

#### Lecture 4

#### To Infinity and Beyond!



#### Question : What would you observe if you were able to know what mass state propagated from source to detector?



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$$Prob(v_{\alpha} \rightarrow v_{\beta}) \propto \left|\sum_{i} U_{\alpha i}^{*} \operatorname{Prop}(v_{i}) U_{\beta i}\right|^{2}$$



Question : What would you observe if you were able to know what mass state propagated from source to detector?

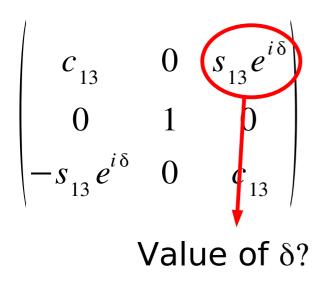
$$Prob(v_{\alpha} \rightarrow v_{\beta}) \propto \sum_{i} |U_{\alpha i}^{*} \operatorname{Prop}(v_{i})U_{\beta i}|^{2}$$
$$\rightarrow \sum_{i} |U_{\alpha i}^{2}| |U_{\beta i}|^{2}$$

The Prop term is just a phase rotation so vanishes

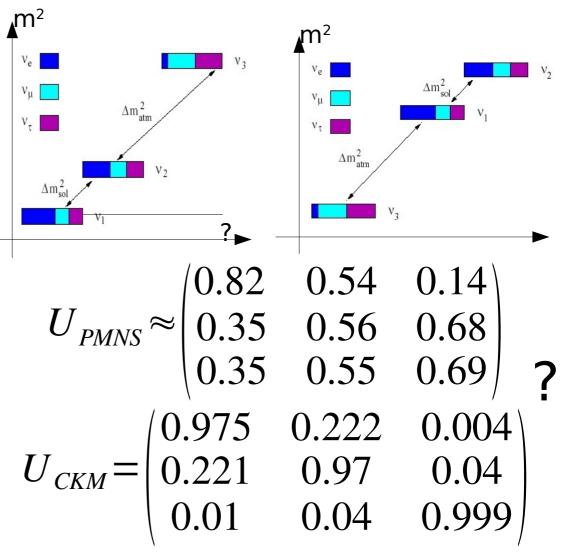
The probability is now a constant – there is flavour change if mixing can still happen – but now the oscillation has vanished, as the interference between mass states no longer exists...

### The Quest





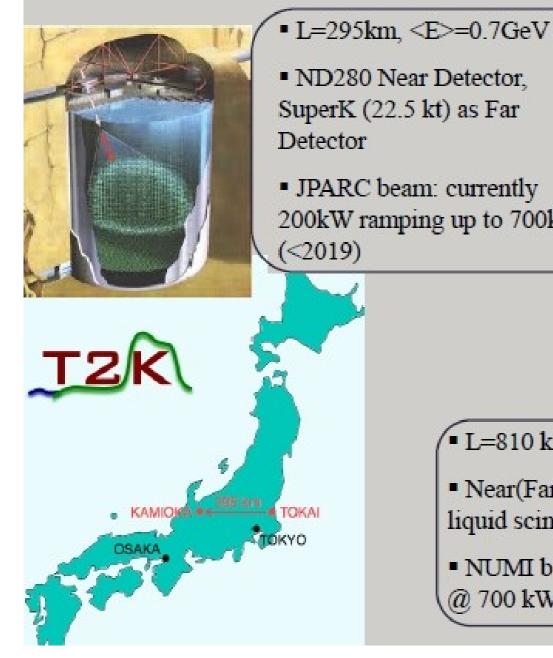
#### Normal or Inverted mass heirarchy?

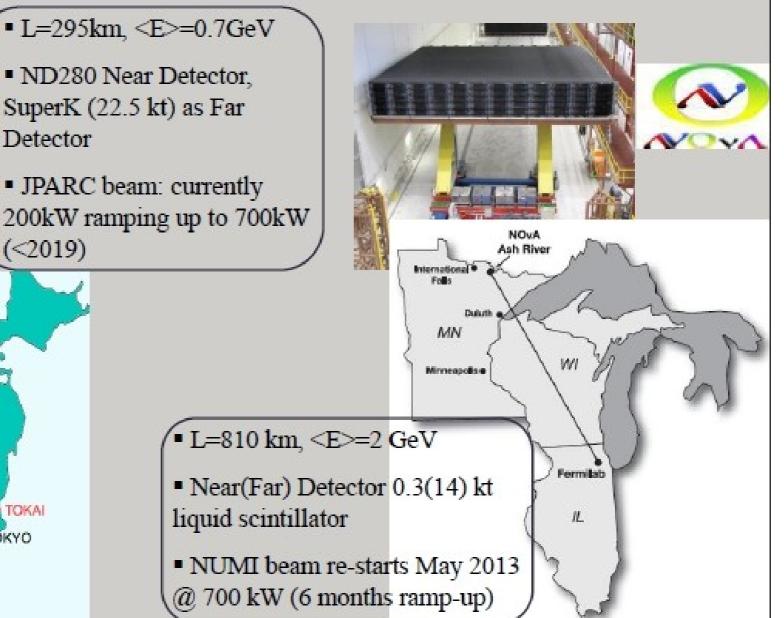


Better estimates of the oscillation parameters using accelerators
Is θ<sub>23</sub> maximal?
Is the neutrino Majorana?
What is the absolute mass?

#### **Current Experiments**







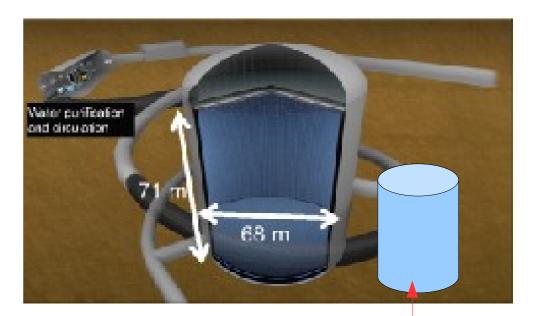
#### Next generation



#### DUSEL Underground Neutrino Experiment (DUNE)

#### Hyper-Kamiokande 300 km baseline



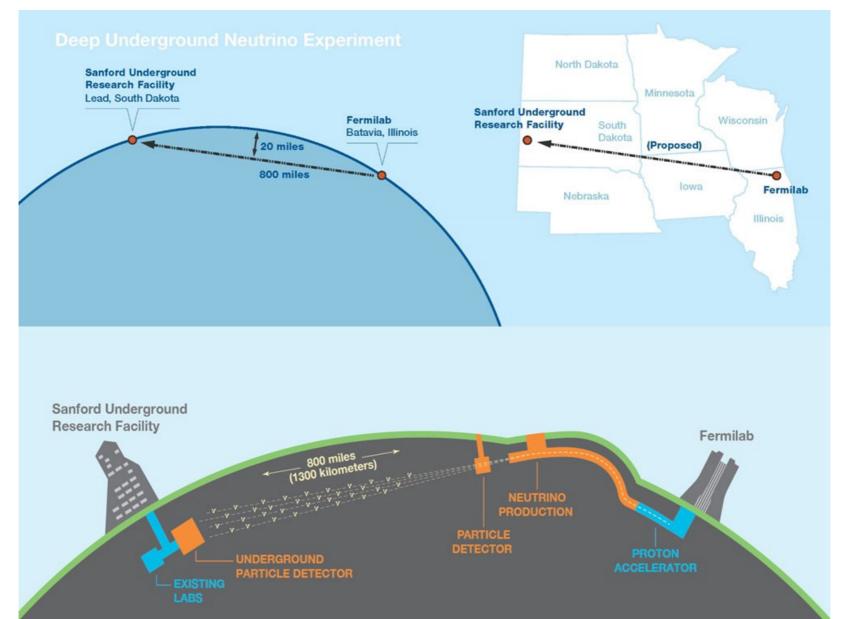


#### SK (to scale'ish)

### MW beamsmulti-kton far detectors

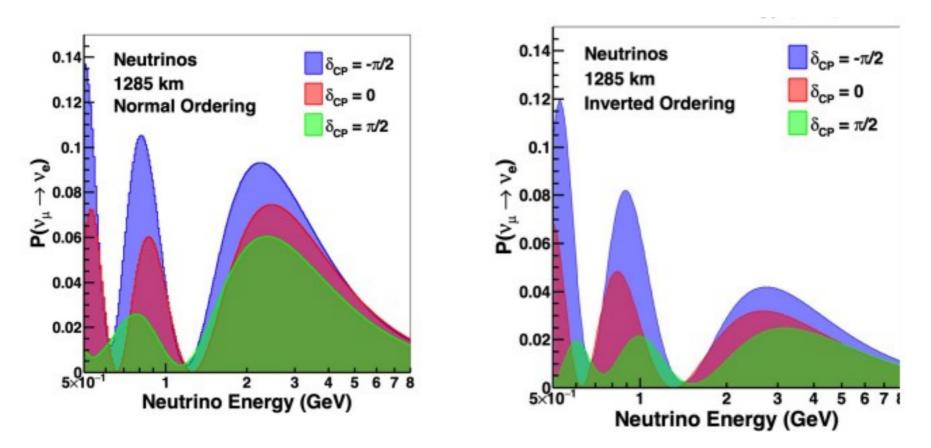


#### DUNE in the USA





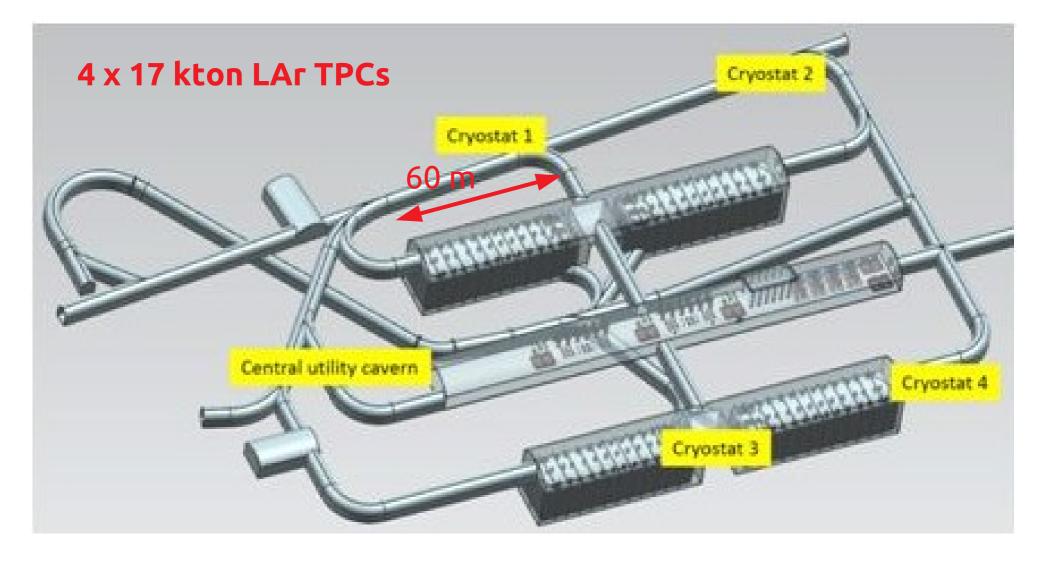




 DUNE operates a wide-band beam
 Comparison of the peaks of the first AND second oscillation maxima can be used to measure the mass ordering and δ<sub>CP</sub>

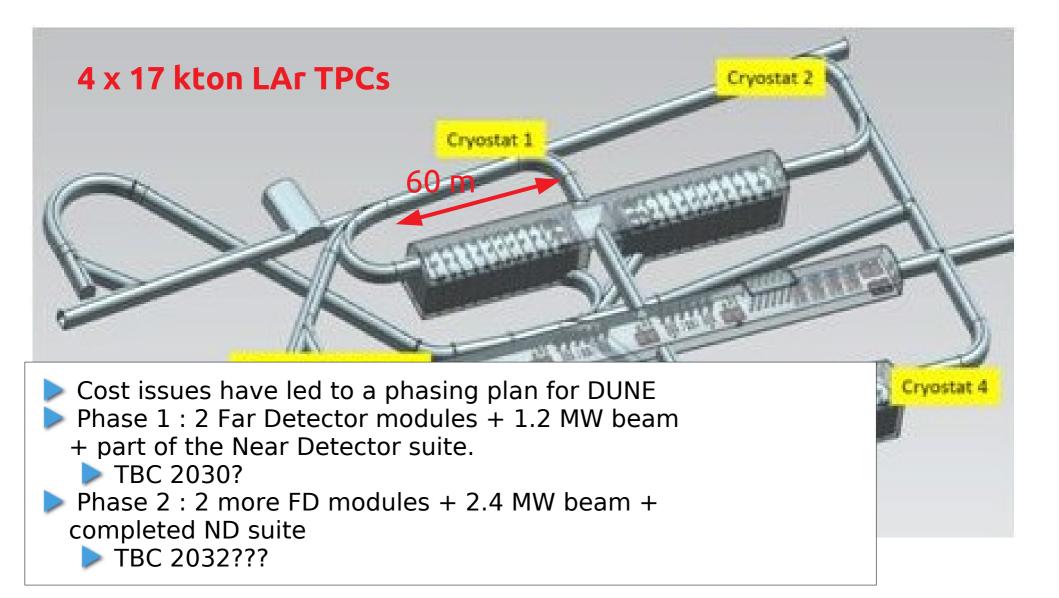


#### **DUNE Far Detector**



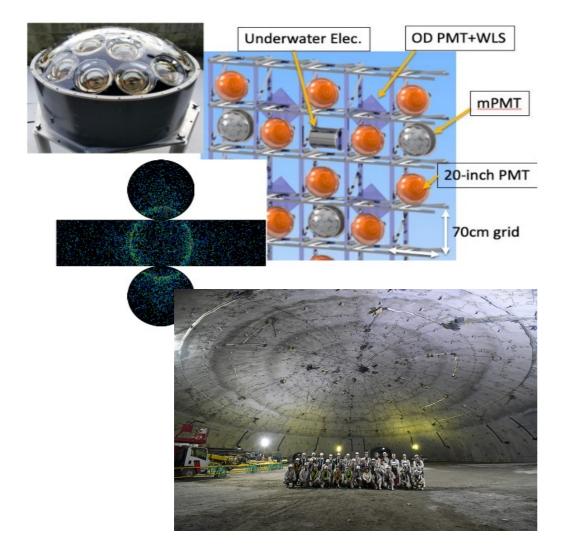


#### **DUNE Far Detector**



#### Hyper-Kamiokande





Three detectors:
HK Far Detector
Upgraded Near detector
New "Intermediate" detector

 FarDet complete : 2028
 Beam upgrades complete : 2028
 First data : 2028-2029

Construction through to 2028'ish

Super-K: 25 kton water Hyper-K: 200 kton



## Dune / HK Comparison

	DUNE	Нурег-К	T2K
Beam Energy	3 GeV	0.7 GeV	0.7 GeV
Baseline (L)	800 km	295 km	295 km
Beam Power	1.2 MW	1.2 MW	0.5 MW
Type of Beam	Wideband	Off-axis	Off-axis
Mass of far detector	40 kton (P1) up to 80 kton (P2)	190 kton	22.5 kton
Technology	Liquid Ar TPC	Water Cerenkov	Water Cerenkov
Running from	2030'ish	2028'ish	Now



#### *CP violation and the Mass Hierarchy*



Measuring  $\delta_{CP}$  is the ultimate goal of neutrino oscillation experiments. How?  $\delta_{CP}$  shows up in the imaginary part of the PMNS matrix.

$$Prob(v_{\alpha} \rightarrow v_{\beta}) = \delta_{\alpha\beta} - 4\sum_{i>j} \Re(U_{\alpha i}^{*}U_{\beta i}U_{\alpha j}U_{\beta j}^{*}) \sin^{2}(\Delta m_{ij}^{2}\frac{L}{4E})$$
$$+ 2\sum_{i>j} \Im(U_{\alpha i}^{*}U_{\beta i}U_{\alpha j}U_{\beta j}^{*}) \sin(\Delta m_{ij}^{2}\frac{L}{2E})$$
$$= 0 \text{ if } a = \beta$$

CP violation can only take place in *appearance* experiments

Look for 
$$P(v_{\mu} \rightarrow v_{e}) \neq P(\overline{v_{\mu}} \rightarrow \overline{v_{e}})$$

In all it's naked glory  

$$P(v_{\mu}(\overline{v_{\mu}}) \rightarrow v_{e}(\overline{v_{e}})) = P_{1} + P_{2} + P_{3} + P_{4}$$

$$P_{1} = \sin^{2} \theta_{23} \underline{\sin^{2} 2 \theta_{13}} \left(\frac{\Delta_{13}}{B_{-+}}\right)^{2} \sin^{2}(\frac{B_{+-}}{2}L)$$

$$P_{2} = \cos^{2} \theta_{23} \sin^{2} 2 \theta_{12} \left(\frac{\Delta_{12}}{A}\right)^{2} \sin^{2}(\frac{A}{2}L)$$

$$P_{3} = J \cos \delta \cos(\frac{\Delta_{23}}{2}L) \left(\frac{\Delta_{12}}{A} \frac{\Delta_{13}}{B_{-+}}\right) \sin(\frac{A}{2}L) \sin(\frac{B_{-+}}{2}L)$$

$$P_{4} = \pm J \sin \delta \sin(\frac{\Delta_{23}}{2}L) \left(\frac{\Delta_{12}}{A} \frac{\Delta_{13}}{B_{-+}}\right) \sin(\frac{A}{2}L) \sin(\frac{B_{-+}}{2}L)$$

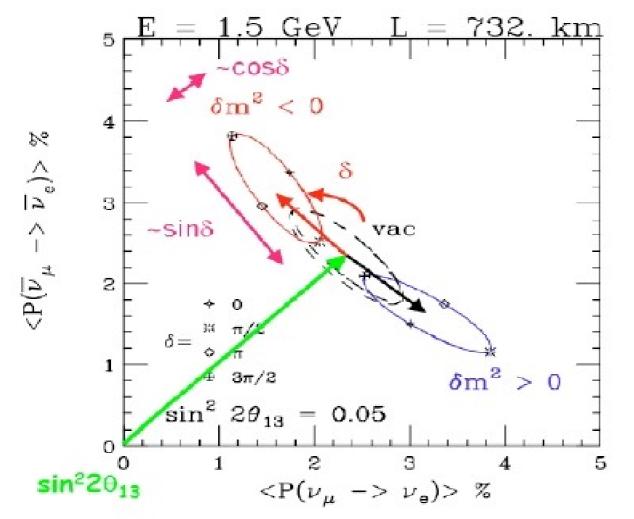
$$\Delta_{ij} = \frac{\Delta m_{ij}^{2}}{2E} \qquad A = \sqrt{2}G_{F}N_{e}$$

$$J = \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \sin 2\theta_{13}$$

#### Degeneracies



Experiments only measure at most two numbers; but probability has three unknowns and parameters with errors.

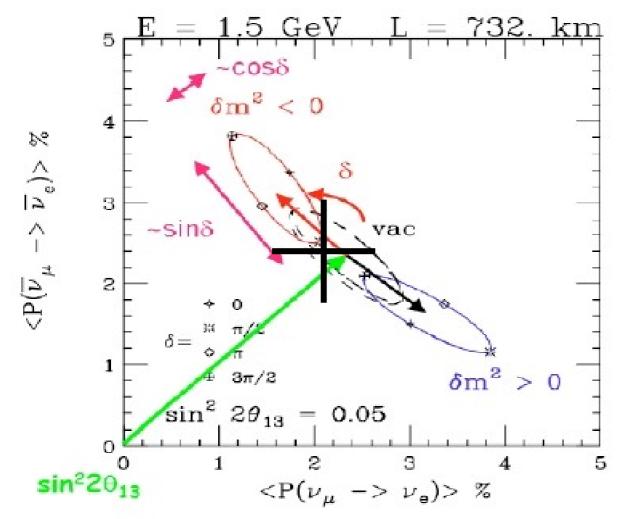


Need more than one measurement at different L/E to disentangle the parameter space

#### Degeneracies



Experiments only measure at most two numbers; but probability has three unknowns and parameters with errors.



Need more than one measurement at different L/E to disentangle the parameter space

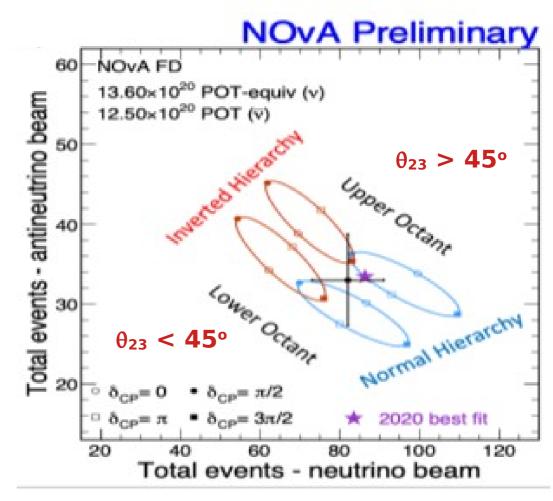
#### Mass Hierarchy measurements



As baseline grows, matter effects increase

At distances of around 1000 km we can unambiguously identify the mass hierarchy

Once we've done that we need to determine CP phase



## JUNO



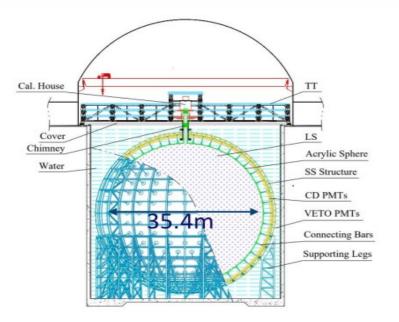
**Neutrino source:** 26.6 GW<sub>th</sub> from nuclear reactors

Experiment location: Jiangmen, China Baseline: 53km

Main detector technology: Liquid

Scintillator

Current Status: Under construction

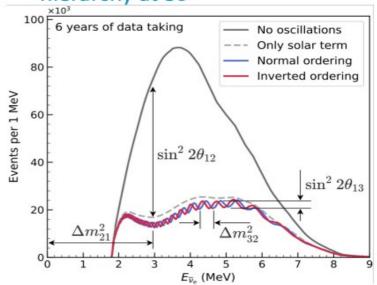


Largest liquid scintillator detector ever build

□ JUNO will measure  $\bar{\nu}_e$  from Yangjiang and Taishan power plants

#### ❑ Main goal: Neutrino Mass ordering

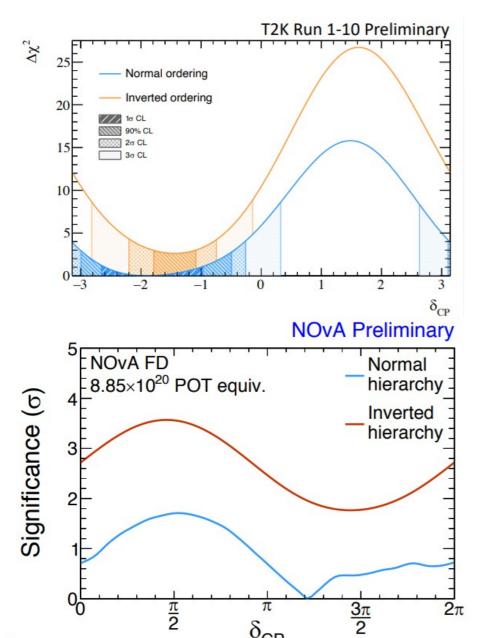
- Simultaneous measurement of  $\Delta m^2{}_{31}$  and  $\Delta m^2{}_{32}$
- Independent of **\delta**CP and octant of  $\theta_{23}$ 
  - 6 years operation to determine mass hierarchy at  $3\sigma$



Data taking to begin this year

### Hints of $\delta_{CP}$ ? T2K & NOvA





Normal ordering weakly favoured

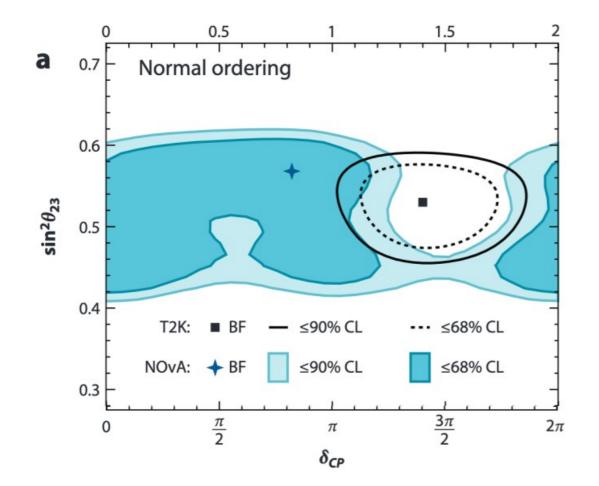
- $> \delta_{CP} = 0$  disfavoured at  $2\sigma$
- $> \delta_{CP} > 0$  disfavoured at  $3\sigma$

Best fit: Normal hierarchy favoured at 1.8 σ

Excludes  $\delta_{CP} = \pi / 2$  in the inverted hierarchy at > 3 σ

#### Slight tension





Experiments are complementary : different baselines and energies mean that size of the mass ordering and  $\delta_{CP}$ effects are different

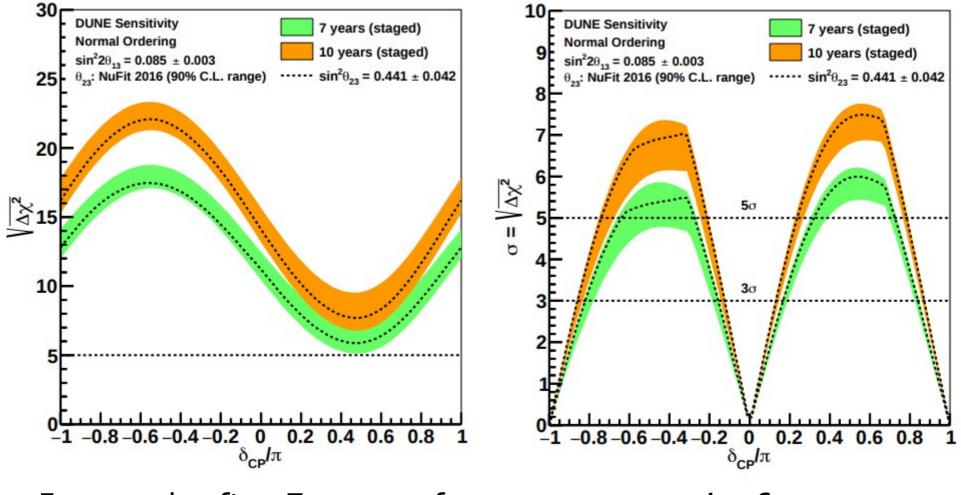
A combined fit of T2K and NOVA data is in the works.



## Future project sensitivities



#### $\delta_{CP}$ : DUNE Sensitivity

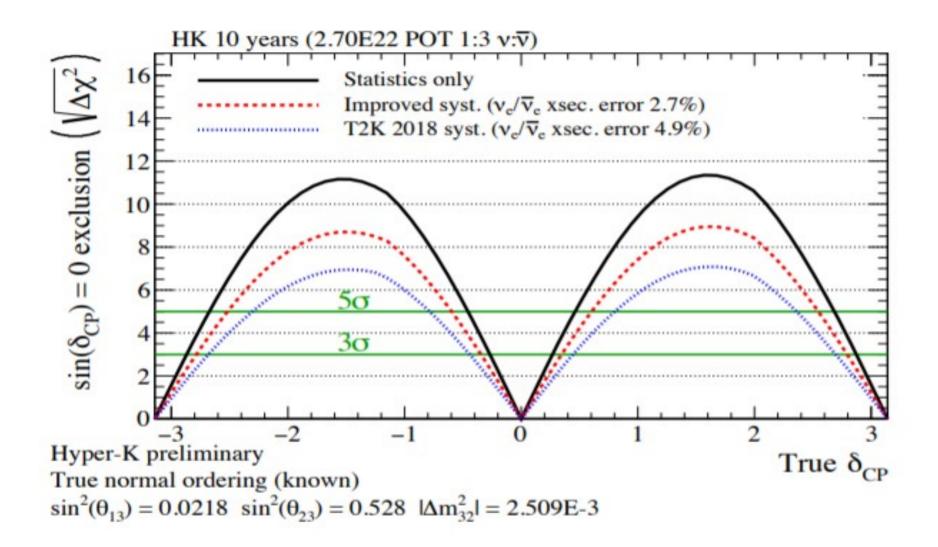


> 5  $\sigma$  reach after 7 years of running over entire  $\delta_{CP}$  range

> 5  $\sigma$  reach after 10 years if  $\delta_{CP}$  exists in ±[0.2-0.8] $\pi$ 



#### HK $\delta_{CP}$ Sensitivity



## A return to $0\nu\beta\beta$ decay

 $m_2$ 

 $m_1$ 

m<sub>3</sub>



$$\Gamma(0\,\nu\beta\beta)\propto|\langle m_{\nu_e}\rangle|^2=|\sum_i|U_{ei}^2|m_ie^{i\phi_i}|^2$$

In the inverted ordering :  $m_3 << m_1 \approx m_2$ ,  $\Delta m_{13}^2 \approx \Delta m_{23}^2$ and  $m_3$  is the lightest mass state, so we can write

$$m_{\nu_{e}}^{2} = \left\| U_{e1} \right\|^{2} \sqrt{m_{3}^{2} + \Delta m_{23}^{2}} + \left| U_{e2} \right|^{2} e^{i\alpha_{2}} \sqrt{m_{3}^{2} + \Delta m_{23}^{2}} + \left| U_{e3} \right|^{2} e^{i\alpha_{3}} m_{3}^{2} \right\|^{2}$$

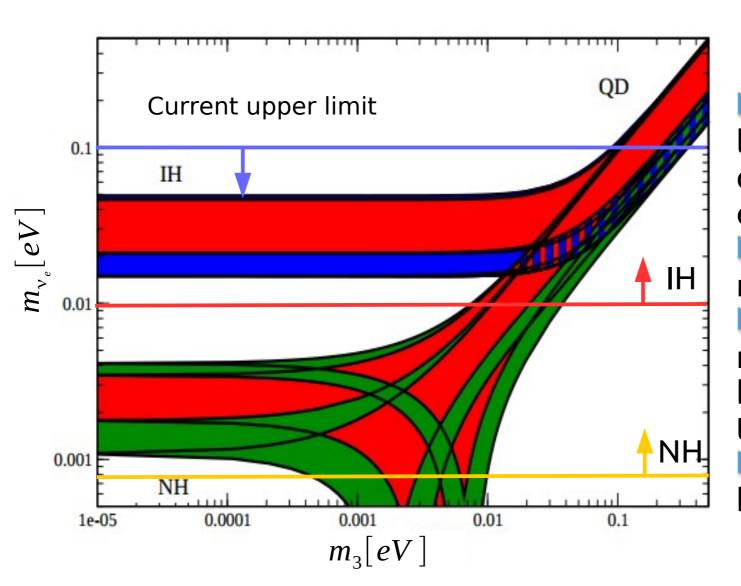
Setting m<sub>3</sub> to zero (not a bad approximation) one can show that

$$m_{v_e} > \sqrt{\Delta m_{23}^2} \cos^2 \theta_{13} (1 - 2 \sin^2 \theta_{12})$$

i.e for the inverted hierarchy, the average electron neutrino mass would have a *lower limit at small m*<sub>3</sub>

#### Mass hierarchy & 0νββ decay

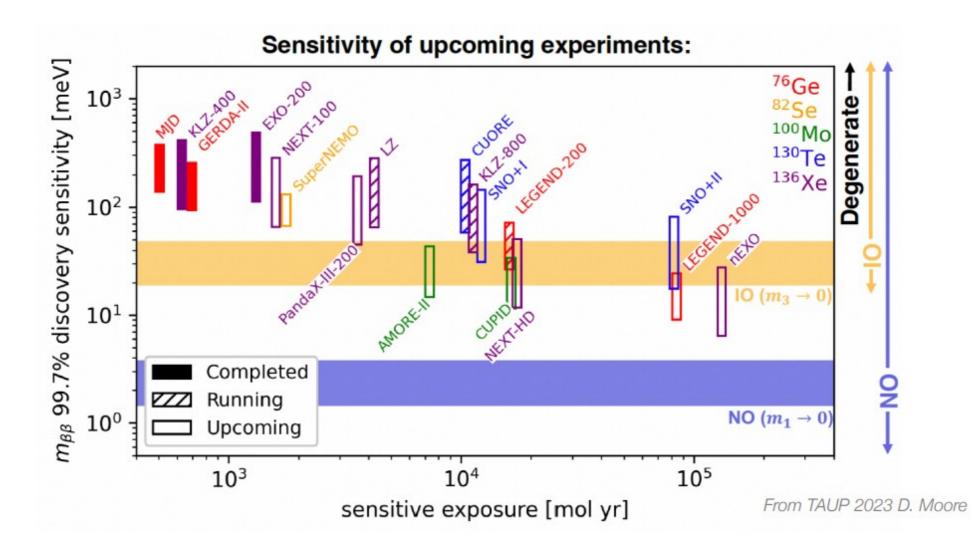




Experimental limit needs to decrease by a factor of 10 Limit scales with mass and run time Experiments need to be 10 times bigger and run 10 times longer These are being built now.

#### Exp. sensitivities





#### Mass Hierarchy Determination



A number of different experiments, both accelerator and Onbb decay focused, are now trying to determine the mass hierarchy.

**Timescale** : ~ 5 years from now for 4  $\sigma$  good indication from NOVA + T2K + JUNO

#### Measurement of $\delta_{\mathsf{CP}}$



Next generation of experiments are being planned to measure this

**Timescale** : 6-8 years from now (including 5 for construction) for  $3\sigma$  sensitivity to distinguish from no CP-violation scenario (if true  $\delta_{CP}$  is  $\pi/2$ ). 15-20 years for a measurement of  $\delta_{CP}$  to a

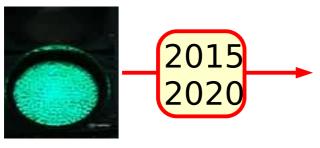
precision of 20° (if true  $\delta_{CP}$  is  $\pi/2$ ).

# The Roadmap - 2005

We are at the beginning of a global coordinated effort to unravel the neutrino sector

> Measure 23 sector to 10% MINOS, K2K, OPERA, miniBoone

Measure  $\theta_{13}$ ; Probably need 2 measurements at different L/E and an antineutrino measurement to unravel ambiguities. T2K/NOvA, Reactor experiments



Now

Precision measurements of all parameters Phase 2 Superbeams, β beams,

**Neutrino Factories** 

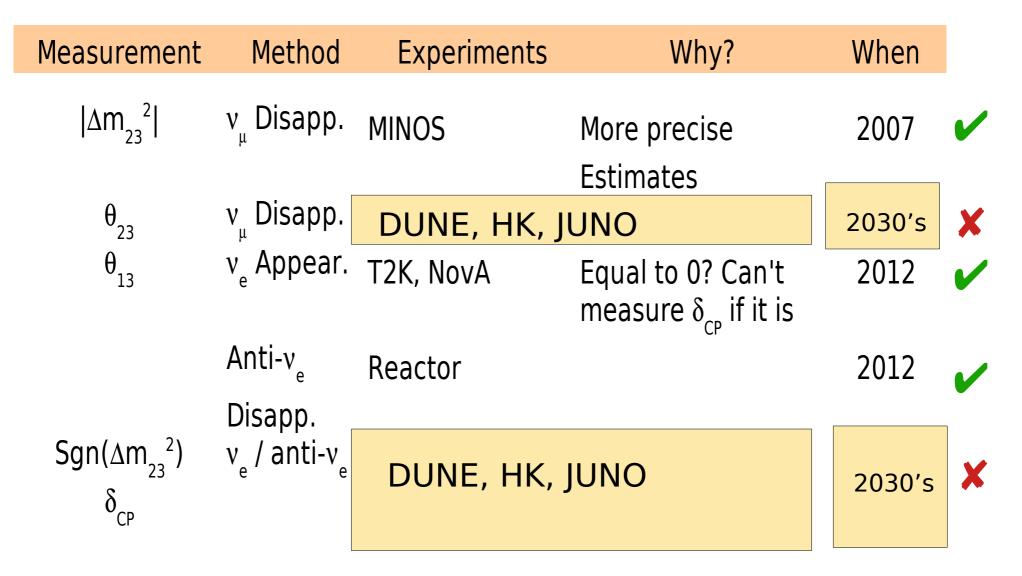
# The next 20 years – 2009 ARWICK

Measurement	Method	Experiments	Why?	When
∆m <sub>23</sub> <sup>2</sup>	$v_{\mu}^{}$ Disapp.	MINOS	More precise Estimates	2007
$\theta_{23}$ $\theta_{13}$	$v_{\mu}^{}$ Disapp. $v_{e}^{}$ Appear.	T2K, NovA T2K, NovA	Is it maximal? Equal to 0? Can't measure $\delta_{CP}$ if it is	2009 2012
	Anti-v <sub>e</sub> Disapp.	Reactor		2012
Sgn( $\Delta m_{23}^{2}$ ) $\delta_{CP}$	v <sub>e</sub> / anti-v <sub>e</sub>	T2KK, neutrino Factory, ???	Unification, GUT Lepton asymmetry	2025?

# The next 20 years – 2009 ARWICK

Measurement	Method	Experiments	Why?	When	
Δm <sub>23</sub> <sup>2</sup>	$v_{\mu}^{}$ Disapp.	MINOS	More precise Estimates	2007	~
$\theta_{_{23}}$	$\nu_{_{\mu}}$ Disapp.	T2K, NovA	Is it maximal?	2009	×
$\theta_{_{13}}$	$v_{e}^{}$ Appear.	T2K, NovA	Equal to 0? Can't measure $\delta_{_{\rm CP}}$ if it is	2012	~
	Anti-v <sub>e</sub> Diconn	Reactor		2012	~
Sgn( $\Delta m_{23}^{2}$ ) $\delta_{CP}$	Disapp. v <sub>e</sub> / anti-v <sub>e</sub>	T2KK, neutrino Factory, ???	Unification, GUT Lepton asymmetry	2025?	×

# The next 20 years – 2024 VARWICK

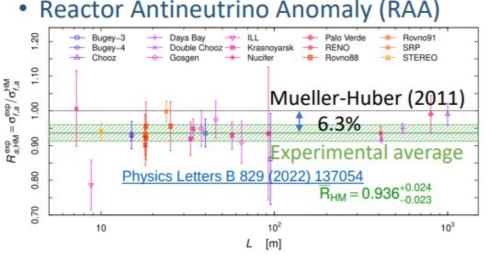


# ANOMALIES

# ANOMALIES EVERYWHERE

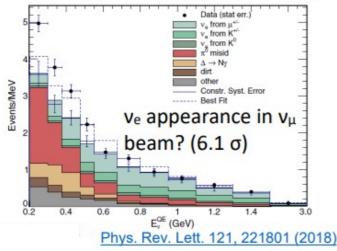
LIGHTYE



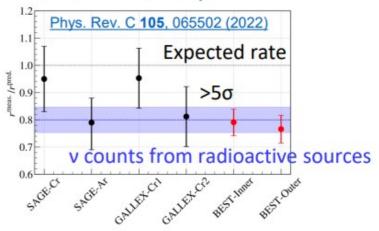


#### Reactor Antineutrino Anomaly (RAA)

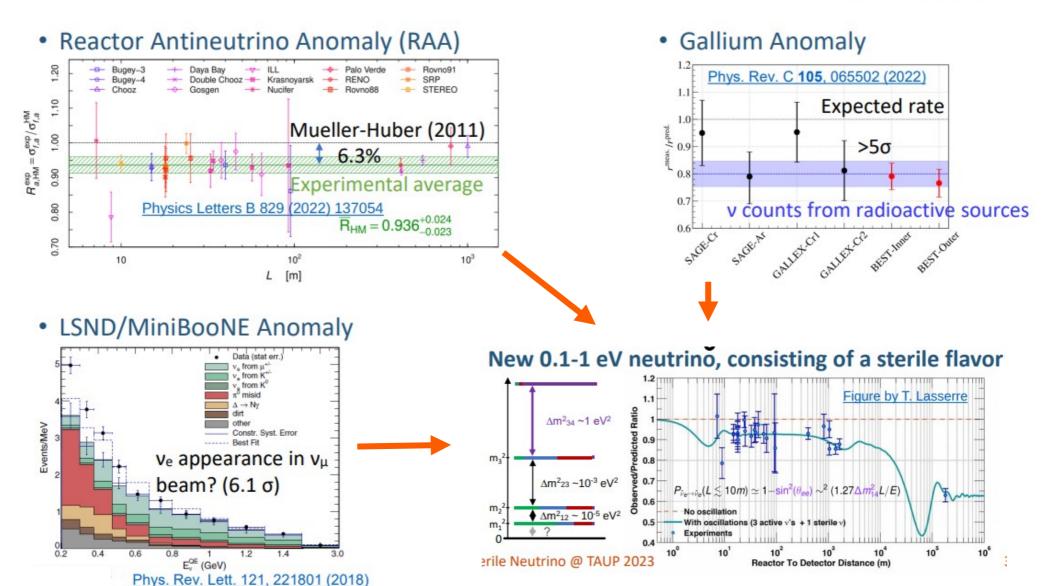
#### LSND/MiniBooNE Anomaly



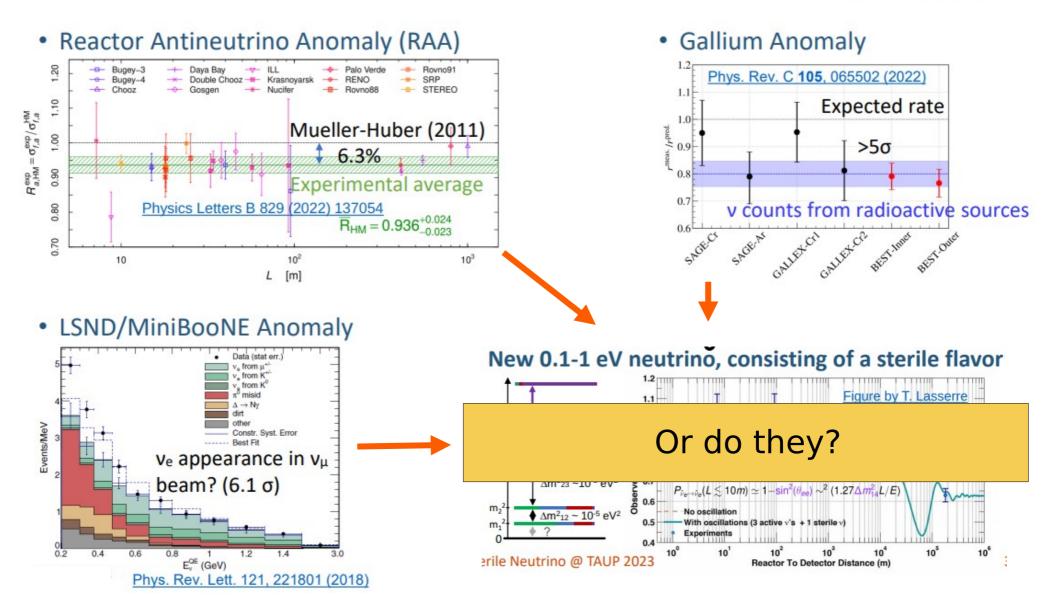
#### Gallium Anomaly













# The Gallium Anomaly

We've discussed the Homestake experiment which studied

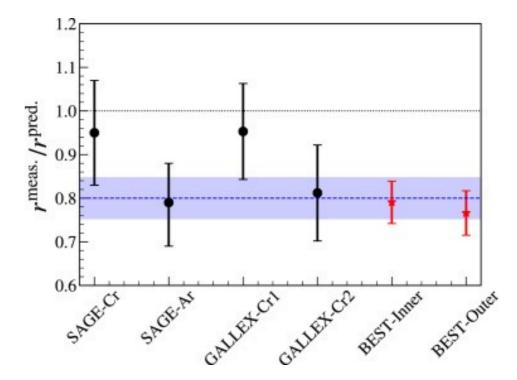
$$v_e + Cl^{37} \rightarrow Ar^{37} + e^{-1}$$

A couple of experiments (SAGE and GALLEX) also studied

 $v_e + Ga \rightarrow Ge + e^-$ 

In early 2000's the response of GALLEX was being tested using MCi radioactive sources.

Sources emitted  $\nu_{\rm e}$  which were then observed using the standard Ge signature



 $L/E \approx 0.1 \, m/0.1 \, MeV \rightarrow \Delta m^2 \approx 1 \, eV^2$ 

(or is it our understanding of the low energy v-Ga cross section, or is it just bad luck?)

# The reactor anomalies ARWICK

pre-2011 : measurement of the total neutrino flux from reactors agreed with expectation.

In 2011, new techniques in modelling nuclear reactions led to a re-evaluation of the expected electron antineutrino flux. The new estimate was about 6% higher than the old.

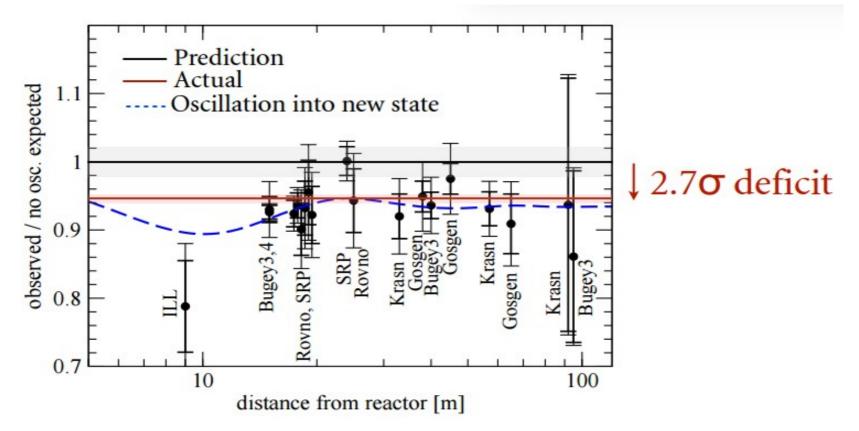
Suddenly all the experiments now observed a general deficit of electron antineutrinos being detected at the detector

$$N(\overline{\mathbf{v}}_e) = \Phi^{old}(\overline{\mathbf{v}}_e) \sigma \longrightarrow \Phi^{new}(\overline{\mathbf{v}}_e) \sigma \times P(\overline{\mathbf{v}}_e \rightarrow \mathbf{v}_s)$$

Could this be (i) the new flux estimate is just a bit dodgy or (ii) we have short baseline neutrino oscillations to a sterile state?

### **Reactor Anomaly**

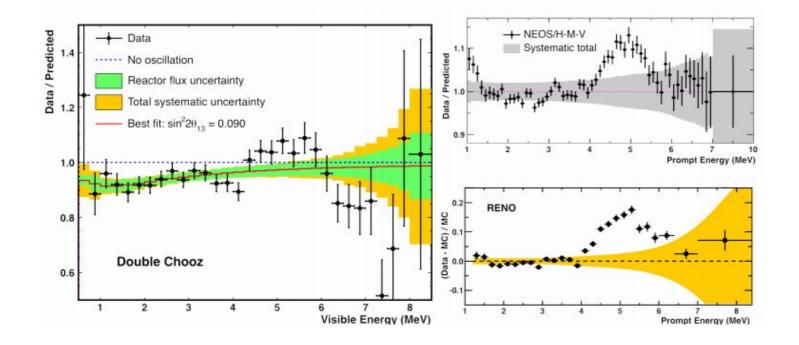




Deficit consistent with a sterile state with  $\Delta m^2 \sim 1.5 \text{ eV}^2$ Reactor antineutrino flux calculations are VERY hard to do It's almost certain that this is an issue with the calculation of the antineutrino flux NOT steriles.



### The Bump

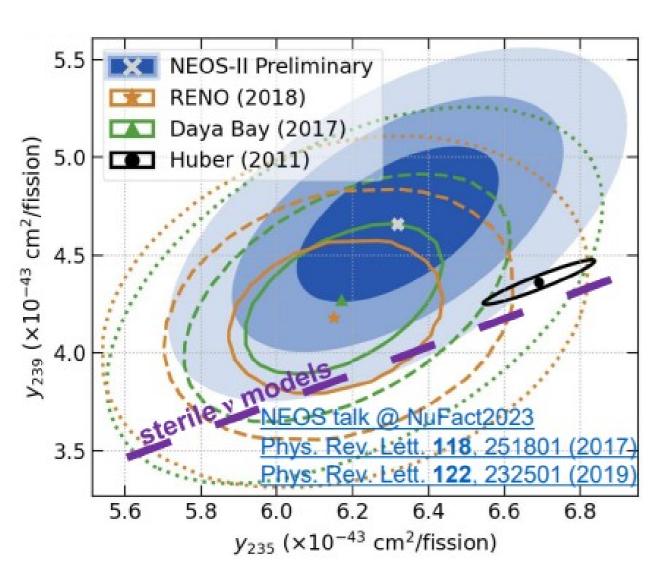


Overall there is a deficit of events with the new reactor flux estimates

- Between 4-6 GeV there seems to be an excess beyond the flux errors
- Seen in all reactor experiments
- This is quite hard to explain away using sterile neutrinos!
- Prejudice is that this is due to modelling reactor flux



### New fluxes - again



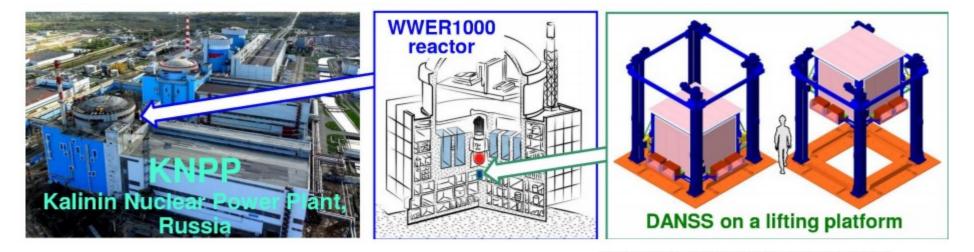
Reactor flux deficit has probably gone away now

"New" 2011 flux overestimated the flux from U-235

New flux measurements suggest that the reactor flux deficit was not real

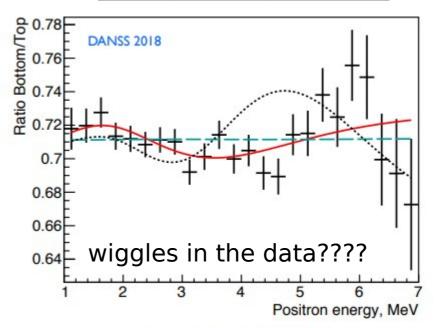


### **Reactor Experiments**



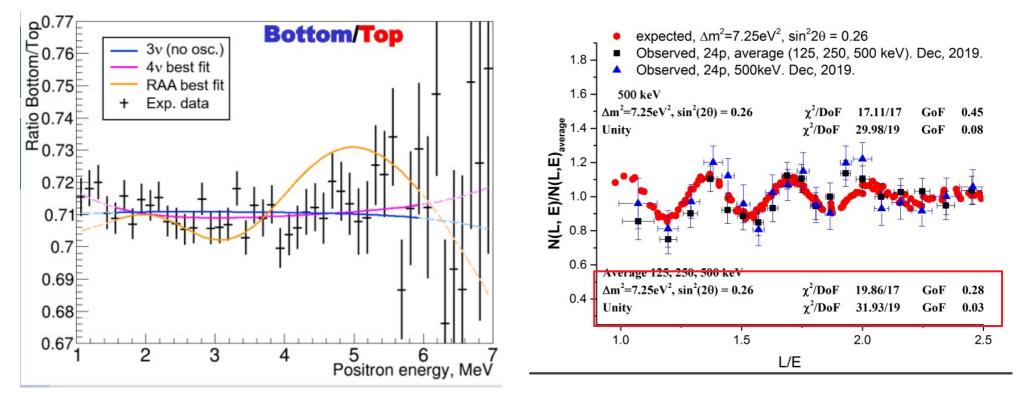
 Installed on a moveable platform under a 3 GW reactor
 Large neutrino flux
 Variable source-distance distance using the same detector
 Down : 12.7 m from reactor

Up : 10.7 m from reactor





### **Reactor Experiments**



DANSS (2020) No visible effect

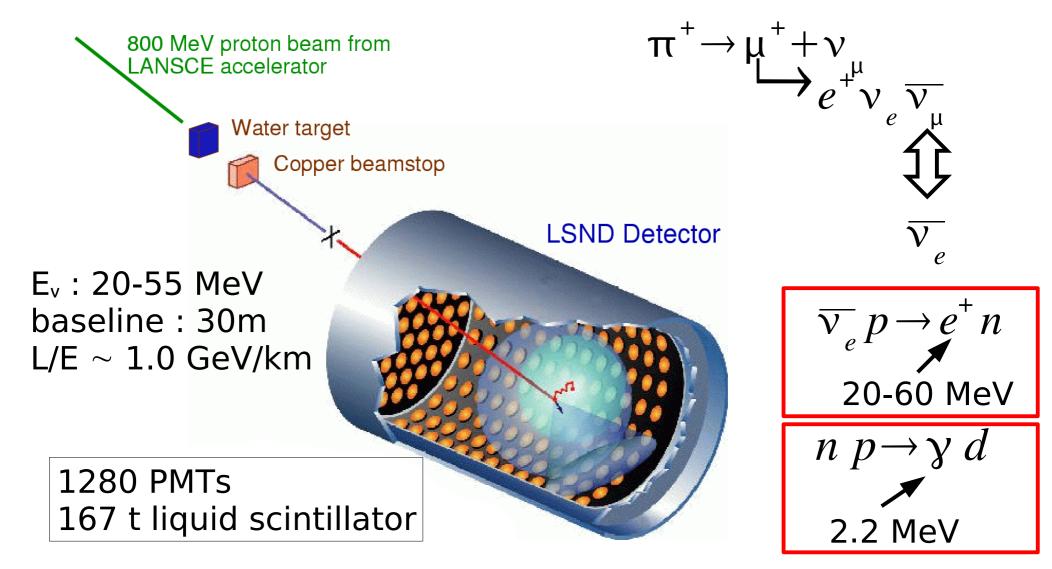
Neutrino4 (2020) Claimed signal

Situation unclear : other experiments (Stereo, SoLiD, Prospect) don't see oscillations like this.

### LSND



The LSND experiment was the first accelerator experiment to report a positive appearance signal

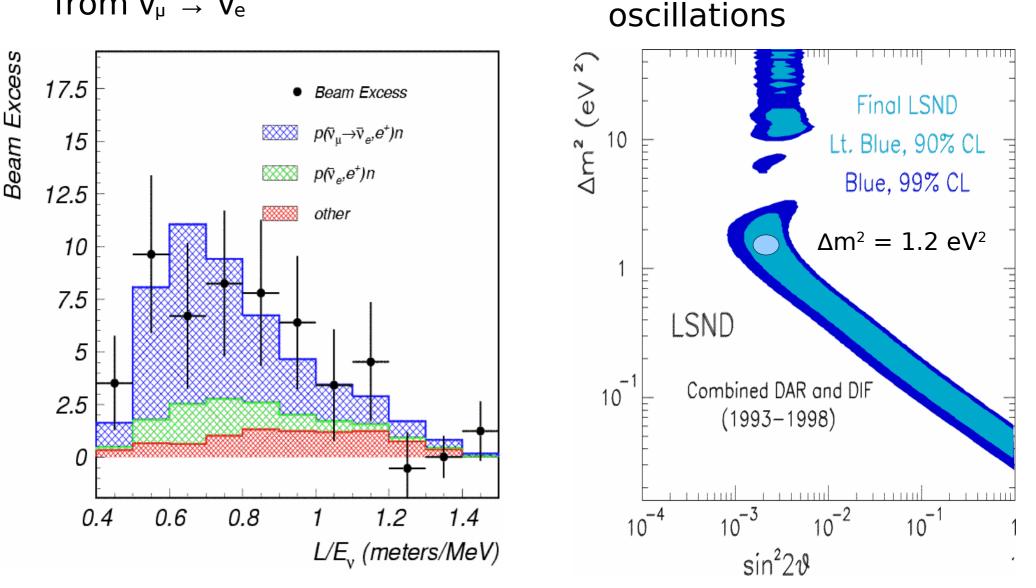


### LSND Result (1997)



3.3  $\sigma$  evidence for

87.9  $\pm$  22.4  $\pm$  6 excess events from  $\overline{v}_{\mu}$   $\rightarrow$   $\overline{v}_{e}$ 



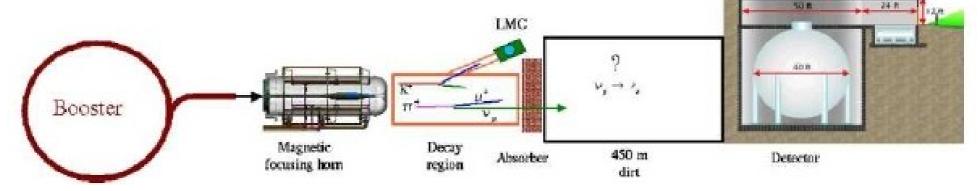
### MiniBooNE



142.00

I-I slope

Ran from 2002 to 2014 at Fermilab



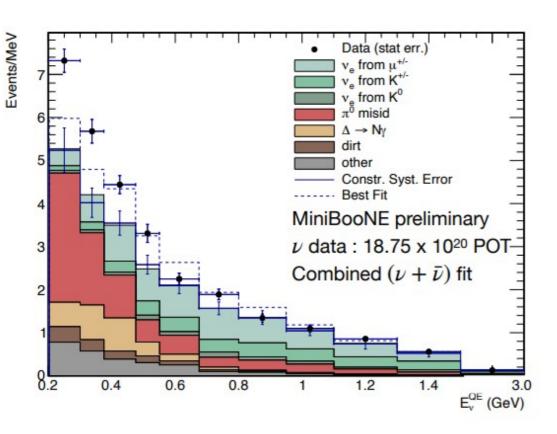
•Average neutrino energy  $\approx 1 \text{ GeV}$ 

- •L/E the same as LSND
- Same technology as LSND

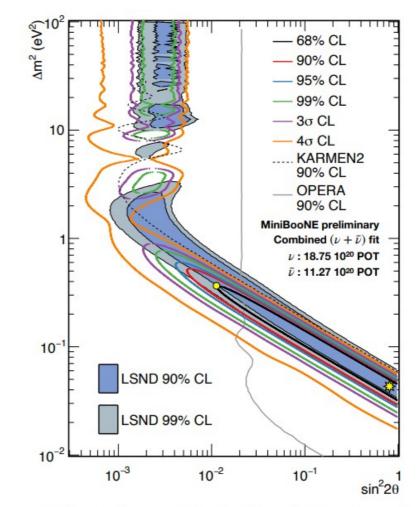
 Different energy = different event types = different systematics



### miniBooNE Results



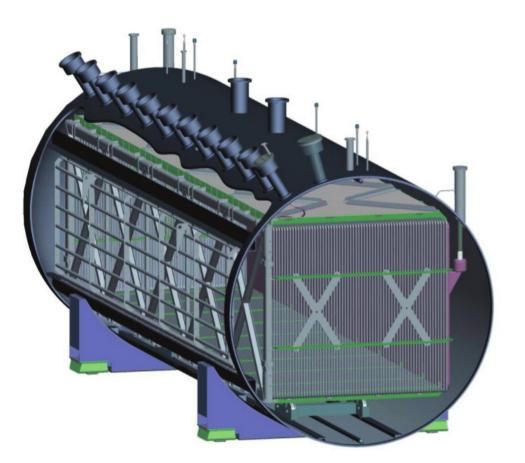
Excess at the level of 4.8  $\sigma$ 



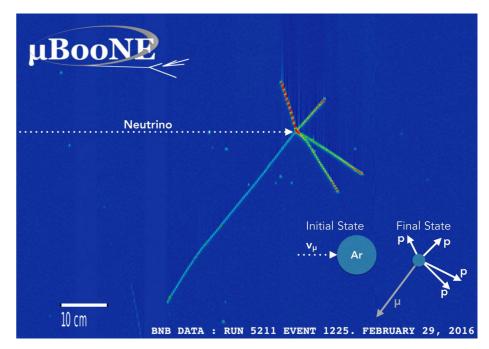
**Neutrino + Anti-Neutrino Mode**  $(\Delta m^2, \sin^2 2\theta) = (0.043 \text{ eV}^2, 0.807)$  $\chi^2/ndf = 21.7/15.5 \text{ (prob = 12.3\%)}$ 

### MicroBooNE



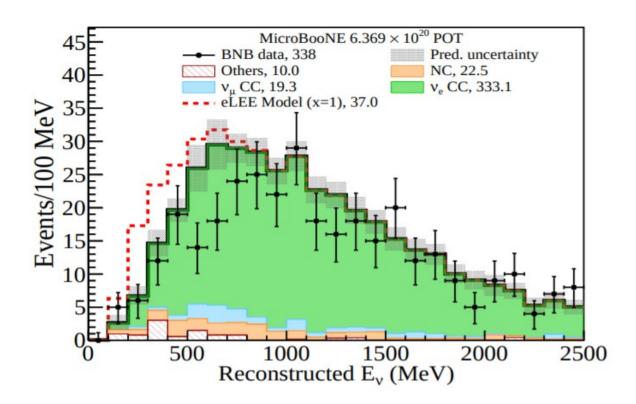


 170 ton LAr TPC
 Operating in the same beam as LSND and miniBooNE
 Capable of reconstructing electrons and photons





# Low Energy Excess



Reconstructed energy spectrum for inclusive  $\nu_{\rm e}$  event sample

No sign of excess of low energy electrons or photons.

?????

LSND/MiniBoone are seeing something though. What?

Doesn't rule out steriles though. Decaying sterile neutrinos?

**CPT Violation?** 

3+1 sterile? 3+2 ? 3+n ?





### Lorentz violation?

### Extra dimensions?

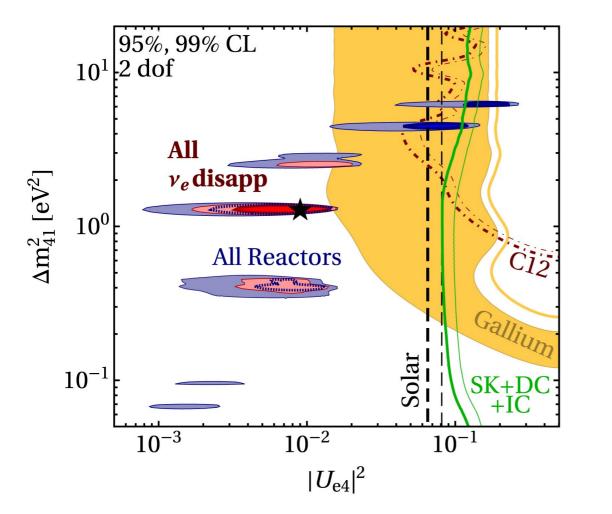
Experimental problems?

No bleedin' idea

Wait for more data

### Global analysis



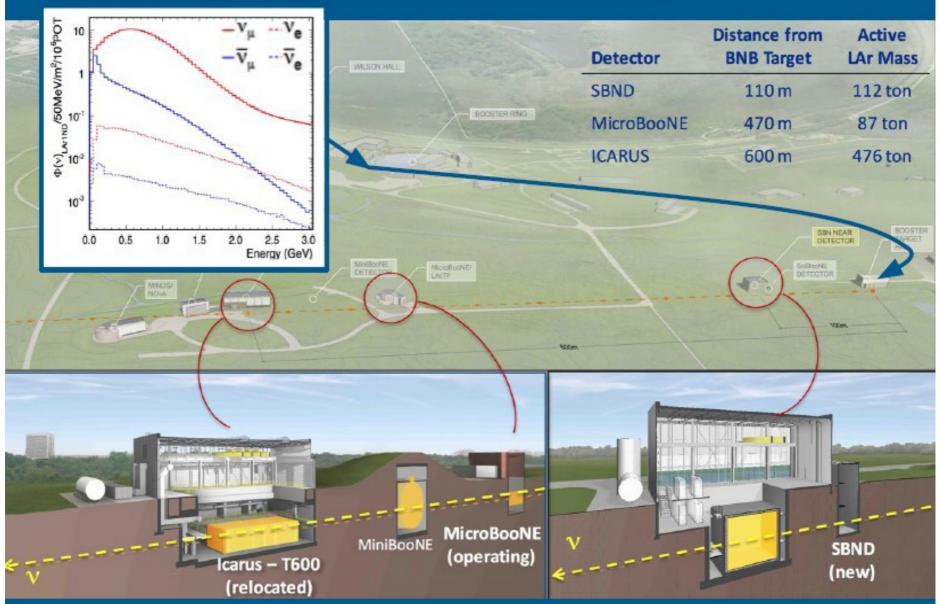


It's very hard to fit all of the data to a 3+1 (or other) models.

A consistent picture does not leap out from all these anomalies.

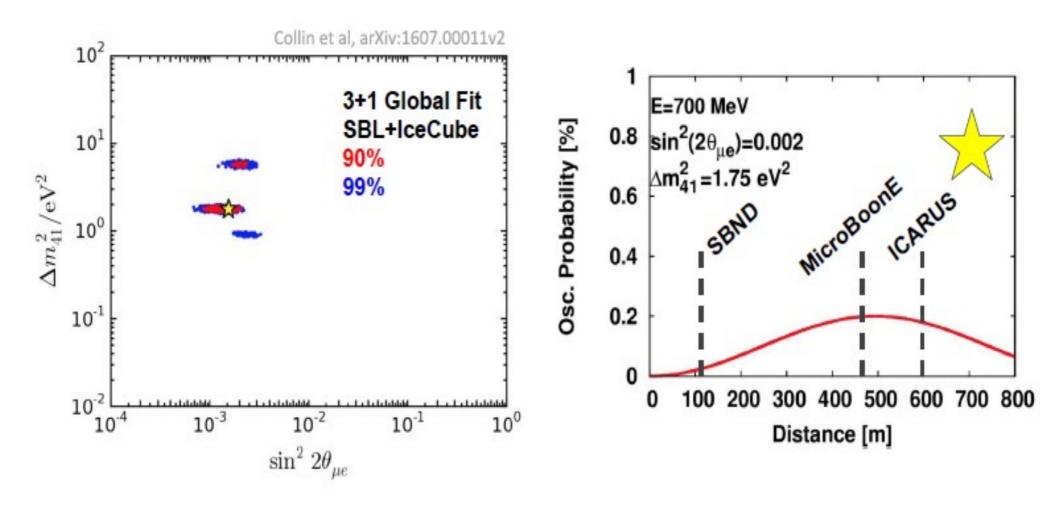
### **SBN** Program







### SBND

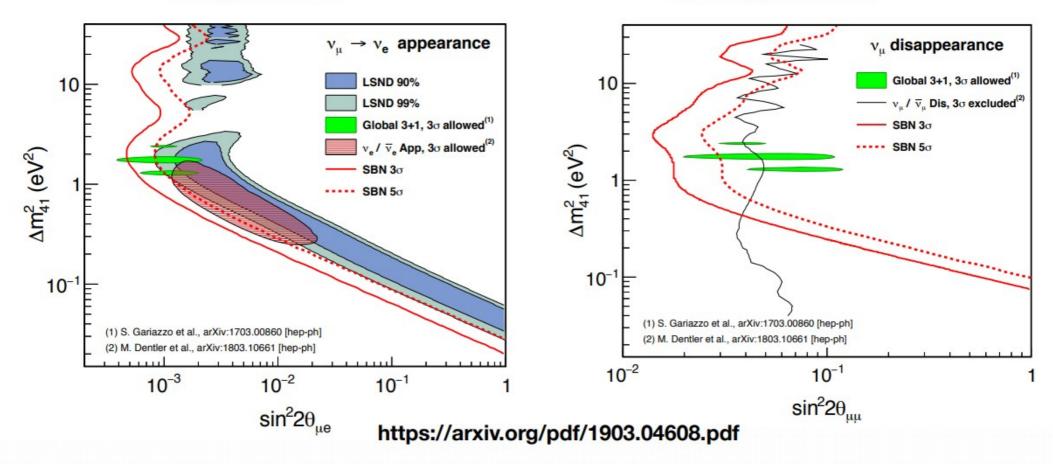


### SBND



#### ve appearance

#### v<sub>µ</sub> disappearance



• SBN cover much of the parameters allowed by past anomalies at  $>5\sigma$  significance

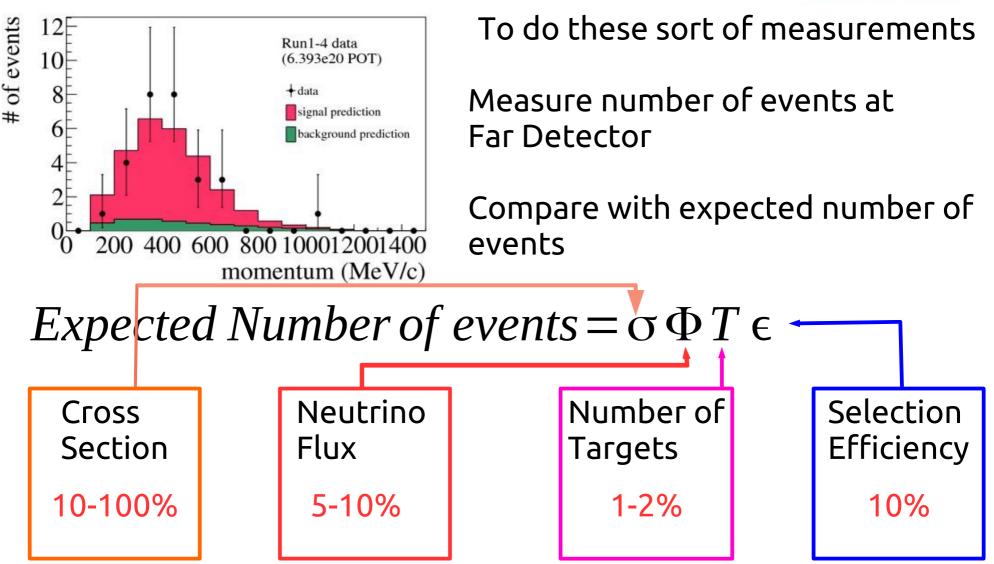
Starts taking data soon



### Neutrino Cross-sections

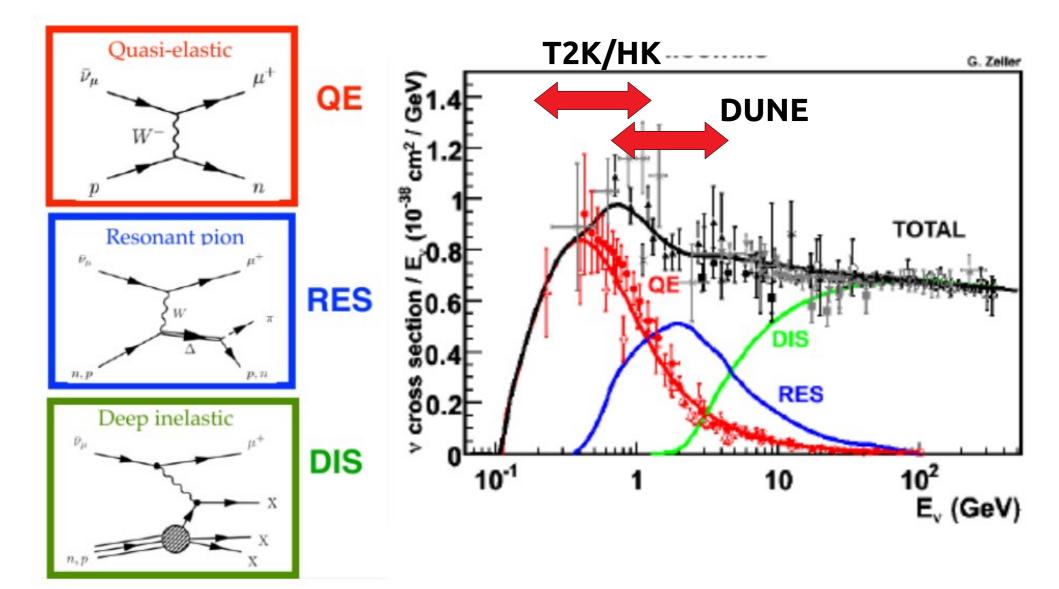
## Systematic Uncertainties







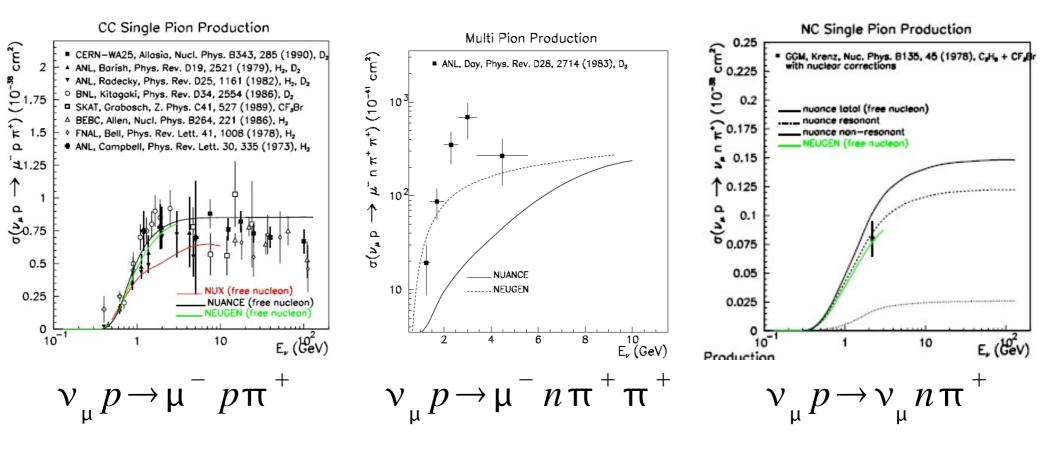
### Neutrino Interactions



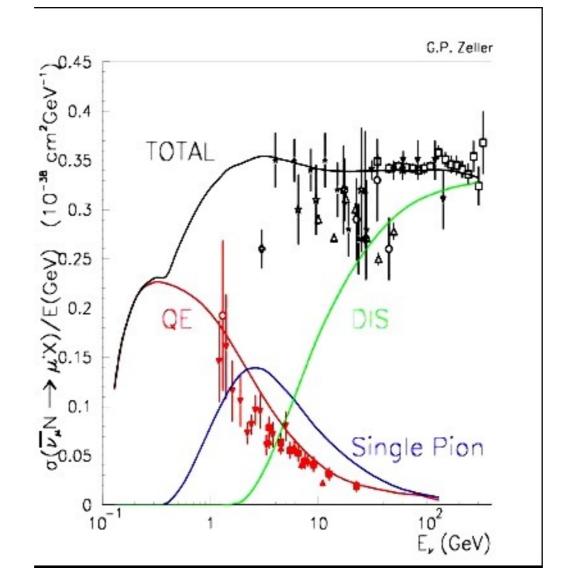
### Xsec data pre 2007



### The data was impressively imprecise



# World Data for Antineutrinos





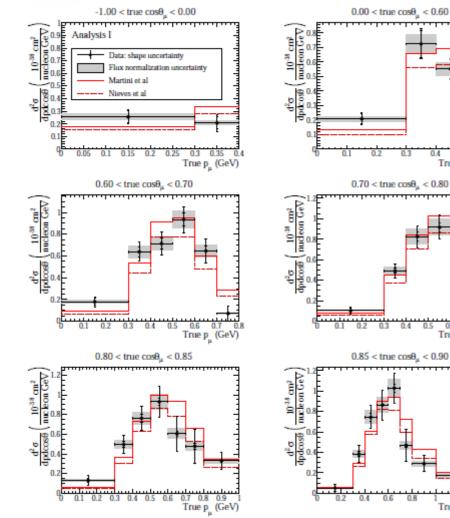
### It's slowly getting better

True p. (GeV)

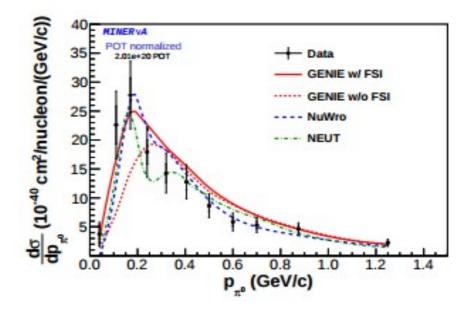
0.6

True p. (GeV)

1.2 1.4 Truep (GeV)



CC  $0\pi$  differential Xsec from T2K arXiv:1602.03652

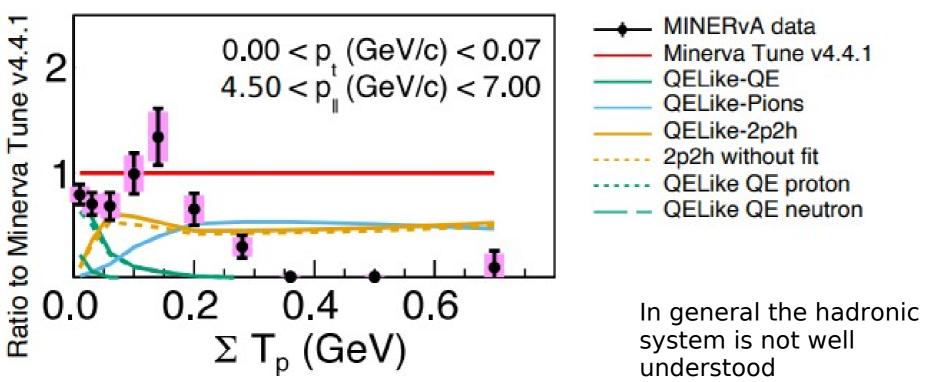


### CC $\pi^{0}$ differential xsec from **MINERVA** Phys.Lett. B749 (2015) 130-136

Lot's of effort going into trying to understand neutrino interaction cross sections



### But still not good



Total proton kinetic energy

D Ruterbories et al. Simultaneous measurement of proton and lepton kinematics in quasielasticlike v  $\mu$ -hydrocarbon interactions from 2 to 20 gev. Physical review letters, 129(2):021803, 2022.

# **Concluding Remarks**



Neutrinos are massive  $\rightarrow$  extensions needed to the Standard Model

Neutrino oscillation parameters still need to better measured;  $\delta_{CP}$  and ordering have to be measured.

Next generation of experiments will hopefully get a handle on these parameters : data coming from 2029 and the early 2030's.

Many opportunities for BSM in the neutrino sector

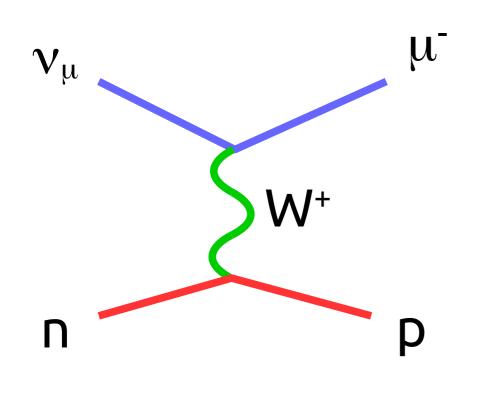
We are getting perilously close to a neutrino mass measurement – perhaps in the next 5-10 years?

Majorana or Dirac? We may be lucky with an intensive  $0\nu\beta\beta$  program; look out for LEGEND 1000

New neutrino machines may be coming with muon storage ring technology

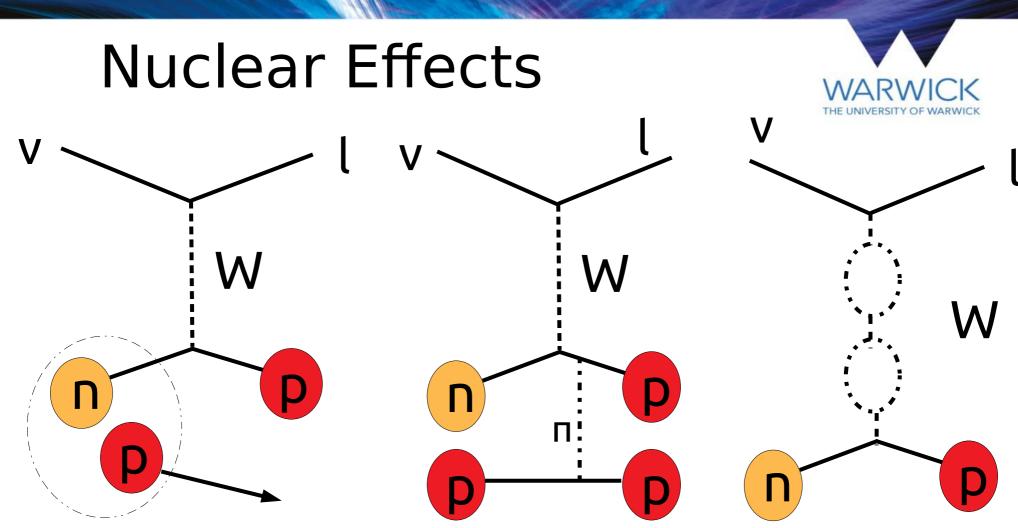
# **Quasi-Elastic Scattering**





- Usually though of as a single nucleon knock-on process
- In the past has been used as a "standard candle" to normalise other cross sections
- Heavily studied in the 1970's and 1980's and considered to be "understood"

II. Energy reconstruction is unbiased assuming 2 body  $E_{\nu;rec} = \frac{2(m_N - E_B)E_\mu - (E_B^2 - 2m_N E_B + m_\mu^2)}{2(m_N - E_B - E_\mu + |p_\mu|\cos\theta_\mu)}$ kinematics



quasi-deuteron

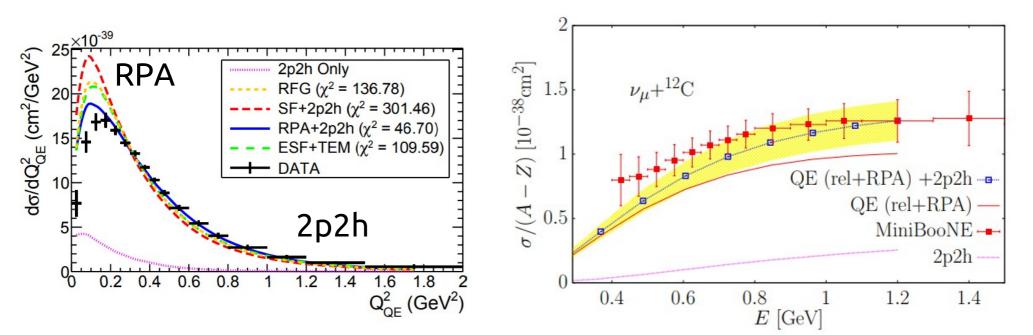
Short-range correlations (SRC)

Meson Exchange Currents (MEC)

2p2h processes - medium to high  $Q^2$ 

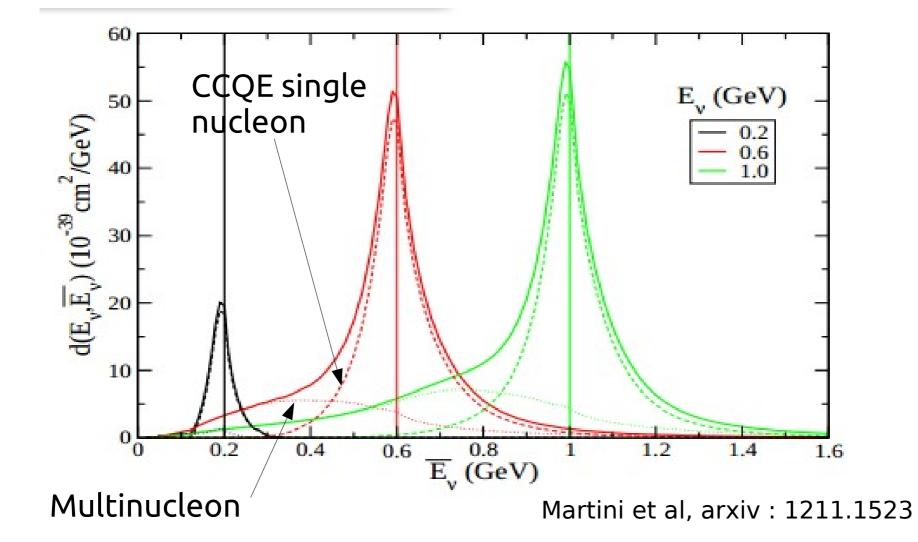
**RPA effects** W polarisation changes strength of weak interaction





Models change Q<sup>2</sup> shape in different regions Models add a new channel which increases the total cross section

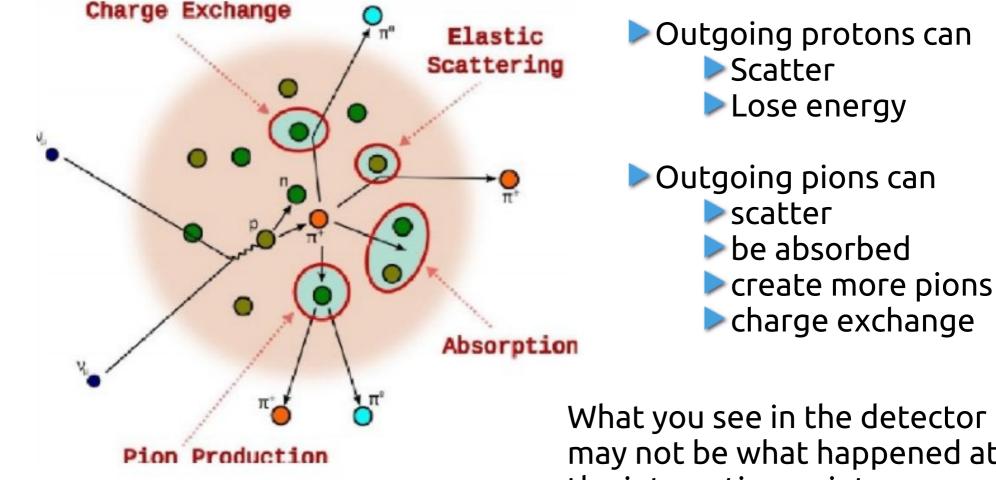
# Effect on energy reconstruction





### **Final State Interactions**

### In the nuclear medium

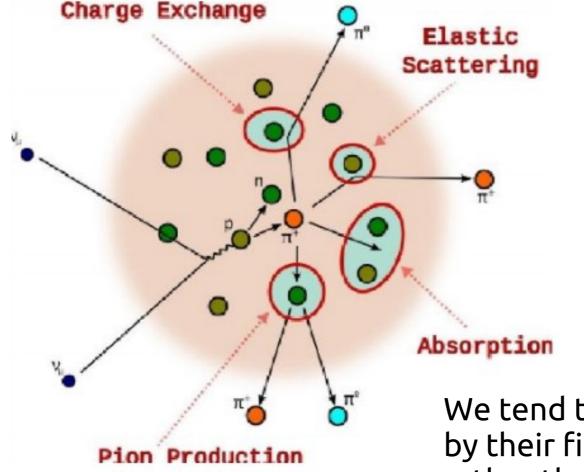


may not be what happened at the interaction point



### Final State Interactions

### In the nuclear medium



Outgoing protons can
 Scatter
 Lose energy

Outgoing pions can
 scatter
 be absorbed

- create more pions
- charge exchange

We tend to categorise events by their final state content now rather than their theoretical "label"