

Flavor-violating new physics at the intensity frontier

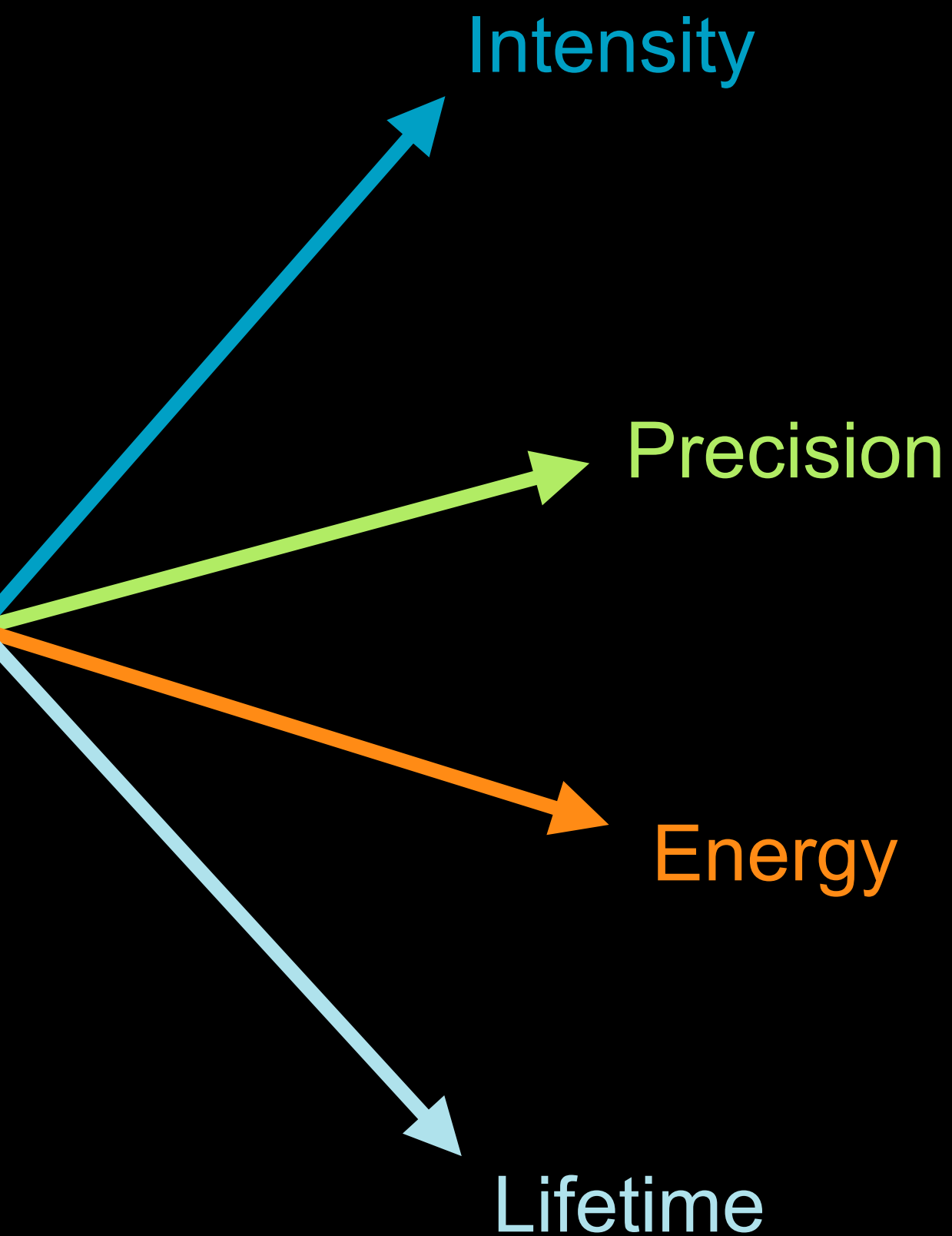


Matheus Hostert
Harvard University
mhostert@g.harvard.edu

The Mitchell Conference 2024
May 23rd, 2024

Going beyond the Standard Model with Muons

The “progress axes” for muon facilities



Rare decay searches (**Intensity** & **Precision**)

$10^{16} - 10^{18}$ muons in clean environments

This talk: Five-track events at the Mu3e experiment

This talk: Muon-induced baryon number violation at Mu2e

Lepton Flavor Beyond the Standard Model

Accidental symmetry in the Standard Model

$$U(1)_B \times U(1)_{L_e} \times U(1)_{L_\mu} \times U(1)_{L_\tau} \quad \text{or} \quad U(1)_{B+L} \times U(1)_{B-L} \times U(1)_{L_e-L_\mu} \times U(1)_{L_e+L_\tau-2L_\mu}$$

J. Heeck (arXiv:1610.07623)

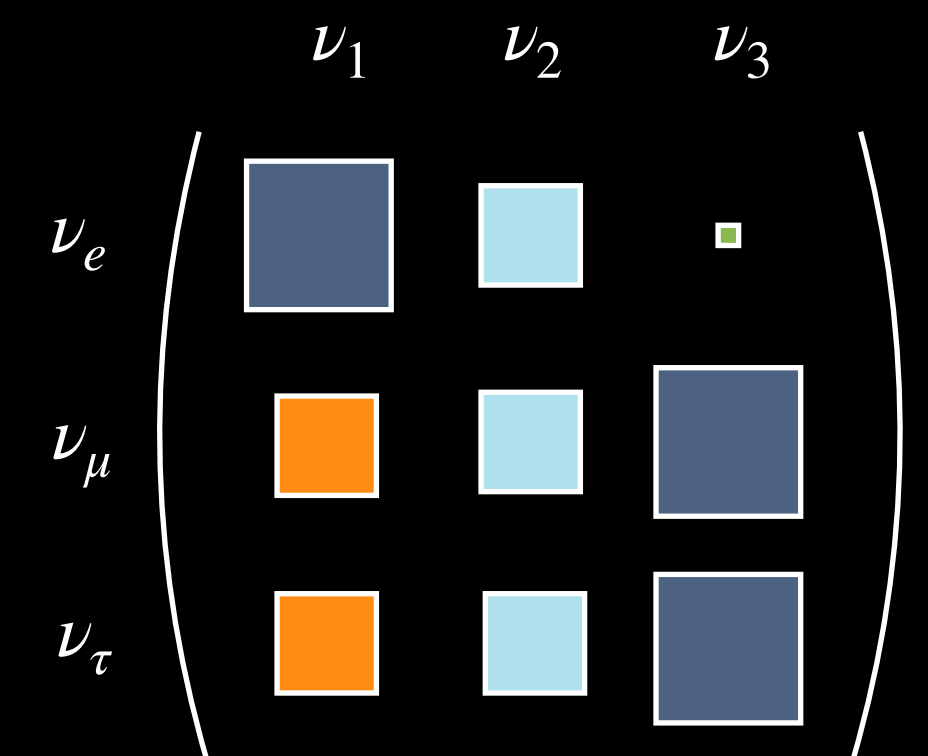
Neutrino masses violate lepton flavor

$$\nu_\alpha \rightarrow \nu_\beta$$

Lucky to have discovered this

“Earth-sized flavor interferometers”

Lepton mixing



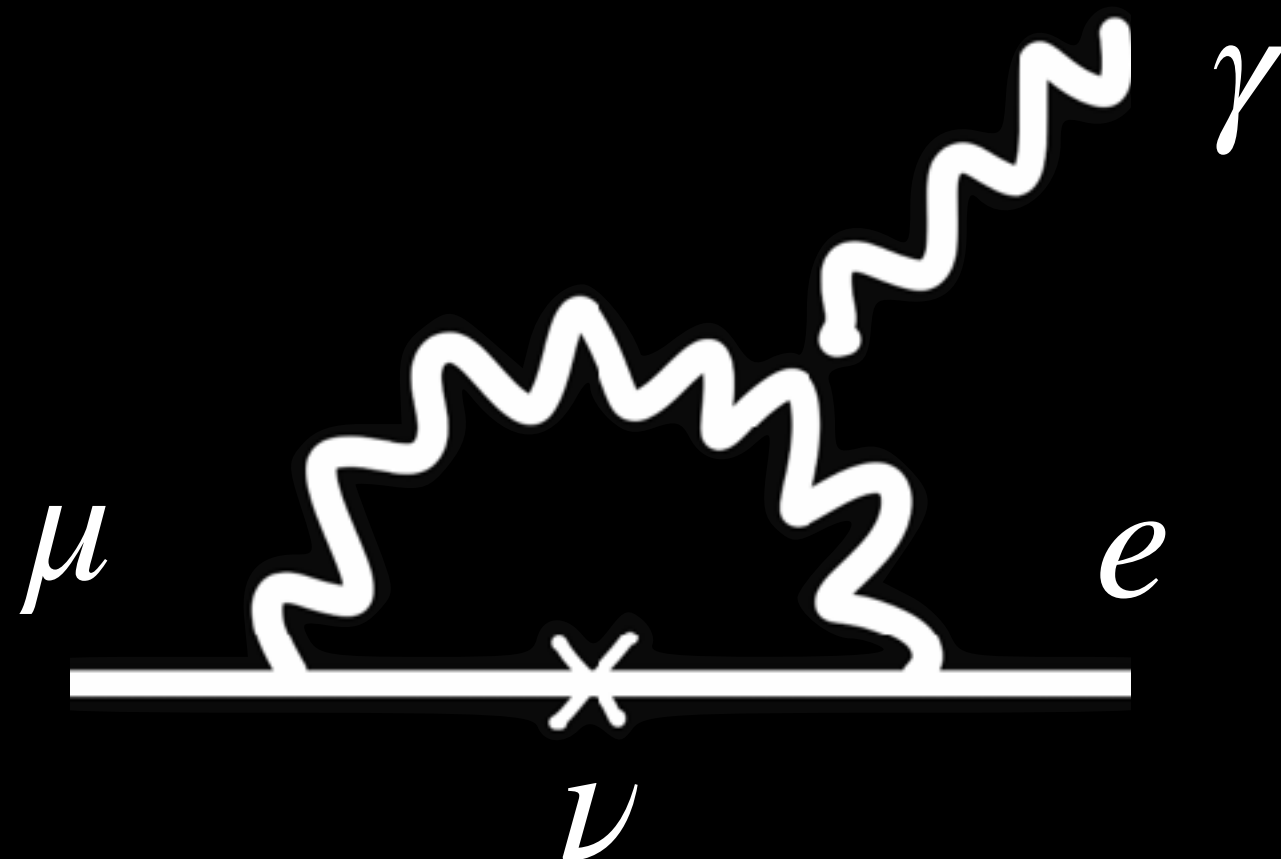
Lepton Flavor Beyond the Standard Model

Accidental symmetry in the Standard Model

$$U(1)_B \times U(1)_{L_e} \times U(1)_{L_\mu} \times U(1)_{L_\tau} \quad \text{or} \quad U(1)_{B+L} \times U(1)_{B-L} \times U(1)_{L_e-L_\mu} \times U(1)_{L_e+L_\tau-2L_\mu}$$

J. Heeck (arXiv:1610.07623)

But in charged lepton sector, this is unobservable:



$$\mathcal{B}(\mu \rightarrow e\gamma) \sim \frac{3\alpha}{32\pi} \frac{m_\nu^4}{M_W^4} \sim 10^{-53}$$

Any measurement of a non-zero rate provides unambiguous evidence for new physics.

Lepton Flavor Beyond the Standard Model

Accidental symmetry in the Standard Model

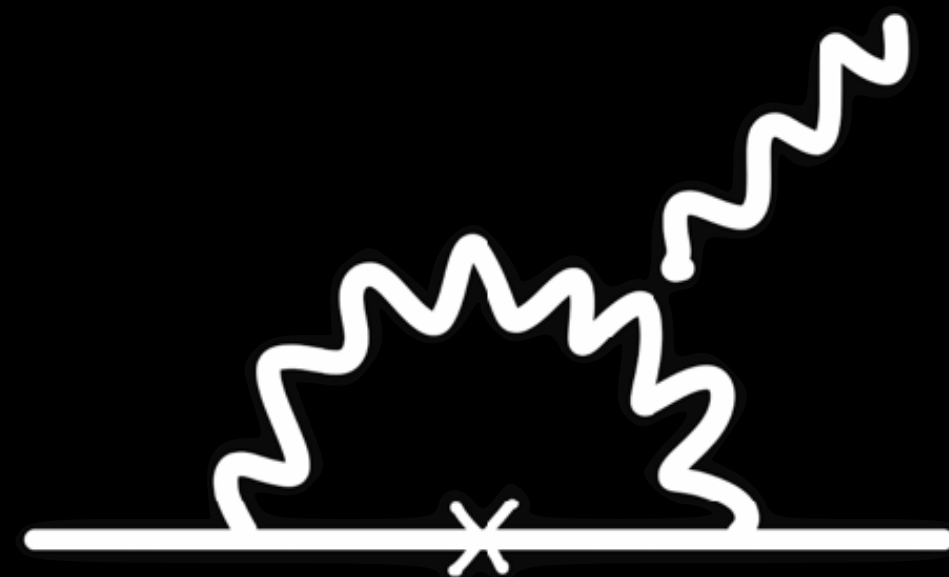
$$U(1)_B \times U(1)_{L_e} \times U(1)_{L_\mu} \times U(1)_{L_\tau} \quad \text{or} \quad U(1)_{B+L} \times U(1)_{B-L} \times U(1)_{L_e-L_\mu} \times U(1)_{L_e+L_\tau-2L_\mu}$$

J. Heeck (arXiv:1610.07623)

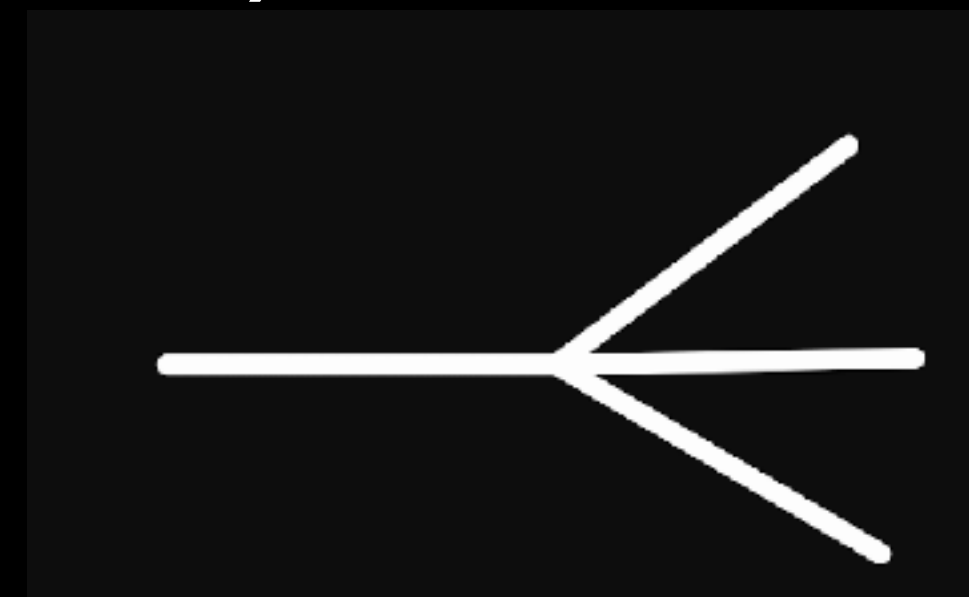
Muons are the lamppost for this symmetry factor:

$$\Delta(L_e - L_\mu) = 2$$

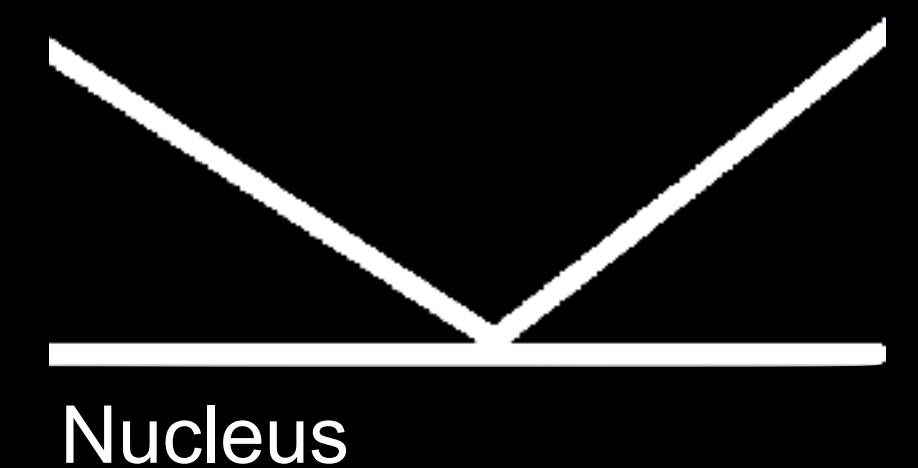
$$\mu \rightarrow e\gamma$$



$$\mu \rightarrow eee$$



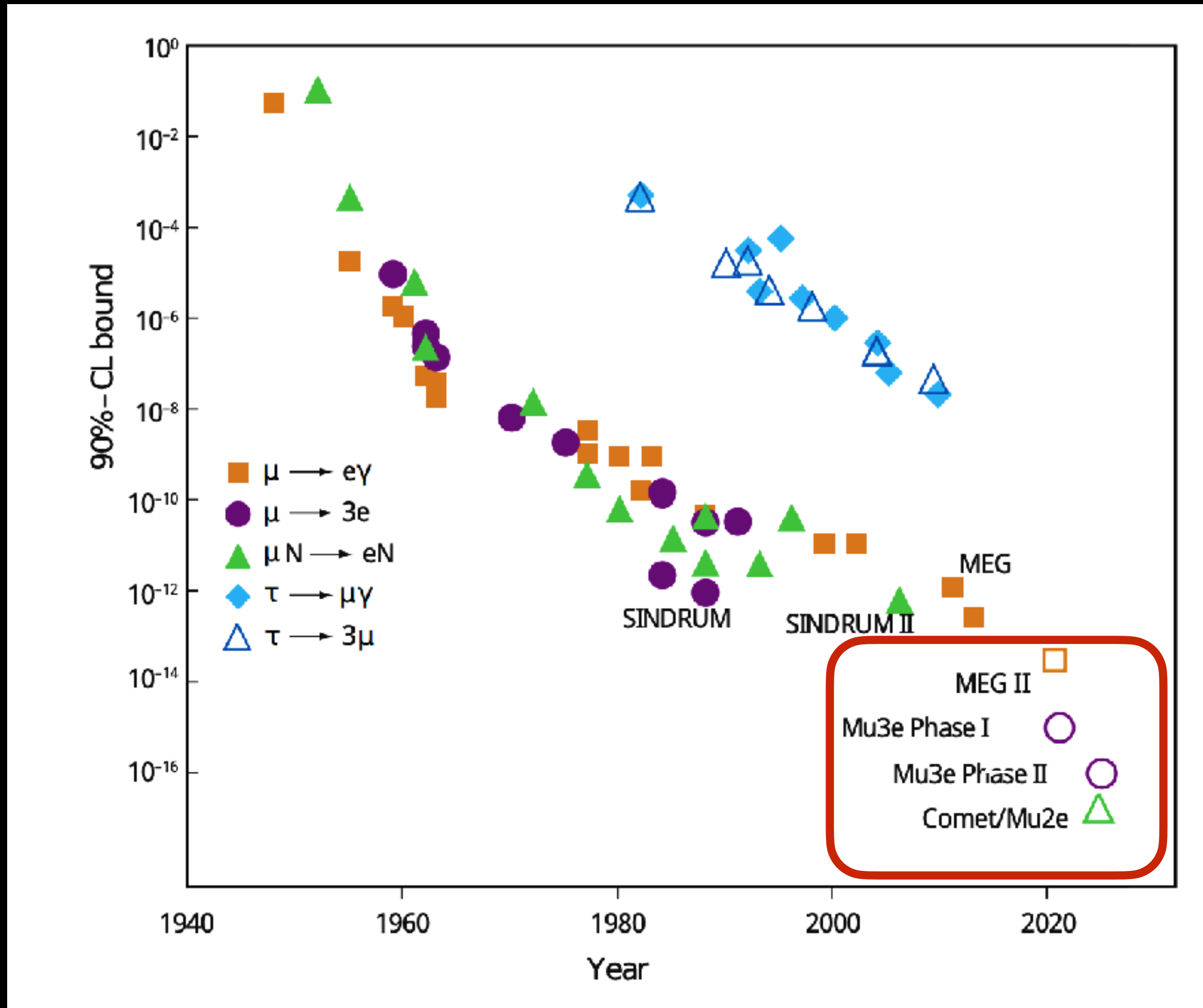
$$\mu A \rightarrow eA$$



Going beyond the Standard Model

Muon facilities

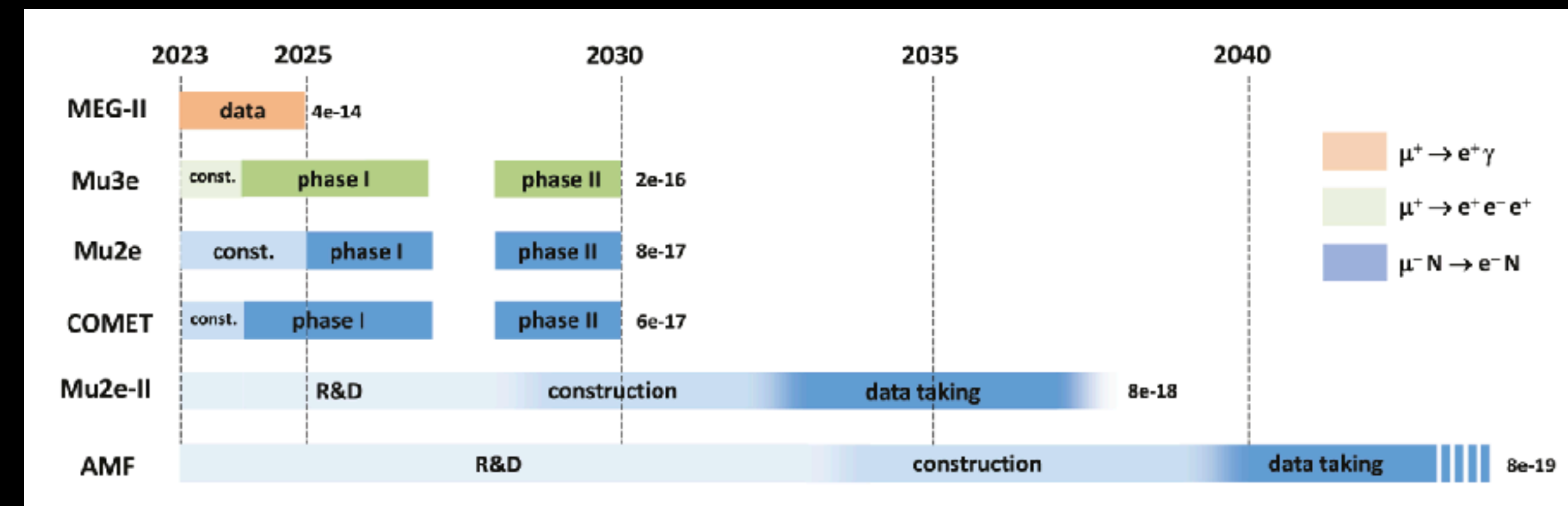
Huge progress is coming. And soon!



L. Calibbi, G. Signorelli, arXiv:1709.00294

Reaction	Present limit	Expected Limit	Experiment
$\mu^+ \rightarrow e^+\gamma$	$< 4.2 \times 10^{-13}$	5×10^{-14}	MEG II
$\mu^+ \rightarrow e^+e^-e^+$	$< 1.0 \times 10^{-12}$	10^{-16}	Mu3e
$\mu^-Al \rightarrow e^-Al^\dagger$	$< 6.1 \times 10^{-13}$	10^{-17}	Mu2e, COMET
$\mu^-Si/C \rightarrow e^-Si/C^\dagger$	—	5×10^{-14}	DeeMe

Snowmass 2021 Rare and Precision Frontier Report



Beyond Effective Field Theory

New physics exclusively at low scale?

$$\mathcal{L}(\text{SM}) \neq \mathcal{L}(\text{new fields})$$

New physics exclusively at high scale?

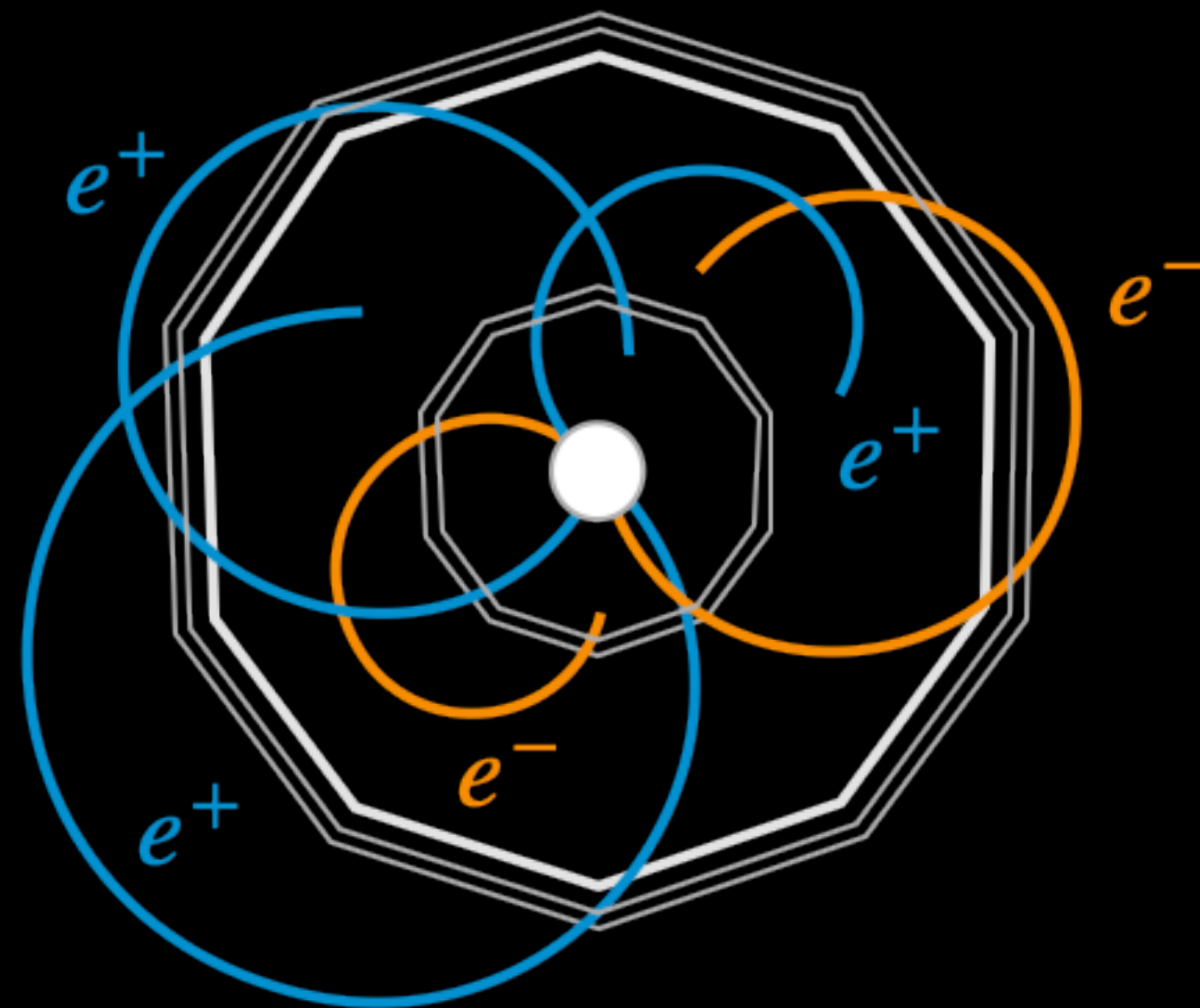
$$\mathcal{L}(\text{SM}) \neq \frac{1}{\Lambda^n} \mathcal{O}(\text{SM})^{4+n}$$

$$\mathcal{L}(\text{SM}) \neq \mathcal{L}(\text{new fields}) + \frac{1}{\Lambda^n} \mathcal{O}(\text{SM, new fields})^{4+n} + \frac{1}{\Lambda^n} \mathcal{O}(\text{SM})^{4+n}$$

E.g., axion-like-particles, $\partial_\mu a(\mu\gamma^\mu e)$, QCD Axions, Majorons, Flavons, etc

New particle production in μ^+ decays

Multi-electron final states at ~~Mu3e~~ Mu5e

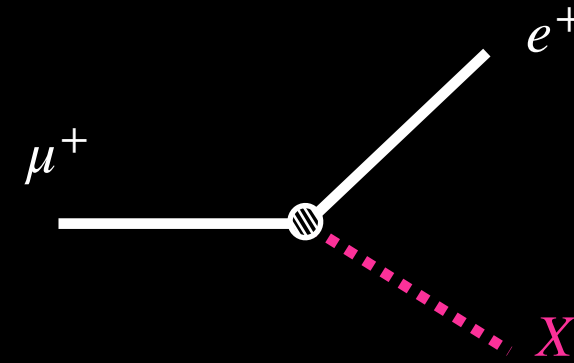


Light particle production at Mu3e

An overview



(1) $\mu^+ \rightarrow e^+ X_{\text{inv}}$ — Peak in the Michel spectrum.



Current limits: $\mathcal{B} \lesssim 10^{-5}$

Projected reach: $\mathcal{B} \lesssim 10^{-8}$

AK. Perrevoort (Ph.D. thesis), [10.11588/heidok.00024585](https://doi.org/10.11588/heidok.00024585)

L. Calibbi, D. Redigolo, R. Ziegler, J. Zupan, [10.1007/JHEP09\(2021\)173](https://doi.org/10.1007/JHEP09(2021)173)

See also $\mu^+ \rightarrow e^+ a(\gamma^* \rightarrow e^+ e^-)$ for low masses,

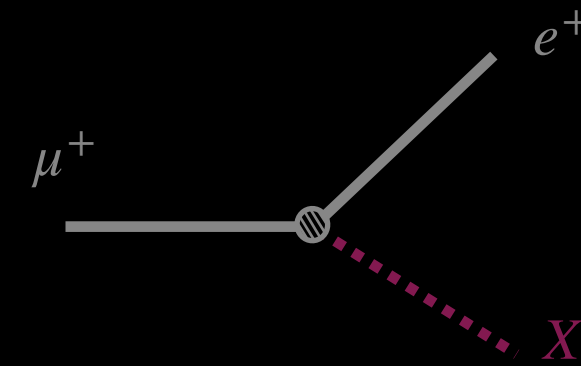
S. Knapen, T. Opferkuch, D. Redigolo, [arXiv:2311.17915](https://arxiv.org/abs/2311.17915)

Light particle production at Mu3e

An overview



(1) $\mu^+ \rightarrow e^+ X_{\text{inv}}$ — Peak in the Michel spectrum.

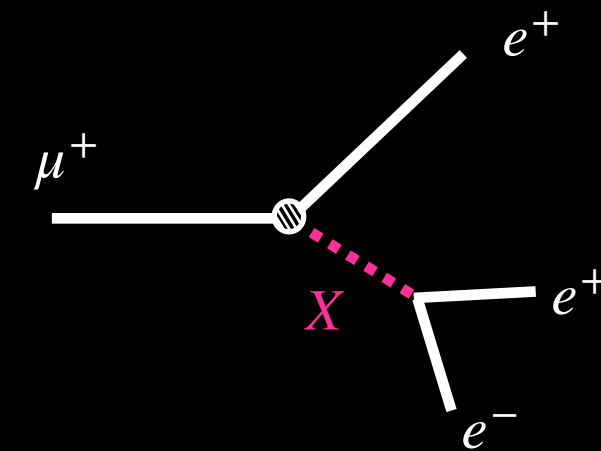


Current limits: $\mathcal{B} \lesssim 10^{-5}$
Projected reach: $\mathcal{B} \lesssim 10^{-8}$

AK. Perrevoort (Ph.D. thesis), [10.11588/heidok.00024585](https://doi.org/10.11588/heidok.00024585)
L. Calibbi, D. Redigolo, R. Ziegler, J. Zupan, [10.1007/JHEP09\(2021\)173](https://doi.org/10.1007/JHEP09(2021)173)

See also $\mu^+ \rightarrow e^+ a(\gamma^* \rightarrow e^+ e^-)$ for low masses,
S. Knapen, T. Opferkuch, D. Redigolo, [arXiv:2311.17915](https://arxiv.org/abs/2311.17915)

(2) $\mu^+ \rightarrow e^+(X \rightarrow e^+ e^-)$ — Visible resonance



Current limits: $\mathcal{B} \lesssim 3 \times 10^{-12}$
Expected reach: $\mathcal{B} \lesssim 10^{-15}$ or better

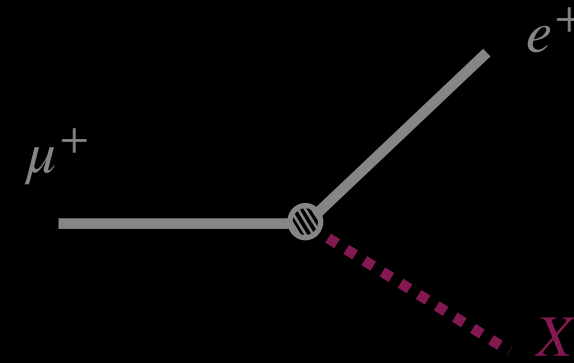
J. Heeck, W. Rodejohann, [10.1016/j.physletb.2017.11.067](https://doi.org/10.1016/j.physletb.2017.11.067)
SINDRUM-I coll., [10.1016/0370-2693\(86\)90339-4](https://doi.org/10.1016/0370-2693(86)90339-4)

Light particle production at Mu3e

An overview



(1) $\mu^+ \rightarrow e^+ X_{\text{inv}}$ — Peak in the Michel spectrum.

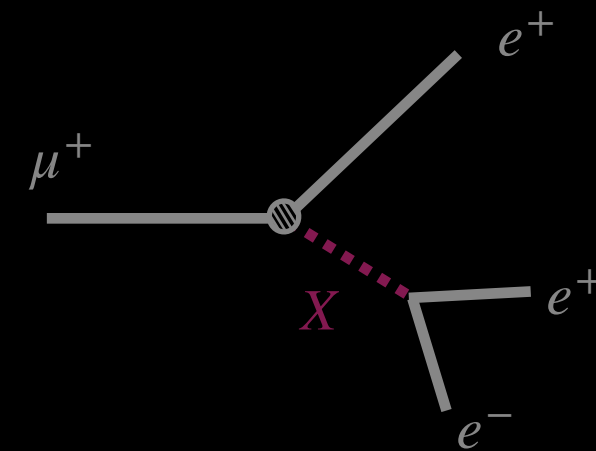


Current limits: $\mathcal{B} \lesssim 10^{-5}$
 Projected reach: $\mathcal{B} \lesssim 10^{-8}$

AK. Perrevoort (Ph.D. thesis), [10.11588/heidok.00024585](https://doi.org/10.11588/heidok.00024585)
 L. Calibbi, D. Redigolo, R. Ziegler, J. Zupan, [10.1007/JHEP09\(2021\)173](https://doi.org/10.1007/JHEP09(2021)173)

See also $\mu^+ \rightarrow e^+ a(\gamma^* \rightarrow e^+ e^-)$ for low masses,
 S. Knapen, T. Opferkuch, D. Redigolo, [arXiv:2311.17915](https://arxiv.org/abs/2311.17915)

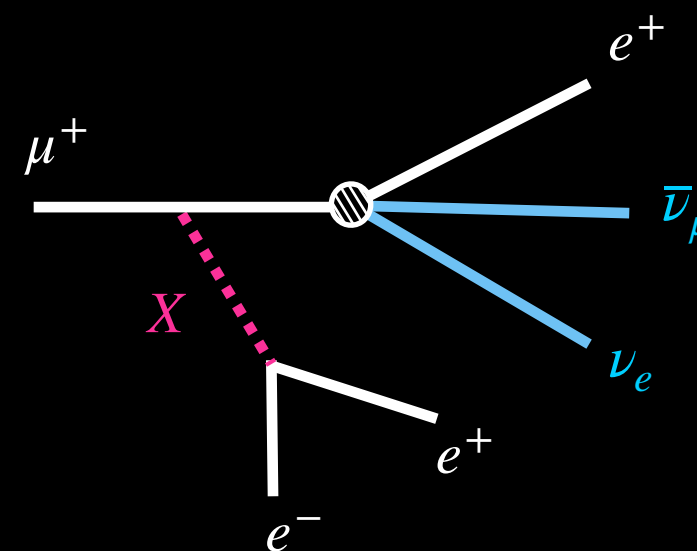
(2) $\mu^+ \rightarrow e^+(X \rightarrow e^+ e^-)$ — Visible resonance



Current limits: $\mathcal{B} \lesssim 3 \times 10^{-12}$
 Expected reach: $\mathcal{B} \lesssim 10^{-15}$ or better

J. Heeck, W. Rodejohann, [10.1016/j.physletb.2017.11.067](https://doi.org/10.1016/j.physletb.2017.11.067)
 SINDRUM-I coll., [10.1016/0370-2693\(86\)90339-4](https://doi.org/10.1016/0370-2693(86)90339-4)

(3) $\mu^+ \rightarrow e^+ \nu \nu (X \rightarrow e^+ e^-)$ — Visible resonance + missing E



Projected reach: $\mathcal{B} \lesssim 10^{-9} - 10^{-11}$.

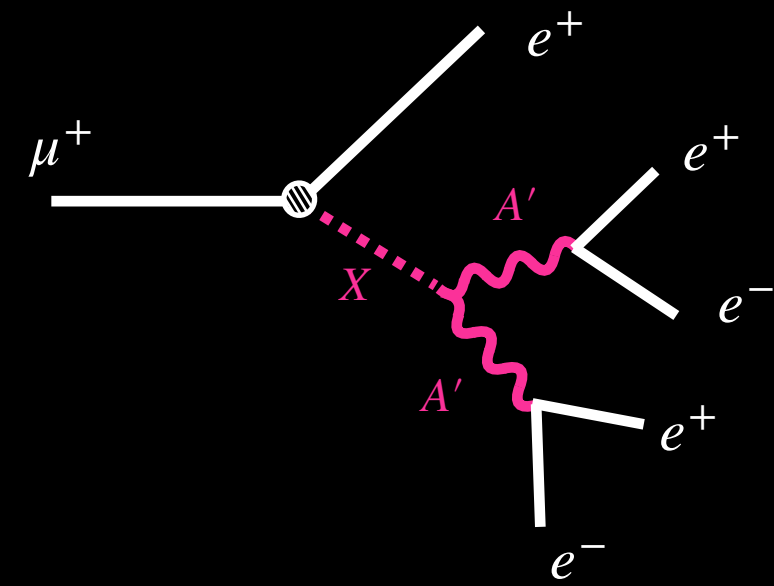
B. Echenard, R. Essig, Y.M. Zhong, [10.1007/JHEP01\(2015\)113](https://doi.org/10.1007/JHEP01(2015)113)
 AK. Perrevoort (Ph.D. thesis), [10.11588/heidok.00024585](https://doi.org/10.11588/heidok.00024585)
 S. Knapen, T. Opferkuch, D. Redigolo, [arXiv:2311.17913](https://arxiv.org/abs/2311.17913)

Light particle production at Mu3e

An overview



(4) $\mu^+ \rightarrow e^+(X \rightarrow e^+e^-e^+e^-)$ – This talk



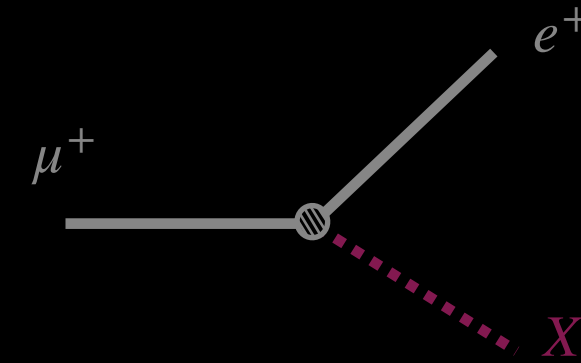
Projected reach: $\mathcal{B} \lesssim 10^{-12} - 10^{-14}$

Cascade of 2-body decays.

Also, the first study of SM five-track rate.

MH, T. Menzo, M. Pospelov, J. Zupan, [10.1007/JHEP10\(2023\)006](https://arxiv.org/abs/10.1007/JHEP10(2023)006)

(1) $\mu^+ \rightarrow e^+X_{\text{inv}}$ – Peak in the Michel spectrum.



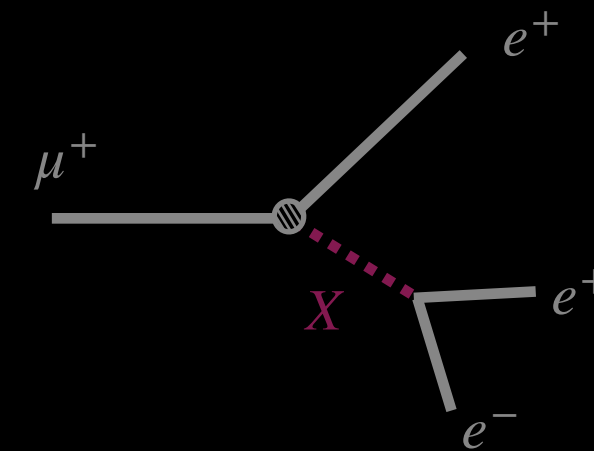
Current limits: $\mathcal{B} \lesssim 10^{-5}$

Projected reach: $\mathcal{B} \lesssim 10^{-8}$

AK. Perrevoort (Ph.D. thesis), [10.11588/heidok.00024585](https://arxiv.org/abs/10.11588/heidok.00024585)
L. Calibbi, D. Redigolo, R. Ziegler, J. Zupan, [10.1007/JHEP09\(2021\)173](https://arxiv.org/abs/10.1007/JHEP09(2021)173)

See also $\mu^+ \rightarrow e^+a(\gamma^* \rightarrow e^+e^-)$ for low masses,
S. Knapen, T. Opferkuch, D. Redigolo, [arXiv:2311.17915](https://arxiv.org/abs/2311.17915)

(2) $\mu^+ \rightarrow e^+(X \rightarrow e^+e^-)$ – Visible resonance

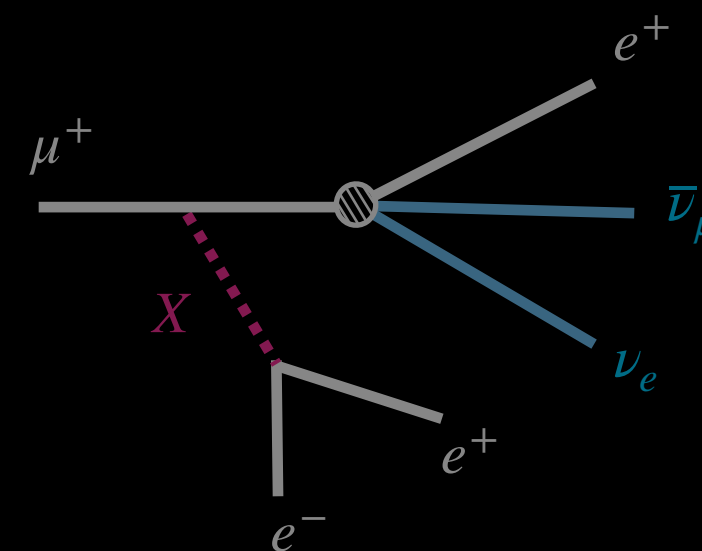


Current limits: $\mathcal{B} \lesssim 3 \times 10^{-12}$

Expected reach: $\mathcal{B} \lesssim 10^{-15}$ or better

J. Heeck, W. Rodejohann, [10.1016/j.physletb.2017.11.067](https://arxiv.org/abs/10.1016/j.physletb.2017.11.067)
SINDRUM-I coll., [10.1016/0370-2693\(86\)90339-4](https://arxiv.org/abs/10.1016/0370-2693(86)90339-4)

(3) $\mu^+ \rightarrow e^+\nu\nu(X \rightarrow e^+e^-)$ – Visible resonance + missing E



Projected reach: $\mathcal{B} \lesssim 10^{-9} - 10^{-11}$.

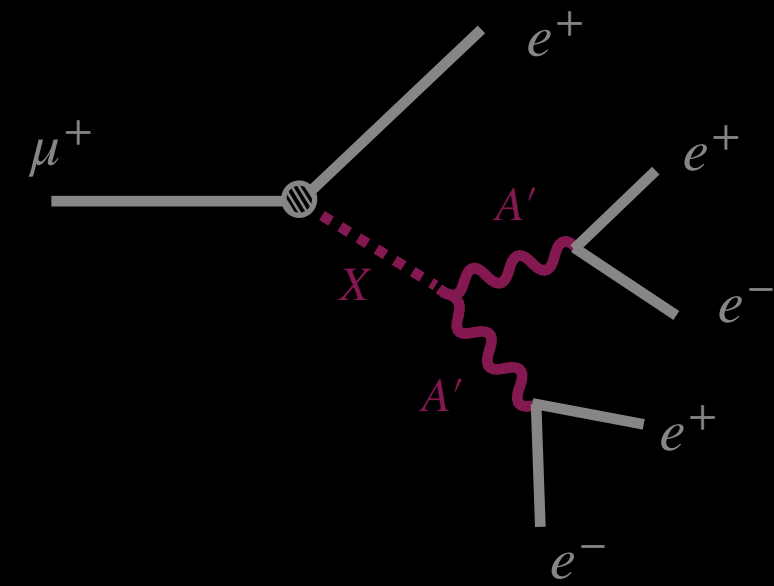
B. Echenard, R. Essig, Y.M. Zhong, [10.1007/JHEP01\(2015\)113](https://arxiv.org/abs/10.1007/JHEP01(2015)113)
AK. Perrevoort (Ph.D. thesis), [10.11588/heidok.00024585](https://arxiv.org/abs/10.11588/heidok.00024585)
S. Knapen, T. Opferkuch, D. Redigolo, [arXiv:2311.17913](https://arxiv.org/abs/2311.17913)

Light particle production at Mu3e

An overview



(4) $\mu^+ \rightarrow e^+(X \rightarrow e^+e^-e^+e^-)$ – This talk



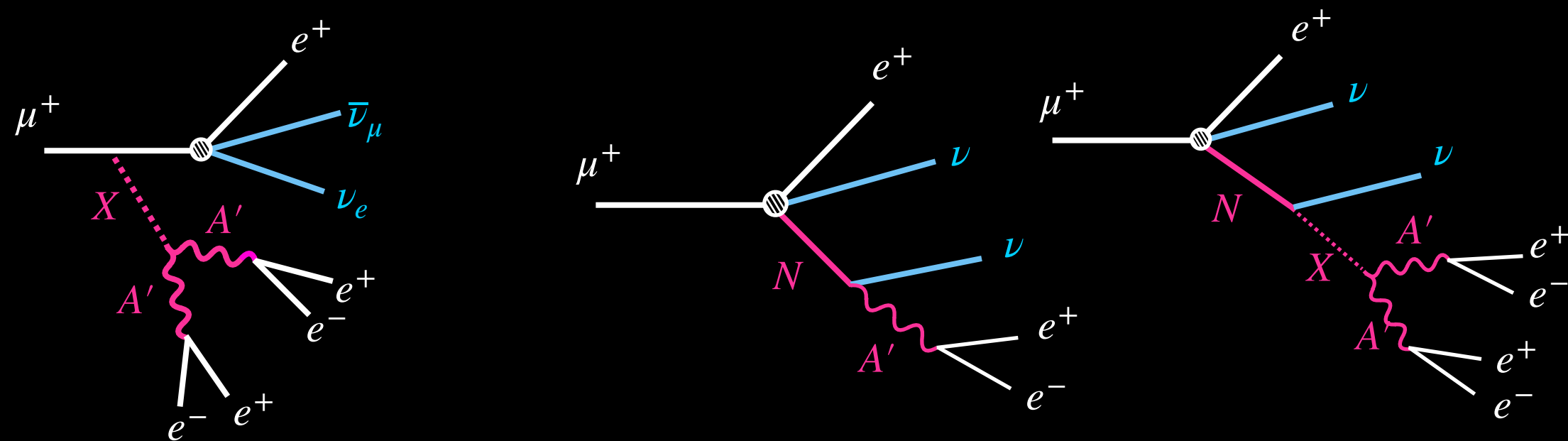
Projected reach: $\mathcal{B} \lesssim 10^{-12} - 10^{-14}$

Cascade of 2-body decays.

Also, the first study of SM five-track rate.

MH, T. Menzo, M. Pospelov, J. Zupan, [10.1007/JHEP10\(2023\)006](https://arxiv.org/abs/10.1007/JHEP10(2023)006)

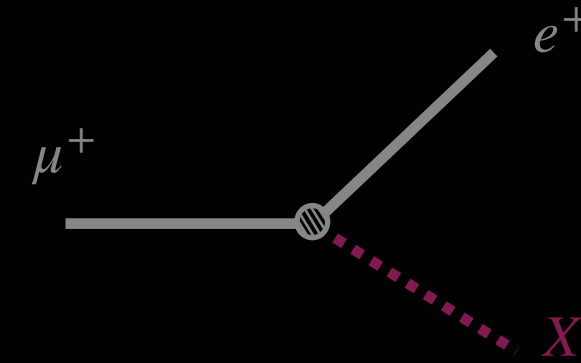
(5) Other modes (not studied)



Flavor-preserving version of (4).

Neutrino portal to (3) and (4). Sensitive to mixing of the heavy “dark” neutrino N to electron and muon.

(1) $\mu^+ \rightarrow e^+X_{\text{inv}}$ – Peak in the Michel spectrum.



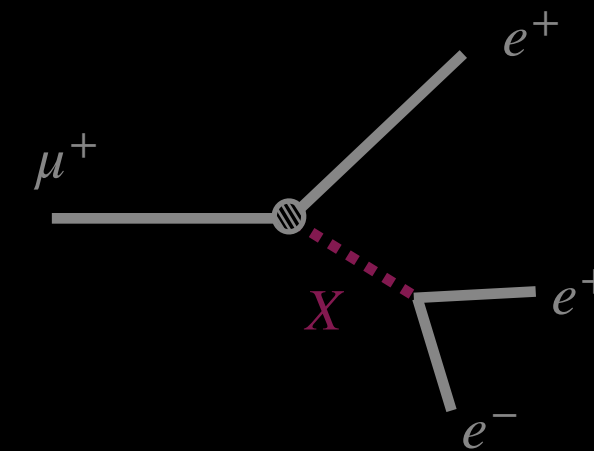
Current limits: $\mathcal{B} \lesssim 10^{-5}$

Projected reach: $\mathcal{B} \lesssim 10^{-8}$

AK. Perrevoort (Ph.D. thesis), [10.11588/heidok.00024585](https://arxiv.org/abs/10.11588/heidok.00024585)
L. Calibbi, D. Redigolo, R. Ziegler, J. Zupan, [10.1007/JHEP09\(2021\)173](https://arxiv.org/abs/10.1007/JHEP09(2021)173)

See also $\mu^+ \rightarrow e^+a(\gamma^* \rightarrow e^+e^-)$ for low masses,
S. Knapen, T. Opferkuch, D. Redigolo, [arXiv:2311.17915](https://arxiv.org/abs/2311.17915)

(2) $\mu^+ \rightarrow e^+(X \rightarrow e^+e^-)$ – Visible resonance

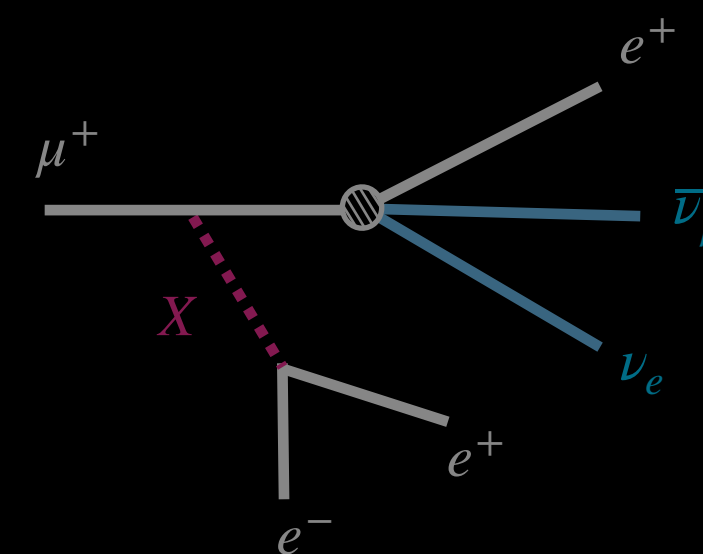


Current limits: $\mathcal{B} \lesssim 3 \times 10^{-12}$

Expected reach: $\mathcal{B} \lesssim 10^{-15}$ or better

J. Heeck, W. Rodejohann, [10.1016/j.physletb.2017.11.067](https://arxiv.org/abs/10.1016/j.physletb.2017.11.067)
SINDRUM-I coll., [10.1016/0370-2693\(86\)90339-4](https://arxiv.org/abs/10.1016/0370-2693(86)90339-4)

(3) $\mu^+ \rightarrow e^+\nu\nu(X \rightarrow e^+e^-)$ – Visible resonance + missing E



Projected reach: $\mathcal{B} \lesssim 10^{-9} - 10^{-11}$.

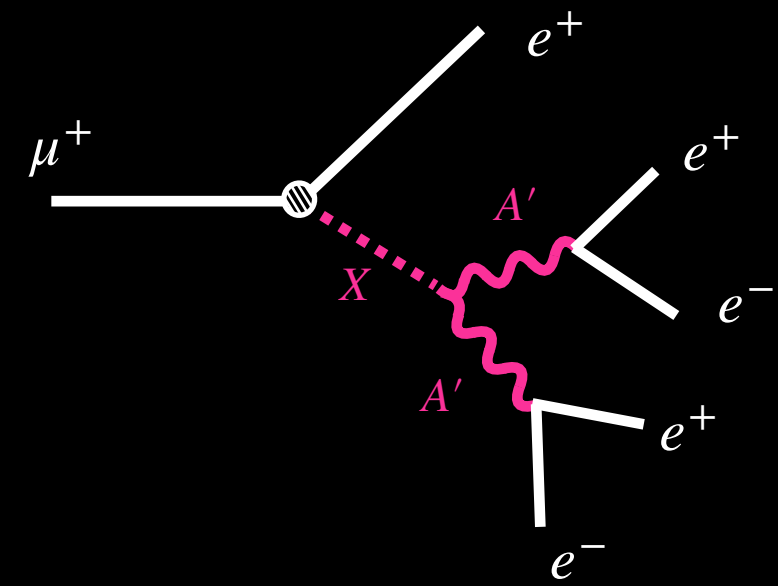
B. Echenard, R. Essig, Y.M. Zhong, [10.1007/JHEP01\(2015\)113](https://arxiv.org/abs/10.1007/JHEP01(2015)113)
AK. Perrevoort (Ph.D. thesis), [10.11588/heidok.00024585](https://arxiv.org/abs/10.11588/heidok.00024585)
S. Knapen, T. Opferkuch, D. Redigolo, [arXiv:2311.17913](https://arxiv.org/abs/2311.17913)

Light particle production at Mu3e

An overview



(4) $\mu^+ \rightarrow e^+(X \rightarrow e^+e^-e^+e^-)$ — Two visible resonances



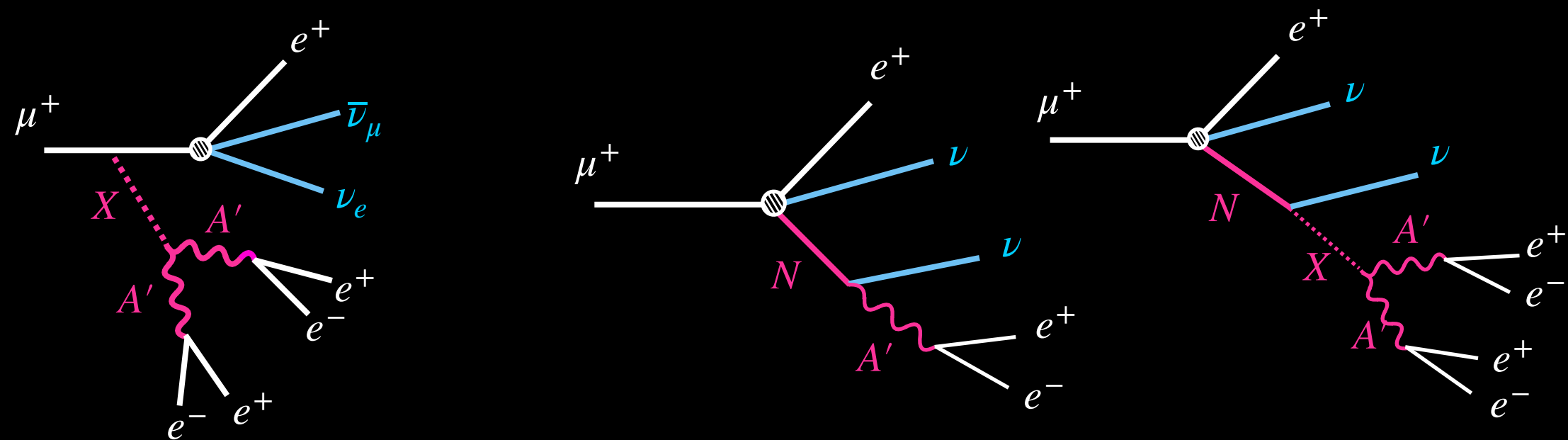
Projected reach: $\mathcal{B} \lesssim 10^{-12} - 10^{-14}$

Cascade of 2-body decays.

Also, the first study of SM five-track rate.

MH, T. Menzo, M. Pospelov, J. Zupan, [10.1007/JHEP10\(2023\)006](https://arxiv.org/abs/10.1007/JHEP10(2023)006)

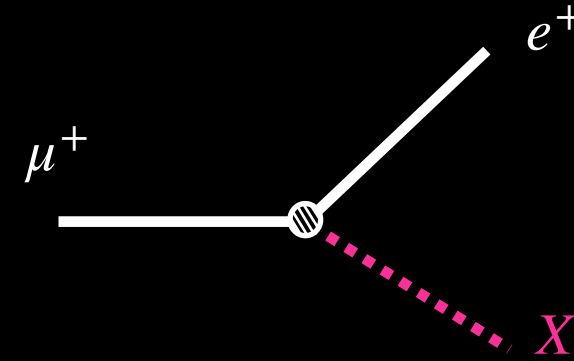
(5) Other modes (not studied)



Flavor-preserving version of (4).

Neutrino portal to (3) and (4). Sensitive to mixing of the heavy “dark” neutrino N to electron and muon.

(1) $\mu^+ \rightarrow e^+X_{\text{inv}}$ — Peak in the Michel spectrum.



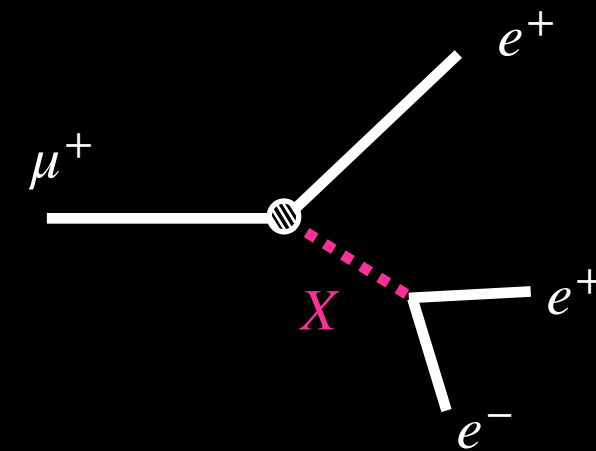
Current limits: $\mathcal{B} \lesssim 10^{-5}$

Projected reach: $\mathcal{B} \lesssim 10^{-8}$

AK. Perrevoort (Ph.D. thesis), [10.11588/heidok.00024585](https://arxiv.org/abs/10.11588/heidok.00024585)
L. Calibbi, D. Redigolo, R. Ziegler, J. Zupan, [10.1007/JHEP09\(2021\)173](https://arxiv.org/abs/10.1007/JHEP09(2021)173)

See also $\mu^+ \rightarrow e^+a(\gamma^* \rightarrow e^+e^-)$ for low masses,
S. Knapen, T. Opferkuch, D. Redigolo, [arXiv:2311.17915](https://arxiv.org/abs/2311.17915)

(2) $\mu^+ \rightarrow e^+(X \rightarrow e^+e^-)$ — Visible resonance

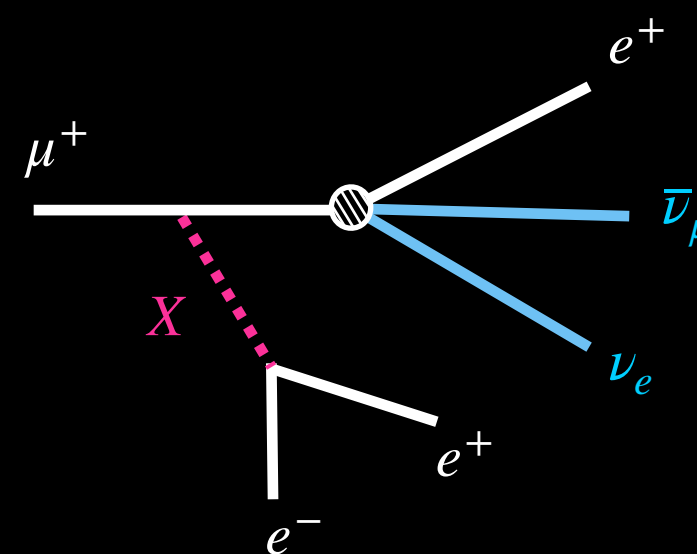


Current limits: $\mathcal{B} \lesssim 3 \times 10^{-12}$

Expected reach: $\mathcal{B} \lesssim 10^{-15}$ or better

J. Heeck, W. Rodejohann, [10.1016/j.physletb.2017.11.067](https://arxiv.org/abs/10.1016/j.physletb.2017.11.067)
SINDRUM-I coll., [10.1016/0370-2693\(86\)90339-4](https://arxiv.org/abs/10.1016/0370-2693(86)90339-4)

(3) $\mu^+ \rightarrow e^+\nu\nu(X \rightarrow e^+e^-)$ — Visible resonance + missing E



Projected reach: $\mathcal{B} \lesssim 10^{-9} - 10^{-11}$.

B. Echenard, R. Essig, Y.M. Zhong, [10.1007/JHEP01\(2015\)113](https://arxiv.org/abs/10.1007/JHEP01(2015)113)
AK. Perrevoort (Ph.D. thesis), [10.11588/heidok.00024585](https://arxiv.org/abs/10.11588/heidok.00024585)
S. Knapen, T. Opferkuch, D. Redigolo, [arXiv:2311.17913](https://arxiv.org/abs/2311.17913)

Rare muon decays at Mu3e

Higgsed $U(1)_d$ — more is different

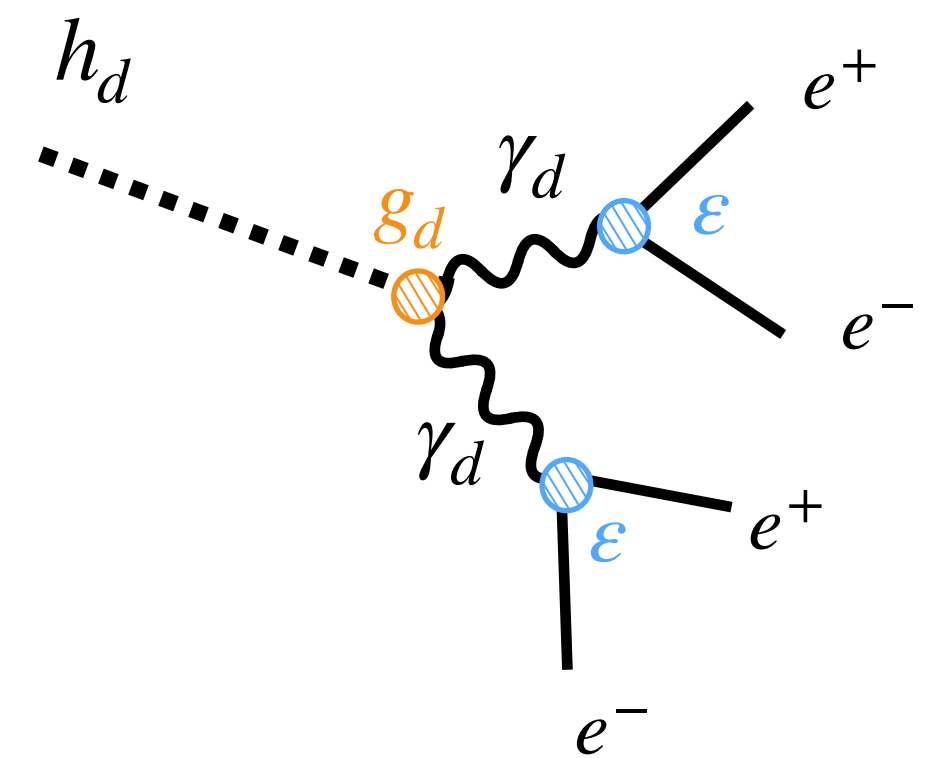
MH, T. Menzo, M. Pospelov, J. Zupan, [JHEP 10 \(2023\) 006](#)

Higgsed dark $U(1)_d$: dark photon (γ_d) gets a mass from the dark Higgs (h_d), and kinetically mixes with hypercharge:

$$\mathcal{L}_{\text{Kin}} \supset -\frac{\varepsilon}{2c_W} F_{\mu\nu}^d B^{\mu\nu}$$

If $m_{h_d} > 2m_{\gamma_d} > 4m_e$, dark Higgs decays to four leptons in cascades of 2-body decays.

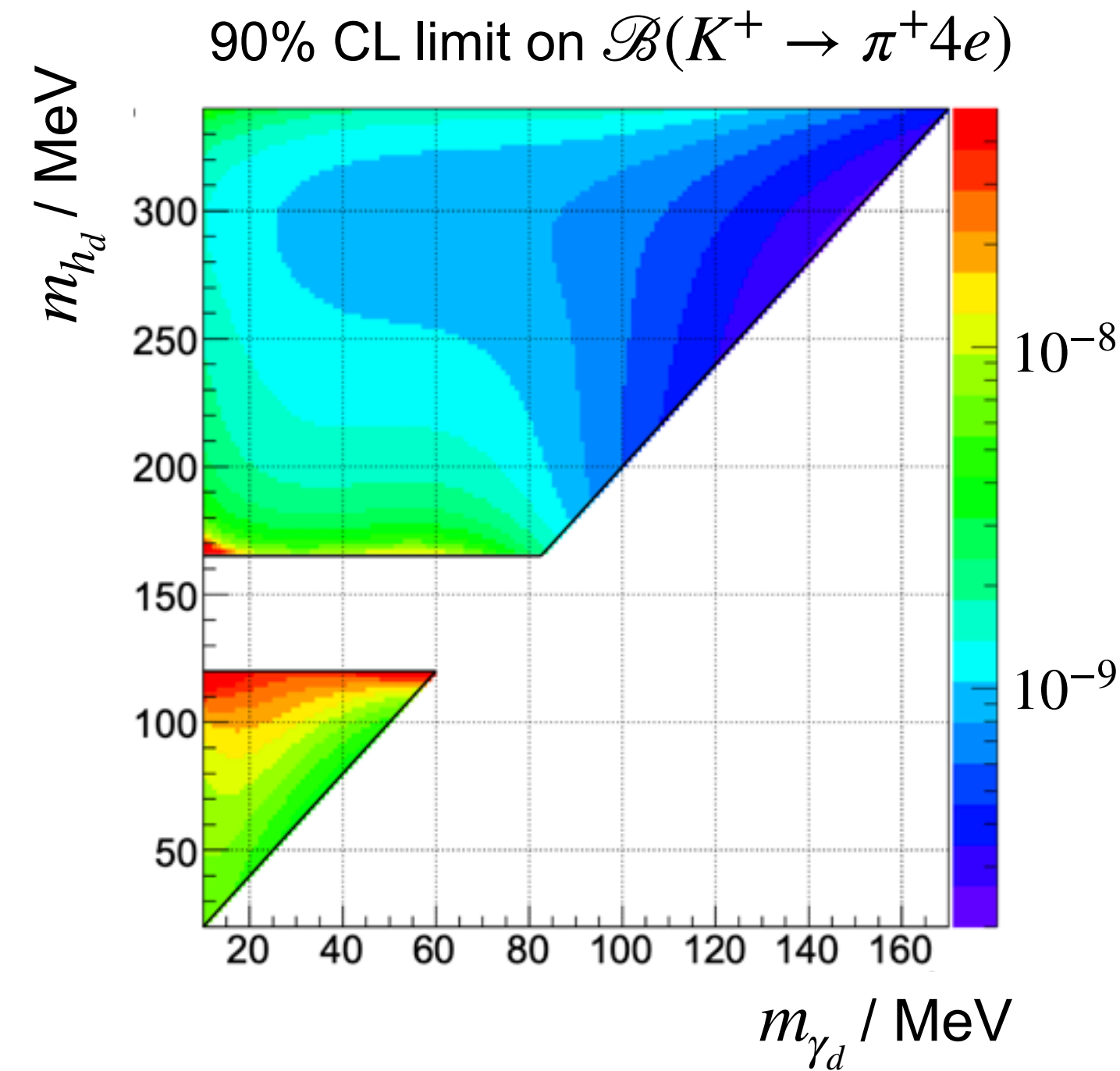
Simple and well-motivated model — multiplication of leptons comes “for free.”



Rare muon decays at Mu3e

Higgsed $U(1)_d$ — more is different

MH, T. Menzo, M. Pospelov, J. Zupan, [JHEP 10 \(2023\) 006](#)



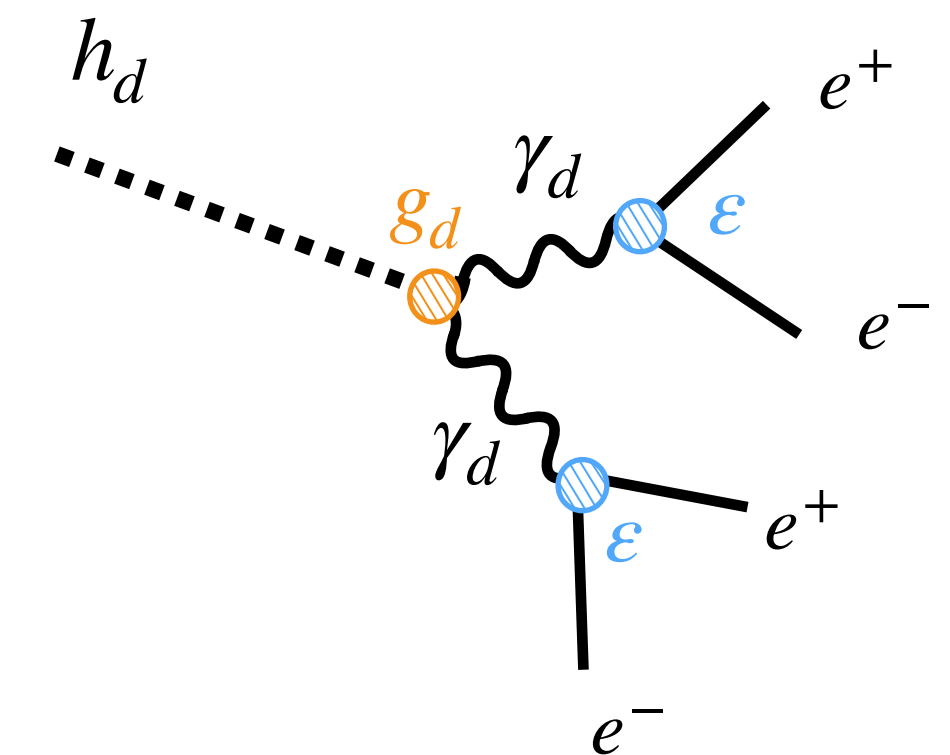
Higgsed dark $U(1)_d$: dark photon (γ_d) gets a mass from the dark Higgs (h_d), and kinetically mixes with hypercharge:

$$\mathcal{L}_{\text{Kin}} \supset -\frac{\varepsilon}{2c_W} F_{\mu\nu}^d B^{\mu\nu}$$

If $m_{h_d} > 2m_{\gamma_d} > 4m_e$, dark Higgs decays to four leptons in cascades of 2-body decays.

Simple and well-motivated model — multiplication of leptons comes “for free.”

Searches at kaon, e+e- colliders, and LHC target the coupling of h_d with the Higgs and ε , which can be small.



Recently targeted by a new five-track search at NA62.

$$K^+ \rightarrow \pi^+(h_d \rightarrow \gamma_d \gamma_d \rightarrow 2(e^+ e^-))$$

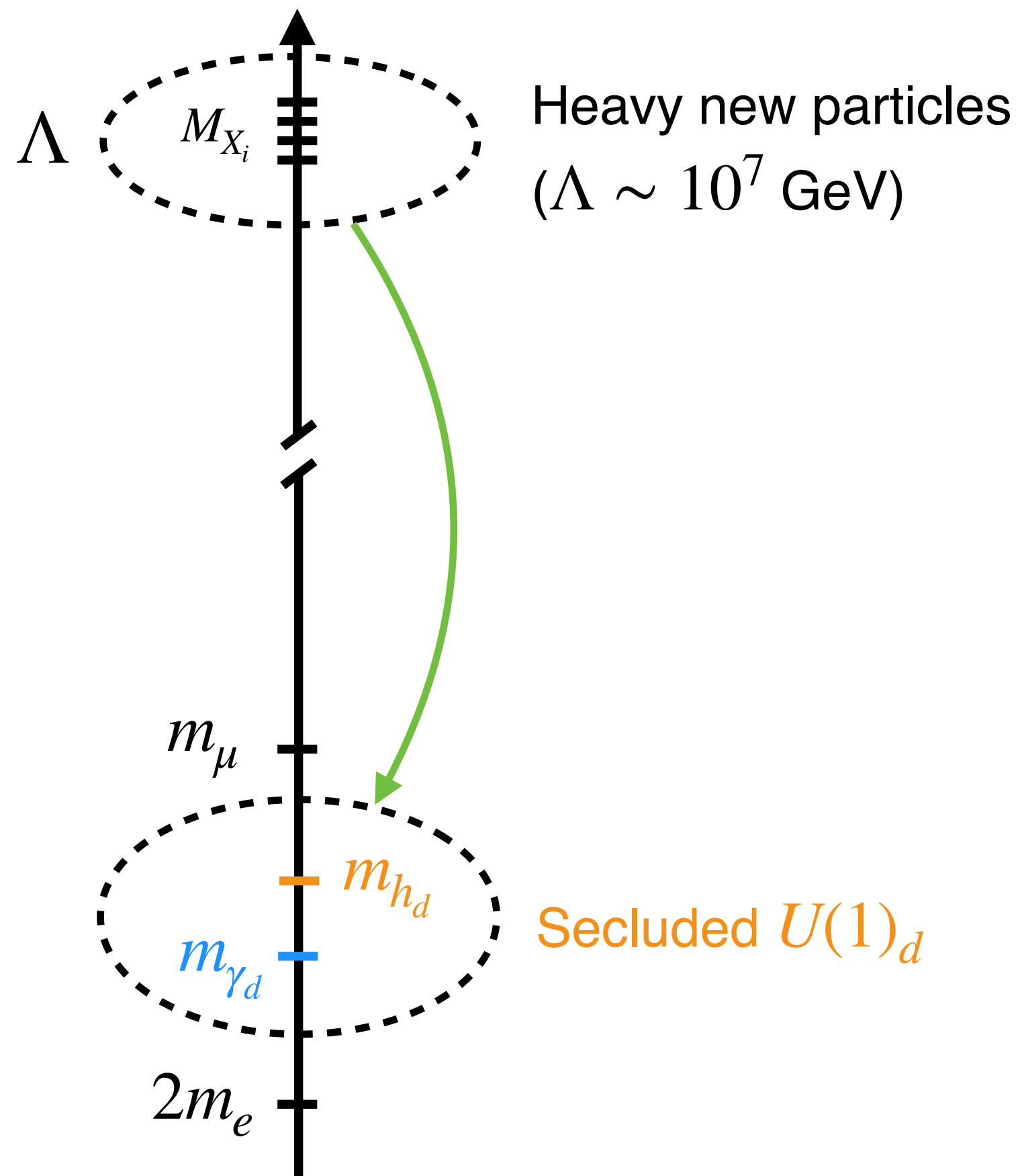
MH, M. Pospelov, [10.1103/PhysRevD.105.015017](#)

NA62 coll., [10.1016/j.physletb.2023.138193](#)

Consider now new operators with cLFV couplings to leptons.

Rare muon decays at Mu3e

Higgsed $U(1)_d$



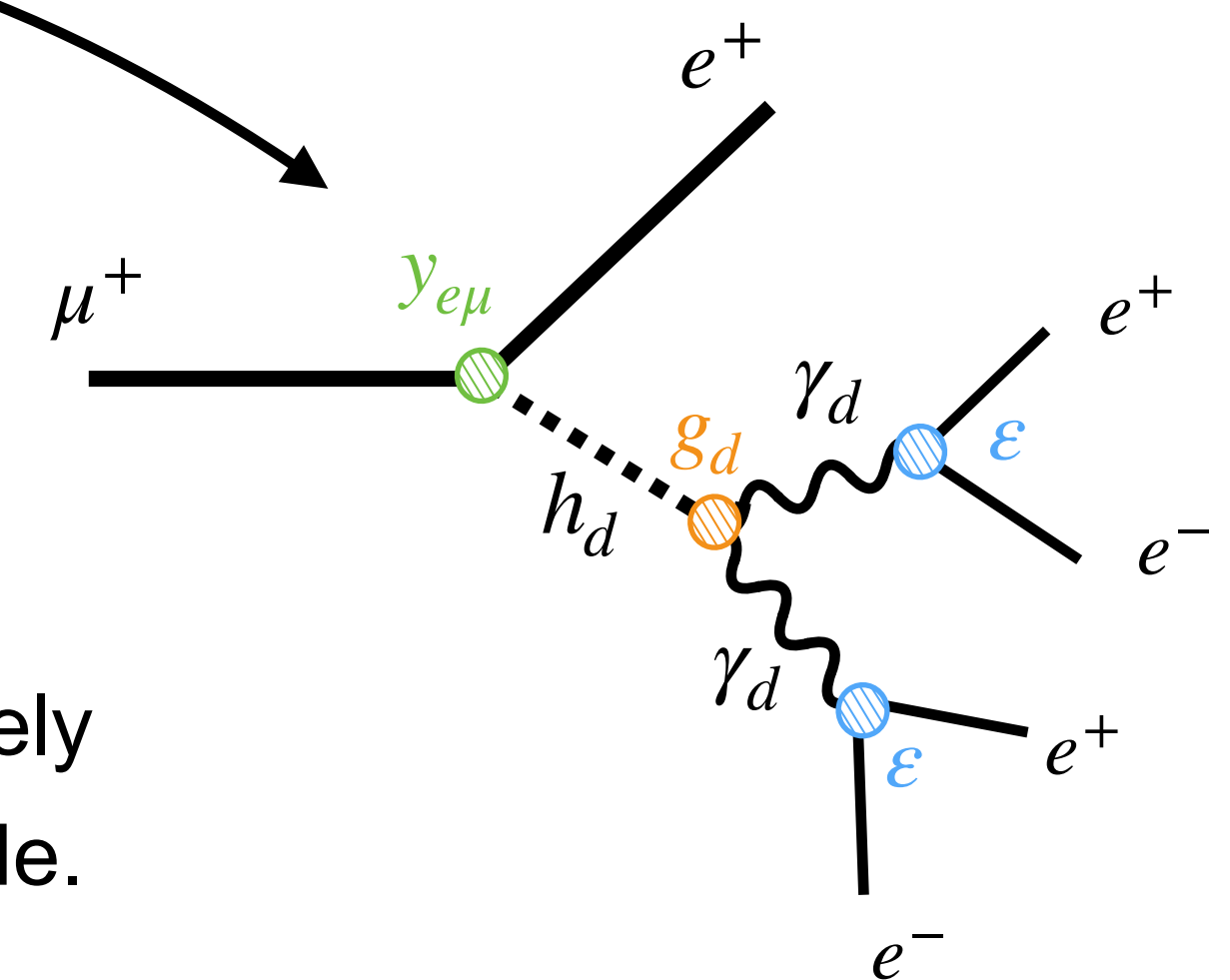
Lowest-dimension operators in the " h_d - EFT" that violate flavor:

$$\mathcal{L}_{\text{cLFV}} \supset \frac{|h_d|^2}{\Lambda^2} \left(Y_{e\mu} \bar{L}_\mu H e_R + Y_{\mu e} \bar{L}_e H \mu_R \right) \xrightarrow[\cancel{U(1)_d}]{\text{EW}} h_d \left(y_{e\mu} \bar{\mu}_L e_R + y_{\mu e} \bar{e}_L \mu_R \right), \quad y_{e\mu} = \frac{Y_{e\mu} v_{\text{EW}} v_d}{\sqrt{2} \Lambda^2}$$

In mass basis, SM Higgs continues to have diagonal couplings, but **dark Higgs** does not.

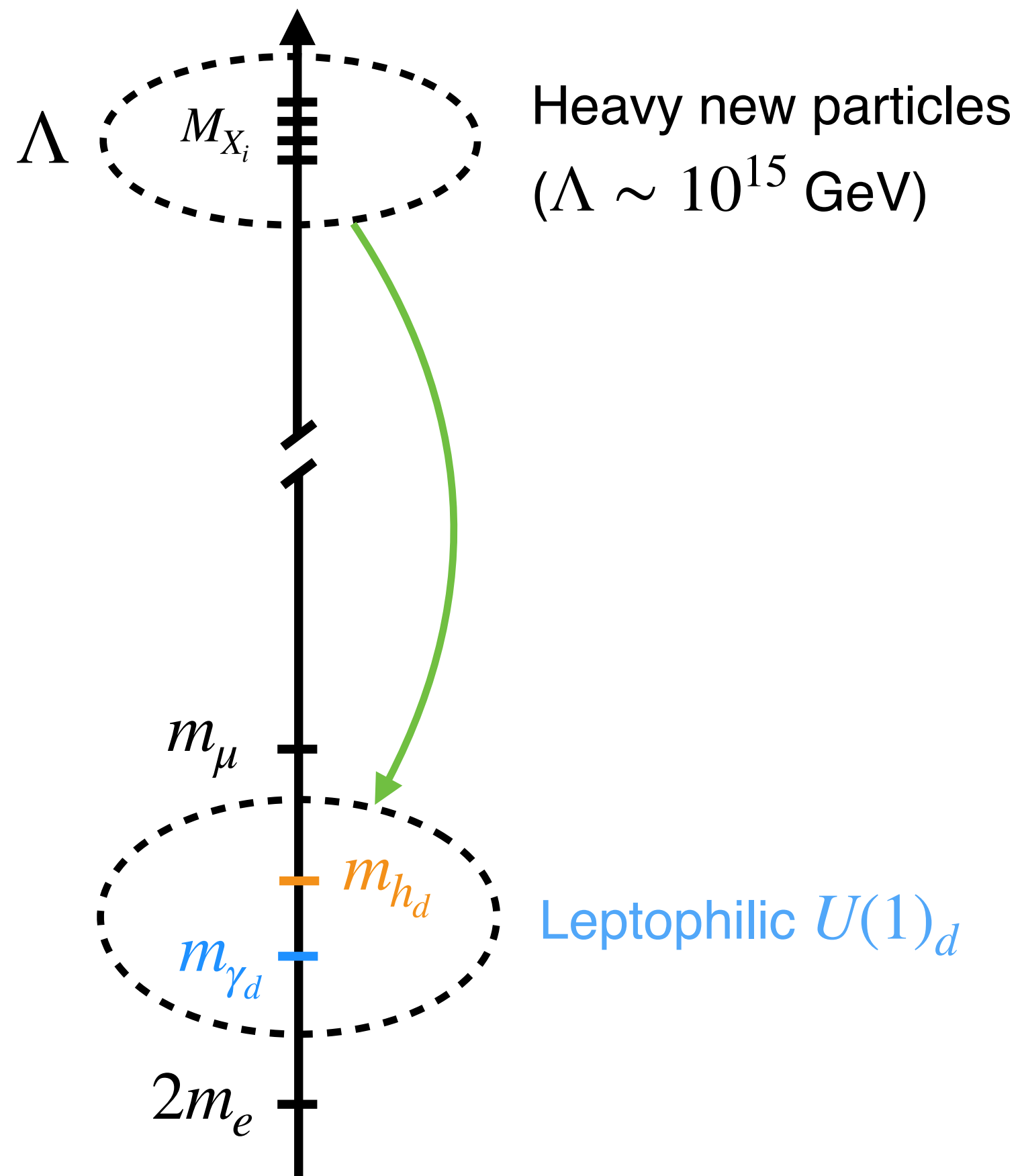
If $m_\mu - m_e > m_{h_d} > 2m_{\gamma_d} > 4m_e$:

Muon decays via a 2-body process $\mu^+ \rightarrow e h_d$, ultimately leading to a total of five tracks at the end of the cascade.



Rare muon decays at Mu3e

Higgsed $U(1)_d$



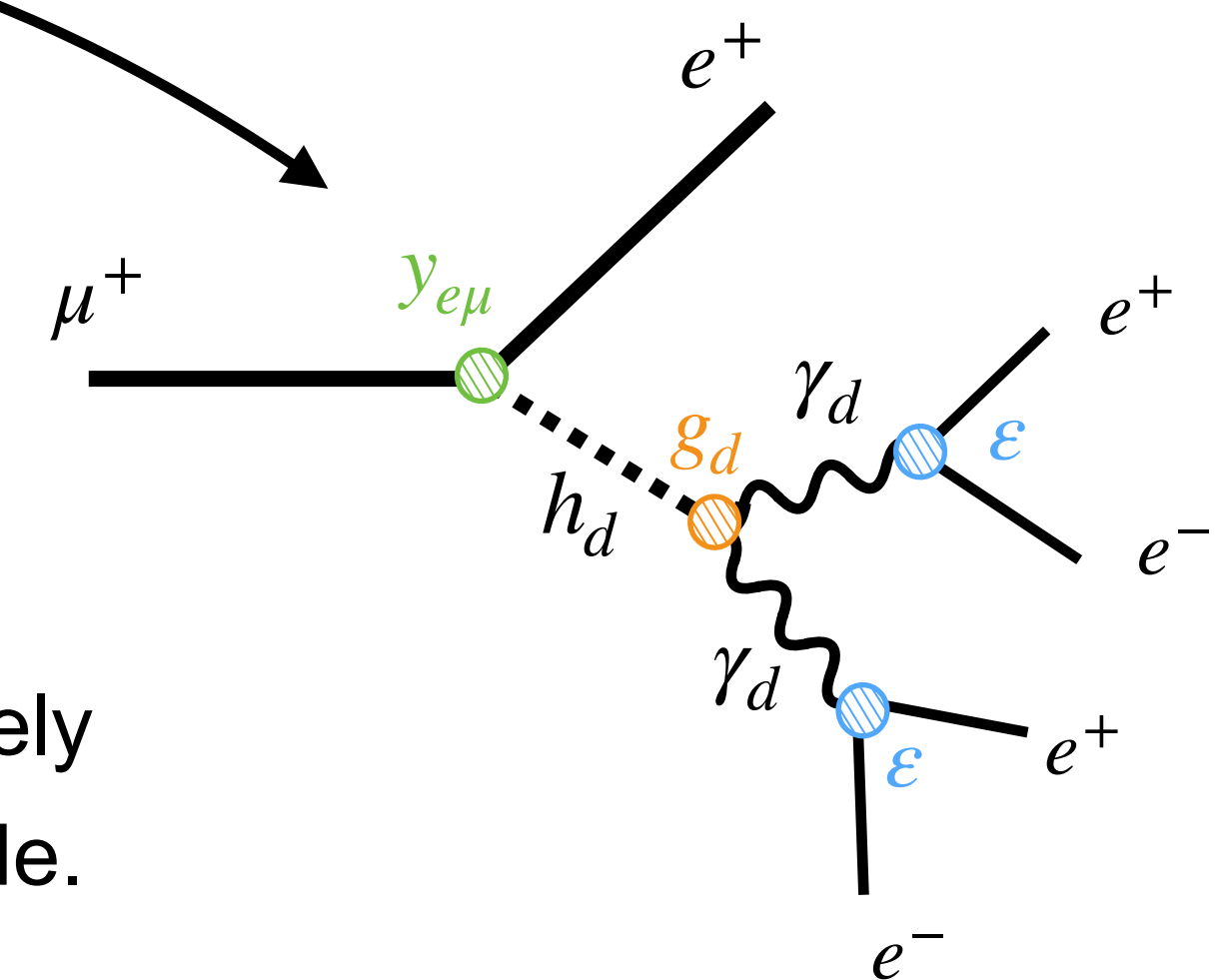
Lowest-dimension operators in the “ h_d - EFT” that violate flavor*:

$$\mathcal{L}_{\text{cLFV}} \supset \frac{h_d}{\Lambda} \left(Y_{e\mu} \bar{L}_\mu H e_R + Y_{\mu e} \bar{L}_e H \mu_R \right) \xrightarrow[\cancel{U(1)_d}]{\text{EW}} h_d \left(y_{e\mu} \bar{\mu}_L e_R + y_{\mu e} \bar{e}_L \mu_R \right), \quad y_{e\mu} = \frac{Y_{e\mu} v_{\text{EW}}}{\sqrt{2}\Lambda}$$

In mass basis, SM Higgs continues to have diagonal couplings, but **dark Higgs** does not.

If $m_\mu - m_e > m_{h_d} > 2m_{\gamma_d} > 4m_e$:

Muon decays via a 2-body process $\mu^+ \rightarrow e h_d$, ultimately leading to a total of five tracks at the end of the cascade.



Rare muon decays at Mu3e

Mu3e at PSI

Aiming for $\mathcal{B}(\mu^+ \rightarrow e^+e^+e^-) < 10^{-16}$

(4 orders of magnitude improvement on current limits).

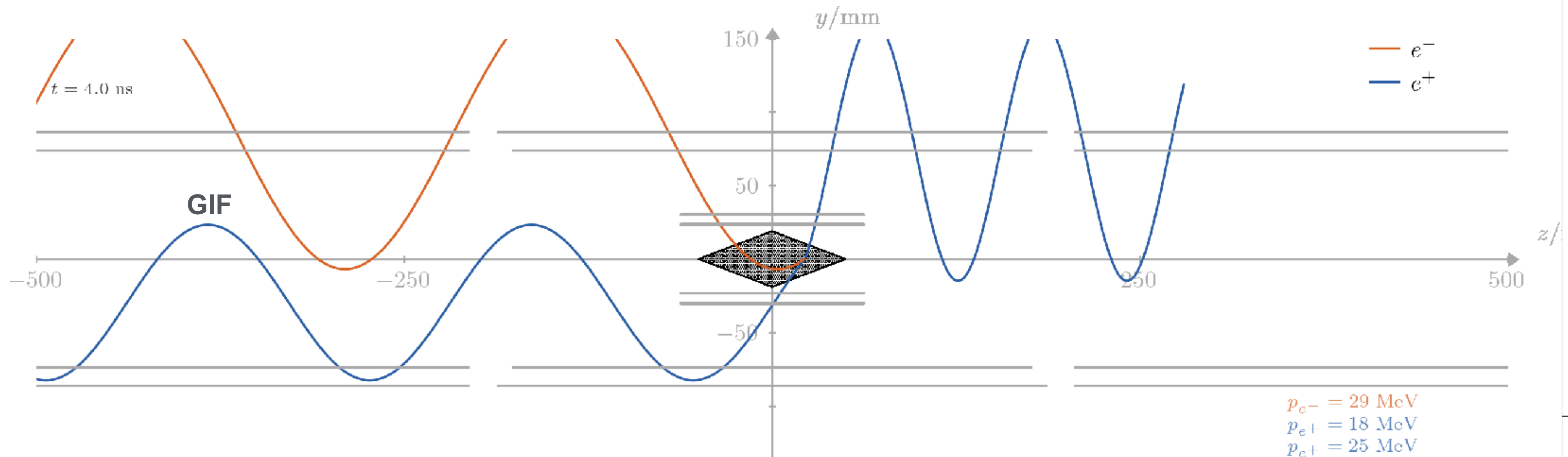
Phase-I: $\gtrsim 2 \times 10^{15} \mu^+$ decays

Phase-II: $\gtrsim 5 \times 10^{16} \mu^+$ decays



- 1) About 10^8 muons/s from 2.4 mA proton beam,
- 2) Low pion contamination, $< 2 \times 10^{-7}$ fraction,
- 3) Each layer has about $\sim 0.1\%$ radiation length.
- 4) $B = 1$ T magnetic field

30 MeV e^+/e^- deflected by about 2°
in 1 % of radiation length due to multiple scattering.



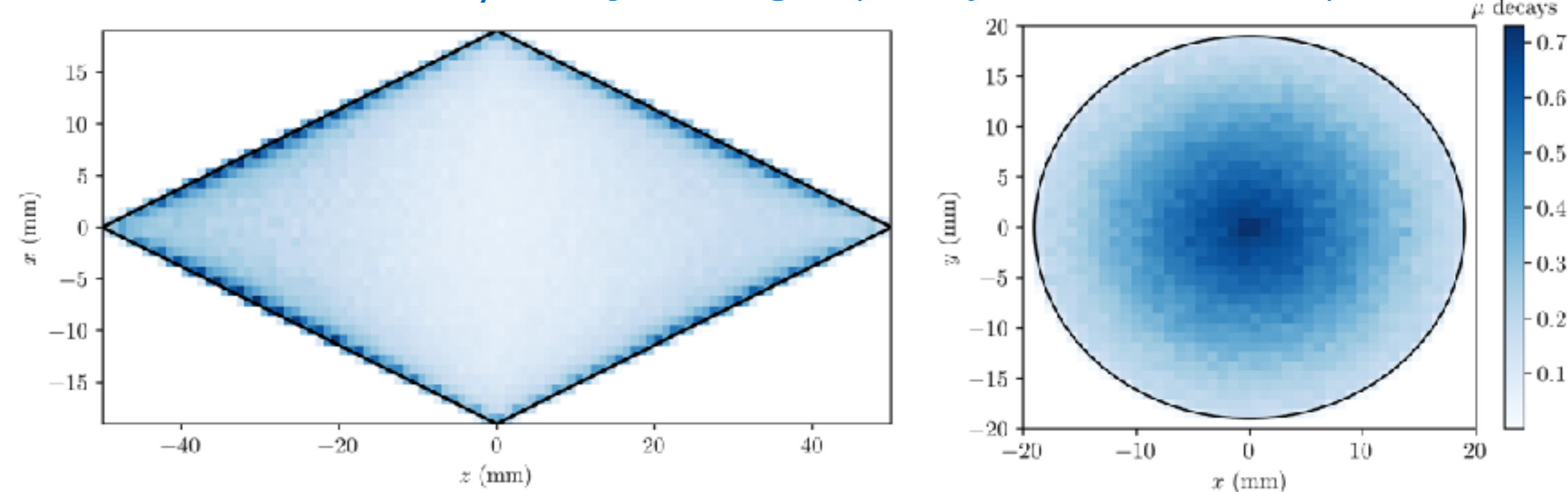
Rare muon decays at Mu3e

A theorist's fast MC for the detector

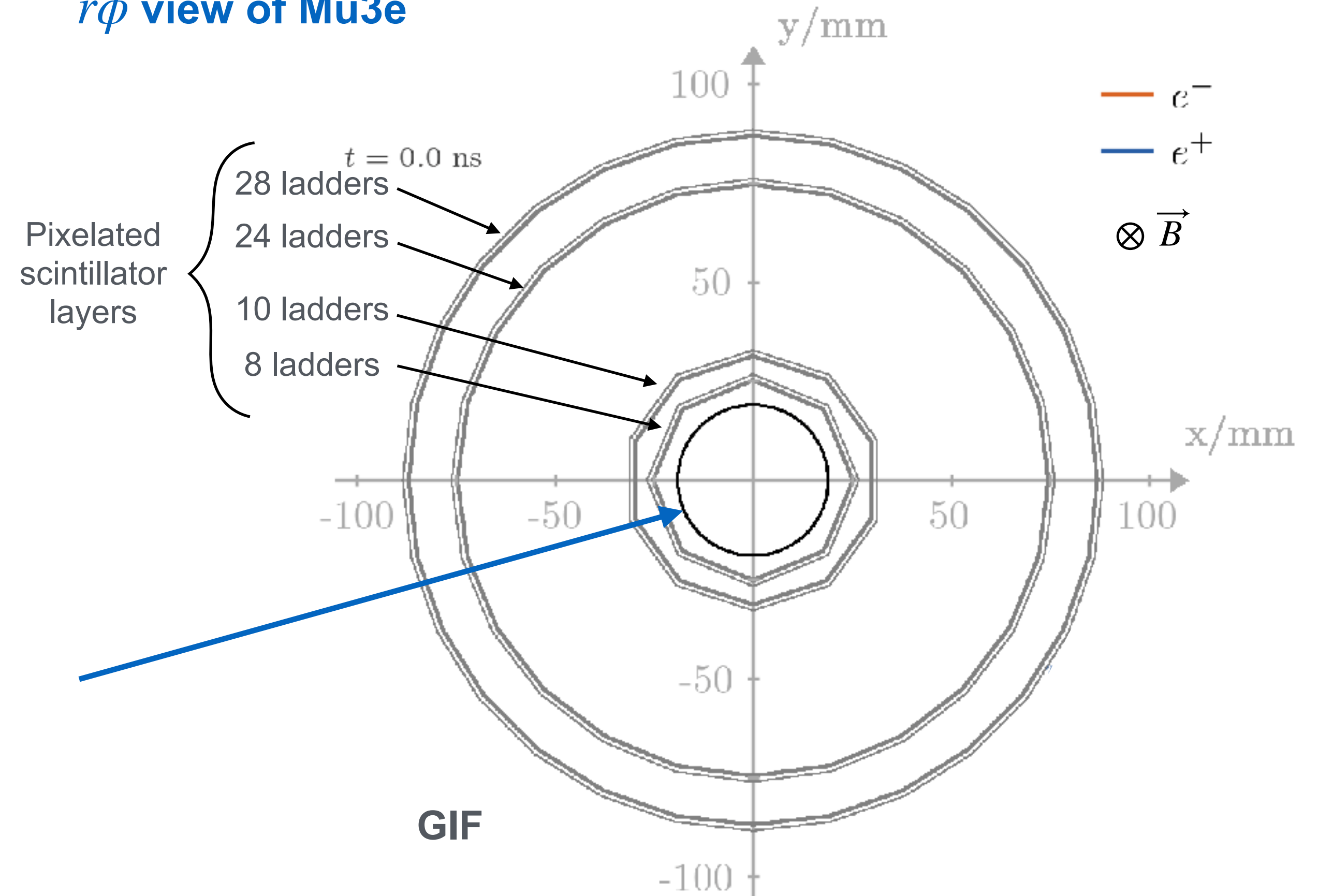
MH, T. Menzo, M. Pospelov, J. Zupan, *JHEP* 10 (2023) 006

- 1) Generating muon decays with MadGraph5 v3.5.0 and Scikit-HEP phase-space package (unpolarized μ).
- 2) Place muons on surface of Mylar target.*
- 3) Draw helical trajectories with $B = 1$ T, smearing $|p_e|$ with energy-dependent Gaussians.*
- 4) Signal selection based on # of hits on scintillator layers.

70 μm Mylar target (decays on the surface)



$r\phi$ view of Mu3e



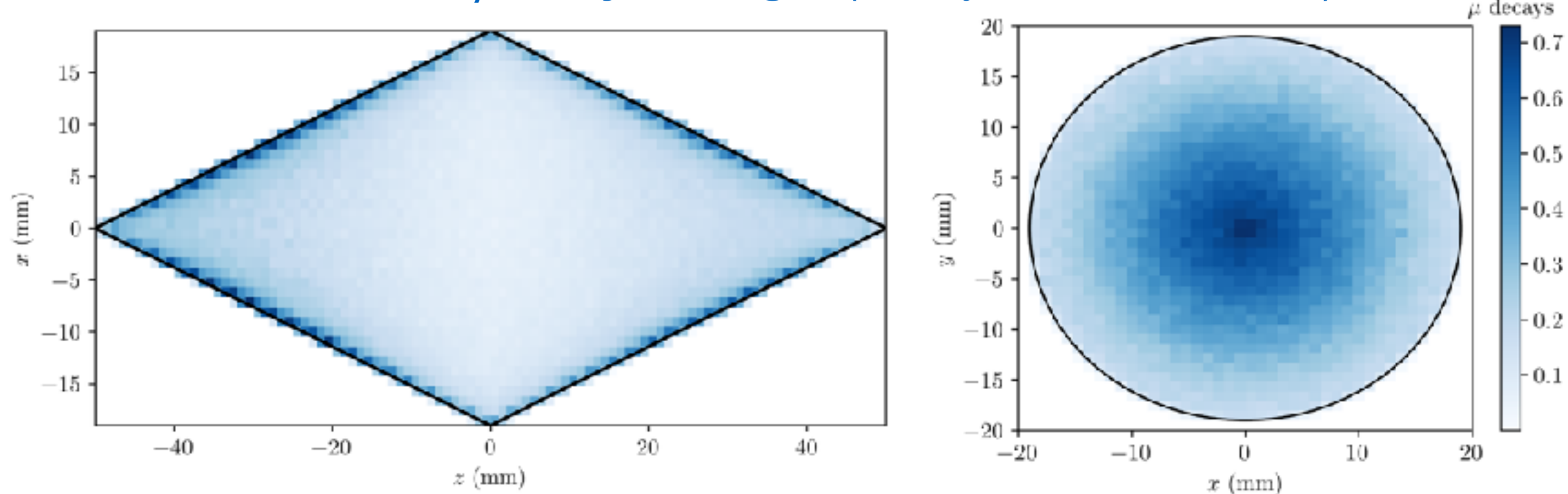
Rare muon decays at Mu3e

A theorist's fast MC for the detector

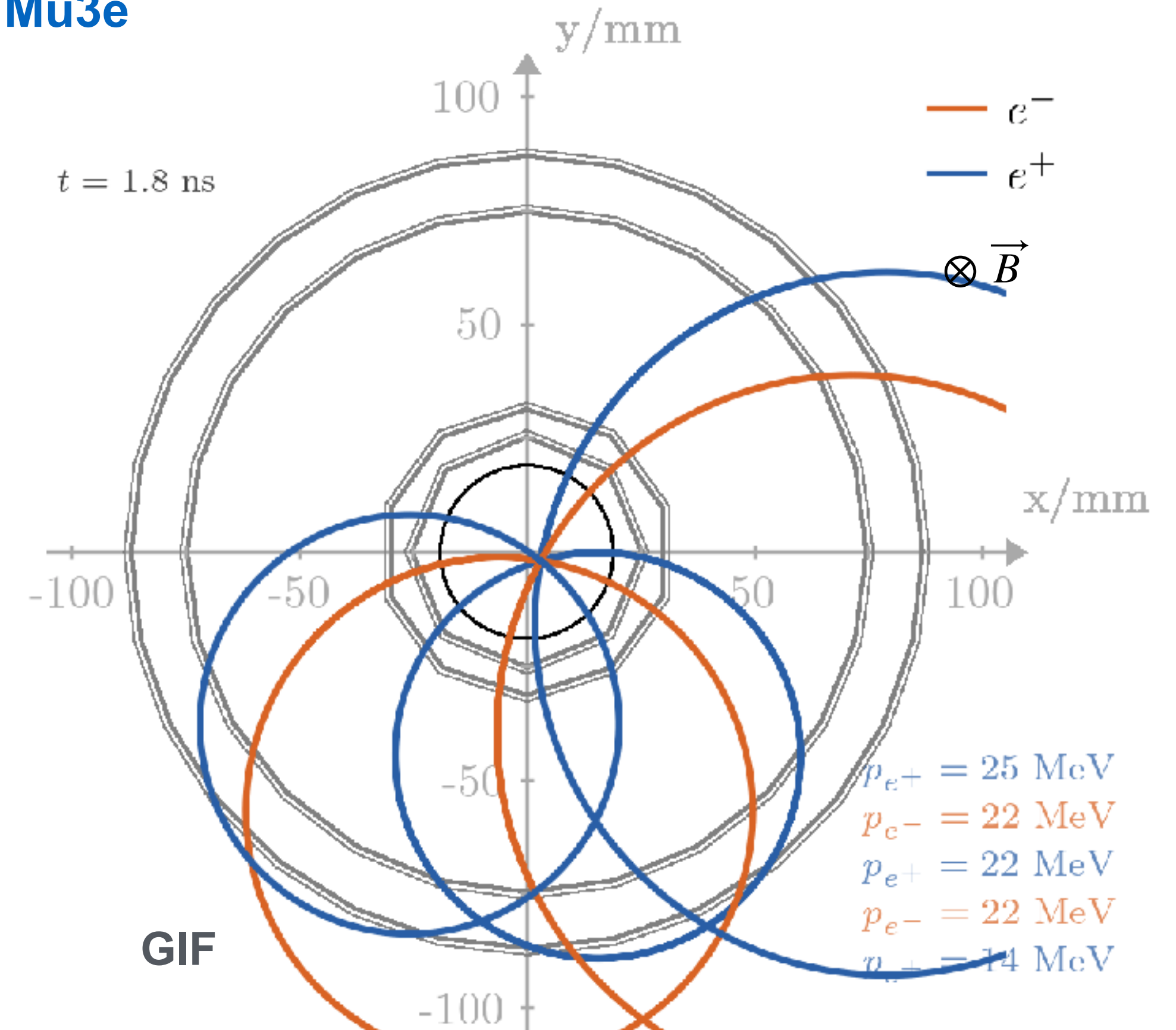
MH, T. Menzo, M. Pospelov, J. Zupan, [JHEP 10 \(2023\) 006](#)

- 1) Generating muon decays with MadGraph5 v3.5.0 and Scikit-HEP phase-space package (unpolarized μ).
- 2) Place muons on surface of Mylar target.*
- 3) Draw helical trajectories with $B = 1$ T, smearing $|p_e|$ with energy-dependent Gaussians.*
- 4) Signal selection based on # of hits on scintillator layers.

70 μm Mylar target (decays on the surface)



$r\phi$ view of Mu3e



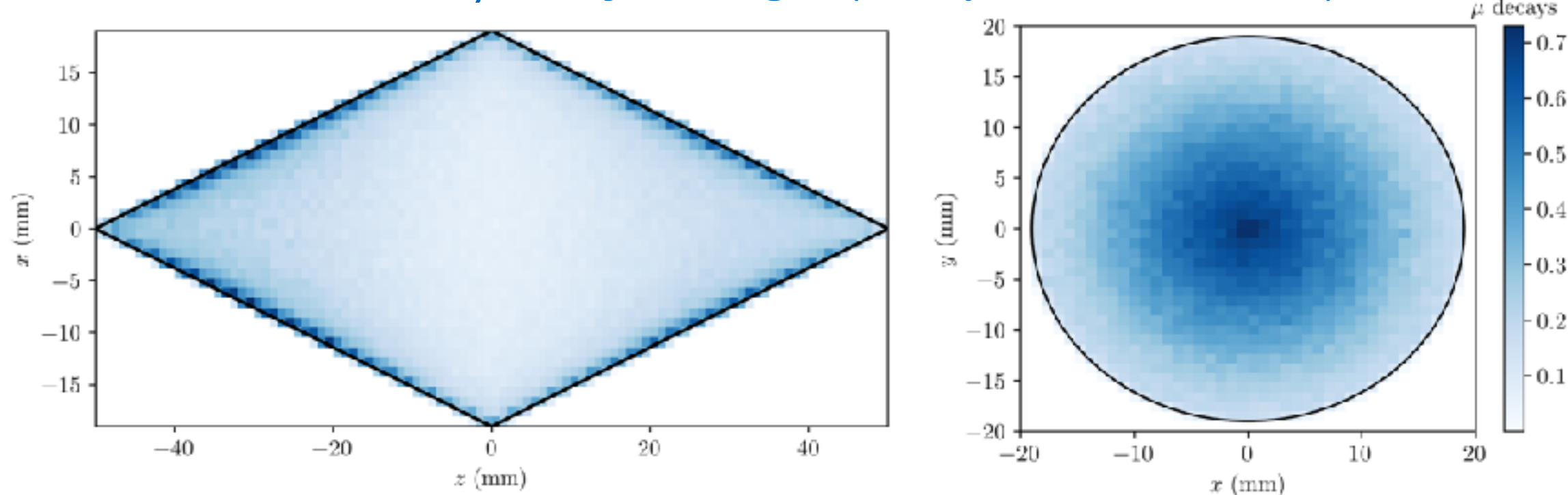
Rare muon decays at Mu3e

A theorist's fast MC for the detector

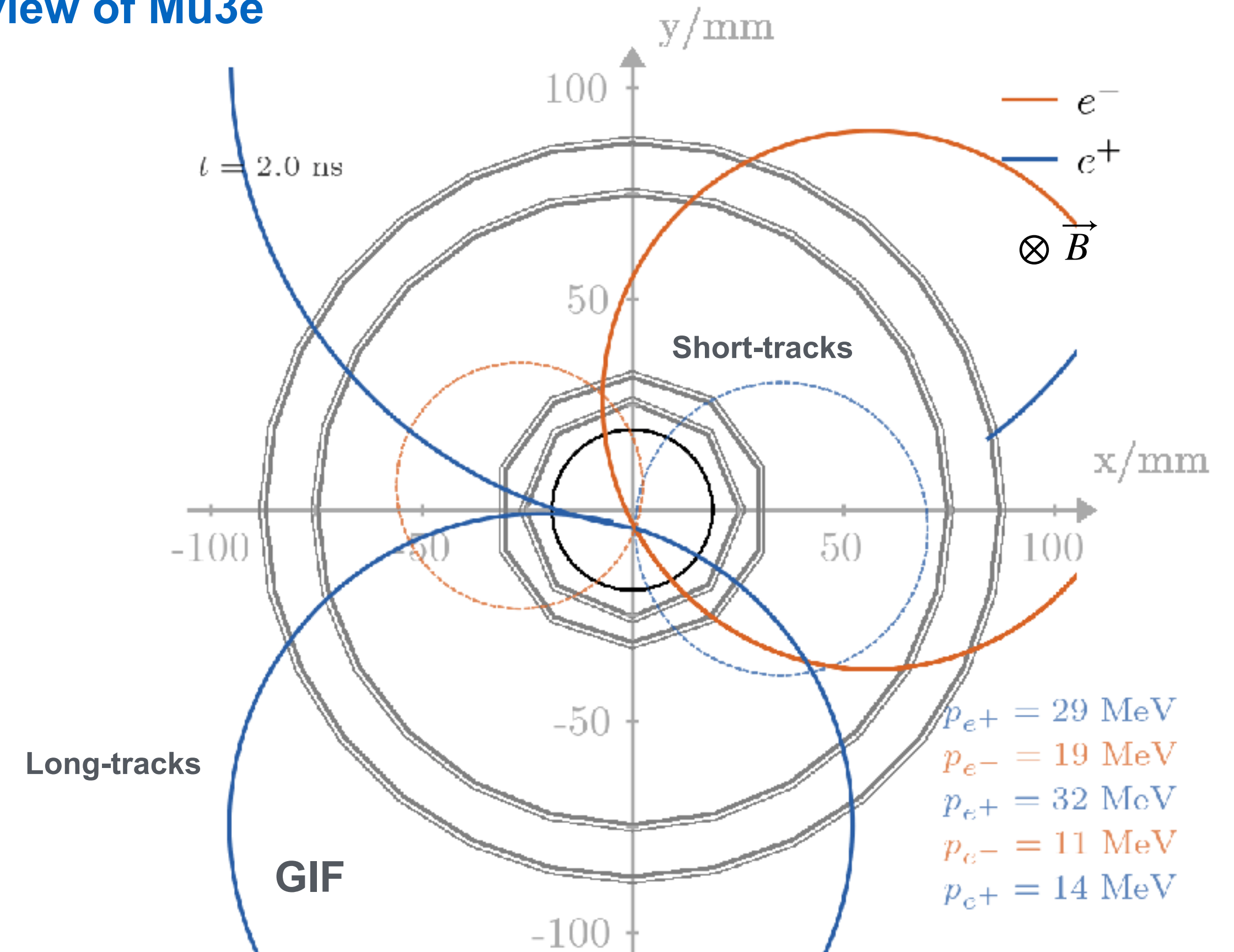
MH, T. Menzo, M. Pospelov, J. Zupan, [JHEP 10 \(2023\) 006](#)

- 1) Generating muon decays with MadGraph5 v3.5.0 and Scikit-HEP phase-space package (unpolarized μ).
- 2) Place muons on surface of Mylar target.*
- 3) Draw helical trajectories with $B = 1$ T, smearing $|p_e|$ with energy-dependent Gaussians.*
- 4) Signal selection based on # of hits on scintillator layers.

70 μm Mylar target (decays on the surface)



$r\phi$ view of Mu3e



Rare muon decays at Mu3e

The Standard Model rate

MH, T. Menzo, M. Pospelov, J. Zupan, [JHEP 10 \(2023\) 006](#)

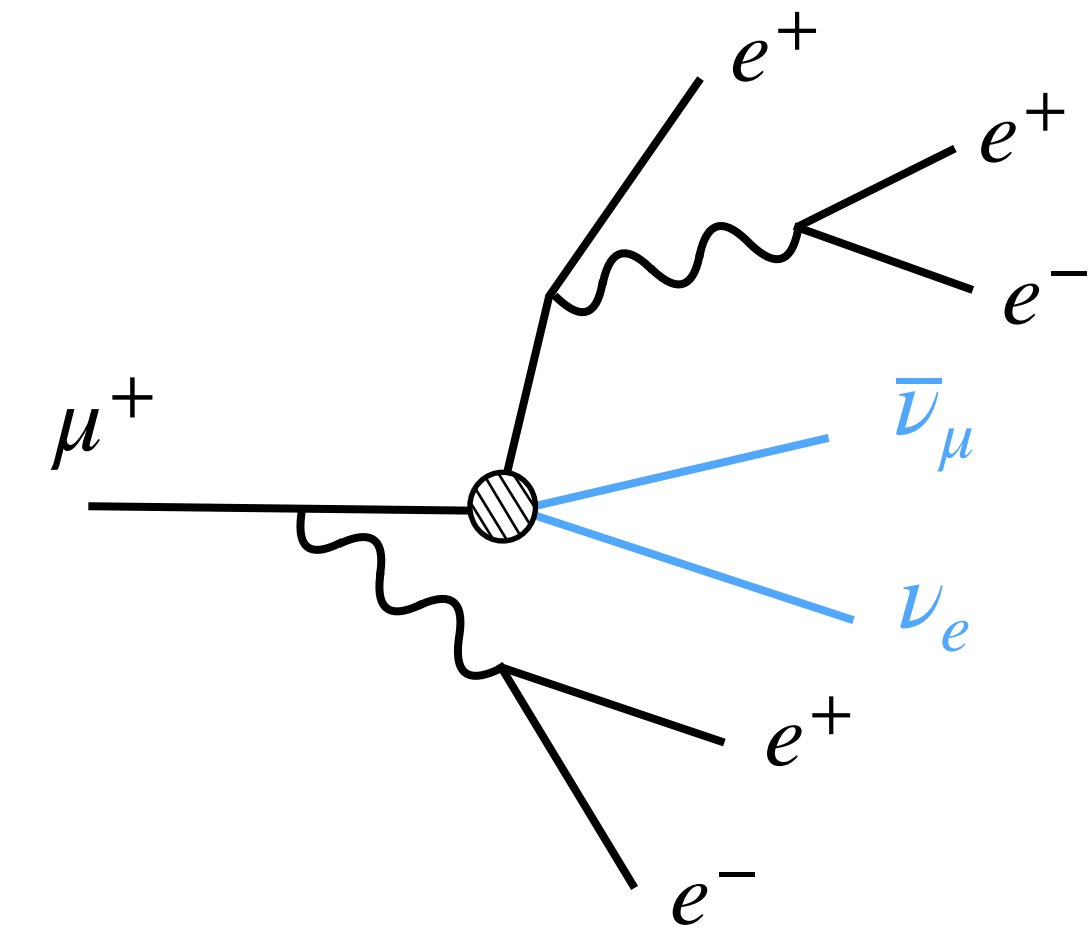
From MadGraph5 v3.5.0, we can calculate the total rate:

Leading order in G_F and α — negligible MC stats error

$$\mathcal{B}(\mu^+ \rightarrow e^+e^+e^-e^+e^-\nu\nu) \simeq 3.9 \times 10^{-10},$$

but this is not all observable. Some simple truth-level cuts illustrate the challenge:

$$\mathcal{B}(\mu^+ \rightarrow e^+e^+e^-e^+e^-\nu\nu \mid \text{all } p_{e^\pm}^{\text{T,true}} > 10 \text{ MeV}) = (1.4 \pm 0.1) \times 10^{-14}.$$



1 of 84 diagrams

The smallest decay rate measurement for fundamental particles involving 2nd and 3rd generation?

Rare muon decays at Mu3e

The Standard Model rate

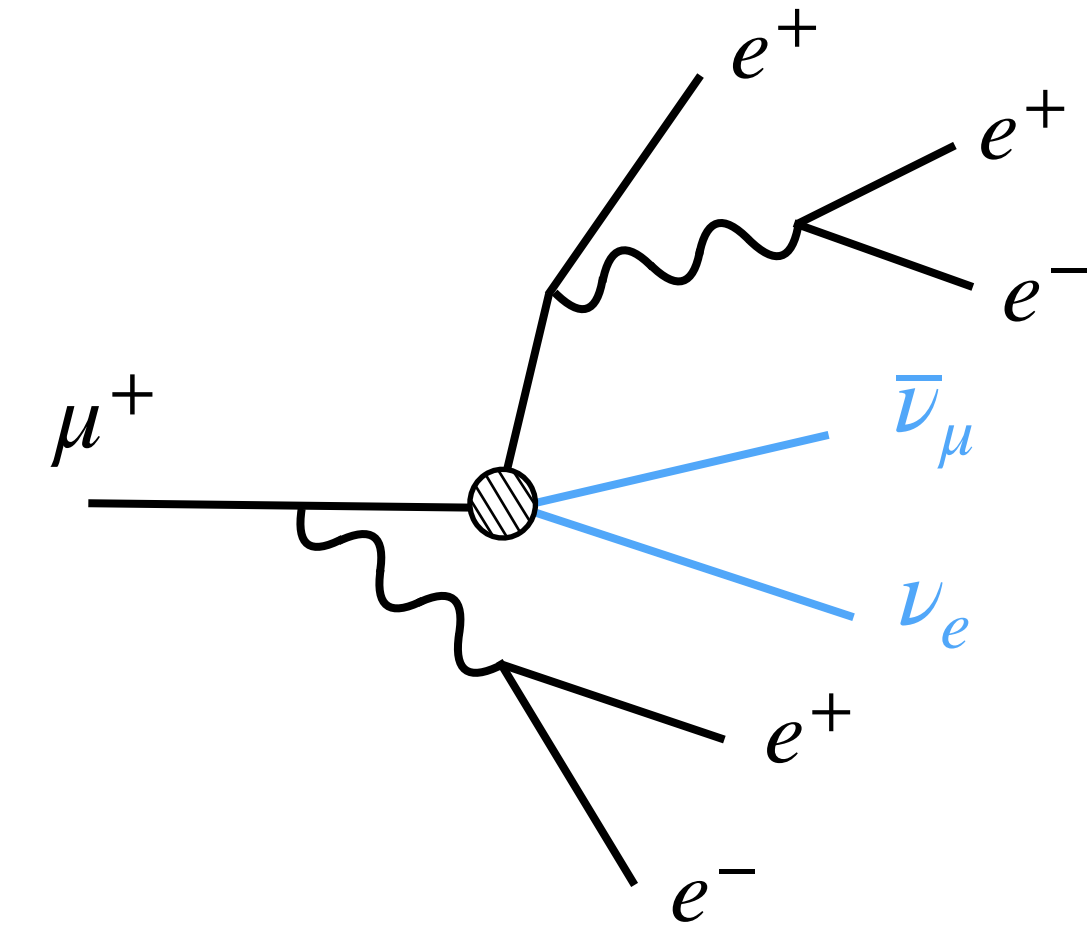
MH, T. Menzo, M. Pospelov, J. Zupan, [JHEP 10 \(2023\) 006](#)

From MadGraph5 v3.5.0, we can calculate the total rate:
 Leading order in G_F and α — negligible MC stats error

$$\mathcal{B}(\mu^+ \rightarrow e^+e^+e^-e^+e^-\nu\nu) \simeq 3.9 \times 10^{-10},$$

but this is not all observable. Some simple truth-level cuts illustrate the challenge:

$$\mathcal{B}(\mu^+ \rightarrow e^+e^+e^-e^+e^-\nu\nu \mid \text{all } p_{e^\pm}^{\text{T,true}} > 10 \text{ MeV}) = (1.4 \pm 0.1) \times 10^{-14}.$$



1 of 84 diagrams

The smallest decay rate measurement for fundamental particles involving 2nd and 3rd generation?

When looking for neutrino-less channels, this SM rate will not be an issue. Missing energy cuts are very effective:

$$\mathcal{B}(\mu^+ \rightarrow e^+e^+e^-e^+e^-\nu\nu \mid E_{\text{missing}}^{\text{true}} < 20 \text{ MeV}) = (8.9 \pm 0.3) \times 10^{-14}$$

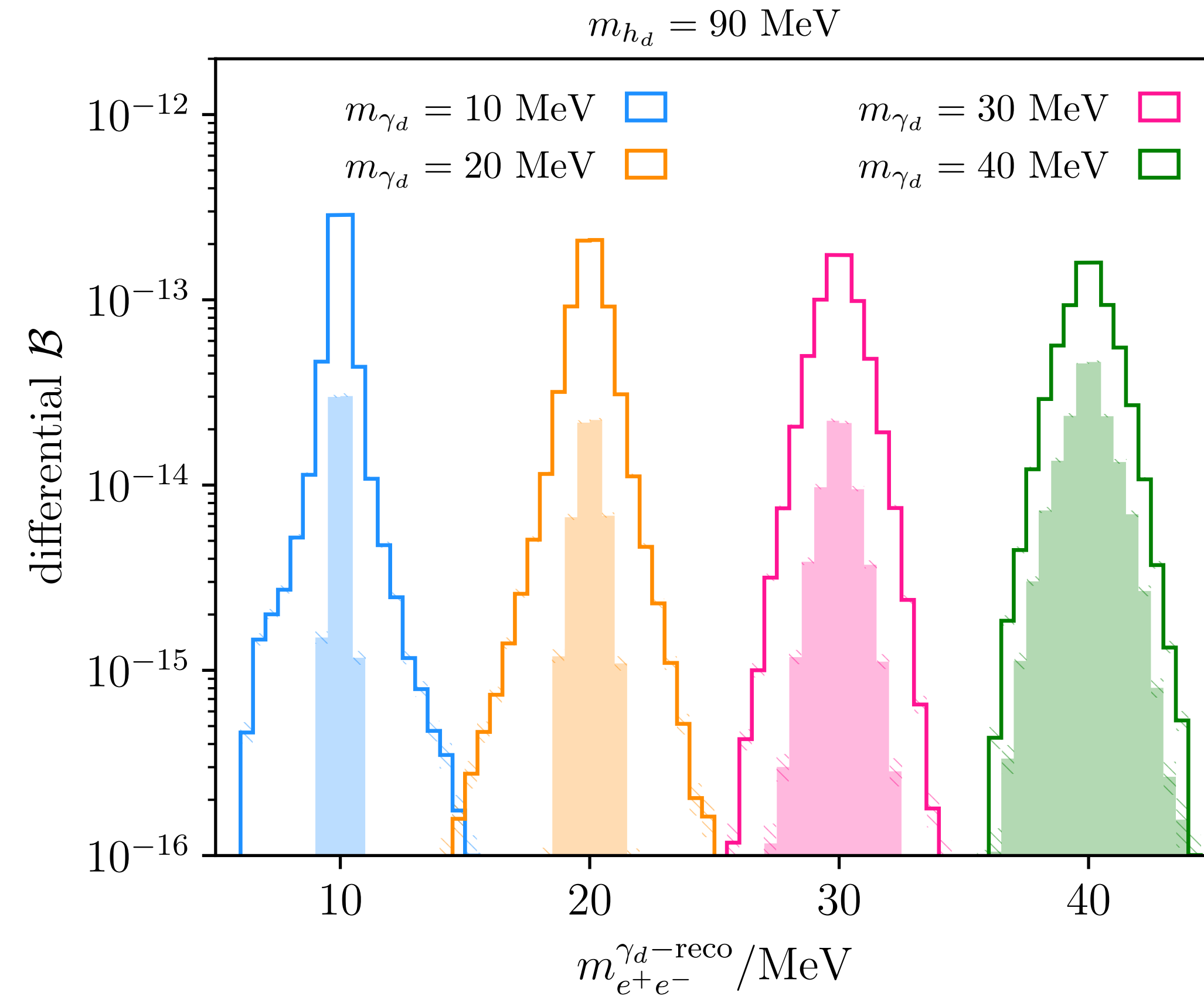
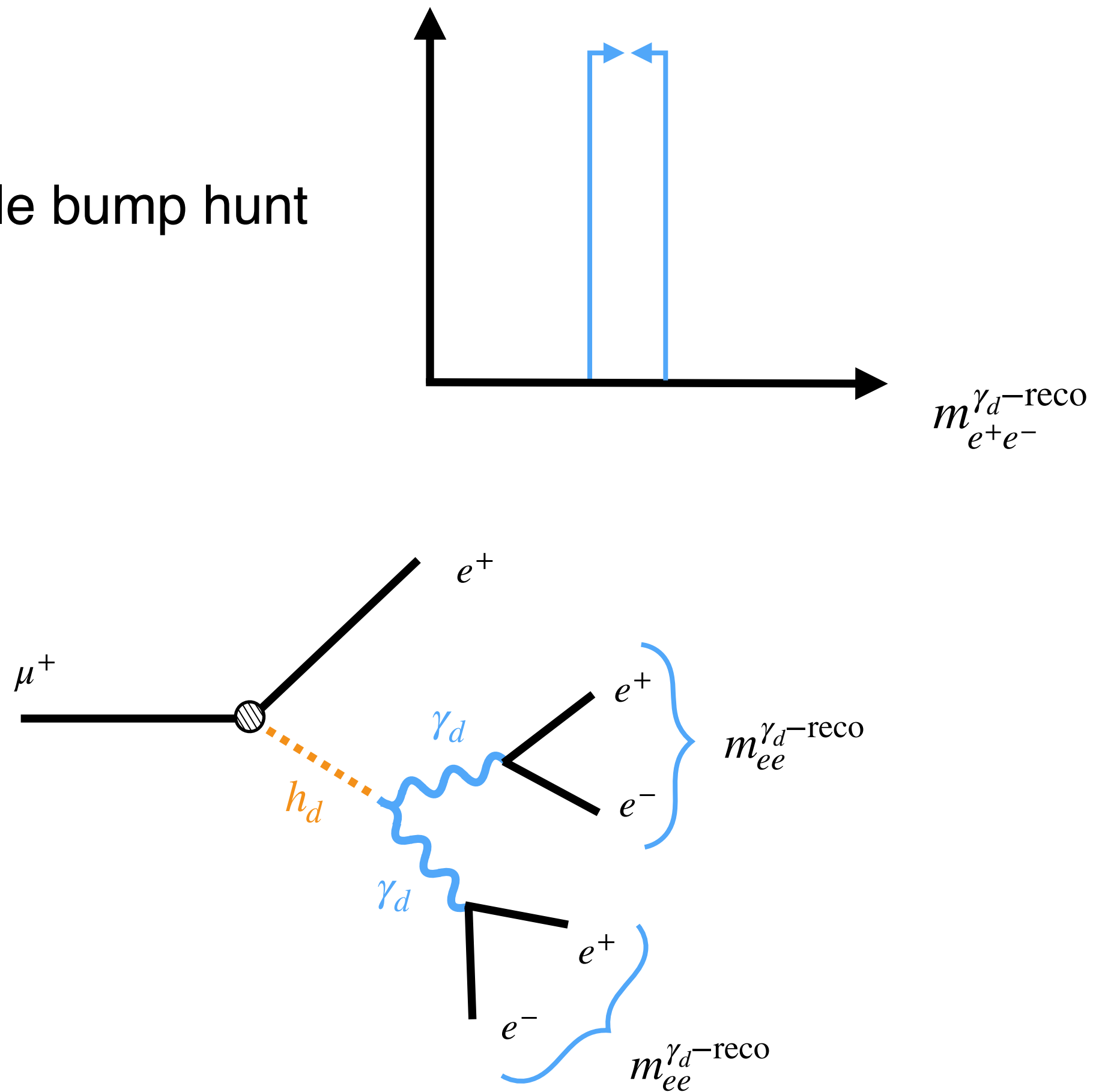
$$\mathcal{B}(\mu^+ \rightarrow e^+e^+e^-e^+e^-\nu\nu \mid E_{\text{missing}}^{\text{true}} < 10 \text{ MeV}) = (1.1 \pm 0.2) \times 10^{-15}$$

Rare muon decays at Mu3e

Neutrinoless five-track events

MH, T. Menzo, M. Pospelov, J. Zupan, *JHEP* 10 (2023) 006

Double bump hunt

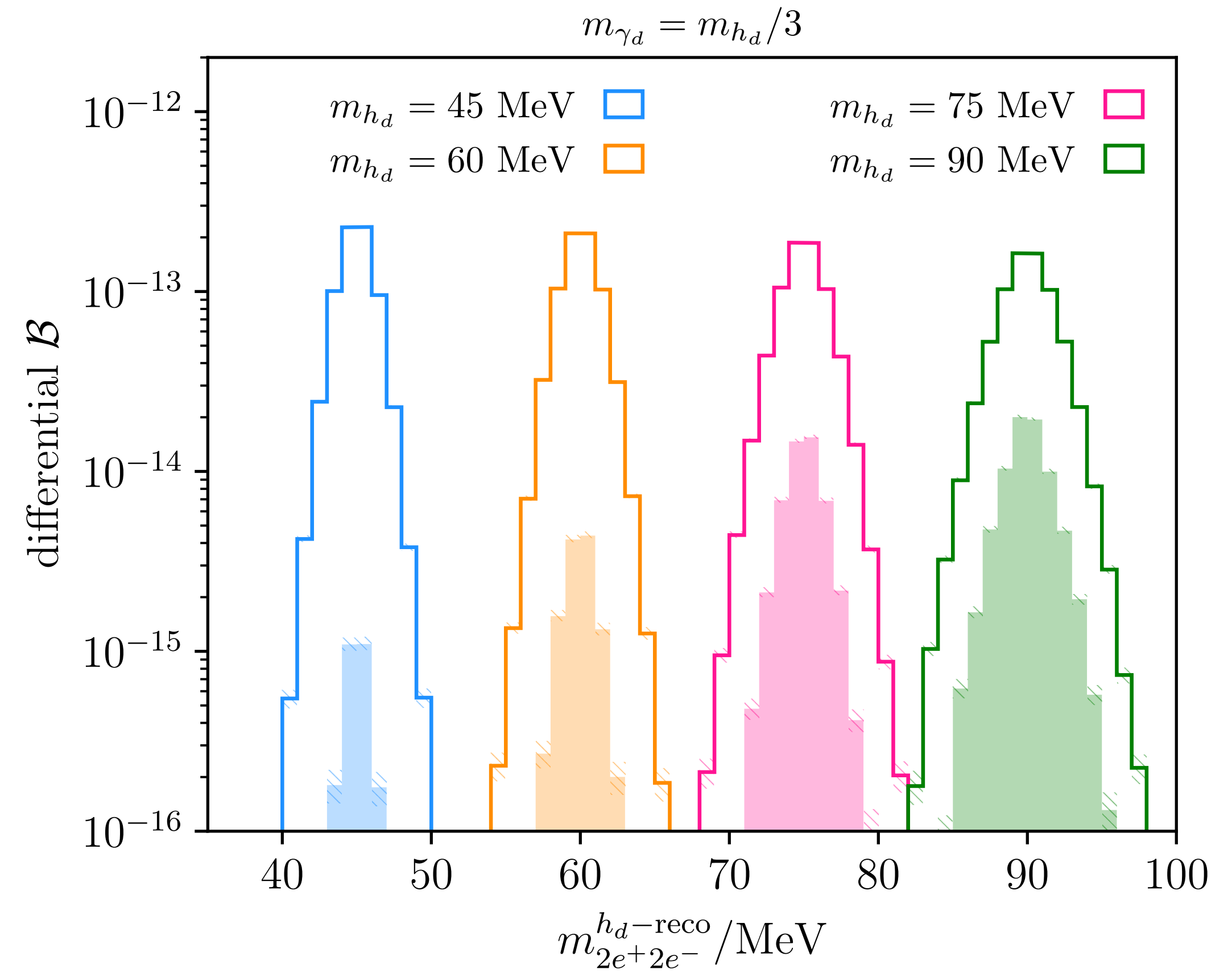
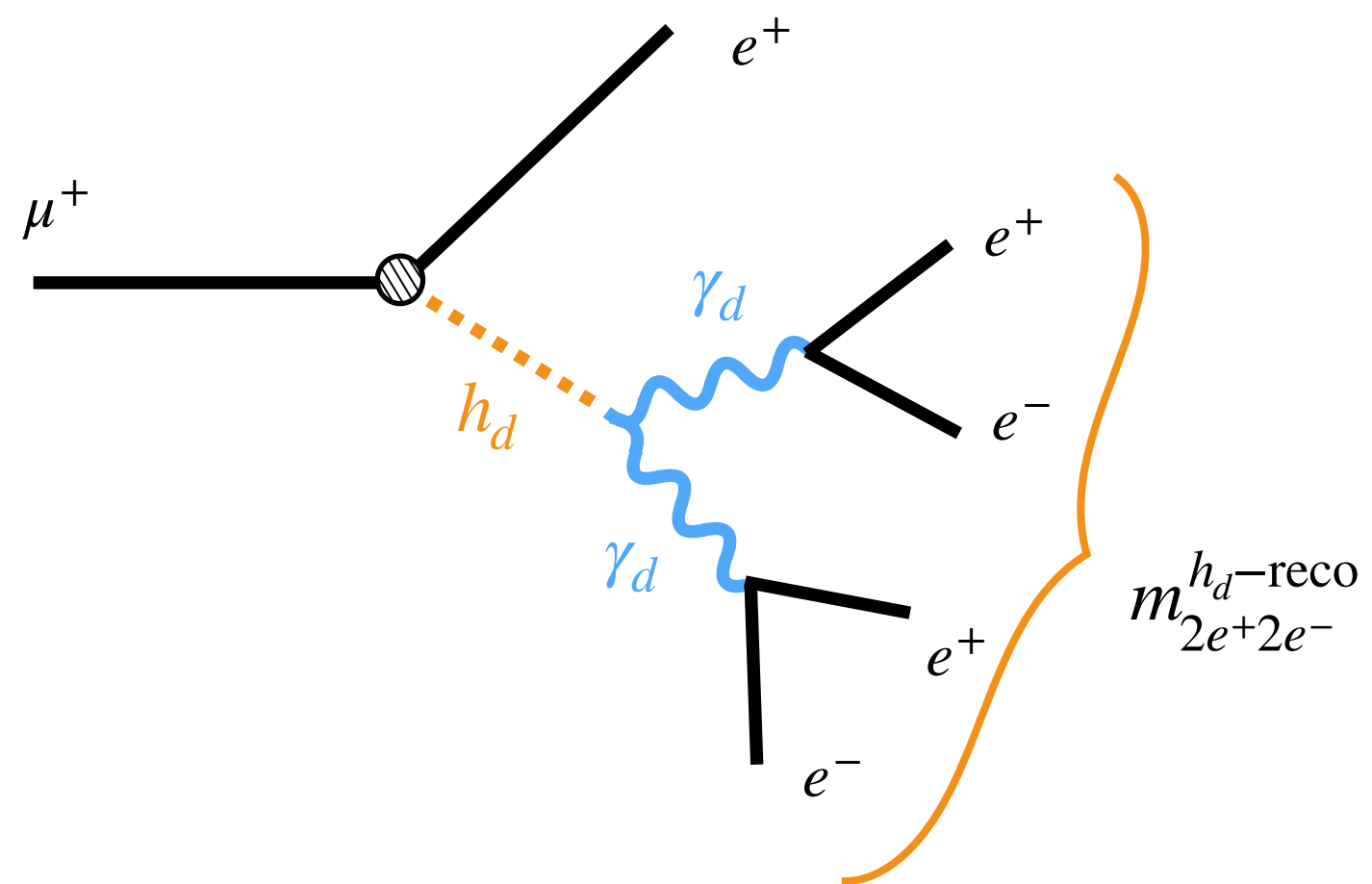
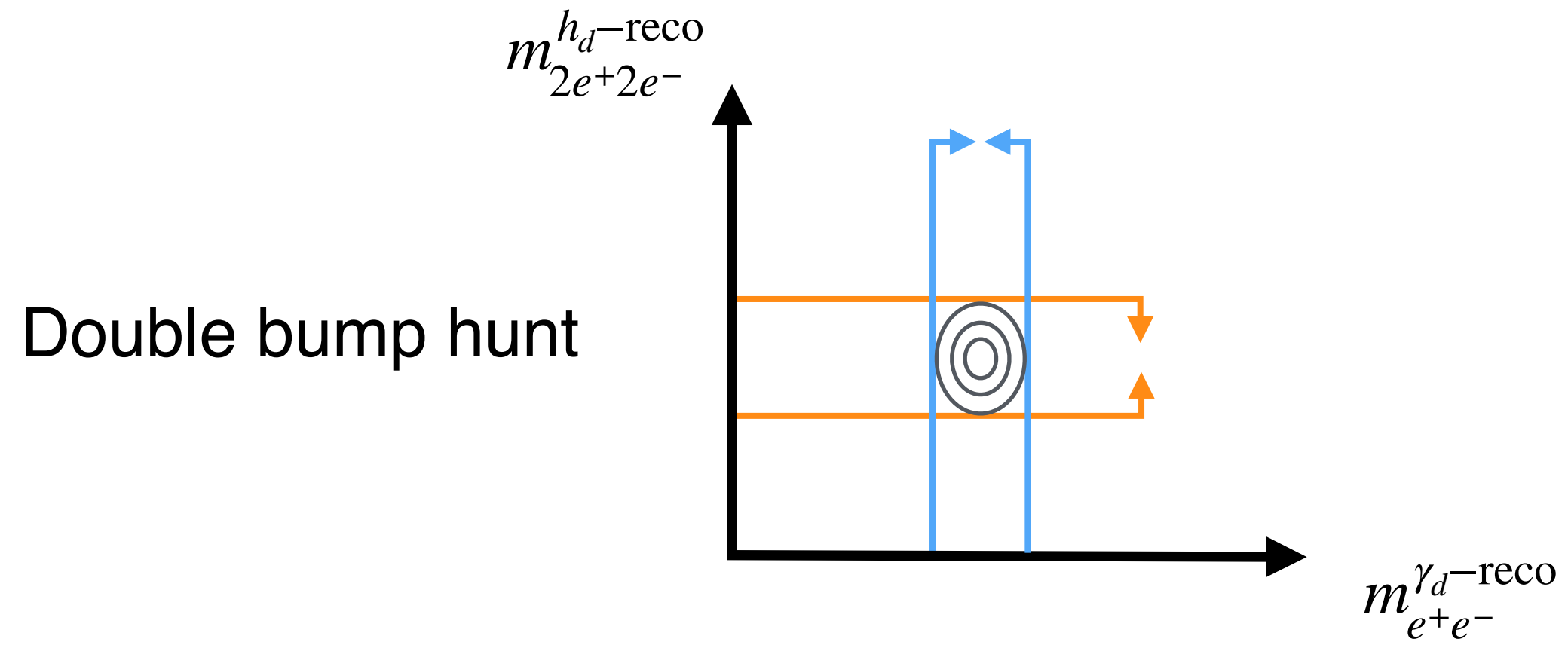


We find: $\sigma_{m_{\gamma_d}} / m_{\gamma_d} = 2.3\%$

Rare muon decays at Mu3e

Neutrinoless five-track events

MH, T. Menzo, M. Pospelov, J. Zupan, *JHEP* 10 (2023) 006



We find: $\sigma_{m_{\gamma_d}}/m_{\gamma_d} = 2.3\%$ and $\sigma_{m_{h_d}}/m_{h_d} = 1.5\%$

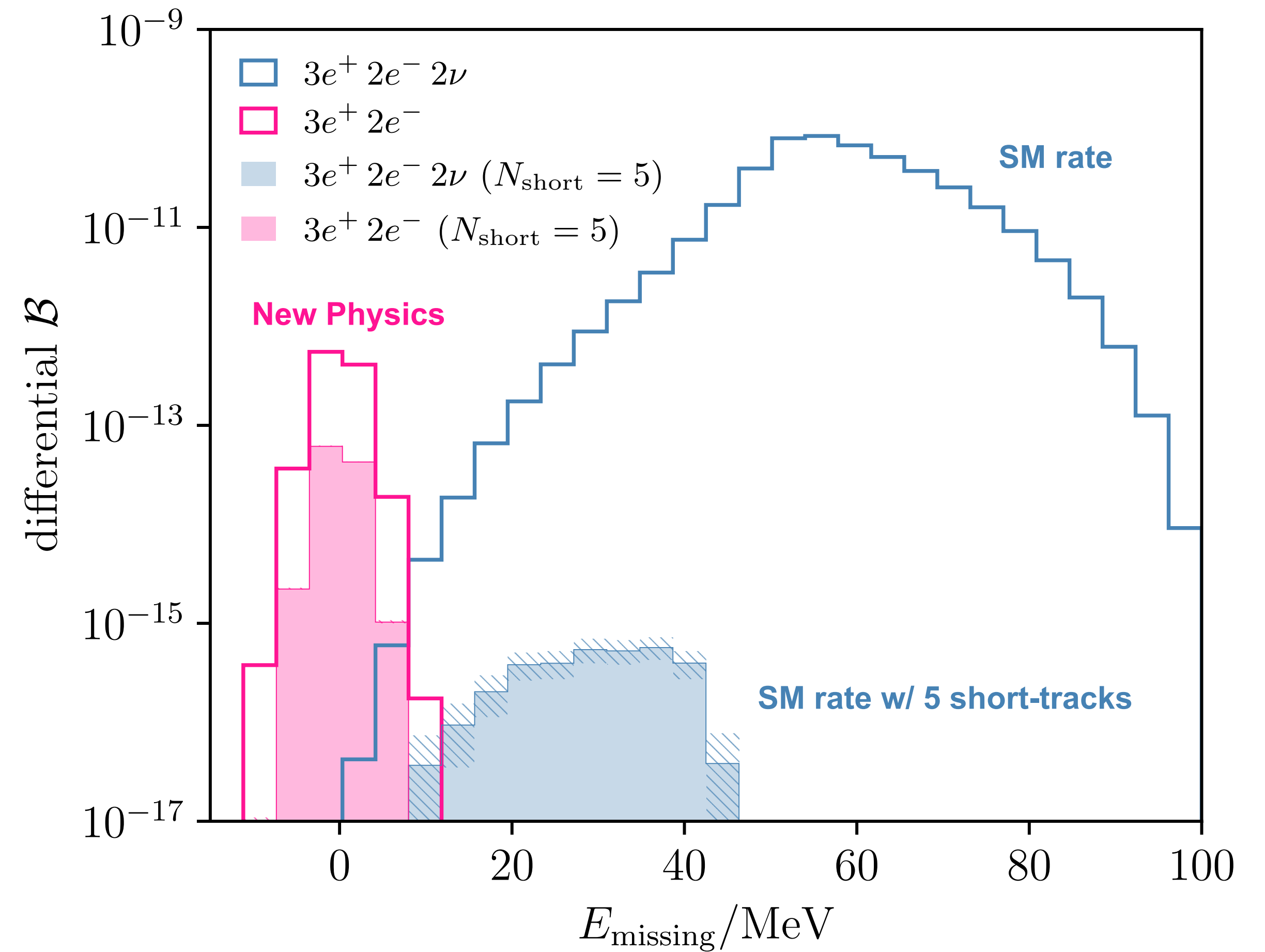
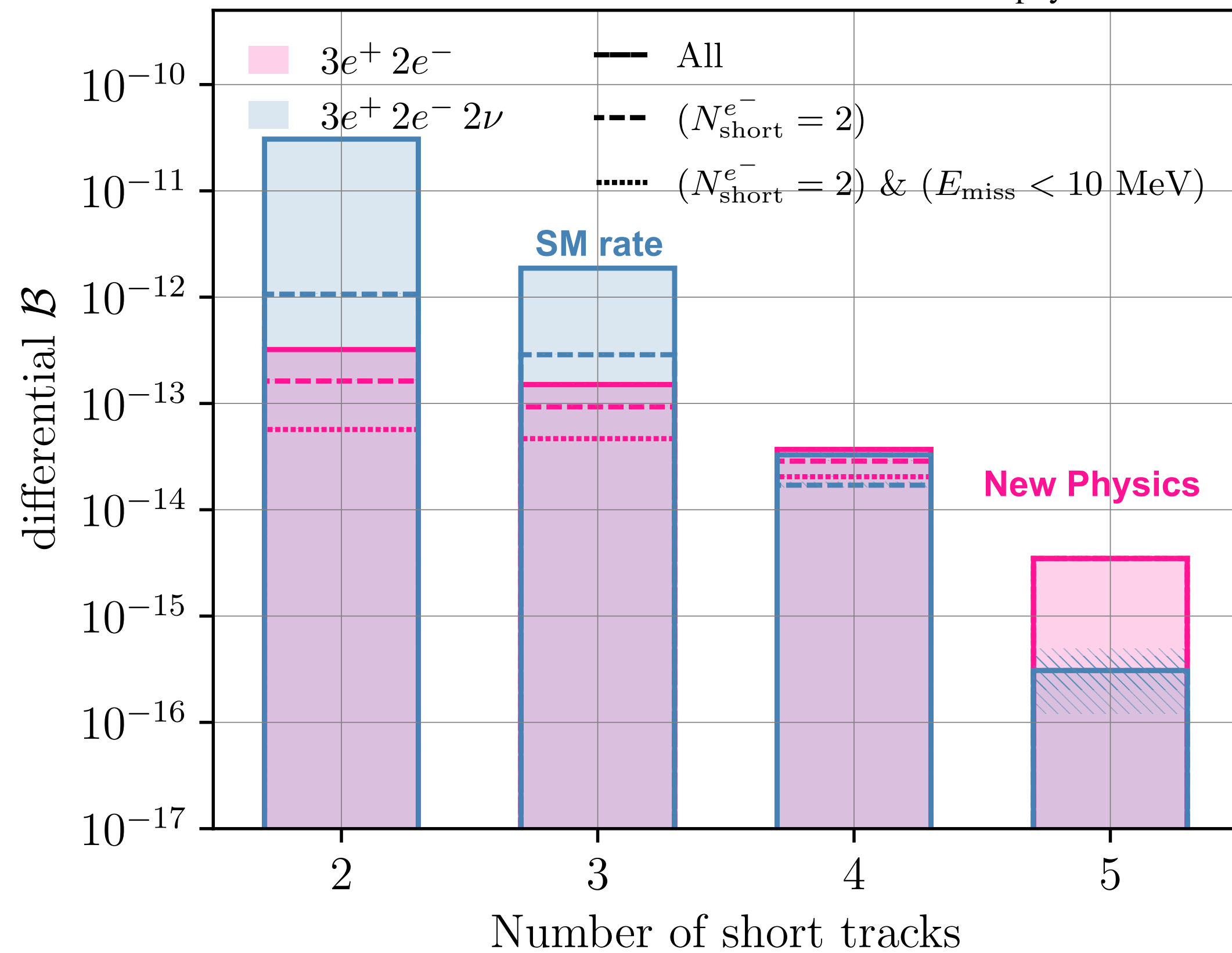
Rare muon decays at Mu3e

Signal selection for new physics

MH, T. Menzo, M. Pospelov, J. Zupan, *JHEP* 10 (2023) 006

Short-tracks: ≥ 4 hits

$m_{\gamma_d} = 30$ MeV and $m_{h_d} = 90$ MeV $\mathcal{B}_{\text{new physics}} = 10^{-12}$



Rare muon decays at Mu3e

Backgrounds

MH, T. Menzo, M. Pospelov, J. Zupan, [JHEP 10 \(2023\) 006](#)

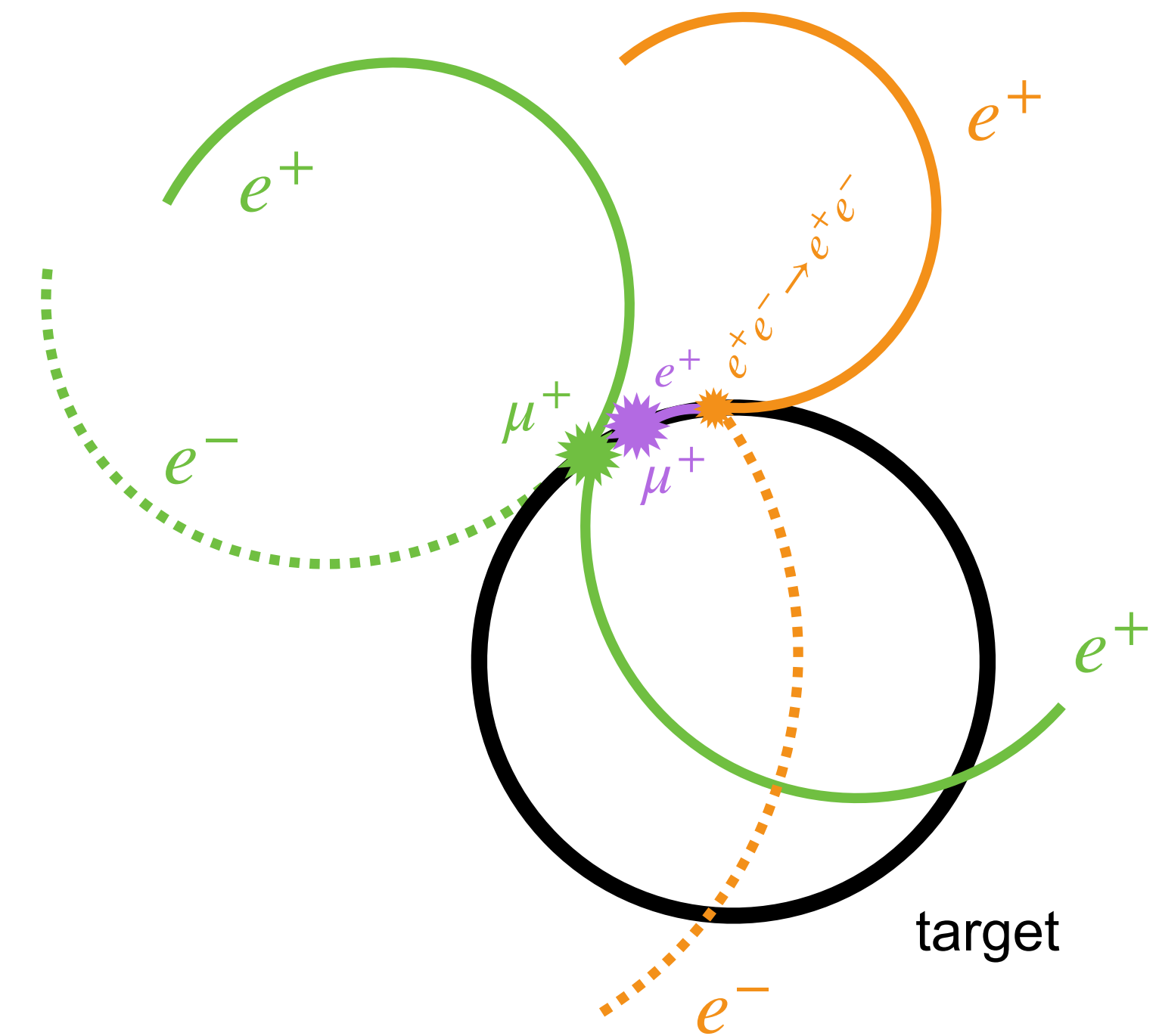
Five-track SM decay is not going to be a show-stopper.

The most worrisome backgrounds, however, will arise from **accidentals**.

- $\mu^+ \rightarrow e^+e^+e^-\nu\nu$ in coincidence with $\mu^+ \rightarrow e^+\nu\nu$, where one of the positrons produces a Bhabha electron.

Before any kinematical cuts, we estimate this rate to be around

3 out of 10^{12} muon decays with a stopped muon rate of $10^8 \mu/s$.



Further experimental studies are needed, but a background-free search may be possible.

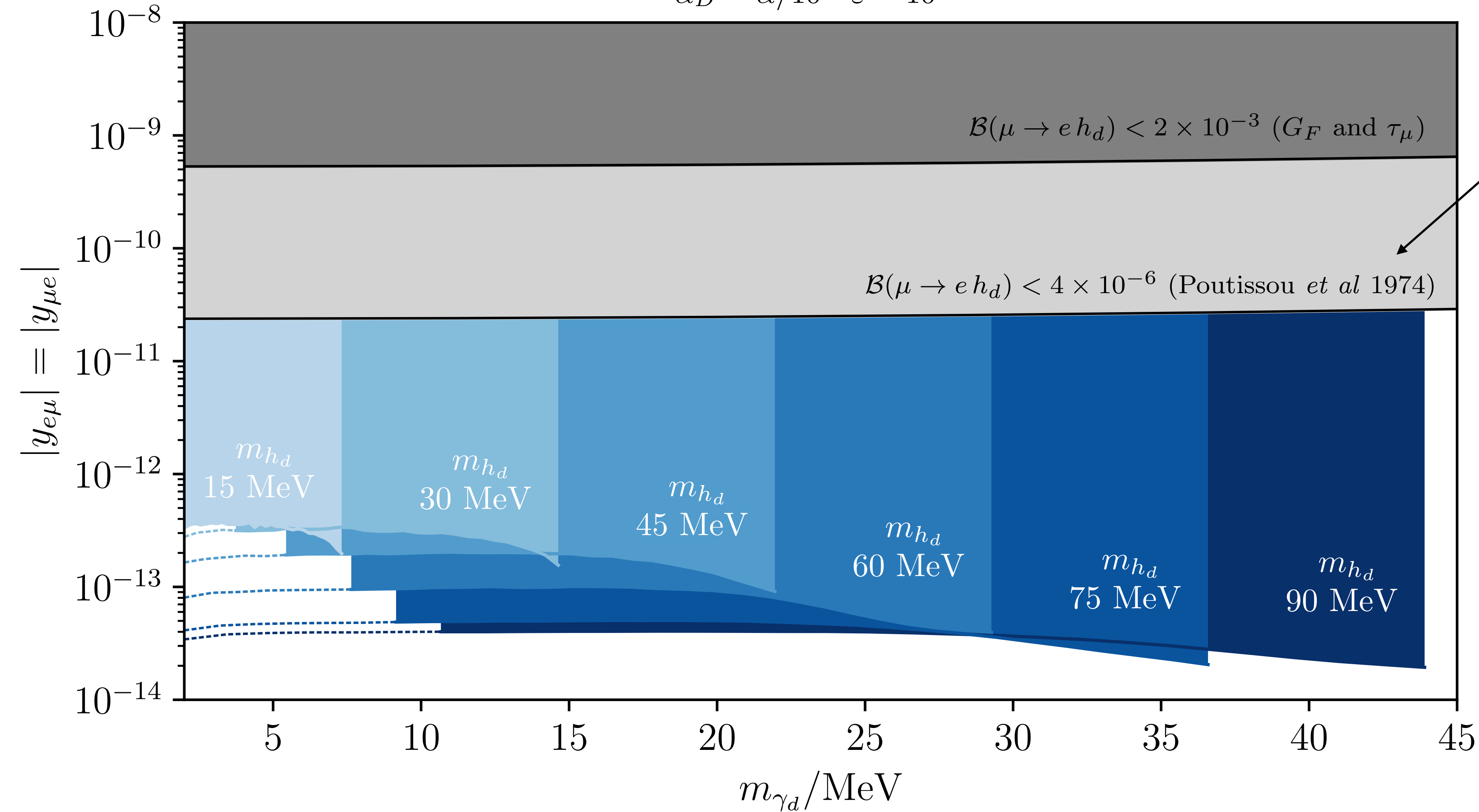
It would also be interesting to investigate four-track events with only $2(e^-e^+)$.

Rare muon decays @ Mu3e

$U(1)_d$ with charged Lepton Flavor Violation

MH, T. Menzo, M. Pospelov, J. Zupan, *JHEP* 10 (2023) 006

$$\alpha_D = \alpha/10 \quad \varepsilon = 10^{-4}$$



Calorimetric search for $E_{\text{vis}} \simeq m_\mu$

Conservatively showing corresponding reach of **1 decay out of 10^{12} muons**, after signal selection.

New physics scale as high as:

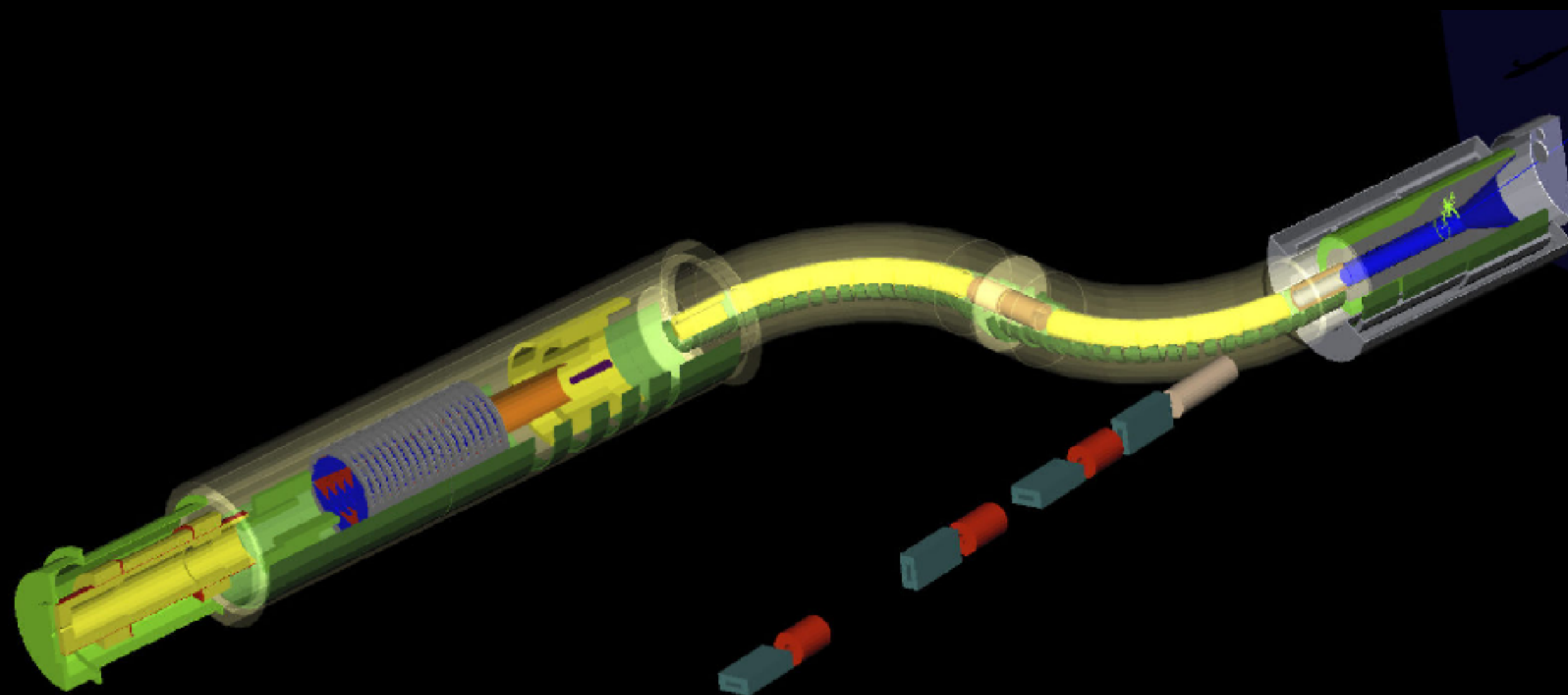
$$\Lambda < 10^7 \text{ GeV if secluded}$$

$$\Lambda < 10^{15} \text{ GeV if leptophilic}$$



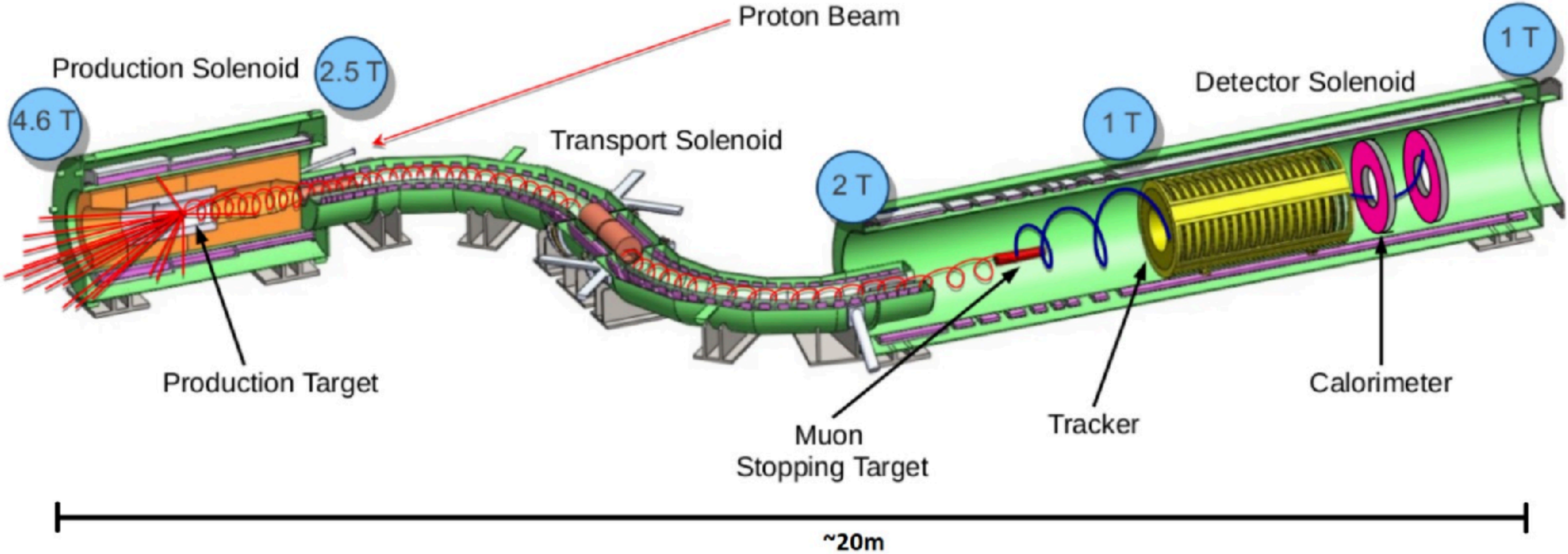
Extracting more energy out of μ^- capture

Muon-induced baryon number violation



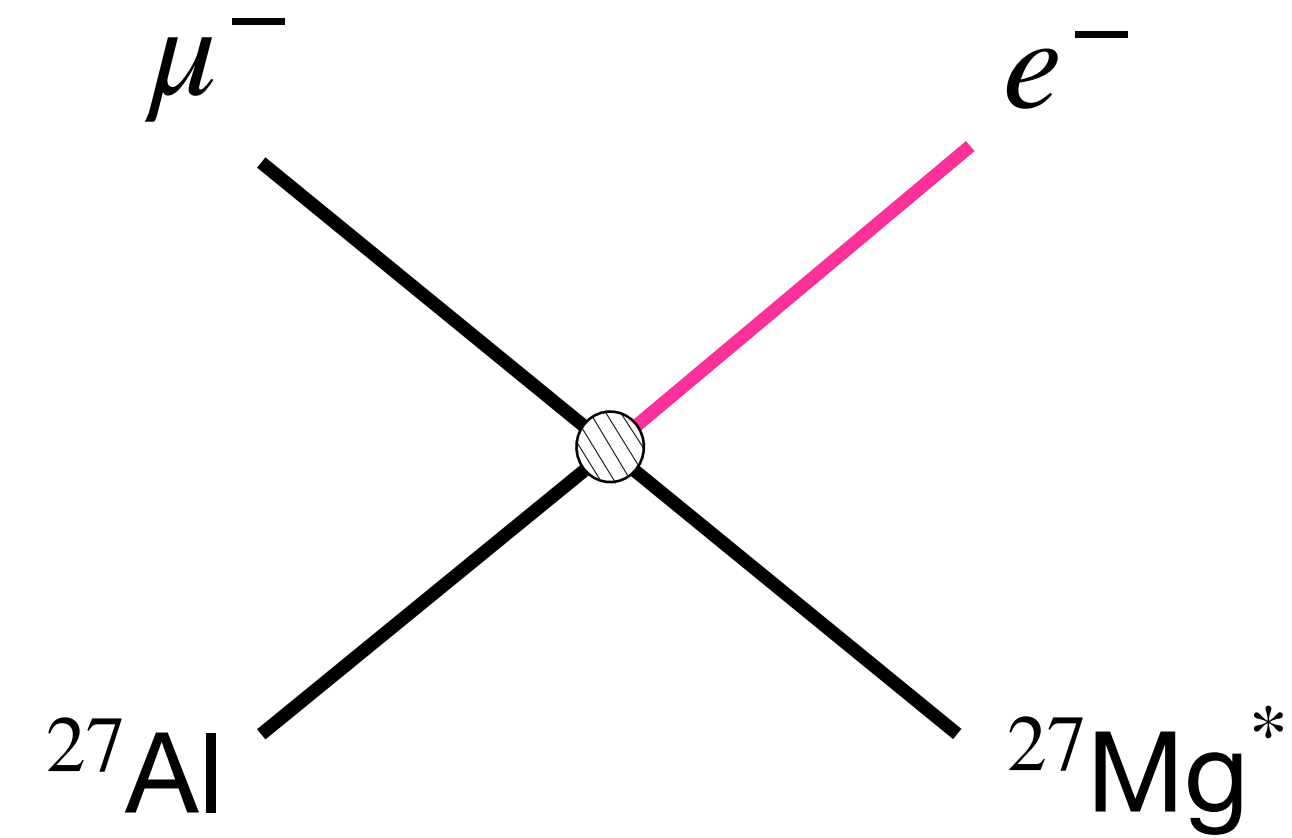
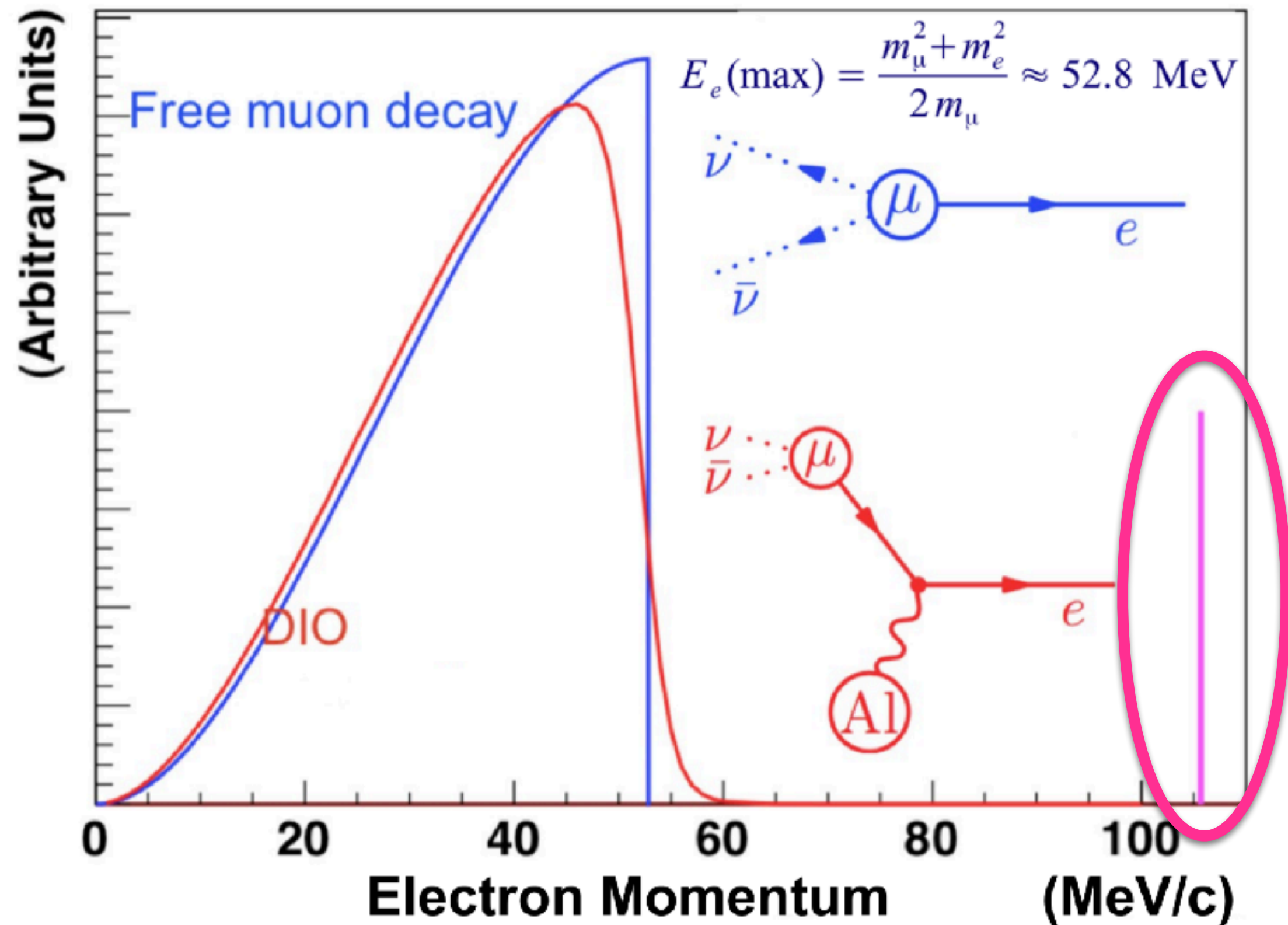
Mu2e on $\mu \rightarrow e$ conversion

Mono-energetic conversion electrons



Mu2e on $\mu \rightarrow e$ conversion

Mono-energetic conversion electrons



Conversion Electron: $E_{\text{cap}} \sim 104.9 \text{ MeV}$

Can we overshoot this value with new physics?

A genuine source of $E_{e^-} > E_{\text{cap}}$ in muon capture can arise if we destroy a baryon.

New light particles
at Mu2e/COMET

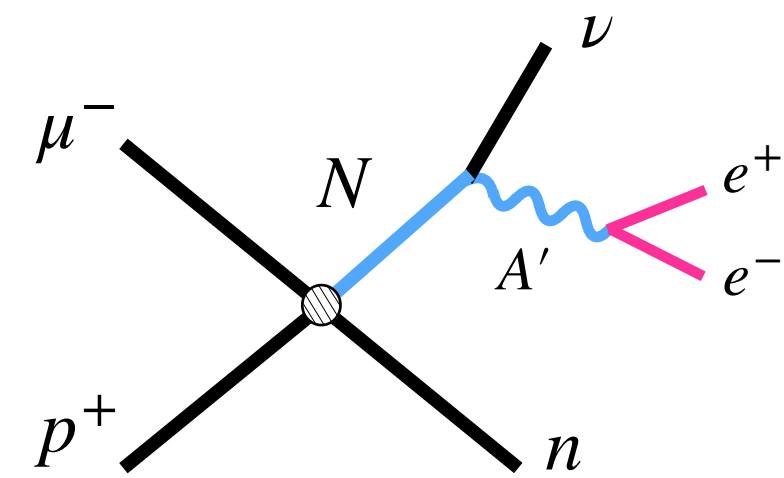
Soft spectrum
under μ DIO

Electron energy

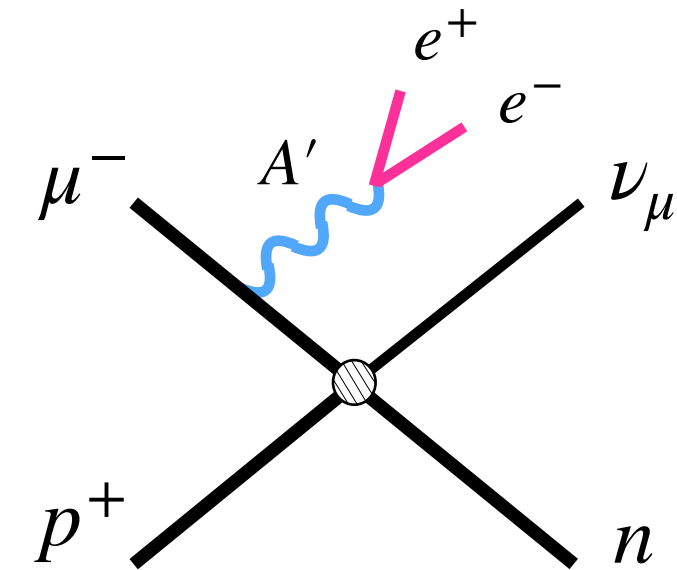
$$\delta E_{e^-} = E_{e^-} - m_\mu$$

B conservation

LF Conserving

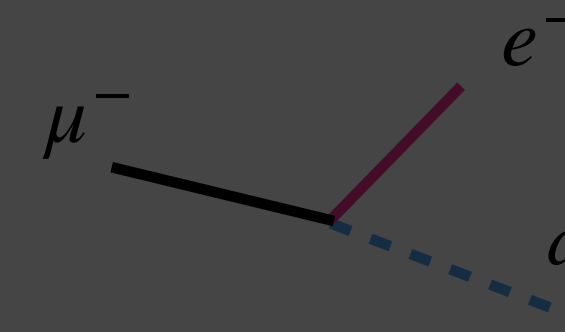


Heavy Neutral Leptons
 $\delta E_{e^+e^-} < 0$

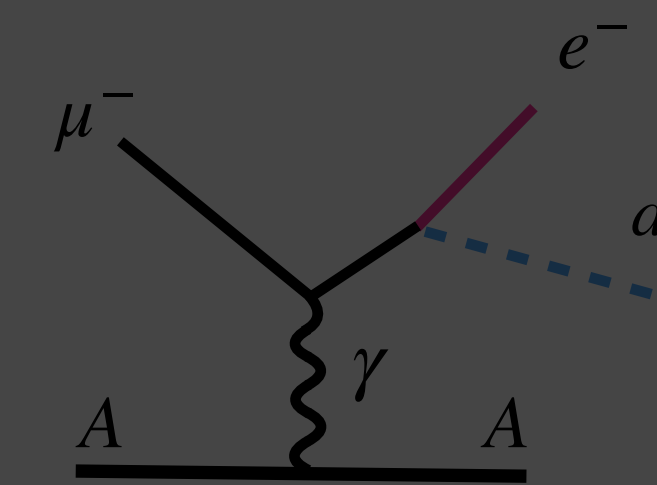


Dark Photons
 $\delta E_{e^+e^-} < 0$

Apparent LF Violating

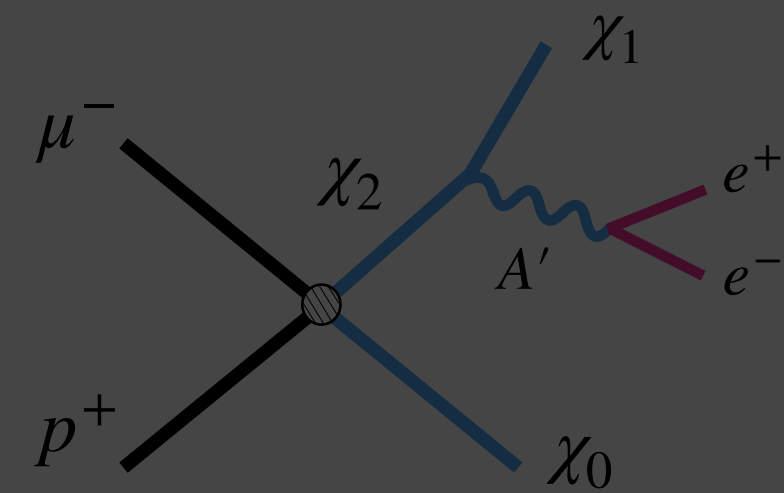


Decay-in-orbit
 $\delta E_{e^-} < 0$

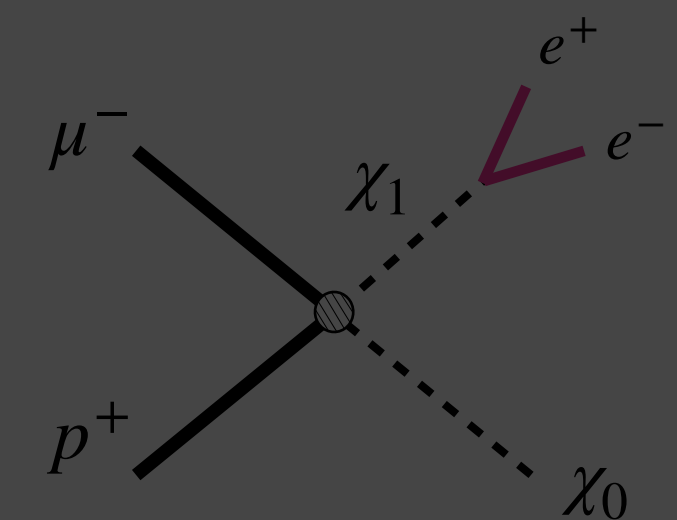


Axion-like-particles
 $\delta E_{e^-} < 0$

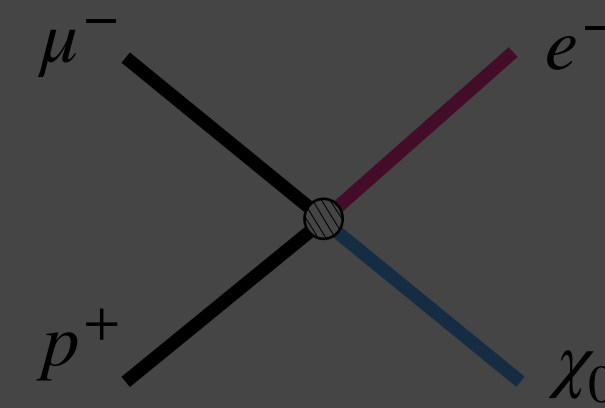
Apparent B Violating



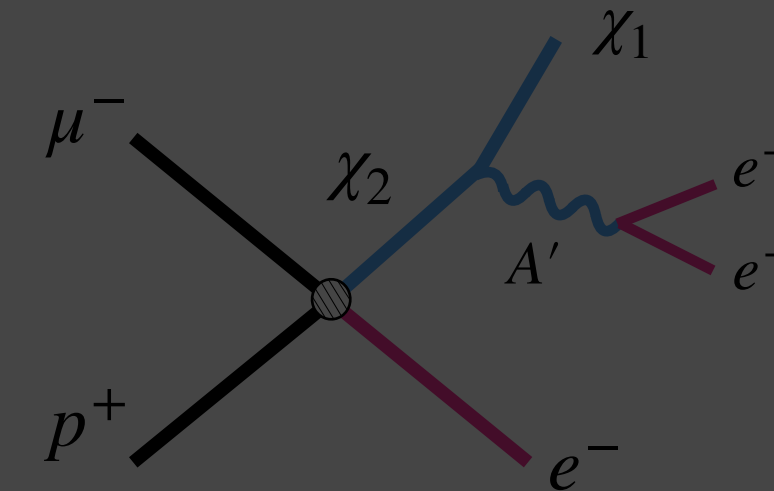
Dark Baryon Sector
 $\delta E_{e^+e^-} \lesssim m_p - m_0$



Dark Baryon Sector:
 $\delta E_{e^+e^-} \lesssim m_p - m_0$



Dark Baryon Sector:
 $\delta E_{e^-} \lesssim m_p - m_0$



Dark Baryon Sector:
 $\delta E_{e^+e^-} \lesssim m_p - m_1$

New light particles
at Mu2e/COMET

Soft spectrum
under μ DIO

Electron energy

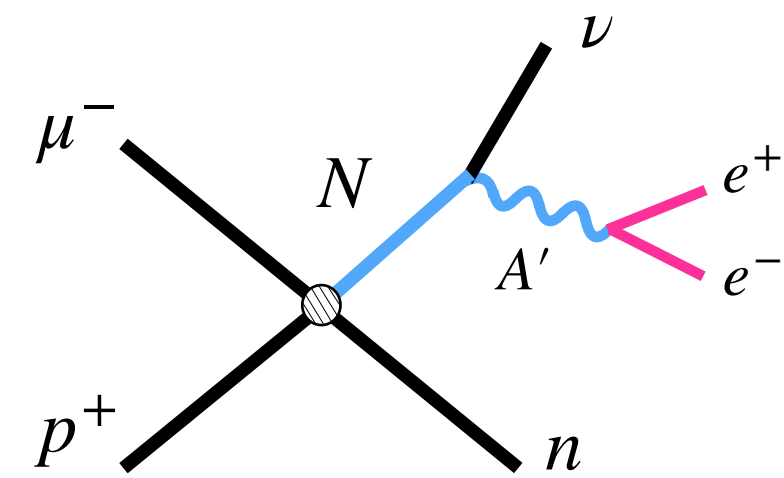
$$\delta E_{e^-} = E_{e^-} - m_\mu$$

B conservation

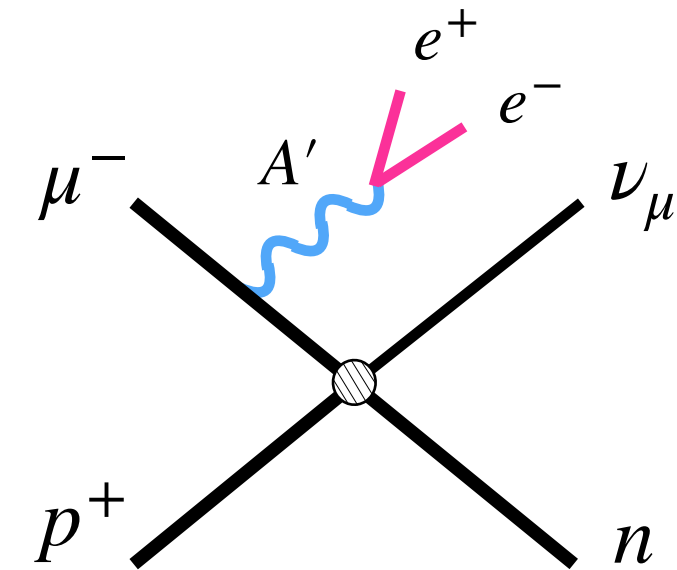
Apparent B Violating

LF Conserving

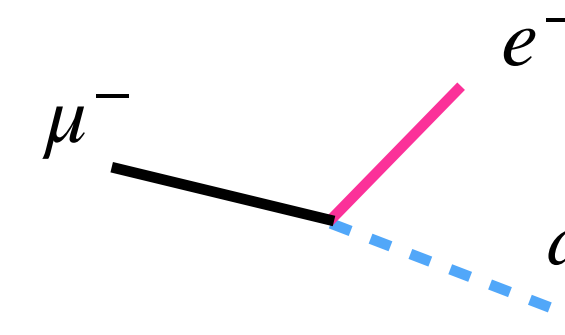
Apparent LF Violating



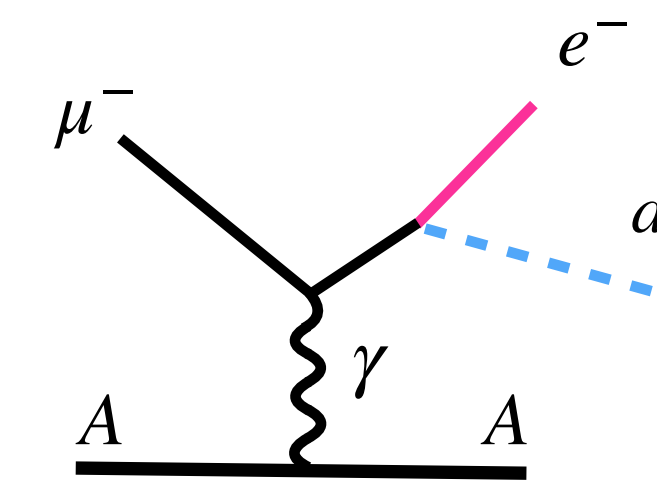
Heavy Neutral Leptons
 $\delta E_{e^+e^-} < 0$



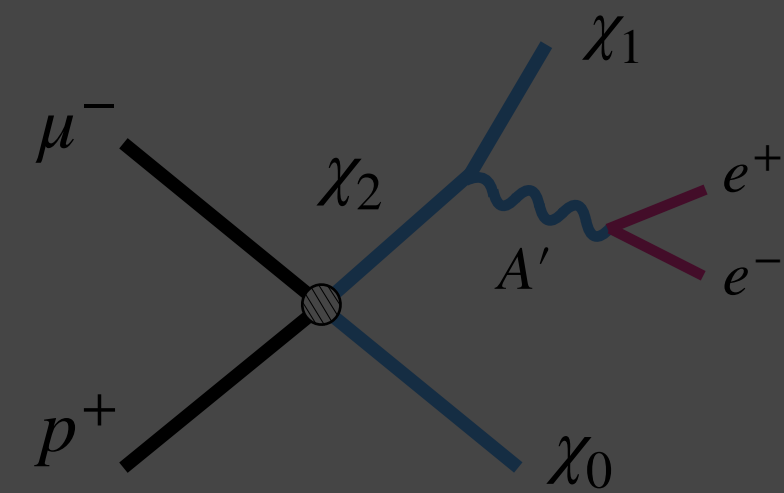
Dark Photons
 $\delta E_{e^+e^-} < 0$



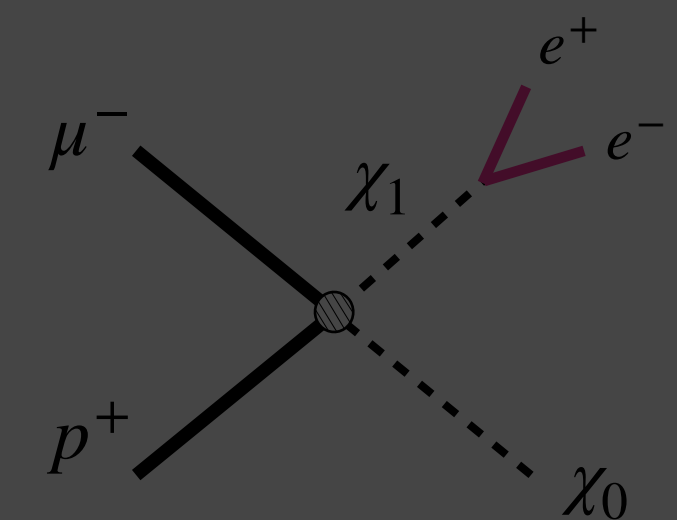
Decay-in-orbit
 $\delta E_{e^-} < 0$



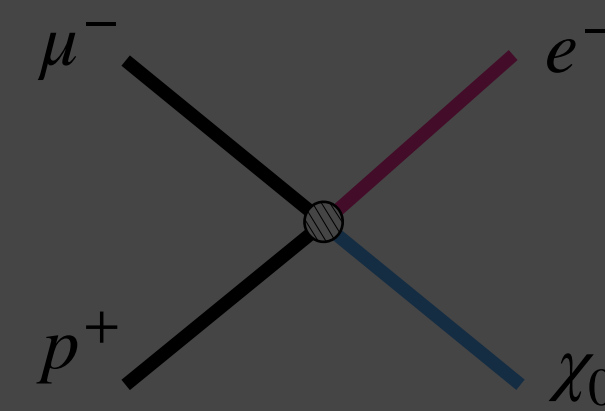
Axion-like-particles
 $\delta E_{e^-} < 0$



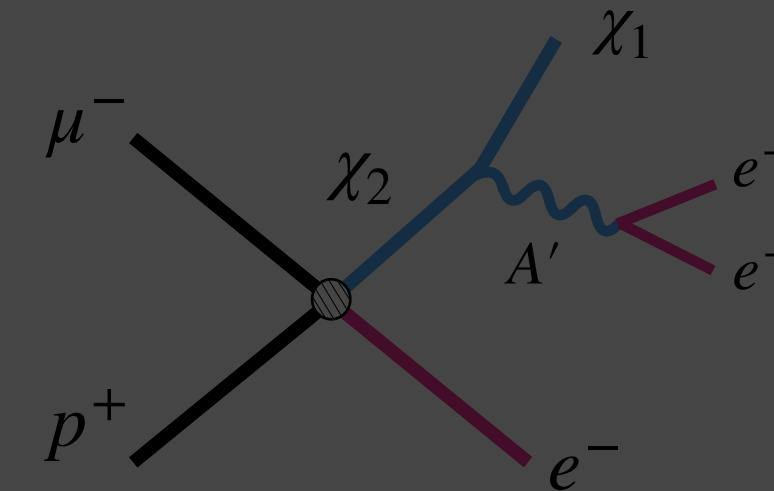
Dark Baryon Sector
 $\delta E_{e^+e^-} \lesssim m_p - m_0$



Dark Baryon Sector:
 $\delta E_{e^+e^-} \lesssim m_p - m_0$



Dark Baryon Sector:
 $\delta E_{e^-} \lesssim m_p - m_0$



Dark Baryon Sector:
 $\delta E_{e^+e^-} \lesssim m_p - m_1$

New light particles
at Mu2e/COMET

Harder spectrum
above μ DIO

Electron energy

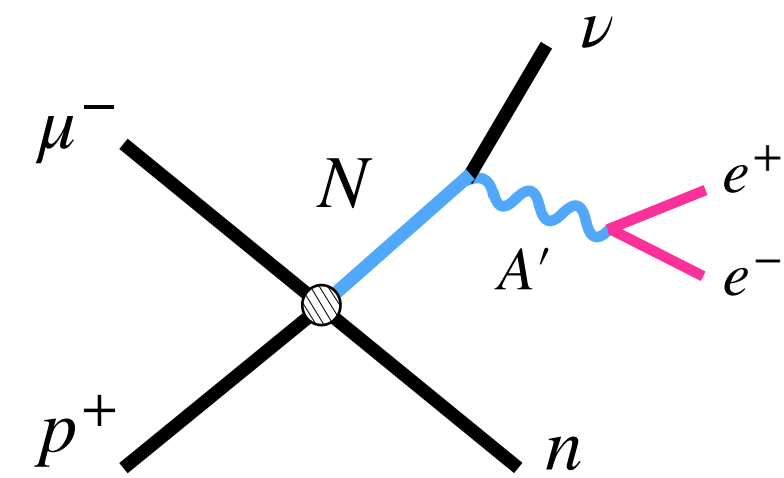
$$\delta E_{e^-} = E_{e^-} - m_\mu$$

B conservation

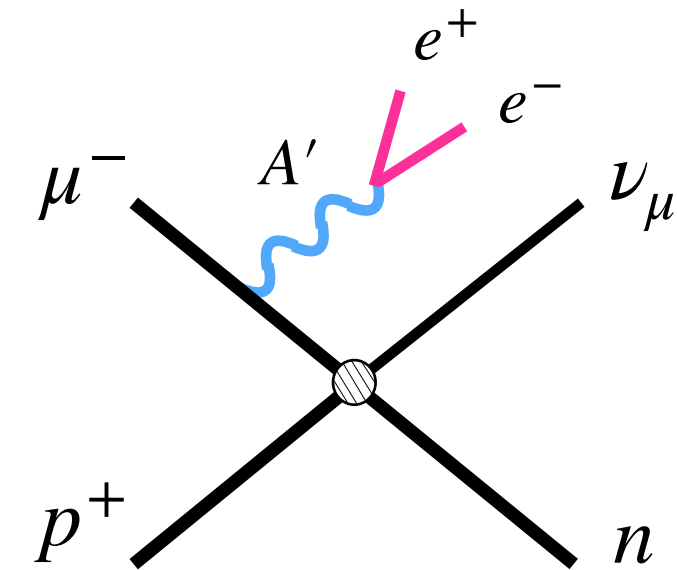
Apparent B Violating

LF Conserving

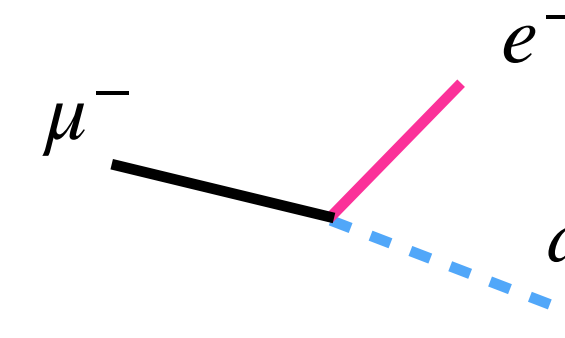
Apparent LF Violating



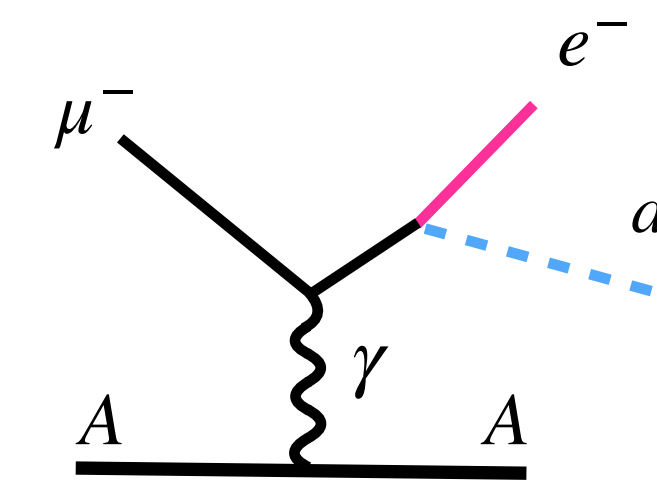
Heavy Neutral Leptons
 $\delta E_{e^+e^-} < 0$



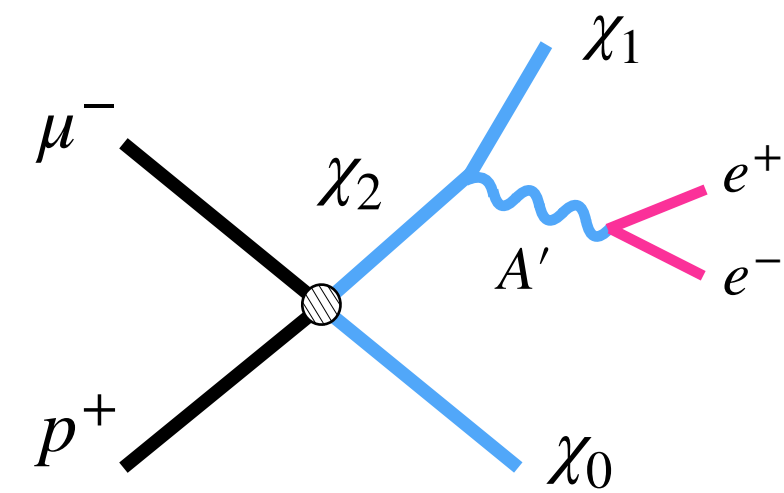
Dark Photons
 $\delta E_{e^+e^-} < 0$



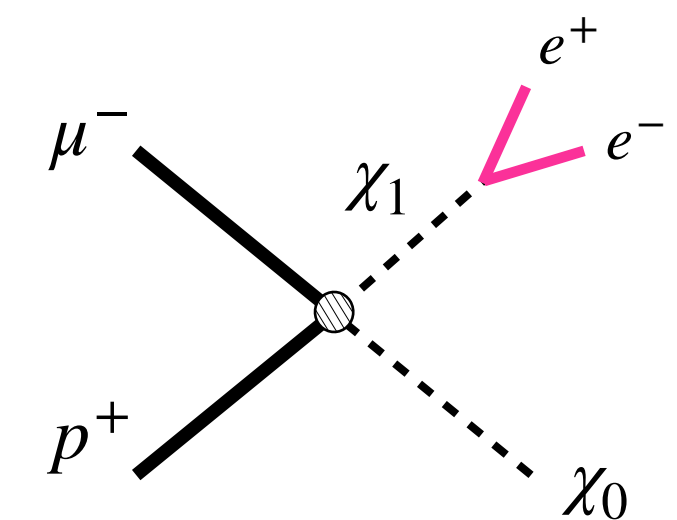
Decay-in-orbit
 $\delta E_{e^-} < 0$



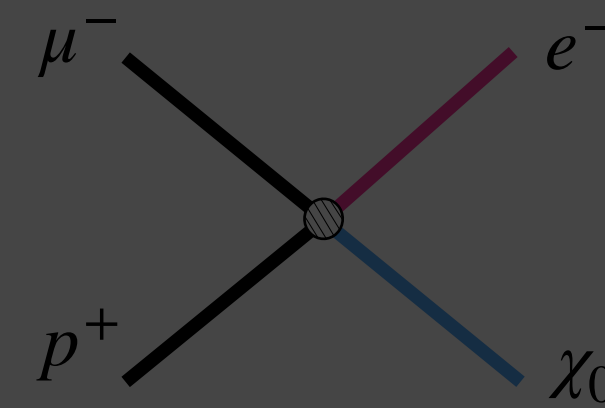
Axion-like-particles
 $\delta E_{e^-} < 0$



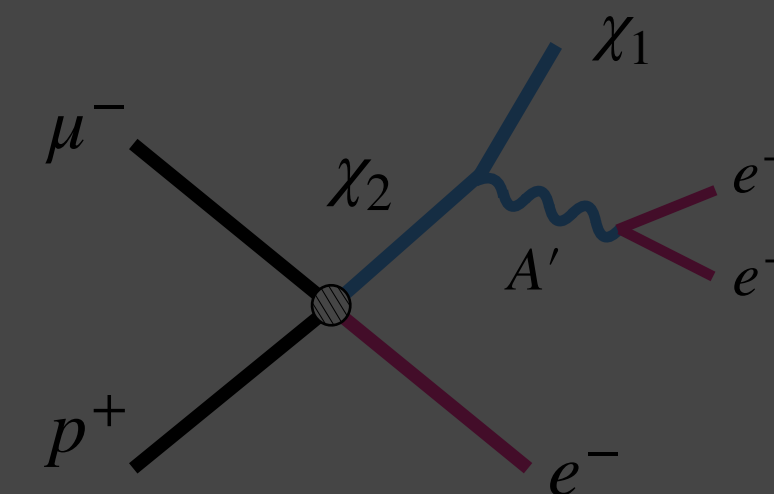
Dark Baryon Sector
 $\delta E_{e^+e^-} \lesssim m_p - m_0$



Dark Baryon Sector:
 $\delta E_{e^+e^-} \lesssim m_p - m_0$



Dark Baryon Sector:
 $\delta E_{e^-} \lesssim m_p - m_0$



Dark Baryon Sector:
 $\delta E_{e^+e^-} \lesssim m_p - m_1$

New light particles
at Mu2e/COMET

Harder spectrum
above μ DIO

Electron energy

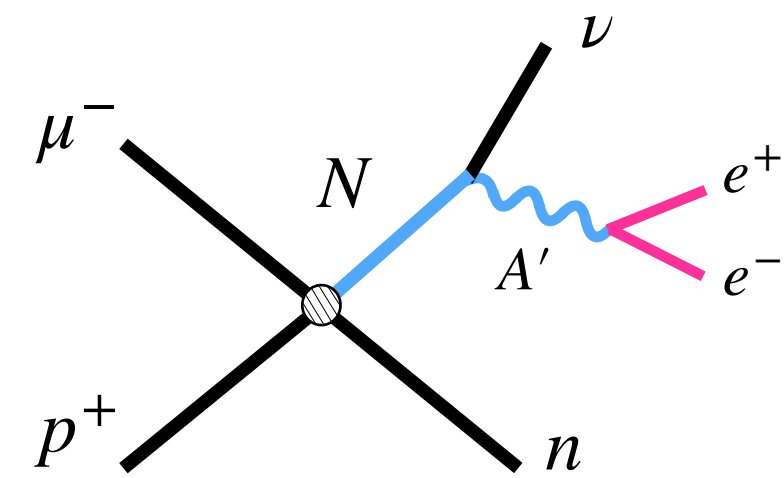
$$\delta E_{e^-} = E_{e^-} - m_\mu$$

B conservation

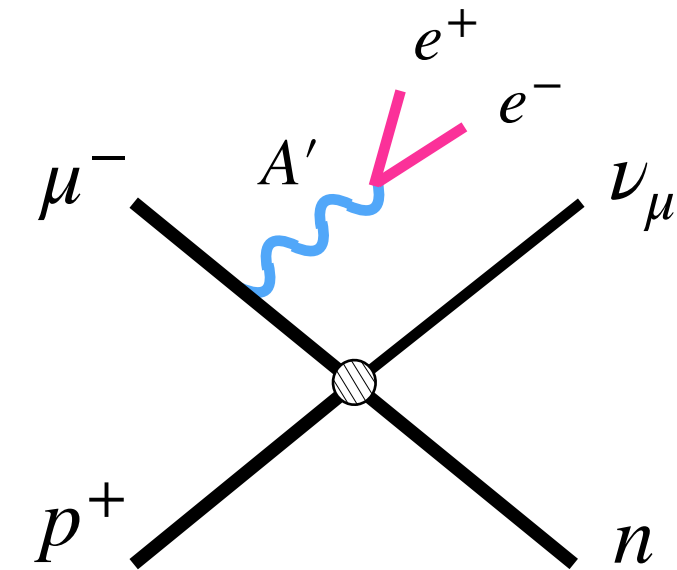
Apparent B Violating

LF Conserving

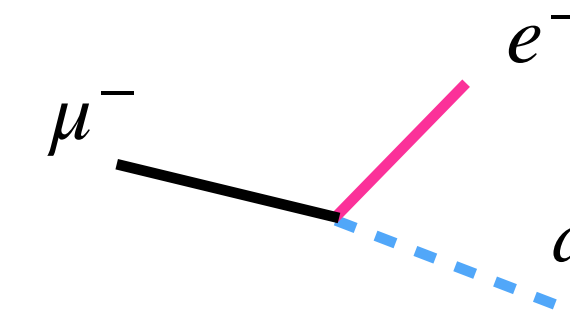
Apparent LF Violating



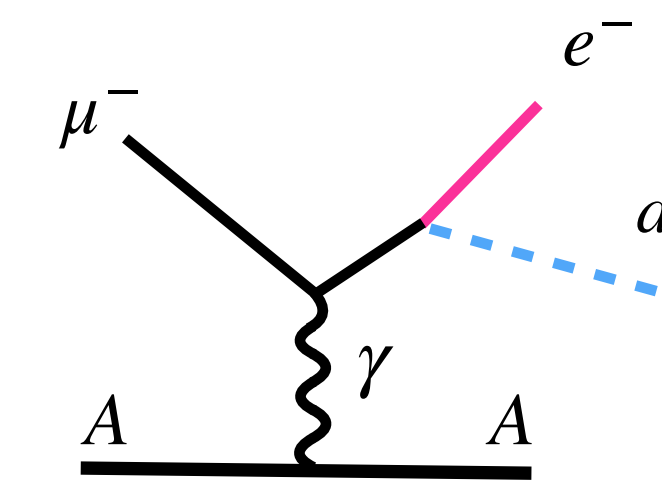
Heavy Neutral Leptons
 $\delta E_{e^+e^-} < 0$



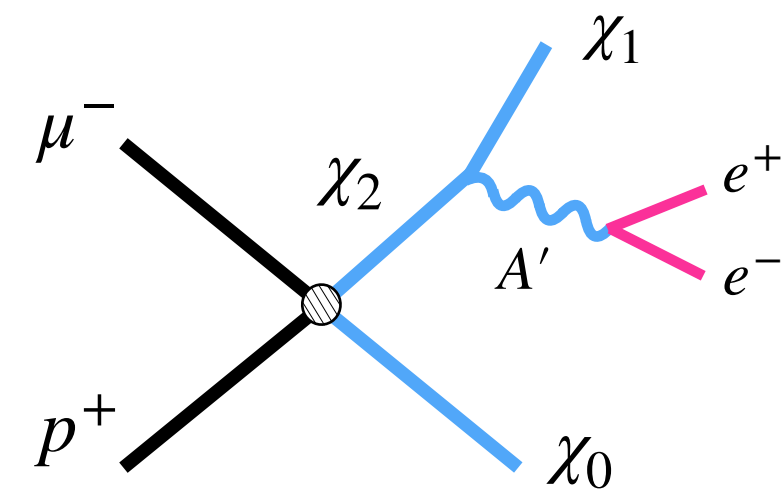
Dark Photons
 $\delta E_{e^+e^-} < 0$



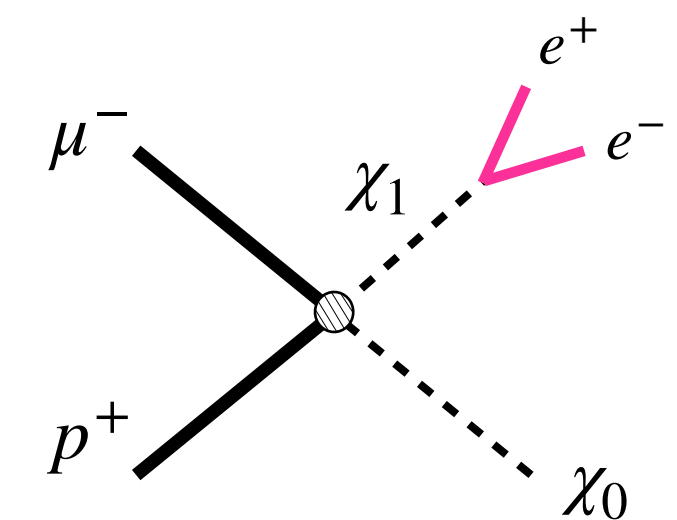
Decay-in-orbit
 $\delta E_{e^-} < 0$



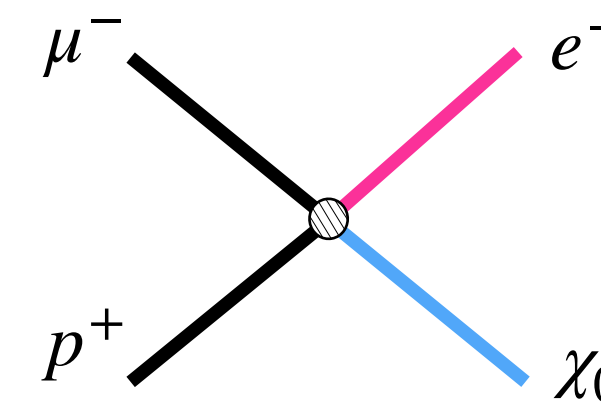
Axion-like-particles
 $\delta E_{e^-} < 0$



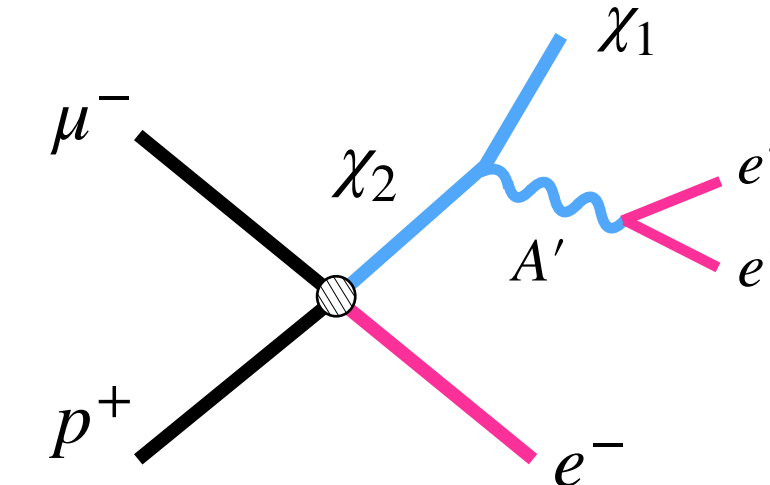
Dark Baryon Sector
 $\delta E_{e^+e^-} \lesssim m_p - m_0$



Dark Baryon Sector:
 $\delta E_{e^+e^-} \lesssim m_p - m_0$



Dark Baryon Sector:
 $\delta E_{e^-} \lesssim m_p - m_0$



Dark Baryon Sector:
 $\delta E_{e^+e^-} \lesssim m_p - m_1$

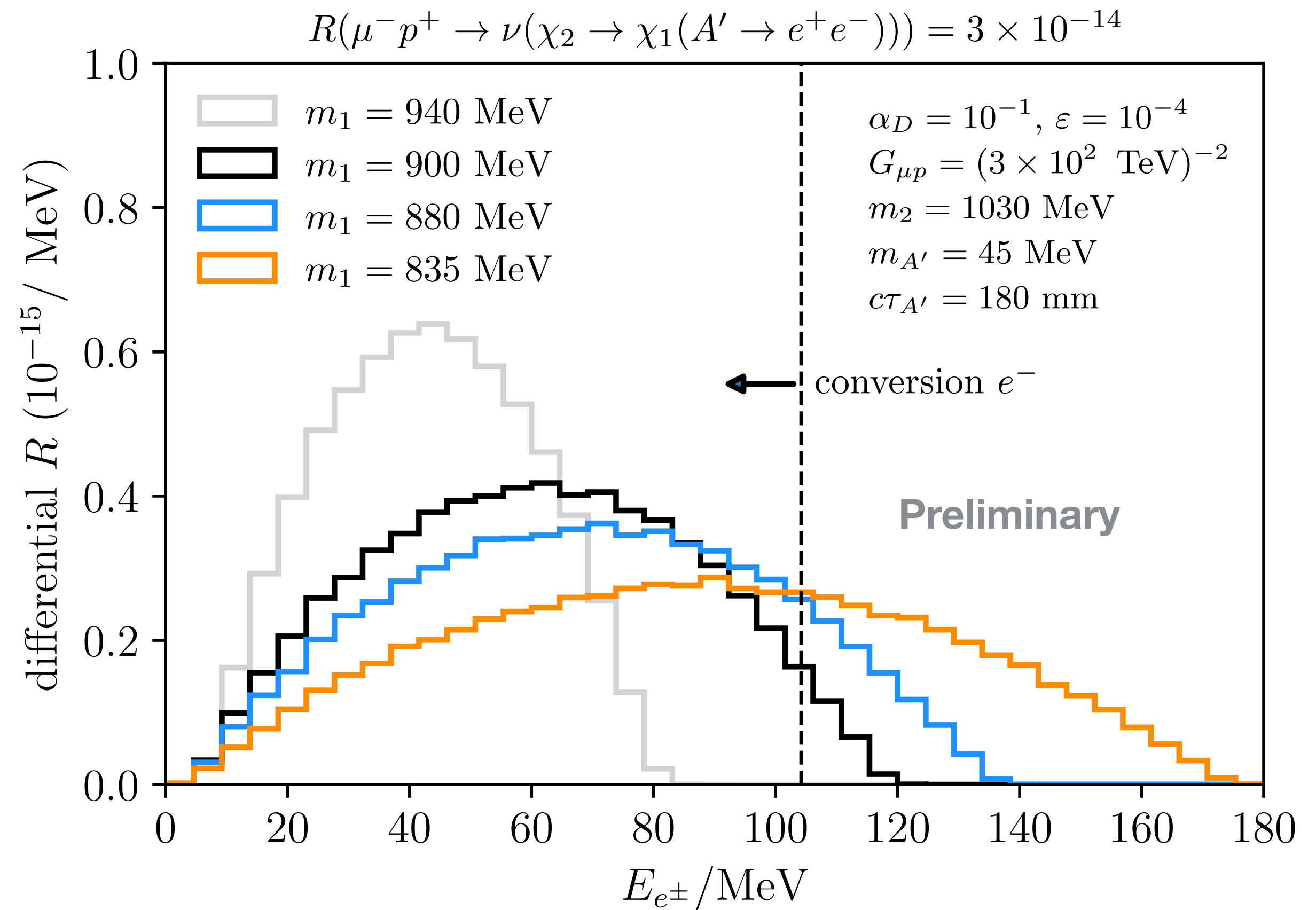
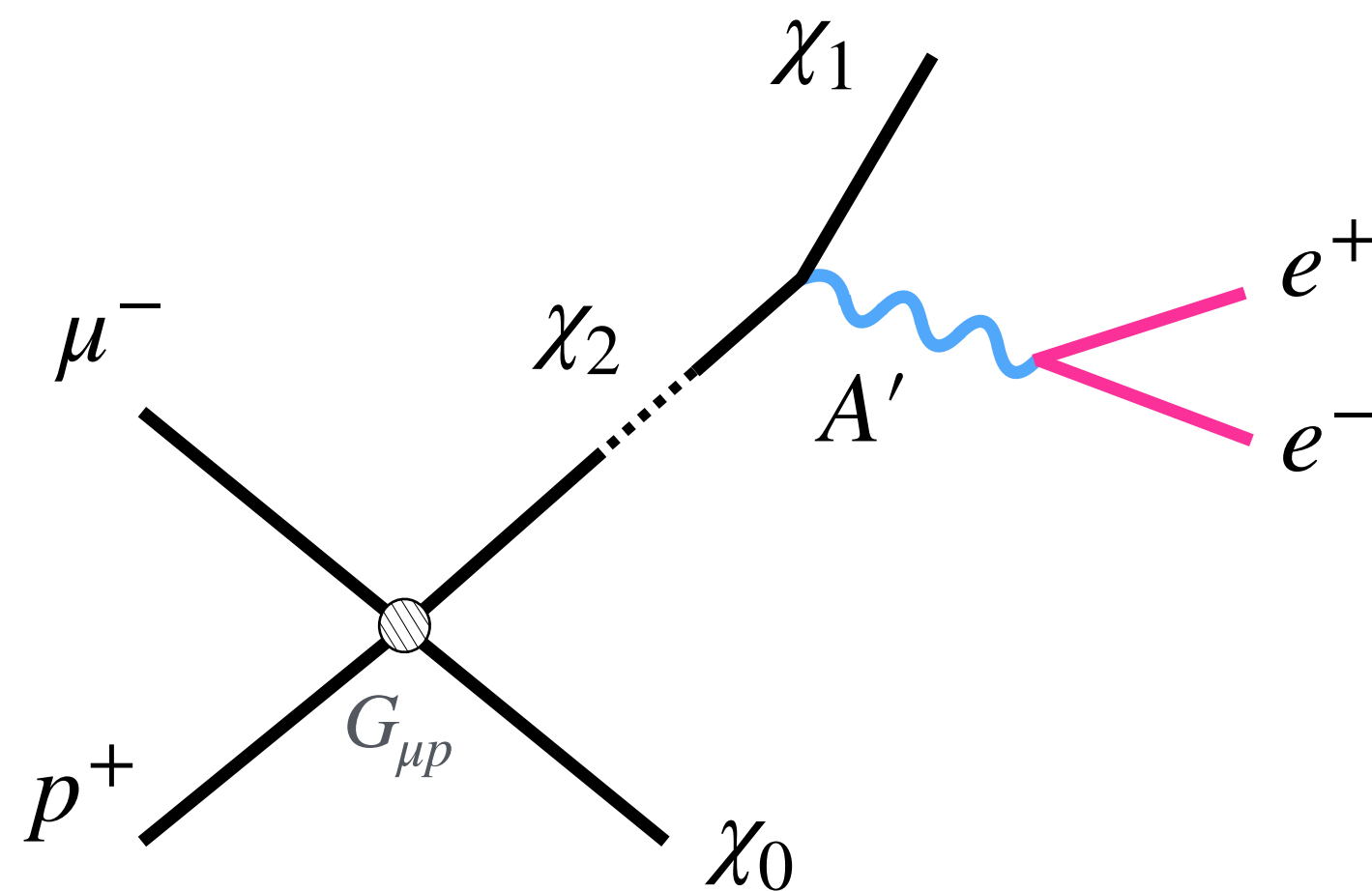
Dark particle production in $\mu \rightarrow e$ conversion

Borrowing energy from the proton

P. Fox, MH, T. Menzo, M. Pospelov, J. Zupan (in progress)

Consider new dark particles χ_2, χ_1 , and χ_0 . Schematically:

$$\mathcal{L} \supset G_{\mu p}(\bar{\mu}\chi_2)(\bar{p}\chi_0) + A'_\mu (g_D\bar{\chi}_2\gamma^\mu\chi_1 + e\varepsilon J_{\text{EM}})$$



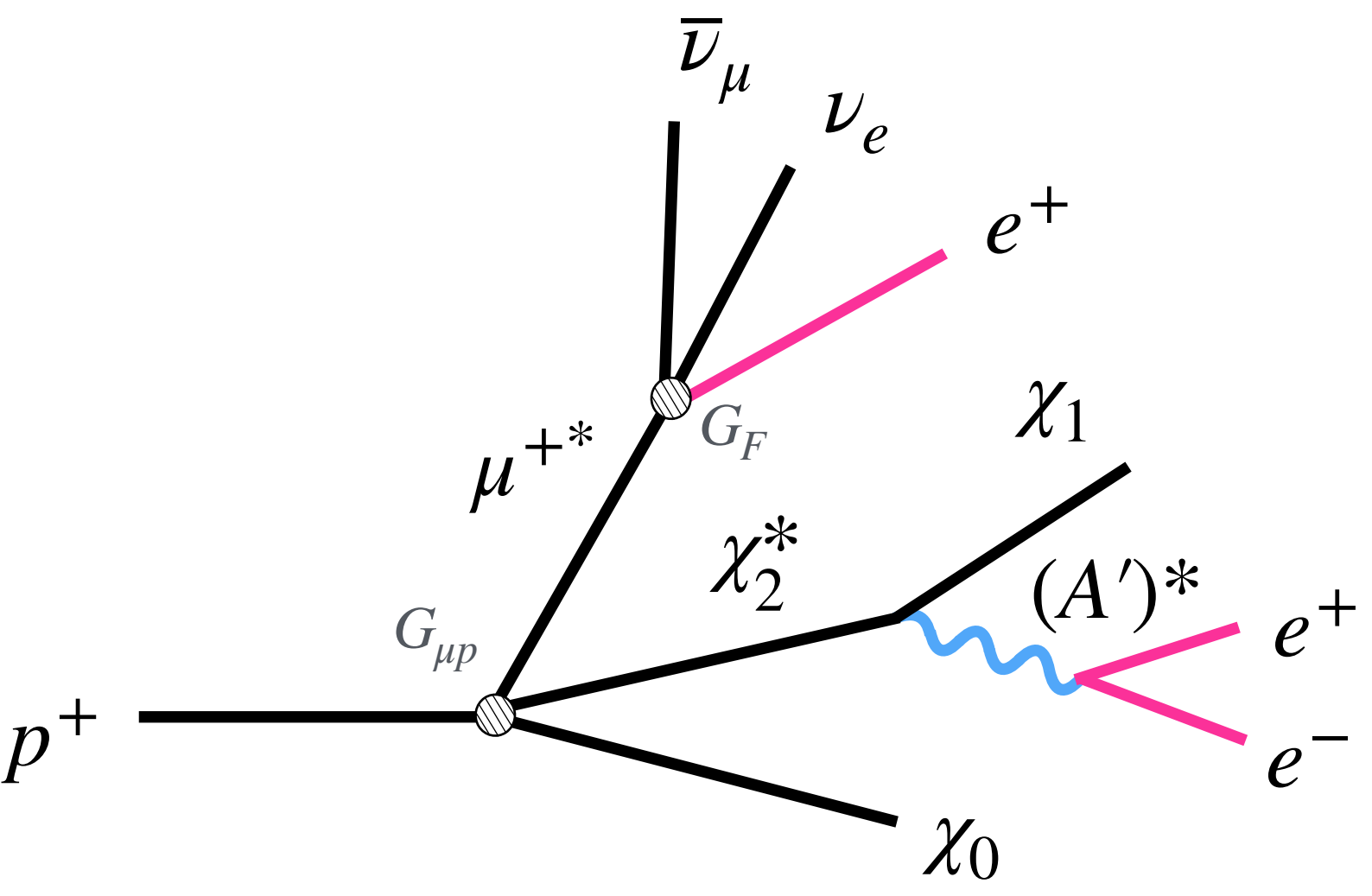
Challenge 1) Proton decay

Suppression by fine tuning the spectrum

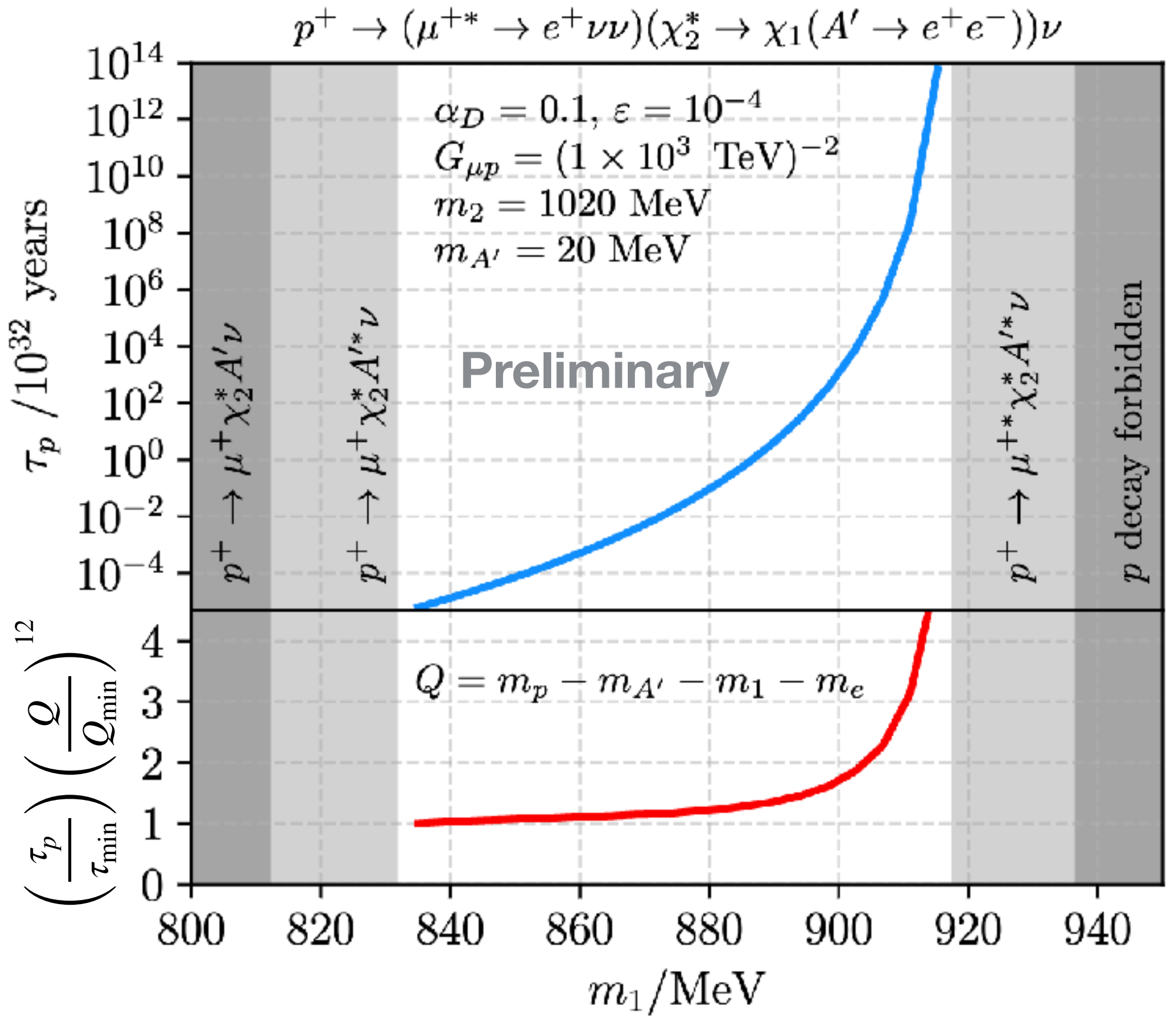
P. Fox, MH, T. Menzo, M. Pospelov, J. Zupan (in progress)

Proton decay is suppressed by “off-shellness” and the small Q -value.

Even if $\tau_p \sim 10^{32}$ years, not excluded as protons decay to very soft tracks.



Proton decay to 7 particles via **off-shell** μ^+ and χ_2 (possibly A')



Challenge 2) Neutron stars

Muon capture leads to a new equilibrium

P. Fox, MH, T. Menzo, M. Pospelov, J. Zupan (in progress)

The core of a Neutron Star may have as much as 5% of its particle number in muons.

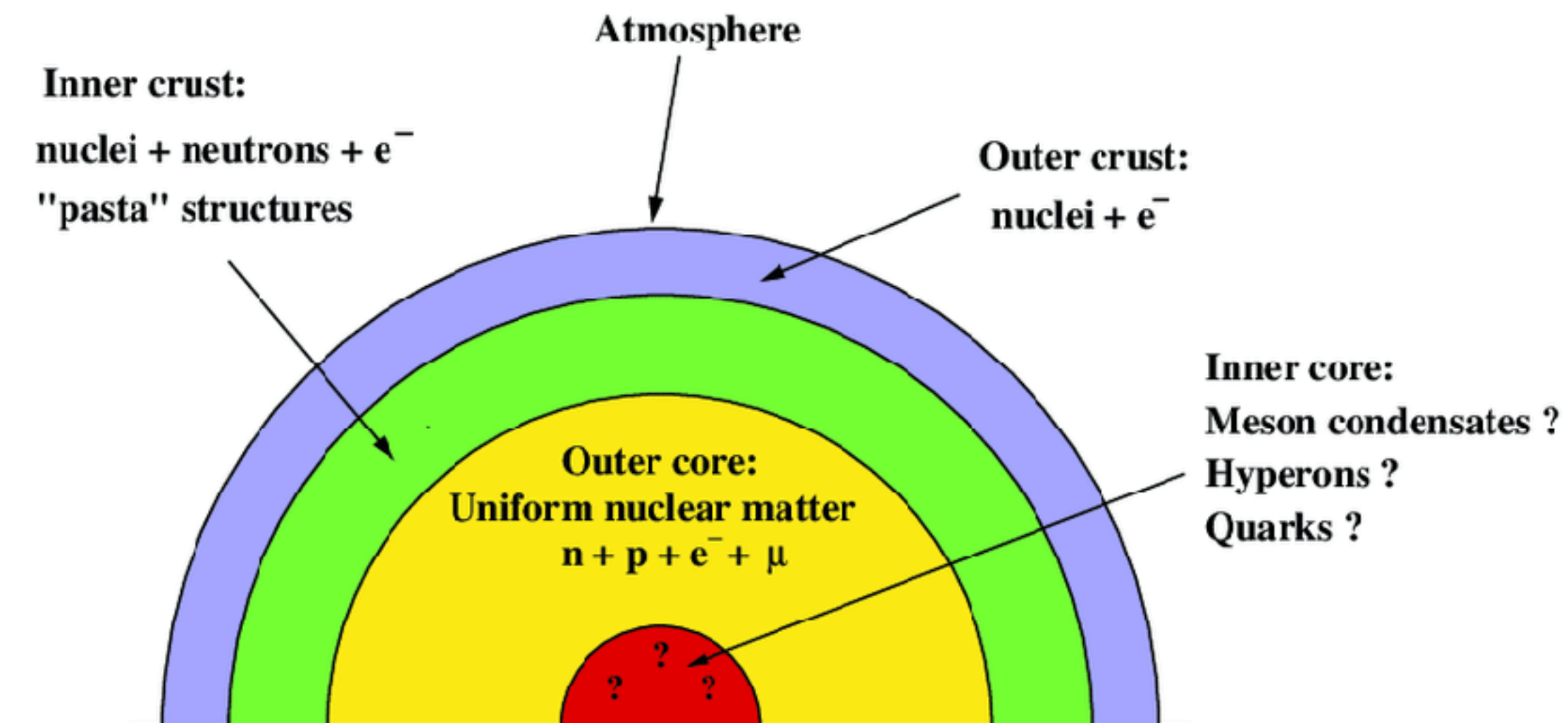
The muons in the Neutron Star will destroy protons/neutrons

This process happens “fast” in the history of the star

$$\Gamma_{\mu^- p^+ \rightarrow \chi_1 \chi_2}^{\text{NS}} = \langle \sigma_{\mu p} v \rangle n_p \simeq \Gamma_{\mu^- p^+}^{\text{Lab}} \frac{n_p}{|\psi(0)|^2} > \frac{1}{10^6 \text{ s}}$$

A new equilibrium is then found and the pressure drops.

To support observed mass-radius relations,
 χ_1 particles must have self-interactions.



Charged Lepton Flavor Violation is exotic enough and we are looking for it hard enough that new particles, light or heavy, may be first discovered through their flavor-violating couplings.

1) Suggested an additional muon decay target for Mu3e: $\mu \rightarrow 5e$ within and beyond the SM.

2) Sensitivity to new physics scale can be as strong as $\Lambda \sim 10^7/10^{15}$ GeV.

3) Measurement of the SM rate is more challenging, but may not be impossible.

4) New speculations for $\mu \rightarrow e$: tap into baryonic energy reservoir in muon capture

5) Experimental implication: spectrum of e^- as well as e^+ with higher energy endpoint.

Back-up slides

Rare muon decays at Mu3e

Relaxing requirements to just 2 electrons?

MH, T. Menzo, M. Pospelov, J. Zupan, [JHEP 10 \(2023\) 006](#)

