

Conservation of baryon number B is an accidental symmetry of the SM

Based only on the symmetry group $SU(3)_c \times SU(2)_L \times U(1)_Y$ there is no reason that baryons are stable

However, the SM does not contain any fields that can mediate B-violating interactions:

$$o_{abcd}^{(1)} = \left[\frac{d^{C}}{d_{\alpha aR}} u_{\beta bR} \right] \left[\frac{d^{C}}{d_{iYcL}} \ell_{jdL} \right] \epsilon_{\alpha \beta Y} \epsilon_{ij}$$

$$o_{abcd}^{(2)} = \left[\frac{d^{C}}{d_{i\alpha aL}} q_{j\beta bL} \right] \left[\frac{d^{C}}{d_{iYcR}} \ell_{dR} \right] \epsilon_{\alpha \beta Y} \epsilon_{ij}$$

$$o_{abcd}^{(2)} = \left[\frac{d^{C}}{d_{\alpha aR}} u_{\beta bR} \right] \left[\frac{d^{C}}{d_{iYcR}} \ell_{dR} \right] \epsilon_{\alpha \beta Y} \epsilon_{ij}$$

$$o_{abcd}^{(5)} = \left[\frac{d^{C}}{d_{\alpha aR}} u_{\beta bR} \right] \left[\frac{d^{C}}{d_{iYcR}} \ell_{dR} \right] \epsilon_{\alpha \beta Y} \epsilon_{ij}$$

$$O_{abcd}^{(1)} = \begin{bmatrix} \overline{d_{\alpha aR}} & u_{\beta bR} \end{bmatrix} \begin{bmatrix} \overline{d_{i YcL}} & \ell_{j dL} \end{bmatrix} \varepsilon_{\alpha \beta Y} & \varepsilon_{ij}$$

$$O_{abcd}^{(4)} = \begin{bmatrix} \overline{d_{i \alpha aL}} & q_{j \beta bL} \end{bmatrix} \begin{bmatrix} \overline{d_{k YcL}} & \ell_{k dL} \end{bmatrix} \varepsilon_{\alpha \beta Y} (\overline{\tau} \varepsilon)_{ij} \cdot (\overline{\tau} \varepsilon)_{k \ell}$$

$$o_{abcd}^{(5)} = \left(\frac{d^{C}}{d_{\alpha aR}} u_{\beta bR} \right) \left(\frac{C}{u_{YcR}} t_{dR} \right) \epsilon_{\alpha \beta \gamma}$$

$$o_{abcd}^{(3)} = \left(\overline{q_{i\alpha aL}^{C}} \ q_{j\beta bL}\right) \left(\overline{q_{k\gamma cL}^{C}} \ \ell_{kdL}\right) \epsilon_{\alpha\beta\gamma} \ \epsilon_{ij} \ \epsilon_{k\ell} \qquad o_{abcd}^{(6)} = \left(\overline{u_{\alpha aR}^{C}} \ u_{\beta bR}\right) \left(\overline{q_{\gamma cR}^{C}} \ \ell_{dR}\right) \epsilon_{\alpha\beta\gamma}$$

Weinberg, Phys.Rev.Lett. 43 (1979) 1566-1570



Baryogenesis?

GUT?

Supersymmetry?

Lepton number violation?

Dark matter?

A smoking gun signal of B-violation is proton decay

$$p \to e^+ \pi^0$$

$$p \to e^+ \gamma$$

Can be realized in a wide range of different models

$$p \to \mu^+ \pi^0$$

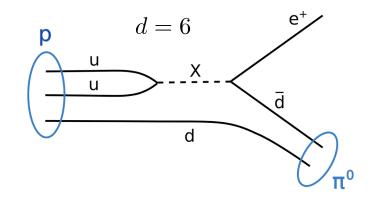
$$p \to \bar{\nu} K^+$$

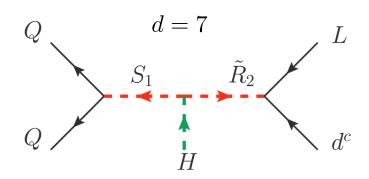
- Operator dimensions d=6, d=7, d=8, ...
- Flavoured final states: muon, kaon, ...
- Vector meson final states
- Also dinucleon decays, possible overlap with neutron-antineutron oscillation (see next talk)

$$(\Delta B, \Delta L) = (0, 2) : \min(d) = 5$$

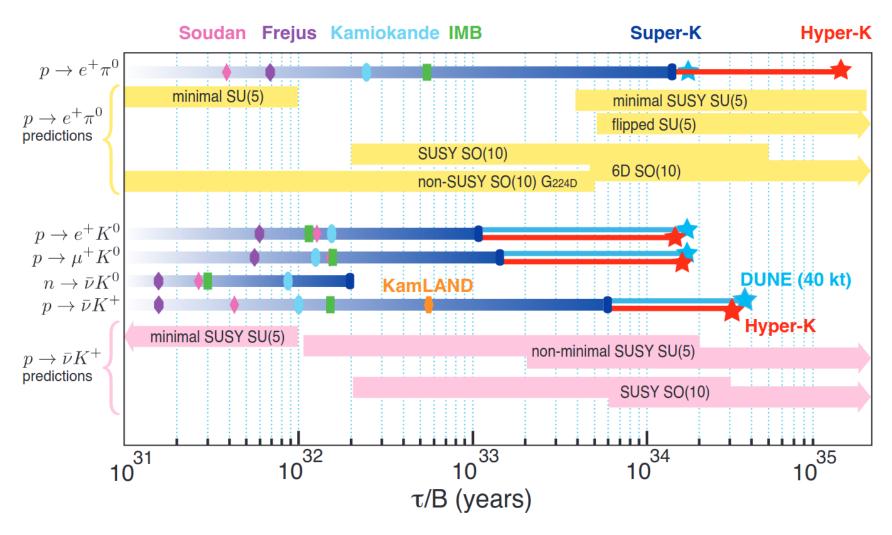
 $(1, -1) : \min(d) = 6$
 $(1, 1) : \min(d) = 7$
 $(2, 0) : \min(d) = 9$

$$\mathcal{L}_{\text{eff}} \supset \sum_{i} \sum_{d} C_{i}^{(d)} \mathcal{O}_{i}^{(d)} \implies C_{i}^{(d)} \propto \frac{1}{\Lambda^{d-4}} \implies \tau_{p \to \dots} \propto \frac{1}{\Lambda^{2d-8}}$$





Upcoming experiments will significantly improve the sensitivity: JUNO (scintillator), Hyper-Kamiokande (Cherenkov), DUNE (LAr TPC)



Hyper-Kamiokande collaboration, arXiv:1805.04163 [physics.ins-det]

For the neutrino modes, only the (decay products of) the charged mesons are detected

Even though these are *primarily* neutrino experiments, they cannot detect the final state neutrinos from proton decays

At the same time we are aware of the need for NP in the neutrino sector



Dirac: $\nu_L \neq \nu_R^c$

Majorana: $\nu_L = \nu_R^c$

What is the nature of neutrinos?

$$\mathcal{L}_{\mathrm{Dirac}} \supset -y_{ij}^{\nu} \tilde{H} L_i N_j \longrightarrow y_{\nu} \sim 10^{-12}$$

$$\mathcal{L}_{\text{Majorana}} \supset -y_{ij}^{\nu} \tilde{H} \bar{L}_i N_j - M_{ij} \bar{N}^c{}_i N_j + \text{h.c.}$$

In either scenario we can have low scale RHNs such that $\, m_N < m_p \,$

This could then lead to proton decay with light HNLs in the final state $p \to \pi^+ N$

How can we distinguish HNLs from SM neutrinos?

Helo, Heeck, Ota, JHEP 06 (2018) 047

d=6 SMEFT

$$egin{aligned} \mathcal{O}_1 = & [\overline{d_R}^c u_R] [\overline{Q^c} L], \ \mathcal{O}_2 = & [\overline{Q^c} Q] [\overline{u_R}^c e_R], \ \mathcal{O}_3 = & [\overline{Q^c} Q]_1 [\overline{Q^c} L]_1, \ \mathcal{O}_4 = & [\overline{Q^c} Q]_3 [\overline{Q^c} L]_3, \ \mathcal{O}_5 = & [\overline{d_R}^c u_R] [\overline{u_R}^c e_R], \end{aligned}$$

$\mathsf{d=}6\,N_{\!R}\text{-}\mathsf{SMEFT}$

$$\mathcal{O}_{N1} = [\overline{Q^c}Q][\overline{d_R}^cN],$$
 $\mathcal{O}_{N2} = [\overline{u_R}^cd_R][\overline{d_R}^cN].$

		нею, нееск, О	la, JHEP 06 (2018) 04
$\overline{\text{Modes }(p)}$	$\pi^+ + E$	$\pi^0 e^+$	$K^+ + E \hspace{-0.6em}/ \hspace{0.2em}$
Current [yrs]	$3.9 \cdot 10^{32} [8]$	$1.6 \cdot 10^{34} [9]$	$5.9 \cdot 10^{33} [10]$
Future [yrs]		$1.2 \cdot 10^{35} \ [48]$	$> 3 \cdot 10^{34} [49]$
\mathcal{O}_1	V	$\overline{}$	\checkmark
\mathcal{O}_2		1	
\mathcal{O}_3	\checkmark		\checkmark
\mathcal{O}_4			\checkmark
\mathcal{O}_5		\checkmark	
\mathcal{O}_{N1}	1	-\	√
\mathcal{O}_{N2}			✓

Isosymmetry: $\mathcal{O}_1, \mathcal{O}_3$:

$$\mathcal{O}_1, \mathcal{O}_3: \qquad \Gamma(p \xrightarrow{\mathcal{O}_{1,3}} \pi^+ \bar{\nu}_e) = 2\Gamma(p \xrightarrow{\mathcal{O}_{1,3}} \pi^0 e^+)$$

Violation of this relation can hint at the existence of HNL modes

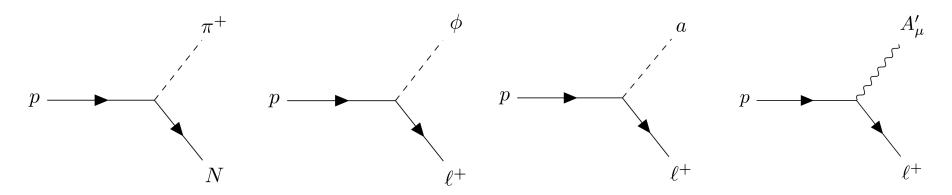
The light LLPs can also be or bosonic fields

ALPs/Majoron:
$$\mathcal{L}\supset \frac{\partial_{\mu}a}{f_a}ar{f}\gamma^{\mu}\gamma_5 f$$
 Freeze-in scalar DM: $\mathcal{L}\supset \frac{1}{\Lambda}\phi^2ar{f}f$

New light gauge bosons
$$D_{\mu}\supset ig_{B-L}q_{B-L}B'_{\mu}$$
 $D_{\mu}\supset ig_{L_{\mu}-L_{\tau}}q_{L_{\mu}-L_{\tau}}B''_{\mu}$

Leads to new proton decay modes $p \to \ell^+ Z'_{\mu}$ $p \to \ell^+ a$ $p \to \ell^+ \phi$

In principle the only condition needed to write down a proton decay operator is $m_{\mathrm{NP}} < m_p$



Many models with light LLPs feature NP at high scales reachable in proton decay

No reason for the NP to ensure proton stability unless the symmetry is explicit

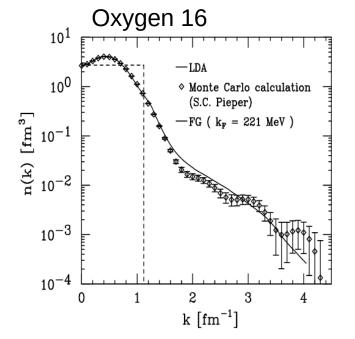
How to search for such modes with finals state LLPs?

The LLP mass is a "free" parameter: few well-motivated benchmarks apart from the phenomenologically driven seesaw RHN, QCD axion, or freeze-in/out DM

Decay width generally depends on all masses involved

$$\Gamma_{\psi \to ij} = \frac{1}{16\pi} \frac{\lambda^{1/2}(m_{\psi}, m_i, m_j)}{m_{\psi}^3} |\sum_{I} C_I \mathcal{M}_I^{\psi \to ij}|^2 \qquad |\vec{p}_i| = \frac{\lambda^{1/2}(m_{\psi}^2, m_i^2, m_j^2)}{2m_{\psi}}$$

For 2-body decays the final state momenta are completely determined by the masses

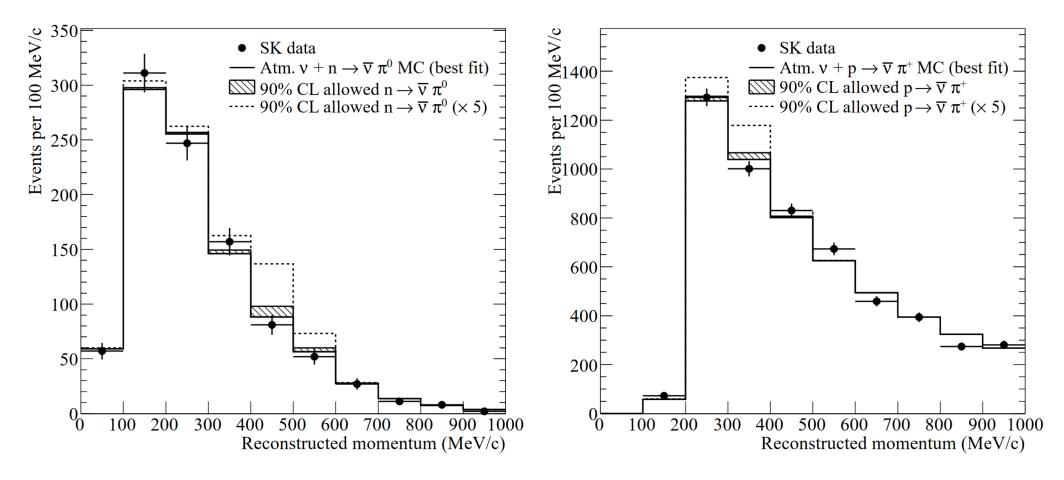


In the ideal scenario this leads to a sharp peak at the given momentum

Fermi motion will "spread" this peak

Super-K and Hyper-K are both made up of water, where oxygen has most of the protons

Benhar, nucl-th/0307061 [nucl-th]

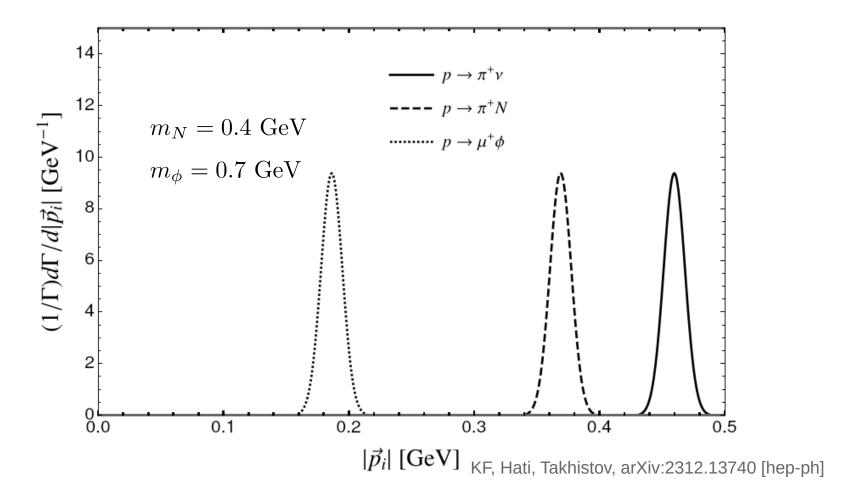


Super-Kamiokande collaboration, Phys.Rev.Lett. 113 (2014) 12, 121802

For 2-body decays $n \to \bar{\nu}\pi^0$ (left) and $p \to \bar{\nu}\pi^+$ (right)

Fermi motion and BG are simulated with MC

Since the left-handed neutrino mass is "known" the peaks are expected at specific pion momenta



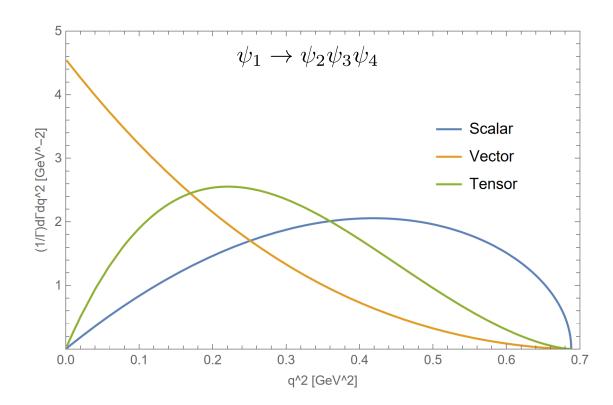
For a non-zero LLP mass the peak moves to lower momenta $\hbox{Super-Kamiokande has a cut at 200 MeV for} \ \ p \to \mu^+ + E_{\rm miss}$ The same cut applies for charged pions (since they decay to muons)

For 3-body decays the distribution is more spread out

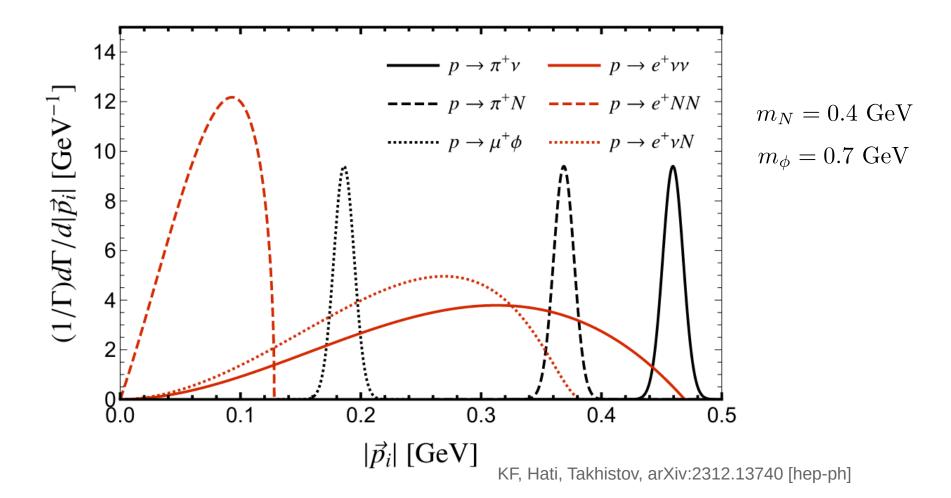
$$\frac{d\Gamma_{\psi \to ijk}}{d|\vec{p_i}|} = \frac{1}{(2\pi)^3} \frac{1}{32m_{\psi}^3} \frac{2m_{\psi}|\vec{p_i}|}{\sqrt{m_i^2 + |\vec{p_i}|^2}} \int_{t^-}^{t^+} dt |\mathcal{M}_{\psi \to ijk}|^2$$

The distribution also depends on the type of interaction:

Scalar: $(\psi_1\psi_2)(\psi_3\psi_4)$ Vector: $(\psi_1\gamma_\mu\psi_2)(\psi_3\gamma^\mu\psi_4)$ Tensor: $(\psi_1\sigma_{\mu\nu}\psi_2)(\psi_3\sigma^{\mu\nu}\psi_4)$



For two LLPs in the final state we have double the mass d.o.f.s



Peak of the distribution again shifts to lower momenta for higher masses

For electrons there is a lower cut at 100 MeV

For the 3-body modes the currents are scalar ($\nu\nu$, NN) and vector (ν N)

Explicitly these are some examples of operators with singlet NP:

O	Operator	$(\Delta B, \Delta L)$	Dim	Decay modes	New Field(s)
$\overline{{\cal O}_{d^2uN}}$	$\epsilon^{abc} \left(\bar{d}_a^c N \right) \left(\bar{d}_b^c u_c \right)$	(1, 1)	6	$p(n) \to \pi^{+(0)} \bar{N}$	sterile neutrino
$\overline{\mathcal{O}_{Dd^2uar{N}}}$	$\epsilon^{abc} \left(\bar{N} \gamma_{\mu} d_a \right) \left(\bar{d}_b^c D^{\mu} u_c \right)$	(1, -1)	7	$n \to N\gamma$ $p(n) \to \pi^{+(0)}N\gamma$	sterile neutrino
$\mathcal{O}_{du^2e\phi}$	$ \epsilon^{abc} \left(\bar{d}_a^c u_b \right) \left(\bar{e}^c u_c \right) \phi^{\dagger} $	(1, 1)	7	$p \to e^+ \phi$ $p(n) \to e^+ \pi^{0(-)} \phi$	dark scalar, majoron
$\mathcal{O}_{d^2Qar{L}X}$	$\epsilon^{abc} \left(\bar{Q}_a^{ci} \gamma_\mu d_b \right) \left(\bar{L}_i d_c \right) X^\mu$	(1, -1)	7	$n \to \nu X / e^- \pi^+ X$ $p(n) \to \nu \pi^{+(0)} X$	dark photon
$\overline{\mathcal{O}_{dQ^2ar{L}ar{H}\phi}}$	$\epsilon^{abc} \left(\bar{Q}_a^{ci} Q_b^j \right) \left(\bar{L}_i d_c \right) H_j^{\dagger} \phi^{\dagger}$	(1, -1)	8	$n \rightarrow \nu \phi / e^- \pi^+ \phi$	dark scalar, majoron
$\overline{{\cal O}_{Dd^2Qar{L}a}}$	$\epsilon^{abc}(\partial_{\mu}a)\left(\bar{Q}_{a}^{ci}\gamma^{\mu}d_{b}\right)\left(\bar{L}_{i}d_{c}\right)$	(1, -1)	8	$n \rightarrow \nu a / e^- \pi^+ a$	axion-like particles
$\overline{{\cal O}_{Dd^2uar Na}}$	$\epsilon^{abc}(\partial_{\mu}a)\left(\bar{N}\gamma^{\mu}d_{a}\right)\left(\bar{d}_{b}^{c}u_{c}\right)$	(1, -1)	8	$n \to Na$ $p(n) \to \pi^{+(0)} Na$	axion-like particle with sterile neutrino
$\mathcal{O}_{duQear{L}ar{N}}$	$\epsilon^{abc} \left(\bar{e}^c u_a \right) \left(\bar{Q}_b^{ci} \gamma_\mu d_c \right) \left(\bar{L}_i \gamma^\mu N^c \right)$	(1,-1)	9	$p \to e^+ \nu N$ $n \to e^+ e^- N$	sterile neutrino
$\mathcal{O}_{du^2eN^2}$	$ \epsilon^{abc} \left(\bar{d}_a^c u_b \right) \left(\bar{e}^c u_c \right) \left(\bar{N}^c N \right) $	(1, 3)	9	$p \to e^+ \bar{N} \bar{N}$	sterile neutrino

KF, Hati, Takhistov, arXiv:2312.13740 [hep-ph]

Explicit model example: SO(10)

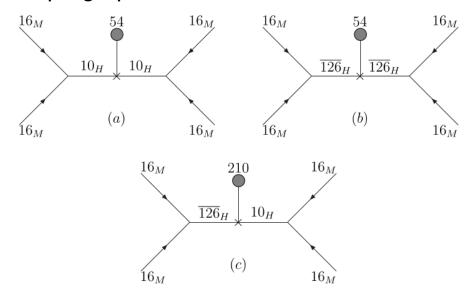
A single multiplet leads to all SM fermion fields plus a HNL:

$$16 \longrightarrow (3,2,1/6) \oplus (1,2,-1/2) \oplus (\bar{3},1,1/3) \oplus (\bar{3},1,-2/3) \oplus (1,1,1) \oplus (1,1,0)$$

A minimal model contains an intermediate $SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_{B-L}$

Leads to proton decay at dimension 5 with supersymmetry

Supergraphs:



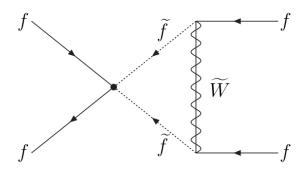
Depends also on SUSY breaking scale

$$210 \oplus 54$$
 breaks $SO(10)$

126 breaks
$$SU(2)_R \times U(1)_{B-L}$$

10 breaks
$$SU(2)_L \times U(1)_Y$$

Dressed diagram at dimension 5:



Goh, Mohapatra, Nasri, Ng, Phys.Lett.B 587 (2004) 105-116

We consider a non-SUSY model with intermediate Pati-Salam symmetry and D-parity breaking

$$m_{\rm GUT} \gg m_D > m_{\rm PS} \gg m_R > m_{B-L} \gg m_{\rm SM}$$

Leads to a dimension-6 operator $\mathcal{O}_{d^2uN} = \epsilon^{abc} \left(d_a N \right) \left(d_b u_c \right)$

$$p \left\{ \begin{array}{c} u & & & \\ u & & & \\ u & & & -\overline{126}_{H} & - \overline{10}_{H} & \\ d & & & & 1210_{H} \\ & & & & & N \end{array} \right\} \pi^{+}$$

The decay rate will depend on strong running and a nuclear form factor

$$\mathcal{M}_{p\to\pi^+N} = U'(\mu_{\rm NP}, \mu_0) F_p^{\pi^+}(\mu_0, m_N^2) u_p P_R \bar{u}_N$$

Scalar masses are generated at PS breaking, when the 210 gets a vev

$$\tau_{p \to N\pi^{+}} = 0.81 \times 10^{35} \frac{\left(\frac{m_N^2}{\text{GeV}^2} + 0.86\right)^{-1}}{\lambda^{1/2} \left(\frac{m_p^2}{\text{GeV}^2}, \frac{m_N^2}{\text{GeV}^2}, \frac{m_{\pi^{+}}^2}{\text{GeV}^2}\right)} \times \frac{\left(\frac{m_{126}}{2 \times 10^8 \text{ GeV}}\right)^4 \left(\frac{m_{10}}{2 \times 10^8 \text{ GeV}}\right)^4}{\lambda_{dN}^2 \lambda_{ud}^2 \left(\frac{v_{(1,1,15)}}{2 \times 10^8 \text{ GeV}}\right)^4} \text{ yrs}$$

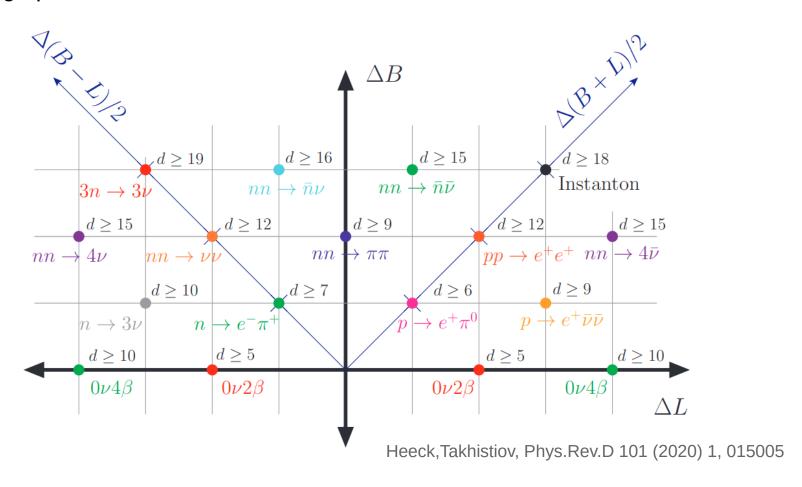
Conclusions:

- Operators with light LLPs can lead to non-canonical proton decay
- In this way proton decay can be an observable for axions, dark photons, ...
- For some LLP masses these modes may have been cut away at Super-Kamiokande

Thank you

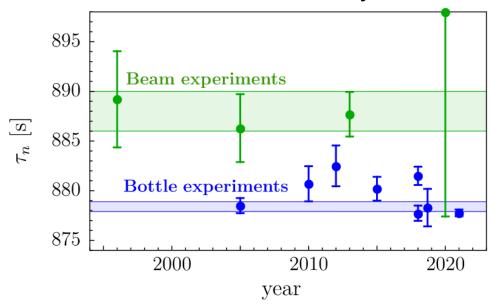
Backup

There are many more classes of modes, depending upon the dimension of the underlying operator

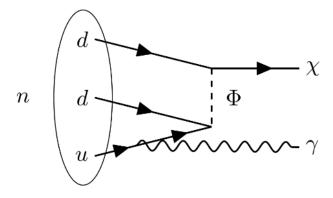


In combination with the flavor aspect (e.g. muon or kaon final states), as well as vector mesons (ρ , ω), the number of possible decay modes is very large

Neutron lifetime anomaly



Fornal, Universe 9 (2023) 10, 449



Fornal, Grinstein, Phys.Rev.Lett. 120 (2018) 19, 191801

Bottle and beam neutron lifetimes disagree

Can be solved with dark neutron decays

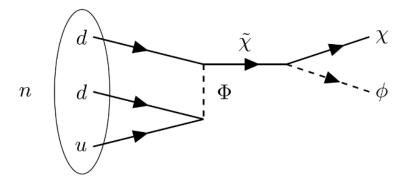
Requires very specific DM masses:

$$937.900 \text{ MeV} < m_{\chi} + m_{\phi} < 939.565 \text{ MeV}$$

 $937.900 \text{ MeV} < m_{\chi} < 938.783 \text{ MeV}$

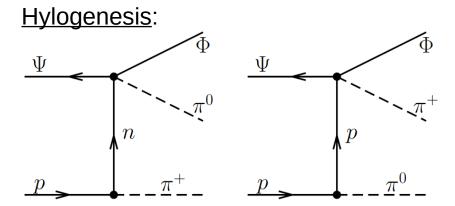
And low-scale NP:

$$\frac{|\lambda_q \lambda_\chi|}{M_\Phi^2} \approx 6.7 \times 10^{-6} \text{ TeV}^{-2}$$



JUST 2024-06-12, Kåre Fridell 19

Some related examples:



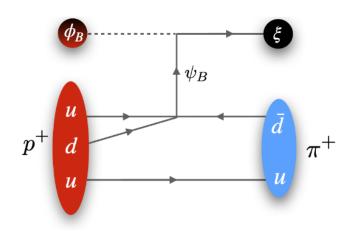
Demidov, Gorbunov, Phys.Rev.D 93 (2016) 3, 035009

Dark matter has baryon number

Simultaneous generation of the dark matter abundance and baryon asymmetry

Leads to "induced" proton decay

Mesogenesis:



Berger, Elor, Phys.Rev.Lett. 132 (2024) 8, 081002

Again dark matter and baryogenesis in a single model

CP-violation comes from B-meson oscillation

Again leads to induced proton decay

In both cases: unusual kinematics

See also:

Liang, Liao, Ma, Wang, JHEP 12 (2023) 172

Ema, McGehee, Pospelov, Ray, arXiv:2405.18472 [hep-ph]

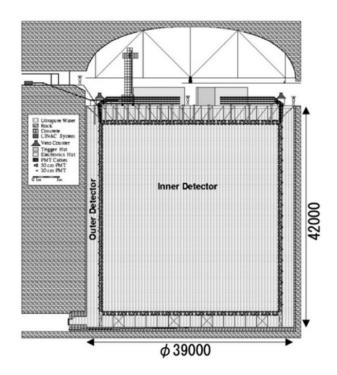
Ge, Ma, arXiv:2406.00445 [hep-ph]

+ ...

Current experimental limits on the proton lifetime imply NP scales $\Lambda_{\rm BNV}\gtrsim 10^{15-16}$ GeV

Super-Kamiokande

1996~Present



$$\tau_{p\to e^+\pi^0} > 2.4 \times 10^{34} \text{ years @ 90\% C.L.}$$

$$\tau_{p \to \mu^+ \pi^0} > 1.6 \times 10^{34} \text{ years @ 90\% C.L.}$$

Super-Kamiokande collaboration, Phys.Rev.D 102 (2020) 11, 112011

Other decay modes are typically constrained at lifetimes that are one or two orders of magnitude lower.

For contrast:

Neutrinoless double beta decay:

$$\tau_{0\nu\beta\beta}^{^{136}\text{Xe}} \ge 3.3 \times 10^{26} \text{ years } @ 90\% \text{ C.L.}$$

KamLAND-Zen collaboration, Phys.Rev.Lett. 130 (2023) 5, 051801

Many GUTs come with high-scale RHNs that lead to seesaw and/or leptogenesis

We consider a non-SUSY model with intermediate Pati-Salam symmetry and D-parity breaking

$$SO(10) \longrightarrow SU(4)_c \times SU(2)_L \times SU(2)_R \times D \longrightarrow$$

$$SU(4)_c \times SU(2)_L \times SU(2)_R \longrightarrow$$

$$SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} \longrightarrow$$

$$SU(3)_c \times SU(2)_L \times U(1)_R \times U(1)_{B-L} \longrightarrow$$

$$SU(3)_c \times SU(2)_L \times U(1)_Y \longrightarrow$$

$$SU(3)_c \times SU(2)_L \times U(1)_Y \longrightarrow$$

$$SU(3)_c \times U(1)_{em}$$

The left- and right-handed symmetries can be related via D-parity before LR breaking Here a scalar field $\sigma \sim (1,1,0)$ aquires a vev that breaks the D-parity Leads to a separation of the RHN mass and LR symmetry breaking Active neutrino gets a type-ii seesaw mass