

# Minimal Dark Matter Freeze-in with Low Reheating Temperatures (Implications for Direct Detection)

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Texas A&M**

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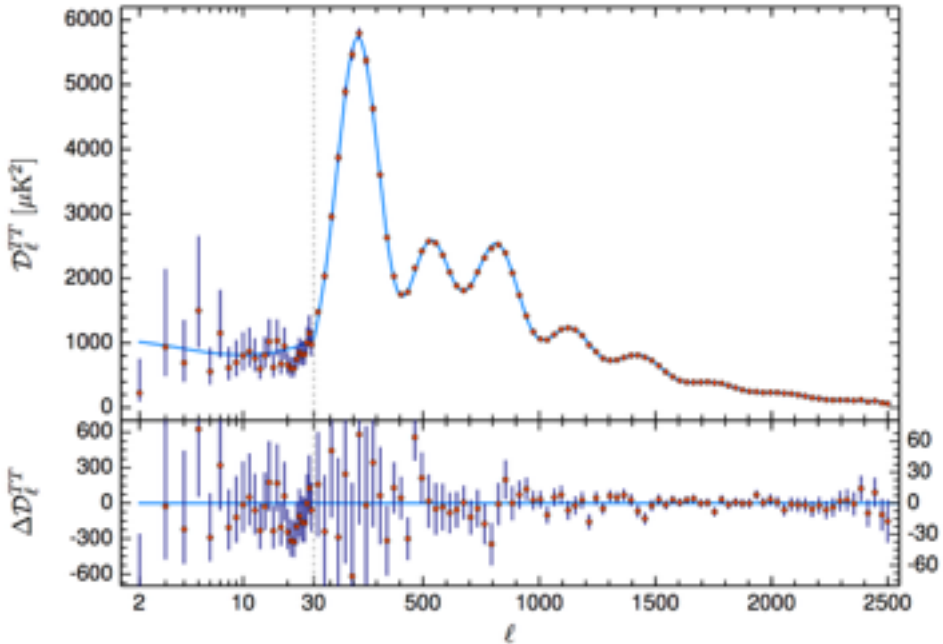
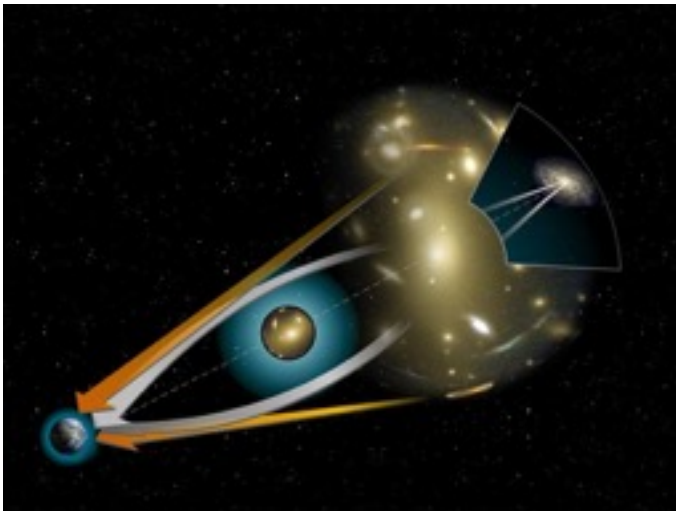
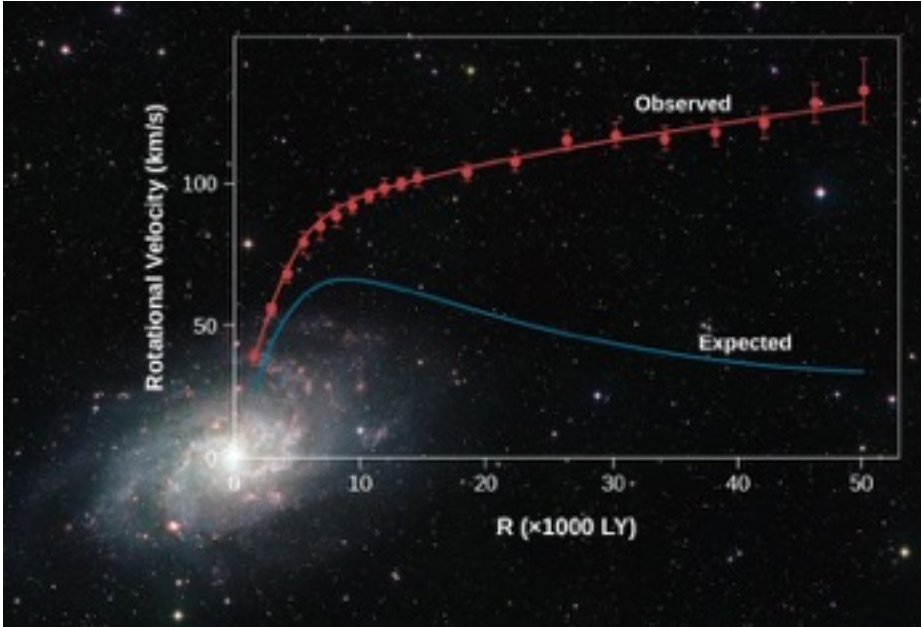
# Evidence for Dark Matter from all scales: Gravitational Interaction

Rotation Curves of Galaxies

Gravitational Lensing

Structure Formation

Cosmic Microwave Background (CMB)

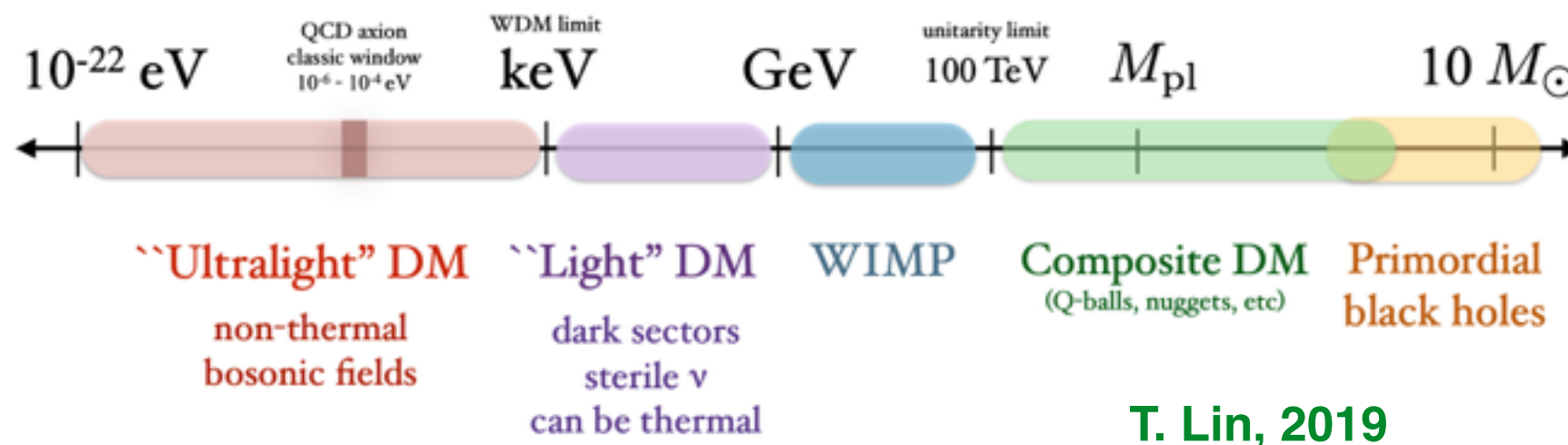


# Nature of Dark Matter?

our knowledge is limited:

DM can be explained by candidates with a mass range spanning over 90 orders of magnitude.

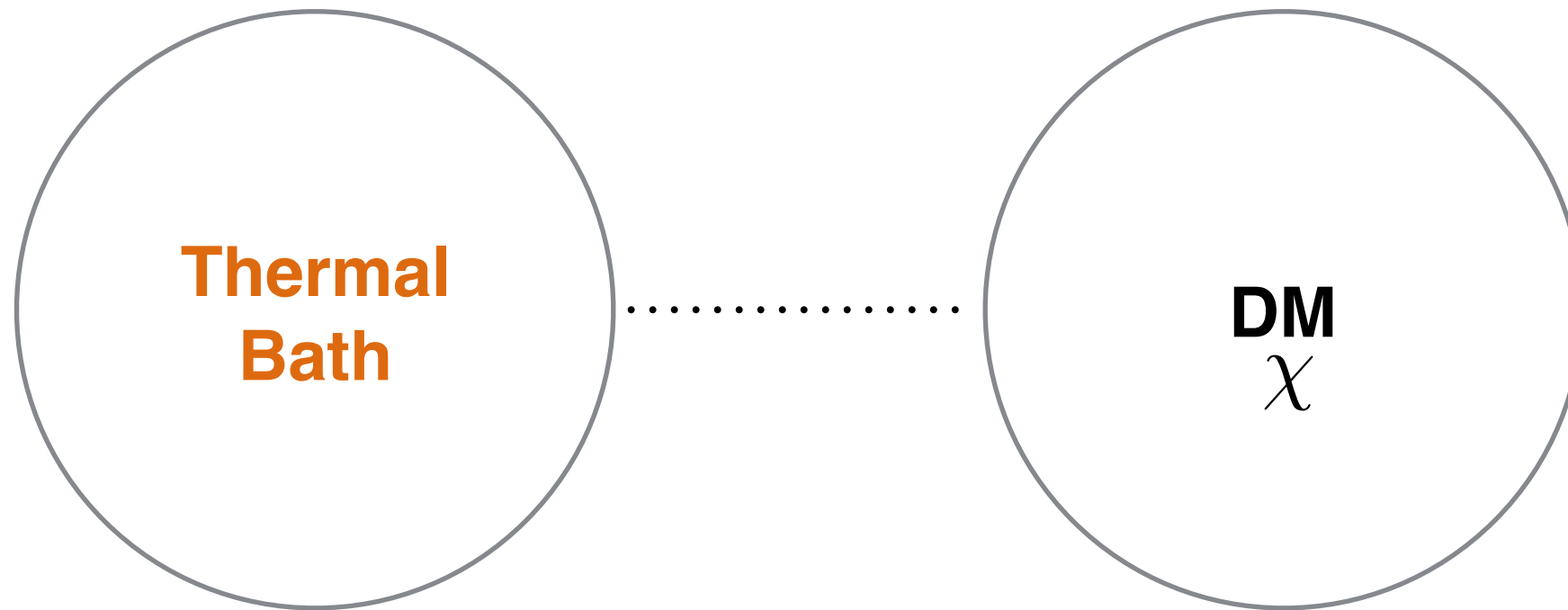
each model can only be partially constrained.



**Ultimate goal:**

**Direct detection of DM through non-gravitational interactions!**

A well-studied approach to produce DM:  
through interaction with the Standard Model **thermal bath**.



depending on the interaction:  
DM abundance is mainly established by  
**freeze-out** or **freeze-in** mechanisms.

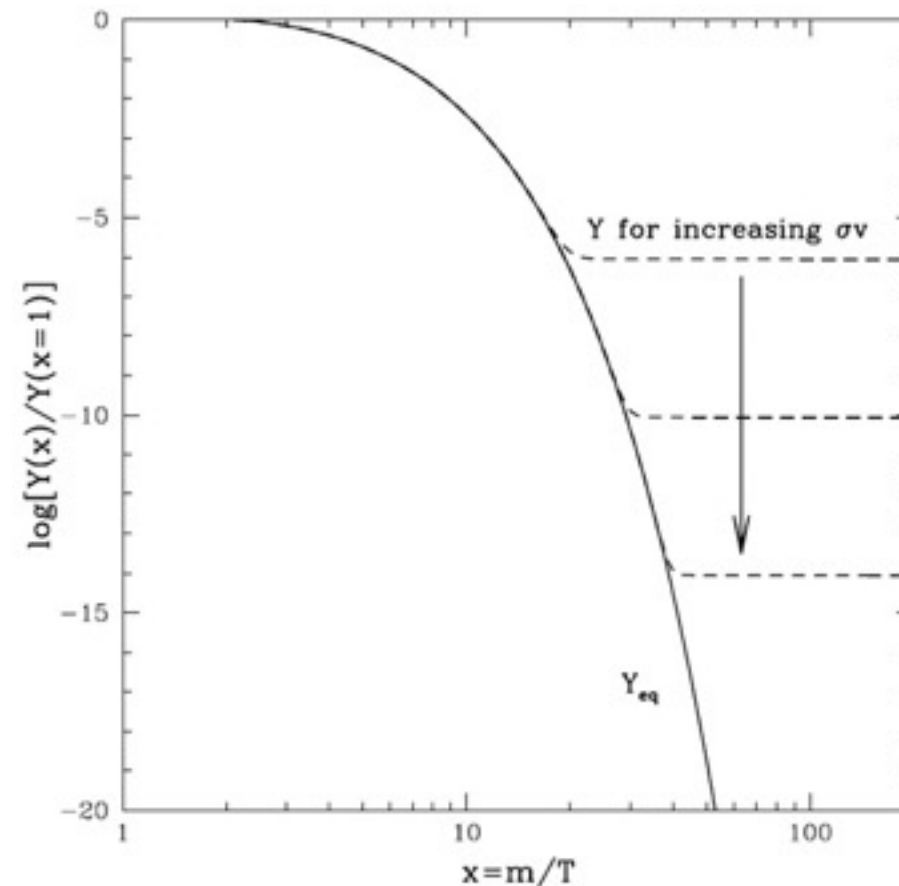
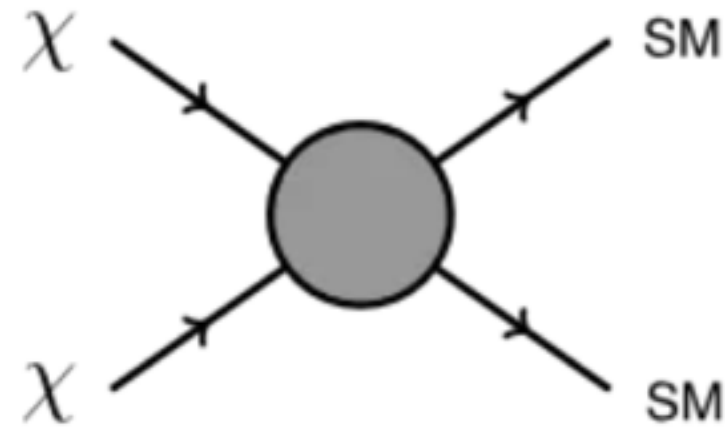
# Freeze-out:

$$\dot{n}_\chi + 3Hn_\chi = -\langle\sigma v\rangle (n_\chi^2 - n_{\chi,\text{eq}}^2)$$

Due to thermalization:  
no dependence on the initial  
temperature of the bath

## Example:WIMPs

**weak-scale couplings,  
weak scale mass**



# WIMPs: benchmark targets for direct detection experiments

## Nuclear recoil

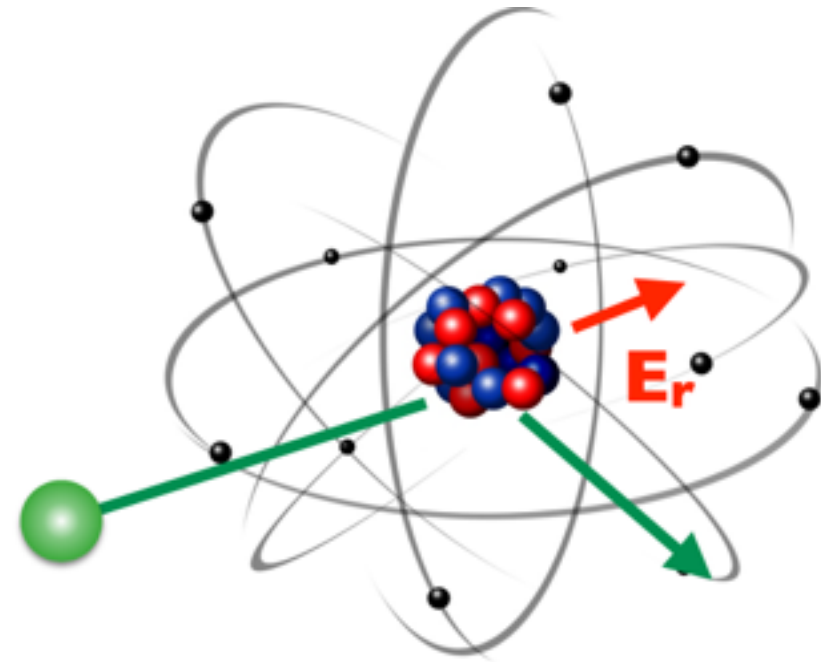
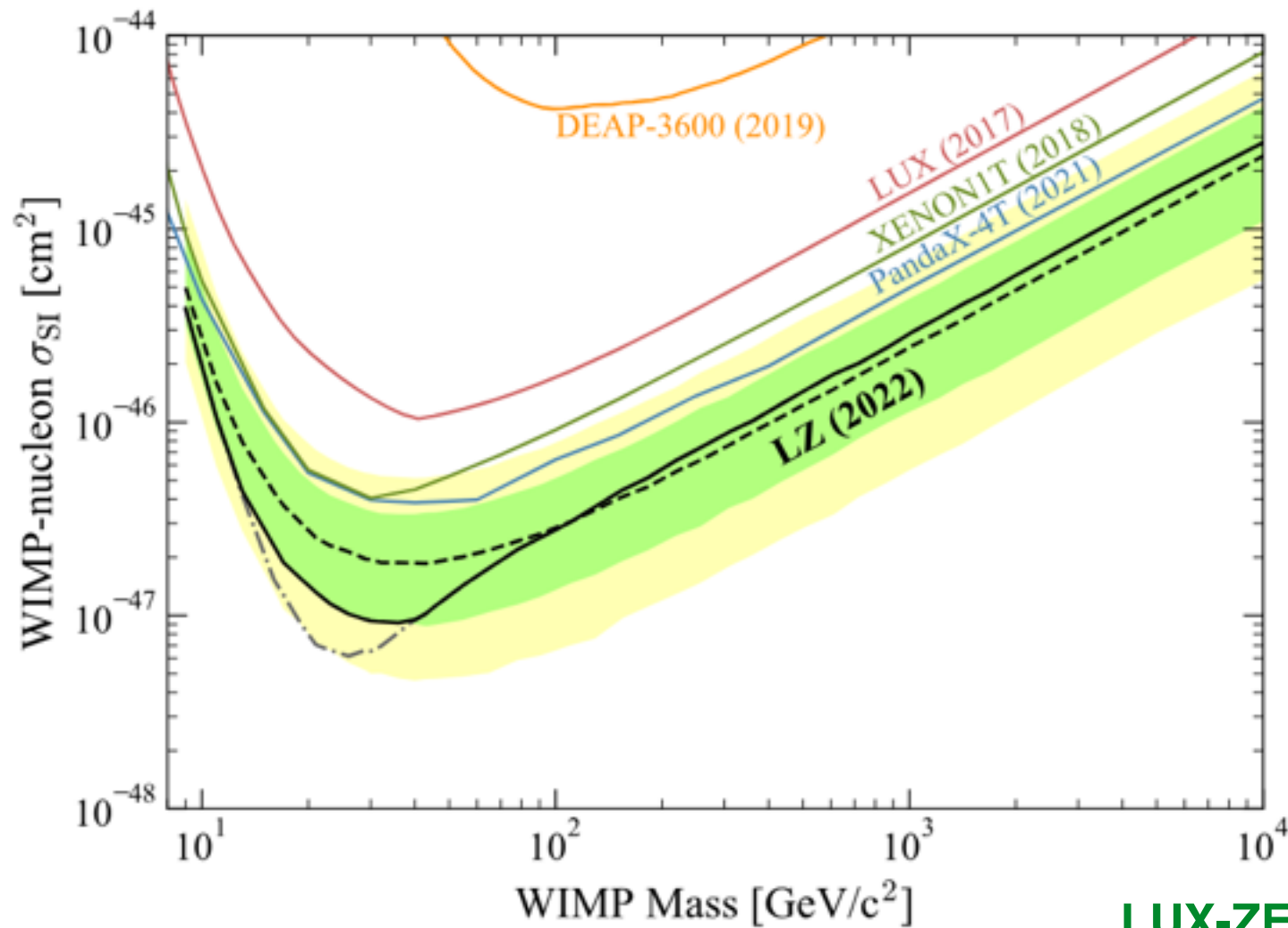


image credit: Carmen Carmona



LUX-ZEPLIN (LZ) Experiment, 2022

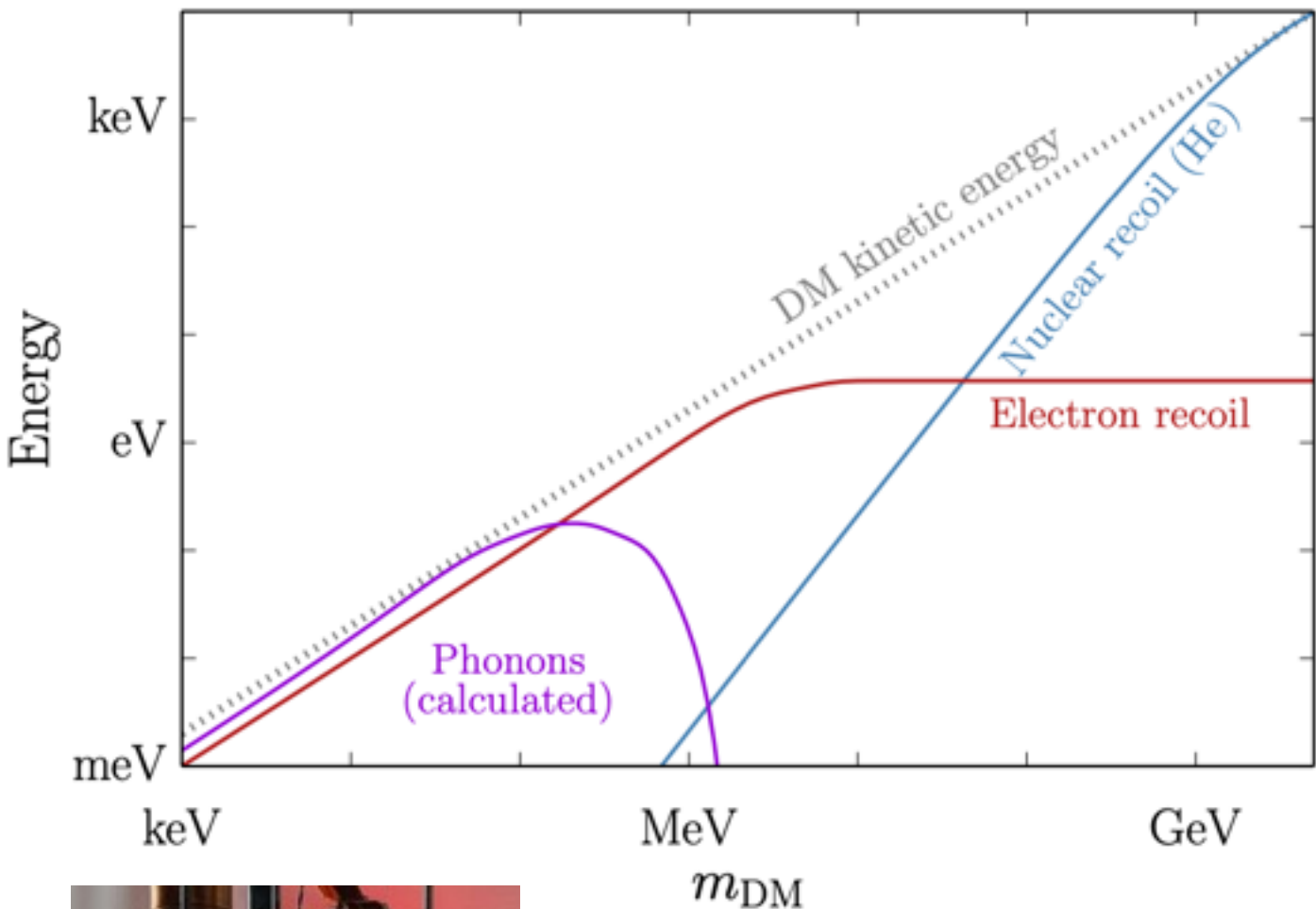
DM signal: a recoil rate that exceeds  
the detector-internal background

multi-ton-scale target masses

a clear path for even larger  
detectors to reach the neutrino fog



# Direct detection of Sub-GeV DM:



T. Lin, 2019

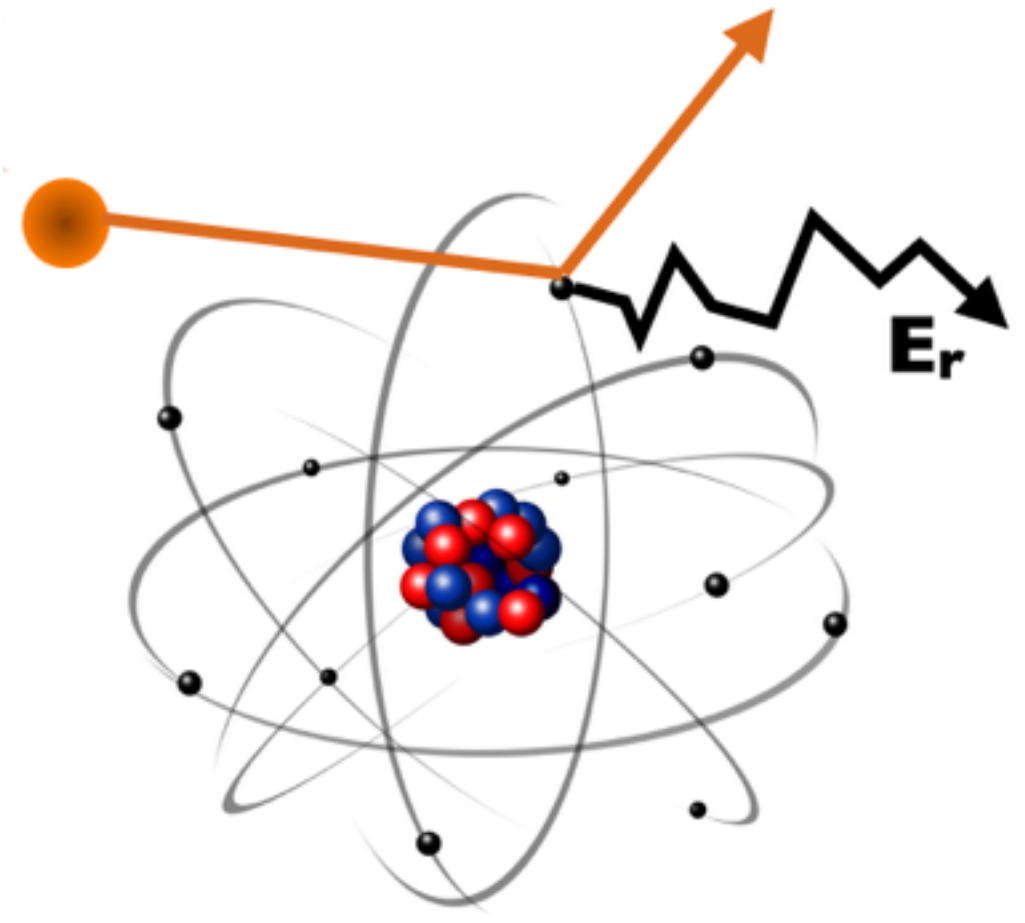


image credit: Carmen Carmona

Electron recoil

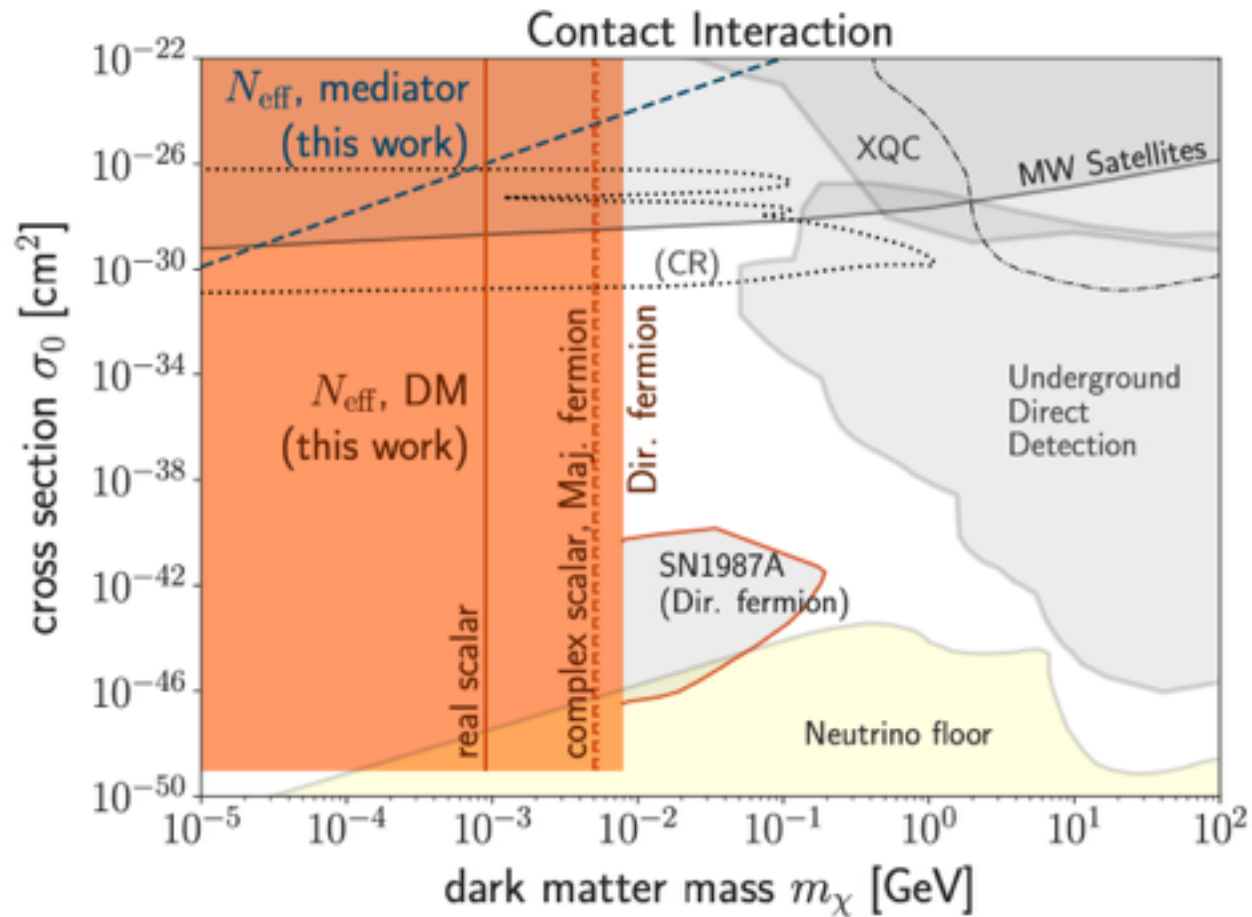


SENSEI collaboration

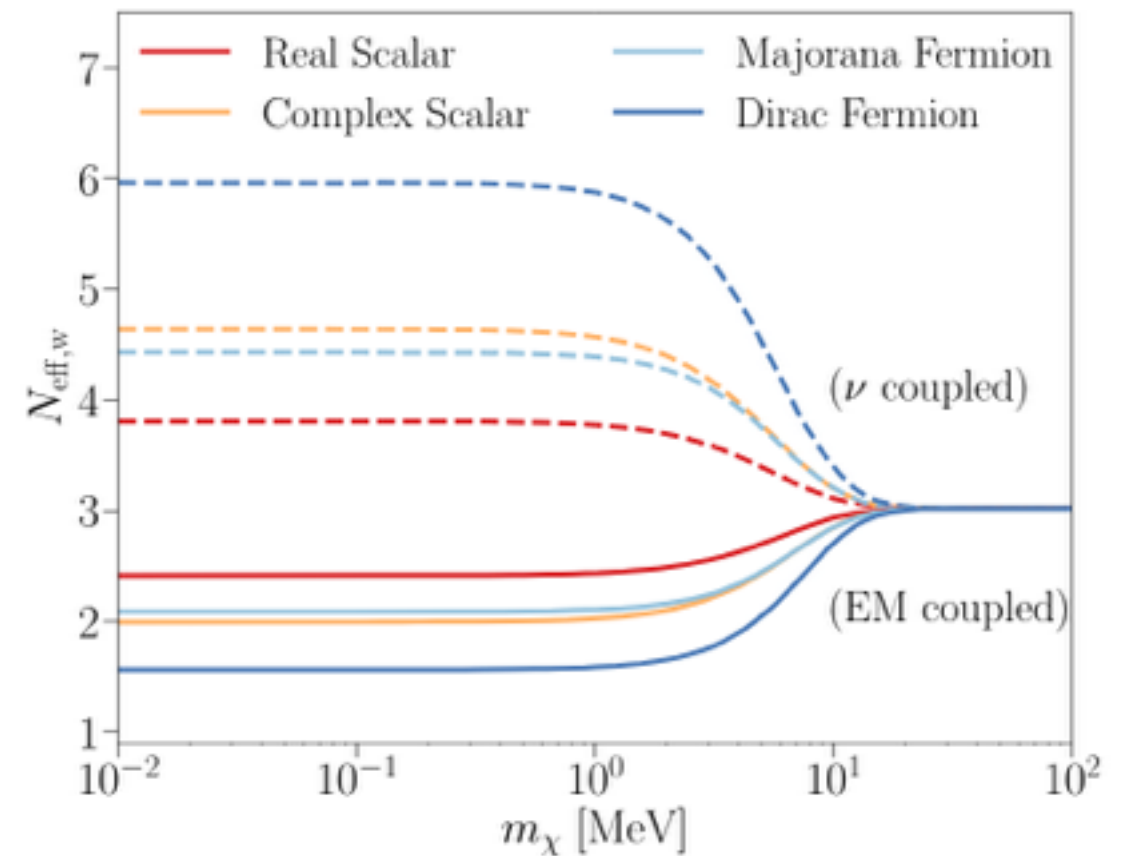
Cutting-edge technologies!

# Thermal production of MeV DM is disallowed by BBN

light DM requires dark sectors



G. Krnjaic, S. D. McDermott, 2019



R. An, V. Gluscevic, E. Calabrese, J. C. Hill, 2022

**Alternative: freeze-in!**



# Freeze-in:

the DM final abundance is built up gradually over time

$$\dot{n}_\chi + 3Hn_\chi = -\langle\sigma v\rangle (n_\chi - n_{\chi,\text{eq}})$$

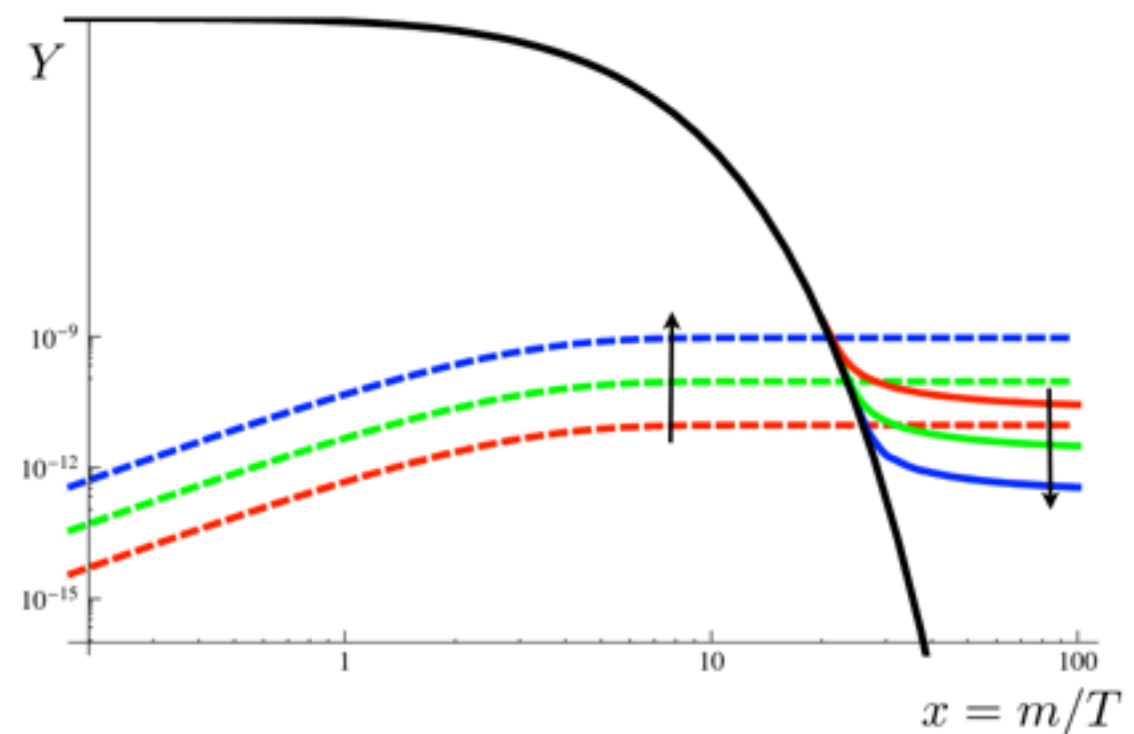
renormalizable operators and very small coupling

$$\lambda \ll 1 \quad Y_\chi \sim \lambda^2 \frac{m_{\text{Pl}}}{T} \sim \lambda^2 \frac{m_{\text{Pl}}}{m_\chi}$$

L. J. Hall, K. Jedamzik, J. March-Russell, S. M. West, 2009

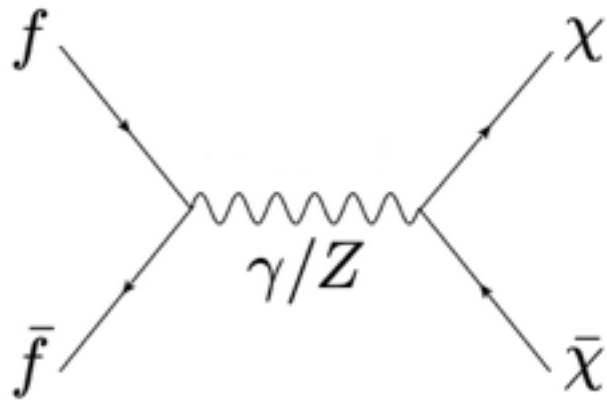
# IR freeze-in:

insensitive to temperatures above DM mass



# Benchmark freeze-in model:

$$\mathcal{L} \supset \frac{\epsilon}{2} F'_{\mu\nu} F^{\mu\nu}$$



L. J. Hall, K. Jedamzik, J. March-Russell, S. M. West, 2009

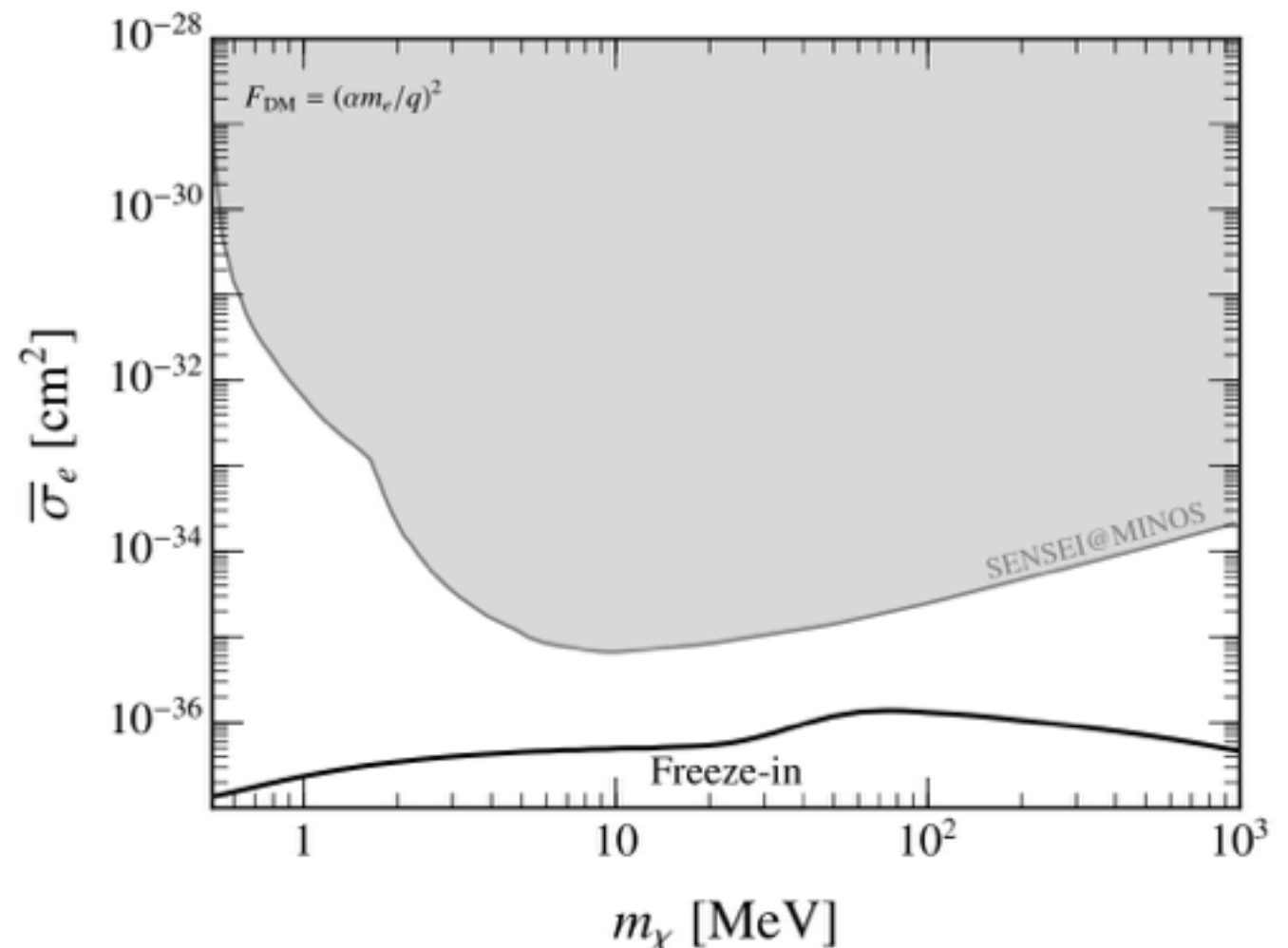
X. Chu, T. Hambye, M. H. G. Tytgat, 2012

R. Essig, J. Mardon, T. Volansky, 2012

Freeze-in model:  
extraordinarily **small coupling** between  
the DM and the SM.

Despite this, **the ultralight mediator** leads to  
a large enhancement of the direct detection  
cross section at low momentum transfers.

**target of  
direct detection program!**

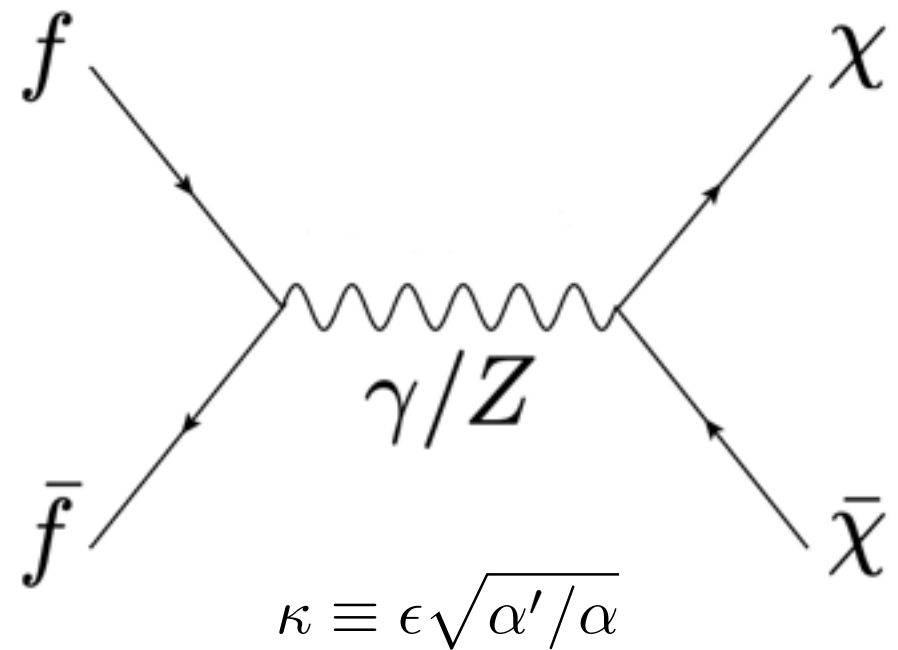


# Relic abundance:

$$\dot{n}_\chi + 3Hn_\chi = \sum_B \langle \sigma_{B\bar{B} \rightarrow \chi\bar{\chi}} v \rangle (n_\chi^{\text{eq}})^2$$

$$Y_\chi(x) = \int_{x_{\text{rh}}}^x dx' \frac{s}{Hx'} \left[ \sum_B \langle \sigma_{B\bar{B} \rightarrow \chi\bar{\chi}} v \rangle (Y_\chi^{\text{eq}})^2 \right]$$

$$x \equiv m_\chi/T$$



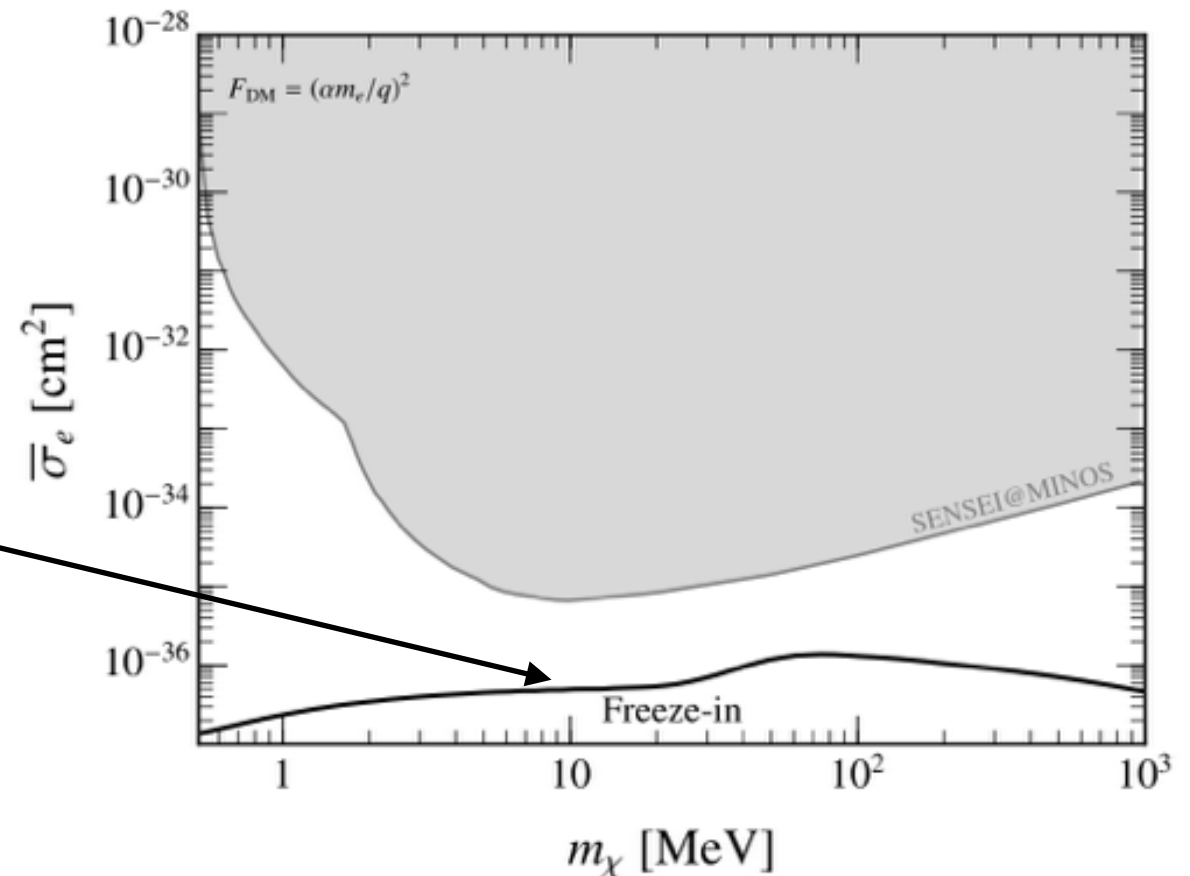
## Previous studies:

$$T_{\text{rh}} \gg m_\chi : x_{\text{rh}} = 0$$

$$\text{fixed } m_\chi : \Omega_\chi = \Omega_{\text{CDM}}$$

→ unique  $\kappa(m_\chi)$  → unique  $\bar{\sigma}_e(m_\chi)$

$$\bar{\sigma}_e = \frac{16\pi\mu_{\chi e}^2\alpha^2\kappa^2}{(\alpha m_e)^4}$$



but reheating temperature can be below the mass!

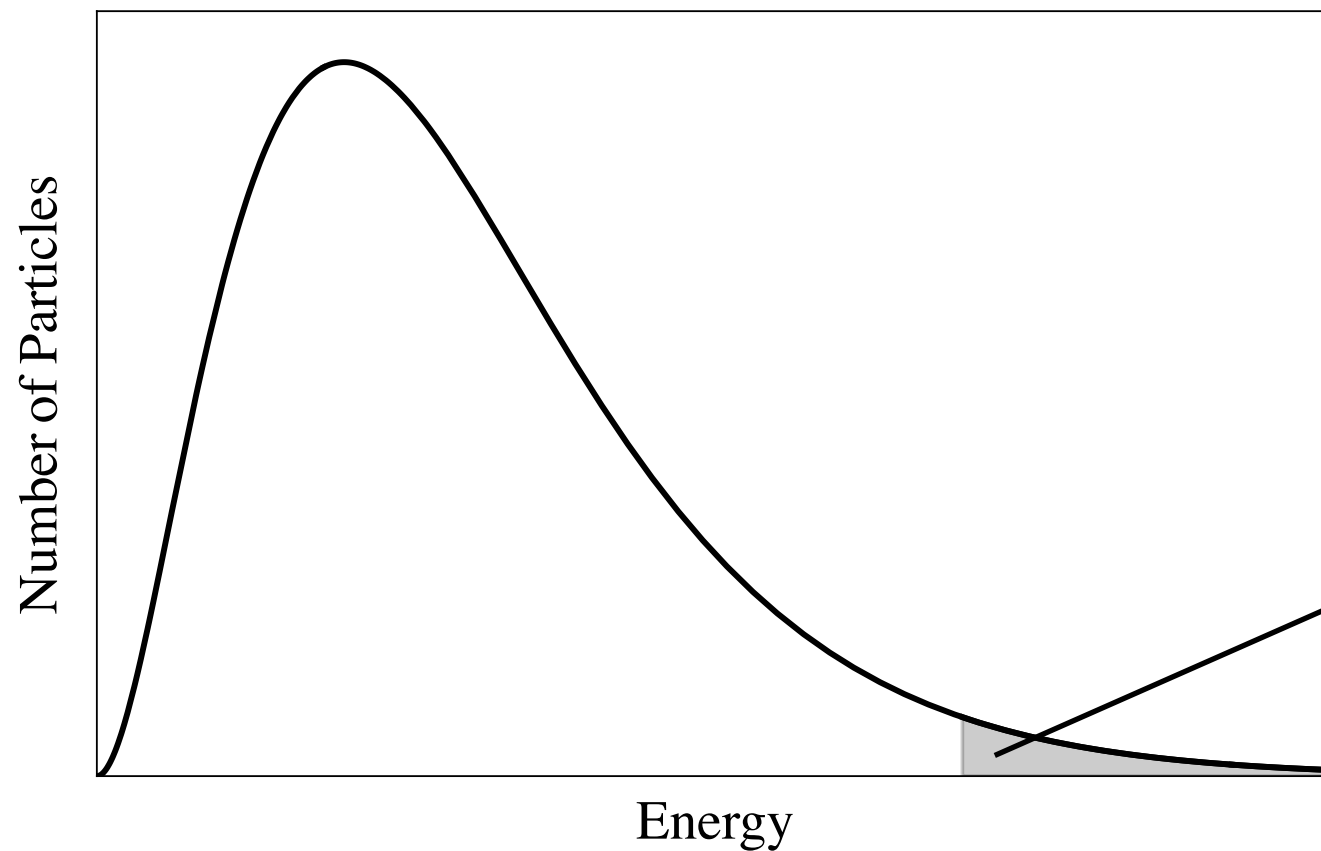
# Impact of reheating temperature:

$$5 \text{ MeV} \lesssim T_{\text{rh}} \ll m_\chi$$

V. A. Kuzmin, V. A. Rubakov, 1998

$$\Gamma_{\text{production}} \sim e^{-2m_\chi/T}$$

C. Cosme, F. Costa, O. Lebedev, 2023

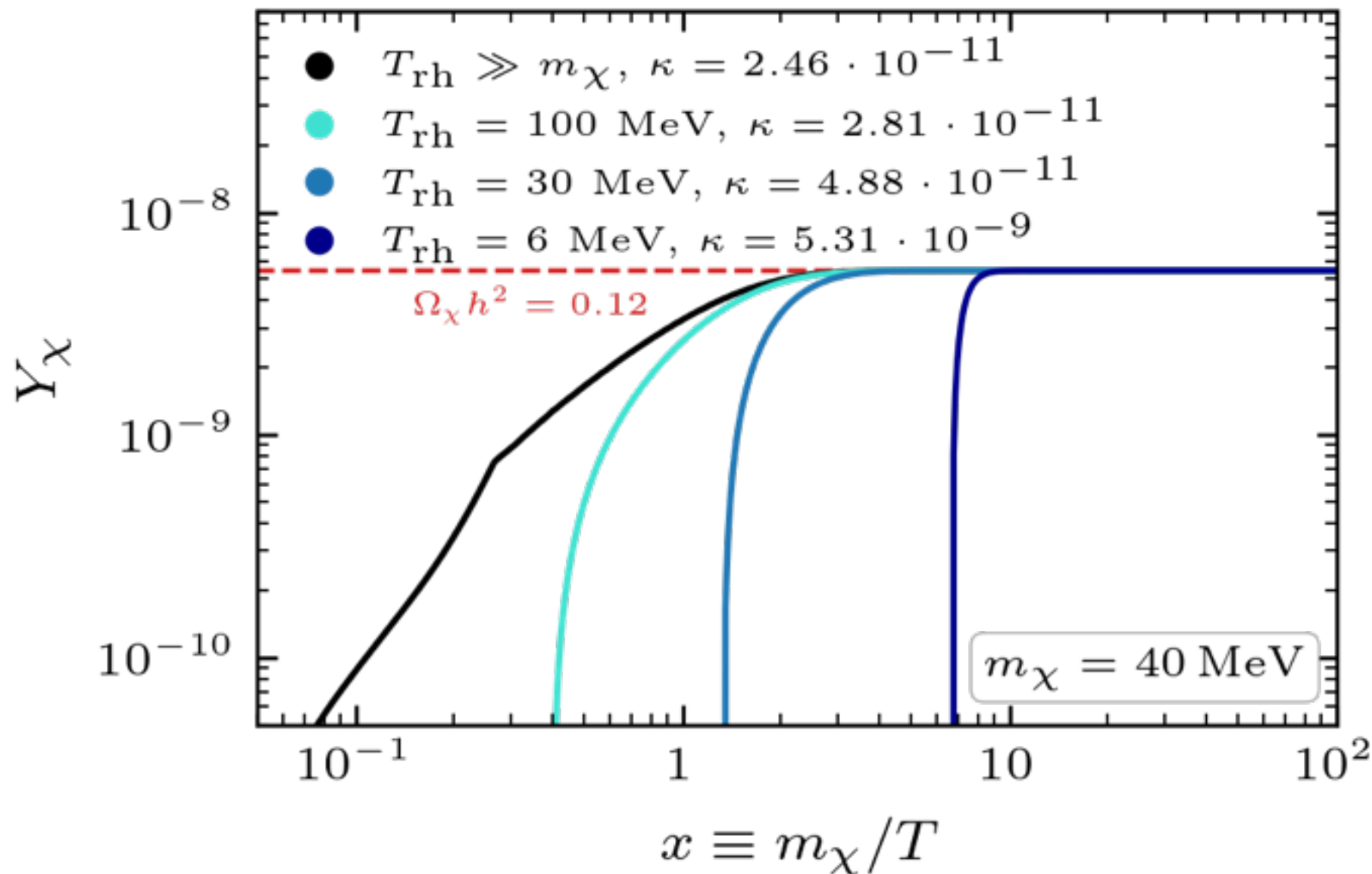
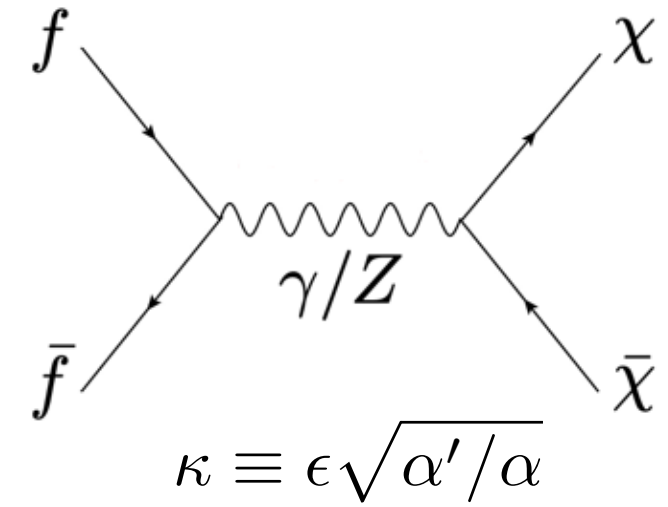


$$Y_\chi(x) = \int_{x_{\text{rh}}}^x dx' \frac{s}{Hx'} \left[ \sum_B \langle \sigma_{B\bar{B} \rightarrow \chi\bar{\chi}} v \rangle (Y_\chi^{\text{eq}})^2 \right]$$

to match the relic abundance:

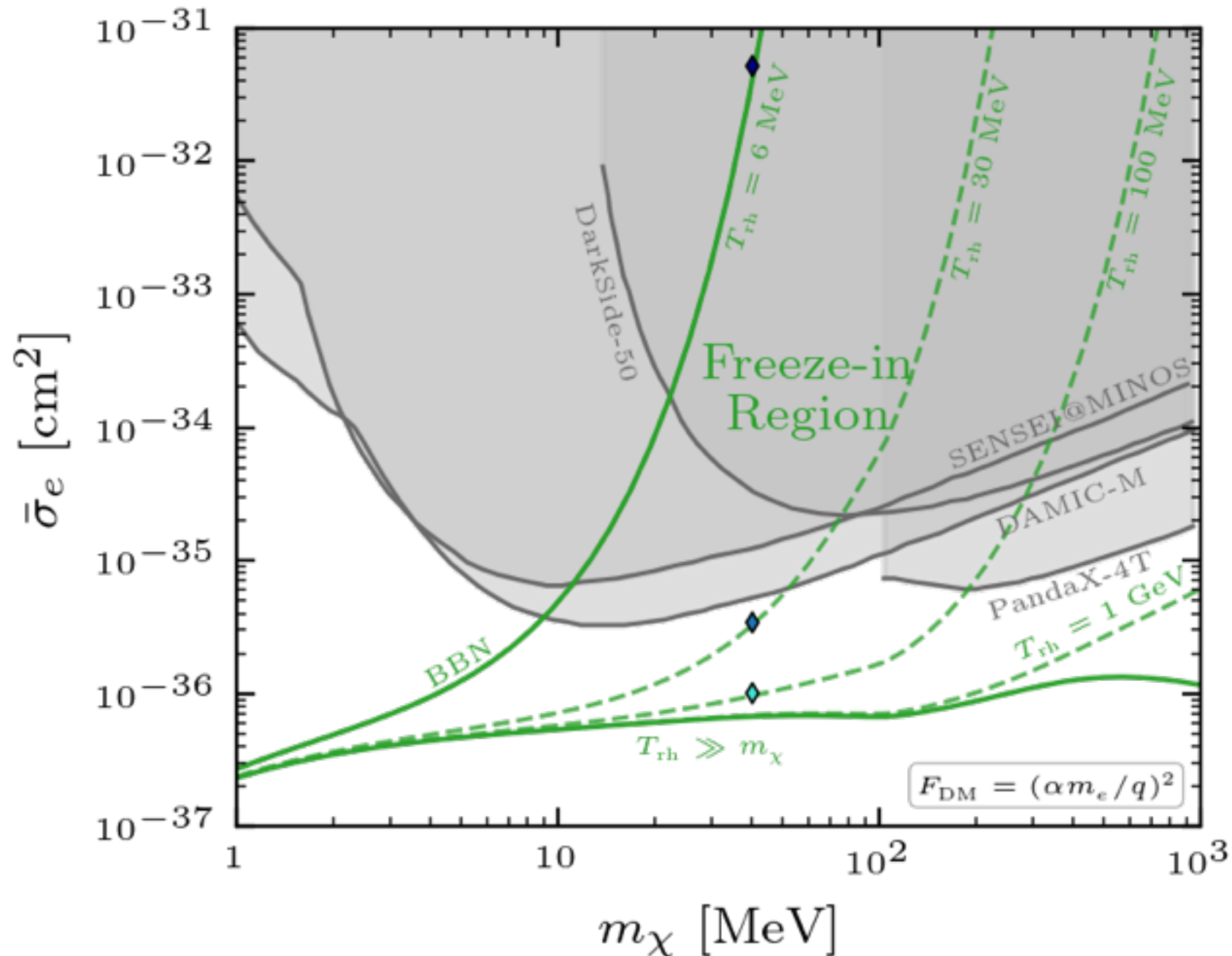
larger portal coupling, larger scattering cross-section!

# Impact of reheating temperature on freeze-in benchmark:



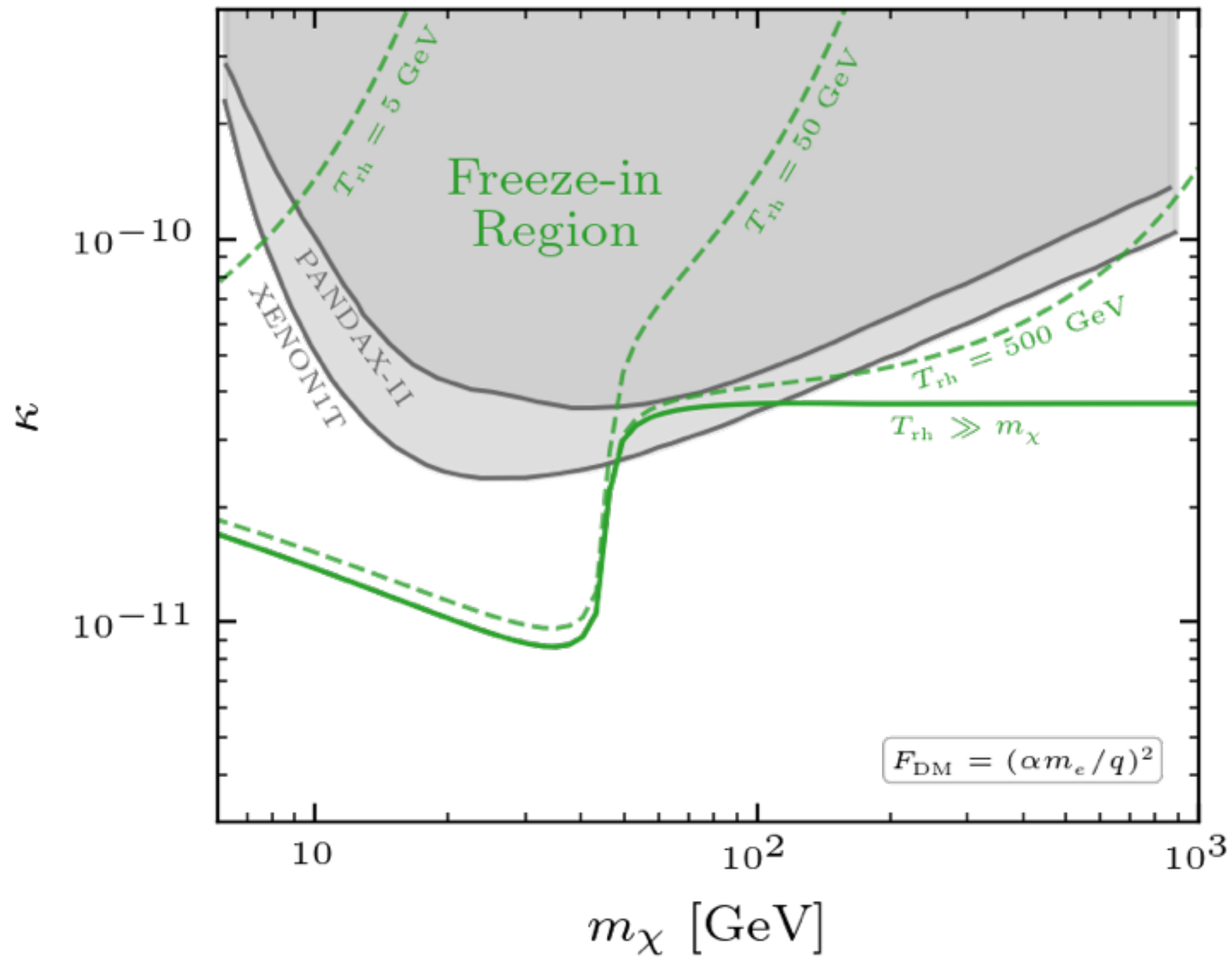


# Low reheating temperature: Implications for direct detection



$$\frac{\kappa(T_{\text{rh}} \ll m_\chi)}{\kappa(T_{\text{rh}} \gg m_\chi)} \sim \sqrt{x_{\text{rh}}} e^{x_{\text{rh}}}$$

Freeze-in benchmark target:  
a region defined by reheating temperature rather than a single curve.

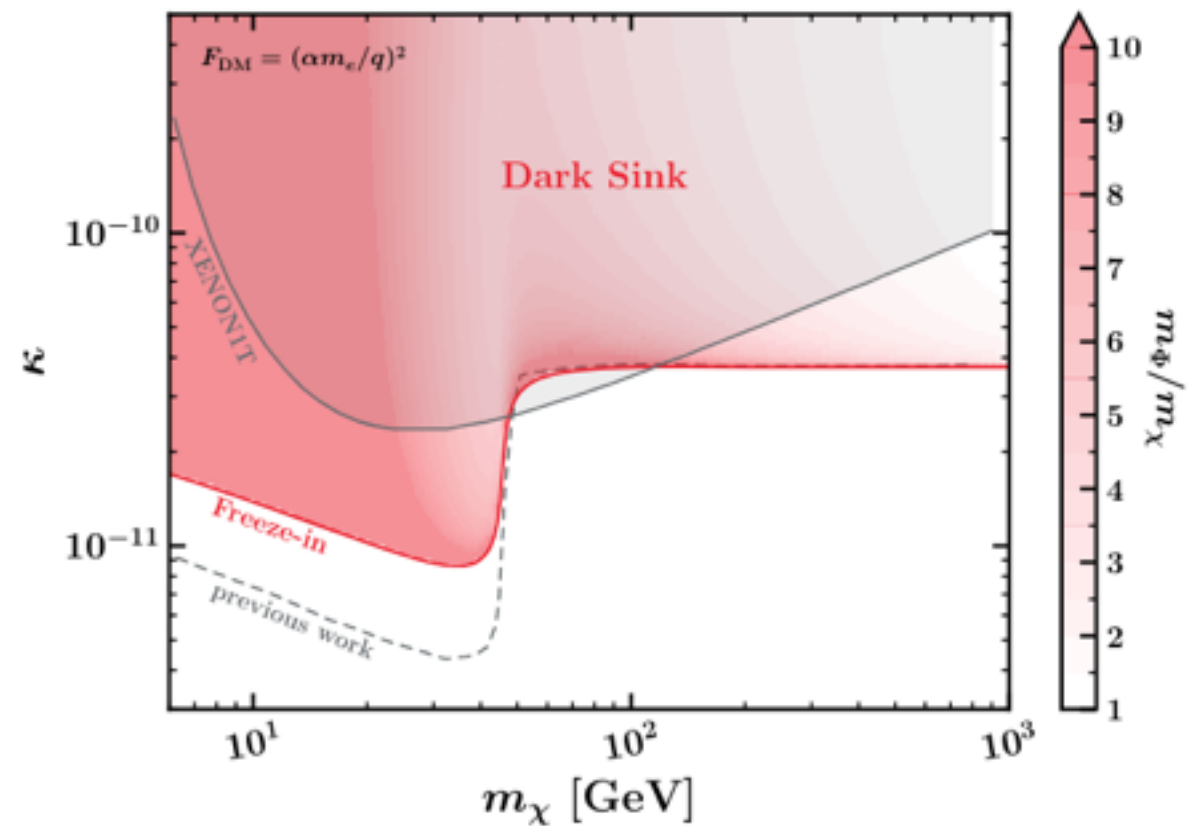
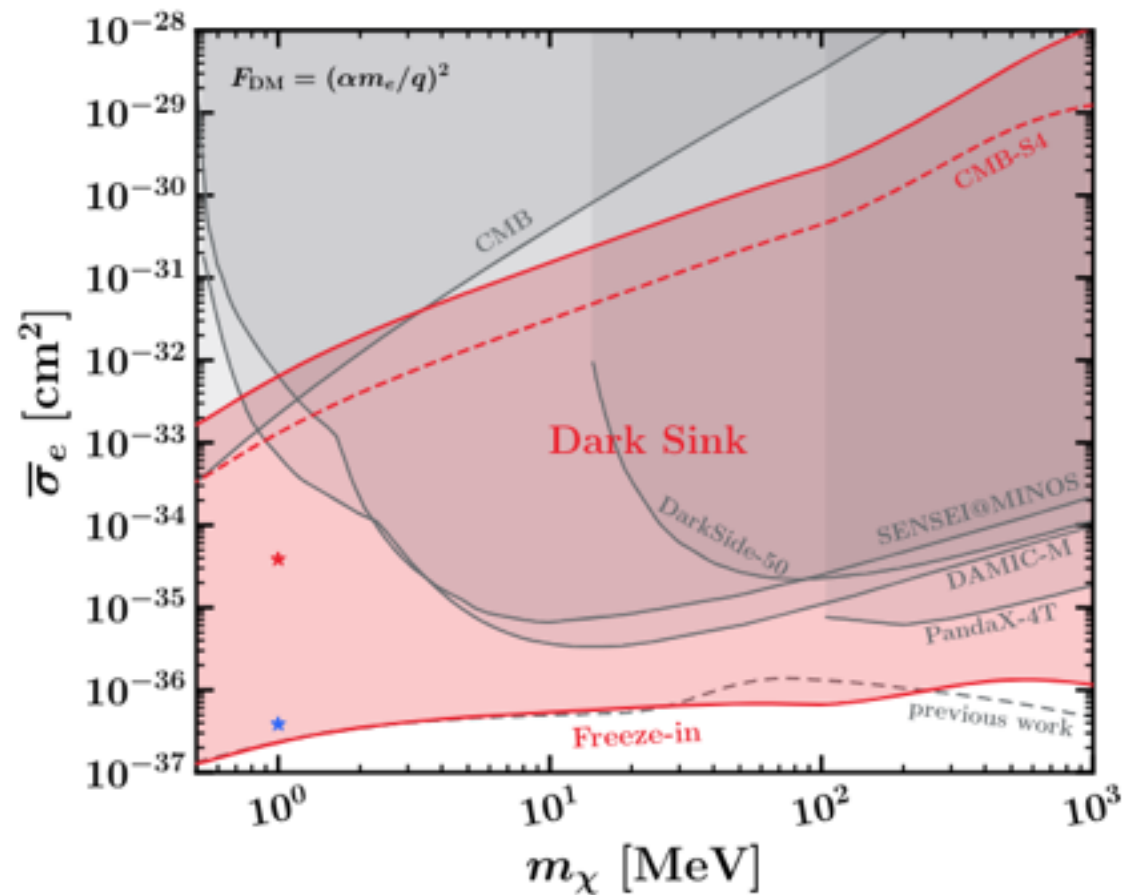


# Alternative:

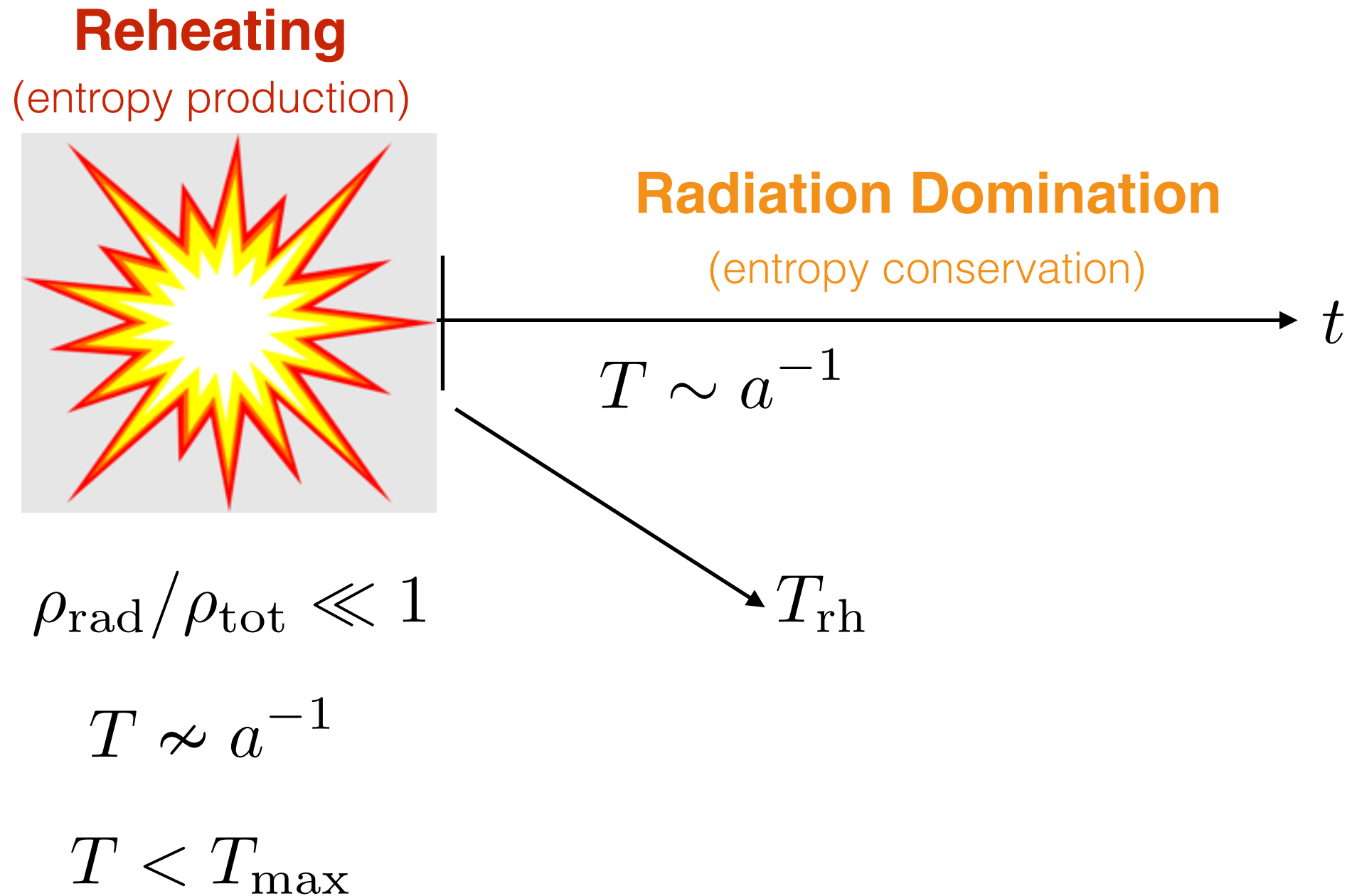
Opening up the parameter space with high reheating temperature:

more complicated dark sectors that introduce new dark degrees of freedom.

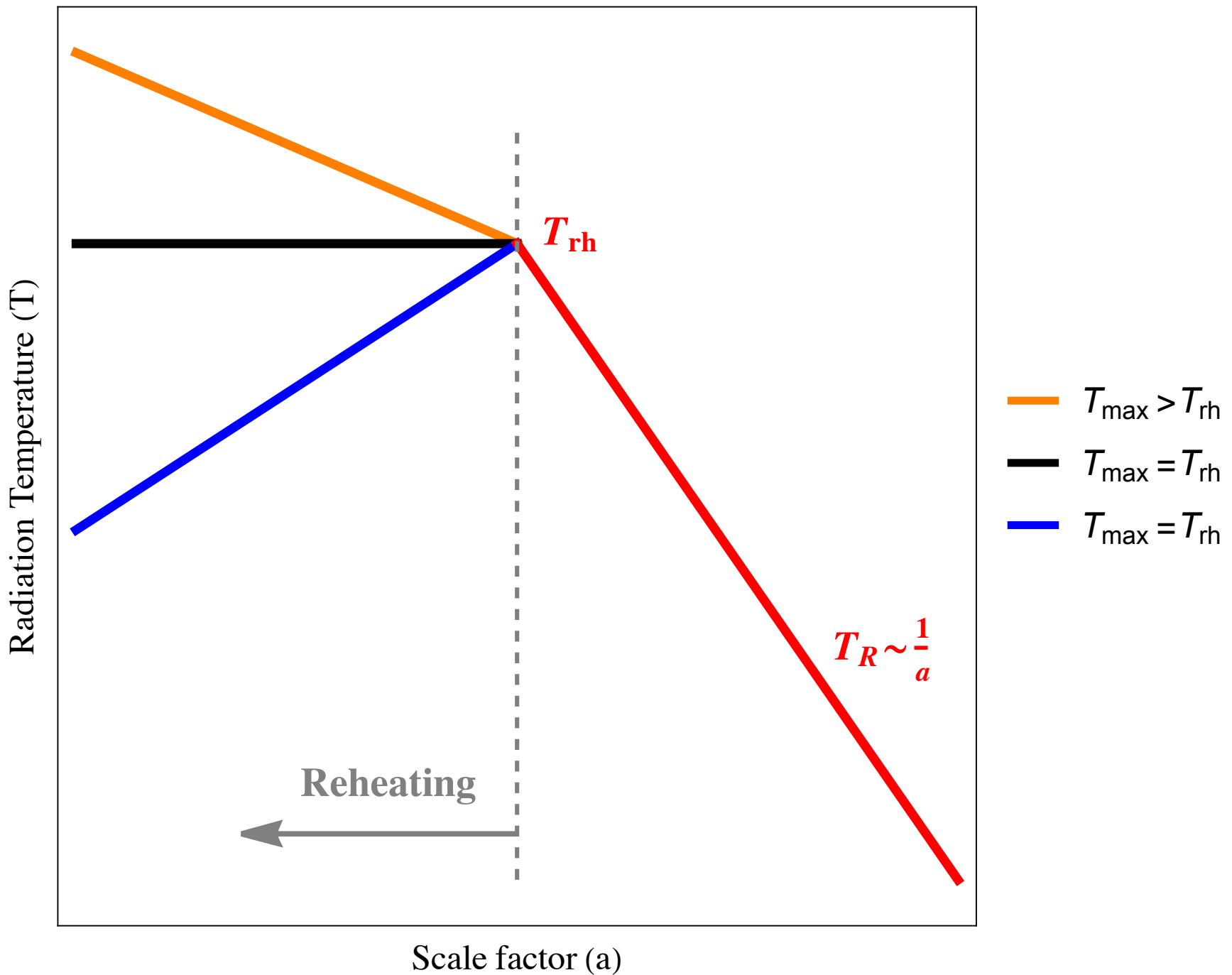
P. N. Bhattiprolu, R. McGehee, A. Pierce, 2023



# Maximum temperature of the Universe:



# Maximum temperature vs. reheating temperature:





inflaton decays to radiation directly

**D.J. H. Chung, E. W. Kolb, A. Riotto, 1998**

**G. F. Giudice, E. W. Kolb, A. Riotto, 2000**

**E. W. Kolb, A. Notari, A. Riotto, 2003**

inflaton decays to an unstable particle which then decays to radiation

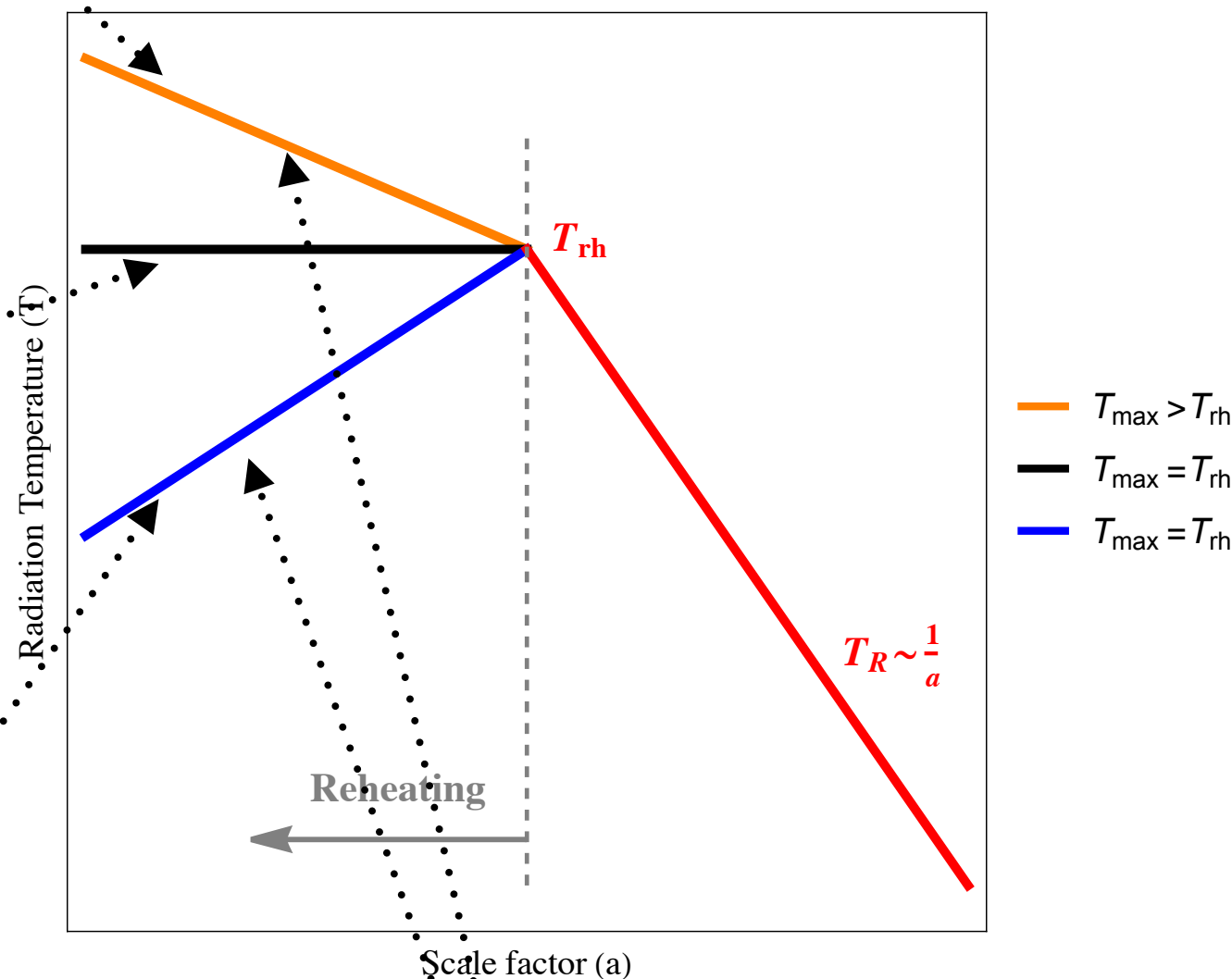
**C. Cosme, F. Costa, O. Lebedev, 2024**

inflaton has generic dissipation rate dependent on temperature and scale factor

**R. T. Co, E. Gonzalez, K. Harigaya, 2021**

Resonant reheating: s-channel inflaton annihilation

**B. Barman, N. Bernal, Y. Xu, 2024**



# Conclusion:

The impact of the reheating temperature on the benchmark freeze-in model.

A reheating temperature below the mass of DM suppresses production rate; a larger portal coupling is required to achieve the observed relic abundance. This enhancement consequently lifts up the freeze-in benchmark target for direct detection.

A potential future detection that lies between the current observational limits and the traditional freeze-in benchmark would directly probe the reheating temperature and the conditions of the universe in its earliest moments.

# DM-electron scattering rate

particle physics

$$\frac{d\langle\sigma v\rangle}{d\ln E_R} = \frac{\bar{\sigma}_e}{8\mu_{\chi e}^2} \int q \, dq |f(k, q)|^2 |F_{DM}(q)|^2 \eta(v_{min})$$

$$\bar{\sigma}_e = \frac{\mu_{\chi e}^2}{16\pi m_\chi^2 m_e^2} \overline{|\mathcal{M}_{\chi e}(q)|^2}_{q^2=\alpha^2 m_e^2}$$

$$F_{DM}(q) \simeq \begin{cases} 1 & \text{heavy mediator} \\ \frac{\alpha m_e}{q} & \text{electric dipole moment} \\ \frac{\alpha^2 m_e^2}{q^2} & \text{light mediator} \end{cases}$$

$$\mathcal{L} \supset -\frac{1}{4}\hat{X}_{\mu\nu}\hat{X}^{\mu\nu} + \frac{\epsilon_Y}{2}\hat{X}_{\mu\nu}\hat{B}^{\mu\nu} - e'\hat{X}_\mu\bar{\chi}\gamma^\mu\chi.$$

$$\hat{Z}_\mu = Z_\mu$$

$$\hat{A}_\mu = A_\mu + \epsilon A'_\mu$$

$$\hat{X}_\mu = A'_\mu - \epsilon \tan \theta_W Z_\mu.$$

$$\epsilon \equiv \epsilon_Y \cos \theta_W$$

$$\begin{aligned} \mathcal{L} \supset & -\epsilon e A'_\mu J_{\text{EM}}^\mu - e' J_{\text{DM}}^\mu (A'_\mu - \epsilon \tan \theta_W Z_\mu) \quad (\text{S3}) \\ & + i\epsilon e [F'^{\mu\nu} W_\mu^+ W_\nu^- - (\partial_\mu W_\nu^+ - \partial_\nu W_\mu^+) A'^\mu W^{-\nu} \\ & + (\partial_\mu W_\nu^- - \partial_\nu W_\mu^-) A'^\mu W^{+\nu}]. \end{aligned}$$

$$\begin{aligned} \overline{|\mathcal{M}|}_{f\bar{f}\rightarrow\chi\bar{\chi}}^2 = \frac{32}{3}\pi^2\alpha^2\kappa^2 N_f (s + 2m_\chi^2) & \left[ \frac{Q_f^2}{s^2} (s + 2m_f^2) - 2Q_f V_f \tan\theta_W \frac{(s + 2m_f^2)(s - m_Z^2)}{s [(s - m_Z^2)^2 + m_Z^2\Gamma_Z^2]} \right. \\ & \left. + \tan^2\theta_W \frac{V_f^2 (s + 2m_f^2) + A_f^2 (s - 4m_f^2)}{(s - m_Z^2)^2 + m_Z^2\Gamma_Z^2} \right], \end{aligned} \quad (\text{S4})$$

$$\overline{|\mathcal{M}|}_{\phi^+\phi^-\rightarrow\chi\bar{\chi}}^2 = \frac{32}{3}\pi^2\alpha^2\kappa^2 \left(1 + \frac{2m_\chi^2}{s}\right) \left(1 - \frac{4m_\phi^2}{s}\right), \quad (\text{S5})$$

$$\overline{|\mathcal{M}|}_{W^+W^-\rightarrow\chi\bar{\chi}}^2 = \frac{8}{27}\pi^2\alpha^2\kappa^2 \left(\frac{m_Z}{m_W}\right)^4 \frac{(s + 2m_\chi^2)(s - 4m_W^2)(s^2 + 20sm_W^2 + 12m_W^4)}{s^2 [(s - m_Z^2)^2 + m_Z^2\Gamma_Z^2]}, \quad (\text{S6})$$