



Instituto de  
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Teórica  
UAM-CSIC

**UAM**  
Universidad Autónoma  
de Madrid



# Gravitational Waves from Hidden Sectors

Particle Production in the Early Universe — CERN, Sept. 9–13, 2024

Eric Madge (IFT-UAM/csIC)

based on: Breitbach et al., JCAP **07** (2019) 007

Banerjee et al., PRD **104** (2021) 5

Madge et al., SciPost Phys. **12** (2022) 5, 171

Madge et al., JHEP **10** (2023) 171

Caprini et al. (LISA CosWG), arXiv:2403.03723 [astro-ph.CO]

# GWs from Hidden Sectors

[image credit: ChatGPT/DALL-E]

## cosmological sources

inflation



bosonic instabilities



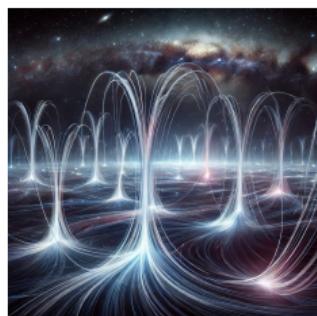
thermal fluctuations



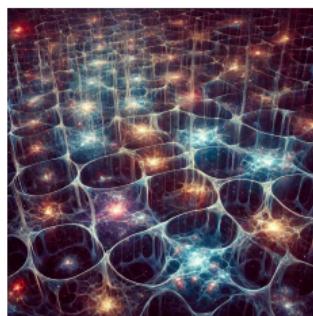
phase transitions



cosmic strings



domain walls



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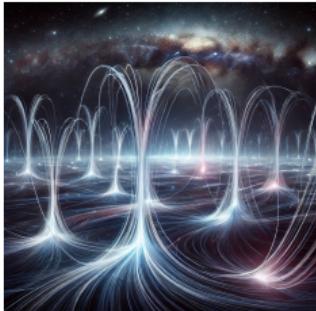
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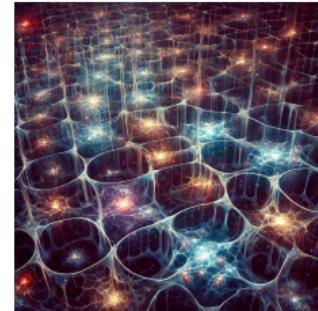
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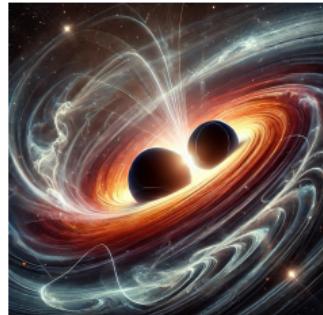


domain walls



## astrophysics

binary mergers



exotic objects



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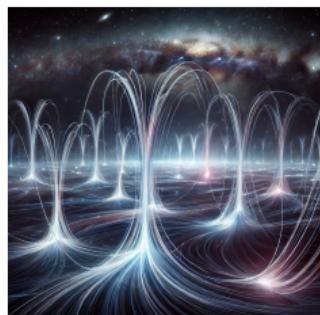
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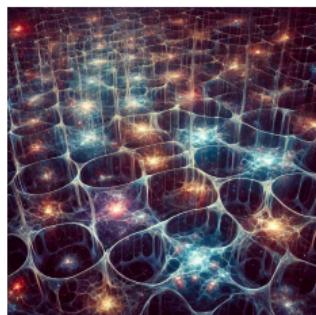
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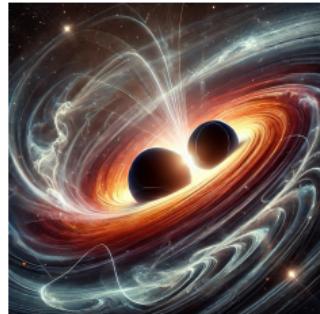


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# SGWB from Primordial Sources

peak frequency

set by characteristic scale  $f_*^{-1}$  at  
production:  $f_*^{-1} \lesssim H_*^{-1}$



$$f_0 \sim \frac{a_0}{a_*} H_* \frac{f_*}{H_*}$$
$$\sim 0.1 \text{ mHz} \left( \frac{T_*}{1 \text{ TeV}} \right) \left( \frac{f_*}{H_*} \right)$$

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peak amplitude

$$\rho_{\text{GW}} \sim M_{\text{pl}}^2 \langle h_{ij} h_{ij} \rangle, \quad \square \bar{h}_{\mu\nu} \sim \frac{T_{\mu\nu}}{M_{\text{pl}}^2}$$



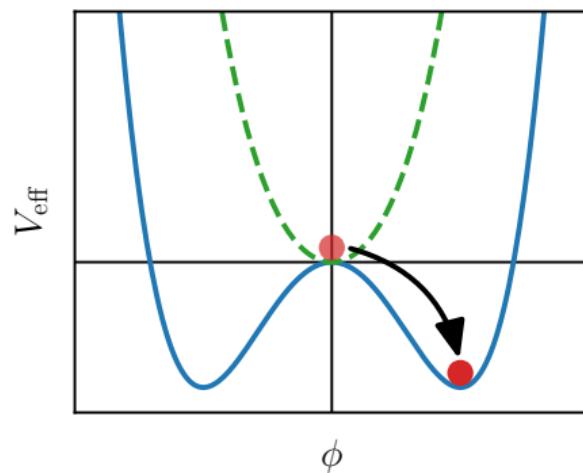
$$\Omega_{\text{GW}} \sim \left( \frac{a_*}{a_0} \right)^4 \frac{1}{\rho_c} \frac{\rho_{\text{source}}^2}{f_*^2 M_{\text{pl}}^2}$$
$$\sim \left( \frac{a_*}{a_0} \right)^4 \left( \frac{H_0}{H_*} \right)^2 \left( \frac{H_*}{f_*} \right)^2 \Omega_{\text{source}}^2$$

# Cosmological Phase Transition

1. Cosmological Phase Transition
2. Bosonic Instabilities
3. Conclusions

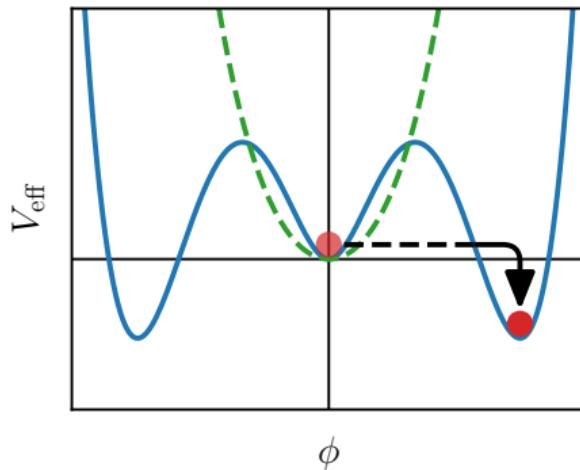
# Cosmological Phase Transitions

- thermal corrections typically restore spontaneously broken symmetries at high temperatures  
➡ symmetry breaking phase transition
- can be **crossover** or first-order



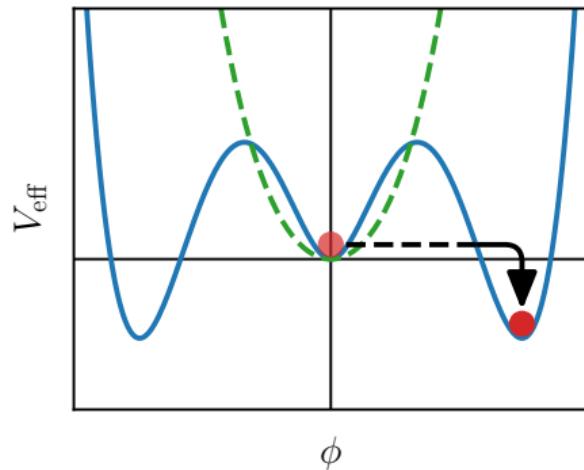
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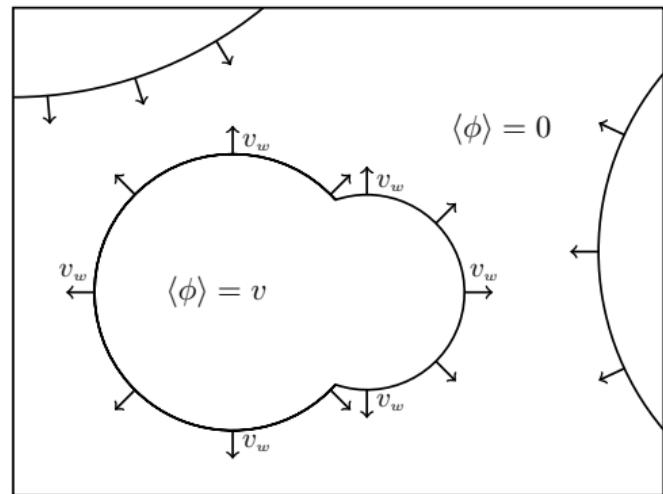
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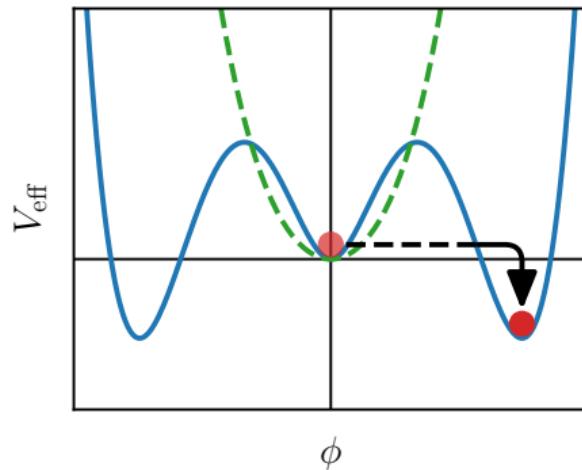
GW production:

1. vacuum bubble collisions



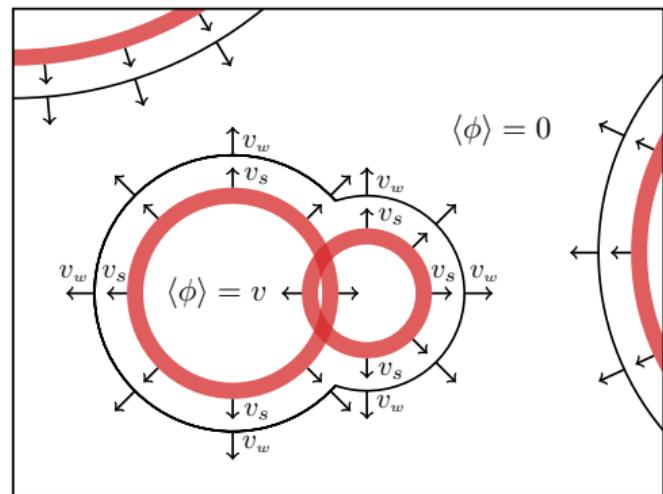
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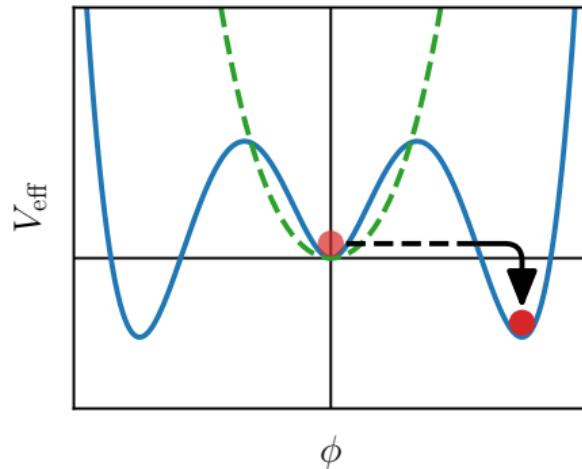
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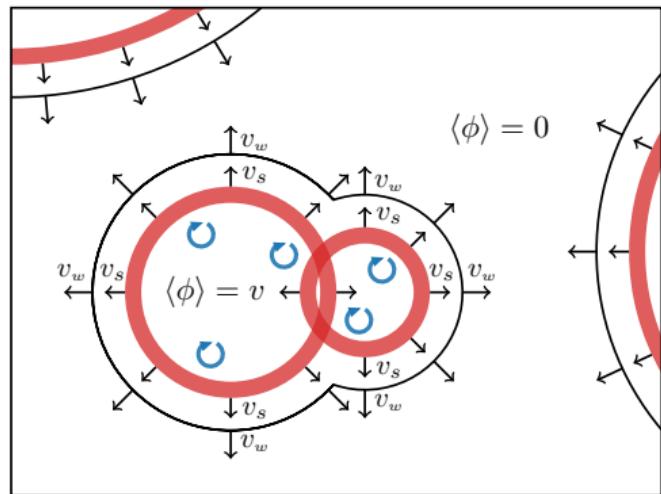
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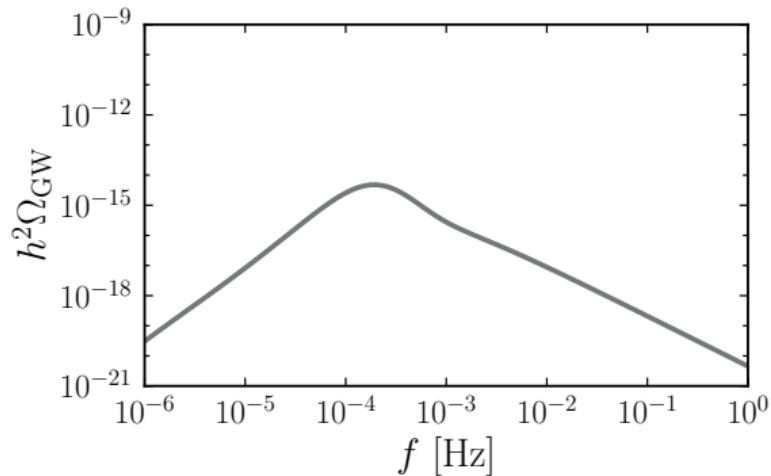
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3. turbulence and vortical motion



# Phase Transition Parameters and Gravitational Wave Spectrum

Gravitational Wave spectrum obtained from numerical simulations and analytical arguments, expressed in terms of few parameters:



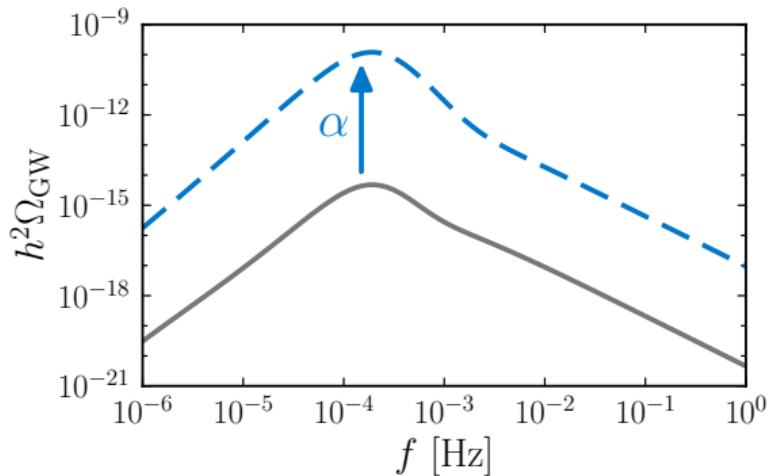
$$\begin{aligned} \text{critical action: } S_{\text{crit}} &= \frac{1}{T} \int d^3x \left[ \frac{1}{2} (\nabla \phi)^2 + V_{\text{eff}}(\phi, T) \right] \\ \text{nucleation rate: } \Gamma(T) &= A(T) \exp \left[ -S_{\text{crit}}(T) \right] \end{aligned}$$

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Gravitational Wave spectrum obtained from numerical simulations and analytical arguments, expressed in terms of few parameters:

strength/  
energy budget

$$\alpha = \frac{\rho_{\text{vac}}}{\rho_{\text{rad}}^*} \simeq \frac{\Delta V_{\text{eff}}}{\rho_{\text{rad}}^*}$$



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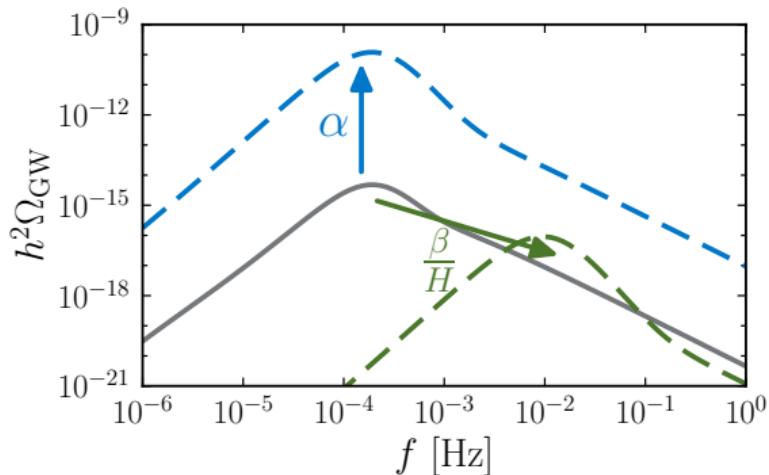
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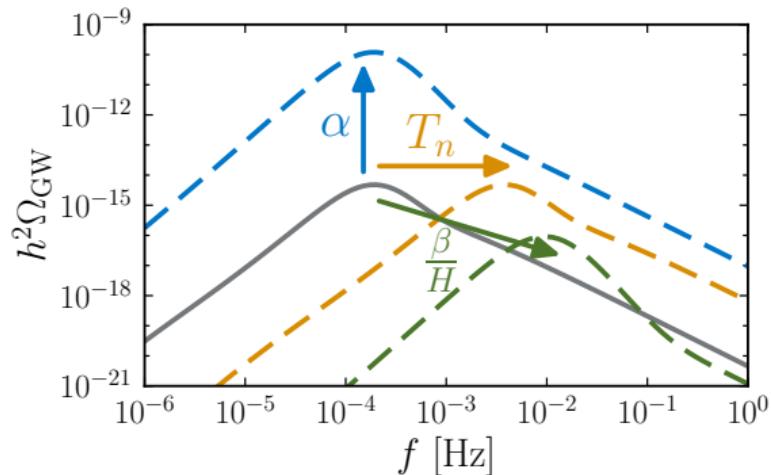
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$$T_* \simeq T_n \quad (\Gamma(T_n) \simeq [H(T_n)]^4)$$



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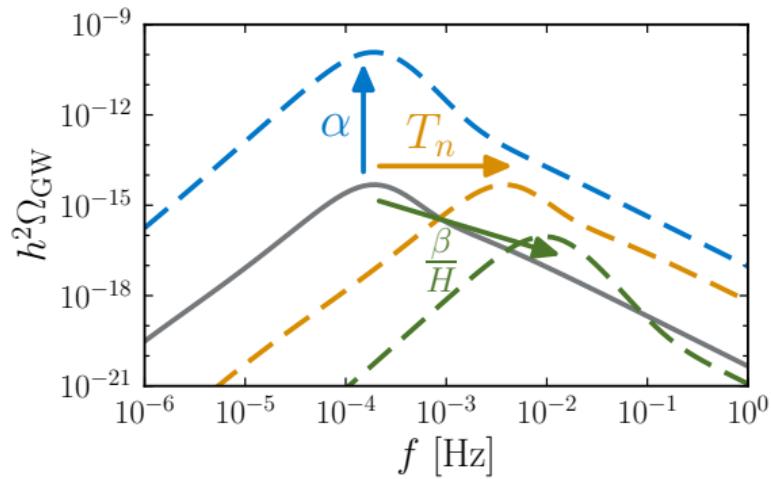
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also: bubble dynamics:

wall velocity, efficiency factors, etc.



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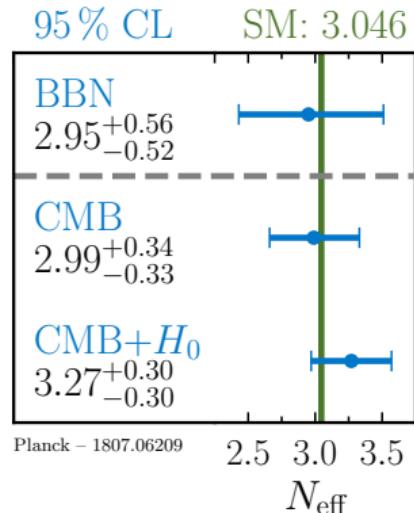
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# Decoupled Hidden Sectors

- sub-MeV hidden sectors contribute to the effective number of neutrino species  $N_{\text{eff}}$

$$\rho_{\text{rad}} = \frac{\pi^2}{30} \sum_i g_i T_i^4 = \left[ 1 + \frac{7}{8} \left( \frac{4}{11} \right)^{\frac{4}{3}} N_{\text{eff}} \right] \rho_{\gamma}$$

- at  $T \lesssim \text{MeV}$ :  
additional relativistic DOFs in thermal equilibrium with photons are excluded

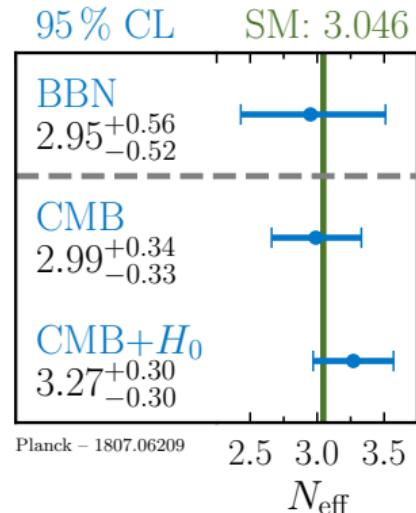


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⇒ sub-MeV hidden sector must be **colder** than SM

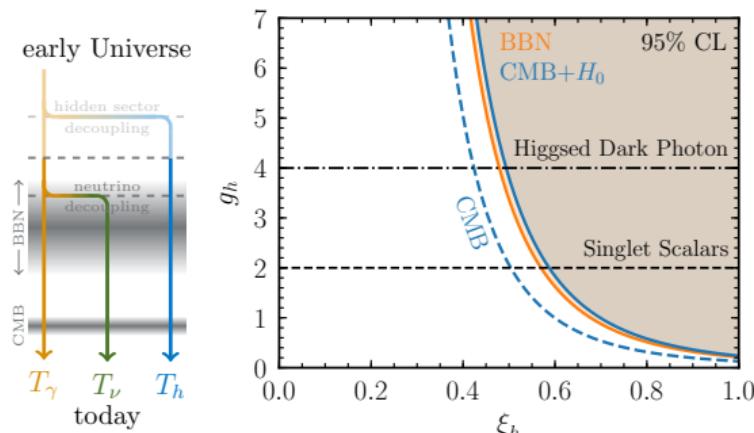
# Hidden Sector Cosmology

Breitbach et al. (JCAP, 2019)

completely decoupled

$$\xi_h \equiv \frac{T_h}{T_\gamma} < 1$$

$$N_{\text{eff}} = N_{\text{eff}}^{\text{SM}} + \frac{4}{7} \left( \frac{11}{4} \right)^{\frac{4}{3}} g_h \xi_h^4$$



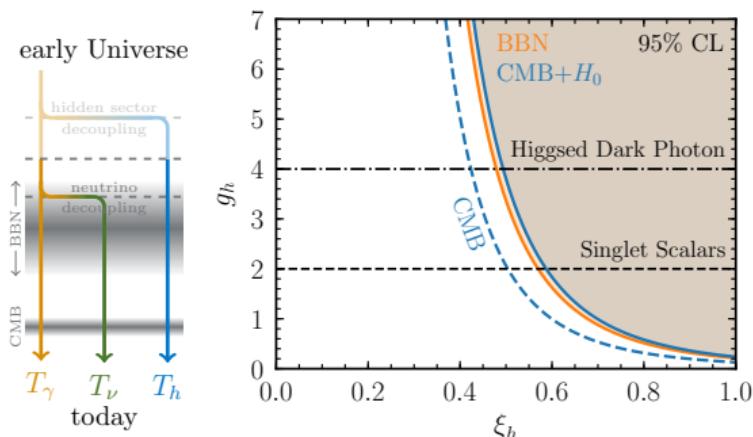
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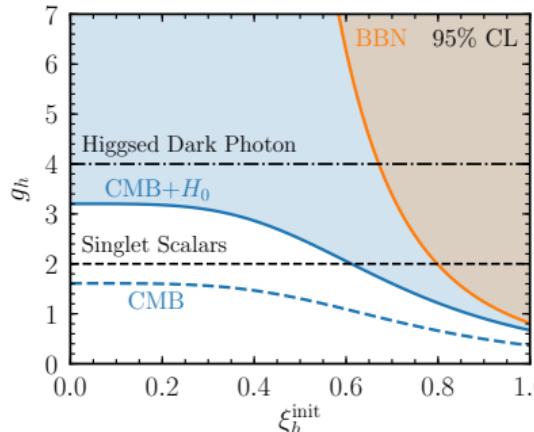
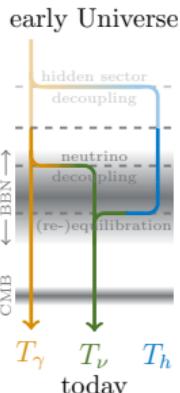
$\nu$ -quilibration

CMB

$$N_{\text{eff}} = N_{\text{eff}}^{\text{SM}} \left[ 1 + \frac{g_h}{g_\nu} (\xi_h^{\text{init}})^4 \right] \left[ 1 + \frac{g_h}{g_\nu} \right]^{\frac{1}{3}}$$

BBN

early Universe



# Phase Transitions in Secluded Hidden Sectors

Breitbach et al. (JCAP, 2019)  
Fairbairn et al. (JHEP, 2019)

temperature ratio:  $\xi_h \equiv \frac{T_h}{T_\gamma}$

- $\alpha \simeq \alpha_h \xi_h^4$        $\alpha_h \equiv [\alpha]_{\xi_h=1}$

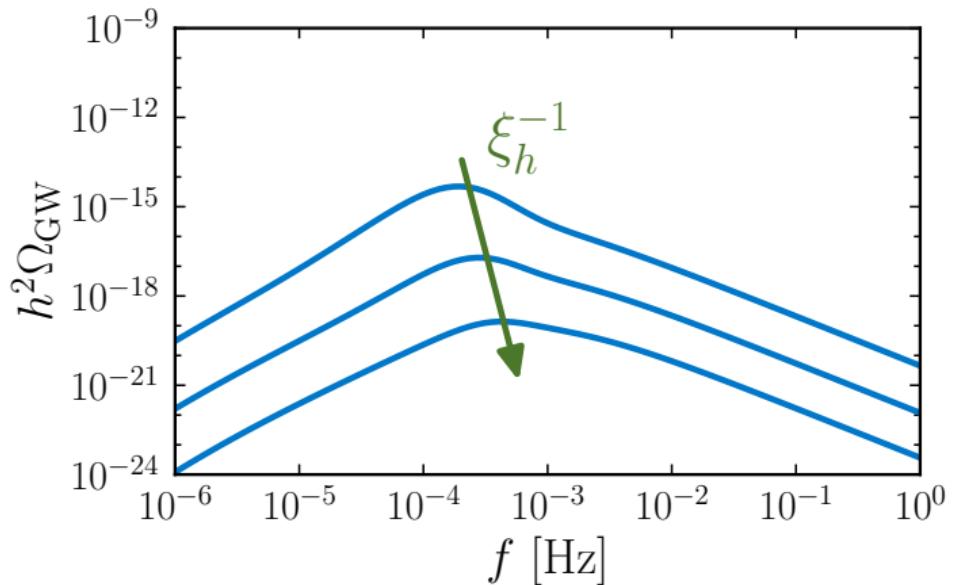
- $f_{\text{peak}}^0 \sim T_{n,\gamma} = \frac{T_{n,h}}{\xi_h}$

- $\frac{\beta}{H}$   $\xi_h$ -independent

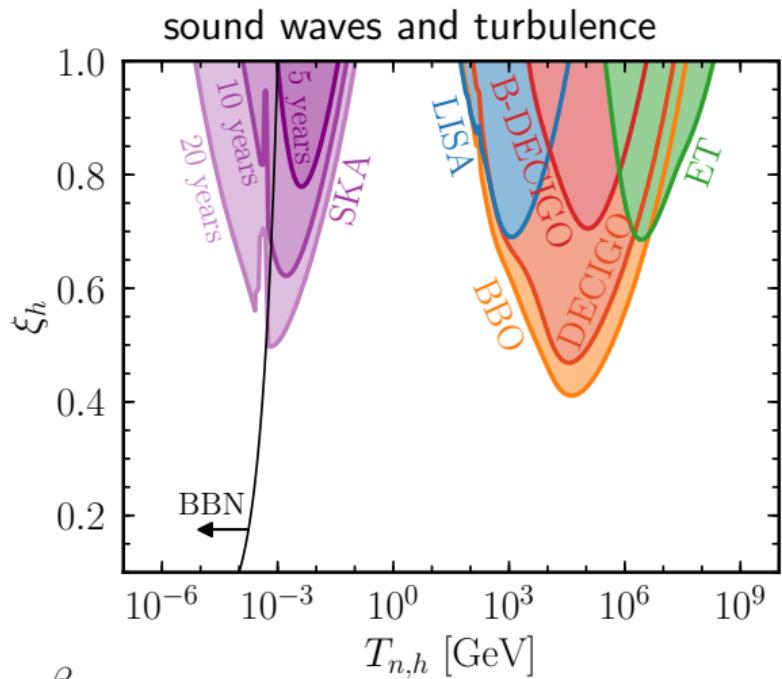
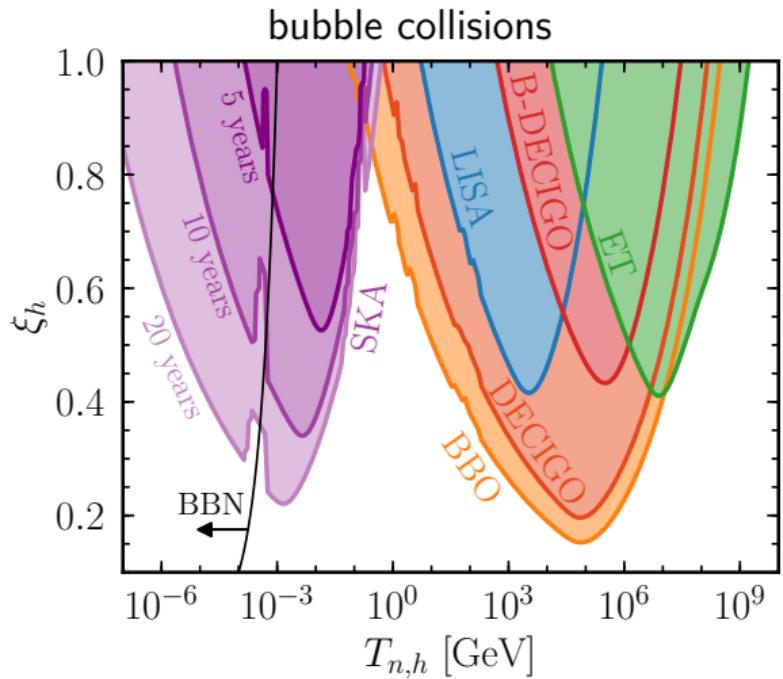
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# Sensitivity



$$\alpha_h = 0.1, \quad \frac{\beta}{H_*} = 10$$

# Parameter Reconstruction

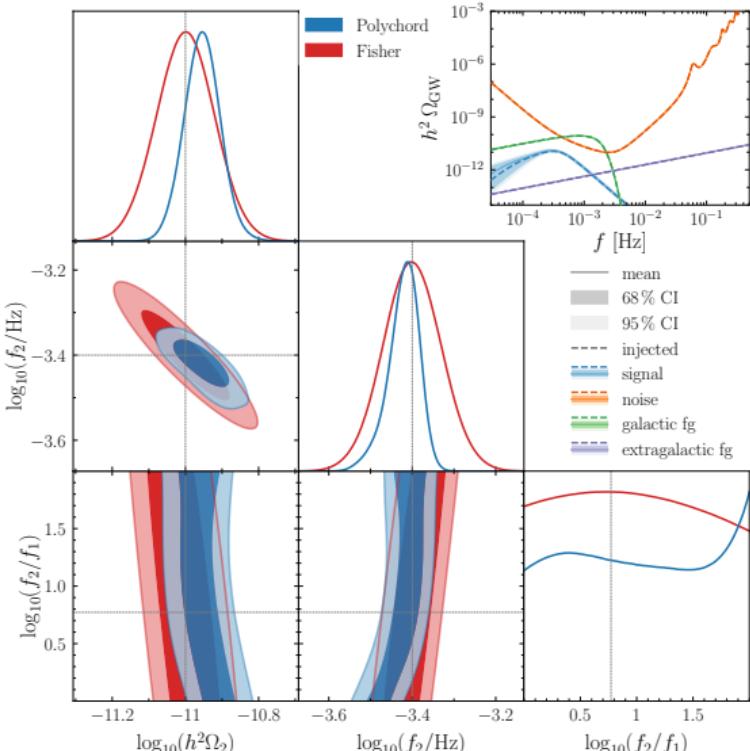
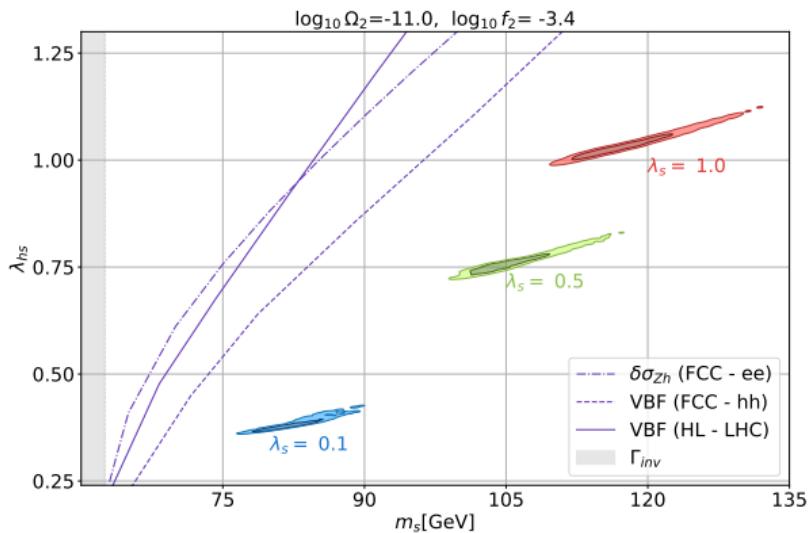
Caprini et al. arXiv:2403.03723 [astro-ph.Co]

Lewicki et al. (JHEP, 2022); Ellis et al. (JHEP, 2023)

SGWBinner: Caprini et al. (JCAP, 2019); Flauger et al. (JCAP, 2021)

example: singlet w/  $\mathbb{Z}_2$  symmetry

$$\Delta\mathcal{L} = -\frac{\mu_s^2}{2} s^2 - \frac{\lambda_s}{4} s^4 - \frac{\lambda_{hs}}{2} s^2 H^\dagger H$$



# Bosonic Instabilities

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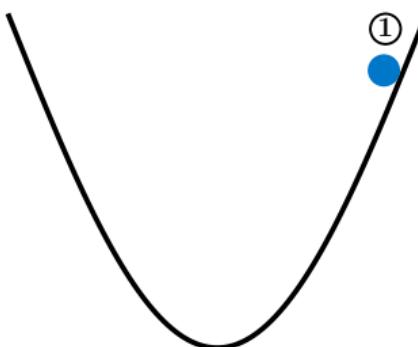
# Bosonic Instabilities: Audible Axions

Machado et al. (JHEP 2019, PRD 2020)  
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## Misalignment Mechanism

$$\mathcal{L} \supset \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - V(\phi)$$

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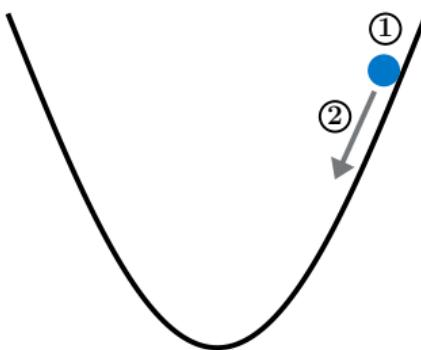
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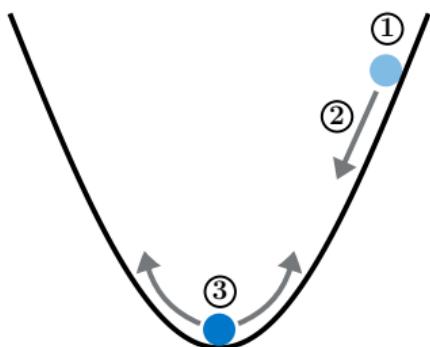
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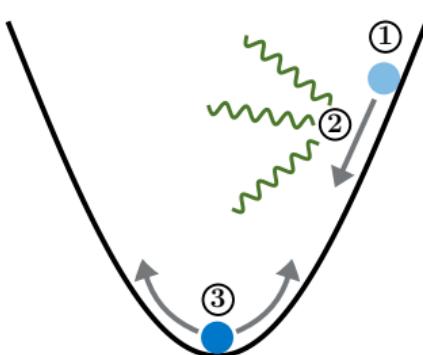
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e.g. to deplete axion abundance  
Agrawal et al. (JHEP, 2018)  
Kitajima et al. (PLB 2018)  
or for dark-photon dark-matter  
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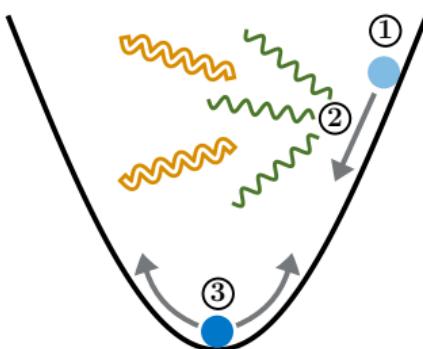
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- ⇒ gravitational wave emission from dark photons

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dark photon EoM:  $X''_{\pm}(\tau, k) + \omega_{\pm}^2(k)X_{\pm}(\tau, k) = 0$        $\omega_{\pm}^2(k) = \left( k^2 \mp k \frac{\alpha\phi'(\tau)}{f_a} \right)$

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- largest growth for  $\tilde{k} = \left| \frac{\alpha \phi'(\tau)}{2 f_a} \right|$  with  $|\omega^2(\tilde{k})| = \tilde{k}^2$

# Dark Photon Production

dark photon EoM:

$$X''_{\pm}(\tau, k) + \omega_{\pm}^2(k) X_{\pm}(\tau, k) = 0$$

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➡  $\sim$  energy transfer stops

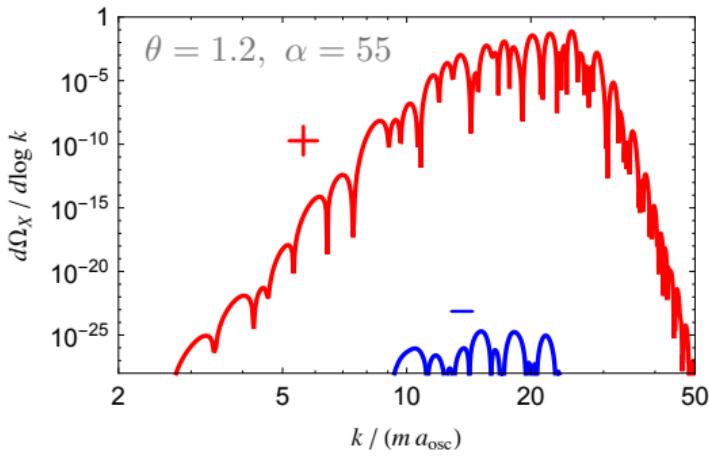
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➡ ~ energy transfer stops



[Machado et al. (JHEP 2019)]

dark photon spectrum:

- peaked around  $\tilde{k} \approx a_{\text{osc}} m_a (\alpha \theta / 2)^{2/3}$
- first tachyonic helicity dominates

# Gravitational Wave Spectrum

GWs generated at  $t_*$  around the time when the tachyonic band closes:

- peak frequency:

$$f_{\text{peak}} \sim 2 \frac{\tilde{k}_*}{a_0} \sim 4 \text{ nHz} \left( \frac{\alpha \theta}{100} \right)^{\frac{2}{3}} \left( \frac{m_a}{10^{-15} \text{ eV}} \right)^{\frac{1}{2}}$$

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■ peak amplitude:

$$\Omega_{\text{GW}}^{\text{peak}} \sim \frac{\left( \rho_X^*/f_{\text{peak}}^* \right)^2}{\rho_c M_{\text{pl}}^2} \left( \frac{a_*}{a_0} \right)^4 \sim 10^{-7} \left( \frac{f_a}{M_{\text{pl}}} \right)^4 \left( 100 \frac{\theta^2}{\alpha} \right)^{\frac{4}{3}}$$

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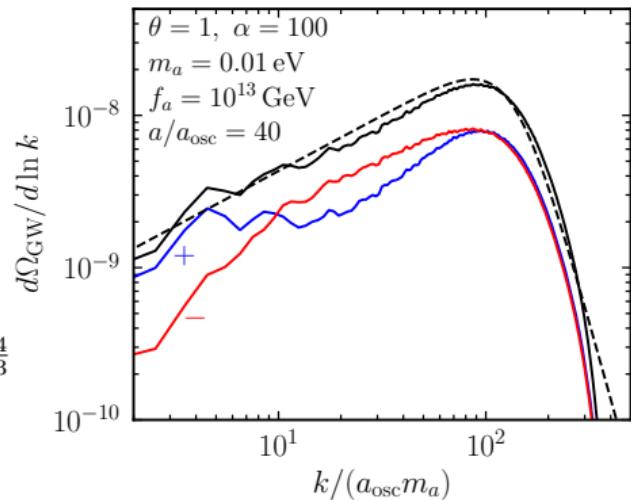
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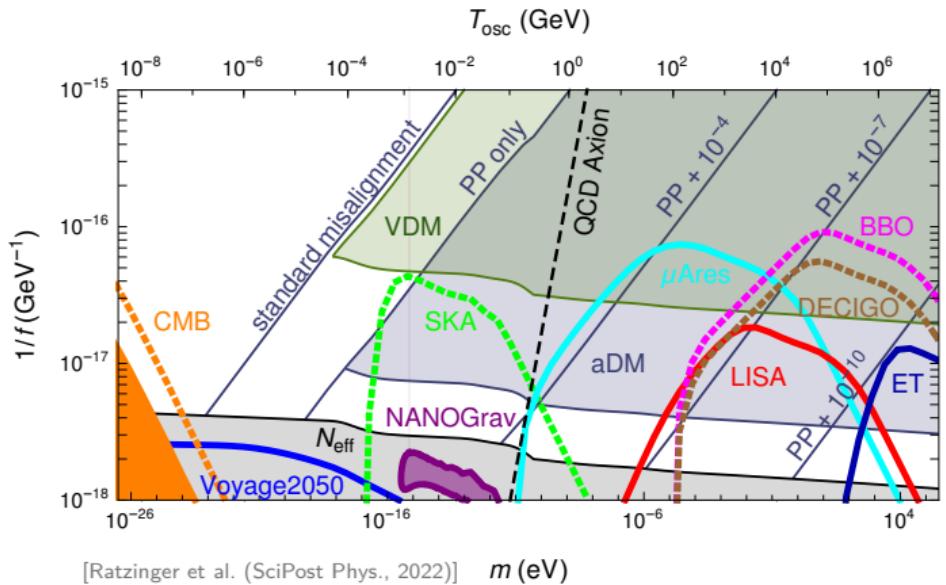
## ■ spectral shape from lattice:

[Ratzinger, Schwaller, Stefanek (SciPost Phys. 2022)]

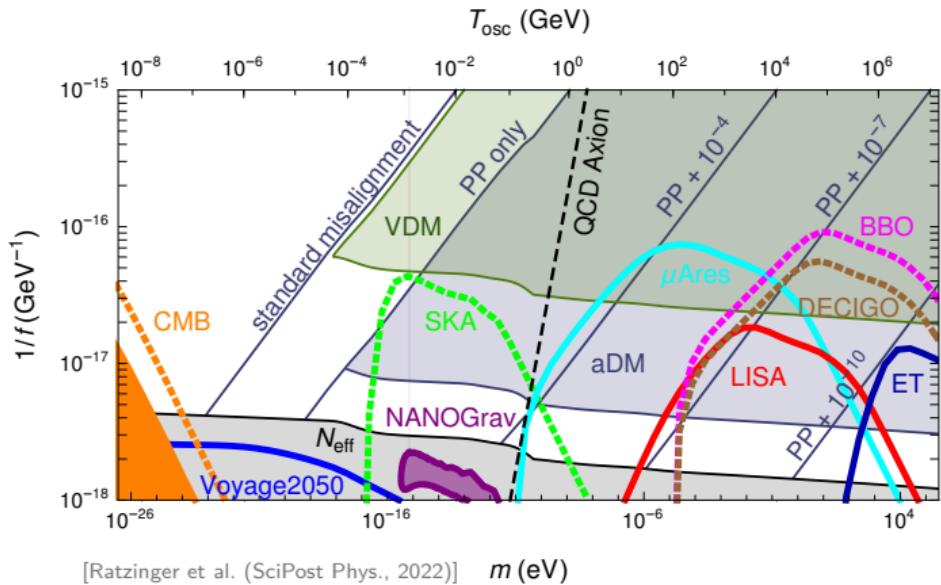
$$\Omega_{\text{GW}} = \Omega_{\text{GW}}^{\text{peak}} \mathcal{S}(f/f_{\text{peak}}), \quad \mathcal{S}(x) = x^{0.73} \left[ \frac{1}{2} \left( 1 + x^{4.2} \right) \right]^{\frac{-4.96 - 0.73}{4.2}}$$



# Parameter Constraints

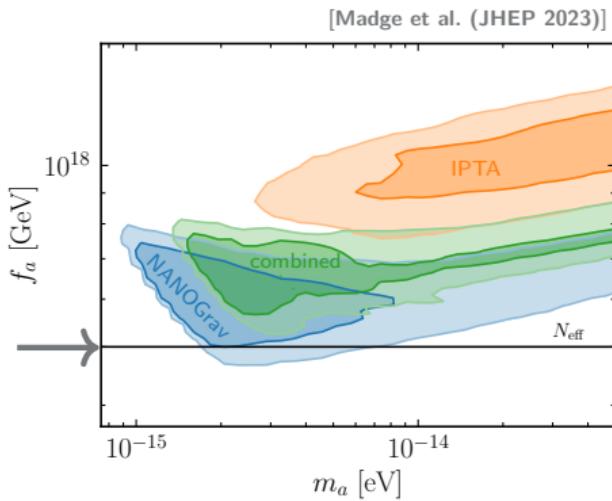


# Parameter Constraints



$$\Delta N_{\text{eff}} \sim 9.1 \left( \frac{\theta f_a}{M_{\text{pl}}} \right)^2$$

(also:  $\Omega_a > \Omega_{\text{DM}}$ )

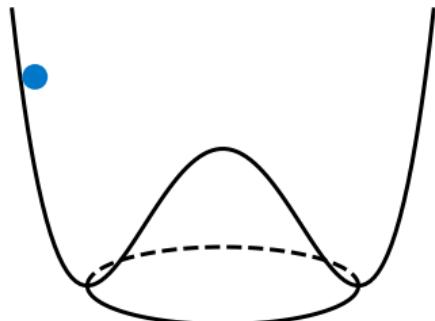


# Kinetic Misalignment

Co, Harigaya (PRL, 2020)  
Co et al. (PRL, 2020)

misalignment + large initial velocity  $\implies$  DM abundance and GW amplitude set by  $\dot{\phi}_0$

- complex scalar  $P$  with  $V(P) \sim |P|^4$  and initial displacement  $|P| \gg f_a$

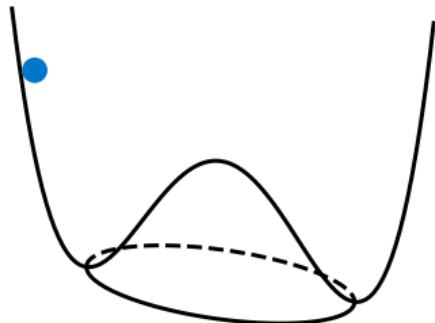


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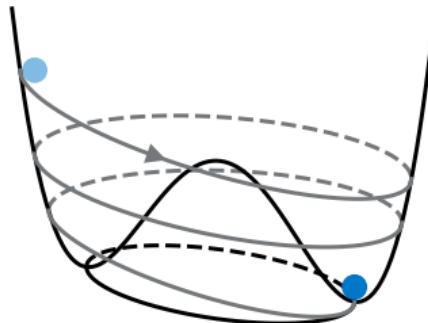


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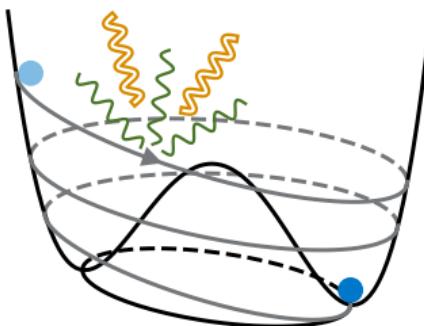


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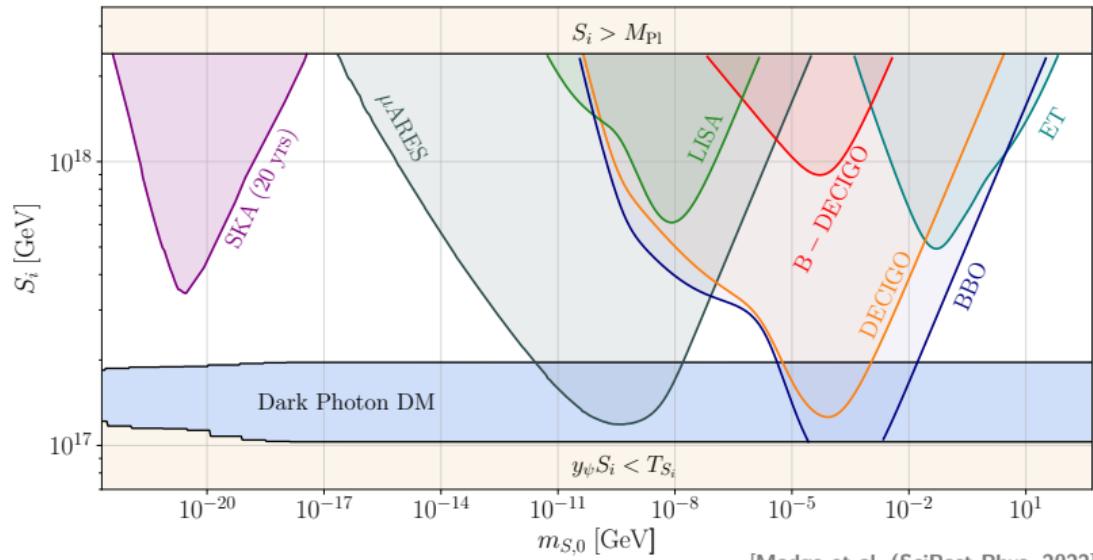
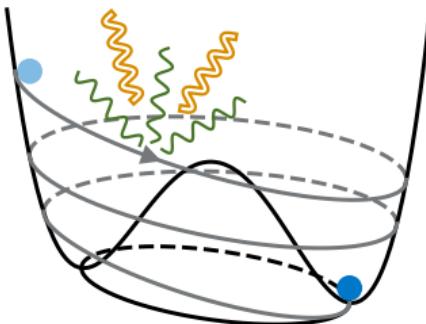
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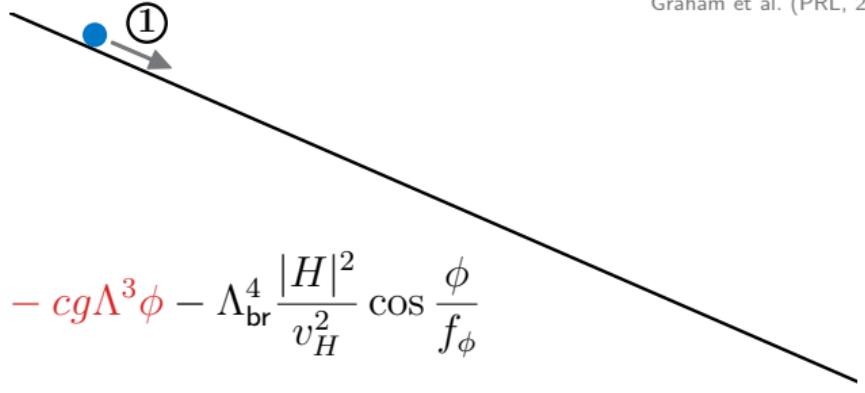
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# Relaxion

Graham et al. (PRL, 2015)

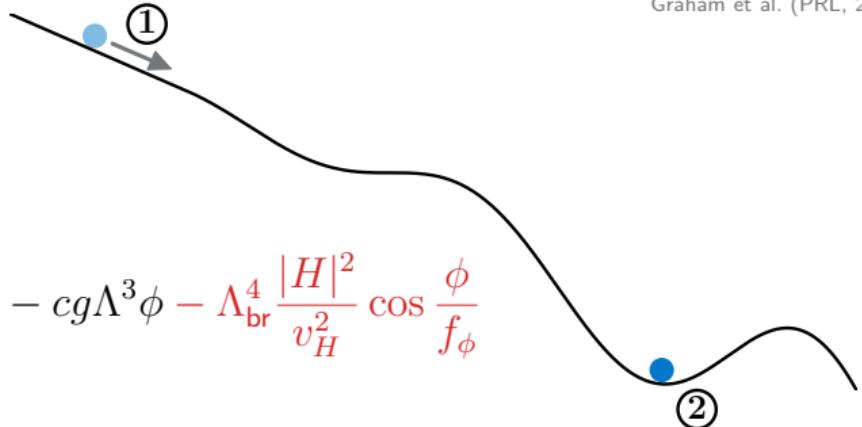


$$V(H, \phi) = \underbrace{\left( \Lambda^2 - g\Lambda\phi \right)}_{\mu_H^2(\phi)} |H|^2 + \lambda |H|^4 - cg\Lambda^3\phi - \Lambda_{\text{br}}^4 \frac{|H|^2}{v_H^2} \cos \frac{\phi}{f_\phi}$$

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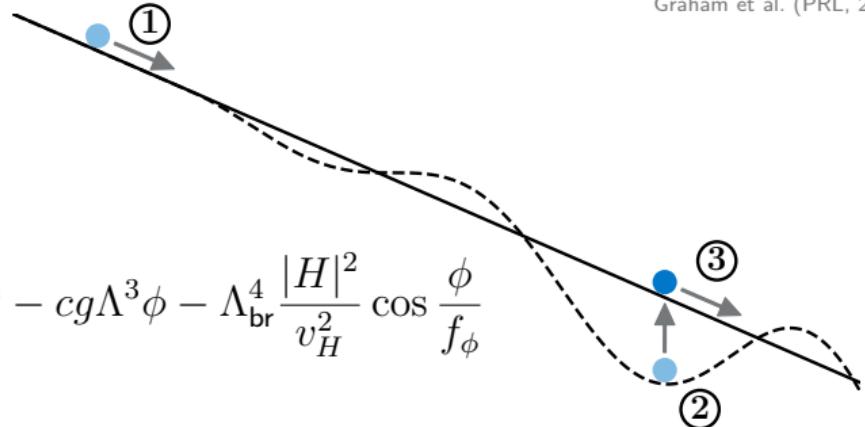


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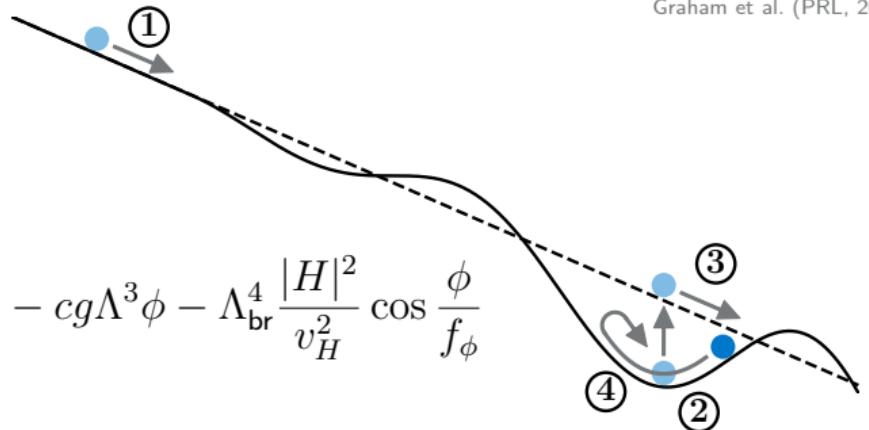
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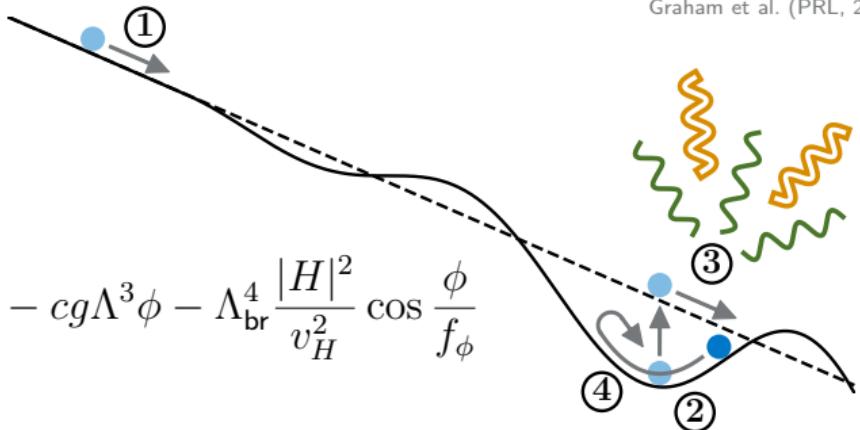


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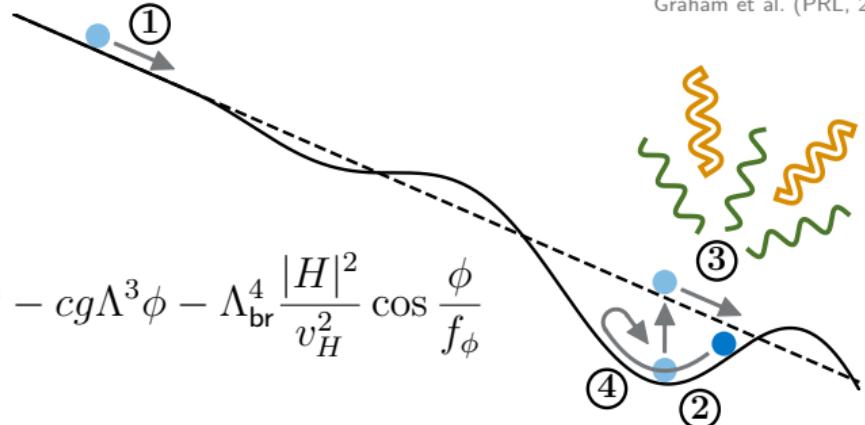


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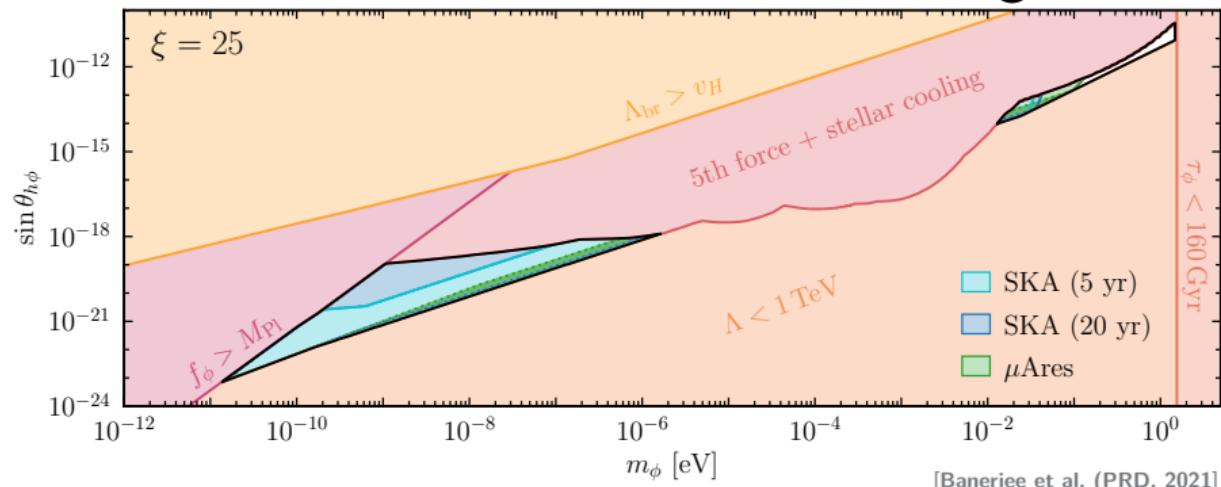
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# Conclusions

1. Cosmological Phase Transition
2. Bosonic Instabilities
3. Conclusions

# Conclusion

- Hidden sectors can generate GWs in several ways
- The hidden sector can be decoupled
  - ➡ GW spectrum suppressed:  $f_{\text{peak}}^0 \sim \xi_h$ ,  $\alpha \sim \xi_h^4$
- ALPs coupled to dark photons can produce SGWB via tachyonic instability

Thank you for your attention!



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Teórica  
UAM-CSIC

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Universidad Autónoma  
de Madrid



# Gravitational Waves from Hidden Sectors

Particle Production in the Early Universe — CERN, Sept. 9–13, 2024

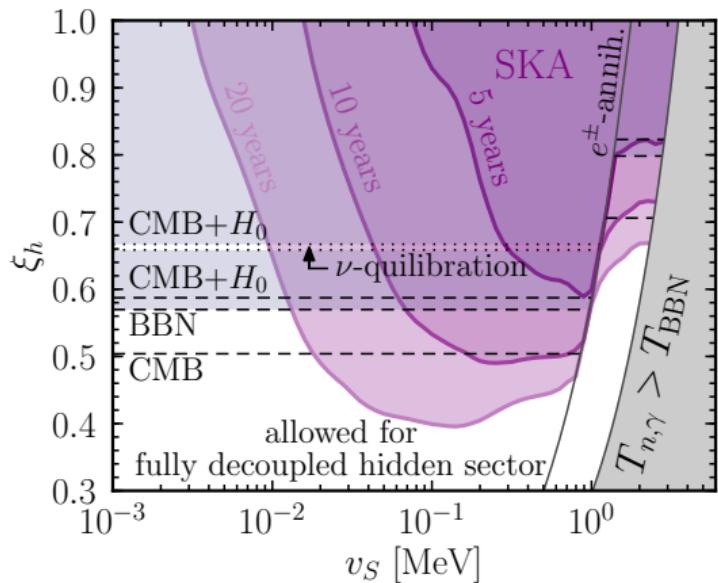
Eric Madge (IFT-UAM/csic)

backup slides

# Hidden Sector Benchmark Models

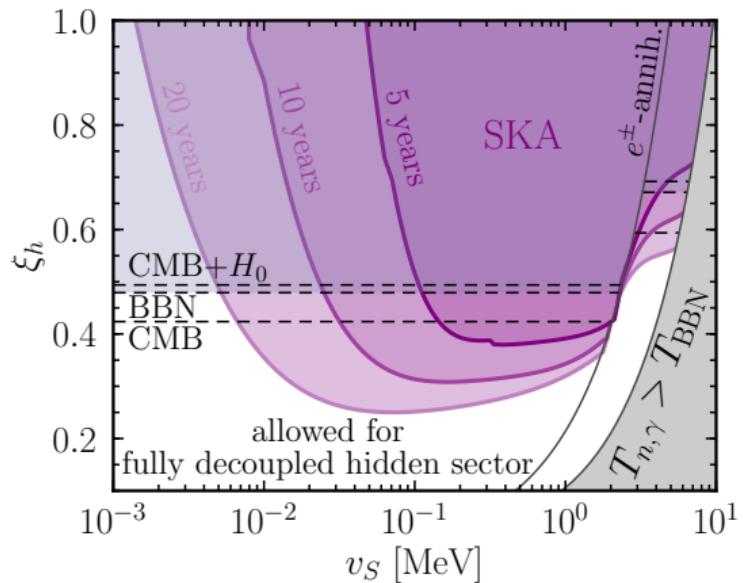
## Singlet Scalars:

- 2 real scalars  $S$  and  $A$
- $\langle S \rangle = v_S, \langle A \rangle = 0, A$   $Z_2$ -odd

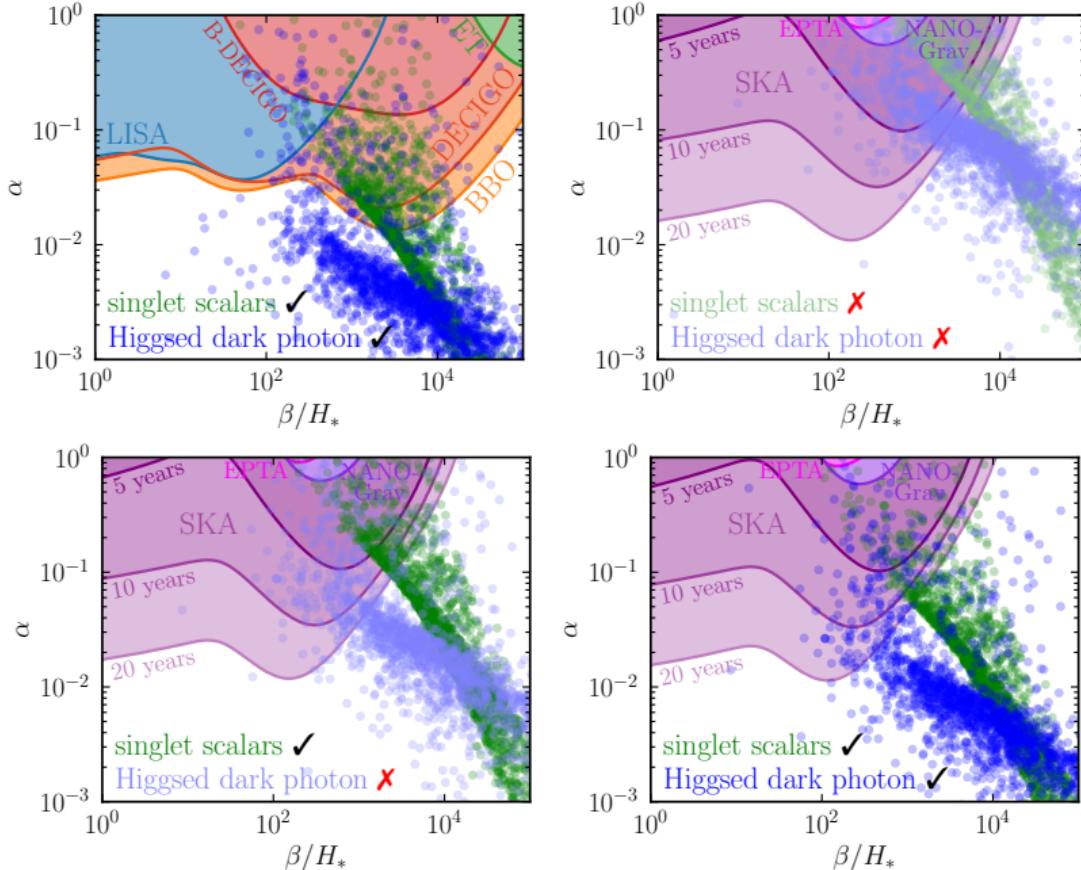


## Dark Photon:

- complex SM singlet scalar
- charged under dark  $U(1)_D$



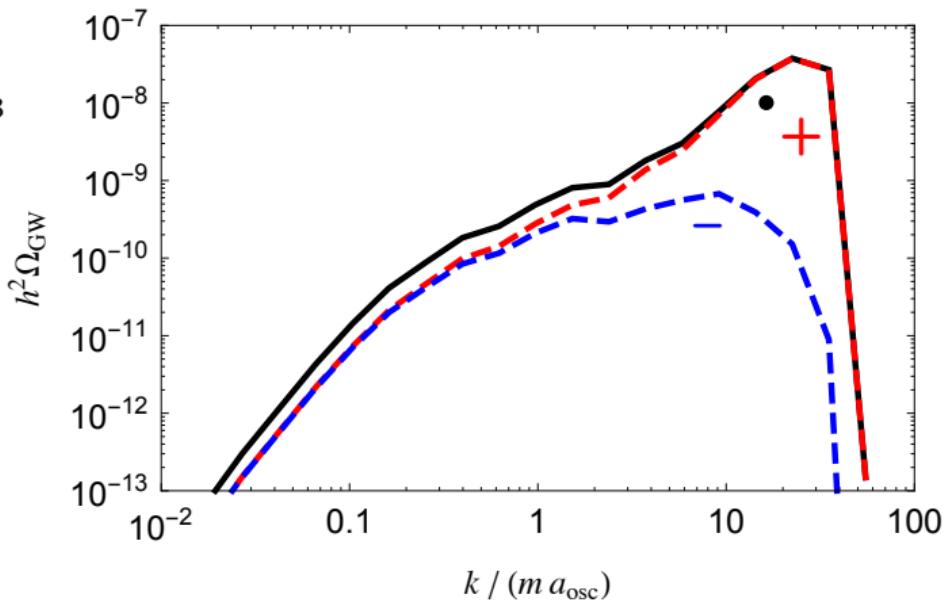
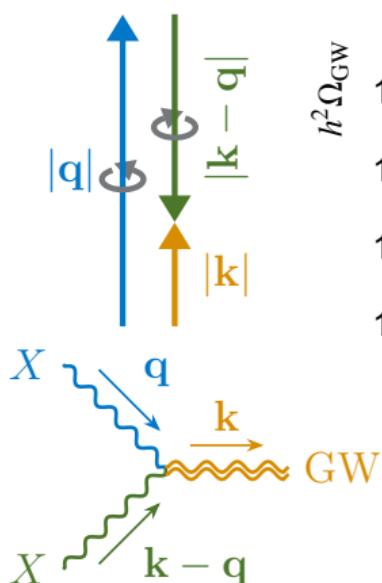
# Hidden Sector Phase Transition Detectability



# Audible Axion GW Spectrum

$f \ll f_{\text{peak}}$ :

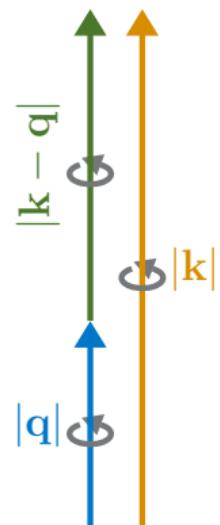
- unpolarized
- causality:  $\sim f^3$



[Machado et al. (JHEP, 2019)]

$f \gg f_{\text{peak}}$ :

- polarized
- $|\mathbf{k} - \mathbf{q}| > \tilde{k}_{\text{osc}}$
- $\Rightarrow$  exp. suppression

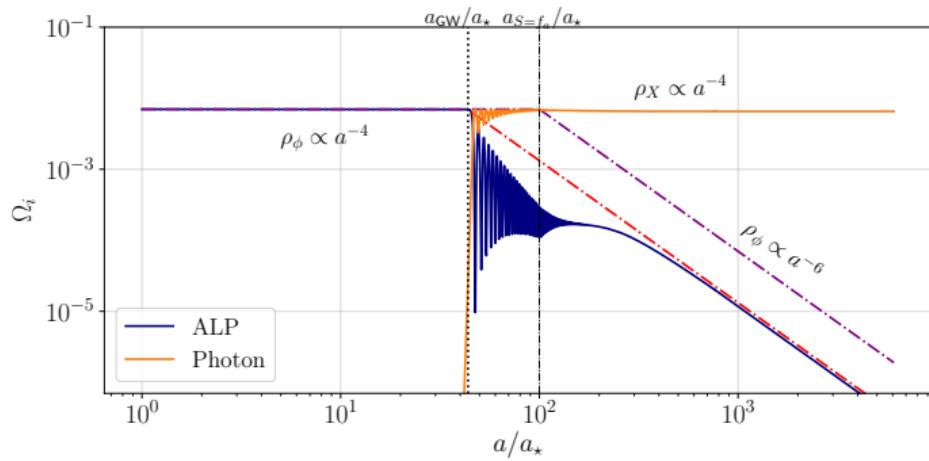
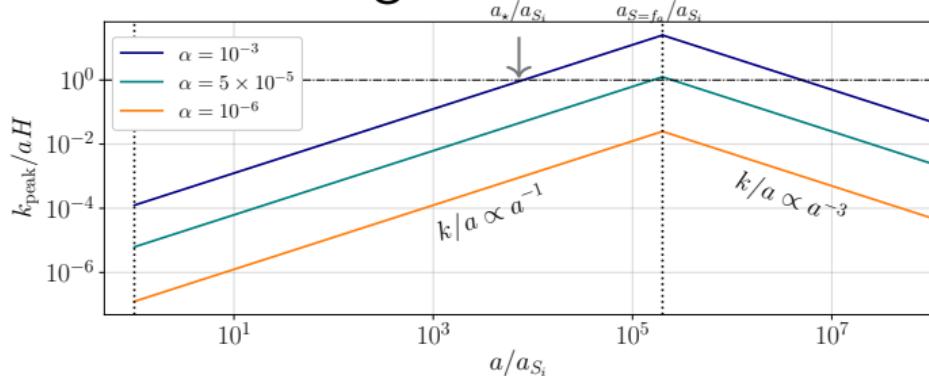


# Dark Photon Production in Kinetic Misalignment

$$X''_{\pm} + \left( k^2 \mp k \frac{\alpha \phi'}{S} \right) X_{\pm} = 0$$

$$\implies \tilde{k} = \frac{\alpha \phi'}{2S} \sim \begin{cases} \text{const.}, & S > f_{\phi} \\ a^{-2}, & S = f_{\phi} \end{cases}$$

- $X$  production becomes efficient at  $a = a_*$  when  $\tilde{k} > a_* H_*$
- backreaction on axion motion delayed until  $a = a_{\text{GW}}$  by  $X$  mode growth time



# Gravitational Wave Spectrum in Kinetic Misalignment

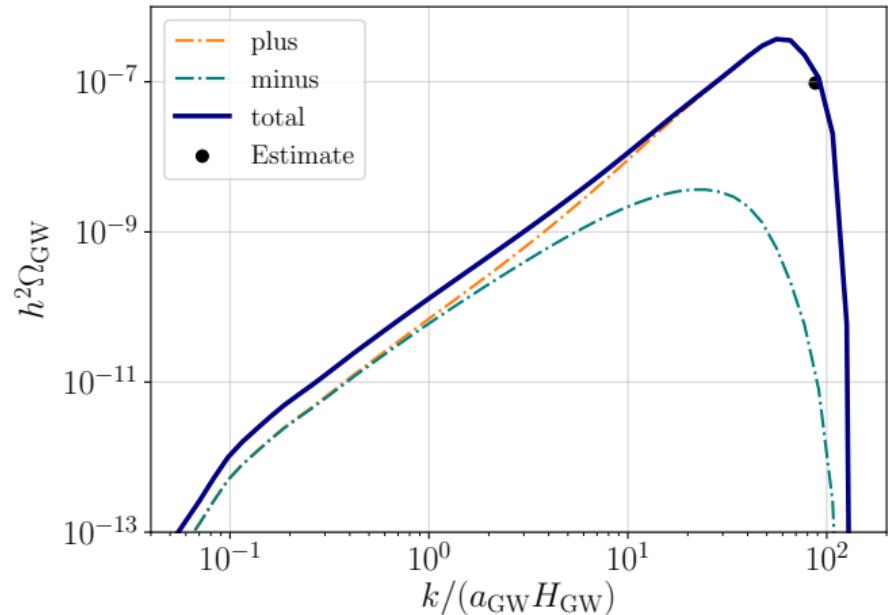
⇒ similar spectral shape as before, but with different parametric dependence:

- GW emitted around  $a = a_{\text{GW}}$  when  $X$  modes have grown

$$\Rightarrow f_{\text{peak}} \propto \alpha \sqrt{\frac{m_{S,0}}{f_\phi} \frac{S_i}{M_{\text{Pl}}}}$$

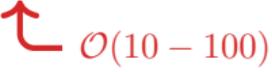
- amplitude set by axion kinetic energy

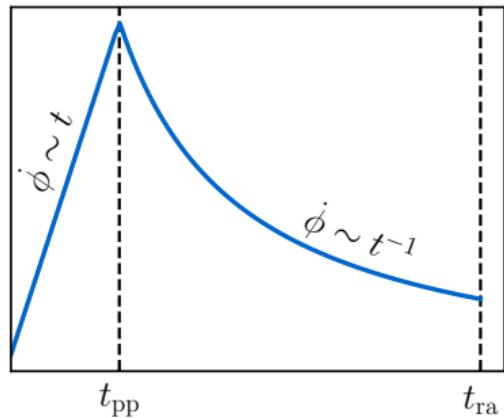
$$\Rightarrow \Omega_{\text{GW}}^{\text{peak}} \propto \frac{S_i^4}{M_{\text{Pl}}^4}$$



# Relaxion Evolution

$$\mathcal{L} \supset -\frac{\alpha}{4} \frac{\phi}{f_\phi} X_{\mu\nu} \tilde{X}^{\mu\nu} \implies \ddot{\phi} + 3H\dot{\phi} - \frac{\Lambda_{\text{br}}^4}{f_\phi} + \frac{\alpha}{f_\phi} \frac{\langle \tilde{X}_{\mu\nu} X^{\mu\nu} \rangle}{4a^4} = 0$$

- initially:  $\langle \tilde{X}X \rangle$  negligible  $\implies \dot{\phi} \sim t$
- dark photon friction kicks in when  $\frac{\alpha}{4a^4} \langle \tilde{X}X \rangle \sim \Lambda_{\text{br}}^4$   
 $\implies$  define time of particle production:  $\left. \frac{\langle \tilde{X}X \rangle}{4a^4} \right|_{t_{\text{pp}}} = \frac{\Lambda_{\text{br}}^4}{\alpha}$
- relaxion reaches terminal velocity:  $\dot{\phi} = \xi H f_\phi / \alpha$   

- relaxion stops when barriers reappear

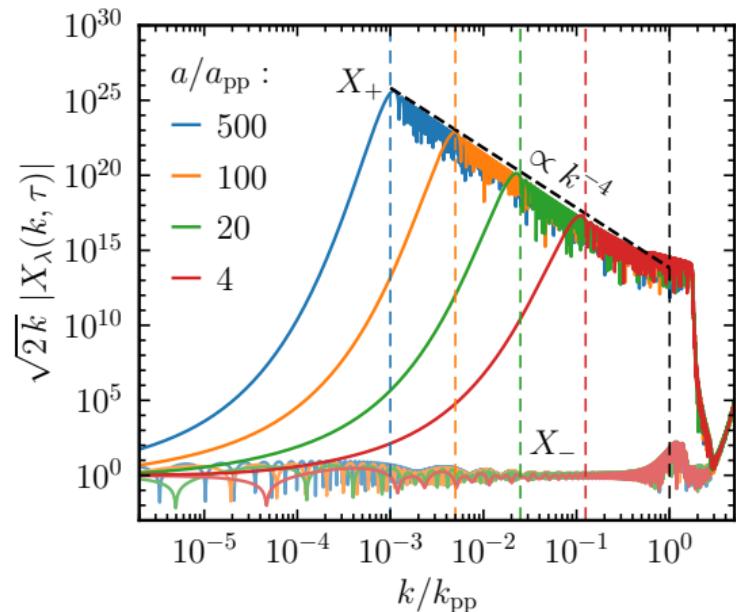


# Dark Photon Production from Relaxion

dark photon EoM:  $X''_{\pm}(\tau, k) + \left( k^2 \mp k \frac{\alpha \phi'(\tau)}{f_\phi} \right) X_{\pm}(\tau, k) = 0$

- $\phi' > 0 \implies$  only '+' helicity experiences tachyonic instability
- energy predominantly transferred to most tachyonic mode:  $k = \frac{\alpha \phi'}{2 f_\phi} = \frac{\xi a H}{2}$
- after exiting the tachyonic band:  $X(k, \tau) \propto \cos(k\tau)/\sqrt{2k}$

$\implies X_+(k, \tau) \sim k^{-9/2} \cos(k\tau - \xi) \quad \text{for } k > \frac{\xi}{2\tau}$



# Relaxion Gravitational Wave Spectrum

■ IR:  $f \ll f_{\text{peak}}$

$$|\mathbf{q}| \sim |\mathbf{k} - \mathbf{q}| \sim k_{\text{peak}}^X$$

$$\Omega_{\text{GW}}(f) \sim \Omega_{\text{GW}}^{\text{peak}} \xi^2 \frac{f^3}{f_{\text{peak}}^3}$$

■ peak:  $f \sim f_{\text{peak}}$

$$|\mathbf{q}| \sim |\mathbf{k} - \mathbf{q}| \sim k_{\text{peak}}^X$$

$$\Omega_{\text{GW}}(f_{\text{peak}}) = \Omega_{\text{GW}}^{\text{peak}}$$

■ UV:  $f \gg f_{\text{peak}}$

$$|\mathbf{q}| \sim k_{\text{peak}}^X, \quad |\mathbf{k} - \mathbf{q}| \sim k$$

$$\Omega_{\text{GW}}(f) \sim \Omega_{\text{GW}}^{\text{peak}} \frac{f_{\text{peak}}^4}{f^4}$$

