

Theory Overview of Offshell Higgs Physics

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CMS Topical Workshop on Off-shell Higgs Boson Production at the LPC

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UNIVERSITÀ
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Disclaimer

- I will give an overview of the successes, opportunities and challenges for Higgs studies in the offshell regime.
- Try to be as comprehensive as possible.
- Focus mostly on Higgs production through gluon fusion and decay to massive EW boson pair, $gg \rightarrow (H) \rightarrow VV$.
- Will not discuss:
 - Non-interfering VV background → **John's talk**
 - BSM effects (including SMEFT) → **Alejo's talk**

Why study the Higgs boson?

Goals of Higgs physics studies:

- Determine **properties** of Higgs boson (mass, spin, CP properties, ...).
- Determine **interactions** with other SM particles.
- **Is the Higgs (solely) responsible for EWSB?**
- Can the Higgs lead us to NP?

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Coupling to Higgs is proportional to mass

$$g_{Hf\bar{f}} \sim \frac{m_f}{v} \quad g_{HVV} \sim M_V$$

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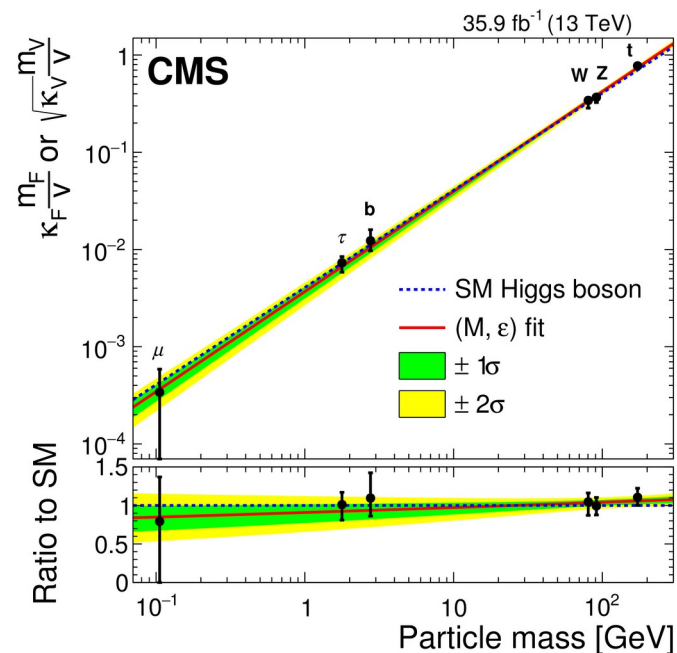
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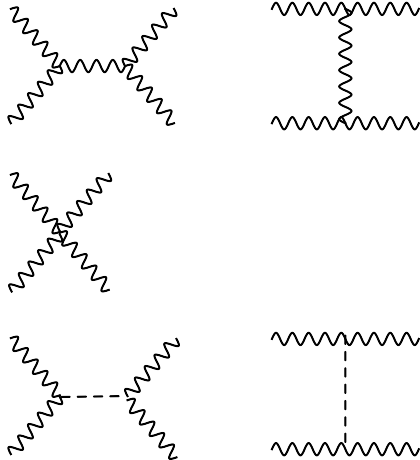
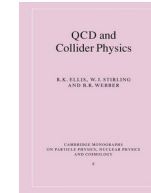
$$g_{Hf\bar{f}} \sim \frac{m_f}{v} \quad g_{HVV} \sim M_V$$



Unitarization of massive amplitudes

Apart from generating masses, EWSB mechanism also **unitarizes massive scattering amplitudes**.

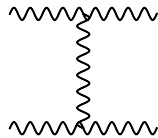
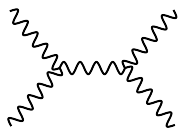
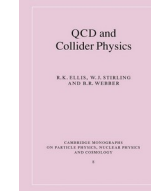
Textbook example: $W^+(p_+) + W^-(p_-) \rightarrow W^+(k_1) + W^-(k_2)$ $p_{\pm} = (E, 0, 0, \pm p)$



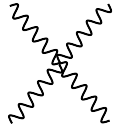
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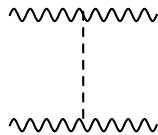
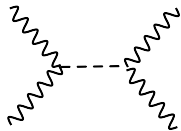
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$$\sim A \left(\frac{p^2}{m_W^2} \right)^2 + B \left(\frac{p^2}{m_W^2} \right)$$



$$\sim -A \left(\frac{p^2}{m_W^2} \right)^2 + \tilde{B} \left(\frac{p^2}{m_W^2} \right)$$

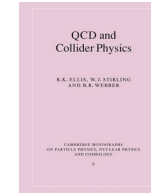


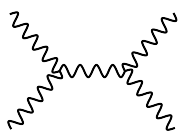
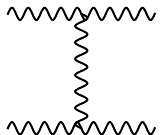
→ Violation of unitarity due to **longitudinal vector boson modes**.

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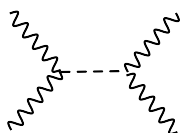
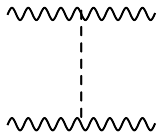


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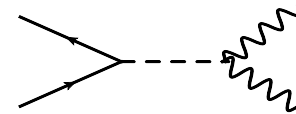
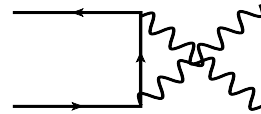
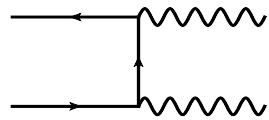
$$\sim -(B + \tilde{B}) \frac{p^2}{m_W^2}$$

→ Violation of unitarity due to **longitudinal vector boson modes**.

→ Higgs boson cancels out high-energy behavior of longitudinal modes – **amplitude remains finite in high-energy limit**.

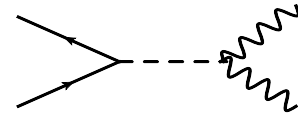
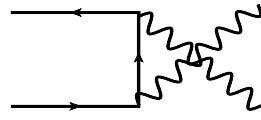
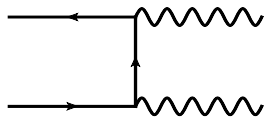
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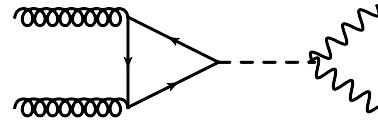
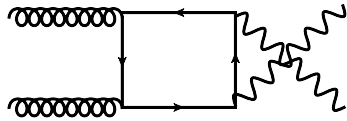
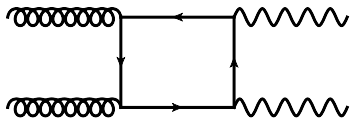


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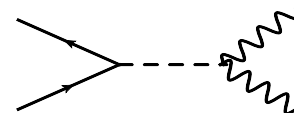
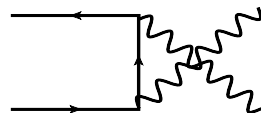
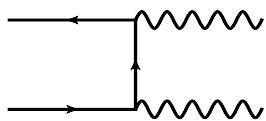


... and in $gg \rightarrow (H) \rightarrow VV$

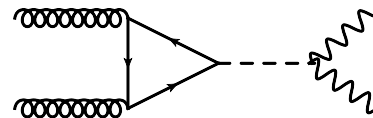
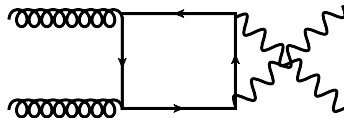
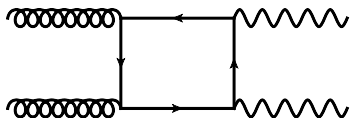


Unitarization of massive amplitudes

The same thing happens in e.g. $t\bar{t} \rightarrow VV$



... and in $gg \rightarrow (H) \rightarrow VV$



Studying offshell Higgs production allows us to confirm that the Higgs is indeed unitarizing scattering amplitudes – essential part of EWSB.

Offshell Higgs

➔ $gg \rightarrow H \rightarrow VV$ must have a **large contribution in the offshell region.**

- **~ 10%** of events have $m_{VV} > 2m_V$.

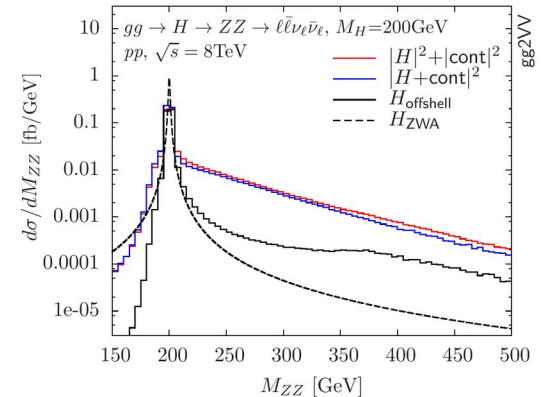
[Kauer, Passarino (2012); Kauer (2013)]

- **Contrary to expectations** from narrow width approximation:

$$\frac{\Gamma_H}{m_H} \simeq \frac{4 \text{ MeV}}{125 \text{ GeV}} \sim 10^{-5}$$

→ Naively expect a **very narrow resonance** and hence offshell cross section **highly suppressed.**

- Instead, relatively large number of offshell events – **dramatic failure of NWA.**
- *What else can we do with offshell Higgs?*



[Kauer, Passarino, 2012]:

Higgs Width Determination

- Direct measurement of **Higgs width** limited by detector resolution:

$$\Gamma_H \lesssim 1 \text{ GeV} \quad \text{with} \quad \Gamma_H^{\text{SM}} \simeq 4 \text{ MeV}$$

- Consider $i \rightarrow H \rightarrow f$:

- Onshell cross section: $M_{VV} \approx m_H^2 \quad \sigma \propto g_i^2 g_f^2 / \Gamma_H$

- Offshell cross section: $M_{VV} \gg m_H^2 \quad \sigma \propto g_i^2 g_f^2$

[Caola, Melnikov (2013)]

- Consider rescaling couplings and width such that onshell rate is unchanged:

$$g_i \rightarrow \alpha g_i; \quad \Gamma_H \rightarrow \alpha^4 \Gamma_H$$

- Offshell cross section is $\sigma_{\text{off}} = \alpha^4 \sigma_H^{\text{off}} - \alpha^2 \sigma_{\text{intf}} = \frac{\Gamma_H}{\Gamma_H^{\text{SM}}} \sigma_H^{\text{off}} - \sqrt{\frac{\Gamma_H}{\Gamma_H^{\text{SM}}}} \sigma_{\text{intf}}$

Interference term with different scaling of width!

- Comparing this with number of observed events \rightarrow **bound on Higgs width**.

Higgs Width Determination

- Cut-and-count: $\Gamma_H \lesssim 21 \times \Gamma_H^{\text{SM}}$ [Caola, Melnikov (2013)]
- Matrix element methods: $\Gamma_H \lesssim 25 \times \Gamma_H^{\text{SM}}$ [Campbell, Ellis, Williams (2013)]
- $H \rightarrow WW$ $\Gamma_H \lesssim 45 \times \Gamma_H^{\text{SM}}$ [Campbell, Ellis, Williams (2013)]

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10 years of work....

ATLAS: $\Gamma_H = 4.5_{-2.5}^{+3.3}$ MeV **CMS:** $\Gamma_H = 3.2_{-1.7}^{+2.4}$ MeV

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Remarkable progress: from **constraint of three orders of magnitude** to **50% error** in a decade!

Caveat

- Underlying assumption: Higgs **onshell couplings** same as **offshell couplings**.
- Valid in SM, but Higgs width fully predicted by SM → consistency check.
- New Physics could **change the behavior of the couplings** in such a way that the **Higgs width is the same** as in SM!

[Englert, Spannowksy (2014); Englert, Soreq, Spannowsky (2014), Azatov, Grojean, Paul, Salvioni (2016),]

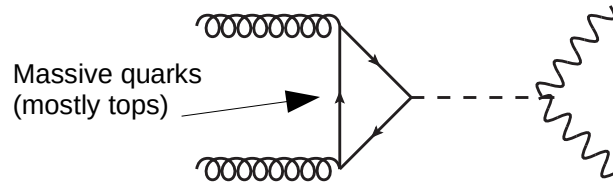
- Parametrize couplings using e.g. SMEFT and perform **simultaneous determinations** of these and Higgs width using offshell data.
- → constraints on **light quark Yukawa couplings**.

[Balzani, Gröber, Vitti (2023)]

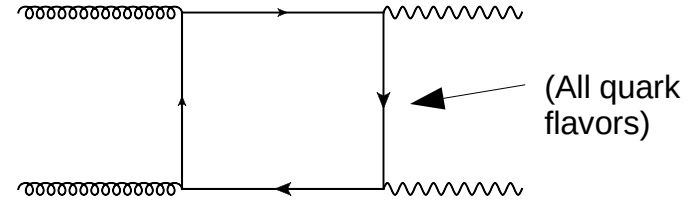
→ Talk by Alejo

Ingredients for theoretical predictions

Need to include both signal and background amplitudes:



“signal” A_s



“background” A_b

$$|A_{ZZ}|^2 = |A_s|^2 + |A_b|^2 + 2\text{Re}[{}_s A_b^*]$$

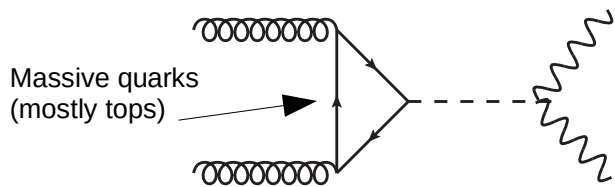
$$\rightarrow \sigma_{\text{full}} = \sigma_{\text{sigl}} + \sigma_{\text{bkgd}} + \sigma_{\text{intf}}$$

Physical observable

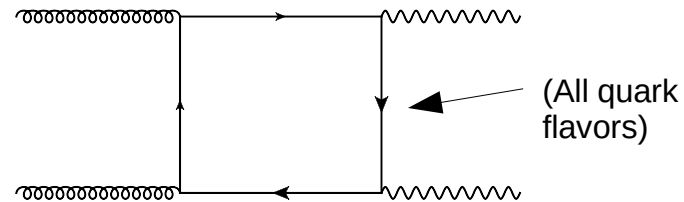
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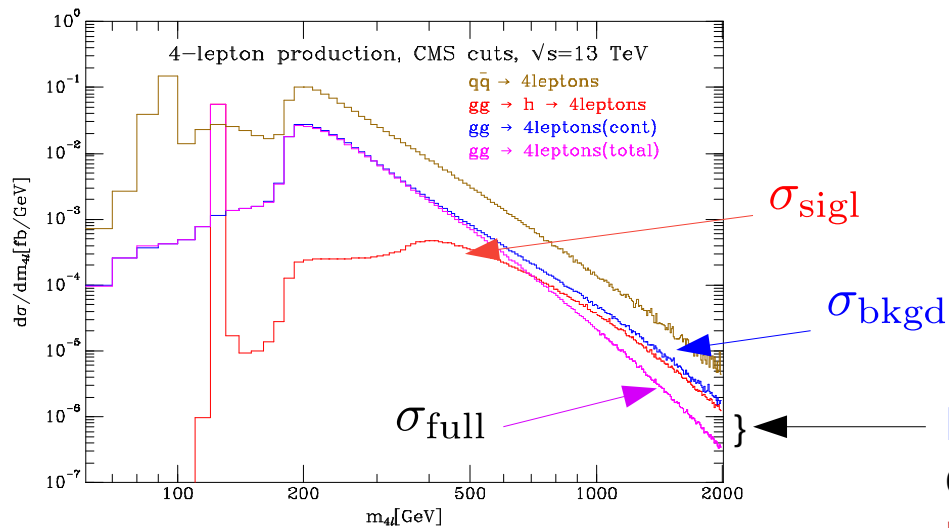
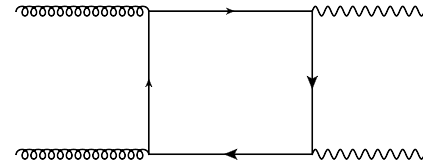
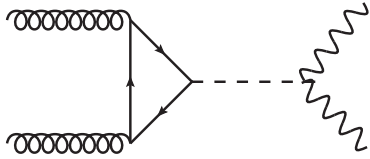
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Physical observable

Large and negative

Loop-induced processes →
challenging calculations!

Leading order results



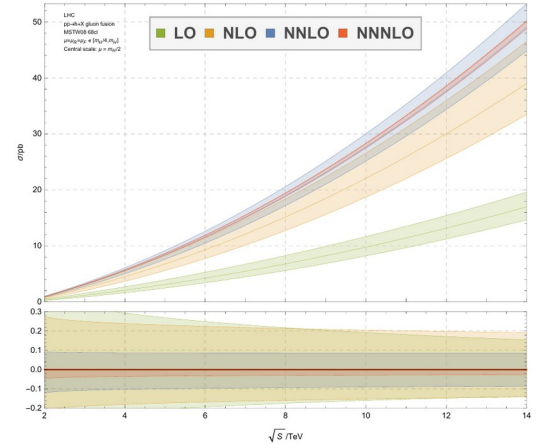
- Stable V bosons [Dicus, Kao, Repko (1987); Glover, van der Bij (1989)]
- Including decays [Matsuura, van der Bij (1991); Zecher, Matsuura, van der Bij (1994)]
- gg2VV [Binoth, Kauer, Mertsch (2008)]
- MCFM [Campbell, Ellis, Williams (2011)]

Large destructive interference at high energies – sign of Higgs unitarizing massive scattering amplitudes.

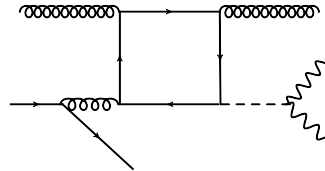
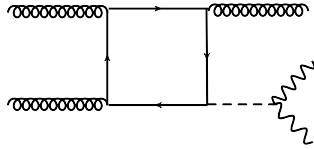
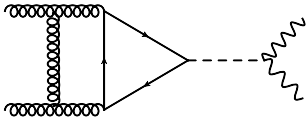
[Campbell, Ellis, Williams (2013)]

NLO Calculations

- Observe **large QCD corrections** to Higgs production through gluon fusion in infinite top limit.
- Two challenges in computing higher order results:
 - **Loop amplitude**
 - **IR singularities**
- Since LO process is loop-induced, NLO results requires **two-loop amplitude – bottleneck**.
- IR singularities are NLO-like and can be treated with **standard NLO subtraction techniques**.
- Relevant amplitudes for **signal process** have been known for many years.



[Anastasiou, Duhr, Dulat, Herzog, Mistlberger, (2015)]



[Dawson (1991)]

Djouadi, Spira, Zerwas (1991);
Djouadi, Graudenz, Spira, Zerwas (1995)

Harlander, Kant (2005)

Anastasiou, Beerli, Bucherer, Daleo, Kunszt (2006)

Aglietti, Bonciani, Degrossi, Vicini (2007)]

[Ellis, Hinchcliffe, Soldate, van der Bij (1988)

Baur, Glover, van der Bij (1991)]

+ modern one-loop generators, e.g.

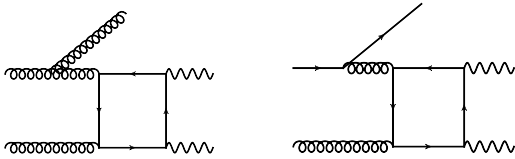
➢ MadGraph [Alwall et al, (2014)]

➢ OpenLoops [Cascioli, Maierhöfer, Pozzorini (2012); Buccioni, Pozzorini, Zoller (2018); Buccioni et al (2019)]

➢ ...

NLO Calculations

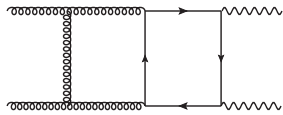
Background amplitudes are more demanding:



Massless quarks: analytic results

[Caola, Melnikov, RR, Tancredi (2015)]

Massless + massive quarks: automated one-loop tools (OpenLoops, MadGraph, ...)



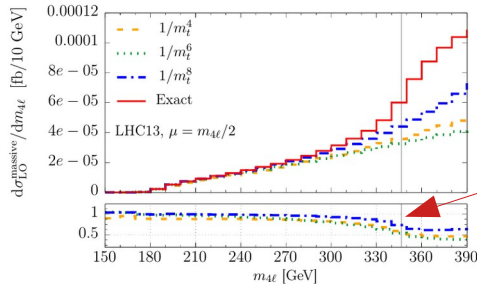
- Massless quarks: **challenging but achievable**

[von Manteuffel, Tancredi (2015); Caola, Henn, Melnikov, Smirnov, Smirnov (2015)]

- **Massive quarks in the loop: very demanding – bottleneck for many years**

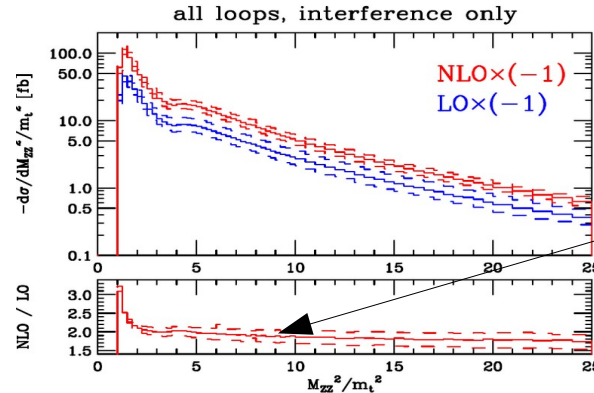
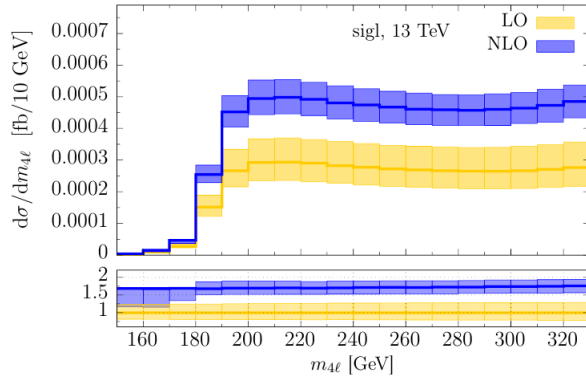
- Computed using expansion in $1/m_t$

[Dowling, Melnikov (2015); Czakon, Campbell, Kirchner, Ellis (2016);
Caola, Dowling, Melnikov, RR, Tancredi (2016)]



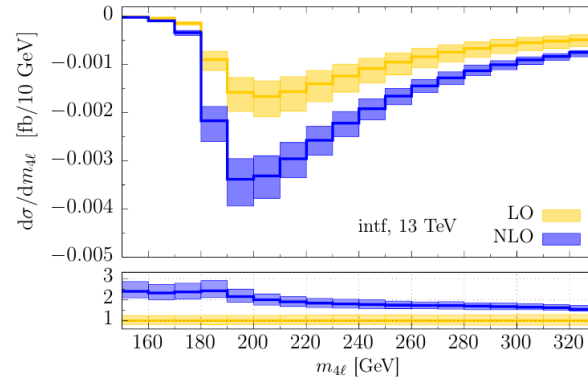
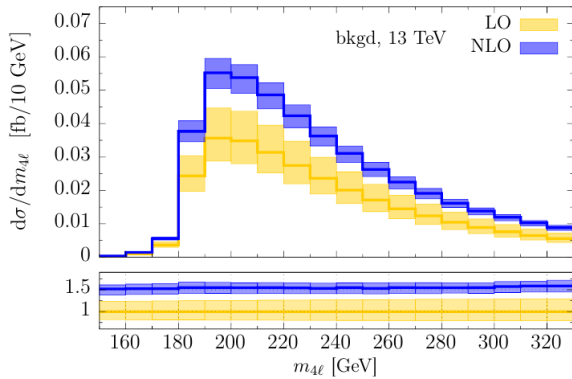
- Expansion valid for $m_{VV} < 2m_t$.
- **Breaks down above top-pair production threshold.**

NLO results: ZZ final state



[Czakon, Campbell, Kirchner, Ellis (2016)]

Padé approximant above top-pair threshold.



- Minor differences between two calculations, but **qualitative agreement** on impact of NLO effects.
- Corrections for signal, background, interference are **large and similar**, but not **identical**.
- Similar results for WW final state.

[Caola, Dowling, Melnikov, RR, Tancredi (2016)]

NLO Results

- NLO corrections combined with NNLO QCD + NLO EW results for ZZ production:

[Grazzini, Kallweit, Wieseemann, Yook (2018), (2021)]

- All partonic channels included.
- Two-loop background amplitudes estimated through **reweighting procedure**.
- Idea**: Assume QCD effects are similar for massless and massive quark loops.

$$\frac{A_b^{2\text{-loop}}(u, d, s, c, b, t)}{A_b^{1\text{-loop}}(u, d, s, c, b, t)} \approx \frac{A_b^{2\text{-loop}}(u, d, s, c, b)}{A_b^{1\text{-loop}}(u, d, s, c, b)}$$

$$\Rightarrow A_b^{2\text{-loop, rwgt.}}(u, d, s, c, b, t) = \frac{A_b^{2\text{-loop}}(u, d, s, c, b)}{A_b^{1\text{-loop}}(u, d, s, c, b)} A_b^{1\text{-loop}}(u, d, s, c, b, t)$$

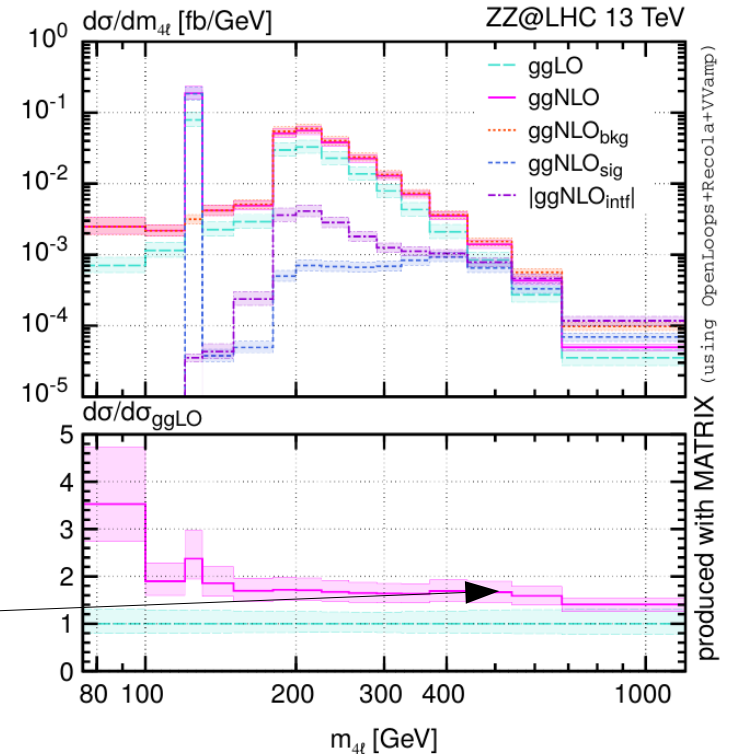
(implemented at amplitude-squared level).

➔ **results above top-pair threshold.**

Publicly available through MATRIX.

- WW channel also included.

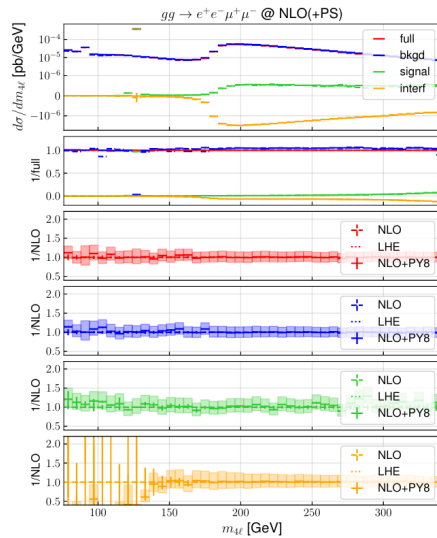
[Grazzini, Kallweit, Lindert, Pozzorini, Wieseemann (2019)]



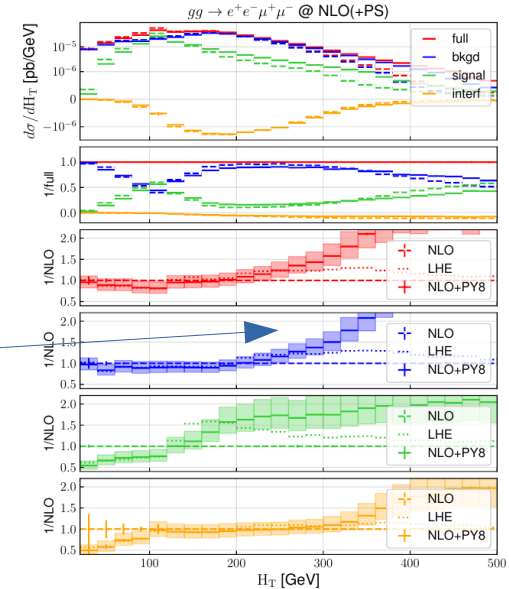
NLO + PS Results

- NLO-accurate calculation matched to parton showers in POWHEG-BOX.

[Alioli, Ferrario Ravasio, Lindert, RR (2021); Alioli, Caola, Luisoni, RR (2016)]



- Two-loop background amplitudes either computed in $1/m_t$ expansion or through reweighting.
- Main observable m_{VV} is **inclusive** – effect of PS is small.
- For **exclusive** observables, e.g. H_T , it can be substantial.



→ Talk by Simone

Summary: where are we today?

- ☹️ Most advanced calculation available: **(approximate) NLO**
 - Difficulty of computing background amplitudes at two-loops with massive (virtual) quarks.
 - Approximations:
 - Expansion in $1/m_t$ – limited to $m_{VV} < 2m_t$
 - Reweighting
- 😊 (Approximate) NLO matched to PS → unweighted events
- 😊 Public: MATRIX and POWHEG-BOX

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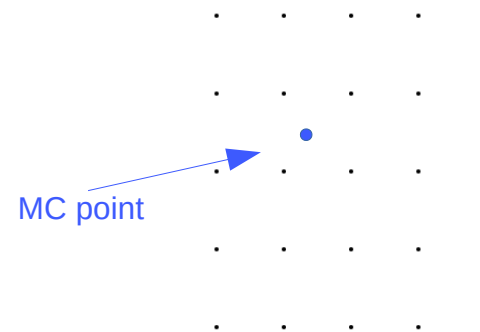
Where should we go from here?

1. Complete NLO corrections
2. Beyond NLO
3. EW effects

Towards Complete NLO Corrections

- Two-loop massive background amplitudes have been computed **numerically**.
 - Fixed values of top, W, Z masses.
- Evaluation time: 1-24 hours/phase space point.
- Typical number of points in MC integration ~ 100k.
- Interfacing these calculations with MC integrators is **tricky but doable**.
- **Better idea (?)** : Pre-generate a grid and then interpolate between them to obtain virtual amplitude at MC point.
 - Re-use grid for runs with minor differences in inputs (e.g. pdf sets).

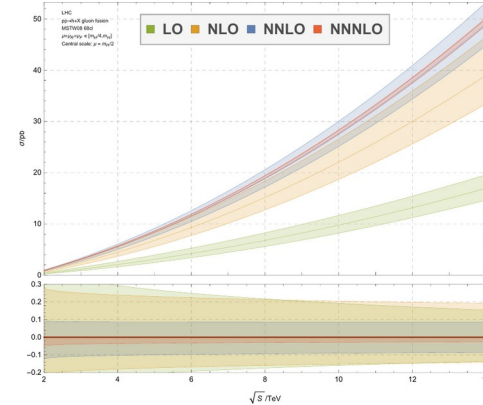
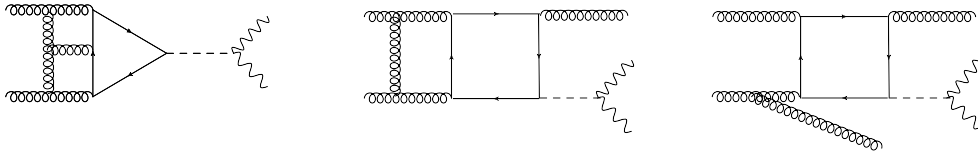
[Agarwal, Jones, von Manteuffel (2020), Brønnum-Hansen, Chen (2020, 2021)]



Shouldn't be any major obstacles to including these amplitudes in NLO codes and obtaining **complete NLO results**.

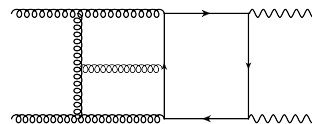
Beyond NLO in QCD

- Onshell Higgs production (in infinite top limit):
 - NNLO corrections **large** ($k \sim 1.2-1.3$).
 - Scale uncertainty at NLO **doesn't capture higher order corrections**.
 - Top mass effects are small. [Czakon, Harlander, Klappert, Niggetiedt (2021)]
- Assuming same is true for offshell Higgs → **need NNLO corrections** (with full top mass dependence).
- NNLO corrections for **signal** process known.



[Anastasiou, Duhr, Dulat, Herzog, Mistlberger, (2015)]

- Background** requires three-loops corrections
→ **beyond current abilities**.



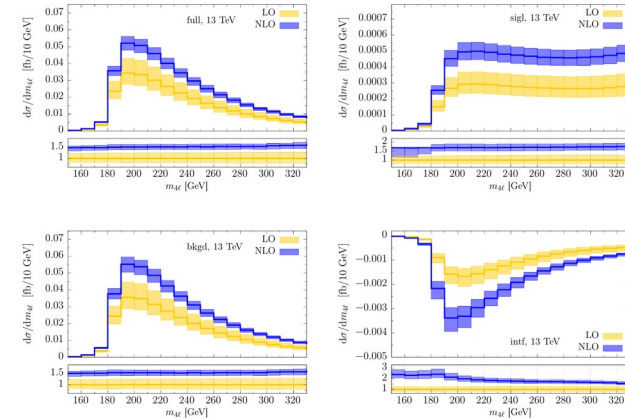
- What can we do?*
 - Reweighting
 - Additional radiation
 - (Better) approximations

Reweighting

- Corrections to **signal**, **background** and interference are similar.
- Rescale **background** and interference by corrections to **signal** at NNLO.

$$d\sigma_{\text{bkgd.}}^{\text{NNLO}} \approx \frac{d\sigma_{\text{sigl.}}^{\text{NNLO}}}{d\sigma_{\text{sigl.}}^{\text{NLO}}} d\sigma_{\text{bkgd.}}^{\text{NLO}}$$

In conclusion, in all cases radiative corrections have the effect of increasing the absolute size of the individual contributions. However, **the relative size of the corrections for the individual contributions is quite different**, especially at small $m_{4\ell}$ values, and the full result is a combination of all of those effects. Only at large invariant masses ($m_{4\ell} \gtrsim 400$ GeV) the relative size of the corrections becomes similar for signal, background and interference. **It is therefore difficult to make a direct connection between the QCD corrections beyond NLO for the signal, which are known to be relatively large** (see Ref. [92] and references therein), **and the other contributions**, where they are not known. Nevertheless, the NLO corrections in the off-shell region are not that different among the three contributions, and the QCD effects beyond NLO are expected to be significant. Therefore, in order to approximately take higher-order corrections into account, one might be tempted to **rescale our NLO result for the off-shell cross section** by using the relative impact of the QCD corrections beyond NLO evaluated in the off-shell region for the signal contribution [92]. Needless to say, much care should be taken when following such approach.

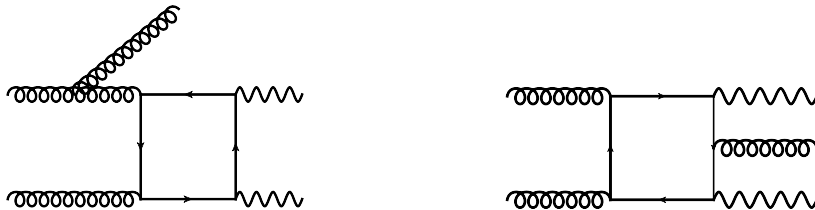


[Grazzini, Kallweit, Wiesemann, Yook (2021)]

- How to evaluate uncertainties?
- Use NLO results?

Adding radiation

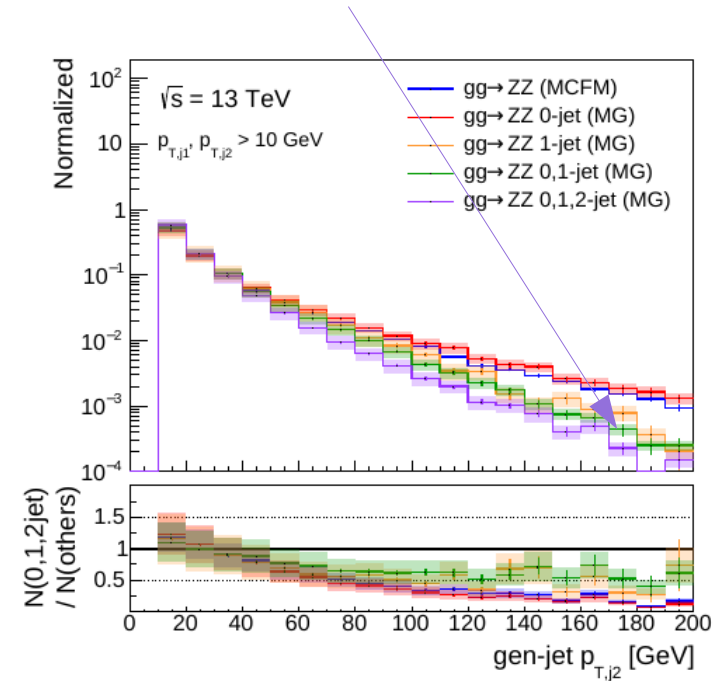
- NLO calculation supplies **one jet** (**matrix-element level**).
- **Further jets** through **PS** – from radiation from IS and FS partons.
- Miss radiation from virtual quarks in loop.



- Can include **second jet** at **ME level** using jet merging.

See also [Cascioli et al (2013)] for 0 and 1-jet merging in SHERPA.

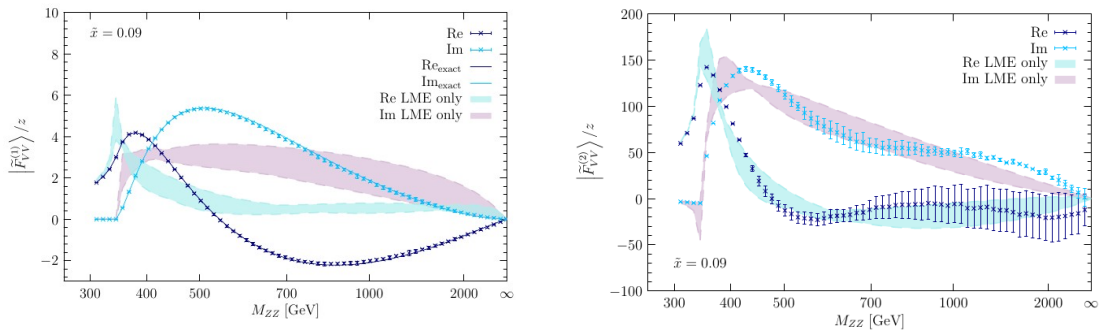
- [Li et al (2020)] using MadGraph and MLM merging.
- Softer second jets from **ME** compared to **PS**.



Better approximations

- Expansion in $1/m_t$ valid for $m_{VV} < 2m_t$.
 - Also include **expansion around top production threshold** and in **small mass limit** $m_t \rightarrow 0$.
 - Combine using **Padé approximants**.
- Results valid across **all of phase space**.

[Gröber, Maier, Rauh (2017), (2019); Davies, Gröber, Maier, Rauh, Steinhauser (2020)]



Extend to 3-loop for NNLO corrections?

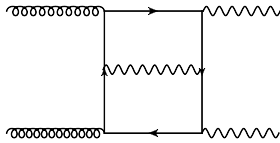
[Gröber, Maier, Rauh (2019)]

Electroweak Corrections

- EW corrections expected to be **enhanced** in high-energy regime.
- NLO EW corrections + NLL EW Sudakov corrections computed for ZZ and ZZj, merged with MEPS@NLO.

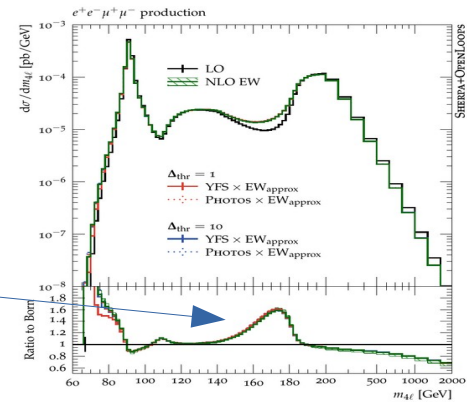
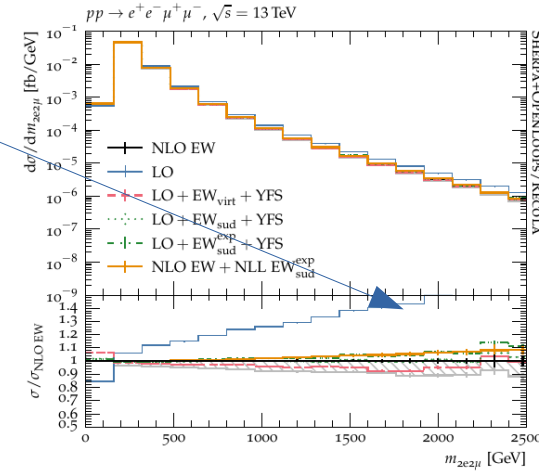
[Bothmann, Napoletano, Schönherr, Schumann, Villani (2021)]

- EW corrections to $\mathcal{O}(\alpha_s)$ processes only.
 - EW corrections to $gg \rightarrow (H) \rightarrow ZZ$ **not included**.
- Would require challenging two-loop amplitudes.



- QED radiation provided by **parton showers** (e.g. SHERPA, PHOTOS)
 - provide accurate approximation of EW effects in $q\bar{q} \rightarrow 4\ell$

[Gütschow, Schönherr (2020)]



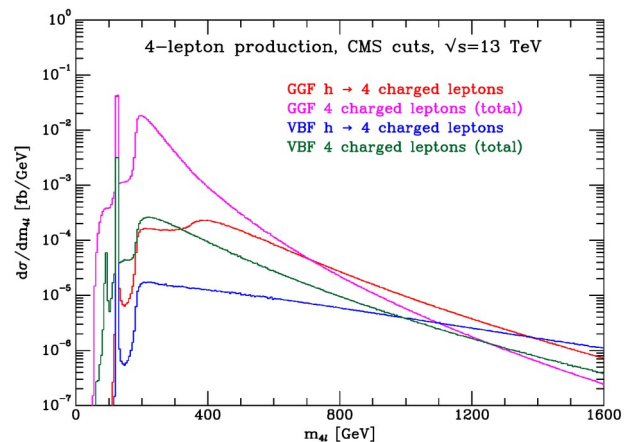
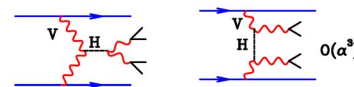
- SHERPA: [Krauss, Schönherr (2008)]
- PHOTOS: [Barberio, van Eijck, Was (1991); Barberio, Was (1994); Golonka, Was (2006); Davidson, Przdziński, Was (2016)]

Other production processes

Offshell Higgs in VBF:

[Campbell, Ellis (2015)]

- Higgs exchange in **s- and t-channels**.
- Same pattern of **large destructive interference** at high energies.
- Less stringent constraints on Higgs width.

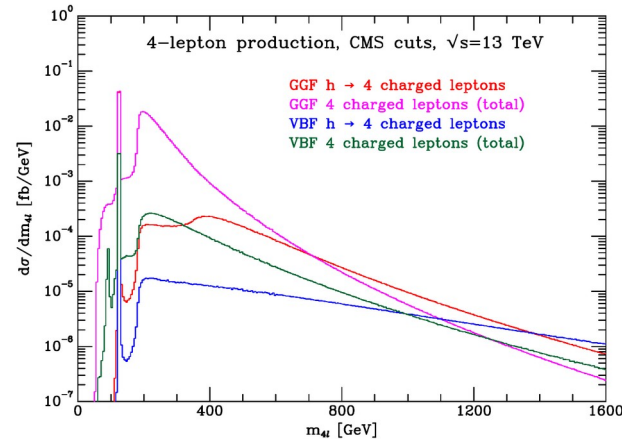
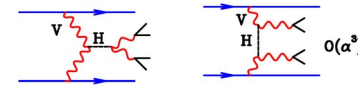


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- **Not loop-induced**: NLO QCD corrections can be obtained in e.g. MadGraph.
- [Alwall et al, (2014)]
- NNLO QCD results **unknown** but **feasible**.
- QCD corrections **mild** (\sim few percent at NNLO) so NNLO **might not be necessary**.

Conclusions

- Theoretical predictions for offshell Higgs production in gluon-fusion:
 - (Approximate) NLO QCD + PS.
 - Publicly available codes: POWHEG and MATRIX
 - Full NLO QCD corrections should be feasible.
 - As experimental precision improves, this might not be sufficient.
 - Ideas to include higher order effects:
 - Reweighting;
 - Jet merging;
 - Approximating multi-loop amplitudes using simultaneous expansions and Padé approximants;
 - QED effects in parton showers.
- We have made remarkable progress in ~ 10 years, largely due to dialogue between theorists and experimentalists.
- I'm excited to see what the next decade will bring for offshell Higgs phenomenology!



THANK YOU FOR YOUR ATTENTION