

Nonperturbative signals in jet observables

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Nonperturbative and topological aspects of QCD

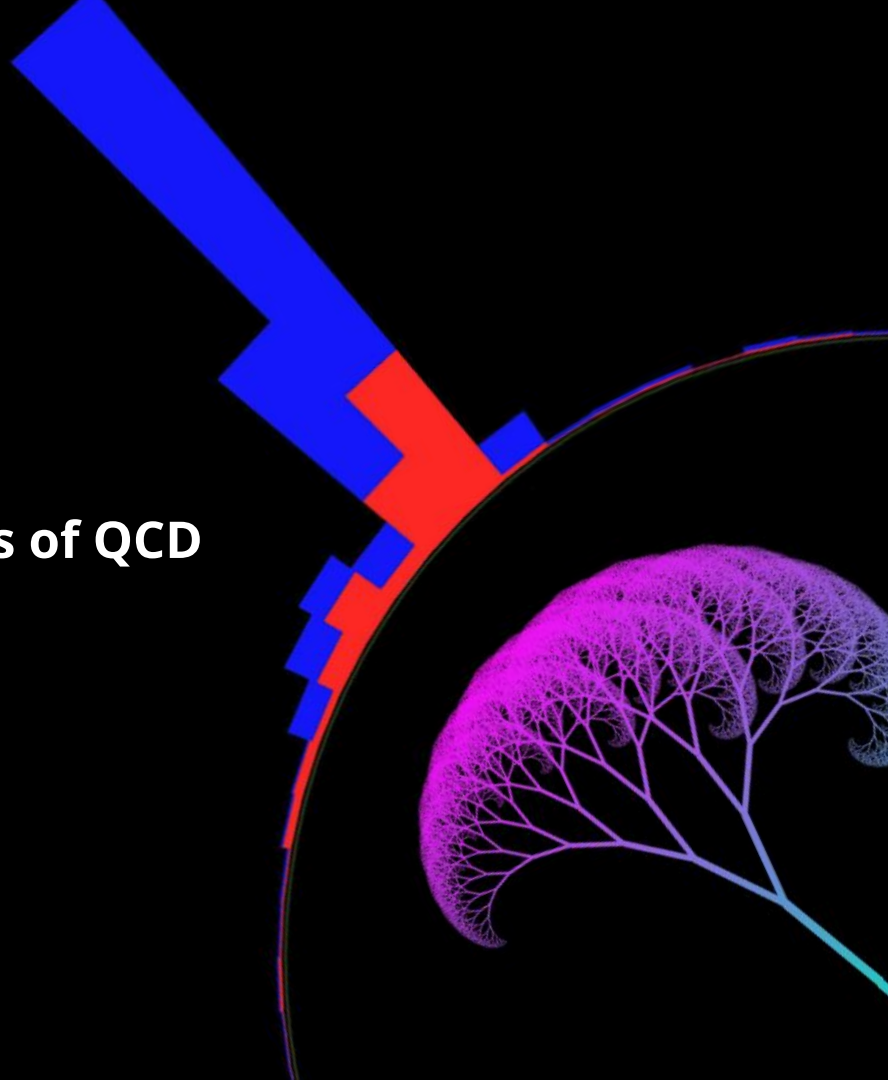
May 29th-30th



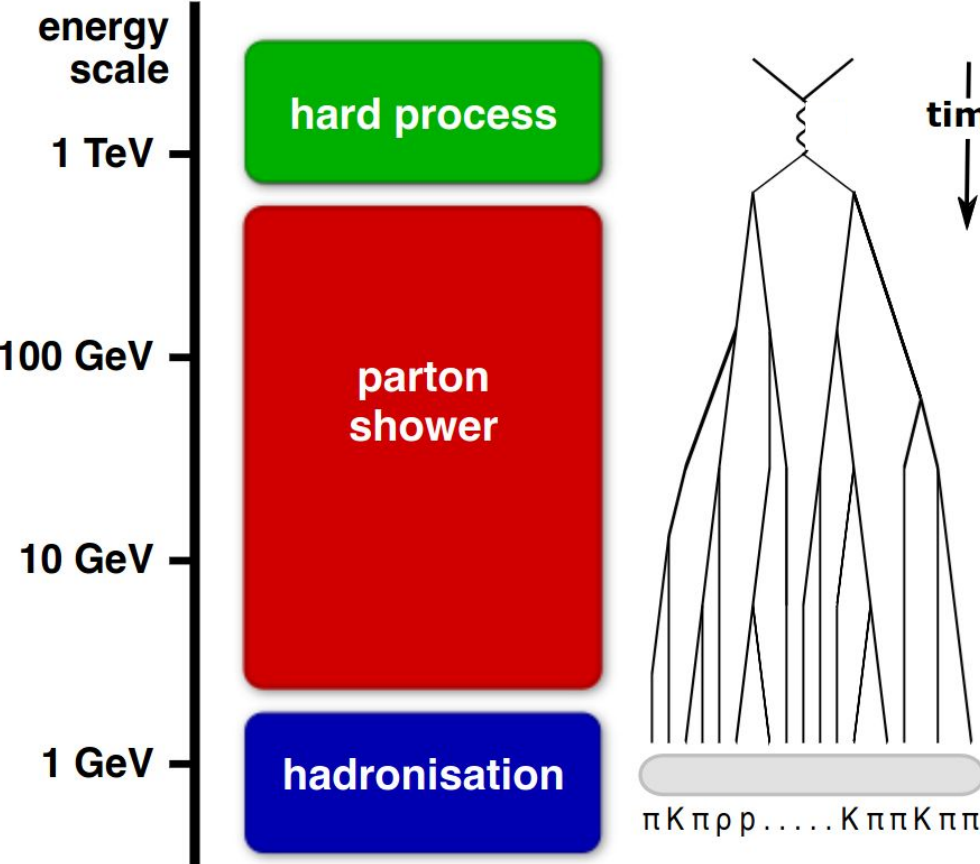
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European Research Council



Jet formation is a multiscale probe of QCD evolution



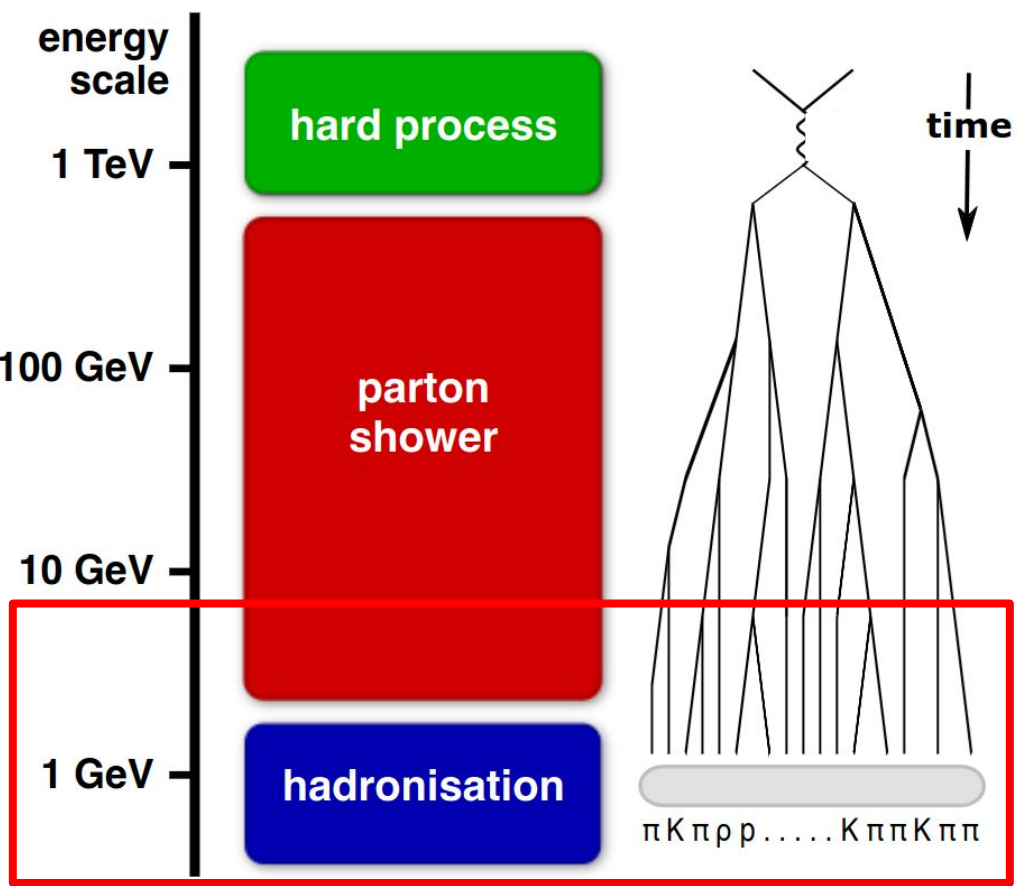
From $Q \sim 1 \text{ TeV}$ down to $\Lambda_{\text{QCD}} \sim 200 \text{ MeV}$

Jet $p_T \leftrightarrow$ parton cascade "length"

Depending on observable, jet p_T , and radius R : sensitivity to parton shower, hadronization, underlying event, color reconnection, ...

G. Salam's sketch

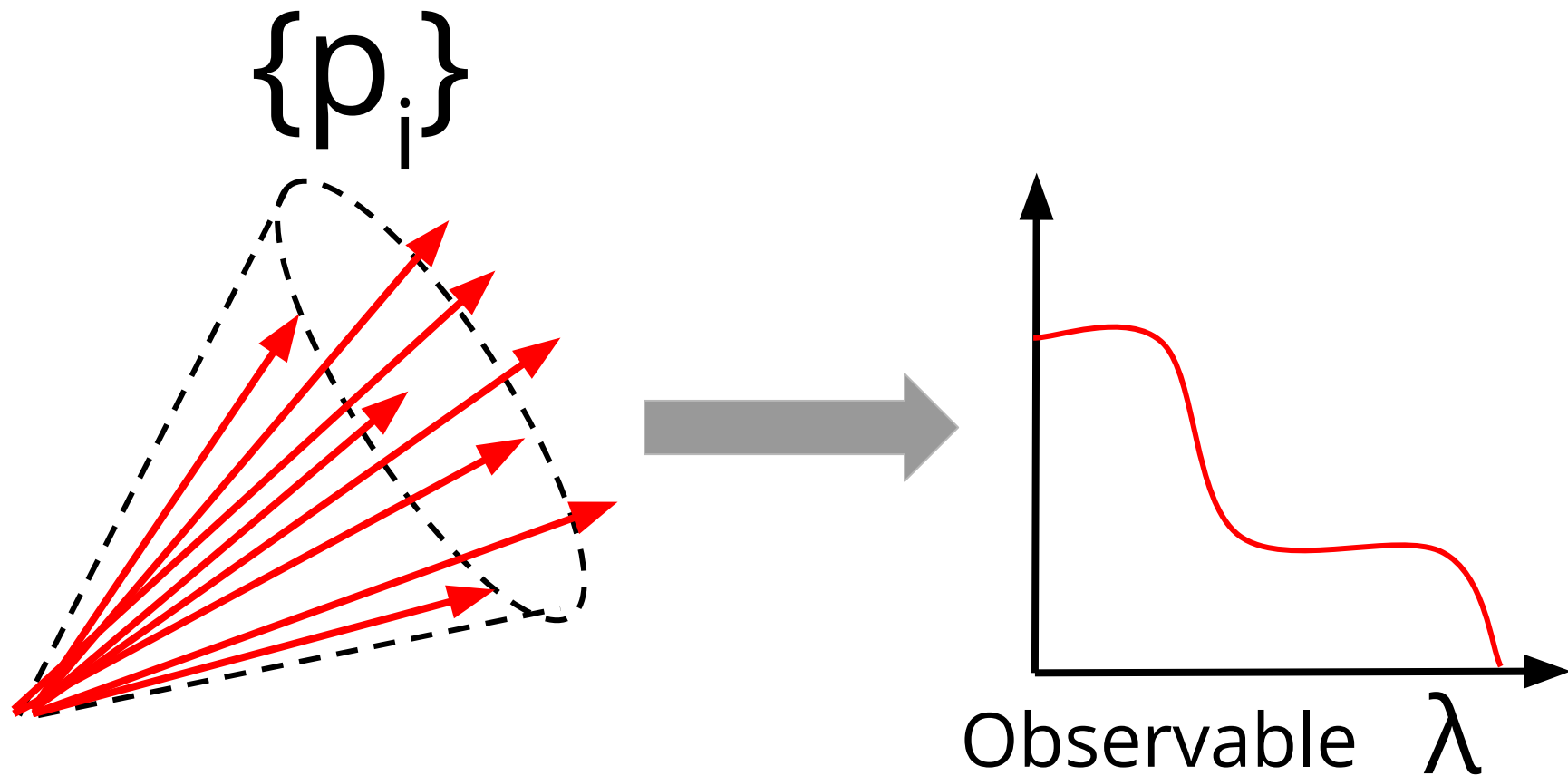
Jet formation is a multiscale probe of QCD evolution



focus on this

G. Salam's sketch

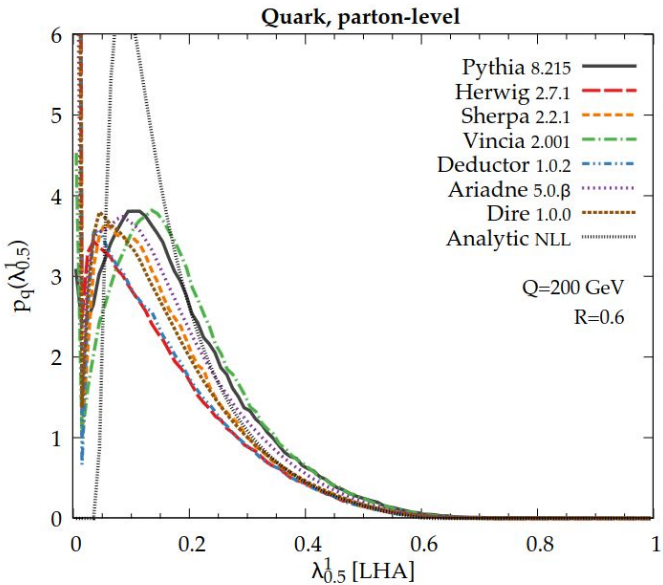
Jet substructure in a nutshell



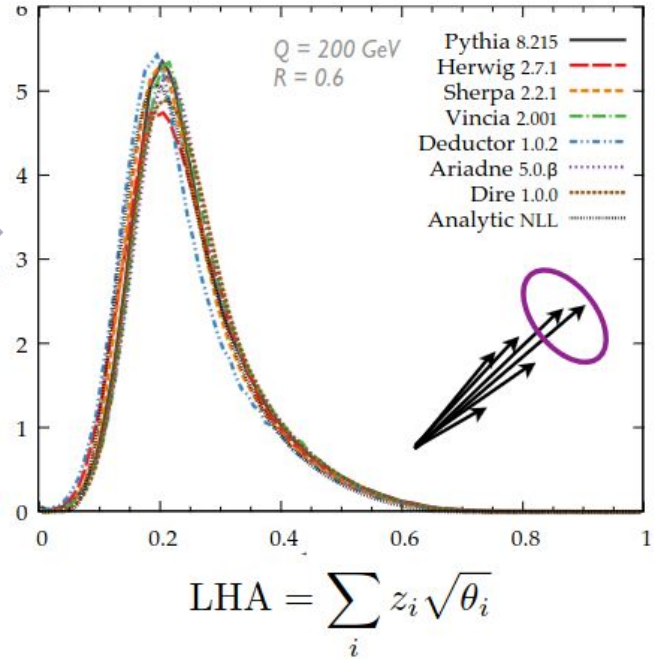
Identifying onset of hadronization in jet showers

Nontrivial to separate “perturbative” & “nonperturbative” components

Parton-level



Hadron-level

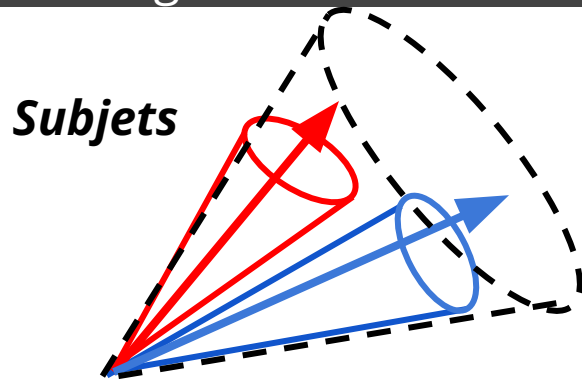


p_T -weighted angular distance

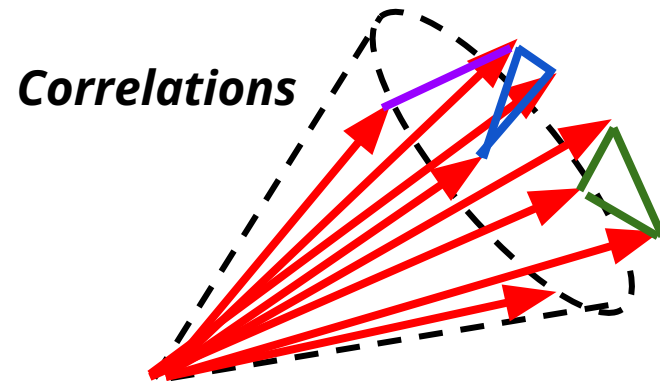
This talk:

Two approaches to understand jet showers in a **modular fashion**

Clustering-based observables

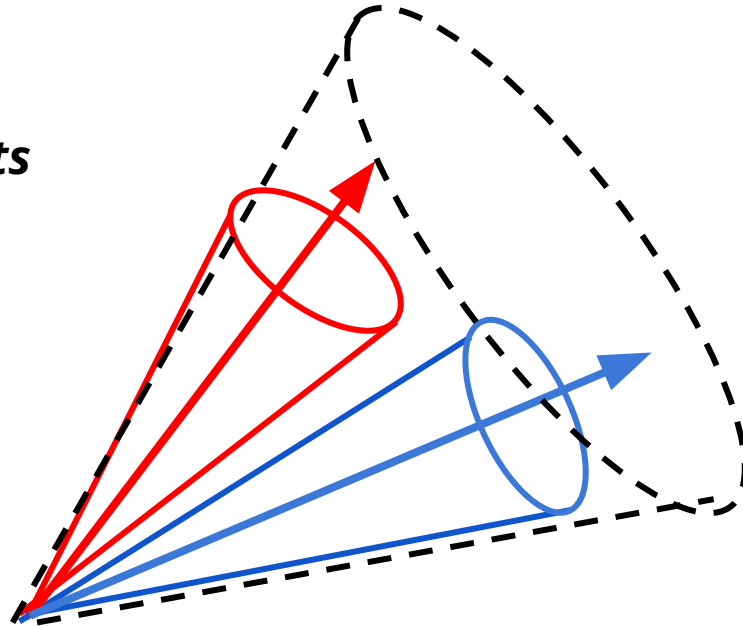


Energy-flow-based observables



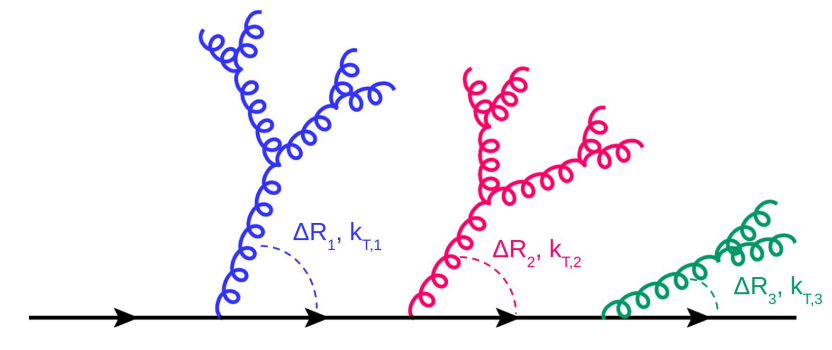
Clustering-based observables

Subjets

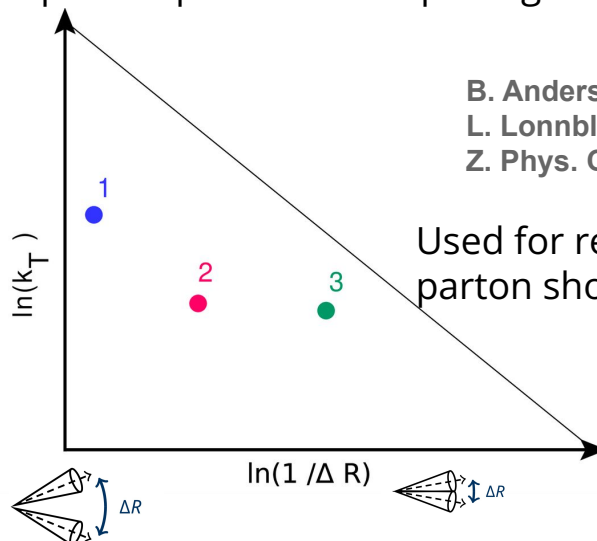


Phase-space of QCD branchings in the Lund plane

Lund planes (or diagrams) are a 2D representation of the phase-space of $1 \rightarrow 2$ splittings:



k_T : relative transverse momentum of emission
 ΔR : angular opening of emission and core



B. Andersson, G. Gustafson,
 L. Lonnblad, and U. Pettersson,
 Z. Phys. C43 (1989) 625

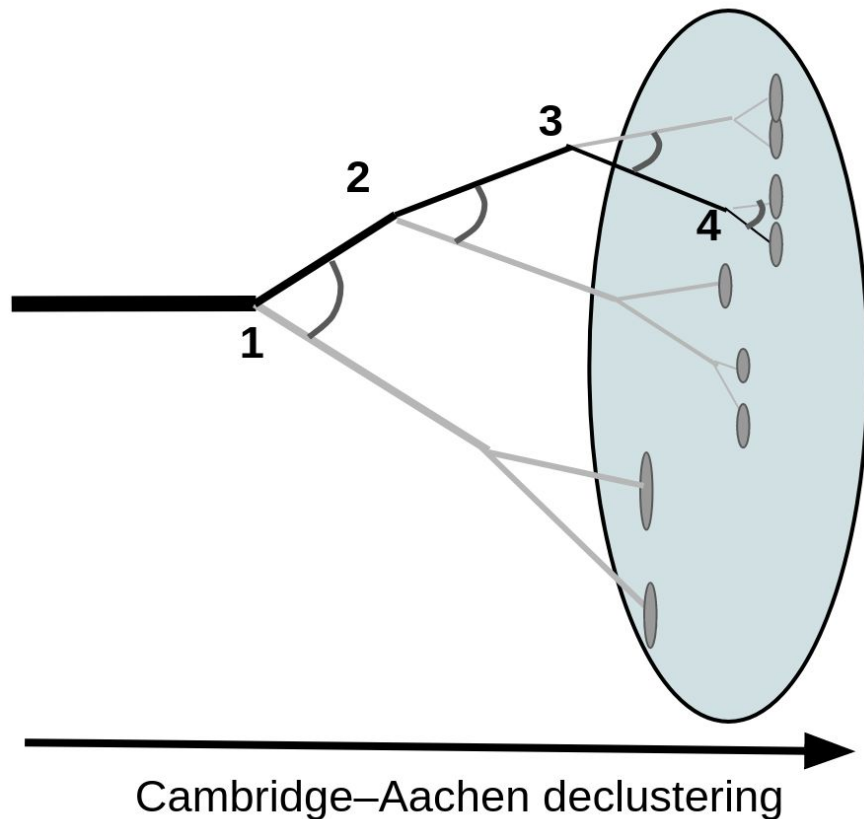
Used for resummation and
 parton shower development

In soft & collinear limit of QCD, emissions fill the Lund plane uniformly

$$\mathcal{P} \propto \alpha_s \frac{dk_T}{k_T} \frac{d\Delta R}{\Delta R} = \alpha_s d \ln(k_T) d \ln(\Delta R) \leftarrow \text{approximate self-similarity of QCD}$$

Promoting the Lund plane to a tool: the Lund jet plane

F. Dreyer, G. Salam, G. Soyez, JHEP12(2018)064



1. Jet is reclustered with Cambridge–Aachen algorithm (pairwise clustering with angular ordering)
2. Follow clustering tree in reverse (large \rightarrow small angles), **along the hardest branch**
3. Register kinematics of branching at each step

$$\Delta R = \sqrt{(y^{\text{softer}} - y^{\text{harder}})^2 + (\phi^{\text{softer}} - \phi^{\text{harder}})^2}$$

$$\text{CMS, ALICE} \quad k_{\text{T}} = p_{\text{T}}^{\text{softer}} \Delta R$$

$$\text{ATLAS} \quad z = p_{\text{T}}^{\text{softer}} / (p_{\text{T}}^{\text{harder}} + p_{\text{T}}^{\text{softer}})$$

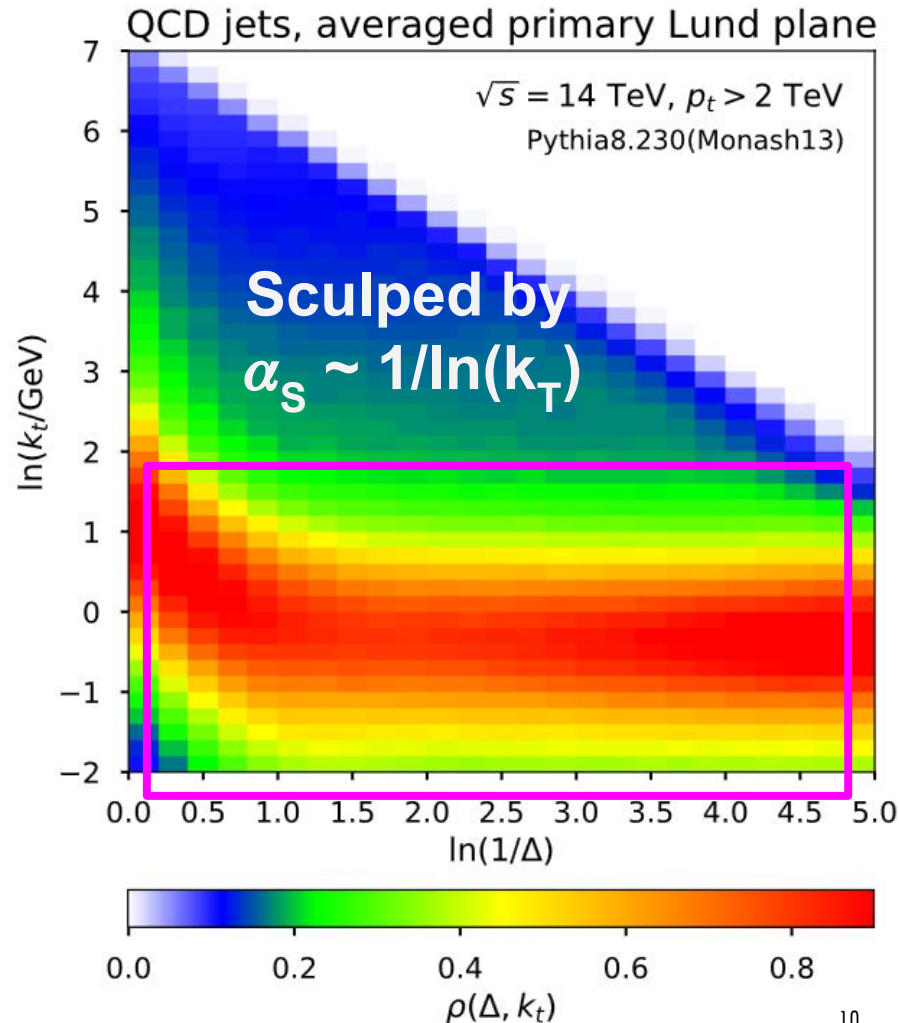
Define a *jet-averaged* number of emissions, the “primary” Lund jet plane density

$$\rho(k_T, \Delta R) \equiv \frac{1}{N_{\text{jets}}} \frac{d^2 N_{\text{emissions}}}{d \ln(k_T/\text{GeV}) d \ln(R/\Delta R)}$$

At leading order, it’s “sculpted” by $\alpha_S(k_T)$

$$\rho(k_T, \Delta R)_{\text{LO}} \approx \frac{2}{\pi} C_R^{\text{eff}} \alpha_S(k_T)$$

With $C_R = C_A = 3$ for $g \rightarrow gg$ or $C_F = 4/3$ for $q \rightarrow qg$

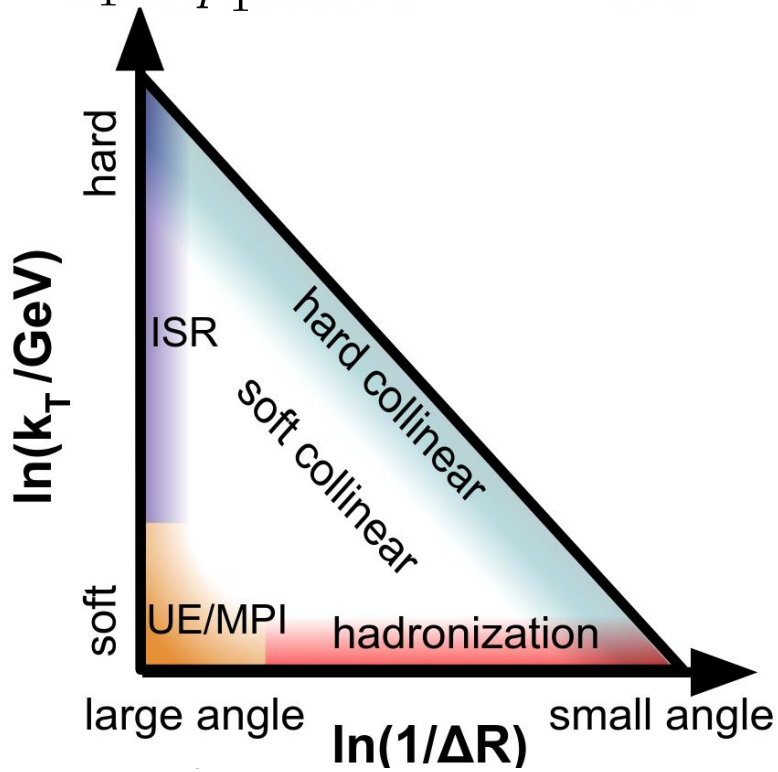


Mechanisms “factorize” in the Lund jet plane

F. Dreyer, G. Salam, G. Soyez, JHEP12(2018)064

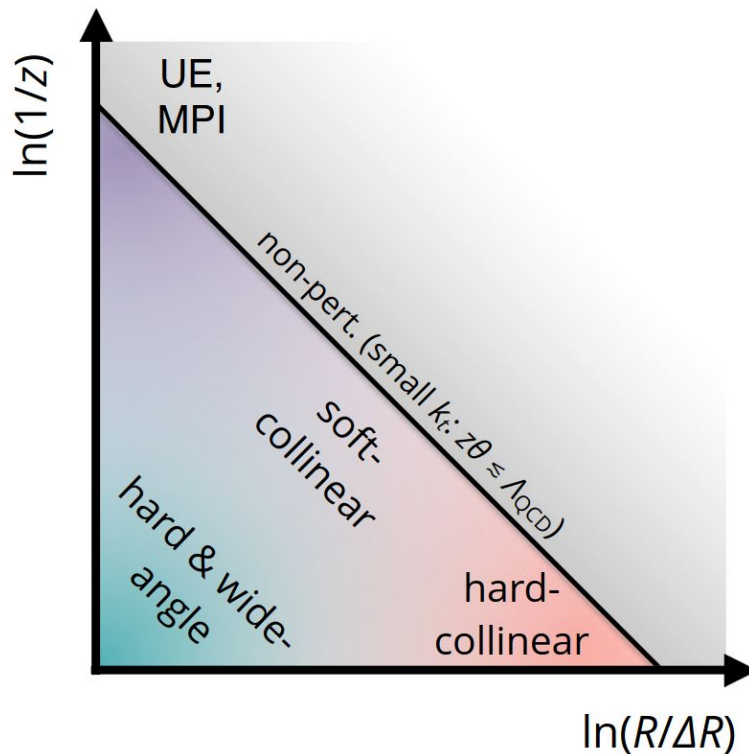
CMS Lund plane coordinates

$$k_T = p_T^{\text{softer}} \Delta R \quad \text{vs} \quad \Delta R$$



ATLAS Lund plane coordinates

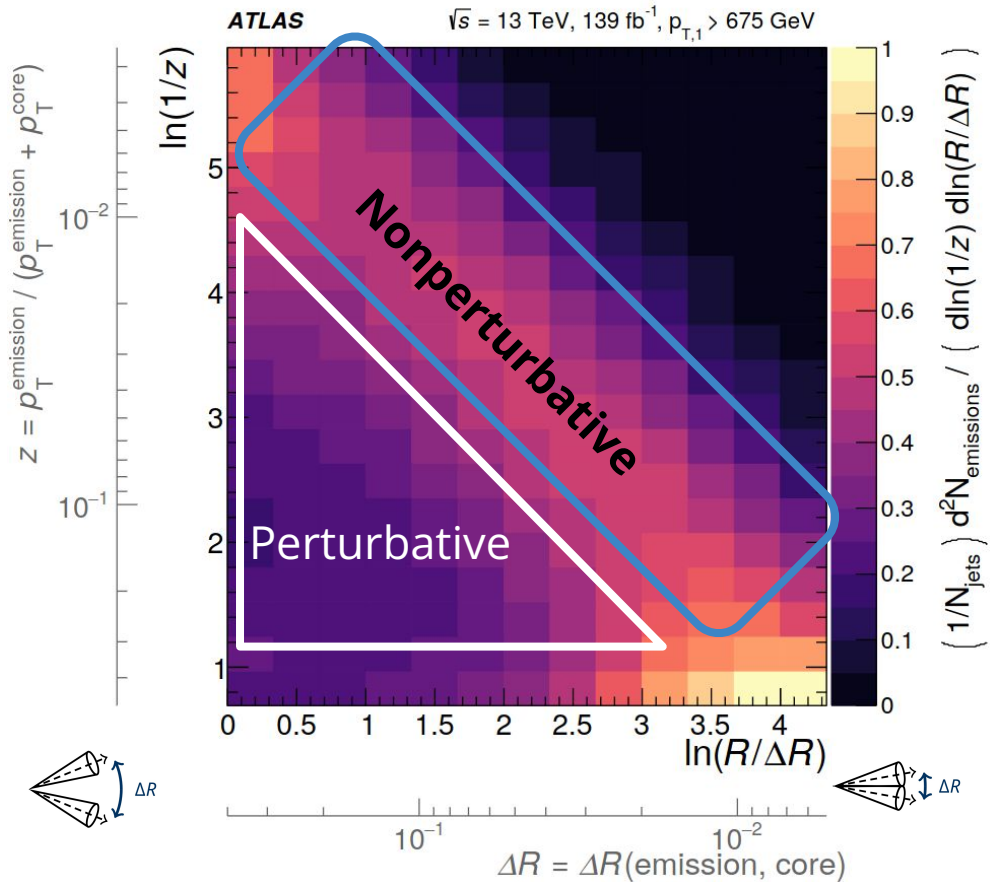
$$z = p_T^{\text{softer}} / (p_T^{\text{harder}} + p_T^{\text{softer}}) \quad \text{vs} \quad \Delta R$$



ATLAS primary Lund jet plane density

R=0.4 jets (standard R in Run-2)

[PRL 124, 222002 \(2020\)](#)



Dijet selection,

$$p_{T, \text{jet}1} > 675 \text{ GeV} \ \& \ p_{T, \text{jet}2} > \frac{2}{3} p_{T, \text{jet}1}$$

Charged-particle tracks for substructure

Momentum fraction of the emissions for vertical axis of Lund plane:

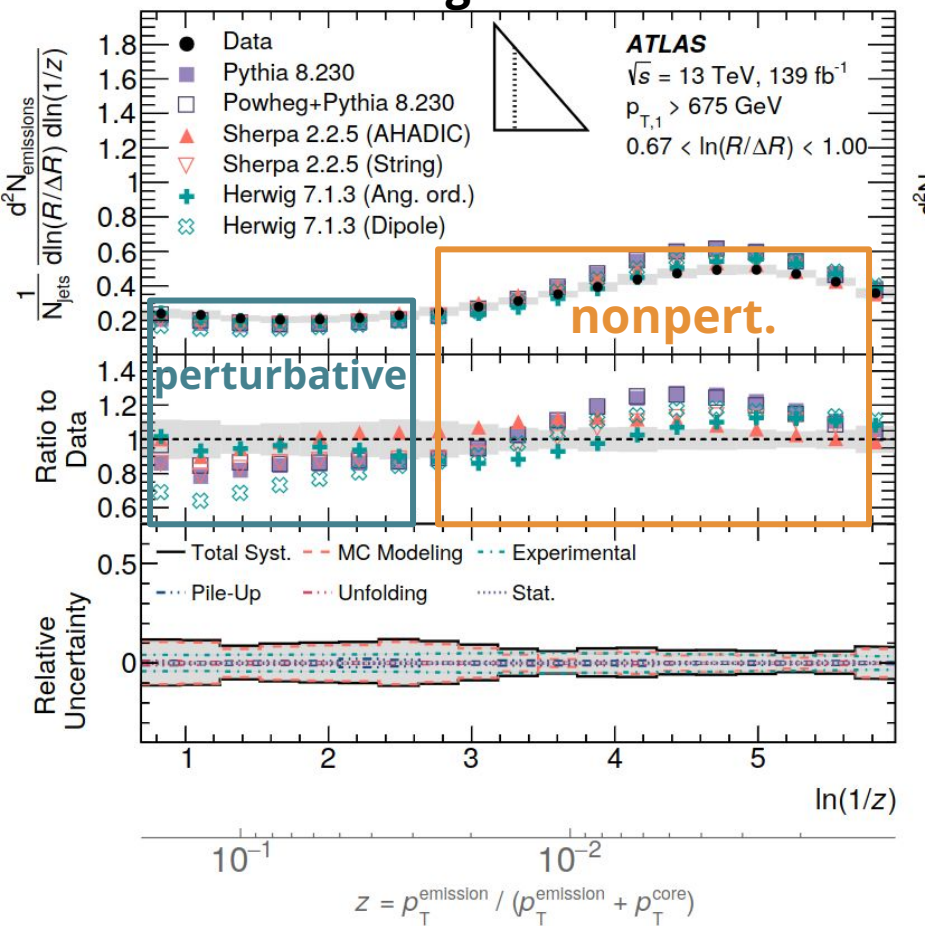
$$z = p_{T, \text{softer}} / (p_{T, \text{softer}} + p_{T, \text{harder}})$$

Multidimensional unfolding

Factorization properties in action (ATLAS)

[PRL 124, 222002 \(2020\)](#)

Fixed-angle slice



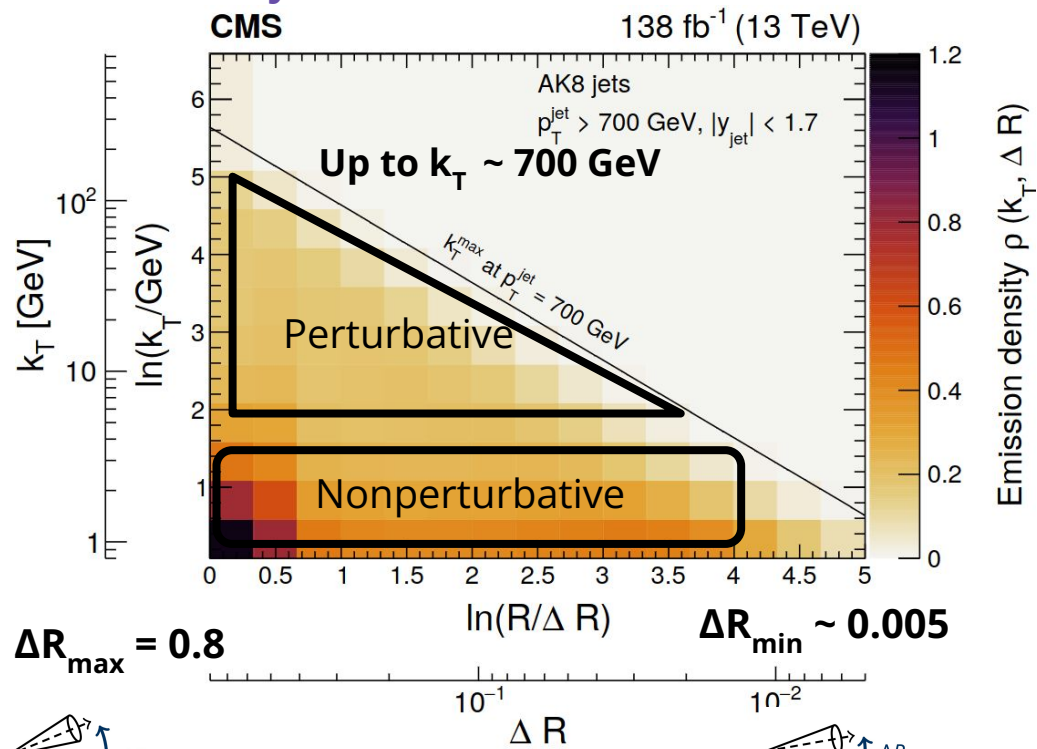
Variation of hadronization model,
 with the same parton shower
 (**Sherpa2 string vs hadronization**)

Variation of parton shower,
 same hadronization model
 (**Herwig7.1 angle vs dipole**)

CMS primary Lund jet plane densities

arXiv:2312.16343, accepted by JHEP

$R=0.8$ jets

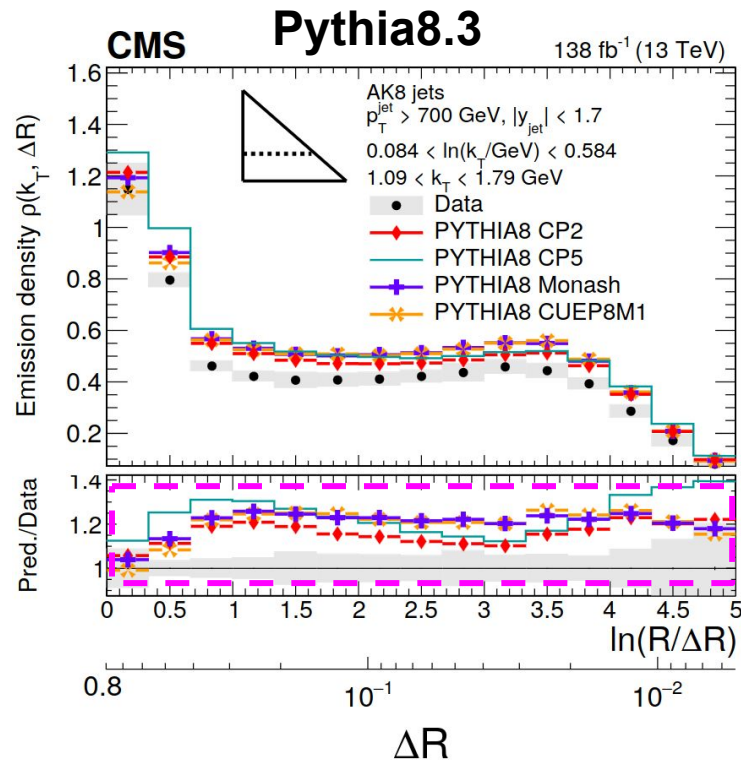


Probing k_T from $\sim 1 \text{ GeV}$ to 700 GeV ,
 and $0.005 < \Delta R < 0.8$

$$k_T = p_T^{\text{softer}} \Delta R$$

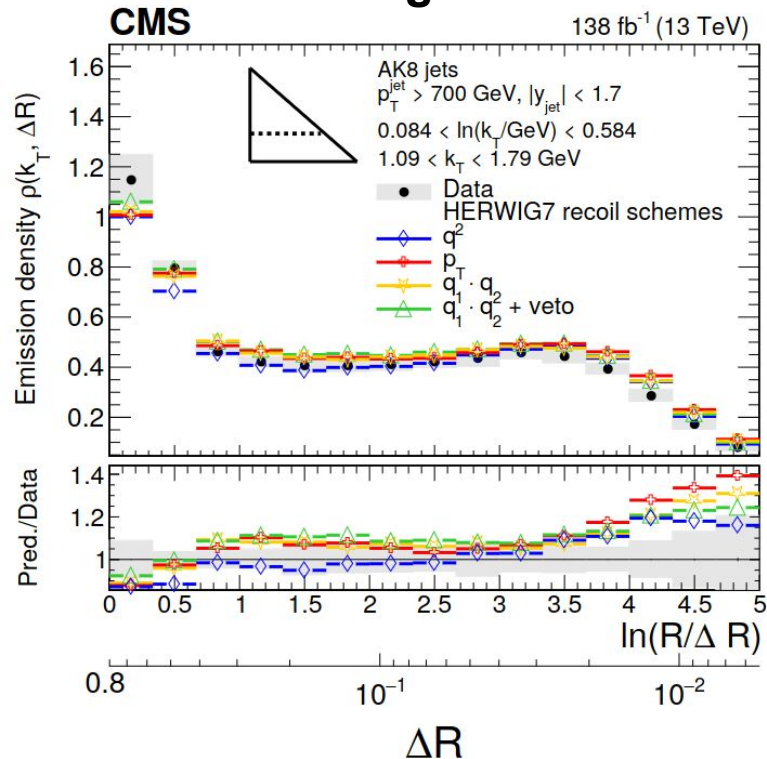
Lund vs cluster fragmentation?

Hadronization region ($k_T \sim 1$ GeV)



Lund string (**PYTHIA8** overshoots) data by 15-20% in hadronization region

Herwig7.2

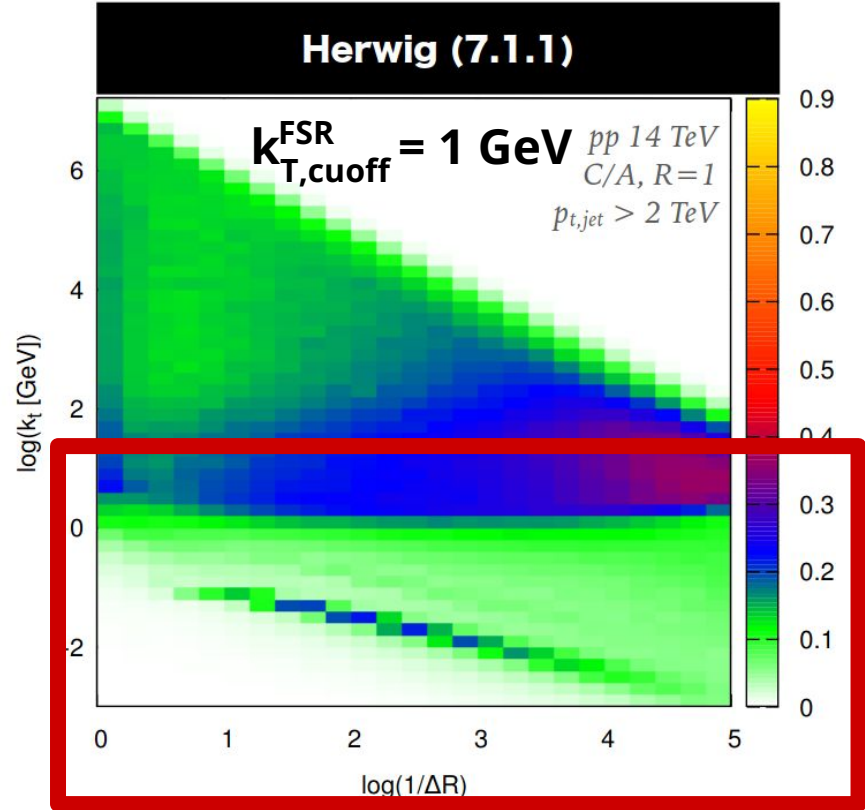
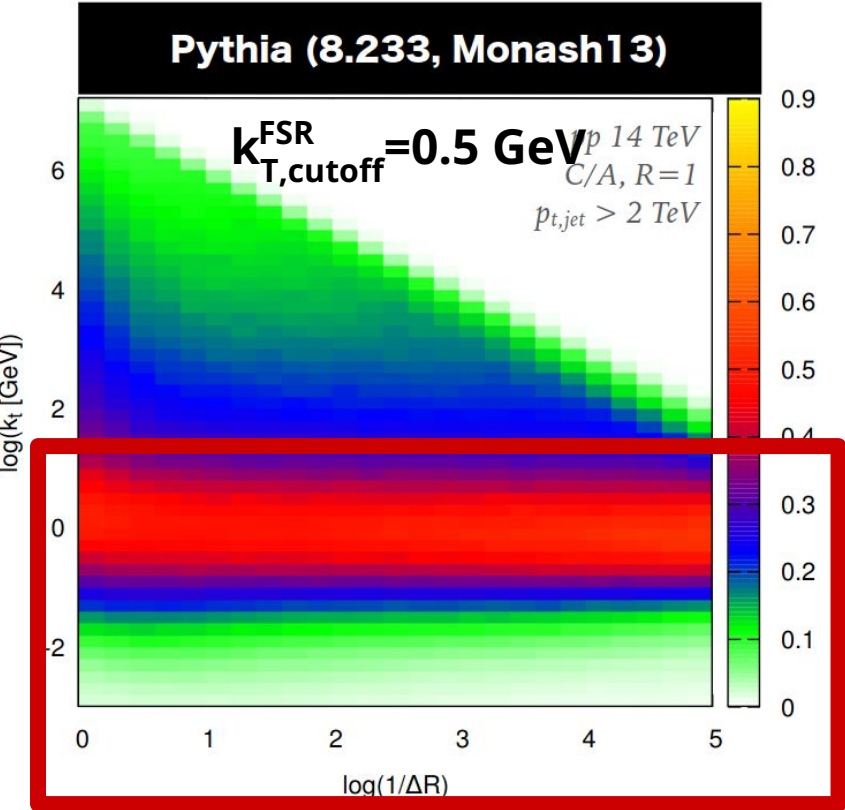


Cluster model in better agreement...
(HERWIG7/SHERPA2)

...Or could it be something else, e.g., the FSR k_T cutoff choice?

average pp Lund density: **parton level**

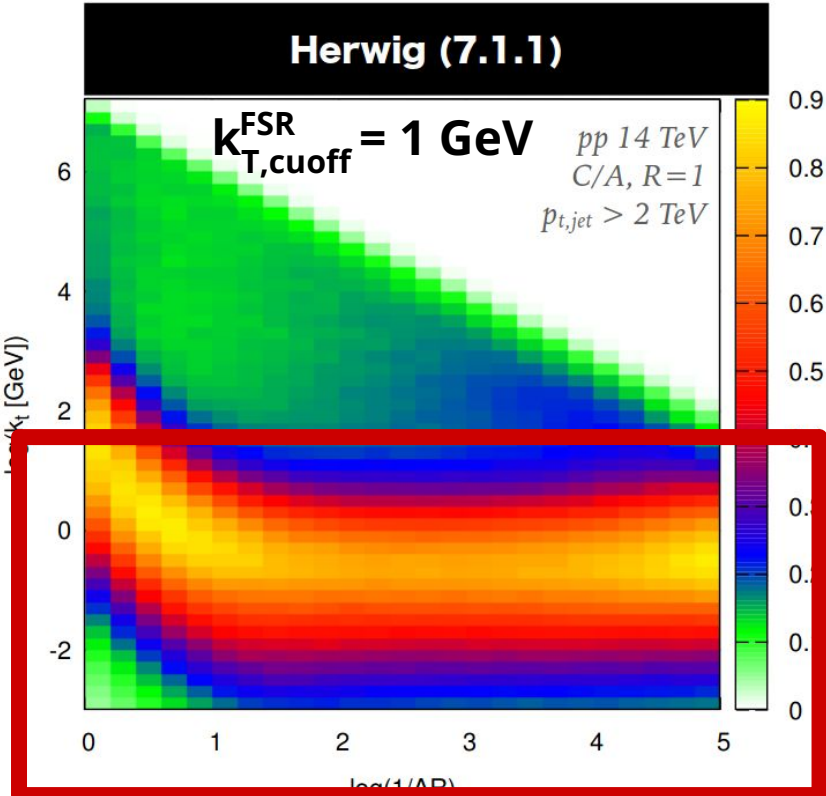
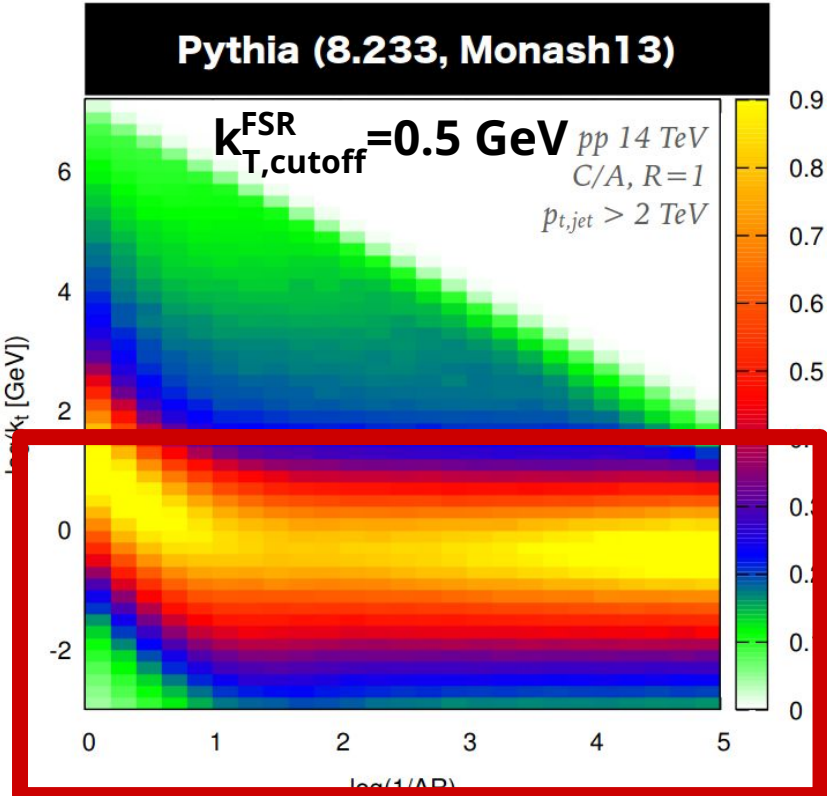
G. Salam's slide



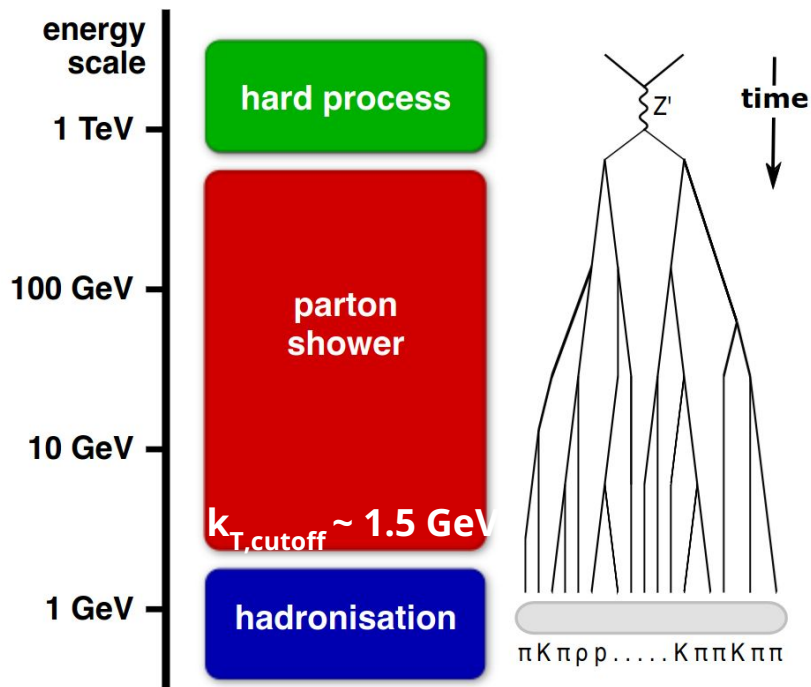
Hadron-level: FSR k_T cutoff choice shouldn't matter...

average pp Lund density: **hadron level (with underlying event / MPI)**

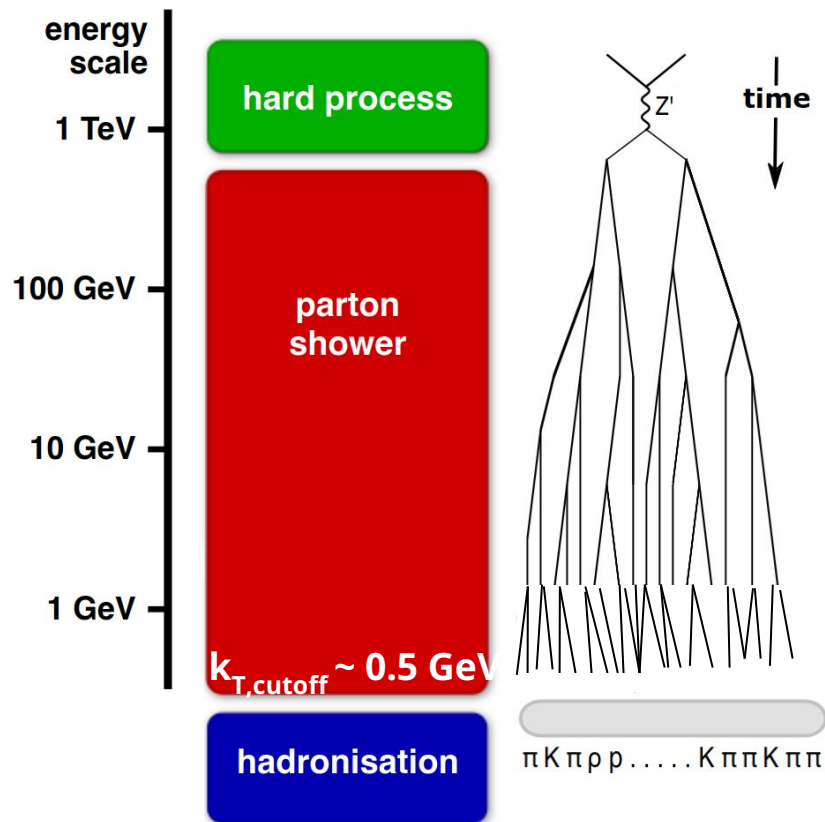
G. Salam's slide



Higher shower $k_{T,cutoff}$



Lower shower $k_{T,cutoff}$

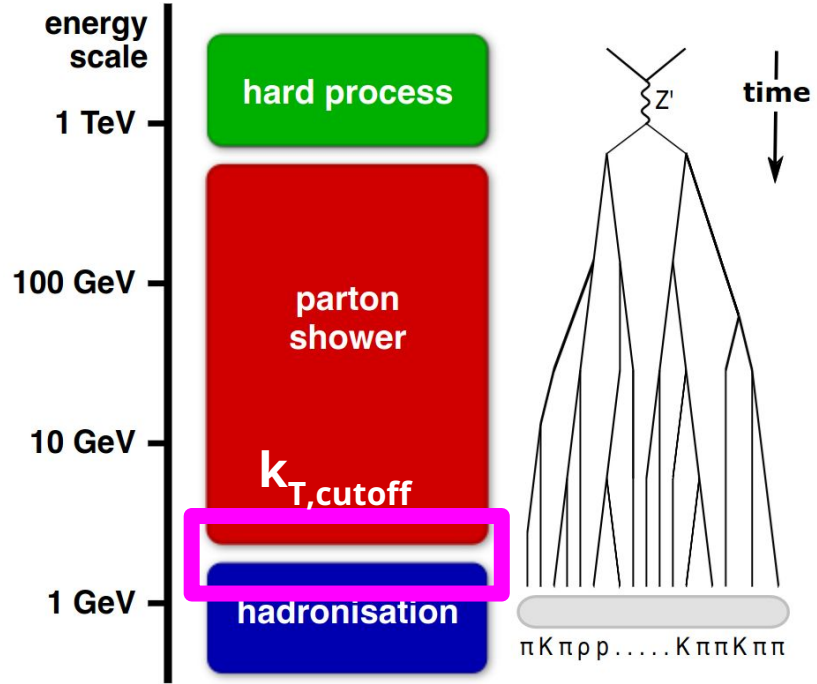
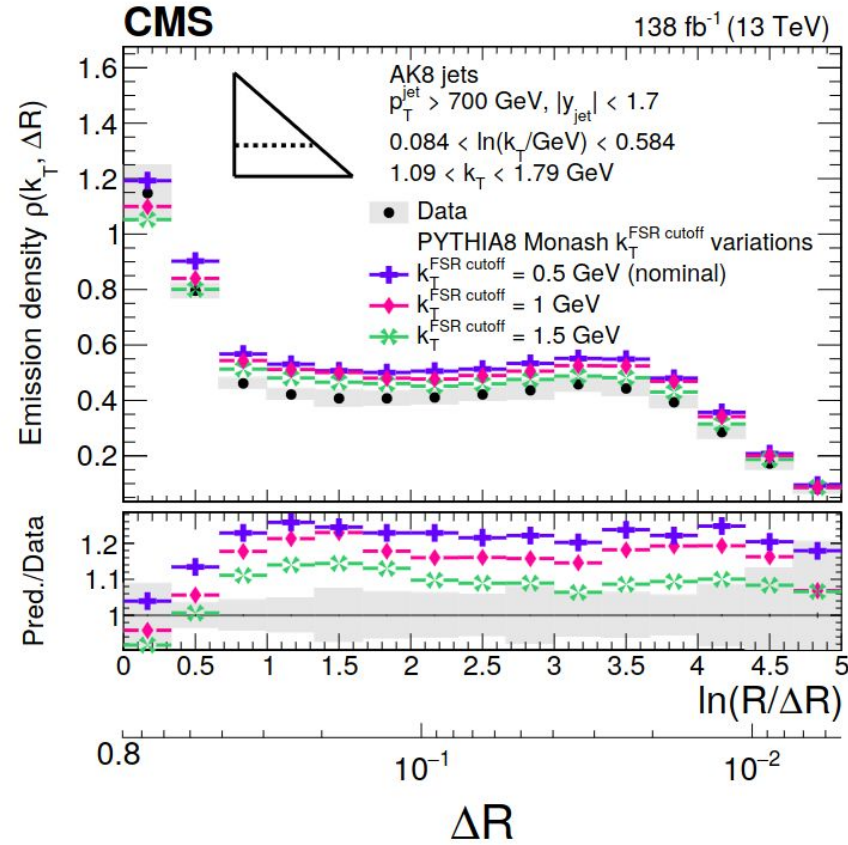


Could it lead to double counting?

PYTHIA8 shower $k_{T,cutoff}$ variations ($k_T \sim 1$ GeV)

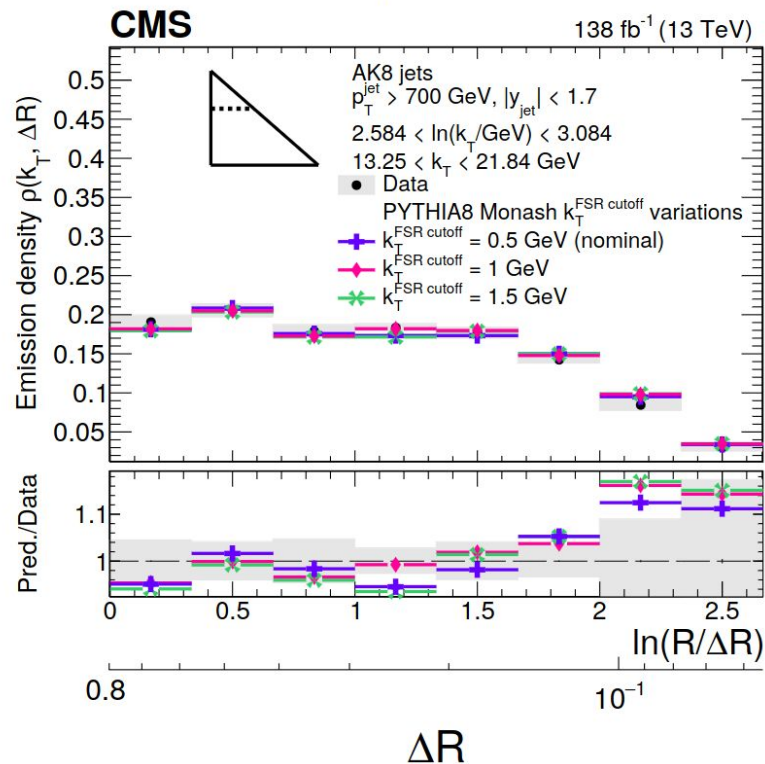
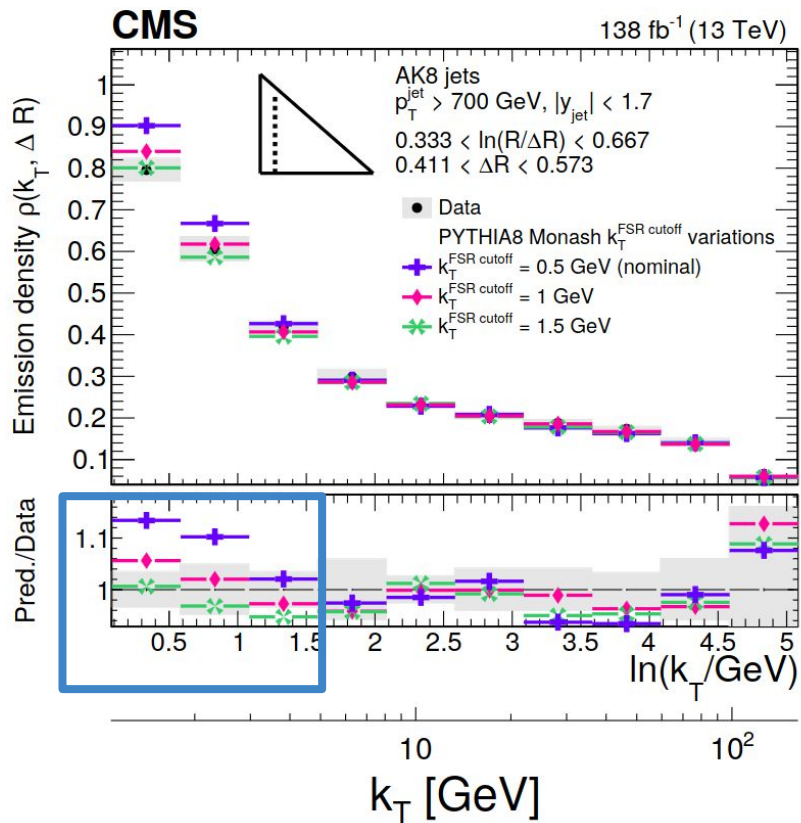
Larger FSR $k_{T,cutoff} \Leftrightarrow$ fewer Lund emissions

Data “prefers” higher FSR $k_{T,cutoff} = 1.5$ GeV for PYTHIA8



Low shower $k_{T,cutoff} \Rightarrow$ “double counting”

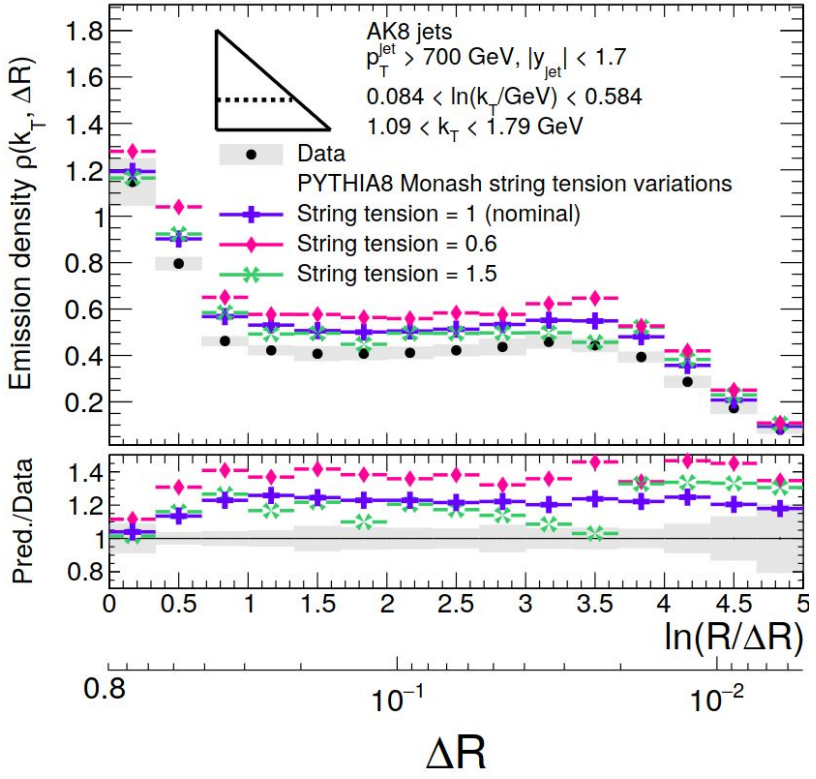
Shower $k_{T,cutoff}$ decouples at $k_T \sim 4$ GeV



String tension sensitivity

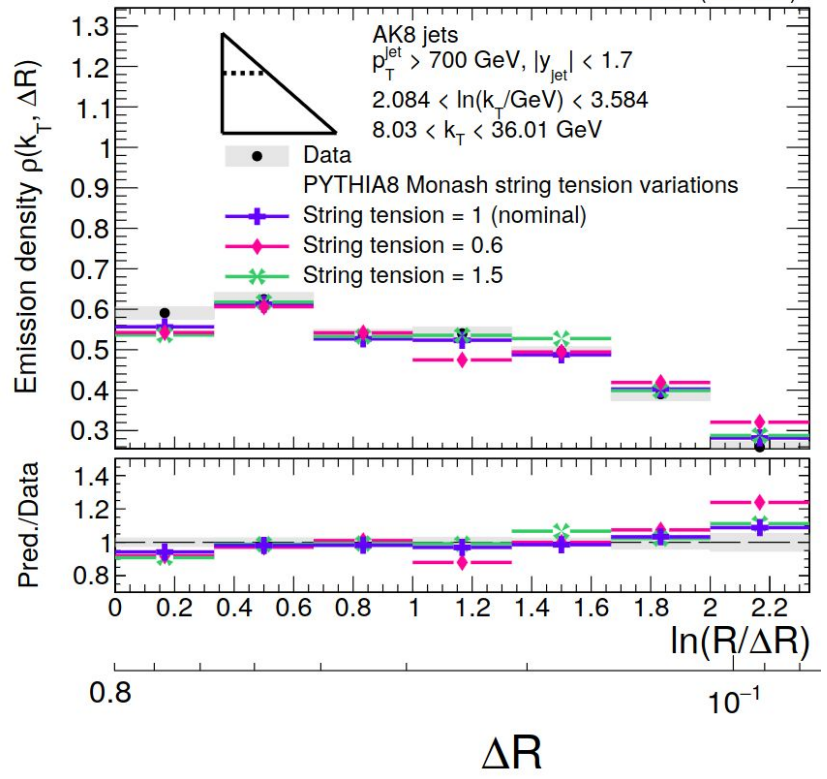
Low $k_T \sim 1$ GeV

138 fb⁻¹ (13 TeV)



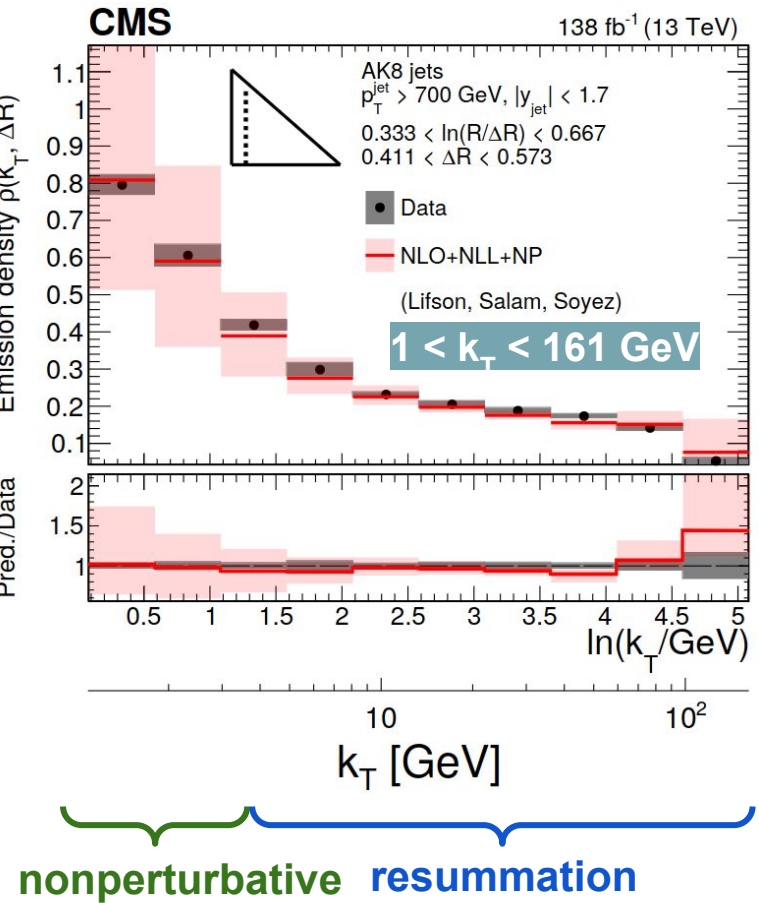
High $k_T > 8 - 36$ GeV

138 fb⁻¹ (13 TeV)

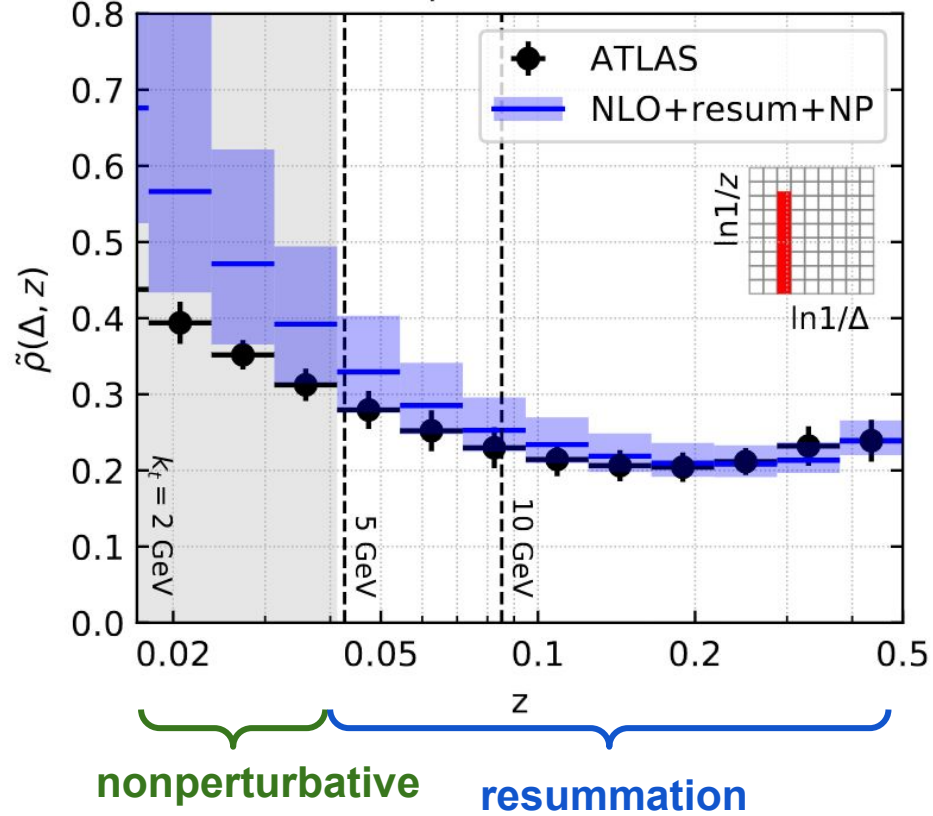


Similar onset for analytical calculations ($k_T \sim 3$ GeV)

Calculations from A. Lifson, G. Salam, G. Soyez [JHEP10\(2020\)170](https://arxiv.org/abs/1908.07548)

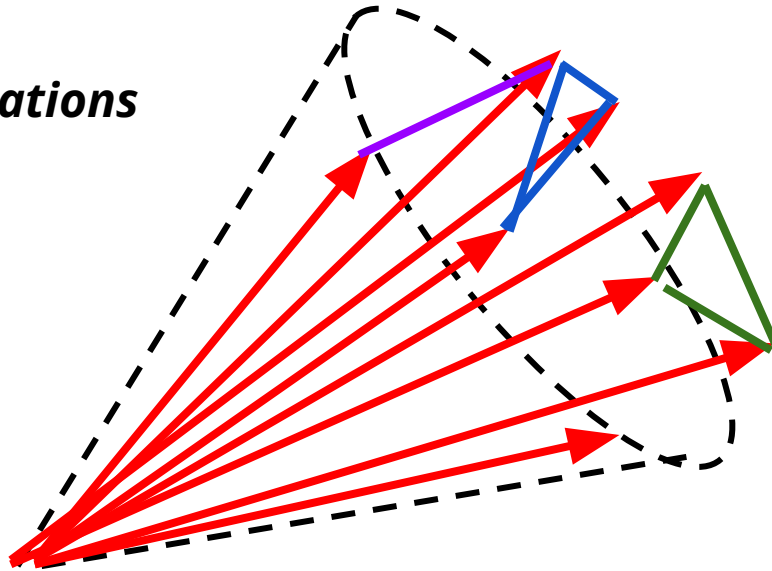


ATLAS setup: $0.147 < \Delta < 0.205$

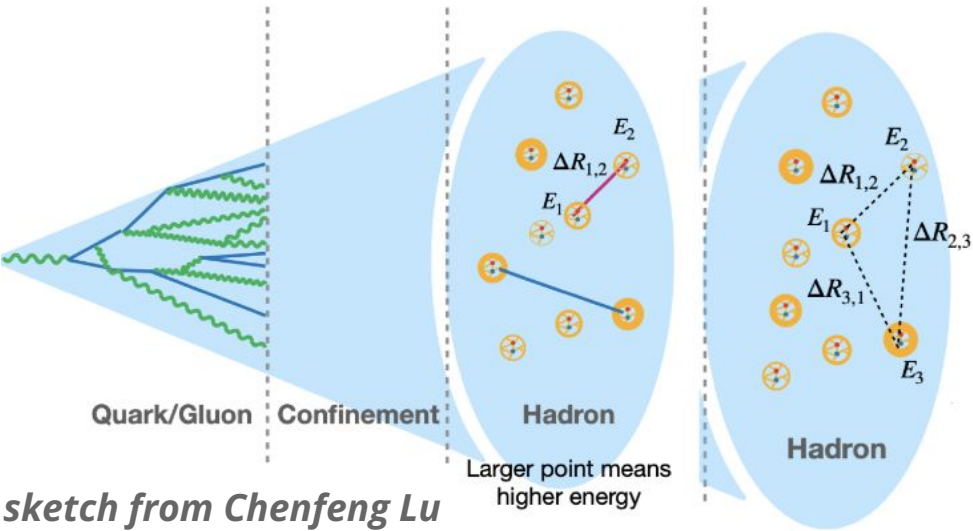


Energy-flow-based observables

N-particle correlations



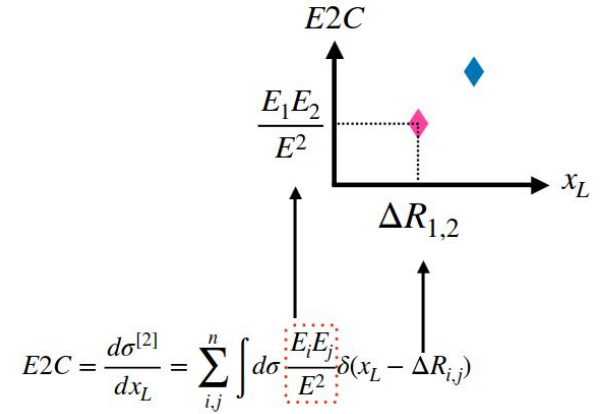
Energy-energy correlators



sketch from Chenfeng Lu

Mapping out different stages of jet formation

Energy-weighted two-particle correlations



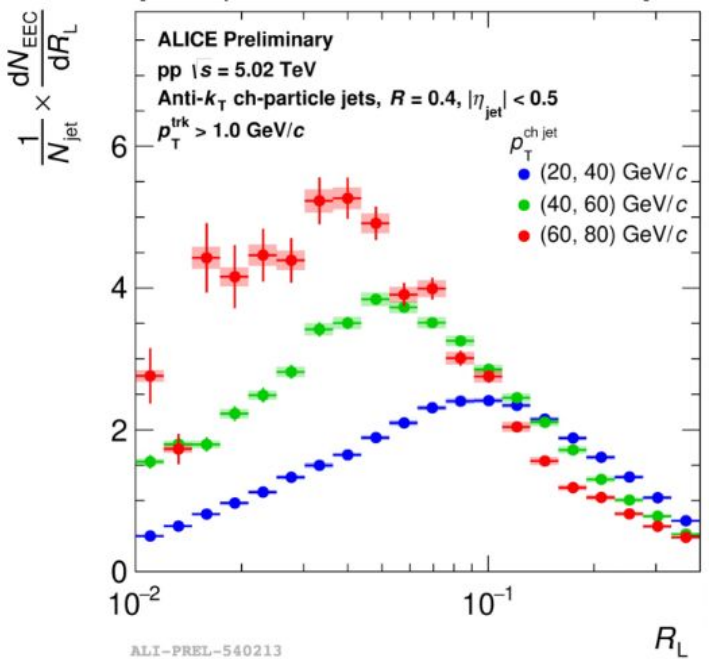
Angular separation $x_L == \Delta R_{ij} = \sqrt{\Delta y^2 + \Delta \varphi^2}$

Energy weights $E_i E_j$: hard pairs are rewarded, soft pairs are penalized

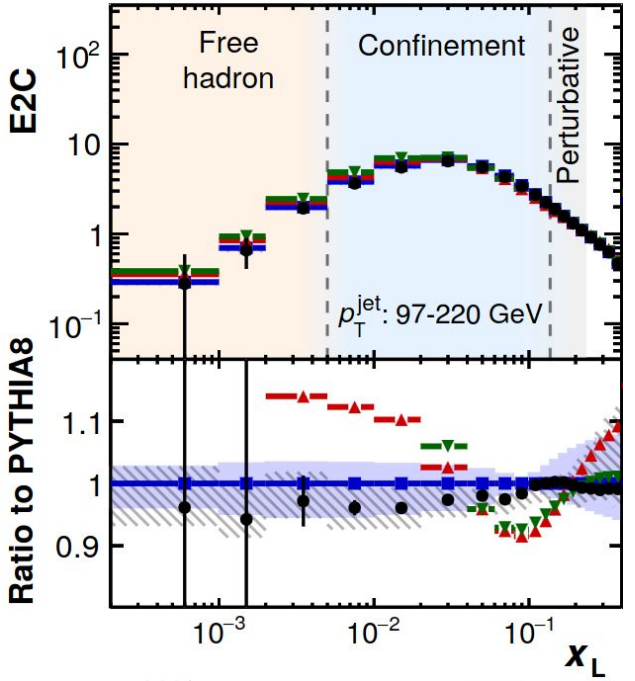
Proposed since the early days of QCD for e^+e^- , now explored specifically for jet substructure

Energy-energy correlators

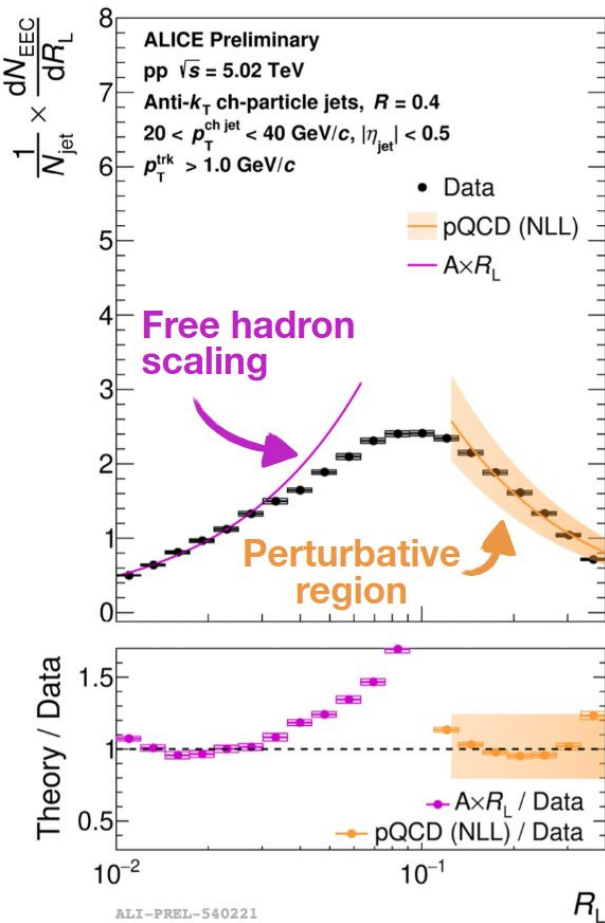
Separation of perturbative & nonperturbative regimes



CMS



Comparison to analytical calculations

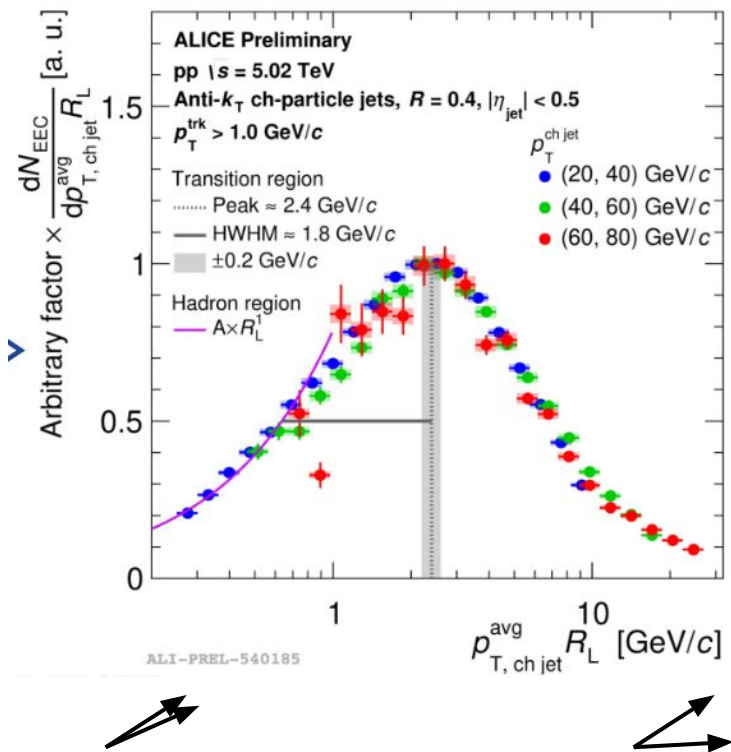
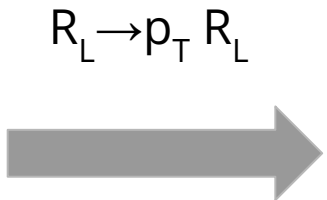
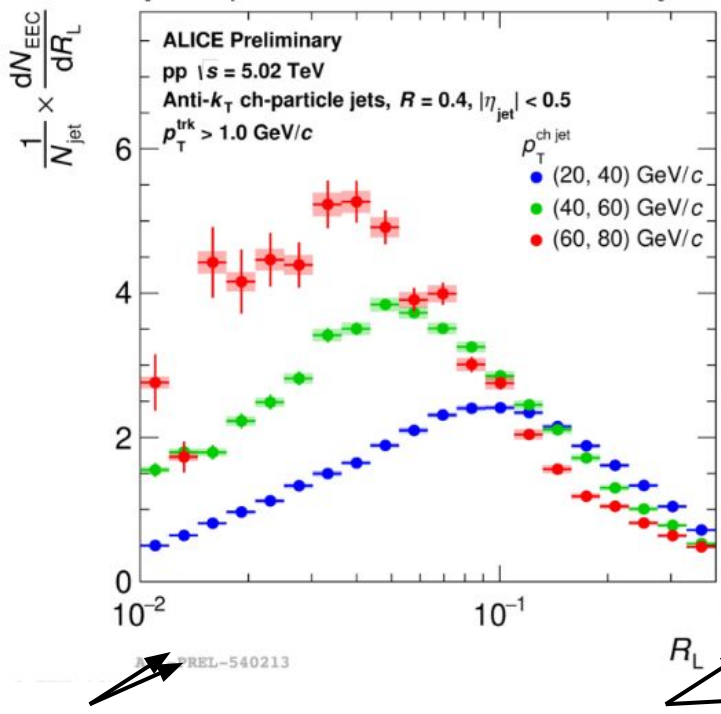


Based on K. Lee, B. Meçaj, I. Moutl [arXiv:2205.03414](https://arxiv.org/abs/2205.03414)

Perturbative region at high- R_L (NLO+NLL+NP)

At small R_L , free-hadron scaling is followed, deviation due to transition to short-distance physics

Scaling behavior with jet p_T

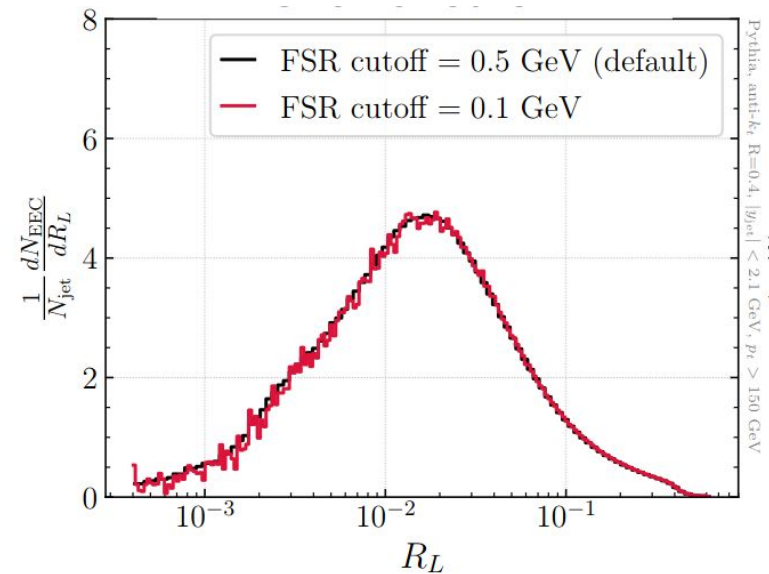


Peak of $p_T^{jet} R_L$ distribution suggests a characteristic universal scale $\lambda_{NP} \sim 2-3$ GeV

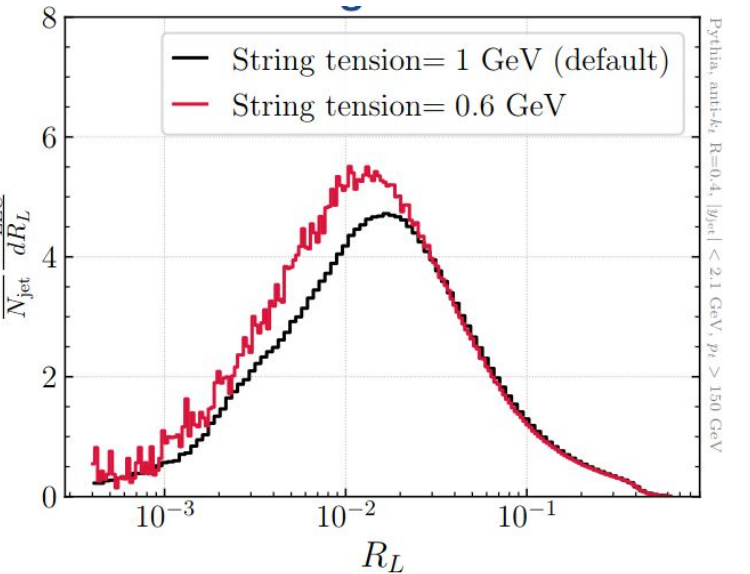
Sensitivity to infrared scales in MC

[A. Soto-Ontoso, [ECT* 2024 workshop](#)]

Shower $k_{T,cutoff}$



String tension



Not sensitive to FSR k_T cutoff (different from Lund plane), but sensitive to string tension

Comparison with MC generators

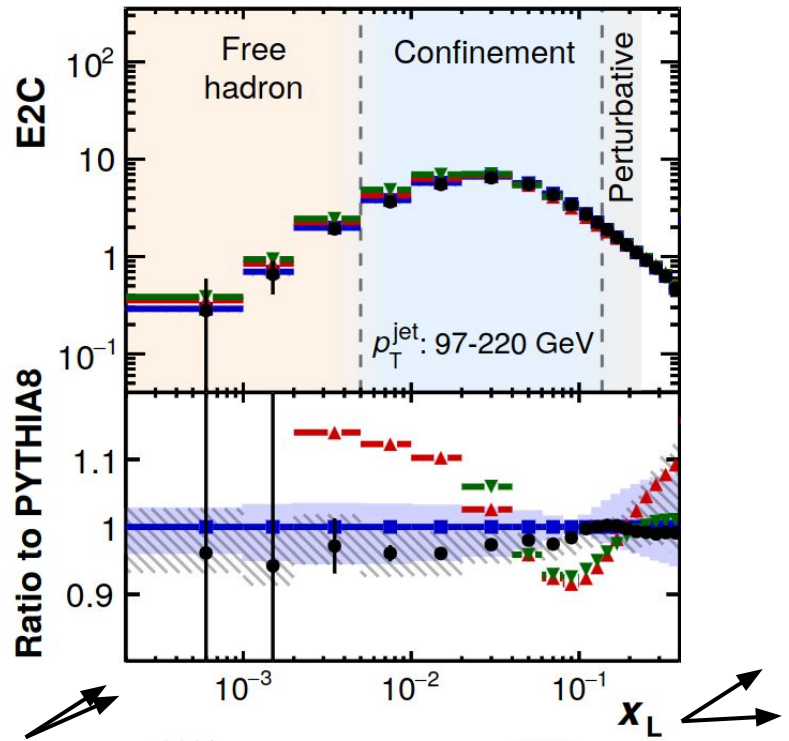
PYTHIA8 (string model) describes data in nonperturbative regions

HERWIG7/SHERPA2 (cluster models) off by ~20% at small x_L

(Seemingly) opposite conclusions wrt the Lund plane analyses

arXiv:2402.13864,
submitted to PRL

CMS

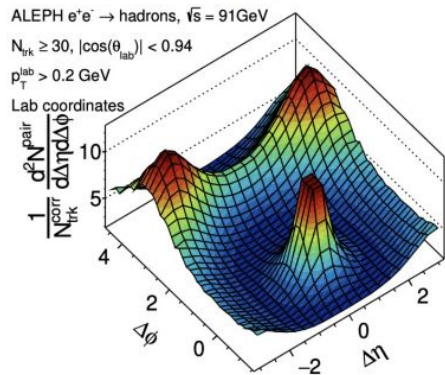


Two-particle angular correlations (*a la* heavy-ions)

Unexpected nonzero v_2 in high-multiplicity pp and pPb by CMS (PLB 765 (2017) 193, PLB 718 (2013) 795)

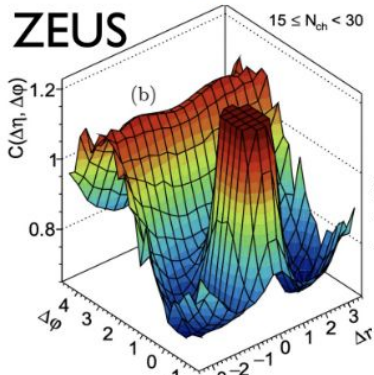
Since then, searches pushing the boundaries towards even smaller systems

e^+e^-
 $N_{ch} \sim 30$



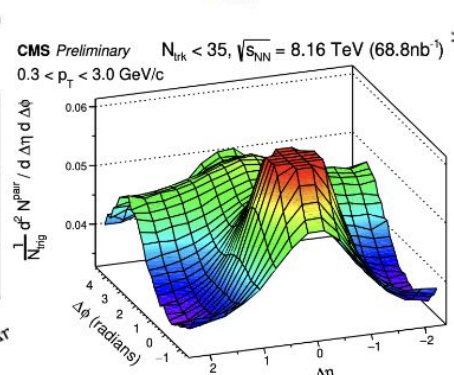
PRL 123 212002 (2019)
Cristian Baldenegro (Sapienza)

ep
 $N_{ch} \sim 30$



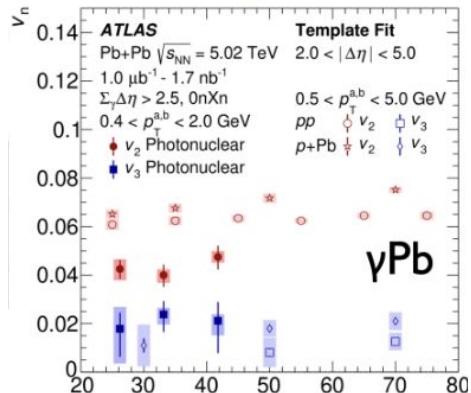
JHEP 04 (2020) 070

γp
 $N_{ch} \sim 20$



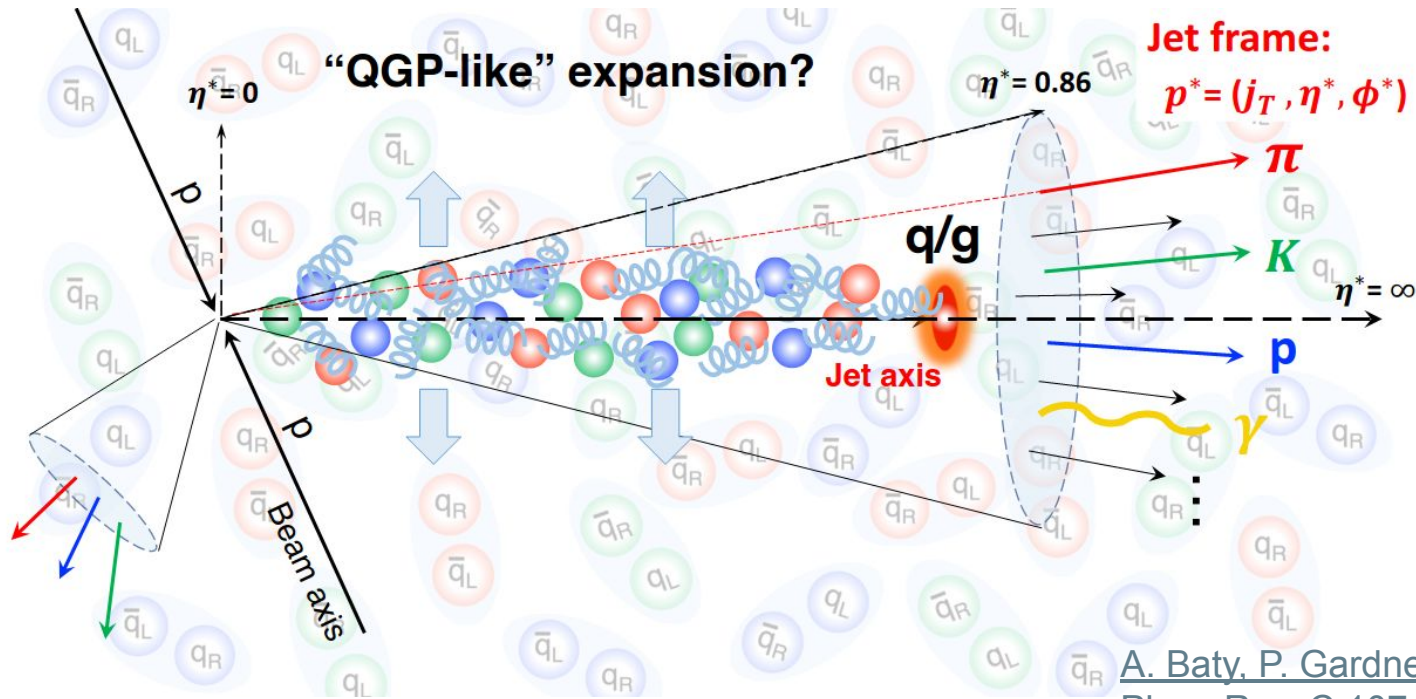
PLB 844 (2023) 137905
nonpQCD&topology @ CERN-TH

γPb
 $N_{ch} \sim 40$



PRC, 104 014903 (2021)³⁰

Search for intrajet collective behavior (small system?)



A. Baty, P. Gardner, W. Li,
[Phys. Rev. C 107 \(2023\) 064908](#)

high N_{ch} category

CMS

138 fb⁻¹ (pp 13 TeV)

CMS

138 fb⁻¹ (pp 13 TeV)

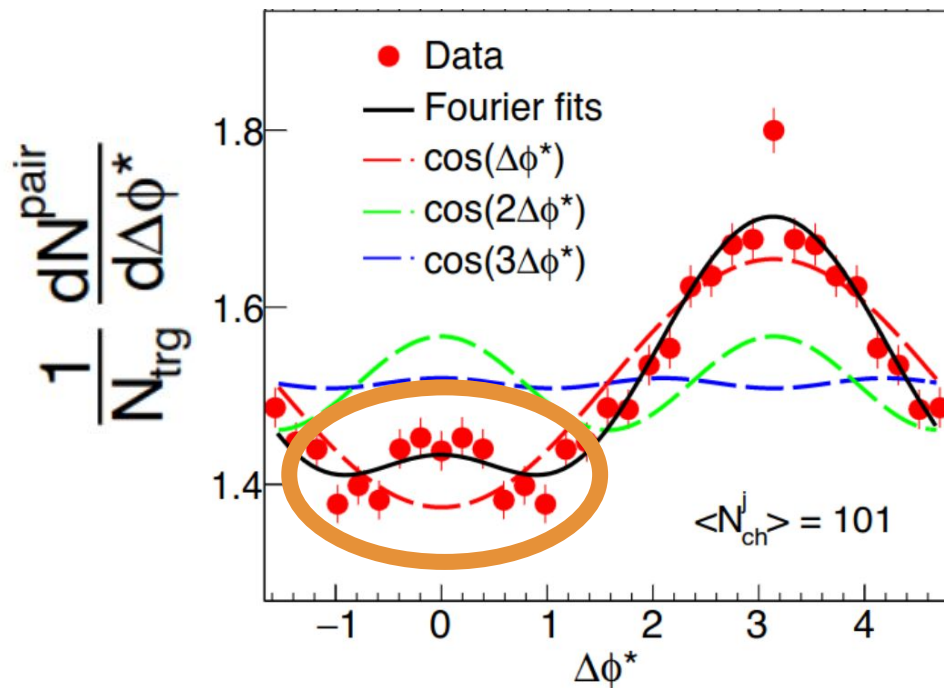
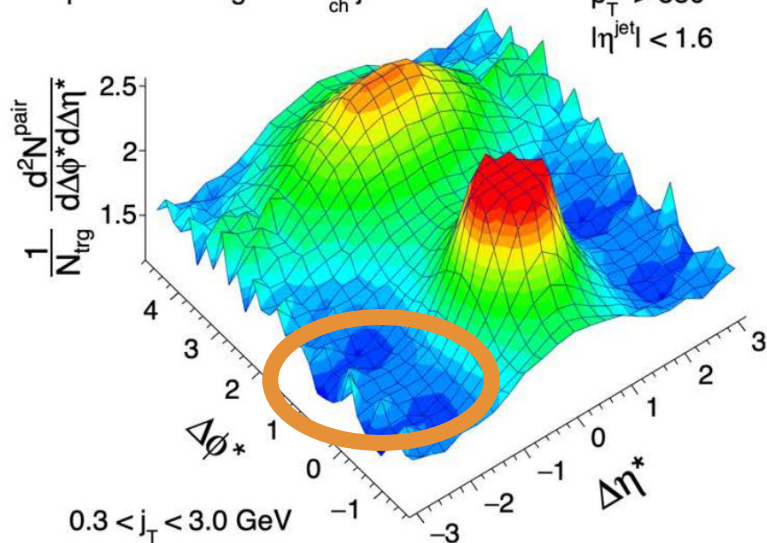
$$\langle N_{ch}^j \rangle = 101$$

Top 0.0023% highest- N_{ch}^j jets

Anti k_T R=0.8

$$p_T^{jet} > 550$$

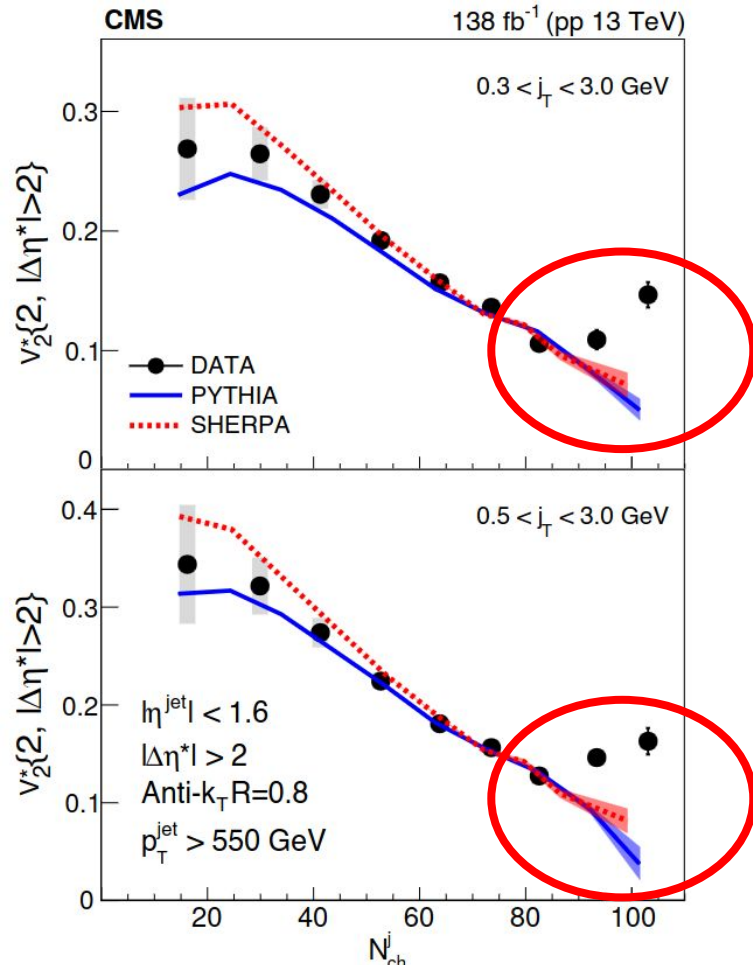
$$|\eta^{jet}| < 1.6$$



Near-side ridge-like structure at $\Delta\phi^ \sim 0$*

single-particle $v_2 = \sqrt{V_2}$ vs N_{ch}

[arXiv:2312.17103](https://arxiv.org/abs/2312.17103), submitted to PRL



Nonzero v_2 reproduced by
SHERPA2, PYTHIA8 CP5 up to $N_{ch} \sim 80$

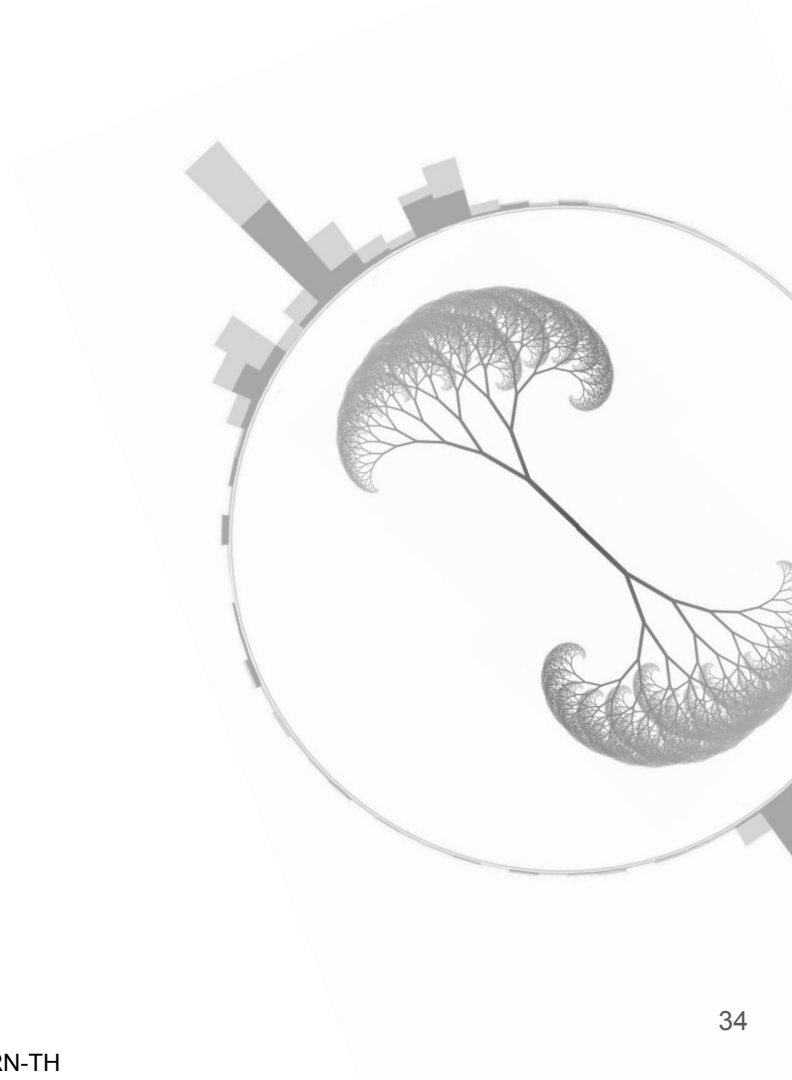
Increasing v_2 with large N_{ch}
not described by these MC predictions

Could be extended (e.g., EEC in $\Delta\eta$ - $\Delta\phi$?
Lund emissions as function of $k_{T,cut}$?)

Summary

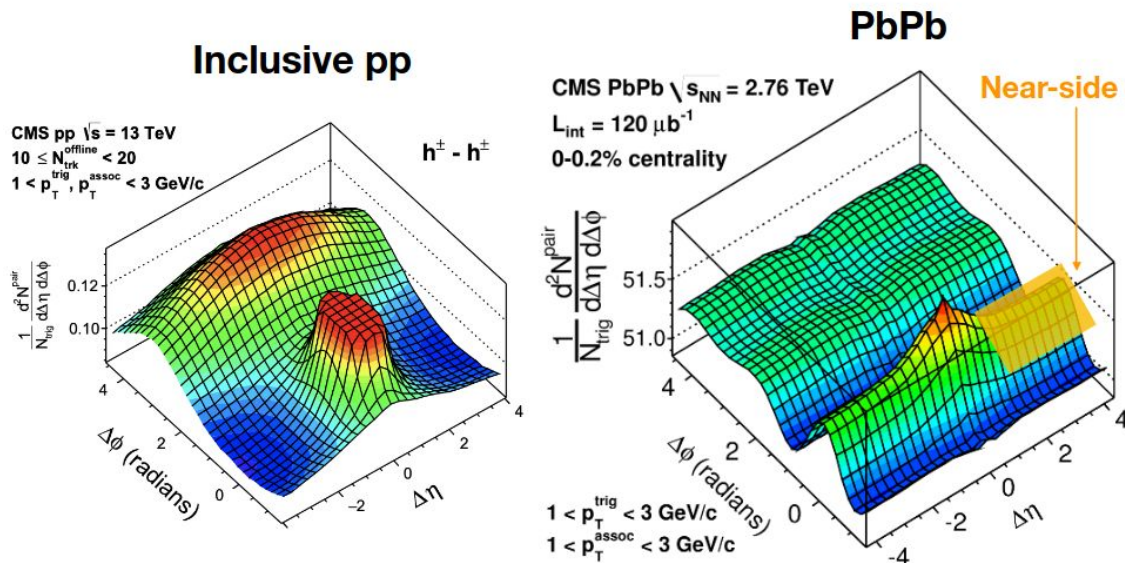
- Mapping out weakly- and strongly-coupled regimes via the **Lund jet plane picture** and with **N-point energy correlators**
- Collective-like behavior in jets with high- N_{ch}

Example of synergy between heavy-ion & high-energy communities
- Lund plane & EECs have complementary sensitivities to infrared scales



Two-particle angular correlations (*a la* heavy-ions)

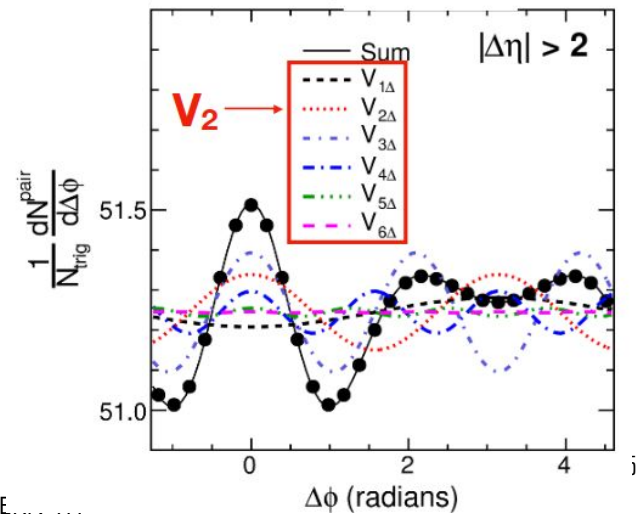
- **Near-side ridge** typical sign of collective behavior
- Fourier harmonics decomposition, nonzero $V_{2\Delta}$ associated with anisotropic expansion



$$\frac{1}{N_{\text{ch}}} \frac{dN^{\text{pair}}}{d\Delta\phi} \propto \sum_{n=1}^{\infty} V_{n\Delta} \cos(n\Delta\phi)$$

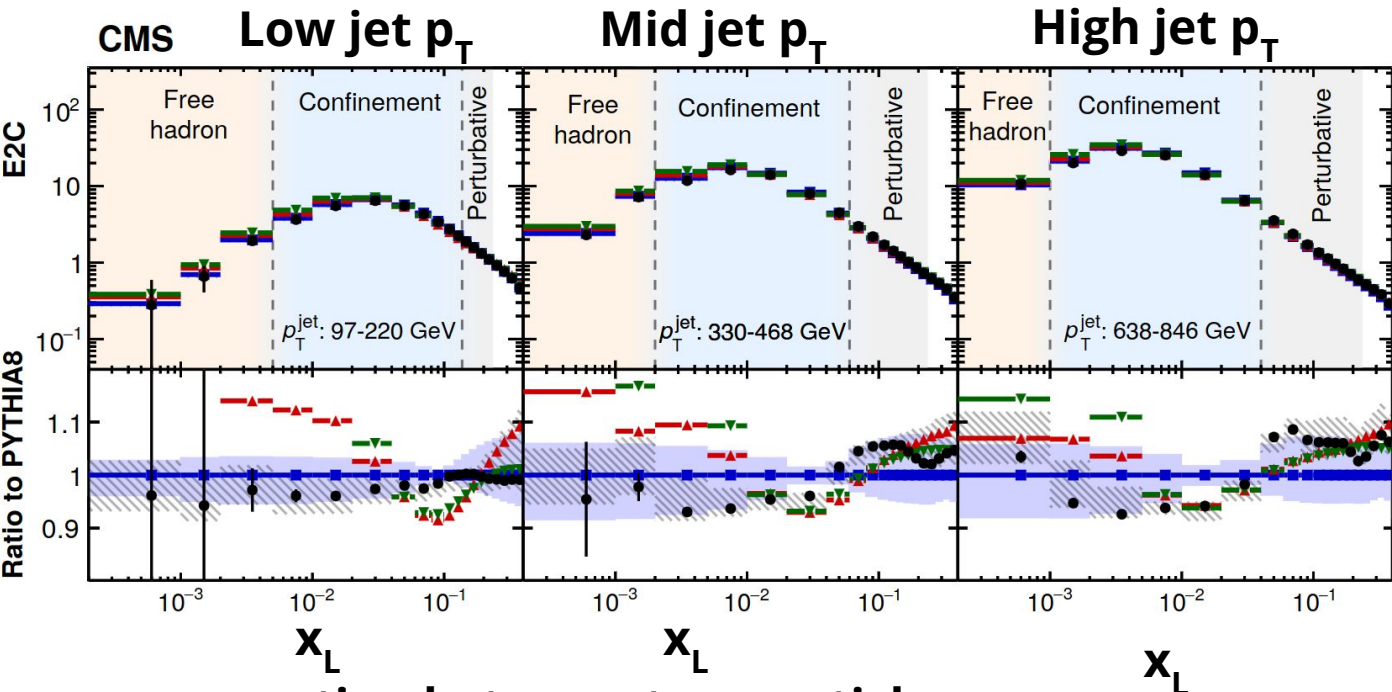
CMS PbPb $\sqrt{s_{\text{NN}}} = 2.76$ TeV
 $L_{\text{int}} = 120 \mu\text{b}^{-1}$
 0-0.2% centrality

1D slice



CMS, Phys. Lett. B 765 (2017) 193

Two-point correlators (E2C)



Free hadron region (low x_L)

PYTHIA8 CP5 describes data better than **HERWIG7 CH3/SHERPA2**

Perturbative region (high x_L)

PYTHIA8 CP5 undershoots data at higher jet p_T

HERWIG7 CH3 & SHERPA2 describe data better

x_L == separation between two particles

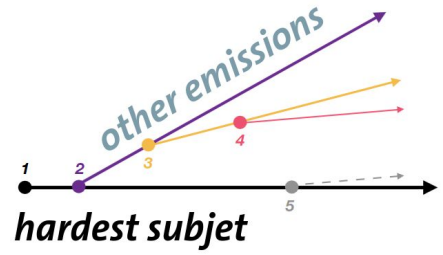
- Data
- PYTHIA8 CP5 (p_T ord.)
- ▲ HERWIG7 CH3 (ang. ord.)
- ▼ SHERPA2

ATLAS Lund subjet multiplicities

Proposed by [R. Medves, A. Soto-Ontoso, G. Soyez, JHEP04\(2023\)104](#)

[arXiv:2402.13052](#),
submitted to *PLB*

Count emissions with $k_T > k_{T,cut}$.
Using the **full** Lund jet tree (N_{Lund})
or for primary Lund emissions ($N_{Lund}^{primary}$)

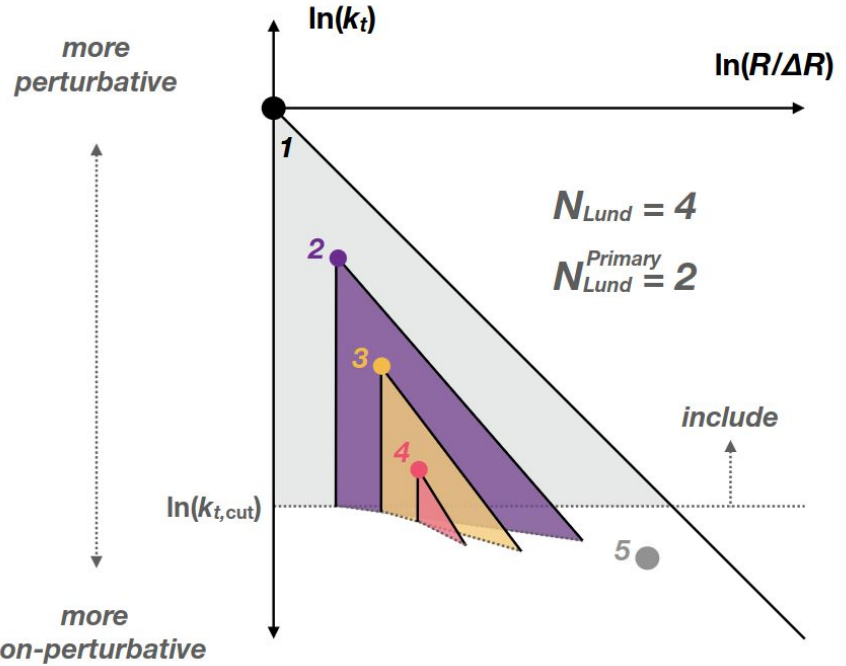


More inclusive observable, closely related to (sub)jet multiplicities at LEP

Charged-particles for substructure, data-based rescaling for an effective full-particle k_T

$$k_{T,eff} = k_{T,ch} * (p_{T,jet}^{ch} / p_{T,jet})$$

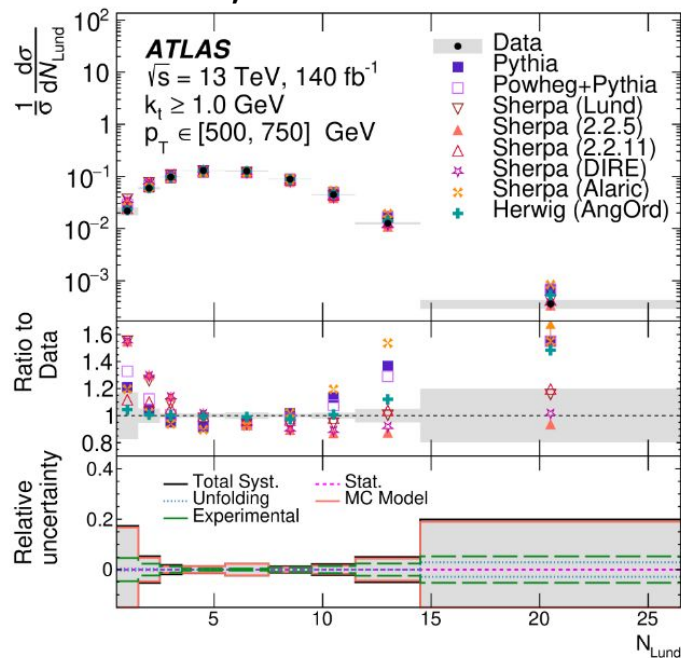
charged-to-full rescaling factor



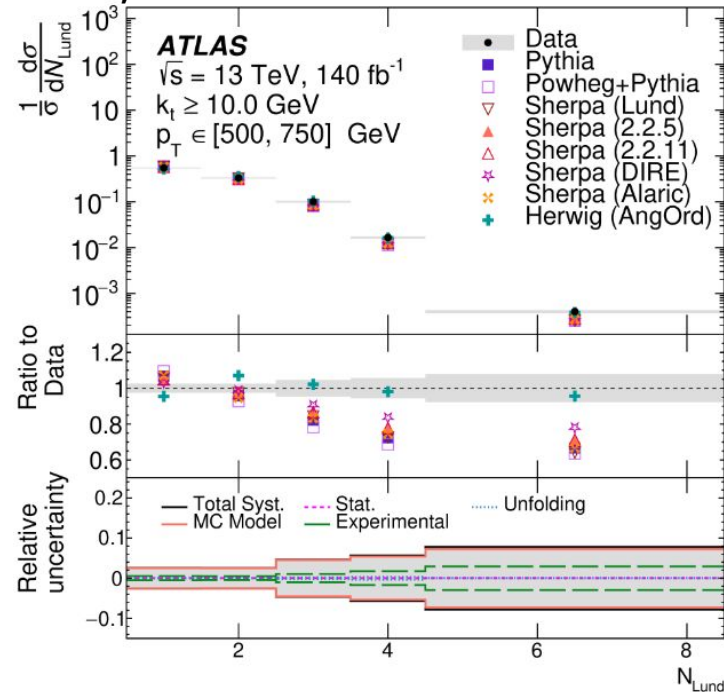
Lund subjet multiplicity distributions

Unfolded to the particle level, correcting jet p_T & subjet multiplicity for a given $k_{T,cut}$

$k_{T,cut} = 1 \text{ GeV (soft)}$



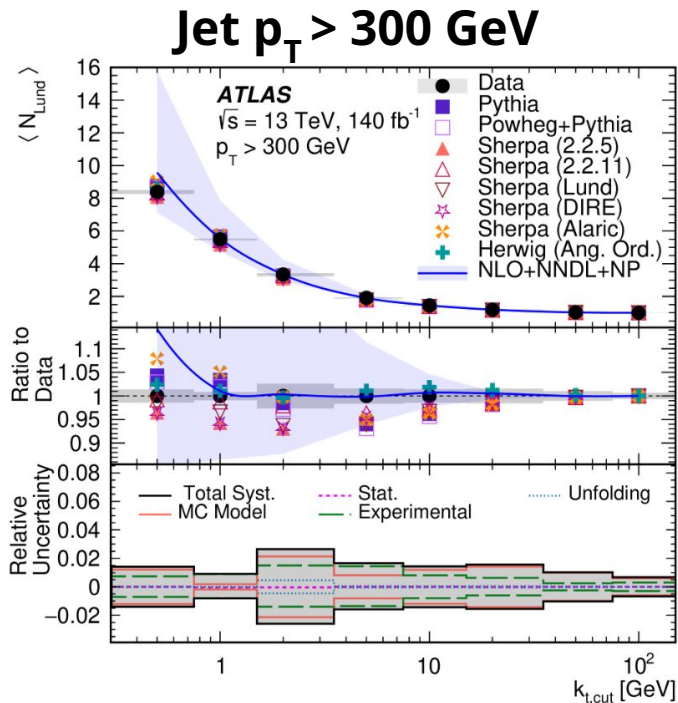
$k_{T,cut} = 10 \text{ GeV (hard)}$



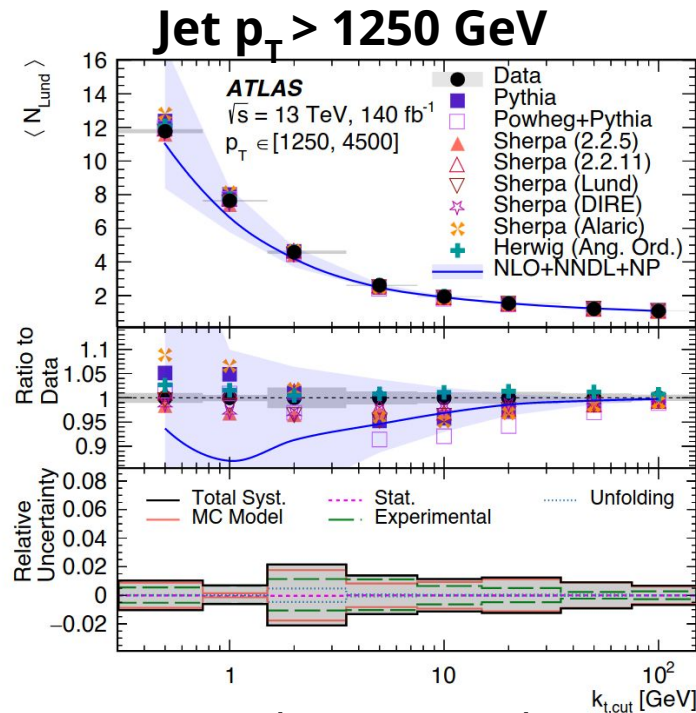
Challenging to describe high- N_{Lund} tails

Sherpa2 describes the $k_{T,cut} = 1 \text{ GeV}$ category better. Better global description by **Herwig7** angle-ordered

averaged Lund subjet multiplicities vs $k_{T, \text{cut}}$



In good agreement with pQCD calculation (NLO+NNDL+NP), high-order resummation



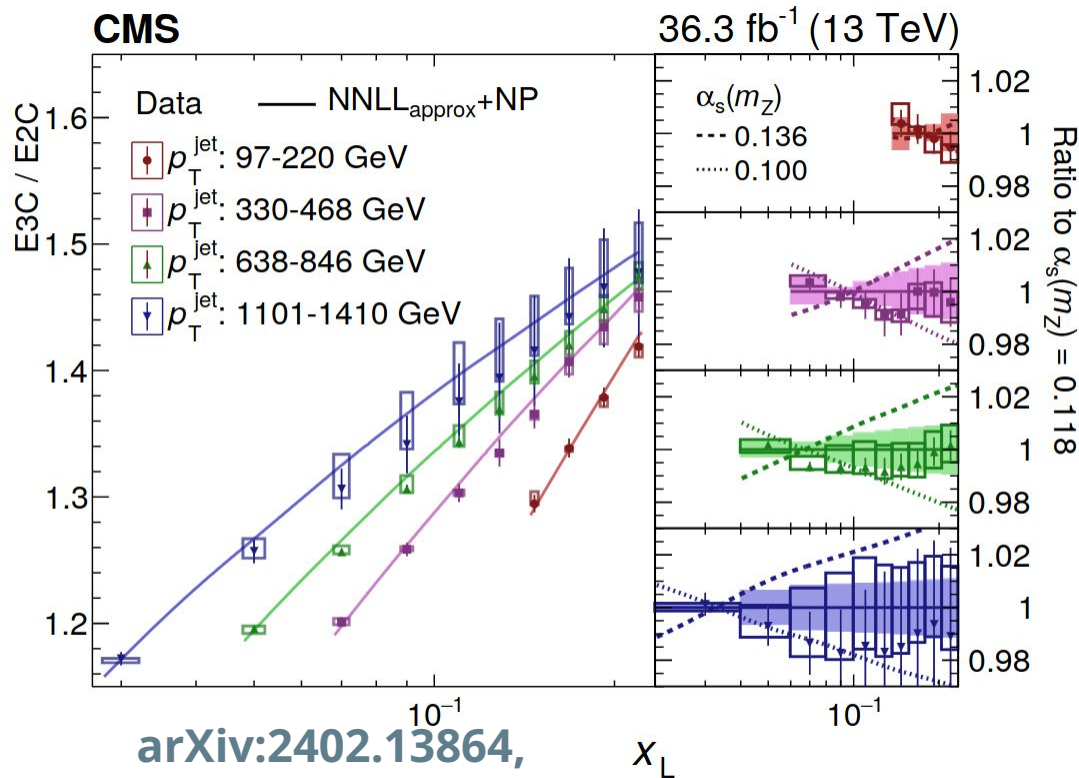
Better description by **Herwig7 angle-ordered**

$$\langle N^{(\text{Lund})}(\alpha_s; L) \rangle = \left[\underbrace{h_1(\alpha_s L^2)}_{\text{DL}} + \underbrace{\sqrt{\alpha_s} h_2(\alpha_s L^2)}_{\text{NDL}} + \underbrace{\alpha_s h_3(\alpha_s L^2)}_{\text{NNDL}} + \dots \right]$$

Other MCs tend to **undershoot** 39

Extraction of α_s from jet substructure

Ratio of three-point to two-point correlators (E3C/E2C)



arXiv:2402.13864,
submitted to PRL

Using **NLO+NNLL_{approx}** pQCD calculation
with nonperturbative corrections

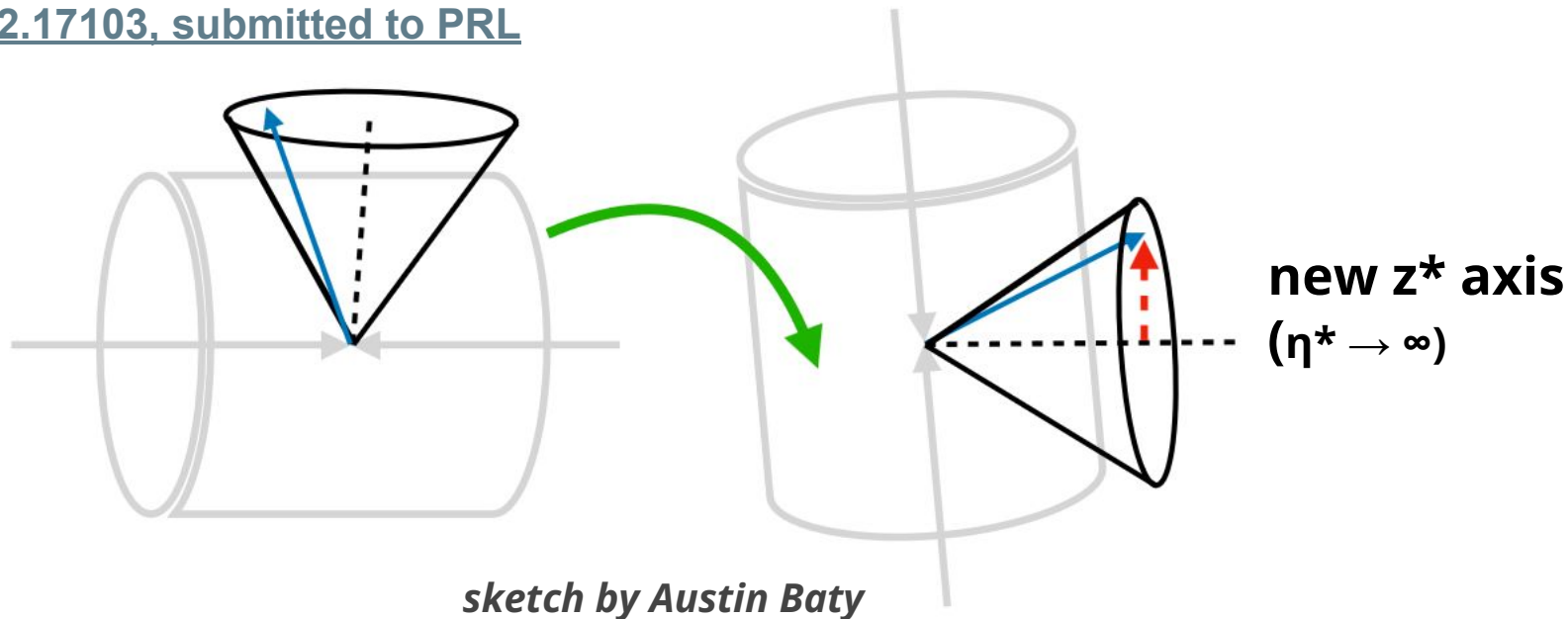
$$\alpha_s(m_Z) = 0.1229^{+0.0040}_{-0.0050} (\sim 4\%)$$

Most precise extraction of $\alpha_s(m_Z)$
with jet substructure

Quark/gluon degeneracy broken in
E3C/E2C ratio, allows for breaking
“10% uncertainty” barrier

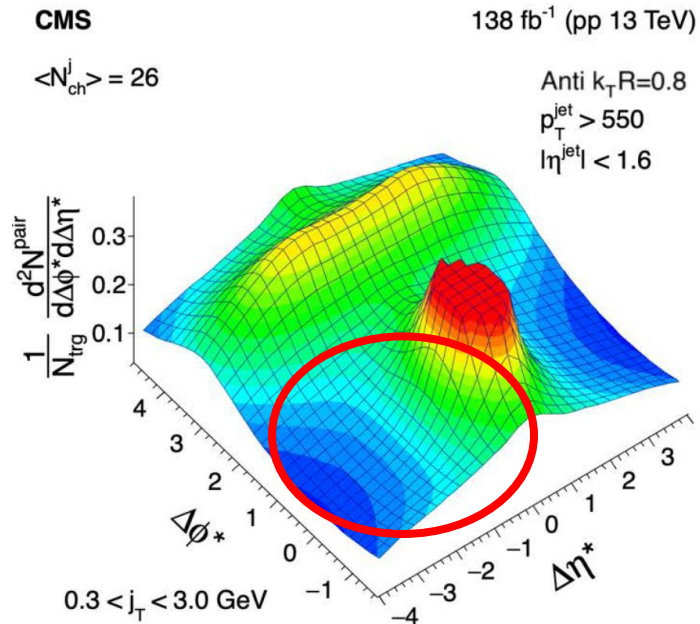
Rotated reference frame such that z^* axis is aligned with jet axis

[arXiv:2312.17103](https://arxiv.org/abs/2312.17103), submitted to PRL

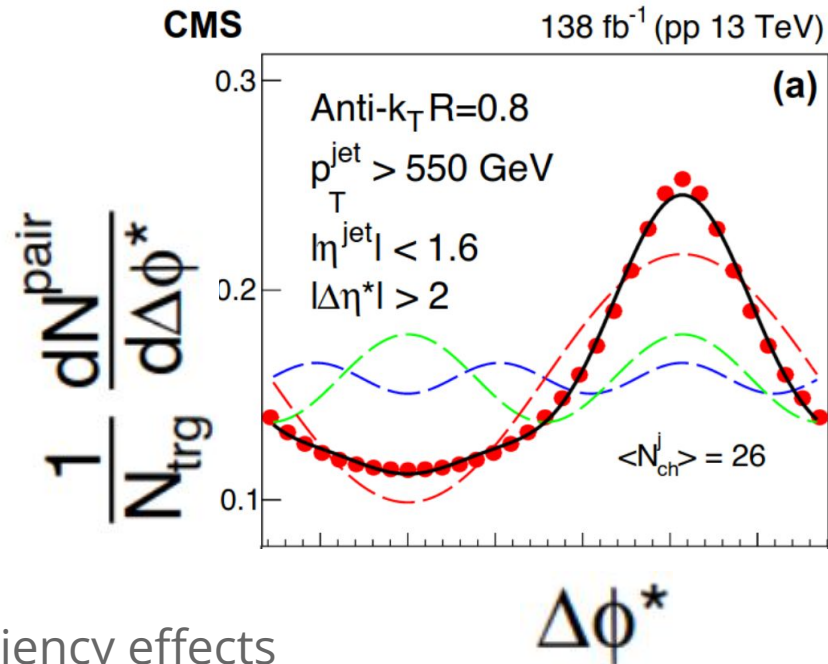


Particle correlations using φ^* and η^* coordinates (restricted to $0.86 < |\eta^*| < 5$),
transverse momentum relative to the jet axis j_T ($0.3 < j_T < 3 \text{ GeV}$)

inclusive N_{ch} category



$$\frac{1}{N_{\text{ch}}^j} \frac{dN^{\text{pair}}}{d\Delta\phi^*} \propto \sum_{n=1}^{\infty} V_{n\Delta} \cos(n\Delta\phi^*)$$



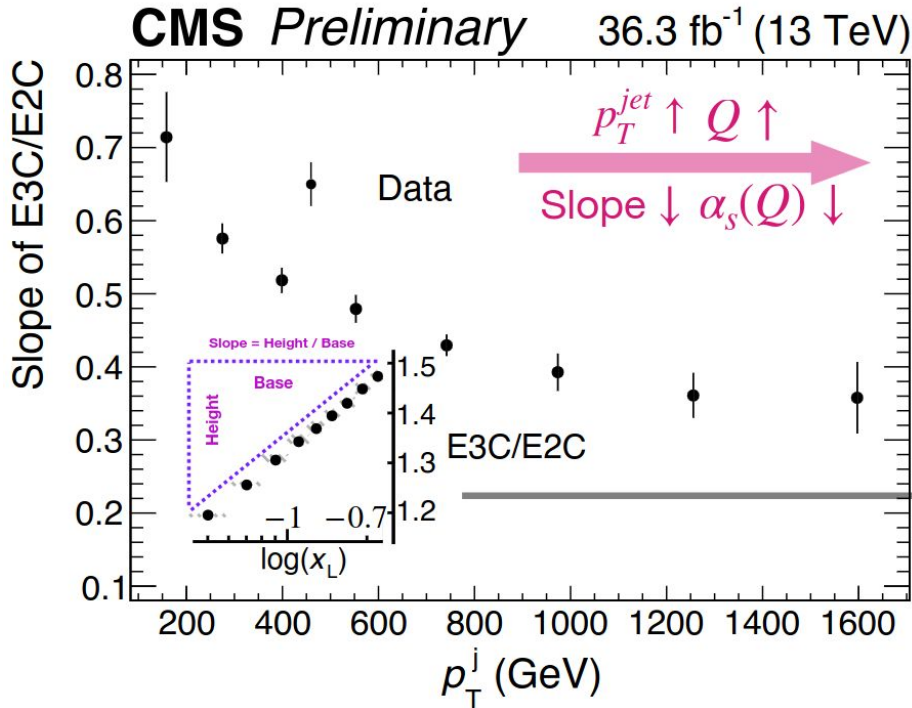
2D distributions corrected for acceptance/efficiency effects

No near-side ridge at $\Delta\phi^* \sim 0$

[arXiv:2312.17103](https://arxiv.org/abs/2312.17103), submitted to PRL

E3C/E2C sensitive to running α_s

CMS-PAS-SMP-22-015

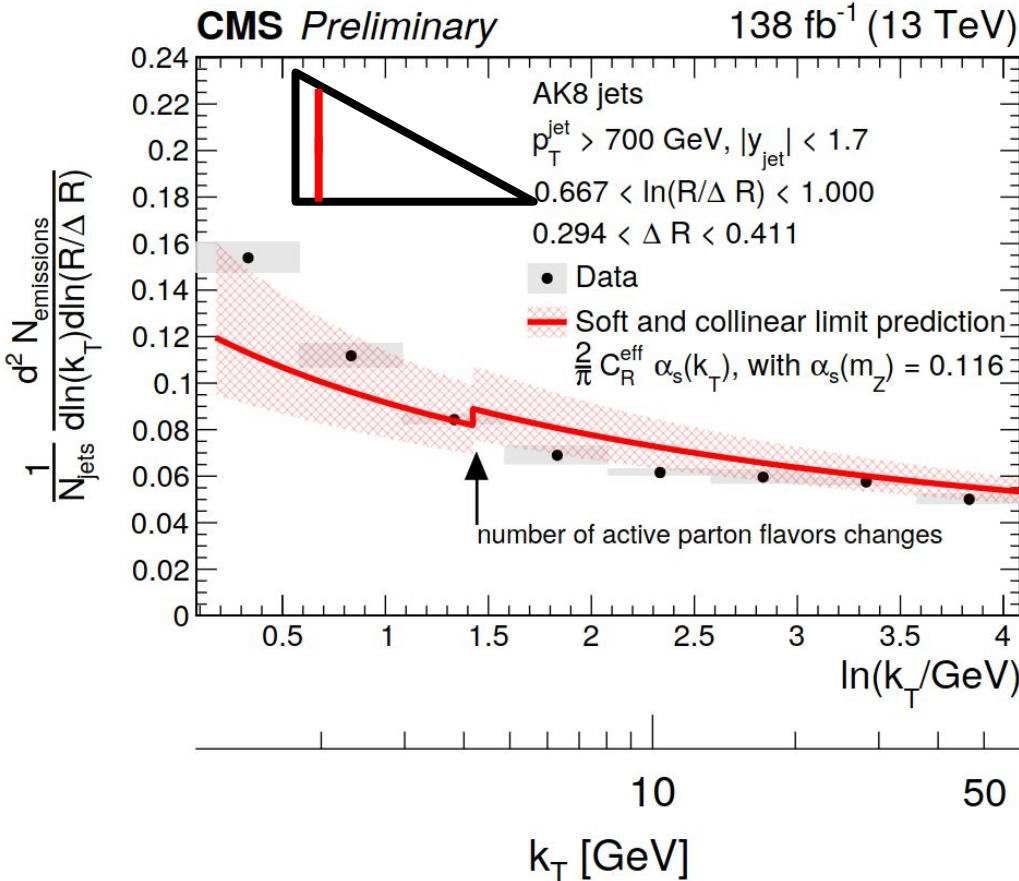


At LL, slope of E3C/E2C ratio sensitive to $\alpha_s(Q)$

$$\frac{\Delta}{\ominus} \propto \alpha_s(Q) \ln x_L + O(\alpha_s^2)$$

Quark/gluon fraction sensitivity is reduced in the E3C/E2C ratio, without losing sensitivity to $\alpha_s(Q)$ running

Running of α_s in the jet shower

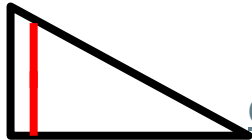


Recall LO pocket formula for Lund density:

$$\frac{1}{N_{\text{jets}}} \frac{d^2 N_{\text{emissions}}}{d \ln(k_T) d \ln(R/\Delta R)} \simeq \frac{2}{\pi} C_R \alpha_s(k_T)$$

Running $\alpha_s(k_T)$ from few GeV to ~60 GeV qualitatively describes the data
 (Assuming q/g fractions from PYTHIA8)

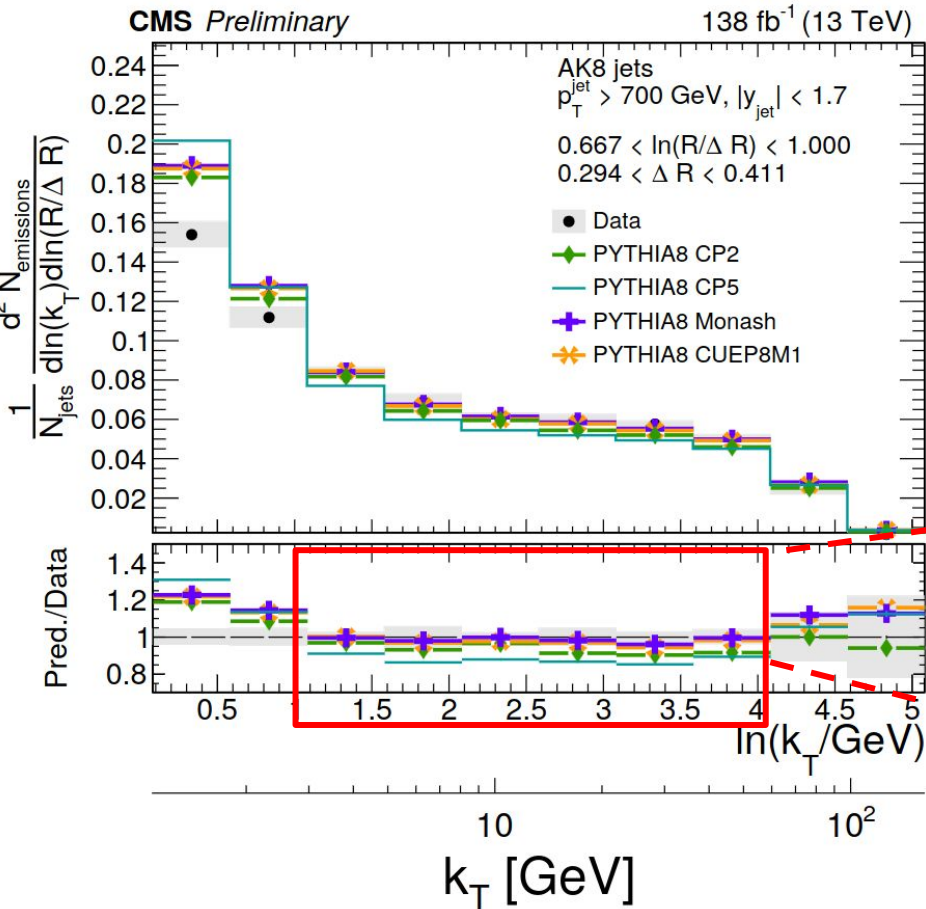
Large angle emissions



$R = 0.8$ Most important difference between PY8 tunes is α_s^{FSR}

CMS-PAS-SMP-22-007

$$\frac{1}{N_{\text{jets}}} \frac{d^2 N_{\text{emissions}}}{d \ln(k_T) d \ln(R/\Delta R)} \simeq \frac{2}{\pi} C_R \alpha_s(k_T)$$

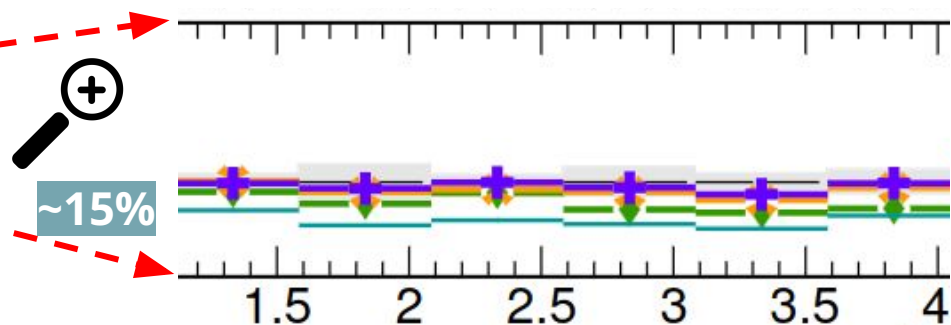


Monash/CUEP8M1: $\alpha_s^{\text{FSR}}(m_Z) = 0.1365$
(best description)

CP2: $\alpha_s^{\text{FSR}}(m_Z) = 0.130$

CP5: $\alpha_s^{\text{FSR}}(m_Z) = 0.118$

LJP data can be used to constrain $\alpha_s^{\text{FSR}}(m_Z)$ for MC tuning



k_T between 3 – 50 GeV