

# Preliminary tracking results

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MuCol workshop on RCS, pulsed magnets & powering (15 May 2024, CERN)

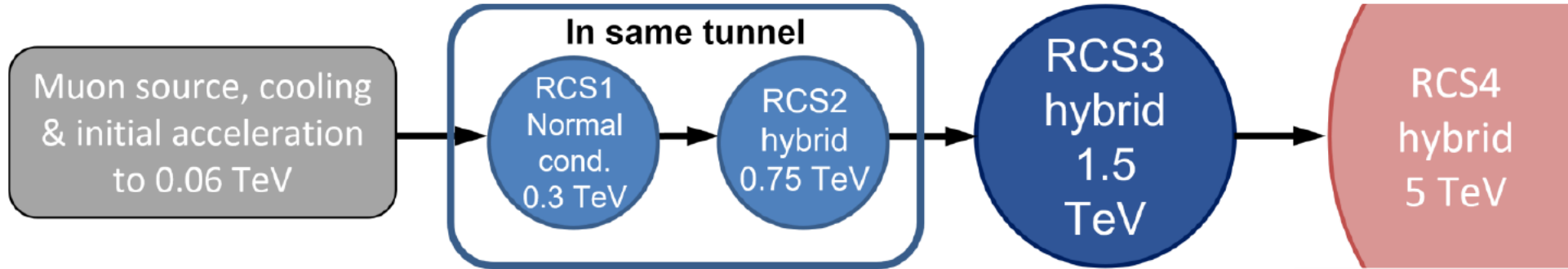


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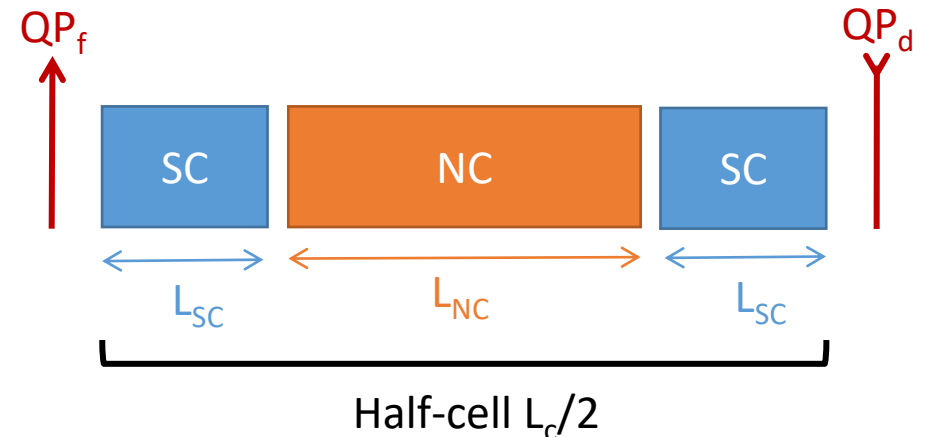


# Structure of a RCS

- Chain of RCS



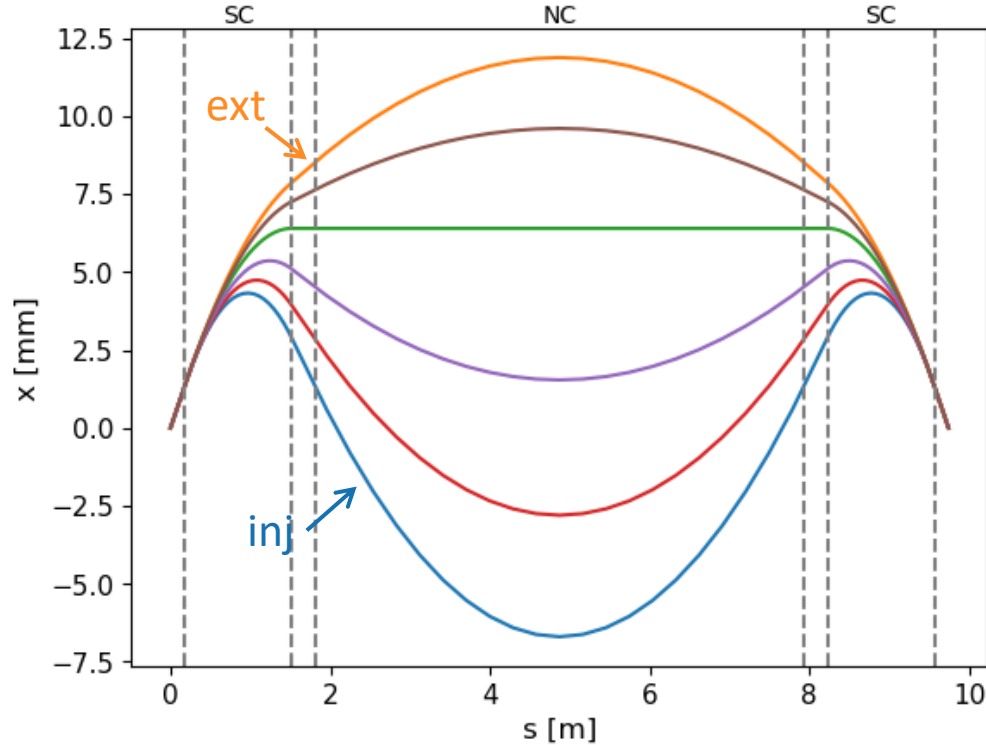
- Study focused on RCS2: hybrid synchrotron
- Structure of RCS: FODO cells with phase advance:  $\mu=90^\circ$
- RCS2 geometric parameters:
  - $C=5990\text{m}$
  - $n_{\text{arc}}=26$
  - $n_{\text{RF}}=26$
  - $n_c=8$  cells per arc



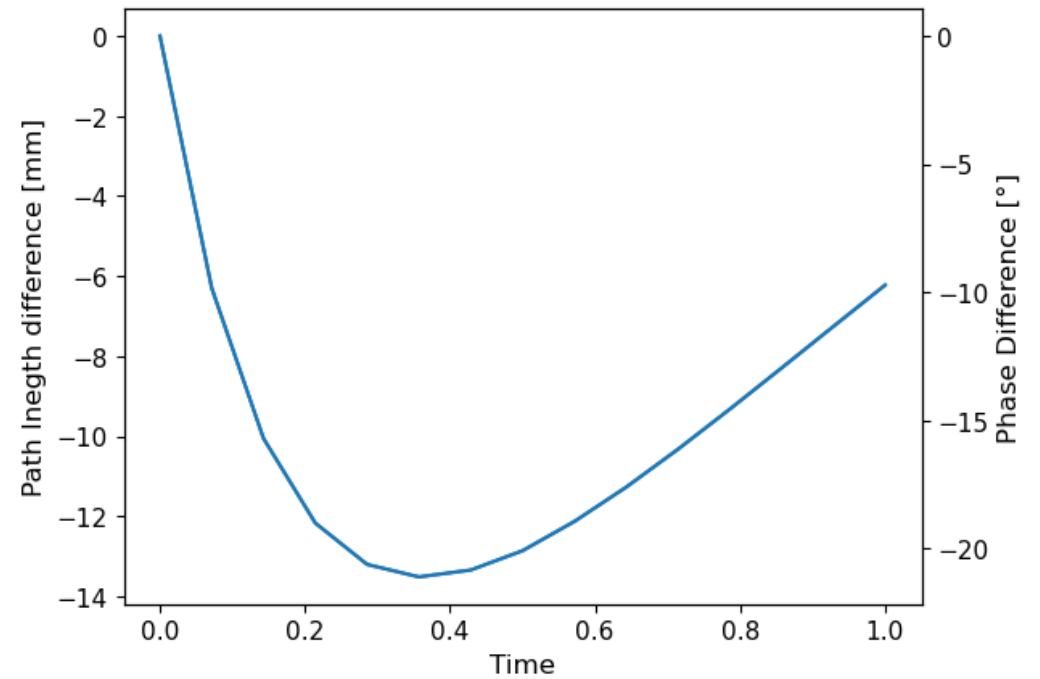
# Difference of trajectory during ramping

## Results from Xsuite

Trajectories from injection to extraction



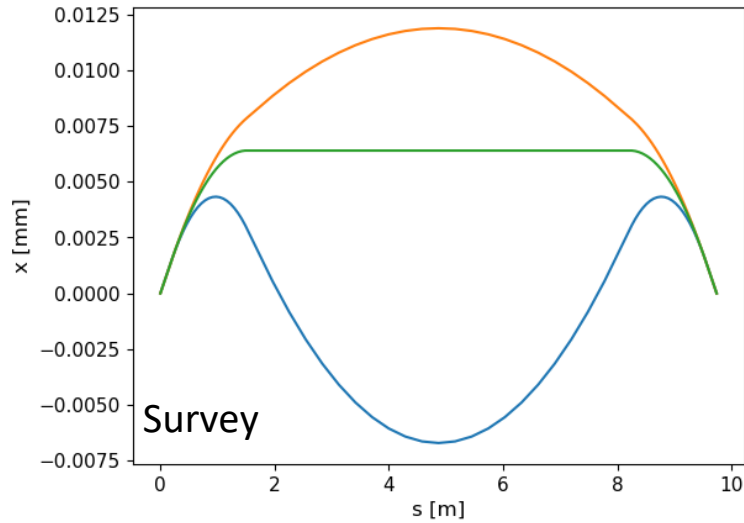
Path length difference from injection



RF tuning ?

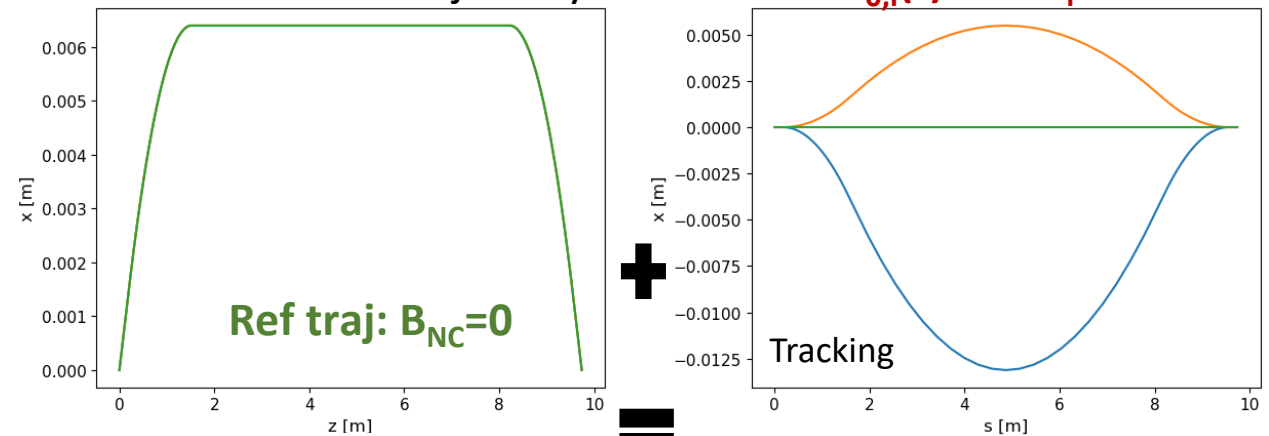
# Defining a reference trajectory during ramping

① Reference trajectory is not constant.  
Normalized strength and bending of reference trajectory varies together:  $k_{0,i}(t) = h_i(t)$

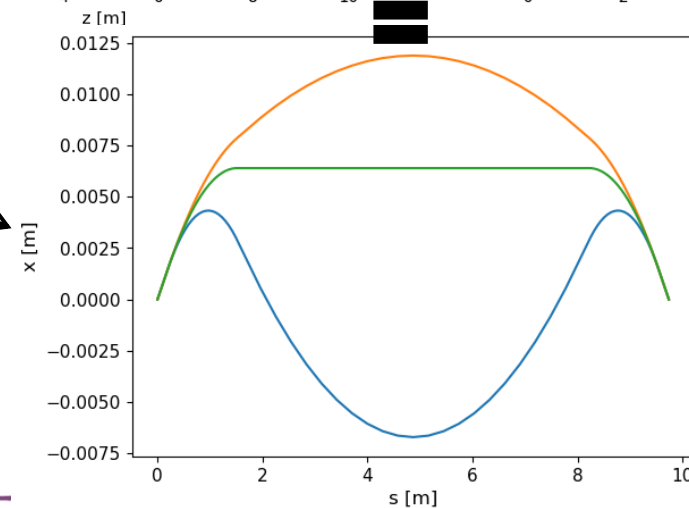


② Reference trajectory is constant

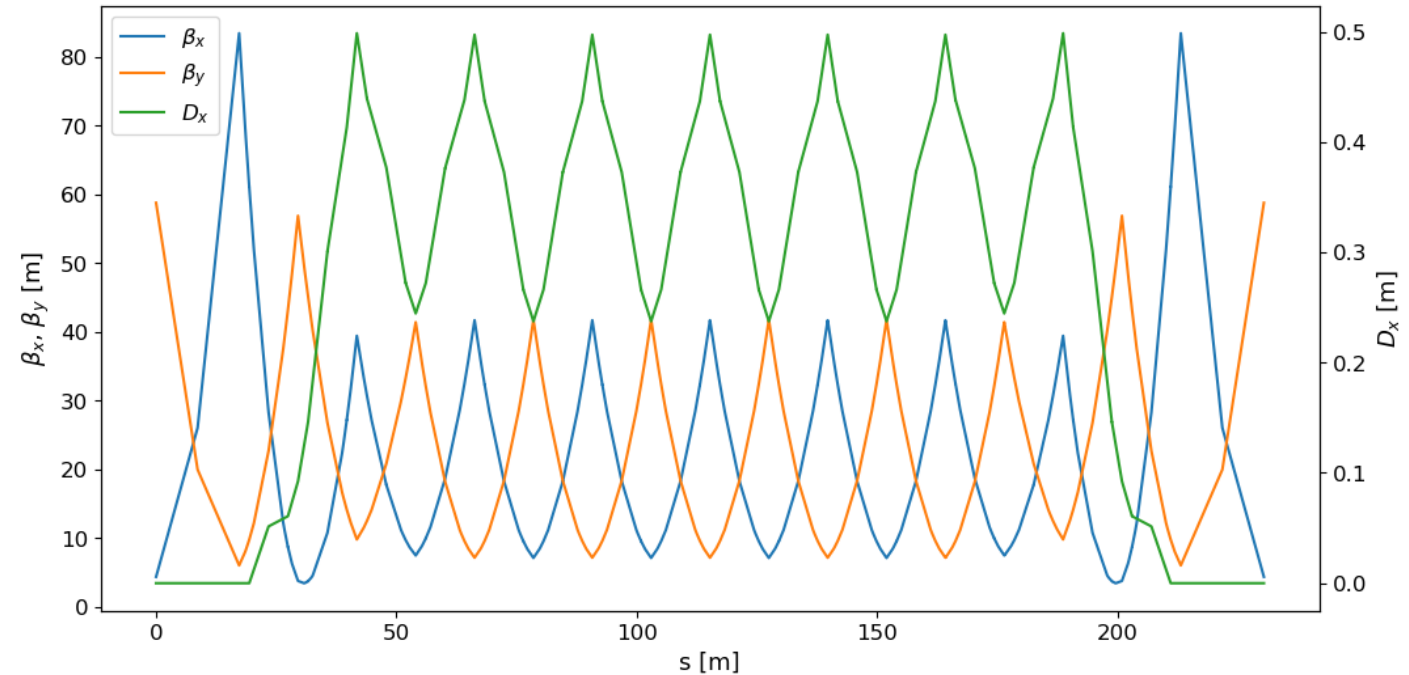
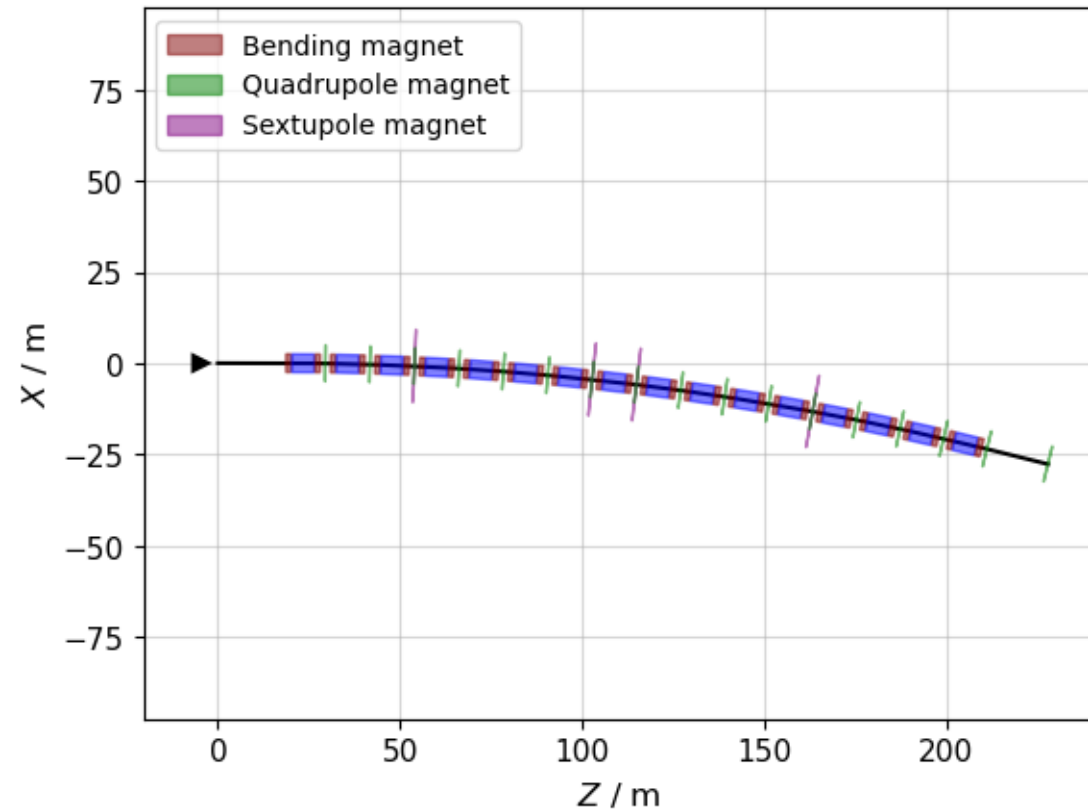
Only normalized strength of dipole varies and bending of reference trajectory is constant:  $k_{0,i}(t)$  and  $h_i = h^*$



Same trajectories



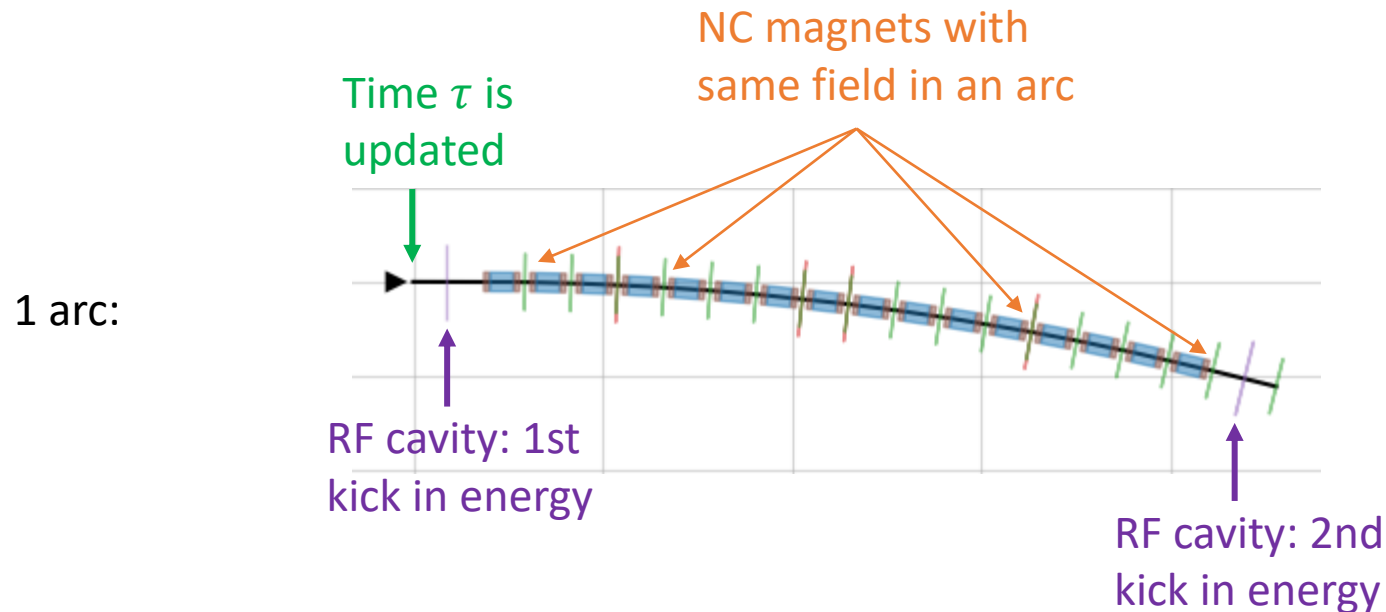
# Structure of an arc and optics



- FODO structure, base of  $\mu=90^\circ$
- Dispersion suppressor for RF insertion (cavity + energy kick)
- Quad and Sextupoles: thin multipole approximation
- Dipoles: thick bend, sliced before tracking

# Ramping in Xsuite

- How is ramping done in RCS ?
  - Magnets can include time  $\tau$ -varying attributes like the normalized strength  $k_0$
  - Time variable  $\tau$  is updated only at the beginning of the lattice (each arc here): the magnet fields are updated only at the beginning of each arc.

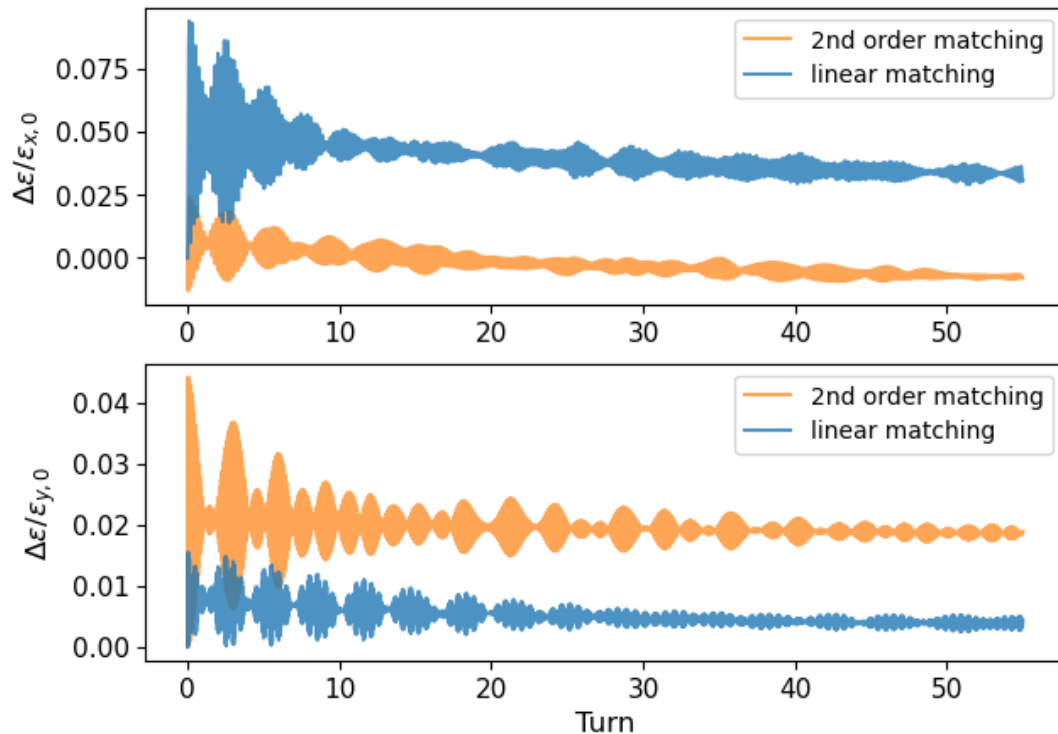


# Impact of Montague functions

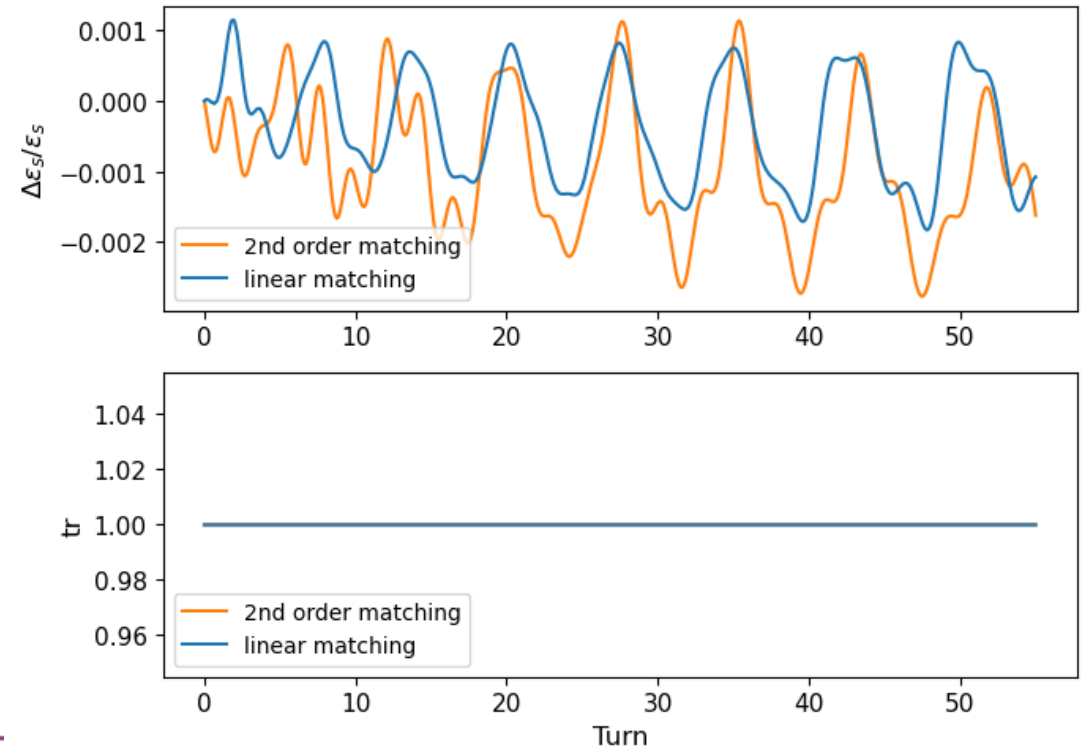
Initial distribution  
 $\epsilon_n^h = \epsilon_n^v = 25 \mu m \text{ rad}$   
 $\sigma_z \sigma_E = 0.025 \text{ eVs}$

- Dependence of Twiss parameters on relative energy difference  $\delta$ :  $\beta_x(\delta)$ ,  $\beta_y(\delta)$ ,  $\alpha_x(\delta)$ ,  $\alpha_y(\delta)$
- Beam is linearly adapted but not perfectly adapted (higher order)  $\rightarrow$  emittance growth.  
 We superficially get rid of the problem by initially matching the beam to the optics depending on  $\delta \rightarrow$  **Work on optics to be done !**

Relative transverse emittance growth

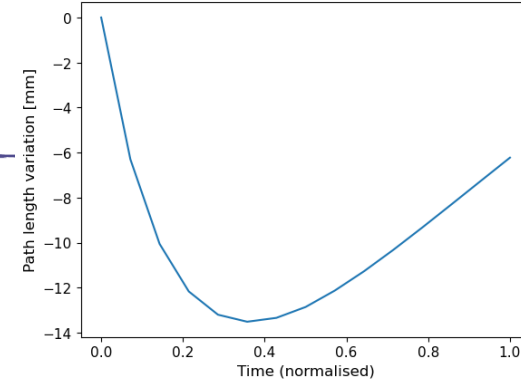


Relative longitudinal emittance growth and transmission

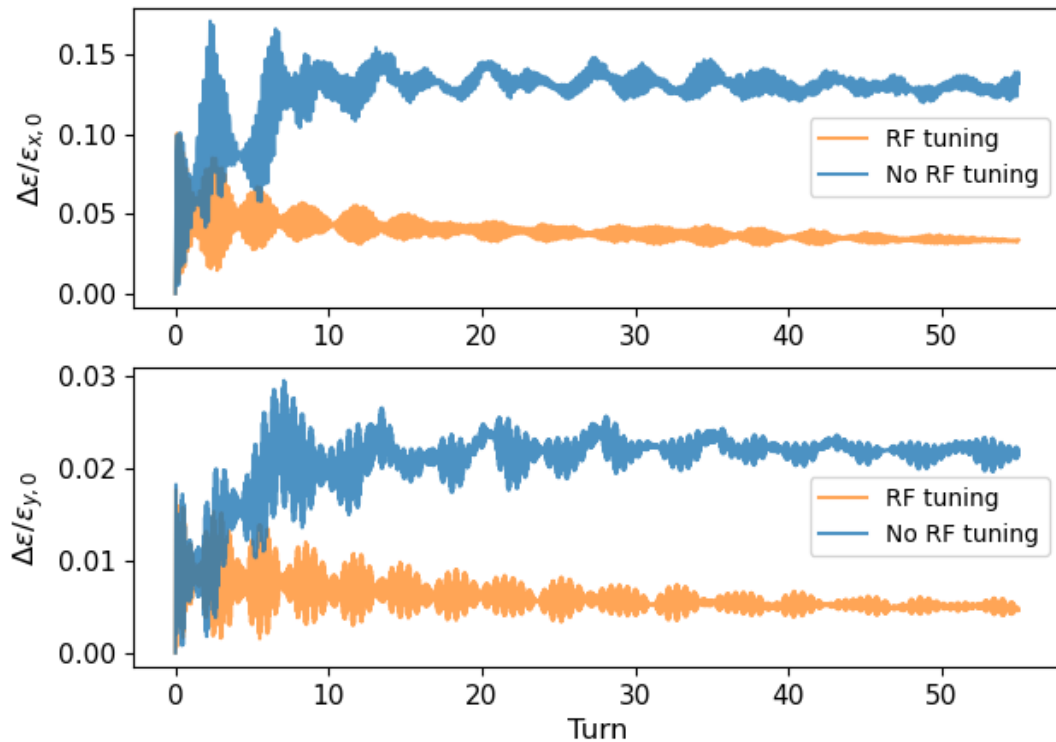


# Effect of path length difference and RF tuning

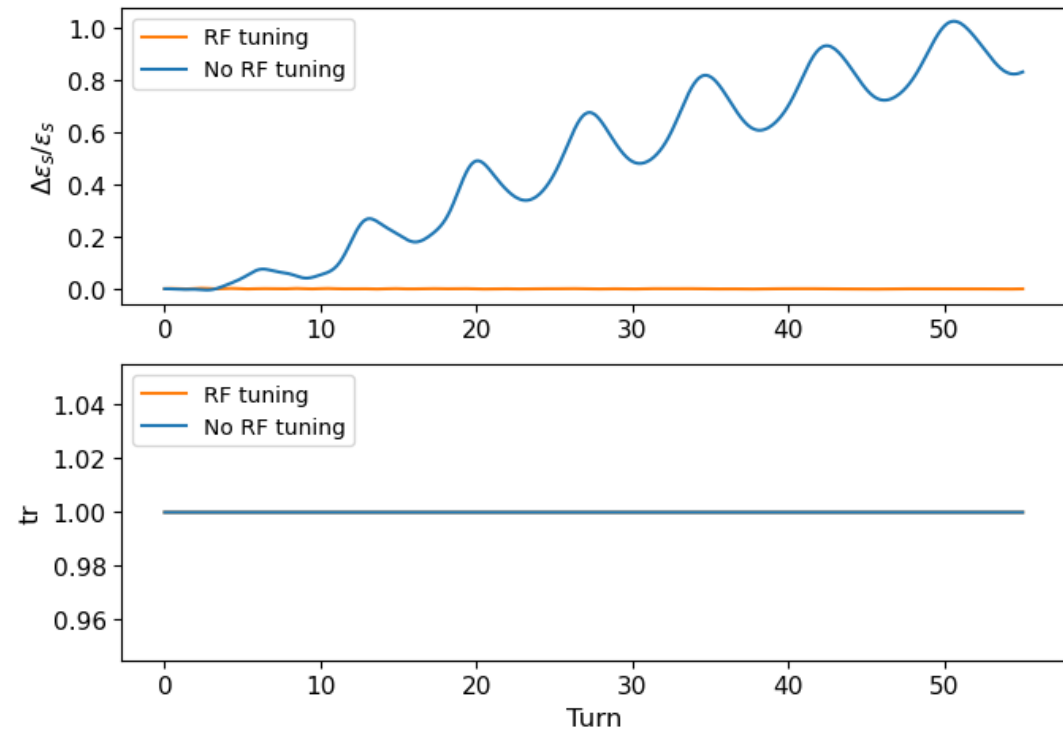
RF tuning  $\leftrightarrow$  Applies a time shift to the particle when going through the RF cavity equal to the time of flight difference with the reference trajectory.



### Relative transverse emittance growth



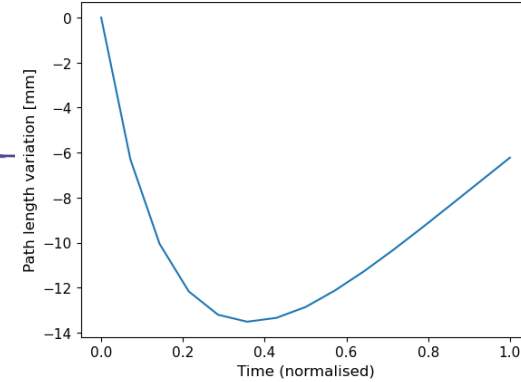
### Relative longitudinal emittance growth and transmission



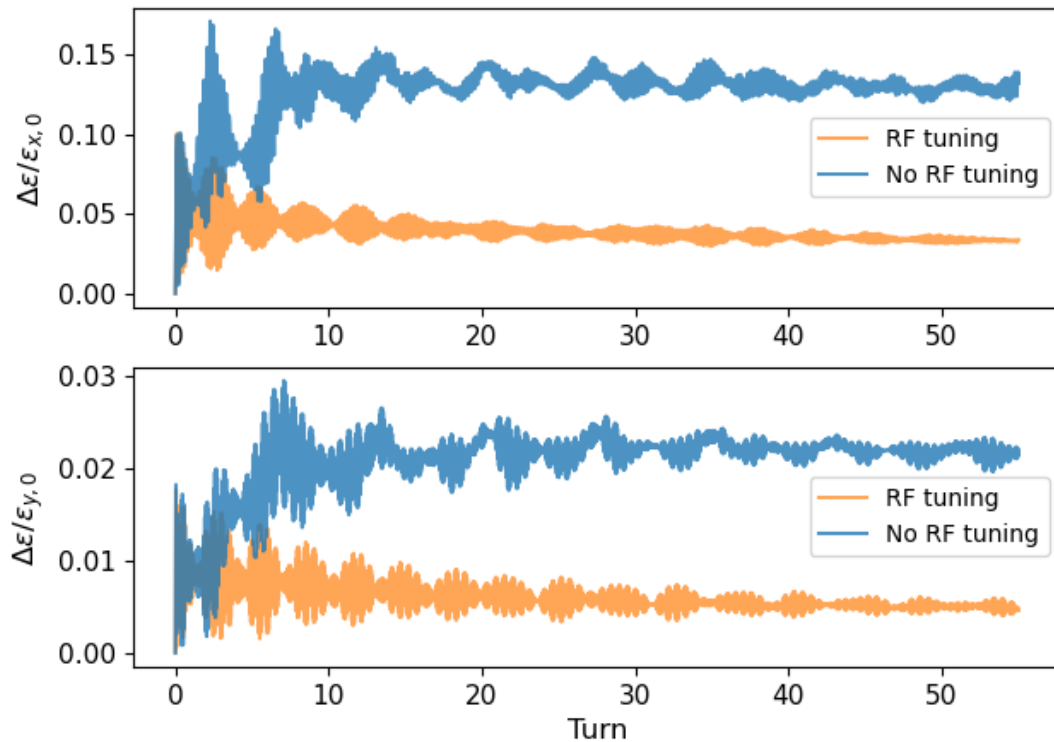


# Effect of path length difference and RF tuning

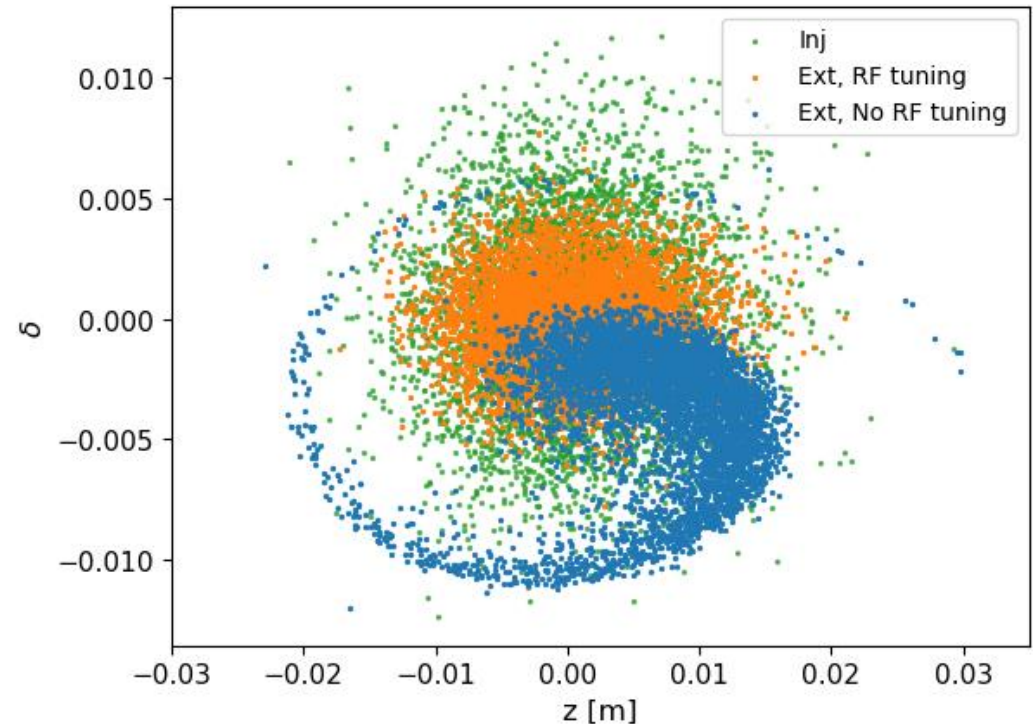
RF tuning  $\leftrightarrow$  Virtually give a  $\Delta z$  shift to the reference trajectory when going through the RF cavity :



Relative transverse emittance growth



Longitudinal phase-space



# Adding higher multipolar component to the dipoles

- So far, dipoles only had b1 component = dipolar component
- No alignment errors, no rolls, no fringe field: « perfect vertical field »
- Include b3 and b5 => systematic errors added to all the SC dipoles
- Different dipole designs: different b3/b5 to be tested
- Correct chromaticity after introducing b3:  $dq_x=5$ ,  $dq_y=5$

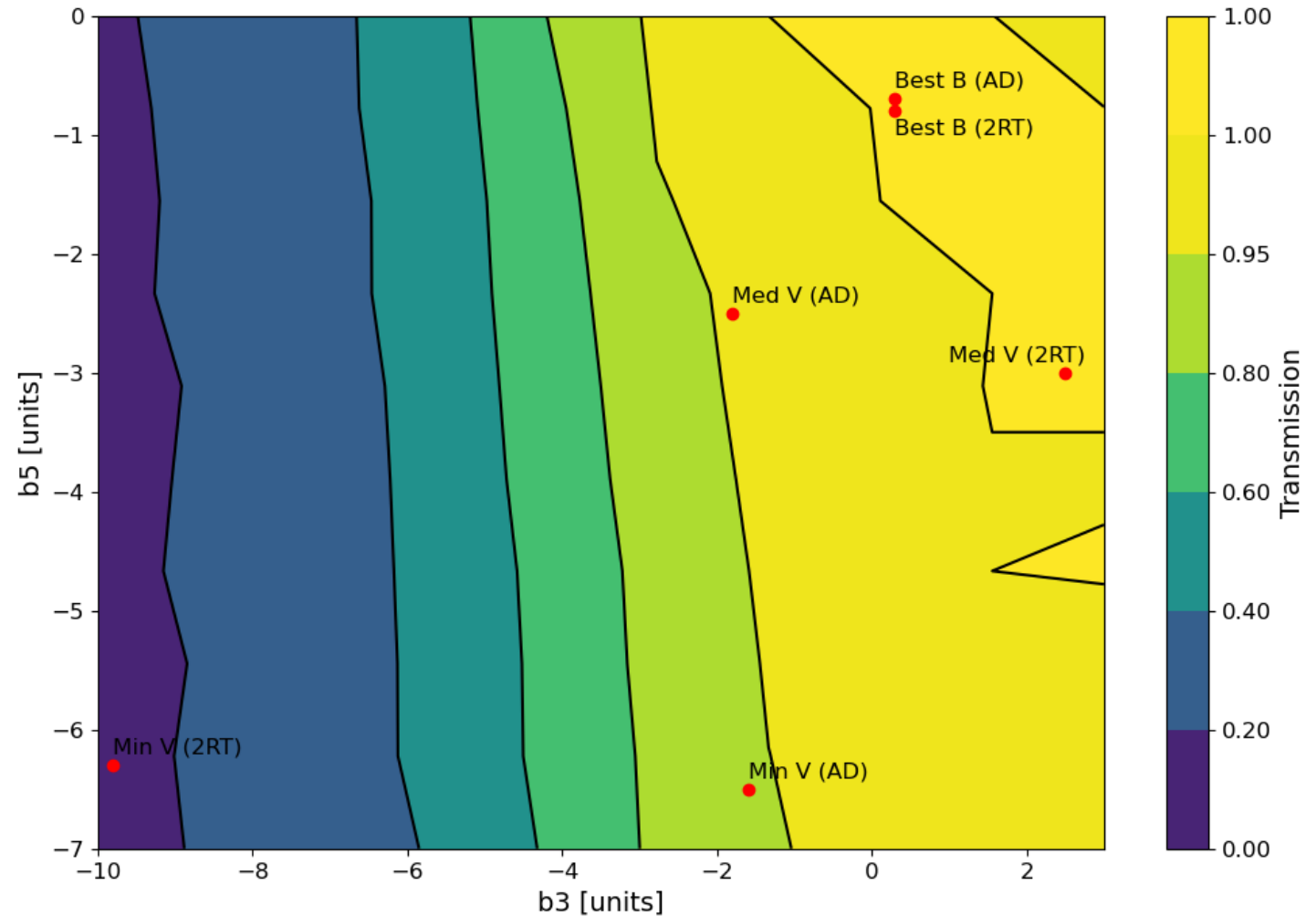
2 RTs *		b3 [units]	b5 [units]
(Min V)	1. Minimum Volume	-9.8	-6.3
(Med V)	2. Median Volume	2.5	-3.0
(Best B)	3. Best Field Quality	0.3	-0.8

Additional coils (AD) *		b3 [units]	b5 [units]
	1. Minimum Volume	-1.6	-6.5
	2. Median Volume	-1.8	-2.5
	3. Best Field Quality	0.3	-0.7

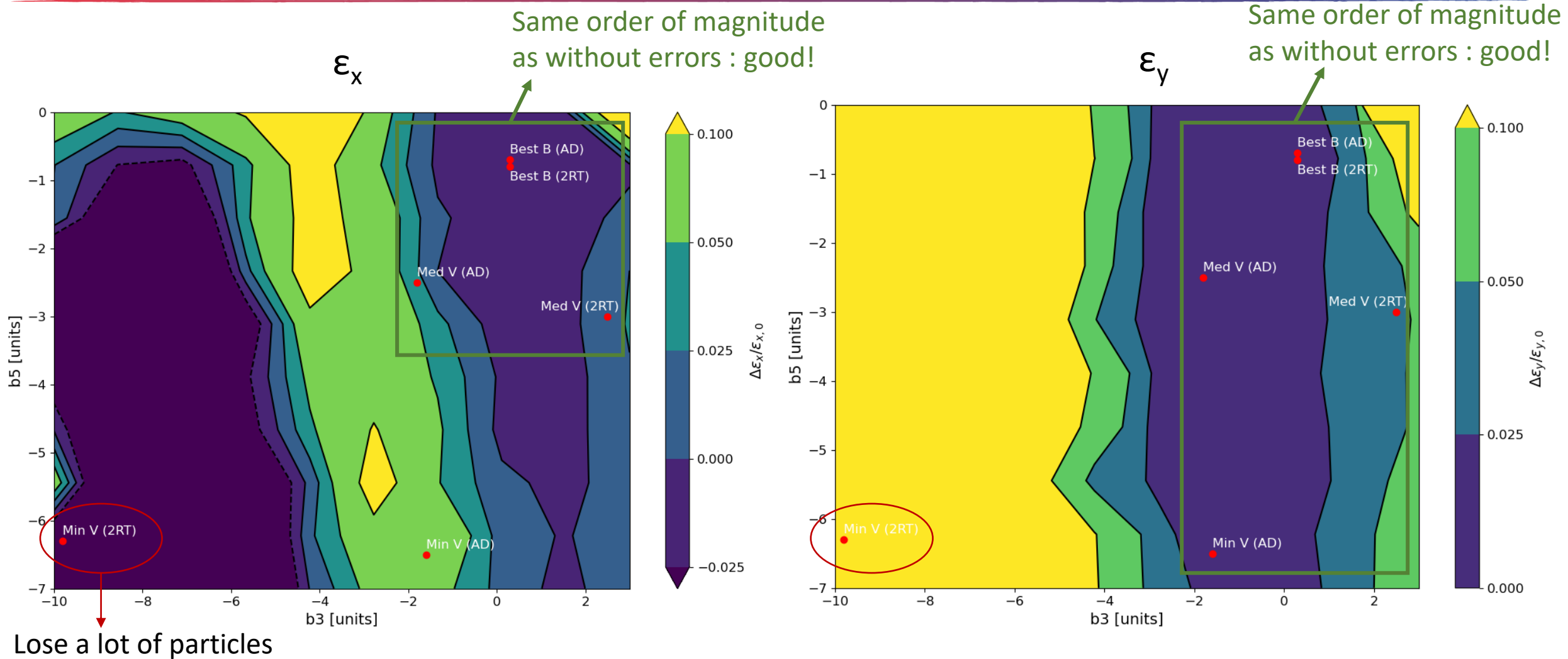
\* Initial Magnetic Design of Superconducting Dipoles in Acceleration Stage - Siara Fabbri, Luca Bottura (IMCC-MuCol annual meeting 2024)

## Transmission map

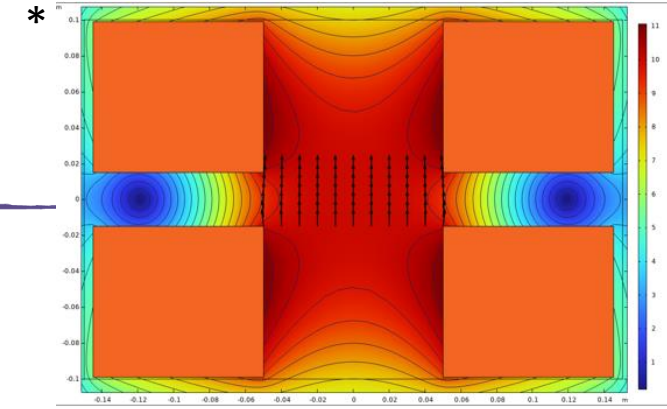
- Rough scan :  $10 * 10$  points  
→ get an idea of the good/bad regions
- Minimum volume (2RT) : not good enough
- Best field + MedV designs are the best
- Optics not yet optimised : could improve those results



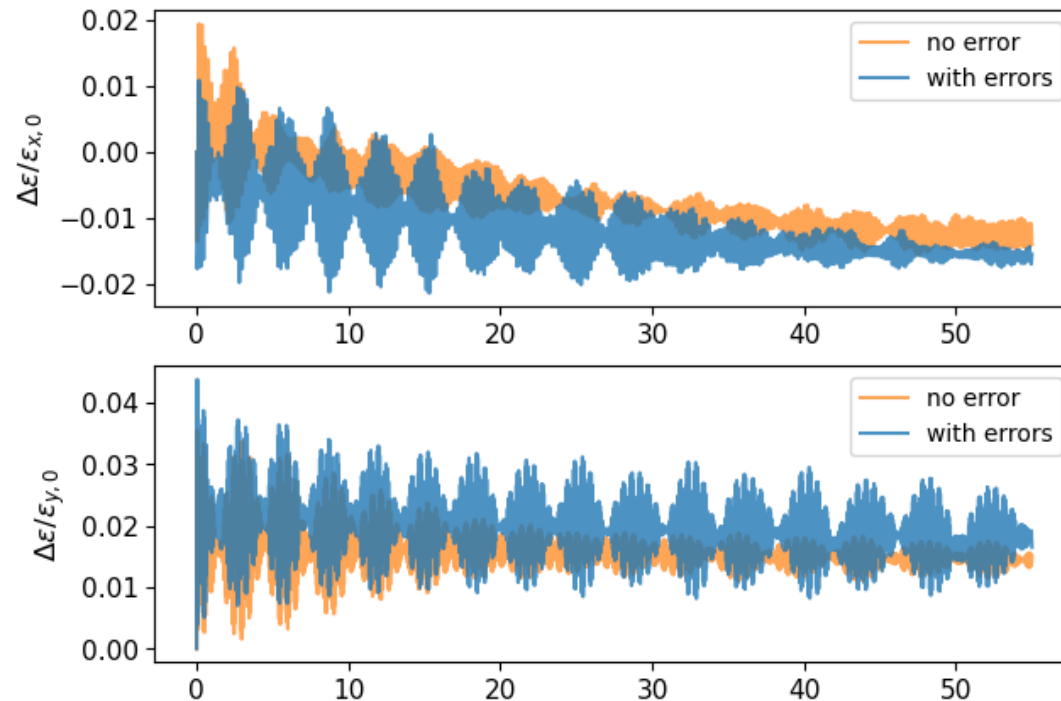
# Rough scan of b3/b5 component Emittance growth



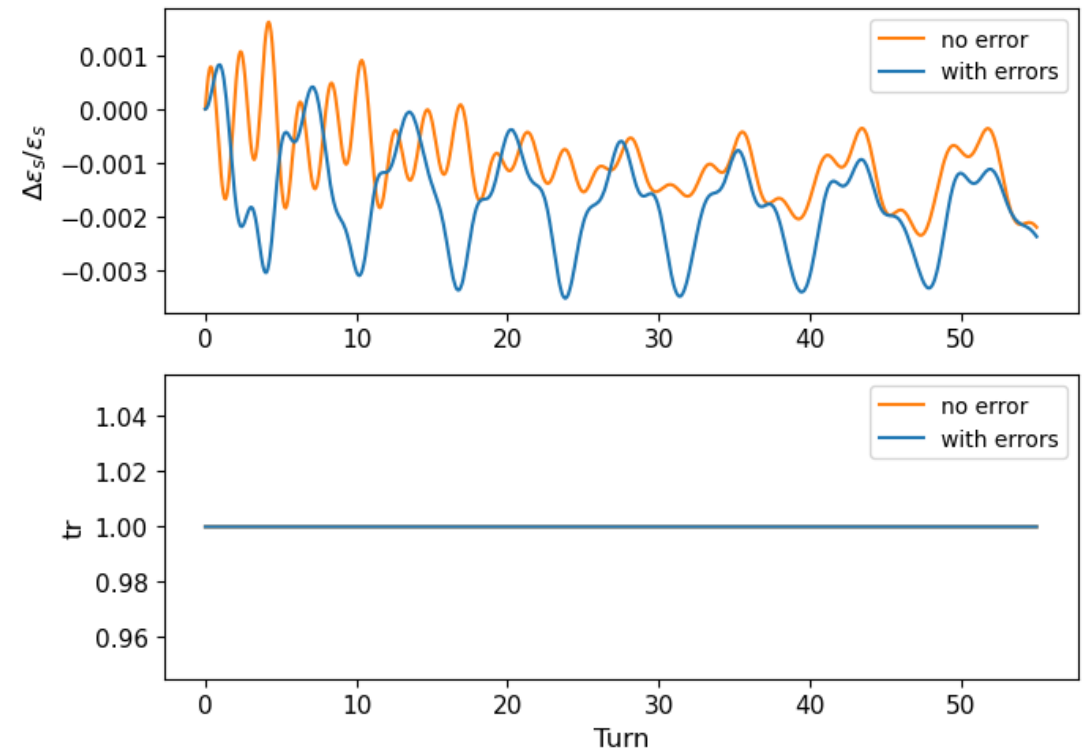
# Best Field Quality (2RT)



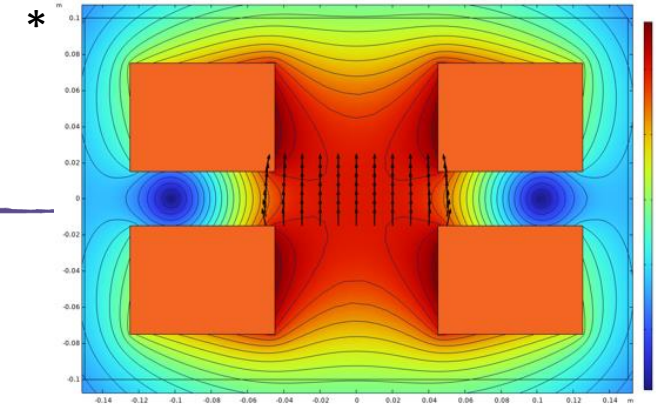
- Relative transverse emittance growth



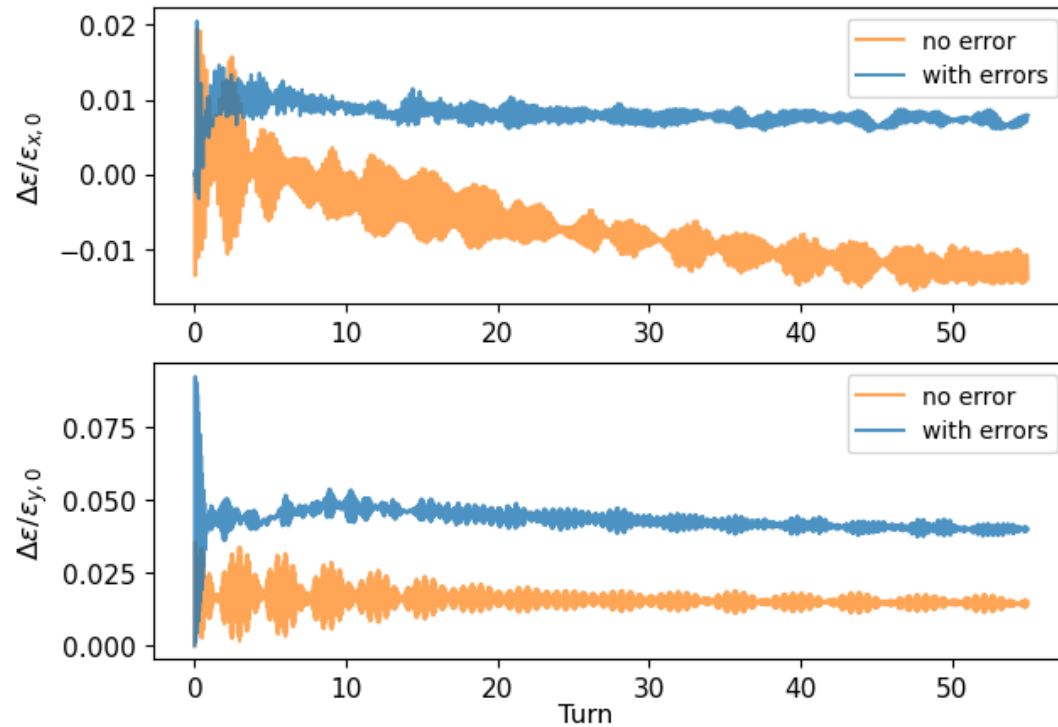
- Relative longitudinal emittance growth and transmission



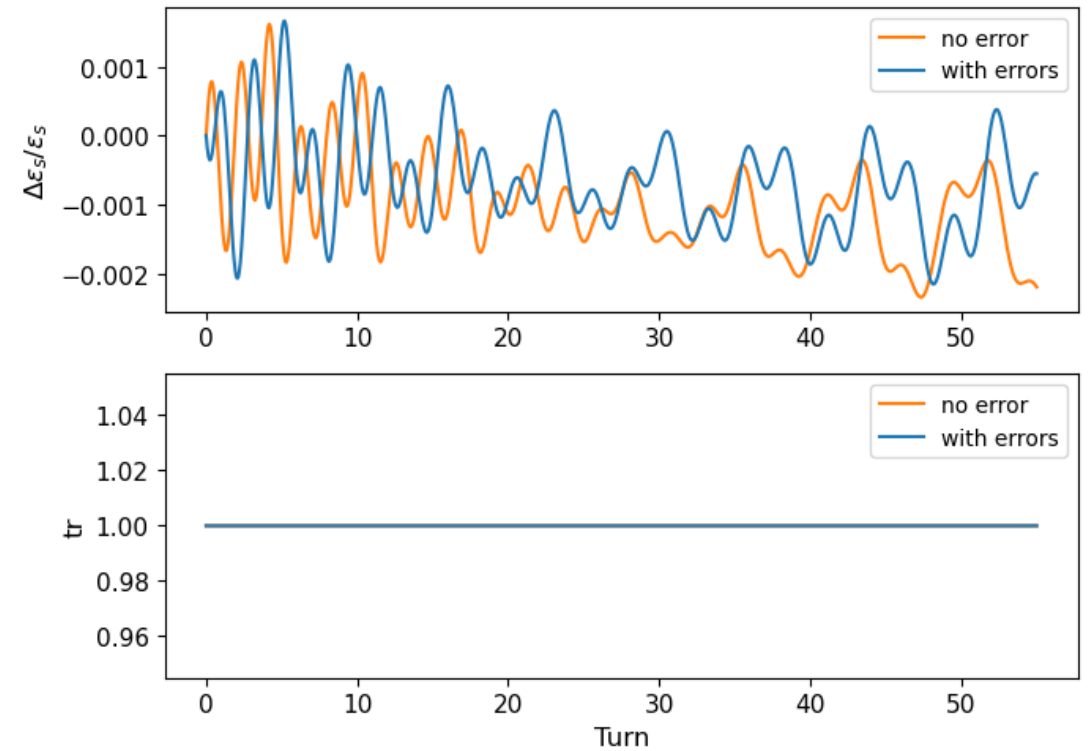
# Median Volume (2RT)



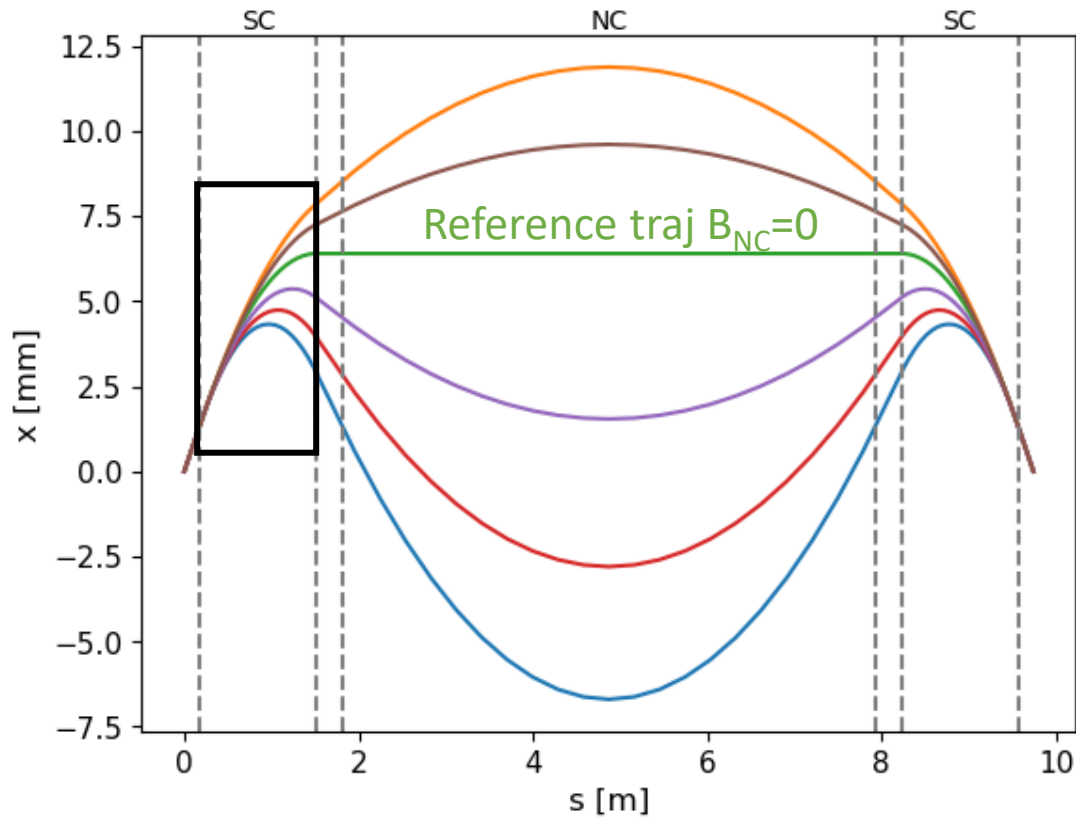
- Relative transverse emittance growth



- Relative longitudinal emittance growth and transmission



# Good field region of SC dipoles

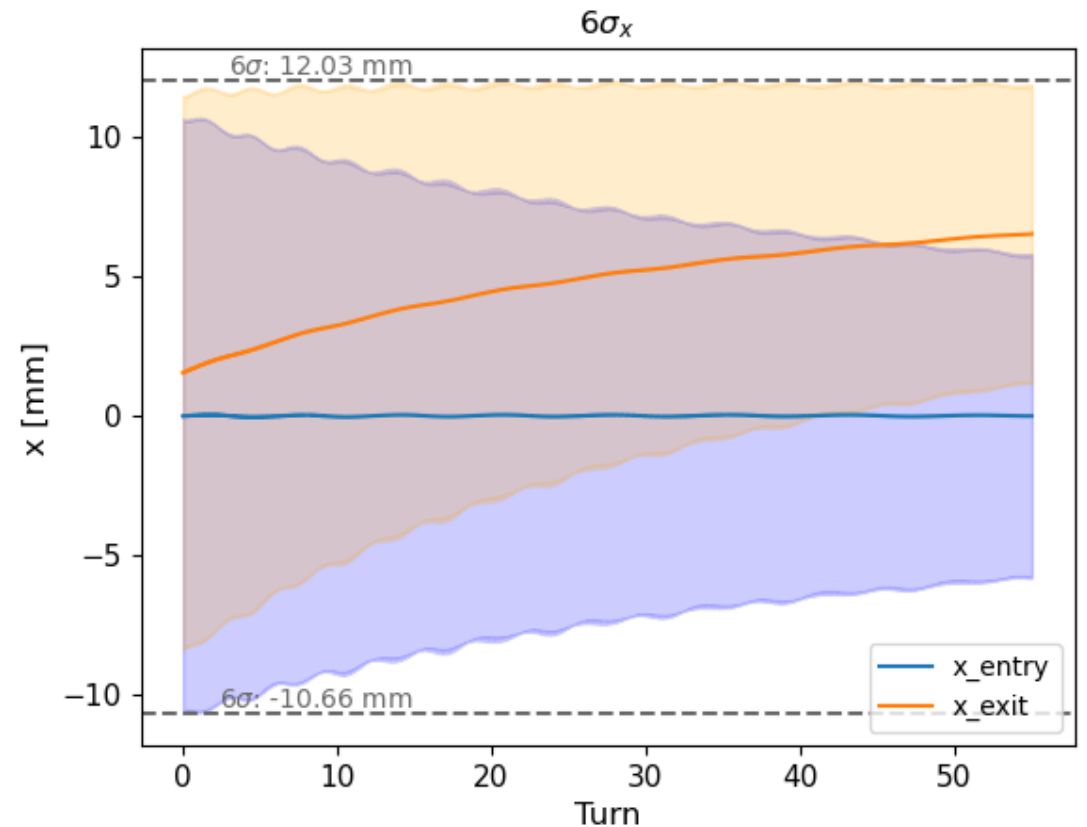
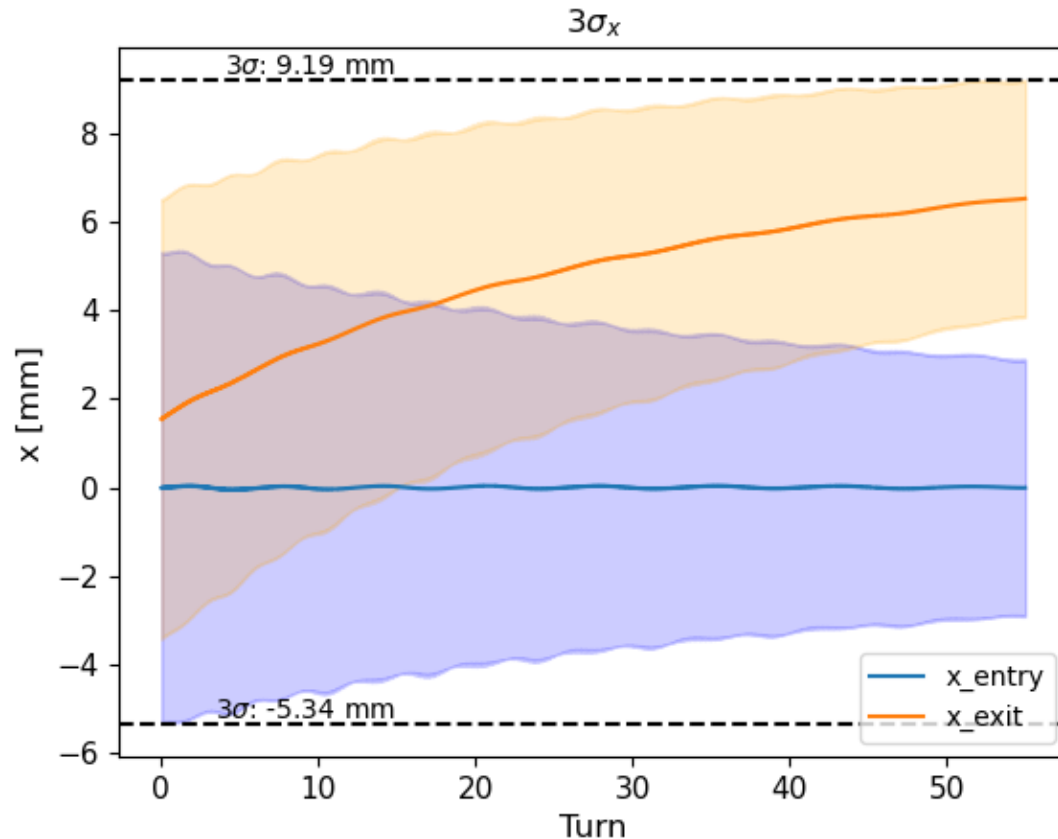


- Estimate the good field region: take into account the excursion of trajectories and the effect of optics
- Choose the reference trajectory
- Tracking in a dipole where  $\beta$  and  $D$  are maxima, so we get the « larger beam size » :

$$\sigma_x = \sqrt{\epsilon_x \beta_x + D_x^2 \sigma_\delta^2}$$

- No errors

# GFR: Horizontal plane x



Horizontal plane  $\sigma_x$

- $3\sigma$  : ~ 15 mm width
- $6\sigma$  : ~ 23 mm width

About 20 mm horizontal width for the good field region should be enough → not a lot of travelling in the outer side of GFR

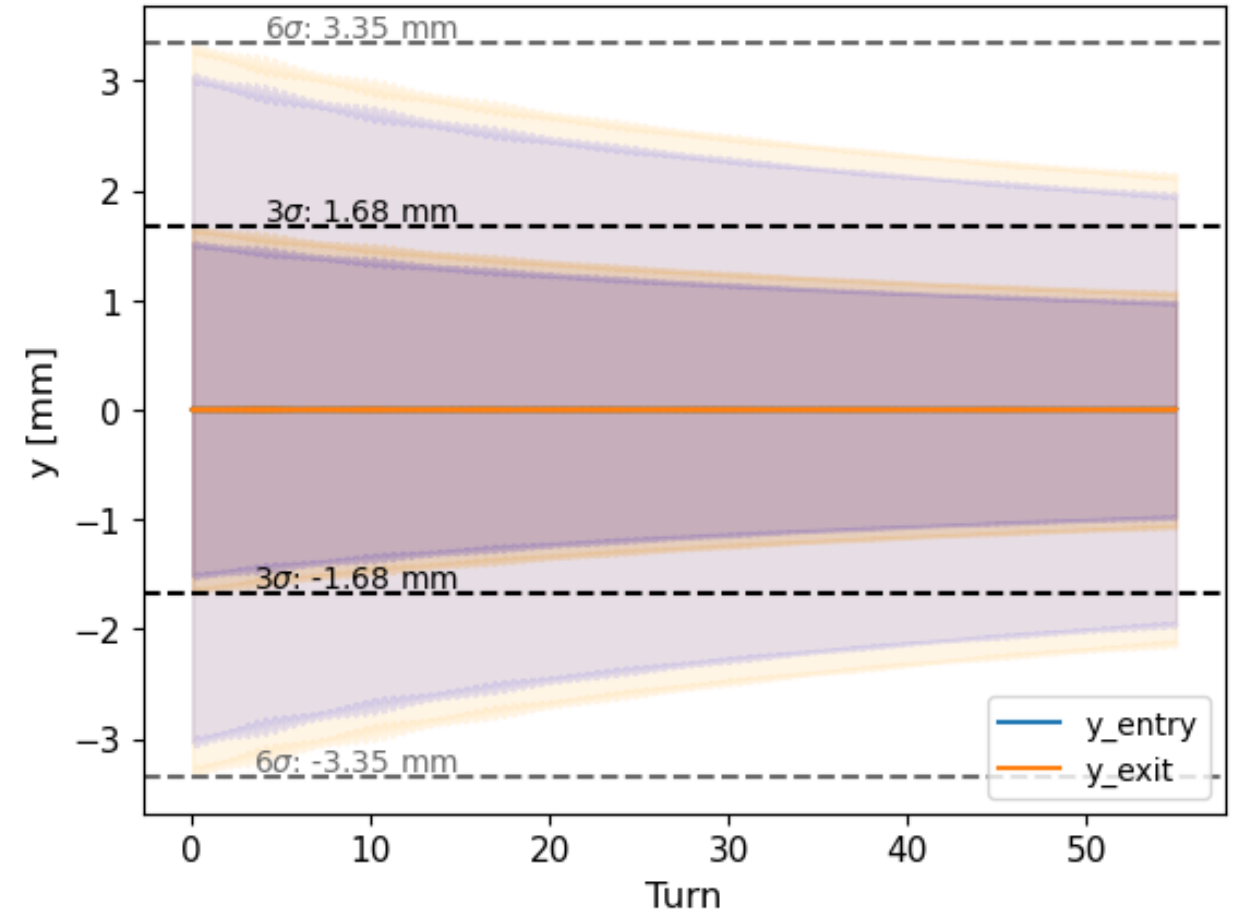


# GFR: Vertical plane y

Vertical plane  $\sigma_y$

- $3\sigma$  : ~ 3 mm width
- $6\sigma$  : ~ 7 mm width
- No excursion of the trajectory in the vertical plane : much smaller region

**GFR x : ~ 20 mm**  
**GFR y: much less needed**



# Conclusions and perspectives

- First tracking studies conducted
- Impact of preliminary optics and RF tuning
- Tracking integrating systematic errors b3/b5 from dipole designs
  - Have an idea of which designs could be used
- Get a rough idea of the width of the GFR with tracking studies
  
- What's next ?
  - Work on optics
  - Add misalignment/roll errors and random errors (jitters) on dipoles
  - Include passive correction schemes



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