

# Exploring the perspectives of superconducting materials in SRF for quantum sensing

*Enrico Silva*

INFN/University Roma Tre  
enrico.silva@uniroma3.it



*A. Alimenti, G. Mota, A. Magalotti, N. Pompeo, K. Torokhtii, P. Vidal Garcia*



*M. Bertucci, E. Chyhyrynets, D. Di Gioacchino,  
C. Gatti, G. Ghigo, D. Torsello, C. Pira (P.I.)*



*G. Celentano, A. Mancini,  
A. Masi, A. Vannozzi*



*S. Posen*

**SAMARA**

Superconducting Alternative Materials  
for Accelerating cavities and haloscope  
Resonators for Axions

PRIN  
IRONMOON



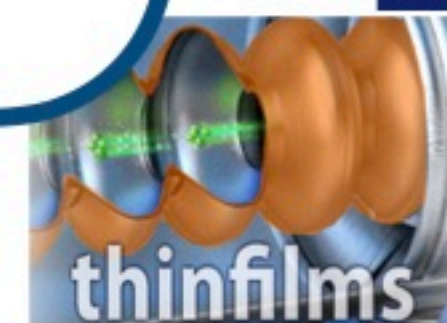
ADDENDUM  
FCC-GOV-CC-0218  
(KE5084/ATS)



*V. Braccini, E. Bellingeri, A.  
Leveratto, F. Loria*



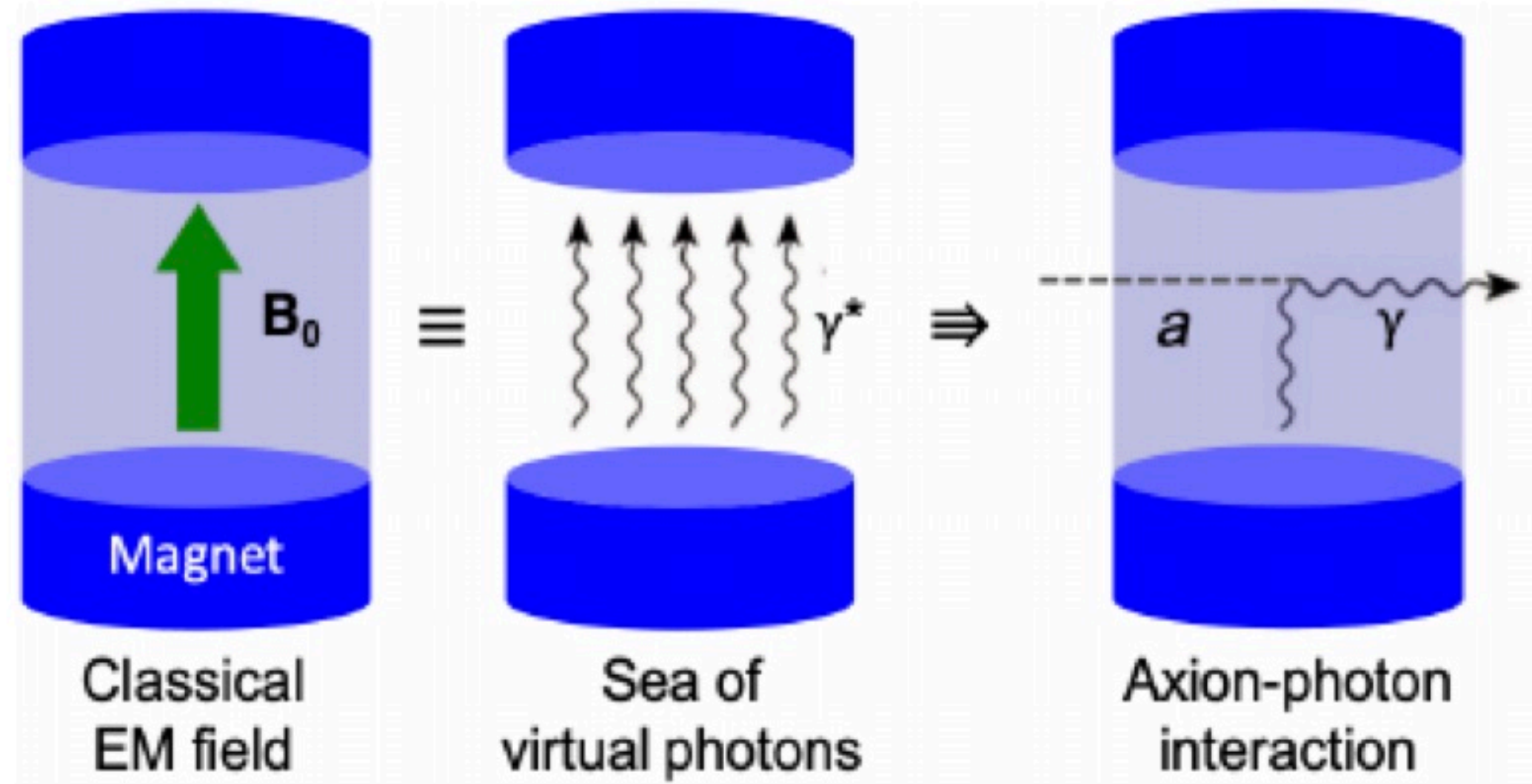
*M. Putti*



- Motivation: Search for axions → Haloscopes
- Cavity haloscopes → surface impedance in dc magnetic fields → the problem(s)
- Surface impedance in superconductors in dc fields: vortex motion, geometric effect, nontrivial role of  $\lambda$  (and deconstruction of “well known” rules of thumb)
- Experimental technique: two-tone dielectric loaded resonator
- Results: NbTi, a case study. Fe(Se,Te). YBCO. (Nb<sub>3</sub>Sn)
- Perspective superconductors for Haloscopes
- Summary

# Search for axions: microwave Haloscopes (High-Q cavities)

Inverse Primakov effect  $\mathcal{L}_{a\gamma\gamma} = -g_{a\gamma\gamma} a \vec{E}_{rf} \cdot \vec{B}$



$$P_{a \rightarrow \gamma\gamma} \propto \left( B^2 c_{nl} V \frac{Q_{nm} Q_a}{Q_{nm} + Q_a} \right) (g_{a\gamma\gamma}^2)$$

Figure of merit:  
 **$Q \cdot B^2$**

- High Q resonant cavities
- Axion mass
- in high magnetic fields  $B$
- low  $T$  ( $\sim 0.1 \div 1$  K)
- large, curved surfaces

- **Superconductor**
- **microwaves**
- **vortex motion!**
- **any superconductor**
- **deposition issues**

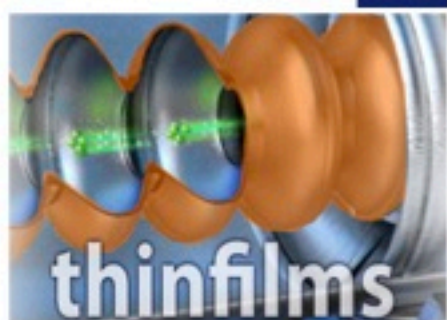


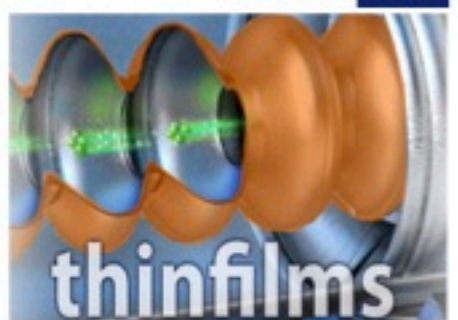
Figure of merit:  
 $Q \cdot B^2$

$$Q \propto \frac{1}{R_s}$$

Surface resistance

- High Q resonant cavities
- Axion mass
- in high magnetic fields  $B$
- low  $T$  ( $\sim 0.1 \div 1$  K)
- large, curved surfaces

- **Superconductor**
- **microwaves**
- **vortex motion!**
- **any superconductor**
- **deposition issues**



# High-Q cavities: low surface resistance

Figure of merit:  
 $Q \cdot B^2$

$$Q \propto \frac{1}{R_s}$$

Surface resistance

- High Q resonant cavities
- Axion mass
- in high magnetic fields  $B$
- low  $T$  ( $\sim 0.1 \div 1$  K)
- large, curved surfaces

geometry  $B - J_{mw}$

vortex motion

$R_s$

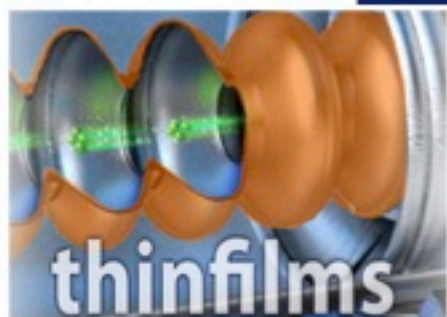
quasiparticle  
conductivity

impurities

London  
penetration  
depth

beware!

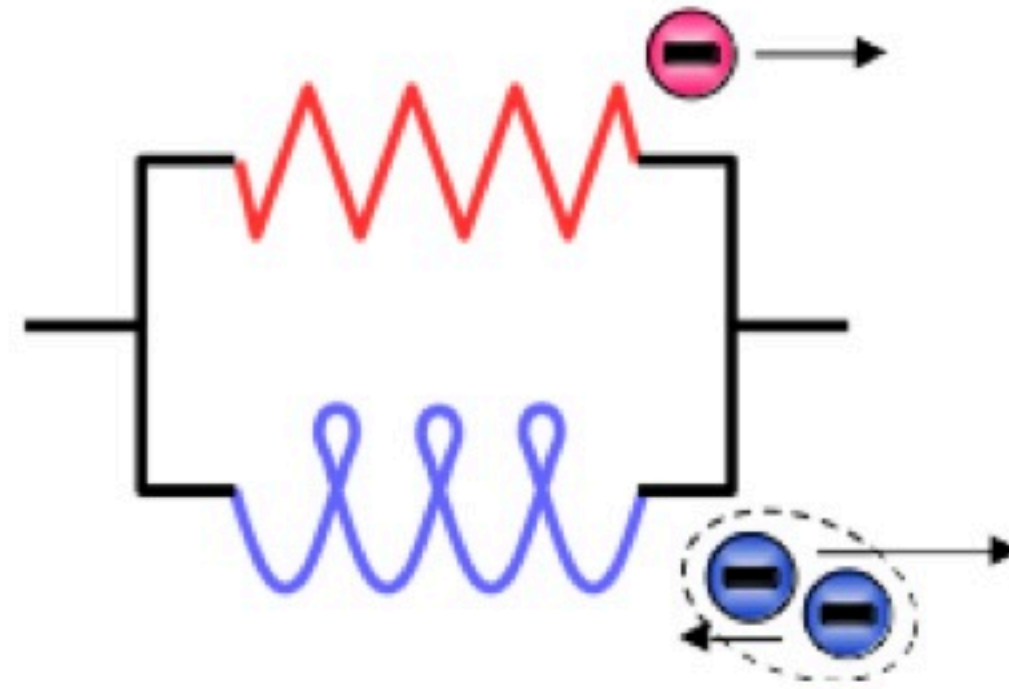
- **Superconductor**
- **microwaves**
- **vortex motion!**
- **any superconductor**
- **deposition issues**



# Surface impedance in a dc magnetic field

$$Z_s = \frac{E_{//}}{H_{//}} = R_s + iX_s = Z_s(\sigma_2 fl, \rho_v, R_{res})$$

Two fluid conductivity



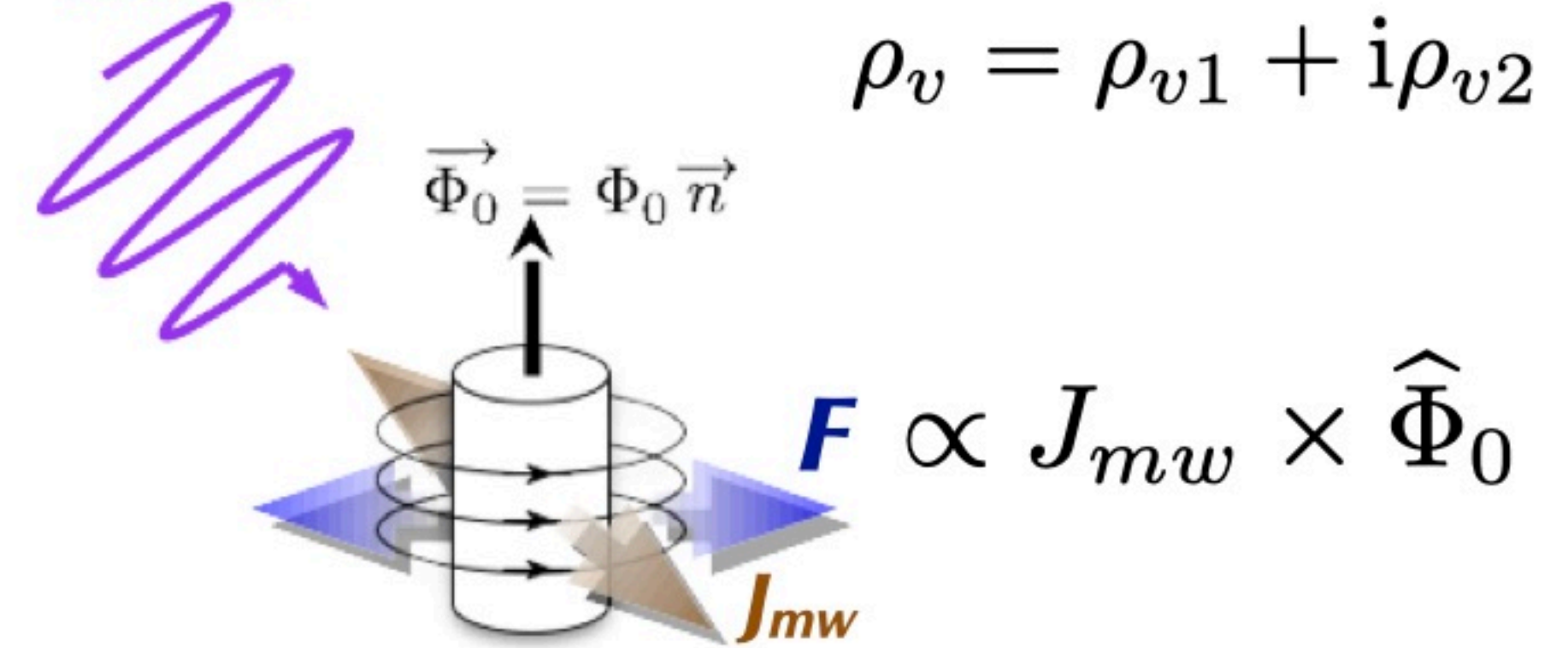
$$\sigma_1 - i\sigma_2 = \frac{n_n e^2 \tau}{m} - i \frac{1}{\omega \mu_0 \lambda^2}$$



All quantities depend on  $B$

vortex motion resistivity

microwave  
e.m. field



$$\rho_v = \rho_{v1} + i\rho_{v2}$$

$$\tilde{\rho} = \frac{\rho_v + i \frac{1}{\sigma_2}}{1 + i \frac{\sigma_1}{\sigma_2}}$$

Coffey, Clem *PRL* 67 (1991)

$$\omega = 2\pi\nu$$

# Surface impedance in a dc magnetic field

$$Z_s = \sqrt{i \frac{\omega \mu_0}{\sigma}} = \sqrt{i \omega \mu_0 \tilde{\rho}}$$

$$\tilde{\rho} = \frac{\rho_v + i \frac{1}{\sigma_2}}{1 + i \frac{\sigma_1}{\sigma_2}}$$

$$\sigma_1 - i\sigma_2 = \frac{n_n e^2 \tau}{m} - i \frac{1}{\omega \mu_0 \lambda^2}$$

$$\rho_v = \rho_{v1} + i\rho_{v2}$$

vortex motion resistivity,  
“the new actor in town”

# Surface impedance in a dc magnetic field

$$Z_s = \sqrt{i \frac{\omega \mu_0}{\sigma}} = \sqrt{i \omega \mu_0 \tilde{\rho}}$$

$$\tilde{\rho} = \frac{\rho_v + i \frac{1}{\sigma_2}}{1 + i \frac{\sigma_1}{\sigma_2}}$$

$$\sigma_1 - i\sigma_2 = \frac{n_n e^2 \tau}{m} - i \frac{1}{\omega \mu_0 \lambda^2}$$

$$\rho_v = \rho_{v1} + i\rho_{v2}$$

vortex motion resistivity,  
“the new actor in town”

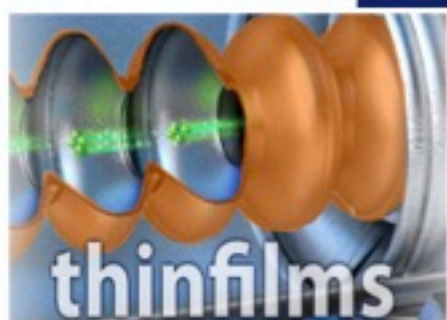
## Deconstruction of “well known” rules of thumb

Assume to be far from the transition line:  $T \ll T_c \rightarrow R_s \simeq \frac{\Re[\tilde{\rho}]}{2\lambda}$

### Zero field, B=0

$$Z_s \simeq \frac{1}{2} \sigma_1 \omega^2 \mu_0^2 \lambda^3 + i \omega \mu_0 \lambda$$

$$R_s \simeq \frac{1}{2} \sigma_1 \omega^2 \mu_0^2 \lambda^3 (+R_{res})$$





# Surface impedance in a dc magnetic field

$$Z_s = \sqrt{i \frac{\omega \mu_0}{\sigma}} = \sqrt{i \omega \mu_0 \tilde{\rho}}$$

$$\tilde{\rho} = \frac{\rho_v + i \frac{1}{\sigma_2}}{1 + i \frac{\sigma_1}{\sigma_2}}$$

$$\sigma_1 - i\sigma_2 = \frac{n_n e^2 \tau}{m} - i \frac{1}{\omega \mu_0 \lambda^2}$$

$$\rho_v = \rho_{v1} + i\rho_{v2}$$

vortex motion resistivity,  
“the new actor in town”

$\rho_{v1}$  dominant at even few mT

## Deconstruction of “well known” rules of thumb

Assume to be far from the transition line:  $T \ll T_c$   
 $B \ll B_{c2} \rightarrow R_s \simeq \frac{\Re[\tilde{\rho}]}{2\lambda}$

### Zero field, B=0

$$Z_s \simeq \frac{1}{2} \sigma_1 \omega^2 \mu_0^2 \lambda^3 + i\omega \mu_0 \lambda$$

$$R_s \simeq \frac{1}{2} \sigma_1 \omega^2 \mu_0^2 \lambda^3 (+R_{res})$$

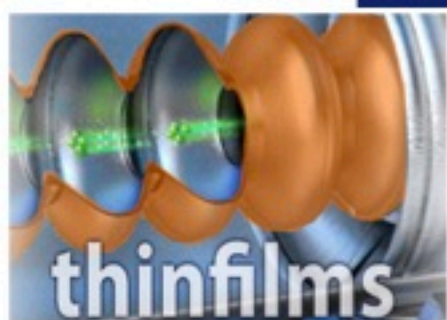
### Mixed state, B≠0

$$Z_s \simeq \frac{1}{2\lambda} \rho_v(\omega, B, T) + i\omega \mu_0 \lambda$$

$$R_s \simeq \frac{1}{2\lambda} \rho_{v1}(\omega, B, T)$$

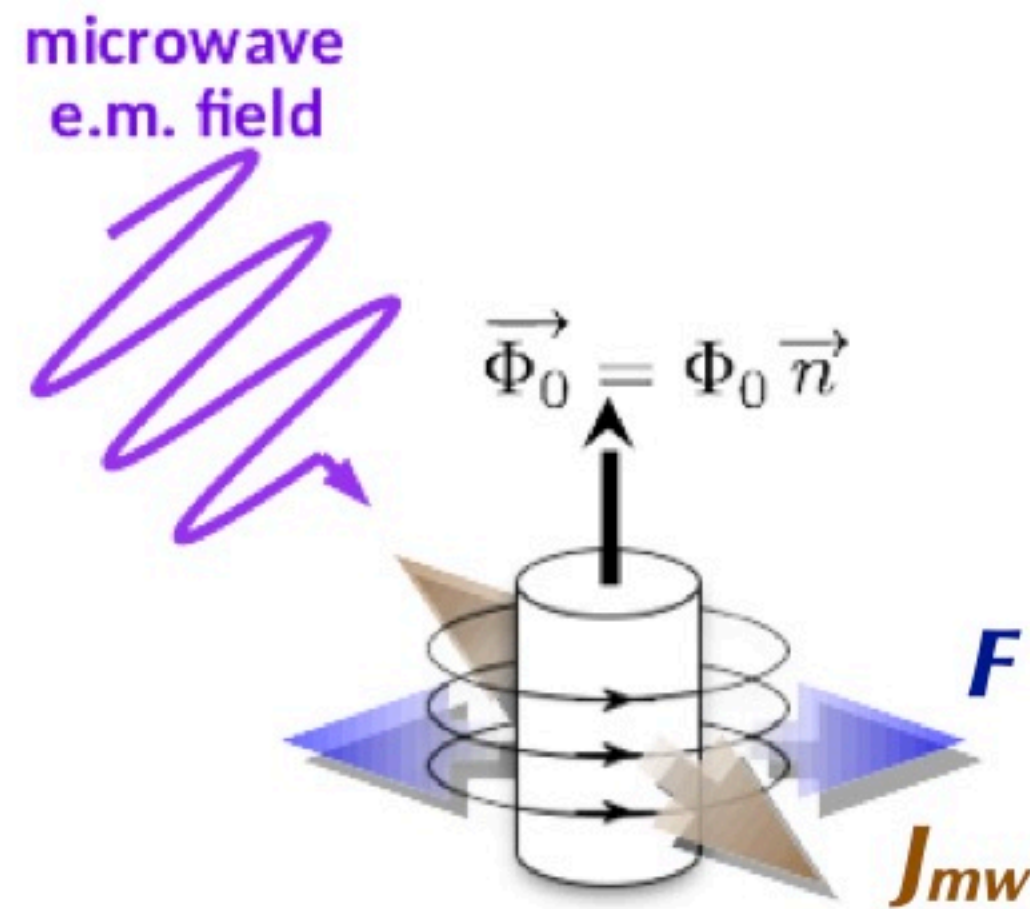
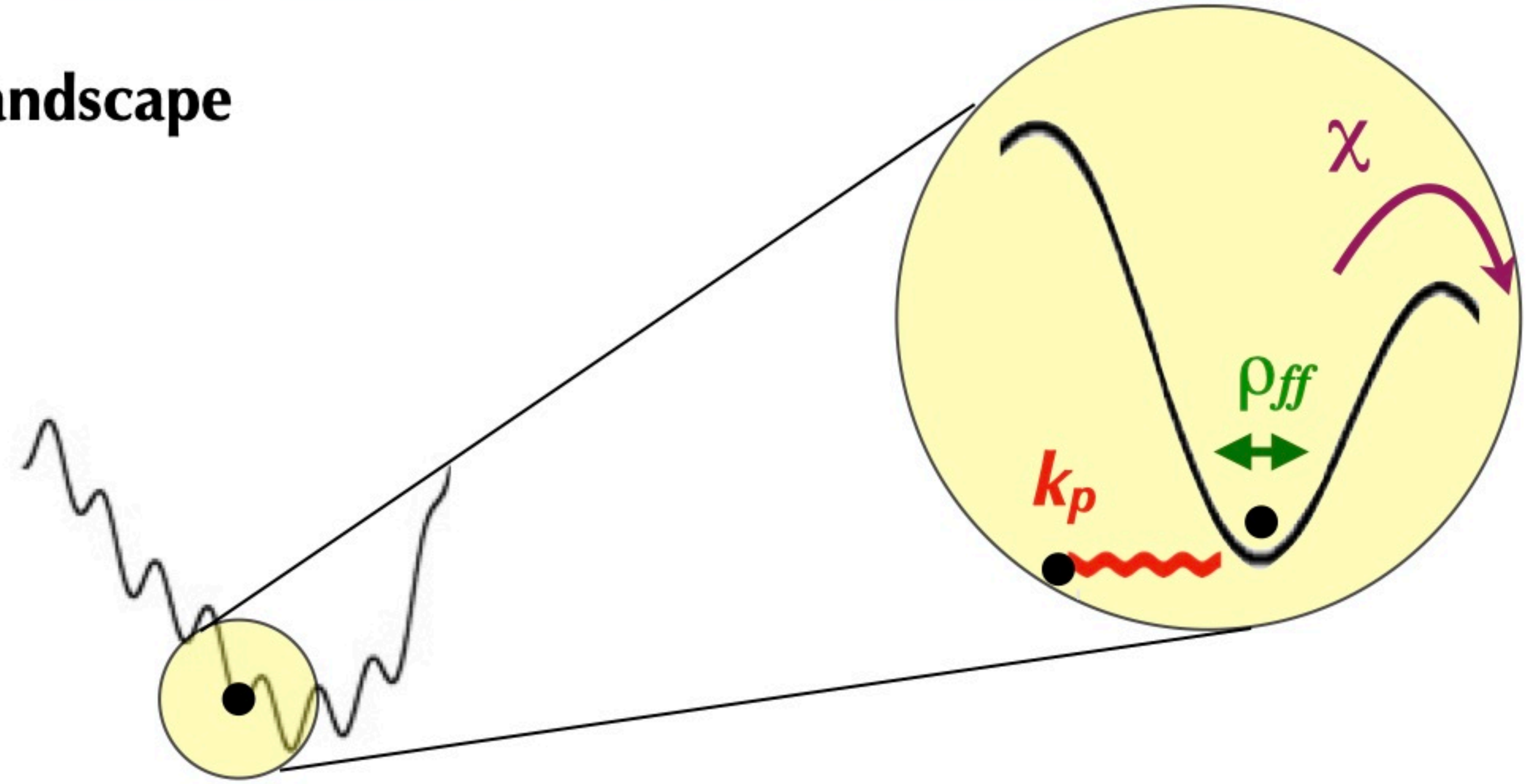
- No  $R_s \propto \omega^2$  dependence
- $\lambda$  large  $\rightarrow$  decreases  $R_s$
- $R_{res}$  irrelevant

physics of vortex motion resistivity required



# Microwave vortex complex resistivity

- vortex ↔ particle in a pinning potential landscape subjected to the Lorentz force
- Tiny vortex oscillations (< 1nm)
- Local pinning potential
- Quasi-equilibrium vortex matter



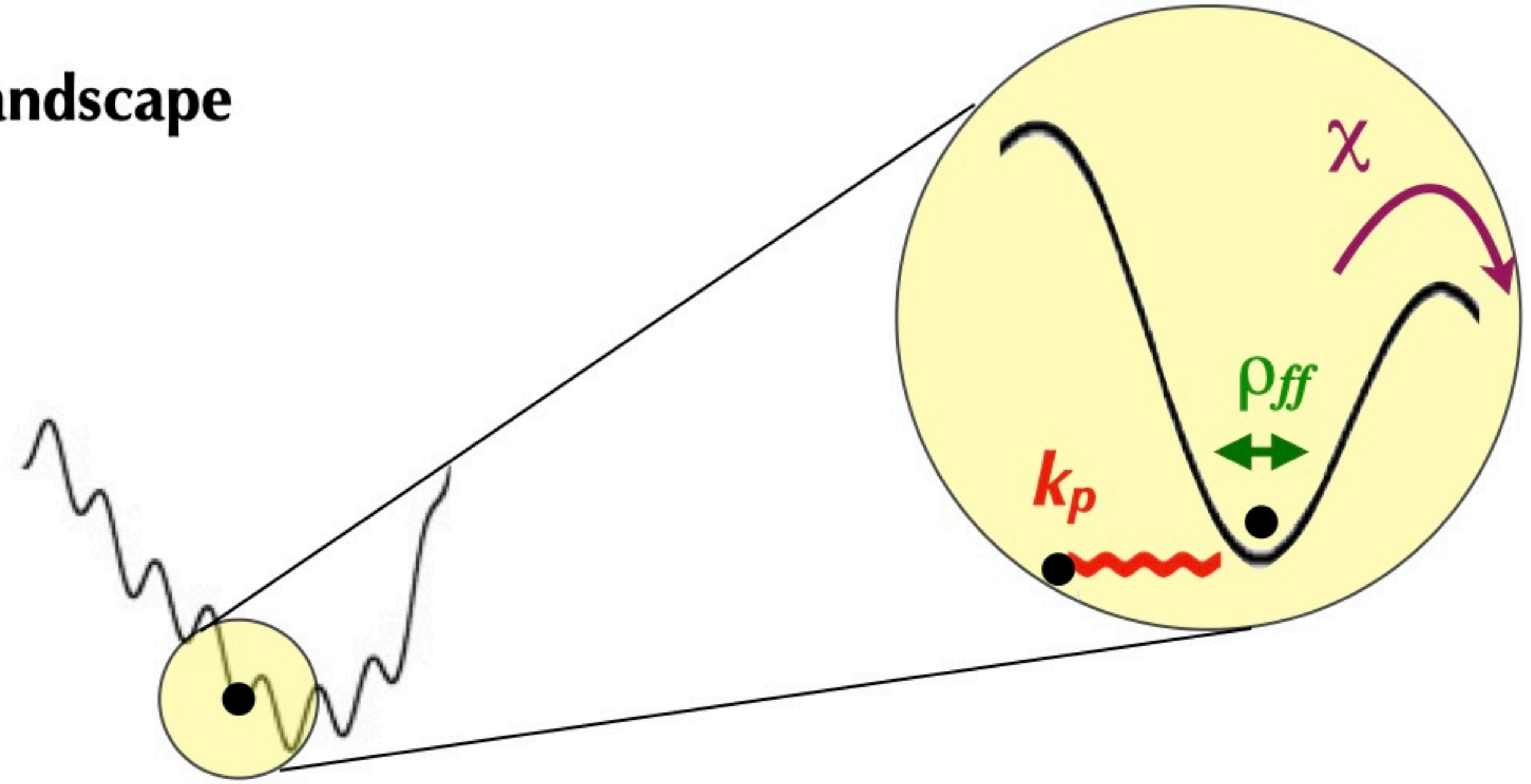
$$\rho_{v1}(H) + i\rho_{v2}(H) = \rho_{ff} \frac{\chi + i\frac{\nu}{\nu_0}}{1 + i\frac{\nu}{\nu_0}}$$

Gittleman, Rosenblum *PRL* **16** (1966); Coffey, Clem *PRL* **67** (1991); Brandt *PRL* **67** (1991); Placais et al, *PRB* **54** (1996); N. Pompeo, E.Silva *PRB* **78** 094503 (2008); E.Silva, N. Pompeo, O. Dobrovolskiy, *Phys. Sci. Rev.* **2** 20178004 (2017) - overview



# Microwave vortex complex resistivity

- vortex  $\leftrightarrow$  particle in a pinning potential landscape subjected to the Lorentz force
- Tiny vortex oscillations ( $< 1\text{nm}$ )
- Local pinning potential
- Quasi-equilibrium vortex matter



flux-flow resistivity  $\rho_{ff}$ ,  
 pinning constant  $k_p$ ,  
 crossover frequency  $\nu_0$   
 creep factor  $\chi$ .  
 (low  $T$ :  $\chi = 0$ )

$$\rho_{v1}(H) + i\rho_{v2}(H) = \rho_{ff} \frac{\chi + i\frac{\nu}{\nu_0}}{1 + i\frac{\nu}{\nu_0}}$$

$k_p \oplus \rho_{ff} \oplus \chi$

Gittleman, Rosenblum *PRL* **16** (1966); Coffey, Clem *PRL* **67** (1991); Brandt *PRL* **67** (1991); Placais et al, *PRB* **54** (1996); N. Pompeo, E.Silva *PRB* **78** 094503 (2008); E.Silva, N. Pompeo, O. Dobrovolskiy, *Phys. Sci. Rev.* **2** 20178004 (2017) - overview



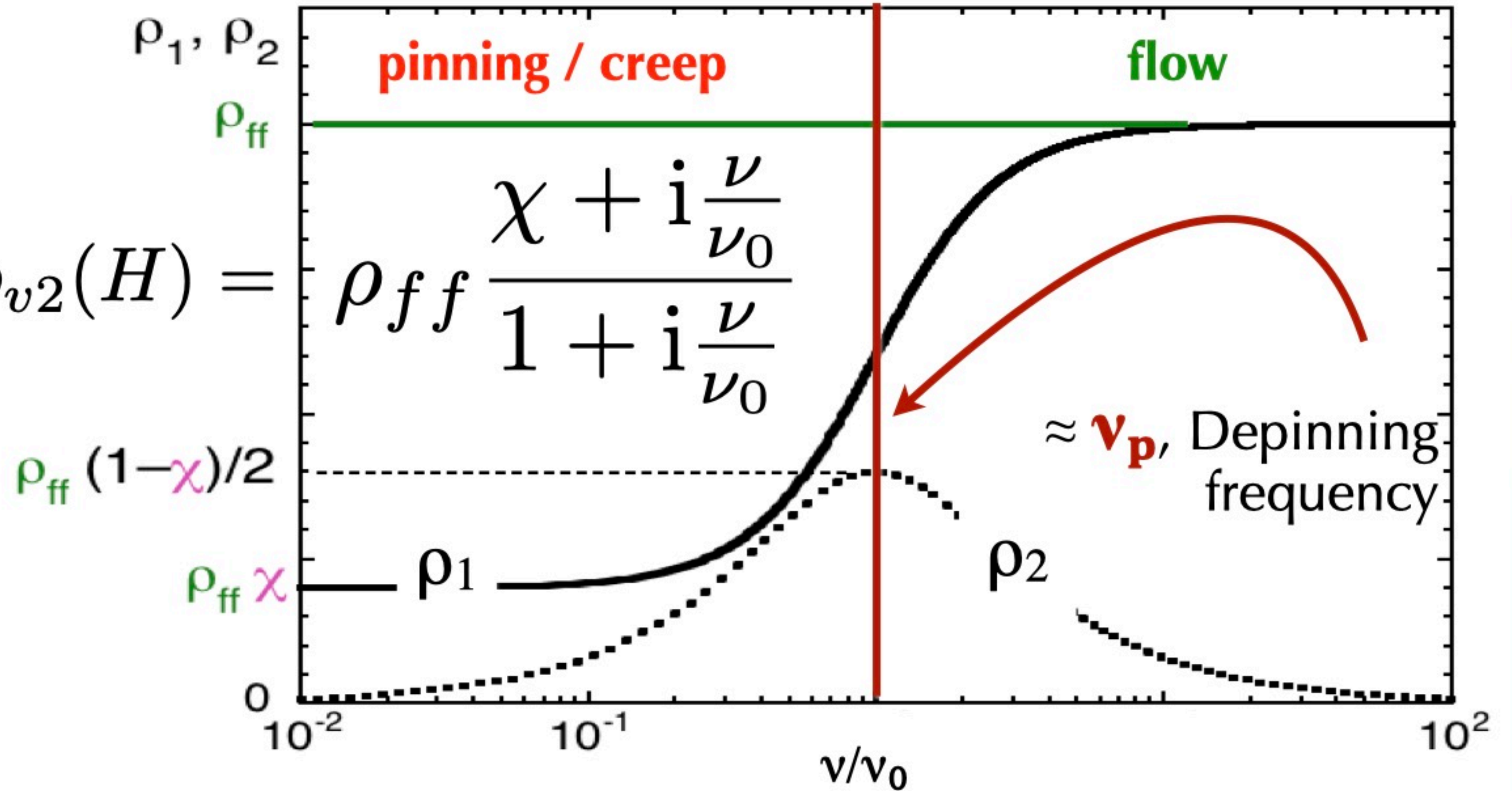
# Microwave vortex complex resistivity

$\nu_0 \approx \nu_p$ , Depinning frequency.  
Figure of merit for applications

$$\rho_{v1}(H) + i\rho_{v2}(H) =$$

$$\rho_{ff} \frac{\chi + i \frac{\nu}{\nu_0}}{1 + i \frac{\nu}{\nu_0}}$$

**flux-flow resistivity**  $\rho_{ff}$   
**pinning constant**  $k_p$   
**crossover frequency**  $\nu_0$   
**creep factor**  $\chi$   
(low  $T$ :  $\chi = 0$ )



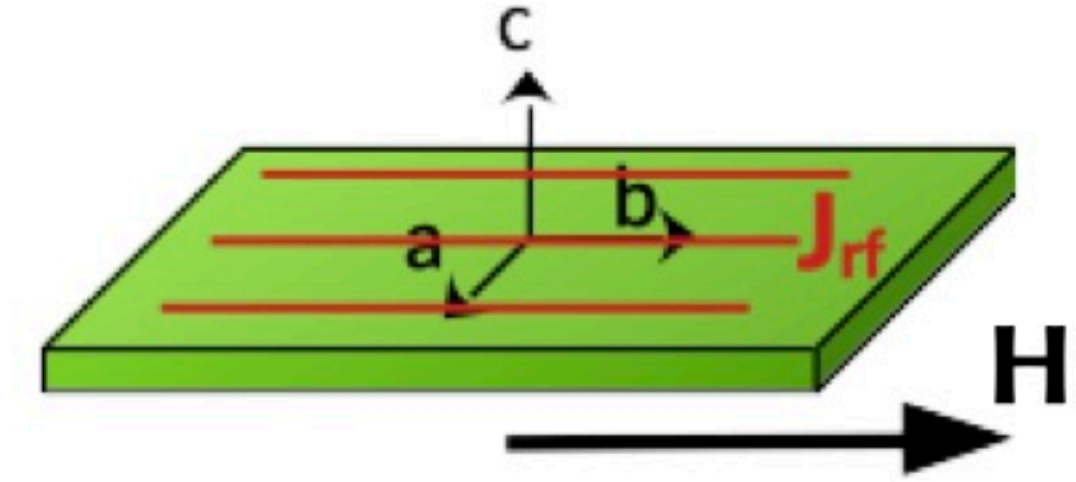
Gittleman, Rosenblum *PRL* **16** (1966); Coffey, Clem *PRL* **67** (1991); Brandt *PRL* **67** (1991); Placais et al, *PRB* **54** (1996);  
N. Pompeo, E.Silva *PRB* **78** 094503 (2008); E.Silva, N. Pompeo, O. Dobrovolskiy, *Phys. Sci. Rev.* **2** 20178004 (2017) - overview



# Geometry: fluxons are flexible!

Force on fluxons:  $F \propto J_{mw} \times \hat{\Phi}_0$

Ideal haloscope configuration:  $J_{mw} // \hat{\Phi}_0 \Rightarrow \rho_v = 0$



Flexible fluxons:



a contribution always exists, and depends on:

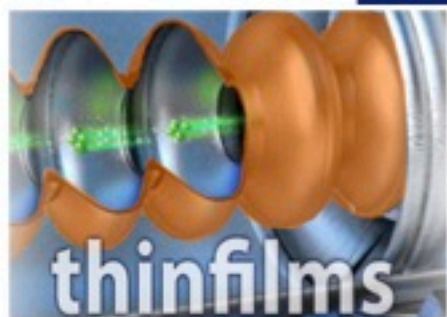
- kind of pinning (point, linear...)
- temperature
- material anisotropy (anisotropic materials  $\rightarrow$  more flexible fluxons)
- fluxon stiffness (coherence length, penetration depth)

$$\rho_v = c_{ff} \rho_{ff} \frac{\chi + i \frac{\nu}{\nu_0}}{1 + i \frac{\nu}{\nu_0}}$$

$c_{ff}$ : alignment factor

$c_{ff} = 0$ : ideal force-free configuration

$c_{ff} = 1$ :  $J_{mw} \perp H$



# To predict the performances of a superconductor...

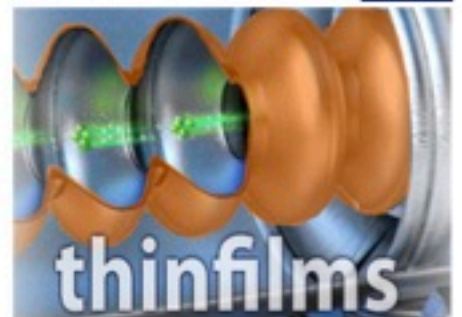
$$\begin{array}{l}
 T \ll T_c \\
 B \ll B_{c2}
 \end{array}
 \quad
 R_s \simeq \frac{1}{2} \underbrace{c_{ff}}_{\text{yellow}} \underbrace{\rho_{ff}}_{\text{green}} \frac{1}{1 + \underbrace{(\nu_0/\nu)^2}_{\text{green}}} \frac{1}{\underbrace{\lambda}_{\text{red}}}$$

theoretical evaluations: only oversimplified models, many material parameters.  
Measure?

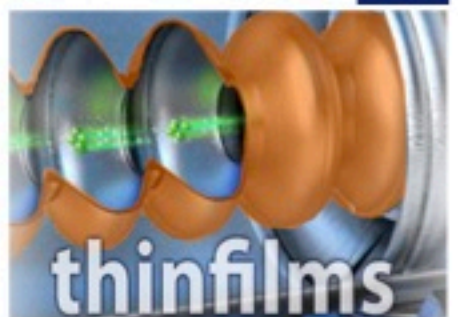
can be measured with  $H \perp J_{mw}$

can be measured/taken from literature

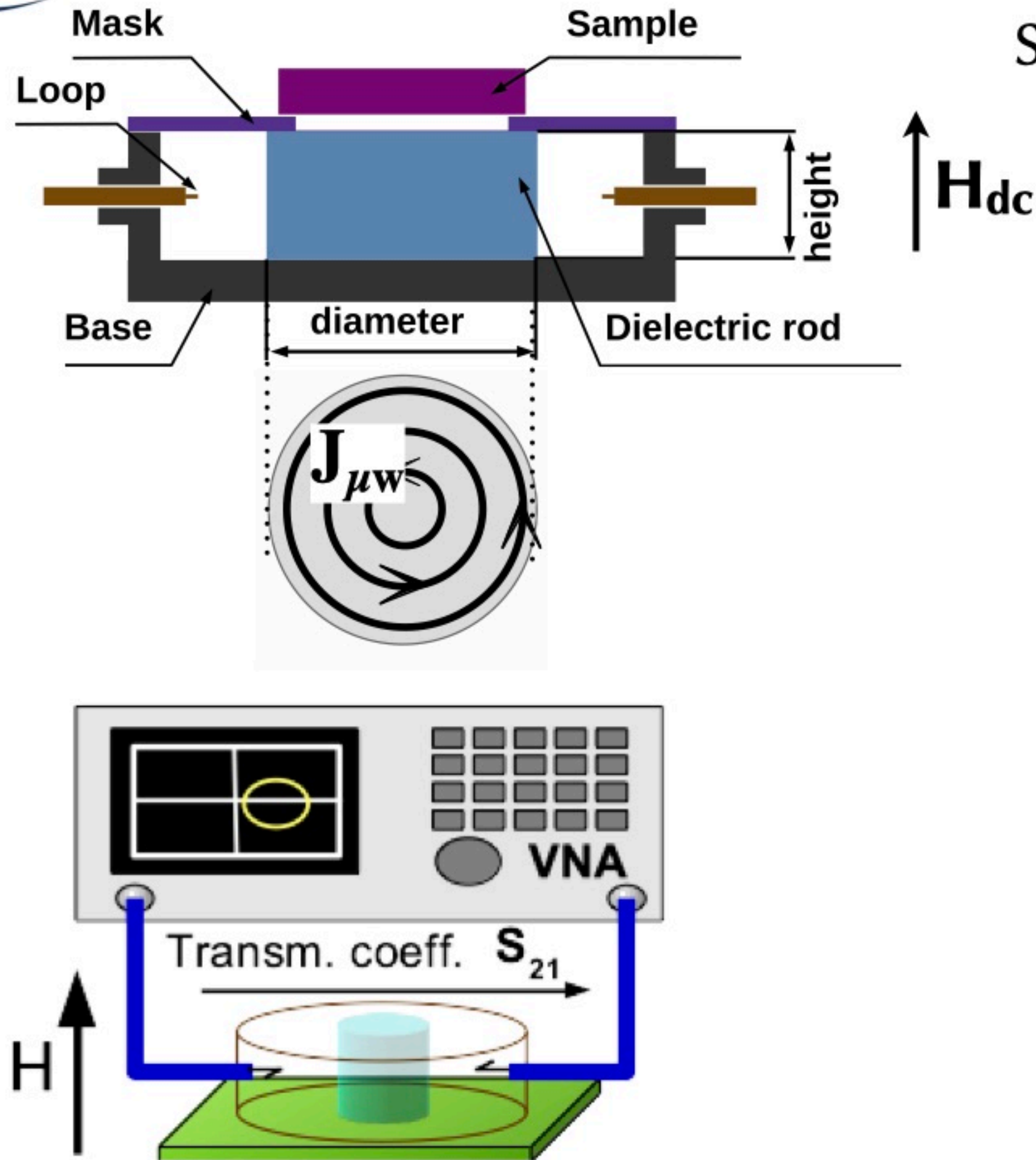
Note: formula is a limiting expression. Calculations were made with the full expressions



## Technique: measuring the surface impedance whence the vortex motion parameters



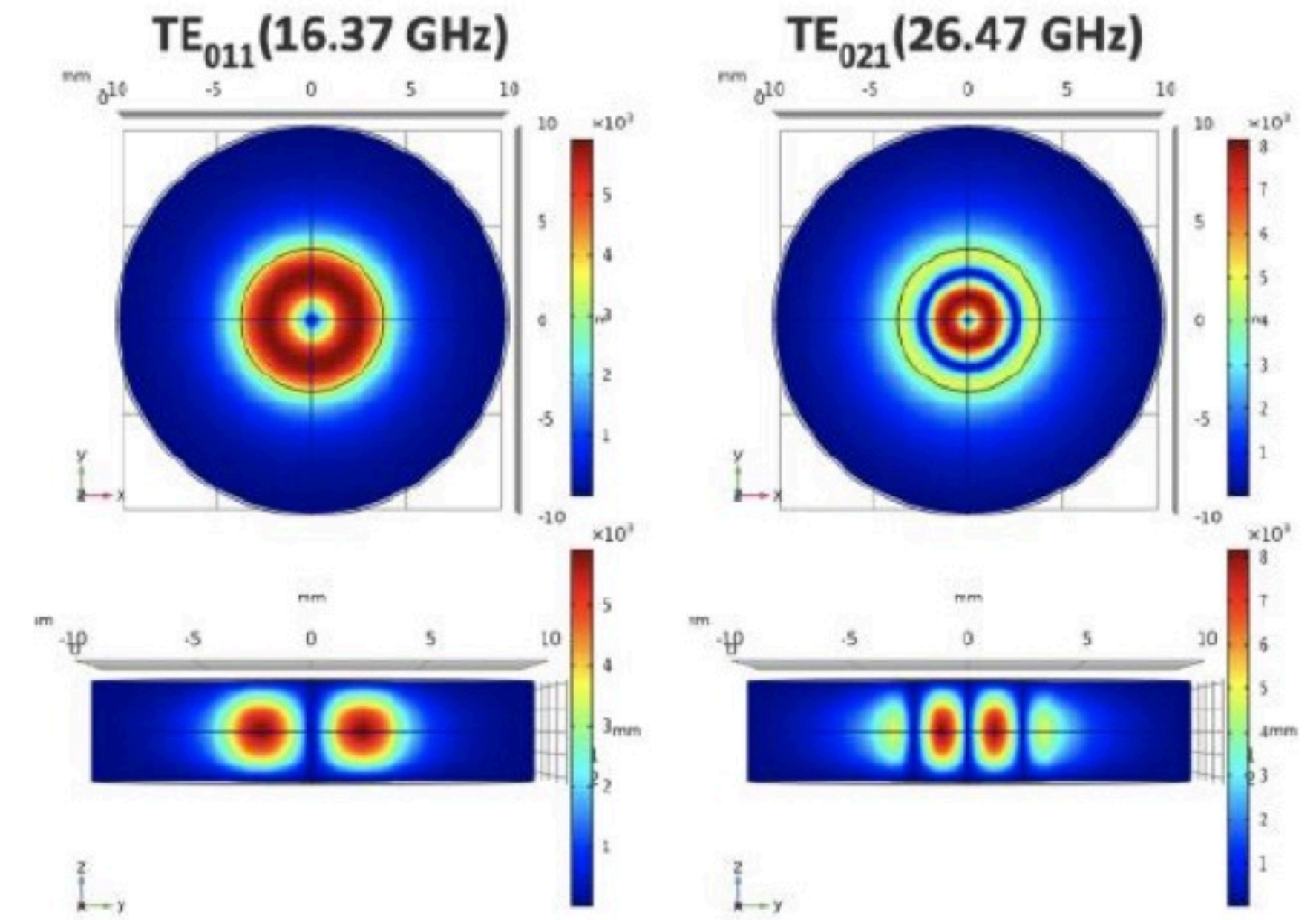
# Microwave technique: dielectric loaded resonator



Sapphire loaded resonator

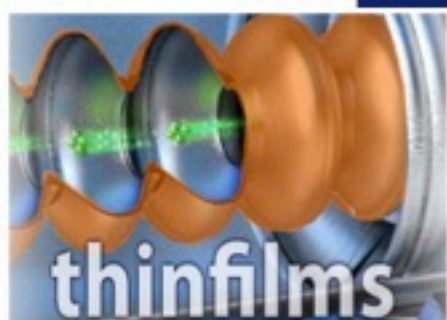


Probing area  
 $\varnothing \leq 20$  mm



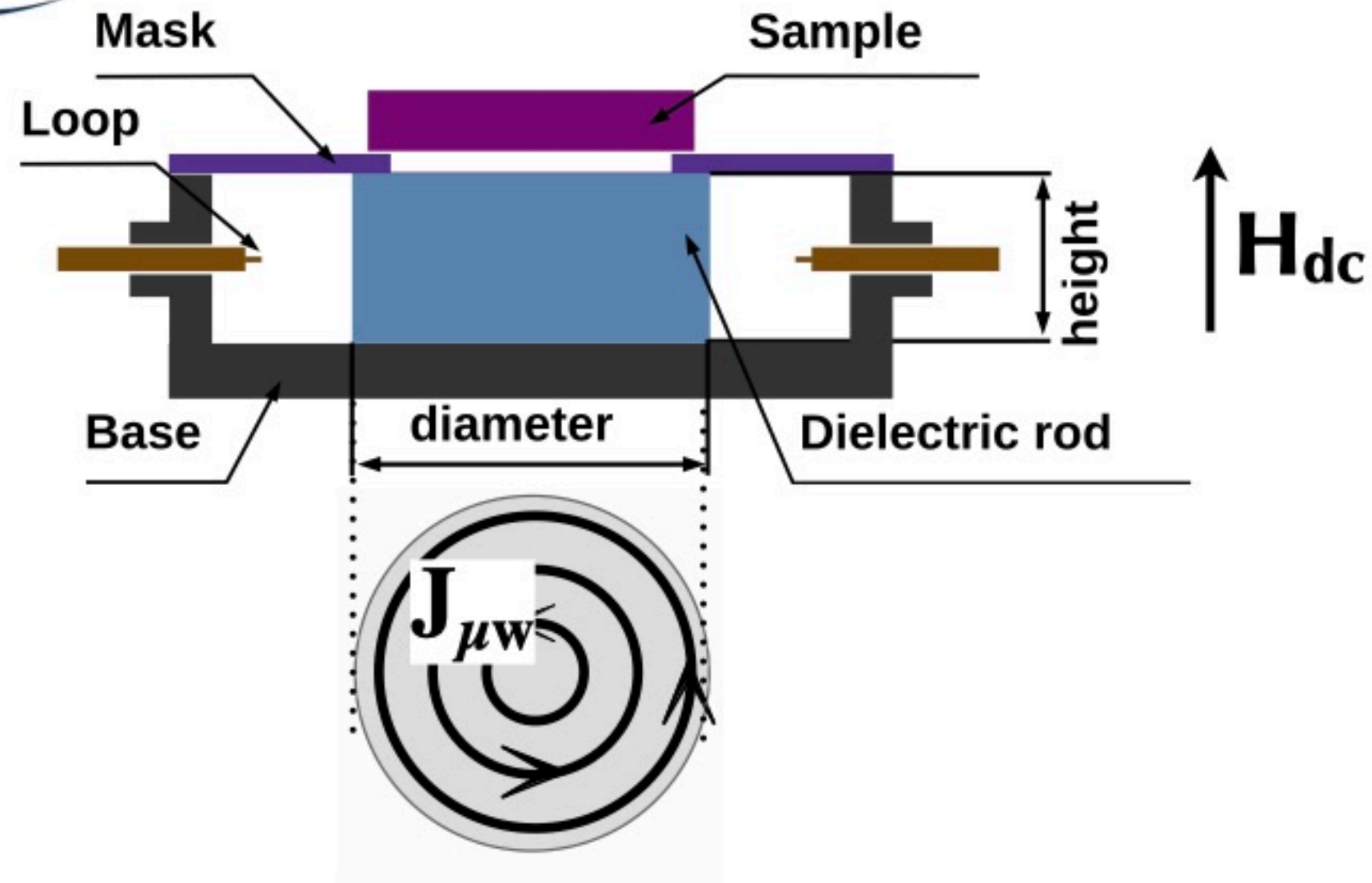
K. Torokhtii et al J. Phys.: Conf. Ser. 1065 052027 2018  
A. Alimenti et al., Meas. Sci. Technol., 30 065601 2019

N. Pompeo et al., Measurement 184 109937 2021  
A. Alimenti et al., IEEE Instrum. Meas. Magazine 24 12 2021



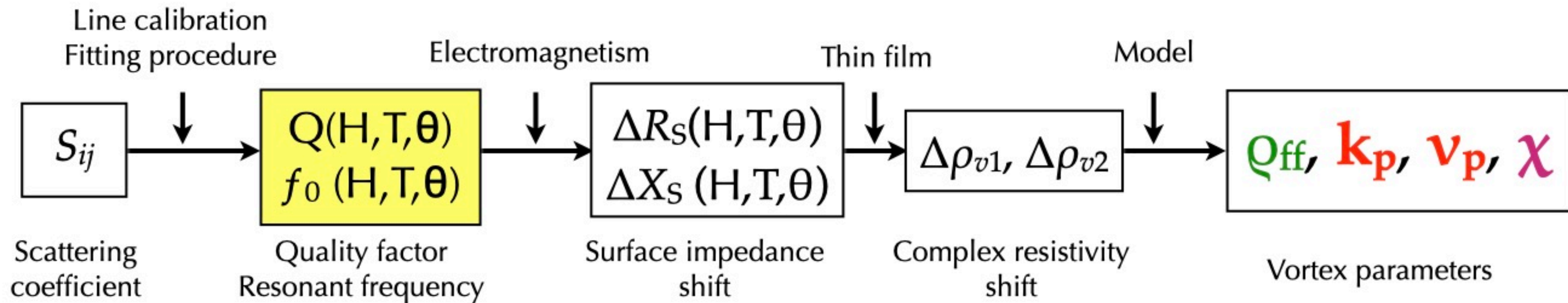
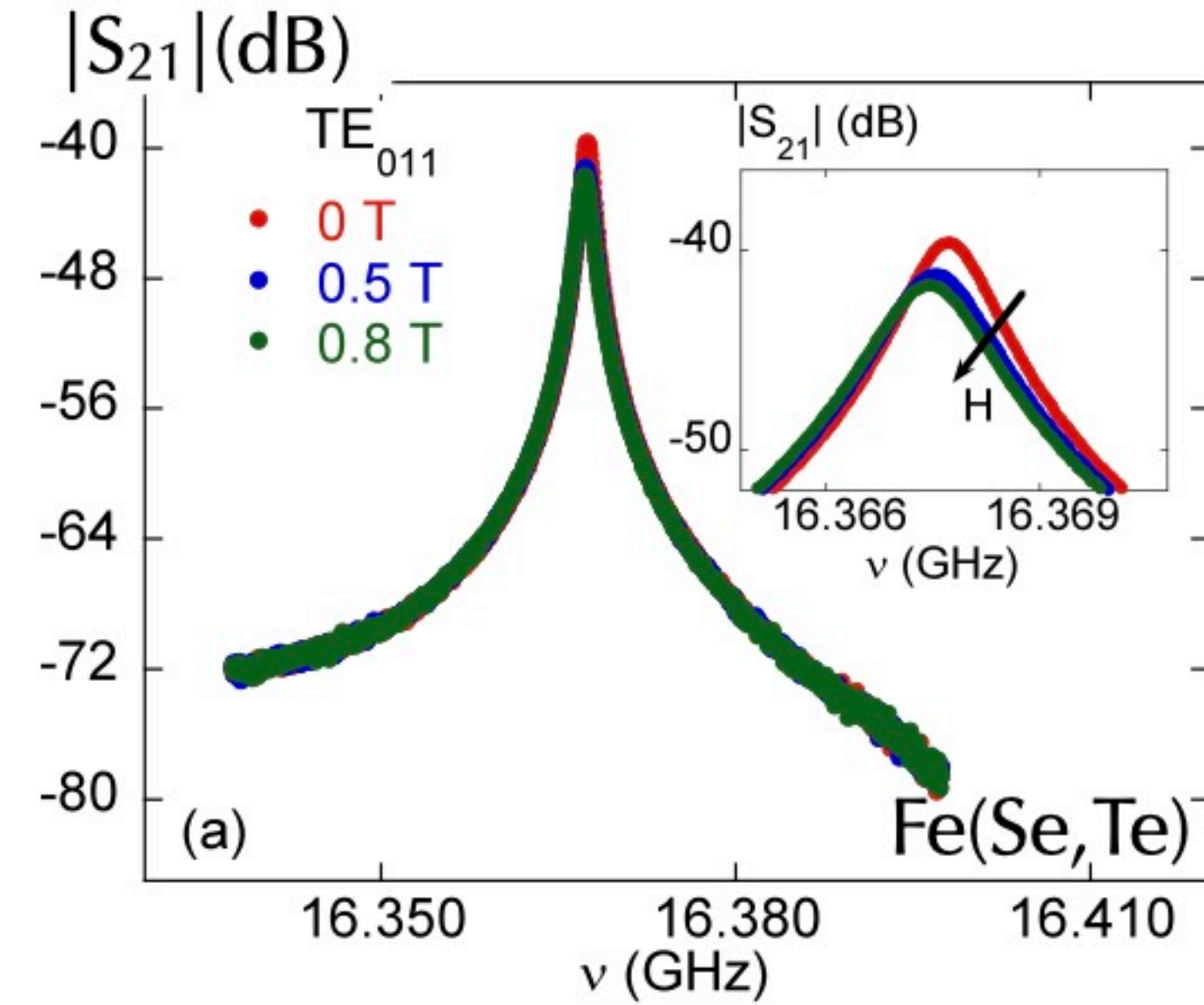


# Microwave technique: dielectric loaded resonator



$\mu_0 H \leq 12 \text{ T}$   
 $T \geq 4 \text{ K}$   
 variable angle  
 (up to 1.2 T)  
 Dual frequency  
 14/24 GHz  
 16/27 GHz

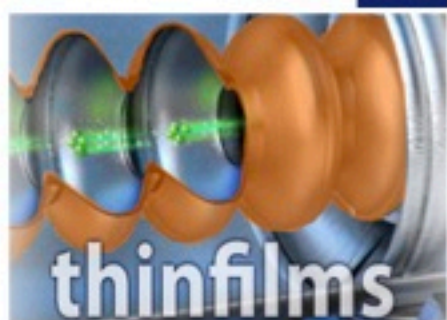
Sapphire loaded resonator



See Pablo Vidal García  
 Tue, 12:41

K. Torokhtii et al J. Phys.: Conf. Ser. 1065 052027 2018  
 A. Alimenti et al., Meas. Sci. Technol., 30 065601 2019

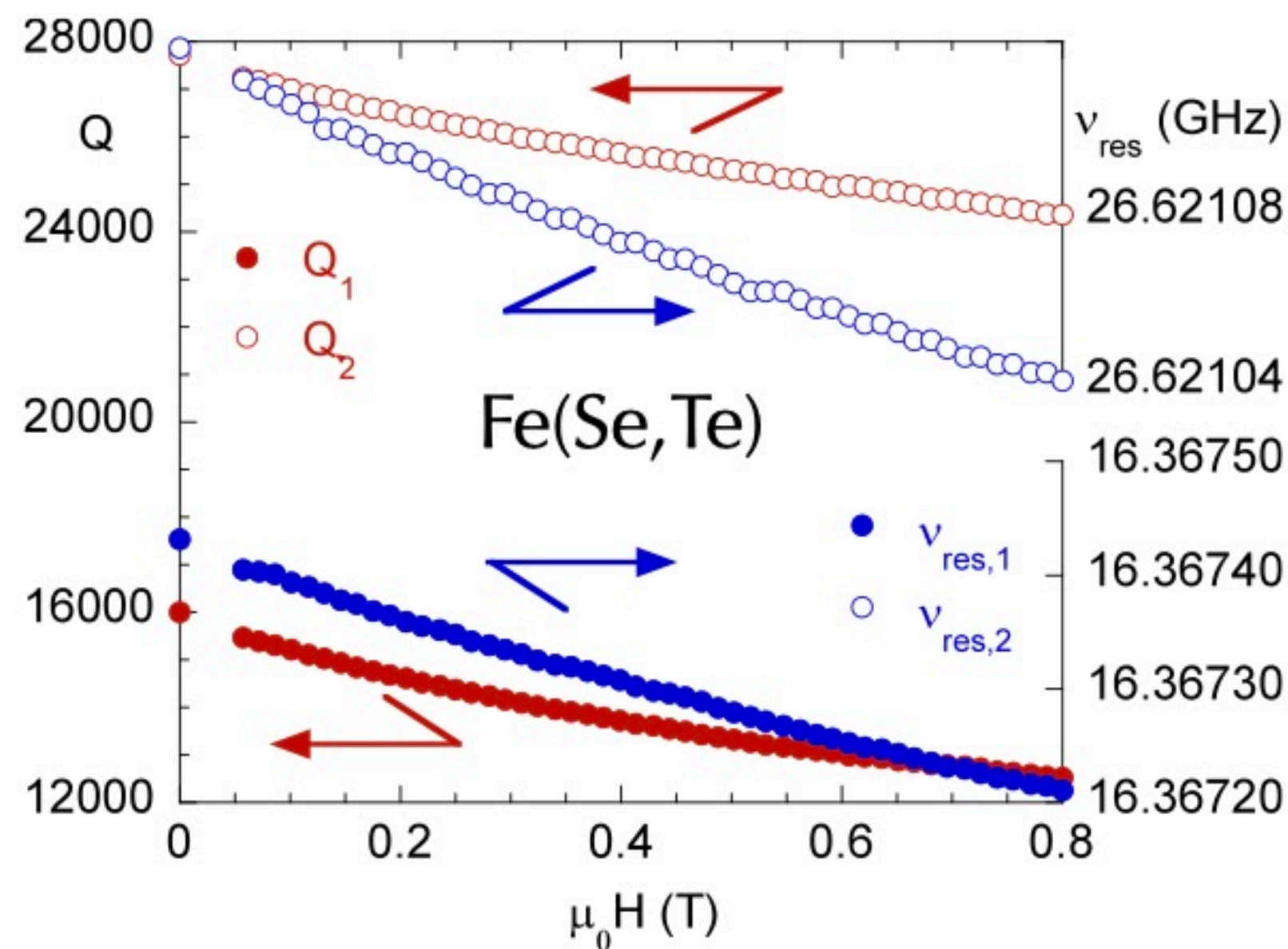
N. Pompeo et al., Measurement 184 109937 2021  
 A. Alimenti et al., IEEE Instrum. Meas. Magazine 24 12 2021



# Microwave technique: data analysis

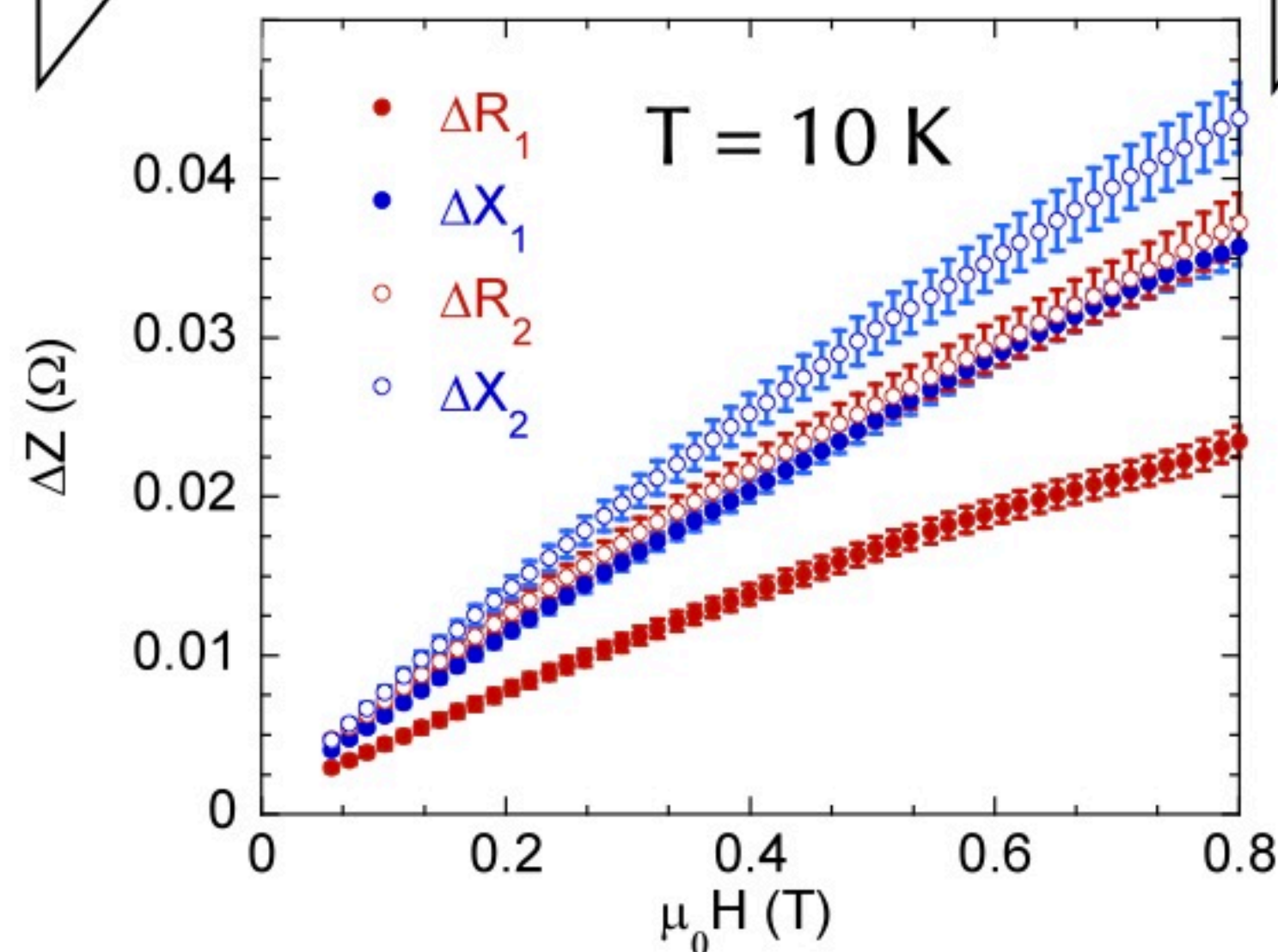
Two-mode measurements 16 GHz / 27 GHz, low fields

Q-factor and resonance frequency vs. H

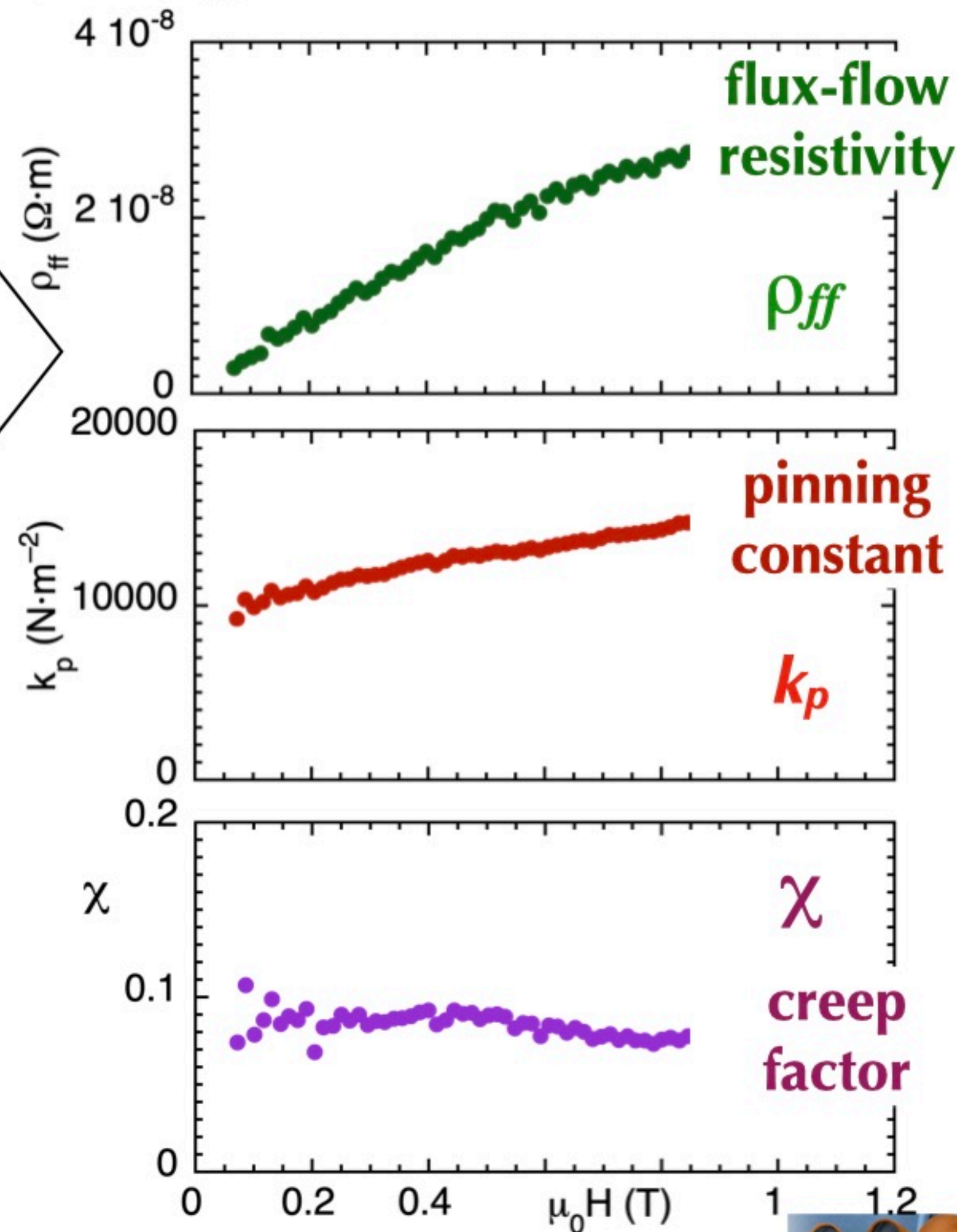


electromagnetism

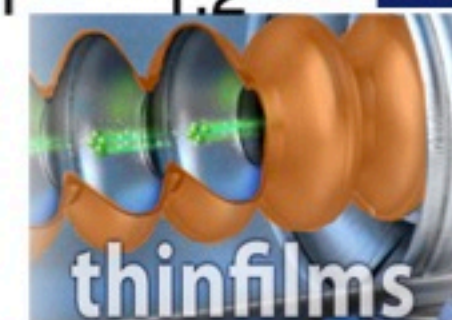
Surface impedance shift



data inversion



N. Pompeo et al., Measurement 184 109937 2021

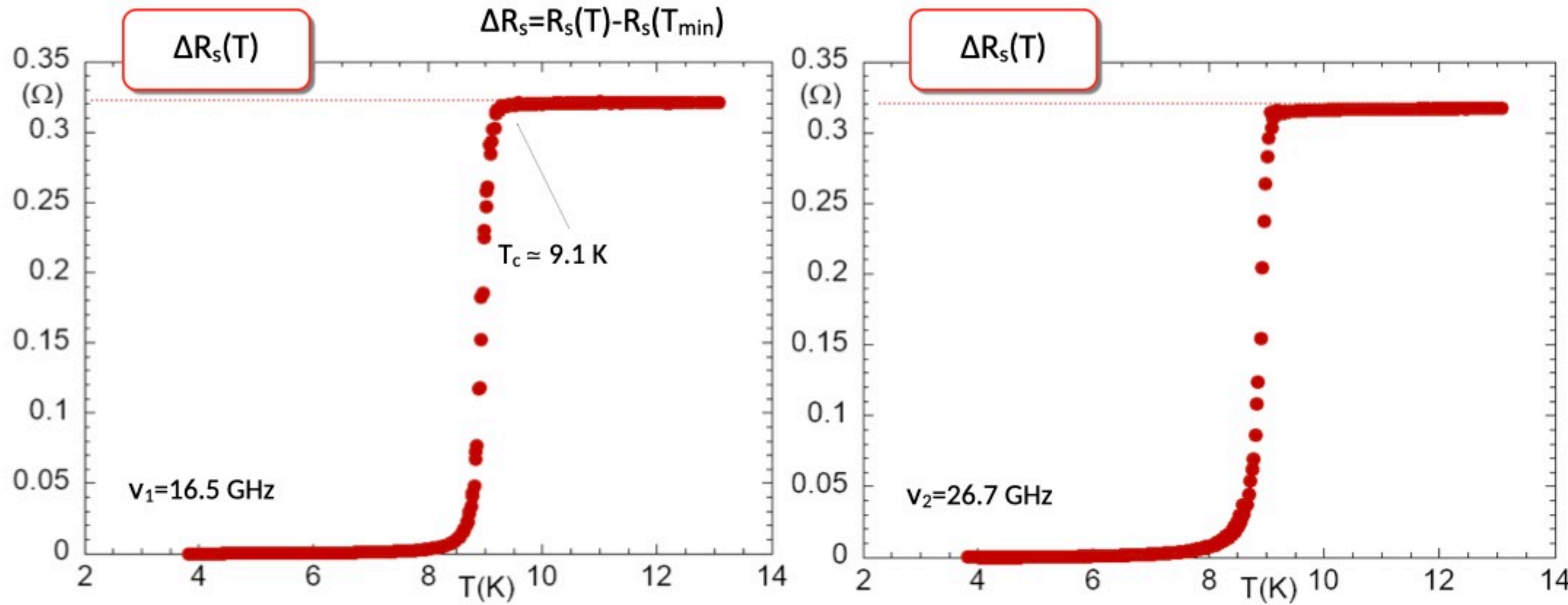


## NbTi: a case study

Measurements in fields  
 $\mu_0 H \leq 1.2 \text{ T}$

# NbTi samples

- Nb<sub>40</sub>Ti<sub>60</sub> film (d≈1.70(15) μm) on quartz (1.2 mm)



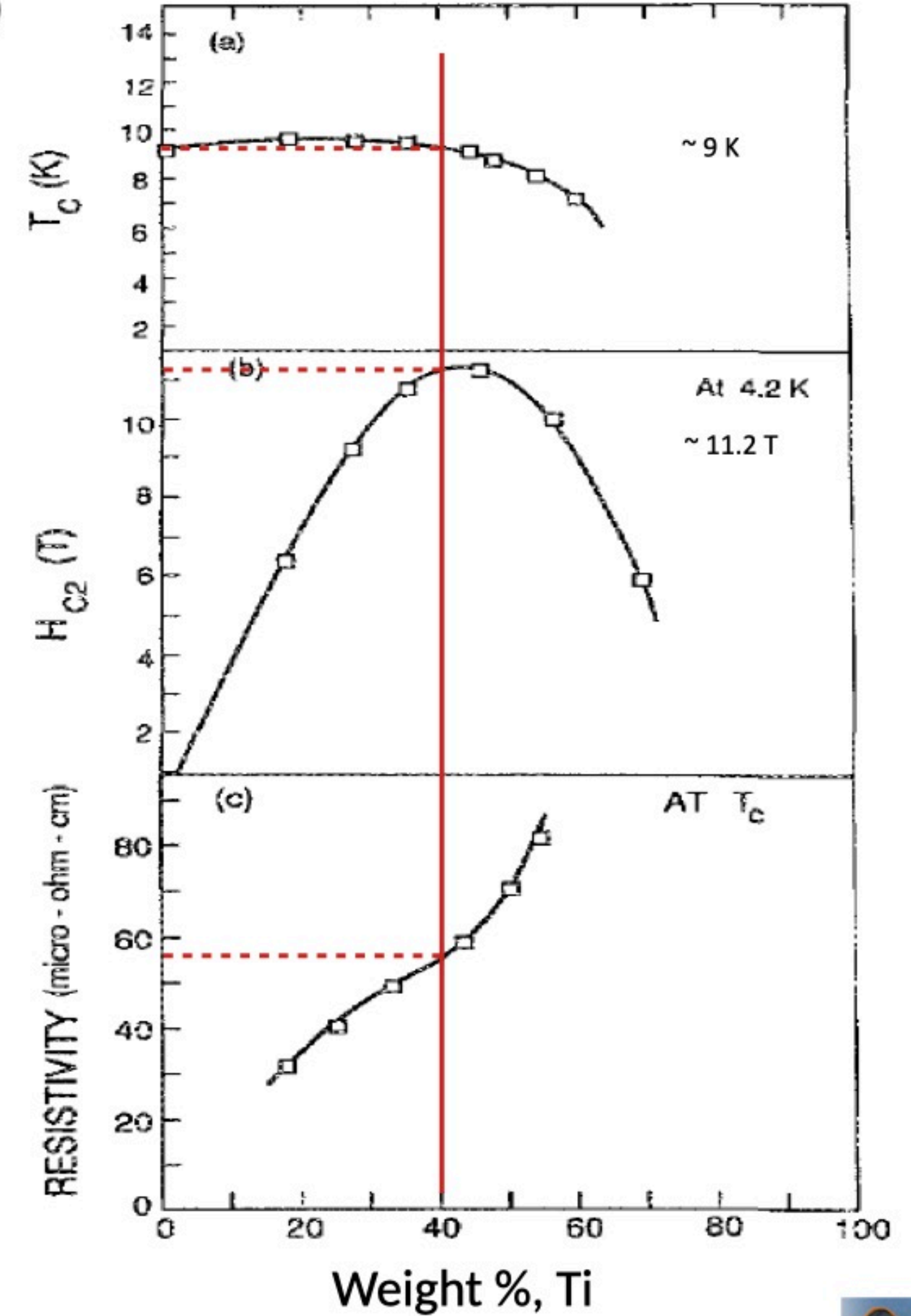
- Normal state resistivity:

$$\rho_n = R_s(T > T_c) \cdot d \simeq 5.4(5) \cdot 10^{-7} \Omega\text{m}$$

$\delta_n \geq 2.9 \mu\text{m} \Rightarrow$  thin film regime in the normal state

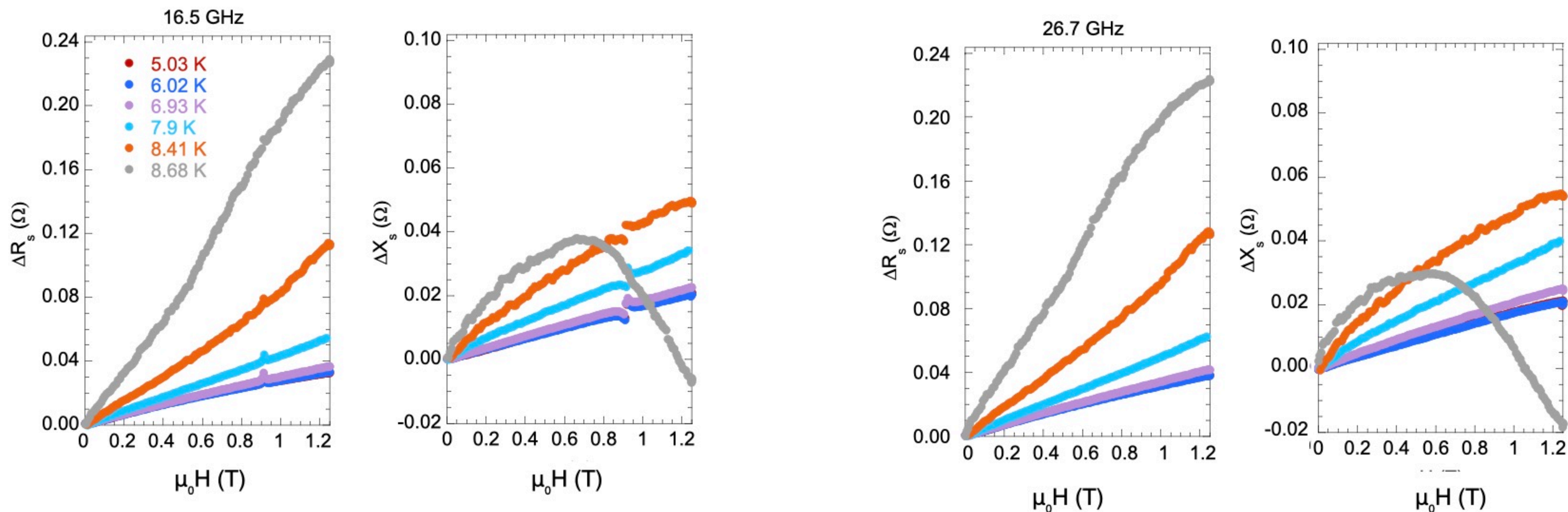
	$T_c$ [K]	$\lambda$ [Å]
Nb <sub>0.40</sub> Ti <sub>0.60</sub>	9.0	3000
Nb <sub>0.55</sub> Ti <sub>0.45</sub>	9.6	2300

(atomic %) Benvenuti et al, 5<sup>th</sup> Workshop RF Supercond. 1991



Meingast et al., JAP 66 5962 (1989)

# NbTi: shift of the surface impedance



- All T :  $\Delta R$  &  $\Delta X$  increase with H  
→ vortex motion

- Near  $T_c$ : large  $\Delta R \sim R_n$  &  $\Delta X < 0$   
→ e.m. thin film & 2-fluids contribution



# NbTi: determination of vortex parameters

Simultaneous fits of  $Z_s(H) - Z_s(0)$

$$Z_s = \sqrt{i\omega\mu_0\tilde{\rho}} \quad \tilde{\rho} \simeq \rho_v + i\frac{1}{\sigma_2}$$

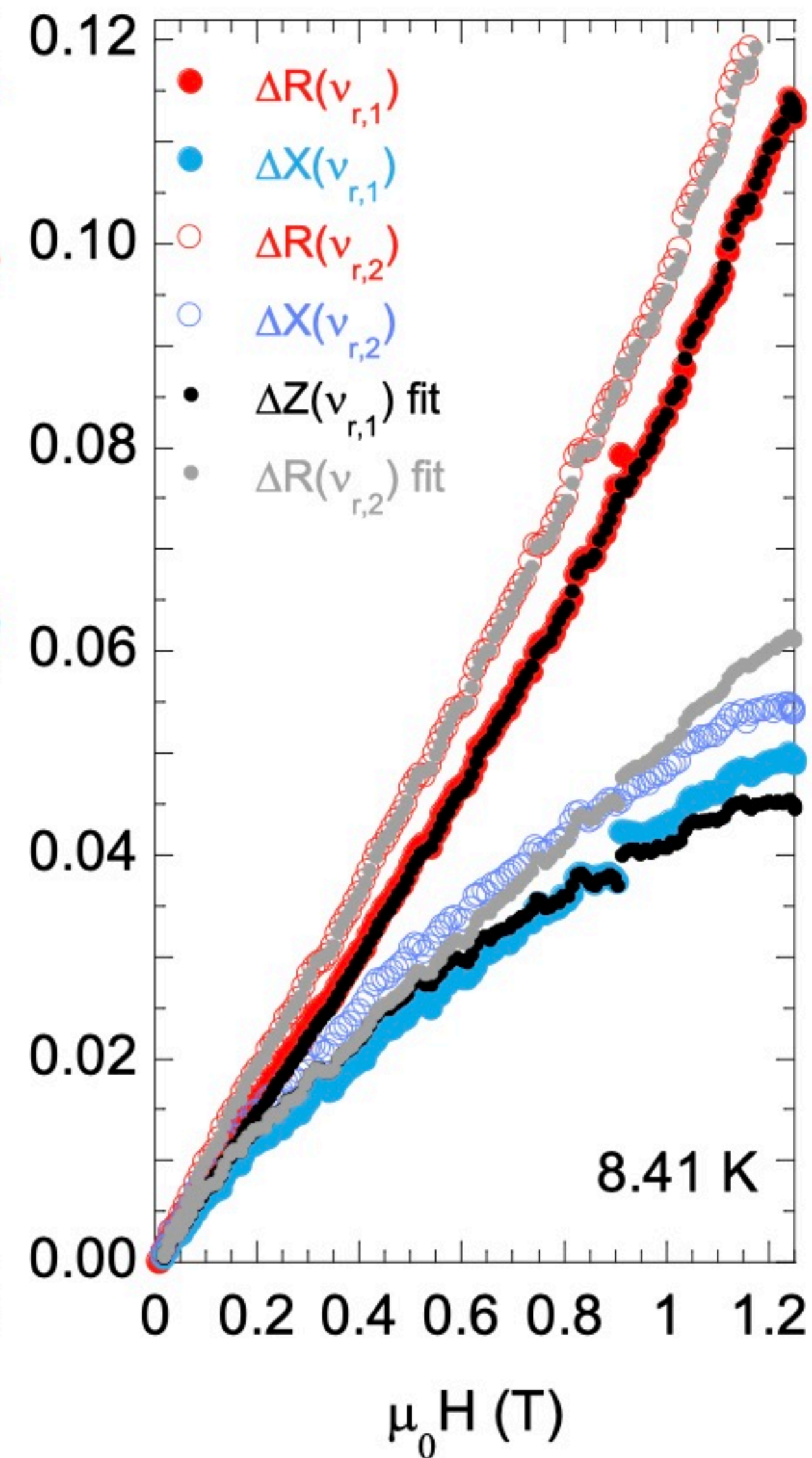
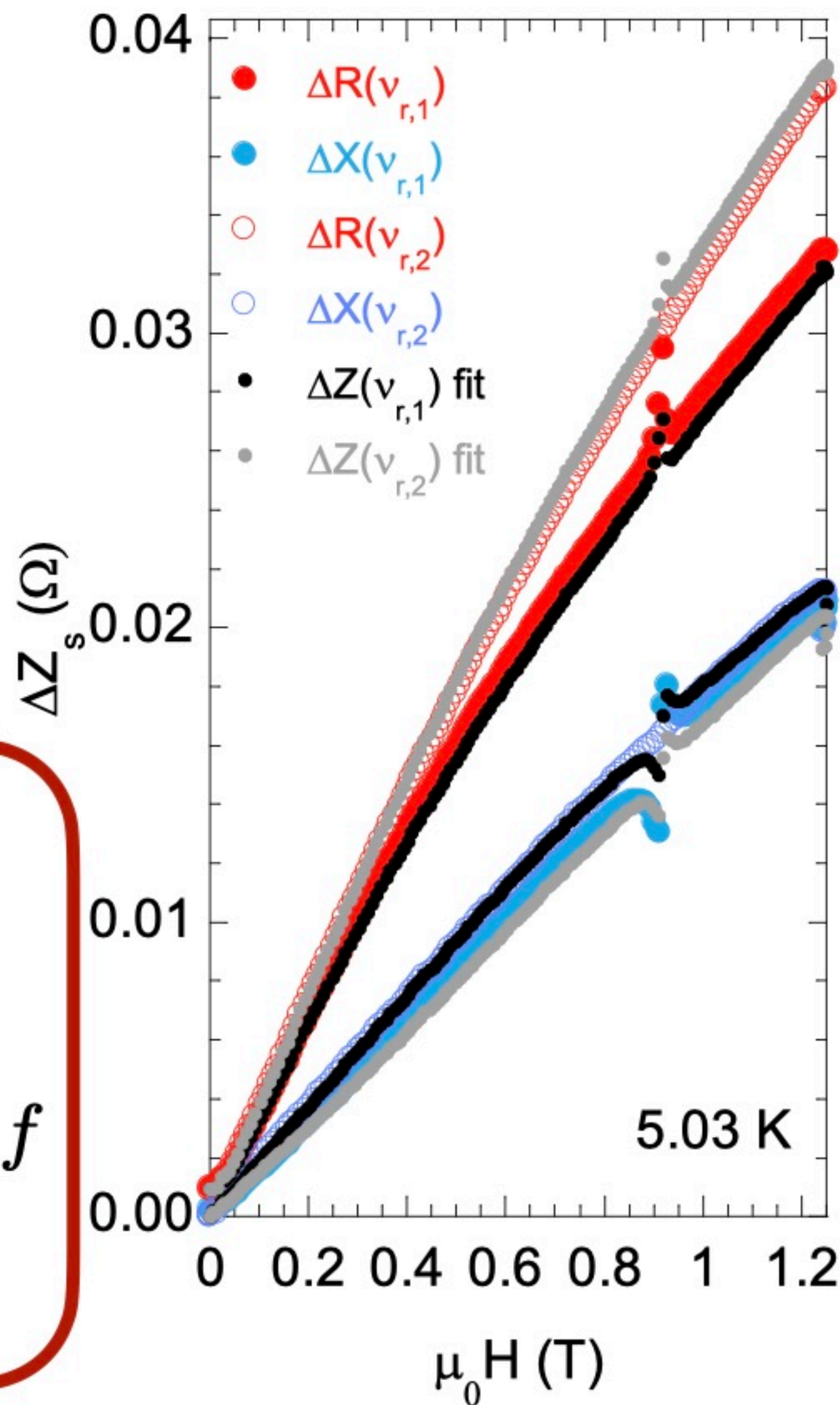
$$\sigma_2 = \frac{1}{\omega\mu_0\lambda^2} \quad \rho_v = \rho_{ff} \frac{1 + i\frac{\nu_0}{\nu}}{1 + \left(\frac{\nu_0}{\nu}\right)^2}$$

Fits yield:  $\rho_{ff}$

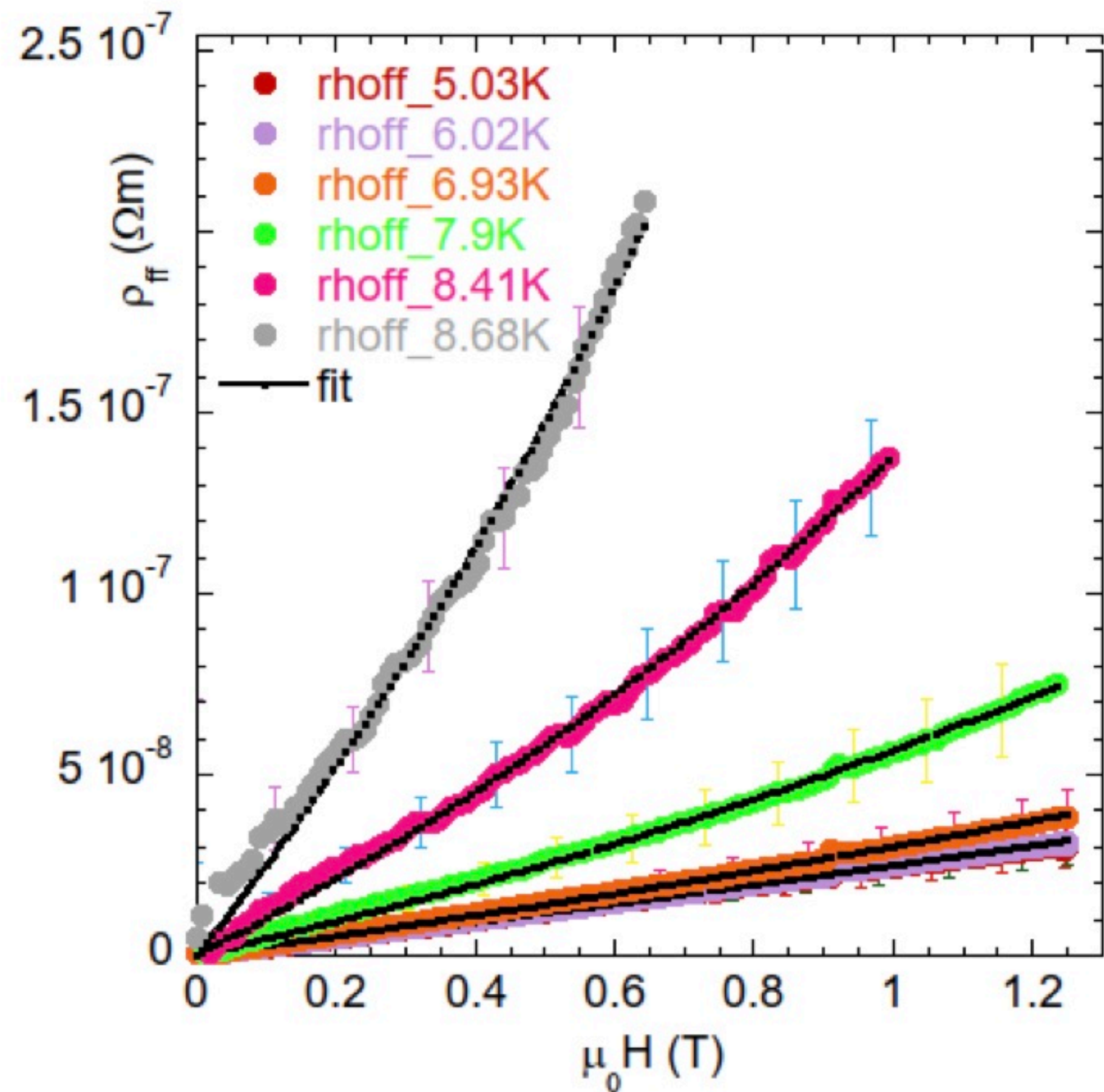
$\nu_0$

$$k_p = \nu_0 \Phi_0 B / \rho_{ff}$$

at each  $H$  and  $T$

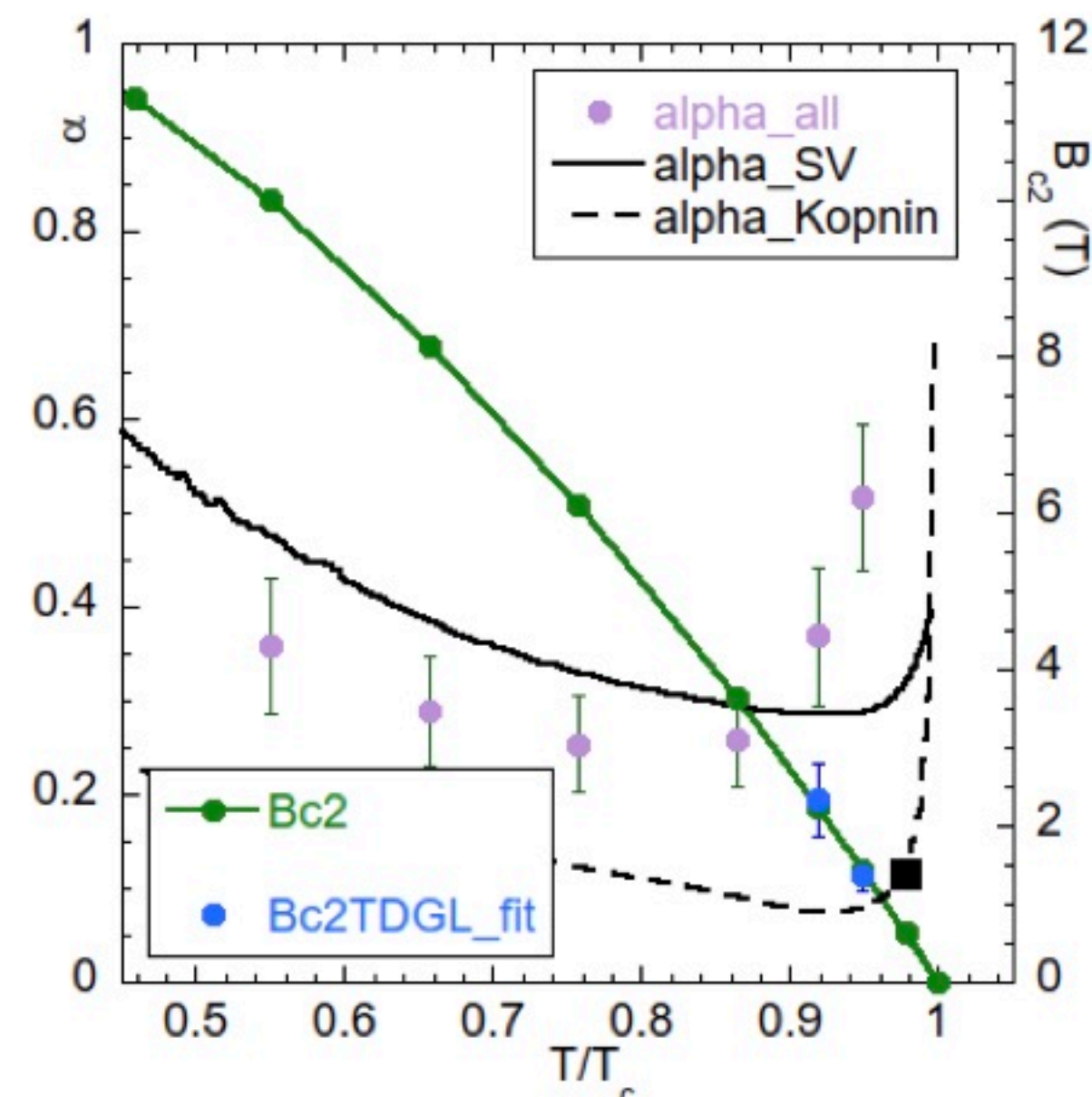


# NbTi: Flux-flow resistivity

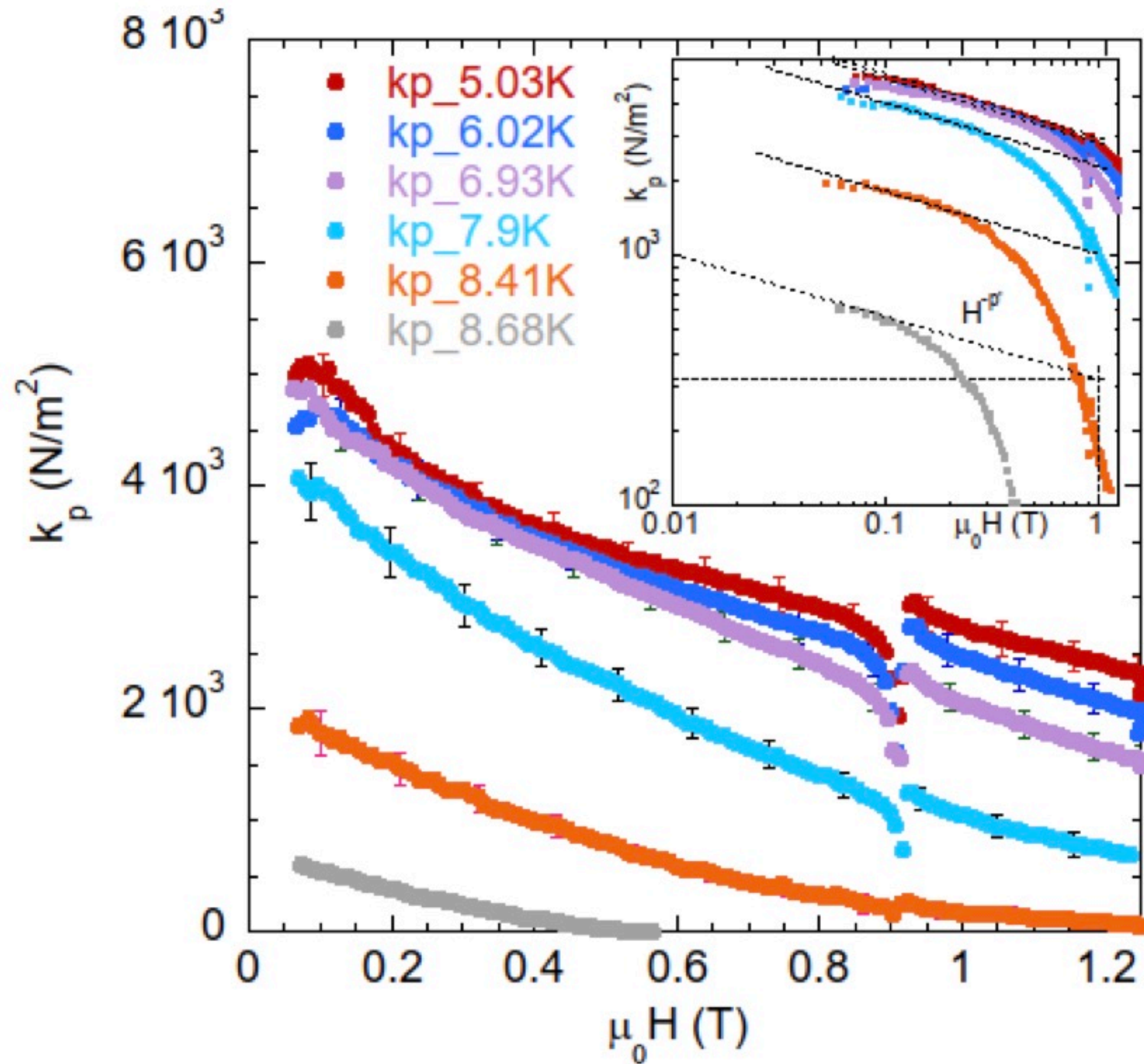


TDGL fits: excellent agreement

$$\rho_{ff} = \rho_n \frac{\alpha B}{(\alpha - 1)B + B_{c2}}$$

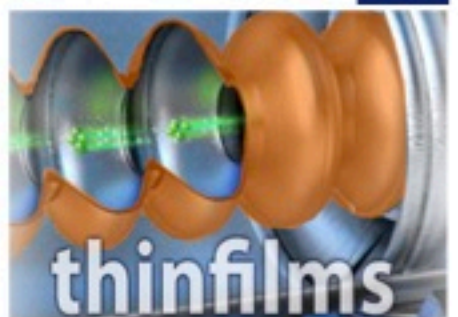


# NbTi: pinning constant (Labusch parameter)



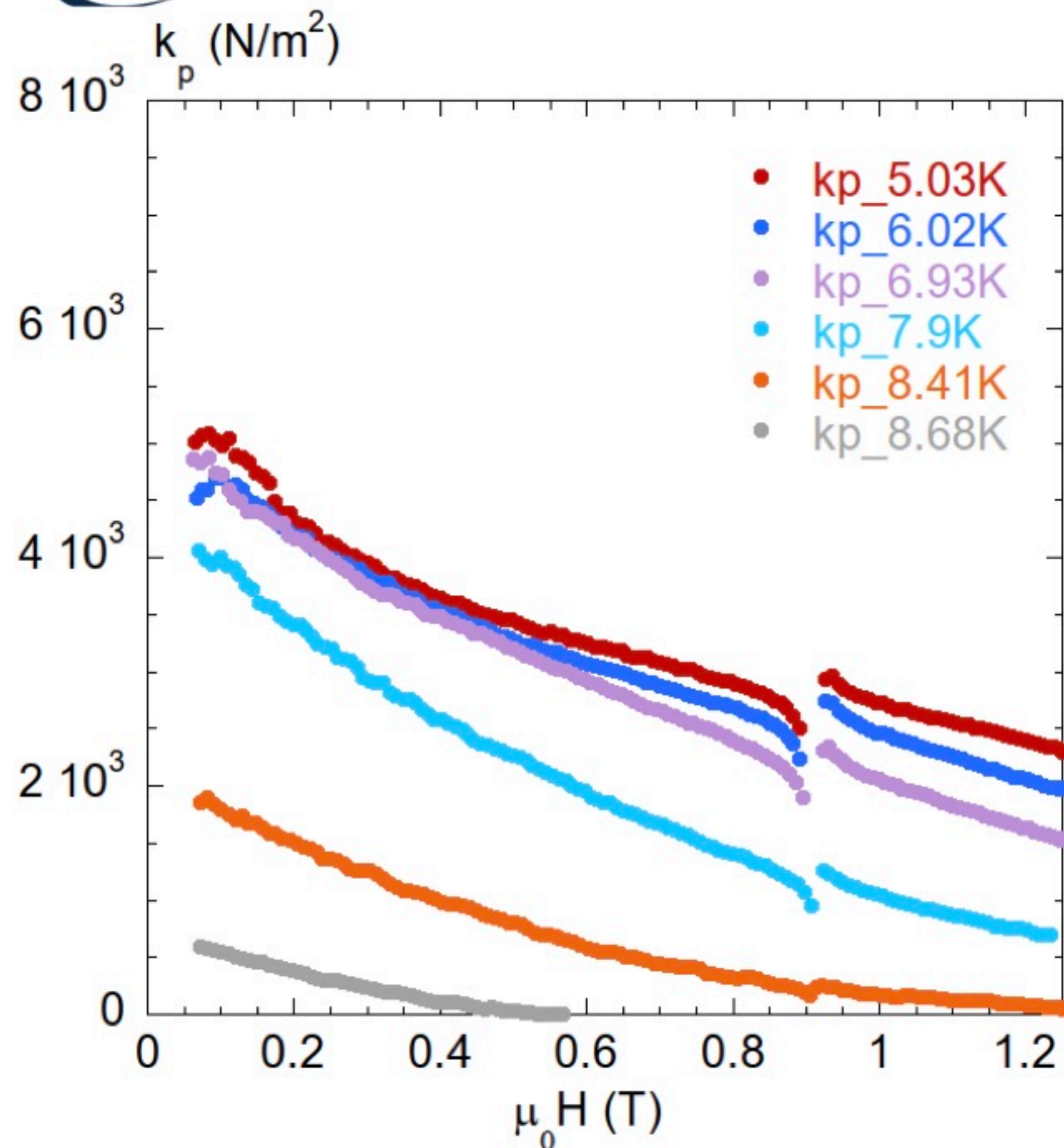
$k_p$  decreases with  $H$   
 → depends on fluxon density  
 → fluxons are NOT individually pinned by defects  
 → collective pinning regime

What are the effective pinning centers?

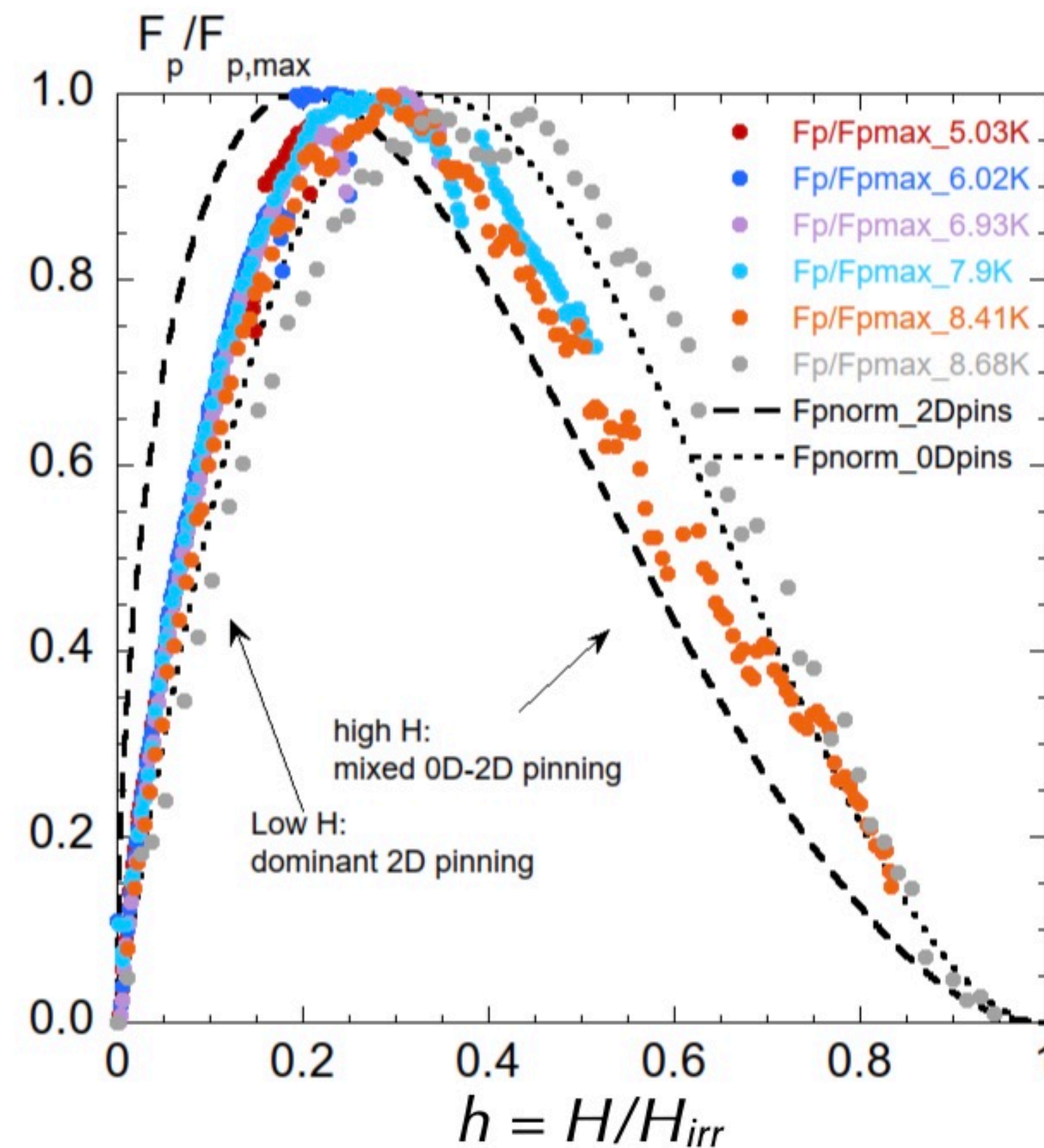
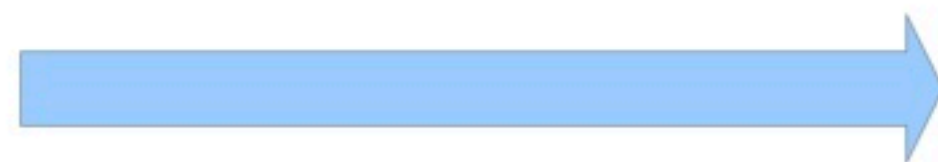




# NbTi: Dew-Hughes pinning analysis



$$F_p(T, B) = \frac{k_p(T, B)\xi(T)B}{\Phi_0}$$



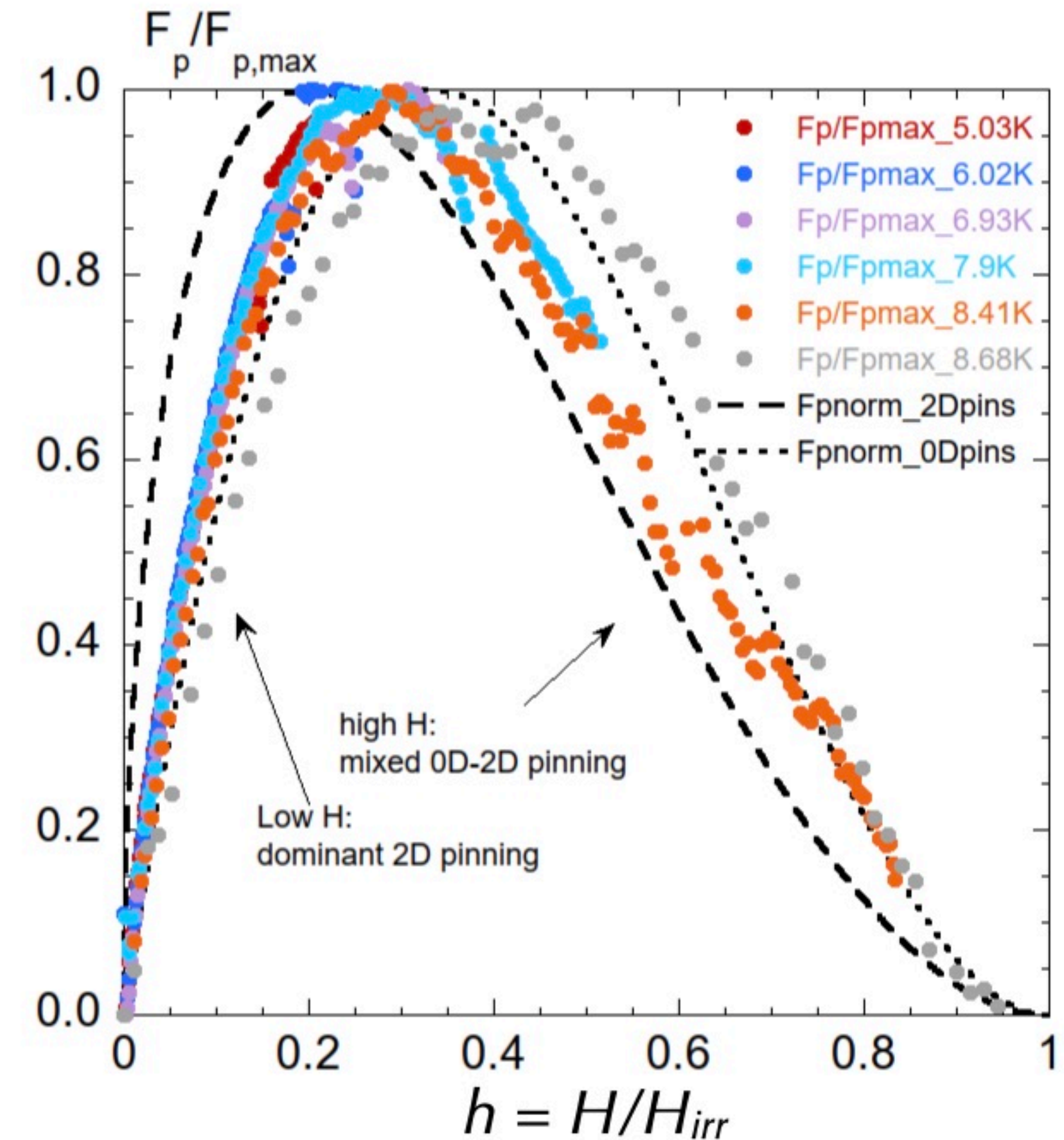
Dew-Hughes scaling analysis:  $F_p / F_{p,max} = A \cdot h^p (1 - h)^q$

D. Dew-Hughes, Philos. Mag. A J. Theor. Exp. Appl. Phys. 30, 293 (1974).



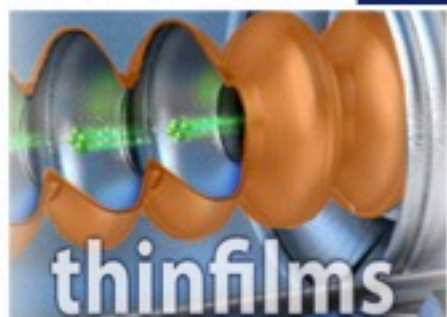
# NbTi: Dew-Hughes pinning analysis

- data satisfactorily scale with a reduced field  $H_{irr} \sim 0.6 H_{c2}$
- Theory:  $q = 2$ ;  $p = 0.5$  (2D pinning),  $p = 1$  (0D pinning)
- Result:  $q = 2$ ;  $p = 0.75$   
 $\Rightarrow$  admixture of point (0D) and grain boundary (2D) pinning
- **point pinning dominates at low fields**
- **grain boundaries dominate at high fields**



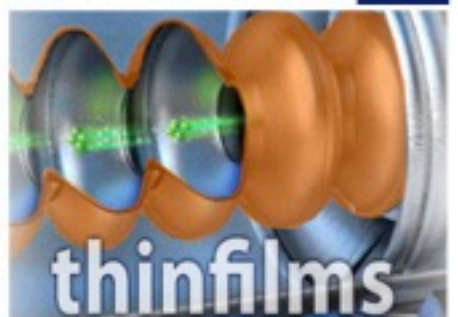
Dew-Hughes scaling analysis:  $F_p / F_{p,max} = A \cdot h^p (1 - h)^q$

D. Dew-Hughes, Philos. Mag. A J. Theor. Exp. Appl. Phys. 30, 293 (1974).



## Comparison: Fe(Se,Te), YBaCuO

Measurements in fields  
 $\mu_0 H \leq 12 \text{ T}$





FeSe<sub>0.5</sub>Te<sub>0.5</sub> Thin film (PLD) on CaF<sub>2</sub>

$T_c = 18$  K

thickness  $d \sim 240$  nm

$\rho_n = 3.0(2) \times 10^{-6} \Omega\text{m}$

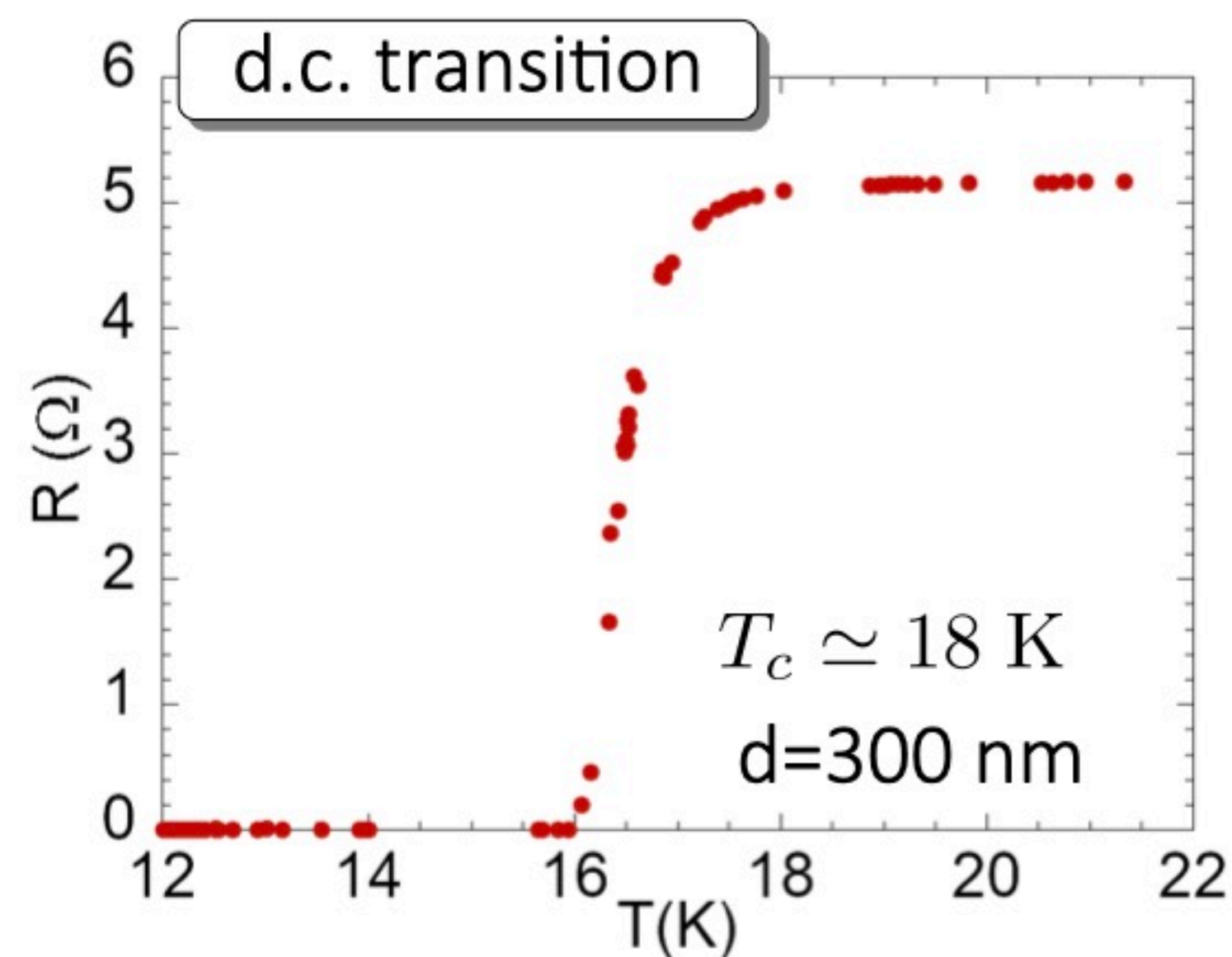
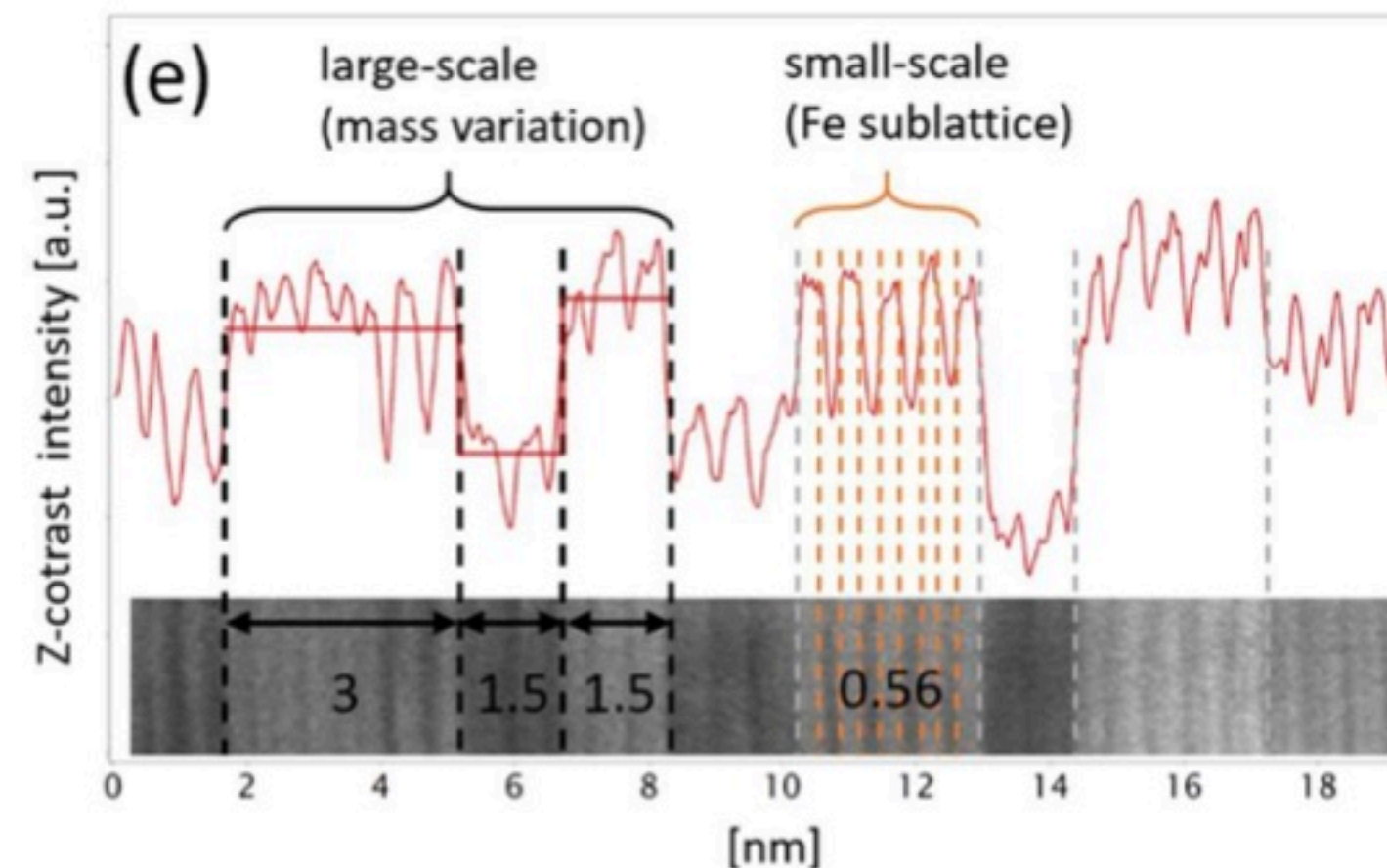
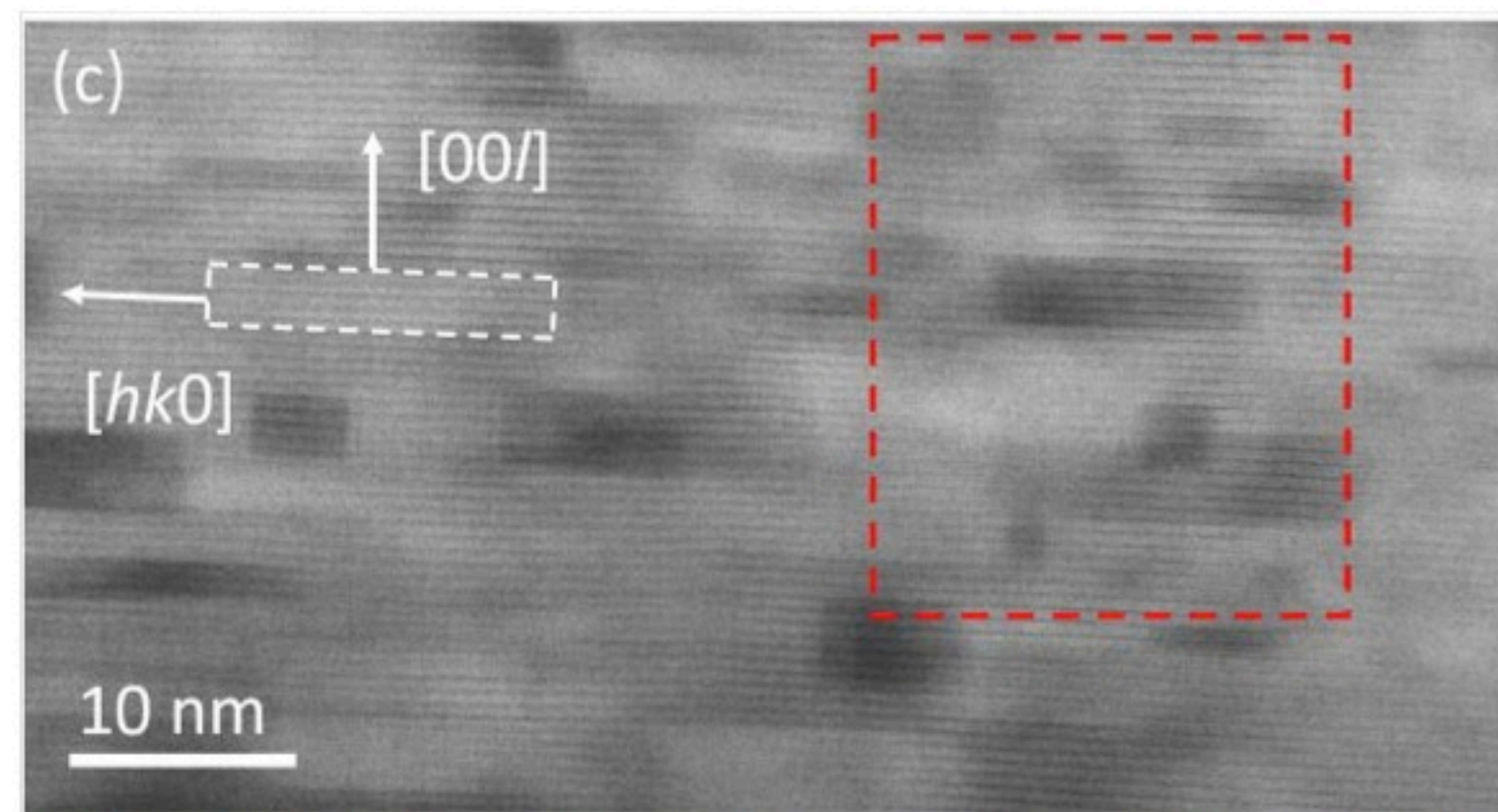
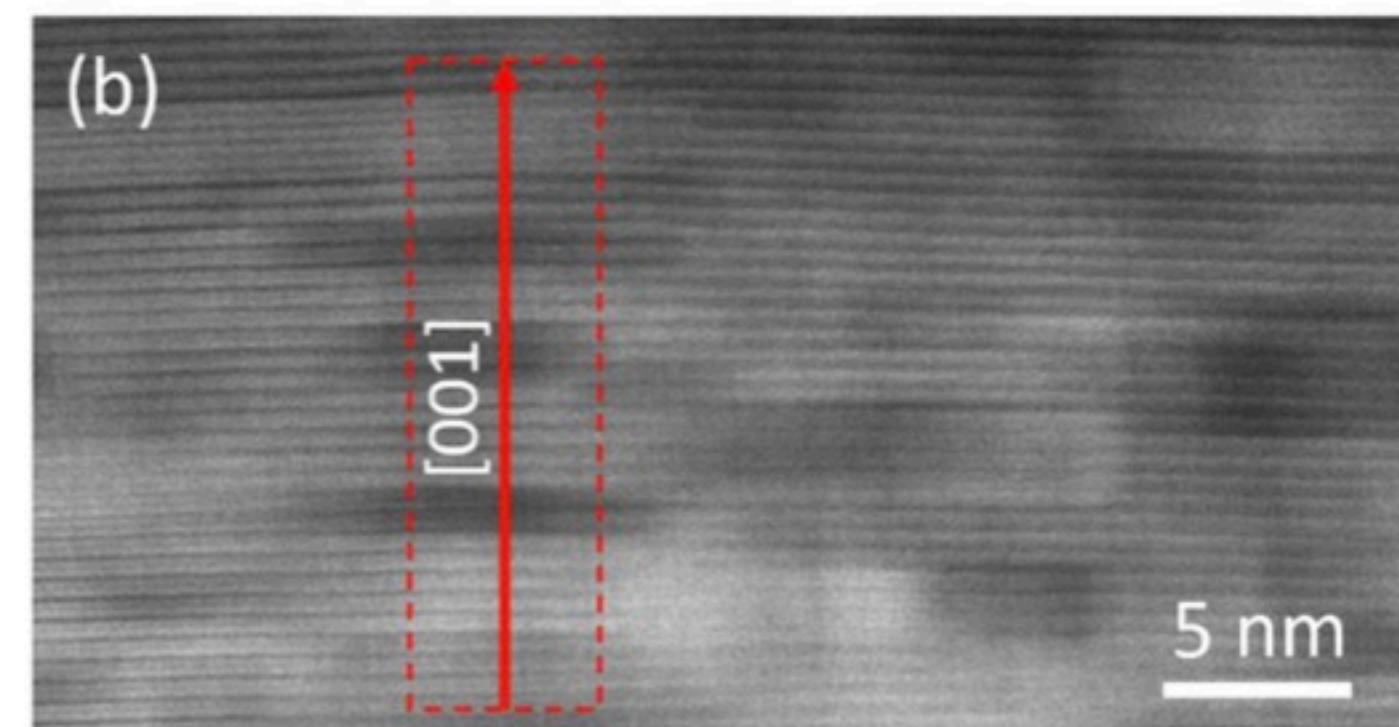
$T_{\text{onset}} - T_{\text{zero}} = 0.6$  K

RRR=1.1



STEM, EELS,  
HRSTEM

complex pinning  
landscape most likely



In-plane rotated grains  
EELS: Clusters with different stoichiometry  
(different  $T_c$ )

Figure 3. b) STEM Z-contrast image; e) Z-contrast intensity profile along the red line marked in (b).

A. Palenzona et al., SuST 25 115018 2012  
V. Braccini et al., APL 103 172601 2013

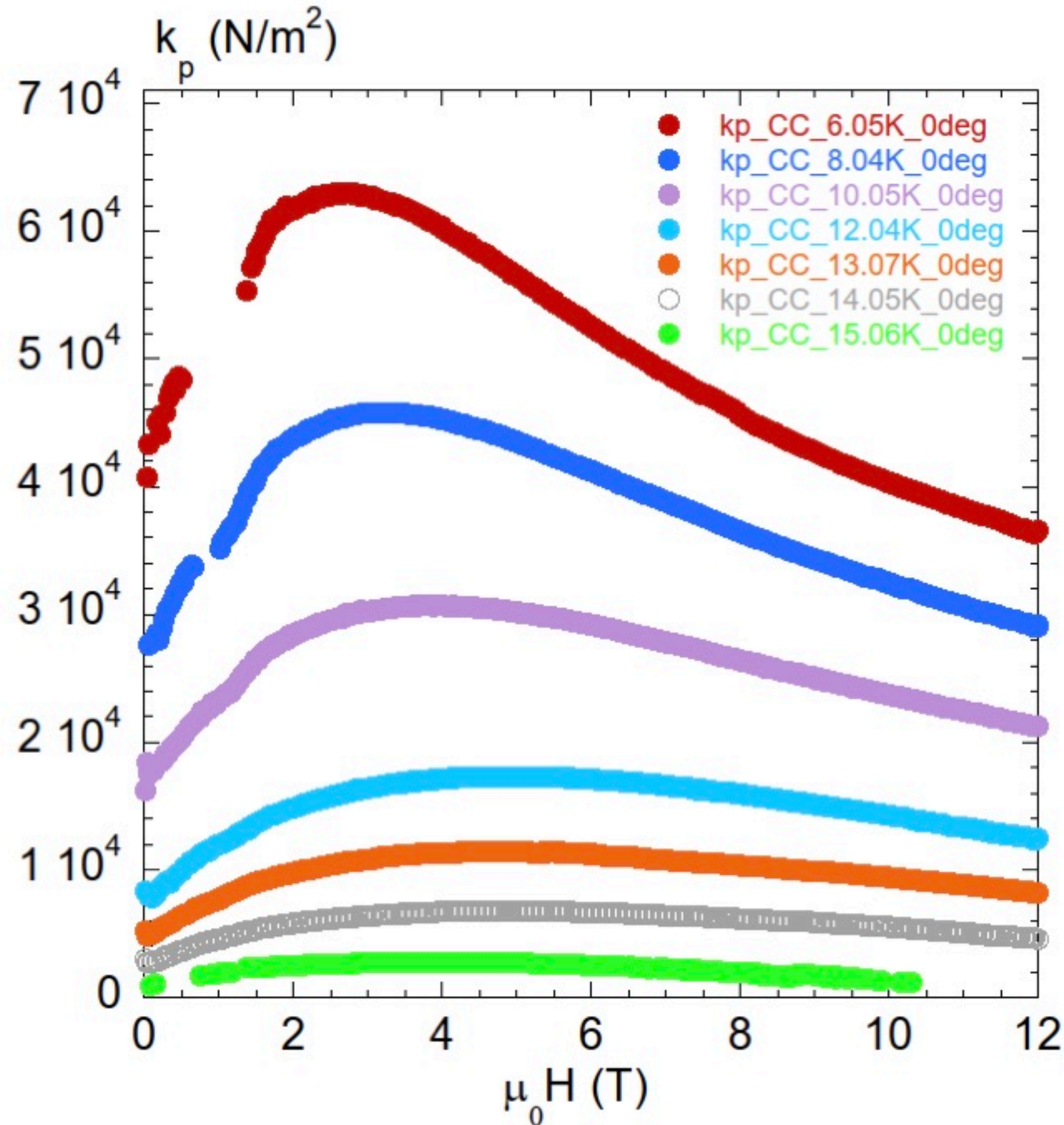
M. Scuderi et al.,  
Sci. Rep. (2021)

Masood Rauf Khan et al.,  
Materials (2021)

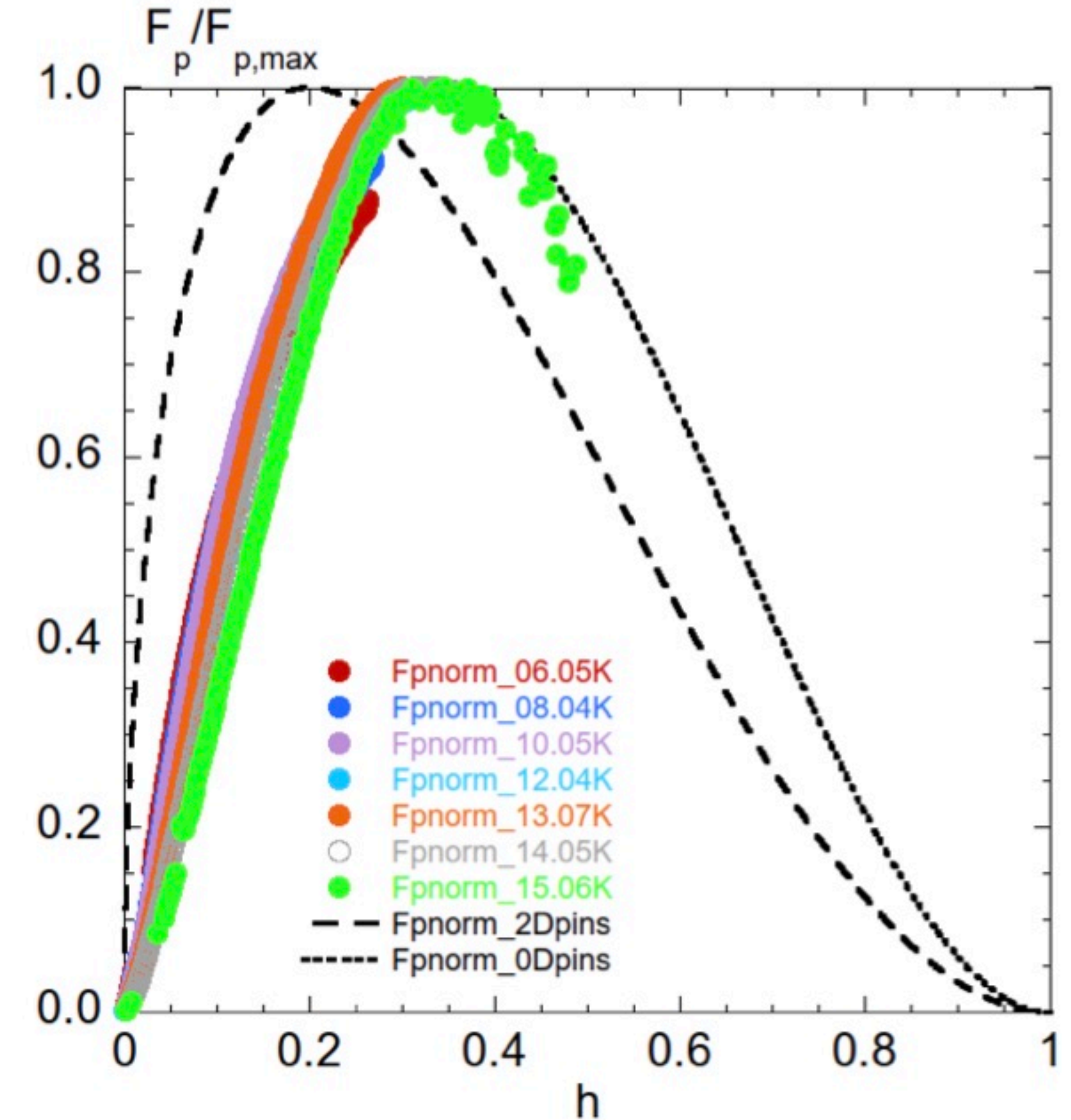


# Fe(Se,Te): Dew-Hughes pinning analysis

Pinning in Fe(Se,Te) is firmly due to point pinning

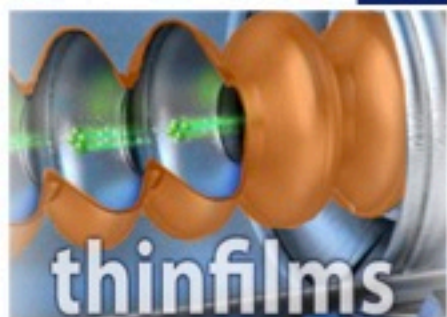


$$F_p(T, B) = \frac{k_p(T, B)\xi(T)B}{\Phi_0}$$



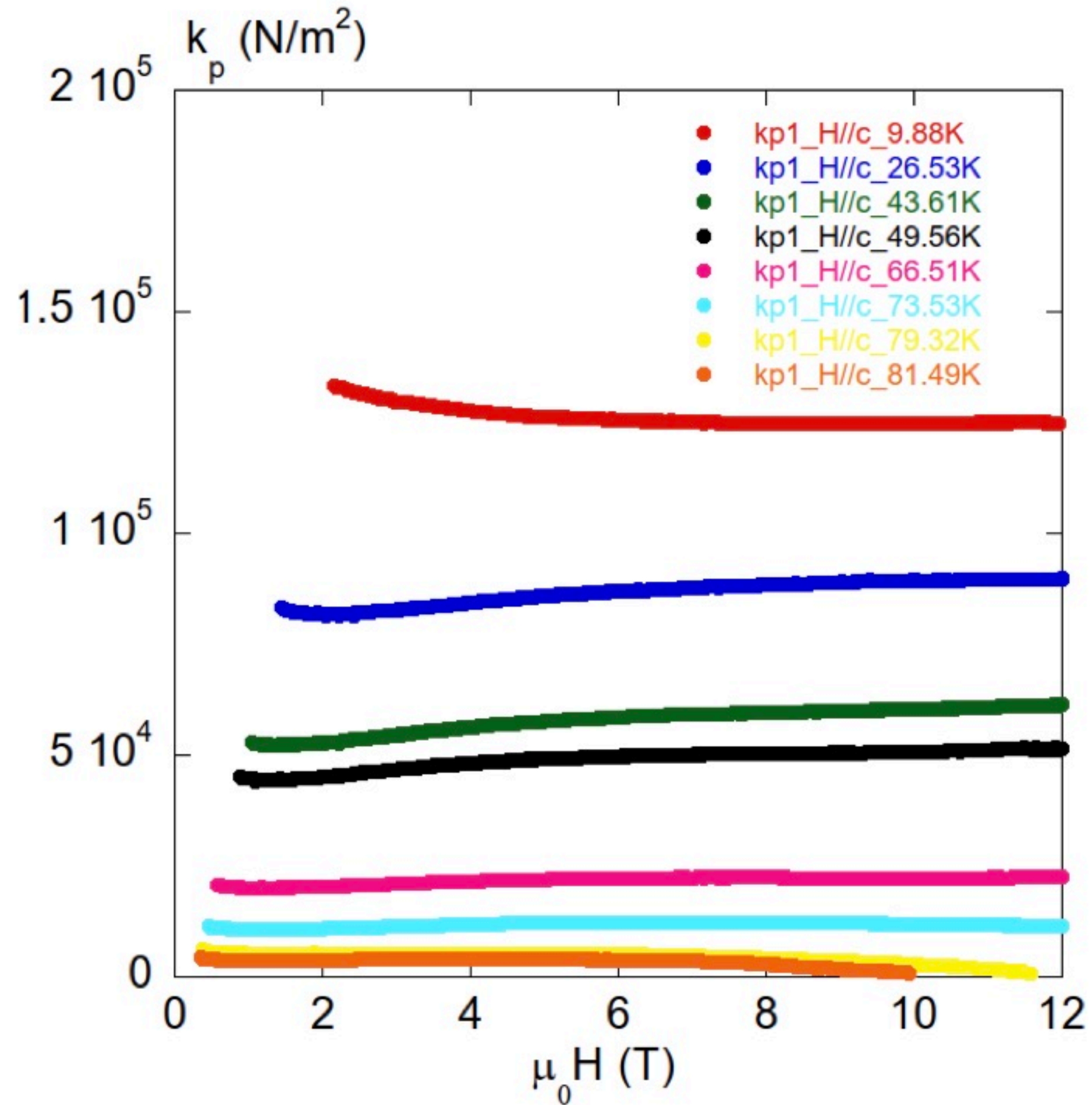
Dew-Hughes scaling analysis:  $F_p / F_{p,max} = A \cdot h^p (1 - h)^q$

D. Dew-Hughes, Philos. Mag. A J. Theor. Exp. Appl. Phys. 30, 293 (1974).

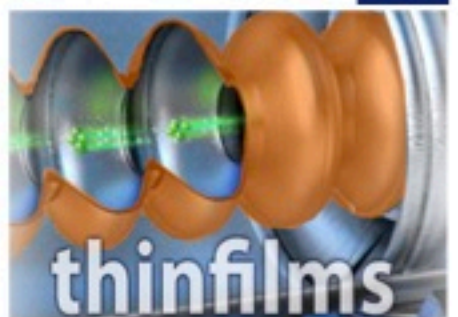


# YBaCuO: single pinning regime

**Pinning in YBaCuO: single vortex pinning.  
Impossible to determine whether 0D, 2D pinning**



Sample details: V. Pinto et al., Coatings, vol. 10, no. 9, art. id. 860, 2020.  
 YBCO pristine,  
 CSD growth  
 Substrate: LAO  
 Thickness: 80 nm  
 $T_c(0) = 89.86$  K



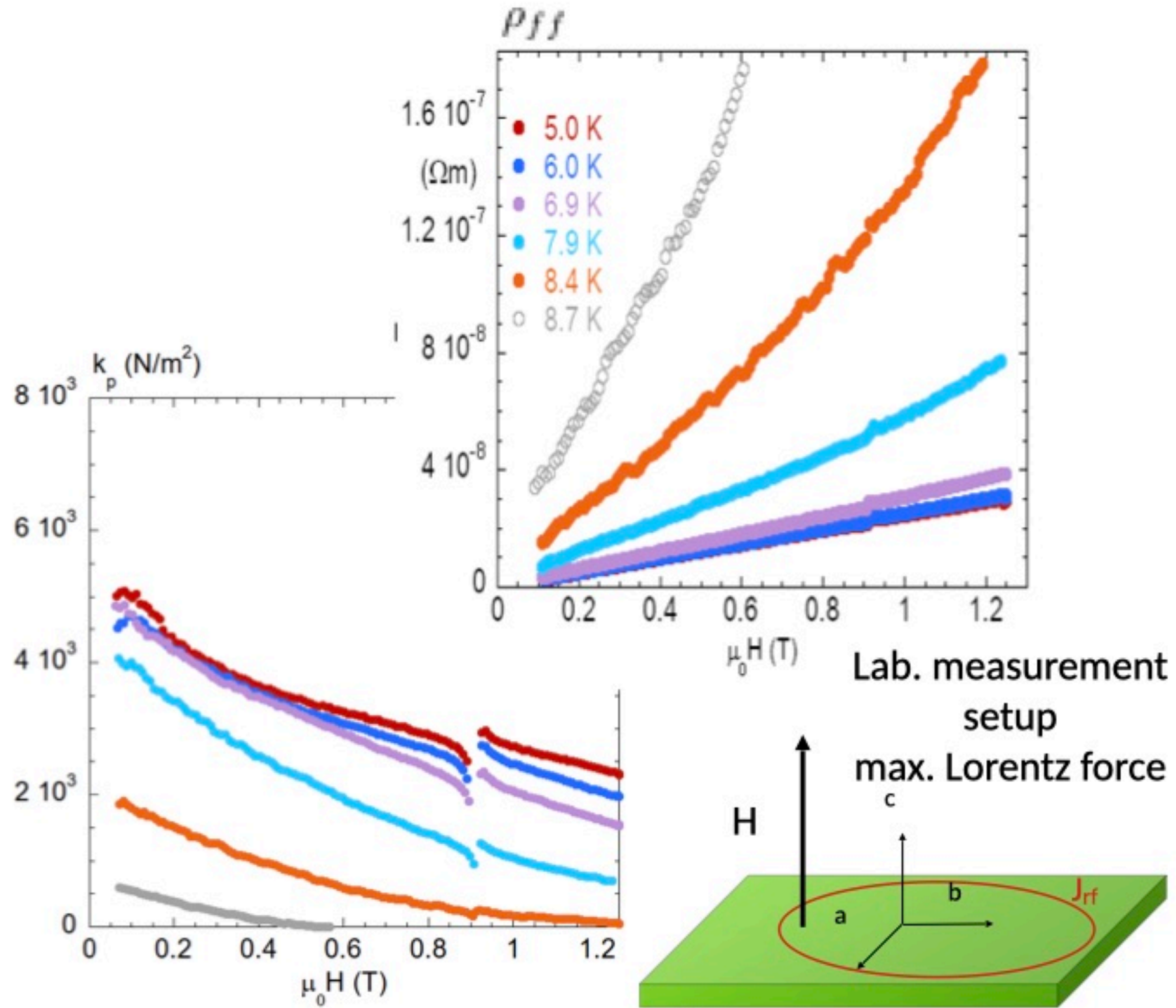
## Reexamination of NbTi haloscope data: experimental estimate of $c_{ff}$

Combining vortex parameters +  
 $R_s+iX_s$  data on an haloscope

⇒ experimental determination of the alignment factor  $c_{ff}$

# NbTi: reexamination of haloscope data - procedure

## Vortex parameters: this work



## model

$$Z_s = \sqrt{i \frac{\omega \mu_0}{\sigma}} = \sqrt{i \omega \mu_0 \tilde{\rho}}$$

$$\tilde{\rho} = \frac{\rho_v + i \frac{1}{\sigma_2}}{1 + i \frac{\sigma_1}{\sigma_2}}$$

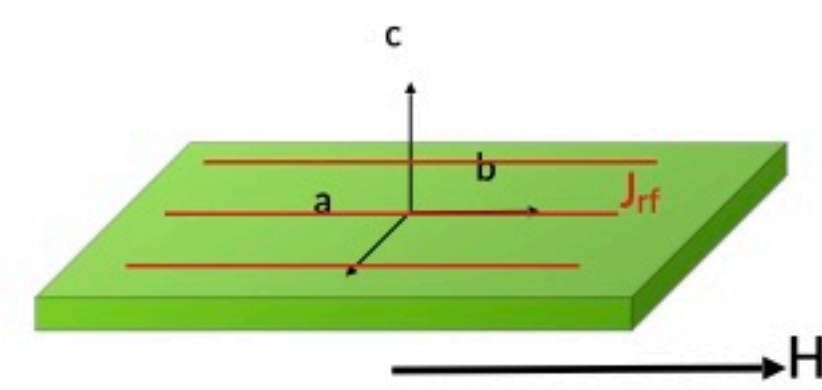
$$\sigma_1 - i \sigma_2 = \frac{n_n e^2 \tau}{m} - i \frac{1}{\omega \mu_0 \lambda^2}$$

$$\rho_v = c_{ff} \rho_{ff} \frac{\chi + i \frac{\nu}{\nu_0}}{1 + i \frac{\nu}{\nu_0}}$$

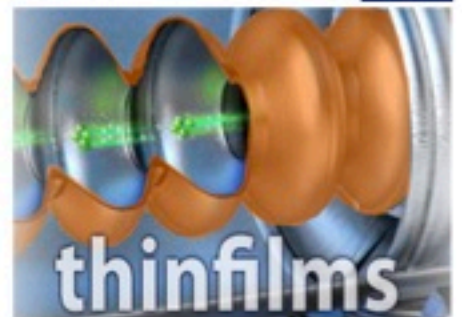
+

fit to nominally force-free configuration data  
with one parameter:  $c_{ff}$

⇒

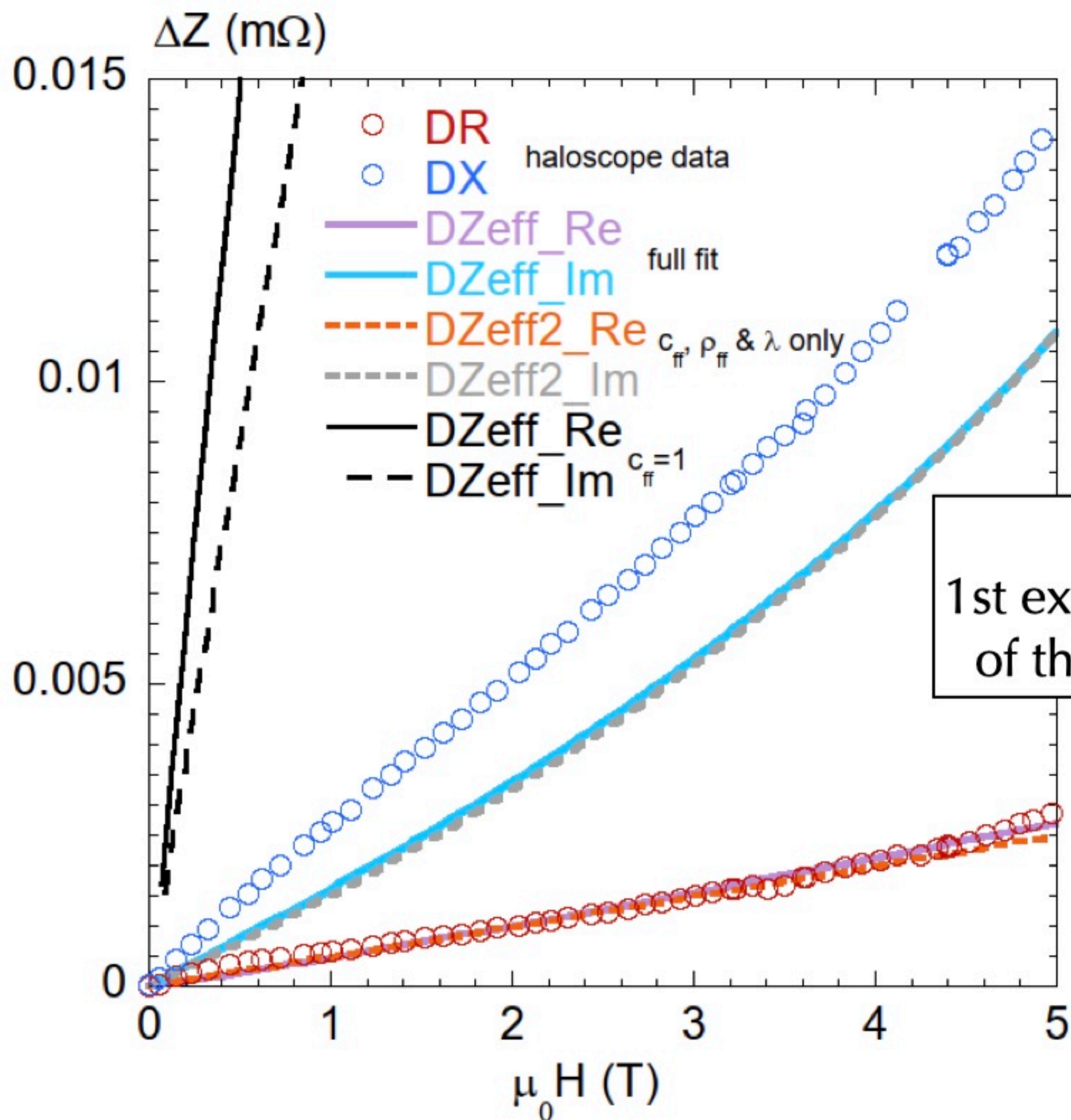


Haloscope  
"force free" config.

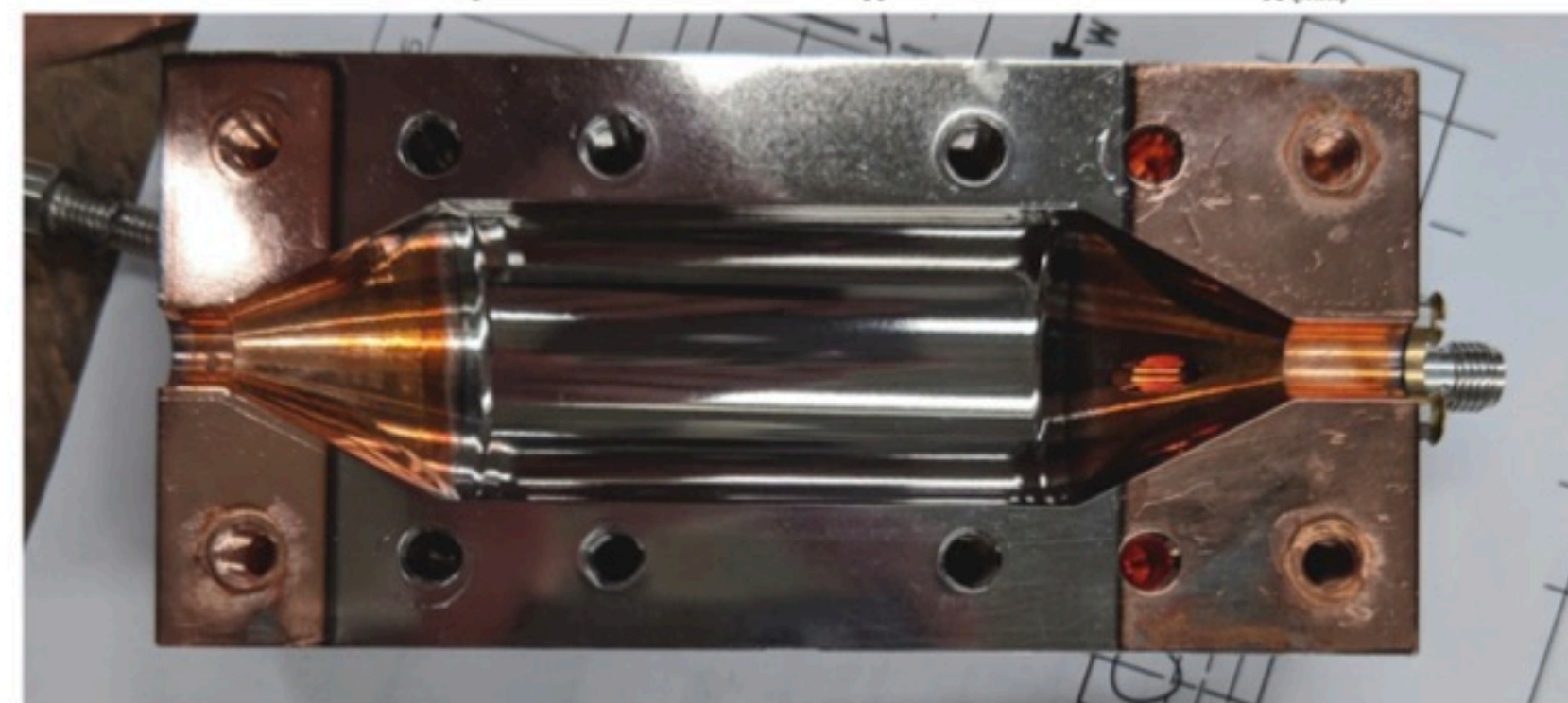




# NbTi: reexamination of haloscope data - results



$c_{ff} = 0.012$   
 1st experimental estimate  
 of the alignment factor

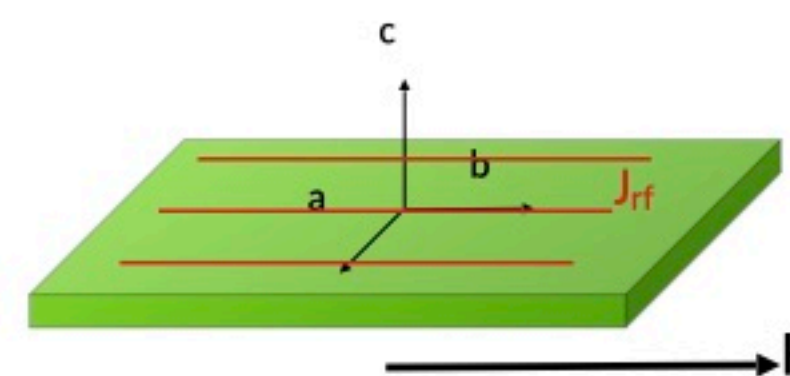


**NbTi haloscope**

Alesini et al.

*Phys. Rev. D* **99** 101101(R) (2019)

fit to nominally force-free configuration data  
 with one parameter:  $c_{ff}$



Haloscope  
"force free" config.



## Evaluation of the potential for haloscopes

# Comparison of superconductors

$$R_s \simeq \frac{1}{2} c_{ff} \rho_{ff} \frac{1}{1 + (\nu_0/\nu)^2} \frac{1}{\lambda}$$

calculated at  $B = 5 \text{ T}$

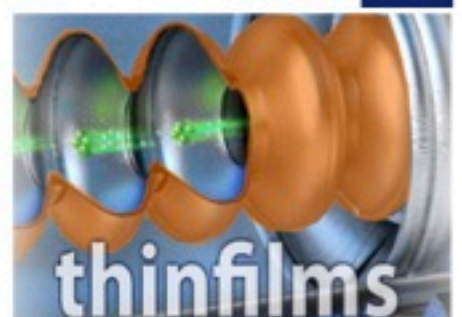
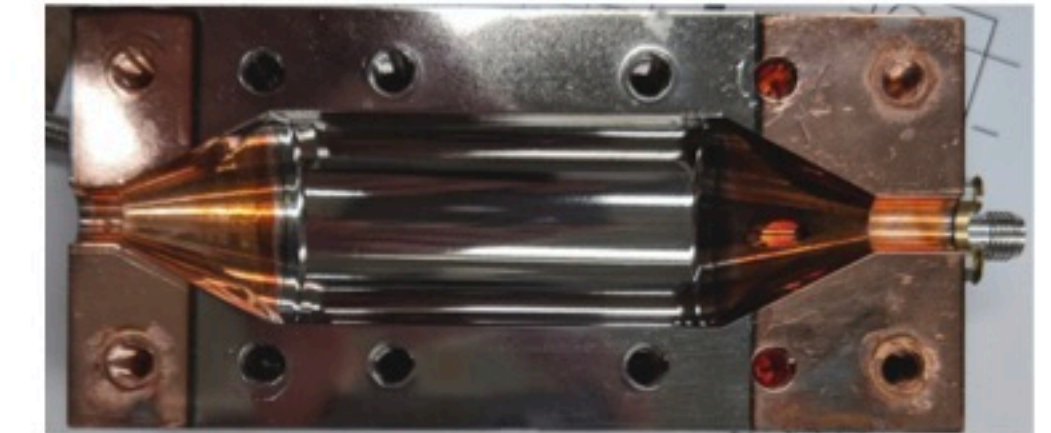
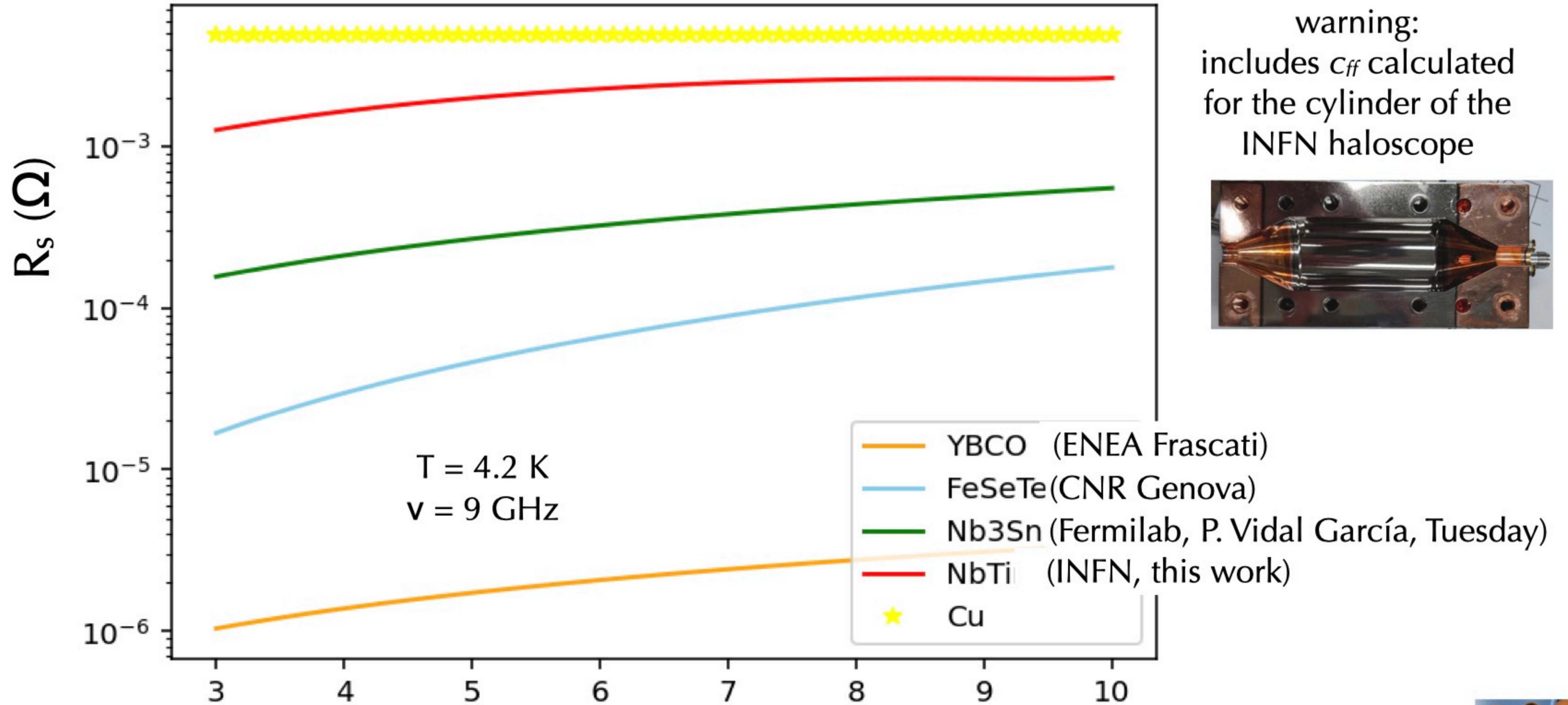
$T = 4.2 \text{ K}$

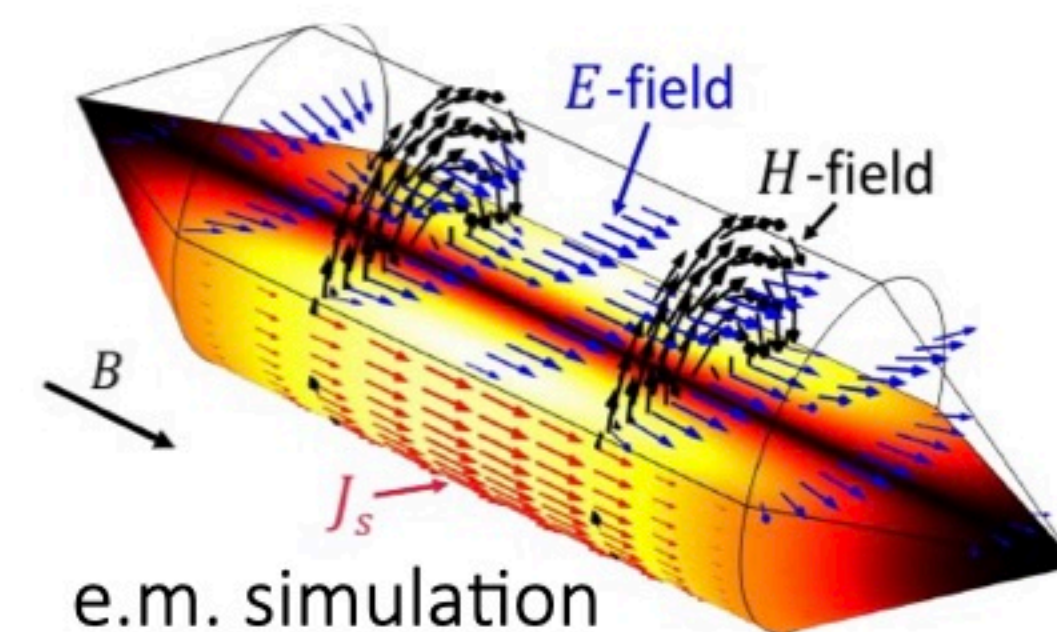
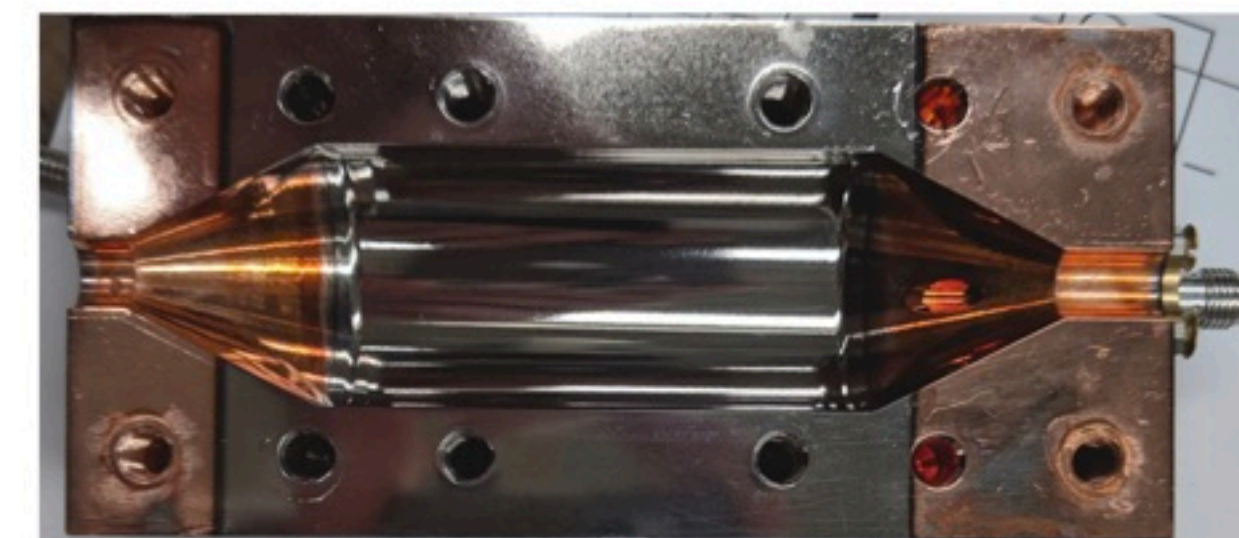
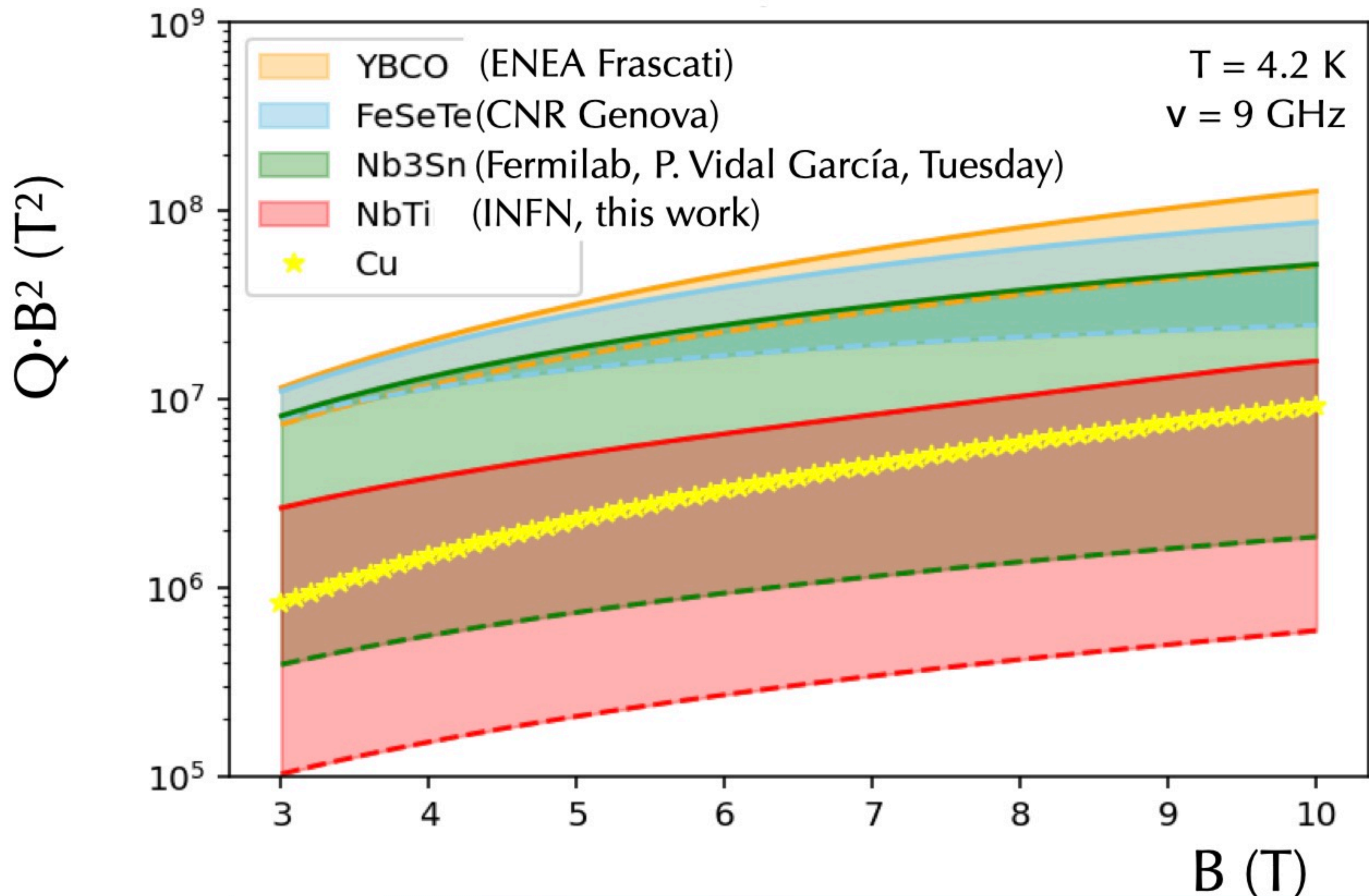
$\nu = 9 \text{ GHz}$

	NbTi	Nb <sub>3</sub> Sn	YBaCuO	Fe(Se,Te)
$c_{ff}$	0.012 (this work)	0.011 (calculated)	0.0042 (calculated)	0.093 (calculated)
$\rho_{ff} (\mu\Omega \cdot \text{cm})$	10	1.2	0.54	3.2
$\nu_0 (\text{GHz})$	1.5	1.3	59	69
$k_p (\text{N} \cdot \text{m}^{-2})$	100	7055	$7.1 \cdot 10^6$	$1.4 \cdot 10^5$
$\frac{1}{1 + (\nu_0/\nu)^2}$	0.973	0.98	0.023	0.017
$\lambda (\text{nm})$	300 (literature)	250 (P. Vidal García, TUE)	150 (ab, literature)	540 (ab, literature)
$R_s (\text{m}\Omega)$	2.1	0.27	0.0017	0.046



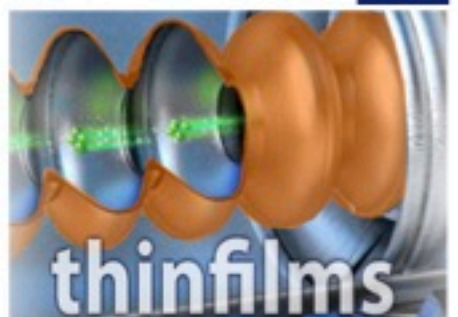
# Comparison of superconductors: $R_s$ vs $B$ - haloscope configuration





# Summary

- dc field: totally different paradigm for RF superconductivity
- to predict/estimate haloscope performances, vortex physics is required...
- ... but it's not sufficient: geometry plays a major role
- the usual (for vortex physics) rule “strong pinning = good, weak pinning = bad” does not necessarily applies.
- ... so that all features (pinning,  $\lambda$ , geometry, operating frequency, ...) should be estimated
- ... as well as the design of the haloscope (cones: are they *really* better if superconducting?)



- dc field: totally different paradigma for RF superconductivity
- to predict/estimate haloscope performances, vortex physics is required...
- ... but it's not sufficient: geometry plays a major role
- the usual (for vortex physics) rule “strong pinng = good, weak pinning = bad” does not necessarily applies.
- all features (pinning,  $\lambda$ , geometry, operating frequency, ...) should be estimated
- ... as well as the design of the haloscope (cones: are they *really* better if superconducting?)

**Thank you for your attention!**

