

N-subjettiness

Jesse Thaler

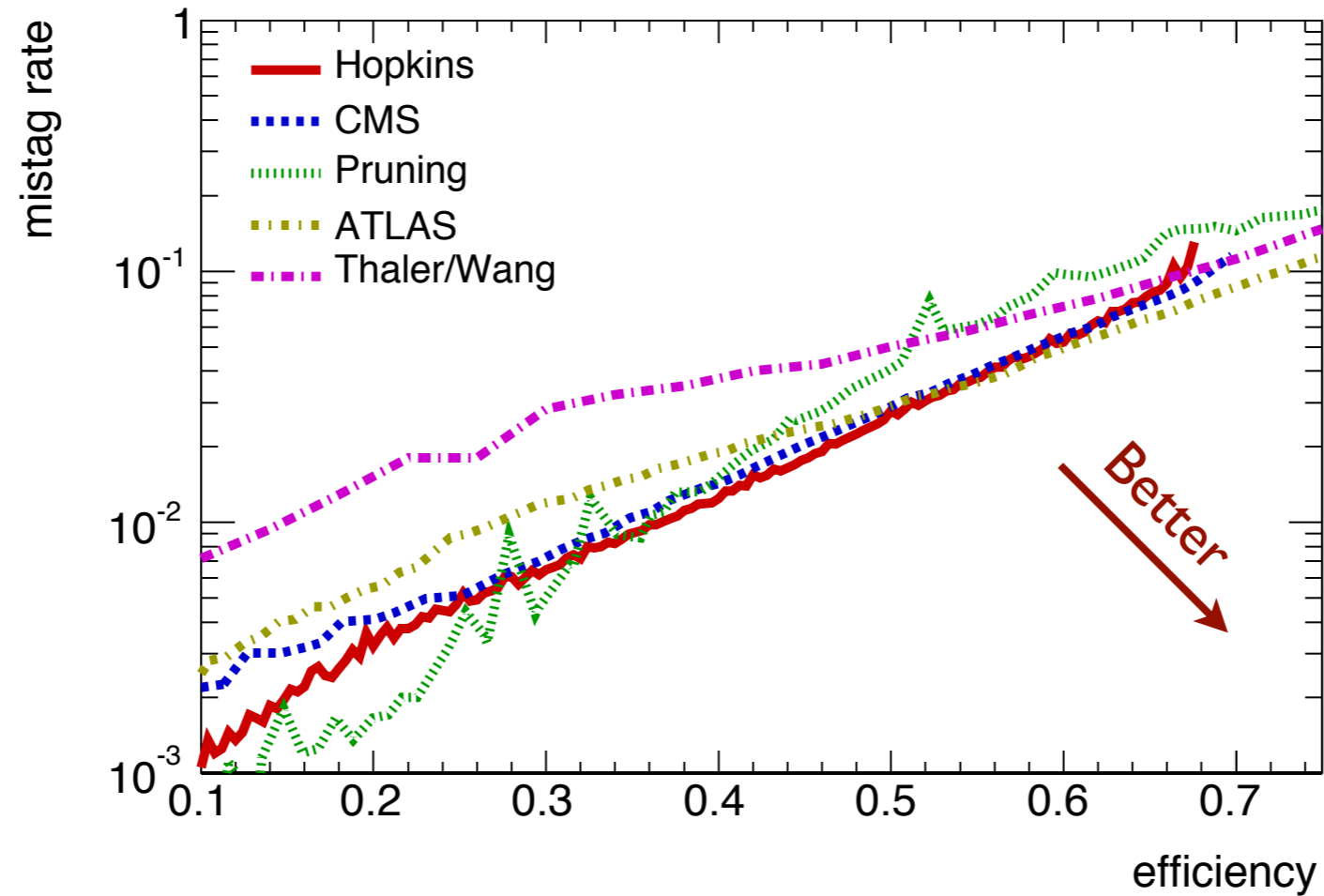


Boost 2011 Workshop

Based on work with Ken Van Tilburg: 1011.2268 & Ken's MIT Senior Thesis

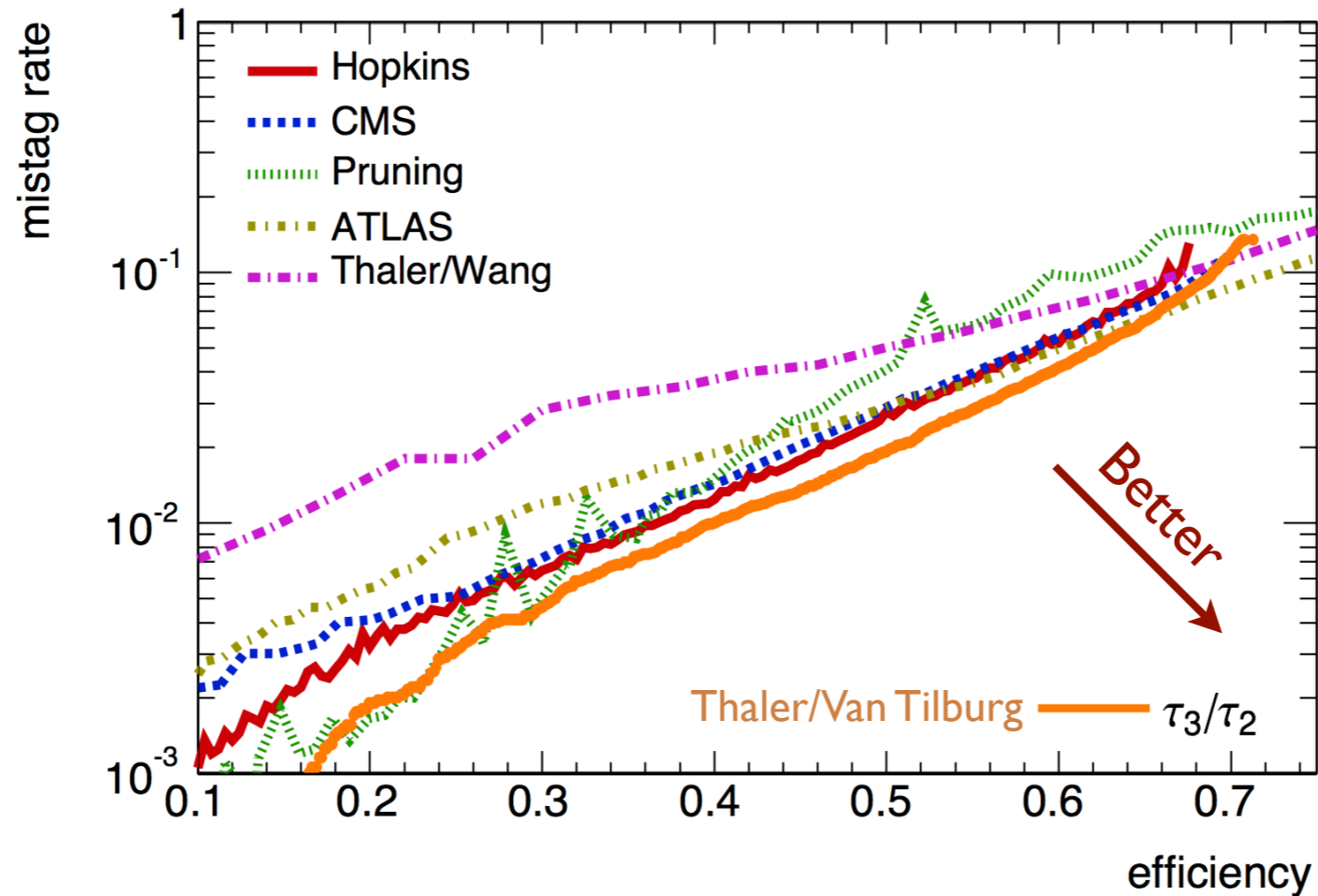
Top Tagging c. 2010

$500 \text{ GeV} < p_T < 600 \text{ GeV}$



Top Tagging c. 2011

$500 \text{ GeV} < p_T < 600 \text{ GeV}$



fixed $160 \text{ GeV} < m_{\text{jet}} < 240 \text{ GeV}$ cut
one-dimensional cut on τ_3/τ_2

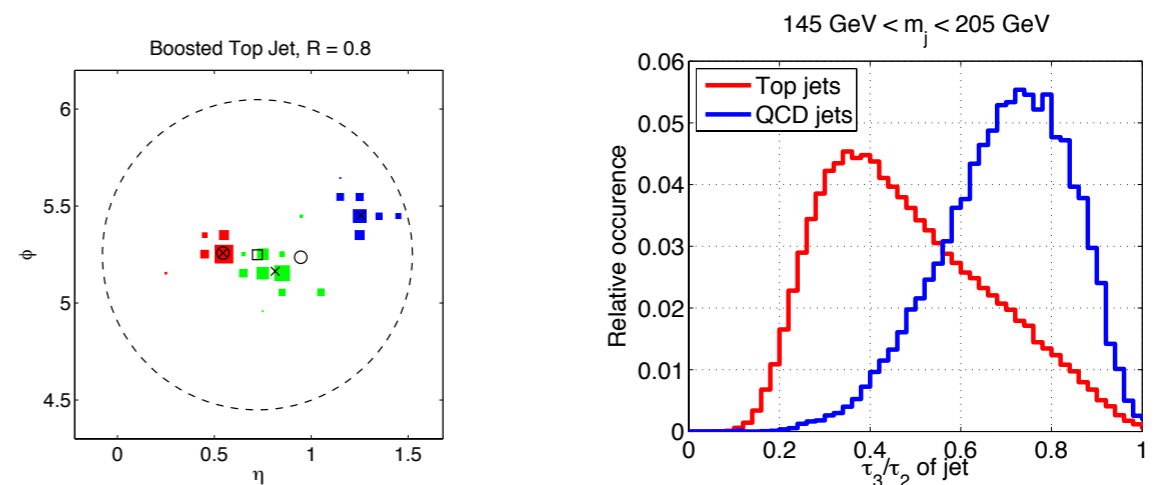
N-subjettiness

A New Substructure Measure

$$\tau_N = \frac{1}{d_0} \sum_k p_{T,k} \min_A \{ \Delta R_{A,k} \}$$

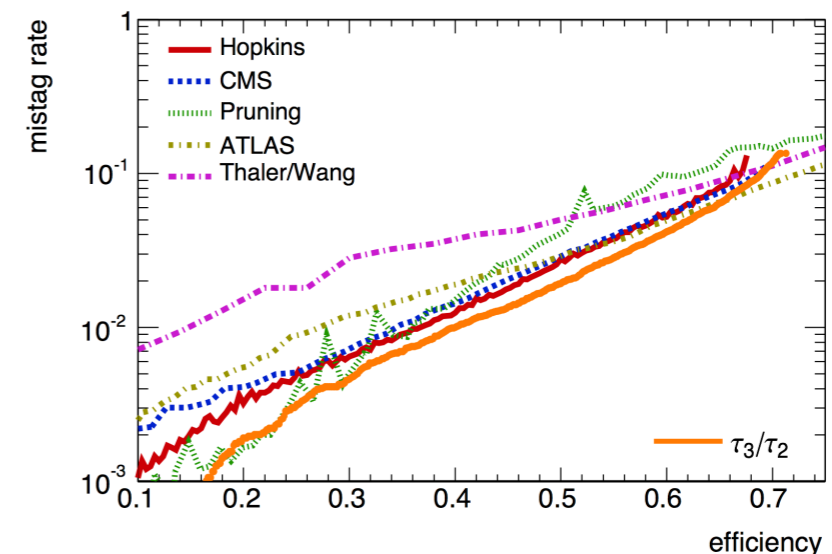
Top Tagging with τ_3/τ_2

(W/Z/H Tagging with τ_2/τ_1)



Minimization & Boost2010

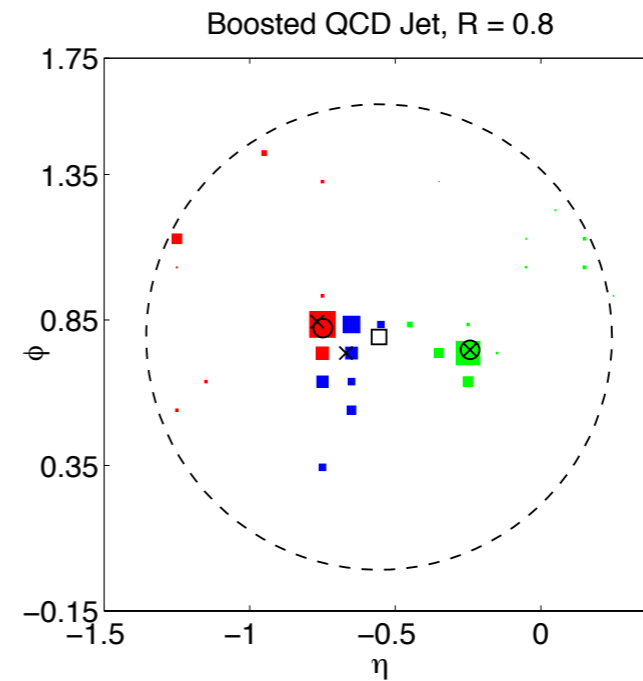
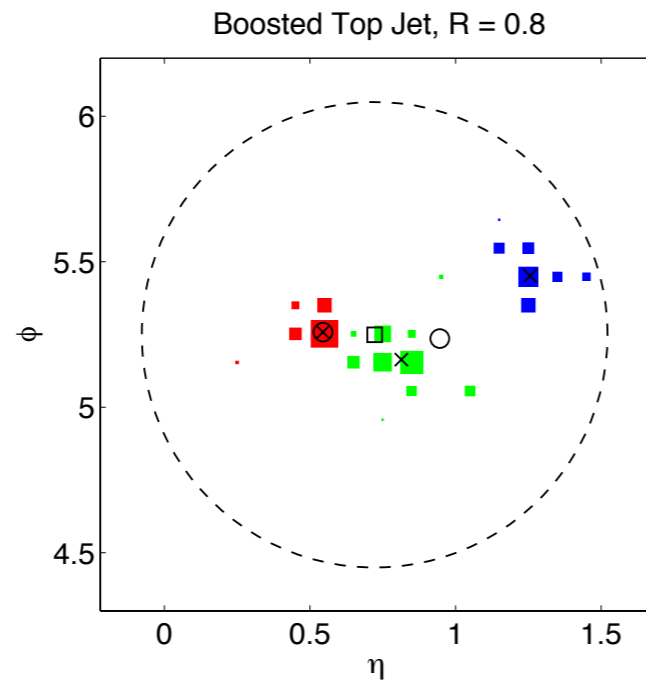
(Thoughts on Jet Algorithms)



[Thaler, Van Tilburg: 1011.2268; See also J.-H. Kim: 1011.1493]

Jet Substructure by Eye

Two jets with $m_{\text{jet}} = m_{\text{top}}$. Coloring by exclusive k_T .



“Algorithmic”

$$\{p_i\} \rightarrow p_{\text{jet}}, \text{yes/no}$$

Tagging
Methods:

Jet Shape Cut

$$f(\{p_i\}) < f_{\text{cut}} \quad \leftarrow \text{(Eventually)}$$

Hybrid

$$f(\{p_i\}, \text{alg. info}) < f_{\text{cut}}$$

Introducing N-subjettiness

“There ... seems to be a rule in physics that the longer you let theorists play with an idea, the more likely it is that they’ll give it a silly name.”

— Flip Tanedo, USLHC Blog, April 22, 2011

N-subjettiness: Degree to which a jet has N subjets!

$$\tau_N \simeq 0 \quad \Rightarrow \quad \leq N \text{ subjets}$$

$$\tau_N \simeq 1 \quad \Rightarrow \quad > N \text{ subjets}$$

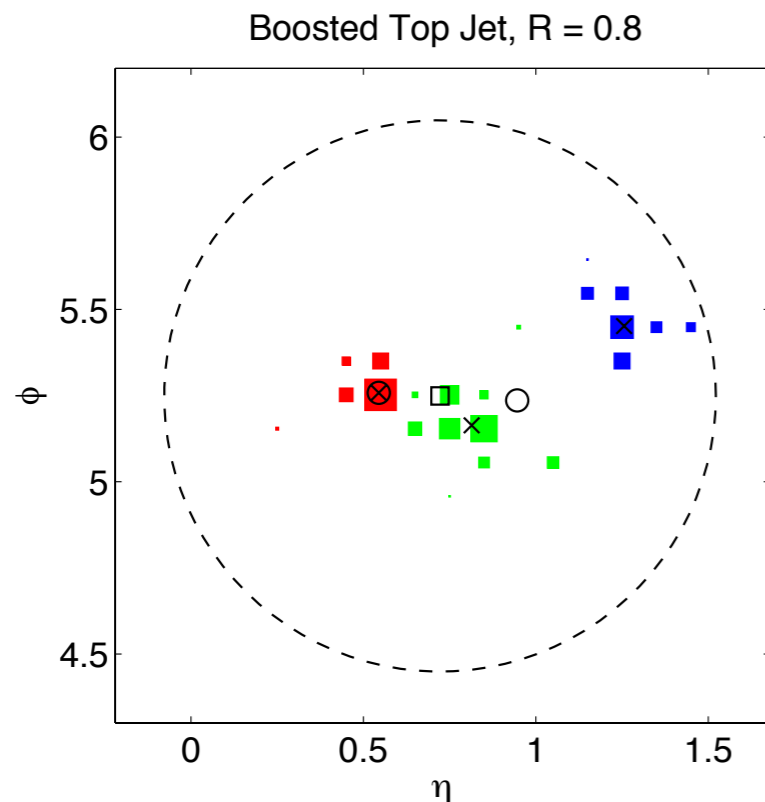
(You prefer “Voronoi-Tessellated Angularities”?)

Adapted from “N-jettiness” (See Iain’s talk)

[Stewart, Tackmann, Waalewijn: 1004.2489]

Introducing N-subjettiness

A Hybrid Jet Shape: $\tau_N = f(\{p_k\}, \{p_{\text{axes}}\})$



$$\tau_N = \frac{1}{d_0} \sum_k p_{T,k} \min_A \{ \Delta R_{A,k} \}$$

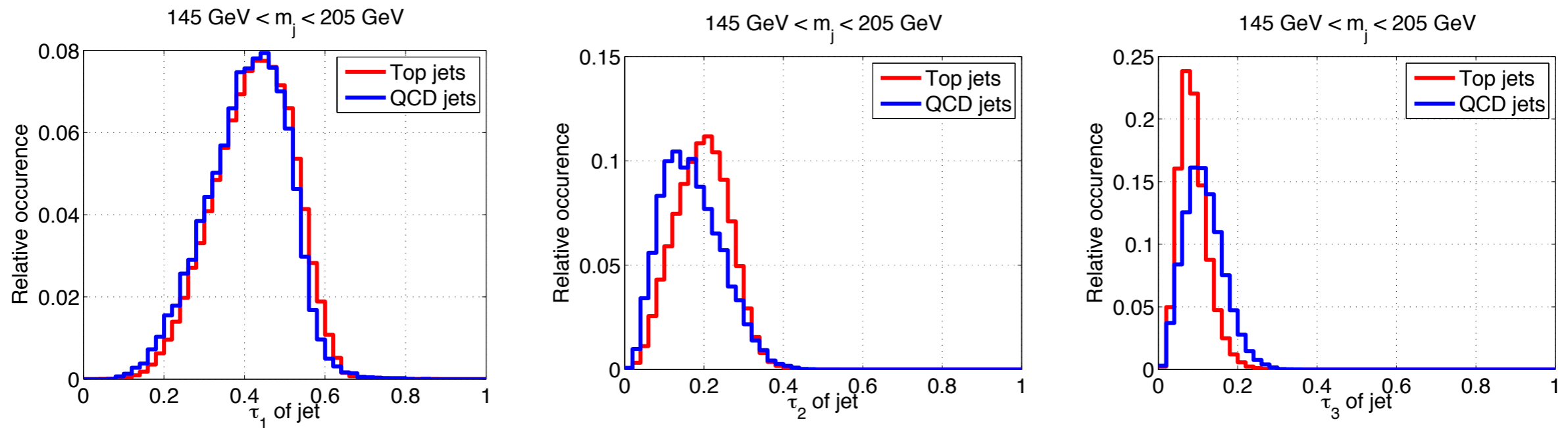
↑ Sum over constituents ↑ Minimize distance to candidate subjet axes

Later: Minimize τ_N over all possible subjet axes, becomes a true jet shape

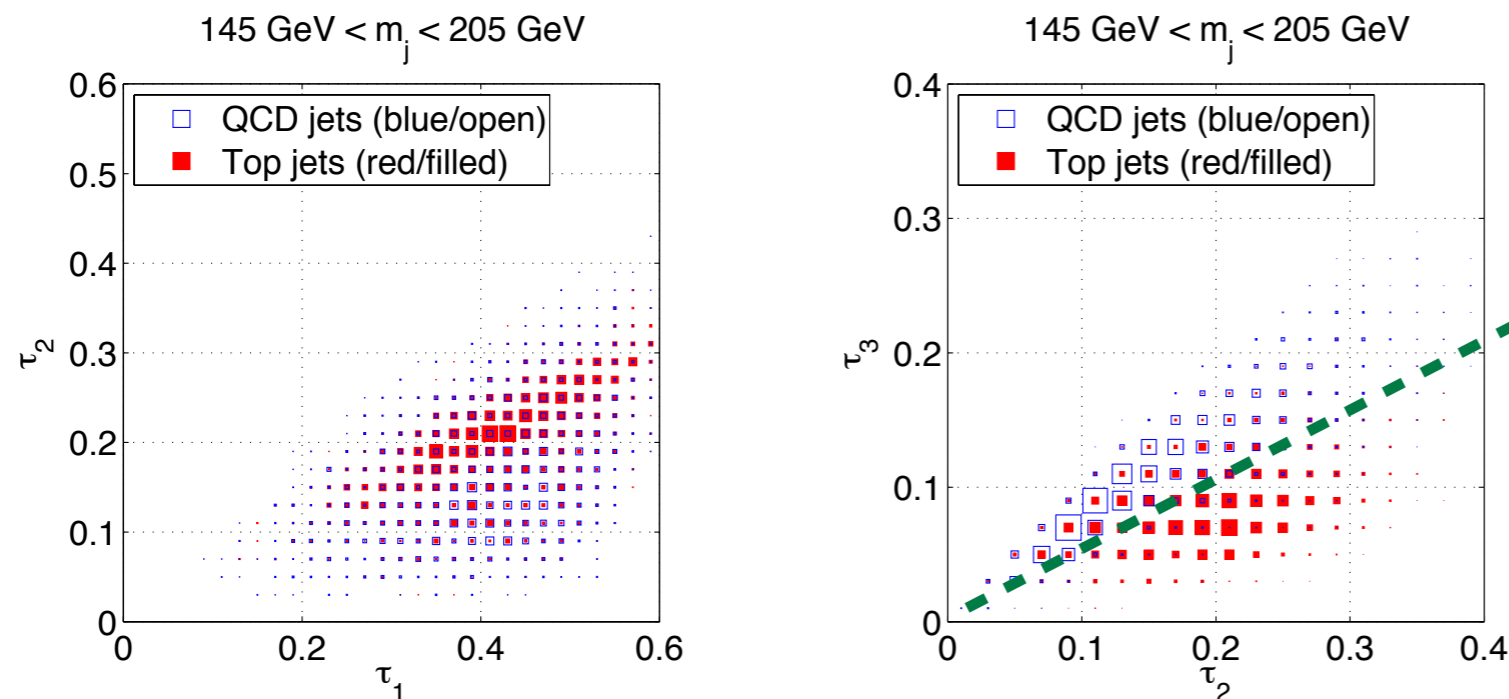
Jet shape that “counts” number of subjets!



Raw N-subjettiness for Tops

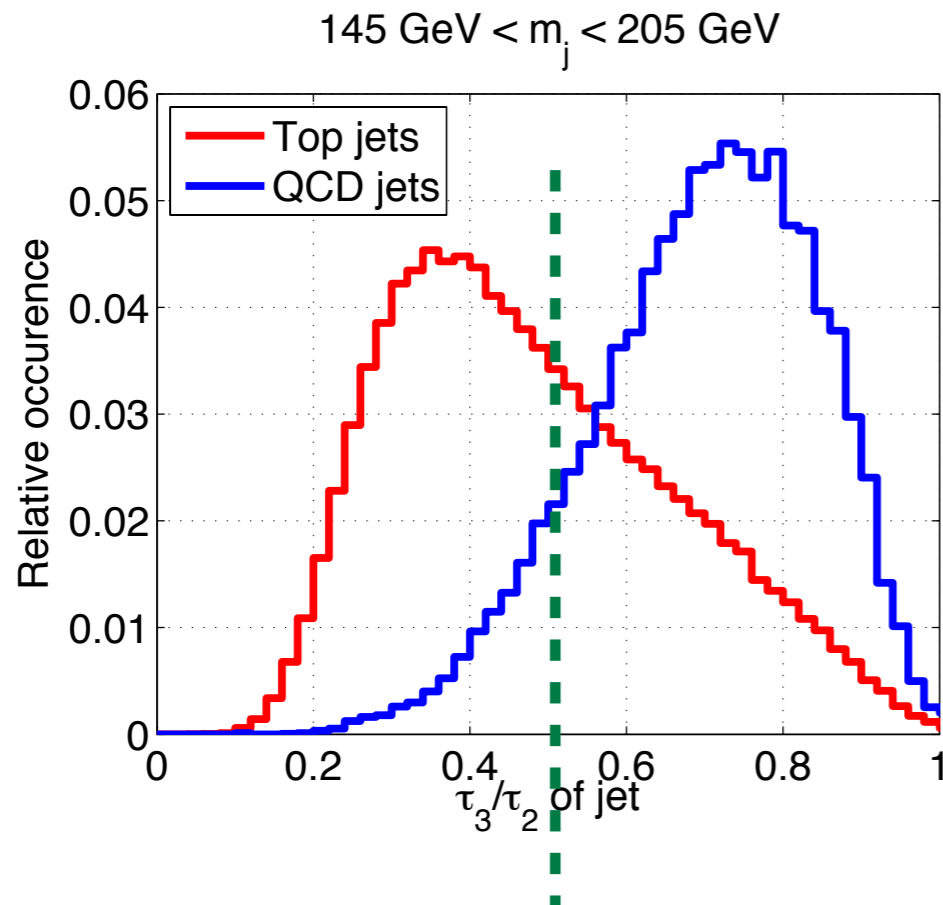


Some raw distinguishing power...



...but suggests multivariate cut!

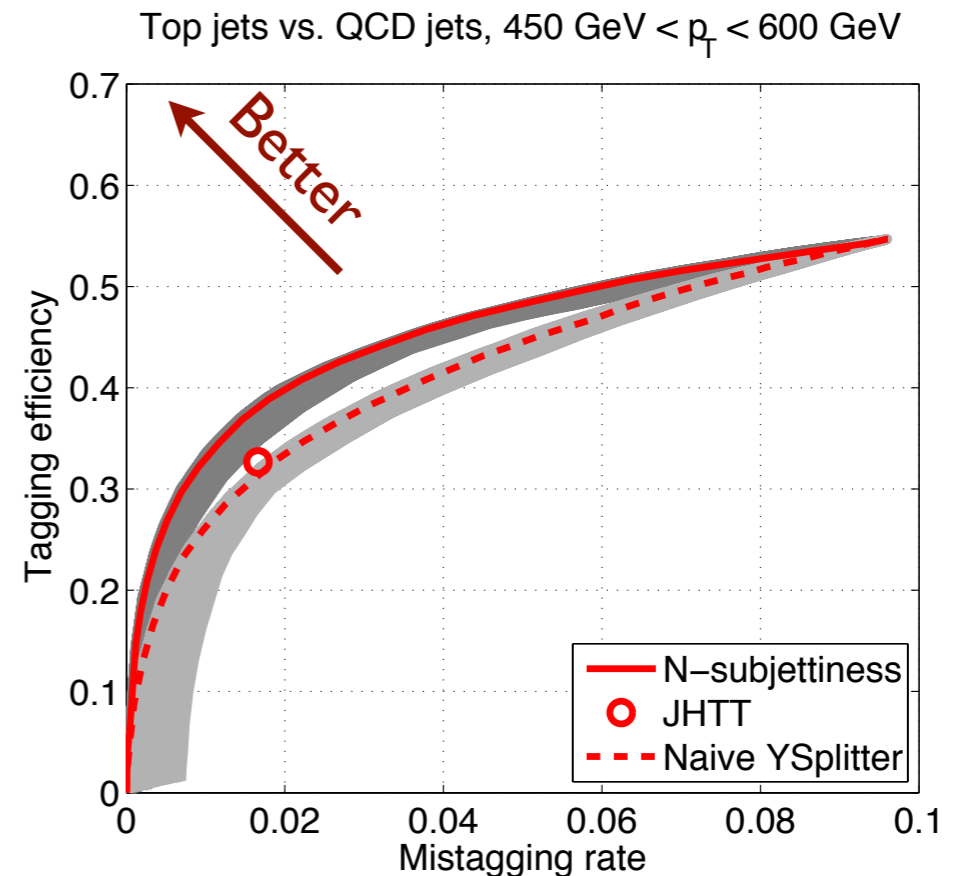
N-subjettiness for Boosted Tops



Flexible cut to adjust
signal acceptance vs.
background rejection

τ_3/τ_2 : Boosted Tops

τ_2/τ_1 : Boosted W/Z/H



Compares favorably
to existing methods!

(But “Theorist Detector”.
Our study before the
Boost2010 Proceedings)

Variations/Improvements

Different Angular Weighting

$$\tau_N = \frac{1}{d_0} \sum_k p_{T,k} \min_A \{ \Delta R_{A,k}^\beta \}$$

$\beta = 1$: \approx Jet Broadening

$\beta = 2$: \approx Thrust

$\beta = 2-a$: \approx Angularities

(Can also add dependence on axis energy. Doesn't seem to help tagging.)

Different Subject Axes

Initial Study: Exclusive k_T Subjects

Better Choice: **Axes that Minimize τ_N !**

Minimization

Classic problem in computer science!

$$\begin{array}{ccc} \tau_N = \min_{\{p_{\text{axes}}\}} \tilde{\tau}_N & \tilde{\tau}_N = \frac{1}{d_0} \sum_k p_{T,k} \min_A \{ \Delta R_{A,k}^\beta \} \\ \uparrow & \uparrow \\ \text{True Jet Shape} & \text{Hybrid Jet Shape} \end{array}$$

$\beta = 2$ (\approx thrust): “k-means clustering”

\approx iterative jet finding, fixed number of jets, voronoi boundaries

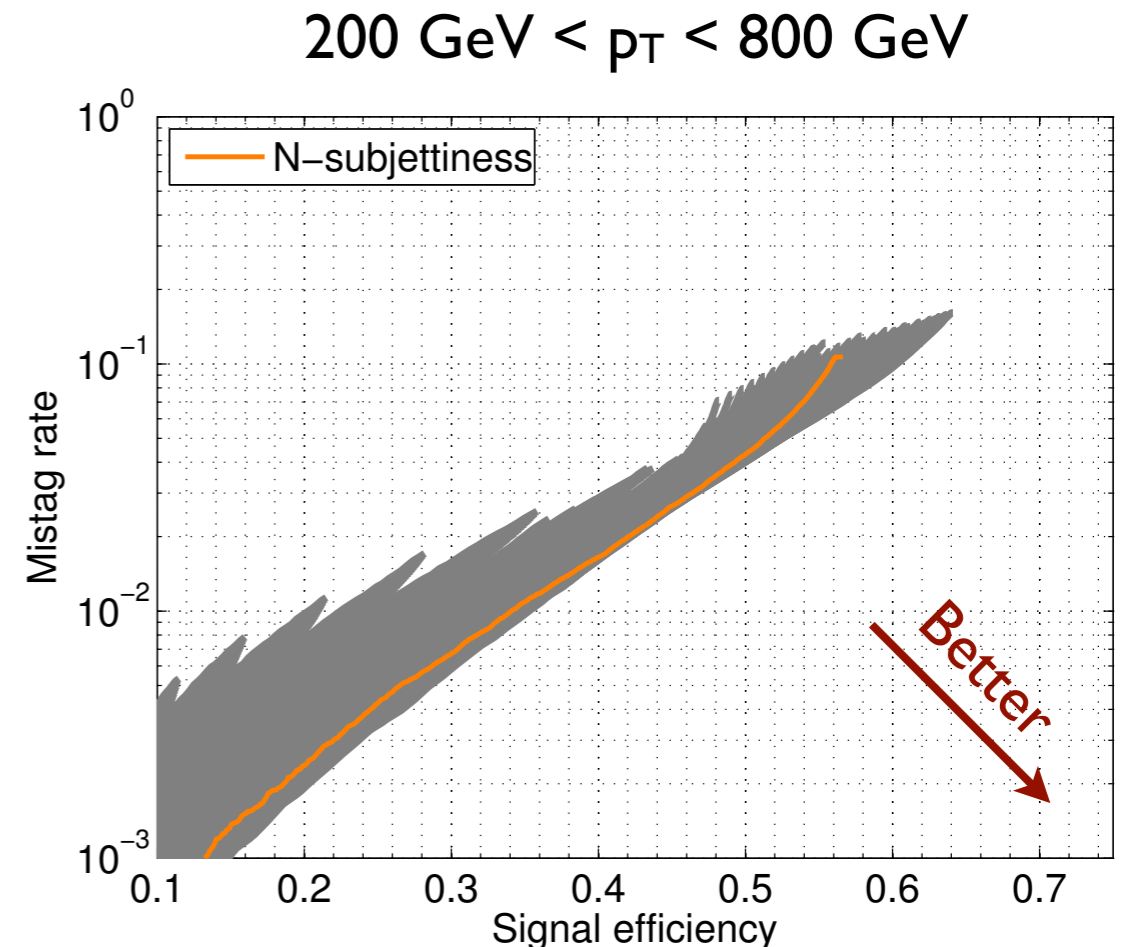
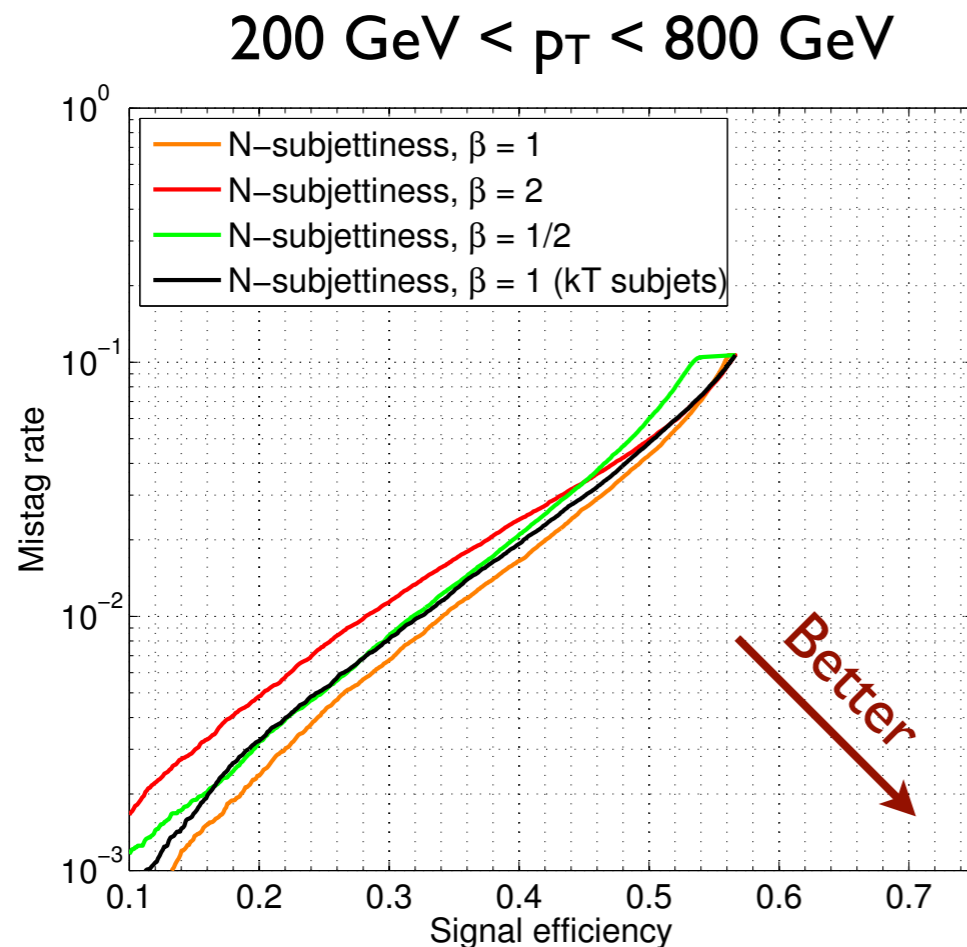
$$\frac{\partial \tilde{\tau}_1}{\partial \vec{p}_{\text{axis}}} = 0 \quad \Rightarrow \quad \vec{p}_{\text{axis}} = \sum_k \vec{p}_k$$

i.e. jet axis = jet momentum

$\beta = 1$ (\approx jet broadening): We developed new minimization algorithm,
jet axis \neq jet momentum, kind of like a “median” jet

N-subjettiness Variations

Using Boost 2010 Samples

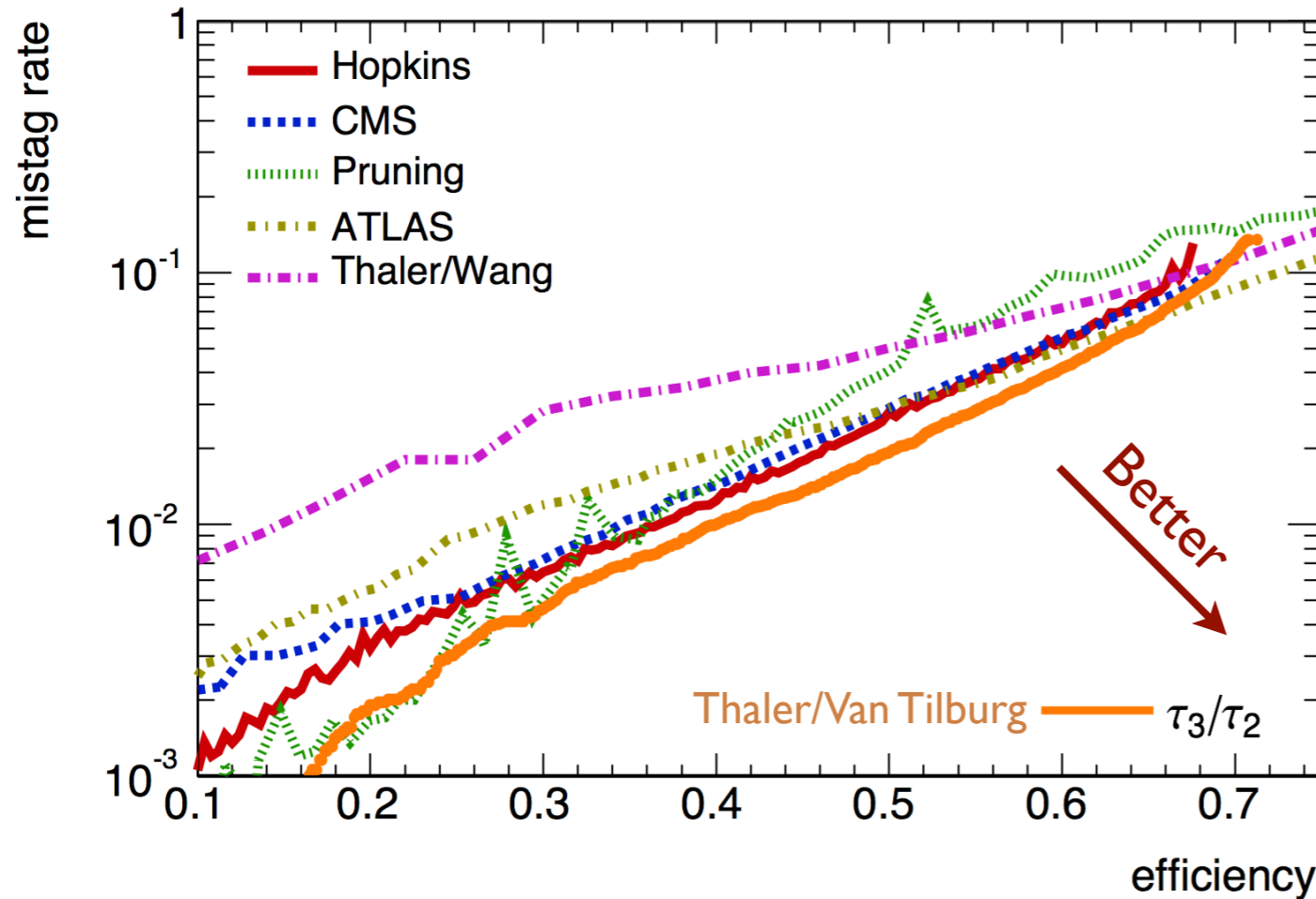


Best for Top Tagging:
 τ_3/τ_2 Cut

Jet Broadening Measure ($\beta = 1$)
Axes from Minimization

Can improve by adjusting
slope of τ_3, τ_2 cut.
Many multivariate options.

Top Tagging c. 2011



$500 \text{ GeV} < p_T < 600 \text{ GeV}$

fixed jet mass cut:
160 GeV to 240 GeV

one-dimensional cut
on τ_3/τ_2 (from minimum)

N-subjettiness:

- Intuitive measure of “number of subjects”
- Based on true jet shape (hybrid still an option)
- Plays well with multivariate methods
- Calculable (resummable?) in perturbation theory
- Excellent tagging performance out of the box
- Ratio τ_N/τ_{N-1} has reduced JES sensitivity
- Plays well with grooming

Thoughts on Jet Algorithms

Hybrid Jet Shape: $\tau_N = f(\{p_k\}, \{p_{\text{axes}}\})$

Minimization of any hybrid jet shape defines a jet algorithm!

Not a new idea... Stable cone finding:

Minimize
over axis A: $\tau_1(R_0) = \sum_k p_{Tk} \min(\Delta R_{A,k}, R_0)^2 \leftarrow \text{Key!}$

Solution: $p_{\text{jet}} = \sum_k p_k$ in cone [Ellis, Huston, Tonnesmann]

In CS optimization: cluster finding = minimization

N-jettiness Jets?

Minimize τ_N ($\beta = 2$) = k-means clustering

[See Chekanov]

Quasi-minimize $\tau_N(R_0)$ ($\beta = 2$) \approx anti- k_T (!)

(if N known, because jet axis = jet momentum)

Potential Benefits of Jets from τ_N

τ_N defines jet directions *and* quality measure
Controllable split-merge (allows “recoil” like in anti- k_T)
With $\beta \neq 2$, can study jet axis \neq jet momentum
And anti- k_T is very close to doing this already

Potential Issues with Jets from τ_N

Have to know N ahead of time (is this really a problem?)
Hard to guarantee global minimum (recall seeded cone IRC non-safety)
 R_0 leads to local minima and slow convergence

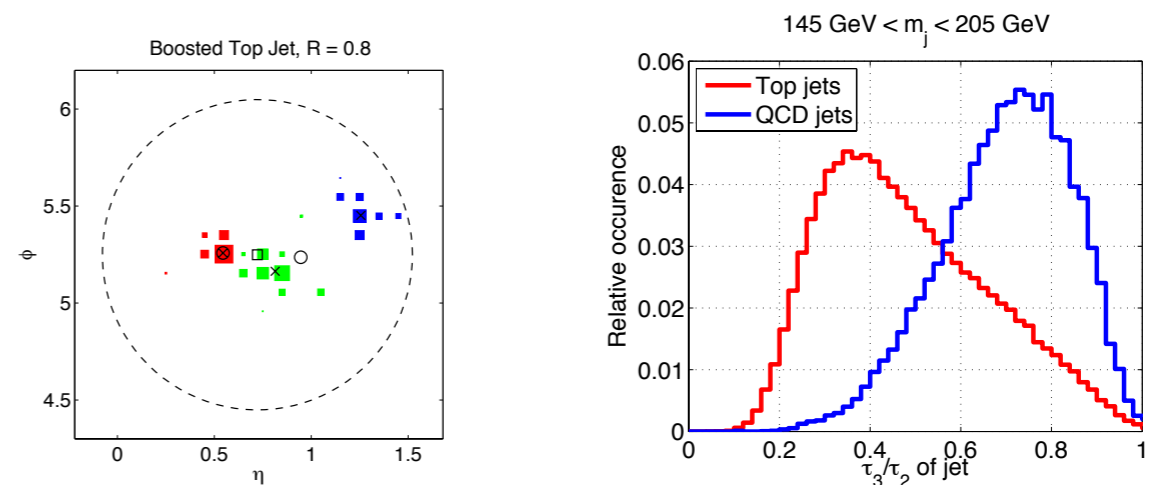
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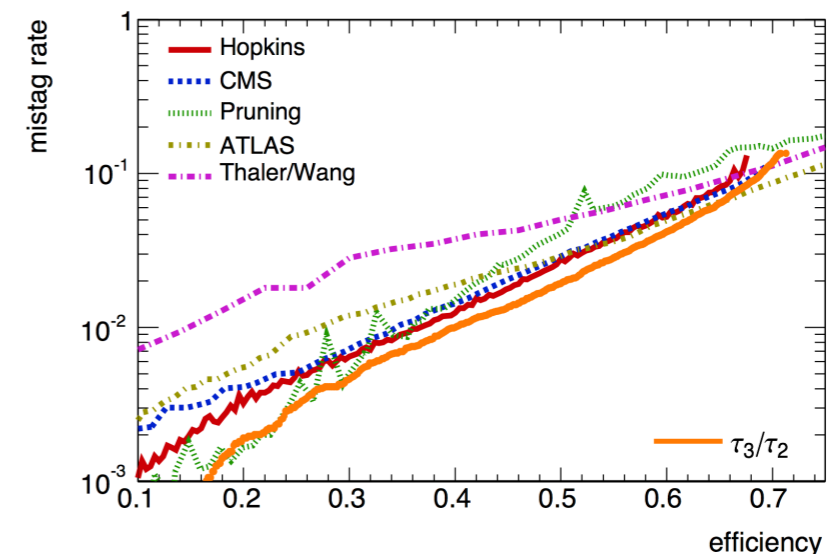
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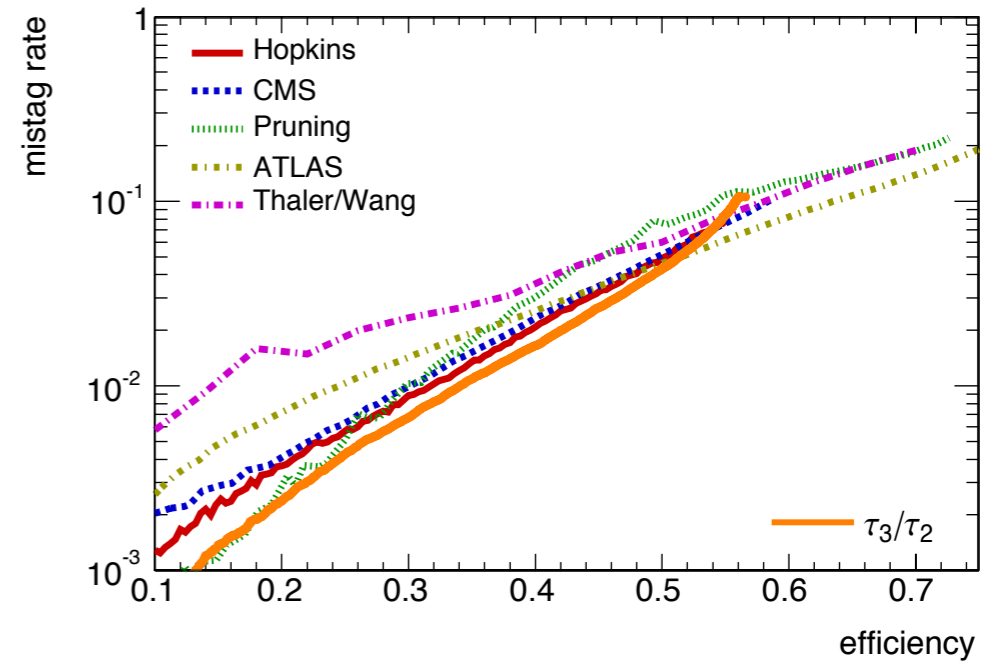
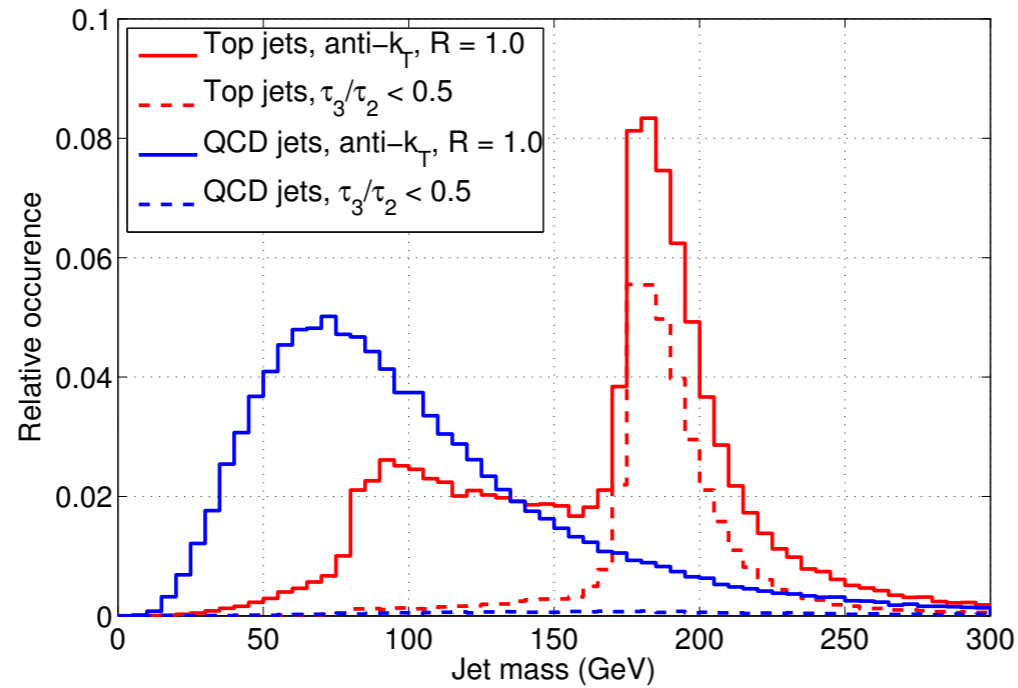
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Backup Slides

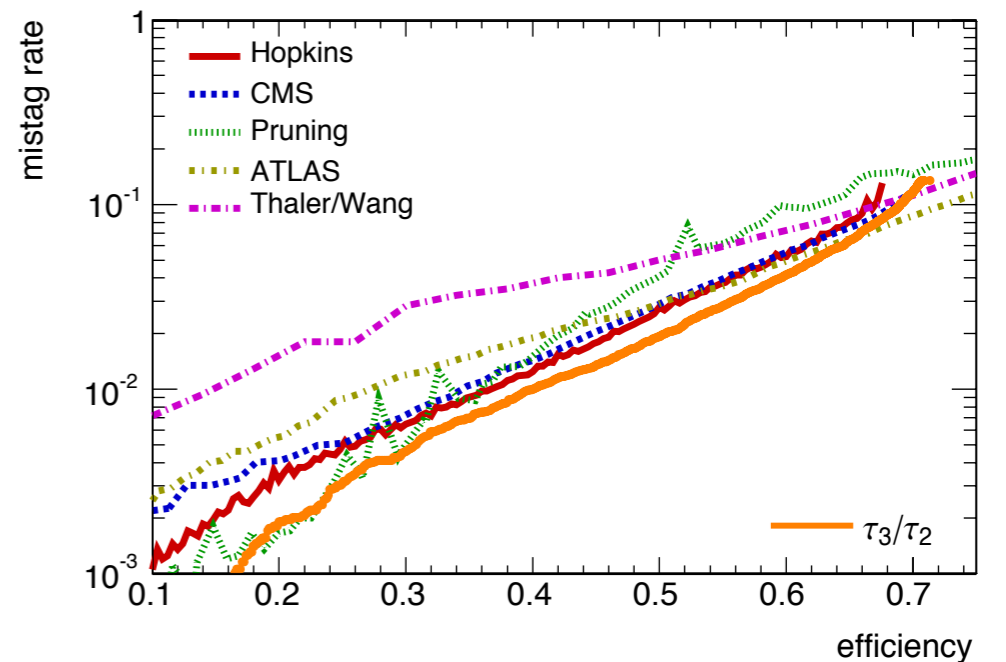
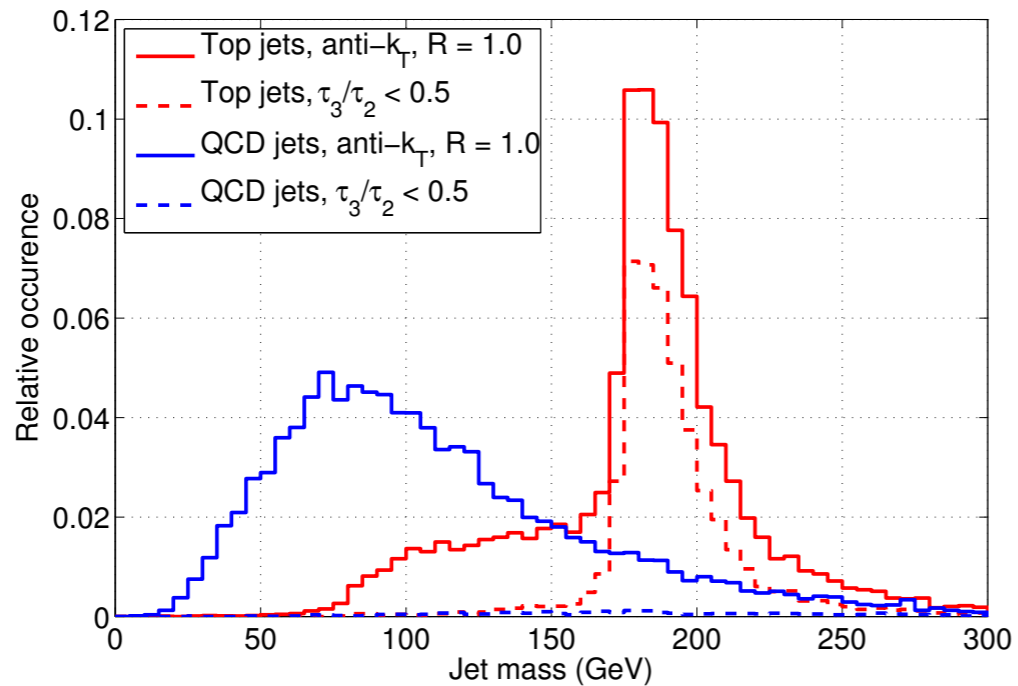
More Plots

Using Boost 2010 Samples

200 GeV
< p_T <
800 GeV



500 GeV
< p_T <
600 GeV



W Tagging

