

# Dark photon lifetime: closer look at SM resonances

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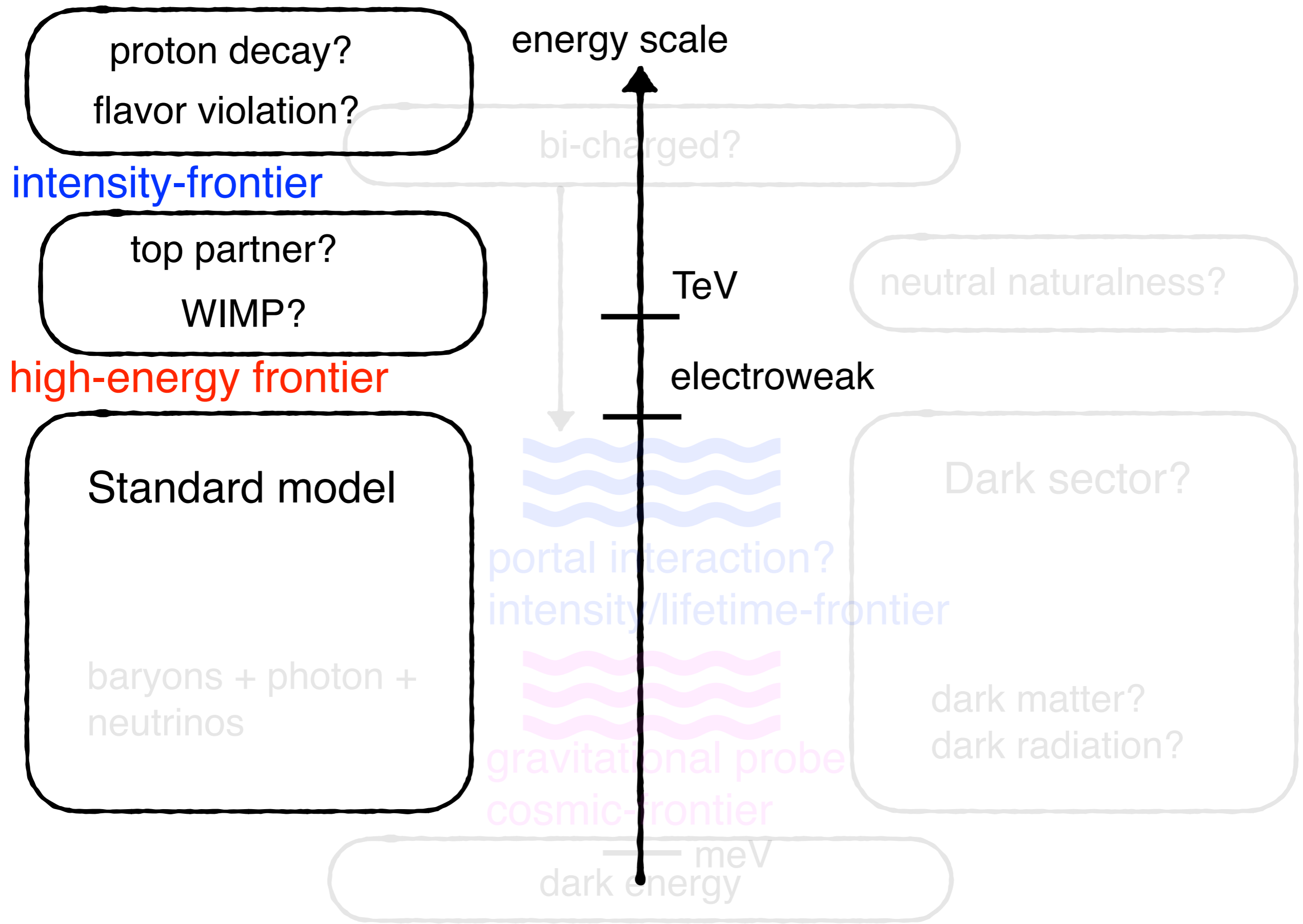


Based on

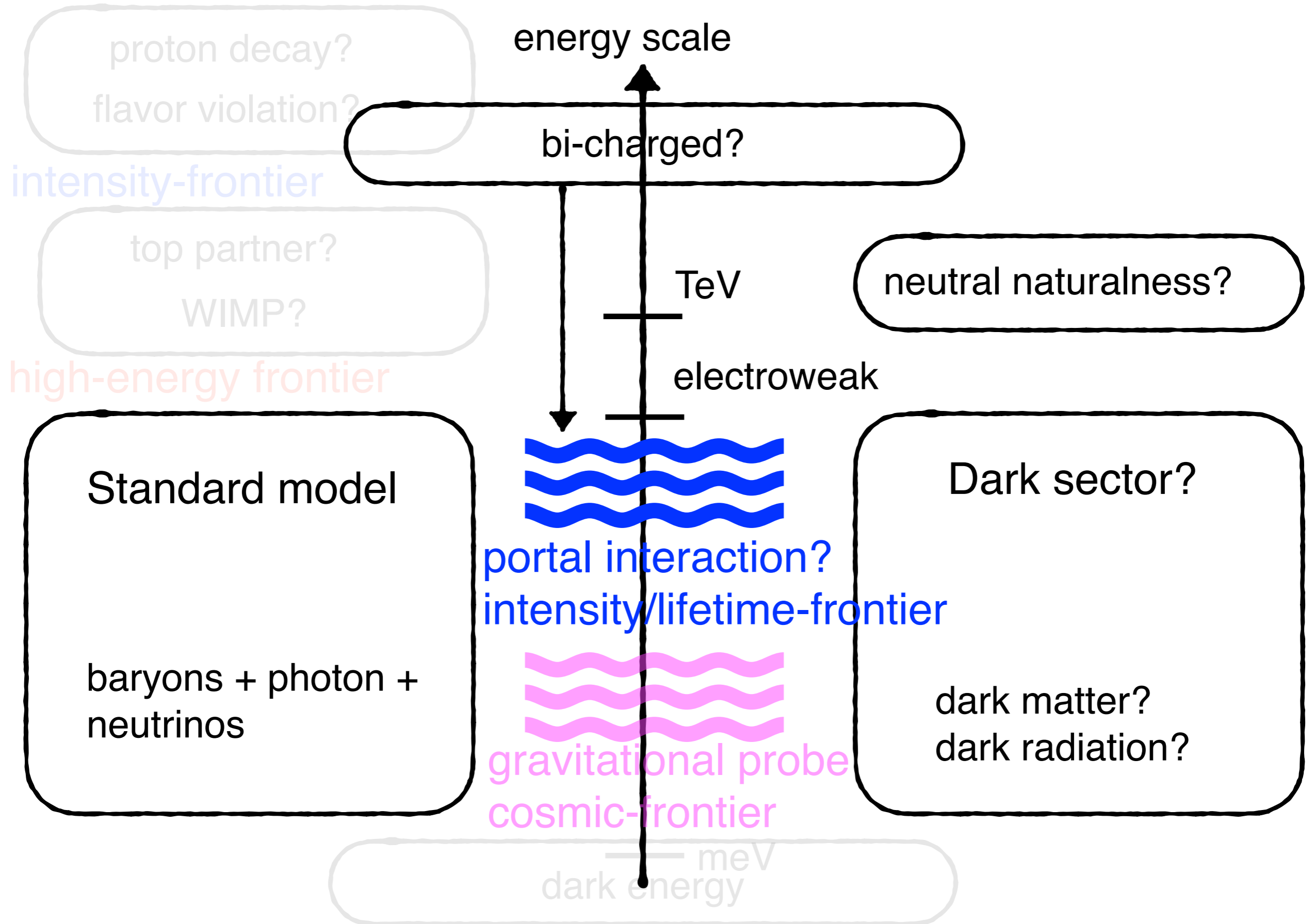
AK, Takumi Kuwahara, Shigeki Matsumoto, Yu Watanabe and Yuki Watanabe, [arXiv:2404.06793](https://arxiv.org/abs/2404.06793)

July 3, 2024 @ LLP2024

# High-energy physics



# High-energy? physics



# Contents

## Review of dark photon

- long-lived dark photon searches
- resonant decay through mixing with SM resonances

## Closer look at mixing with SM resonances

- conventional computation of resonant decay
- caveat in large kinetic mixing

# Intensity frontier

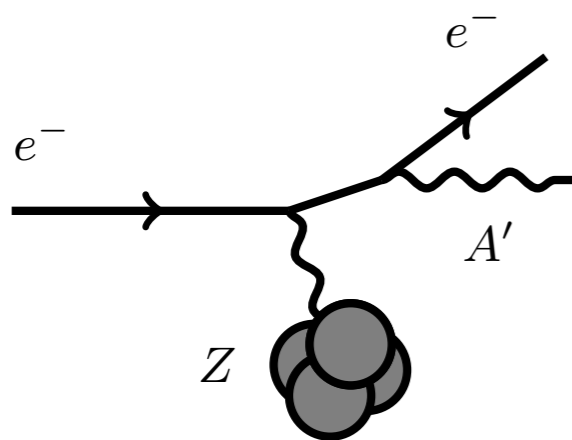
Dark photon portal  $\mathcal{L} \supset \frac{\epsilon_Y}{2} Y^{\mu\nu} F'_{\mu\nu}$

- kinetic mixing between the hyper-charge gauge boson and dark photon
- SM particles feebly couple to dark photon  $\mathcal{L} \supset \epsilon e j_{\text{em}}^\mu A'_\mu$   $\epsilon_Y \cos \theta_W = \epsilon$
- mass from dark Higgs (or Stueckelberg)

Beam-dump experiment e.g., CHARM, E137, SHiP...

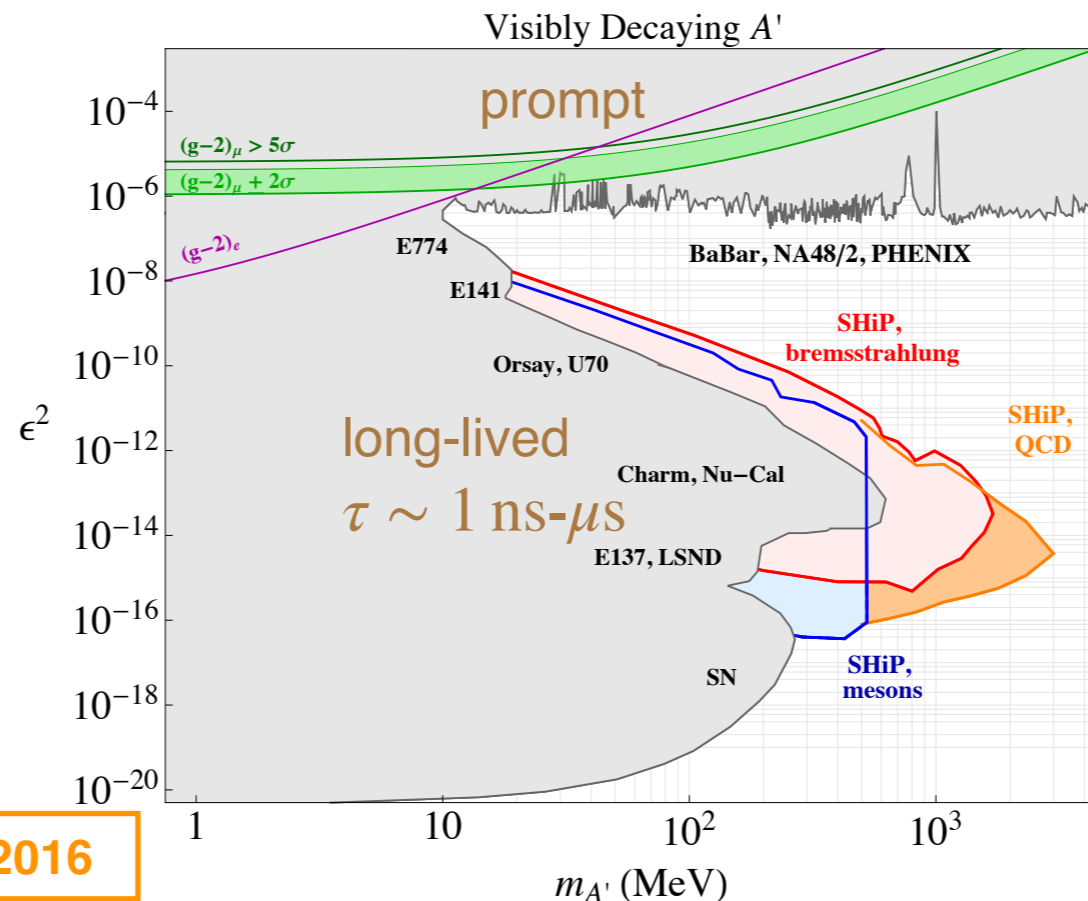
Talk by Anne-Marie Magnan

target



shield

detector



$$A' \rightarrow e^+e^-$$

# Lifetime frontier

## LHC lifetime frontier

- HL-LHC (2027+)  $\mathcal{L} = 3 \text{ ab}^{-1}$ 
  - intensity frontier as well as high-energy frontier

Berlin and Kling, PRD, 2019

### - FASER(2)

- forward direction  $\theta_{\text{det}} = 2 \times 10^{-3}$
- more boosted and thus shorter lifetime particles come

$$p_{\text{geo}} \sim p_T / \theta_{\text{det}}$$

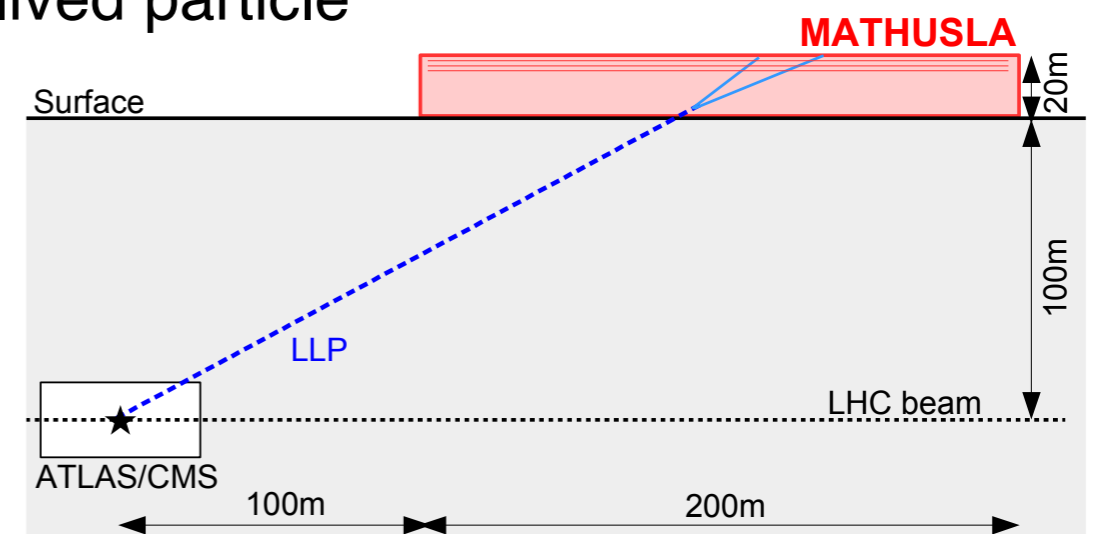
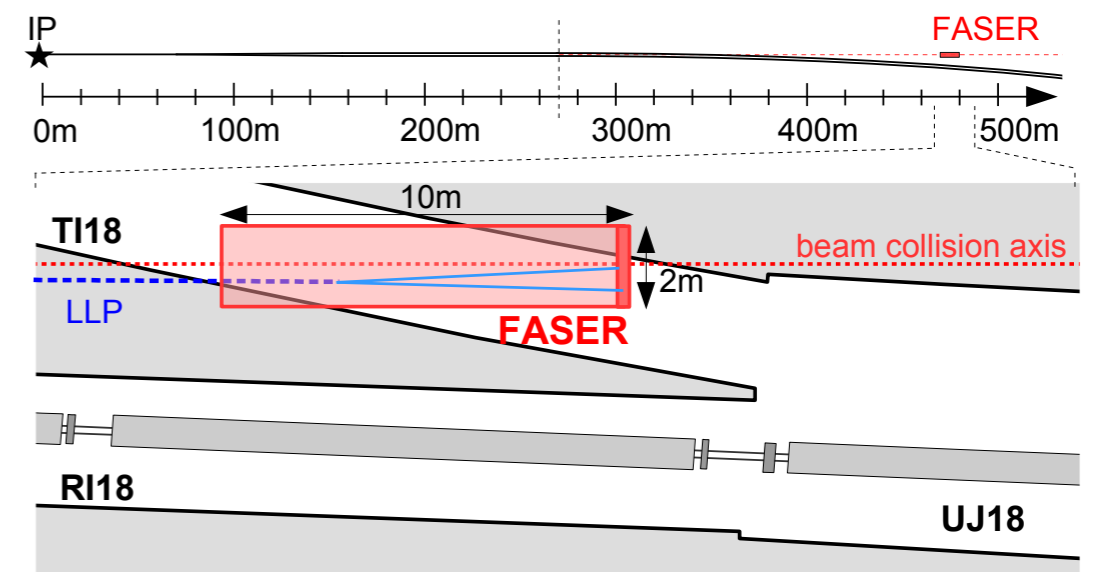
Talks by Felix Kling,  
Yuxiao Wang and  
Motoya Nonaka

- typical transverse momentum is determined by the production process of long-lived particle

### - MATHUSLA (CODEX-b)

- off-axis  $\theta_{\text{det}} = 0.5$
- less boosted and thus longer lifetime particles come

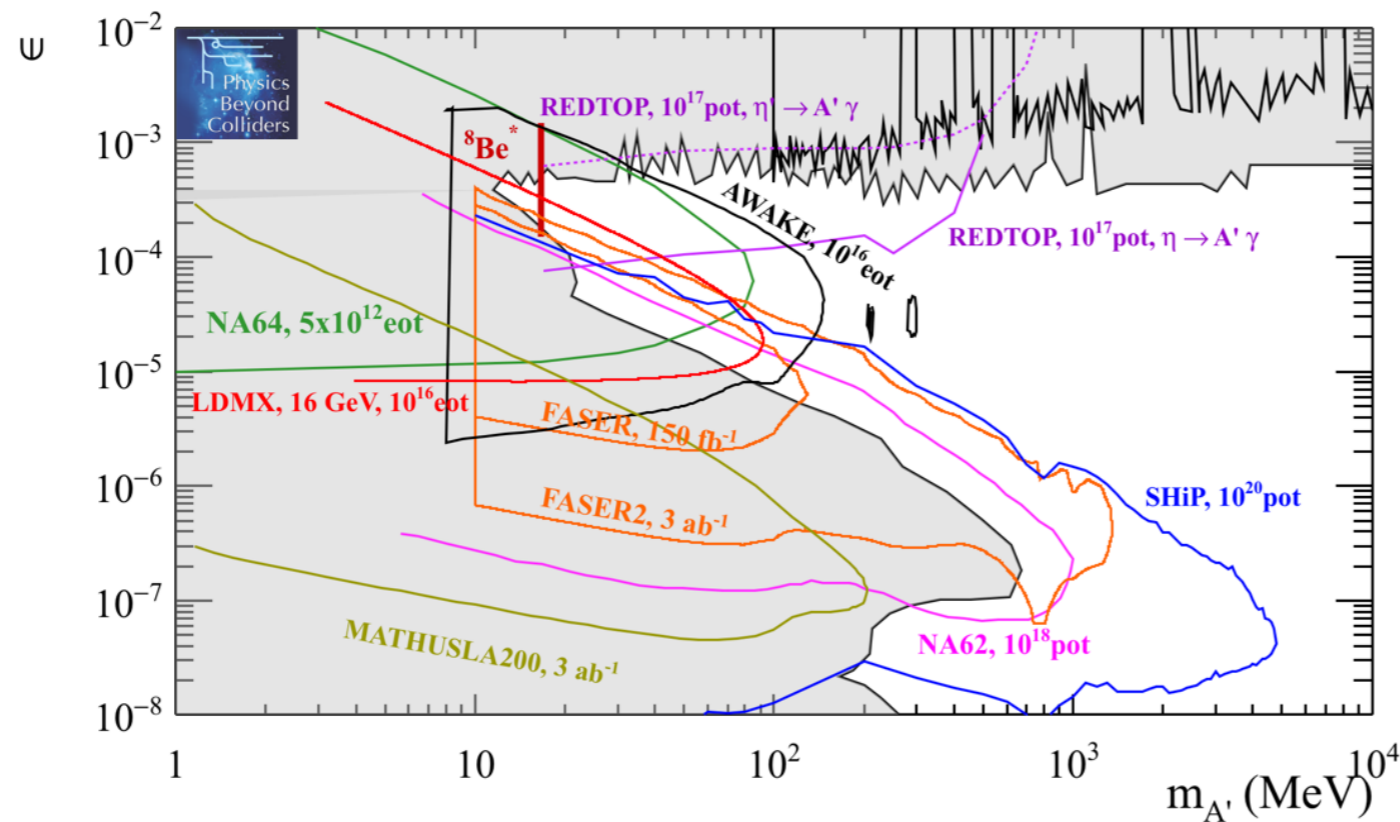
Talks by Jake Pfaller  
and Erez Etzion



# Intensity/lifetime frontier

## Dark photon portal

- minimal dark photon model



Physics Beyond Colliders  
collaboration, J. Phys. G, 2020

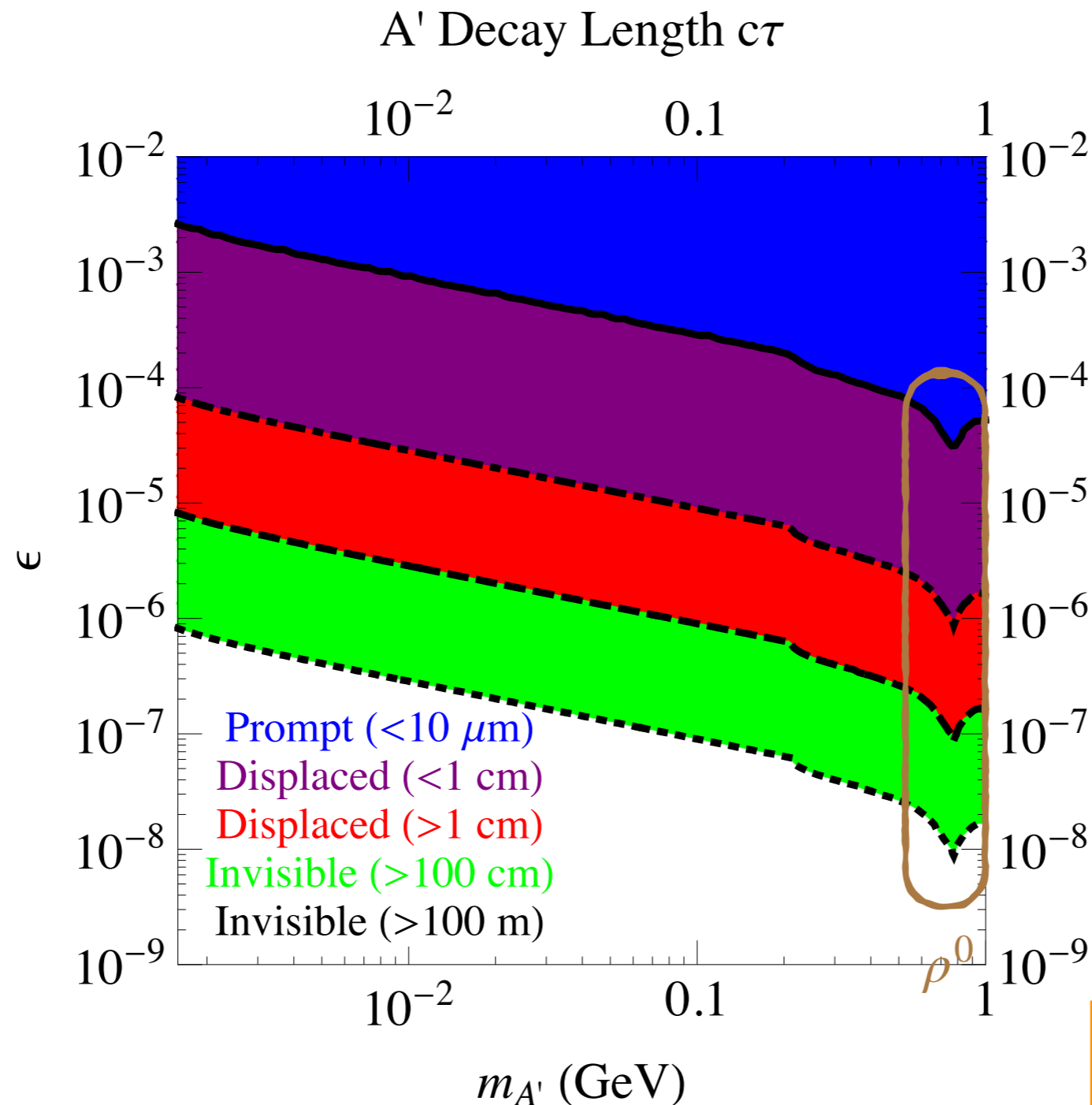
- upper bound determined by the lifetime (should be sufficiently long-lived)
- lower bound determined by the lifetime (should decay) and production
- in the minimal dark photon model, only one parameter (kinetic mixing) for a given dark photon mass

$$\Gamma(A' \rightarrow \bar{f}f) \simeq \frac{1}{3} \alpha \epsilon^2 Q_f^2 m_{A'}$$

# Resonant decay through mixing

## Short lifetime in a specific mass

- thorough mixing with SM resonances  $A' \rightarrow V^* \rightarrow \bar{f}f$  or hadrons



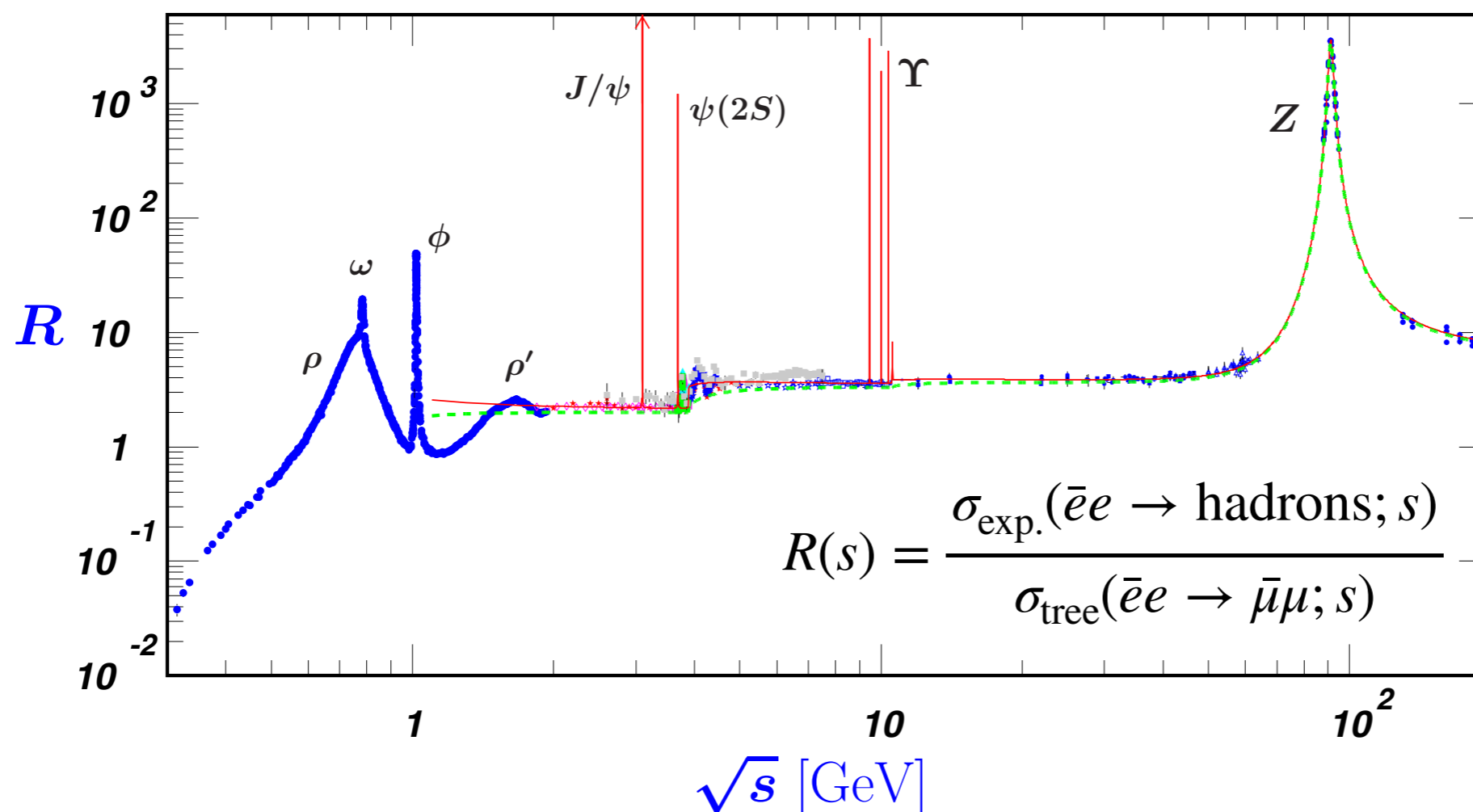
Essig, Harnik, Kaplan,  
and Toro, PRD, 2010



# Conventional computation

All SM resonances are relevant

- with the same quantum number (neutral, spin 1)



PDG 2022

Multiplying R-ratio by decay width to muon pair

$$\Gamma(A' \rightarrow \text{hadrons}) = \Gamma(A' \rightarrow \bar{\mu}\mu) \times R(m_{A'}^2)$$

- misses non-hadronic resonances like true muonium (later)

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# Closer look at conventional computation

## Mass mixing basis

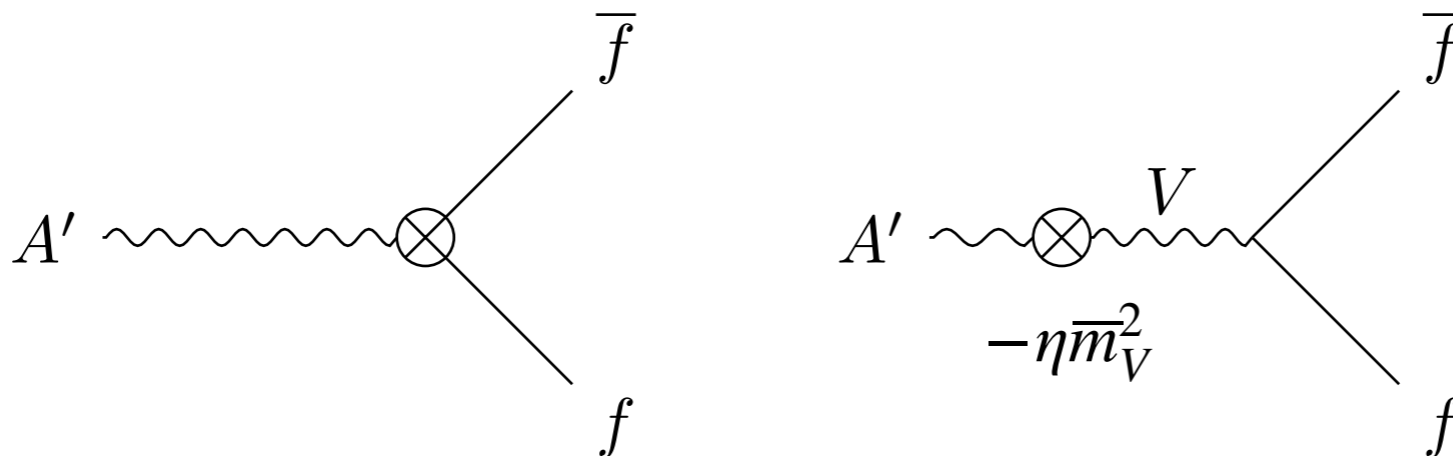
$$\mathcal{L} \supset \bar{m}_V^2 (V_\mu, A'_\mu) \begin{pmatrix} 1 & -\eta \\ -\eta & \delta^2 + \eta^2 \end{pmatrix} \begin{pmatrix} V^\mu \\ A'^\mu \end{pmatrix} \quad \delta = \frac{\bar{m}_{A'}}{\bar{m}_V} \quad \text{- ratio of mass parameter (input mass)}$$

- effective mixing parameter  $\propto \epsilon$

- one can obtain “classical” mass eigenstates by diagonalizing it
- $\delta=1$  corresponds to mass degenerate limit (though eigenvalues split by  $\eta$ )

## “Mass insertion” method

- using off-diagonal part as a perturbation



# “Mass insertion” method

## Width of dark photon

$$\Gamma^{\text{MI}}(A' \rightarrow \bar{f}f) = \frac{M_{A'}}{16\pi} \frac{4}{3} \left| \bar{g}_f^{A'} + \bar{g}_f^V \frac{-\eta \bar{m}_V^2}{M_{A'}^2 - \bar{m}_V^2 + i\bar{m}_V \bar{\Gamma}_V} \right|^2 \quad M_{A'}^2 = \bar{m}_V^2(\delta^2 + \eta^2)$$

$$\bar{\Gamma}_V = \frac{\bar{m}_V}{16\pi} \frac{4}{3} g_V^2 \quad \text{- decay width in the absence of dark photon}$$

- in the mass degenerate limit, second term is resonantly large

$$\Gamma^{\text{MI}}(A' \rightarrow \bar{f}f) \simeq \frac{M_{A'}}{16\pi} \frac{4}{3} \left( \bar{g}_f^V \frac{\eta}{\bar{\Gamma}_V / \bar{m}_V} \right)^2$$

- A' width is larger than that of V for  $\eta > \bar{\Gamma}_V / \bar{m}_V$
- the enhancement can be 10 orders of magnitude for narrow resonance like true muonium, J/ψ and Y
- is perturbation valid?

# “Classical” method

## Width of dark photon

$$\mathcal{L} \supset \bar{m}_V^2 (V_\mu, A'_\mu) \begin{pmatrix} 1 & -\eta \\ -\eta & \delta^2 + \eta^2 \end{pmatrix} \begin{pmatrix} V^\mu \\ A'^\mu \end{pmatrix}$$

- diagonalizing mass and compute the width at tree level
- in the mass degenerate limit, one obtains **nearly (but not exactly) identical particle** with half width of original SM particles at the tree level

$$\Gamma(A' \rightarrow \bar{f}f) \simeq \Gamma(V \rightarrow \bar{f}f) \simeq \frac{m_{A'}}{16\pi} \frac{2}{3} g_V^2$$

- this does not depend on mixing parameter and thus not valid at small mixing parameter

## “Mass insertion” vs “Classical”

- (as demonstrated later) “mass insertion” is valid for small mixing parameter, while “classical” is valid for large

# “Pole” method

## Mixed propagator

$$\begin{aligned}
 \text{Diagram 1: } & \text{Wavy line } X \text{ with a shaded circle} = \text{Wavy line } X + \overset{\Pi_{XX}}{\text{Wavy line } X \text{ with a white circle}} + \overset{\Pi_{XY}}{\text{Wavy line } X \text{ with a white circle and a shaded circle}} \\
 \text{Diagram 2: } & \text{Wavy line } X \text{ with a shaded circle and wavy line } Y = \text{Wavy line } X \text{ with a white circle and wavy line } Y + \text{Wavy line } X \text{ with a white circle and wavy line } Y \text{ with a shaded circle} \\
 \text{Diagram 3: } & \text{Wavy line } Y \text{ with a shaded circle and wavy line } Y = \text{Wavy line } Y + \text{Wavy line } Y \text{ with a white circle and wavy line } X \text{ with a shaded circle} + \text{Wavy line } Y \text{ with a white circle and wavy line } Y \text{ with a shaded circle}
 \end{aligned}$$

$$D_{XX}(s) = \frac{1}{s - m_X^2 - \Pi_{XX}(s) - \frac{\Pi_{XY}(s)^2}{s - m_Y^2 - \Pi_{YY}(s)}} - \text{imaginary part of one-loop mixing does not have classical interpretation (i.e., quantum effect)}$$

- find complex poles of mixed propagator (solution of Schwinger-Dyson)
- most robust (by definition of unstable “particles”)

# Trum muonium

## Spin 1 bound states of muon-anti muon

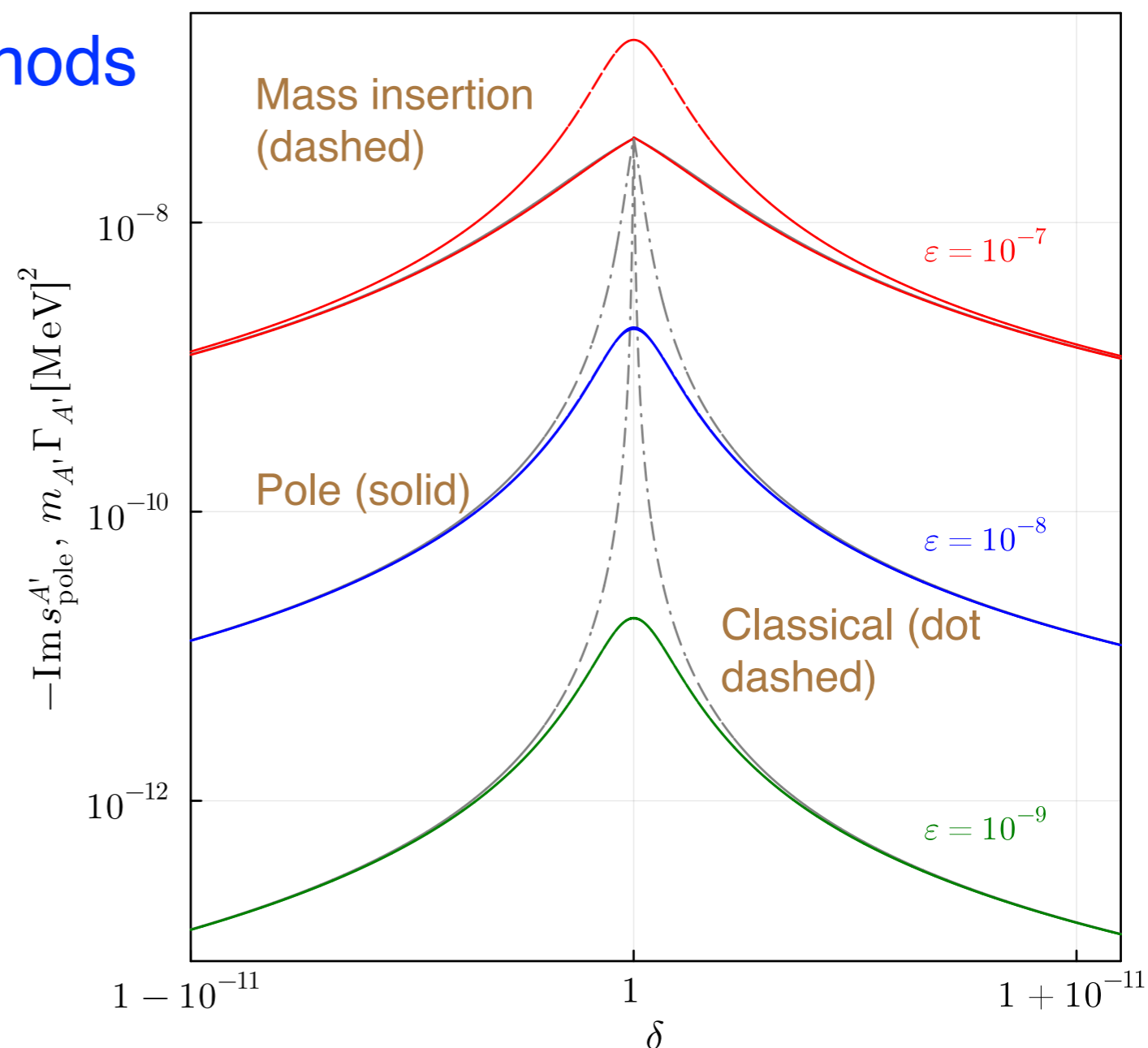
Matsumoto, Watanabe and Watanabe, JHEP, 2023

- narrow resonance  $\bar{m}_V \simeq 2m_\mu$
- $\bar{\Gamma}_V \simeq 3.66 \times 10^{-10} \text{ MeV}$

AK, Kuwahara, Matsumoto, Watanabe and Watanabe, arXiv:2404.06793

## Comparison of three methods

- all agree away from mass degenerate limit
- “mass insertion” is valid for  $\epsilon < 3.2 \times 10^{-8}$  while “classical” is valid for  $\epsilon > 3.2 \times 10^{-8}$
- critical value  $\epsilon_{\text{cr}}$  corresponds to  $\eta = \bar{\Gamma}_V / \bar{m}_V$



# Trum muonium

## Anti-resonance of decay width

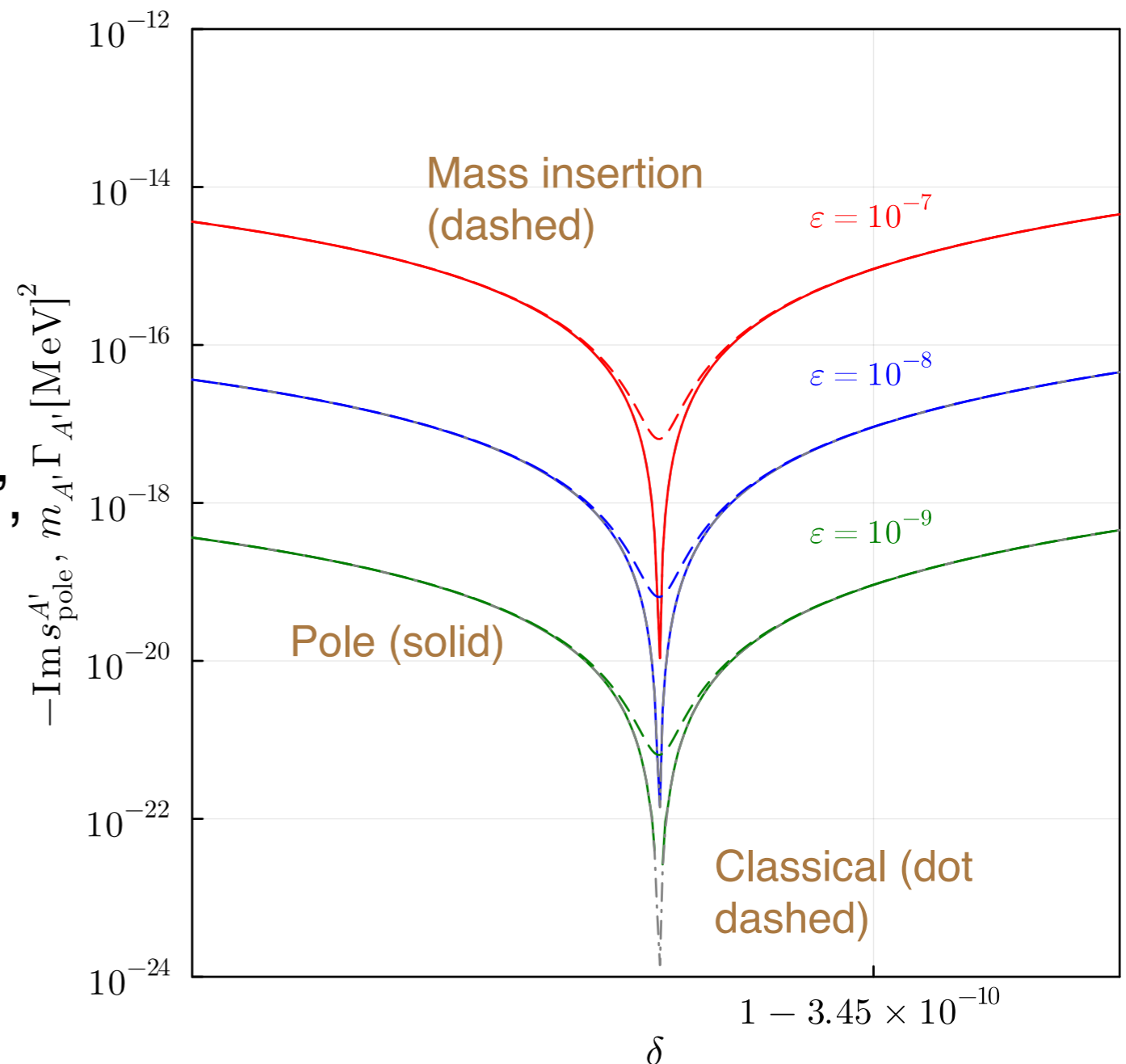
- slightly below resonance of decay width
- destructive interference of two contributions

$$\Gamma^{\text{MI}}(A' \rightarrow \bar{f}f) = \frac{M_{A'}^2}{16\pi} \frac{4}{3} \left| \bar{g}_f^{A'} + \bar{g}_f^V \frac{-\eta \bar{m}_V^2}{M_{A'}^2 - \bar{m}_V^2 + i\bar{m}_V \bar{\Gamma}_V} \right|^2$$

- “classical” agrees with “Pole”, but not “mass insertion”

Matsumoto, Watanabe and Watanabe, JHEP, 2023

AK, Kuwahara, Matsumoto, Watanabe and Watanabe, arXiv:2404.06793





# Summary

## Critical mixing parameter

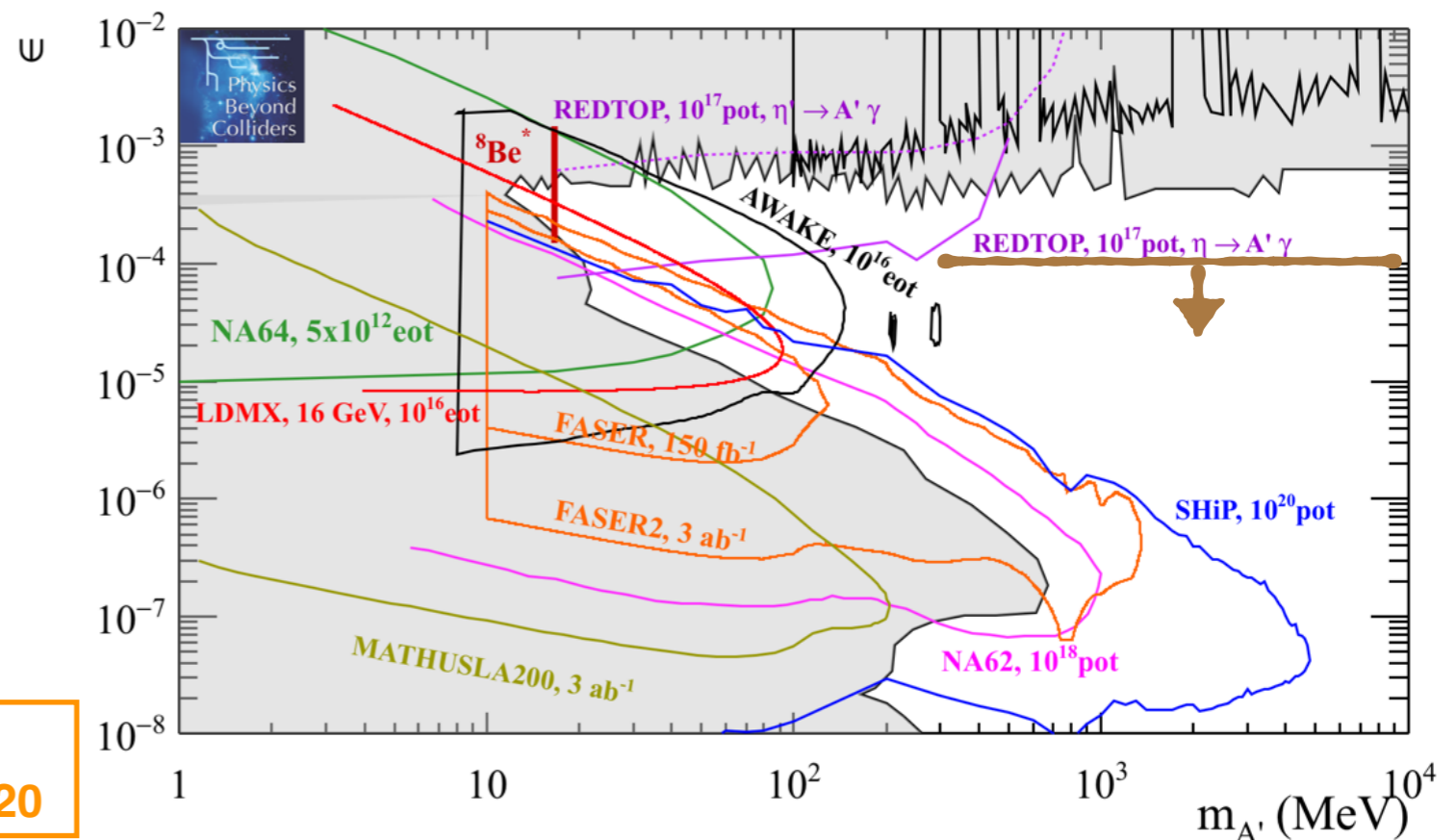
- corresponds to  $\eta = \bar{\Gamma}_V / \bar{m}_V$
- checked for  $\rho$  and Z-boson as well as true monism
- conventional multiplication of R-ratio for hadrons is justified for  $\epsilon < \epsilon_{cr}$
- smaller for narrower resonance

## Non-hadronic resonance

- to be added by hand
- not only resonance but also anti-resonance

AK, Kuwahara, Matsumoto, Watanabe and Watanabe, arXiv:2404.06793

Mesons	Mass (MeV)	Width (MeV)	Branching ratio to $e^-e^+$	Critical mixing $\epsilon_{cr}$
$\rho$ (770)	775.26	149.1	$4.72 \times 10^{-5}$	$9.53 \times 10^{-1}$
$\omega$ (782)	782.66	8.68	$7.38 \times 10^{-5}$	$5.26 \times 10^{-1}$
$\phi$ (1020)	1019.461	4.249	$2.979 \times 10^{-4}$	$1.81 \times 10^{-1}$
$J/\psi$ (1S)	3090.9	$9.26 \times 10^{-2}$	$5.971 \times 10^{-2}$	$1.10 \times 10^{-3}$
$\psi$ (2S)	3686	$2.94 \times 10^{-1}$	$7.93 \times 10^{-3}$	$4.95 \times 10^{-3}$
$\psi$ (3770)	3773.7	27.2	$9.6 \times 10^{-6}$	$8.04 \times 10^{-1}$
$\psi$ (4040)	4039	80	$1.07 \times 10^{-5}$	$9.05 \times 10^{-1}$
$\psi$ (4160)	4191	70	$6.9 \times 10^{-6}$	$9.25 \times 10^{-1}$
$\Upsilon$ (1S)	9460	$5.4 \times 10^{-2}$	$2.38 \times 10^{-2}$	$7.64 \times 10^{-4}$
$\Upsilon$ (2S)	10023	$3.198 \times 10^{-2}$	$1.91 \times 10^{-2}$	$6.38 \times 10^{-4}$
$\Upsilon$ (3S)	10355	$2.032 \times 10^{-2}$	$2.18 \times 10^{-2}$	$4.68 \times 10^{-4}$
$\Upsilon$ (4S)	10579.4	20.5	$1.57 \times 10^{-5}$	$4.81 \times 10^{-1}$
$\Upsilon$ (10860)	10885.2	37	$8.3 \times 10^{-6}$	$7.67 \times 10^{-1}$
$\Upsilon$ (11020)	11000	24	$5.4 \times 10^{-6}$	$7.04 \times 10^{-1}$



Physics Beyond Colliders  
collaboration, J. Phys. G, 2020

**Thank you**

# GeV dark sector

## Motivations

- weak top-down reason
  - closer to electroweak scale is more natural (Higgs portal)
  - with supersymmetry  $\nu' = \sqrt{\frac{\epsilon g}{g'}} \nu$
- strong bottom-up reason
  - relic abundance of heavy ( $> 100$  TeV) stable particles overclose the Universe (Unitarity bound)
  - light (sub-GeV) dark matter evades high-energy collider experiments
    - dominating background from  $Z \rightarrow \nu\bar{\nu}$
    - higher-energy hadron collider is worse
  - light (sub-GeV) dark matter evades direct-detection experiments
    - not enough recoil energy

# GeV dark sector

## Motivations

- strong bottom-up reason
  - multiple dark matter candidates
    - most strongly coupled one does not need to be a dominant component
    - evade late-time annihilation constraints from CMB
      - this is not so trivial XENON1T collaboration, PRL, 2019 & 2019
    - e.g., electron and proton from the dark-sector point of view
- dark sector phenomenology
  - in the following, dark matter = lightest stable particle in dark sector
    - lower bound of the coupling to SM from the relic abundance
    - need new experimental strategy (low background)

# Geometric acceptance

## Efficiency factor

$$N_{\text{signal}} \simeq N_{A'} \times \text{Br}(e^+e^-) \times \text{effic.}$$

$$\text{effic.} = \frac{1}{N_{\text{events}}} \int_{z_{\min}}^{z_{\max}} dz \sum_{\substack{\text{events} \\ \in \text{geom.}}} \frac{m}{p_z} \Gamma e^{-z(m/p_z)\Gamma} \quad \frac{p_z}{m} = v_z \gamma$$

- Lorentz boost

- decay position

- events  $\in$  geom. is generically  $z$  and  $p_z$  dependent

- strong dependence in Sea Quest due to KMAG

- if weak dependence

$$\text{effic.} \approx \mathcal{A} \frac{1}{N_{\text{events}}} \sum_{\text{events}} \left( e^{-z_{\min}(m/p_z)\Gamma} - e^{-z_{\max}(m/p_z)\Gamma} \right)$$

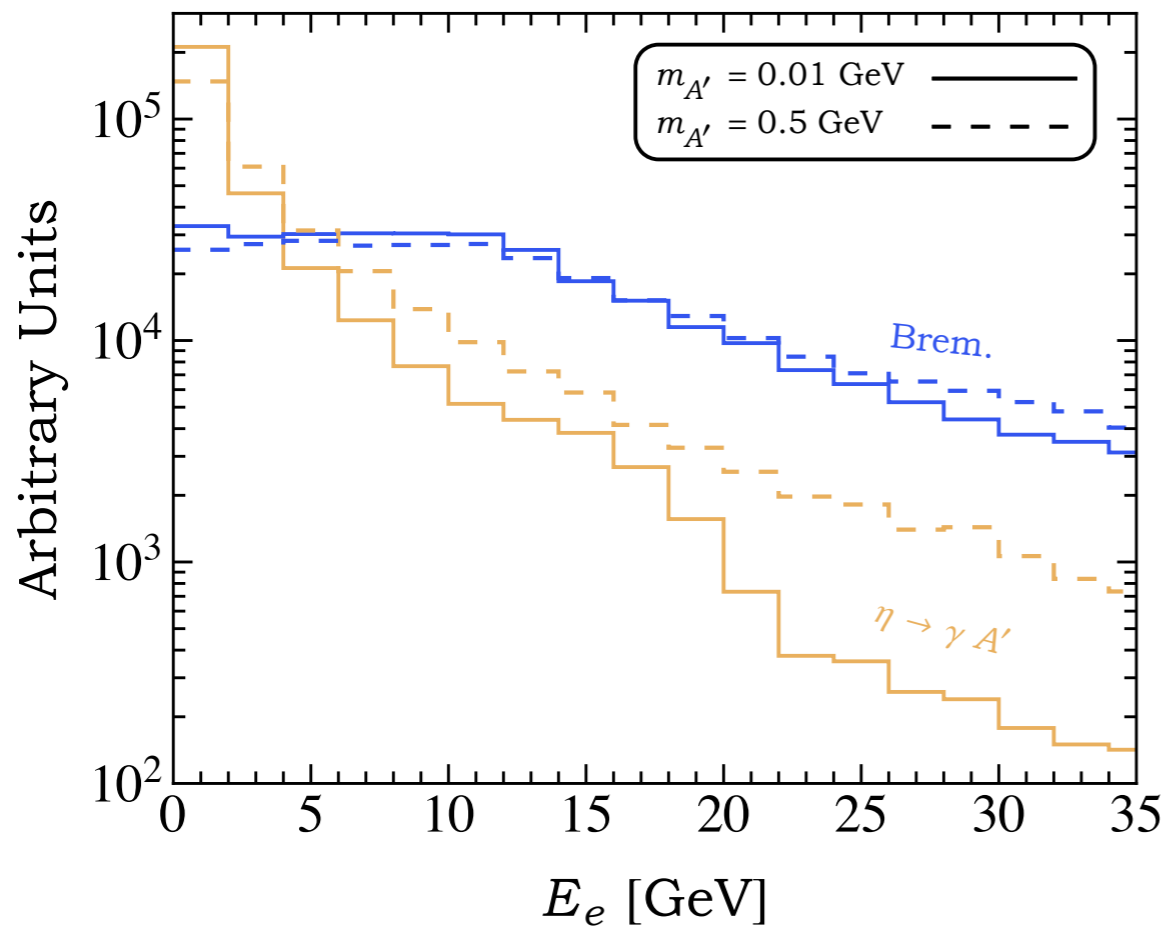
- geometrical acceptance

# Geometric acceptance

## Kinematics@SeaQuest

- minimal model

$$A' \rightarrow e^+ e^-$$

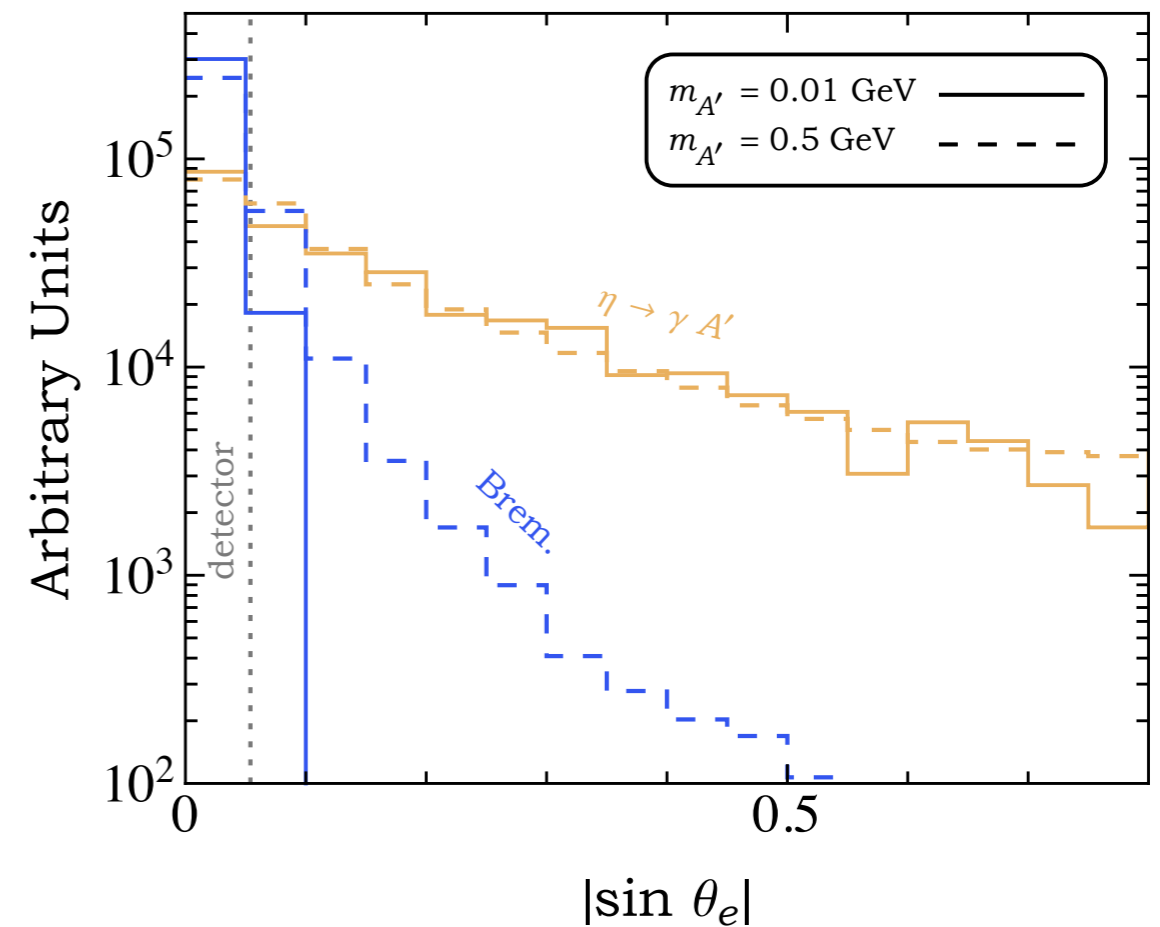


-  $A'$  from Bremsstrahlung is more energetic

-  $\gamma$  takes away energy (smaller impact for heavier  $A'$ )

Berlin, Gori, Schuster, and Toro, PRD, 2018

$$A' \rightarrow e^+ e^-$$



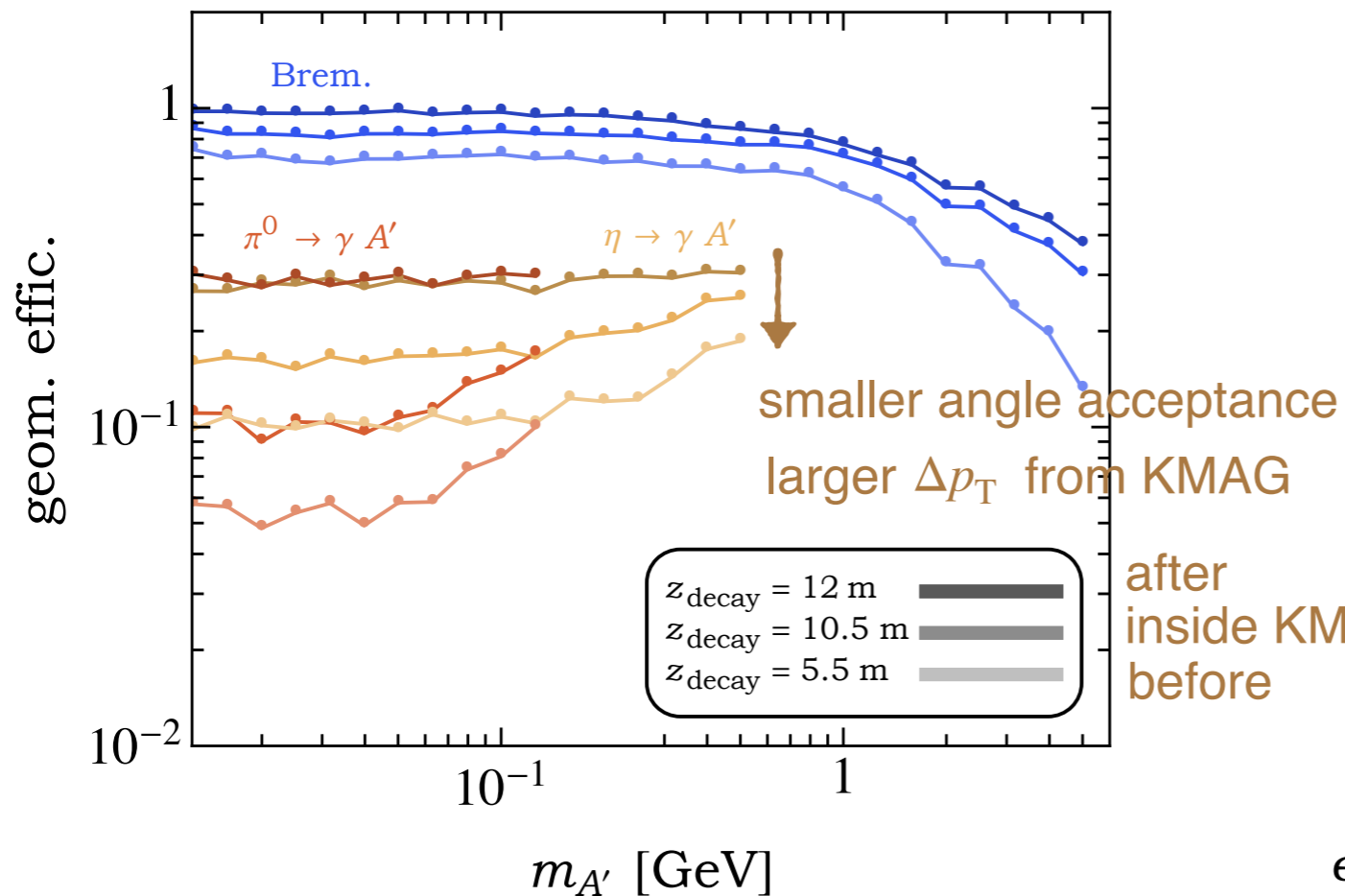
-  $A'$  from Bremsstrahlung is more boosted

- lower collimation for heavier

# Geometric acceptance

## Efficiency factor@SeaQuest

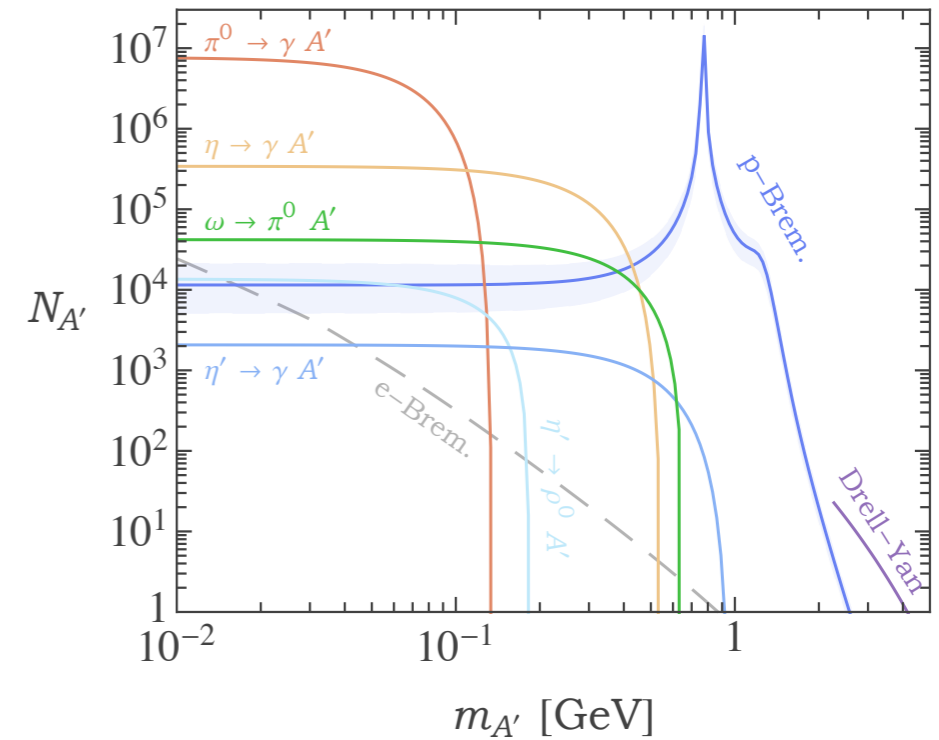
- minimal model  
 $A' \rightarrow e^+ e^-$



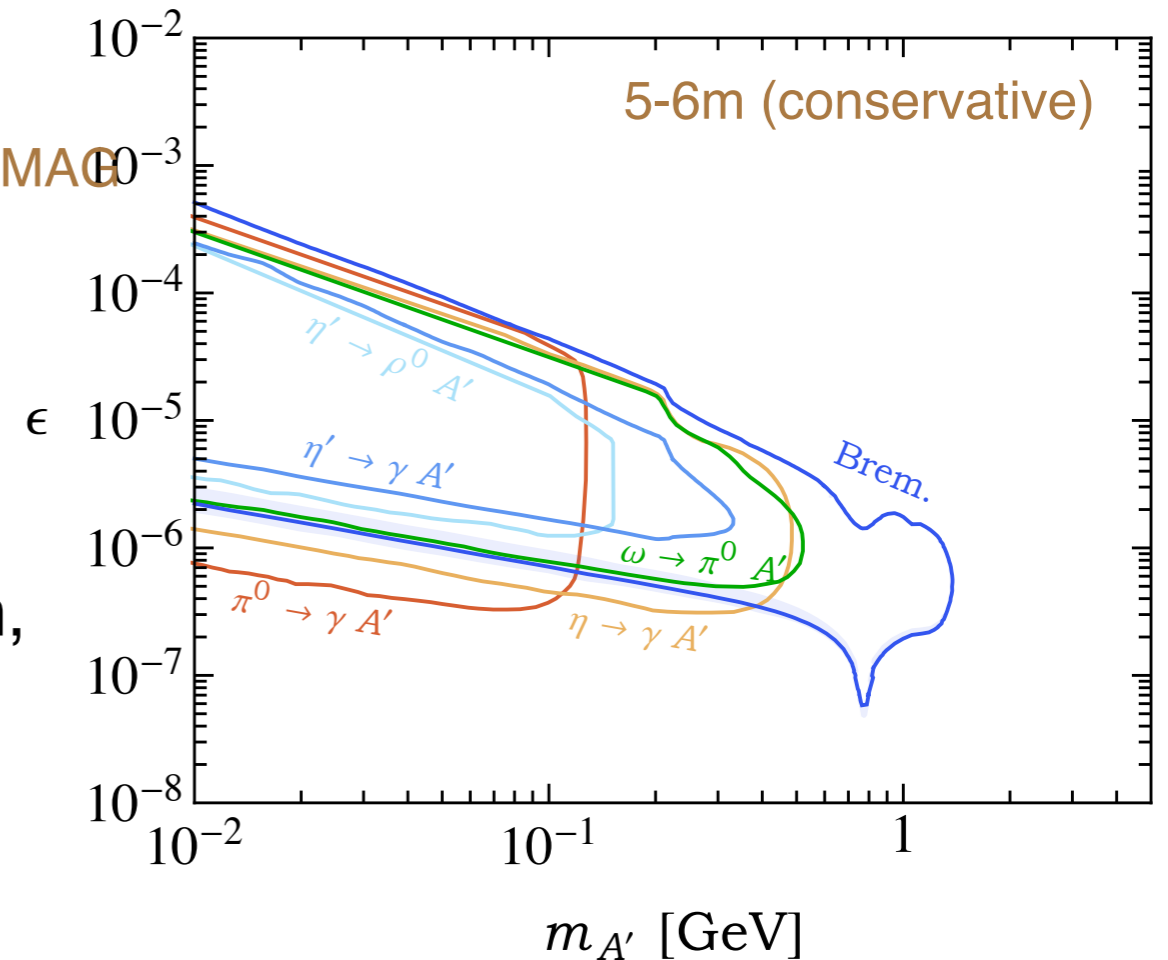
- meson decay is good in production,  
 but bad in detection

Berlin, Gori, Schuster, and Toro, PRD, 2018

$E_{\text{beam}} = 120 \text{ GeV}, 1.44 \times 10^{18} \text{ POT}, \epsilon = 10^{-6}$



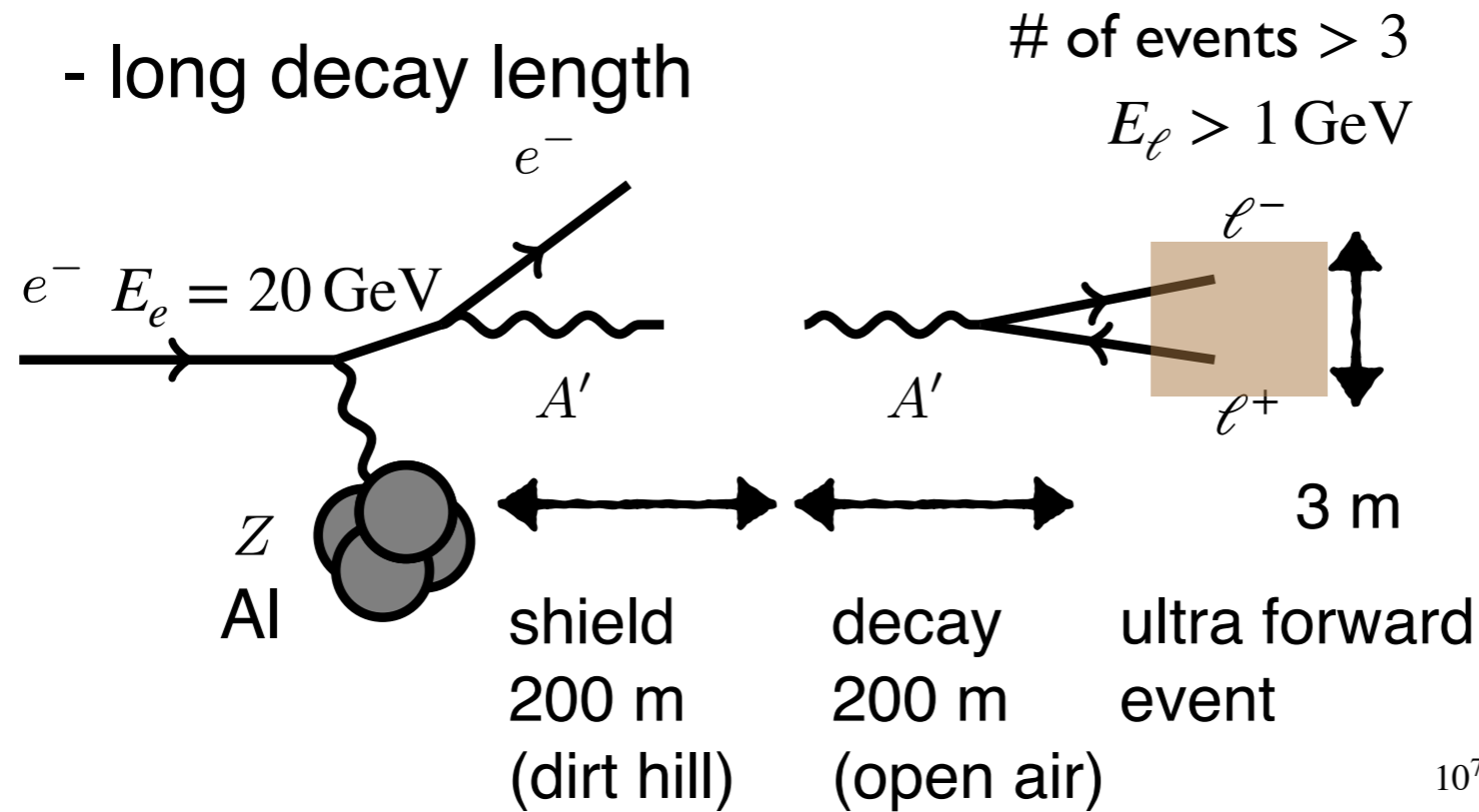
$A' \rightarrow e^+ e^-$



# Electron beam dump

## SLAC E137

- long decay length



- production

- suppressed for  $m_{A'} \gtrsim 2 \text{ GeV}$

