

QCD (for Colliders)

Lecture 3

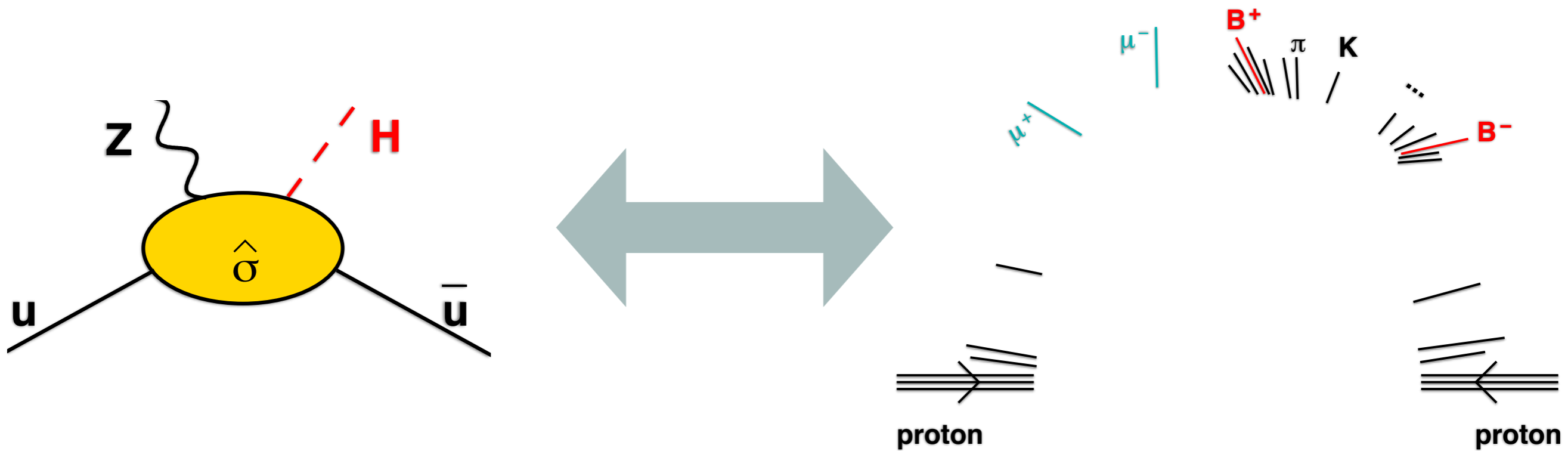
Gavin Salam

University of Oxford, All Souls College & Department of Physics

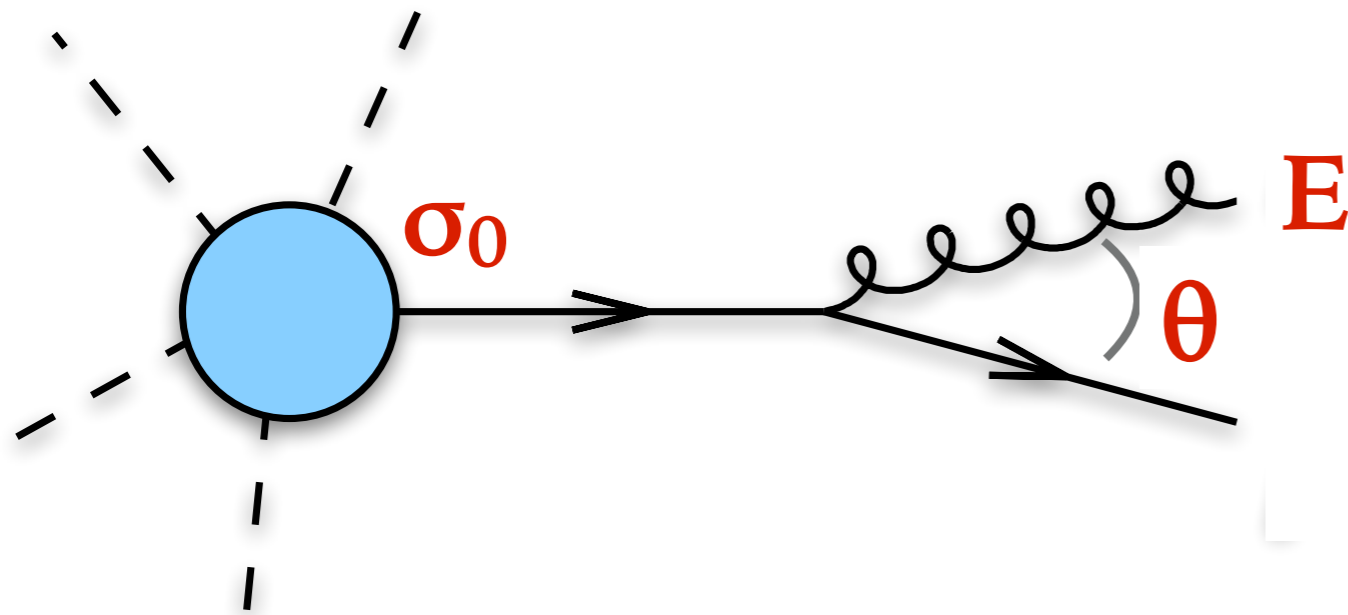
2024 European School of High-Energy Physics

Peebles, Scotland, September 2024

the real world?



GLUON EMISSION FROM A QUARK



Consider an emission with

- ▶ energy $E \ll \sqrt{s}$ (“soft”)
- ▶ angle $\theta \ll 1$
 (“collinear” wrt quark)

Examine correction to
some hard process with
cross section σ_0

$$d\sigma \simeq \sigma_0 \times \frac{2\alpha_s C_F}{\pi} \frac{dE}{E} \frac{d\theta}{\theta}$$

This has a divergence when $E \rightarrow 0$ or $\theta \rightarrow 0$
[in some sense because of quark propagator going on-shell]

Suppose we're not inclusive — e.g. calculate probability of emitting a gluon

Probability P_g of emitting gluon from a quark with energy Q :

$$P_g \simeq \frac{2\alpha_s C_F}{\pi} \int^Q \frac{dE}{E} \int^1 \frac{d\theta}{\theta} \Theta(E\theta > Q_0)$$

We cut off the integral for transverse momenta ($p_T \simeq E\theta$) below some non-perturbative threshold Q_0 .

*On the grounds that perturbation theory doesn't apply for $p_T \sim \Lambda_{\text{QCD}}$
i.e. language of quarks and gluons becomes meaningless*

With this cutoff, the result is

$$P_g \simeq \frac{\alpha_s C_F}{\pi} \ln^2 \frac{Q}{Q_0} + \mathcal{O}(\alpha_s \ln Q)$$

this is called a “double logarithm”
[it crops up all over the place in QCD]

Suppose we're not inclusive — e.g. calculate probability of emitting a gluon

Probability P_g of emitting gluon from a quark with energy Q :

$$P_g \simeq \frac{2\alpha_s C_F}{\pi} \int_{Q_0}^Q \frac{dE}{E} \int_{\frac{Q_0}{E}}^1 \frac{d\theta}{\theta}$$

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Suppose we're not inclusive — e.g. calculate probability of emitting a gluon

Suppose we take $Q_0 \sim \Lambda_{\text{QCD}}$, what do we get?

Let's use $\alpha_s = \alpha_s(Q) = 1/(2b \ln Q/\Lambda)$

[Actually over most of integration range this is optimistically small]

$$P_g \simeq \frac{\alpha_s C_F}{\pi} \ln^2 \frac{Q}{Q_0} \rightarrow \frac{C_F}{2b\pi} \ln \frac{Q}{\Lambda_{\text{QCD}}} \rightarrow \frac{C_F}{4b^2\pi \alpha_s}$$

Put in some numbers:

$Q = 100 \text{ GeV}$, $\Lambda_{\text{QCD}} \simeq 0.2 \text{ GeV}$, $C_F = 4/3$, $b(\equiv b_0) \simeq 0.6$

$$P_g \simeq 2.2$$

This is supposed to be an $O(\alpha_s)$ correction.

But the final result $\sim 1/\alpha_s$

QCD hates to not emit gluons!

correct way of doing it: with running coupling inside the integral

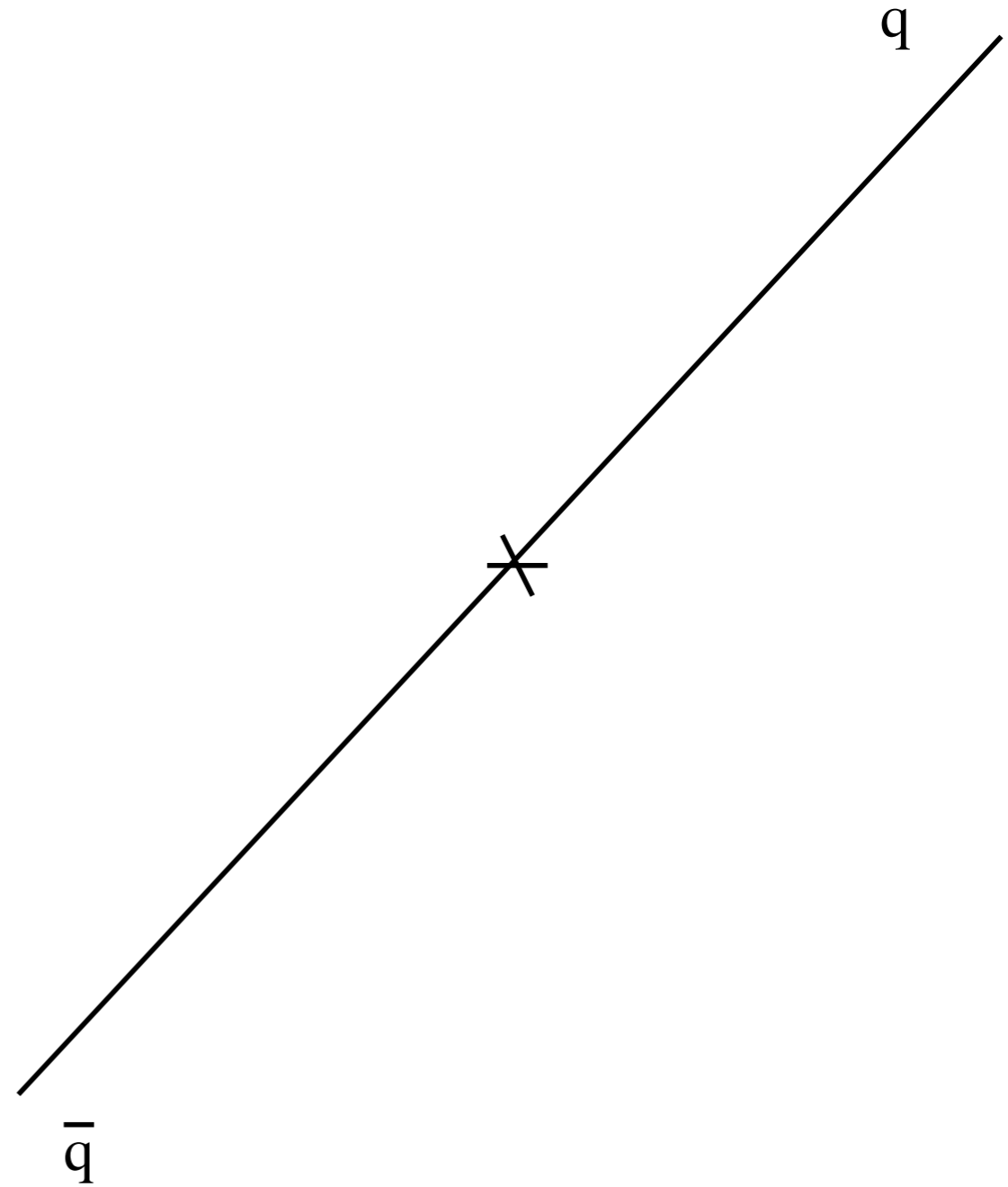
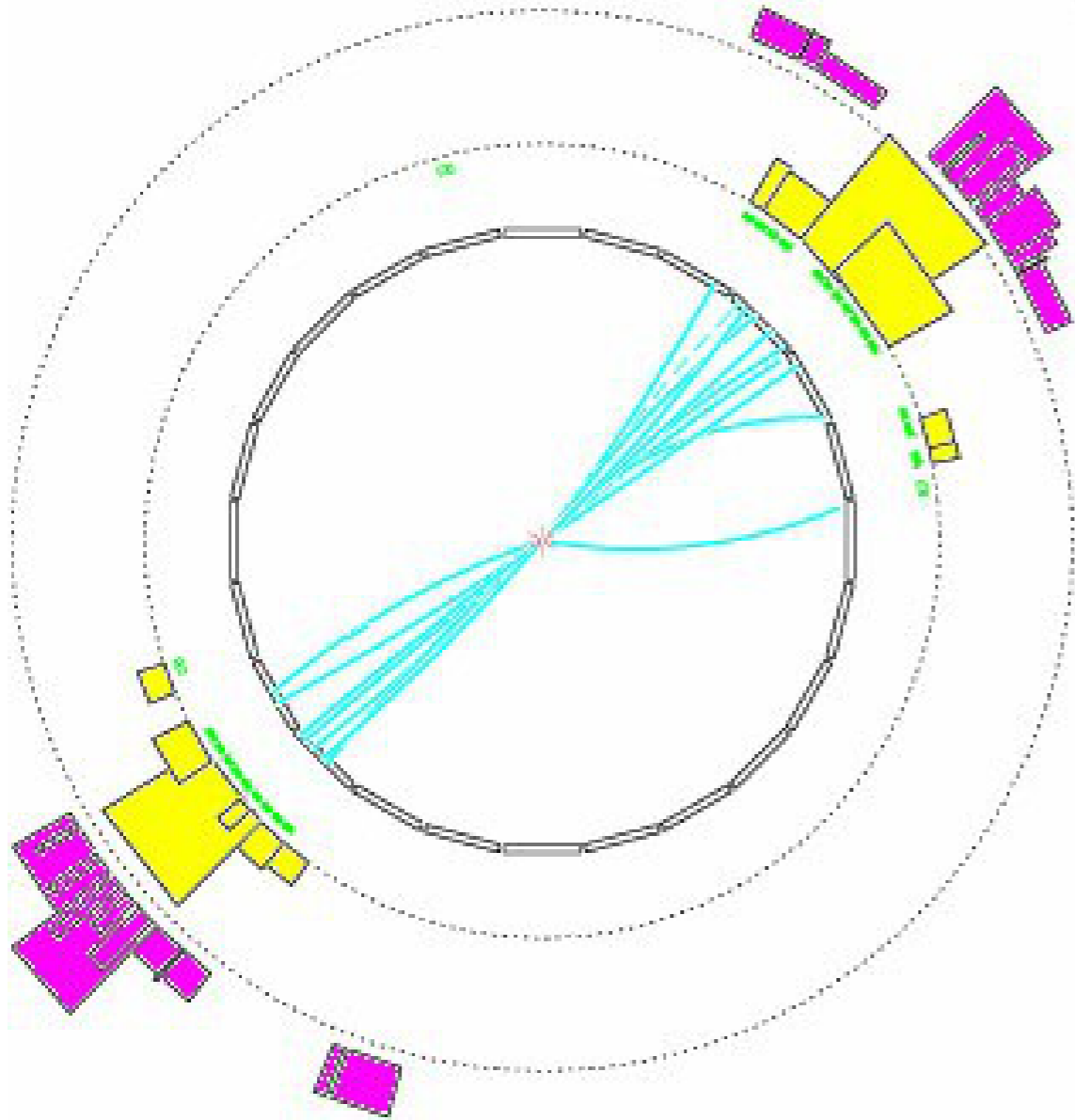
Adding running coupling is straightforward: just use $\alpha_s(p_t)$ with $p_t = E\theta$, in the integrand:

$$P_g = \frac{2C_F}{\pi} \int_{Q_0}^Q \frac{dp_t}{p_t} \alpha_s(p_t) \int_{p_t/Q}^1 \frac{dz}{z} = \frac{C_F}{\pi b_0} \left(\ln \frac{Q}{\Lambda} \ln \ln \frac{Q}{\Lambda} + \dots \right)$$

Structure of answer changes a bit: it's larger than $1/\alpha_s(Q)$, by a factor $\ln \ln Q/\Lambda$.

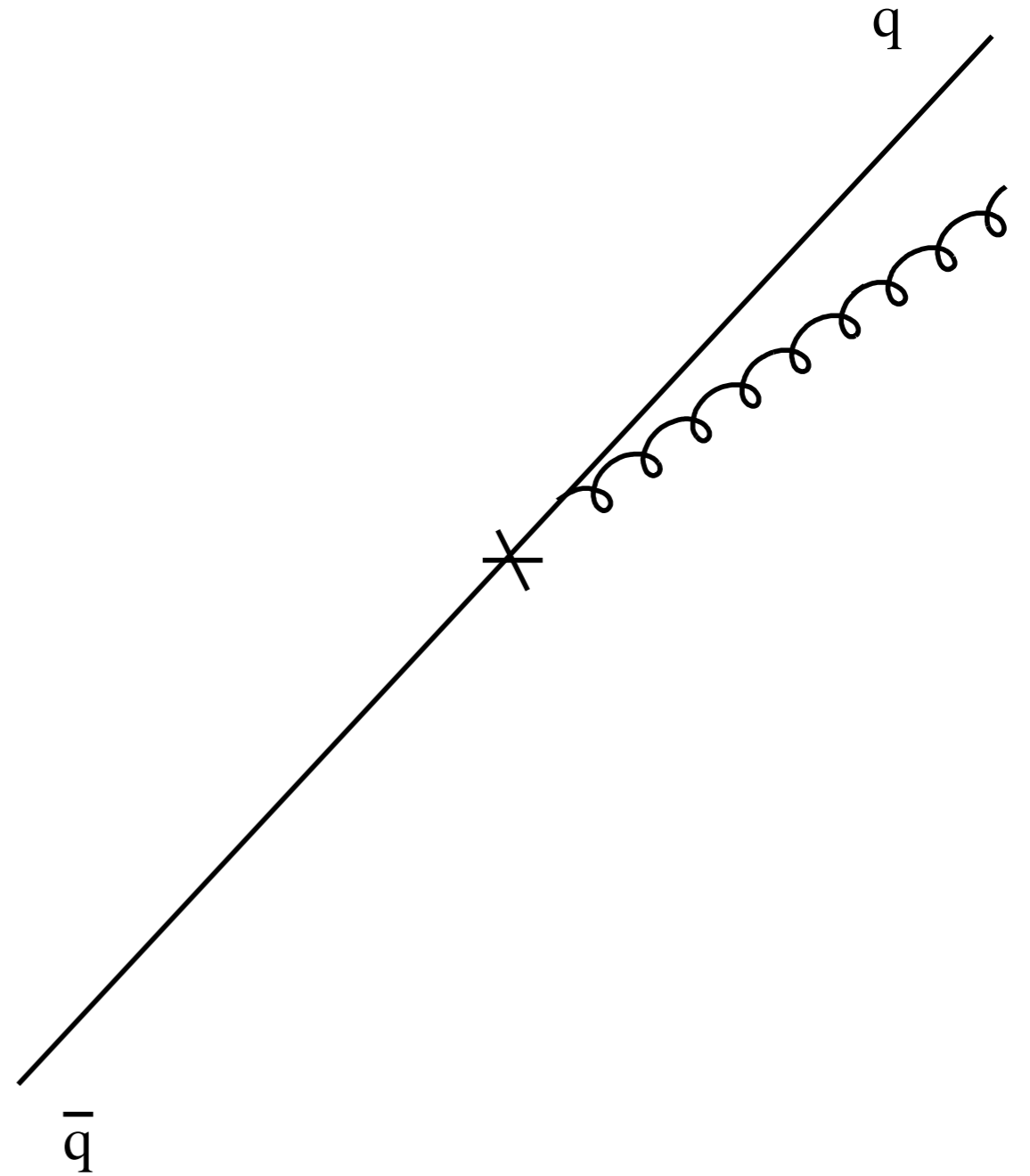
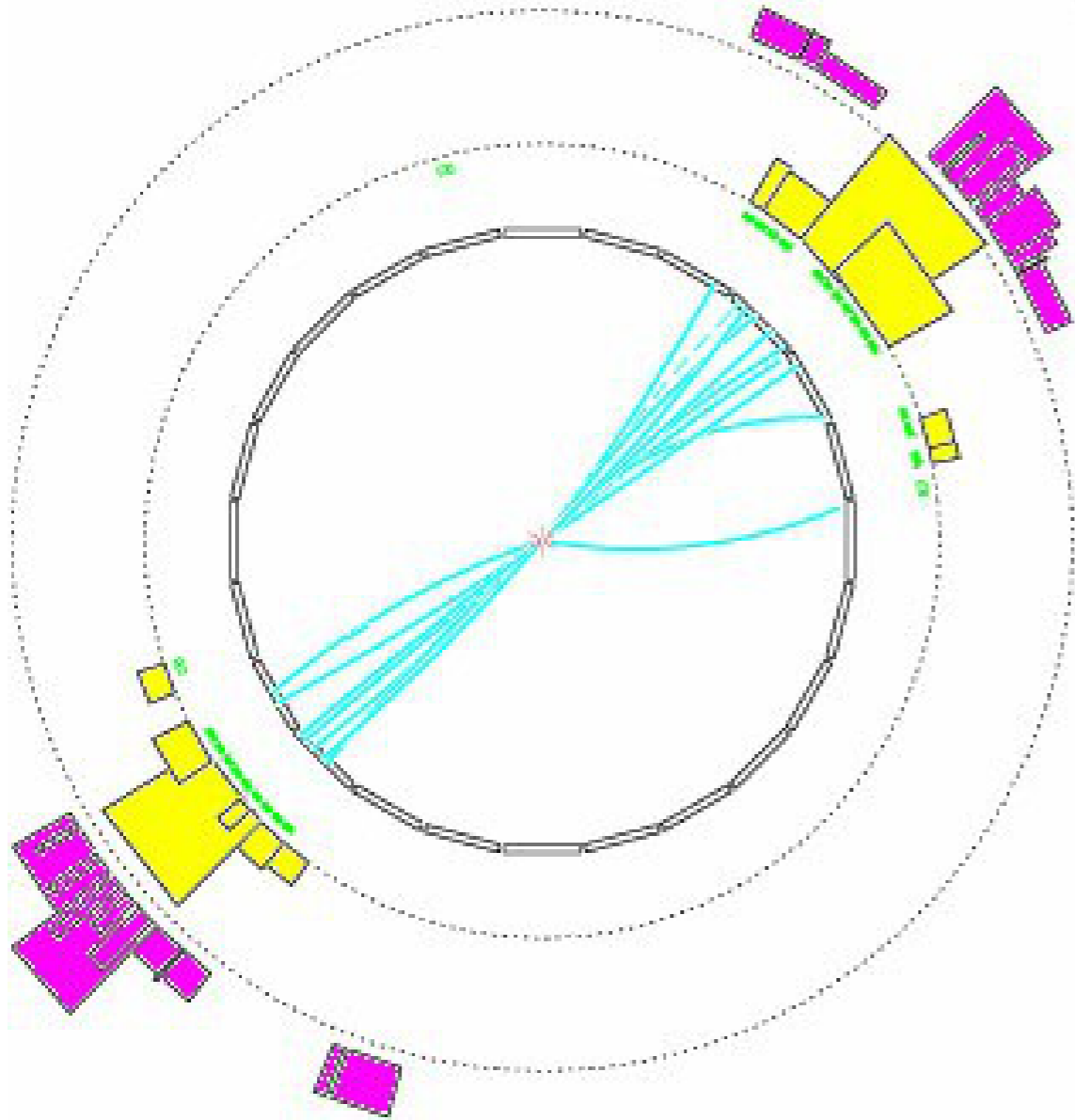
But to keep expressions simple in these lectures we'll often restrict ourselves to a fixed-coupling approximation.

Picturing a QCD event



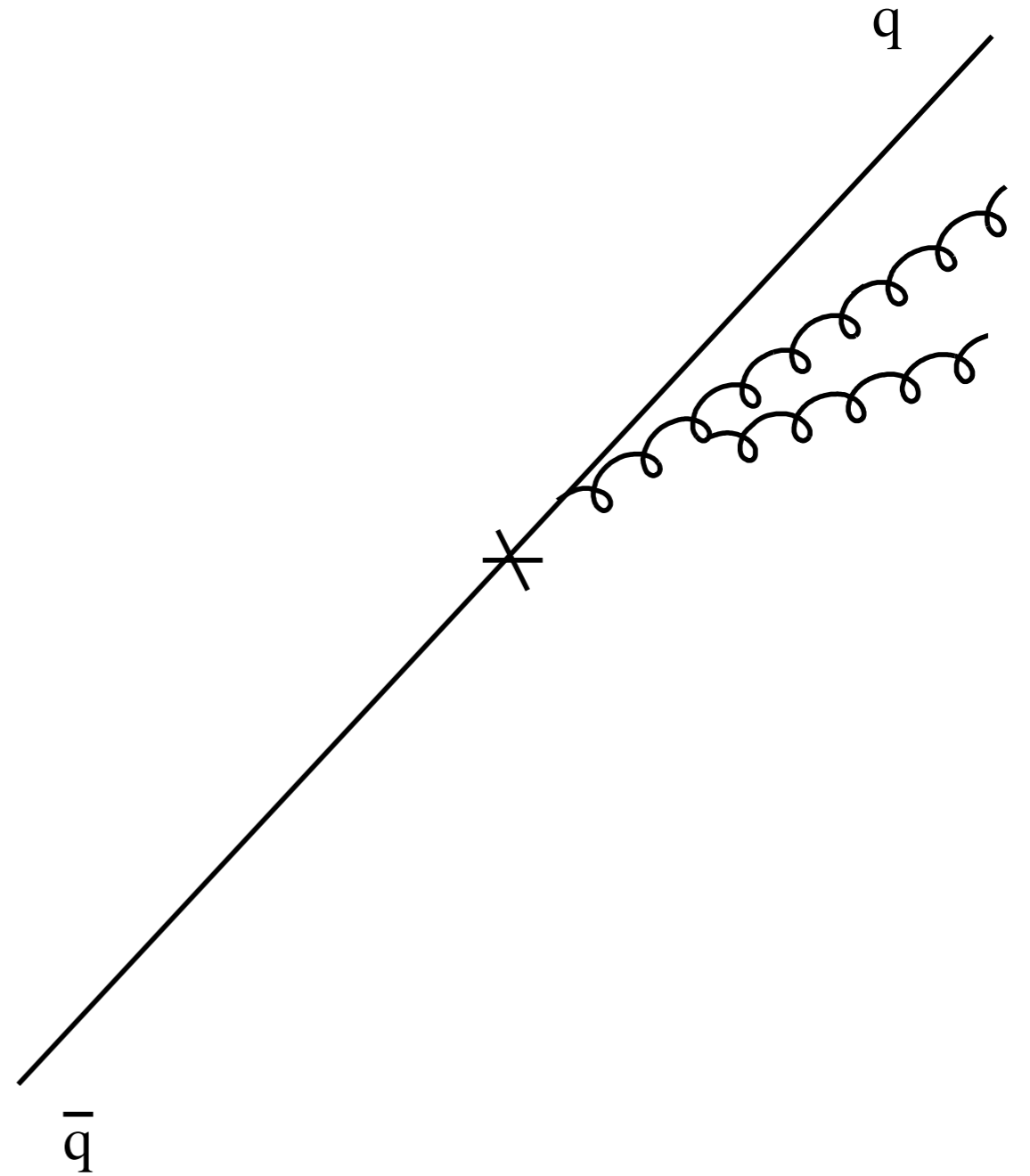
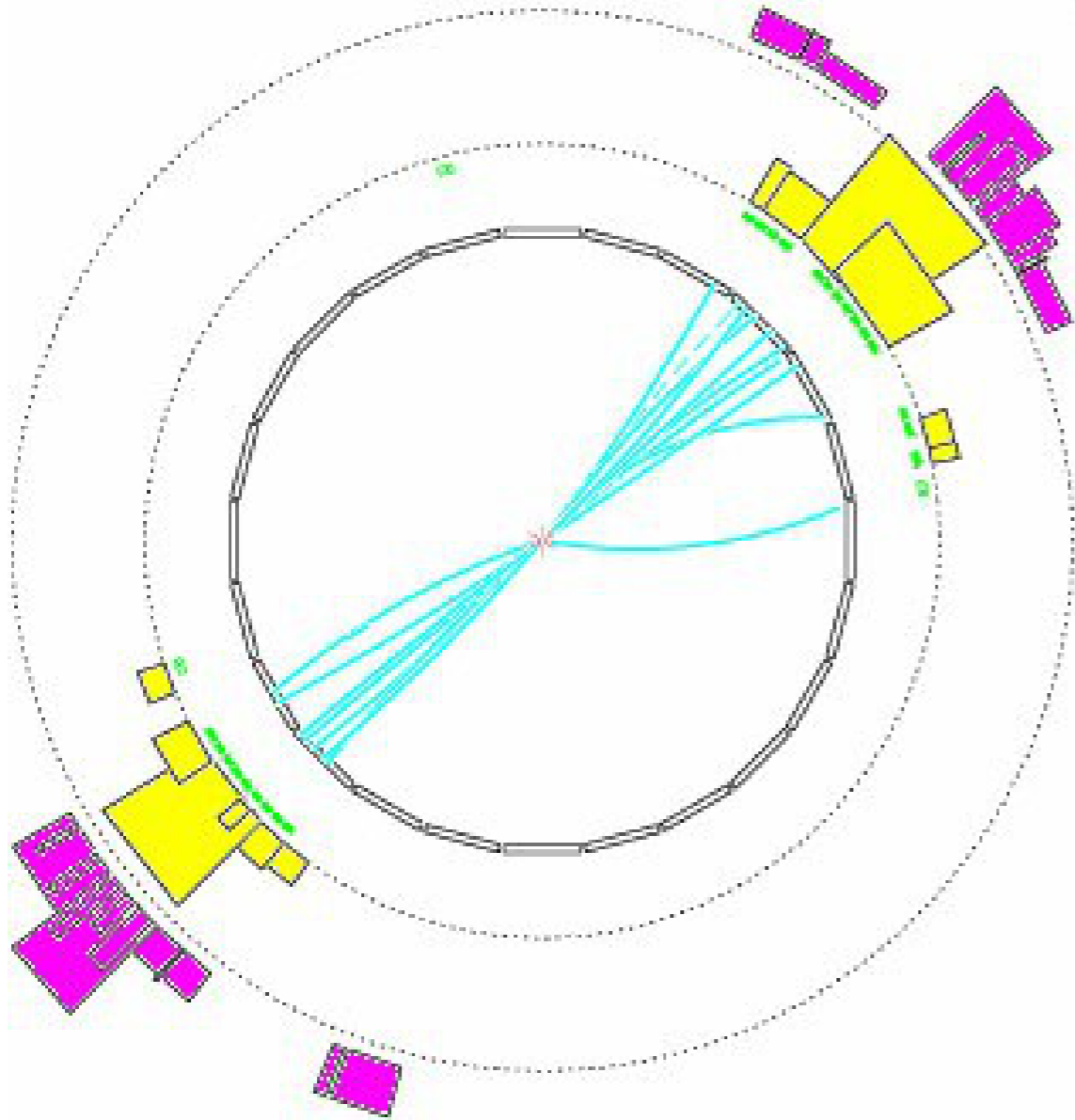
Start off with a qqbar system

Picturing a QCD event



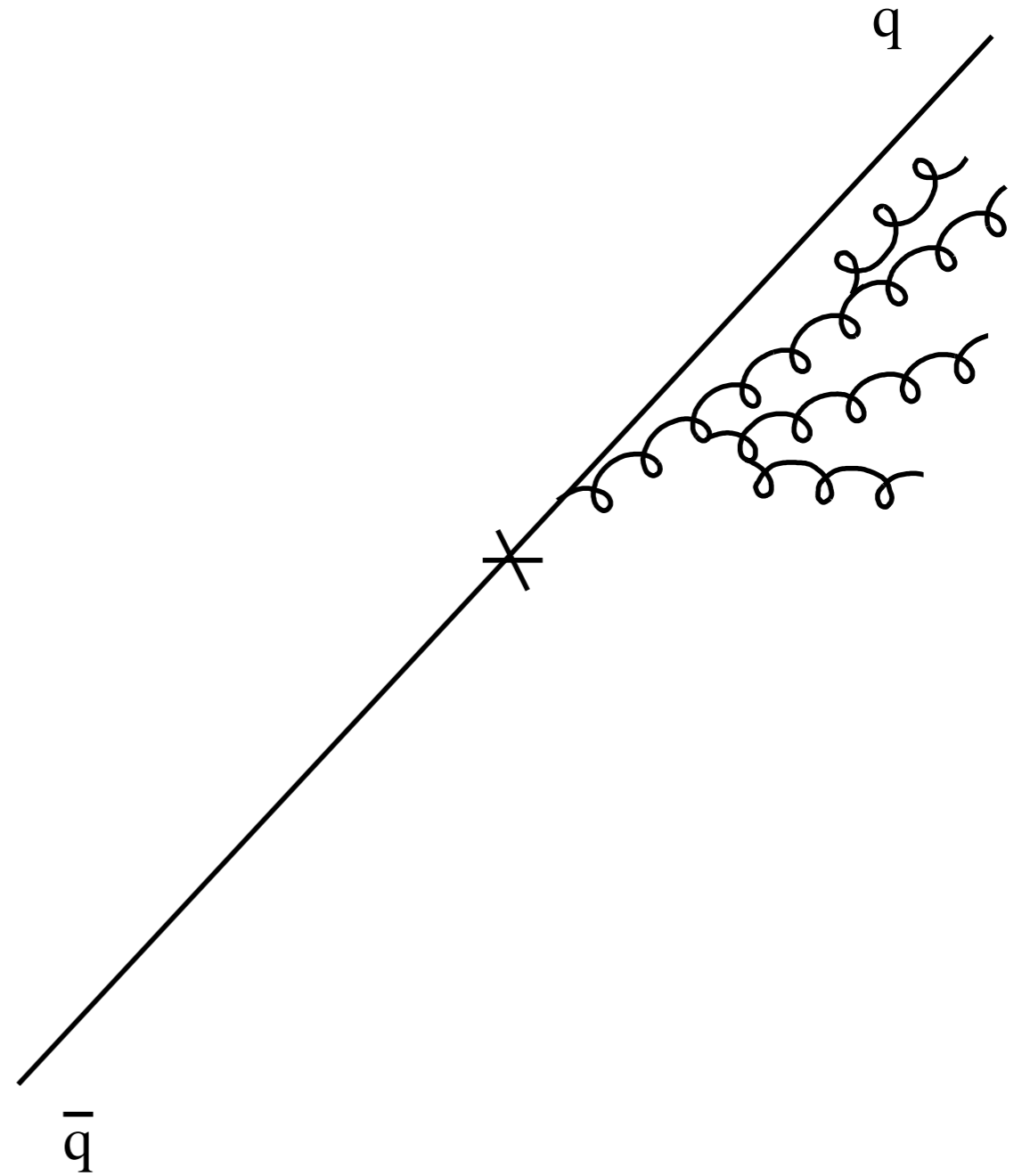
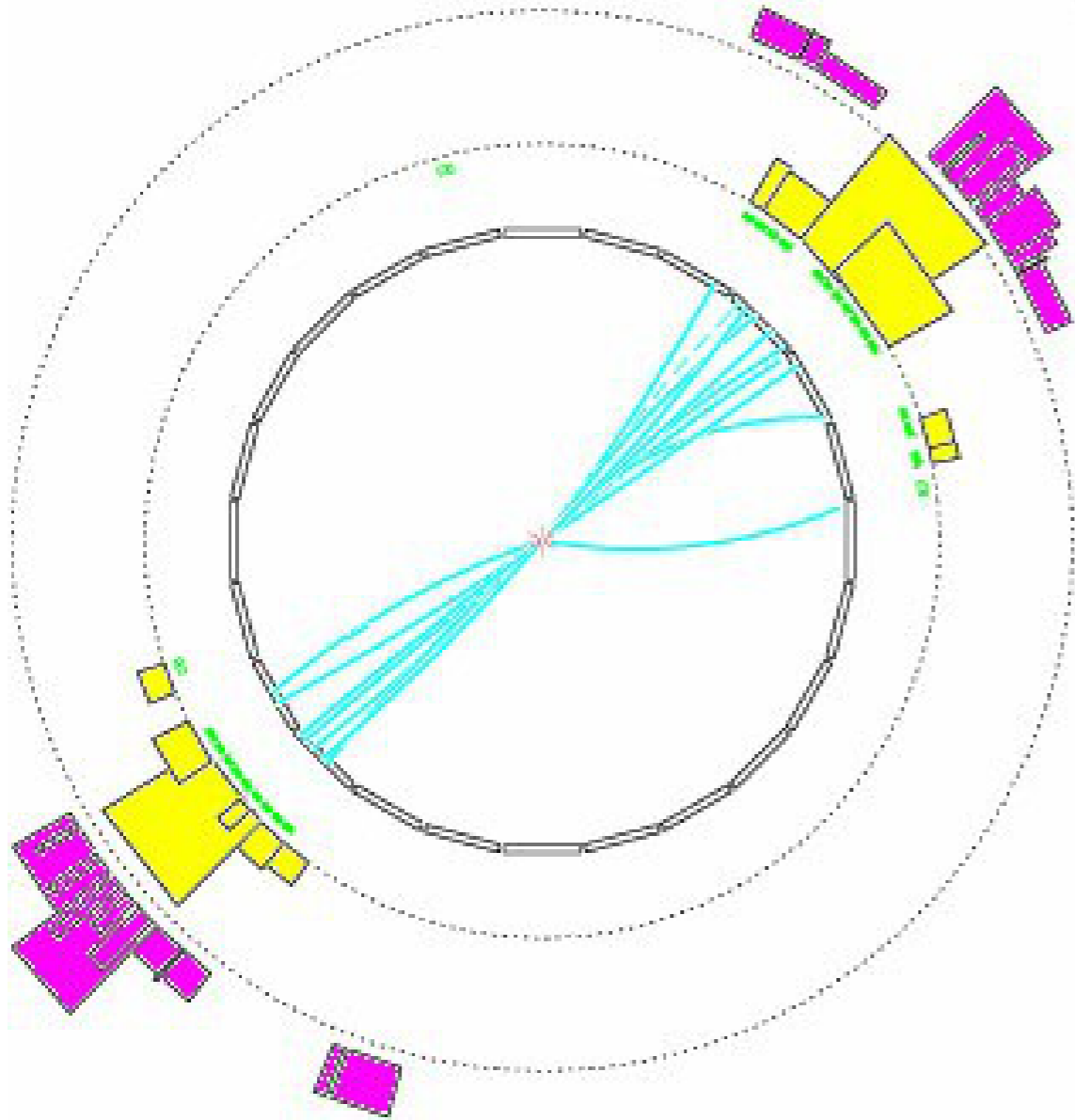
**Start off with a $q\bar{q}$ system
a gluon gets emitted at small angles**

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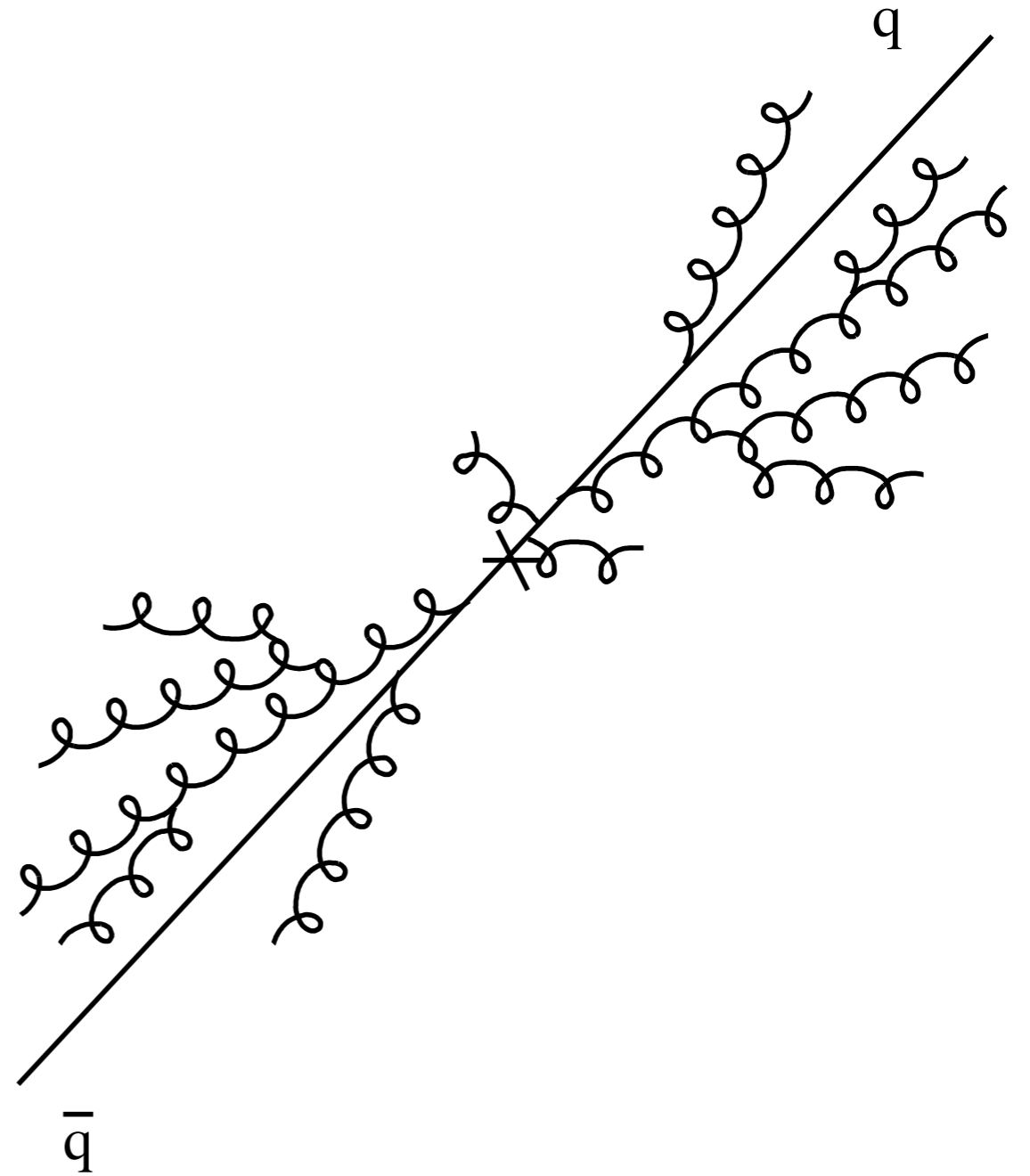
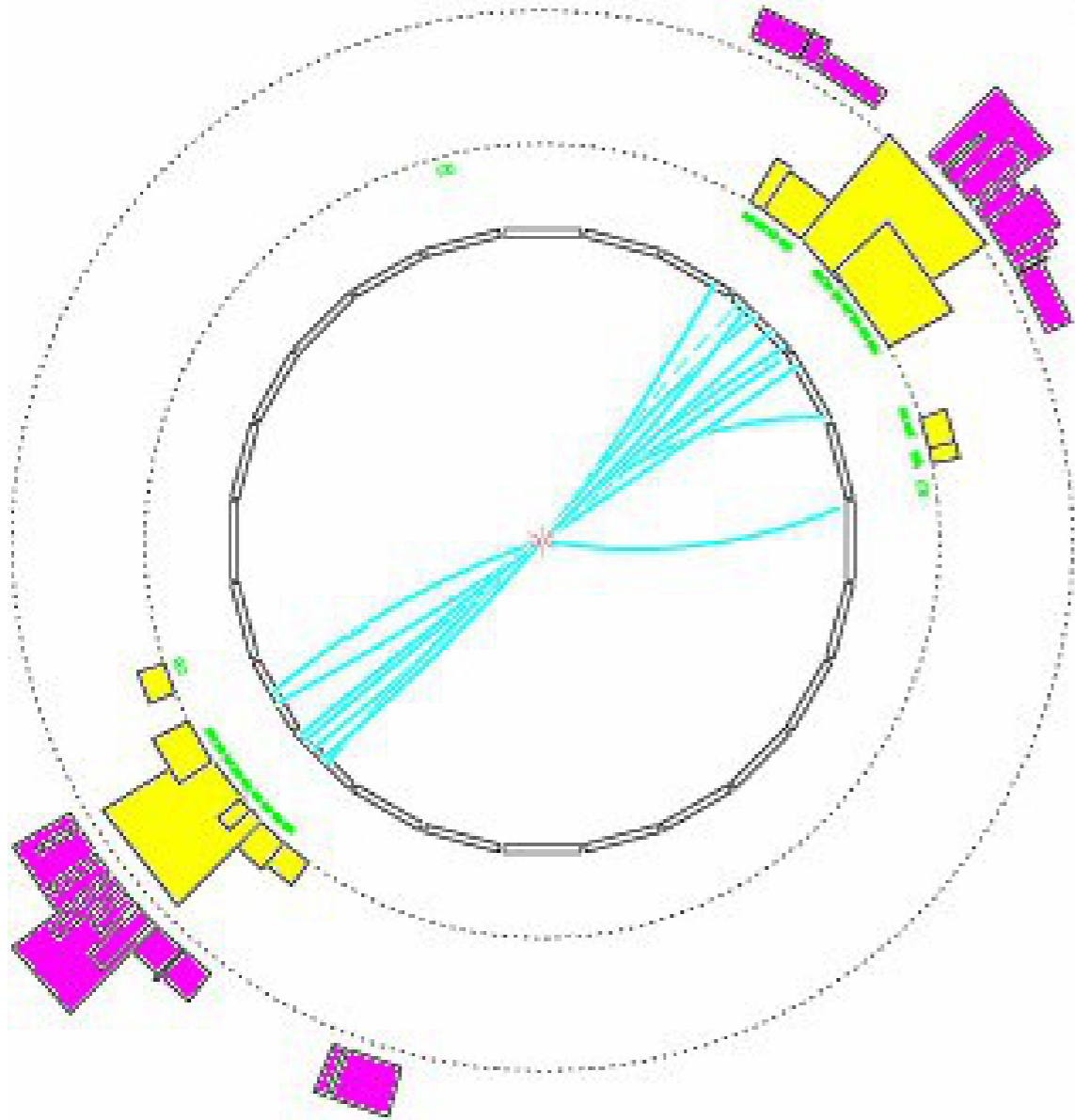
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it radiates a further gluon**

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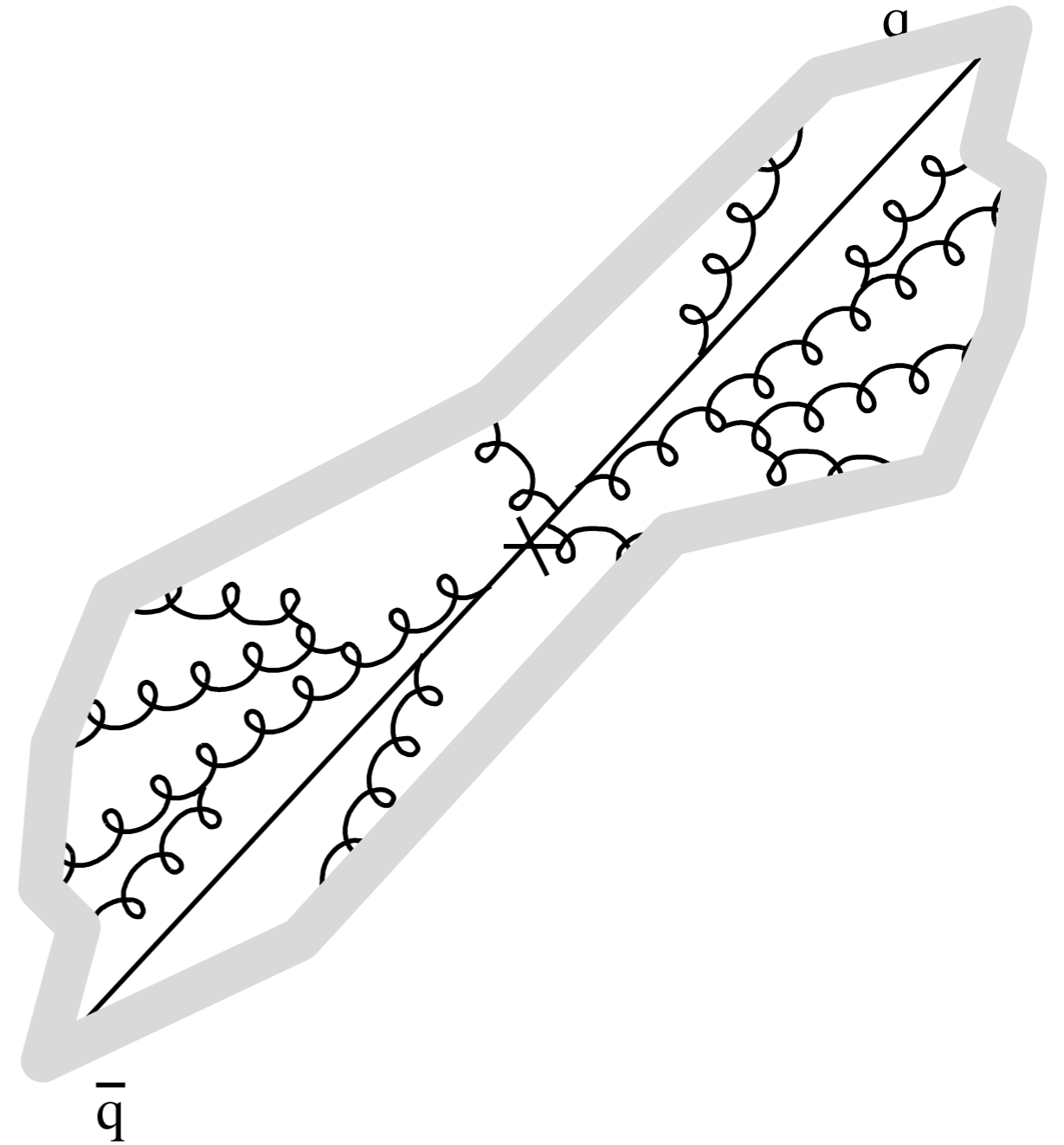
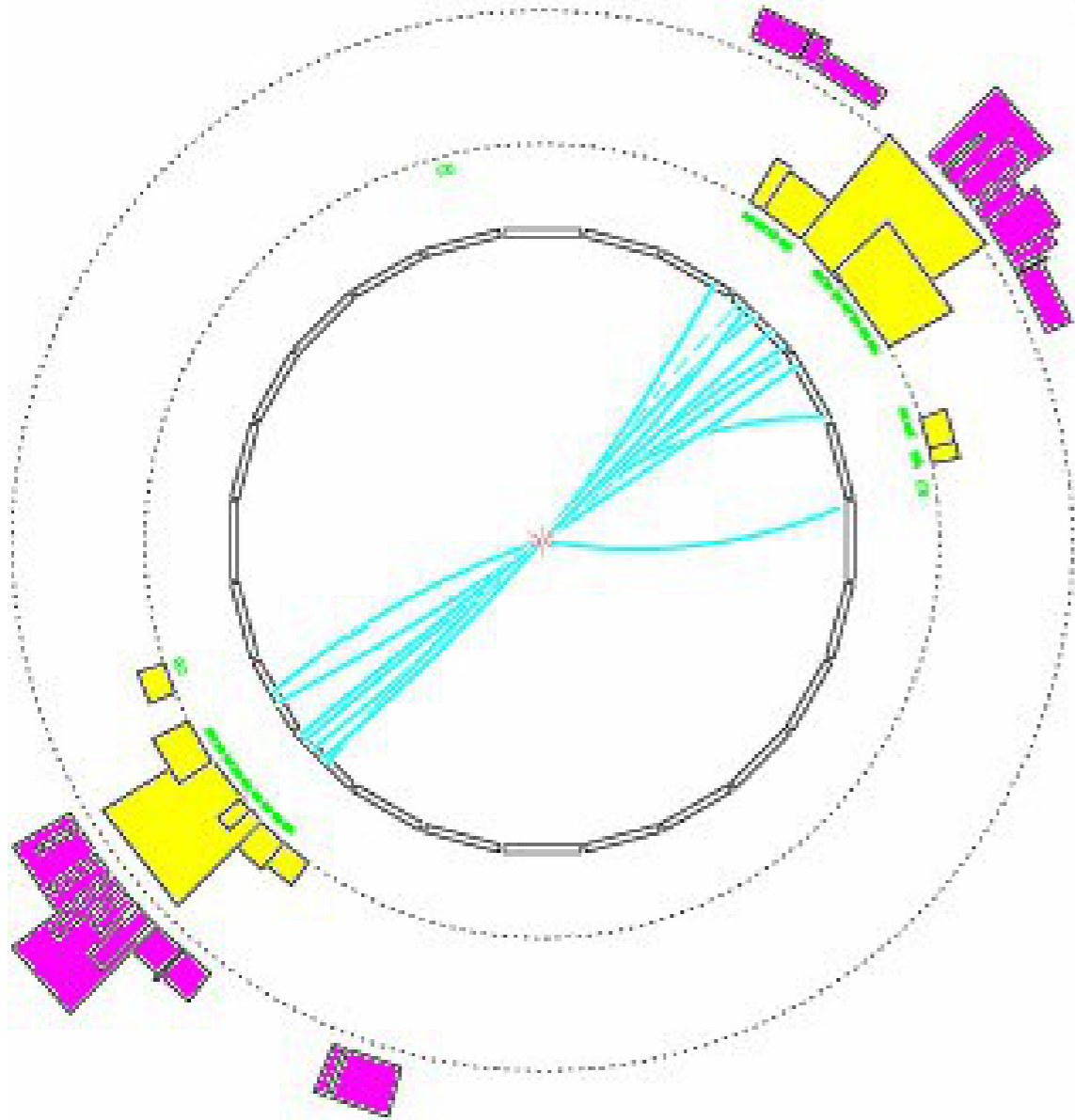
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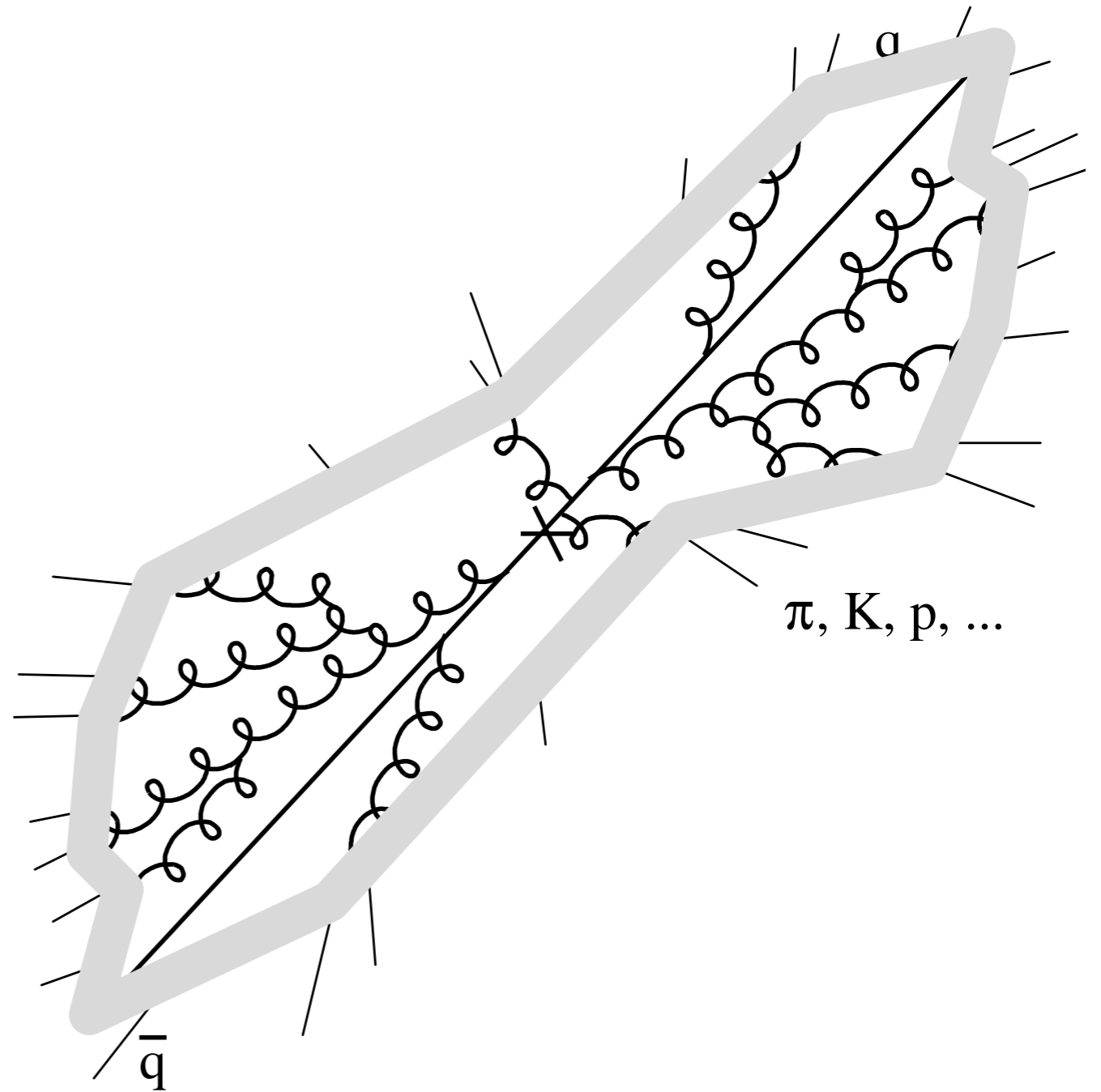
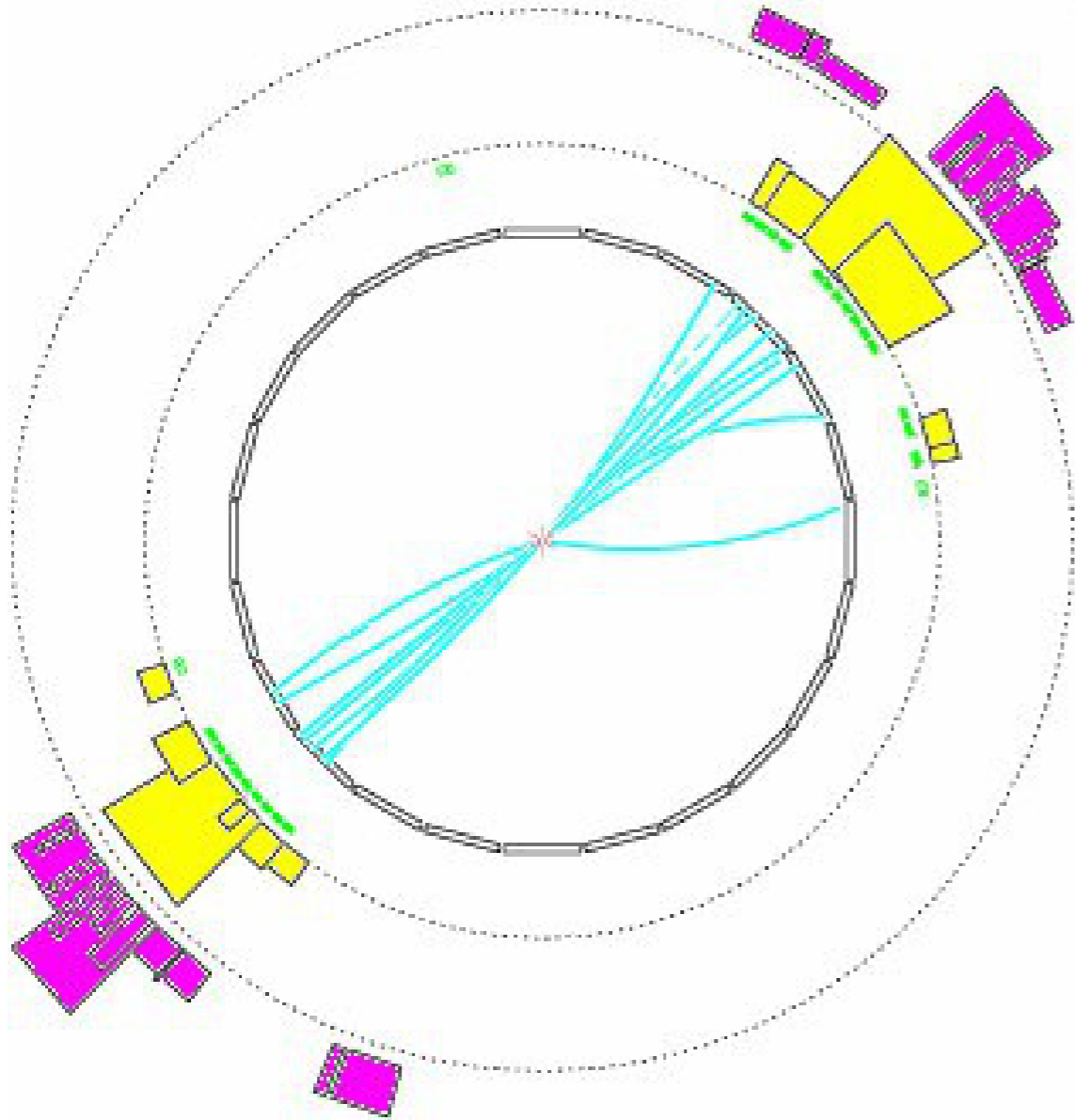
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Picturing a QCD event



then a non-perturbative transition occurs

Picturing a QCD event



then a non-perturbative transition occurs

giving a pattern of hadrons that “remembers” the gluon branching
(hadrons mostly produced at small angles wrt $q\bar{q}$ directions — two **“jets”**)

resummation and parton showers

the previous slides applied in practice

Resummation

Analytical, or semi-numerical, calculation of dominant logarithmically enhanced terms, to all orders in the strong coupling.

Applies when you place a strong constraint on an observable.

Calculations are often specific to a single observable.

Parton shower Monte Carlo

Simulation of emission of arbitrary number of particles, usually ordered in angle or p_t .

Underlying algorithm should reproduce many of the singular limits of multi-particle QCD amplitudes, including virtual corrections.

Can be used to calculate arbitrary observables.

Resummation: one way of seeing the underlying key idea

Calculate cross section for some **observable** $v(p_1, \dots, p_m)$, a function of the event momenta, to be less than some cut V .

Illustrate structure in soft limit, fixed coupling, ignore secondary emissions from soft gluons.

$$\sigma(v(\text{emissions}) < V) =$$


$$\begin{aligned} & \sigma_0 \lim_{\epsilon \rightarrow 0} \sum_{m=0}^{\infty} \frac{1}{m!} \prod_{i=1}^m \left(\frac{2\alpha_s C_F}{\pi} \int_{\epsilon} \frac{dE_i}{E_i} \int_{\epsilon} \frac{d\theta_i}{\theta_i} \int_0^{2\pi} \frac{d\phi_i}{2\pi} \right) \times \\ & \times \sum_{n=0}^{\infty} \frac{1}{n!} \prod_{i=m+1}^{m+n} \left(-\frac{2\alpha_s C_F}{\pi} \int_{\epsilon} \frac{dE_i}{E_i} \int_{\epsilon} \frac{d\theta_i}{\theta_i} \int_0^{2\pi} \frac{d\phi_i}{2\pi} \right) \times \\ & \times \Theta(V - v(p_1, \dots, p_m)) \end{aligned}$$

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*Any number of real gluons
(independent of each other if
angles are all very different)*



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$$\times \Theta(V - v(p_1, \dots, p_m))$$

Any number of virtual gluons

constraint from observable, involves just real gluons

Resummation example result

- It's common to ask questions like “*what is the probability that a Z boson is produced with transverse momentum $< p_T$* ”
- Answer is given (\sim) by a “**Sudakov form factor**”, i.e. the probability of not emitting any gluons with transverse momentum $> p_T$.

$$P(Z \text{ trans.mom.} < p_T) \simeq \exp \left[-\frac{2\alpha_s C_F}{\pi} \ln^2 \frac{M_Z}{p_T} \right]$$

- when p_T is small, the logarithm is large and compensates for the smallness of α_s — so you need to **resum log-enhanced terms to all orders in α_s** .

What do we know about resummation?

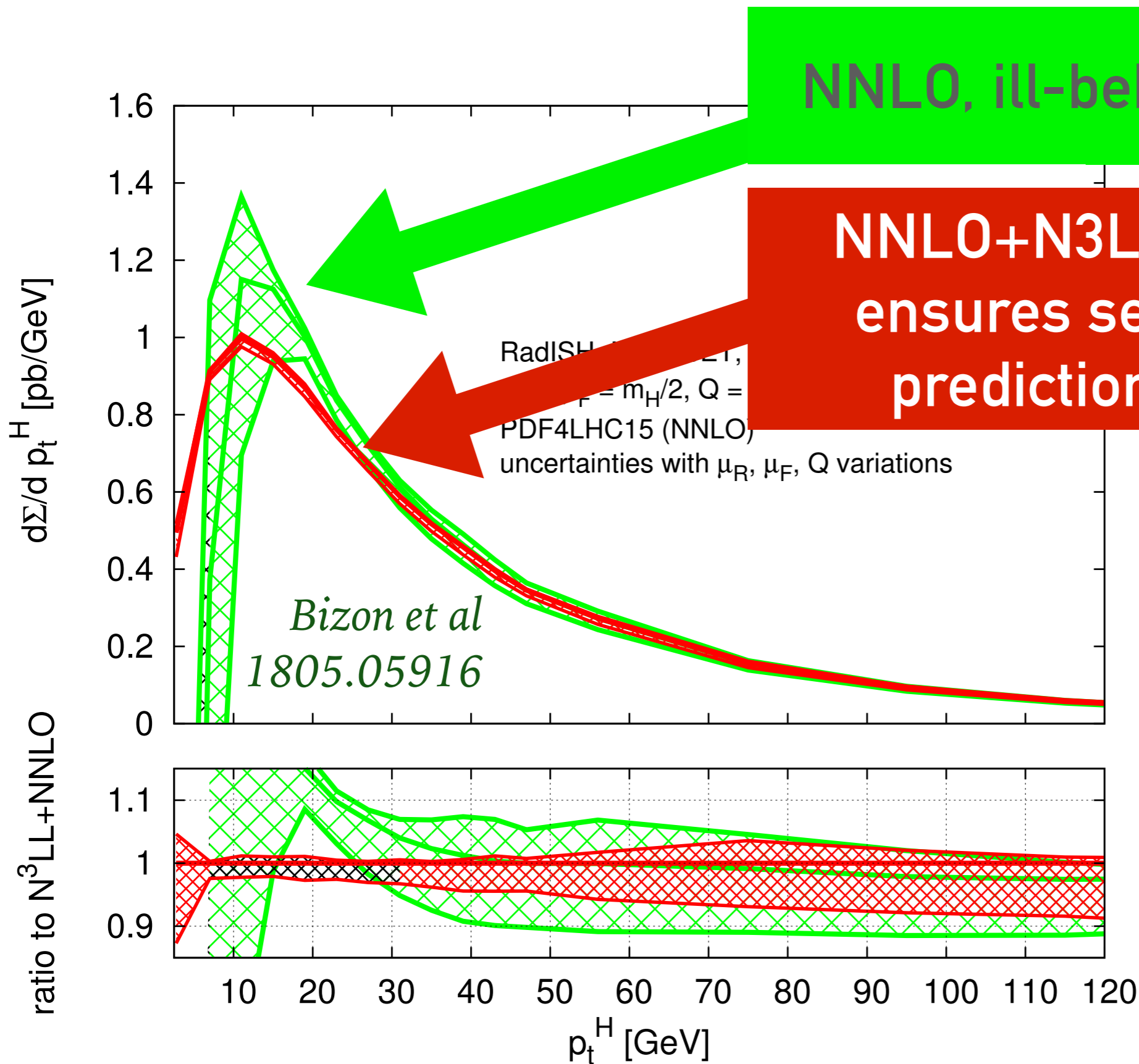
- You'll sometimes see mention of “NNLL” or similar
- This means next-next-to-leading logarithmic
- Most common definition of **Leading logarithmic (LL)**: you sum all terms with **$p=n+1$ (for $n=1\dots\infty$)** in

$$\exp \left[- \sum_{n,p} \alpha_s^n \ln^p \frac{M_H}{p_T} \right]$$

- **NLL**: include all terms with **$p=n$ (for $n=1\dots\infty$)**
- **NNLL**: include all terms with **$p=n-1$ (for $n=1\dots\infty$)**

In real life, the function that appears in the resummation is sometimes instead a Fourier or Mellin transform of an exponential

Resummation of Higgs p_T spectrum (same formula, with $C_F \rightarrow C_A$)

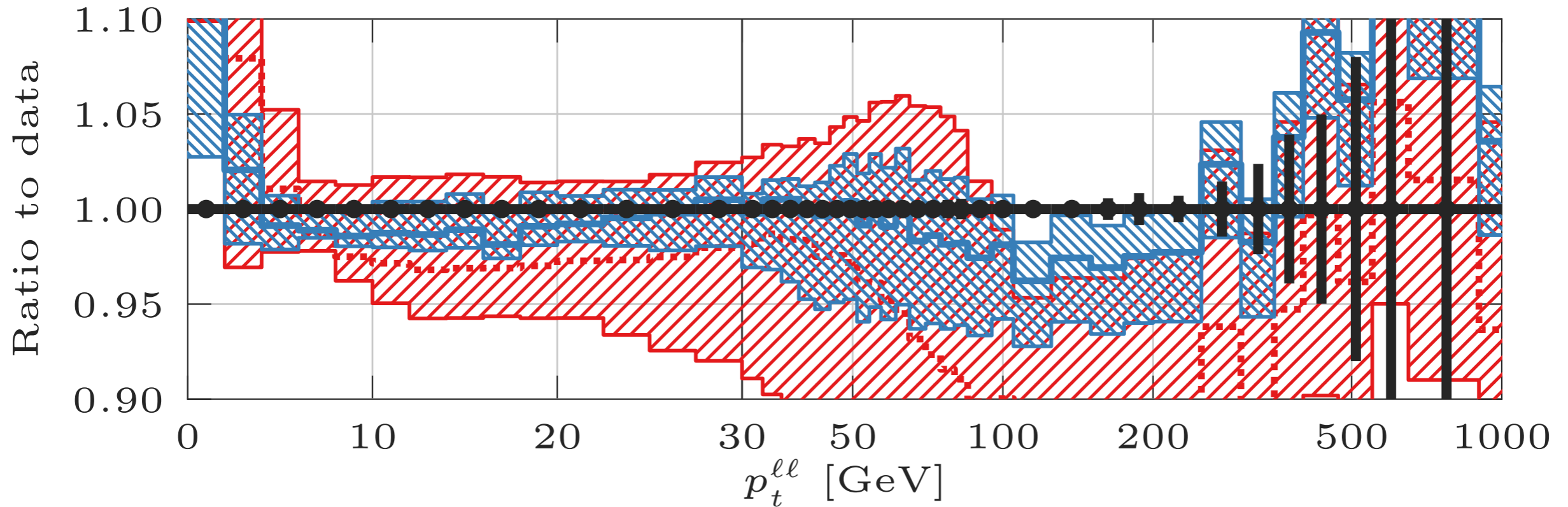





NNLO, ill-behaved at small p_t .

NNLO+N3LL, resummation ensures sensible, reliable predictions at small p_t .

This kind of resummation is an input to nearly all LHC Higgs studies, W mass determinations and some strong-coupling determinations

Resummation of Z p_T spectrum v. data



	NNLO+NNLL	NNLOJET+RadISH NNPDF4.0 (NNLO)
	N^3 LO+ N^3 LL	13 TeV, $pp \rightarrow Z/\gamma^*(\rightarrow \ell^+\ell^-) + X$ symmetric cuts
	ATLAS data	uncertainties with μ_R, μ_F, Q , matching variations

Chen et al
2203.01565

resummation v. parton showers (the basic idea, ignoring secondary emsn. from gluons)

- a resummation predicts **one observable** to high accuracy
- a parton shower takes the same idea of a Sudakov form factor and uses it to generate emissions
- from probability of not emitting gluons above a certain p_T , you can deduce p_T distribution of first emission

1. use a random number generator (r) to sample that p_T distribution

deduce p_T by solving $r = \exp \left[-\frac{2\alpha_s C_A}{\pi} \ln^2 \frac{p_{T,\max}^2}{p_T^2} \right]$

2. repeat for next emission, etc., until p_T falls below some non-perturbative cutoff

**very similar to radioactive decay, with time $t \sim 1/p_T$
and a decay rate $\sim (\log t) / t$**

A toy shower

<https://github.com/gavinsalam/zuoz2016-toy-shower>

(fixed coupling, primary branching only, only p_T , no energy conservation, no PDFs, etc.)

```
#!/usr/bin/env python3
# an oversimplified (QED-like) parton shower
# for Zuoz lectures (2016) by Gavin P. Salam
from random import random
from math import pi, exp, log, sqrt

ptHigh = 100.0
ptCut = 1.0
alphas = 0.12
CA=3

def main():
    for iev in range(0,10):
        print ("\nEvent", iev)
        event()

def event():
    # start with maximum possible value of Sudakov
    sudakov = 1
    while (True):
        # scale it by a random number
        sudakov *= random()
        # deduce the corresponding pt
        pt = ptFromSudakov(sudakov)
        # if pt falls below the cutoff, event is finished
        if (pt < ptCut): break
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def ptFromSudakov(sudakovValue):
    """Returns the pt value that solves the relation
    Sudakov = sudakovValue (for 0 < sudakovValue < 1)
    """
    norm = (2*CA/pi)
    # r = Sudakov = exp(-alphas * norm * L^2)
    # --> log(r) = -alphas * norm * L^2
    # --> L^2 = log(r)/(-alphas*norm)
    L2 = log(sudakovValue)/(-alphas * norm)
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if __name__ == "__main__": main()
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```
% python ./toy-shower.py

Event 0
    primary emission with pt = 58.4041962726
    primary emission with pt = 3.61999582015
    primary emission with pt = 2.31198814996

Event 1
    primary emission with pt = 32.1881228375
    primary emission with pt = 10.1818306204
    primary emission with pt = 10.1383134201
    primary emission with pt = 7.24482350383
    primary emission with pt = 2.35709074796
    primary emission with pt = 1.0829758034

Event 2
    primary emission with pt = 64.934992001
    primary emission with pt = 16.4122436094
    primary emission with pt = 2.53473253194

Event 3
    primary emission with pt = 37.6281171491
    primary emission with pt = 22.7262873764
    primary emission with pt = 12.0255817868
    primary emission with pt = 4.73678636215
    primary emission with pt = 3.92257832288

Event 4
    primary emission with pt = 21.5359449851
    primary emission with pt = 4.01438733798
    primary emission with pt = 3.33902663941
    primary emission with pt = 2.02771620824
    primary emission with pt = 1.05944759028

. . .
```

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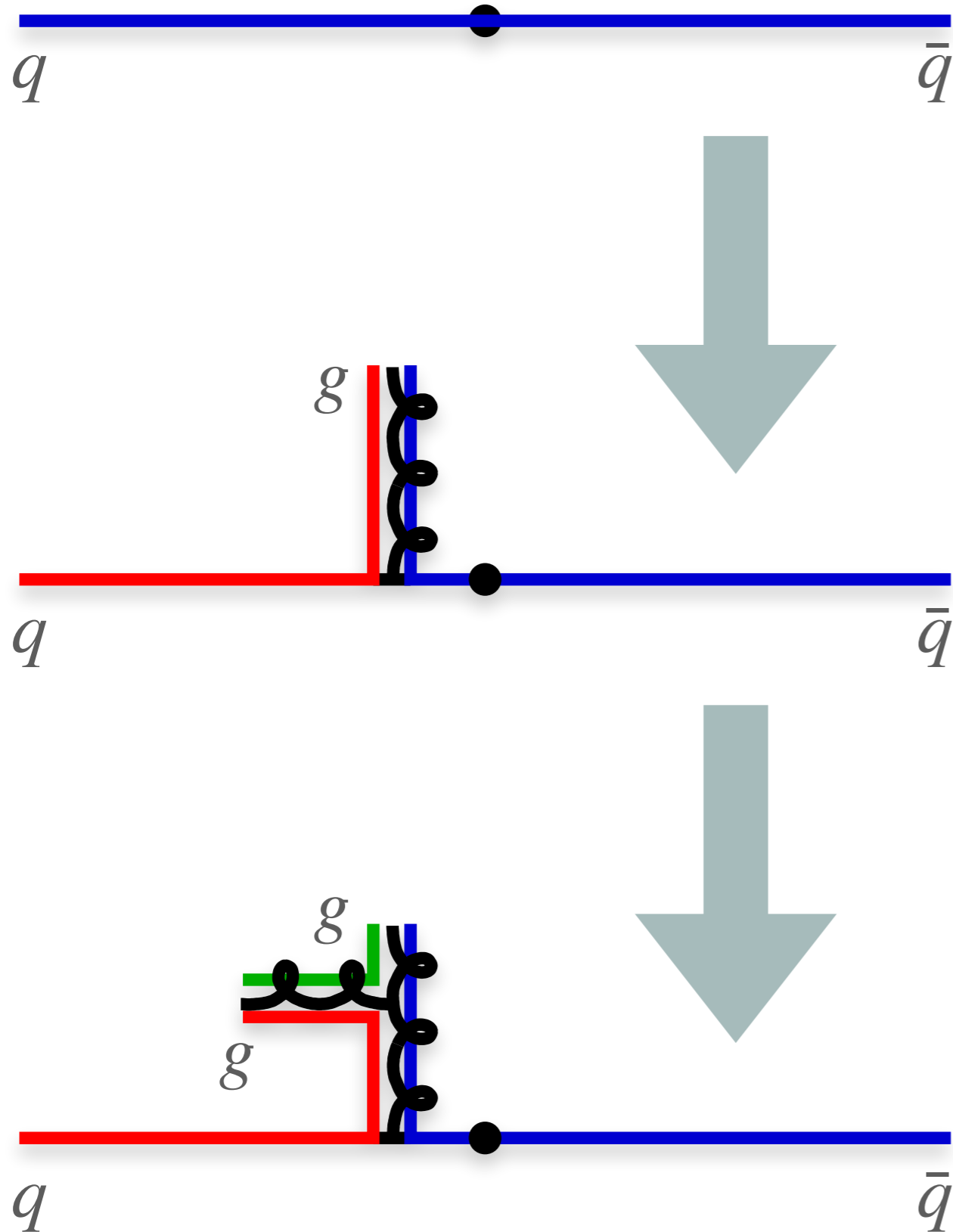
```
Event 2
```

```
primary emission with pt = 64.934992001
primary emission with pt = 16.4122436094
primary emission with pt = 2.53473253194
```

If you want to play: replace $C_A=3$ (emission from gluons) with $C_F=4/3$ (emission from quarks) and see how pattern of emissions changes (multiplicity, p_T of hardest emission, etc.)

Secondary, tertiary gluons: many showers use **colour dipoles** (Pythia, Sherpa & option in Herwig)

Original dipole MC: Ariadne (90's)



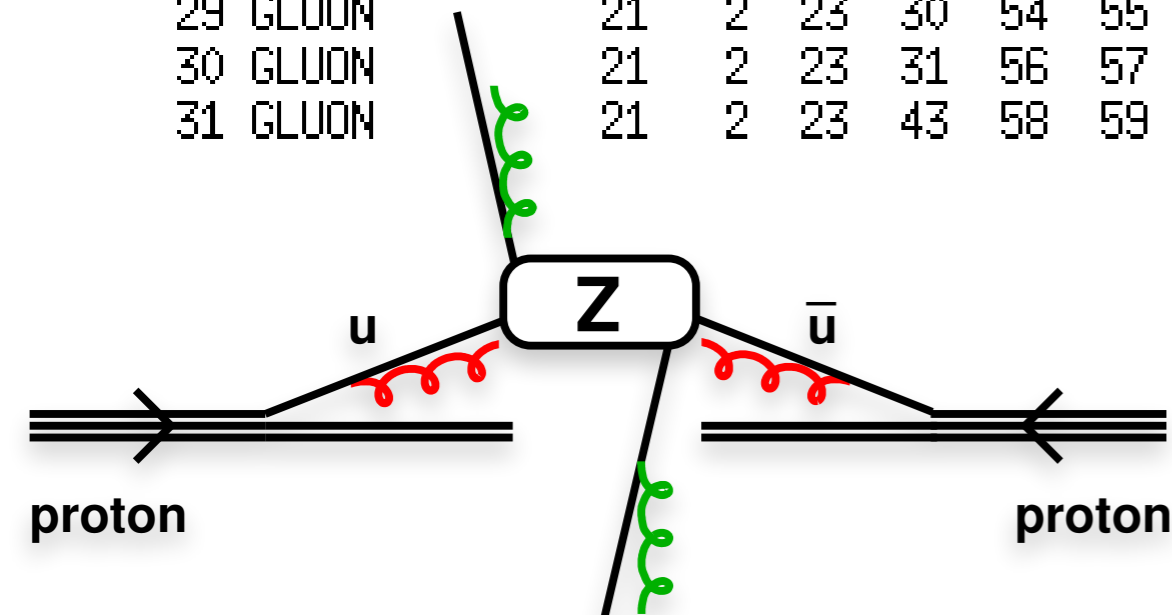
- Use large- N_C idea of colour structure
- Initial $q\bar{q}$ event = 1 colour dipole.
- Radiated gluon turns 1 dipole \rightarrow 2 dipoles
- Each dipole then radiates independently (different colour \equiv no interference), creating new colour dipoles at each step

Event record from a real-world shower (Herwig6 — old shower with compact record)

IHEP	ID	IDPDG	IST	MO1	MO2	DA1	DA2	P-X	P-Y	P-Z	ENERGY	MASS
9	UQRK	94	141	4	6	11	16	2.64	-9.83	592.2	590.2	-49.07
10	CONE	0	100	4	5	0	0	-0.27	0.96	0.1	1.0	0.00
11	GLUON	21	2	9	12	32	33	-1.02	3.59	5.6	6.7	0.75-
12	GLUON	21	2	9	13	34	35	0.25	1.46	3.6	4.0	0.75-
13	GLUON	21	2	9	14	36	37	-0.87	1.62	4.7	5.1	0.75-
14	GLUON	21	2	9	15	38	39	-0.81	4.17	3611.7	3611.7	0.75-
15	GLUON	21	2	9	16	40	41	-0.19	-1.01	1727.7	1727.7	0.75-
16	UD	2101	2	9	25	42	41	0.00	0.00	1054.6	1054.6	0.32-
17	GLUON	94	142	5	6	19	21	-2.23	0.44	-233.5	232.8	-18.36
18	CONE	0	100	5	8	0	0	0.77	0.64	0.2	1.0	0.00
19	GLUON	21	2	17	20	43	44	1.60	0.58	-2.1	2.8	0.75
20	UD	2101	2	17	21	45	44	0.00	0.00	-2687.6	2687.6	0.32
21	UQRK	2	2	17	32	46	45	0.63	-1.02	-4076.9	4076.9	0.32
22	Z0/GAMA*	23	195	7	22	251	252	-257.66	-219.68	324.8	477.5	88.56
23	UQRK	94	144	8	6	25	31	258.06	210.29	33.9	345.5	86.10
24	CONE	0	100	8	5	0	0	0.21	0.17	-1.0	1.0	0.00
25	UQRK	2	2	23	26	47	42	26.82	24.33	23.7	43.3	0.32
26	GLUON	21	2	23	27	48	49	8.50	8.18	6.0	13.3	0.75
27	GLUON	21	2	23	28	50	51	73.27	61.24	12.0	96.2	0.75
28	GLUON	21	2	23	29	52	53	73.66	58.54	-6.3	94.3	0.75
29	GLUON	21	2	23	30	54	55	67.58	52.13	-7.3	85.7	0.75
30	GLUON	21	2	23	31	56	57	6.98	4.60	2.3	8.7	0.75
31	GLUON	21	2	23	43	58	59	1.24	1.26	3.6	4.1	0.75

**INITIAL
STATE
SHOWER**

**FINAL
STATE
SHOWER**



simulations use General Purpose Monte Carlo event generators

THE BIG 3



Herwig 7



Pythia 8



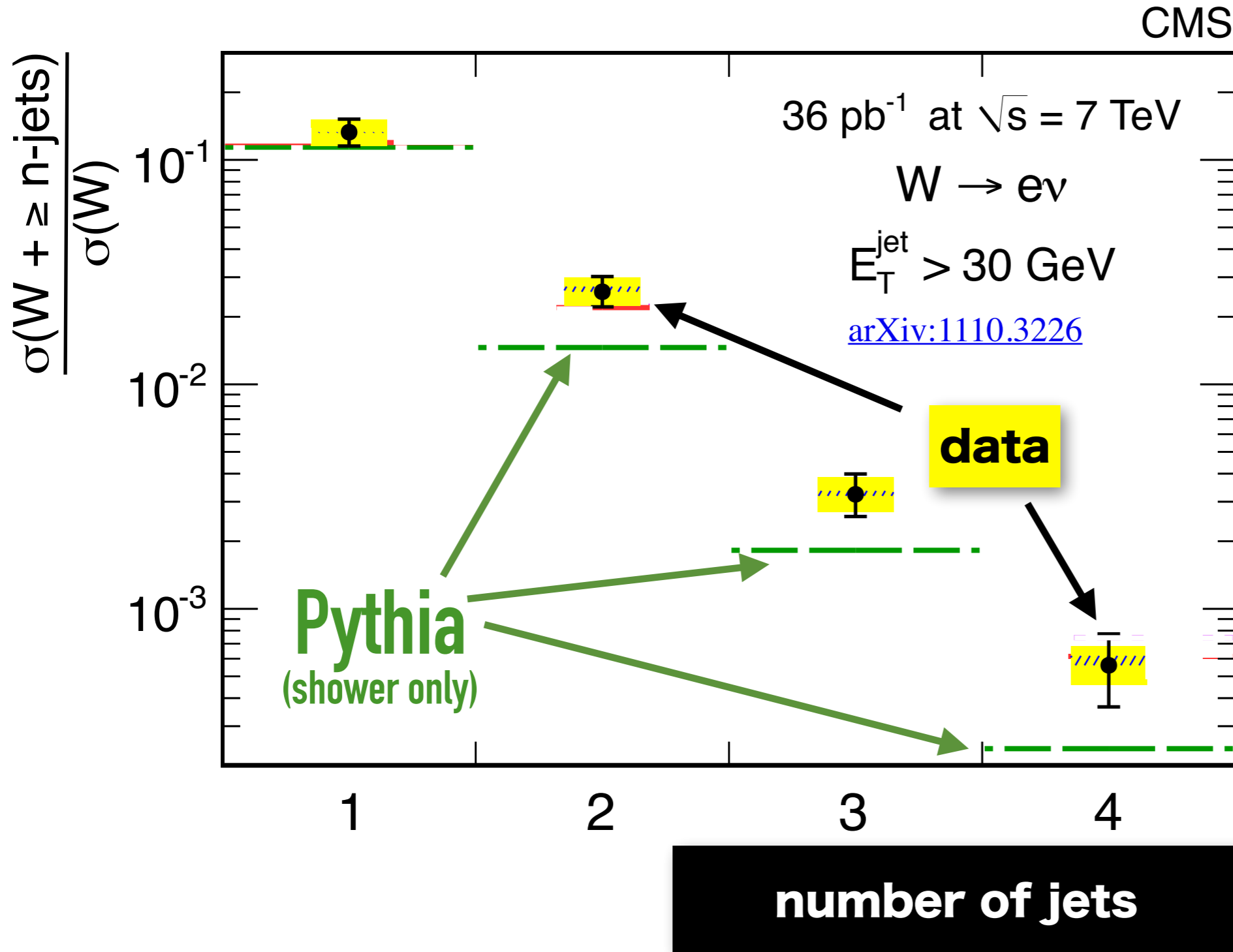
Sherpa 3

used in $\sim 95\%$ of ATLAS/CMS publications
they do an amazing job simulating vast swathes of data;
collider physics would be unrecognisable without them

combining showers & fixed order

*essential for accurate cross sections
& multijet states*

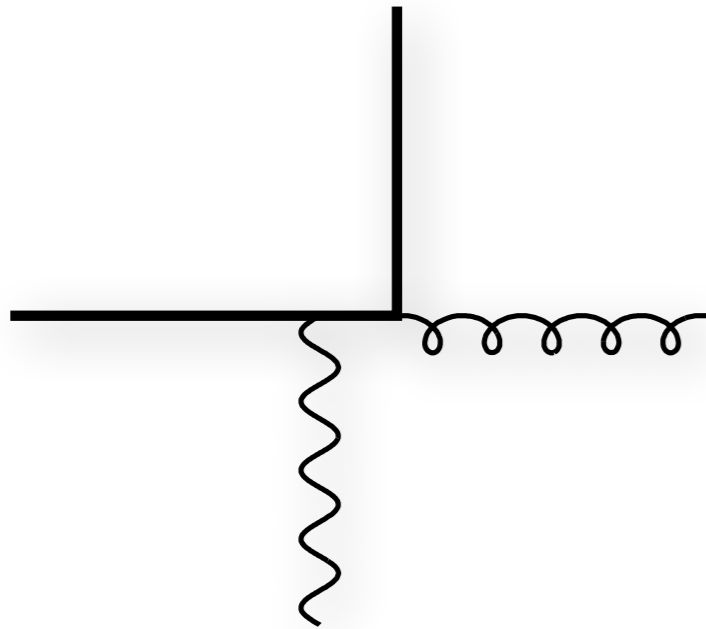
E.g. jet multiplicity in events with a W v. Pythia



shower MCs on their own cannot reproduce pattern of hard multijet states

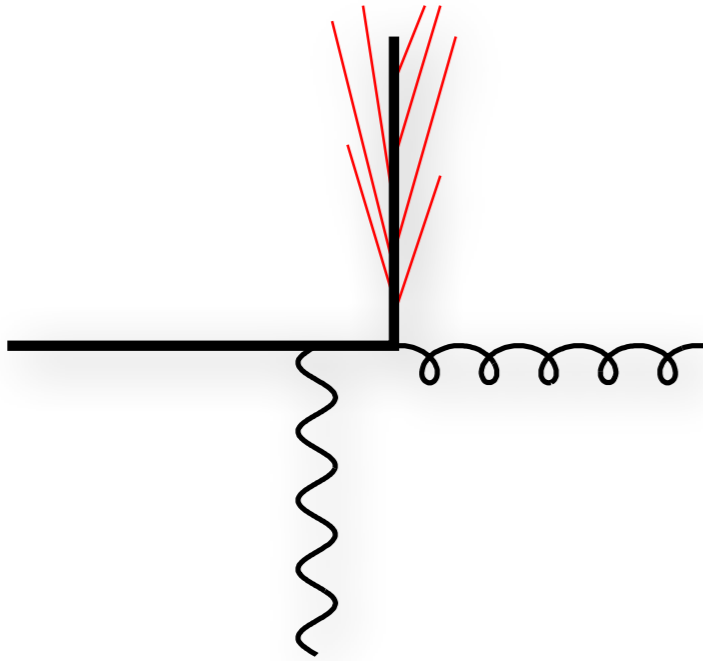
(there are topologies that are almost inaccessible via showering)

MLM matching



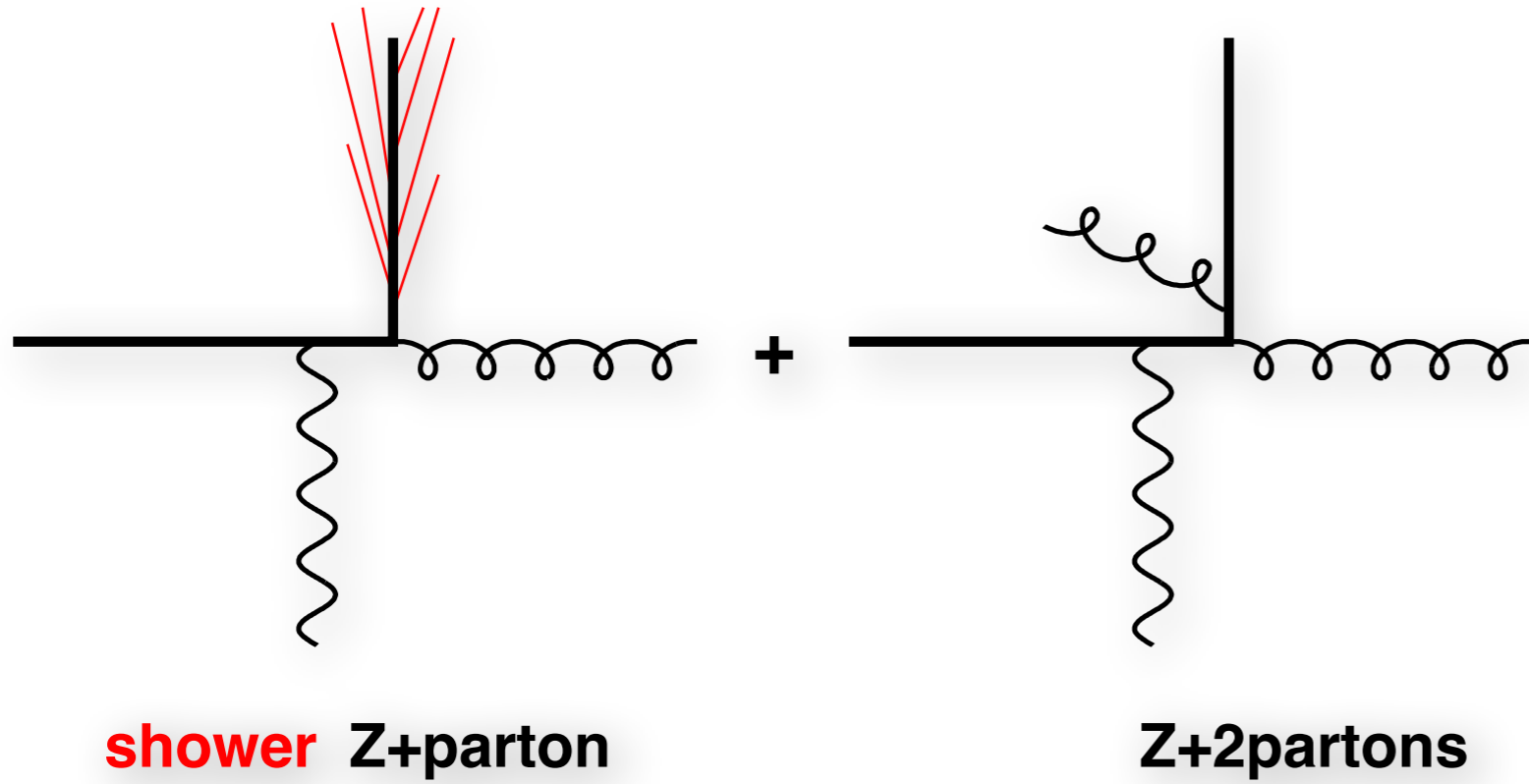
Z+parton

MLM matching

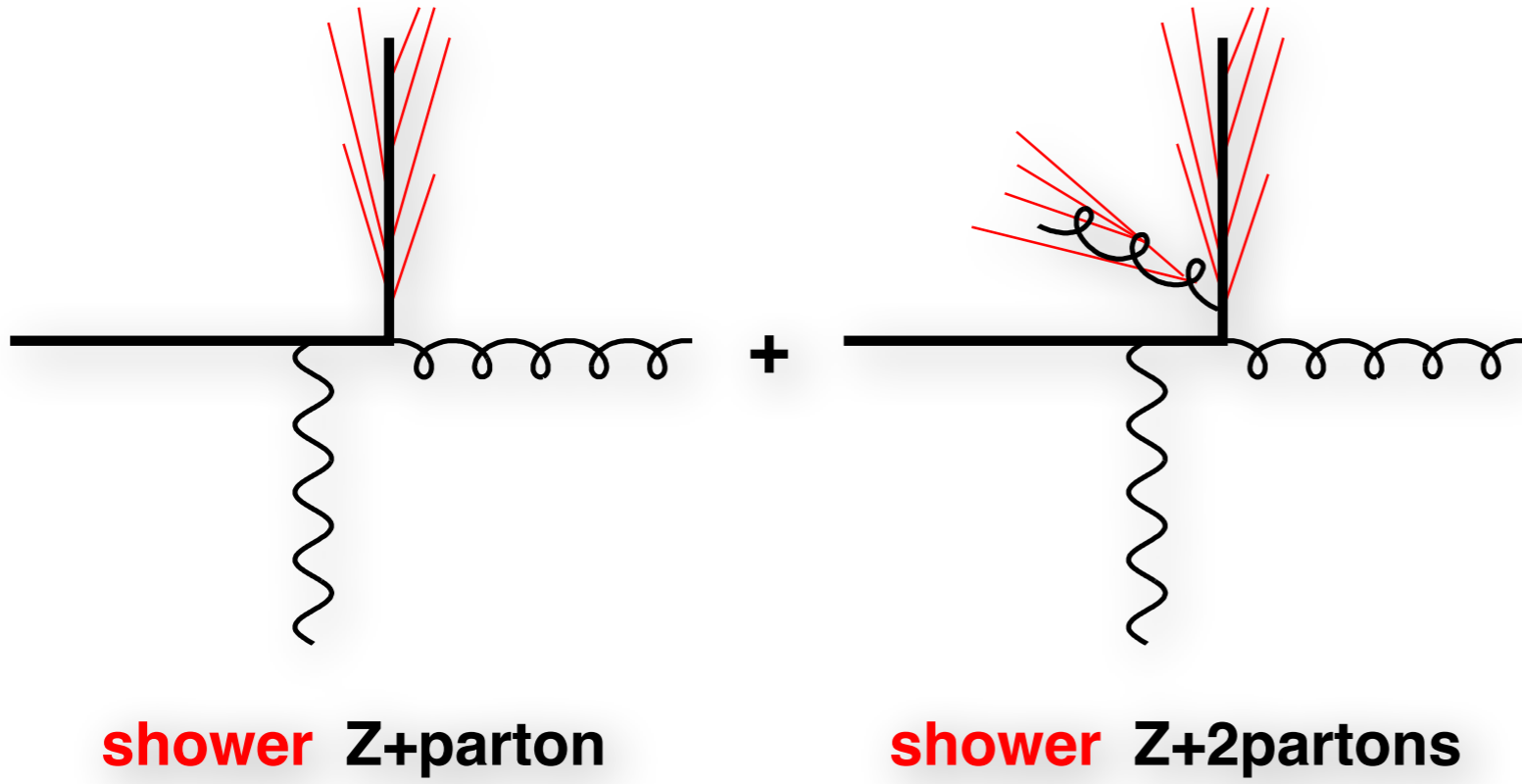


shower Z+parton

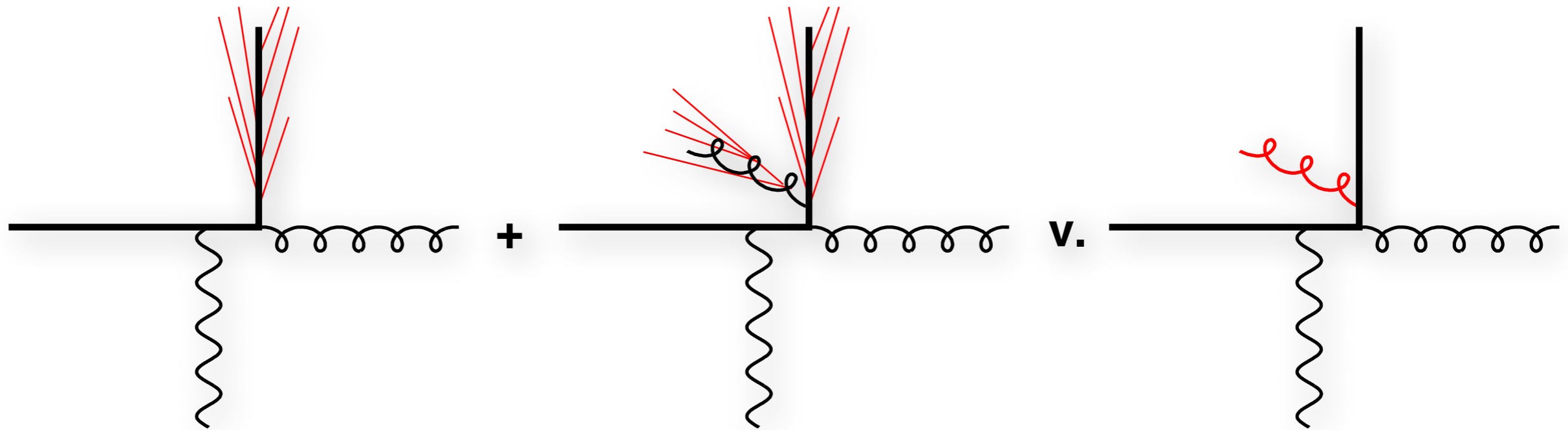
MLM matching



MLM matching



MLM matching

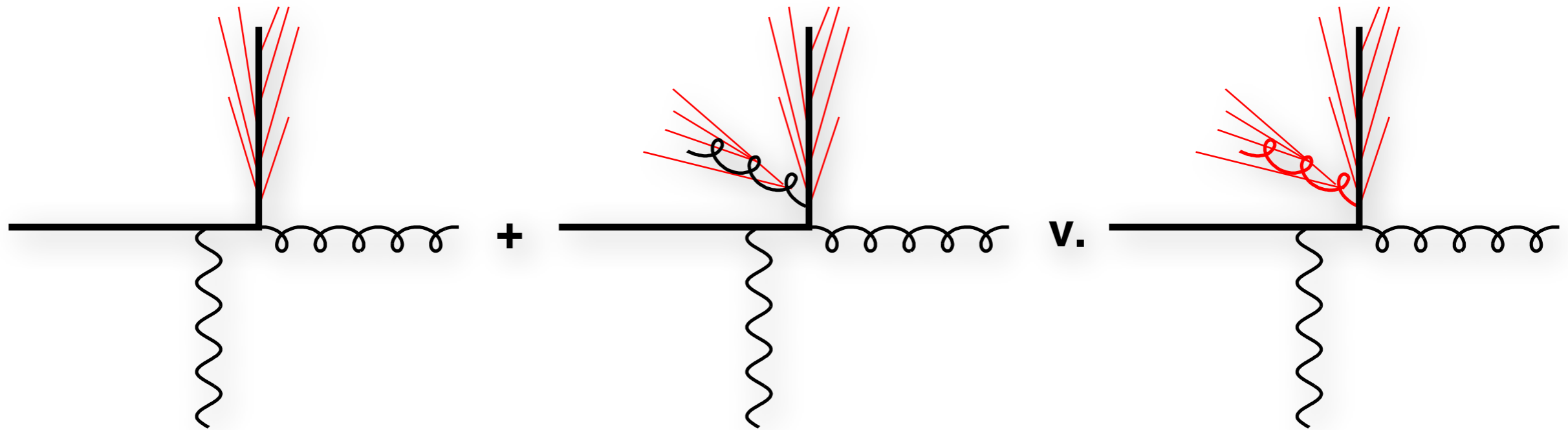


shower Z+parton

shower Z+2partons

shower of Z+parton
generates hard gluon

MLM matching

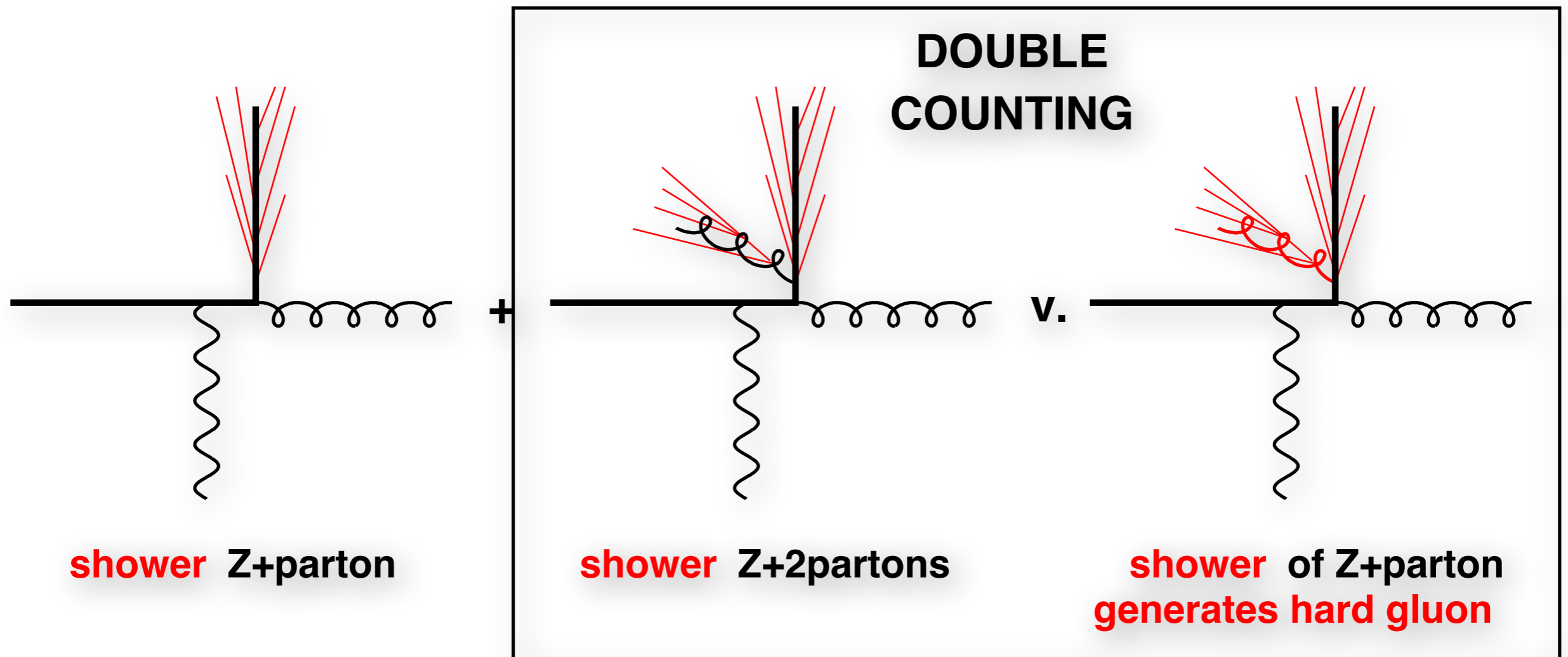


shower Z+parton

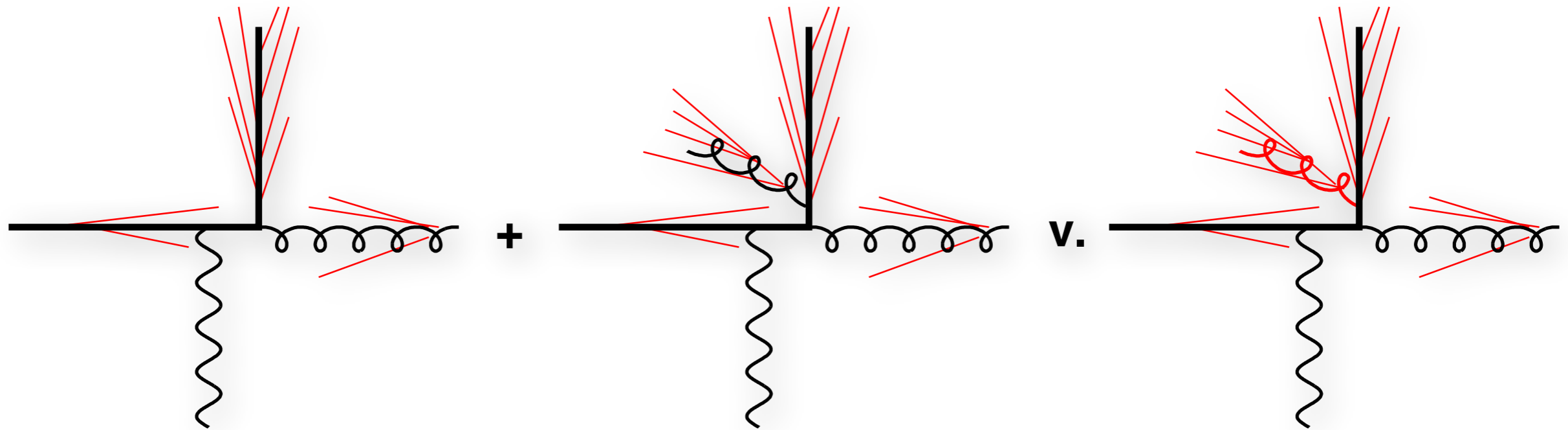
shower Z+2partons

shower of Z+parton
generates hard gluon

MLM matching



MLM matching

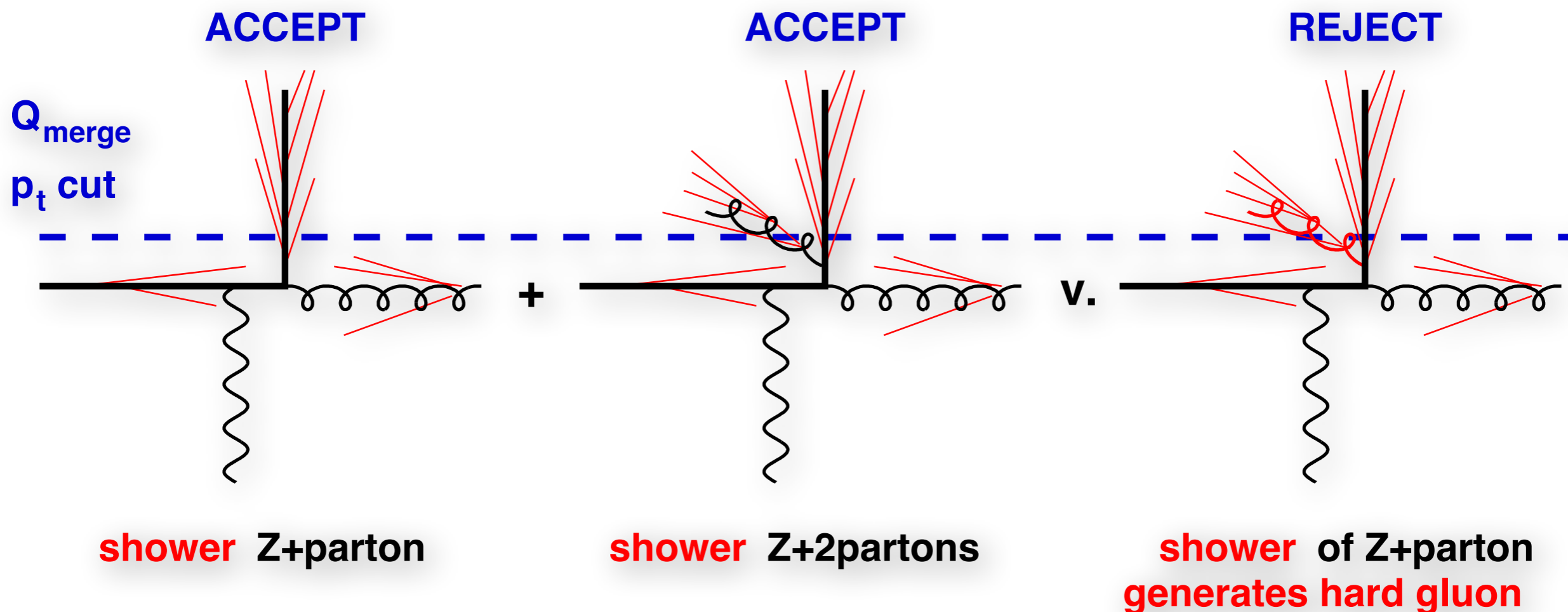


shower Z+parton

shower Z+2partons

shower of Z+parton
generates hard gluon

MLM matching



- Hard jets above scale Q_{merge} have distributions given by tree-level ME
- Rejection procedure eliminates “double-counted” jets from parton shower
- Rejection generates Sudakov form factors between individual jet scales

An alternative approach is called **CKKW** (similar in spirit, Sudakov put in manually)₃₂

Combining NLO accuracy with parton showers (1)

MC@NLO ideas

Frixione & Webber '02

- ▶ Expand your Monte Carlo branching to first order in α_s
Rather non-trivial – requires deep understanding of MC
- ▶ Calculate differences wrt true $\mathcal{O}(\alpha_s)$ both in real and virtual pieces
- ▶ If your Monte Carlo gives correct soft and/or collinear limits, those differences are **finite**
- ▶ Generate extra partonic configurations with phase-space distributions proportional to those differences and shower them

$$\text{MC@NLO} = \text{MC} \times \left(1 + \alpha_s(\sigma_{1V} - \sigma_{1V}^{\text{MC}}) + \alpha_s \int dE(\sigma_{1R}(E) - \sigma_{1R}^{\text{MC}}(E)) \right)$$

All weights finite, but can be ± 1

almost any process can be generated automatically in MadGraph5_aMCatNLO (+ Pythia); also in Sherpa & Herwig

Combining NLO accuracy with parton showers (2)

POWHEG ideas

Aims to work around MC@NLO limitations

Nason '04

- ▶ the (small fraction of) negative weights
- ▶ the tight interconnection with a specific MC

Principle

- ▶ Write a simplified Monte Carlo that generates **just one emission** (the hardest one) which alone gives the correct NLO result.

Essentially uses special Sudakov

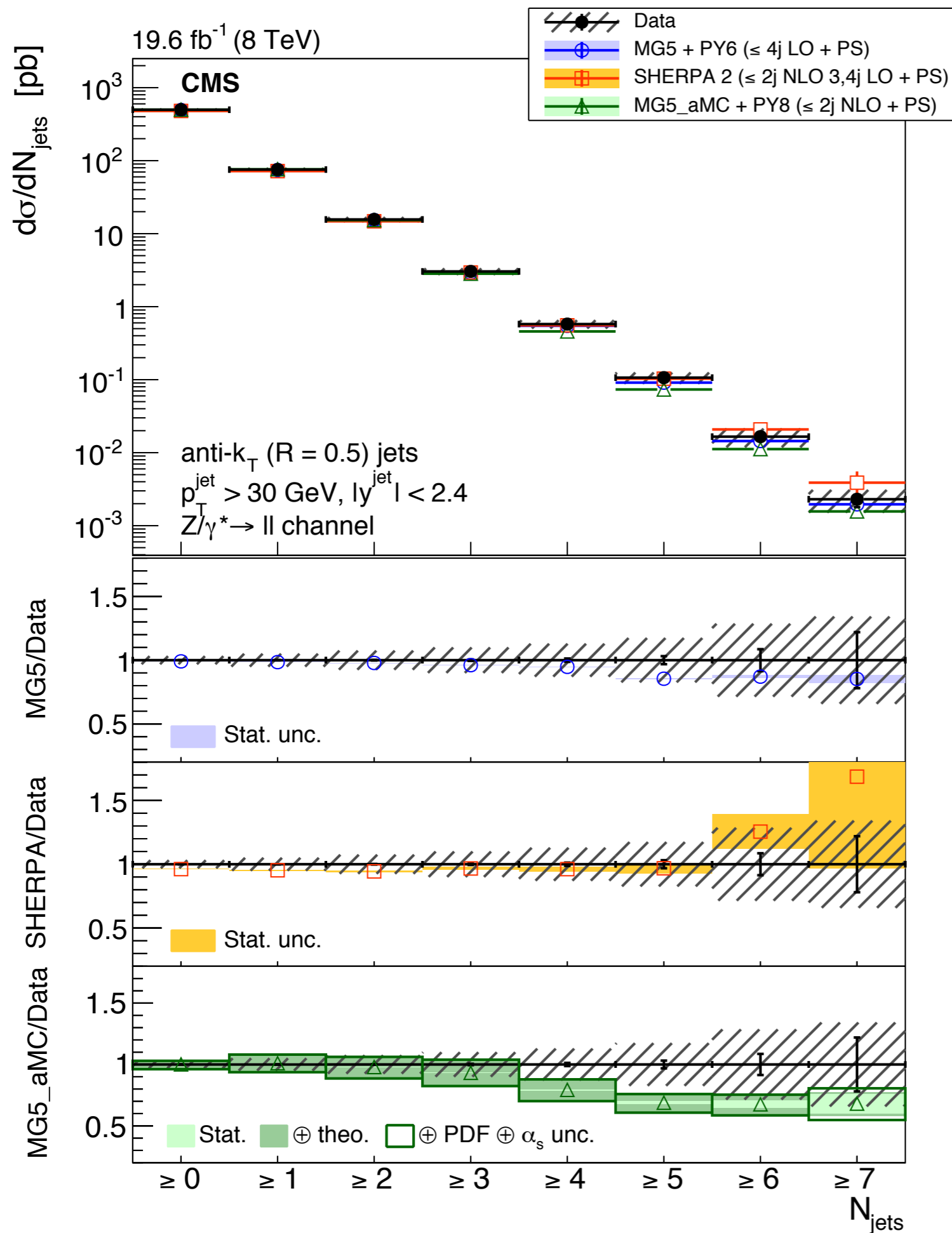
$$\Delta(k_t) = \exp\left(-\int \text{exact real-radiation probability above } k_t\right)$$

- ▶ Lets your default parton-shower do branchings below that k_t .

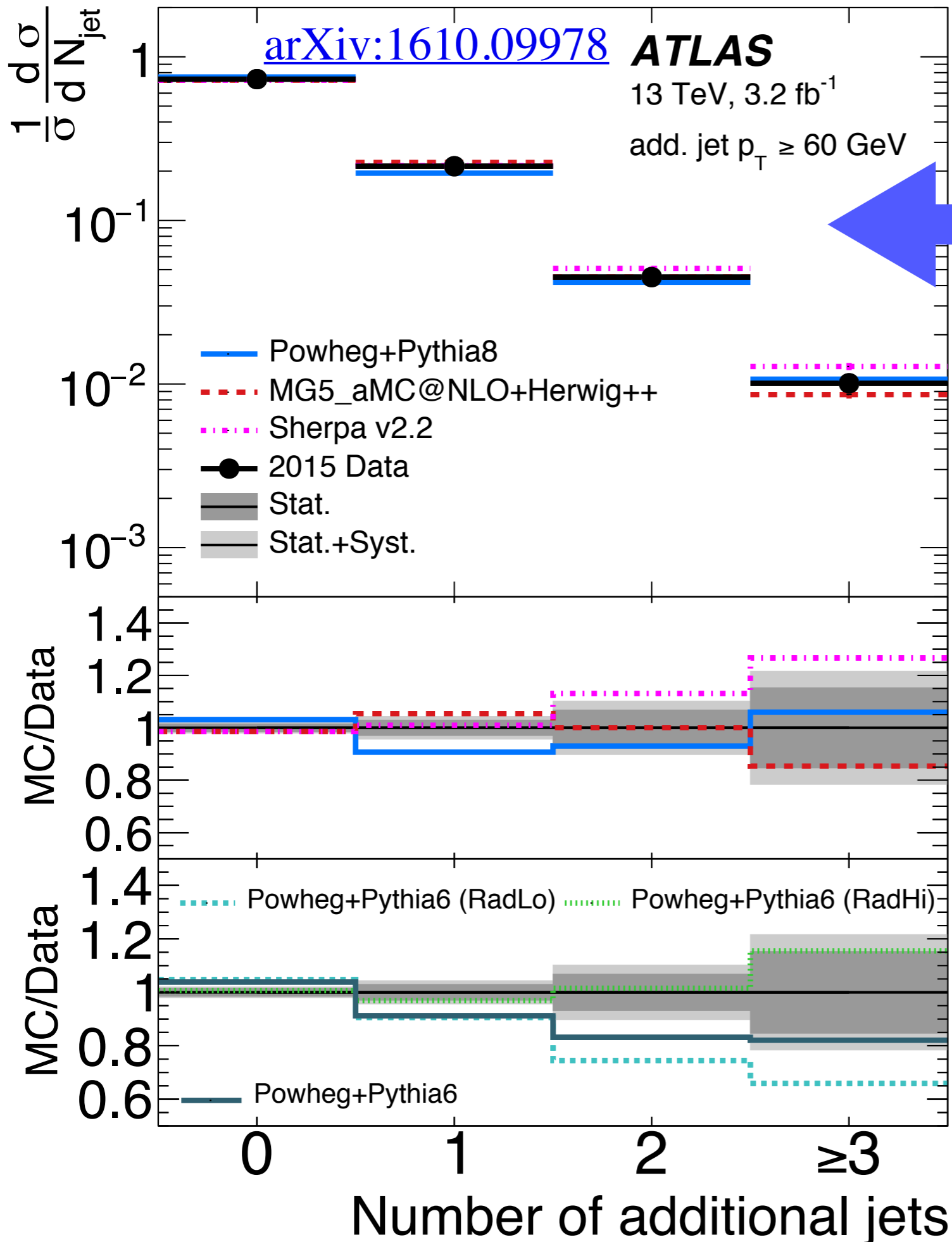
**most processes available in the POWHEGBox
(+Pythia or Herwig; or natively in Herwig)**

Other advances & research directions

- (Much) more efficient ways of combining tree-level and showers: Vincia
- Getting shower samples that are simultaneously NLO accurate at different multiplicities (FxFx, Sherpa NLO matching)
- Showers with NNLO fixed order: MiNNLO, Geneva, [UNNLOPS]
- Showers that are NLL accurate: PanScales, Alaric, Apollo, FHP
- Steps towards NNLL accurate showers: PanScales
- Understanding interplay of matching & log accuracy, subleading colour accuracy in showers, etc.

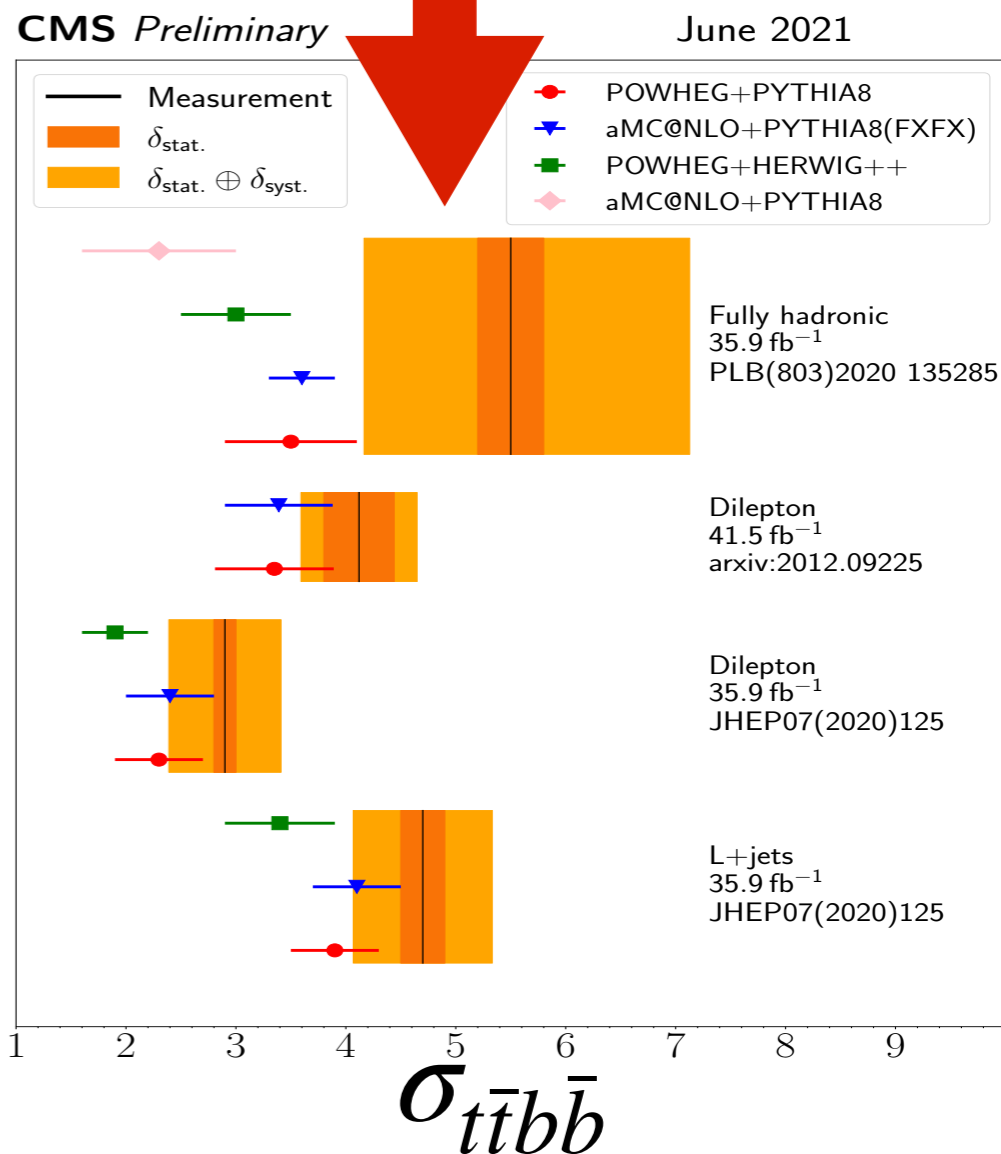


- Modern tools give good predictions for multijet rates **with vector bosons**
- (up to ~ 4 jets, sometimes beyond)



Modern tools → decent predictions for top quarks + jets

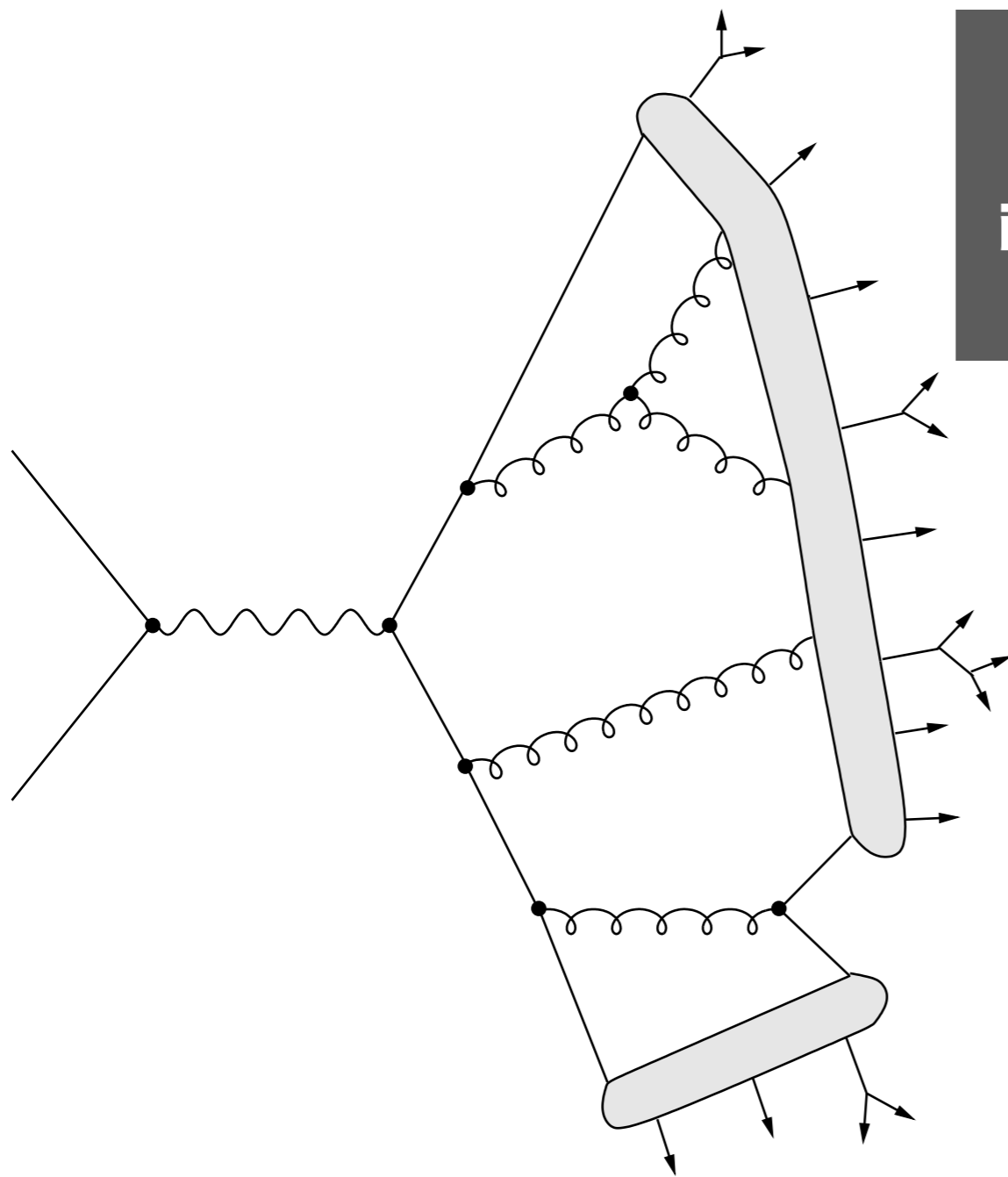
top quarks + heavy-flavour a bit worse?



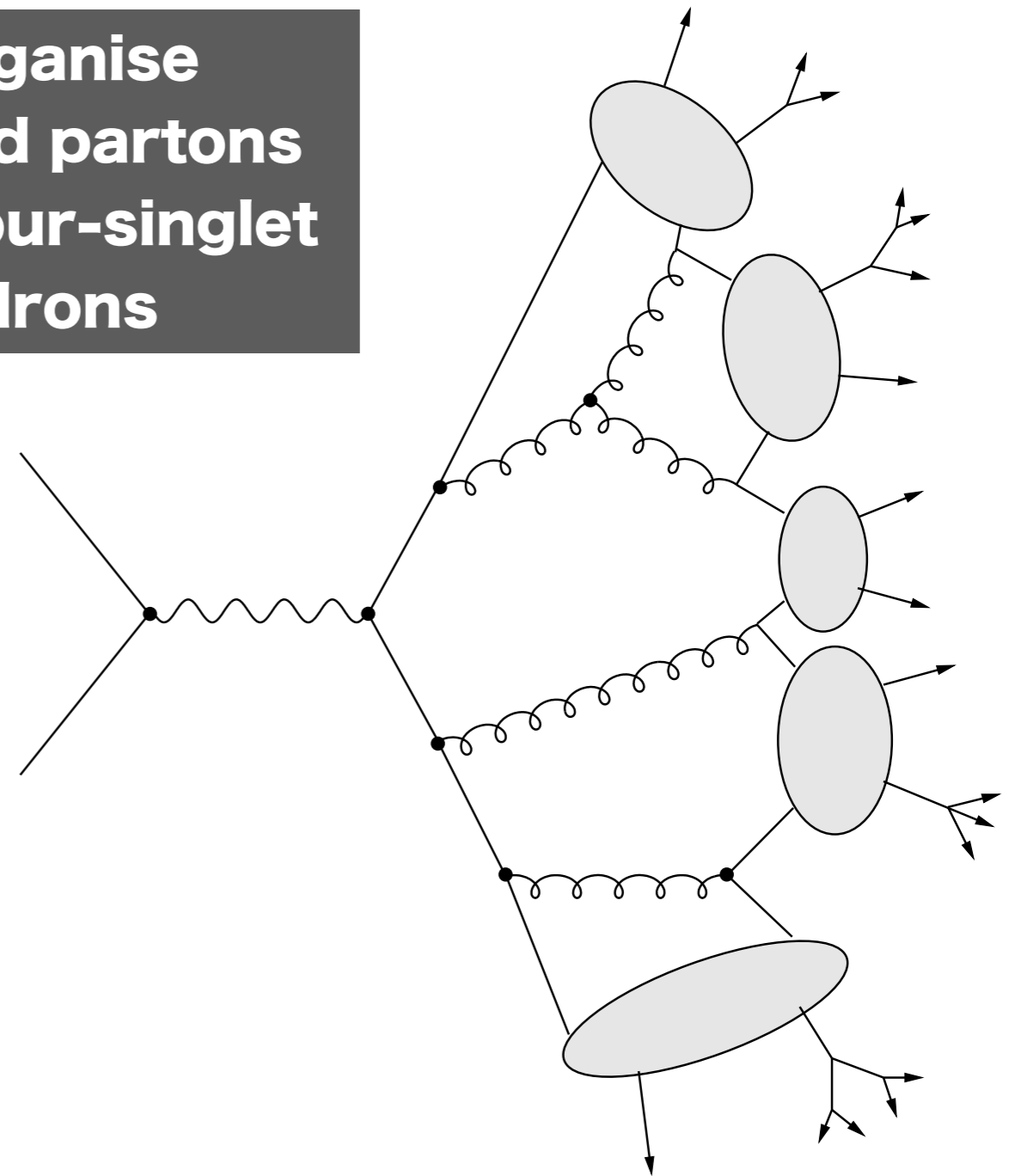
hadronisation & MPI

*essential models for realistic events
i.e. events with hadrons*

two main models for the parton-hadron transition (“hadronisation”)



reorganise
coloured partons
into colour-singlet
hadrons

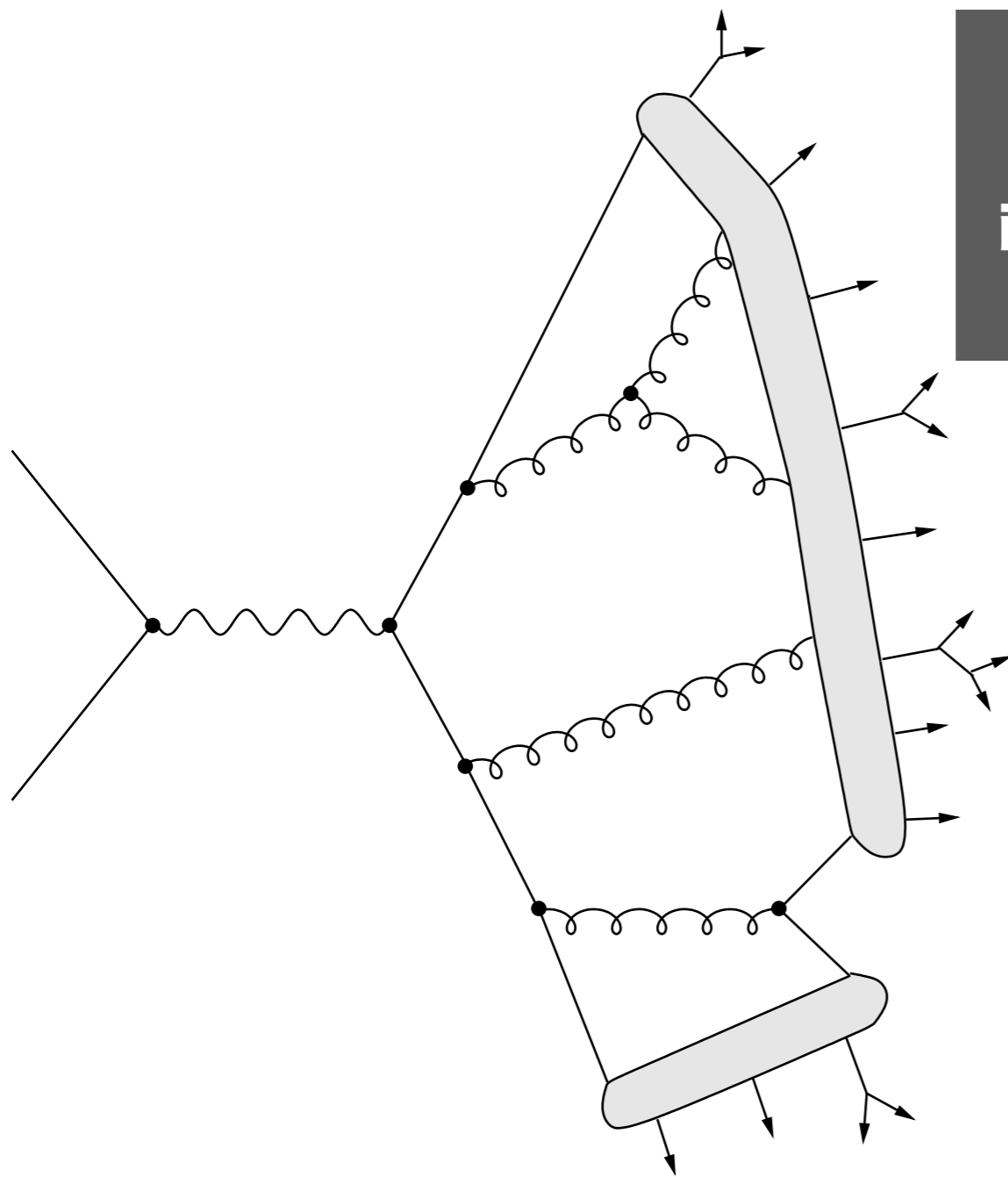


String Fragmentation
(Pythia and friends)

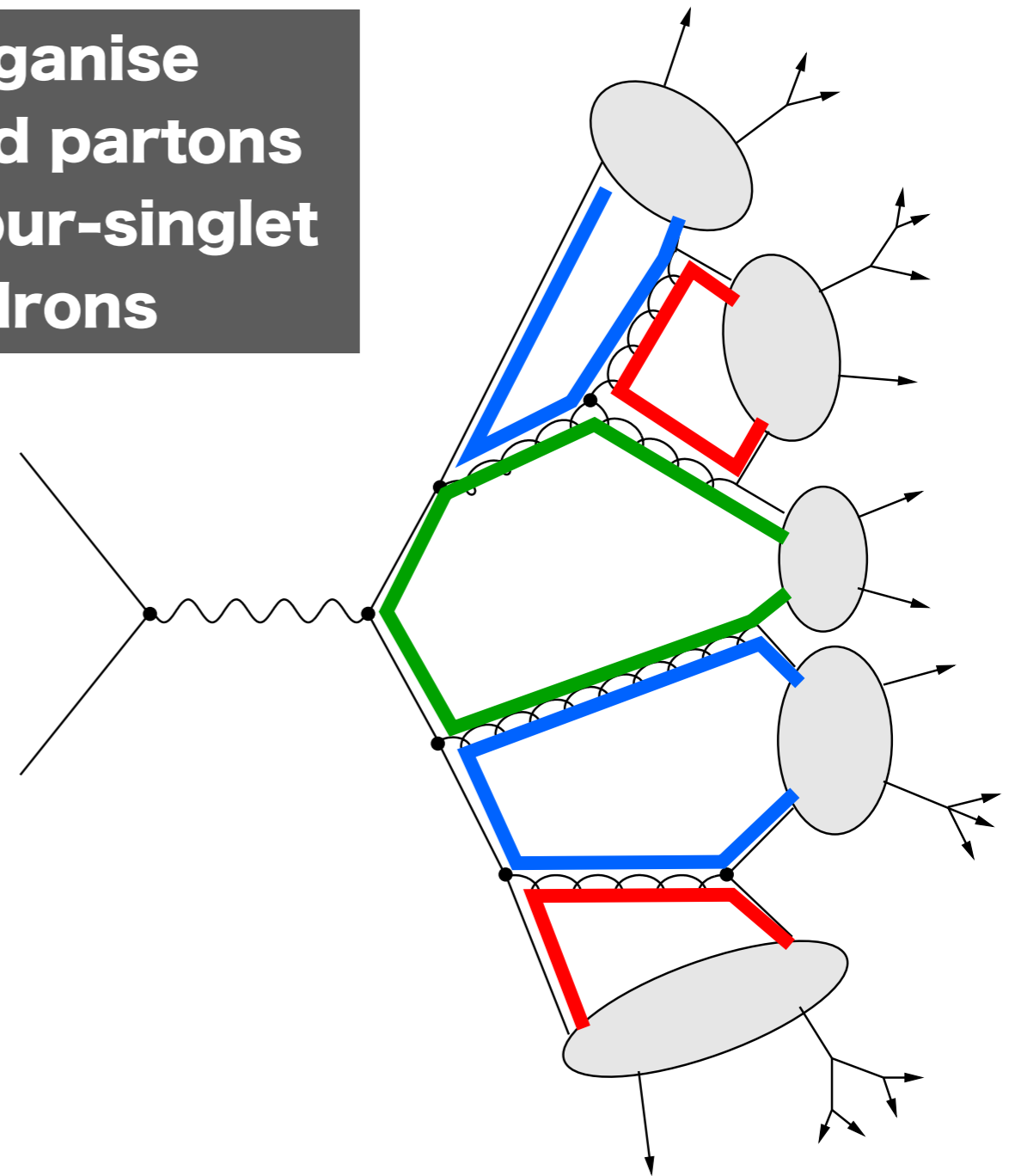
Cluster Fragmentation
(Herwig) (& Sherpa)

Pictures from ESW book

two main models for the parton-hadron transition (“hadronisation”)



reorganise
coloured partons
into colour-singlet
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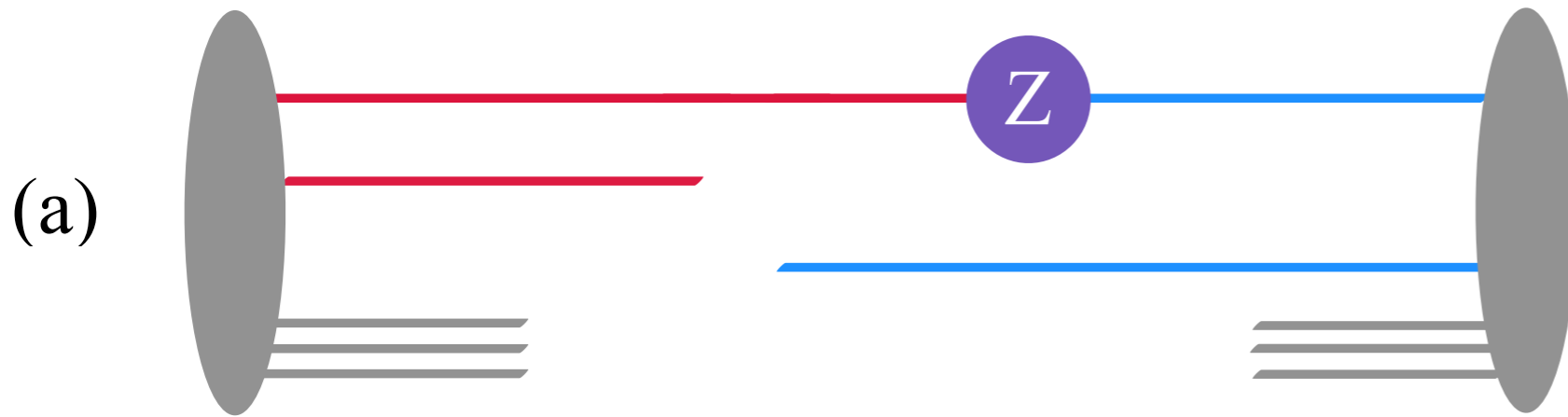


String Fragmentation
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Cluster Fragmentation
(Herwig) (& Sherpa)

Pictures from ESW book

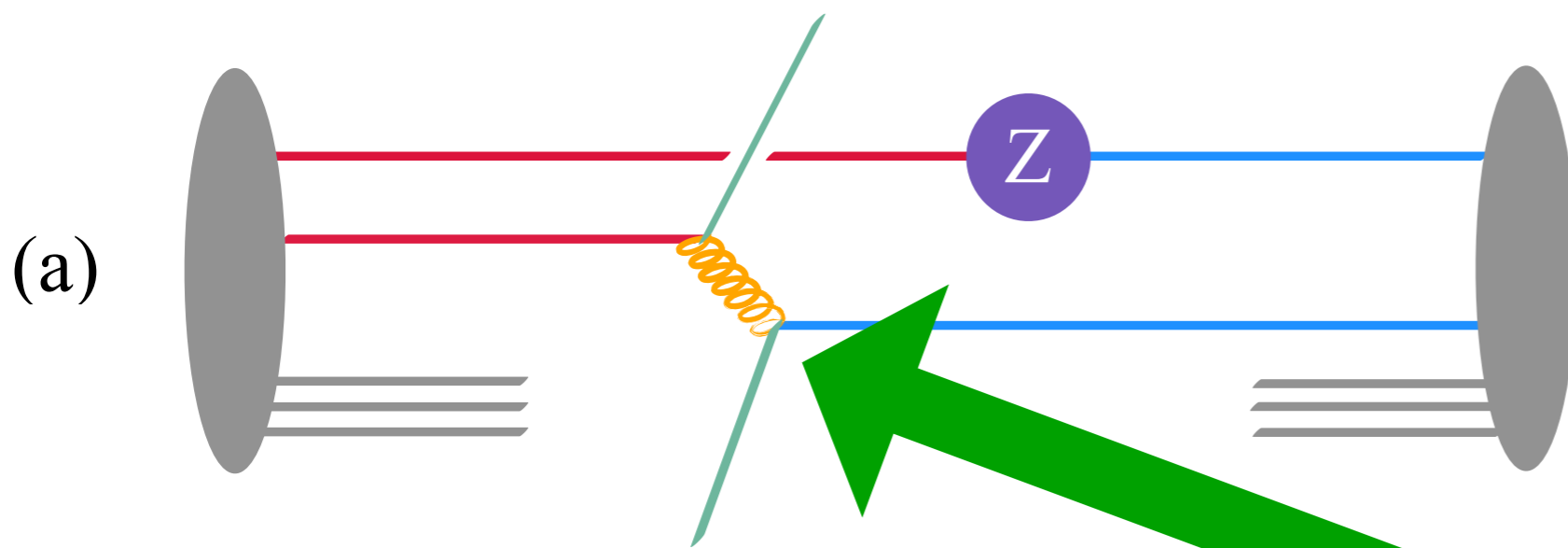
multi-parton interactions (MPI, a.k.a. **underlying event**)



figures taken from
[2307.05693](#)

Models such as
Pythia have ~ 10
MPI scatterings per
hard pp collision

multi-parton interactions (MPI, a.k.a. **underlying event**)



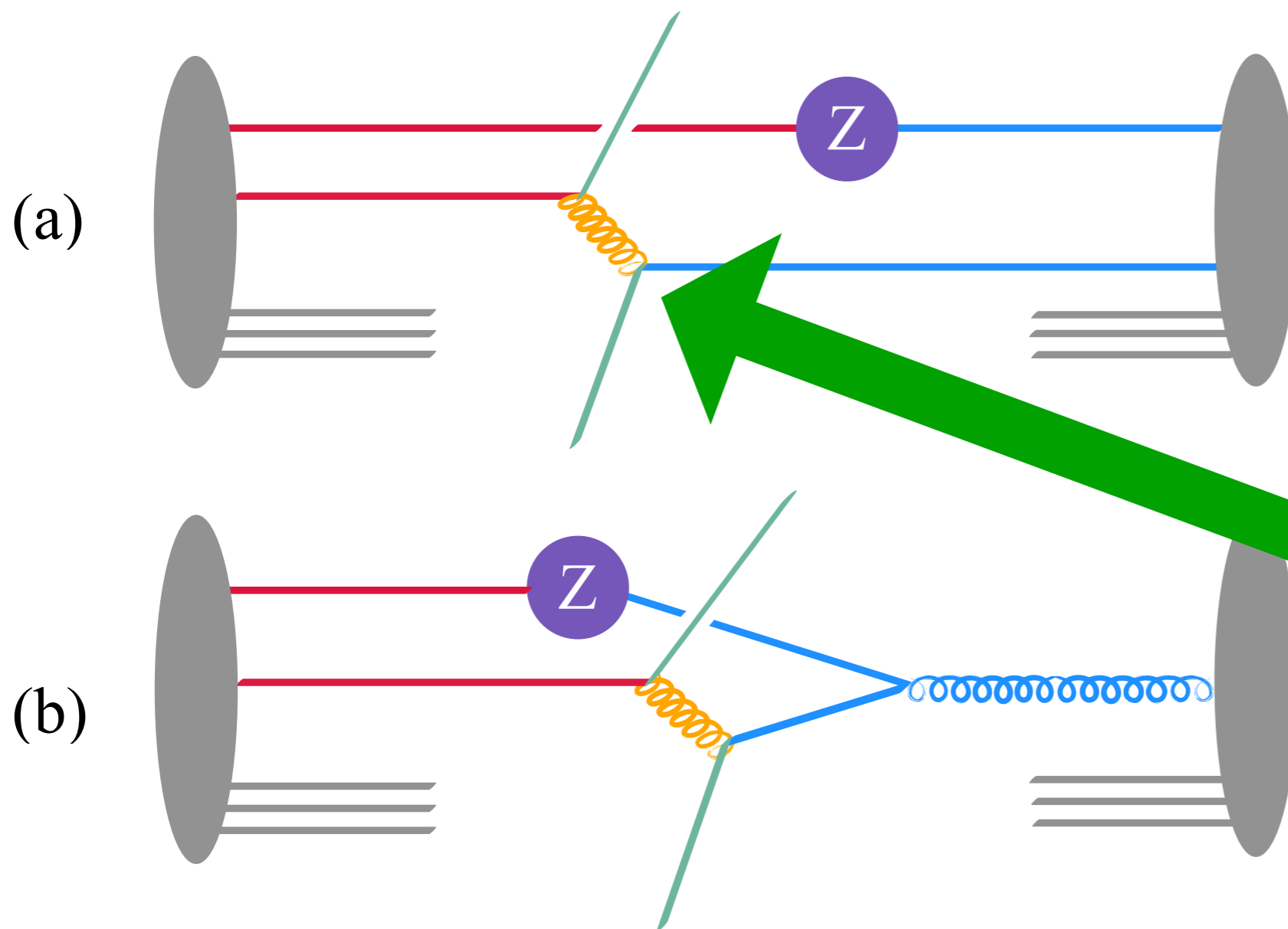
*figures taken from
2307.05693*

**Additional 2→2
scatterings of
multiple other
partons in the
incoming protons**

Models such as
Pythia have ~ 10
MPI scatterings per
hard pp collision

multi-parton interactions (MPI, a.k.a. **underlying event**)

*figures taken from
2307.05693*

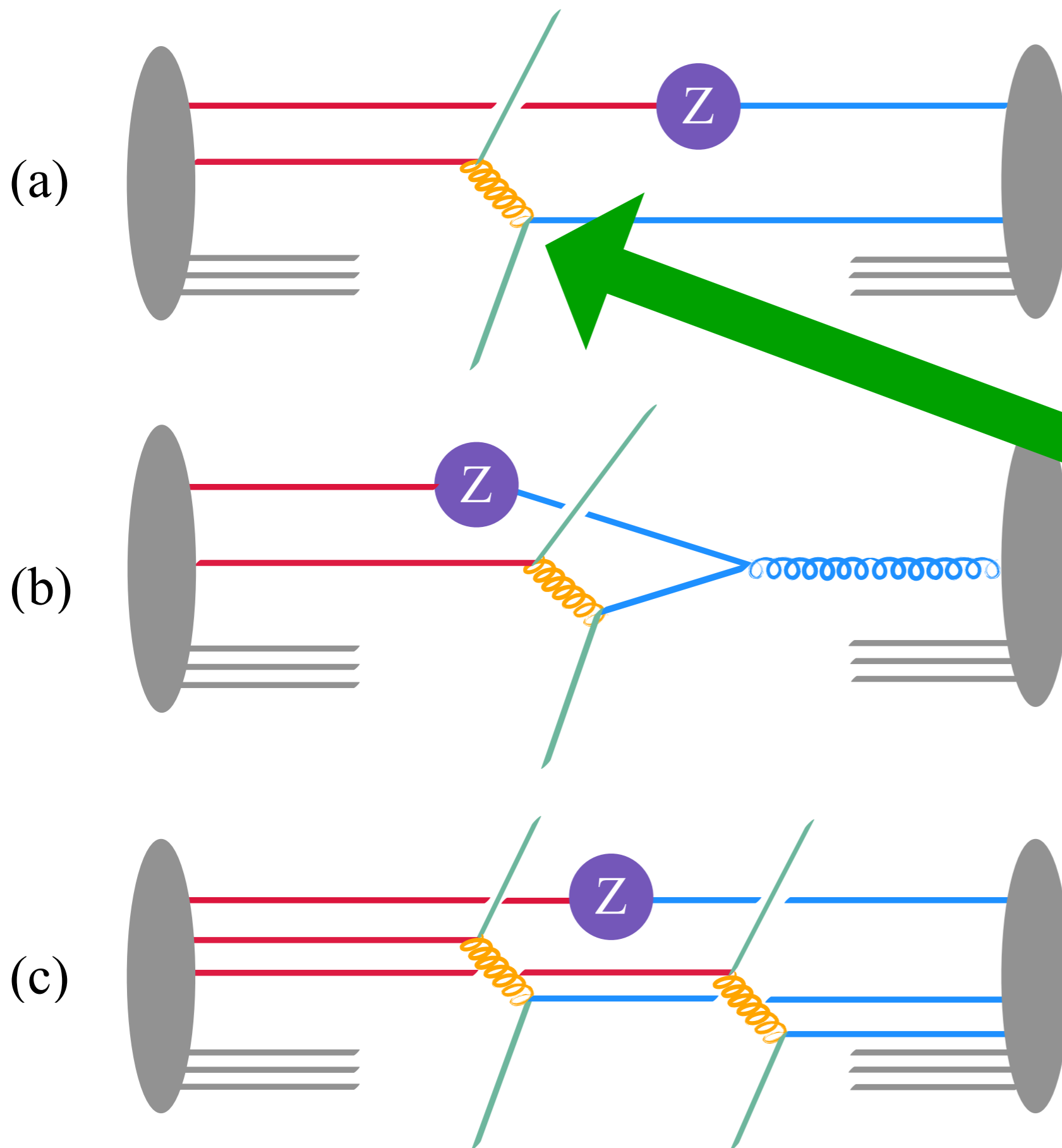


Additional 2→2 scatterings of multiple other partons in the incoming protons

Models such as Pythia have ~ 10 MPI scatterings per hard pp collision

multi-parton interactions (MPI, a.k.a. **underlying event**)

figures taken from
[2307.05693](#)

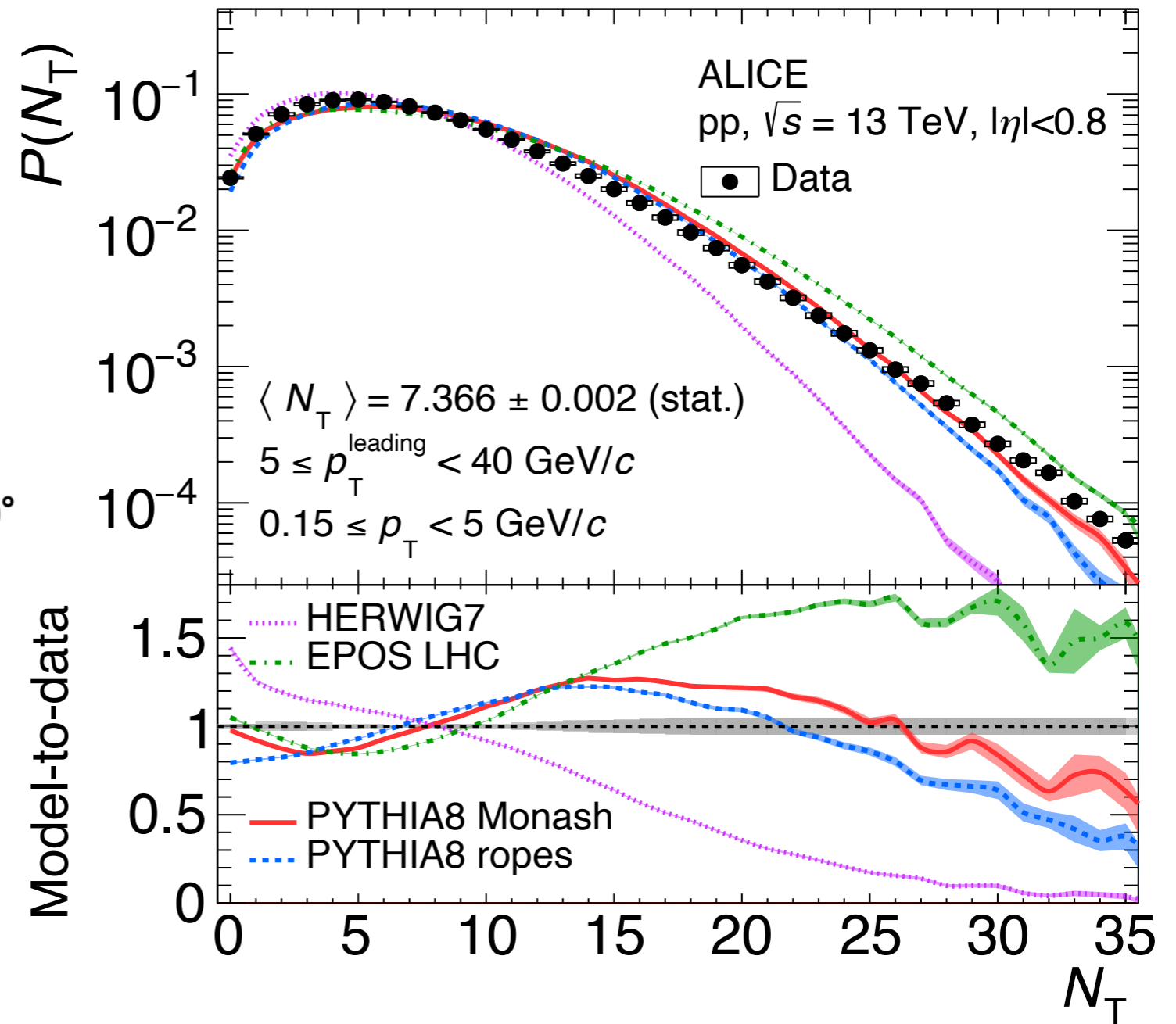
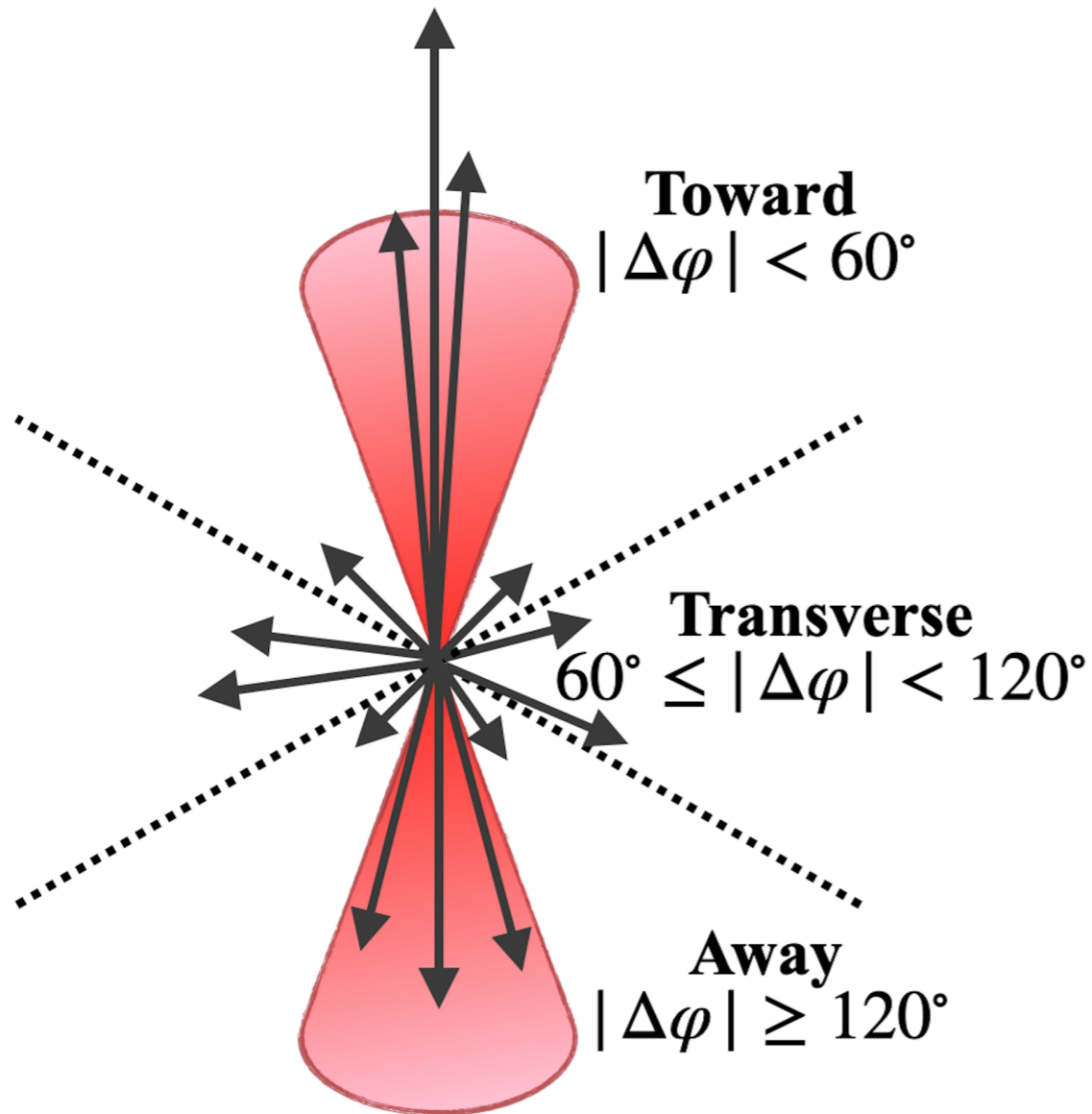


Additional 2→2 scatterings of multiple other partons in the incoming protons

Models such as Pythia have ~ 10 MPI scatterings per hard pp collision

Underlying event properties v. MCs

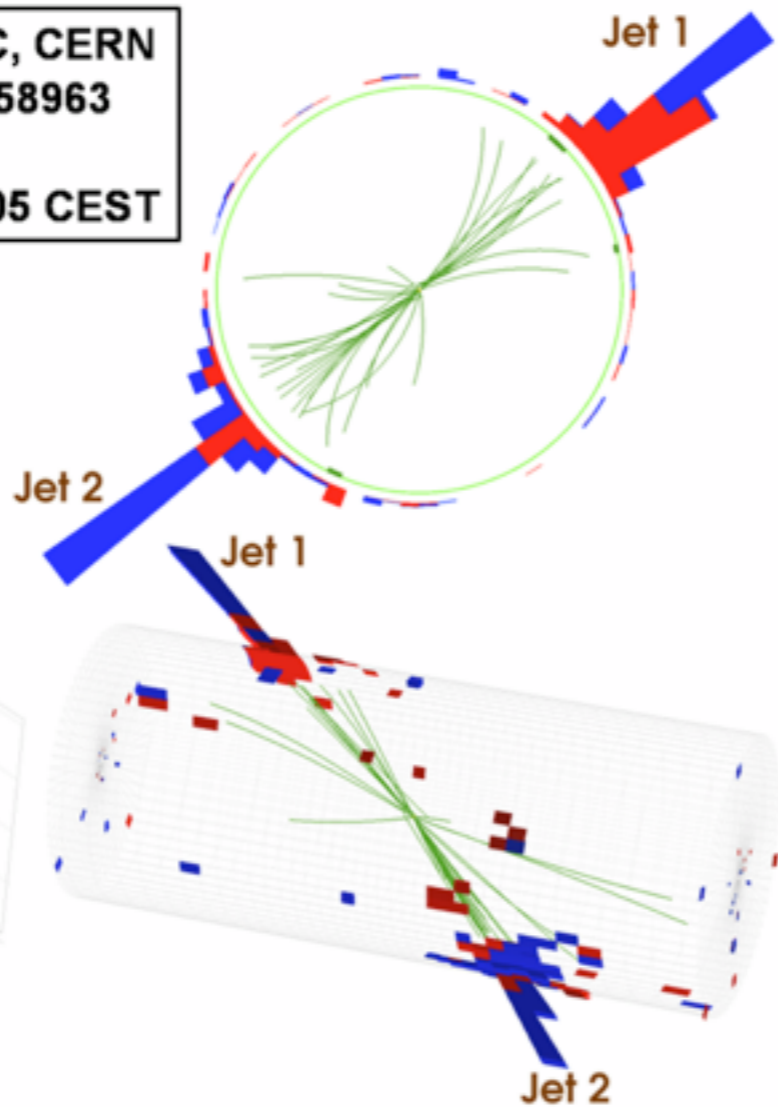
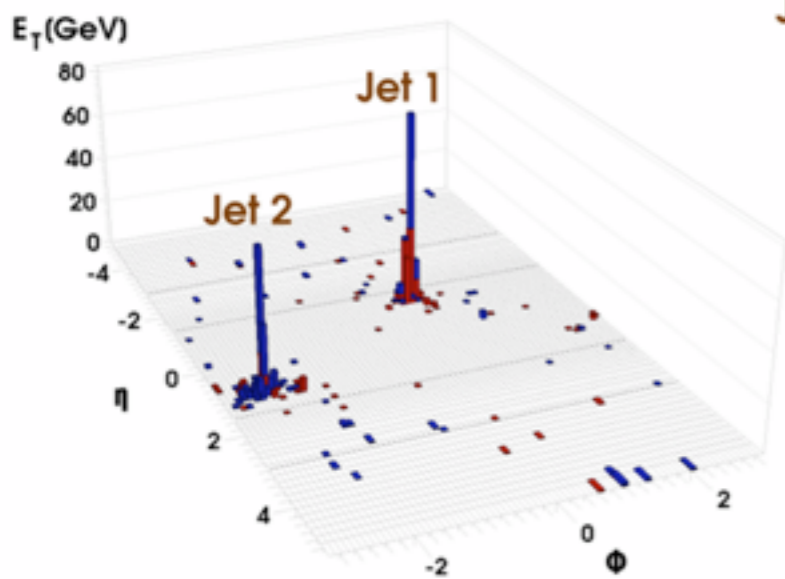
2301.10120



N_T = charged particle multiplicity in the transverse region



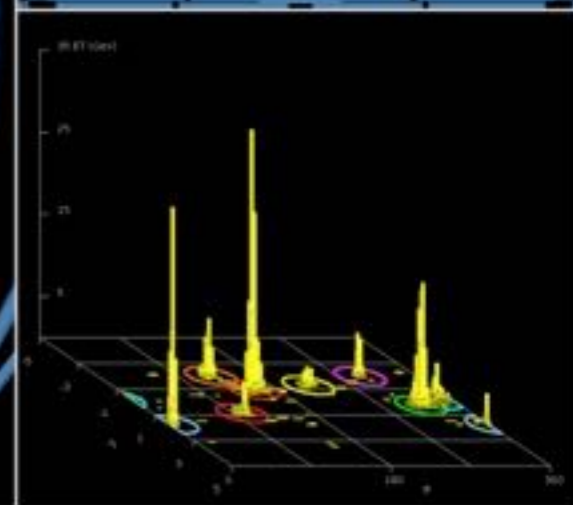
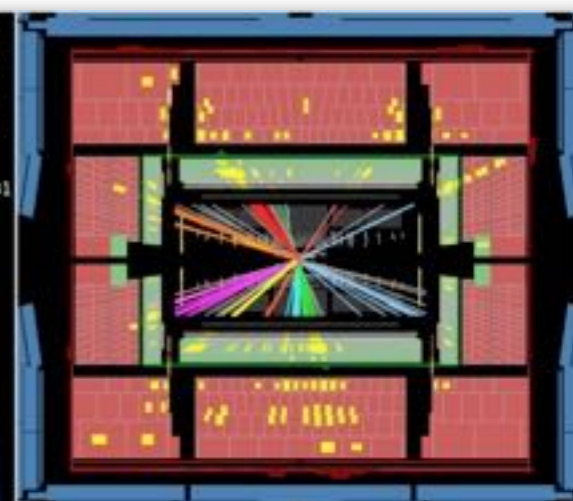
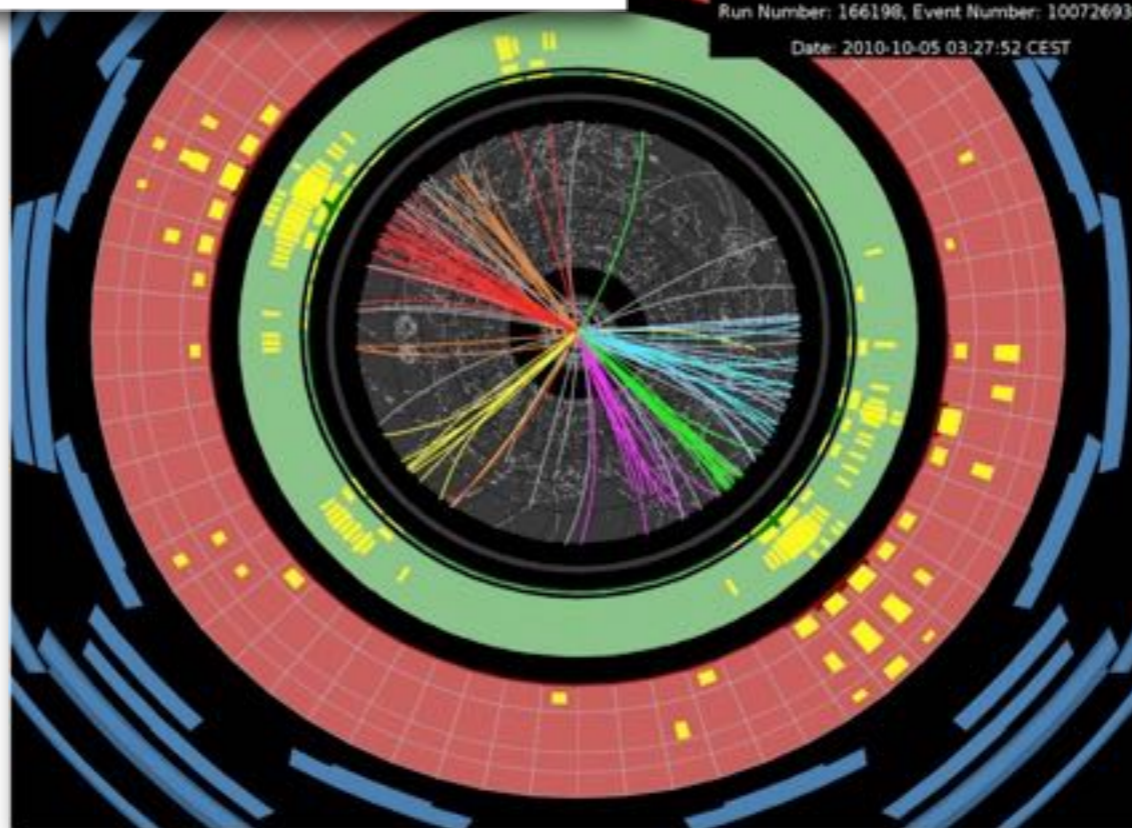
CMS Experiment at LHC, CERN
Run 133450 Event 16358963
Lumi section: 285
Sat Apr 17 2010, 12:25:05 CEST



jets

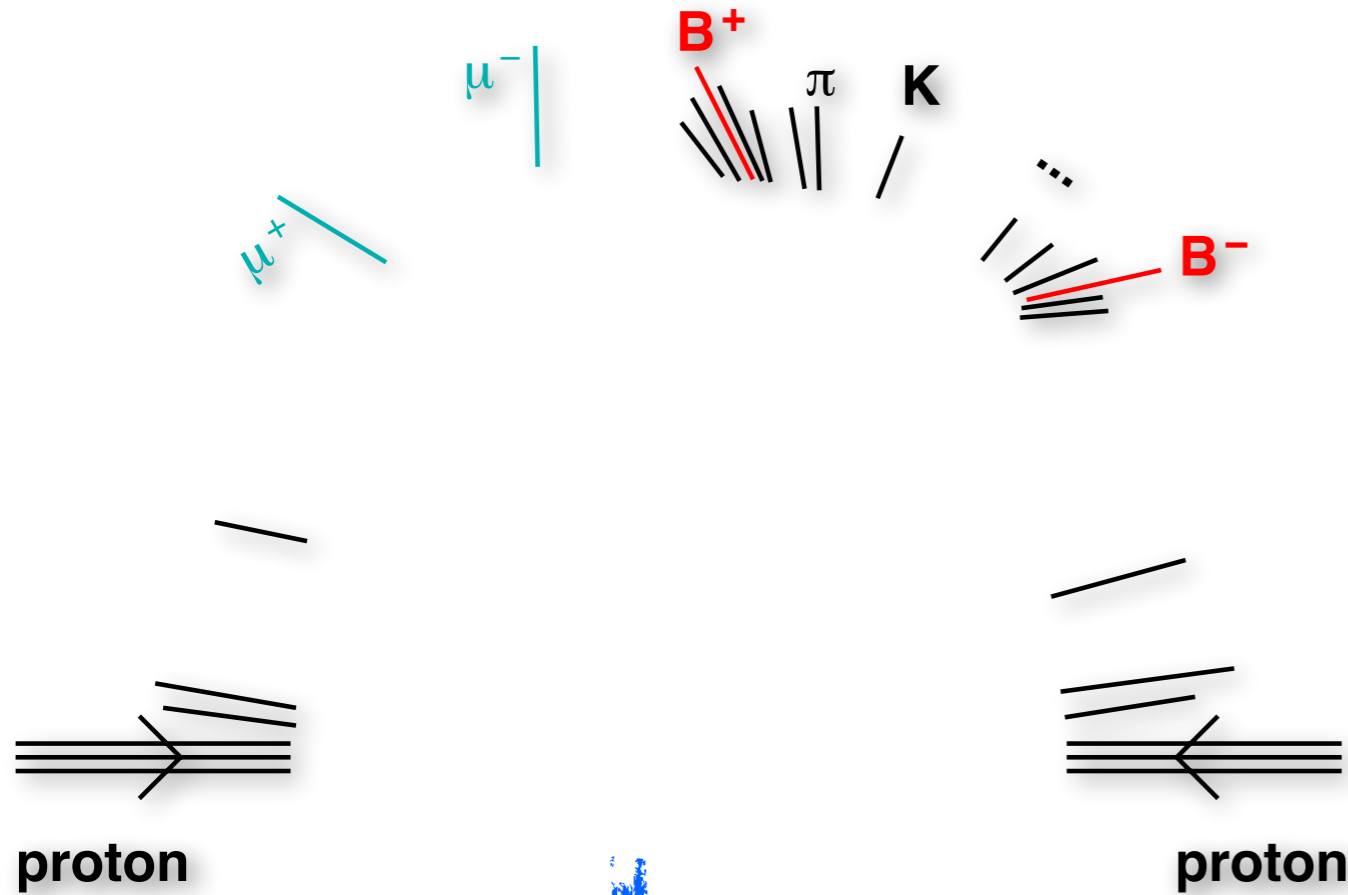
i.e. how we make sense of the hadronic part of events

ATLAS
EXPERIMENT
Run Number: 166198, Event Number: 100726931
Date: 2010-10-05 03:27:52 CEST

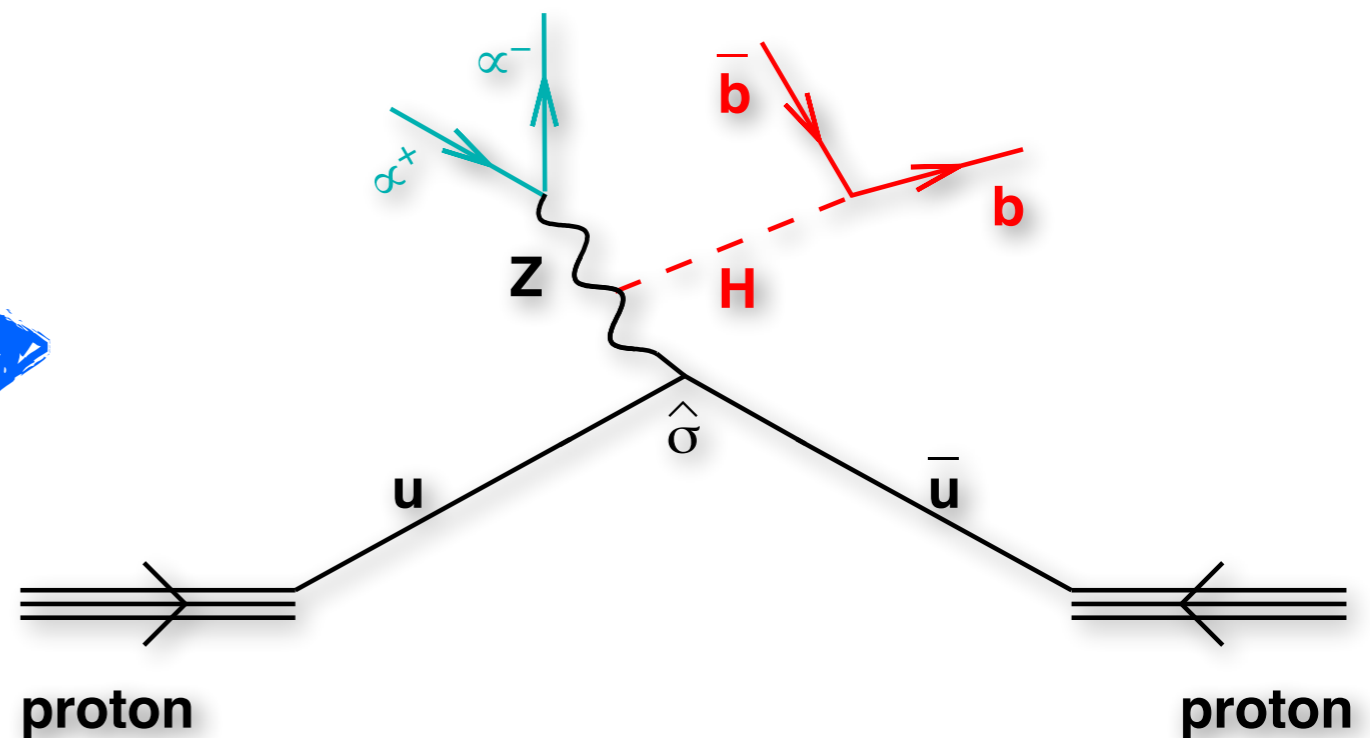


jets

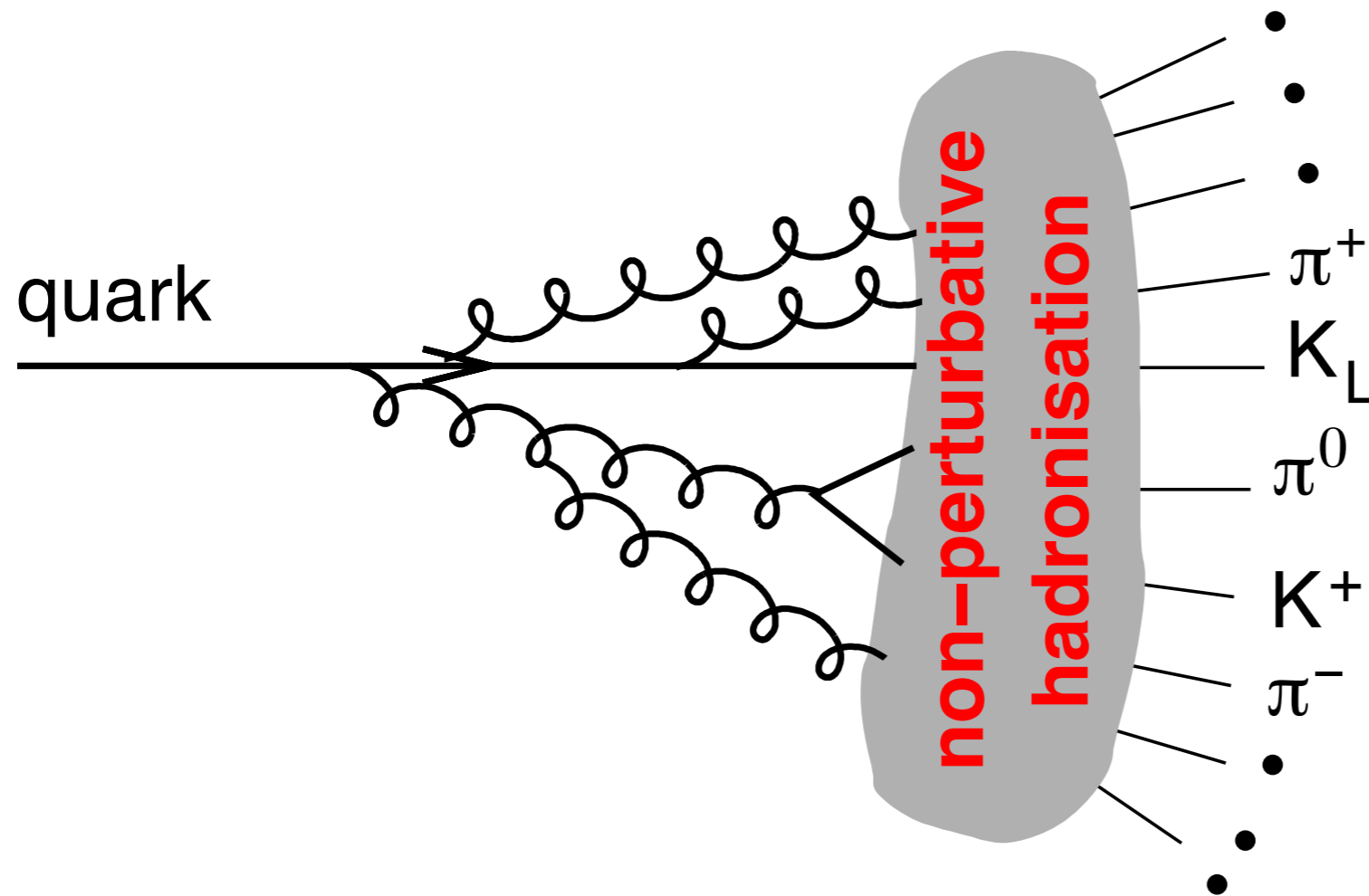
i.e. how we make sense of the hadronic part of events



Interpretation



Why do we see jets?



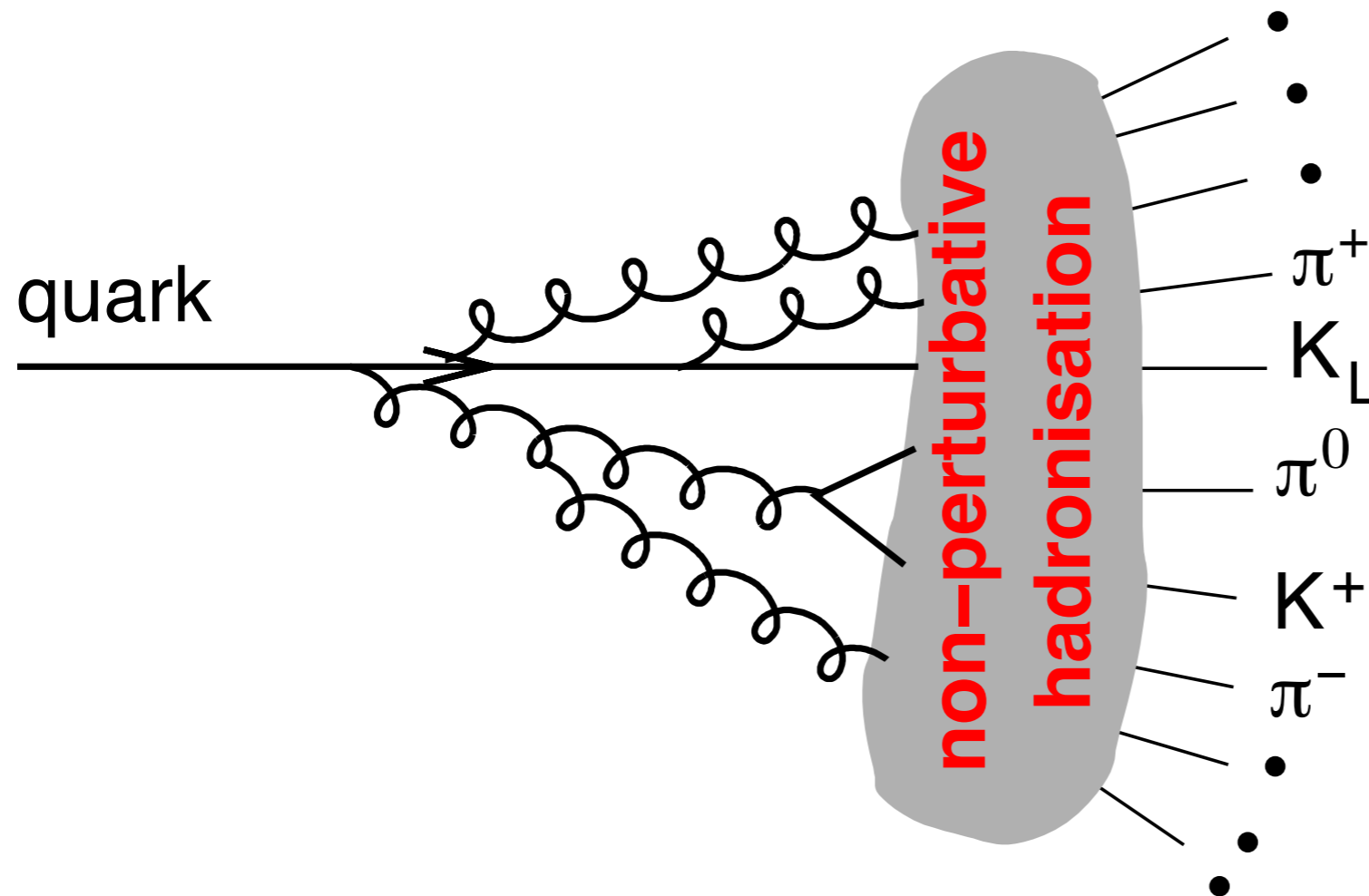
Gluon emission

$$\int \alpha_s \frac{dE}{E} \frac{d\theta}{\theta} \gg 1$$

Non-perturbative physics

$$\alpha_s \sim 1$$

Why do we see jets?



Gluon emission

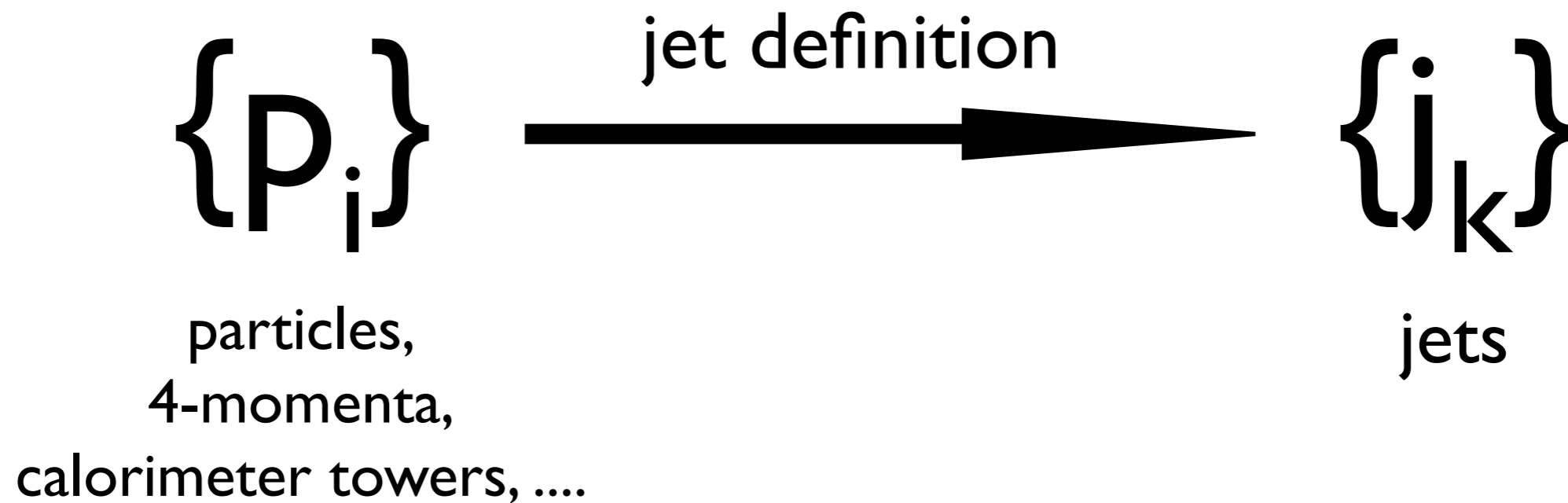
$$\int \alpha_s \frac{dE}{E} \frac{d\theta}{\theta} \gg 1$$

Non-perturbative
physics

$$\alpha_s \sim 1$$

While you can see jets with your eyes, **to do quantitative physics**, you need an algorithmic procedure that **defines what exactly a jet is**

make a choice, specify a **Jet Definition**

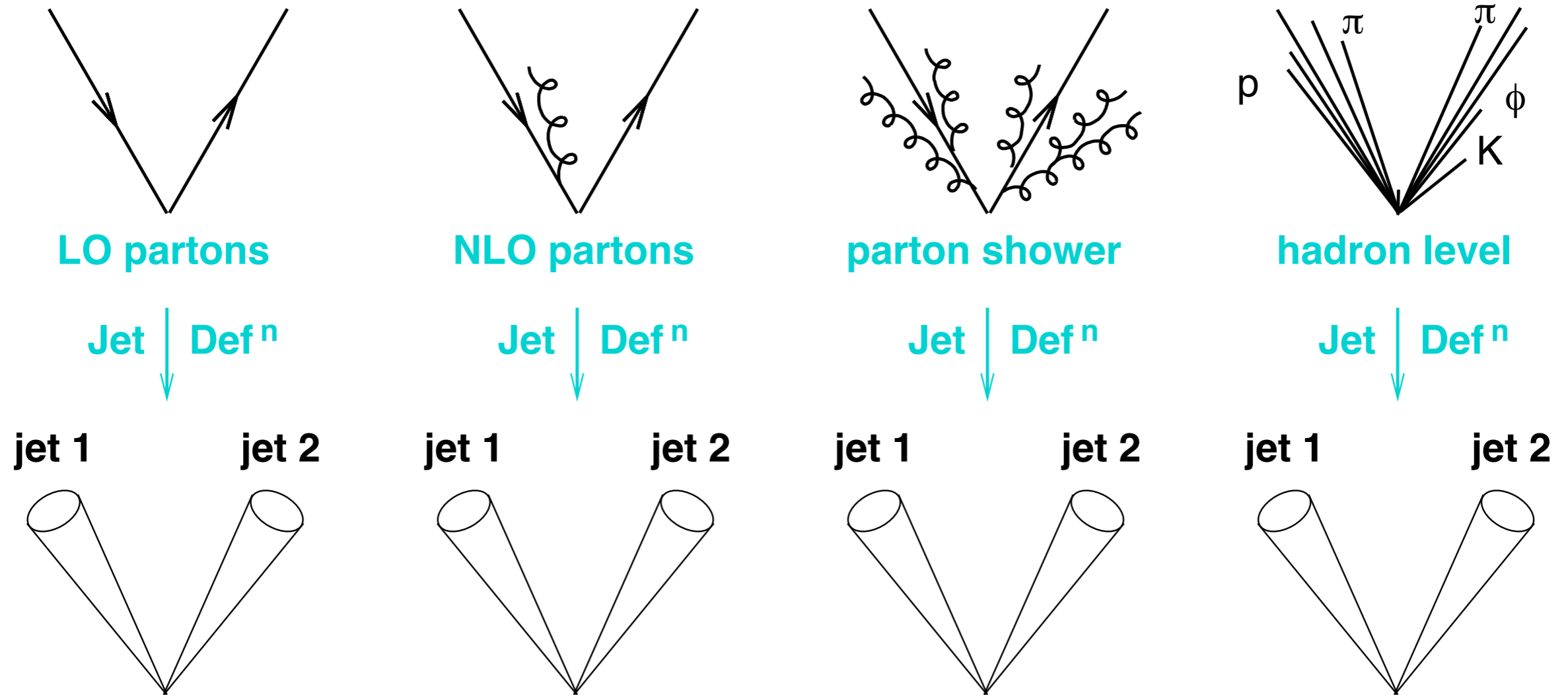


- Which particles do you put together into a same jet?
- How do you recombine their momenta (4-momentum sum is the obvious choice, right?)

“Jet [definitions] are legal contracts between theorists and experimentalists”
-- MJ Tannenbaum

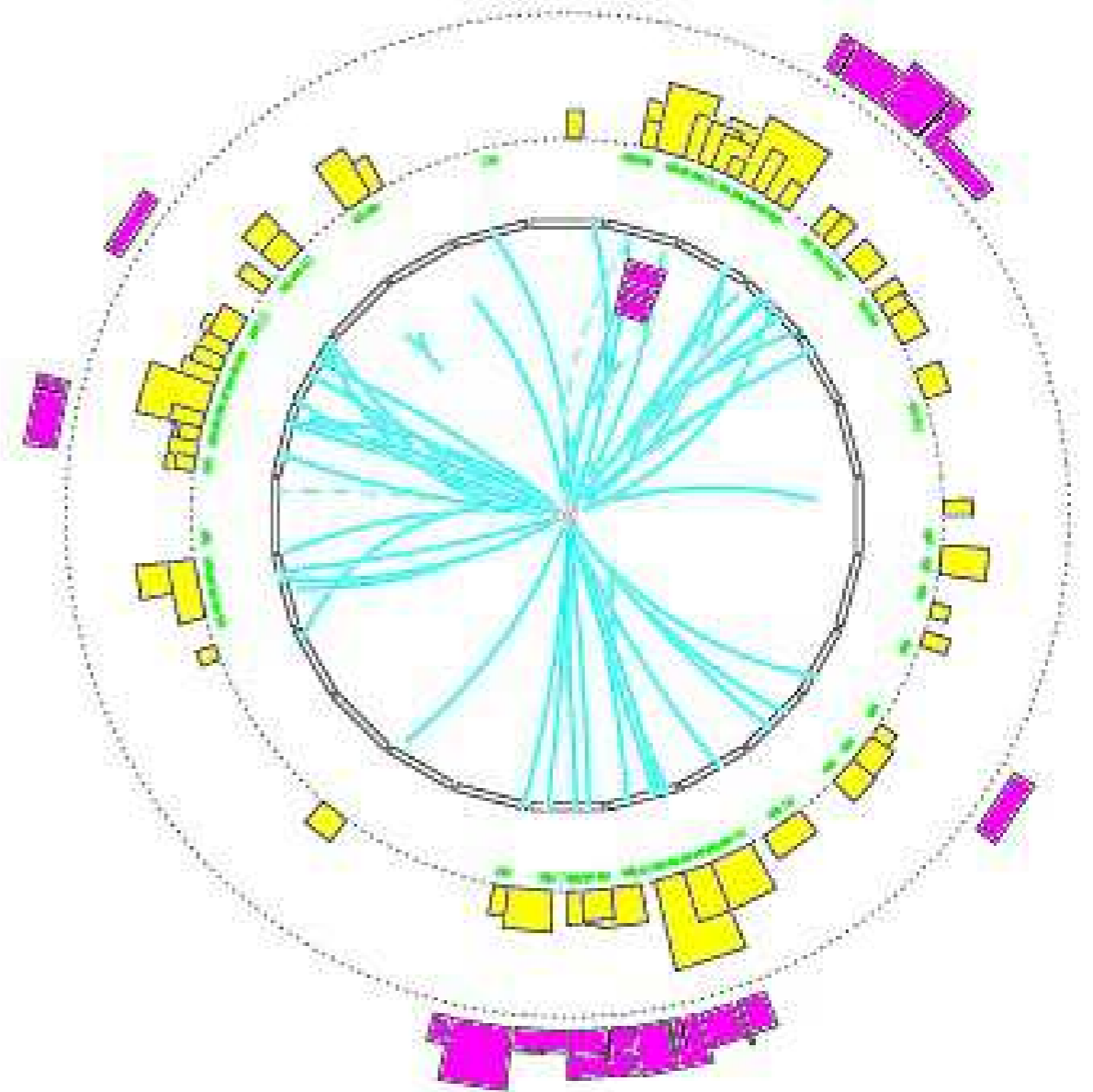
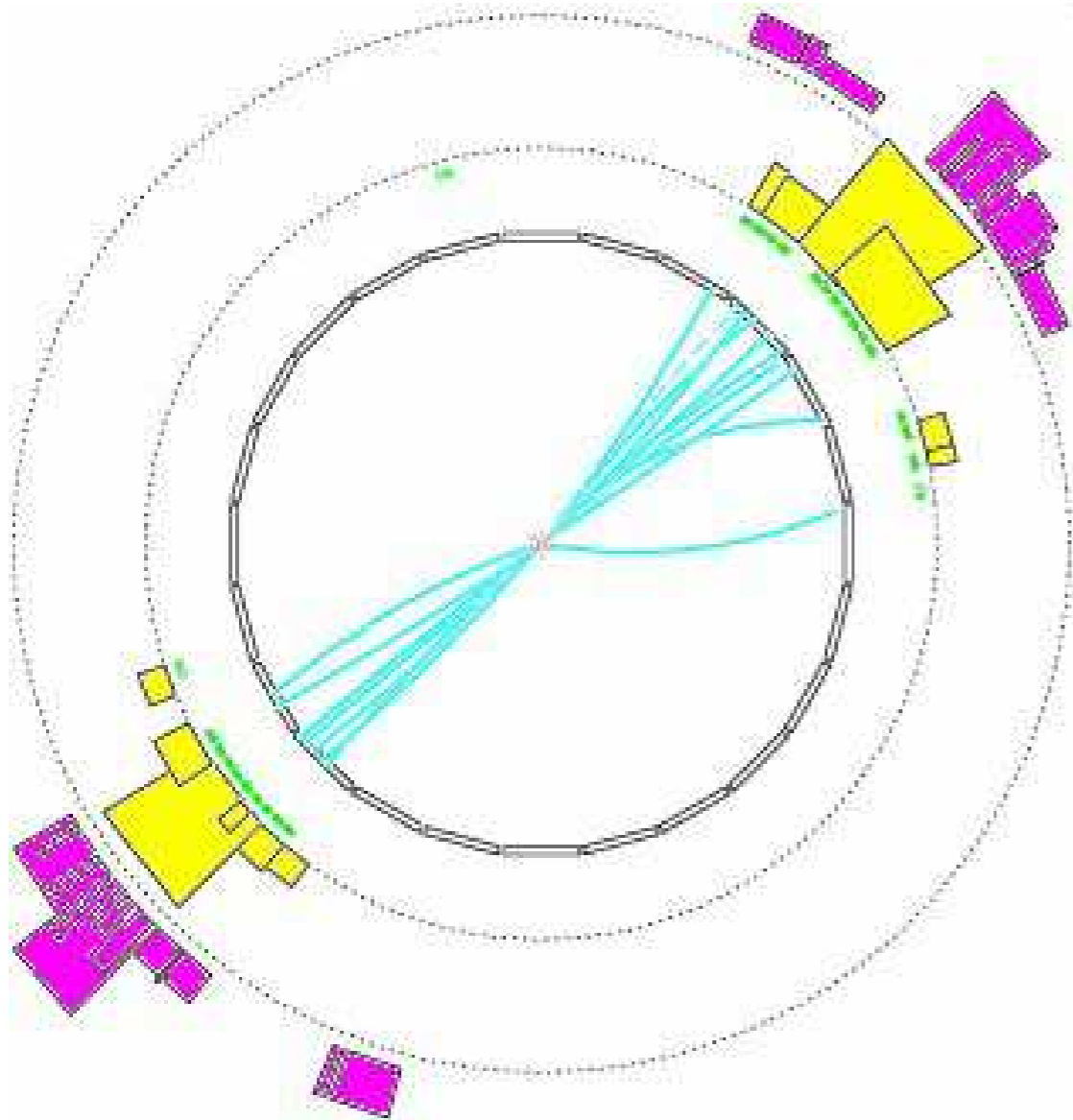
They're also a way of organising the information in an event
1000's of particles per events, up to 40.000,000 events per second

what should a jet definition achieve?

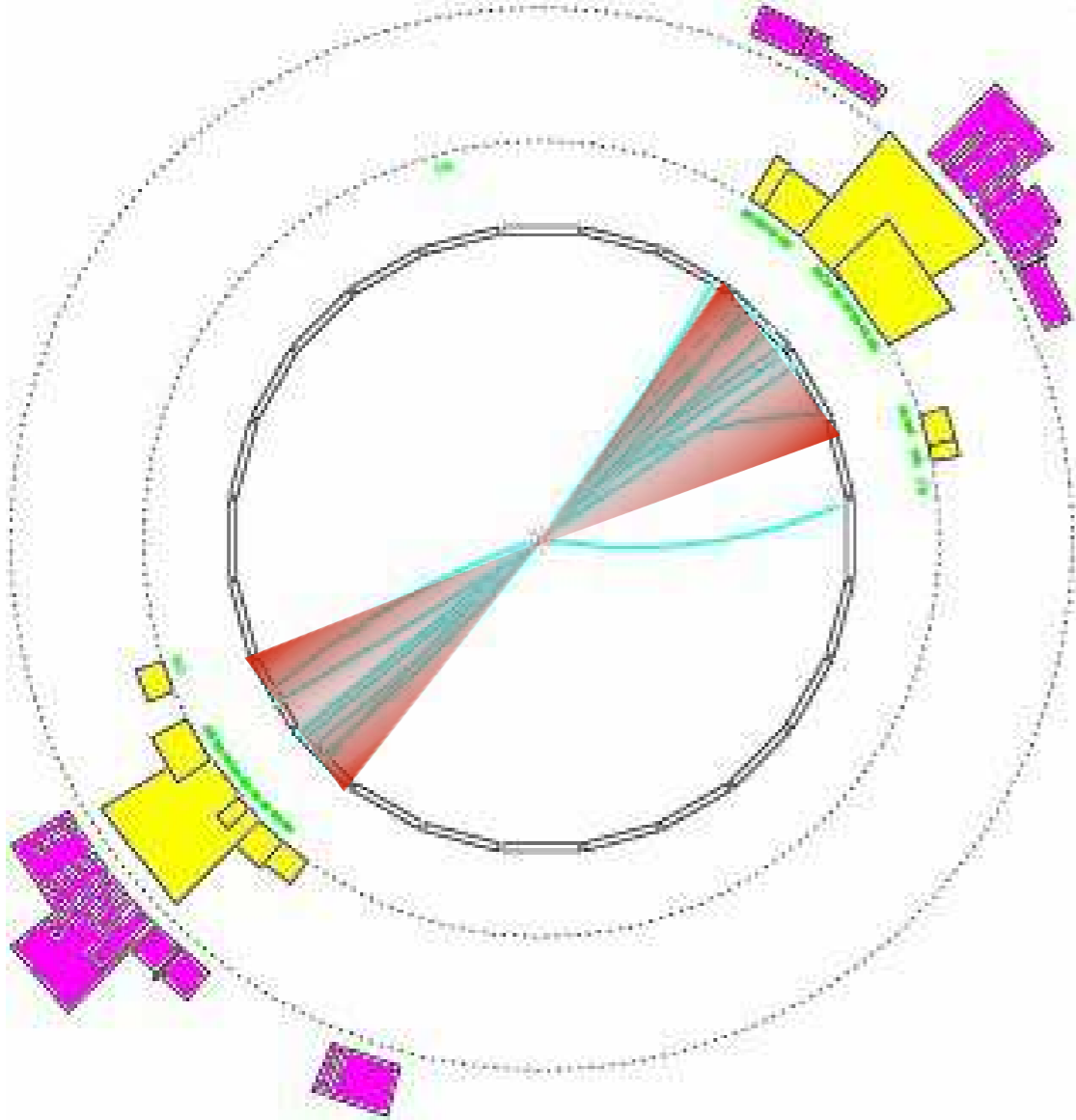


projection to jets should be resilient to QCD effects

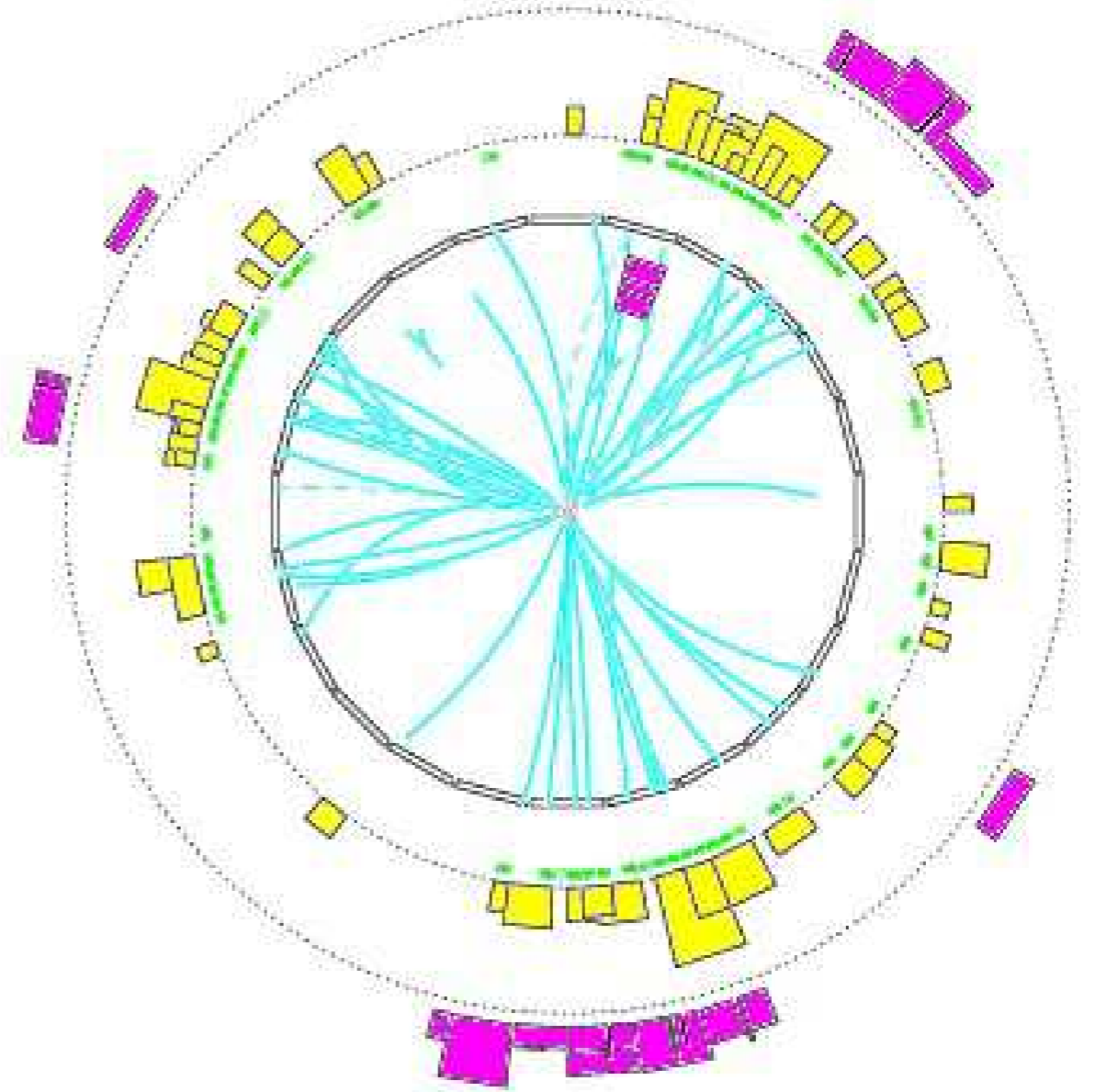
Reconstructing jets is an ambiguous task



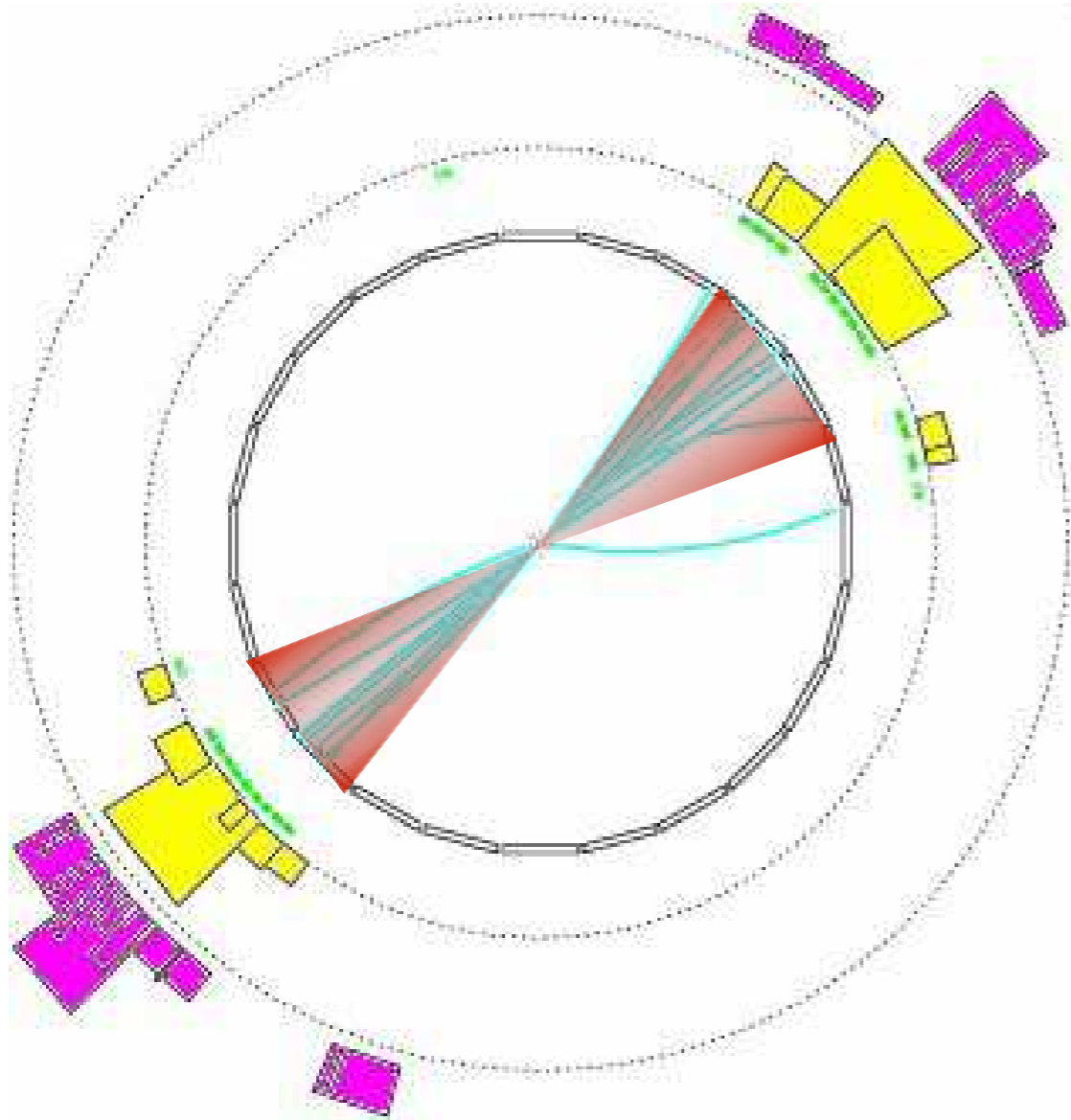
Reconstructing jets is an ambiguous task



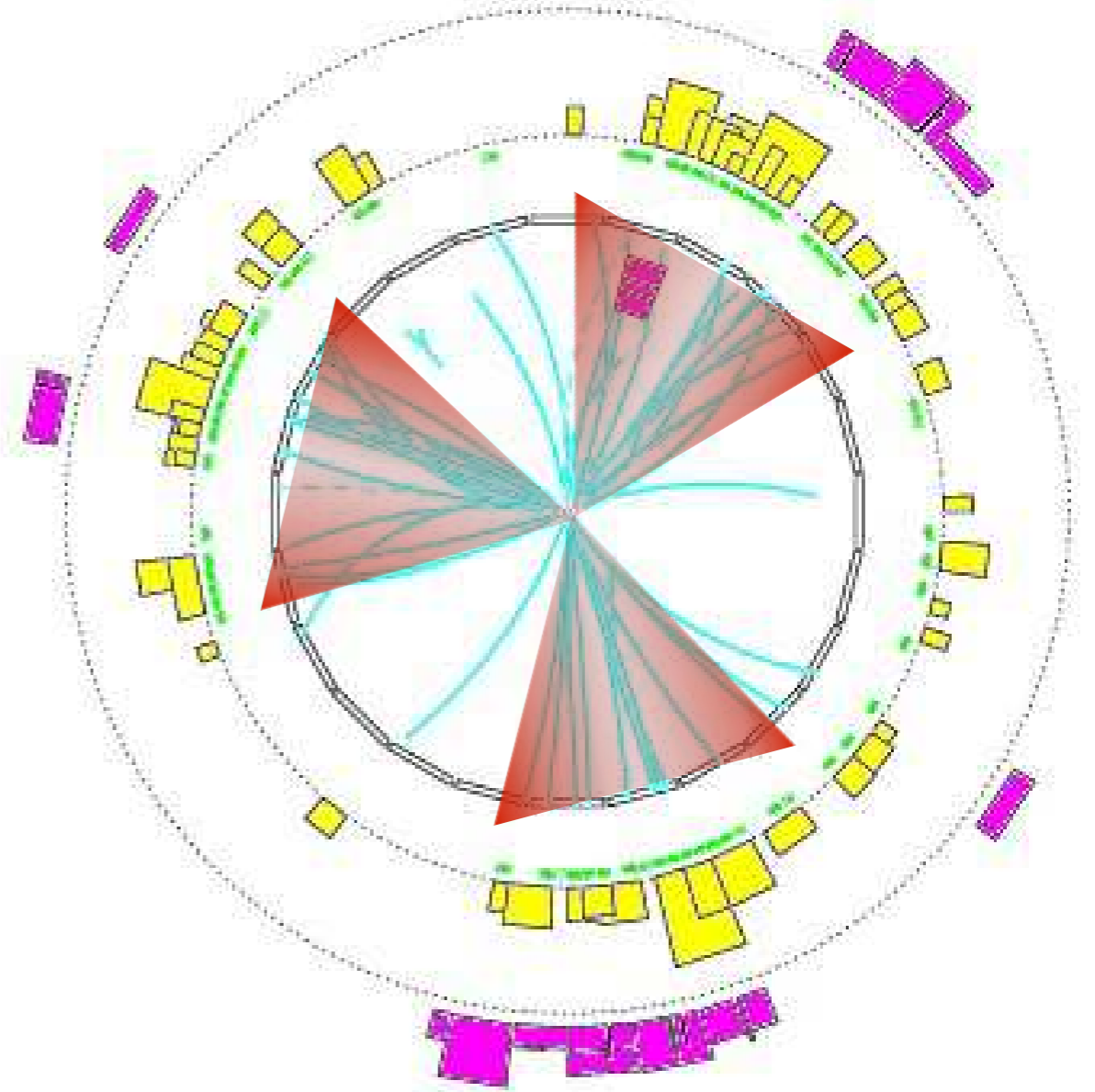
2 clear jets



Reconstructing jets is an ambiguous task

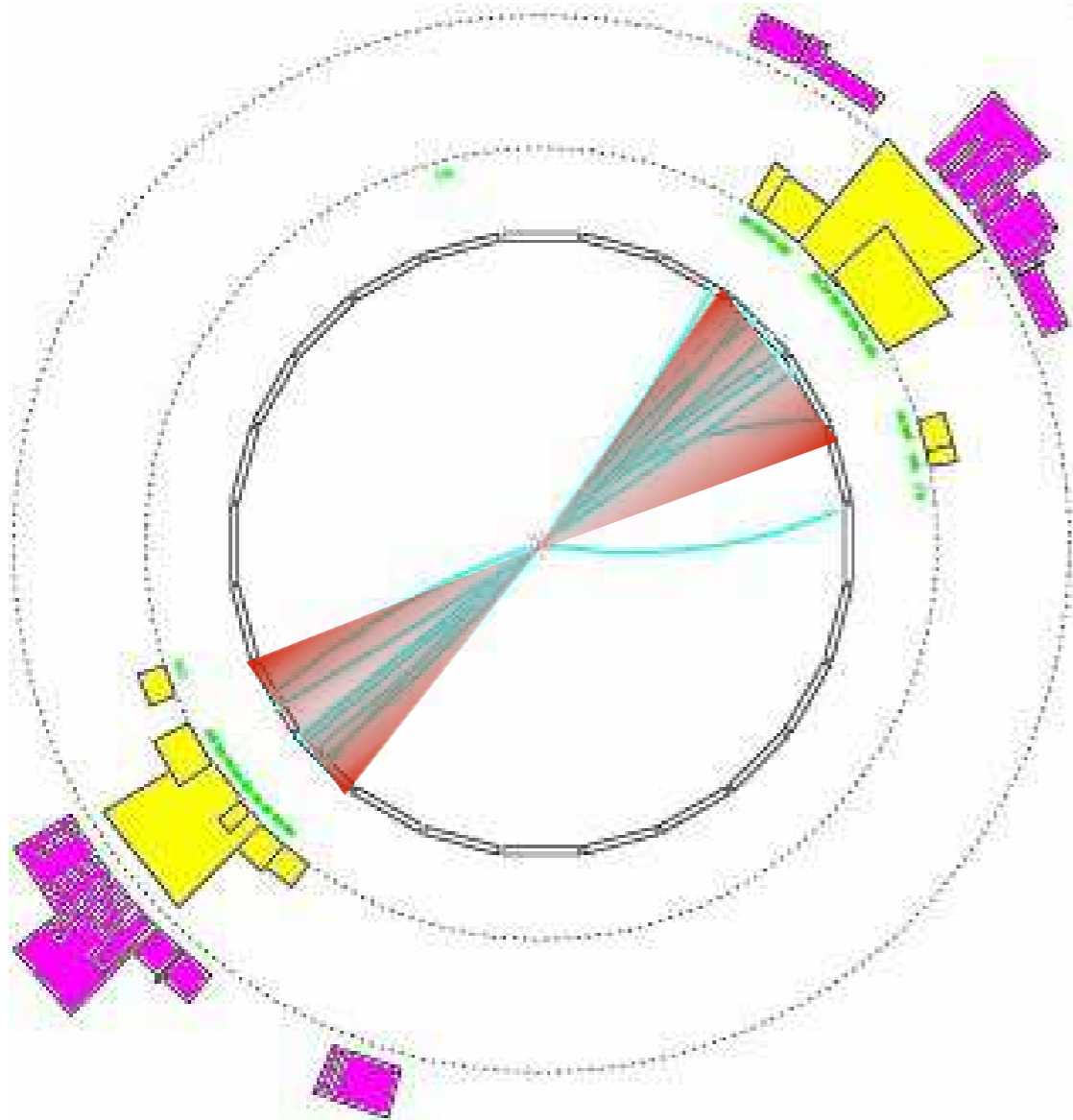


2 clear jets

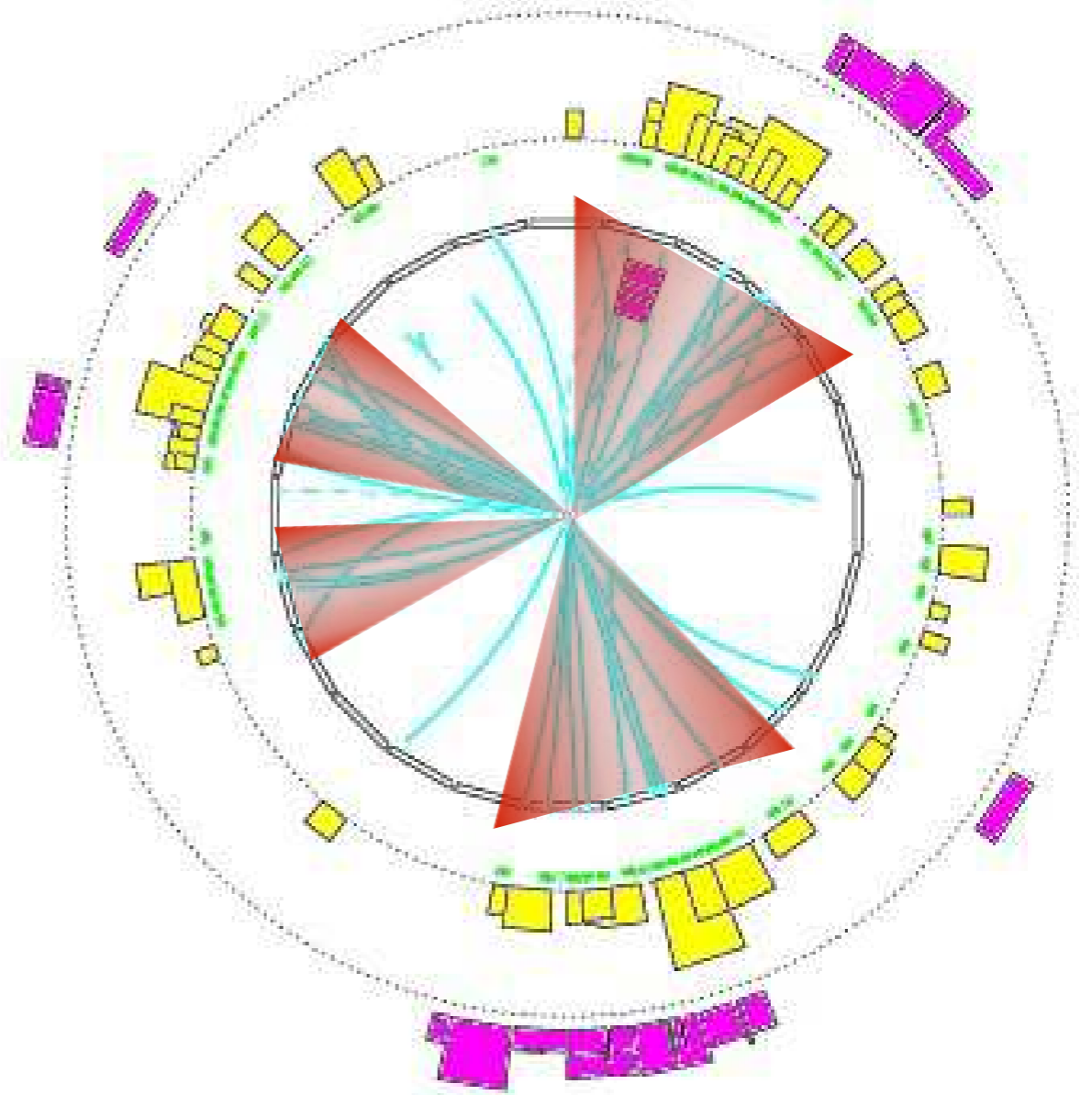


3 jets?

Reconstructing jets is an ambiguous task



2 clear jets



3 jets?
or 4 jets?

Jet definition ingredients

Jet algorithm

A set of rules that you apply to combine particles into jets

Jet algorithm parameters

Thresholds that help specify when two particles belong to the same jet or not.

Most hadron collider jet algorithms have two threshold parameters:

- **Jet angular radius parameter R :**

particles closer in angle than R get recombined

(NB: usually implemented as a condition on the distance parameter on the standard hadron collider rapidity-azimuth $[y, \varphi]$ cylinder)

- **Transverse momentum threshold:**

jets should have $p_T > p_{T,\min}$

the main jet algorithm at the LHC

$$\Delta R_{ij}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$$

$$y = \frac{1}{2} \ln \frac{E + p_z}{E - p_z}$$

A Sequential recombination algorithm

Involves calculating “clustering distance” between pairs of particles

$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = \frac{1}{p_{ti}^2}$$

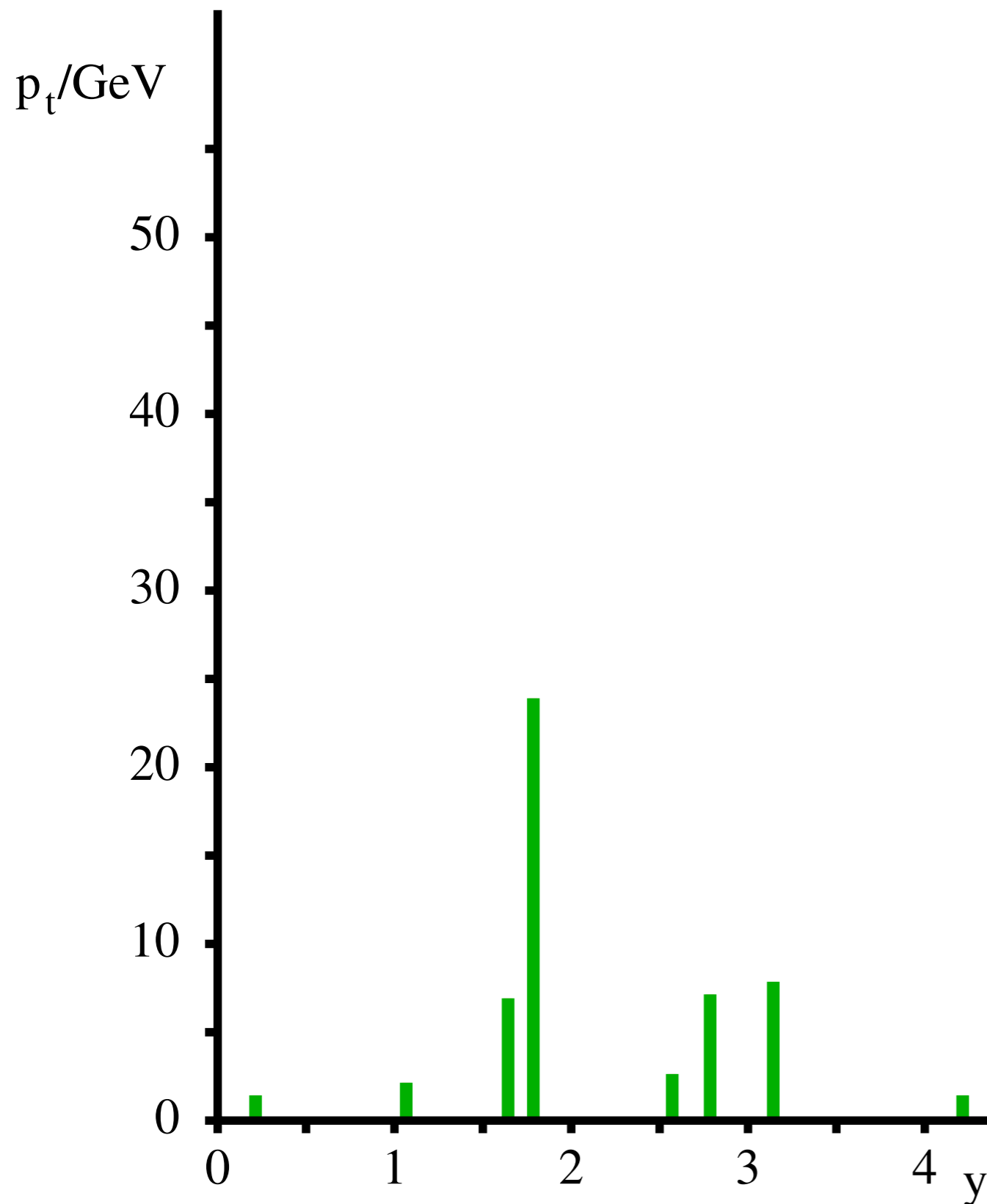
1. Find smallest of d_{ij} , d_{iB}
2. If ij , recombine them
3. If iB , call i a jet and remove from list of particles
4. repeat from step 1 until no particles left

Only use jets with $p_t > p_{t,min}$

anti- k_t algorithm

Cacciari, GPS & Soyez, 0802.1189

Anti- k_t jet clustering example

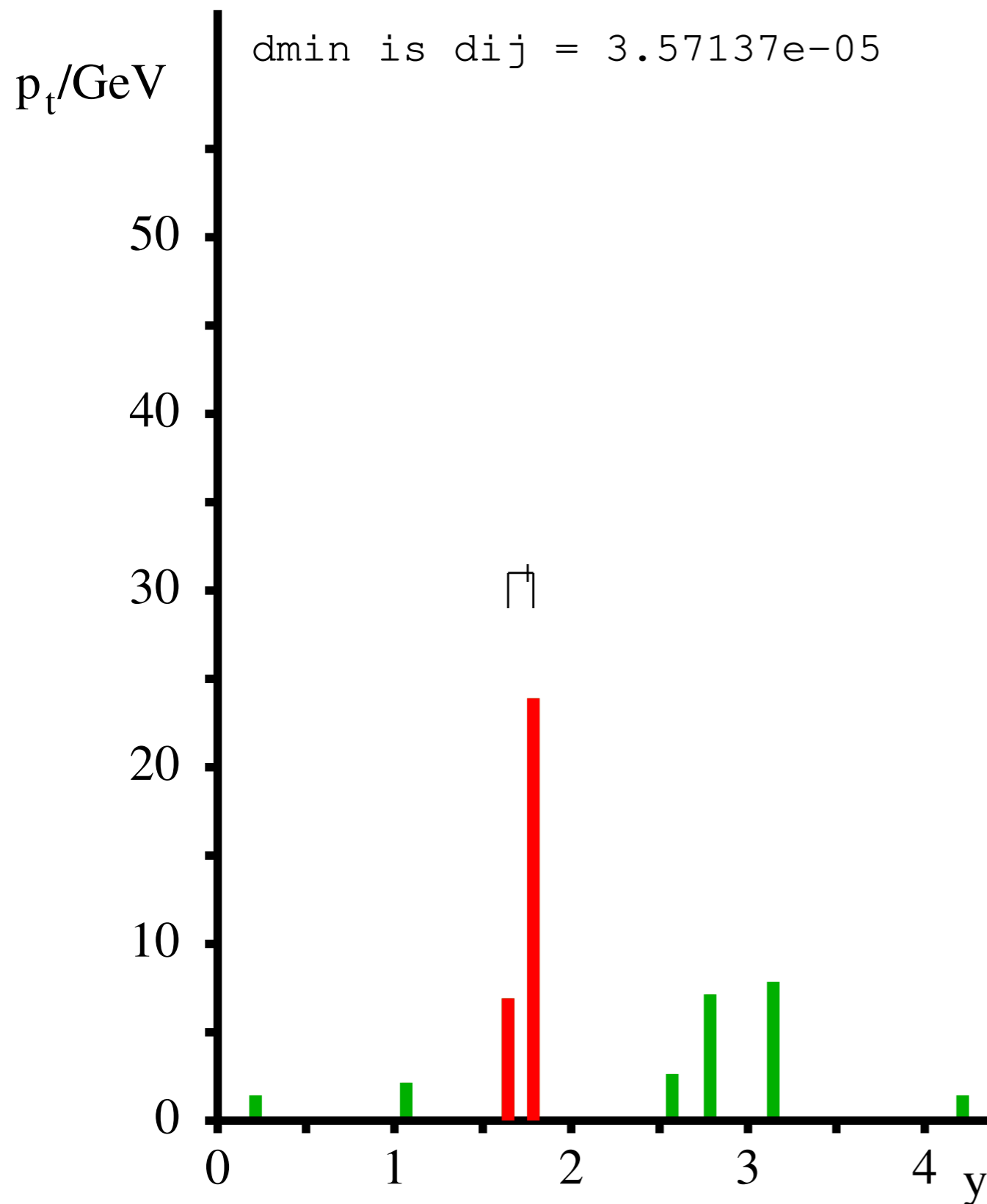


$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}$$

$$d_{iB} = \frac{1}{p_{ti}^2} \quad \begin{array}{l} \text{[here } R=2.0 \\ p_{T,\min}=20 \text{ GeV} \\ \text{at LHC: } R=0.4 - 1.0 \end{array}$$

$$\Delta R_{ij}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2 \quad y = \frac{1}{2} \ln \frac{E + p_z}{E - p_z}$$

Anti- k_t jet clustering example

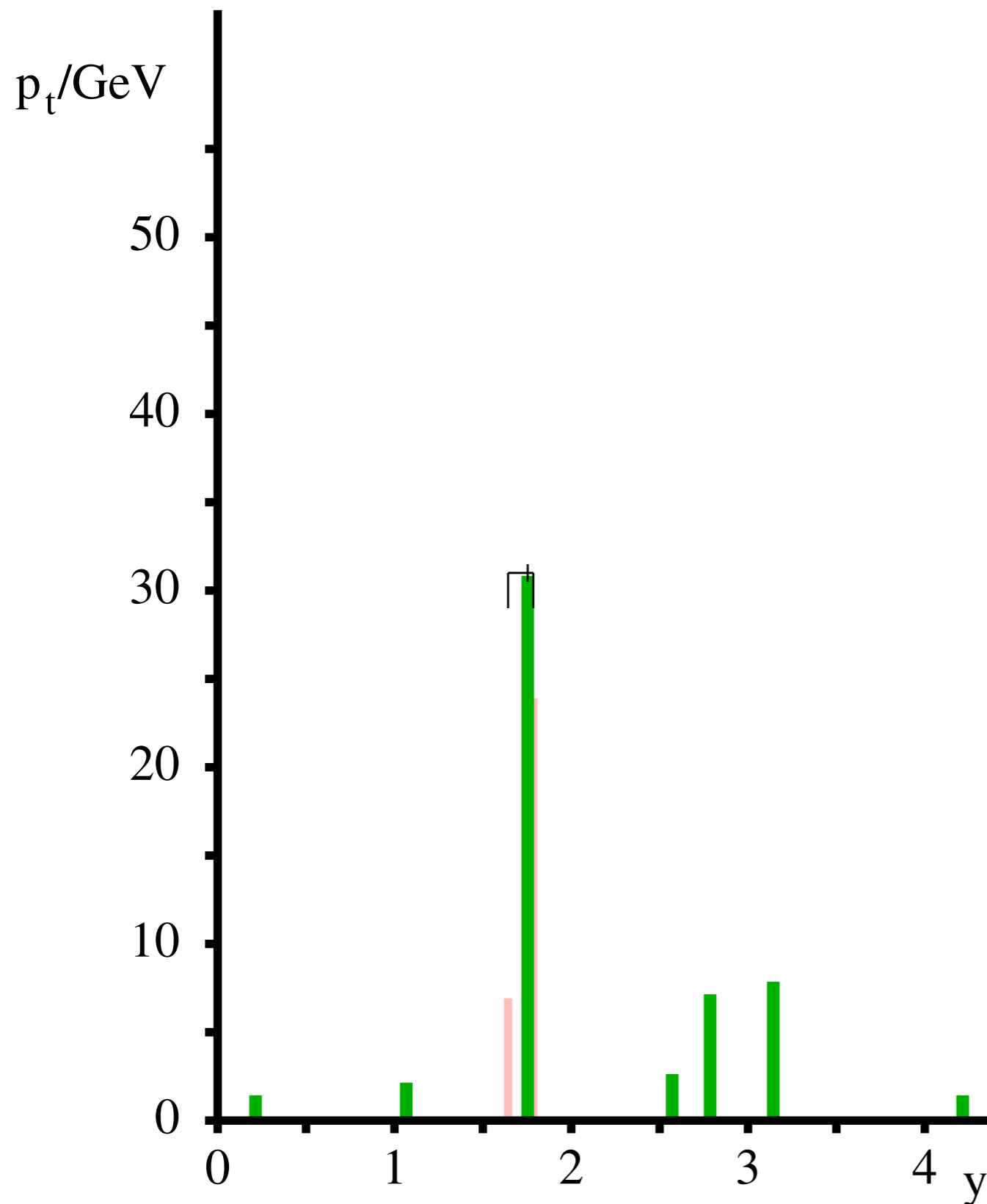


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Anti- k_t jet clustering example

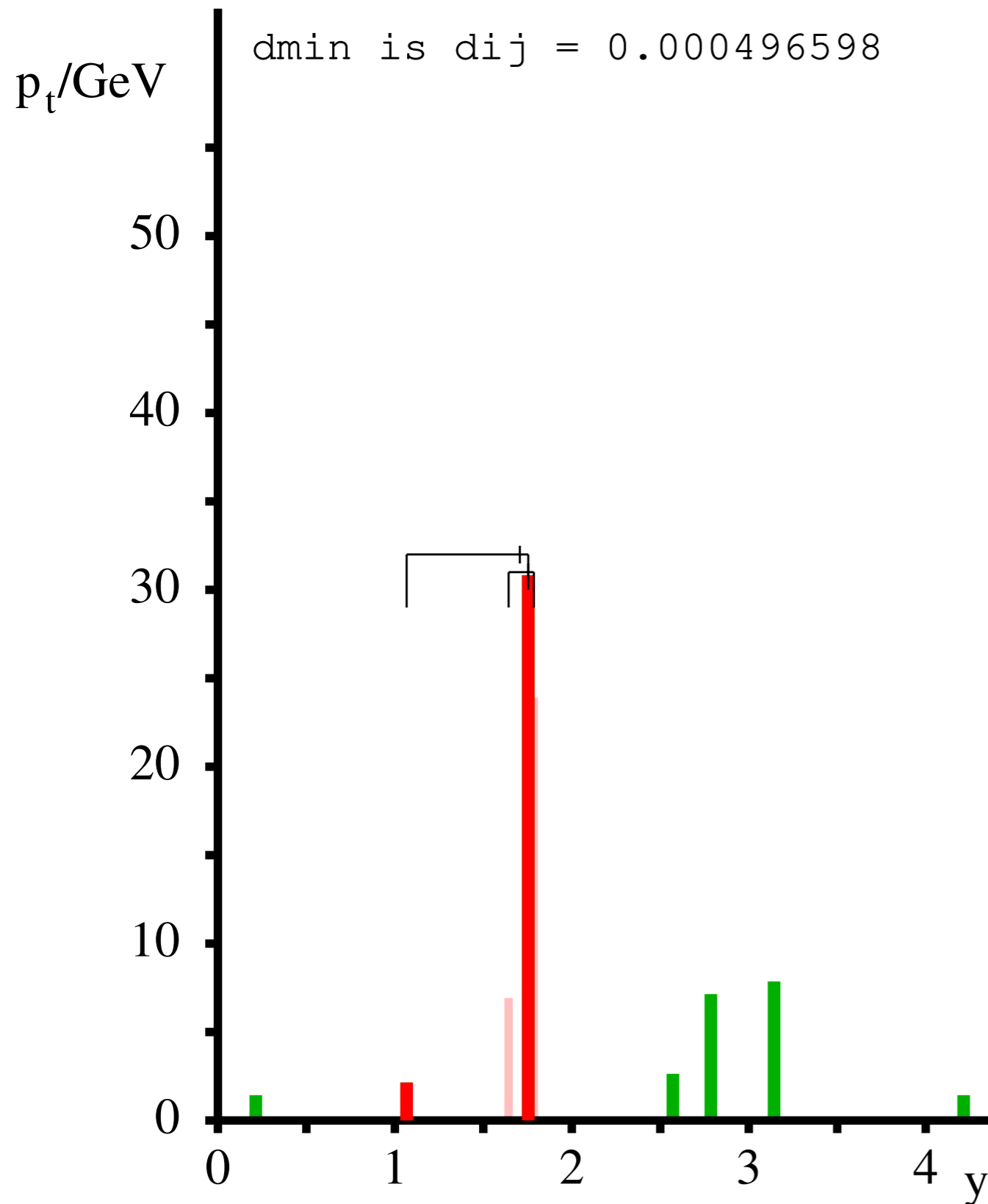


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Anti- k_t jet clustering example

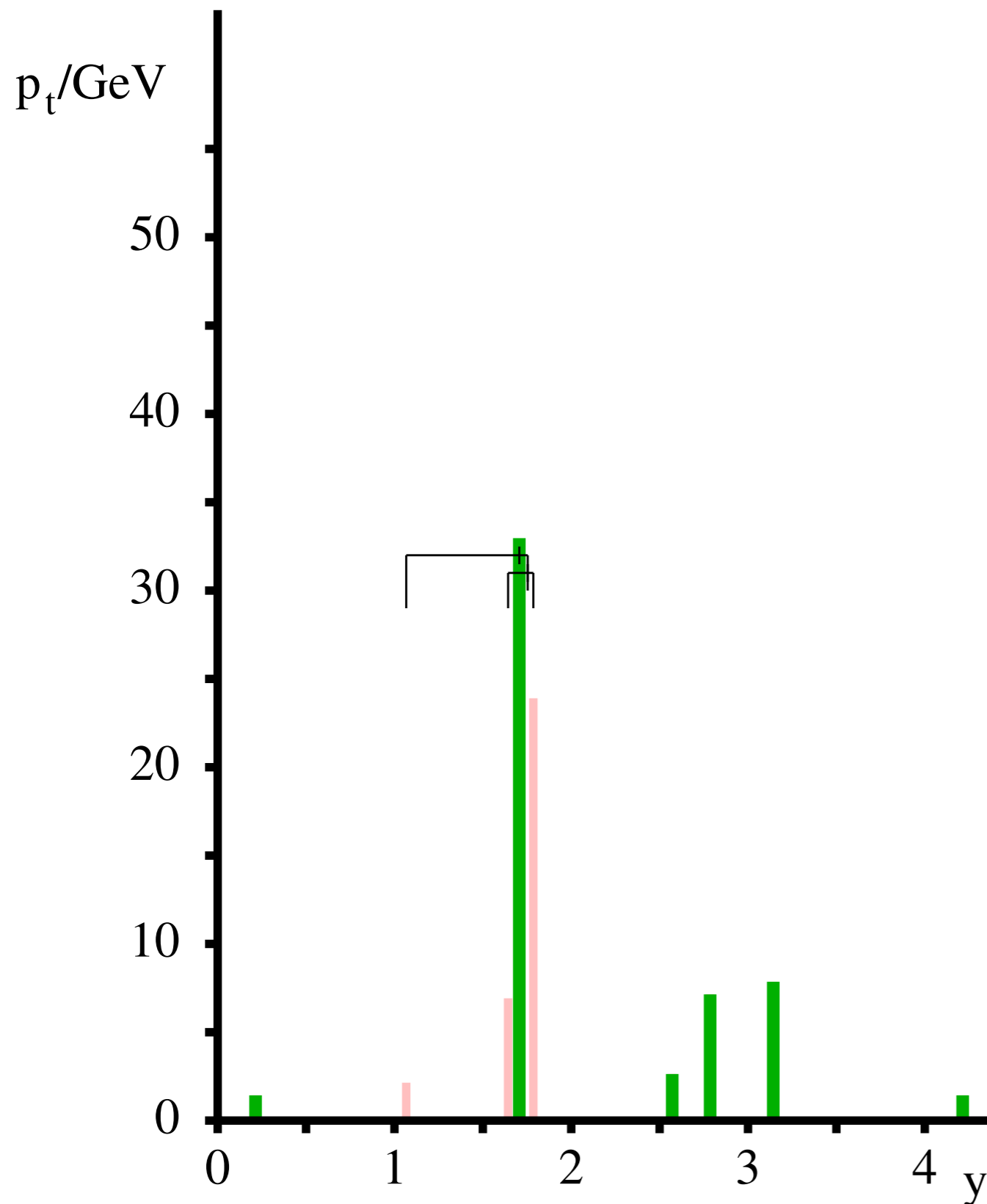


$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}$$

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Anti- k_t jet clustering example

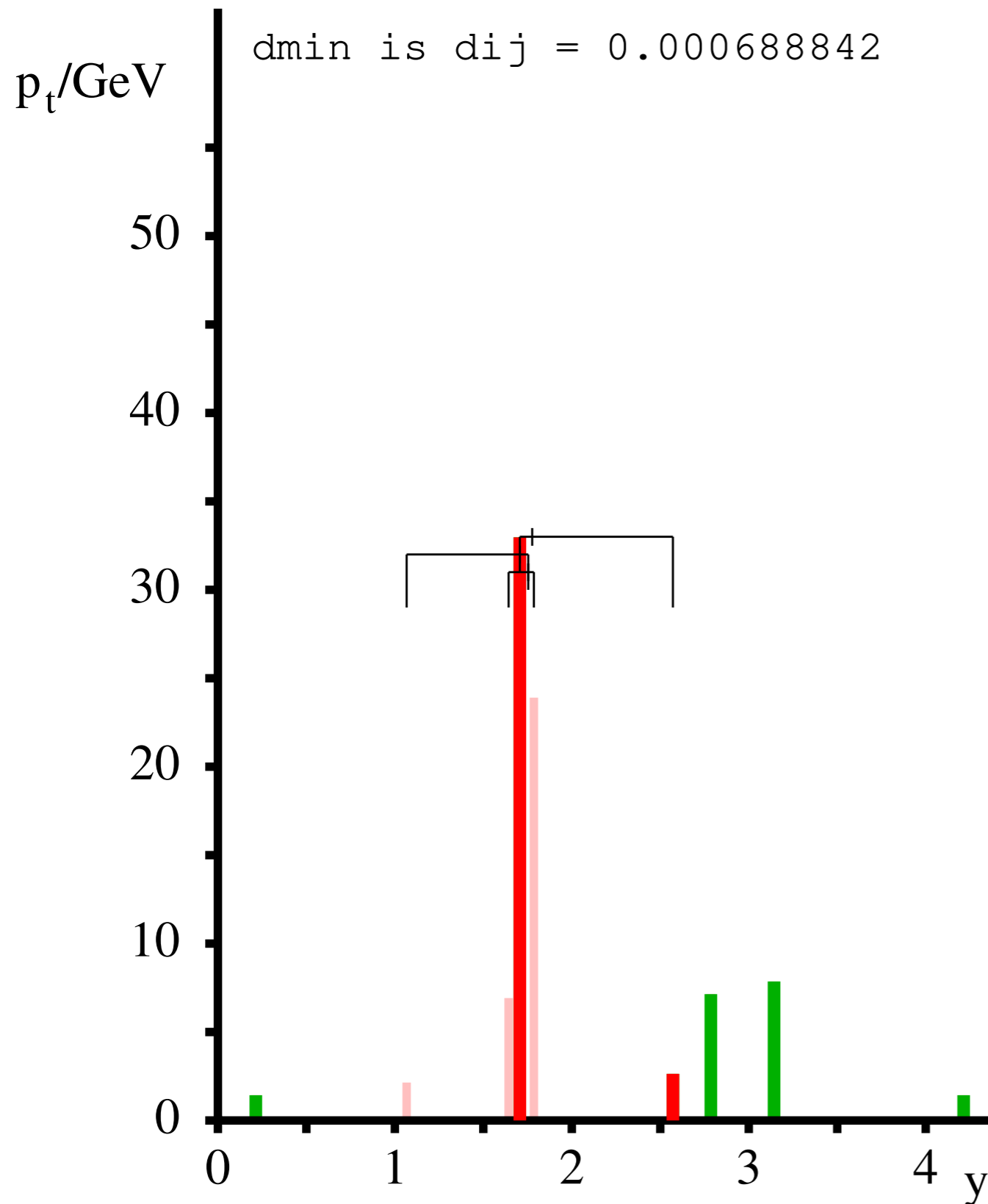


$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}$$

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Anti- k_t jet clustering example

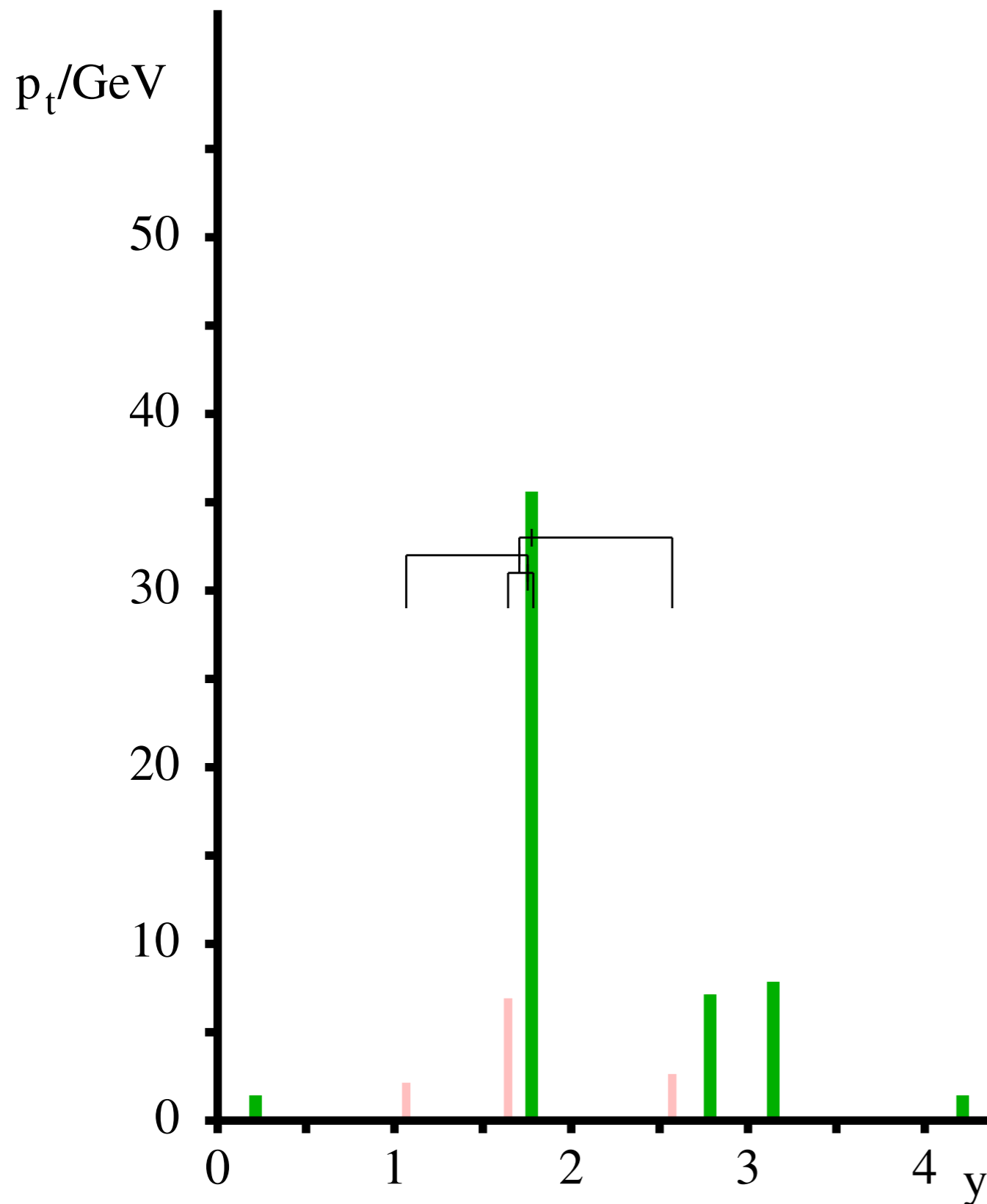


$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}$$

$$d_{iB} = \frac{1}{p_{ti}^2} \quad \begin{array}{l} \text{[here } R=2.0 \\ p_{T,\min}=20 \text{ GeV} \\ \text{at LHC: } R=0.4 - 1.0 \end{array}$$

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Anti- k_t jet clustering example

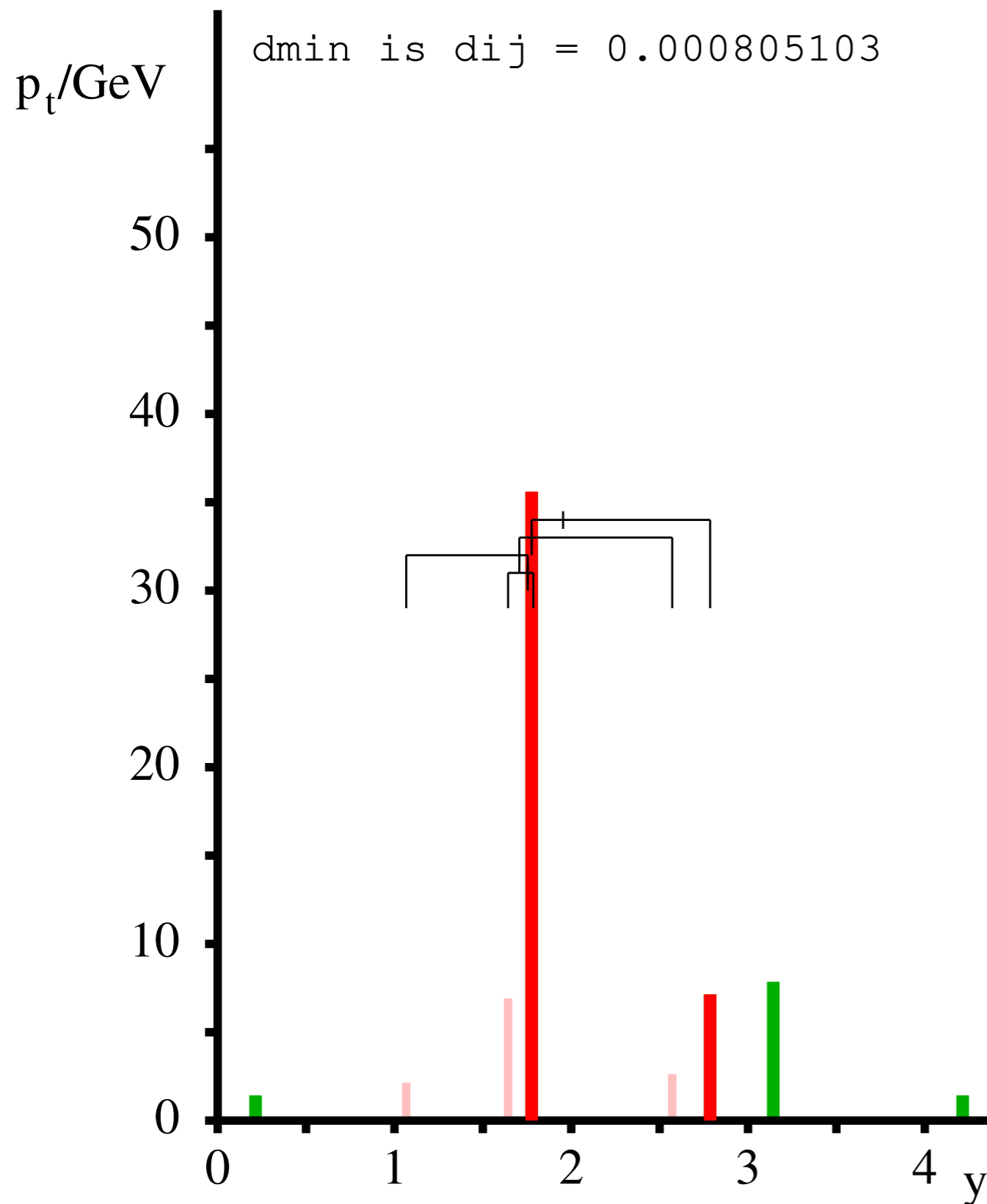


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Anti- k_t jet clustering example

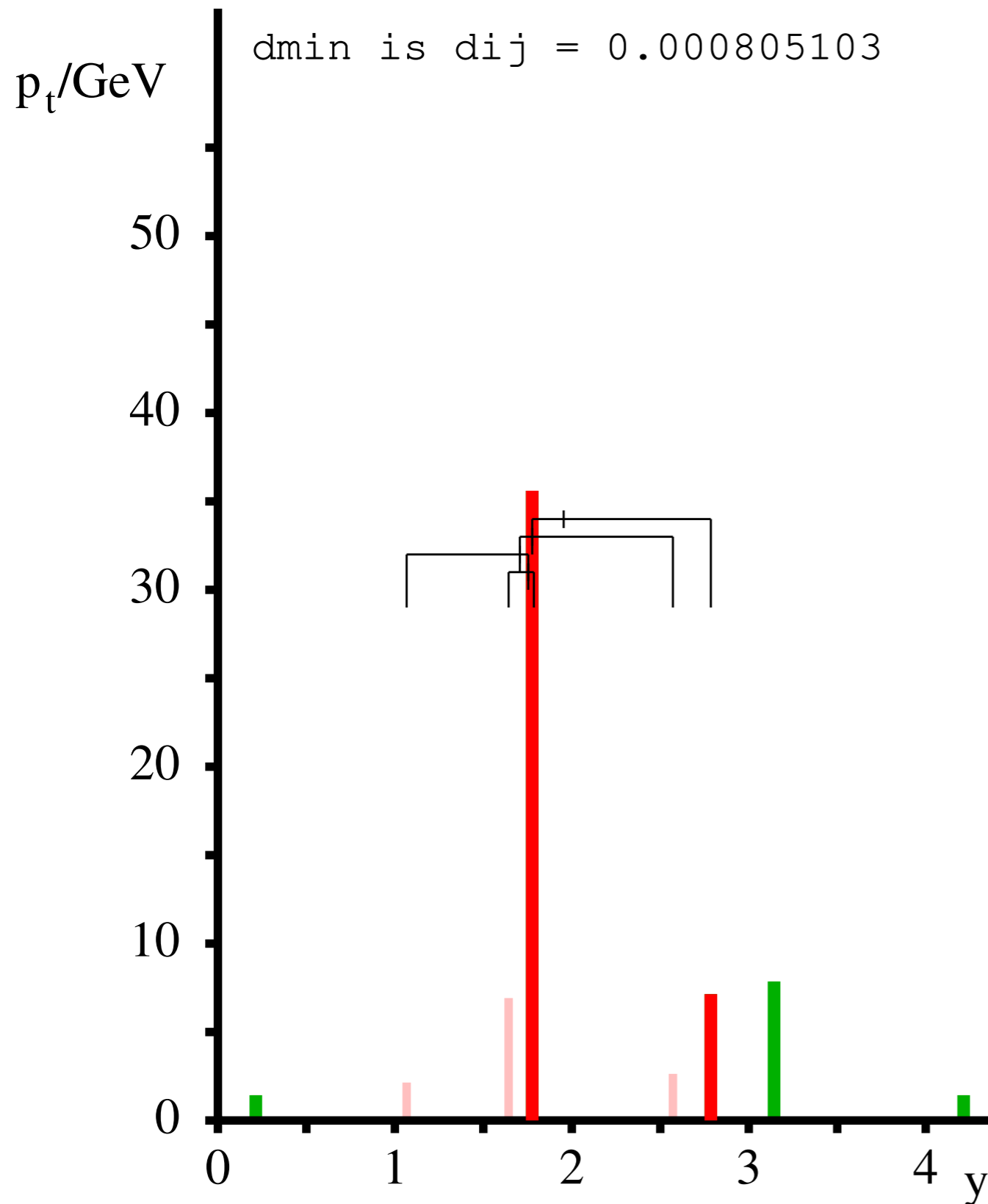


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Anti- k_t jet clustering example



Anti- k_t gradually makes its way through the “blob” at rapidity 2.5–3

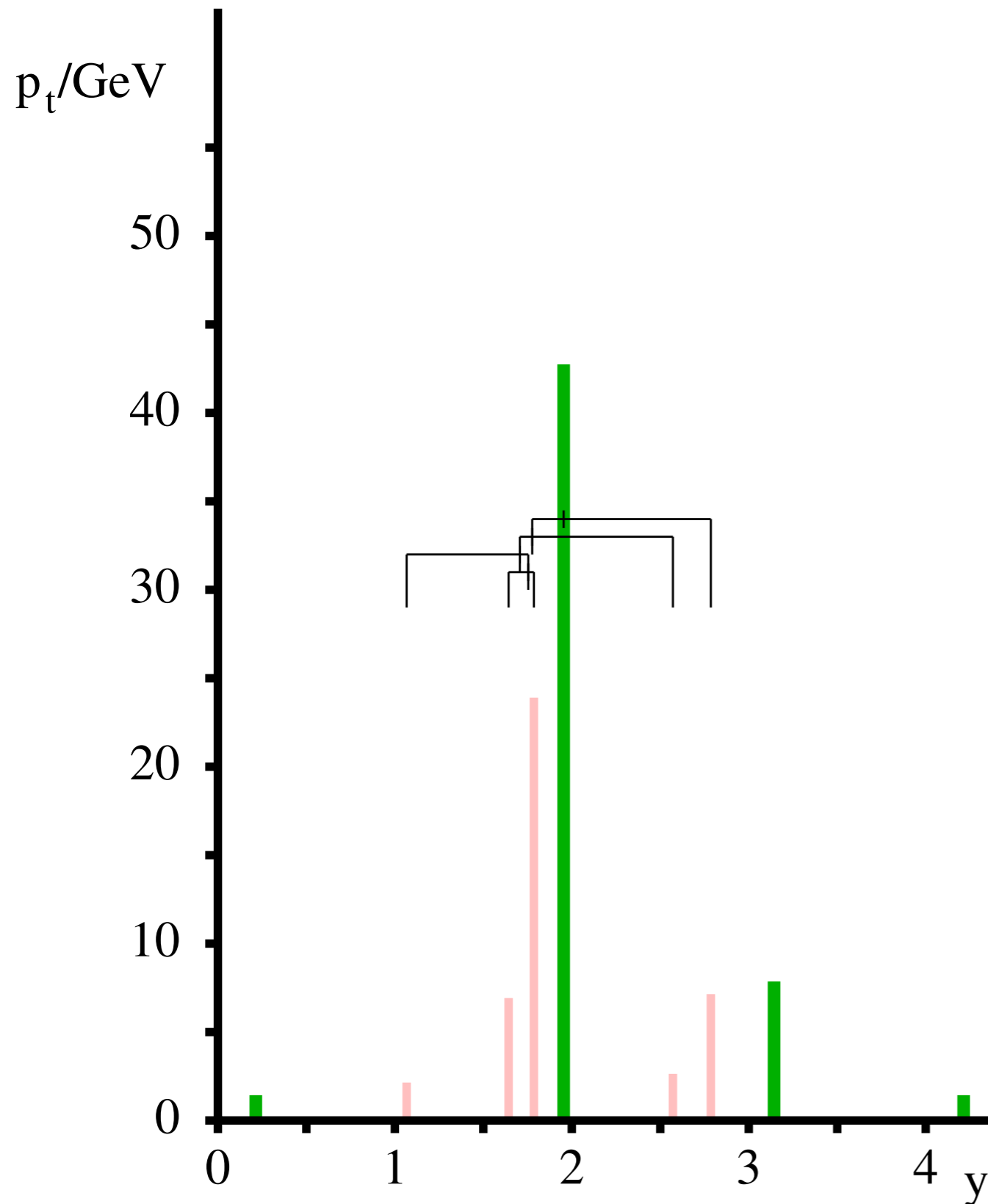
Dominant hierarchy in clustering is distance from the jet core

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Anti- k_t jet clustering example



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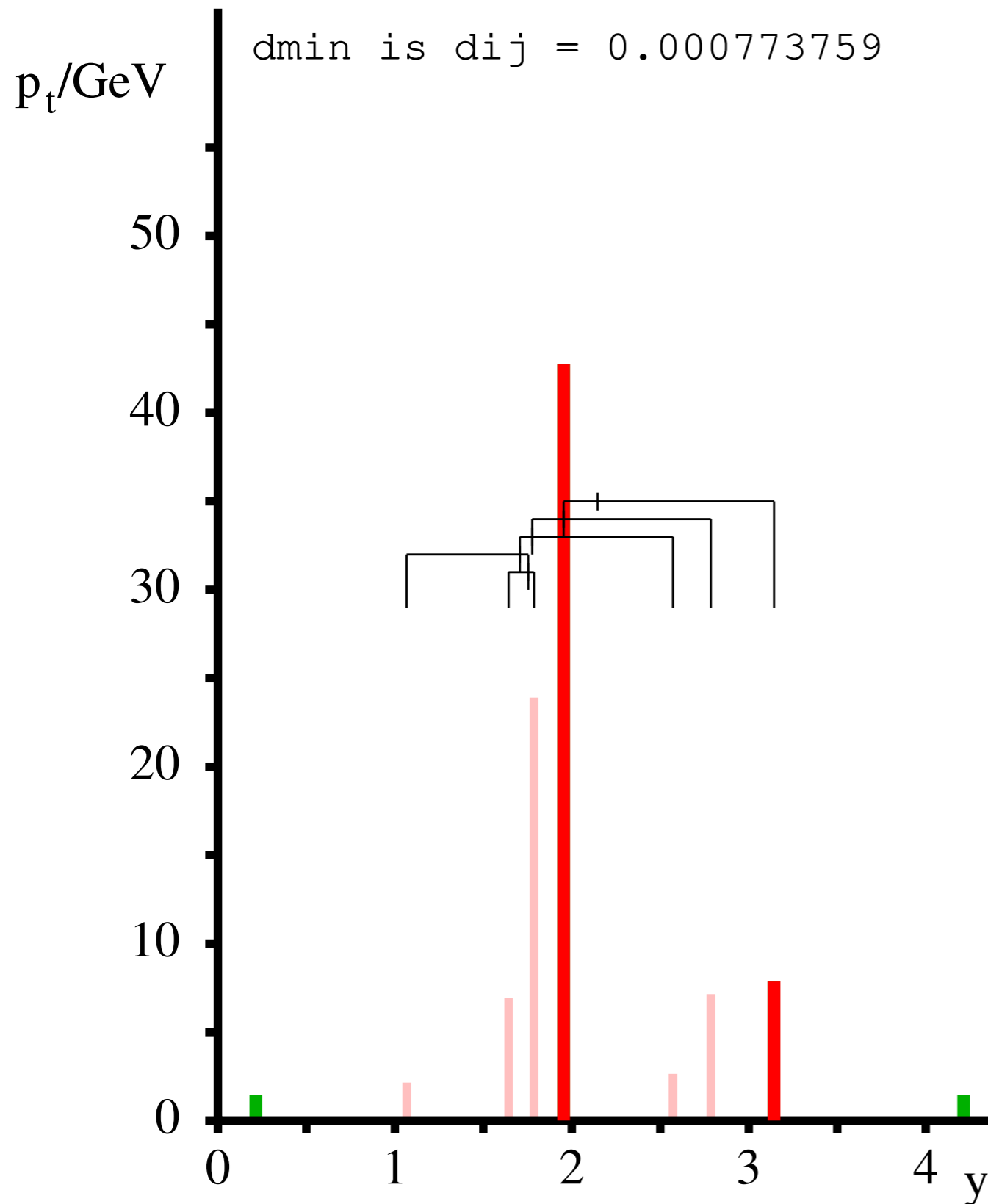
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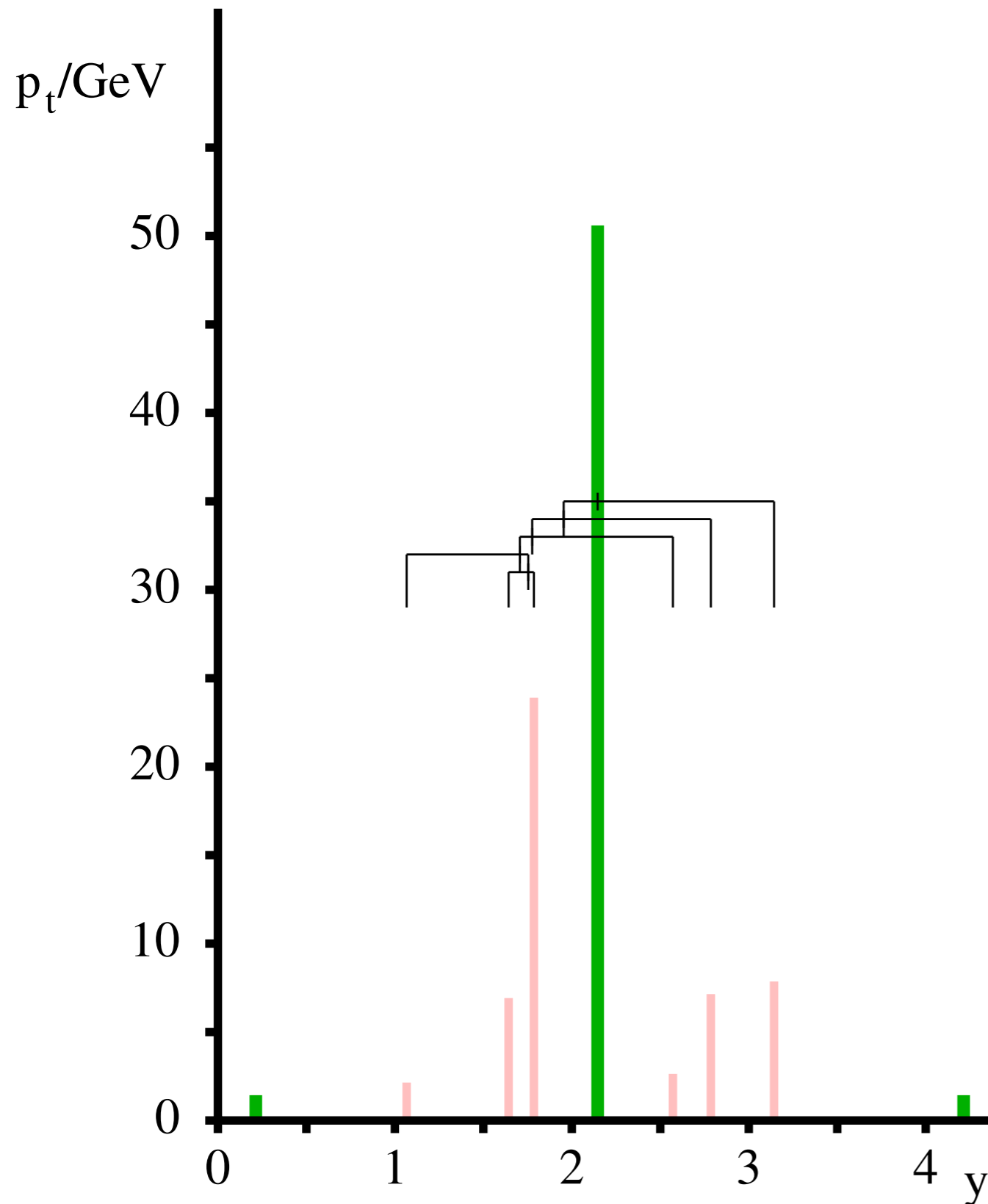
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Anti- k_t jet clustering example



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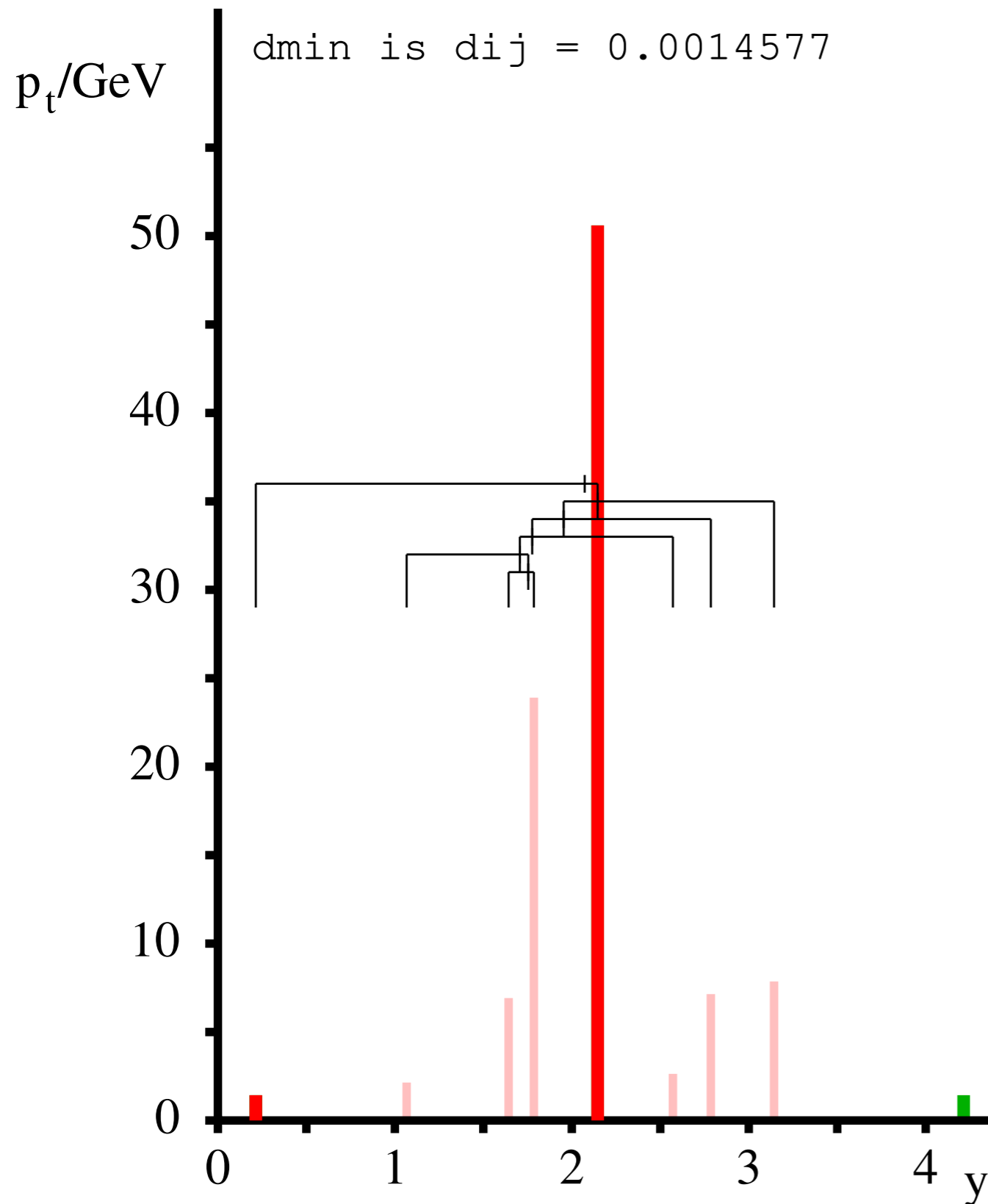
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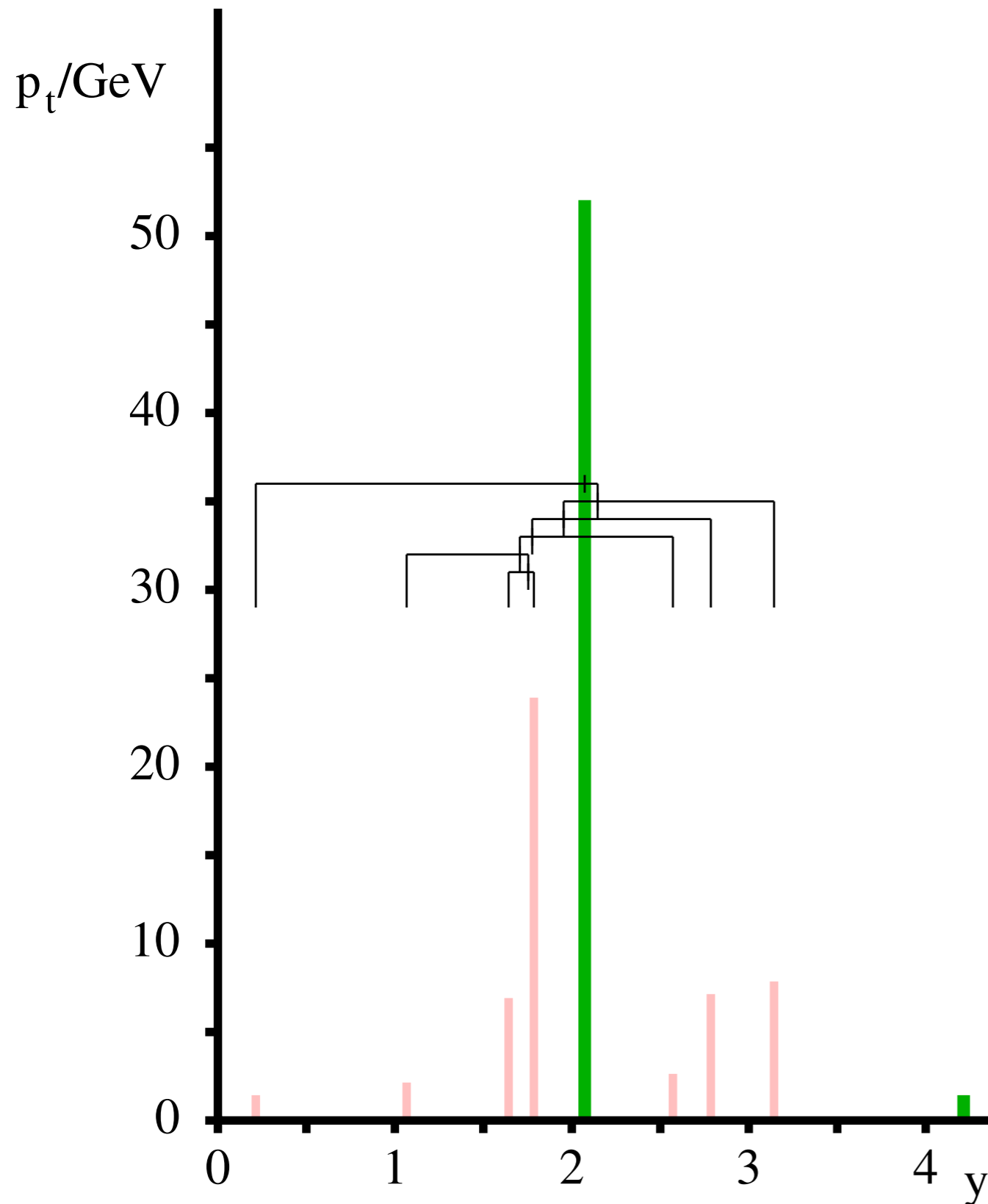
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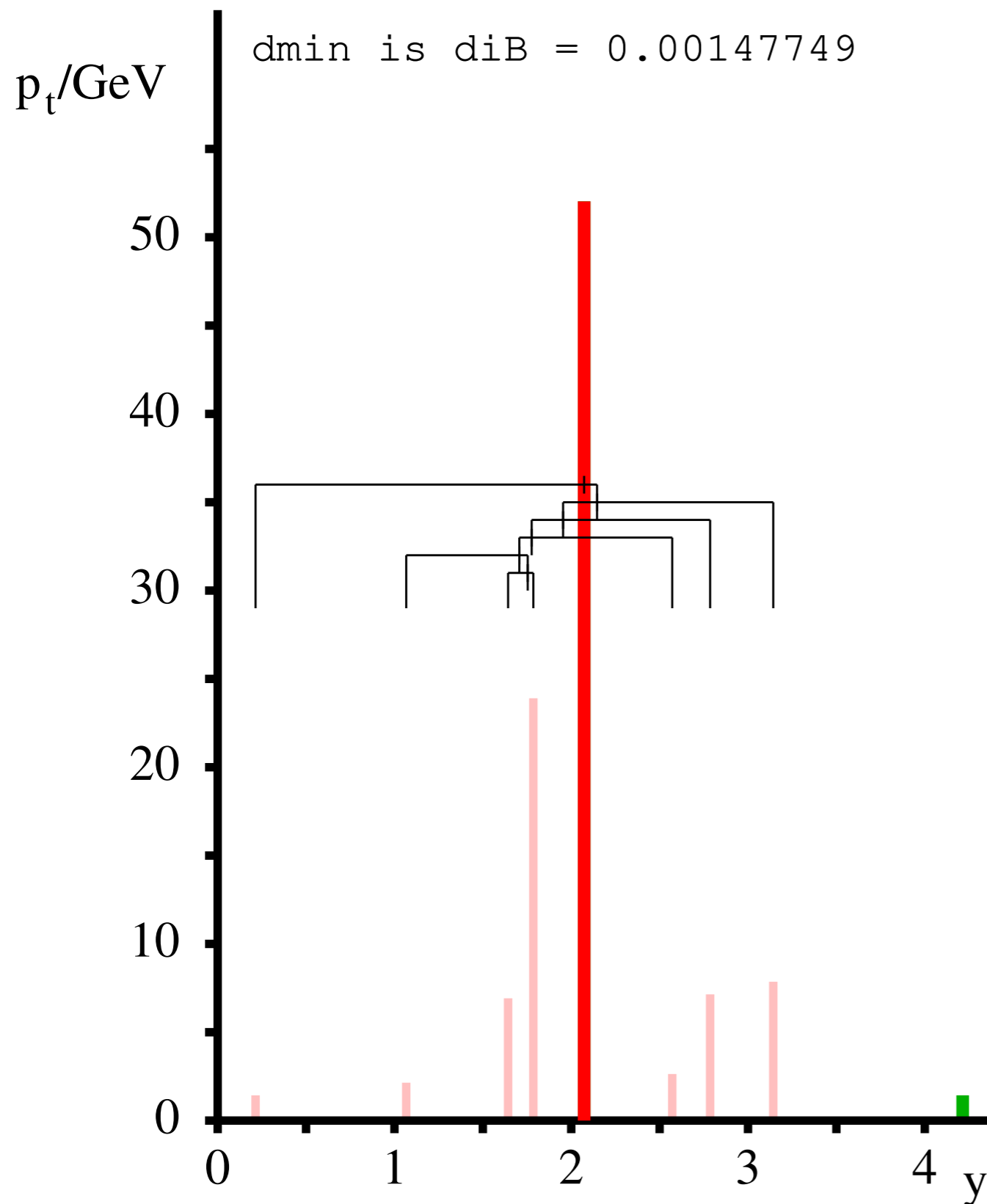
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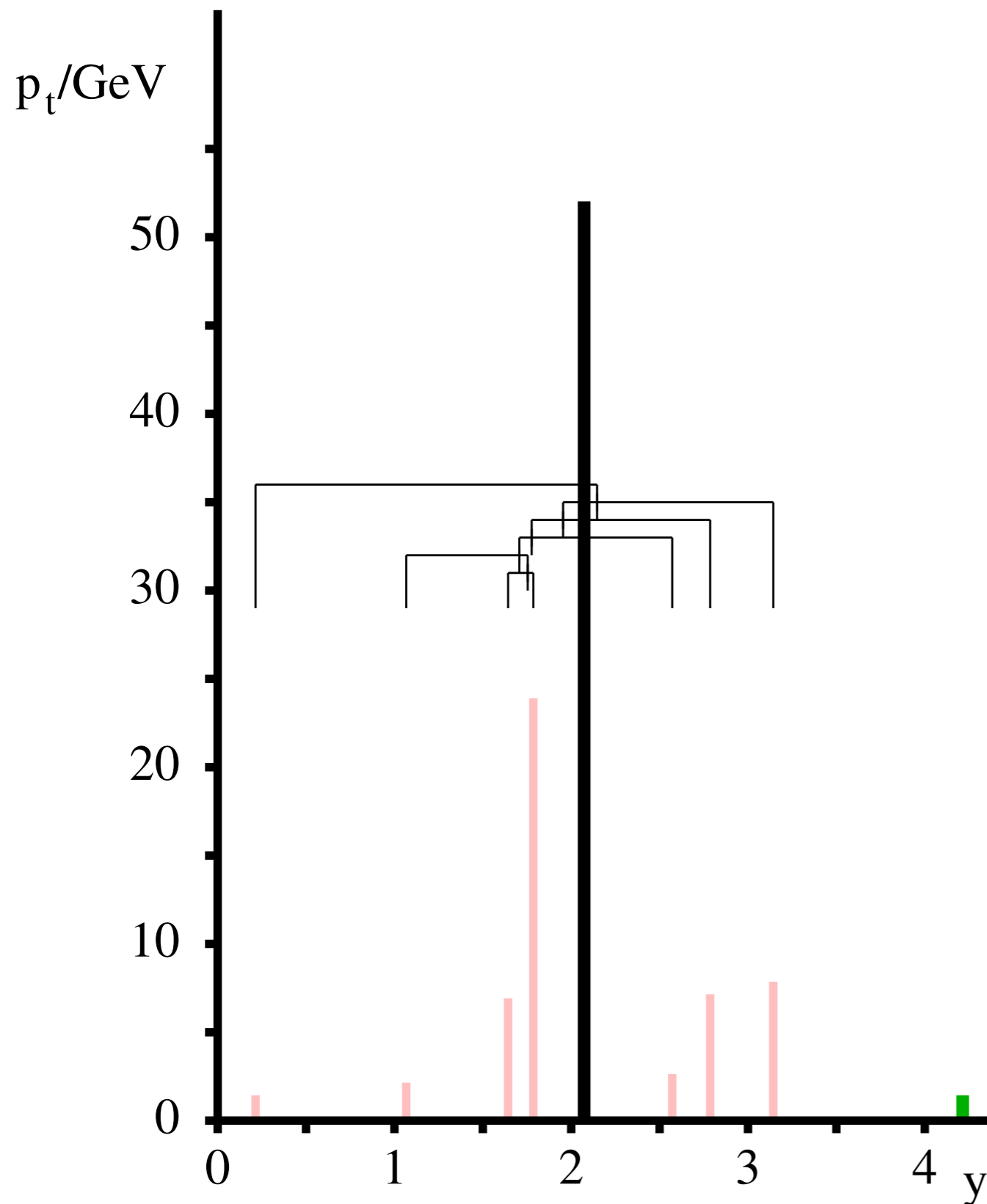
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Anti- k_t jet clustering example



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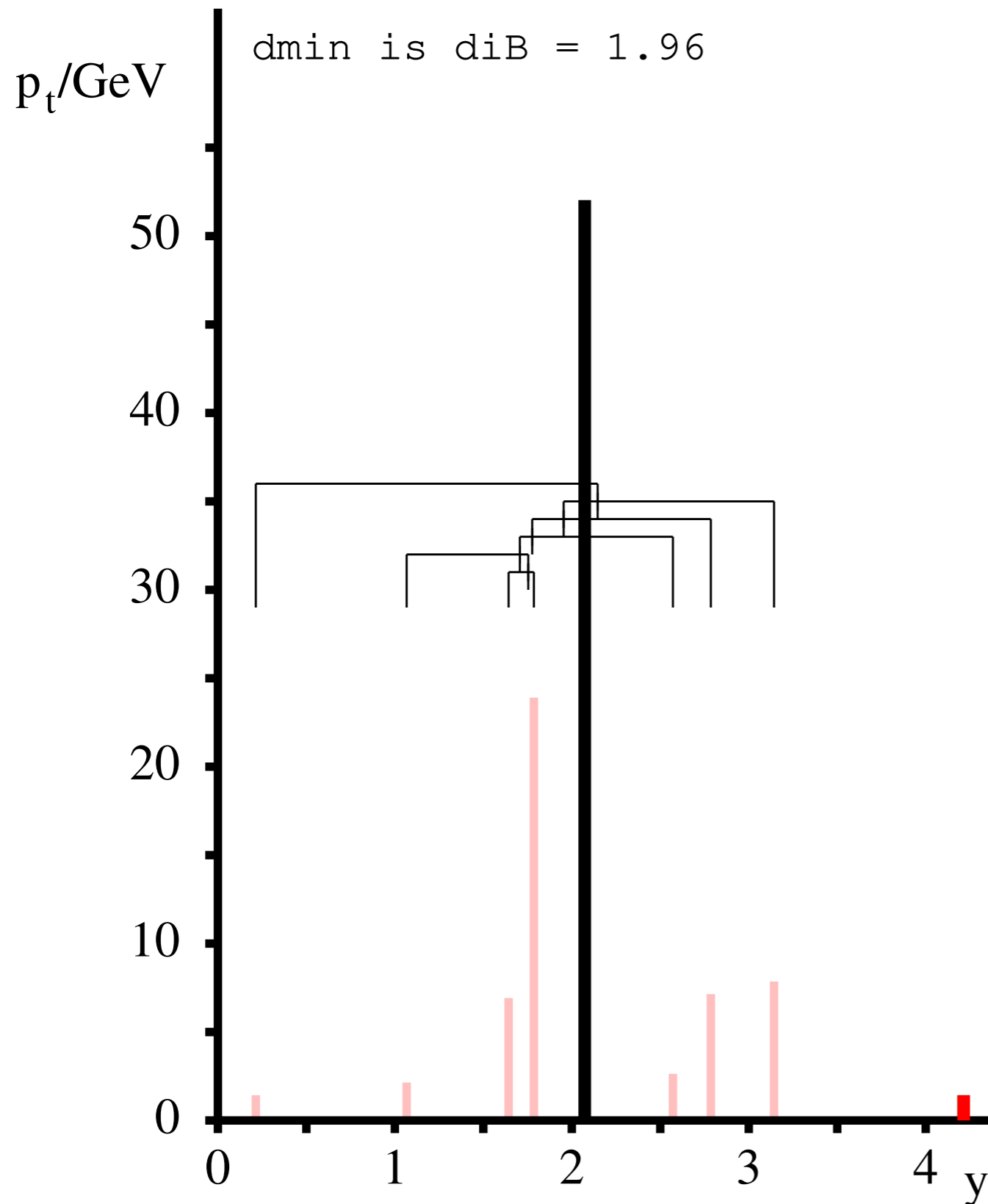
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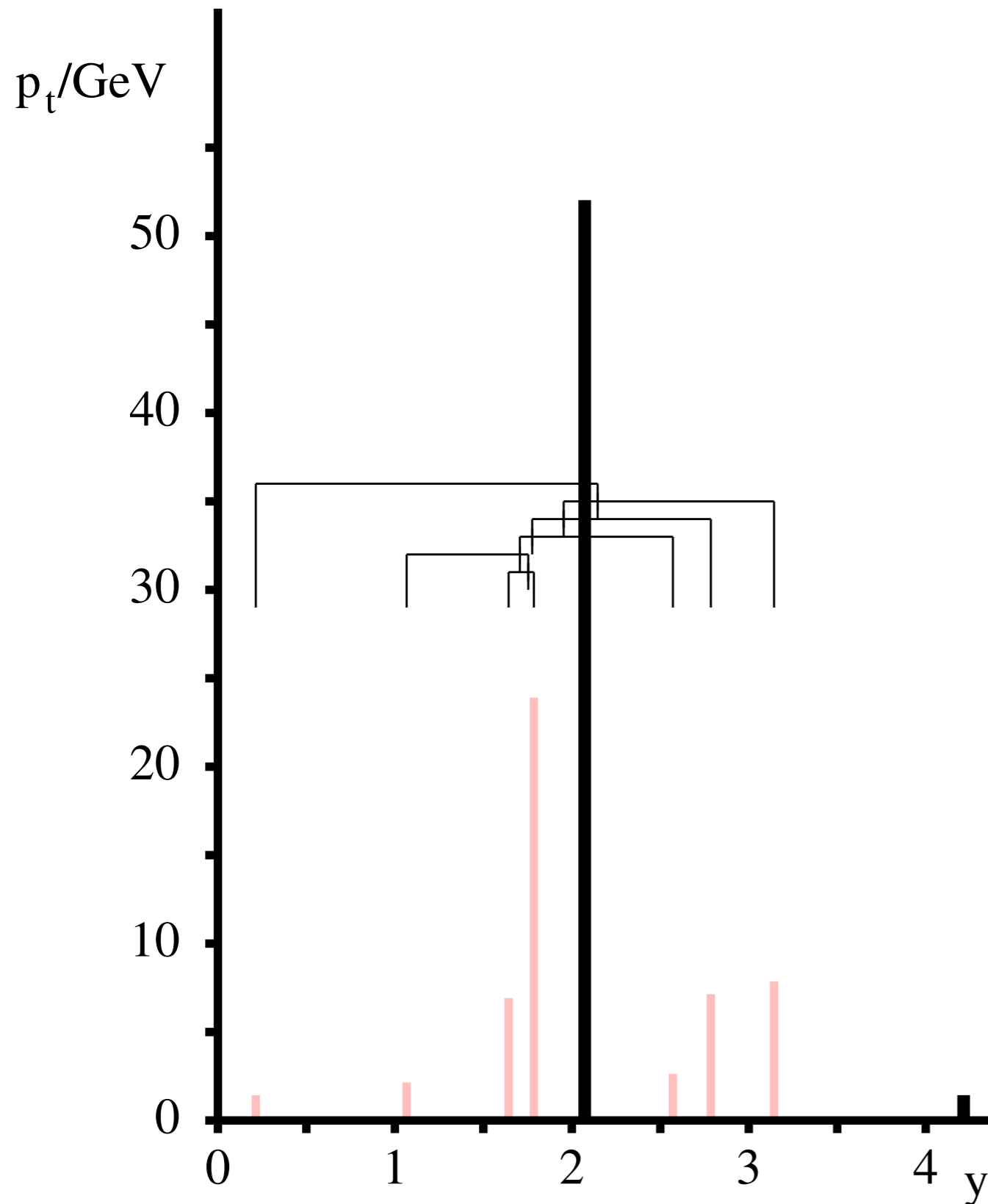
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Anti- k_t jet clustering example



Anti- k_t gradually makes its way through the “blob” at rapidity 2.5–3

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anti- k_t in action [full simulated event]

Clustering grows
around hard cores

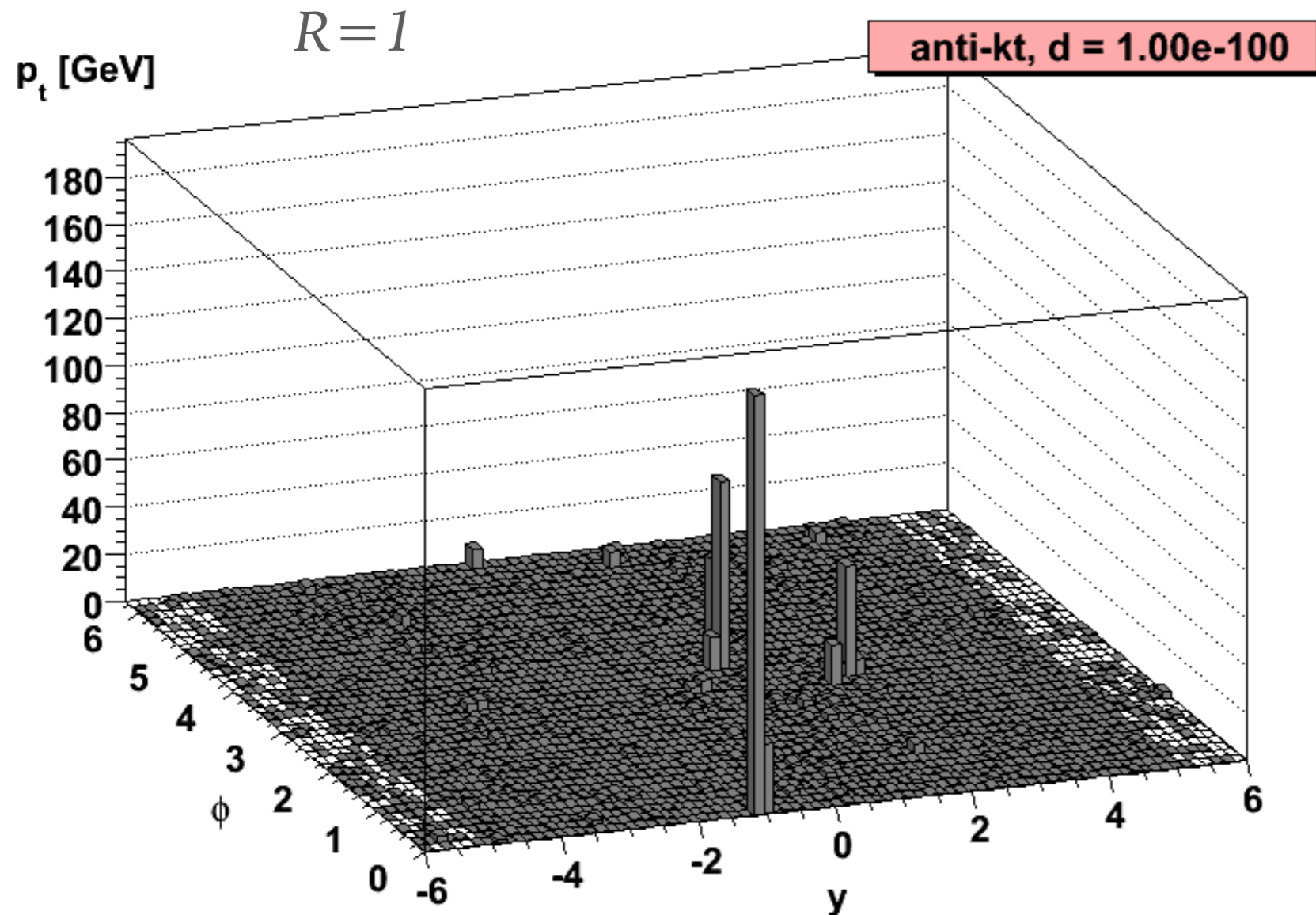
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$$R=1$$

anti- k_t in action [full simulated event]

Clustering grows around hard cores

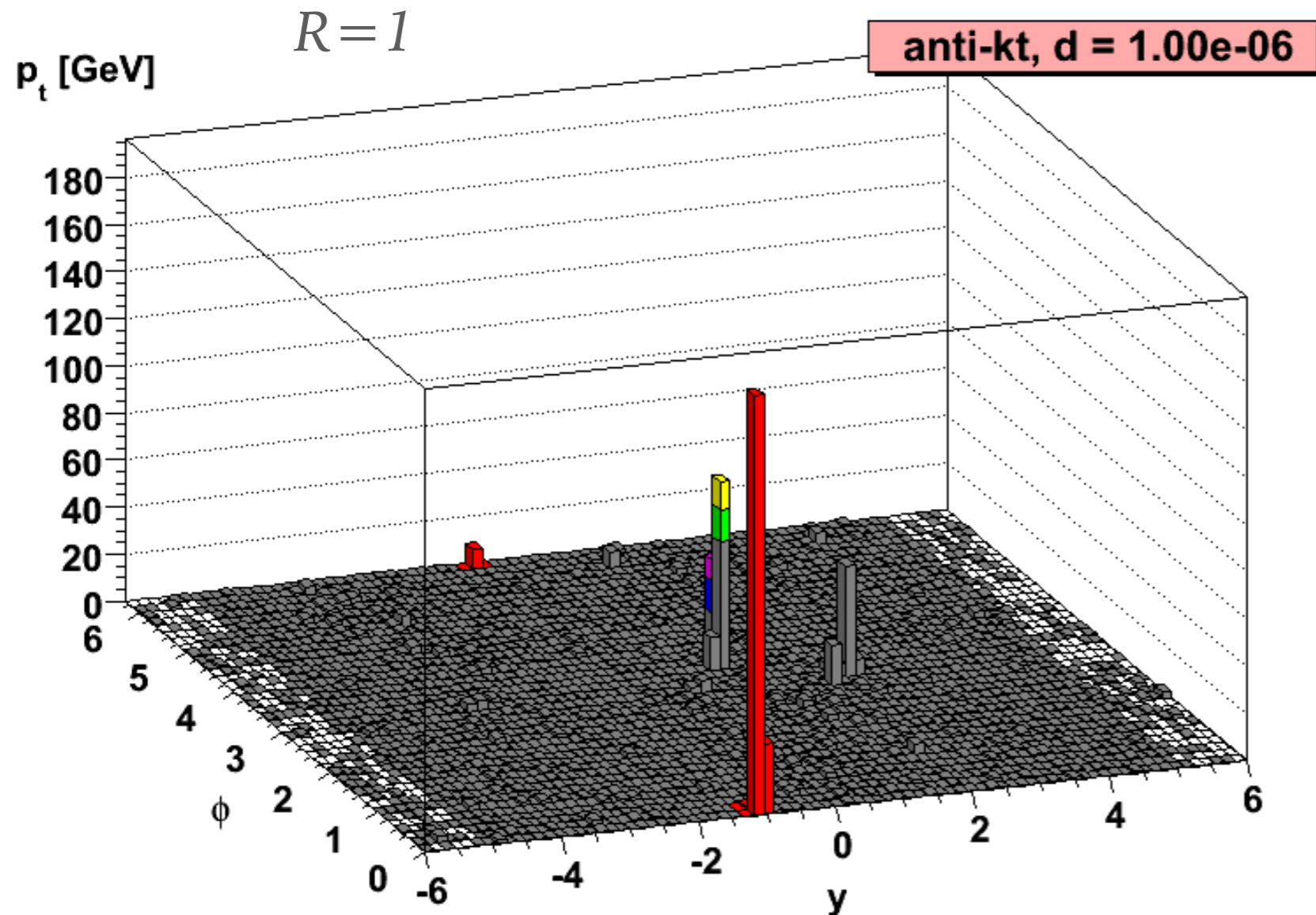
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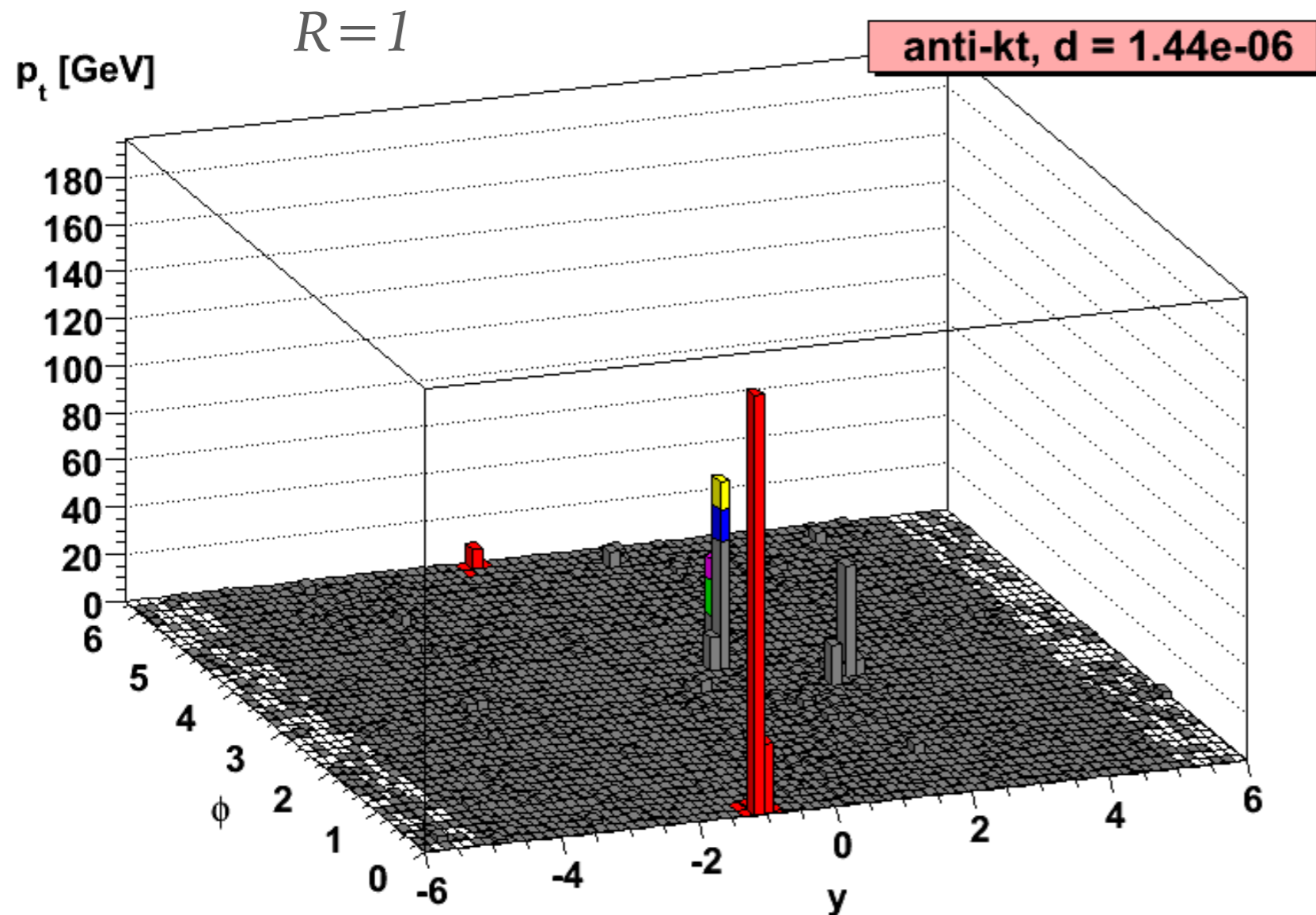
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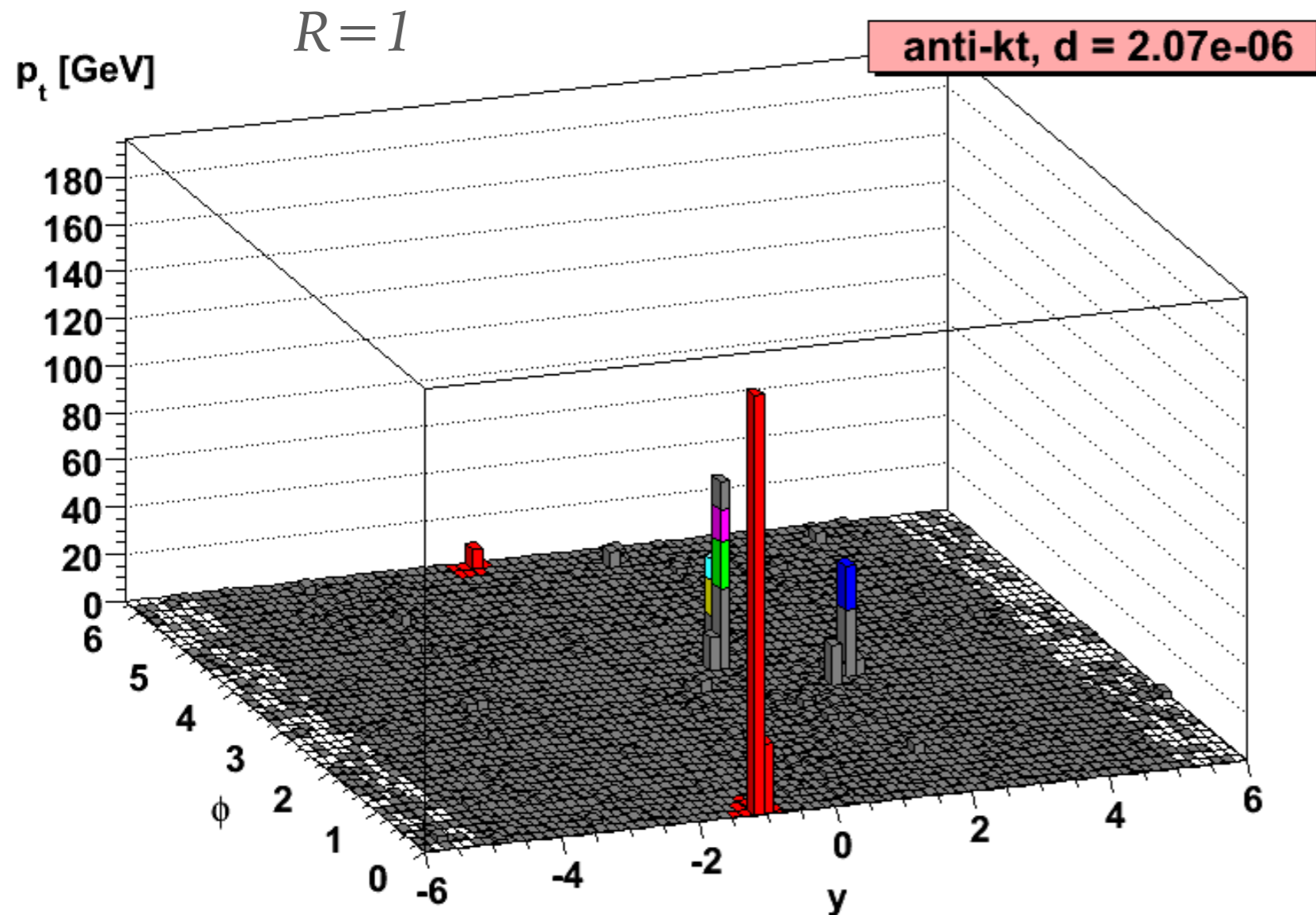
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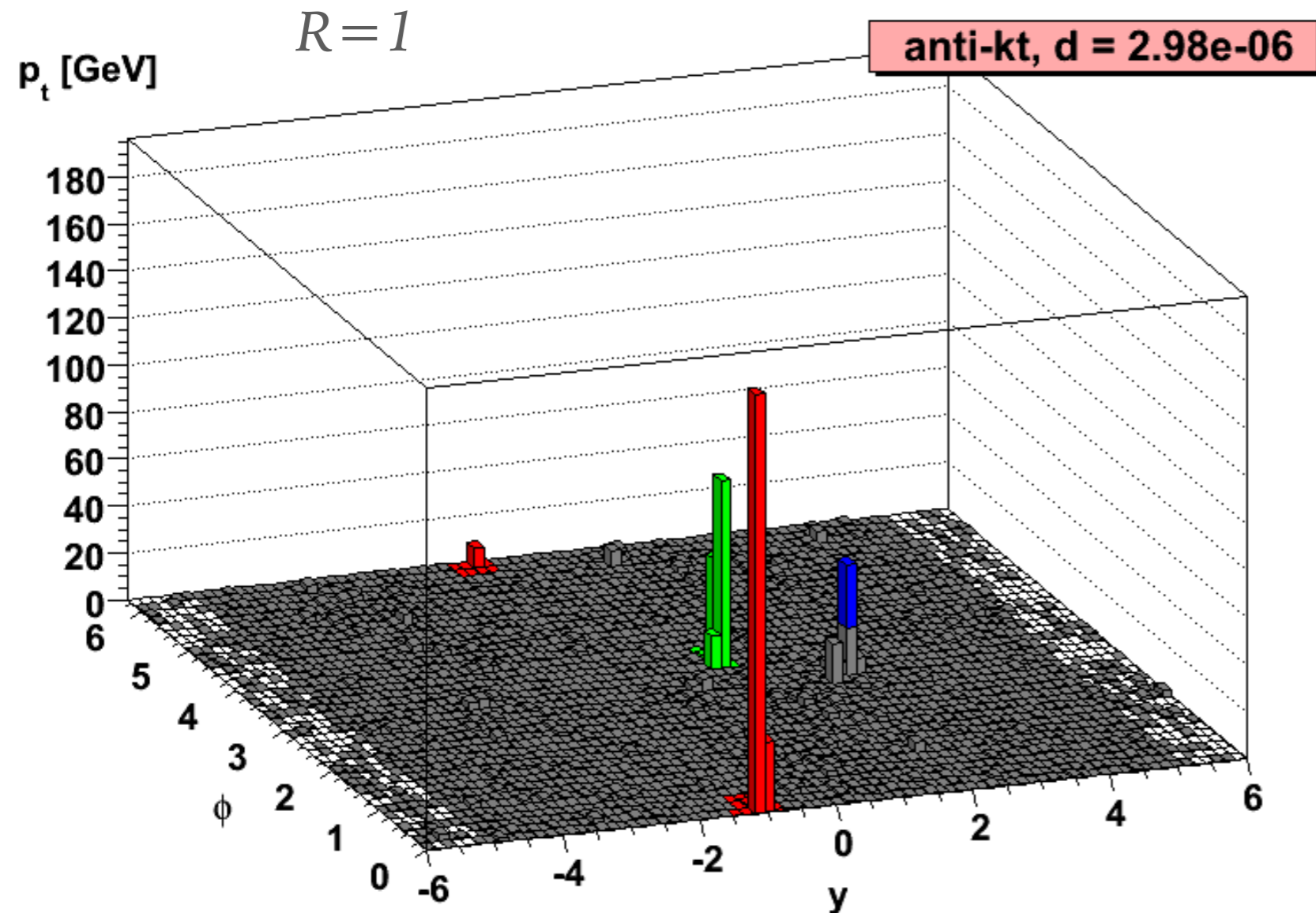
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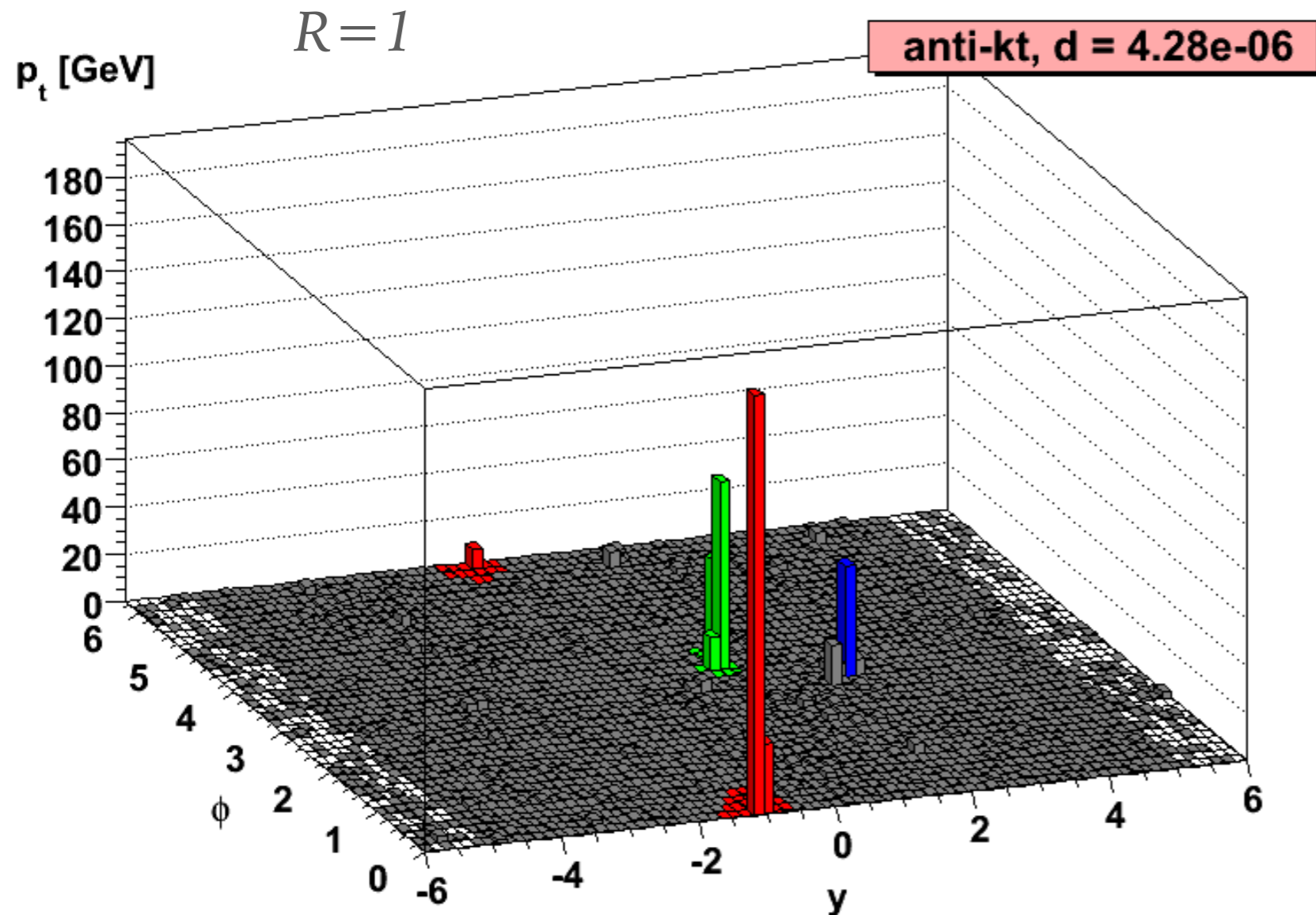
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anti- k_t in action [full simulated event]

Clustering grows around hard cores

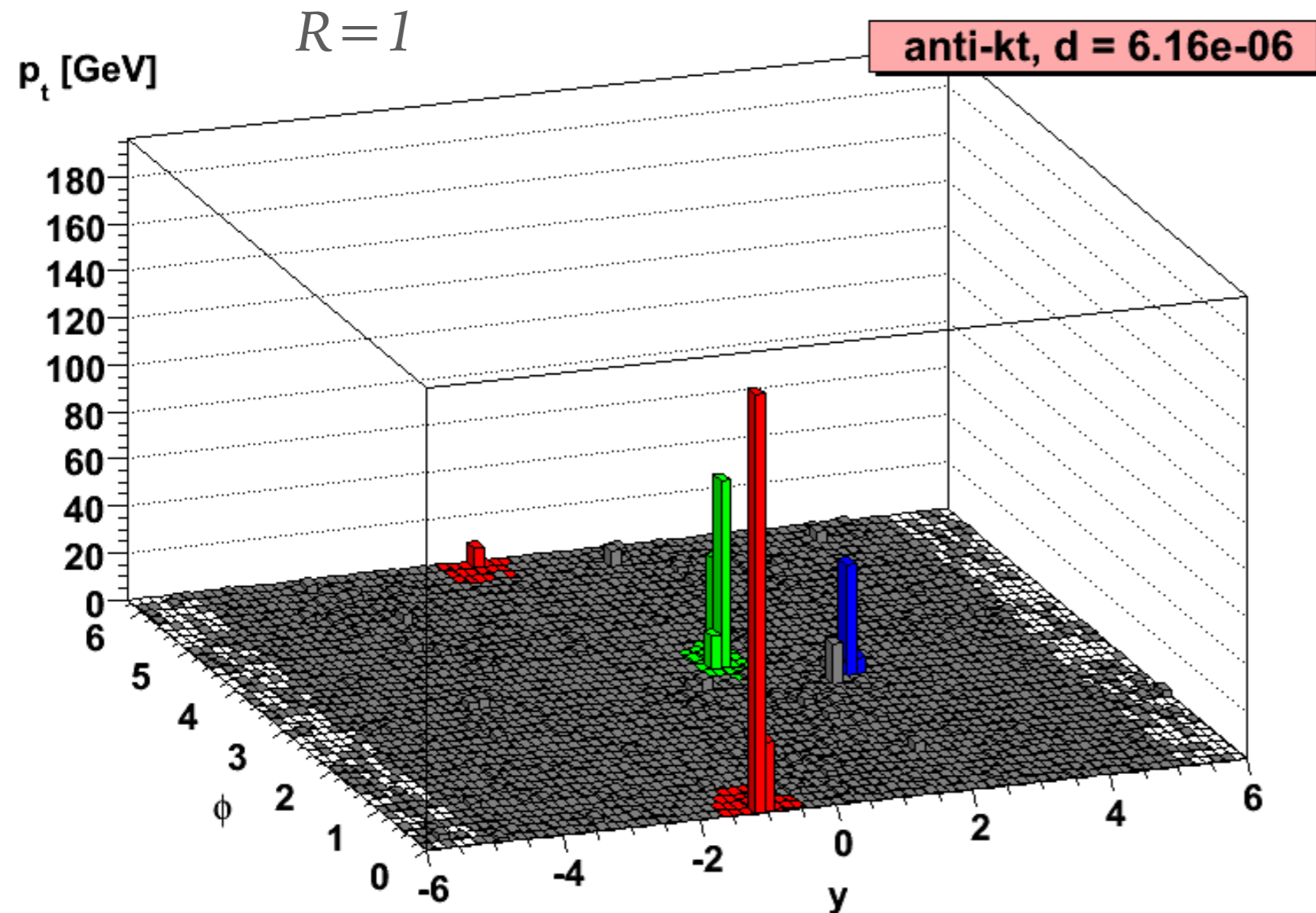
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Clustering grows around hard cores

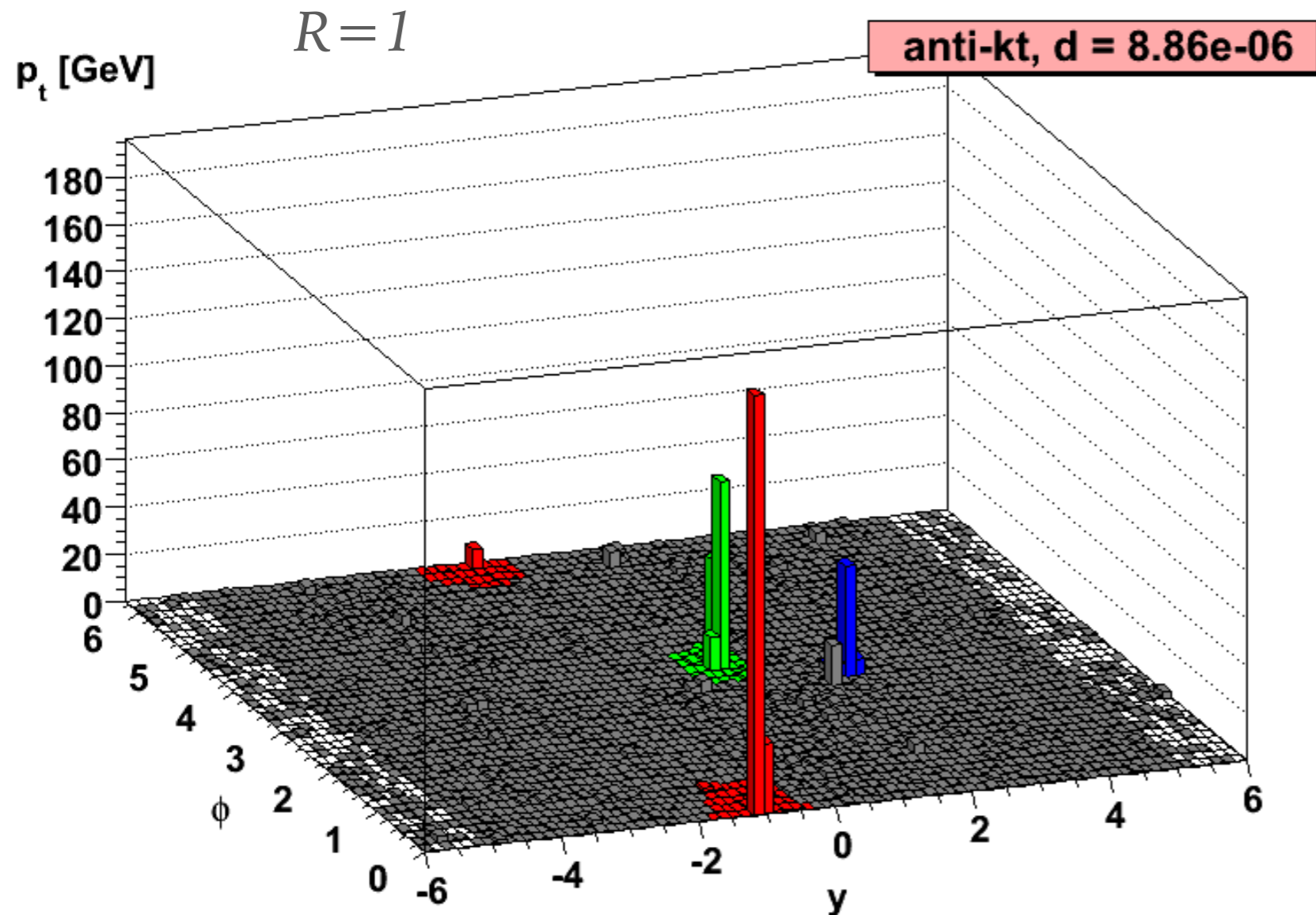
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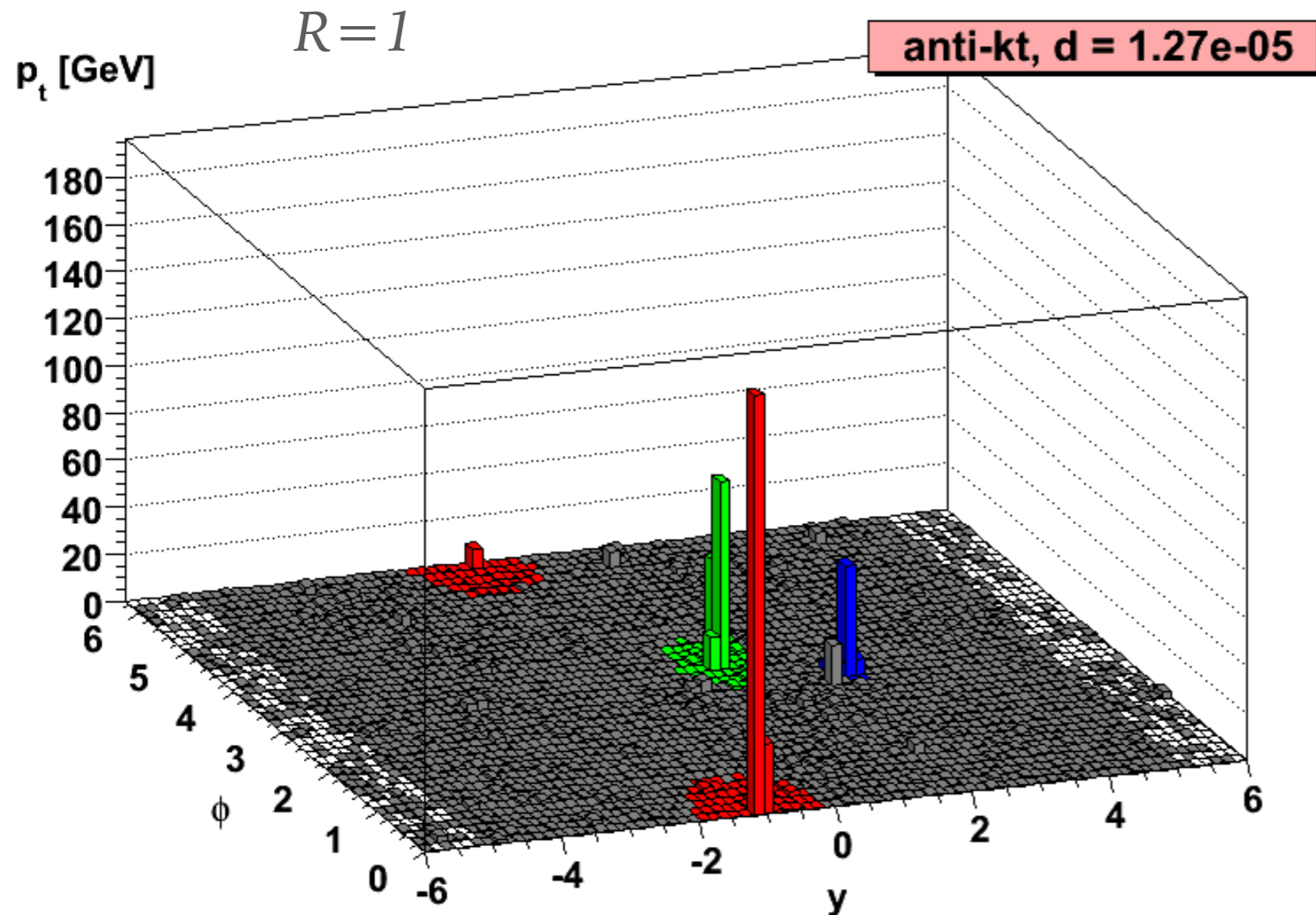
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anti- k_t in action [full simulated event]

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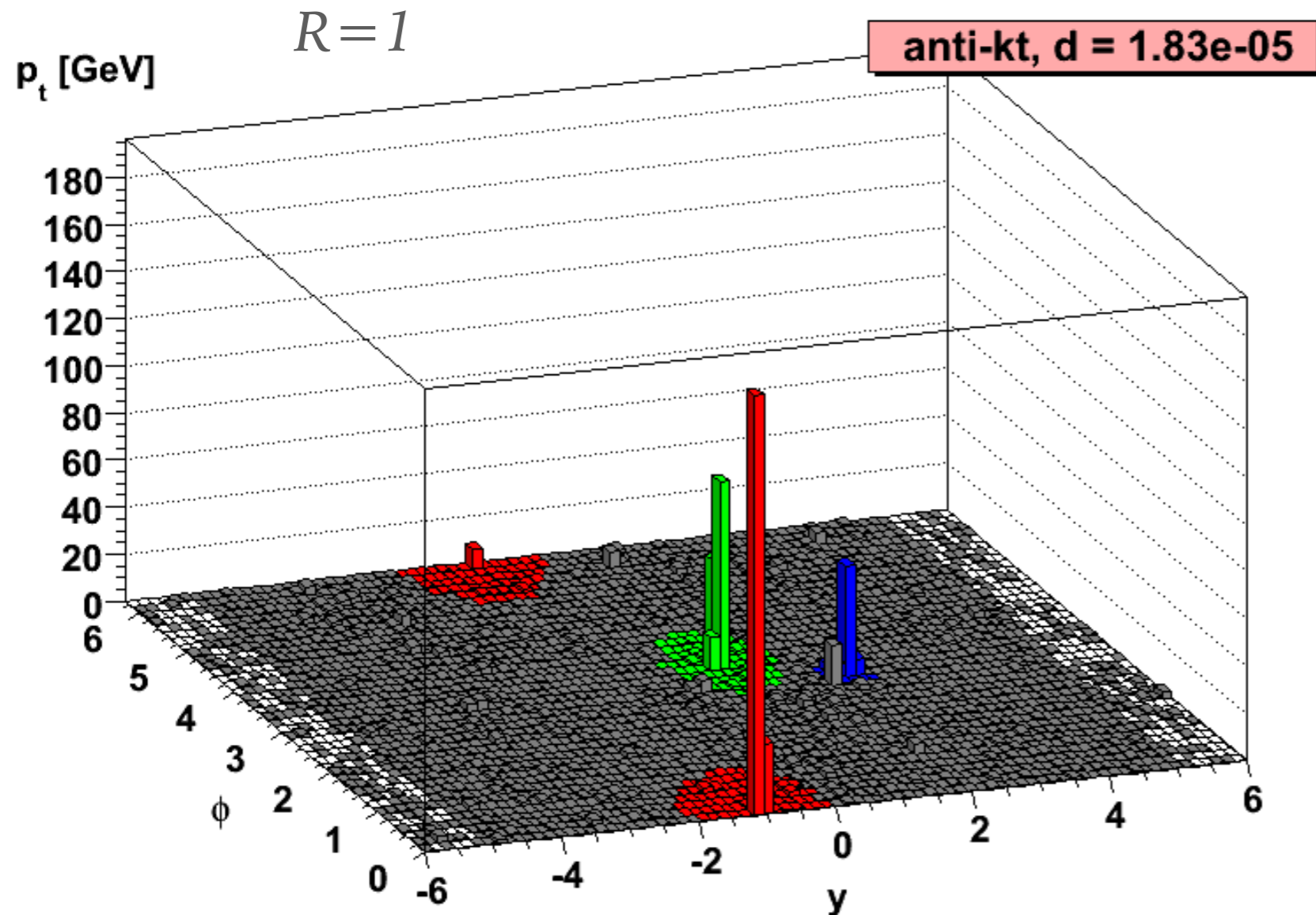
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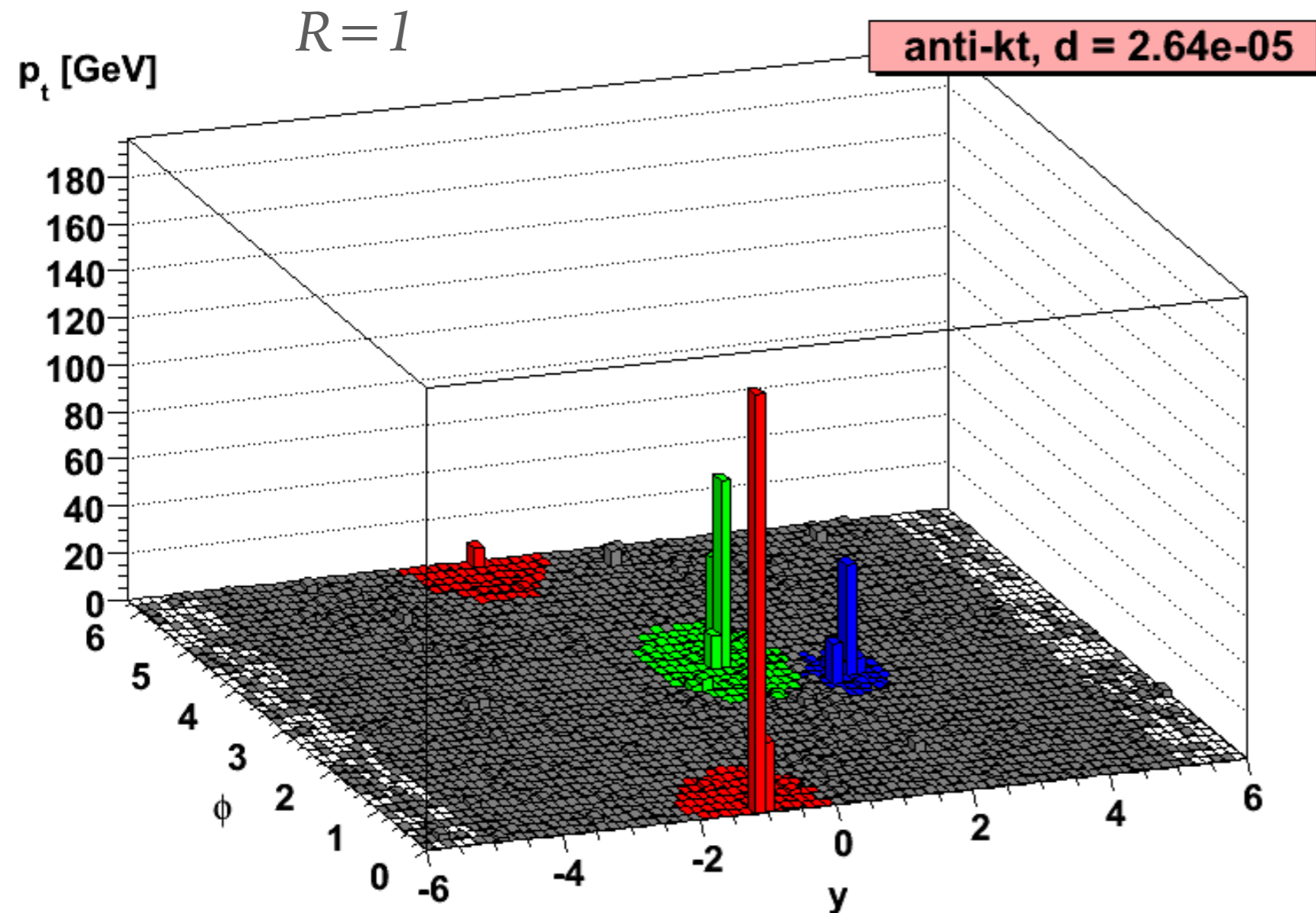
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anti- k_t in action [full simulated event]

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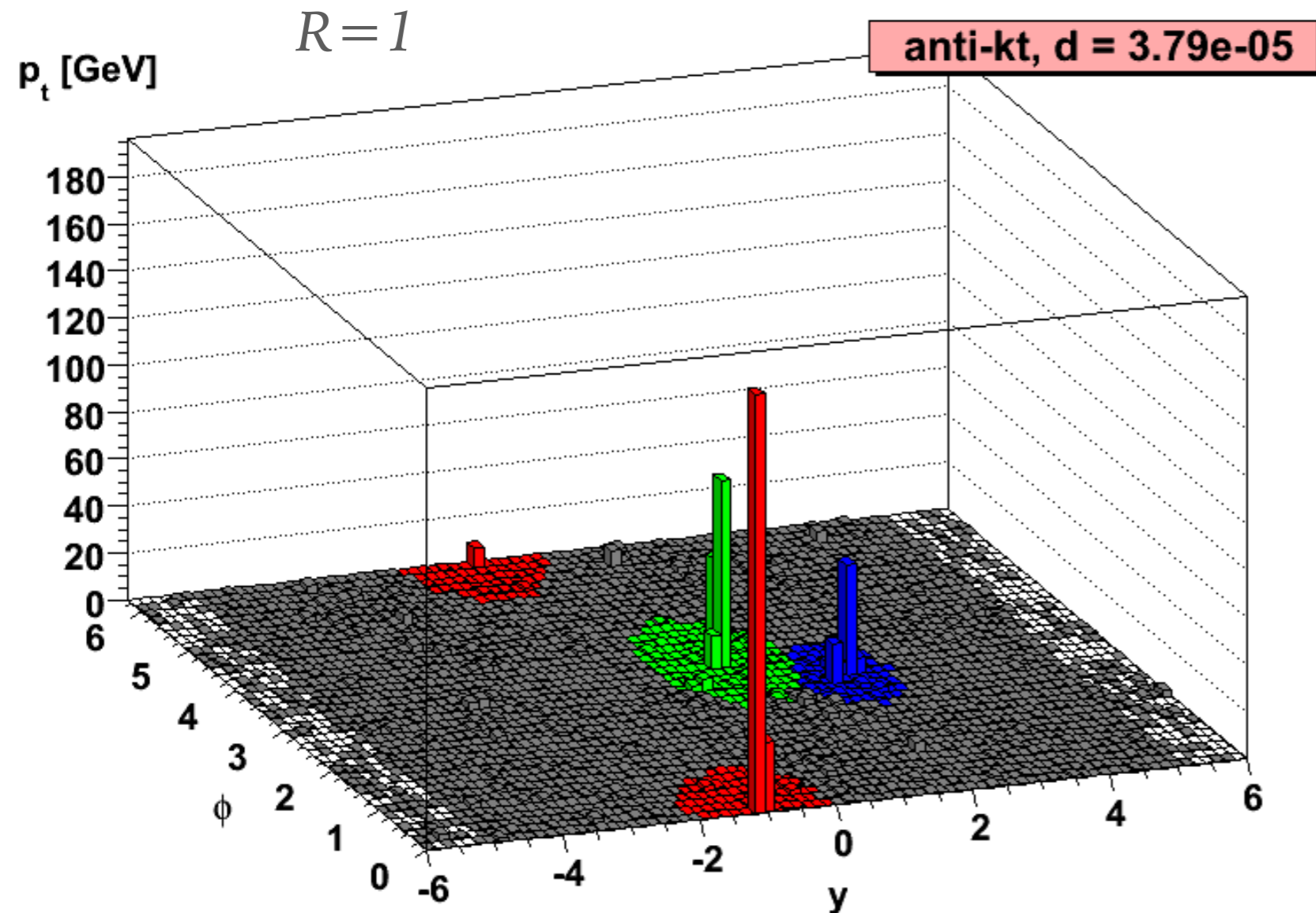
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anti- k_t in action [full simulated event]

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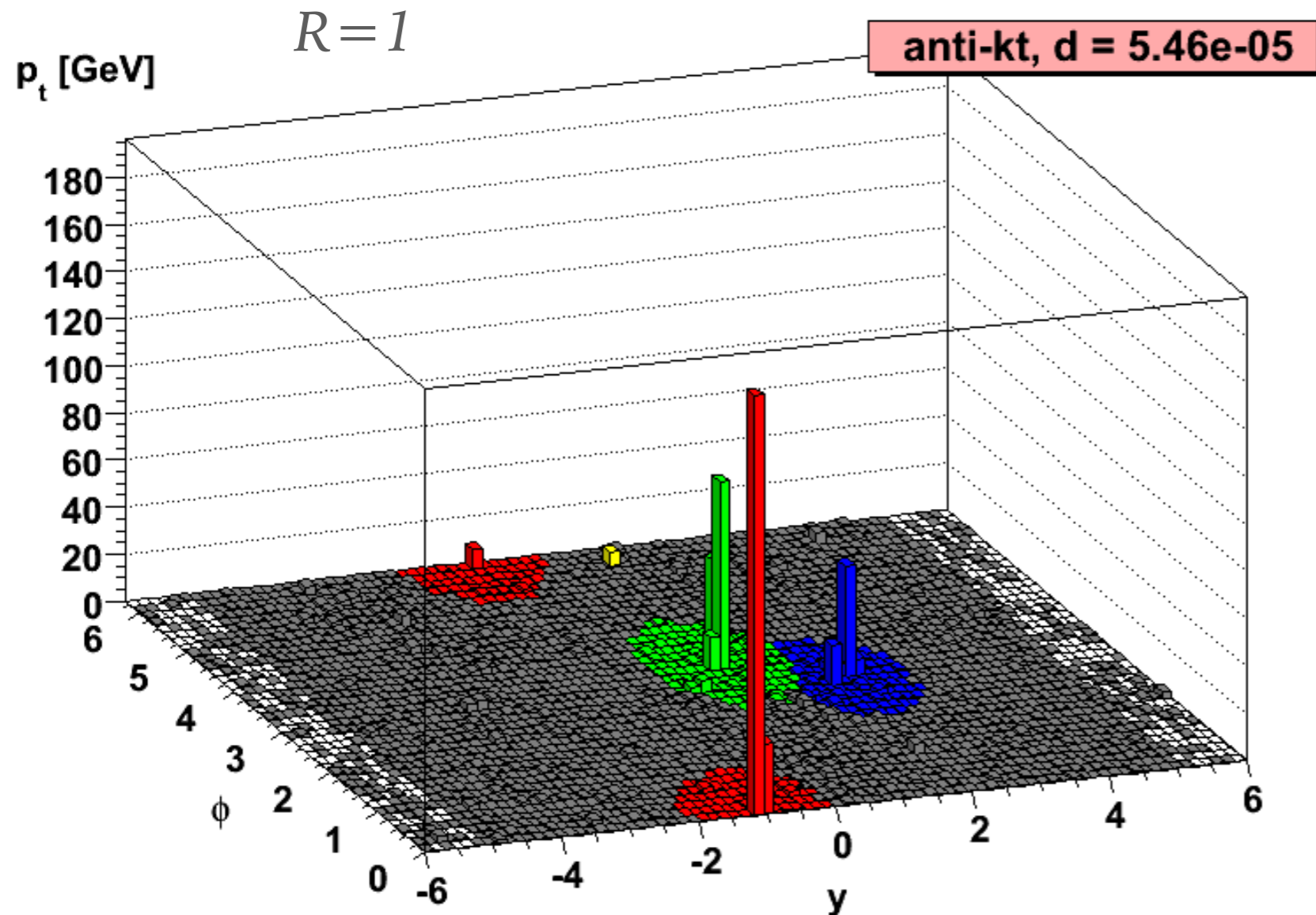
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Clustering grows around hard cores

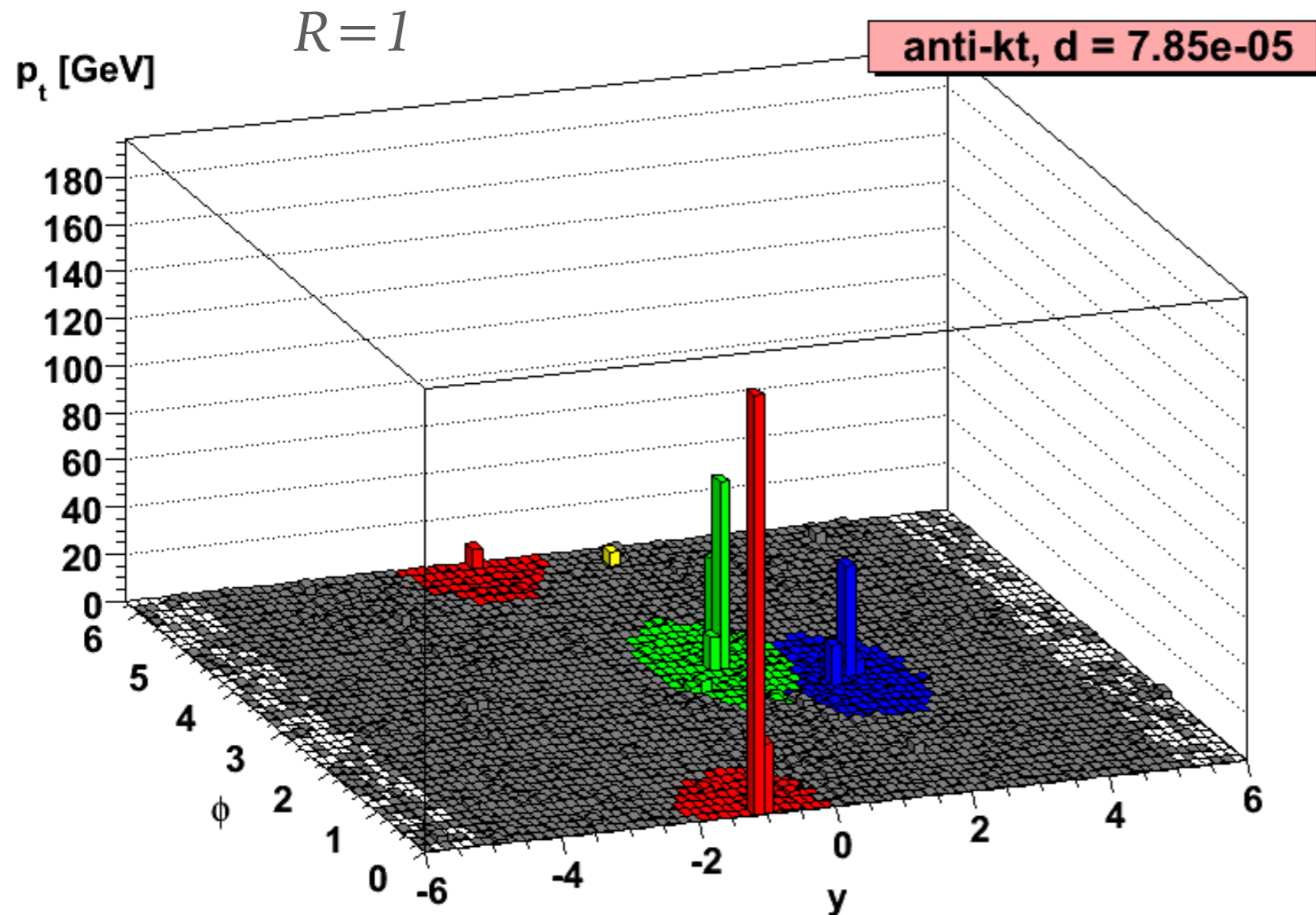
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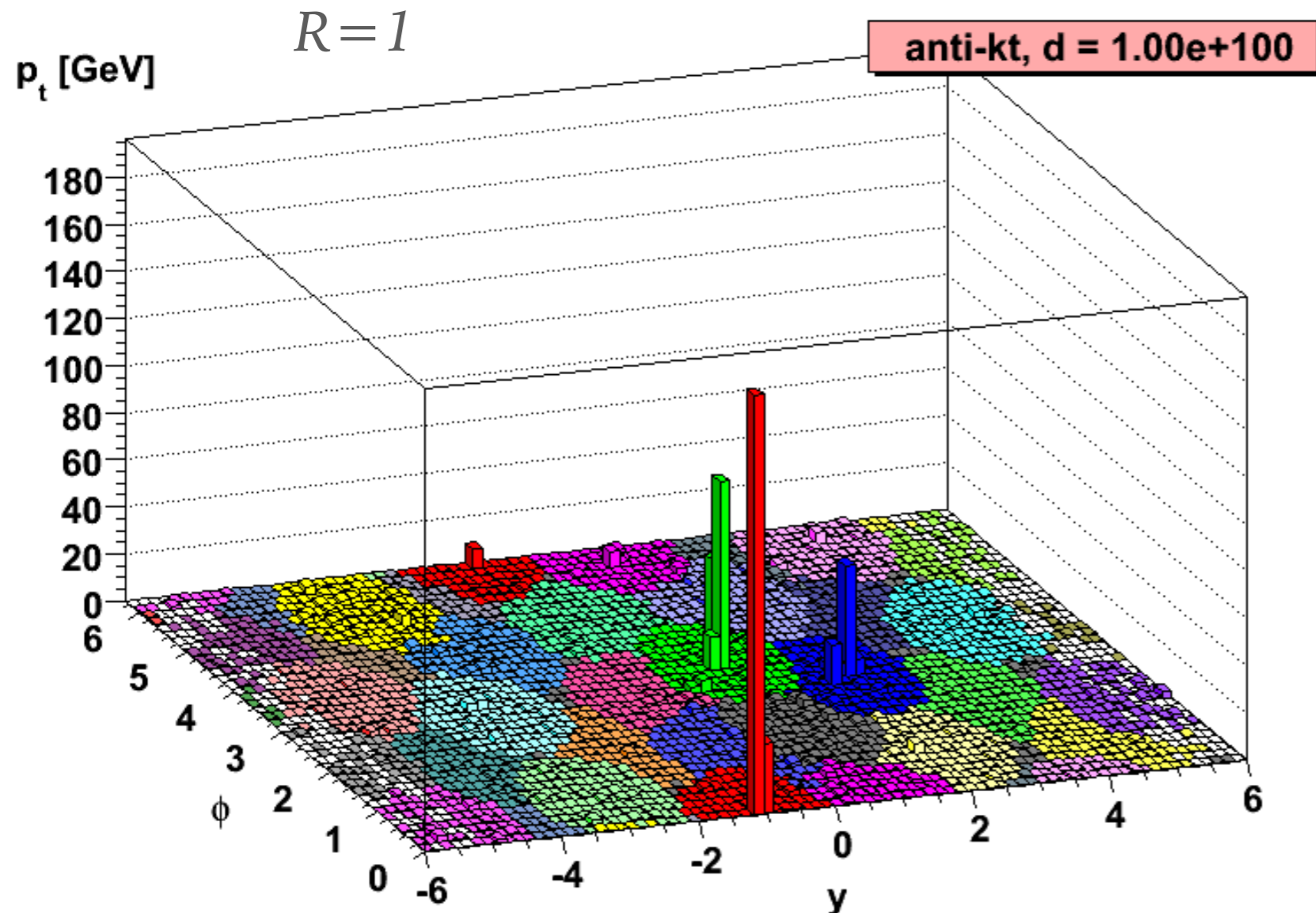
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anti- k_t in action [full simulated event]

Clustering grows around hard cores

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Anti- k_t gives circular jets (“cone-like”) in a way that’s infrared safe

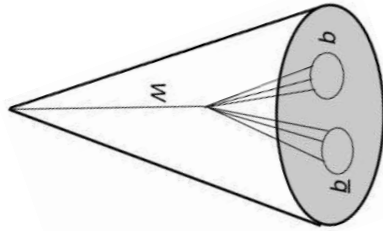
- Uses the anti- k_t algorithm
- Uses a jet radius $R=0.4$
- Uses a transverse momentum threshold that is typically at least 20 GeV (exact value depends on the analysis)

Radius and p_T threshold choices give a good compromise between

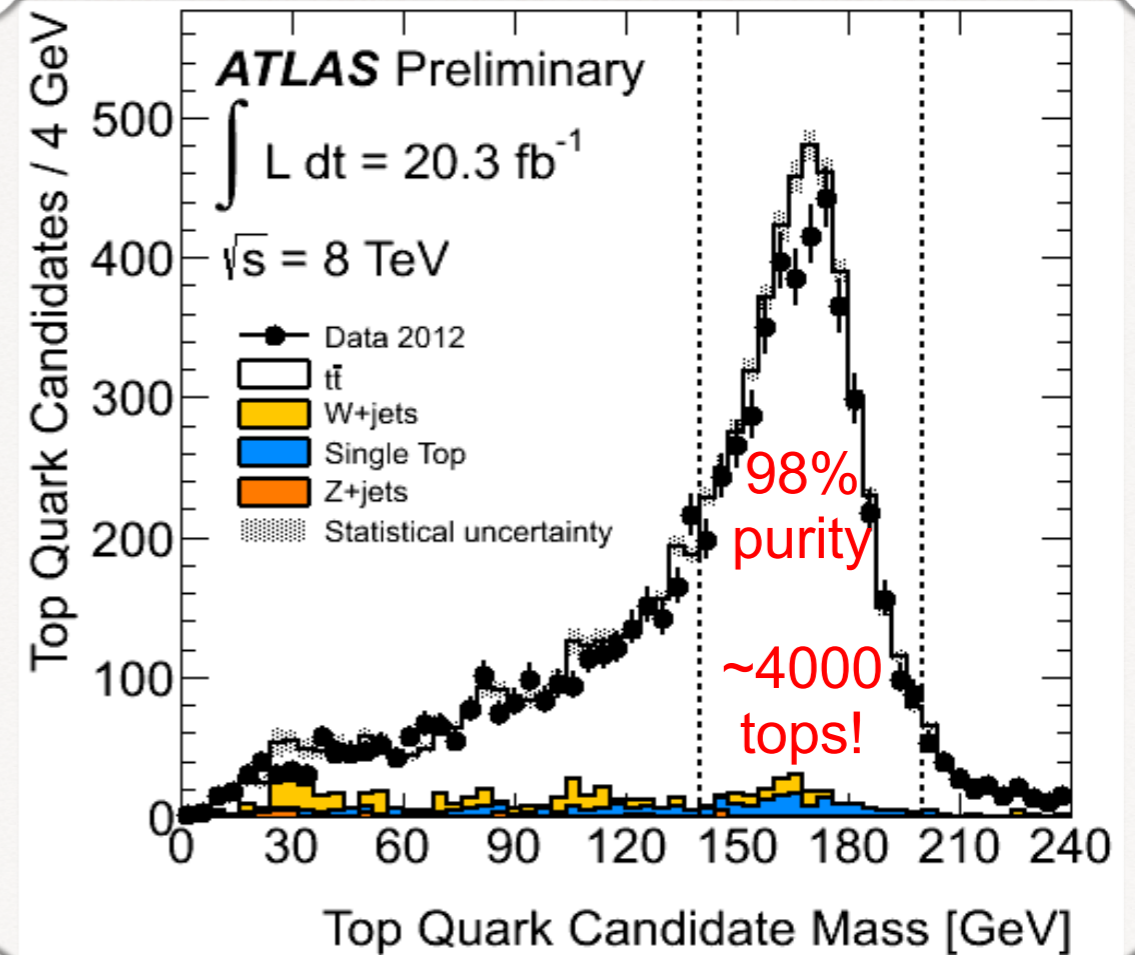
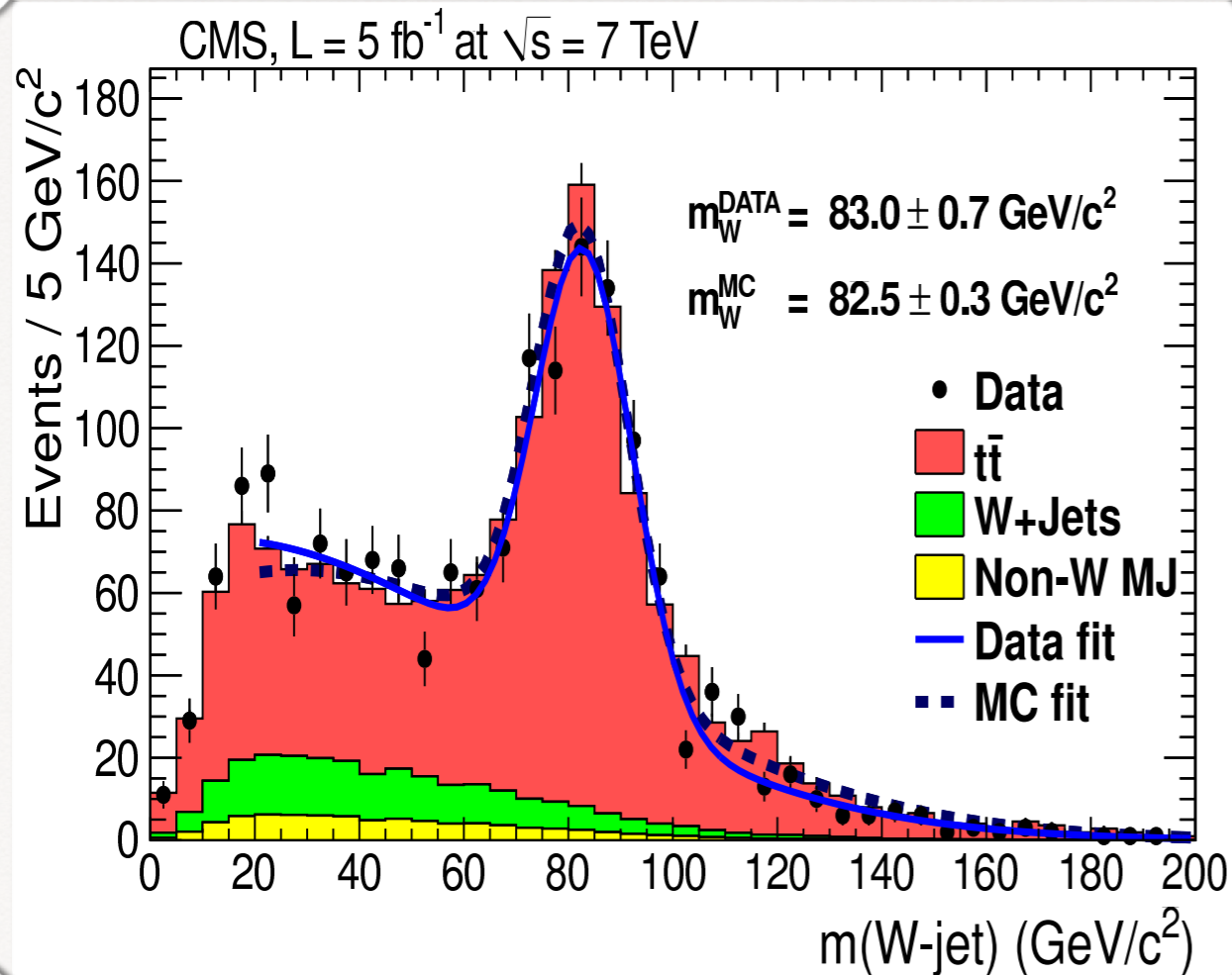
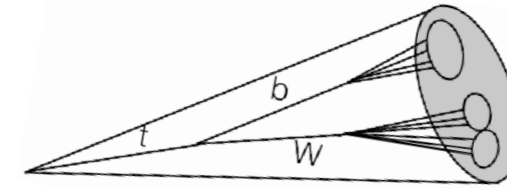
- ability to resolve multi-jet physics
- loss of radiation from jets
- additional spurious jets
- contamination from pileup

Seeing W's and tops in a single high- p_T jet

W's in a single jet

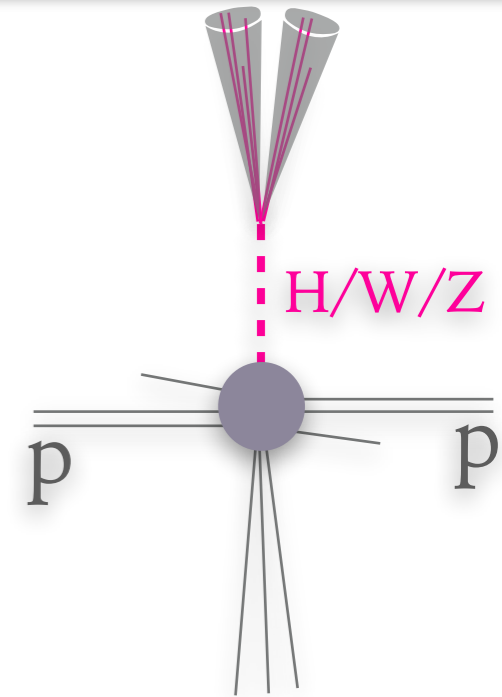


tops in a single jet

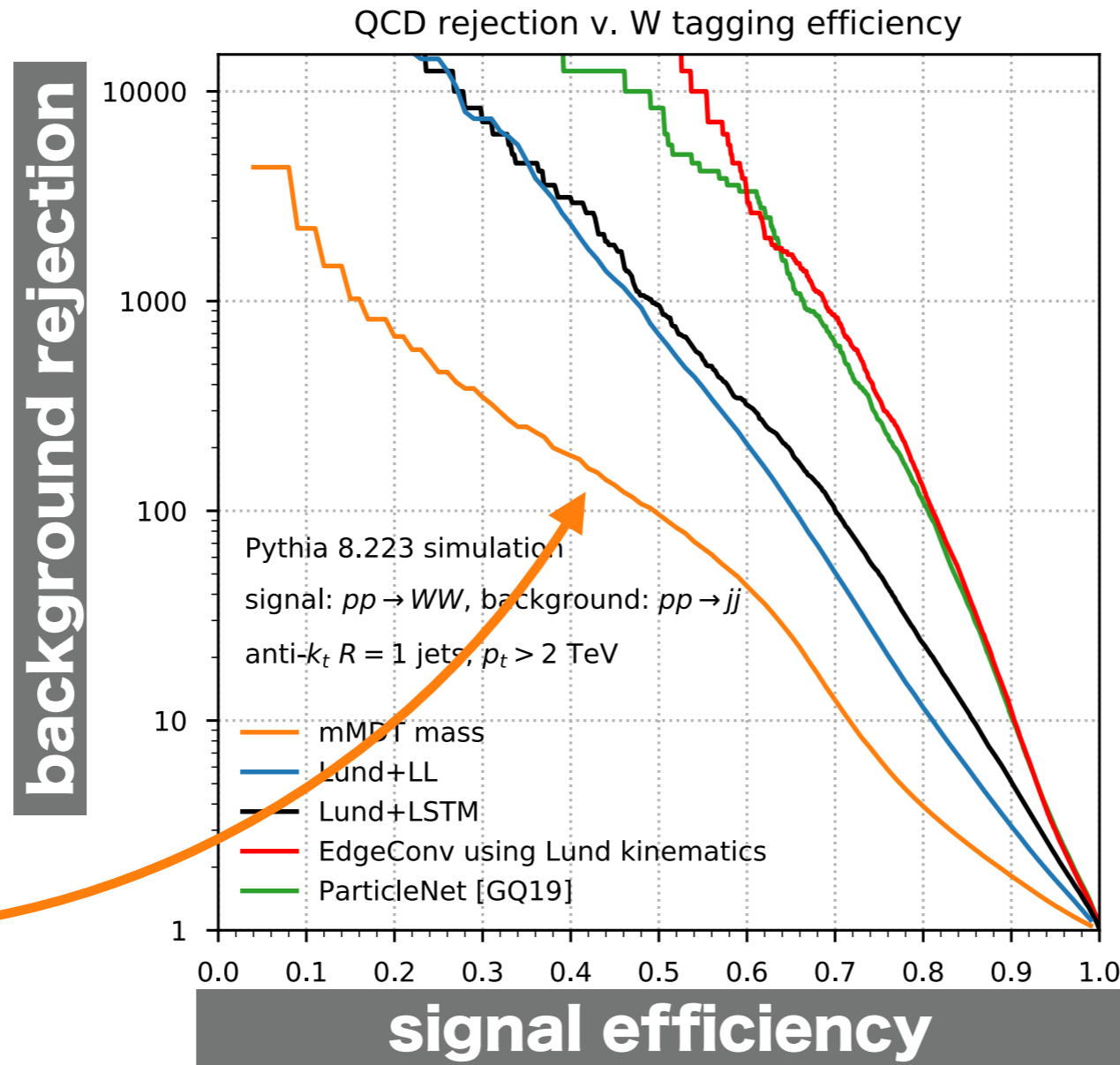


using full jet/event information for H/W/Z-boson tagging

F. Dreyer & H. Qu, 2012.08526

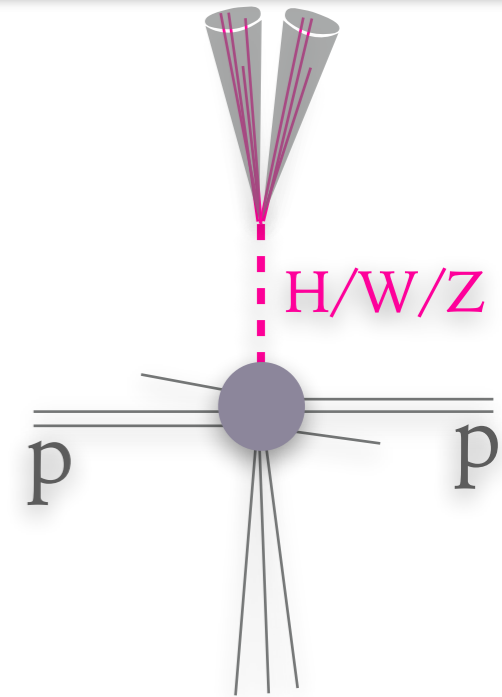


*QCD rejection
with
just jet mass
(SD/mMDT)
i.e. 2008 tools
& their
2013/14
descendants*

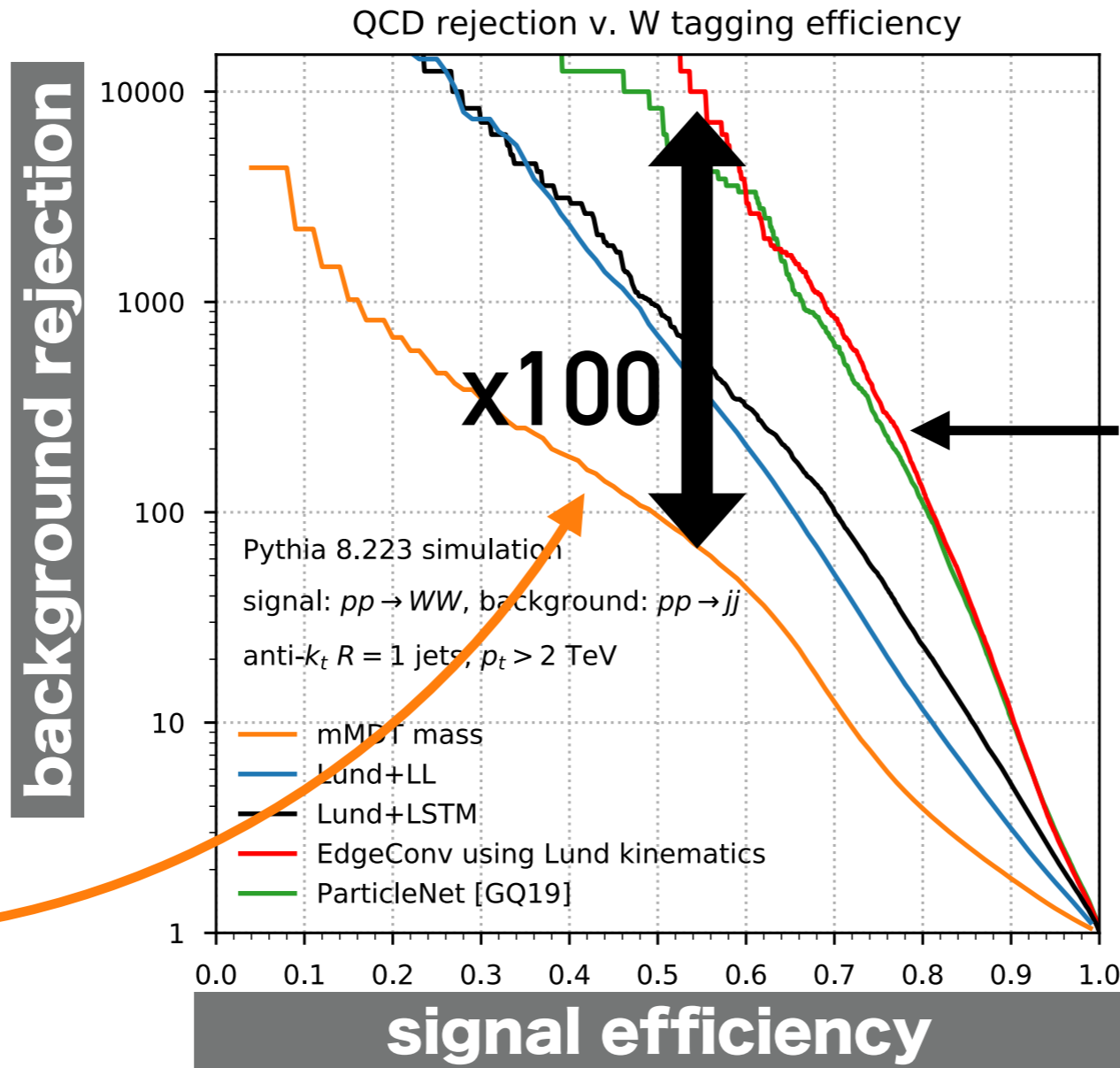


using full jet/event information for H/W/Z-boson tagging

F. Dreyer & H. Qu, 2012.08526



QCD rejection with just jet mass (SD/mMDT) i.e. 2008 tools & their 2013/14 descendants



QCD rejection with use of full jet substructure (2019 tools) 100x better

First started to be exploited by Thaler & Van Tilburg with “N-subjettiness” (2010/11)

conclusions

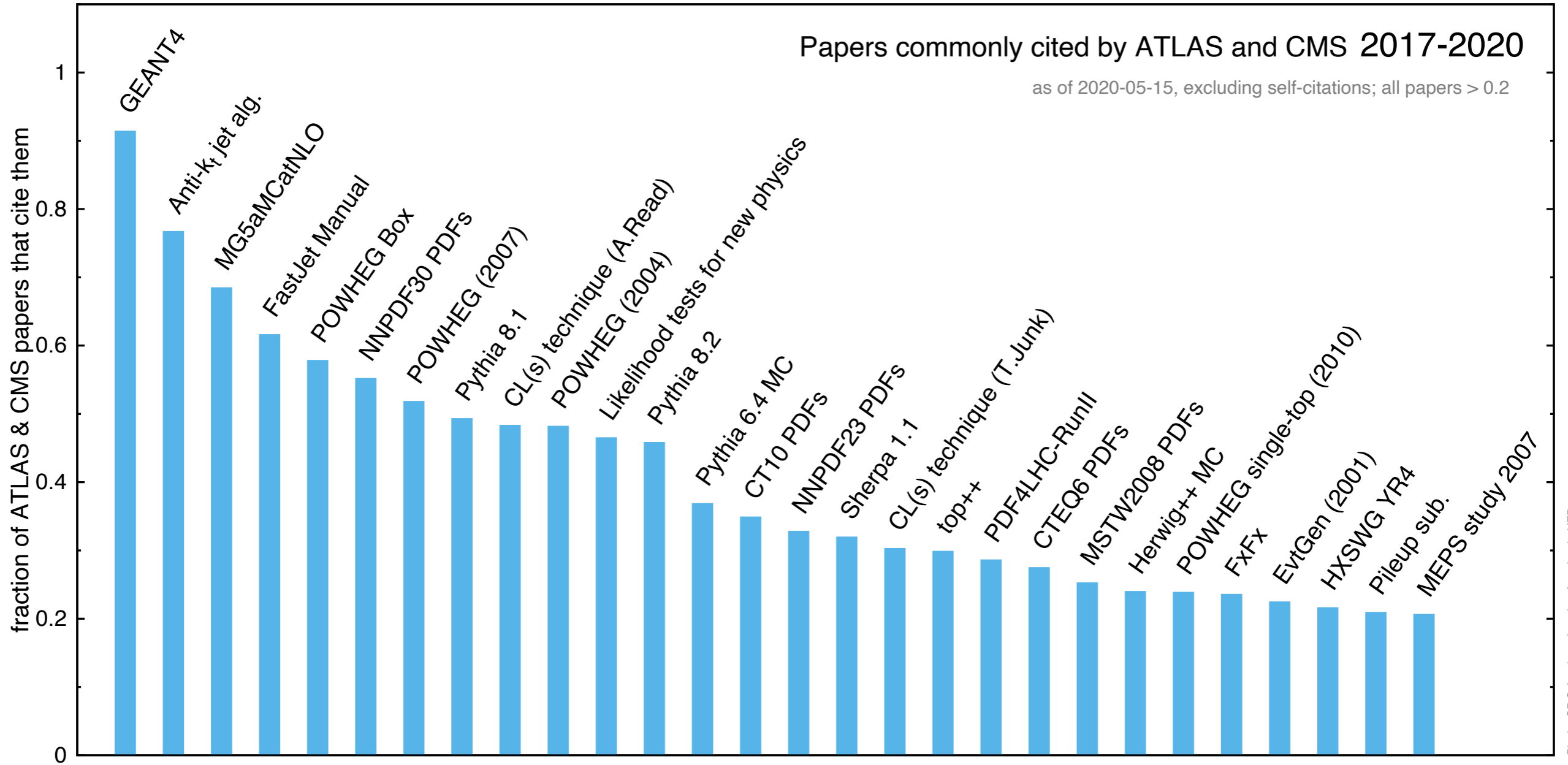
ATLAS $H \rightarrow WW^*$ ANALYSIS [1604.02997]

3 Signal and background models

The ggF and VBF production modes for $H \rightarrow WW^*$ are modelled at next-to-leading order (NLO) in the strong coupling α_s with the POWHEG MC generator [22–25], interfaced with PYTHIA8 [26] (version 8.165) for the parton shower, hadronisation, and underlying event. The CT10 [27] PDF set is used and the parameters of the PYTHIA8 generator controlling the modelling of the parton shower and the underlying event are those corresponding to the AU2 set [28]. The Higgs boson mass set in the generation is 125.0 GeV, which is close to the measured value. The POWHEG ggF model takes into account finite quark masses and a running-width Breit–Wigner distribution that includes electroweak corrections at NLO [29]. To improve the modelling of the Higgs boson p_T distribution, a reweighting scheme is applied to reproduce the prediction of the next-to-next-to-leading-order (NNLO) and next-to-next-to-leading-logarithm (NNLL) dynamic-scale calculation given by the HRES 2.1 program [30]. Events with ≥ 2 jets are further reweighted to reproduce the p_T^H spectrum predicted by the NLO POWHEG simulation of Higgs boson production in association with two jets ($H + 2$ jets) [31]. Interference with continuum WW production [32, 33] has a negligible impact on this analysis due to the transverse-mass selection criteria described in Section 4 and is not included in the signal model.

Jets are reconstructed from topological clusters of calorimeter cells [50–52] using the anti- k_t algorithm with a radius parameter of $R = 0.4$ [53]. Jet energies are corrected for the effects of calorimeter non-

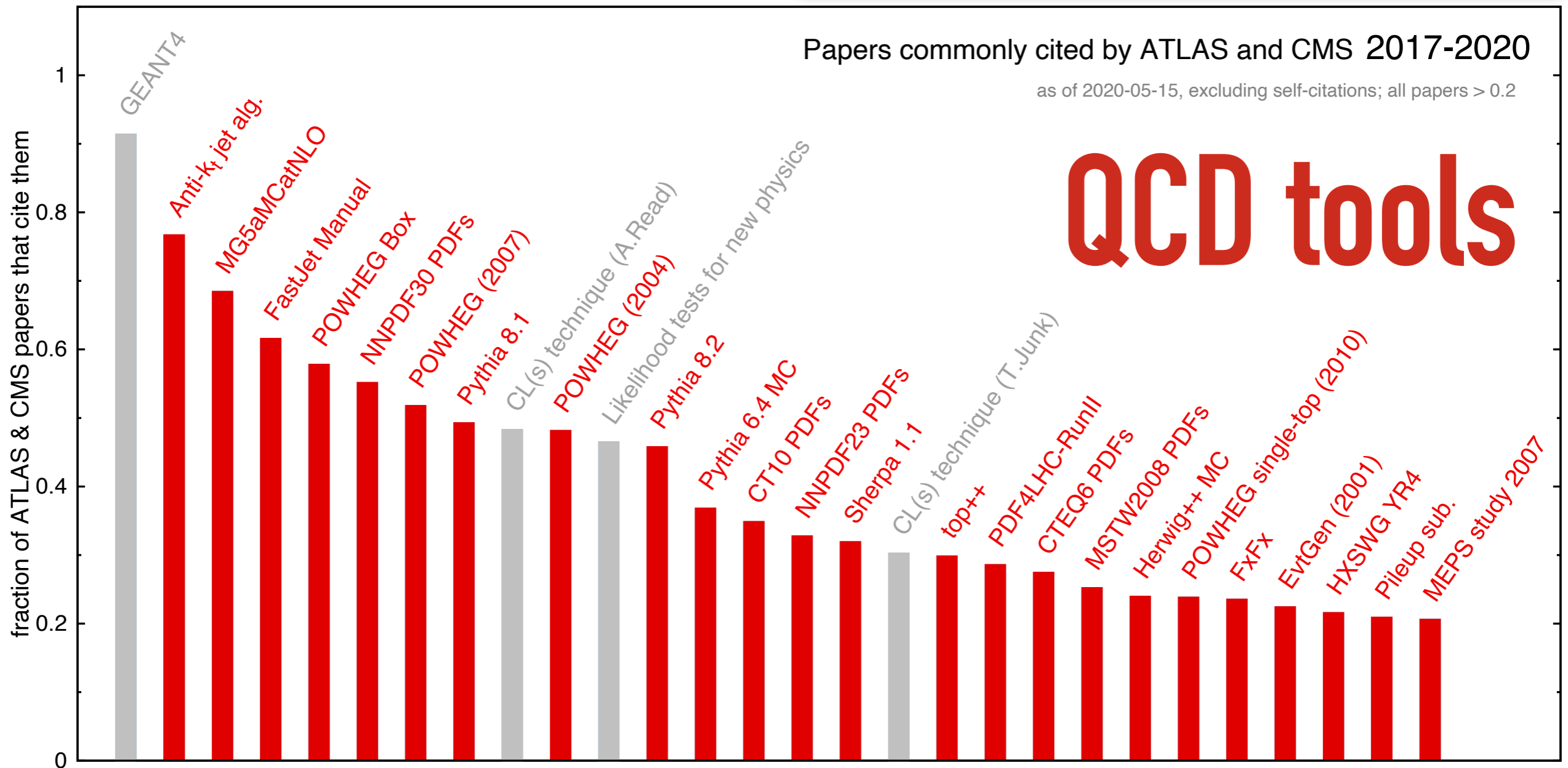
WHAT DO ATLAS & CMS USE MOST FREQUENTLY?



Plot by GP Salam based on data from InspireHEP

WHAT DO ATLAS & CMS USE MOST FREQUENTLY?

in the last 2 lectures we've seen a good number of the tools used at LHC



Plot by GP Salam based on data from InspireHEP

CONCLUSIONS

- A huge number of ingredients goes into hadron-collider predictions and studies (α_s , PDFs, matrix elements, resummation, parton showers, non-perturbative models, jet algorithms, etc.)
- a key idea is the separation of (time) scales, “factorisation”
 - **short timescales:** the hard process
 - **long timescales:** hadronic physics
 - **in between:** parton showers, resummation, DGLAP
- as long as you ask the right questions (e.g. look at jets, not individual hadrons), you can exploit this separation for quantitative, accurate, collider physics
- maximising accuracy and information extracted is today’s research frontier

Extra resources

Introductory level

QCD lecture notes from CERN schools, e.g.

- Peter Skands, [arXiv:1207.2389](https://arxiv.org/abs/1207.2389)
- GPS, [arXiv:1011.5131](https://arxiv.org/abs/1011.5131) (getting increasingly dated!)

More advanced

Slides from QCD and Monte Carlo specific schools

- CTEQ schools: <https://www.physics.smu.edu/scalise/cteq/#Summer>
- MCNet schools: <https://www.montecarlonet.org/schools/>

Books

- QCD and collider physics, Ellis, Stirling & Webber
- The Black Book of Quantum Chromodynamics, Campbell, Huston & Krauss

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