{ s}, \dot{P} = 10^{-15}, P_0 = 10 \text{ ms}, M = 1.4 M_{\odot}$$



Summary

- ▶ NS Heating is a promising alternative/complementary method to test Dark Matter.
 - ▶ Allows access to *velocity*- and *momentum*-dependent interactions
 - ▶ Probes the *Sub-GeV* DM mass regime
 - ▶ Multiple targets make it ideal for testing *DM-lepton* interactions
- ▶ Some *old and warm NSs* have been observed suggesting an *internal heating* mechanism
 - ▶ *Vortex creep heating*: If this is the dominant mechanism, DM effects could be *difficult to detect or observe*.

Thank you

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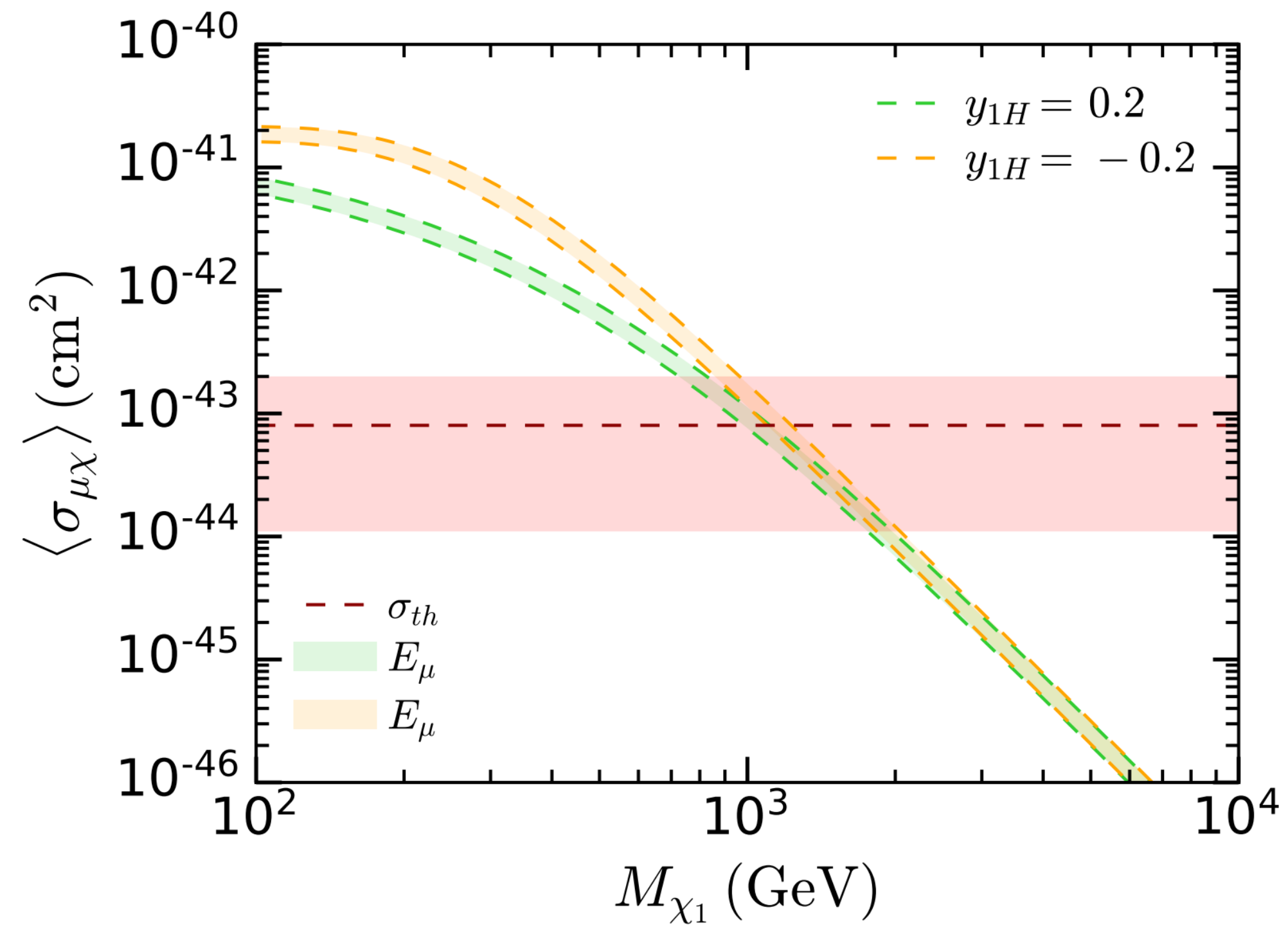
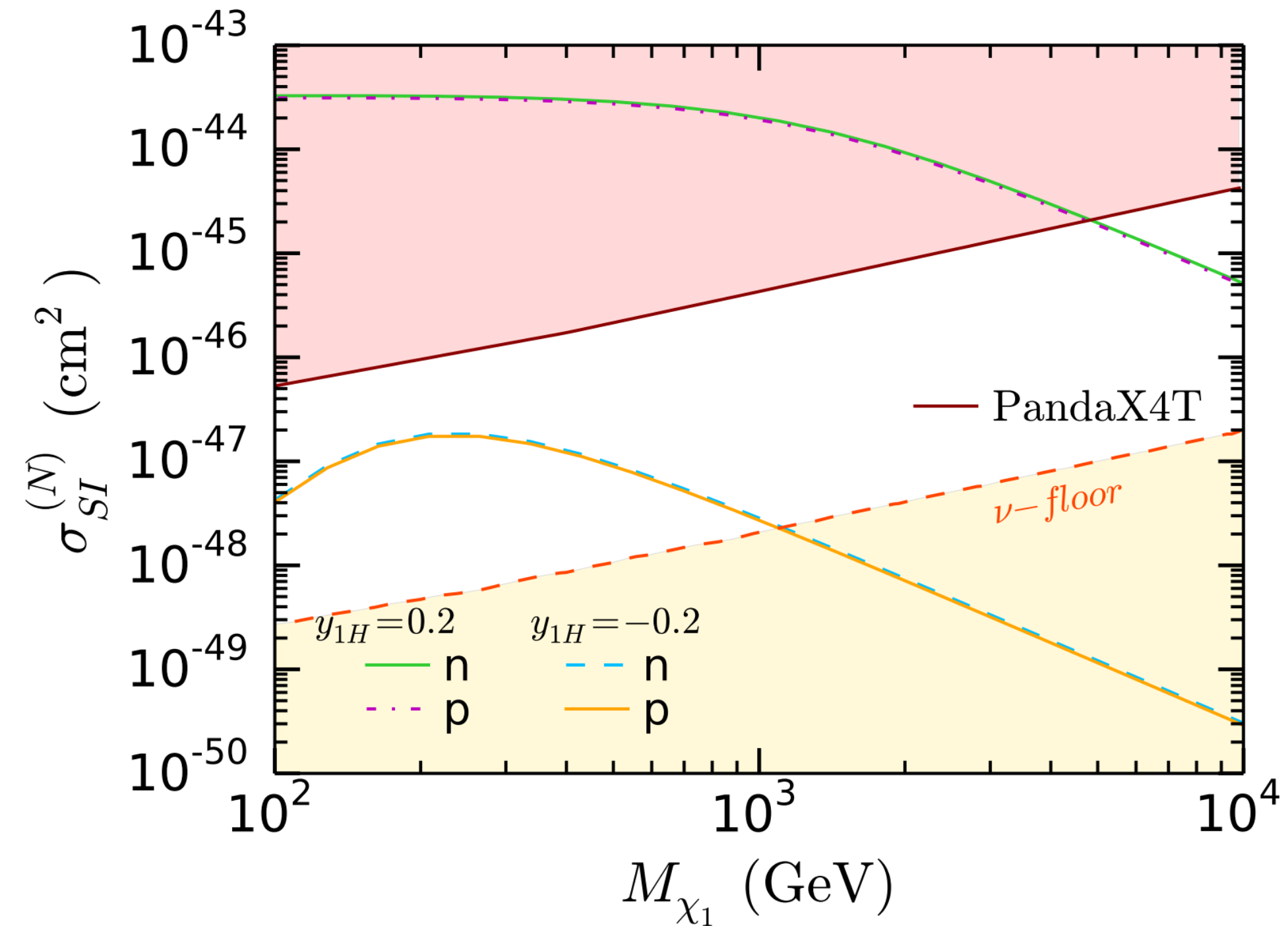
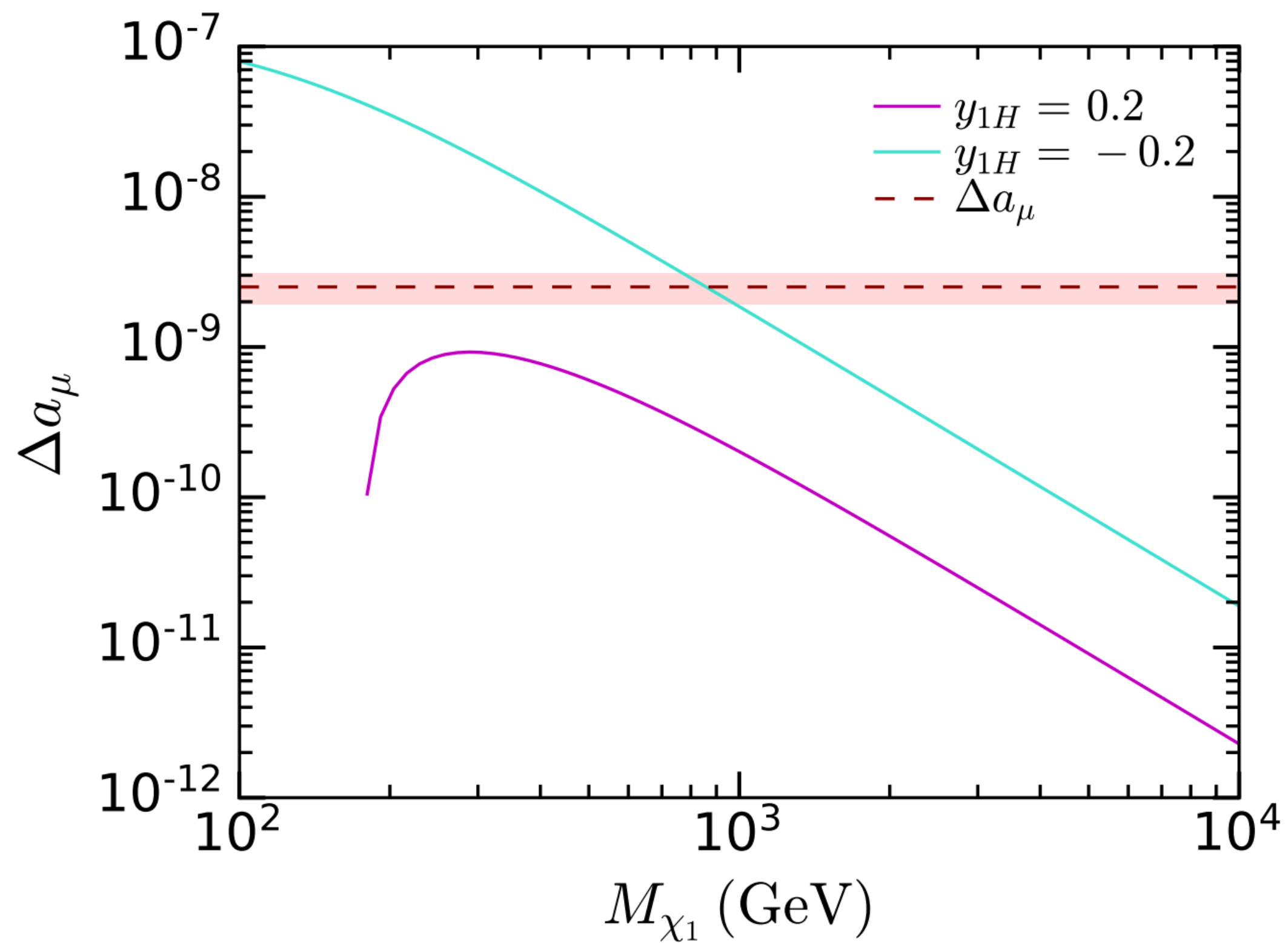


Back up slides



DM models: tree-level coupling

Field	Spin	SU(3) _C	SU(2) _L	U(1) _Y	Z ₂
χ_S	1/2	1	1	0	—
ξ_D	1/2	1	2	-1/2	—
η_D	1/2	1	2	1/2	—
\tilde{L}	0	1	2	-1/2	—



Neutron star

- Neutron star of $M_{\star} = 1.4 M_{\odot}$, And radius of $R_{\star} \sim 12 \text{ km}$
- EOS: APR- EOS (A. Akmal, V.R. Pandharipande, D.G. Ravenhall) *Phys.Rev.C58:1804-1828,1998*
- pion condensation

A lot of uncertainty: Many different Equations of state!

Neutron star cooling: Neutrino emission

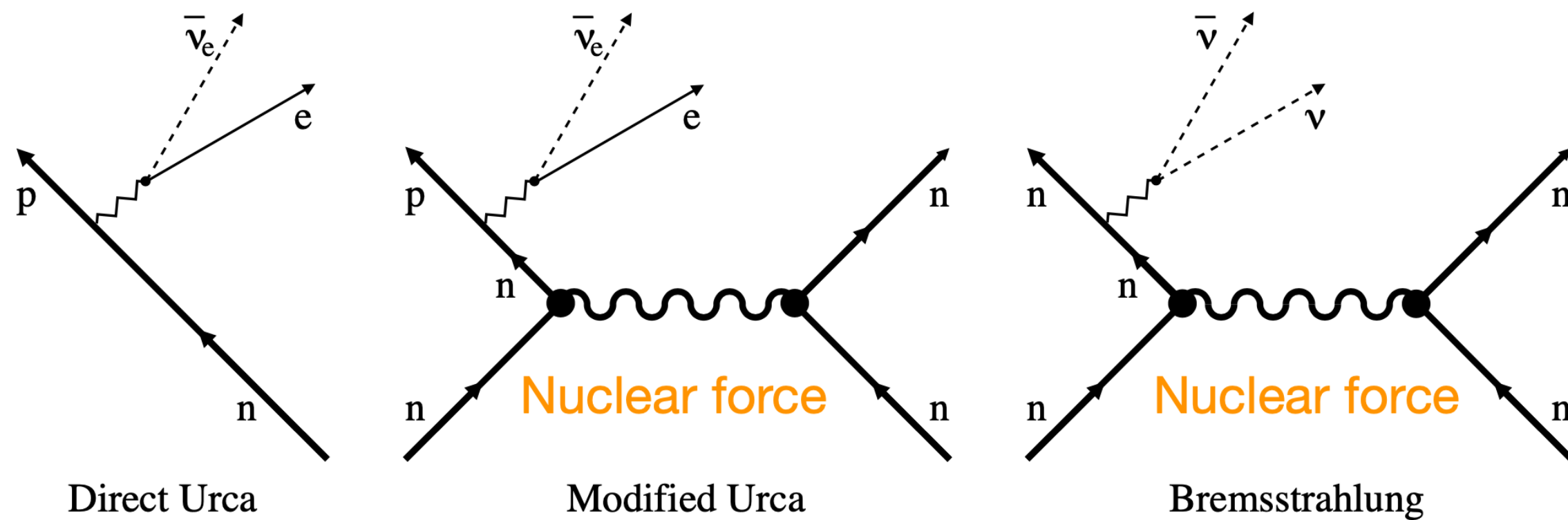


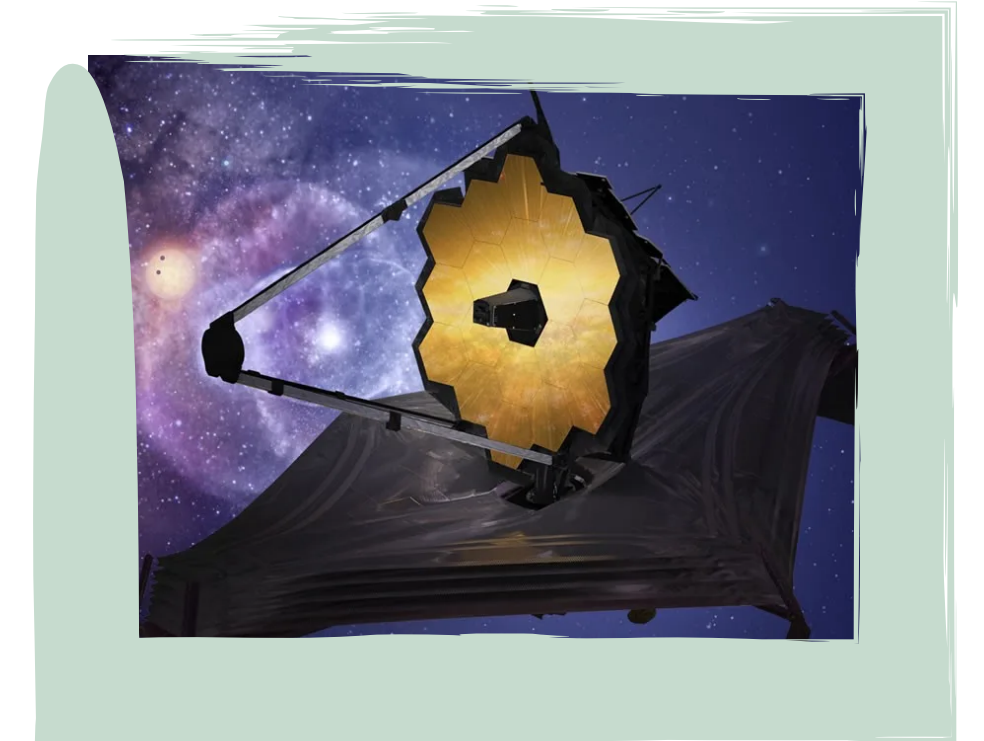
Figure taken from Natsumi Nagata

Yet, a lot to do!

Possible observations

- Sensitivity at **James Webb Space Telescope**. For this we need
 - Exposure time ~ 1 day
 - Distance $\sim 10 \text{ pc}$

Nearest NS is discovered at 100 pc (!)



Future possibilities



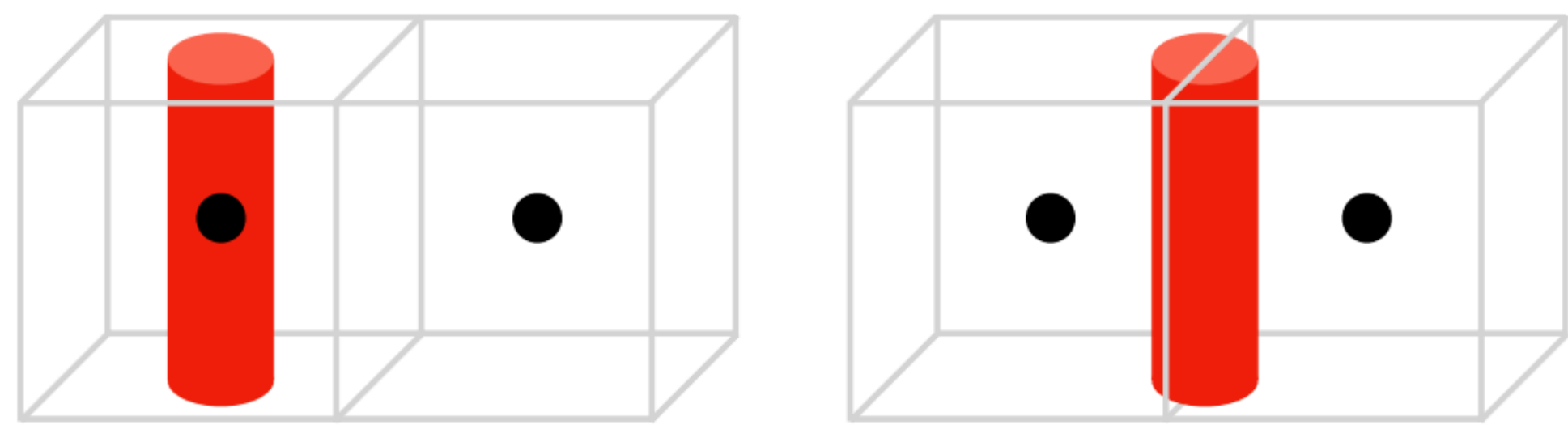
FAST (radio telescope)



Thirty Meter Telescope



Extremely Large Telescope



$E_{\text{pin}} < 0$ Nuclear pinning

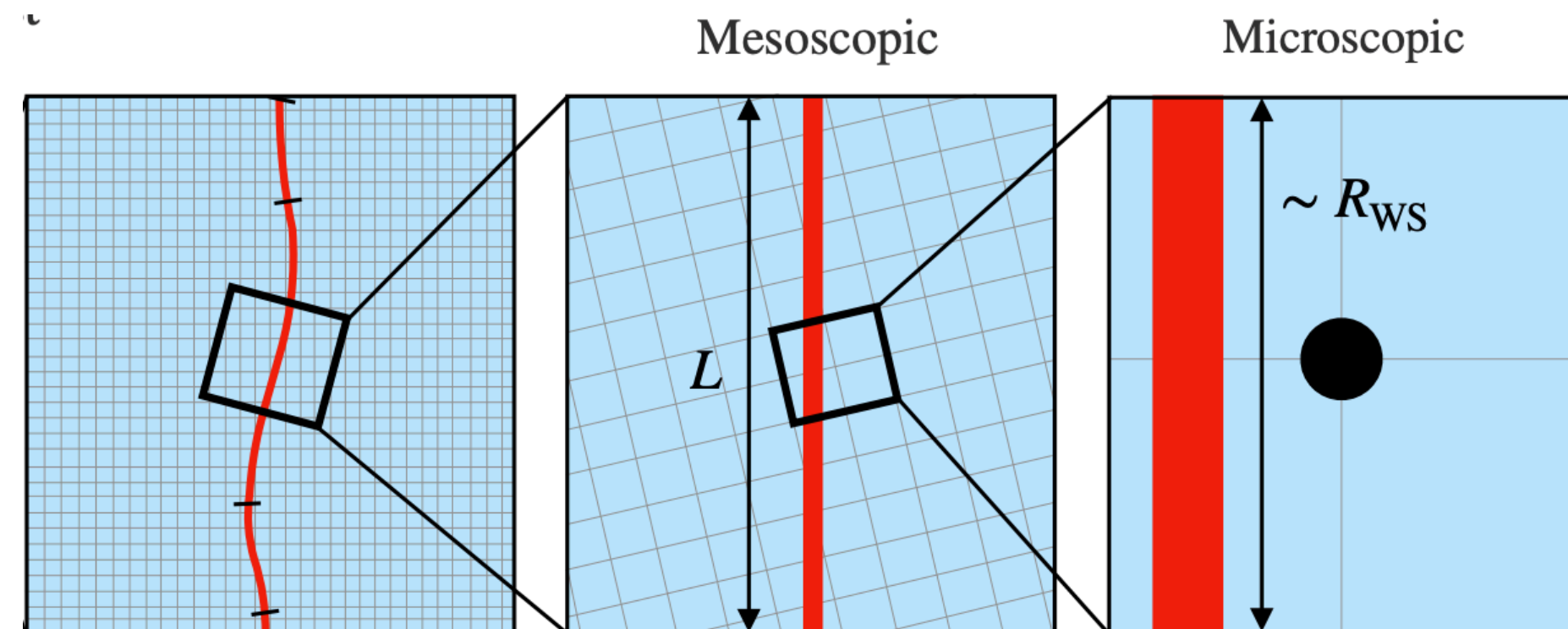
Interstitial pinning $E_{\text{pin}} > 0$

Evaluation of E_{pin}

- Semi-classical approach [Donati, Pizzochero (2004)]
Thomas-Fermi approx. (Interacting fermi gas of nucleons)
[Seveso, Pizzochero, Grill, Haskell (2015)]
- Quantum approach [Avogadro, Barranco, Broglia, Vigezzi (2008)]
[Klausner, et al. [2303.18151]]
Hartree-Fock-Bogoliubov approx

Evaluation of f_{pin}

- Microscopic
Estimation using E_{pin} derived from fm-size box
- Mesoscopic
Average f_{pin} along a mesoscopic length $L \simeq (10^3 - 10^4)$ fm



Theoretical approaches for Vortex creep

Table from Motoko's

		E_{pin} -evaluation	
		Semi-classical	Quantum
f_{pin} -evaluation	Micro.	Donati, et al. (2004)	Avogadro, et al. (2008)
	Meso.	Seveso, et al. (2015)	Klausner, et al [2303.18151]

$$J_{\text{pin}} \simeq \int_{R_{\text{in}}}^{R_{\text{out}}} dR d\theta d\phi R^3 \sin^2 \theta \cdot \frac{f_{\text{pin}}}{\kappa}$$

$$f_{\text{pin}}|_{\text{NP}} \simeq \frac{|E_{\text{pin}}|}{\Delta r \Delta L}$$