

# Jet substructure on the Lund plane

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Workshop on medical and high energy physics

@ Sonora, Mexico

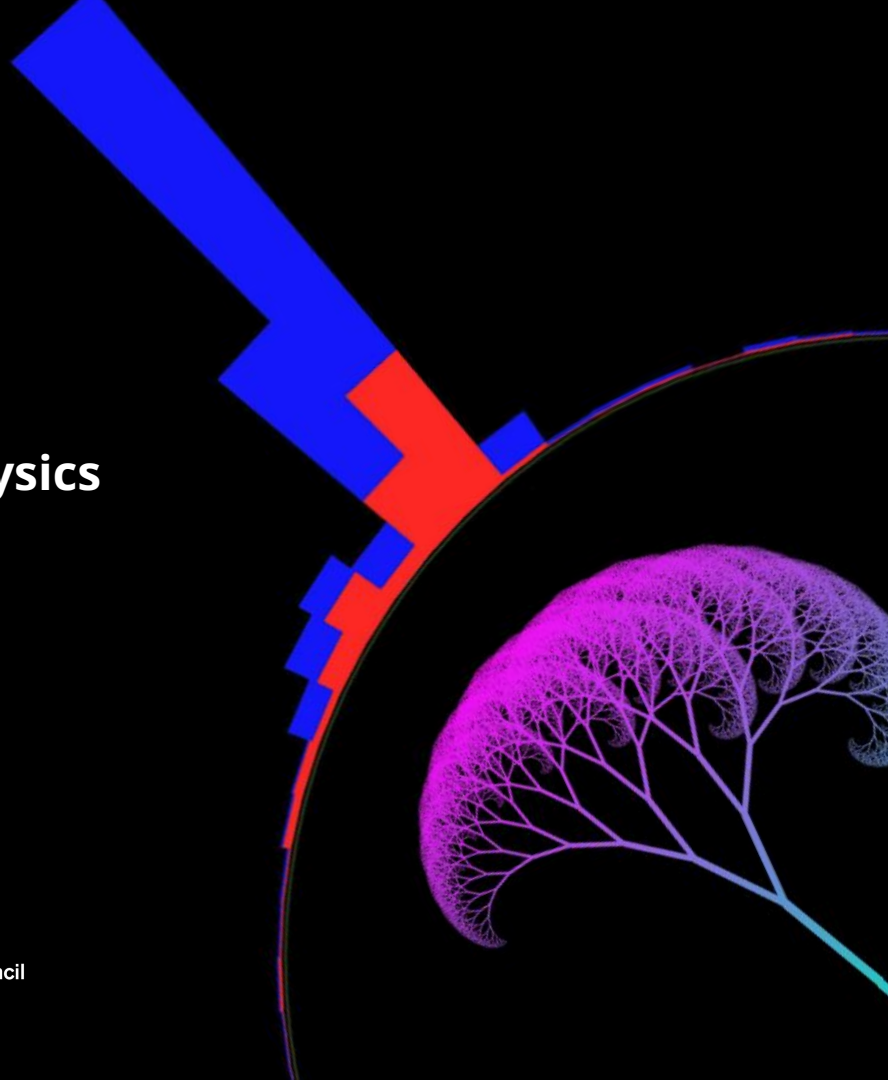
May 21<sup>st</sup>-24<sup>th</sup>



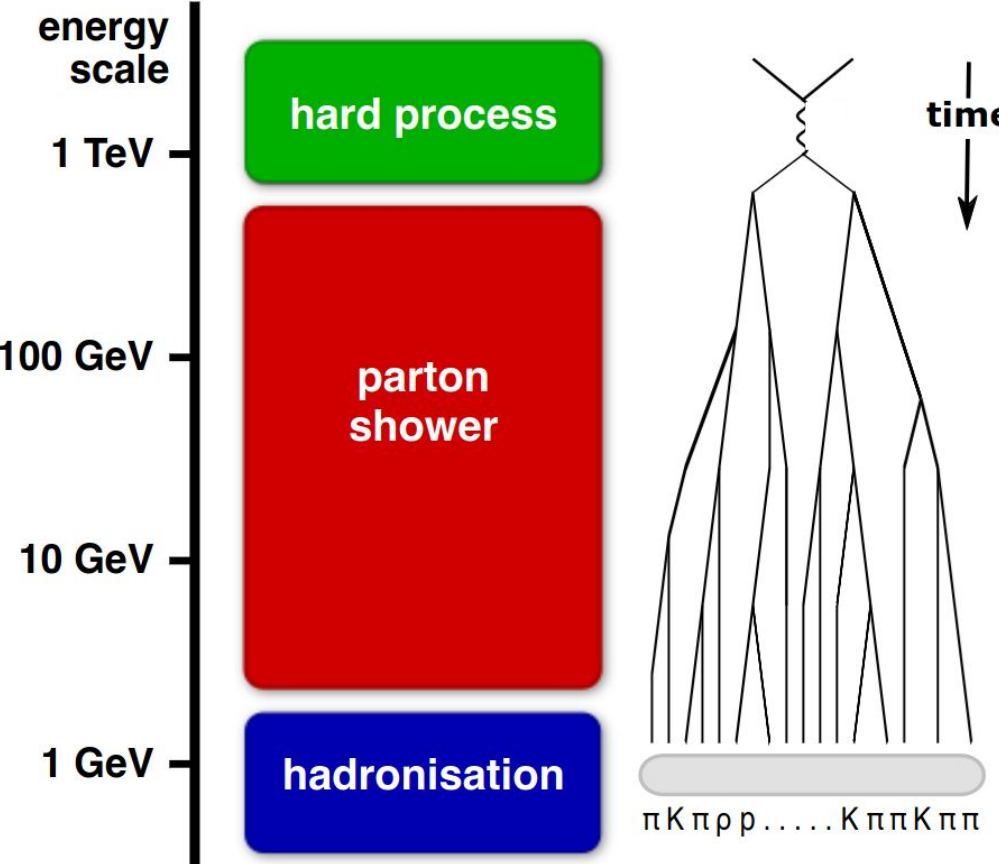
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UNIVERSITÀ DI ROMA



European Research Council



# Jet formation is a multiscale probe of QCD evolution



From  $Q \sim 1 \text{ TeV}$  to  $\Lambda_{\text{QCD}} \sim 200 \text{ MeV}$

Depending on observable & jet  $p_T$  and  $R$ : sensitivity to parton shower, hadronization, underlying event, color reconnection, ...

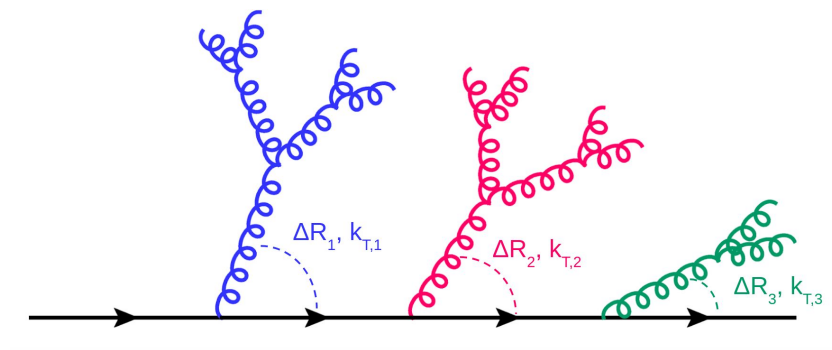
Higher jet  $p_T \Rightarrow$  "longer" parton cascade

*Results on jet fragmentation functions covered by **Ezra Lesser** next*

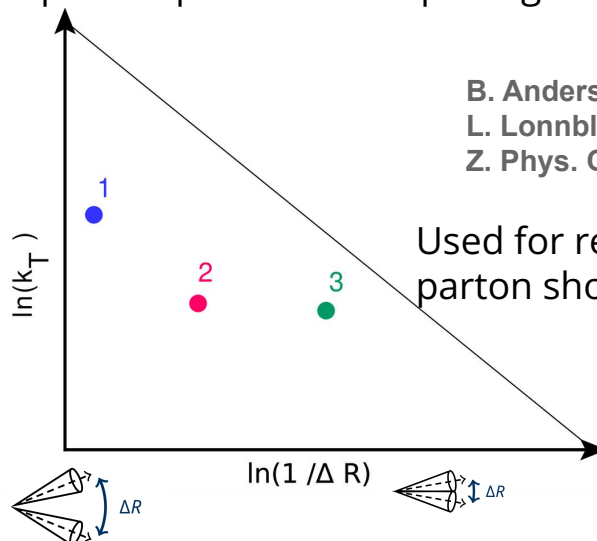
*G. Salam's sketch*

# Phase-space of QCD branchings in the Lund plane

Lund planes (or diagrams) are a 2D representation of the phase-space of  $1 \rightarrow 2$  splittings:



$k_T$ : relative transverse momentum of emission  
 $\Delta R$ : angular opening of emission and core



B. Andersson, G. Gustafson,  
 L. Lonnblad, and U. Pettersson,  
 Z. Phys. C43 (1989) 625

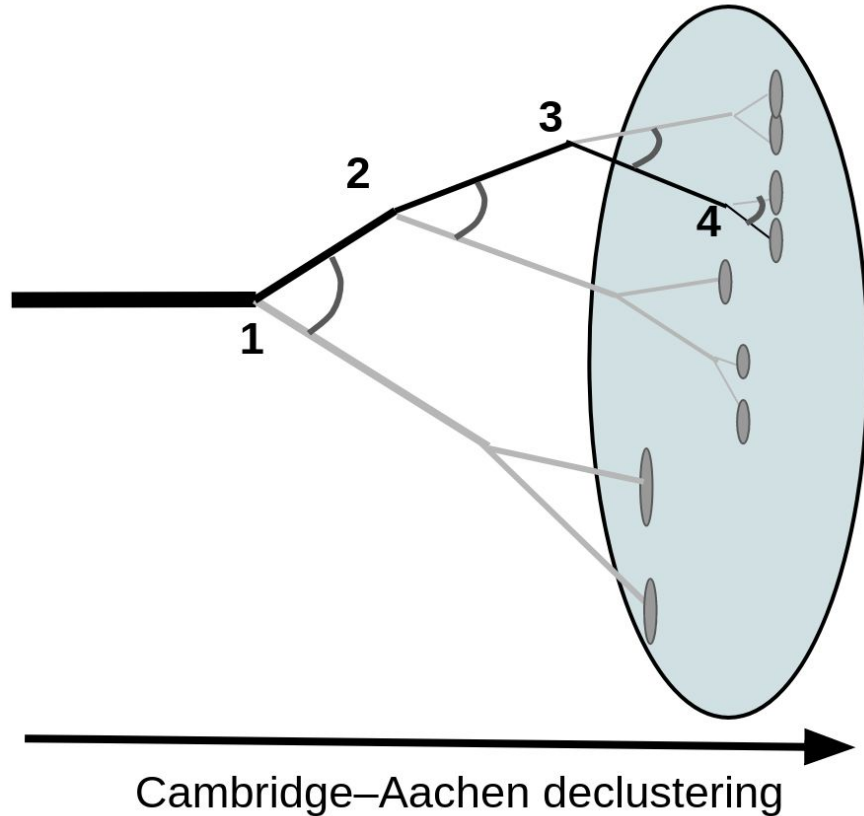
Used for resummation and  
 parton shower development

In soft & collinear limit of QCD, emissions fill the Lund plane uniformly

$$\mathcal{P} \propto \alpha_s \frac{dk_T}{k_T} \frac{d\Delta R}{\Delta R} = \alpha_s d \ln(k_T) d \ln(\Delta R) \leftarrow \text{approximate self-similarity of QCD}$$

# Constructing the primary Lund jet plane (LJP)

F. Dreyer, G. Salam, G. Soyez, JHEP12(2018)064



1. Jet is reclustered with Cambridge–Aachen algorithm (pairwise clustering with angular ordering)
2. Follow clustering tree in reverse (large  $\rightarrow$  small angles), **along the hardest branch**
3. Register kinematics of branching at each step

$$\Delta R = \sqrt{(y^{\text{softer}} - y^{\text{harder}})^2 + (\phi^{\text{softer}} - \phi^{\text{harder}})^2}$$

$$k_T = p_T^{\text{softer}} \Delta R \quad \text{CMS}$$

$$z = p_T^{\text{softer}} / (p_T^{\text{harder}} + p_T^{\text{softer}})$$

Measured by ATLAS, CMS, [ALICE](#) (low  $p_T \sim 20$  GeV)

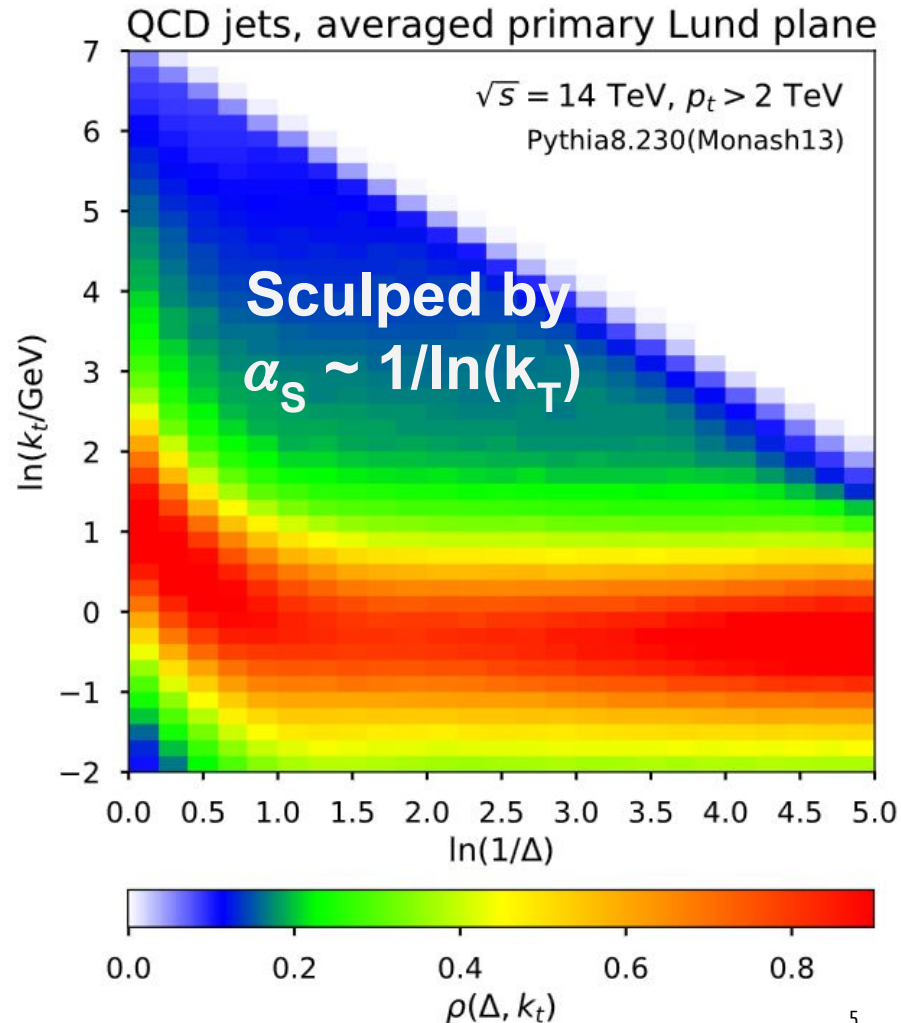
Define a *jet-averaged* number of emissions, the “primary” Lund jet plane density

$$\rho(k_T, \Delta R) \equiv \frac{1}{N_{\text{jets}}} \frac{d^2 N_{\text{emissions}}}{d \ln(k_T/\text{GeV}) d \ln(R/\Delta R)}$$

At leading order, it’s “sculpted” by  $\alpha_S(k_T)$

$$\rho(k_T, \Delta R)_{\text{LO}} \approx \frac{2}{\pi} C_R^{\text{eff}} \alpha_S(k_T)$$

With  $C_R = C_A = 3$  for  $g \rightarrow gg$  or  $C_F = 4/3$  for  $q \rightarrow qg$

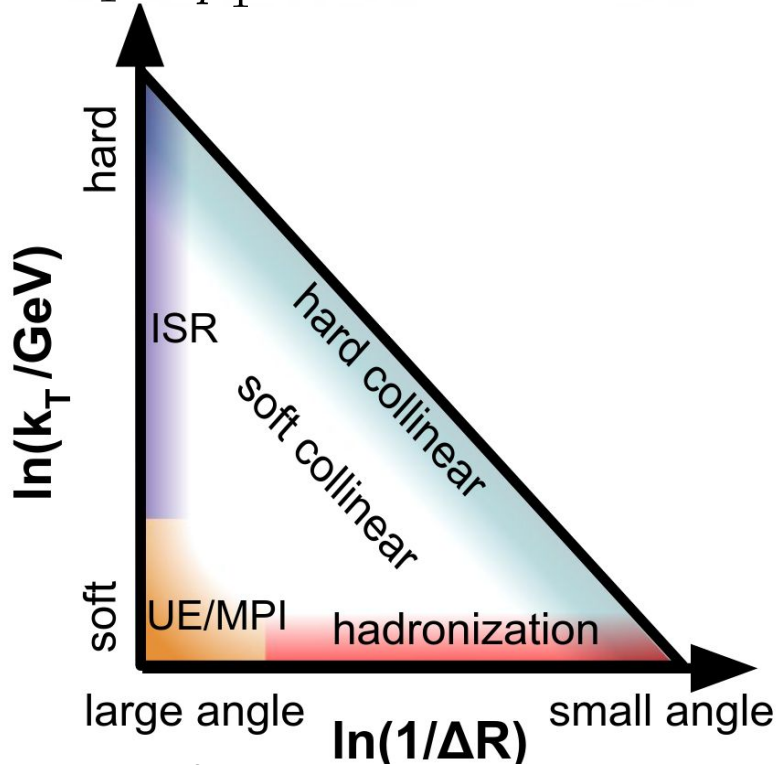


# Mechanisms “factorize” in the Lund jet plane

*F. Dreyer, G. Salam, G. Soyez,  
JHEP12(2018)064*

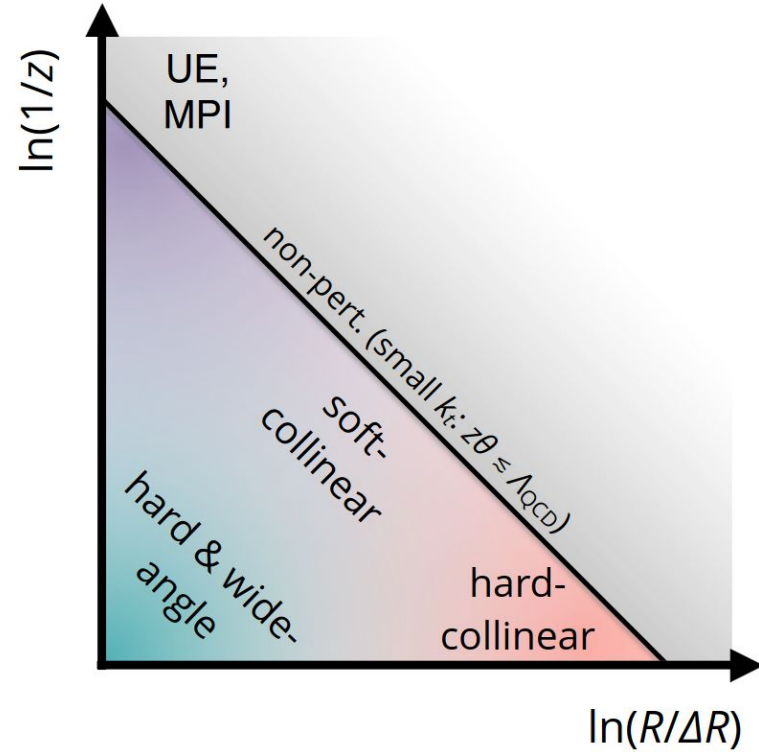
## CMS Lund plane coordinates

$$k_T = p_T^{\text{softer}} \Delta R \quad \text{vs} \quad \Delta R$$



## ATLAS Lund plane coordinates

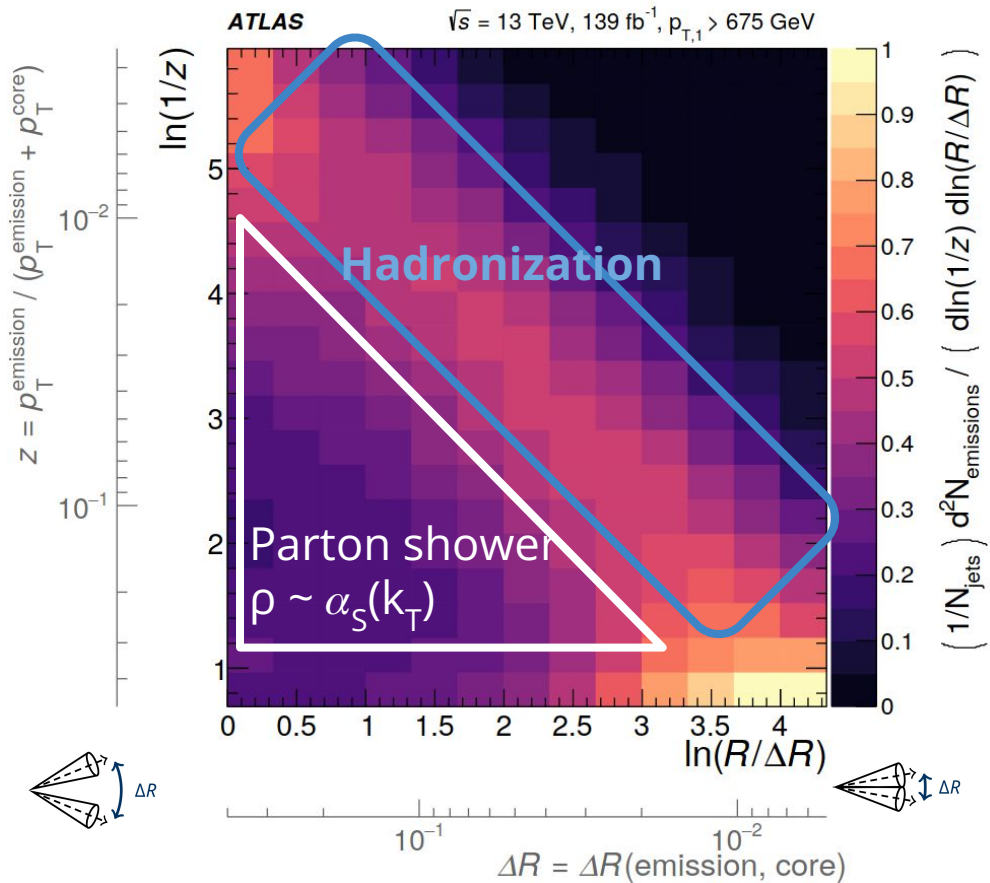
$$z = p_T^{\text{softer}} / (p_T^{\text{harder}} + p_T^{\text{softer}}) \quad \text{vs} \quad \Delta R$$



# ATLAS primary Lund jet plane density

*R=0.4 jets (standard R in Run-2)*

[PRL 124, 222002 \(2020\)](#)



Dijet selection,

$$p_{T, \text{jet}1} > 675 \text{ GeV} \ \& \ p_{T, \text{jet}2} > \frac{2}{3} p_{T, \text{jet}1}$$

Charged-particle tracks for substructure

Momentum fraction of the emissions for vertical axis of Lund plane:

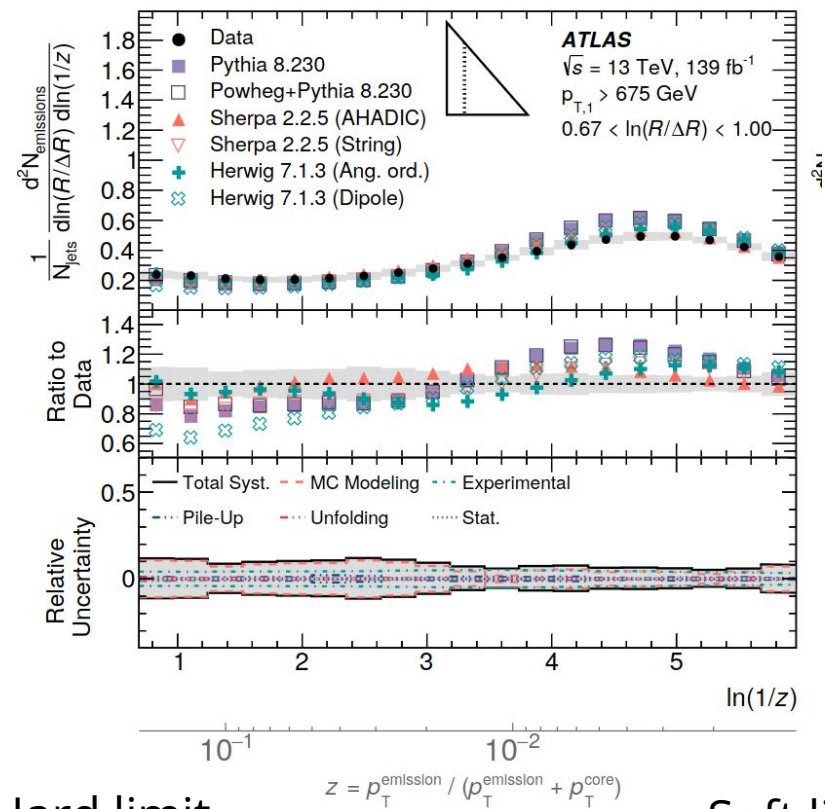
$$z = p_{T, \text{softer}} / (p_{T, \text{softer}} + p_{T, \text{harder}})$$

**Multidimensional unfolding**

# Factorization properties in action (ATLAS)

## Fixed-angle slice

[PRL 124, 222002 \(2020\)](#)



Hard limit  
(high  $z$ )

Soft limit  
(small  $z$ )

Variation of hadronization model,  
same parton shower  
(**Sherpa2 string vs hadronization**)

Variation of parton shower,  
same hadronization model  
(**Herwig7.1 angle vs dipole**)

Variation of matrix element  
(**Pythia8 vs Powheg+Pythia8**)

Best global description by  
**Herwig7.1 angle-ordered**

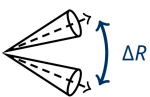
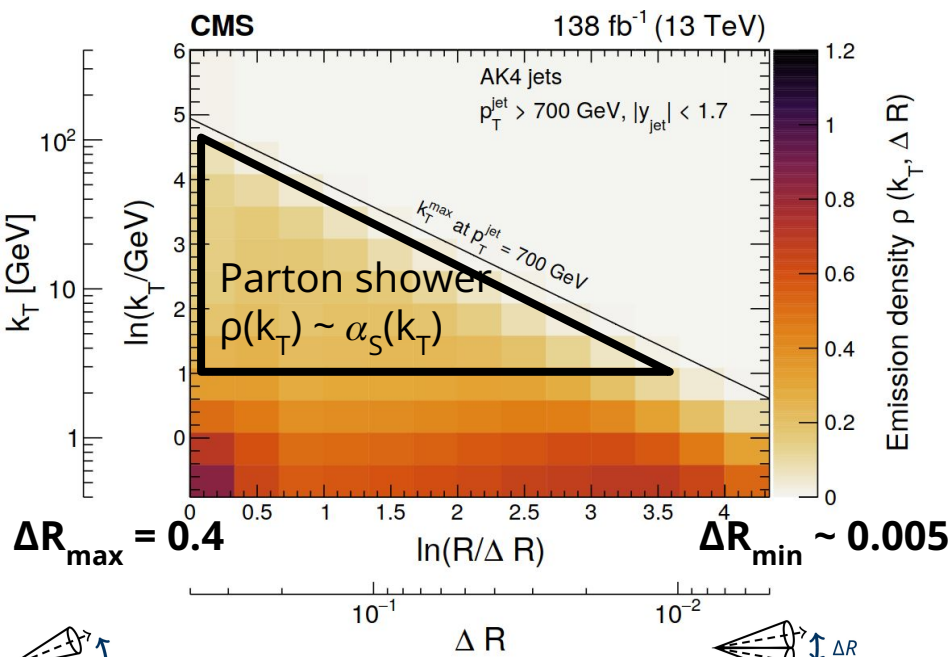


# CMS primary Lund jet plane densities

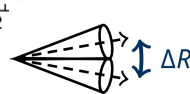
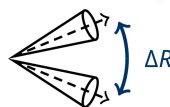
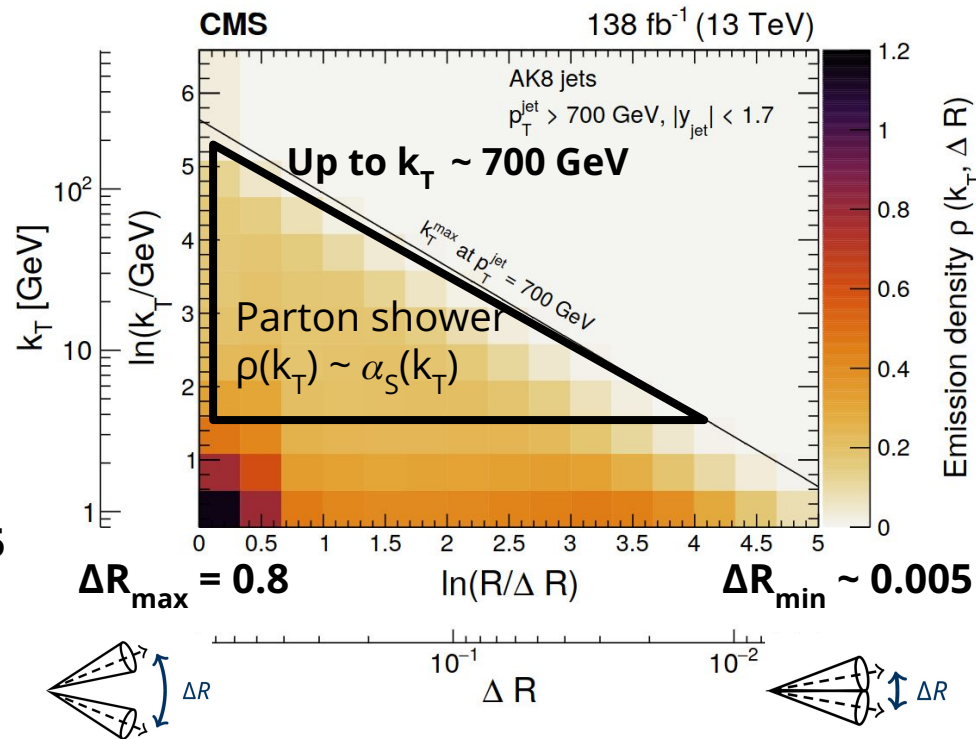
arXiv:2312.16343, accepted by JHEP

$p_T^{\text{jet}} > 700$  GeV,  
charged particles for substructure

*R=0.4 (standard R in Run-2)*



*R=0.8 (large-angle & harder emissions)*

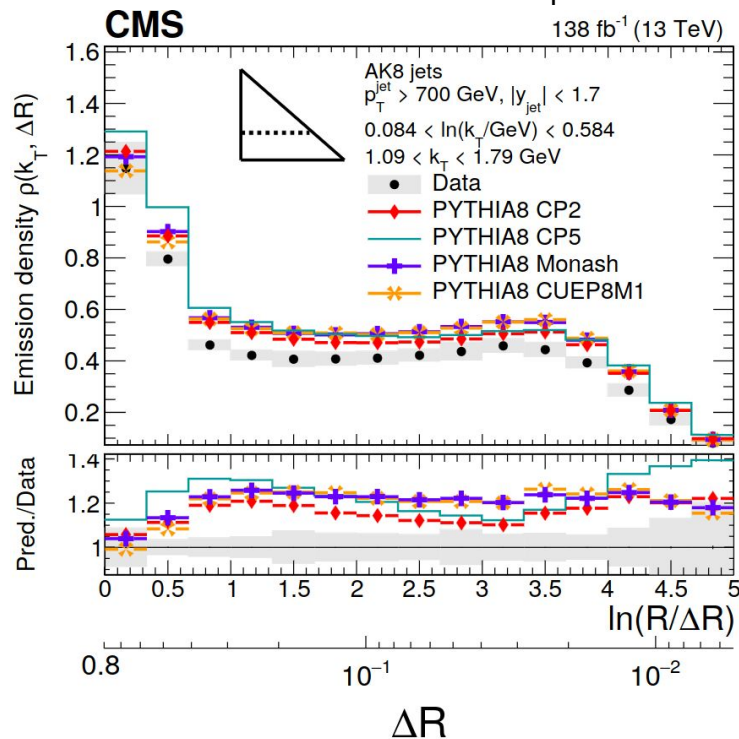


**Multidimensional unfolding**

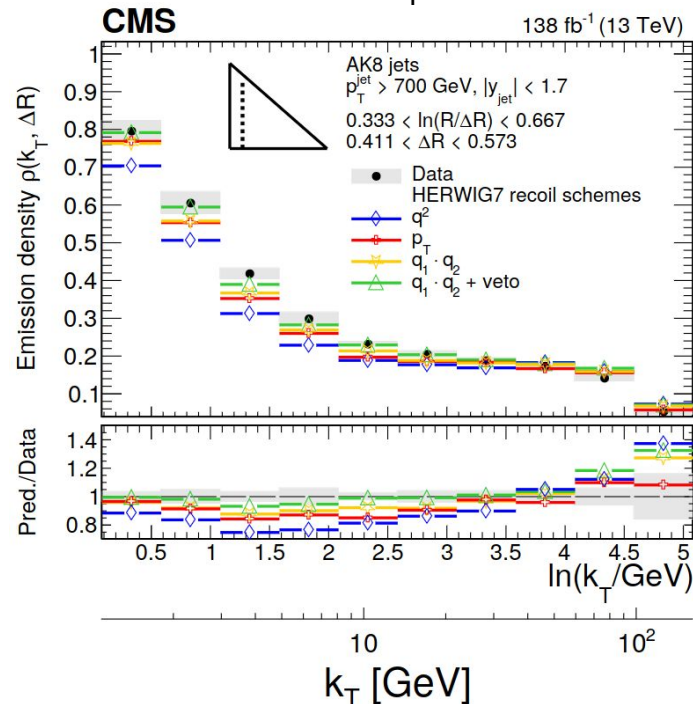
Emission density is flat for hard & collinear emissions due to  $\alpha_S(k_T) \sim 1/\ln(k_T)$

# CMS Lund plane slices

Hadronization region ( $k_T \sim 1$  GeV)



Large-angles ( $k_T = 1 - 200$  GeV)



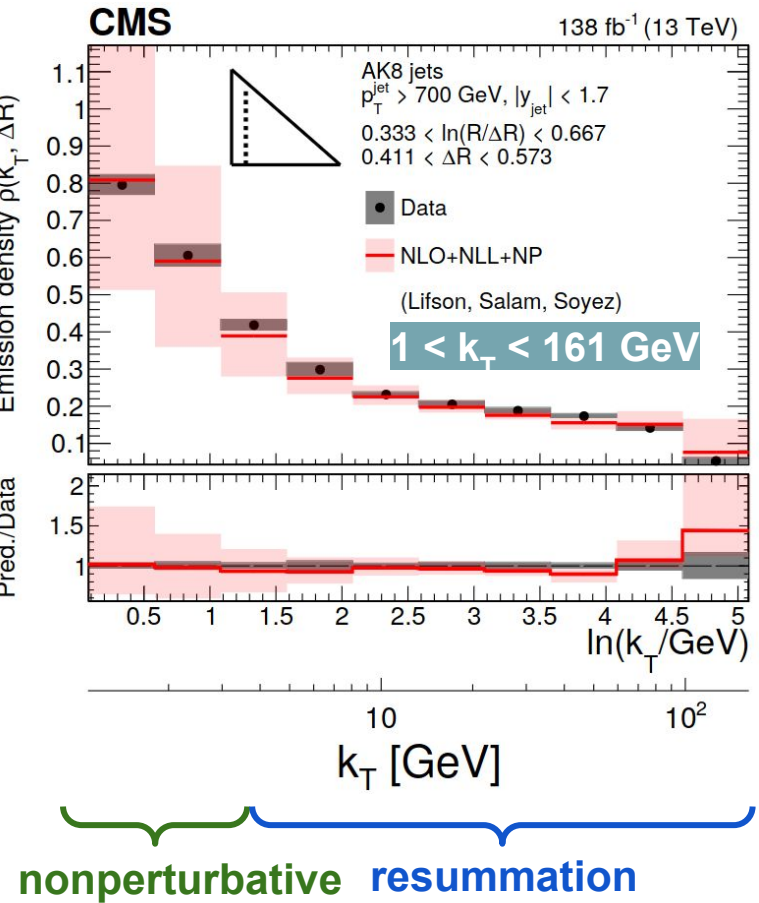
Sensitivity to parton shower recoil scheme (**Herwig7**)

Better description by  
 Herwig7 angle-ordered with  $q_1, q_2 + \text{veto}$

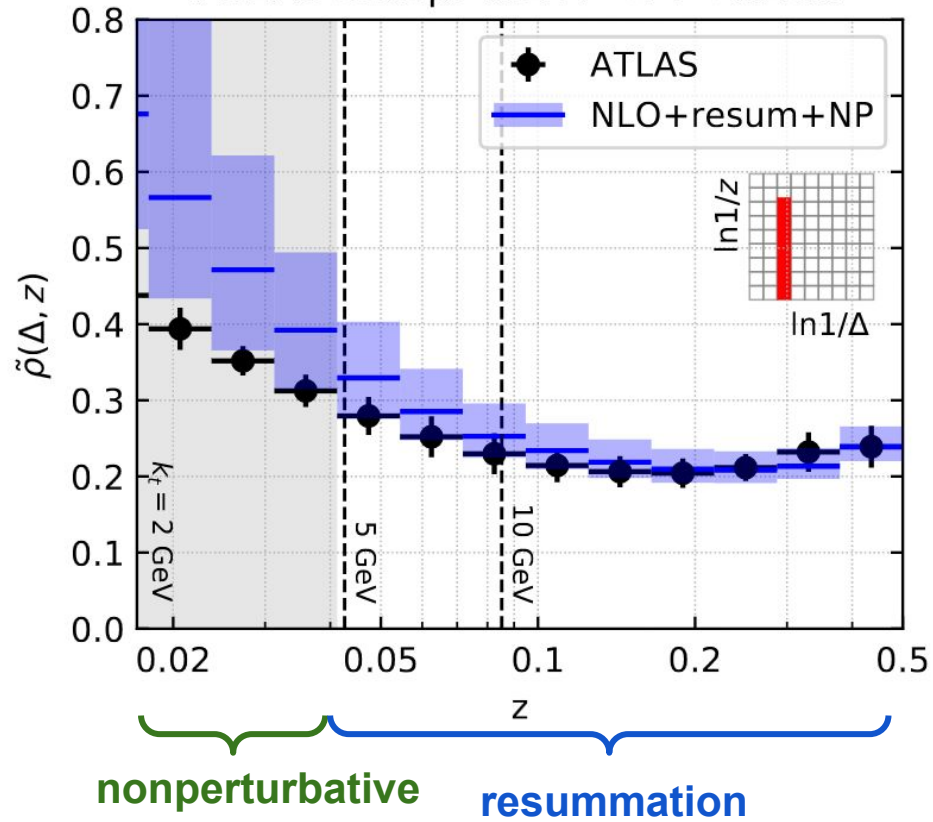
**PYTHIA8** overshoots data by 15-20%  
 in hadronization region

# Described well by pQCD calculations (NLO+NLL+NP)

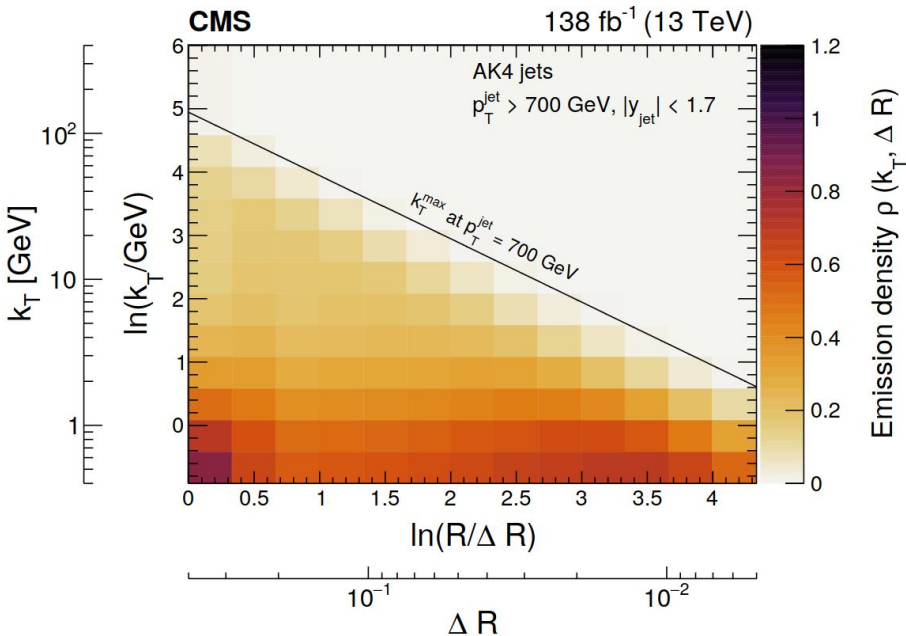
Calculations from A. Lifson, G. Salam, G. Soyez [JHEP10\(2020\)170](https://arxiv.org/abs/1909.01567)



ATLAS setup:  $0.147 < \Delta < 0.205$



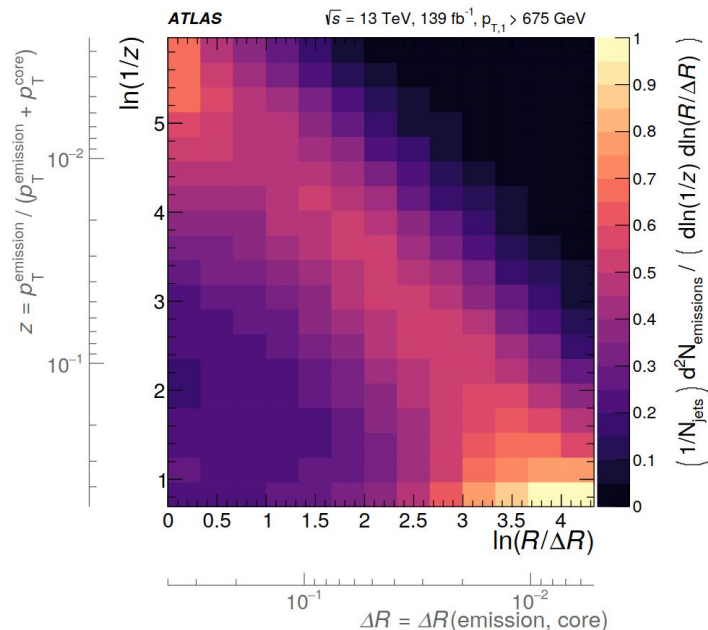
# Complementarity of ATLAS & CMS representations



$k_T$ : hard-scale of  $1 \rightarrow 2$  branching

Shower & hadronization regions separated via “horizontal” cuts

More sensitive to detector smearing effects



$z$ : “core” and “emission”  $p_T$ -balance

More resilient to smearing effects (cancels in  $z$  ratio)

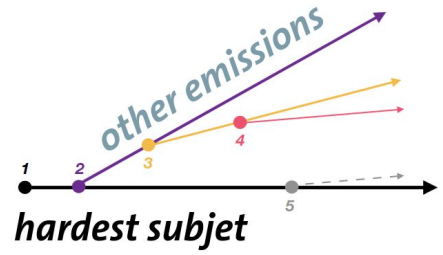
Hard-scale is “fuzzier” ( $k_T = z p_T^{\text{mother}} \Delta R$ )

# ATLAS Lund subjet multiplicities

Proposed by [R. Medves, A. Soto-Ontoso, G. Soyez, JHEP04\(2023\)104](#)

[arXiv:2402.13052](#),  
submitted to *PLB*

Count emissions with  $k_T > k_{T,cut}$ .  
Using the **full** Lund jet tree ( $N_{Lund}$ )  
or for primary Lund emissions ( $N_{Lund}^{primary}$ )

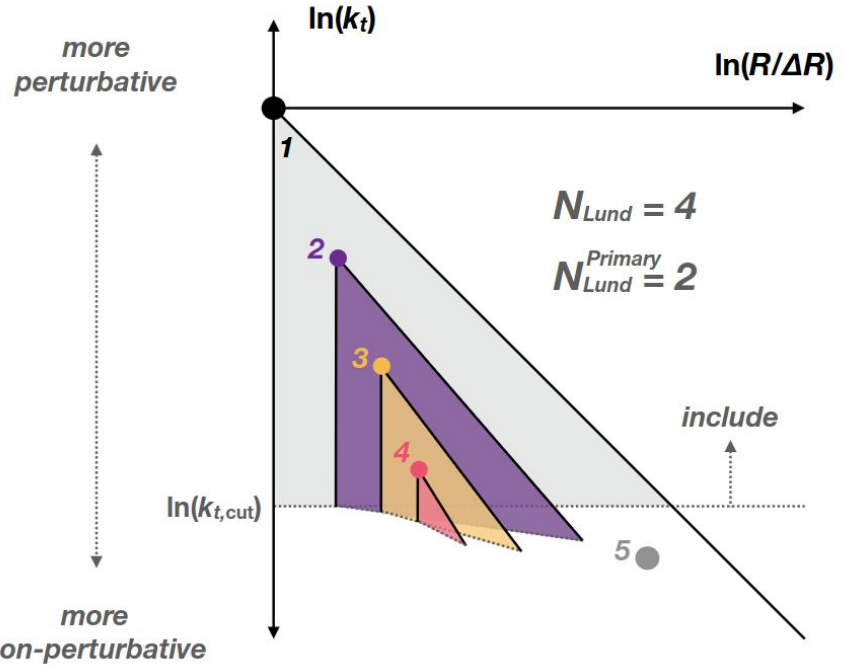


**More inclusive observable**, closely related to (sub)jet multiplicities at LEP

**Charged-particles for substructure**, data-based rescaling for an effective full-particle  $k_T$

$$k_{T,eff} = k_{T,ch} * \left( \frac{p_{T,jet}}{p_{T,jet}} \right)$$

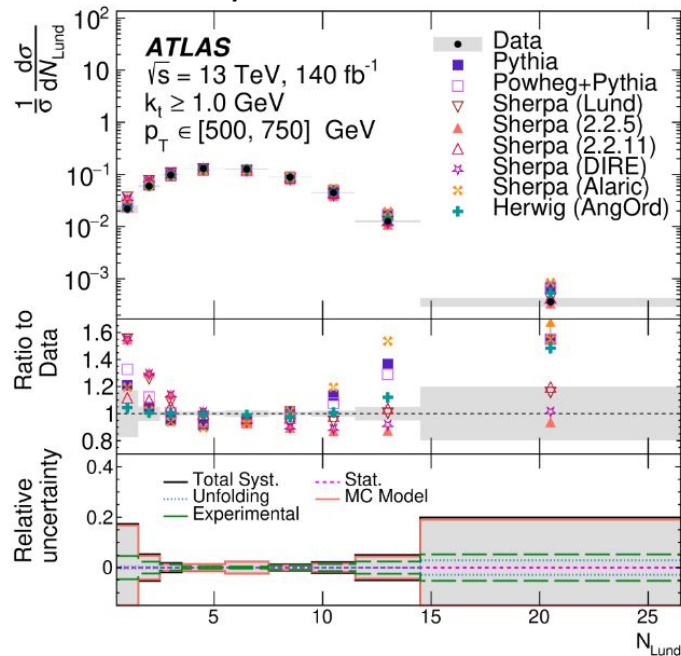
**charged-to-full rescaling factor**



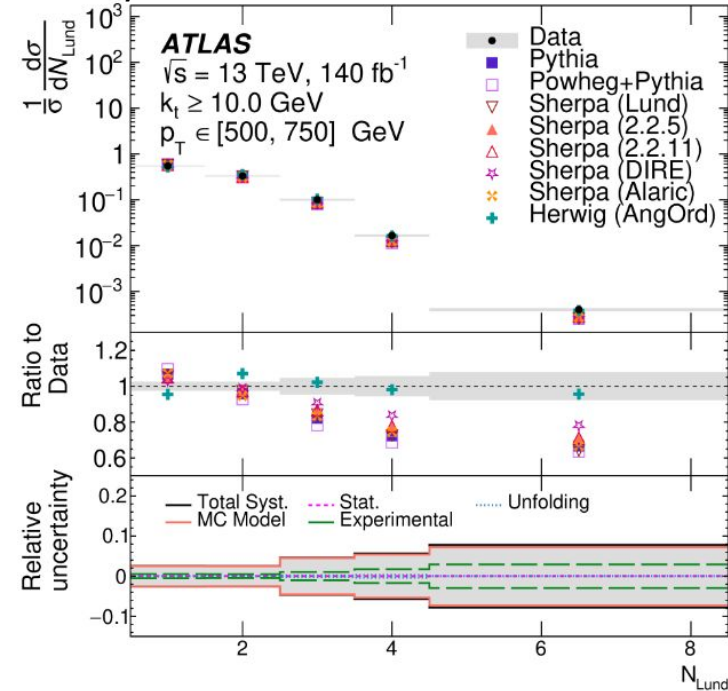
# Lund subjet multiplicity distributions

Unfolded to the particle level, correcting jet  $p_T$  & subjet multiplicity for a given  $k_{T,cut}$

$k_{T,cut} = 1 \text{ GeV (soft)}$



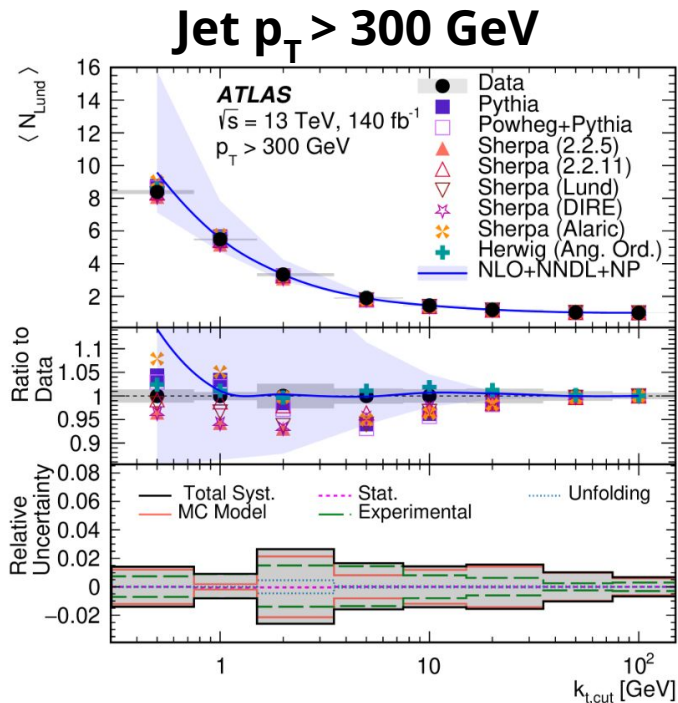
$k_{T,cut} = 10 \text{ GeV (hard)}$



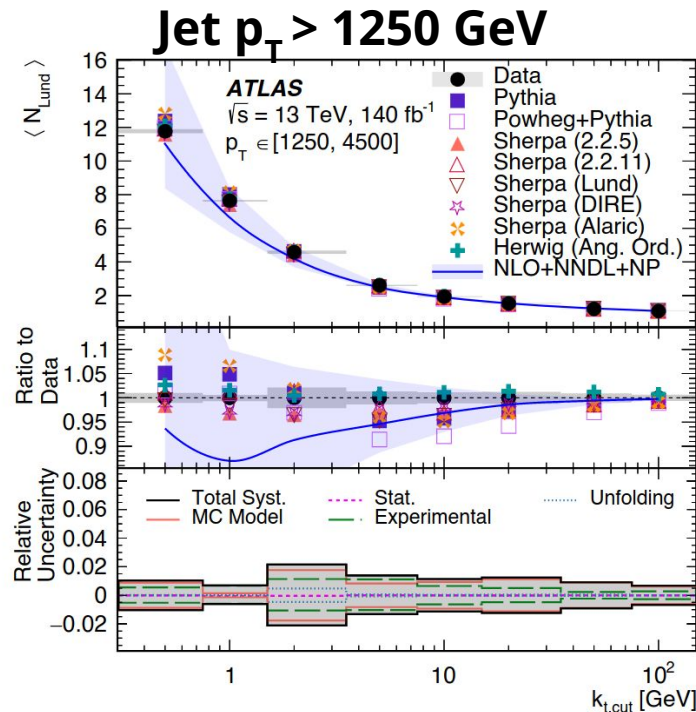
Challenging to describe high- $N_{Lund}$  tails

**Sherpa2** describes the  $k_{T,cut} = 1 \text{ GeV}$  category better. Better global description by **Herwig7** angle-ordered

# averaged Lund subjet multiplicities vs $k_{T, \text{cut}}$



In good agreement with pQCD calculation (NLO+NNDL+NP), high-order resummation

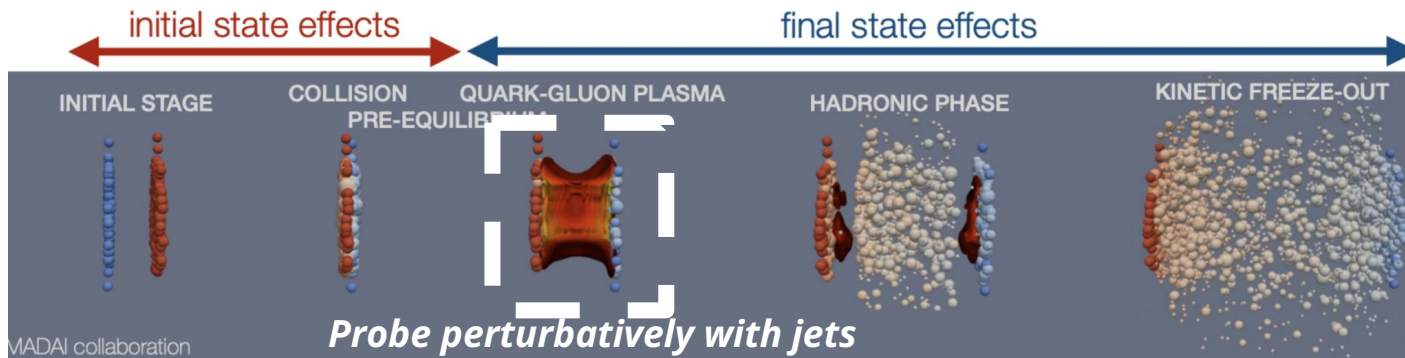


Better description by **Herwig7 angle-ordered**

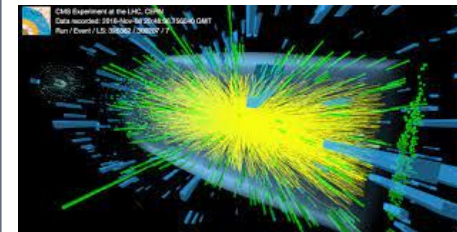
$$\langle N^{(\text{Lund})}(\alpha_s; L) \rangle = \left[ \underbrace{h_1(\alpha_s L^2)}_{\text{DL}} + \underbrace{\sqrt{\alpha_s} h_2(\alpha_s L^2)}_{\text{NDL}} + \underbrace{\alpha_s h_3(\alpha_s L^2)}_{\text{NNDL}} + \dots \right]$$

Other MCs tend to **undershoot** 15

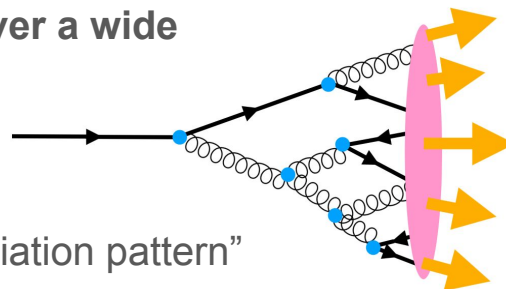
# Probing QCD at high densities & high temperatures



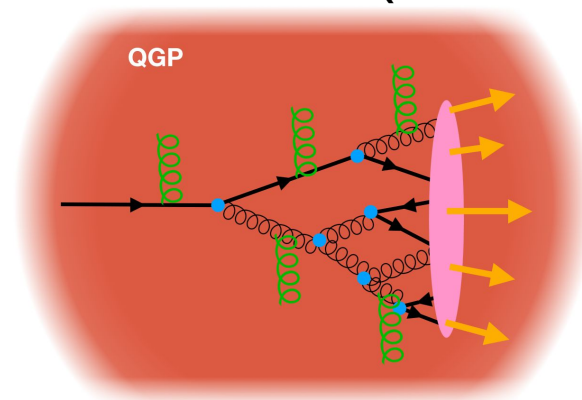
What we see



pp ("vacuum")



PbPb (in medium)



Jets are used to probe the medium over a wide range of momentum scales

Jet quenching == "modification of jet radiation pattern"

sketches from Rey Cruz



# Spacetime picture of quark-gluon plasma evolution

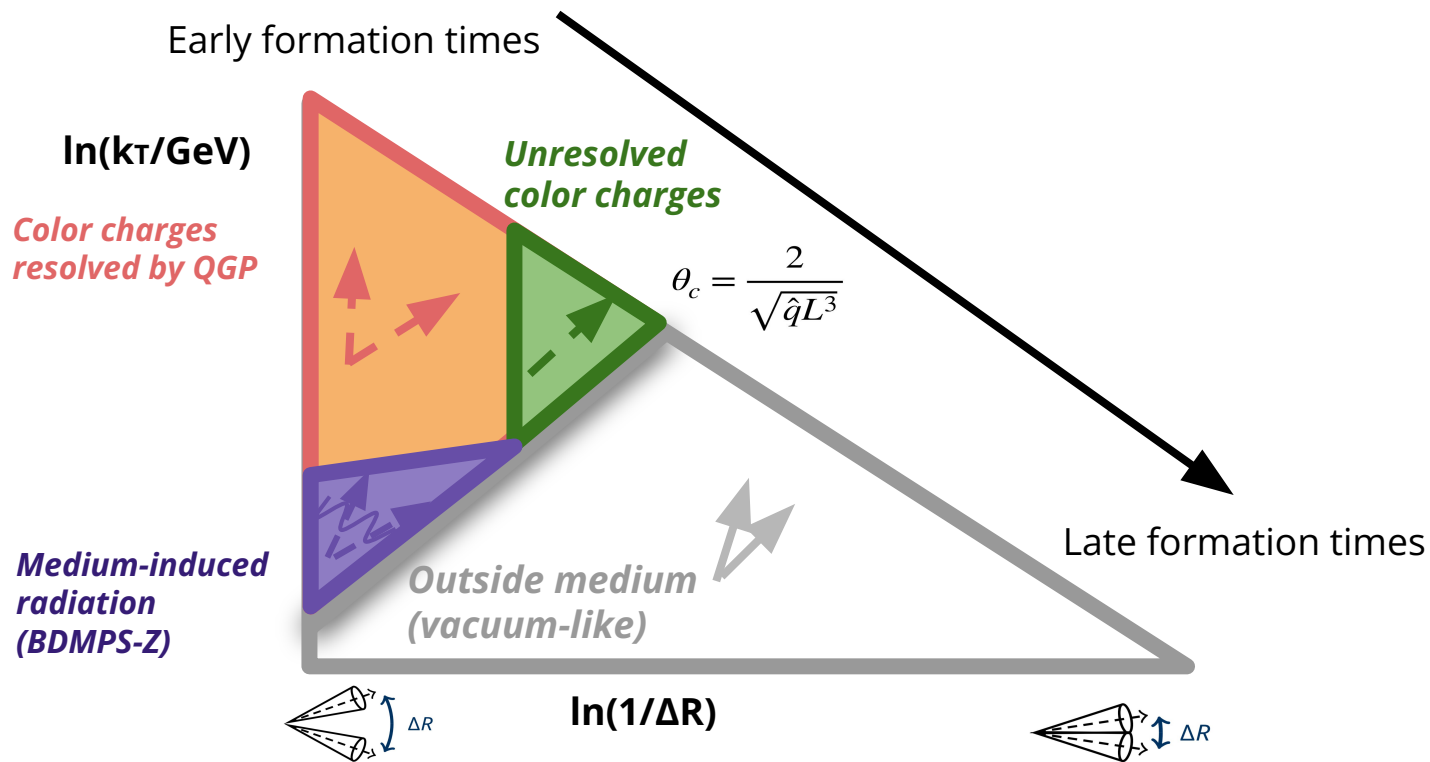


diagram inspired on regions from [P. Caucal, A. Soto, A. Takacs, PRD 105, 114046 \(2022\)](#)

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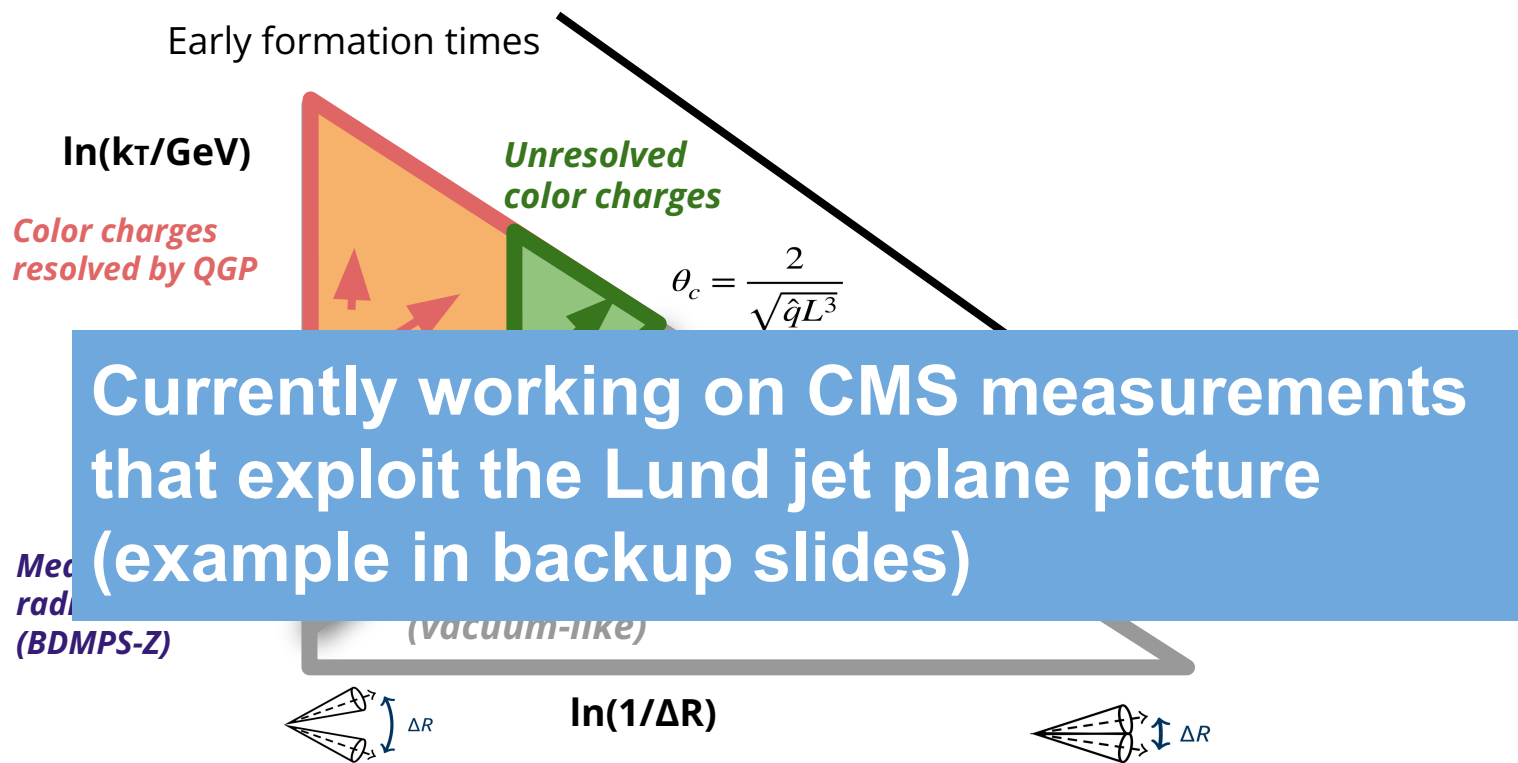
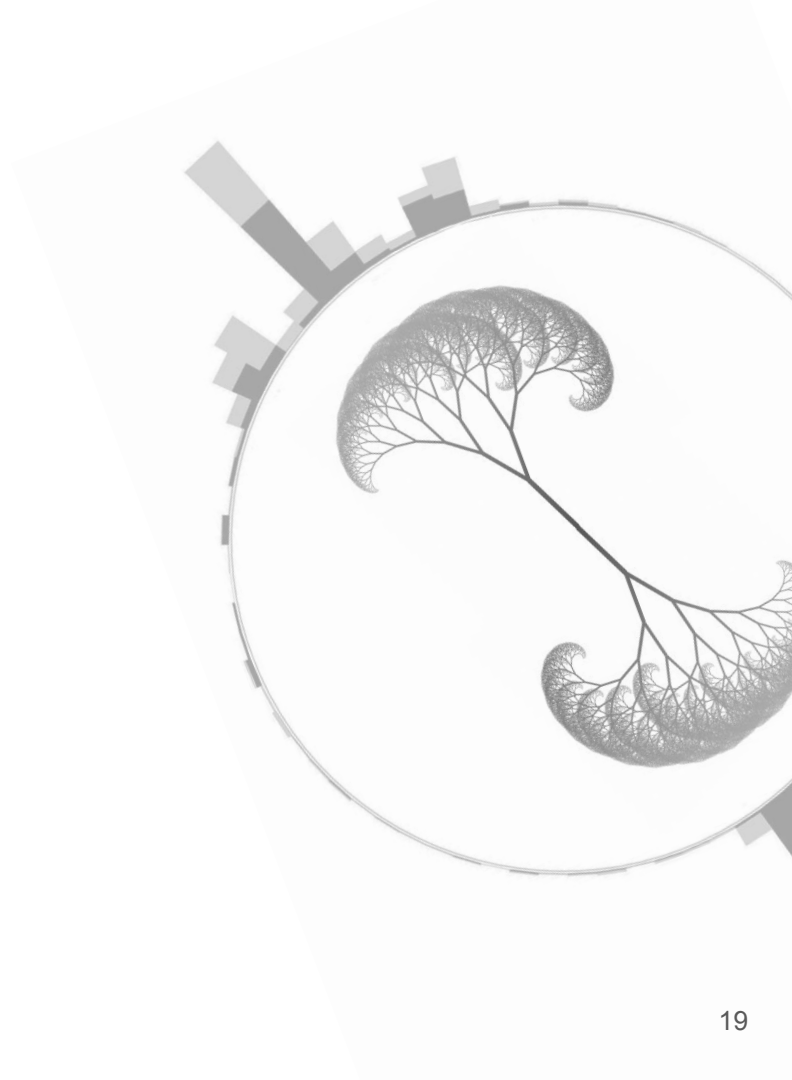


diagram inspired on regions from [P. Caucal, A. Soto, A. Takacs, PRD 105, 114046 \(2022\)](#)

# Summary

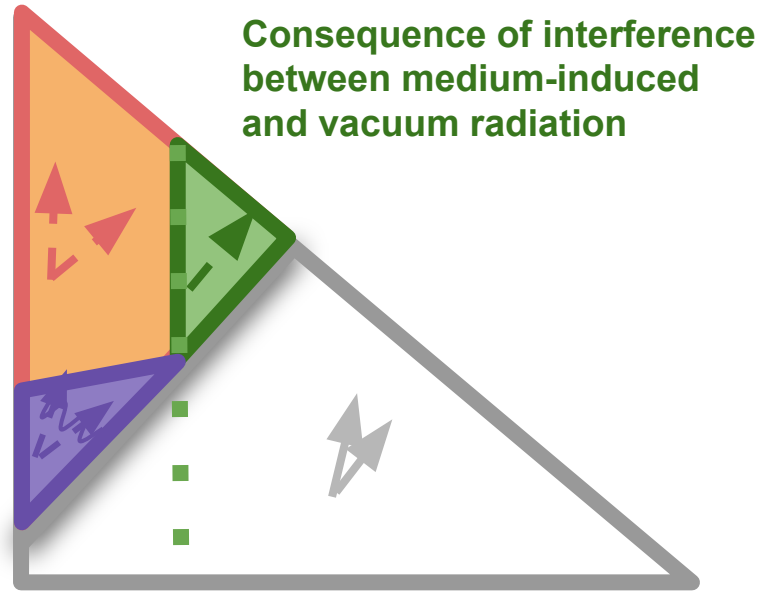
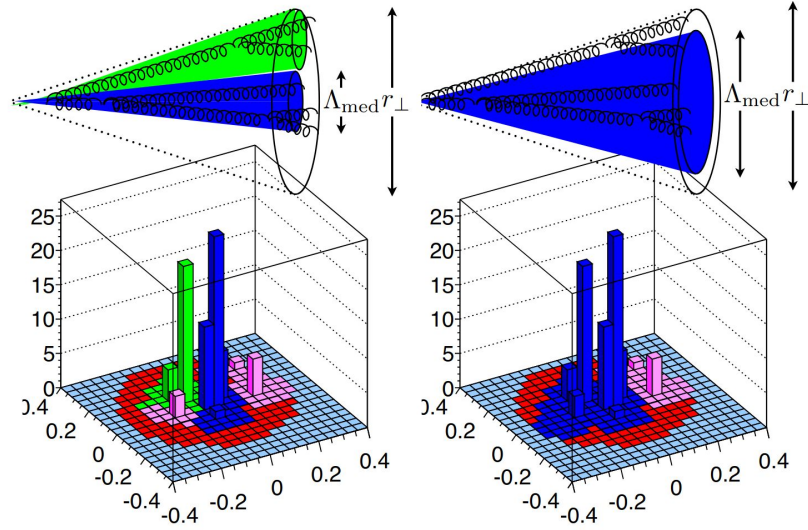
- Mapping out weakly- and strongly-coupled regimes via the **Lund jet plane picture**
- Potential to map out spacetime evolution of quark-gluon plasma using Lund plane
- Other LHC substructure results can be found [here](#)



# Medium resolution length (color decoherence)

*Resolved as two charges*  
→ more quenching

*Resolved as a single charge*  
→ less quenching



Is the critical angle large enough?  
 $\vartheta_c \sim O(10^{-2} - 10^{-1})?$

Diagrams from [J. Casalderrey-Solana, Y. Mehtar-Tani, C. A. Salgado, K. Tywoniuk, arXiv:1210.7765](#)

# Soft-drop grooming

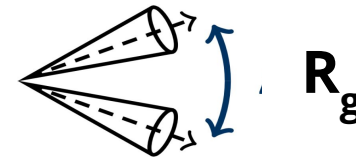
M. Dasgupta, A. Fregoso, S. Marzani, G. P. Salam, JHEP09 (2013) 029  
 A. J. Larkoski, S. Marzani, G. Soyez, J. Thaler, JHEP 1405 (2014) 146

**Soft Drop** grooming to control **large** UE contribution:

$$z_g = \frac{\min(p_T^{(1)}, p_T^{(2)})}{p_T^{(1)} + p_T^{(2)}} > z_{\text{cut}} \left( \frac{\Delta R_{12}}{R} \right)^{\beta_{\text{sd}}}$$

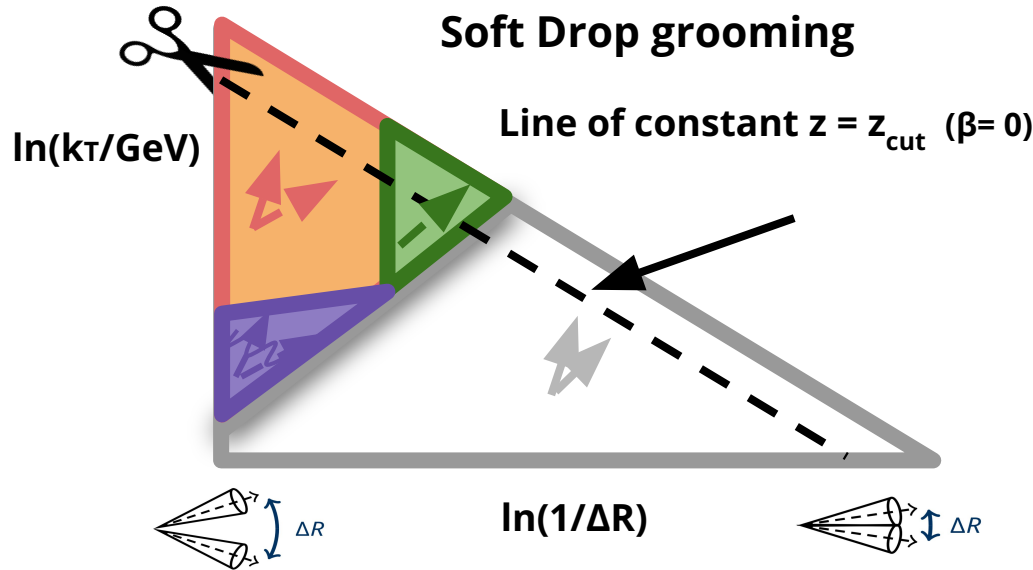
(typical choice in heavy-ions is  $\beta_{\text{SD}} = 0$ ,  $z_{\text{cut}} = 0.2$ )

*Hard two-prong structure is exposed*



$R_g$  is expected to be sensitive to color decoherence effects

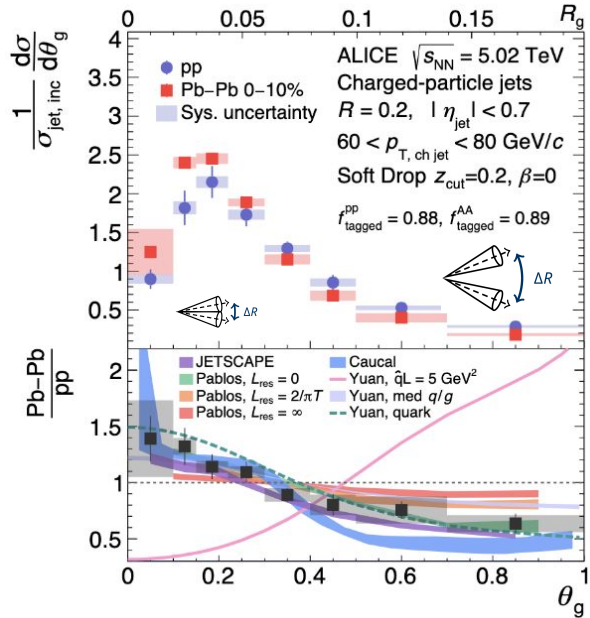
*Y. Mehtar-Tani, K. Tywoniuk, JHEP04(2017)125*



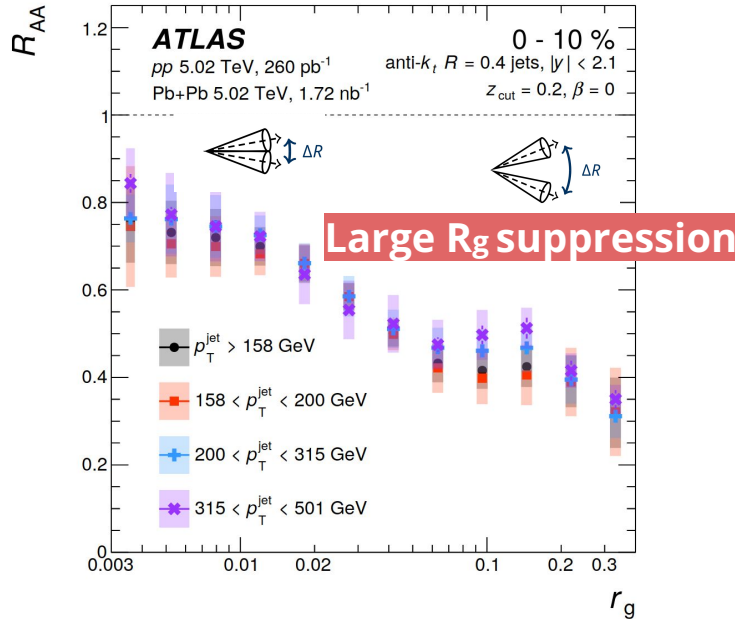
1-splitting per jet

# Previous measurements in inclusive jet events

## Groomed jet radius $R_g$

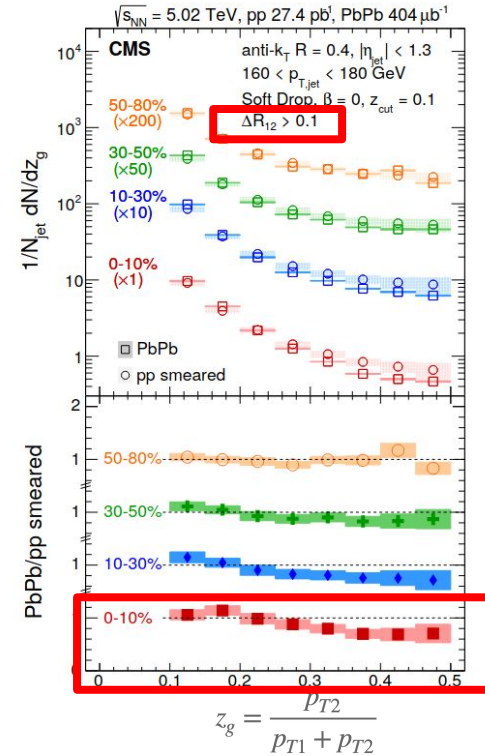


[ALICE, PRL 128.102001](#)



[ATLAS, PRC 107, 054909](#)

## Splitting function



[CMS, PRL 120, 142302 \(2018\)](#)

**Broad angular structures are more suppressed in PbPb.**

*Consequence of color decoherence?*

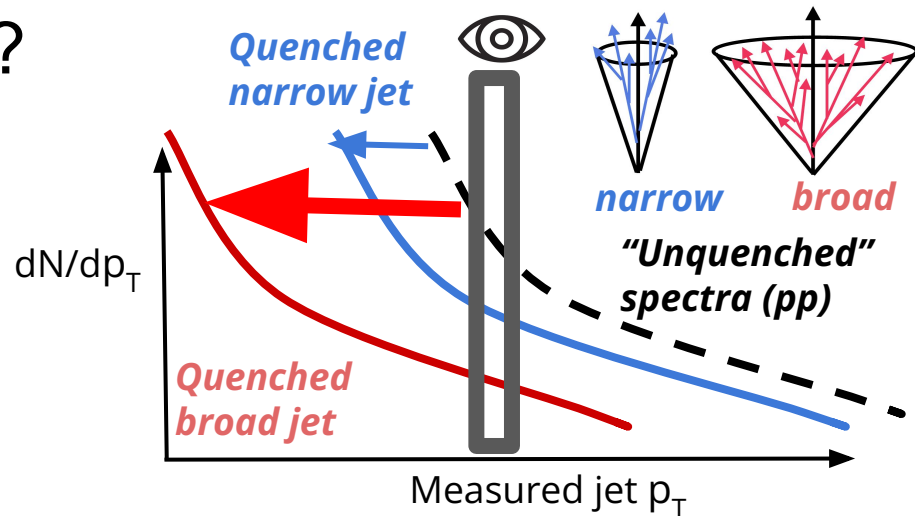
*Is a finite critical angle necessary to describe jet quenching?*

# Selection bias in inclusive jets?

Jets with a **broad** early vacuum shower are expected to be more quenched

**Glueon jets** (which are broad) are quenched more strongly than **quark jets** (which are narrow)

Potential effect in a jet  $p_T$  bin: **a narrowing effect**



# Selection bias in inclusive jets?

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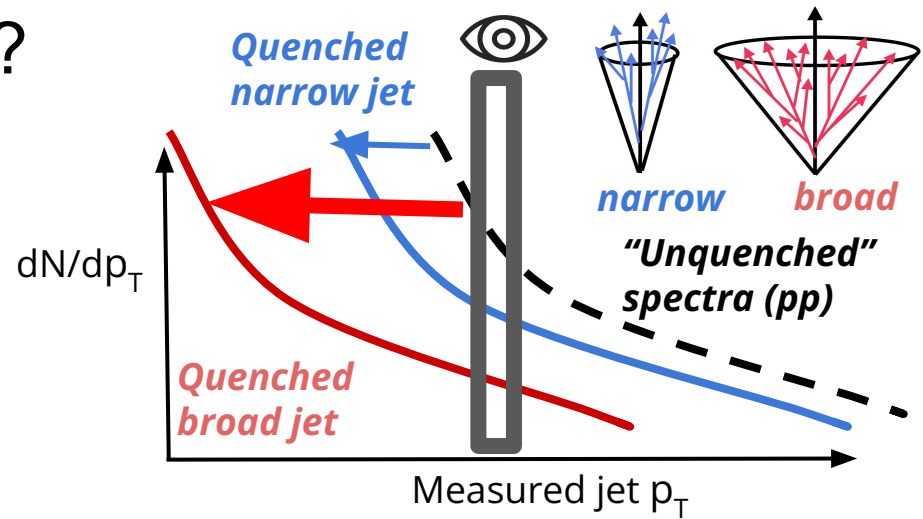
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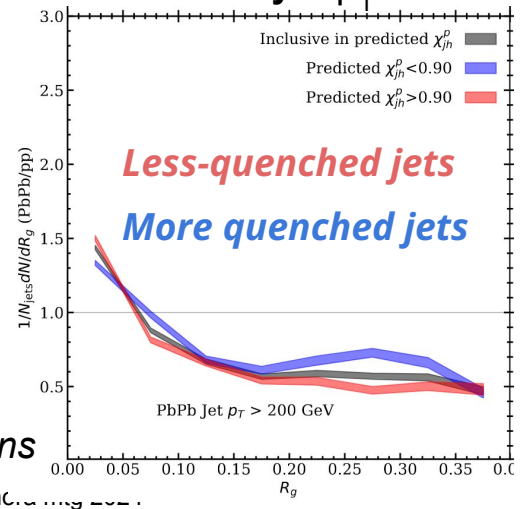
One way of controlling this effect is by selecting jets according to their **unquenched**  $p_T$

[J. Brewer, Q. Brodsky, K. Rajagopal, JHEP02\(2022\)175](#)

[J. Brewer, J. Milhano, J. Thaler PRL 122, 222301 \(2019\)](#)



## Final-state jet $p_T$ cut



[Y.L. Du, D. Pablos, K. Tywoniuk, JHEP 21 \(2020\), 206](#)

Hybrid model calculations



# Selection bias in inclusive jets?

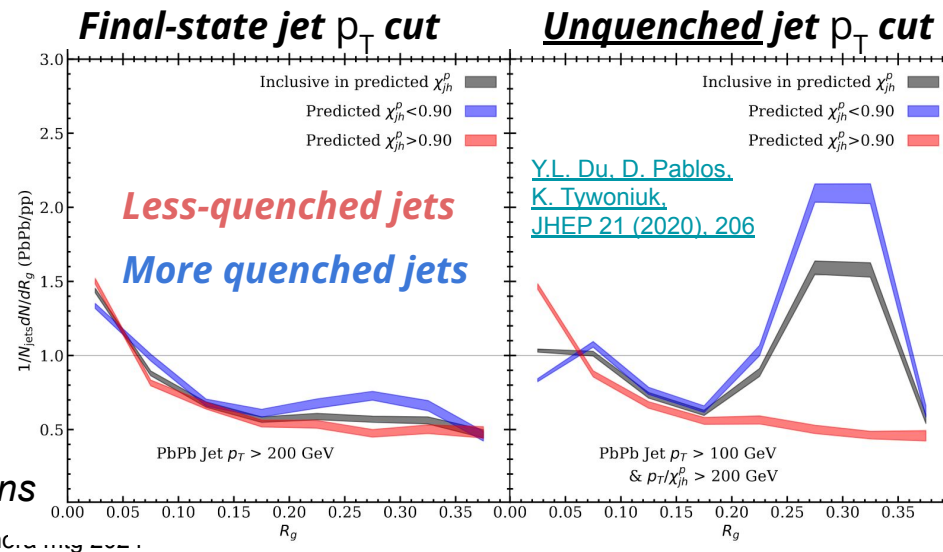
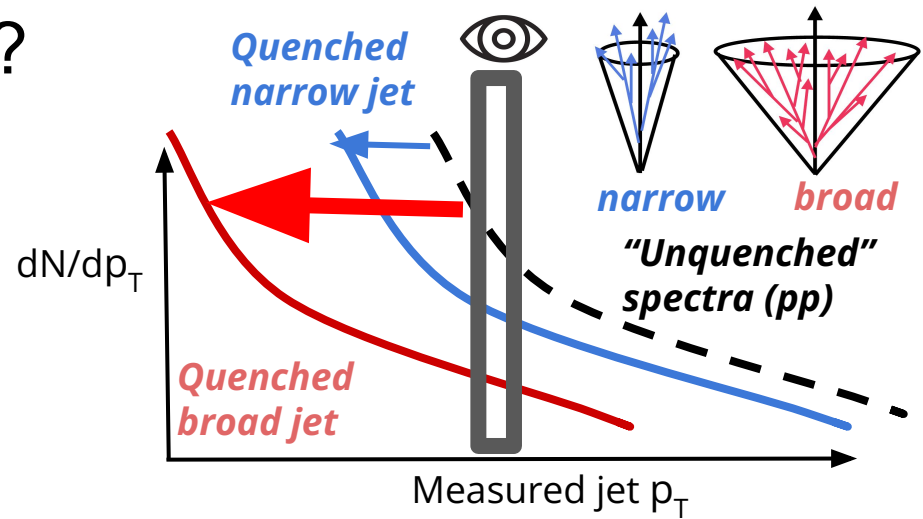
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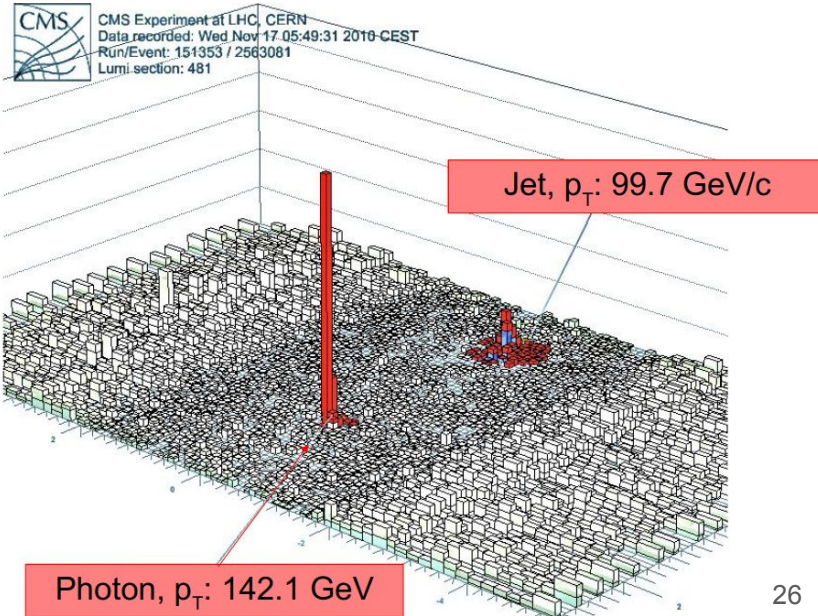
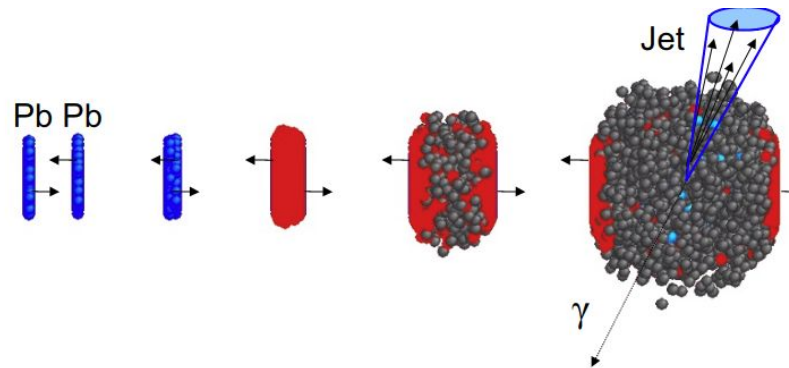


Hybrid model calculations

# Jet substructure using photon-tagged jets

Photon  $p_T^\gamma$  can be used as a proxy for unquenched  $p_T^{\text{jet}}$

Compare pp and PbPb with the same  $p_T^\gamma$



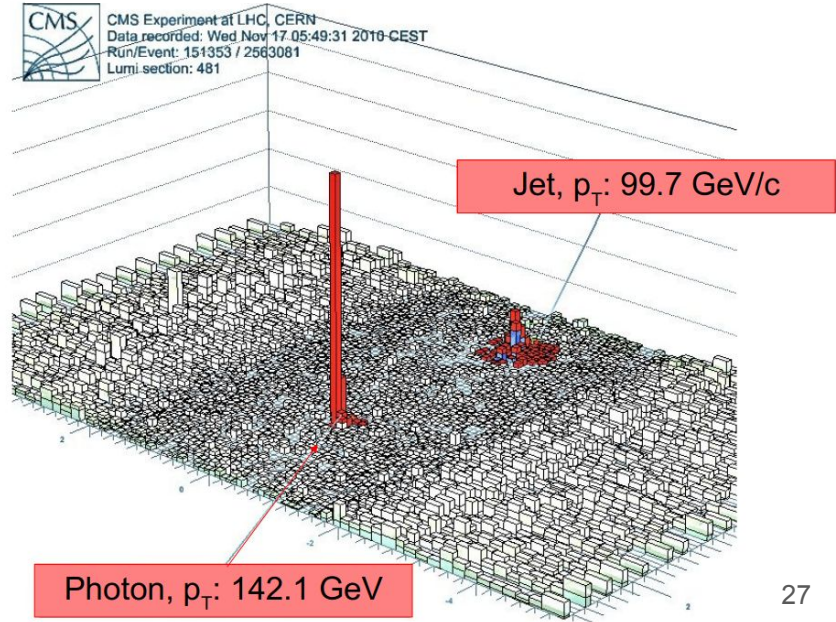
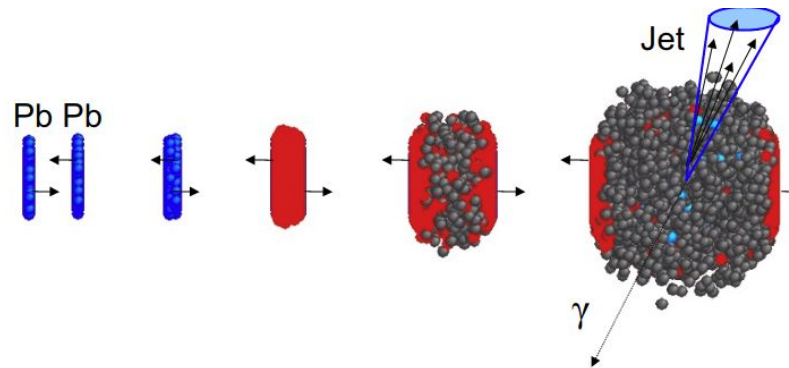
# Jet substructure using photon-tagged jets

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Compare pp and PbPb with the same  $p_T^\gamma$

## Measurement setup:

- Isolated photon with  $p_T^\gamma > 100$  GeV with  $|\eta^\gamma| < 1.44$
- anti- $k_T$  jets with  $R = 0.2$ ,  $\Delta\phi_{\gamma,\text{jet}} > \frac{2}{3}\pi$  and  $|\eta^{\text{jet}}| < 2$
- $R_g(z_{\text{cut}} = 0.2, \beta = 0)$  and jet girth  $g = \frac{1}{p_T^{\text{jet}}} \sum_i p_T^i \Delta R_{i,\text{jet}}$



# Jet substructure using photon-tagged jets

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## Measurement setup:

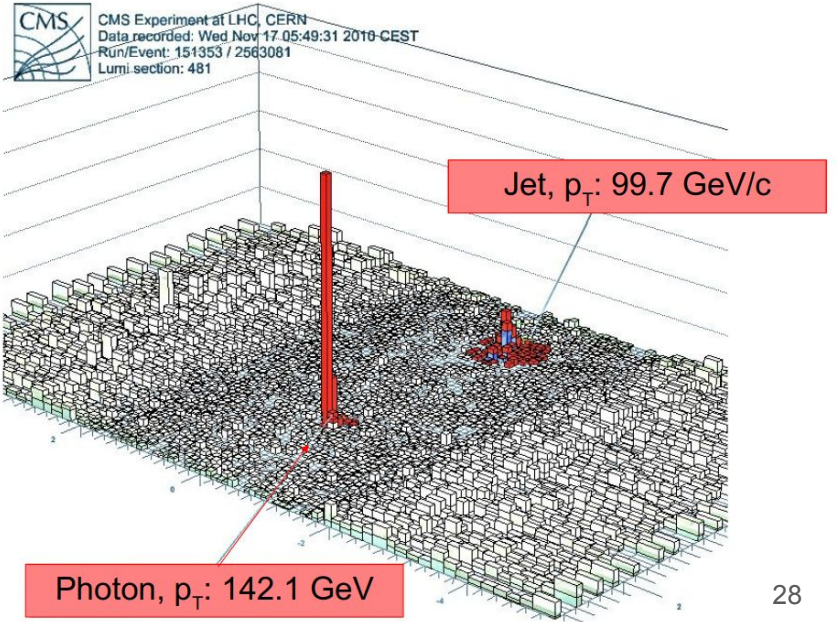
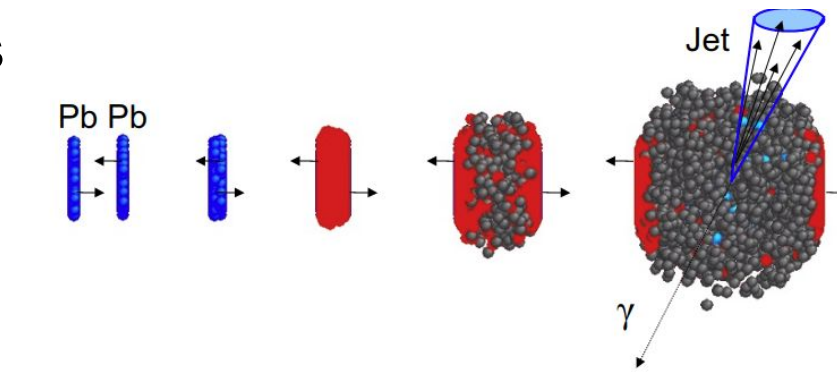
- Isolated photon with  $p_T^\gamma > 100$  GeV with  $|\eta^\gamma| < 1.44$
- anti- $k_T$  jets with  $R = 0.2$ ,  $\Delta\phi_{\gamma,\text{jet}} > \frac{2}{3}\pi$  and  $|\eta^{\text{jet}}| < 2$
- $R_g(z_{\text{cut}} = 0.2, \beta = 0)$  and jet girth  $g = \frac{1}{p_T^{\text{jet}}} \sum_i p_T^i \Delta R_{i,\text{jet}}$

## Two categories for measurement:

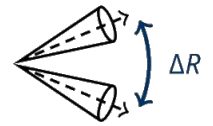
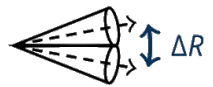
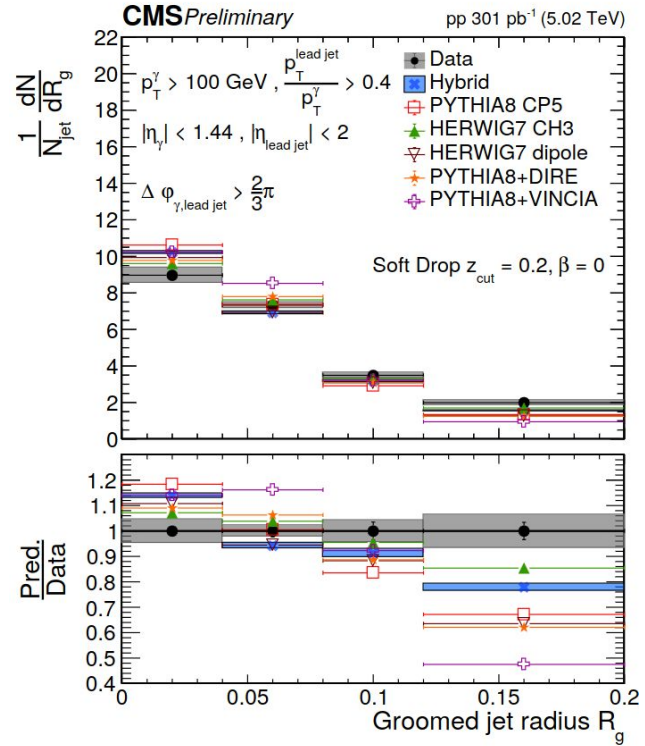
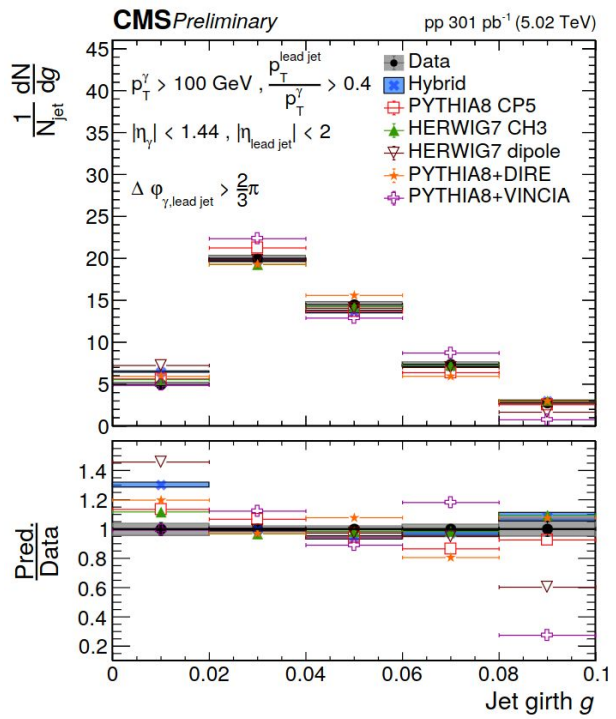
- $p_T^{\text{jet}}/p_T^{\text{photon}} > 0.4$  (quenched and nonquenched jets)
- $p_T^{\text{jet}}/p_T^{\text{photon}} > 0.8$  (less quenched jets)

Bkg from neutral meson diphoton decays subtracted with template fits and ABCD method

## corrections with D'Agostini unfolding

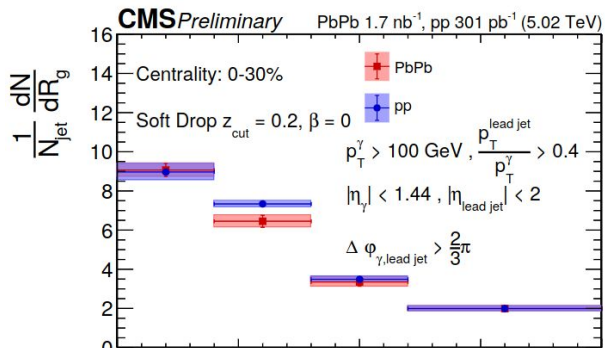
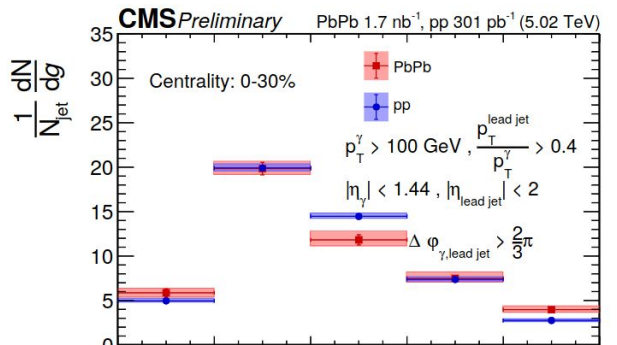


# Photon-tagged jets with $p_T^{\text{jet}}/p_T^\gamma > 0.4$ (proton-proton) **CMS-PAS-HIN-23-001, link soon**

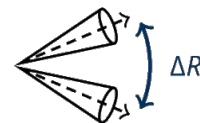
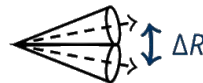
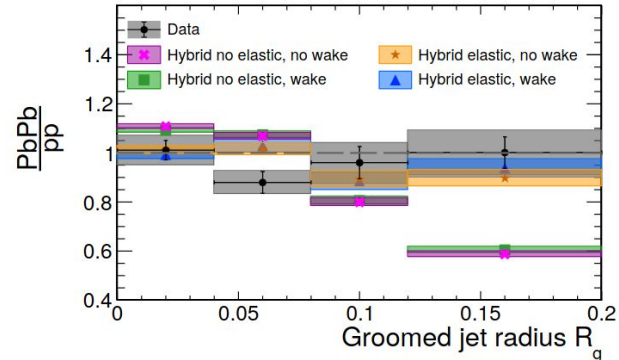
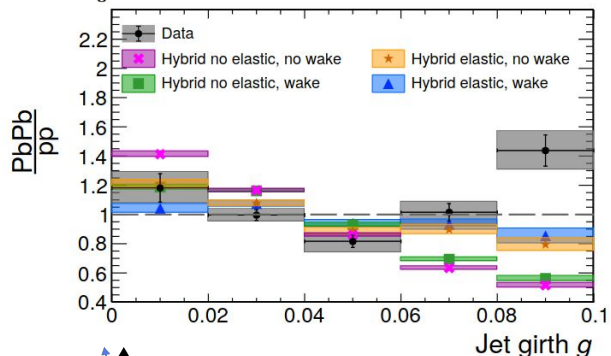


Differences of data and MC simulation of factors of up to 2  
 best global description by **HERWIG7 angular-ordered (CH3)**

# Photon-tagged jets with $p_{T}^{\text{jet}}/p_{T}^{\gamma} > 0.4$ in **PbPb** and **pp** (selecting quenched and less quenched jets)

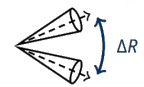
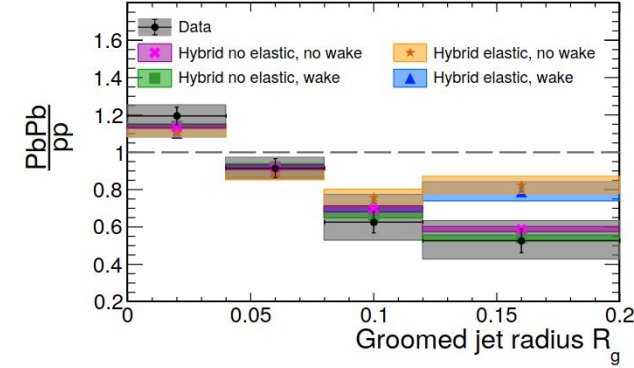
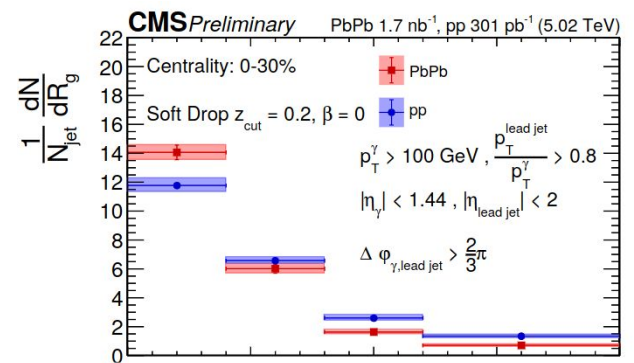
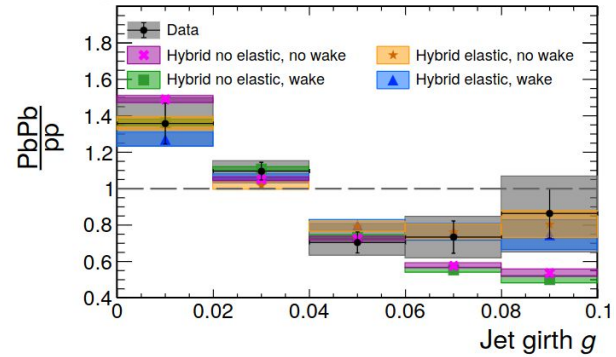
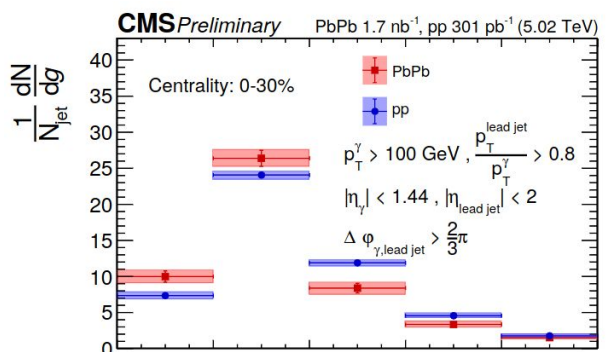


**No narrowing**



No angular narrowing observed in  $\gamma$ +jet events in contrast to inclusive jets

With stronger selection bias  $p_T^{\text{jet}}/p_T^\gamma > 0.8$

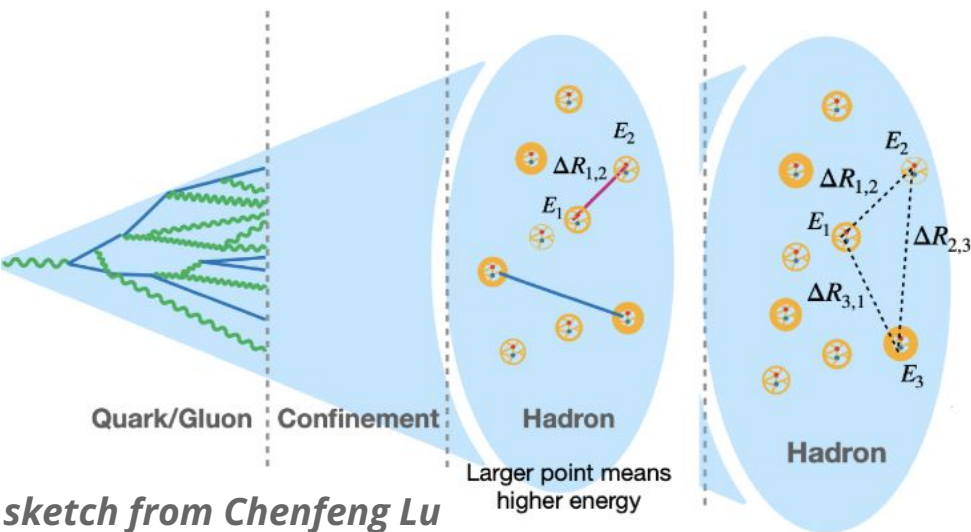


**Narrowing**

Predictions w/ Molière scatterings (large-angle deflections) give best global description ( $\mathcal{S}_c = 0$ ). No sensitivity to wake effect. [J. Casalderrey-Solana et al, JHEP01\(2020\)044](#)

# Energy-energy correlators (CMS)

arXiv:2402.13864, submitted to PRL



Energy-weighted two-particle angular correlations

$$C = \frac{d\sigma}{dx_L} = \sum_{i,j} d\sigma \frac{E_i E_j}{E^2} \delta(x_L - \Delta R_{i,j})$$

$$C = \frac{d\sigma}{dx_L} = \sum_{i,j,k} d\sigma \frac{E_i E_j E_k}{E^2} \times \delta(x_L - \max(\Delta R_{i,j}, \Delta R_{i,k}, \Delta R_{j,k}))$$

Angular separation  $x_L == \Delta R_{ij} = \sqrt{\Delta y^2 + \Delta \varphi^2}$

**Energy weights:** soft contributions are penalized, hard contributions are rewarded

Preliminary results  
also by [ALICE](#) and [STAR](#)

*Mapping out different stages of jet formation*



# Energy-energy correlators (CMS)

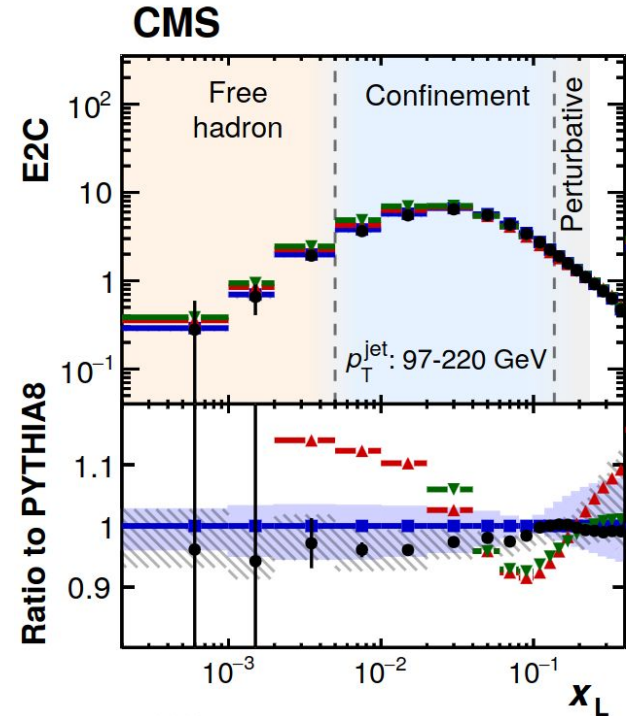
arXiv:2402.13864, submitted to PRL



At least two anti- $k_T$   $R = 0.4$  jets,  
 $p_{T, \text{jet}}$  from 100 GeV – 2 TeV

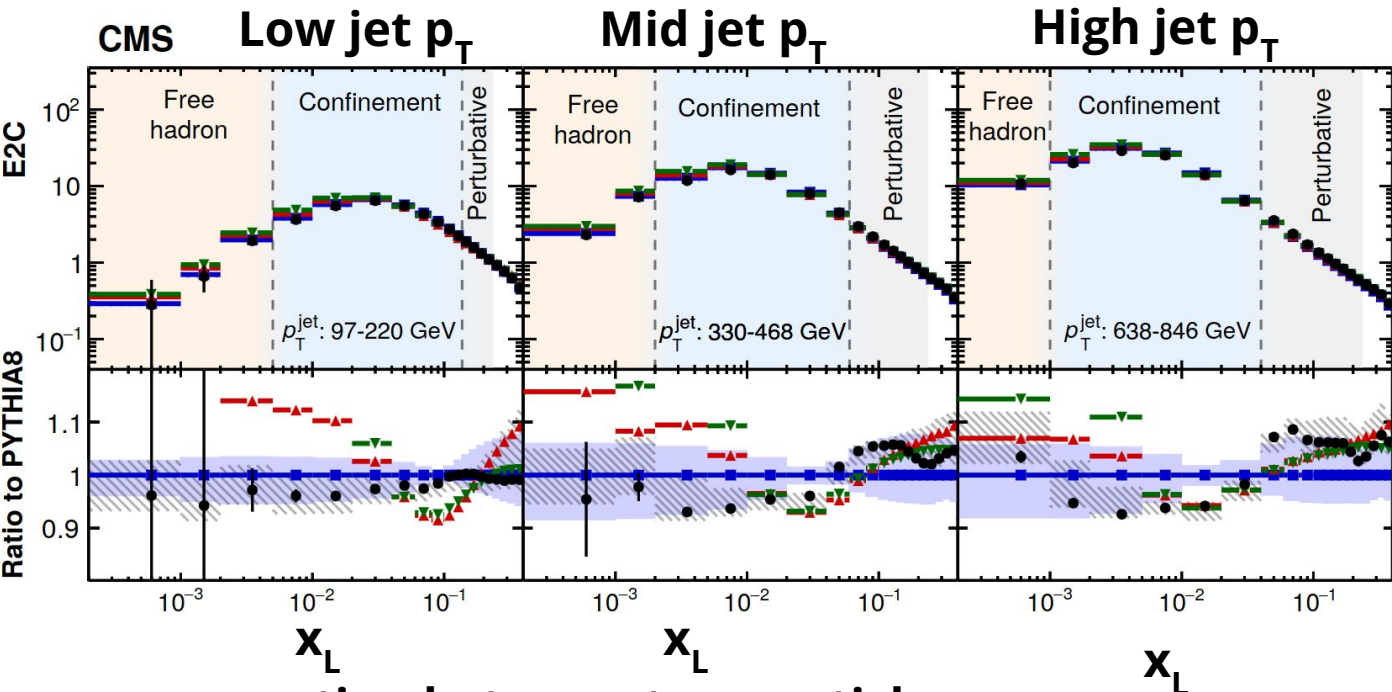
Distributions unfolded to stable particle level  
( $x_L$ ,  $p_T$ , & energy weights)

**Parton shower and hadronization regimes**  
(similar to Lund plane factorization)



$x_L$  == angular separation between two particles

# Two-point correlators (E2C)



**Free hadron region (low  $x_L$ )**

**PYTHIA8 CP5** describes data better than **HERWIG7 CH3/SHERPA2**

**Perturbative region (high  $x_L$ )**

**PYTHIA8 CP5** undershoots data at higher jet  $p_T$

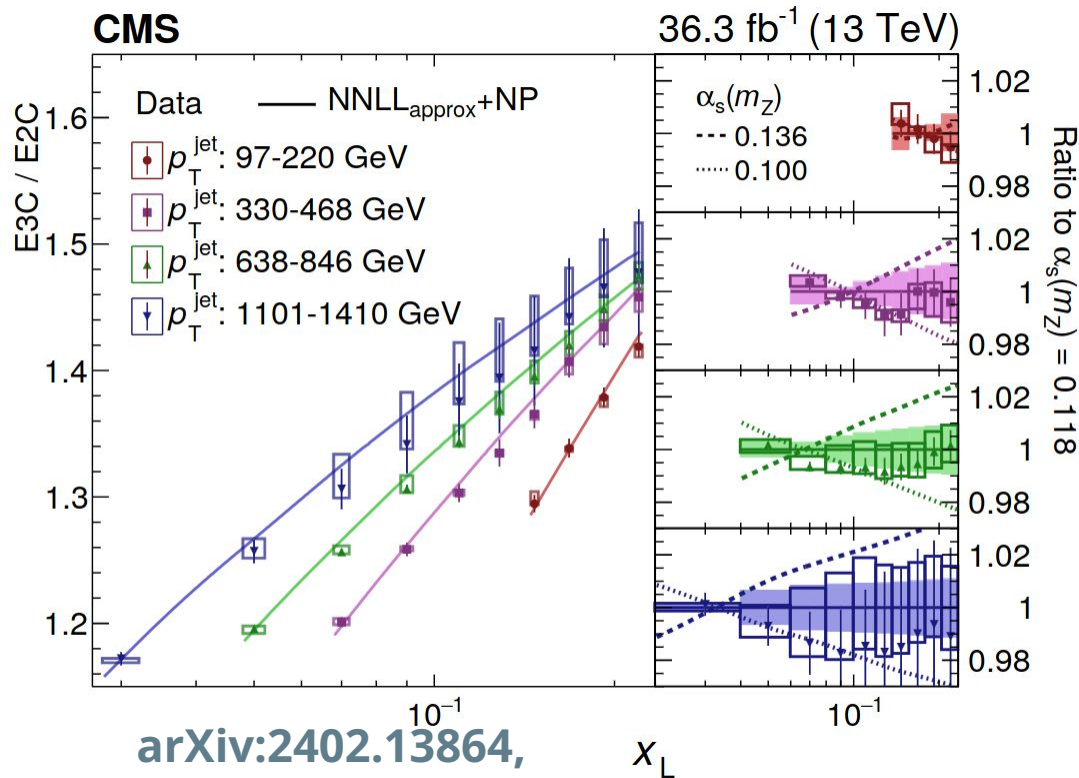
**HERWIG7 CH3 & SHERPA2** describe data better

$x_L$  == separation between two particles

- Data
- PYTHIA8 CP5 ( $p_T$  ord.)
- ▲ HERWIG7 CH3 (ang. ord.)
- ▼ SHERPA2

# Extraction of $\alpha_s$ from jet substructure

Ratio of three-point to two-point correlators (E3C/E2C)



arXiv:2402.13864,  
submitted to PRL

Using **NLO+NNLL<sub>approx</sub>** pQCD calculation  
with nonperturbative corrections

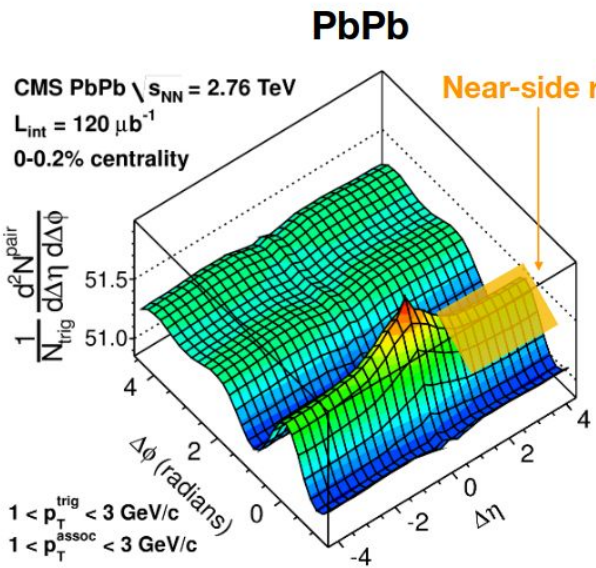
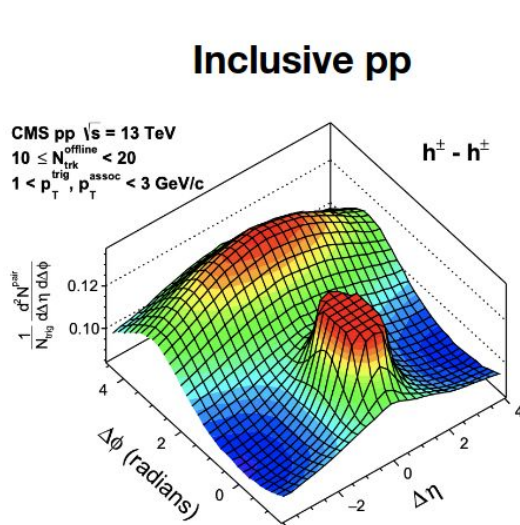
$$\alpha_s(m_Z) = 0.1229^{+0.0040}_{-0.0050} (\sim 4\%)$$

Most precise extraction of  $\alpha_s(m_Z)$   
with jet substructure

Quark/gluon degeneracy broken in  
E3C/E2C ratio, allows for breaking  
“10% uncertainty” barrier

# Two-particle angular correlations

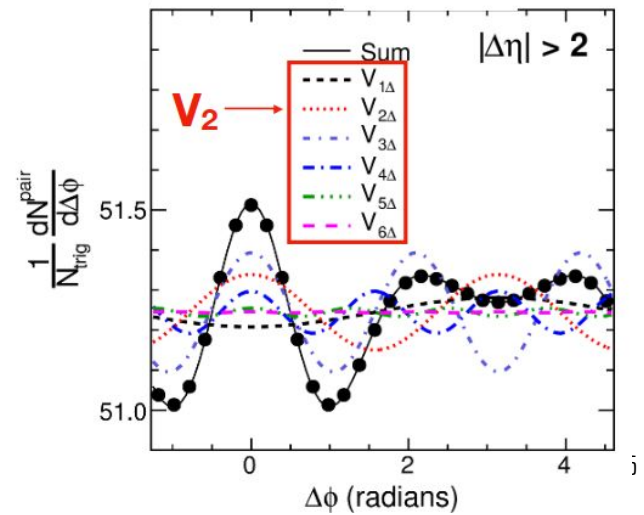
- **Near-side ridge** typical sign of collective behavior
- Fourier harmonics decomposition, nonzero  $V_{2\Delta}$  associated with anisotropic expansion



$$\frac{1}{N_{\text{ch}}} \frac{dN^{\text{pair}}}{d\Delta\phi} \propto \sum_{n=1}^{\infty} V_{n\Delta} \cos(n\Delta\phi)$$

CMS PbPb  $\sqrt{s_{\text{NN}}} = 2.76$  TeV  
 $L_{\text{int}} = 120 \mu\text{b}^{-1}$   
 0-0.2% centrality

**1D slice**



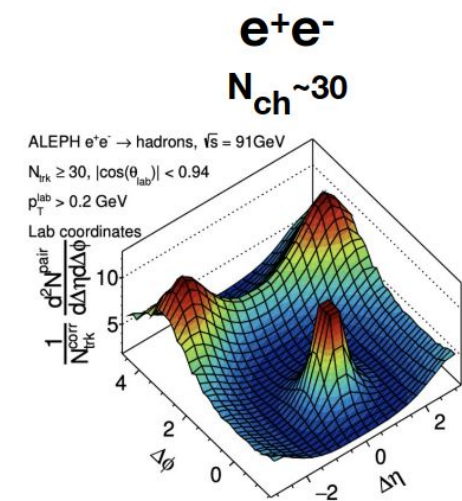
CMS, Phys. Lett. B 765 (2017) 193

# What about smaller systems?

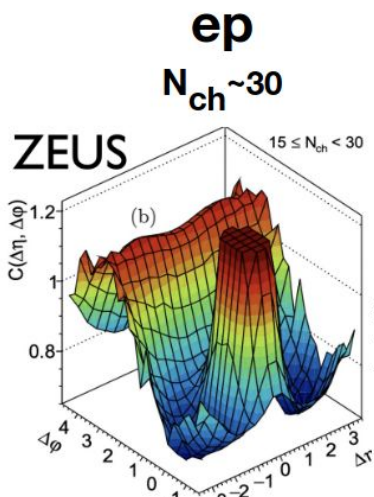
Unexpected nonzero  $v_2$  in high-multiplicity pp and pPb by CMS (*PLB* 765 (2017) 193, *PLB* 718 (2013) 795)

→ QGP droplet formation or emergent property of high-multiplicity QCD processes?

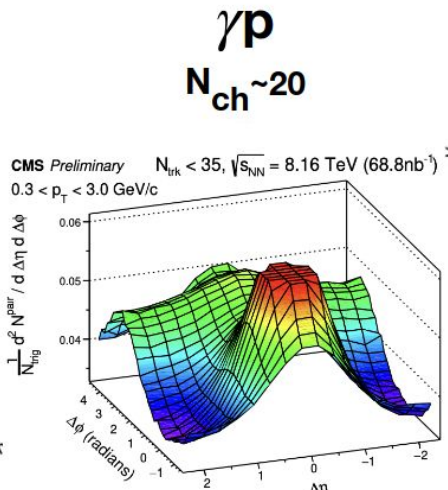
Since then, searches pushing the boundaries towards even smaller systems



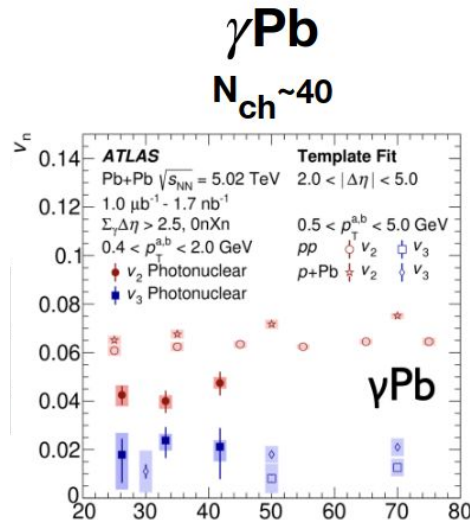
PRL 123 212002 (2019)  
Cristian Baldenegro (Sapienza)



JHEP 04 (2020) 070



PLB 844 (2023) 137905  
Sonora mtg, 2024



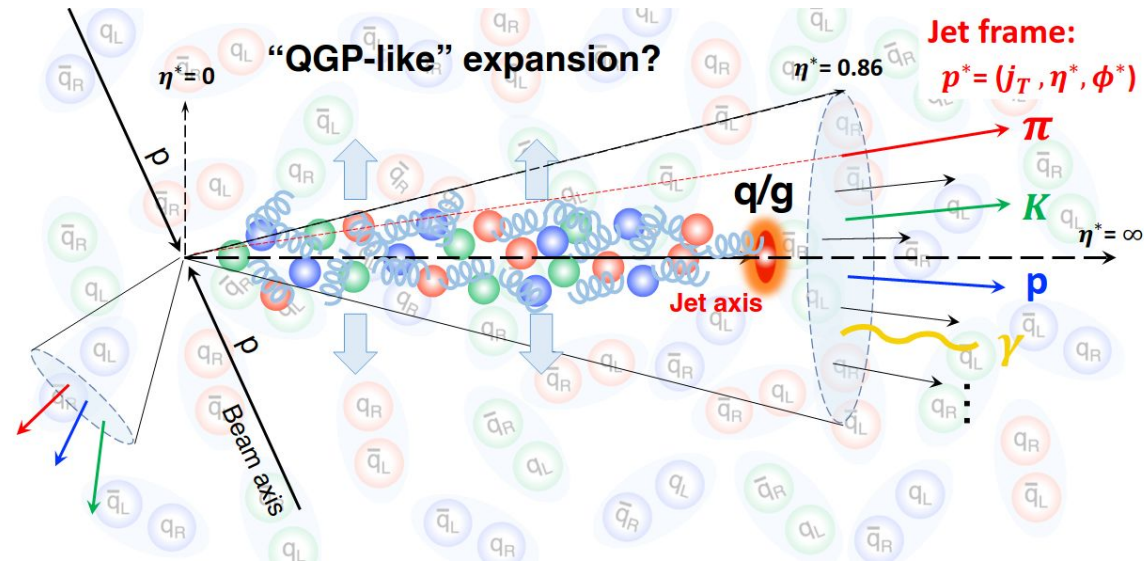
PRC, 104 014903 (2021)<sup>37</sup>

# Search for intrajet collective behavior in CMS

[arXiv:2312.17103](https://arxiv.org/abs/2312.17103), submitted to PRL

$p_{T,\text{jet}} > 550 \text{ GeV}$ , anti- $k_T$   $R = 0.8$ ,  $|\eta^{\text{jet}}| < 1.6$

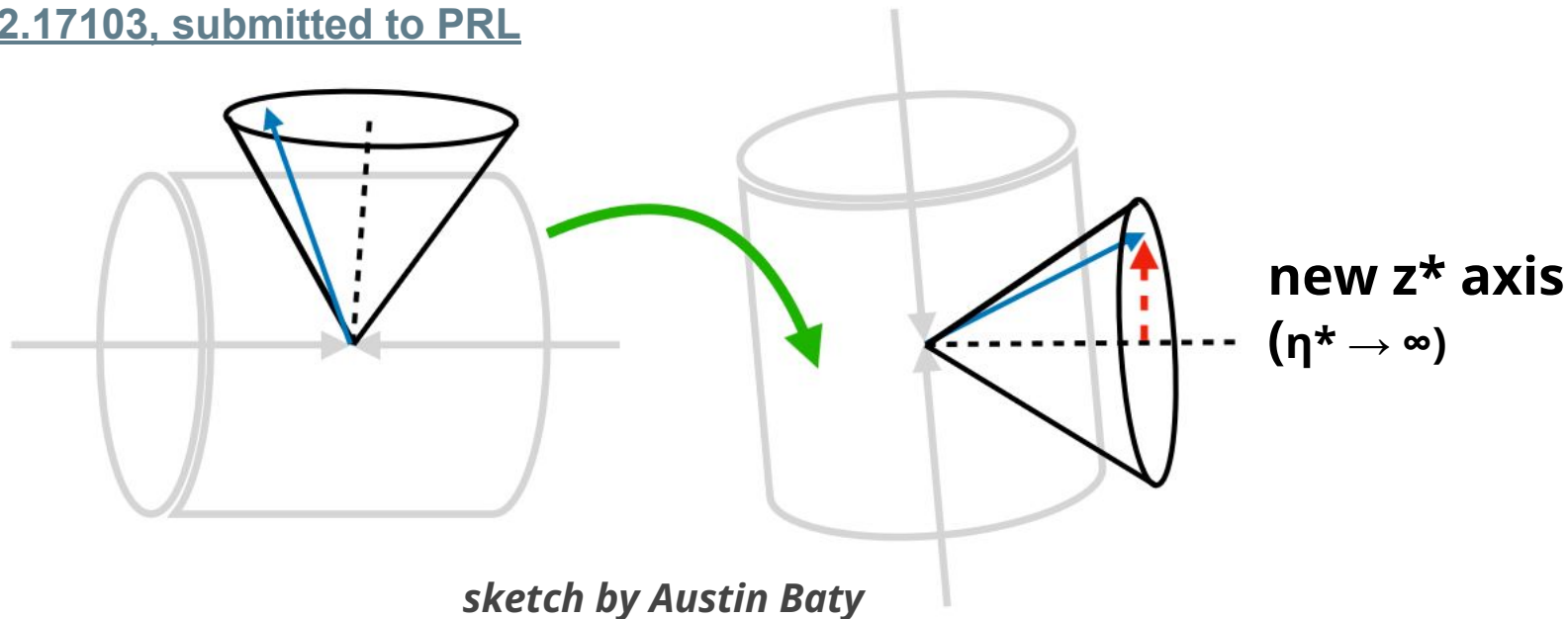
Charged-particle constituents used for two-particle correlations  
(pileup mitigation + low  $p_{T,\text{ch}}$ )



A. Baty, P. Gardner, W. Li,  
Phys. Rev. C 107 (2023) 064908

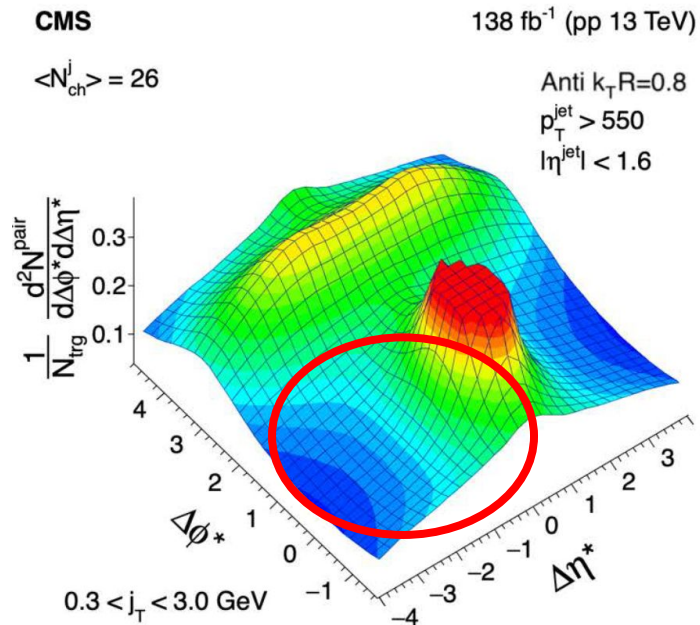
# Rotated reference frame such that $z^*$ axis is aligned with jet axis

[arXiv:2312.17103](https://arxiv.org/abs/2312.17103), submitted to PRL

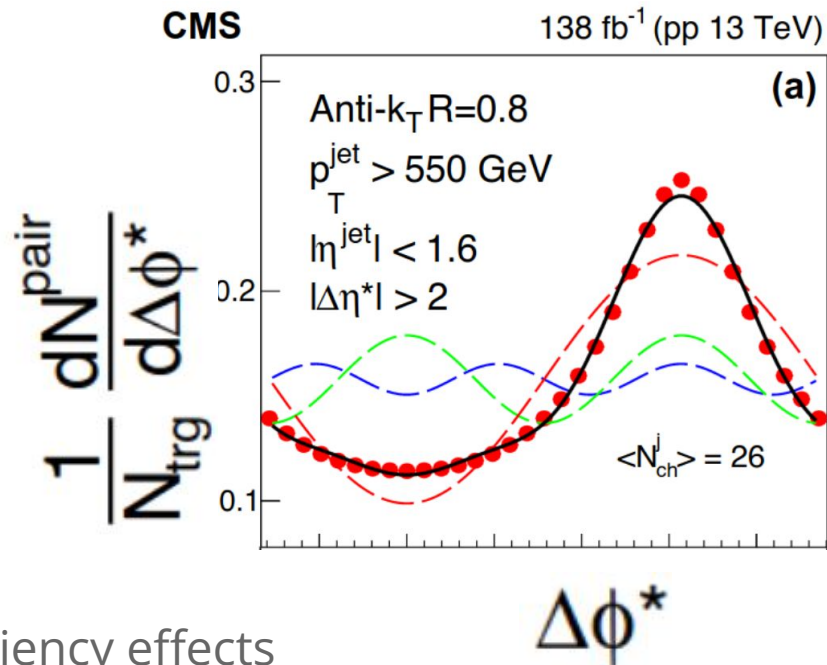


Particle correlations using  $\varphi^*$  and  $\eta^*$  coordinates (restricted to  $0.86 < |\eta^*| < 5$ ),  
transverse momentum relative to the jet axis  $j_T$  ( $0.3 < j_T < 3 \text{ GeV}$ )

# inclusive $N_{ch}$ category



$$\frac{1}{N_{ch}^j} \frac{dN^{pair}}{d\Delta\phi^*} \propto \sum_{n=1}^{\infty} V_{n\Delta} \cos(n\Delta\phi^*)$$



2D distributions corrected for acceptance/efficiency effects

**No near-side ridge at  $\Delta\phi^* \sim 0$**

[arXiv:2312.17103](https://arxiv.org/abs/2312.17103), submitted to PRL



# high $N_{ch}$ category

arXiv:2312.17103, submitted to PRL

CMS

138 fb<sup>-1</sup> (pp 13 TeV)

CMS

138 fb<sup>-1</sup> (pp 13 TeV)

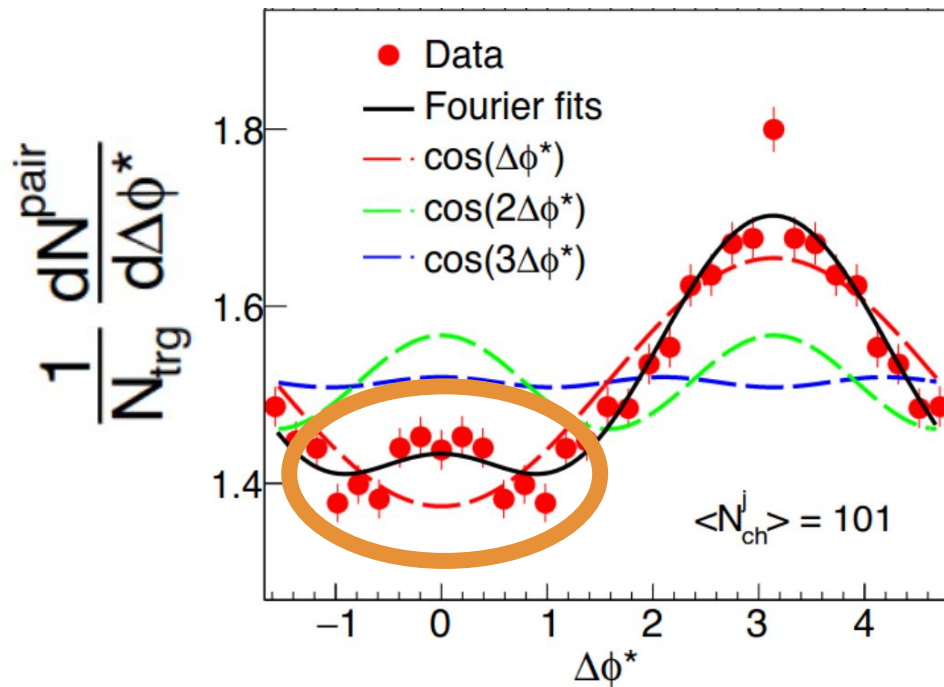
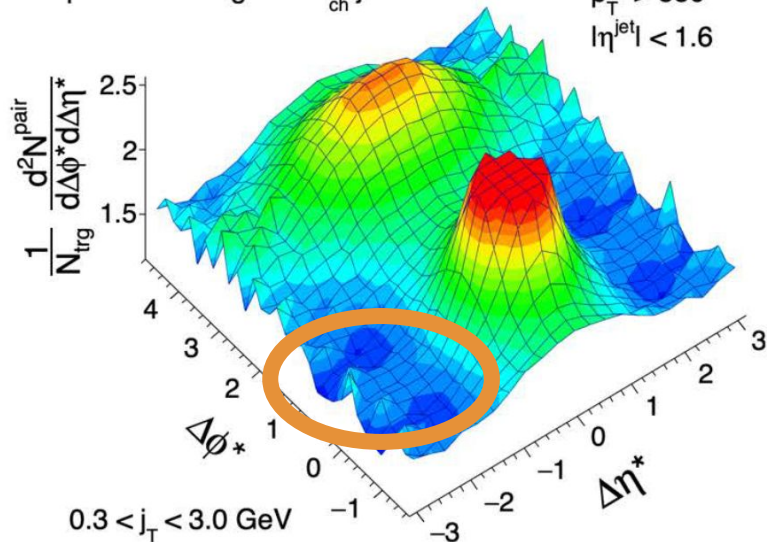
$$\langle N_{ch}^j \rangle = 101$$

Top 0.0023% highest- $N_{ch}^j$  jets

Anti  $k_T$ -R=0.8

$$p_T^{\text{jet}} > 550$$

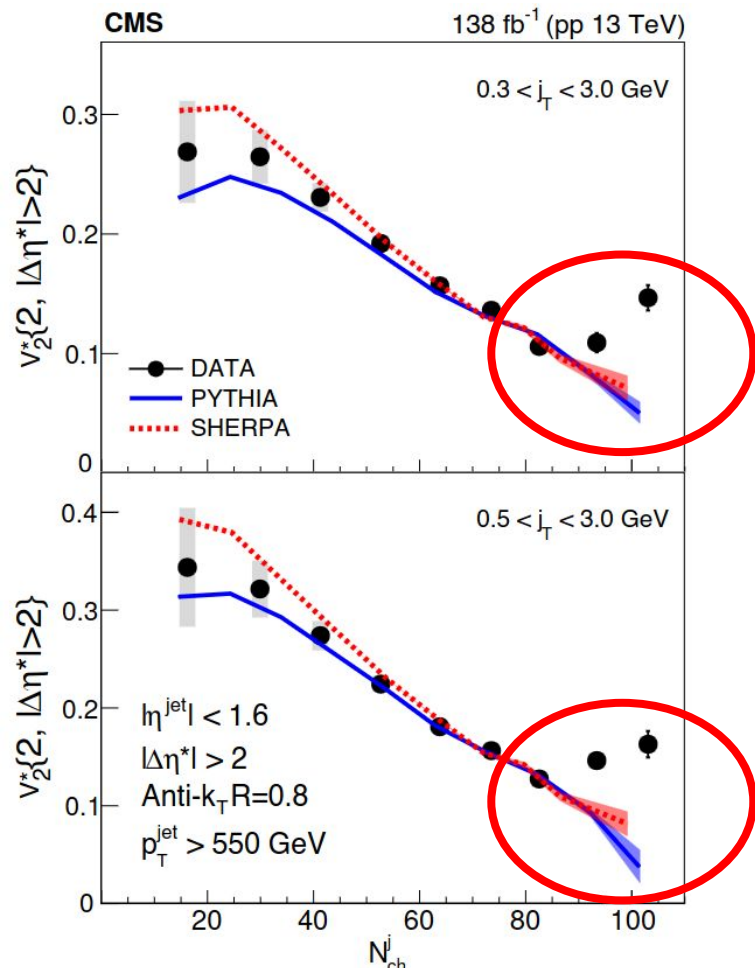
$$|\eta^{\text{jet}}| < 1.6$$



*Near-side ridge-like structure at  $\Delta\phi^* \sim 0$*

# single-particle $v_2 = \sqrt{V_2}$ vs $N_{ch}$

[arXiv:2312.17103](https://arxiv.org/abs/2312.17103), submitted to PRL

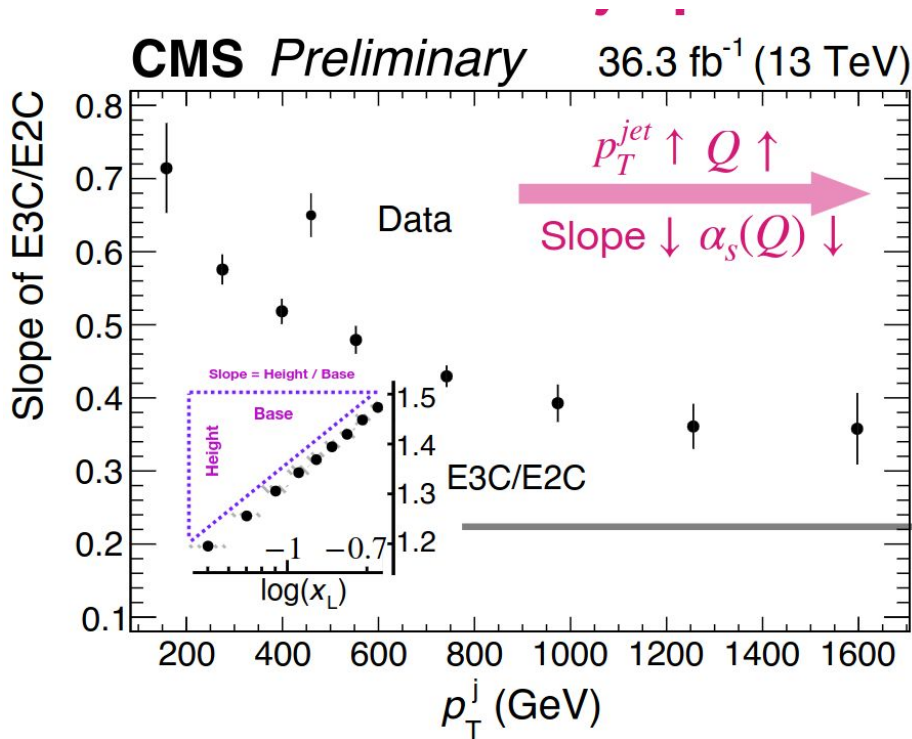


Nonzero  $v_2$  reproduced by  
**SHERPA2, PYTHIA8 CP5** up to  $N_{ch} \sim 80$

Increasing  $v_2$  with large  $N_{ch}$  not  
expected by these MC predictions

# E3C/E2C sensitive to running $\alpha_s$

CMS-PAS-SMP-22-015

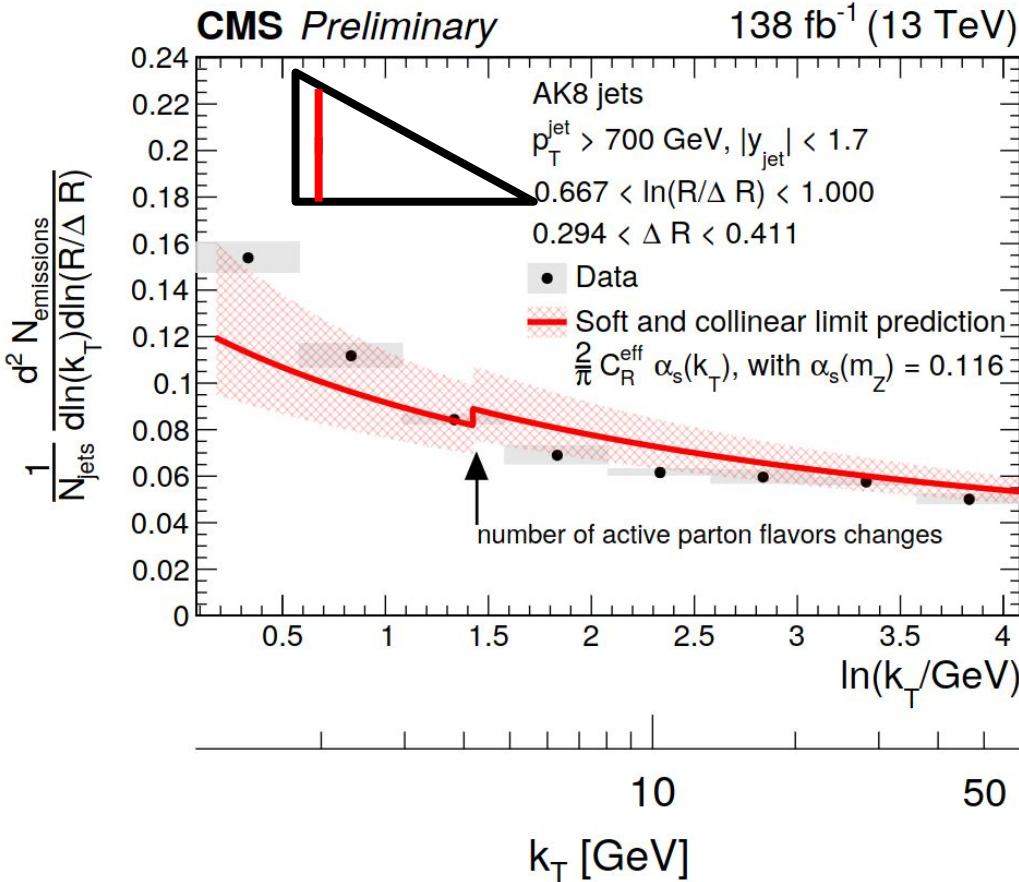


At LL, slope of E3C/E2C ratio sensitive to  $\alpha_s(Q)$

$$\frac{\Delta}{\ominus} \propto \alpha_s(Q) \ln x_L + O(\alpha_s^2)$$

Quark/gluon fraction sensitivity is reduced in the E3C/E2C ratio, without losing sensitivity to  $\alpha_s(Q)$  running

# Running of $\alpha_s$ in the jet shower



Recall LO pocket formula for Lund density:

$$\frac{1}{N^{\text{jets}}} \frac{d^2 N_{\text{emissions}}}{d \ln(k_T) d \ln(R/\Delta R)} \simeq \frac{2}{\pi} C_R \alpha_s(k_T)$$

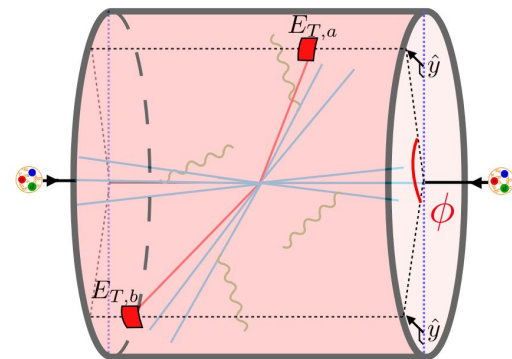
**Running  $\alpha_s(k_T)$  from few GeV to ~60 GeV qualitatively describes the data**  
 (Assuming q/g fractions from PYTHIA8)

**energy-weighted cross section**

$$\frac{d\sigma_{\text{EEC}}}{dR_L} = \sum_{i,j} \int d\sigma(R'_L) \frac{p_{T,i} p_{T,j}}{p_{T,\text{jet}}^2} \delta(R'_L - R_{L,ij})$$

$$R_L = \sqrt{\Delta\phi_{ij}^2 + \Delta\eta_{ij}^2}$$

*Observable connected to conformal field theory approaches*

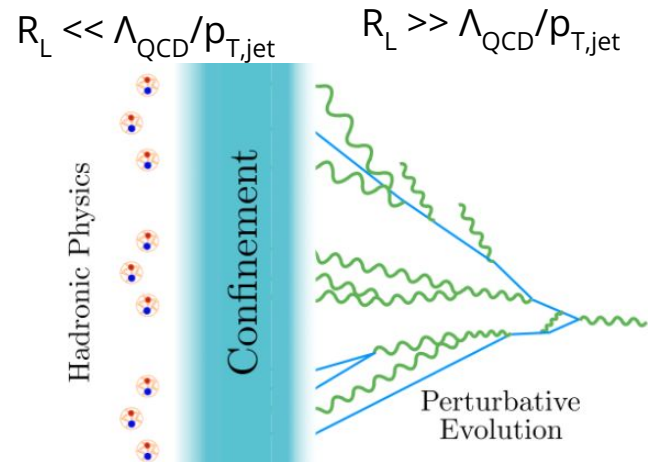


*sketch from Ian Mout*

Soft particle pairs are “penalized” with small energy weights (typically at small  $R_L$ )

Hard radiation is “rewarded” with larger weights (typically at large  $R_L$ )

***No jet grooming to suppress soft physics is required***

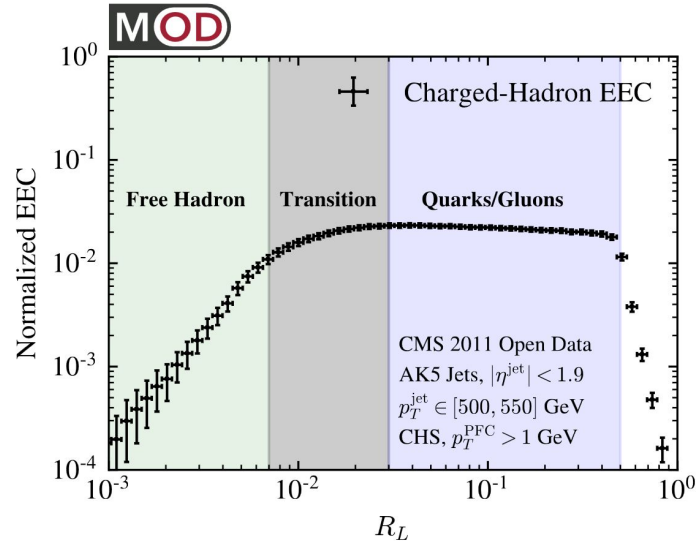


$$\frac{d\sigma_{\text{EEC}}}{dR_L} = \sum_{i,j} \int d\sigma(R'_L) \frac{p_{T,i} p_{T,j}}{p_{T,\text{jet}}^2} \delta(R'_L - R_{L,ij})$$

## How to measure these experimentally?

1. For a given pair of jet constituents, fill a histogram with weight =  $p_{T,i} p_{T,j} / p_{T,\text{jet}}^2$  at entry  $R_L = \Delta R_{ij}$
2. Iterate step 1 for all possible pairs in the jet (there will be multiple histogram entries per jet)
3. Do this for all jets, and you obtain an energy-weighted two-particle correlation distribution

[P. Komiske, I. Mout, J. Thaler, H.X. Zhu, PRL 130, 051901](#)



## Proof of concept using CMS OpenData

Access to scaling properties of QCD

# Generalized angularities in dijet and Z+jet events

CMS, [arXiv:2109.03340](https://arxiv.org/abs/2109.03340),  
**JHEP 01 (2022) 188**

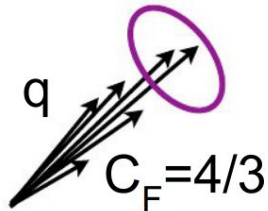
$$\lambda_{\beta}^{\kappa} = \sum_{i \in \text{jet}} z_i^{\kappa} \left( \frac{\Delta R_i}{R} \right)^{\beta} \quad z_i \equiv \frac{p_{Ti}}{\sum_{j \in \text{jet}} p_{Tj}}$$

$\kappa$  &  $\beta$  are parameters set by user

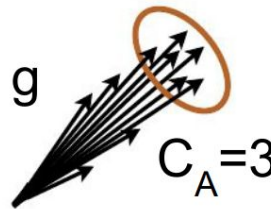
Sensitive to quark vs gluon differences  
 (subset of them are IRC-safe)

[JHEP 1707 \(2017\) 091](https://arxiv.org/abs/1707.091)

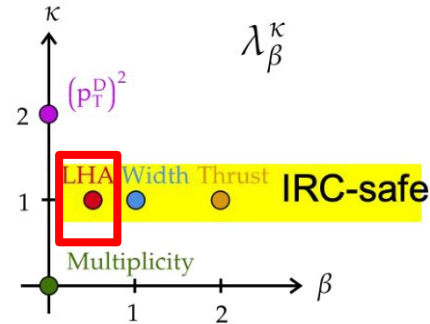
**Z+jet (quark-like)**



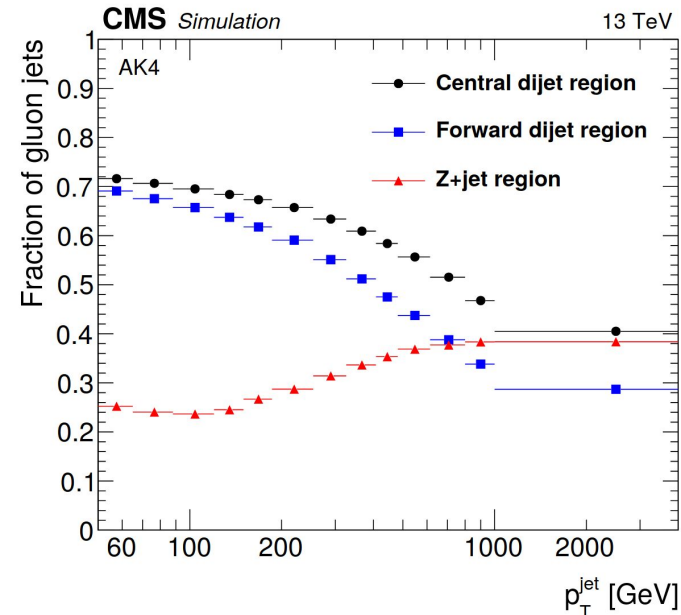
**Dijet (gluon-like)**

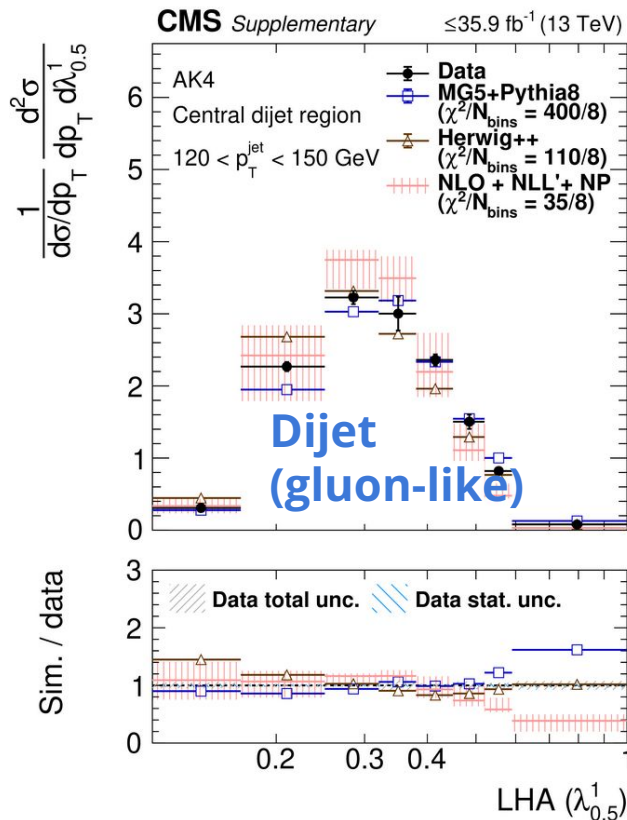
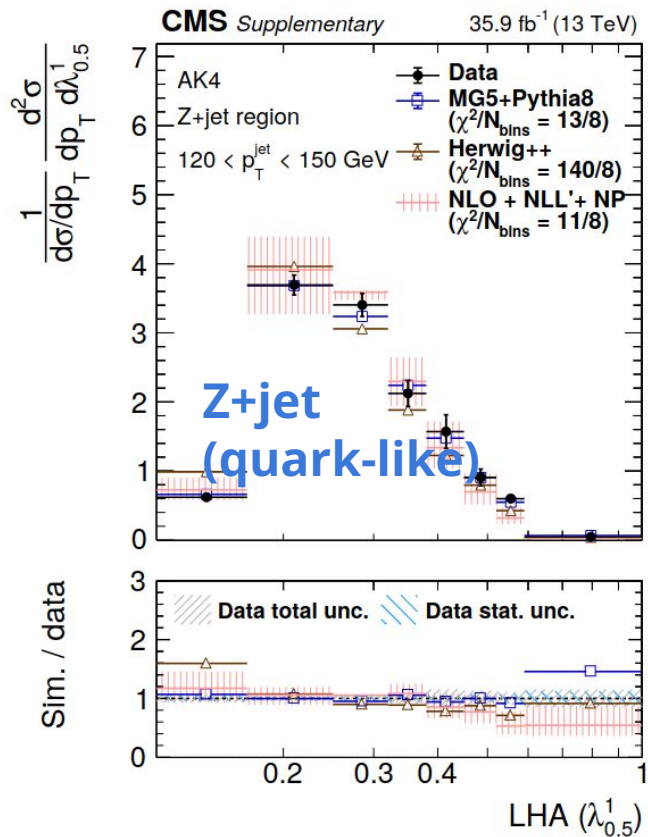


Ungroomed vs groomed with  $z_{\text{cut}} = 0.1$ ,  $\beta_{\text{SD}} = 0$ ,  
 $R = 0.4$  vs  $R = 0.8$   
 charged-only vs charged+neutrals



Will show a specific angularity (LHA)





**Jets in dijets (gluon-like) broader than Z+jets (quark-like)**

More challenging to describe **gluon-enriched jets (dijet)**

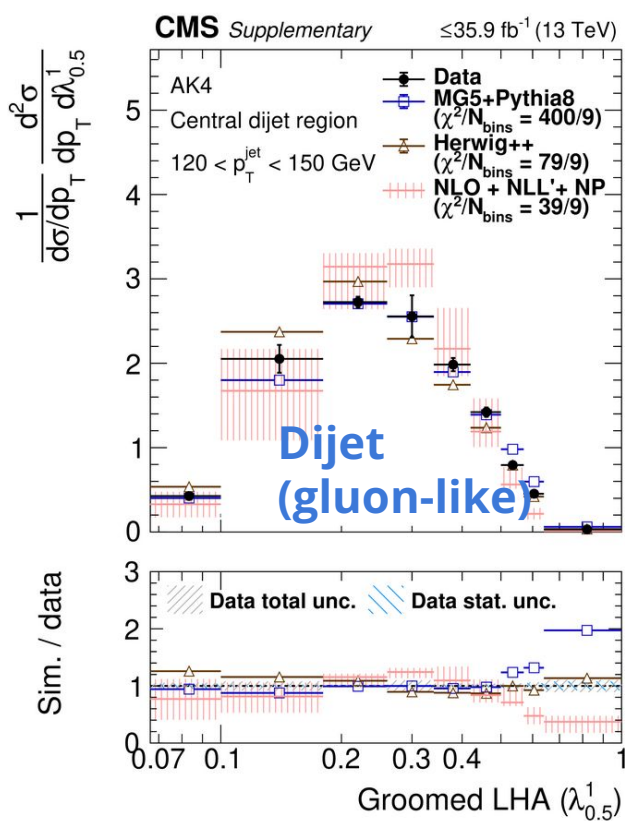
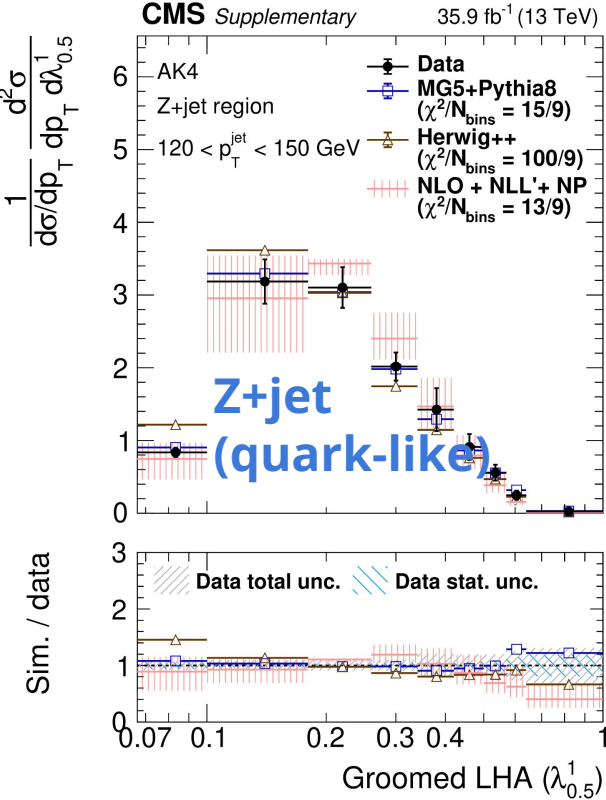
$$\kappa = 0.5, \beta = 1$$

$$\lambda_\beta^\kappa = \sum_{i \in \text{jet}} z_i^\kappa \left( \frac{\Delta R_i}{R} \right)^\beta \quad z_i \equiv \frac{p_{Ti}}{\sum_{j \in \text{jet}} p_{Tj}}$$

pQCD calculations [D. Reichelt, S. Caletti, O. Fedkevych, S. Marzani, S. Schumann, G. Soyez, JHEP 03 \(2022\) 131](#)



# Groomed Les Houches Angularity in Z-jet and dijet events



**Soft-drop grooming**  
(z<sub>cut</sub> = 0.1, β<sub>sd</sub> = 0) to remove soft and wide-angle radiation

More challenging to describe **gluon-enriched jets**

Mismodeling at large LHA increase after removing soft&wide-angle radiation

$$\kappa = 0.5, \beta = 1$$

$$\lambda_{\beta}^{\kappa} = \sum_{i \in \text{jet}} z_i^{\kappa} \left( \frac{\Delta R_i}{R} \right)^{\beta} \quad z_i \equiv \frac{PT_i}{\sum_{j \in \text{jet}} PT_j}$$

pQCD calculations [D. Reichelt, S. Caletti, O. Fedkevych, S. Marzani, S. Schumann, G. Soyez, JHEP 03 \(2022\) 131](#)

# Dijet/Z+jet ratio (g-enriched/q-enriched)

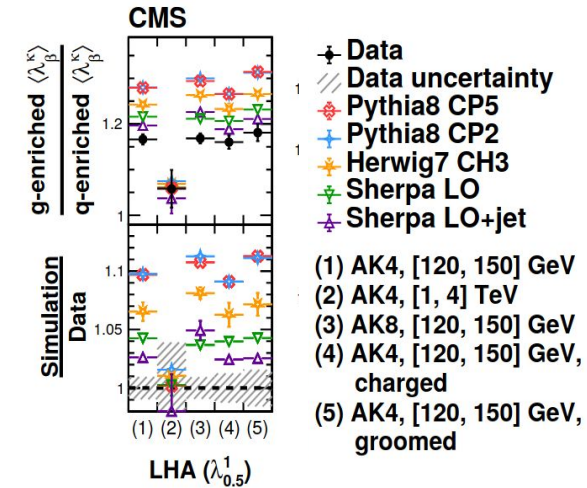
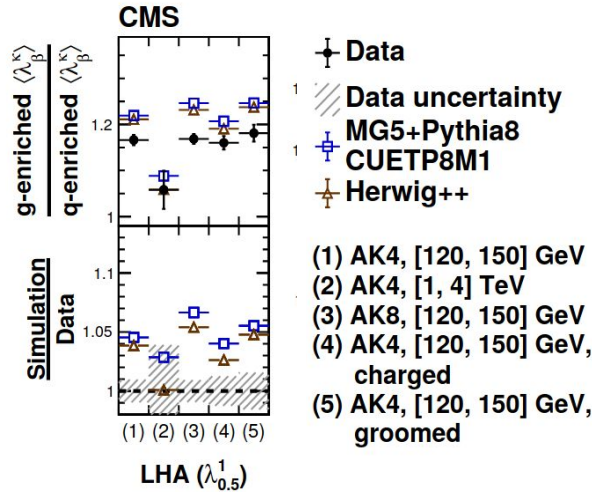
CMS, [arXiv:2109.03340](https://arxiv.org/abs/2109.03340),  
JHEP 01 (2022) 188

- uncertainties partially cancel in dijet/Z+jet ratio
- MC simulations overestimate g-enriched/q-enriched ratio
- g-enriched / q-enriched ratio is better modelled with “old” PYTHIA8/HERWIG7 tunes

gluon-LHA/quark-LHA > 1  
(mostly due to  $C_A > C_F$ )

“old” CMS tunes  
( $< \sim 5\%$  off)

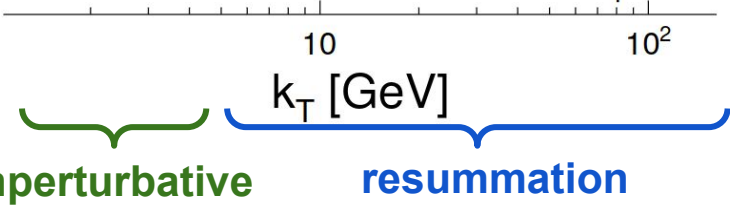
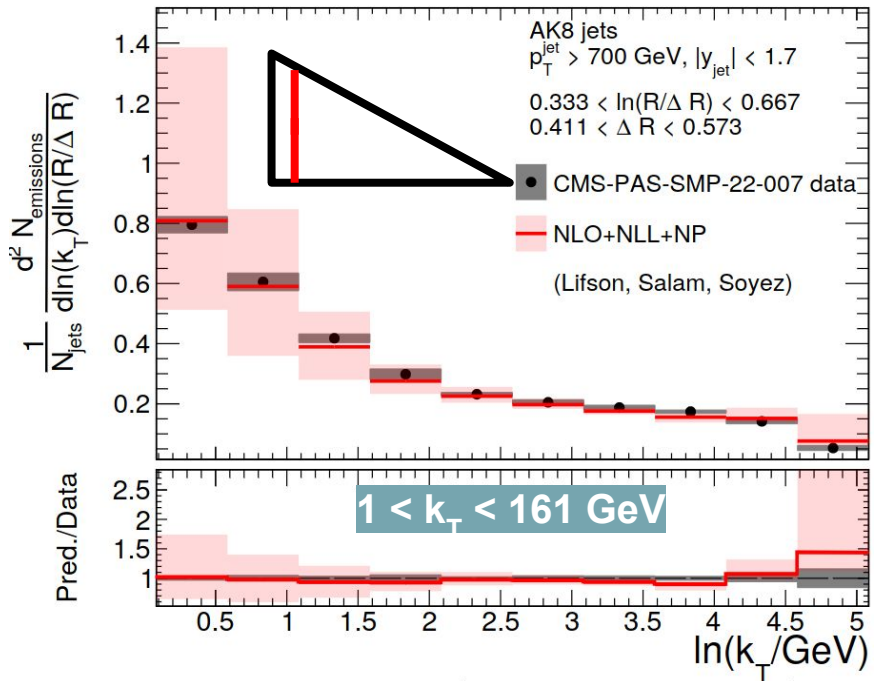
“new” CMS tunes  
(up to  $\sim 10\%$  off)



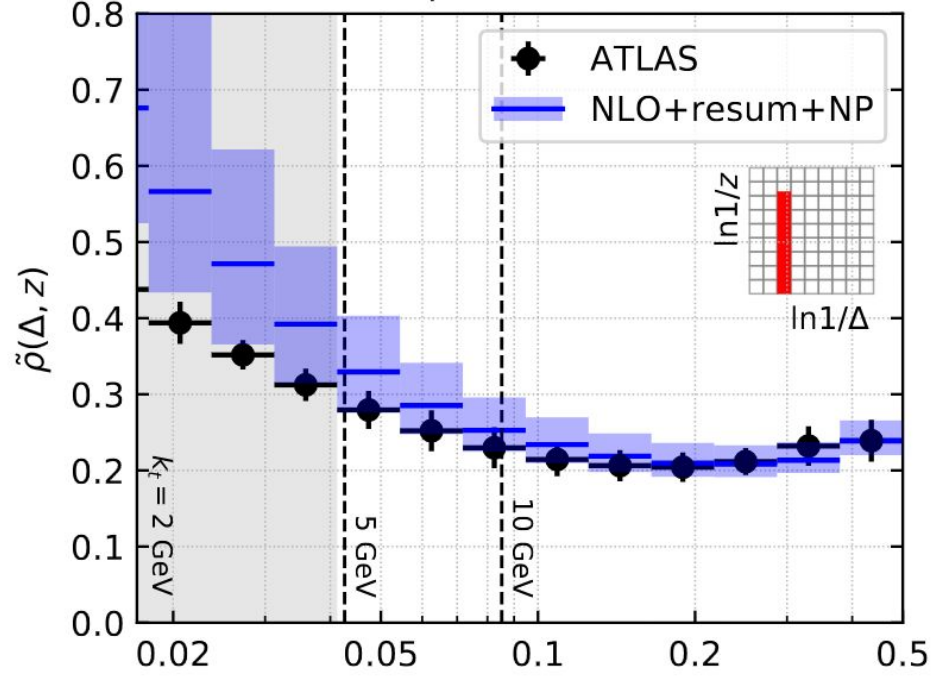
full summary plot in backup  
(other angularities)

# Comparison to pQCD analytical calculations (NLO+NLL+NP)

Calculations based on [JHEP10\(2020\)170](#)



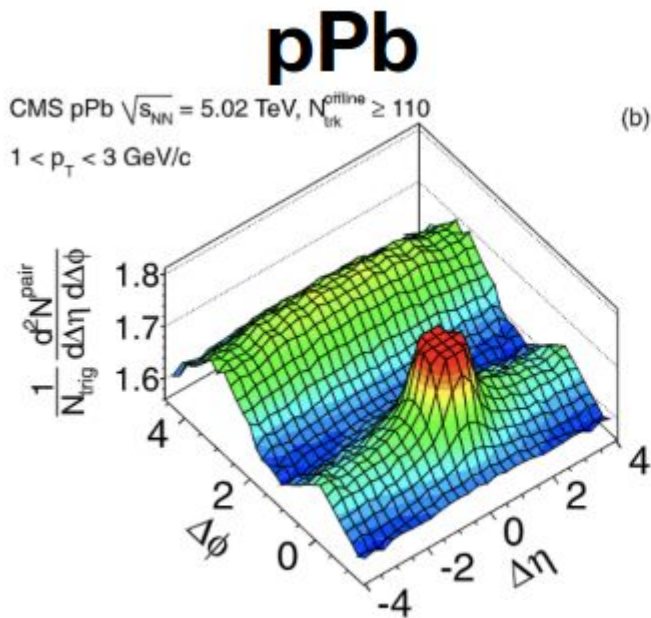
ATLAS setup:  $0.147 < \Delta < 0.205$



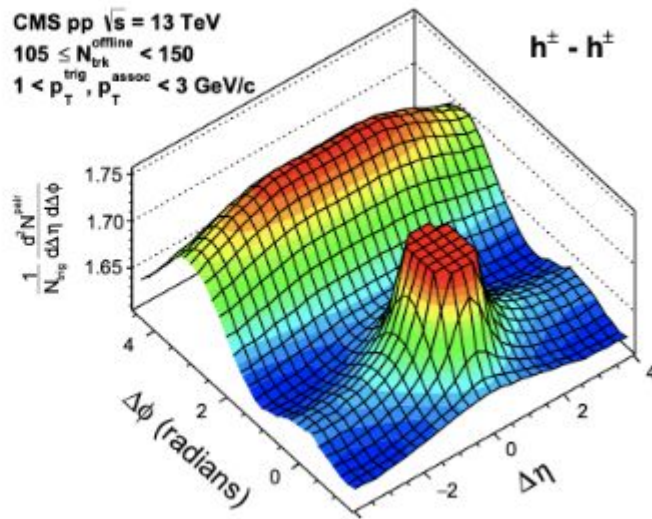
A. Lifson, G. Salam, G. Soyez [JHEP10\(2020\)170](#)

data from ATLAS Lund plane,  
[PRL 124, 222002 \(2020\)](#)

# Ridge in pPb and high-multiplicity pp

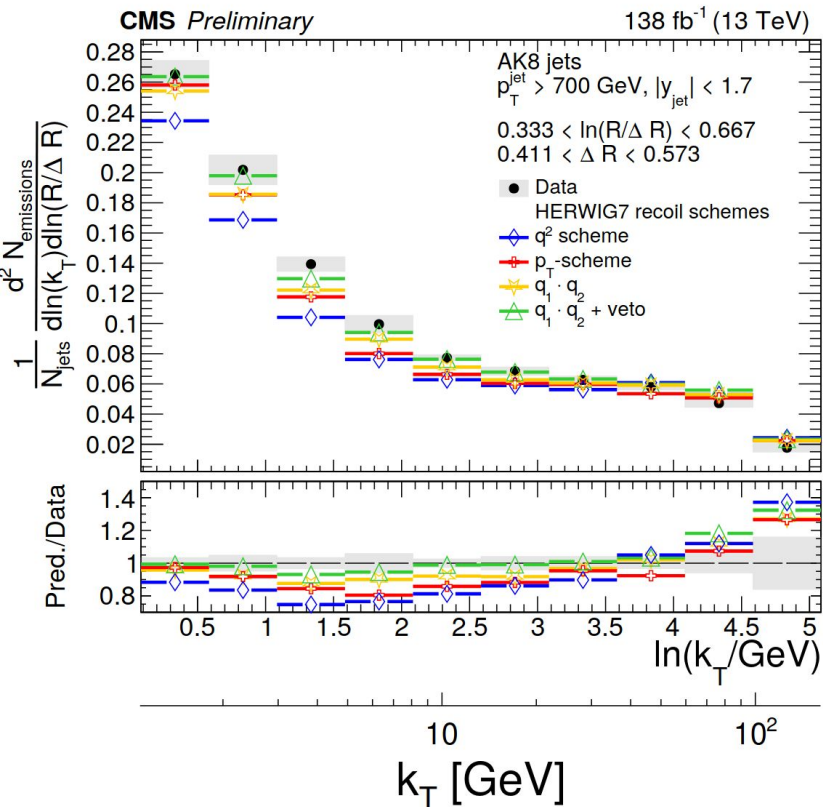


## High-multiplicity pp

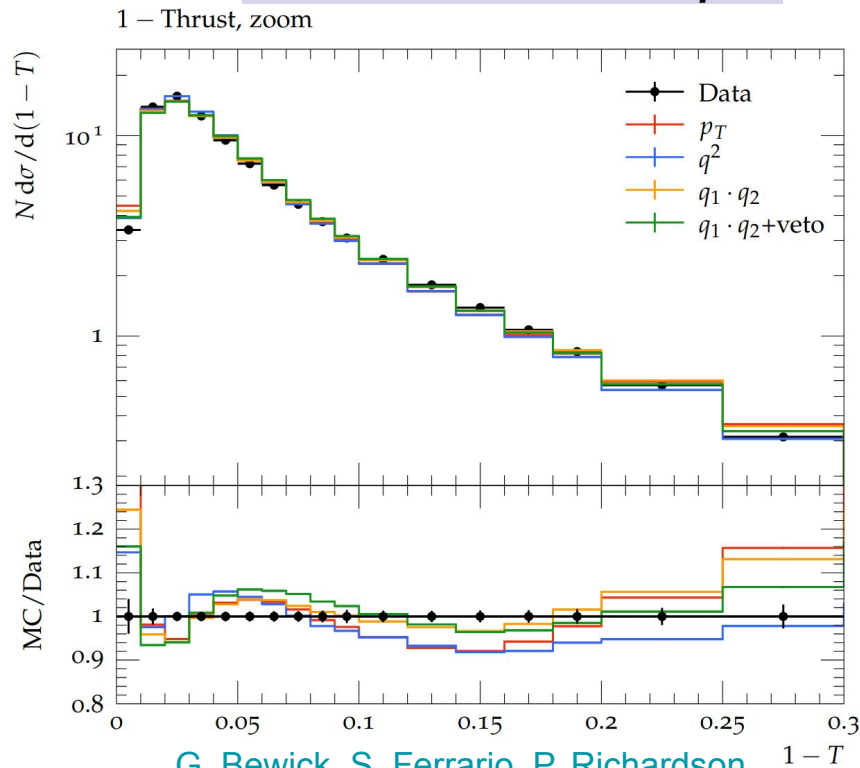


# Sensitivity to recoil scheme choice, important ingredient to reach NLL accuracy

## high- $p_T$ quark and gluon jets



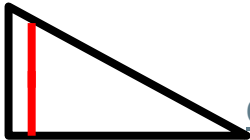
## Thrust in $e^+e^-$ at Z mass pole



[G. Bewick, S. Ferrario, P. Richardson, M. H. Seymour, arXiv:1904.11866](#)

LJP data favors  $q_1 q_2 + \text{veto}$  scheme, consistent with trends in event shape variables at LEP

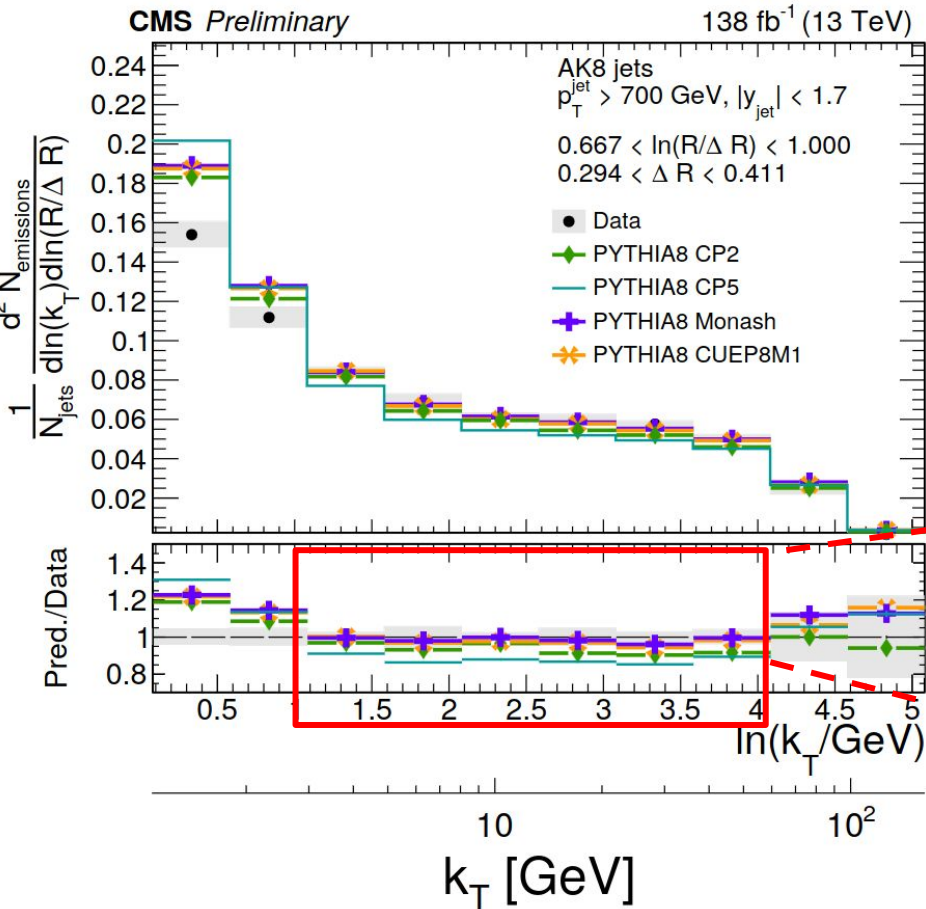
Large angle emissions



$R = 0.8$  Most important difference between PY8 tunes is  $\alpha_s^{\text{FSR}}$

CMS-PAS-SMP-22-007

$$\frac{1}{N_{\text{jets}}} \frac{d^2 N_{\text{emissions}}}{d \ln(k_T) d \ln(R/\Delta R)} \simeq \frac{2}{\pi} C_R \alpha_s(k_T)$$



**Monash/CUEP8M1:**  $\alpha_s^{\text{FSR}}(m_Z) = 0.1365$   
*(best description)*

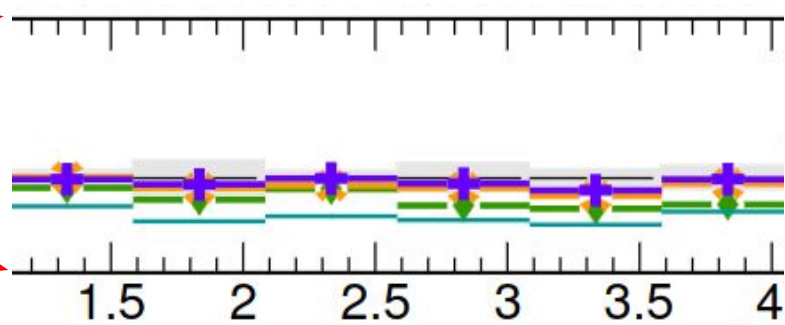
**CP2:**  $\alpha_s^{\text{FSR}}(m_Z) = 0.130$

**CP5:**  $\alpha_s^{\text{FSR}}(m_Z) = 0.118$

LJP data can be used to constrain  $\alpha_s^{\text{FSR}}(m_Z)$  for MC tuning



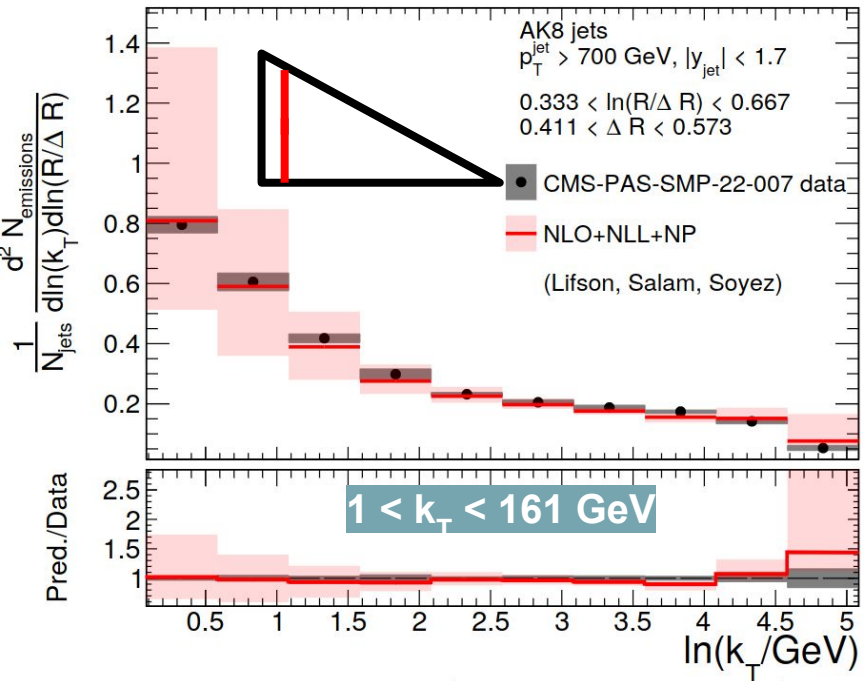
~15%



$k_T$  between 3 – 50 GeV

# pQCD analytical calculations (NLO+NLL+NP)

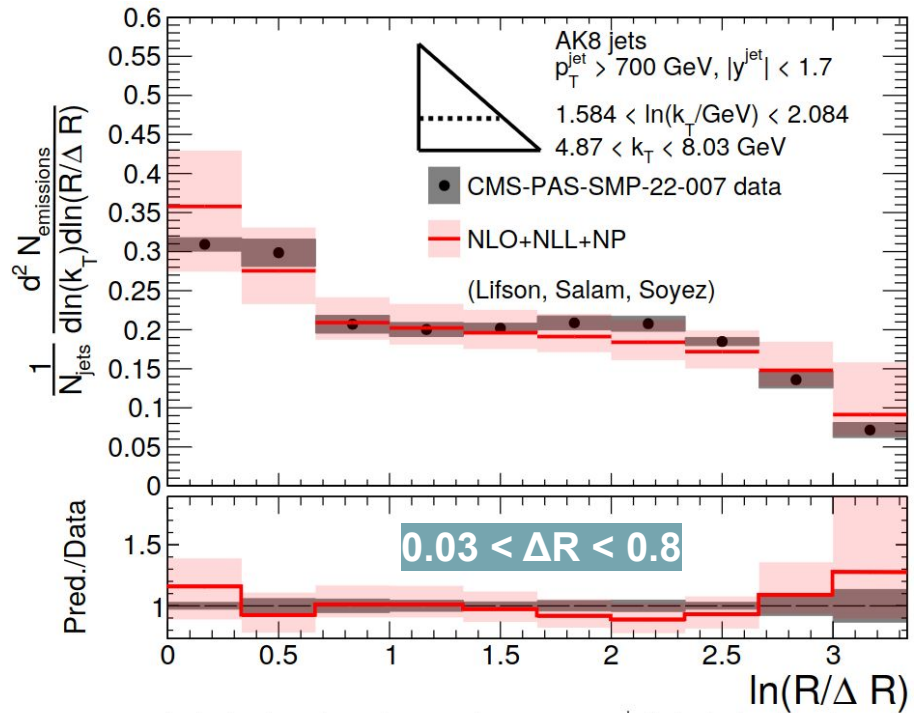
based on A. Lifson, G. Salam, G. Soyez [JHEP10\(2020\)170](#)



10      10<sup>2</sup>

$k_T$  [GeV]

nonperturbative      resummation  
 (unc. mostly perturbative)



0.8      10<sup>-1</sup>

$\Delta R$

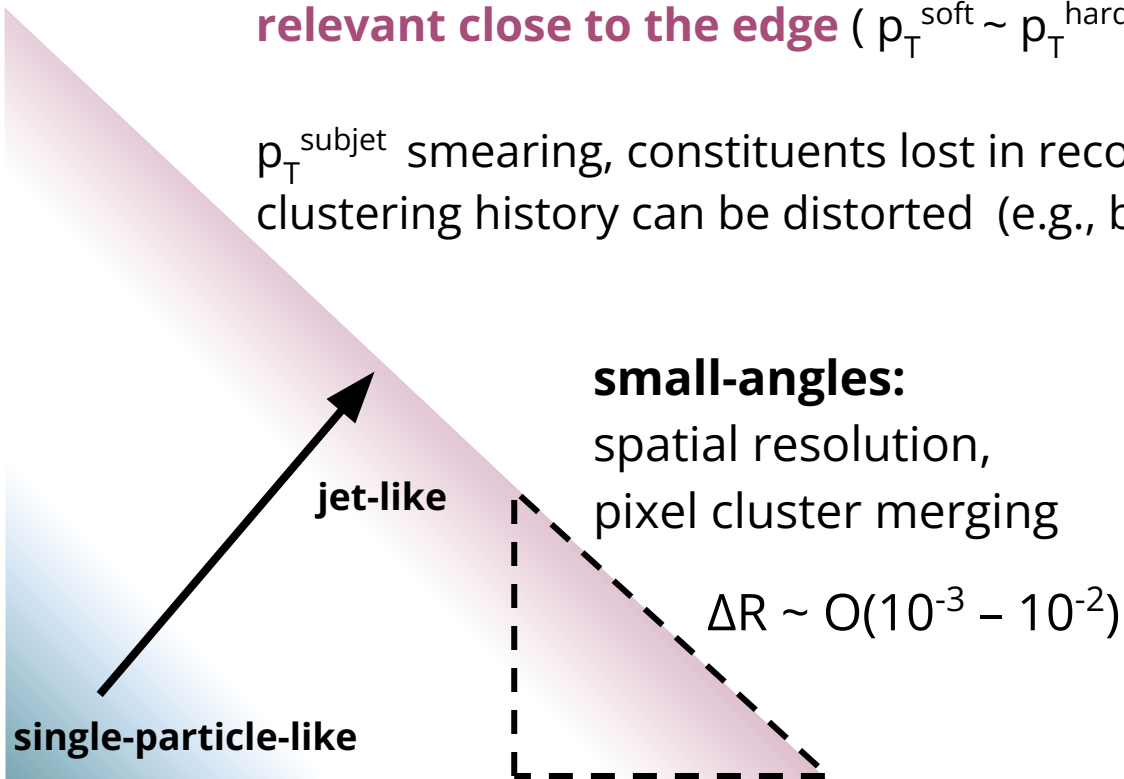
← Nonglobal logs, clustering logs

# selected detector effects

relevant close to the edge ( $p_T^{\text{soft}} \sim p_T^{\text{hard}}$ ):

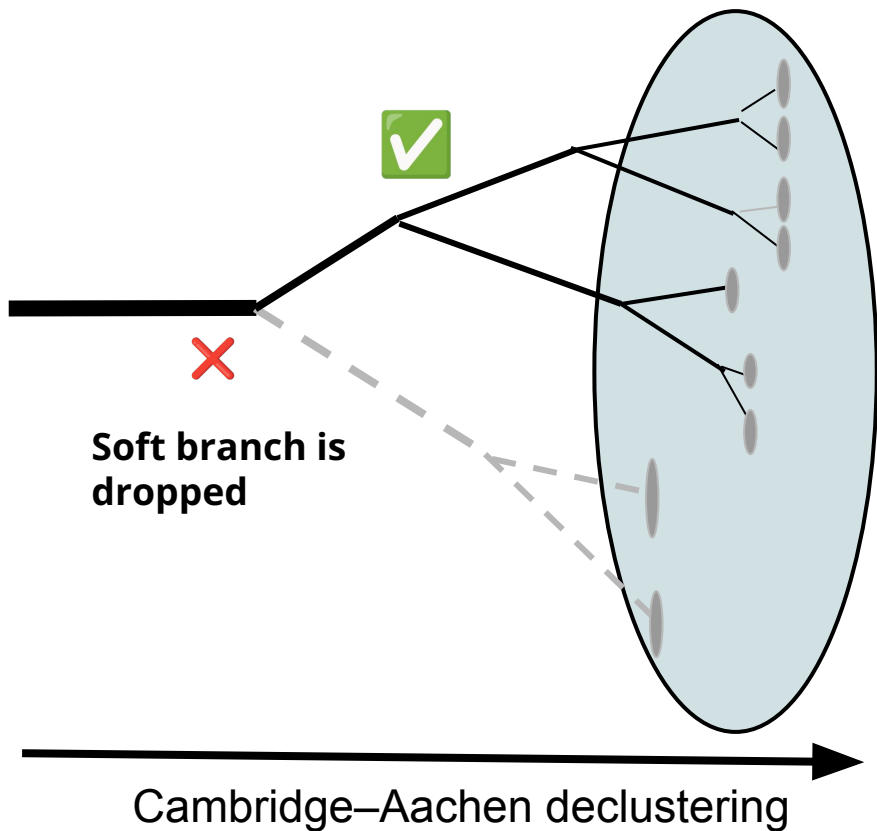
$p_T^{\text{subject}}$  smearing, constituents lost in reconstruction, clustering history can be distorted (e.g., branch swaps)

residual PU  
contributions  
(large  $\Delta R$ ,  
low  $k_T$ )





# (Intermezzo) soft-drop grooming algorithm



1. Jet is reclustered with Cambridge–Aachen (CA), which clusters particles with **angular ordering**
2. Follow the CA clustering history in reverse. Check if the branch satisfies the soft-drop condition:

$$z = p_T^{\text{softer}} / (p_T^{\text{softer}} + p_T^{\text{harder}}) > z_{\text{cut}} (\Delta R/R)^\beta$$

(a typical choice is  $z_{\text{cut}} = 0.1, \beta = 0$ )

If the splitting fails the SD condition, the branch is removed

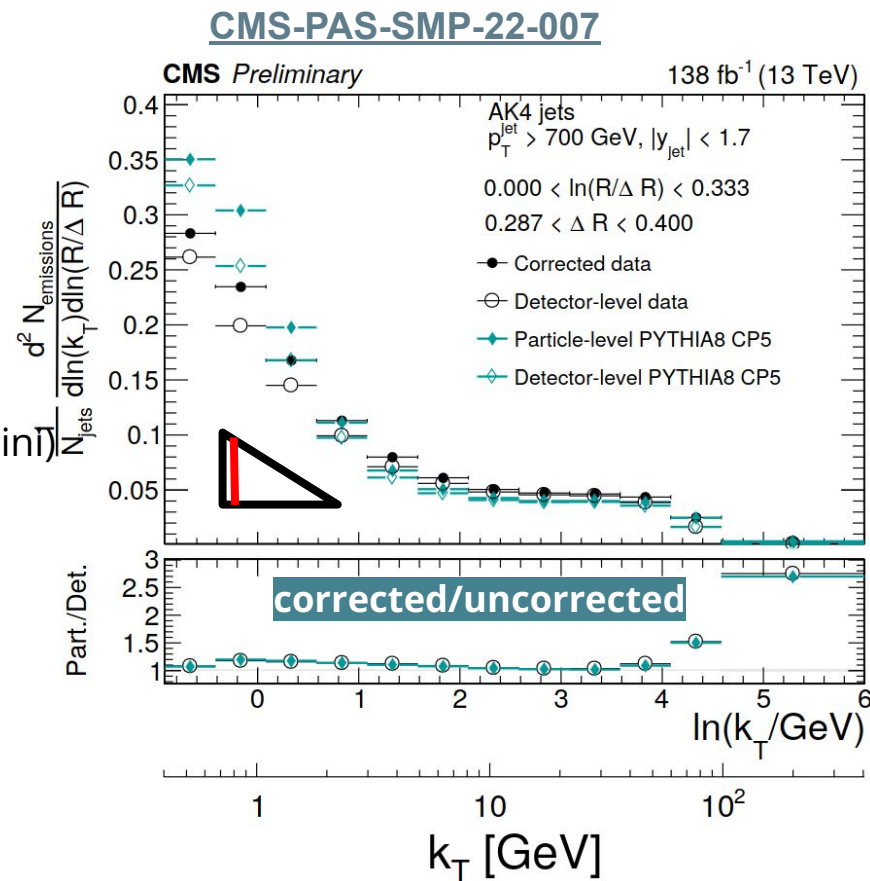
3. Repeat 2 until SD condition is satisfied, which yields a **soft-drop groomed jet**

# Corrections to particle level

Sequential set of corrections:

1. **Background:** bin-by-bin correction to account for det-level emissions not matched to truth-level emissions.
2. **Multidimensional regularized unfolding (D'Agostini)** of primary Lund jet plane ( $p_T^{\text{jet}}$ ,  $k_T$ ,  $\Delta R$ ).
3. **Efficiency:** bin-by-bin correction to account for hadron-level emissions without matching.

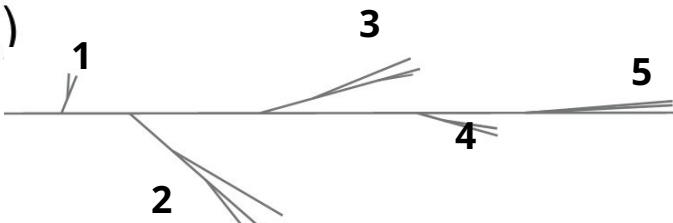
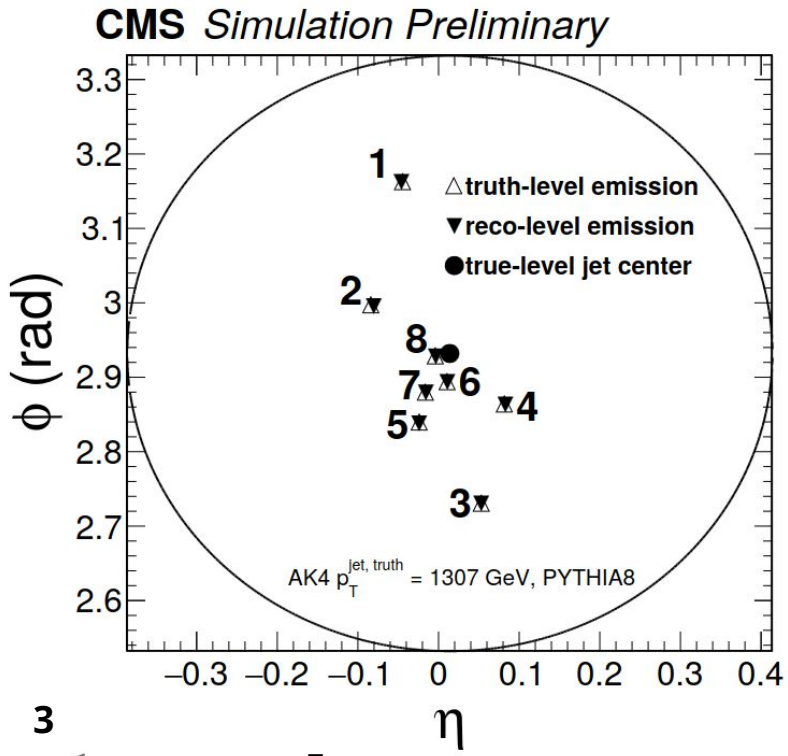
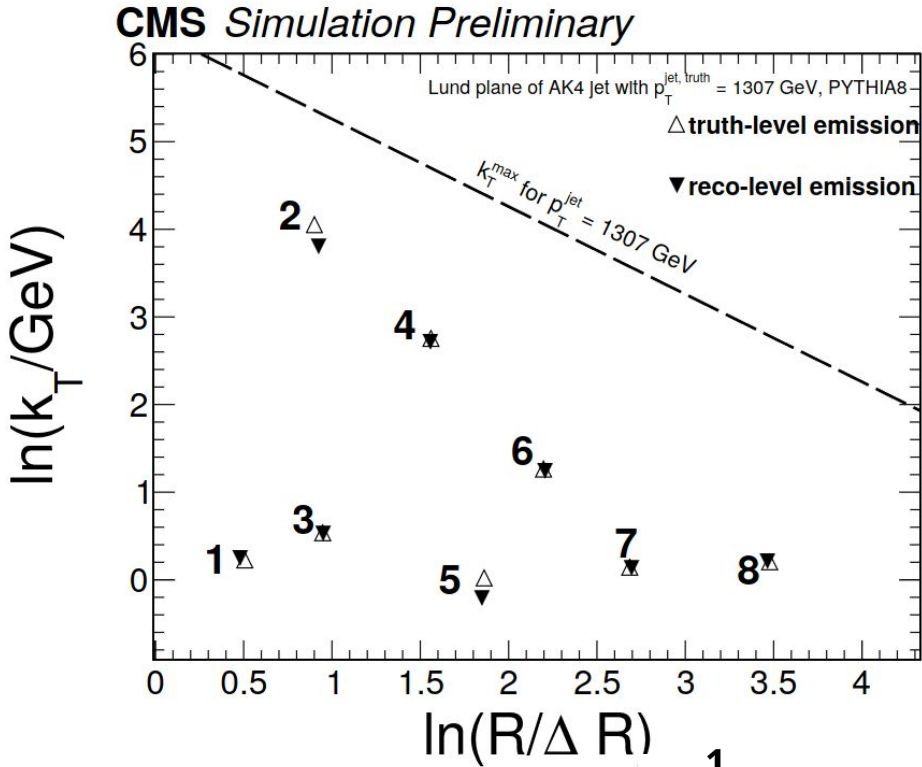
**PYTHIA8 CP5** chosen as nominal to also propagate parton shower scale uncertainties



smearing becomes more important at high  $k_T$

# Matching emissions at detector level and particle level

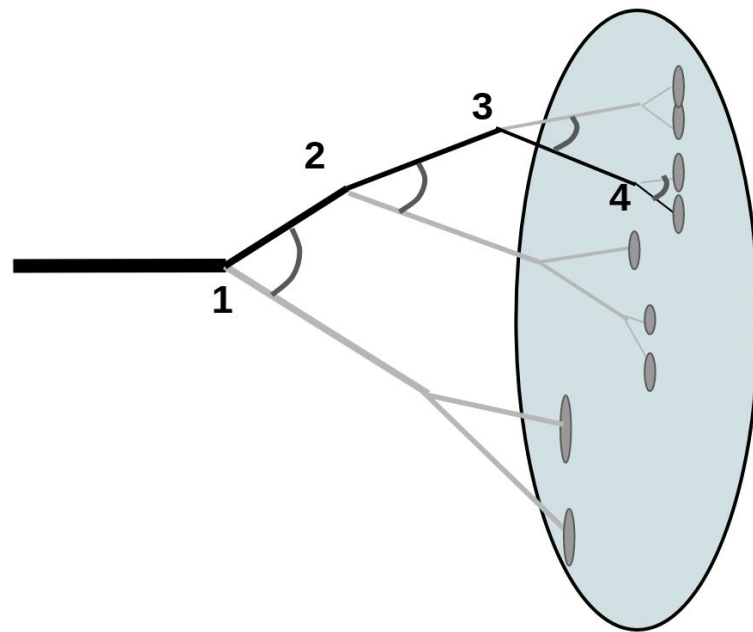
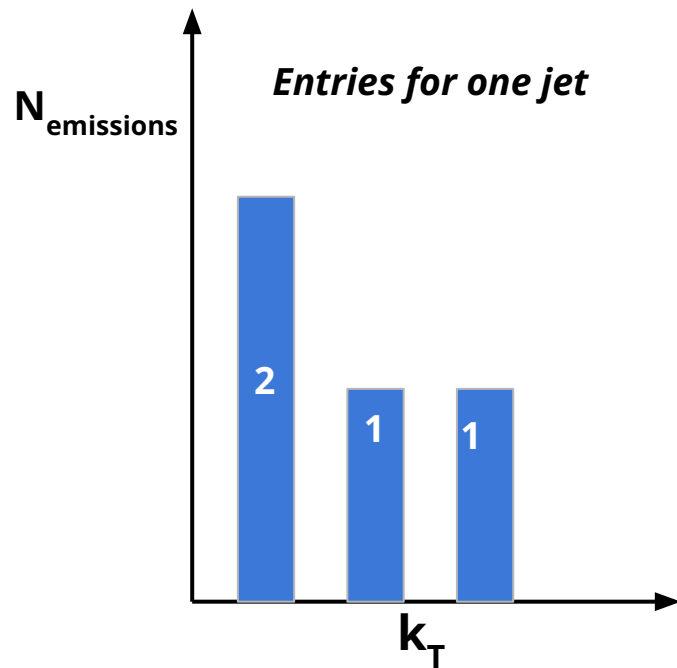
Migration matrix and other MC-based corrections derived from matched part-level and det-level splittings.



[CMS-PAS-SMP-22-007](#)

# detector-level statistical correlations

LJP is a multicomponent observable (i.e., multiple entries per jet) → bins are statistically correlated at det level



bin-to-bin correlations of up to ~5–10%, measured covariance matrix used in unfolding

(can be important for other observables, e.g. Lund multiplicities, energy correlators, ...)

# Systematic uncertainties

**Shower & hadronization model uncertainty**  
(2-7% in the bulk, 10% at kinematical edge)

decorrelated into prior bias  $\otimes$  response pieces

**Tracking reco. efficiency model uncertainty,**  
1-2% in bulk, dominates at 10-20% at edge

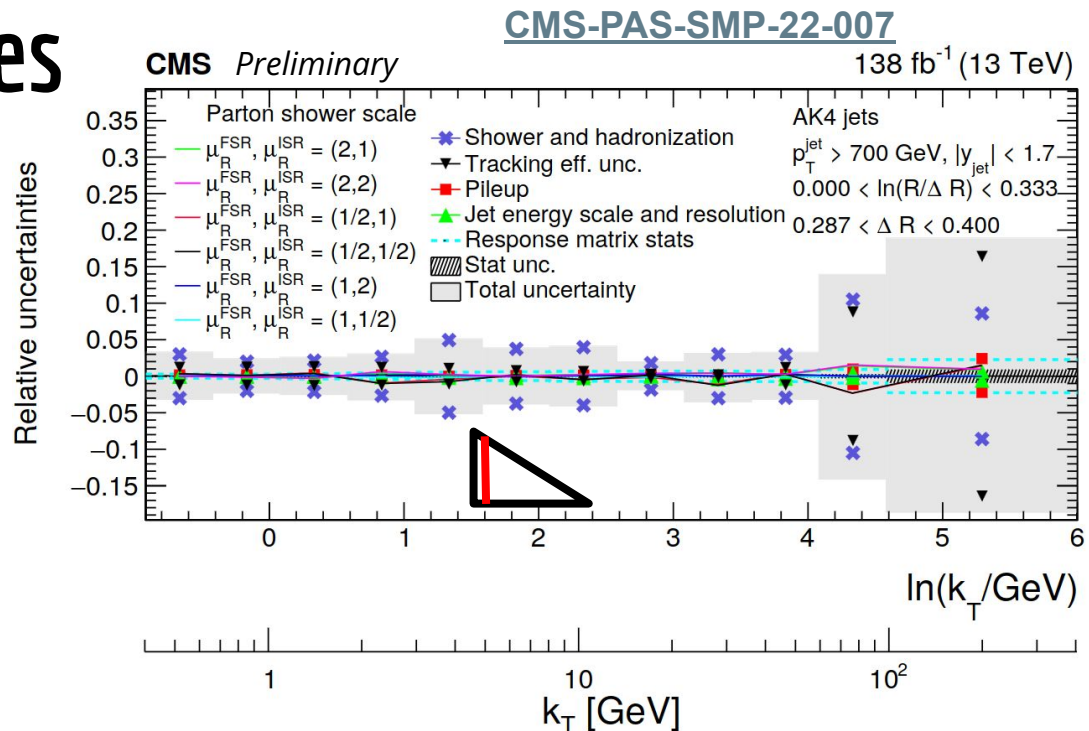
**Subleading components** ( $< \sim 1\%$ ):

Parton shower scale

Response matrix stats

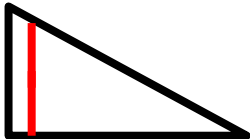
Jet energy scale and resolution uncertainties

Pileup modeling



Dominated by **shower & hadronization modeling** in bulk of Lund plane & by **tracking efficiency** at high  $k_T$

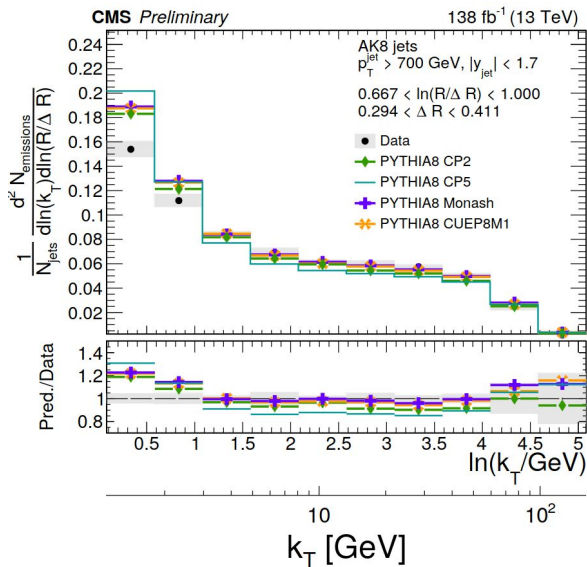
Large angle emissions



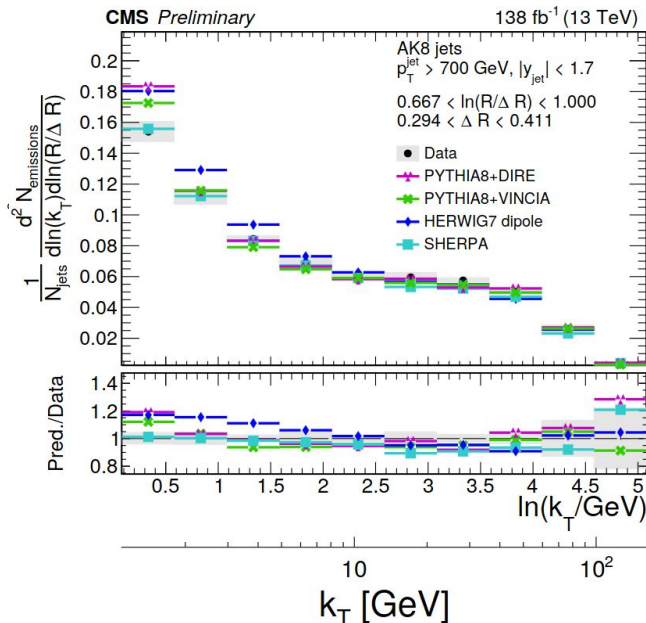
$R = 0.8$

Comparison to parton showers & tunes

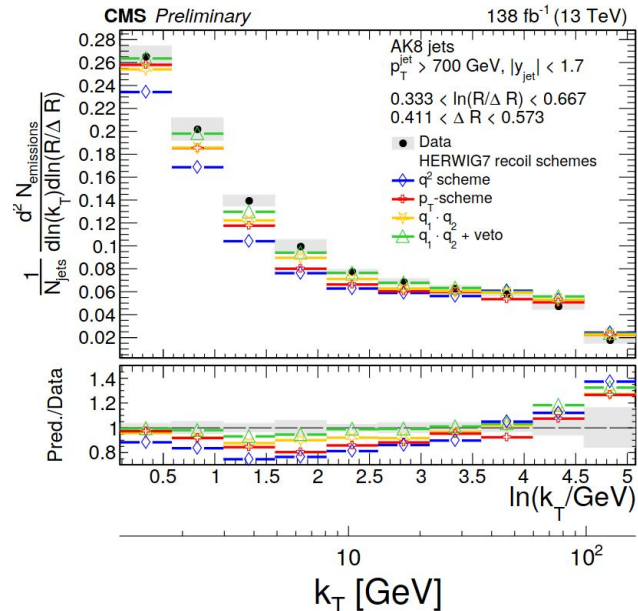
CMS-PAS-SMP-22-007



**PYTHIA8 tunes**  
 (CP2, CP5, Monash, CUEP8m1)



**Dipole showers**  
 (Vincia, Dire, Herwig7 dipole, Sherpa)



**Herwig7 recoil schemes,**  
 (angle-ordered showers)

Data/MC differences of 10–20%. Most important difference for PYTHIA8 tunes is the  $\alpha_S^{\text{FSR}}(m_Z)$  value.

**HERWIG7 angle-ordered** describes better the data than **HERWIG7 dipole**

**Factorization of effects can be exploited in MC tuning**