

PYTHIA WEEK 2024, OXFORD - 2nd MAY 2024

MINNLO_{PS} (& PYTHIA)

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University of Oxford

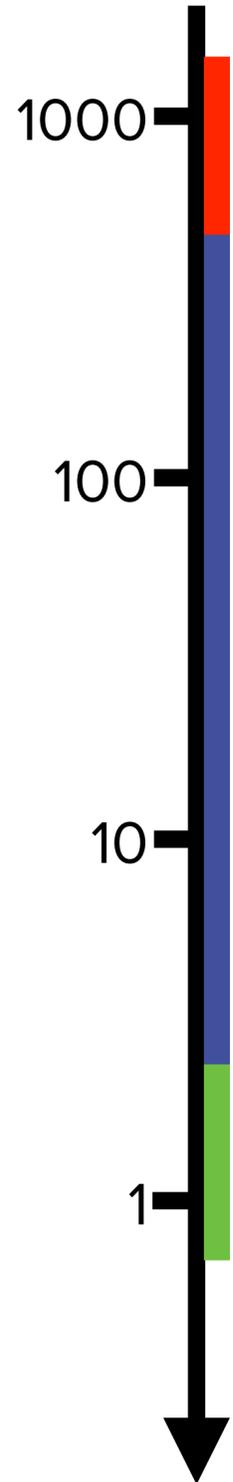


UNIVERSITY OF
OXFORD

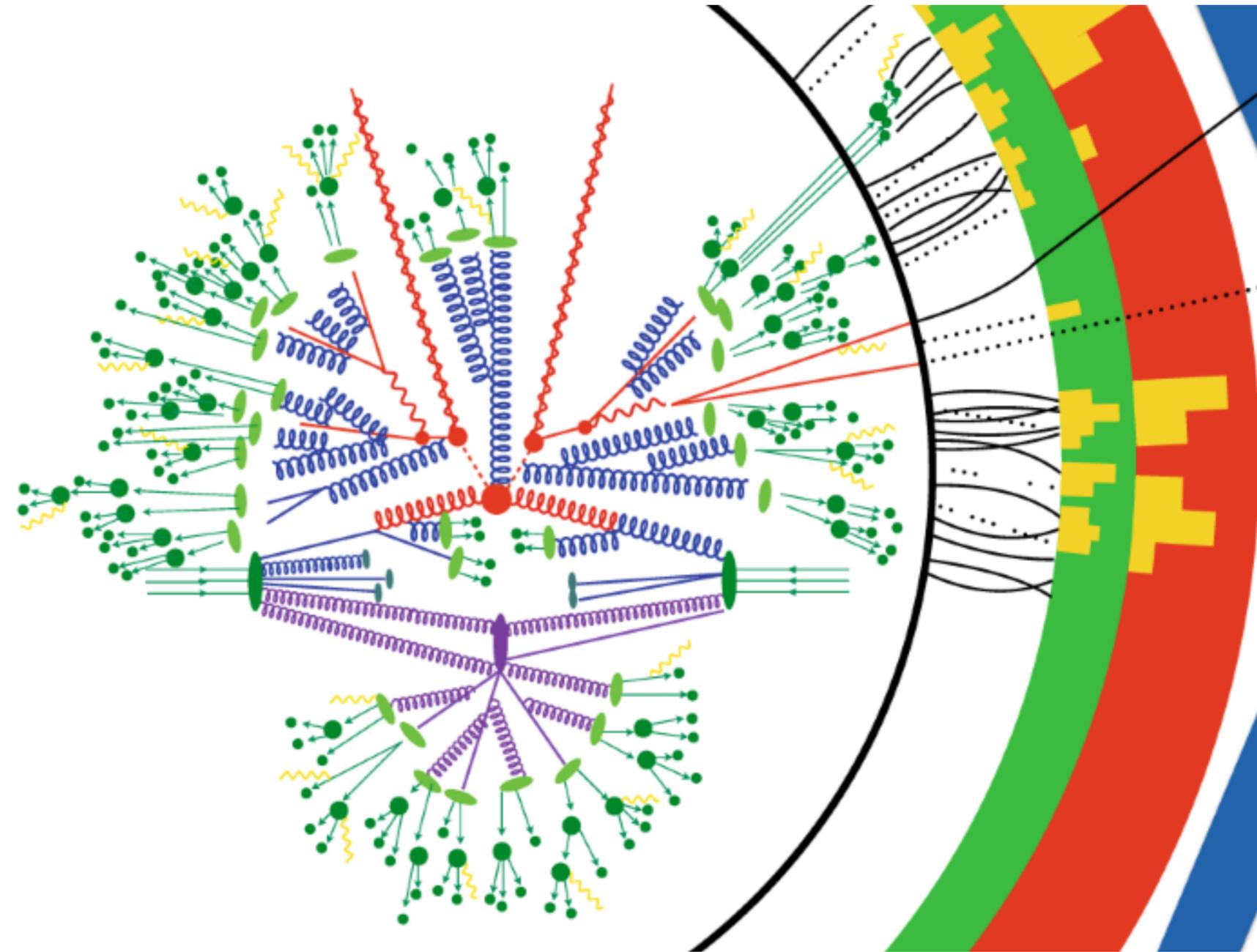
1. THE PROBLEM

LHC EVENT

ENERGY
SCALE [GeV]

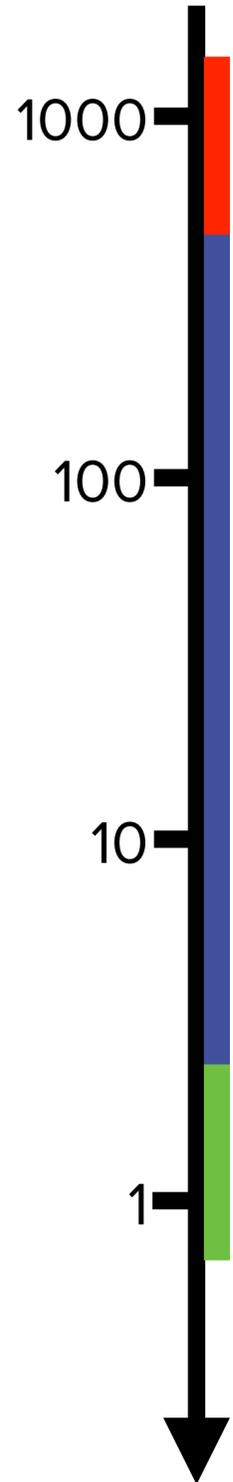


- 1. HARD SCATTERING
- 2. PARTON SHOWER
- 3. HADRONIZATION
- 4. UNDERLYING EVENT

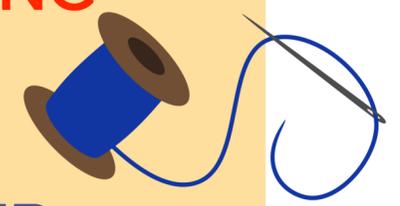


LHC EVENT

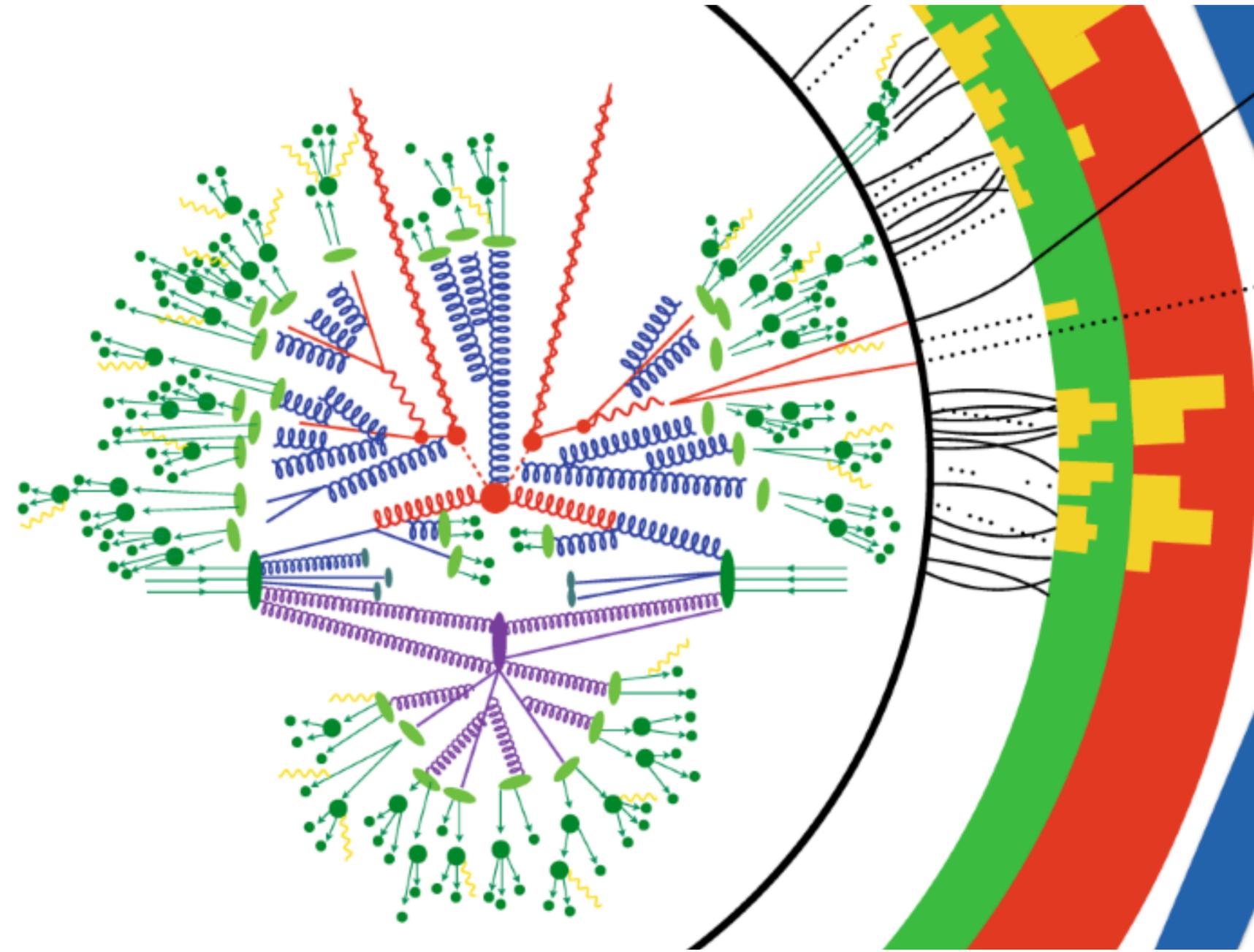
ENERGY
SCALE [GeV]



- 1. HARD SCATTERING
- 2. PARTON SHOWER



- 3. HADRONIZATION
- 4. UNDERLYING EVENT

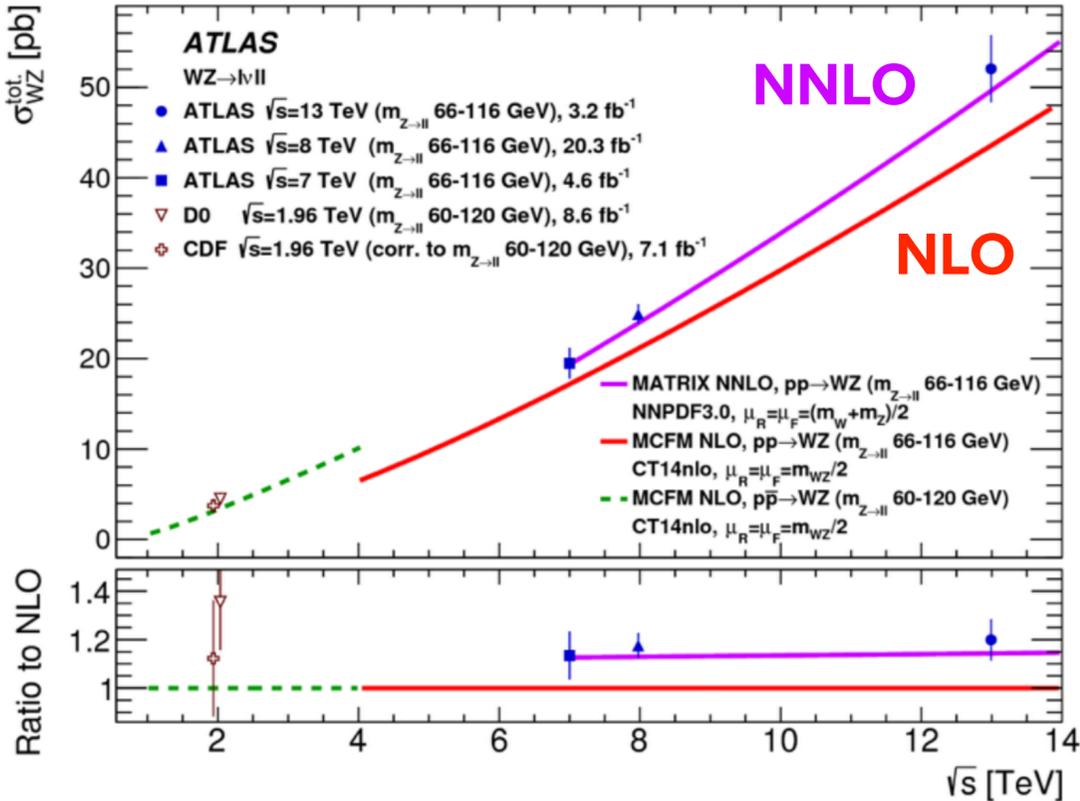


HARD SCATTERING

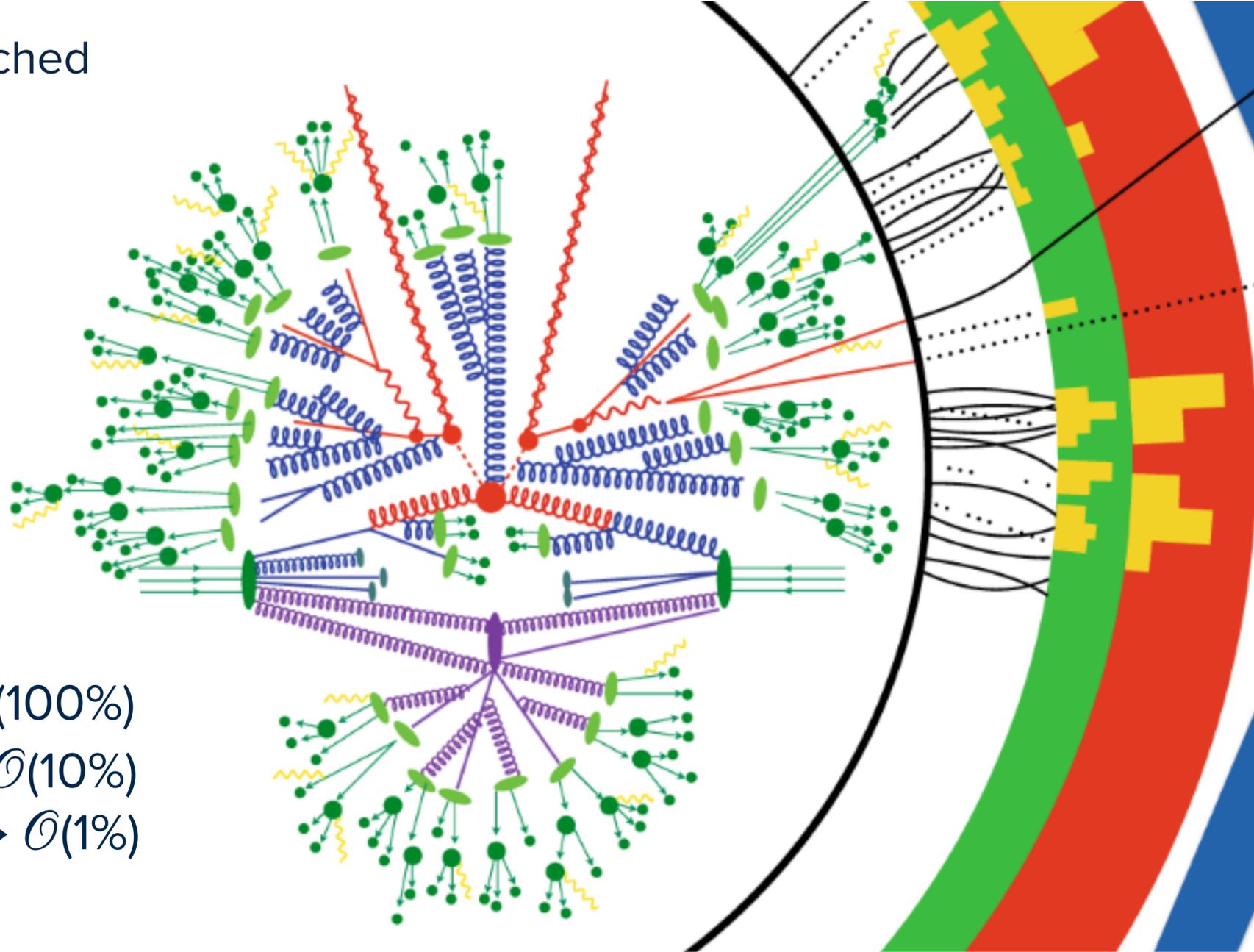
$$\mu \sim Q \gg \Lambda_{QCD}$$

Studied with fixed-order calculations. Precision is reached through perturbation theory:

$$\sigma = \sigma_{LO}(1 + \alpha_s \delta_{NLO} + \alpha_s^2 \delta_{NNLO} + \mathcal{O}(\alpha_s^3))$$



LO → $\mathcal{O}(100\%)$
 NLO → $\mathcal{O}(10\%)$
 NNLO → $\mathcal{O}(1\%)$



PARTON SHOWER

$$\Lambda_{QCD} < \mu < Q$$

Cascade of particles from the high-energy limit to the detector level. It is constructed starting from the factorization of QCD amplitudes in the infra-red limit:

$$|M_{n+1}|^2 \rightarrow |M_n|^2 \cdot K$$

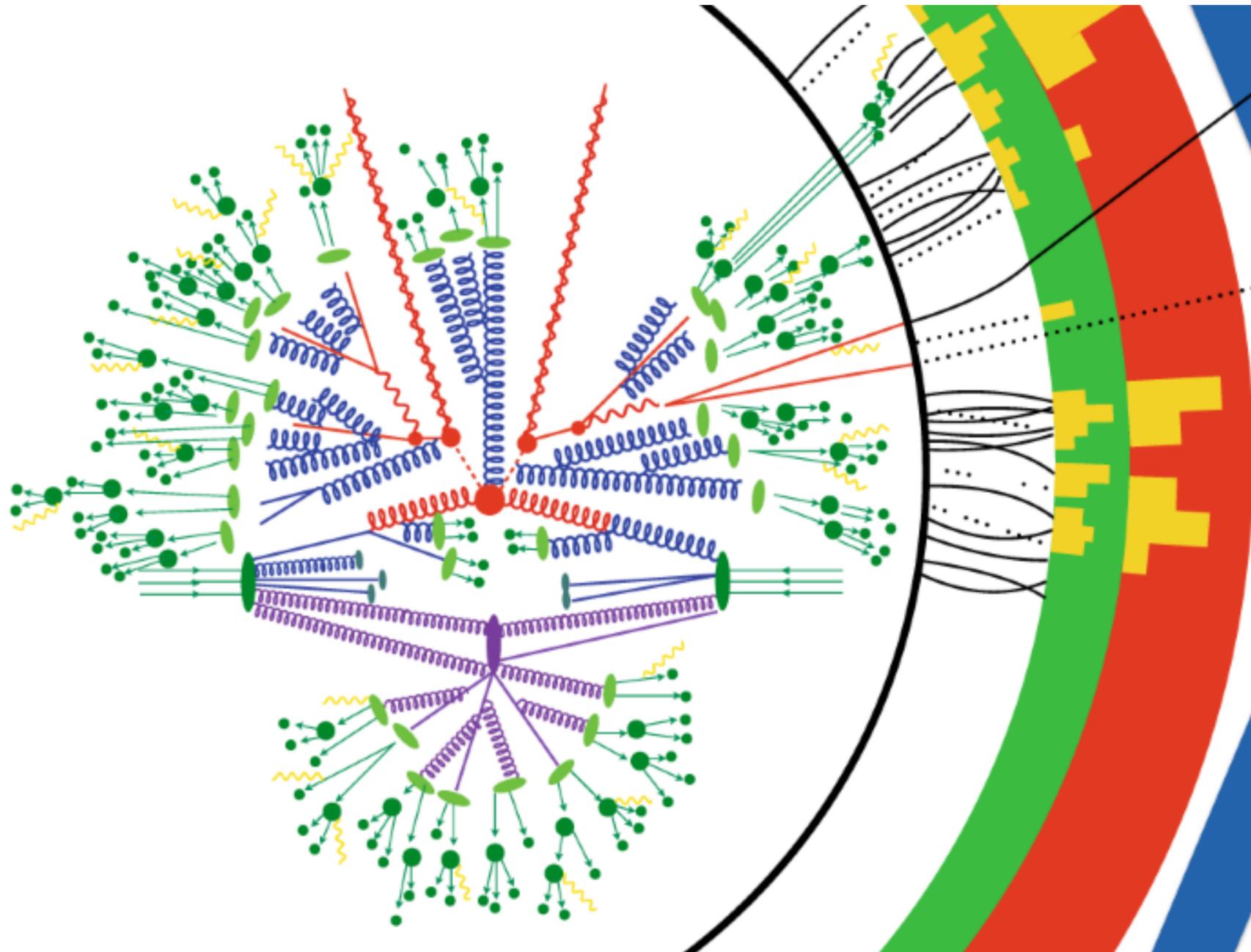
For a specific observable (e.g. event-shape V):

$$\Sigma(V < e^{-|L|}) = \exp(\underbrace{Lg_1(\alpha_s L)}_{\text{LL}} + \underbrace{g_2(\alpha_s L)}_{\text{NLL}} + \alpha_s \underbrace{g_3(\alpha_s L)}_{\text{NNLL}} + \dots)$$

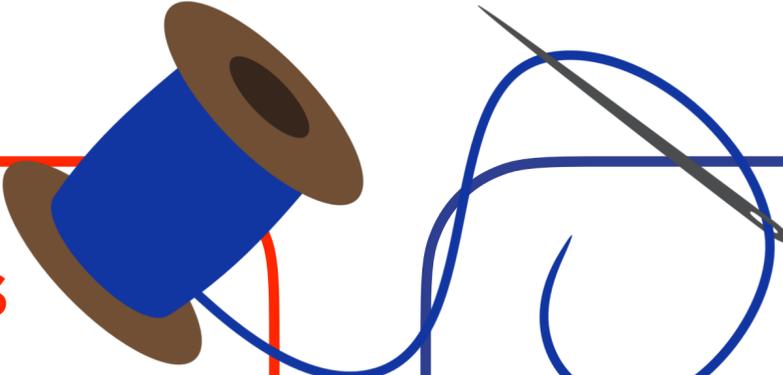
Most showers are only LL accurate.



Lots of progress done in recent years to improve the accuracy of parton showers (**NLL showers are available**). However, LHC phenomenology is not possible with these new tools yet.



MATCHING



FIXED-ORDER CALCULATIONS

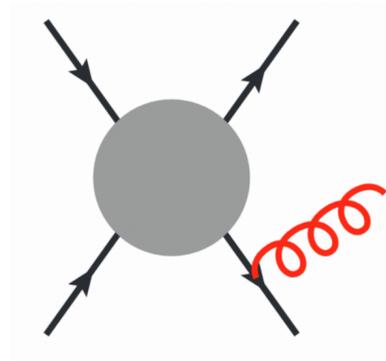
- ✓ Systematically improvable accuracy.
State of the art: NNLO.
- ✗ Not realistic (few final state particles, not suitable for exclusive observables).

PARTON SHOWER

- ✓ Realistic final states.
Flexible in MC codes.
- ✗ Low accuracy, usually only LL.

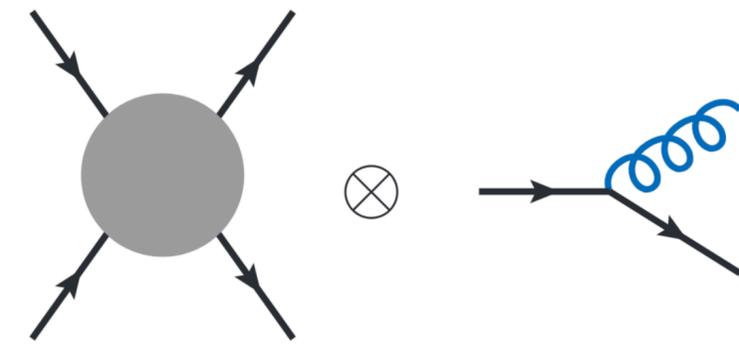
WHAT'S THE PROBLEM?

FIXED-ORDER CALCULATIONS



Correct real emission

PARTON SHOWER



Approximate real emission

!! DOUBLE COUNTING !!

2. THE SOLUTION

THE POWHEG METHOD

[Nason '04; Frixione, Nason, Oleari '07; Alioli, Nason, Oleari, Re '10]

Master Formula

$$d\sigma_{\text{pwg}} = d\Phi_F \bar{B}(\Phi_F) \left\{ \Delta_{\text{pwg}}(\Lambda_{\text{pwg}}) + \int d\Phi_{\text{rad}} \Delta_{\text{pwg}}(p_{T,\text{rad}}) \frac{R(\Phi_F, \Phi_{\text{rad}})}{B(\Phi_F)} \right\}$$

NLO NORMALIZATION (= xs)

$$\bar{B}(\Phi_F) = B(\Phi_F) + V(\Phi_F) + \int d\Phi_{\text{rad}} [R(\Phi_{FJ}) - C(\Phi_{FJ})]$$

FIRST (= hardest) EMISSION
obtained with the correct matrix element R/B

$$\Delta(p_T) = \exp \left\{ - \int d\Phi'_{\text{rad}} \frac{R(\Phi_F, \Phi'_{\text{rad}})}{B(\Phi_F)} \Theta(p'_T - p_T) \right\}$$

When using a p_T -ordered shower (most common option, like PYTHIA), we apply a p_T veto: all the emissions produced by the shower must be softer than the first emission produced by POWHEG.

THE POWHEG METHOD

[Nason '04; Frixione, Nason, Oleari '07; Alioli, Nason, Oleari, Re '10]

Master Formula

$$d\sigma_{\text{pwg}} = d\Phi_F \bar{B}(\Phi_F) \left\{ \Delta_{\text{pwg}}(\Lambda_{\text{pwg}}) + \int d\Phi_{\text{rad}} \Delta_{\text{pwg}}(p_{T,\text{rad}}) \frac{R(\Phi_F, \Phi_{\text{rad}})}{B(\Phi_F)} \right\}$$

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When using a p_T -ordered shower (most common option, like PYTHIA), we apply a p_T veto: all the emissions produced by the shower must be softer than the first emission produced by POWHEG.

NLO+PS ACCURACY

THE MINNLO_{PS} METHOD

[Monni, Nason, Re, Wiesemann, Zanderighi '19]

Master Formula

$$d\sigma_F^{\text{MiNNLO}_{\text{PS}}} = d\Phi_{\text{FJ}} \bar{B}^{\text{MiNNLO}_{\text{PS}}}(\Phi_{\text{FJ}}) \left\{ \Delta_{\text{pwg}}(\Lambda_{\text{pwg}}) + \int d\Phi_{\text{rad}} \Delta_{\text{pwg}}(p_{\text{T,rad}}) \frac{R(\Phi_{\text{FJ}}, \Phi_{\text{rad}})}{B(\Phi_{\text{FJ}})} \right\}$$

NNLO NORMALIZATION (= xs)

**SECOND EMISSION
obtained à la POWHEG**

$$\bar{B}^{\text{MiNNLO}_{\text{PS}}}(\Phi_{\text{FJ}}) =$$

THE MINNLO_{PS} METHOD

[Monni, Nason, Re, Wiesemann, Zanderighi '19]

Master Formula

$$d\sigma_F^{\text{MiNNLO}_{\text{PS}}} = d\Phi_{\text{FJ}} \bar{B}^{\text{MiNNLO}_{\text{PS}}}(\Phi_{\text{FJ}}) \left\{ \Delta_{\text{pwg}}(\Lambda_{\text{pwg}}) + \int d\Phi_{\text{rad}} \Delta_{\text{pwg}}(p_{\text{T,rad}}) \frac{R(\Phi_{\text{FJ}}, \Phi_{\text{rad}})}{B(\Phi_{\text{FJ}})} \right\}$$

SECOND EMISSION
obtained à la POWHEG

NNLO NORMALIZATION (= xs)

$$\bar{B}^{\text{MiNNLO}_{\text{PS}}}(\Phi_{\text{FJ}}) = \left(B(\Phi_{\text{FJ}}) + V(\Phi_{\text{FJ}}) + \int d\Phi_{\text{rad}} R(\Phi_{\text{FJ}}, \Phi_{\text{rad}}) \right)$$

Born contribution
that already has
an emission J

Virtual+Real correction
on F+J



DIVERGENT

THE MINNLO_{PS} METHOD

[Monni, Nason, Re, Wiesemann, Zanderighi '19]

Master Formula

$$d\sigma_F^{\text{MiNNLO}_{\text{PS}}} = d\Phi_{\text{FJ}} \bar{\mathbf{B}}^{\text{MiNNLO}_{\text{PS}}}(\Phi_{\text{FJ}}) \left\{ \Delta_{\text{pwg}}(\Lambda_{\text{pwg}}) + \int d\Phi_{\text{rad}} \Delta_{\text{pwg}}(p_{\text{T,rad}}) \frac{\mathbf{R}(\Phi_{\text{FJ}}, \Phi_{\text{rad}})}{\mathbf{B}(\Phi_{\text{FJ}})} \right\}$$

SECOND EMISSION
obtained à la POWHEG

NNLO NORMALIZATION (= xs)

$$\bar{\mathbf{B}}^{\text{MiNNLO}_{\text{PS}}}(\Phi_{\text{FJ}}) = e^{-\tilde{\mathbf{S}}(p_{\text{T}})} \left(\mathbf{B}(\Phi_{\text{FJ}}) (1 + \alpha_s \tilde{\mathbf{S}}^{(1)}) + \mathbf{V}(\Phi_{\text{FJ}}) + \int d\Phi_{\text{rad}} \mathbf{R}(\Phi_{\text{FJJ}}) \right)$$

Appropriate
Sudakov form factor

$$\tilde{\mathbf{S}}(p_{\text{T}}) = \int_{p_{\text{T}}^2}^{Q^2} \frac{dq^2}{q^2} \left[A \log \frac{Q^2}{q^2} + B \right]$$

Born contribution
that already has
an emission J

 ~~DIVERGENT~~

Virtual+Real correction
on F+J

Correct NLO on F+J

THE MINNLO_{PS} METHOD

[Monni, Nason, Re, Wiesemann, Zanderighi '19]

Master Formula

$$d\sigma_F^{\text{MiNNLO}_{\text{PS}}} = d\Phi_{\text{FJ}} \bar{\mathbf{B}}^{\text{MiNNLO}_{\text{PS}}}(\Phi_{\text{FJ}}) \left\{ \Delta_{\text{pwg}}(\Lambda_{\text{pwg}}) + \int d\Phi_{\text{rad}} \Delta_{\text{pwg}}(p_{\text{T,rad}}) \frac{\mathbf{R}(\Phi_{\text{FJ}}, \Phi_{\text{rad}})}{\mathbf{B}(\Phi_{\text{FJ}})} \right\}$$

SECOND EMISSION
obtained à la POWHEG

NNLO NORMALIZATION (= xs)

$$\bar{\mathbf{B}}^{\text{MiNNLO}_{\text{PS}}}(\Phi_{\text{FJ}}) = e^{-\tilde{\mathcal{S}}(p_{\text{T}})} \left(\mathbf{B}(\Phi_{\text{FJ}}) (1 + \alpha_s \tilde{\mathcal{S}}^{(1)}) + \mathbf{V}(\Phi_{\text{FJ}}) + \int d\Phi_{\text{rad}} \mathbf{R}(\Phi_{\text{FJJ}}) + (D(p_{\text{T}}) - \alpha_s D^{(1)}(p_{\text{T}}) - \alpha_s^2 D^{(2)}(p_{\text{T}})) \mathcal{F} \right)$$

Appropriate
Sudakov form factor

$$\tilde{\mathcal{S}}(p_{\text{T}}) = \int_{p_{\text{T}}^2}^{Q^2} \frac{dq^2}{q^2} \left[A \log \frac{Q^2}{q^2} + B \right]$$

Born contribution
that already has
an emission J



~~DIVERGENT~~

Virtual+Real correction
on F+J

Correct NLO on F+J

α_s^3 correction needed
for NNLO normalization

spreading
 $\Phi_{\text{F}} \rightarrow \Phi_{\text{FJ}}$

THE MINNLO_{PS} METHOD

- Starting equation from p_T -resummation:

$$\frac{d\sigma}{d\Phi_F dp_T} = \frac{d\sigma^{\text{sing}}}{d\Phi_F dp_T} + R(p_T) = \frac{d}{dp_T} \left\{ e^{-\tilde{S}(p_T)} \mathcal{L}(p_T) \right\} + R(p_T) = e^{-\tilde{S}(p_T)} \left[D(p_T) + \frac{R(p_T)}{e^{-\tilde{S}(p_T)}} \right]$$

$$D(p_T) \equiv -\frac{d\tilde{S}(p_T)}{dp_T} \mathcal{L}(p_T) + \frac{d\mathcal{L} p_T}{p_T}$$

- Combine with FJ fixed-order $d\sigma_{\text{FJ}}$:

$$d\sigma_F = d\sigma_F^{\text{sing}} + [d\sigma_{\text{FJ}}]_{\text{f.o.}} - [d\sigma_F^{\text{sing}}]_{\text{f.o.}}$$

$$\bar{B}^{\text{MINNLO}_{\text{PS}}}(\Phi_{\text{FJ}}) = e^{-\tilde{S}(p_T)} \left(B(\Phi_{\text{FJ}})(1 + \alpha_s \tilde{S}^{(1)}) + V(\Phi_{\text{FJ}}) + \int d\Phi_{\text{rad}} R(\Phi_{\text{FJJ}}) + (D(p_T) - \alpha_s D^{(1)}(p_T) - \alpha_s^2 D^{(2)}(p_T)) \mathcal{F} \right)$$

THE MINNLO_{PS} METHOD

- Starting equation from p_T -resummation:

$$\frac{d\sigma}{d\Phi_F dp_T} = \frac{d\sigma^{\text{sing}}}{d\Phi_F dp_T} + R(p_T) = \frac{d}{dp_T} \left\{ e^{-\tilde{S}(p_T)} \mathcal{L}(p_T) \right\} + R(p_T) = e^{-\tilde{S}(p_T)} \left[D(p_T) + \frac{R(p_T)}{e^{-\tilde{S}(p_T)}} \right]$$

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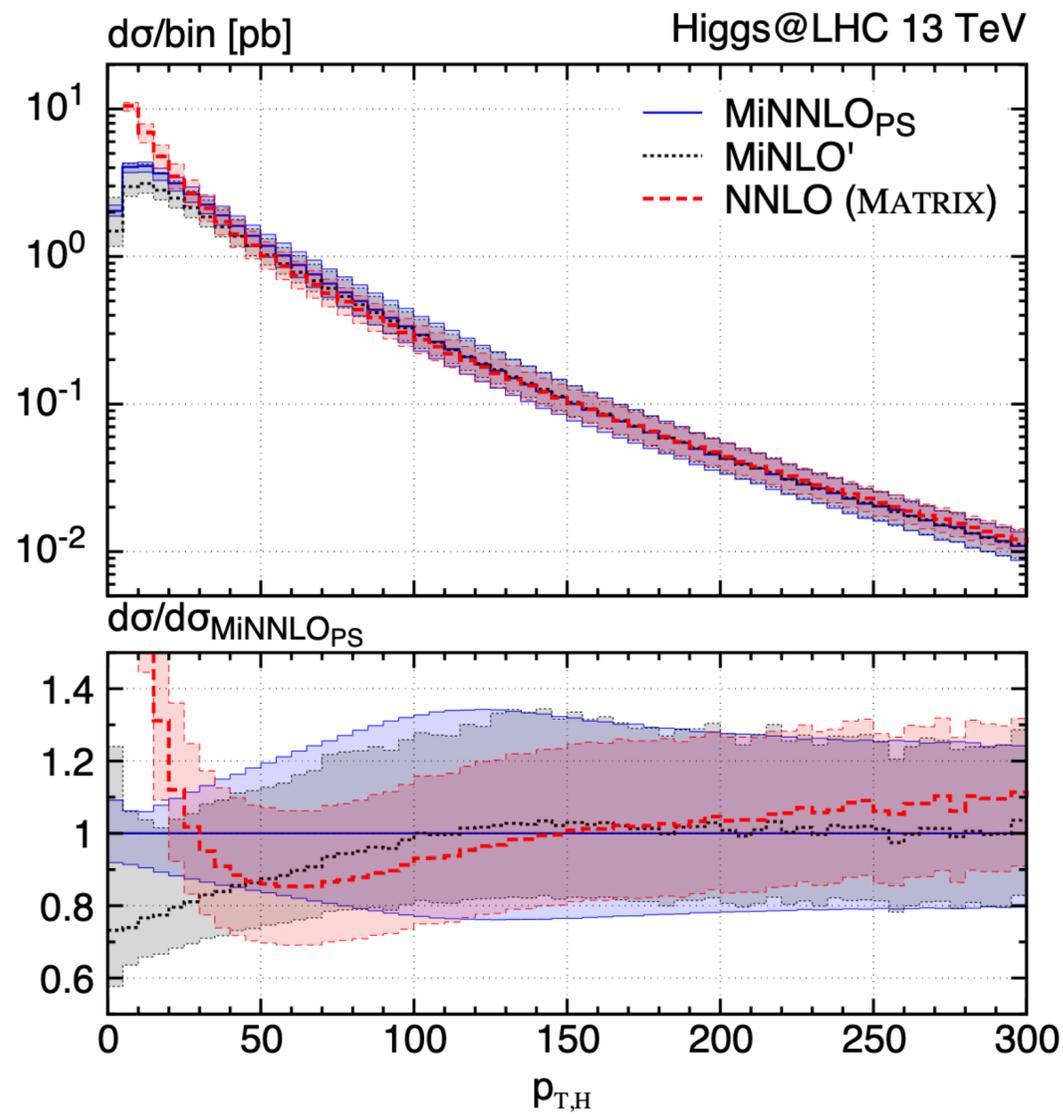
NNLO+PS ACCURACY

3. WHAT CAN WE DO WITH MINNLO_{PS}?

2 → 1 PROCESSES

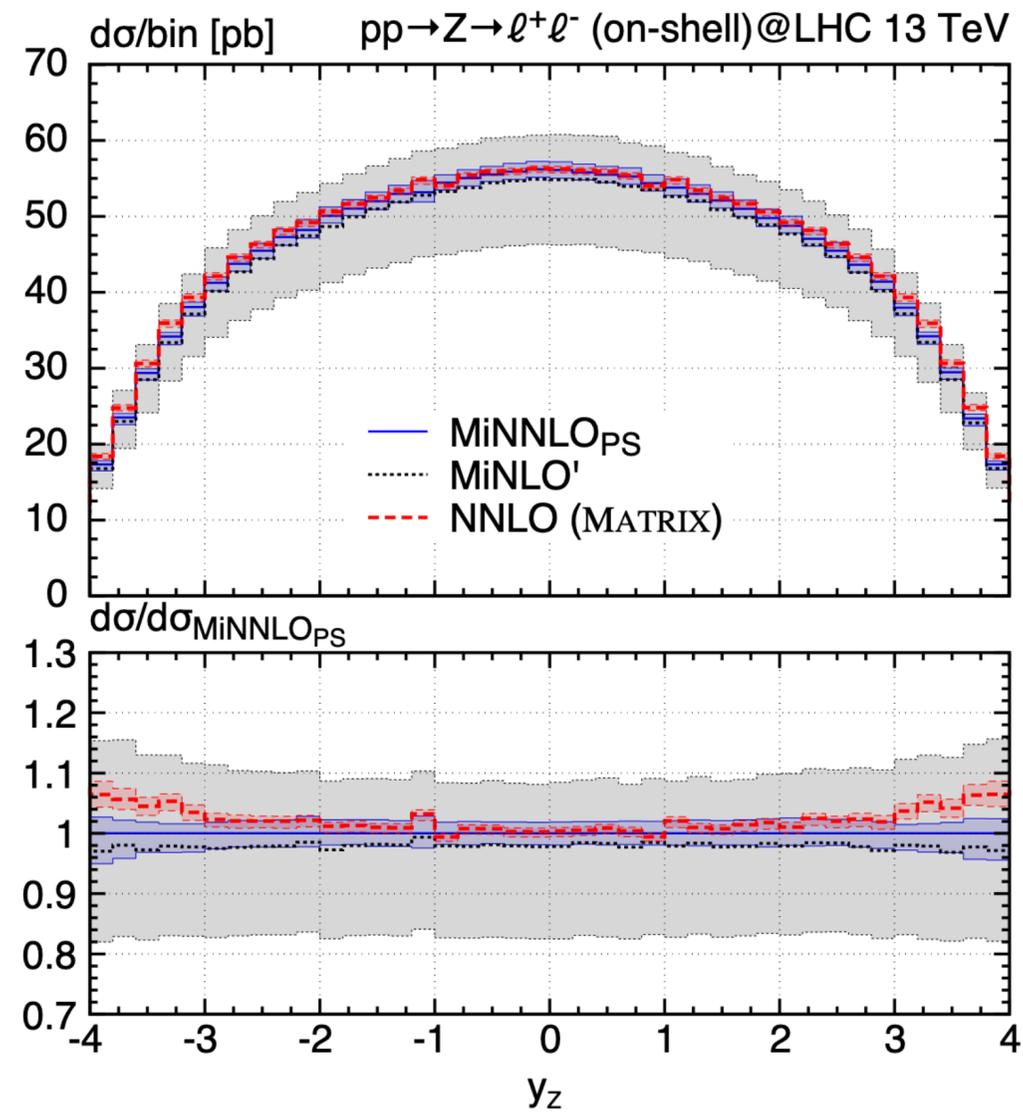
H production

[1908.06987]



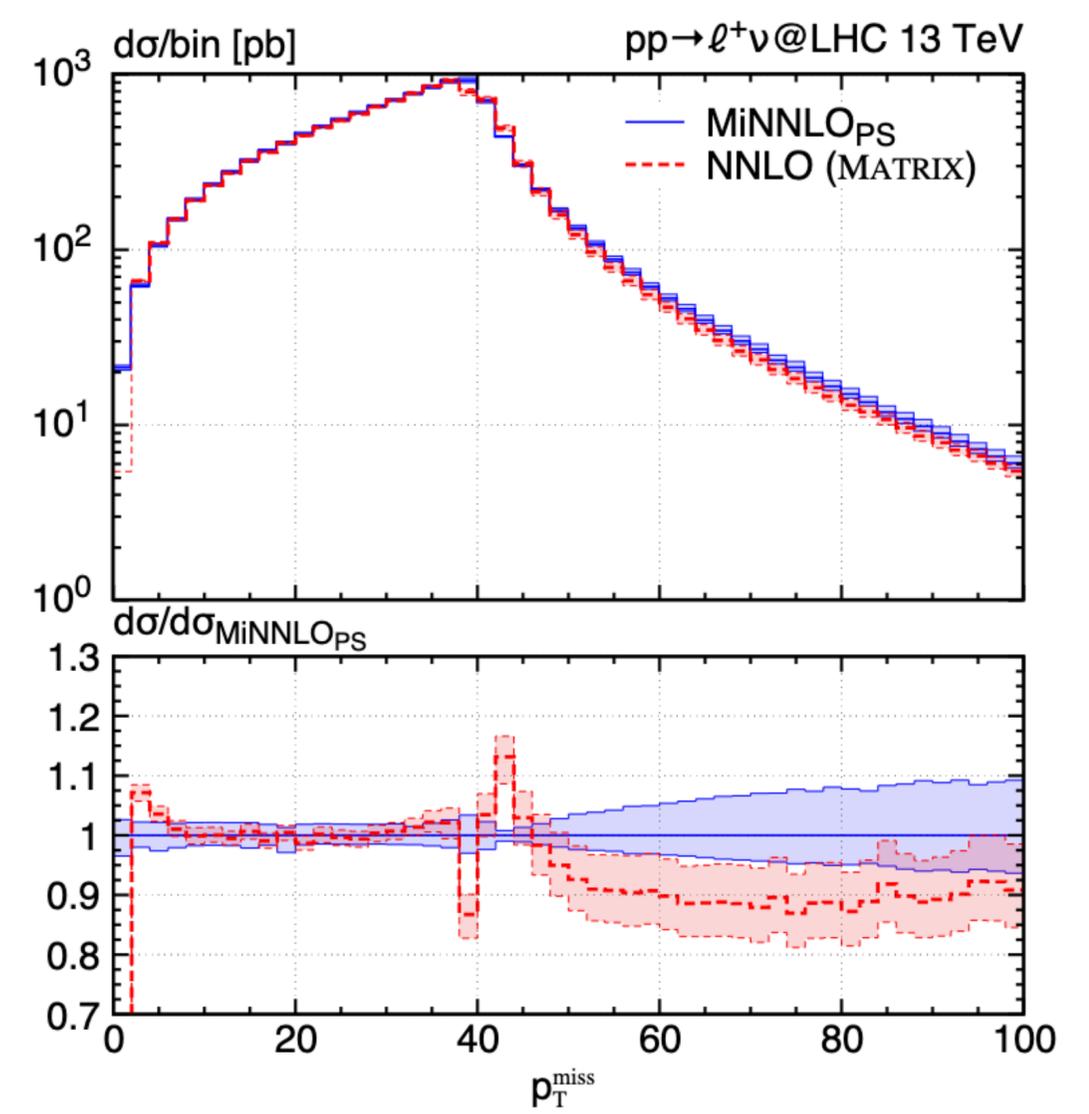
Z production

[1908.06987]



W production

[2006.04133]



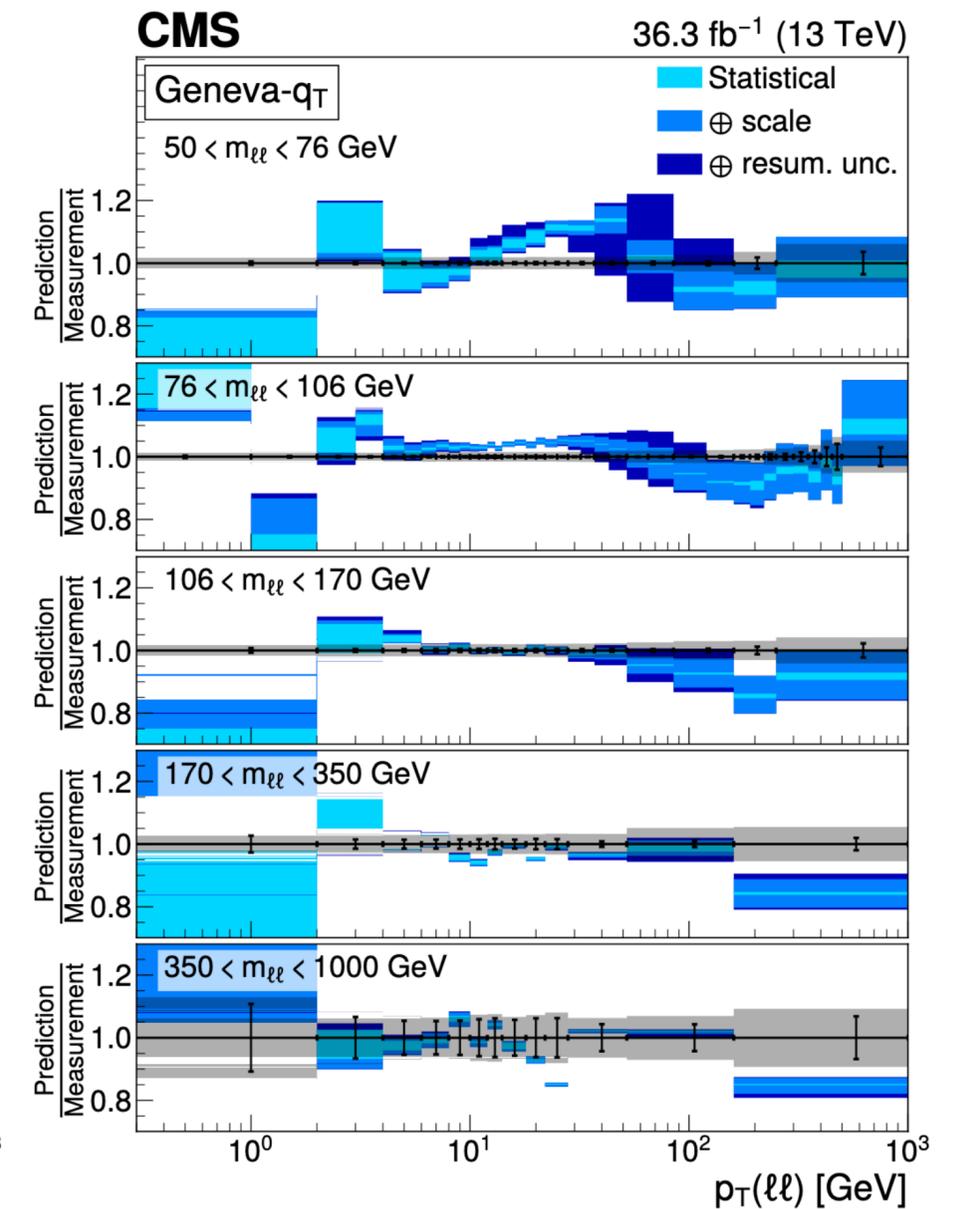
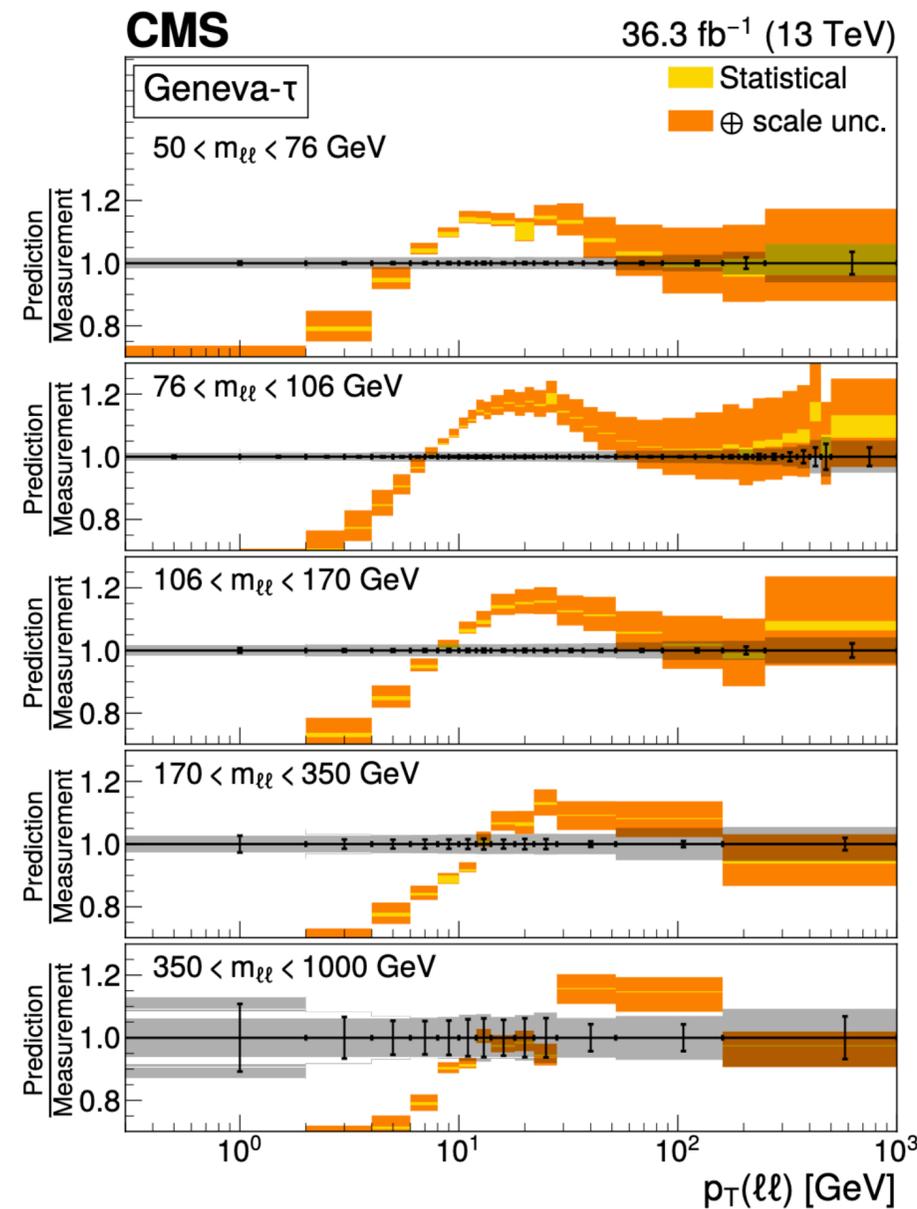
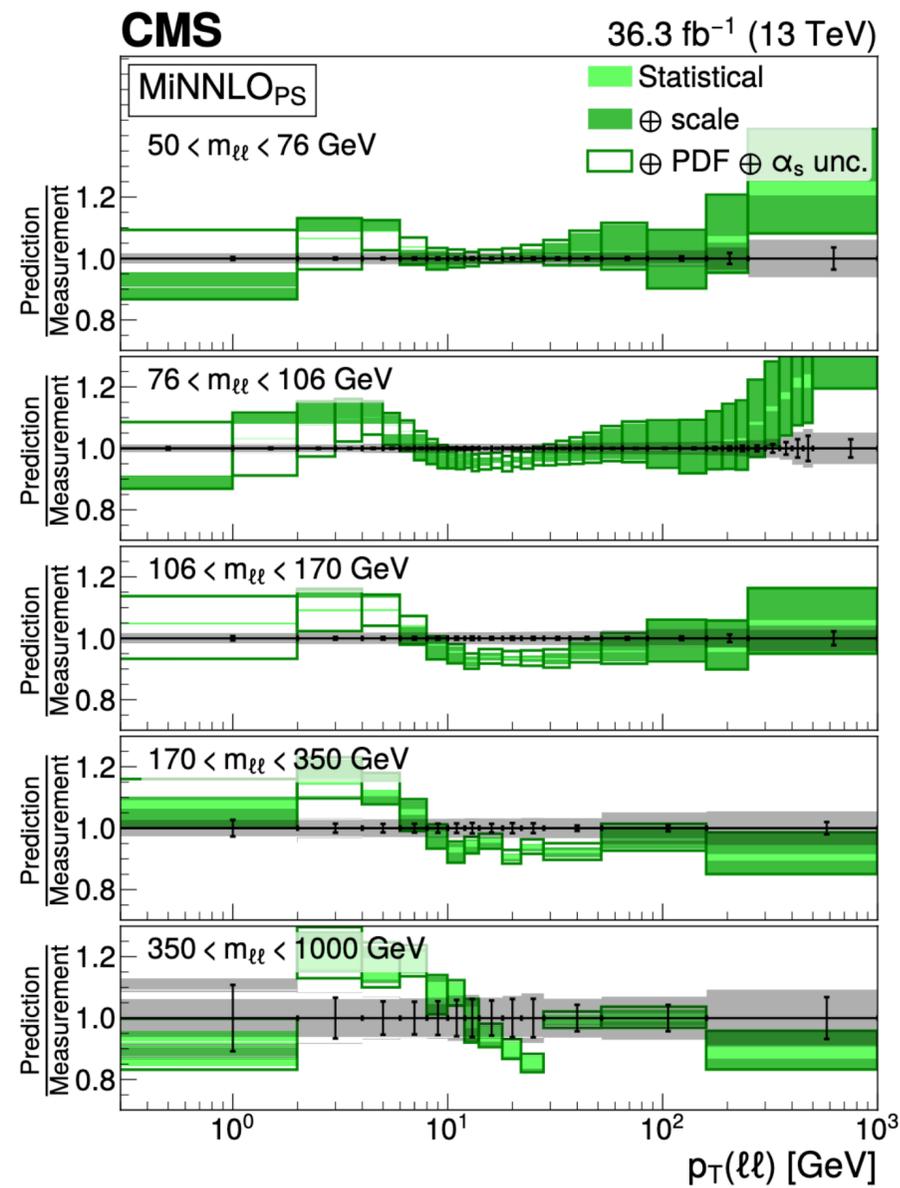
DY: COMPARISON TO DATA

[CMS 2205.04897]

MINNLO_{PS}

GENEVA

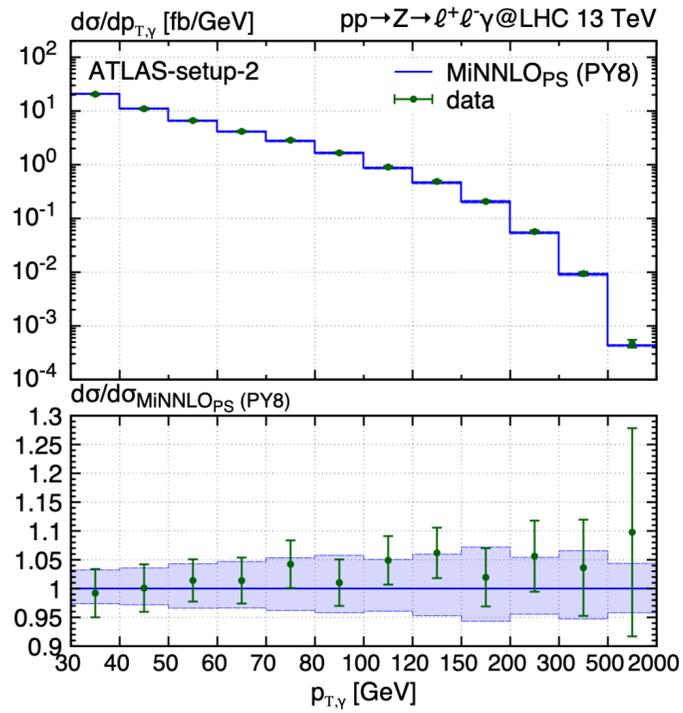
GENEVA-q_T



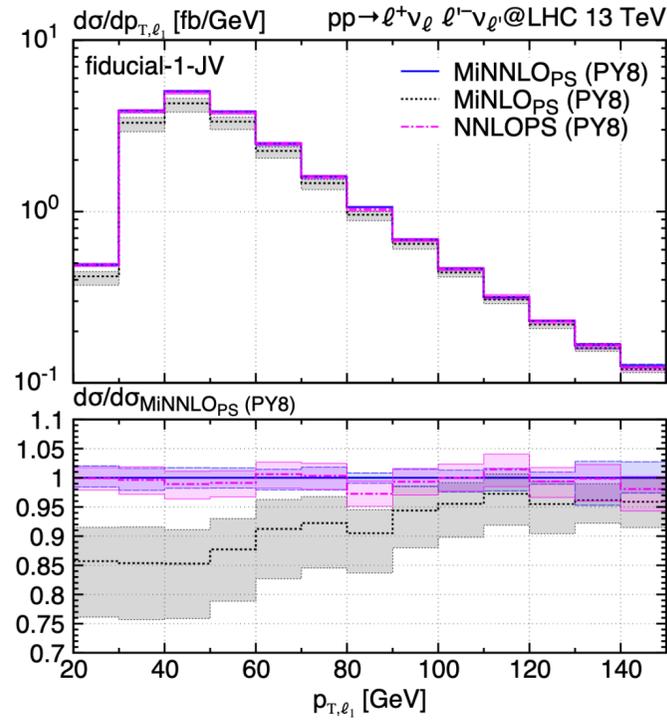
2 → 2 PROCESSES

<https://powhegbox.mib.infn.it/>

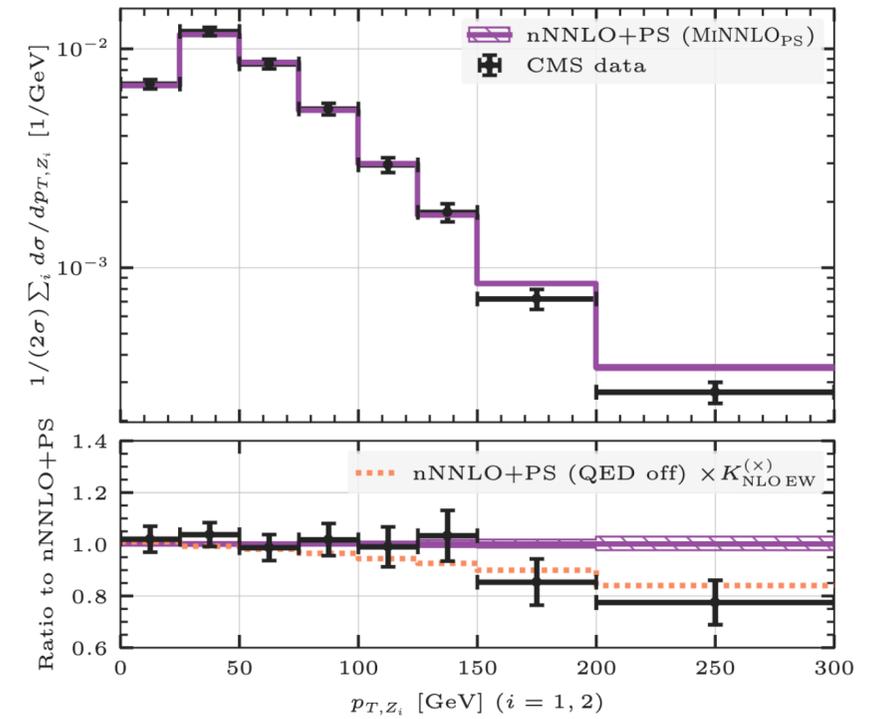
Zγ [2010.10478]



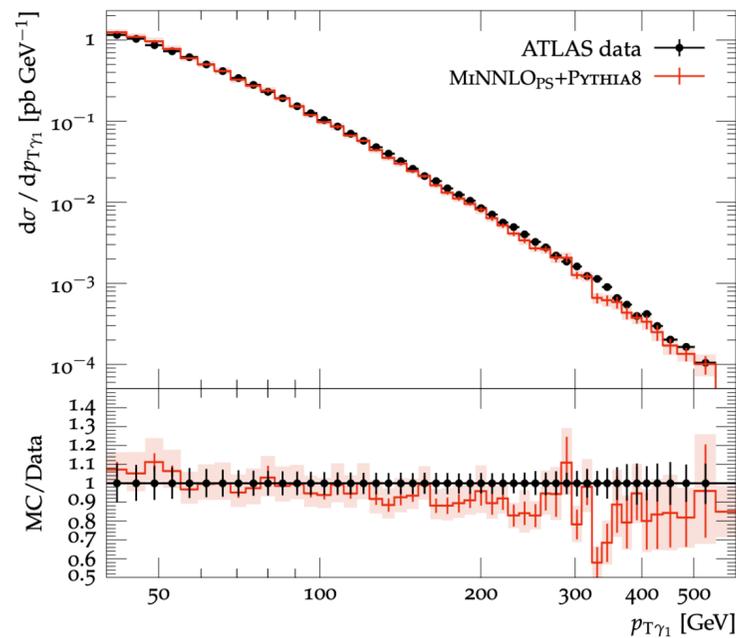
ZZ [2108.05337]



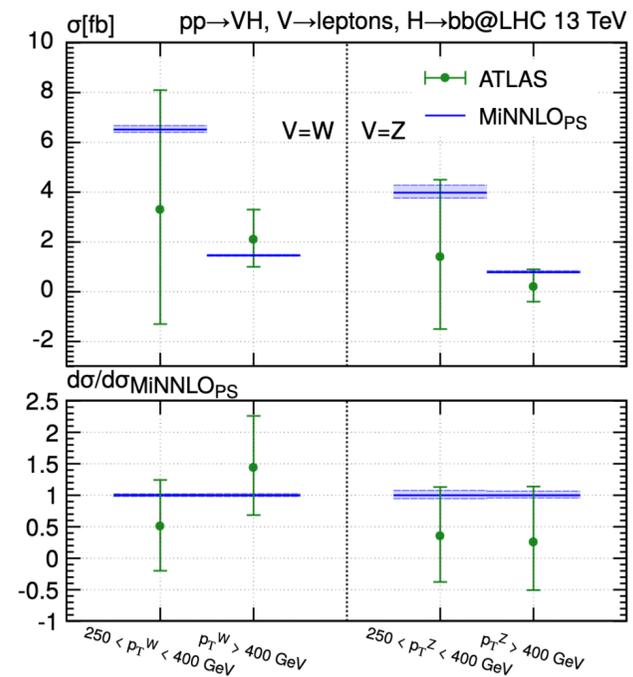
WW [2103.12077]



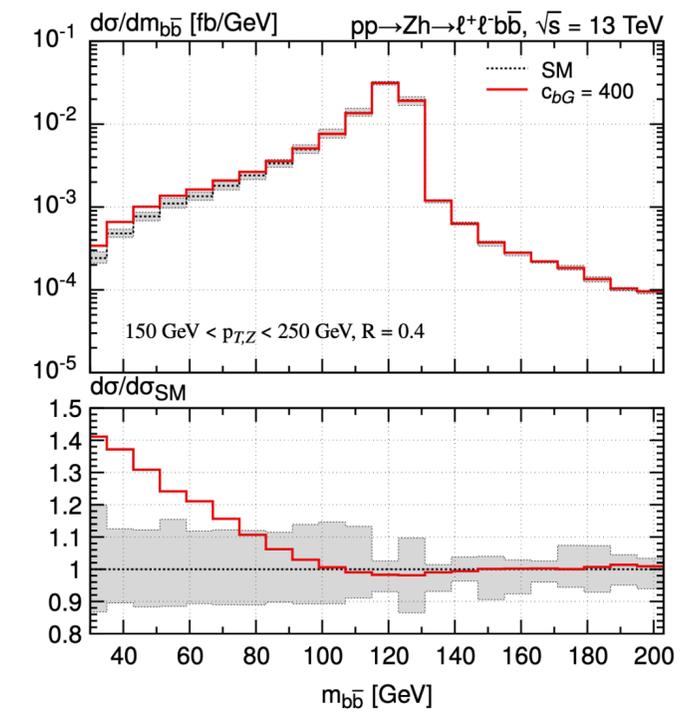
γγ [2204.12602]



VH (H→bb) [2112.04168]

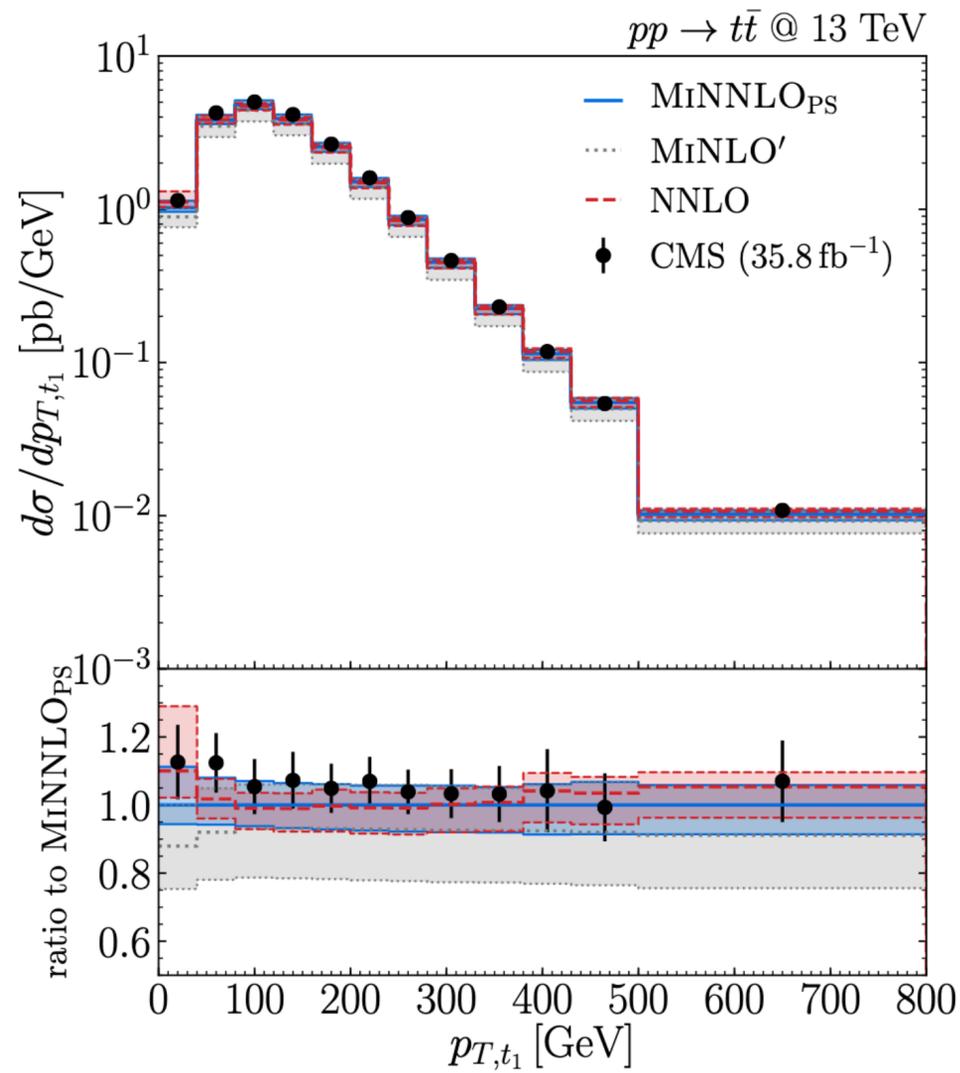


ZH (H→bb) SMEFT [2204.00663]

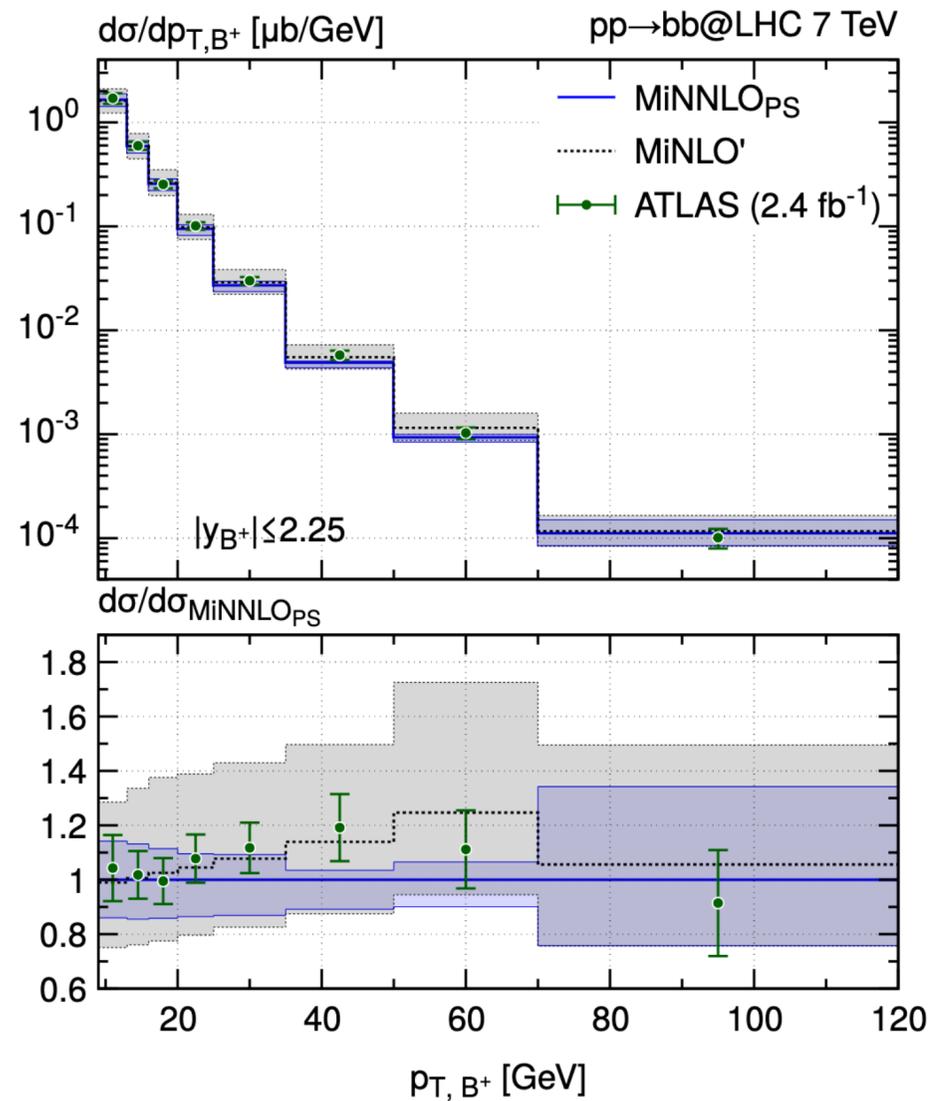


QQ PRODUCTION

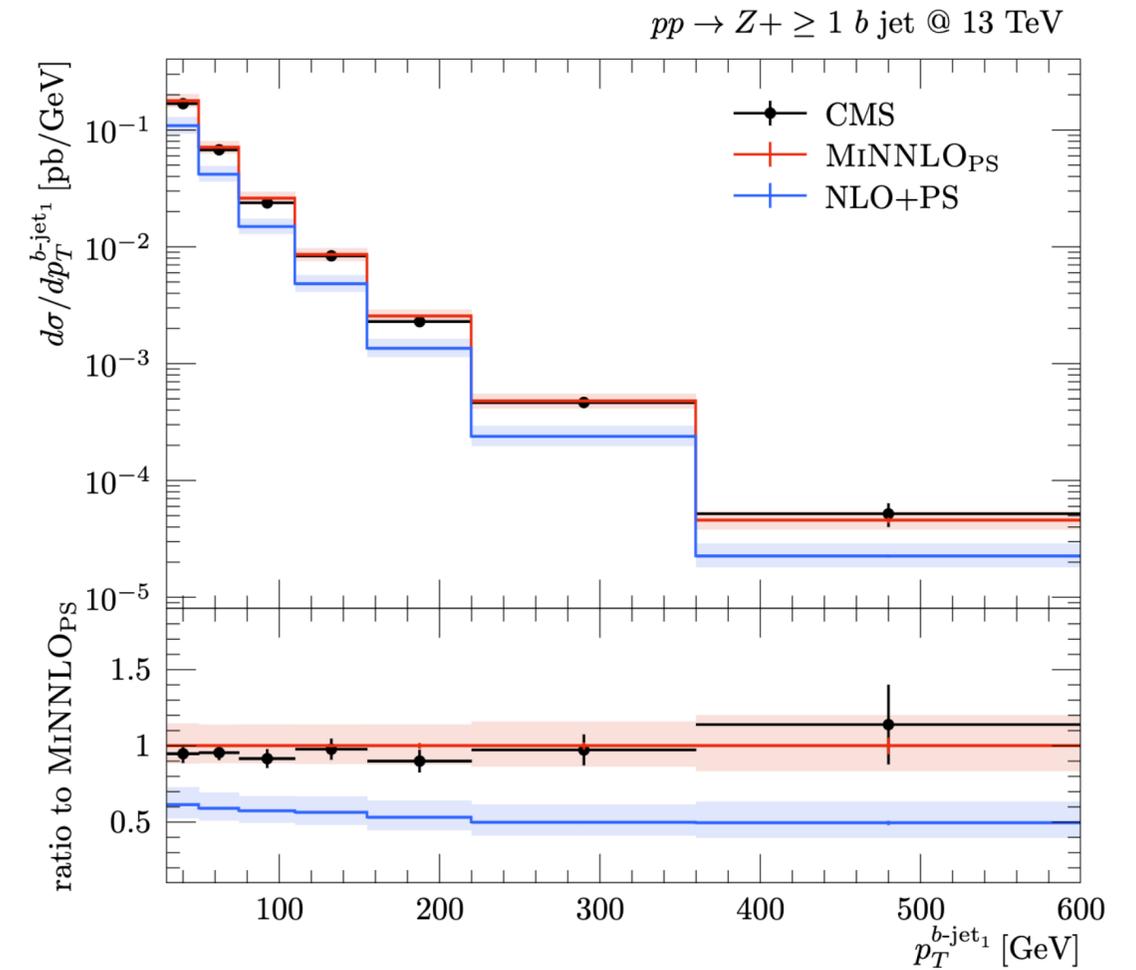
tt production
[2012.14267, 2112.12135]



bb production
[2112.04168]



bbZ production
[2404.08598]

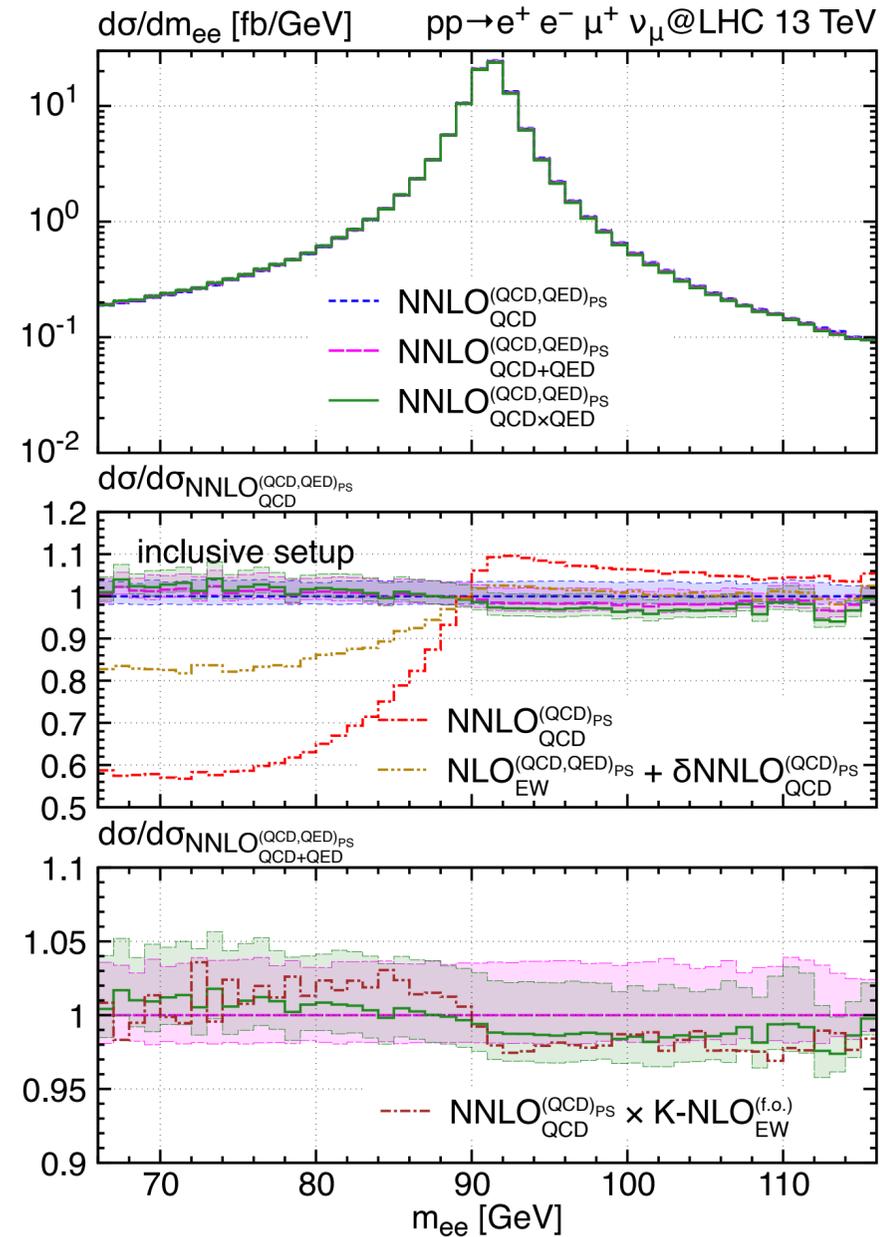


4. WHAT ARE THE NEXT STEPS?

INCLUSION OF NLO EW CORRECTIONS

WZ production

[2208.12660]



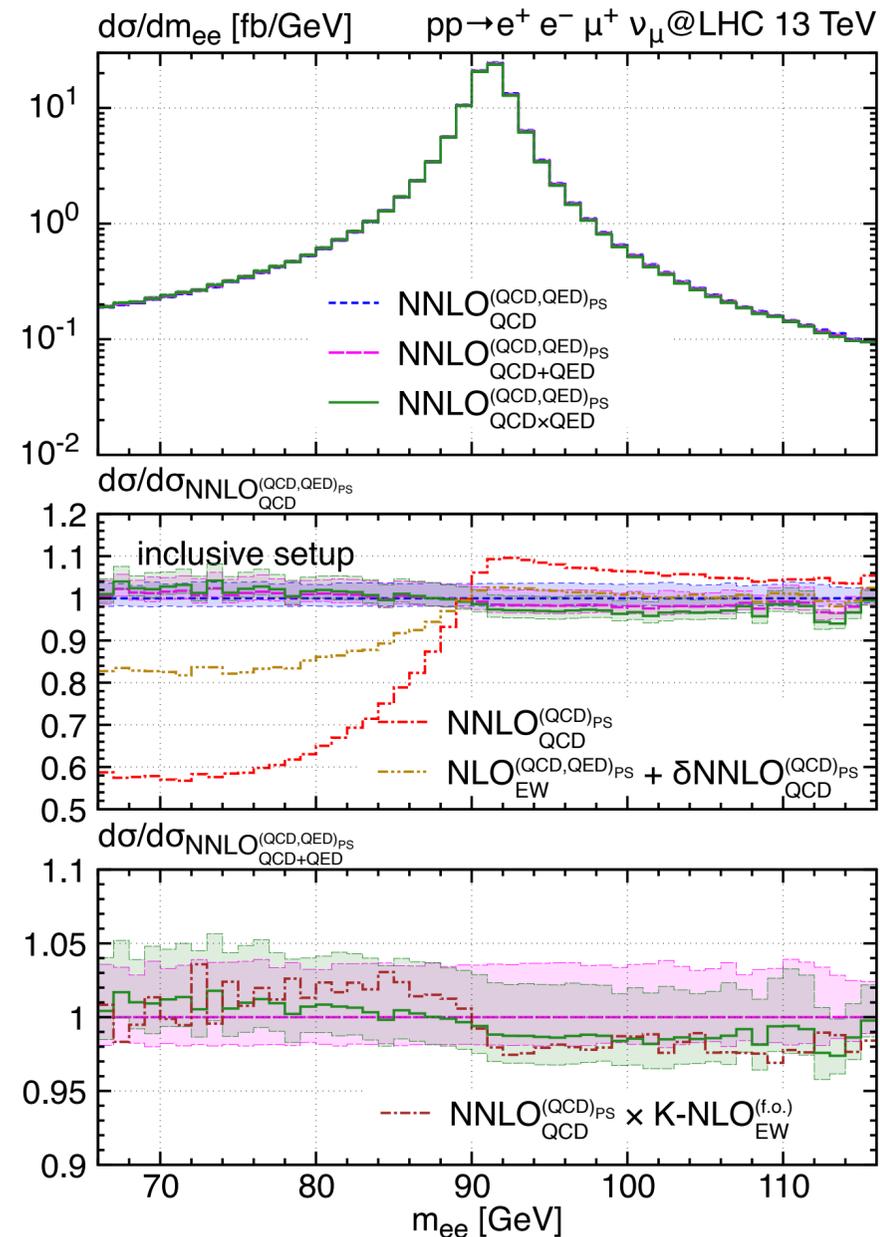
NNLO(QCD) & NLO(EW) matched to PS through a-posteriori reweighting

1. $\text{NNLO}_{\text{QCD}}^{(\text{QCD}, \text{QED})_{\text{PS}}} + \text{NLO}_{\text{EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}} - \text{LO}^{(\text{QCD}, \text{QED})_{\text{PS}}} = \text{NNLO}_{\text{QCD+EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}}$
2. $\text{NNLO}_{\text{QCD}}^{(\text{QCD}, \text{QED})_{\text{PS}}} + \text{NLO}_{\text{EW}}^{(\text{QED})_{\text{PS}}} - \text{LO}^{(\text{QED})_{\text{PS}}}$
3. $\text{NNLO}_{\text{QCD}}^{(\text{QCD})_{\text{PS}}} + \text{NLO}_{\text{EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}} - \text{LO}^{(\text{QCD})_{\text{PS}}}$
4. $\text{NNLO}_{\text{QCD}}^{(\text{QCD}, \text{QED})_{\text{PS}}} \times \text{NLO}_{\text{EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}} / \text{LO}^{(\text{QCD}, \text{QED})_{\text{PS}}} = \text{NNLO}_{\text{QCD}\times\text{EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}}$
5. $\text{NNLO}_{\text{QCD}}^{(\text{QCD}, \text{QED})_{\text{PS}}} \times \text{NLO}_{\text{EW}}^{(\text{QED})_{\text{PS}}} / \text{LO}^{(\text{QED})_{\text{PS}}}$
6. $\text{NLO}_{\text{EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}} \times \text{NNLO}_{\text{QCD}}^{(\text{QCD})_{\text{PS}}} / \text{LO}^{(\text{QCD})_{\text{PS}}}$
7. $\text{NNLO}_{\text{QCD}}^{(\text{QCD})_{\text{PS}}} \times \text{NLO}_{\text{EW}}^{\text{f.o.}} / \text{LO}^{\text{f.o.}}$

INCLUSION OF NLO EW CORRECTIONS

WZ production

[2208.12660]



NNLO(QCD) & NLO(EW) matched to PS through a-posteriori reweighting

1. $NNLO_{QCD}^{(QCD, QED)_{PS}} + NLO_{EW}^{(QCD, QED)_{PS}} - LO^{(QCD, QED)_{PS}} = NNLO_{QCD+EW}^{(QCD, QED)_{PS}}$
2. $NNLO_{QCD}^{(QCD, QED)_{PS}} + NLO_{EW}^{(QED)_{PS}} - LO^{(QED)_{PS}}$
3. $NNLO_{QCD}^{(QCD)_{PS}} + NLO_{EW}^{(QCD, QED)_{PS}} - LO^{(QCD)_{PS}}$
4. $NNLO_{QCD}^{(QCD, QED)_{PS}} \times NLO_{EW}^{(QCD, QED)_{PS}} / LO^{(QCD, QED)_{PS}} = NNLO_{QCD \times EW}^{(QCD, QED)_{PS}}$
5. $NNLO_{QCD}^{(QCD, QED)_{PS}} \times NLO_{EW}^{(QED)_{PS}} / LO^{(QED)_{PS}}$
6. $NLO_{EW}^{(QCD, QED)_{PS}} \times NNLO_{QCD}^{(QCD)_{PS}} / LO^{(QCD)_{PS}}$
7. $NNLO_{QCD}^{(QCD)_{PS}} \times NLO_{EW}^{f.o.} / LO^{f.o.}$

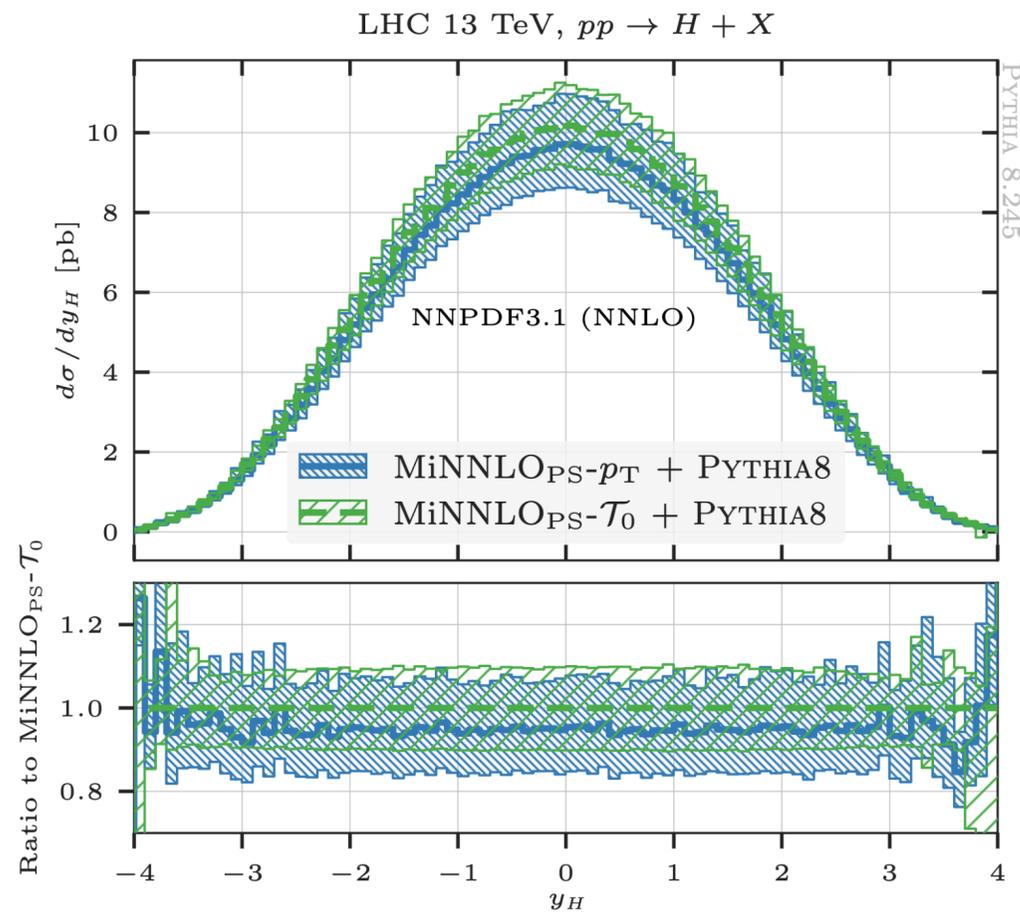
TOWARDS AN ON-THE-FLY GENERATION

ongoing!

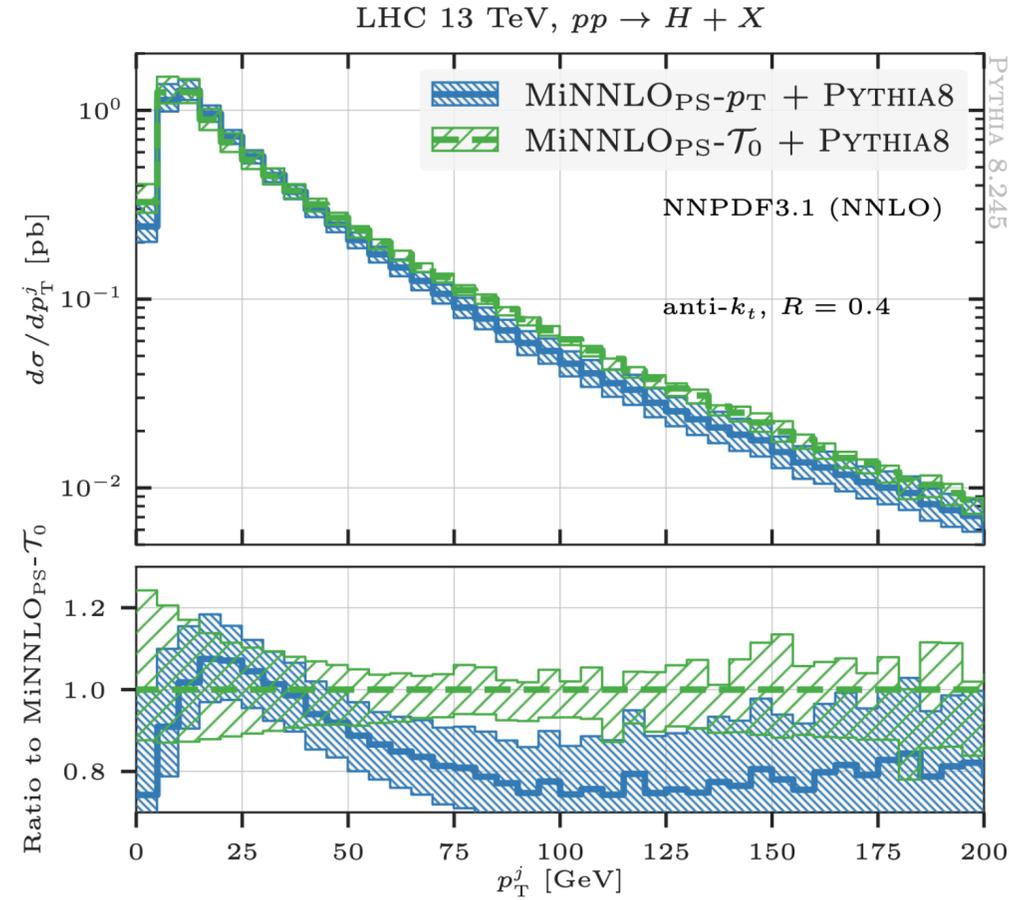
PROCESSES WITH JETS

[2402.00596]

H production (τ_0)

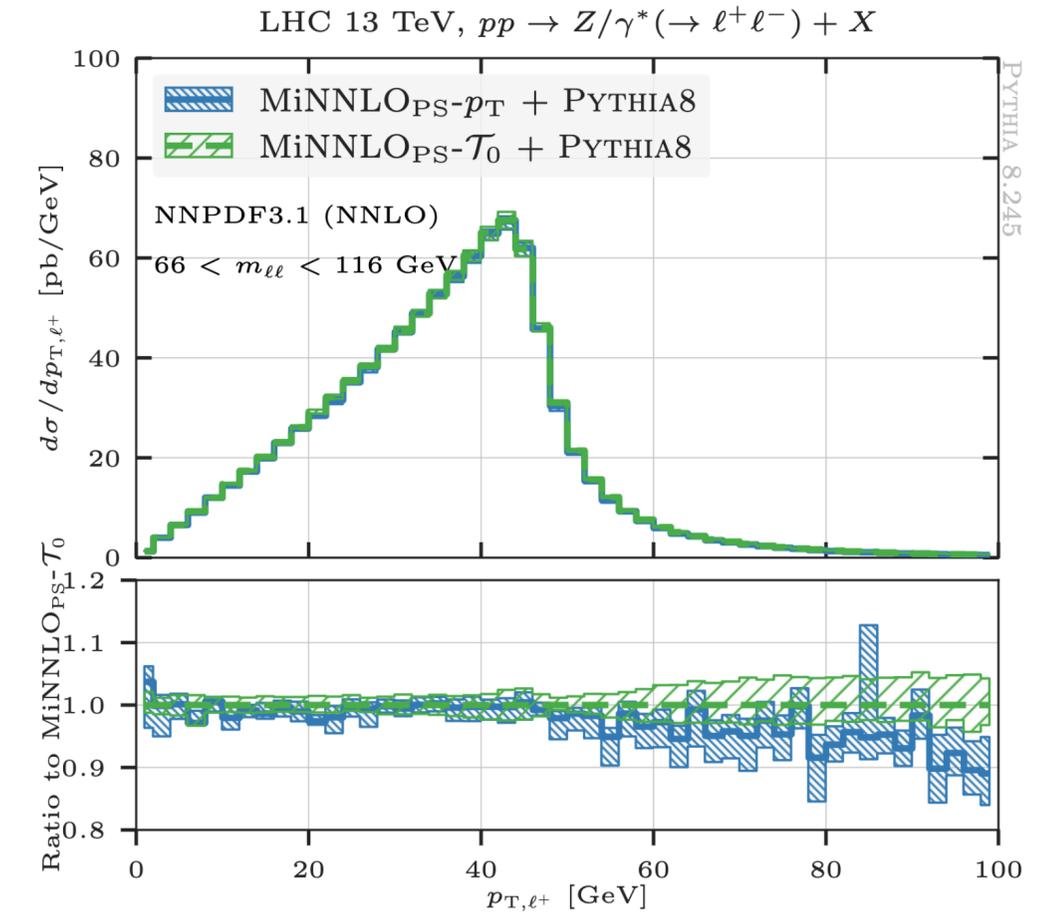


NNLO observable



NLO observable

Z production (τ_0)

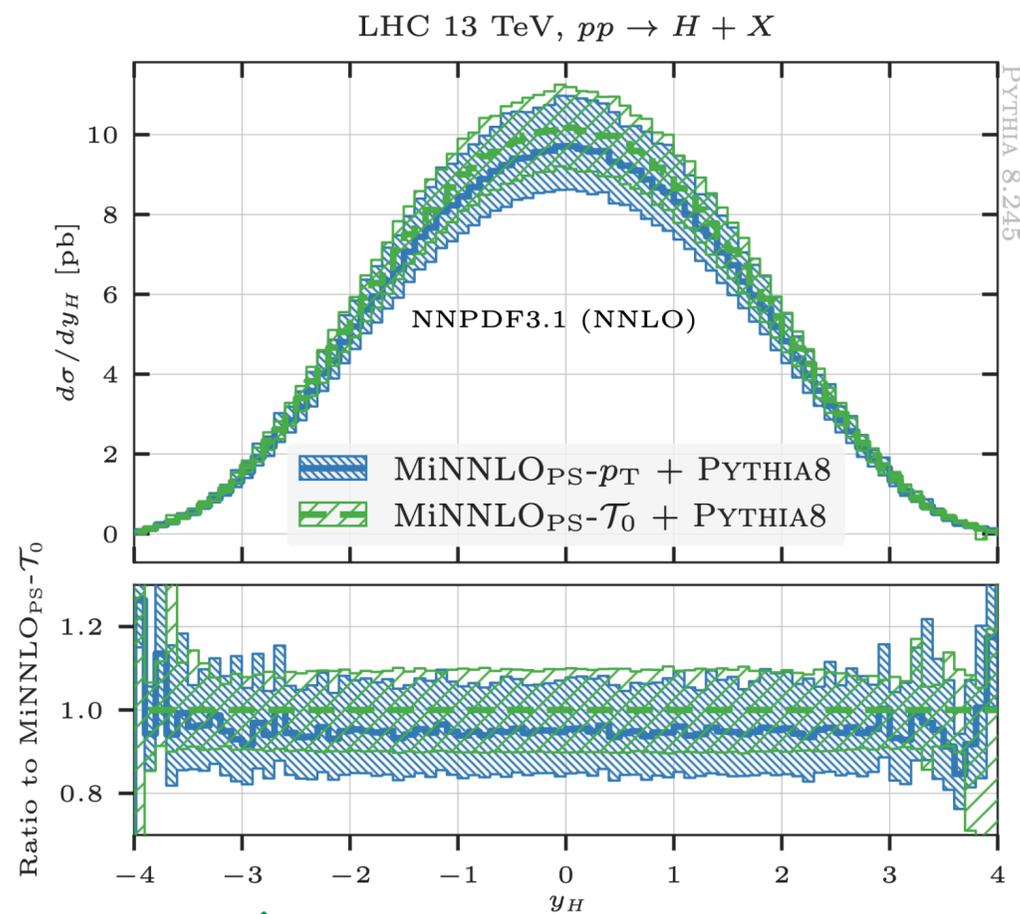


NNLO observable

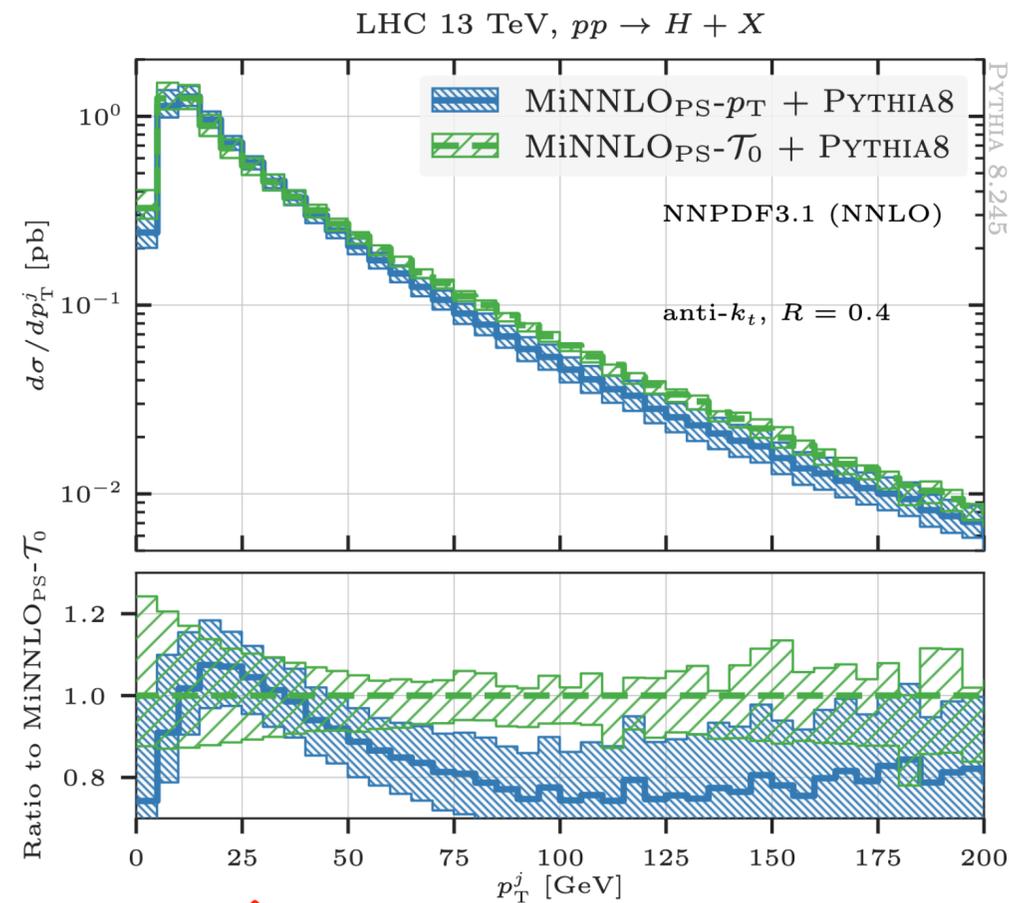
PROCESSES WITH JETS

[2402.00596]

H production (τ_0)

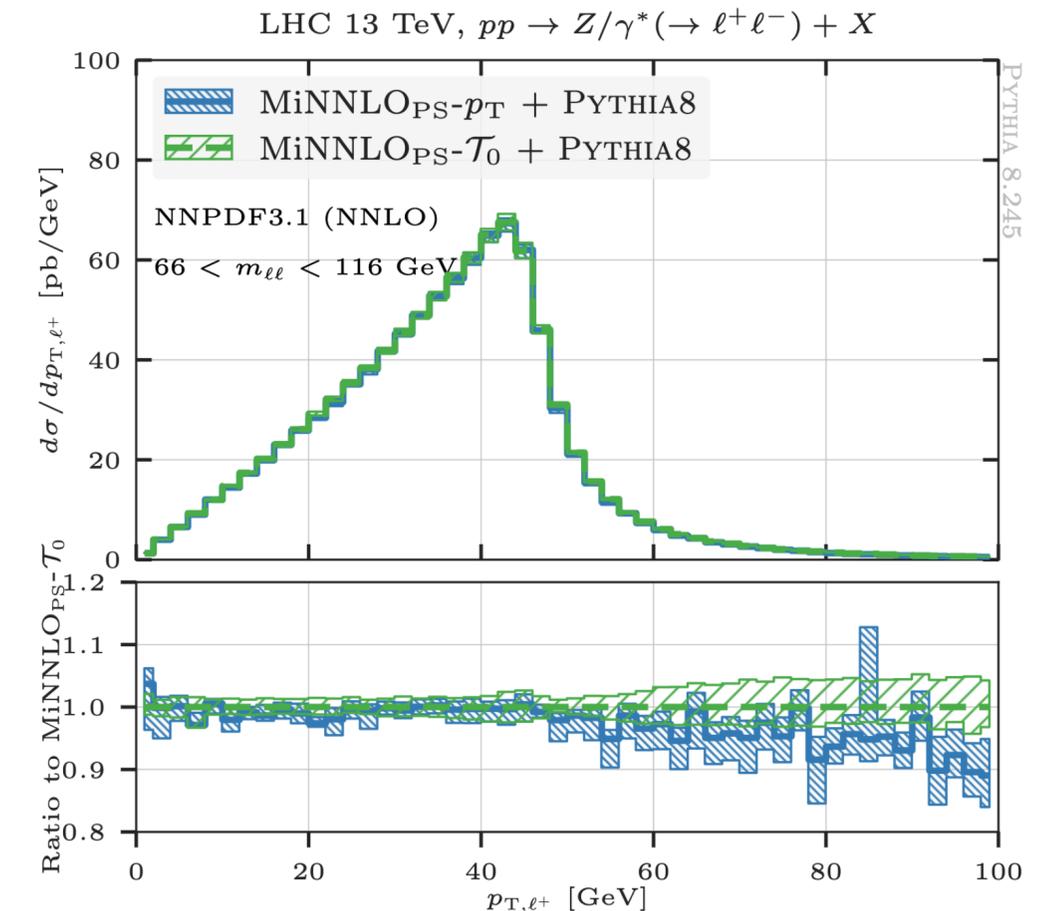


✓ NNLO observable



✗ NLO observable

Z production (τ_0)



✓ NNLO observable

!! The matching with the shower is NOT trivial !!

SUMMARY

<https://powhegbox.mib.infn.it/>

2019	H/Z	[1908.06987]
2020	$Z\gamma$	[2010.10478]
	tt	[2012.14267]
	W	[2006.04133]
2021	WW	[2103.12077]
	ZZ	[2108.05337]
	VH (H \rightarrow bb)	[2112.04168]
2022	VH (H \rightarrow bb)(SMEFT)	[2204.00663]
	$\gamma\gamma$	[2204.12602]
	WZ	[2208.12660]
2023	bb	[2302.01645]
2024	H/Z (jettiness)	[2402.00596]
	bb \rightarrow H	[2402.04025]
	bbZ	[2404.08598]

Different possible outlooks:

1. Inclusion of EW effects
2. Extension to processes with jets
3. NNLO+PS for LEP
4. “FONLL” approach for 5FS/4FS
5. ...

MAIN MESSAGE:

NNLO+PS IS POSSIBLE NOWADAYS

5. HOW TO RUN MINNLO_{PS}

(VERY COMPLICATED) STEPS TO FOLLOW

1. DOWNLOAD THE CODE
2. COMPILE THE CODE
3. RUN THE CODE

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EXAMPLE: DY with MiNNLO_{PS}

```
$ svn checkout --username anonymous --password anonymous svn://powhegbox.mib.infn.it/trunk/POWHEG-BOX-V2
```

```
$ cd POWHEG-BOX-V2
```

```
$ svn co --username anonymous --password anonymous svn://powhegbox.mib.infn.it/trunk/User-Processes-V2/Zj
```

```
$ cd Zj/ZjMiNNLO
```

```
$ make (make main-PYTHIA8-lhef)
```

```
$ cd suggested-run
```

```
$ cp powheg.input-save powheg.input
```

```
$ ../pwhg_main (echo pwgevents.lhe | ../main-PYTHIA8-lhef)
```

```
alphas_from_pt 1 ! (default 0) if 1, uses alphas from PDF evolution tool (e.g.
! MINLO SETTINGS
minlo 1 ! (default 0) if 1, activate minlo
minnlo 1 ! (default 0) if 1, activate miNNlo
largeptscales 0 ! (default 0) if 0, at large pt, use muR=muF~Q in fixed order
! if 1, at large pt, use muR=muF=pt in the fixed-c
#00 0.5 ! (default 0) 00 value used in profiled scales (see 2006_041
```

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Have fun!

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