

New era in dark matter searches the dawn of the (nuclear) clocks

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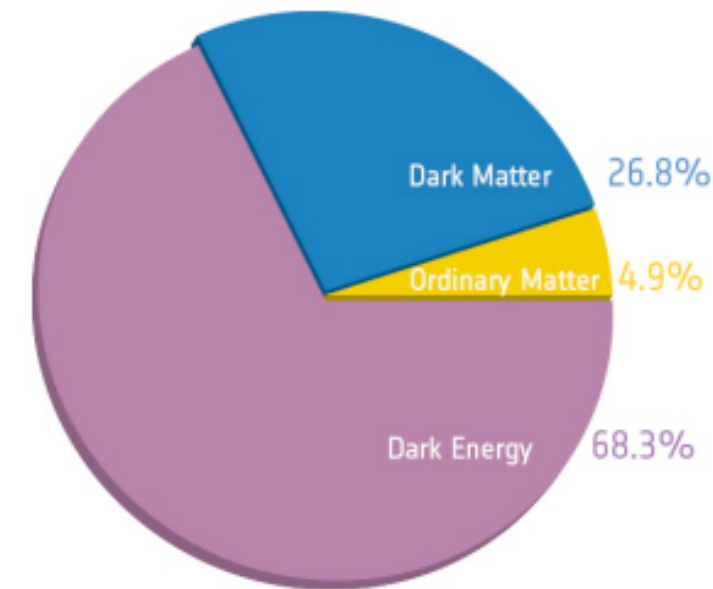


Outline

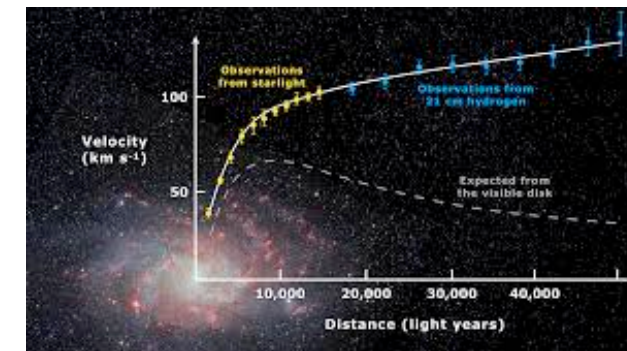
- Intro. (spin-0) ultralight dark-matter (UDM)
- Current status, UDM searches
- Nuclear clock (news, robustness & sensitivity)
- Summary

Usually in this part we discuss:

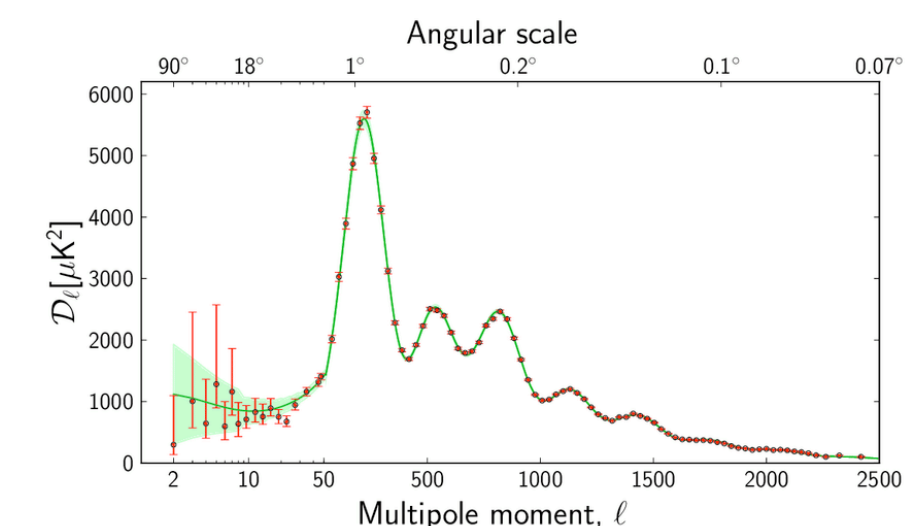
- **Unseen Mass:** The dark matter (DM) constitutes about 85% of the total mass of the universe



- **Galaxy Formation & rotation curves:** The gravitational influence of DM plays vital role in formation and evolution of galaxies & motions of stars



- **Cosmic Microwave Background (CMB):** Observations of the temperature fluctuations shows excellent agreement with the Λ CDM model



Instead we'll take a different path following a theorist perspective

If you study the literature you'd find $\mathcal{O}(10^4)$ papers of model building of dark matter

Showing 1–50 of 11,662 results

Search v0.5.6 released 2020-

Query: order: -announced_date_first; size: 50; classification: Physics (grp_physics)::High Energy Physics - Phenomenology (hep-ph); include_cross_list: True; terms: AND abstract=model; AND abstract=dark; AND abstract=matter

Refine query

New search

50

results per page. Sort results by

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4

5

...

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1. [arXiv:2404.03963](#) [pdf, other] hep-ph astro-ph.CO

Composite Dark Matter with Forbidden Annihilation

Authors: [Tomohiro Abe](#), [Ryosuke Sato](#), [Takumu Yamanaka](#)

Abstract: A **dark matter model** based on QCD-like $SU(N_c)$ gauge theory with electroweakly interacting **dark** quarks is discussed. Assuming the **dark** quark mass m is smaller than the dynamical scale... [More](#)

Submitted 5 April, 2024; originally announced April 2024.

Comments: 30 pages, 11 figures

Report number: OU-HET-1219

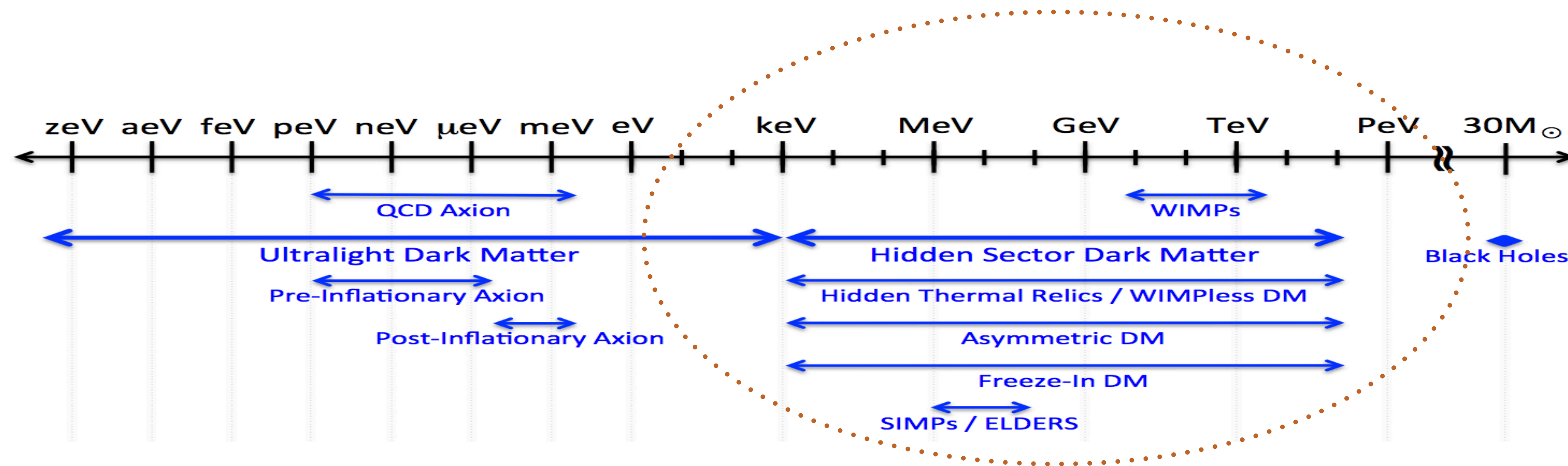
2. [arXiv:2404.03666](#) [pdf, other] hep-ph

Exploring the Frontiers: Challenges and Theories Beyond the Standard Model

Authors: [Dhananjay Saikumar](#)

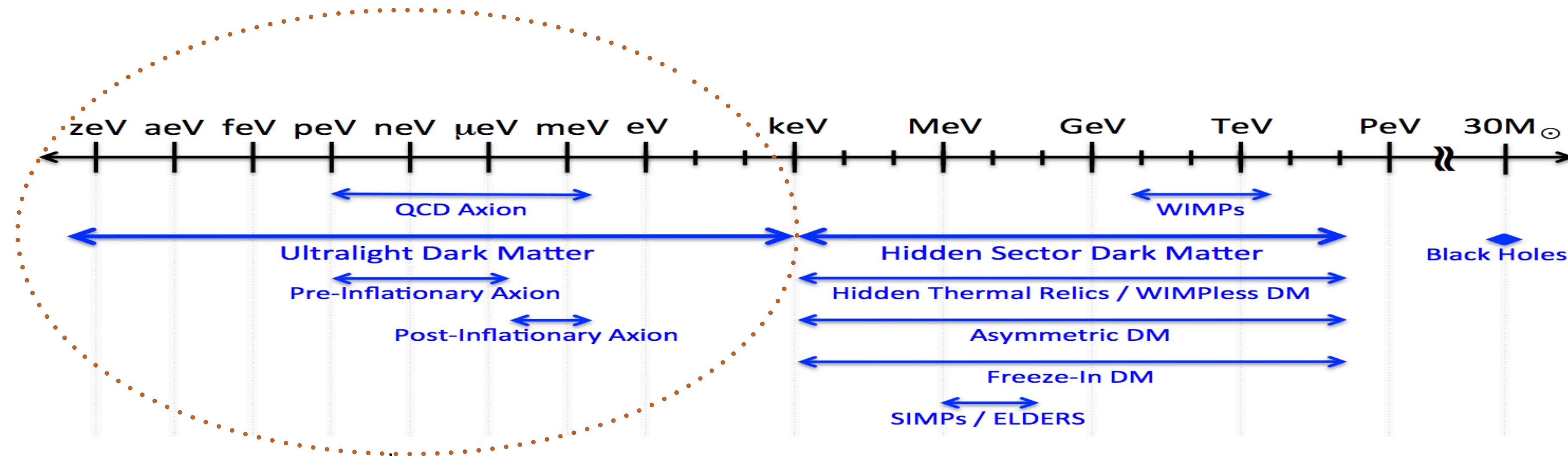
Abstract: Quantum Field Theory (QFT) forms the bedrock of the Standard **Model** (SM) of particle

The space of possible theories is vast, but some of it is rather involved ...



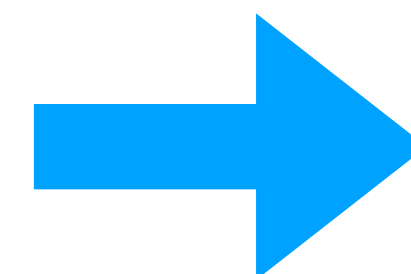
Heavy, super-eV thermal dark matter (DM)
behaves as gas of individual quanta
indep. of initial conditions (thermal)
however, viable models are non-minimal

The space of possible theories is vast, but some of it is rather involved ...



Ultralight sub-eV DM (UDM)

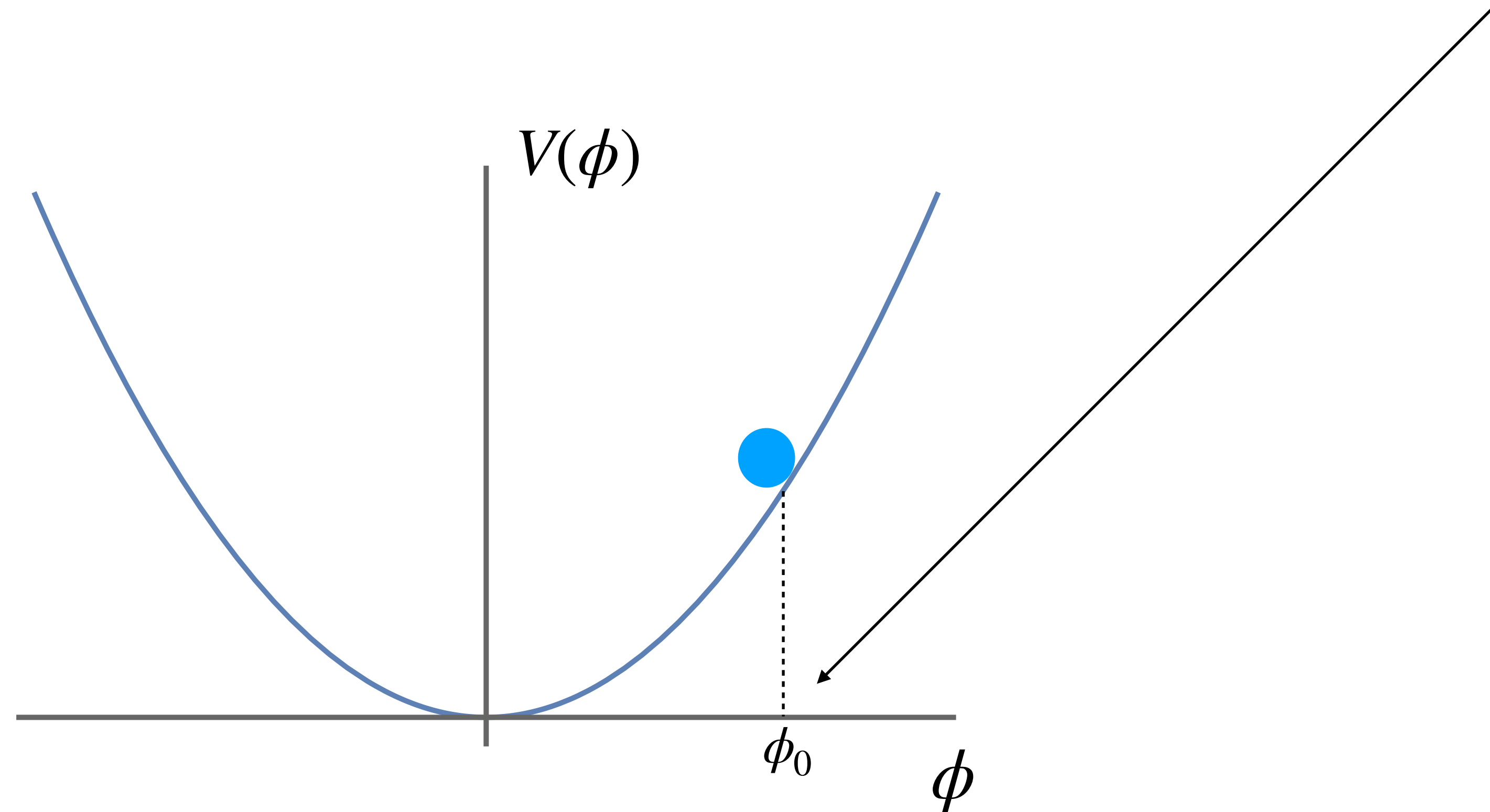
DM behaves as homogenous classical field
initial condition dependent (non-thermal)
viable very simple models, but hard to probe



Our focus today

The simplest ever model of ultralight dark matter

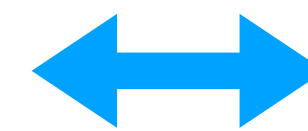
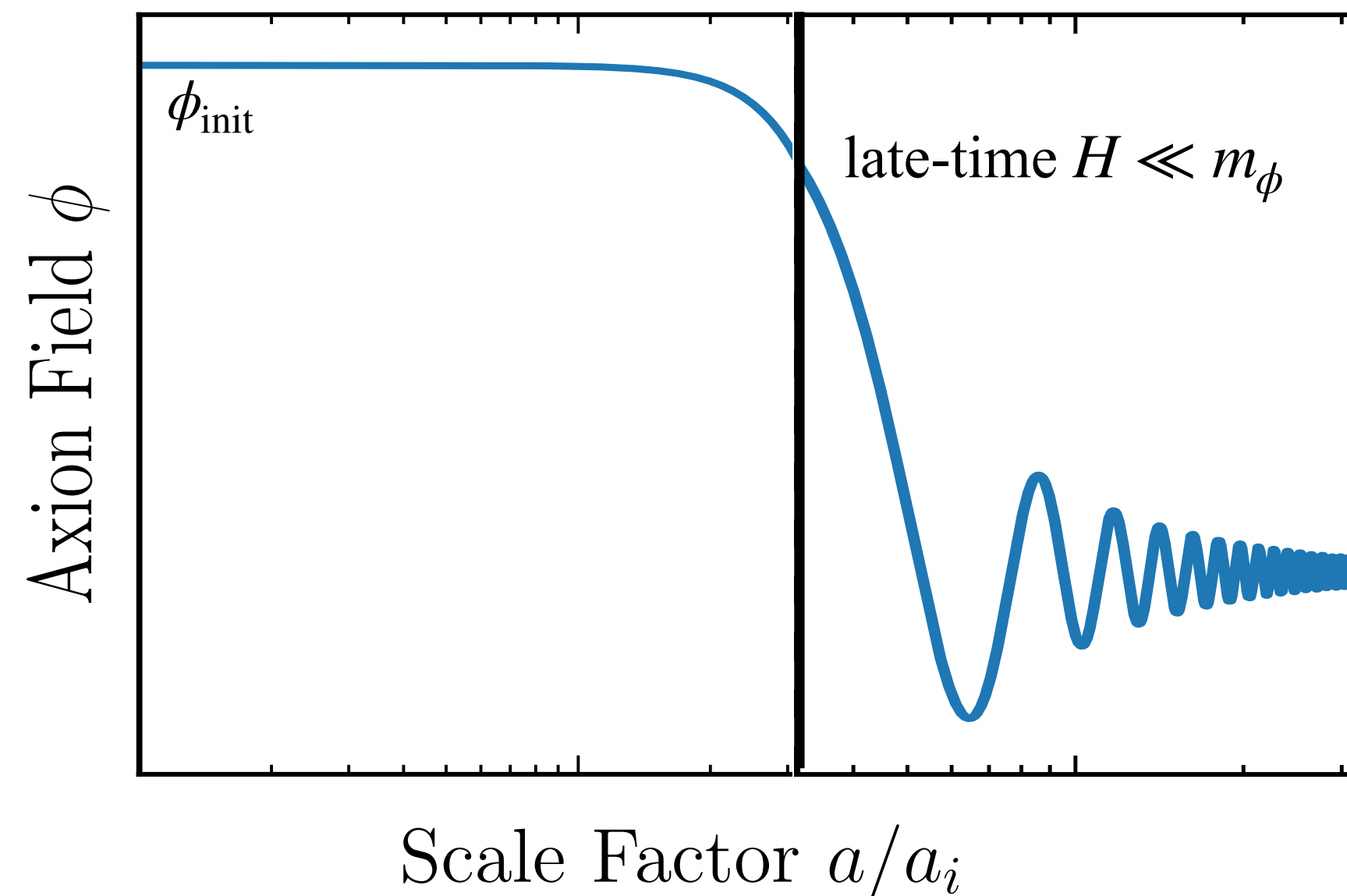
- Just free (pseudo-) scalar light field, $\mathcal{L} \in m_\phi^2 \phi^2$, with some initial homogenous condition, $\phi_{\text{init}} = \phi_0$



- What would be the cosmological evolution of such a field (assume $H \ll m_\phi$) ?

Late time evolution of scalar field, approximate oscillatory

- Just free (pseudo-) scalar light field, $\mathcal{L} \in m_\phi^2 \phi^2$, with some initial homogenous condition, $\phi_{\text{init}} = \phi_0$
- The field oscillates around the minimum with late-time solution looks like:



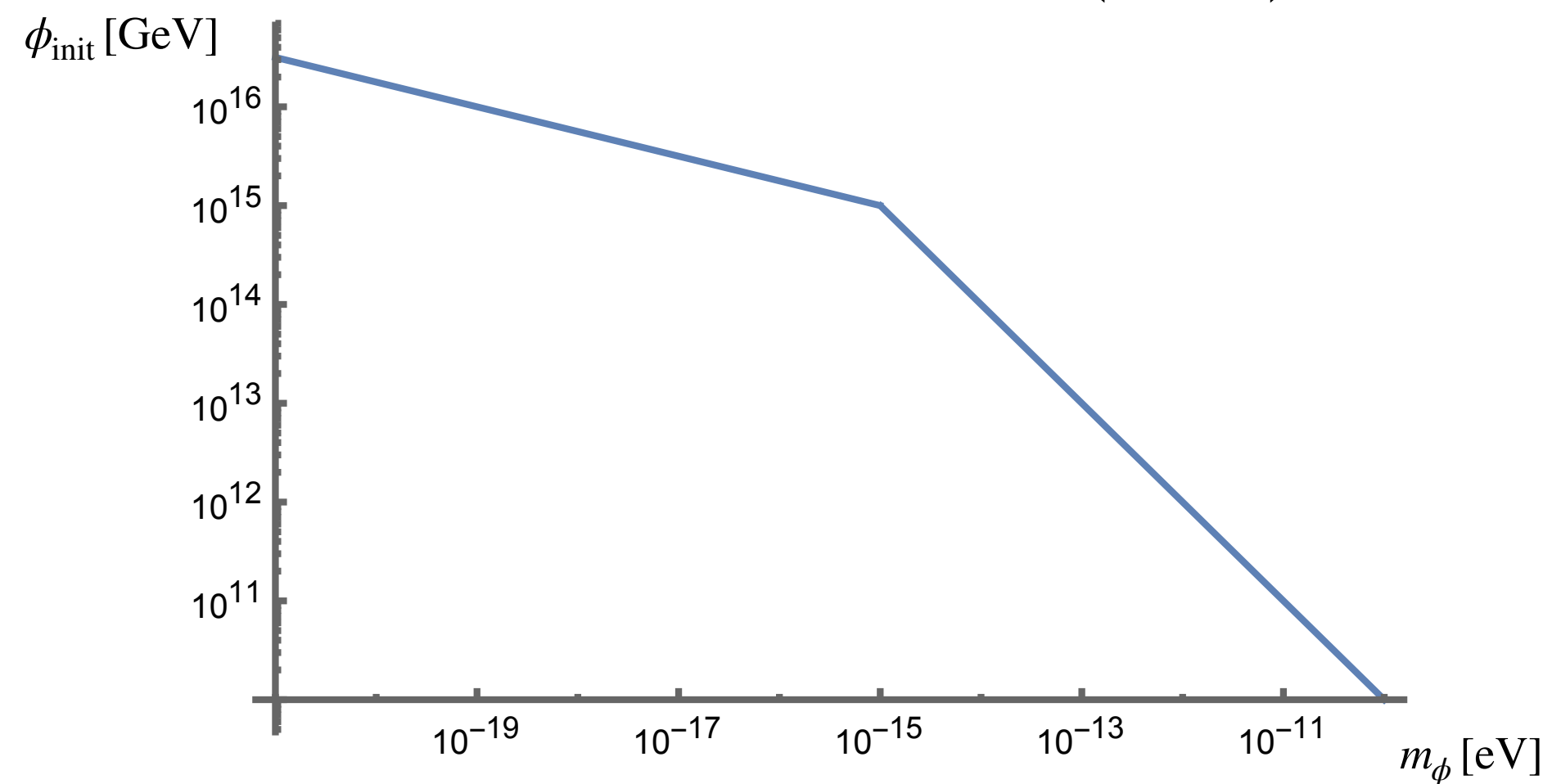
$$\phi(t) \approx \phi_0 \left(\frac{a_i}{a} \right)^{\frac{3}{2}} \cos(m_\phi t)$$

Implication for ultralight dark matter (UDM) cosmology

● What is the impact of the scalar field behavior $[\phi(t) \approx \phi_0 \left(\frac{a_i}{a}\right)^{\frac{3}{2}} \cos(m_\phi t)]$ on the cosmology:

(i) The EOS satisfies $w_\phi = p_\phi/\rho_\phi = 0$, and the energy density scales as $\rho_\phi \propto a^{-3} \Leftrightarrow$ ordinary matter

(ii) The density goes like amplitude square, $\rho_\phi \sim \phi_0^2 \left(\frac{a}{a_{\text{osc}}}\right)^{-3} \Rightarrow$ the DM density is mapped to initial value, ϕ_0 :



$$\phi_{\text{init}} \equiv \theta f(f_{\text{min}}) = \begin{cases} 10^{18} \text{ GeV} \left(\frac{10^{-27} \text{ eV}}{m_\phi}\right)^{\frac{1}{4}} & m_\phi \lesssim 10^{-15} \text{ eV} \\ 10^{15} \text{ GeV} \left(\frac{10^{-15} \text{ eV}}{m_\phi}\right) & m_\phi \gtrsim 10^{-15} \text{ eV} \end{cases}$$

[assuming (“best case”) MeV reheating]

(iii) Can be it considered as a classical field? $N_\phi^{\text{occup}} \sim 10^3 \times \left(\frac{\text{eV}}{m}\right)^4 \Rightarrow$ sub-eV UDM behaves classically

Ultralight scalar => simplest dark matter (DM) model

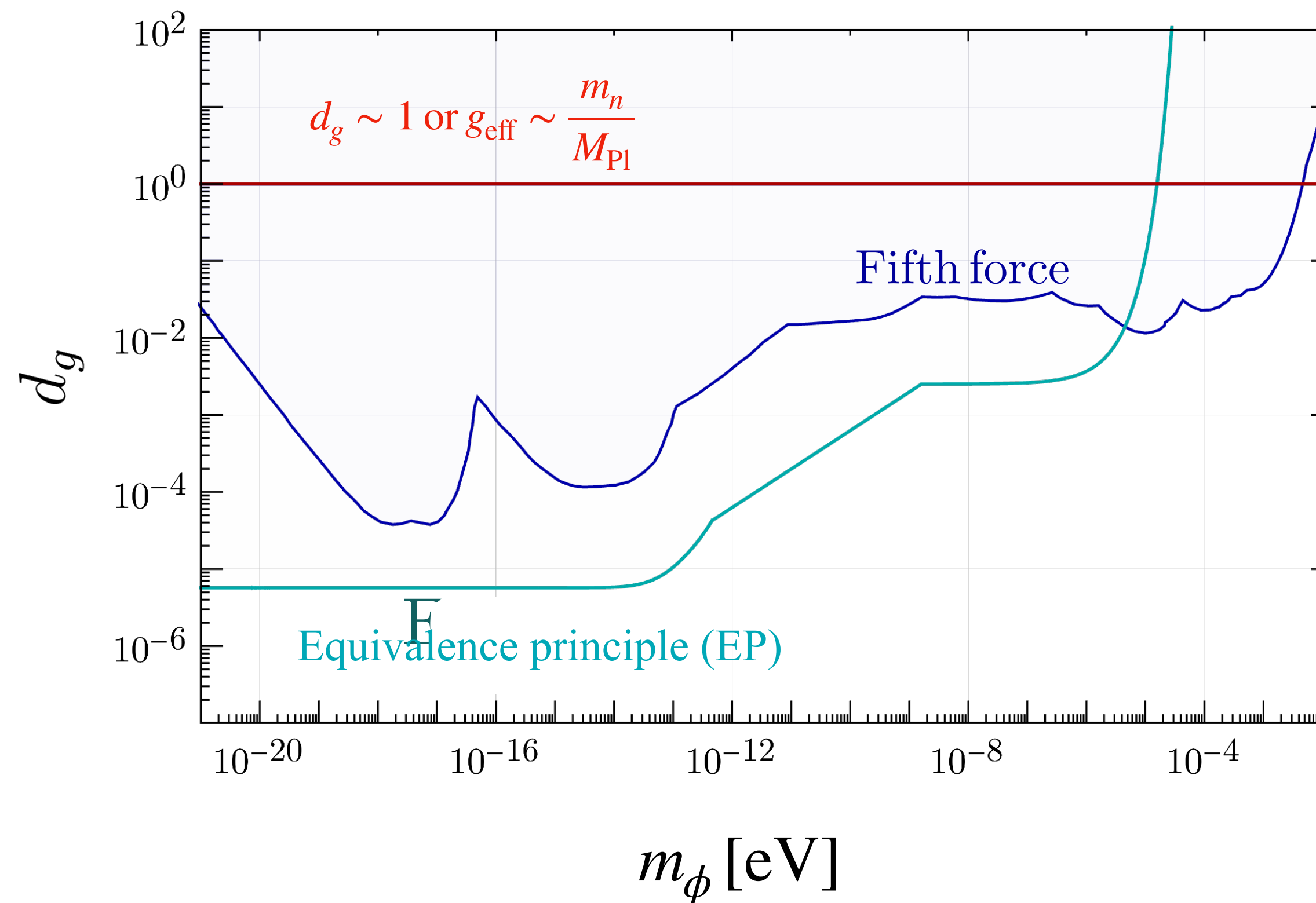
- A sub-eV misaligned homogeneous scalar field => viable DM model
- Its amplitude oscillates with frequency equal to its mass, $\omega \sim \text{Hz} \times \frac{m_\phi}{10^{-15} \text{ eV}}$
- However, this field has no coupling to us (apart from gravitational), how can we search for it?
- A minimal plausible assumption is that it'd couple to us suppressed by some very high scale (Planck suppressed?), which are extremely weak, for instance:

scalar coupling
effecting energy levels
pseudo-scalar axial coupling
magnetic/spin-observables

$$\mathcal{L}_{\text{Pl}} \in d_g \frac{\alpha_s}{\pi} \frac{\phi}{M_{\text{Pl}}} GG + \frac{a}{32\pi^2 f} G\tilde{G} \implies d_g \frac{m_n}{M_{\text{Pl}}} \phi \bar{n}n + \frac{m_n}{f} a \bar{n}\gamma_5 n$$

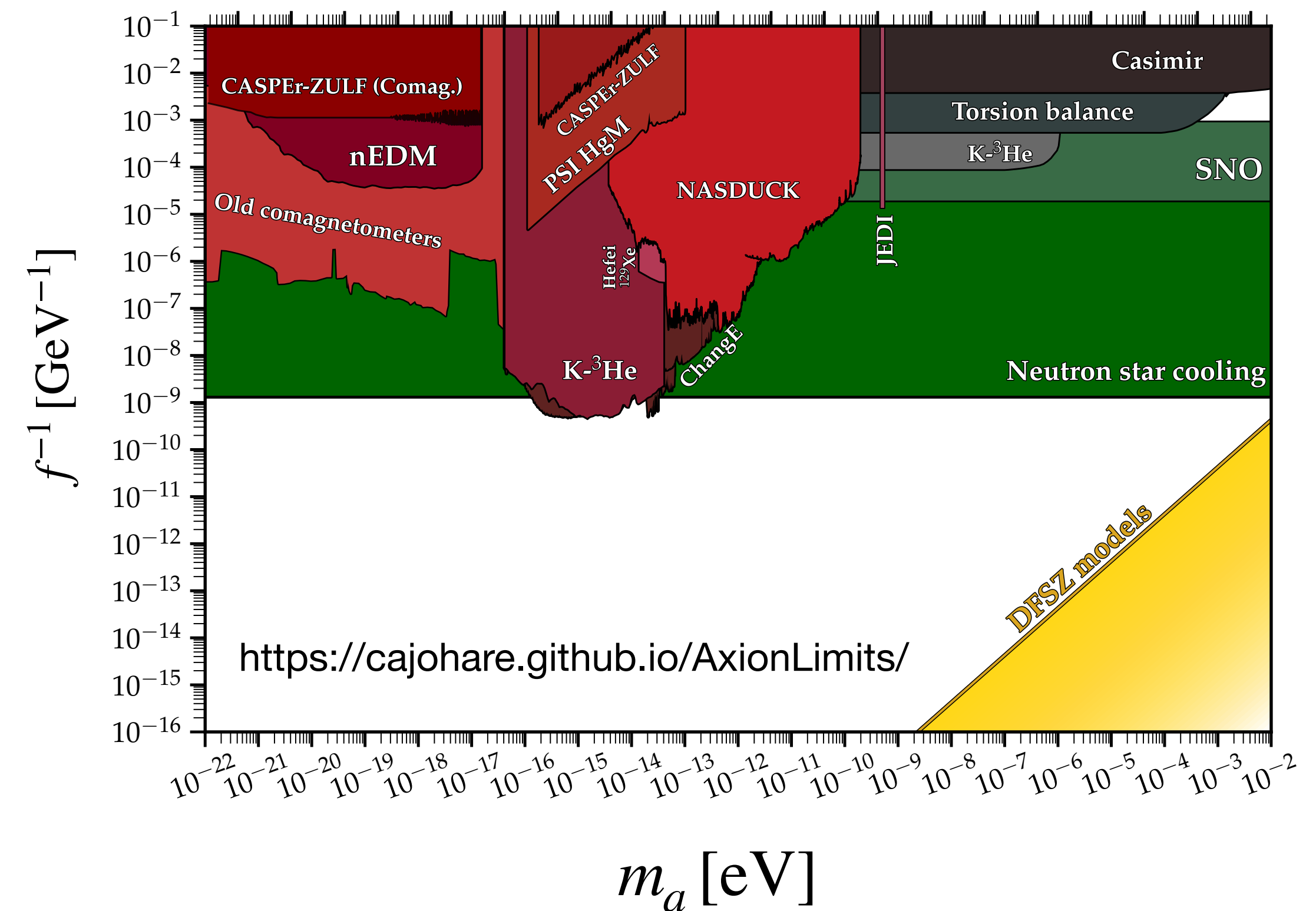
Scalar coupling vs/ pseudo-scalar axial coupling

$$\mathcal{L}_{\text{Pl}} \in d_g \frac{\phi}{M_{\text{Pl}}} \frac{\alpha_s}{\pi} GG \implies d_g \frac{m_n}{M_{\text{Pl}}} \phi \bar{n}n$$



EP: Planck suppressed operators excluded for $m_\phi \lesssim 10^{-5}$ eV
 5th force: operators are excluded for $m_\phi \lesssim 10^{-3}$ eV

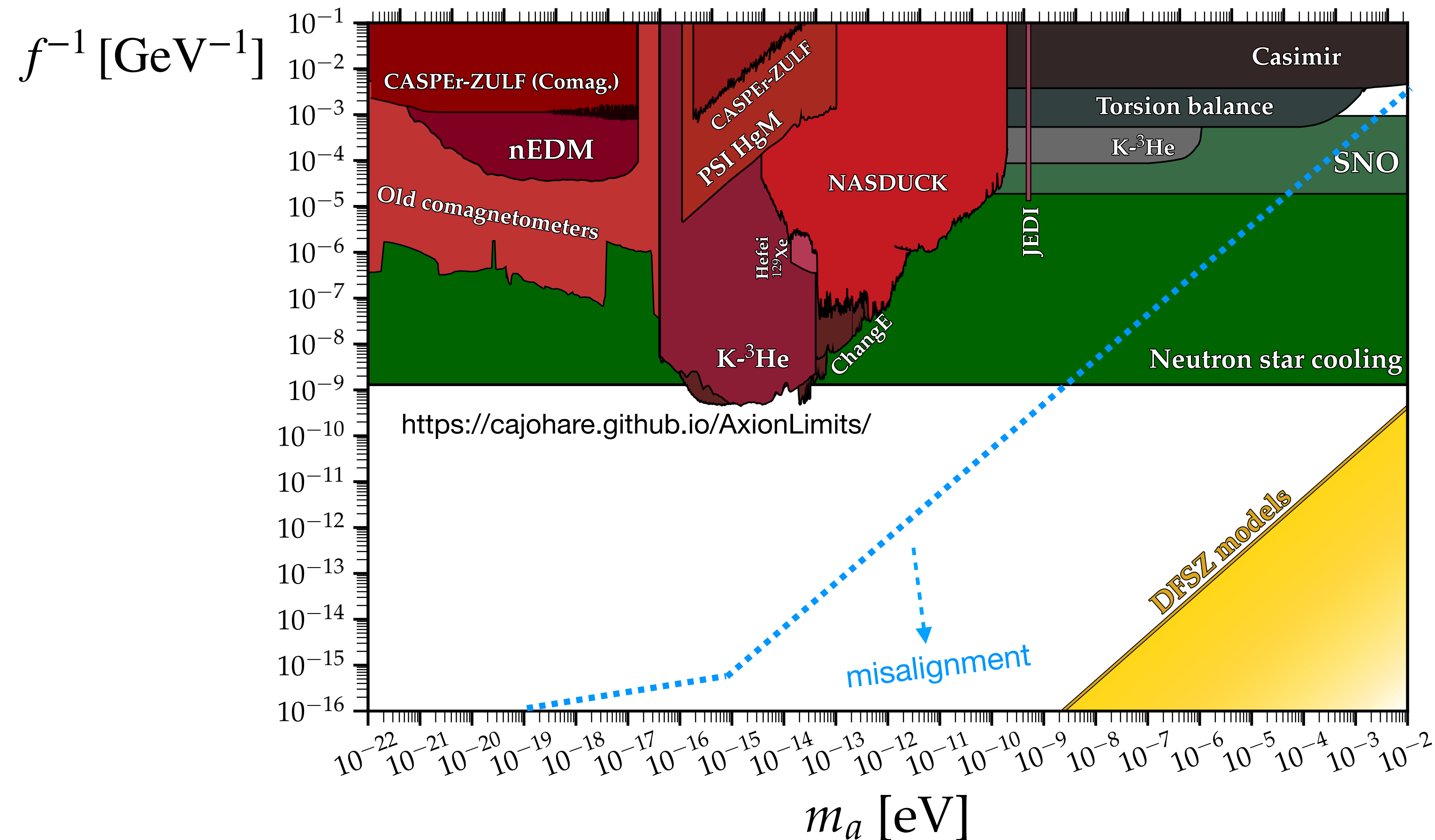
$$\mathcal{L}_{\text{axion}} \in \frac{a}{32\pi^2 f} G\tilde{G} \implies \frac{m_n}{f} a \bar{n}\gamma_5 n$$



Bounds only constrain coupling that are $\sim 10^{12}$ weaker than the Planck scale

Status of ultralight dark matter (ULDM) pseudoscalar axial coupling

$$\mathcal{L}_{\text{axion}} \in \frac{a}{32\pi^2 f} G\tilde{G}$$



Bounds are significantly weaker than scalar ones & in most regions far from probing minimal misalignment ULDM models

Axion - the scalar way, the power of clocks #1

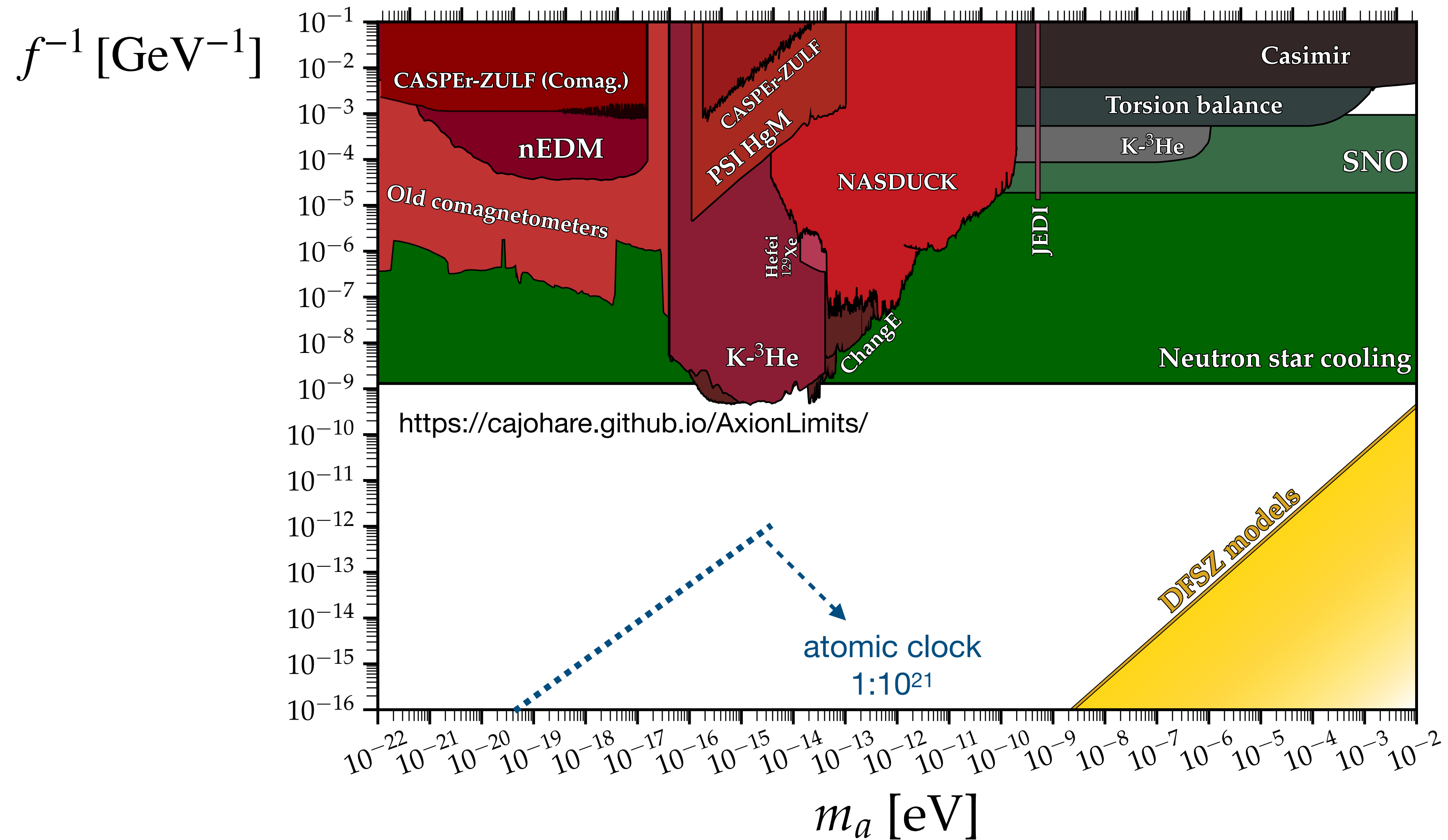
- Maybe should accept that probing axions is work in progress (new proposals)
- The sensitivity to scalar interaction is 10^{12} stronger, can we use it?
- Axion models do predict quadratic scalar coupling that are suppressed however by $m_a^2/f^2 \Rightarrow$ hopeless to probe
- Yet, in the case of QCD-like-axion only suppressed by $\frac{\partial \ln m_\pi}{\partial \theta^2} \sim \frac{m_{u,d}}{\Lambda_{\text{QCD}}}$, $\theta = a/f$
- Target for clocks $\text{MeV} \times \theta^2 \bar{n}n \Rightarrow \frac{\delta f}{f} \sim \frac{\delta m_N}{m_N} \sim 10^{-16} \times \cos(2m_a) \times \left(\frac{10^{-15} \text{ eV}}{m_\phi} \frac{10^9 \text{ GeV}}{f} \right)^2$

Banerjee, GP, Safronova, Savoray & Shalit (22)

Kim & GP (22)

Axion - the scalar way, the power of clocks #1

$$\mathcal{L}_{\text{axion}}^{\text{eff}} \in 10^{-3} \theta^2(t) m_N \bar{n}n$$



Naively: clocks can efficiently search for the oscillating signal of a light QCD-like-axion

Axion - the scalar way, the power of clocks #2, stochasticity

- Due to velocity dispersion, $\theta^2(t) \Rightarrow$ sharp resonance + **continuum at lower frequencies**

Masia-Roig et. al (23)

- To understand qualitatively, let's consider first linear coupling, say that changes α :

$$\delta E(t) \leftrightarrow m_e \alpha^2 (1 + \theta(t)) \propto \frac{\sqrt{\rho_{\text{DM}}}}{m_a} \cos \omega t, \text{ with } \omega \approx m_a \left(1 + \frac{v^2}{2} \right), \text{ and } P(v) \propto \exp\left(\frac{-v^2}{\sigma^2}\right), \text{ with } \sigma \sim 10^{-3}$$

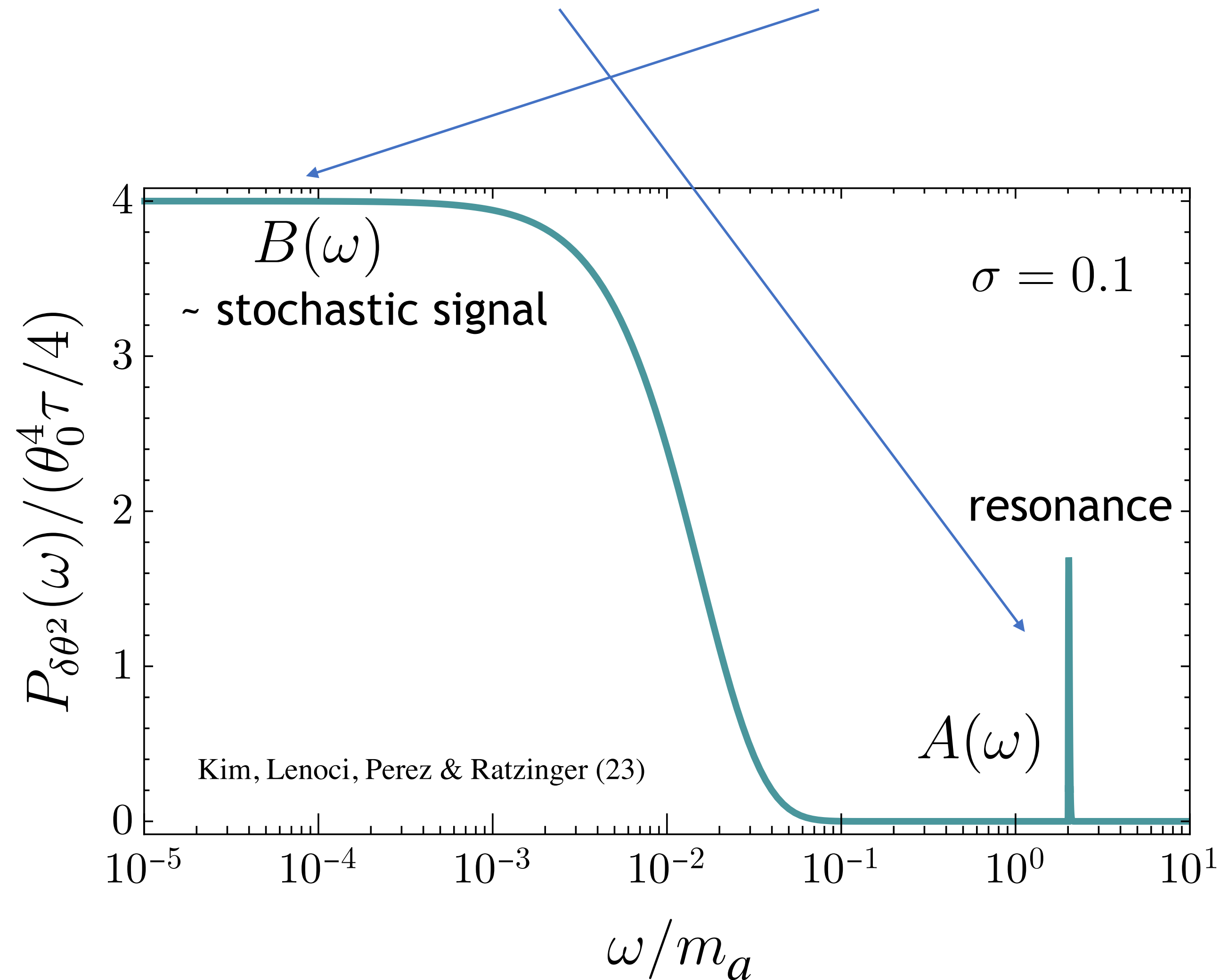
- Frequency transformed: it would result in a sharp signal at $\omega \sim m_a$ with width of $\mathcal{O}(10^{-6})$

- However our signal is quadratic $\delta E(\omega) \propto \int \delta E(t) e^{i\omega t} \theta(t)^2 dt \sim \delta(\omega - 2m_a) + F(\omega, m_a, \sigma)$

$$F(\omega, m_a, \sigma) \propto \int e^{i\omega t} P(v_1) P(v_2) \cos \left[m_a \left(\frac{v_1^2 - v_2^2}{2} \right) t \right] dt d\vec{v}_1 d\vec{v}_2$$

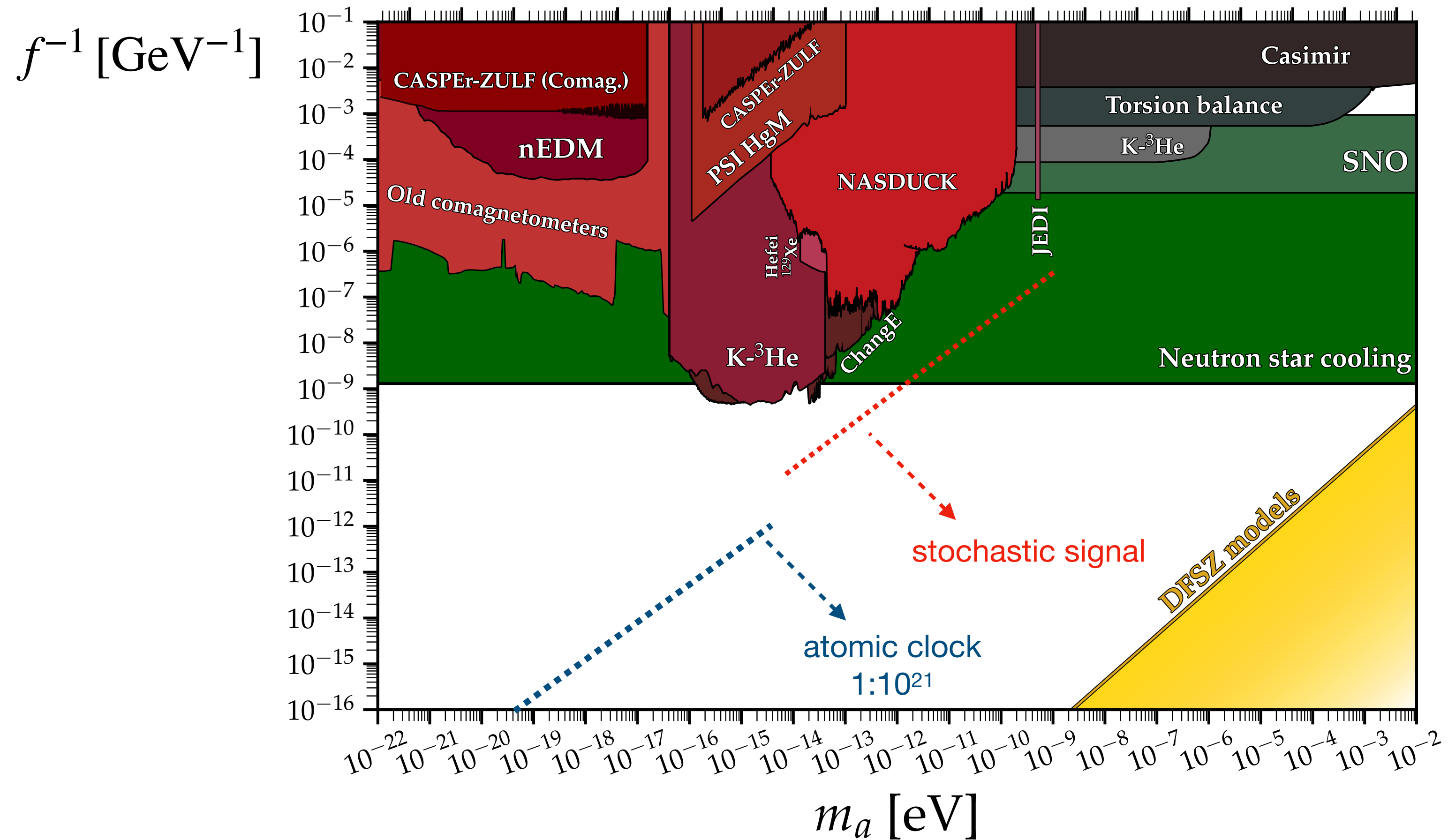
Power spectrum of quadratic (axion) UDM

$$\delta E(\omega) \propto \delta(\omega - 2m_a) + F(\omega, m_a, \sigma)$$



Power spectrum of quadratic (axion) UDM, the stochastic signal

$$\mathcal{L}_{\text{axion}}^{\text{eff}} \in 10^{-3} \theta^2(t) m_N \bar{n} n$$



Naively: clocks can efficiently search for the oscillating signal of a light QCD-like-axion

Searching for scalar coupling to the strong/nuclear sector - a key for progress - large class of UDM models

- QCD axion models: $\frac{a}{f} G\tilde{G} \Rightarrow \left(\frac{a}{f}\right)^2 \bar{n}n$

- Dilaton: $d_g \frac{\alpha_s}{\pi} \frac{\phi}{M_{\text{Pl}}} GG \Rightarrow d_g \frac{\phi}{M_{\text{Pl}}} \frac{m_N}{M_{\text{Pl}}} \bar{n}n$

see however Hubisz, Ironi, GP & Rosenfeld (24)

- Higgs-mixing / relaxion: $\sin \theta_{H\phi} \frac{\alpha_s}{4\pi v} H GG \Rightarrow \sin \theta_{H\phi} \frac{\phi}{v} m_N \bar{n}n$

Piazza and M. Pospelov (10); Banerjee, Kim & GP (19)

- Nelson-Barr UDM: $\left(\epsilon_{\text{NB}} = \frac{y_s^2 V_{us}^2}{16\pi^2} \right) \frac{\phi}{f} m_u \bar{u}u \Rightarrow \epsilon_{\text{NB}} \frac{\phi}{f} m_u \bar{n}n$ \w w Dine, Ratzinger & Savoray, tomorrow?

⋮

Why probing the strong sector w/ clocks is challenging ?

To understand let's talk about how clocks probe DM
(theorist's perspective - simplified model ...)

Atomic clock in 1-slide

- A clock requires an apparatus that repeat itself in a very precise manner
- Atomic clocks are based on cases where there are electronic transitions between stable 2-level system, $H \approx \Delta E \times \sigma_Z$
- In the experiment, via laser, one prepare a linear combination of these levels

$$\psi^+(t=0) \sim \frac{|0\rangle + |1\rangle}{\sqrt{2}} \implies \psi(t)^+ \propto \frac{|0\rangle + \exp(i\Delta Et) |1\rangle}{\sqrt{2}}$$

$$|\langle \psi^+(t=0) | \psi^+(t) \rangle|^2 = \cos^2 \left(\frac{\Delta Et}{2} \right) \iff \text{perfect pendulum}$$

Clocks and ultralight DM (UDM) search?

- Established that clock is a perfect oscillator: $|\langle \psi^+(t=0) | \psi^+(t) \rangle|^2 = \cos^2 \left(\frac{\Delta E t}{2} \right)$
- Why is it an excellent ultralight DM (UDM) detector?

For electronic transitions: $\Delta E \propto m_{\text{reduced}} \alpha^2$, with $m_{\text{reduced}} \approx m_e \left(1 - \frac{m_e}{m_{\text{nuc}}} \right)$

- Scalar DM could couple to F^2 or to the electron would induce oscillatory

component: $\Delta E \propto \left[\text{const} + \frac{\sqrt{2\rho}}{m_{\text{UDM}}} \cos(m_{\text{UDM}} t) \right]$ which atomic clocks can sense

Observables directly probing coupling to QCD/nuclear sector

- Regular transition are sensitive to the reduced mass:

$$\Delta E \propto m_{\text{reduced}} \alpha^2, \quad m_{\text{reduced}} \approx m_e \left(1 - \frac{m_e}{m_{\text{nuc}}} \right), \quad \text{however } \frac{m_e}{Am_p} \sim 10^{-5} \quad (A \text{ is number of nucleons})$$

- Hyperfine clocks via the g-factor, however their sensitivity is “only” $1:10^{12-14}$

- One can use vibrational modes in molecules, scales like $\sqrt{\frac{m_e}{Am_p}} \sim 10^{-3}$

In vapor see: Oswald, Nevsky, Vogt, Schiller, Figuerora, Zhang, Tretiak, Antypas, Budker, Banerjee & GP (21) In corr. spec.: Madge, GP, Meir (last month)

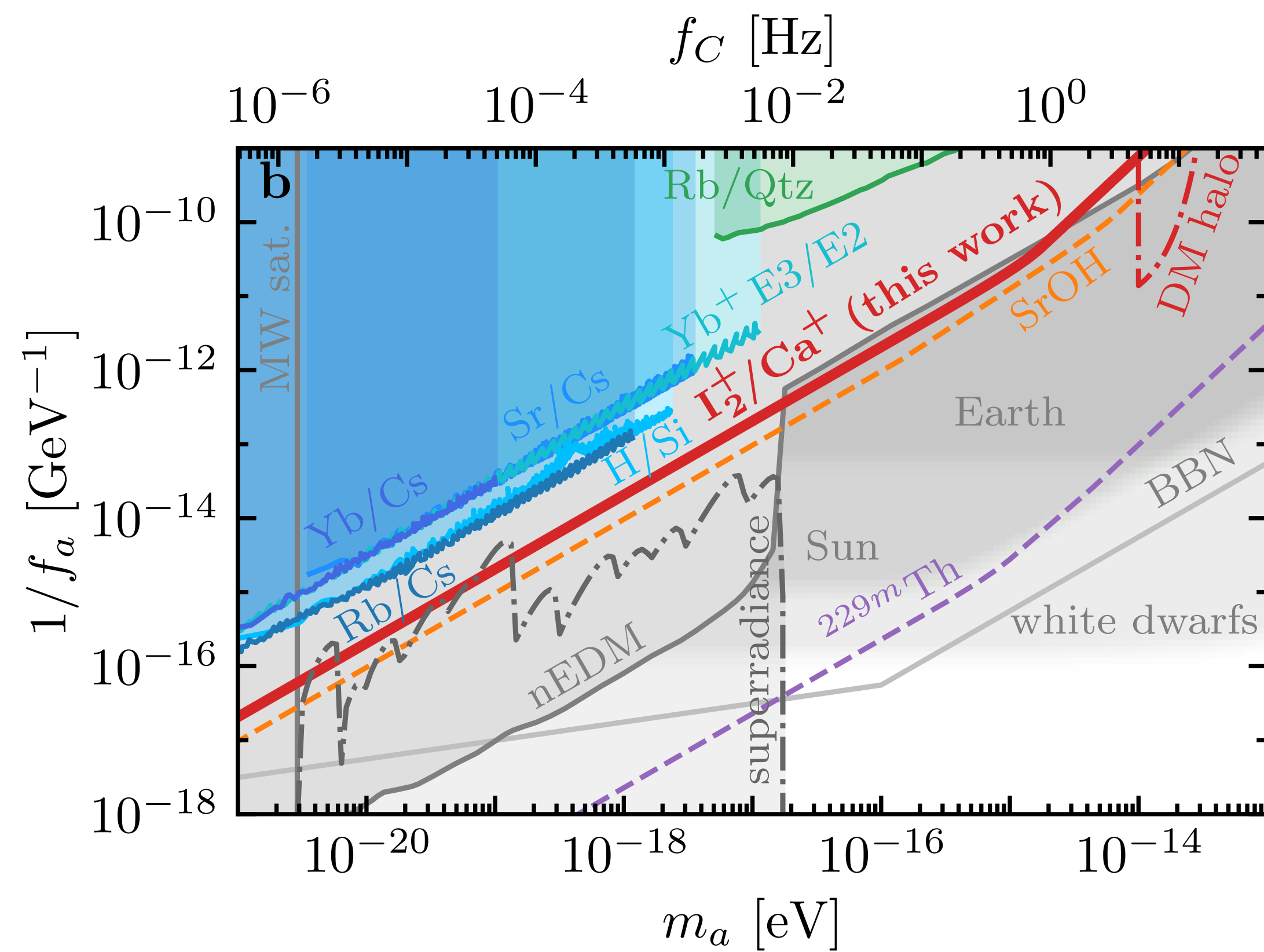
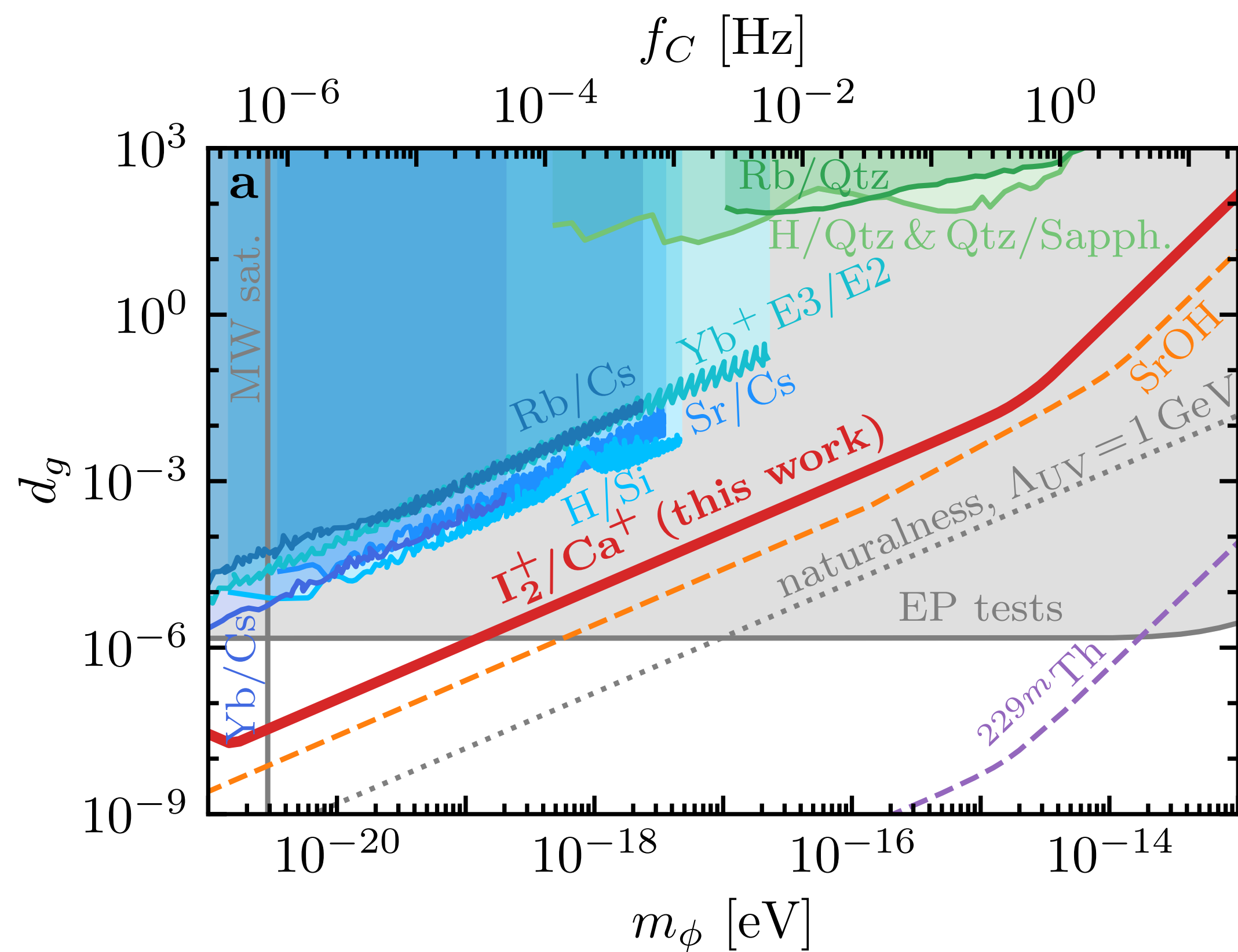
- Or charge radius effect, scales like $A^{8/3} \alpha \left(\frac{m_{\text{Bohr}}}{m_p} \right)^3$

Banerjee, Budker, Filzinger, Huntemann, Paz, GP, Porsev & Safronova (23)

All result with a suppression factor, $R_{\text{atom}} \sim 10^{3-5}$

Observables directly probing coupling to QCD/nuclear sector

Madge, GP, Meir (24)



Bottomline: accessing the nucleus is hard \w atomic clocks, sensitivity suppressed by $R_{\text{atom}} \sim 10^{3-5}$

Why all of this is about to change by potentially improving the sensitivity by a factor of 10^8-10^{10} ?

Laser excitation of the Th-229 nucleus

(i) on the sensitivity and its robustness

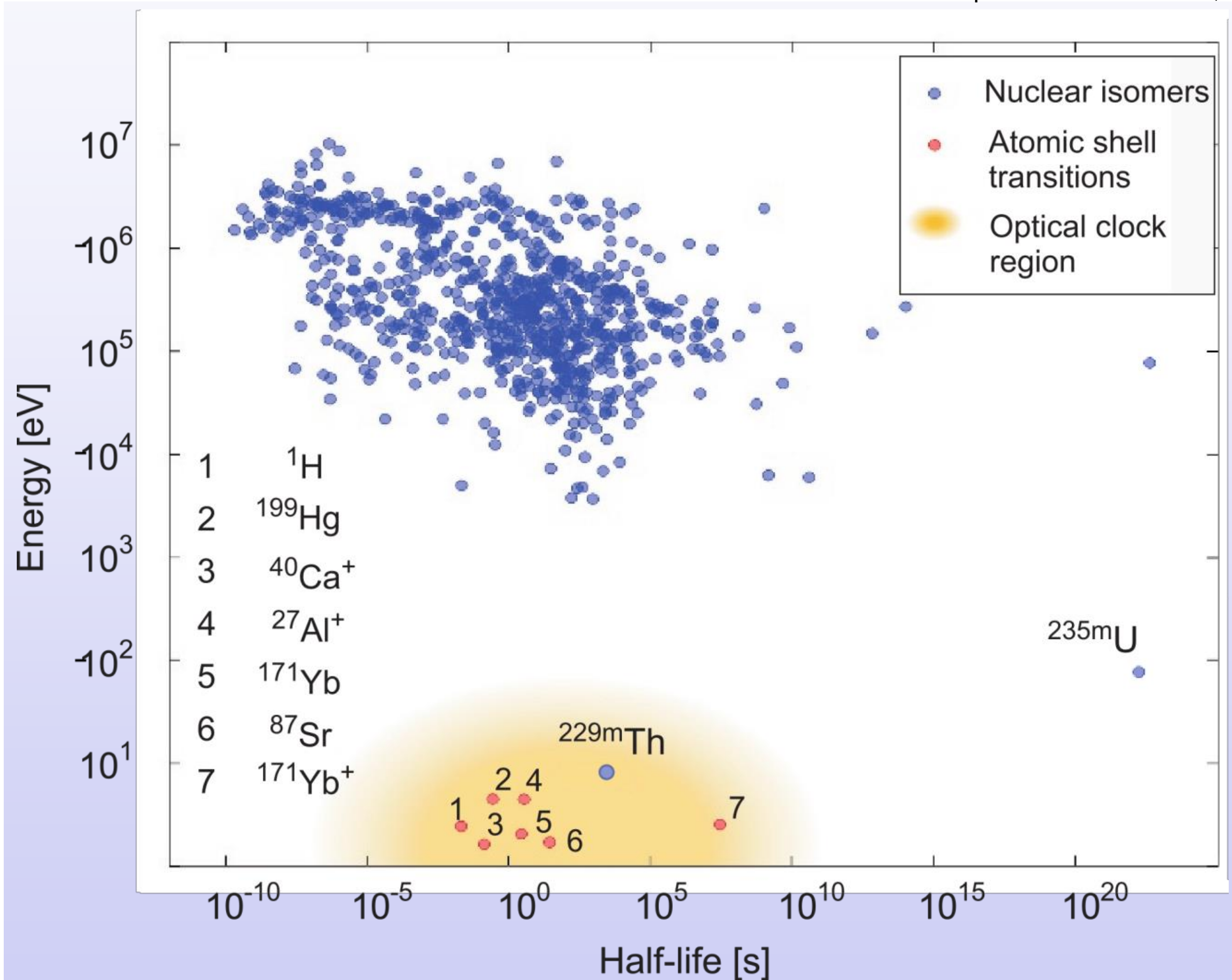
with: Doron Gazit, Joachim Kopp , Gil Paz & Konstantin Springmann ...

(ii) BSM implications

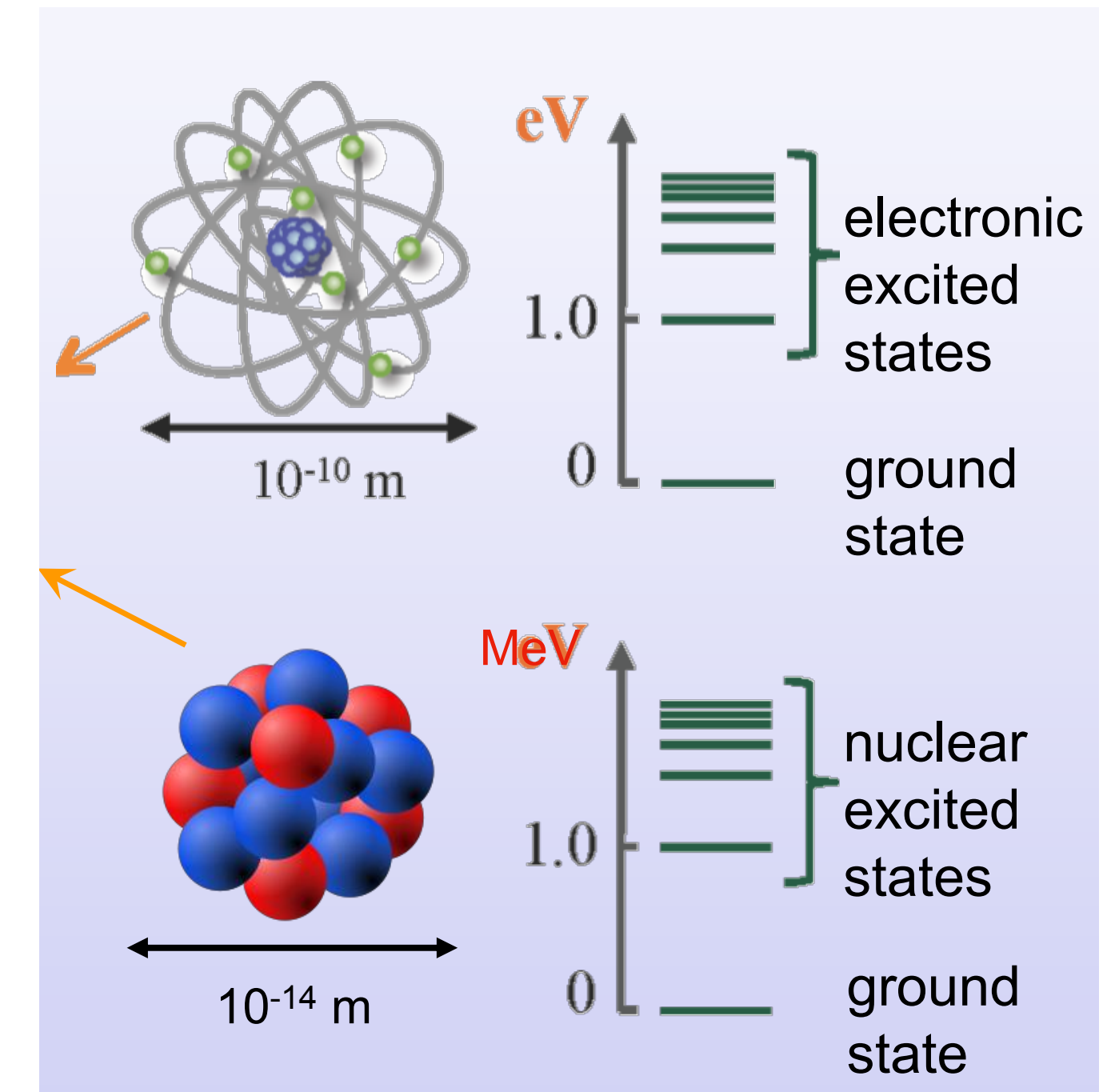
with: Elina Fuchs, Fiona Kirk, Eric Madge, Chaitanya Paranjape, Ekkehard Peik & Wolfram Ratzinger

Natural fine tuning, Th-229 isomeric excitation

Peter G. Thirolf: MIAPbP Workshop: Quantum Sensors, Garching, 28.8.-8.9.2

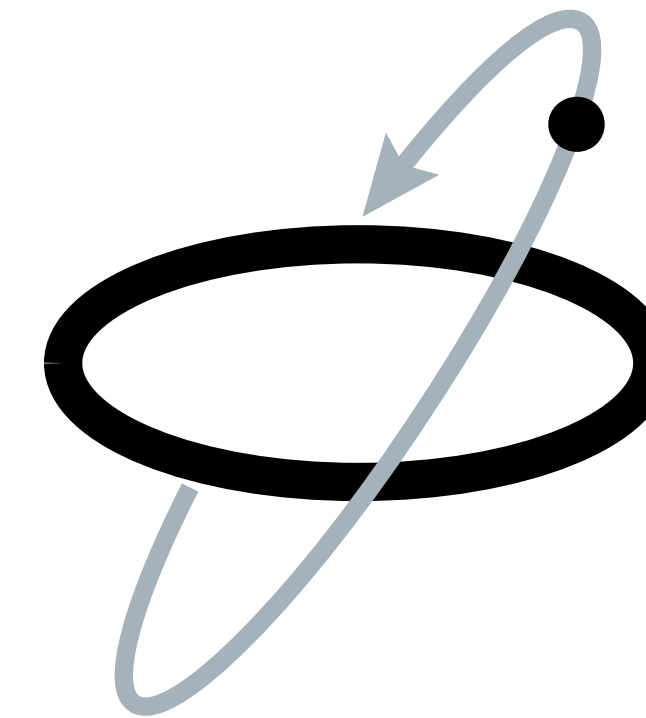
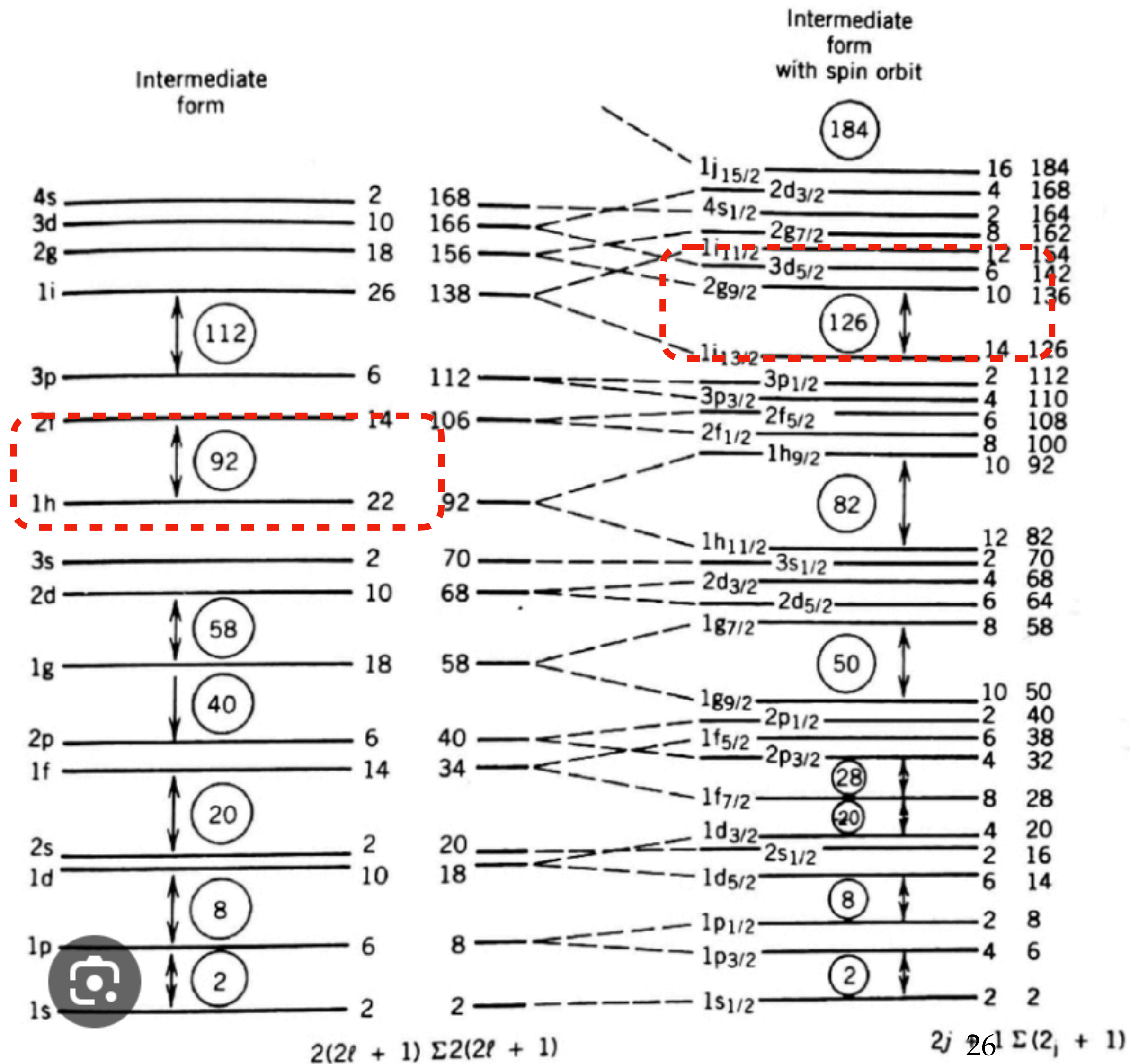


lowest E^* of all ca. 186000 presently known nuclear excited states

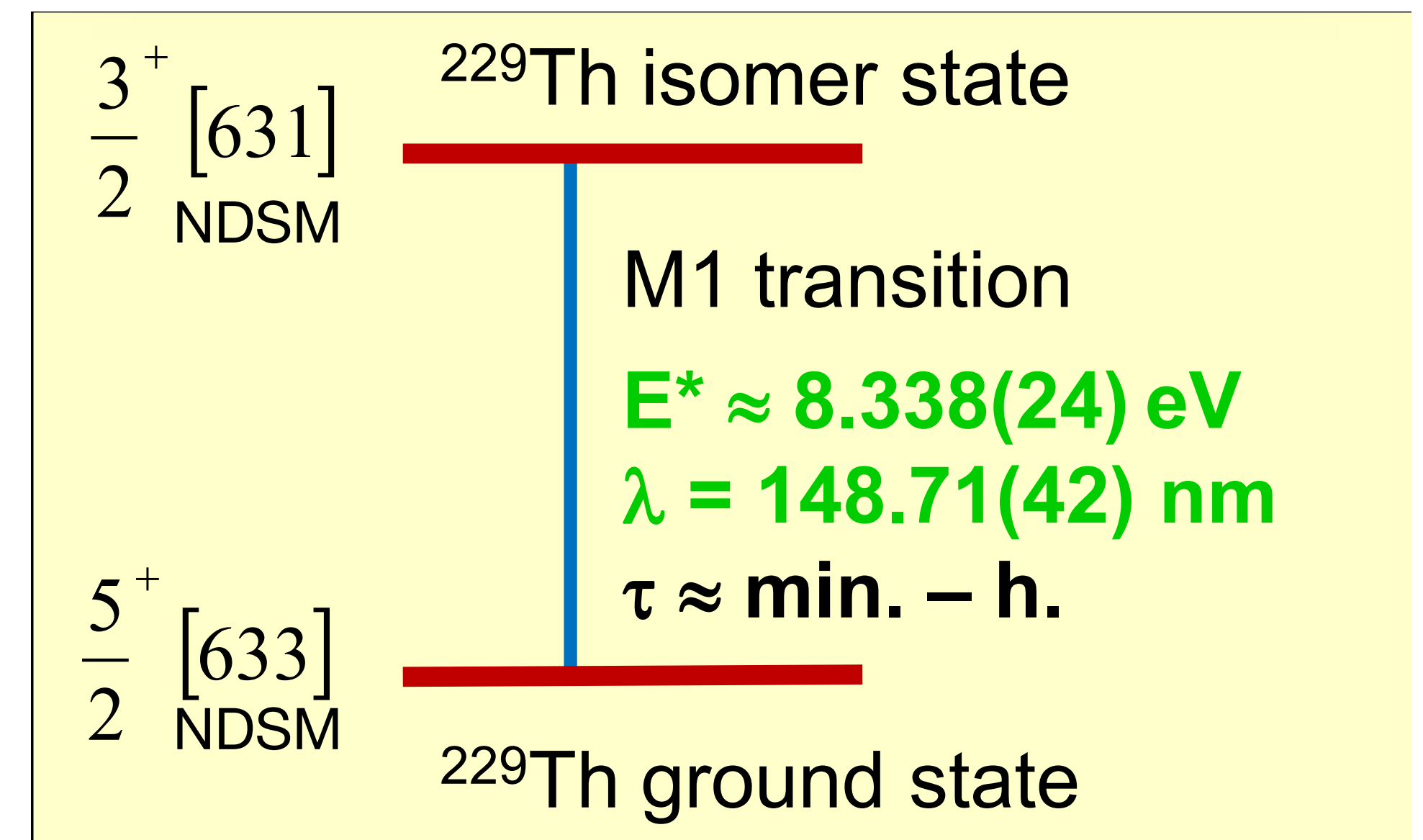


Th-229 shell's structure, one unpaired neutron, the transition

90 protons, 139 neutrons



The nuclear level structure “can be described”
in terms of an elliptic core and an unpaired neutron
Beeks et al: Nat. Rev. (21)



The (other) April revolution?

Laser Excitation of the Th-229 Nucleus

J. Tiedau¹,* M. V. Okhapkin¹,* K. Zhang¹,* J. Thielking¹, G. Zitzer¹, and E. Peik¹†
Physikalisch-Technische Bundesanstalt, 38116 Braunschweig, Germany

F. Schaden,¹ T. Pronebner¹, I. Morawetz, L. Toscani De Col¹, F. Schneider¹, A. Leitner,
M. Pressler, G. A. Kazakov¹, K. Beeks¹, T. Sikorsky, and T. Schumm¹‡
Vienna Center for Quantum Science and Technology, Atominstitut, TU Wien, 1020 Vienna, Austria

(Received 5 February 2024; revised 12 March 2024; accepted 14 March 2024; published 29 April 2024)

The 8.4 eV nuclear isomer state in Th-229 is resonantly excited in Th-doped CaF₂ crystals using a tabletop tunable laser system. A resonance fluorescence signal is observed in two crystals with different Th-229 dopant concentrations, while it is absent in a control experiment using Th-232. The nuclear resonance for the Th⁴⁺ ions in Th:CaF₂ is measured at the wavelength 148.3821(5) nm, frequency 2020.409(7) THz, and the fluorescence lifetime in the crystal is 630(15) s, corresponding to an isomer half-life of 1740(50) s for a nucleus isolated in vacuum. These results pave the way toward Th-229 nuclear laser spectroscopy and realizing optical nuclear clocks.

Laser excitation of the ²²⁹Th nuclear isomeric transition in a solid-state host

R. Elwell,¹ Christian Schneider,¹ Justin Jeet,¹ J. E. S. Terhune,¹ H. W. T. Morgan,²
A. N. Alexandrova,² H. B. Tran Tan,^{3,4} Andrei Derevianko,³ and Eric R. Hudson^{1,5,6}

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⁶*Center for Quantum Science and Engineering, University of California Los Angeles, Los Angeles, CA, USA*

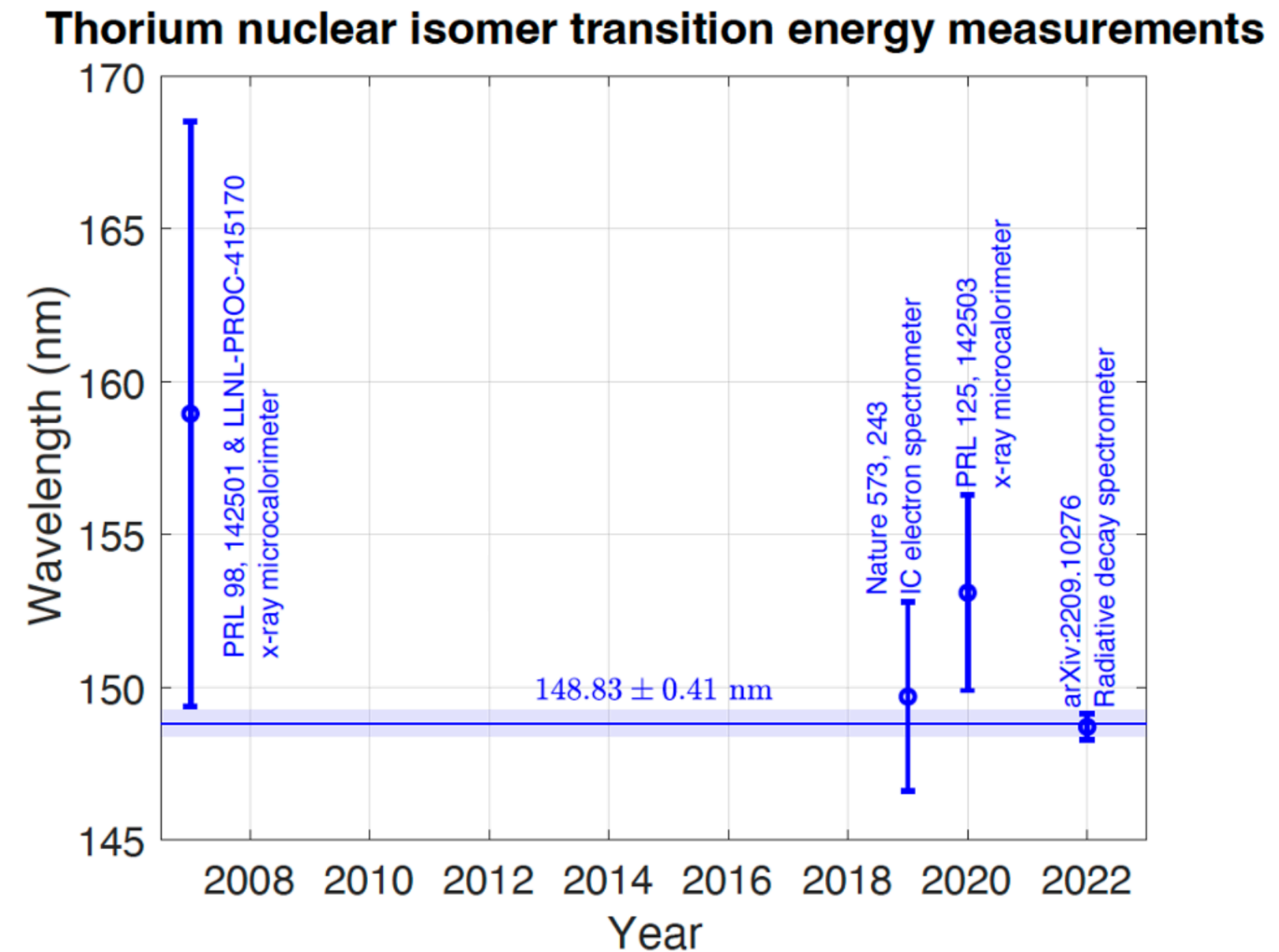
(Dated: April 19, 2024)

LiSrAlF₆ crystals doped with ²²⁹Th are used in a laser-based search for the nuclear isomeric transition. Two spectroscopic features near the nuclear transition energy are observed. The first is a broad excitation feature that produces red-shifted fluorescence that decays with a timescale of a few seconds. The second is a narrow, laser-linewidth-limited spectral feature at 148.38219(4)_{stat}(20)_{sys} nm (2020407.3(5)_{stat}(30)_{sys} GHz) that decays with a lifetime of 568(13)_{stat}(20)_{sys} s. This feature is assigned to the excitation of the ²²⁹Th nuclear isomeric state, whose energy is found to be 8.355733(2)_{stat}(10)_{sys} eV in ²²⁹Th:LiSrAlF₆.



Moore's law - quantum sensors

The situation prior to this months' publications:



Peter G. Thirolf: MIAPbP Workshop: Quantum Sensors, Garching, 28.8.-8.9.2

Over the last 2 yrs error on $\delta f/f$ has been reduced to:
0.1 (2020) \Rightarrow 0.001 (2022) \Rightarrow 0.000001 (Apr/24)

Enhanced sensitivity, ^{229}Th

- How to estimate the sensitivity say of UDM that couples only to the QCD sector?
- Let's break the energy difference according to nucl' & Coulomb parts, following the lore:

$$\Delta E_{\text{nu-clock}} \sim \Delta E_{\text{nu}} - \Delta E_{\text{EM}} \sim 8 \text{ eV} \ll \Delta E_{\text{nu}} \sim \Delta E_{\text{EM}} \sim \frac{Z^2 \alpha}{\Lambda_{\text{QCD}} A^{1/3} \times A} \sim \text{MeV}$$

Therefore the lore says: $K_{\text{canc}} = \Delta E_{\text{nu}} / \Delta E_{\text{nu-clock}} \sim 10^5 \gg 1$

- Now let's assume that we have a UDM couples only to the QCD sector:

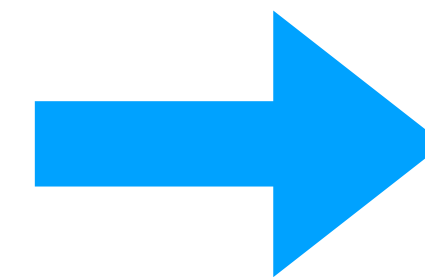
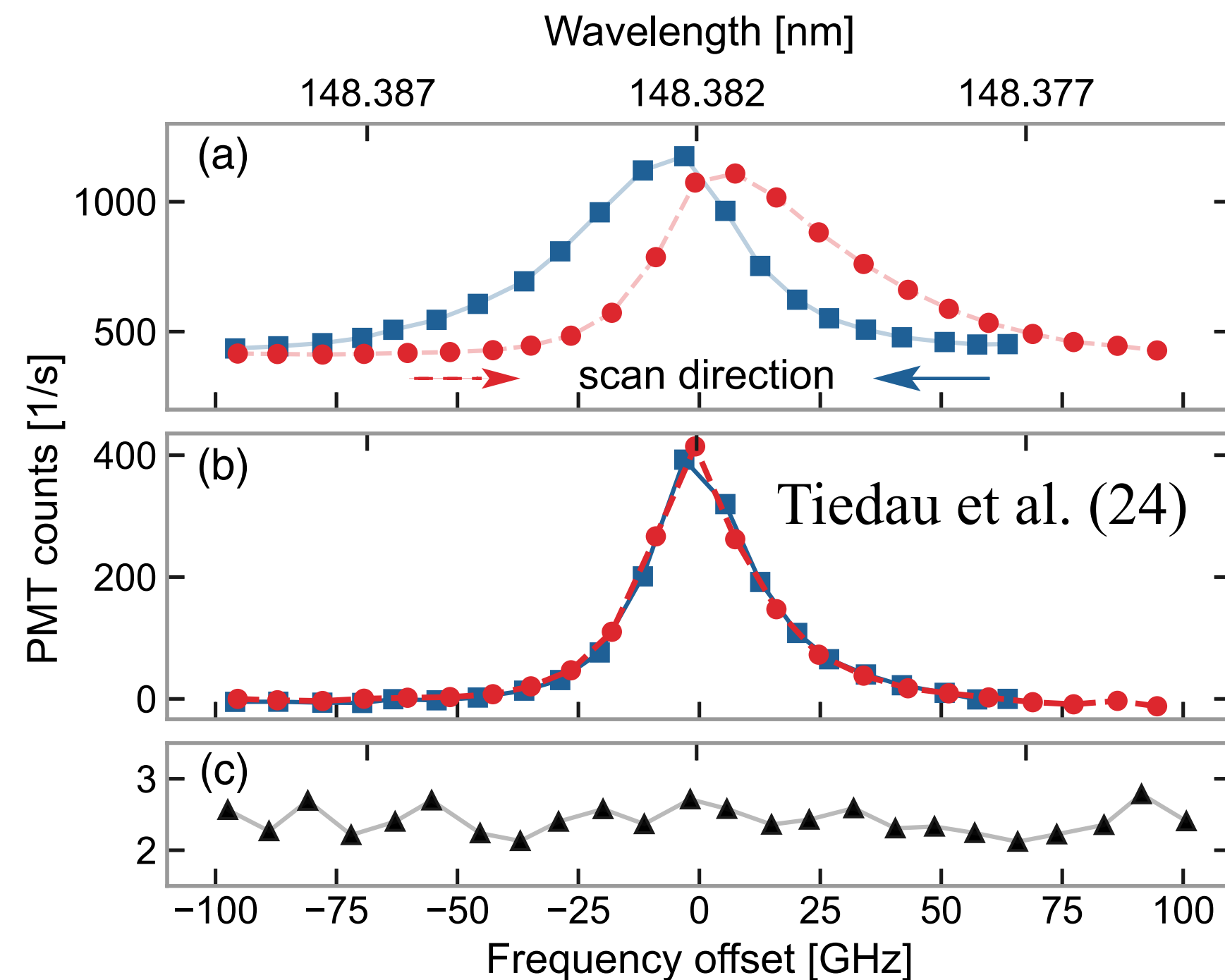
$$\frac{\delta_{\text{UDM}}(\Delta E_{\text{nu-clock}})}{\Delta E_{\text{nu-clock}}} = \frac{\Delta E_{\text{nu}}(t) - \Delta E_{\text{EM}}}{\Delta E_{\text{nu-clock}}} \Rightarrow \frac{\Delta E_{\text{nu}}(t)}{\Delta E_{\text{nu-clock}}} \sim \frac{\Delta E_{\text{nu}}}{\Delta E_{\text{nu-clock}}} \times d_g \frac{m_N}{M_{\text{Pl}}} \cos(m_\phi t) \sim 10^5 \times d_g \frac{m_N}{M_{\text{Pl}}} \cos(m_\phi t)$$



enhancement of $R_{\text{atom}} \times K_{\text{canc}} \sim 10^{8-10}$ relative to existing probes of QCD!

What was measured ?

- Used a super broad super powerful laser ~ few GHz to shine on a ^{229}Th lattice
- Scan the frequencies (width of 10^{-5} to cover region of 0.1 eV!), then after ~ 1000 s got back fluorescence at a specific frequency equal to: $2020.409(3-7)$ THz resulting with



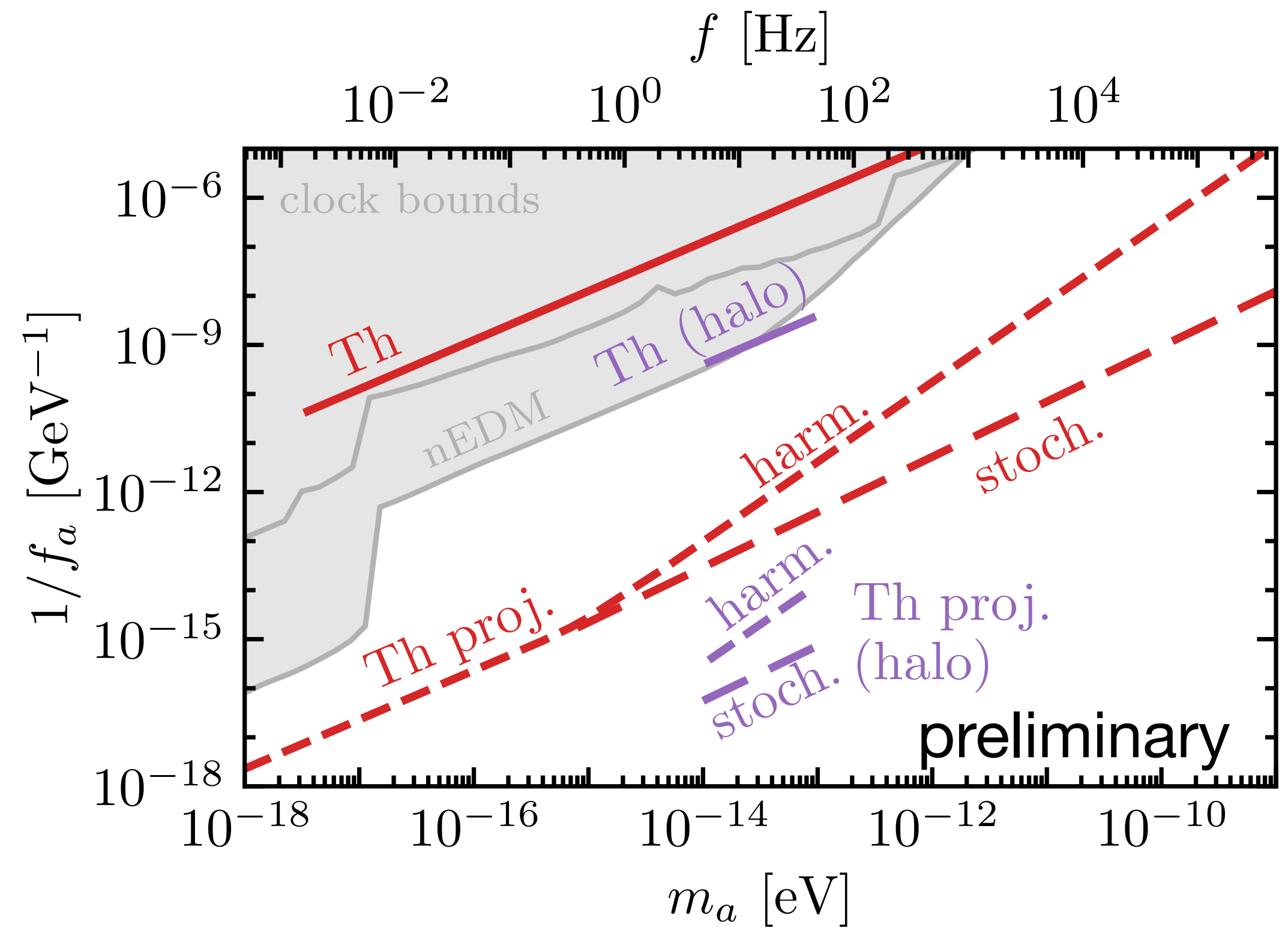
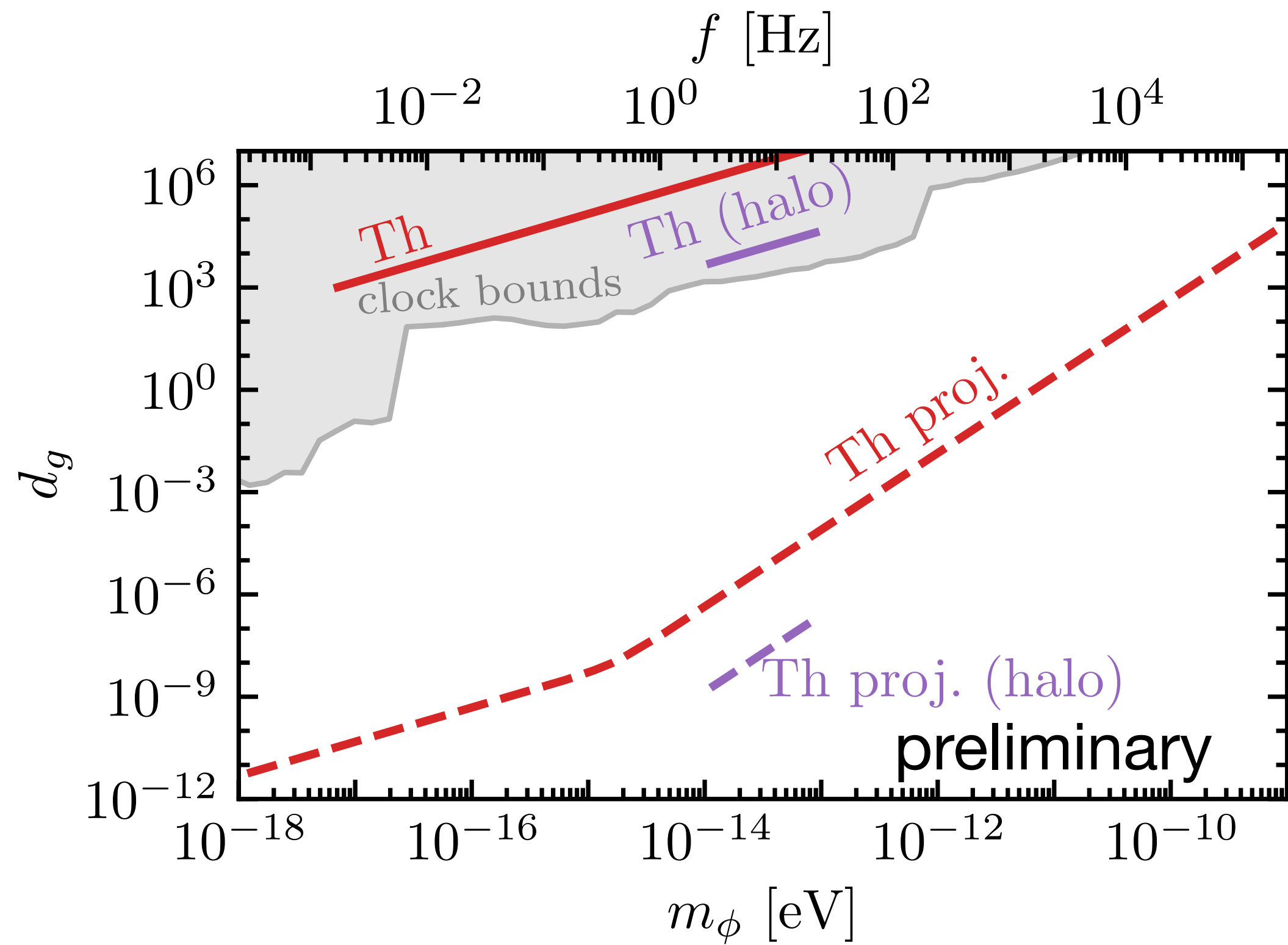
$$\frac{\delta f}{f} \sim 10^{-6}$$

Present and future implications

with: Elina Fuchs, Fiona Kirk, Eric Madge, Chaitanya Paranjape, Ekkehard Peik & Wolfram Ratzinger

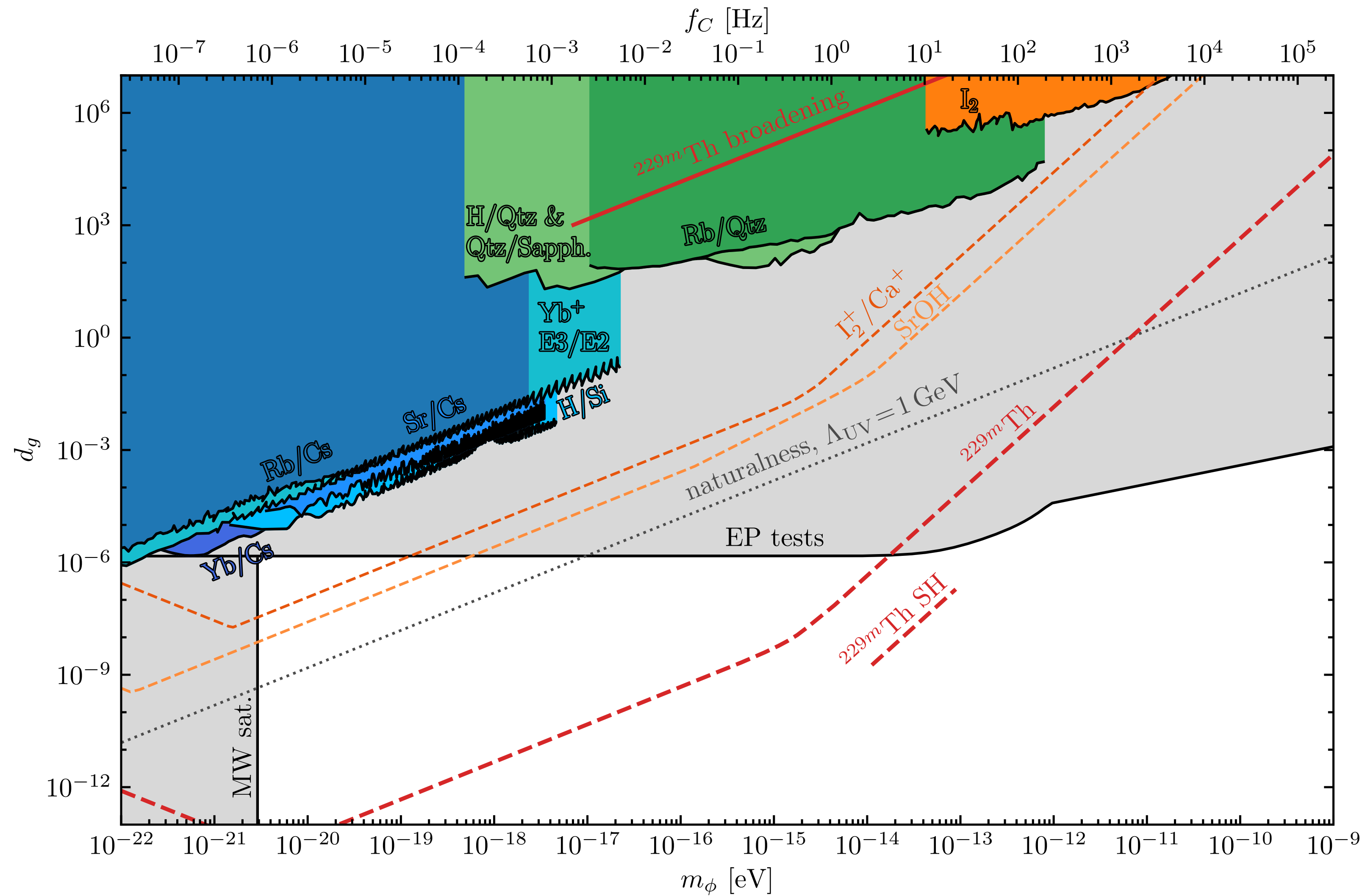
- We have now $\frac{\delta f}{f} \sim 10^{-6}$, effectively this should be translated to effective sensitivity of $\frac{\delta f}{f} \times R_{\text{atom}} \times K_{\text{canc}} \sim 10^{-14} - 10^{-16}$ of atomic clocks, only 2-3 orders of mag from the frontier
- However, how can we use the existing info?
- Line shape analysis, if the UDM oscillating faster than measurement time it'd lead to broadening of the line beyond what has been observed \Rightarrow new constrain (would take over soon ...)

Using Th-229 to search for oscillating UDM signal



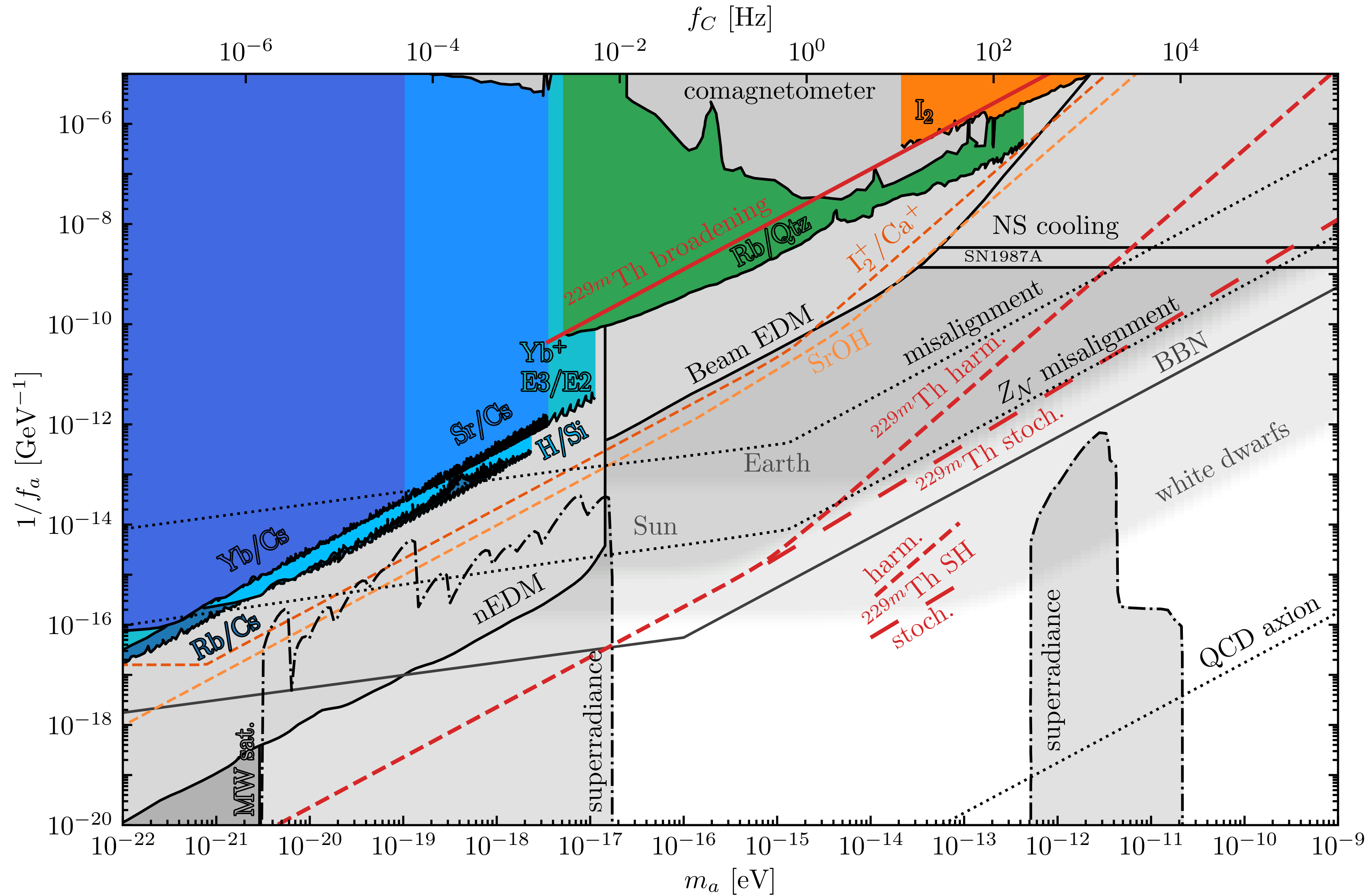
with: Elina Fuchs, Fiona Kirk, Eric Madge, Chaitanya Paranjape, Ekkehard Peik & Wolfram Ratzinger

Scalar coupling to QCD & nuclear clock



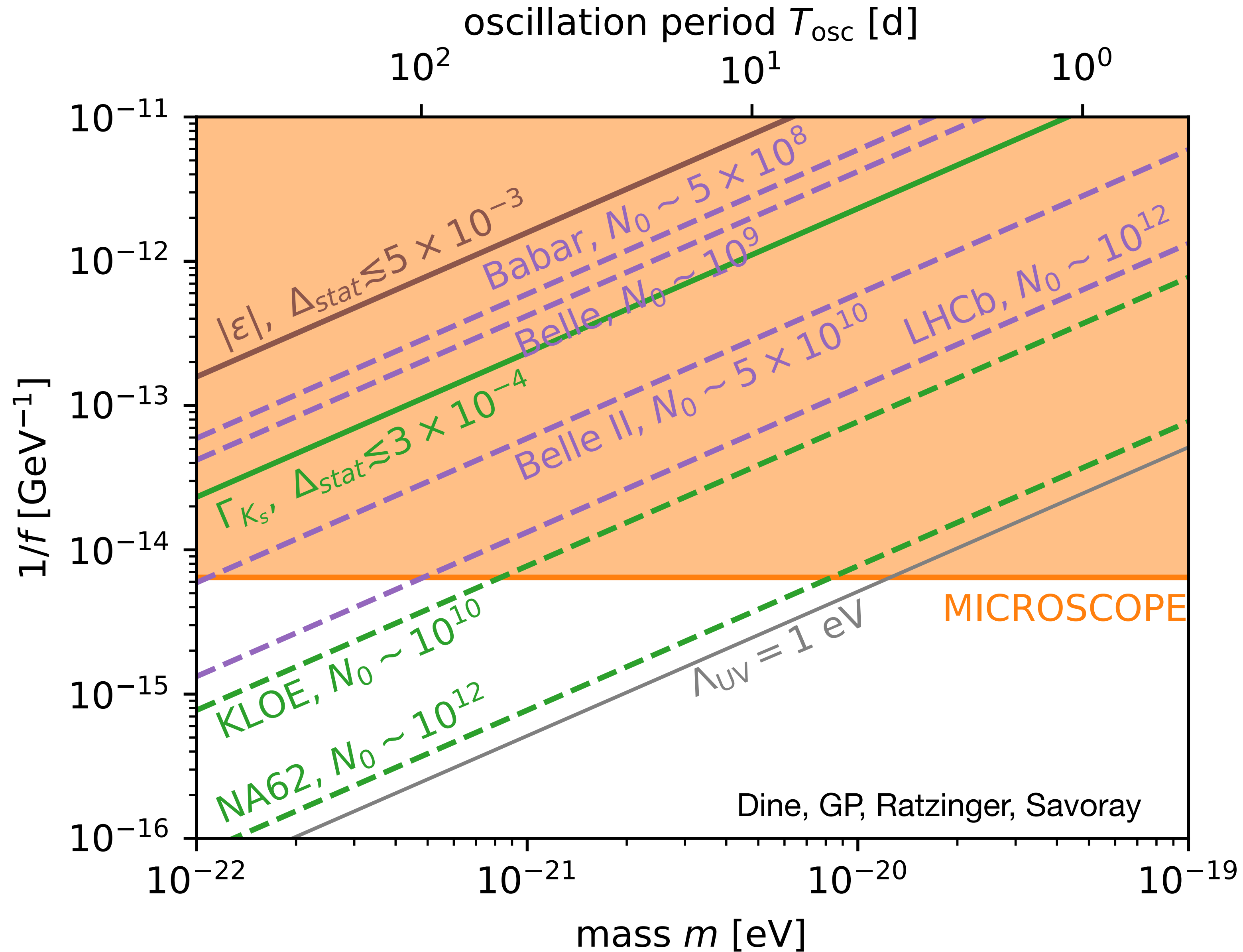
with: Elina Fuchs, Fiona Kirk, Eric Madge, Chaitanya Paranjape, Ekkehard Peik & Wolfram Ratzinger

QCD-axion-like & nuclear clock

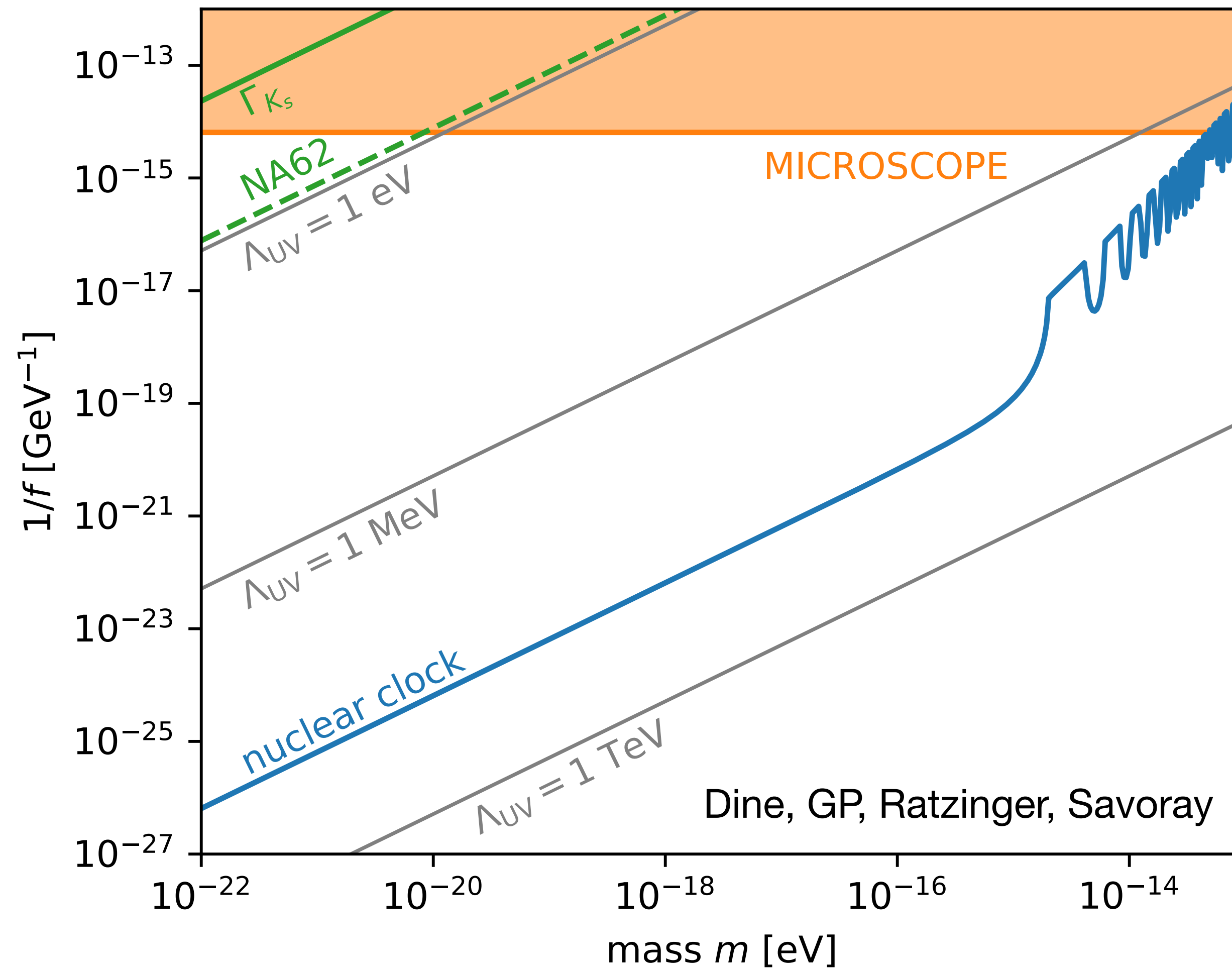


with: Elina Fuchs, Fiona Kirk, Eric Madge, Chaitanya Paranjape, Ekkehard Peik & Wolfram Ratzinger

Nelson-Barr-UDM parameter space, luminosity exp.



Nelson-Barr-UDM & nuclear clock



How robust is the sensitivity factor?

with: Doron Gazit, Joachim Kopp , Gil Paz & Konstantin Springmann ...

- Can we measure or test this enhancement factor, $K_{\text{canc}} = \Delta E_{\text{nu}} / \Delta E_{\text{nu-clock}} \sim 10^5 \gg 1$?
- Calculation of the nuclear binding energy difference is very challenging ...
- Can instead consider at the electrostatic binding energy of the two states
- A crude way could be via imagining that the nuclear is a classical object
- Given the shape and charge density of both states we can evaluate ΔE_{EM}
- However, shape and density are hard to measure, one can use simplification assuming that the nucleus is a spheroid of a constant density

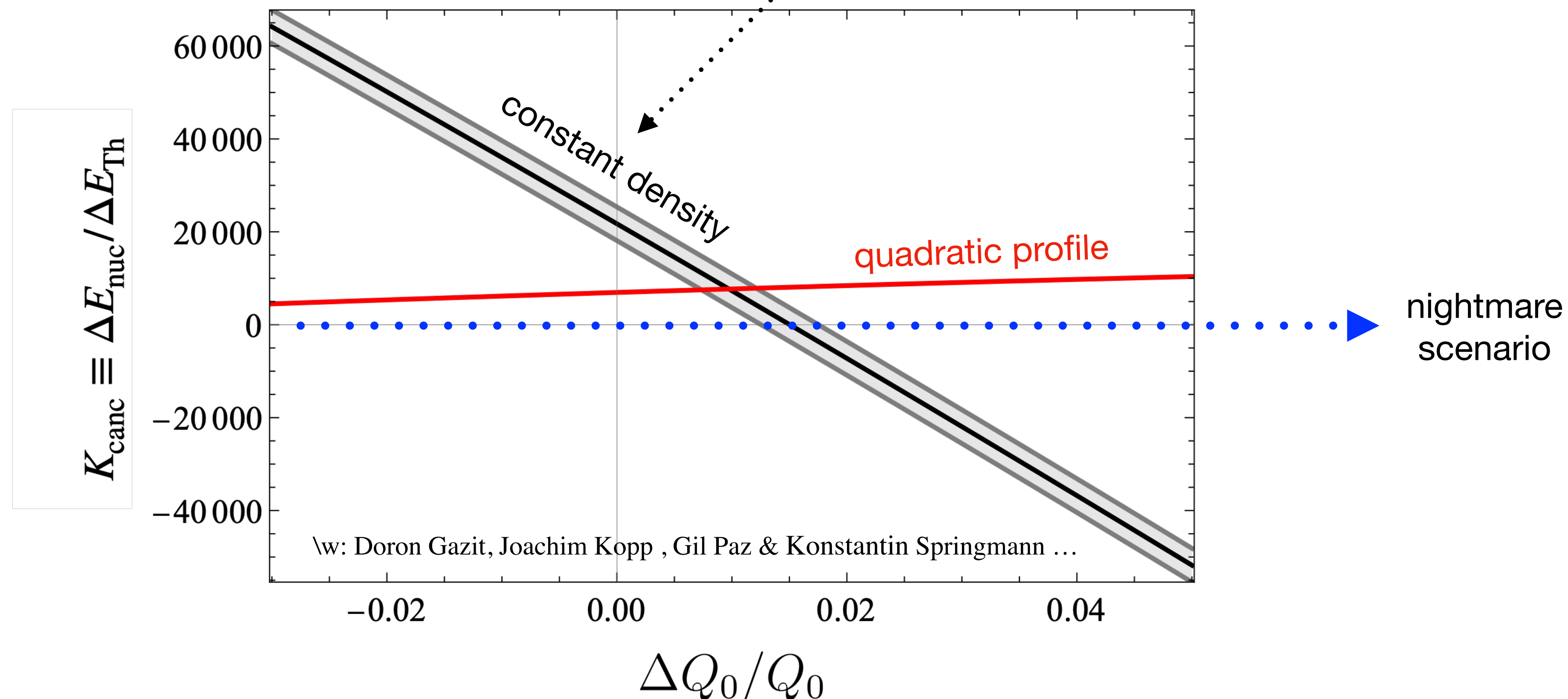
Berengut, Dzuba, Flambaum & Porsev (09); Fadeev, Berengut & Flambaum (20)

Estimating the sensitivity factor spheroid model

- In the const' density - spheroid model one finds $\Delta E_{\text{EM}} \approx -485 \text{ MeV} \frac{\Delta \langle r^2 \rangle}{\langle r^2 \rangle} + 11.6 \text{ MeV} \frac{\Delta Q_0}{Q_0}$,

Berengut, Dzuba, Flambaum & Porsev (09); Fadeev, Berengut & Flambaum (20)

with $\langle r^2 \rangle$ & Q_0 being the charge radius square, and the quadrupole moment, Δ stands for isomer-ground-state difference, w $\Delta Q_0/Q_0 = -0.01(4)$



Conclusions

- Most well motivated models coupled to the QCD/nuclear sector, however currently we have only limited ways to probe the UDM-nuclear coupling
- Nuclear clock will change it all:
 - (i) direct coupling to the nuclear parameters
 - (ii) enhanced sensitivity due to the fine cancellation
- New measurement => game changer moving to precision nuclear clock phase
- Existing measurement might already give impressive bound (but not strongest)
- Discussed robustness

Backups

NB-UDM signature & parameter space

• What is the size of the effect? $\delta a \sim \frac{\sqrt{\rho_{\text{DM}}}}{m_{\text{NB}} f} \cos(m_{\text{NB}} t) \sim 10^{-4} \times \frac{10^{13} \text{ GeV}}{f} \times \frac{10^{-21} \text{ eV}}{m_{\text{NB}}} \times \cos(m_{\text{NB}} t)$

• How to search such signal?

(i) Luminosity frontier: oscillating CP violation + oscillating CKM angles:

$$\frac{\delta V_{us}}{V_{us}} \sim \delta a \Rightarrow \text{oscillating Kaon decay lifetime}$$

$$\frac{\delta \theta_{\text{KM}}}{\theta_{\text{KM}}} \sim \delta a \Rightarrow \text{oscillating CP violation}$$

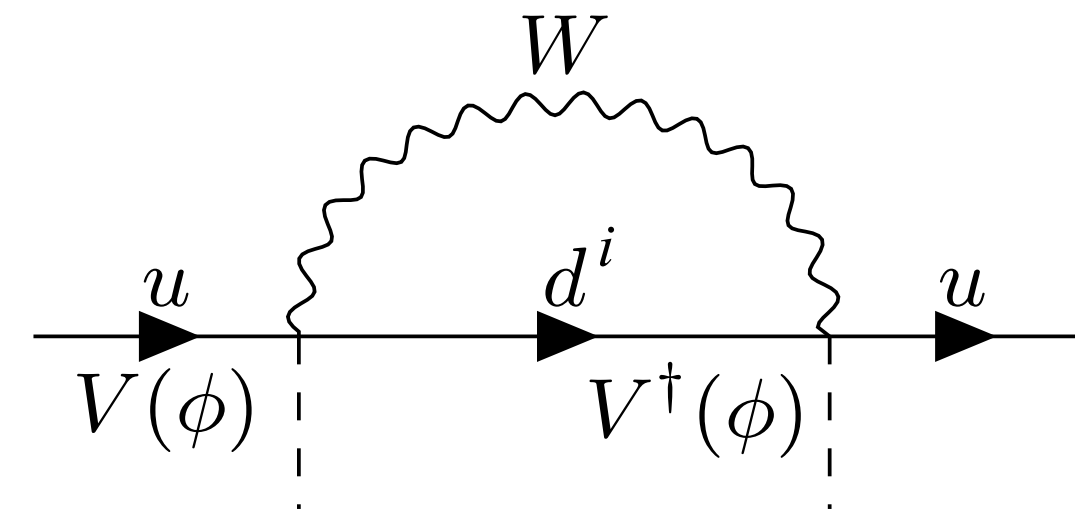
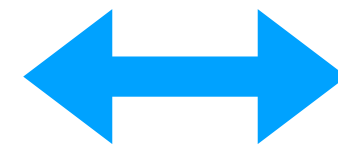
$$\frac{\delta V_{ub}}{V_{ub}} \sim \delta a \Rightarrow \text{oscillating semi inclusive } b \rightarrow u \text{ decay}$$

NB-UDM signature & parameter space

- How to search such signal?

(ii) Equivalence principle (EP)+clocks, at 1-loop scalar coupling to mass is induced:

$$\frac{\Delta m_u}{m_u} \approx \frac{3}{32\pi^2} y_s^2 |V_{us}^{\text{SM}}|^2 \frac{a}{f}$$



- EP $\Rightarrow f \gtrsim 10^{14}$ GeV
- Nuclear clock (1:10²⁴) $\Rightarrow f \gtrsim 10^{19}$ GeV $\times \frac{m_{\text{NB}}}{10^{-15}$ eV

Challenges

- Minimal misalignment DM bound, can't be satisfied: $f \gtrsim 10^{15} \text{ GeV} \left(\frac{10^{-19} \text{ eV}}{m_\phi} \right)^{\frac{1}{4}}$, but pretty close ...
- Naive naturalness => currently only probing sub-MeV cutoff, $\Delta m_a \approx \frac{y_b |V_{ub}| m_u \Lambda_{\text{UV}}}{16\pi^2 f}$
- Rely on NB construction, w/ Z_2 and a (non-anomalous) $U(1)$

Two models:

$$Q^{U(1)}(\Phi, u_1, Q_1, d_1, u_2, Q_2, d_1) = (+1, +1, +1, +1, -1, -1, -1)$$

$$Q^{U(1)}(\eta, \Phi, \psi, \psi^c, \bar{u}_1) = +1, +1/2, -1/2, -1/2, +1 \quad (\eta \text{ additional flavon})$$

Planck suppression for ultralight spin 0 field

- Let's consider some dimension 5 operators, and ask if current sensitivity reach the Planck scale (assumed linear coupling and that gravity respects parity):

Graham, Kaplan, Rajendran;
 Stadnik & Flambaum;
 Arvanitaki Huang & Van Tilburg (15)

$$m_\phi = 10^{-18} \text{ eV} \quad (1/\text{hour})$$

operator	current bound	type of experiment
$\frac{d_e^{(1)}}{4 M_{\text{Pl}}} \phi F^{\mu\nu} F_{\mu\nu}$	$d_e^{(1)} \lesssim 10^{-4}$ [58]	DDM oscillations
$\frac{\tilde{d}_e^{(1)}}{M_{\text{Pl}}} \phi F^{\mu\nu} \tilde{F}_{\mu\nu}$	$\tilde{d}_e^{(1)} \lesssim 2 \times 10^6$ [68]	Astrophysics
$\frac{ d_{m_e}^{(1)} }{M_{\text{Pl}}} \phi m_e \psi_e \psi_e^c$	$ d_{m_e}^{(1)} \lesssim 2 \times 10^{-3}$ [58]	DDM Oscillations
$i \frac{ \tilde{d}_{m_e}^{(1)} }{M_{\text{Pl}}} \phi m_e \psi_e \psi_e^c$	$ \tilde{d}_{m_e}^{(1)} \lesssim 7 \times 10^8$ [63]	Astrophysics
$\frac{d_g^{(1)} \beta(g)}{2 M_{\text{Pl}} g} \phi G^{\mu\nu} G_{\mu\nu}$	$d_g^{(1)} \lesssim 6 \times 10^{-6}$ [67]	EP test: MICROSCOPE
$\frac{\tilde{d}_g^{(1)}}{M_{\text{Pl}}} \phi G^{\mu\nu} \tilde{G}_{\mu\nu}$	$\tilde{d}_g^{(1)} \lesssim 4$ [69]	Oscillating neutron EDM
$\frac{ d_{m_N}^{(1)} }{M_{\text{Pl}}} \phi m_N \psi_N \psi_N^c$	$ d_{m_N}^{(1)} \lesssim 2 \times 10^{-6}$ [67]	EP test: MICROSCOPE
$i \frac{ \tilde{d}_{m_N}^{(1)} }{M_{\text{Pl}}} \phi m_N \psi_N \psi_N^c$	$ \tilde{d}_{m_N}^{(1)} \lesssim 4$ [69]	Oscillating neutron EDM

DDM = direct dark matter searches

For updated compilation see: Banerjee, Perez, Safronova, Savoray & Shalit (22)

Status of spin-0 UDM, generalized quality problem

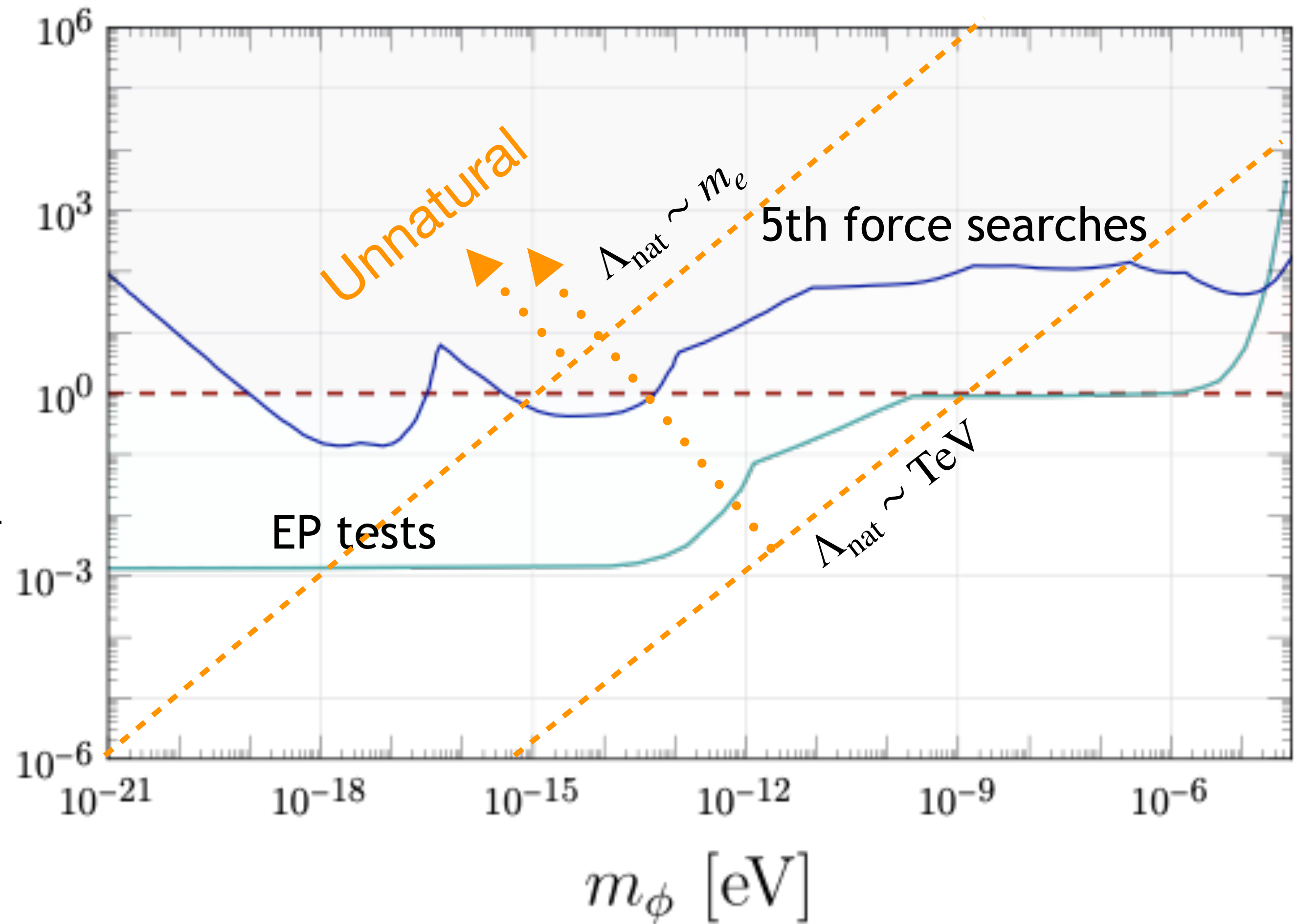
- It seems that genially linearly-coupled models are in troubles, however:
If coupling is quadratic or more than situation is better -

$\frac{d_e^{(2)}}{8M_{\text{Pl}}^2} \phi^2 F^{\mu\nu} F_{\mu\nu}$	$d_e^{(2)} \lesssim 10^{11}$ [67]	EP test: MICROSCOPE
$\frac{ d_{m_e}^{(2)} }{2M_{\text{Pl}}^2} \phi^2 m_e \psi_e \psi_e^c$	$ d_{m_e}^{(2)} \lesssim 10^{12}$ [67]	EP test: MICROSCOPE
$\frac{d_g^{(2)} \beta_g}{4M_{\text{Pl}}^2 g} \phi^2 G^{\mu\nu} G_{\mu\nu}$	$d_g^{(2)} \lesssim 10^{11}$ [67]	EP test: MICROSCOPE.
$\frac{ d_{m_N}^{(2)} }{2M_{\text{Pl}}^2} \phi^2 m_N \psi_N \psi_N^c$	$ d_{m_N}^{(2)} \lesssim 10^{11}$ [67]	EP test: MICROSCOPE

For updated compilation see: Banerjee, GP, Safronova, Savoray & Shalit (22)

Naturalness

$$d_{m_e} \lesssim 4\pi m_\phi M_{\text{Pl}} / m_e \Lambda_{\text{nat}} \approx \frac{m_\phi}{10^{-15} \text{ eV}} \frac{m_e}{\Lambda_{\text{nat}}}$$



Linear coupling seems to also be seriously challenged by naturalness

Oscillations of energy levels induced by QCD-axion-like DM

Kim & GP, last month

● Consider axion model w/ $(\alpha_s/8)(a/f)G\tilde{G}$ coupling, usually searched by magnetometers

● However, spectrum depends on $\theta^2 = (a(t)/f)^2$: $m_\pi^2(\theta) = B\sqrt{m_u^2 + m_d^2 + 2m_u m_d \cos\theta}$
Brower, Chandrasekharan, Negele & Wiese (03)

$$\text{MeV} \times \theta^2 \bar{n}n \Rightarrow \frac{\delta f}{f} \sim \frac{\delta m_N}{m_N} \sim 10^{-16} \times \cos(2m_a) \times \left(\frac{10^{-15} \text{ eV}}{m_\phi} \frac{10^9 \text{ GeV}}{f} \right)^2 \quad \text{vs} \quad m_N \frac{a}{f} \bar{n} \gamma^5 n \Rightarrow (f \gtrsim 10^9 \text{ GeV})_{\text{SN}}$$

It's exciting as clocks (& EP tests) are much more precise than magnetometers
 They can sense oscillation of energy level due to change of mass of the electron or QCD masses to precision of better than $1:10^{18}$!