# Revisiting Chiral Magnetic Effects and Axions

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Bonne retraite, Pierre!

#### Introduction

Axion dark matter

#### Detecting axion DM

A new experimental proposal for axion DM

#### Revisiting Chiral Magnetic Effects

Anomaly in Fermi liquid

#### Axion magnetic vortex

Axion electrodynamics Axion magnetic vortex

#### Conclusion

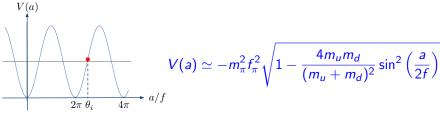
# 1. Introduction

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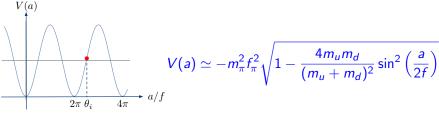
▶ The axion solves the strong CP problem dynamically.



For  $T \ll f$  and  $H \ll m_a$ , the axions are homogeneous and behave collectively as CDM (Preskill+Wise+Wilczek, Abbott+Sikivie, Dine+Fischler 1983):

$$a(t) pprox rac{\sqrt{2
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Axions, coupled to SM particles, live long enough for a large decay constant and may constitue most of DM,  $\rho_a \approx \rho_{\rm DM}$ , (Turner 1986).

$$\Omega_a h^2 \approx 0.23 \times 10^{\pm 0.6} \left( \frac{f}{10^{12} \text{ GeV}} \right)^{1.175} \theta_i^2 F(\theta_i),$$

► In this talk I assume that the (QCD) axions, or possibly ALPs constitute dark matter of our universe, and discuss its detection:

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- Axions are detectable, though not easy, because they couple to SM particles.
- Since Sikivie (1983), many experiments have been proposed and some probe theoretically interesting limits.
- We have proposed a new one, called LACME.
- ▶ It measures CME current in conductors that is directly proportional to electron-axion coupling, sensitive to the UV origin of axions. (DKH+Im+Jeong+Yeom, 2207.06884)

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# 2. Detecting Axions (LACME)

(2207.00997)

# Axion DM couples to electrons

▶ Electrons dominantly couple to  $\dot{a}$ , since  $v_a = |\vec{\nabla} a|/|\dot{a}| \sim 10^{-3}$ :

$$\mathcal{L}_{\mathrm{int}} = C_{\mathrm{e}} rac{\partial_{\mu} a}{f} ar{\psi} \gamma^{\mu} \gamma_{5} \psi pprox C_{\mathrm{e}} rac{\dot{a}}{f} \psi^{\dagger} \gamma_{5} \psi \,.$$

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$$\mu_5 = C_e \frac{\dot{a}}{f} = C_e \frac{\sqrt{2\rho_{\mathrm{DM}}}}{f} \cos{(m_a t)}$$

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- ▶ What does the axial chemical potential  $(\mu_5)$  do to electrons?
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• One can see this, as  $\mu_5$  can be absorbed by the redefining the electron fields,  $\Psi \to \Psi' = e^{-i\mu_5\vec{\Sigma}\cdot\vec{x}/3}\Psi$ :

$$\mathcal{L} = \bar{\Psi} \left( i \partial \!\!\!/ - m + \mu \gamma^0 + \mu_5 \gamma^0 \gamma_5 \right) \Psi$$
  
$$\Rightarrow \bar{\Psi}' \left( i \gamma' \cdot \partial - m + \mu \gamma^0 \right) \Psi'$$

where 
$$\gamma^{\mu\prime}=e^{-i\mu_5ec{f \Sigma}\cdotec{x}}\gamma^\mu e^{i\mu_5ec{f \Sigma}\cdotec{x}}$$
 .

Another way to see this is to take a non-relativistic limit for the electrons by subtracting out its rest mass and integrating out the negative energy states,  $\chi$ :

$$\Psi \equiv \begin{pmatrix} \psi \\ \chi \end{pmatrix} e^{-imt} \quad (\mu_{\mathrm{NR}} \equiv \mu - m)$$

$$\mathcal{L} \Rightarrow \mathcal{L}_{NR} = \psi^{\dagger} \left[ i \partial_0 - \frac{(i \vec{\sigma} \cdot \vec{\nabla} + \mu_5)^2}{2m} \right] \psi + \mu_{NR} \psi^{\dagger} \psi + \cdots$$

 $\blacktriangleright$   $\mu_5$  shifts the momentum along the spin direction:

$$\hat{S}\cdot\vec{p}\rightarrow\hat{S}\cdot\vec{p}+\mu_5$$

- The momentum shift will create an helicity imbalance in polarized medium.
- Under a magnetic field, electrons in the LLL are polarized opposite to the magnetic field:

$$E_n(p_z) = \pm \sqrt{p_z^2 + m^2 + 2|eB|n_z^2}$$

with 
$$2n = 2n_r + 1 + |m_L| - \text{sign}(eB)(m_L + 2s_z)$$

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# chiral magnetic effects in chiral medium

 $\mu_5$  creates an helicity imbalance in medium under magnetic field,  $\vec{B}$ :

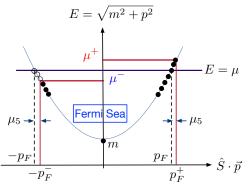


Figure: Polarized medium with  $\mu_5$ .  $(\hat{S} \cdot \vec{p} = -\hat{B} \cdot \vec{p})$ 

### chiral magnetic effects in chiral medium

▶ Helicity imbalance in LLL electrons due to  $\mu_5$ :

$$\Delta 
ho = 
ho_{h=+1/2}^{n=0} - 
ho_{h=-1/2}^{n=0} \simeq rac{|eB|}{2\pi^2} \, \mu_5 v_F \left[ 1 - e^{-(\mu-m)/T} 
ight] \, .$$

CME is a current flow due to the helicity imbalance in (polarized) medium by the axial chemical potential  $\mu_5$  and B

$$\left\langle \vec{j} \right\rangle = v_F \frac{e^2}{2\pi^2} \mu_5 \vec{B}$$
 (For  $T \ll E_F \approx 10 \text{ eV}$ )

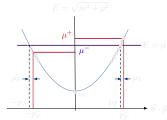


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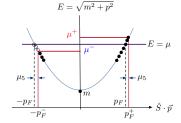


Figure: polarized medium

- Because of the helicity imbalance, there will be a persistent current of electrons along the magnetic field.
- ► Chiral magnetic effect (Fukushima+Kharzeev+Warringa '08)

$$\vec{J} = a\mu_5 \vec{B}$$
 . (a = anomaly coeficient)

- The anomaly  $a = v_F e^2/(2\pi^2)$ . (DKH+Im+Jeong+Yeom '22)
- Since axion DM provides  $\mu_5$ , one can detect axions by measuring CME currents (LACME)!

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We propose a new experiment to detect this non-dissipative currents in conductors (DKH+Jeong+Im+Yeom '22):

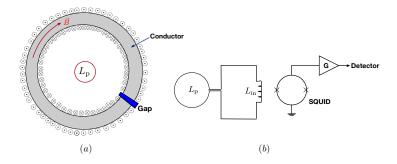


Figure: LACME

Inside the solenoid the axion DM induce both the vacuum current and the CME current:

$$\vec{j} = \left[ \frac{C_{a\gamma\gamma} + 4v_F C_e \frac{\mu_m}{\mu_0}}{\mu_0} \right] \frac{\alpha}{2\pi f} \vec{B} \sqrt{2\rho_{\rm DM}} \cos(m_a t) ,$$

- For a material with large permeability like ferromagnetic conductors,  $\mu_m/\mu_0 \gtrsim v_F^{-1} \approx 10^2$ , the CME current can be dominant.
- ▶ For  $B = 10\,\mathrm{T}$  and  $\rho_a \approx \rho_{\mathrm{DM}}$ , the CME current

$$j^3 = 6.8 \times 10^{-13} \text{Am}^{-2} \left( \frac{v_F}{0.01c} \right) \cdot \left( \frac{10^{12} \text{ GeV}}{f/C_e} \right) \cdot \left( \frac{\mu_m}{100\mu_0} \right)$$

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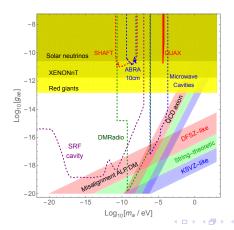
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# Axionic Chiral Magnetic Effects

Projection of LACME from existing axion haloscopes, assuming  $v_F = 0.01, \mu_m \approx 10^2 \mu_0 \ (g_{ae} = 2C_e m_e/f)$ :



# Axion-electron coupling

- ▶ The axion-electron coupling depends on the UV model.
- ► The strength of the axion-electron coupling varies as (See e.g 2106.05816 by Choi+Im+Seong)

$$C_e \simeq egin{cases} \mathcal{O}(1) & ext{DFSZ-like models} \ \mathcal{O}(10^{-4} \sim 10^{-3}) & ext{KSVZ-like models} \ \mathcal{O}(10^{-3} \sim 10^{-2}) & ext{String-theoretic axions} \end{cases}$$

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# 3. Revisiting Chiral Magnetic Effects

(2207.00997 and to appear)

- ► The salient feature of Fermi liquid is the existence of gapless modes, the fluctuations near the Fermi surface:
- Consider a cold medium of (free) electrons.

$$\mathcal{L} = \bar{\psi} \left( i \partial \!\!\!/ - m + \mu \gamma^0 \right) \psi$$
 
$$\downarrow \!\!\!\downarrow$$
 
$$E = -\mu + \sqrt{m^2 + \vec{p}^2}$$

 $\simeq \vec{v}_F \cdot (\vec{p} - \vec{p}_F)$ .

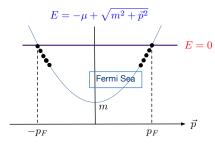


Figure: normal medium

- ► The Fermi liquid is naturally chiral in a sense that a gauge-invariant gap does not exist.
- ▶ We decompose the fermion fields as following (DKH 1998)

$$\psi = \psi_+ + \psi_- \quad ext{with} \quad \psi_\pm = rac{1 \pm ec{lpha} \cdot \hat{oldsymbol{v}}_F}{2} \psi \, ,$$

where  $\psi_+$  describes the modes in the Fermi sea at low energy while  $\psi_-$  the modes in the Dirac Sea. ( $E=-\mu\pm\sqrt{p^2+m^2}$ .)

► The Dirac mass term does not open a gap at the FS. It is a part of the chemical potential:

$$m\bar{\psi}\psi = m\left(\bar{\psi}_{+}\psi_{-} + \bar{\psi}_{-}\psi_{+}\right) = \frac{m^{2}}{2\mu}\bar{\psi}_{+}\gamma^{0}\psi_{+} + \cdots$$

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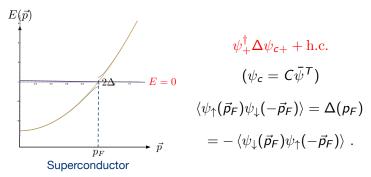
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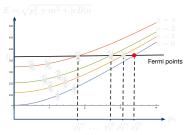
$$m\bar{\psi}\psi = m(\bar{\psi}_{+}\psi_{-} + \bar{\psi}_{-}\psi_{+}) = \frac{m^{2}}{2\mu}\bar{\psi}_{+}\gamma^{0}\psi_{+} + \cdots$$

The only gap that regulates the IR divergence is the Majorana mass term that breaks gauge symmetry as in superconductor:



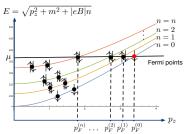
It also breaks the helicity symmetry just like the mass regulator breaks chirality in vacuum.

- ► Fermi liquid is gapless and consists of two chiral modes. It therefore may have axial anomaly (Coleman+Grossman 1982).
- Under a magnetic field, electrons fill Landau levels:



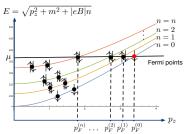
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➤ To calculate the ABJ anomaly in Fermi liquid we consider the anomalous two-point function of LLL electrons in medium, which are 2-dimensional:

$$\Gamma_5^{\mu\nu}(q_1)\delta^{(2)}(q_1+q_2) \equiv \int \Pi_i \mathrm{d}^2 x_i e^{iq_i\cdot x_i} \langle 0| \, \mathrm{T} j^{\mu}(x_1) j_5^{\nu}(x_2) \, |0\rangle \; .$$

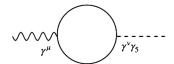


Figure: ABJ anomaly by LLL in Fermi Liquid

▶ For  $q/\mu \to 0$  (Manuel '96: DKH '98), using  $j_5^\nu = \epsilon^{\nu\alpha} j_\alpha$ , the anomalous two-point function of LLL becomes

$$\Gamma_5^{\mu\nu}(q) = \frac{eB}{2\pi^2 v_F} \left[ -\eta^{\mu 0} \epsilon^{\nu 0} + \frac{q^0}{2} \left( \frac{V^\mu \epsilon^{\nu \alpha} V_\alpha}{V \cdot q} + \frac{\bar{V}^\mu \epsilon^{\nu \alpha} \bar{V}_\alpha}{\bar{V} \cdot q} \right) \right] \,,$$

where  $V^{\mu}=(1,0,0,v_F)$  and  $\bar{V}^{\mu}=(1,0,0,-v_F)$ .

▶ The vector current is conserved:

$$q_{\mu}\Gamma_{5}^{\mu\nu}(q)=0$$
.

► The axial current is however anomalous:

$$\langle \partial_
u j_5^
u 
angle_A = ie \int rac{\mathrm{d}^2 q}{4\pi^2} \lim_{q_2 o 0} \lim_{q_2 o 0} e^{iq \cdot x} q_
u A_\mu(q) \Gamma_5^{\mu
u}(q) = rac{e^2 B}{4\pi^2} rac{\mathsf{v}_{ extsf{F}} \epsilon^{\mu
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The ABJ anomaly becomes in the rest frame of the medium

$$\langle \partial_{\nu} j_5^{\nu} \rangle_A = rac{e^2}{16\pi^2} v_{F} \epsilon^{\mu \nu 
ho \sigma} F_{\mu \nu} F_{
ho \sigma} \, .$$

From the anomalous two-point function one can calculate the CME, in the leading order in  $\mu_5$ .

$$\left\langle j^{3} \right
angle = -e\mu_{5} \lim_{q_{0} \to 0} \lim_{q_{3} \to 0} \Gamma_{5}^{30}(q) = \frac{e^{2}B}{2\pi^{2}} v_{F} \mu_{5}.$$

which agrees with our helicity imbalance calculations

▶ The original formula of FKW (2008) missed the factor  $v_F$  for the massive fermions. (DKH+Im+Jeong+Yeom 2022)

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▶ The original formula of FKW (2008) missed the factor  $v_F$  for the massive fermions. (DKH+Im+Jeong+Yeom 2022)

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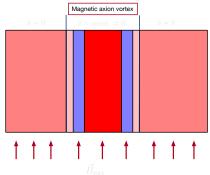
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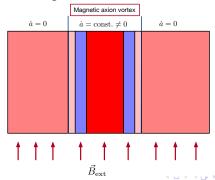
# 3. Magnetic Axion Vortex

with S. Lonsdale (2404.00997)

- Axion electrodynamics admits a stable vortex solution, carrying a constant magnetic flux, in the medium of homogeneous axions with a constant à.
- Under an external magnetic field, an axion vortex forms



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$$\vec{\nabla} \cdot \vec{E} = 0 \,, \quad \vec{\nabla} \times \vec{B} - \frac{\partial}{\partial t} \vec{E} = -g_{a\gamma} \dot{a} \vec{B} \,,$$

- In axion electrodynamics, the magnetic field sources itself producing a current  $\vec{J} = -m\vec{B}$  with  $m = g_{a\gamma}\dot{a}$  even in the absence of charged particles.
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- ▶ When *à* is almost constant, there should exist a topological soliton carrying a finite magnetic flux.
- We therefore ask how the magnetic fields along the vortex should be distributed to minimize its energy for a given magnetic flux, which is topologically conserved.
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▶ The energy for the static magnetic field with  $\vec{J} = -m\vec{B}$  :

$$\mathcal{E} = \int \mathrm{d}^3x \left\{ \frac{1}{2} \vec{B}^2 - \vec{A} \cdot \vec{J} \right\} = \int \mathrm{d}^3x \left\{ \frac{1}{2} \left( \vec{B} + m \vec{A} \right)^2 - \frac{1}{2} m^2 \vec{A}^2 \right\}$$

The minimum energy saturates by configurations that satisfy  $\vec{B} = -m\vec{A}$  in the Coulomb gauge or the Maxwell equation:

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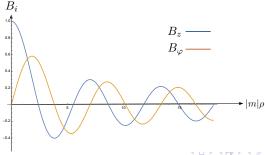
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The minimum energy configuration for a given flux Φ is with the normalization,  $\mathcal{N}=2\pi\int_0^{x_c}xJ_0(x)\mathrm{d}x$ ,

$$B_{\varphi}(\rho) = -m|m|\frac{\Phi}{\mathcal{N}}J_1(|m|\rho), \ B_z(\rho) = m^2\frac{\Phi}{\mathcal{N}}J_0(|m|\rho).$$



- ▶ Consider small fluctuations,  $a_0 + \delta a$ , to study its stability.
- ► For the normal modes inside the magnetic axion vortex

$$\delta a = \theta(t) f(|m|\rho) .$$

Fluctuations induce electric fields from the Faraday's law:

$$E_{z}(\rho) = g_{a\gamma} \delta \ddot{a} \frac{\Phi}{N} \left[ J_{0}(|m|\rho) - |m|\rho J_{1}(|m|\rho) \right],$$
  
$$E_{\varphi}(\rho) = -g_{a\gamma} \delta \ddot{a} \frac{\Phi}{N} m\rho J_{0}(|m|\rho).$$

And it creates axion source that renormalizes the kinetic term

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The S-wave normal modes,  $\delta a = \theta(t)R(|m|\rho)$ , then satisfy after rescaling  $|m|\rho$  to be  $\rho$ ,

$$-\nabla^2 f(\rho) - \frac{\omega^2}{m^2} H(\rho) R(\rho) = -\lambda R(\rho),$$

where 
$$\omega^2=-\ddot{\theta}/\theta$$
,  $\lambda=m_a^2/m^2$ ,  $H=1+g_{a\gamma}^2\,m^2\left(\frac{\Phi}{N}J_0(\rho)\right)^2$ .

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► Axion spectrum inside vortex is that of Schrödinger equation

$$V(\rho) = -\frac{\omega^2}{m^2} H(\rho; m, \Phi)$$

$$-\lambda = -\frac{m_a^2}{m^2}$$

$$V(0) = -\frac{\omega^2}{m^2} H(0; m, \Phi)$$

▶ As an illustration we plot a few low-lying states:

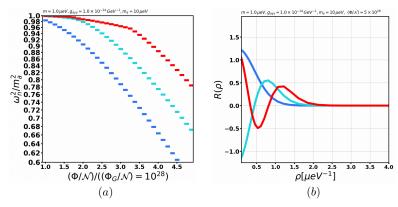


Figure:  $m=1\mu {\rm eV}$ ,  $g_{a\gamma}=10^{-14}\,{\rm GeV}^{-1}$  and  $m_a=10\mu {\rm eV}$ 

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Since the axions decay into photons, however, the magnetic axion vortex will decay into photons eventually.

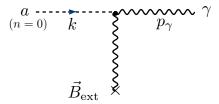


Figure: The ground state axion decays into a single photon.

## Axion magnetic vortex

For the ground state axions,

$$\delta a_{0k_z0} = \sin(\omega_0 t - k_z z) R_{0k_z0}(\rho) = \int \frac{d^2 k_{\perp}}{(2\pi)^2} C_{k_z}(\vec{k}_{\perp}) e^{i(\omega_0 t - k_z z - \vec{k}_{\perp} \cdot \vec{x}_{\perp})},$$

the decay rate becomes at the leading order

$$\Gamma = g_{a\gamma}^2 \omega_0(k_z) \left(\frac{\Phi}{N}\right)^2 |m|^3 \int_{|m|} \frac{d^2 k_{\perp}}{(2\pi)^2} \frac{|C_{k_z}(\vec{k}_{\perp})|^2}{\sqrt{k_{\perp}^2 - |m|^2}}.$$

► The size of the vortex is of galactic scale:

$$m^{-1} = 250 \, \mathrm{pc} \cdot \left( \frac{10^{-14} \, \mathrm{GeV}^{-1}}{g_{a\gamma}} \right) \cdot \left( \frac{\sqrt{0.8 \, \mathrm{GeV cm}^{-3}}}{\dot{a}_0} \right) \, .$$

➤ The magnetic fields are ubiquitous in our universe. At the center of the vortex, along the vortex,

$$B_z(0) = m^2 \frac{\Phi}{N} = 10 \,\mu\,\mathrm{G}\left(\frac{\Phi/N}{10^{44}}\right) \cdot \left(\frac{m}{10^{-35} \mathrm{GeV}}\right)^2$$

The decay rate of the ground state axions

$$\Gamma pprox rac{\pi}{2} g_{a\gamma} B_z(0) = 1.7 \sec^{-1} \left( rac{g_{a\gamma}}{\mathrm{GeV}^{-1}} 
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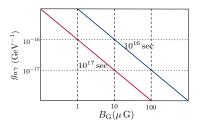


Figure: The lifetime of axions as a function of the magnetic field,  $B_G$ , at the center of the vortex and the axion-photon coupling,  $g_{a\gamma}$ .

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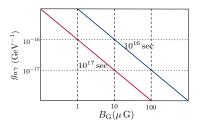


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$$\vec{J} = \frac{e^2}{2\pi^2} \mathbf{v_F} \mu_5 \vec{B} ,.$$

 Using CME, we propose a new experiment to detect the dark matter axions or ALP. (LACME)

$$j^3 = 6.8 \times 10^{-13} \mathrm{Am}^{-2} \left( \frac{v_F \mu_m}{c \mu_0} \right) \left( \frac{\rho_{\mathrm{DM}}}{0.4 \, \mathrm{GeV cm}^{-3}} \right)^{1/2} \left( \frac{10^{12} \, \mathrm{GeV}}{f / C_e} \right) \left( \frac{B}{10 \, \mathrm{Tesla}} \right)$$

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# Thank you for listening!

# Merci, Pierre!