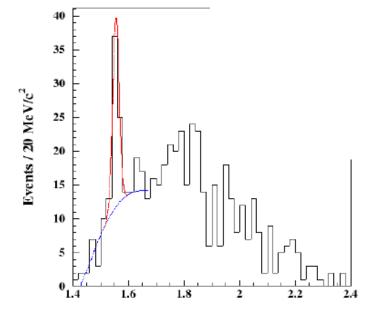
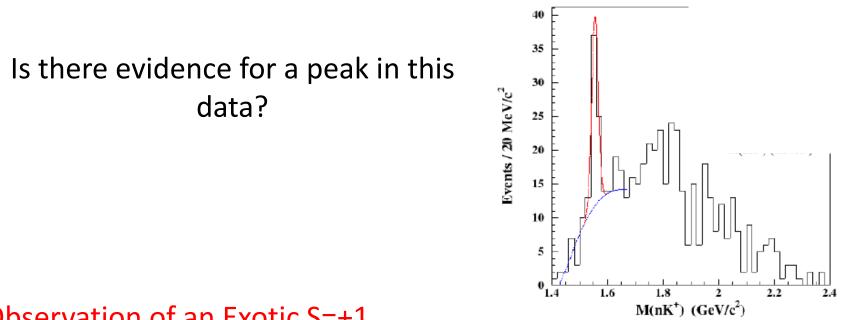
Is there evidence for a peak in this data?



. . . .



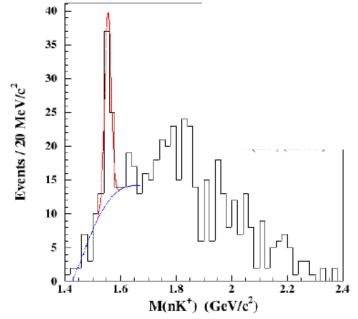
"Observation of an Exotic S=+1

Baryon in Exclusive Photoproduction from the Deuteron"

S. Stepanyan et al, CLAS Collab, Phys.Rev.Lett. 91 (2003) 252001

"The statistical significance of the peak is 5.2 \pm 0.6 $\sigma^{\prime\prime}$

Is there evidence for a peak in this data?



3

"Observation of an Exotic S=+1

Baryon in Exclusive Photoproduction from the Deuteron" S. Stepanyan et al, CLAS Collab, Phys.Rev.Lett. 91 (2003) 252001 "The statistical significance of the peak is $5.2 \pm 0.6 \sigma$ "

"A Bayesian analysis of pentaquark signals from CLAS data"
D. G. Ireland et al, CLAS Collab, Phys. Rev. Lett. 100, 052001 (2008)
"The In(RE) value for g2a (-0.408) indicates weak evidence in favour of the data model without a peak in the spectrum."

Comment on "Bayesian Analysis of Pentaquark Signals from CLAS Data" Bob Cousins, http://arxiv.org/abs/0807.1330

Statistical Issues in Searches for New Physics

Louis Lyons

Oxford & Imperial College, London

CERN School, Sept 2024 Theme: Using data to make judgements about H1 (New Physics) versus H0 (S.M. with nothing new)

Why?

Experiments are expensive and time-consuming so Worth investing effort in statistical analysis → better information from data

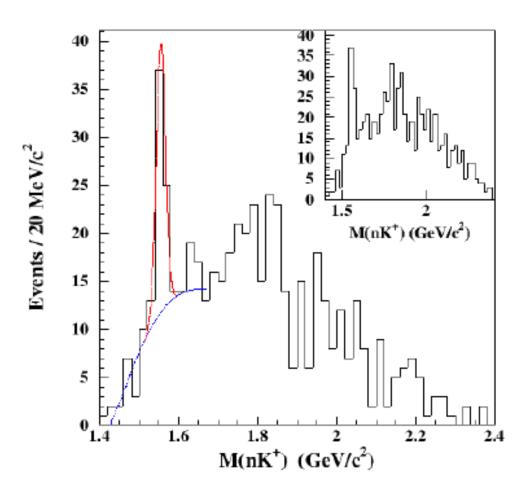
Topics:

Data statistic. p-values. Meaning. $p_0 v p_1$ plots Blind Analysis LEE = Look Elsewhere Effect Why 5 σ for discovery? Significance P(A|B) \neq P(B|A) Wilks' Theorem Blind analyses Background Systematics Coverage Higgs search: Discovery and spin (N.B. Several of these topics have no unique solutions from Statisticians)

Conclusions

Choosing between 2 hypotheses

Hypothesis testing: New particle or statistical fluctuation? H0 = b H1 = b + s



```
2012: H0 = SM
H1 = SM + X, X = H0
```

Meeting at SLAC (2012)

Statistics Cosmo HEP Atomic Ph

```
2012: H0 = SM
H1 = SM + X, X = H0
```

Meeting at SLAC (2012) Value of H0? Statistics Null Hypothesis Cosmo HEP Atomic Phys

```
2012: HO = SM
H1 = SM + X, X = HO
```

Meeting at SLAC (2012) Value of H0? Statistics Null Hypothesis Cosmo 70 km/s/Mpc HEP Atomic Ph

```
2012: H0 = SM
H1 = SM + X, X = H0
```

Meeting at SLAC (2012) Value of H0? Statistics Null Hypothesis Cosmo 70 km/s/Mpc HEP Nobel Prize Atomic Phys

2012: H0 = SM , with particles known at that time. H1 = SM + X, X = H0

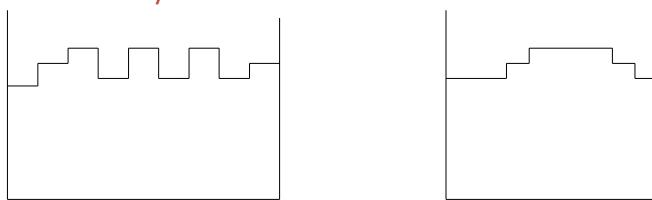
Meeting at SLAC (2012)					
	Value of H0?				
Statistics	Null Hypothesis				
Cosmo	70 km/s/Mpc				
HEP	Nobel Prize				
Atomic Phys	Hydrogen atom = Basis of subject				

HO or HO versus H1?

H0 = null hypothesis

- e.g. Standard Model, with nothing new
- H1 = specific New Physics e.g. Higgs with M_{H} = 125 GeV
- H0: "Goodness of Fit" e.g. χ^2 , p-values
- H0 v H1: "Hypothesis Testing" e.g. *L*-ratio (Remember Neyman-Pearson)
- Measures how much data favours one hypothesis wrt other
- H0 ~ Model Independent H0 v H1 = Model Specific

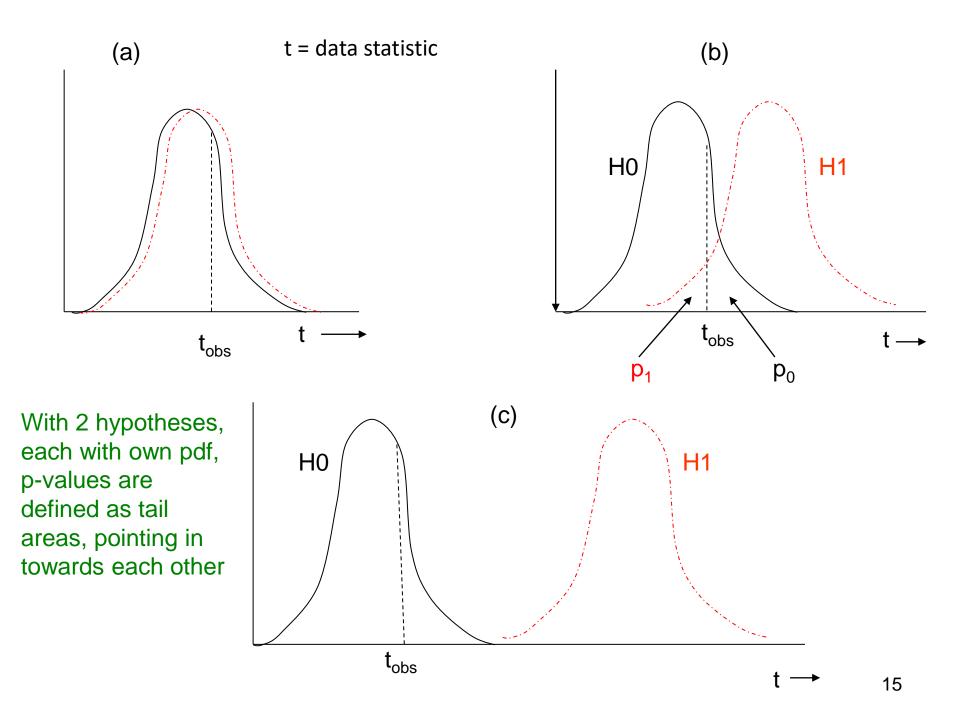
H0 v H1 likely to be more sensitive for H1



Choosing between 2 hypotheses

Possible methods:

 $\Delta \chi^2$ p-value of statistic \rightarrow *In***L**–ratio Bayesian: Posterior odds **Bayes** factor Bayes information criterion (BIC) Akaike (AIC) Minimise "cost" ML methods – See Troels Peterson's talks See 'Comparing two hypotheses' http://www-cdf.fnal.gov/physics/statistics/notes/H0H1.pdf





Concept of pdf Example: Gaussian $\begin{array}{c|c}
\uparrow \\
y \\
\mu \\ x_0 \\ x \\
\end{array}$

y = probability density for measurement x

y =
$$1/(\sqrt{(2\pi)\sigma}) \exp\{-0.5*(x-\mu)^2/\sigma^2\}$$

p-value: probablity that $x \ge x_0$

Gives probability of "extreme" values of data (in interesting direction)

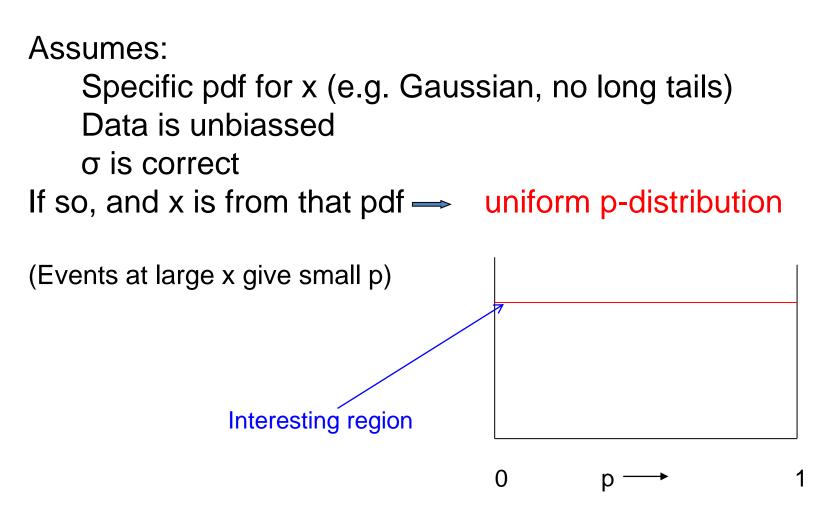
$(x_0-\mu)/\sigma$	1	2	3	4	5
p p	16%	2.3%	0.13%	0.003%	$0.3*10^{-6}$

i.e. Small p = unexpected

p-values for non-Gaussian distributions

e.g. Poisson counting experiment, bgd = b $P(n) = e^{-b} * b^{n}/n!$ {P = probability, not prob density} ₩ ₩ b=2.9 Ρ 0 10 n

p-values, contd



p-values and σ

p-values often converted into equivalent Gaussian σ e.g. $3*10^{-7}$ is " 5σ " (one-sided Gaussian tail) Does NOT imply that pdf = Gaussian (Simply easier to remember number of σ , than p-value.)

Combining different p-values

Several results quote independent p-values for same effect:

p₁, p₂, p₃.... e.g. 0.9, 0.001, 0.3

What is combined significance? Not just $p_{1*}p_{2*}p_{3}$

If 10 expts each have p ~ 0.5, product ~ 0.001 and is clearly **NOT** correct combined p

$$S = z * \sum_{i=0}^{n-1} (-\ln z)^{j} / j! , \quad z = p_1 p_2 p_3$$

(e.g. For 2^{-5} measurements, S = z $(1 - \ln z) \ge z$)

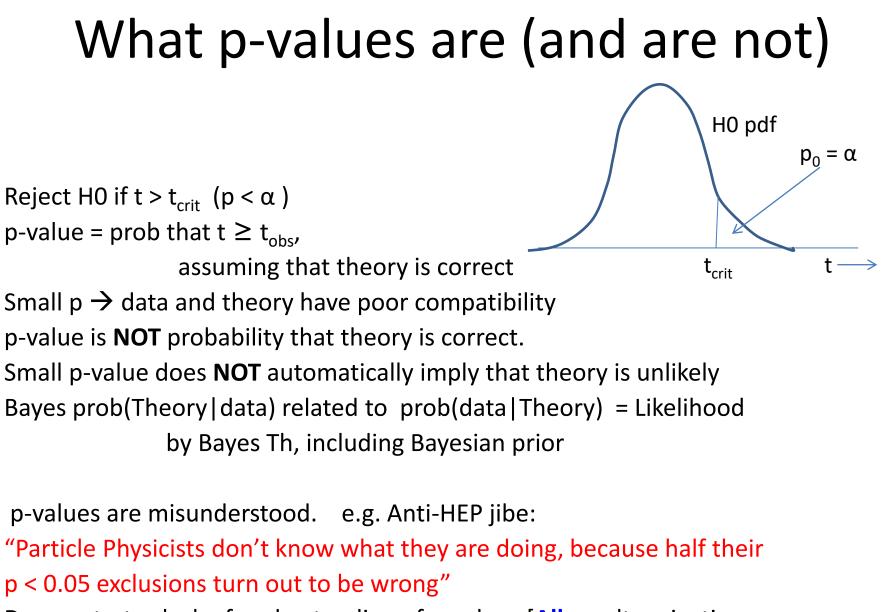
Problems:

Recipe is not unique (Uniform dist in n-D hypercube → uniform in 1-D)
 Formula is not associative

Combining {{p₁ and p₂}, and then p₃} gives different answer

from {{ p_3 and p_2 }, and then p_1 }, or all together Due to different options for "more extreme than x_1 , x_2 , x_3 ". 3) Small p's due to different discrepancies

****** Better to combine data ***********



Demonstrates lack of understanding of p-values [All results rejecting energy conservation with $p < \alpha = .05$ cut will turn out to be 'wrong'] p-values banned in some fields!

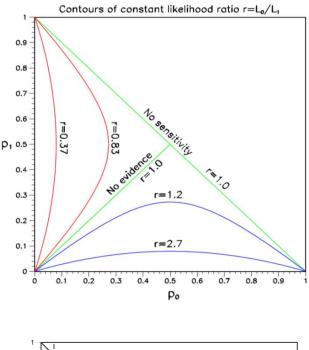
$p_0 v p_1 plots$

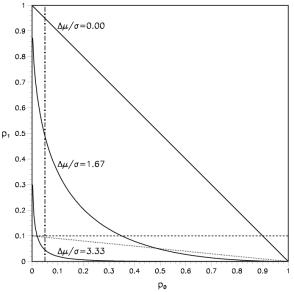
Preprint by Luc Demortier and LL, "Testing Hypotheses in Particle Physics: Plots of p₀ versus p₁" http://arxiv.org/abs/1408.6123

For hypotheses H0 and H1, p_0 and p_1 are the tail probabilities for data statistic t

Provide insights on:

CLs for exclusion Punzi definition of sensitivity **Relation of p-values and Likelihoods** Probability of misleading evidence Jeffreys-Lindley paradox

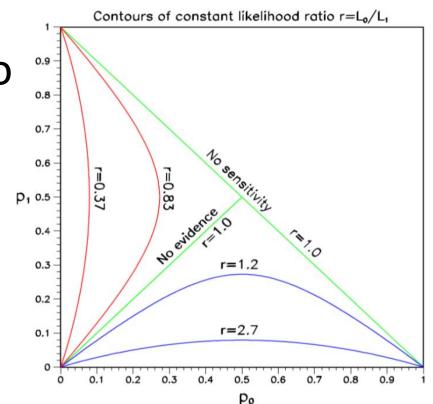




Why $p \neq$ Likelihood ratio

Measure different things: p_0 refers just to H0; \mathcal{L}_{01} compares H0 and H1

Depends on amount of data: 0.1 e.g. Poisson counting expt little data: 0 0.1 For H0, $\mu_0 = 1.0$. For H1, $\mu_1 = 10.0$ Observe n = 10 $p_0 \simeq 10^{-7}$ $\mathcal{L}_{01} \simeq 10^{-5}$ Now with 100 times as much data, $\mu_0 = 100.0$ $\mu_1 = 1000.0$ Observe n = 160 $p_0 \simeq 10^{-7}$ $\mathcal{L}_{01} \simeq 10^{+14}$

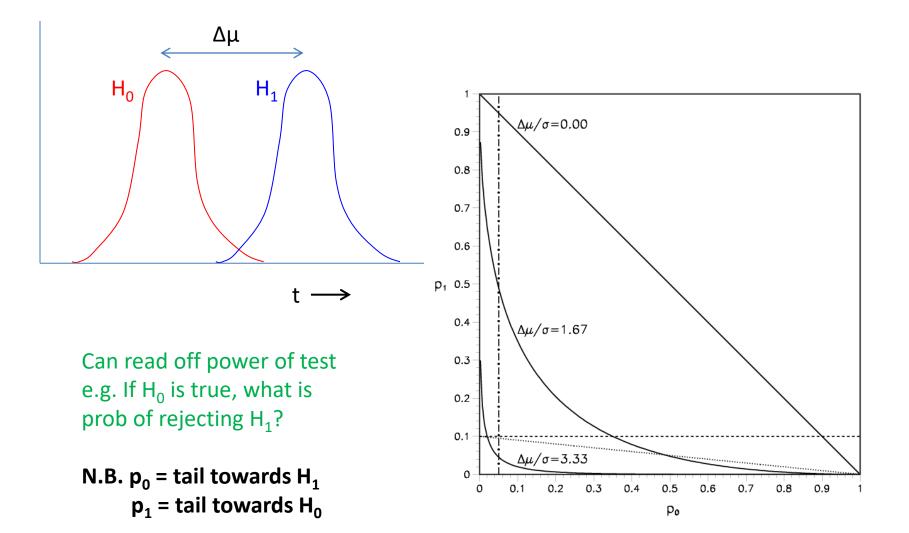


or

N.B. In HEP, data statistic is typically \mathcal{L}_{01} Can think of method as: p-value, where data statistic just happens to be \mathcal{L}_{01} ; \mathcal{L}_{01} method where p-values are just used for calibration. $CLs = p_1/(1-p_0) \rightarrow diagonal line$

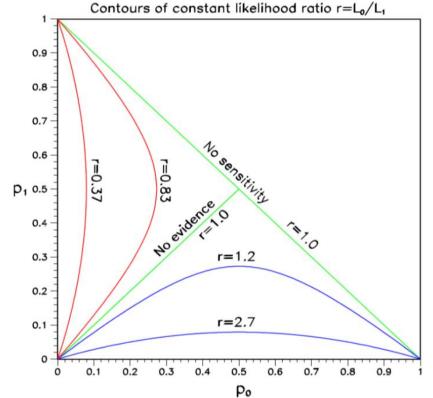
Provides protection against excluding H₁ when little or no sensitivity

Punzi definition of sensitivity: Enough separation of pdf's for no chance of ambiguity



Jeffreys-Lindley Paradox

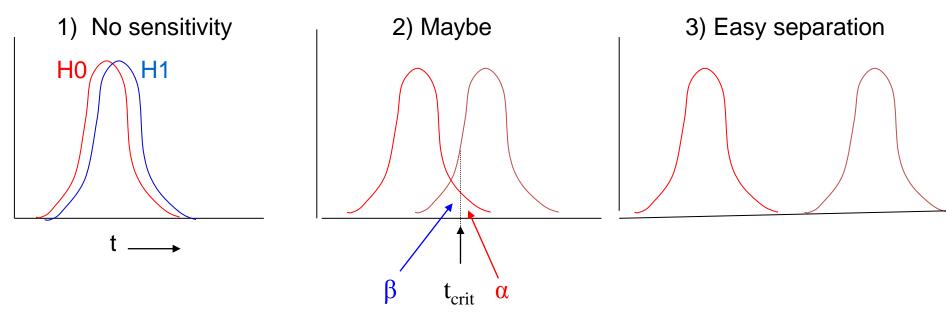
H0 = simple, H1 has μ free p₀ can favour H₁, while B₀₁ can favour H₀ B₀₁ = L₀ / $\int L_1(s) \pi(s) ds$



Likelihood ratio depends on signal : e.g. Poisson counting expt small signal s: For H₀, $\mu_0 = 1.0$. For H₁, $\mu_1 = 10.0$ Observe n = 10 $p_0 \sim 10^{-7}$ $L_{01} \sim 10^{-5}$ and favours H₁ Now with 100 times as much signal s, $\mu_0 = 100.0$ $\mu_1 = 1000.0$ Observe n = 160 $p_0 \sim 10^{-7}$ $L_{01} \sim 10^{+14}$ and favours H₀

 B_{01} involves intergration over s in denominator, so a wide enough range will result in favouring H_0 However, for B_{01} to favour H_0 when p_0 is equivalent to 5σ , integration range for s has to be O(10⁶) times Gaussian widths

Frequentist procedure to choose between 2 hypotheses



Procedure: Obtain expected distributions for data statistic (e.g. \mathcal{L} -ratio) for H0 and H1 Choose α (e.g. 95%, 3 σ , 5 σ ?) and CL for p_1 (e.g. 95%) Given b, α determines t_{crit} b+s defines β . For s > s_{min}, separation of curves \rightarrow discovery or excln $1-\beta = Power \text{ of test}$ Now data: If $t_{obs} \ge t_{crit}$ (i.e. $p_0 \le \alpha$), discovery at level α If $t_{obs} < t_{crit}$, no discovery. If $p_1 < 1-CL$, exclude H1

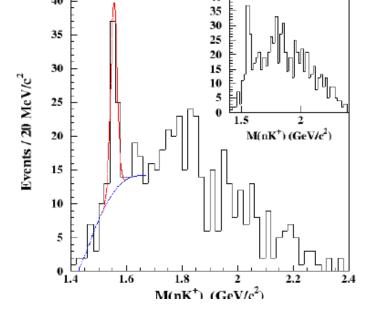
- Prob of bgd fluctuation at that place = local p-value Prob of bgd fluctuation 'anywhere' = global p-value Global p > Local p
- Where is `anywhere'?
- a) Any location in this histogram in sensible range
- b) Any location in this histogram
- c) Also in histogram produced with different cuts, binning, etc.
- d) Also in other plausible histograms for this analysis
- e) Also in other searches in this PHYSICS group (e.g. SUSY at CMS)
- f) In any search in this experiment (e.g. CMS)
- g) In all CERN expts (e.g. LHC expts + NA62 + OPERA + ASACUSA +)
- h) In all HEP expts

etc.

- d) relevant for graduate student doing analysis
- f) relevant for experiment's Spokesperson

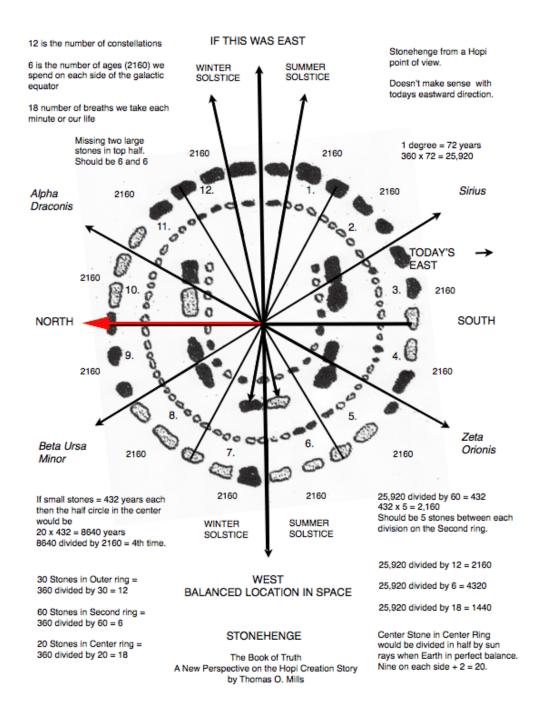
INFORMAL CONSENSUS:

Quote local p, and global p according to a) above. Explain which global p



Example of LEE: Stonehenge





Are alignments significant?

- Atkinson replied with his article "Moonshine on Stonehenge" in <u>Antiquity</u> in 1966, pointing out that some of the pits which had used for his sight lines were more likely to have been natural depressions, and that he had allowed a margin of error of up to 2 degrees in his alignments. Atkinson found that the probability of so many alignments being visible from 165 points to be close to 0.5 rather that the "one in a million" possibility which had claimed.
- had been examining stone circles since the 1950s in search of astronomical alignments and the <u>megalithic yard</u>. It was not until 1973 that he turned his attention to Stonehenge. He chose to ignore alignments between features within the monument, considering them to be too close together to be reliable. He looked for landscape features that could have marked lunar and solar events. However, one of's key sites, Peter's Mound, turned out to be a twentieth-century rubbish dump.

Why 5σ for Discovery?

Statisticians ridicule our belief in extreme tails (esp. for systematics) Our reasons:

- 1) Past history (Many 3σ and 4σ effects have gone away)
- 2) LEE (see earler)
- 3) Worries about underestimated systematics
- 4) Subconscious Bayes calculation

 $\frac{p(H_1|x)}{p(H_0|x)} = \frac{p(x|H_1)}{p(x|H_0)} * \frac{\pi(H_1)}{\pi(H_0)}$ $\frac{p(H_0|x)}{p(x|H_0)} = \frac{p(x|H_1)}{\pi(H_0)} * \frac{\pi(H_1)}{\pi(H_0)}$ $\frac{p(H_1|x)}{p(x|H_0)} = \frac{p(x|H_1)}{\pi(H_0)} * \frac{\pi(H_1)}{\pi(H_0)}$ $\frac{p(H_1|x)}{p(H_0|x)} = \frac{p(x|H_1)}{p(x|H_0)} * \frac{\pi(H_1)}{\pi(H_0)}$

"Extraordinary claims require extraordinary evidence"

N.B. Points 2), 3) and 4) are experiment-dependent

Alternative suggestion:

L.L. "Discovering the significance of 5σ " http://arxiv.org/abs/1310.1284

How many σ 's for discovery?

SEARCH	SURPRISE	ΙΜΡΑϹΤ	LEE	SYSTEMATICS	Νο. σ
Higgs search	Medium	Very high	Μ	Medium	5
Single top	No	Low	No	No	3
SUSY	Yes	Very high	Very large	Yes	7
B _s oscillations	Medium/Low	Medium	Δm	No	4
Neutrino osc	Medium	High	sin²2ϑ, Δm²	No	4
$B_s \rightarrow \mu \mu$	No	Low/Medium	No	Medium	3
Pentaquark	Yes	High/V. high	M, decay mode	Medium	7
(g-2) _µ anom	Yes	High	No	Yes	4
H spin ≠ 0	Yes	High	No	Medium	5
4 th gen q, l, v	Yes	High	M, mode	No	6
Dark energy	Yes	Very high	Strength	Yes	5
Grav Waves	No	High	Enormous	Yes	8

Suggestions to provoke discussion, rather than `delivered on Mt. Sinai'/

Bob Cousins: "2 independent expts each with 3.5 obtter than one expt with 5 o"

'Discoveries' that don't need 5σ

- When H0 is not preferred.
- When no LEE.
- For example:
 - Muon anomalous magnetic moment
 - No $H^0 \rightarrow \mu^+ \mu^-$
 - No di-H⁰ production
 - Choice of neutrino mass hierarchy



Significance = S/\sqrt{B} or similar ?

Potential Problems:

- Uncertainty in B
- •Non-Gaussian behaviour of Poisson, especially in tail
- •Number of bins in histogram, no. of other histograms [LEE]
- •Choice of cuts, bins (Blind analyses)

For future experiments:

• Optimising: Could give S =0.1, B = 10^{-4} , S/ \sqrt{B} = 10

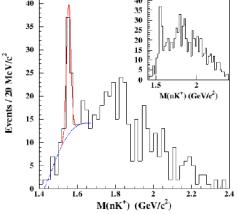
Wilks' Theorem

Data = some distribution e.g. mass histogram For H0 and H1, calculate best fit weighted sum of squares S_0 and S_1 Examples: 1) H0 = polynomial of degree 3H1 = polynomial of degree 52) H0 = background only 35 30 H1 = bgd+peak with free M_0 and cross-section Events / 20 MeV/c² 25 3) H0 = normal neutrino hierarchy 20 15 H1 = inverted hierarchy10 1.6 If H0 true, S₀ distributed as χ^2 with ndf = v_0 If H1 true, S₁ distributed as χ^2 with ndf = v_1

If H0 true, what is distribution of $\Delta S = S_0 - S_1$? Expect not large. Is it χ^2 ?

Wilks' Theorem: ΔS distributed as χ^2 with ndf = $v_0 - v_1$ provided:

- a) H0 is true
- b) H0 and H1 are nested
- c) Params for H1 \rightarrow H0 are well defined, and not on boundary
- d) Data is asymptotic



Wilks' Theorem, contd

Examples: Does Wilks' Th apply?

1) H0 = polynomial of degree 3

H1 = polynomial of degree 5

YES: Δ S distributed as χ^2 with ndf = (d-4) – (d-6) = 2

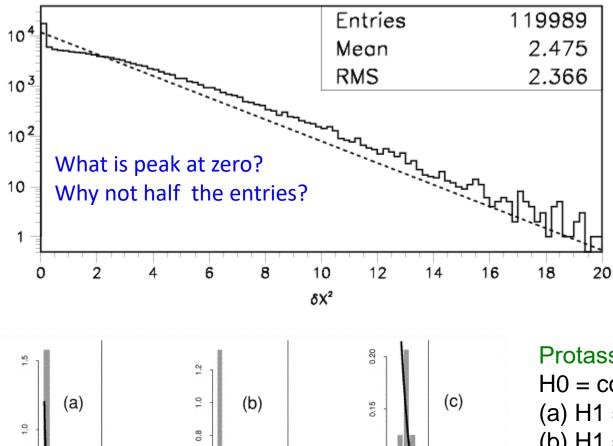
2) H0 = background only H1 = bgd + peak with free M₀ and cross-section NO: H0 and H1 nested, but M₀ undefined when H1 \rightarrow H0. $\Delta S \neq \chi^2$ (but not too serious for fixed M)

3) H0 = normal neutrino hierarchy H1 = inverted hierarchy NO: Not nested. $\Delta S \neq \chi^2$ (e.g. can have $\Delta \chi^2$ negative)

N.B. 1: Even when W. Th. does not apply, it does not mean that ΔS is irrelevant, but you cannot use W. Th. for its expected distribution.

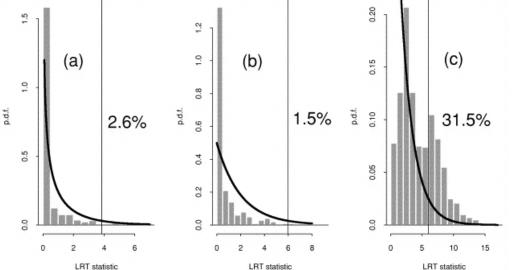
N.B. 2: Especially for large ndf, better to use ΔS , rather than S_1 and S_0 separately

Is difference in S distributed as χ^2 ?



Demortier: H0 = quadratic bgd H1 = + Gaussian of fixed width,

variable location & ampl



Protassov, van Dyk, Connors, H0 = continuum (a) H1 = narrow emission line

- (b) H1 = wider emission line
- (c) H1 = absorption line

Nominal significance level = 5%

Is difference in S distributed as χ^2 ?, contd.

So need to determine the ΔS distribution by Monte Carlo

N.B.

- 1) For mass spectrum, determining ΔS for hypothesis H1 when data is generated according to H0 is not trivial, because there will be lots of local minima
- If we are interested in 5σ significance level, needs lots of MC simulations (or intelligent MC generation)
- 3) Asymptotic formulae may be useful (see K. Cranmer, G. Cowan, E. Gross and O. Vitells, 'Asymptotic formulae for likelihood-based tests of new physics', <u>http://link.springer.com/article/10.1140%2Fepjc%2Fs10052-011-1554-0</u>)

BLIND ANALYSES

Why blind analysis? Data statistic, selections, corrections, method

Methods of blinding Add random number to result * Study procedure with simulation only Look at only first fraction of data Keep the signal box closed Keep MC parameters hidden Keep unknown fraction visible for each bin

Disadvantages Takes longer time Usually not available for searches for unknown

After analysis is unblinded, don't change anything unless

Luis Alvarez suggestion re "discovery" of free quarks

SYSTEMATICS

Uncertainties:

Statistical: Limited accuracy of measurements Poisson fluctuations on counts Results vary for repetitions Uncertainties decrease with more data Systematics: Uncertain calibrations Uncontrolled effects Mis-modelling Formulae not relevant Results stay biased for repetitions 'No' reduction of systematics with more data Most relevant for later stages of analysis as more data are collected early stages of analysis when calibrations are not so good.

Usually small number of 'Params of Interest', but can be thousands of 'Nuisance Params' for systematics.

If you are not spending a lot more time on estimating systematics than on statistical uncertainties, something is wrong.

Quote result as $x \pm \sigma_{stat} \pm \sigma_{syst}$

Systematics

- PHYSTAT-Systematics Wokshop:
- <u>https://indico.cern.ch/event/1051224/</u>

- Talks on Systematics at other Workshops, e.g.
- Kyle Cranmer "Systematics: Misery or Muse?" at "Statstistics meets ML" (Sept 2024):

https://indico.cern.ch/event/1407421/timetable/?view=standard

Incorporating systematics

Many methods, e.g:

Move nuisance parameter v associated with systematic (e.g. jet energy scale), and see how much answer s (e.g. M_{top}) changes.

With information on v from subsidiary measurement, expand Likelihood to get $\mathcal{L}(s, v)$. Then 'profile' over v.

Bayesian equiv: Get Posterior $P(s,v) = \mathcal{L}(s, v)^* \Pi(s, v)$, and then 'marginalize' over v.

Reminder of Profile ${\cal L}$

Stat uncertainty on s from width of $\boldsymbol{\mathcal{L}}$ fixed at υ_{best}

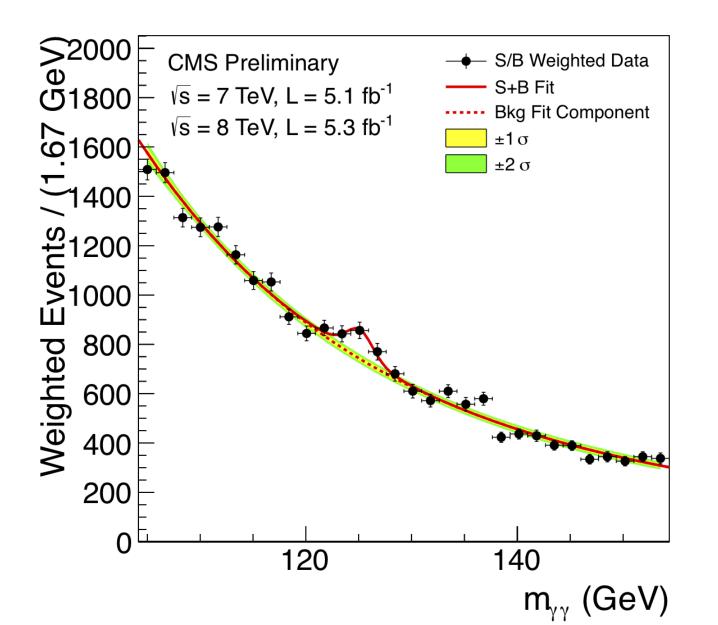
Total uncertainty on s from width of $\mathcal{L}(s, v_{\text{prof}(s)}) = \mathcal{L}_{\text{prof}}(s)$ $v_{\text{prof}(s)}$ is best value of v at that s $v_{\text{prof}(s)}$ as fn of s lies on green line

Contours of $ln \mathcal{L}(s, v)$ s = physics param v = nuisance param S

υ

Total uncert \geq stat uncertainty

Background systematics



Background systematics, contd

Signif from comparing χ^{2} 's for H0 (bgd only) and for H1 (bgd + signal)

Typically, bgd = functional form f_a with free params

e.g. 4th order polynomial

Uncertainties in params included in signif calculation

```
But what if functional form is different ? e.g. f<sub>b</sub>
```

Typical approach:

If f_b best fit is bad, not relevant for systematics

If f_b best fit is ~comparable to f_a fit, include contribution to systematics But what is '~comparable'?

Other approaches:

```
Profile likelihood over different bgd parametric forms
http://arxiv.org/pdf/1408.6865v1.pdf?
Background subtraction
sPlots
Non-parametric background
Bayes
```

etc

No common consensus yet among experiments on best approach {Spectra with multiple peaks are more difficult}

"Handling uncertainties in background shapes: the discrete profiling method"

Dauncey, Kenzie, Wardle and Davies (Imperial College, CMS) <u>arXiv:1408.6865v1</u> [physics.data-an] Has been used in CMS analysis of $H \rightarrow \gamma \gamma$

Problem with 'Typical approach': Alternative functional forms do or don't contribute to systematics by hard cut, so systematics can change discontinuously wrt $\Delta\chi^2$

Method is like profile \mathcal{L} for continuous nuisance params Here 'profile' over discrete functional forms

Reminder of Profile ${\cal L}$

Stat uncertainty on s from width of $\boldsymbol{\mathcal{L}}$ fixed at υ_{best}

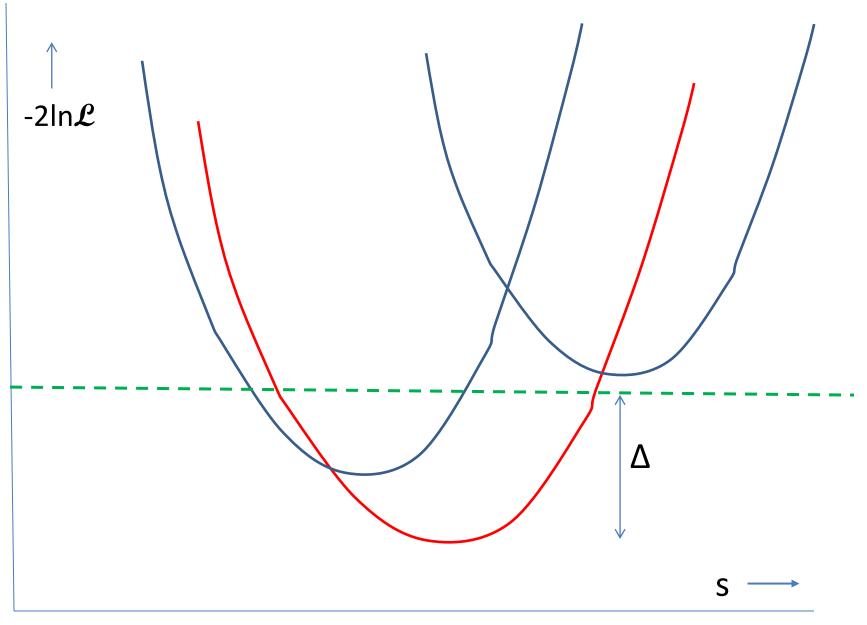
Total uncertainty on s from width of $\mathcal{L}(s, v_{\text{prof}(s)}) = \mathcal{L}_{\text{prof}}(s)$ $v_{\text{prof}(s)}$ is best value of v at that s $v_{\text{prof}(s)}$ as fn of s lies on green line

Contours of $ln \mathcal{L}(s, v)$ s = physics param v = nuisance param

S

υ

Total uncert \geq stat uncertainty



Red curve: Best value of nuisance param vBlue curves: Other values of vHorizontal line: Intersection with red curve \rightarrow statistical uncertainty

'Typical approach': Decide which blue curves have small enough Δ Systematic is largest change in minima wrt red curves'.

Profile L: Envelope of lots of blue curves Wider than red curve, because of systematics (υ) For \mathcal{L} = multi-D Gaussian, agrees with 'Typical approach'

Dauncey et al use envelope of finite number of functional forms

Point of controversy!
Two types of 'other functions':
a) Different function types e.g. Σa_i x_i versus Σa_i/x_i
b) Given fn form but different number of terms
DDKW deal with b) by -2lnL → -2lnL + kn

n = number of extra free params wrt best

k = 1, as in AIC (= Akaike Information Criterion)

Opposition claim choice k=1 is arbitrary.

DDKW agree but have studied different values, and say k =1 is optimal for them.

Also, any parametric method needs to make such a choice

WHY LIMITS?

Michelson-Morley experiment \rightarrow death of aether

HEP experiments: If UL on expected rate for new particle < expected, exclude particle

CERN CLW (Jan 2000) FNAL CLW (March 2000) Heinrich, PHYSTAT-LHC, "Review of Banff Challenge"

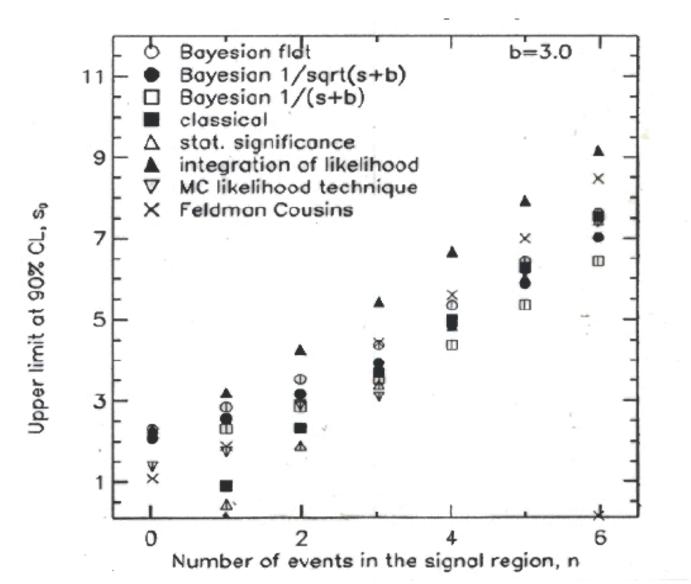
Methods (no systematics)

Bayes (needs priors e.g. const, $1/\mu$, $1/\sqrt{\mu}$, μ ,) Frequentist (needs ordering rule, possible empty intervals, F-C) Likelihood (DON'T integrate your L) $\chi^2 (\sigma^2 = \mu)$ $\chi^2 (\sigma^2 = n)$

Recommendation 7 from CERN CLW: "Show your L"
1) Not always practical
2) Not sufficient for frequentist methods

Ilya Narsky, FNAL CLW 2000

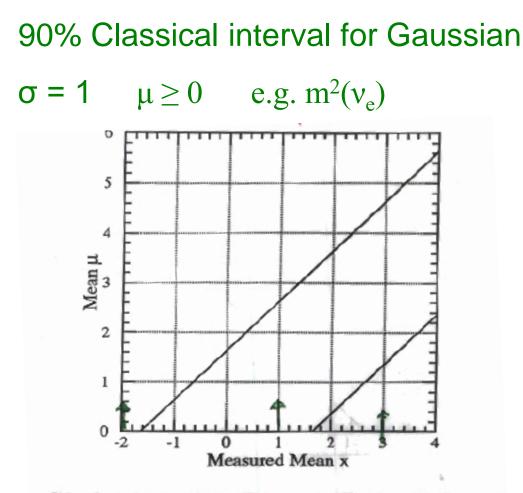
Counting expt. Observe n. Expected bgd b. Calculate UL

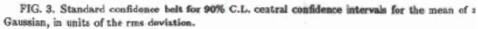


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DESIRABLE PROPERTIES

- Coverage
- Interval length, but
- Behaviour when n < b
- Limit increases as σ_b increases
- Unified with discovery and interval estimation





$X_{obs} = 3$	Two-sided range
$X_{obs} = 1$	Upper limit
X _{obs} =-2	No region for μ

FELDMAN - COUSINS

Wants to avoid empty classical intervals \rightarrow

Uses "L-ratio ordering principle" to resolve
 ambiguity about "which 90% region?"
 [Neyman + Pearson say L-ratio is best for
 hypothesis testing]

Unified \rightarrow No 'Flip-Flop' problem

Classical (Neyman) Confidence Intervals

Uses only P(data|theory)

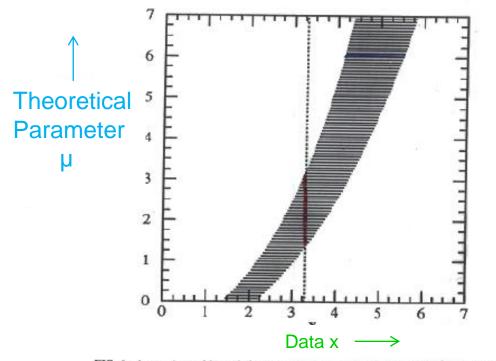


FIG. 1. A generic confidence belt construction and its use. For each value of μ , one draws a horizontal acceptance interval $[x_1, x_2]$ such that $P(x \in [x_1, x_2] | \mu) = \alpha$. Upon performing an experiment to measure x and obtaining the value x_0 , one draws the dashed vertical line through x_0 . The confidence interval $[\mu_1, \mu_2]$ is the union of all values of μ for which the corresponding acceptance interval is intercepted by the vertical line.

Example:

Param = Temp at centre of Sun

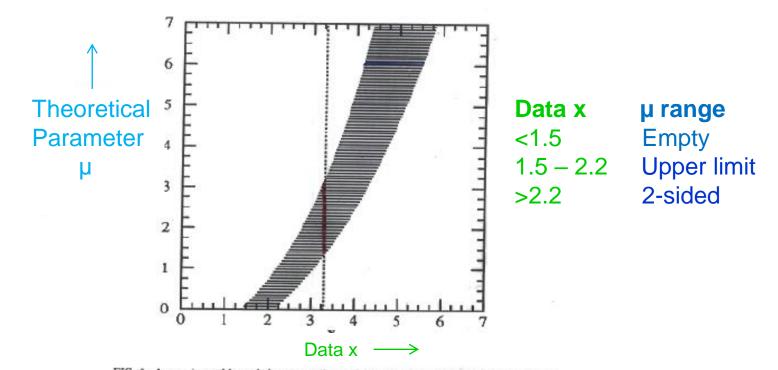
Data = Est. flux of solar neutrinos

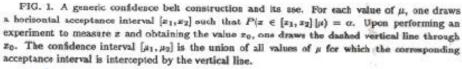
$Prob(\mu_l < \mu < \mu_u) = \alpha$

No prior for μ

Classical (Neyman) Confidence Intervals

Uses only P(data|theory)





Example:

Param = Temp at centre of Sun Data = est. flux of solar neutrinos

No prior for μ



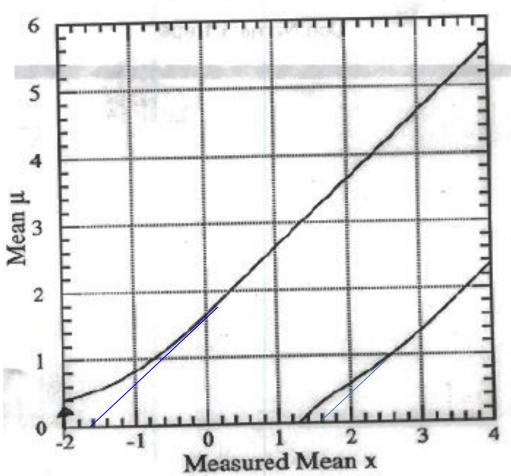


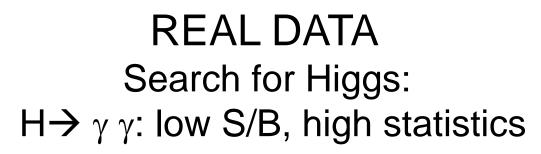
FIG. 10. Plot of our 90% confidence intervals for mean of a Gaussian, constrained to be non-negative, described in the text.

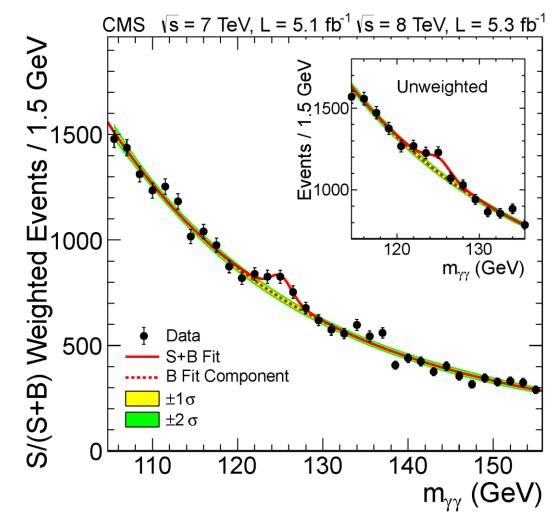
GENERAL COMMENT ABOUT PARAMETERS, DISCOVERY, EXCLUSION......

As well as quoting your result, it is also important to present 'expected result' (slightly ambiguous)

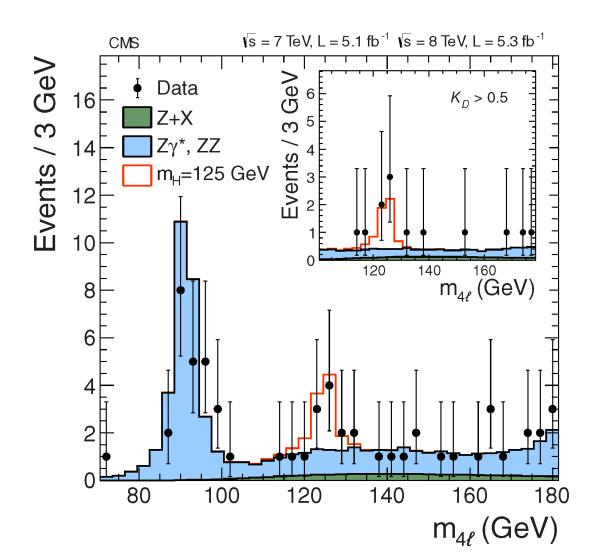
Important to justify proposal for analysis, experiment, accelerator....

Also useful for checking that actual result is reasonable; and for comparing sensitivities of competing experiments.

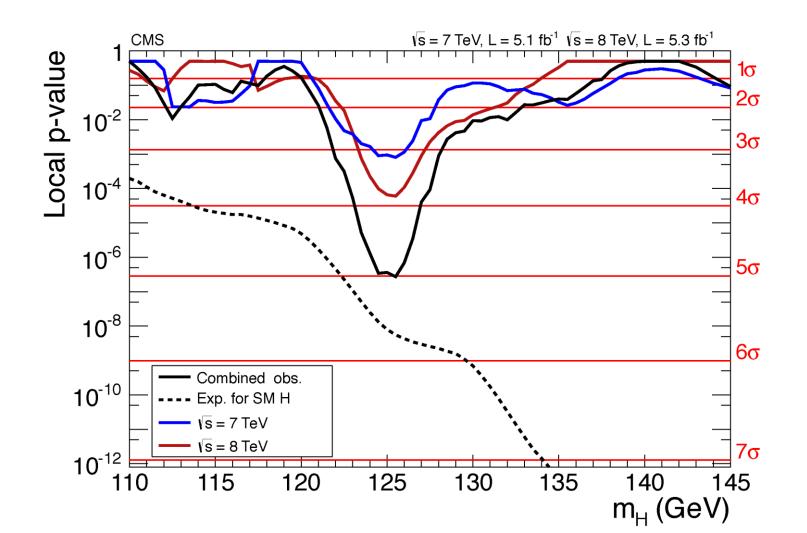




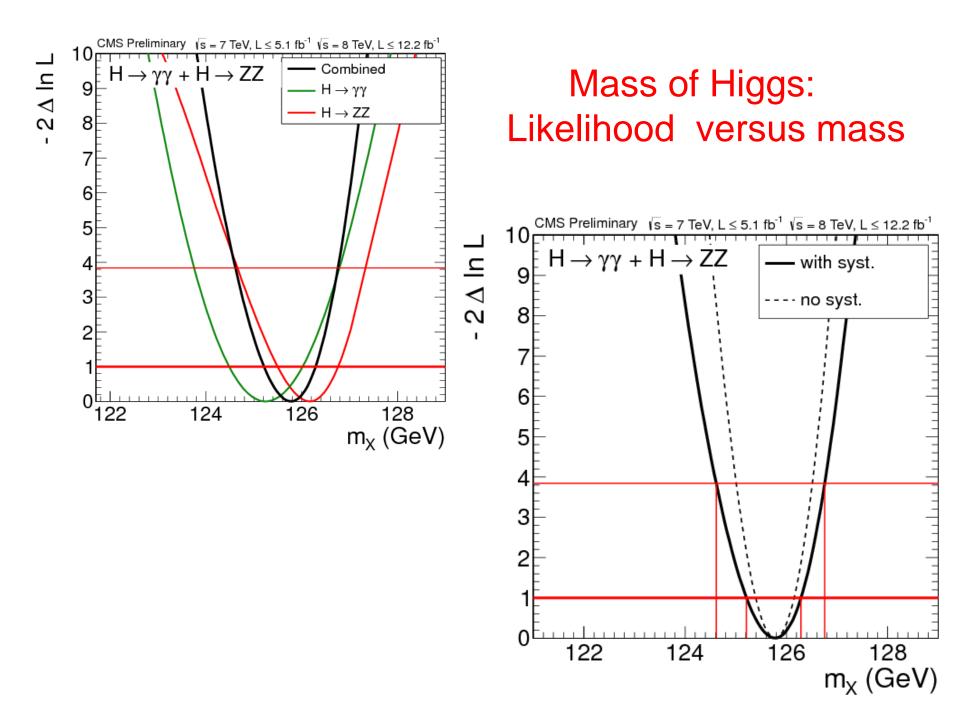
$H \rightarrow Z Z \rightarrow 4$ I: high S/B, low statistics



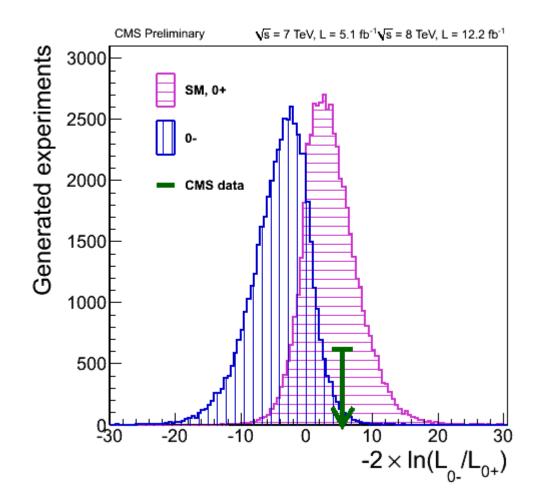
p-value for 'No Higgs' versus m_H



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Comparing O⁺ versus O⁻ for Higgs (like Neutrino Mass Hierarchy)



http://cms.web.cern.ch/news/highlights-cms-results-presented-hcp

Conclusions

Resources:

Software exists: e.g. RooStats

Books exist: Barlow, Cowan, James, Lista, Lyons, Roe,.....

`Data Analysis in HEP: A Practical Guide to Statistical Methods', Behnke et al. PDG sections on Prob, Statistics, Monte Carlo

CMS and ATLAS have Statistics Committees (and BaBar and CDF earlier) – see their websites

PHYSTAT meetings: https://phystat.github.io/Website/

Before re-inventing the wheel, try to see if Statisticians have already found a solution to your statistics analysis problem.

Don't use a square wheel if a circular one already exists.

"Good luck"

