Overview of Plasma Wakefield Accelerators Massimo.Ferrario@LNF.INFN.IT



Spa – 15 November 2024

Livingstone Diagram



Energy of colliders is plotted in terms of the laboratory energy of particles colliding with a proton at rest to reach the same center of mass energy.

VOLUME 43, NUMBER 4

PHYSICAL REVIEW LETTERS

23 JULY 1979

Laser Electron Accelerator

T. Tajima and J. M. Dawson Department of Physics, University of California, Los Angeles, California 90024 (Received 9 March 1979)

An intense electromagnetic pulse can create a weak of plasma oscillations through the action of the nonlinear ponderomotive force. Electrons trapped in the wake can be accelerated to high energy. Existing glass lasers of power density 10^{18} W/cm² shone on plasmas of densities 10^{18} cm⁻³ can yield gigaelectronvolts of electron energy per centimeter of acceleration distance. This acceleration mechanism is demonstrated through computer simulation. Applications to accelerators and pulsers are examined.

VOLUME 54, NUMBER 7

PHYSICAL REVIEW LETTERS

18 FEBRUARY 1985

Acceleration of Electrons by the Interaction of a Bunched Electron Beam with a Plasma

Pisin Chen^(a) Stanford Linear Accelerator Center, Stanford University, Stanford, California 94305

and

J. M. Dawson, Robert W. Huff, and T. Katsouleas Department of Physics, University of California, Los Angeles, California 90024 (Received 20 December 1984)

A new scheme for accelerating electrons, employing a bunched relativistic electron beam in a cold plasma, is analyzed. We show that energy gradients can exceed 1 GeV/m and that the driven electrons can be accelerated from $\gamma_0 mc^2$ to $3\gamma_0 mc^2$ before the driving beam slows down enough to degrade the plasma wave. If the driving electrons are removed before they cause the collapse of the plasma wave, energies up to $4\gamma\delta mc^2$ are possible. A noncollinear injection scheme is suggested in order that the driving electrons can be removed.

Livingstone Diagram with PWFA



Surface charge density

$$\sigma = e n \delta x$$



Surface electric field

$$E_x = -\sigma/\epsilon_0 = -e \, n \, \delta x/\epsilon_0$$

Restoring force

$$m\frac{d^2\delta x}{dt^2} = e E_x = -m \omega_p^2 \delta x$$

Plasma frequency

$$\omega_{\rm p}^{\ 2} = \frac{{\rm n} e^2}{\varepsilon_0 {\rm m}}$$

Plasma oscillations

$$\delta x = (\delta x)_0 \, \cos \left(\omega_p \, t \right)$$

Principle of plasma acceleration



Principle of plasma acceleration

From Maxwell's equations, the electric field in a (positively) charged sphere with uniform density n_i at location **r** is

$$\vec{E}(r) = \frac{q_i n_i}{3\epsilon_0} r$$

The field is **increasing** inside the sphere Let's put some numbers

$$n_i = 10^{16} \text{ cm}^{-3}$$

 $R = 0.5$
 $E \approx 10 \frac{GV}{m}$



























This accelerator fits into a human hair!



Diffraction - Self injection - Dephasing – Depletion



PWFA beam line at SPARC_LAB





Plasma Temperature and Density



Principle of plasma acceleration

Driven by Radiation Pressure





LWFA

driven by high-power lasers. produces high-current e-beam

PWFA

driven by high-current e-beams. produces high-brightness e-beams.

LWFA limitations: Diffraction, Dephasing, Depletion PWFA limitations: Head Erosion, Hose



Linear Wakefields (R. Ruth / P. Chen 1986)













Non Linear Regime – Ellipsoidal Bubble Model



Uniform Cylindrical Beam Model with ionized gas background



 \mathbf{f}_{e} : charge neutralisation factor

$$E_r = \frac{I(1 - f_e)}{2\pi\varepsilon_o a^2 c} r \quad \text{for } r \le a$$
$$E_r = \frac{I(1 - f_e)}{2\pi\varepsilon_o c} \frac{1}{r} \quad \text{for } r > a$$

f_m : current neutralisation factor

$$B_{\vartheta} = \mu_o \frac{I(1 - f_m)}{2\pi a^2} r \text{ for } r \le a$$
$$B_{\vartheta} = \mu_o \frac{I(1 - f_m)}{2\pi a^2} \frac{a^2}{r} \text{ for } r > a$$

Lorentz Force

$$F_r = e\left(E_r - bcB_{\mathcal{J}}\right) = \frac{eE_r}{g^2}\left(1 - g^2f_e + b^2g^2f_m\right)$$

Generalized Envelope Equation

$$\mathcal{S}^{(1)} + \frac{(bg)^{(1)}}{bg} \mathcal{S}^{(1)} + \frac{K}{bg} \mathcal{S} = \frac{2I(1 - g^2 f_e + b^2 g^2 f_m)}{I_A (bg)^3 \mathcal{S}} + \frac{\theta_n^2}{(bg)^2 \mathcal{S}^3}$$

Matching in a Plasma Accelerator with $f_e = n_p/n_e$ and $f_m = 0$

$$\sigma'' + \frac{\gamma'}{\gamma}\sigma' + \frac{k_{ext}^2}{\gamma}\sigma = \frac{2I(1 - \gamma^2 f_e + \gamma^2 f_m)}{I_A \gamma^3 \sigma} + \frac{\varepsilon_n^2}{\gamma^2 \sigma^3}$$

Let consider the charge screening effect of the plasma background with particle density $n_{p_{,}}$ by defining $f_e = n_p/n_e$, where n_e is the bunch particle density and $f_m = 0$. We also do not include any external focusing element so that $k_{ext} = 0$. The envelope equation can be recast as:

$$\sigma'' + \frac{\gamma'}{\gamma}\sigma' + \frac{2In_p}{I_A\gamma n_e\sigma} = \frac{2I}{I_A\gamma^3\sigma} + \frac{\varepsilon_n^2}{\gamma^2\sigma^3}$$

or by recalling the definition of the Alfven current I_A and of the beam current $I=ecn_e\pi\sigma^2$ it can be written in a more familiar form as:



$$\sigma'' + \frac{\gamma'}{\gamma}\sigma' + \frac{k_p^2}{2\gamma}\sigma = \frac{2I}{I_A\gamma^3\sigma} + \frac{\varepsilon_n^2}{\gamma^2\sigma^3}$$



Transverse beam dynamics inside the plasma



Courtesy P. Tomassini

With the typical beam parameters in a plasma accelerator: 1 kA peak current, 1 μ m normalized emittance, injection energy γ_0 =300 and spot size about 5 μ m, the laminarity parameter (43) results to be $\rho < 1$, i.e. the beam is emittance dominated. We have also to neglect the adiabatic damping term, setting $\gamma'=0$ i.e. no acceleration. This approximation is quite strong but it will allow us to find at least a proper matching condition that holds at the entrance of the plasma column. It follows that the envelope equation can be approximated by the reduced expression:











The near future

EUROPEAN PLASMA RESEARCH ACCELERATOR WITH EXCELLENCE IN APPLICATIONS



EUPRAXIA

A New European High-Tech User Facility



FEATURE EOPRAXIA

EUPRAXIA is the first European project that develops a dedicated particle accelerator research infrastructure based on novel plasma acceleration concepts driven by innovative laser and linac technologies.

> Building a facility with very high field plasma accelerators, driven by lasers or beams 1 – 100 GV/m accelerating field

> > Shrink down the facility size Improve Sustainability

Producing particles and photons to support several urgent and timely science cases

Drive short wavelength FEL Pave the way for future Linear Colliders



Surf's up Simulation of electron-driven plasma wakefield acceleration, showing the drive electron beam (orange/purple), the plasm wake (arev) and wakefield-ionised electrons forming a witness beam (orange)

USER FACILITY PLASMA AC

Ralph Assmann, Massimo Ferrario and Carsten Welsch describe the status of the ESFRI project EuPRAXIA, which aims to develop the first dedicated research infrastructure based on novel plasma-acceleration concepts.

nergetic beams of particles are used to explore the This scientific success story has been made possib fundamental forces of nature, produce known and through a continuous cycle of innovation in the physics unknown particles such as the Higgs boson at the and technology of particle accelerators, driven for many LHC, and generate new forms of matter, for example at the decades by exploratory research in nuclear and particle ature FAIR facility. Photon science also relies on particle physics. The invention of radio-frequency (RF) technology earns: electron beams that emit pulses of intense synhrotron light, including soft and hard X-rays, in either tens of MeV per metre. Very-high-energy accelerators were circular or linear machines. Such light sources enable constructed with RF technology, entering the GeV and time-resolved measurements of biological, chemical and finally the TeV energy scales at the Tevatron and the LHC. physical structures on the molecular down to the atomic New collision schemes were developed, for example the cale, allowing a diverse global community of users to mini "beta squeeze" in the 1970s, advancing luminosit nvestigate systems ranging from viruses and bacteria and collision rates by orders of magnitudes. The invention to materials science, planetary science, environmental of stochastic cooling at CERN enabled the discovery of science, nanotechnology and archaeology. Last but not the W and Z bosons 40 years ago least, particle beams for industry and health support many However, intrinsic technological and conceptual limits societal applications ranging from the X-ray inspection mean that the size and cost of RF-based particle accelof cargo containers to food sterilisation, and from chip erators are increasing as researchers seek higher beam Welsch University manufacturing to cancer therapy. energies. Colliders for particle physics have reached a of Liverpool/INFN.

Massimo Ferrario

https://www.eupraxia-facility.org/



FEL is a well established technology

(But a widespread use of FEL is partially limited by its size and costs)

Funded by the European Union



Linac Coherent Light Source (LCLS) Conceptual Design Report - SLAC-R-593 April 2002 UC-414



It's a CHALLENGE: the FEL is extremely sensitive to the beam quality.

 $\begin{array}{c|c} \mbox{Low (geometric) emittances: } \epsilon_{x,y} < \frac{\lambda_0}{4\pi} & \mbox{Low emittances} \\ \mbox{Low relative energy spread } \sigma_{\gamma}: & \sigma_{\gamma} < \frac{1}{2}\rho_{fel} \\ & \mbox{where} & \rho_{fel} = \frac{1}{4\pi} \left[\frac{2\pi^2}{\gamma^3} \left(\lambda_u K \left[JJ \right] \right)^2 \frac{I_{peak}}{\Sigma_e I_A} \right]^{1/3} \\ \mbox{Exponential growth} & \mbox{gain length} & \mbox{saturation} \\ P(z) = \frac{1}{9}P_0 e^{z/L_g} & \mbox{L}_g = \frac{\lambda_u}{4\pi\sqrt{3}\rho_{fel}} & \mbox{P}_F \sim 1.6 \ \rho_{fel}P_{beam} \end{array}$

=> A poor beam quality causes an increase of L_g and a reduction of P_F

Basic beam quality achieved in pilot FEL experiments









- The EuPRAXIA Consortium today: 54 institutes from 18 countries plus CERN
- Included in the ESFRI Road Map
- Efficient fund raising:
- –Preparatory Phase consortium (funding EU, UK, Switzerland, in-kind)
- –Doctoral Network (funding EU, UK, inkind)
- -EuPRAXIA@SPARC_LAB (Italy, in-kind)
- -EuAPS Project (Next Generation EU)





Distributed Research Infrastructure





A large collection of the best European know-hows in accelerators, lasers an plasma technologies

Network organization - Sites (PWFA/LWFA)

- National nodes
- Technology clusters

4 candidates for LWFA:

- CLPU, Salamanca
- CNR-INO, Pisa
- ELI ERIC, Prague
- EPAC-RAL, UK

EUPRAXIA Headquarter and Site 1: EuPRAXIA@SPARC_LAB





- Frascati's future facility
- > 130 M€ invest funding
- Beam-driven plasma accelerator
- Europe`s most compact and most southern FEL
- The world`s most
 compact RF accelerator
 (X band with CERN)

EuPRAXIA@SPARC_LAB



Expected SASE FEL performances

54	Chapter 2. Free Electron Laser design principle				
	Units	Full RF case	Plasma case		
Electron Energy	GeV	1	1		
Bunch Charge	pC	200	30		
Peak Current	kA	2	3		
RMS Energy Spread	%	0.1	1		
RMS Bunch Length	fs	40	4		
RMS matched Bunch Spot	μm	34	34		
RMS norm. Emittance	μm	1	1		
Slice length	μm	0.5	0.45		
Slice Energy Spread	%	0.01	0.1		
Slice norm. Emittance	μm	0.5	0.5		
Undulator Period	mm	15	15		
Undulator Strength K		1.03	1.03		
Undulator Length	m	12	14		
Gain Length	m	0.46	0.5		
Pierce Parameterp	x 10 ⁻³	1.5	1.4		
Radiation Wavelength	nm	3	3		
Undulator matching β_u	m	4.5	4.5		
Saturation Active Length	m	10	11		
Saturation Power	GW	4	5.89		
Energy per pulse	μJ	83.8	11.7		
Photons per pulse	x 10 ¹¹	11	1.5		

Table 2.1: Beam parameters for the EuPRAXIA@SPARC_LAB FEL driven by X-band linac or Plasma acceleration

In the Energy region between Oxygen and Carbon K-edge 2.34 nm - 4.4 nm (530 eV -280 eV) water is almost transparent to radiation while nitrogen and carbon are absorbing (and scattering)



Coherent Imaging of biological samples protein clusters, VIRUSES and cells living in their native state Possibility to study dynamics ~10¹¹ photons/pulse needed Courtesy F. Stellato, UniToV

Single Protein Imaging with hard x-rays



Single Protein Imaging with hard x-rays



Static picture of a macromolecule

- Short wavelength (X-ray)
- High energy per pulse

Required properties

- Ultra-short pulse (few femtoseconds)
- Coherence

Single Protein Imaging



http://lcls.slac.stanford.edu/AnimationViewLCLS.asp

Coulomb Explosion of Lysozyme (50 fs) Single Molecule Imaging with Intense X-rays



Atomic and molecular dynamics occur at the *fsec*-scale

J. Hajdu, Uppsala U.

Plasma collider challenges



HALHF: A Hybrid, Asymmetric, Linear Higgs Factory



The novelty: A multistage plasma-based linac

>Length: 16 PWFA stages (5-m long): ~400 m total length

>Gradient: 6.4 GV/m (in plasma)—1.2 GV/m (average)

- > Efficiency: 38% = 72% depletion, 53% wake extraction
- > No damping ring required due to high-emittance electrons



Number of stages		16
Plasma density	cm^{-3}	1.5×10^{16}
In-plasma acceleration gradient	GV/m	6.4
Average gradient (incl. optics)	GV/m	1.2
Length per stage ^a	m	5
Energy gain per stage ^a	GeV	31.9
Initial injection energy	GeV	5
Driver energy	GeV	31.25
Driver bunch population	10 ¹⁰	2.7
Driver bunch length (rms)	μm	27.6
Driver average beam power	MW	21.4
Driver bunch separation	ns	5
Driver-to-wake efficiency	%	74
Wake-to-beam efficiency	%	53
Driver-to-beam efficiency	%	39
Wall-plug-to-beam efficiency	%	19.5
Cooling req. per stage length	kW/m	100



Simulated with Wake-T

Plasma density: 7 x 10¹⁵ cm⁻³ Driver/witness charge: 4.3/1.6 nC

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Conclusions

- Accelerator-based High Energy Physics will at some point become practically limited by the size and cost of the proposed e⁺e⁻ colliders for the energy frontier.
- Novel Acceleration Techniques and Plasma-based, high gradient accelerators open the realistic vision of very compact accelerators for scientific, commercial and medical applications.
- The R&D now concentrates on beam quality, stability, staging and continuous operation. These are necessary steps towards various technological applications.
- The progress in advanced accelerators benefits from strong synergy with general advances in technology, for example in the laser and/or high gradient RF structures industry.
- A major milestone is an operational, 1 GeV compact accelerator. Challenges in repetition rate and stability must be addressed. This unit could become a stage in a high-energy accelerator..
- PILOT USER FACILITIES Under Construction (EuPRAXIA)



LPAW 2025 – Ischia Island



LPAW 2025 Laser and Plasma Accelerators Workshop 2025 14-18 April 2025, Ischia Island, Italy



https://agenda.infn.it/event/42311/

The Laser and Plasma Accelerators Workshop 2025 (LPAW 2025) will be held at Hotel Continental Ischia, in the Ischia Island (Campania, Italy), from Monday 14 to Friday 18 April 2025.

The Laser and Plasma Accelerators Workshop (LPAW) series is one of the leading workshops in the field of plasma-based acceleration and radiation generation.

The following scientific topics will be the main focus of the conference:

•Plasma-based lepton acceleration (experiments, simulations, theory, diagnostics...).

•Plasma-based ion acceleration (experiments, simulations, theory, diagnostics...).

•Secondary radiation generation and applications (experiments, simulations, theory, diagnostics...).

John Dawson Thesis Prize

"John Dawson Thesis Prize" is awarded on a biannual basis to the best PhD thesis in the area of plasma accelerators driven by laser or particle beams. The prize will be awarded for fundamental (theoretical or experimental) or applied aspects. Each prize winner will receive a certificate of merit, up to 500 Euros, and financial support to attend the "Laser and Plasma Accelerators Workshop," where the prize will be awarded.

Thank for your attention

EuPRAXIA High Brightness Photo-injector with Velocity Bunching







High Quality Electron Beams





Courtesy E. Chiadroni



World's Most Compact RF Linac: X Band



12	20	1 mm ((a))
¹ ¹	10	
E ^{acc} /≺E	30	
ŧ	z [m]	
1.	E.m. design: done	
2.	Thermo-mechanical analysis: done	
3.	Mechanical design: done	Pressure distribution
4.	Vacuum calculations: done	LL47
5.	Dark current simulations: done	1,6-12 0, 15 30 45 60 75 90 Z [cm]
6.	Waveguide distribution simulation with attenuation calculations: <i>done</i>	The second secon

-q=1e-1 -q=1e-12

	Value	
PARAMETER	with linear	w/o
	tapering	tapering
Frequency [GHz]	11.9942	
Average acc. gradient [MV/m]	60	
Structures per module	2	
Iris radius a [mm]	3.85-3.15	3.5
Tapering angle [deg]	0.04	0
Struct. length L _s act. Length (flange-to-flange) [m]	0.94 (1.05)	
No. of cells	112	
Shunt impedance R [MΩ/m]	93-107	100
Effective shunt Imp. R _{sh eff} [MΩ/m]	350	347
Peak input power per structure [MW]	70	
Input power averaged over the pulse [MW]	51	
Average dissipated power [kW]	1	
P _{out} /P _{in} [%]	25	
Filling time [ns]	130	
Peak Modified Poynting Vector [W/µm ²]	3.6	4.3
Peak surface electric field [MV/m]	160	190
Unloaded SLED/BOC Q-factor Q ₀	150000	
External SLED/BOC Q-factor Q _E	21300	20700
Required Kly power per module [MW]	20	
RF pulse [µs]	1.5	
Rep. Rate [Hz]	100	





Courtesy D. Alesini

Plasma Module







- 40 cm long capillary $\rightarrow 1^{st}$ prototype for the EuPRAXIA facility
 - Made with special junction to allow negligible gas leaks (<10⁻¹⁰ mbar)
- Operating conditions
 - 1 Hz repetition rate (to be increased up to 100 Hz)
 - 10 kV 380 A minimum values for ionization
 - 6 inlets for gas injection. Electro-valve aperture time 8-12 ms



A. Biagioni, V. Lollo



Courtesy A. Biagioni, R. Pompili



Radiation Generation: FEL





Courtesy L. Giannessi

Principle of plasma acceleration

Driven by Radiation Pressure



LWFA limitations: Diffraction, Dephasing, Depletion PWFA limitations: Head Erosion, Hose