

Neutron-antineutron oscillation and antinucleon-nuclear interactions

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FuPhy2024

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Outline

1. Neutron-antineutron oscillation
 - Background and today's situations
 - New proposals to improve the sensitivity of the search
2. Antinucleon-nucleus interaction
 - Optical potential model for antiprotons/antineutrons
 - Discuss possible research that can be done in this context

Background: neutron-antineutron oscillation

- Theoretical motivations:
 - Baryon number violation $|\Delta B|=2$
 - Could help distinguish SU(8) and SO(10) GUT models
- Previous measurements:
 - Free neutrons: ILL (1994)
 - Bound neutrons: Super-Kamiokande (2015)

Mean $n\bar{n}$ -oscillation time $> 8.6 \times 10^7$ s, CL = 90% (free n)
 Mean $n\bar{n}$ -oscillation time $> 4.7 \times 10^8$ s, CL = 90% [g] (bound n)

GUT models	Oscillation period $\tau_{n\bar{n}} = 10^6 \sim 10^{10}$ sec ?
$SU(2)_L \times U(1)_Y$ (GWS)	forbidden
minimal SU(5)	forbidden
$SU(4)_C \times SU(2)_L \times SU(2)_R$	yes
SO(10)	too slow
SO(10) with low-E (~ 100 TeV) $SU(4)_C$	yes
E_6	too slow
SUSY-SU(5)	too rapid
SUSY- E_6	yes

R.N.Mohapatra, NIM A284 (1989) 1
 K.S. Babu, R.N. Mohapatra, PLB518 (2001) 269

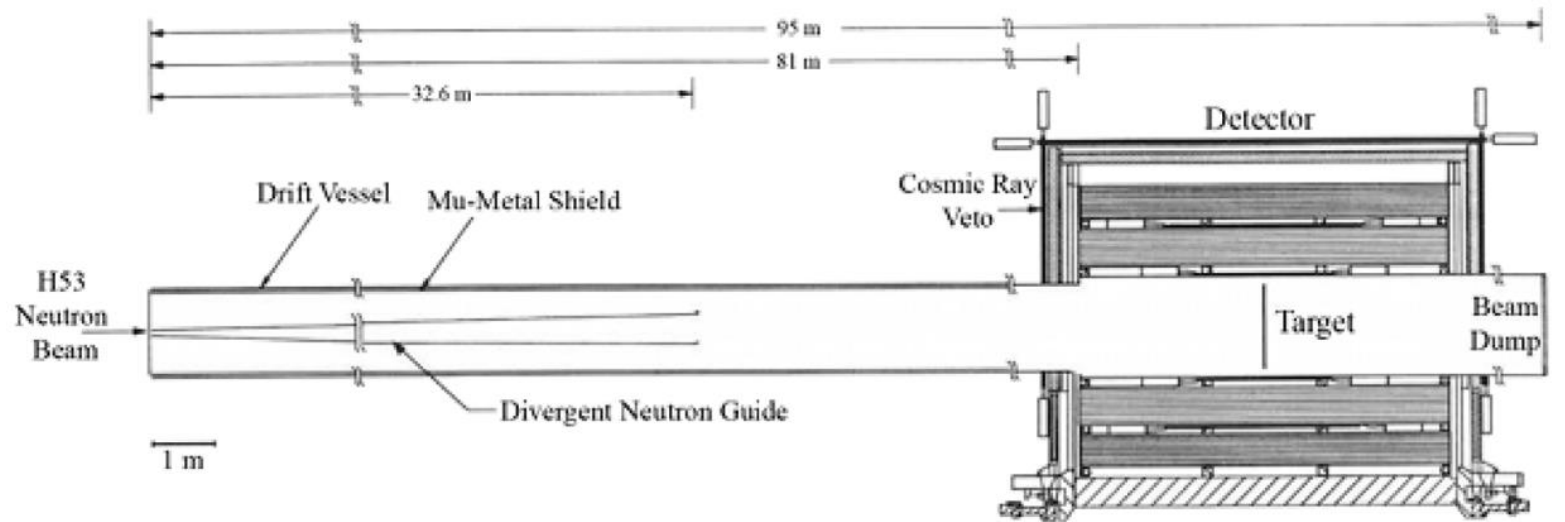
Previous experiment at ILL (1994)

- Cold neutron flux: 2 meV, 1.25×10^{11} n/s
- Flight path: 76.5 m, 0.1 s
- Magnetic field: < 10 nT, pressure: < 0.01 Pa
- Searched for \bar{n} by annihilation to pions (130 μm -thick graphite film as the annihilation target, $\epsilon_{\text{det}} = 0.52$)
- Accumulated observation time: $Y_{\bar{n}} = 2 \times 10^7$ s

$$P_{n\bar{n}} \approx \left(\frac{t_{\text{TOF}}}{\tau} \right)^2$$

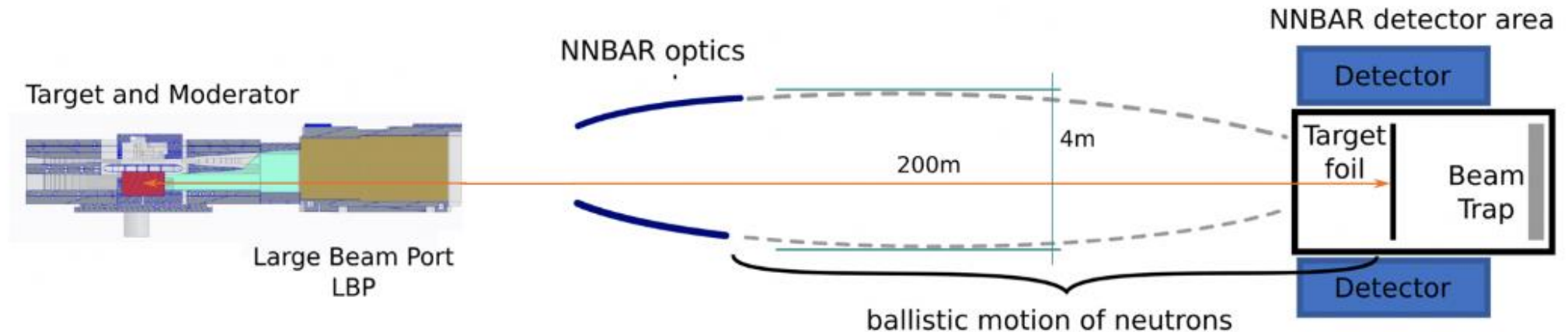
$$Y_{\bar{n}} = \epsilon \cdot \Phi_n \cdot P_{n\bar{n}} \cdot t_{\text{meas}}$$

$$\rightarrow \tau_{n\bar{n}} > 8.6 \times 10^7 \text{ s (90\% C.L.)}$$



Future experiment at ESS

- Spallation neutrons moderated by a cold source: 2.7×10^{15} n/sr/s
- Large-aperture neutron guides (4 m diameter) with neutron optics ($> 4 \text{ \AA}$), Flight path of 200 m
- Factor of $(1000)^{1/2} \sim 32$ improved figure of merit $\sqrt{(N \cdot t^2)}$ compared to the ILL experiment



F. Backman et al, JINST 17, P10046 (2022)

Recent developments:

New proposals in view of the future opportunities (ESS in Sweden, new research reactor in Japan) that involve knowledge of low-energy antineutron-nucleus interactions

Low energy neutron-nucleus interaction (neutron optics)

- At low energy ($\lesssim 10$ meV), neutron-nucleus scattering dominated by the s-wave \rightarrow Fermi potential

Fermi pseudo-potential

$$V_F = \frac{2\pi\hbar^2 N a_0}{\mu}$$

- N : number density of nuclei
- a_0 : the s-wave scattering length
- μ : the neutron-nucleus reduced mass
- For alloy/compound (e.g. NiP):
 $a_0 \rightarrow (a_{0,1}n_1 + a_{0,2}n_2)/(n_1 + n_2)$

Material	s-wave scattering length b (fm)	Fermi potential V_F (neV)
Be	7.778-0.002 i	249.01-0.068 i
C	6.648-0.0009732 i	195.3-0.029 i
P	5.130-0.0478 i	47.53-0.443 i
Ni	10.30-1.248 i	243.5-29.52 i
NiP	—	213.2-0.0229 i

b : bound scattering length $b = \frac{A+1}{A} a$

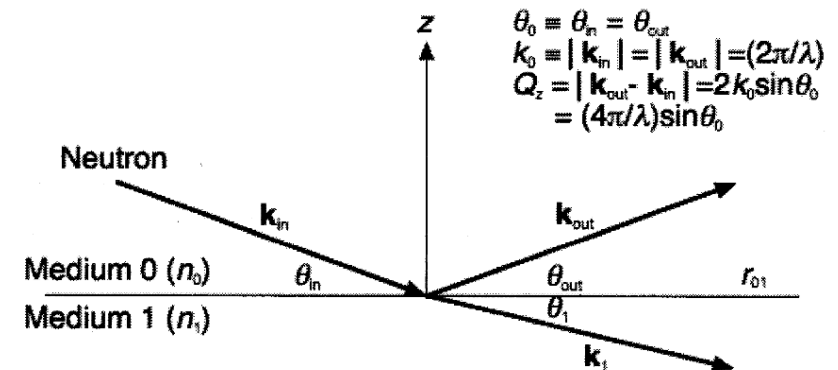
- Totally reflection of neutron with an incident angle $\vartheta \leq \vartheta_c$:

$$E_{\perp} = E (\sin\theta)^2 \leq V_F, \text{ the critical angle } \theta_c = \sin^{-1}(\sqrt{V_F/E})$$

- Ultracold neutrons (UCNs): neutrons with energies $\lesssim 300$ neV

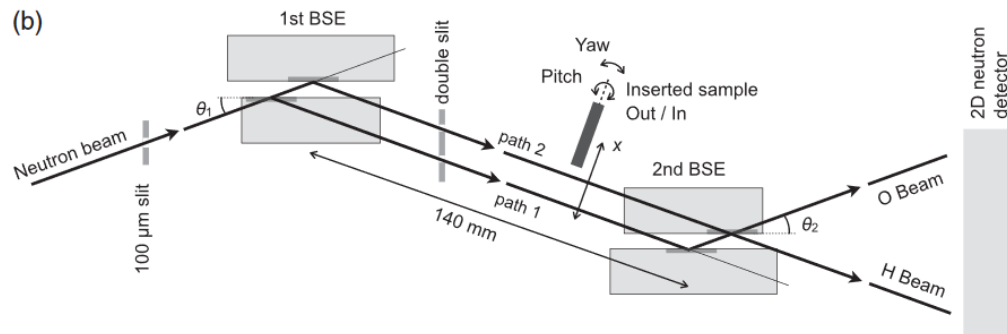
\rightarrow totally reflected with any incident angle

\rightarrow can be stored for time ~ 100 s in material containers



Low energy neutron-nucleus interaction (neutron optics)

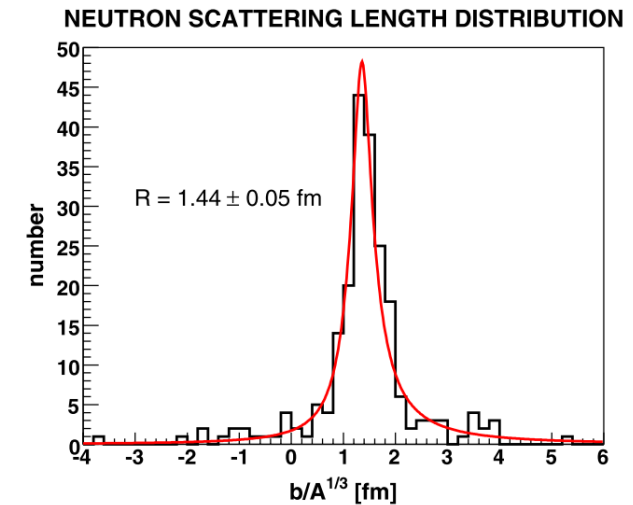
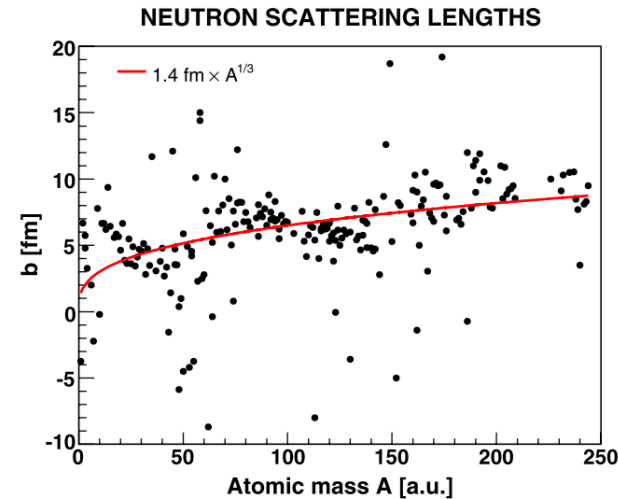
- Experimental determination:
 - Measured by neutron interferometry



- Determined with precision of $\sim 0.1-1\%$

Sample	b_c (fm)
Si ^a	4.060 ± 0.027
Ti	-3.477 ± 0.062
Al	3.408 ± 0.050
	3.423 ± 0.027
	3.466 ± 0.020
V	-0.522 ± 0.004
	-0.520 ± 0.004
V averaged	-0.521 ± 0.003
V-Ni alloy ^c	-0.062 ± 0.001

- Nuclide dependence:



- Largely scales as $A^{1/3}$, but scatters due to the nuclear structures

V.V. Nesvizhevsky, G. Pignol & K.V. Protasov, PRD **77**, 034020 (2008)

Recent proposals for the n-nbar oscillation search

▪ Antineutron mirror:

- (Anti)neutron mirrors to extend the observation time by 10^4
- **10-20%** error on nbar-A scattering length is acceptable
V. V. Nesvizhevsky et al. *Phys. Rev. Lett.*, **122**, 221802 (2019)
K. V. Protasovet al. *Phys. Rev. D*, **102**, 075025 (2020)

▪ Use of ultracold neutrons (T. Shima 2023):

- Use of stored ultracold neutrons instead of a neutron beam
- Design a material vessel coating which has the identical n/nbar Fermi potential to **a few %**
T. Shima: NEWS colloquium, [RCNP Osaka \(2023\)](#)

▪ Neutron-gas interaction to compensate the magnetic field:

- Pre-select the spin state of a neutron beam, fill the neutron path with gas which cancels the magnetic potential (loosen the magnetic field requirement $S = (2\vec{\mu}_n \cdot \vec{B} - V_n + V_{\bar{n}})$
V. Gudkov et al., *Phys. Lett. B* **808**, 135636 (2020).

→ **Key: the scattering length of antineutrons with nucleus**

→ **Next pages: neutron-material interaction in the n-nbar oscillation**

Formalism of n-nbar oscillation (in vacuum)

$$i \frac{\partial}{\partial t} \begin{pmatrix} \psi_n(t) \\ \psi_{\bar{n}}(t) \end{pmatrix} = \begin{pmatrix} E_n + U_n(t) - i\Gamma_\beta & \varepsilon \\ \varepsilon & E_{\bar{n}} + U_{\bar{n}}(t) - i\Gamma_\beta \end{pmatrix} \begin{pmatrix} \psi_n(t) \\ \psi_{\bar{n}}(t) \end{pmatrix}$$

- In vacuum, $U_n(t) = -|\mu_n| \cdot B$, $U_{\bar{n}}(t) = |\mu_n| \cdot B$ $\omega \equiv U_n - U_{\bar{n}}$
- Starting from $\psi_n(0) = 1$, the oscillation probability is

$$P_{n\bar{n}}(t) = |\psi_{\bar{n}}(t)|^2 = \frac{4\varepsilon^2}{\omega^2 + 4\varepsilon^2} \exp(-\Gamma_\beta t) \cdot \sin^2 \left(\frac{1}{2} \sqrt{\omega^2 + 4\varepsilon^2} t \right)$$

- Quasi-free limit (the potential difference (sufficiently small magnetic field $\lesssim 10$ nT):

$$\omega t \ll 1 \quad \Rightarrow \quad P_{n\bar{n}}(t) \approx \varepsilon^2 t^2 \cdot \exp(-\Gamma_\beta t) = (t/\tau_{n\bar{n}})^2 \cdot \exp(-\Gamma_\beta t)$$

of detected nbar over time : $Y_{\bar{n}} = \epsilon_{\text{et}} \cdot \Phi_n \cdot P_{n\bar{n}} \cdot t_{\text{meas}}$

→ contains $P_{n\bar{n}}$ and thus $\tau_{n\bar{n}}$

Wall interactions in n-nbar oscillation

$$i \frac{\partial}{\partial t} \begin{pmatrix} \psi_n(t) \\ \psi_{\bar{n}}(t) \end{pmatrix} = \begin{pmatrix} E_n + U_n(t) - i\Gamma_\beta & \varepsilon \\ \varepsilon & E_{\bar{n}} + U_{\bar{n}}(t) - i\Gamma_\beta \end{pmatrix} \begin{pmatrix} \psi_n(t) \\ \psi_{\bar{n}}(t) \end{pmatrix}$$

- The n-nbar wall potential difference (quasi-free limit not applicable):

$$\omega_W \equiv U_n(t) - U_{\bar{n}}(t) = O(10^{-7}[\text{eV}]) \gg \varepsilon < 10^{-12} \text{eV} \quad \nu \equiv \frac{1}{2} \sqrt{\omega_W^2 + 4\varepsilon^2}$$

- Solution of the differential equation:

$$\begin{pmatrix} \psi_n(t_W) \\ \psi_{\bar{n}}(t_W) \end{pmatrix} = \exp \left[- \left(iE_n + \frac{\Gamma_\beta}{2} \right) t_W \right] \cdot \begin{pmatrix} \cos \nu t_W + i\omega_W \sin \nu t_W / (2\nu) & -\frac{i\varepsilon}{\nu} \sin \nu t_W \\ -\frac{i\varepsilon}{\nu} \sin \nu t_W & \cos \nu t_W - i\omega_W \sin \nu t_W / (2\nu) \end{pmatrix} \begin{pmatrix} \psi_n(0) \\ \psi_{\bar{n}}(0) \end{pmatrix}$$

→ Suppression of oscillation inside the wall: $\varepsilon/\nu \ll 1$

→ The wave function acquires a phase by going through the wall: $(\cos \nu t_W \pm i\omega_W/(2\nu) \sin \nu t_W)$

- Sensitivity

$$P_{n\bar{n}} \approx (\cos \nu t_W)^{2N} \left(\frac{t_s}{\tau_{n\bar{n}}} \right)^2 \quad Y_{\bar{n}} = \varepsilon_{\text{det}} \cdot \Phi_n \cdot P_{n\bar{n}} \cdot t_{\text{meas}}$$

N : # of wall collisions, t_W : dwell time in the wall

t_s : free flight time between wall interaction

Impact of nbar scattering length to the sensitivity (UCNs)

T. Shima: NEWS colloquium, [RCNP Osaka \(2023\)](#)

$$P_{n\bar{n}} \approx (\cos \nu t_W)^{2N} \left(\frac{t_s}{\tau_{n\bar{n}}} \right)^2 \quad Y_{\bar{n}} = \varepsilon_{\text{det}} \cdot \Phi_n \cdot P_{n\bar{n}} \cdot t_{\text{meas}}$$

Realistic numbers:

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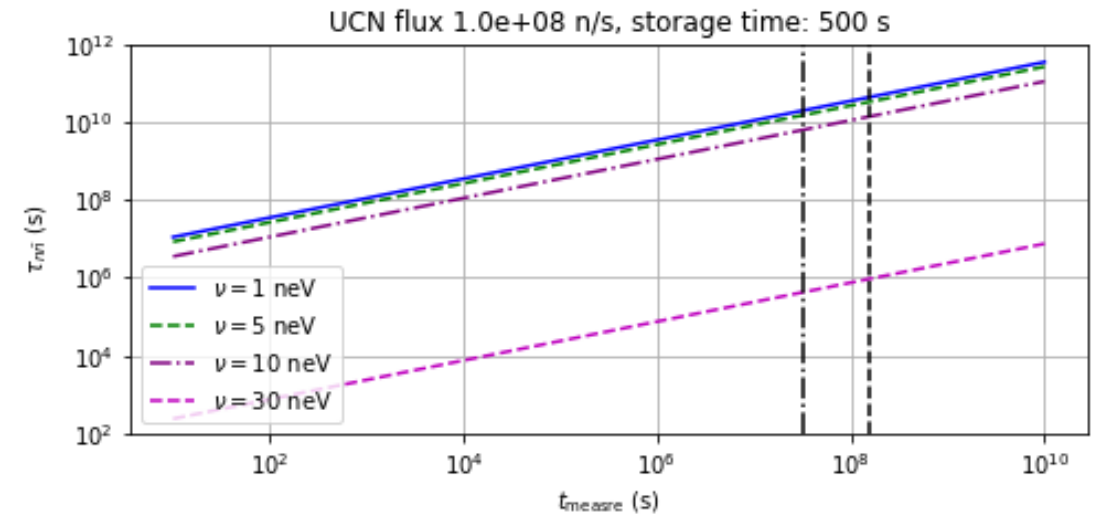
- Free flight time $t_{\text{free}} = 1$ s
- Wall dwell time $t_W \sim 10$ ns
- Number of collisions: $N = 500$
- Storage lifetime: $t_{\text{free}} \times N = 500$ s
- UCN flux: $\Phi_n \sim 10^8/\text{s}$

Wall material:

Al (59%) Mg (41%), theoretically $V_{F,n} = 58.3$ neV, $\nu = 0.5$ neV

E. Friedman & A. Gal, Phys. Rev. D **78**, 016002 (2008)

$\rightarrow \tau_{n\bar{n}} > 10^{10}$ s in 1 year



Very sensitive to the n-nbar potential difference!

Other proposals for the n - \bar{n} oscillation search

- Possible design of coating that has close potentials experienced by n and \bar{n} :
 - Compound/alloy of elements: take number average of the scattering length (e.g. NiP)

Element	Atomic mass	a_{nA} (fm)	$a_{\bar{n}A}$ (fm)	Moler ratio
Al	27.0	3.449	4.29	0.59
Mg	24.3	5.375	4.15	0.41

- $a_{\bar{n}A} = 4.23$ fm, $a_{nA} = 4.37$ fm \rightarrow 1% difference

TABLE I. Parameters that characterize the interaction of \bar{n} with different materials: $b_{\bar{n}A}$ (the scattering length), $U_{\bar{n}}$ (the complex optical potential for this material), $\tau_{\bar{n}}$ (the time of storage of \bar{n} with close-to-zero vertical energy on a horizontal surface in Earth's gravitational field). Calculations for all elements are averaged over the natural isotopic compositions.

Element	$b_{\bar{n}A}$ [fm]	$U_{\bar{n}}$ [neV]	$\tau_{\bar{n}}$ [s]
C	$3.5 - i$	$103 - i29$	1.7
Mg	$3.5 - i$	$39 - i11$	1.0
Si	$3.7 - i$	$48 - i13$	1.2
Ni	$4.7 - i$	$111 - i24$	2.3
Cu	$4.7 - i$	$104 - i22$	2.2
Zr	$5.3 - i$	$59 - i11$	1.8
Mo	$5.3 - i$	$89 - i16$	2.3
W	$6.5 - i$	$106 - i16$	3.0
Pb	$6.7 - i$	$57 - i8.6$	2.3
Bi	$6.7 - i$	$49 - i7$	2.1

V. V. Nesvizhevsky et al. *Phys. Rev. Lett.*, **122**, 221802 (2019)

K. V. Protasov et al. *Phys. Rev. D*, **102**, 075025 (2020)

V. Gudkov et al., *Phys. Lett. B* **808**, 135636 (2020).

Other proposals for the n-nbar oscillation search

- Other proposals:

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- V. Gudkov et al., 2020: Pre-select the spin state of a neutron beam, fill the neutron path with gas s.t. the magnetic potential is canceled to zero (loosen the magnetic field requirement)

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K. V. Protasov et al. *Phys. Rev. D*, **102**, 075025 (2020)

V. Gudkov et al., *Phys. Lett. B* **808**, 135636 (2020).

Antineutron/antiproton-nucleus interaction: available data

- pbar-nuclear scattering/annihilation:
 - pbar elastic scattering: PS184 (D, C, Ca, Pb)
 - ASACUSA : pbar elastic scattering/annihilation at 100 MeV/c (C) and 15.3 MeV/c (125 keV)
 - KEK-E-074: pbar elastic scattering/annihilation at 470-880 MeV/c (C, Al, Cu)
 - ..
- nbar-nuclear annihilation:
 - OBELIX (PS201): nbar annihilation at 100-400 MeV/c
- pbar atom spectroscopy: PS209

Table 1 Experimental results for antinucleon-nucleus interaction at low energies

target	\bar{p} atoms	\bar{p} ann.	\bar{p} scatt.	\bar{n} ann.
C	+		+	+
O	+			
Ne		+		
Al				+
Ca	+		+	
Fe	+			
Ni	+	+		
Cu				+
Zr	+			
Ag				+
Cd	+			
Sn	+	+		+
Te	+			
Pt		+		
Pb	+		+	+
data points	90	7	88	42

E. Friedman, *Hyperfine Interact.*, **234**, 77–84 (2015).

→ No direct scattering data exists for nbar, but the model can be developed upon pbar data, checked by available nbar annihilation data

Optical potential model (Batty-Friedman-Gal)

- Scattering wavefunction

- Only the s-wave amplitude considered: $f(\theta) \rightarrow f_0$

$$\psi = e^{i\mathbf{k}\mathbf{r}} + f(\theta) \frac{e^{i\mathbf{k}\mathbf{r}}}{r},$$

$$\psi = e^{i\mathbf{k}\mathbf{r}} + \int \rho(\mathbf{r}') f_0 \frac{e^{i\mathbf{k}\mathbf{r}}}{|\mathbf{r} - \mathbf{r}'|} \psi_{\text{eff}}(\mathbf{r}'),$$

- "tp model"

$$(\nabla^2 + k^2)\psi(\mathbf{r}) = -4\pi a_0^{\text{eff}} \rho(\mathbf{r})\psi(\mathbf{r}) \quad \Rightarrow \quad V_{\text{opt}} = -4\pi \frac{\hbar^2}{2\mu} a_0^{\text{eff}} \rho(\mathbf{r}).$$

μ : reduced mass
 ρ : nucleon density

$$2\mu V_{\text{opt}}(r) = -4\pi \left(1 + \frac{\mu}{M} \frac{A-1}{A} \right) [b_0(\rho_n + \rho_p) + b_1(\rho_n - \rho_p)]$$

b_0 : iso-scalar scattering length
 b_1 : iso-vector scattering length

- Nucleon density distribution parameterization:

$$\rho_{n,p}(r) = \frac{\rho_{0n,0p}}{1 + \exp((r - R_{n,p})/a_{n,p})}$$

- b_0, b_1 : scattering lengths, R : radius, a : diffuseness of the Woods-Saxon potential

Unified optical potential model approach applied to pbar-atom data

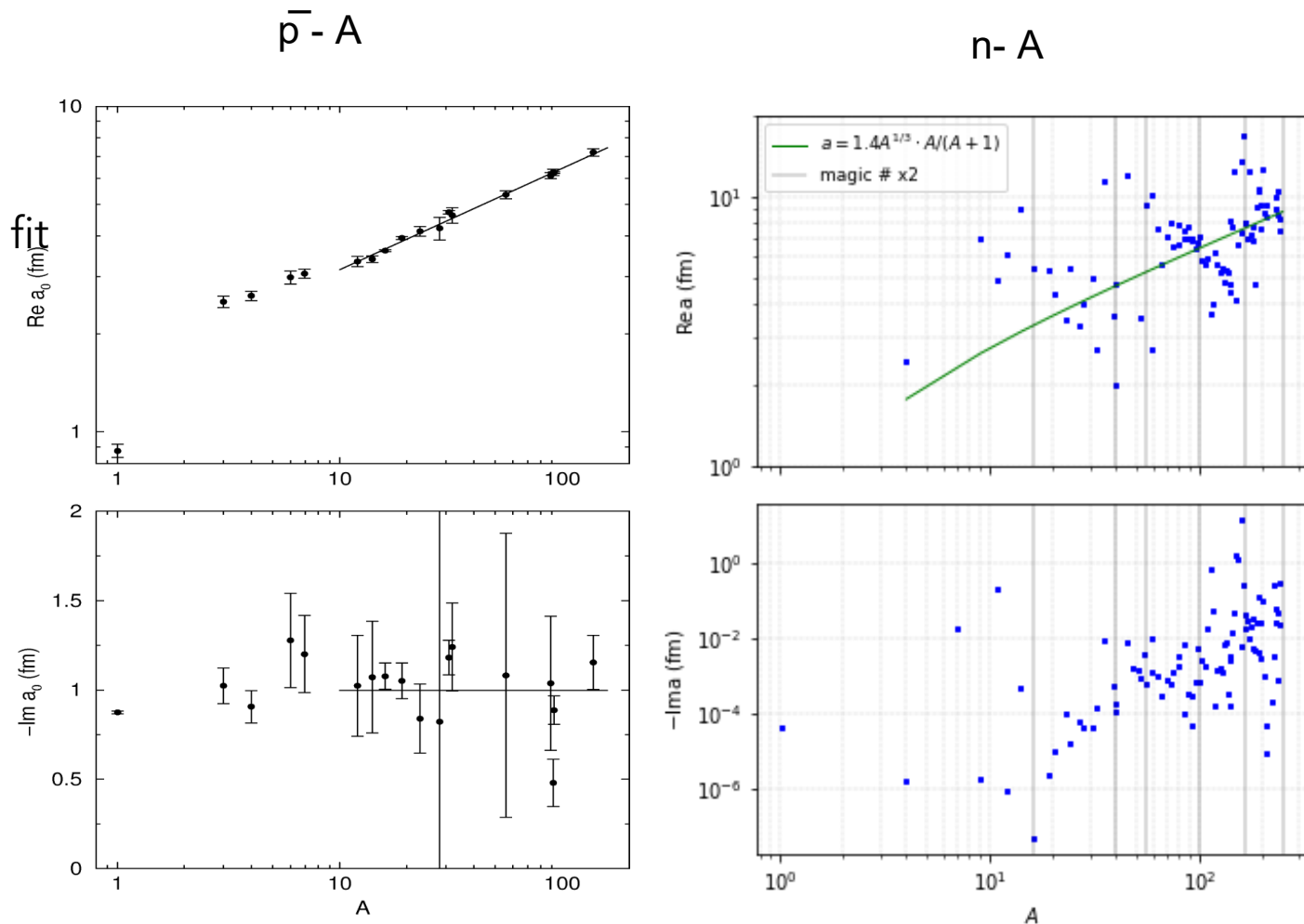
- $\text{Re}(a)$ and $\text{Im}(a)$ can be derived by strong-interaction-induced energy shifts and width of pbar atoms
- Used the pbar-atom data to determine the optical potential model parameters by global fit
 - Good agreement for $A > 10$
- C.J. Batty et al. 2001:
 - Isoscalar model
- E. Friedman et al. 2005: model with different neutron/proton distribution neutron-proton radius fitted by isotope data by PS209
 - Consistent with $\text{Im}(b_1)=0$

$$\text{Re } a_0 = (1.54 \pm 0.03) A^{0.311 \pm 0.005} \text{ fm,}$$

$$\text{Im } a_0 = -1.00 \pm 0.04 \text{ fm.}$$

Parameter uncertainty at % level

2024-04-09



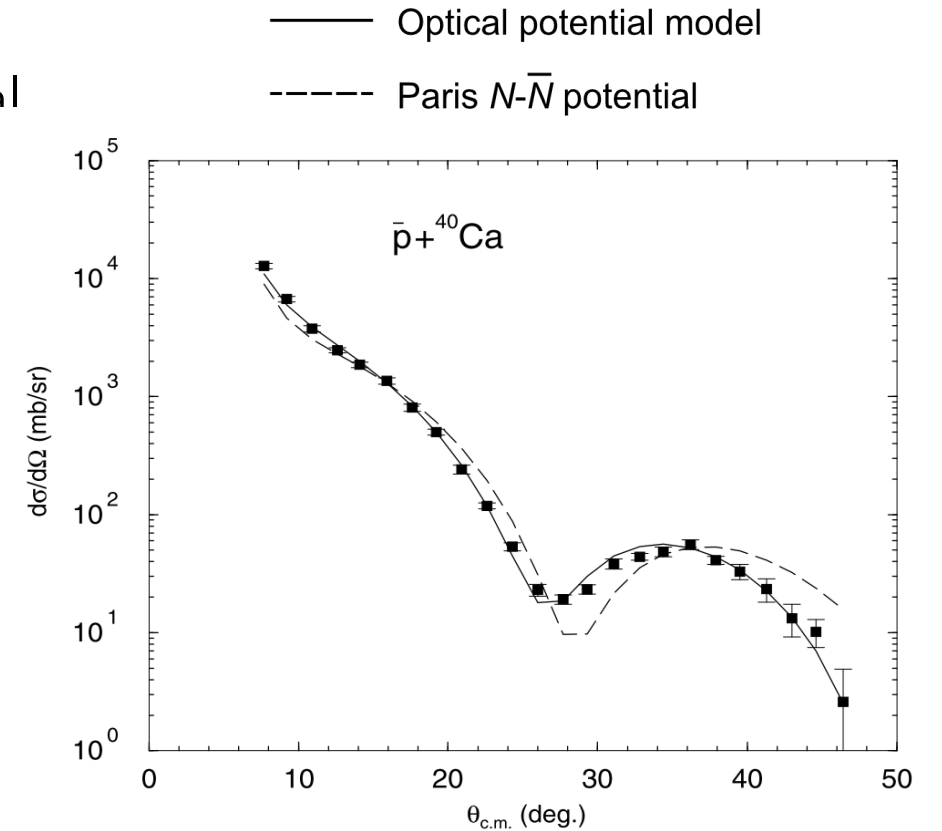
C. J. Batty, E. Friedman, and A. Gal, *Nucl. Phys. A*, **689**, 721–740 (2001).

T. Higuchi, FuPhy2024

E. Friedman, A. Gal, and J. Mareš, *Nucl. Phys. A*, **761**, 283–295 (2005)

Elastic scattering

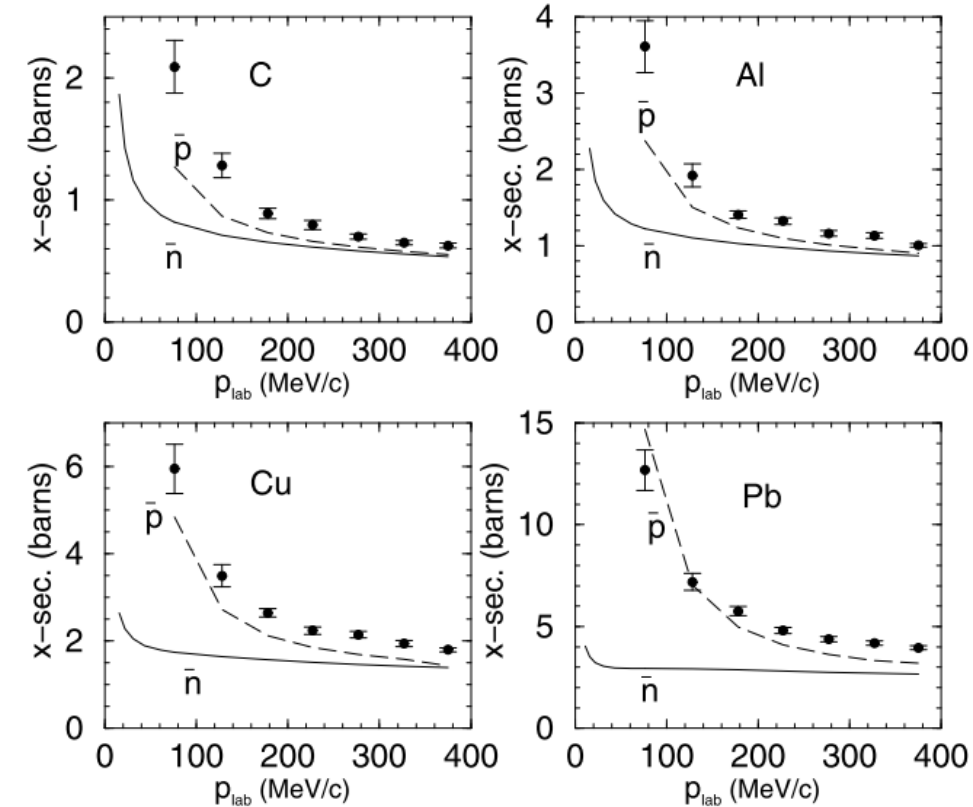
- The simple optical potential reproduces the experimental data better than the Paris N-Nbar potential (at least for this case)
- The same optical potential model works for both the $E < 0$ (bound) and $E > 0$ (scattering) cases



E. Friedman, A. Gal, B. Loiseau, and S. Wycech, *Nucl. Phys. A* **943**, 101–116 (2015).

Discrepancy in the annihilation data

- Annihilation cross section calculated by the optical potential shows a severe discrepancy with the OBELIX nbar data
 - Theory underestimates the cross-section
- Scarce data exists for pbar annihilation at the corresponding energies (100-400 MeV/c) → Recent works by ASACUSA

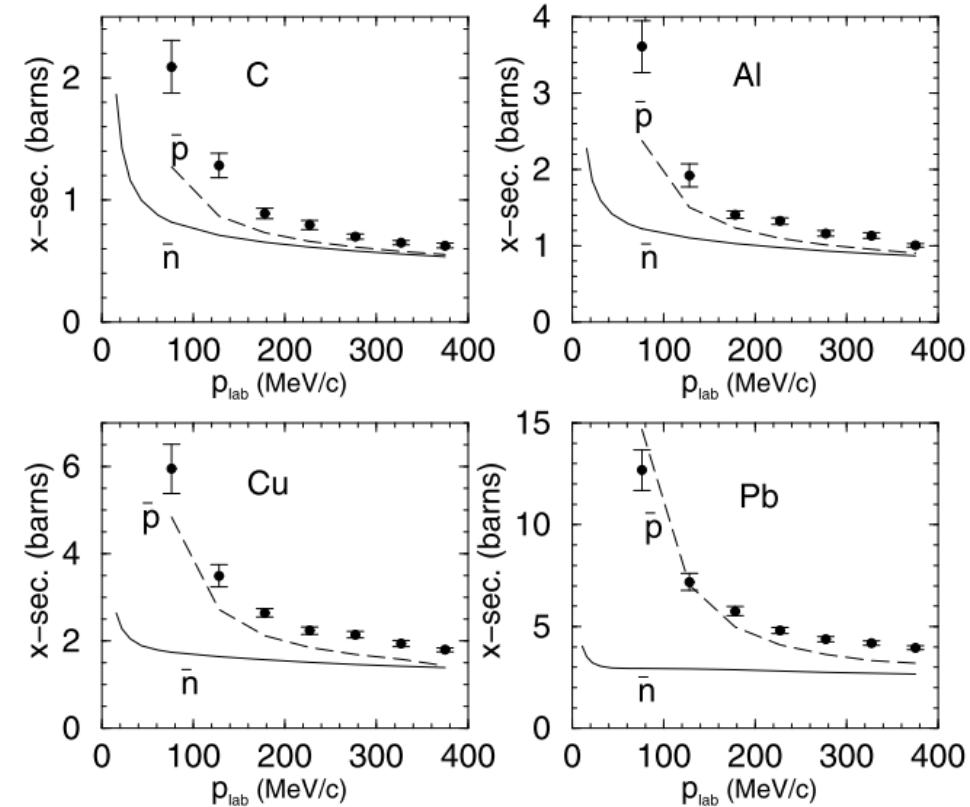
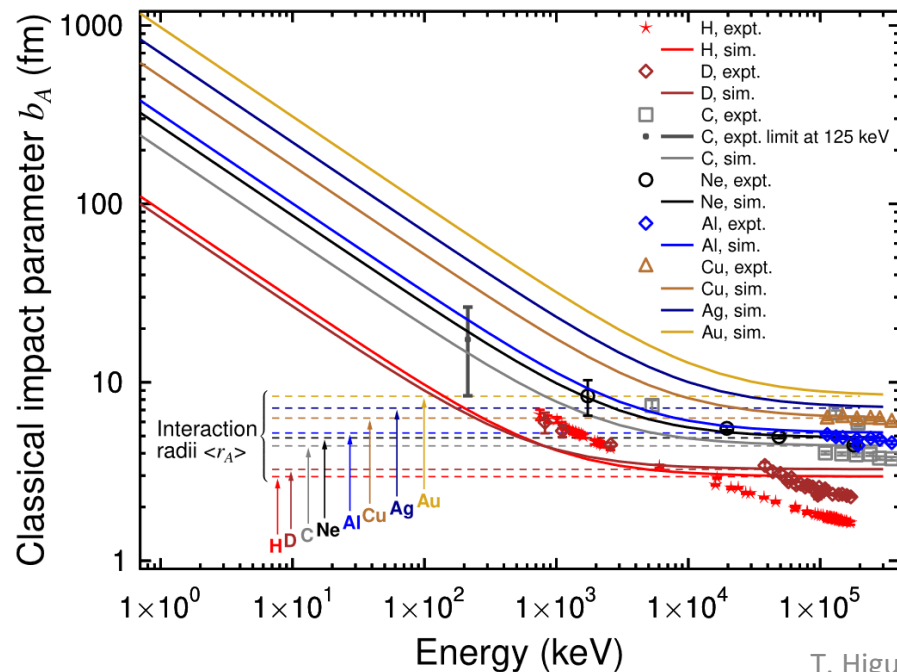


Data ● : nbar experiment (not pbar!)

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Latest summary in unit of classical impact factor $\sigma_A = \pi b_A^2$



Data ● : nbar experiment (not pbar!)

Summary of the situations and proposals

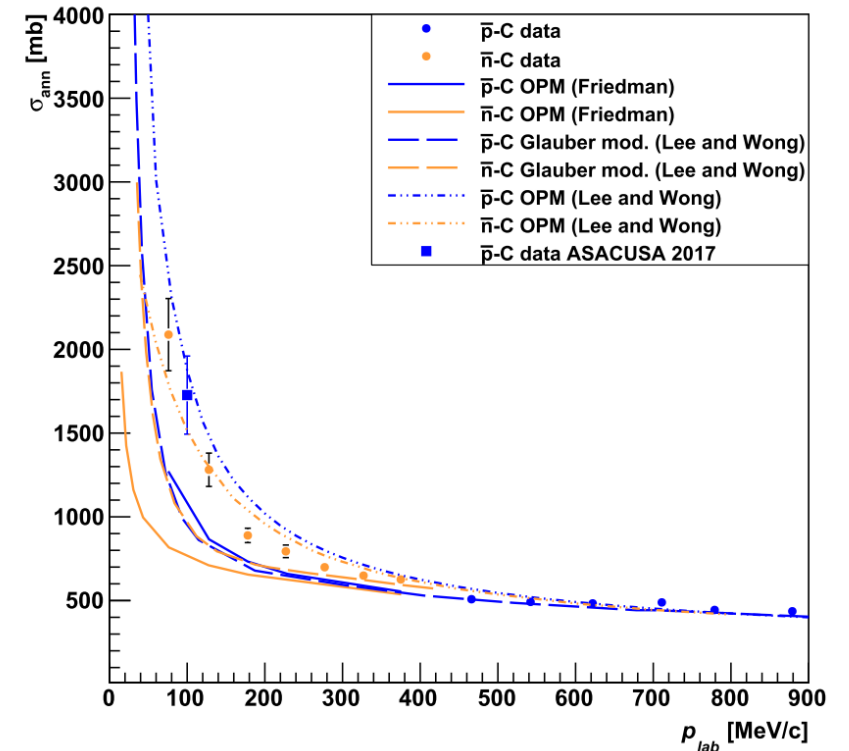
- The optical potential model developed upon the pbar-atom spectroscopy data works well to explain elastic scatterings, but lacks full experimental verification

Possible pbar experiments in this context:

- **Annihilation cross-section measurement** in a 100-400 MeV/c momentum range
 - Future facility providing DC beam with variable momentum would be desirable
 - **Verification of vanishing of isovector terms**
 - Elastic scattering and pbar-atom spectroscopy with isotopes
- ❖ Coordination of theoretical and experimental works are essential

Annihilation cross-section

- Still not enough pbar annihilation data to judge the nbar discrepancy is due to insufficiency of the theory or some experimental systematics
 - More measurements in 100-400 MeV/c desirable, but preferably done at a DC pbar source
- Recently proposed alternative model (Lee and Wong 2018):
 - Employs more complex model of nucleon density distribution (“double diffuseness”)
 - Possible further theoretical investigation based on *ab-initio* nucleon density distribution



H. Aghai-Khozani et al., Nucl. Phys. A, **970**, 366–378 (2018)

Isovector term of the scattering length

$$2\mu V_{opt}(r) = -4\pi \left(1 + \frac{\mu}{M} \frac{A-1}{A} \right) [b_0(\rho_n + \rho_p) + b_1(\rho_n - \rho_p)]$$

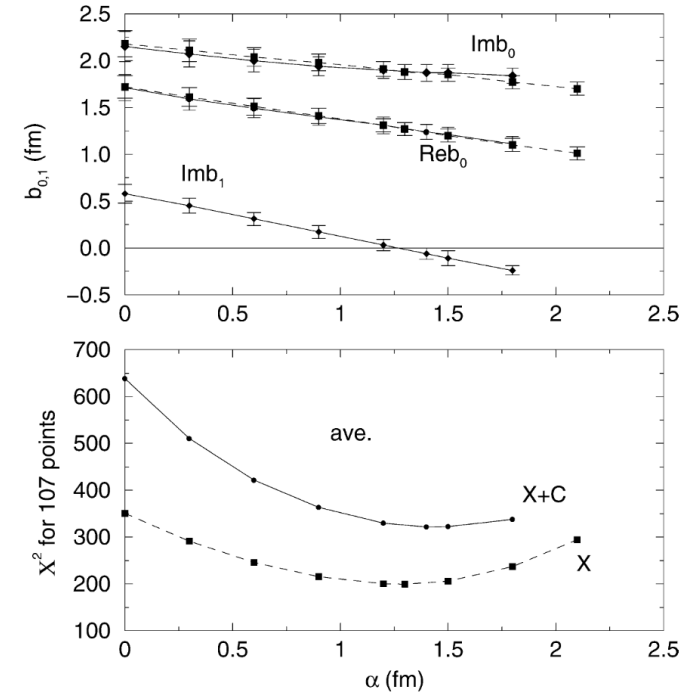
- The negligible iso-vector term $b_1=0$ in the $t\rho$ potential model is the basis of applying the pbar scattering length to nbar studies, but in fact there has never been explicit check
 - In the global fits, b_1 has correlation with proton/neutron density asymmetry parameters
 - E. Friedman et al. 2005:

The vanishing of $\text{Im } b_1$ at the best-fit points for the two acceptable models for neutron densities deserves a comment. We note that the four $\bar{N}N$ potentials considered in Table 3 of Ref. [1] yield for $\text{Im } b_1$ values which are a factor of 10–20 smaller than the corresponding values of $\text{Im } b_0$, so it is conceivable that also for the *effective* phenomenological parameters a similar situation will hold.

Despite the use of many groups of isotopes all along the periodic table, the parameters of the isovector part of the potential could not be determined in *global* fits, and are therefore assumed to be consistent with zero.

- However, the charge independence of pbar-n (\leftrightarrow nbar-p) reaction against pbar-p is not trivial
 - Jean-Marc Richard 2022:

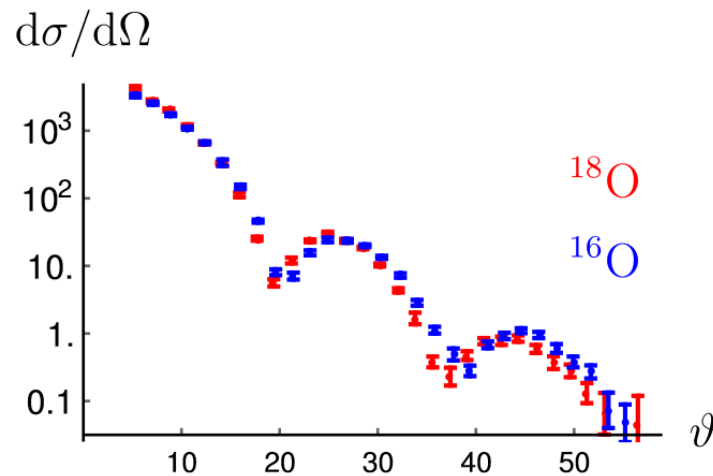
A comparison of ^{16}O and ^{18}O isotopes, see Fig. [11], does not indicate any striking isospin dependence of the $\bar{p}N$ interaction, when averaged on spins. However, at very low energy, some isospin dependence is suggested by the data and analyses by the PSI79 and OBELIX (PS201) [66, 67].



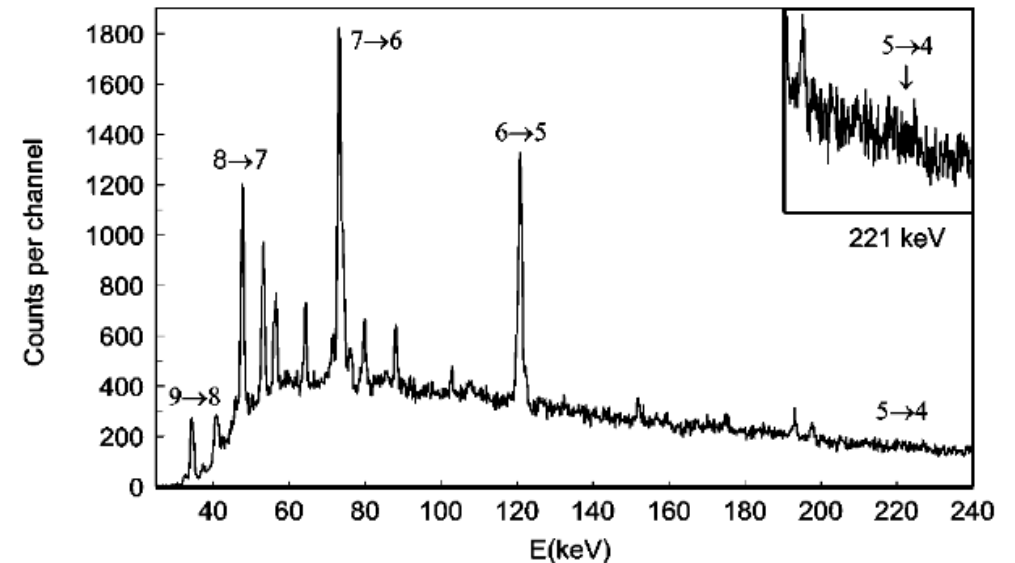
E. Friedman, A.Gal, & J. Mareš, *Nucl. Phys. A*, **761**, 283(2005).
 J-M. Richard, Handbook of Nuclear Physics (2022)

Isvector term of the scattering length

- To explicitly study the isovector term of the scattering length, isotopes with well understood nucleon density distribution are suited, e.g. Ca isotopes
- Scattering (previous study exists for ^{16}O & ^{18}O)
- pbar atom (previous work by PS209, but missing the effectively lowest $(n,l) = (5,4)$ level widths



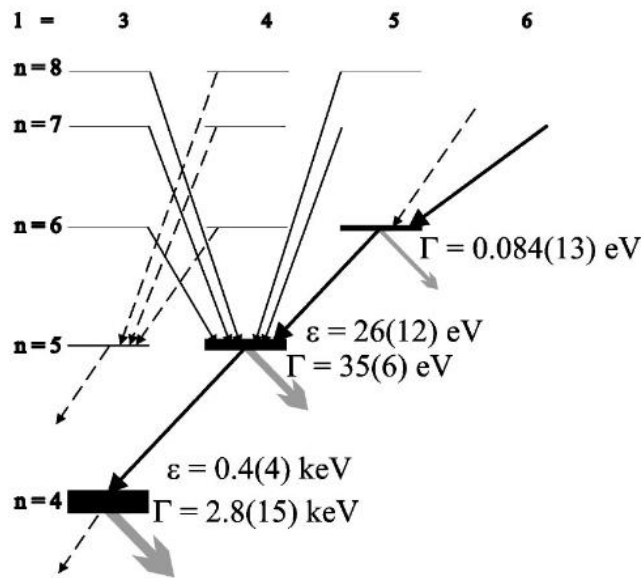
G. Bruge et al. Phys. Lett., **169B**,14 (1986).



G. Bruge et al. Phys. Lett., **169B**,14 (1986).

pbar-Ca spectroscopy by PS209

- Ge detector resolution is not sufficient, so used the intensity balance method to indirectly estimate the width of the transitions
 - The broadening by annihilation causes
- Possibility of applying a superconducting transition-edge sensor (TES) (a few eV resolution) to directly determine the width of the $(n,l) = (6,5) \rightarrow (5,4)$ around 120 keV (cf. Nancy Paul's talk tomorrow)



Strong interaction level widths and shifts determined by PS209 experiment.

Z	A	lower level n, l	Γ_{low} (eV)	ϵ_{low} (eV)	Γ_{up} (eV)	ϵ_{up} (eV)
			A		B	
			A		B	
8	16O	3,2	484(25)	103(10)		
20	40Ca	5,4		5(12)	0.059(18)	
	42Ca			17(14)	0.080(28)	
	43Ca			62(30)	0.073(42)	
	44Ca			31(10)	0.077(23)	
	48Ca			33(12)	0.116(17)	
26	54Fe	5,4	545(45)	155(60)	2.9(6)	
	56Fe		545(54)	167(22)	3.3(5)	
	57Fe		638(35)	164(25)	3.7(4)	
	58Fe		2017(203)	-115(115)	4.1(10)	

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Conclusions

- The precise knowledge of antinucleon scattering length has potential of revolutionize the sensitivity of the neutron-antineutron oscillation search
- The optical potential model of antinucleon-nucleus has sufficient precision ($\sim 1\%$) to be applied to the above purpose, but lacks full experimental verification
- Proposed possibilities of experimental/theoretical studies focusing

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