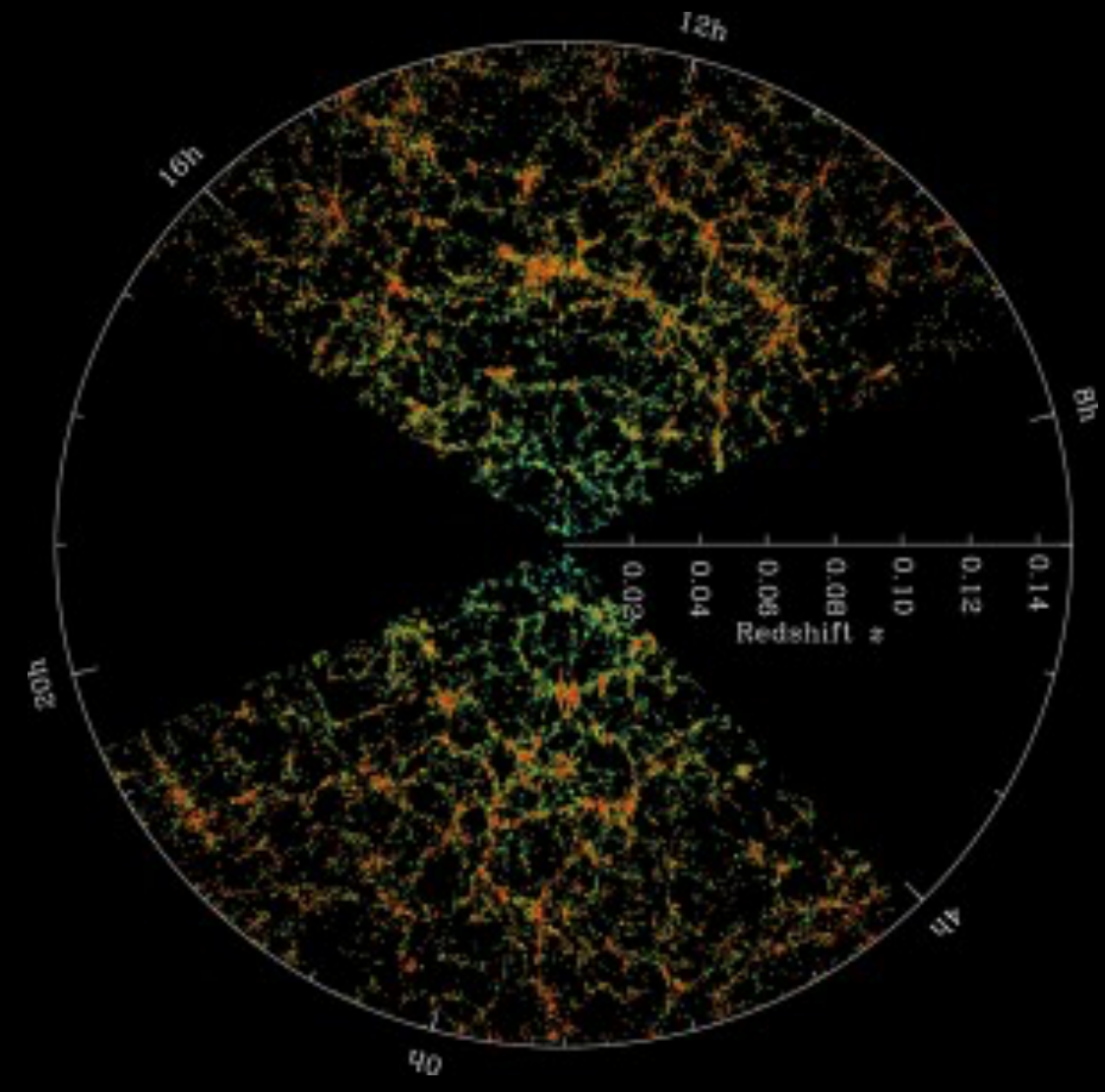
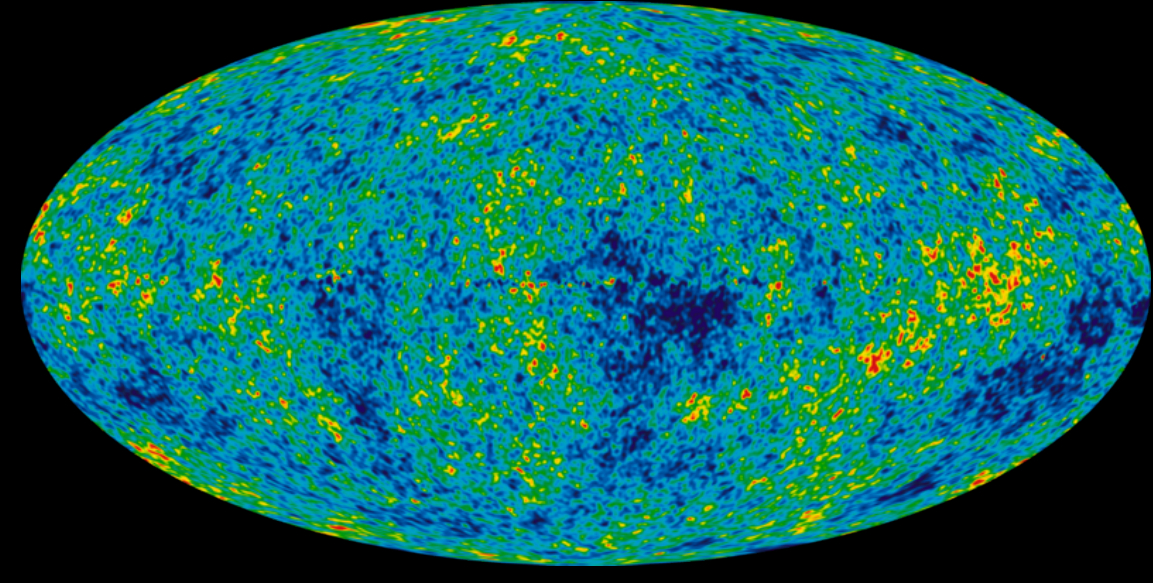


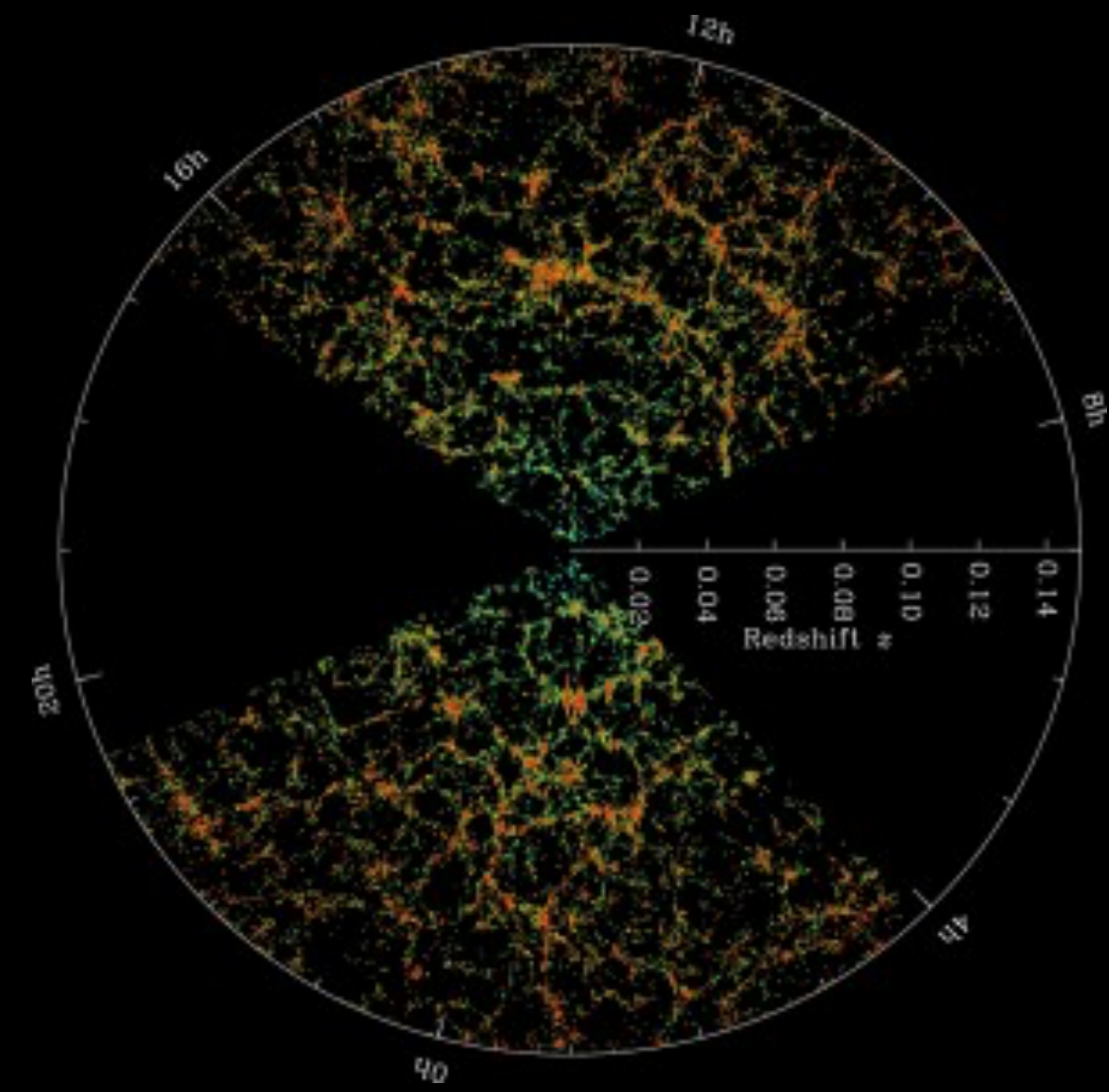
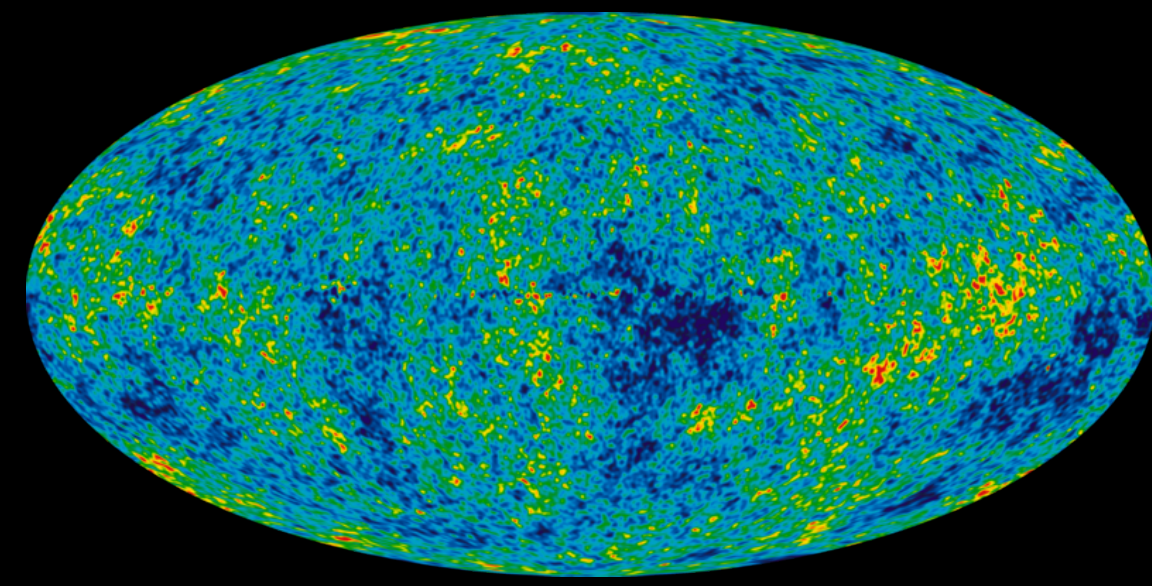
Seeing highly anisotropic gravitational wave backgrounds from phase transitions

Arushi Bodas

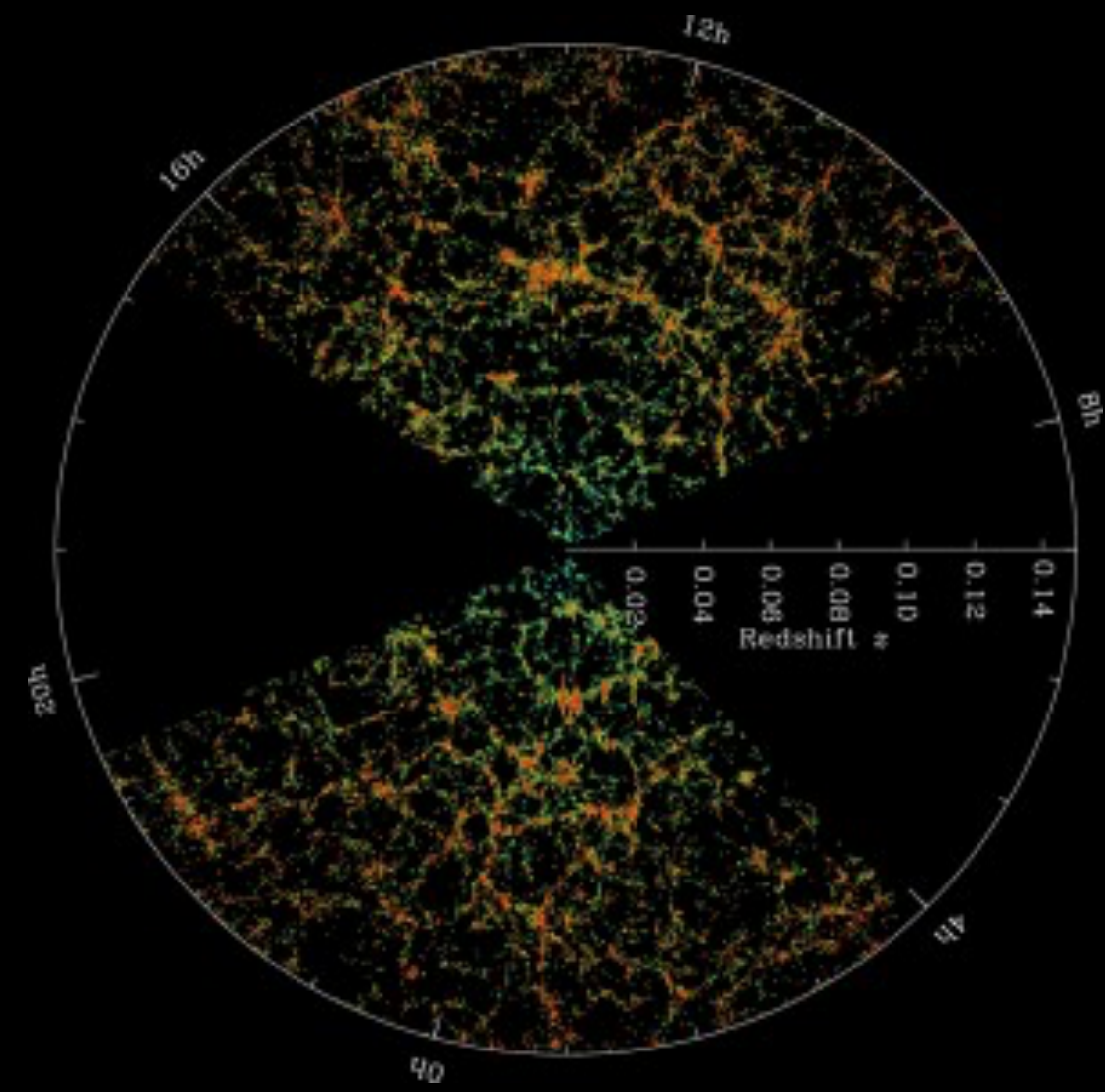
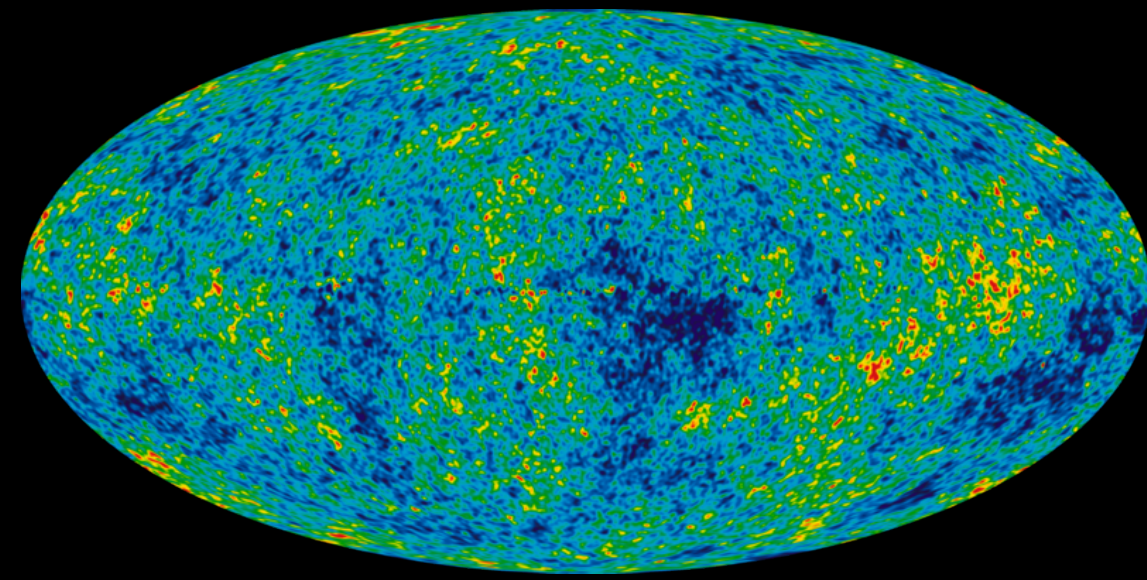
AB, R. Sundrum: *JHEP* 06 (2023) 029

AB, K. Harigaya, K. Inomata, T. Terada, L-T Wang: Ongoing work...





Quantum fluctuations of a scalar field + inflation



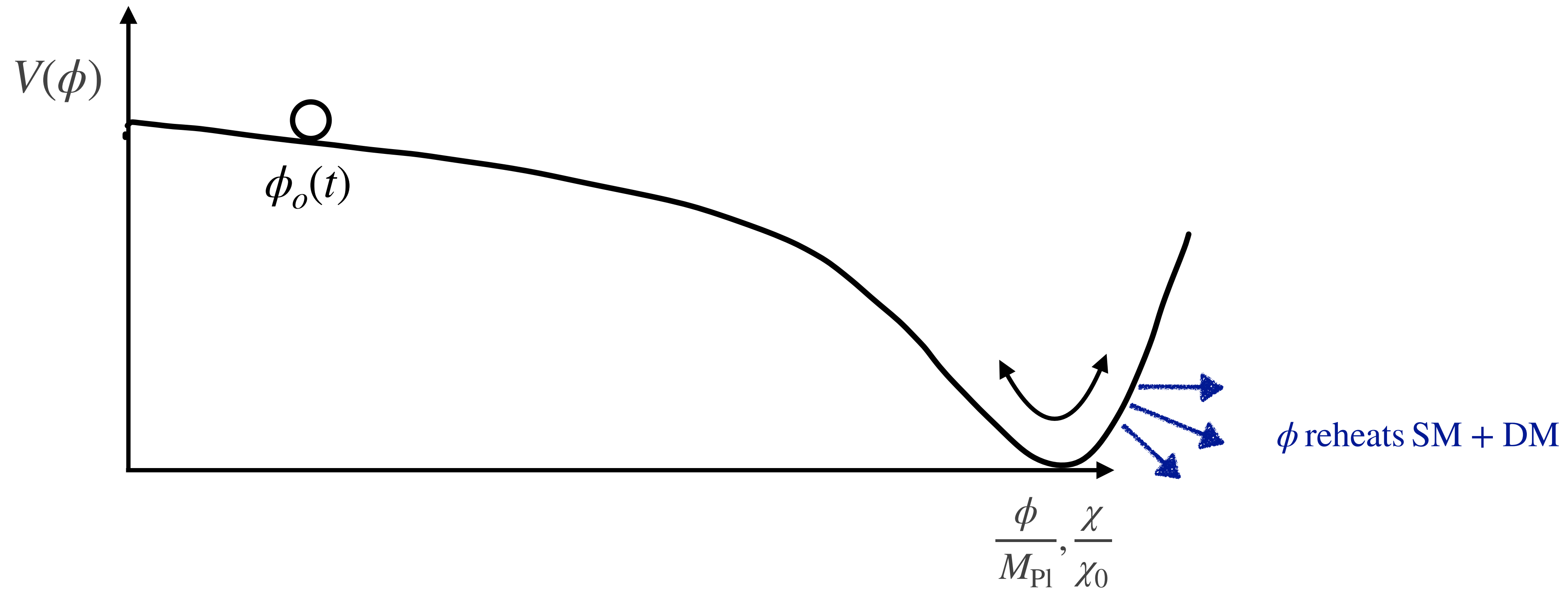
Quantum fluctuations of a scalar field + inflation

Anisotropy maps are windows into inflationary physics

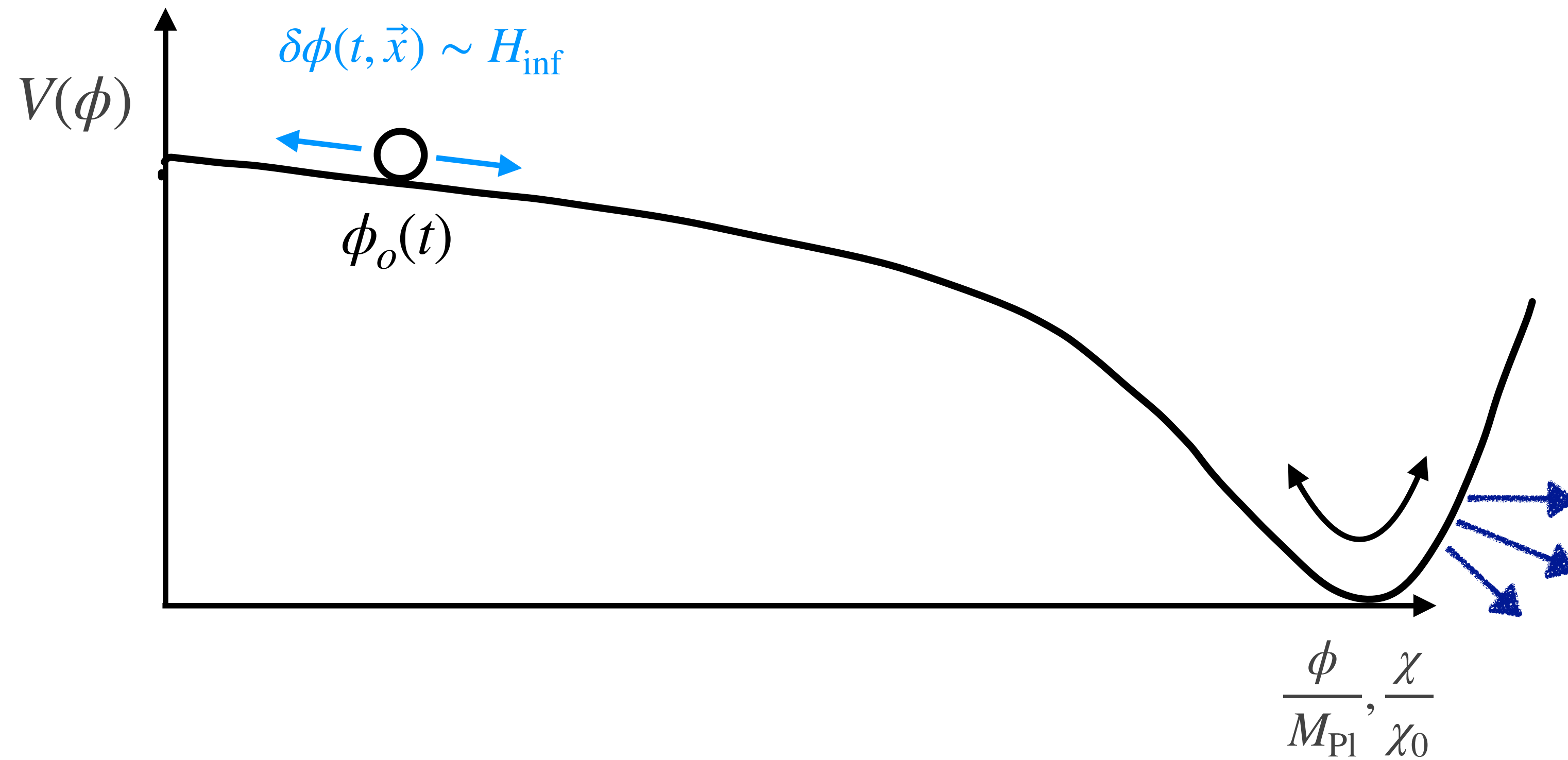
Common origin of known datasets

- Current observations tell us that density perturbations in all Standard Model (SM) species and Dark Matter (DM) originate from the same inflationary fluctuation (e.g. the inflaton).
[Planck, 1807.06211](#)
- Current observations (CMB) already constrain the prospect of seeing new inflationary physics in future datasets based on SM and DM species (line-intensity, large scale structure).
- Can we think of a fluctuation map that could be very different from the CMB?

Multi-field inflation: Inflaton + ALP (χ)



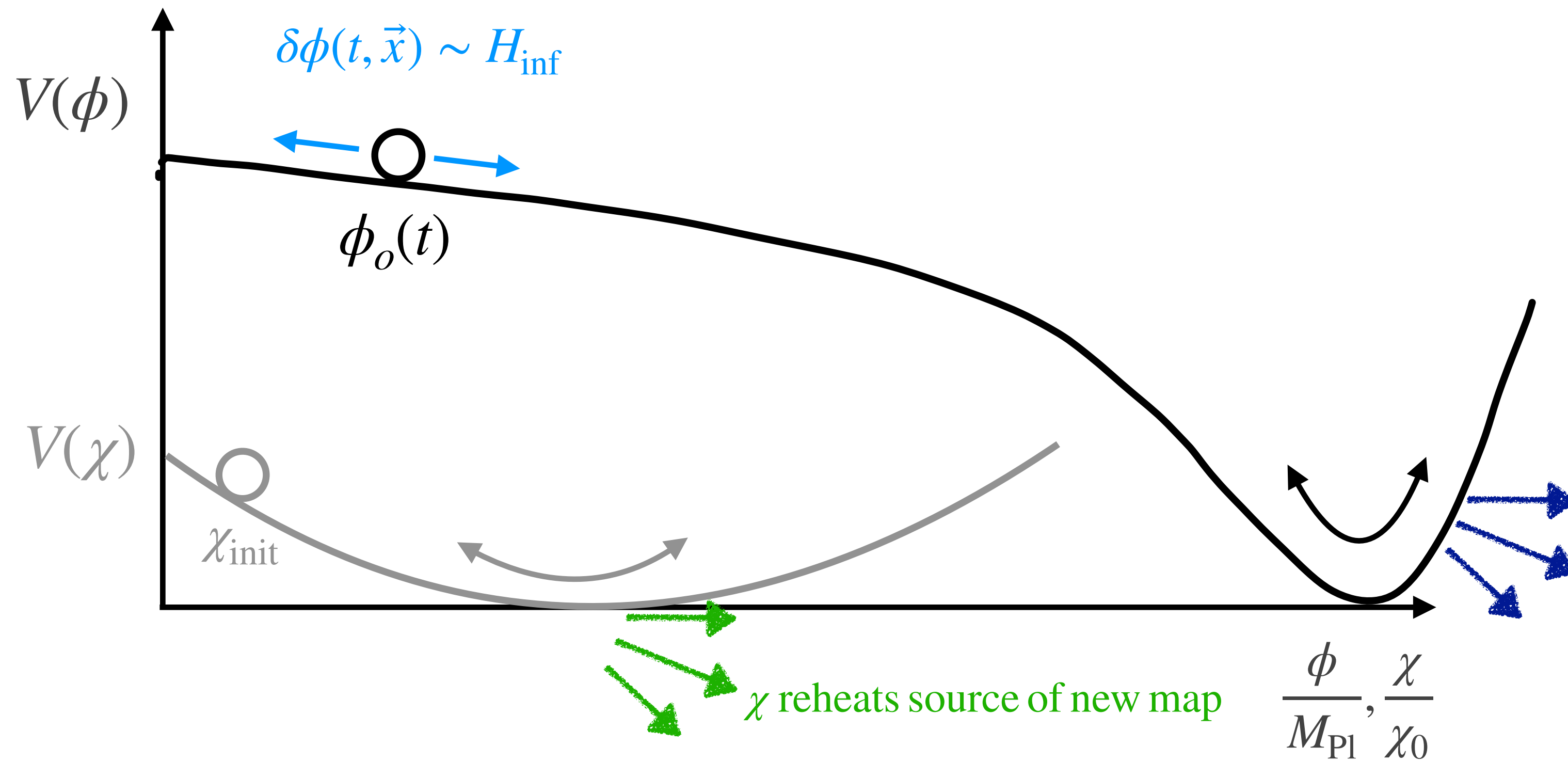
Multi-field inflation: Inflaton + ALP (χ)



ϕ reheats SM + DM

$$\delta_{\text{SM}} \equiv \left. \frac{\Delta V}{V} \right|_{\phi} \sim \frac{H_{\text{inf}} \delta\phi}{\dot{\phi}_0}$$

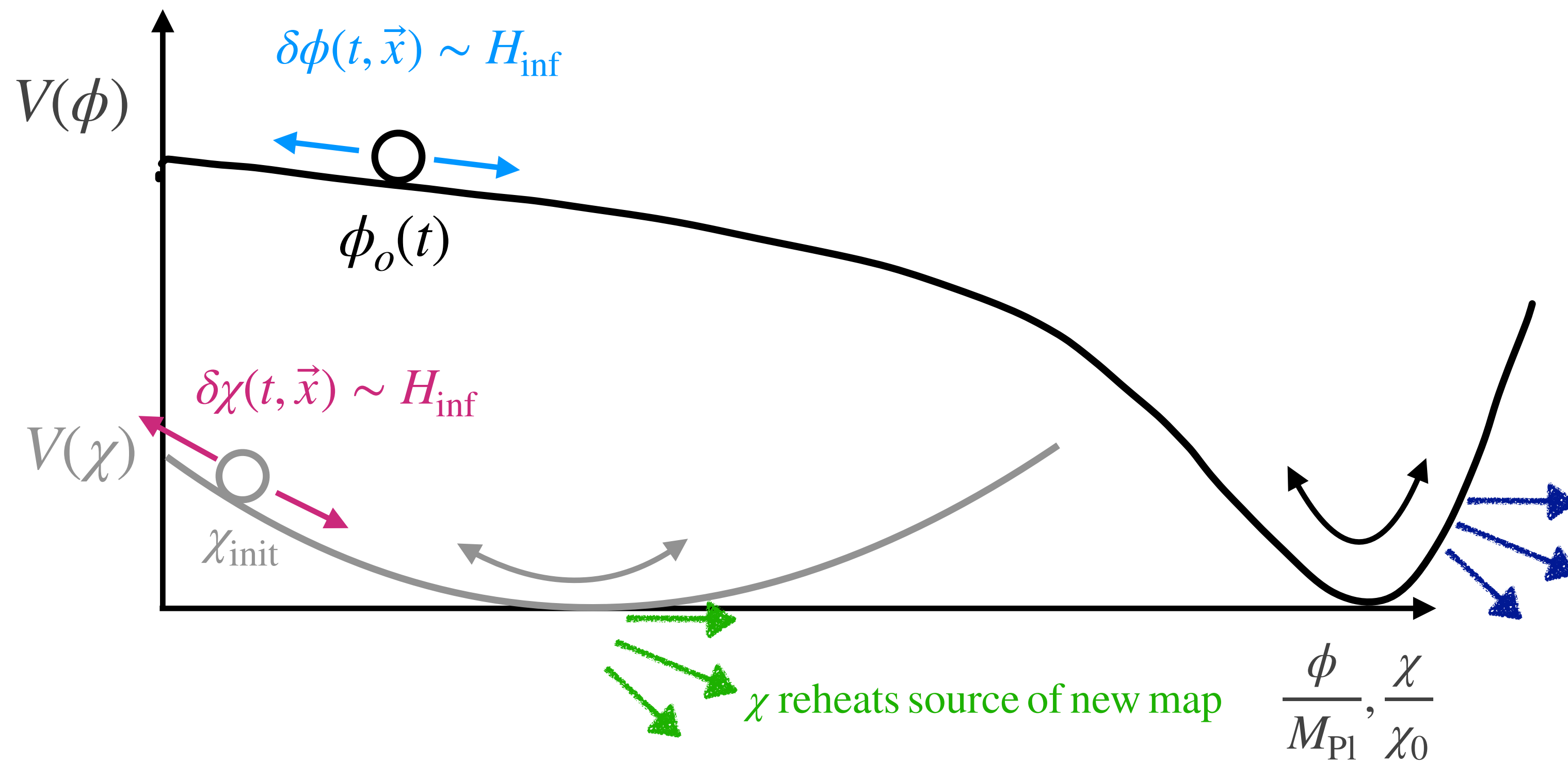
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Multi-field inflation: Inflaton + ALP (χ)



ϕ reheats SM + DM

$$\delta_{SM} \equiv \left. \frac{\Delta V}{V} \right|_{\phi} \sim \frac{H_{inf} \delta\phi}{\dot{\phi}_0}$$

$$\delta_{new} \equiv \left. \frac{\Delta V}{V} \right|_{\chi} \sim \frac{\delta\chi}{\chi_{init}}$$

What's the messenger?

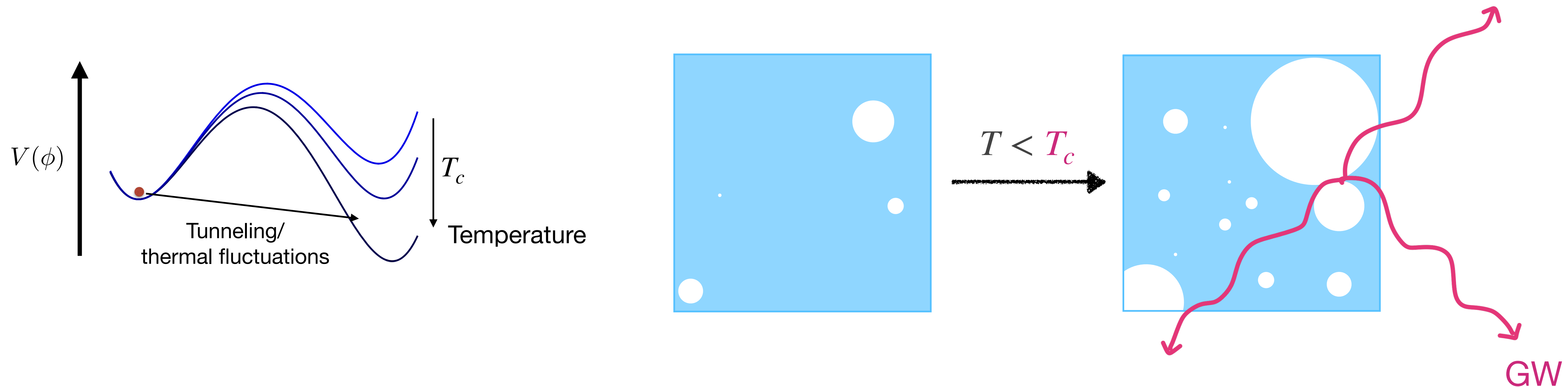
- Copiously produced in the early universe
- Free-streaming (does not thermalize with SM and DM)
- Could be detectable with the technology that we have today

What's the messenger?

- Copiously produced in the early universe
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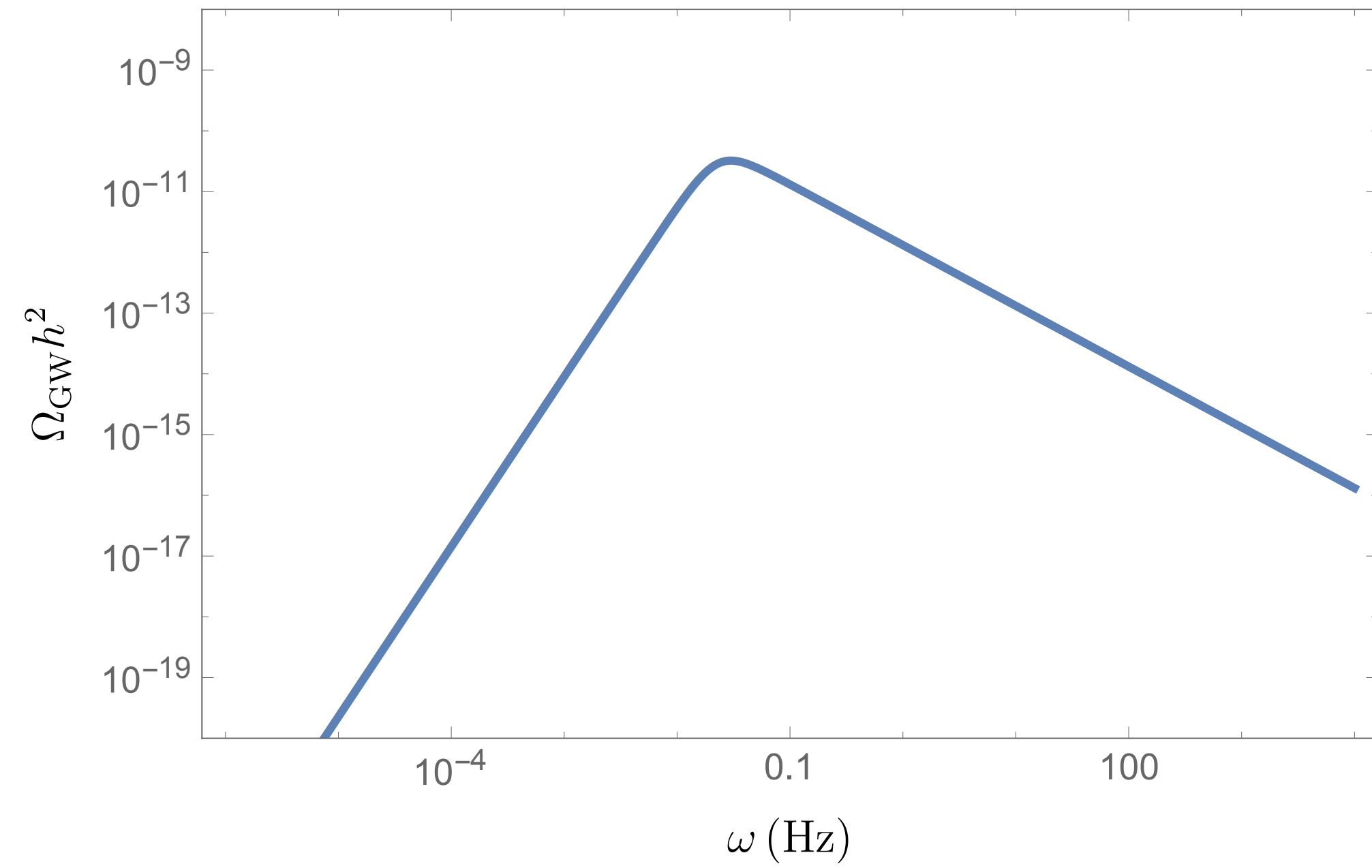
Gravitational waves!

Case 1: Gravitational waves from a phase transition



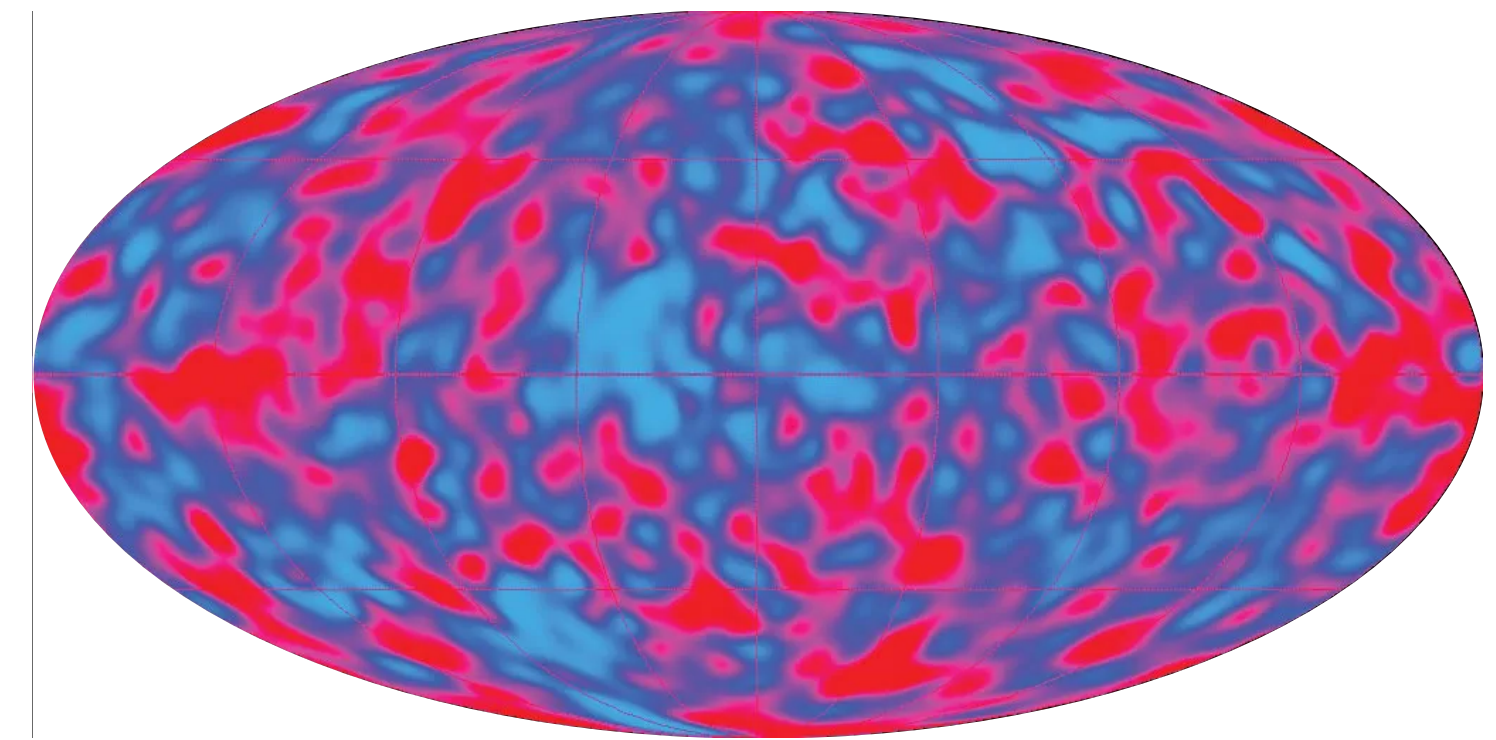
- Many extensions of SM have PTs at $T_c \sim 1 - 1000 \text{ TeV}$. Frequency of GW from such PTs would be redshifted to $10^{-4} - 10^{-1} \text{ Hz}$ today, which is the target frequency range of many proposed space-based experiments such as LISA, BBO, etc.

Frequency spectrum



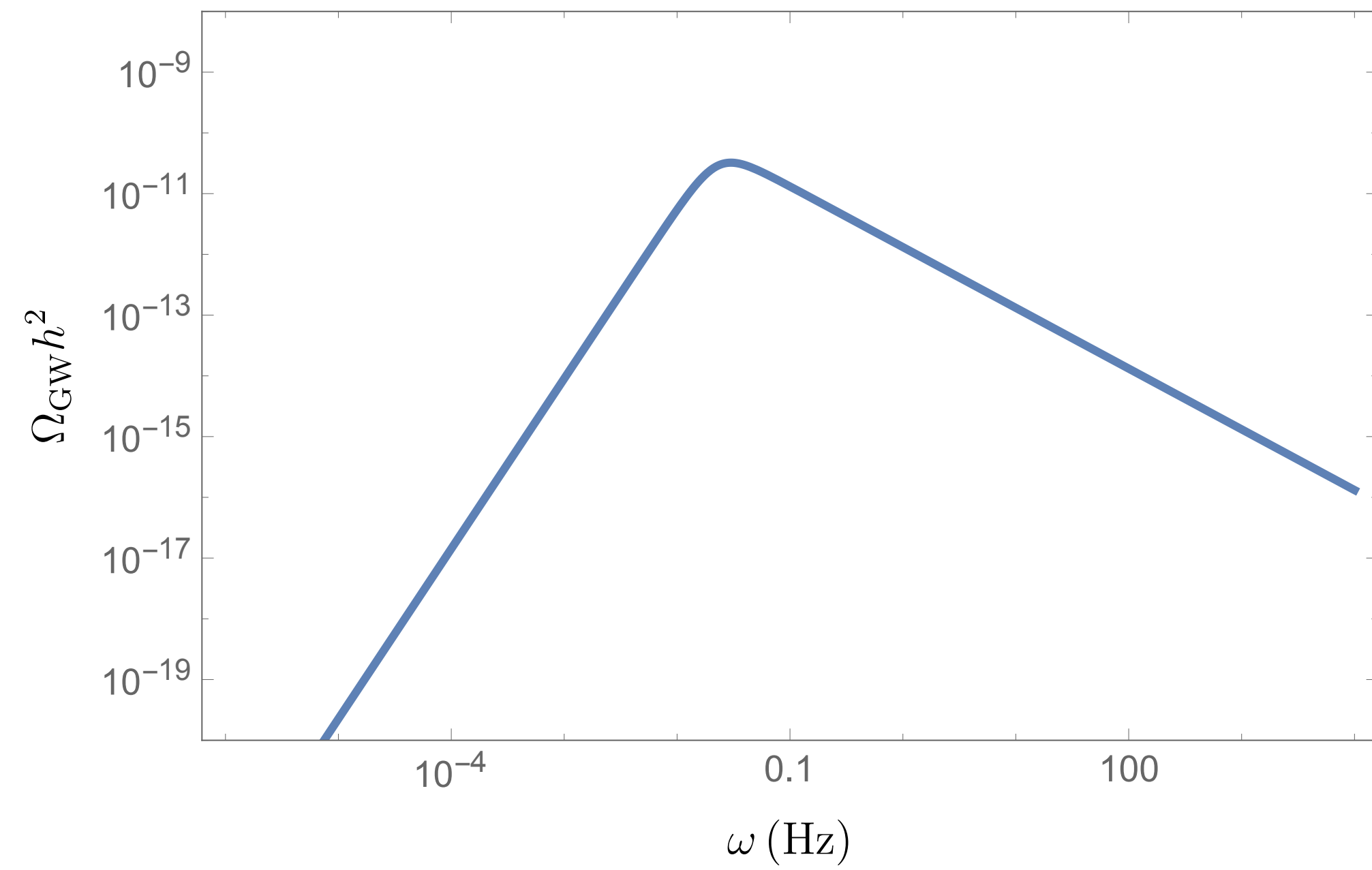
Sub-horizon physics

Angular power spectrum



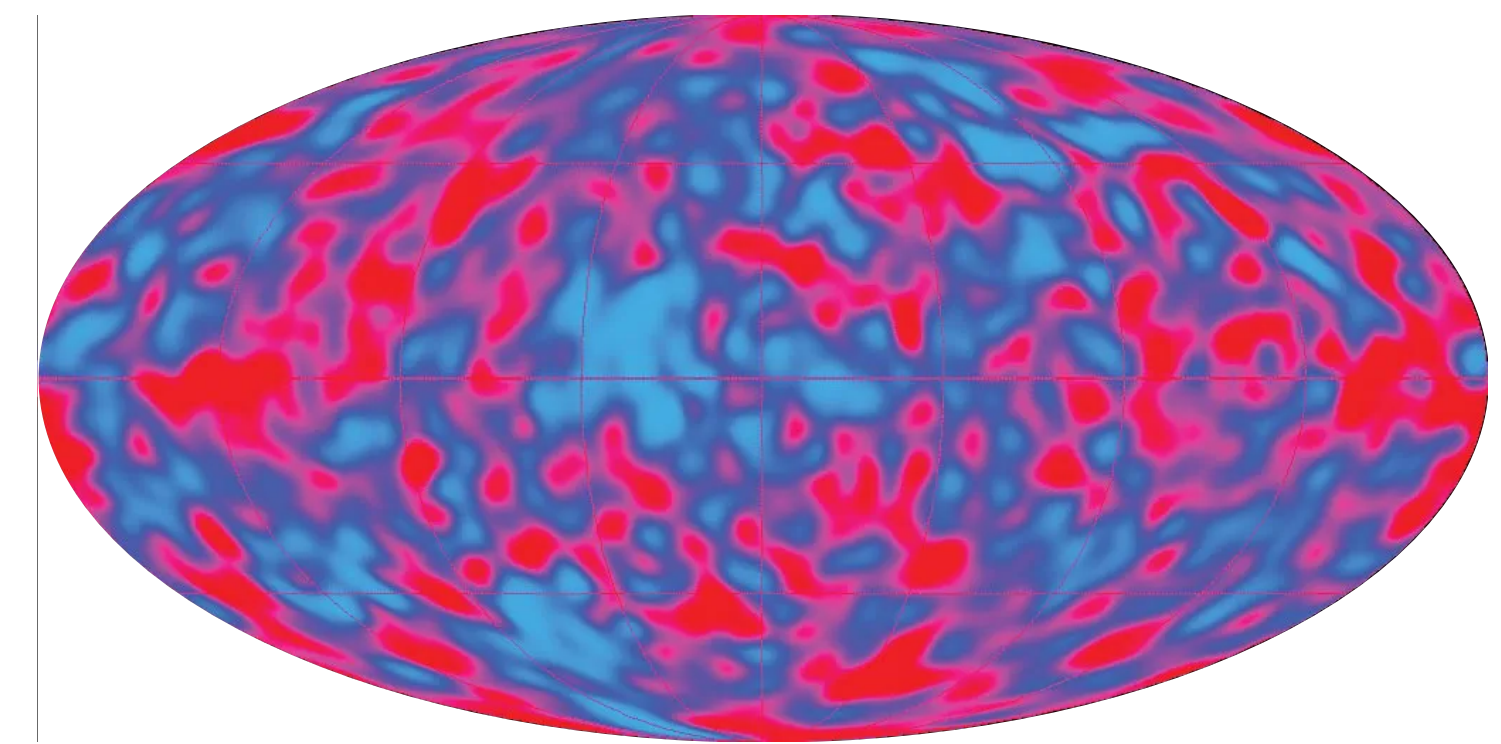
Super-horizon physics

Frequency spectrum



Sub-horizon physics

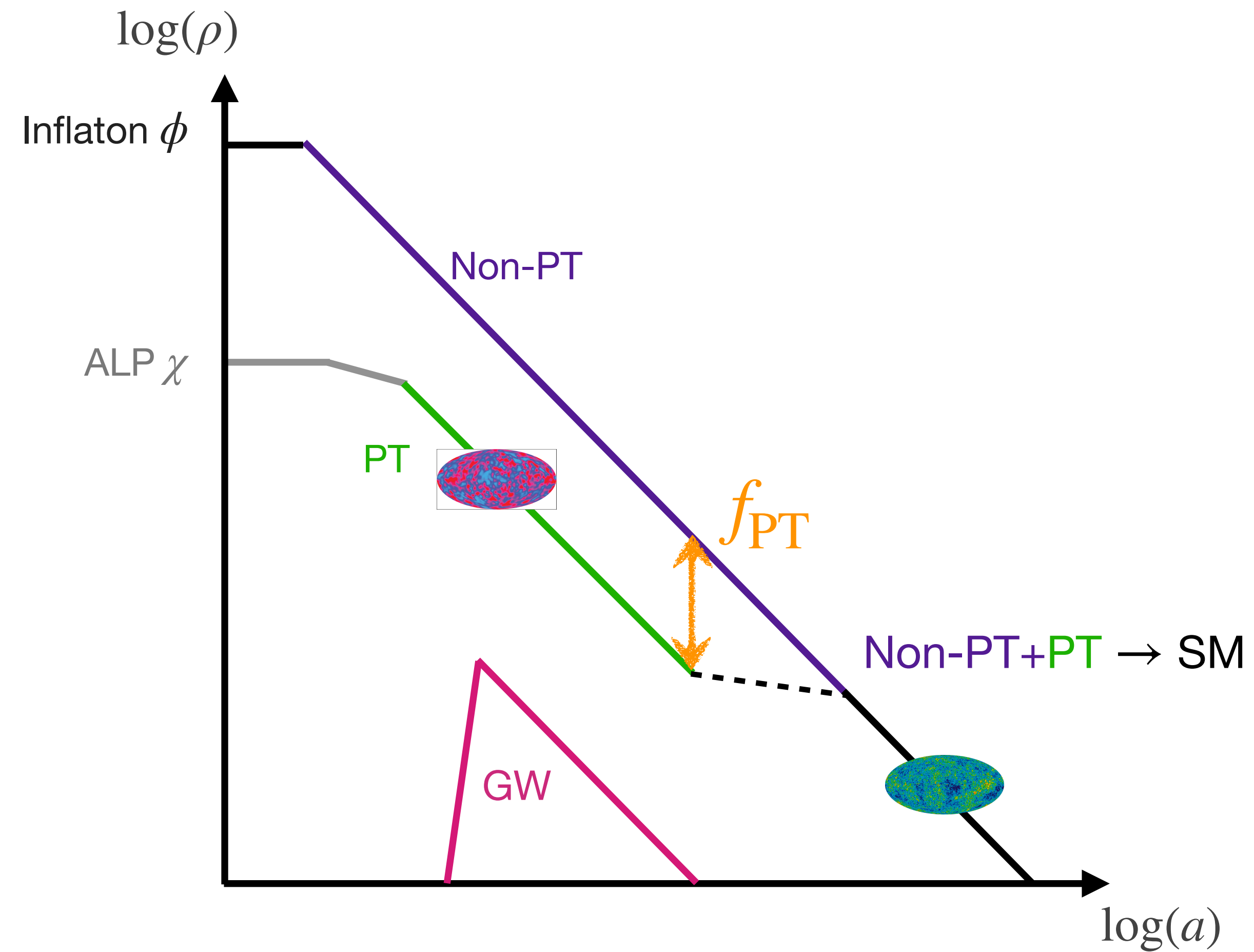
Angular power spectrum



Super-horizon physics

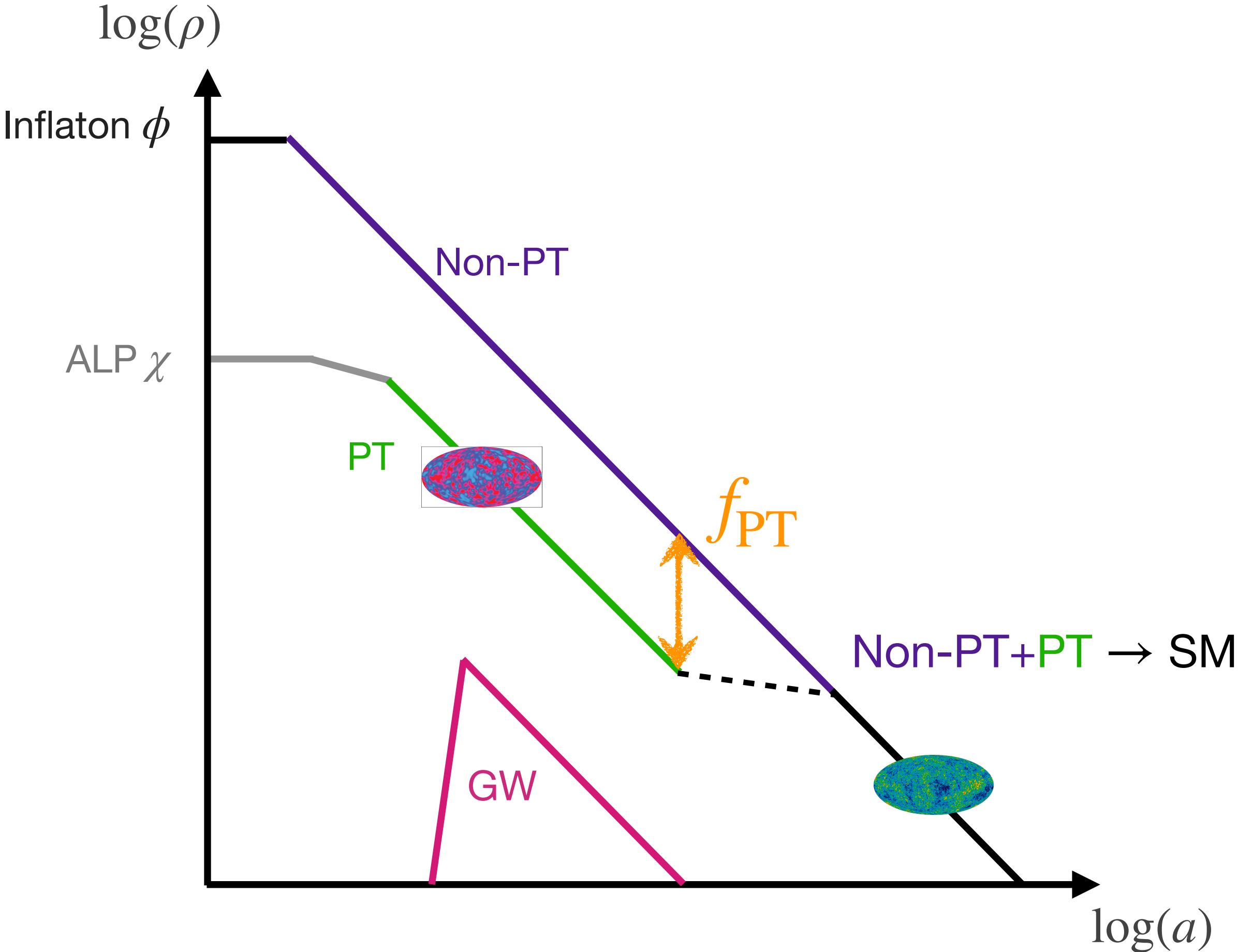
A model of isocurvature GWB

Geller, Hook, Sundrum, Tsai 1803.10780



A model of isocurvature GWB

Geller, Hook, Sundrum, Tsai 1803.10780



$$\delta_{GW} \sim \delta_\chi + \delta_\phi$$

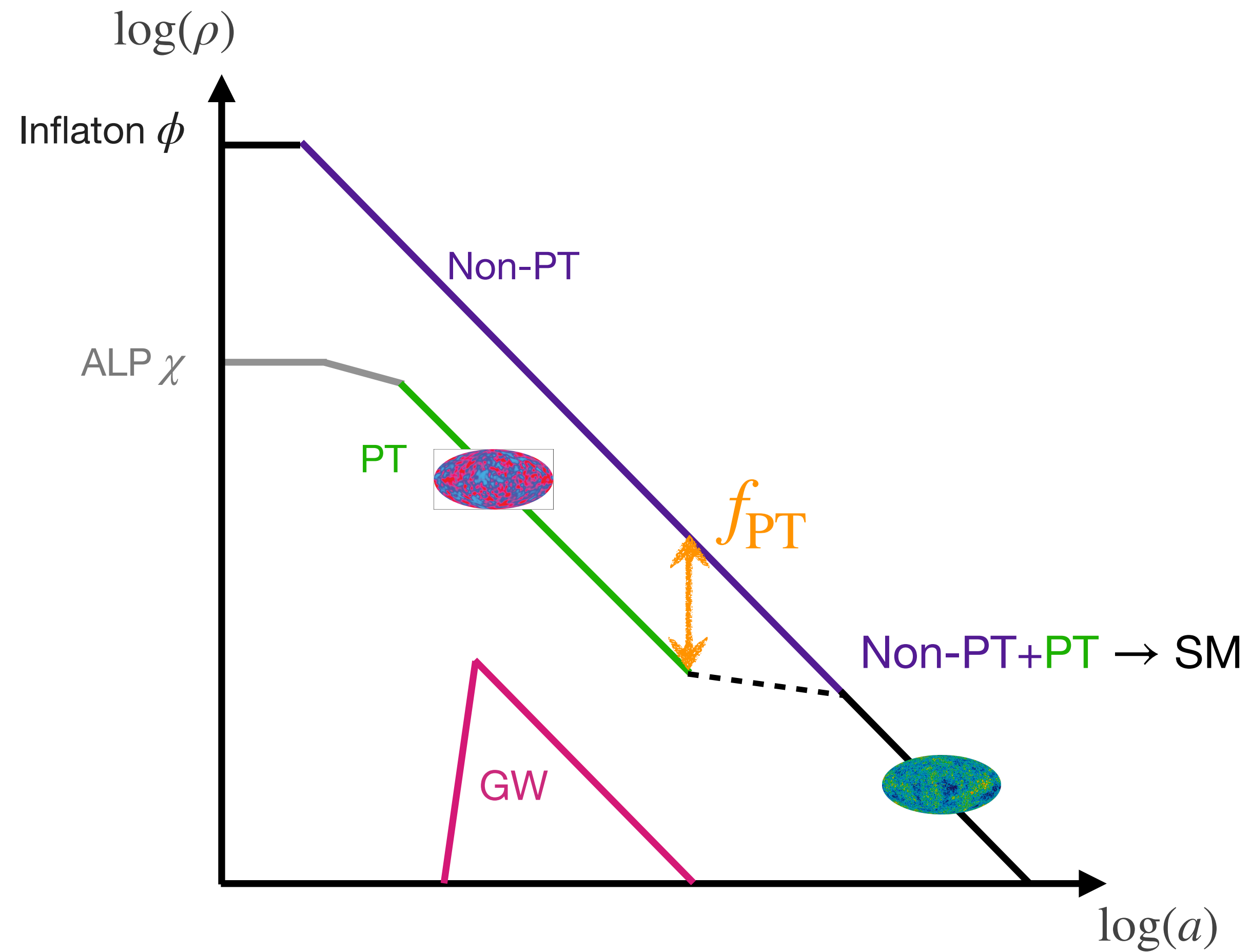
Sachs-Wolfe contribution $\sim 10^{-5}$

$$\delta_{CMB} \sim \delta_\phi + f_{PT} \delta_\chi \sim 10^{-5}$$

$$f_{PT} = \frac{\rho_{PT}}{\rho_{total}} \ll 1$$

Large isocurvature is more interesting

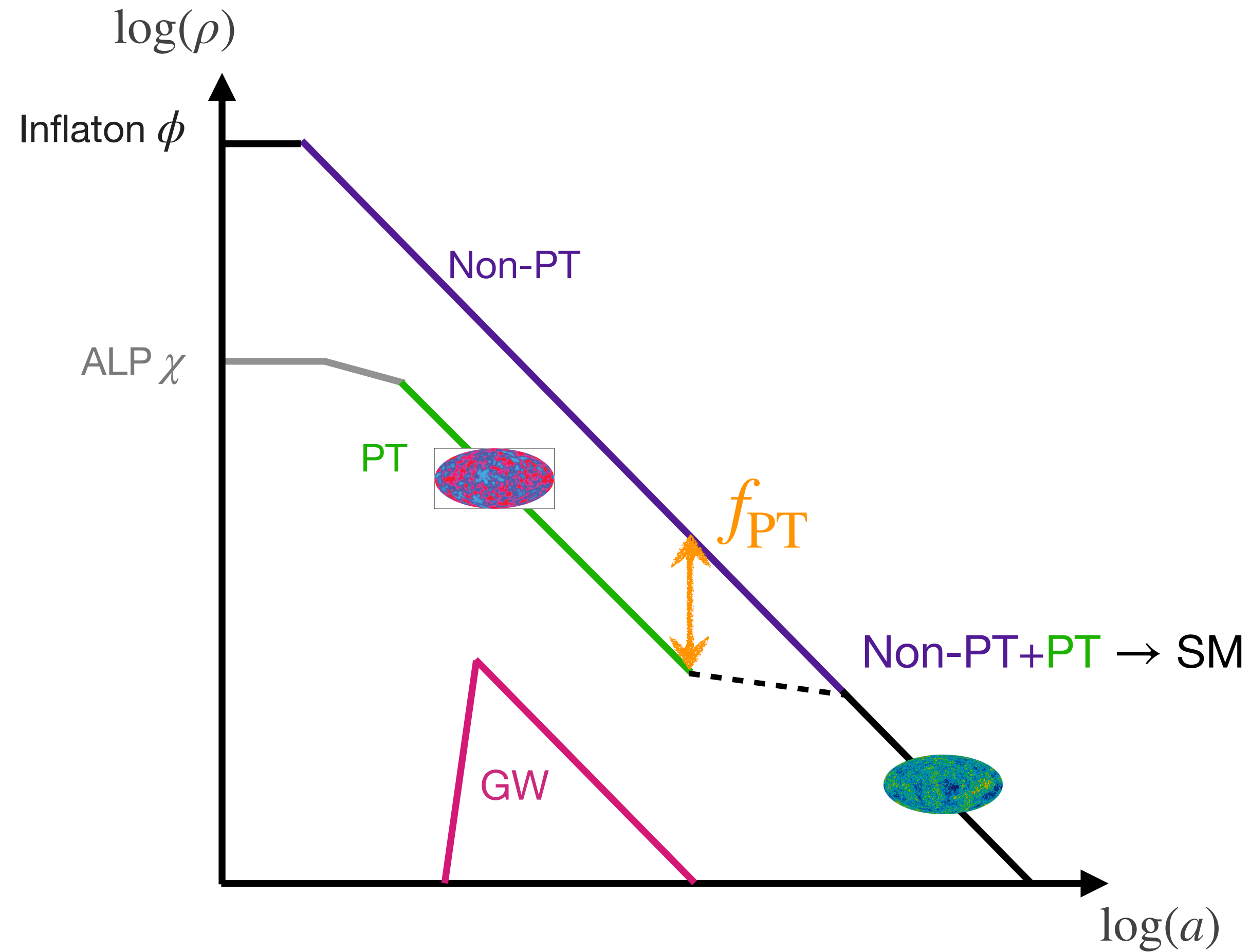
Geller, Hook, Sundrum, Tsai 1803.10780



$$\delta_{GW} \sim \delta_{\chi} + \delta_{\phi} \sim 10^{-5}$$

Large isocurvature is more interesting

Geller, Hook, Sundrum, Tsai 1803.10780

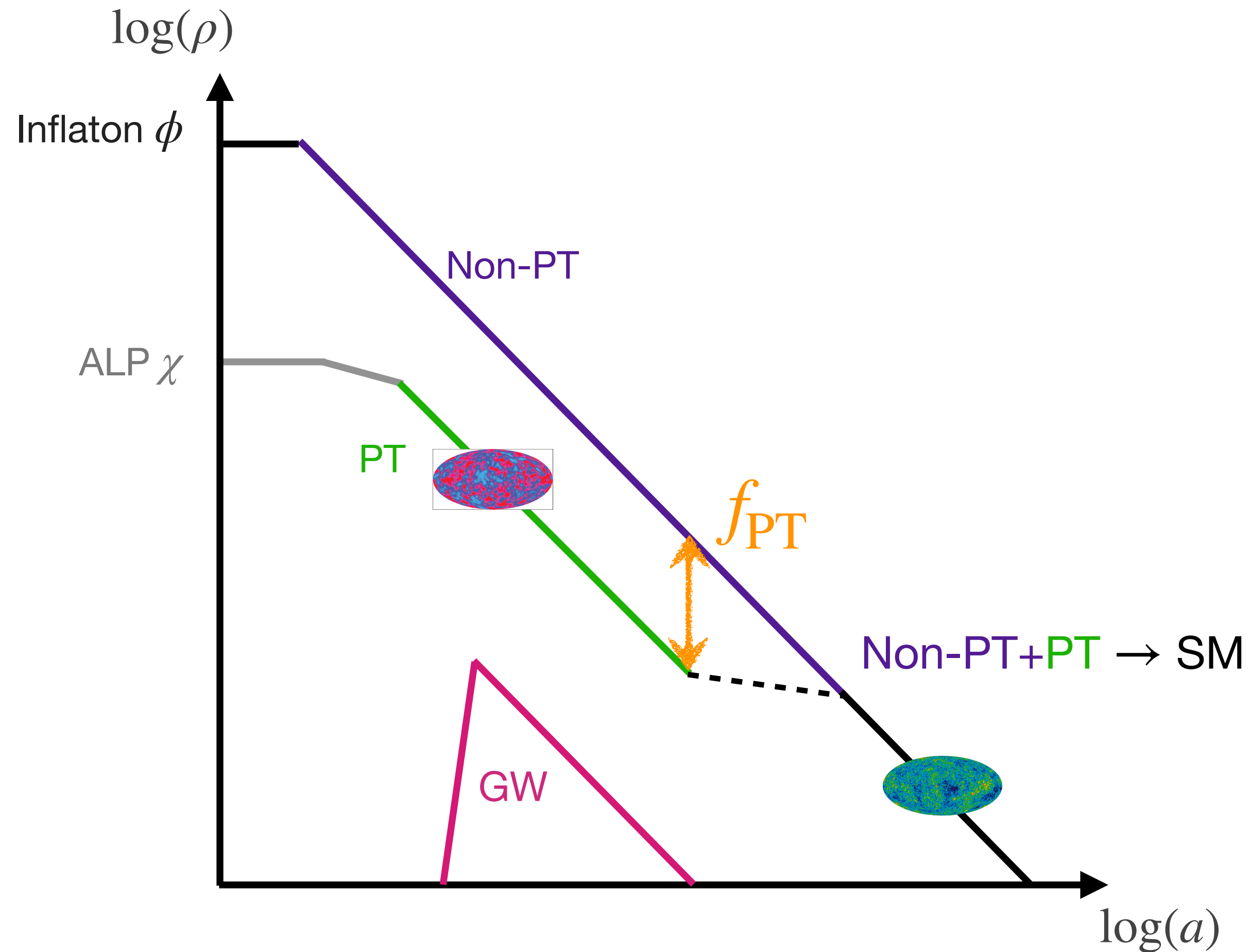


$$\delta_{GW} \sim \delta_{\chi} + \delta_{\phi} \rightarrow \sim 10^{-5}$$

- $\delta_{\chi} > 10^{-5}$ is more distinct

Large isocurvature is more interesting

Geller, Hook, Sundrum, Tsai 1803.10780



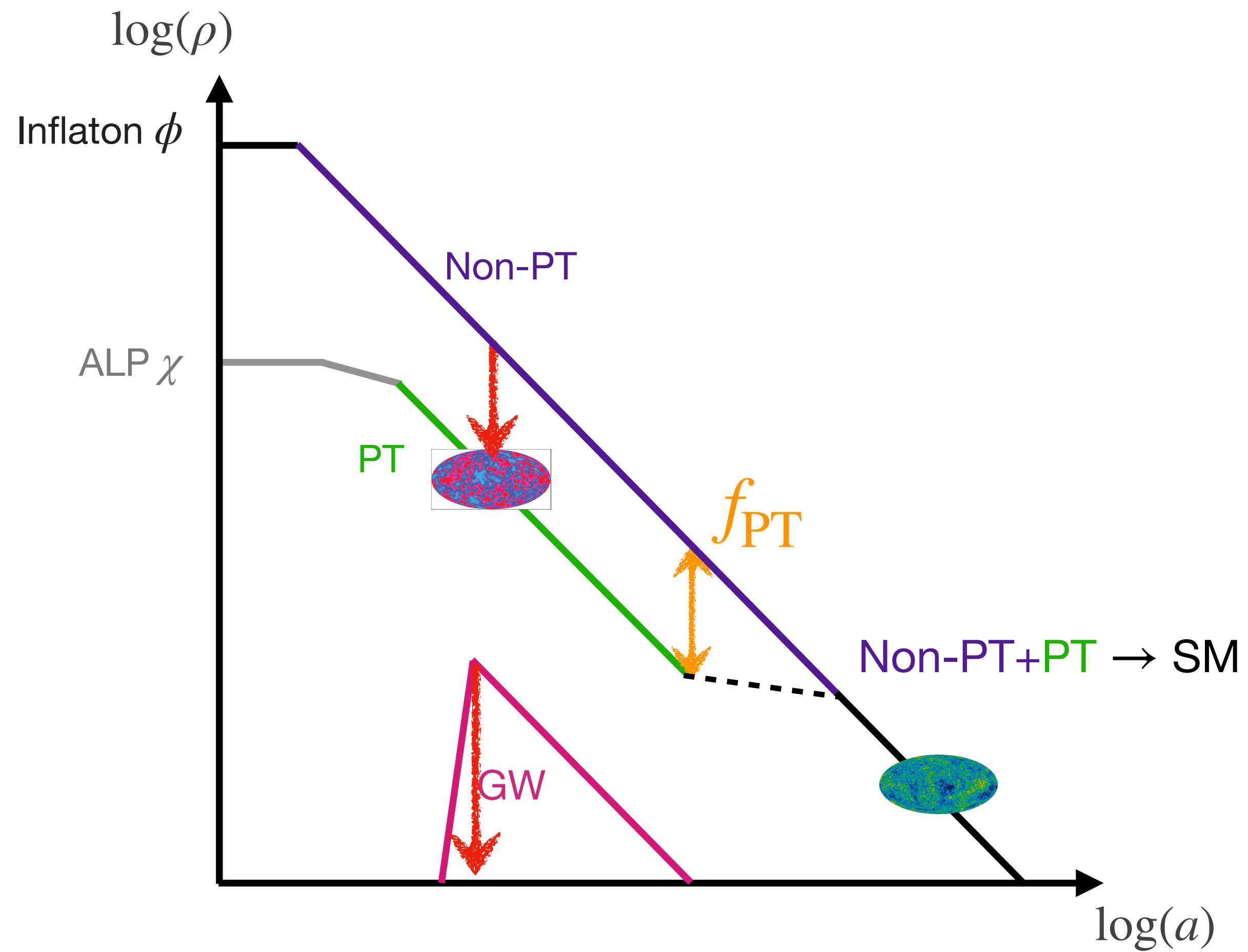
$$\delta_{\text{GW}} \sim \delta_{\chi} + \delta_{\phi} \rightarrow \sim 10^{-5}$$

- $\delta_{\chi} > 10^{-5}$ is more distinct

- $\delta_{\chi} \sim \frac{H_{\text{inf}}}{\chi_{\text{init}}} \rightarrow$ in high-scale inflation

$H_{\text{inf}} \sim 10^{-5} M_{\text{Pl}}$, any sub-Planckian misalignment χ_{init} gives $\delta_{\chi} > 10^{-5}$

The tradeoff

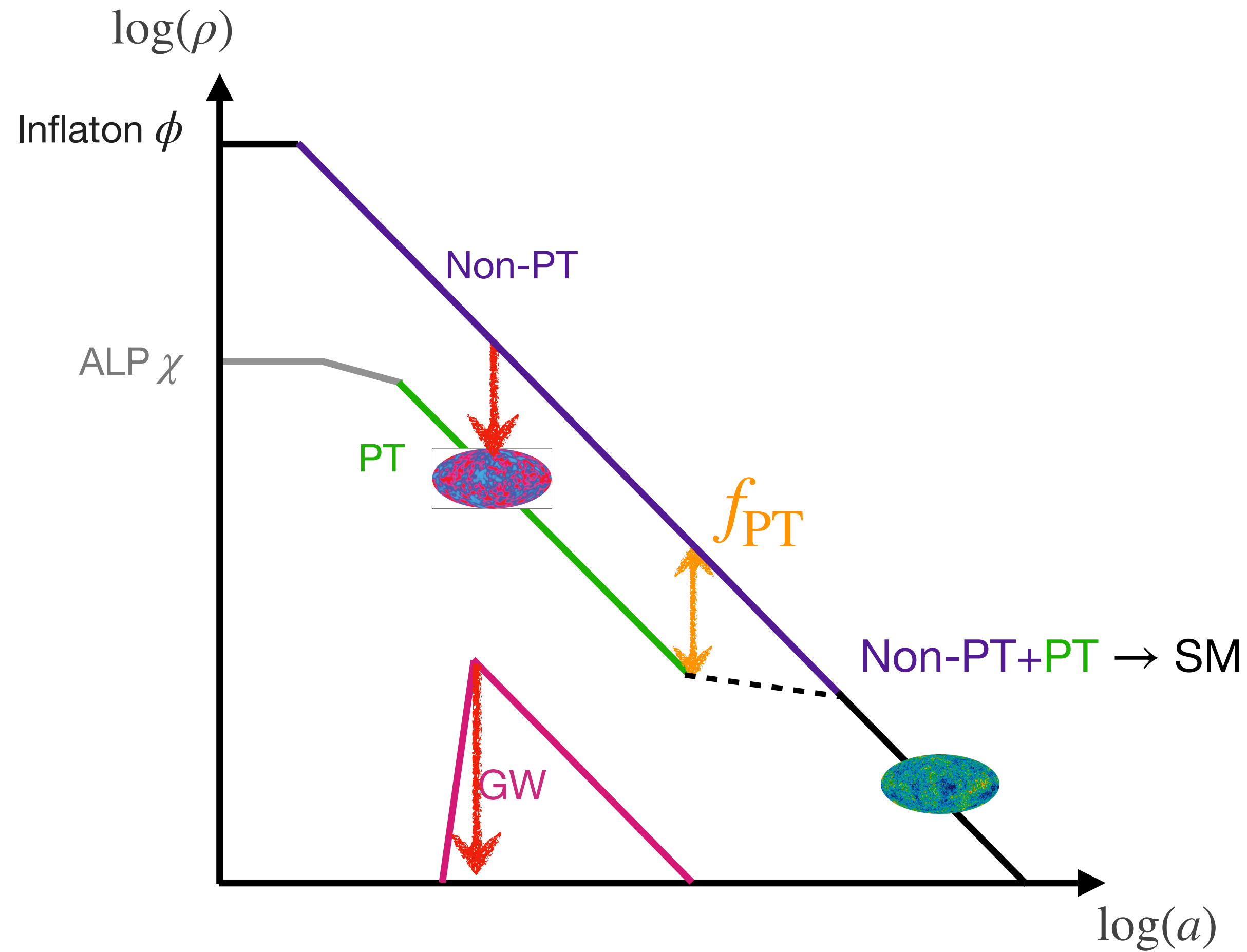


$$\delta_{\text{GW}} \sim \delta_{\chi} + \delta_{\phi}$$

$$\delta_{\text{CMB}} \sim \delta_{\phi} + f_{\text{PT}} \delta_{\chi} \sim 10^{-5}$$

$$\Omega_{\text{GW}} := \frac{\rho_{\text{GW}}}{\rho_{\text{total}}} \propto f_{\text{PT}}^2$$

The tradeoff



$$\delta_{GW} \sim \delta_\chi + \delta_\phi$$

$$\delta_{CMB} \sim \delta_\phi + f_{PT} \delta_\chi \sim 10^{-5}$$

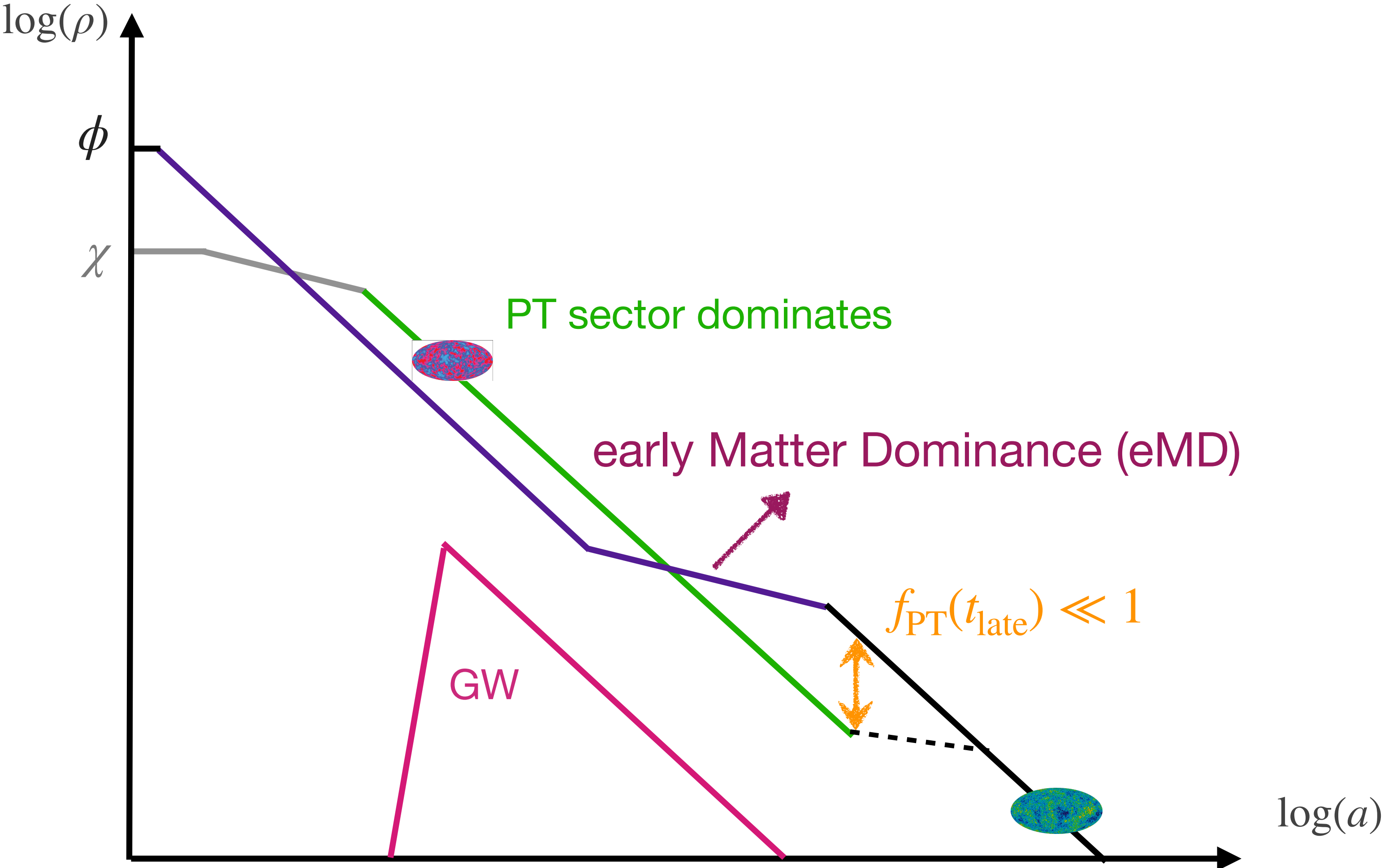
$$\Omega_{GW} := \frac{\rho_{GW}}{\rho_{total}} \propto f_{PT}^2$$

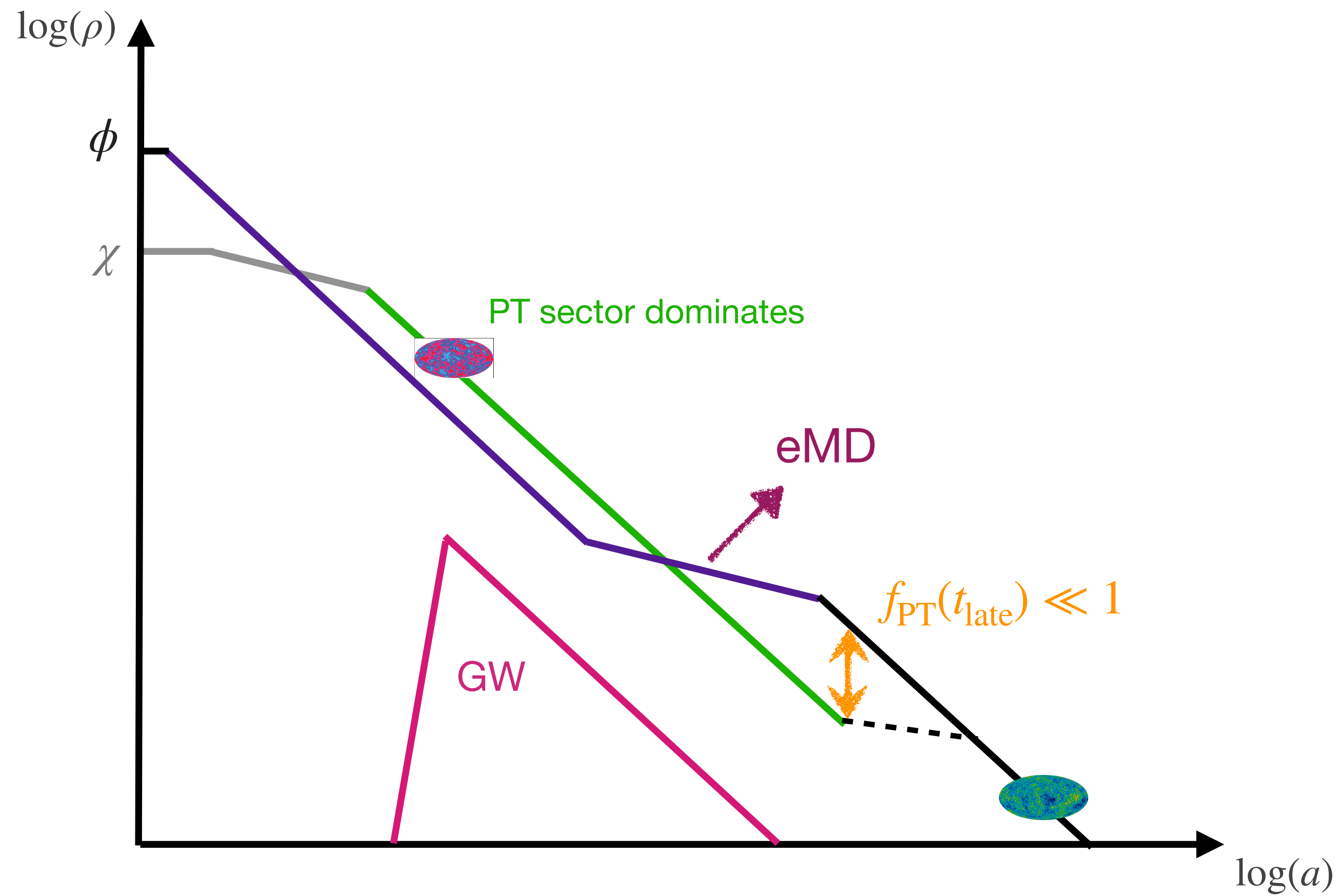
$$h^{TT} \propto \rho_{PT}$$

$$\rho_{GW} \propto (h^{TT})^2 \propto \rho_{PT}^2$$

Can the PT sector be dominant during phase transition?

AB, R. Sundrum: JHEP 06 (2023) 029



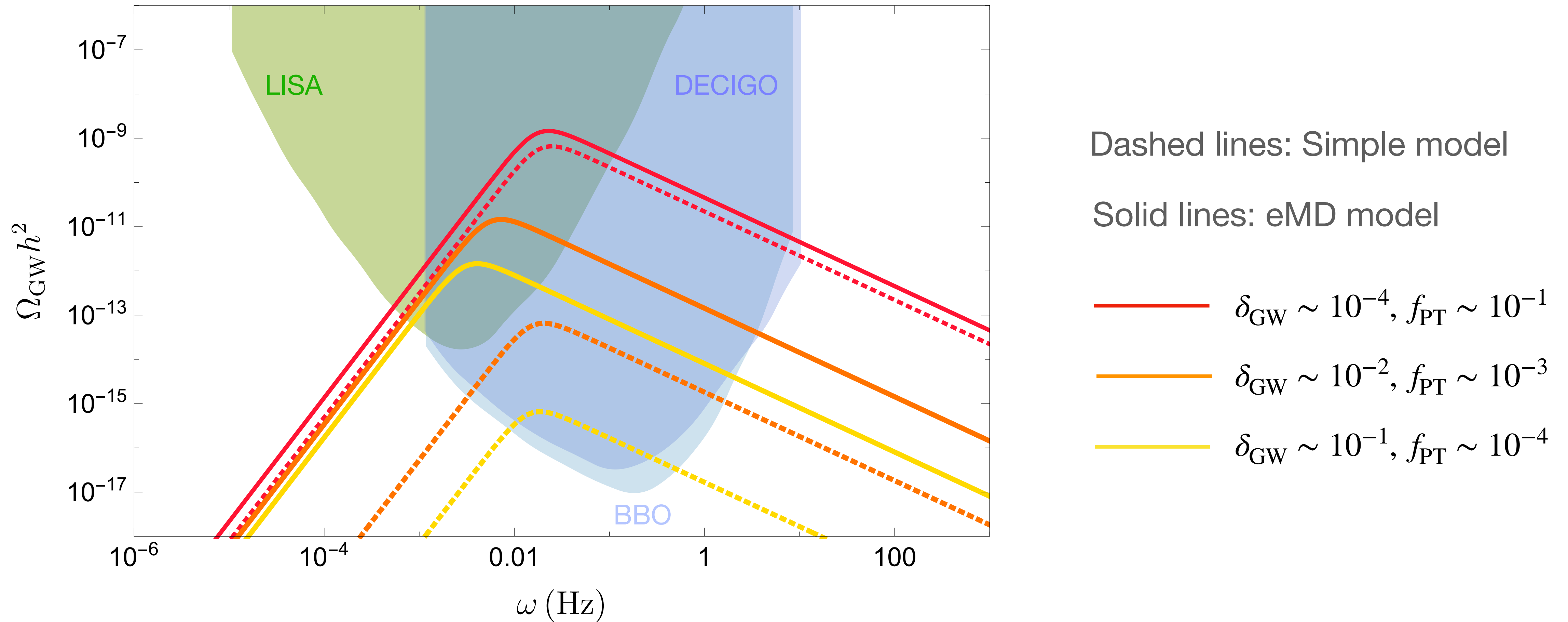


No suppression at production

Relative dilution from eMD

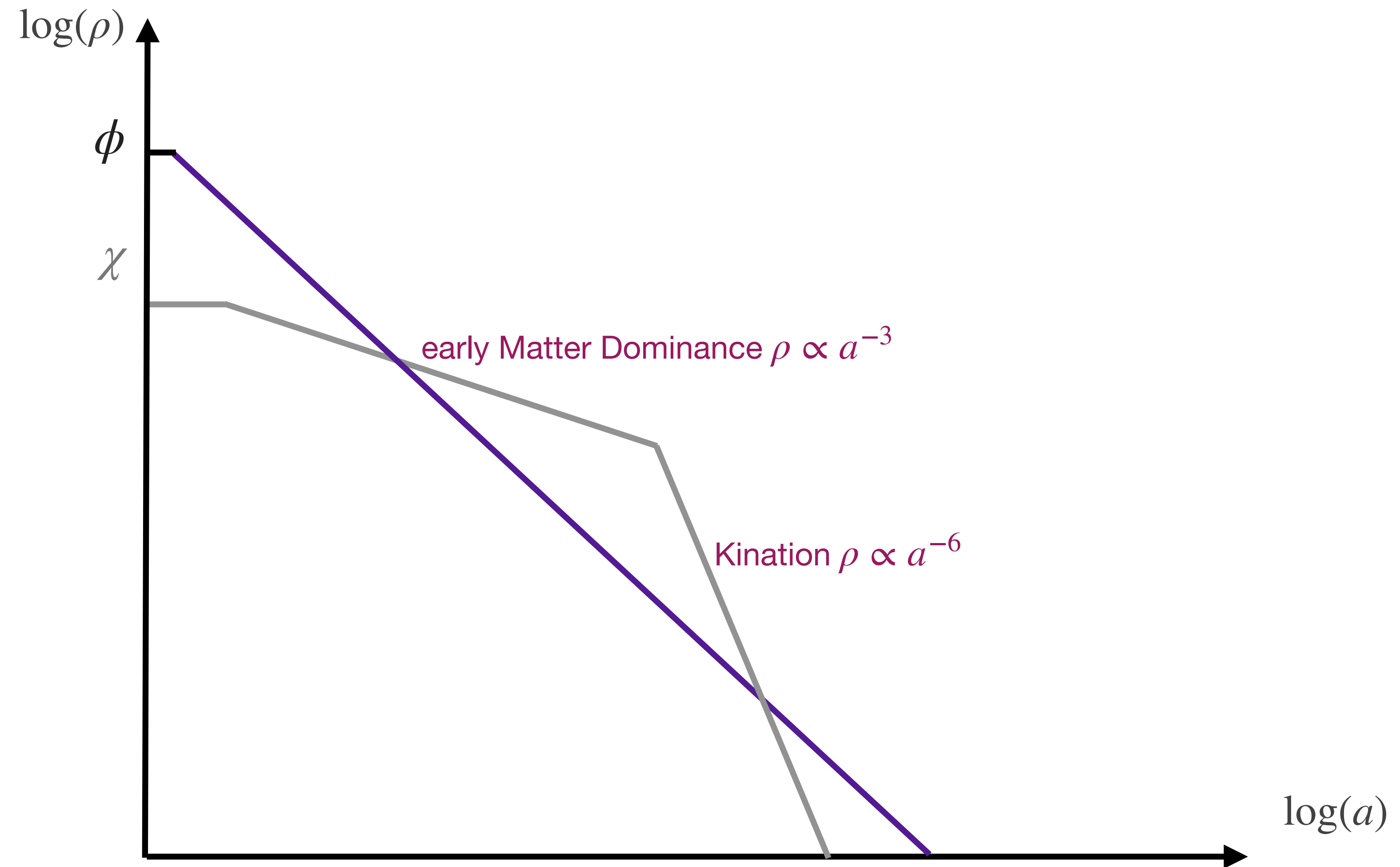
$$\Omega_{\text{GW}}^{\text{today}} \propto f_{\text{PT}} \text{ instead of } f_{\text{PT}}^2$$

Improvement in the GWB signal



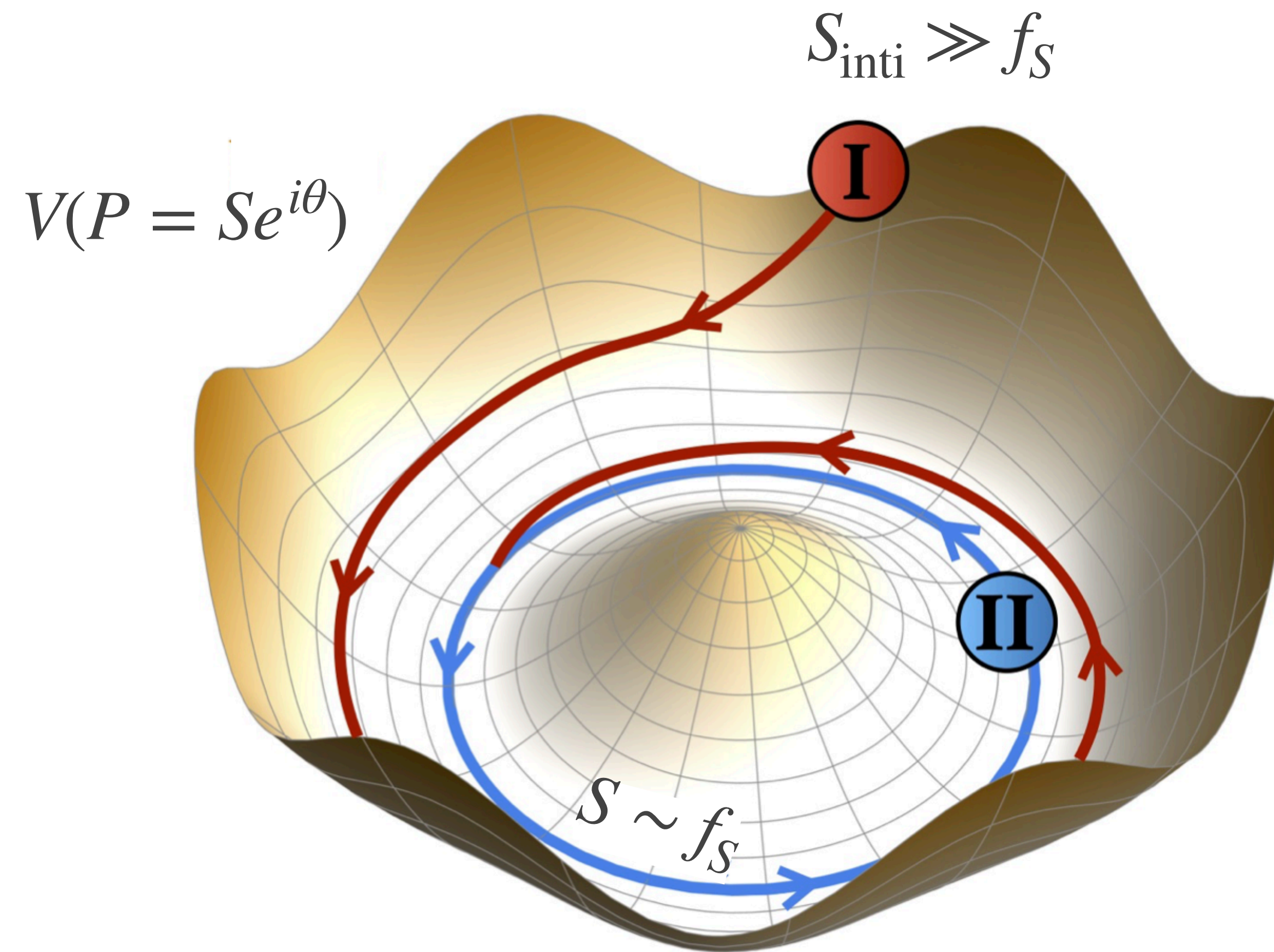
Another possibility

Matter domination followed by a period of kination: rotating ALP field



Rotating axial field

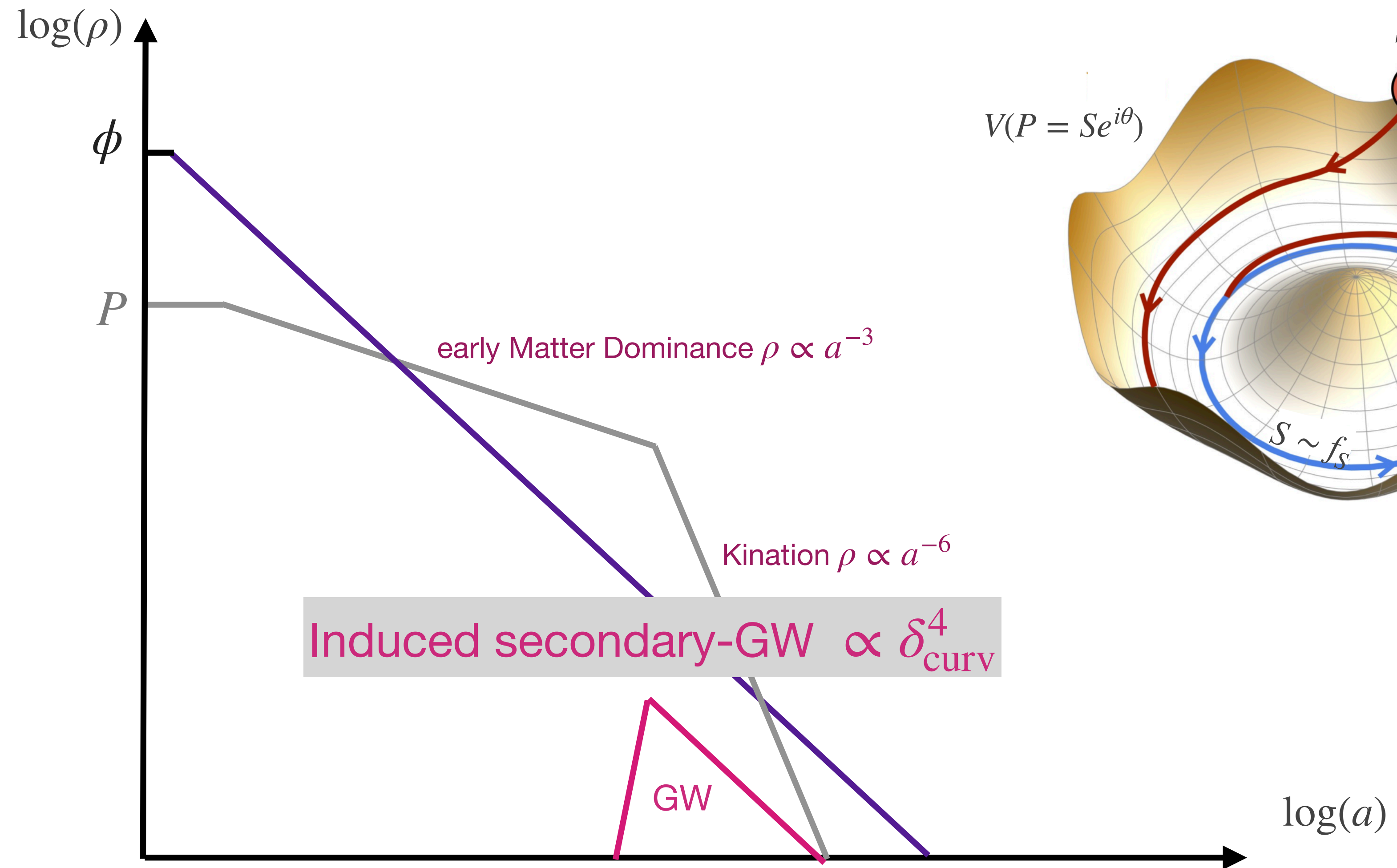
K. Harigaya, R. Co 1910.02080



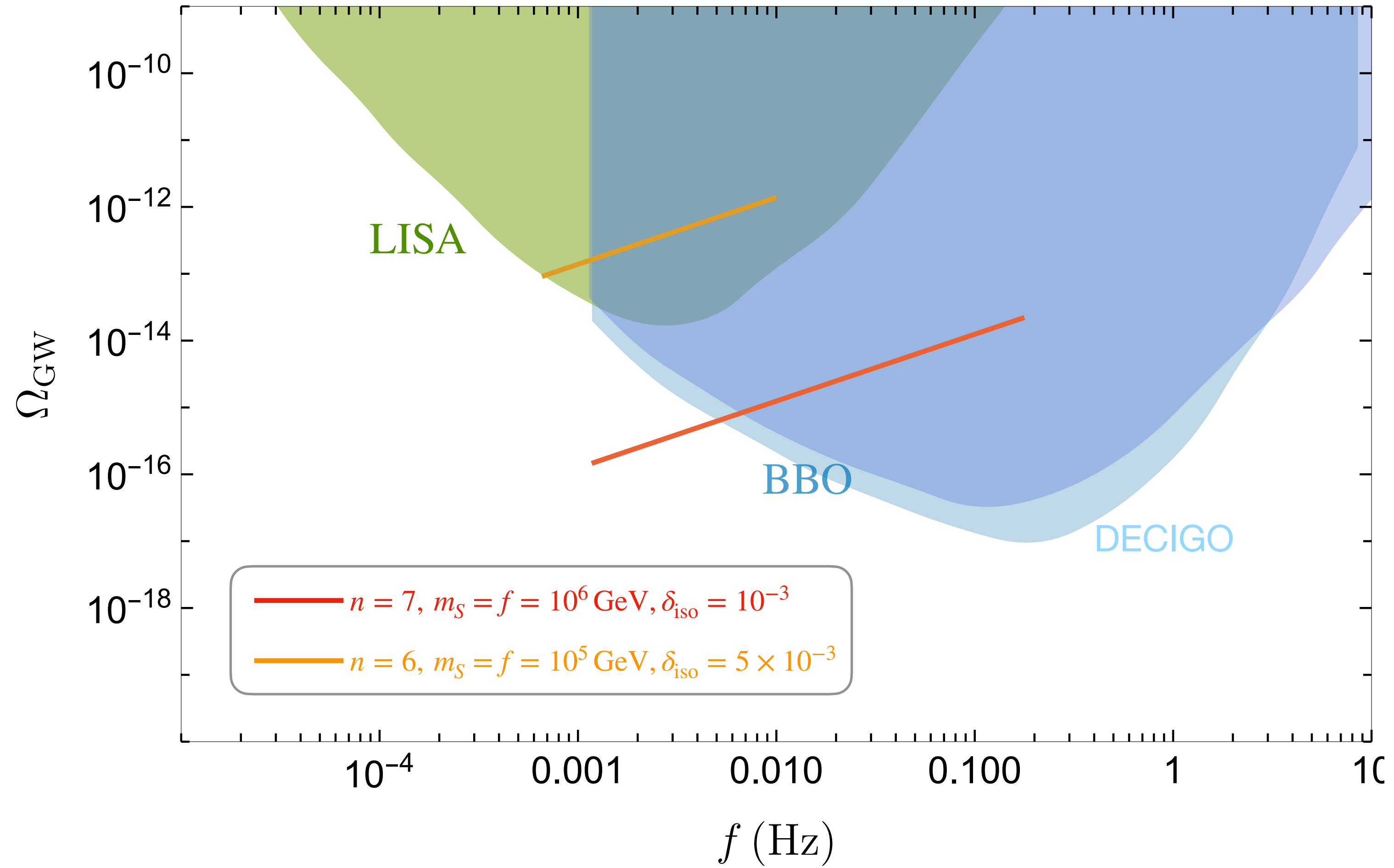
Y. Gouttenoire et al. 2111.01150

Case 2: Induced secondary-GW

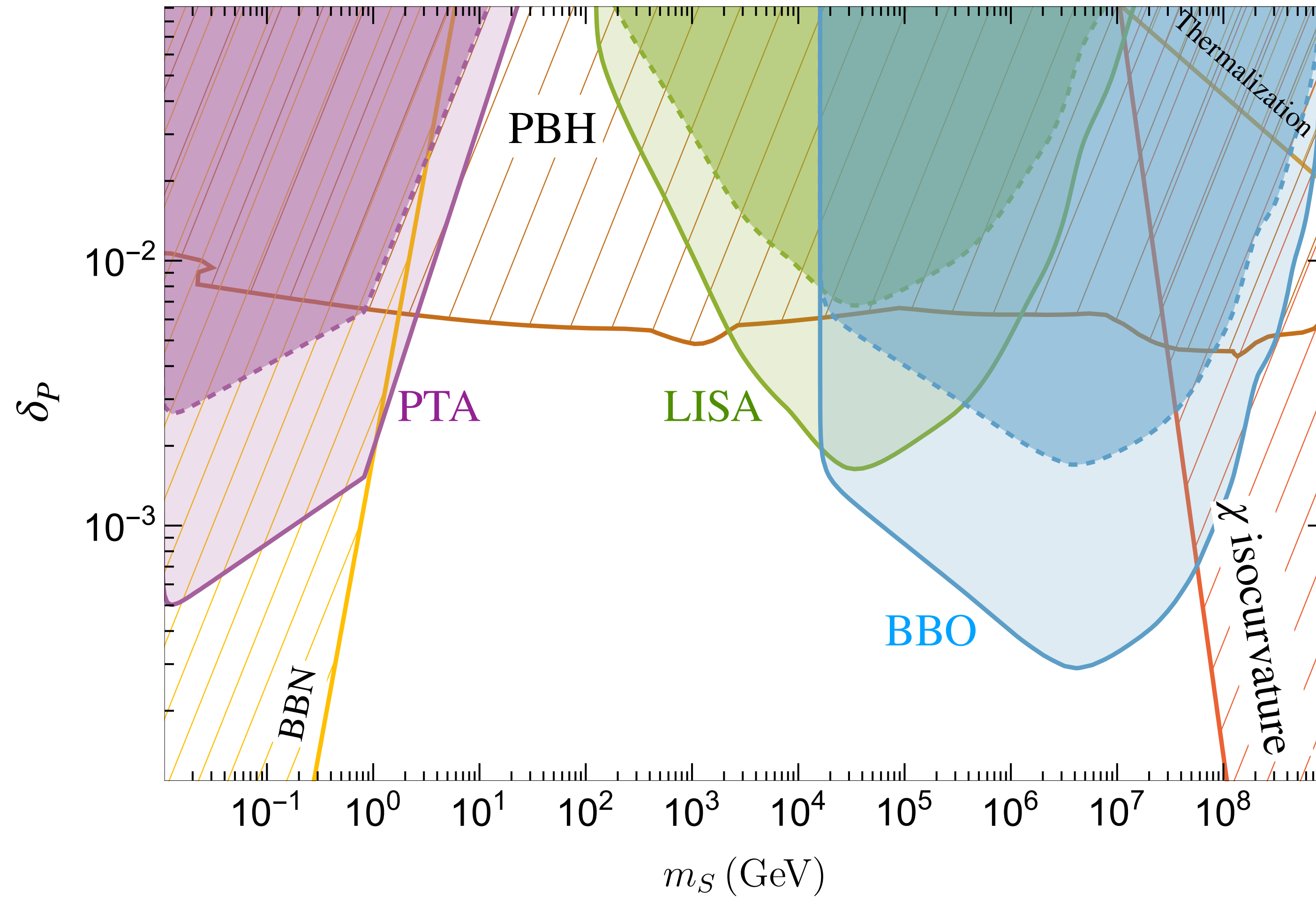
Matter domination followed by a period of kination: rotating ALP field



Preliminary...



Preliminary...

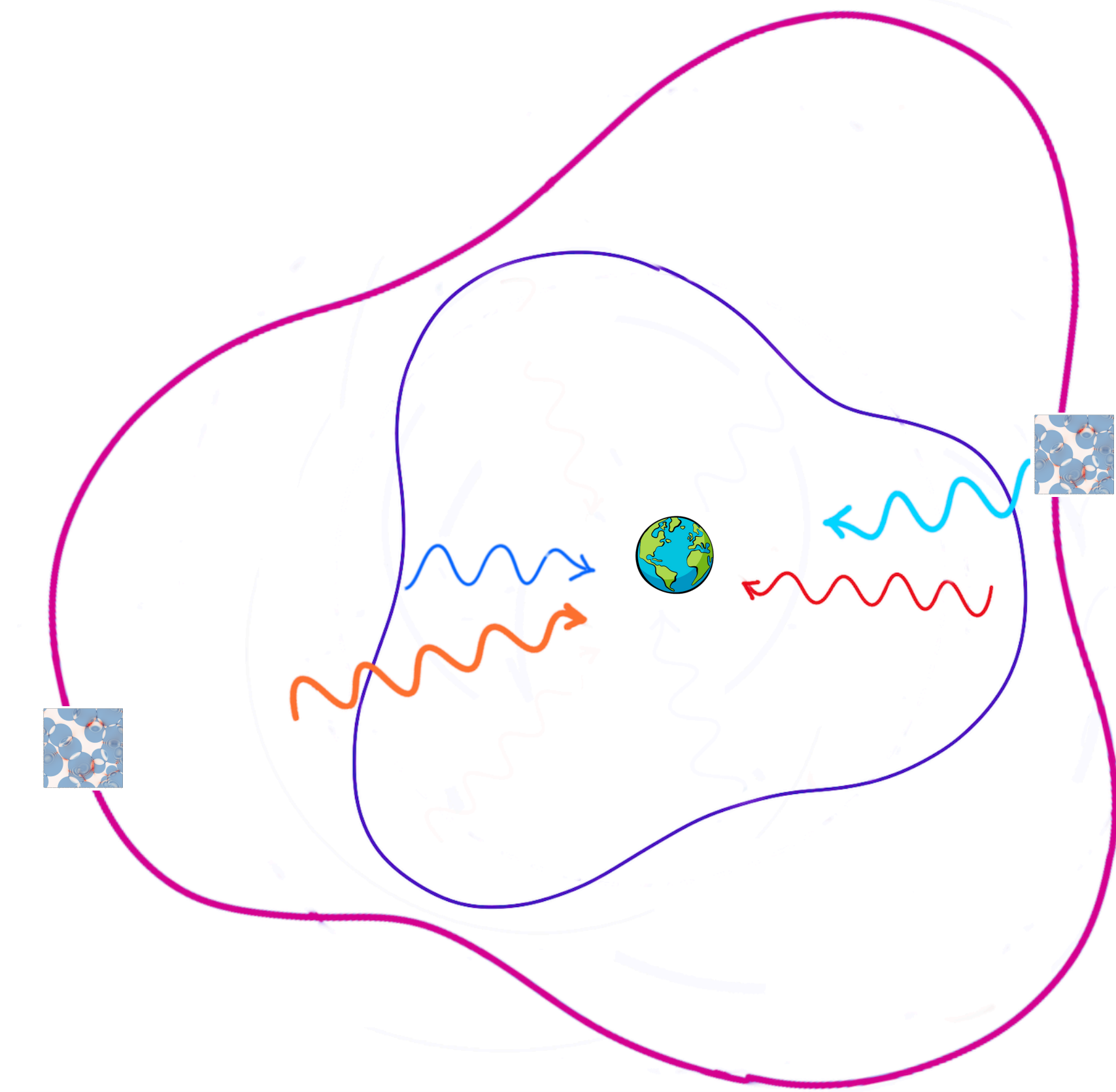


Summary

- There can be new cosmological fluctuation maps significantly different from CMB.
- Such maps can be realized in GWB (first-order phase transition, induced secondary-GW).
- GWB with large (large scale) fluctuations are interesting both experimentally and theoretically.
- Modified post-inflationary cosmologies play an important role in the observability of these highly anisotropic GWB.

Back-up slides

Bubbles are unresolvable

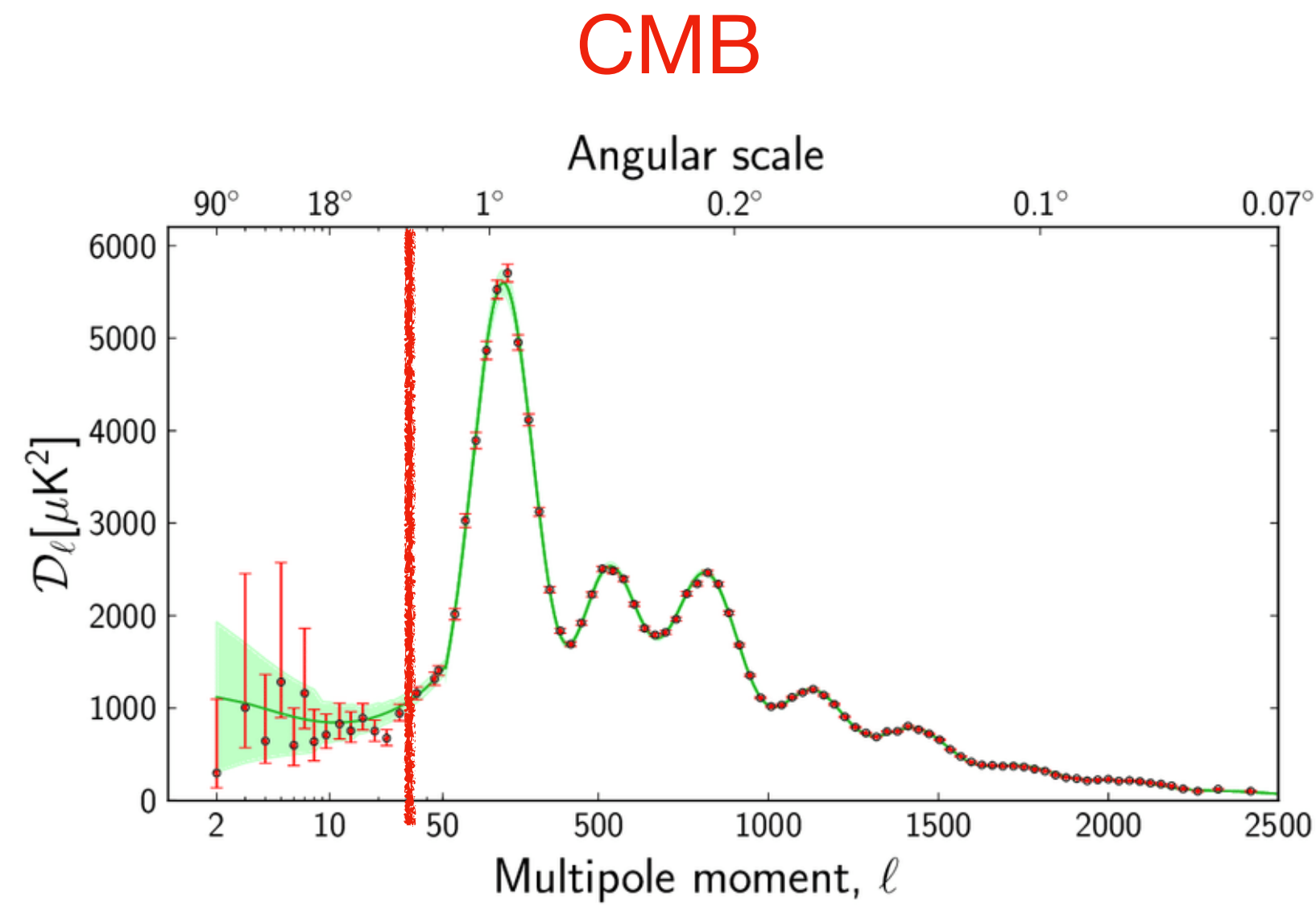


Caution: Zoomed in!

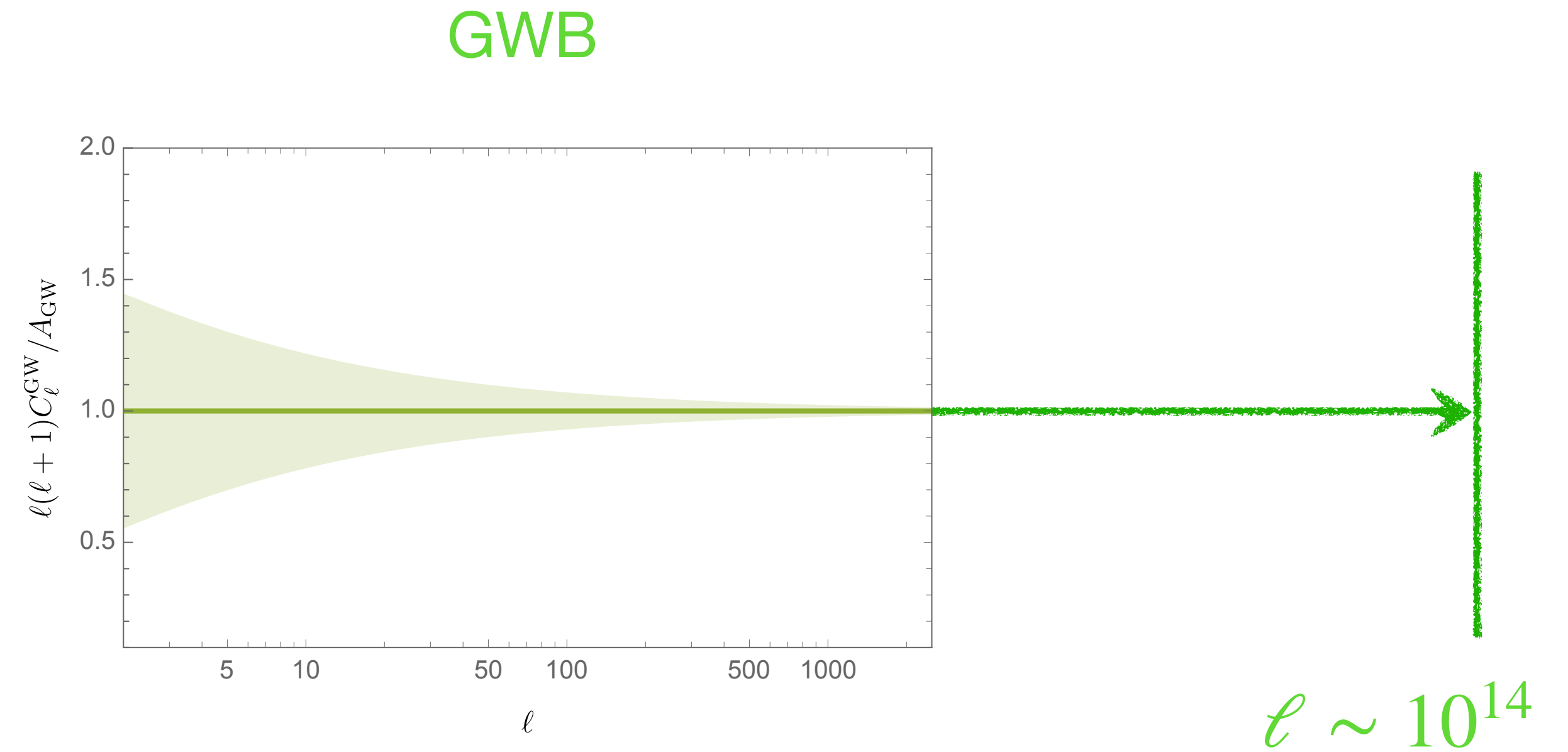
$> 10^{18}$ bubble collisions/arcsec²
⇒ Bubbles are unresolvable
sources : getting a course
grained picture of GWB

GWB is a “pristine” map

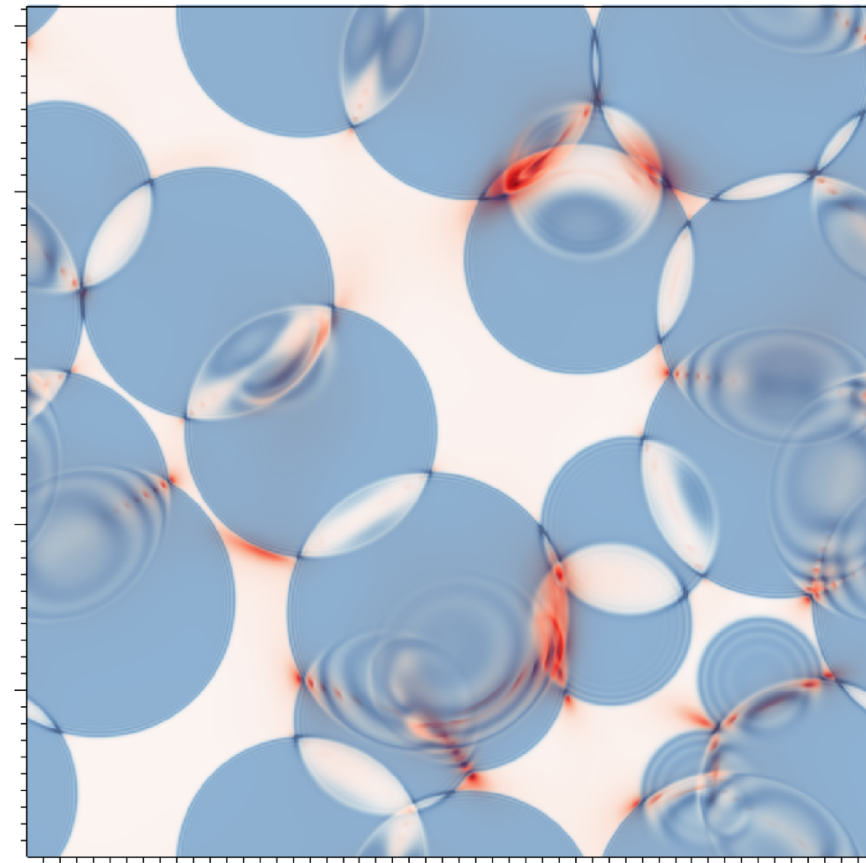
Earlier production + free-streaming of GW → large range of scales is unaltered by sub-horizon physics



Planck



Energy density in GWB from PT (2)



Power released in bubble collision

$$\frac{dE_{\text{GW}}}{dt} \sim G_N \left(\frac{d^3 Q}{dt^3} \right)^2$$

Quadrupole moment

$$Q \sim \rho_{\text{lat}} r^5 \rightarrow \frac{d^3 Q}{dt^3} \sim \rho_{\text{lat}} \frac{r^5}{(\Delta t_{\text{PT}})^3}$$

Typical time scale /length scale
(Duration of the PT)

$$r \sim \Delta t_{\text{PT}} \equiv \beta^{-1}$$

GW energy density released in bubble collision

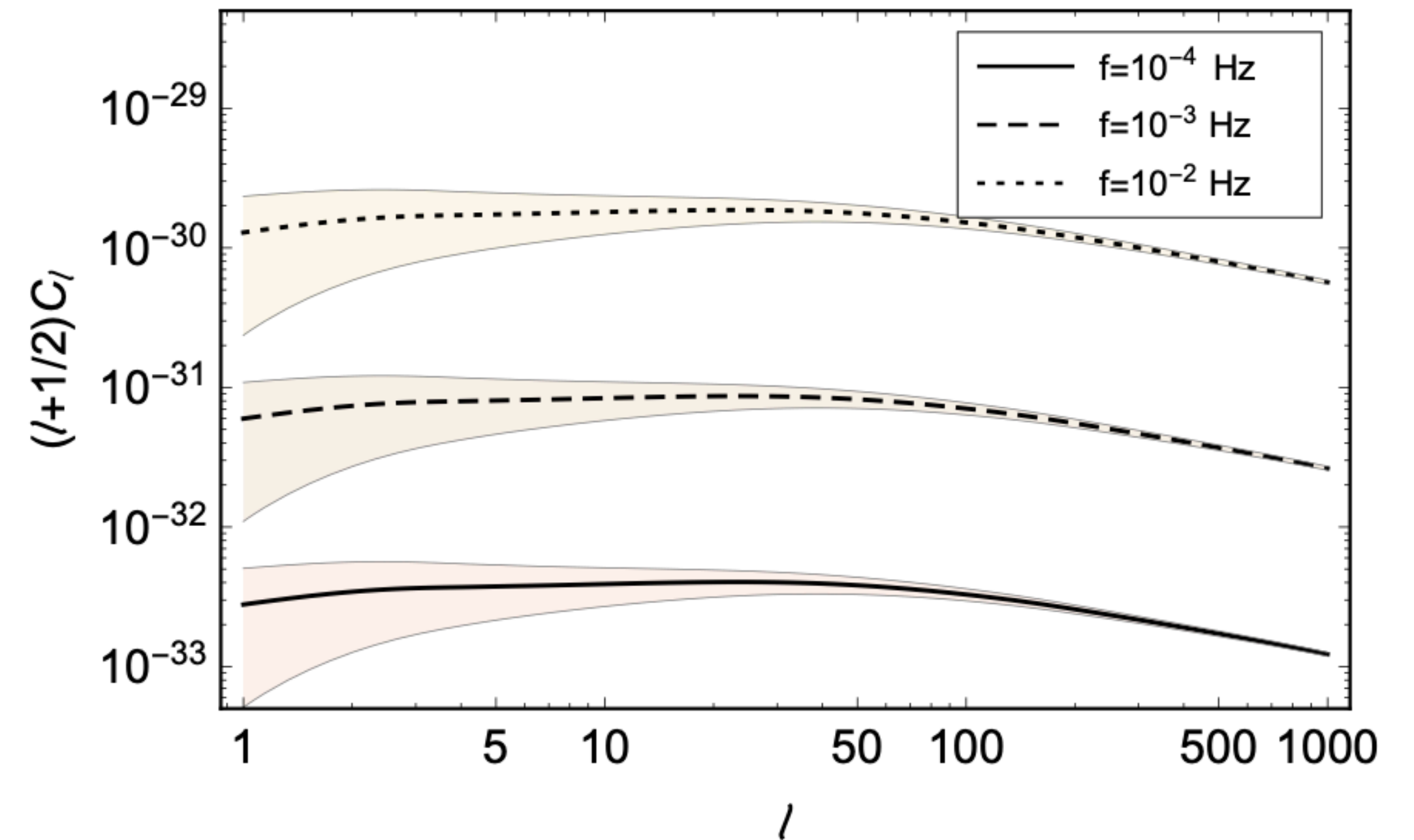
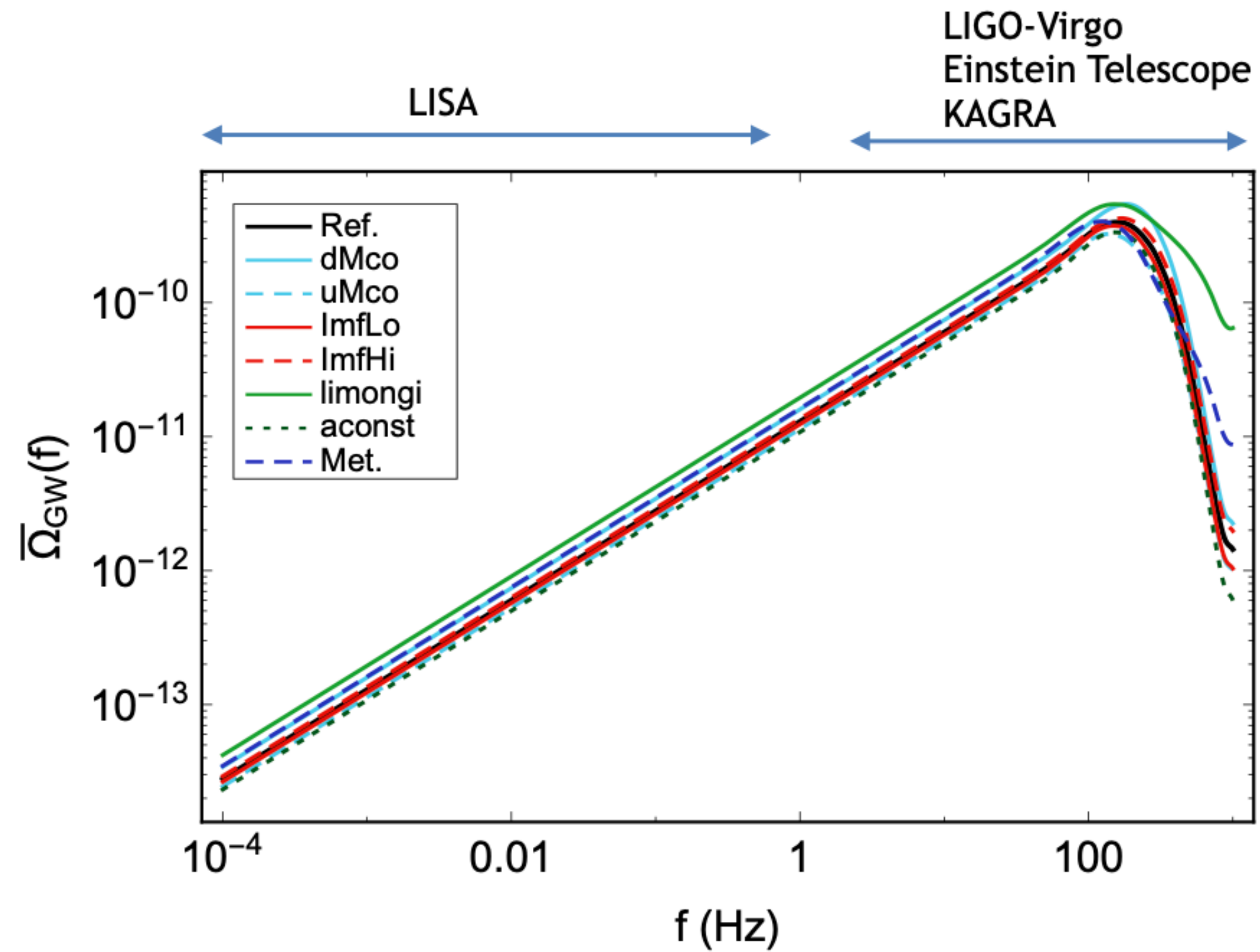
$$\rho_{\text{GW}} \sim \frac{dE_{\text{GW}}}{dt} \frac{\Delta t_{\text{PT}}}{r^3} \sim \frac{G_N \rho_{\text{lat}}^2}{\beta^2}$$

$$G_N \rho_{\text{total}} \sim H^2$$

$$\rho_{\text{GW}} \sim \left(\frac{H}{\beta} \right)^2 \left(\frac{\rho_{\text{lat}}}{\rho_{\text{total}}} \right)^2 \rho_{\text{total}}$$

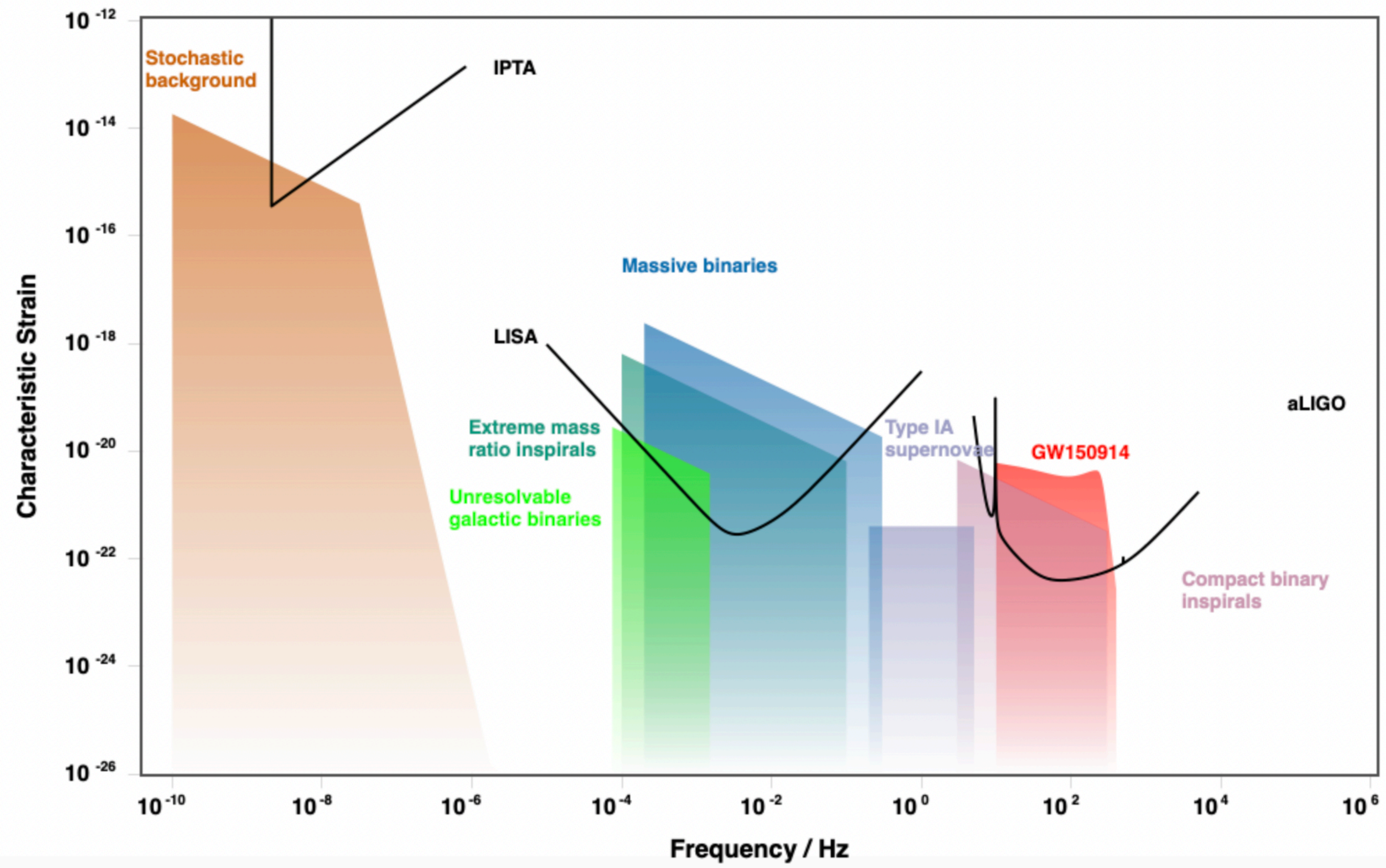
Astrophysical foregrounds in mHz range

Inspiring stellar-mass BH



Giulia Cusin, Irina Dvorkin, Cyril Pitrou, Jean-Philippe Uzan: 1904.07757v2

Also see: 2201.08782v from LISA working group



rhcole.com/apps/GWplotter/