



UNIVERSITY  
*of York*

# Lifetime measurements in $^{53}\text{Ca}$

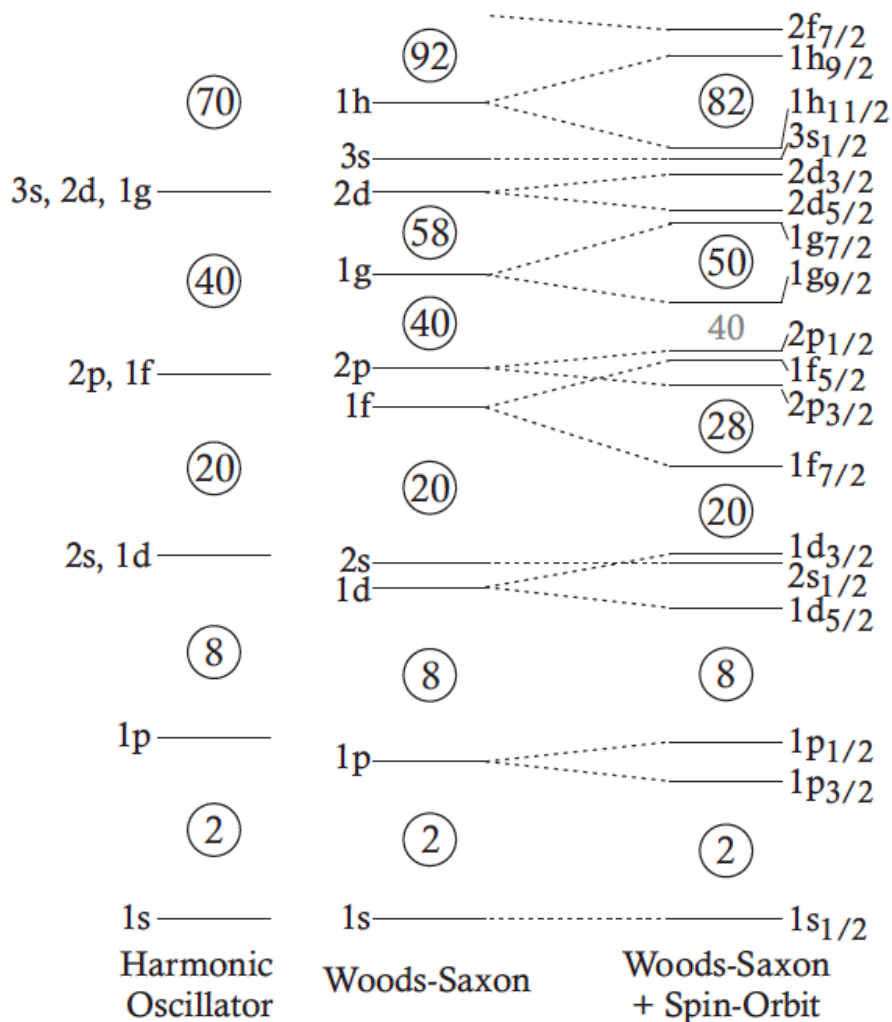
**S. Chen**

on behalf of the HiCARI collaboration  
and the RIBF-170 collaboration

University of York

Liverpool, 10<sup>th</sup> April 2024

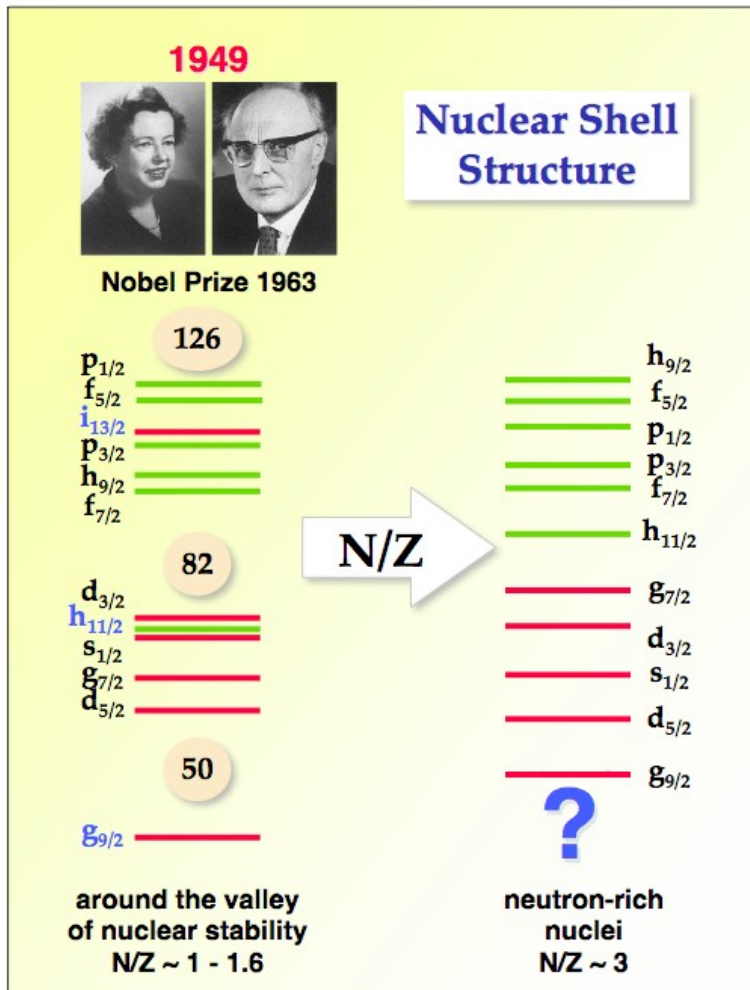
# Shell structures and nuclear forces



Maria Goeppert-Mayer  
& Hans D. Jensen  
1963

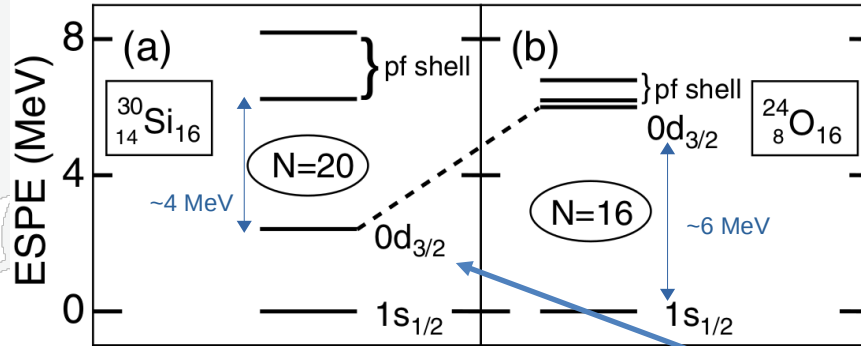
Maria Goeppert-Mayer, Phys. Rev. **75**, 1969 (1949)  
O. Haxel, Phys. Rev. **75**, 1766 (1949)

# Shell structures and nuclear forces

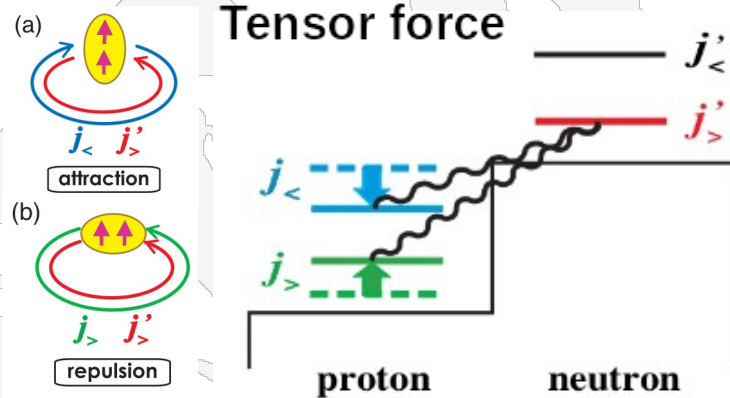


- Shell structure and magic numbers were the cornerstones of the shell model for many decades
- Experiments on exotic nuclei found magic numbers are not immutable throughout the nuclear chart
- Shell structure is now recognized as local concept

# Shell structures and nuclear forces



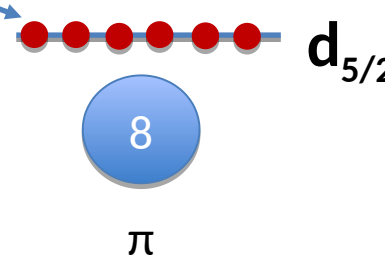
T. Otsuka et al., Phys. Rev. Lett. **87**, 082502 (2001)



T. Otsuka et al., Phys. Rev. Lett. **95**, 232502 (2005)

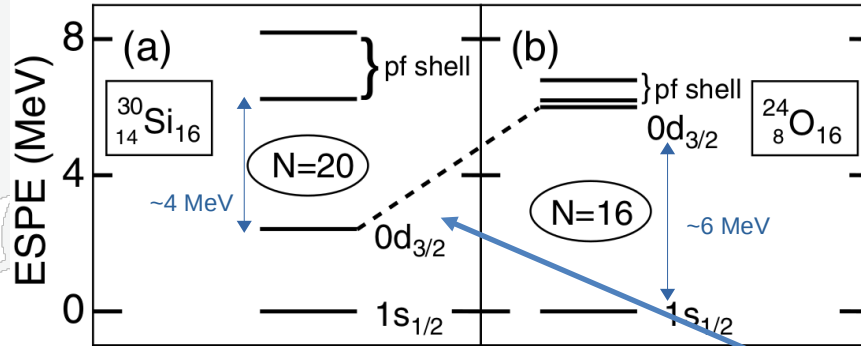
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	25Ne	26Ne	27Ne
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		22C	

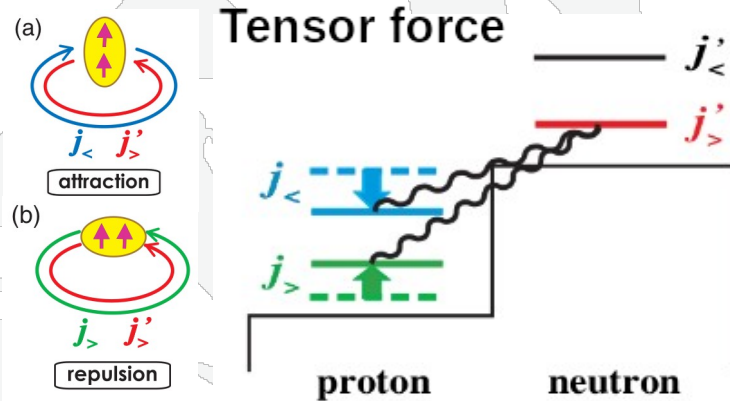


$^{30}\text{Si} \rightarrow ^{24}\text{O}$ : absence of strong  $\pi 0d_{5/2} - \nu 0d_{3/2}$  attraction  
 $\Rightarrow N = 16$  new magic number in oxygen

# Shell structures and nuclear forces



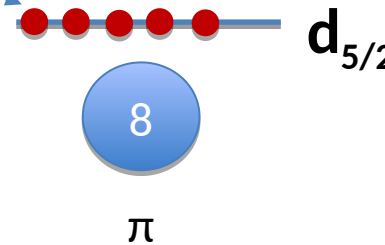
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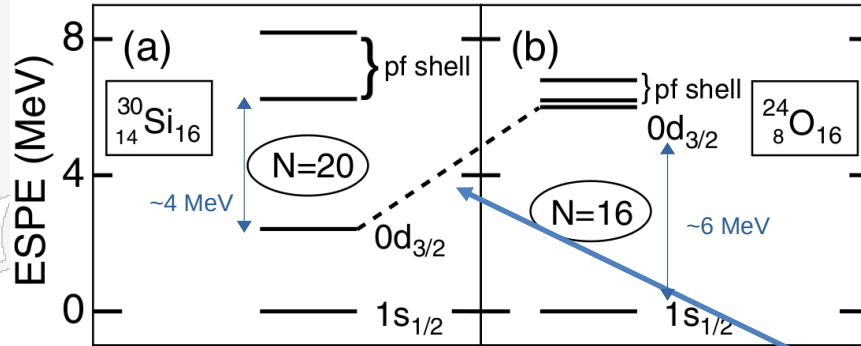
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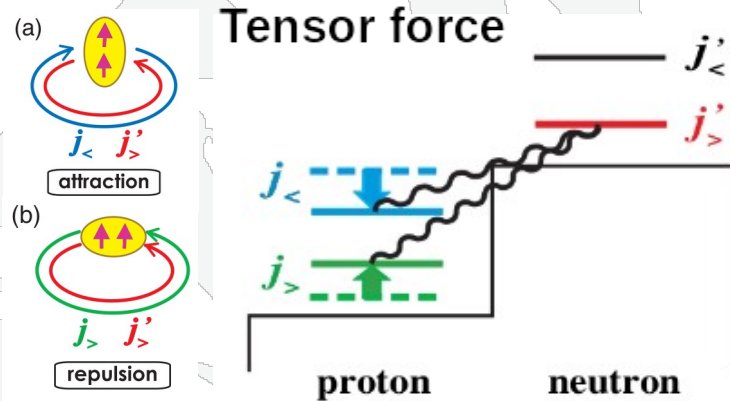


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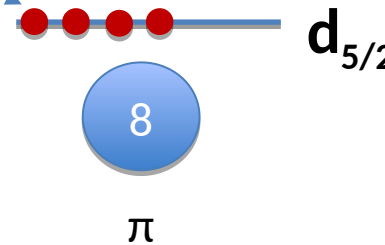
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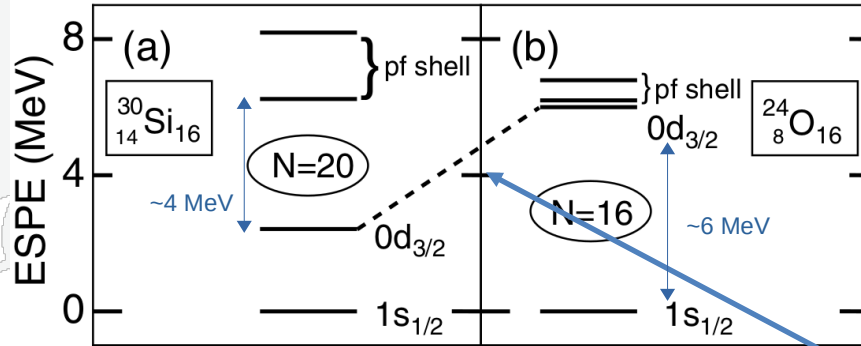
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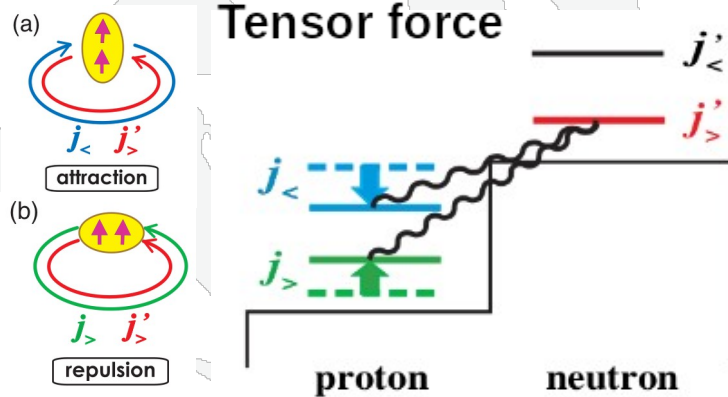


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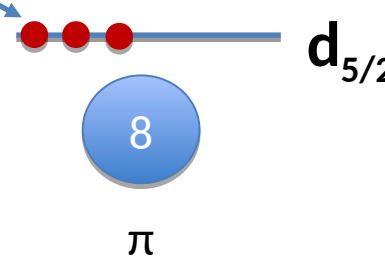
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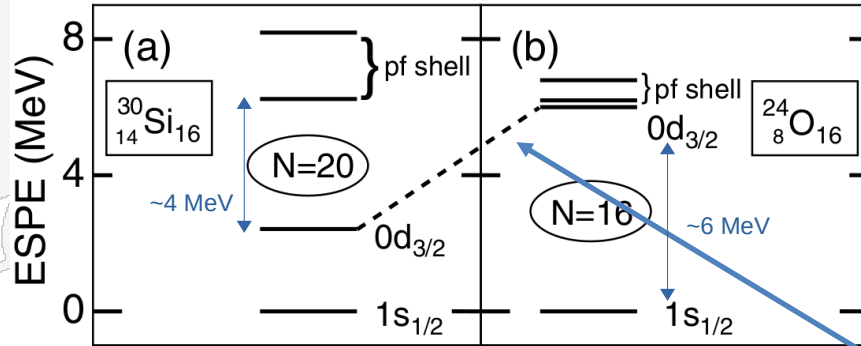
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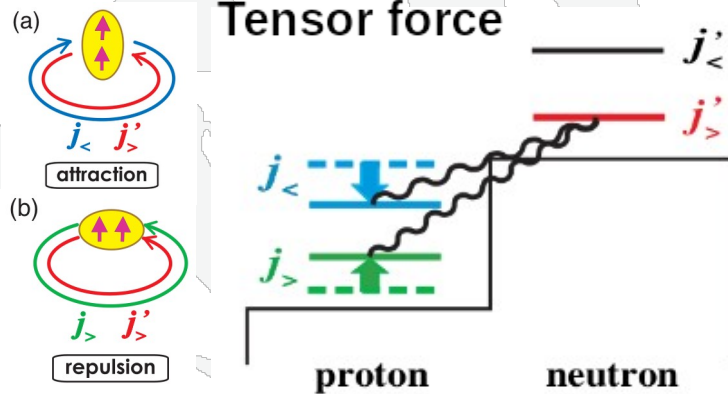


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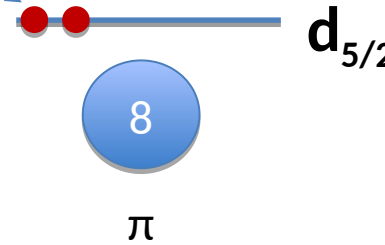


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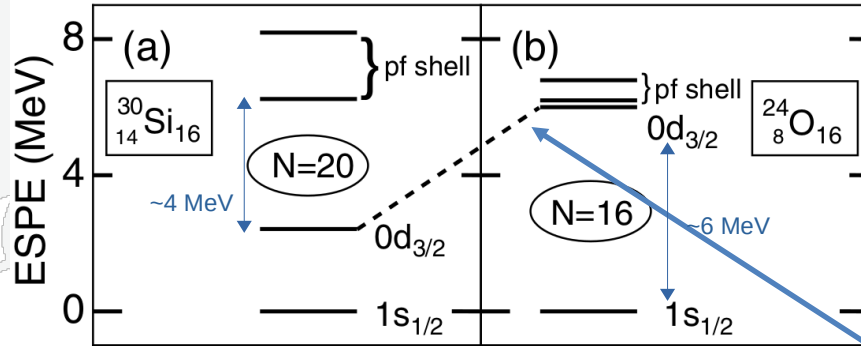
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	$^{31}\text{S}$	$^{32}\text{S}$	$^{33}\text{S}$
	$^{30}\text{P}$	$^{31}\text{P}$	$^{32}\text{P}$
	$^{29}\text{Si}$	$^{30}\text{Si}$	$^{31}\text{Si}$
	$^{28}\text{Al}$	$^{29}\text{Al}$	$^{30}\text{Al}$
	$^{27}\text{Mg}$	$^{28}\text{Mg}$	$^{29}\text{Mg}$
	$^{26}\text{Na}$	$^{27}\text{Na}$	$^{28}\text{Na}$
	$^{25}\text{Ne}$	$^{26}\text{Ne}$	$^{27}\text{Ne}$
	$^{24}\text{F}$	$^{25}\text{F}$	$^{26}\text{F}$
	$^{23}\text{O}$	$^{24}\text{O}$	$^{25}\text{O}$
	$^{22}\text{N}$	$^{23}\text{N}$	$^{24}\text{N}$
		$^{22}\text{C}$	

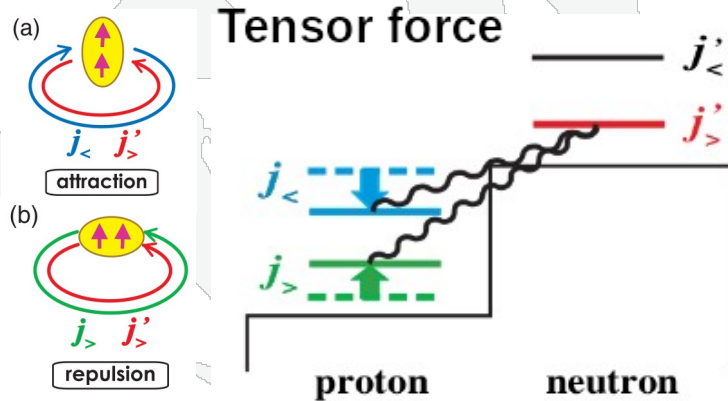




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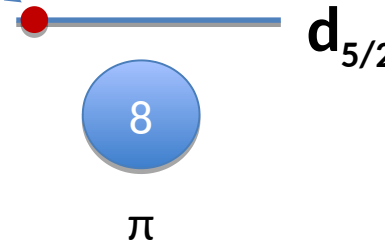
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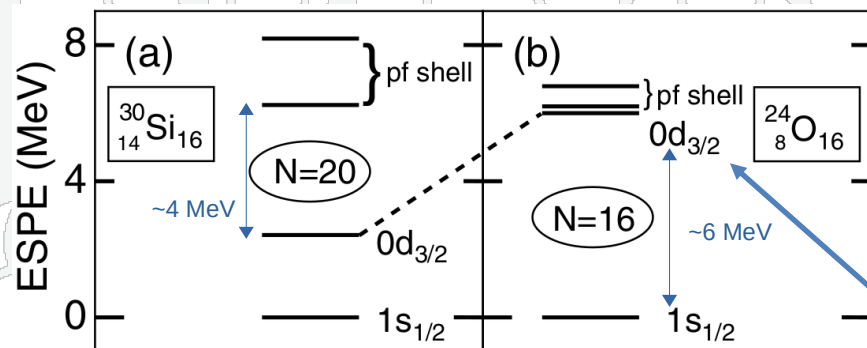
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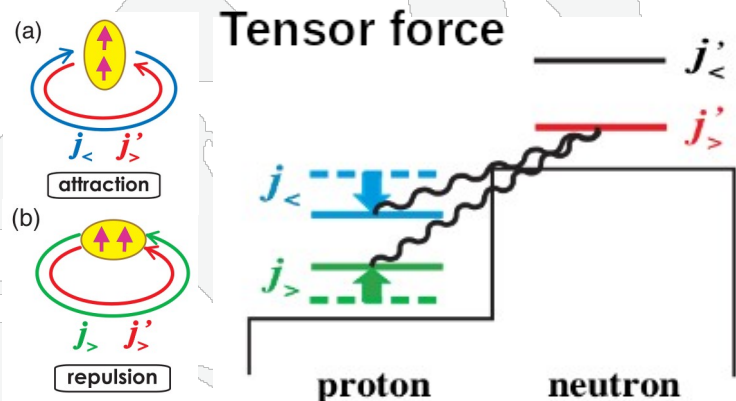


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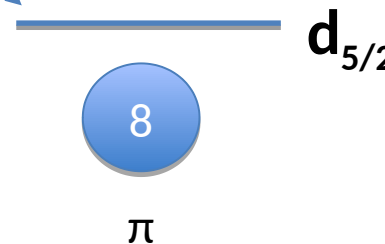
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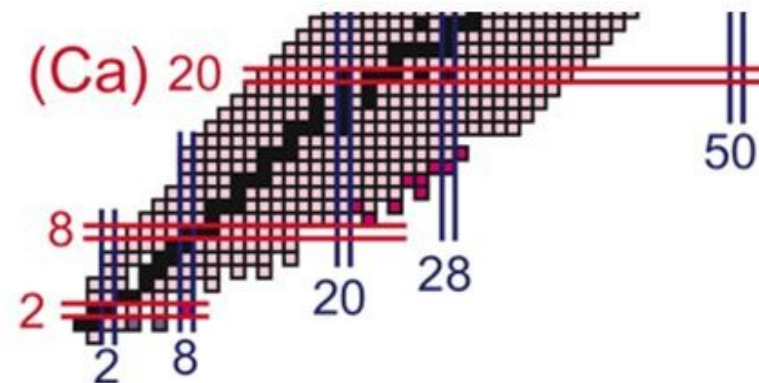
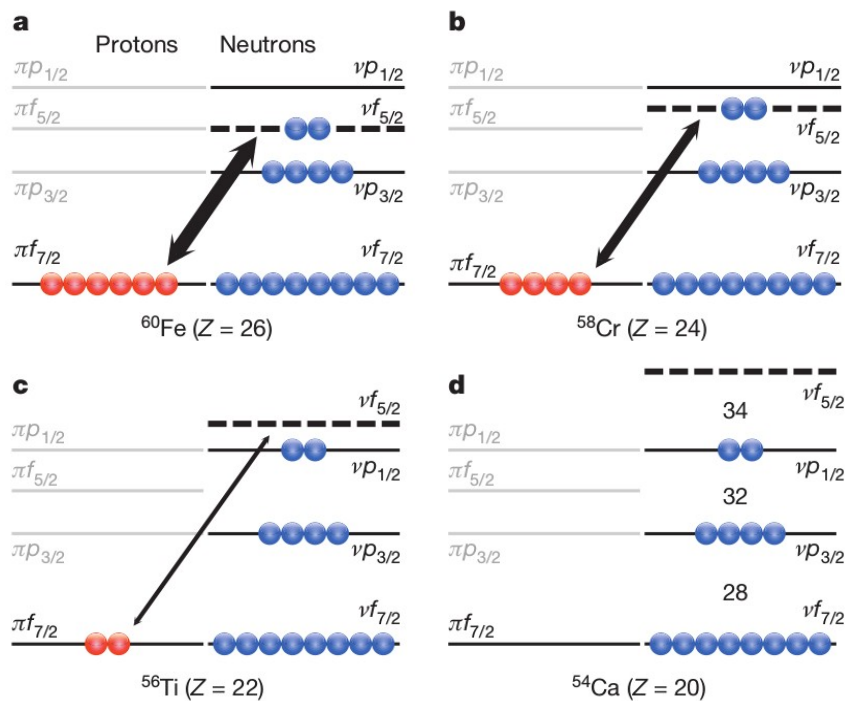


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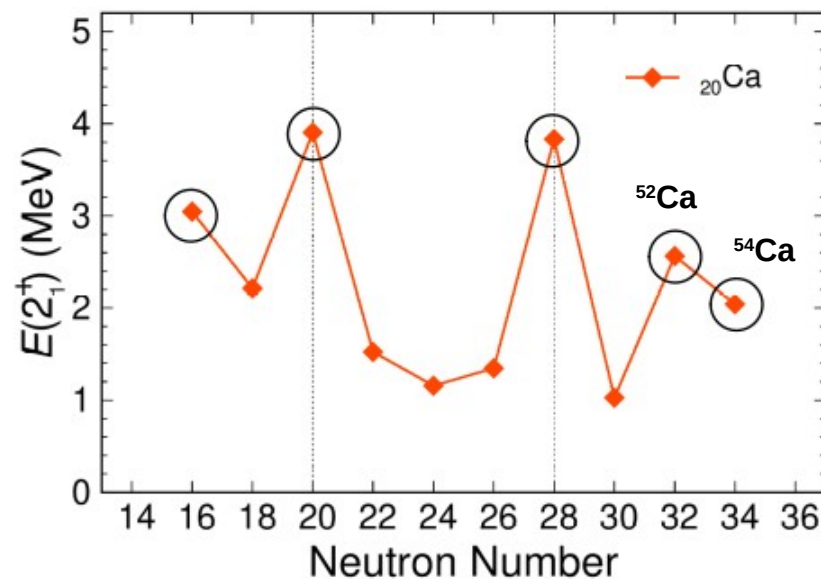
# N = 32,34 shell closure in Ca isotopes



D. Steppenbeck *et al.*, Nature **502**,207-10 (2013)



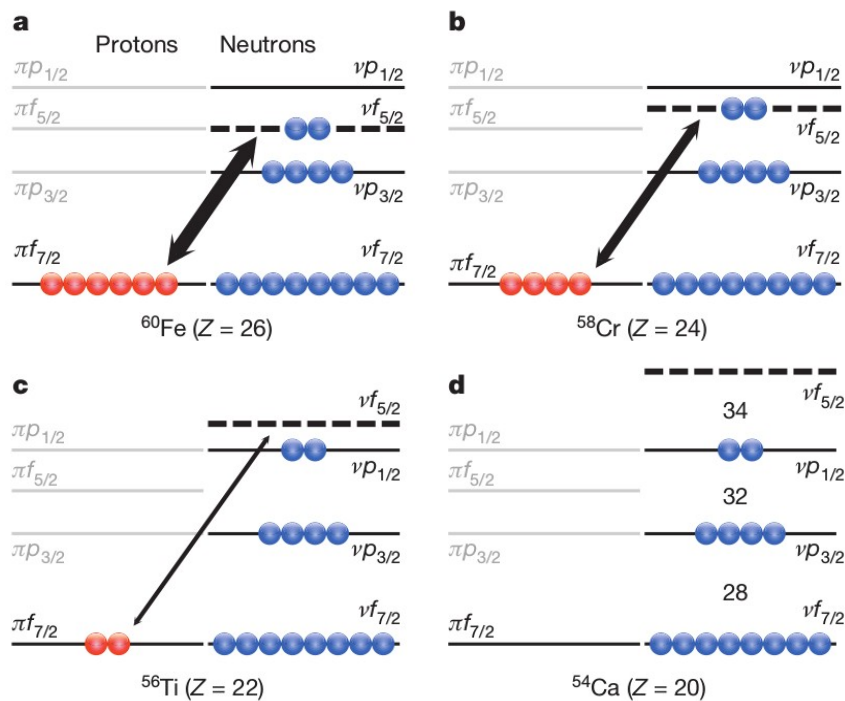
(sub-)shell closure at N = 16, 20, 28, 32, 34



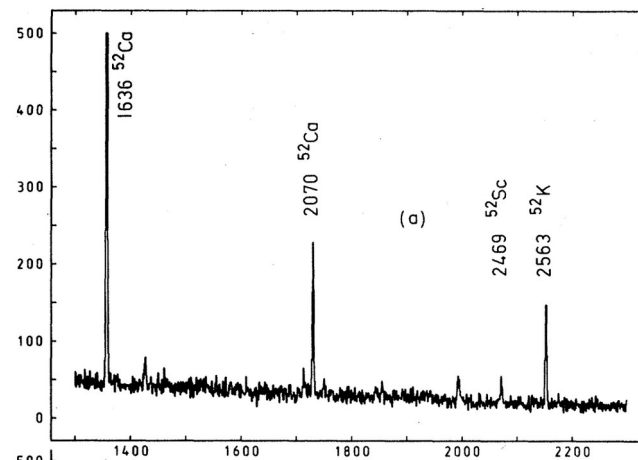
- Absence of strong  $\pi f_{7/2} - \nu f_{5/2}$  attraction make N = 32,34 new magic number in calcium

# $N = 32$ shell closure in $^{52}\text{Ca}$

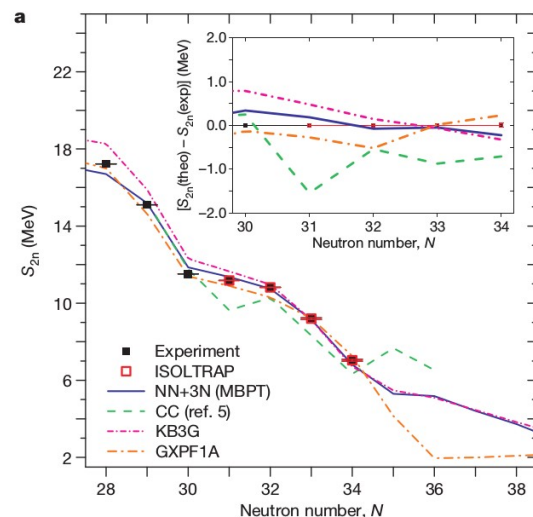
D. Steppenbeck *et al.*, Nature **502**,207-10 (2013)



A. Huck *et al.*, Phys. Rev. C **31**,2226-2237 (1985)



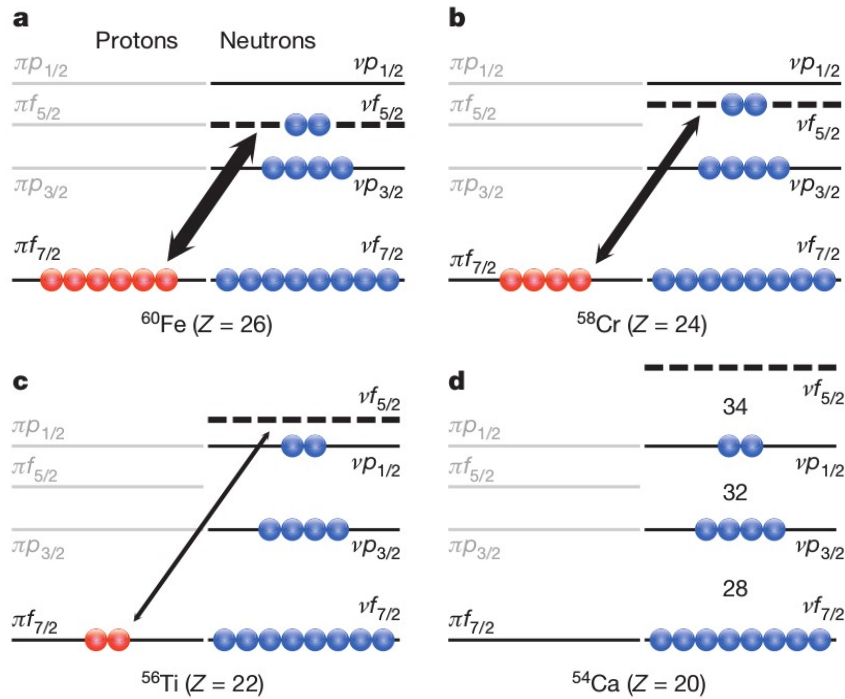
F. Wienholtz *et al.*, Nature **498**, 346-349 (2013)



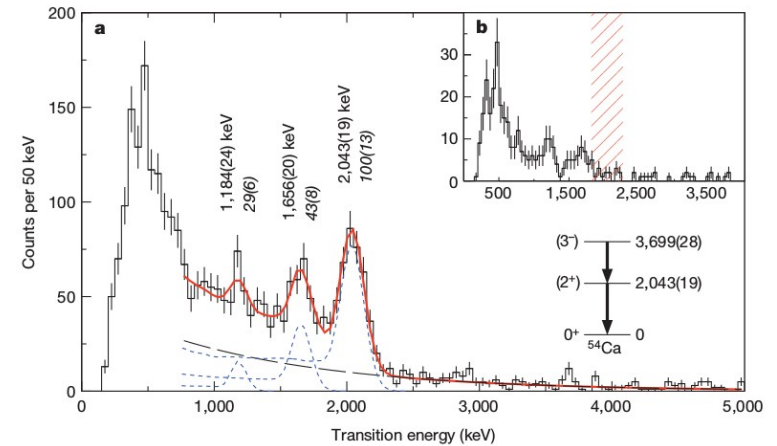
- Absence of strong  $\pi f_{7/2} - \nu f_{5/2}$  attraction make  $N = 32, 34$  new magic number in calcium
- Experimental evidences for  $N = 32$  magic
  - Large  $E(2^+_1)$
  - Mass measurement: large empirical two-neutron shell gap

# N = 34 shell closure in $^{54}\text{Ca}$

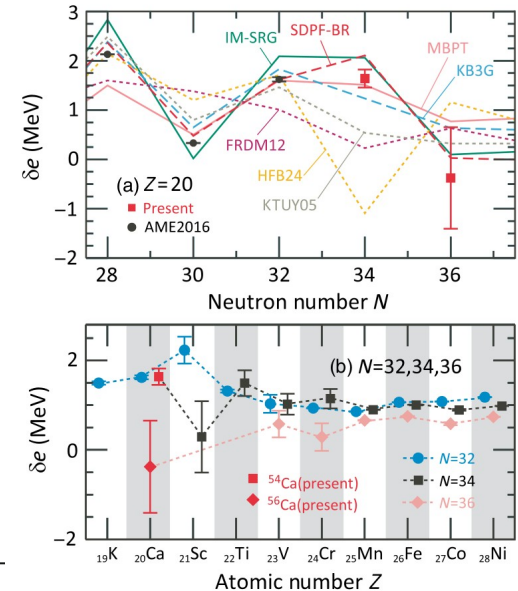
D. Steppenbeck *et al.*, Nature **502**,207-10 (2013)



D. Steppenbeck *et al.*, Nature **502**,207-10 (2013)



S. Michimasa *et al.*, Phys. Rev. Lett. **121**, 022506 (2018)

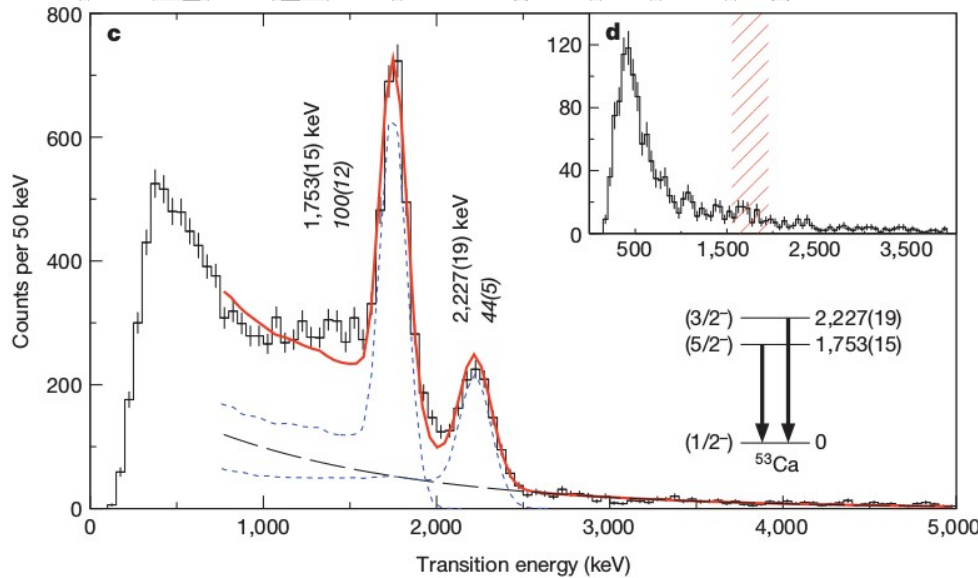


- Absence of strong  $\pi f_{7/2} - \nu f_{5/2}$  attraction make  $N = 32, 34$  new magic number in calcium
- Experimental evidences for  $N = 34$  magic
  - $E(2^+_1)$ : first evidence of magicity
  - Mass measurement:  $N = 34$  shell gap similar size with  $N = 32$  shell gap

# Excitation of $^{53}\text{Ca}$



D. Steppenbeck *et al.*, Nature **502**,207-10 (2013)



$E_x = 2220$  keV via  $\beta$ -decay,

F. Perrot *et al.* PRC **74**,014313 (2006)

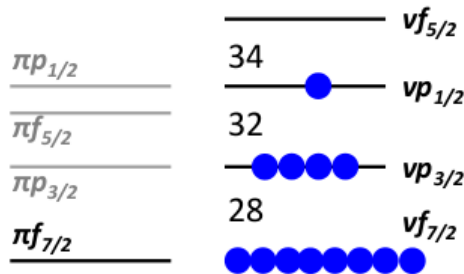
S. Chen *et al.*, PRL **123**,142501 (2019)

State	Energy (keV)	GXPf1Bs	NNLOsat	NN+3N (Inl)
3/2-	2220(13)	2061	2635	2611
5/2-	1738(17)	1934	1950	2590

## Lifetime measurements:

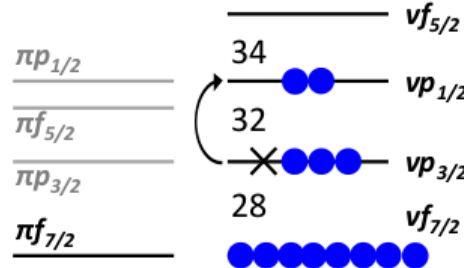
- E2 transition probability
- Benchmarks to test different theoretical descriptions beyond excitation energies

g.s. (1/2-)



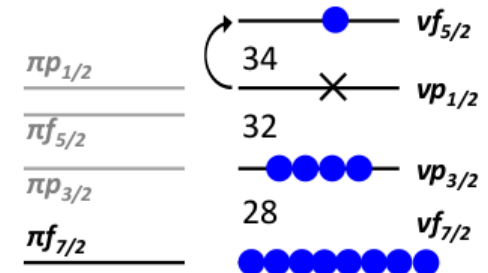
$^{53}\text{Ca}$  (Z=20)

2220 keV (3/2-)



$^{53}\text{Ca}$  (Z=20)

1753 keV (5/2-)



$^{53}\text{Ca}$  (Z=20)

# Lifetime measurement method

- Detect prompt gamma rays from fast moving ( $\sim 0.5c$ ) particles
- Doppler correction for prompt gamma

$$E_{\gamma 0} = E_{\gamma} \frac{1 - \beta \cos \theta}{\sqrt{1 - \beta^2}}$$

- Finite excitation state lifetime lead to  $\theta$  and  $\beta$  distribution different from zero lifetime

==> asymmetric peak shape after  
Doppler-correction

- Peak shape analysis to extract excitation state lifetime

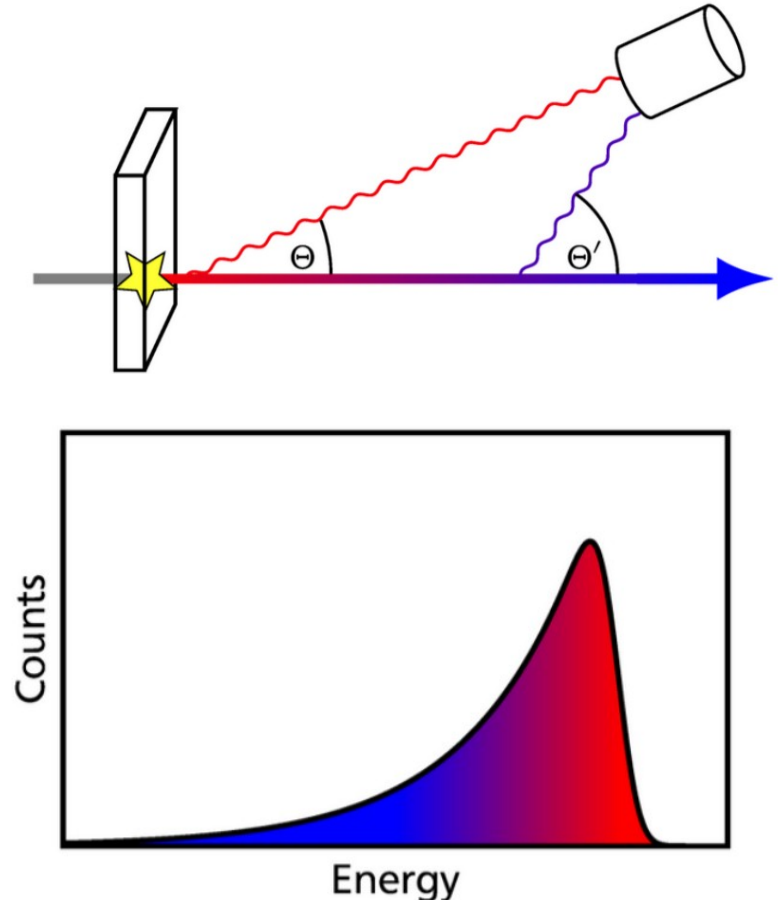


Figure: Schematic diagram of lifetime measurement method (Thesis, S. Heil, 2019)

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- Peak shape analysis to extract excitation state lifetime

==> complicated lifetime responses,  
need compare with detailed simulations

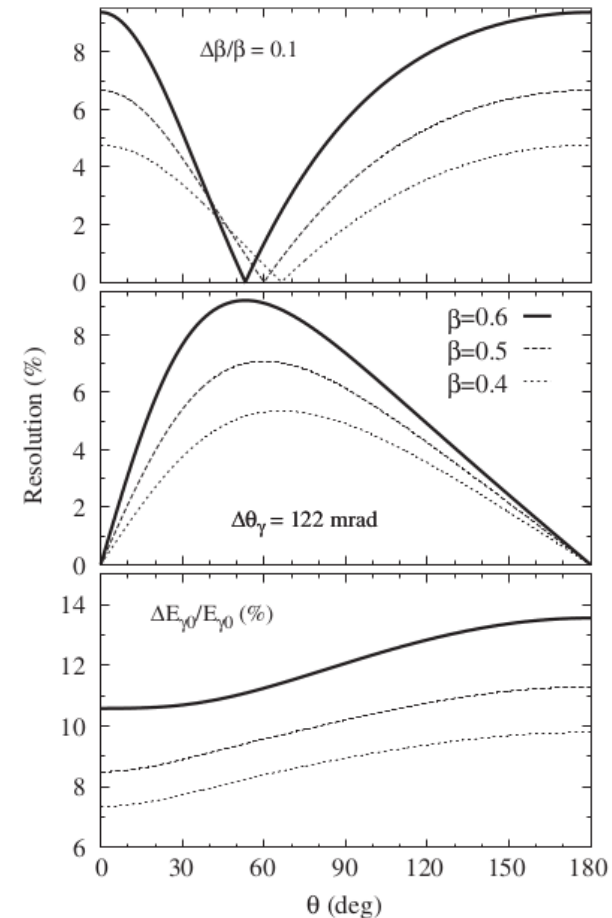
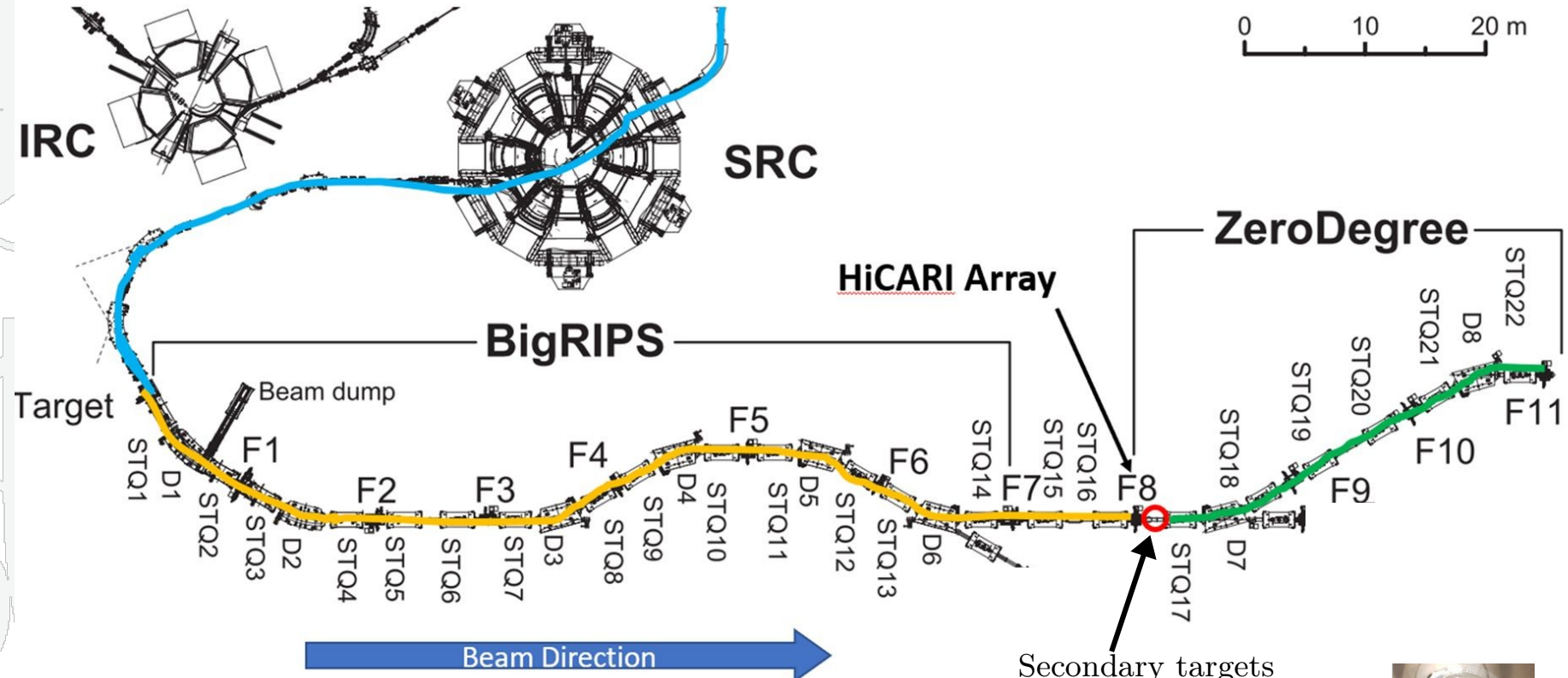


Figure: Doppler broadening as a function of gamma-emission angle (P. Doornenbal, PTEP **2012**, 03C004)



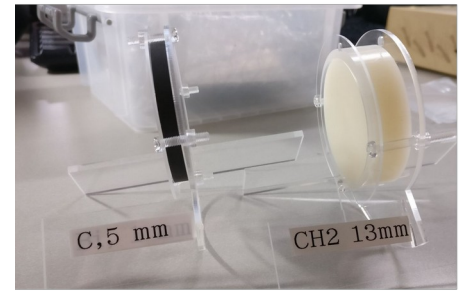
# Experiment Setup at RIBF

0 10 20 m



- █ Primary Beam: 70 Zn Beam on Be target 354MeV/u
- █ Secondary Beam: Tuned to Sc isotopes
- █ Tertiary Beam: Tuned to Ca isotopes 220 MeV/u

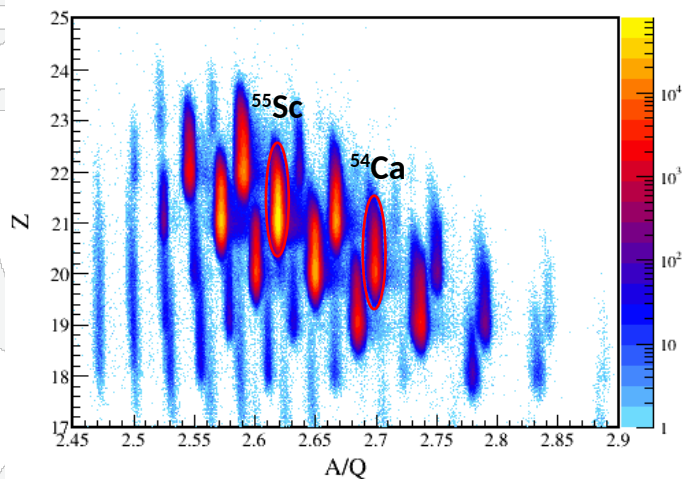
Secondary targets



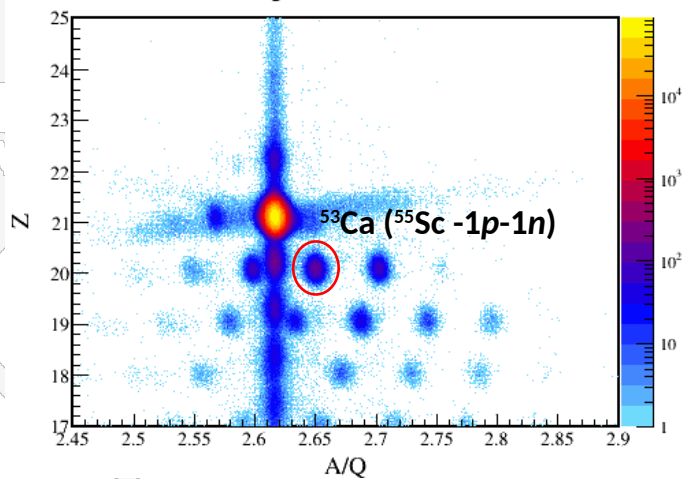
# Particle Identification

neutron-rich Ca setting

BigRIPS PID

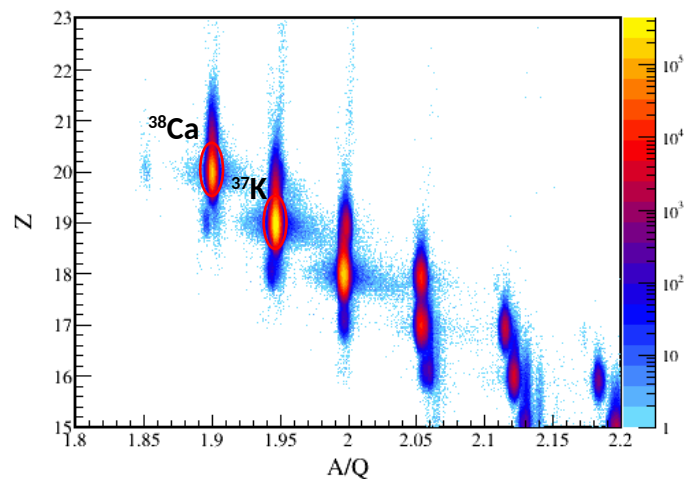


ZeroDegree PID of  $^{55}\text{Sc}$  beam

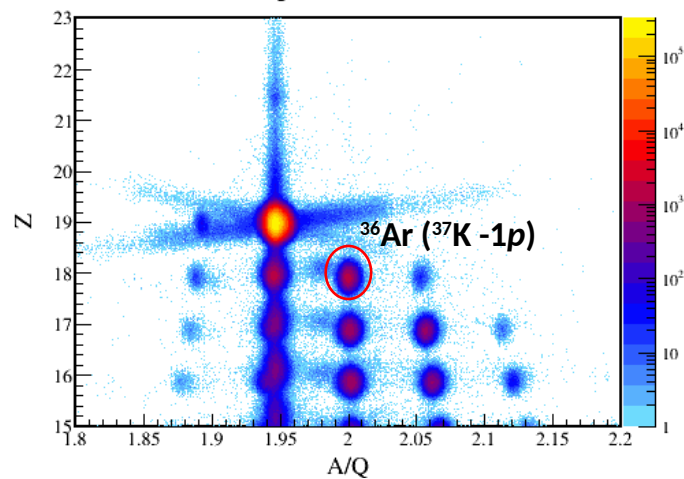


proton-rich Ca setting

BigRIPS PID



ZeroDegree PID of  $^{37}\text{K}$  beam



# Experiment Setup - HiCARI

- High-resolution Cluster Array at the RIBF (RIKEN Accel. Prog., (2021), K. Wimmer, et. al.)
- Hybrid HPGe array:
  - 6 x Miniball cluster (6 segments)
  - 4 x SuperClover cluster (4 segments)
  - 1 x Gretina Quad cluster (position sensitive)
  - 1 x Gretina P3 cluster (position sensitive)

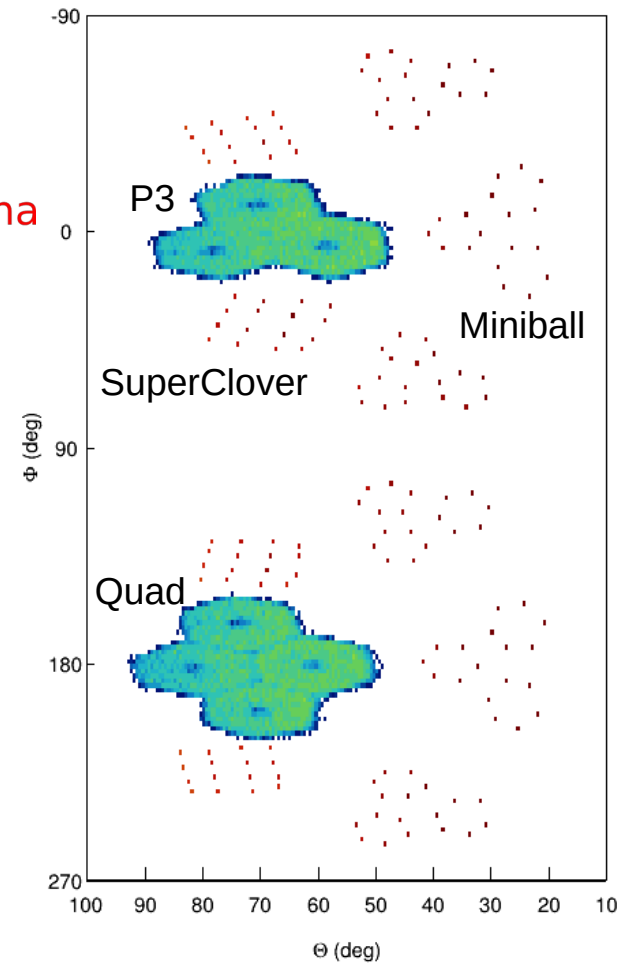
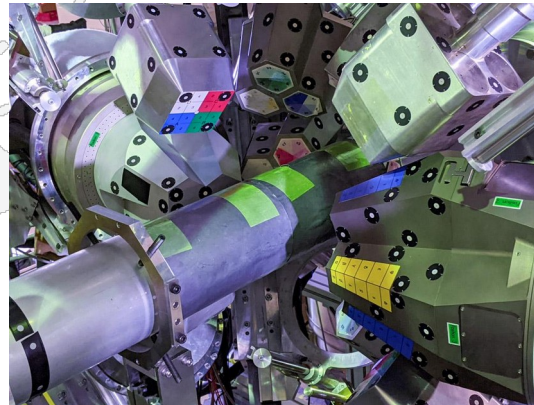
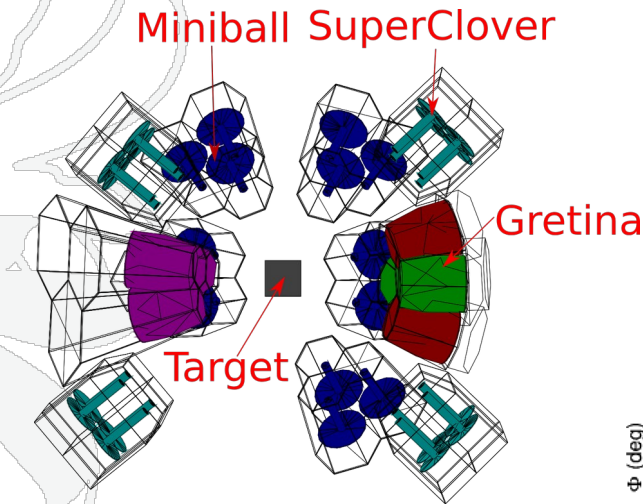
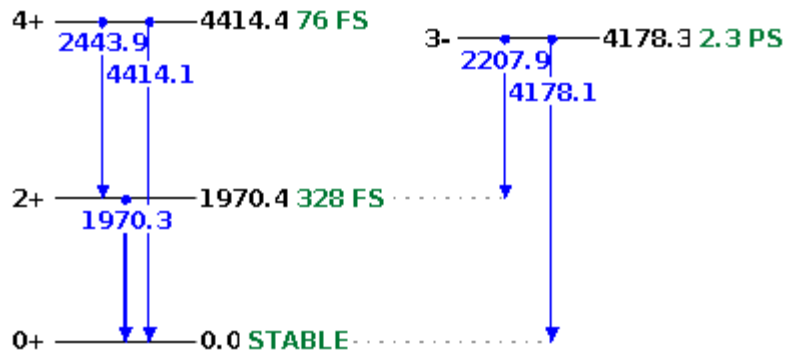


Figure: HiCARI array

# Benchmark – $^{36}\text{Ar}$ from $^{37}\text{K} - 1p$

$^{36}\text{Ar}$  low-lying excitation states from NNDC



- Spectra of CH2 target have worse energy resolutions, due to large  $\beta$  uncertainty
- $^{36}\text{Ar}$  low-lying excitation states: known energy and lifetime  
==> Benchmark Geant4 simulations

Spectra of  $^{37}\text{K}(\text{C},\text{X})^{36}\text{Ar}$

Spectra of  $^{37}\text{K}(\text{CH}_2,\text{X})^{36}\text{Ar}$

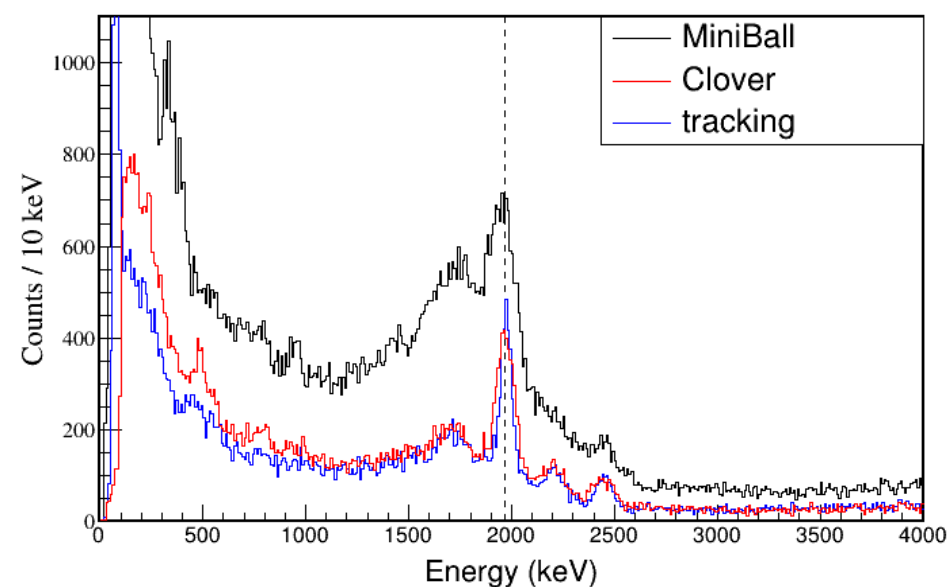
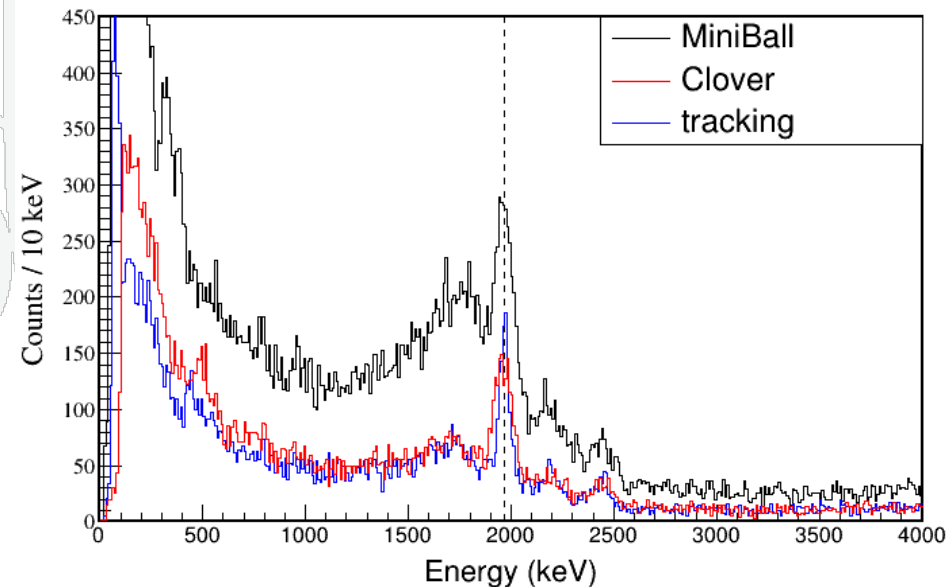
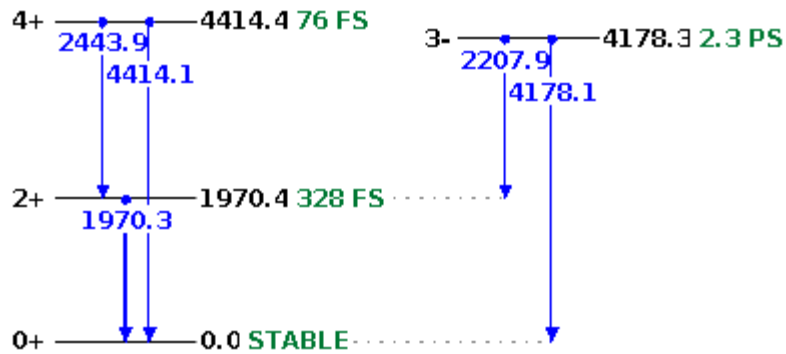


Figure: Doppler-corrected gamma-ray energy spectra

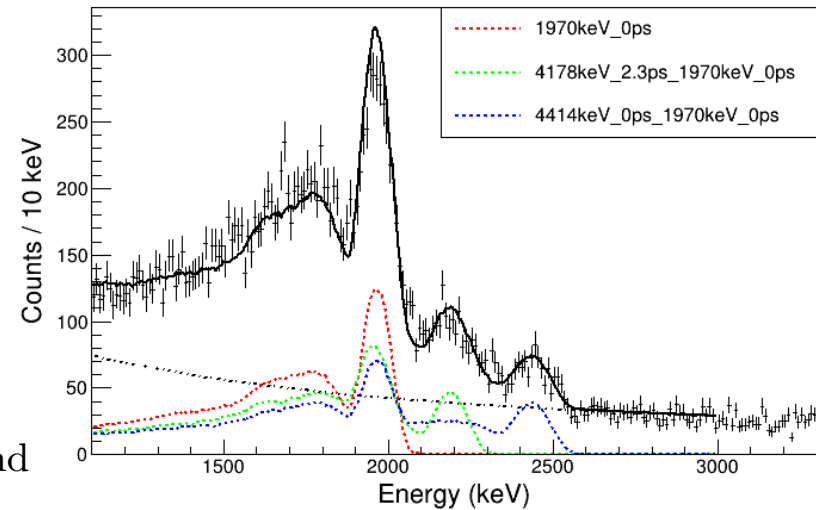
# Benchmark – $^{36}\text{Ar}$ from $^{37}\text{K} - 1p$

$^{36}\text{Ar}$  low-lying excitation states from NNDC

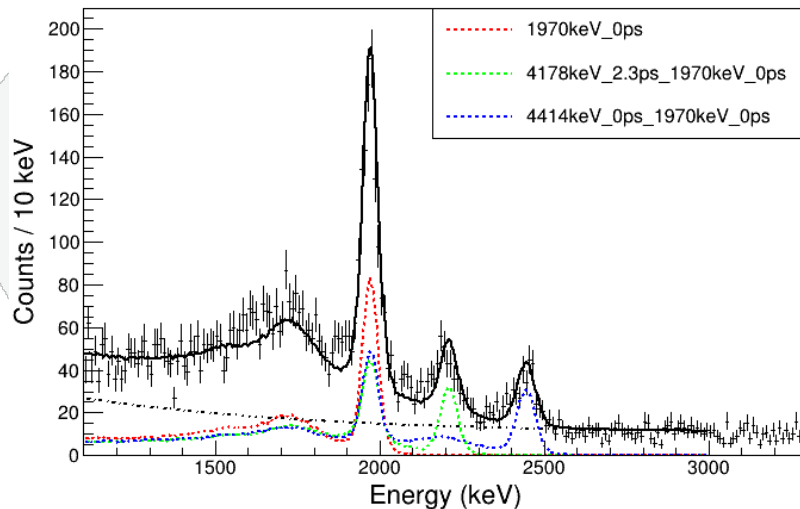


- Fitting function:  
Geant4 simulations + double-expo background

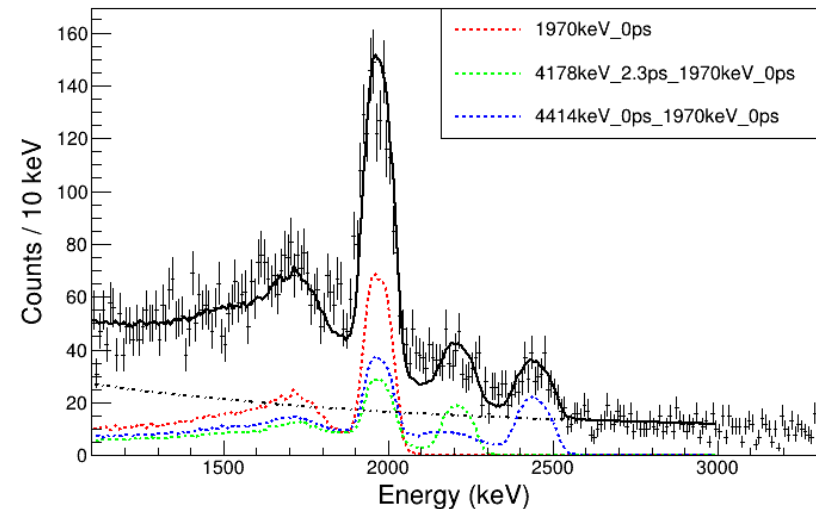
Spectra of  $^{37}\text{K}(\text{C},\text{X})^{36}\text{Ar}$  {MiniBall}



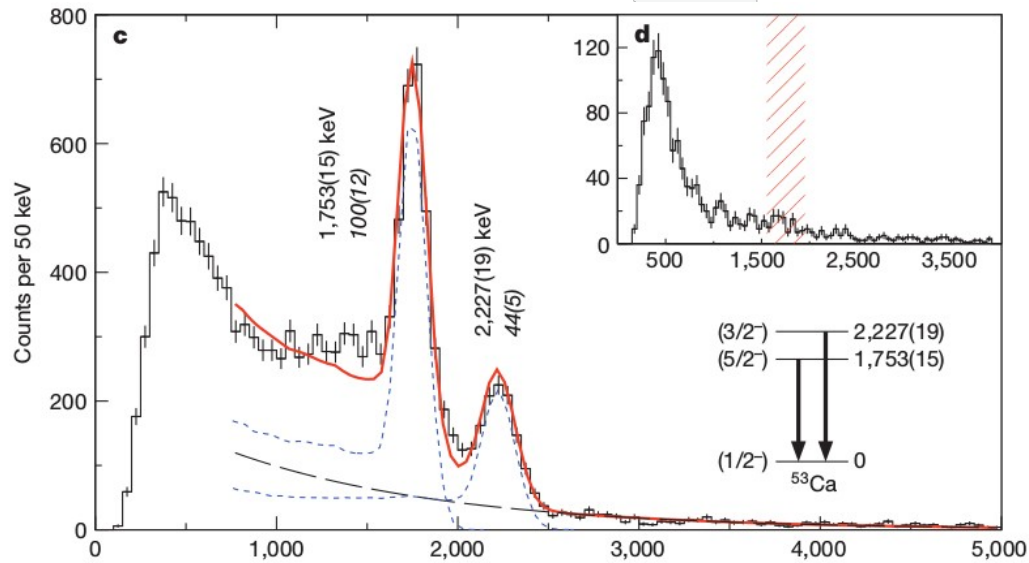
Spectra of  $^{37}\text{K}(\text{C},\text{X})^{36}\text{Ar}$  {tracking}



Spectra of  $^{37}\text{K}(\text{C},\text{X})^{36}\text{Ar}$  {Clover}



# $^{53}\text{Ca}$ from $^{55}\text{Sc} - 1p1n$

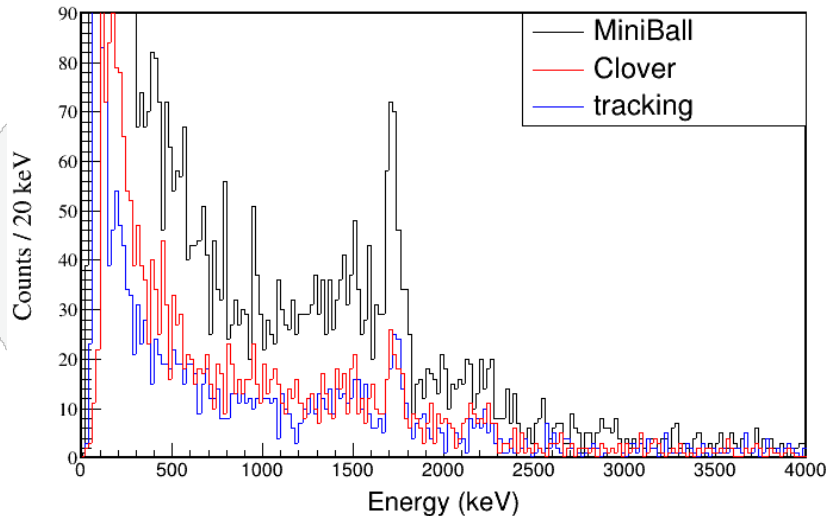


## Previous measurement:

Gamma-ray spectra measured with NaI(Tl) detectors

D. Steppenbeck *et al.*, Nature  
**502**,207-10 (2013)

Spectra of  $^{55}\text{Sc}(\text{C},\text{X})^{53}\text{Ca}$



Spectra of  $^{55}\text{Sc}(\text{CH}_2,\text{X})^{53}\text{Ca}$

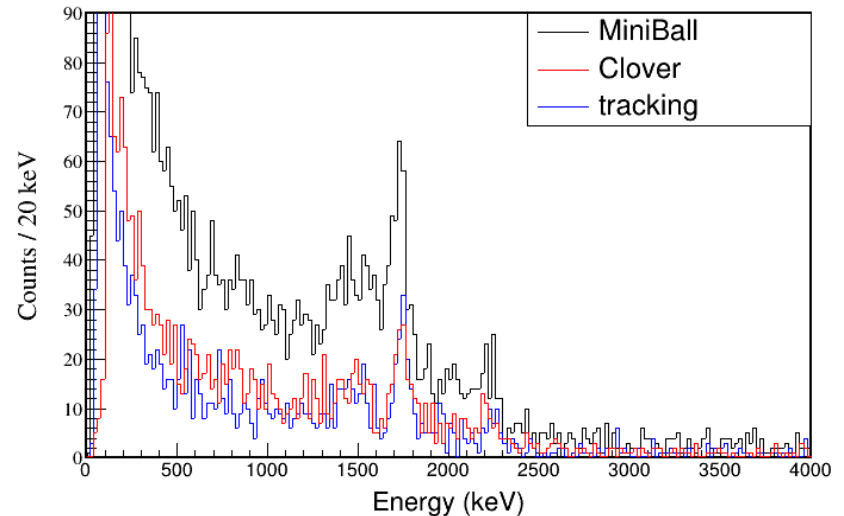
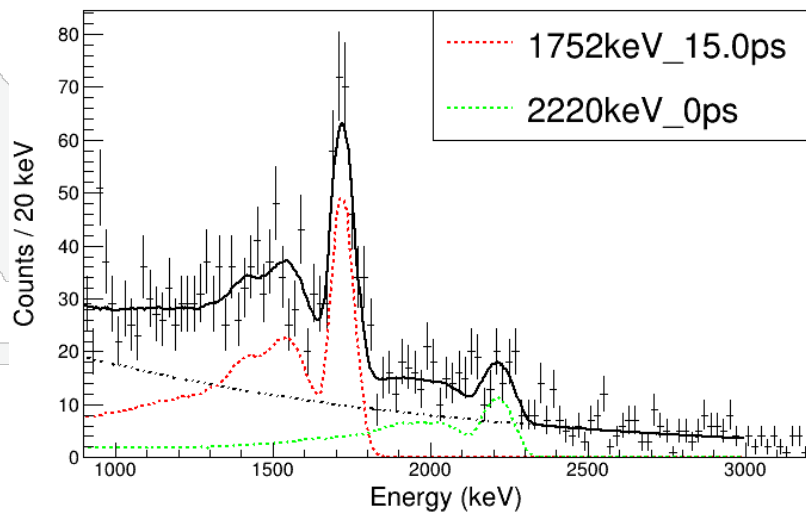


Figure: Doppler-corrected gamma-ray energy spectra

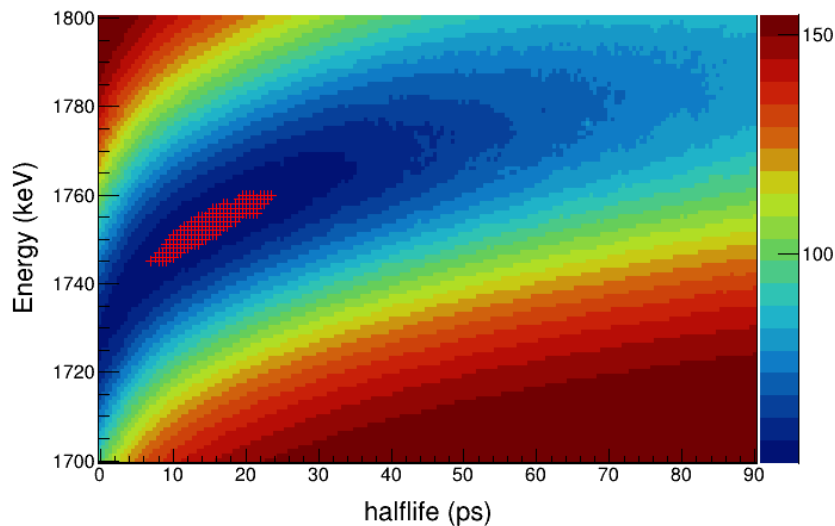
# $^{53}\text{Ca}$ from $^{55}\text{Sc} - 1p1n$



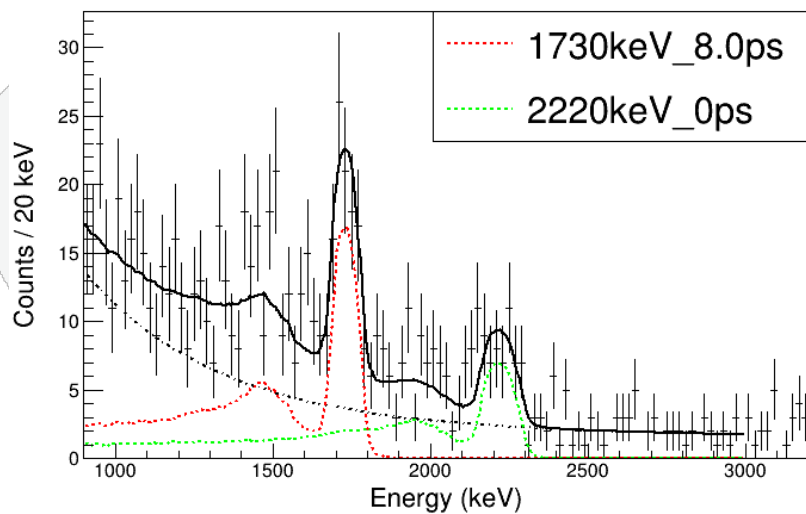
Spectra of  $^{55}\text{Sc}(C,X)^{53}\text{Ca}$  {MiniBall}



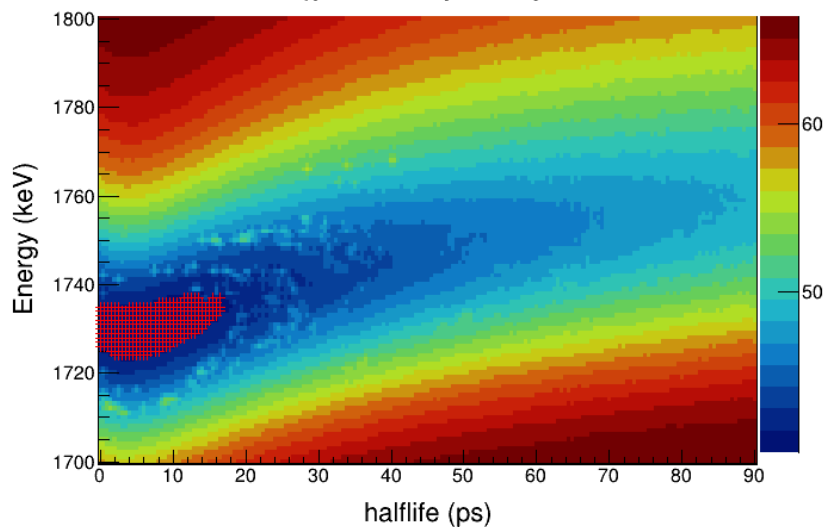
$\chi^2$  surface {Miniball}



Spectra of  $^{55}\text{Sc}(C,X)^{53}\text{Ca}$  {Clover}



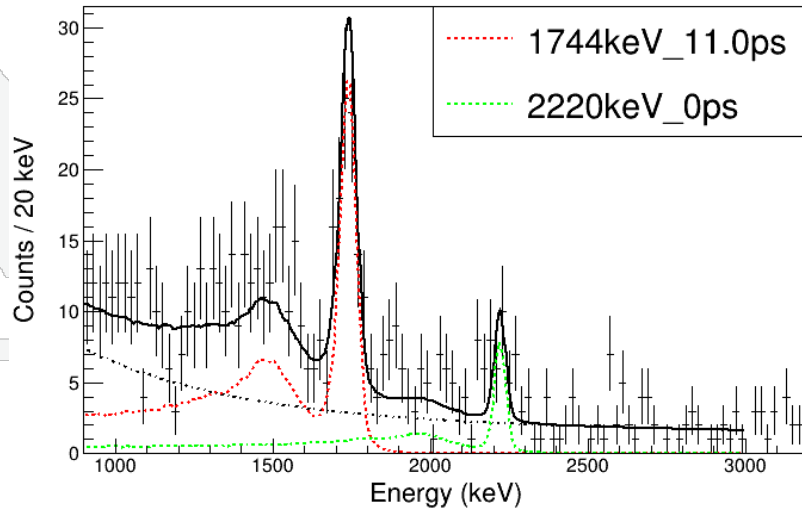
$\chi^2$  surface {Clover}



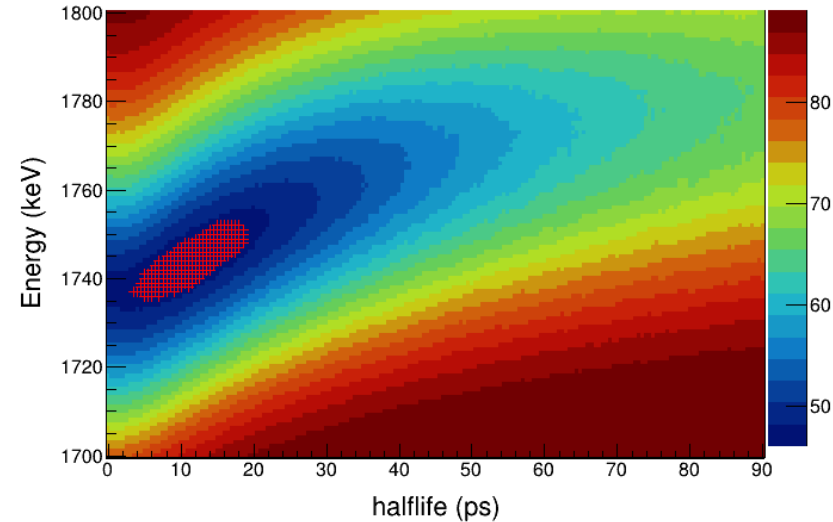
# $^{53}\text{Ca}$ from $^{55}\text{Sc} - 1p1n$



Spectra of  $^{55}\text{Sc}(C,X)^{53}\text{Ca}$  {tracking}



$\chi^2$  surface {tracking}



## Preliminary results:

	Energy / keV	Half-life / ps
Miniball	1752(8)	15(8)
Clover	1730(6)	8(8)
tracking	1744(8)	11(8)
weighted	1740(4)	11(5)

- only statistic uncertainties are considered
- weighted by  $1/\sigma^2$
- deduced  $B(E2, 5/2^- \rightarrow 1/2^-) = 3.2_{-1.0}^{+2.8} e^2\text{fm}^4$

## Theoretical calculations:

	Energy / keV	$B(E2) / e^2\text{fm}^4$	Half-life_Exp / ps
UFP-CA	1767	5.11	7.0
VS-IMSRG	2116	0.785	45

- Shell Model calculations using UFP-CA interaction (by Alex Brown)
- Valence-space in-medium similarity renormalization group (VS-IMSRG) using chiral effective field theory (EFT) interaction (by Jason Holt, 2019)



# Summary

- Performed in-beam gamma-ray spectroscopy measurement in neutron-rich Ca isotopes with a Hybrid HPGe array at RIBF
- Benchmarked the simulation with  $^{36}\text{Ar}$  spectra, the obtained gamma-ray response functions well reproduced the peak shapes
- Analysed the  $^{53}\text{Ca}$  spectra with detailed simulations, the lifetime of the  $5/2^-$  state is extracted to be  $11(5)$  ps, leading to a  $B(E2, 5/2^- \rightarrow 1/2^-) = 3.2_{-1.0}^{+2.8} \text{ e}^2\text{fm}^4$
- Experimental results are compared with Shell-Model calculations using UFP-CA interaction, and VS-IMSRG approach using EFT interactions with 2N and 3N forces

# Collaborations



**University of York:** S. Chen, R. Crane, W. Marshall, R. Taniuchi, M. Petri, S. Paschalis, M. Bentley, L. Tetley



**RIKEN:** P. Doornenbal, H. Baba, F. Browne, B. Mauss, B. Moon, H. Sakurai, D. Suzuki



大阪大学 核物理研究センター

**RCNP:** N. Aoi, E. Ideguchi, S. Iwazaki, A. Kohda, Y. Yamamoto



**Universität zu Köln:** C. Fransen, H. Hess, P. Reiter, S. Thiel



**LBNL:** H. Crawford, C. Campbell, A. Macchiavelli, P. Fallon, M. Cromaz, R. Clark, A. Frotscher



**CSIC:** K. Wimmer



**Korea University:** J. Kim



**University of Tokyo:** T. Koiwai



**University of Surrey:** T. Parry



**KU Leuven:** H. de Witte



**TRIUMF:** J. Holt



**MSU:** B. A. Brown

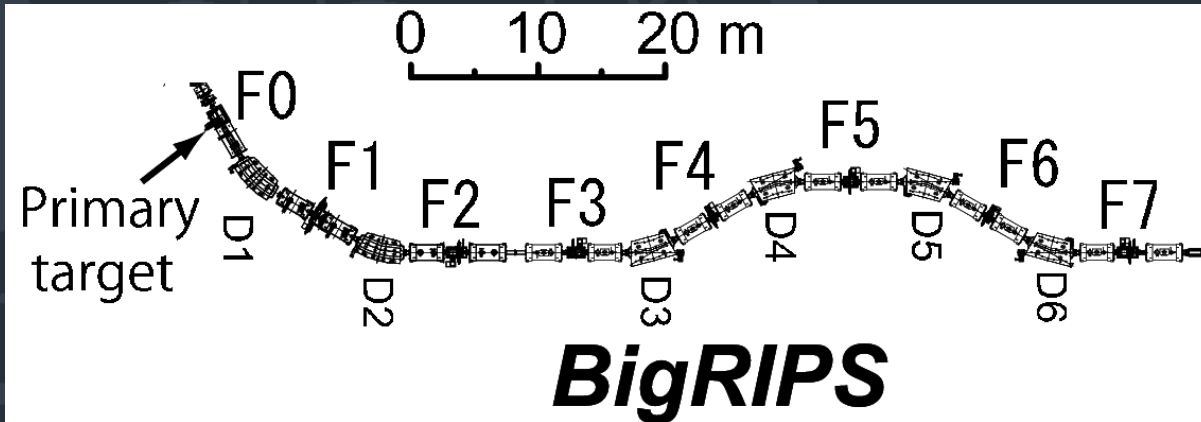
**Thank you for your attention**



UNIVERSITY  
*of York*

# Backup

# BigRIPS Separator



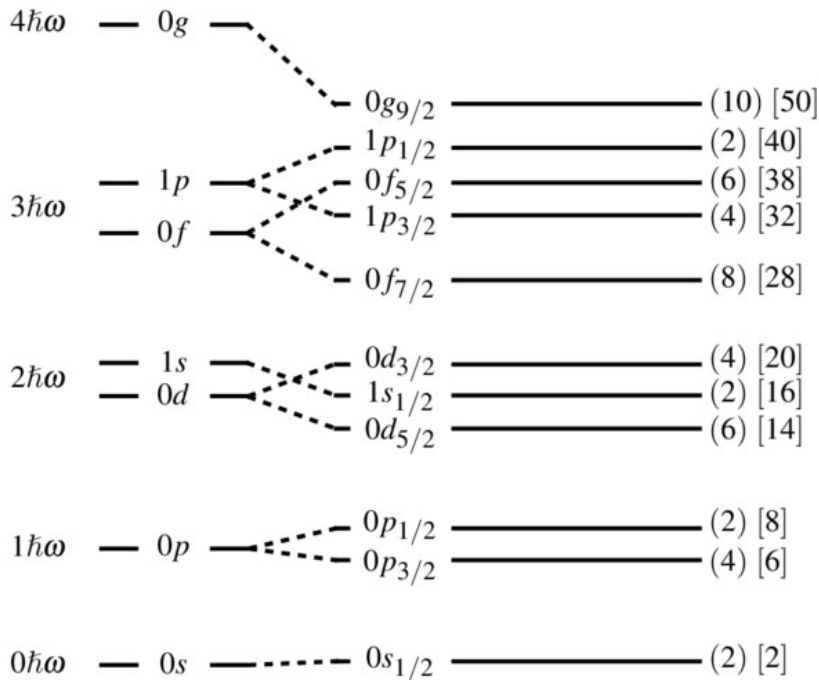
## Big RIKEN Projectile Fragment Separator

- $B\rho$ - $\Delta E$ - $B\rho$  separation
- Large acceptance
  - $\Delta\theta = \pm 40$  mrad
  - $\Delta\phi = \pm 50$  mrad
  - $\Delta p/p = \pm 3\%$
- Event-by-event  $B\rho$ -TOF- $\Delta E$  particle identification

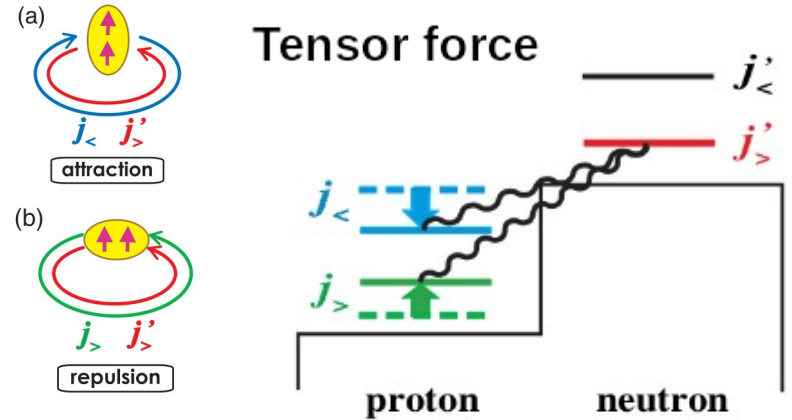
# Shell structures and nuclear forces

Woods-Saxon  
potential

with Spin-Orbital  
(L-S) force

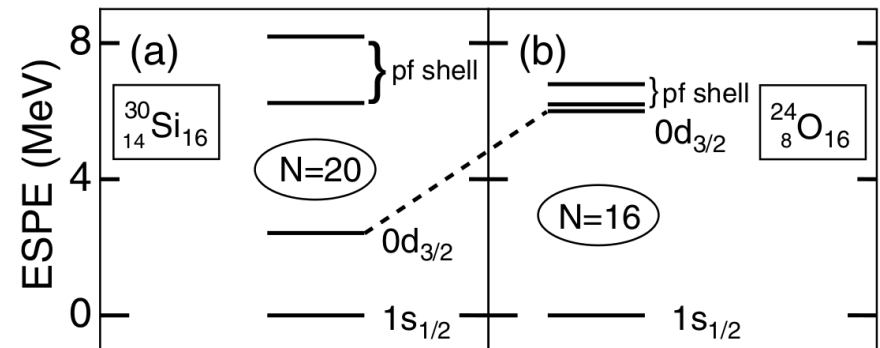


- spin-orbital splitting:  
 $E(j_> = l + s) < E(j_< = l - s)$
- conventional magic numbers:  
2, 8, 20, 28, 50, ...



T. Otsuka *et al.*, Phys. Rev. Lett. **95**, 232502 (2005)

$^{30}\text{Si} \rightarrow ^{24}\text{O}$ : absence of strong  $\pi 0d_{5/2} - \nu 0d_{3/2}$  attraction  
 $\Rightarrow N = 16$  new magic number in oxygen



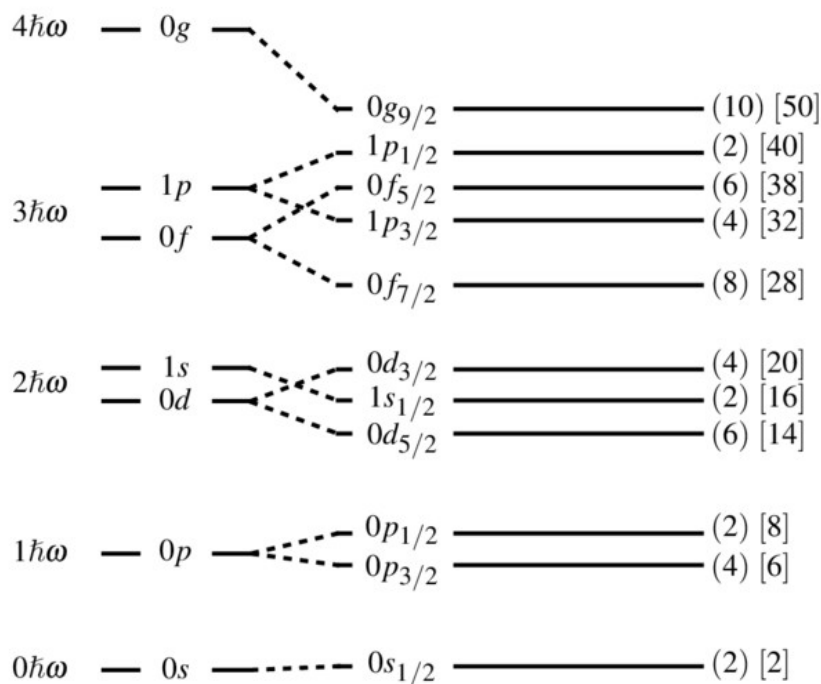
T. Otsuka *et al.*, Phys. Rev. Lett. **87**, 082502 (2001)

# Shell structures and nuclear forces

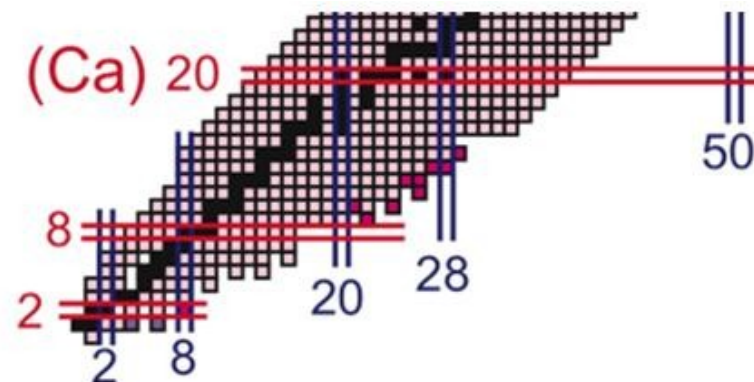


Woods-Saxon  
potential

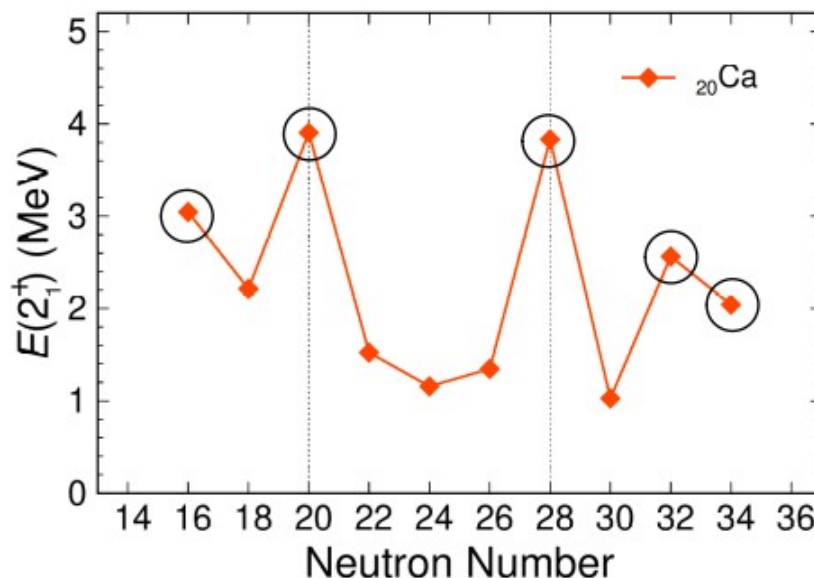
with Spin-Orbital  
(L-S) force



- spin-orbital splitting:  
 $E(j_> = l + s) < E(j_< = l - s)$
- conventional magic numbers:  
2, 8, 20, 28, 50, ...



(sub-)shell closure at  $N = 16, 20, 28, 32, 34$

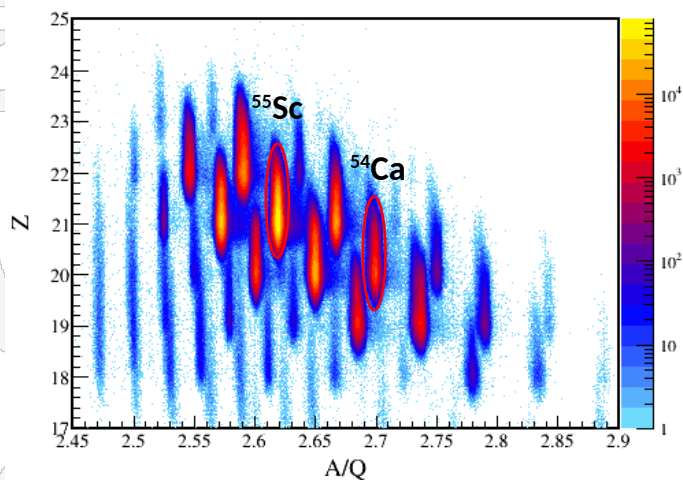


# Particle Identification

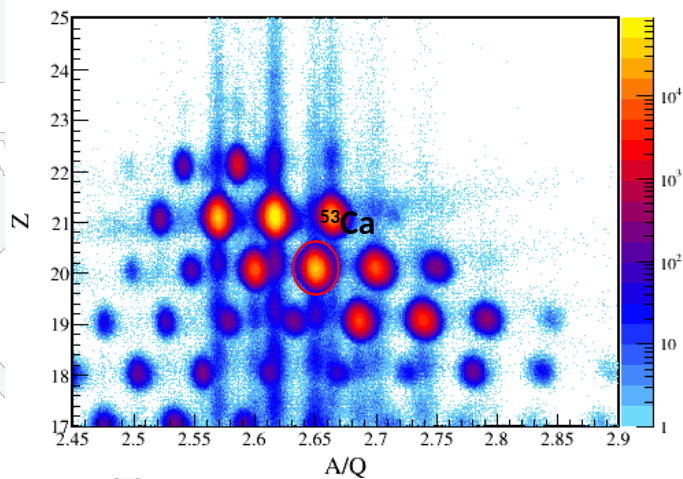


neutron-rich Ca setting

BigRIPS PID

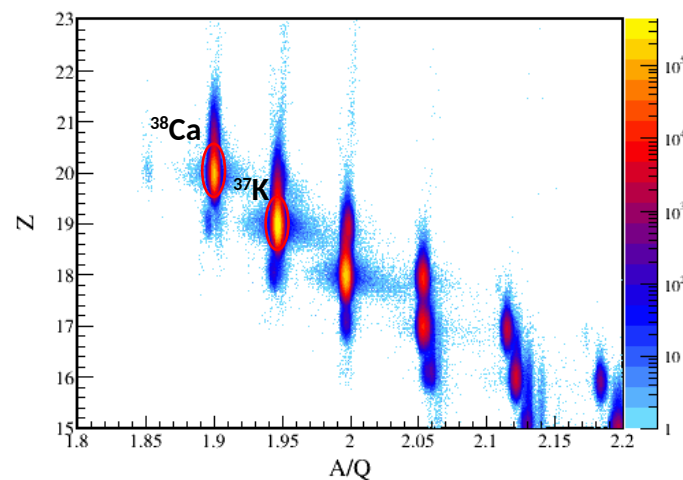


ZeroDegree PID

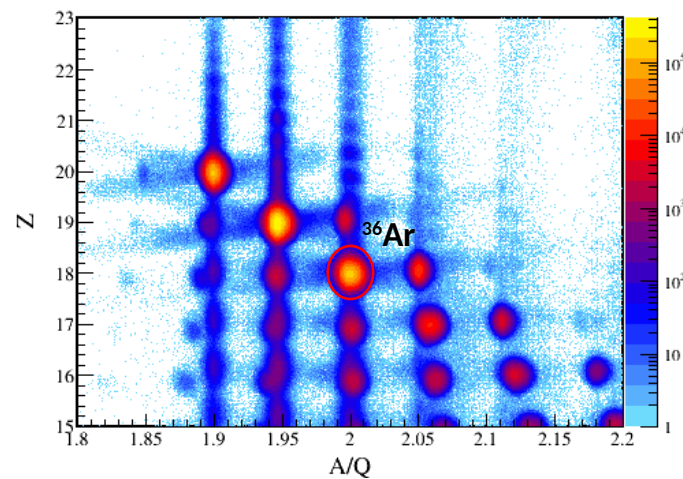


proton-rich Ca setting

BigRIPS PID



ZeroDegree PID



# Doppler-correction



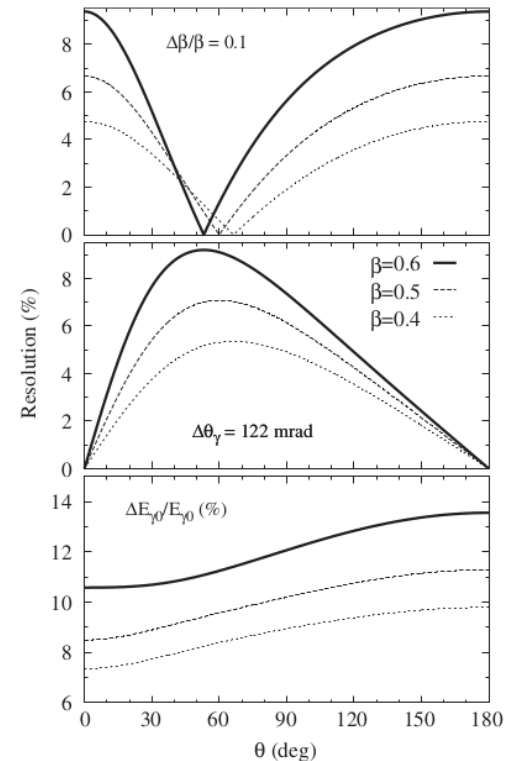
P. Doornenbal, PTEP **2012**, 03C004

- Doppler correction for prompt gamma

$$\frac{E_\gamma}{E_{\gamma 0}} = \frac{\sqrt{1 - \beta^2}}{1 - \beta \cos \vartheta_\gamma}$$

- Doppler-corrected gamma energy resolution:

$$\left(\frac{\Delta E_{\gamma 0}}{E_{\gamma 0}}\right)^2 = \left(\frac{\beta \sin \vartheta_\gamma}{1 - \beta \cos \vartheta_\gamma}\right)^2 \times (\Delta \vartheta_\gamma)^2 + \left(\frac{\beta - \cos \vartheta_\gamma}{(1 - \beta^2)(1 - \beta \cos \vartheta_\gamma)}\right)^2 \times (\Delta \beta)^2 + \left(\frac{\Delta E_{\text{intr}}}{E_\gamma}\right)^2.$$

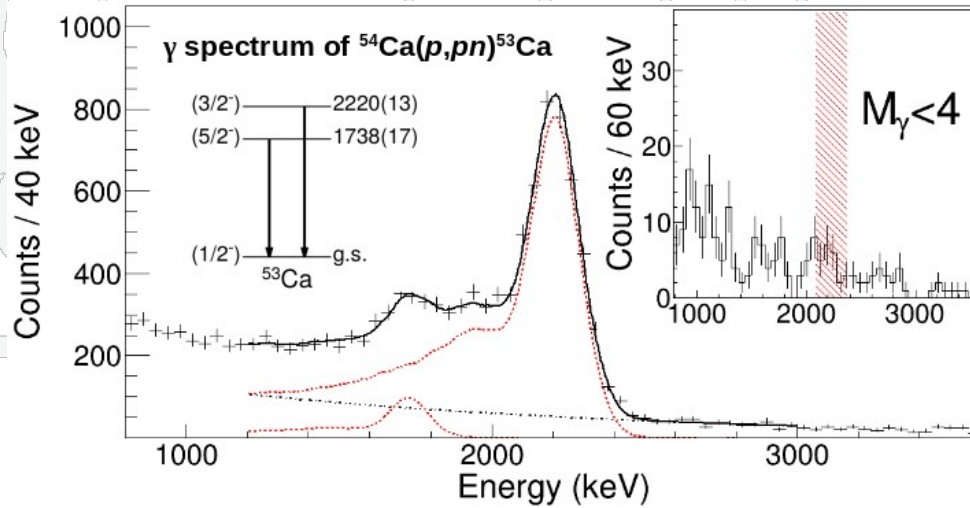


**Fig. 1.** Doppler broadening due to  $\Delta\beta$ ,  $\Delta\vartheta_\gamma$ , and  $\Delta E_{\text{intr}}$  as a function of the  $\gamma$ -ray emission (detector) angle  $\vartheta_\gamma$ . Three different velocities were assumed. The upper panel displays only the velocity uncertainty effect for  $\Delta\beta/\beta = 0.1$ , while the middle panel displays the broadening due to a detector opening angle of  $\Delta\vartheta_\gamma = 122$  mrad. In the bottom panel, the sum effect including an intrinsic energy resolution of 6% at 1.33 MeV is displayed. The calculations were performed for a 1 MeV  $\gamma$ -ray energy assuming a square-root dependence of the intrinsic energy resolution.



# Excitation of $^{53}\text{Ca}$

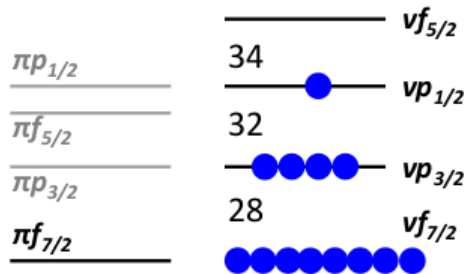
S. Chen et al., Phys. Rev. Lett. **123**,142501 (2019)



$E_x = 2220$  keV via  $\beta$ -decay,  
F. Perrot et al. PRC **74**,014313 (2006)

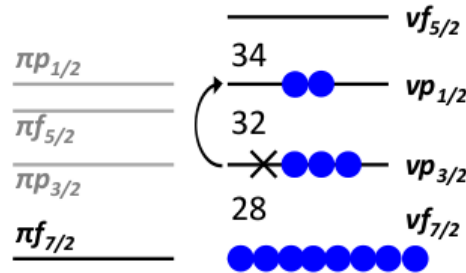
$^{53}\text{Ca}$  populated via  $^{54}\text{Ca} \rightarrow ^{53}\text{Ca}$

g.s.  $(1/2^-)$



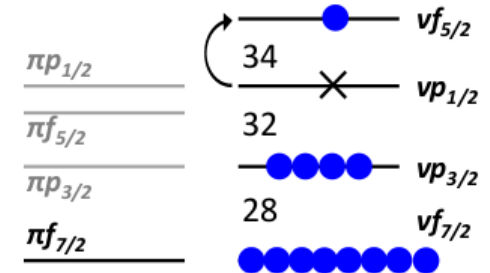
$^{53}\text{Ca}$  (Z=20)

2220 keV  $(3/2^-)$



$^{53}\text{Ca}$  (Z=20)

1753 keV  $(5/2^-)$

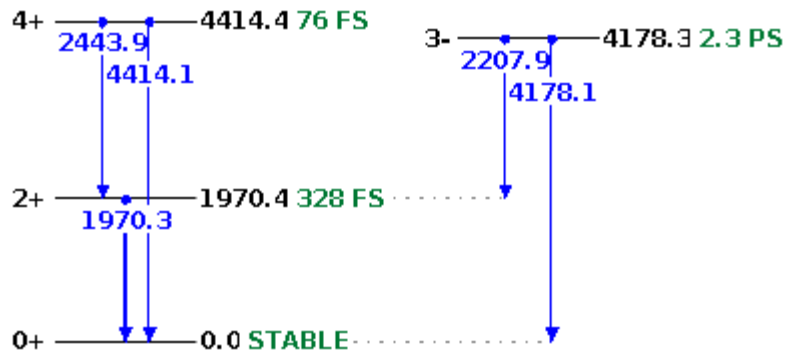


$^{53}\text{Ca}$  (Z=20)

# Benchmark – $^{36}\text{Ar}$ from $^{37}\text{K} - 1p$



$^{36}\text{Ar}$  low-lying excitation states from NNDC

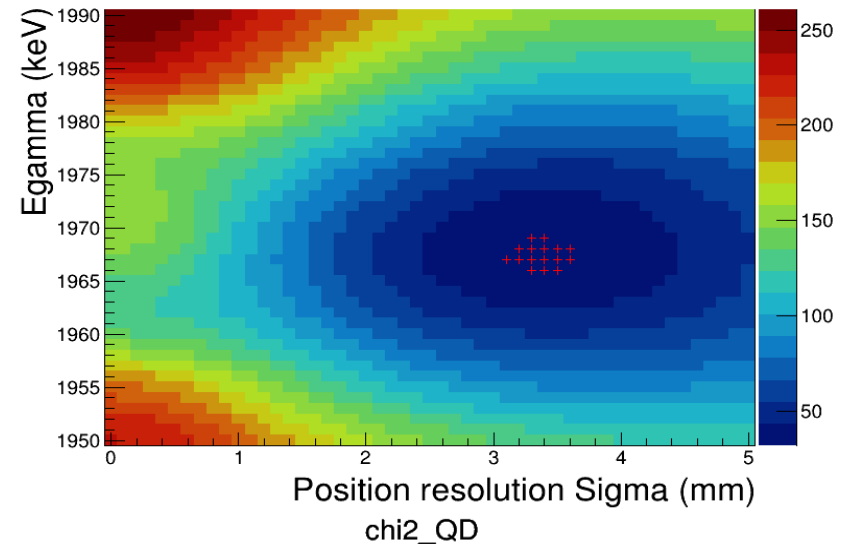


- Fix  $4^+ \rightarrow 2^+$  and  $3^- \rightarrow 2^+$  energies and lifetimes
- Study  $2^+ \rightarrow 0^+$  energy and **tracking detectors position resolution**
- Red markers:  $1-\sigma$  region ( $\text{min-chi}^2 + 1$ )
- MinChi2 at

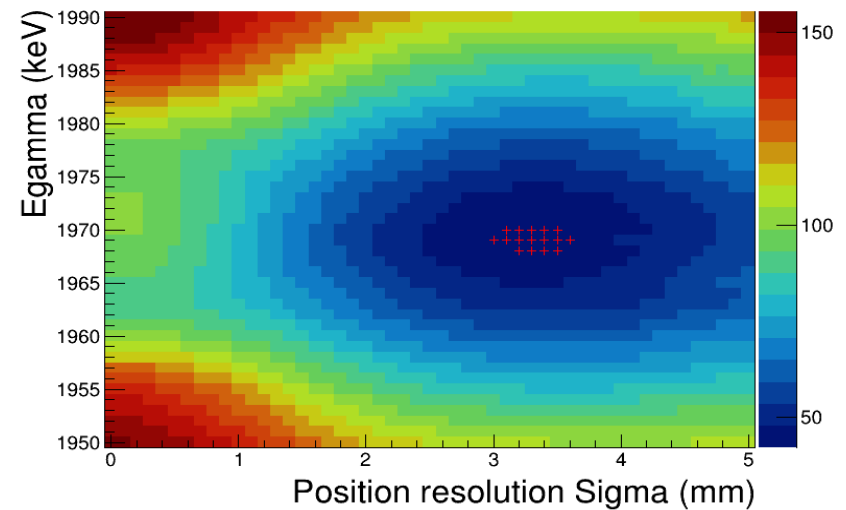
1967keV, **3.3mm** (P3)

1969keV, **3.3mm** (Quad)

chi2\_P3



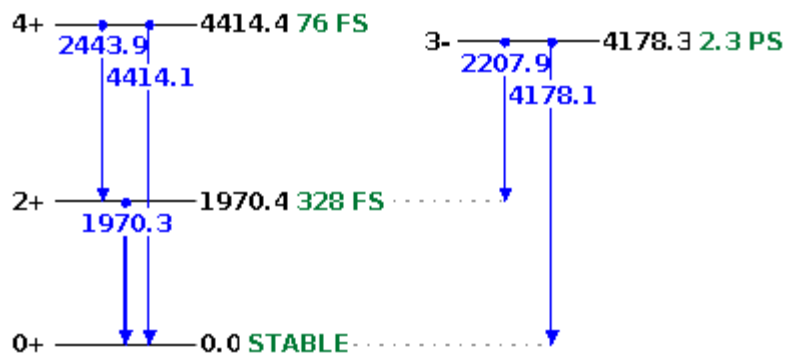
chi2\_QD



# Benchmark – $^{36}\text{Ar}$ from $^{37}\text{K} - 1p$

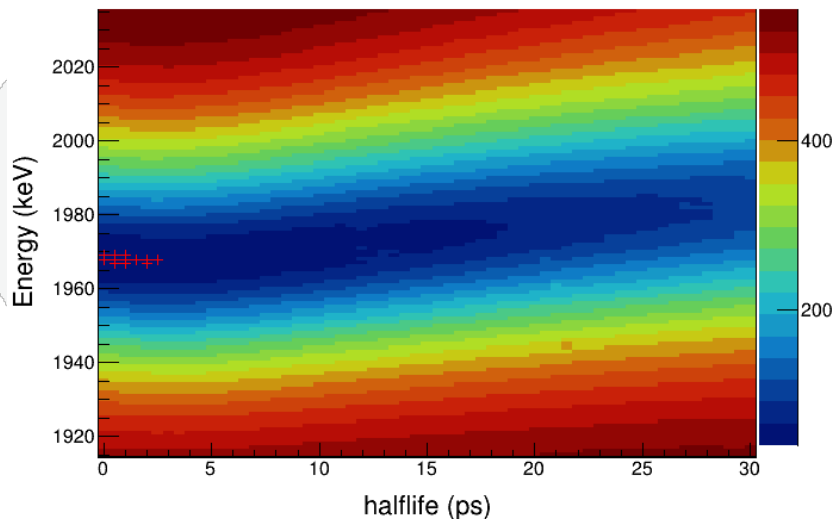


$^{36}\text{Ar}$  low-lying excitation states from NNDC

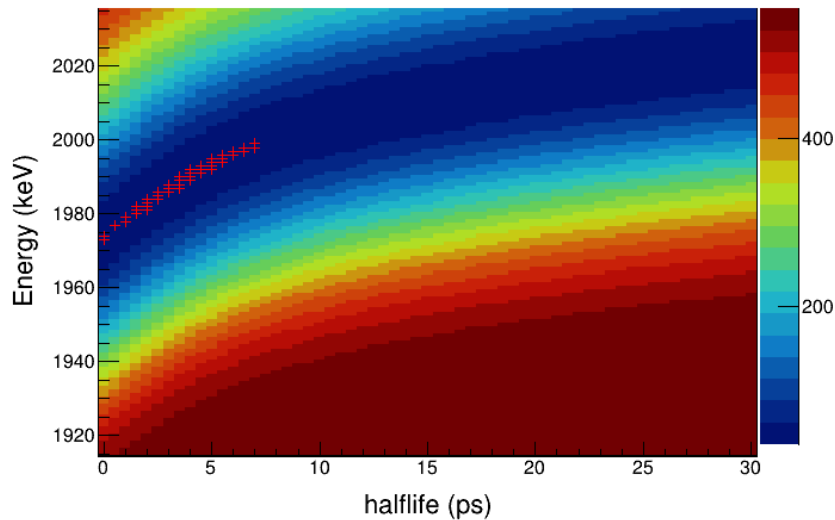


- Fix  $4+ \rightarrow 2+$  and  $3- \rightarrow 2+$  energies and lifetimes
- Study  $2+ \rightarrow 0+$  energy and lifetime
- Red markers:  $1-\sigma$  region ( $\text{min-}\chi^2 + 1$ )

$\chi^2$  surface {tracking}



$\chi^2$  surface {Miniball}



$\chi^2$  surface {Clover}

