Beam Emittance by QP Scan Method

Task: Measure the Emittance of the Laser Beam

Your tasks in green frames

Introduction

Quadrupole scan method:

If β is known unambiguously as in a circular machine, then a single profile measurement determines ϵ by

 $\sigma_y^2 = \epsilon \beta_y$.

But it is not easy to be sure in a transfer line which β to use, or rather, whether the beam that has been measured is matched to the β -values used for the line. This problem can be resolved by using a single quadrupole scan system consists of a quadrupole magnet and a drift space s (Fig. 1). The transformation matrix M of this system for the Y direction can be obtained Using a thin-lens approximation for the quadrupole with K=±1/f, where f is the focusing strength of the quadrupole (- for focusing and + for defocusing)



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Introduction of σ -Matrix (see for example: K. Wille; Physik der Teilchenbeschleuniger, Teubner)

$$\sigma = \begin{pmatrix} \sigma_{11} & \sigma_{12} \\ \sigma_{21} & \sigma_{22} \end{pmatrix} = \begin{pmatrix} \sigma_{y}^{2} & \sigma_{yy'} \\ \sigma_{yy'} & \sigma_{y'}^{2} \end{pmatrix} = \varepsilon_{rms} \begin{pmatrix} \beta & -\alpha \\ -\alpha & \gamma \end{pmatrix} = \sigma \text{ matrix}$$

$$\varepsilon_{rms} = \sqrt{\det \sigma} = \sqrt{\sigma_{11}\sigma_{22} - \sigma_{12}^{2}} \qquad (\beta\gamma - \alpha^{2} = 1)$$

Beam width_{rms} of measured profile =
$$\sigma_y = \sqrt{\sigma_{11}} = \sqrt{\beta(s) \cdot \varepsilon}$$

Transformation of s-Matrix through the elements of an accelerator: The evolution of a beam matrix between two points s_1 and s_0 of an uncoupled transfer line is described by the following matrix equation:

$$\sigma_{s1} = M \cdot \sigma_{s0} \cdot M^{t}$$

$$M = \begin{pmatrix} M_{11} & M_{12} \\ M_{21} & M_{22} \end{pmatrix}; M^{t} = \begin{pmatrix} M_{11} & M_{21} \\ M_{12} & M_{22} \end{pmatrix}$$

The distances between screens or from Quadrupole to screen s and Quadrupole field strength 1/f are given, therefore the transport matrix M is known. Applying the transport matrix gives:

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$$\sigma_{s_{1}} = M \cdot \sigma_{s_{0}} \cdot M^{t}$$

$$= \begin{pmatrix} M_{11} & M_{12} \\ M_{21} & M_{22} \end{pmatrix} \cdot \begin{pmatrix} \sigma_{11} & \sigma_{12} \\ \sigma_{21} & \sigma_{22} \end{pmatrix}_{s_{0}} \cdot \begin{pmatrix} M_{11} & M_{21} \\ M_{12} & M_{22} \end{pmatrix} = \sigma^{measured} = \begin{pmatrix} \sigma_{y}^{2} & \sigma_{yy'} \\ \sigma_{y'y} & \sigma_{y'}^{2} \end{pmatrix}_{s_{1}}^{measured} = \varepsilon_{mms} \begin{pmatrix} \beta & -\alpha \\ -\alpha & \gamma \end{pmatrix}$$

$$= \begin{pmatrix} M_{11} & M_{12} \\ M_{21} & M_{22} \end{pmatrix} \cdot \begin{pmatrix} \sigma_{11}M_{11} + \sigma_{12}M_{12} & \sigma_{11}M_{21} + \sigma_{12}M_{22} \\ \sigma_{21}M_{11} + \sigma_{22}M_{12} & \sigma_{12}M_{21} + \sigma_{22}M_{22} \end{pmatrix}$$

$$= \begin{pmatrix} M_{11}(\sigma_{11}M_{11} + \sigma_{12}M_{12}) + M_{12}(\sigma_{21}M_{11} + \sigma_{22}M_{12}) & \cdots \\ \cdots & \cdots & \cdots \end{pmatrix}$$

$$\sigma_{11}^{new} = \sigma_{y}^{2} \stackrel{new}{=} M_{11}^{2} \sigma(s_{0})_{11}^{2} 2M_{11} M_{12} \sigma(s_{0})_{12}^{2} + M_{12}^{2} \sigma(s_{0})_{22}^{2} \quad (\sigma_{12} = \sigma_{21}) \quad (1)$$

Transferred/measured beam width² from s_n Unknown at QP (at s_0)

Solving $\sigma(s_n)_{11} \sigma(s_0)_{12}$ and $\sigma(s_0)_{22}$ while Matrix elements are known: <u>Needs minimum of three</u> different measurements, either three screens or three different Quadrupole settings with different field strength K = 1/f. We will use in the following some more focal length values and use a fit.

$$\sigma_{11}^{new} = \sigma_y^{2 new} = M_{11}^{2} \sigma(s_0)_{11} + 2M_{11} M_{12} \sigma(s_0)_{12} + M_{12}^{2} \sigma(s_0)_{22}$$

with
$$M = S Q = \begin{pmatrix} 1 & s \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ K & 1 \end{pmatrix} = \begin{pmatrix} 1 - s/f & s \\ -s/f & 1 \end{pmatrix} = \begin{pmatrix} M_{11} & M_{12} \\ M_{21} & M_{22} \end{pmatrix}$$

$$\sigma_{y}^{2} = (1-s/f)^{2} \sigma(s_{0})_{11} + 2s(1-s/f)\sigma(s_{0})_{12} + s^{2} \sigma(s_{0})_{22}$$

$$\sigma_{y}^{2} = (s/f)^{2} \sigma_{11}^{2} + (s/f)(2\sigma_{11}^{2} + 2s\sigma_{12}^{2}) + (\sigma_{11}^{2} + 2s\sigma_{12}^{2} + s^{2}\sigma_{22}^{2})$$

Parabola fit as a function of the quadrupole excitation (s/f) and the parameters (a,b,c) of $\sigma_y^2 = ax^2 + bx + c$ (width²!!!) contain the unknown beam properties σ_{11} , σ_{12} and σ_{22} .

$$a = \sigma_{11}$$
 $b = 2\sigma_{11} + 2s\sigma_{12}$ $c = \sigma_{11} + 2s\sigma_{12} + s^2\sigma_{22}$ or

 $\sigma_{11} = a$ $\sigma_{12} = (b - 2\sigma_{11}) / 2s$ $\sigma_{22} = (c - \sigma_{11} - 2s\sigma_{12}) / s^2$

$$\varepsilon_{rms} = \sqrt{\det \sigma} = \sqrt{\sigma_{11}\sigma_{22} - \sigma_{12}^2}$$





Beam Phosphor Screen Work Station Frame Image Grabber Processor Fiber Optic Link CCD Camera/Filters Mirror Telephoto Lens

By changing the lenses with different focal length f one can take pictures from the camera. The distance of the lens to the screen can be measured by a simple ruler. The camera is connected to a Computer where the readout software is installed. The pictures (.jpg) can be saved and can be loaded into a free software called "ImageJ" where a profile of an area can be displayed and the curser position and the value is displayed (8 bit). The σ of the profiles have to be found for each focal length and the emittance have to be calculated on an prepared Excel sheet..

Your tasks in green frames

Calibration

Use mm-grid to calibrate the readout setup.

Select ROI (where beam image will appear), plot profile, use cursor and enter measurement into pre-prepared Excel sheet "QP emittance.xlsx"

 Calibration
 Image: Calibration

 Line Image: Calibratic calibration

 distance
 Image: Calibratic calibraticalibratic calibr

All yellow cells will be calculated automatically





Check: Do not saturate (255) <u>Take some profiles at</u> <u>same distance</u> <u>lens-screen s with</u> <u>different focal length f.</u>



$$\sigma_{y \text{ measured}}^{2} = M_{1}^{2}\sigma_{11} + 2M_{11}M_{12}\sigma_{12} + M_{12}^{2}\sigma_{22} \qquad \mathcal{E}$$

$$M = S Q = \begin{pmatrix} 1 & s \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ K & 1 \end{pmatrix} = \begin{pmatrix} 1 - s/f & s \\ -s/f & s \end{pmatrix} = \begin{pmatrix} M_{11} & M_{12} \\ M_{21} & M_{22} \end{pmatrix}$$

 $\sigma = \begin{pmatrix} \sigma_{11} & \sigma_{12} \\ \sigma_{21} & \sigma_{22} \end{pmatrix} = \begin{pmatrix} \sigma_{y}^{2} & \sigma_{yy}^{2} \\ \sigma_{yy}^{2} & \sigma_{yy}^{2} \end{pmatrix} = \varepsilon_{rms} \begin{pmatrix} \beta & -\alpha \\ -\alpha & \gamma \end{pmatrix} = \sigma matrix$

$$\sigma_{y}^{2} = (s/f)^{2} \sigma_{11} + (s/f)(2\sigma_{11} + 2s\sigma_{12}) + (\sigma_{11} + 2s\sigma_{12} + s^{2}\sigma_{22})$$



Adjust the aperture so that the image looks quite gaussian at its larges size!

(255)





Introduction of readout software

- PHYTEC Vision Demo 2.2 for camera readout
- ImageJ for Data treatment

CCD Readout: Introduction

• readout program PHYTEC Vision Demo 2.2



CCD Readout: Introduction



ImageJ: Introduction



- load image file \rightarrow File \rightarrow Open (Shortcut: Ctrl + O)
- select ROI: in start panel: select left button (below "File"), usually already pre-selected then with left mouse button: draw rectangular ROI
- plot horizontal projection \rightarrow Analyze \rightarrow Plot Profile (Shortcut: Ctrl + k)



save data -> list data points

-> save data as <u>.csv file (required for profile fitting)</u>

ImageJ: Introduction



ImageJ: Introduction



• additional data fitting

- > create data file \rightarrow e.g. Excel or simple ASCII text file with Notepad
- repeat fitting as described before

Devices

• CCD

Phytec USB-CAM 051H

Resolution	2592 x 1944 (5 MPix) , 2048 x 1536 (3,1MPix), 1600 x 1200 (2MPix), 1280 x 960 (1,2MPix) 1024 x 768 (0,8MPix), 640 x 480 (VGA)			
Model	USB- CAM- 051H	USB- CAM- 151H	USB- CAM- 052H	USB-CAM-152H
color / monochrom	monochrom		color	
Sensor Format	1/2,5"			
Image Sensor	Aptina MT9P031, CMOS			
Pixel Size	2,2 μm x 2,2 μm			
Color format	Y8		RGB32, RGGB (Raw)	
Lens Holder	C / CS – Mount			
fps	6 fps to 52 fps			
Dynamic Range	8 bit			
Shutter	Rolling			
Light sensitivity	1,4 V/lux-sec			
Interface	USB 2.0 High Speed			
Exposure time	1/10.000 s to 30 s			
Gain	0 dB to 18 dB			
White Balance	6 dB bis +6 dB			
Power supply	4,5 V bis 5,5V DC			
Power Consumption	Circa 250 mA bei 5V			
Feature (optional)	-	ext. Trigger, Digital- Output	-	ext. Trigger, Digital-Output
Temperature range	-5°C bis +45°C			
Dimensions (B x L x H)	36 mm x 36 mm x 25 mm			
Fixing	1/4" and M6x8 on all sides			
Weight	70 g			
Connection	USB Mini-B			
Feature- Connection	-	Hirose HR10A- 7R-4P	-	Hirose HR10A-7R-4P

screen

- > material: white paper
- grid target
 - spacing: 1 mm
- Laser: LaserBoyII

BMI Bayerische Laserboy II Wasserwaage 649 015

Allgemeine Informationen
Artikelnummer
EAN
Hersteller
Hersteller-ArtNr
Hersteller-Typ
√erpackungseinheit
Artikelklasse

Technische Informationen Länge der Signalstrecke

Sichtbare Signalstrecke Rotierende Signalstrecke

Laserklasse

ET1117000 4007368050049 BMI Bayerische 649 015 649 015 1 Stück Messlaser



BMI Bayerische Laserboy II Wasserwaage 649 015 Länge der Signalstrecke 30m, Laserklasse 2, Sichtbare Signalstrecke,

30m