

# A study of Charge collection noise in the LGAD with Geant4 and TCAD

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Timing resolution  $\sigma_t$  is given by  $\sigma_t^2 = \sigma_{tw}^2 + \sigma_j^2 + \sigma_L^2$

$\sigma_{tw}^2$  : Time walk

$S$  : Pulse height

$\sigma_j^2$  : Jitter

$\sigma_n$  : Noise

$\sigma_L^2$  : Landau noise

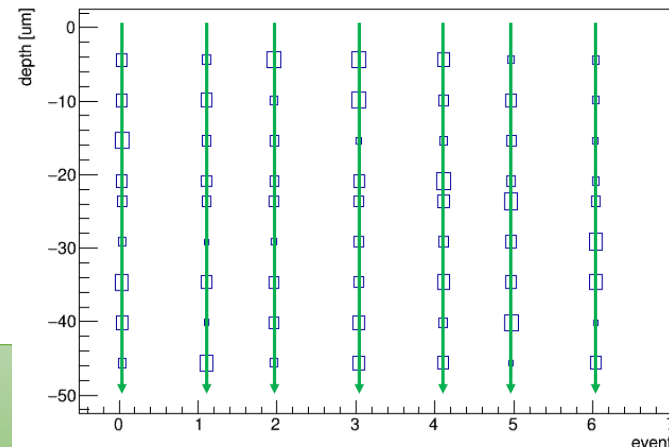
$t_r$  : Rise time

$$\sigma_j = \frac{\sigma_n}{\left| \frac{dV}{dt} \right|} = \frac{\sigma_n}{\left| \frac{S}{t_r} \right|} = \frac{t_r}{\left| \frac{S}{\sigma_n} \right|}$$



arises from varying energy deposit by particle in each event.

MIP Geant4 Simulation



Landau noise : Charge collection noise

Objective :

1. Calculate the magnitude of Landau noise
2. Optimize the sensor thickness

Method : Create a pulse shape using TCAD and Geant4

Geant4 : Energy deposit per event

TCAD: Pulse shape by charge at certain depth



Scale a pulse shape for each event using energy deposit.

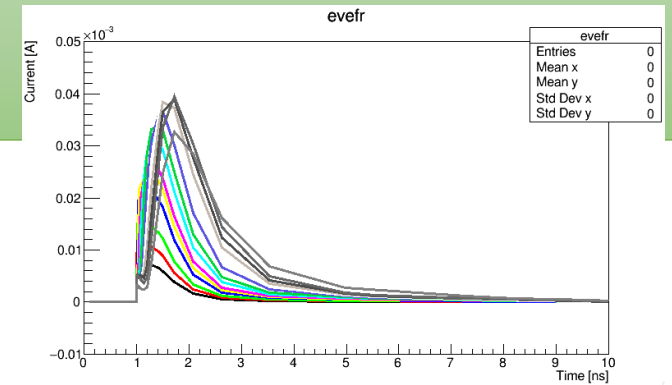


Create a pulse shape in each event.

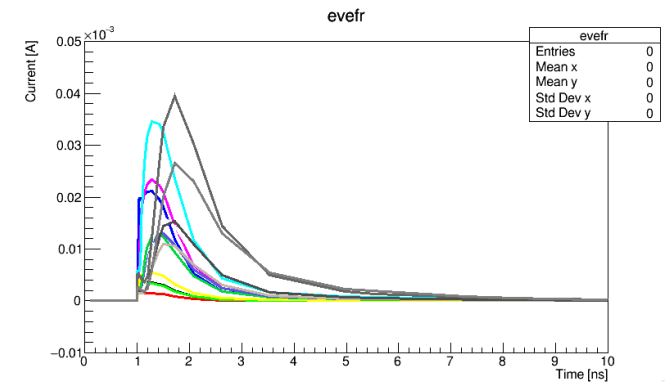
# Method (TCAD&Geant4)

## Pulse shape generation method

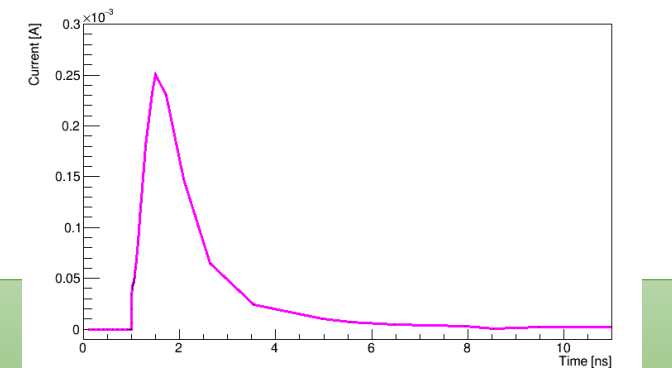
1. Prepare template for the pulse shape for energy deposit at each depth by TCAD.
2. Scaled the pulse height template to the energy deposit simulated by Geant4.
3. Combine all pulse shapes created by 2.



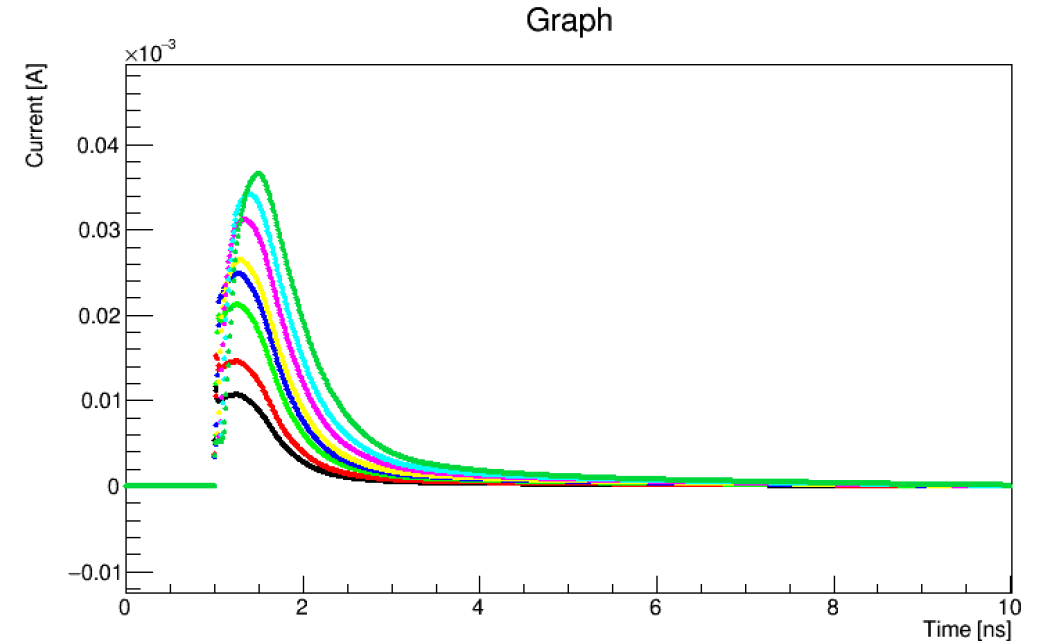
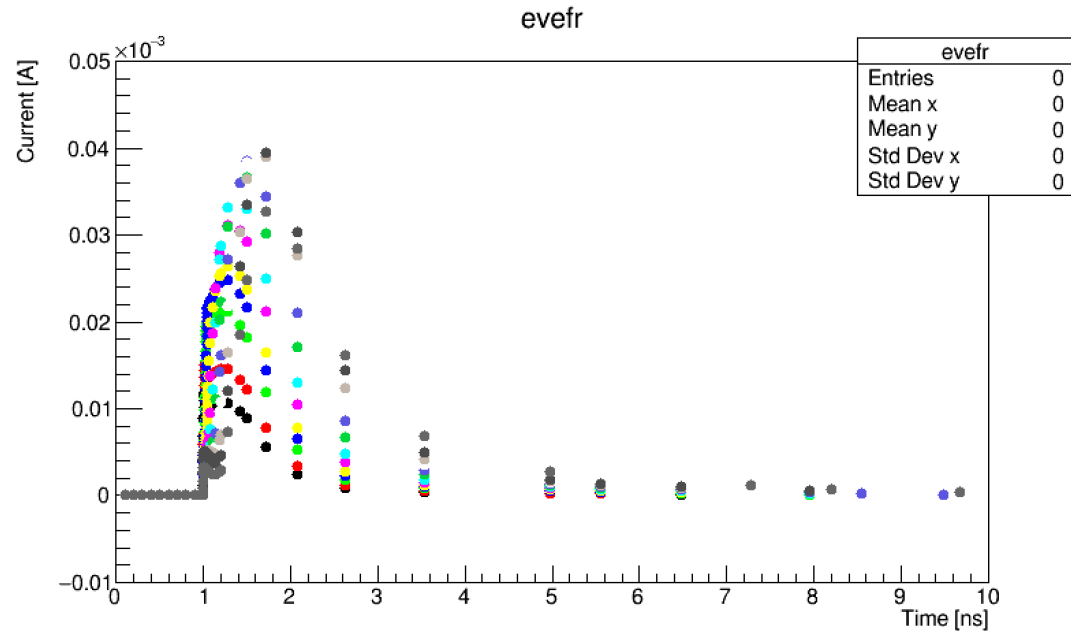
Scaling



Combine



## Interpolation of simulated points



Finding the arrival time is challenging due to non-continuous plots in TCAD.

→ Interpolate between data points.

→ More accurately determining the arrival time at 50% constant fraction.

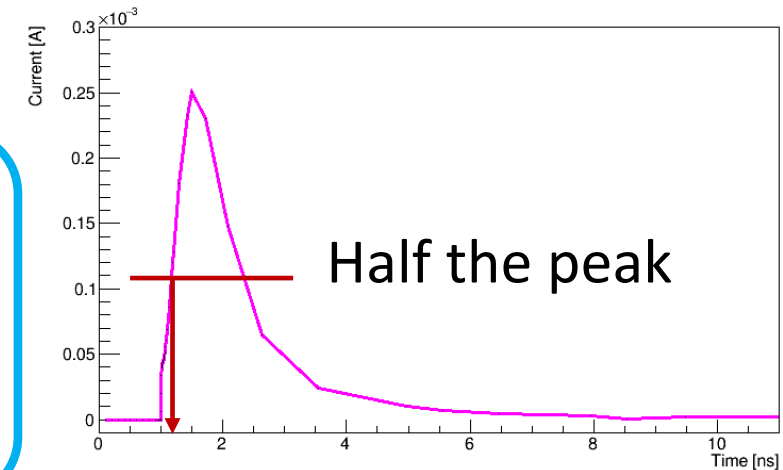
## Arrival time

Defining Arrival time for the Signal : At half the peak  
→ To disregard the term of  $\sigma_{tw}$

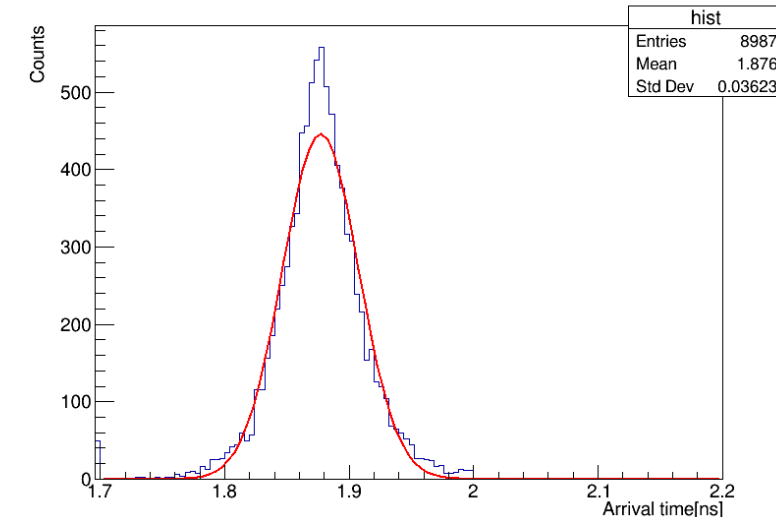
$$\sigma_t^2 = \cancel{\sigma_{tw}^2} + \sigma_j^2 + \sigma_L^2$$

Create pulse shapes for 10,000 events.

1. Find the arrival time of pulse shape in each event.
2. Fill the arrival time of each event to the histogram and fit with a Gaussian.



Arrival time

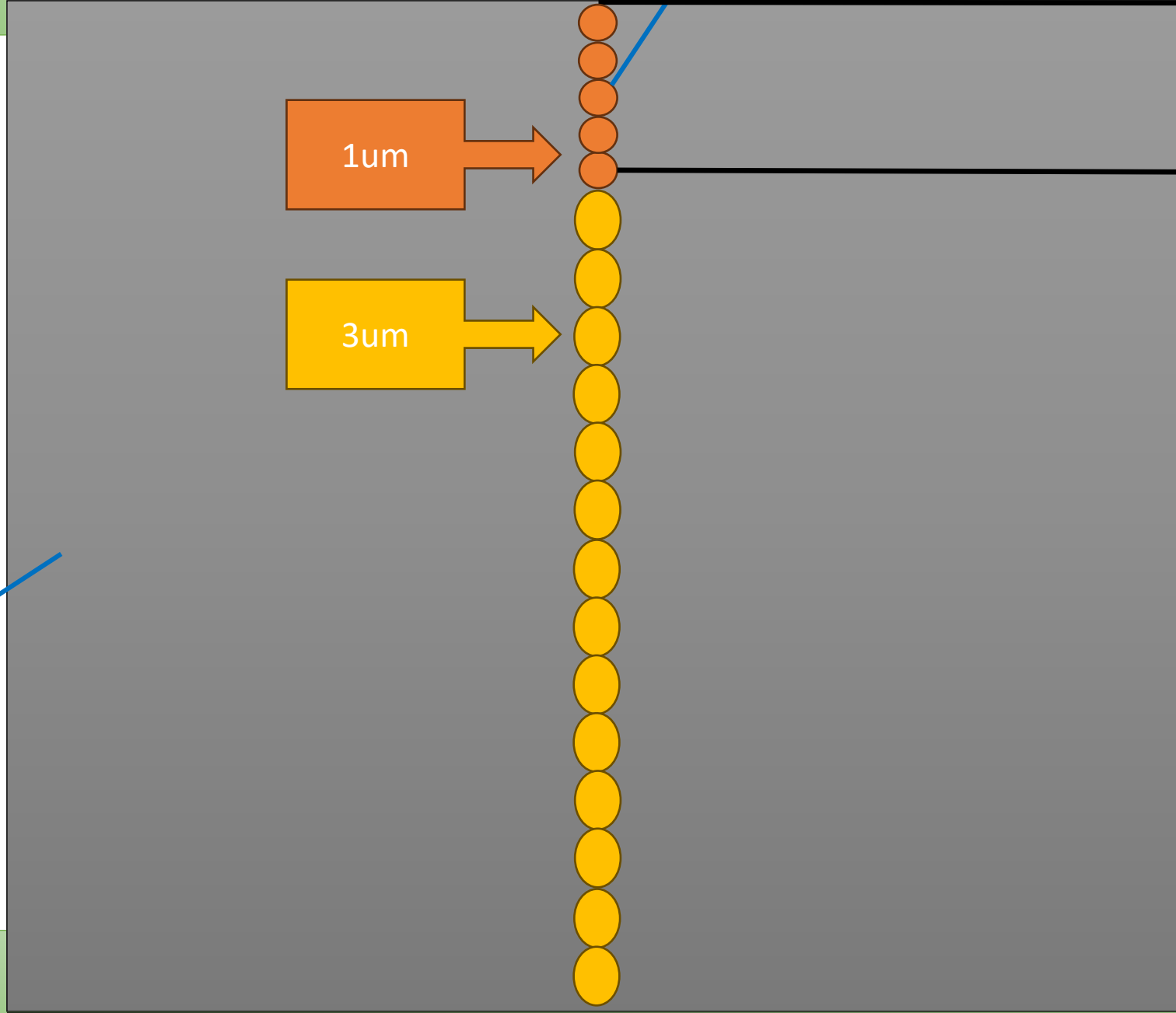


# Set up (TCAD)

Finely segmented line charge near the surface.

Depleted zone

Charge



0um

5um

50um

## The Sensitive Detector region in the LGAD

- Active Thickness

Simulated pulse shape 10, 15, 20 ,30 ,40 ,50um with the same amount of charge at the certain depth.

- Temperature 20 °C

- Bias Voltage for each thickness. → Use the voltage before break down.

Thickness [um]	20	50
Bias Voltage[V]	90	180



## The Sensitive Detector region in the LGAD

- Thickness

Wafer ( Thickness of the supporting wafer ) 150 $\mu$ m

Active Thickness (Thickness of the depleted zone) 10, 15, 20, 30, 40, 50 $\mu$ m

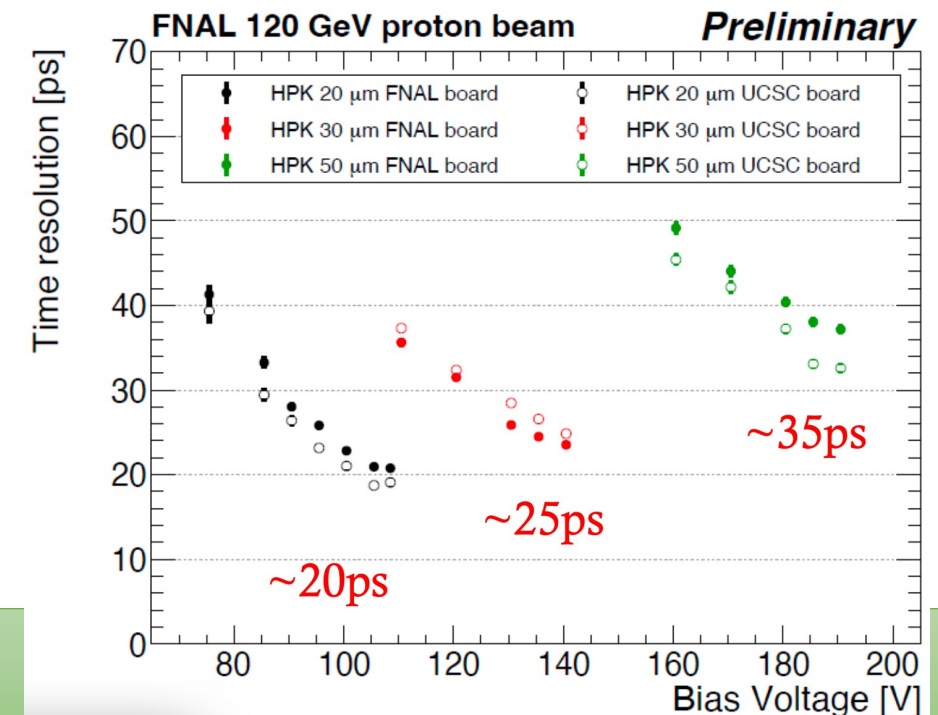
## The Beam information

FTBF set-up

events : 10,000

particle : proton

energy : 120 GeV



Example events : Depth profile of Energy deposit (proton)

Sum of energy deposit [ eV/um] (1event )(max step 0.1um)[ 50um ]

Edep(eV) Depth	1event	2event	3event	4event	5event	6event	7event
1 um	154	255	147	154	115	104	39
2 um	212	18	213	1378	22	252	187
3 um	345	82	342	154	540	187	118
4 um	349	153	367	111	158	108	154
5 um	169	198	320	291	194	306	262
8 um	338	244	360	136	97	133	565
11um	165	223	84	144	154	100	32
14um	446	180	360	252	291	226	288
17um	313	183	1670	241	352	165	288

Landau noise (50um proton)

Fig 1 : Signals from multiple events(1000events)

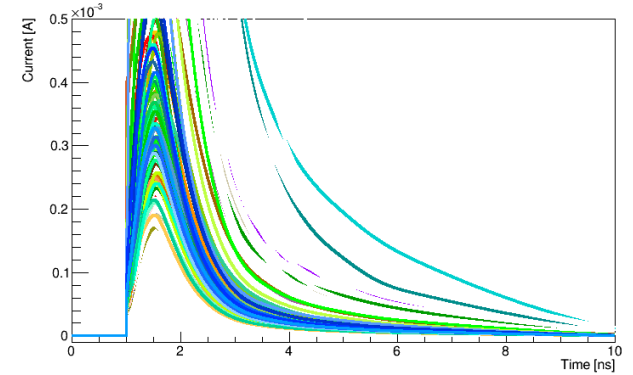


Fig 2 : Filled Arrival time to the histogram and fitted.

$$\sigma = 0.0366594 \pm 0.000370517 \text{ [ns]}$$

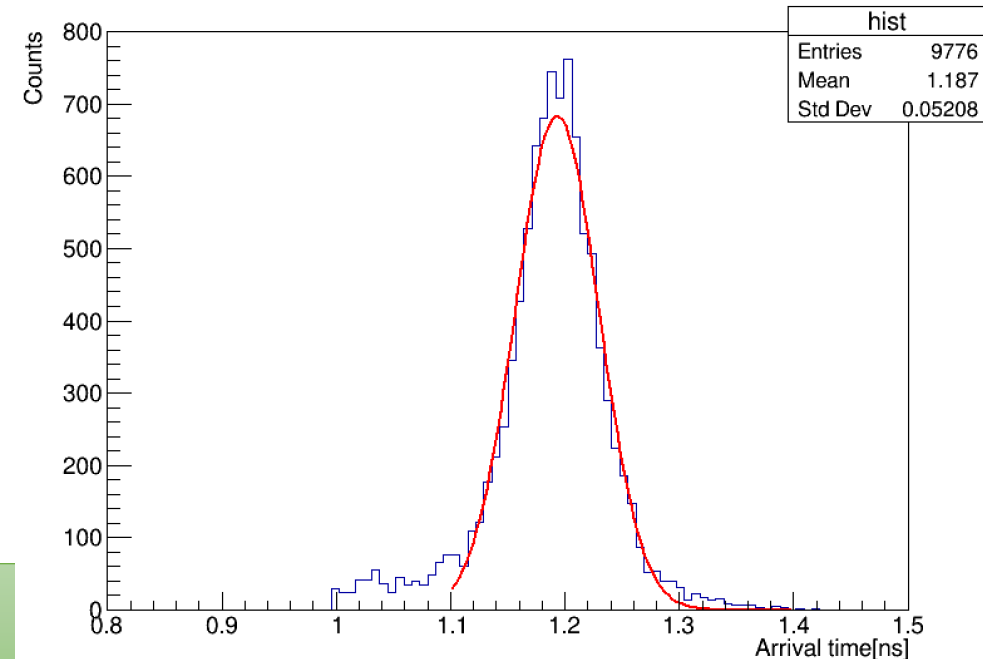
Fig 2



Landau noise = 36.7  $\pm$  0.4ps

Value of measurement : 35ps

Arrival time



Landau noise (20um proton)

Fig 1 : Signals from multiple events(1000events)

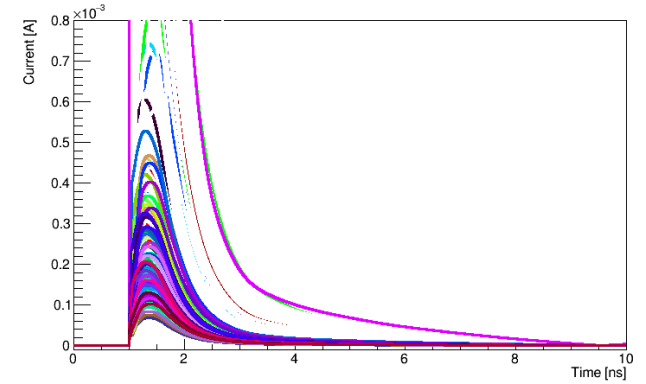


Fig 2 : Filled Arrival time to the histogram and fitted.

$$\sigma = 0.0182402 \pm 0.000338450 \text{ [ns]}$$



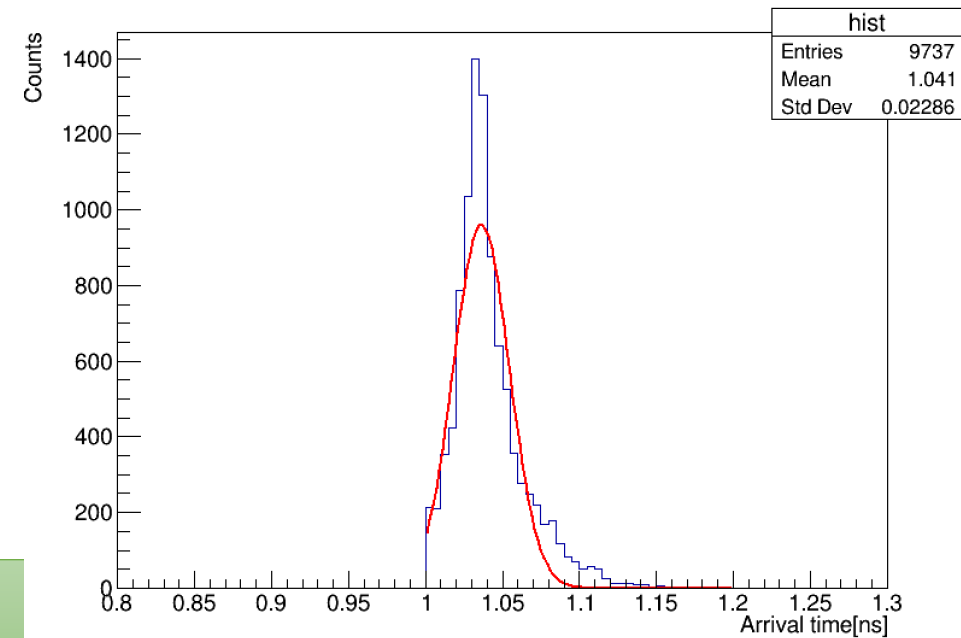
Landau noise = 18.2 ± 0.3ps

Value of measurement : 20ps

Fig 2



Arrival time



- The charge collection noise (Landau noise) values obtained by simulation results are very close to testbeam results at FTBF.

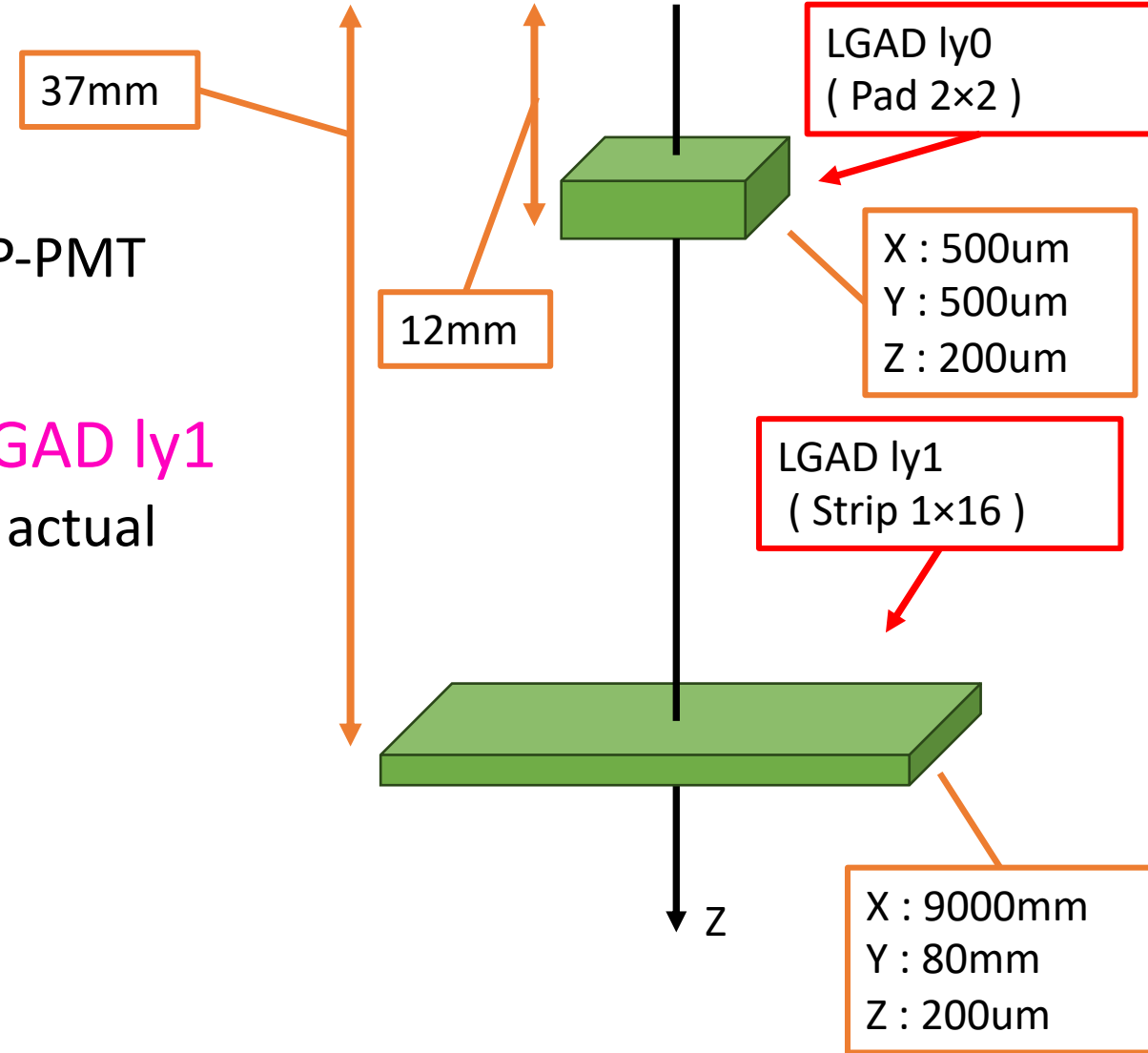
## To do

- Investigate the Landau noise for beta-ray.
- Investigate the Landau noise of other thickness to optimize sensor thickness.

# Back up

## The Geometry for proton

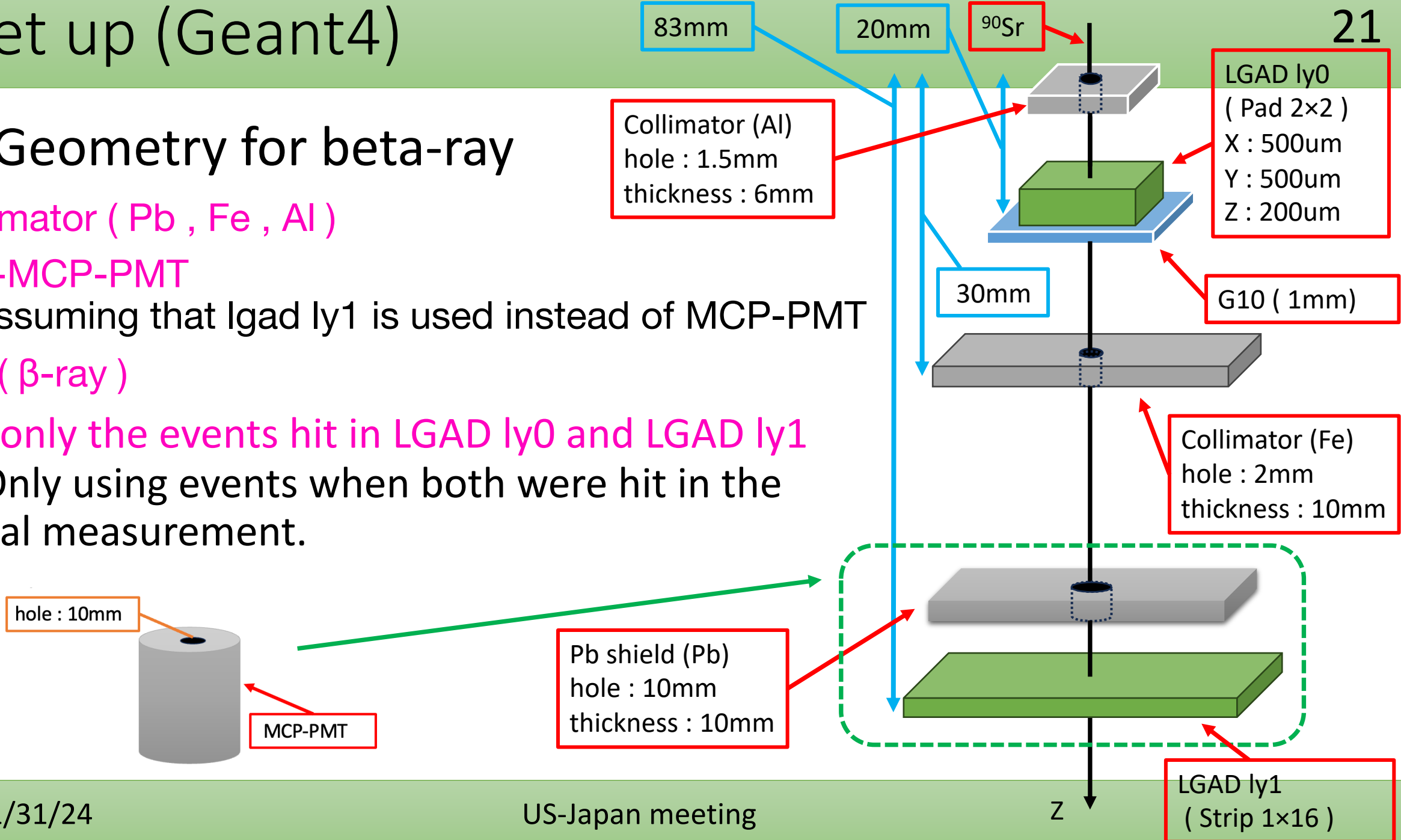
- Non-MCP-PMT  
→ Assuming that lgad ly1 is used instead of MCP-PMT
- Proton beam
- Use only the events hit in LGAD ly0 and LGAD ly1  
→ Only using events when both were hit in the actual measurement.



# Set up (Geant4)

## The Geometry for beta-ray

- Collimator ( Pb , Fe , Al )
- Non-MCP-PMT  
→ Assuming that lgad ly1 is used instead of MCP-PMT
- $^{90}\text{Sr}$  (  $\beta$ -ray )
- Use only the events hit in LGAD ly0 and LGAD ly1  
→ Only using events when both were hit in the actual measurement.



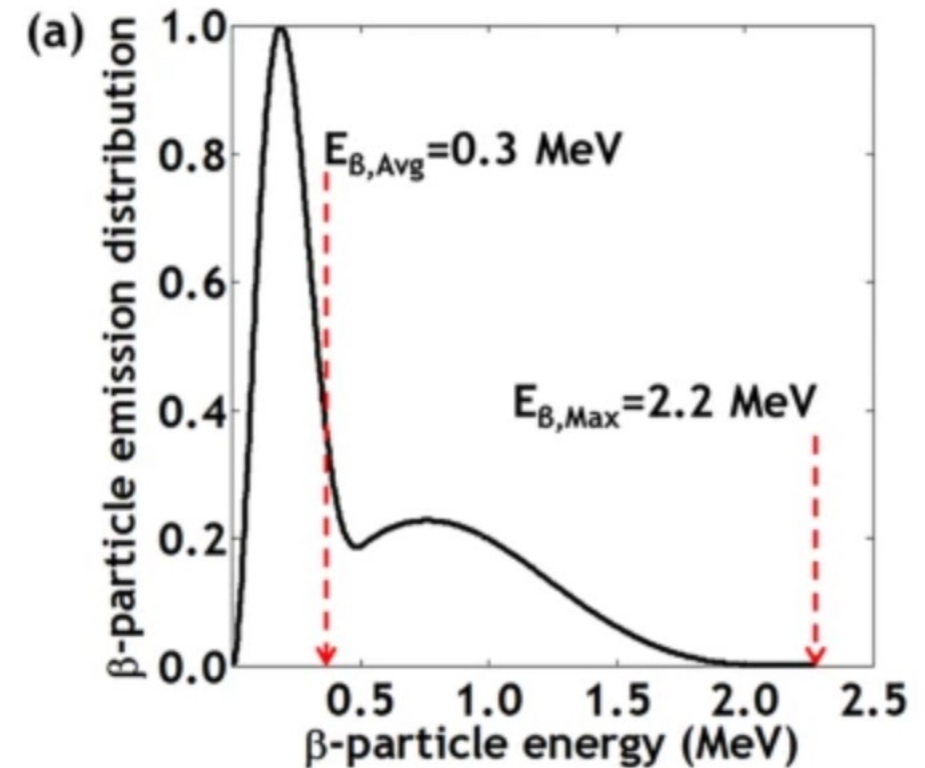
LGAD ly1  
( Strip 1x16 )



## Spectrum of $^{90}\text{Sr}$

- The spectrum of  $\beta$ -ray is given by this.
- For reproduction in Geant4 , mean and std-dev are necessary.  
→ Attempt reproduction.

Figure 1

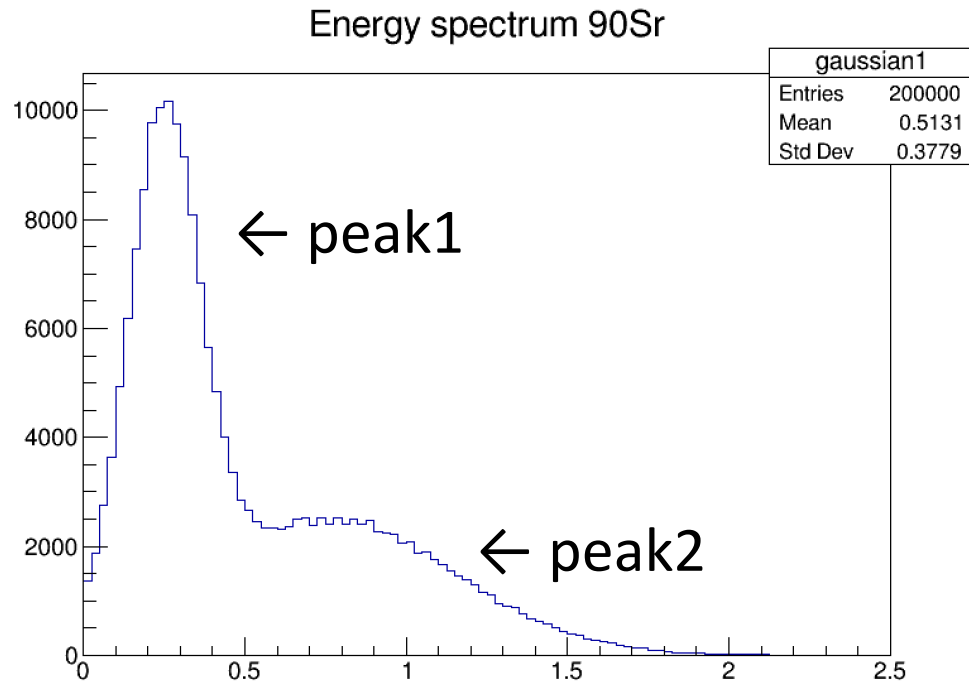


Ref : <https://www.nature.com/articles/srep38182>

## Spectrum of $^{90}\text{Sr}$

Successfully reproduced ?

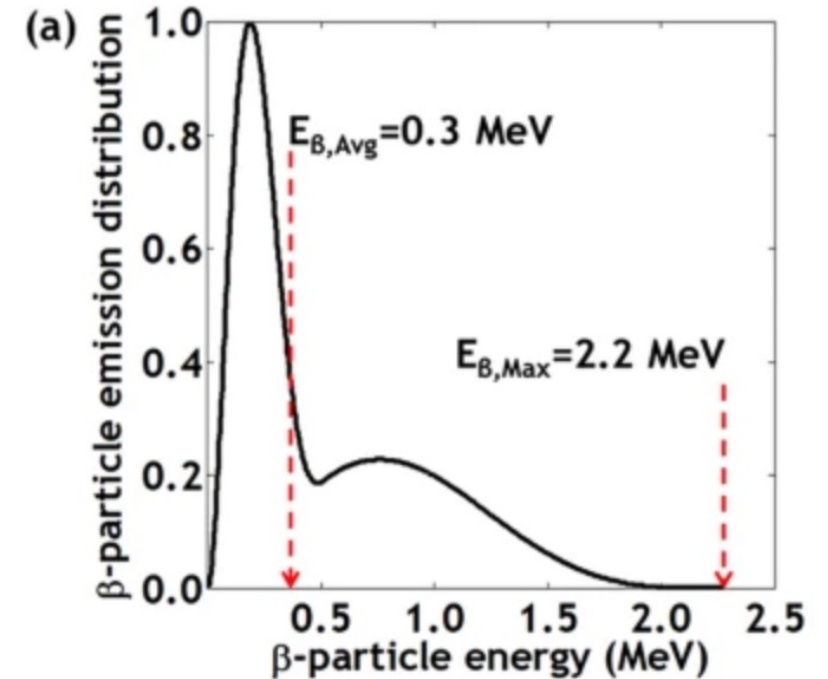
Max Energy [ peak1 : 0.54MeV , peak2 : 2.2MeV ]



peak1 : mean = 0.25 , std\_dev = 0.11

peak2 : mean = 0.75 , std\_dev = 0.4

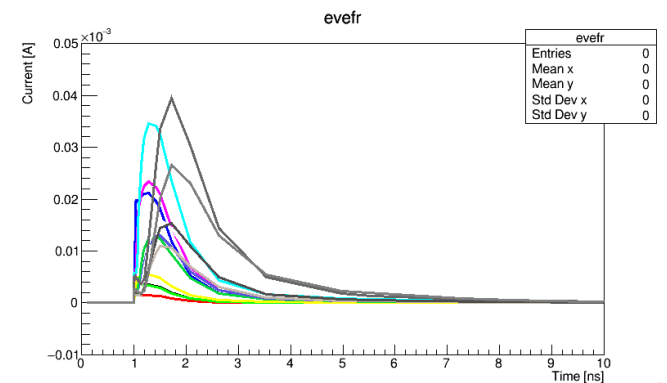
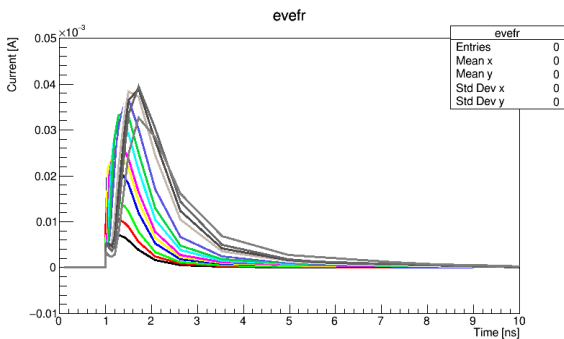
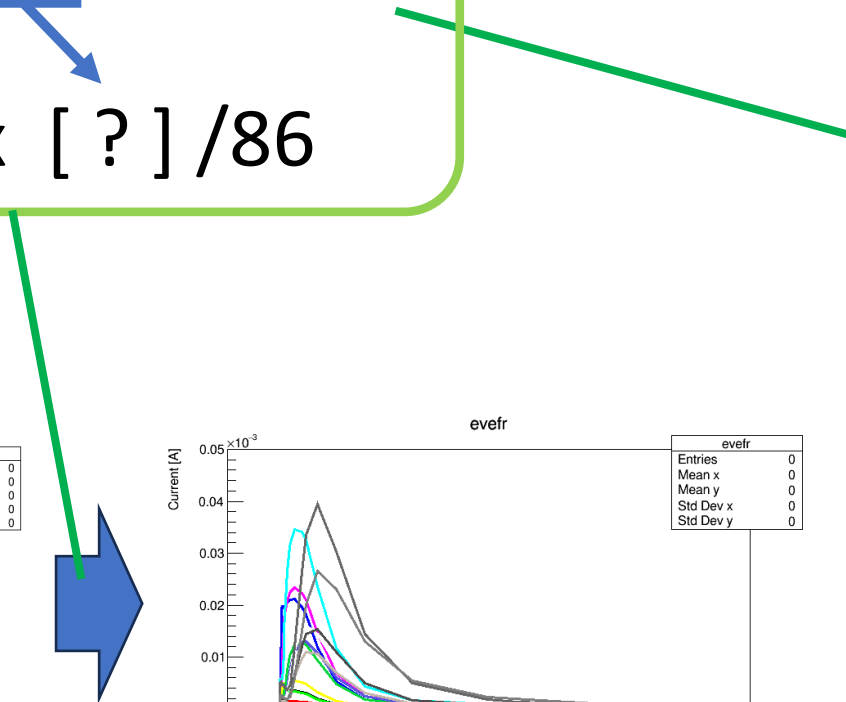
Figure 1



Ref : <https://www.nature.com/articles/srep38182>

$E_{dep}/3.6 = [ ? ]$  eh pairs

Pulse shape x  $[ ? ] / 86$



## Example

Depth	Edep(eV) 1event	eh pairs
5 um (1-5um)	632	87
10 um(6-10um)	600	83
20 um(16-20um)	568	78
25 um(21-25um)	480	66
30 um(26-30um)	292	40
35 um(31-35um)	911	126
40 um(36-40um)	721	100
45 um(41-45um)	306	42



# Beta-ray

# Results(TCAD&Geant4)

## 50um beta-ray

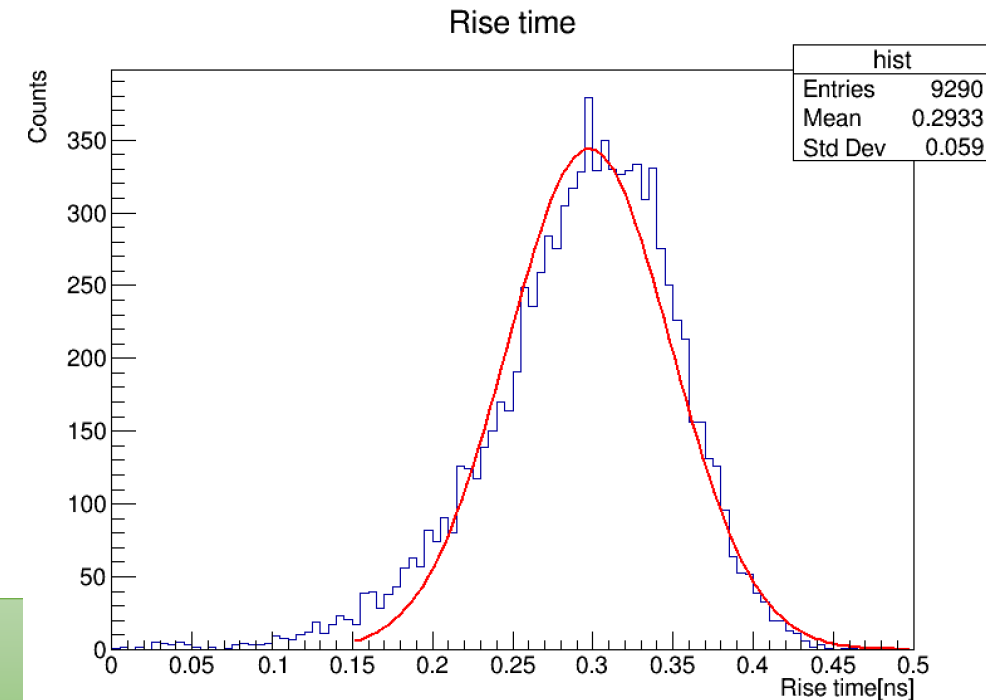
右下図：得られた Rise time を hist に詰め、gaus で fit

Rise time : Peak の 20% と 80% における  
到達時間の差を Rise time とする。

$$\sigma = 0.0511741 \pm 0.000428595$$



$$\text{Rise time} = 51.2 \pm 0.4 \text{ ps}$$



# Results(TCAD&Geant4)

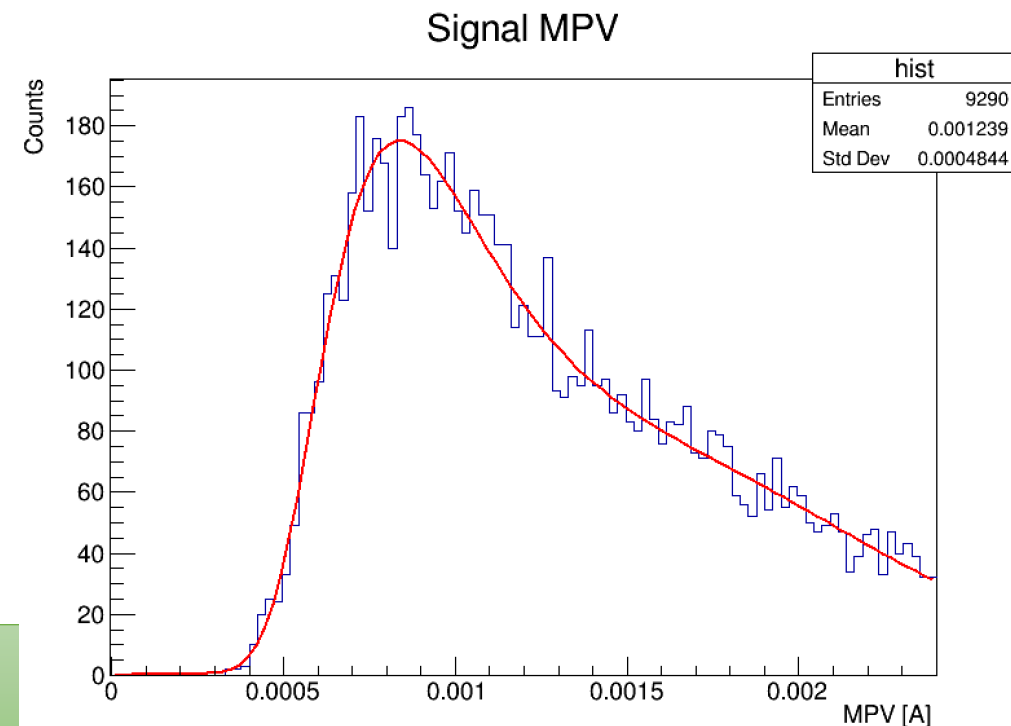
## 50um beta-ray

右下図：右上図のPulse Shape から得られるMPVを  
histに詰め、landau+gaus で fit

$$\text{MPV} = 0.867660 \pm 0.0133960 \text{ [A]}$$



$$\text{MPV} = 867.7 \pm 13.4 \text{ mA}$$



# Results(TCAD&Geant4)

## 20um beta-ray

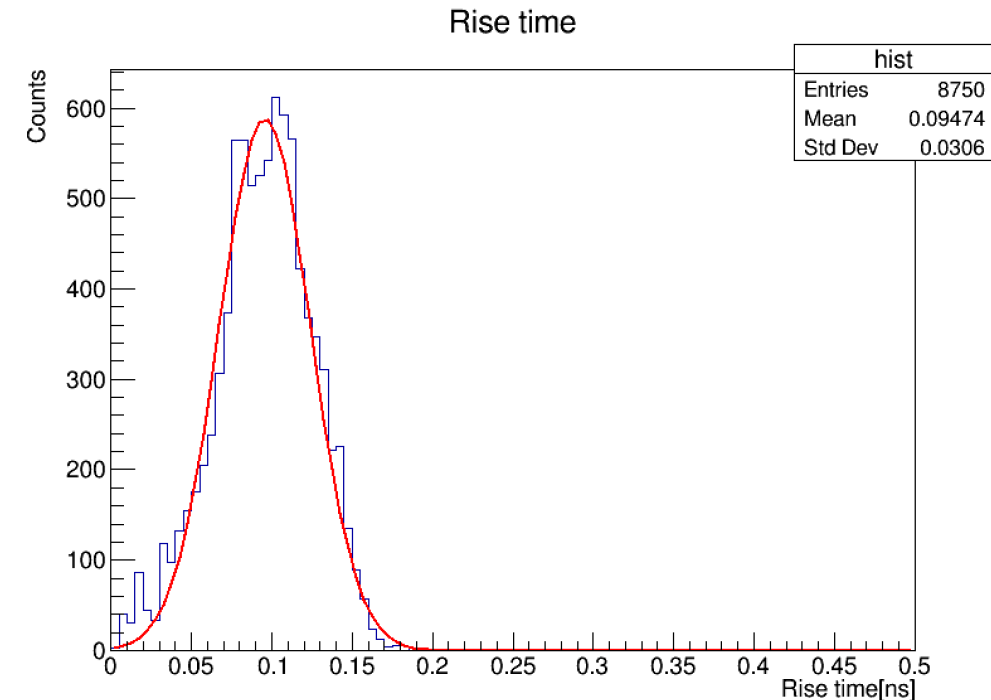
右下図：得られた Rise time を hist に詰め、gaus で fit

Rise time : Peak の 20% と 80% における  
到達時間の差を Rise time とする。

$$\sigma = 0.0284967 \pm 0.000230491$$



$$\text{Rise time} = 28.5 \pm 0.2 \text{ ps}$$



# Results(TCAD&Geant4)

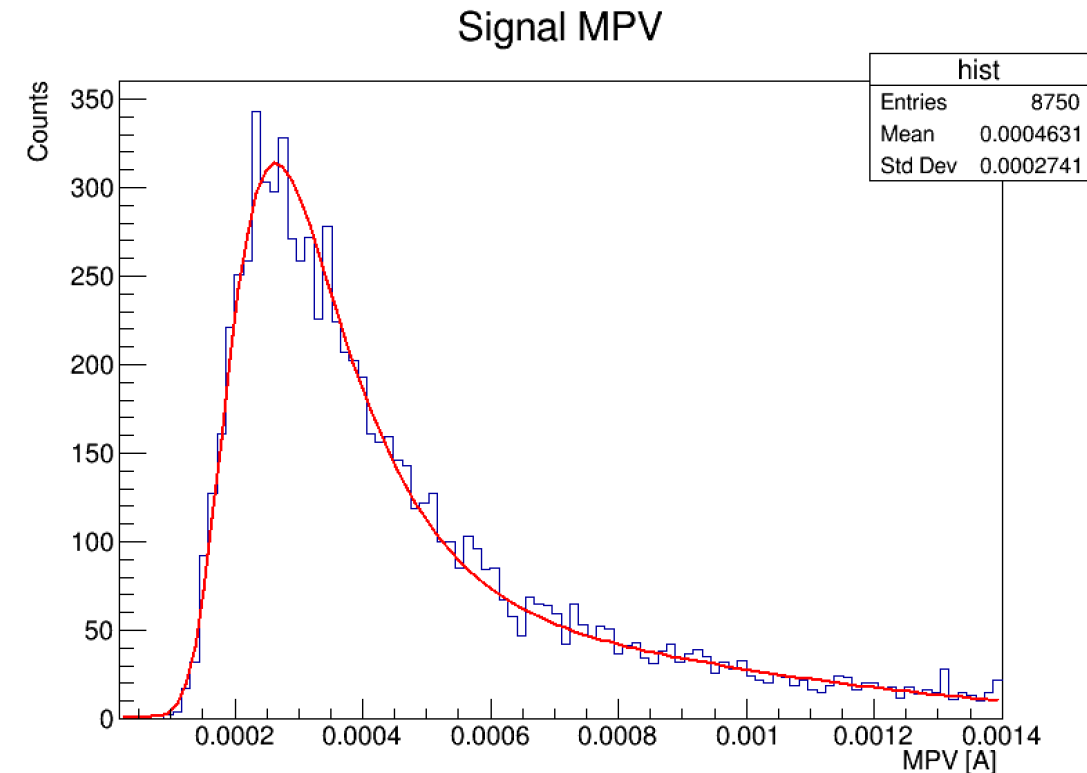
## 20um beta-ray

右下図：右上図のPulse Shape から得られるMPVを  
histに詰め、landau+gaus で fit

$$\text{MPV} = 0.276459 \pm 0.0224658 \text{ [A]}$$



$$\text{MPV} = 276.5 \pm 2.2 \text{ mA}$$





# Proton

# Results(TCAD&Geant4)

## 50um proton

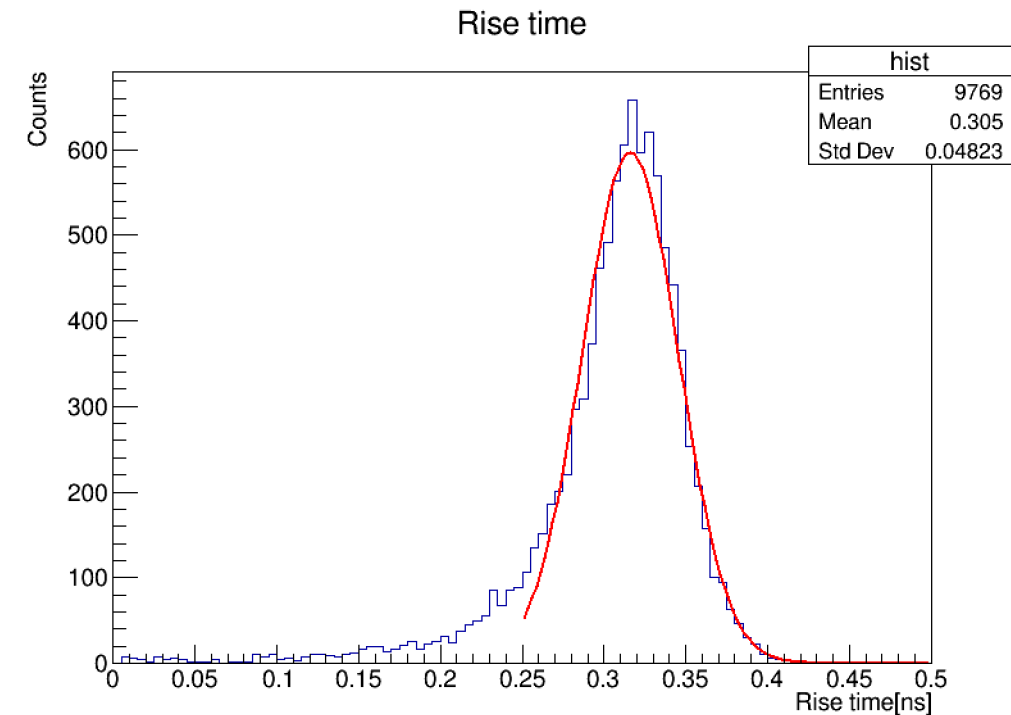
右下図：得られた Rise time を hist に詰め、gaus で fit

Rise time : Peak の 20% と 80% における  
到達時間の差を Rise time とする。

$$\sigma = 0.0294424 \pm 0.000284029$$



$$\text{Rise time} = 29.4 \pm 0.3 \text{ ps}$$



# Results(TCAD&Geant4)

## 50um proton

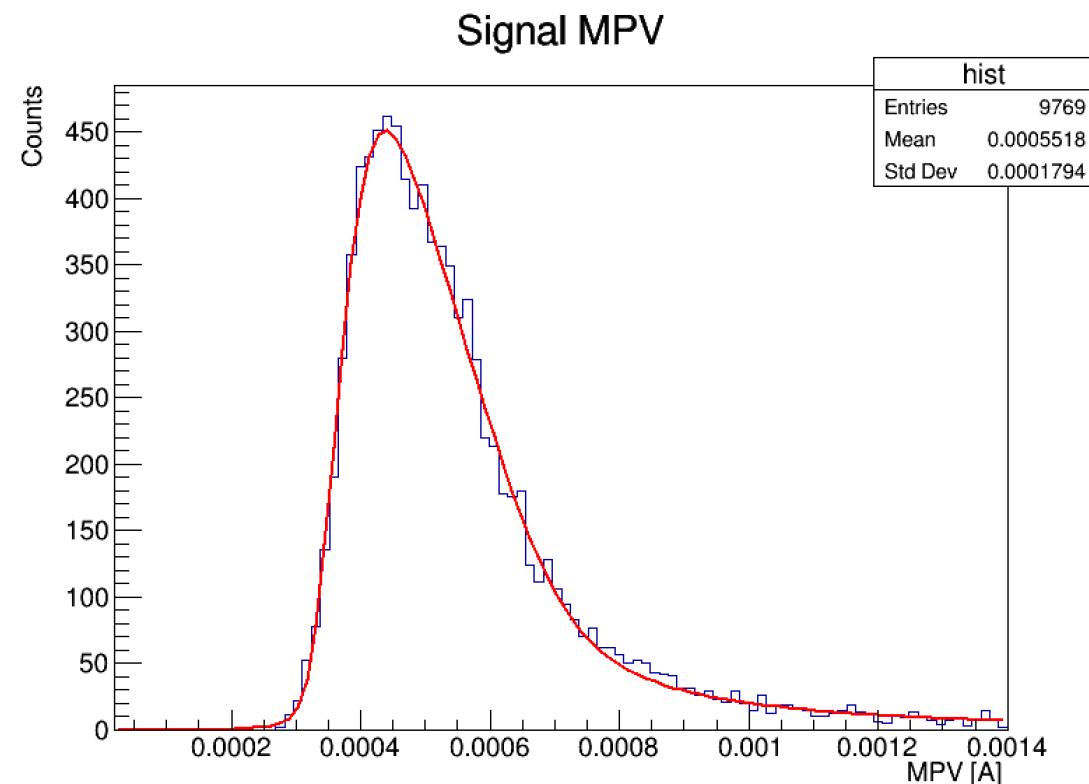
右下図：右上図のPulse Shape から得られるMPVを  
histに詰め、landau +gausで fit

$$0.438359 \pm 0.00182167$$

$$\text{MPV} = 0.438359 \pm 0.00182167 \text{ [A]}$$



$$\text{MPV} = 438.4 \pm 1.8 \text{ mA}$$



# Results(TCAD&Geant4)

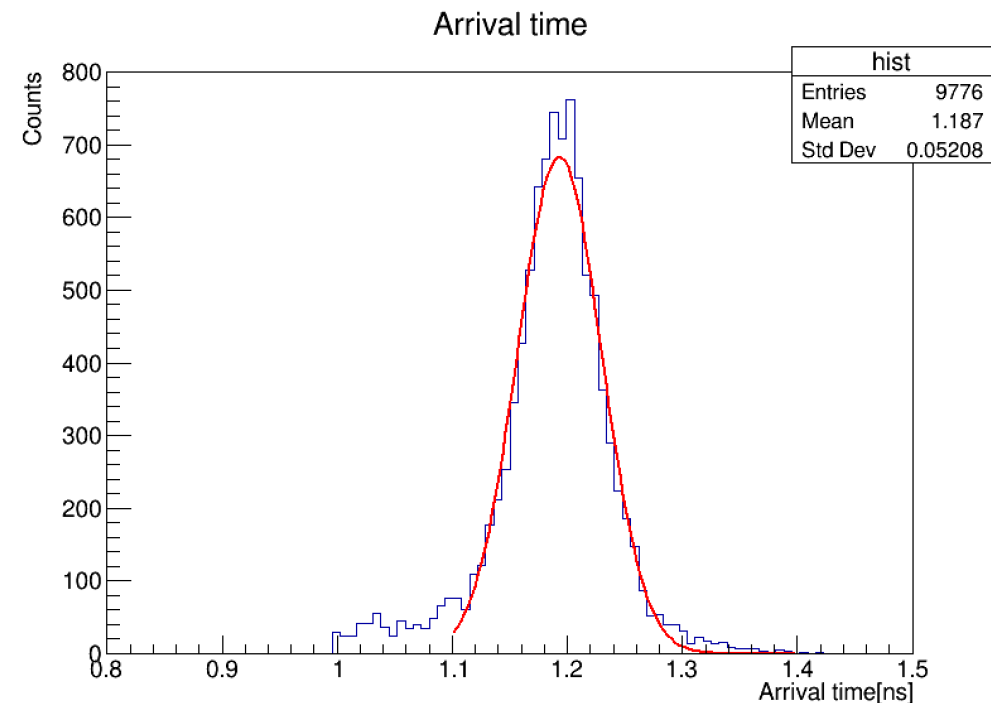
## 50um proton

右下図：得られた arrival time を hist に詰め、gaus で fit

$$\sigma = 0.0366594 \pm 0.000370517$$



$$\text{Landau noise} = 36.7 \pm 0.4 \text{ ps}$$



# Results(TCAD&Geant4)

## 20um proton

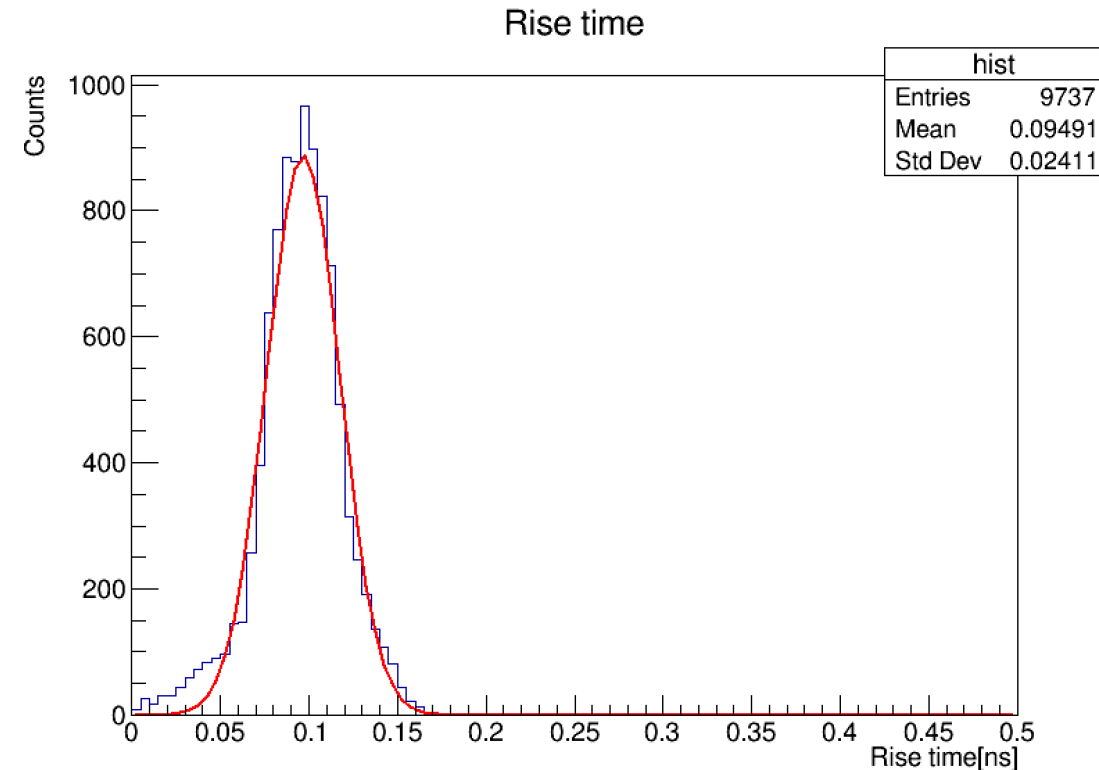
右下図：得られた Rise time を hist に詰め、gaus で fit

Rise time : Peak の 20% と 80% における  
到達時間の差を Rise time とする。

$$\sigma = 0.0208266 \pm 0.000216161$$



$$\text{Rise time} = 20.8 \pm 0.2 \text{ ps}$$



# Results(TCAD&Geant4)

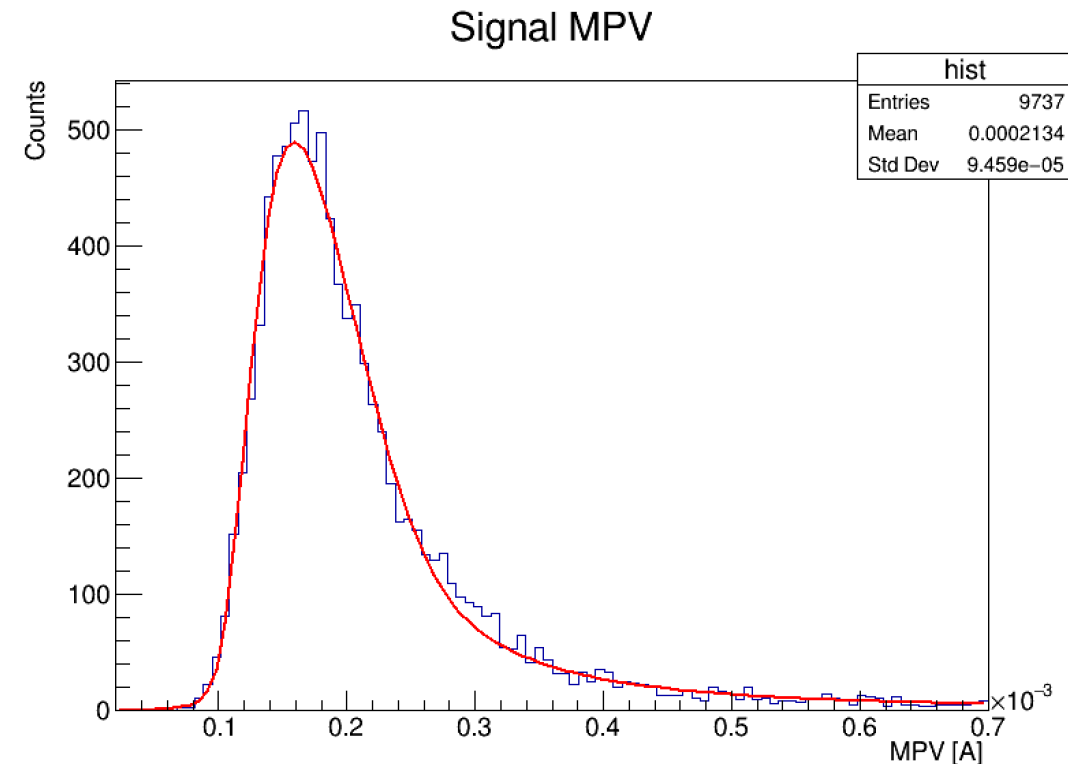
## 20um proton

右下図：右上図のPulse Shape から得られるMPVを  
histに詰め、landau +gausで fit

$$\text{MPV} = 0.159041 \pm 0.00118928 \text{ [A]}$$



$$\text{MPV} = 159.0 \pm 1.2 \text{ mA}$$



# Results(TCAD&Geant4)

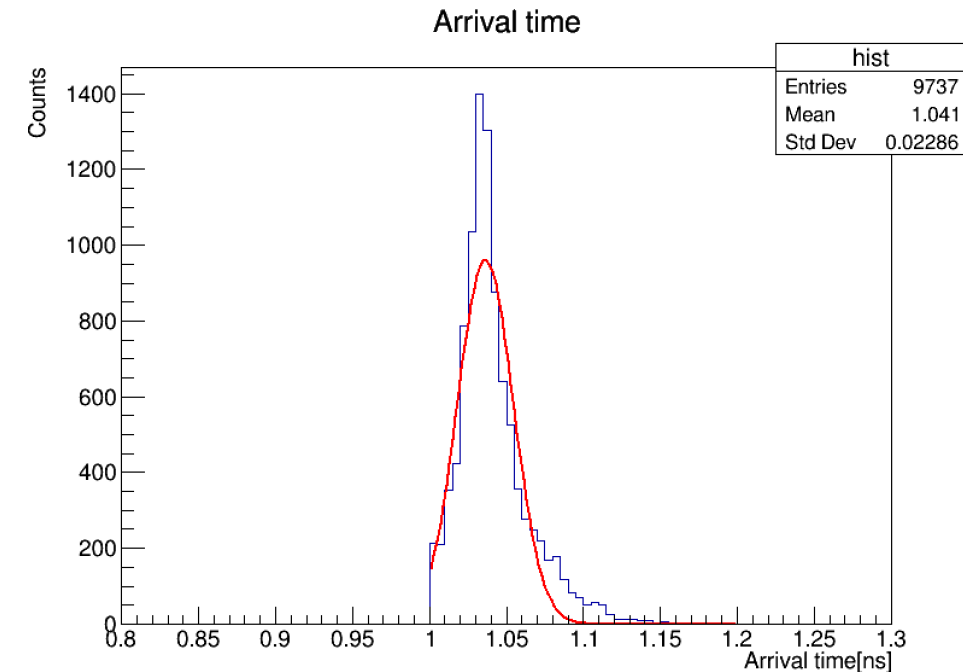
## 20um proton

右下図：得られた arrival time を hist に詰め、gaus で fit

$$\sigma = 0.0182402 \pm 0.000338450$$



Landau noise = 18.2 ± 0.3 ps



# Other



## Threshold and Cut-off

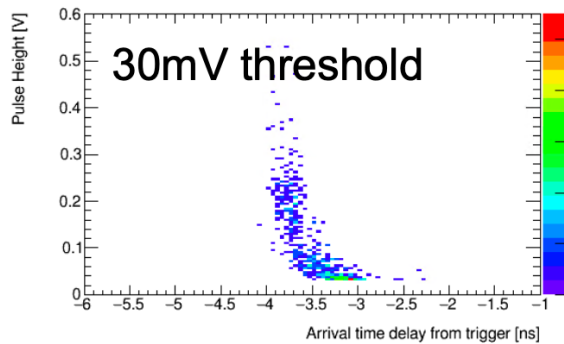
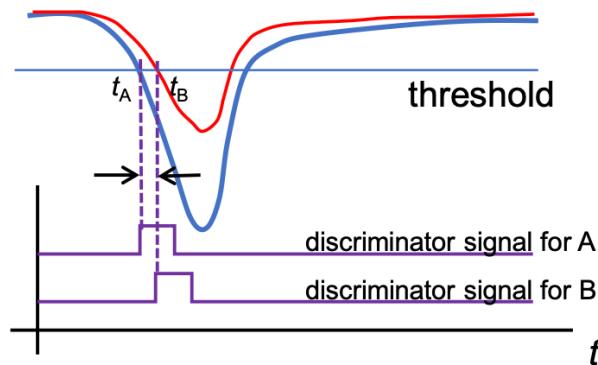
- Threshold Secondary particles produced → Cuts below 0.0um
- Cut-off energy deposit → 0.0 mV
- Limits of step → depl 0.1um , wafer 1mm , respectively
- Only interactions involving charged particles
- Plotted the only events of hits in LGAD ly0 and LGAD ly1  
→ Only using events when both were hit in the actual experiment

## タイムウオークの軽減

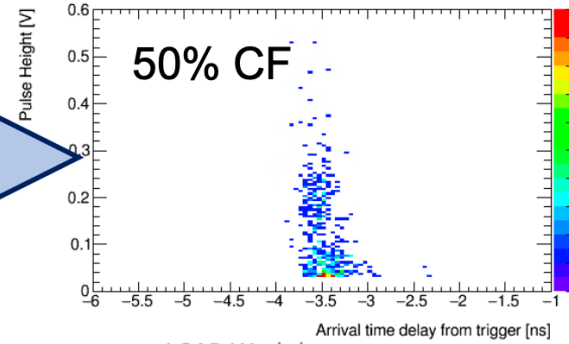
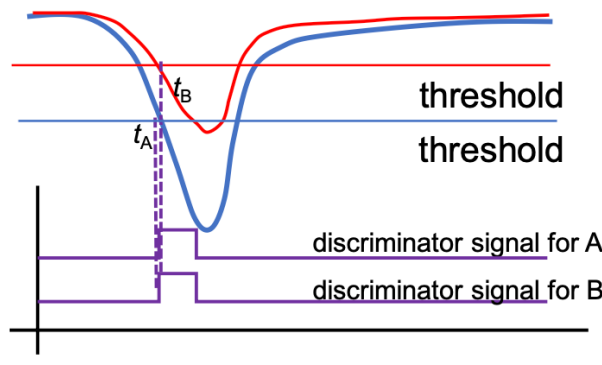
Constant Fraction (CF) 閾値を利用

例えば50%CFなら...

Fixed threshold



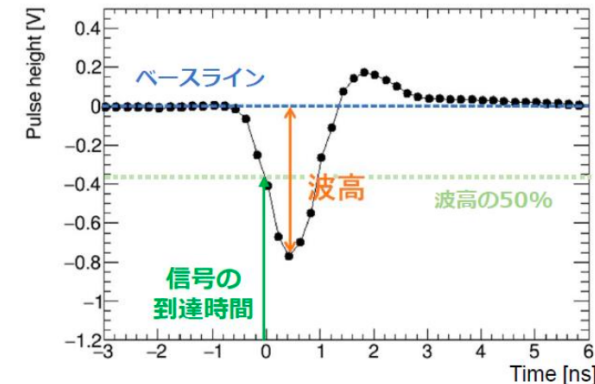
CF threshold



時間分解能

$$\sigma_t^2 = \sigma_{tw}^2 + \sigma_j^2 + \sigma_L^2$$

波高ごとに信号の到達時間の threshold を変える



信号の大きさによる ArrivalTime の影響が減少？