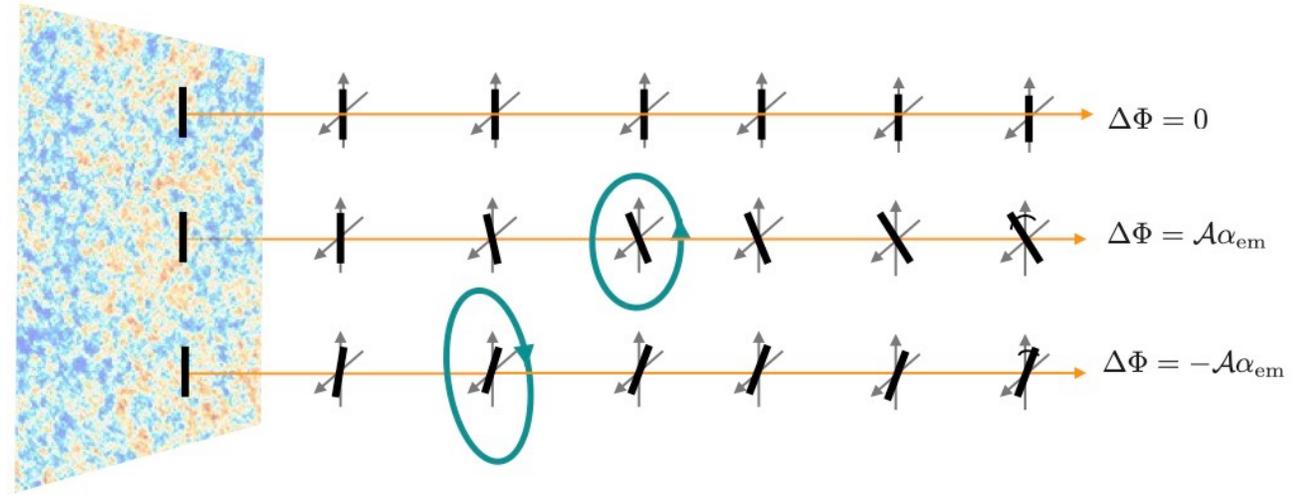


# CMB Birefringence from Axion Strings



Andrew J. Long  
Rice University  
@ Mitchell Conference  
May 26, 2024

# Summary

- If a [hyper-light axion-like particle](#) exists in Nature, the associated cosmological [network of axion strings](#) can leave an imprint on [CMB polarization](#) through birefringence
- We use existing [measurements of anisotropic birefringence](#) (Planck, SPT, ...) to place constraints on this scenario. Next-generation telescopes (CMB-S4) will probe  $O(1)$  electromagnetic anomaly coefficients and thereby probe the axion's UV embedding
- We argue that measurements of anisotropic birefringence could not only reveal the presence of a hyper-light ALP in Nature, but also lead to a [measurement of its mass](#)
- Our ongoing work (very early stages) seeks to use [machine learning](#) techniques (spherical CNN) to detect the subtle signal of axion strings in CMB polarization data

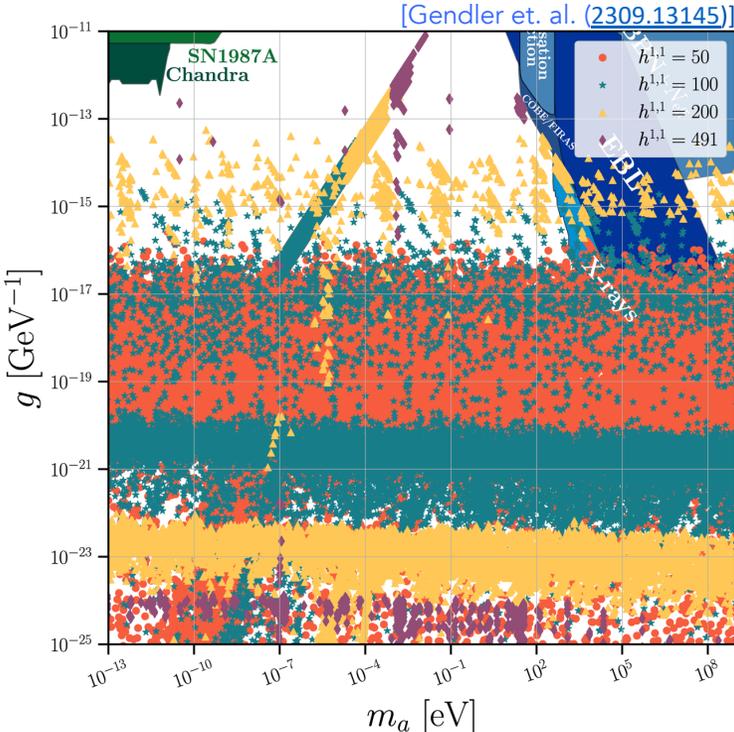
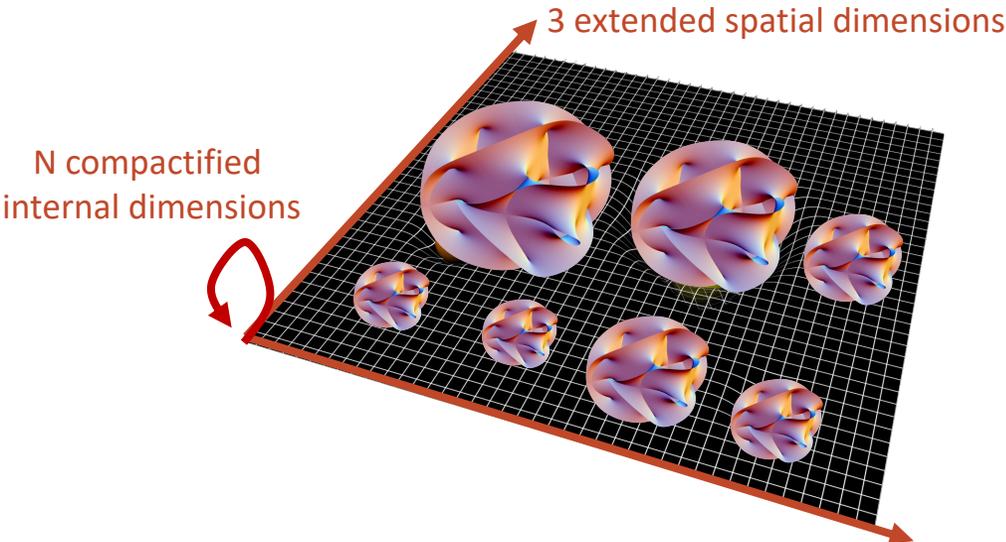
axion-like particles  
& cosmic axion strings

# Theory landscape: axion-like particles

axion-like particles

$$\mathcal{L} \supset \frac{1}{2}(\partial a)^2 - \frac{1}{2}m_a^2 a^2 - \frac{1}{4}g_{a\gamma\gamma} a F_{\mu\nu} \tilde{F}^{\mu\nu}$$

ALPs from extra dimensions  
(such as string theory)



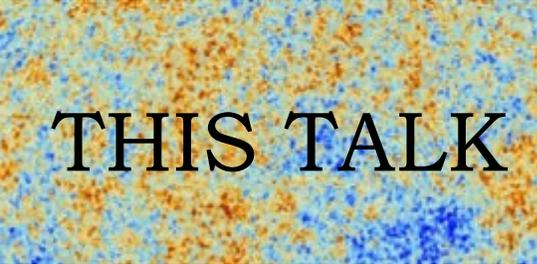
[Gendler et. al. (2309.13145)]

# Theory landscape: axion-like particles

axion-like particles

$$\mathcal{L} \supset \frac{1}{2}(\partial a)^2 - \frac{1}{2}m_a^2 a^2 - \frac{1}{4}g_{a\gamma\gamma} a F_{\mu\nu} \tilde{F}^{\mu\nu}$$

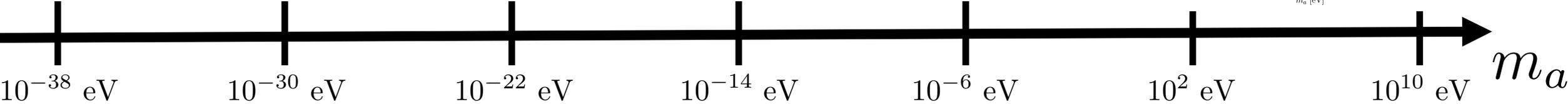
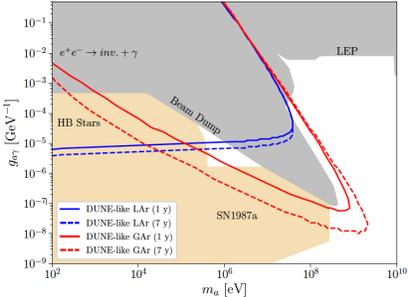
hyper-light axion-like particles  
(testable with cosmology)



ultra-light axion-like particles  
(dark matter candidate)



heavy axion-like particles  
(testable in the lab)



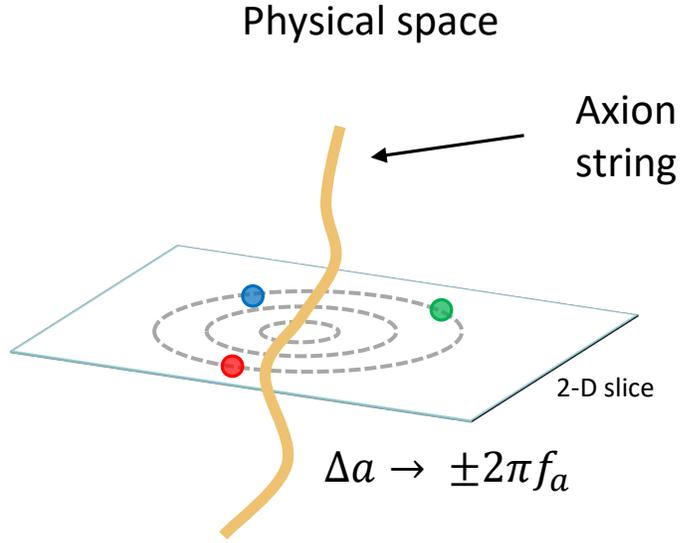
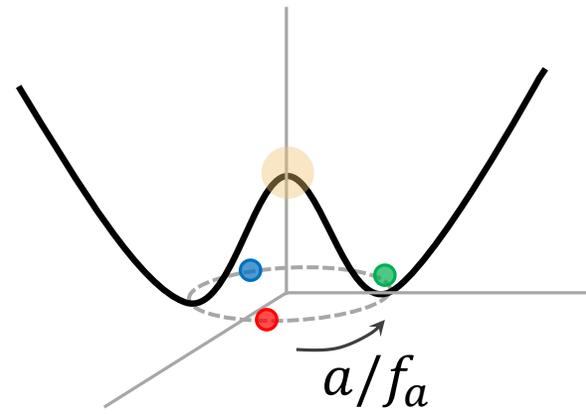
# ALPs form axion strings

[Kibble (1976)]  
[Vilenkin & Vachaspati (1987)]

string formation:  
early-universe phase transition

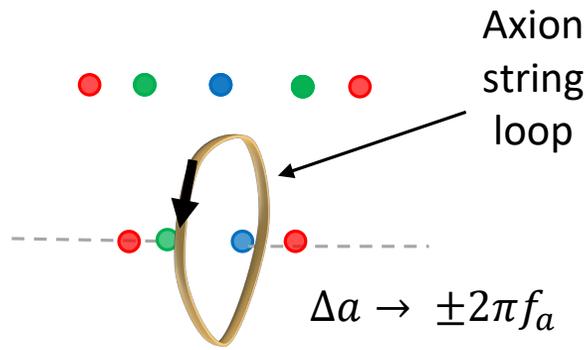
Field space  

$$V(\phi) = -\mu^2|\phi|^2 + \lambda|\phi|^4$$



**string thickness = microscopic**

**string length = cosmological**



Clockwise (+); or  
anti-clockwise (-)

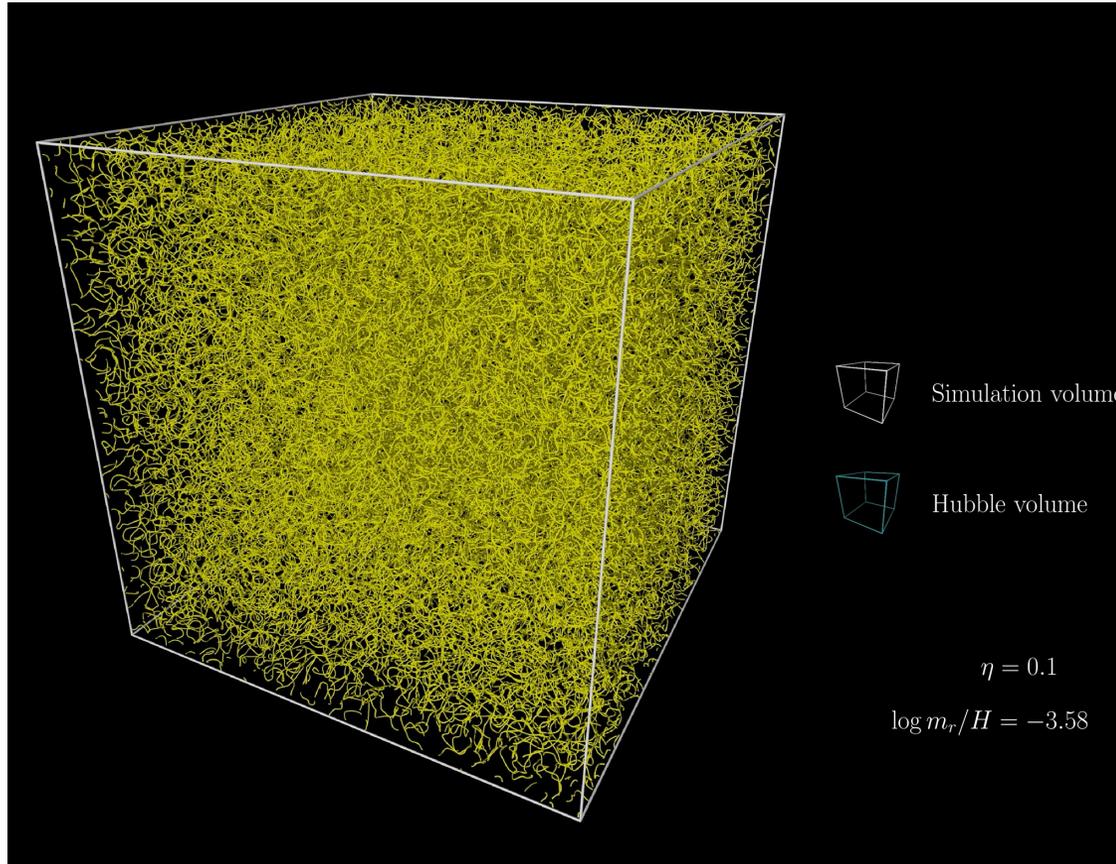
assume:  $T_{RH} > f_a$

image credit: Mudit Jain (2021)

# A cosmic string network

[Buschmann et. al. (2022)]

string network simulation:



- string network is in scaling
- new loops are formed from reconnection
- loops emit axions and collapse
- typical string length tracks Hubble
- average energy density tracks Hubble
- today:  $O(1-10)$  strings per Hubble volume

**How can we detect axion strings in the Universe today?**

birefringence  
from axion strings

# How could we detect an axion string?

[Harvey & Naculich (1989)], [Carroll, Field, Jackiw (1990,91)], [Harari, Sikivie (1992)]  
 [Fedderke, Graham, Rajendran (2019)], [Agrawal, Hook, Huang (2019)]  
 [Yin, Dai, Ferraro (2021) & (2023)]

assume interaction  
 with electromagnetism:  
 standard Chern-Simons coupling

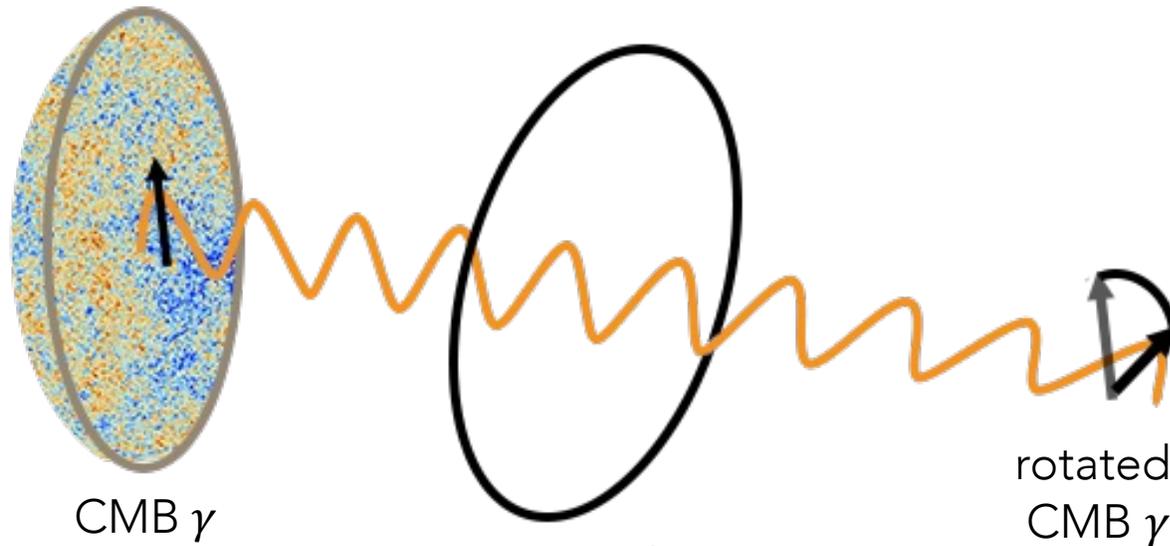
$$\mathcal{L}_{\text{int}} = -\frac{1}{4} g_{a\gamma\gamma} a F \tilde{F}$$

$$g_{a\gamma\gamma} = -\mathcal{A} \frac{\alpha_{\text{em}}}{\pi f_a}$$

$$\mathcal{A} = \sum Q_{\text{PQ}} Q_{\text{em}}^2 \sim \# / 9$$

axion-induced birefringence:  
 an electromagnetic wave  
 traveling through a varying axion field  
 has its plane of polarization rotated

$$\alpha = \frac{1}{2} g_{a\gamma\gamma} \int_C dX^\mu \partial_\mu a(X)$$



rotation angle

$$\alpha = g_{a\gamma\gamma} \pi f_a$$

$$\equiv -\mathcal{A} \alpha_{\text{em}}$$

$$\approx -0.42^\circ \mathcal{A}$$

axion string loop

$$\Delta a = 2\pi f_a$$

\* birefringence can be measured through E-B cross correlation

# The loop-crossing model

## Assumptions

- All loops are circles
- Randomize loop orientation
- Randomize loop location in space
- All loops same radius at any time
- Loop radius evolves tracking Hubble

$$R(t) = \zeta_0 / H(t)$$

- Number of loops tracks Hubble

$$\rho(t) = \xi_0 \mu(t) H(t)^2$$

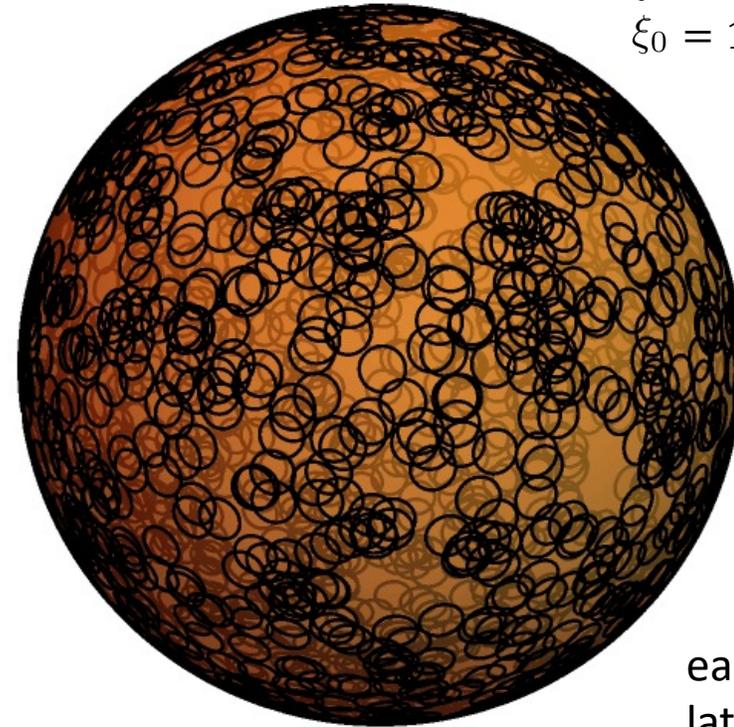
## Model Parameters

$$\{m_a, \mathcal{A}, \zeta_0, \xi_0\}$$

## loop-crossing model

$$\zeta_0 = 1.0$$

$$\xi_0 = 1.0$$



early time -> small loops  
late time -> large loops

# Expected birefringence signal

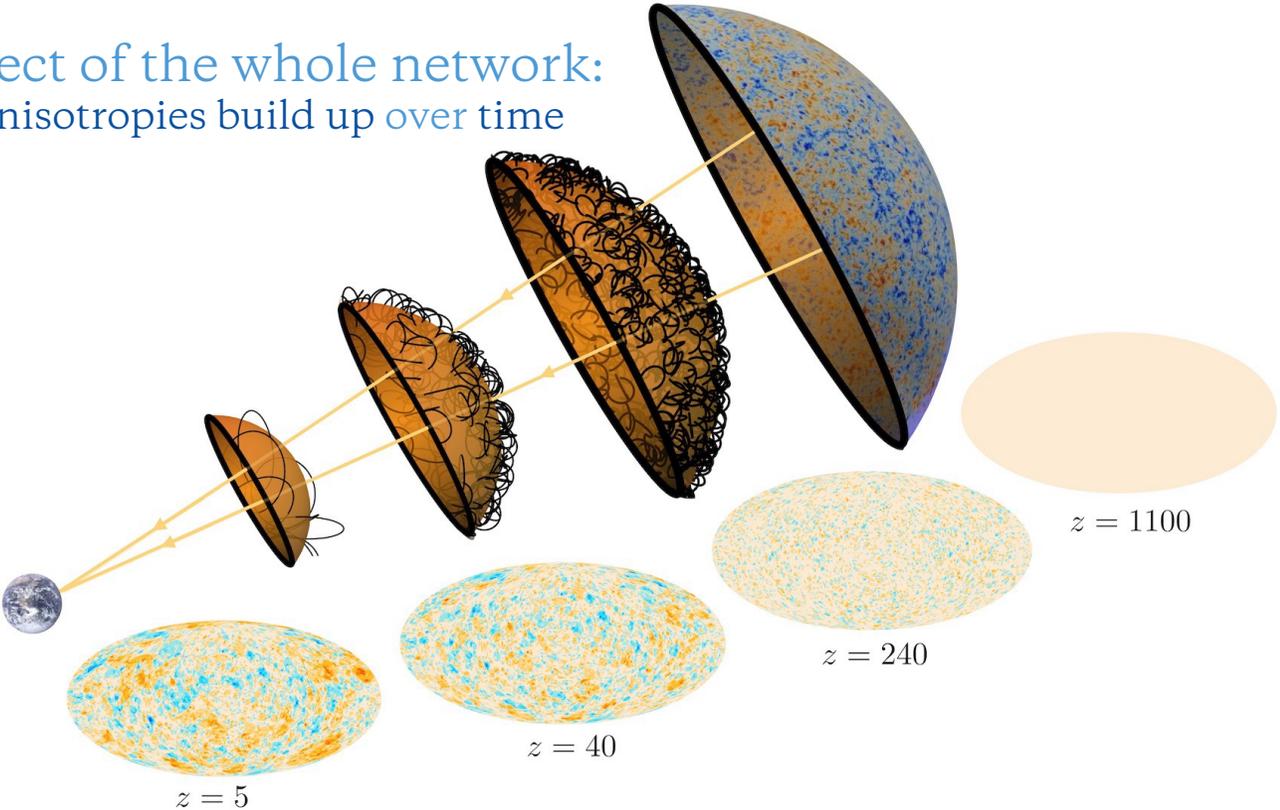
[Jain, AL, Amin, arXiv:2103.10962]

[Jain, Hagimoto, AL, Amin, arXiv:2208.08391]

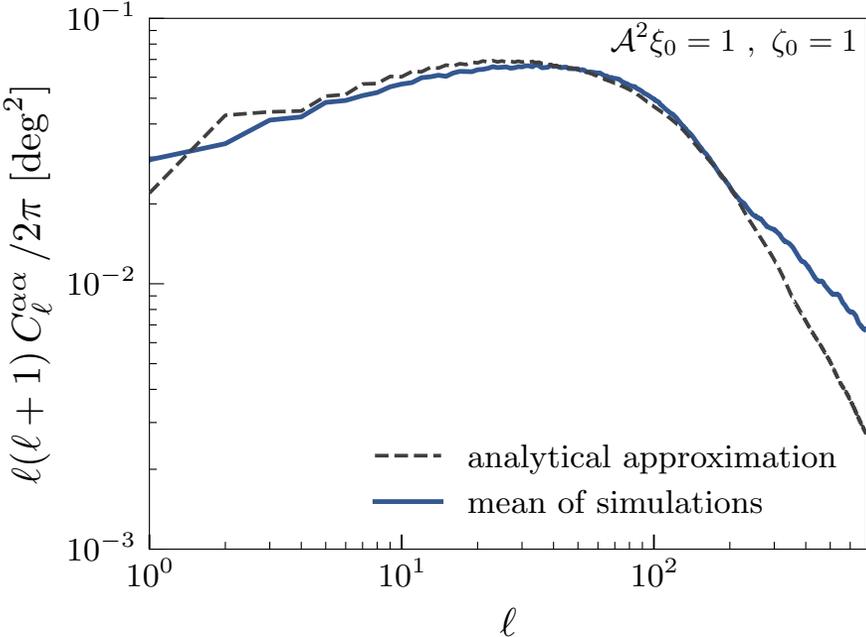
loop-crossing model:  
a network of circular loops

$\mathcal{A}$  = dimensionless axion-photon coupling  
 $\xi_0$  = dimensionless loop density (Hubble units)  
 $\zeta_0$  = dimensionless loop length (Hubble units)

effect of the whole network:  
anisotropies build up over time



angular power spectrum:



**approx. scale invariant up to  $l \sim 100$**

**degeneracy:  $\langle \alpha \alpha \rangle \sim \mathcal{A}^2 \xi_0$**

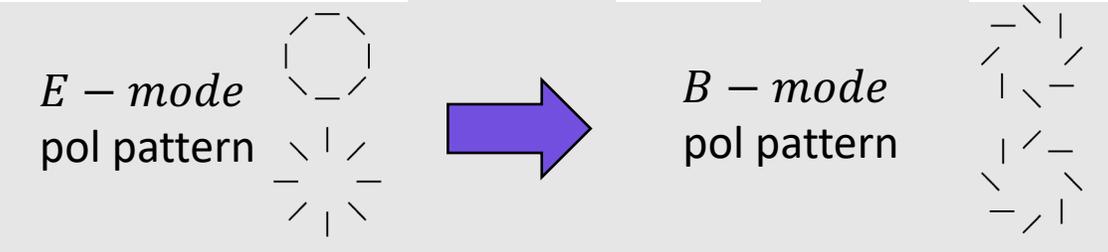
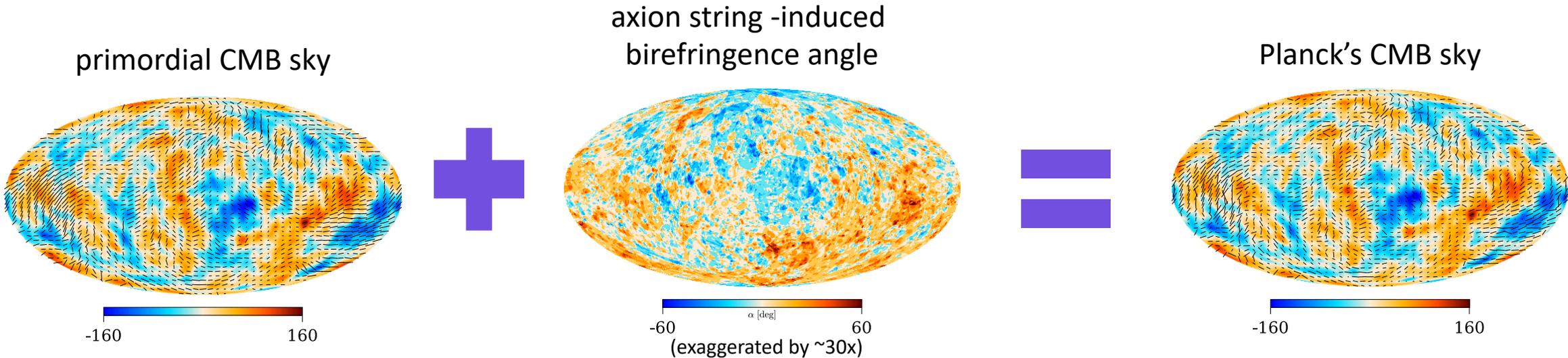
\* need  $m_a \lesssim 3H_{\text{cmb}} \approx 10^{-28}$  eV for the network to survive until after recombination

# Effect on CMB polarization

How does birefringence affect the CMB's temperature and polarization?

$$T(\hat{n}) \rightarrow T(\hat{n})$$

$$[Q \pm iU](\hat{n}) \rightarrow [(Q \pm iU)e^{\pm 2i\Delta\Phi}](\hat{n})$$



Signal of axion string-induced cosmological birefringence

$$\begin{cases} \langle TB \rangle \neq 0 \\ \langle EB \rangle \neq 0 \end{cases}$$

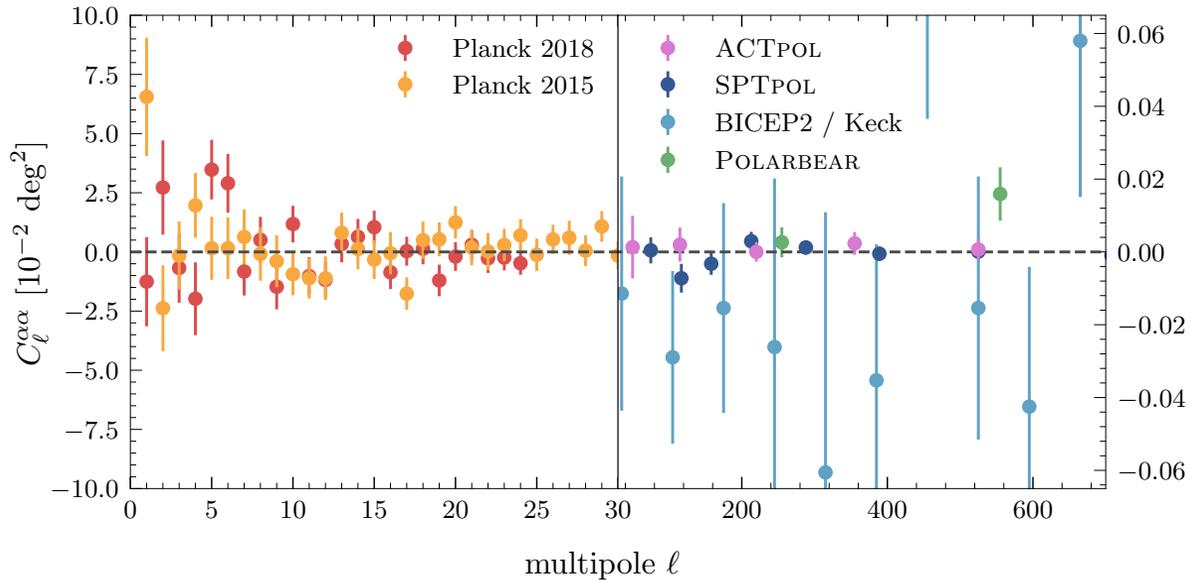
$$C_\ell^{EB} \sim \sin(4\Delta\Phi) (C_\ell^{EE} - C_\ell^{BB})$$

constraints  
from CMB polarization data

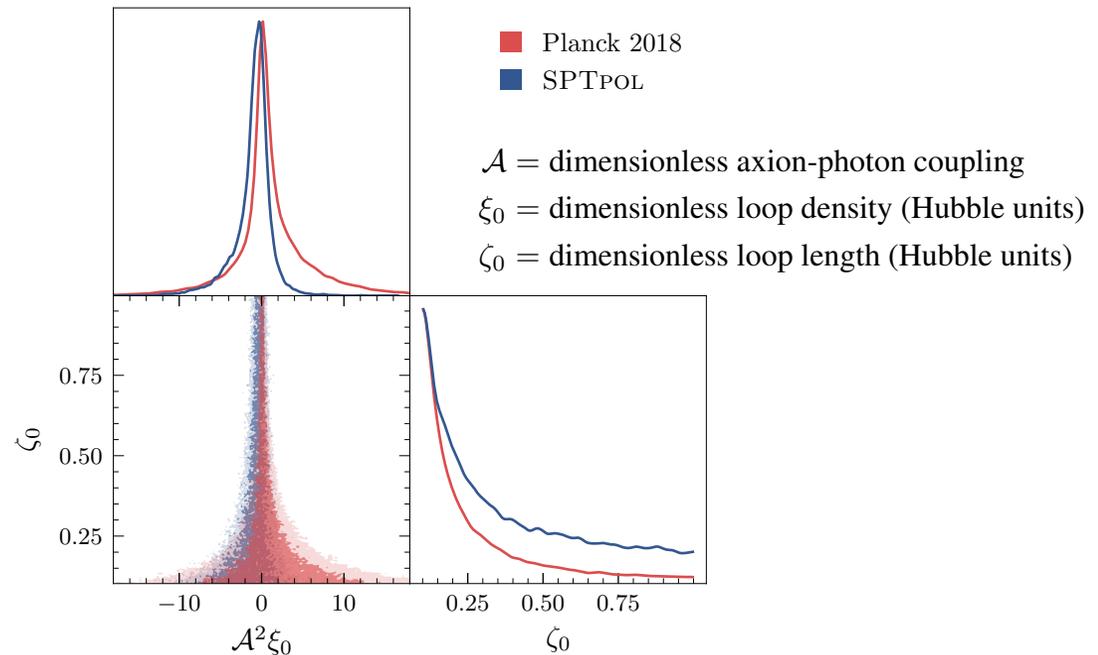
# Constraints from anisotropic birefringence

[Jain, AL, Amin, arXiv:2103.10962]  
 [Jain, Hagimoto, AL, Amin, arXiv:2208.08391]  
 see also: Yin, Dai, & Ferraro (2111.12741)

measurements of CMB polarization:  
 no evidence for anisotropic birefringence



a constraint on axion strings networks  
 & their coupling to electromagnetism:



constraints:

SPTPOL:  $\mathcal{A}^2 \xi_0 < 3.7$  at 95% CL

# Implications

CMB observations constrain:

$$\text{SPTPOL: } \mathcal{A}^2 \xi_0 < 3.7 \text{ at 95\% CL}$$

Typical axion-photon coupling:

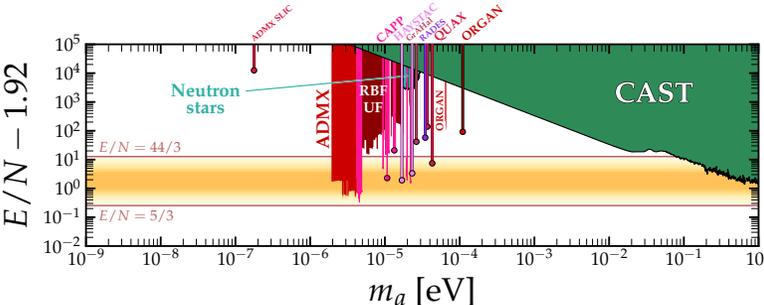
$$\mathcal{A} = 1/3$$

Typical loop abundance:

$$\xi_0 = 30$$

$$\mathcal{A}^2 \xi_0 \approx 3.3$$

... already probing an  $O(1)$  anomaly coefficient!  
... but still large uncertainties in  $\xi_0$  (from sims)



# Projected sensitivity

future telescopes  
probes of isotropic + aniso. birefringence

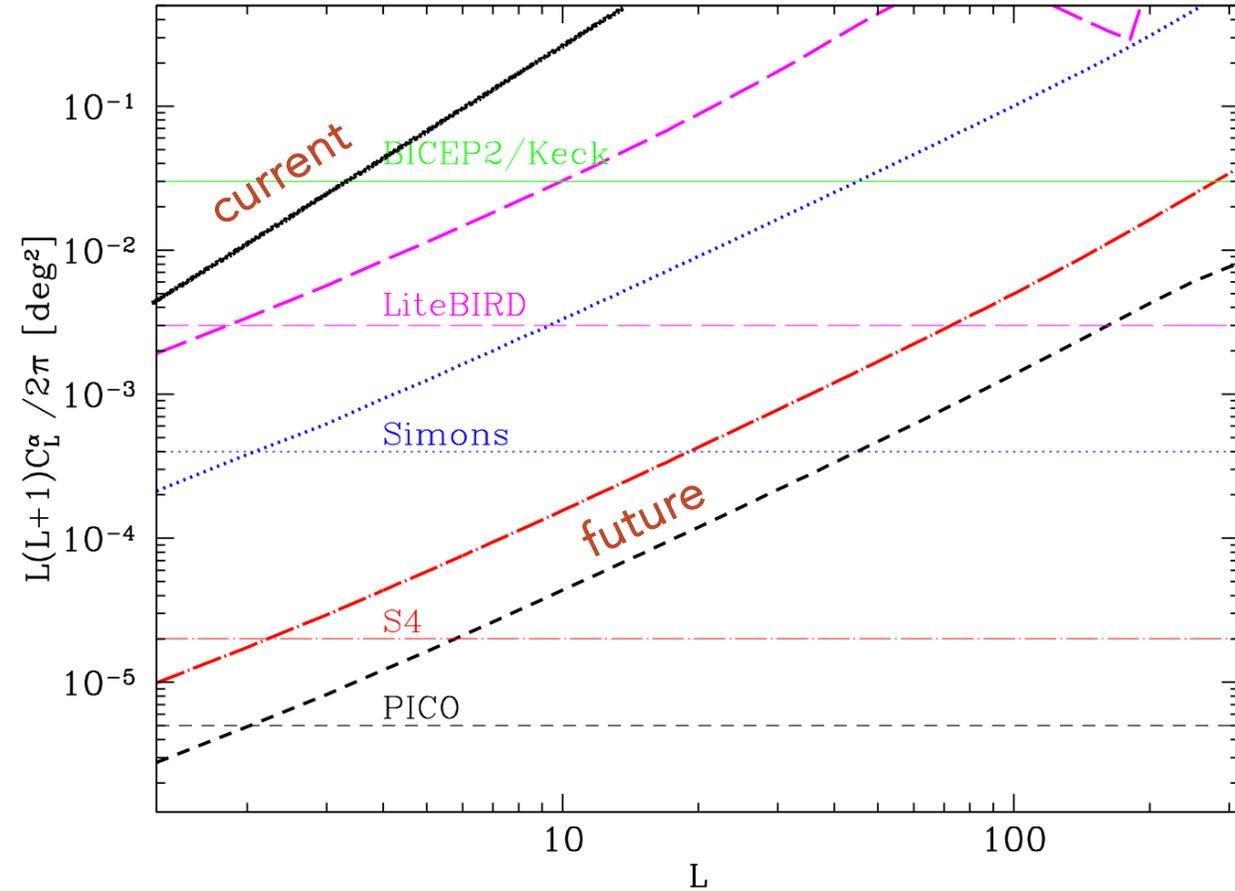
| Current  |                        |                     | LiteBIRD |                        |                     | SO       |                        |                     | CMB-S4-like |                        |                     | PICO     |                        |                     |
|----------|------------------------|---------------------|----------|------------------------|---------------------|----------|------------------------|---------------------|-------------|------------------------|---------------------|----------|------------------------|---------------------|
| $\alpha$ | $A_\alpha$             | $\sqrt{C_2^\alpha}$ | $\alpha$ | $A_\alpha$             | $\sqrt{C_2^\alpha}$ | $\alpha$ | $A_\alpha$             | $\sqrt{C_2^\alpha}$ | $\alpha$    | $A_\alpha$             | $\sqrt{C_2^\alpha}$ | $\alpha$ | $A_\alpha$             | $\sqrt{C_2^\alpha}$ |
| /        | $10^{-2} \text{deg}^2$ | $/$                 | /        | $10^{-3} \text{deg}^2$ | $/$                 | /        | $10^{-4} \text{deg}^2$ | $/$                 | /           | $10^{-5} \text{deg}^2$ | $/$                 | /        | $10^{-5} \text{deg}^2$ | $/$                 |
| -        | -                      | -                   | 1.3      | 2.7                    | 0.9                 | 0.56     | 3                      | 0.29                | 0.1         | 1.4                    | 0.065               | 0.05     | 0.4                    | 0.035               |
| -        | -                      | -                   | 1.5      | 3.3                    | 1.0                 | 0.66     | 4                      | 0.35                | 0.11        | 2.0                    | 0.08                | 0.06     | 0.5                    | 0.04                |
| -        | -                      | -                   | 1.4      | 3.5                    | 1.0                 | 0.64     | 5.0                    | 0.4                 | 0.13        | 2.5                    | 0.09                | 0.08     | 1.2                    | 0.06                |
| 30       | 2                      | 3                   | 1.6      | 4.0                    | 1.1                 | 0.71     | 5.5                    | 0.4                 | 0.15        | 3.3                    | 0.1                 | 0.09     | 1.4                    | 0.065               |

BLE II. Current and forecasted 68% CL bounds on the uniform and the anisotropic CPR parameters.

$$A_\alpha = L(L + 1)C_L^\alpha / 2\pi$$

future CMB polarization measurements will drastically improve sensitivity to axion-string induced anisotropic birefringence

diagonal = allows multipoles to vary independently  
horizontal = restricts to a scale invariant spectrum



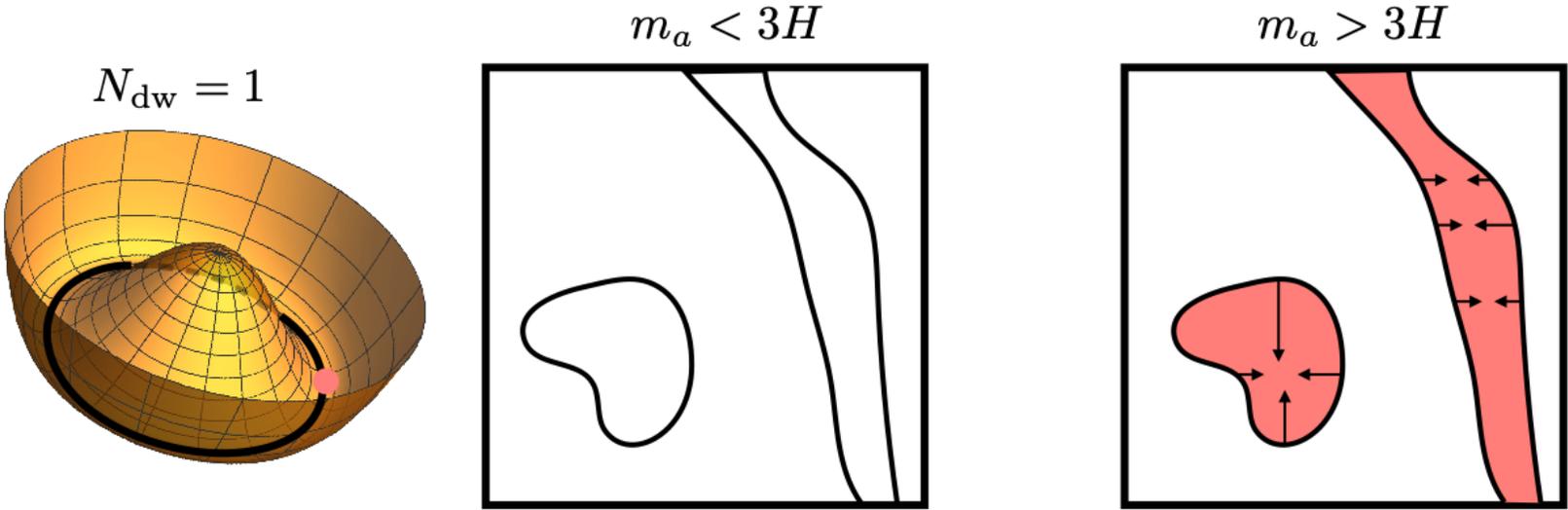
effect of  
varying ALP mass

# Collapse of the string-wall network

[Jain, Hagimoto, AL, Amin, arXiv:2208.08391]

Axion strings become connected together by domain walls

... the string-wall network collapses (for  $N_{dw} = 1$ )



let's consider:  $\begin{cases} m_a \lesssim 3H_{\text{CMB}} \simeq 3 \times 10^{-29} \text{ eV} & \text{(string network survives until after recombination)} \\ m_a \gtrsim 3H_0 \simeq 5 \times 10^{-33} \text{ eV} & \text{(string network collapses before today)} \end{cases}$

# Impact on birefringence

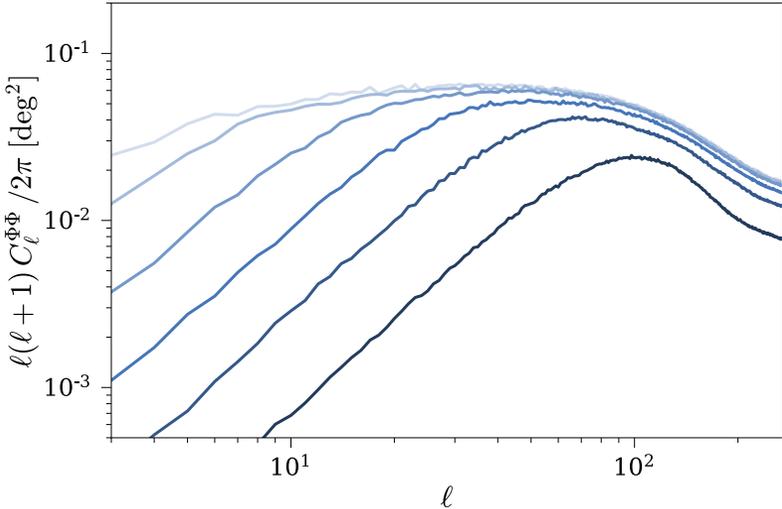
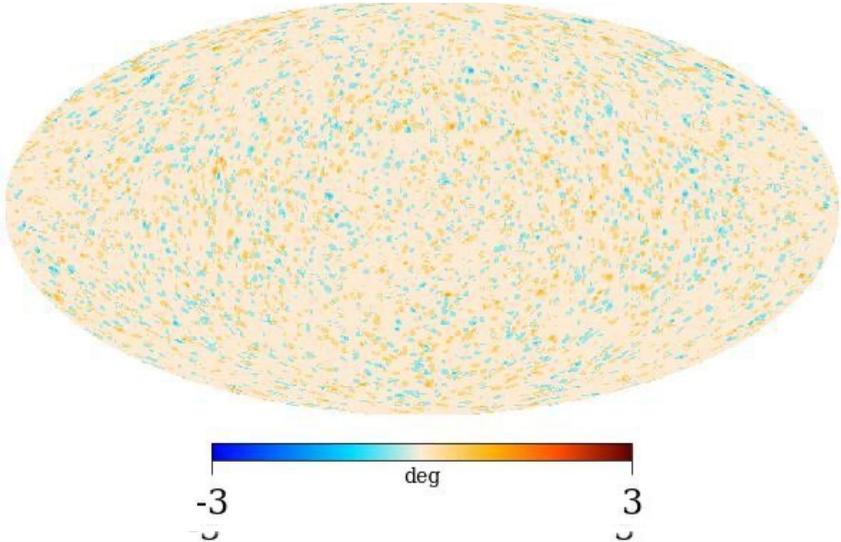
(assuming  $N_{\text{DW}} = 1$ )

raise the ALP mass  
(network collapses earlier)

[Jain, Hagimoto, AL, Amin, arXiv:2208.08391]

see also: [Ferreira, Gasparotto, Hiramatsu, Obata, & Pujolas (2023)]

$$m_a = 2 \times 10^{-29} \text{ eV} \quad (z_c = 404)$$



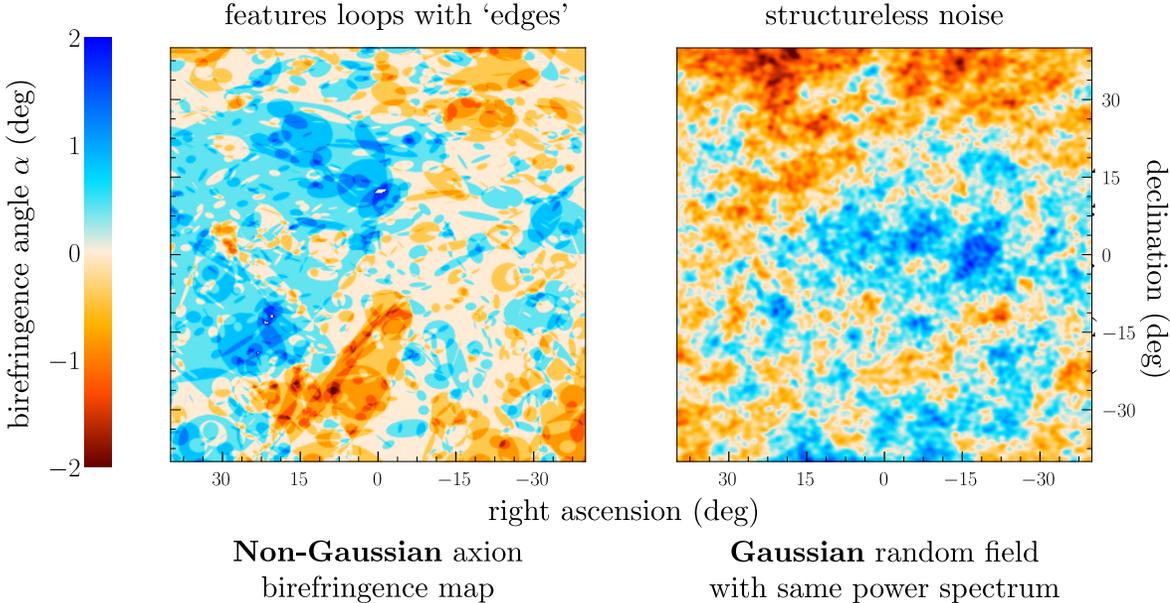
**strong scale dependence → possible to measure  $m_a$**

signatures of  
non-Gaussianity

# Birefringence non-Gaussianity

[Hagimoto & AL, arXiv:2306.07351]  
see also: Yin, Dai, Ferraro (2305.02318)

axion-string induced birefringence:  
loop-like features are visibly non-Gaussian



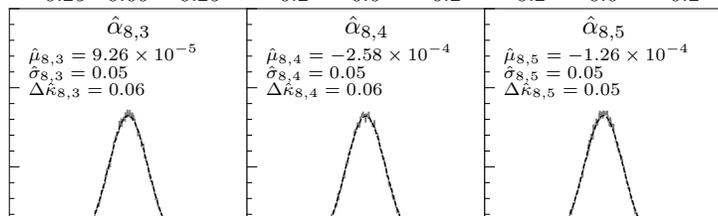
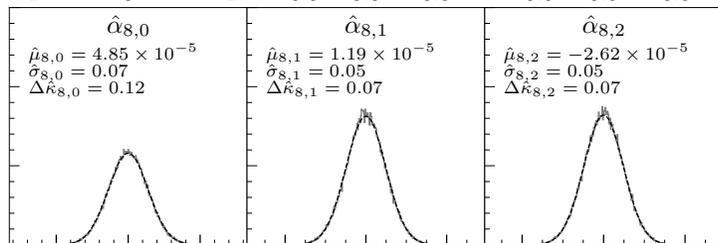
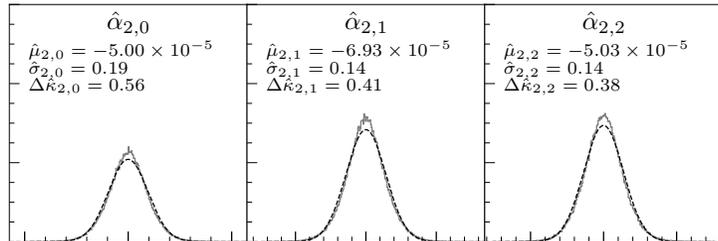
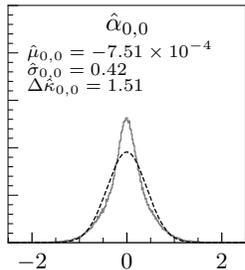
How to best quantify the non-Gaussian birefringence and develop tests to extract these features from the data?

# Measures of NG 1: kurtosis

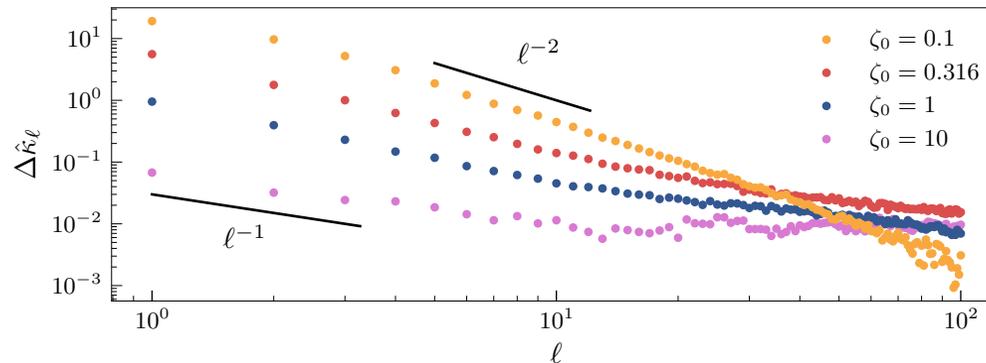
distribution over  $\hat{a}_{\ell m}$ 's  
less Gaussian at lower  $\ell$

kurtosis  
a measure of Gaussianity

$$\kappa_{\ell m} = \frac{\langle |\hat{a}_{\ell m} - \langle \hat{a}_{\ell m} \rangle|^4 \rangle}{\langle |\hat{a}_{\ell m} - \langle \hat{a}_{\ell m} \rangle|^2 \rangle^2} = 3 \text{ for Gaussian}$$



scaling with multipole index  
more Gaussian on smaller scales



analytical model  
~ inverse with # loops

$$\Delta\hat{\kappa}_\ell \sim \frac{\zeta_0}{8\xi_0} \left( 1 + \frac{\pi}{\lambda\zeta_0\ell} \right)^2$$

recall:  $R(t) = \zeta_0/H(t)$

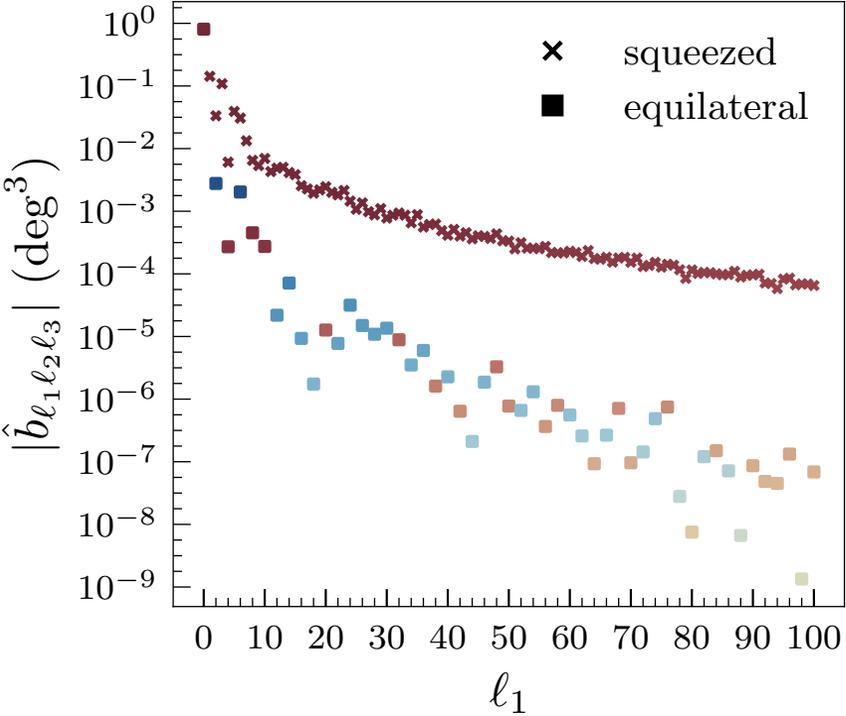
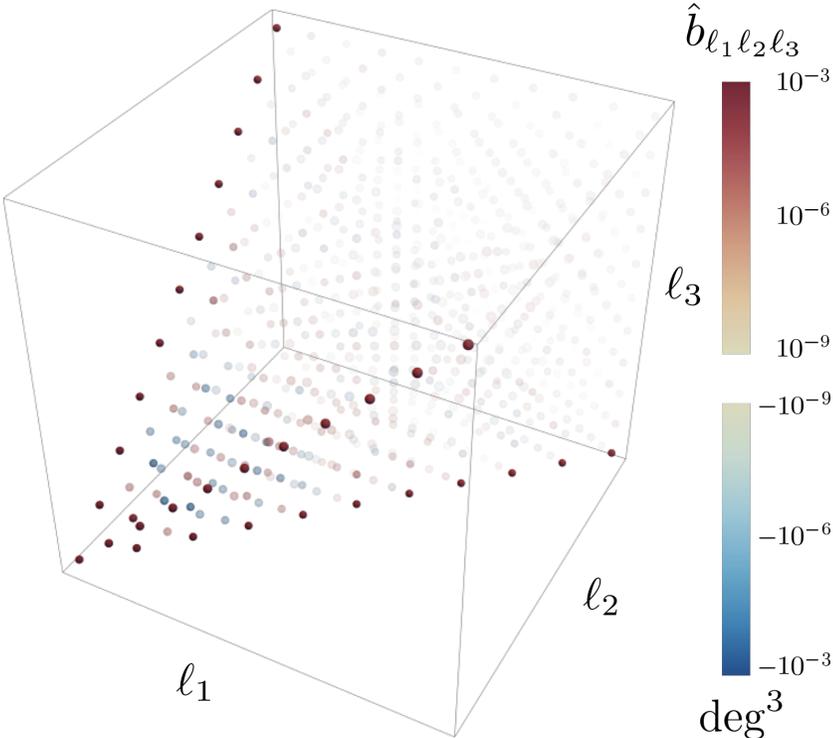
# Measures of NG 2: bispectrum

[Hagimoto & AL, arXiv:2306:07351]

bispectrum  
3-point correlations

$$\hat{b}_{\ell_1 \ell_2 \ell_3} = h_{\ell_1 \ell_2 \ell_3}^{-1} \sum_{m_1=-\ell_1}^{\ell_1} \sum_{m_2=-\ell_2}^{\ell_2} \sum_{m_3=-\ell_3}^{\ell_3} \begin{pmatrix} \ell_1 & \ell_2 & \ell_3 \\ m_1 & m_2 & m_3 \end{pmatrix} \hat{\alpha}_{\ell_1 m_1} \hat{\alpha}_{\ell_2 m_2} \hat{\alpha}_{\ell_3 m_3}$$

single realization  
largest in squeezed triangle form



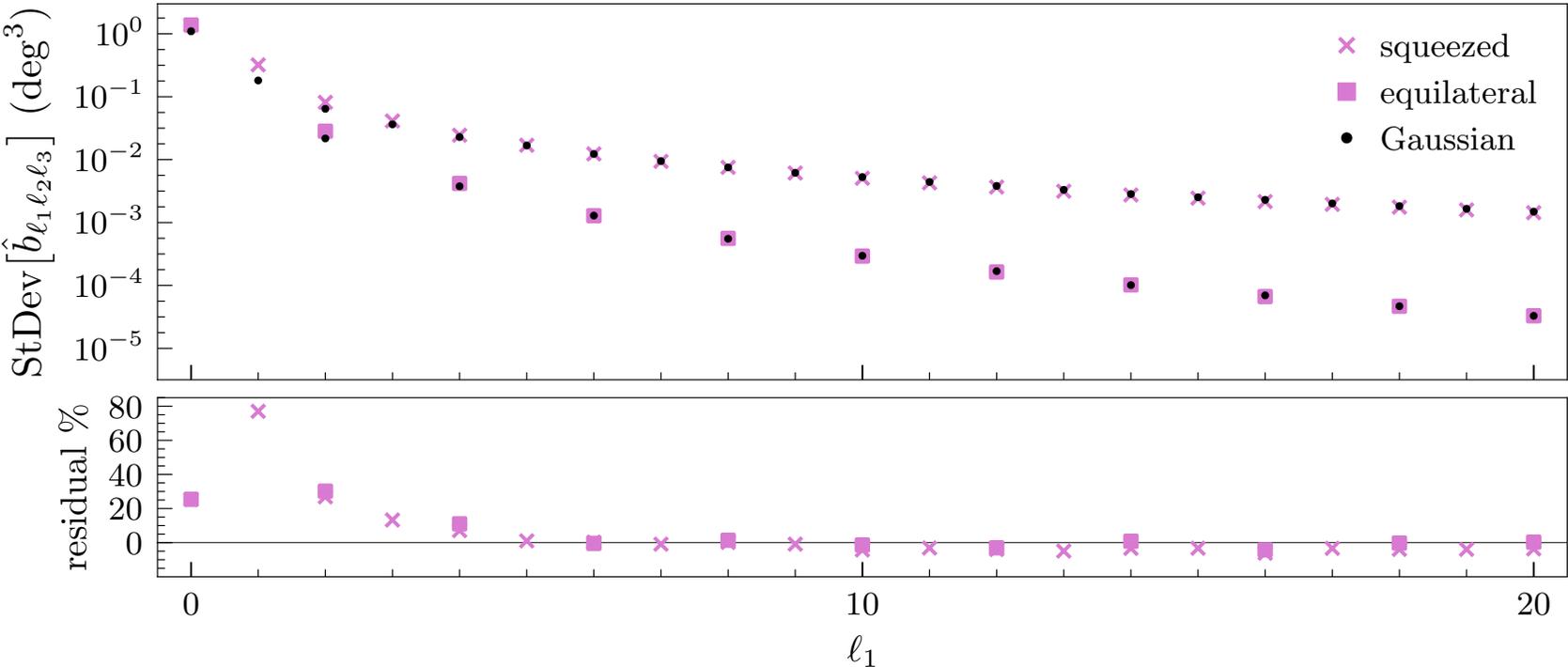
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$$\hat{b}_{\ell_1 \ell_2 \ell_3} = h_{\ell_1 \ell_2 \ell_3}^{-1} \sum_{m_1=-\ell_1}^{\ell_1} \sum_{m_2=-\ell_2}^{\ell_2} \sum_{m_3=-\ell_3}^{\ell_3} \begin{pmatrix} \ell_1 & \ell_2 & \ell_3 \\ m_1 & m_2 & m_3 \end{pmatrix} \hat{\alpha}_{\ell_1 m_1} \hat{\alpha}_{\ell_2 m_2} \hat{\alpha}_{\ell_3 m_3}$$

average bispectrum  
and comparison with Gaussian random field



# Measures of NG 3: scattering transform

Yin, Dai, Ferraro (2023)

std. method  
power spectrum

signal:  $I_0(\mathbf{x})$   
 plane wave:  $\phi_{\mathbf{k}}(\mathbf{x})$   
 $P_{\mathbf{k}}(\mathbf{x}) = \langle |I_0 * \phi_{\mathbf{k}}|^2 \rangle(\mathbf{x})$

new method  
scattering transform

wavelet:  $\psi^{j,l}(\mathbf{x})$

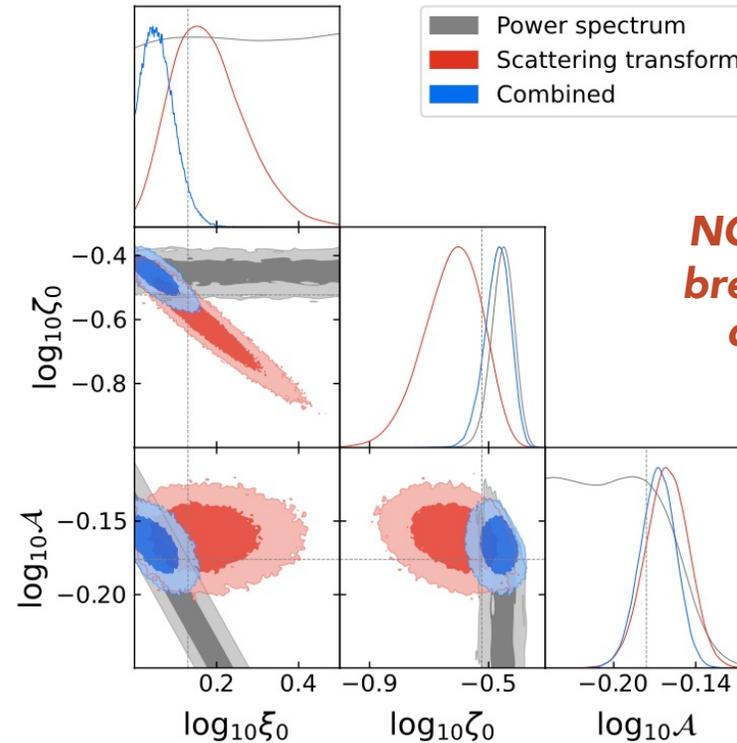
$$I_1^{j,l}(\mathbf{x}) = \langle |I_0 * \psi^{j,l}|^2 \rangle(\mathbf{x})$$

$$I_2^{j_1,l_1,j_2,l_2}(\mathbf{x}) = \langle |I_1^{j_1,l_1} * \psi^{j_2,l_2}|^2 \rangle(\mathbf{x})$$

$$s_1^j = \langle I_1^{j,l} \rangle_{\mathbf{x},l}$$

$$s_2^{j_1,j_2} = \langle I_2^{j_1,l_1,j_2,l_2} \rangle_{\mathbf{x},l_1,l_2}$$

comparison  
pow-spec vs. scatt-transform



**NG information  
breaks the  $A^2 \xi_0$   
degeneracy**

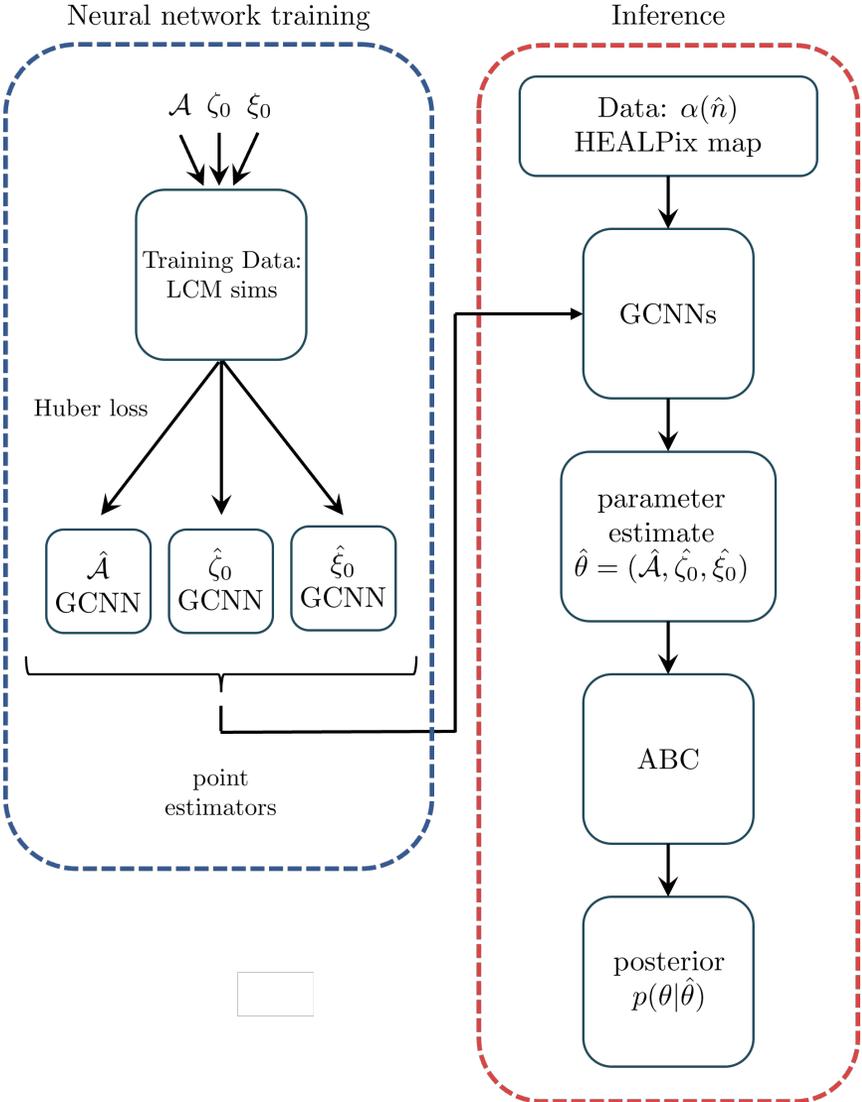
(b)  $A^2 \xi_0 = 0.6$ ,  $A = 2/3$ ,  $\zeta_0 = 0.3$

machine learning  
for axion string identification

# Machine learning for axion strings

--- early stages ---

goal: to train an AI to identify features of axion strings in CMB polarization maps



Ray Hagimoto (Rice U grad)

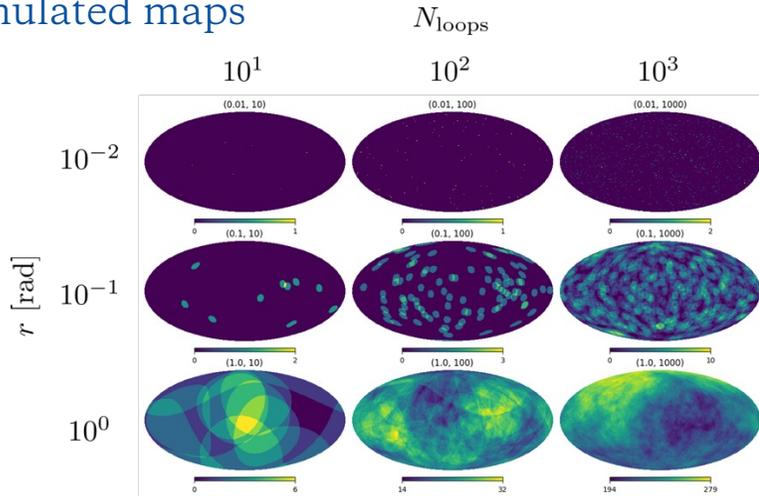
# Machine learning for axion strings

--- early stages ---

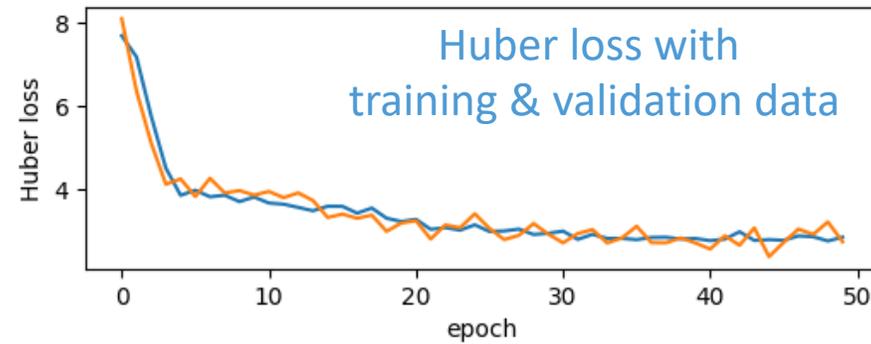


Ray Hagimoto  
(Rice U grad)

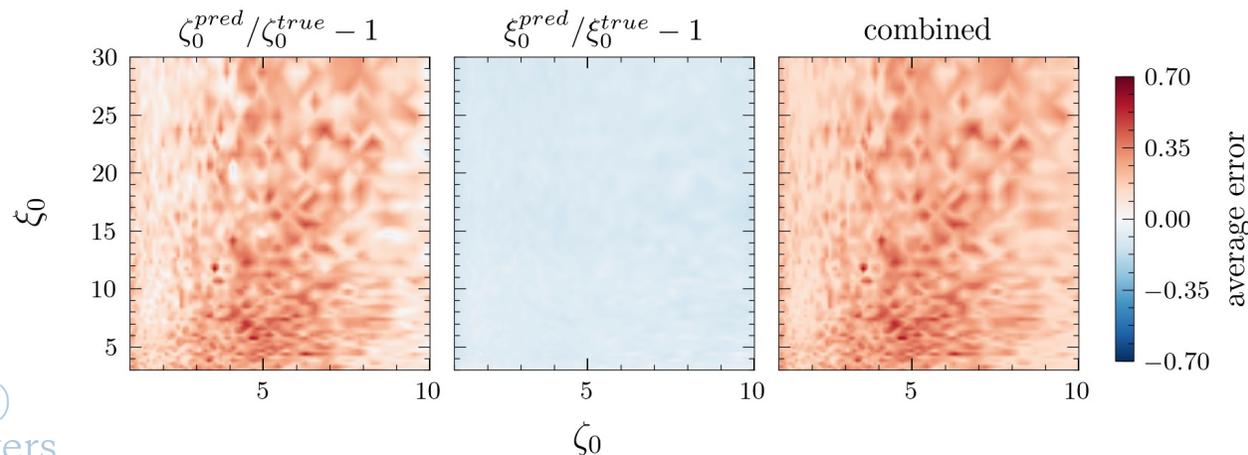
simulated maps



training



how well is it working? ... not bad!



things to do  
& where we're going:

- detector noise
- beyond LCM sims
- real CMB data
- projections

package: DeepSphere (Python)  
architecture: 3 conv + 3 pool layers

summary  
& conclusion

# Summary

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- We use existing [measurements of anisotropic birefringence](#) (Planck, SPT, ...) to place constraints on this scenario. Next-generation telescopes (CMB-S4) will probe  $O(1)$  electromagnetic anomaly coefficients and thereby probe the axion's UV embedding
- We argue that measurements of anisotropic birefringence could not only reveal the presence of a hyper-light ALP in Nature, but also lead to a [measurement of its mass](#)
- Our ongoing work (very early stages) seeks to use [machine learning](#) techniques (spherical CNN) to detect the subtle signal of axion strings in CMB polarization data