

Spin Alignment as a Dissipative Structure In Heavy-ion Collisions

PRC.109.064916, arXiv:2206.11890, ...

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兰州大学
LANZHOU UNIVERSITY

- **Dissipative Structure**
- Spin Alignment as Dissipative Structure
- Shear Induced Tensor Polarization (SITP)
- Diffusion Induced Tensor Polarization (DITP)
- Summary & Outlook

Dissipation

3



time

Dissipative Structures

4



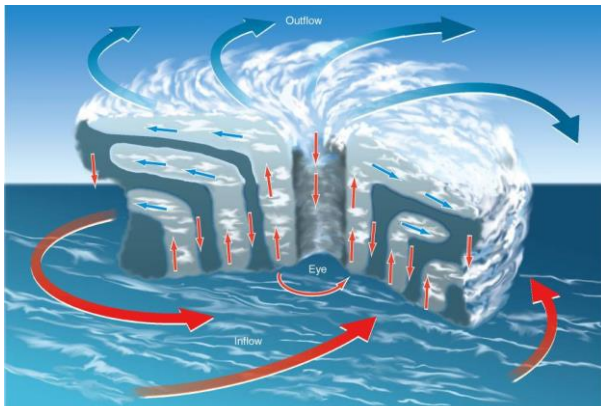
Local Equilibrium



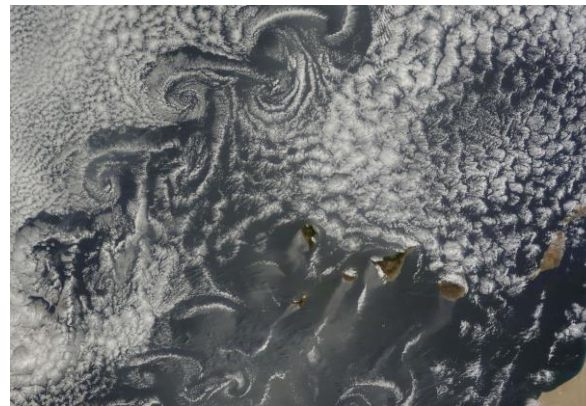
Off Equilibrium



Global Equilibrium



Hurricane



Karman's Vortices



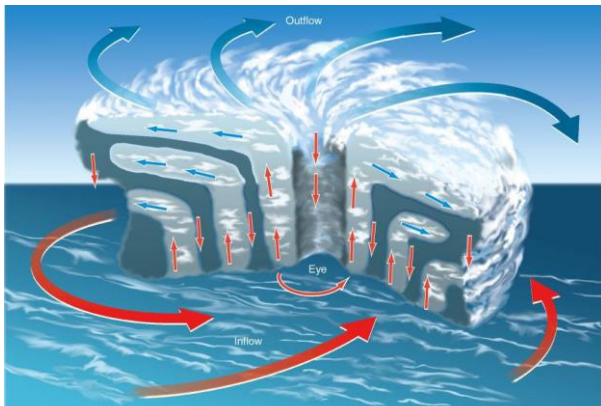
B-Z Reaction

Dissipative Structures

5

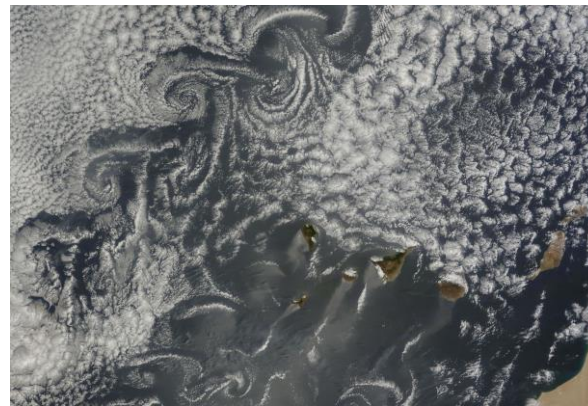


Entropy Flow in **Open** System Or **Freeze-Out**



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Hurricane



Karman's Vortices



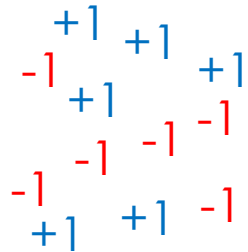
B-Z Reaction

- Dissipative Structure
- **Spin Alignment as Dissipative Structure**
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- Diffusion Induced Tensor Polarization (DITP)
- Summary & Outlook

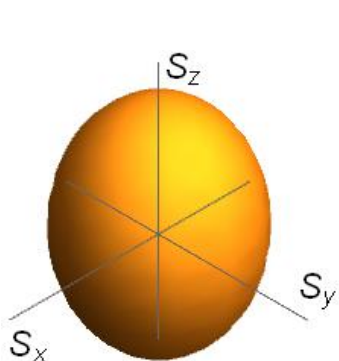
Spin Alignment (Gen. Intro.)

7

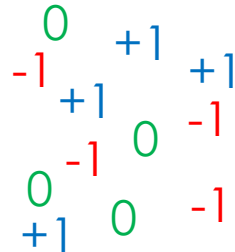
Negatively
Polarized



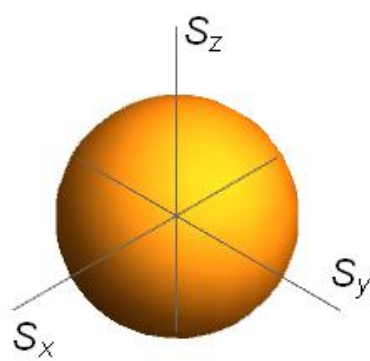
$$\overline{S_x^2} \sim \overline{S_y^2} < \overline{S_z^2}$$



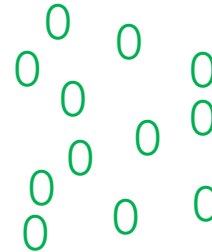
Unpolarized



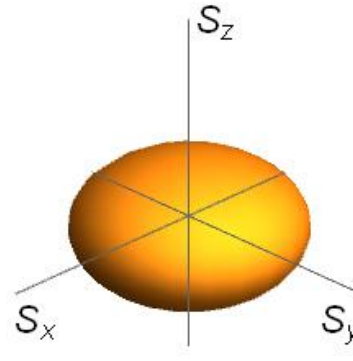
$$\overline{S_x^2} = \overline{S_y^2} = \overline{S_z^2}$$



Positively
Polarized



$$\overline{S_x^2} \sim \overline{S_y^2} > \overline{S_z^2}$$



● Picture

- Observable
- Experimental Measurement
- Mechanism

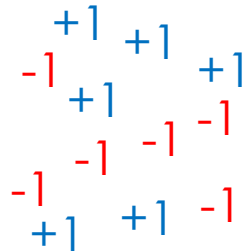
Tensor Polarization:

Anisotropy of
Spin Fluctuation

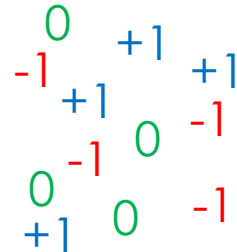
Spin Alignment (Gen. Intro.)

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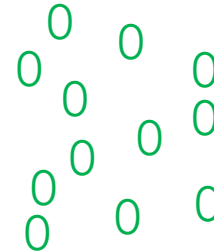
Negatively
Polarized



Unpolarized



Positively
Polarized

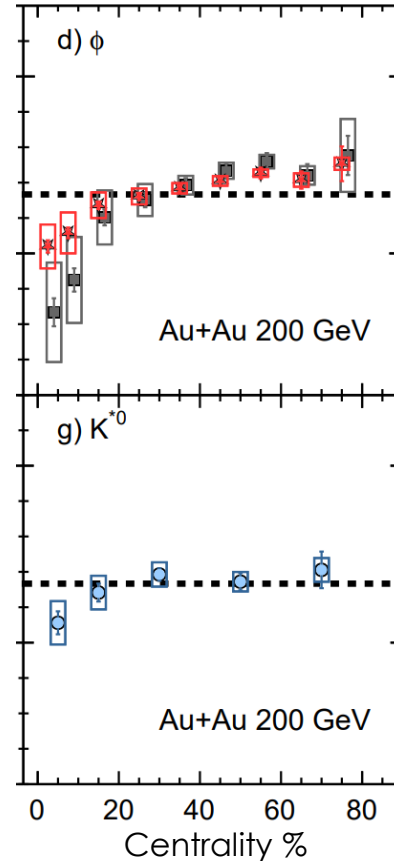
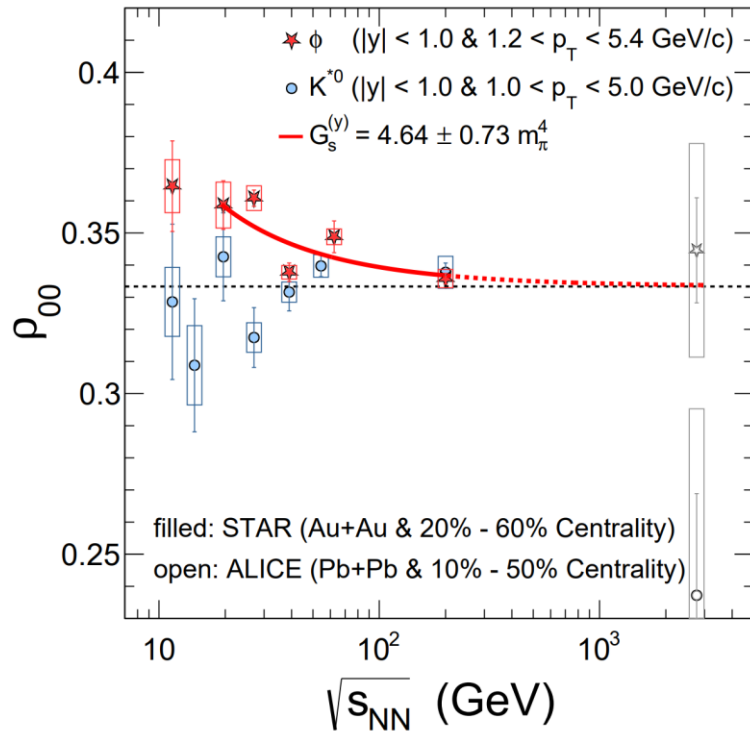


- Picture
- **Observable**
- Experimental Measurement
- Mechanism

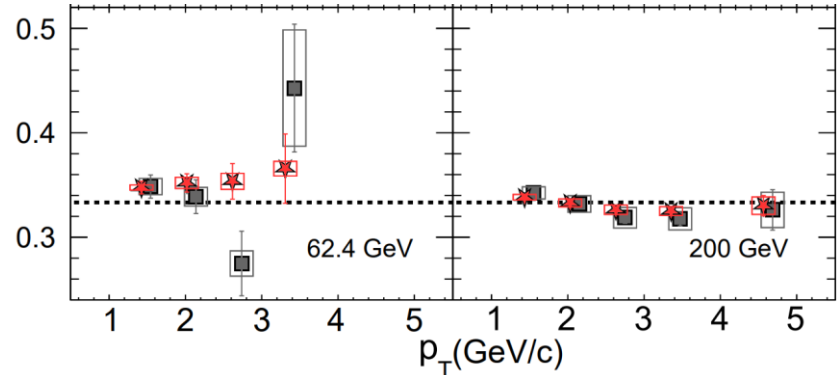
$$\delta\rho_{00} \equiv \rho_{00} - \frac{1}{3}$$

Chance for
Occupying $|0\rangle$

Spin Alignment (Gen. Intro.)



- Picture
- Observable
- **Experimental Measurement**
- Mechanism



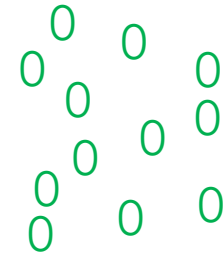
Nature volume 614, 244 (2023)

Spin Alignment (Gen. Intro.)

0 +1 +1
 -1 +1 -1
 0 -1 0
 +1 0 -1

Polarization of Q, \bar{Q}
 (Z. Liang & X. Wang,
 PLB 629, 20 (2005))

Vorticity
 (F. Becattini, et al.,
 PRC 77, 024906 (2008))

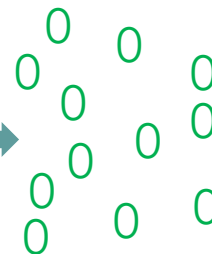


Fluctuating Strong Forces or Gluon Fields
 (X. Sheng, et al., PRL 131, 042304 (2023);
 A. Kumar, et al., PRD 108, 016020 (2023))

0 +1 +1
 -1 +1 -1
 0 -1 0
 +1 0 -1

Medium Modification
 on Spectral Properties

Viscous Damping: $\partial(\beta u)$



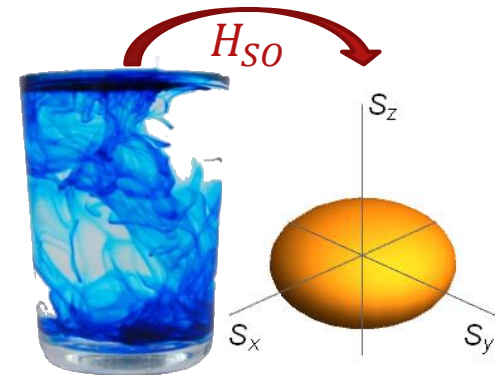
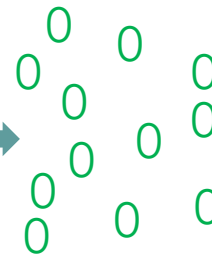
- Picture
- Observable
- Experimental Measurement
- **Mechanism**

0 +1 +1
 -1 +1 -1
 0 -1 0
 +1 0 -1

Medium Modification
 on Spectral Properties

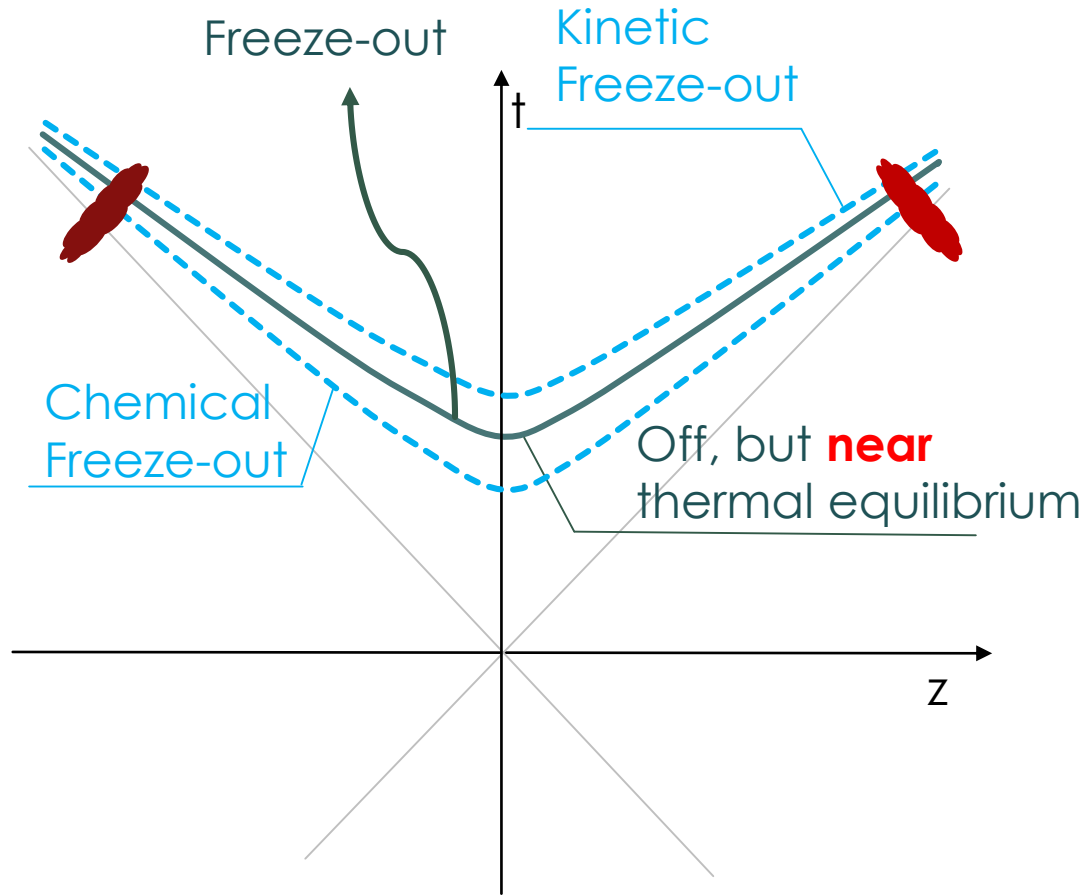
Diffusion: $\partial(\beta \mu_S)$

$K^* \checkmark \phi \times$

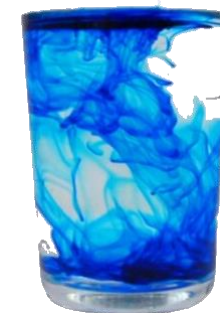


Framework & Assumption

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Diffusion coefficients
evaluated
near equilibrium



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Linear Response

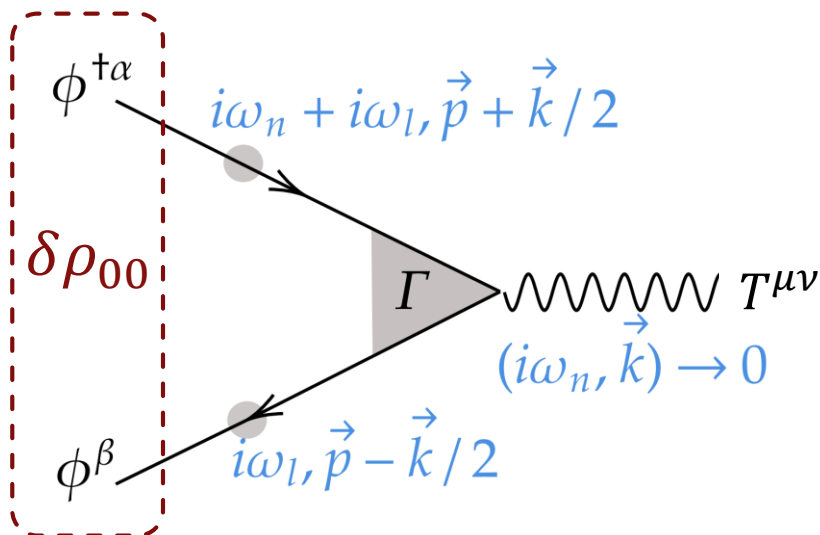
$$\delta\rho_{00} = \lim_{k^0 \rightarrow 0} \frac{\tilde{q}_T^{\mu\nu}(k^0, \vec{k} = 0)}{2k^0} \frac{\partial_\mu(\beta u_\nu)}{\bar{\beta}}$$

In Equilibrium

Driven by Flow and Thermal Gradients

$$\tilde{q}_T^{\mu\nu} \equiv \int d^4x e^{ik \cdot x} \left[\delta\rho_{00} \left(x' + \frac{x}{2} \right), T^{\mu\nu} \left(x' - \frac{x}{2} \right) \right]$$

(Belinfante) Stress-Energy Tensor



D. N. Zubarev,
Nonequilibrium statistical
thermodynamics

$$\delta\rho_{00}(\vec{p}) = \mathcal{N}^{-1} \left[\epsilon_{\langle\alpha\beta\rangle}^0 - \alpha_0 \tilde{\Delta}_{\alpha\beta} \right] \int d^3\vec{X} W_{(1)}^{\alpha\beta}$$

Projectors and Polarizers

$$W_{(1)}^{\alpha\beta} = -E_p \int \frac{dp^0}{2\pi} \sum_{a,b=T}^L \mathcal{A}_a(p) \mathcal{A}_b(p) \Delta_a^{\beta\rho}(p) \Delta_b^{\sigma\alpha}(p) \text{Re}\left\{ \tilde{\Gamma}_{\rho\sigma}^{\mu\nu}(p;p) \right\} \frac{\partial n}{\partial p^0} \frac{\partial_\mu(\beta u_\nu)}{\bar{\beta}}$$

Bose Distribution

Assumption:

- There is no pole on p^0 in $\tilde{\Gamma}_{\rho\sigma}^{\mu\nu}(i\omega_n + p^0, \vec{p}; p^0, \vec{p})$
- Time reversesal symmetry on $\tilde{\Gamma}$
 $\tilde{\Gamma}_{\rho\sigma}^{\mu\nu}(p; q) = \tilde{\Gamma}_{\sigma\rho}^{\mu\nu}(q; p)$
- $\lim_{q \rightarrow 0} \partial_{q^0} \tilde{\Gamma}(p+q; p)$ is real
- Or, \mathcal{A} is analytic on the upper-half complex plane, and real on the real axis.

$$\delta\rho_{00}(\vec{p}) = \mathcal{N}^{-1} \left[\epsilon_{\langle\alpha}^0 \epsilon_{\beta\rangle}^0 - \alpha_0 \tilde{\Delta}_{\alpha\beta} \right] \int d^3\vec{X} W_{(1)}^{\alpha\beta}$$

$$W_{(1)}^{\alpha\beta} = -E_p \int \frac{dp^0}{2\pi} \sum_{a,b=T}^L \mathcal{A}_a(p) \mathcal{A}_b(p) \Delta_a^{\beta\rho}(p) \Delta_b^{\sigma\alpha}(p) \text{Re} \left\{ \tilde{\Gamma}_{\rho\sigma}^{\mu\nu}(p;p) \right\} \frac{\partial n}{\partial p^0} \frac{\partial_\mu(\beta u_\nu)}{\bar{\beta}}$$

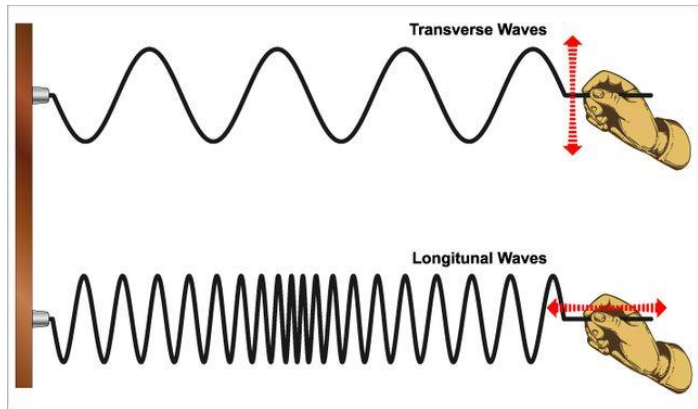
$$\tilde{\Gamma}_{\rho\sigma}^{\mu\nu}(p,p) = -p^{(\nu} \partial_{p\mu)} \tilde{S}_{\rho\sigma}^{-1}(p) + g^{\nu\mu} \tilde{S}_{\rho\sigma}^{-1}(p) - g^{(\mu\alpha} \tilde{S}_{\rho\alpha}^{-1}(p) \delta_{\sigma}^{\nu)} - g^{(\mu\beta} \tilde{S}_{\beta\sigma}^{-1}(p) \delta_{\rho}^{\nu)}$$

Inspired by B. S. DeWitt, Phys. Rev. 162, 1239 (1967)

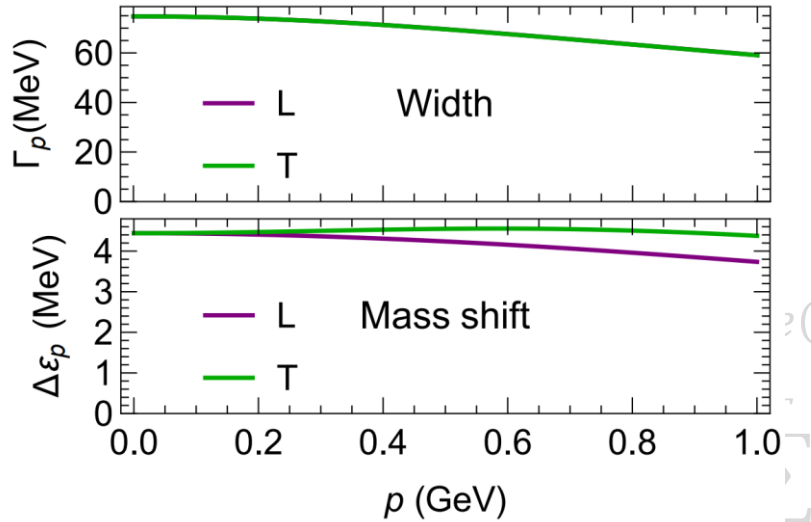
- Non-perturbative expression under certain assumptions
- Meson-medium interactions are encoded in the spectral function \mathcal{A} and Propagator \tilde{S}

$$\delta\rho_{00}(\vec{p}) = - \left[\epsilon_{\langle\alpha\beta\rangle}^0 - \alpha_0 \tilde{\Delta}_{\alpha\beta} \right]$$

$$\times \int \frac{d^3\vec{X}}{\mathcal{N}} T \partial_\mu (\beta u_\nu) E_p \int \frac{d\varepsilon}{2\pi} \frac{\partial n}{\partial \varepsilon} \left\{ \begin{aligned} & -Re(\Pi_T - \Pi_L) \mathcal{A}_L \mathcal{A}_T p^{(\nu} \frac{\varepsilon}{\kappa^2} \left(1 - \frac{\varepsilon\Omega}{\varsigma} \right) u^{(\alpha} \tilde{\Delta}_T^{\beta)\mu)} \\ & + \sum_{a=L}^T \mathcal{A}_a^2 \left[\begin{aligned} & 2p^\mu p^\nu (1 + \partial_\varsigma Re\Pi_a) + u^\mu p^\nu \partial_\varepsilon Re\Pi_a \\ & - g^{\mu\nu} (\bar{p}^2 - M^2 + Re\Pi_a) \end{aligned} \right] \Delta_a^{\alpha\beta} \\ & - \sum_{a,b} \mathcal{A}_a \mathcal{A}_b 2\Delta_a^{\mu(\beta} \Delta_b^{\nu\alpha)} (\bar{p}^2 - M^2 + Re\Pi_a) \end{aligned} \right\}$$



Caused by splitting of spectral properties between the L & T modes



W. Dong, et al., PRD 109, 056025 (2024)

$$\Delta_L - \tilde{\Delta}_L \sim \mathcal{O}\left(\frac{\Omega}{M} \sqrt{\frac{T}{M}}\right) \tilde{\Delta}_T^{(\beta)\mu}$$

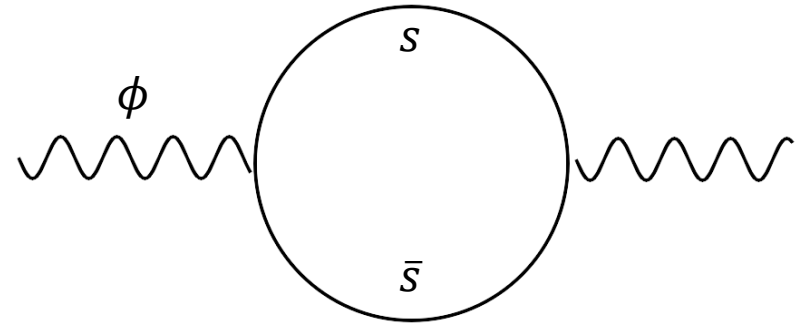
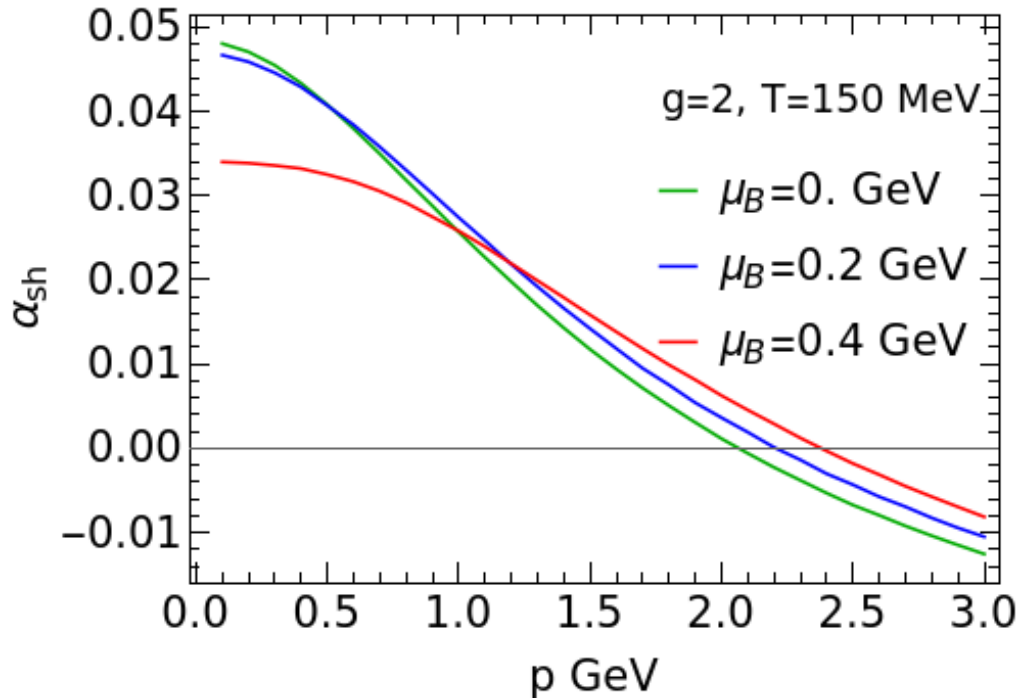
$$\left[\mathcal{A}_a^2 \left[\begin{array}{c} 2p^\mu p^\nu (1 + \partial_\zeta \text{Re}\Pi_a) + u^\mu p^\nu \partial_\epsilon \text{Re}\Pi_a \\ -g^{\mu\nu} (\bar{p}^2 - M^2 + \text{Re}\Pi_a) \end{array} \right] \Delta_a^{\alpha\beta} \right]_{a=L}$$

$$\left[- \sum_{a,b} \mathcal{A}_a \mathcal{A}_b 2\Delta_a^{\mu(\beta} \Delta_b^{\nu\alpha)} (\bar{p}^2 - M^2 + \text{Re}\Pi_a) \right]$$

After neglecting L, T splitting & difference between Δ & $\tilde{\Delta}$

$$\delta\rho_{00}^{SITP} = \alpha_{sh} \partial_\mu (\beta u_\nu) \epsilon^{\langle\mu} \epsilon^{\nu\rangle}$$

$$\alpha_{sh} \equiv \mathcal{N}_0^{-1} T E_p \int \frac{d\varepsilon}{\pi} \frac{\partial n}{\partial \varepsilon} \mathcal{A}^2 (\bar{p}^2 - M^2 + \text{Re}\bar{\Pi}) \quad \text{Off-Shell}$$



$\partial_\mu(\beta u_\nu) \sim \frac{\beta}{\tau} \sim \mathcal{O}(0.1)$
at the end of partonic phase

After neglecting L, T splitting & difference between Δ & $\tilde{\Delta}$

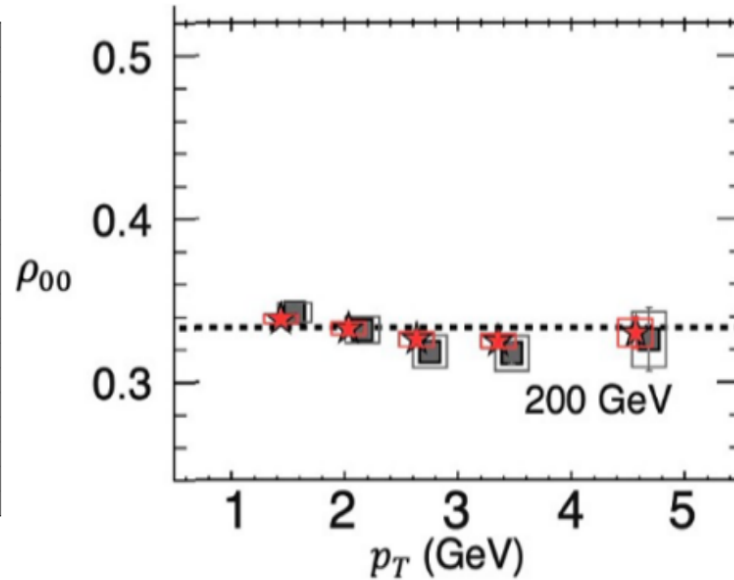
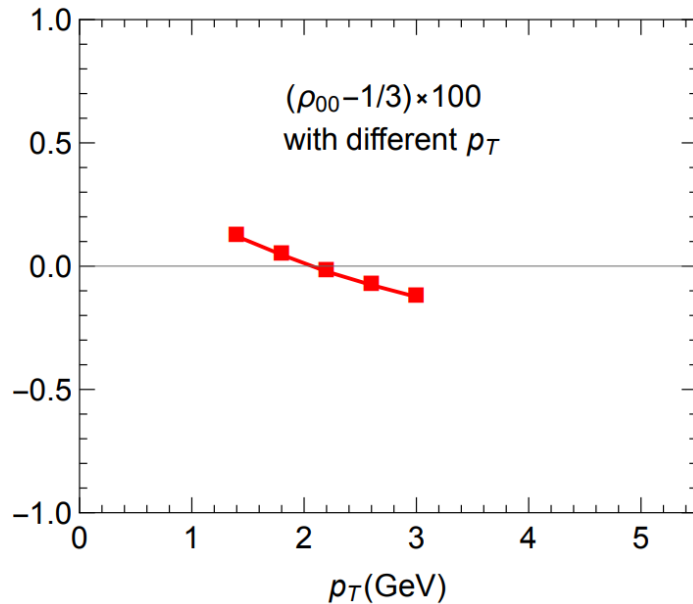
$$\delta\rho_{00}^{SITP} = \alpha_{sh} \partial_\mu(\beta u_\nu) \epsilon^{\langle\mu} \epsilon^{\nu\rangle}$$

$$\alpha_{sh} \equiv \mathcal{N}_0^{-1} T E_p \int \frac{d\varepsilon}{\pi} \frac{\partial n}{\partial \varepsilon} \mathcal{A}^2(\bar{p}^2 - M^2 + Re\bar{\Pi}) \quad \text{Off-Shell}$$

Phenomenology (p_T)

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Au + Au @ 200 GeV (Using CLVisc)



After neglecting L, T splitting & difference between Δ & $\tilde{\Delta}$

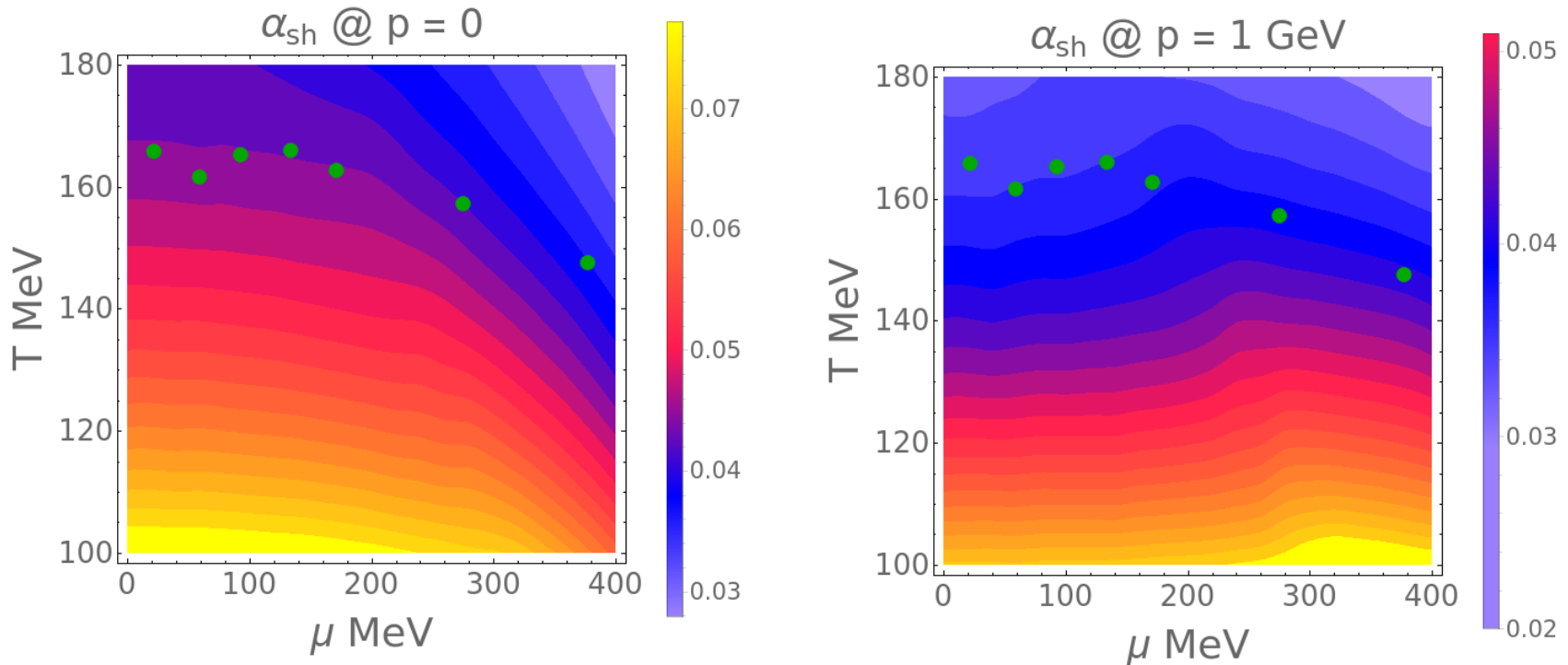
$$\delta\rho_{00}^{SITP} = \alpha_{sh} \partial_{\mu} (\beta u_{\nu}) \epsilon^{\langle \mu \nu \rangle}$$

$$\alpha_{sh} \equiv \mathcal{N}_0^{-1} T E_p \int \frac{d\varepsilon}{\pi} \frac{\partial n}{\partial \varepsilon} \mathcal{A}^2 (\bar{p}^2 - M^2 + Re \bar{\Pi}) \quad \text{Off-Shell}$$

Phenomenology ($\sqrt{s_{NN}}$)

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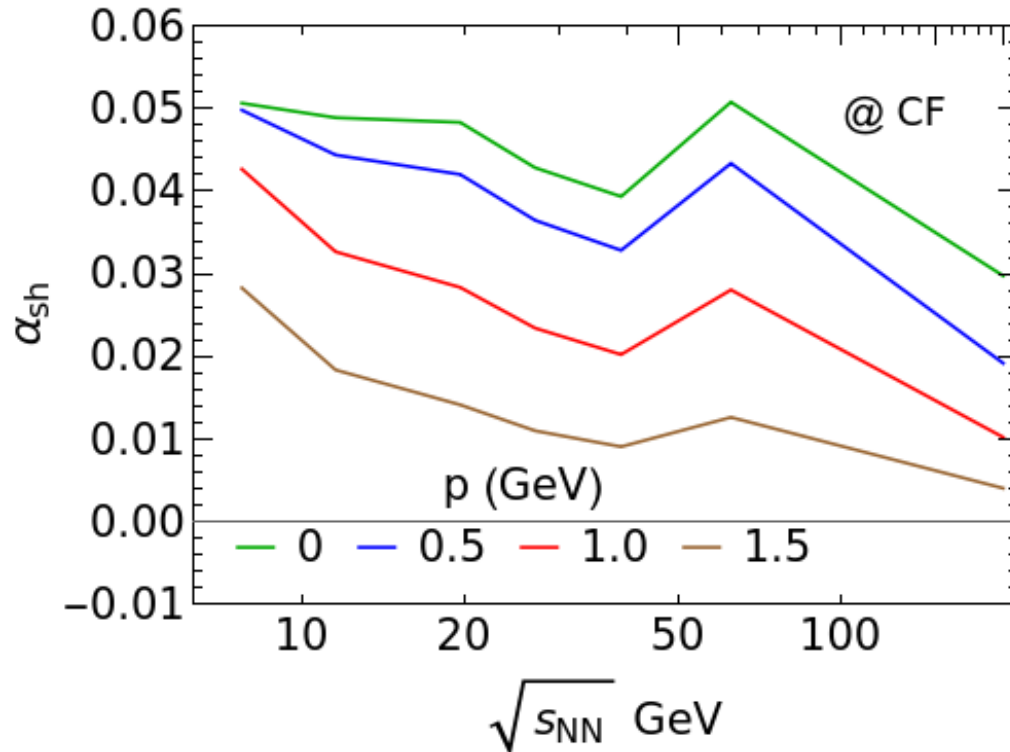
Dots for Chemical Freeze-Out from: STAR, PRC 96, 044904 (2017)



After neglecting L, T splitting & difference between Δ & $\tilde{\Delta}$

$$\delta\rho_{00}^{SITP} = \alpha_{sh} \partial_{\mu} (\beta u_{\nu}) \epsilon^{\langle \mu} \epsilon^{\nu \rangle}$$

$$\alpha_{sh} \equiv \mathcal{N}_0^{-1} T E_p \int \frac{d\varepsilon}{\pi} \frac{\partial n}{\partial \varepsilon} \mathcal{A}^2 (\bar{p}^2 - M^2 + Re \bar{\Pi}) \quad \text{Off-Shell}$$



? $\partial_\mu(\beta u_\nu)$ at lower $\sqrt{s_{NN}}$

After neglecting L, T splitting & difference between Δ & $\tilde{\Delta}$

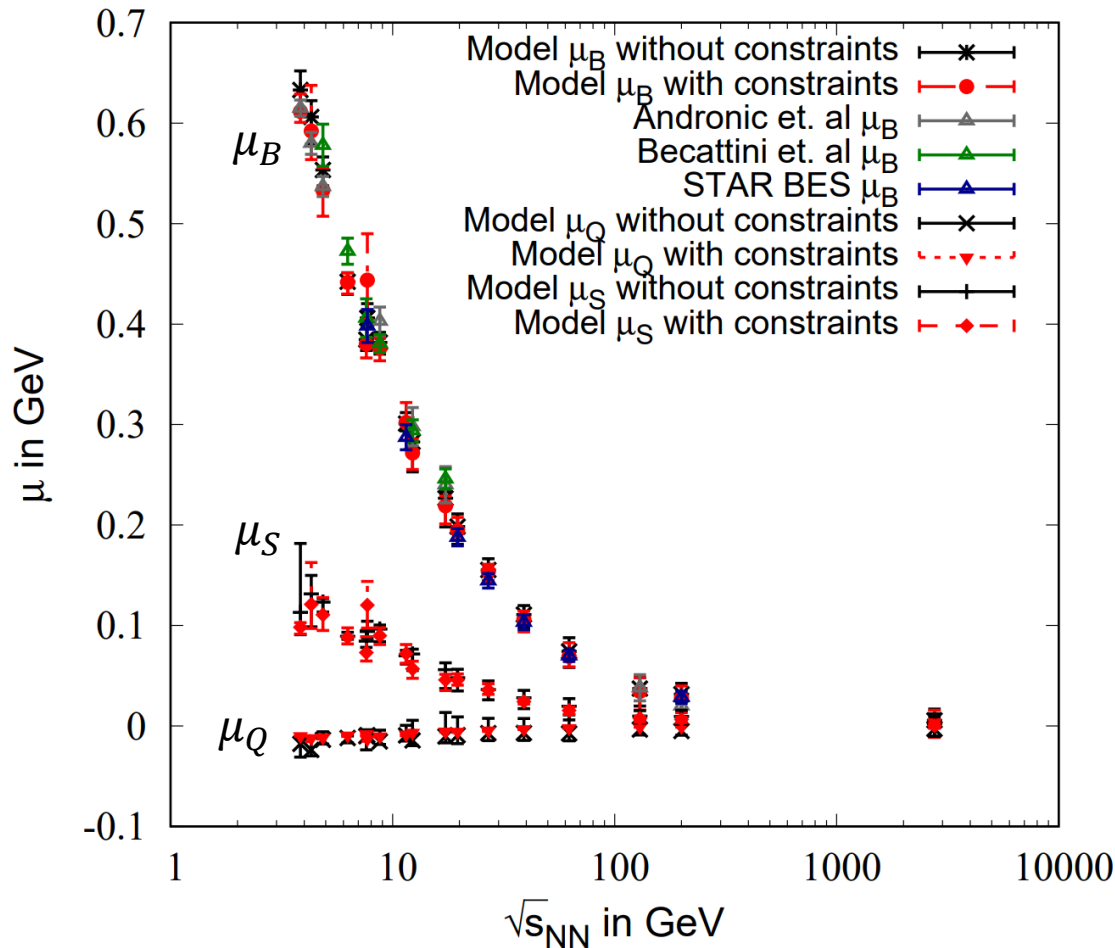
$$\delta\rho_{00}^{SITP} = \alpha_{sh} \partial_\mu(\beta u_\nu) \epsilon^{\langle\mu} \epsilon^{\nu\rangle}$$

$$\alpha_{sh} \equiv \mathcal{N}_0^{-1} T E_p \int \frac{d\varepsilon}{\pi} \frac{\partial n}{\partial \varepsilon} \mathcal{A}^2(\bar{p}^2 - M^2 + Re\bar{\Pi}) \quad \text{Off-Shell}$$

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Strange-Baryon Correspondence

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In Partonic Phase:

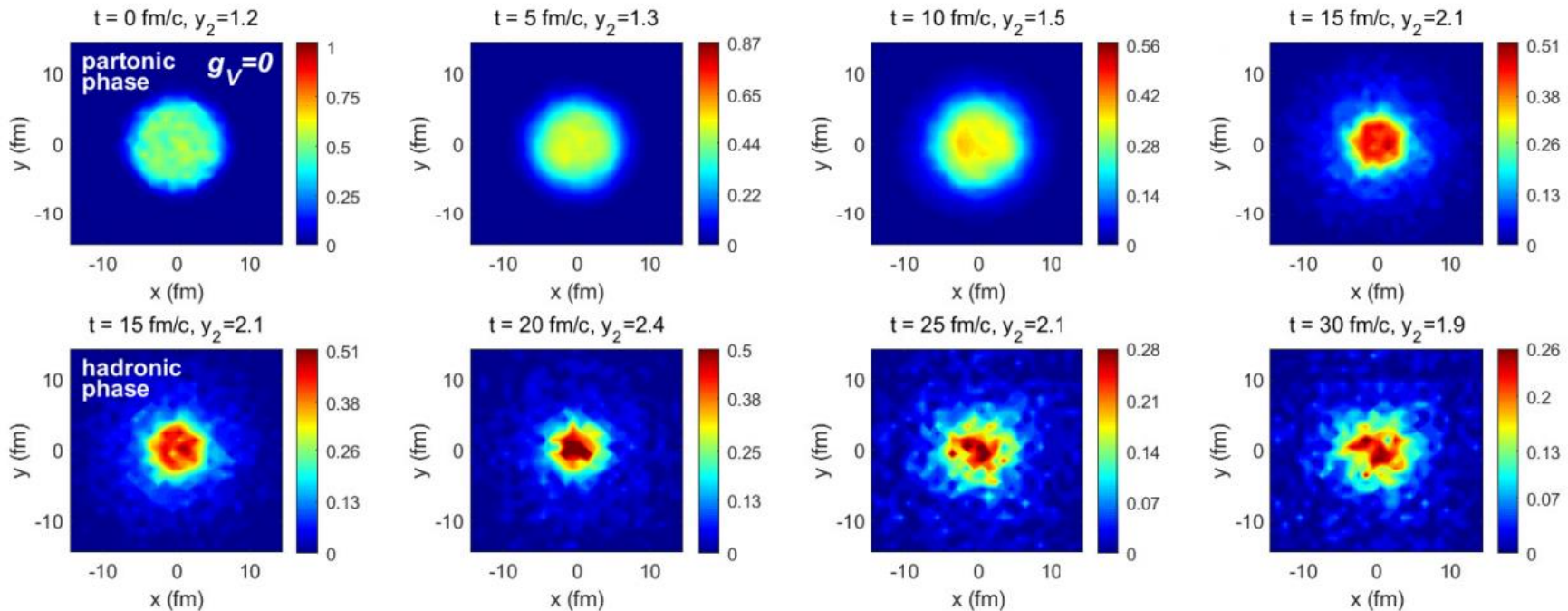
$$N_S \propto \exp\left(\frac{\frac{1}{3}\mu_B - \mu_S}{T}\right)$$

$$N_{\bar{S}} \propto \exp\left(\frac{-\frac{1}{3}\mu_B + \mu_S}{T}\right)$$

$$N_S = N_{\bar{S}} \Rightarrow \mu_S = \frac{1}{3}\mu_B$$

Strange-Baryon Correspondence

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K. Sun, et al., EPJA 57 (2021) 11, 313

Strange-Baryon Correspondence: $\partial(\beta\mu_S) \rightarrow \mu'_S(\mu_B)\partial(\beta\mu_B)$

Enhanced During a 1st –
order phase transition

A new probe of 1st – order phase transition?

Linear Response

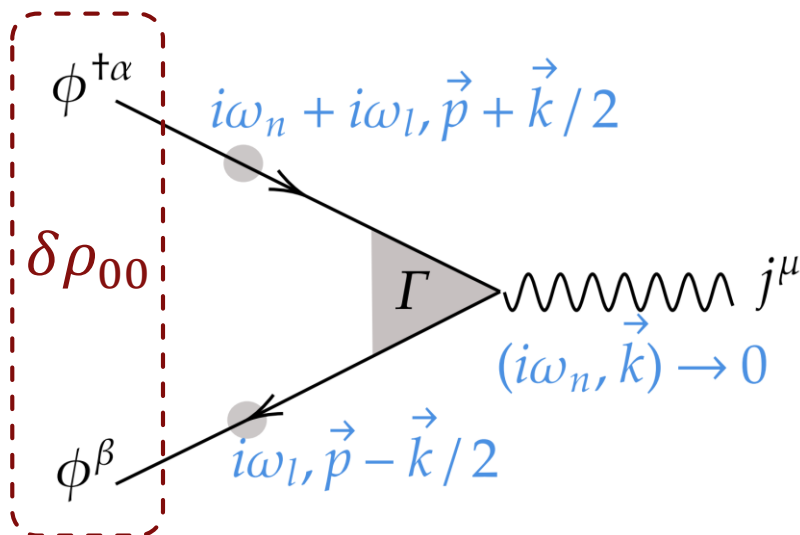
$$\delta\rho_{00} = \lim_{k^0 \rightarrow 0} \frac{\tilde{q}_J^\mu(k^0, \vec{k} = 0)}{2k^0} \frac{\partial_\mu(\beta\mu_S)}{\bar{\beta}}$$

In Equilibrium

Driven by S Charge Density and Thermal Gradients

$$\tilde{q}_J^\mu \equiv \int d^4x e^{ik \cdot x} \left[\delta\rho_{00} \left(x' + \frac{x}{2} \right), j^\mu \left(x' - \frac{x}{2} \right) \right]$$

(Belinfante) Stress-Energy Tensor



D. N. Zubarev,
Nonequilibrium statistical
thermodynamics

$$\delta\rho_{00}(\vec{p}) = \mathcal{N}^{-1} \left[\epsilon_{\langle\alpha\epsilon_{\beta}^0}^0 - \alpha_0 \tilde{\Delta}_{\alpha\beta} \right] \int d^3\vec{X} W_{(1)}^{\alpha\beta} \quad \text{Projectors and Polarizers}$$

$$W_{(1)}^{\alpha\beta} = E_p \int \frac{dp^0}{2\pi} \sum_{a,b=T}^L \mathcal{A}_a(p) \mathcal{A}_b(p) \Delta_a^{\beta\rho}(p) \Delta_b^{\sigma\alpha}(p) \text{Re} \left\{ \tilde{\Gamma}_{\rho\sigma}^{\mu}(p; p) \right\} \frac{\partial n}{\partial p^0} \frac{\partial_{\mu}(\beta\mu_s)}{\bar{\beta}} \quad \text{Bose Distribution}$$

$$\tilde{\Gamma}_{\rho\sigma}^{\mu}(p, p) = q_{\beta} \partial_{\vec{p}_{\mu}} \tilde{S}_{\rho\sigma}^{-1}(p)$$

Assumption:

- There is no pole on p^0 in $\tilde{\Gamma}_{\rho\sigma}^{\mu}(i\omega_n + p^0, \vec{p}; p^0, \vec{p})$
- Time reversesal symmetry on $\tilde{\Gamma}$
 $\tilde{\Gamma}_{\rho\sigma}^{\mu}(p; q) = \tilde{\Gamma}_{\sigma\rho}^{\mu}(q; p)$
- $\lim_{q \rightarrow 0} \partial_{q^0} \tilde{\Gamma}(p + q; p)$ is real
- Or, \mathcal{A} is analytic on the upper-half complex plane, and real on the real axis.

DITP (General Form)

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Sensitive to p Orientation

$$\delta\rho_{00}^{DITP} = \int \frac{d^3\vec{X}}{\mathcal{N}} \left[\left(\vartheta_{sp}^p \frac{\tilde{p}^\mu}{m} + \vartheta_{sp}^u u^\mu \right) \epsilon_{\langle\alpha\epsilon\beta\rangle} \tilde{\Delta}_L^{\alpha\beta} + \vartheta_\Delta \epsilon_\alpha \epsilon_\beta u^{(\alpha} \tilde{\Delta}_T^{\beta)\mu} - \alpha_0 \left(\vartheta_{tt}^p \frac{\tilde{p}^\mu}{m} + \vartheta_{tt}^u u^\mu \right) \right] \frac{\partial_\mu (\beta \mu_S)}{T}$$

$$\vartheta_{sp}^p = \vartheta_L^p - \vartheta_T^p; \quad \vartheta_{sp}^u = \vartheta_L^u - \vartheta_T^u; \quad \vartheta_{tt}^p = \vartheta_L^p + 2\vartheta_T^p; \quad \vartheta_{tt}^u = \vartheta_L^u + 2\vartheta_T^u$$

$$\vartheta_L^p = -q m T^2 E_p \int \frac{dp^0}{\pi} (1 + \partial_{p^2} \text{Re}\Pi_L) \mathcal{A}_L^2(p) \left(1 + \frac{\Omega^2 \vec{p}^2}{p^2 m^2} \right) \frac{\partial n}{\partial p^0}$$

$$\vartheta_L^u = -q T^2 E_p \int \frac{dp^0}{\pi} \left(\Omega + \Omega \partial_{p^2} \text{Re}\Pi_L + \frac{1}{2} \partial_{p^0} \text{Re}\Pi_L \right) \mathcal{A}_L^2(p) \left(1 + \frac{\Omega^2 \vec{p}^2}{p^2 m^2} \right) \frac{\partial n}{\partial p^0}$$

$$\vartheta_T^p = -q m T^2 E_p \int \frac{dp^0}{\pi} (1 + \partial_{p^2} \text{Re}\Pi_T) \mathcal{A}_T^2(p) \frac{\partial n}{\partial p^0}$$

$$\vartheta_T^u = -q T^2 E_p \int \frac{dp^0}{\pi} \left(\Omega + \Omega \partial_{p^2} \text{Re}\Pi_T + \frac{1}{2} \partial_{p^0} \text{Re}\Pi_T \right) \mathcal{A}_T^2(p) \frac{\partial n}{\partial p^0}$$

$$\vartheta_\Delta = q T^2 E_p \int \frac{dp^0}{\pi} \mathcal{A}_L(p) \mathcal{A}_T(p) \left(1 - \frac{p^0}{p^2} \Omega \right) \frac{p^0 \text{Re}(\Pi_T - \Pi_L)}{\vec{p}^2} \frac{\partial n}{\partial p^0}$$

Caused by L/T splitting → small

To Global Spin Alignment

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In a **static** medium

The polarizer ϵ_0 can be expressed explicitly in the MRF as

$$\epsilon_0 = \frac{1}{m} \begin{pmatrix} E_p & \mathbf{p} \\ \mathbf{p} & m\mathbb{I} + (E_p - m)\hat{\mathbf{p}}\hat{\mathbf{p}} \end{pmatrix} \begin{pmatrix} 0 \\ \hat{\mathbf{z}} \end{pmatrix}, \quad (21)$$

where $\hat{\mathbf{p}} \equiv \mathbf{p}/|\mathbf{p}|$, and $\hat{\mathbf{z}}$ is the spin quantization axis in the particle rest frame (PRF). Hence, in the MRF,

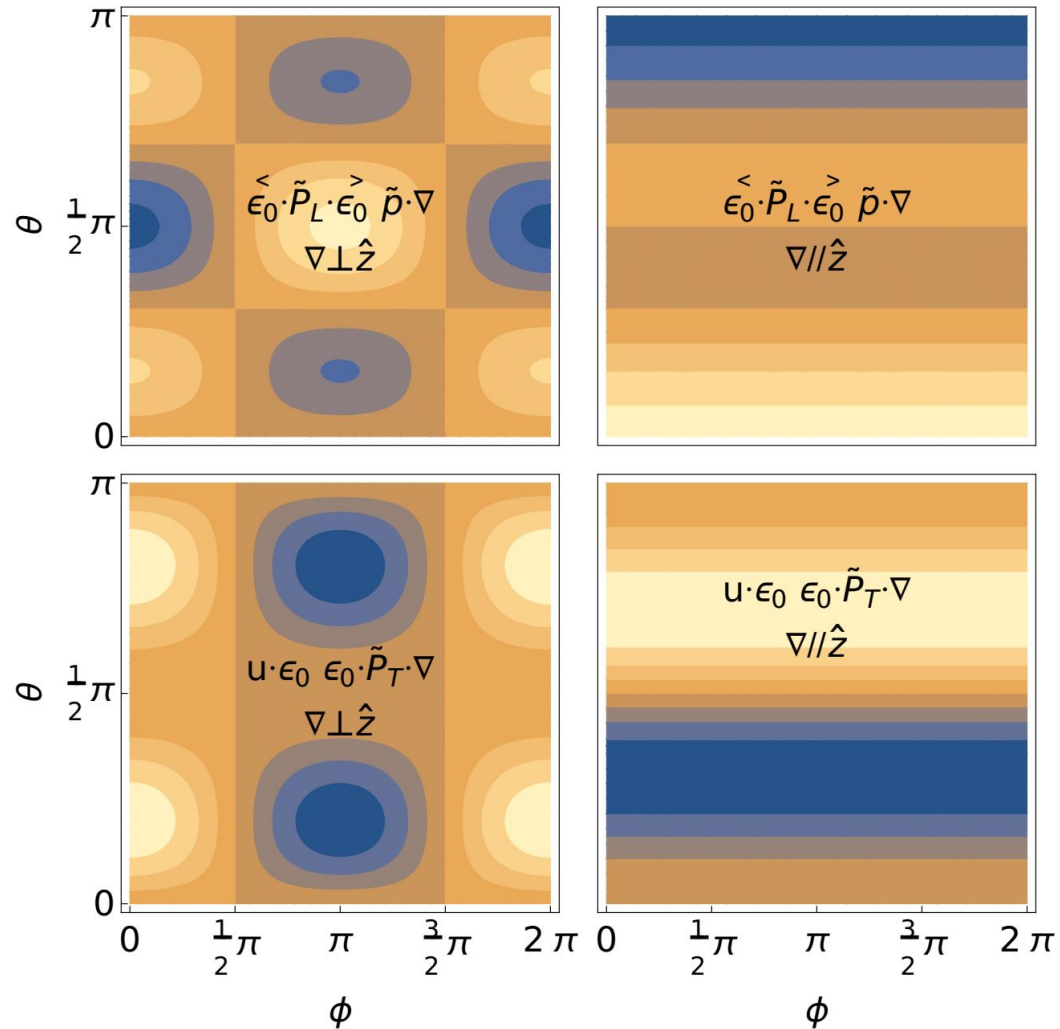
$$\begin{aligned} \epsilon_{\langle\alpha}^0 \epsilon_{\beta\rangle}^0 \tilde{P}_L^{\alpha\beta} \tilde{\mathbf{p}} \cdot \partial &= \left[\frac{(\mathbf{p} \cdot \hat{\mathbf{z}})^2}{\mathbf{p}^2} - \frac{1}{3} \right] (E_p \partial_t + \mathbf{p} \cdot \nabla), \\ \epsilon_{\langle\alpha}^0 \epsilon_{\beta\rangle}^0 \tilde{P}_L^{\alpha\beta} u \cdot \partial &= \left[\frac{(\mathbf{p} \cdot \hat{\mathbf{z}})^2}{\mathbf{p}^2} - \frac{1}{3} \right] \partial_t, \\ \epsilon_{\alpha}^0 \epsilon_{\beta}^0 u^{(\alpha} \tilde{P}_T^{\beta)\mu} \partial_{\mu} &= -\frac{(\mathbf{p} \cdot \hat{\mathbf{z}})}{m} [\hat{\mathbf{p}} \times (\hat{\mathbf{z}} \times \hat{\mathbf{p}})] \cdot \nabla. \end{aligned} \quad (22)$$

Tensor structures related to the p-orientation

All vanish after the integration over p-orientation → **Local Polarization Only**

Oriental Distribution

In a **static** medium



- Dissipative Structure
- Spin Alignment as Dissipative Structure
- Shear Induced Tensor Polarization (SITP)
- Diffusion Induced Tensor Polarization (DITP)
- **Summary & Outlook**

- Discovery of SITP & DITP, with a magnitude proportional to $\partial(\beta u)$ & $\partial(\beta\mu_s)$
- Both SITP & DITP are dissipative → Spin alignment as a dissipative structure in spin space.
- The transport coefficients are evaluated non-perturbatively, under certain assumptions, by employing the Ward-Takahashi identity.
- Coefficients are sensitive to the medium modification to the spectral functions → SITP & DITP employed as novel probe of in-medium spectral property.
- Off-Shell Effect → SITP; L & T Splitting → SITP & DITP
- SITP → Global & Local Spin Alignment; DITP → Local Spin Alignment in static medium.
- SITP is promising for describing the pT dependencies.
- Once the “local” spin alignments are measured, the DITP effect might be a novel probe of the QCD first order phase transition

Validity of Assumption:

- There is no pole on p^0 in $\tilde{\Gamma}_{\rho\sigma}^{\mu\nu}(i\omega_n + p^0, \vec{p}; p^0, \vec{p})$ ✗
- Time reversal symmetry on $\tilde{\Gamma}$
 $\tilde{\Gamma}_{\rho\sigma}^{\mu\nu}(p; q) = \tilde{\Gamma}_{\sigma\rho}^{\mu\nu}(q; p)$ ✓
- $\lim_{q \rightarrow 0} \partial_{q^0} \tilde{\Gamma}(p + q; p)$ is real ?
- Or, \mathcal{A} is analytic on the upper-half complex plane, and real on the real axis. ✗

- Evaluate the transport coefficients of SITP & DITP with the mesonic spectral functions obtained using FRG.
- Hydro-gradients at freeze-out at various collisional energies obtained using iEBE-MUSIC simulation.
- Look into the freeze-out condition phenomenologically.