



# Optimisation of the CLIC RTML

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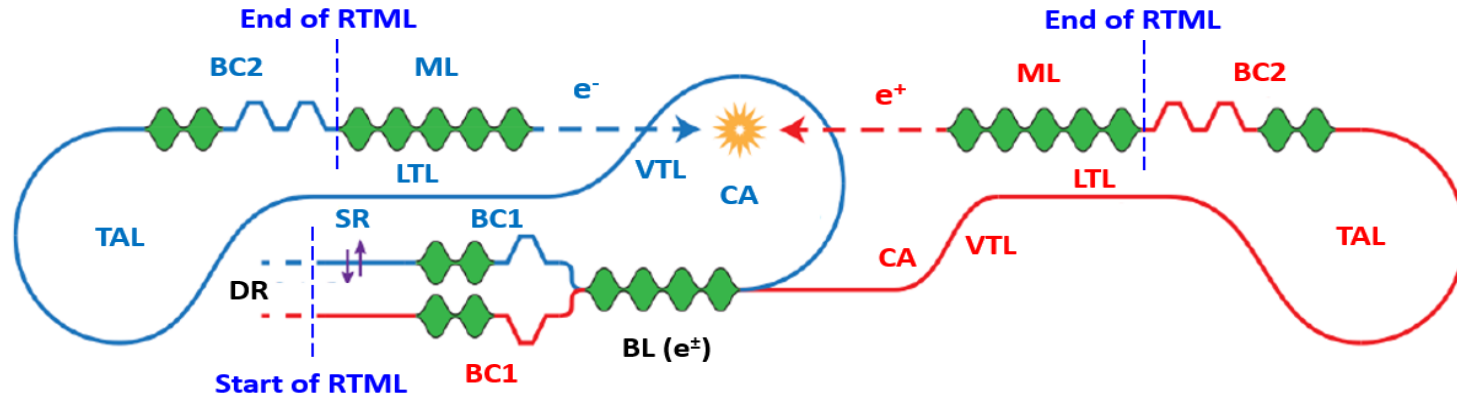
CLIC Project Meeting @ CERN

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# Outline

- Introduction to CLIC RTML
- Optimisation of BC1 and BC2
- Static imperfections and BBA corrections
- Jitter amplifications
- Alternative booster linac
- Conclusions

# Ring To Main Linac (RTML)



- Spin rotator (SR), used only for the  $e^-$  beam, aimed at achieving any arbitrary spin rotation.
- Bunch compressor 1 (BC1), composed of 2 GHz RF cavities working at zero acceleration mode and a chicane.
- Booster linac (BL), composed of the same 2 GHz RF cavities as BC1, is common to the  $e^-$  and  $e^+$  beams and accelerates from 2.86 GeV to 9 GeV .
- Central arc (CA) and vertical transfer line (VTL) to transport the beam to the underground tunnel.
- Long transfer line (LTL) to transport the beam to the starting point of the two main linacs.
- Turn around loop (TAL) to bend the beam by  $180^\circ$  and direct it towards the interaction point (IP).
- Bunch compressor 2 (BC2), composed of 12 GHz RF cavities working at zero acceleration mode and two chicanes.

# Beam parameters @ 380 GeV

- Beam parameters **assumed** at the entrance of the RTML

- Beam parameters by design (perfect machine) **required** at the end of the RTML

Beam parameter	Unit	Value
Beam energy	GeV	2.86
Number of bunches per train		352
Number of particles per bunch		$5.2 \times 10^9$
Bunch charge	nC	0.83
RMS bunch length	um	1800
RMS energy spread	%	0.12
Normalized emittance, $\epsilon_{n,x}$	nm·rad	700
Normalized emittance, $\epsilon_{n,y}$	nm·rad	5

Beam parameter	Unit	Value
Beam energy	GeV	9
Number of bunches per train		352
Number of particles per bunch		$5.2 \times 10^9$
Bunch charge	nC	0.83
RMS bunch length	um	70
RMS energy spread	%	< 1.7
Normalized emittance, $\epsilon_{n,x}$	nm·rad	< 800
Normalized emittance, $\epsilon_{n,y}$	nm·rad	< 6

- Normalised **emittance budgets** at the end of the RTML, **required** for at least **90% machines** after BBA corrections

Normalized emittance budgets	$\epsilon_{n,x}$	$\epsilon_{n,y}$
Without imperfections	< 800	< 6
With static imperfections	< 820	< 8
With dynamic imperfections	< 850	< 10

# Motivation

- Some **remaining problems** in previous studies:
  - In the **CDR** published 2012, RTML was well designed, but the **imperfections were not studied**. Besides, a very **high gradient** (94 MV/m) was assumed for the BC2 X-band, which might be **not realistic and optimum**
  - In the CLIC **PIP report** published in 2018, the BC2 X-band iris aperture was simply increased by a factor of 1.5 to meet the emittance budgets with static imperfections. However, such a **large aperture** ( $a_0 = 5.44$  mm,  $a_0/\lambda = 0.218$ ) would be problematic with **break-down, huge power consumption and cost**
  - In a later study (not finished and not published), a new long X-band structure similar with the **CompactLight X-band** was tried and tested. The power consumption and cost can be much smaller due to reduced aperture, but the **BBA didn't work**. Besides, the **aperture** ( $a_0 = 4.41$  mm,  $a_0/\lambda = 0.176$ ) is **still a bit large** for CLIC
- Nevertheless, there is **more we can do**:
  - The total RF voltage and gradient of BC1 and BC2 was never optimised to reduce the **cost**
  - The **bunch phase shift** effect (raised in damping ring) was never considered and minimised
  - The **BBA corrections** might be also optimised to achieve more easily the emittance budgets

# RF structures

- RF structure parameters

- The *CLIC L-band* (1.5 m long) is assumed in **BC1**, which is the **same with booster linac (BL)**
- The *CLIC TD-31 X-band* (275 mm long) is assumed in **BC2**, just to be the same with the **main linac** (380 GeV, drive-beam based)
- ✓ Original designs are used, without any change in the iris and structure length

Parameter	Unit	BC1	BC2
Structure name		CLIC L-band	CLIC TD-31 X-band
RF frequency	GHz	1.999	11.994
Structure length	m	1.5	0.275
Number of cells		30	33
Phase advance per cell	°	120	120
Working RF phase	°	90	90
First iris radius	mm	20	4.062
Last iris radius	mm	14	2.6
First iris thickness	mm	8	2.525
Last iris thickness	mm	8	1.433

# Optimisation of voltages and angles

- Simulation tools

- **Placet**: for *full simulation* and start-to-end optimisation. Side effects (wakefield, CSR, ISR) considered
- **RF-Track**: for *fast simulation* and bunch longitudinal optimisation. Only BC1 and BC2 chicanes are simulated. Side effects not considered

- **Free parameters to optimise**

- Total RF **voltages** of BC1 and BC2:  $V_1, V_2$
- Bending **angles** of BC1 and BC2 chicanes:  $\theta_1, \theta_2$
- ✓ The two chicanes of BC2 are assumed to be identical, to simplify the optimisation and minimise emittance growth due to ISR effect

- **Goals** to be achieved:

- Final **bunch length**:  $\sigma_z \sim 70 \text{ um}$
- Final **energy spread**:  $\sigma_E/E < 1.7\%$
- **Emittances** (by design):  $\epsilon_{n,x} < 800 \text{ nm}$ ,  $\epsilon_{n,y} < 6 \text{ nm}$
- Minimum bunch **phase shift effect** after RTML
- Minimum **emittance growth** along RTML
- Minimum **total RF voltage** in BC1 and BC2

- **Optimised parameters**

- ✓ BC1 voltage is  $\sim 10\%$  higher than CDR
- ✓ **BC2 voltage is  $\sim 60\%$  lower than CDR**

Parameter	Symbol	Unit	BC1	BC2
Total RF voltage	$V$	MV	450	650
Bending angle	$\theta$	$^\circ$	3.95	1.55

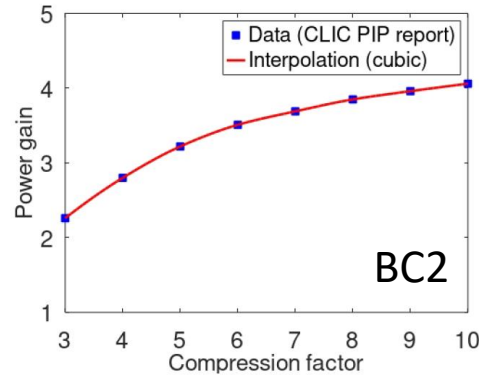
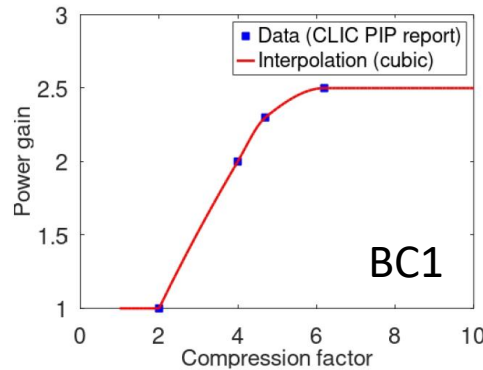
# Optimisation of gradients

## RF system assumptions in optimisation:

- Klystrons

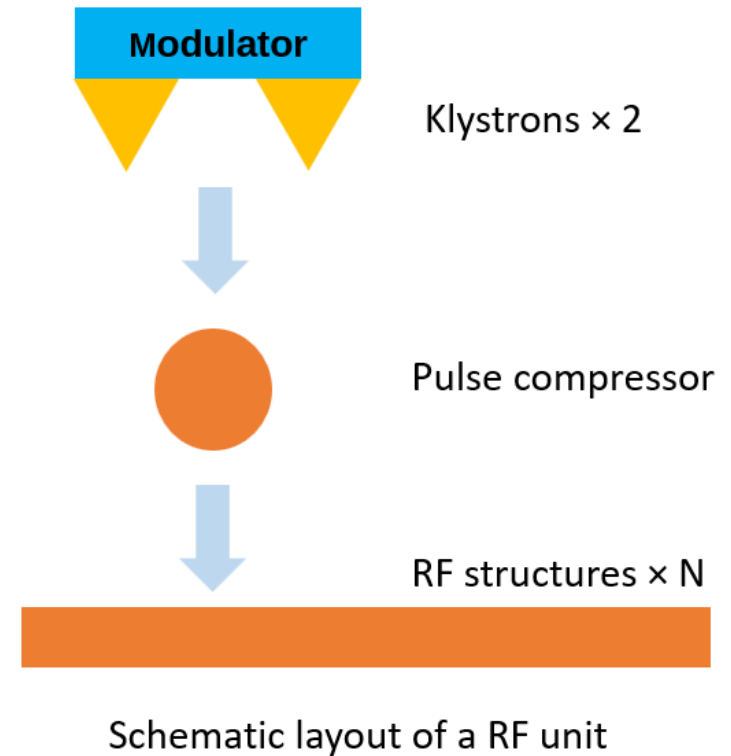
Parameter	Unit	L-band (BC1)	X-band (BC2)
Output power	MW	50	51.4
Pulse length	$\mu\text{s}$	8	2

- Pulse compressors



- Total RF transmission efficiency considered: 90%
- Layout:

RF structures per Module (N)	BC1 (L-band)	BC2 (X-band)
<b>Baseline</b> option	4	8
<b>Alternative</b> option	$2^n$	$2^n$



**New results w.r.t CLIC week (12/2023)  
in the following slides ...**



# Optimisation of gradients

- *CLICopti* is used to estimate RF parameters (peak power, pulse length, breakdown, etc.)
  - Beam loading effects to be studied for BC1, BC2 (though we think cost estimation is not affected at  $\varphi = 90^\circ$ )

- Booster linac (BL) is also reoptimized (similar with BC1)

RF voltage	Unit	BC1	BC2	Booster linac
Before compensation	MV	450	650	6140
After compensation	MV	450.5	659.3	6156.3

- Energy and energy chirp losses are also compensated:

- A scan of the number of RF units is performed to minimise the cost. As a result:

Parameter	Unit	Old		New	
		CDR	PIP	Baseline	Alternative
BC1 RF total voltage	MV	399	477	450.5	
BC1 structure length	m	1.5		1.5	
BC1 RF gradient	MV/m	13.3	15.9	18.770	
BC1 RF peak power	MW	23.8	34.0	47.3	
BC1 RF-to-beam efficiency	%	24.8	22.9	20.8	
BC1 number of klystrons		10 (6)	10	8	
BC1 number of RF structures		20		16	
BC2 RF total voltage	MV	1686.4	1763.0	659.3	
BC2 structure length	m	0.23		0.275	0.275
BC2 structure aperture	mm	<b>3.63</b>	<b>5.44</b>	<b>3.33</b>	
BC2 RF gradient	MV/m	<b>94</b>	<b>98.27</b>	<b>74.916</b>	<b>37.458</b>
BC2 RF peak power	MW	<b>88.4</b>	<b>355.6</b>	<b>39.3</b>	<b>9.8</b>
BC2 RF-to-beam efficiency	%	24.5	7.5	45.1	56.5
BC2 number of klystrons		<b>40</b>	<b>156</b>	<b>8</b>	<b>4</b>
BC2 number of RF structures		<b>78</b>		<b>32</b>	<b>64</b>
BL total voltage	MV	6168.6		6156.3	
BL structure length	m	1.5		1.5	
BL RF gradient	MV/m	14.9		15.089	
BL RF peak power	MW	54.1		55.1	
BL RF-to-beam efficiency	%	20.0		19.9	
BL number of klystrons		138		136	
BL number of RF structures		276		272	

RF structures per Module (N)	BC1 (L-band)	BC2 (X-band)
Baseline option	<b>4</b>	<b>8</b>
Alternative option	<b>2<sup>n</sup></b>	<b>2<sup>n</sup></b>

## Updates w.r.t CLIC week (12/2023):

- **New baseline of RF (more conservative)**

✓ **BC2 expected cost reduced significantly compared with CDR / PIP report!**

- **Baseline RF system option will be studied in the following slides ...**

# Final results after optimisation

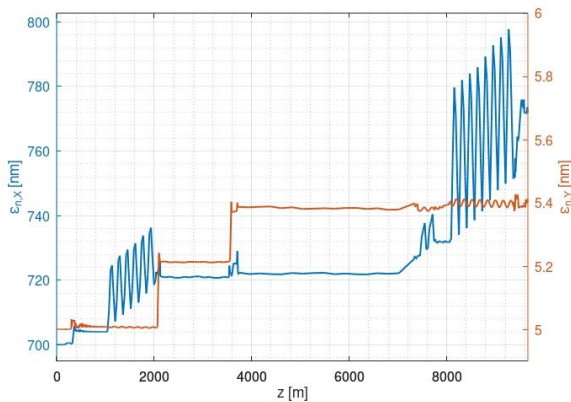
- Final results (e<sup>-</sup> beam) at the end of the RTML (perfect machine):
  - CSR not simulated in CA & TAL by default (small impact but much longer time)
  - Optimised matching sections, **emittances growth reduced significantly** (CDR, PIP  $\epsilon_{x,y}$ : ~790 nm, ~5.8 nm)

W/o CSR simulated in CA & TAL

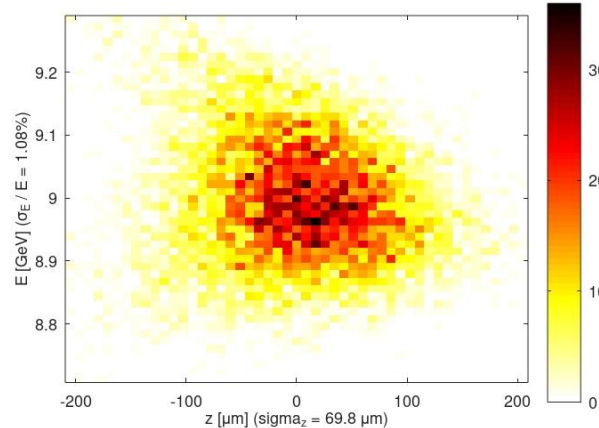
Parameter	Symbol	Unit	Value
Bunch length	$\sigma_z$	$\mu\text{m}$	69.8
Energy spread	$\sigma_E/E$	%	1.1
Horizontal normalized emittance	$\epsilon_{n,x}$	nm	771.5
Vertical normalized emittance	$\epsilon_{n,y}$	nm	5.40

W/ CSR simulated in all sections

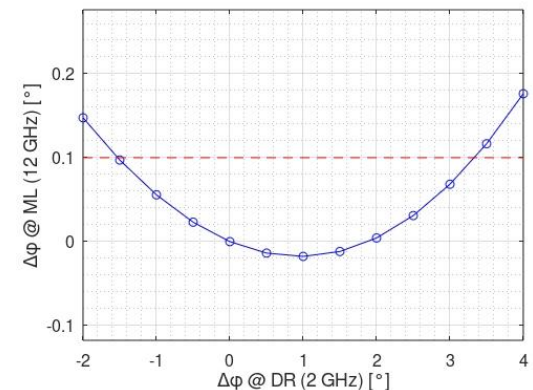
Parameter	Symbol	Unit	Value
Bunch length	$\sigma_z$	$\mu\text{m}$	70.4
Energy spread	$\sigma_E/E$	%	1.1
Horizontal normalized emittance	$\epsilon_{n,x}$	nm	775.2
Vertical normalized emittance	$\epsilon_{n,y}$	nm	5.43



Emittance growth along RTML



Longitudinal phase space at the end



Bunch phase shift effect

- Bunch phase shift effect** from the DR (2 GHz) to the ML (12 GHz) minimised:
  - Assuming  $\pm 0.1^\circ$  tolerance at ML, corresponding **acceptance for DR improved significantly**:  $[-1.5^\circ, +3.3^\circ]$ , much better than the required  $\pm 1.0^\circ$

# Static imperfections and BBA corrections

- **Imperfections considered (same with previous studies)**

- Numbers in PIP report (Table 2.5) might be too conservative (or maybe typos, as the numbers cannot be found in any previous studies). But more conservative errors can still be studied

Imperfection	Unit	CA & TAL	Other sections
Magnet and BPM positron error	$\mu\text{m}$		30
Magnet and BPM tilt error	$\mu\text{rad}$		100
Magnet and BPM roll error	$\mu\text{rad}$		100
Quadrupole strength error	%	0.01	0.1
Other magnet strength error	%		0.1
BPM resolution	$\mu\text{m}$		1
Magnetic-center shift w/ strength		0.35 $\mu\text{m}$ / 5%	
Emittance measurement uncertainty	%		1

**Updates w.r.t CLIC week (12/2023):**

- **BPM errors considered (mistake fixed)**
- **Erros now same with previous studies**

- **Beam based alignment (BBA) correction methods**

- **One-to-one (OTO) correction:** orbit correction

$$\begin{pmatrix} \mathbf{b} \\ 0 \end{pmatrix} = \begin{pmatrix} & \mathbf{R} \\ \beta_0 & \mathbf{I} \end{pmatrix} \cdot \theta$$

b: BPM readings    R: orbit response matrix     $\theta$ : dipole kicker corrections

- **Dispersion-free steering (DFS) correction:** orbit & dispersion correction

$$\begin{pmatrix} \mathbf{b} \\ \omega_d \quad (\eta - \eta_0) \\ 0 \end{pmatrix} = \begin{pmatrix} & \mathbf{R} \\ \omega_d & \mathbf{D} \\ \beta_1 & \mathbf{I} \end{pmatrix} \cdot \theta$$

$\eta$ : dispersion    D: dispersion response matrix

Test beam: energy difference of 5% by magnetic strength scaling in all sections

- **Sextupole-based emittance tuning (SBET) correction:** emittance optimisation by moving sextupoles

Merit function: 
$$M = \sqrt{\left(\frac{\epsilon_x^m - \epsilon_x^i}{\epsilon_x^s - \epsilon_x^i}\right)^2 + \left(\frac{\epsilon_y^m - \epsilon_y^i}{\epsilon_y^s - \epsilon_y^i}\right)^2}$$

$\epsilon^i$ : initial emittance at the entrance of the RTML

$\epsilon^m$ : measured emittance (1% RMS uncertainty assumed)

$\epsilon^s$ : emittance budget for static imperfections

# Static imperfections and BBA corrections

- BBA correction **procedure**

1. ST—LTL: OTO + DFS
2. CA—LTL: SBET
3. TAL1: OTO + DFS + SBET
4. TAL2: OTO + DFS + SBET
5. BC2: OTO + DFS + SBET

- ✓ Small overlap between sections
- ✓ Section split into bins with 20% overlap
- ✓ In each bin, correction in a few iterations
- ✓ DFS followed OTO after all bins in a section
- ✓ Always the first 8 sextupoles used in SBET
- ✓ TAL too long, split into 2 sections

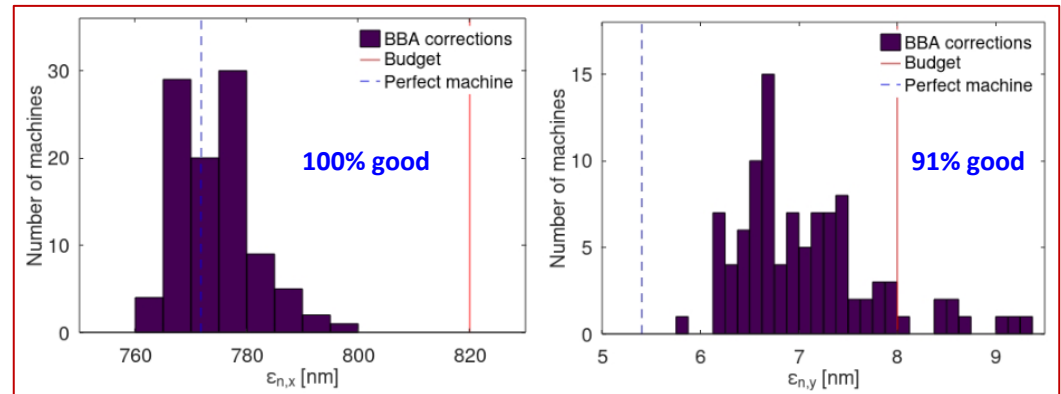
- BBA parameters

- To be optimized for each section

- Results (100 random misaligned machines)

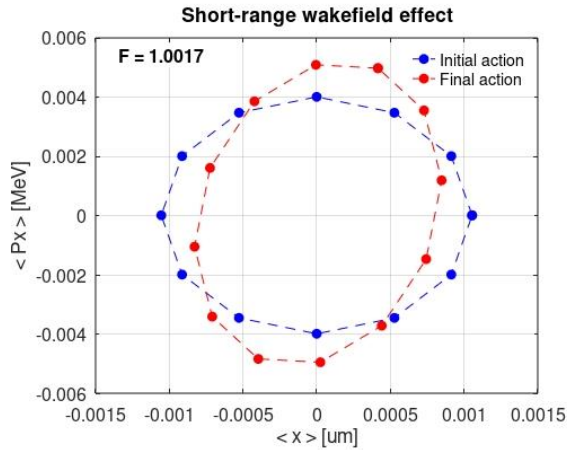
- 91% good machines (required: 90%)
- To be optimised, though satisfied
- \* To understand why X emittance is much better than Y

Parameter	Value
$\beta_0$ (OTO)	2
$\beta_1$ (DFS)	2
$\omega_d$ (DFS)	30
Number of quadrupoles per bin	100
Bin overlap	20%
Number of iterations (OTO)	2
Number of iterations (DFS)	2

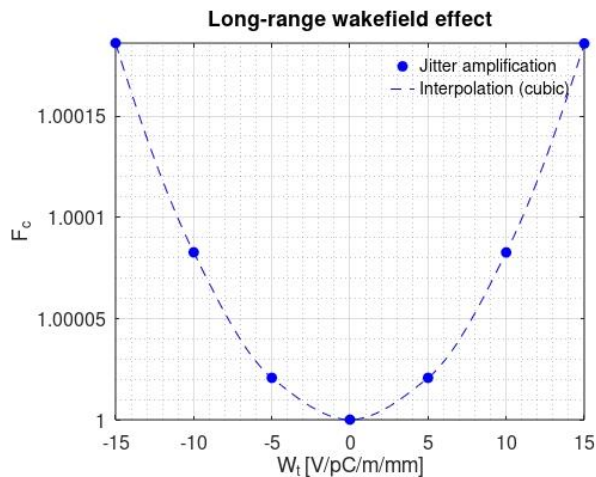


# Jitter amplifications

- Short-range wakefield

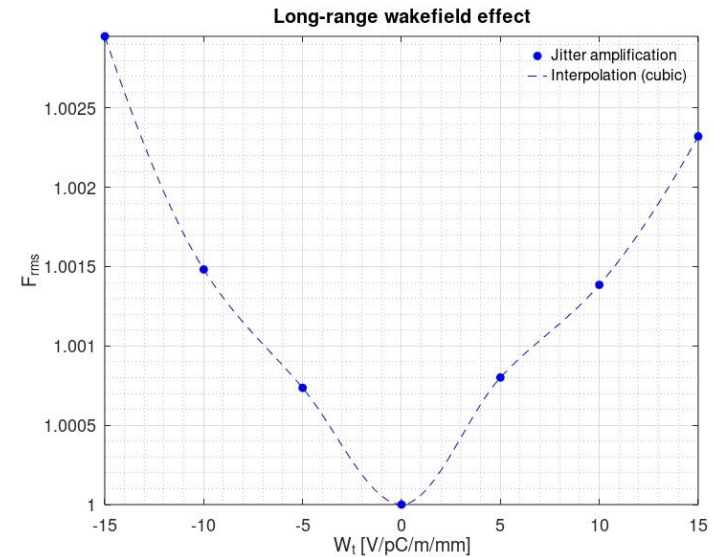


- Long-range wakefield (coherent)



- Long-range wakefield (incoherent)

- 1000 random trains simulated
- 352 bunches per train
- Kick on next bunch simulated
- Worst bunch considered



✓ Effects are very small!!

# Alternative booster linac: X-band

- Optimised configuration

Parameter	Unit	Baseline BL	Alternative BL
BC1 voltage	MV	450.5	489.5
BC1 RF gradient	MV/m	18.770	20.394
BC1 RF peak power required	MW	47.3	55.9
BC1 RF-to-beam efficiency	%	20.8	19.8
BC1 number of klystrons		8	8
BC1 number of RF structures		16	16
BC1 output bunch length	$\mu\text{m}$	<b>407</b>	<b>201</b>
BC2 voltage	MV	659.3	2442.1
BC2 RF gradient	MV/m	74.916	79.289
BC2 RF peak power required	MW	39.3	44.0
BC2 RF-to-beam efficiency	%	45.1	43.5
BC2 number of klystrons		<b>8</b>	<b>28</b>
BC2 number of RF structures		<b>32</b>	<b>112</b>
BL voltage	MV	6156.3	6190.3
BL structure length	m	<b>1.5</b>	<b>0.275</b>
BL RF gradient	MV/m	<b>15.089</b>	<b>58.144</b>
BL RF peak power required	MW	55.1	43.1
BL RF-to-beam efficiency	%	<b>19.9</b>	<b>43.7</b>
BL number of klystrons		<b>136</b>	<b>96</b>
BL number of RF structures		<b>272</b>	<b>384</b>
BL total length	m	<b>530.4</b>	<b>153.6</b>

- Results (quite good)

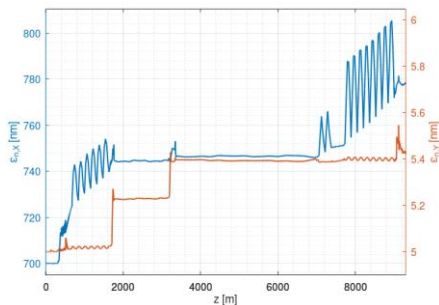
### W/o CSR simulated in CA & TAL

Parameter	Symbol	Unit	Value
Bunch length	$\sigma_z$	$\mu\text{m}$	67.7
Energy spread	$\sigma_E/E$	%	1.5
Horizontal normalized emittance	$\epsilon_{n,x}$	nm	777.8
Vertical normalized emittance	$\epsilon_{n,y}$	nm	5.42

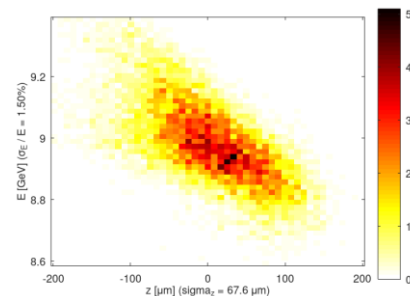
### W/ CSR simulated in all sections

Parameter	Symbol	Unit	Value
Bunch length	$\sigma_z$	$\mu\text{m}$	71.3
Energy spread	$\sigma_E/E$	%	1.5
Horizontal normalized emittance	$\epsilon_{n,x}$	nm	779.2
Vertical normalized emittance	$\epsilon_{n,y}$	nm	5.45

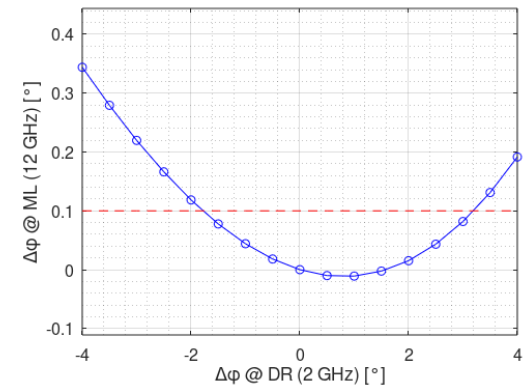
Emittance growth along RTML



Longitudinal phase space at the end



Bunch phase shift effect

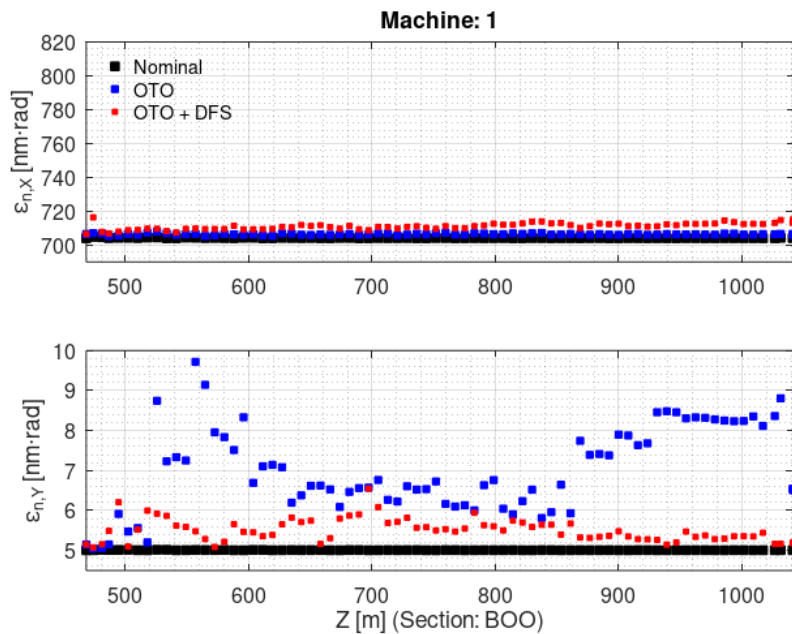


Large acceptance for DR: [-1.8°, +3.5°]

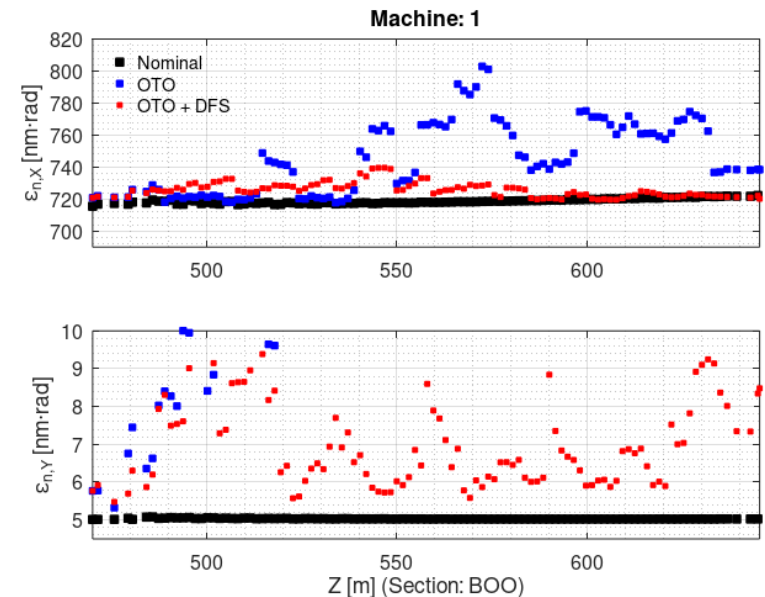


# Alternative booster linac: X-band

- **BBA** study is still **in progress**, which seems **quite difficult** compared with the baseline option (L-band BL)
- Possible **solutions** that would help: reduce a bit the **imperfections**, better **matching** sections, optimise **BBA** parameters and methods, reduce **FODO** length, reduce **bunch length** (complicated w/ significant non-linear effects), use **C-band**, etc.



Baseline (L-band BL)



Alternative (X-band BL)

# Conclusions

- CLIC **RTML** studied and optimised, for  $e^-$  ( $e^+$  study will follow, which is similar and easier), at **380 GeV** stage, for the **drive-beam based** option.
- Some **remaining tough problems** in the RTML are finally **solved**, by reoptimising the bunch compressors, matching sections and the BBA methods
  - **BC2** RF structure **same with ML** now, with **aperture and expected costs** reduced significantly
  - **Bunch phase shift** effect at ML also minimised with **large acceptance for the DR**
  - Conservative **static imperfections** considered and studied. **Emittance budget** achieved with **91%** good machines **after BBA** corrections
  - **Jitter amplification** due to wakefield also studied and found to be **negligible**
- **Baseline** design of RTML (L-band BL) is almost (to be improved a bit) **finished**. Results are already satisfied and **ready for documentation**
- **Alternative option of BL** using **X-band** (same with ML) instead of L-band is designed, with BC1 & BC2 also redesigned shows **good nominal results** (perfect machine). **BBA** study seems difficult but **still in progress**
- **Next steps**
  - **BBA** results for **L-band** BL **can be improved**. For **X-band** BL is **in progress** (try also **C-band** if BBA doesn't work)
  - Try **larger (more conservative) errors** (e.g.  $30\ \mu\text{m} \rightarrow 100\ \mu\text{m}$  position error in some sections, such as **LTL**)
  - **Beam loading** study (to cooperate with *J. Olivares, P. Wang, A. Grudiev* from CERN)
  - **Alternative options** that can be done and discussed:
    - 380 GeV  $\rightarrow$  3 TeV, Drive-beam based  $\rightarrow$  Klystron based, Old DR  $\rightarrow$  New DR (low emittance), etc.



# Acknowledgements

**Thanks very much for your attention!**

We thank C. Gohil, Y. Han and X. Liu for their contributions to previous development of the simulation framework.

We also thank J. Olivares, P. Wang, A. Grudiev, D. Schulte, Y. Papaphilippou and H. Bartosik for the helpful discussions.

# Backup

# Baseline definition

- **Baseline** configuration (baseline is studied and presented, unless otherwise specified):
  - Energy stage of collision: **380 GeV**
  - Main linac mode: **drive-beam based** acceleration
  - Old damping ring design assumed
  - Booster linac: L-band structure
- **Alternative** configurations that can be studied (beam parameters, requirements, RF structures and emittance budgets are all different from baseline)
  - Energy stages: 1.5 TeV & **3 TeV** energy stages (to be studied)
  - Main linac mode: **klystron based** acceleration (to be studied)
  - A **new damping ring design** proposed in 2019, which has much lower horizontal emittances, but higher energy spread, tighter emittance budgets, more difficult RTML design and larger beam-beam effects in BDS, etc. (to be discussed and studied)
  - Booster linac: X-band (being studied)

# Beam parameters: alternatives

- Collection of previous beam parameters (so many versions):

	RTML parameters	Input e <sup>-</sup>							
		380 GeV (or 500 GeV)				3 TeV			
		$\sigma_z$ [um]	$\sigma_E$ [%]	$\epsilon_x$ [nm]	$\epsilon_y$ [nm]	$\sigma_z$ [um]	$\sigma_E$ [%]	$\epsilon_x$ [nm]	$\epsilon_y$ [nm]
Drive-beam based	F. Stulle, LINAC paper (2010)					1600	0.13	500	5
	CLIC CDR (2012) Sec 3.2, 1 GHz DR	1800	0.1	456000	4.8	1800	0.12	500	5
	CLIC CDR (2012) Sec 3.2, 2 GHz DR	1600	0.1	472000	4.8	1800	0.12	500	5
	CLIC CDR (2012) Sec 3.3	1800	0.12	1800	5	1800	0.12	500	5
	CLIC update report (2016)								
	Y. Han, IPAC papers (2015,2016,2017)			700	5			500	5
	Y. Han, JINST paper (2017)					1800		500	5
	CLIC PIP report (2018) Sec 2.3, 2 GHz DR, for $N_b = 4.1 \times 10^9$							535.9	6.5
	CLIC PIP report (2018) Sec 2.4	1800		700	5				
	CLIC PIP report (2018) Sec 8.7, 2 GHz DR, Uniform DR w/ IBS, for $N_b = 5.7 \times 10^9$	1500	0.11	478.9	5				
	CLIC PIP report (2018) Sec 8.7, 2 GHz DR, Traperzium DR w/ IBS, for $N_b = 5.7 \times 10^9$	1300	0.13	535.9	6.5				
	D. Schulte Academic Training slides (2018)	1600		700	5				
	S. Papadopoulou, PRAB paper (2019), Uniform original DR w/ IBS, for $N_b = 4.1 \times 10^9$					1500	0.11	478.9	5
	S. Papadopoulou, PRAB paper (2019), Uniform alternative DR w/ IBS, for $N_b = 4.1 \times 10^9$					1600	0.15	648.7	4.5
(new DR design) S. Papadopoulou, PRAB paper (2019), Traperzium DR w/ IBS, for $N_b = 4.1 \times 10^9$					1600	0.15	434.7	4.2	
S. Papadopoulou, PRAB paper (2019), Traperzium DR w/ IBS, for $N_b = 5.7 \times 10^9$	1600	0.15	472.0	4.6					
C. Gohil, PhD Thesis (2020)	1800	0.11	700	5					
Klystron based	CLIC PIP report (2018)								
	O. Brunner, CLIC-Note-1174 (2022)			< 500	< 5				

# Beam parameters: alternatives

- Beam parameters to be used:

	Parameter (optimised)	Symbol	Unit	380 GeV				3 TeV							
				DBA		KBA		DBA							
				Old DR		New DR		Old DR		New DR		Old DR		New DR	
				e-	e+	e-	e+	e-	e+	e-	e+	e-	e+	e-	e+
Initial beam at entrance of RTML	Number of bunches per pulse	$n_b$		352		485		312							
	Number of particles per bunch	$n_p$	$10^9$	5.2		3.87		3.7							
	Bunch charge	$C_b$	nC	0.83		0.62		0.59							
	Bunch length	$\sigma_z$	um	1800	1600	1800	1600	1800	1600						
	Energy spread	$\sigma_E$	%	0.12	0.15	0.12	0.15	0.12	0.15						
	Normalised horizontal emittance	$\epsilon_{n,x}$	nm	700	472	500	434.7	500	434.7						
	Normalised vertical emittance	$\epsilon_{n,y}$	nm	5	4.6	5	4.2	5	4.2						
Requirement at exit of RTML (nominal, perfect machine)	Bunch length	$\sigma_z$	um	70	70	70	70	44	44						
	Energy spread (maximum)	$\sigma_E$	%	1.7	1.7	1.7	1.7	2.0	2.0						
	Normalised horizontal emittance	$\epsilon_{n,x}$	nm	800											
	Normalised vertical emittance	$\epsilon_{n,y}$	nm	6											
Emittance budget at exit of RTML (w/ static imperfections)	Normalised horizontal emittance	$\epsilon_{n,x}$	nm	820											
	Normalised vertical emittance	$\epsilon_{n,y}$	nm	8											
Emittance budget at exit of RTML (w/ static & dynamic imperfections)	Normalised horizontal emittance	$\epsilon_{n,x}$	nm	850		600?		600?							
	Normalised vertical emittance	$\epsilon_{n,y}$	nm	10		10		10							

- The **baseline option** is: 380 GeV + drive-beam based acceleration (DBA) + old DR, as it was used in most previous RTML and ML studies, and has the lowest energy spread (which makes the optimisation much easier with much lower voltage or cost), and the emittance budget is clear and much easier to achieve, and beam-beam effect in BDS is smaller and was well studied, etc. But **the other options will probably also be studied**

# Optimisation of gradients

- Scan of the number of RF units is performed to minimise the cost

Table 9: Scan of number of modulators for BC1 RF system for the baseline option. Symbol conventions:  $N_{RF}$ : total number of modulators,  $N_K$ : total number of klystrons,  $N_S$ : total number of structures,  $G$ : average loaded gradient,  $C$ : total cost.

$N_{RF}$	$N_K$	$N_S$	$G$ [MV/m]	$C$ [MCHF]
4	8	16	18.770	3.60
5	10	20	15.016	4.50
6	12	24	12.513	5.40
7	14	28	10.725	6.30
8	16	32	9.385	7.20

Table 10: Scan of number of modulators for BC2 RF system for the baseline option. Symbol conventions:  $N_{RF}$ : total number of modulators,  $N_K$ : total number of klystrons,  $N_S$ : total number of structures,  $G$ : average loaded gradient,  $C$ : total cost.

$N_{RF}$	$N_K$	$N_S$	$G$ [MV/m]	$C$ [MCHF]
4	8	32	74.916	2.84
5	10	40	59.933	3.55
6	12	48	49.944	4.26
7	14	56	42.809	4.97
8	16	64	37.458	5.68

Table 11: Scan of number of modulators for booster linac RF system for the baseline option. Symbol conventions:  $N_{RF}$ : total number of modulators,  $N_K$ : total number of klystrons,  $N_S$ : total number of structures,  $G$ : average loaded gradient,  $C$ : total cost.

$N_{RF}$	$N_K$	$N_S$	$G$ [MV/m]	$C$ [MCHF]
68	136	272	15.089	61.20
69	138	276	14.870	62.10
70	140	280	14.658	63.00
71	142	284	14.452	63.90
72	144	288	14.251	64.80

Table 12: Scan of number of modulators for BC1 RF system for the alternative option. Symbol conventions:  $N_{RF}$ : total number of modulators,  $N_K$ : total number of klystrons,  $N_S$ : total number of structures,  $G$ : average loaded gradient,  $C$ : total cost.

$N_{RF}$	$N_K$	$N_S$	$G$ [MV/m]	$C$ [MCHF]
1	2	64	4.692	5.40
2	4	32	9.385	3.60
3	6	24	12.513	3.60
4	8	16	18.770	3.60
5	10	20	15.016	4.50
6	12	12	25.026	4.50
7	14	14	21.451	5.25
8	16	8	37.539	5.40

Table 13: Scan of number of modulators for BC2 RF system for the alternative option. Symbol conventions:  $N_{RF}$ : total number of modulators,  $N_K$ : total number of klystrons,  $N_S$ : total number of structures,  $G$ : average loaded gradient,  $C$ : total cost.

$N_{RF}$	$N_K$	$N_S$	$G$ [MV/m]	$C$ [MCHF]
1	2	128	18.729	2.36
2	4	64	37.458	2.08
3	6	48	49.944	2.46
4	8	32	74.916	2.84
5	10	40	59.933	3.55
6	12	48	49.944	4.26
7	14	28	85.618	4.58
8	16	32	74.916	5.24

Table 14: Scan of number of modulators for booster linac RF system for the alternative option. Symbol conventions:  $N_{RF}$ : total number of modulators,  $N_K$ : total number of klystrons,  $N_S$ : total number of structures,  $G$ : average loaded gradient,  $C$ : total cost.

$N_{RF}$	$N_K$	$N_S$	$G$ [MV/m]	$C$ [MCHF]
67	134	536	7.657	80.40
68	136	272	15.089	61.20
69	138	276	14.870	62.10
70	140	280	14.658	63.00
71	142	284	14.452	63.90
72	144	288	14.251	64.80
73	146	292	14.056	65.70