

Probing dense QCD matter with neutron stars

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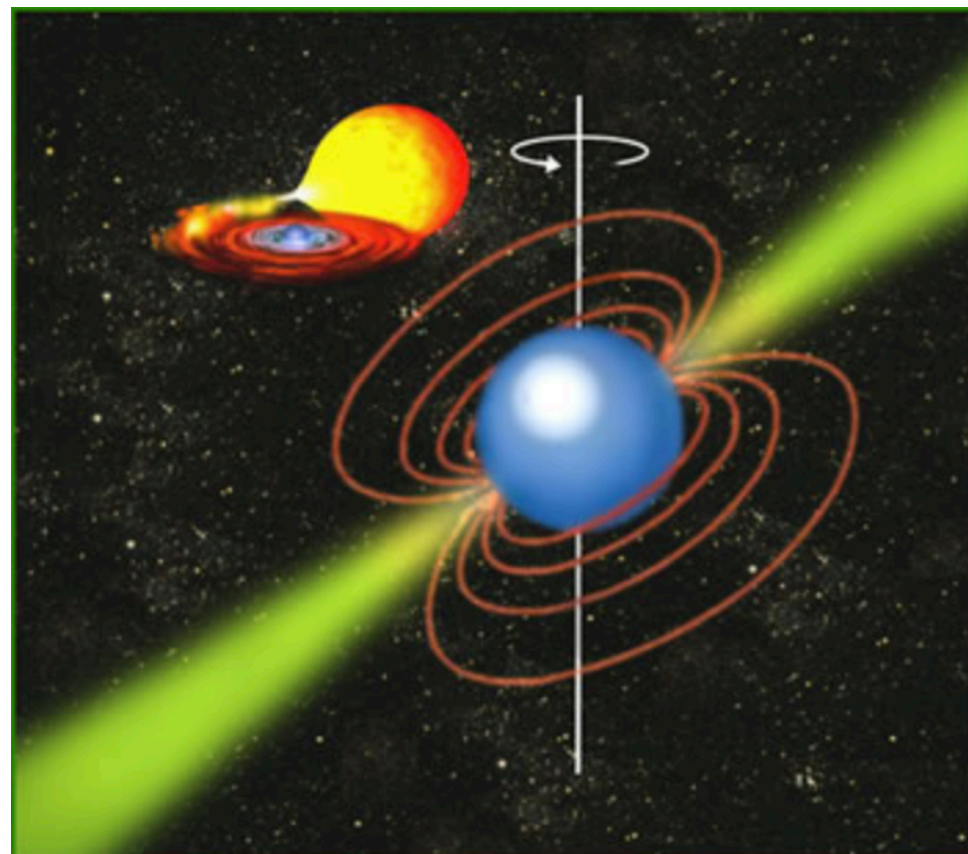
李政道研究所
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The 20th International Conference on QCD in
Extreme Conditions (XQCD 2024)@Lanzhou

July 18th, 2024

Motivation

the most compact objects
second only to black holes



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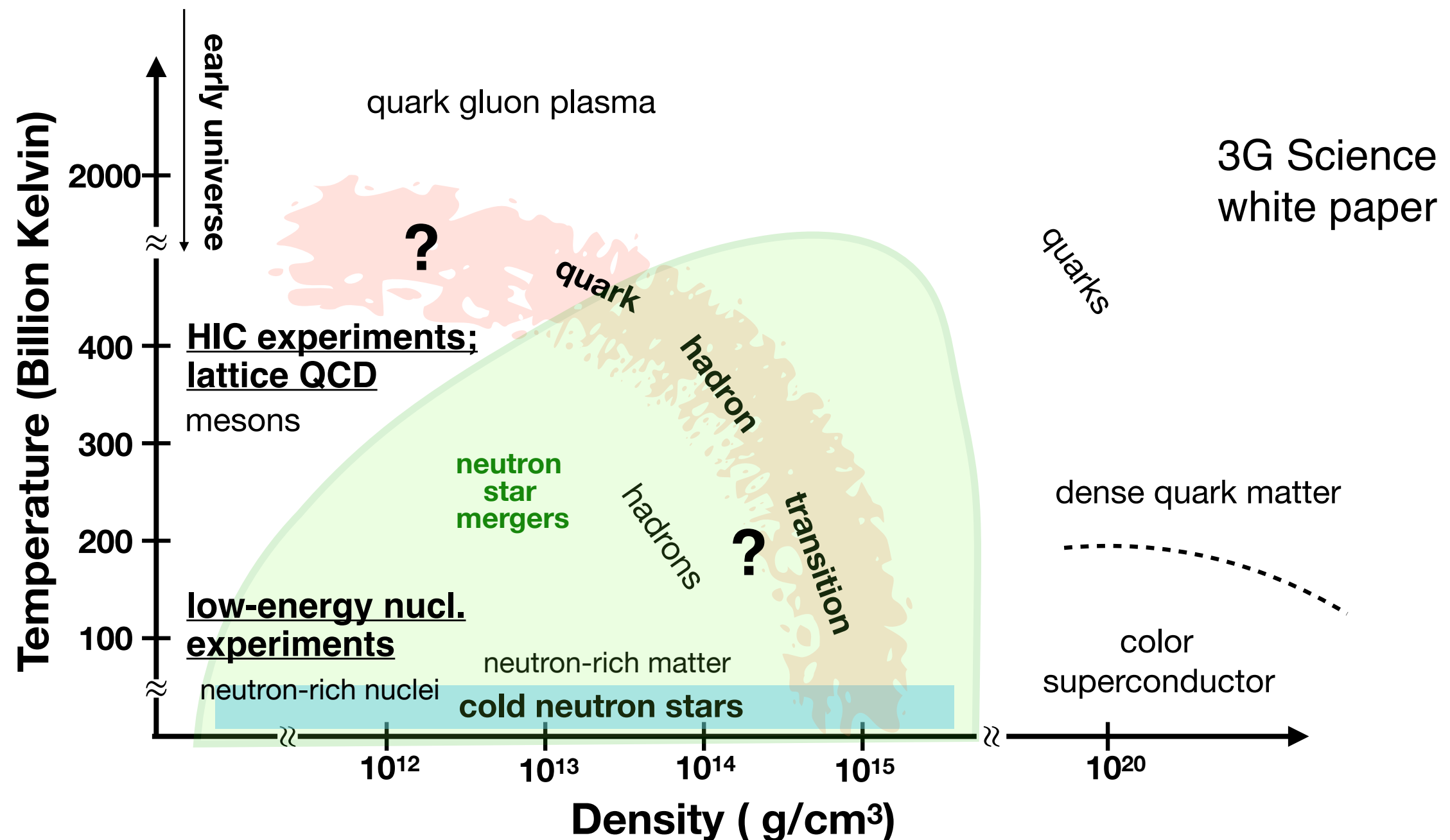
- still far from understanding NSs' composition over half a century since their discovery..
- NS mass-radius \leftrightarrow pressure vs. energy density (***equation of state***): important, yet not enough

main sources for LIGO-Virgo-KAGRA:

- NS, BH binary mergers WDs: $M/R \sim 10^{-4}$
- supernovae, NS/BH formation NSs: $M/R \sim 0.2$
- spinning NSs in x-ray binaries BHs: $M/R = 0.5$
- isolated NSs: instabilities, deformations

mass	radius	density	initial temp
$\sim 1.4 M_{\odot}$	$\mathcal{O}(10 \text{ km})$	$\gtrsim \rho_{\text{nuclear}}$	$\sim 30 \text{ MeV}$

Laboratory for theoretical physics



- no terrestrial experiments can probe such high densities
- reliable first-principle calculations break down at the strongly-interacting regime
- can't calculate properties of cold dense matter; must **observe!**

What can we observe?

- orbital characteristics in binaries
- surface luminosity
- spin
- gravitational waves (NS merger)
- neutrinos (supernova)
- explosions and flares

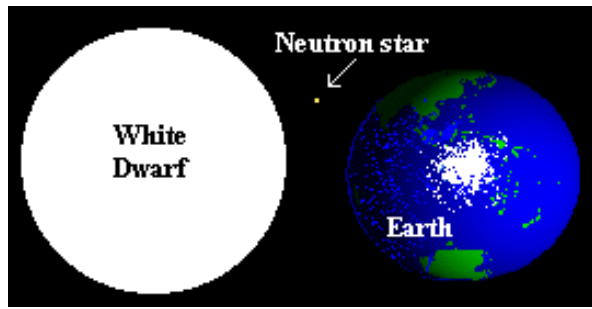
What can we infer?

ground state EoS

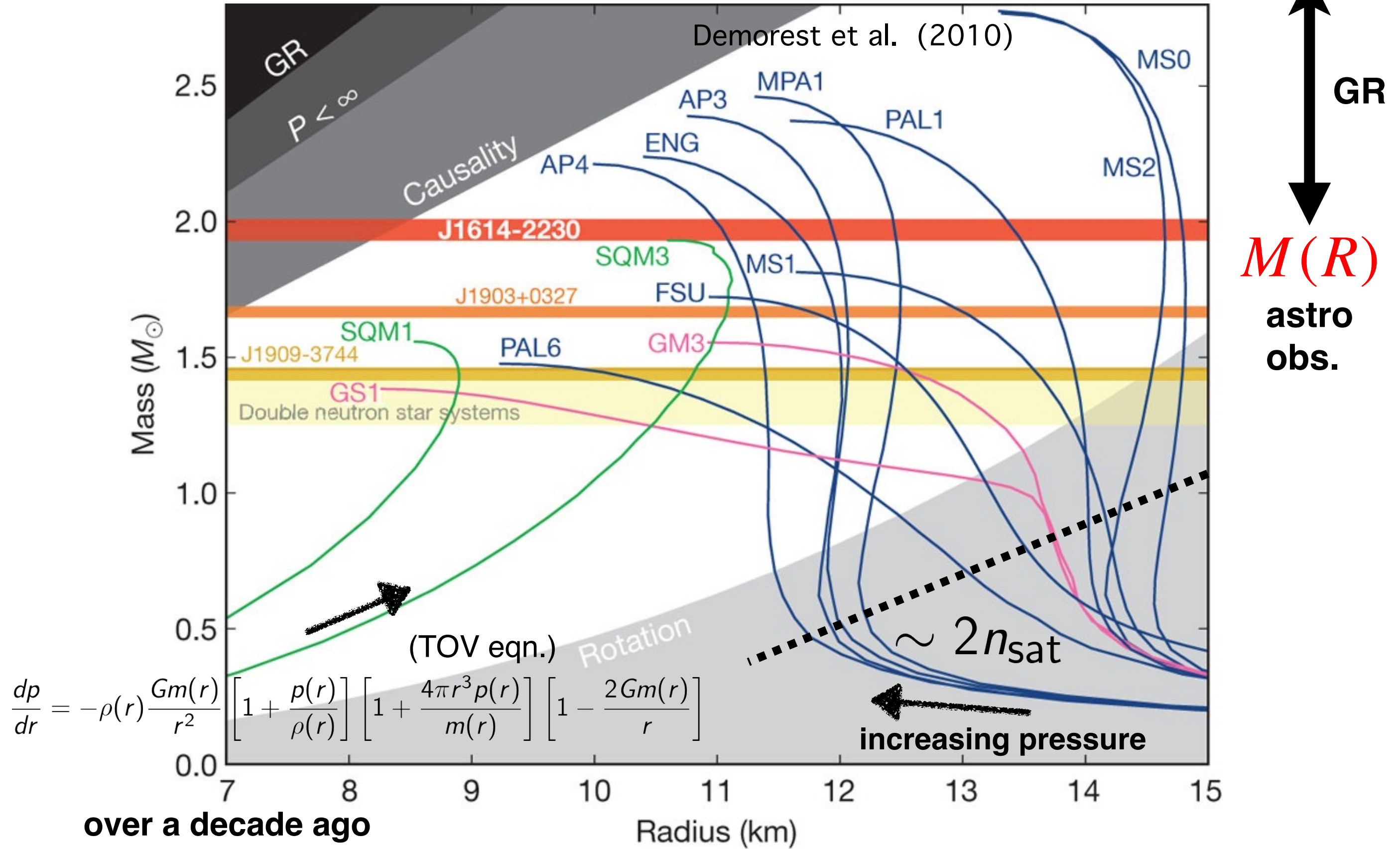
- mass, radius, tidal deformability
- moment of inertia, crust thickness
- oscillation frequencies

lower energy excitations

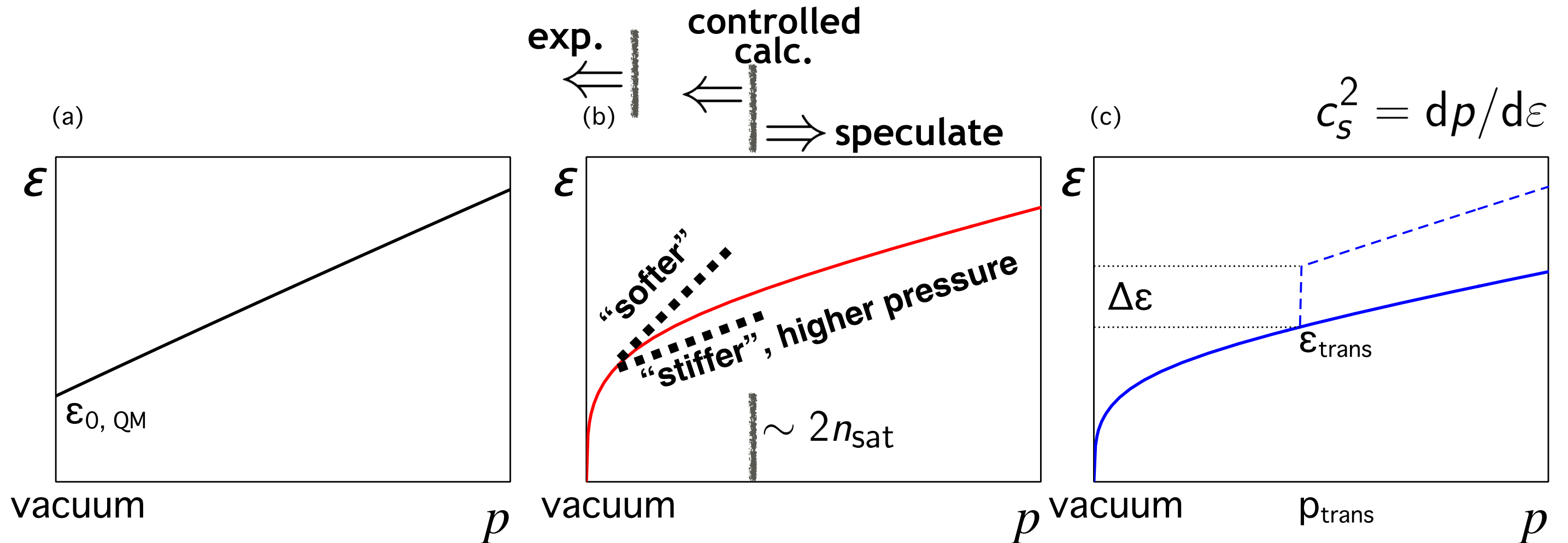
- surface & internal temperatures
- neutrino cooling & scattering rates
- electrical & thermal conductivities
- damping rates



NS mass-radius diagram

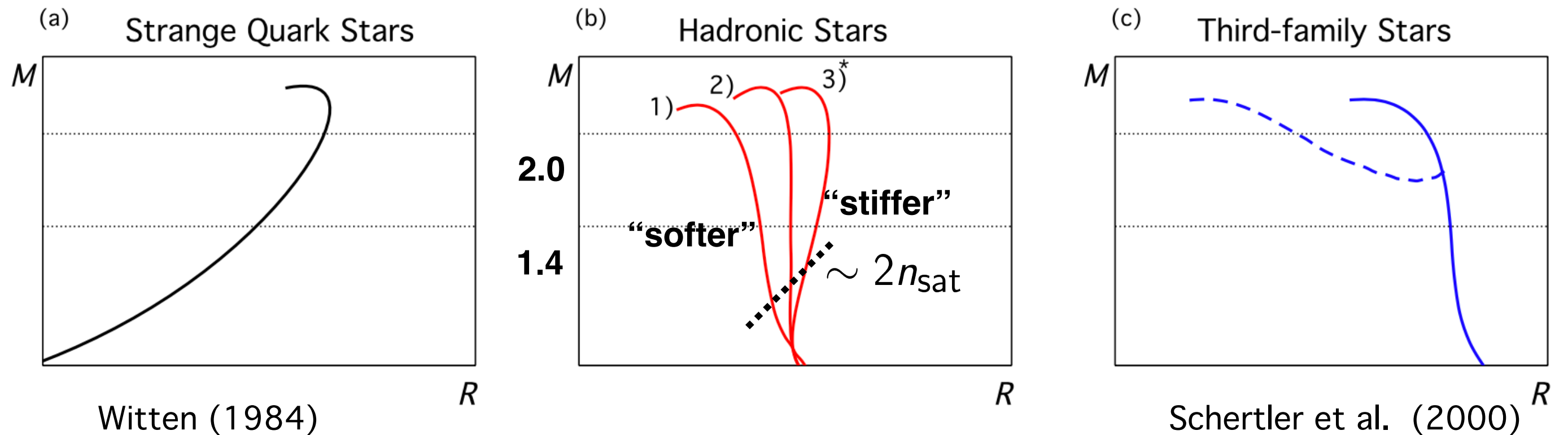


Schematic EoSs from theory



- self-bound quark stars with a bare surface e.g. **strange matter hypothesis**
- continuous (and mostly smooth) profile for normal hadronic EoSs; *also possible with weak/mild phase transition or crossover
- substantial softening e.g. discontinuity in the energy density induced by a strong sharp phase transition; possibly lead to **“third-family stars”**

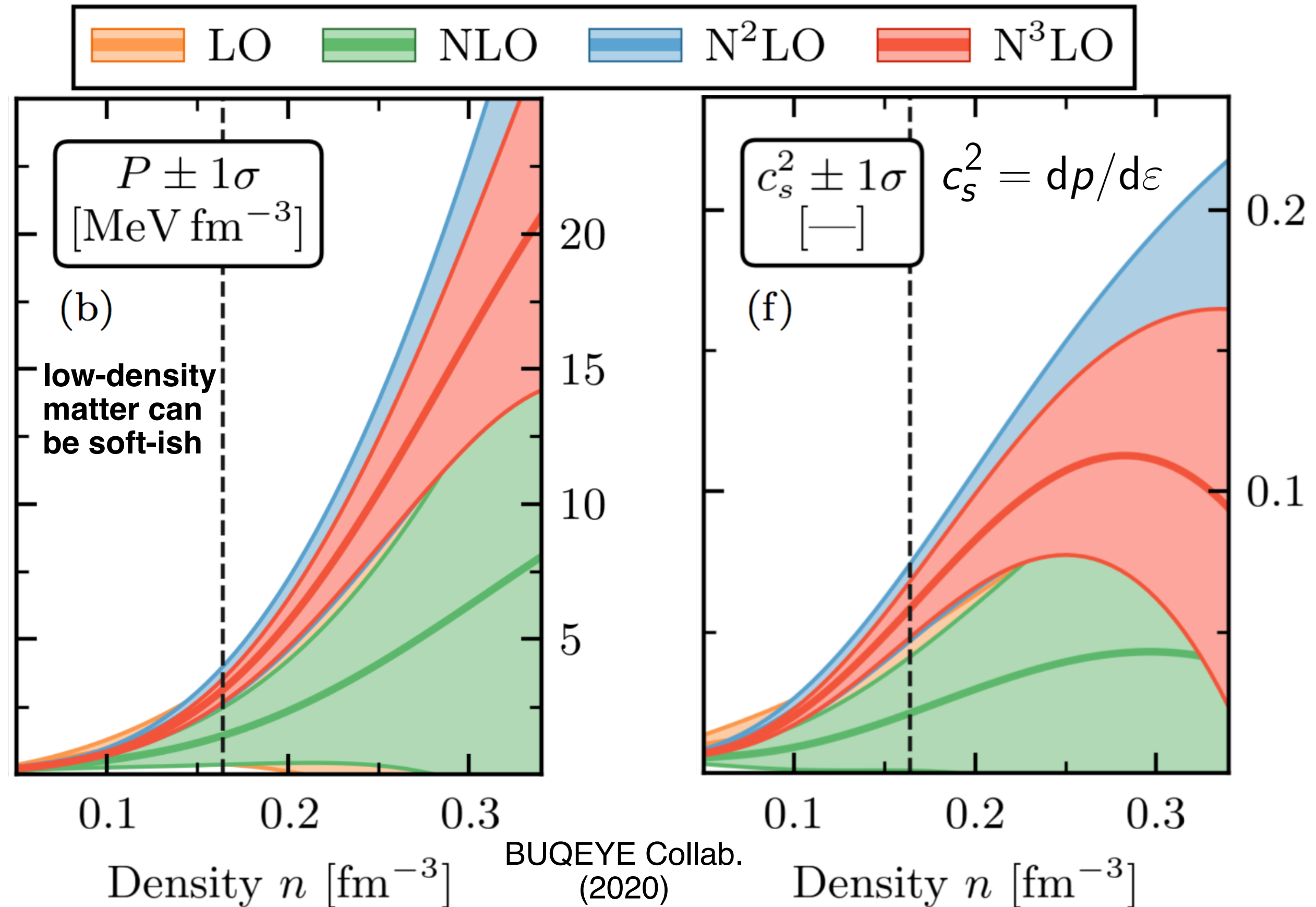
Categories of the $M-R$ relation



- self-bound quark stars with a bare surface e.g. **strange matter hypothesis**
- continuous (and mostly smooth) profile for normal hadronic EoSs; *also possible with weak/mild phase transition or crossover
- substantial softening e.g. discontinuity in the energy density induced by a strong sharp phase transition; possibly lead to **"third-family stars"**

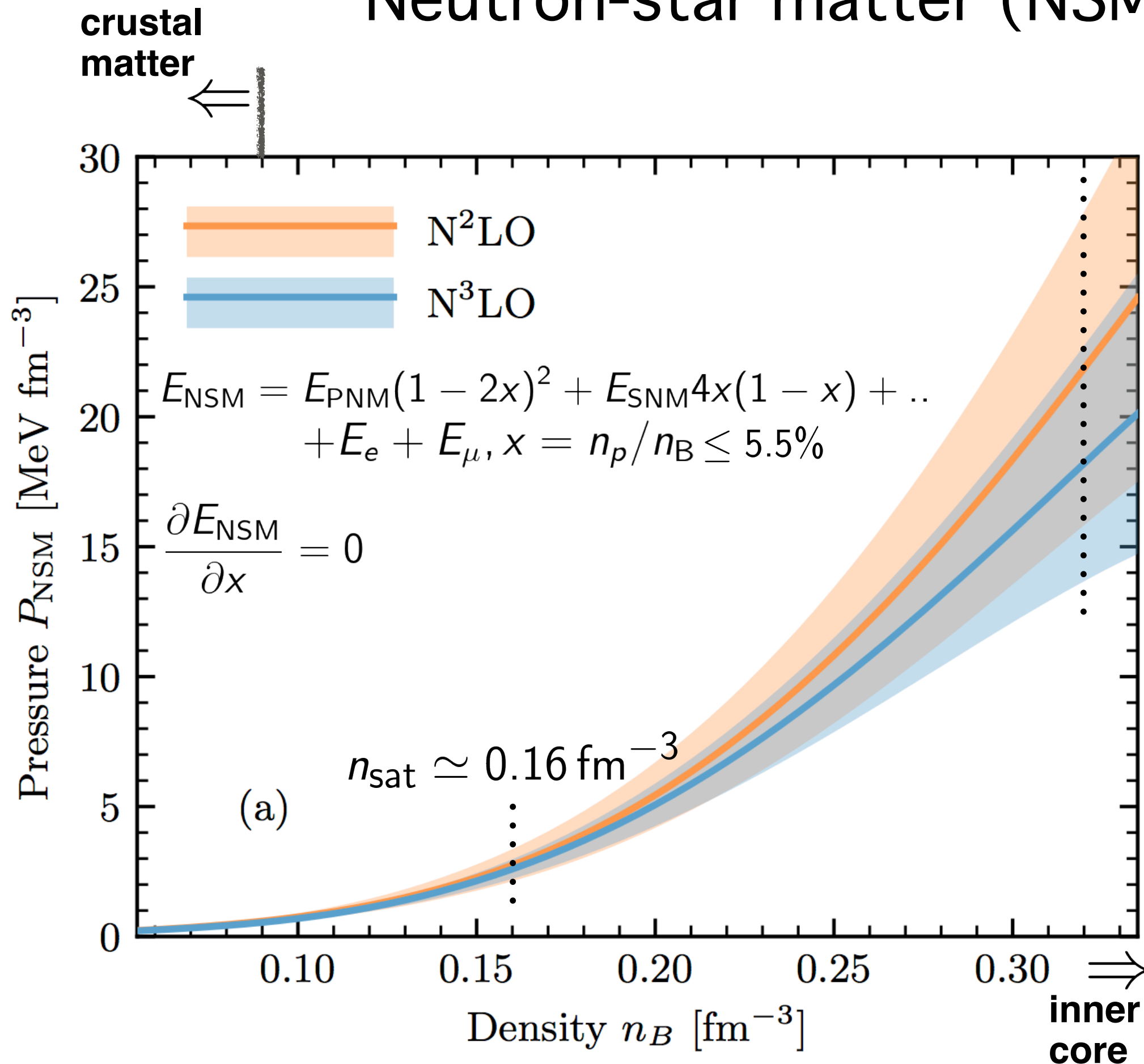
Pure neutron matter (PNM)

Drischler et al.
arXiv:2004.07232



Neutron-star matter (NSM)

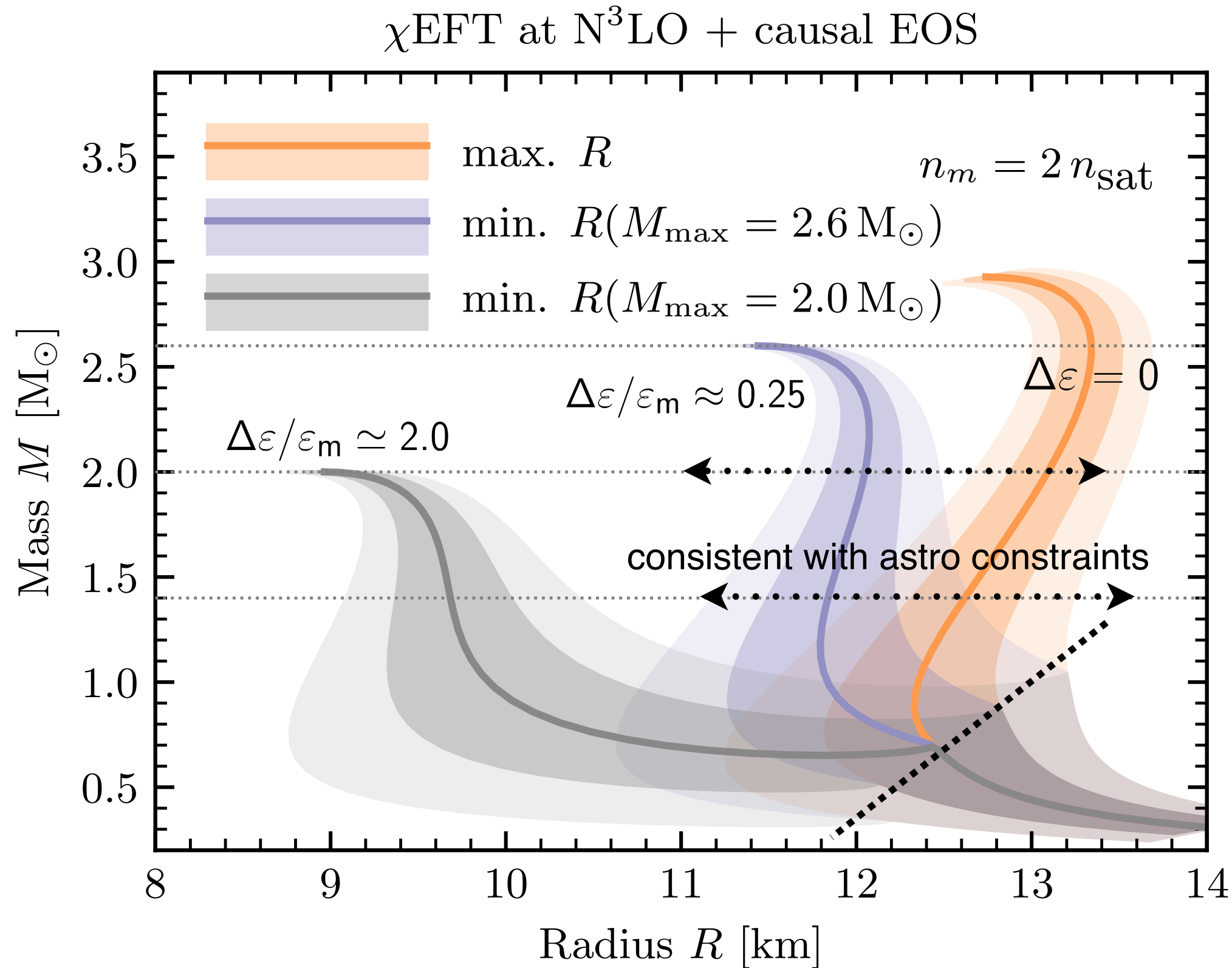
Drischler et al.
(including **SH**),
arXiv:2009.06441



- pressure at low densities [**outer core**] controls typical NS radii: stiff or soft?
- reliably **quantified** uncertainties from chiEFT for beta-equilibrated NSM
- less than **~5%** deviation from PNM pressures
- to **extrapolate** or match at higher densities in the inner core

Bounds from causality

Drischler et al.
(including **SH**),
arXiv:2009.06441



- pressure at low densities [**outer core**] controls typical NS radii: stiff or soft?
- reliably **quantified** uncertainties from χ EFT for beta-equilibrated NSM
- absolute **causal** limits imposed at high densities
- confronted with data: **interplay** between M_{max} and NS radii

Measuring NS masses and radii

pulsar timing (radio) can accurately measure masses

- most are between $1.2M_{\odot}$ and $1.5M_{\odot}$; lowest well-measured mass is $1.174 \pm 0.004M_{\odot}$, highest are $2.08 \pm 0.07M_{\odot}$ and $2.01 \pm 0.04M_{\odot}$
- higher masses are found for some sources (notably black widow pulsars) but these estimates have large uncertainties

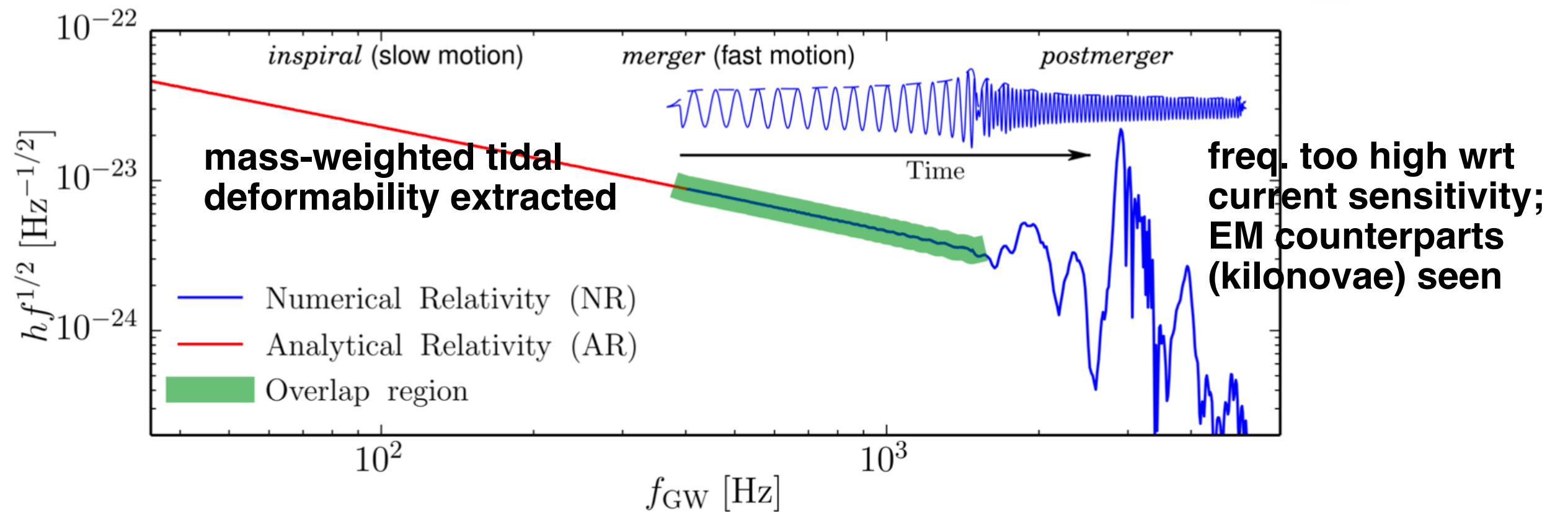
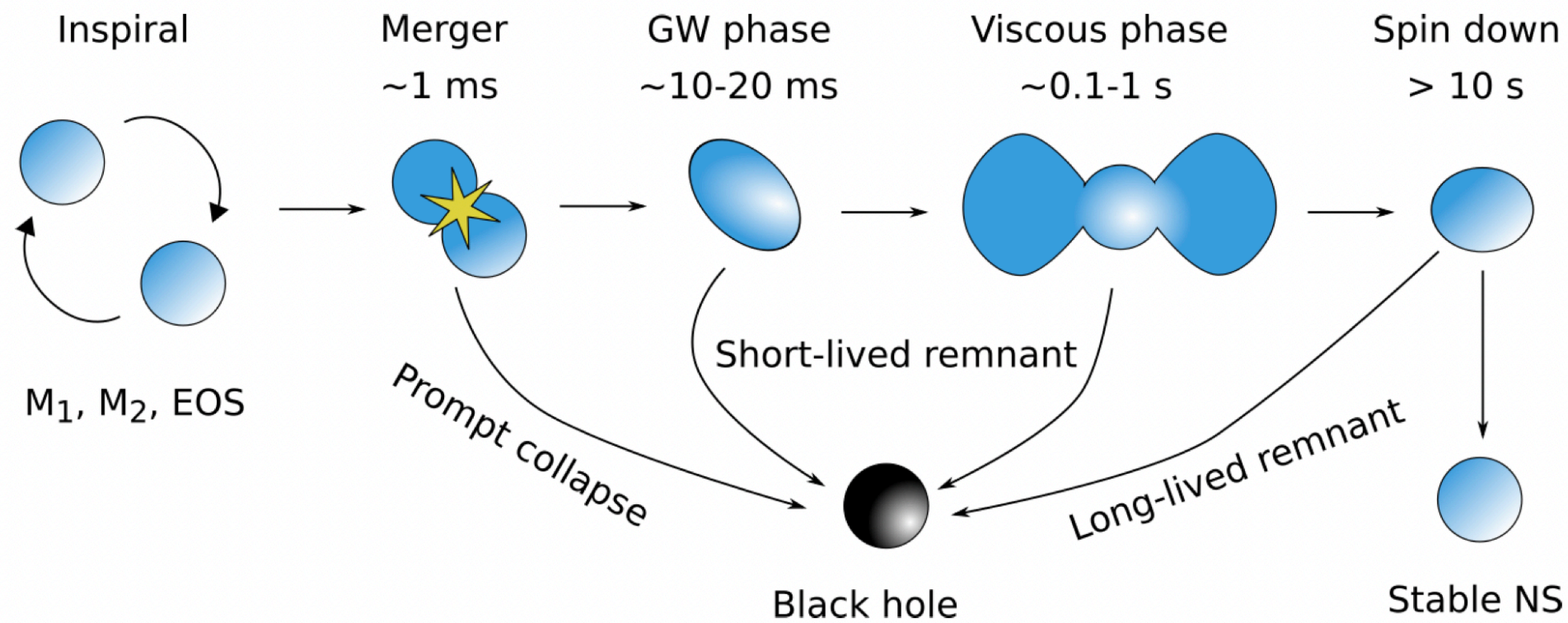
x-ray observations yield radii, but uncertain to a few km:

- quiescent binary sources in globular clusters
- thermonuclear explosions leading to photospheric radius expansion bursters on accreting neutron stars in binaries
- pulse **profile modeling of hot spots** on rapidly rotating neutron stars, e.g., *Neutron Star Interior Composition ExploreR (NICER)* mission

gravitational waves from merging binary neutron stars (BNSs) measure masses and tidal deformabilities

Stages of evolution in BNS mergers

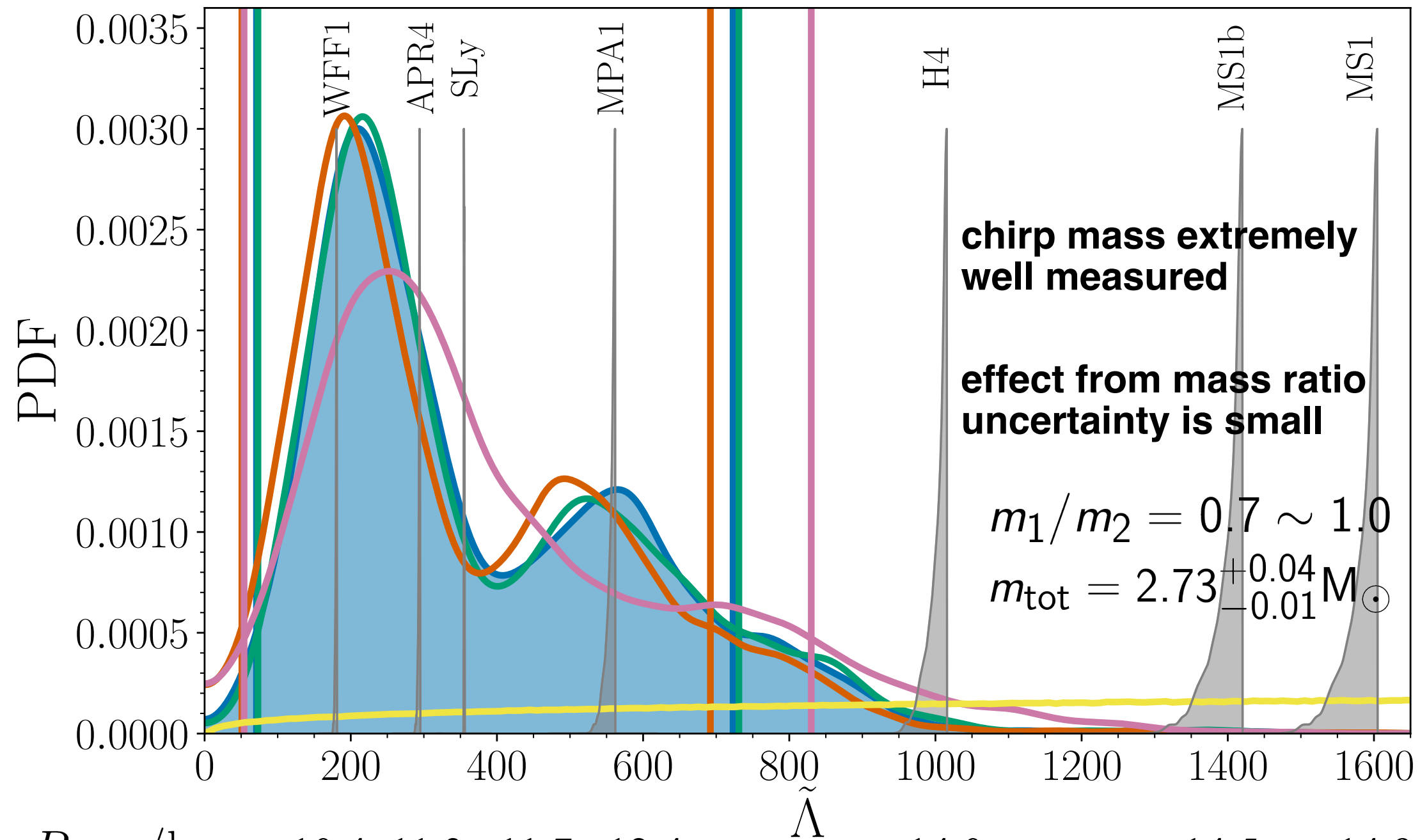
Radice et al. (2020)



Robust limit on NS radius from GW170817

$$\mathcal{M} = (m_1 m_2)^{3/5} / (m_1 + m_2)^{1/5} = 1.186^{+0.001}_{-0.001} M_{\odot}$$

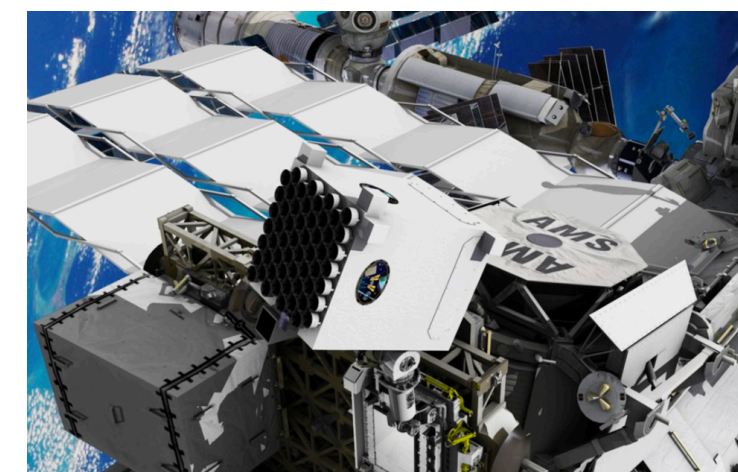
LVC collaboration, arXiv:1805.11579



- **smaller, more compact NS [<13.5 km strongly favored]**

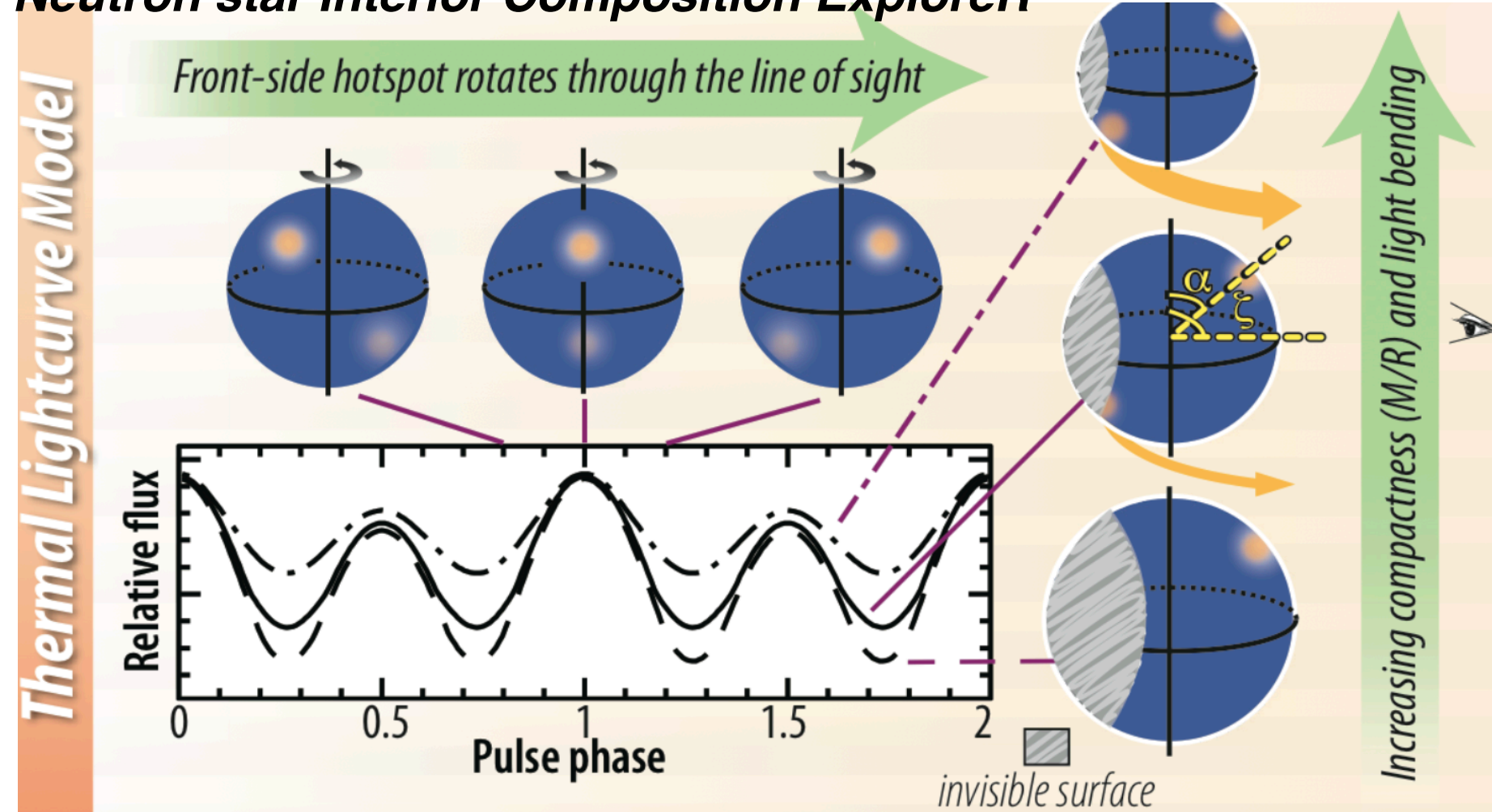
- **larger, puffier NS [almost ruled out..]**

NS radii from hotspots

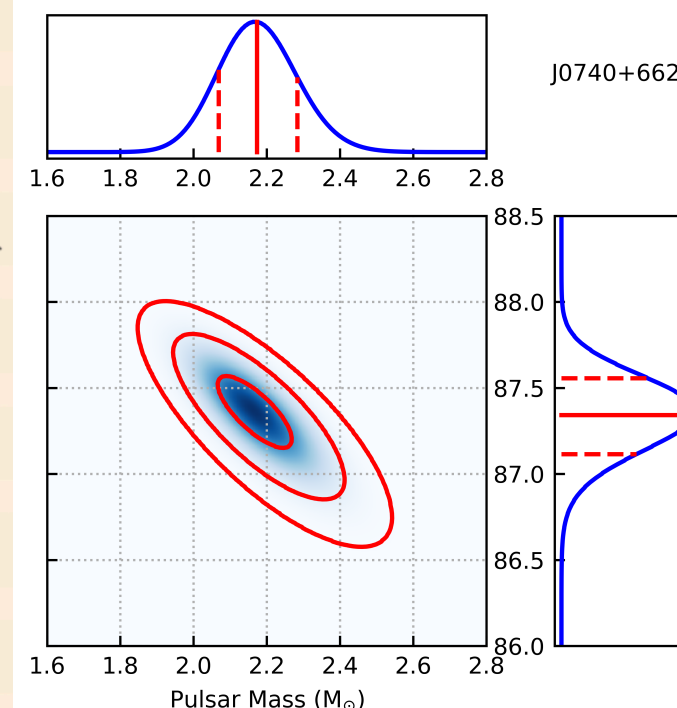


- light-curve modeling of **x-ray** pulse profiles that are sensitive to the **stellar compactness M/R**

Neutron star Interior Composition ExploreR



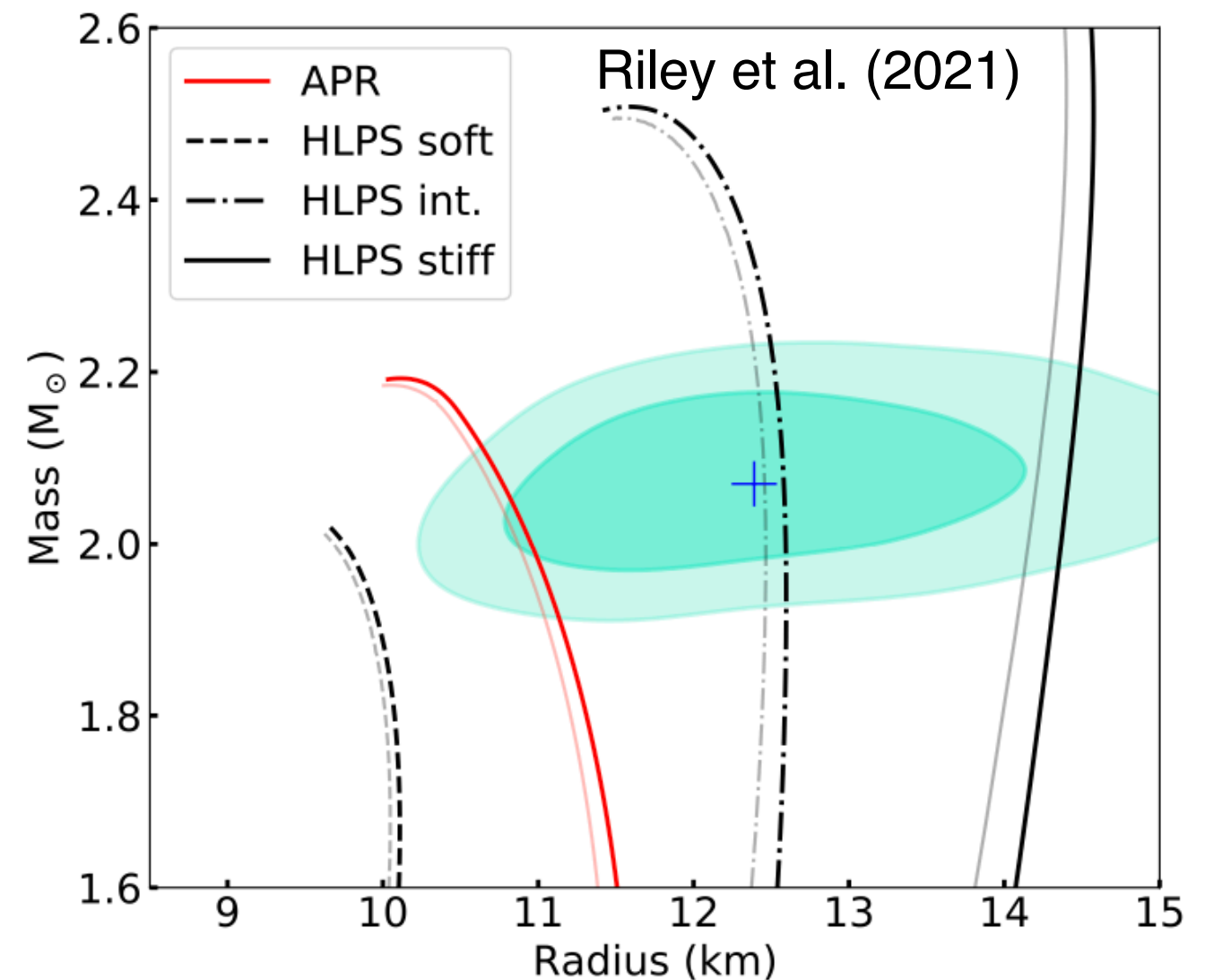
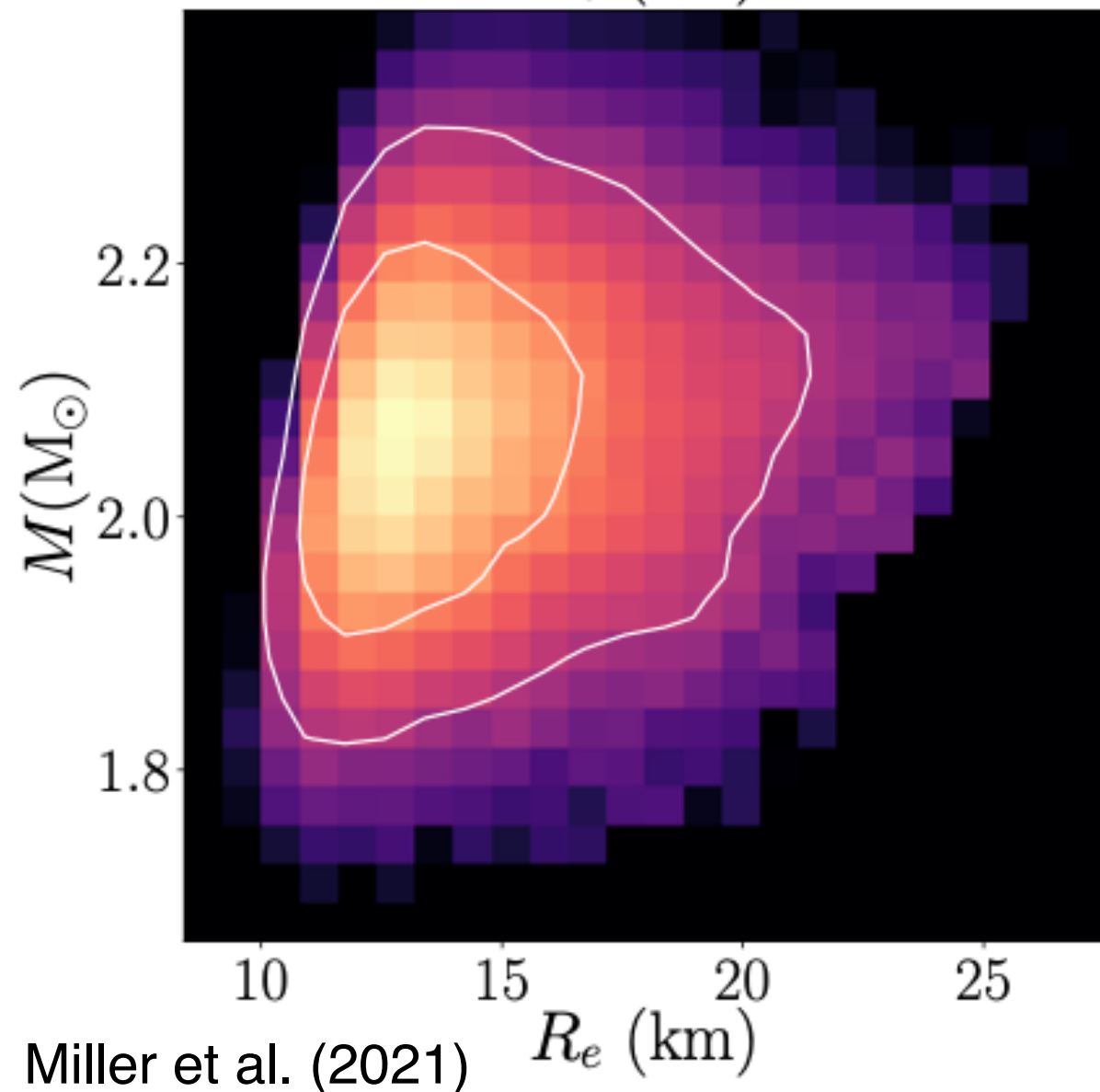
PSR J0740+6620



Cromartie et al.
Nature Astronomy (2019)

- recent data on the **heaviest NS known** so far: combined information with precise mass measurements through **Shapiro delay (radio)**

NS radii from hotspots



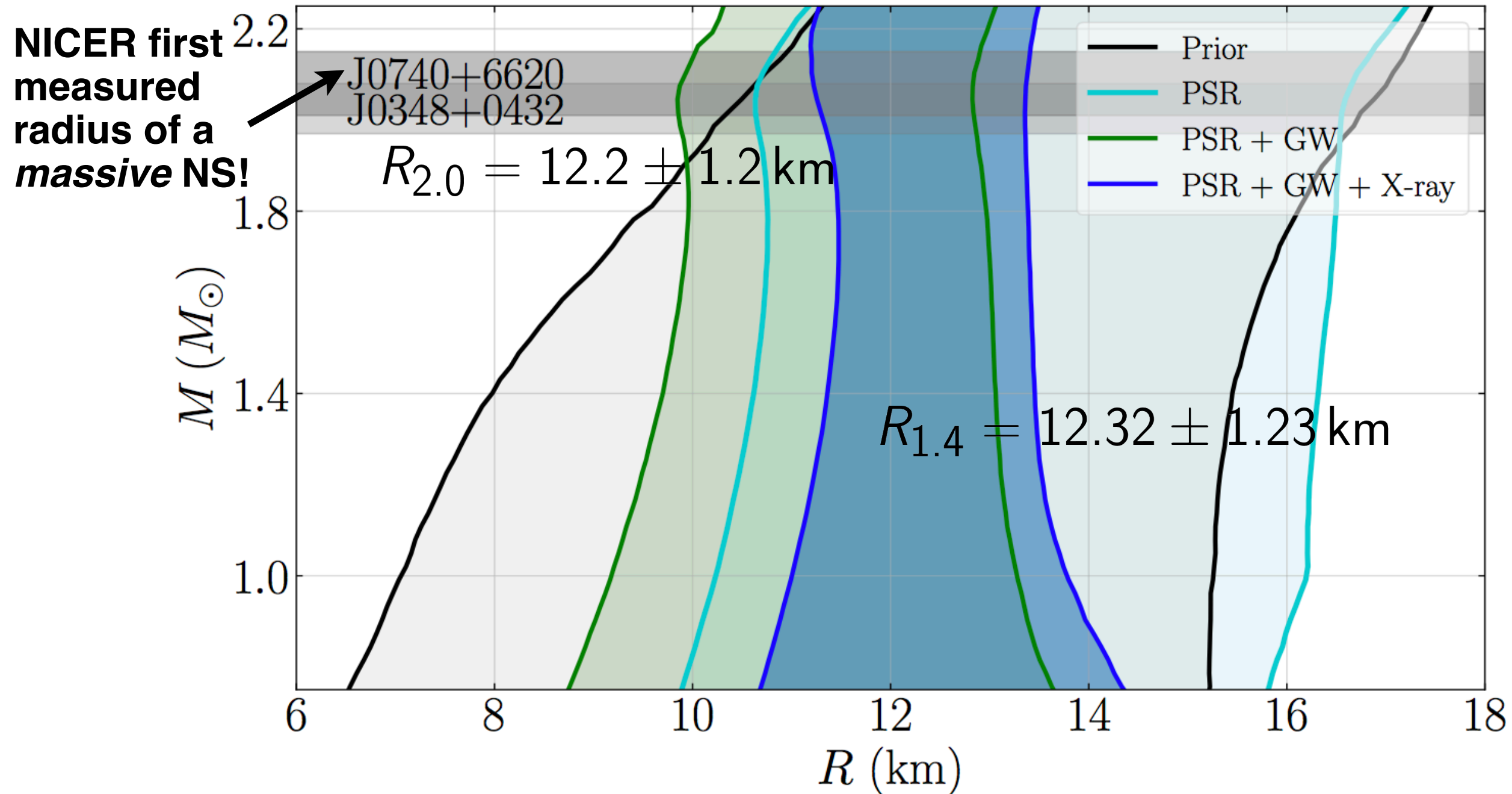
(new!) radius of *massive* PSR J0740+6620 $\sim 2 M_\odot$ $13.7^{+2.6}_{-1.5}$ km vs. $12.4^{+1.3}_{-1.0}$ km

previously: *canonical-mass* PSR J0030+0451 $\sim 1.4 M_\odot$

- analyses of waveforms produced by hotspots of rotation-powered pulsars
- relatively stiffer EoS at intermediate ($2 \sim 3 n_{\text{sat}}$) densities **opposite to GW constraints**

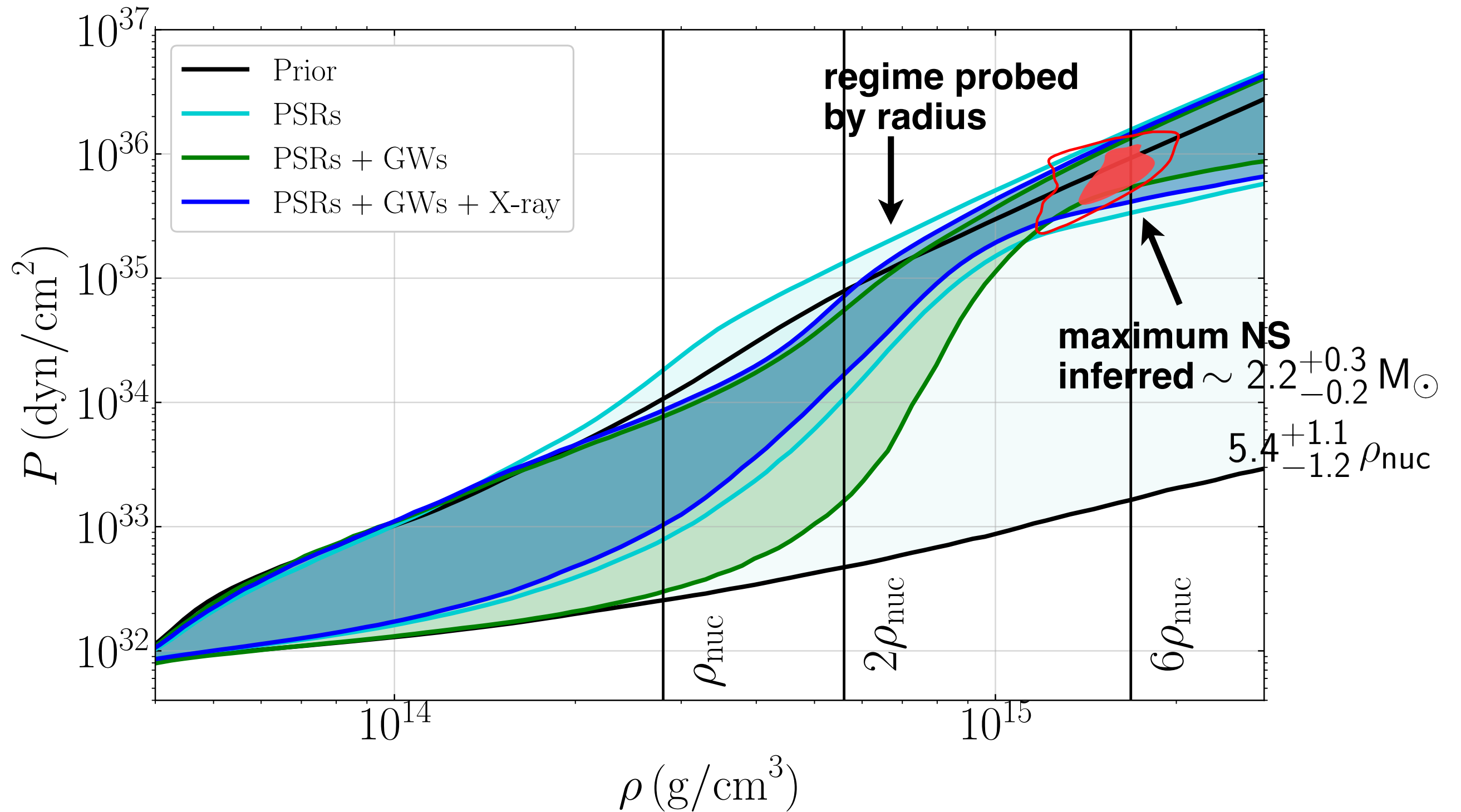
Multimessenger constraints

Legred et al.
(including **SH**),
arXiv:2106.05313



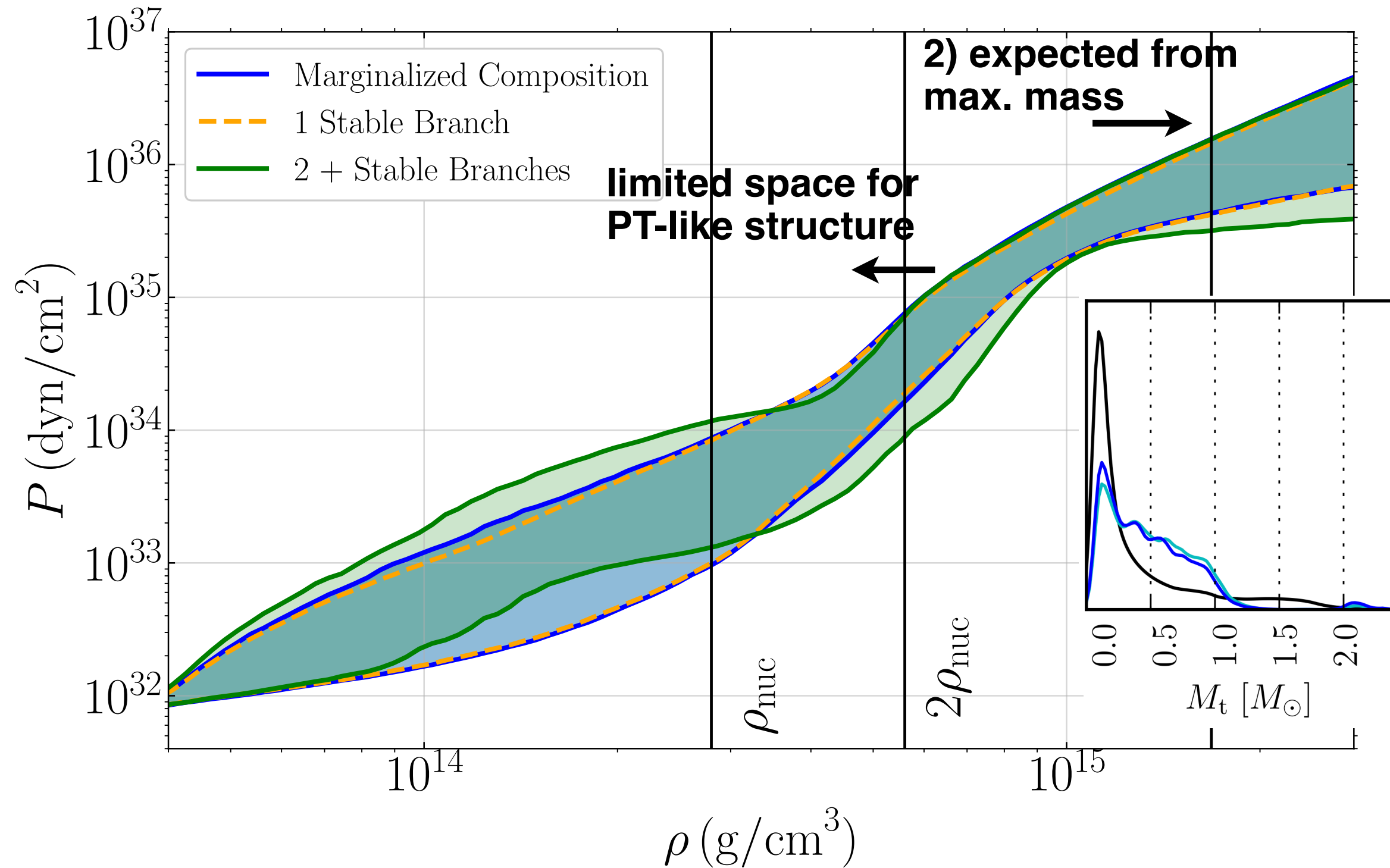
- nonparametric survey conditioned on ensembles of existing model EoSs
- GW170817+190425, NICER J0030 & J0740, and massive pulsars

Pressure vs. density



- towards a converging picture of the EoS at intermediate densities
- (90% symmetric credible intervals) best compatibility with data

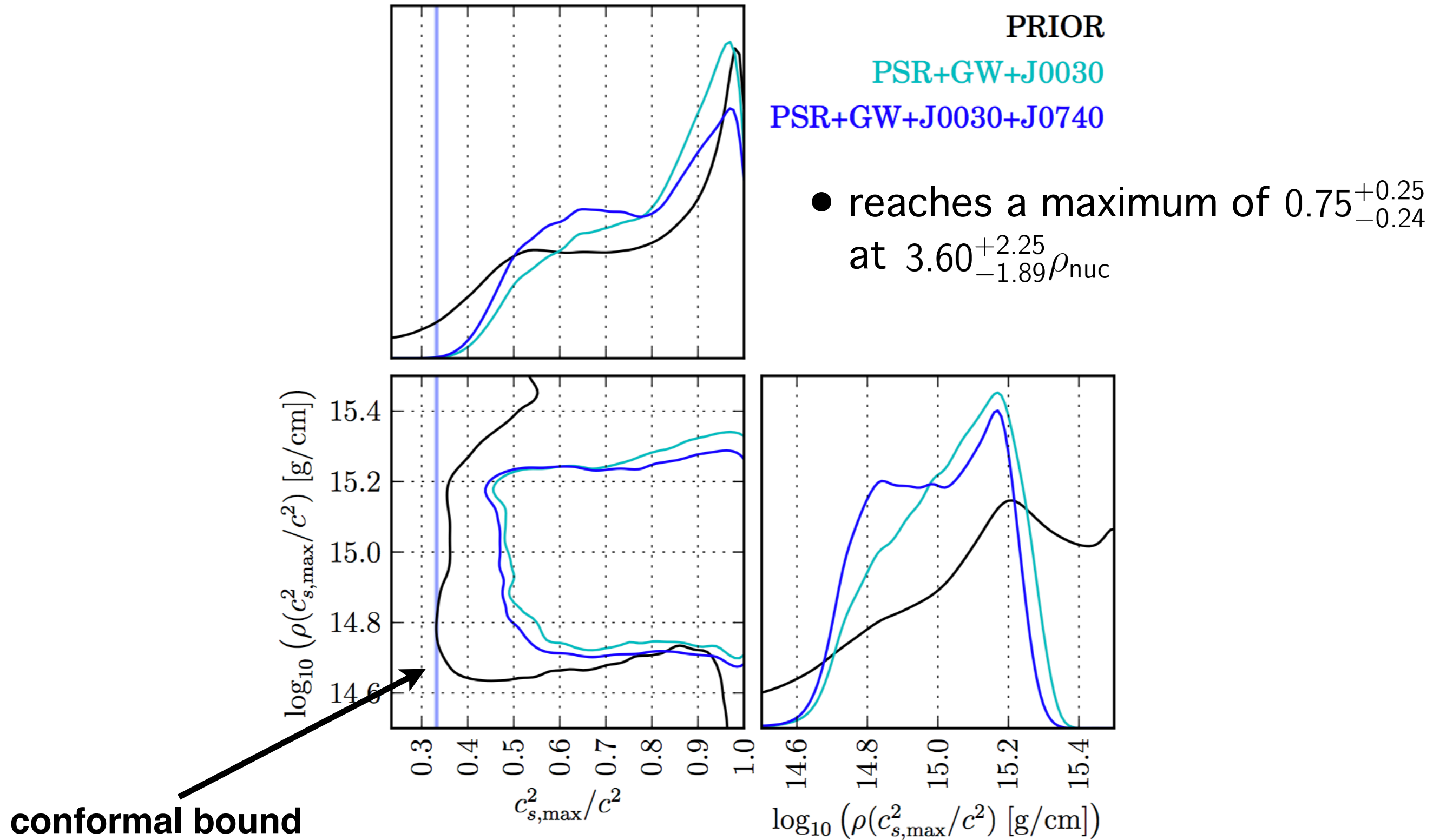
Single branch (minimal) vs. multiple branches



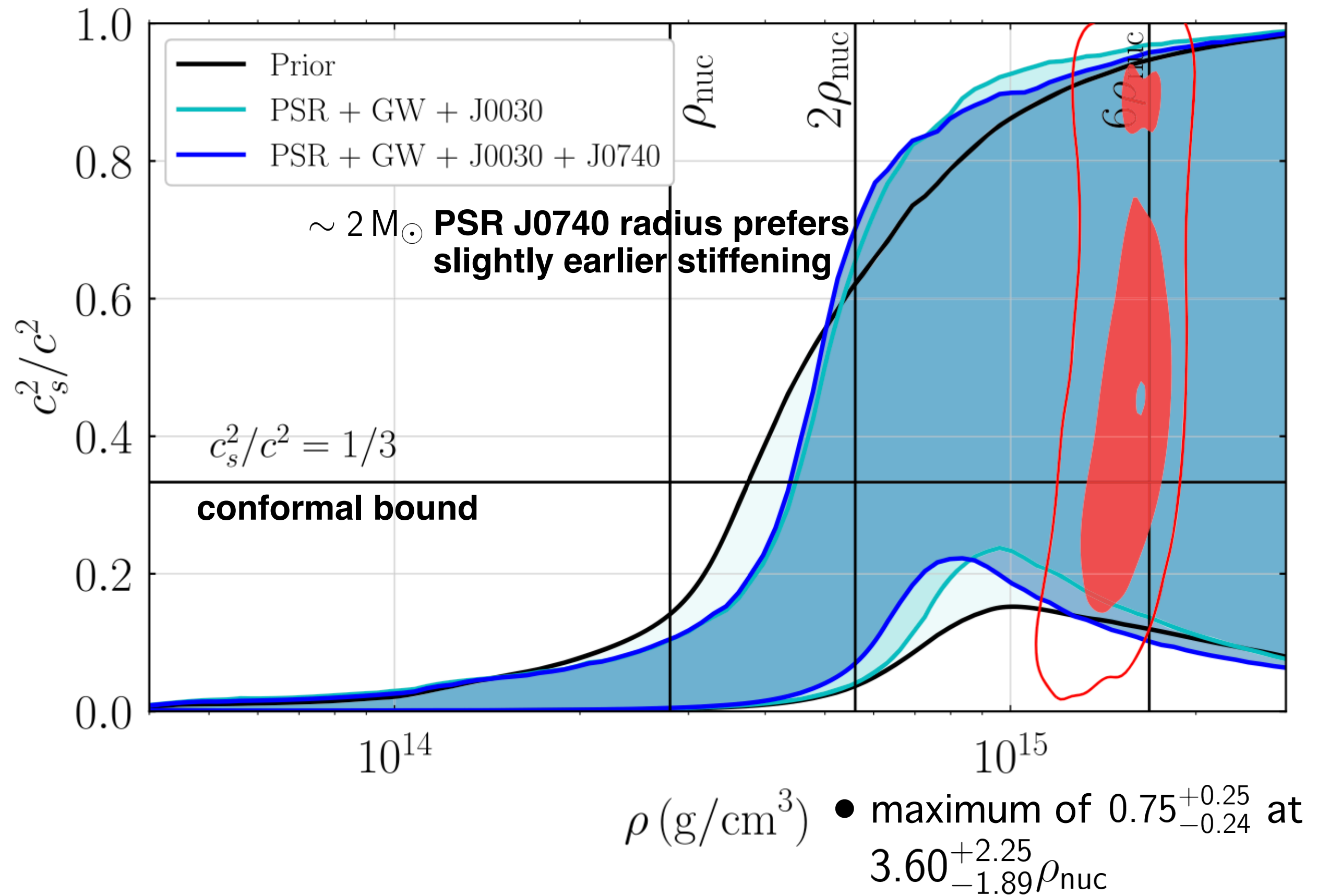
1) mostly driven by radius

- full posterior is dominated by EoSs with a single stable branch
- **onset** for the unstable branch i.e. **extra softening** pushed to two ends

Inferring the peak sound velocity



Inferring the peak sound velocity



Sound speed in dense QCD

$$c_s^2(r) \equiv dp(r)/d\varepsilon(r)$$

how fast pressure rises with energy density

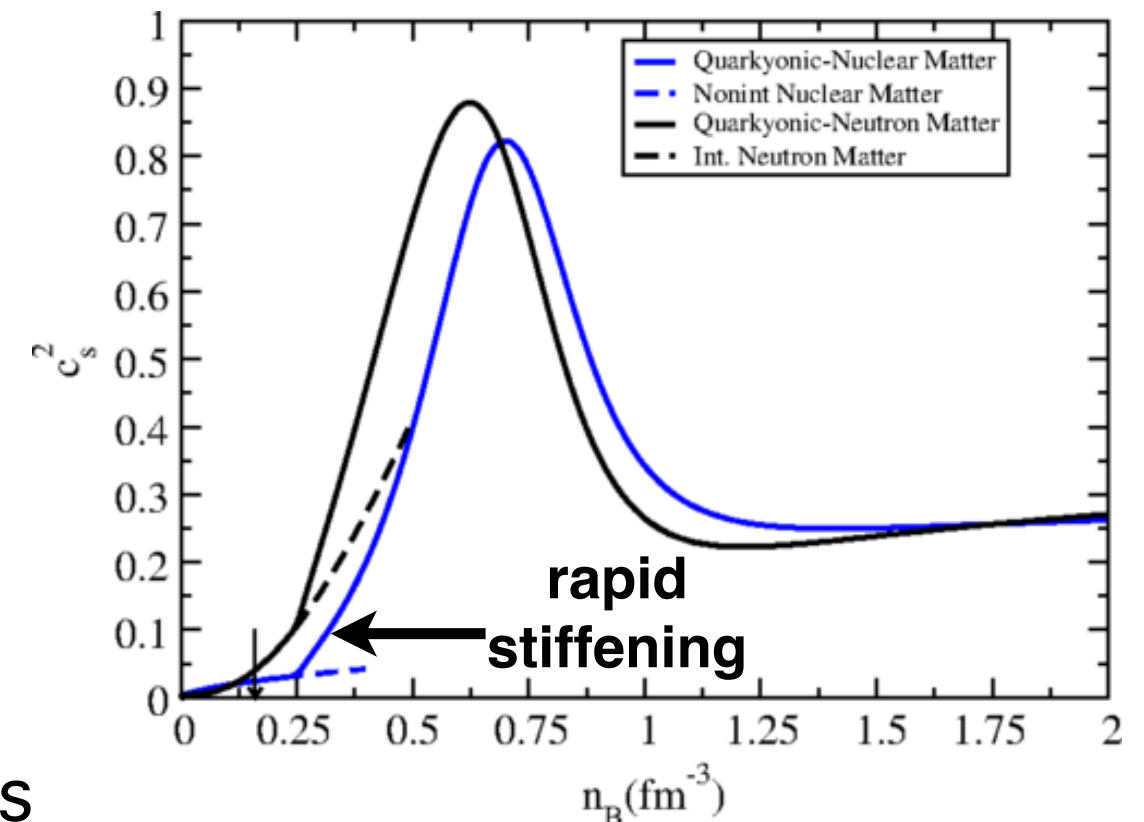
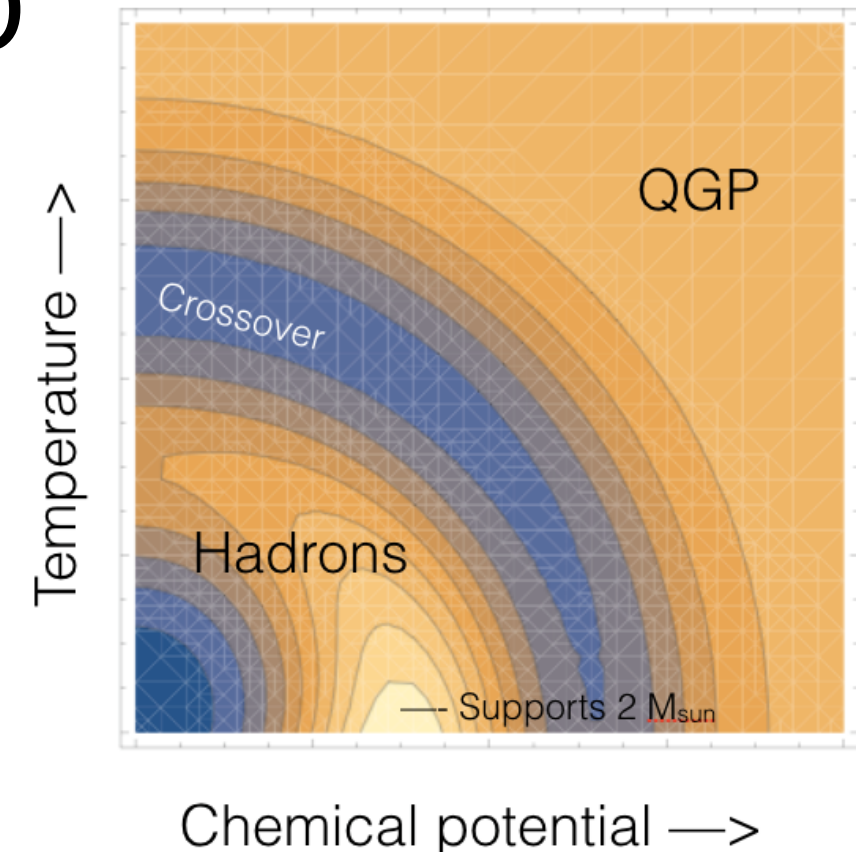
Possible behavior in neutron star interiors

- minimal scenario of normal nuclear matter: smoothly increasing function of pressure
- first-order phase transition scenario: finite energy density **discontinuity** induces sudden **softening** near the phase boundary

- crossover scenario (quarkyonic matter)

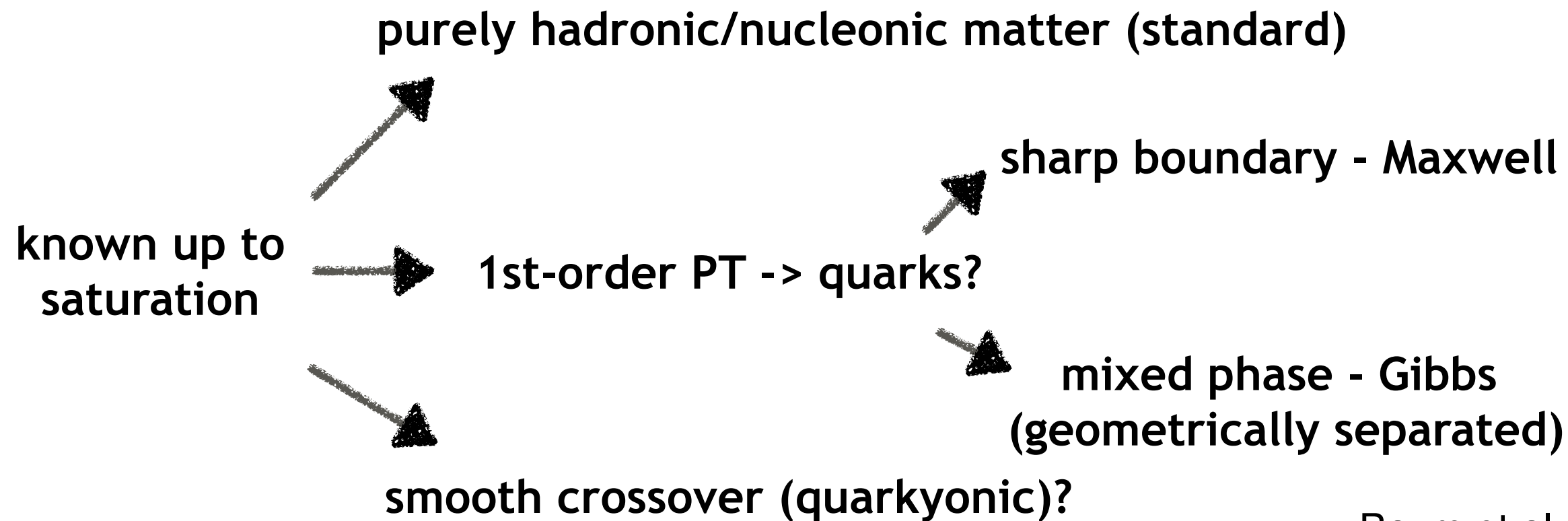
Limits see talks later this afternoon

- asymptotically high density: $\sim 1/3$
- $\sim 4-8$ times saturation: supports massive NSs
- high-T: matches lattice calc./heavy-ion data



McLerran & Reddy,
PRL 122, 122701 (2019)

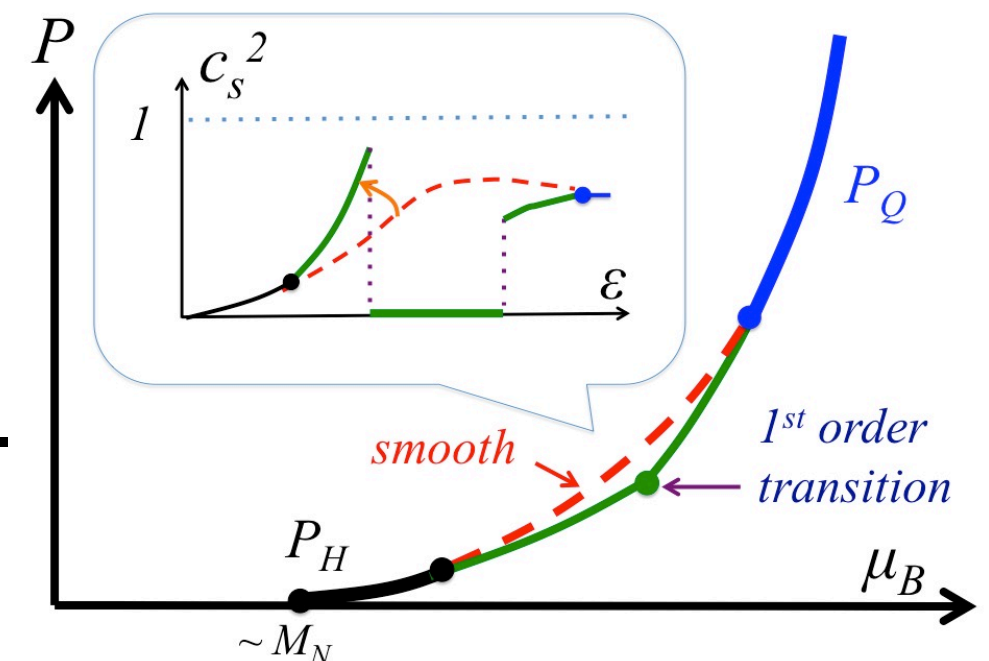
Paths towards high-density EoS



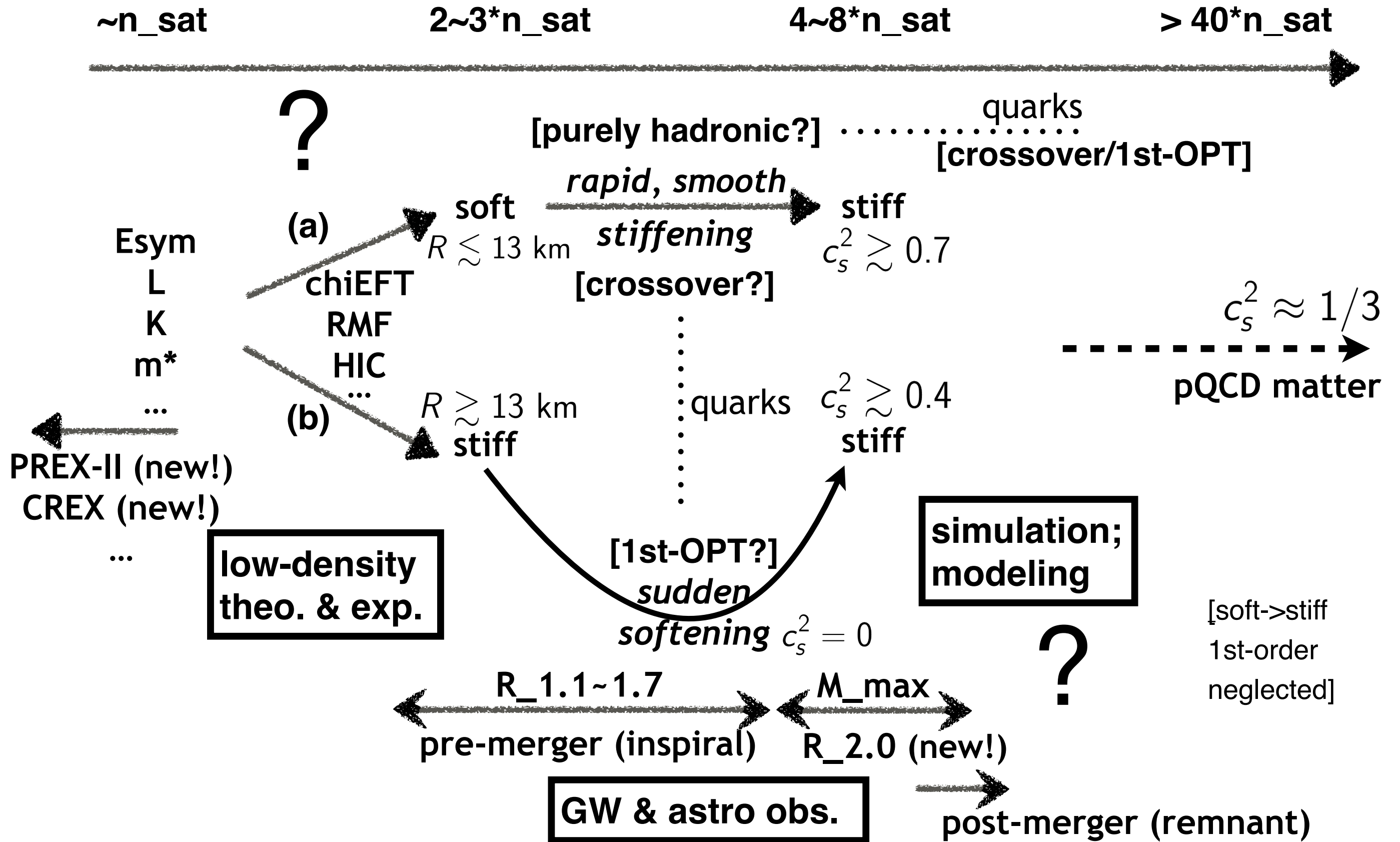
“golden window” in the vicinity of $\sim 2 \cdot n_{\text{sat}}$; hints from exp.?

- **masquerade** problem: EoSs with or without PTs may hardly be distinguishable via observations that constrain M - R only
- crossover models motivated by e.g. lattice calc.
- 1st-OPT: mixed phase (Gibbs) favored if the hadron/quark surface tension is small

Baym et al. Rept. Prog. Phys. 81, 056902 (2018)



Summary: Crossroads

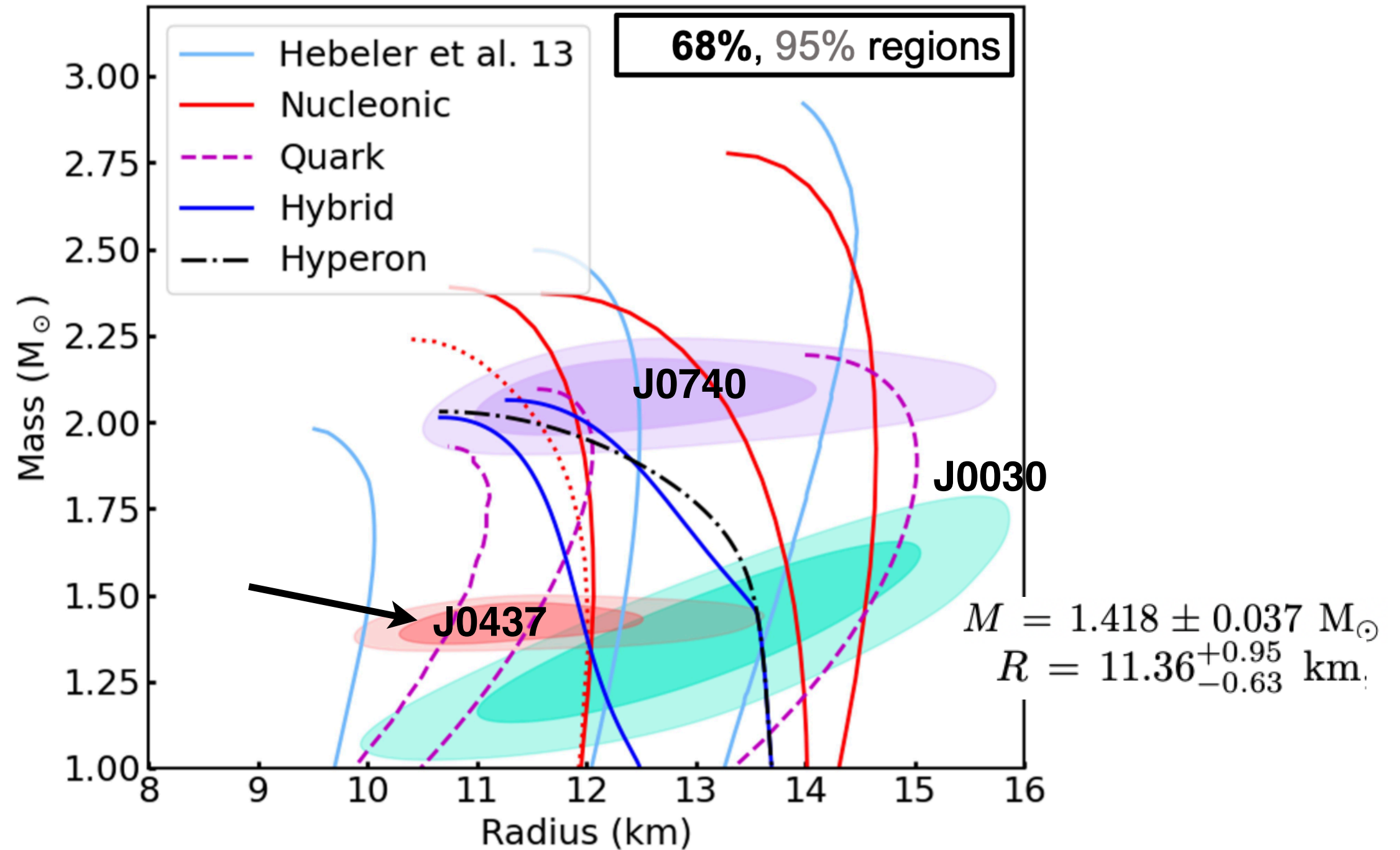


A NICER VIEW OF PSR J0437-4715 (new!)

nearest and brightest
millisecond pulsar

arXiv:2407.06789

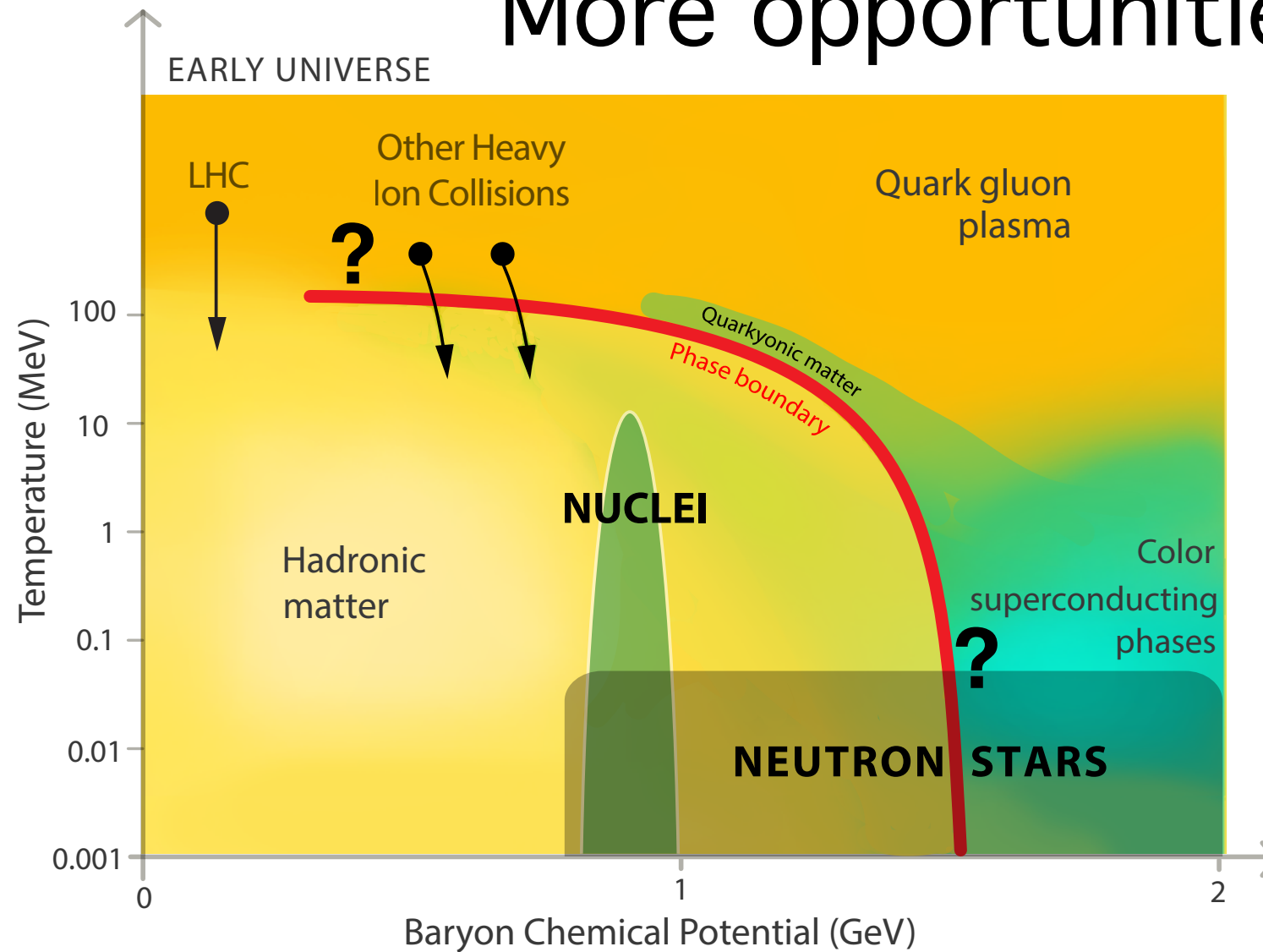
arXiv:2407.06790



mass, distance, inclination all
well known from pulsar timing

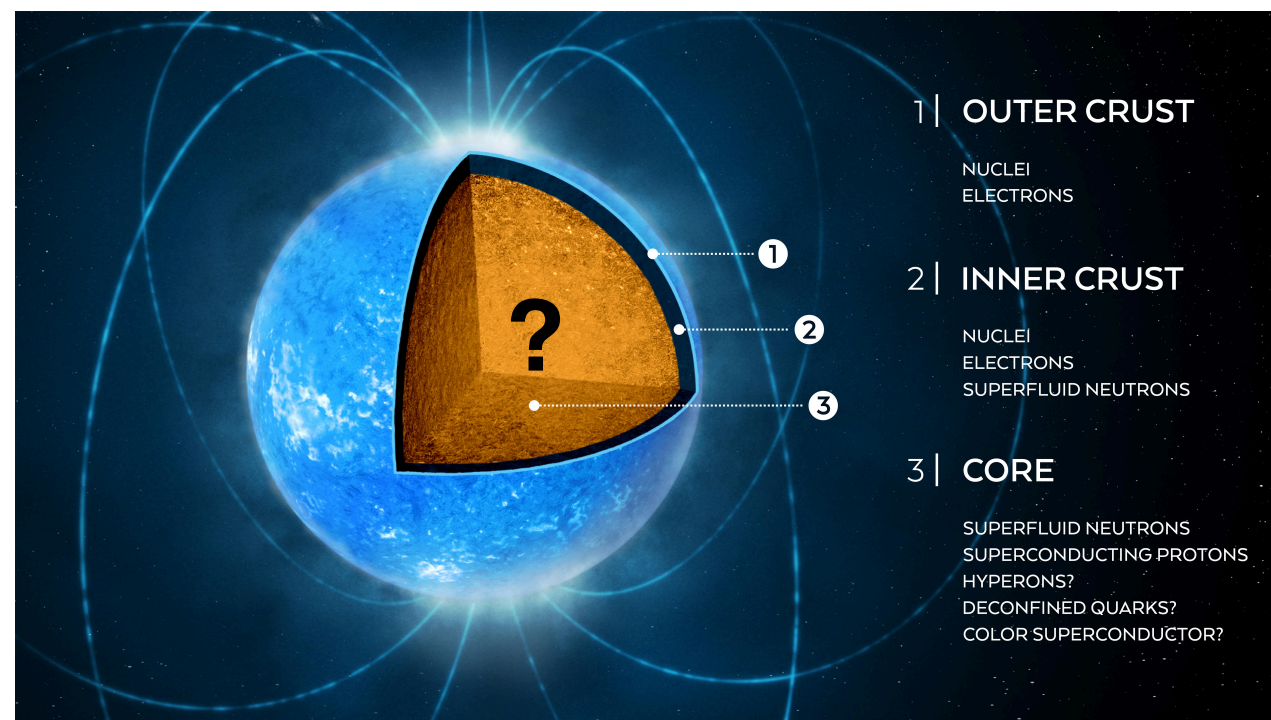
Courtesy: Anna Watts

More opportunities beyond EoS



studying dense QCD with NSs

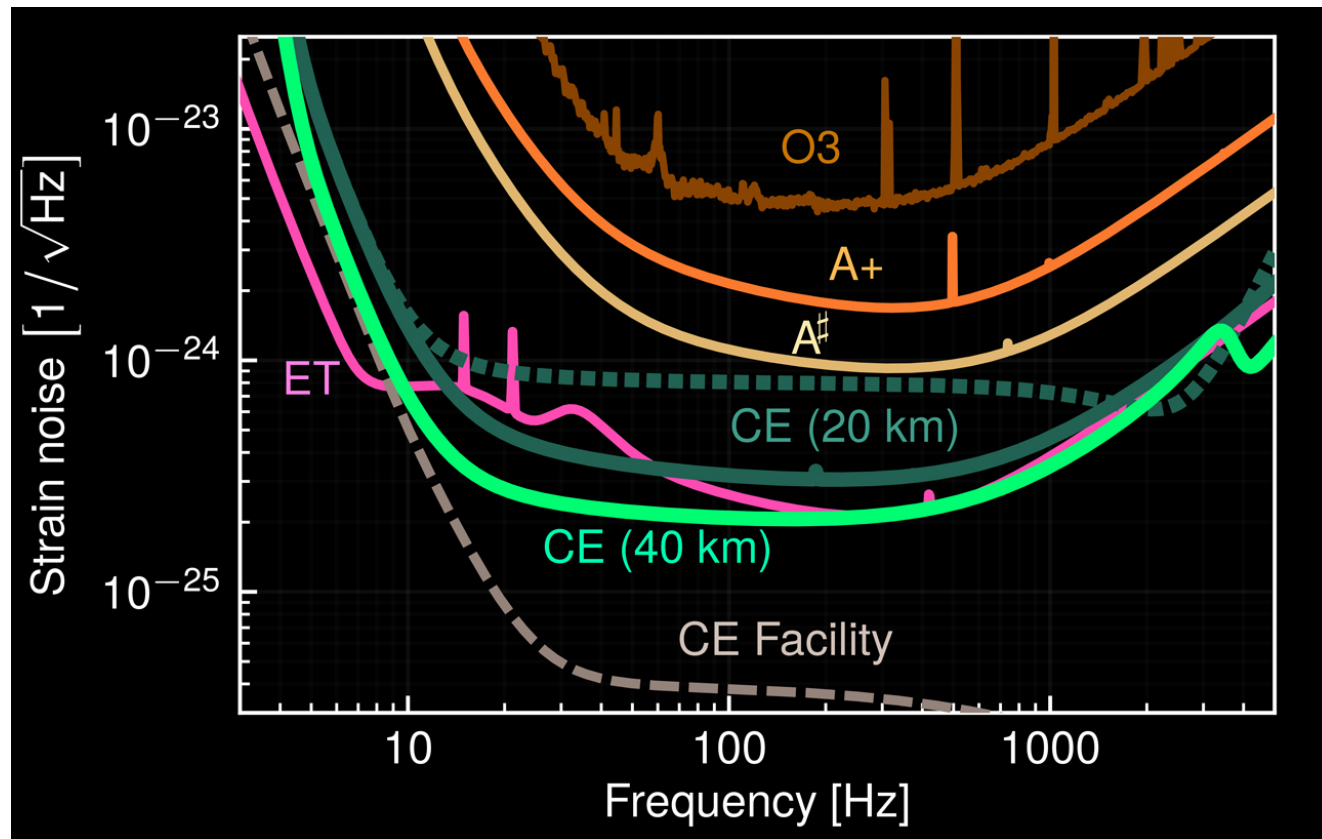
- cooling of NS 1987A? - neutrino emissivity, stellar superfluids **[nuclear theory, transport prop.]**
- merger evolution with astro/GW signals - out-of-equilibrium (visc.) physics; composition details **[simulations, nucleosynthesis]**
- next Galactic supernova? **[neutrino physics]**
- asteroseismology **[hydrodynamics, GR, nucl-th]**
- ...and more - add your own



Rev. Mod. Phys.
88, 021001 (2016)

e.g. stellar oscillations

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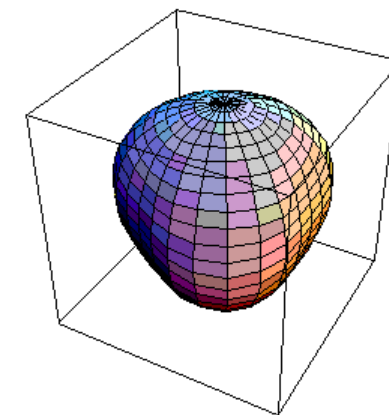
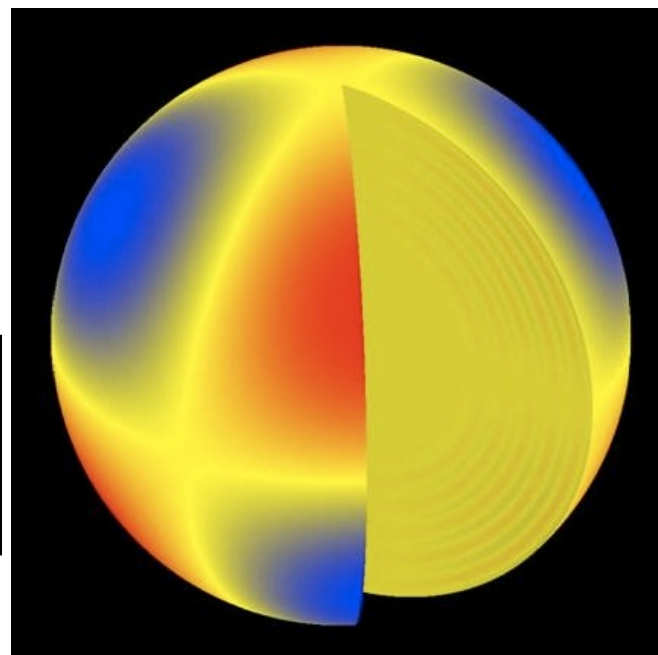


stable oscillation modes (“ringing”)
 -> **continuous** GWs

- *f*-mode (fundamental mode) scales with average density
- *p*-mode (pressure mode) probes the sound speed
- ***g*-mode (gravity mode)** sensitive to composition/thermal gradients
- *w*-mode, *s*-mode, *i*-mode/*r*-mode..

©NASA/Kepler

promising sources for XG detectors



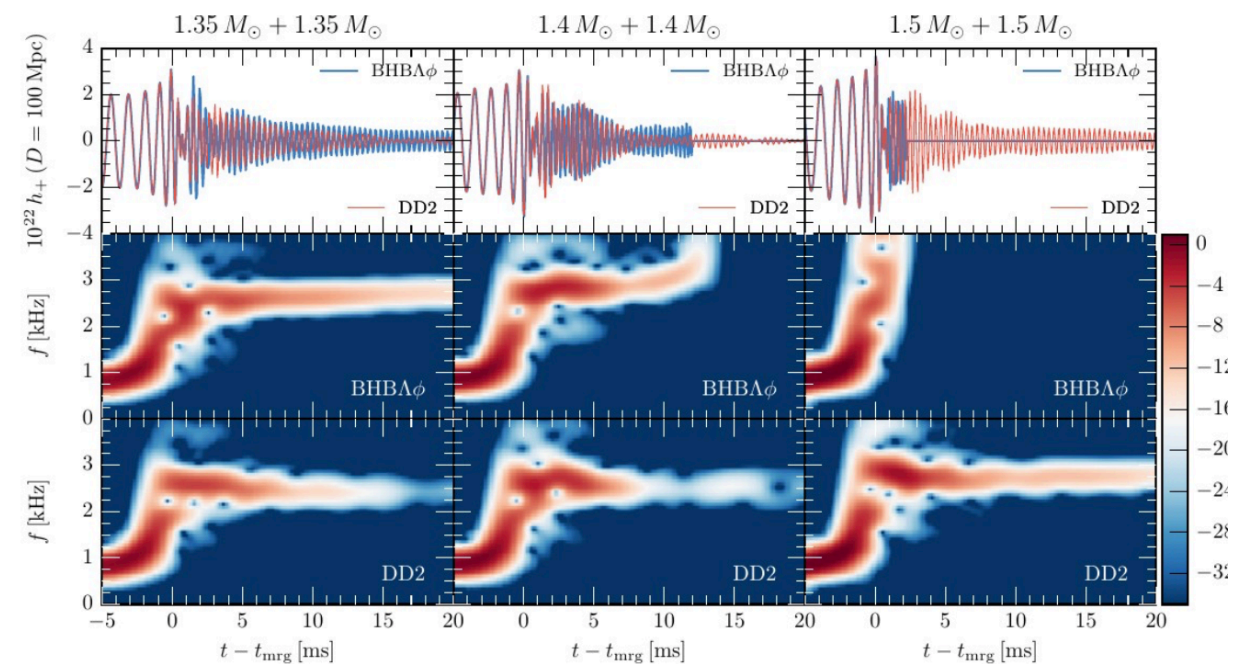
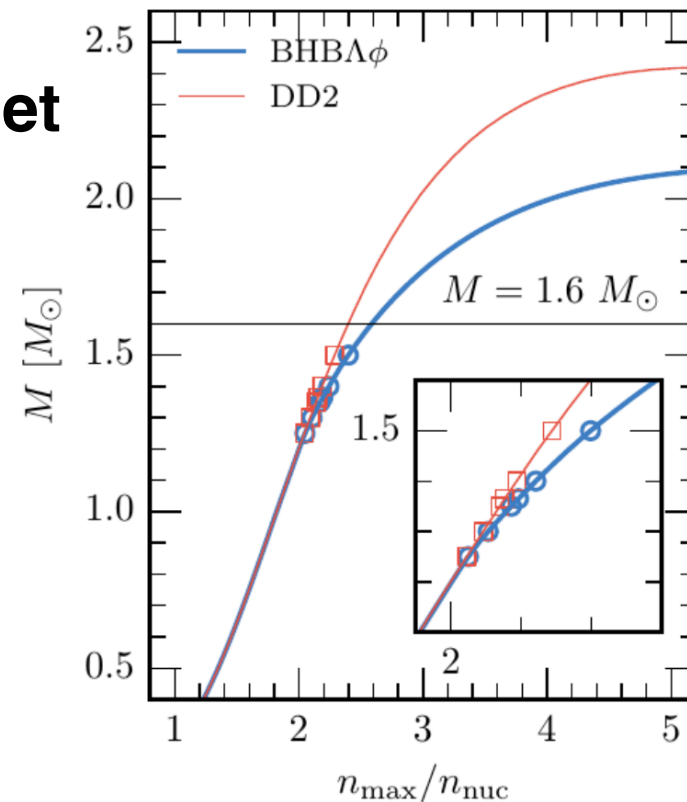
$$l = 3, m = 3$$

small amplitude oscillations ->
 weak (continuous) emission of GWs

e.g. softening effects on post-merger GWs

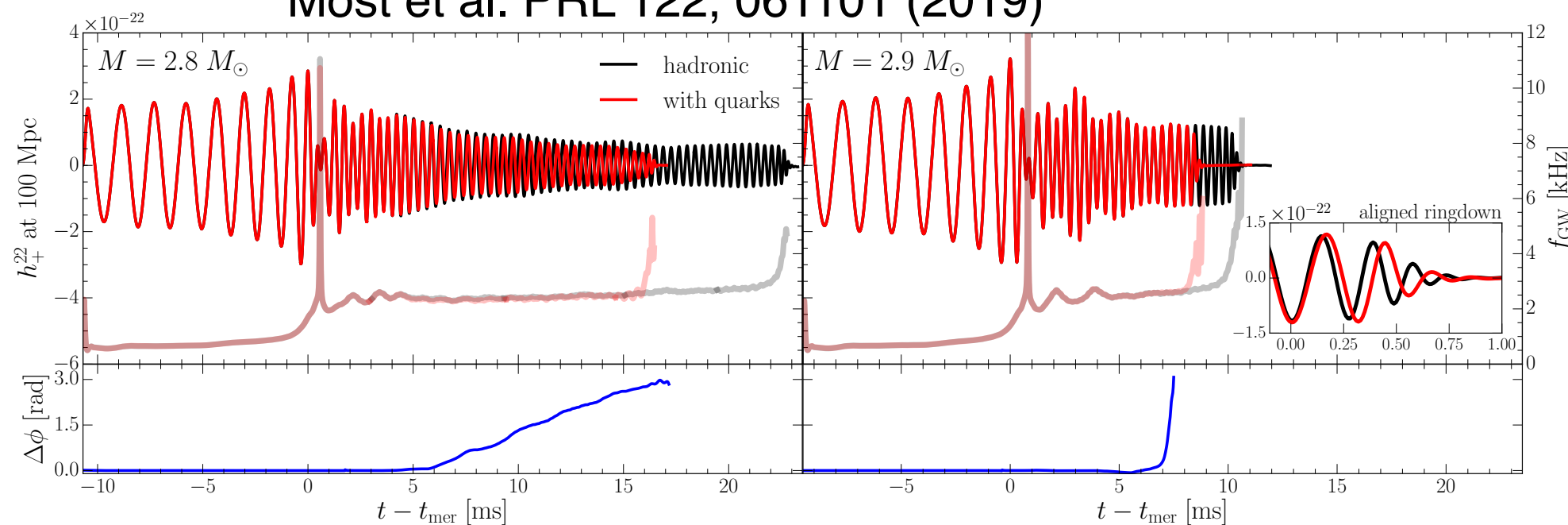
hyperon onset

- more compact remnant (higher central density)
- earlier collapse; higher frequency



Radice et al. ApJL 842, L10 (2017)

Most et al. PRL 122, 061101 (2019)

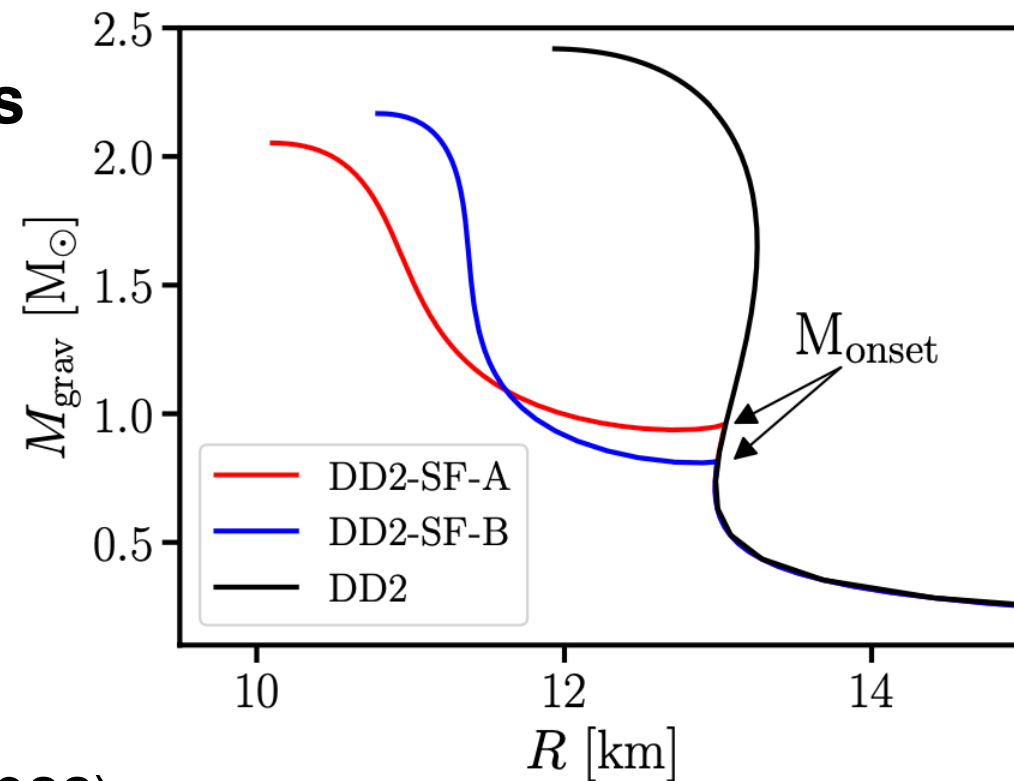


1st-OPT to soft quark matter after merger

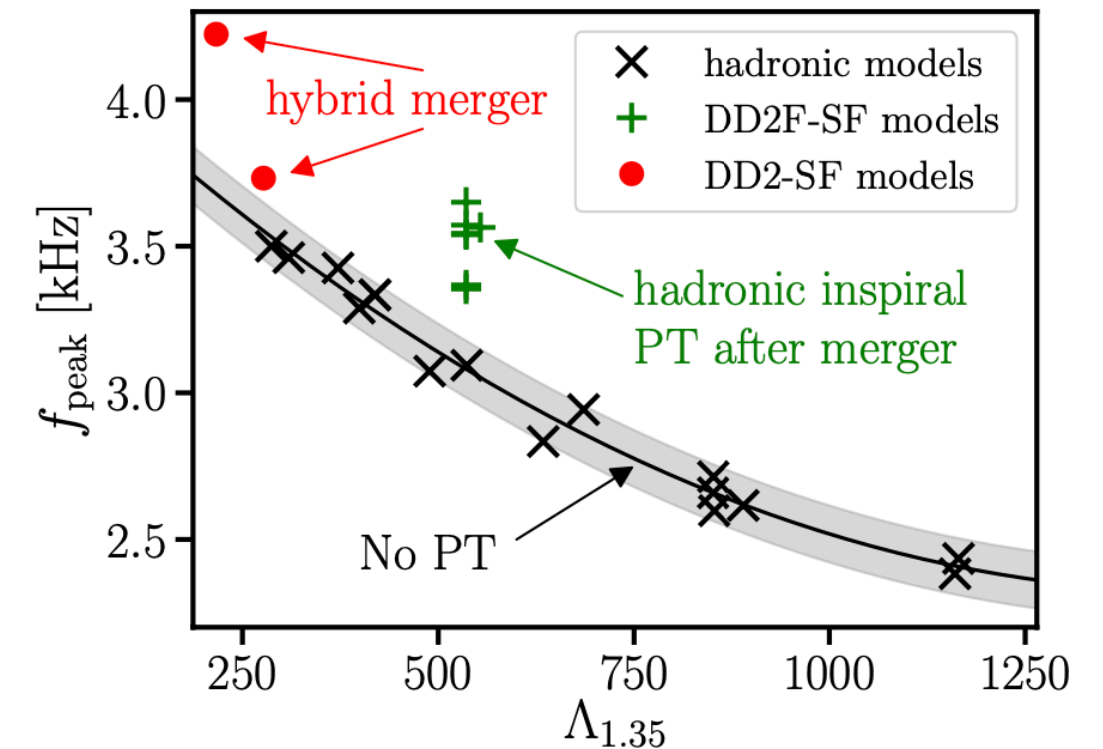
e.g. softening effects on post-merger GWs

third-family stars

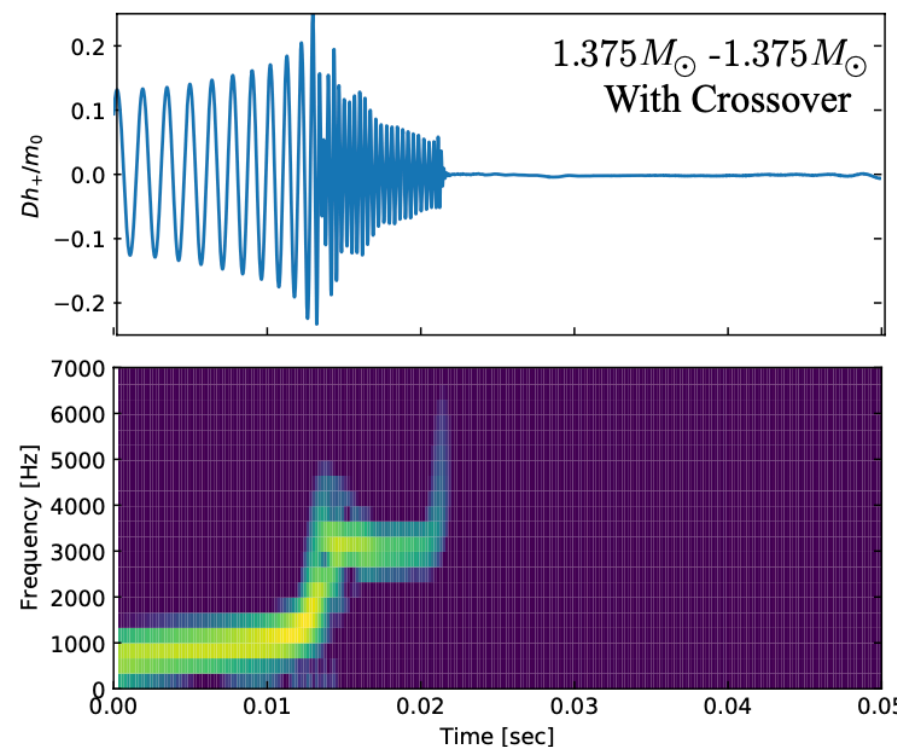
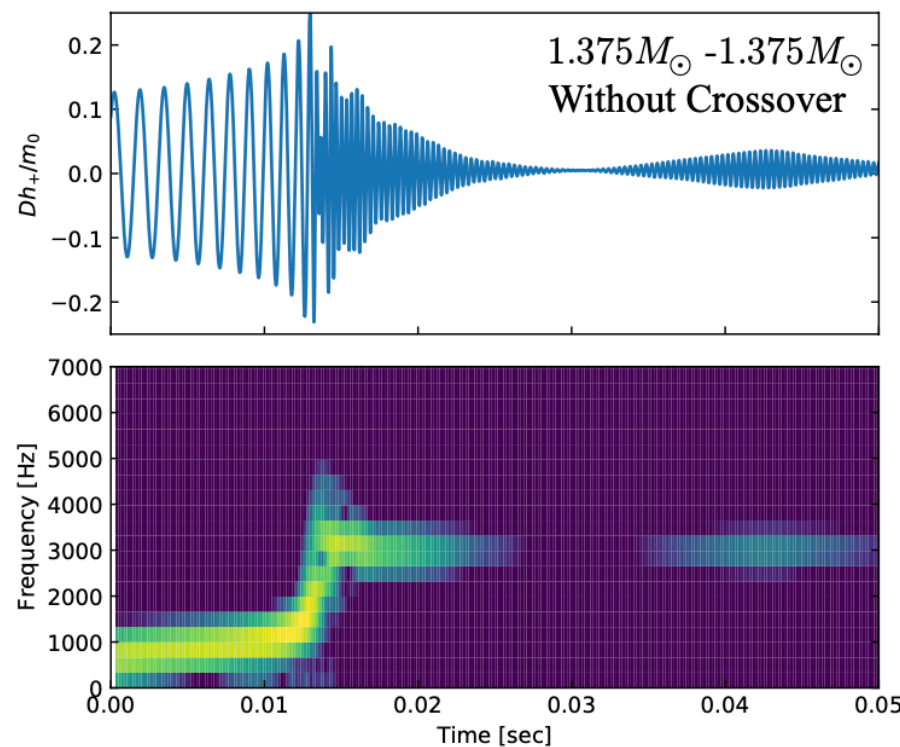
- ***stiff*** EoS at low density -DD2
- strong **1st-OPT** to ***stiff*** quark matter before merger



Fujimoto et al. (2022)



Bauswein & Blacker (2020)



- ***soft*** EoS at low density \sim N3LO chiEFT

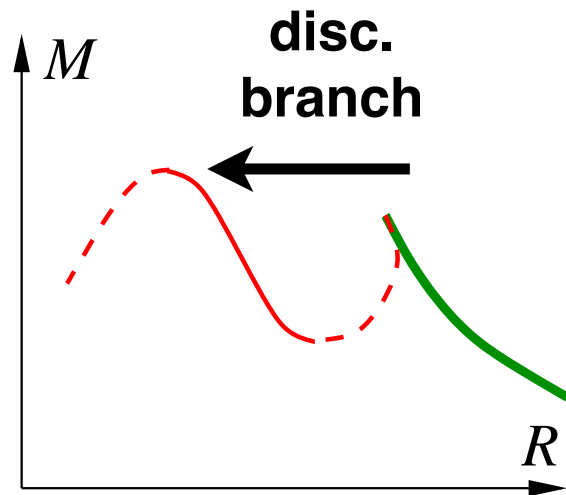
- rapid ***stiffening*** within the crossover regime

crossover into *soft* quark matter after merger

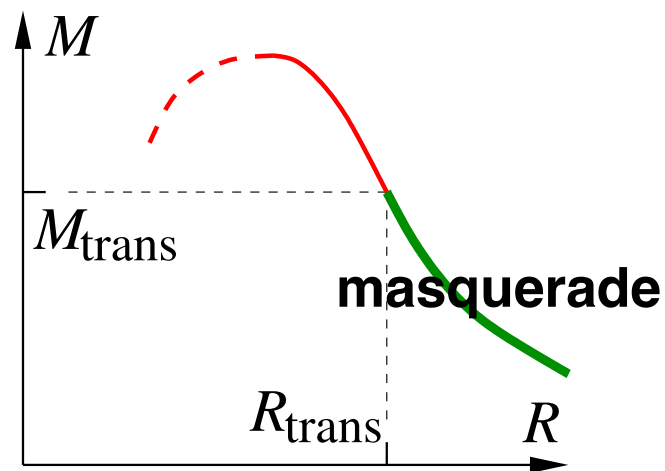
e.g. a population of BNS events

Chatziioannou & SH, arXiv:1911.07091

SH & Steiner, arXiv:1810.10967

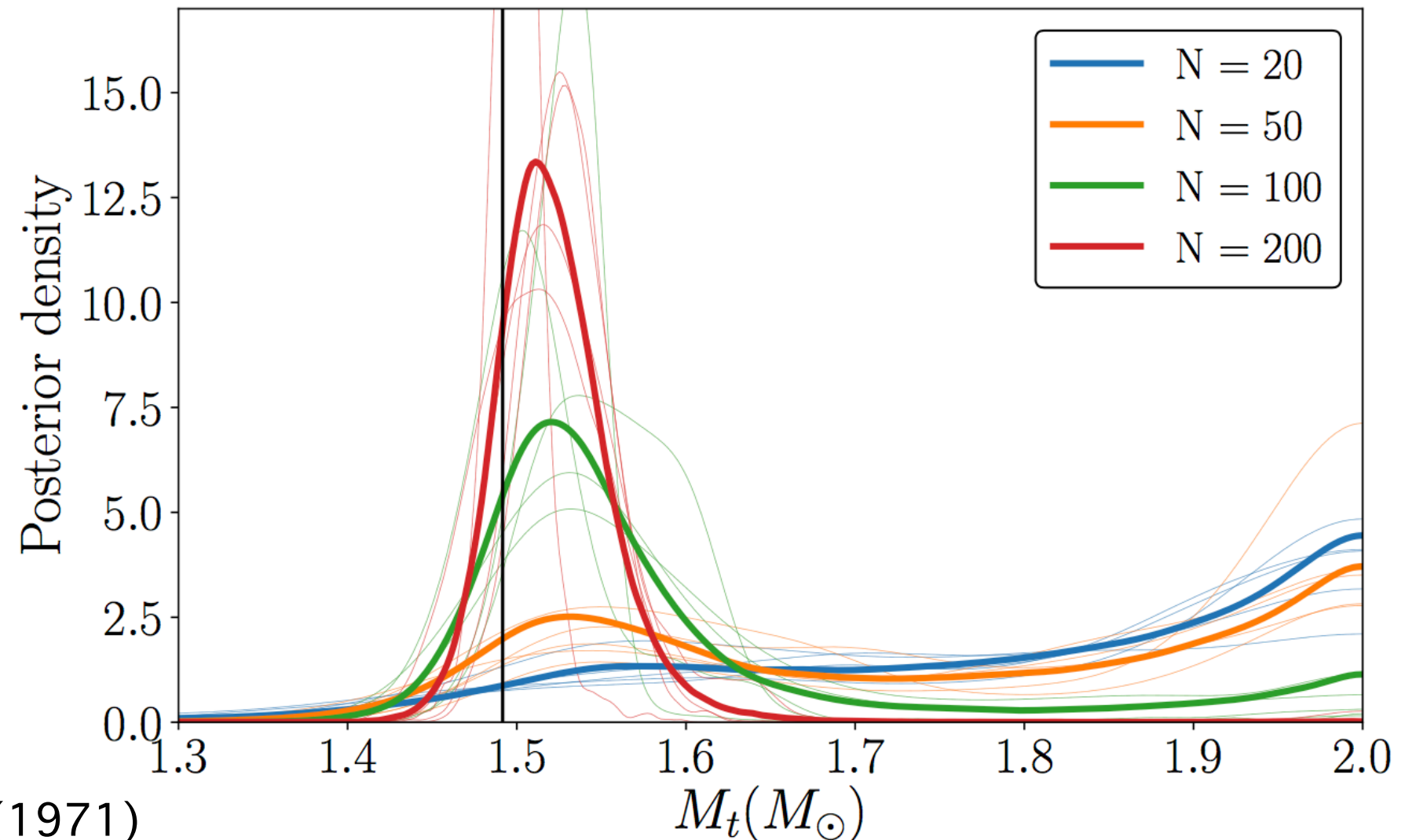


Alford, SH & Prakash
PRD 88, 083013 (2013)



critical strength to trigger an instability

$$\frac{\Delta \epsilon_{\text{crit}}}{\epsilon_{\text{trans}}} = \frac{1}{2} + \frac{3}{2} \frac{p_{\text{trans}}}{\epsilon_{\text{trans}}} \quad \text{Seidov (1971)}$$



- may help identify third-family stars [strong 1st-OPT] with **inspiral** GWs
- requires multiple (**$N \sim 50-100$**) future detections to separate different families: NS-NS, NS-HS, HS-HS mergers

Looking forward

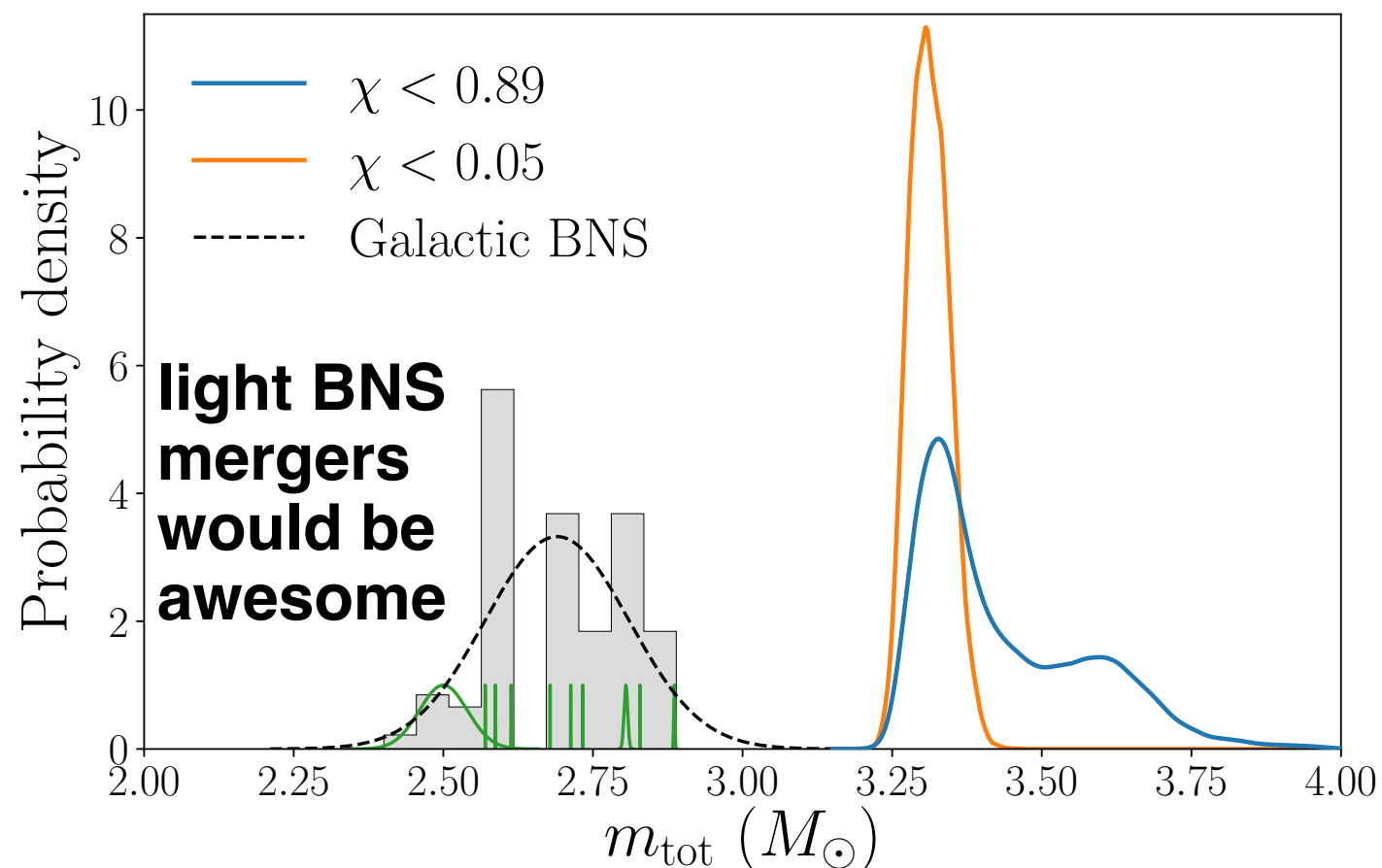
LVC collaboration
arXiv:2006.12611

GW190425

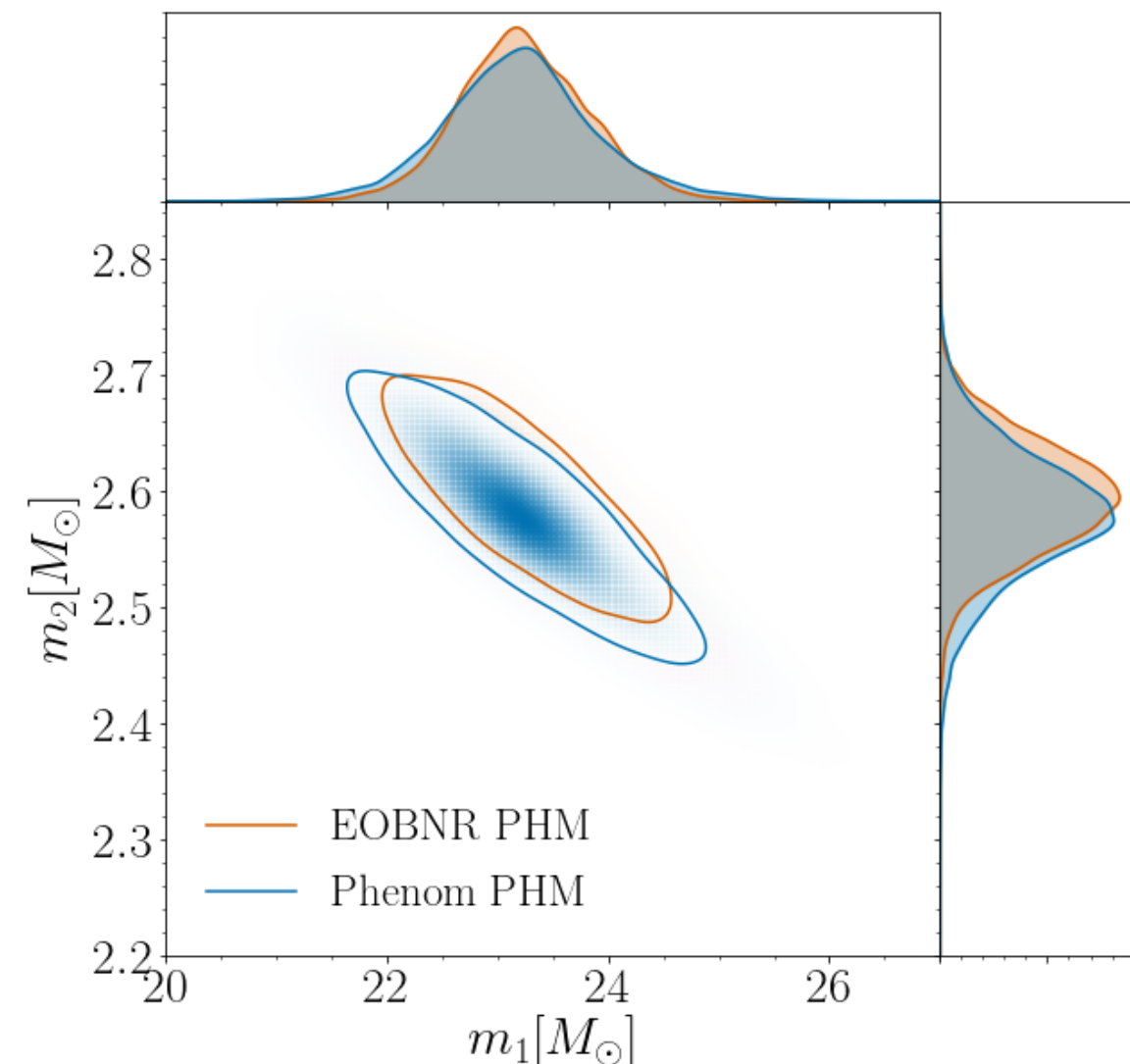
hunting for surprises..

- total mass ~ 3.4 solar masses
- signal too weak to provide further EoS constraints $R < 16$ km

LVC collaboration
arXiv:2001.01761



see events of GWTC-2: arXiv:2010.14527



GW190814

more mass-gap objects?

- component of ambiguous nature
- most **asymmetric** system observed

NSBH mergers

LVK collaboration
arXiv:2106.15163

THE ASTROPHYSICAL JOURNAL LETTERS, 915:L5 (24pp), 2021 July 1

<https://doi.org/10.3847/2041-8213/ac082e>

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Observation of Gravitational Waves from Two Neutron Star–Black Hole Coalescences

Table 2
Source Properties of GW200105 and GW200115

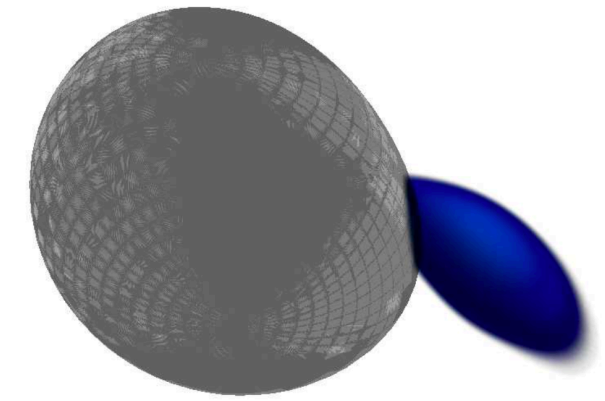
	GW200105		GW200115	
	Low Spin ($\chi_2 < 0.05$)	High Spin ($\chi_2 < 0.99$)	Low Spin ($\chi_2 < 0.05$)	High Spin ($\chi_2 < 0.99$)
Primary mass m_1/M_\odot	$8.9^{+1.1}_{-1.3}$	$8.9^{+1.2}_{-1.5}$	$5.9^{+1.4}_{-2.1}$	$5.7^{+1.8}_{-2.1}$
Secondary mass m_2/M_\odot	$1.9^{+0.2}_{-0.2}$	$1.9^{+0.3}_{-0.2}$	$1.4^{+0.6}_{-0.2}$	$1.5^{+0.7}_{-0.3}$
Mass ratio q	$0.21^{+0.06}_{-0.04}$	$0.22^{+0.08}_{-0.04}$	$0.24^{+0.31}_{-0.08}$	$0.26^{+0.35}_{-0.10}$
Total mass M/M_\odot	$10.8^{+0.9}_{-1.0}$	$10.9^{+1.1}_{-1.2}$	$7.3^{+1.2}_{-1.5}$	$7.1^{+1.5}_{-1.4}$
Chirp mass \mathcal{M}/M_\odot	$3.41^{+0.08}_{-0.07}$	$3.41^{+0.08}_{-0.07}$	$2.42^{+0.05}_{-0.07}$	$2.42^{+0.05}_{-0.07}$
Detector-frame chirp mass $(1+z)\mathcal{M}/M_\odot$	$3.619^{+0.006}_{-0.006}$	$3.619^{+0.007}_{-0.008}$	$2.580^{+0.006}_{-0.007}$	$2.579^{+0.007}_{-0.007}$
Primary spin magnitude χ_1	$0.09^{+0.18}_{-0.08}$	$0.08^{+0.22}_{-0.08}$	$0.31^{+0.52}_{-0.29}$	$0.33^{+0.48}_{-0.29}$
Effective inspiral spin parameter χ_{eff}	$-0.01^{+0.08}_{-0.12}$	$-0.01^{+0.11}_{-0.15}$	$-0.14^{+0.17}_{-0.34}$	$-0.19^{+0.23}_{-0.35}$
Effective precession spin parameter χ_p	$0.07^{+0.15}_{-0.06}$	$0.09^{+0.14}_{-0.07}$	$0.19^{+0.28}_{-0.17}$	$0.21^{+0.30}_{-0.17}$
Luminosity distance D_L/Mpc	280^{+110}_{-110}	280^{+110}_{-110}	310^{+150}_{-110}	300^{+150}_{-100}
Source redshift z	$0.06^{+0.02}_{-0.02}$	$0.06^{+0.02}_{-0.02}$	$0.07^{+0.03}_{-0.02}$	$0.07^{+0.03}_{-0.02}$

no information on matter effects
no significant EM detections

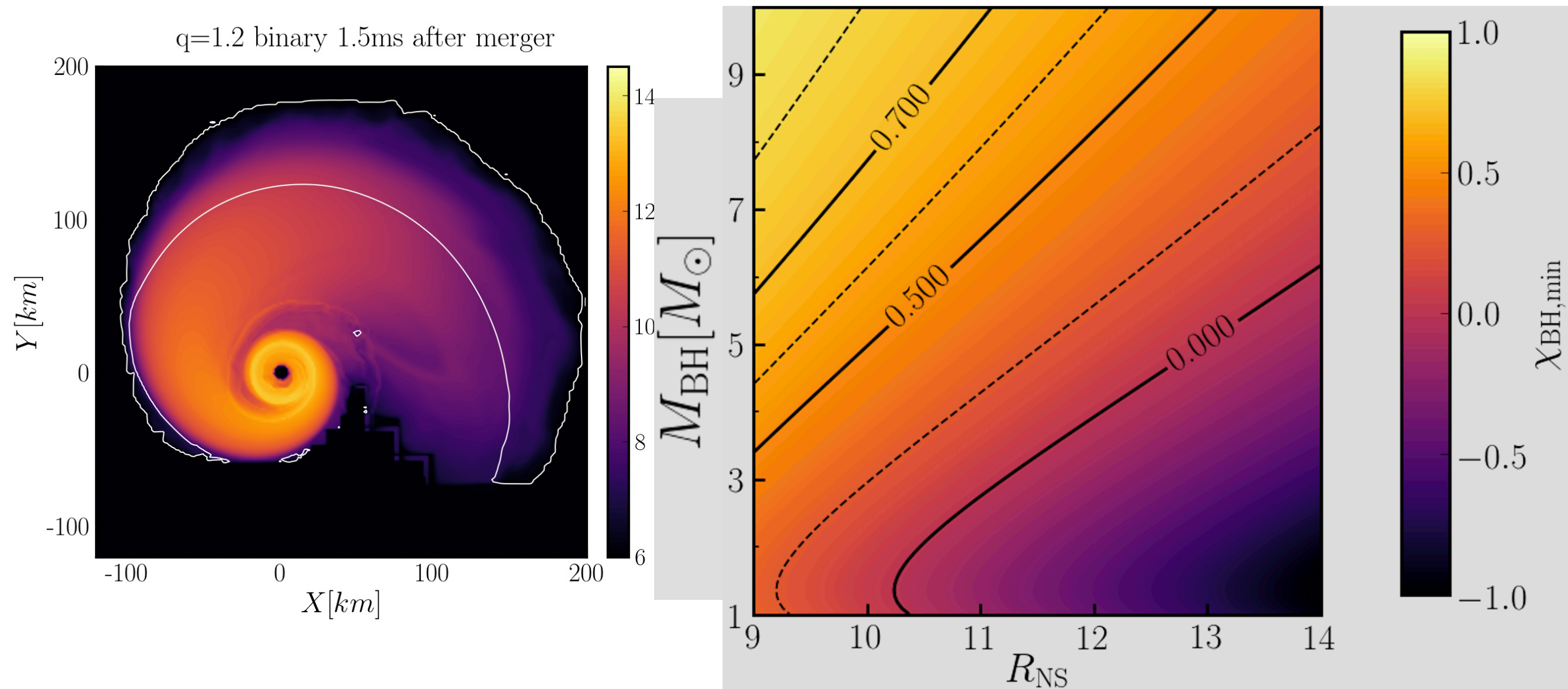
- GW200105: $\sim 1.9 + \sim 9$ solar masses
- GW200115: $\sim 1.5 + \sim 6$ solar masses

see events of GWTC-3: arXiv:2111.03606

Outcome of a NSBH merger



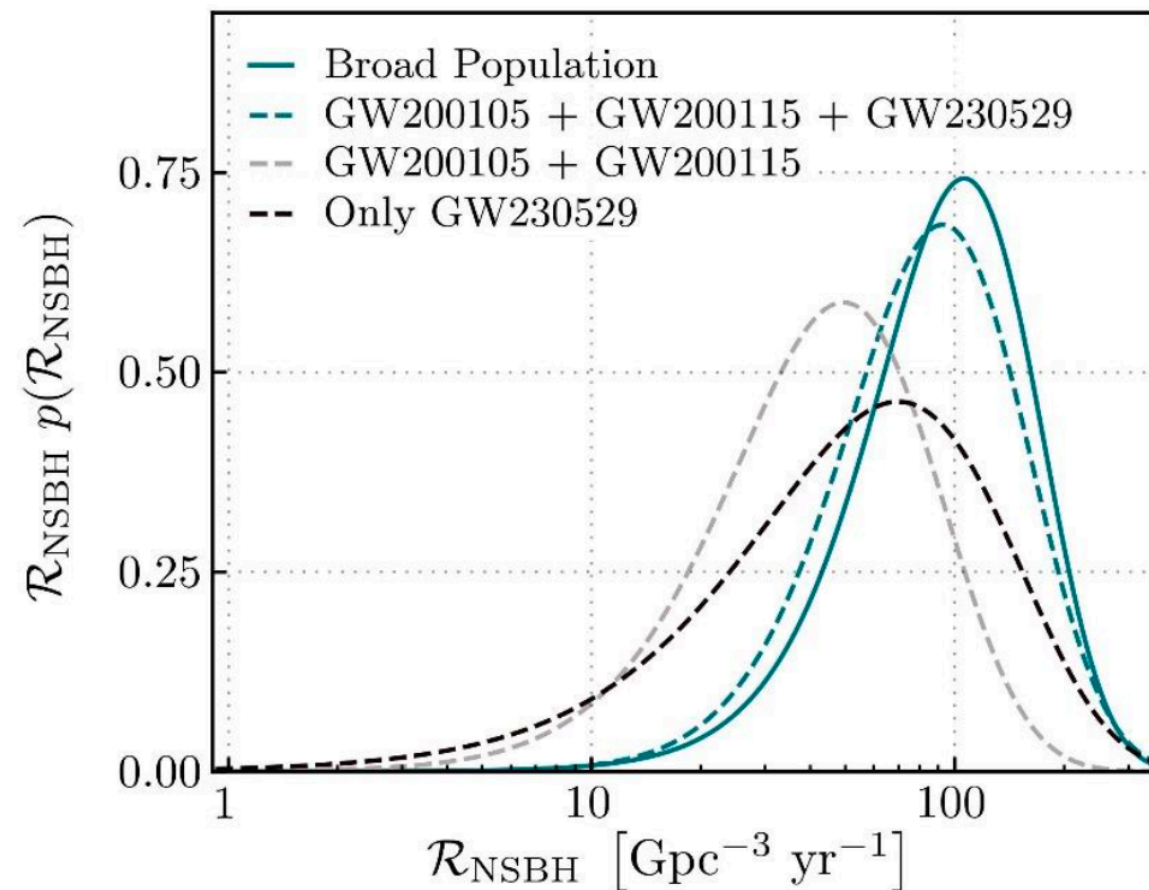
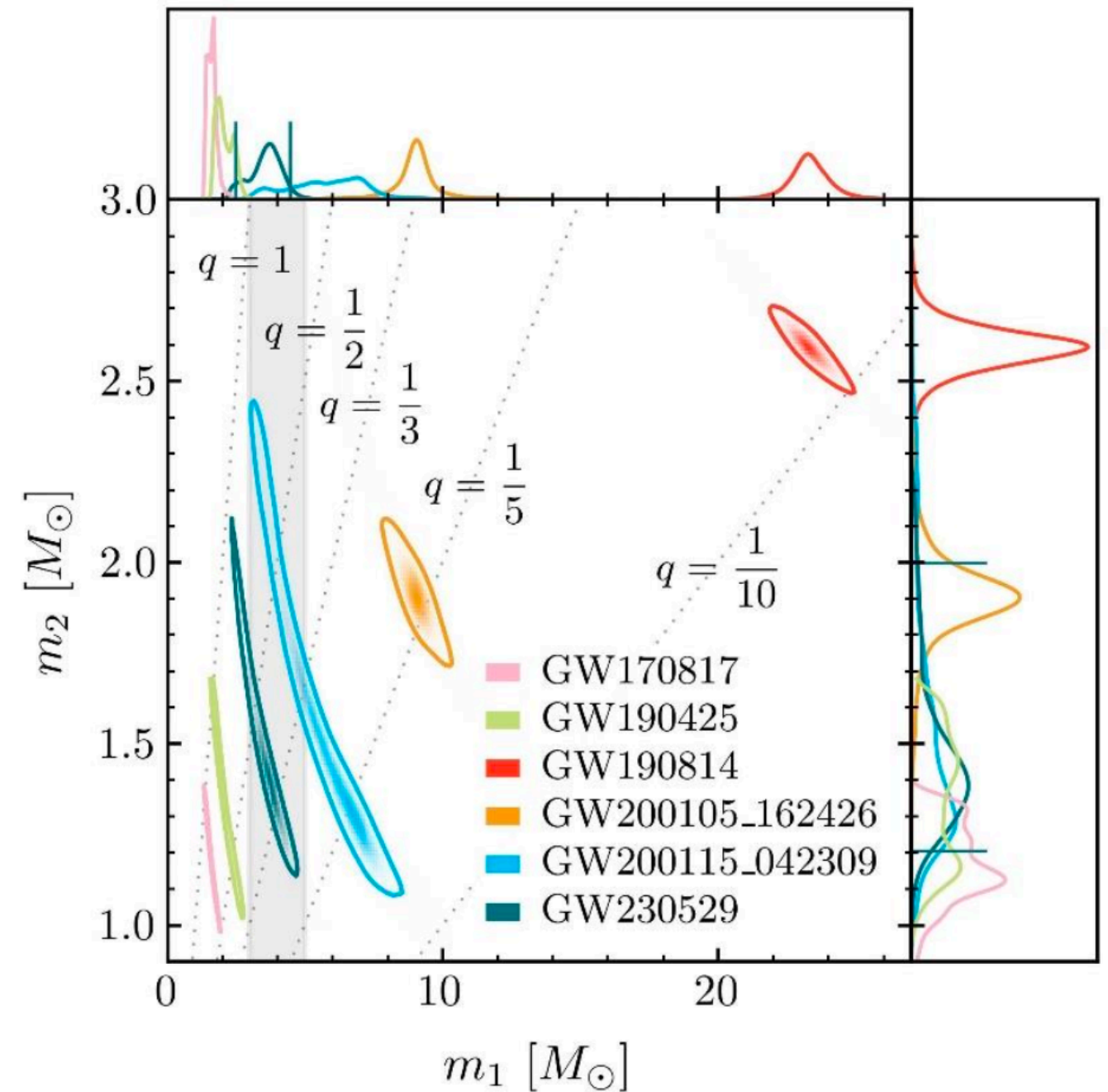
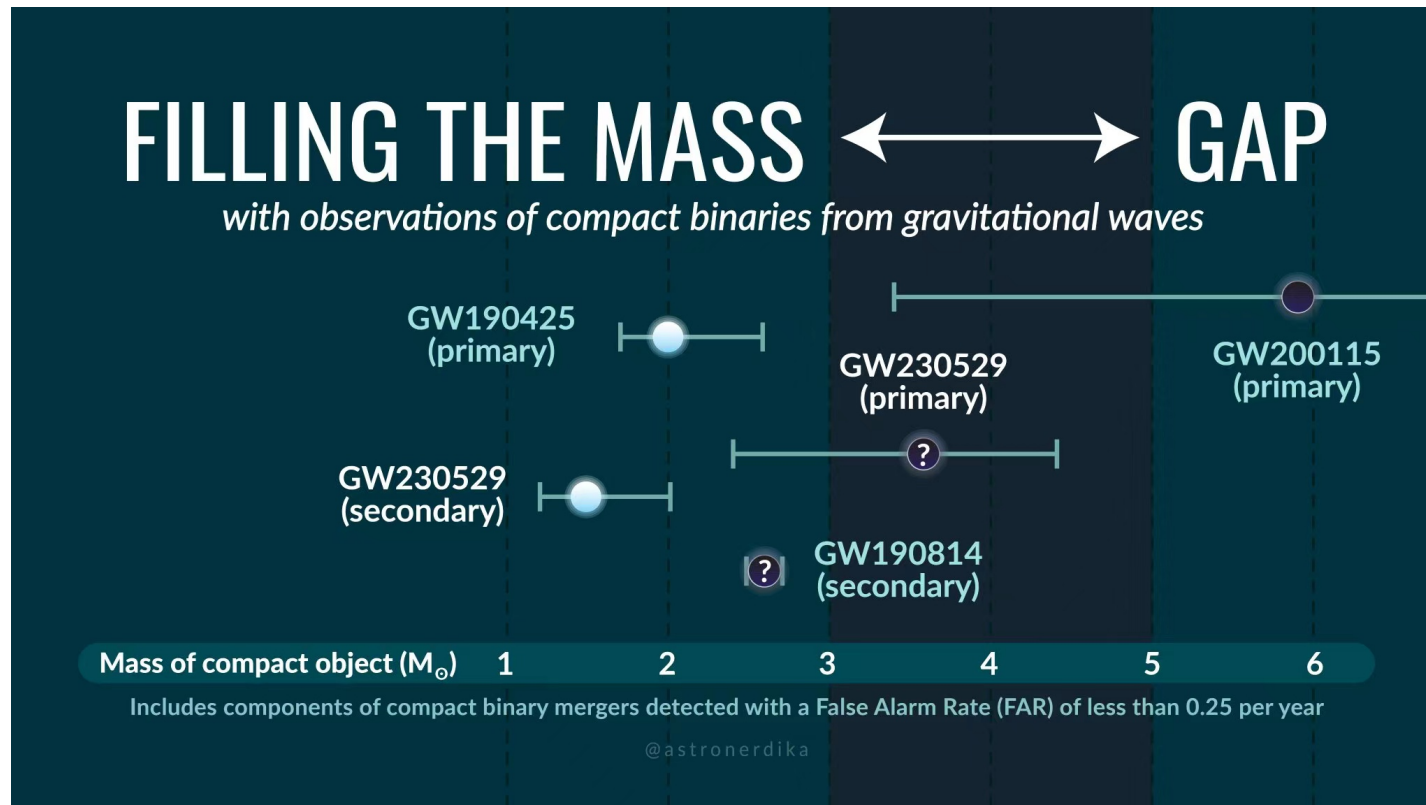
Foucart et al. (2018)



- NS is either tidally disrupted or plunges into the BH - mass ratio, spin, EoS
- radius determines if tides are **measurable** & if **EM** signals can be produced

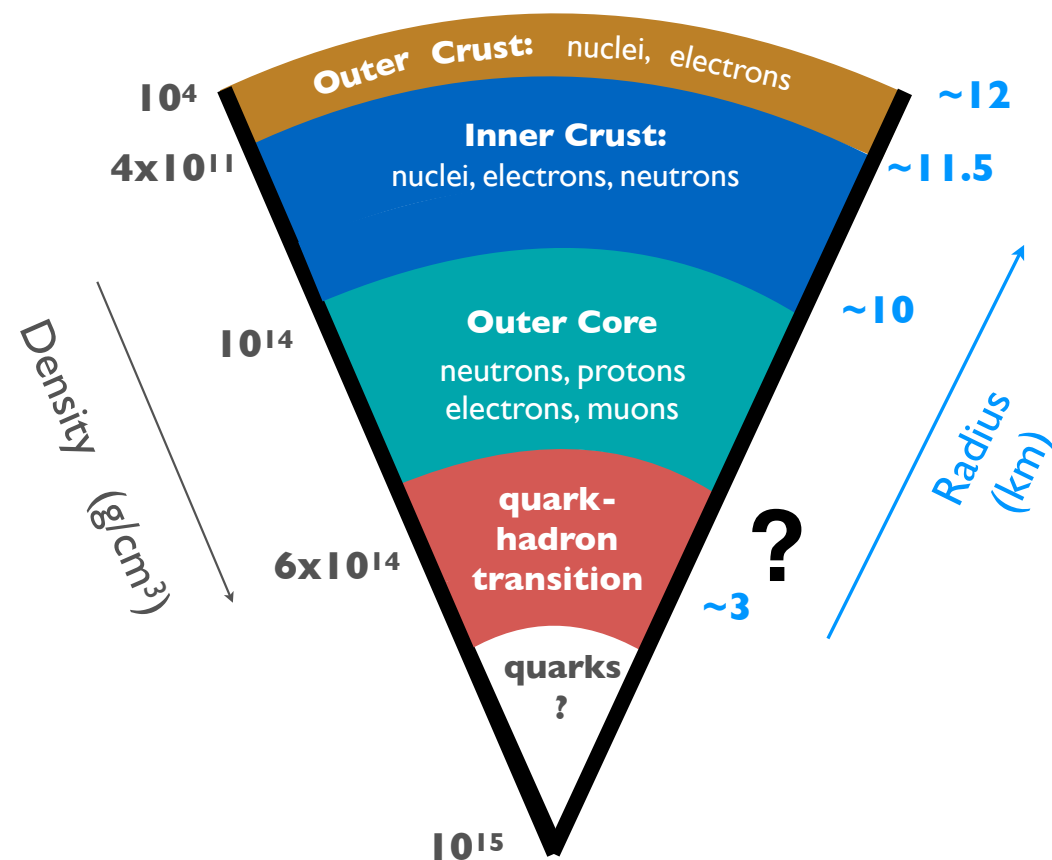
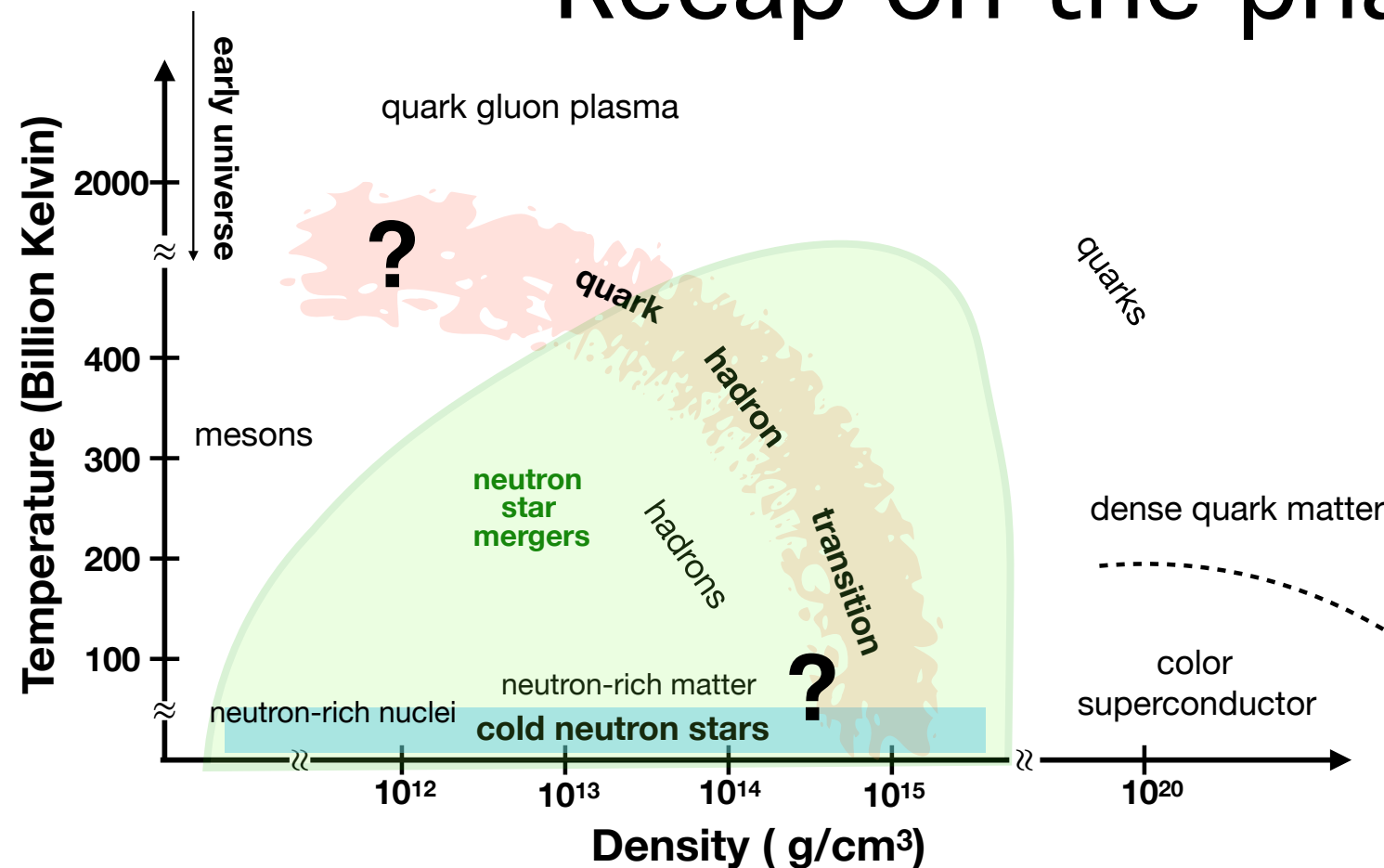
GW230529 (new!)

LVK collaboration
arXiv:2404.04248



- ~ 1.4 (NS) + ~ 3.6 (BH) solar masses
- most **symmetric** NSBH event so far

Recap on the phase diagram



3G Science white paper

puzzle of QM in NSs

- has a phase transition already taken place in canonical-mass (cold) NSs before they merge in the binary system?
- are quarks only able to appear temporarily in the (warm) massive, transient remnant of mergers or supernovae?
- when and how do they emerge - **the onset density, temperature, nature of PT?**
- imprints in observations? possible links to e.g. HICs?

THANK YOU!

Q & A

BACKUP

SLIDES

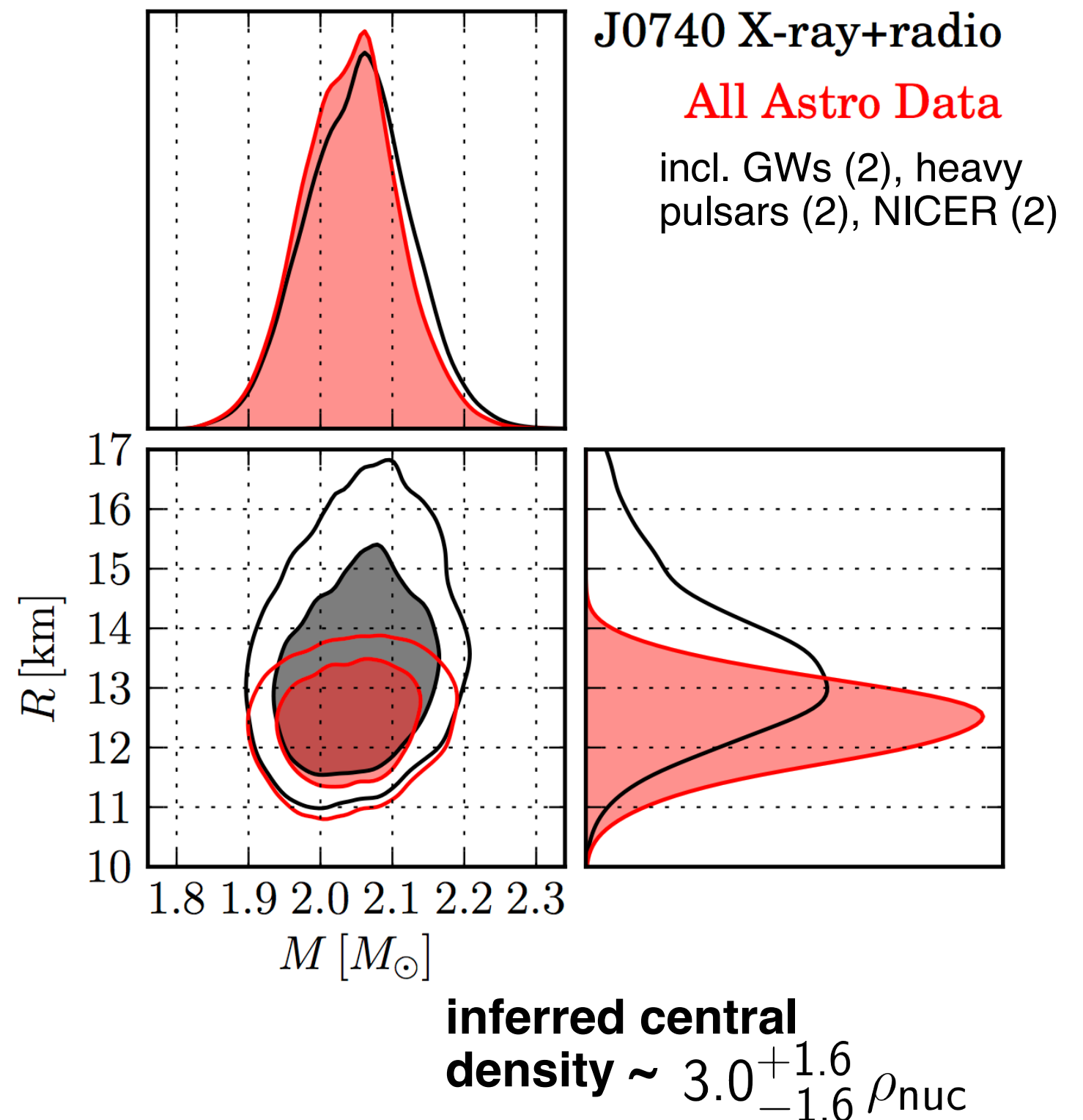
Impact of J0740 radius constraint

Bayesian analyses

- hierarchical inference scheme and the **nonparametric** priors (not assuming a specific functional form but correlations within a function - GP processes)

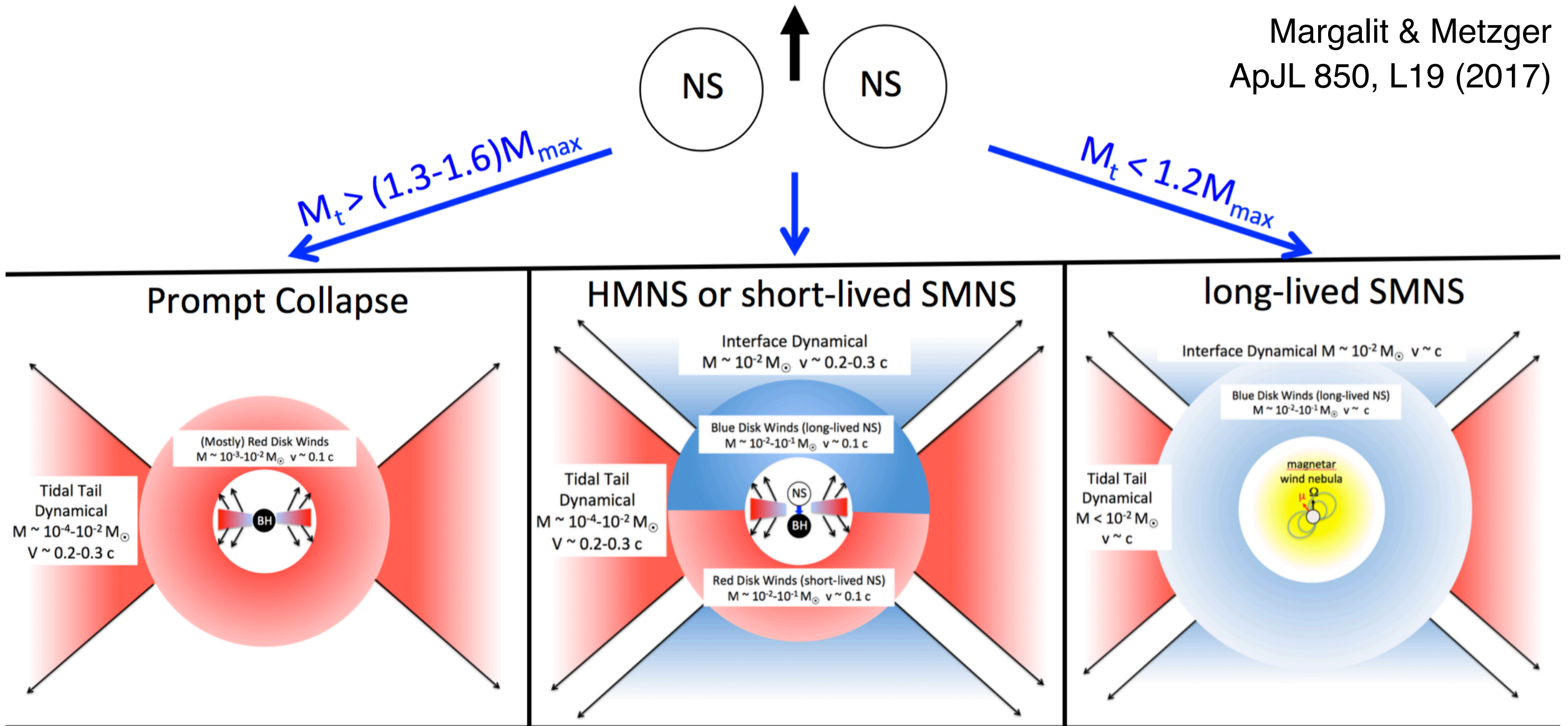
Landry et al., arXiv:2003.04880

- **NICER** data + XMM-Newton: Riley+Watts (Amsterdam) and Miller+ (Maryland/Illinois),
- $12.4^{+1.3}_{-1.0}$ km vs. $13.7^{+2.6}_{-1.5}$ km
- **other** astrophysical observations overall reduce the inferred radius of J0740+6620 from ~ 13.34 km to ~ 12.47 km at 90% credibility



Remnant dynamics

Margalit & Metzger
ApJL 850, L19 (2017)

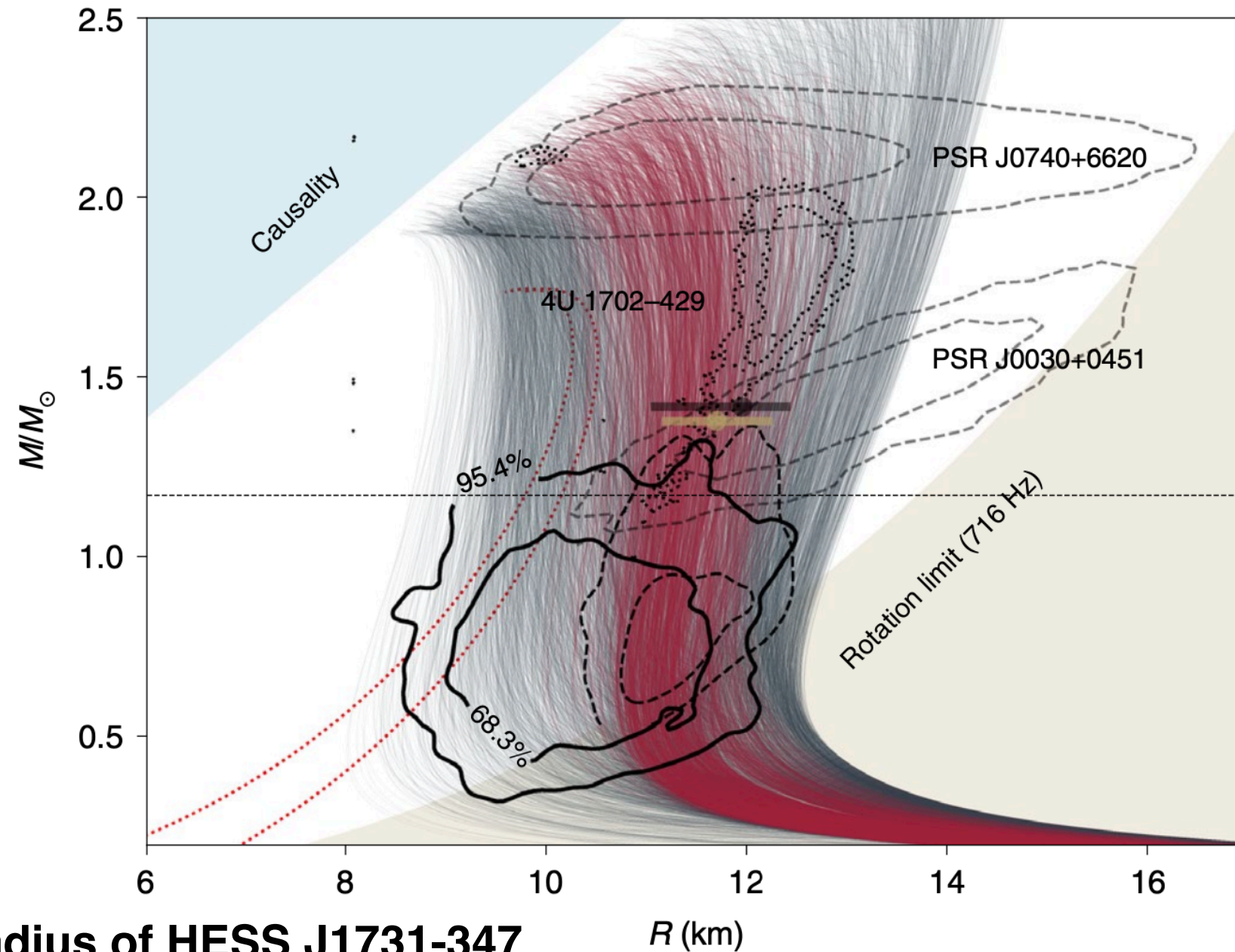


- **GW + EM** constraints from 170817 seem to favor $M_{max} < 2.16 \sim 2.3$ solar masses Ruiz et al. (2018), Rezzolla et al. (2018), Shibata et al. (2019)
- **NS radius > 10.68 km** to prevent prompt collapse Bauswein et al. (2017)

other x-ray probes of NS radii

Article

potential outlier candidate?



Doroshenko et al.
Nature Astronomy 6,
1444 (2022)

new! mass & radius of HESS J1731-347

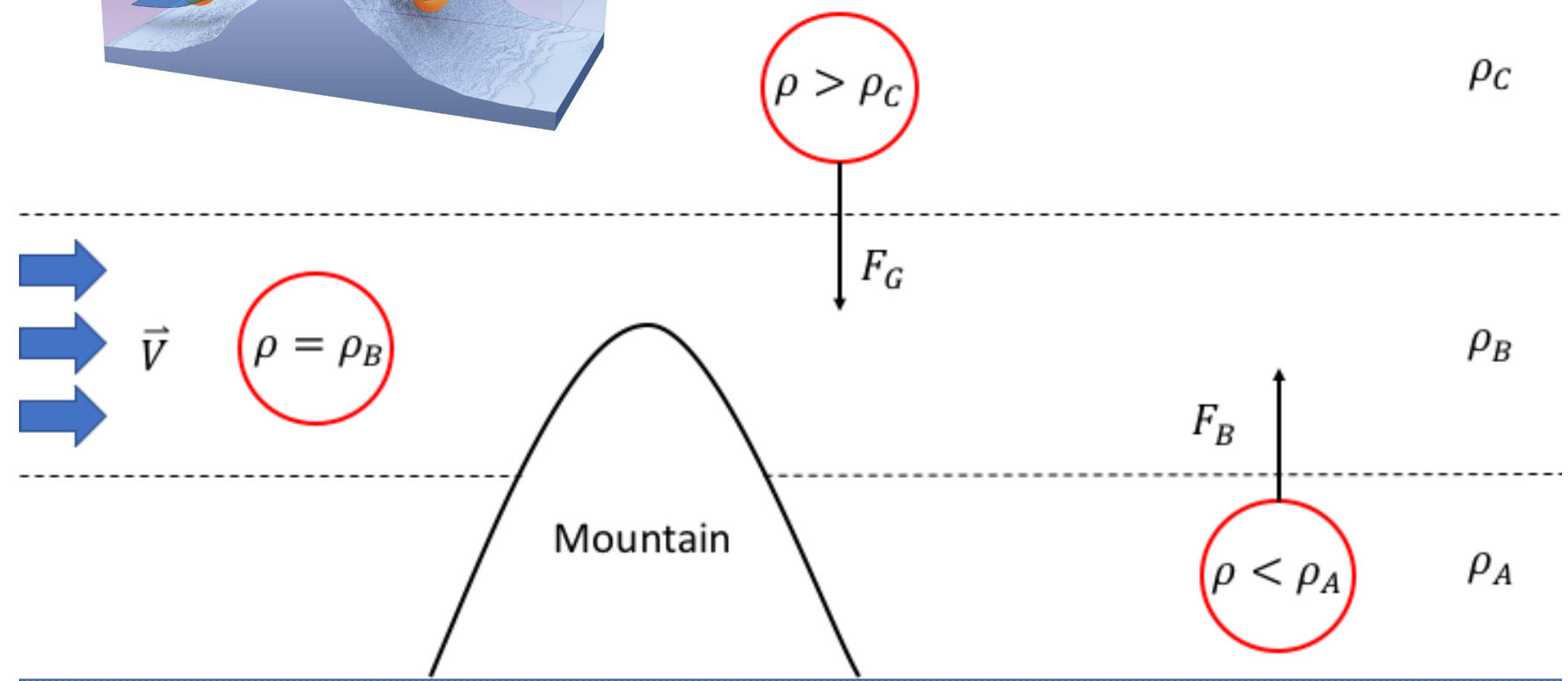
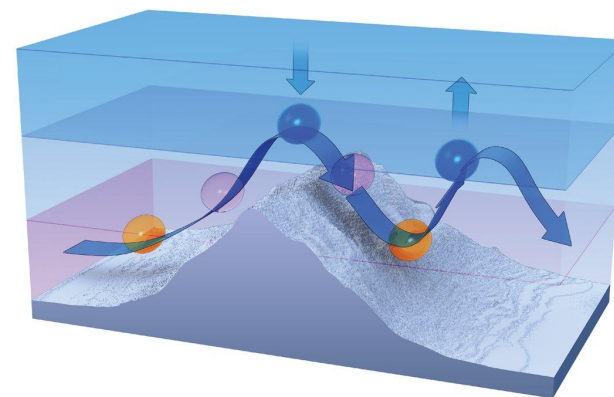
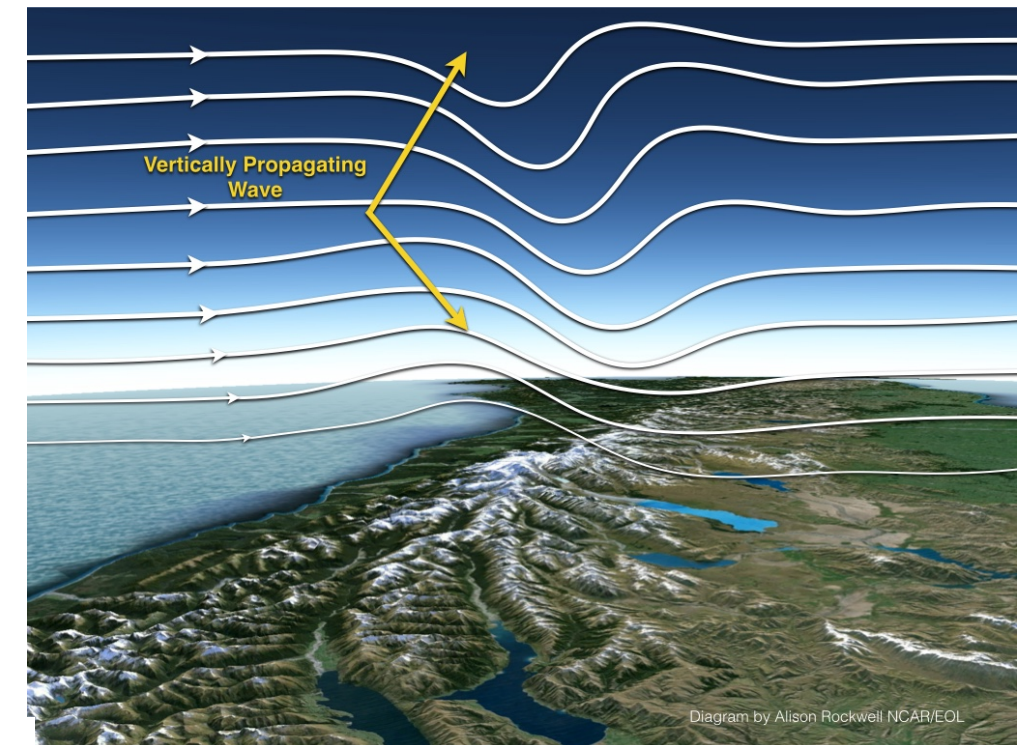
- “A strangely light neutron star within a supernova remnant”

- relies on specific assumptions about EoS prior, atm-models, temp. distribution etc.

g -modes (gravity modes)

restoring forces from buoyancy/gravity

- e.g. atmospheric or ocean waves
- hydrostatic equilibrium: gravitational force balanced by pressure gradient force
- perturbed from equilibrium \rightarrow gravity or buoyancy pulls/pushes it back \rightarrow oscillation



Local (buoyancy) frequency

- pressure instantaneously equilibrated, but not for composition and density
- continuity equation & the equation of motion
- “**adiabatic**” (composition frozen) sound speed vs. “**equilibrium**” sound speed

$$dp/dr = -\rho g$$

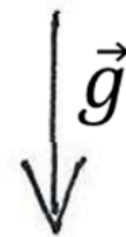
[hydrostatic equilibrium]

$$N^2 \equiv g^2 \left(\frac{1}{c_{eq}^2} - \frac{1}{c_{ad}^2} \right)$$

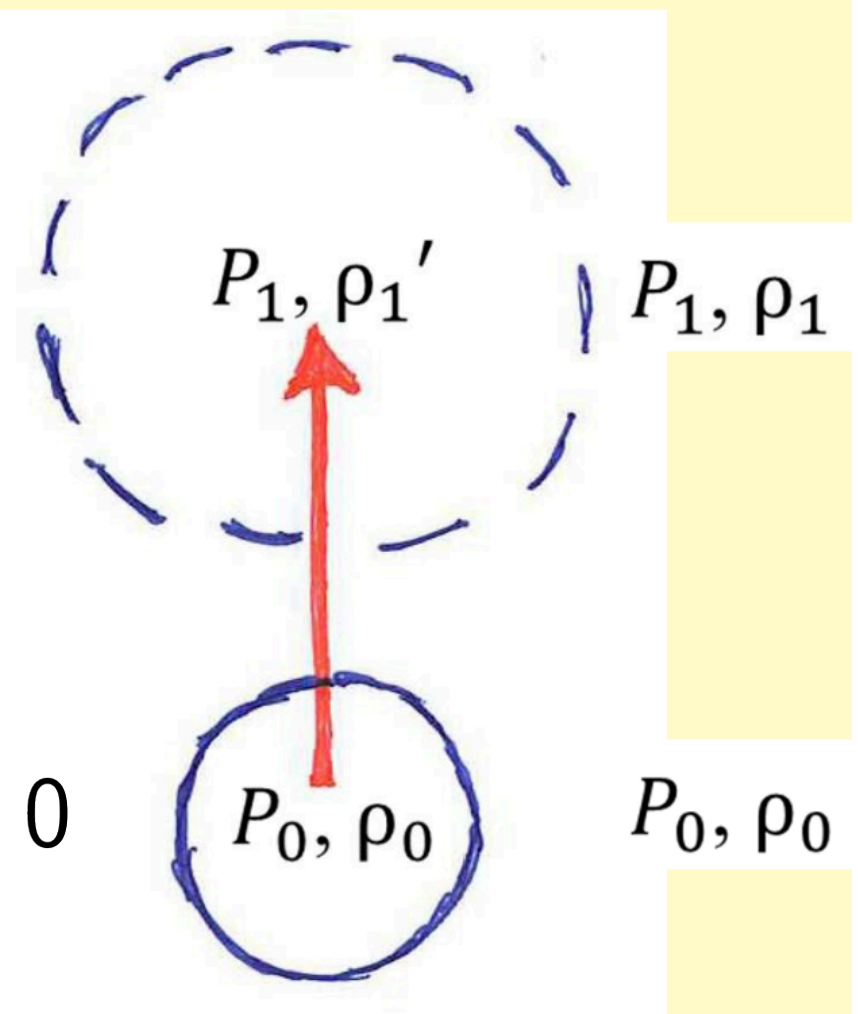
$$c_{eq}^2 = \left(\frac{dp/dr}{d\varepsilon/dr} \right)$$

$$c_{ad}^2 = \left(\frac{\partial p}{\partial \varepsilon} \right)_{y_i}$$

$$\Delta \rho = -\rho \frac{\partial^2 \xi}{\partial t^2}$$



$$\frac{\partial^2 \xi}{\partial t^2} + N^2 \xi = 0$$

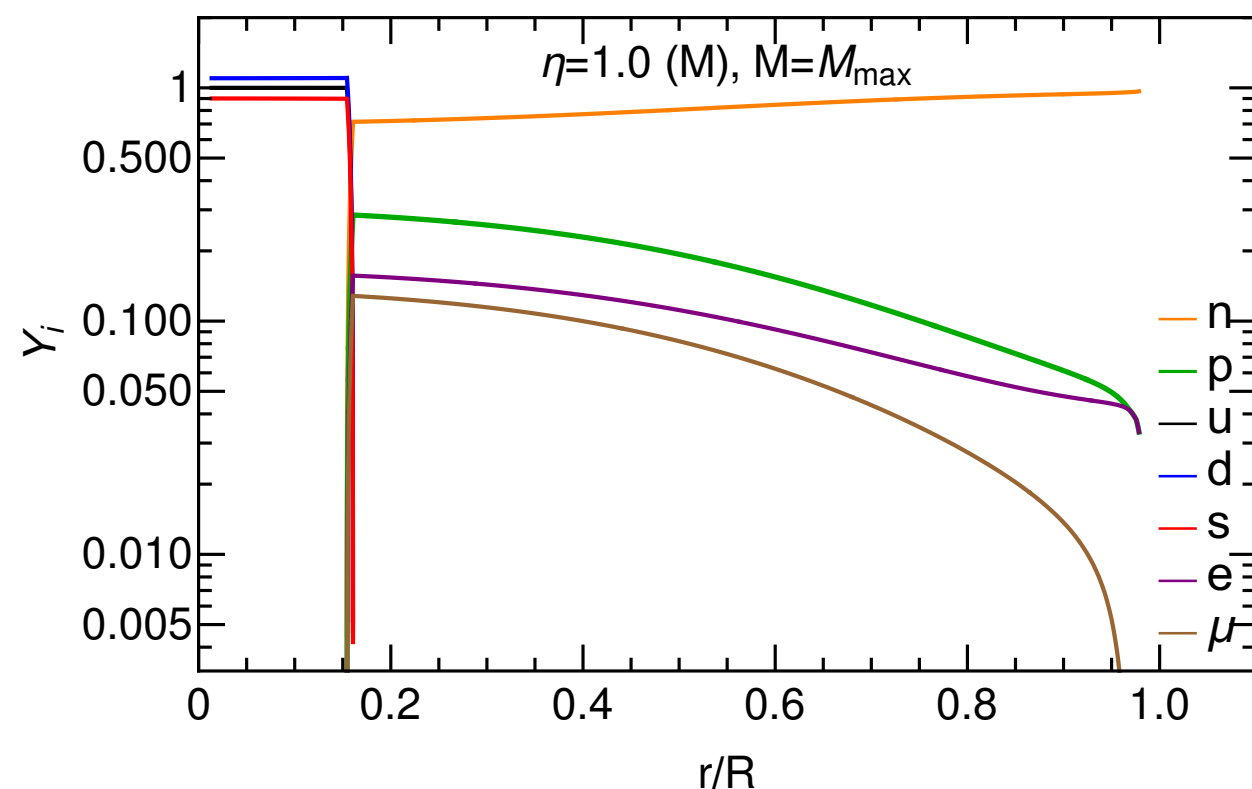


credit: Andreas Reisenegger

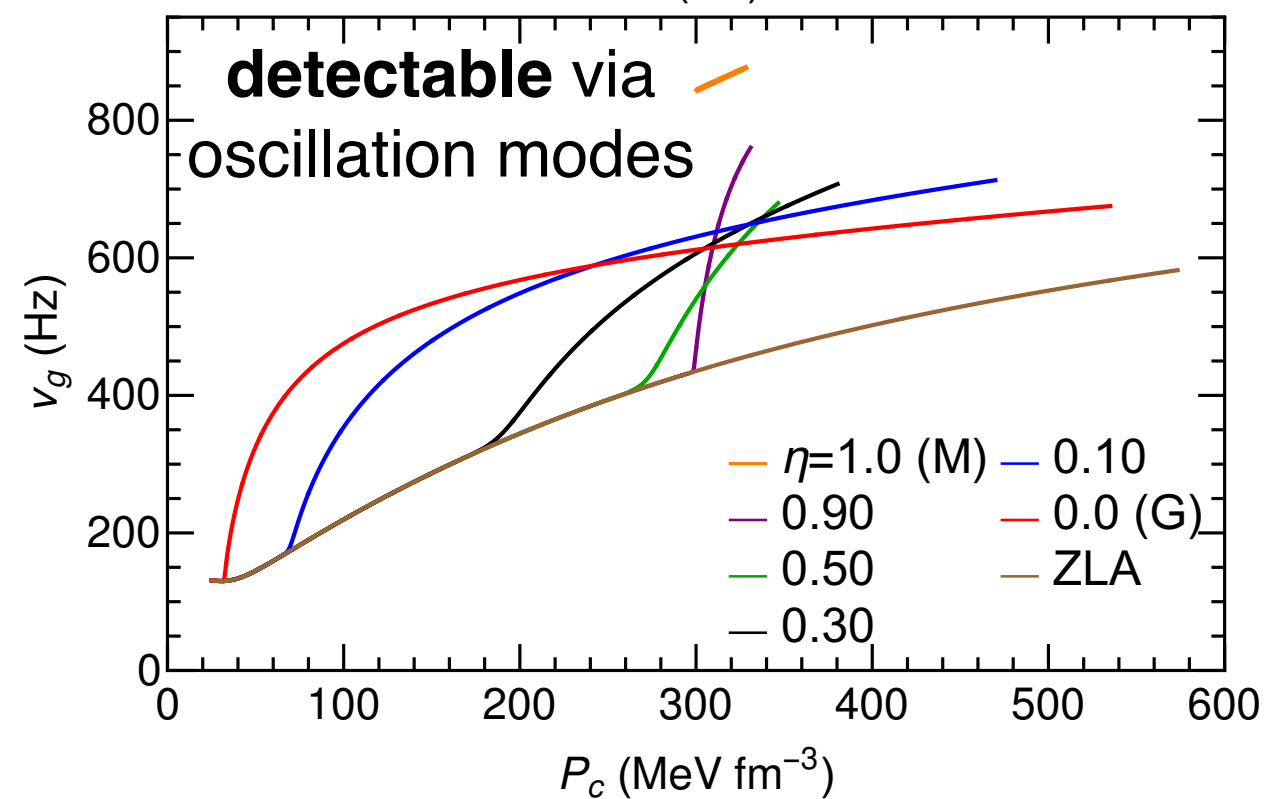
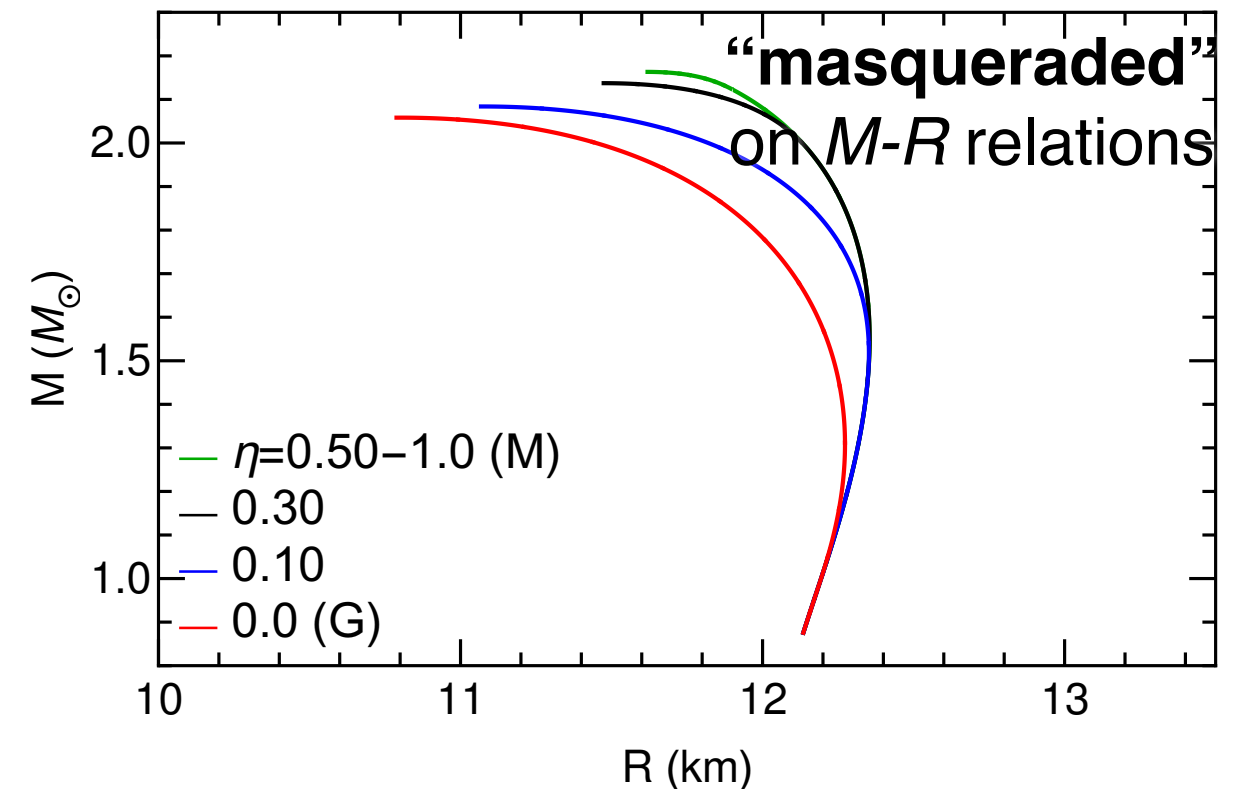
$e^{\nu-\lambda}$ ← [local metric coefficients]

Global g -mode frequency with PTs

- hybrid system under local vs. global charge neutrality in Maxwell (M) vs. Gibbs (G) construction for a 1st-OPT



- “discontinuity” g -mode observed when there exists a sharp boundary
- **distinct signature of exotic phases:** higher frequency indicates larger fraction of quark matter



Constantinou et al. (including **SH**),
arXiv:2302.04289