

# Simplified t-channel dark matter models and LLPs

Dipan Sengupta

University of New South Wales, Sydney

With C.P-Yuan, B. Yan, K. Mohan, Tim Tait, Matthias Becker, Emanuele Copello and Julia Harz + LHC-t-channel Dark Matter Working Group



**UNSW**  
SYDNEY



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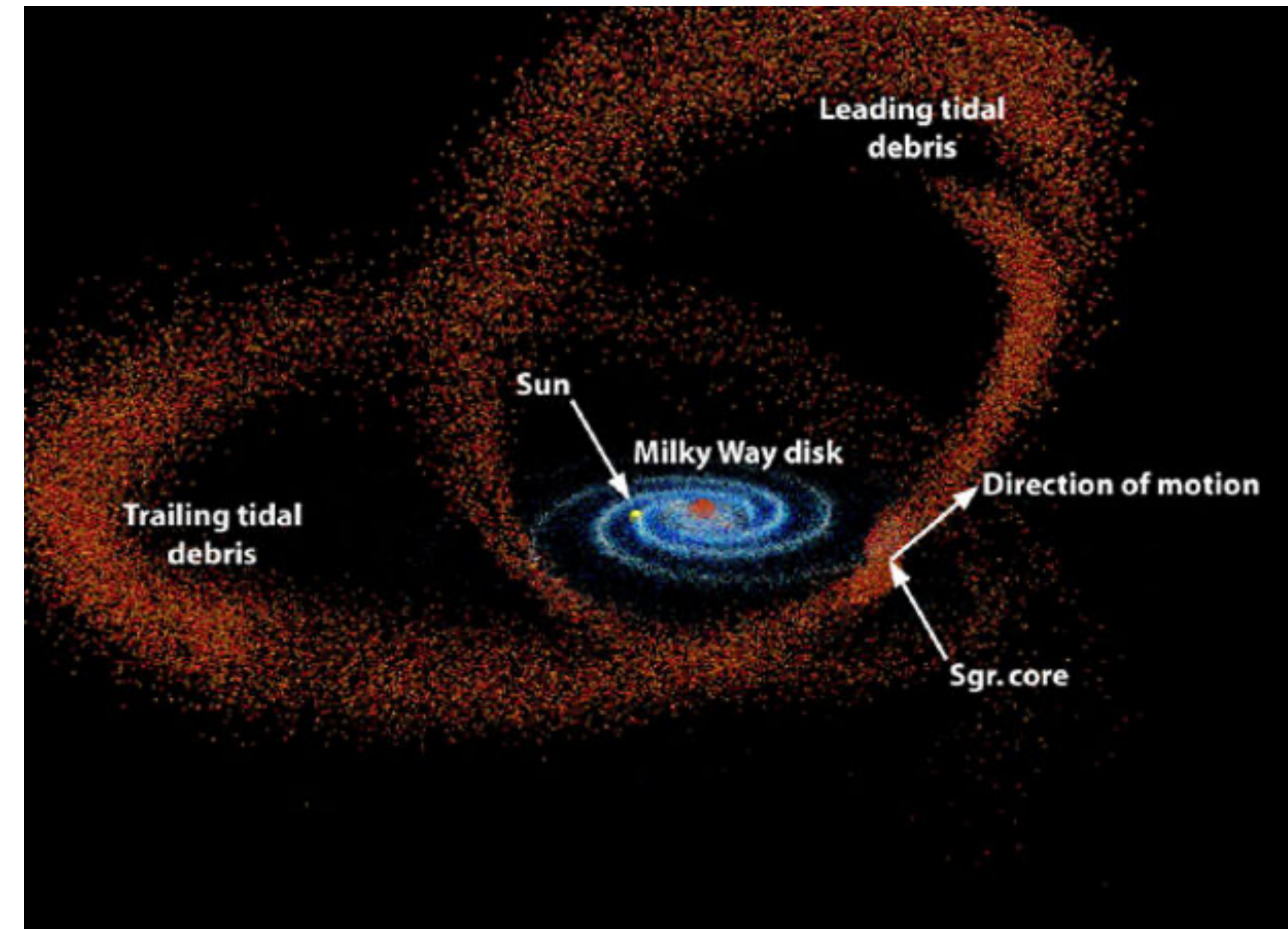
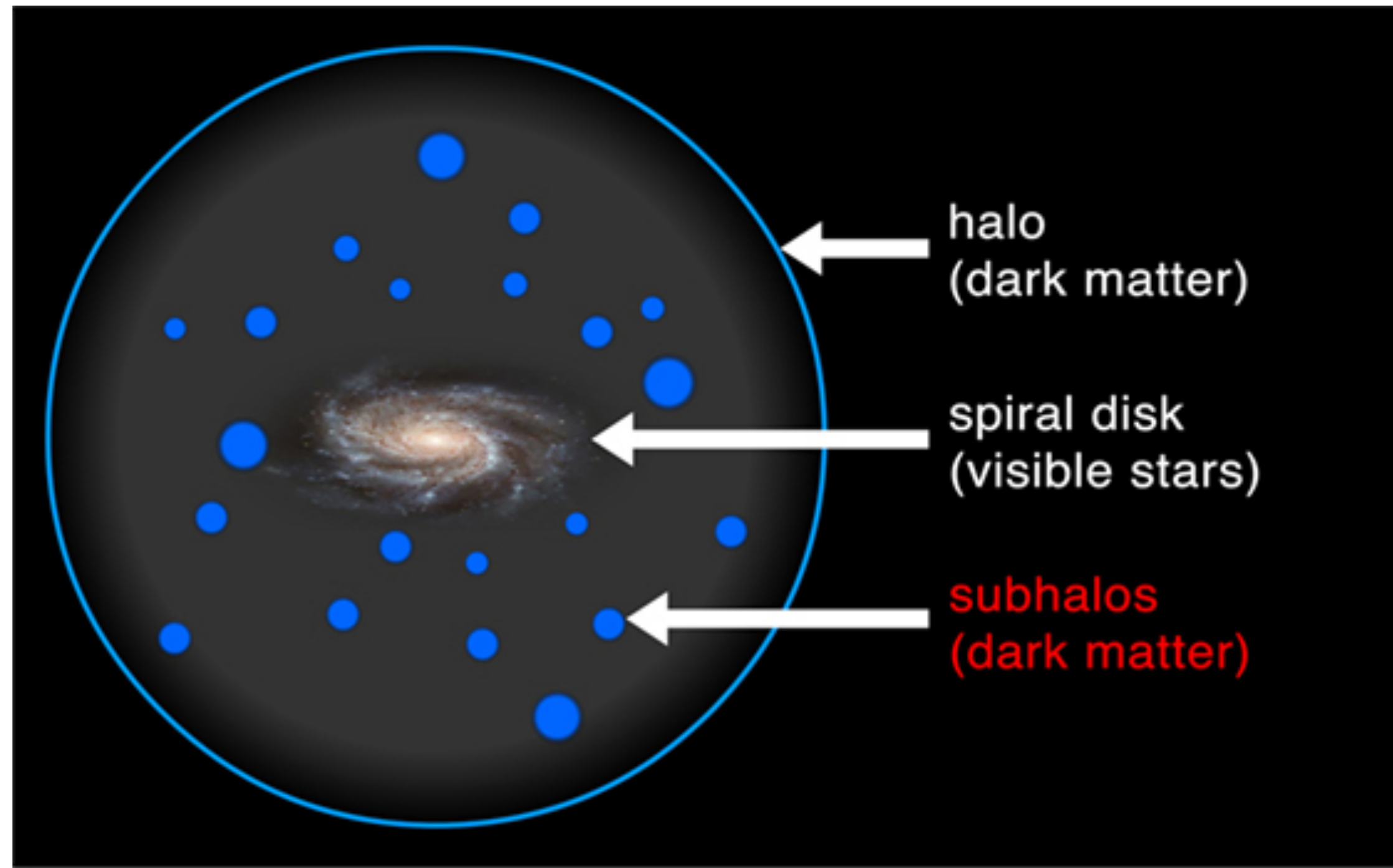
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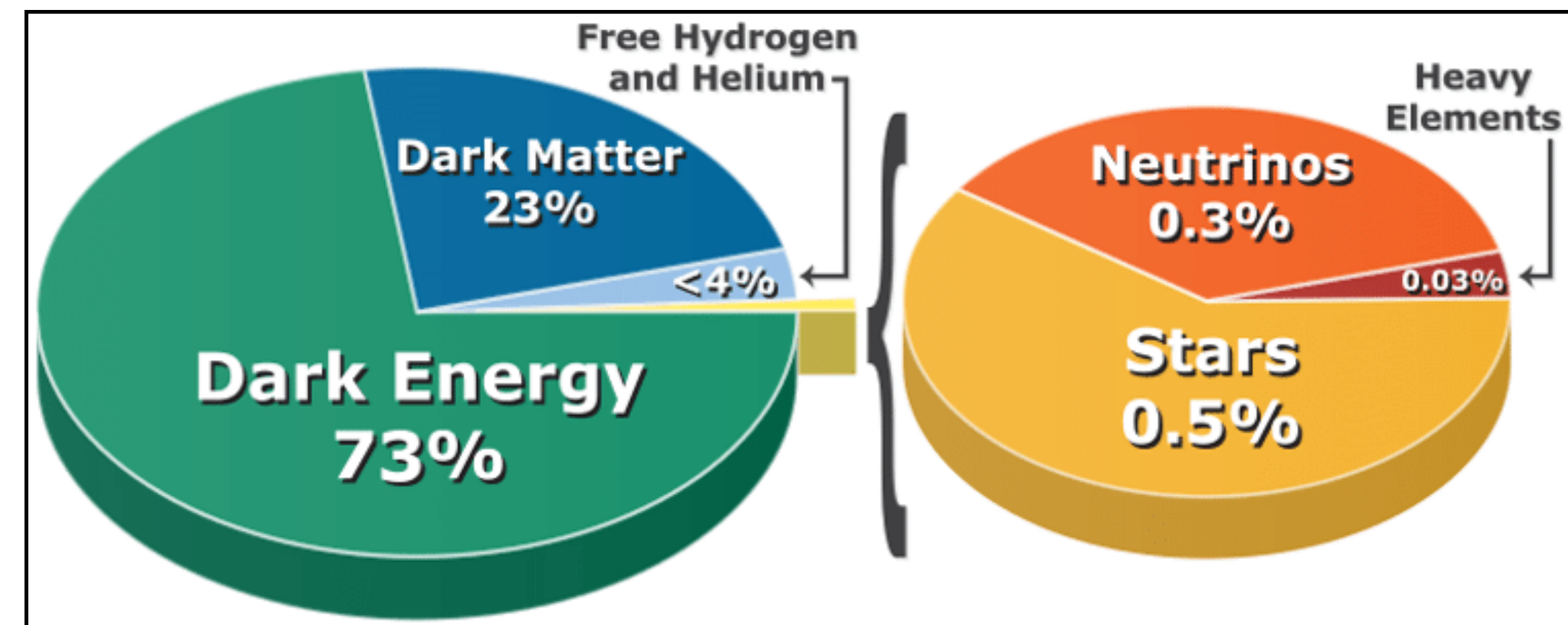


# Properties and the Particle Physics of Dark Matter

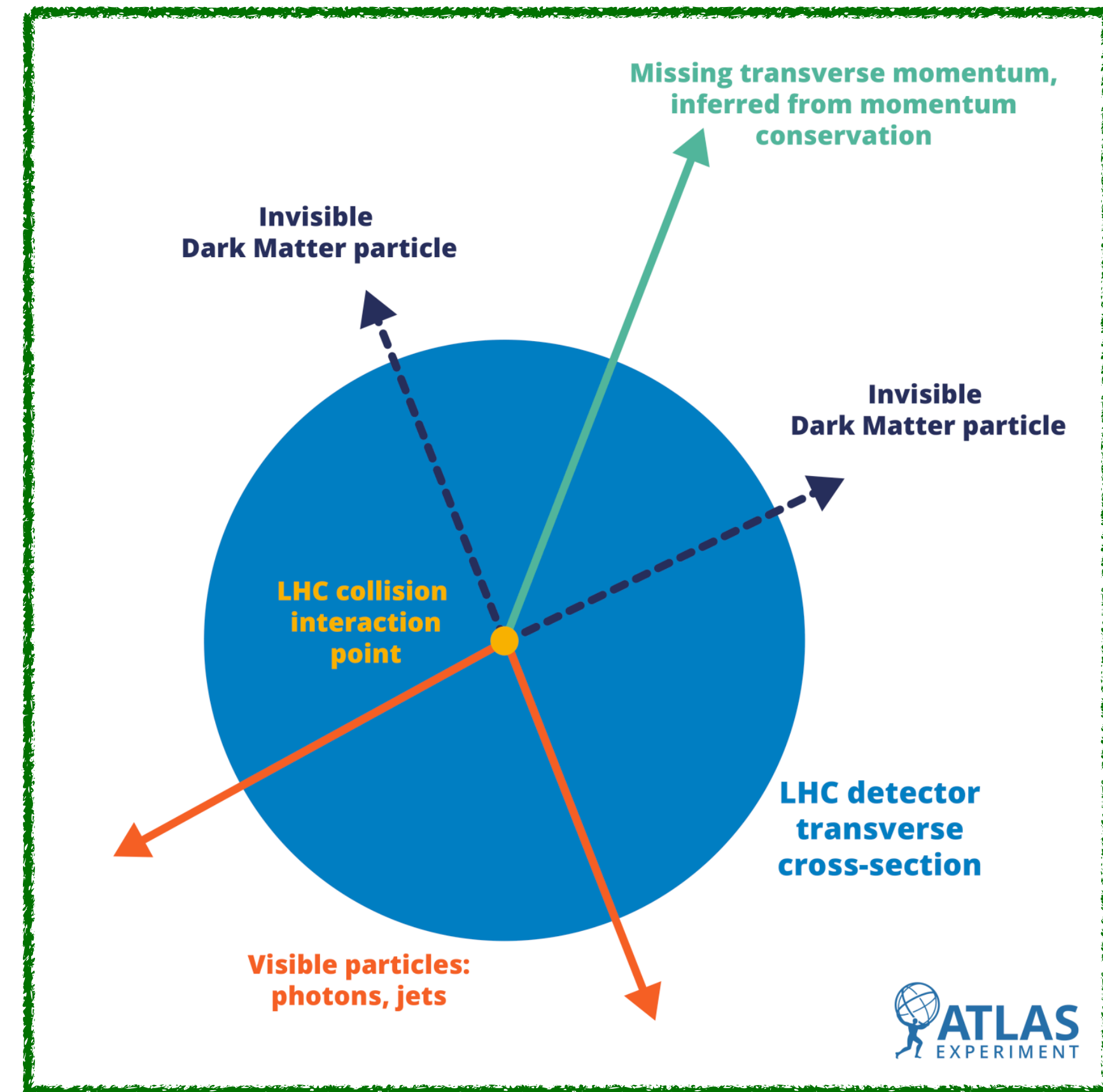
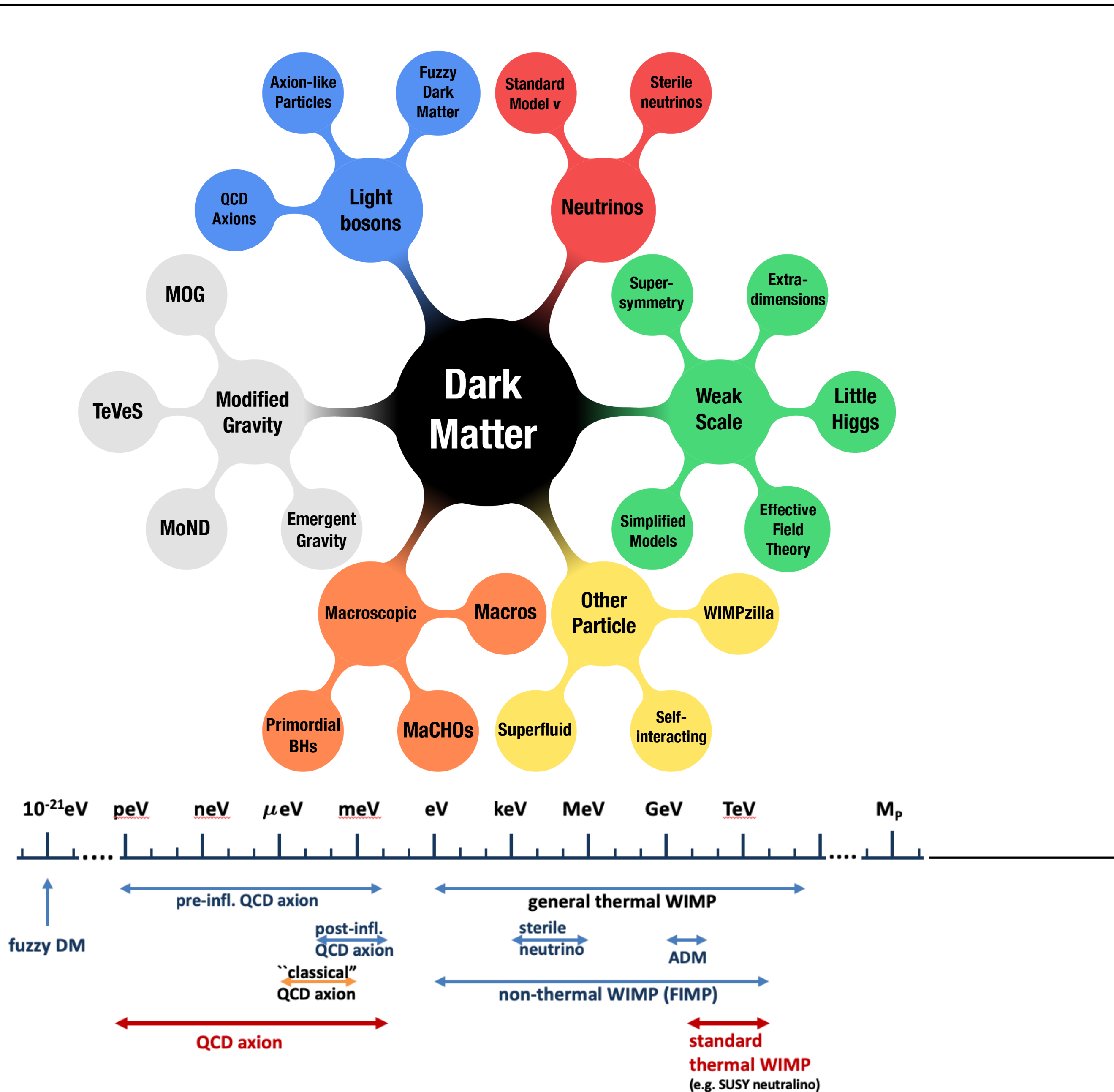


- Cold and Neutral: Non relativistic today.
- Preserves the success of Big Bang Nucleosynthesis (Formation of Atoms and Nuclei in the early Universe)
- “Almost” **Dark** with respect to other forces of nature.
- Collisionless within the DM sector at large scales.
- Stable, on Cosmological time scales.
- Forms halos in the galaxy

Dark Matter belongs in Astronomy/Cosmology .  
Why should we care about colliders ?



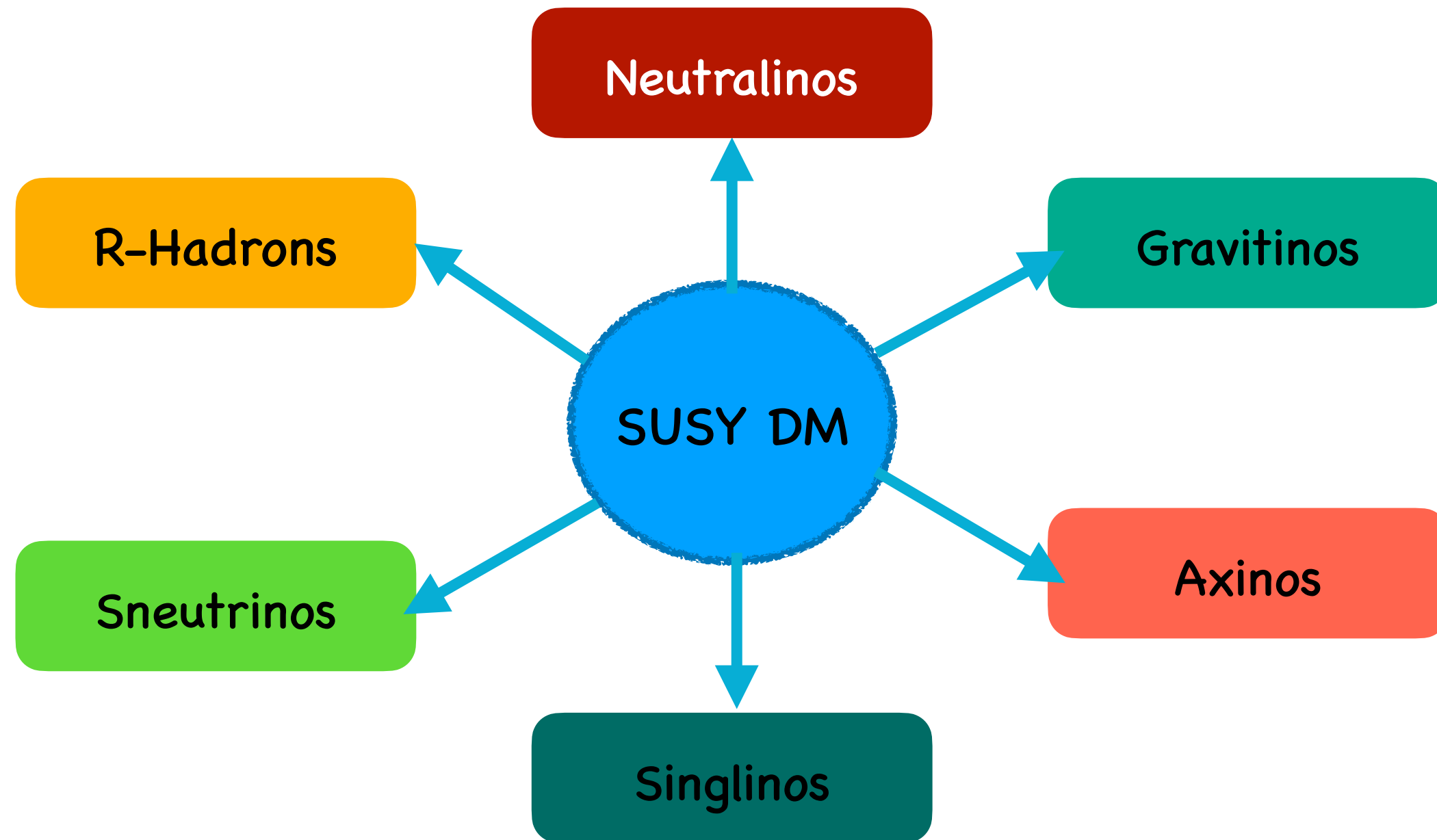
# Dark Matter at Colliders



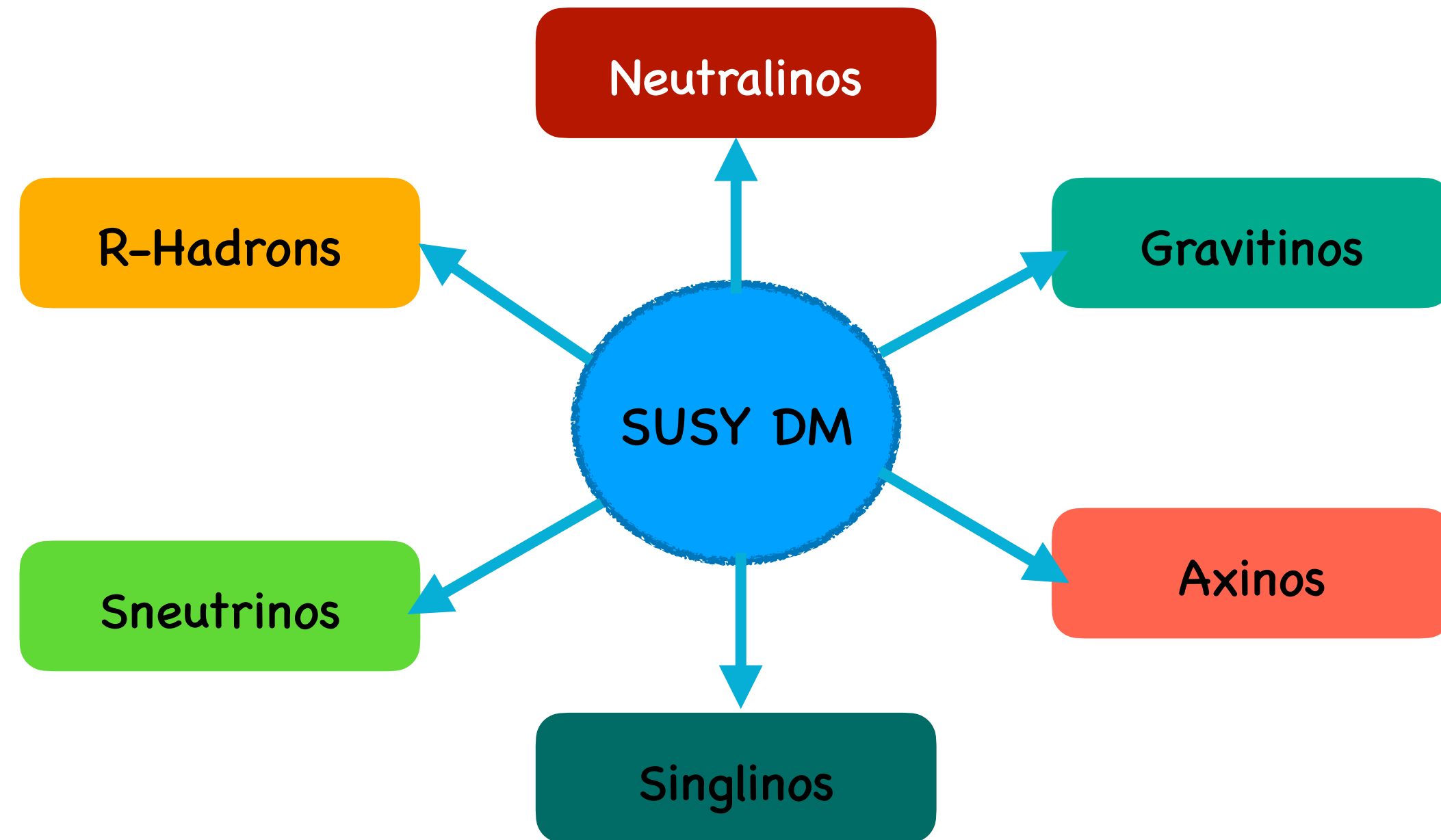
Comment : Even in the event of a missing energy signature, we can't be sure it is dark matter

# Full Models vs EFTs

## Supersymmetry as an Example



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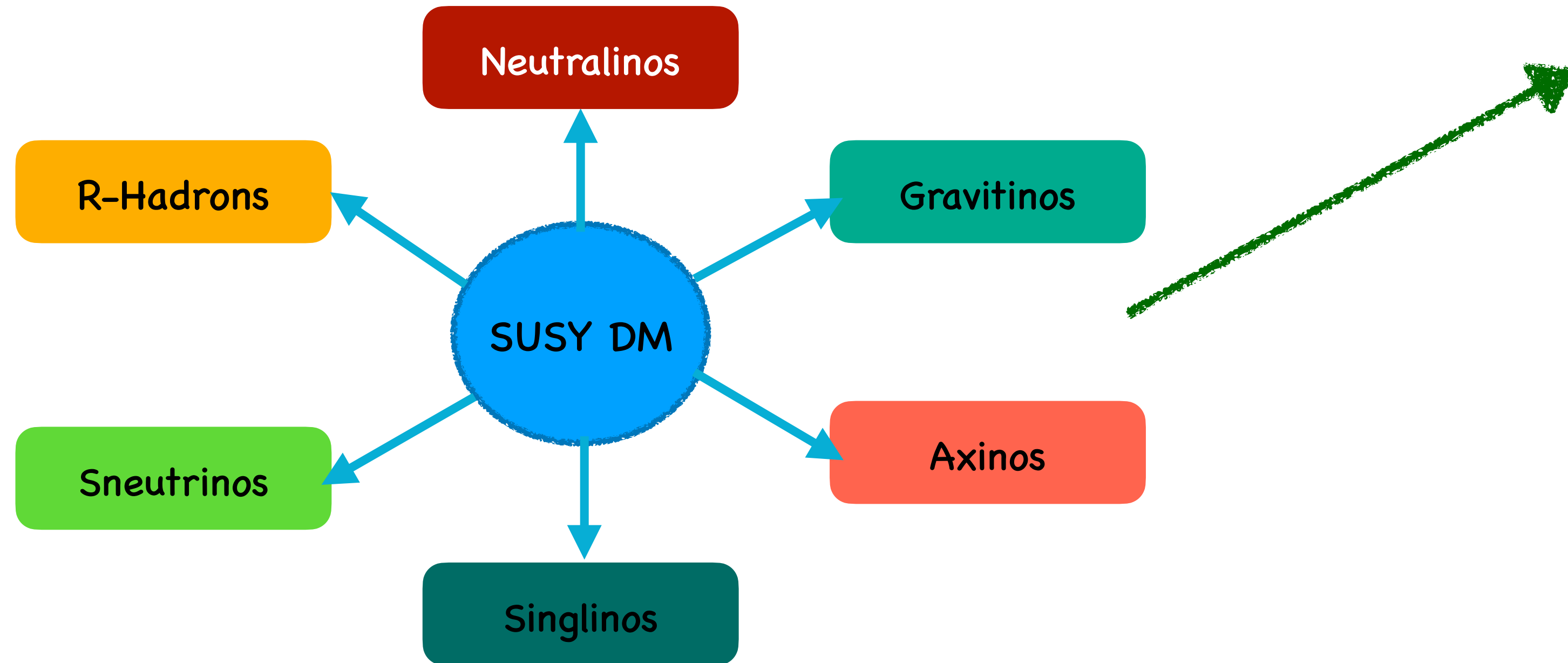


A few mediators with specific DM couplings generates the relic density and direct detection rates.

For heavy mediators, can integrate the mediator out

And classify the DM by spin

## Supersymmetry as an Example



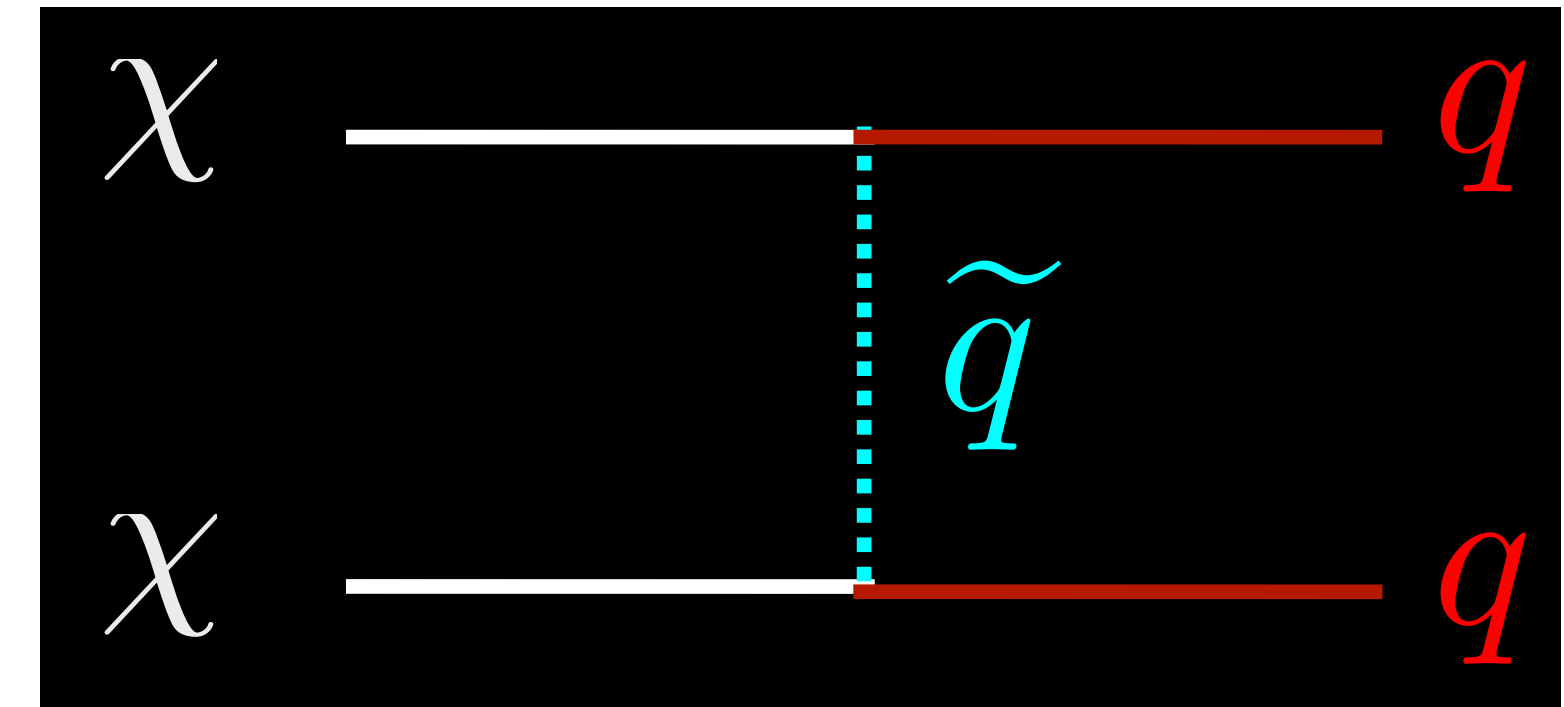
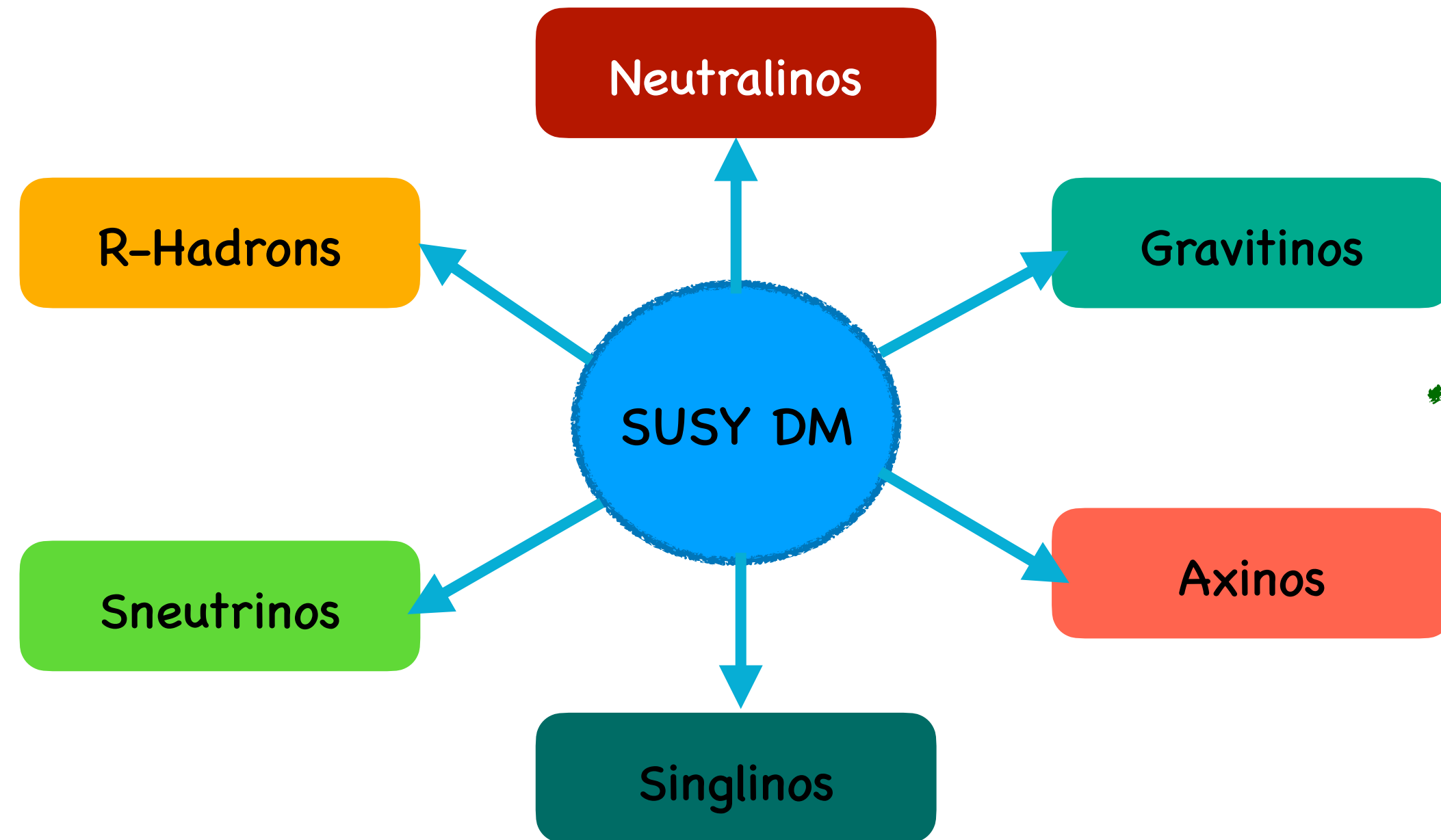
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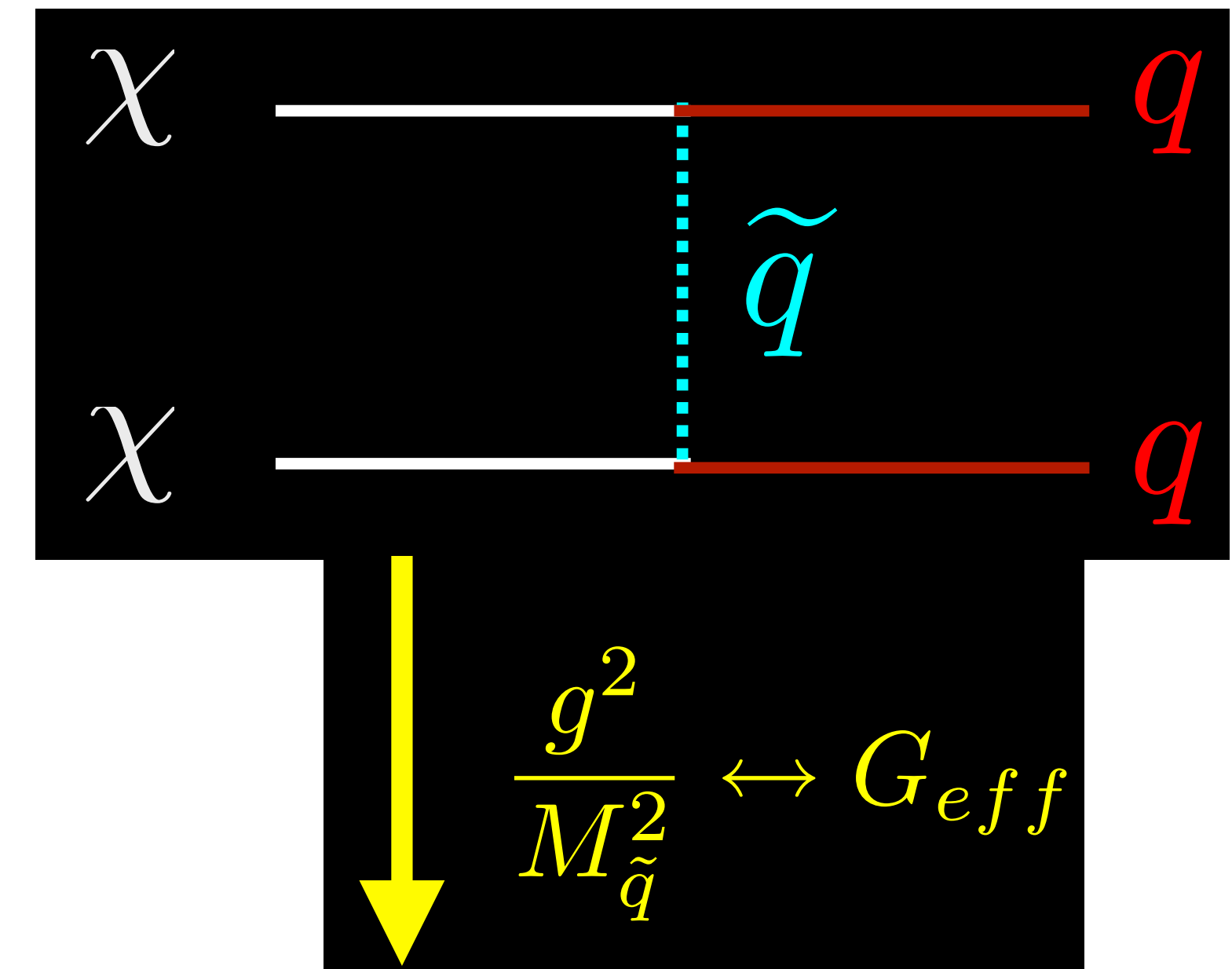
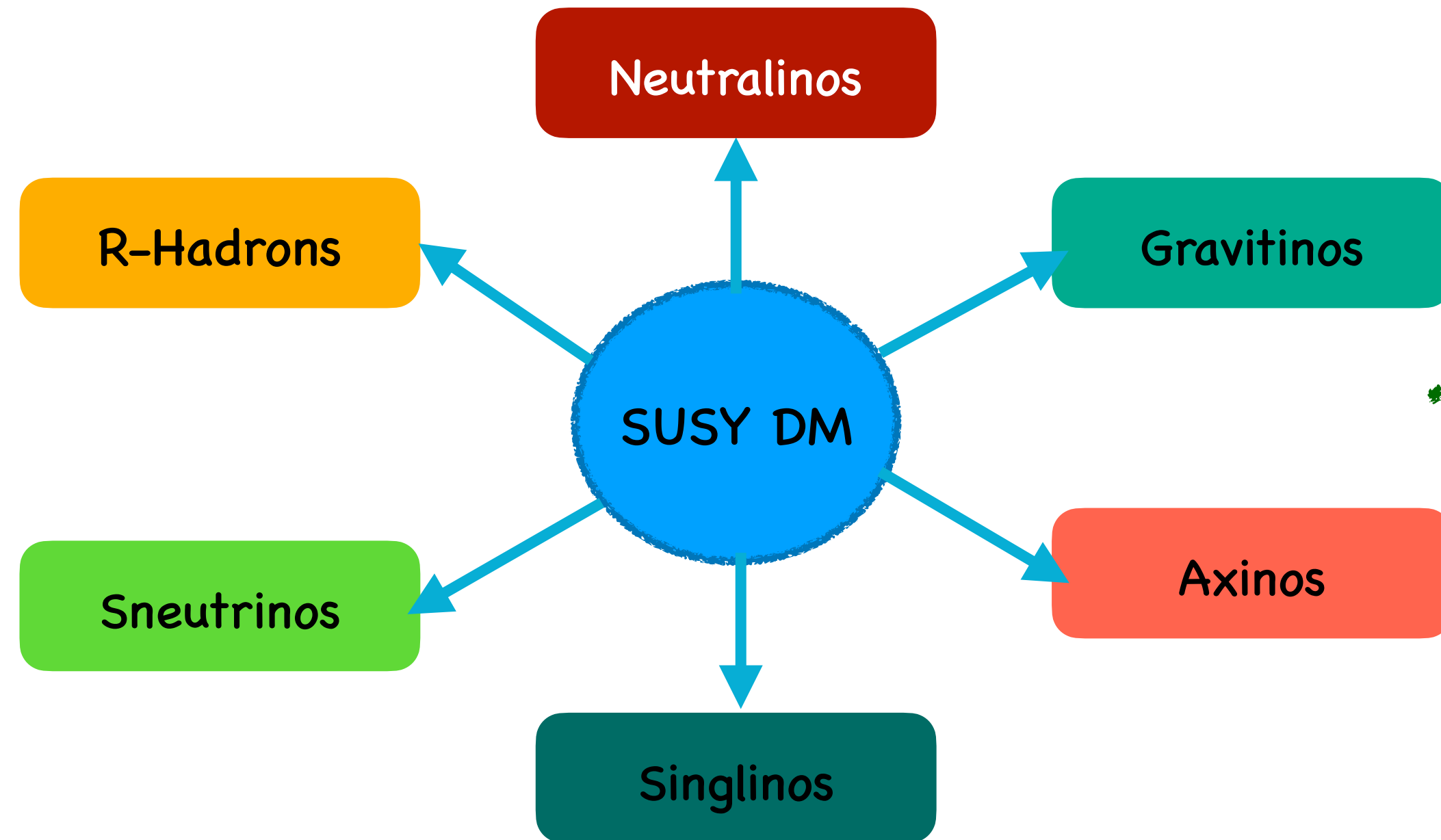
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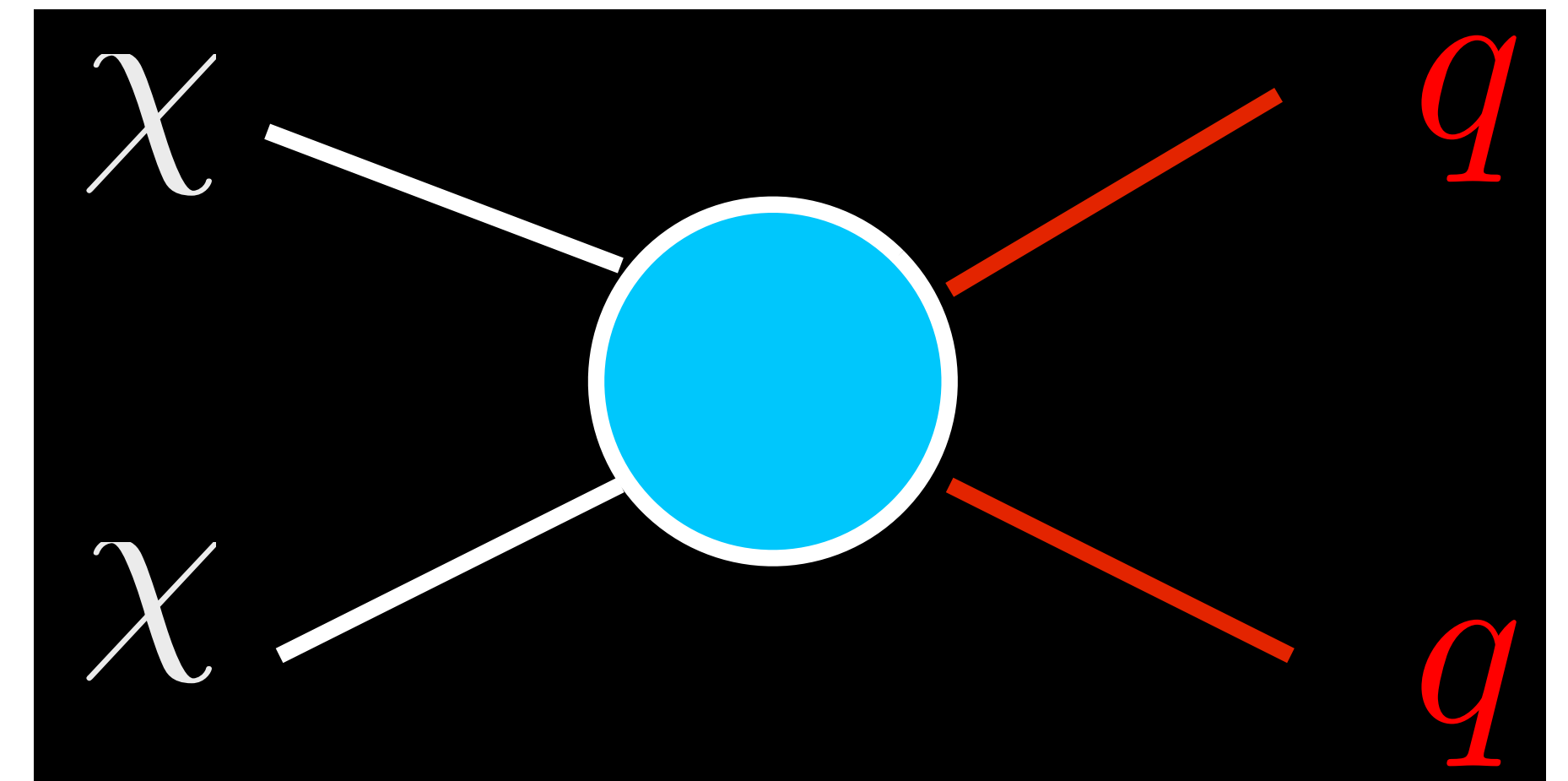
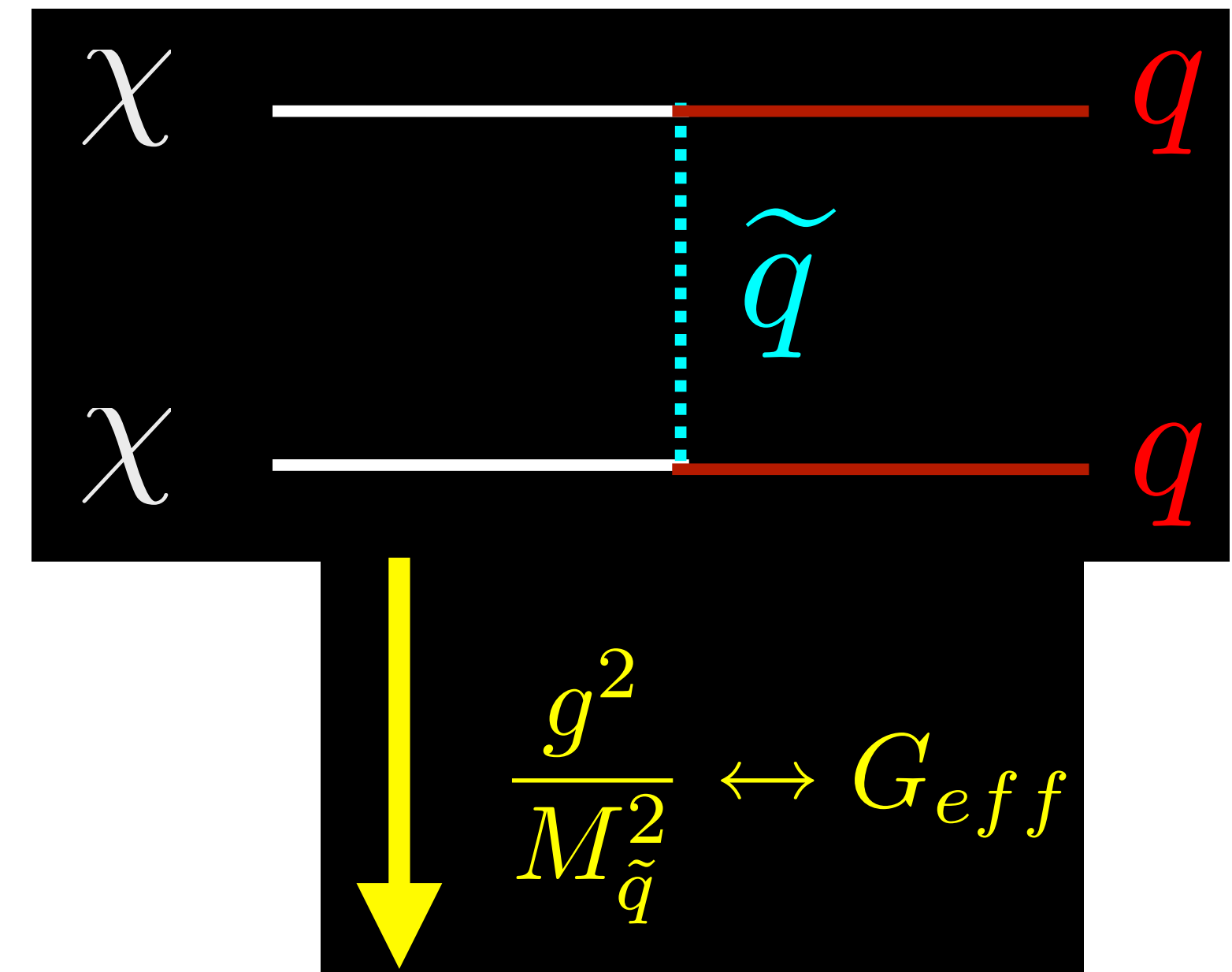
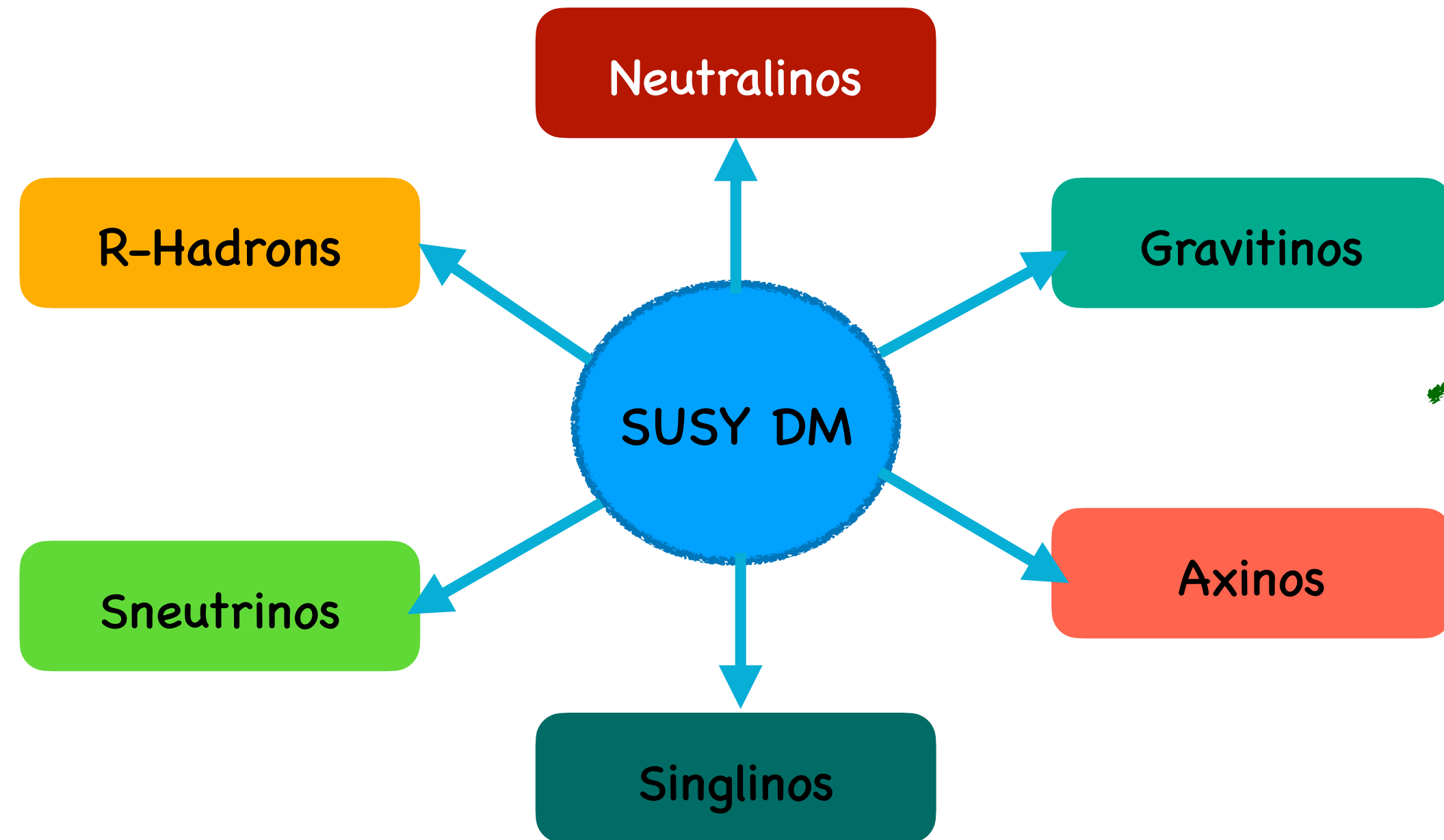
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# Full Models vs EFTs

Majorana Dark Matter: 10 operators with an  
EFT strength  $M$

# Full Models vs EFTs

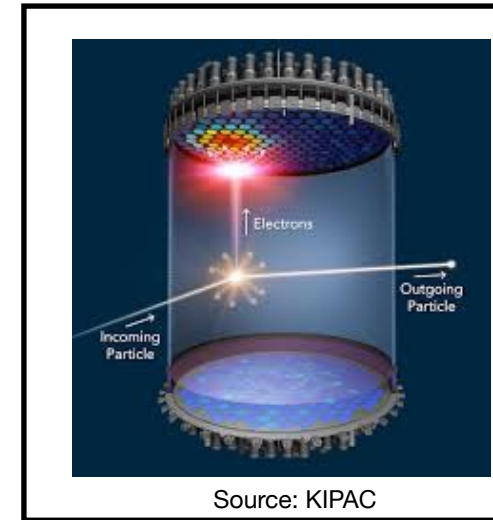
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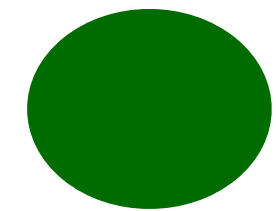
SI Elastic Scattering



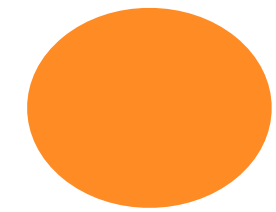
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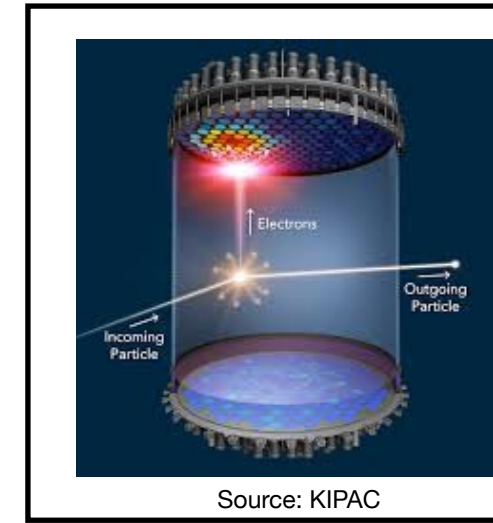
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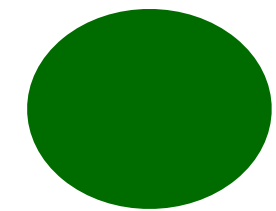
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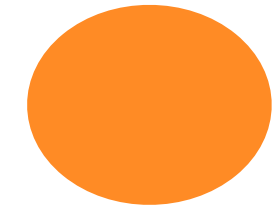
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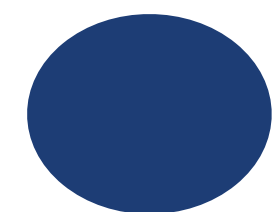
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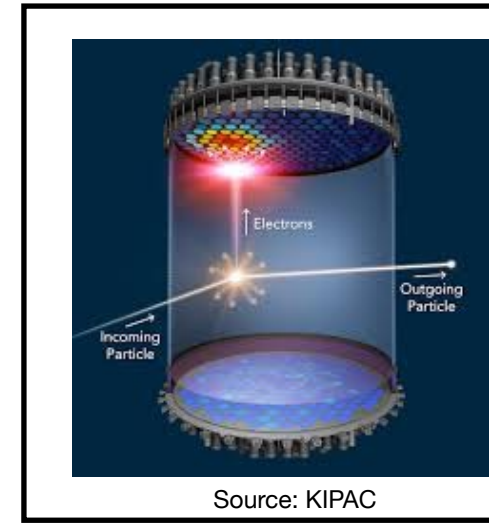
SI Elastic Scattering



SD Elastic Scattering



Annihilation in the galactic halo

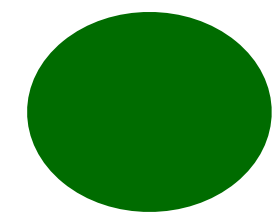


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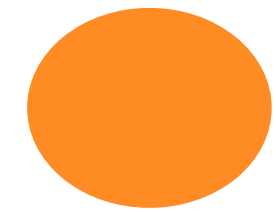


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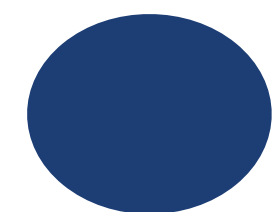
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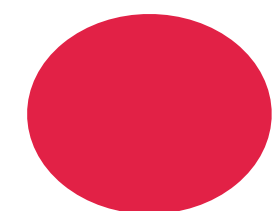
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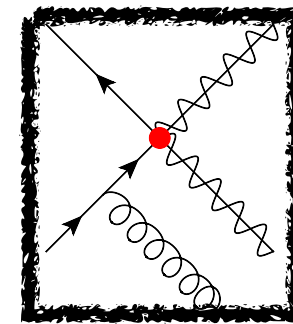
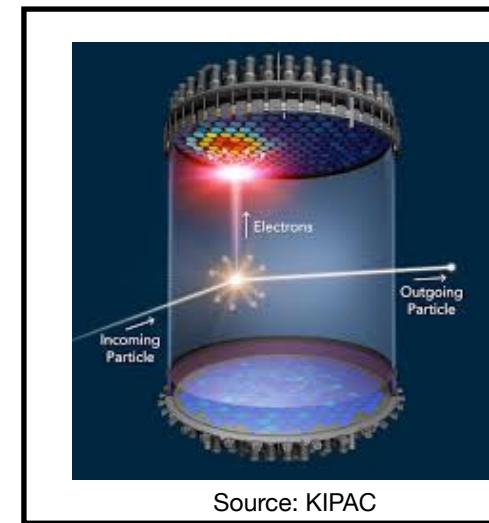
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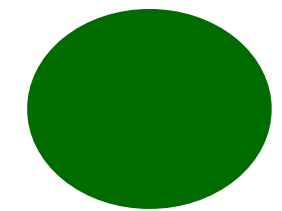
Collider Experiments



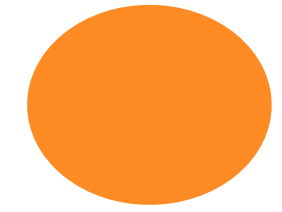
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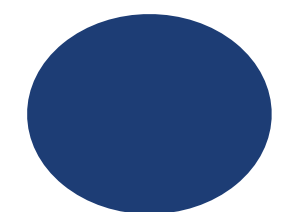
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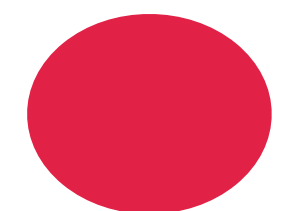
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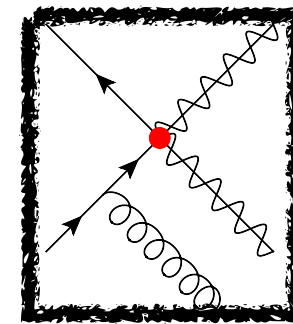
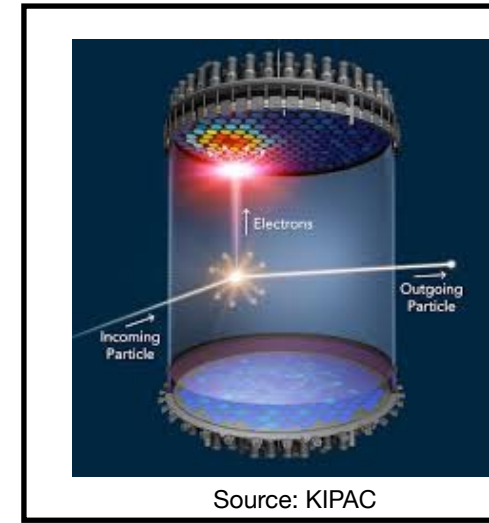
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Collider Experiments



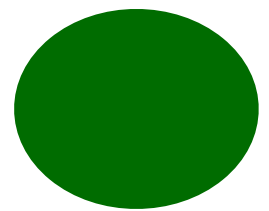
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$$G_\chi [\bar{\chi} \Gamma^\chi \chi] G^2$$

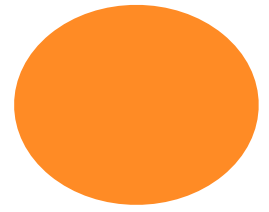
$$\sum_q G_\chi [\bar{q} \Gamma^q q] [\bar{\chi} \Gamma^\chi \chi]$$
 Other operators may be rewritten in this form by using Fierz transformations.

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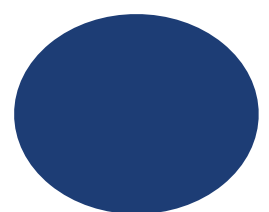
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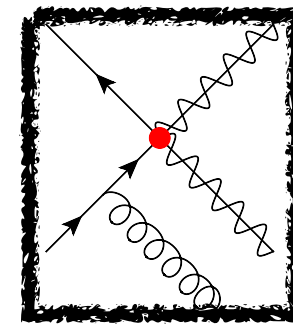
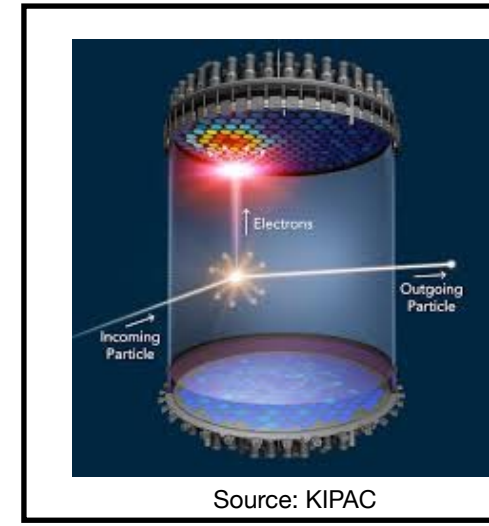
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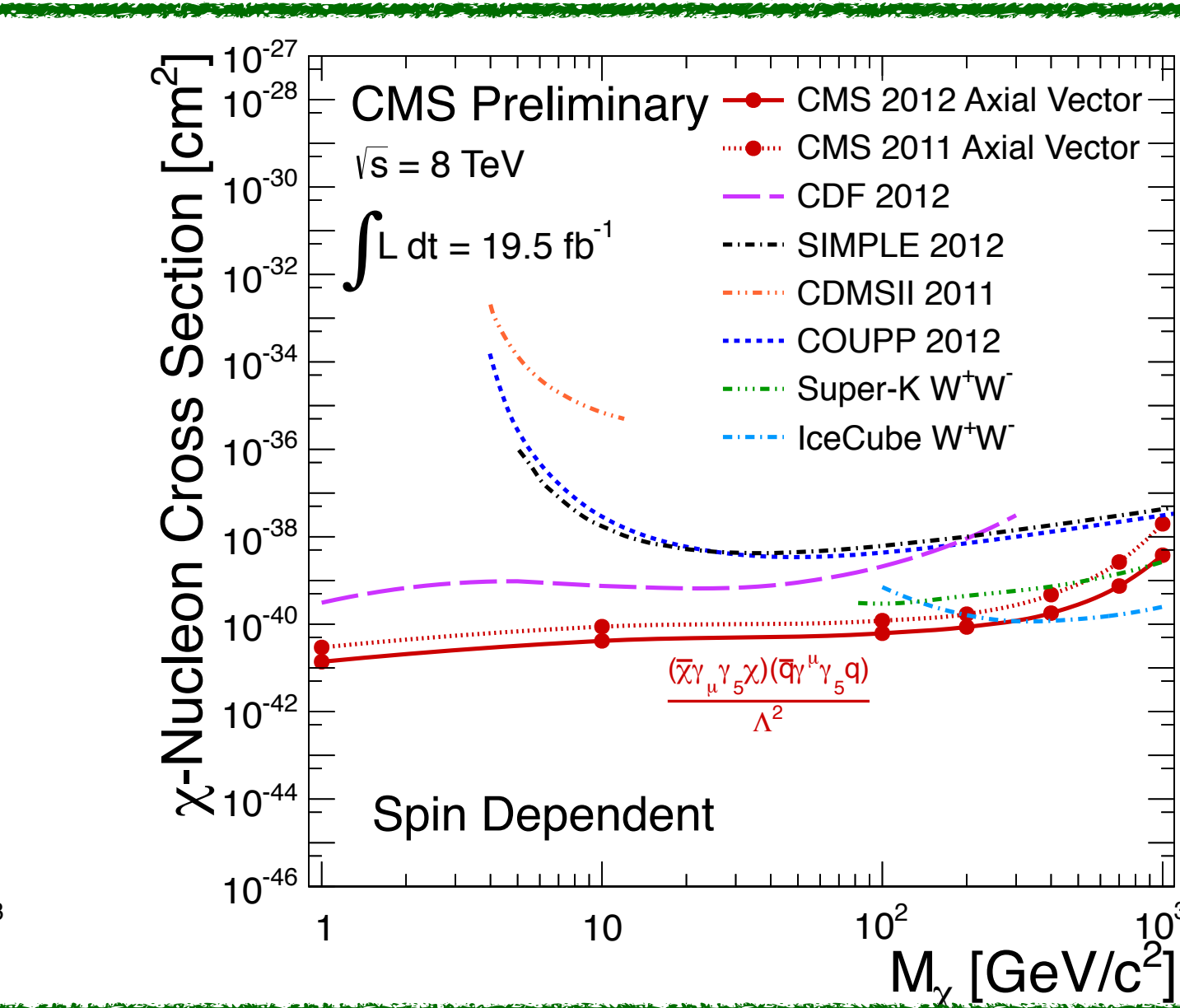
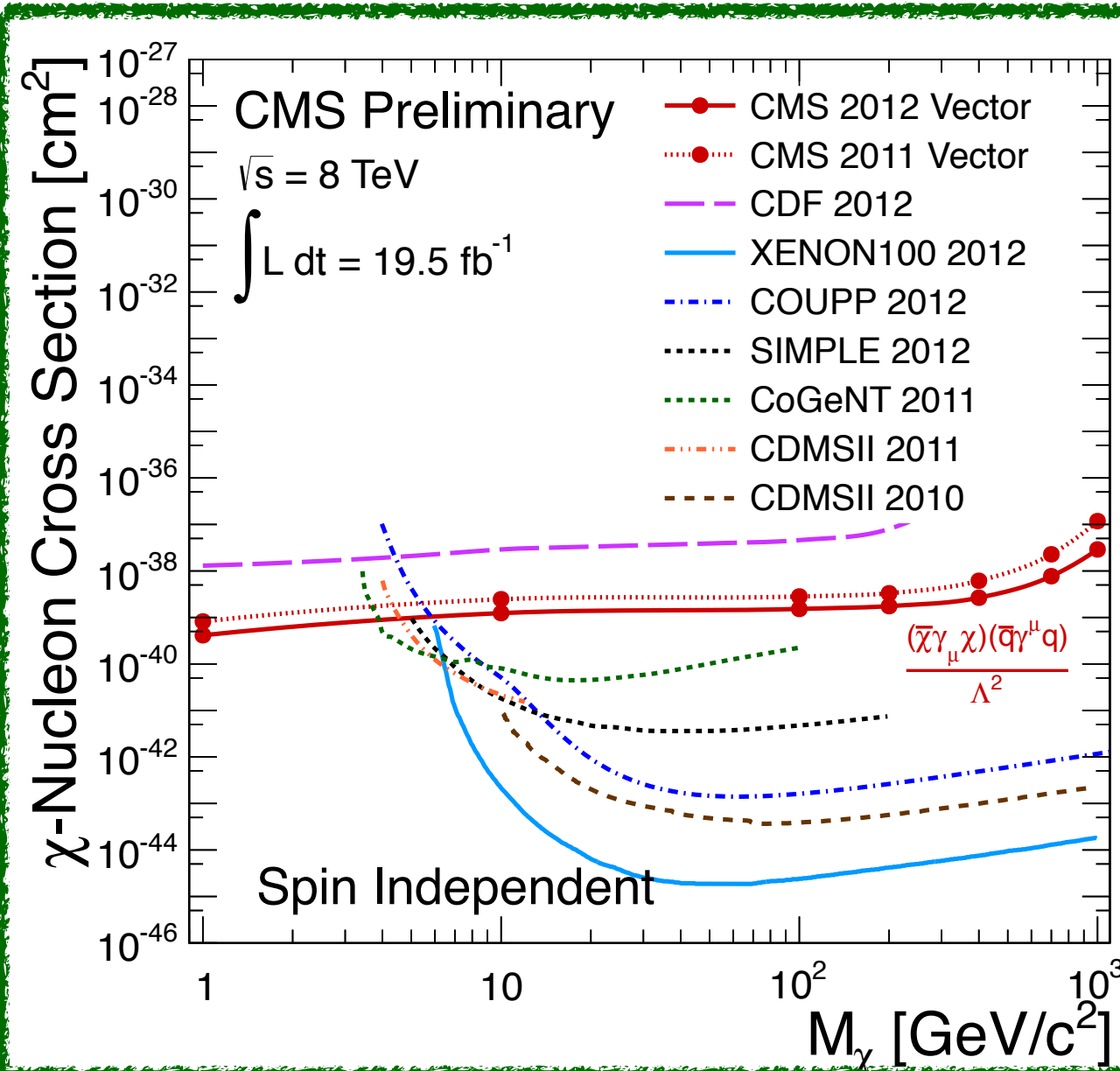
Annihilation in the galactic halo



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 Goodman, Ibe, Rajaraman, Shepherd, TMPT, Yu 1005.1286 & PLB

# EFTs vs Simplified Models

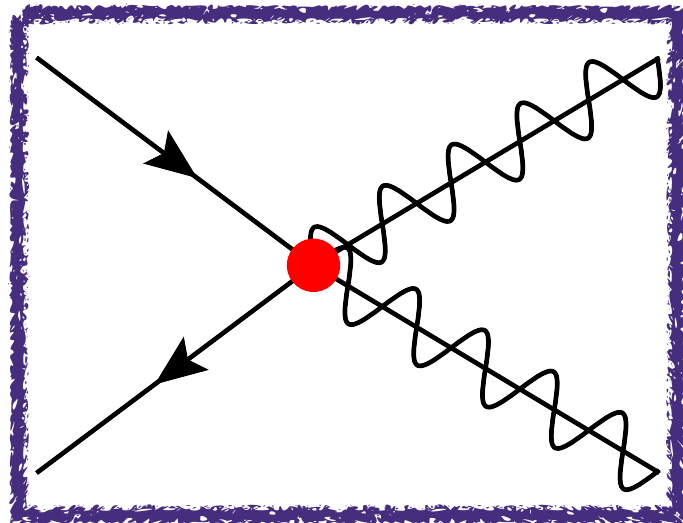
$$\mathcal{L}_{\text{DM-EFT}} = \sum_{f=u,d,s,c,b,t,e,\mu,\tau} \left( \frac{C_1^f}{\Lambda^2} \bar{f} f \bar{\chi} \chi + \frac{C_2^f}{\Lambda^2} \bar{f} \gamma_5 f \bar{\chi} \gamma_5 \chi + \dots \right) \{m_\chi, C_n^f/\Lambda^2\} \quad \text{Justified for } q^2 \ll \Lambda^2$$

The breakdown of EFT is "time-dependent", since energies probed by LHC depend on PDFs, therefore hard to be absolutely quantitative

# EFTs vs Simplified Models

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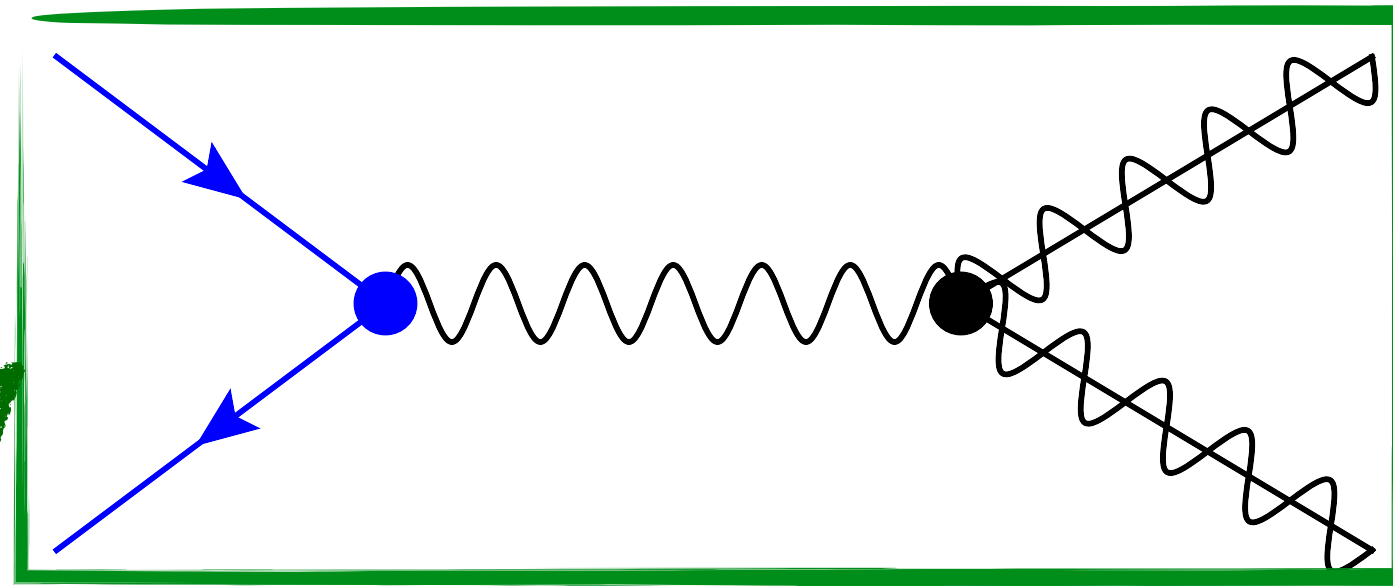
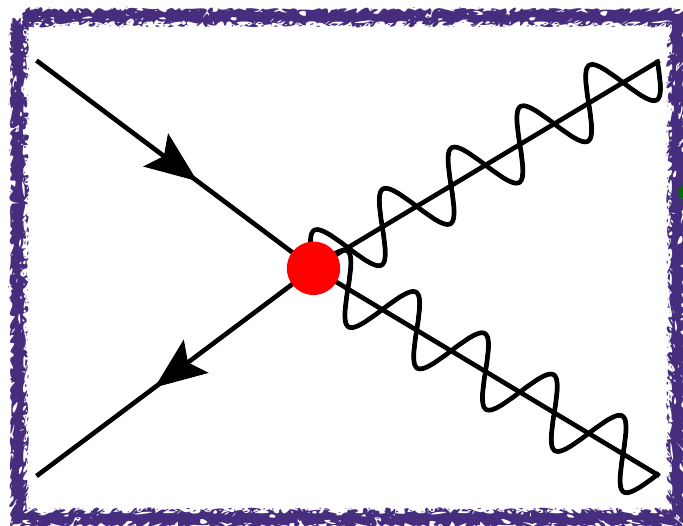
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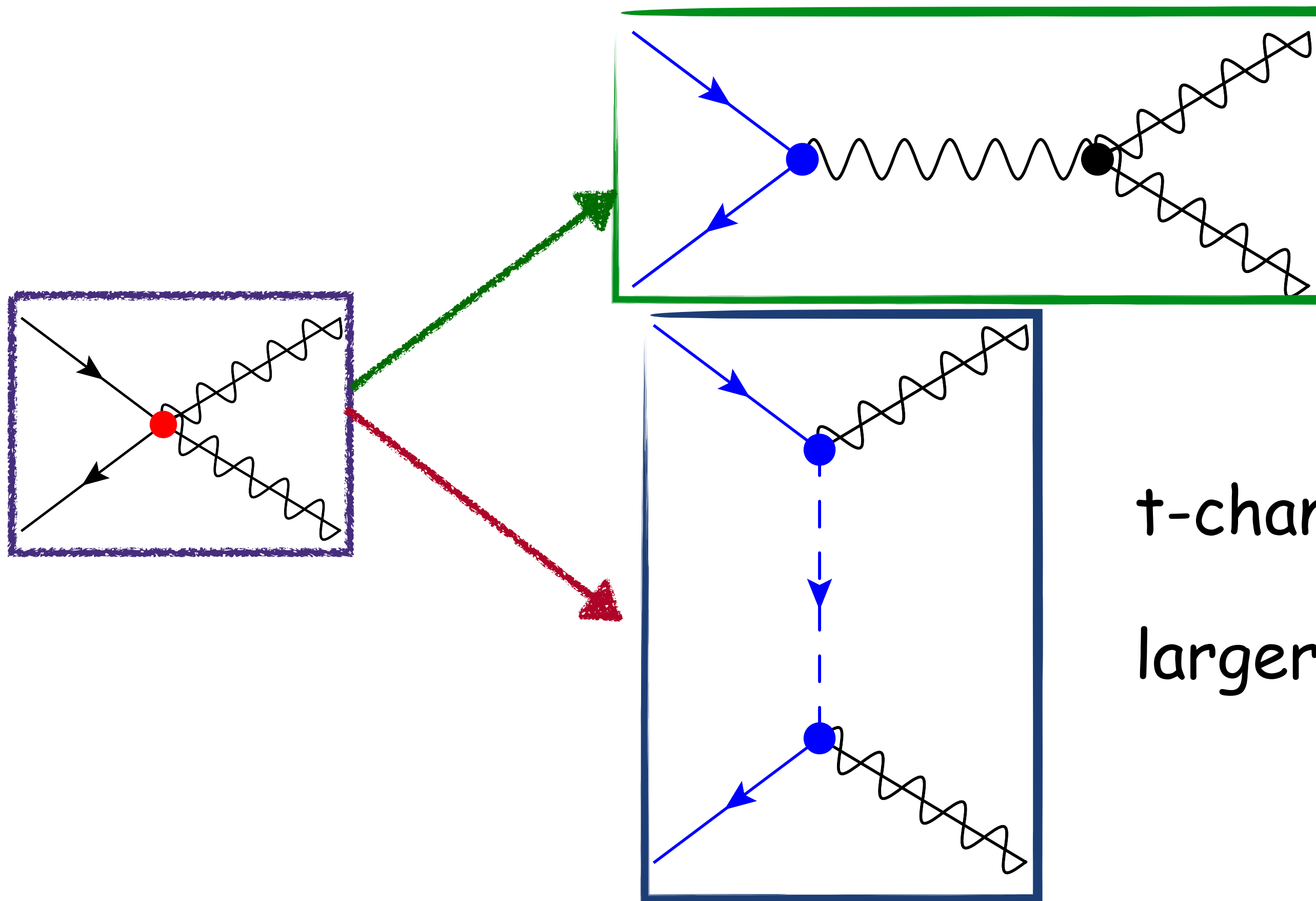


S-channel mediators : Masses can be Larger or smaller than the DM

# EFTs vs Simplified Models

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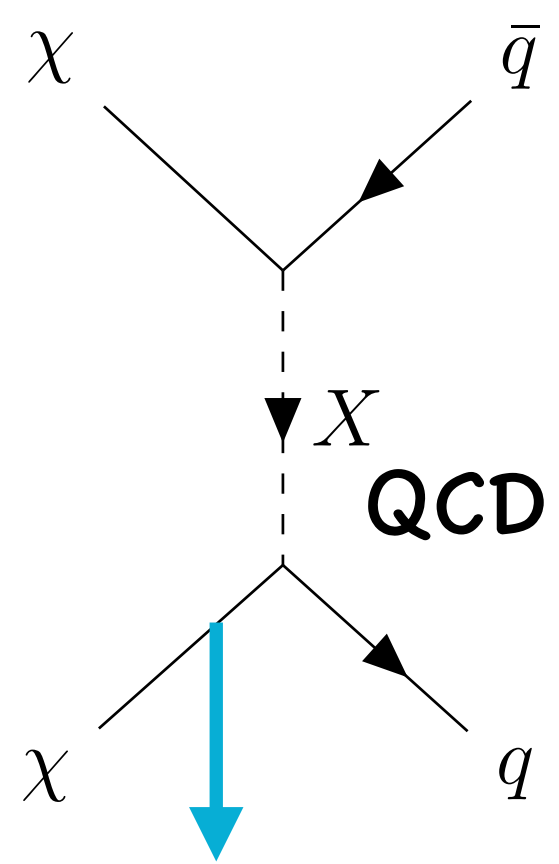


S-channel mediators : Masses can be Larger or smaller than the DM

t-channel mediators : Masses are always larger than the DM (otherwise DM will decay)

# t- channel Simplified Models

A Majorana Fermion Dark Matter (Neutralino) interacting with Scalar Colored Scalar Mediators (Squarks)



Dark Matter particle:  
A Majorana Fermion

$$\mathbf{X} = \tilde{u} = \left\{ \tilde{u}, \tilde{d}, \tilde{s} \right\}, \quad \tilde{d} = \left\{ \tilde{d}, \tilde{s}, \tilde{b} \right\}, \quad \tilde{q} = \left\{ \tilde{u}, \tilde{d}, \tilde{s}, \tilde{c}, \tilde{b}, \tilde{t} \right\}$$

$$\left[ (SU(3), SU(2))_Y \right] \quad (3, 1)_{2/3} \quad (3, 1)_{-1/3} \quad (3, 2)_{-1/6}$$

$$\mathcal{L} \supset \sum_i (D_\mu X_i)^\dagger (D^\mu X_i) + \sum_{i,j} \left( g_{\text{DM},ij} X_i^\dagger \bar{\chi} P_R q_j + g_{\text{DM},ij}^* X_i \bar{q}_j P_L \chi \right)$$

$$\mathcal{L}_{u_R} = \sum_u \left[ (D_\mu \tilde{u})^* (D^\mu \tilde{u}) - M_{\tilde{u}}^2 \tilde{u}^* \tilde{u} + g_{\text{DM}} \tilde{u}^* \bar{\chi} P_R u + g_{\text{DM}}^* \tilde{u} \bar{u} P_L \chi \right]$$

$$\mathcal{L}_{d_R} = \sum_d \left[ (D_\mu \tilde{d})^* (D^\mu \tilde{d}) - M_{\tilde{d}}^2 \tilde{d}^* \tilde{d} + g_{\text{DM}} \tilde{d}^* \bar{\chi} P_R d + g_{\text{DM}}^* \tilde{d} \bar{d} P_L \chi \right]$$

$$\mathcal{L}_{q_L} = \sum_{\tilde{q}} \left[ (D_\mu \tilde{q})^* (D^\mu \tilde{q}) - M_{\tilde{q}}^2 \tilde{q}^* \tilde{q} + g_{\text{DM}} \tilde{q}^* \bar{\chi} P_L q + g_{\text{DM}}^* \tilde{q} \bar{q} P_R \chi \right]$$



# t- channel Simplified Models

Relic Density/velocity averaged cross-section

$$\langle \sigma v \rangle \simeq N_c^f g_{DM}^4 \left[ \frac{m_f^2 \sqrt{1 - \frac{m_f^2}{m_\chi^2}}}{64\pi(m_{\tilde{q}}^2 + m_\chi^2 - m_f^2)^2} + \beta^2 \left\{ \frac{m_\chi^2 \sqrt{m_\chi^4 + m_{\tilde{q}}^4}}{32\pi(m_\chi^2 + m_{\tilde{q}}^2)^4} + \mathcal{O}(m_f^2) \right\} \right]$$

Velocity independent part (s wave)

Velocity dependent part (p wave)

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# t- channel Simplified Models

Relic Density/velocity averaged cross-section

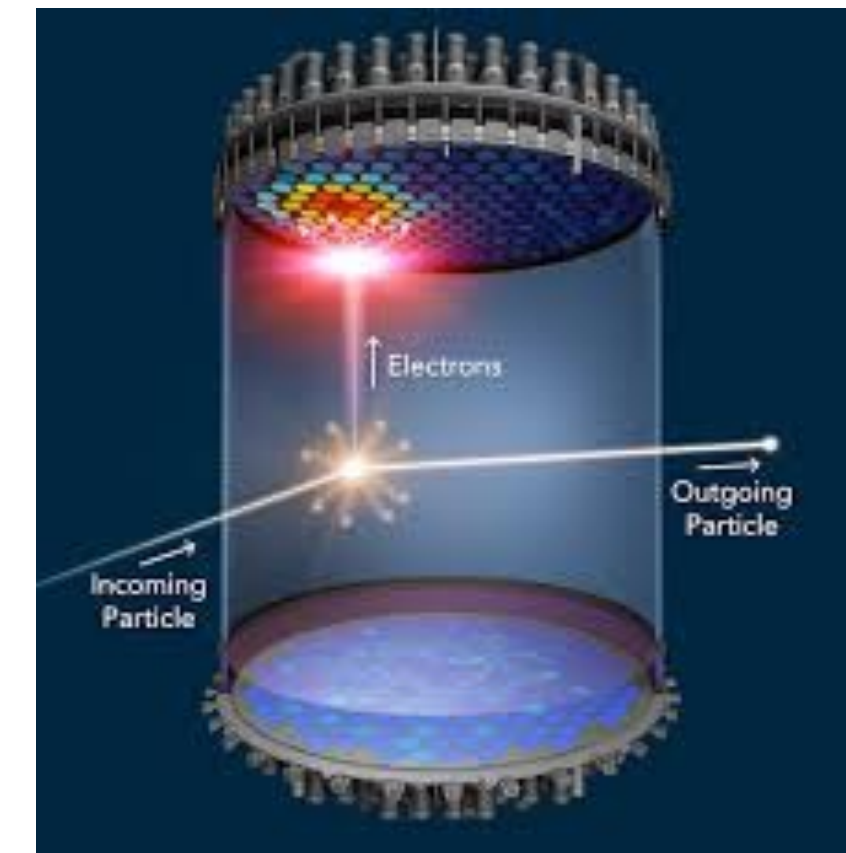
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Velocity independent part (s wave)

Velocity dependent part (p wave)

Spin-Independent : Coherent interaction with the whole Atomic Nucleus

Spin-Dependent : For Axial Vector coupling, couples to the spin of the Nucleus



Source: KIPAC

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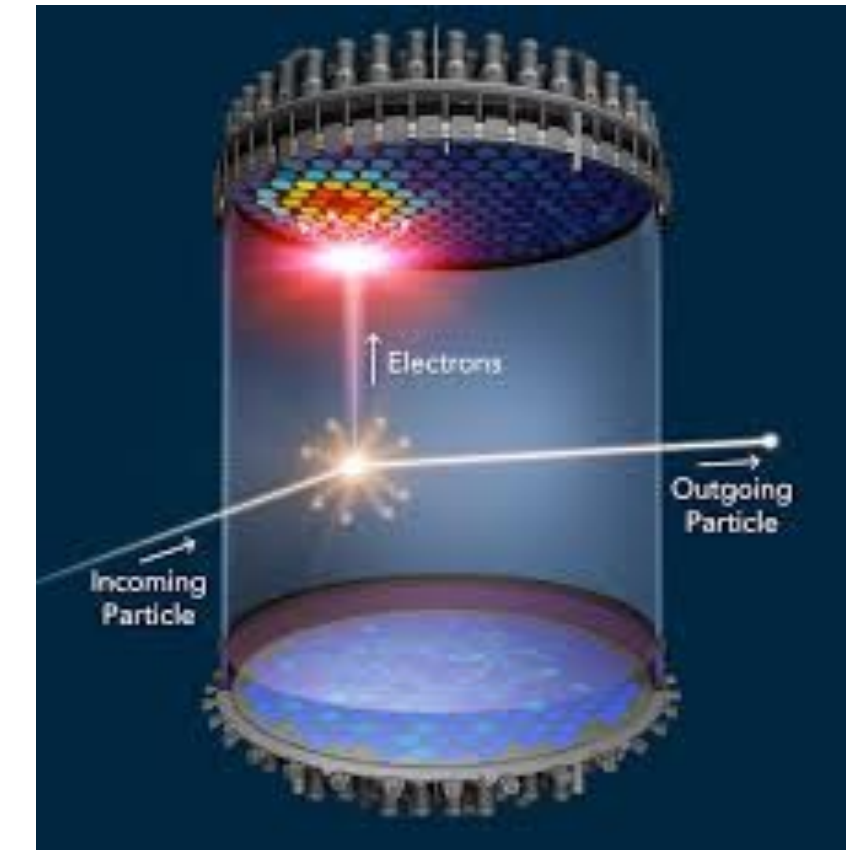
Velocity independent part (s wave)

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- Given a DM model, we need to calculate the spin-independent and spin-dependent cross sections at the quark level and match it at the nucleon level using form factors
- Spin-Independent limits at tree level more constraining than the spin-dependent part



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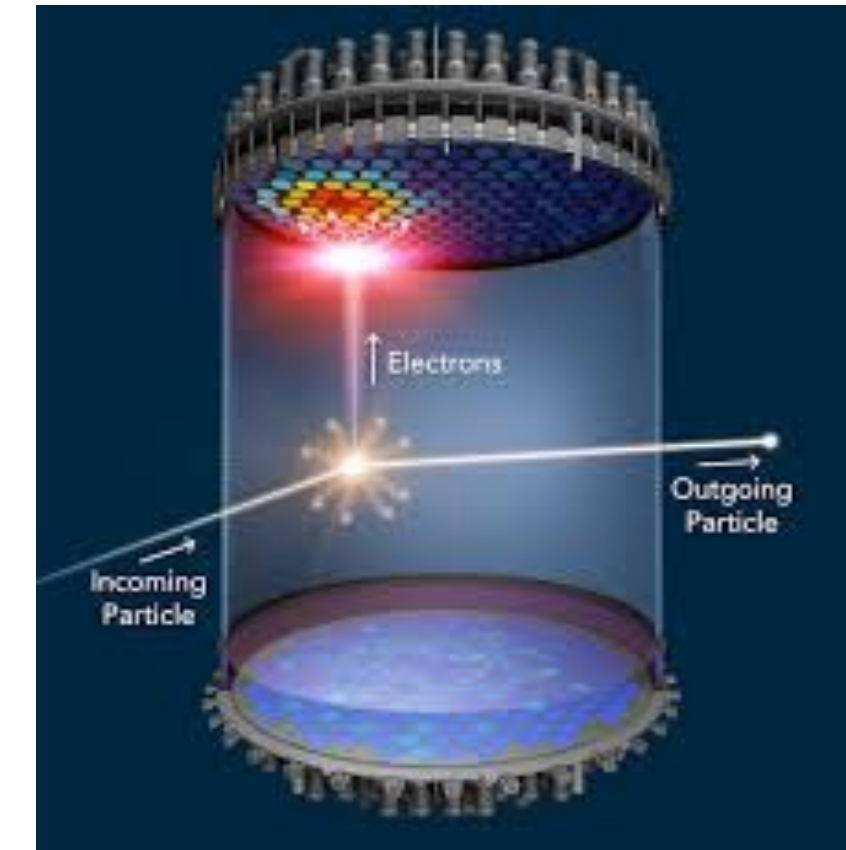
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$$\mathcal{M} = (-ig_{DM})^2 (\bar{\chi} P_R u) \frac{i}{p^2 - M_{\tilde{u}}^2} (\bar{u} P_L \chi) \approx \frac{ig_{DM}^2}{M_{\tilde{u}}^2 - m_\chi^2} \frac{1}{8} [(\bar{\chi} \gamma^\mu \chi)(\bar{u} \gamma_\mu u) - (\bar{\chi} \gamma^\mu \gamma^5 \chi)(\bar{u} \gamma_\mu \gamma^5 u)]$$

SI = 0 for Majorana fermion  
at tree level, Vector Bilinear vanishes

$$\sigma_p = \frac{4}{\pi} \left( \frac{M_\chi m_p}{M_\chi + m_p} \right)^2 |\langle \mathcal{M}_{DD} \rangle_{NR}|^2$$



Source: KIPAC

# t- channel Simplified Models

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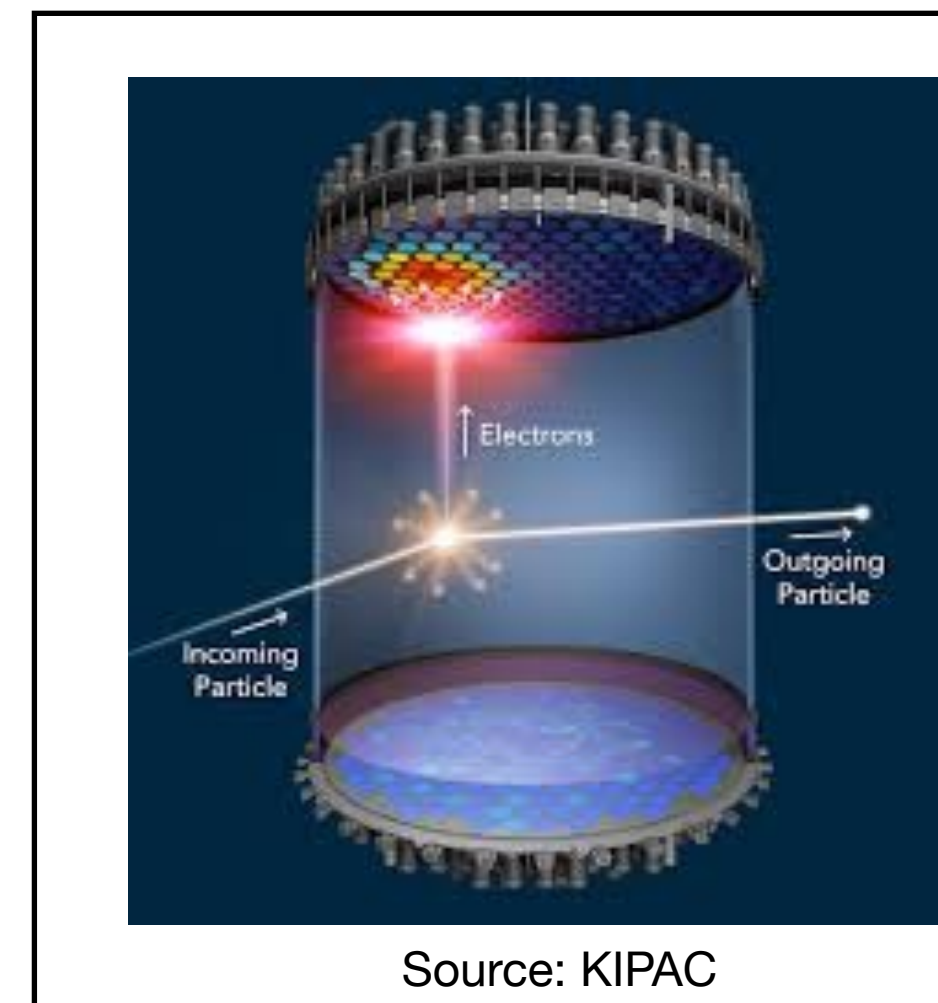
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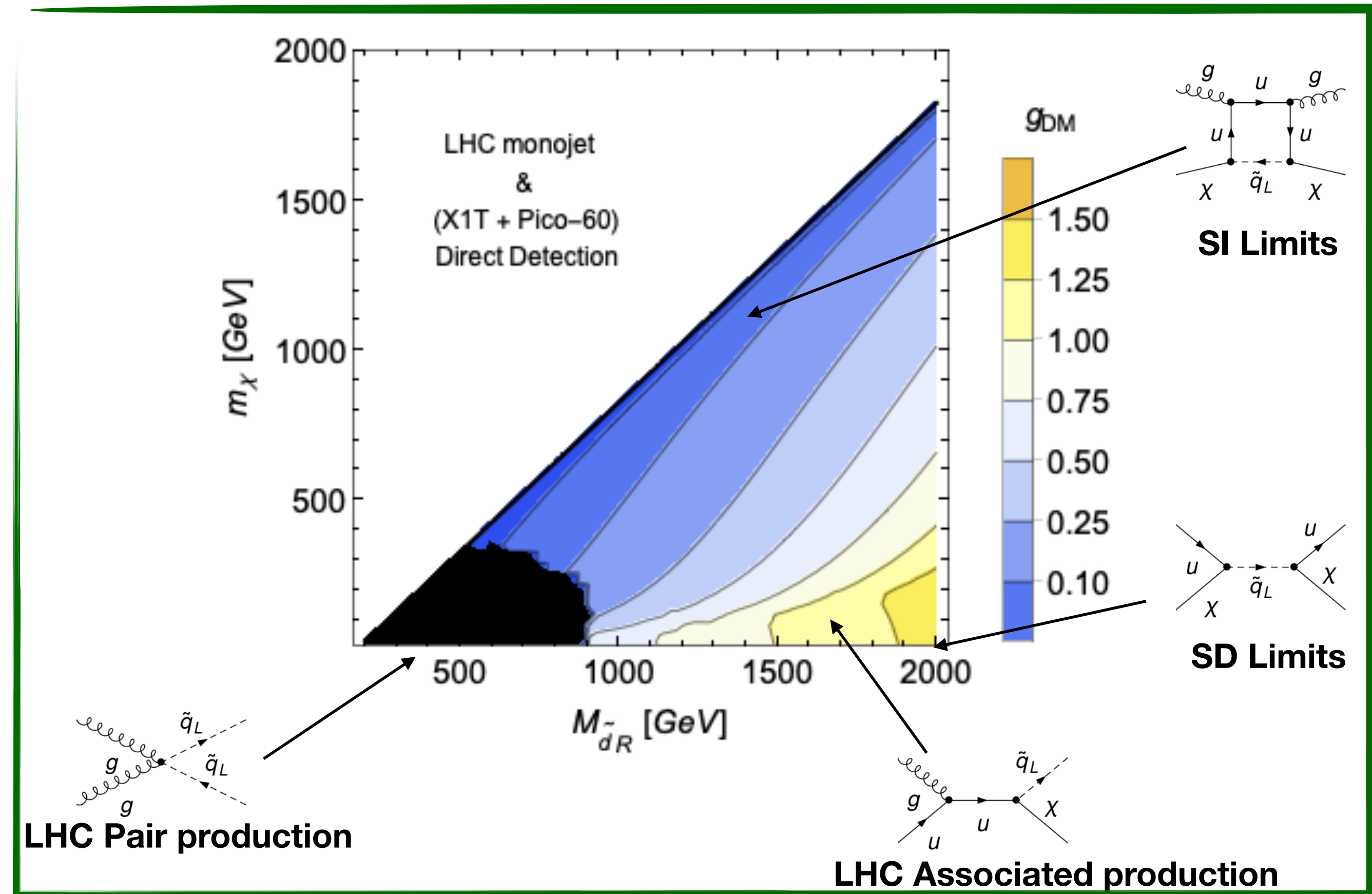
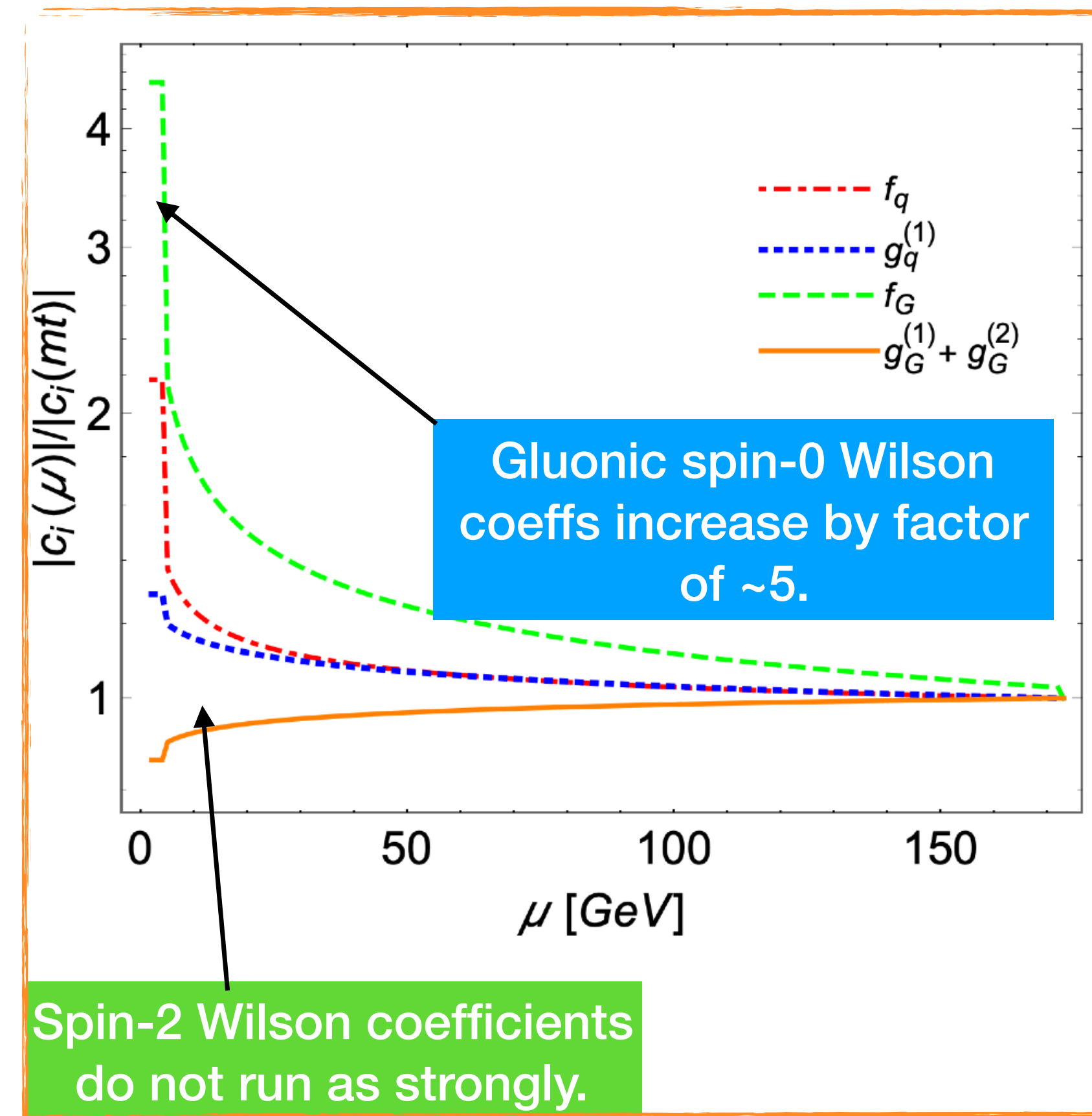
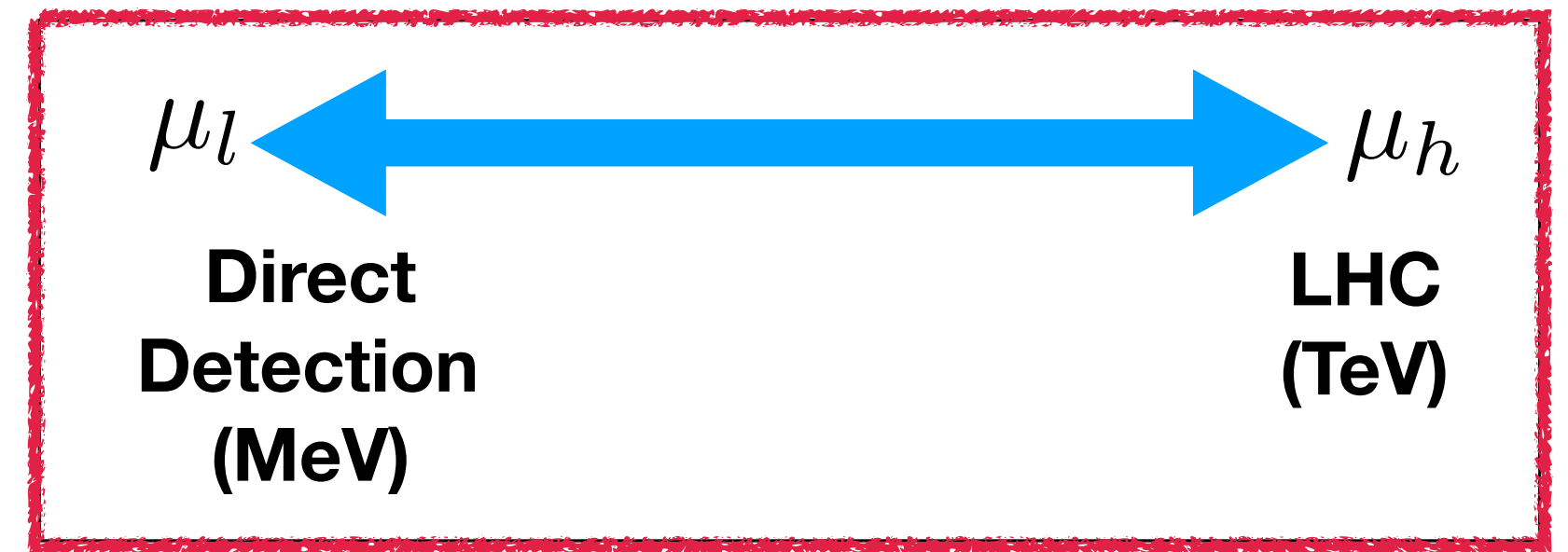
Is the spin-independent 1-loop more sensitive than the tree level spin-dependent direct detection limit?

# t-channel Simplified Models

We also need a Renormalization Group Evolution

At what scale do we define coupling and masses?

If at nuclear scale, to compare to LHC we should run up, for the reverse, run down.



Factor 4 enhancement in cross-section

Take home message

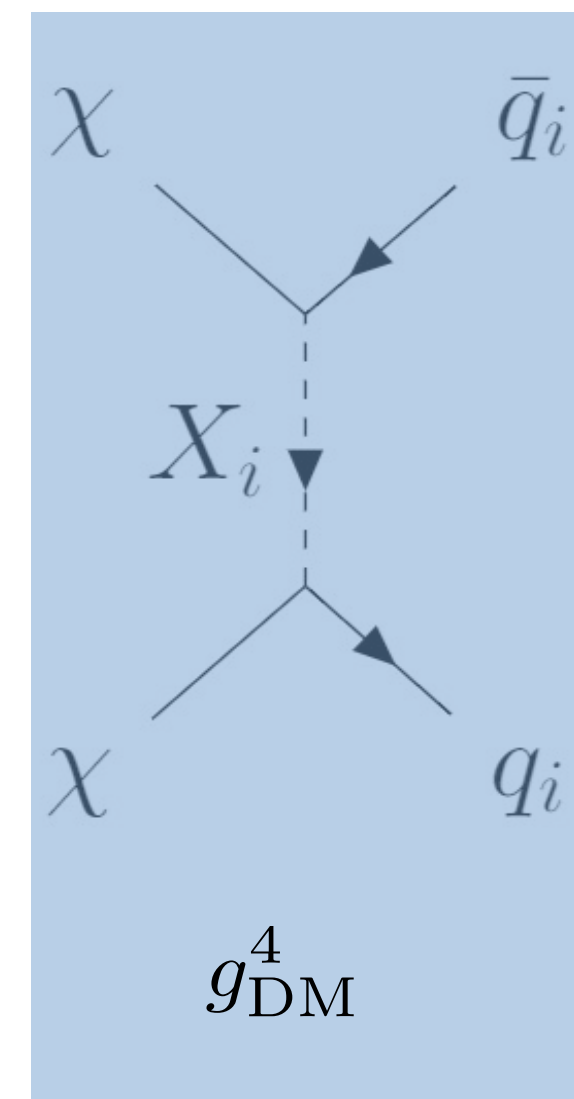
Precision Calculations can significantly improve constraints on the coupling (DM interaction)

See K. Mohan, **DS**, T. Tait, B. Yan, C.P. Yuan. JHEP 05 (2019) 115 for details

# Coannihilations, Radiative and Non-Perturbative Effects in Relic Density Calculation

**Let's go deeper into the same model,  
think of small mass gap between DM and mediator**

$$\delta \equiv \frac{m_X - m_\chi}{m_\chi} \equiv \frac{\Delta m}{m_\chi}, \quad \Delta m \equiv m_X - m_\chi$$

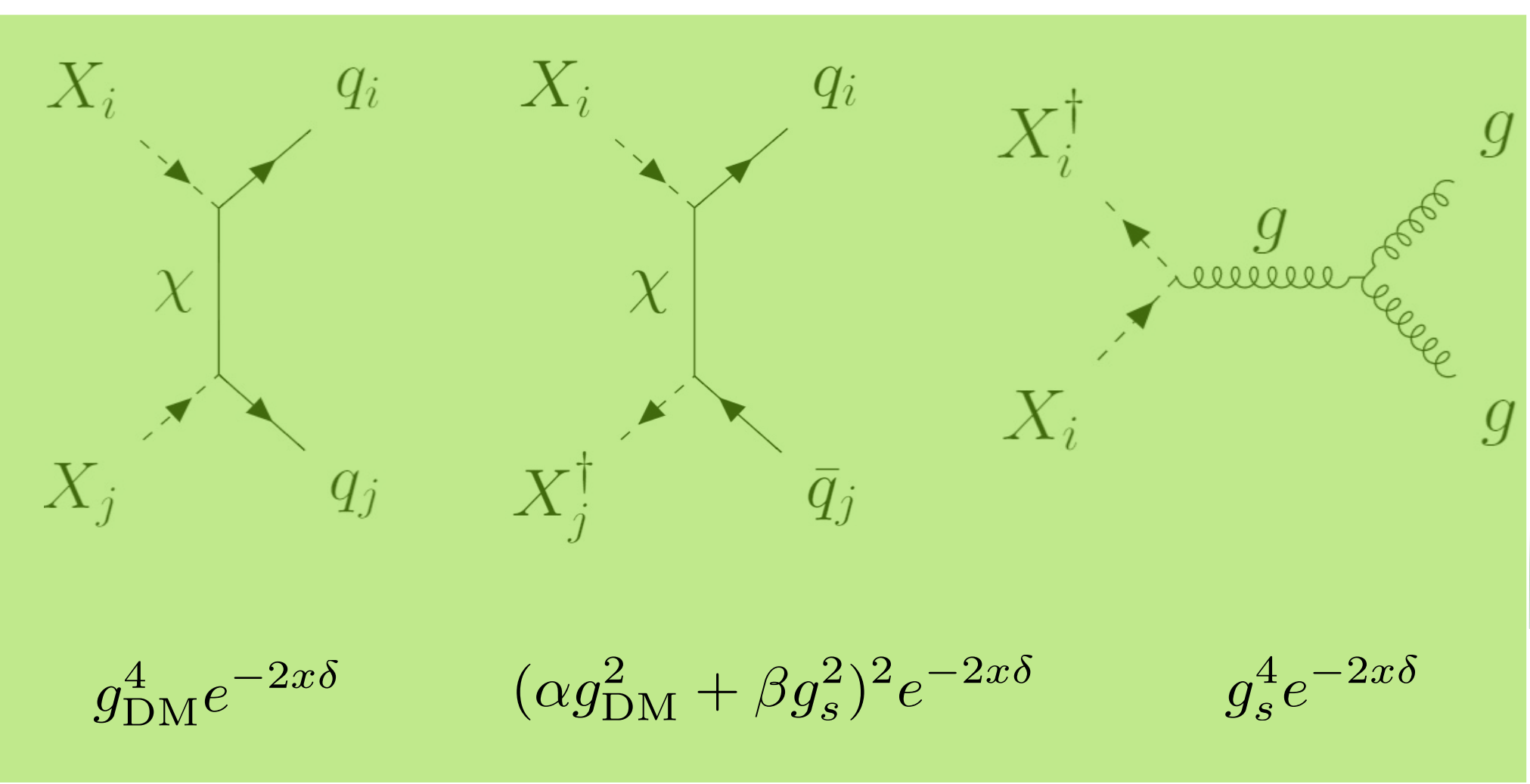
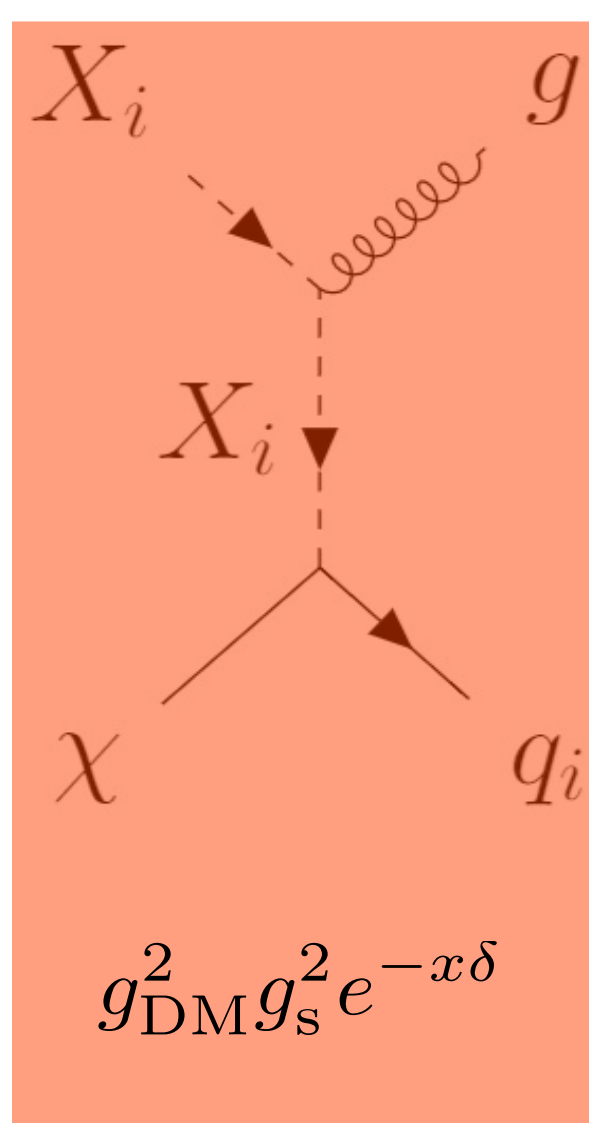
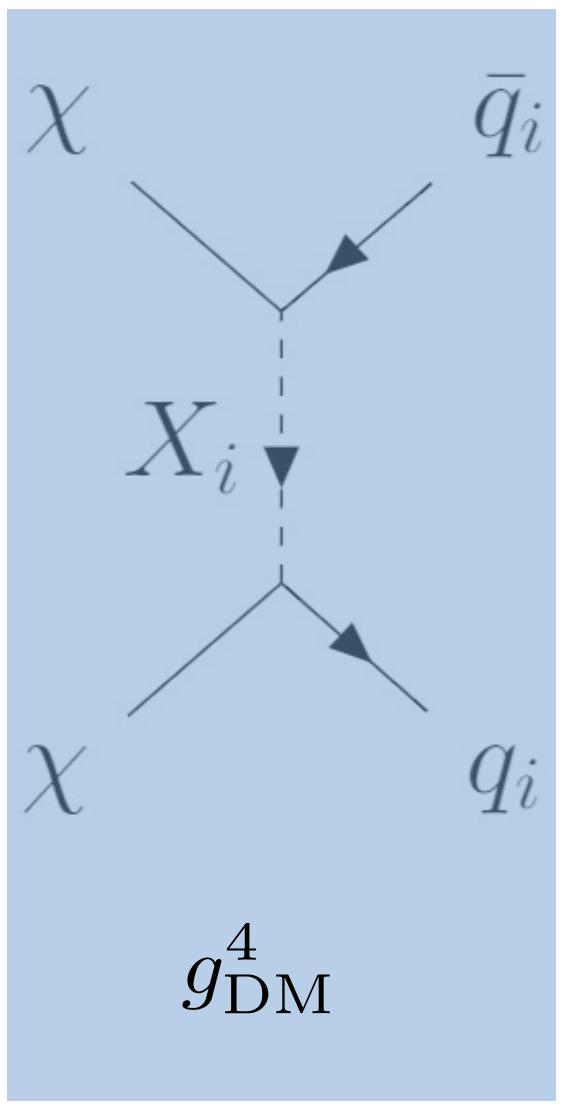


**Large mass gap,  
only relevant process**

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$$\frac{dn}{dt} + 3Hn = -\langle \sigma_{\text{eff}} v \rangle (n^2 - n_{\text{eq}}^2)$$

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Coannihilating channels in Boltzmann equations

Large mass gap,  
only relevant process

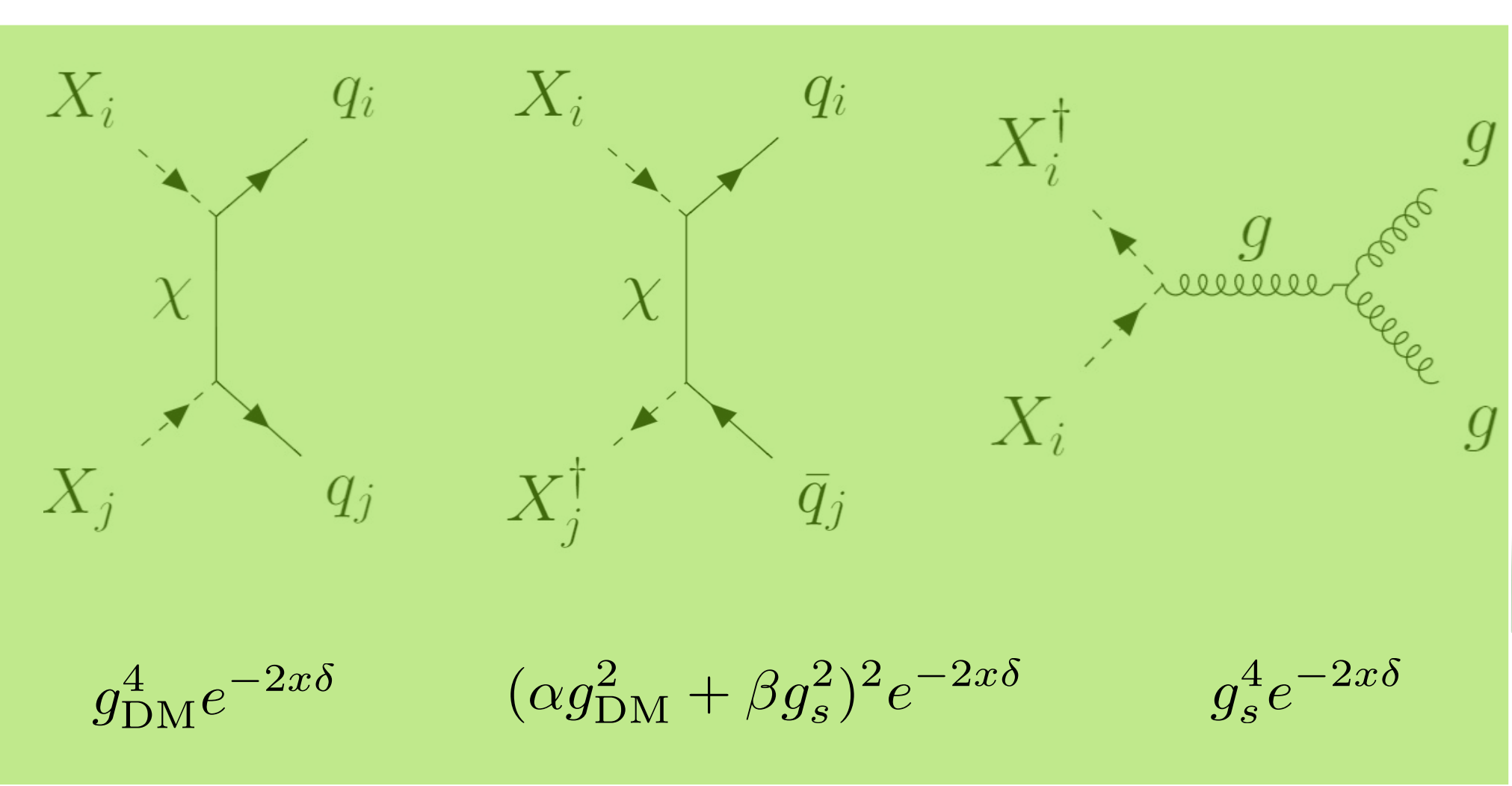
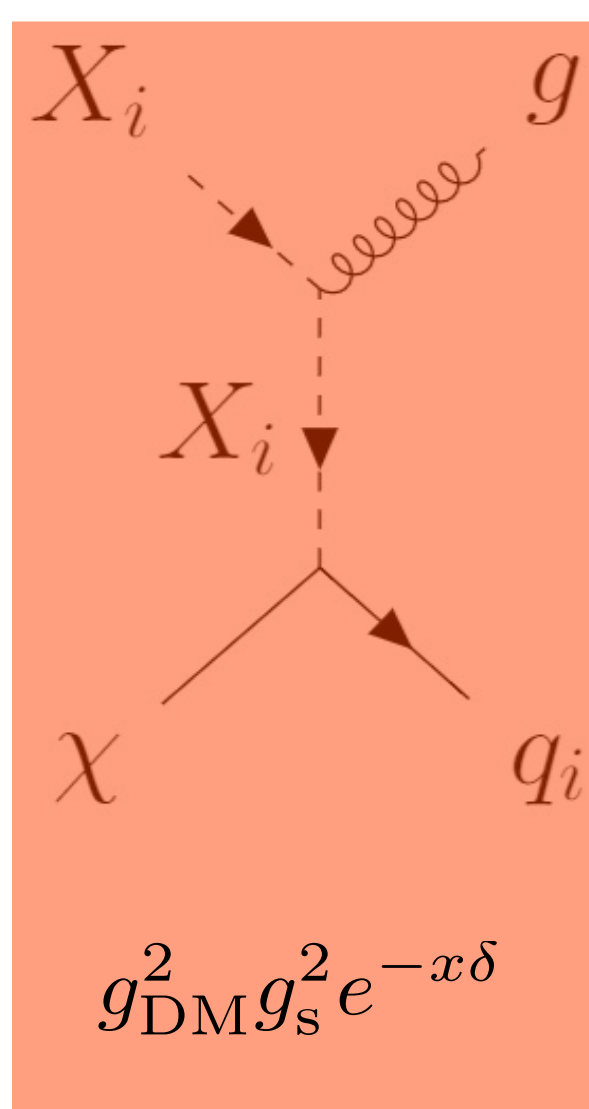
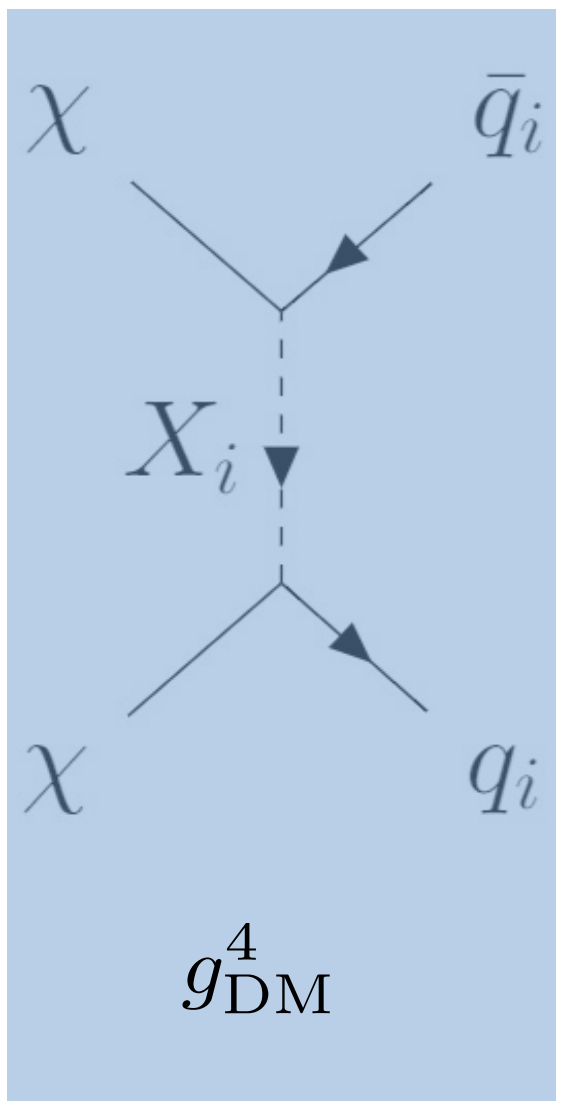
Small mass gap, additional coannihilation channels become relevant



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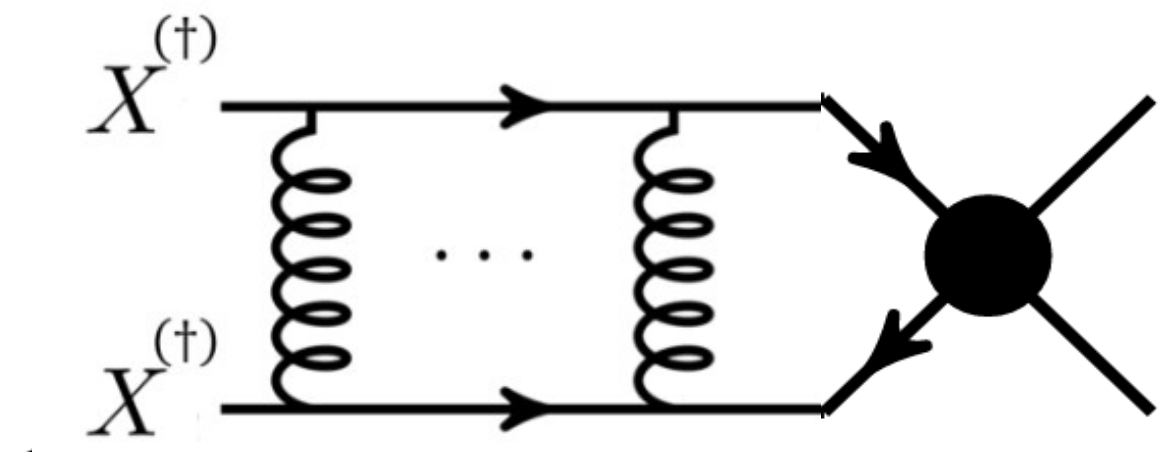
## Assumptions:

- Coannihilating particle will later decay into DM  $n = \sum_{i=1}^N n_i$
- Coannihilating particle in thermal equilibrium with DM particle  $\Gamma(X + SM \longleftrightarrow \chi + SM) \gg H$

Two further novel effects can affect the velocity averaged cross section

# Sommerfeld Enhancement and Bound State Formation in relic abundance

## Sommerfeld Enhancement



$$\mathbf{3} \otimes \bar{\mathbf{3}} = \mathbf{1} \oplus \mathbf{8}$$

$$\mathbf{3} \otimes \mathbf{3} = \bar{\mathbf{3}} \oplus \mathbf{6}$$

- Relevant for  $\alpha \sim v_{\text{rel}}$
- Exchange of  $n$  gluons lead to  $\left(\frac{\alpha}{v_{\text{rel}}}\right)^n \sim 1$ , which requires resummation

Non-relativistic enhancement of cross section due to an attractive potential

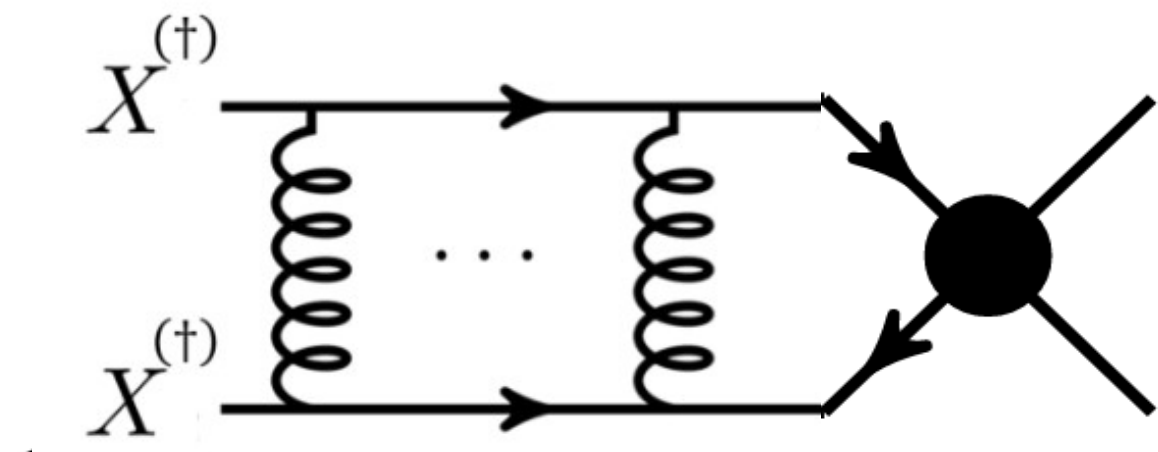
$$V(r)_{\mathbf{3} \otimes \bar{\mathbf{3}}} = \begin{cases} -\frac{4}{3} \frac{\alpha_s^S}{r} & [1] \quad \text{attractive} \\ +\frac{1}{6} \frac{\alpha_s^S}{r} & [8] \quad \text{repulsive} \end{cases}$$

$$\sigma_{\text{SE}} = S_0 \left( \frac{\alpha_s^S C_{[\hat{\mathbf{R}}]}}{v_{\text{rel}}} \right) \sigma_0$$

**Enhancement for attractive potential**

# Sommerfeld Enhancement and Bound State Formation in relic abundance

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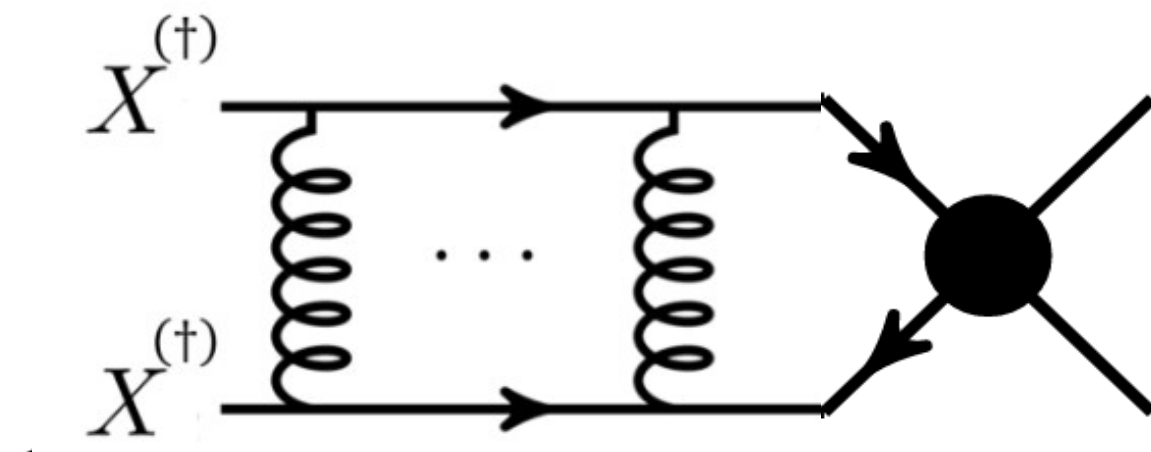
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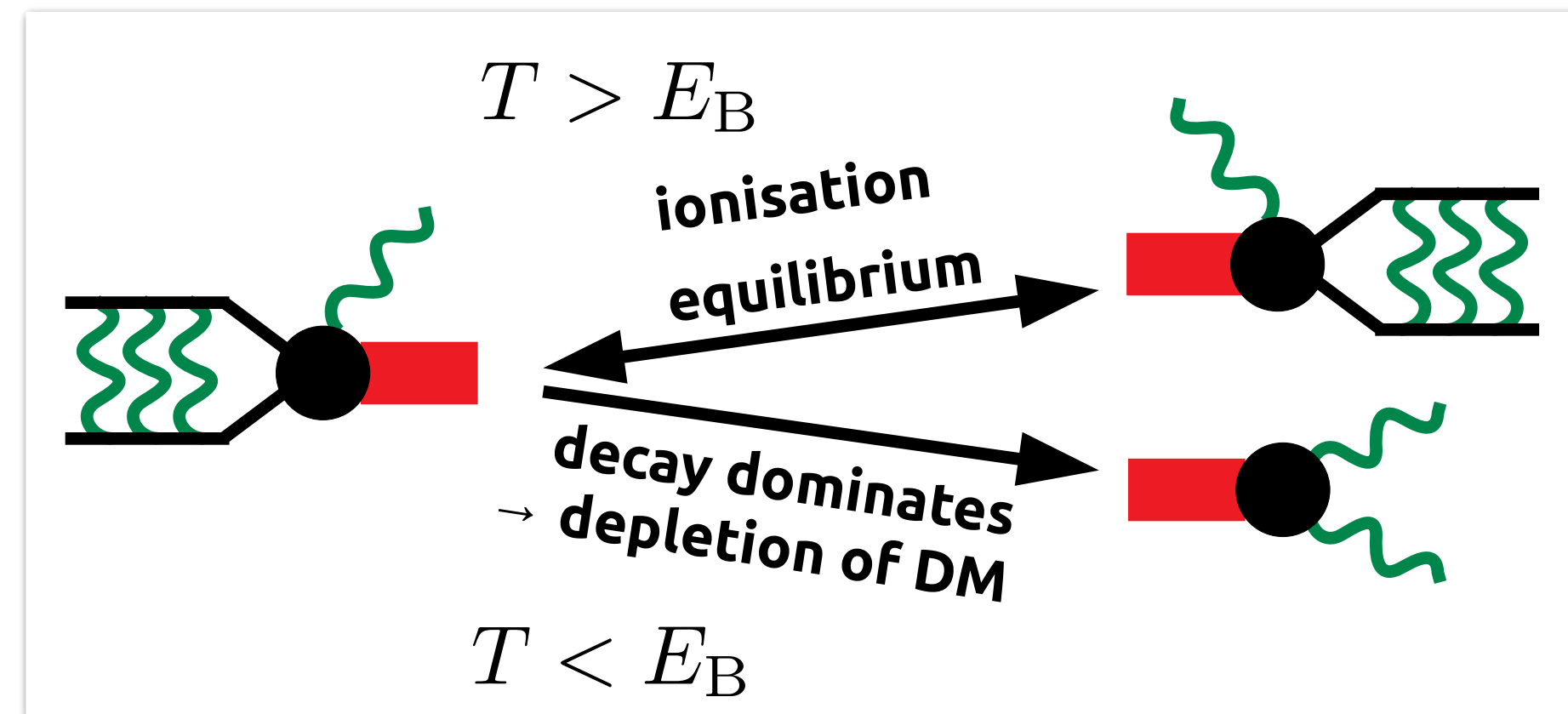
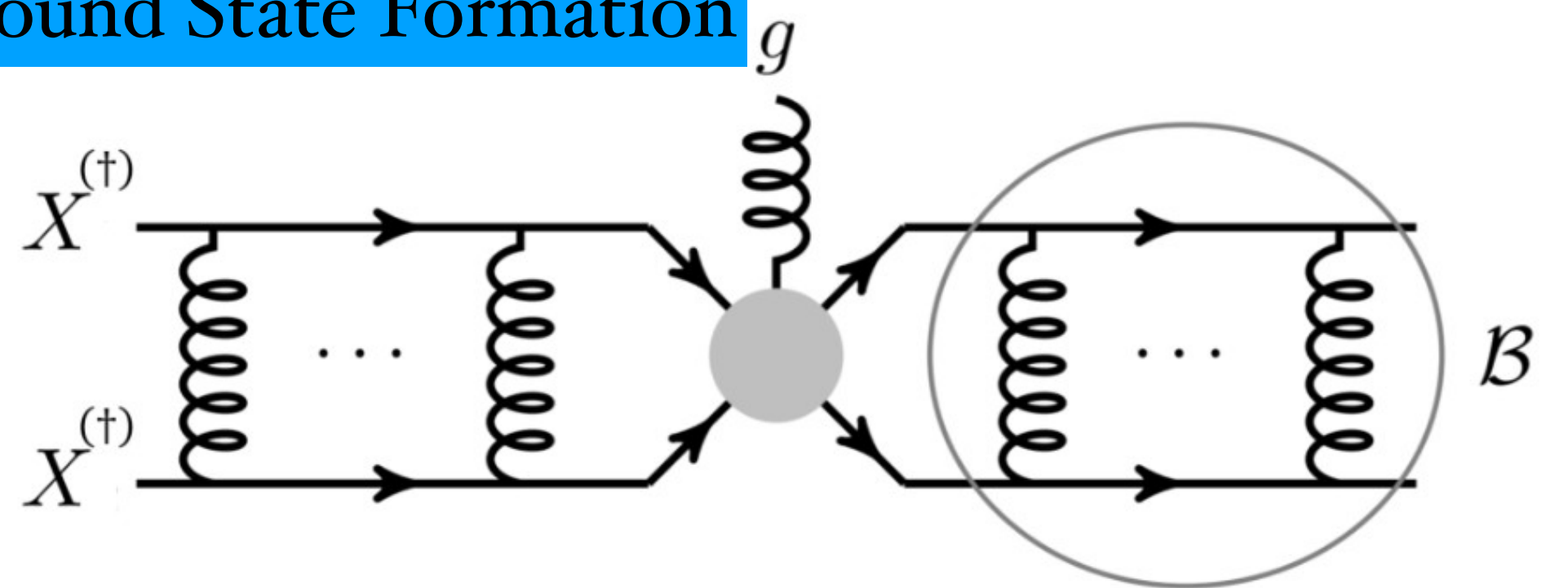
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## Bound State Formation



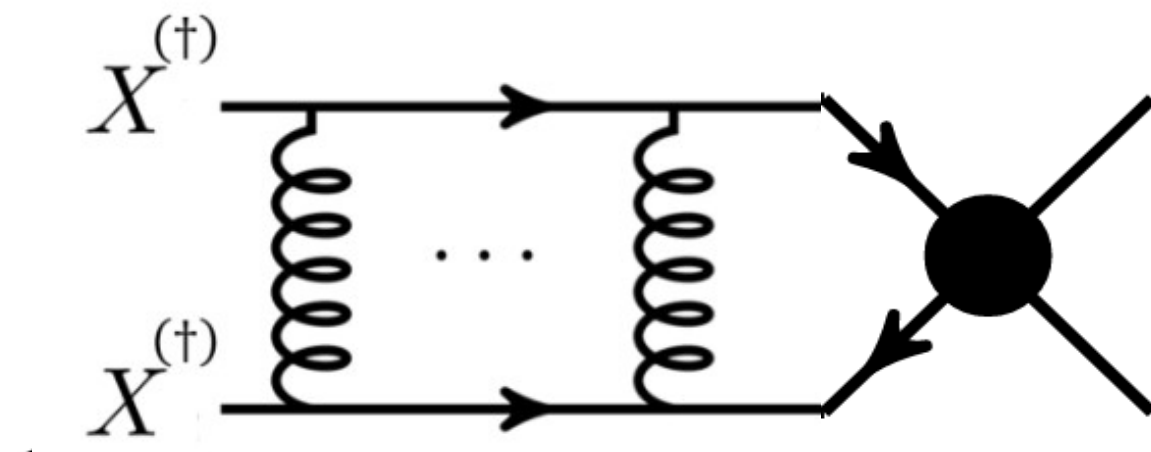
**bound state formation**

**bound state ionisation**

**bound state decay**

# Sommerfeld Enhancement and Bound State Formation in relic abundance

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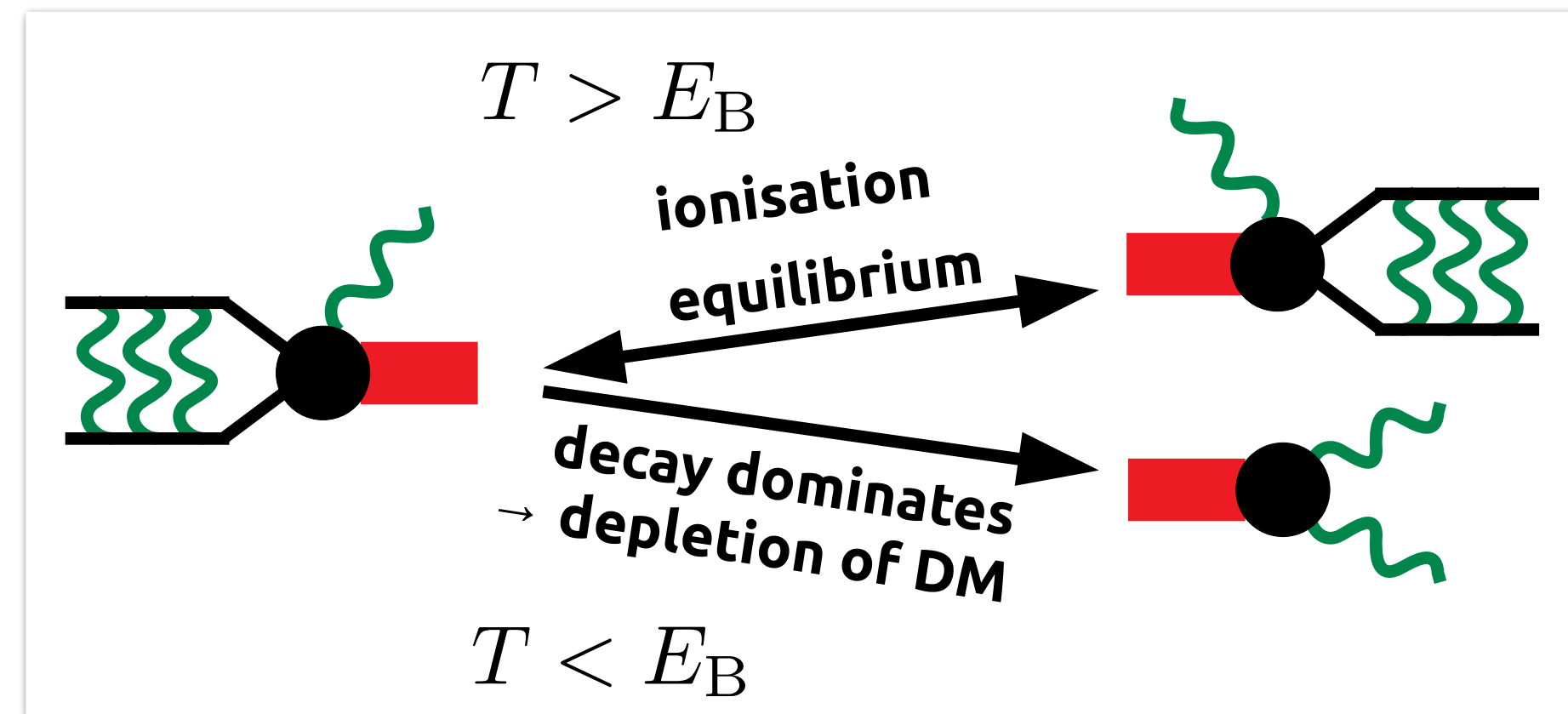
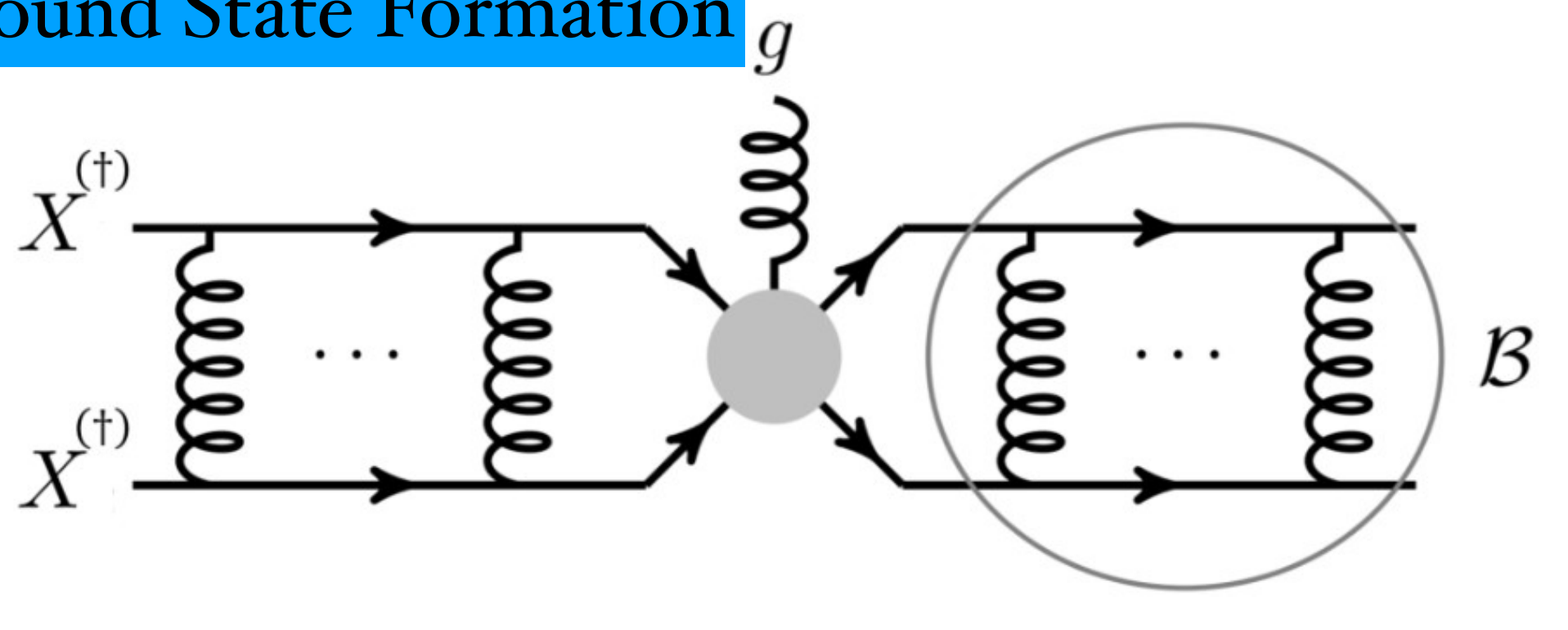
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**bound state formation**

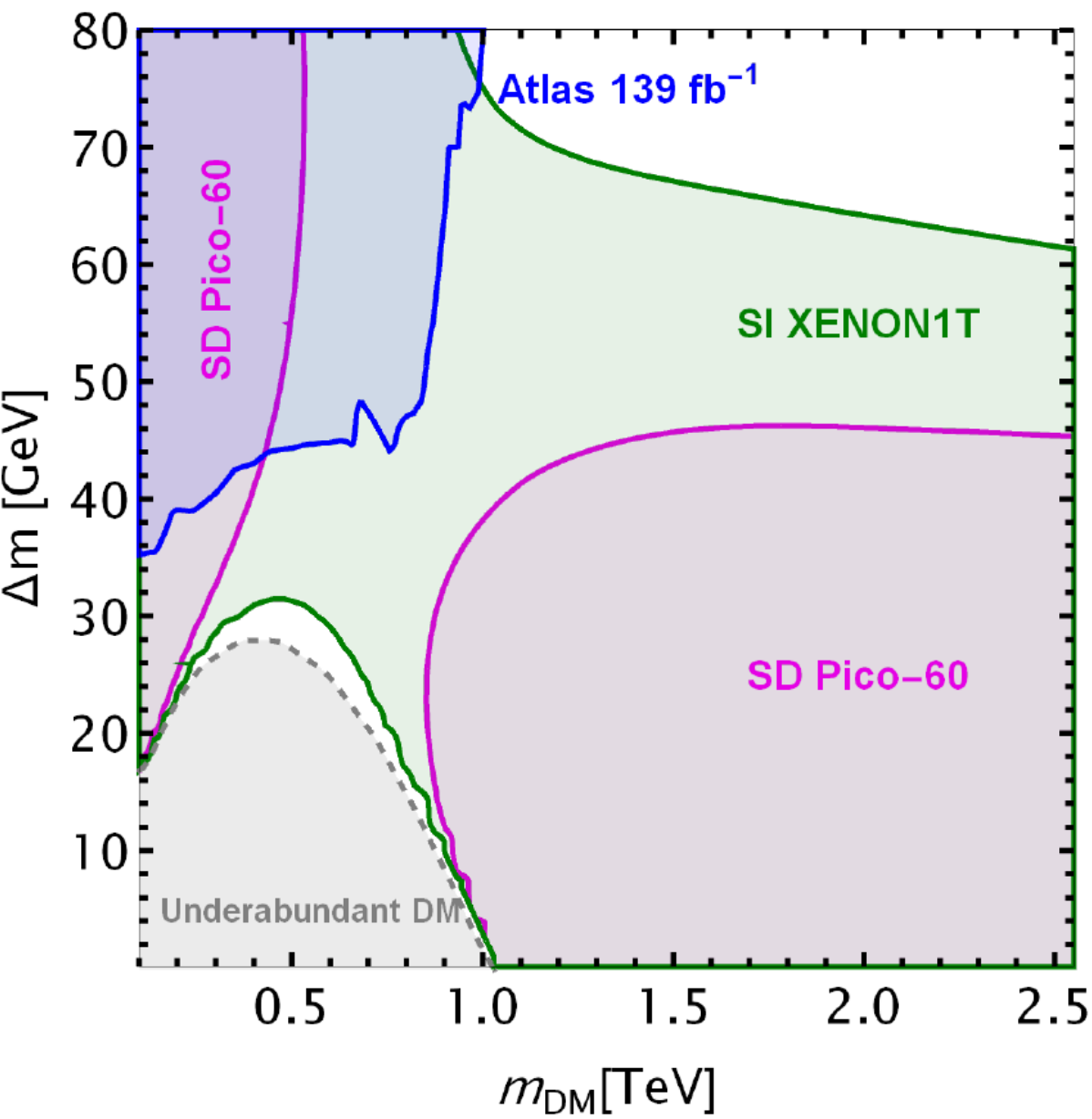
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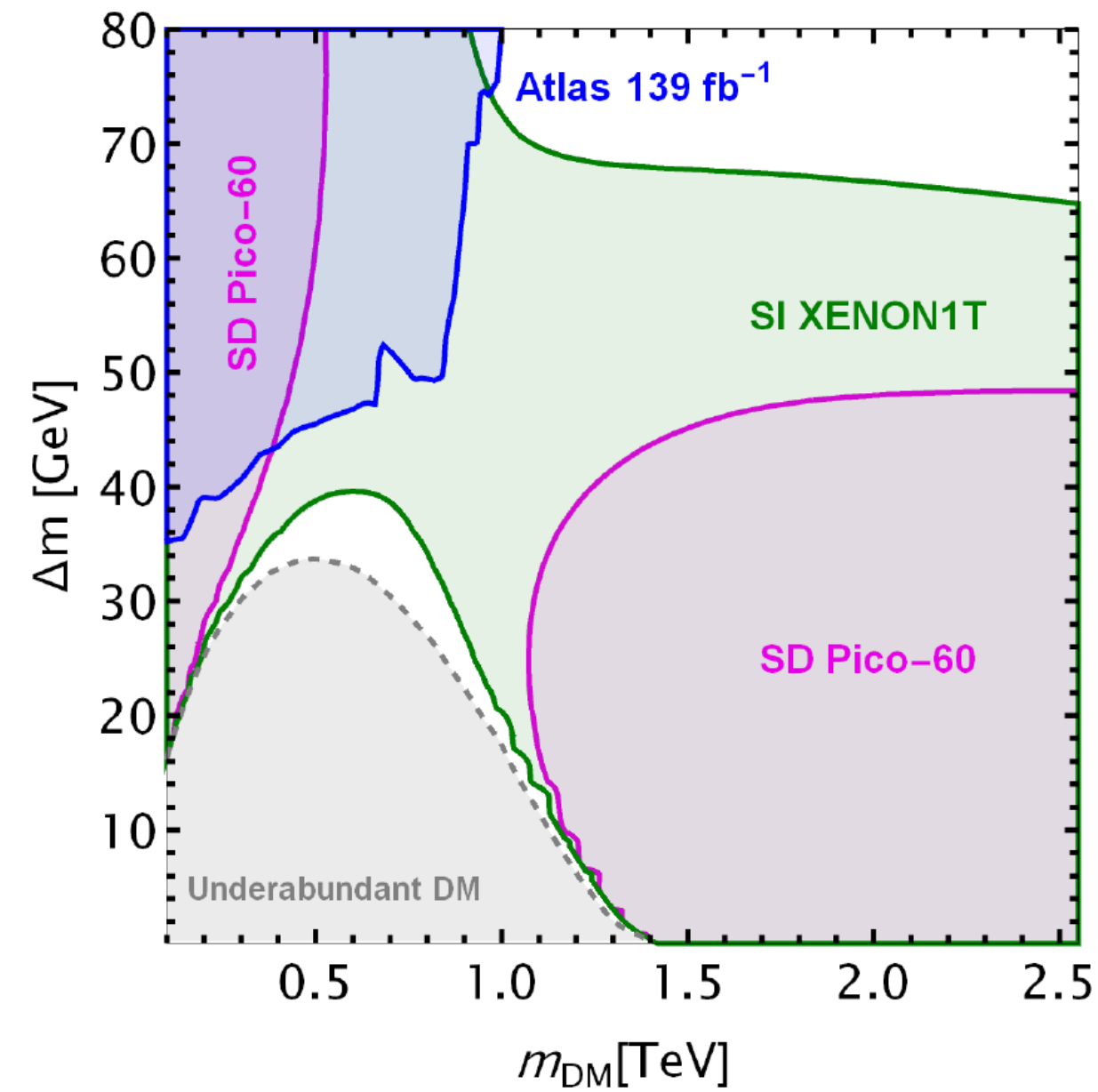
$$\langle \sigma_{\text{eff}} v_{\text{rel}} \rangle = \sum_{ij} \left\langle S \left( \frac{\alpha}{v_{ij}} \right) \cdot \sigma_{ij} v_{ij} \right\rangle \frac{n_{\text{eq},i} n_{\text{eq},j}}{n_{\text{eq}}^2} + \langle \sigma_{\text{BSF}} v_{\text{rel}} \rangle_{\text{eff}} \left( \frac{n_{\text{eq},X}}{n_{\text{eq}}} \right)^2$$

# Impact of Sommerfeld Enhancement and bound states

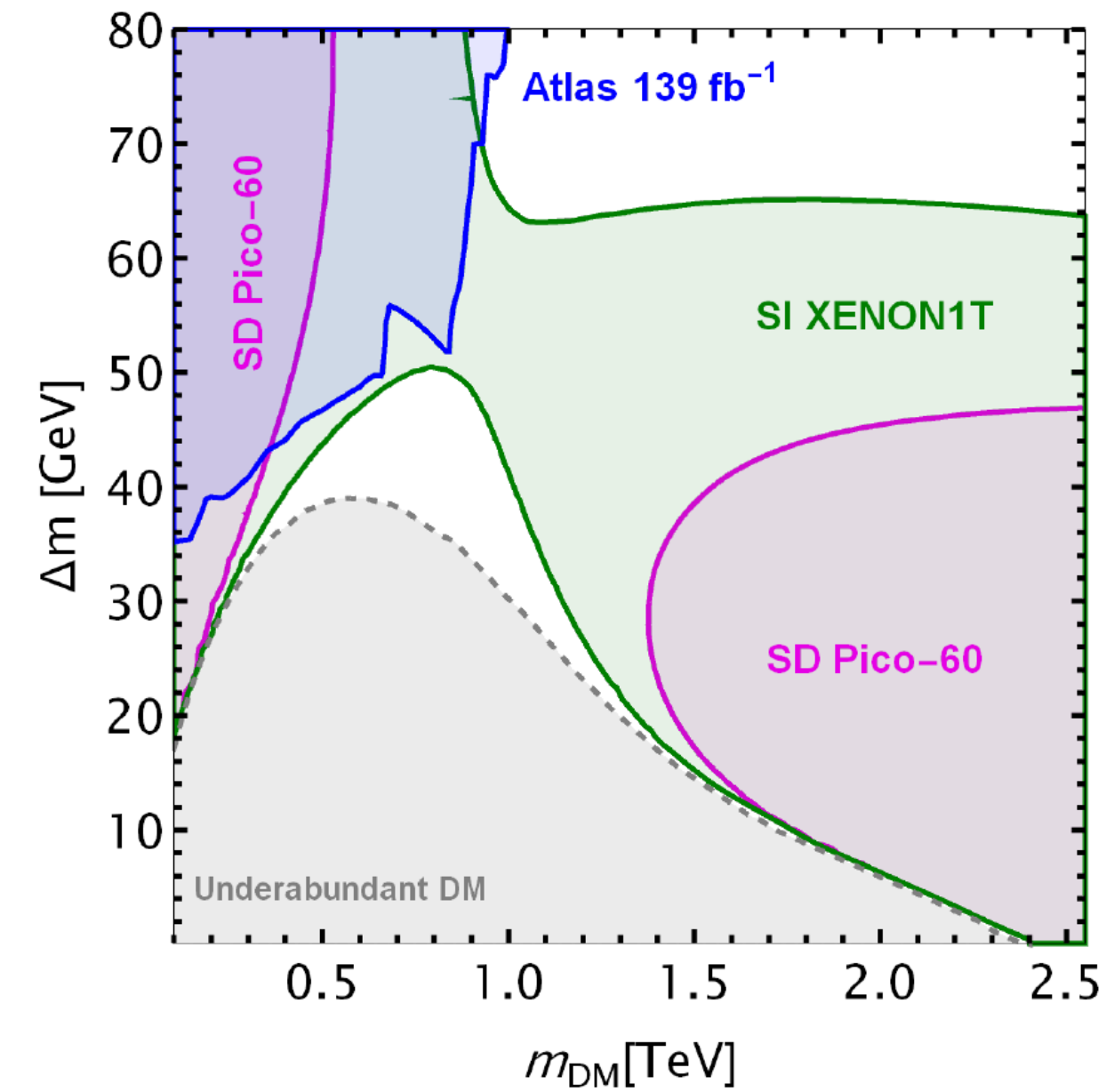
perturbative only



+ Sommerfeld effect



+ bound states

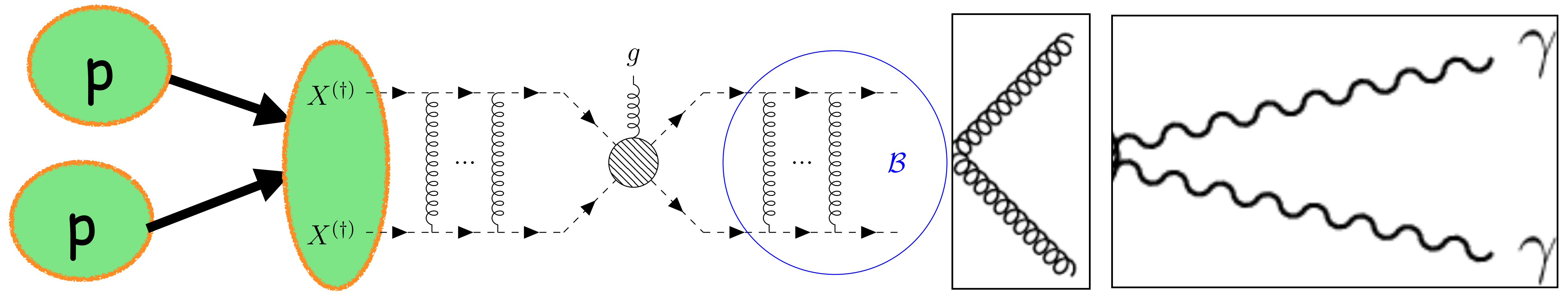


- DD and LHC searches set upper bound on  $g_{DM}$
- Requirement of non-overproduction sets lower bound on  $g_{DM}$

1. The model tightly constrained by Direct Detection,  
2. Model parameters then relaxed by SE + BSF.

- **Correction on  $g_{DM}$  due to SE and BSF lead to altered exclusion limits**
- **opens up parameter space that was previously thought to be excluded**

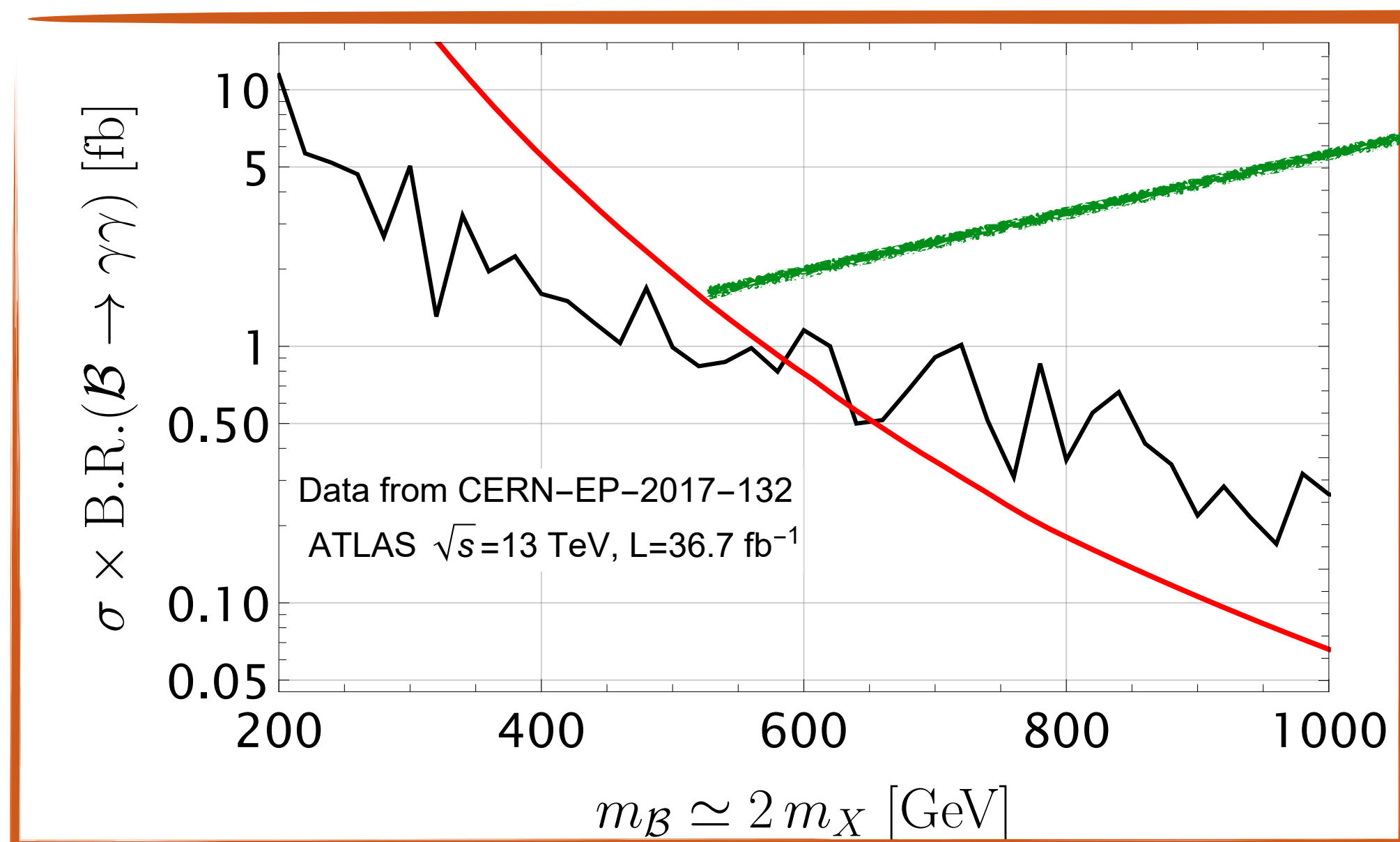
# $t$ -channel Simplified Models : Bound State Production/decay at LHC



$$\sigma(pp \rightarrow B(XX^\dagger)) = \frac{\pi^2}{8m_B^3} \Gamma(B(XX^\dagger))$$

$$\Gamma(\eta_{\tilde{t}} \rightarrow gg) \simeq \frac{4}{3} \alpha_s^2 \frac{|R(0)|^2}{m_{\eta_{\tilde{t}}}^2}$$

$$\Gamma(\eta_{\tilde{t}} \rightarrow \gamma\gamma) = \frac{32}{27} \alpha^2 |R(0)|^2 / m_{\eta_{\tilde{t}}}^2$$



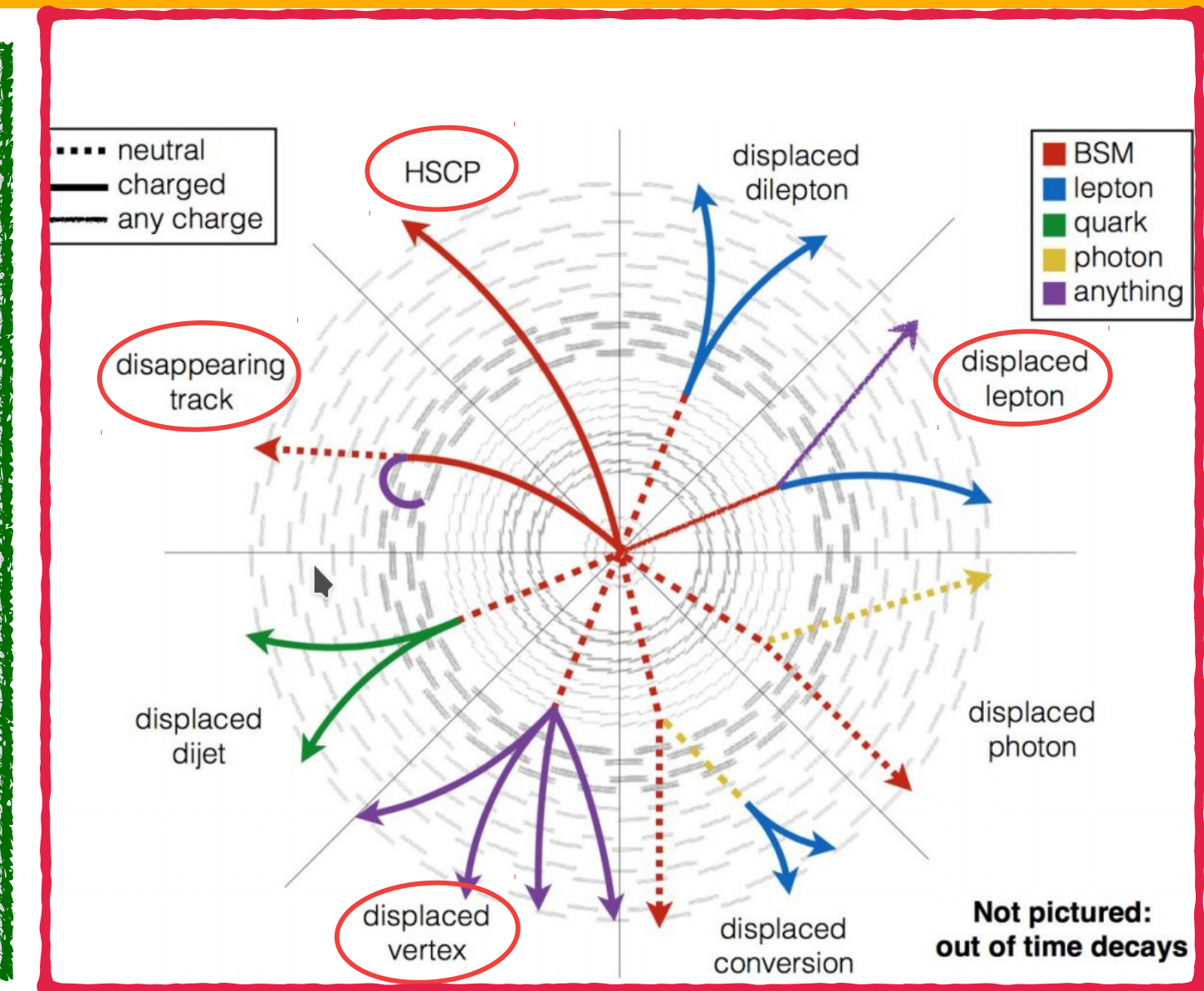
Theoretical Prediction for the uR model

For large stoponium masses,  
could lead to emerging/displaced photons

$$100 \text{ GeV} \lesssim m_X \lesssim 290 \text{ GeV}$$

# t- channel Simplified Models : HSCP searches

- **Heavy:** Implies slow particles,  $\beta < 1.0$
- **Stable:** Lives long enough so it can reach tracker and/or muon detectors or even get past them.
- **Charged:** Can be detected by the muon detectors.



- ★ The massive colored mediator  $X$  travels the detector producing an ionizing track
- ★ If it decays outside the detector, time of flight measured using hits in muon chamber is large.

**dE/dx:** Ionization energy lost.

$$\frac{dE}{dx} \approx Q^2 \left[ \frac{A}{\beta^2} + B \right] \text{ for } \beta \ll 1$$

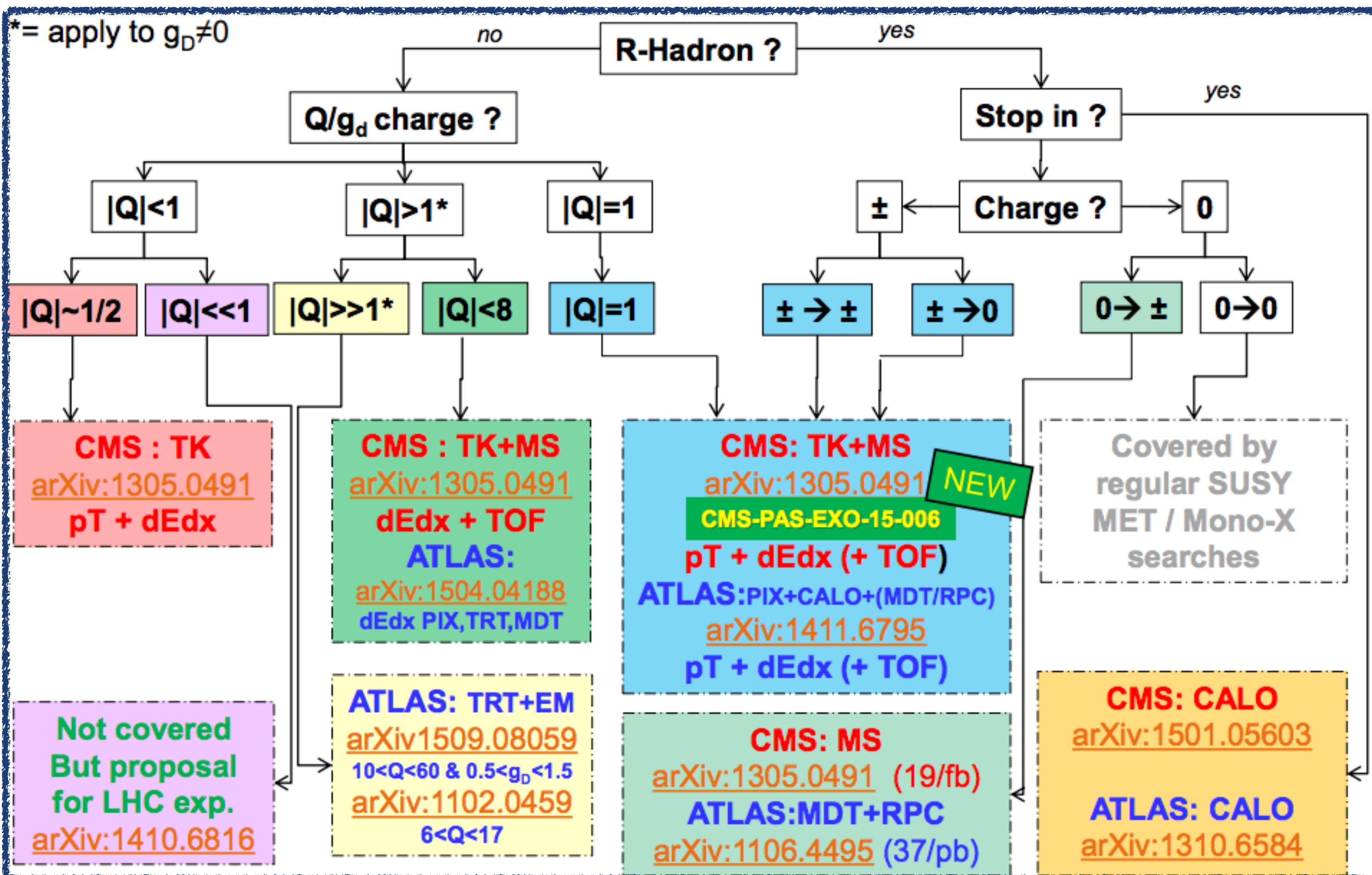
**TOF:** Time of flight

$$\frac{1}{\beta} = 1 + \frac{c\delta_t}{L}$$

Fraction of charged hadrons depend on hadronization model: typically use a cloud hadronization model. (Mackperang, Rizza: hep-ph/0612161, Kraan, hep-ex/0404001)



# t- channel Simplified Models : HSCP searches



Typical Tracker+TOF analysis is more constraining, requires HSCP decays outside the detector

$$\sigma_{\text{eff}} = \sigma \times f_{\text{LLP}}(L, \tau)$$

Fraction of LLPs that decay inside the detector (tracker only) or outside

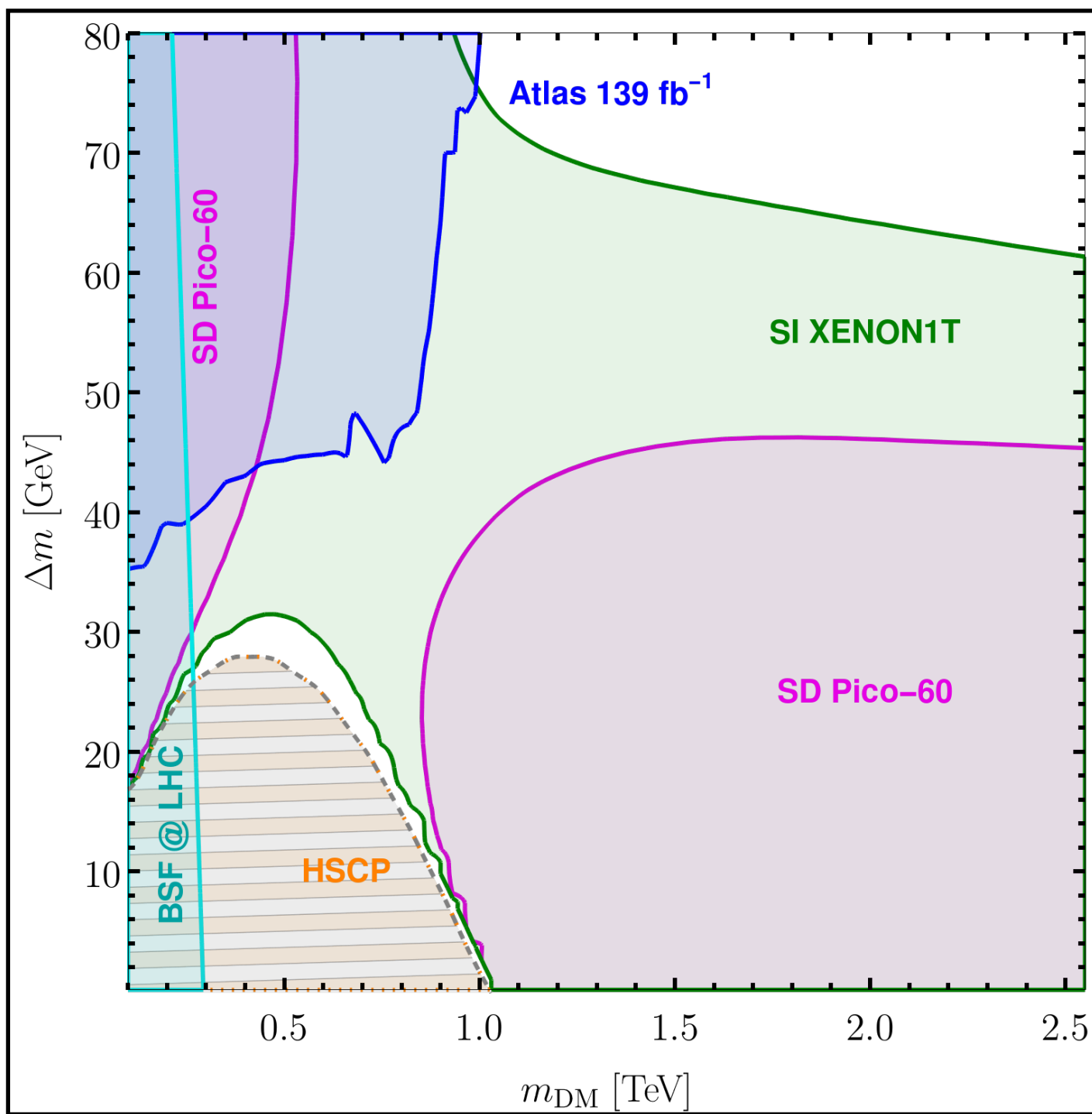
The detector (tracker + TOF):  
Computed using trigger and selection efficiencies (CMS: EPJC 75 (325))

Searches for Heavy Stable Charged Particles at the LHC Past, Present and Future, Loïc Quertenmont. 12 February 2015

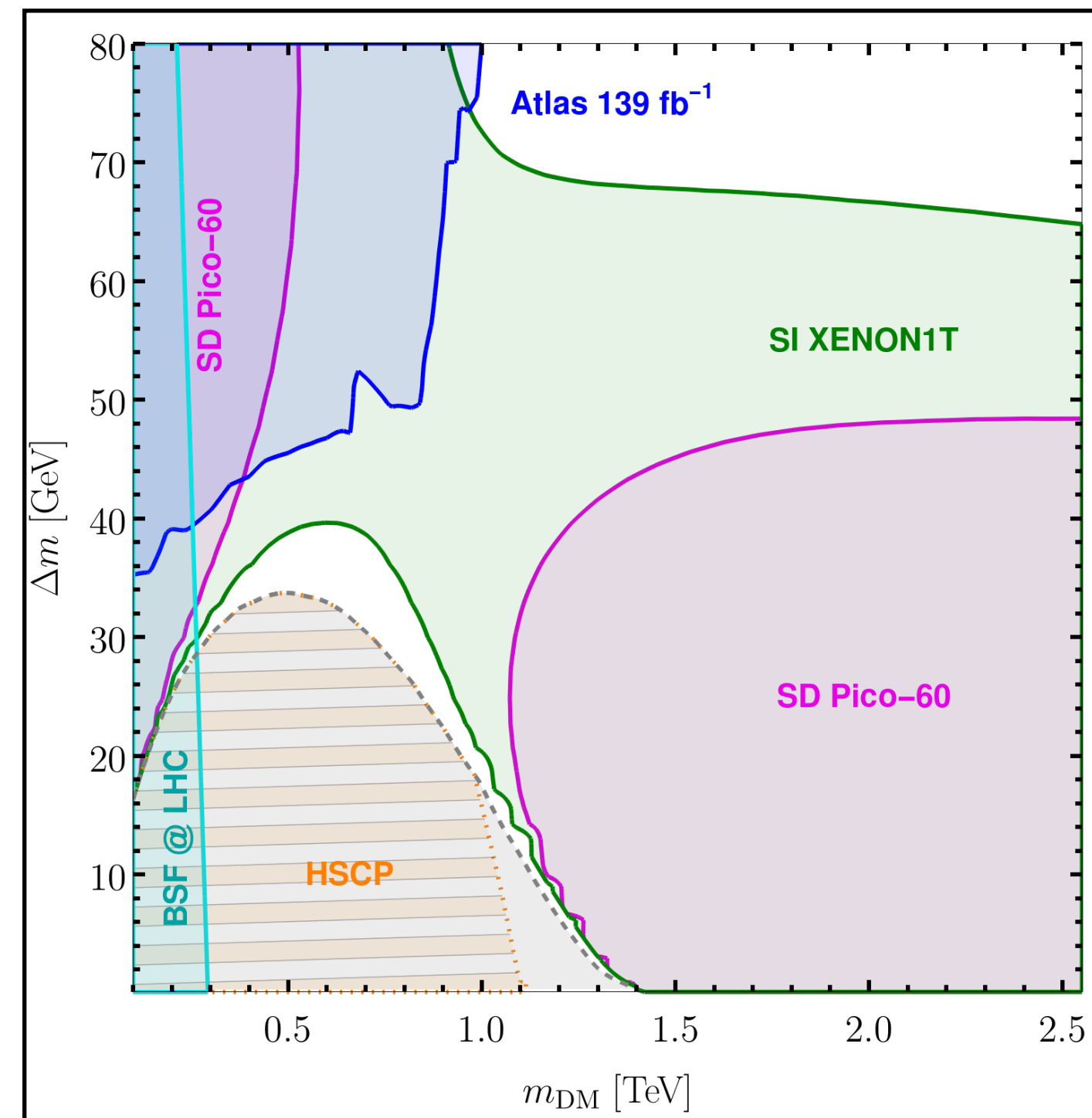
Use two CMS analysis for reinterpretation using cross-section upper limits

1. CMS : Search for LLP in pp collisions : JHEP 07 (2013) 122
2. CMS : Search for heavy stable charged particles CMS-PAS-EXO-16-036

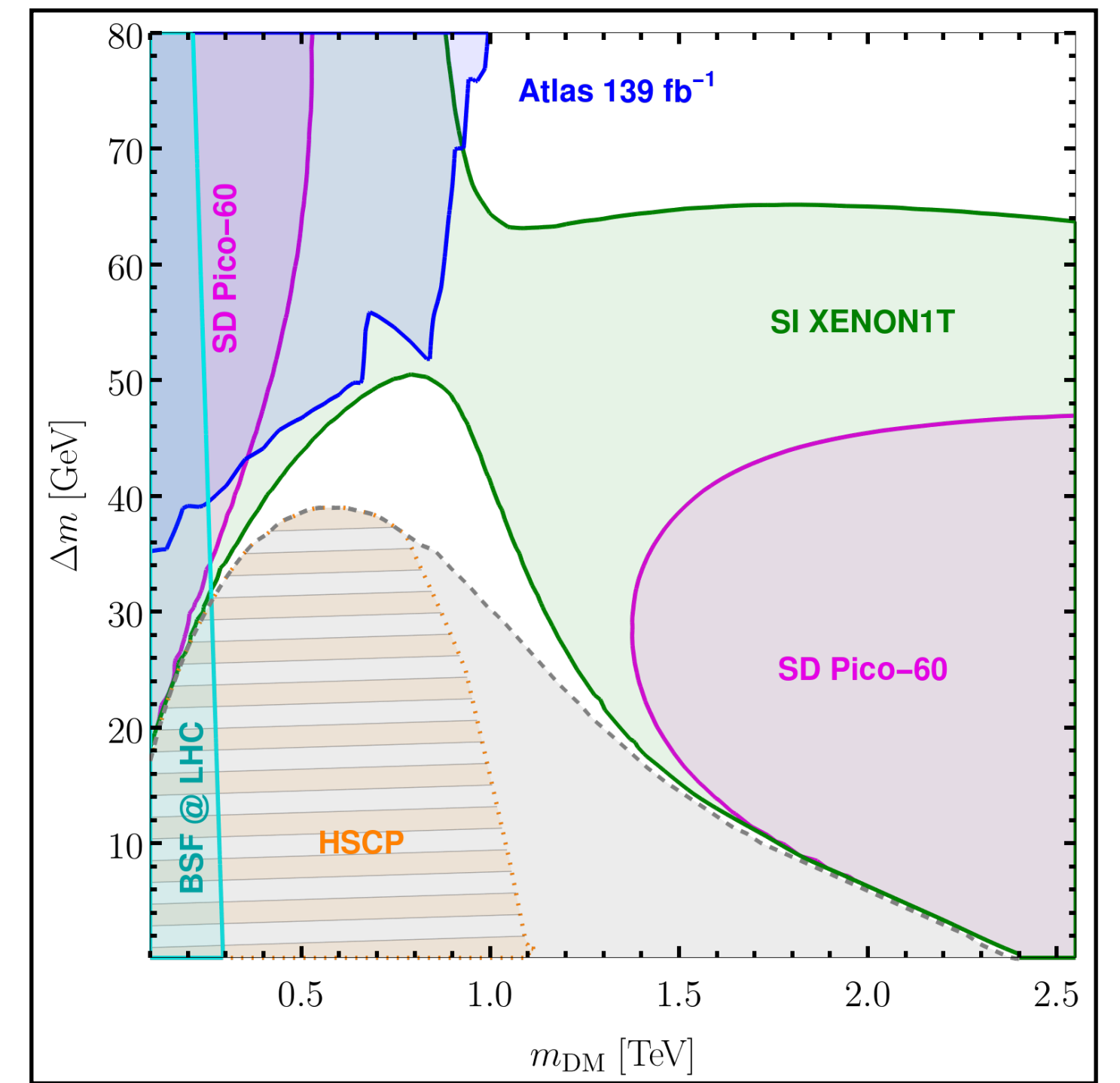
# t- channel Simplified Models : Combined limits



Perturbative Annihilations

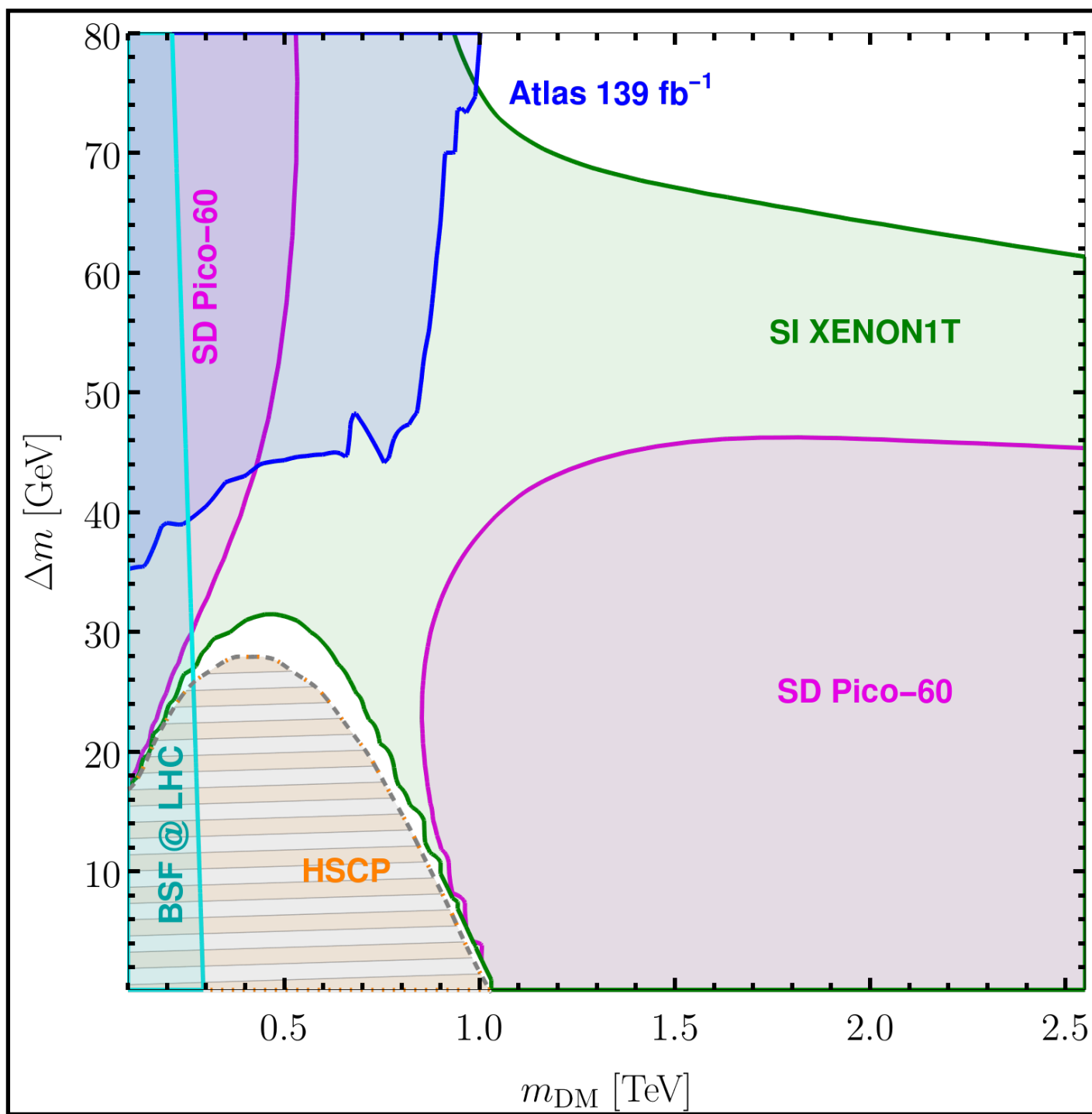


Sommerfeld

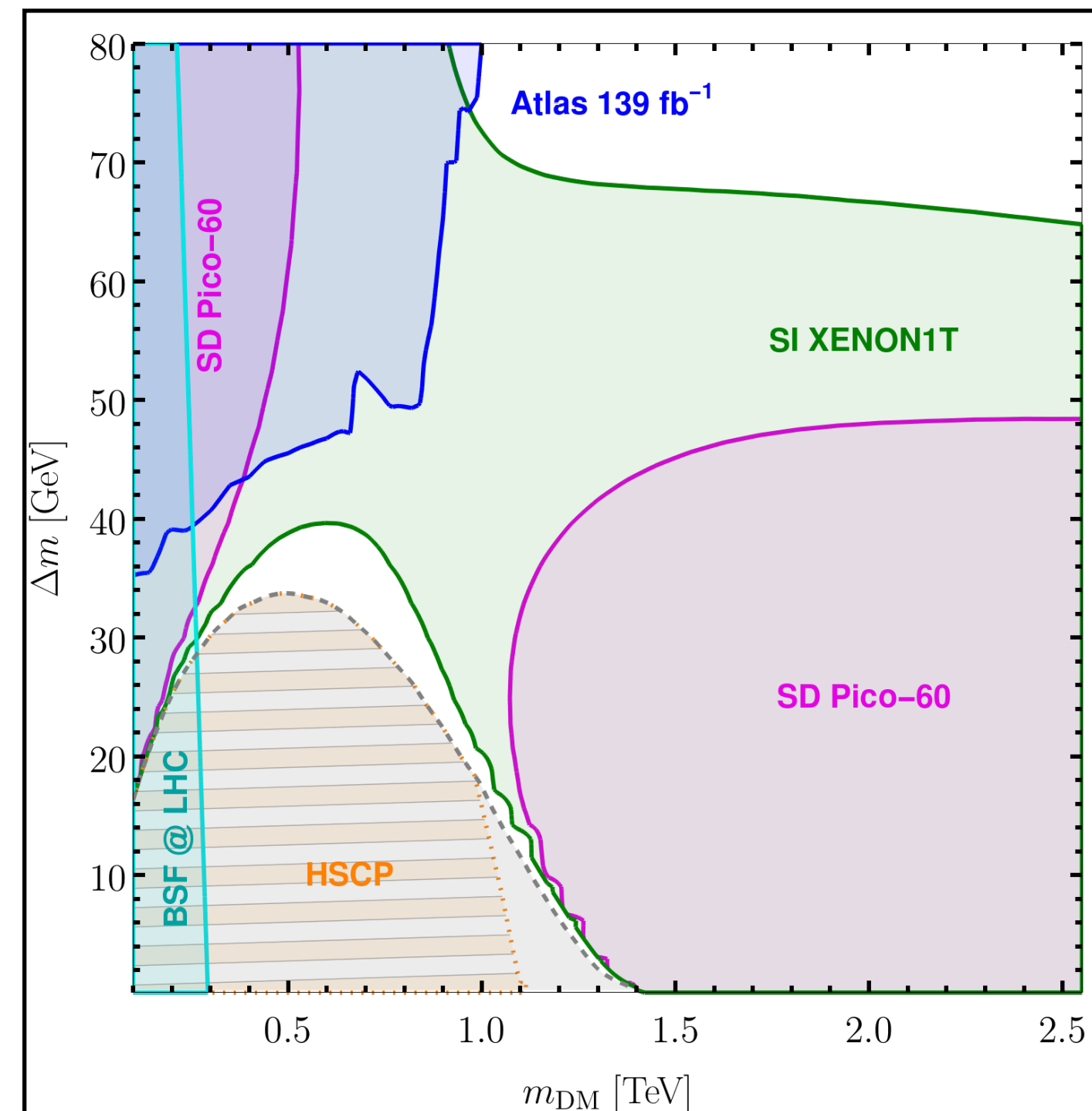


Sommerfeld+BSF

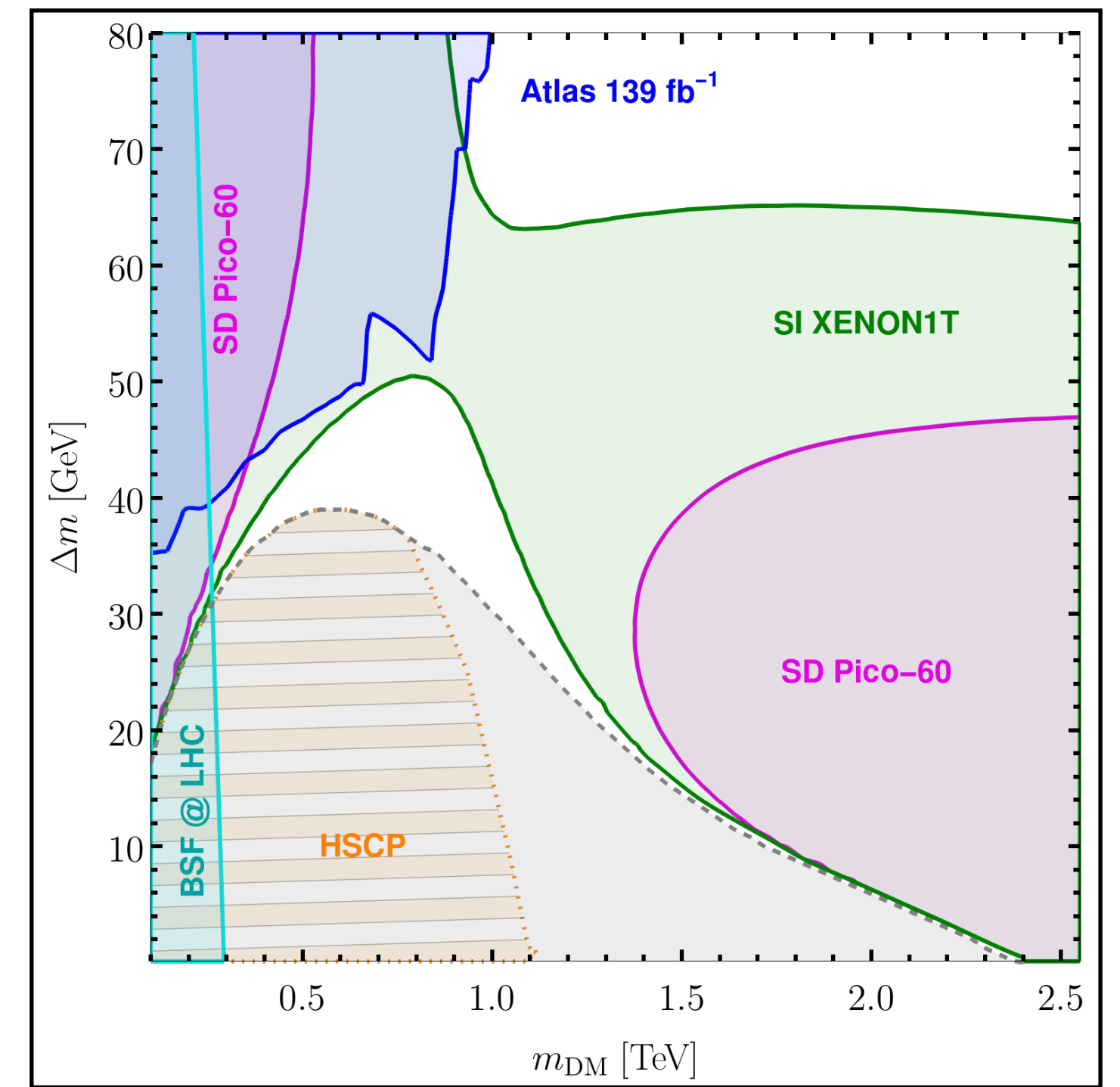
# t-channel Simplified Models : Combined limits



Perturbative Annihilations



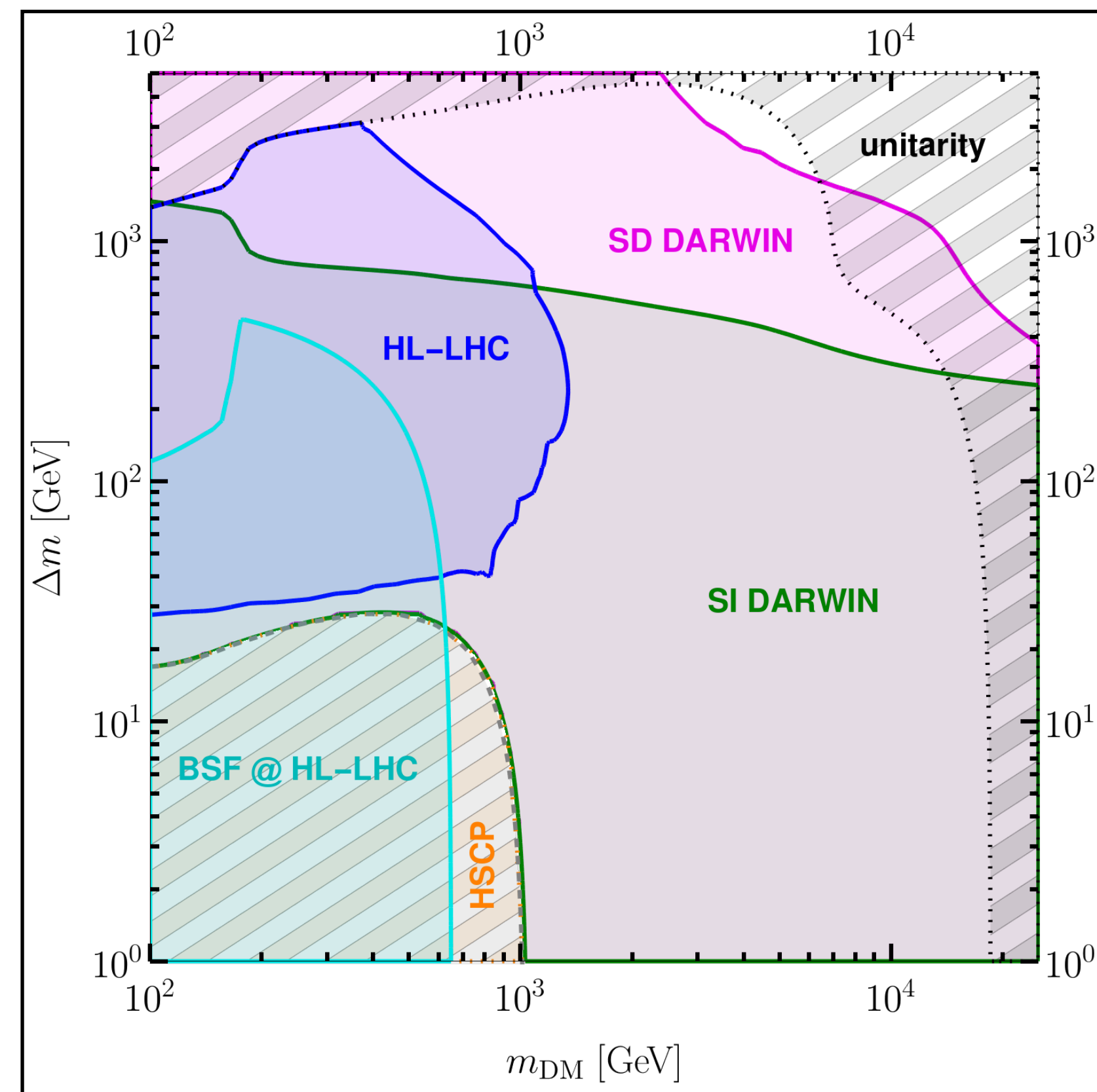
Sommerfeld



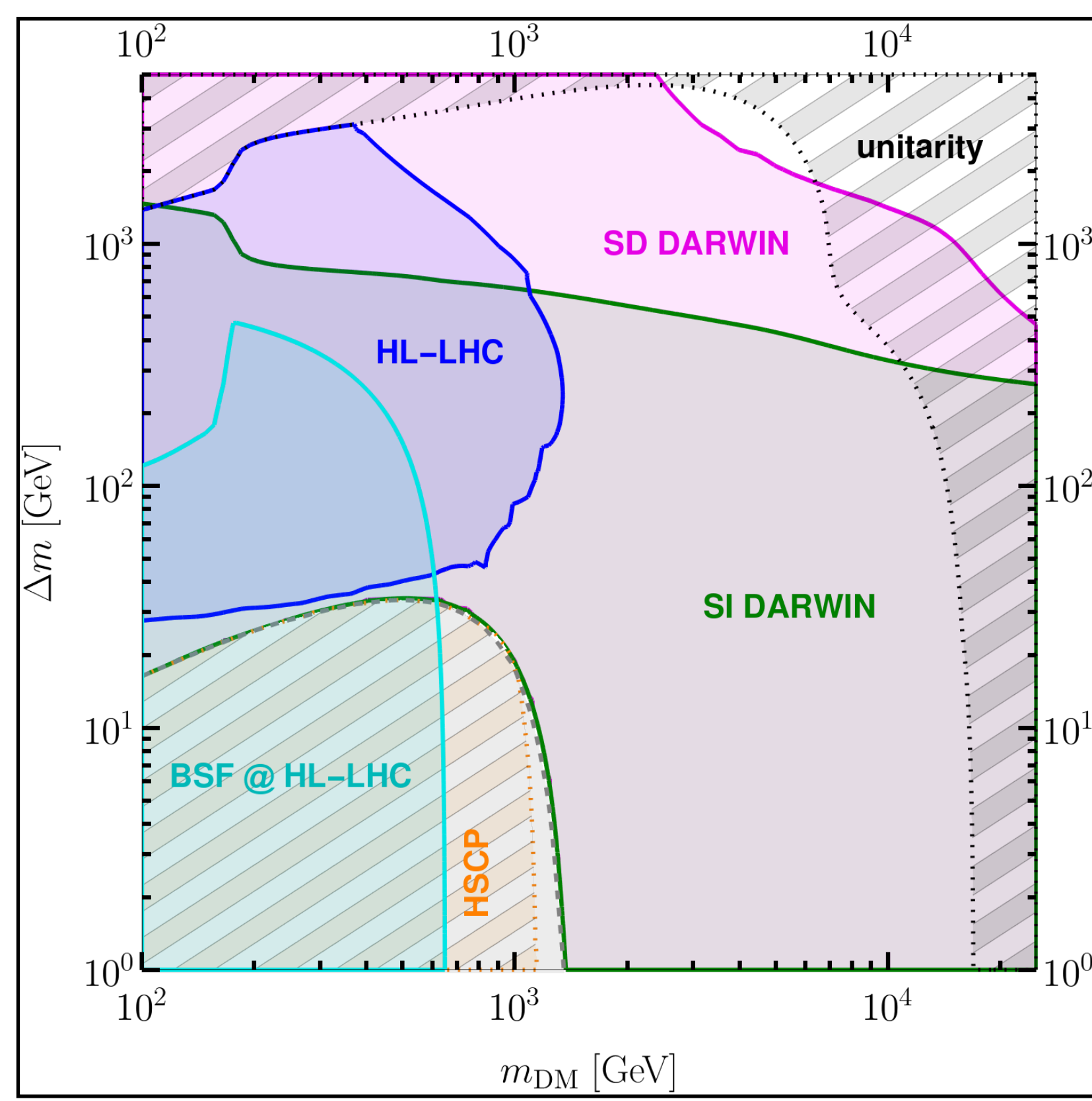
Sommerfeld+BSF

M. Becker, E. Copello, J. Harz K. Mohan, **DS**. JHEP08(2022) 145

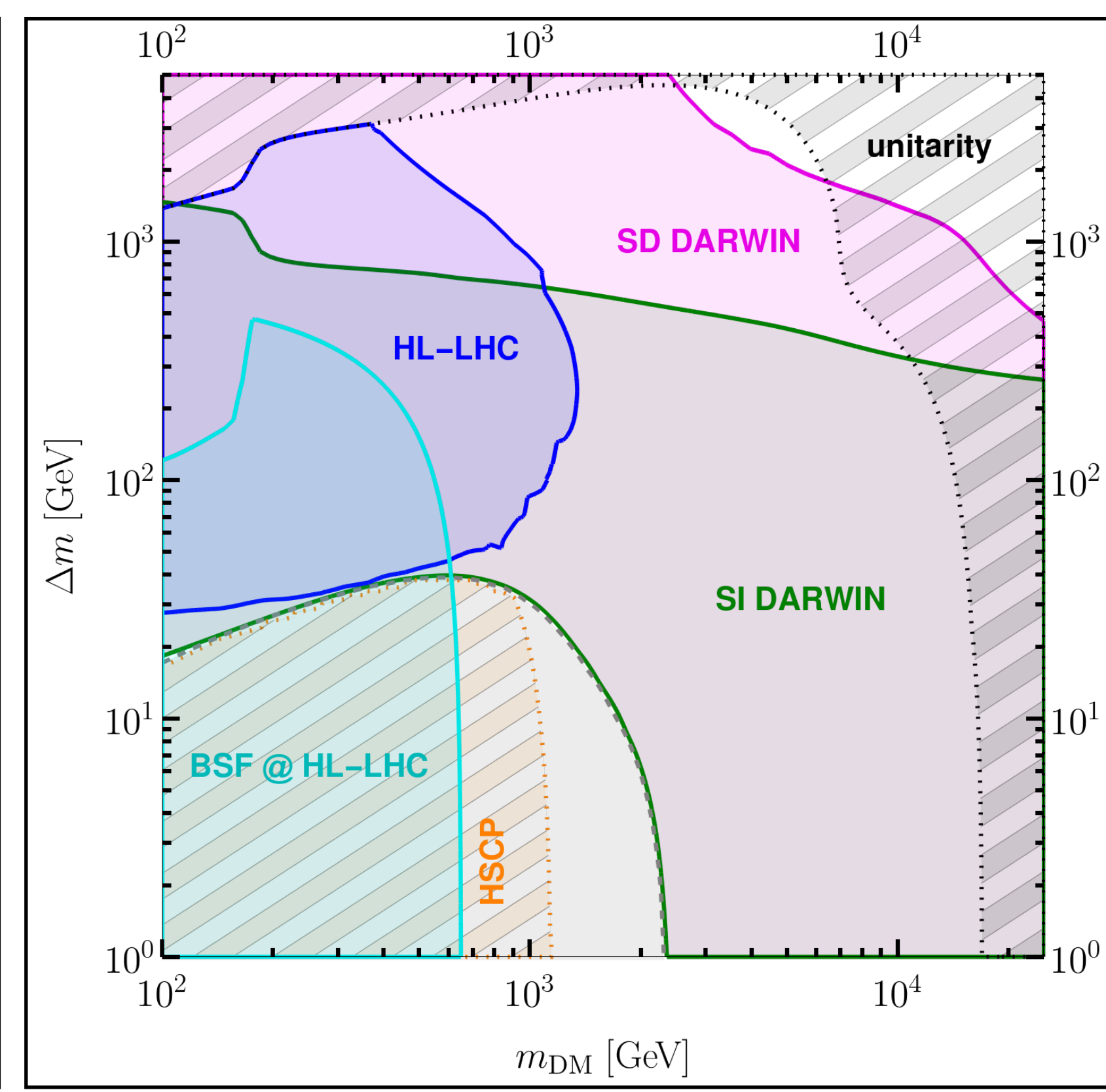
# t-channel Simplified Models : Future projection



Perturbative Annihilations

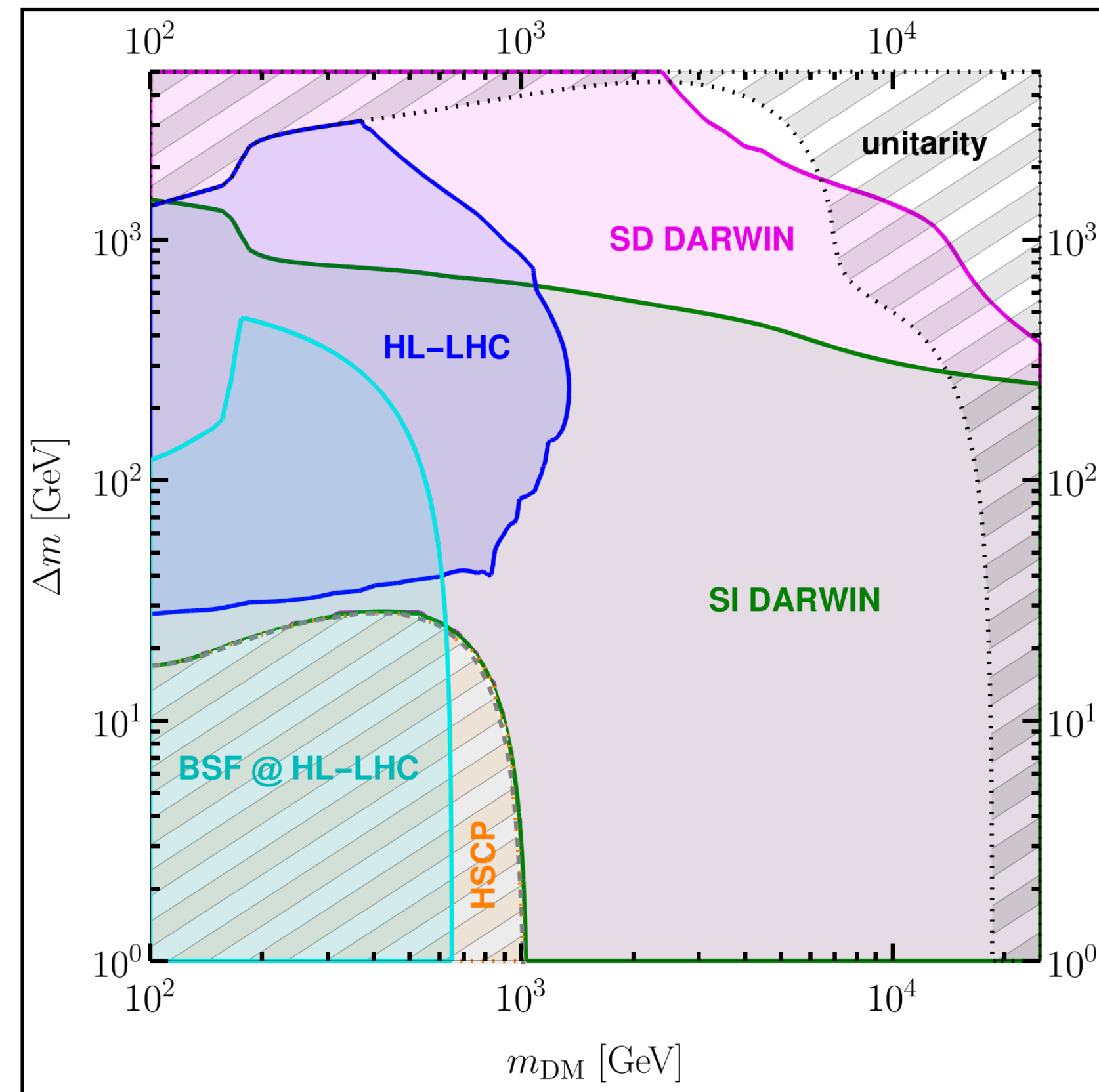


Sommerfeld

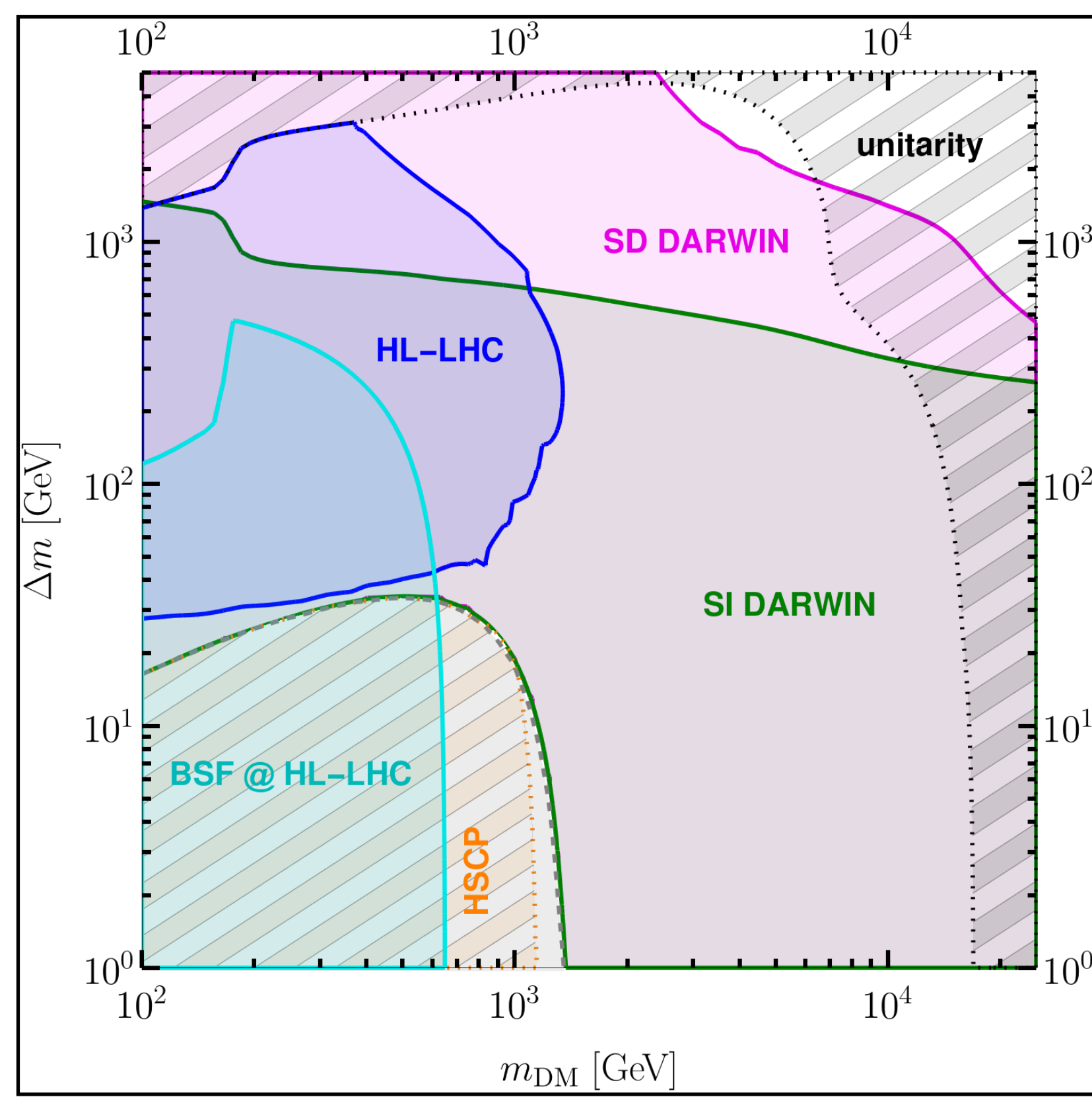


Sommerfeld+BSF

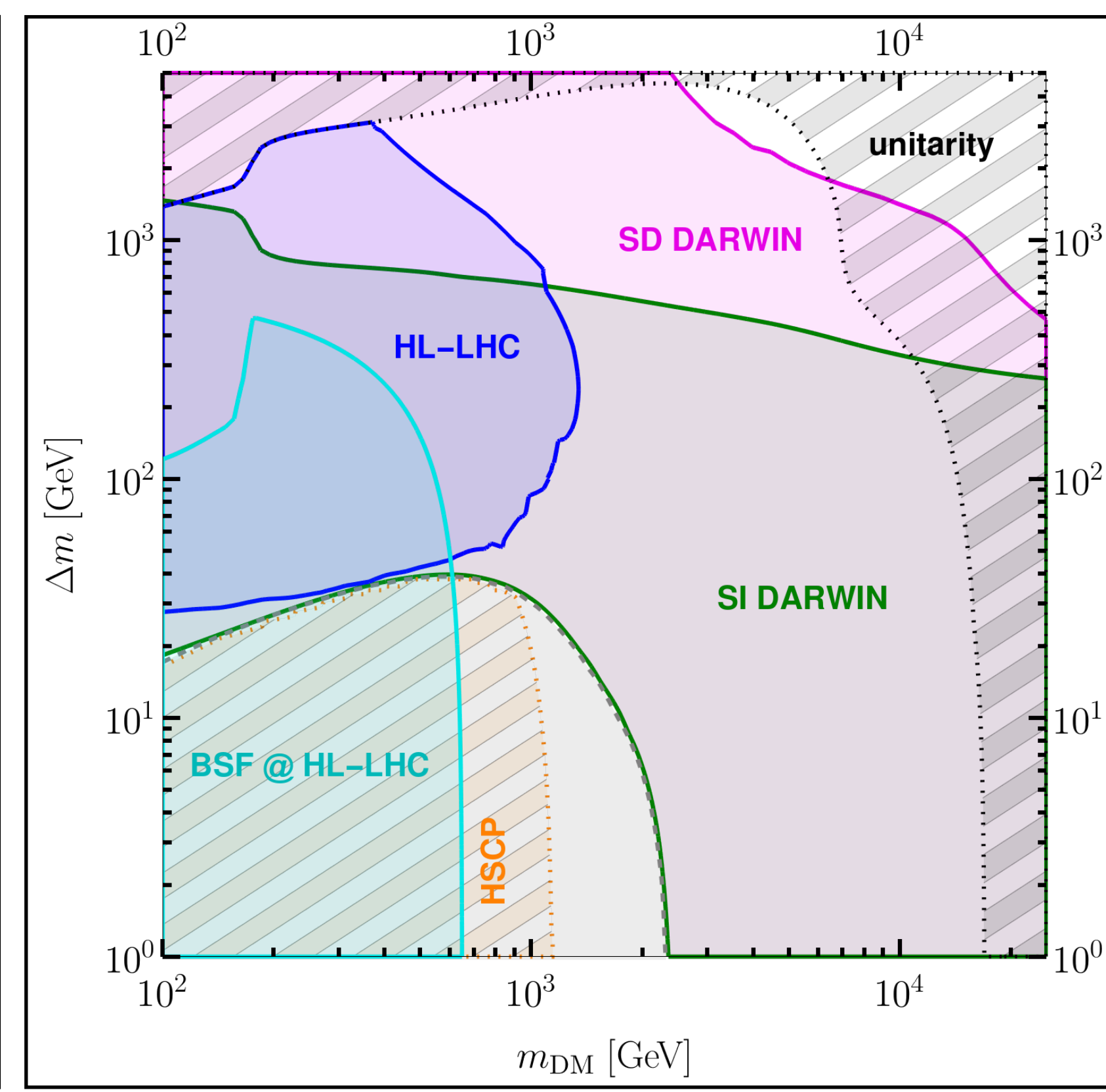
# t-channel Simplified Models : Future projection



Perturbative Annihilations



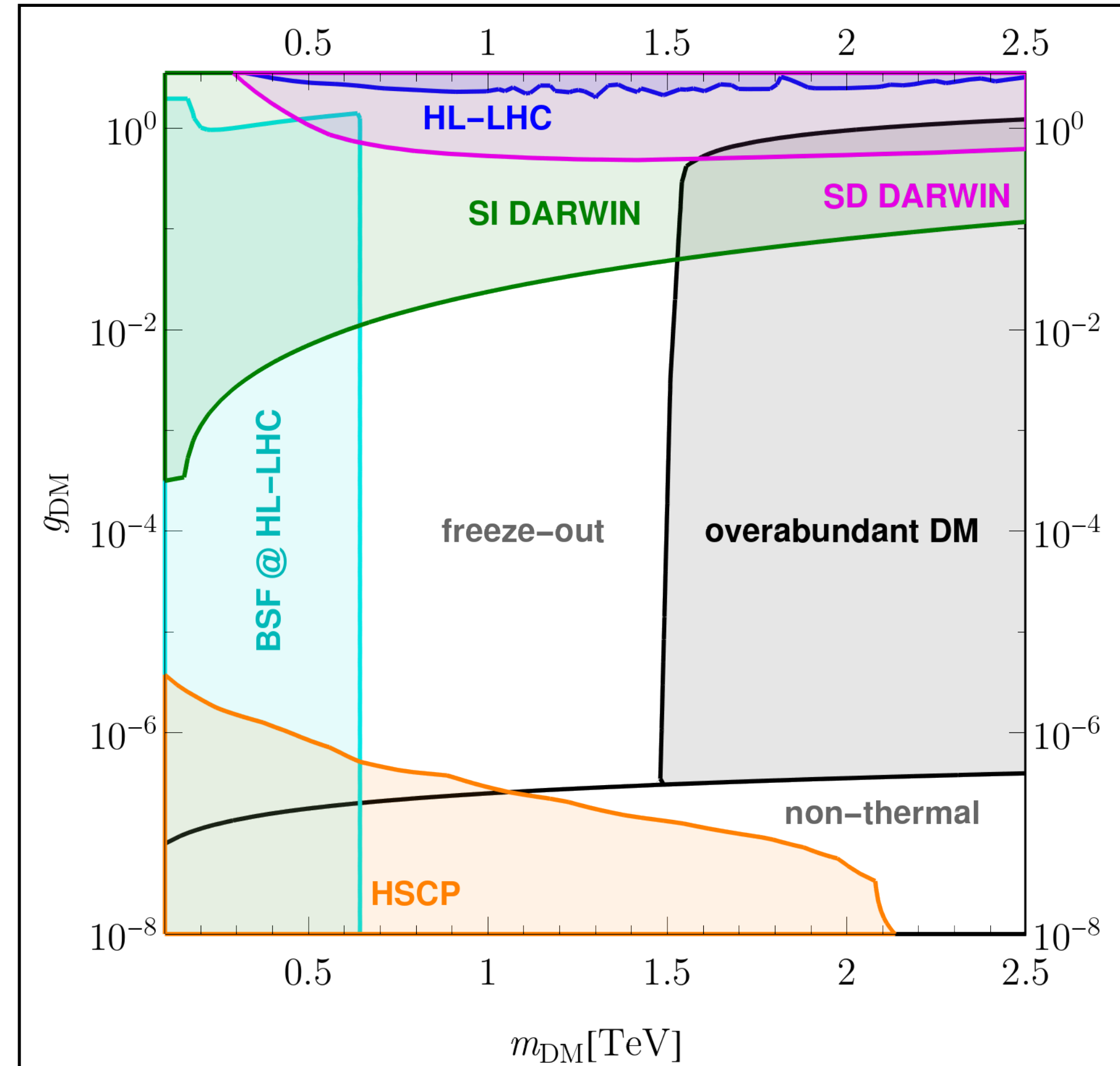
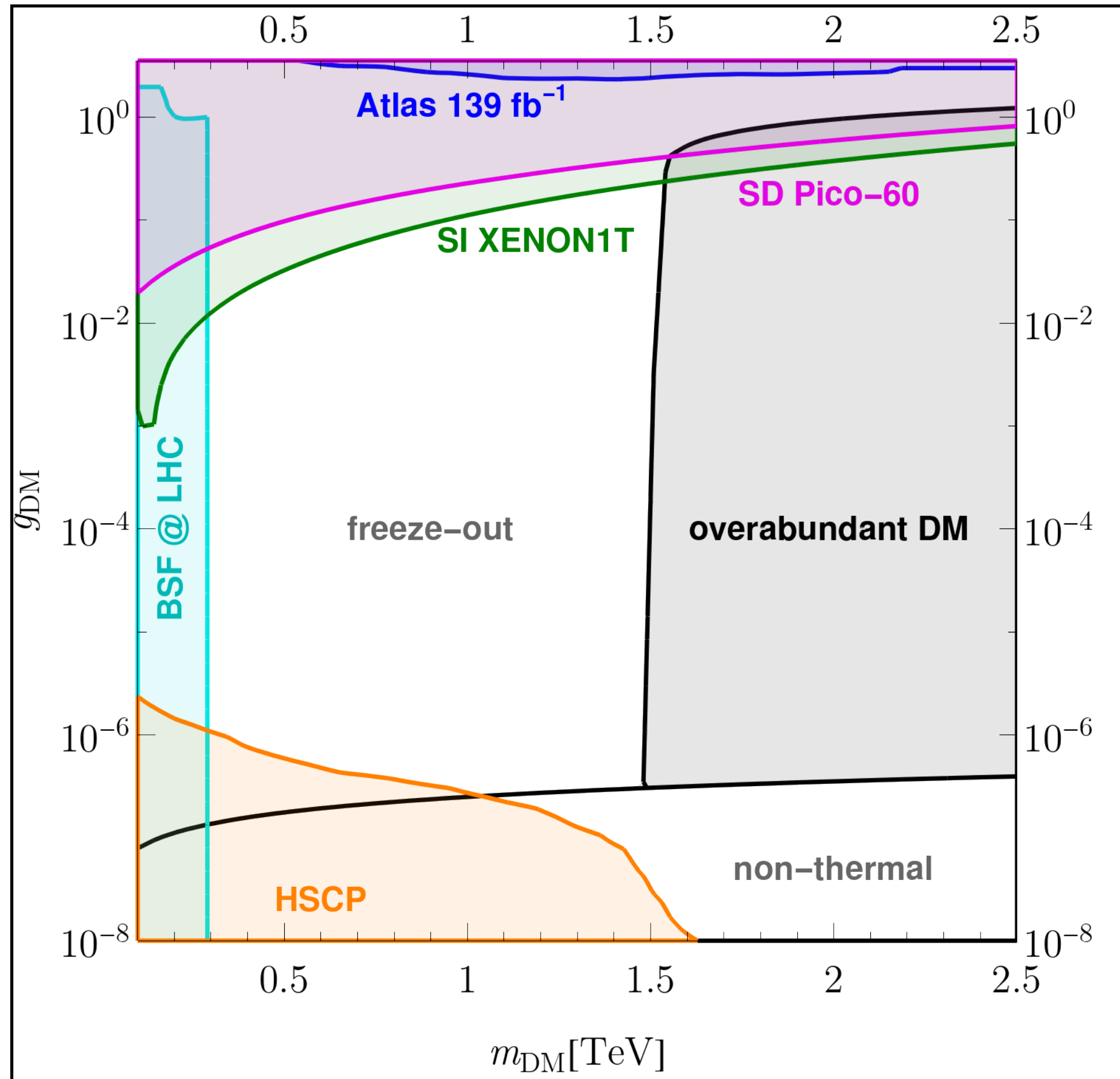
Sommerfeld



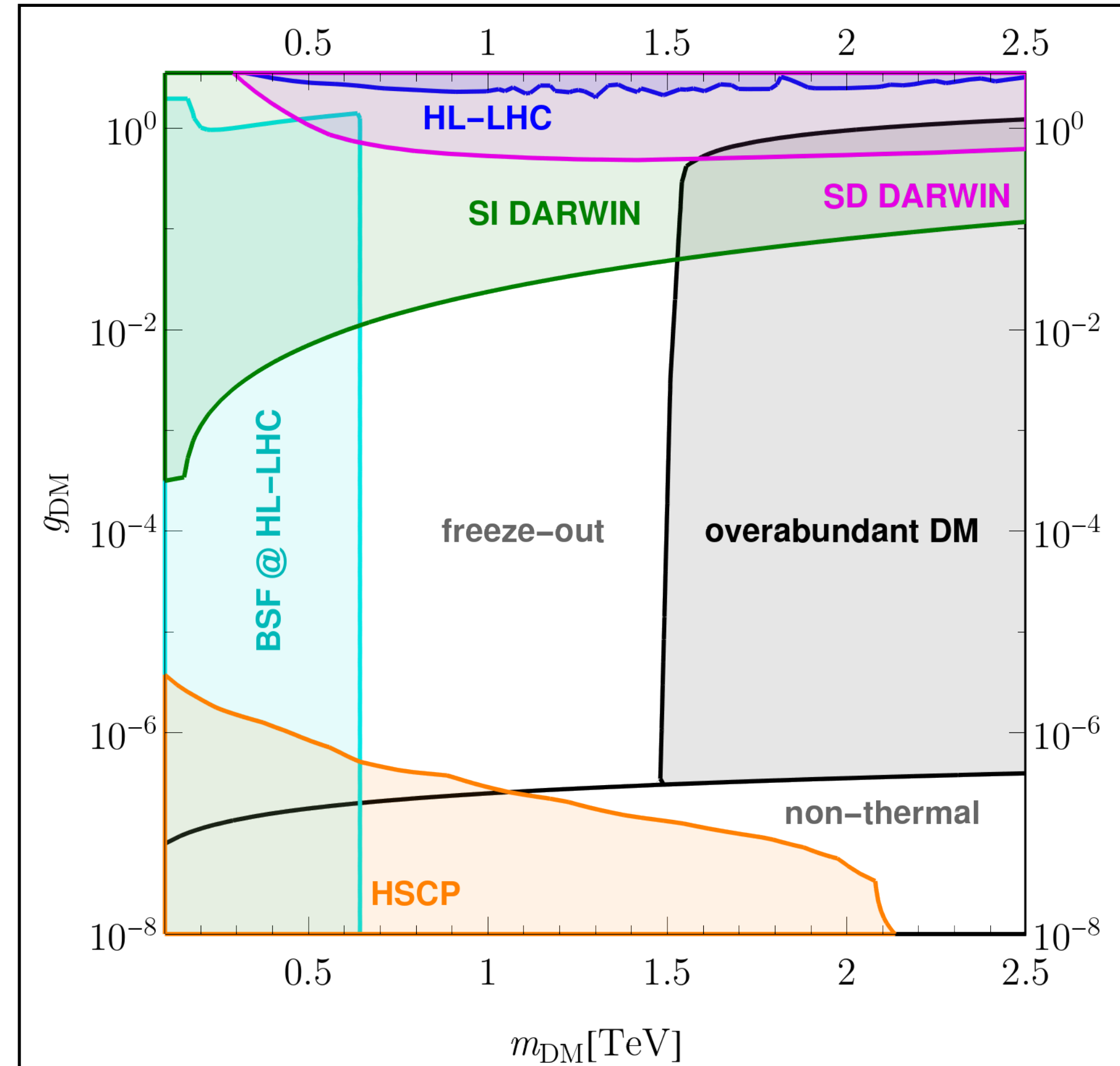
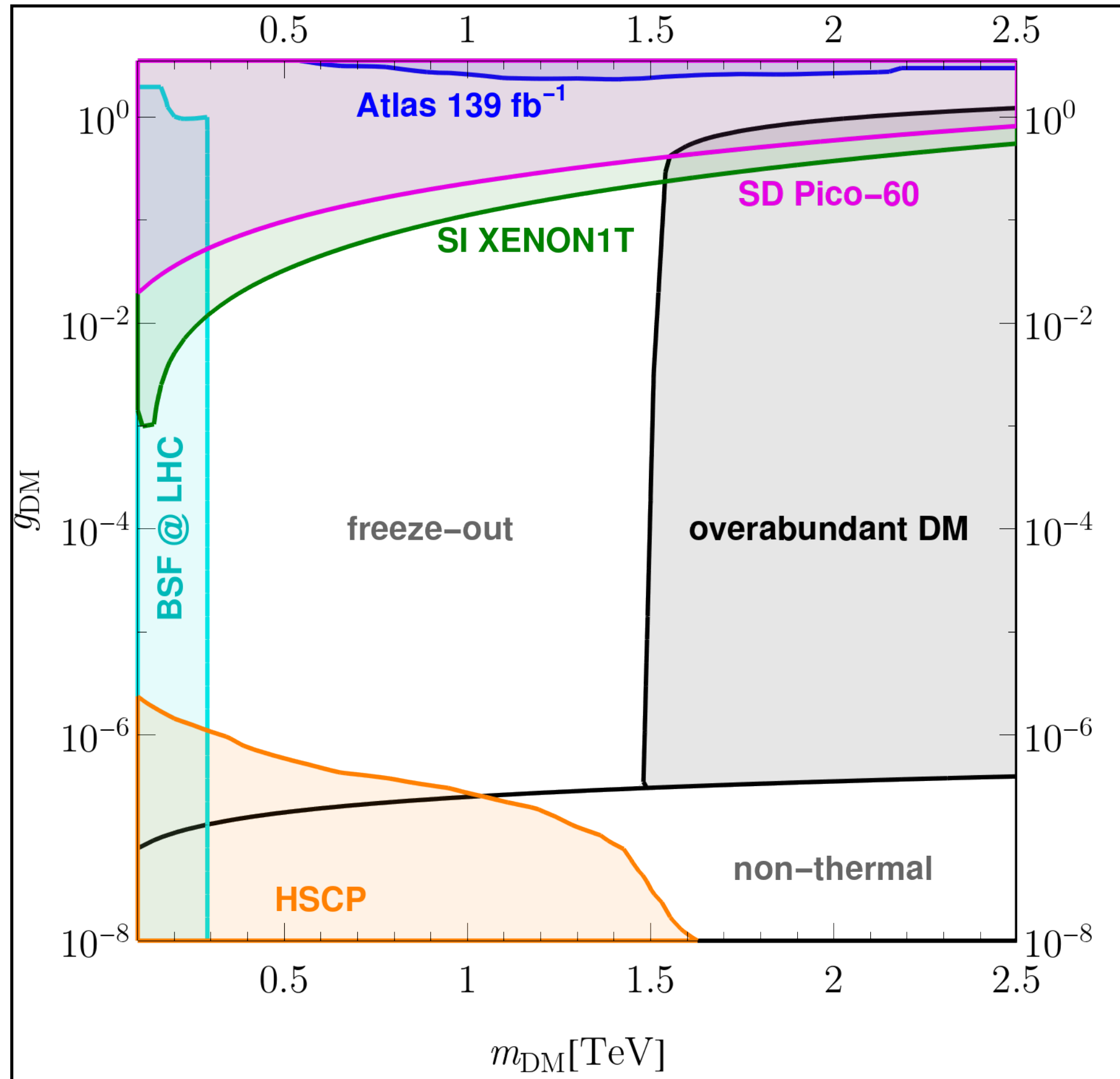
Sommerfeld+BSF

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# t- channel Simplified Models : Current and future projections



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M. Becker, E. Copello, J. Harz K. Mohan, **DS**. JHEP08(2022) 145

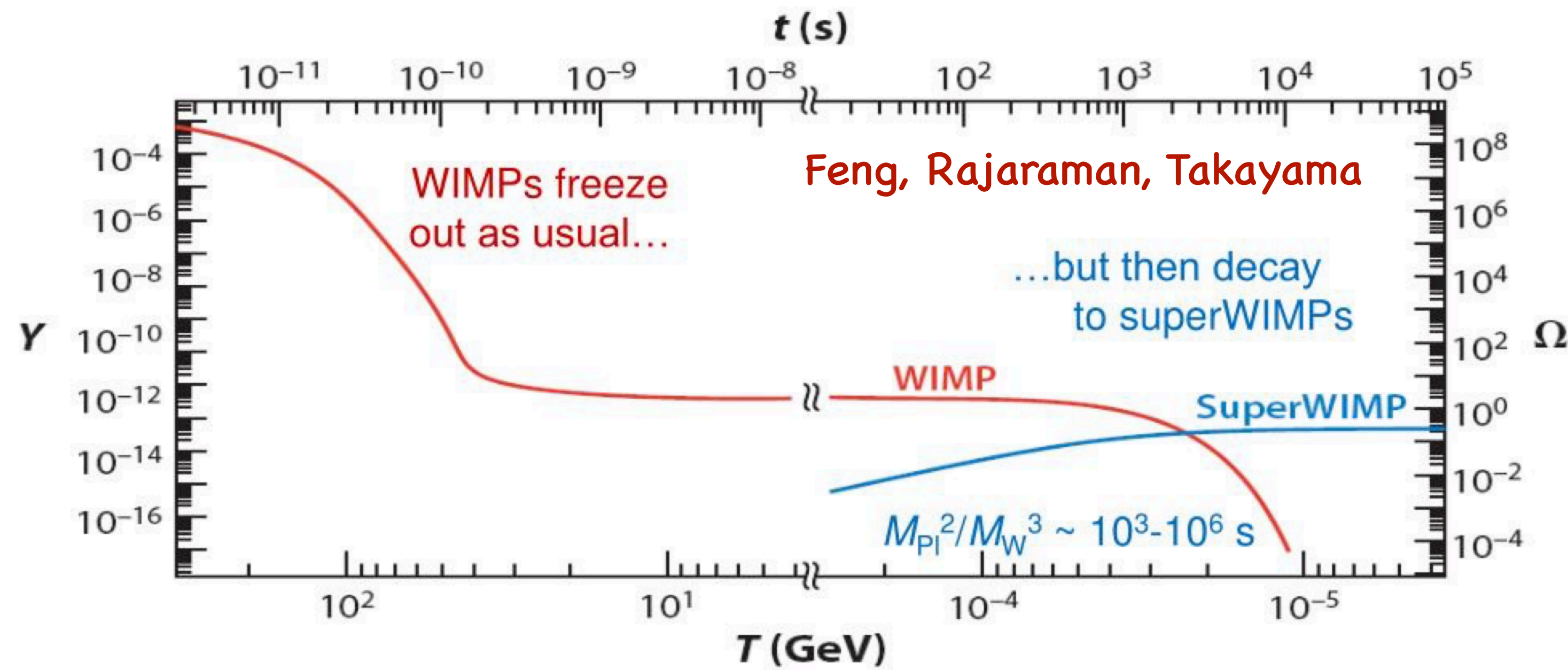
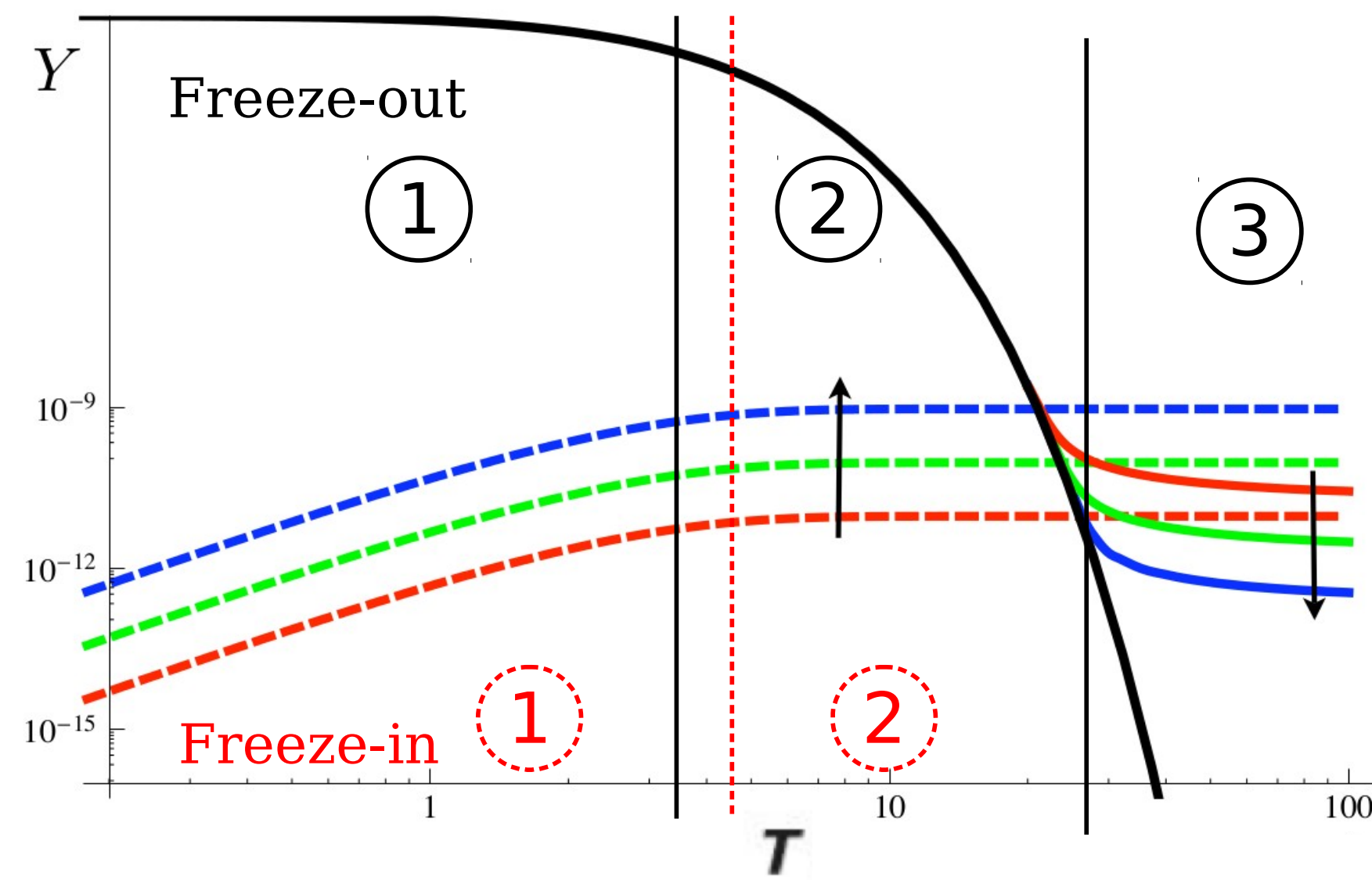
# Alternative Mechanisms of Dark Matter Production

(Non-) Thermal mechanisms

Freeze-In

Super WIMPS

Tweaked from arXiv:0911.1120



Both set ups characterised by extremely weakly interacting particles



# Cosmological Probes of SuperWIMP Dark Matter

## What if Neutralinos are not the Lightest SUSY particle, but next to lightest?

- In Supergravity inspired Supersymmetry scenarios, the gravitino can be the lightest particle, and very very weakly coupled to the neutralino, leading to a long lived neutralino (decaying to a gravitino + a Photon).
- The neutralino (a WIMP) can Freeze-out, and long afterwards decay to gravitino (**SuperWIMP**).
- Being extremely long lived it will escape the detector without a trace (No prompt searches).
- However it will leave definite signatures in Cosmology due to energy dump as photon.

The gravitino mass is a free parameter related to the SUSY breaking scale  $F$       Feng, Rajaraman, Takayama hep-ph/0306204

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$$m_{\tilde{G}} \simeq \langle F \rangle / m_{\text{pl}}$$

Extremely long lived

$$L = c\tau \simeq 2.8 \times 10^{22} \left( \frac{\text{GeV}}{m_{\chi_1^0}} \right)^3 \frac{(1 - 2\epsilon_{SM})}{\epsilon_{SM}^3 (1 + 3(1 - 2\epsilon_{SM}))} m$$

$$\epsilon_{SM} \equiv \frac{E_\gamma}{m_{\chi_1^0}} = \frac{m_{\chi_1^0}^2 - m_{\tilde{G}}^2}{2m_{\chi_1^0}^2}$$

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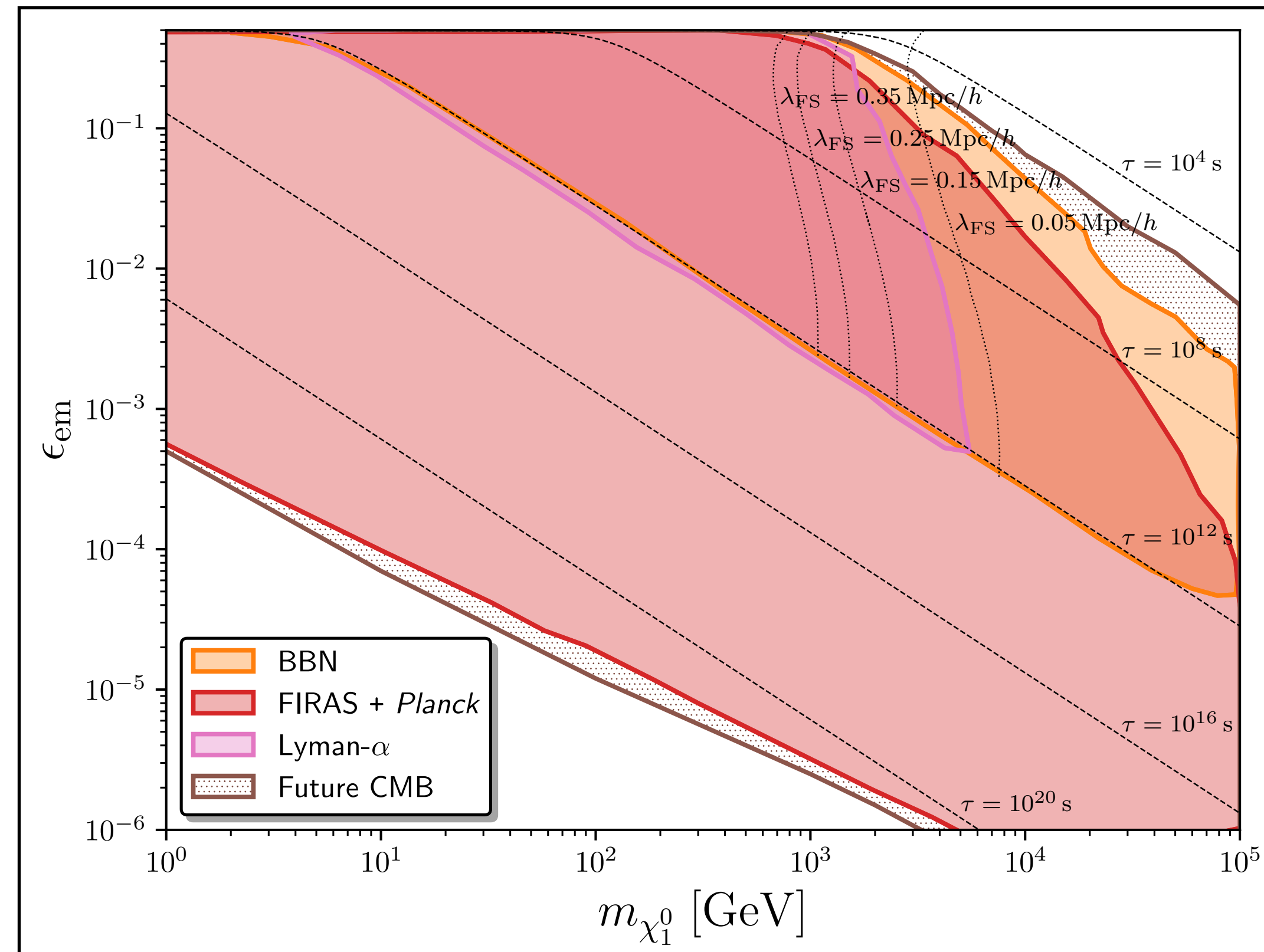
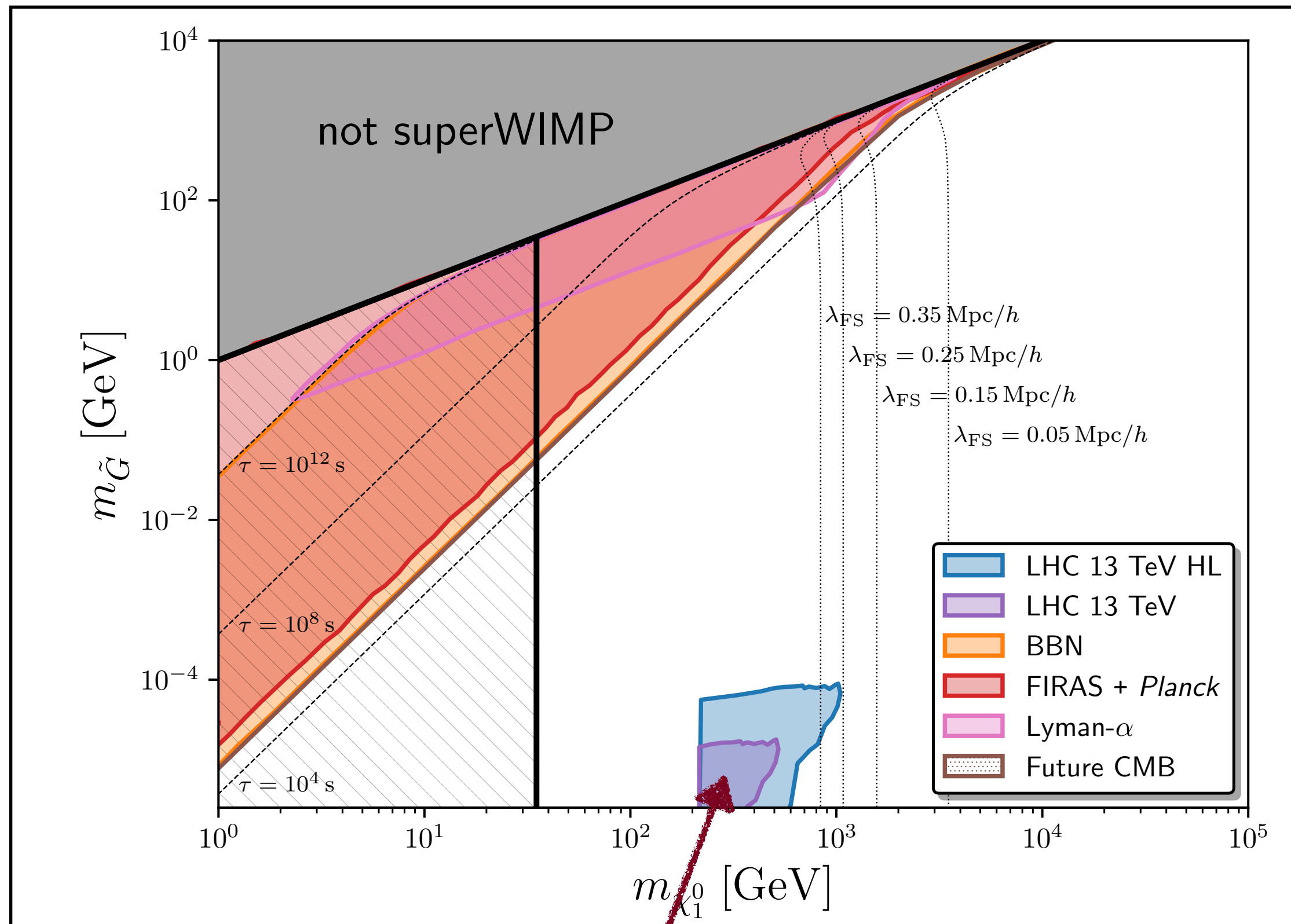
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1. **Big Bang Nucleosynthesis:** Injected photons/energy can photodissociate nuclei and change primordial element abundances
2. **CMB Spectral Distortion:** If the lifetime is about  $10^6$ - $10^{13}$  s can distort the CMB blackbody energy spectrum
3. **CMB Anisotropies:** Temperature and polarization anisotropies due to changes in acoustic peaks of CMB angular spectra
4. **Constraints from Lyman-alpha forest:** A relativistic component of the SuperWIMP leads to a non-zero velocity dispersion, hence a large free streaming scale and suppression of small scale fluctuations

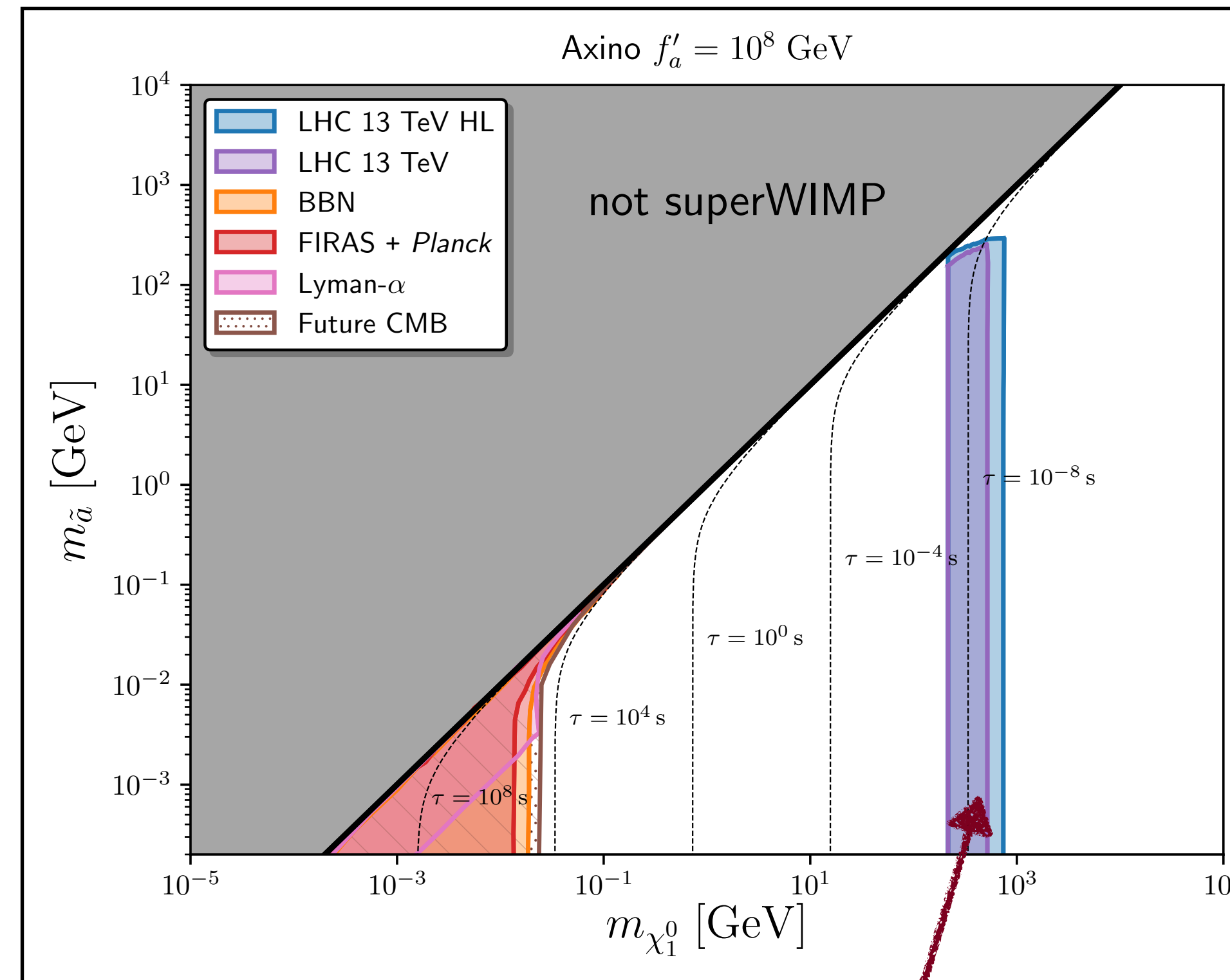
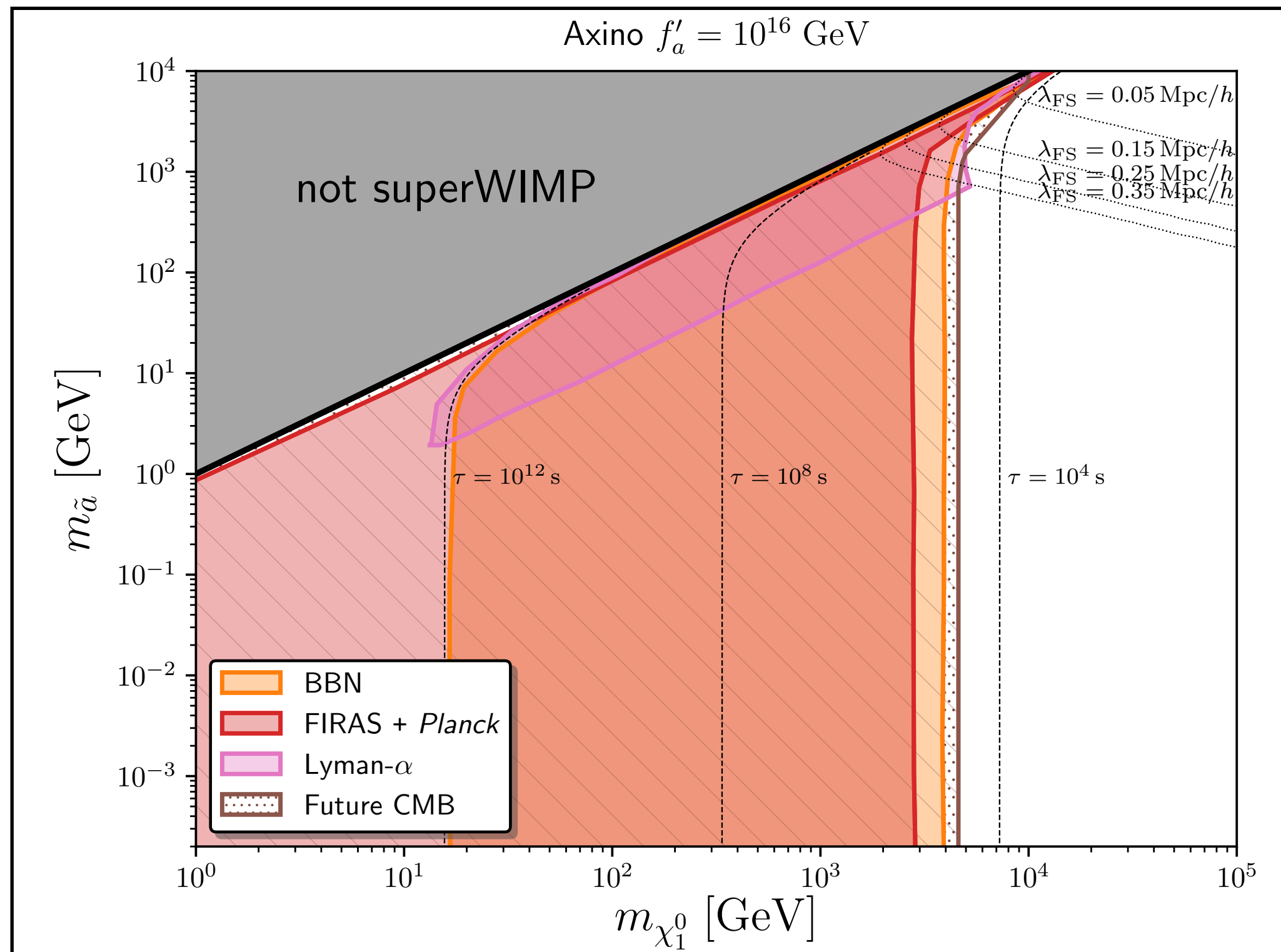
# t-channel Simplified Models : Constraints on gravitino Superwimps



LLP searches reinterpreted from displaced photon searches

1. ATLAS: PRD90 11(2014) 11205
2. CMS: Phys. Rev. D 100, 112003 (2019)

# t- channel Simplified Models : Constraints on axino Superwimps



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# t-channel Simplified Models : Recommendations and benchmarks

## DARK MATTER VIA $t$ -CHANNEL PRODUCTION COSMOLOGY SECTION

A PREPRINT

LHC Dark Matter Working Group

### 2 Contents

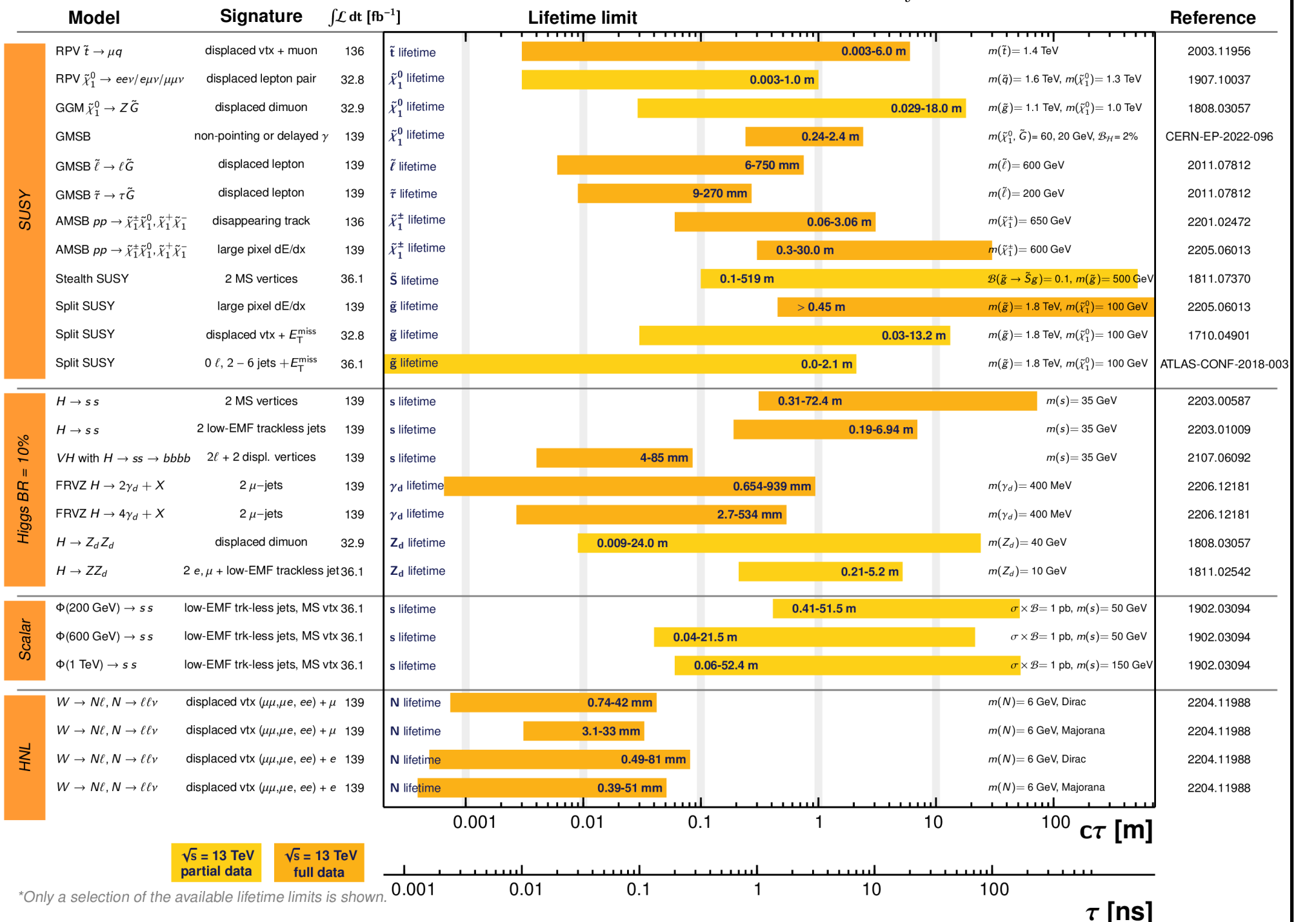
3	<b>1 Introduction: Appearance of long-lived particles in <math>t</math>-channel models</b>	<b>2</b>
4	<b>2 Currently performed searches</b>	<b>2</b>
5	<b>3 Coverage of current searches</b>	<b>3</b>
6	3.1 Freeze-in/superWIMP regime	3
7	3.2 Conversion-driven freeze-out regime	4
8	3.2.1 Quarkphilic minimal model	4
9	3.2.2 Leptophilic minimal model	5
10	3.2.3 Non-minimal models	5
11	3.3 Occurrence of LLPs in canonical freeze-out	7
12	<b>4 Gaps in the current coverage</b>	<b>7</b>

### ATLAS Long-lived Particle Searches\* - 95% CL Exclusion

Status: July 2022

ATLAS Preliminary

$\int \mathcal{L} dt = (32.8 - 139) \text{ fb}^{-1}$   $\sqrt{s} = 13 \text{ TeV}$



# t-channel Simplified Models : Recommendations and benchmarks

We need more recast codes implemented, for which  
We need help and resources from our experimental colleagues

llprecasting / recastingCodes Public

Code Issues Pull requests Actions Projects Security Insights

main 7 Branches 0 Tags

Go to file Code

andlessa Added emerging jets 9bf8363 · last month 274 Commits

- CalRatioDisplacedJet/ATLAS-EXOT-2019-23 Organizing folders 3 months ago
- Delphes\_LLP FIX in DelphesLLP 2 months ago
- DisappearingTracks Mark Goodsell: Added CMS-EXO-19-010 3 years ago
- DisplacedVertices Added missing file last month
- EmergingJets/CMS-EXO-18-001 Added emerging jets last month
- HSCPs Fix in plot label last month
- .gitignore Added gitignore 4 years ago
- README.md Added emerging jets last month

### LLP Recasting Repository

This repository holds example codes for recasting long-lived particle (LLP) searches. The code authors and repository maintainers are not responsible for how the code is used and the user should use discretion when applying it to new models.

### Adding your recasting code

This is an open repository and if you have developed a code for recasting a LLP analysis, we encourage you to include it here. Please contact [llp-recasting@googlegroups.com](mailto:llp-recasting@googlegroups.com) and we will provide you with the necessary information for including your code.

### Repository Structure

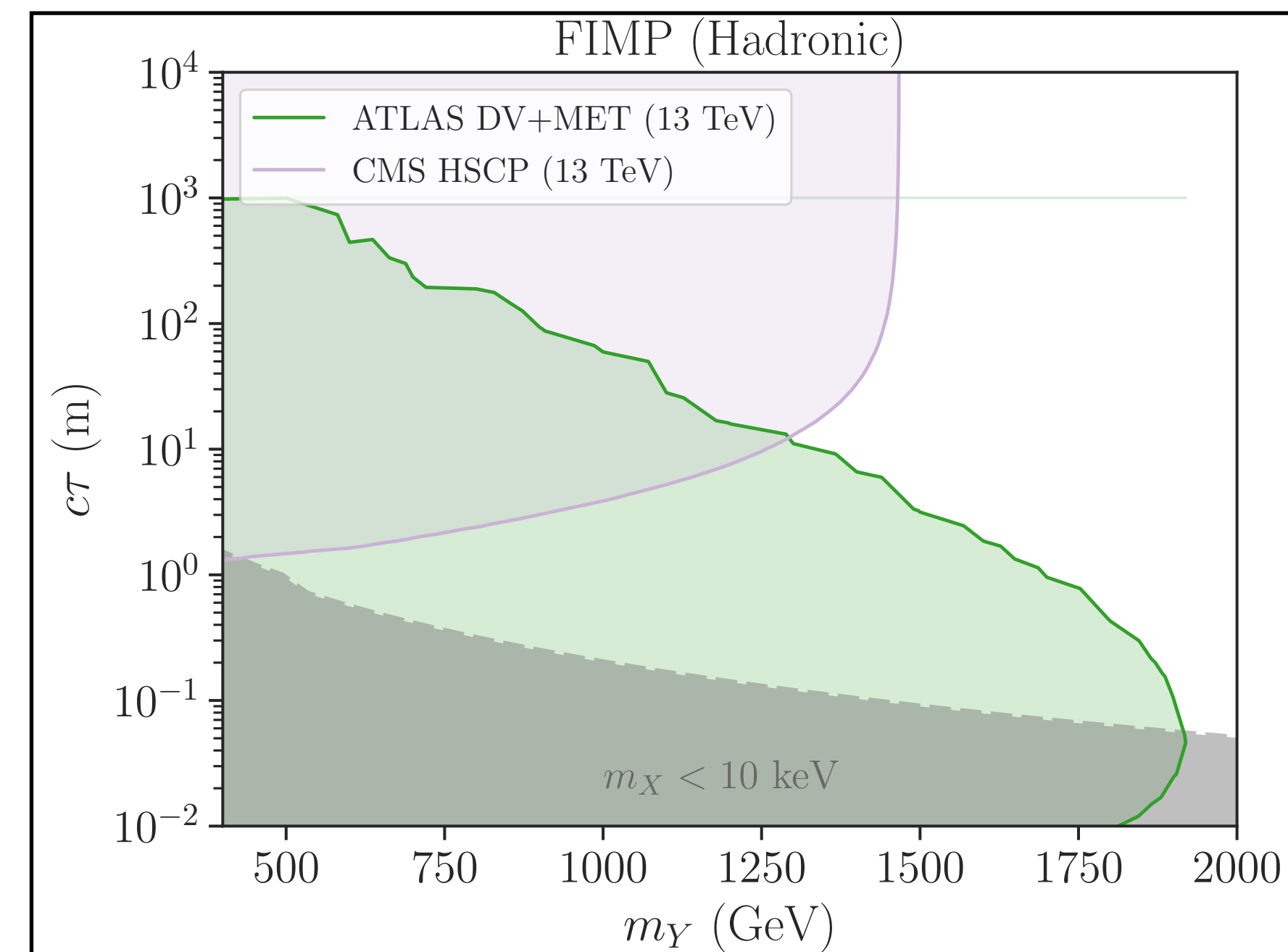
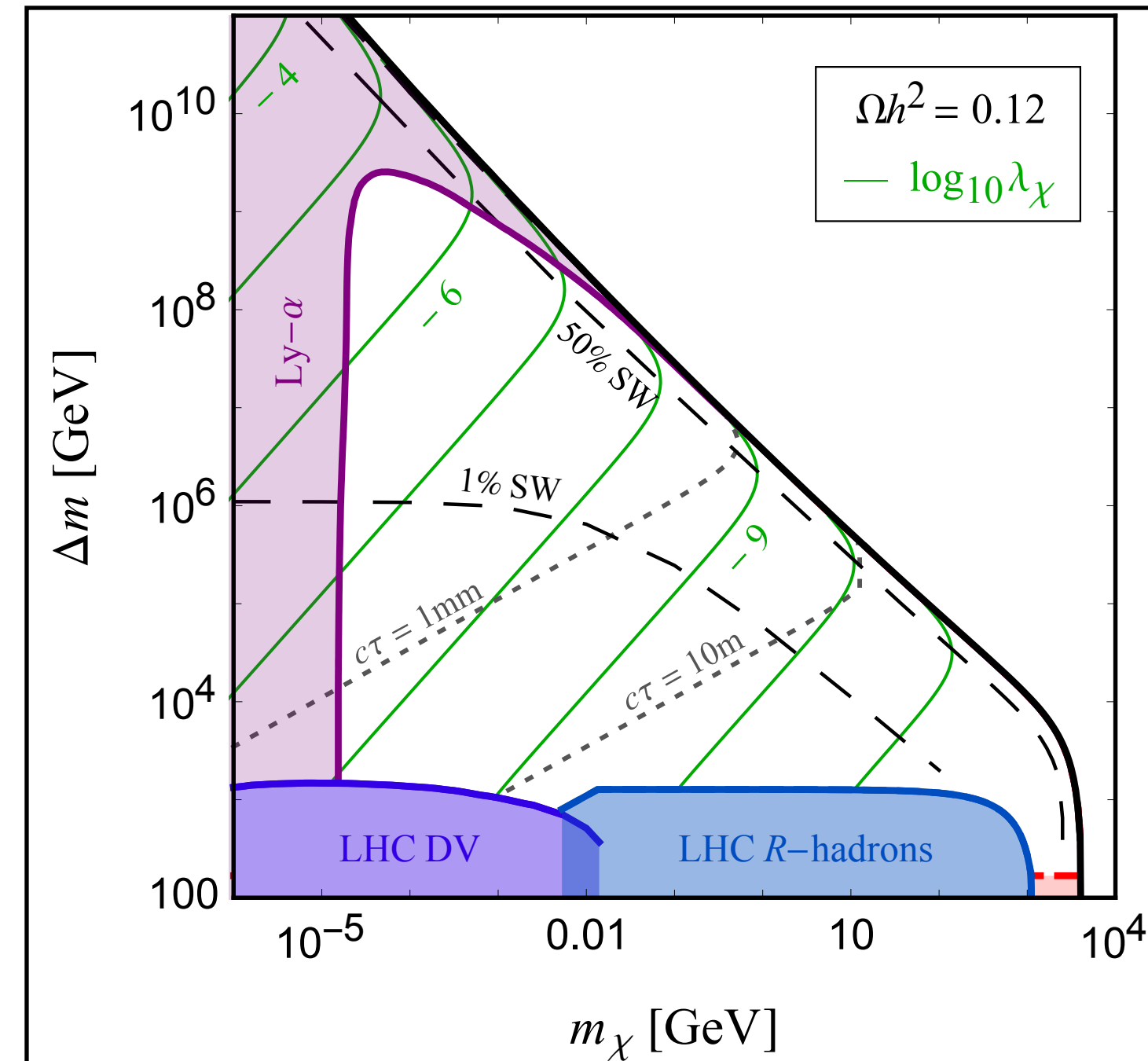
The repository folder structure is organized according to the type of LLP signature and the corresponding analysis and authors:

- Displaced Vertices
  - 13 TeV ATLAS Displaced Jets
  - 13 TeV ATLAS Displaced Vertex plus MET by ALessa
  - 13 TeV ATLAS Displaced Vertex plus MET by GCottin
  - 8 TeV ATLAS Displaced Vertex plus jets by GCottin
- CalRatio Displaced Jets
  - 13 TeV ATLAS Displaced Jets in the calorimeter
- Emerging Jets
- Heavy Stable Charged Particles
  - 13 TeV ATLAS HSCP - 139/fb
  - 13 TeV ATLAS HSCP - 31.6/fb
  - 8 TeV CMS HSCP
- Disappearing Tracks

A README file can be found inside each folder with the required dependencies and basic instructions on how to run the recasting codes.

### Running the Recasting Code

Andre Lessa's Github repo



# Conclusions

- ☀ Simplified models provide a robust pathway to analyze theoretical and experimental Constraints that map to constraints on full-models.
- ☀ t-channel DM models provide a rich phenomenology, with complementary constraints from a variety of signatures
- ☀ LLP searches form a crucial component in closing the gap between freeze-out and non-thermal mechanisms of dark matter in t-channel.
- ☀ Needed: Experiment-theory collaborations, more recast/reinterpretation codes

International Joint Workshop on the Standard Model and Beyond 2024  
& 3rd Gordon Godfrey Workshop on Astroparticle Physics

9–13 Dec 2024  
Australia/Sydney timezone

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