

Projected Sensitivities on Triple Gauge Couplings at the FCC- $\mu\mu$

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- Theoretical Background
- $\mu^- \gamma \rightarrow \mu^- \gamma Z \rightarrow \mu^- \gamma \nu_l \bar{\nu}_l$ process at FCC- μ p Collider
- A Cut-based Analysis
- Sensitivities on aNTGC
- Conclusions
- References



Theoretical Background

- Non-Abelian structure of Standard Model \Rightarrow couplings between gauge bosons.
- Triple couplings
 - $\Rightarrow \gamma WW, ZWW$ in EW
 - $\Rightarrow ZZZ, ZZ\gamma, Z\gamma\gamma$ don't exist at the tree level (No Dim-6 but Dim-8)
- Standard Model - Nothing to expect
- New physics parametrized with effective Lagrangian.
 - enhancing existing couplings
 - introduce non-SM couplings



Theoretical Background

Main goals

- test the non-Abelian structure of the Standard Model.
- exploring new physics beyond the Standard Model.

EFT approach

- adding high-dimensional operators that are invariant under $SU(2)_L \times U(1)_Y$ to the SM Lagrangian.



Theoretical Background

$$\mathcal{L}^{\text{NTGC}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{C_i}{\Lambda^4} (\mathcal{O}_i + \mathcal{O}_i^\dagger)$$

$$\mathcal{O}_{\tilde{B}W} = iH^\dagger \tilde{B}_{\sigma\rho} W^{\sigma\nu} \{D_\nu, D^\rho\} H,$$

$$\mathcal{O}_{BW} = iH^\dagger B_{\sigma\rho} W^{\sigma\nu} \{D_\nu, D^\rho\} H,$$

$$\mathcal{O}_{WW} = iH^\dagger W_{\sigma\rho} W^{\sigma\nu} \{D_\nu, D^\rho\} H,$$

$$\mathcal{O}_{BB} = iH^\dagger B_{\sigma\rho} B^{\sigma\nu} \{D_\nu, D^\rho\} H$$



Theoretical Background

where,

$$B_{\sigma\rho} = (\partial_\sigma B_\rho - \partial_\rho B_\sigma),$$

$$W_{\sigma\rho} = \sigma^i \left(\partial_\sigma W_\rho^i - \partial_\rho W_\sigma^i + g\epsilon_{ijk} W_\sigma^j W_\rho^k \right),$$

$$D_\mu \equiv \partial_\mu - i\frac{g'}{2} B_\mu Y - ig_W W_\mu^i \sigma^i.$$



Photon Spectrum

$$f_{\gamma}(x) = \frac{\alpha}{\pi E_p} \left\{ [1 - x] \left[\varphi\left(\frac{Q_{max}^2}{Q_0^2}\right) - \varphi\left(\frac{Q_{min}^2}{Q_0^2}\right) \right] \right\},$$

where the function φ is given as:

$$\varphi(\theta) = (1 + ky) \left[-\ln\left(1 + \frac{1}{\theta}\right) + \sum_{s=1}^3 \frac{1}{s(1+\theta)^s} \right] + \frac{y(1-l)}{4\theta(1+\theta)^3} + m(1 + \frac{y}{4}) \left[\ln\left(\frac{1-l+\theta}{1+\theta}\right) + \sum_{s=1}^3 \frac{l^s}{s(1+\theta)^s} \right].$$



Photon Spectrum

$$y = \frac{x^2}{(1-x)},$$

$$k = \frac{1 + \mu_p^2}{4} + \frac{4m_p^2}{Q_0^2} \approx 7.16,$$

$$l = 1 - \frac{4m_p^2}{Q_0^2} \approx -3.96,$$



Photon Spectrum

$$m = \frac{\mu_p^2 - 1}{b^4} \approx 0.028.$$

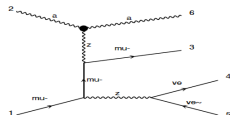
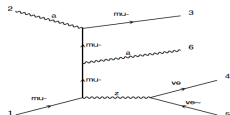
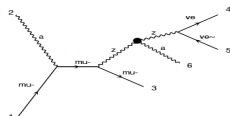
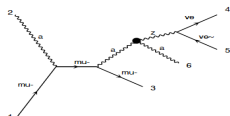
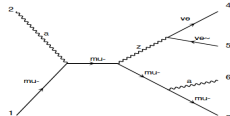
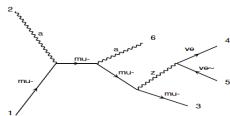
$$\sigma = \int f_\gamma(x) d\hat{\sigma} dE_1.$$

$$\sigma_{Tot} = \sigma_{SM}(\sqrt{s}) + \sigma_{(INT)} + \sigma_{(NP)}$$



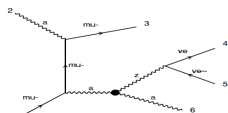
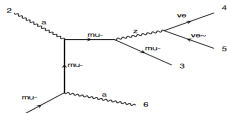
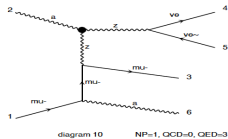
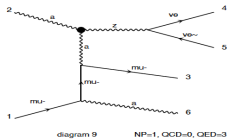
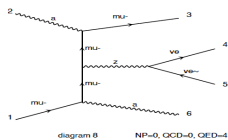
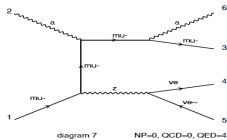
$\mu^- \gamma \rightarrow \mu^- \gamma Z \rightarrow \mu^- \gamma \nu_l \bar{\nu}_l$ process at FCC- μp Collider ($\sqrt{s} = 24.5$ TeV)

Feynman Diagrams



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Feynman Diagrams



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Feynman Diagrams

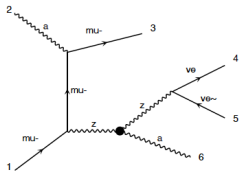


diagram 13 NP=1, QCD=0, QED=3

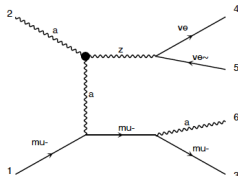
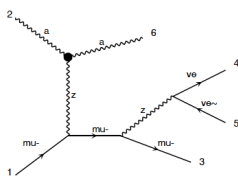
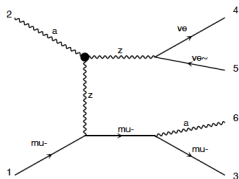


diagram 14 NP=1, QCD=0, QED=3



A Cut-based Analysis

Object-1

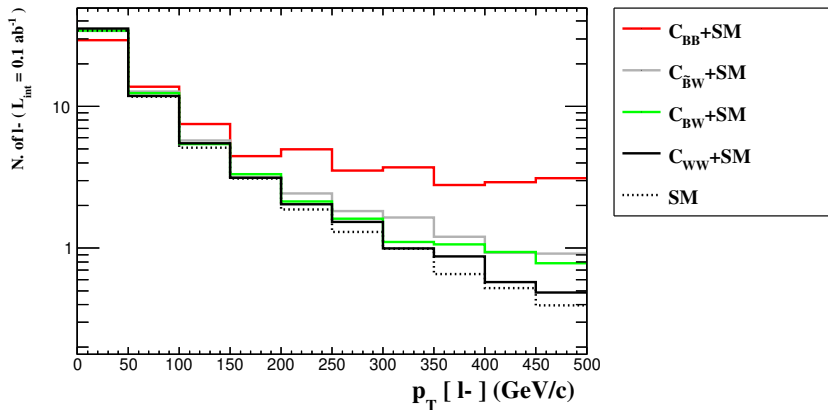


Figure: The number of expected events as a function of p_T^{l-} .

A Cut-based Analysis

Object-II

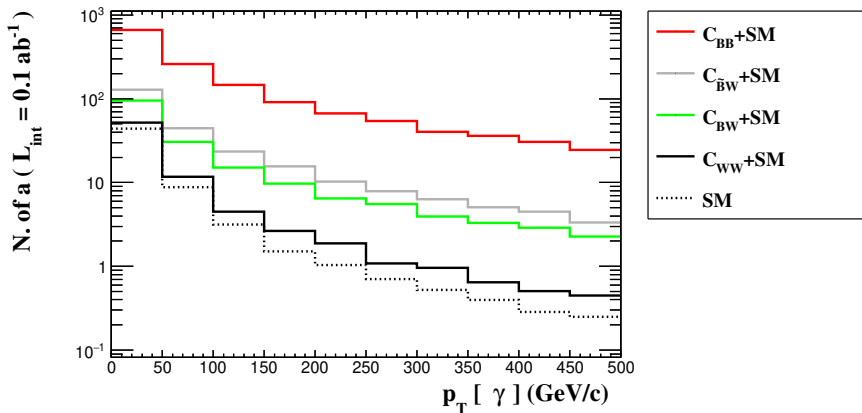


Figure: The number of expected events as a function of p_T^γ .

A Cut-based Analysis

Object-III

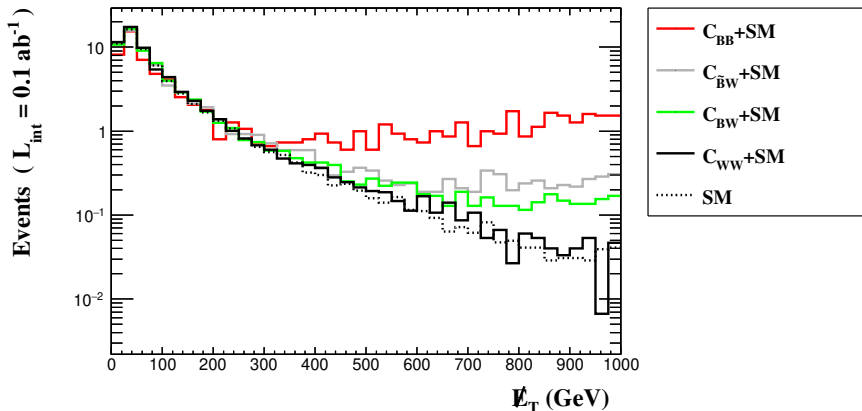


Figure: The number of expected events as a function of missing energy transverse energy E_T^{miss} .



A Cut-based Analysis

Table: Particle-level selections cuts for the signals at the Muon Collider.

Kinematic cuts	$C_{BB}/\Lambda^4, C_{BW}/\Lambda^4, C_{\tilde{B}W}/\Lambda^4, C_{WW}/\Lambda^4$
Cut-I	$p_T^\mu > 70 \text{ GeV}$
Cut-II	$p_T^\gamma > 100 \text{ GeV}$
Cut-III	$\cancel{E}_T > 350$



A Cut-based Analysis

Table: Number of events for $\mu^- \gamma \rightarrow \mu^- \gamma Z \rightarrow \mu^- \gamma \nu_l \bar{\nu}_l$ and SM background after cuts.

Kinematic cuts	C_{BB}/Λ^4	$C_{\tilde{B}W}/\Lambda^4$	C_{BW}/Λ^4	C_{WW}/Λ^4	SM
Cut-0	1718	298	203	79	61
Cut-I	1681	257	163	38	21
Cut-II	795	122	74	14	6
Cut-III	790	117	69	9	1



$$\chi^2 = \left(\frac{\sigma_{SM} - \sigma_{Tot}}{\sigma_{SM} \sqrt{(\delta_{st})^2 + (\delta_{sys})^2}} \right)^2$$

$$\delta_{st} = \frac{1}{\sqrt{N_{SM}}}$$

$$N_{SM} = \mathcal{L}_{int} \times \sigma_{SM}$$

- Sensitivities are obtained at the 95% C.L.



Sensitivities on aNTGC

Couplings	0%	5%	10%
$\mathcal{L} = 5 \text{ ab}^{-1}$			
C_{BB}/Λ^4	$[-0.019; 0.023]$	$[-0.020; 0.024]$	$[-0.022; 0.026]$
C_{BW}/Λ^4	$[-0.066; 0.078]$	$[-0.069; 0.081]$	$[-0.077; 0.089]$
$C_{\tilde{B}W}/\Lambda^4$	$[-0.058; 0.053]$	$[-0.060; 0.056]$	$[-0.066; 0.062]$
C_{WW}/Λ^4	$[-0.18; 0.20]$	$[-0.18; 0.21]$	$[-0.20; 0.23]$



Sensitivities on aNTGC

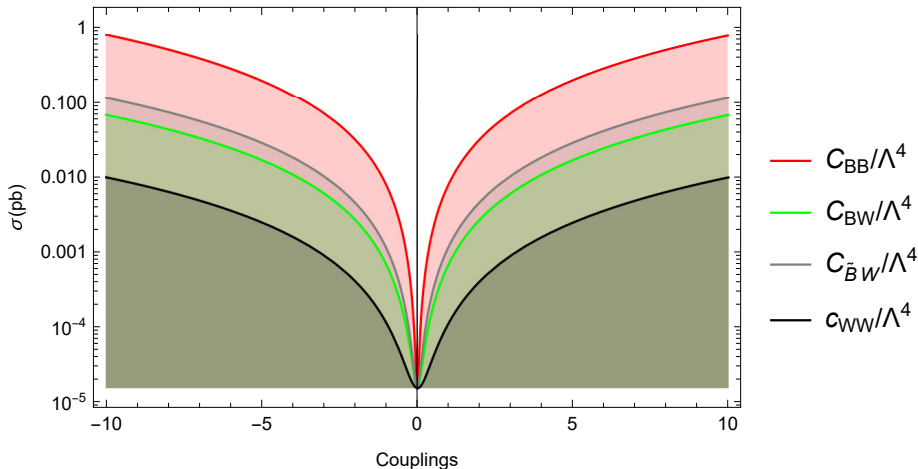


Figure: Cross-section for the process $\mu^- \gamma \rightarrow \mu^- \gamma Z \rightarrow \mu^- \gamma \nu_i \bar{\nu}_i$ in terms of the anomalous C_{BB}/Λ^4 , C_{BW}/Λ^4 , $C_{\tilde{B}W}/\Lambda^4$, C_{WW}/Λ^4 couplings



Experimental Results on aNTGC

$$-1.1 \text{ TeV}^{-4} < \frac{C_{\tilde{B}W}}{\Lambda^4} < 1.1 \text{ TeV}^{-4},$$

$$-2.3 \text{ TeV}^{-4} < \frac{C_{WW}}{\Lambda^4} < 2.3 \text{ TeV}^{-4},$$

$$-0.65 \text{ TeV}^{-4} < \frac{C_{BW}}{\Lambda^4} < 0.64 \text{ TeV}^{-4},$$

$$-0.24 \text{ TeV}^{-4} < \frac{C_{BB}}{\Lambda^4} < 0.24 \text{ TeV}^{-4}.$$



Sensitivities on aNTGC

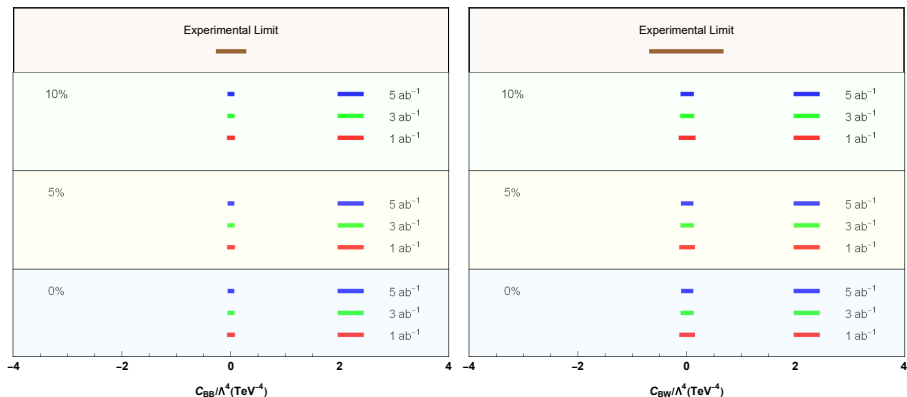


Figure: Comparison of the current experimental limits and projected sensitivity on the anomalous C_{BB}/Λ^4 and C_{BW}/Λ^4 .



Sensitivities on aNTGC

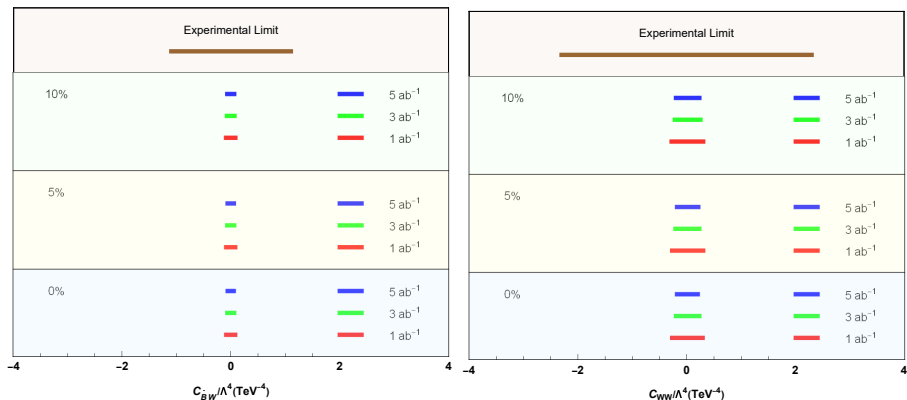






Figure: Comparison of the current experimental limits and projected sensitivity on the anomalous $C_{\tilde{B}W}/\Lambda^4$ and C_{WW}/Λ^4 .



Conclusions

- A study for the sensitivity on dim-8 aNTGC in a model independent way via the process $\mu^- \gamma \rightarrow \mu^- \gamma Z \rightarrow \mu^- \gamma \nu_l \bar{\nu}_l$ at FCC- μp collider has been performed.
- Effective Field Theory(EFT) approach are used to parametrize the new physics effects with high dimensional operator.
- A cut-based method has been applied during the analysis.
- Sensitivities are composed under various systematic uncertainties.
- Obtained results are improved the latest experimental limits by a factor of 8 to 20 times.



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