#### <span id="page-0-0"></span>Charge-breaking opportunities for the early Universe

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Based on: Aoki, Biermann, Borschensky, Ivanov, Mühlleitner, Shibuya, JHEP 02 (2024) 232 = arXiv:2308.04141 Yang, Ivanov, PRD110 (2024) 1, 015001 = arXiv:2401.03264.





Higgses can come in generations  $\rightarrow N$ -Higgs-doublet models (NHDMs).

- T.D. Lee, 1973: 2HDM as a new source of CP-violation (CPV);
- Weinberg, 1976: 3HDM with natural flavor conservation and CPV;
- Intense activity in 70–80's: trying to reconstruct hierarchical quark and lepton masses and mixing patterns from symmetries and their breaking;
- Cosmological consequences: scalar dark matter candidates protected by residual symmetries and strong first-order phase transitions  $\rightarrow$  baryogenesis and GW signals.
- In total,  $\mathcal{O}(10^4)$  papers over 40 years [Branco et al, 1106.0034; Ivanov, 1702.03776]

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# Charge-breaking vacuum in the early Universe

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#### 2HDM potential

2HDM with a softly broken  $\mathbb{Z}_2$  symmetry (review Branco et al, 1106.0034):

$$
V_{\text{tree}} = m_{11}^2 \Phi_1^{\dagger} \Phi_1 + m_{22}^2 \Phi_2^{\dagger} \Phi_2 - m_{12}^2 (\Phi_1^{\dagger} \Phi_2 + \text{h.c.}) + \frac{\lambda_1}{2} (\Phi_1^{\dagger} \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^{\dagger} \Phi_2)^2 + \lambda_3 (\Phi_1^{\dagger} \Phi_1) (\Phi_2^{\dagger} \Phi_2) + \lambda_4 (\Phi_1^{\dagger} \Phi_2) (\Phi_2^{\dagger} \Phi_1) + \frac{\lambda_5}{2} [(\Phi_1^{\dagger} \Phi_2)^2 + \text{h.c.}].
$$

Vacuum stability:  $\lambda_1, \lambda_2 > 0$ ,  $\sqrt{\lambda_1\lambda_2} + \lambda_3 > 0$ ,  $\sqrt{\lambda_1\lambda_2} + \lambda_3 + \lambda_4 - |\lambda_5| > 0$  [Deshpande, Ma, 1978]

• Perturbative unitarity: partial wave amplitudes  $|a_{\ell}| < 1 \rightarrow$  eigenvalues of the 2  $\rightarrow$  2 quartic coupling matrix are  $< 16\pi$  [Lee, Quigg, Thacker, 1977; Kanemura, Kubota, Takasugi, 1993; Logan, 2207.01064], see also [Goodsell, Staub, 1805.07310].

Natural flavor conservation [Glashow, Weinberg; Paschos, 1977] each right-handed fermion sector ( $u_R$ ,  $d_R$ ,  $\ell_R$ ) couples only to one Higgs doublet. Let's choose Type I 2HDM: all RH fermions couple only to  $\Phi_2$ .

#### Charge breaking vacuum

Minimization gives  $\langle \Phi_1 \rangle$ ,  $\langle \Phi_2 \rangle$ , which can be written as

$$
\langle \Phi_1 \rangle = \frac{1}{\sqrt{2}} \left( \begin{array}{c} 0 \\ v_1 \end{array} \right) \, , \quad \langle \Phi_2 \rangle = \frac{1}{\sqrt{2}} \left( \begin{array}{c} u \\ v_2 e^{i\zeta} \end{array} \right) \, ,
$$

- Neutral vacuum:  $u = 0$ , residual symmetry  $SU(2)_L \times U(1)_Y \to U(1)_{EM}$ ; the world we live in.
- Charge-breaking (CB) vacuum:  $u \neq 0$ : no residual symmetry,  $SU(2)_L \times U(1)_Y$  is broken completely, massive photon, no conserved electric charge.
- **The usual procedure: disregard the CB vacuum, assume the neutral vacuum, choose**  $v_1, v_2, \xi$  **as** input, compute  $m_{ij}^2$ , proceed with phenomenology.
- In general 2HDM, at tree level, the necessary and sufficient conditions for the CB minimum were established in [Ivanov, 2007].

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#### $\mathbb{Z}_2$  symmetric 2HDM: the phase diagram



Conditions for the CB minimum:  $\sqrt{\lambda_1 \lambda_2} > \lambda_3$ ,  $\lambda_4 > |\lambda_5|$ , the point  $(m_{11}^2, m_{22}^2)$  inside the CB wedge.



#### $\mathbb{Z}_2$  symmetric 2HDM: the phase diagram



 $\lambda_3 > 0$ 

The neutral/CB boundary is:

$$
\frac{m_{22}^2}{m_{11}^2} = \frac{\lambda_2}{\lambda_3} \, .
$$

The charged Higgs mass depends on the proximity to this boundary:

$$
\frac{m_{H^{\pm}}^2}{v^2} = \frac{\lambda_3}{2} \left( 1 - \frac{m_{11}^2}{m_{22}^2} \frac{\lambda_2}{\lambda_3} \right) .
$$

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## Charge breaking vacuum

In the hot early Universe, the Higgs potential and its minima evolve with temperature  $T \rightarrow$  phase transitions are expected.

Electroweak phase transition (EWPT) ( $v = 0 \Rightarrow v \neq 0$ ) is the most famous example. But other phase transitions could have taken place.

What if the charge-breaking vacuum existed in the hot early Universe in a range of T?

Ginzburg, Ivanov, Kanishev, 0911.2383: a simple tree-level study revealed benchmark 2HDMs with an intermediate CB vacuum at finite T.

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In Aoki et al, 2308.04141, we returned to this possibility with the finite- $\tau$  loop-corrected effective potential and the code BSMPT v2 [Basler, Mühlleitner, Müller, 2007.01725].

- $\bullet$  Is it possible at all to have a CB vacuum at intermediate  $T$ ?
- Are such scenarios compatible with the LHC Higgs results?
- **If they are, what are the characteristic features of such scenarios?**

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#### The formalism

Finite T one-loop corrected effective potential:  $V = V_{tree} + V_{CW} + V_{CT} + V_T$ , where

- $\bullet$   $V_{CW}$ : T-independent one-loop Coleman-Weinberg potential,
- $\bullet$   $V_{CT}$ : T-independent counterterms (keep v and  $m_h$ ),
- $\bullet$   $V_T$ : one-loop thermal corrections at finite T:

$$
V_T = \sum_k n_k \frac{T^4}{2\pi^2} J_{\pm}^{(k)} \left(\frac{m_k^2}{T^2}\right) ,
$$

with summation over all fields,  $n_k$  is the number of d.o.f., J's are the thermal integrals,  $m_k$ depend on the values of scalar fields; full expressions in [Basler et al, 1612.04086, 1803.02846].

Thermal masses are consistently implemented at one loop using the Arnold-Espinosa resummation procedure [Arnold, Espinosa, hep-ph/9212235; Quiros, hep-ph/9901312].

Recently extended to the general 2HDM using the bilinear formalism [Cao, Cheng, Xu, 2305.12764] and the Dirac algebra formalism [Pilaftsis, 2408.04511].

To gain qualitative insights, let's consider a toy model:

- stay with the tree-level potential,
- assume that the main thermal effect is in the quadratic coefficients:

$$
m_{11}^2(T) = m_{11}^2 + c_1 T^2
$$
,  $m_{22}^2(T) = m_{22}^2 + c_2 T^2$ ,  $m_{12}^2(T) = m_{12}^2$ ,

where for Type I 2HDM we have

$$
c_1 = \frac{1}{12} (3\lambda_1 + 2\lambda_3 + \lambda_4) + \frac{1}{16} (3g^2 + g'^2) ,
$$
  
\n
$$
c_2 = \frac{1}{12} (3\lambda_2 + 2\lambda_3 + \lambda_4) + \frac{1}{16} (3g^2 + g'^2) + \frac{1}{12} (y^2 + 3y^2 + 3y^2).
$$

Then one can describe thermal evolution as a straight trajectory on the phase diagram.

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#### Qualitative analysis



The ray passes through the CB wedge if

$$
\frac{c_2}{c_1} > \frac{|m_{22}^2|}{|m_{11}^2|} > \frac{\lambda_2}{\lambda_3}.
$$

- Not easy to satisfy!
- Placing  $T = 0$  point close to the wedge will lead to a dangerously light charged Higgs!
- The plot is for

 $\lambda_1 = 2, \lambda_2 = 0.25, \lambda_3 = 0.6, \lambda_4 = 2.8,$ 

which leads to  $m_{H^{\pm}} = 82$  GeV.

Adding  $m_{12}^2$  plays against the CB phase.

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The procedure adopted in Aoki et al, 2308.04141:

- Scan over parameter space of the tree-level potential to generate seed points:
	- At  $T = 0$ : neutral vacuum,  $v = 246.22$  GeV,  $m_h = 125.09$  GeV
	- At  $T \neq 0$ : intermediate CB phase.
- $\bullet$  For each seed point, analyze the full finite-T one-loop corrected effective potential using BSMPT v2.
- Select points for which the intermediate CB phase survives for the effective potential.
- Use ScannerS [Coimbra et al, 1301.2599] to apply scalar sector constraints (unitarity, STU, flavor physics, HiggsSignals/HiggsBounds).
- **•** Unfortunately, all such seed points are excluded by the LHC data, mainly by  $\mu_{\gamma\gamma}$ , due to the presence of a light  $H^\pm$ .
- So, one more tweak: we explore the parameter space patches in the vicinity of seed points: the CB phase must be present in the full effective potential, but no need to require it in  $V_{tree}$ .

#### Numerical results



Intermediate CB vacuum is possible in the 2HDM — but only at the expense of a large  $\lambda_1$  and EW symmetry non-restoration at high T! Typical predictions: large tan  $\beta \sim 10 - 100$  and rather small  $m_{H^+} \sim 150 - 200$  GeV.



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[Slide borrowed from the talk by Christoph Borschensky at Scalars 2023] Confirmed with BSMPT v3, Basler et al, 2404.19037.

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# Charge-breaking bubbles walls in multi-Higgs-doublet models

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A powerful feature of 3HDM: a lot of new symmetry options available!

abelian groups: [Ferreira, Silva, 1012.2874; Ivanov, Keus, Vdovin, 1112.1660]

 $\mathbb{Z}_2$ ,  $\mathbb{Z}_3$ ,  $\mathbb{Z}_4$ ,  $\mathbb{Z}_2 \times \mathbb{Z}_2$ ,  $U(1)$ ,  $U(1) \times \mathbb{Z}_2$ ,  $U(1) \times U(1)$ .

finite non-abelian groups: [Ivanov, Vdovin, 1210.6553; Darvishi, Pilaftsis, 1912.00887]:

S<sub>3</sub>, D<sub>4</sub>, A<sub>4</sub>, S<sub>4</sub>, Δ(54), Σ(36).

• The classification is exhaustive: any other finite group leads to an accidental continuous symmetry. Accidental symmetries were classified in [Darvishi, Pilaftsis, 1912.00887].

Large finite groups come up with many minima and saddle points

 $\Rightarrow$  consequences for phase transitions!

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The scalar potential

$$
V = -m^2 \left[ \phi_1^{\dagger} \phi_1 + \phi_2^{\dagger} \phi_2 + \phi_3^{\dagger} \phi_3 \right] + \lambda_1 \left[ \phi_1^{\dagger} \phi_1 + \phi_2^{\dagger} \phi_2 + \phi_3^{\dagger} \phi_3 \right]^2 - \lambda_2 \left[ |\phi_1^{\dagger} \phi_2|^2 + |\phi_2^{\dagger} \phi_3|^2 + |\phi_3^{\dagger} \phi_1|^2 - (\phi_1^{\dagger} \phi_1)(\phi_2^{\dagger} \phi_2) - (\phi_2^{\dagger} \phi_2)(\phi_3^{\dagger} \phi_3) - (\phi_3^{\dagger} \phi_3)(\phi_1^{\dagger} \phi_1) \right] + \lambda_3 \left( |\phi_1^{\dagger} \phi_2 - \phi_2^{\dagger} \phi_3|^2 + |\phi_2^{\dagger} \phi_3 - \phi_3^{\dagger} \phi_1|^2 + |\phi_3^{\dagger} \phi_1 - \phi_1^{\dagger} \phi_2|^2 \right),
$$

where terms in blue are  $SU(3)$ -invariant and  $\lambda_3$  term selects out  $\Sigma(36)$  subgroup.

- The model is extremely constrained  $\rightarrow$  numerous relations among scalar masses and couplings.
- Many features remain even if  $\Sigma(36)$  is softly broken [Varzielas, Ivanov, Levy, 2107.08227].

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# Σ(36) 3HDM

[Ivanov, Nishi, 1410.6139]: up to cyclic permutations, the global minimum can only be at

A: 
$$
(\omega, 1, 1)
$$
, A':  $(\omega^2, 1, 1)$ , B:  $(1, 0, 0)$ ,  
C:  $(1, 1, 1)$ ,  $(1, \omega, \omega^2)$ ,  $(1, \omega^2, \omega)$ .

Notation: for example,  $(1, 1, 1)$  denotes the case  $v_1 = v_2 = v_3$ , that is

$$
\left(\langle \phi_1^0 \rangle, \, \langle \phi_2^0 \rangle, \, \langle \phi_3^0 \rangle \right) = \frac{\nu}{\sqrt{6}} \left( 1, \, 1, \, 1 \right).
$$

- In each case, there are  $6$  degenerate global minima:  $A+A'$  or  $B+C.$
- But if we study phase transitions, we want to know:
	- $\triangleright$  Can we have local minima? Can we have CB minima?
	- $\triangleright$  Can we have CB saddle points which would separate neutral minima?
	- ▶ In 2HDM, CB domain walls were recently studied in [Sassi, Moortgat-Pick, 2309.12398] and
	- $\triangleright$  See also [Fu et al, 2409.16359] for non-abelian domain walls and GW signals.

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	- ▶ See also [Fu et al, 2409.16359] for non-abelian domain walls and GW signals.

# Exact  $\Sigma$ (36)



In Yang, Ivanov, arXiv:2401.03264, we find an extremely rich picture, with 69 or 78 extrema in total. Color encodes neutral (black) and charge-breaking extrema (shades of red). Note: for  $\lambda_3 > 2$ , the deepest saddle point is charge-breaking.

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## Softly broken Σ(36)



Adding  $\mathbb{Z}_3$ -preserving soft breaking terms:  $m_{ii}^2(\phi_i^{\dagger} \phi_i)$  with  $m_{11}^2 + m_{22}^2 + m_{33}^2 = 0$ . Parametrizing them via

$$
\mu_1 = \frac{1}{\sqrt{2}} \frac{m_{11}^2 - m_{22}^2}{m^2} \,, \quad \mu_2 = \frac{\sqrt{6}}{2} \frac{m_{33}^2}{m^2} \,.
$$

Coexistence of local and global minima on the plane of soft breaking parameters  $(\mu_1, \mu_2)$ . Also shown: T evolution in benchmark model 1 and benchmark model 2.

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## Softly broken  $\Sigma(36)$  3HDM: benchmark 1



- Used the same simple tree-level thermal evolution with  $m_{ii}^2(T) = m_{ii}^2 + c_i T^2$ .
- A clear example of a deepest CB saddle point.
- The red dashed line indicates an approximate nucleation temperature (criterion: equal depth differences).
- **These features should survive in an accurate** numerical study.

### Softly broken  $\Sigma(36)$  3HDM: benchmark 2



- **•** Here, we have several saddle points, either neutral or charge-breaking, which closely follow each other.
- Which bounce trajectory corresponds to the most probable bubble nucleation? Impossible to answer with this simplistic analysis!

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## Softly broken  $\Sigma(36)$  3HDM: benchmark 2



- **•** Here, we have several saddle points, either neutral or charge-breaking, which closely follow each other.
- Which bounce trajectory corresponds to the most probable bubble nucleation? Impossible to answer with this simplistic analysis!
- **If several saddle points compete, it may happen** than bubbles of the same true and the same false vacua but completely different bubble wall profiles emerge in the Universe. How do they merge? What GW signatures are expected?
- A dedicated numerical study is required!

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- Rich phase transition dynamics in multi-Higgs models around the EW scale!
- $\bullet$  Intermediate charge-breaking phases at finite T or charge-breaking bubble walls between neutral vacua are possible within 2HDM and become more intriguing in the 3HDM.
- Within the 3HDM, competing minima and saddle points are ubiquitous and may lead to highly non-trivial bubble nucleation and coalescence dynamics.
- What happens to fermions during evolution through a CB phase or upon the passage of a CB bubble wall? Any consequences for baryogenesis?

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