

# RF Feedback



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**CERN**



**Advanced Accelerator Physics**

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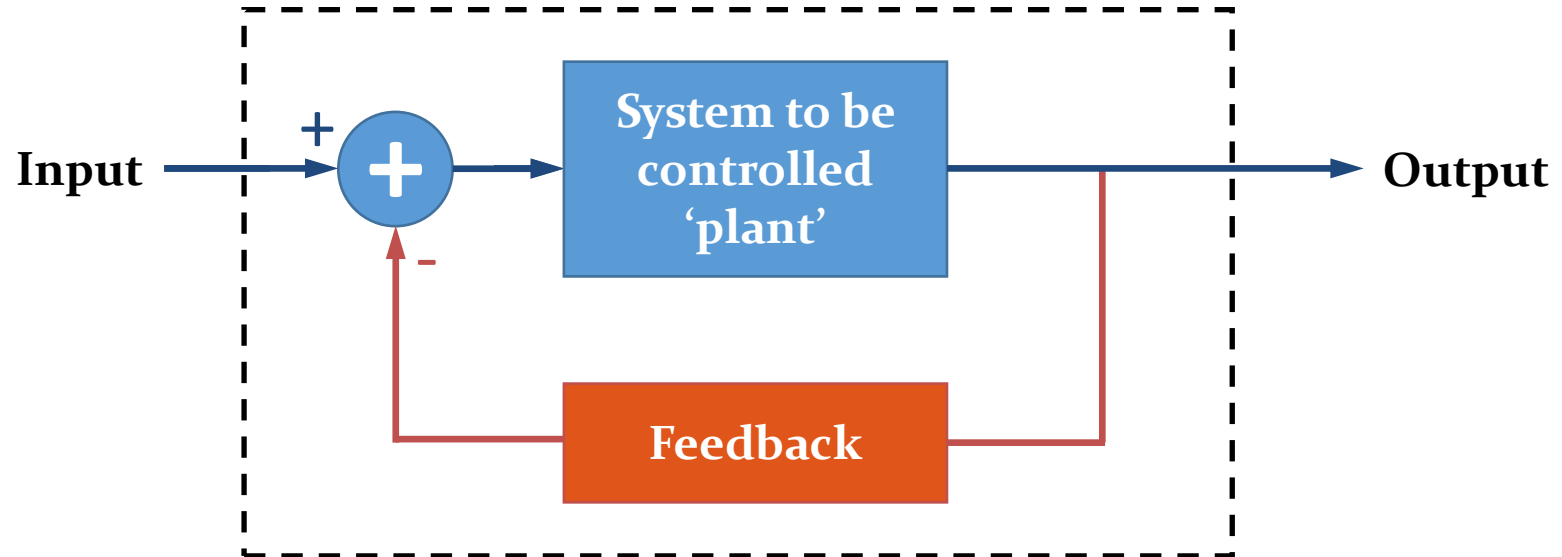
# Outline

- **Introduction**
- **Direct RF feedback**
  - Globally reduce a cavity impedance
- **Long delay feedback**
  - Reduce impedance at revolution frequency harmonics
- **Global feedback**
  - Detect and fight the effect of an instability
  - Time and frequency domain
- **Summary**

# Introduction

# Why feedback?

- **Open loop system subject to**
  - Imperfections
  - Perturbations
- **Feed output back to input → correction**



- **New system with new dynamics**
  - Control parameters of system
  - Make naturally unstable system stable again

# Why **RF** feedback?

Smaller longitudinal emittance  
Higher beam current  
All bunches identical  
Better longitudinal quality  
More luminosity  
More peak intensity

Image current of beam induces voltage surrounding structure

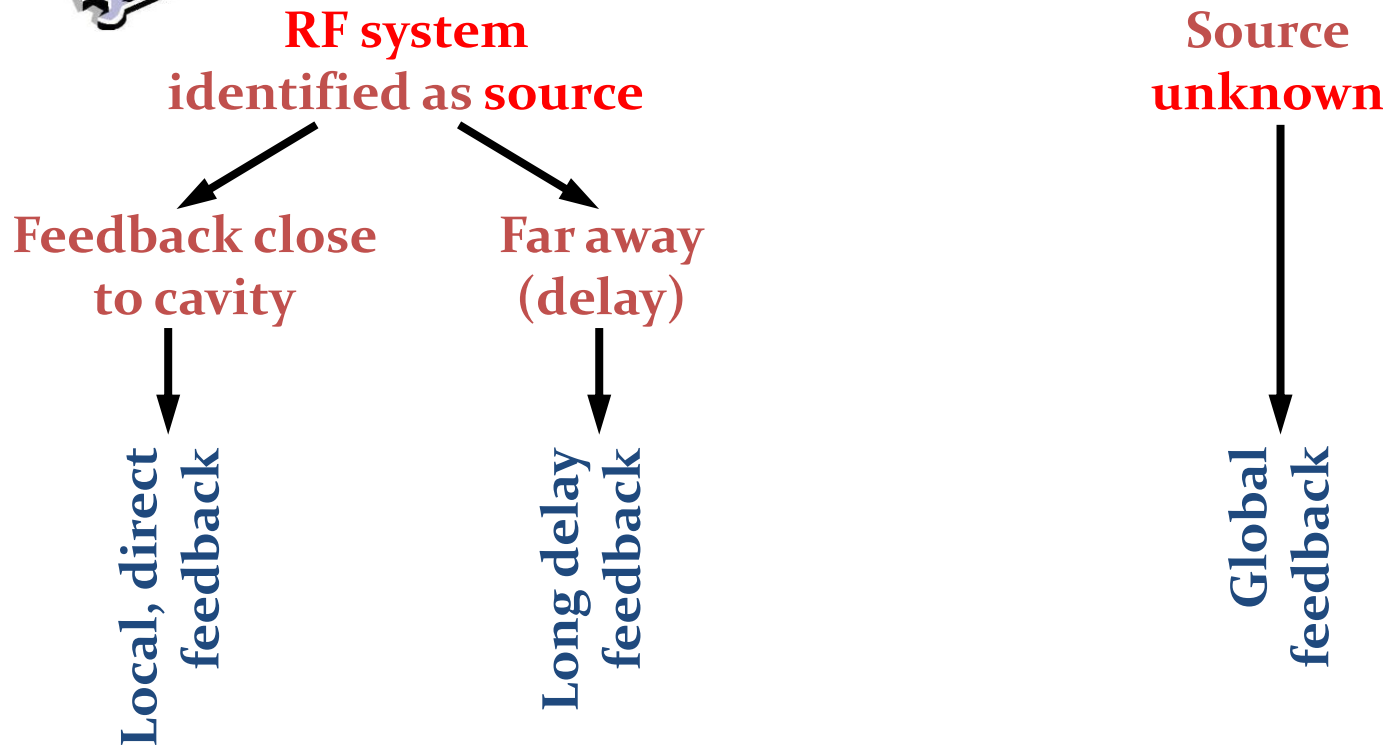
- RF cavities particularly affected due to **intentionally large impedance**
- **Longitudinal instabilities**
- **Degradation of longitudinal beam quality**

How to improve?

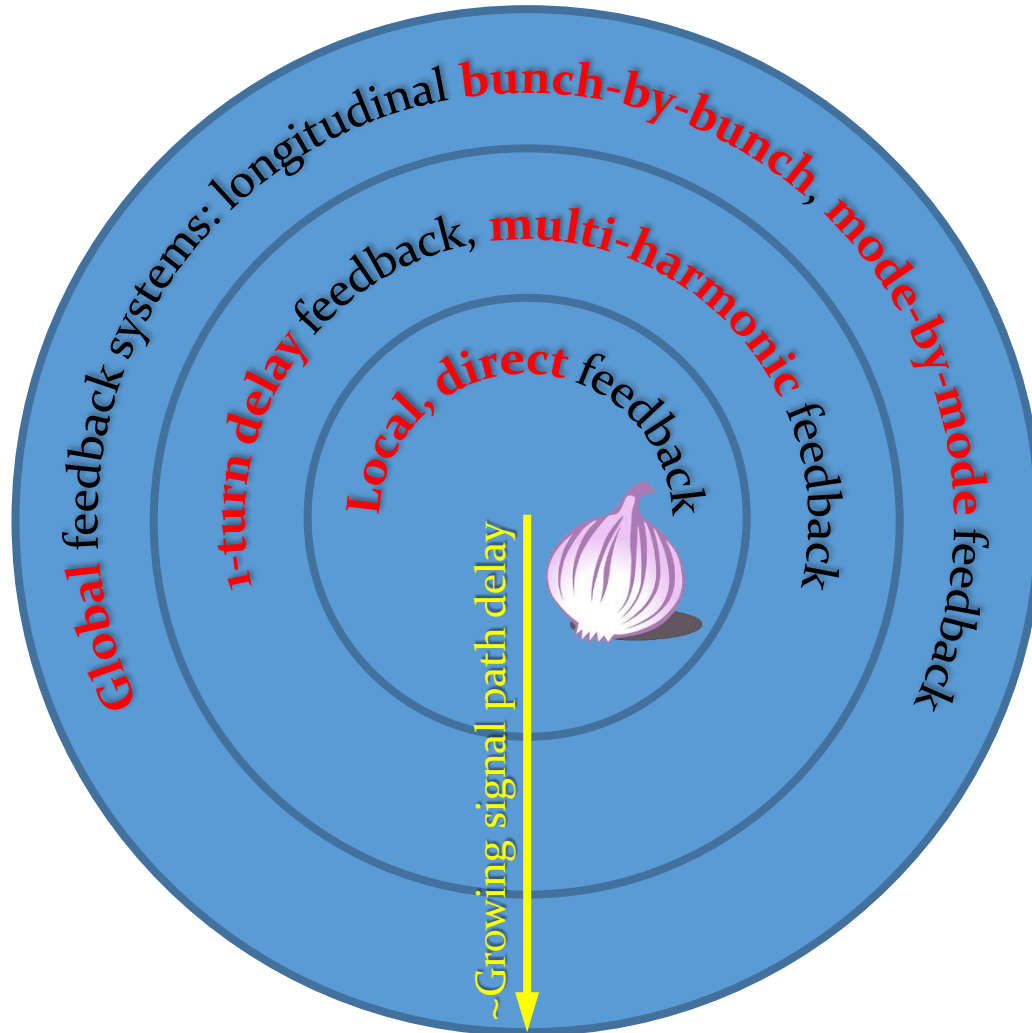
→ **RF feedback**

# Tree of RF feedback systems

- Control longitudinal parameters
- **Longitudinally unstable beam**
- **Beam induced voltage**



# Onion model of RF feedback



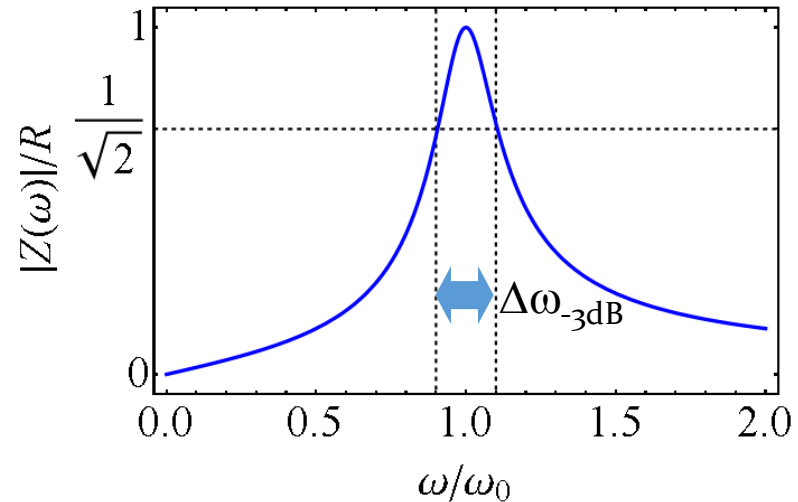
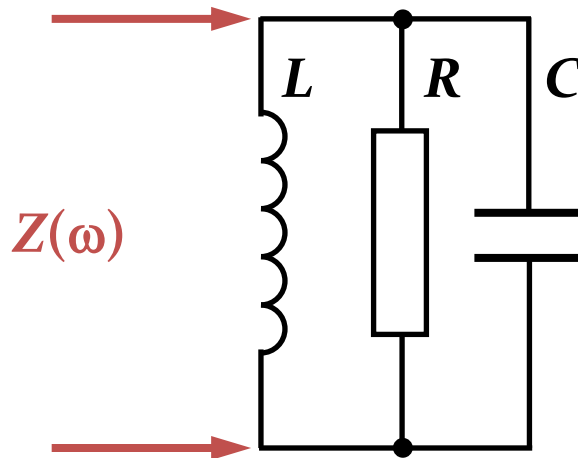
# Direct RF feedback





# Cavity parameters

- The resonance of a cavity can be understood as simple parallel resonant circuit described by  $R$ ,  $L$ ,  $C$

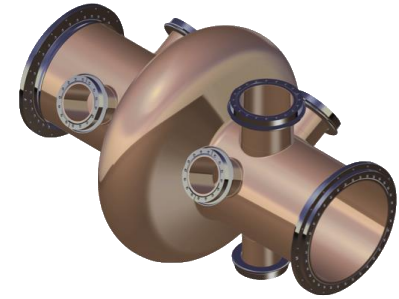


$$Q = \omega_0 RC = \frac{R}{\omega_0 L} \quad Z(\omega) = \frac{R}{1 + iQ \left( \frac{\omega^2 - \omega_0^2}{\omega \omega_0} \right)} \approx \frac{R}{1 + 2iQ \frac{\Delta \omega}{\omega_0}}$$

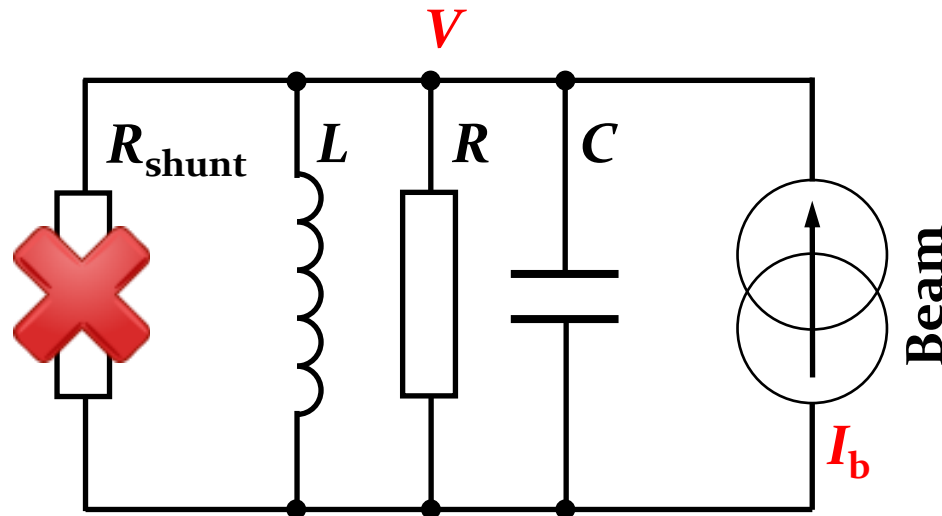
- Resonant circuit can also be described by  $R$ ,  $R/Q$ ,  $\omega_0$  or any other set of three parameters

# Objective of local impedance reduction

- Induced voltage in cavity may cause
  - Dephasing of total cavity voltage
  - Longitudinal instability



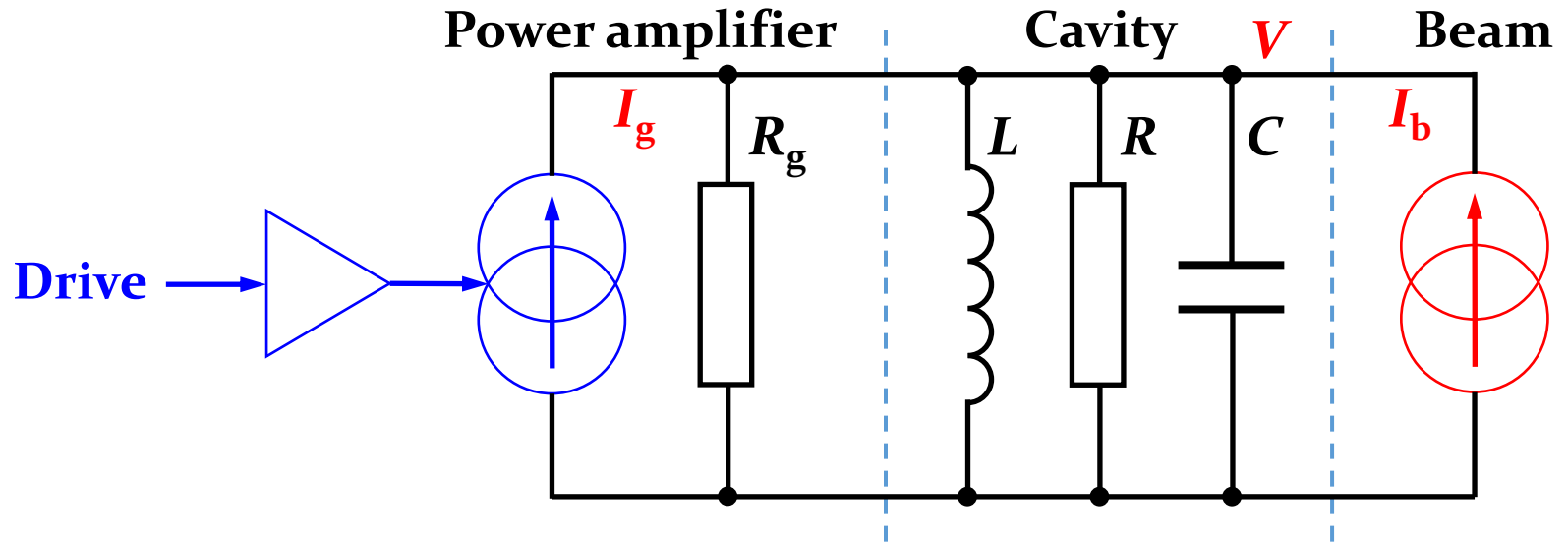
- Reduce beam induced voltage
- Reduce cavity impedance experienced by the beam



- ✓ Beam induced voltage reduced:  $R/(R+R_{shunt})$
- Power for given voltage increased:  $(R+R_{shunt})/R \rightarrow $$$$

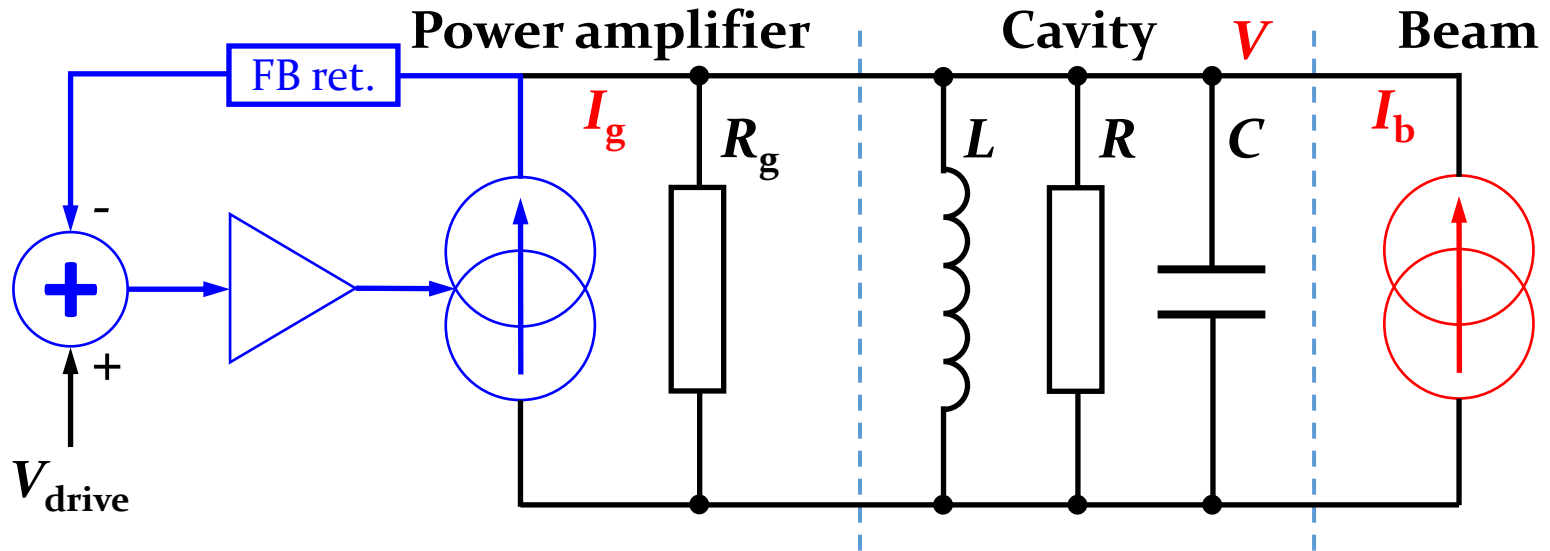
# Direct feedback

- Use amplifier to counteract beam induced voltage  
→ Decrease only apparent impedance experienced by beam



# Direct feedback

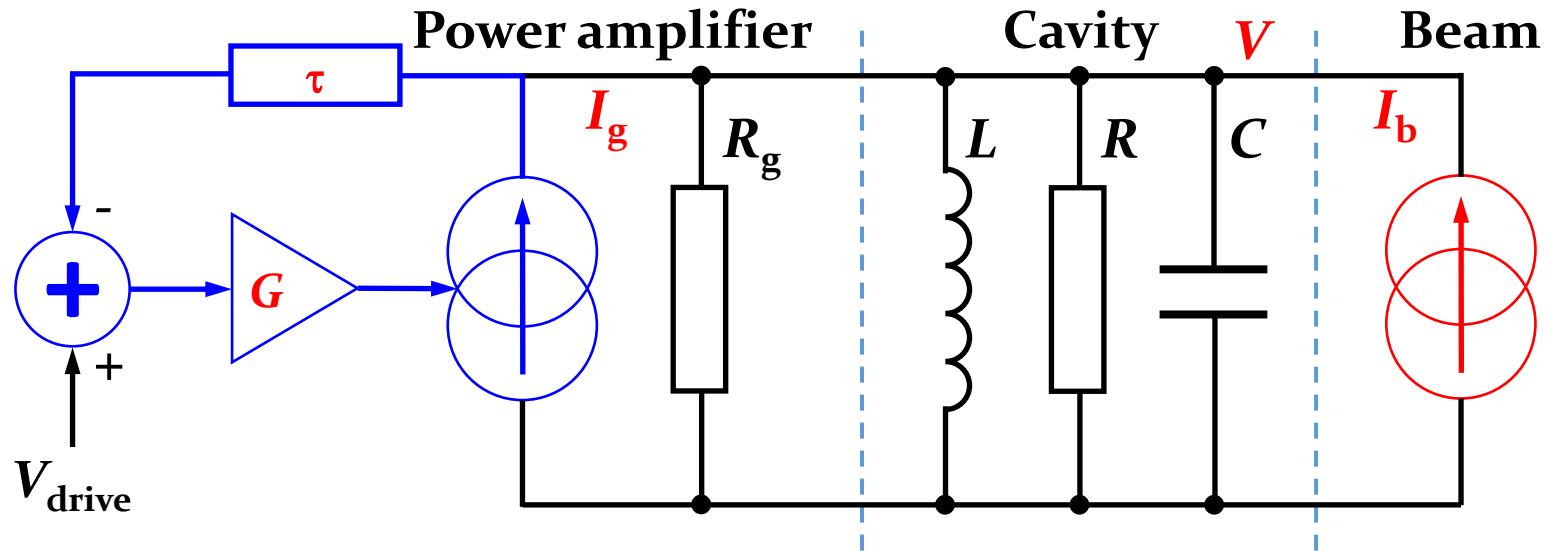
- Use amplifier to counteract beam induced voltage
- Decrease only apparent impedance experienced by beam



- Gap signal,  $V$ : **Beam and generator contributions**
- Drive signal,  $V_{drive}$ : **Pure generator**
- Compare drive signal (no beam) with gap (beam and generator)
- Amplify inverted difference

# Direct feedback

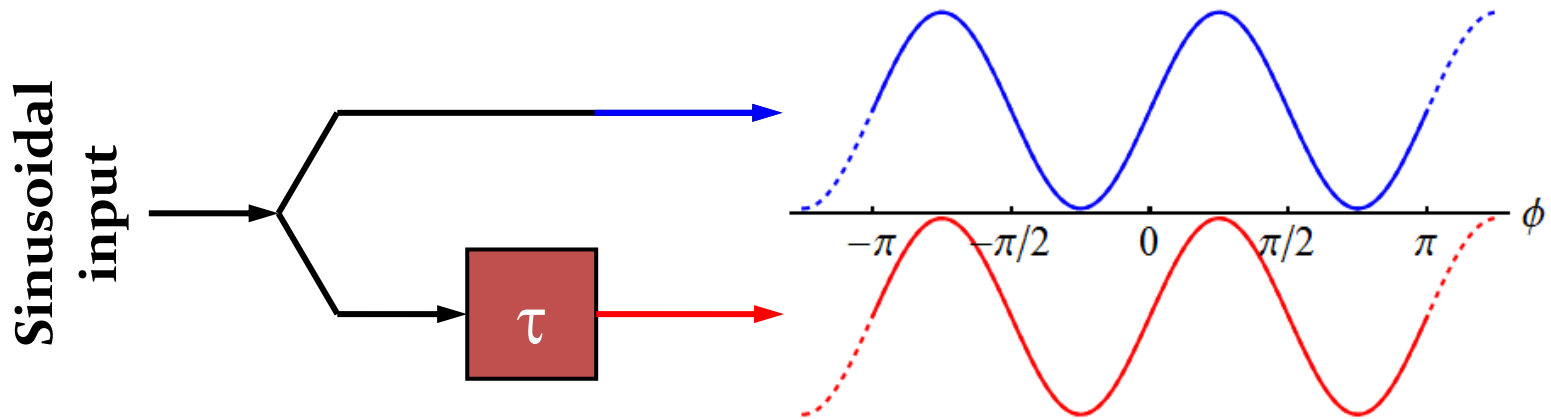
- Use amplifier to counteract beam induced voltage
- Decrease only apparent impedance experienced by beam



- Feedback parameterized by
  - Open **loop gain**,  $G$
  - Total **loop delay**,  $\tau$  → frequency dependent phase shift

# Issue with delay

- **Dephasing due to physical delay**



- **Delay is natural enemy of every feedback system**

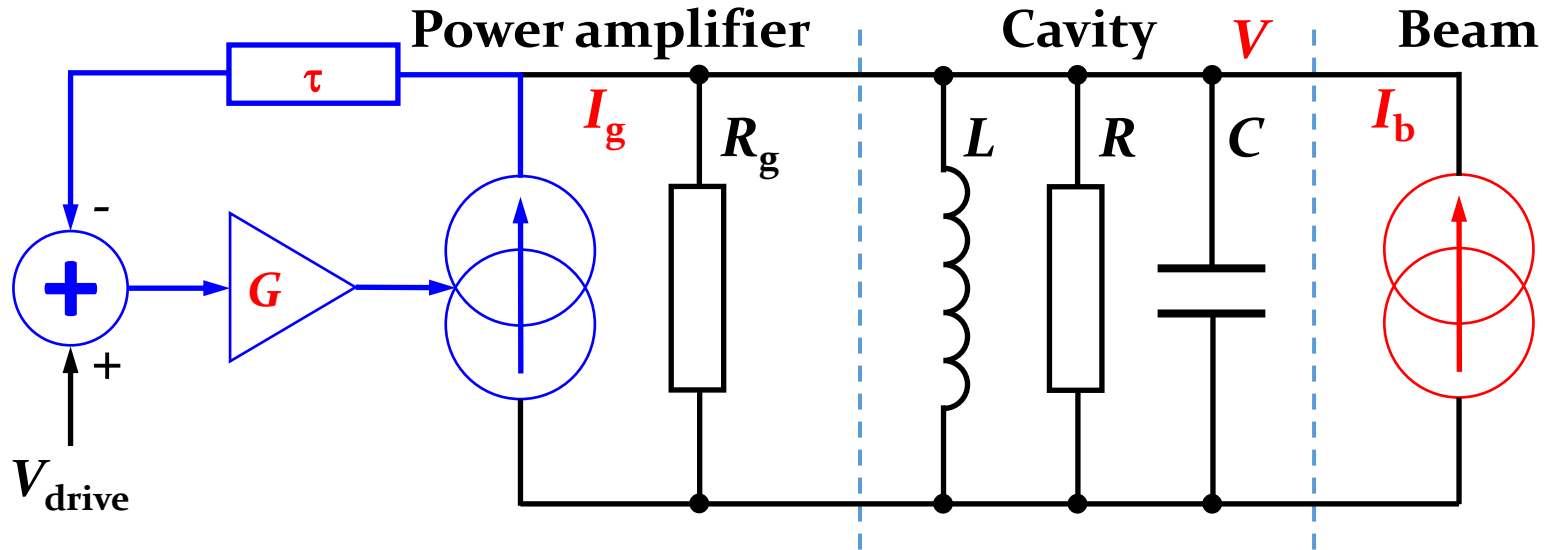
→ **Propagation delay in cables and electronics**

→ **Latency of conversion and signal processing**

→ **Phase rotation of complex signal:**  $e^{-i(\omega-\omega_0)\tau} = e^{-i\Delta\omega\tau}$

# Direct feedback

- Use amplifier to counteract beam induced voltage
- Decrease only apparent impedance experienced by beam



→ Total current in cavity ( $V_{\text{drive}} = 0$ ):

$$I_t(\omega) = I_b(\omega) + I_g(\omega)$$

$$I_g(\omega) = -V_t(\omega) G e^{-i\Delta\omega\tau}$$

# Impedance with direct feedback

- **Total cavity voltage:**  $V_t(\omega) = \frac{I_b(\omega)Z(\omega)}{1 + Z(\omega)Ge^{-i\Delta\omega\tau}}$
- **Impedance with feedback:**  
 → **Differential change of cavity,  $dV_t$  voltage for beam induced current,  $dI_b$**

$$Z_{fb}(\omega) = \frac{dV_t(\omega)}{dI_b(\omega)} = \frac{Z(\omega)}{1 + Z(\omega)Ge^{-i\Delta\omega\tau}}$$



$$Z(\omega) \simeq \frac{R}{1 + 2iQ\frac{\Delta\omega}{\omega_0}} \simeq \frac{R}{2iQ\frac{\Delta\omega}{\omega_0}}$$



$$|\angle Z(\omega)| \simeq \frac{\pi}{2}$$



# Stability with feedback

- Dephasing due to loop delay at  $\Delta\omega_\tau$

$$\Delta\phi_\tau = \Delta\omega_\tau \cdot \tau$$

- Which dephasing results in unity absolute loop gain?

Open loop:  $G|Z(\Delta\omega_\tau)| = G \frac{R}{2Q \frac{\Delta\phi_\tau}{\omega_0\tau}} = 1$

$$\Delta\phi_\tau = G \frac{R \omega_0 \tau}{Q 2}$$

- Phase margin defined as

$$\Delta\phi_m = \pi - \frac{\pi}{2} - \Delta\phi_\tau = \frac{\pi}{2} - G \frac{R \omega_0 \tau}{Q 2}$$

# Stability with feedback

→ **Phase margin:**  $\Delta\phi_m = \frac{\pi}{2} - \Delta\phi_\tau = \frac{\pi}{2} - G \frac{R}{Q} \frac{\omega_0 \tau}{2}$

$$\Delta\phi_{\max} = \frac{\pi}{4}$$

- **Conventional stability limit defined for**

→ **Maximum stable gain:**

$$G_{\max} = \frac{\pi}{2} \frac{1}{R/Q} \frac{1}{\omega_0 \tau}$$

# Impedance with feedback

- Normalized impedance:

$$Z_{\text{fb}}(\omega) = \frac{\frac{1}{G}}{\frac{1}{GR} + e^{-i\Delta\omega\tau} + \frac{4}{\pi}i\frac{G_{\text{max}}}{G}\Delta\omega\tau}$$

Amplifier

$Z(\omega)$

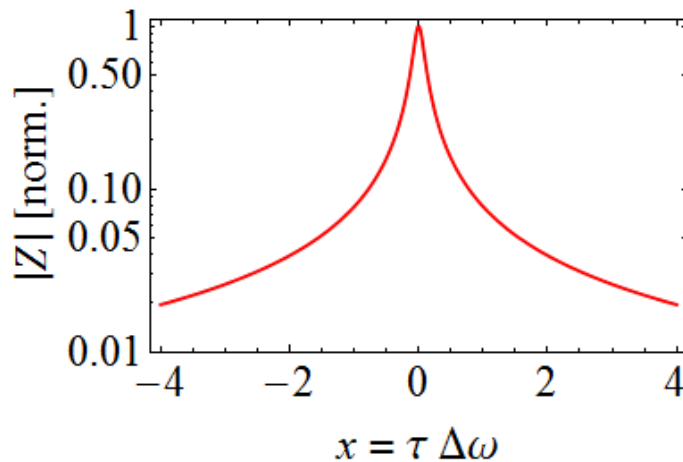


Beam

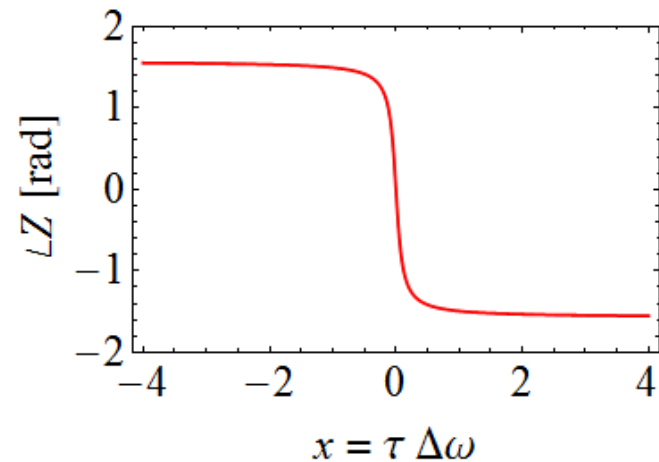
$Z_{\text{fb}}(\omega)$

$$Z_{\text{fb}}(\omega_0) = \frac{R}{1 + GR}$$

$G/G_{\text{max}} = 0.00$



Phase margin: 90.00°



# Example: direct feedback lab experiment

- Coaxial cavity,  $f_o \approx 57$  MHz
- 'Power' amplifier:  $\sim 10$  mW

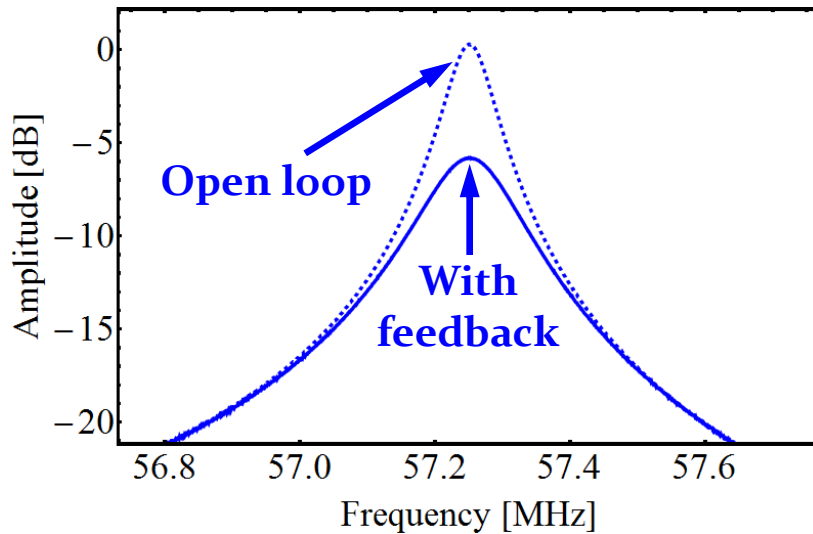


→ No risk of damage

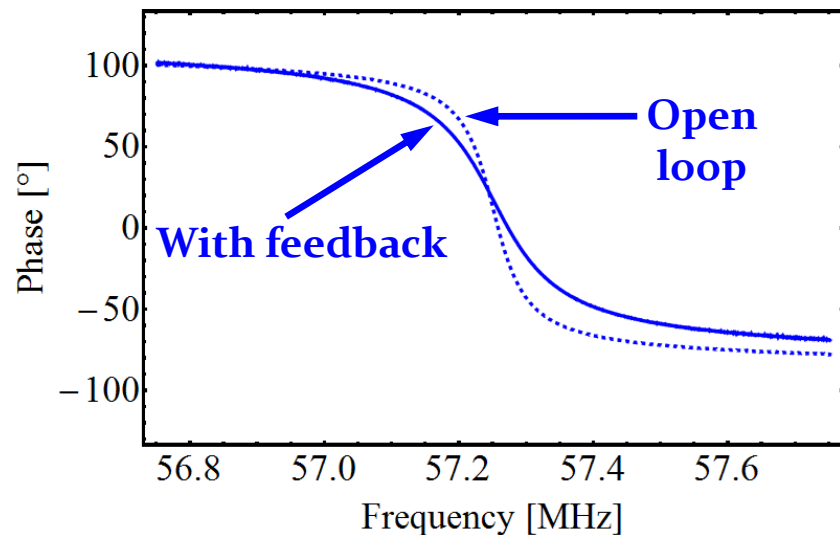
→ Usually more:

**Tens to hundreds of kilowatts**

## Measured transfer function

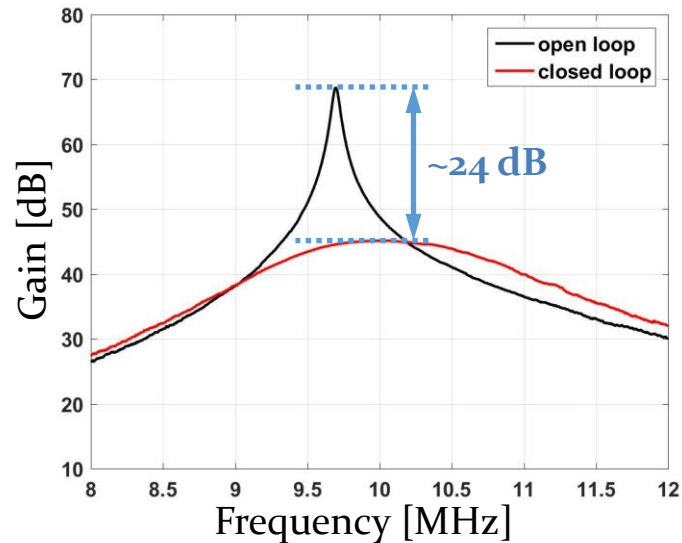


## Phase

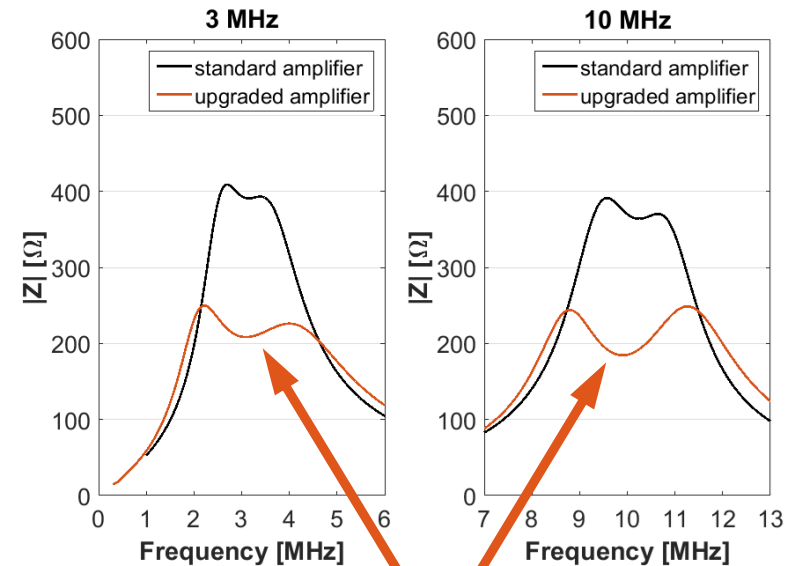


# Example: 10 MHz RF system in CERN PS

## Transfer function with and without feedback



## More feedback gain



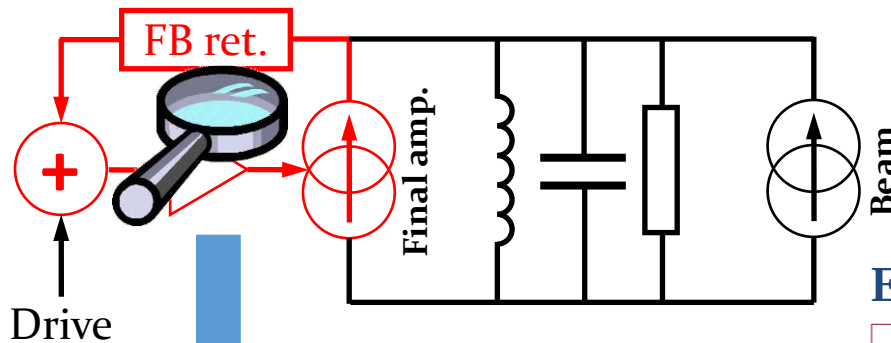
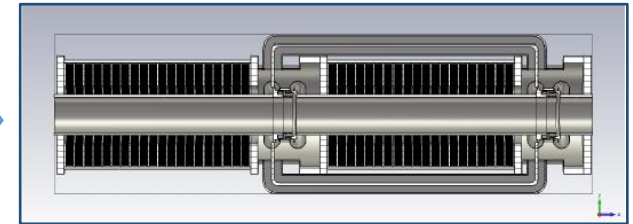
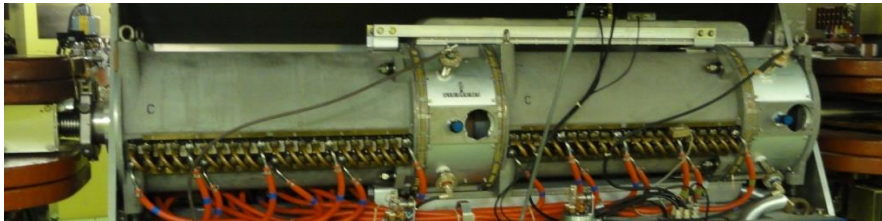
Pushed to  
stability limit

- Feedback gain of 24 dB
- Equivalent impedance,  $Z_{fb}(\omega)$  reduced by more than order of magnitude
- Impedance for amplifier remains unchanged,  $Z(\omega)$

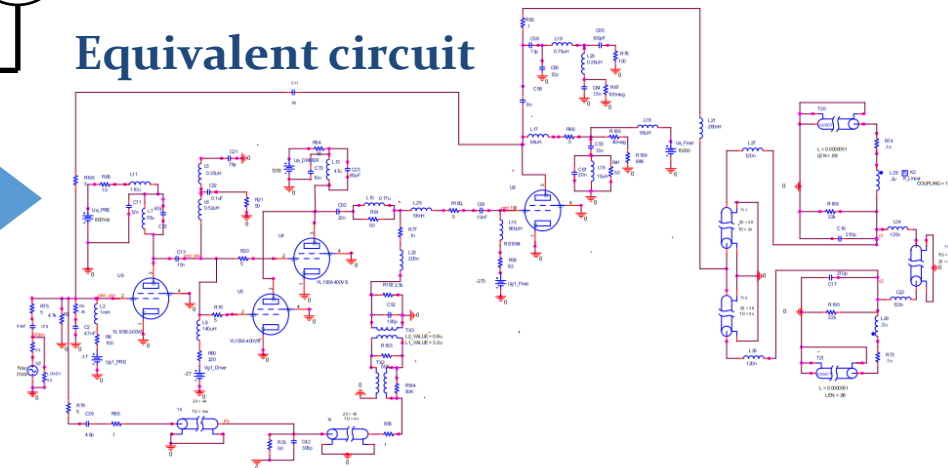


# Example: CERN PS 10 MHz cavity feedback

- 10 + 1 ferrite loaded cavities, tunable from 2.8...10 MHz
- Two resonators excited in parallel by one amplifier



Equivalent circuit

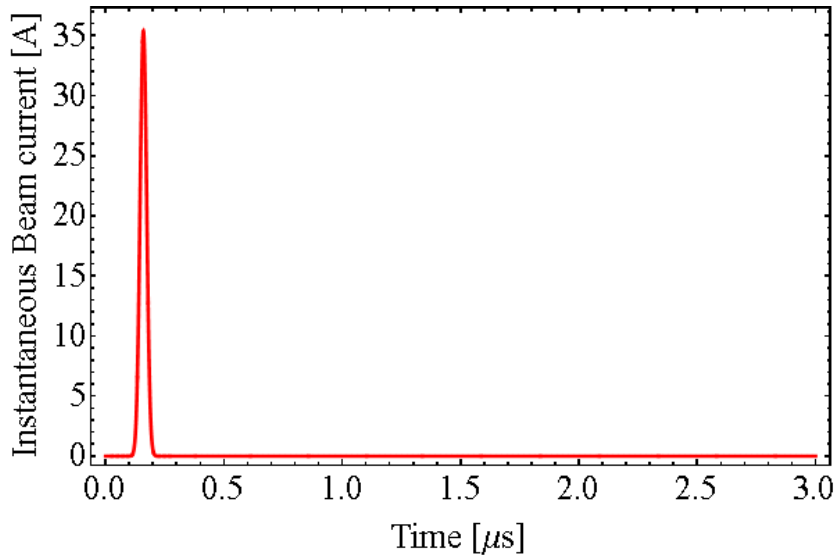


→ Realistic amplifier behaviour with higher order modes

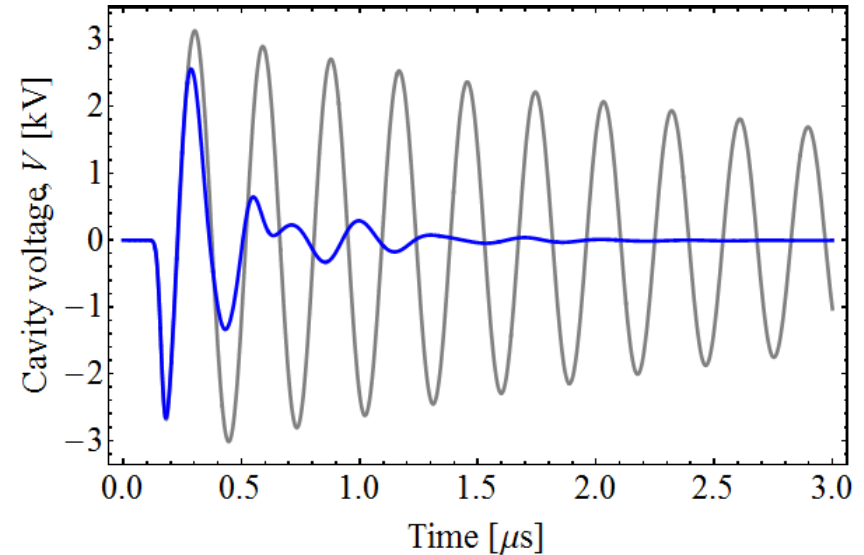
# Modelling a real cavity – time domain

- Time domain response of cavity and amplifier

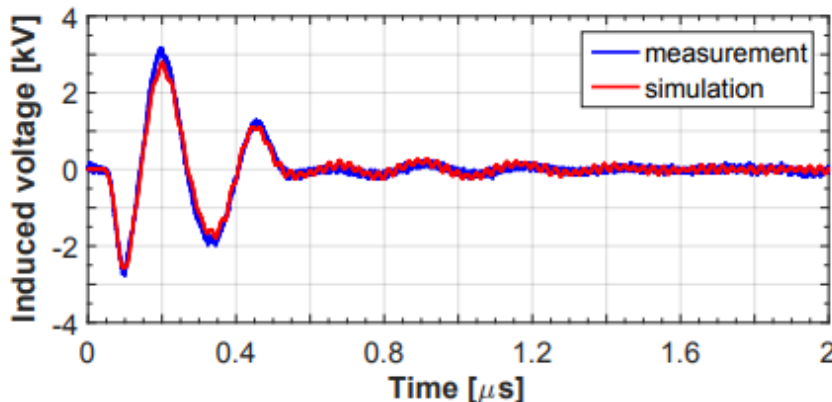
Exciting bunch



Cavity response: closed loop



→ Comparing with measured response to **beam excitation**



- **No instantaneous damping** due to inherent delay
- **Filling time significantly reduced** with feedback

# Limitations of direct feedback

- Contributions to maximum feedback gain

$$G_{\max} = \frac{\pi}{2} \frac{1}{R/Q} \frac{1}{\omega_0 \tau} \quad \text{using} \quad Q = \frac{\omega_0}{\Delta\omega_{-3\text{dB}}}$$

$$= \frac{\pi}{2} \cdot \frac{1}{R} \cdot \frac{1}{\Delta\omega_{-3\text{dB}}} \cdot \frac{1}{\tau}$$

1. Decrease shunt impedance → **not a good idea**
2. Reduction of **delay has physical limits**
  - How close can amplifier be to cavity?
  - Minimum delay of feedback chain?
3. Decrease **bandwidth**
  - Reduce bandwidth of feedback chain instead of cavity?



# Feedback with delay



# Feedback with delay

## Why?

- **Loop delay cannot be made short: amplifier not close enough to cavity**
- **Cavity to be damped has large bandwidth**
- **Need impedance reduction beyond stability limit of direct feedback**

## How?

- **Cleverly use the properties of the beam spectrum**
- **Profit from of slow synchrotron motion**

# Longitudinal beam spectrum

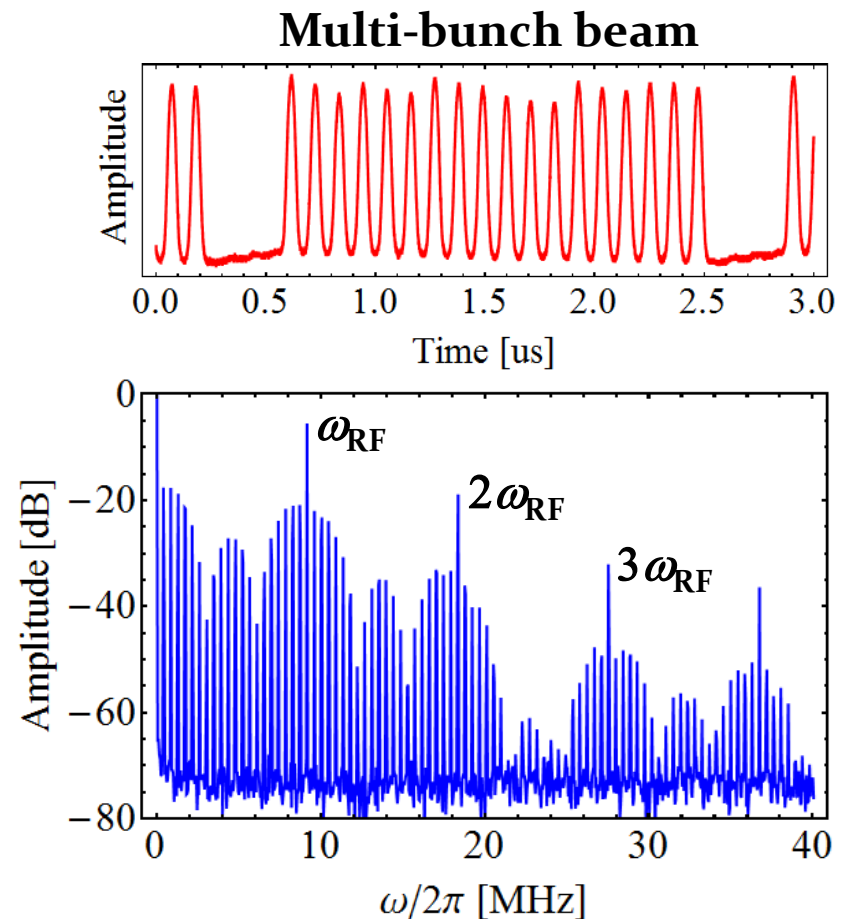
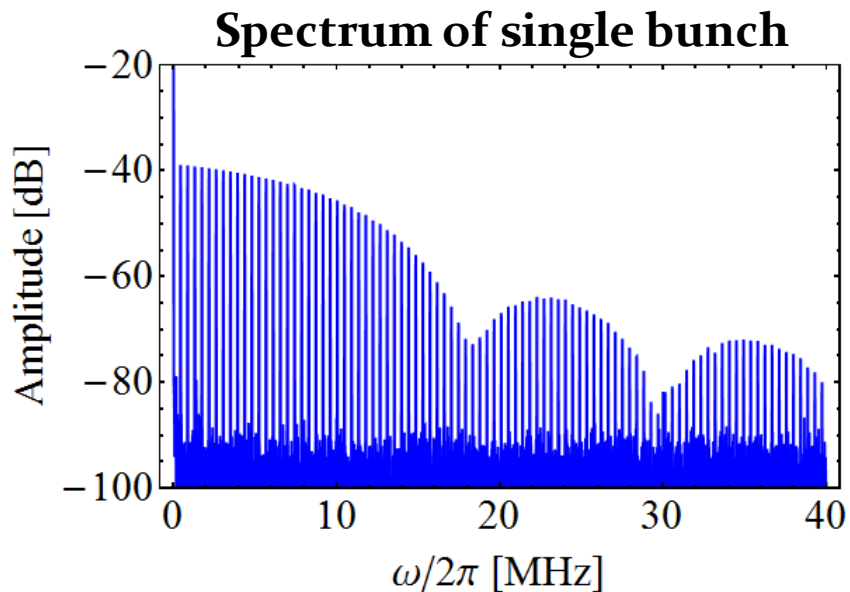
# Longitudinal beam spectrum

- **Circular accelerator**

→ Beam signal periodic with **revolution frequency**:  $\omega_{\text{rev}}$

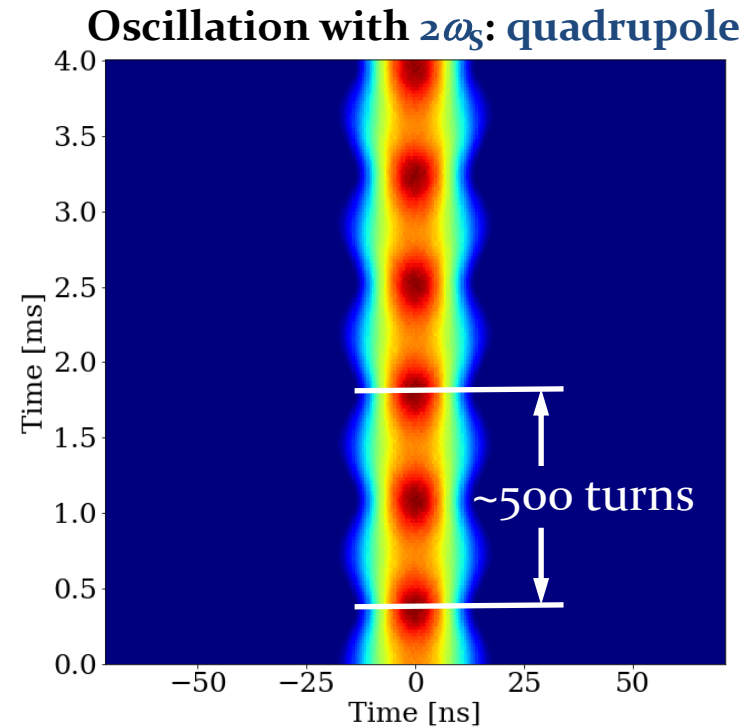
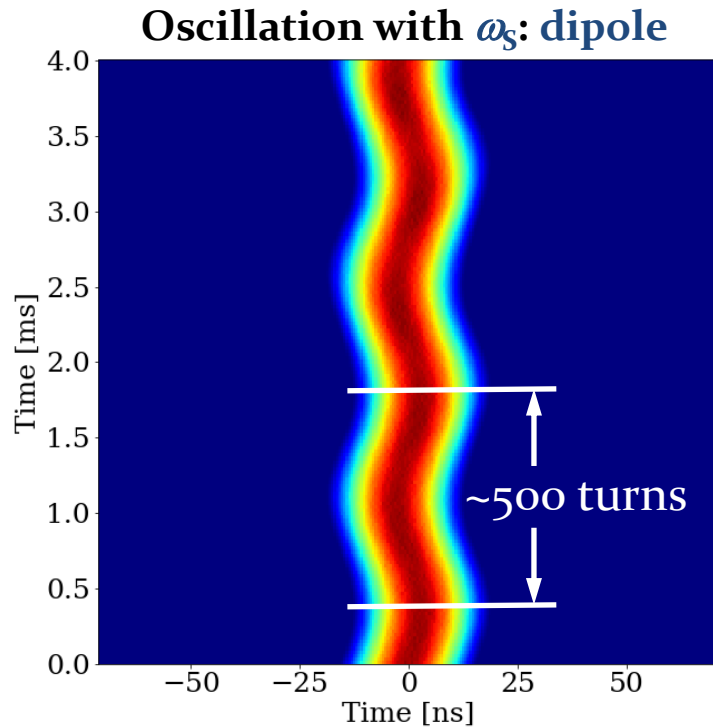
→ **Spectral components at:**

$$\omega = n\omega_{\text{rev}}$$



# Longitudinal beam spectrum

- Longitudinally unstable bunches may perform oscillations  
 → **Synchrotron frequency** is basic periodicity:  $\omega_S$



- Adds sidebands at  $\omega_{\text{rev}}$  harmonics:  $\omega = n\omega_{\text{rev}} \pm m\omega_S$
- Sidebands usually close to  $\omega_{\text{rev}}$  harmonic since  $\omega_S \ll \omega_{\text{rev}}$

# Beam spectrum

→ Beam can only induce voltage at frequencies

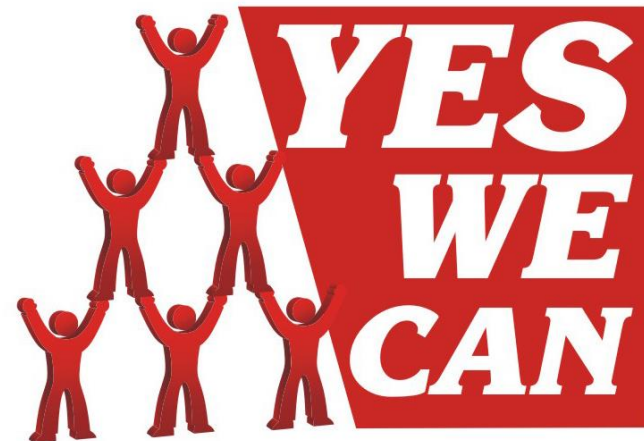
$$\omega = n\omega_{\text{rev}} \pm m\omega_S$$

→ Relevant frequencies from RF point of view

$$\omega = \omega_{\text{RF}} \pm n\omega_{\text{rev}} \pm m\omega_S$$

→ Feedback only needs to damp these frequency components

→ Can one profit from this property for **RF feedback beyond conventional stability limit?**



# Periodic filters

# Periodic notch and comb filters

- **Transfer function periodic in frequency**

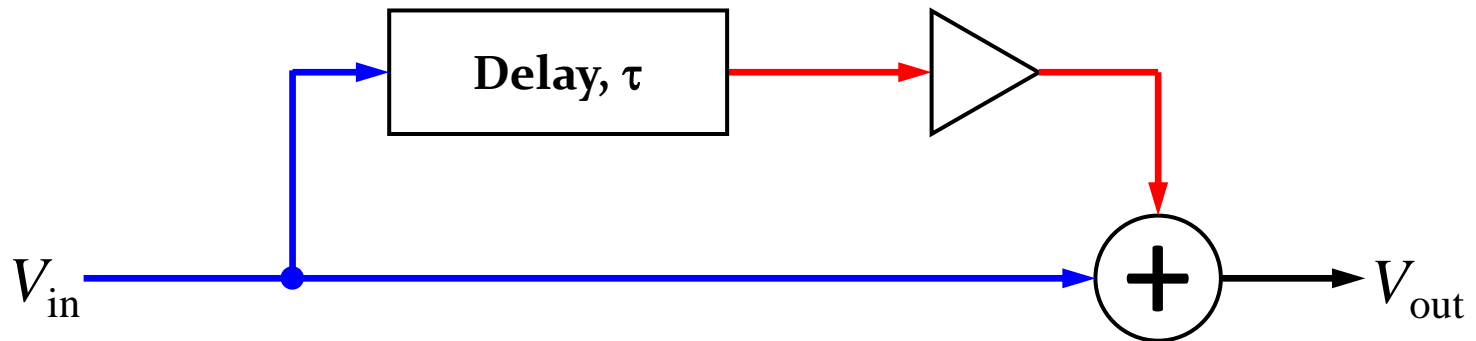
$$H(\omega) = H(\omega \bmod \omega_0)$$

- **Niche application in communication technology**  
→ **Who wants to listen to multiple radio stations at the same time?**
  - **Very useful for circular accelerators thanks to properties of beam spectrum**
- **How to build such filters?**

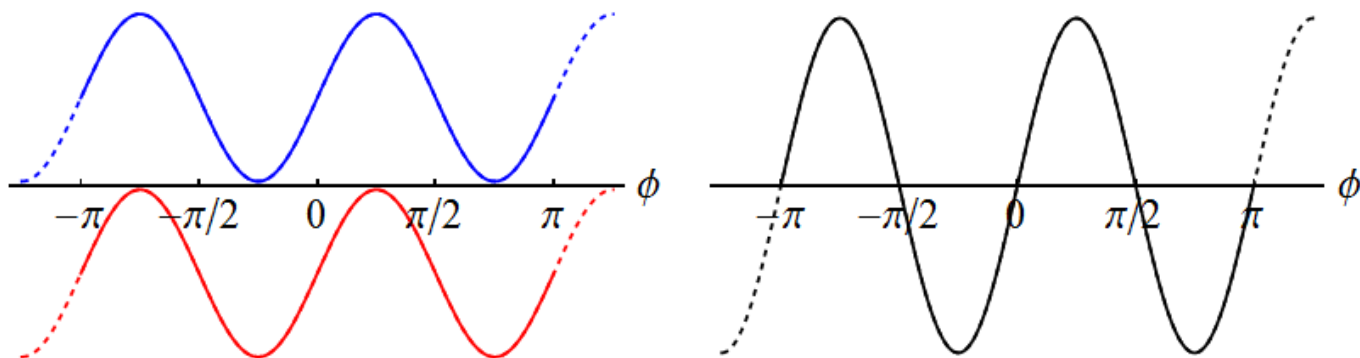


# Periodic notch and comb filters

- Add signal with itself, but delay by a fixed delay,  $\tau$



- Addition (maxima) or subtraction (minima)



$$y(t) = x(t) + x(t - \tau)$$

# Periodic notch and comb filters

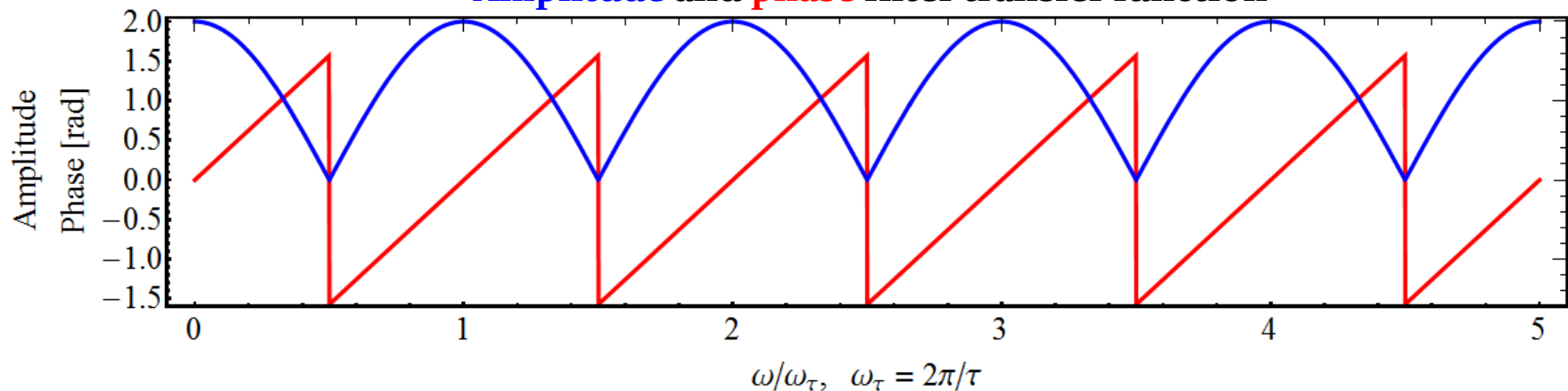
- Add signal with itself, but delay by a fixed delay,  $\tau$

$$x(t) = e^{i\omega t}$$

$$\begin{aligned} y(t) &= x(t) + x(t - \tau) \\ &= e^{i\omega t} + e^{i\omega(t-\tau)} \\ &= e^{i\omega t} (1 + e^{-i\omega\tau}) \end{aligned}$$

- Addition (maxima) or subtraction (minima)

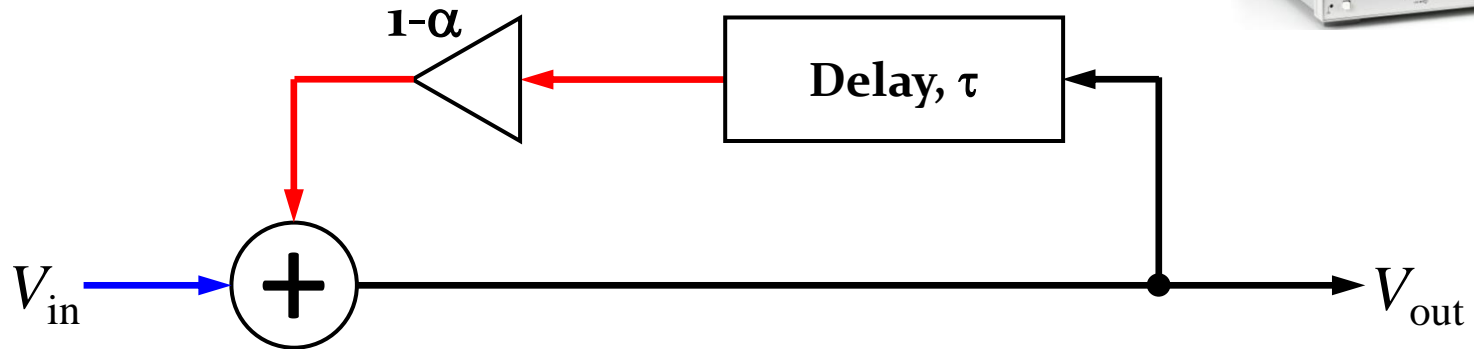
Amplitude and phase filter transfer function



→ Filter to remove (notch) revolution frequency harmonics

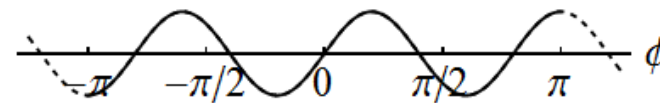
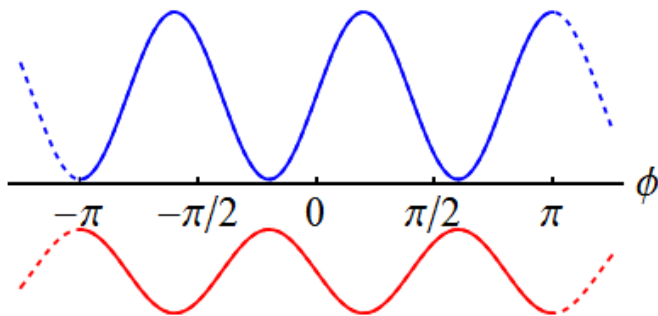
# Periodic notch and comb filters

- Delay output signal by  $\tau$  and add to input signal



- Addition (maxima) or subtraction (minima)

$$y(t) = x(t) + y(t - \tau)$$



# Periodic notch and comb filters

- Delay output signal by  $\tau$  and add to input signal

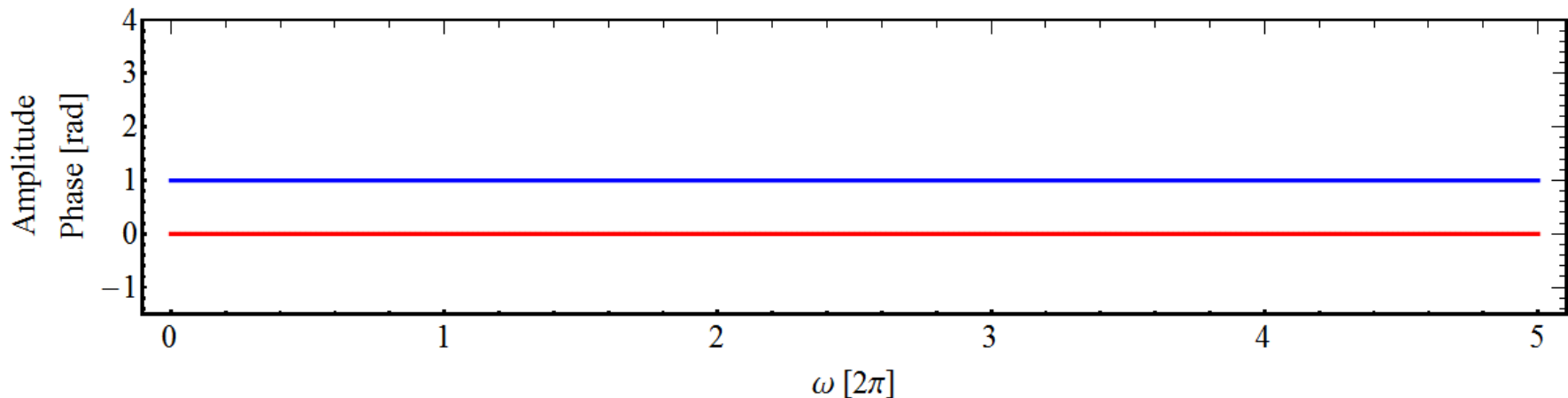
$$y(t) = x(t) + y(t - \tau)$$



- Ansatz:  $y(t) = ae^{i\omega t}$   $y(t) = e^{i\omega t} \cdot \frac{1}{1 - e^{i\omega\tau}}$

- Addition (maxima) or subtraction (minima)

$$\alpha = 0.00$$

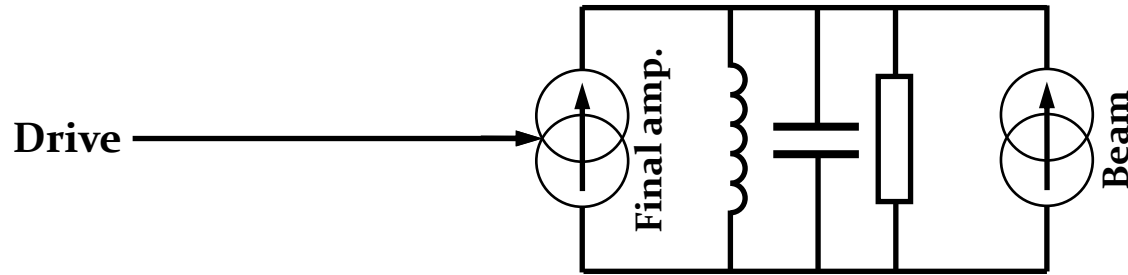


→ Remove everything but revolution frequency harmonics

# Feedback with periodic filters

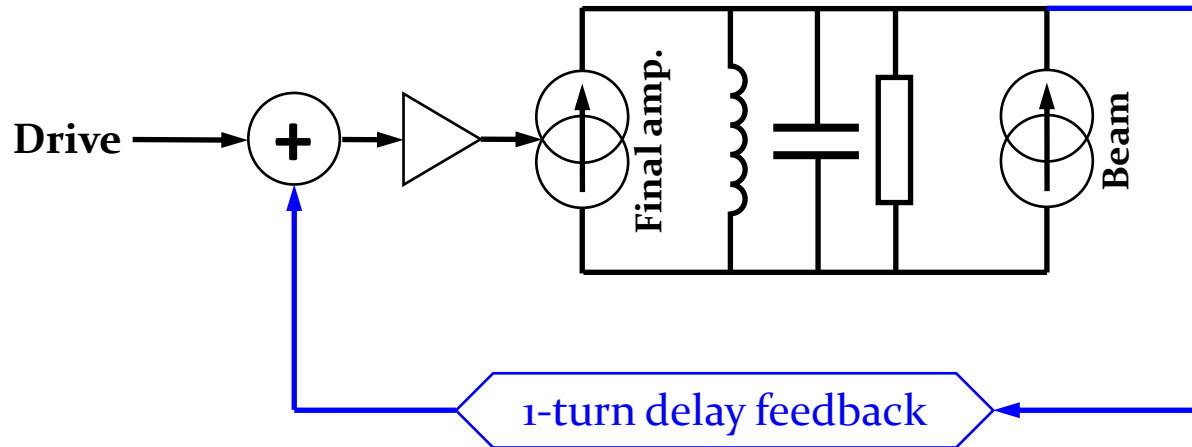
# 1-turn delay feedback

1. **Comb filter** to extract revolution frequency harmonics
2. **Delay** to complete physical delay of cables and signal processing to **1 revolution period**



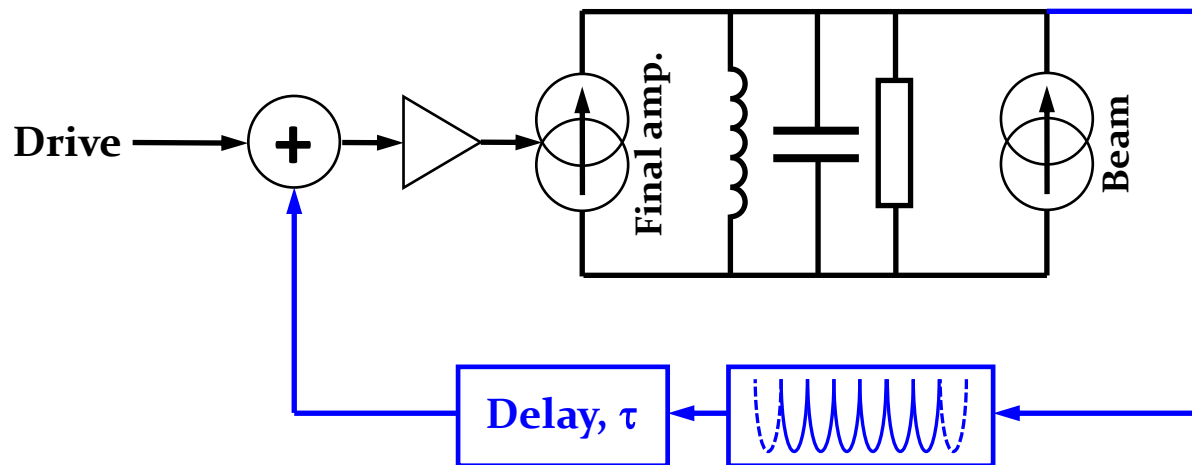
# 1-turn delay feedback

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# 1-turn delay feedback

1. **Comb filter** to extract revolution frequency harmonics
2. **Delay** to complete physical delay of cables and signal processing to **1 revolution period**



$$G \rightarrow GH(\omega)$$

$$Z_{\text{fb}}(\omega) = \frac{Z(\omega)}{1 + Z(\omega)G e^{-i\Delta\omega\tau}}$$

$$\rightarrow Z_{1\text{tfb}}(\omega) = \frac{Z(\omega)}{1 + Z(\omega)GH(\omega)e^{-i\Delta\omega\tau}}$$

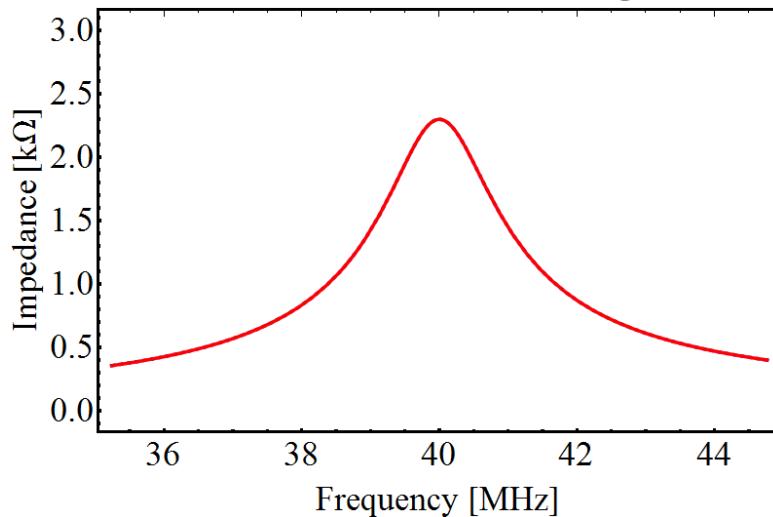


# Cavity transfer function with 1-turn delay FB <sup>40</sup>

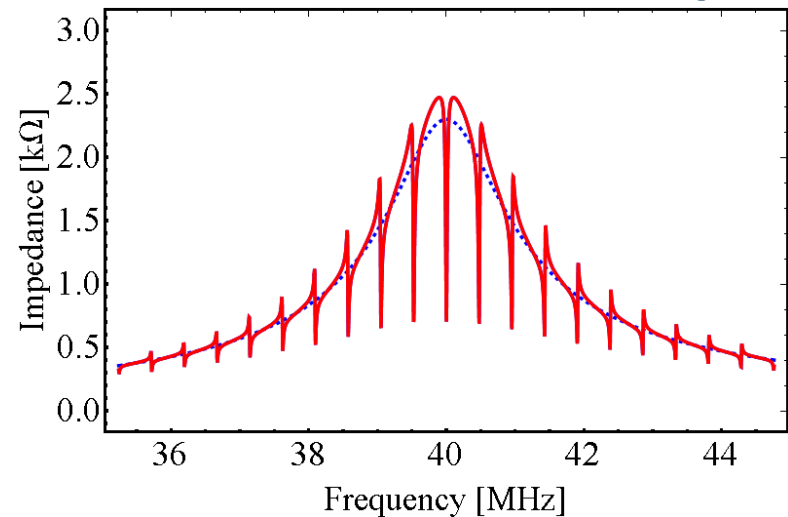
→ **Transfer function with comb filter**

$$\rightarrow Z_{1\text{tfb}}(\omega) = \frac{Z(\omega)}{1 + Z(\omega)GH(\omega)e^{-i\Delta\omega\tau}}$$

**Variation of feedback gain**



**Variation of feedback delay**



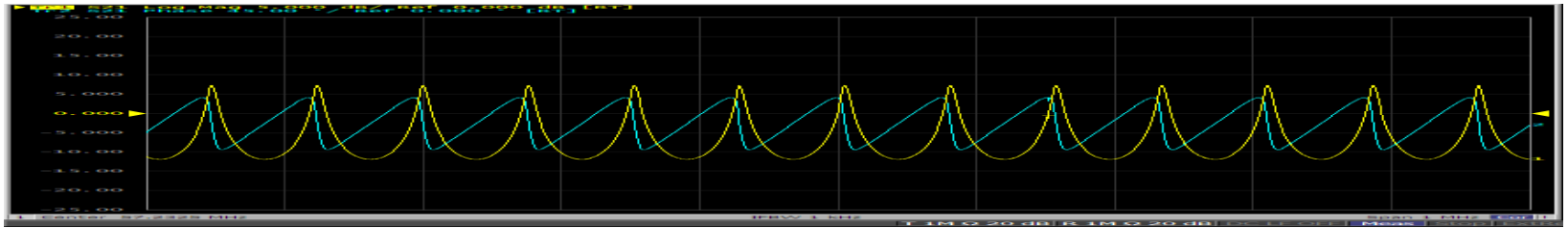
→ **Impedance between revolution frequency harmonics**

→ **Not excited by beam, but potential issue for stability**

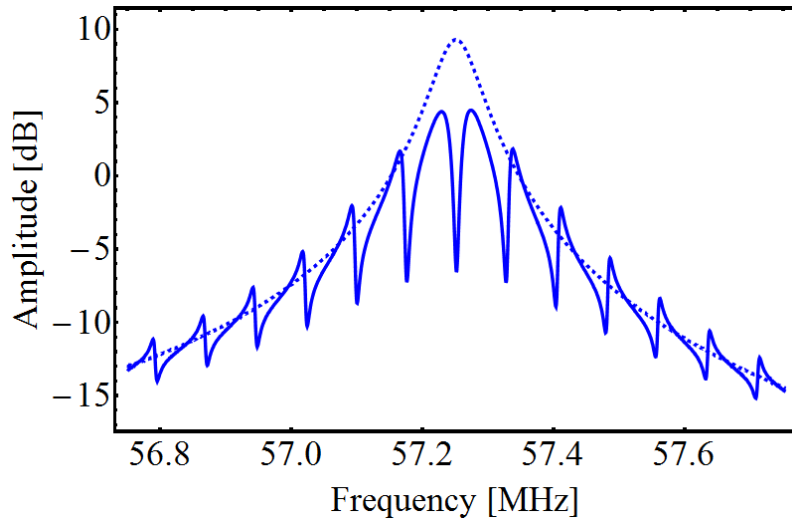
→ **Total delay very critical**

# Example: long delay feedback lab experiment<sup>41</sup>

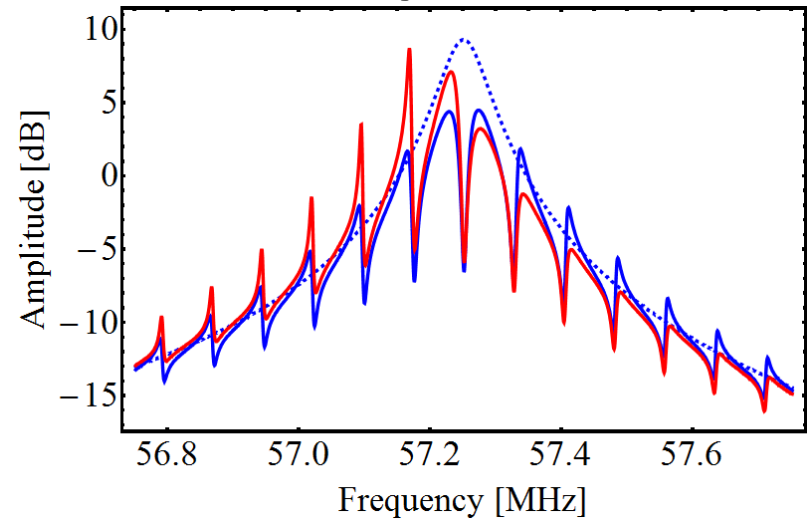
- 1-turn delay feedback around 57 MHz resonator
  - Analogue comb filter with  $\sim 2.5$  km optical fiber delay
  - Accelerator with  $f_{\text{rev}} \approx 76$  kHz ( $2\pi R \approx 4$  km circumference)



Open/closed loop transfer function

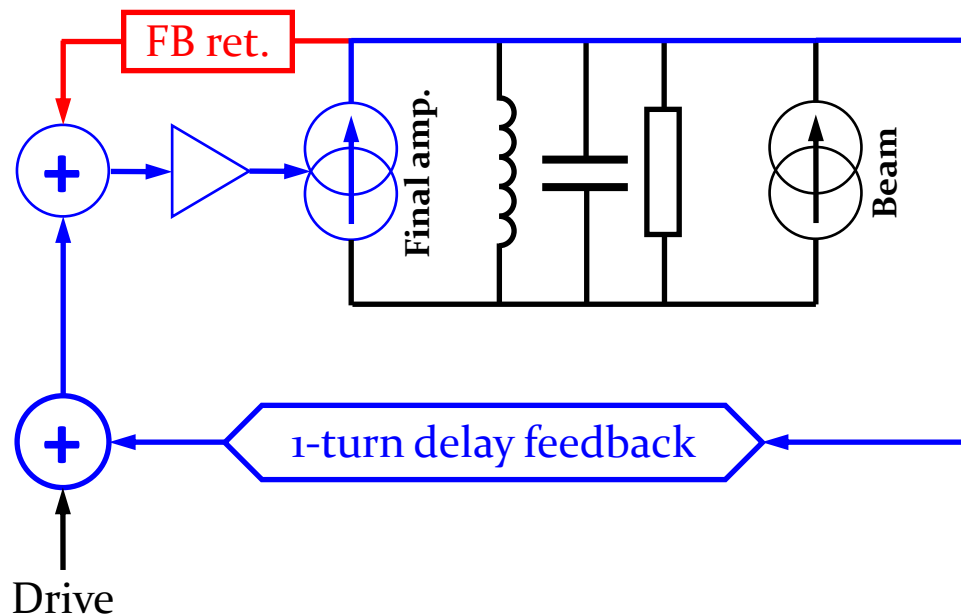
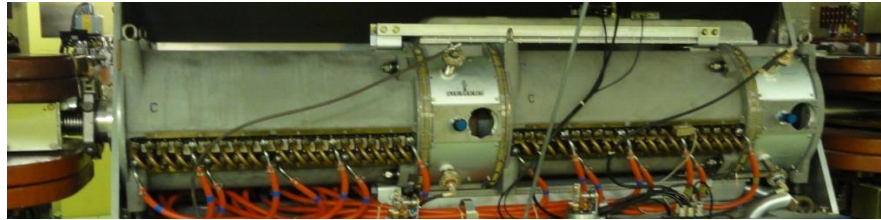


+2/-2 ns delay error ( $\pm 1.4 \cdot 10^{-4}$ )



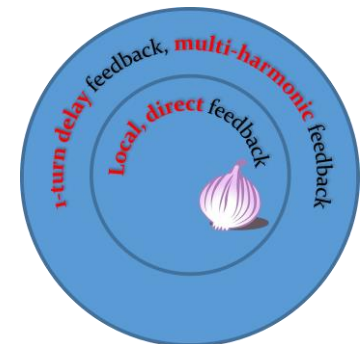
# Example: 1-turn delay in CERN PS

- Combination of direct and 1-turn delay feedback



- Fast wide-band feedback around amplifier (internal)  
 → Gain limited by delay

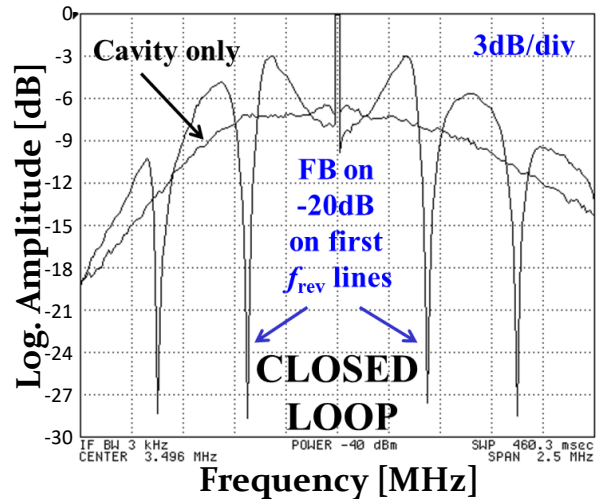
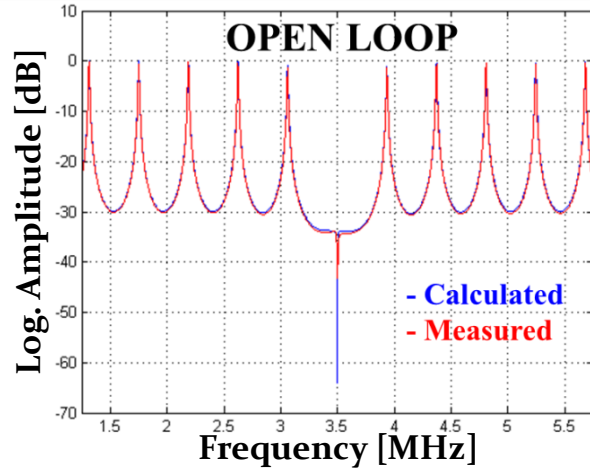
- 1-turn delay feedback  
 → High gain at  $n \times f_{rev}$



# Example: 1-turn delay in CERN PS

→ Reduce cavity impedance beyond stability limit of wide-band FB

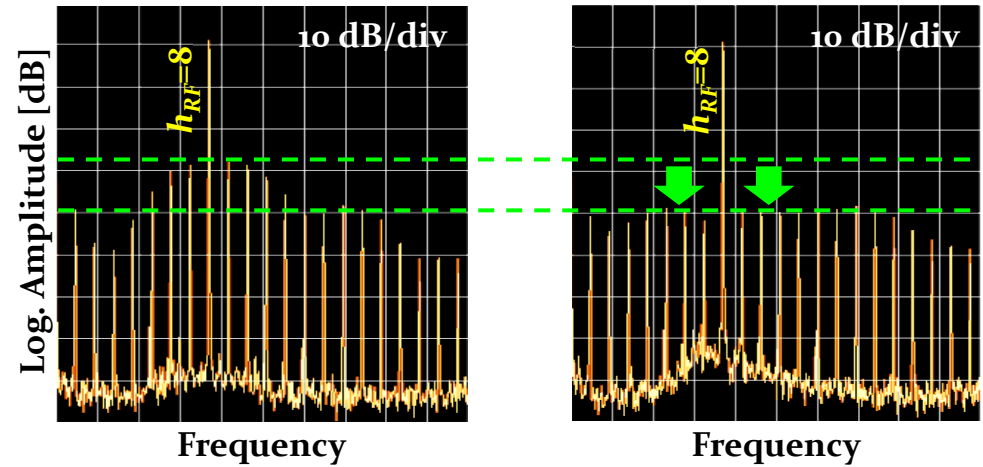
Open/closed loop  
transfer functions



Spectrum at cavity gap return

Feedback off

Feedback on



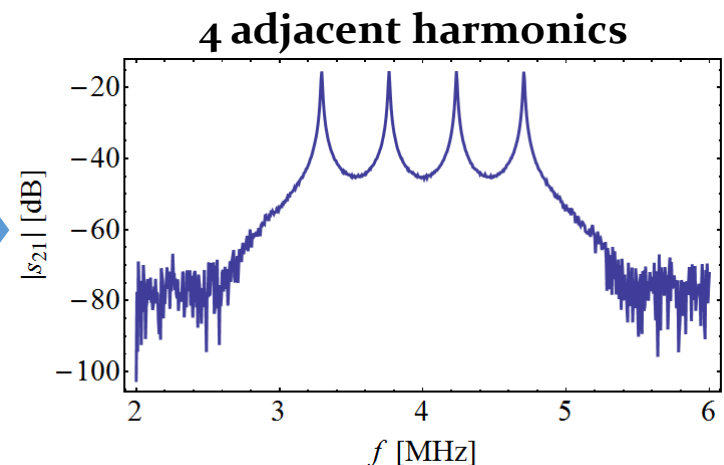
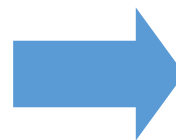
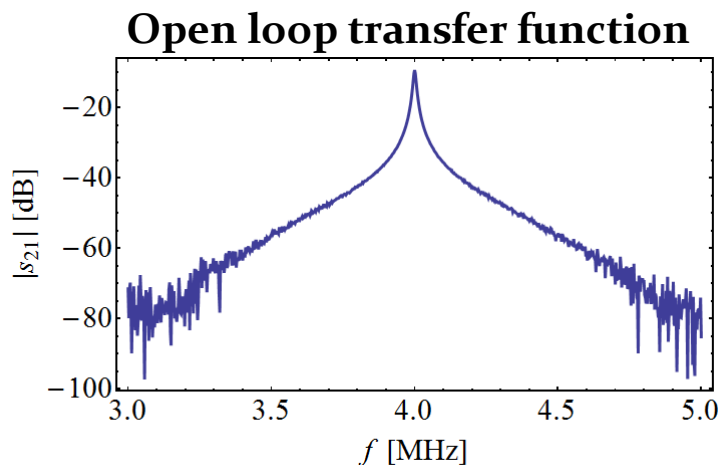
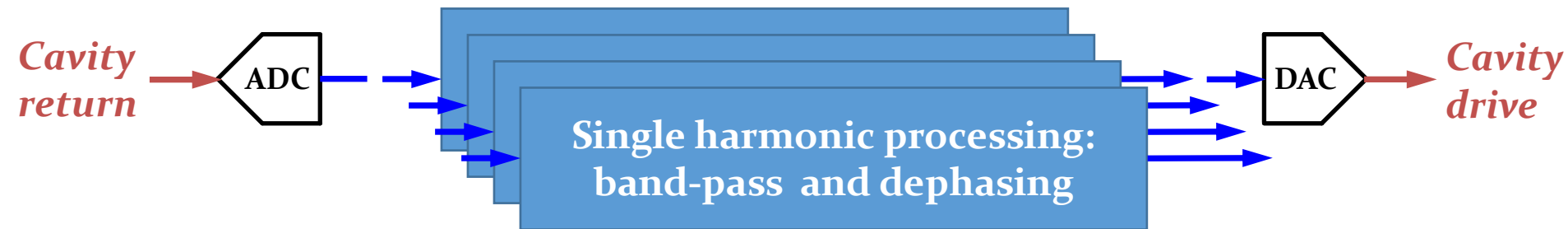
→ Important additional impedance reduction

→ Clever usage of beam periodicity in circular accelerator

# Multi-harmonic feedback

# Treat each harmonic independently

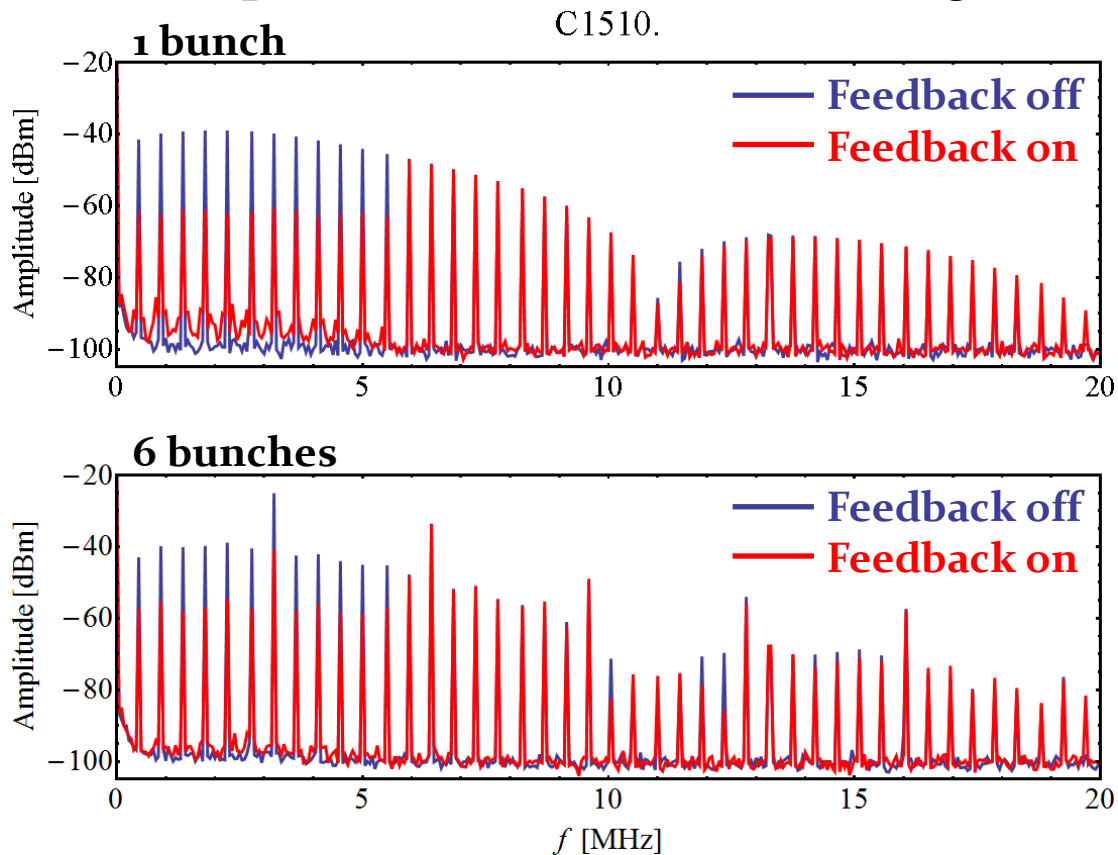
- **Separate feedback loop by harmonic**
  - Full flexibility of individual loop parameters
  - Empowered by processing power of modern digital hardware



# Example: Damping of wide-band cavity

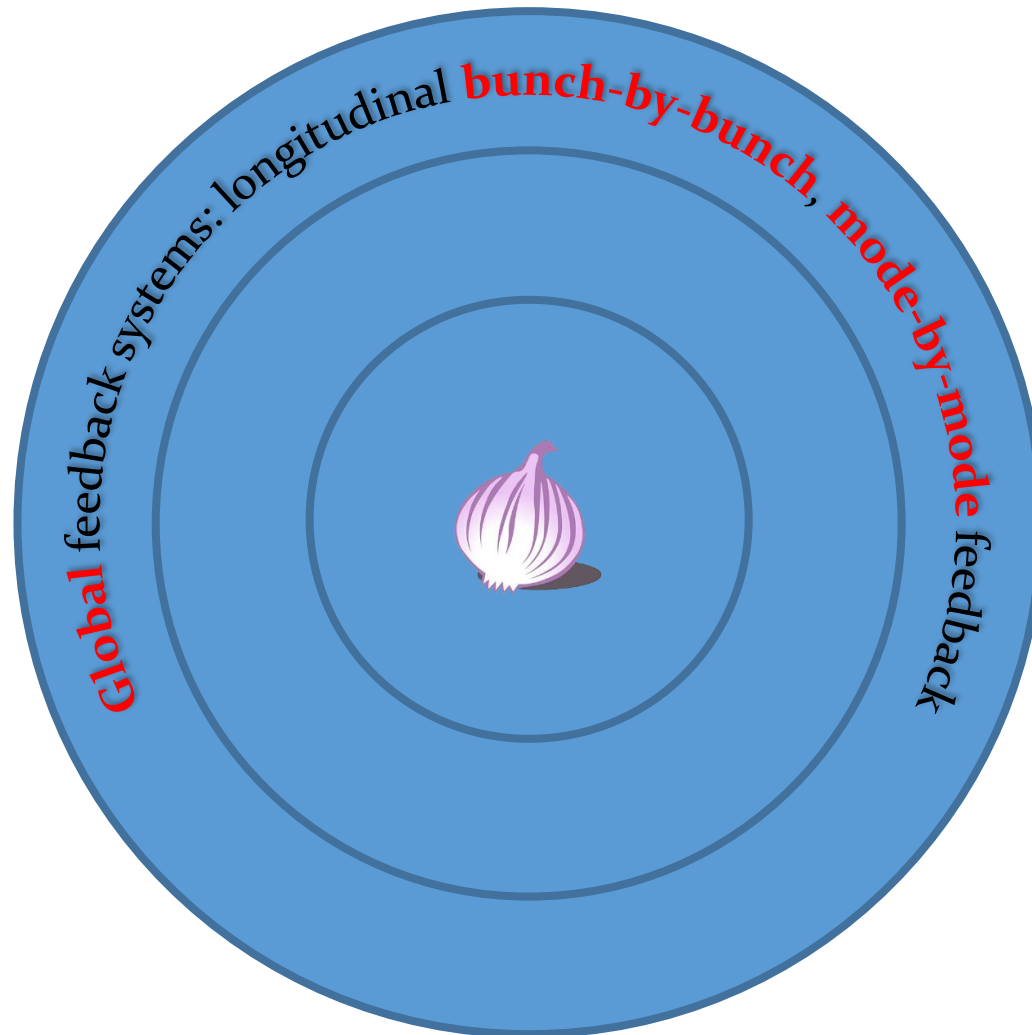
- Multi-harmonic feedback reduces beam induced voltage
- **First 12 revolution frequency harmonics damped**

## Spectrum of beam induced voltage



→ Damping beyond stability limit of direct feedback

# Global feedback



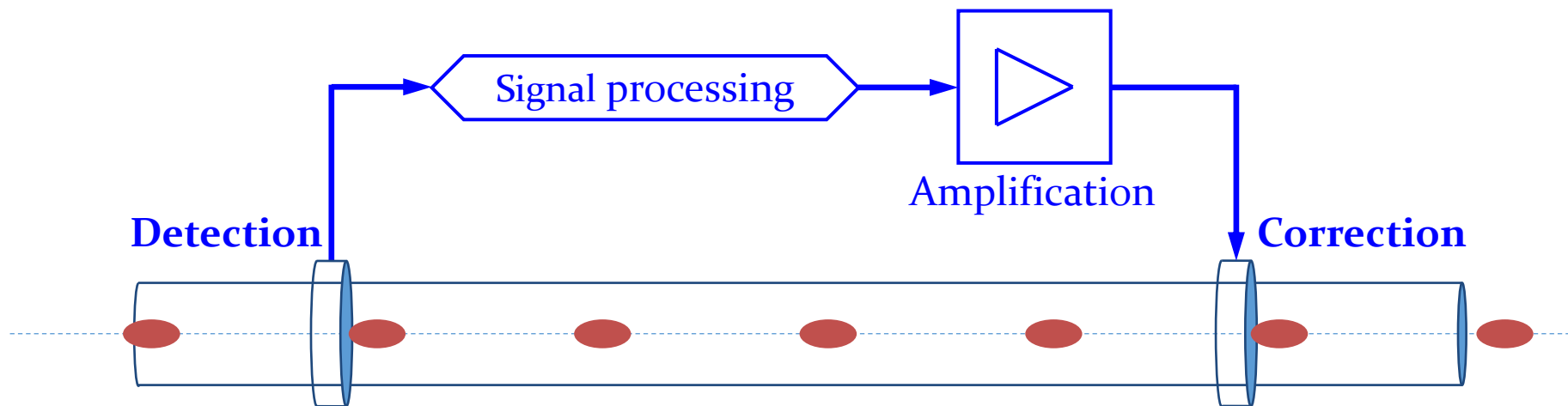


# Global RF feedback

## 1. Detect derivation of beam

→ Transverse: position offset

→ Longitudinal: **phase offset**



## 2. Signal processing to filter relevant information

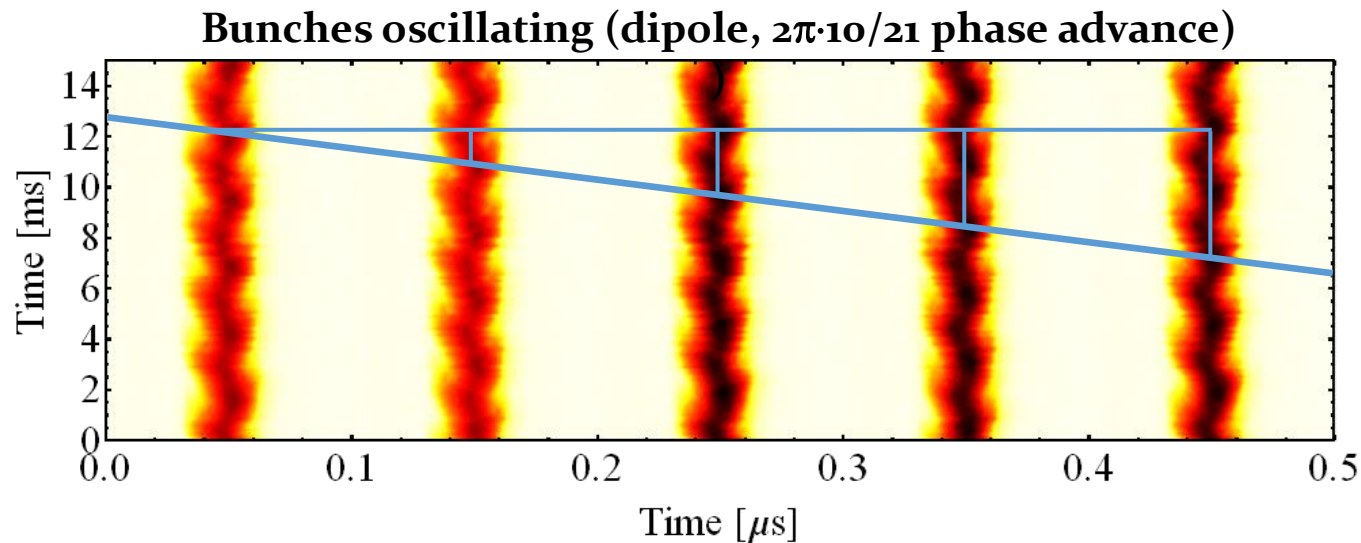
## 3. Amplify and apply correction

→ Drive dedicated kicker

→ Drive accelerating cavities as longitudinal kickers

# Longitudinal oscillation of bunches

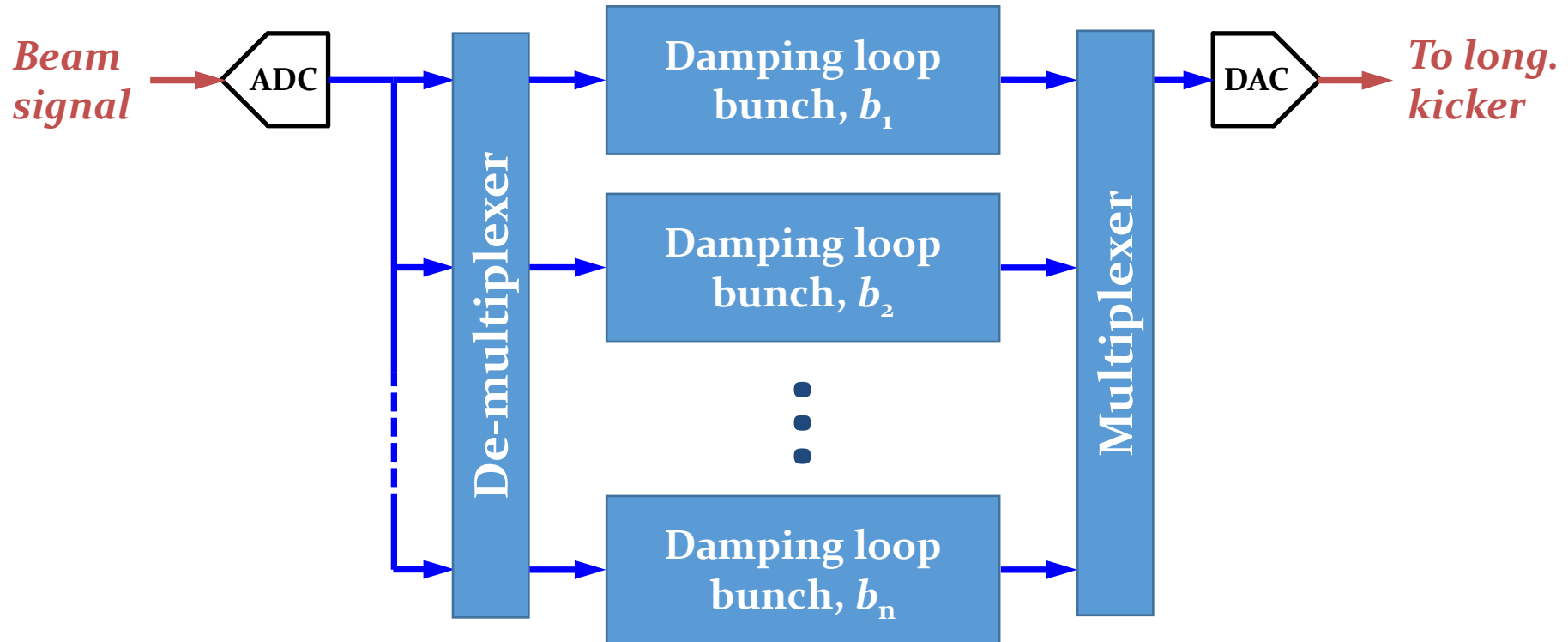
- Longitudinally unstable beam, but **driving source unknown**
- Each bunch oscillation, but not with the same phase



Time domain	Frequency domain
<ul style="list-style-type: none"> <li>• Measure phase of each bunch</li> </ul> <p>→ Apply <b>kick to bring phase back</b> to reference position</p>	<ul style="list-style-type: none"> <li>• Measure spectral component corresponding to mode</li> </ul> <p>→ Apply kick to <b>remove that spectral component</b></p>
→ “Bunch-by-bunch”	→ “Mode-by-mode”

# Time domain: Bunch-by-bunch feedback

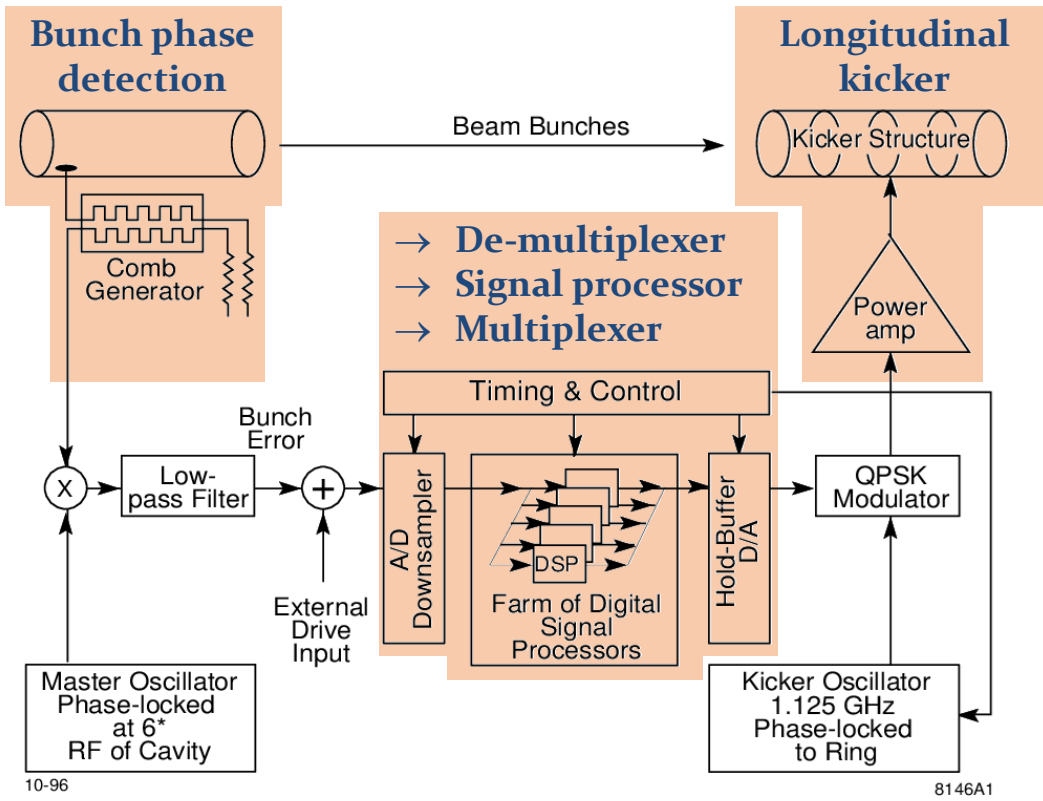
- **Intuitive: Measure oscillation of each bunch and correct**



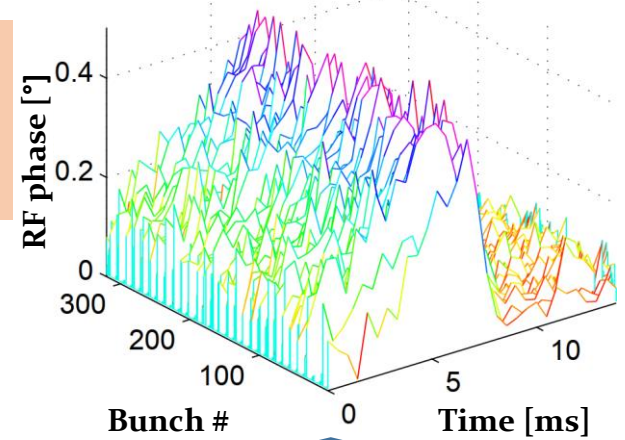
- Multiple feedbacks in **time domain multiplex**
- Flexible control (gain/phase) for each bunch

# Example: Bunch-by-bunch RF feedback

- **Multi-bunch feedback developed for electron storage rings:**  
 Used at Advanced Light Source (ALS) at LBNL, PEP at SLAC, DAΦNE at INFN-LNF, etc.

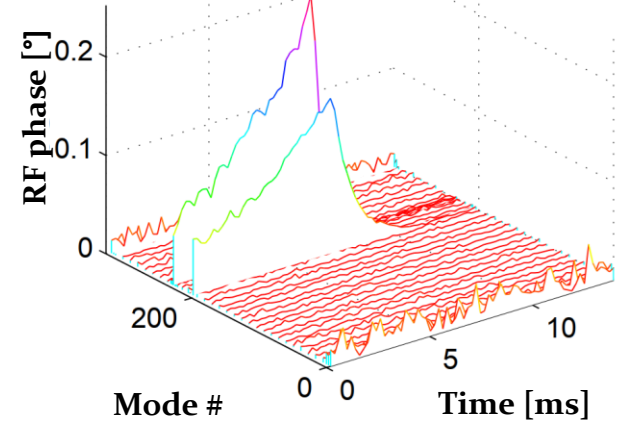


Bunches in time domain



FFT

Modes in frequency domain

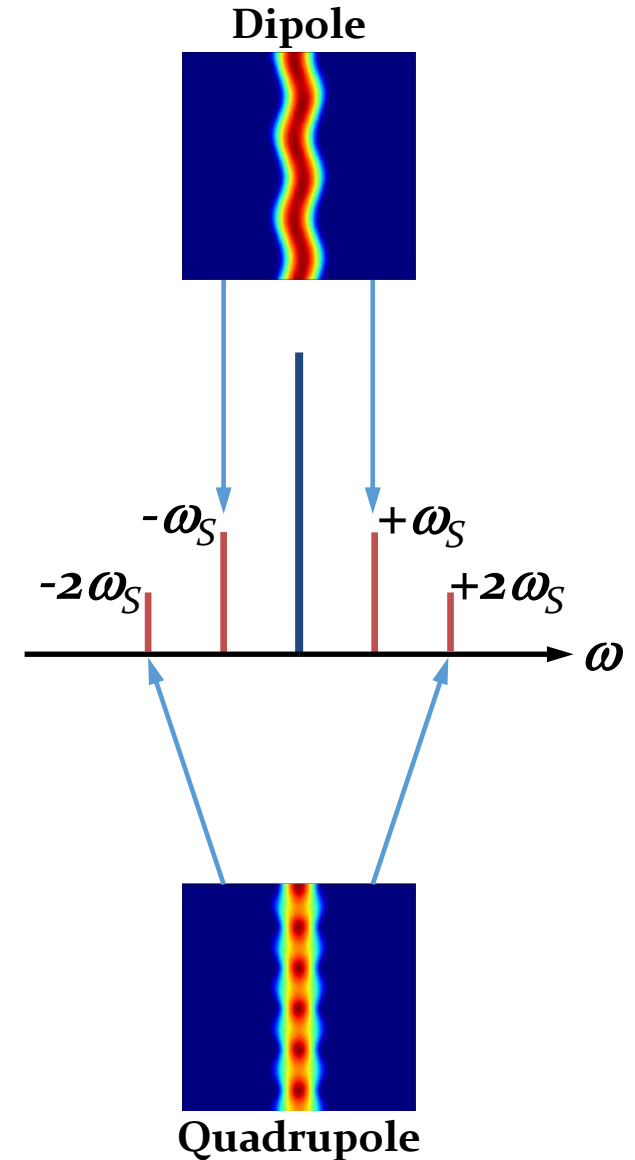
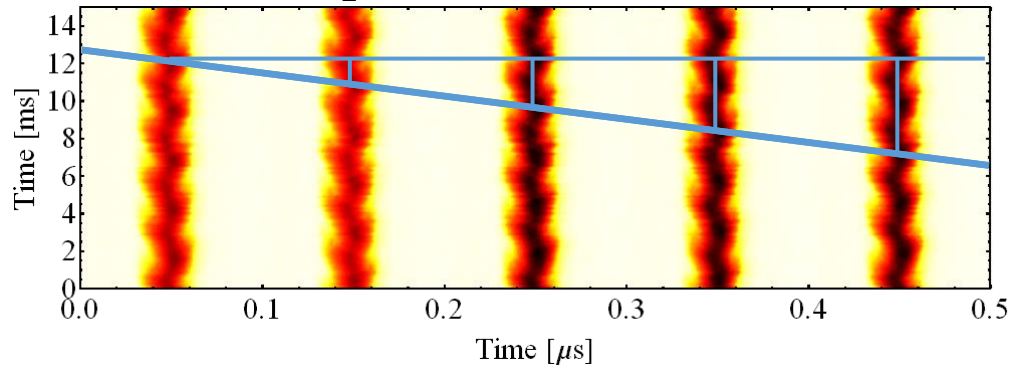


# Frequency domain: Mode-by-Mode

- **Less intuitive: Suppress components in beam spectrum**
- **Fixed phase advance from bunch-to-bunch creates sideband at  $n\omega_{\text{rev}}$**

$$\omega = n\omega_{\text{rev}} \pm m\omega_S$$

$2\pi \cdot 10/21$  phase advance:  $n = 10, m = 1$

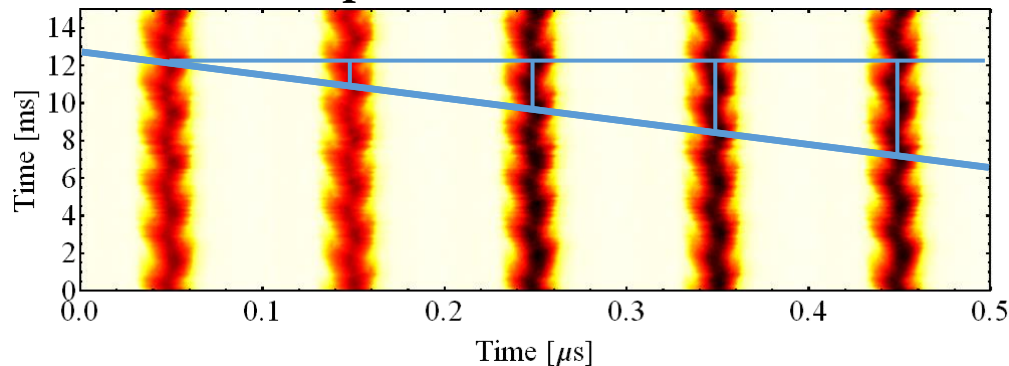


# Frequency domain: Mode-by-Mode

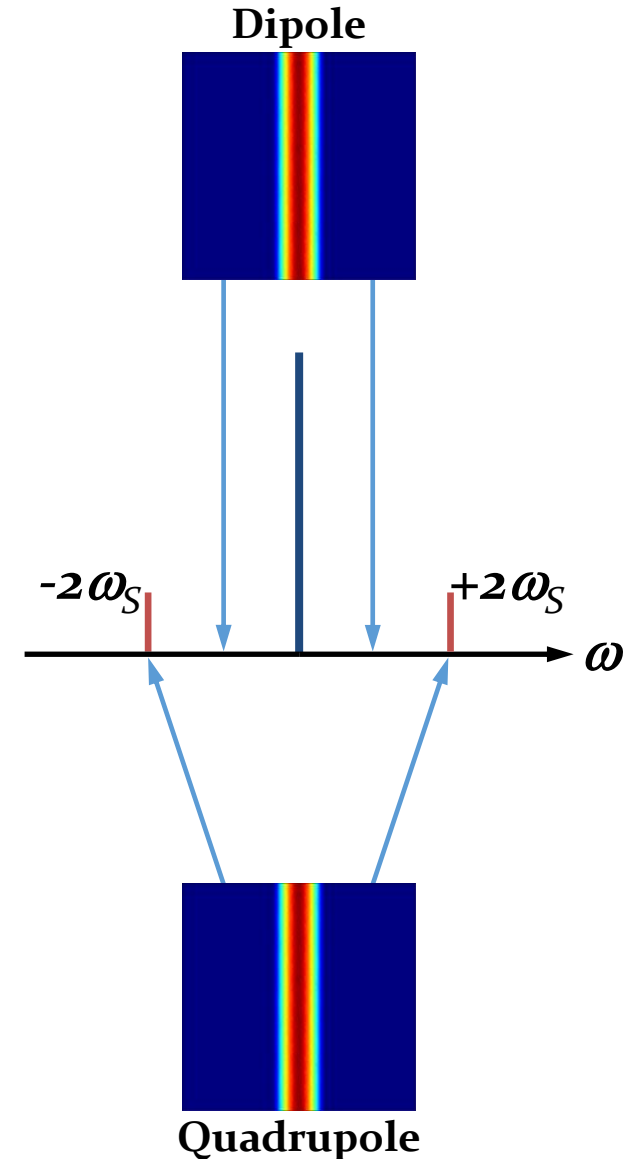
- **Less intuitive: Suppress components in beam spectrum**
- **Fixed phase advance from bunch-to-bunch creates sideband at  $n\omega_{\text{rev}}$**

$$\omega = n\omega_{\text{rev}} \pm m\omega_S$$

$2\pi \cdot 10/21$  phase advance:  $n = 10, m = 1$



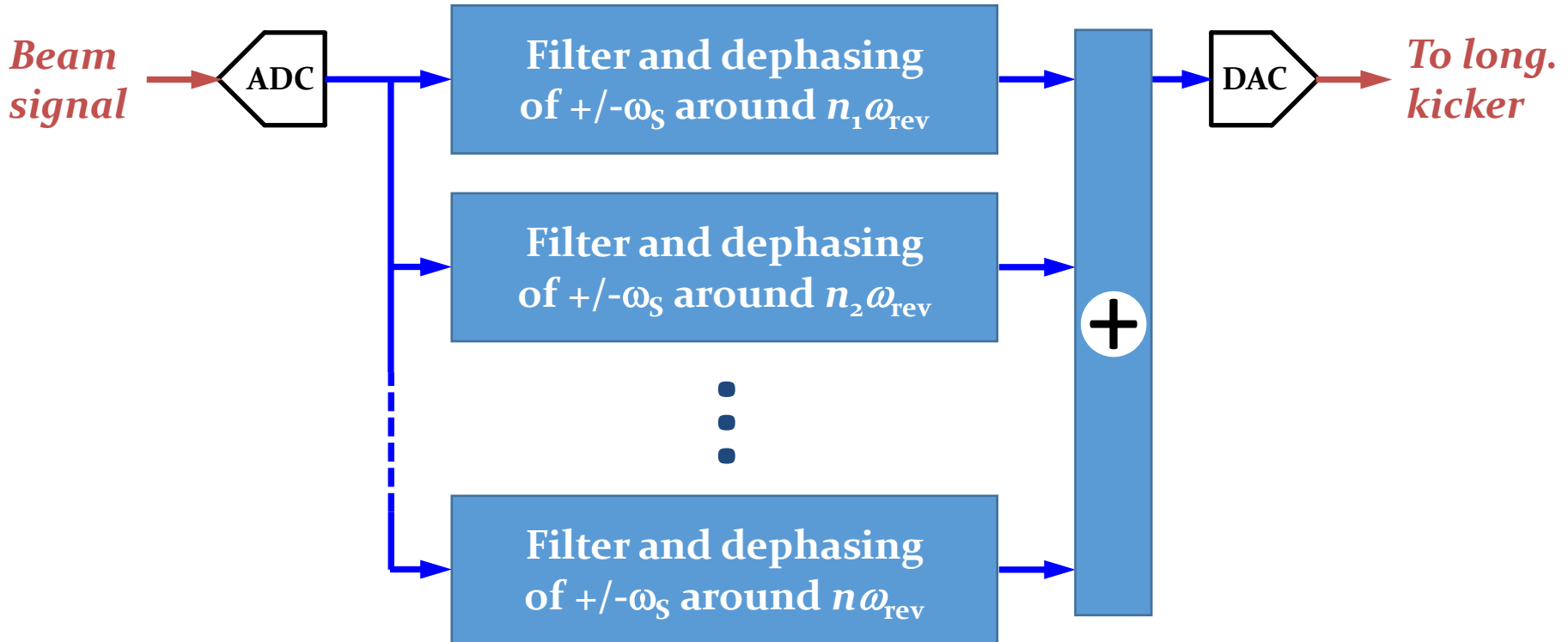
- **No sidebands at  $\pm\omega_S$**   
→ **Dipole oscillations removed**
- **No sidebands at  $\pm 2\omega_S$**   
→ **Quadrupole oscillations removed**



# Mode-by-Mode feedback

1. Filter synchrotron frequency side-bands
2. Inject correction to remove them

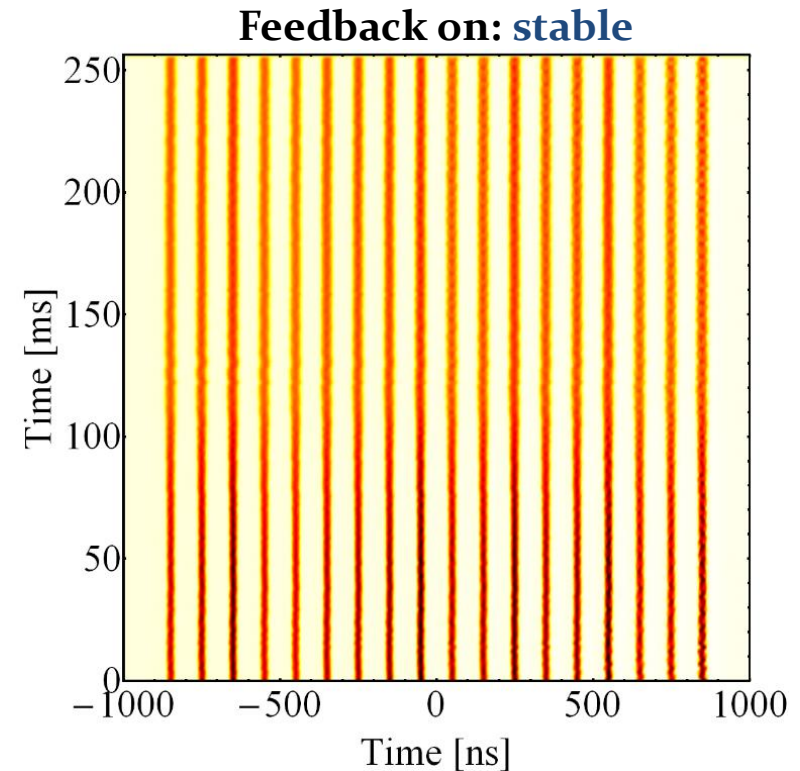
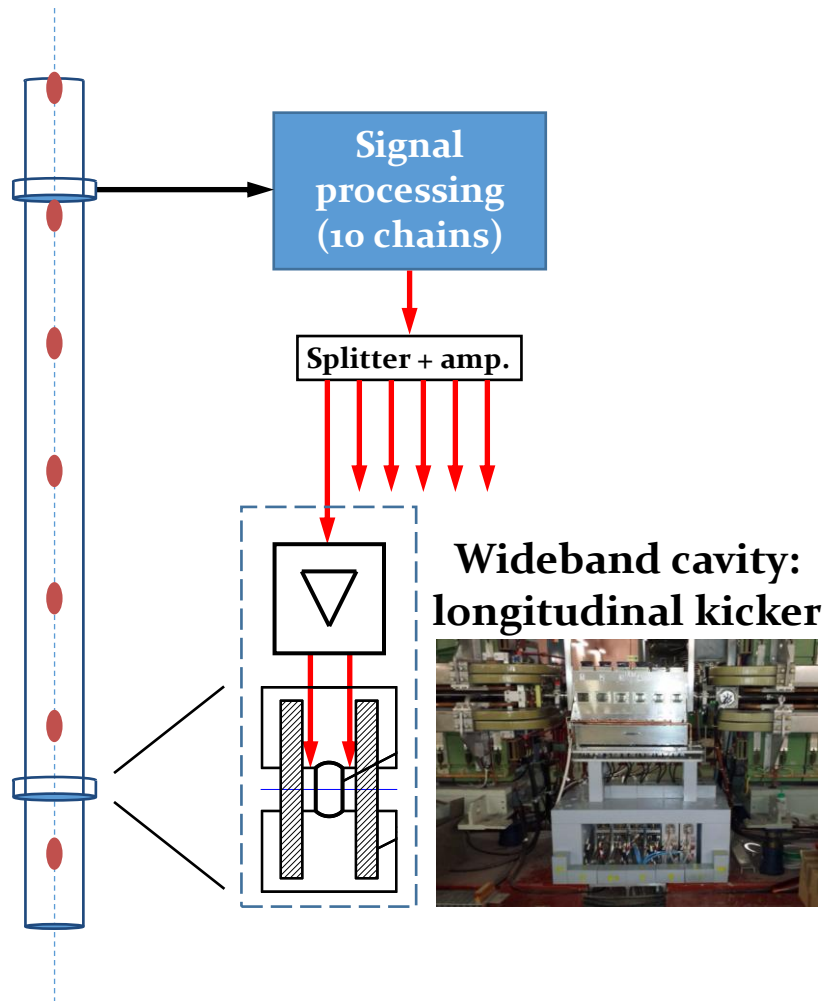
→ Stable beam



- Multiple feedbacks **in parallel**
- Optimum parameters (phase, gain) for each harmonic of  $\omega_{rev}$

# Example: CERN PS coupled-bunch feedback <sup>55</sup>

- Mode-by-mode dipole feedback
- 10 parallel processing chains → stabilize beam for LHC





# Summary

1. **Direct RF feedback**
    - **Globally reduce cavity impedance**
  2. **Long delay feedback**
    - **Reduce impedance at revolution frequency harmonics**
  3. **Global feedback**
    - **Just fix problems of (sometimes) not understood origin**
- **Chose feedback most appropriate to your problem**
    - **Prefer inner layers of feedback onion**
    - **Combination of different RF feedback types**
  - **Delay is principal enemy of almost every RF feedback**
    - **Keep it short, you cannot beat causality!**



# **A big Thank You**

**to all colleagues providing support, material and feedback**

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Giorgia Favia, Javier Galindo, Wolfgang Höfle, Erk Jensen,  
Piotr Kowina, John Molendijk, Damien Perrelet,  
Fumihiko Tamura, Frank Tecker, Dmitry Teytelman,  
Daniel Valuch, Christine Völlinger, Manfred Wendt  
and many more...**

**Thank you very much  
for your attention!**

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- P. Baudrenghien, Low-level RF - Part I: Longitudinal Dynamics and Beam-Based Loops in Synchrotrons, CERN-2011-007, 2011, <http://cds.cern.ch/record/1415913/files/p341.pdf>

# Direct RF feedback on cavity

- You **know** the driving impedance → RF cavity
- You can be **close** to the cavity

Advantages	Disadvantages
<ul style="list-style-type: none"><li>• Shunt impedance reduction of cavity resonance</li><li>• Robust, performance does not depend on beam parameters</li><li>• Excellent transient response</li></ul>	<ul style="list-style-type: none"><li>• Local feedback</li><li>• Amplifier must be close to cavity</li><li>• Feedback system per cavity</li></ul>

# 1-turn delay/multi-harmonic feedback

- You **know** the driving impedance → RF cavity
- You **cannot** be **close** to the cavity

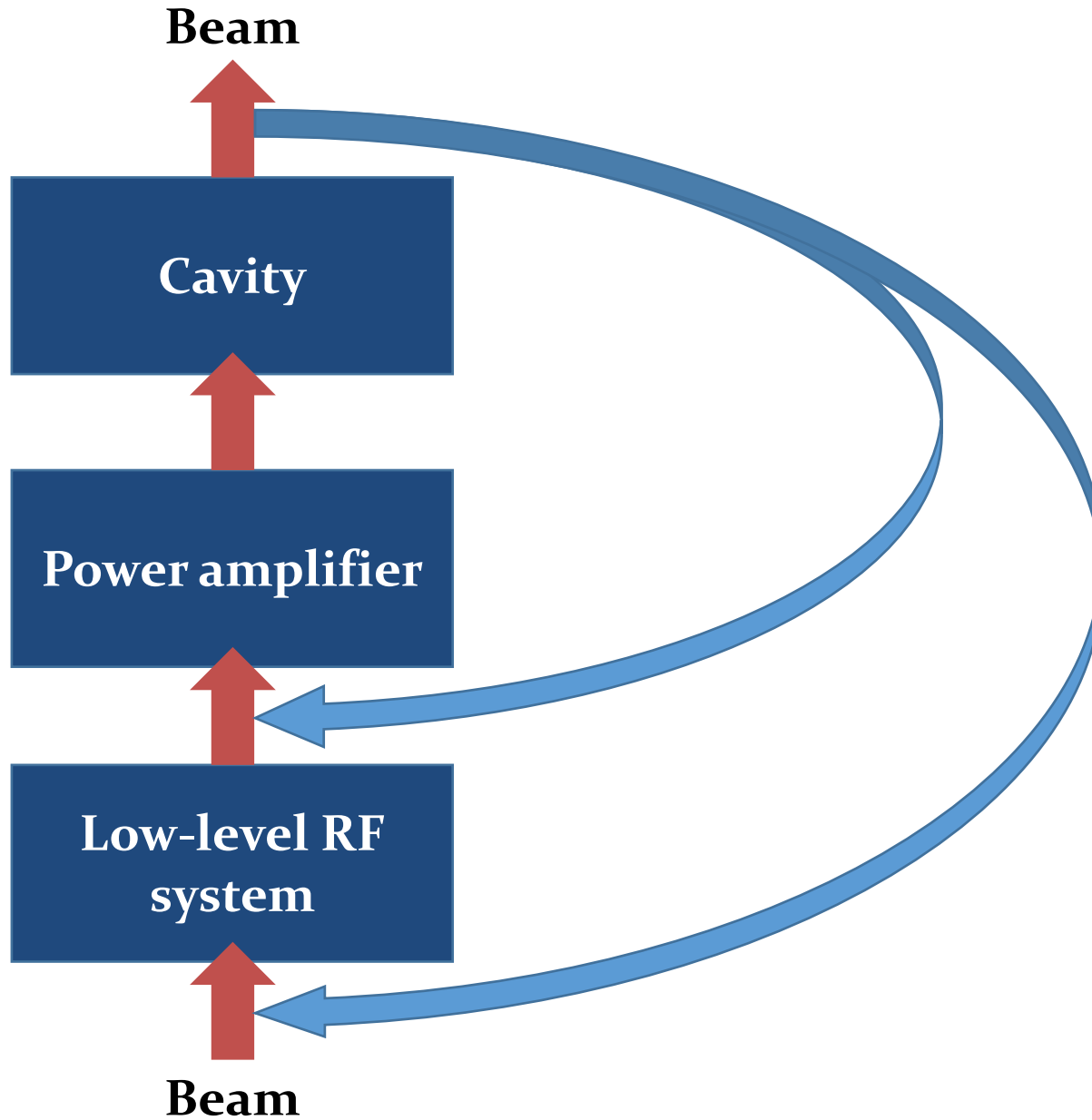
Advantages	Disadvantages
<ul style="list-style-type: none"><li>• Shunt impedance reduction of cavity resonance at revolution frequency harmonics</li><li>• Used in combination with direct feedback</li></ul>	<ul style="list-style-type: none"><li>• Low bandwidth, slow response to transient effects</li><li>• Feedback system per cavity</li></ul>

# Global feedback

- You **do not know** the source of the problem
- You observe and analyse the effect of an instability

Advantages	Disadvantages
<ul style="list-style-type: none"><li>• Globally reduced consequence of instability</li><li>• One feedback sufficient to control instability</li></ul>	<ul style="list-style-type: none"><li>• Treats consequence, not cause of a problem</li><li>• Narrow range of application</li><li>• Dedicated longitudinal kicker</li></ul>

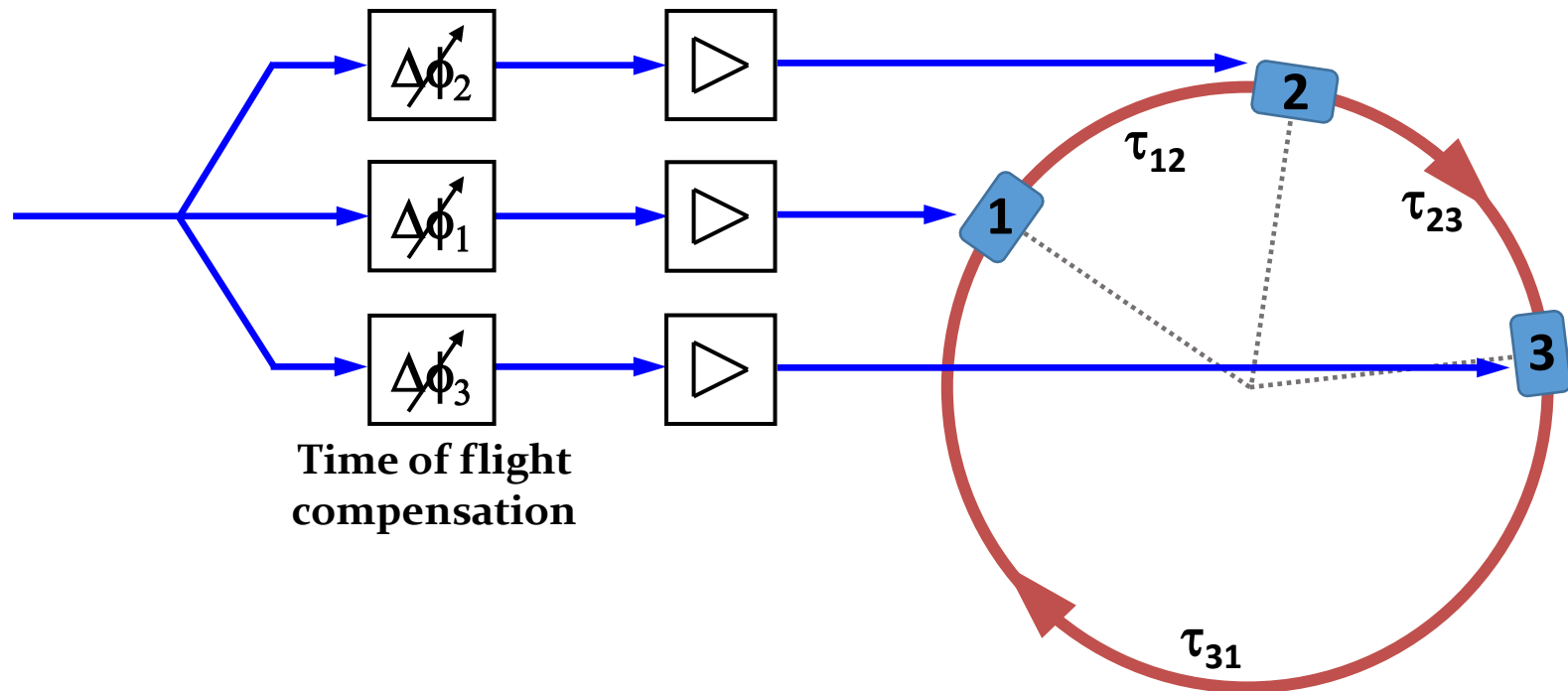
# RF system overview





# Application of global corrections

- **Local** feedbacks → Act on individual RF stations
- **Global** feedbacks → Act on all RF stations simultaneously



- RF distribution to compensate time of flight between stations
- All RF stations applying **correction in unison**

# Frequency and wavelength ranges



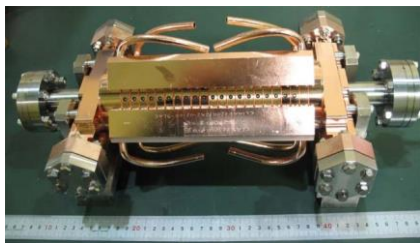
**PS longitudinal damper**



**PS main RF system**



**SPS 200 MHz**



**CLIC 12 GHz**

100 kHz  
3 km

1 MHz  
300 m

10 MHz  
30 m

100 MHz  
3 m

1 GHz  
30 cm

10 GHz  
3 cm

100 GHz  
3 mm



**Long wave**

**Medium/  
short wave**



**VHF**



**Microwave  
links**

