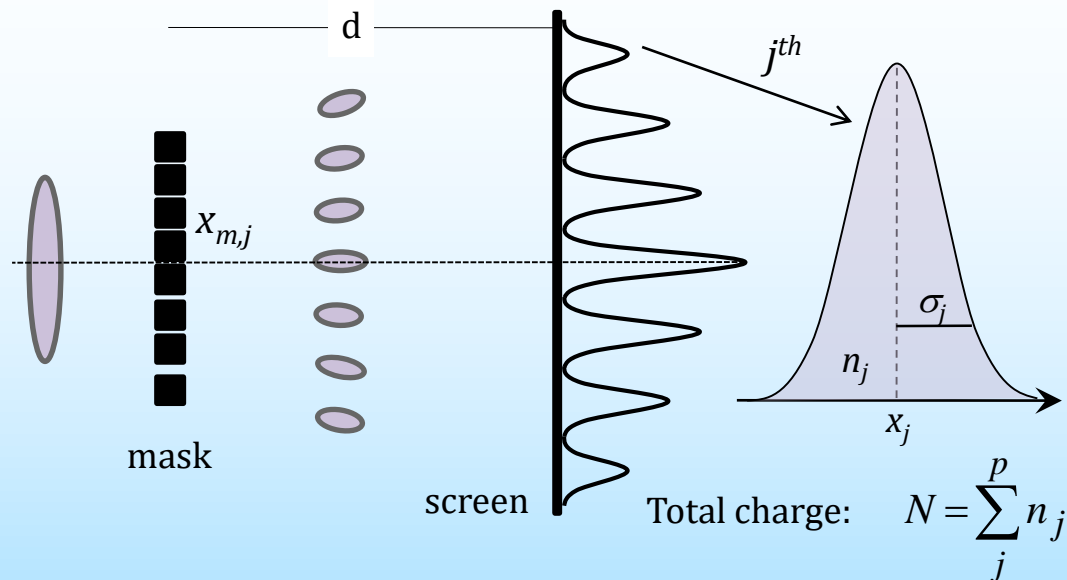


# Laboratory Session on Pepperpot Emittance Measurements

**Ref 1: Emittance Formula for Slits and Pepper-pot  
Measurement, Min Zhang, FERMILAB-TM-1988**

Your tasks in green frames



### In all beamlets:

Mean position:

$$\bar{x} = 1/N \sum_j n_j x_{m,j} = \langle x \rangle$$

Mean divergence:

$$\bar{x}' = 1/N \sum_j n_j \bar{x}'_j = \langle x' \rangle$$

### In $j^{\text{th}}$ beamlet:

Mean divergence:

$$\bar{x}'_j = 1/n_j \sum x'_{ij}$$

rms divergence:

$$\sigma_{j,x'} = \frac{\sigma_j}{d}$$

$$\varepsilon_{rms} = \sqrt{\langle x^2 \rangle \langle x'^2 \rangle - \langle xx' \rangle^2}$$

$$\langle x^2 \rangle = \frac{1}{N^2} \sum_{j=1}^p n_j (x_{m,j} - \bar{x})^2$$

$$\langle x'^2 \rangle = \frac{1}{N^2} \sum_{j=1}^p n_j \left[ \left( \frac{\sigma_j}{d} \right)^2 + (x_{m,j} - \bar{x})^2 \right]$$

$$\langle xx' \rangle^2 = \frac{1}{N^2} \left[ \sum_{j=1}^p n_j x_j \bar{x}'_j - N \bar{x} \bar{x}' \right]^2$$

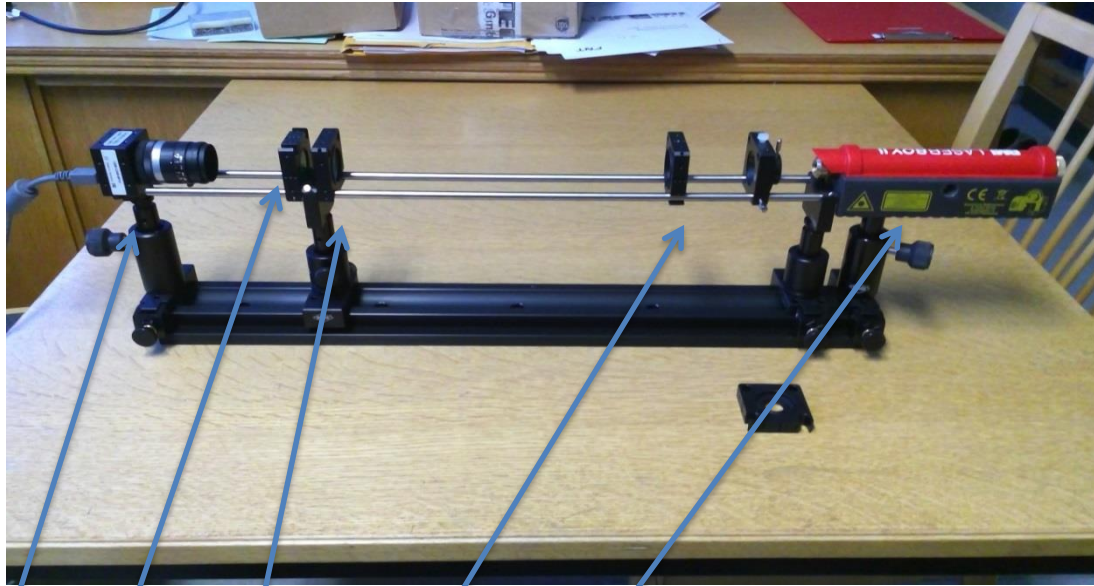
with

$$\sigma_j \equiv \sqrt{\frac{1}{n_j} \sum_{i=1}^{n_j} (X_{ji} - \bar{X}_j)^2},$$

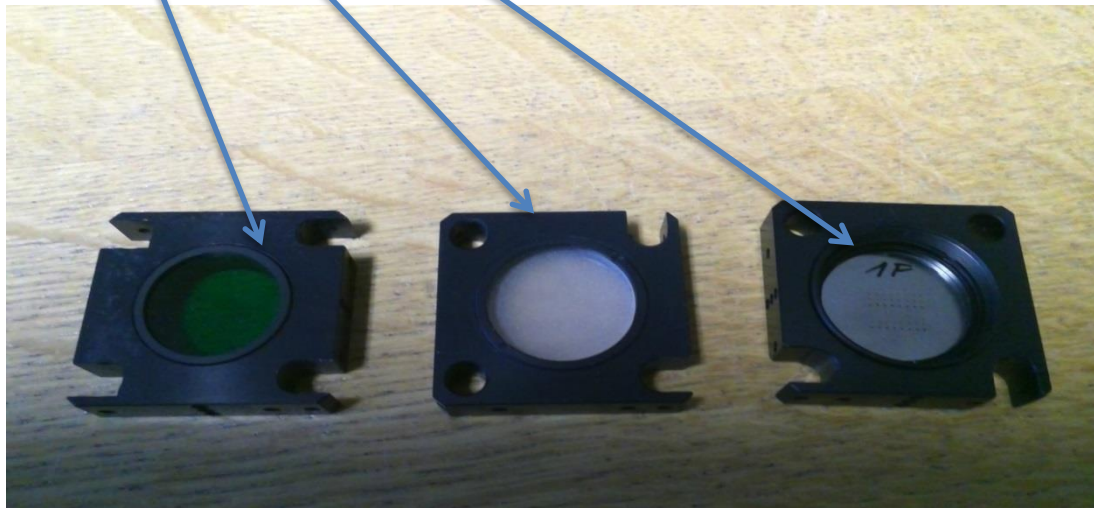
which is the rms spot size of  $j$ -th beamlet on screen.

$p$  = number of slits,  $x_{m,j}$  =  $j$ -th slit position,  $N$  = all particles behind the slits  
 $n_j$  = number of particles passing through slit (weight of spot intensity)

# Pepperpot Emittance Measurement

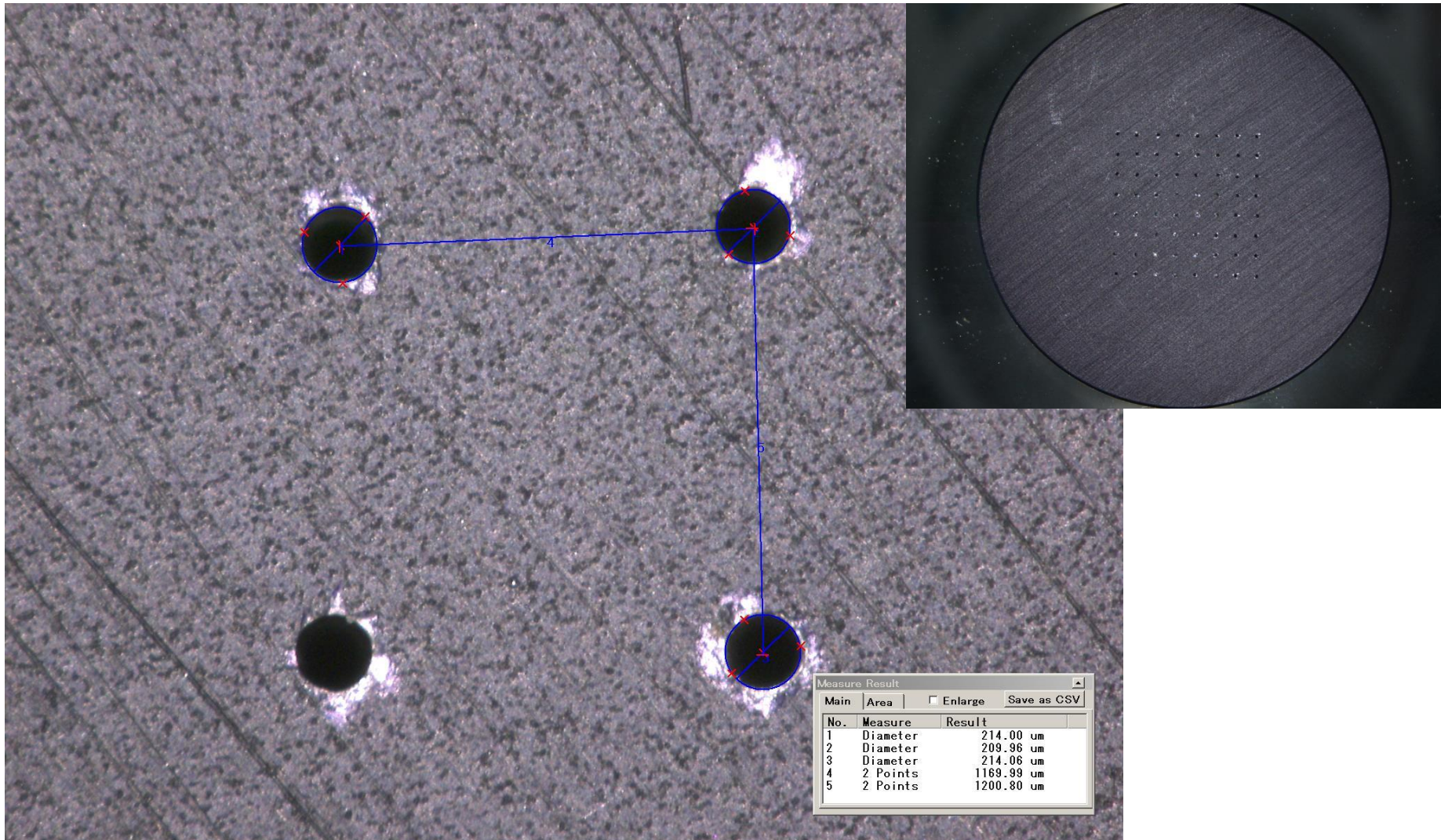


Optical bench with: Camera, Filter, Screen, Pepperpot plate, Laser, Data acquisition (CCD readout), Data analysis (ImageJ), Evaluation program (Excel)





# Pepperpot Emittance Measurement



There are 8 rows with 8 holes each. The holes have a diameter of  $210 \mu\text{m}$ . The horizontal distance is  $1170 \mu\text{m}$  in each row.

# Pepperpot Measurement

---

Only the evaluation of the horizontal phase plane is implemented but... on an optical system horizontal and vertical phase space is symmetric.

Steps to be performed:

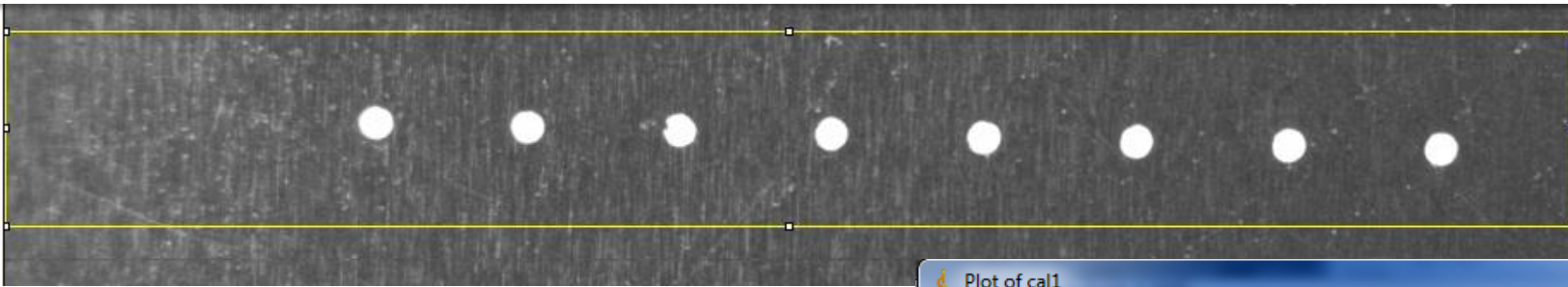
1. We will use a series of horizontal holes calculating the projection of the image to the horizontal axis. Therefore ...  
Make sure all 8 holes are visible, almost aligned and are on a horizontal line (use 2048x1536 resolution)
2. Measure the distance between the holes (in pixels) and calculate the scaling factor  $s$  [pixels/mm]  
To do this: Replace the screen with the pepperpot plate. After this measurement keep the distance screen-camera constant.  
Save the image as an .jpg file
3. Take the pepperpot image on the screen (make sure the camera focuses on the screen), save it and calculate the emittance.

**In more details:** Your tasks in green frames

# Camera Calibration

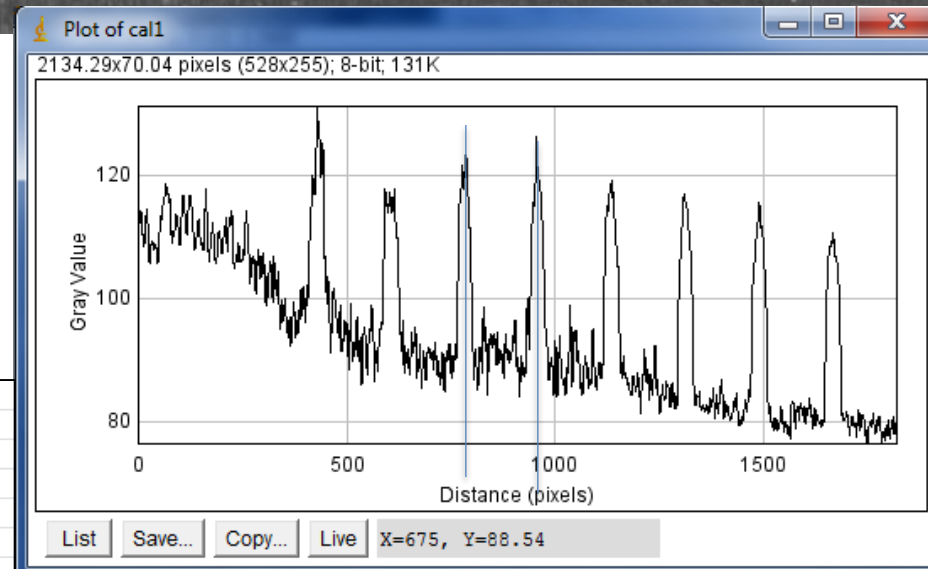
Check: Do not saturate (255)

- To 1) and 2): **Camera Calibration!**: Replace the screen with the pepperpot plate. The distance of the holes (1.170 mm) is known and can be used for calibration. Focus the camera and take a picture of all 8 holes in the middle of the picture and measure the distance in pixels. Hint: Use a white paper to illuminate the holes from the back. Keep the filter in. Use the 4<sup>th</sup> line.



Use ImageJ to open the picture, define an ROI (up to the left side =0!!!) and measure the distance between 2 holes. Enter this number into the pre-prepared Excel sheet "Pepperpot\_calc.xlsx" at c1 and c2. The calibration will be calculated automatically (yellow field).

|                             |                      |                            |        |
|-----------------------------|----------------------|----------------------------|--------|
| For Calibration (pixels/mm) |                      |                            |        |
| dist. Of holes:             | 1.202 mm             | dist. Pepperpot-Screen L = | 188 mm |
| c1=                         | 425 pixel            |                            |        |
| c2=                         | 673 pixel            |                            |        |
| cal:                        | 206.3227953 pixel/mm |                            |        |



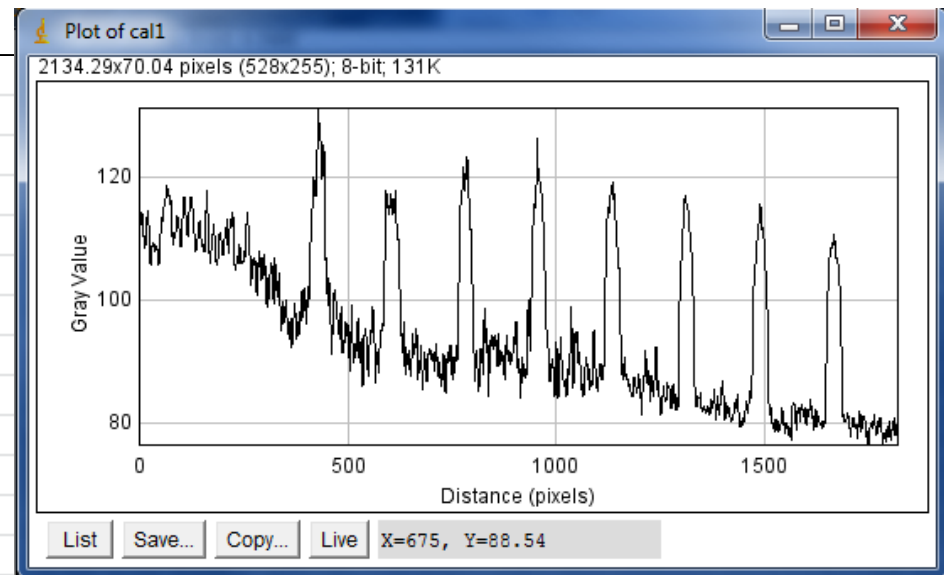
# Camera Calibration

Check: Do not saturate (255)

- Use the picture also to define the positions of the holes:

Measure the x coordinate in Pixels of the center of each hole. Enter this number into the Excel sheet at xs1 to xs8.

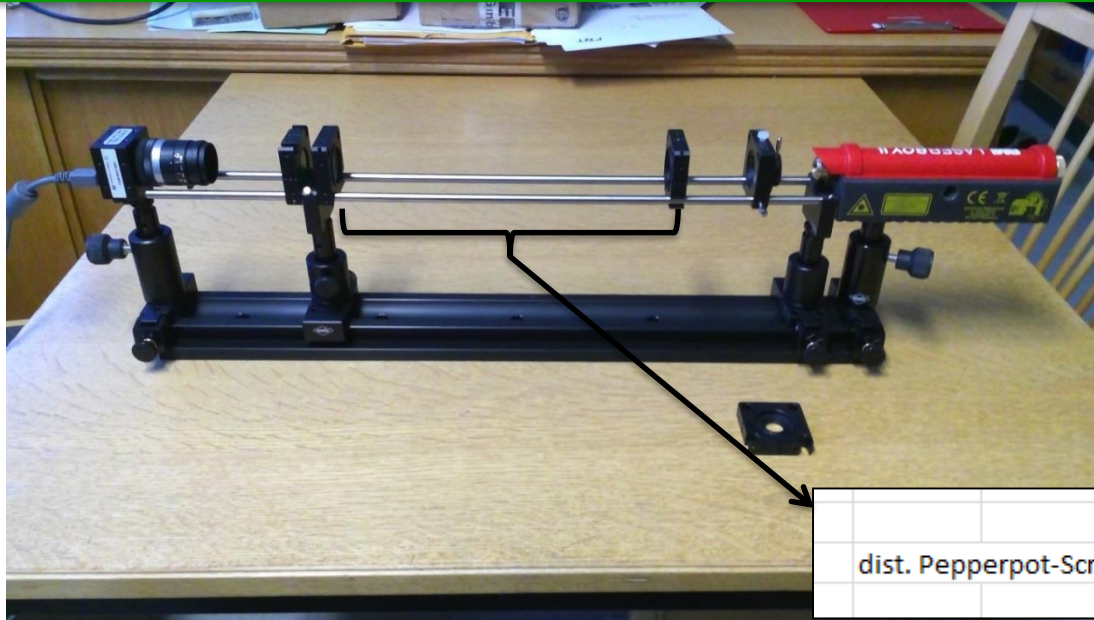
| For Calibration (pixels/mm)                  |             |          |
|--|-------------|----------|
| dist. Of holes:                              | 1.170       | mm       |
| c1=  | 425         | pixel    |
| c2=  | 673         | pixel    |
| cal:   | 206.3227953 | pixel/mm |
| Center Position of hole images of Pepperpot: |             |          |
| xs1  | 460         | pixel    |
| xs2  | 702         | pixel    |
| xs3  | 950         | pixel    |
| xs4  | 1192        | pixel    |
| xs5  | 1428        | pixel    |
| xs6  | 1670        | pixel    |
| xs7  | 1906        | pixel    |
| xs8  | 2160        | pixel    |





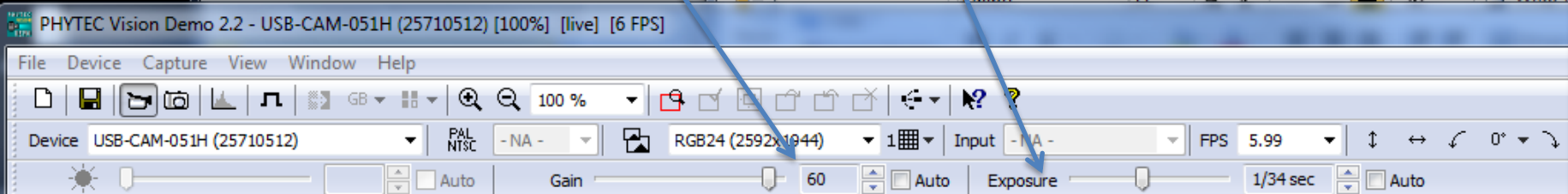
# Camera Calibration

Check: Do not saturate (255)



|                          |          |
|--------------------------|----------|
| dist. Pepperpot-Screen L | 222.8 mm |
|--------------------------|----------|

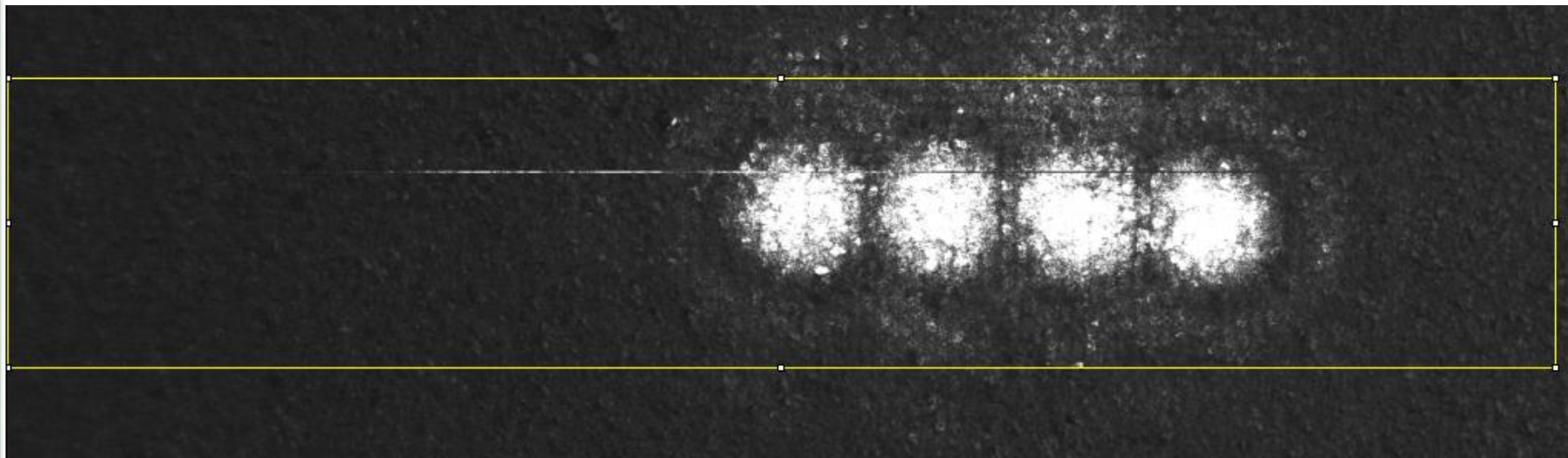
Now put the screen at the **exact location** of the pepperpot (keep camera focus, etc.) and put the pepperpot between the aperture and screen, so that the images of the holes **do not overlap**. Measure the distance L between pepperpot and screen and enter it at L in the Excel sheet. Switch on the laser. Ensure that the one of the rows used for calibration is now illuminated (at least 4 holes should be visible) by the laser and projected on the screen. Ensure that no saturation exist, in case adjust gain and/or exposure time of the camera. Save the picture, that is your measurement!



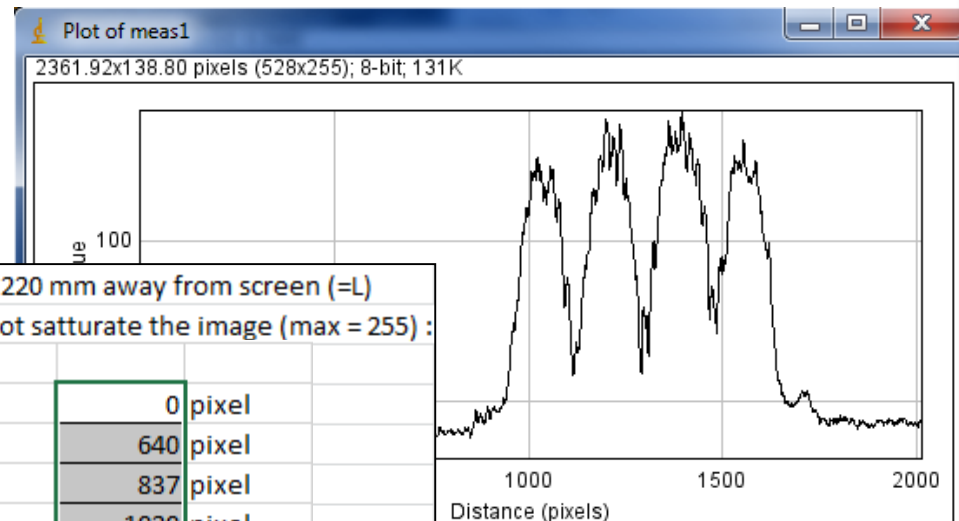


# Experiment

Check: Do not saturate (255)



That is your measurement! Open the picture in ImageJ and define ROI like before (left border is 0). Plot the profile and measure the amplitude and the center position of each visible hole and enter it into Excel as n1-n8 and X1-X8, zeros for holes not visible.



Now put screen on exact position of pepperpot and the pepperpot about 220 mm away from screen (=L)

Measure the intensity and center and RMS of each hole distribution (do not saturate the image (max = 255) :

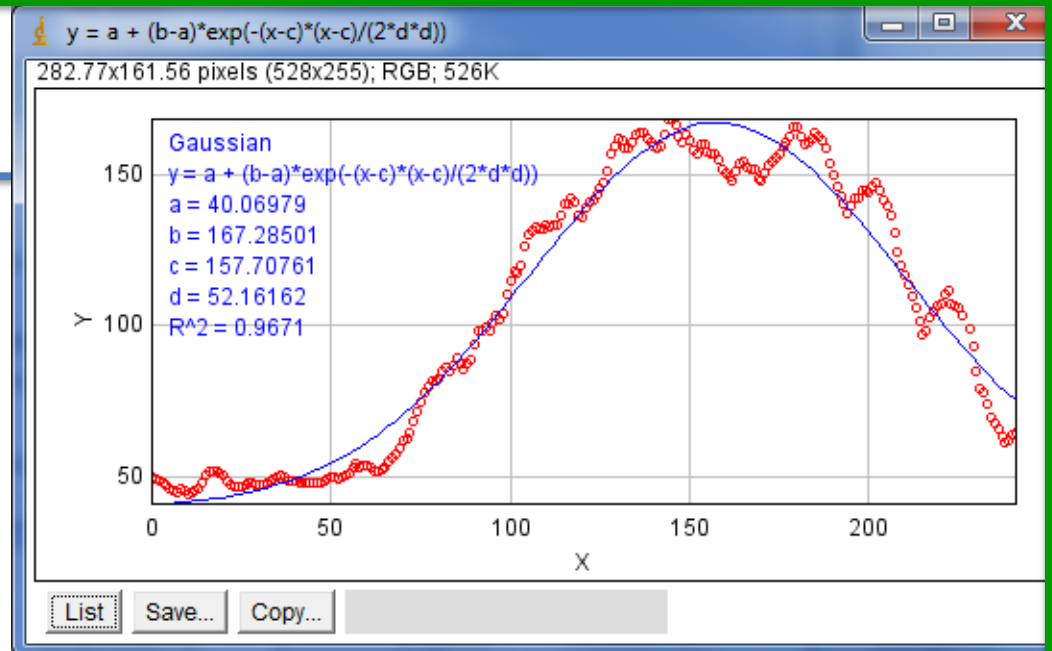
|              |     |          |              |            |  |
|--------------|-----|----------|--------------|------------|--|
| offset       | 15  |          |              |            |  |
| Amplitude n1 | 15  | 0 bits   | Position X1= | 0 pixel    |  |
| Amplitude n2 | 22  | 7 bits   | Position X1= | 640 pixel  |  |
| Amplitude n3 | 122 | 107 bits | Position X1= | 837 pixel  |  |
| Amplitude n4 | 154 | 139 bits | Position X1= | 1020 pixel |  |
| Amplitude n5 | 120 | 105 bits | Position X1= | 1206 pixel |  |
| Amplitude n6 | 115 | 100 bits | Position X1= | 1385 pixel |  |
| Amplitude n7 | 17  | 2 bits   | Position X1= | 1542 pixel |  |
| Amplitude n8 | 15  | 0 bits   | Position X1= | 0 pixel    |  |
| Sum N =      |     | 460 bits |              |            |  |

# Experiment

Now we need the width  $\sigma$  of each hole image. One can do it by hand ( $\sigma = \text{FWHM}/2.36$ ) or can use the fitting algorithm of ImageJ: **See ImageJ**

## Introduction.

Enter each RMS value in the Excel table at RMS1-RMS8. Now Excel calculates  $\langle x \rangle$ ,  $\langle x' \rangle$ ,  $\langle x^2 \rangle$ ,  $\langle x'^2 \rangle$ ,  $\langle xx' \rangle$  and with  $\varepsilon^2 = \langle x^2 \rangle \langle x'^2 \rangle - \langle xx' \rangle^2$  the emittance. It follows the formalism of Ref 1. The result should be a around some  $10^{-6}$  rad.



Now put screen on exact position of pepperpot and the pepperpot about 220 mm away from screen (=L)  
Measure the intensity, offset and center and RMS of each hole distribution (do not saturate the image (max = 255)) :

|              |     |          |              |            |      |          |  |  |
|--------------|-----|----------|--------------|------------|------|----------|--|--|
| offset       | 15  |          |              |            |      |          |  |  |
| Amplitude n1 | 15  | 0 bits   | Position X1= | 0 pixel    | RMS1 | 0 pixel  |  |  |
| Amplitude n2 | 22  | 7 bits   | Position X1= | 640 pixel  | RMS2 | 70 pixel |  |  |
| Amplitude n3 | 122 | 107 bits | Position X1= | 837 pixel  | RMS3 | 48 pixel |  |  |
| Amplitude n4 | 154 | 139 bits | Position X1= | 1020 pixel | RMS4 | 46 pixel |  |  |
| Amplitude n5 | 120 | 105 bits | Position X1= | 1206 pixel | RMS5 | 44 pixel |  |  |
| Amplitude n6 | 115 | 100 bits | Position X1= | 1385 pixel | RMS6 | 46 pixel |  |  |
| Amplitude n7 | 17  | 2 bits   | Position X1= | 1630 pixel | RMS7 | 56 pixel |  |  |
| Amplitude n8 | 15  | 0 bits   | Position X1= | 0 pixel    | RMS8 | 0 pixel  |  |  |
| Sum N =      |     | 460 bits |              |            |      |          |  |  |

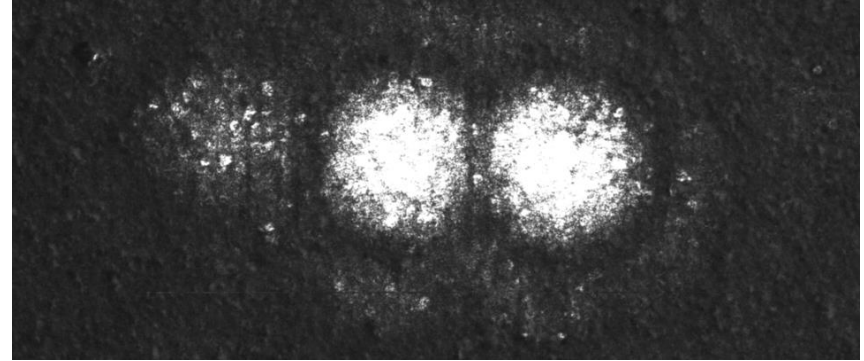
|     |                         |             |             |                 |  |
|-----|-------------------------|-------------|-------------|-----------------|--|
| 99  |                         |             |             |                 |  |
| 100 | $\langle xx' \rangle =$ | -0.00029563 |             |                 |  |
| 101 |                         |             |             |                 |  |
| 102 |                         |             |             |                 |  |
| 103 | Emittance^2 =           | 9.16246E-07 | Emittance = | 0.000957 mm rad |  |
| 104 |                         |             |             | 9.57E-07 rad    |  |

$$\varepsilon_r^2 = \langle x^2 \rangle \langle x'^2 \rangle - \langle xx' \rangle^2$$

# Experiment

Check: Do not saturate (255)

Try to reduce the dimension of the Laser beam by closing the aperture. What happened to the emittance?



|              |     |      |              |      |       |      |      |       |
|--------------|-----|------|--------------|------|-------|------|------|-------|
| Amplitude n1 | 0   | bits | Position X1= | 0    | pixel | RMS1 | 0    | pixel |
| Amplitude n2 | 0   | bits | Position X1= | 0    | pixel | RMS2 | 0    | pixel |
| Amplitude n3 | 0   | bits | Position X1= | 0    | pixel | RMS3 | 0    | pixel |
| Amplitude n4 | 164 | bits | Position X1= | 1219 | pixel | RMS4 | 32.2 | pixel |
| Amplitude n5 | 165 | bits | Position X1= | 1460 | pixel | RMS5 | 29.7 | pixel |
| Amplitude n6 | 0   | bits | Position X1= | 0    | pixel | RMS6 | 0    | pixel |
| Amplitude n7 | 0   | bits | Position X1= | 0    | pixel | RMS7 | 0    | pixel |
| Amplitude n8 | 0   | bits | Position X1= | 0    | pixel | RMS8 | 0    | pixel |
| Sum N =      | 329 | bits |              |      |       |      |      |       |

# Introduction of readout software

- PHYTEC Vision Demo 2.2 for camera readout
- ImageJ for Data treatment

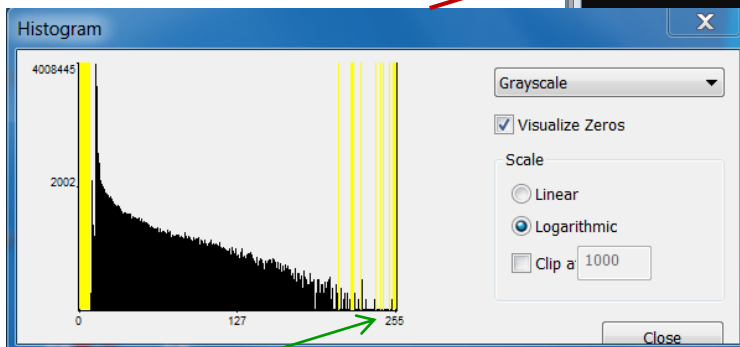


# CCD Readout: Introduction

● readout program

PHYTEC Vision Demo 2.2

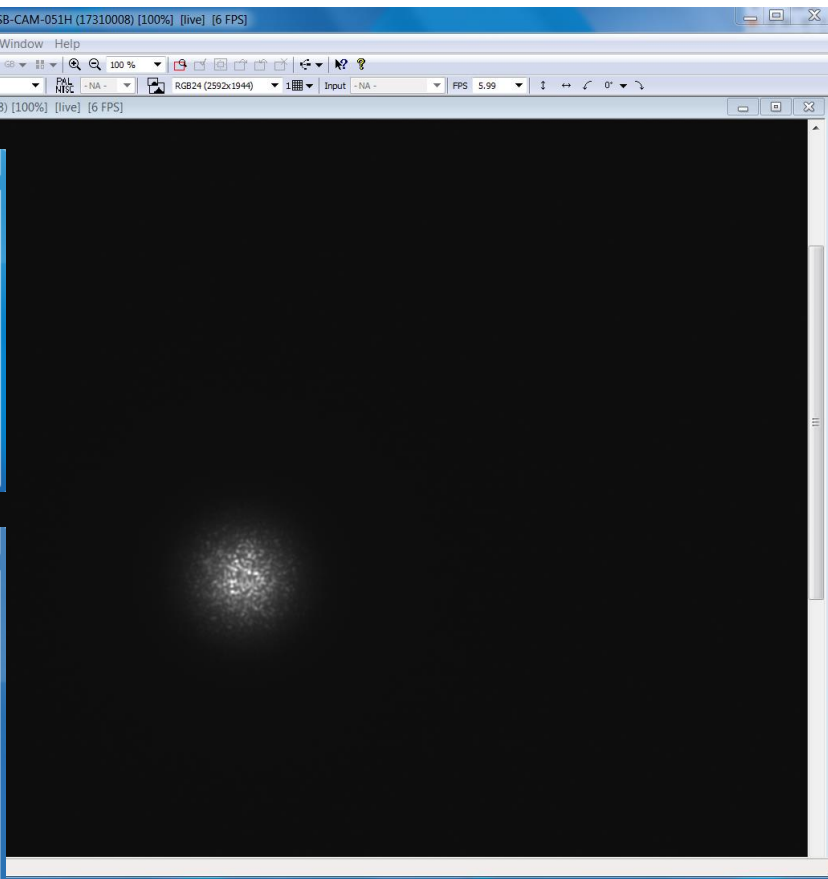
▶ histogram of grey values



The Device Properties window for USB-CAM-051H shows the following settings:

| Parameter      | Value      | Mode |
|----------------|------------|------|
| Gain           | 4          | Auto |
| Exposure       | 1/139 sec  | Auto |
| Auto Reference | 43         |      |
| Auto Max Value | 30.000 sec | Auto |

**Check always:  
Do not saturate  
(255)**



▶ CCD control parameters

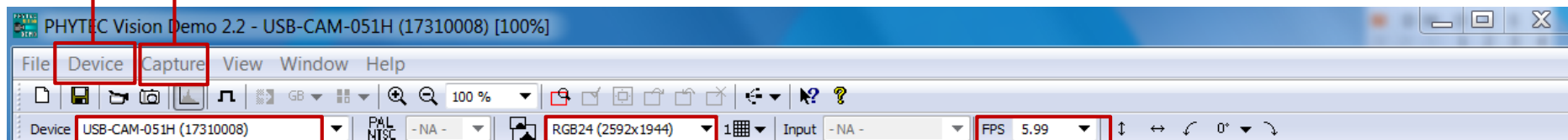
→ Device → Properties

# CCD Readout: Introduction

Start/Stop acquisition → Device → Live (Shortcut: Ctrl + L)

CCD control parameters → Device → Properties

Save image → Capture → Save Image (Shortcut: Ctrl + U): save as Jpeg images



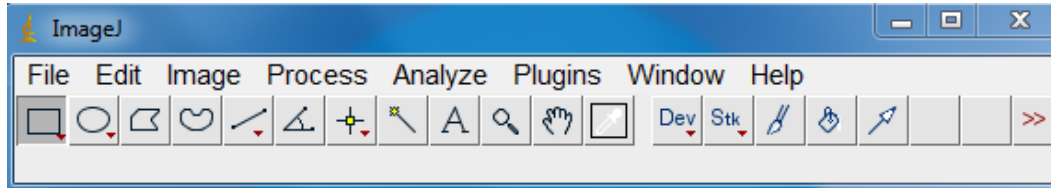
CCD type

readout format  
(RGB, 2592 x 1944 pixel)  
Use 1920 x 1080

readout rate  
(5.99 frames per  
second)

# ImageJ: Introduction

- press icon → access to start panel

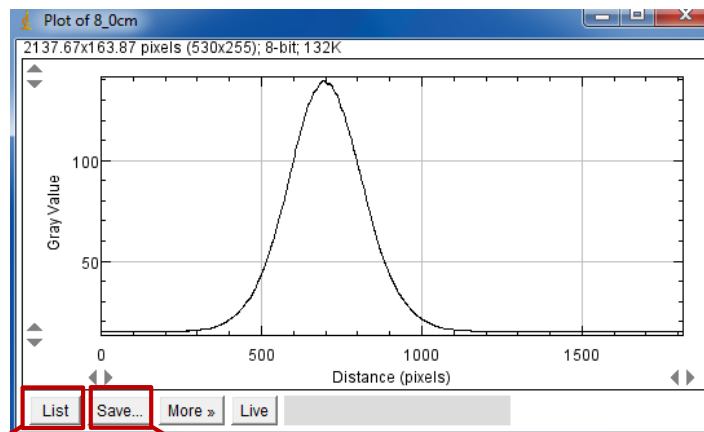


- load image file → File → Open (Shortcut: Ctrl + O)

- select ROI: in start panel: select left button (below "File"), usually already pre-selected  
then with left mouse button: draw rectangular ROI



- plot horizontal projection → Analyze → Plot Profile (Shortcut: Ctrl + k)

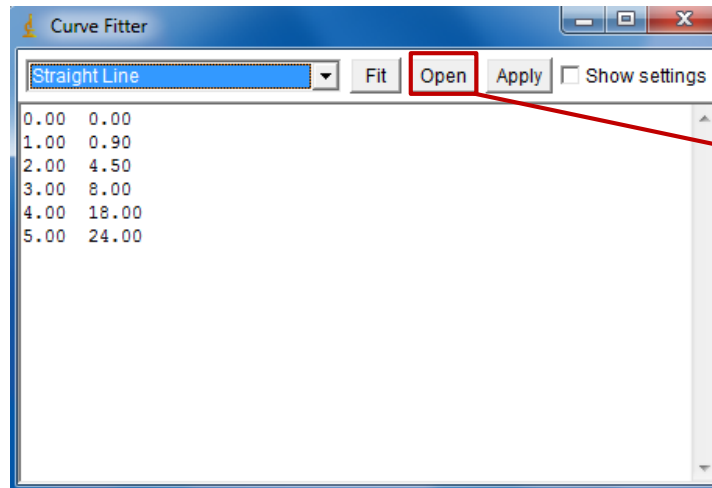


- save data → list data points → save data as .csv file (required for profile fitting)

# ImageJ: Introduction

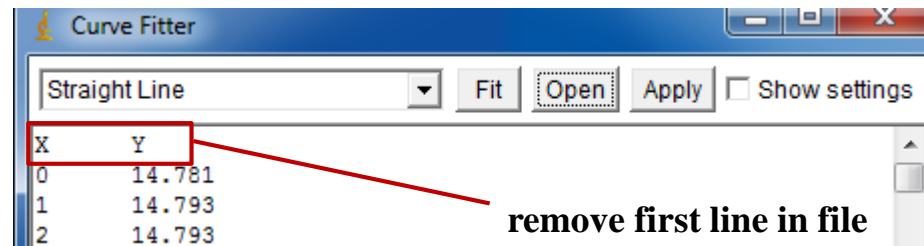
● **profile fitting** → Analyze → Tools → Curve Fitting...

➤ load profile data:



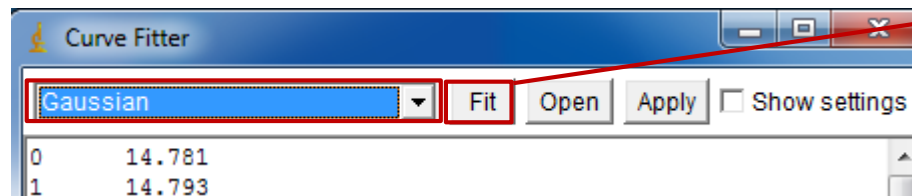
load .csv data file

➤ delete bad data:



remove first line in file

➤ select fit function:



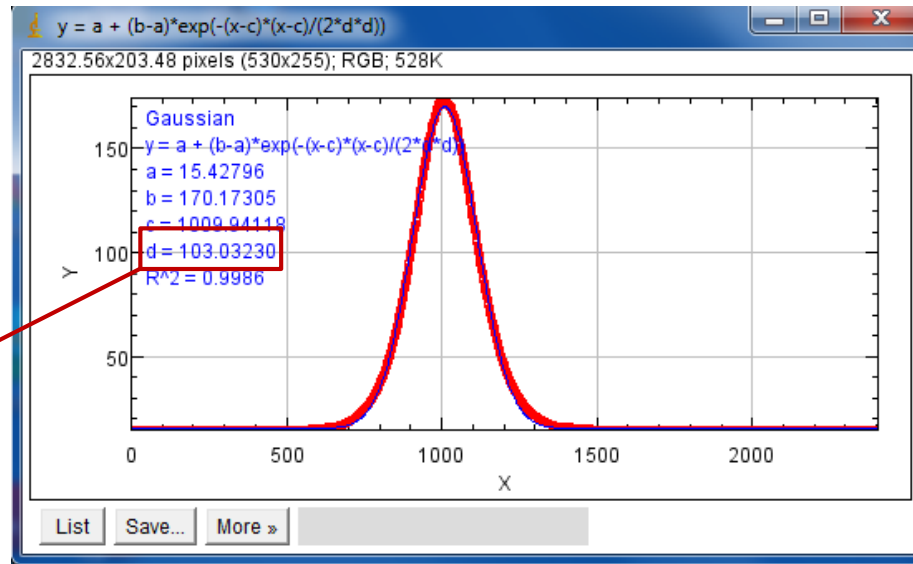
fit profile data

$$y = a + (b - a) \cdot e^{-\frac{(x-c)^2}{2d^2}}$$



# ImageJ: Introduction

➤ fit results:



**1  $\sigma$ -width (in pixel)**

● additional data fitting

- create data file → e.g. Excel or simple ASCII text file with Notepad
- repeat fitting as described before

# Parameters

## ● CCD

### ➤ Phytec USB-CAM 051H

|                        |  |                              |                     |                              |
|------------------------|--|------------------------------|---------------------|------------------------------|
| <b>Resolution</b>      | 2592 x 1944 (5 MPix), 2048 x 1536 (3,1MPix),<br>1600 x 1200 (2MPix), 1280 x 960 (1,2MPix)<br>1024 x 768 (0,8MPix), 640 x 480 (VGA) |                              |                     |                              |
| <b>Model</b>           | <b>USB-CAM-051H</b>  | <b>USB-CAM-151H</b>          | <b>USB-CAM-052H</b> | <b>USB-CAM-152H</b>          |
| color / monochrom      | monochrom  |                              | color               |                              |
| Sensor Format          | 1/2,5"   |                              |                     |                              |
| Image Sensor           | Aptina MT9P031, CMOS   |                              |                     |                              |
| Pixel Size             | 2,2 µm x 2,2 µm  |                              |                     |                              |
| Color format           | Y8   | RGB32, RGGB (Raw)            |                     |                              |
| Lens Holder            | C / CS – Mount   |                              |                     |                              |
| fps                    | 6 fps to 52 fps  |                              |                     |                              |
| Dynamic Range          | 8 bit  |                              |                     |                              |
| Shutter                | Rolling  |                              |                     |                              |
| Light sensitivity      | 1,4 V/lux-sec  |                              |                     |                              |
| Interface              | USB 2.0 High Speed   |                              |                     |                              |
| Exposure time          | 1/10.000 s to 30 s   |                              |                     |                              |
| Gain                   | 0 dB to 18 dB  |                              |                     |                              |
| White Balance          | -  | -6 dB bis +6 dB              |                     |                              |
| Power supply           | 4,5 V bis 5,5V DC  |                              |                     |                              |
| Power Consumption      | Circa 250 mA bei 5V  |                              |                     |                              |
| Feature (optional)     | -  | ext. Trigger, Digital-Output | -                   | ext. Trigger, Digital-Output |
| Temperature range      | -5°C bis +45°C   |                              |                     |                              |
| Dimensions (B x L x H) | 36 mm x 36 mm x 25 mm  |                              |                     |                              |
| Fixing                 | 1/4" and M6x8 on all sides   |                              |                     |                              |
| Weight                 | 70 g   |                              |                     |                              |
| Connection             | USB Mini-B   |                              |                     |                              |
| Feature- Connection    | -  | Hirose HR10A-7R-4P           | -                   | Hirose HR10A-7R-4P           |

## ● screen

➤ **material:** Quarz scatter disk

## ● calibration target

➤ **spacing:** 1.202 mm

## ● Laser: LaserBoyII

### BMI Bayerische Laserboy II Wasserwaage 649 015

#### Allgemeine Informationen

|                    |                |
|--------------------|----------------|
| Artikelnummer      | ET1117000      |
| EAN                | 4007368050049  |
| Hersteller         | BMI Bayerische |
| Hersteller-ArtNr   | 649 015        |
| Hersteller-Typ     | 649 015        |
| Verpackungseinheit | 1 Stück        |
| Artikelklasse      | Messlaser      |



#### Technische Informationen

|                          |     |
|--------------------------|-----|
| Länge der Signalstrecke  | 30m |
| Laserklasse              |     |
| Sichtbare Signalstrecke  |     |
| Rotierende Signalstrecke |     |

BMI Bayerische Laserboy II Wasserwaage 649 015 Länge der Signalstrecke 30m, Laserklasse 2, Sichtbare Signalstrecke,