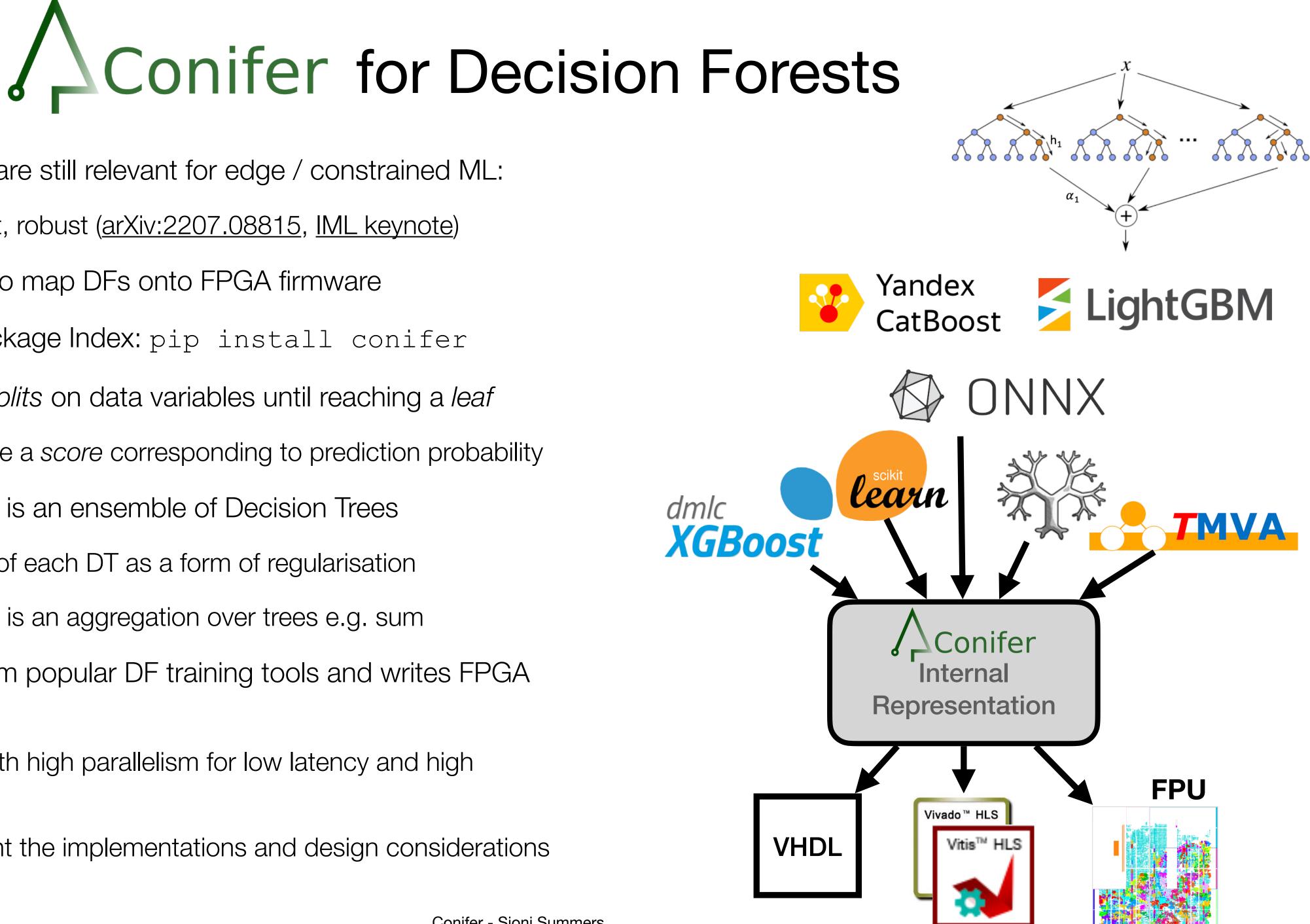


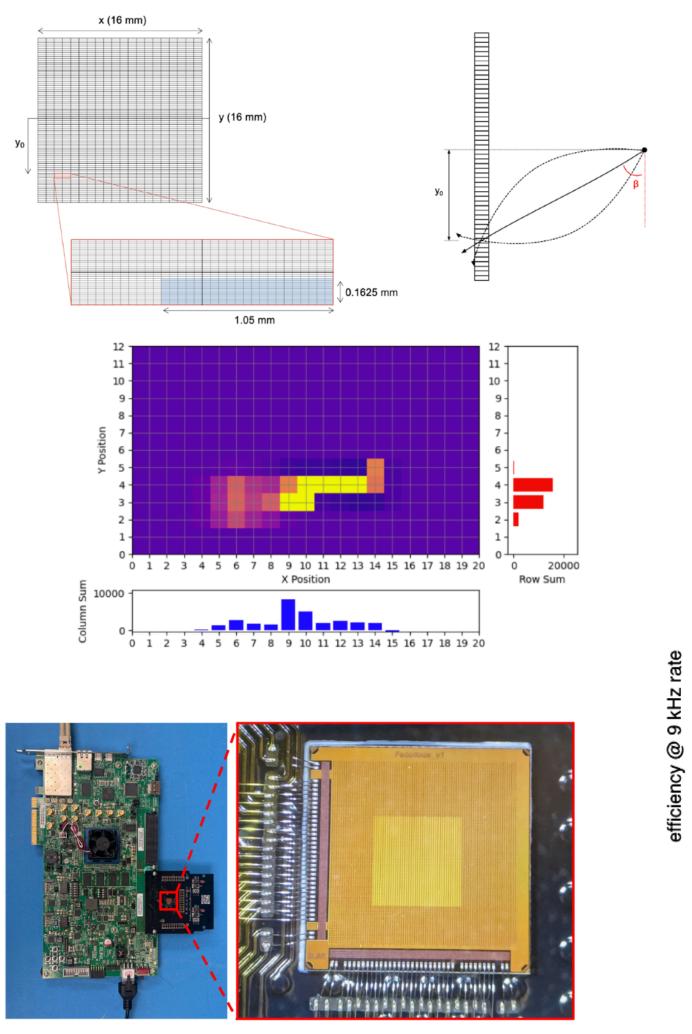
- Under the Canopy: Exploring Conifer for Low-Latency Decision Forests on FPGAs
 - Sioni Summers
 - sioni@cern.ch sioni.web.cern.ch
 - 12th June 2024



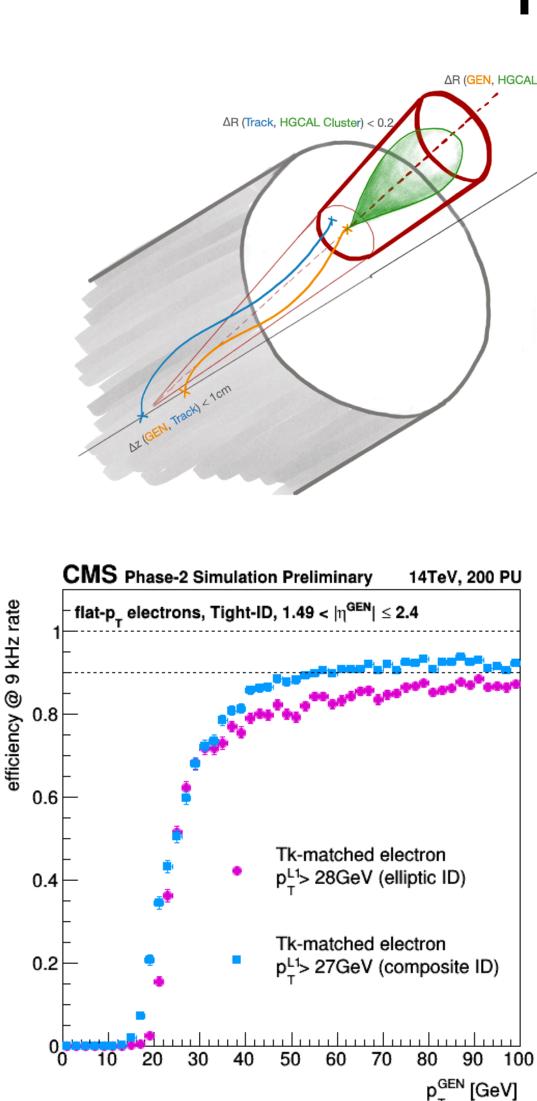
- Decision Forests are still relevant for edge / constrained ML:
 - Fast, lightweight, robust (arXiv:2207.08815, IML keynote)
- **conifer** is a tool to map DFs onto FPGA firmware
 - On Python Package Index: pip install conifer
- A Decision Tree *splits* on data variables until reaching a *leaf*
 - Leaves associate a *score* corresponding to prediction probability
- A Decision Forest is an ensemble of Decision Trees
 - Randomisation of each DT as a form of regularisation
 - Ensemble score is an aggregation over trees e.g. sum
- conifer reads from popular DF training tools and writes FPGA projects
 - Implemented with high parallelism for low latency and high throughput
- This talk will present the implementations and design considerations

Conifer - Sioni Summers



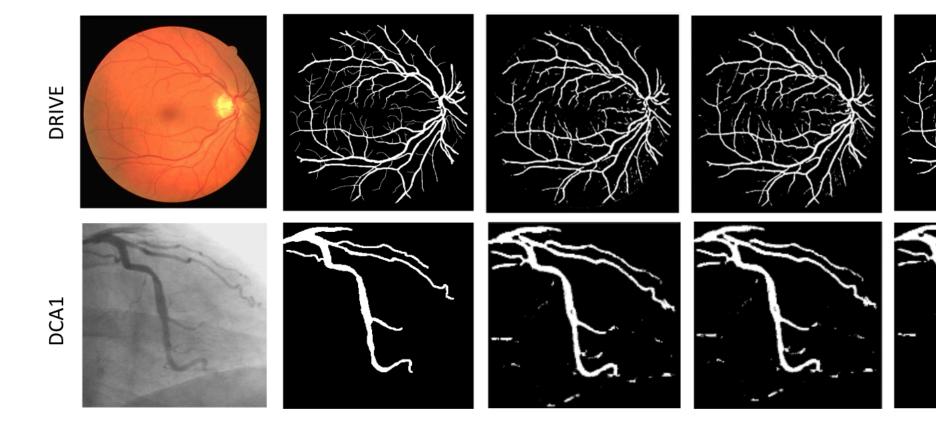


pT filtering in an eFPGA in a tracking detector frontend (25 ns latency, 500 LUTs)



conifer applications

ΔR (GEN, HGCAL Cluster) < 0.2

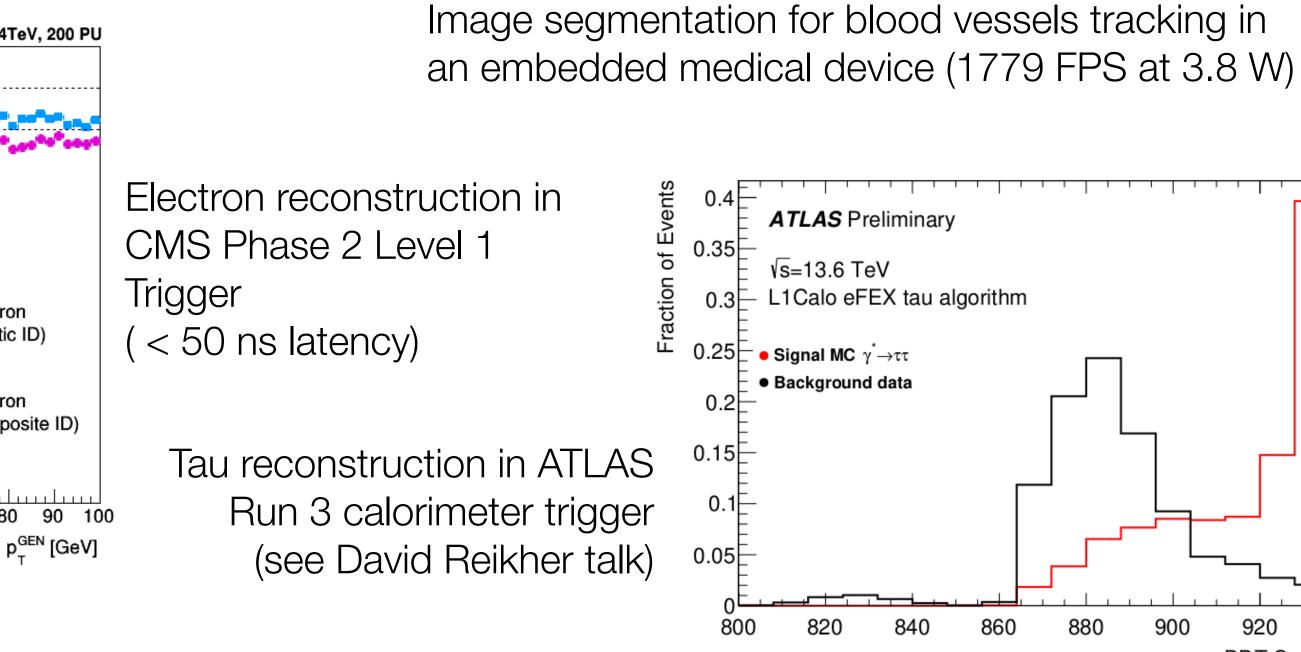


GBDT-7x7

Image

Ground truth

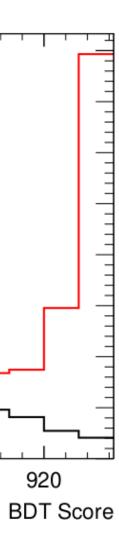
MLP-7x7





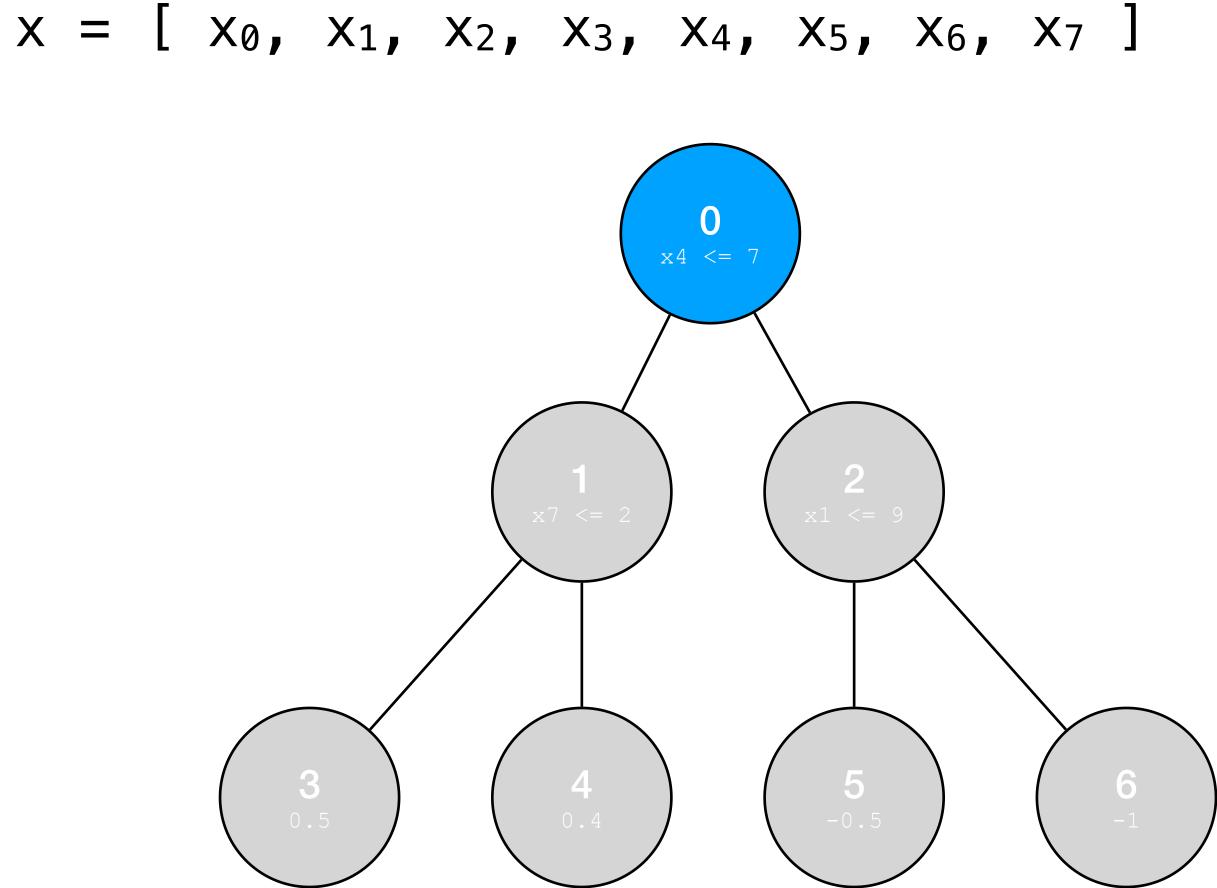
CNN-7x7





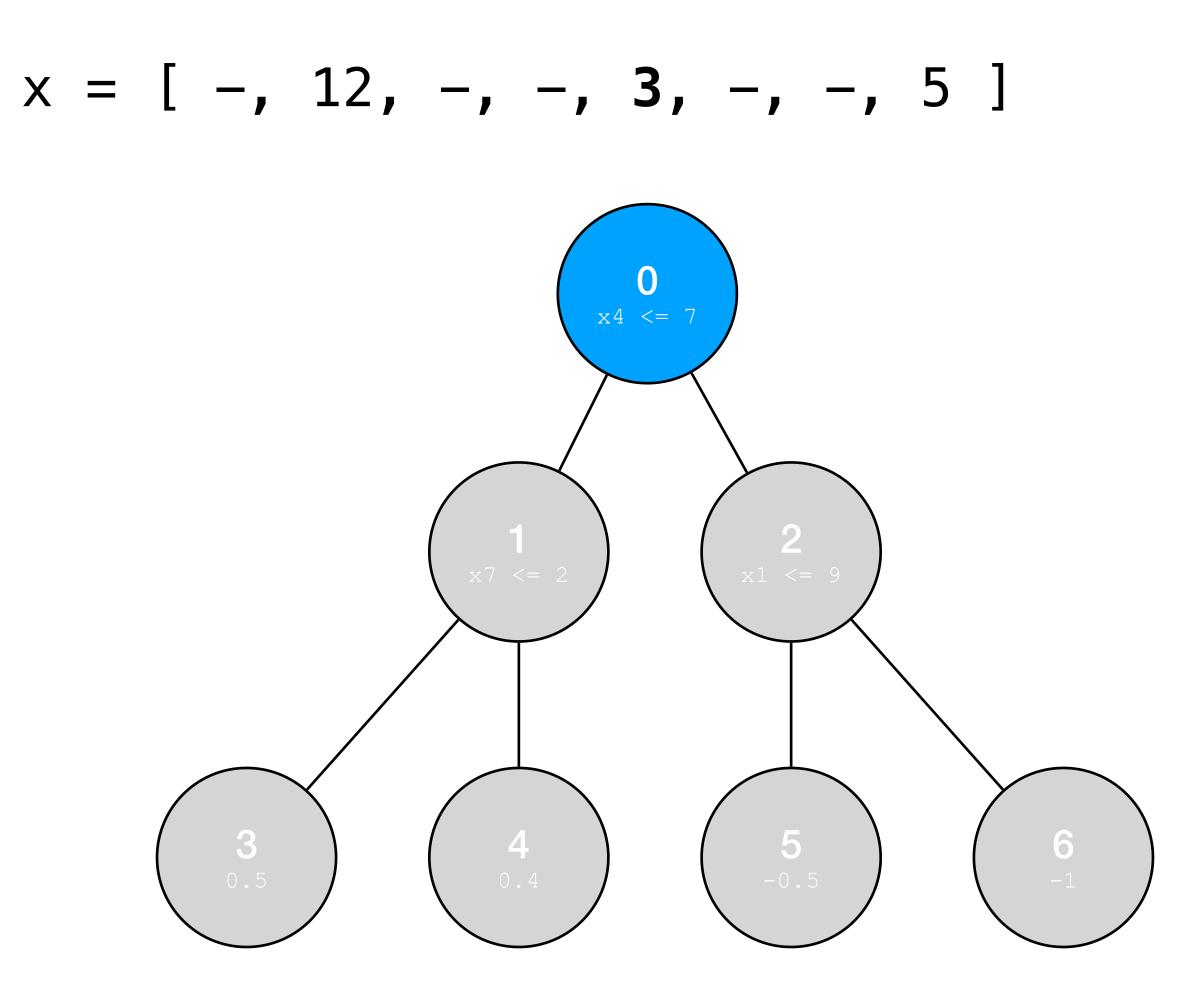


• Start at the root node - compare the selected feature with the threshold, go left or right depending on result



Decision Tree Inference

• Start at the root node - compare the selected feature with the threshold, go left or right depending on result

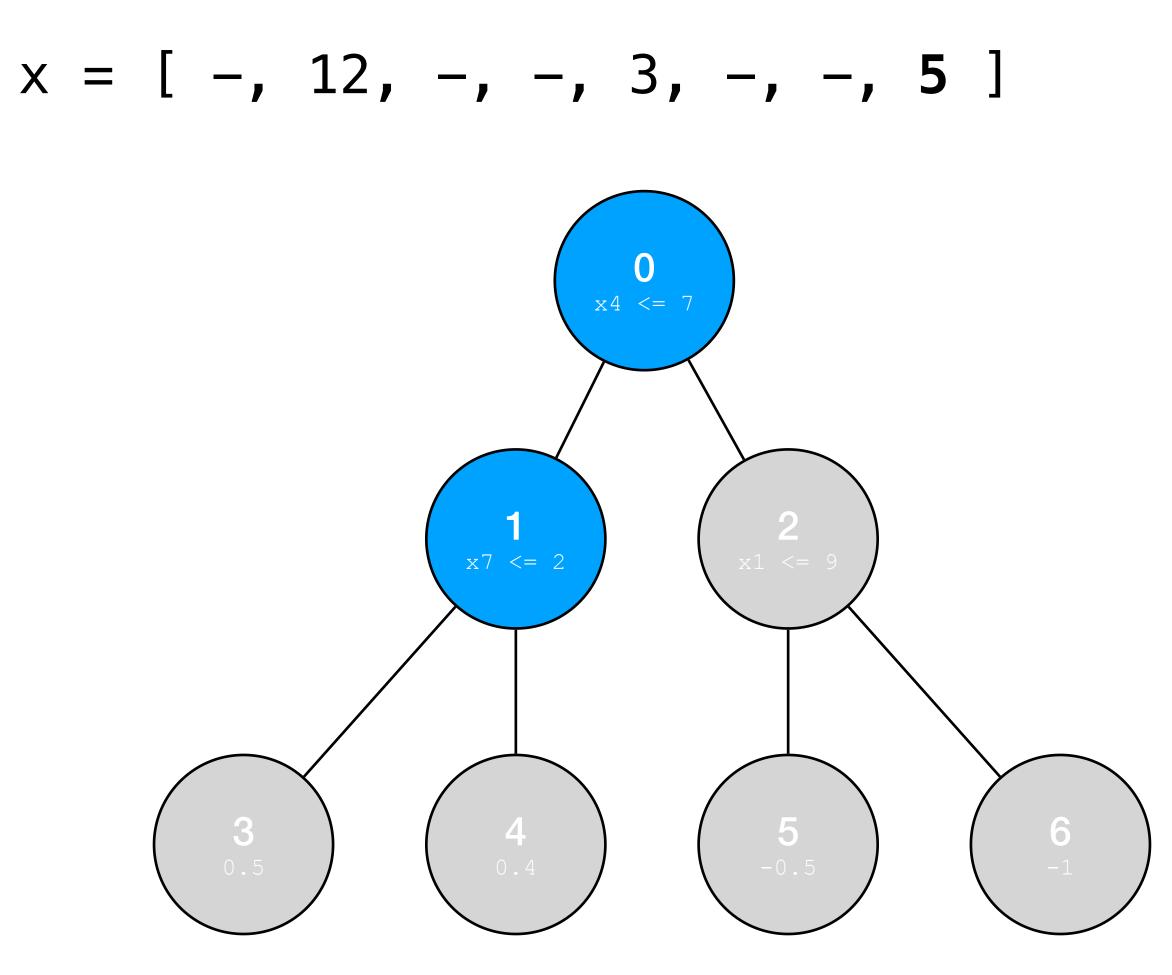


Decision Tree Inference



Decision Tree Inference

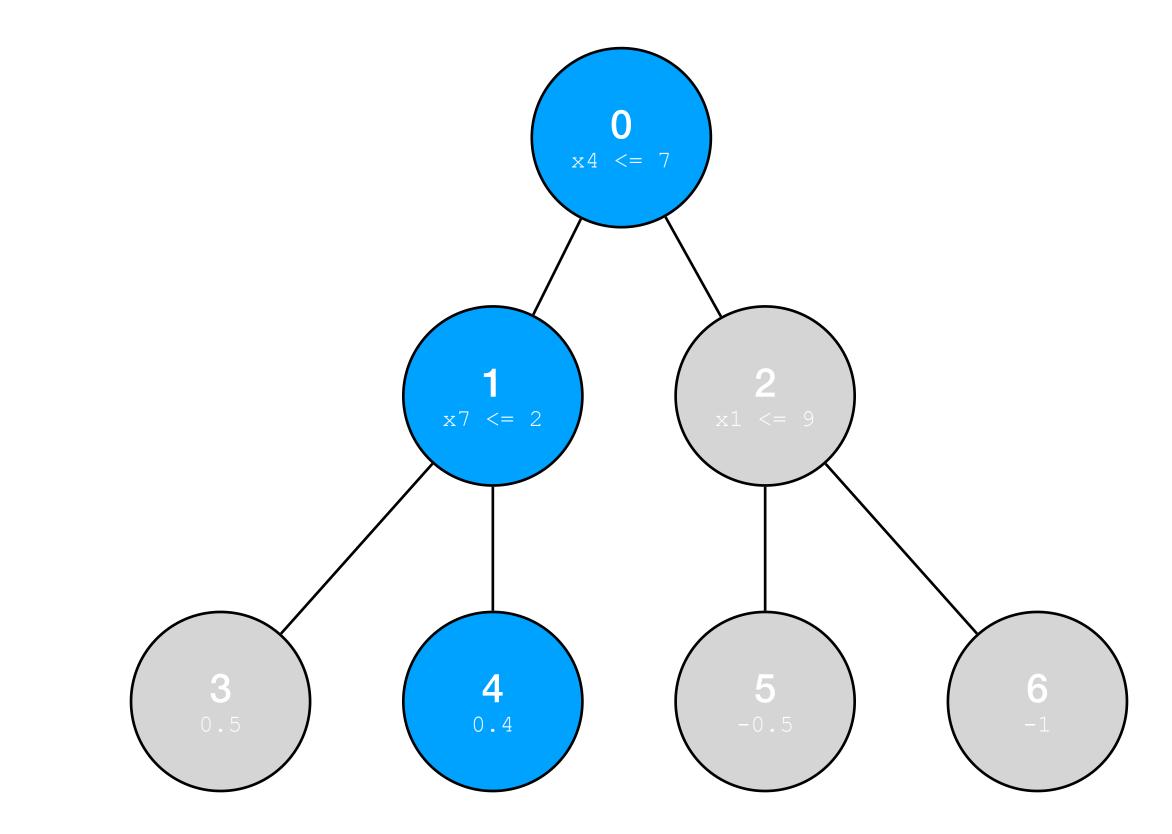
- Start at the root node compare the selected feature with the threshold, go left or right depending on result
- Continue until reaching leaf compare the selected feature with the threshold, go left or right depending on result





Decision Tree Inference

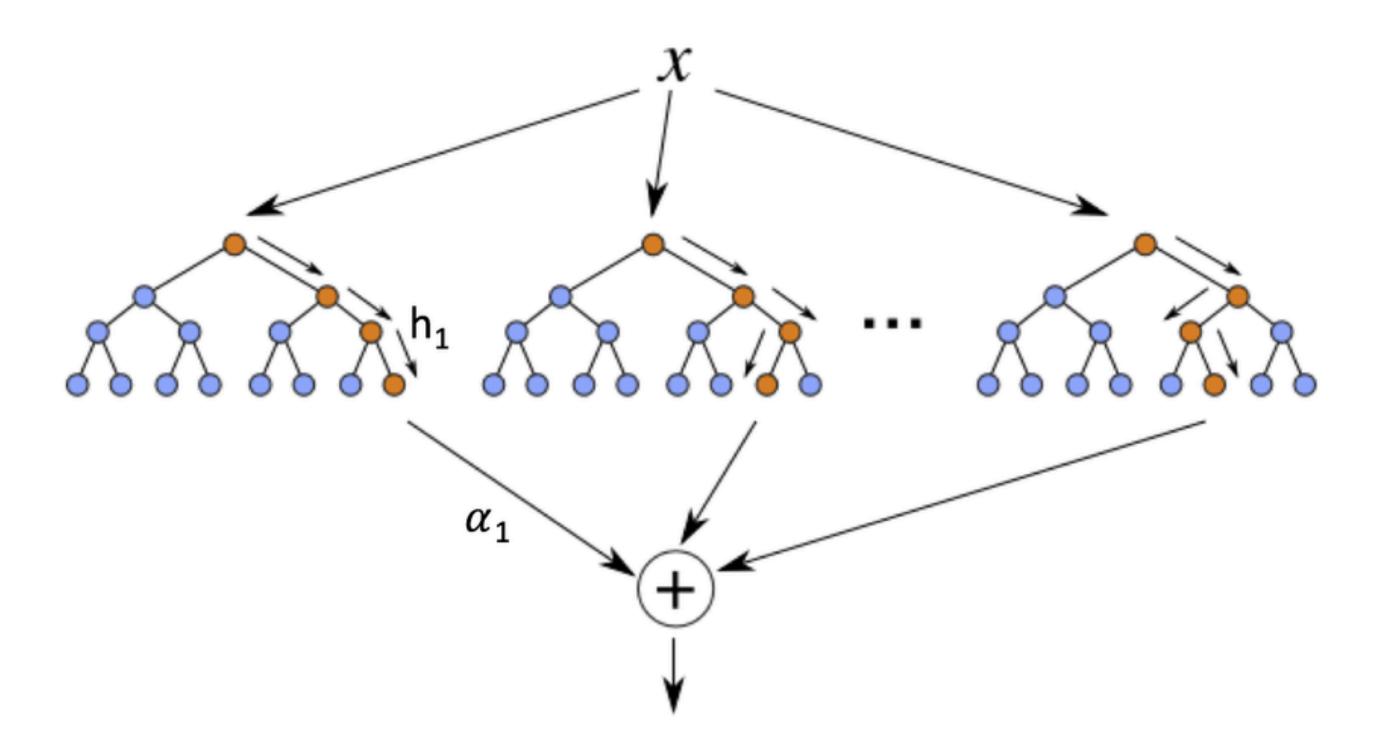
- Start at the root node compare the selected feature with the threshold, go left or right depending on result
- Continue until reaching leaf compare the selected feature with the threshold, go left or right depending on result
- The value of the terminal leaf is the tree prediction





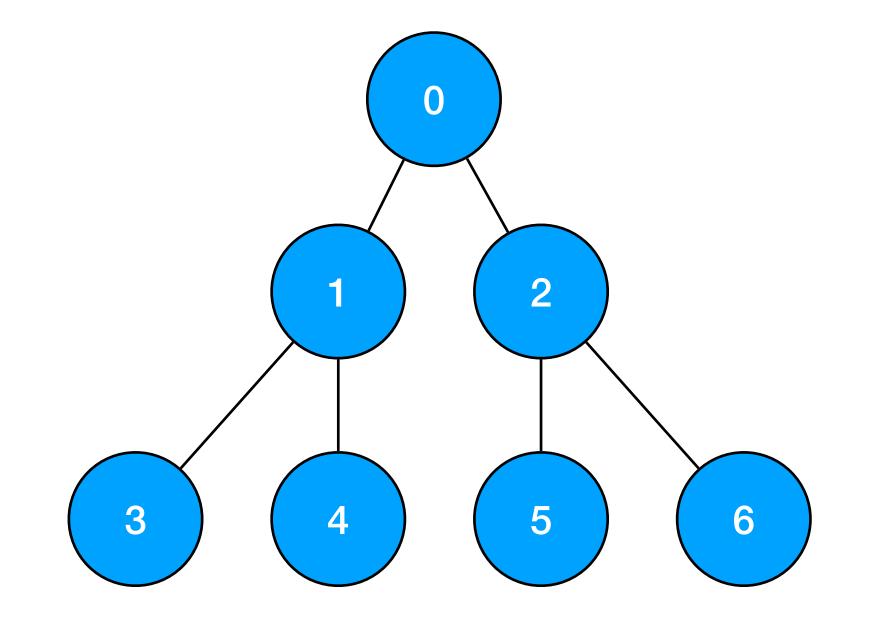
Decision Forest Inference

- Repeat the same procedure for every tree in the ensemble, sum up the tree scores for the BDT prediction
- Apply the inverse of the training loss function to obtain class probabilities



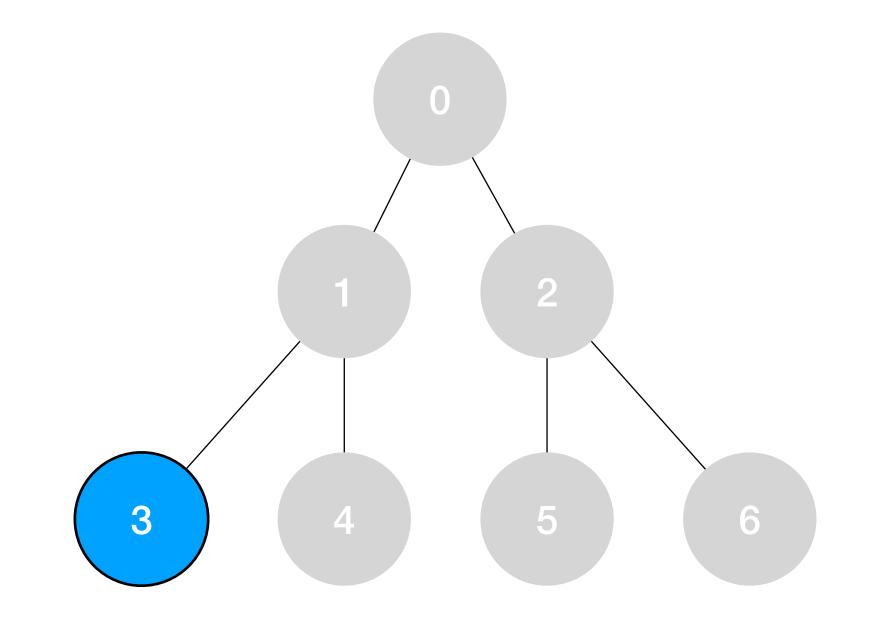


- For a tree: find which leaf is reached given a data sample x
- 'Invert' the problem: for each node ask "does the decision path reach this node?" starting at the leaves



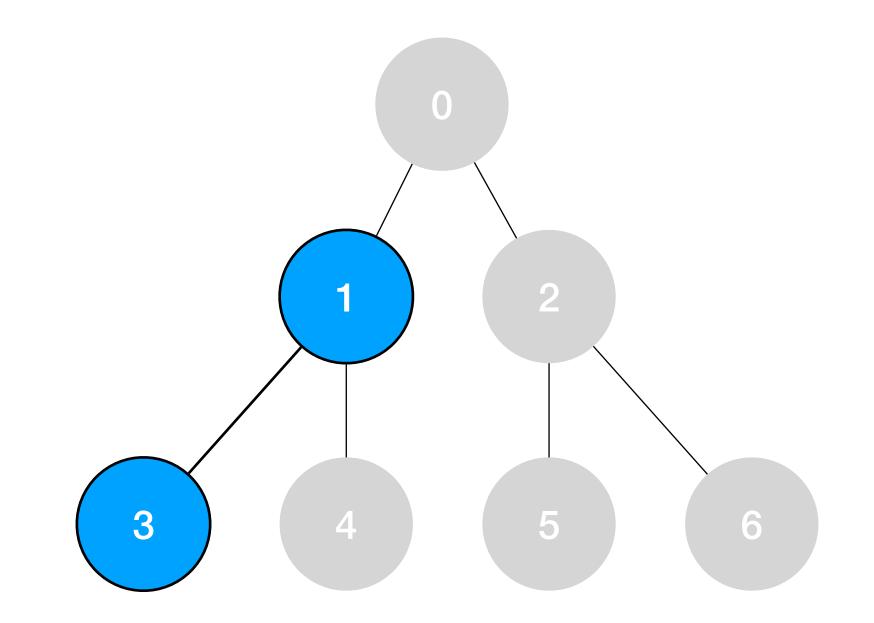


- For a tree: find which leaf is reached given a data sample x
- 'Invert' the problem: for each node ask "does the decision path reach this node?" starting at the leaves
- For leaf node '3':
 - The decision path reaches '3' if: the decision path reached '1' AND the comparison at '1' goes 'left'

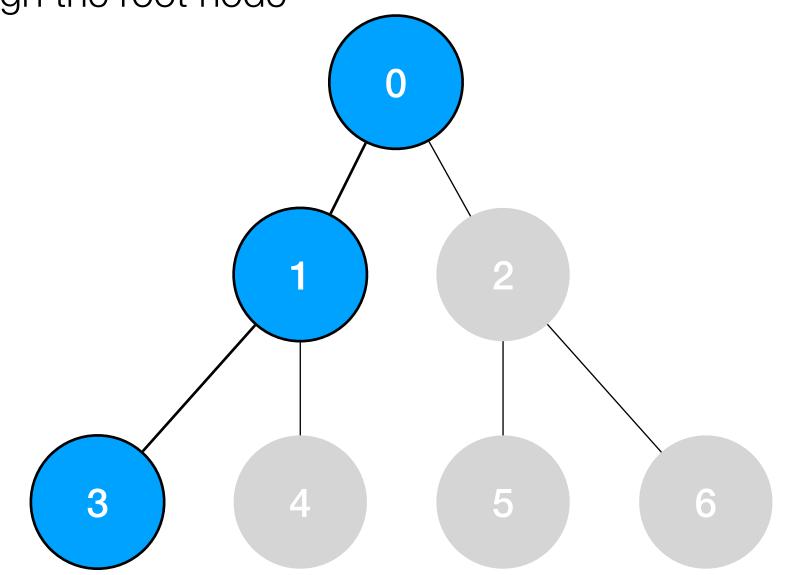




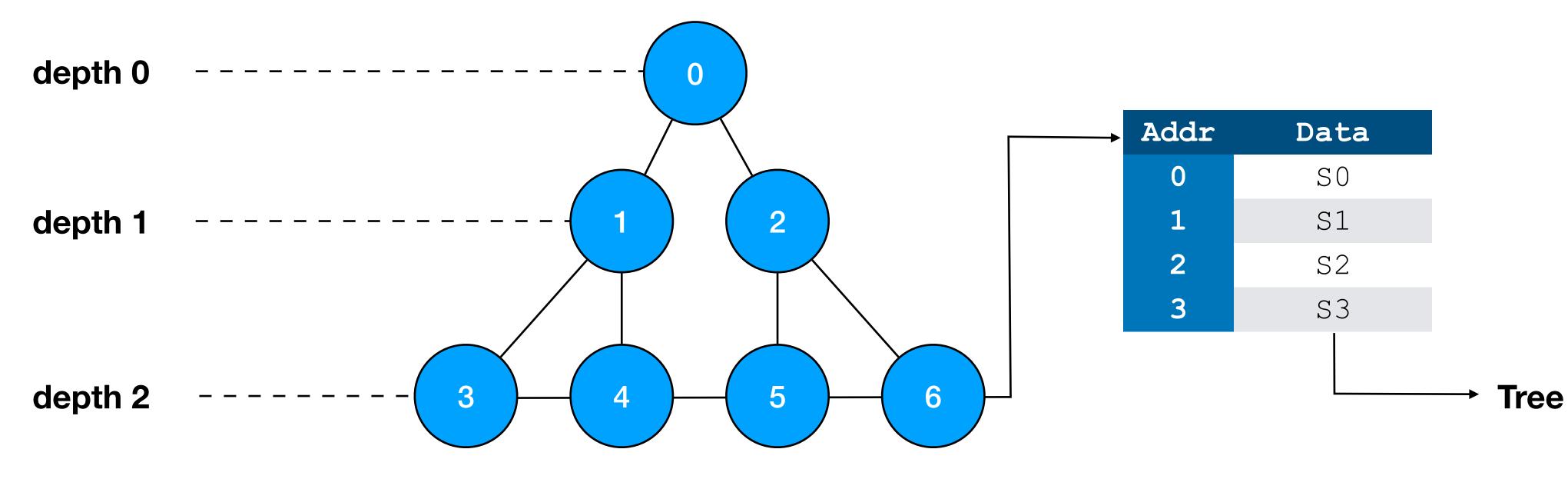
- For a tree: find which leaf is reached given a data sample x
- 'Invert' the problem: for each node ask "does the decision path reach this node?" starting at the leaves
- For leaf node '3':
 - The decision path reaches '3' if: the decision path reached '1' AND the comparison at '1' goes 'left'
- For node '1':
 - The decision path reaches '1' if: the decision path reached '0' AND the comparison at '0' goes 'left'



- For a tree: find which leaf is reached given a data sample x
- 'Invert' the problem: for each node ask "does the decision path reach this node?" starting at the leaves
- For leaf node '3':
 - The decision path reaches '3' if: the decision path reached '1' AND the comparison at '1' goes 'left'
- For node '1':
 - The decision path reaches '1' if: the decision path reached '0' AND the comparison at '0' goes 'left'
- For node '0':
 - The decision path always passes through the root node



- For a tree: find which leaf is reached given a data sample x
- 'Invert' the problem: for each node ask "does the decision path reach this node?" starting at the leaves
- We can **parallelise** this over paths by brute force: evaluate all nodes at the same depth simultaneously
- We can pipeline this over different data: each node can do a comparison on new data with II=1
- For each leaf node we have a boolean: TRUE if the decision path reaches leaf, otherwise FALSE
- Concatenate the boolean for each leaf node \rightarrow select the value corresponding to the leaf



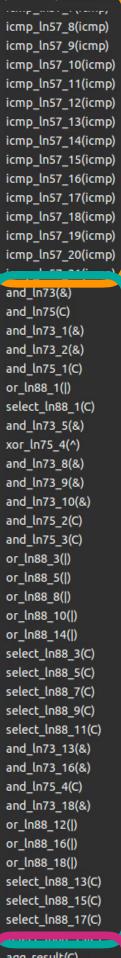
Tree score

Scheduling - Tree

- Did we achieve what we described?
- Vitis HLS Schedule Viewer in GUI
 - Tree depth = 5, some sparsity
- All **comparisons** in parallel at the start
- Cascade of **boolean operations**

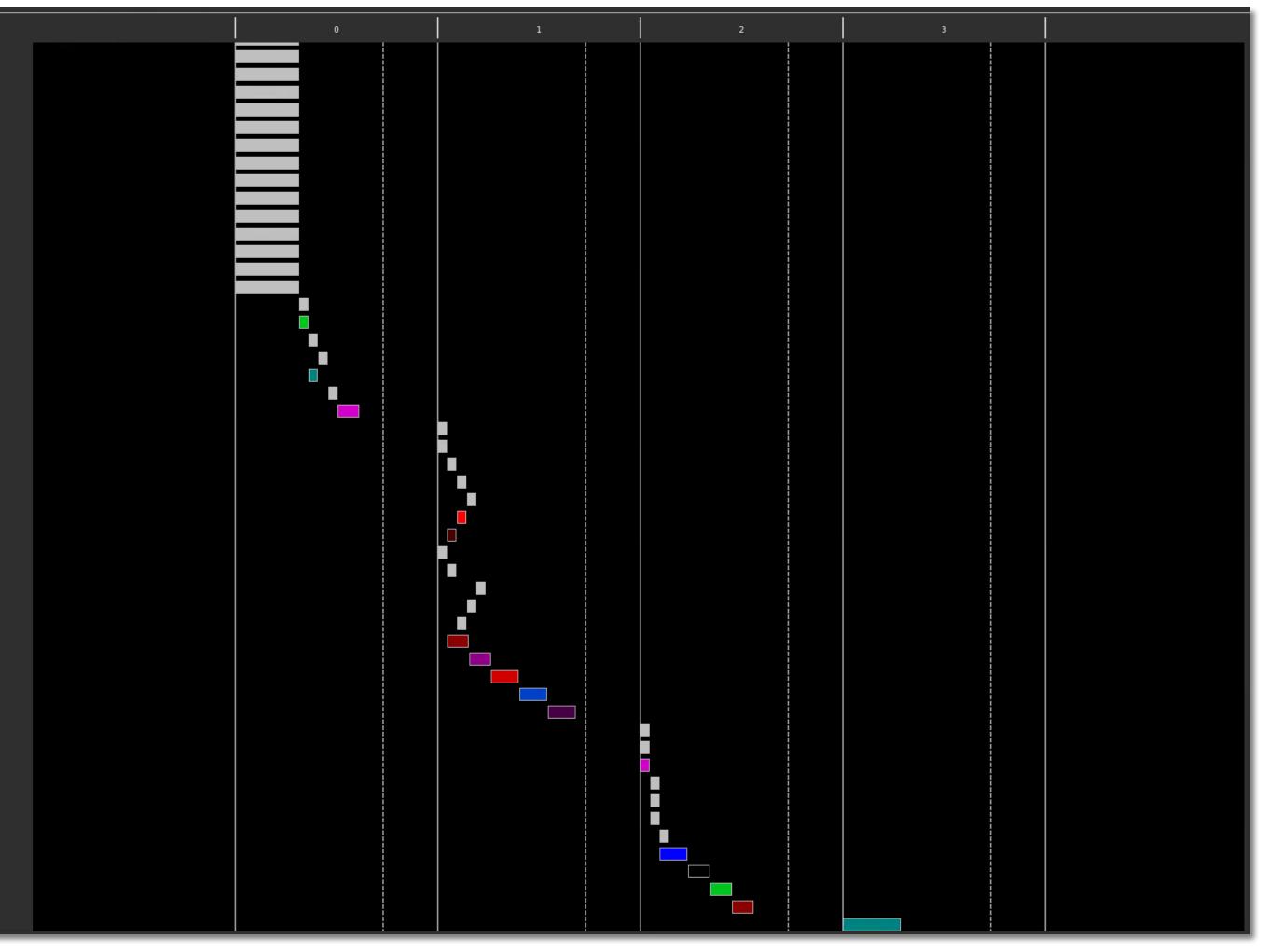
- AND, OR, XOR, NOT

• 'Aggregate' at end



agg_result(C)

t (clock cycles) -



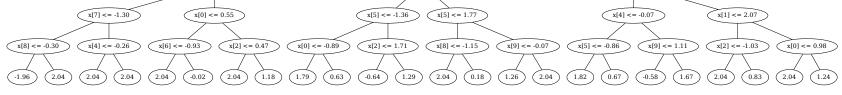
x[0] <= 0.55

x[2] <= 0.47

x[0] <= -0.89

x[6] <= -0.93

x[4] <= -0.26



x[1] <= 1.12

x[9] <= -0.07

x[5] <= -0.86

x[9] <= 1.11

x[5] <= 1.24

x[8] <= -1.15

x[5] <= -1.36

x[2] <= 1.71

14

Scheduling - Forest

- Did we achieve what we described?
- Vitis HLS Schedule Viewer in GUI
 - Number of trees = 20
 - Tree from previous slides is one of them
- All tree inferences performed in parallel
- Tree scores summed in pairs
- Total latency: 7 clock cycles

t (clock cycles)

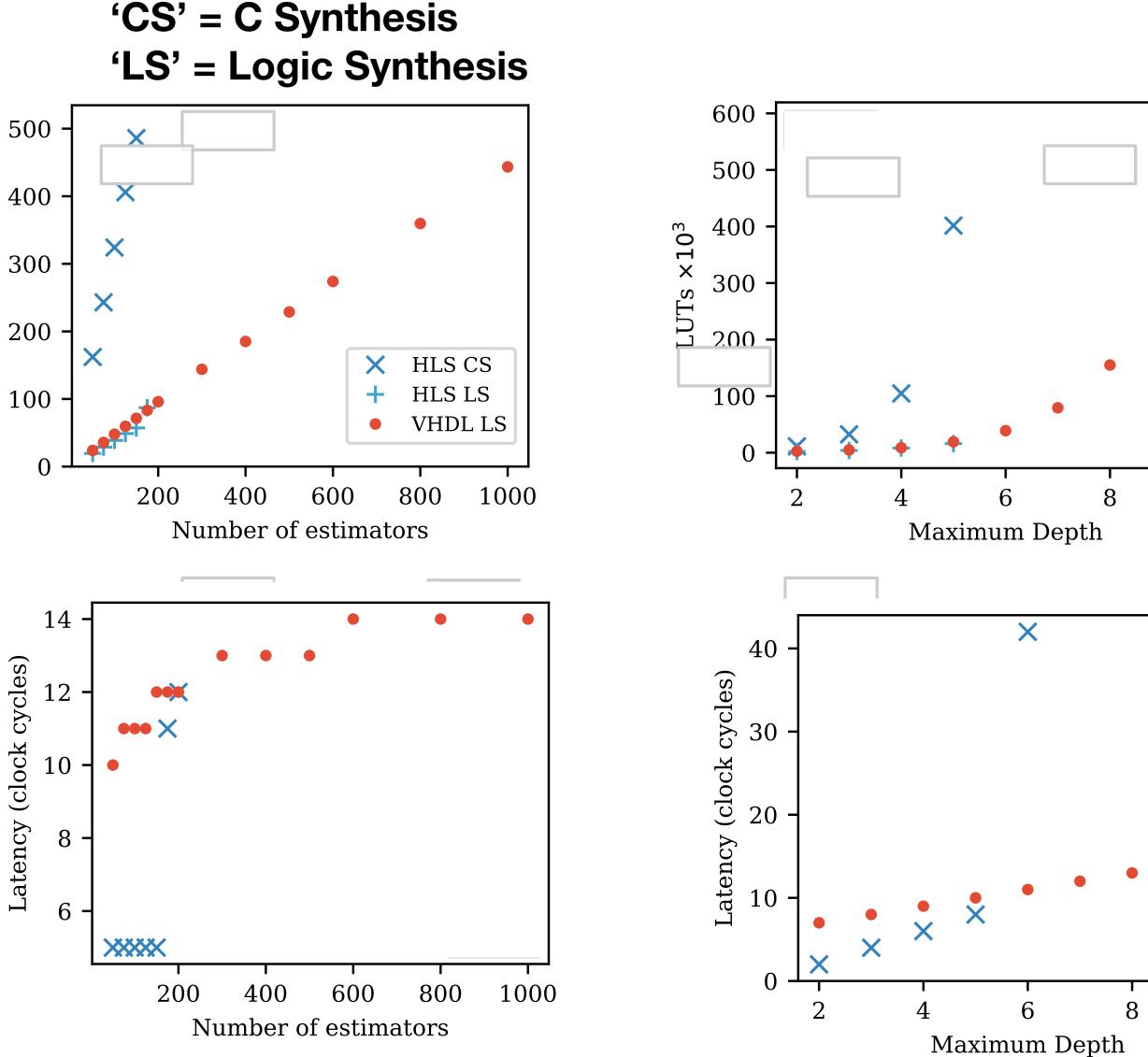
| decision_function_19(function) decision_function af(function) decision_function_f(function) decision_function_af(function) decision_function_af(function) decision_function_11f(function) decision_function_f | Operation\Control Step | 0 | 1 | 2 | 3 | 4 | 5 | 1 |
|---|--|---|---|---|---|---|-----|---|
| decision_function_18(function) decision_function_6(function) decision_function_4(function) decision_function_3(function) decision_function_18(function) decision_function_115(function) decision_function_18(function) decision_function_function_function_function_function_function_function_function_function_function_function_function_function_ | decision function 19(function) | | | | | | i i | |
| decision_function_r(function) decision_functions,S(function) decision_function_s(function) decision_function_s(function) decision_function_r(function) decision_function_r(function) decision_function_r(function) decision_function_r1s(function) decision_fu | | | | | | | | |
| decision_function_sf(function) decision_function, sf(function) decision_function_2f(function) decision_function_1f(function) decision_function_int(function) d | | - | | | | | | |
| decision_function_9(function) decision_function_2(function) decision_function_2(function) decision_function_1(function) decision_function_17(function) decision_function_17(function) decision_function_13(function) decision_function_13(function) decision_function_13(function) decision_function_11(function) decision_function_11(function) decision_function_10(function) decision_function_10(function) decision_function_10(function) decision_function_9(function) decision_function_9(function) decision_function_9(function) decision_function_9(function) decision_function_9(function) decision_function_9(function) decision_function_10(function) decision_function_9(funct | 그는 사람이 가지 않는 것 같아요. 그 것이 같아요. 이렇게 하는 것이 같아요. | - | · | | | | | |
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Implementations

- Conifer has both HLS and VHDL implementations - both targeting the same architecture previously described and fully pipelined
- Within some limits the HLS achieves identical resources to the VHDL
 - After synthesizing the HLS-generated HDL
 - Caveat: plots are with Vivado HLS 2019.2. With recent Vitis HLS the performance is better
- The HLS latency can be lower than the VHDL
 - VHDL pipelining was done 'by hand'
- Resources and latency scales as expected:
 - Resource linear with trees, exponential with depth
 - Latency logarithmic with trees, linear with depth
- Latency within 10-100 ns is achievable

500 -

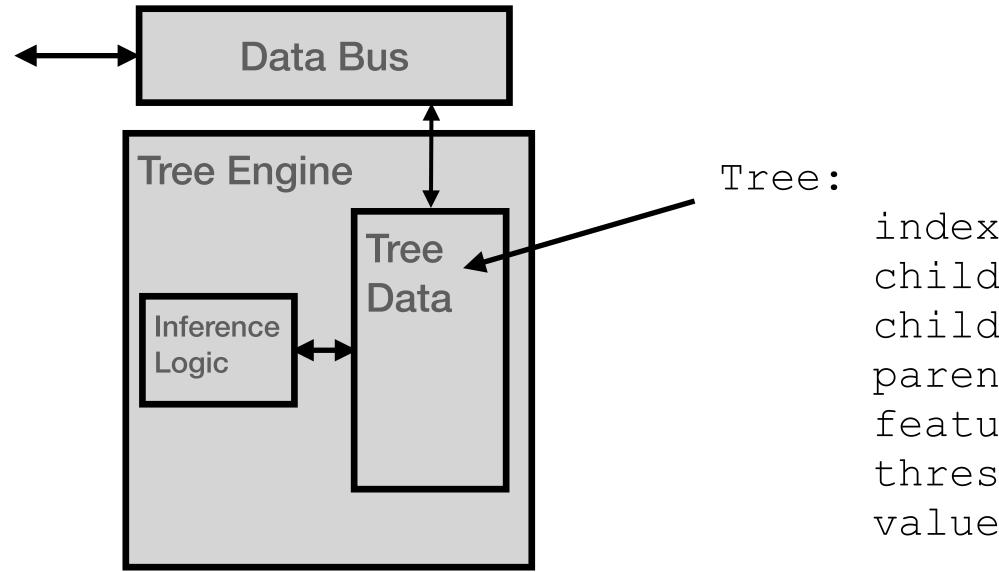




Forest Processing Unit

- So far we looked at 'static' BDT evaluation
 - One trained model \rightarrow one HLS function \rightarrow one IP \rightarrow one bitfile
 - So if the model changes at all, we need to rerun C Synthesis, Logic Synthesis and Implementation \rightarrow takes hours!
- In next section we will look at a more dynamic & reconfigurable implementation called "Forest Processing Unit" (FPU)
- We would like a base design that can perform inference of ~any BDT model afterwards (within some limits)
- And we would like to take advantage of the FPGA to get good performance (fast inference)
- Idea 1: represent the BDT as data, operate inference on that data, and load new data for a new model
- Idea 2: parallelise over trees by having independent 'Tree Engines', aggregate their output for the model

- Idea 1: represent the BDT as data, operate inference on that data, and load new data for a new model over a bus
- Store one node at one address, child indices are pointers to other addresses

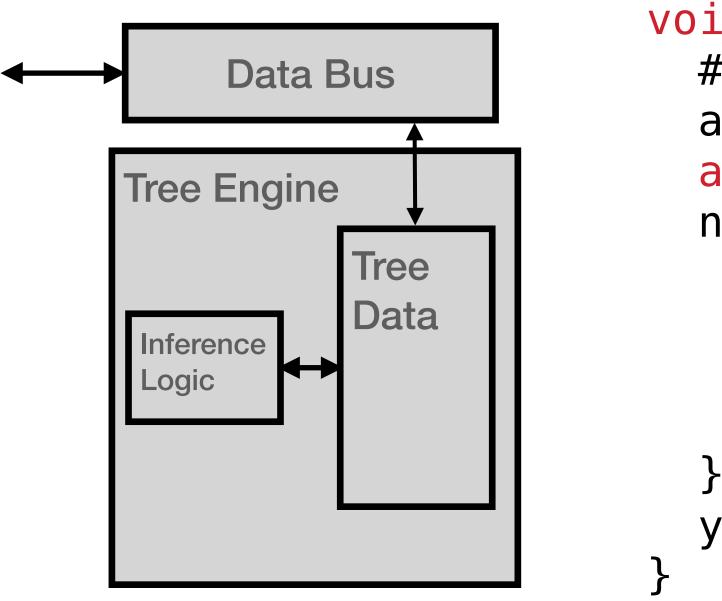


that data, and load new data for a new model over a bus to other addresses

| X | • | [| 0, | 1, | 2, | З, | 4, | 5, | 6] |
|------------|---|-----|-------|-----|-----|-------------|-------------|-------------|-----|
| dren_left | • | [| 1, | 3, | 5, | -2 , | -2 , | -2 , | -2] |
| dren_right | • | [| 2, | 4, | 6, | -2, | -2, | - 2, | -2] |
| nt | • | [| -1, | 0, | 0, | 1, | 1, | 2, | 2] |
| ure | • | [| 4, | 7, | 1, | -2, | -2, | -2 , | -2] |
| shold | • | [| 7, | 2, | 9, | -2, | -2, | -2, | -2] |
| е | • | [- | -1, · | -1, | -1, | 0.5, | 0.4, | -0.5, | -1] |



- Idea 1: represent the BDT as data, operate inference on that data, and load new data for a new model
- To perform inference of a model on some data we need to:
 - Read the next node
 - Compare the appropriate feature with the threshold
 - Get the pointer to the next node
- Upon reaching a leaf, return its score

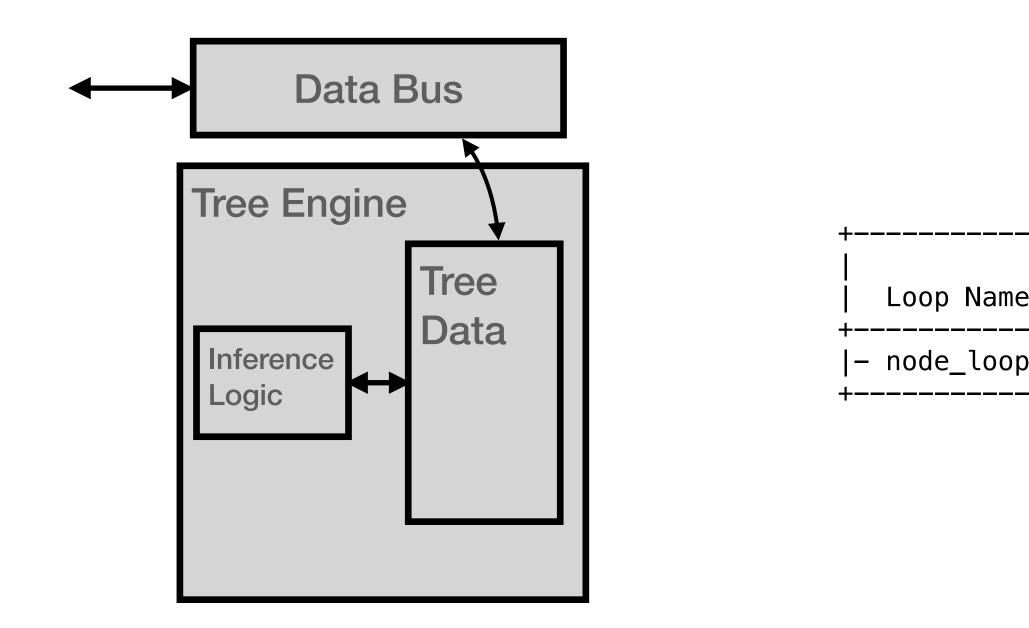


#pragma HLS pipeline ap_int<ADDRBITS> i = 0; auto node = nodes[i]; #pragma HLS pipeline node = nodes[i]; = node.score;

```
void TreeEngine(T X[NVARS], DecisionNode nodes[NN0DES], U& y){
  node_loop : while(!node_is_leaf){
    i = X[node.feature] <= node.threshold ?</pre>
                            node.child_left : node.child_right;
```

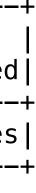


- Idea 1: represent the BDT as data, operate inference on that data, and load new data for a new model
- To perform inference of a model on some data we need to:
 - Read the next node
 - Compare the appropriate feature with the threshold
 - Get the pointer to the next node
- Iteration logic has a 'loop carried dependency' between iterations, and a data dependent latency



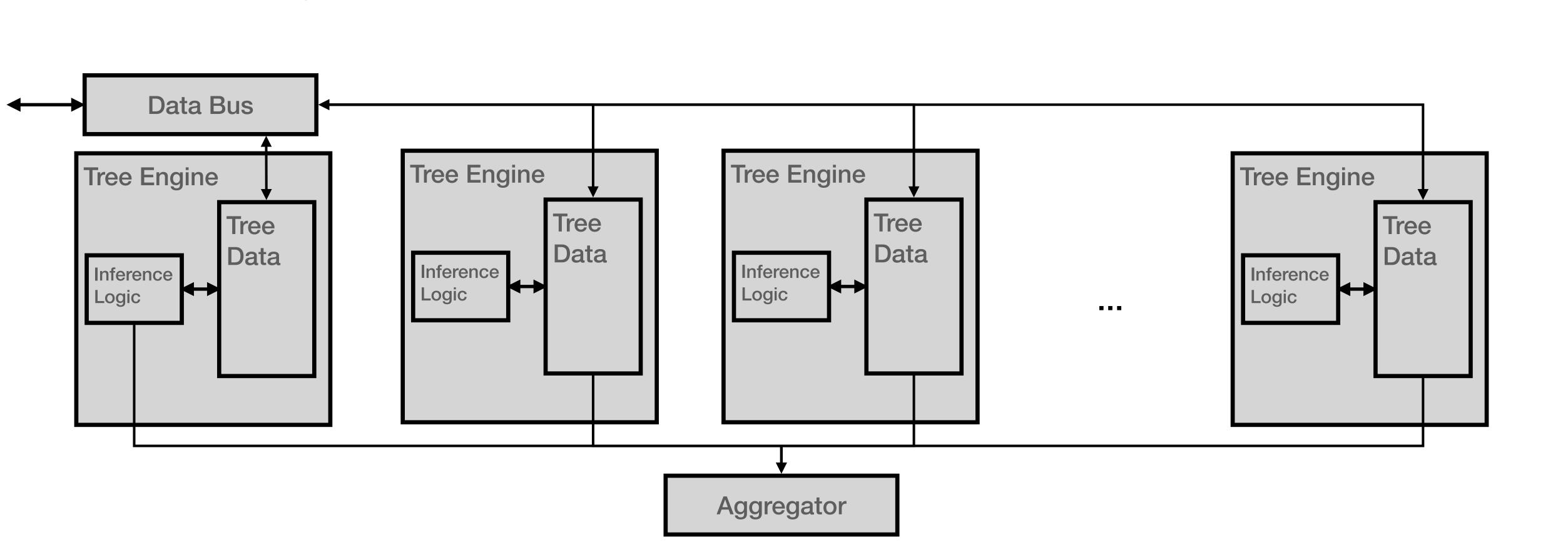
loor

| e | | | | Initiatior achieved | | | Pipelined |
|---|---|---|---|------------------------|---|---|-----------|
| p | ? | ? | 3 | 3 | 1 | ? | yes |





- Idea 2: parallelise over trees by having independent 'Tree Engines', aggregate their output for the model
- Put as many Tree Engines as will fit and achieve timing closure in the FPGA
- Number of Tree Engines will constrain the model size that fits





FPU System Design

- Putting it together
- One function that has arguments for both BDT-data and inference-data, and an 'instruction' parameter for what to do • Define the node memories as static to keep the data in between function calls
 - Load nodes once, perform inference later whenever (multiple times)
 - Later load new nodes for a different model...
- This code is a simplified view of that:

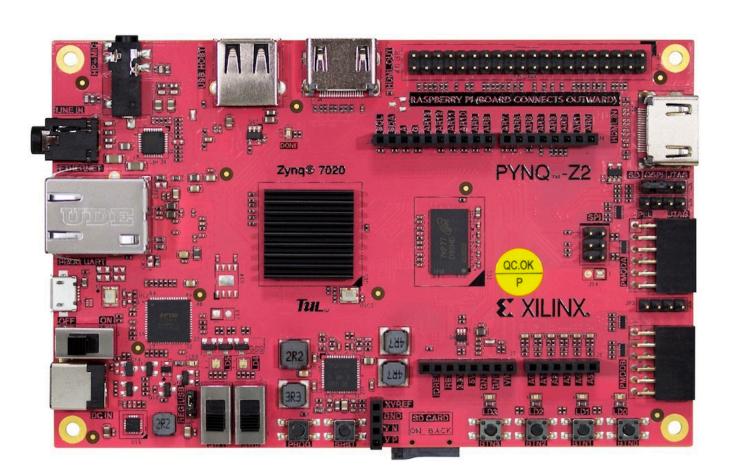
```
#pragma interface ...
static DecisionNode nodes_internal[NTE][NNODES];
#pragma HLS array_partition variable=nodes_int dim=1
if(instruction == 0){
  load_nodes(nodes, nodes_internal);
}
if(instruction == 1){
  decision_function(X, y);
```

void fpu_top_level(int* X, int* y, int instruction, DecisionNode* nodes){



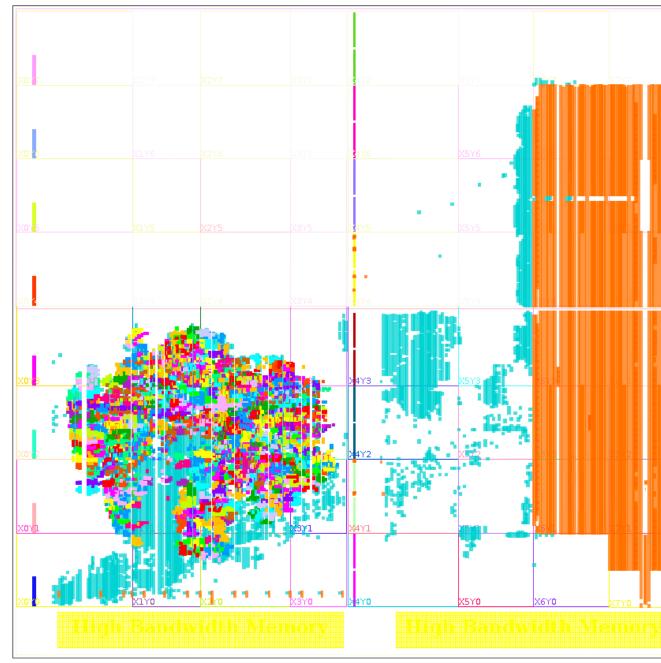
- FPU with 200 Tree Engines in Alveo U50 (top) and 100 Tree Engines in pynq-z2 (bottom)
 - Each TE is highlighted in colour (with a repeating cycle)
- BRAMs for nodes are in columns
- Logic near BRAMs is TE inference logic
- AXI Interfaces used for data bus
 - Both for loading models and inference data
- Whole design is written with HLS
 - HLS as a productivity tool

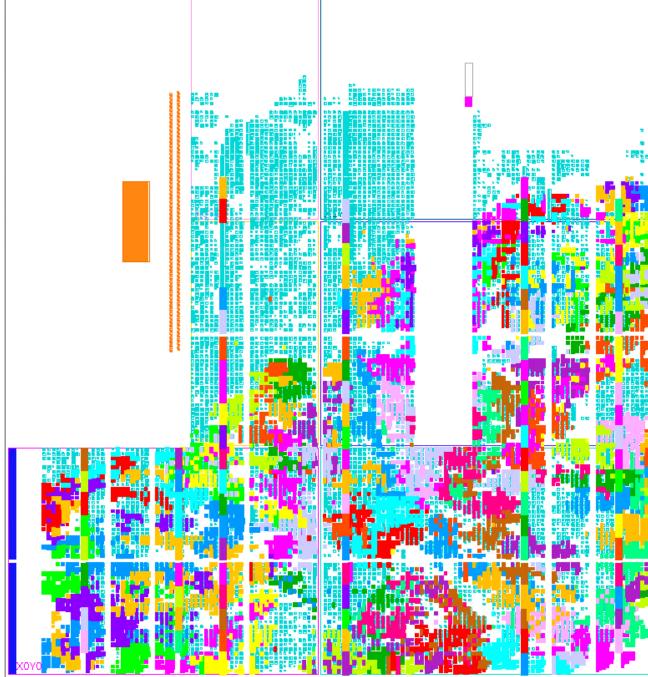




FPU Floorplan









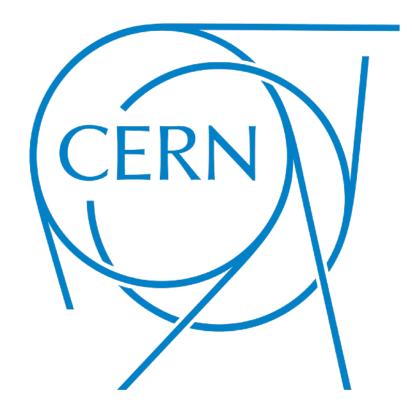


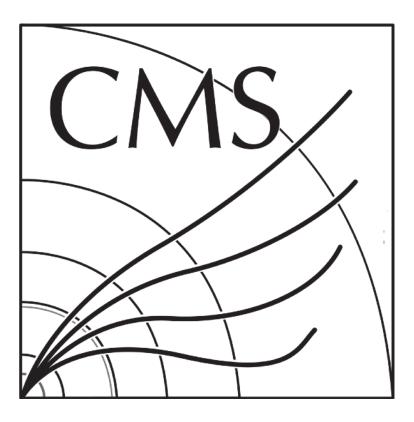


Conclusions

- **conifer** is a tool to map Decision Forests onto FPGA firmware
 - pip install conifer
- In this talk we discussed:
 - Some applications: low latency triggering, embedded frontend
 - Conifer implementation and approach to executing branched prediction
 - HLS and VHDL performance
 - Forest Processing Unit: reconfigurable Decision Forest inference architecture designed with HLS







Backup

HLS Code 1/3

- Perform all the comparisons simultaneously: unroll the loop
- Store boolean results in a fully-partitioned array "comparison"

```
// Execute all comparisons
Compare: for(int i = 0; i < n nodes; i++) {
  #pragma HLS unroll
  // Only non-leaf nodes do comparisons
  // negative values mean is a leaf (sklearn: -2)
  if(feature[i] \ge 0) {
    comparison[i] = x[feature[i]] <= threshold[i];</pre>
  }else{
    comparison[i] = true;
```



HLS Code 2 / 3

• Compute the node activation (true if decision path traverses node, otherwise false)

```
// Determine node activity for all nodes
int iLeaf = 0;
Activate: for(int i = 0; i < n nodes; i++) {
  #pragma HLS unroll
  // Root node is always active
  if(i == 0){
    activation[i] = true;
  }else{
    // If this node is the left child of its parent
    if(i == children left[parent[i]]) {
    }else{ // Else it is the right child
  // Skim off the leaves
  if(children left[i] == -1) { // is a leaf
    activation leaf[iLeaf] = activation[i];
    value_leaf[iLeaf] = value[i];
    iLeaf++;
```

activation[i] = comparison[parent[i]] && activation[parent[i]]; activation[i] = !comparison[parent[i]] && activation[parent[i]];



HLS Code 3/3

• Compute the node activation (true if decision path traverses node, otherwise false)

```
for(int i = 0; i < n leaves; i++) {</pre>
   if(activation_leaf[i]) {
     return value_leaf[i];
   }
```



VHDL

- To the right is the VHDL version of the tree traversal is shown in HLS on the previous slides
- The main difference is that we have to do the scheduling of operations to clock cycles ourselves in VHDL
 - The latency of this section of code depends on the maximum depth of the tree
 - This VHDL is "over pipelined" compared to the HLS

GenAct:

```
activation(0) <= true; -- the root node is always active
for i in 1 to nNodes-1 generate
  LeftChild:
  if i = iChildLeft(iParent(i)) generate
    process(clk)
    begin
      if rising_edge(clk) then
        activation(i) <= comparisonPipe(depth(i))(iParent(i))</pre>
                          and activation(iParent(i));
      end if;
    end process;
  end generate LeftChild;
  RightChild:
  if i = iChildRight(iParent(i)) generate
    process(clk)
    begin
      if rising_edge(clk) then
        activation(i) <= (not comparisonPipe(depth(i))(iParent(i)))</pre>
                           and activation(iParent(i));
      end if;
    end process;
  end generate RightChild;
end generate GenAct;
```



