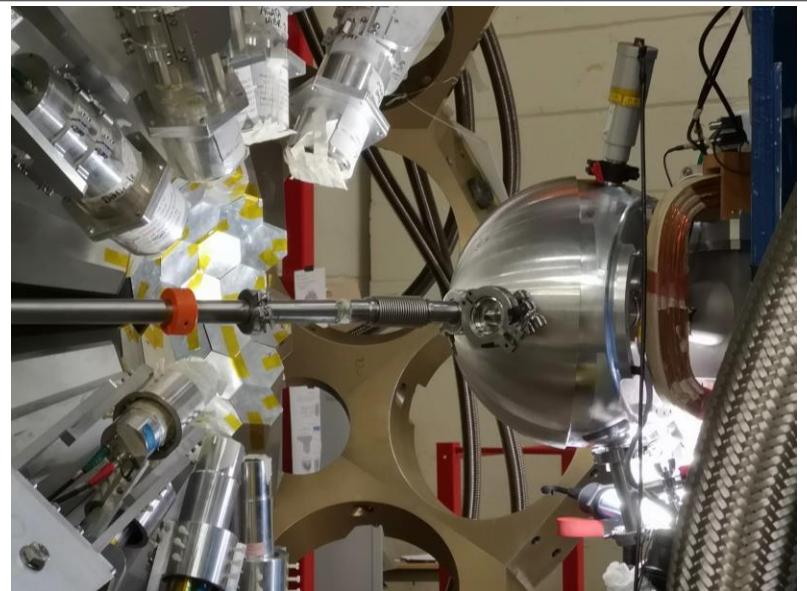


# Octupole deformation in neutron-deficient plutonium isotopes

Hamid Ayatollahzadeh

IOP Joint APP, HEPP, and NP Conference  
University of Liverpool  
08.04.24 – 11.04.24



Istituto Nazionale di Fisica Nucleare  
LABORATORI NAZIONALI DI LEGNARO

**UWS** UNIVERSITY OF THE  
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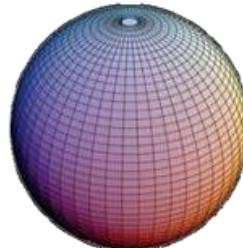
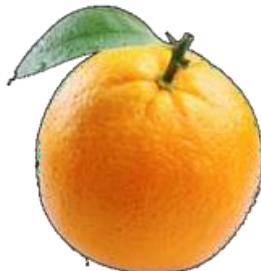
 **SUPA**<sup>®</sup>

# Octupole deformation

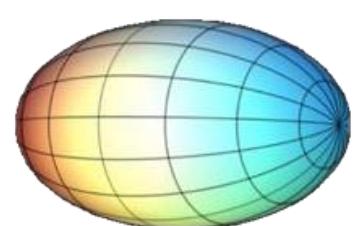
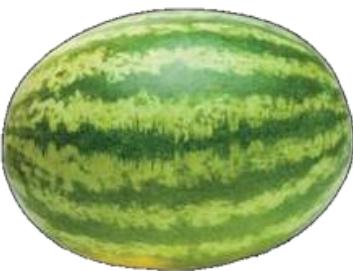
The nuclear shape is described by spherical harmonics multiplied by an expansion coefficient (deformation parameter).

$$R(\theta, \phi) = R_0[1 + \sum_{\lambda, \mu} \alpha_{\lambda, \mu} Y_{\lambda}^{\mu}]$$

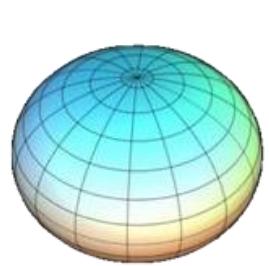
Spherical



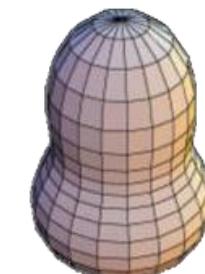
Prolate



Oblate

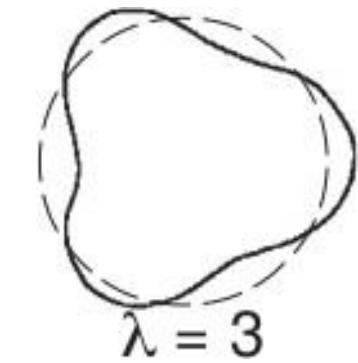
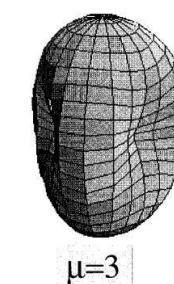
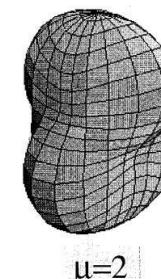
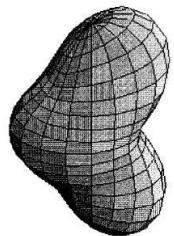
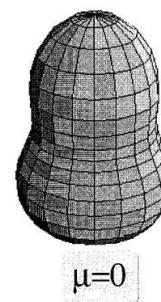


Pear-shaped

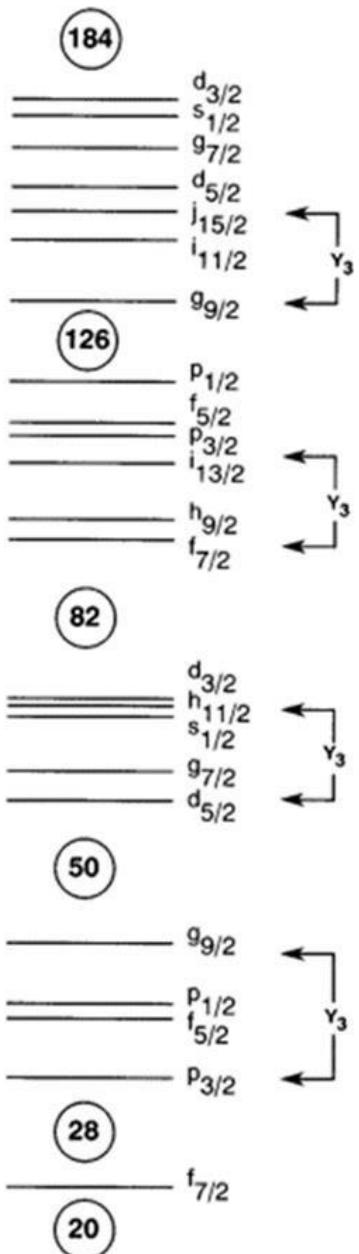


Quadrupole-octupole shapes

$$\beta_2=0.6, \beta_{3\mu}=0.35$$



# Octupole deformation



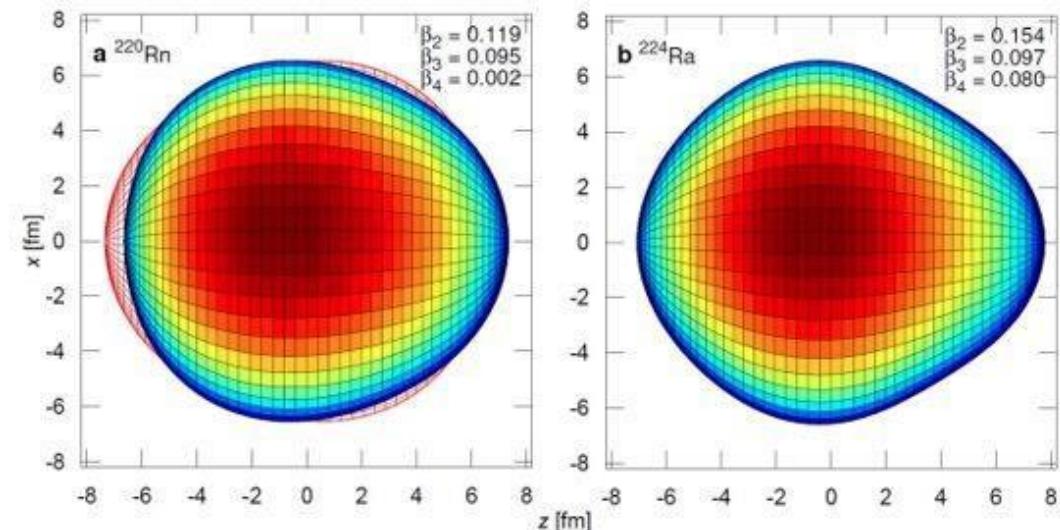
134 (j<sub>15/2</sub>, g<sub>9/2</sub>)

88 (i<sub>13/2</sub>, f<sub>7/2</sub>)

56 (h<sub>11/2</sub>, d<sub>5/2</sub>)

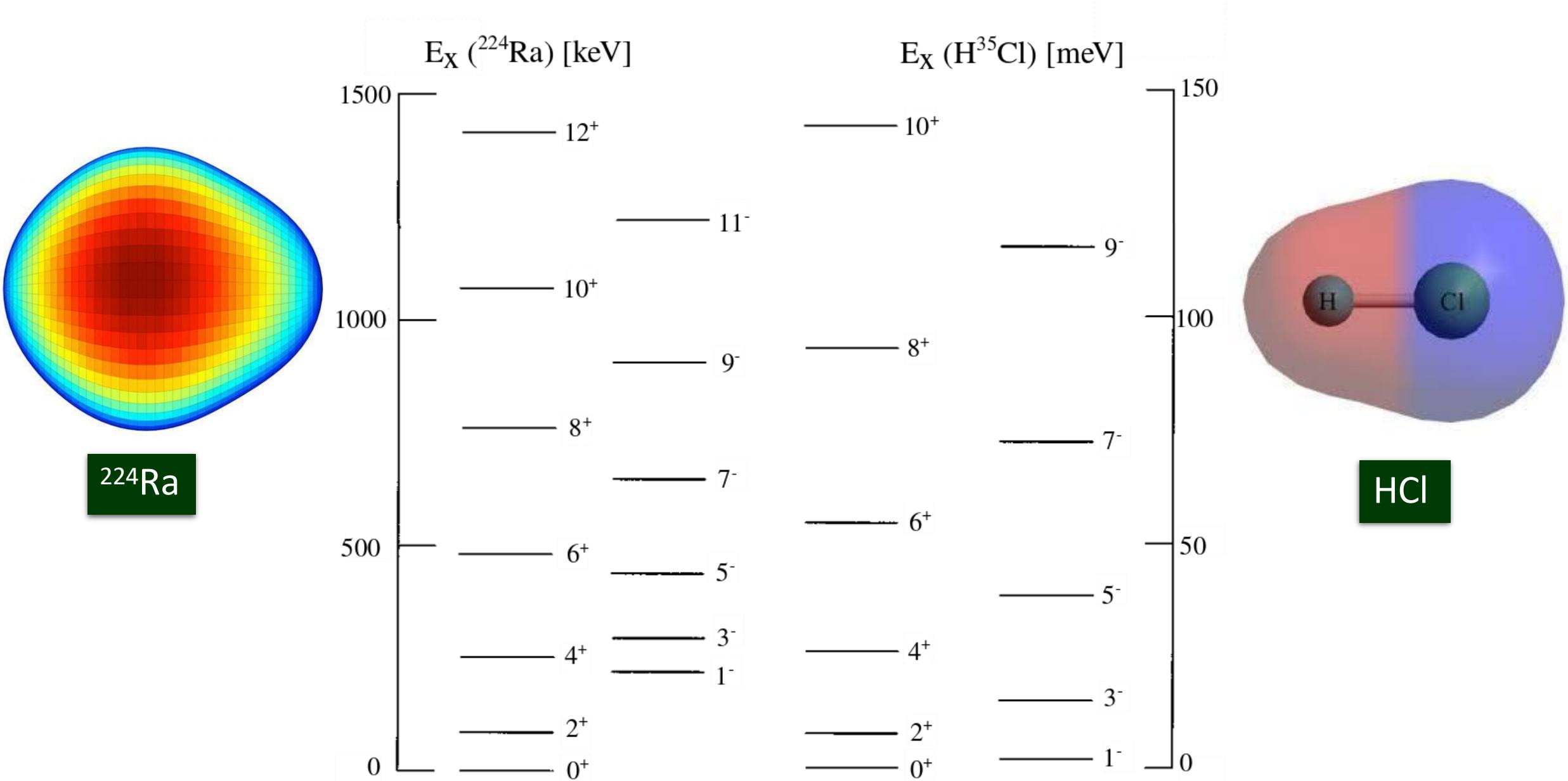
34 (g<sub>9/2</sub>, p<sub>3/2</sub>)

- $\Delta j = \Delta l = 3$
- Reflection-asymmetric nuclei
- Octupole magic numbers:  
34, 56, 88, 134

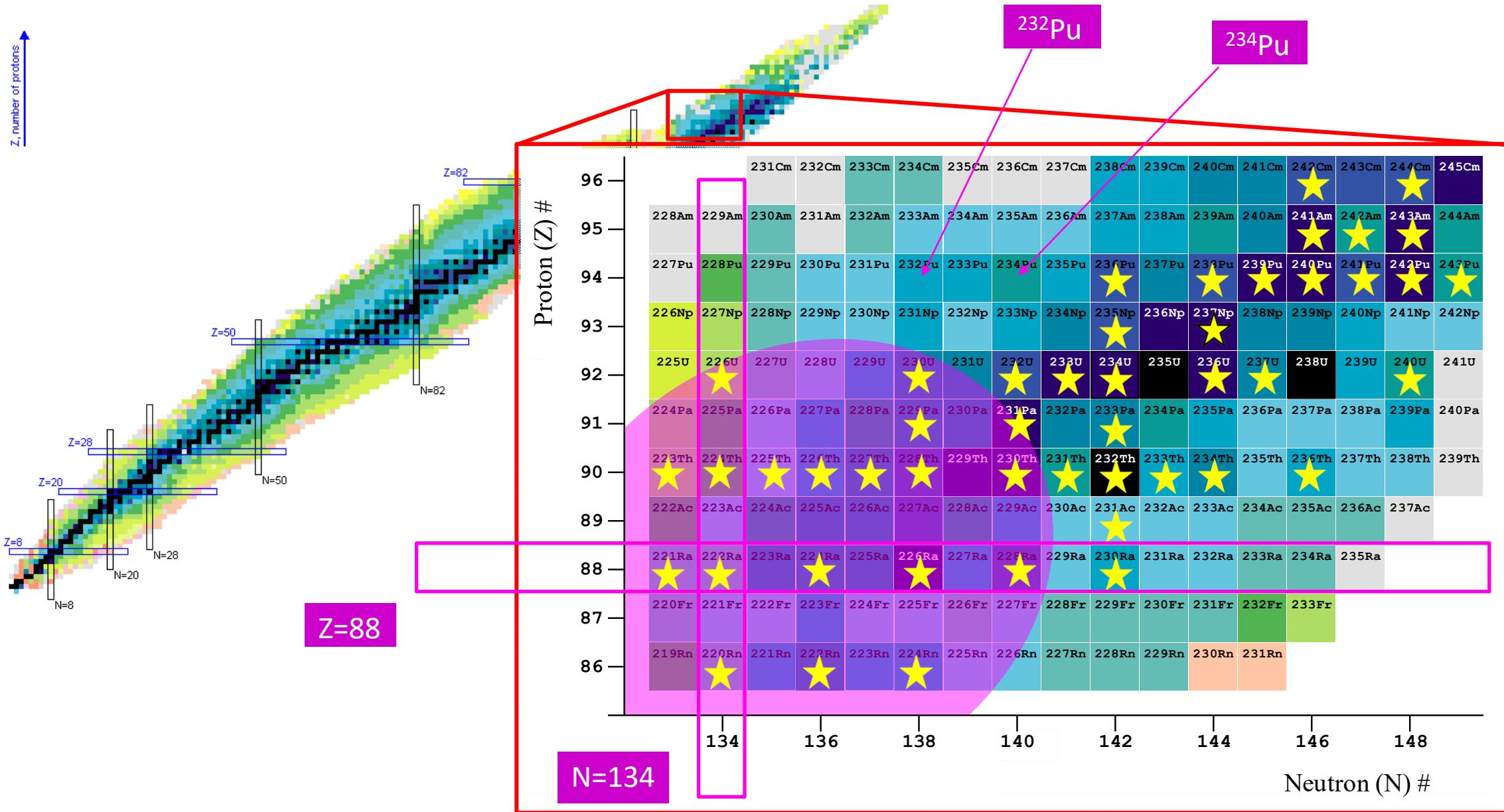


- N=Z=56 close to <sup>112</sup>Ba
- Z=56 N=88 close to <sup>146</sup>Ba
- Z=88 N=134 close to <sup>224</sup>Ra

# Spectroscopic features of octupole deformation

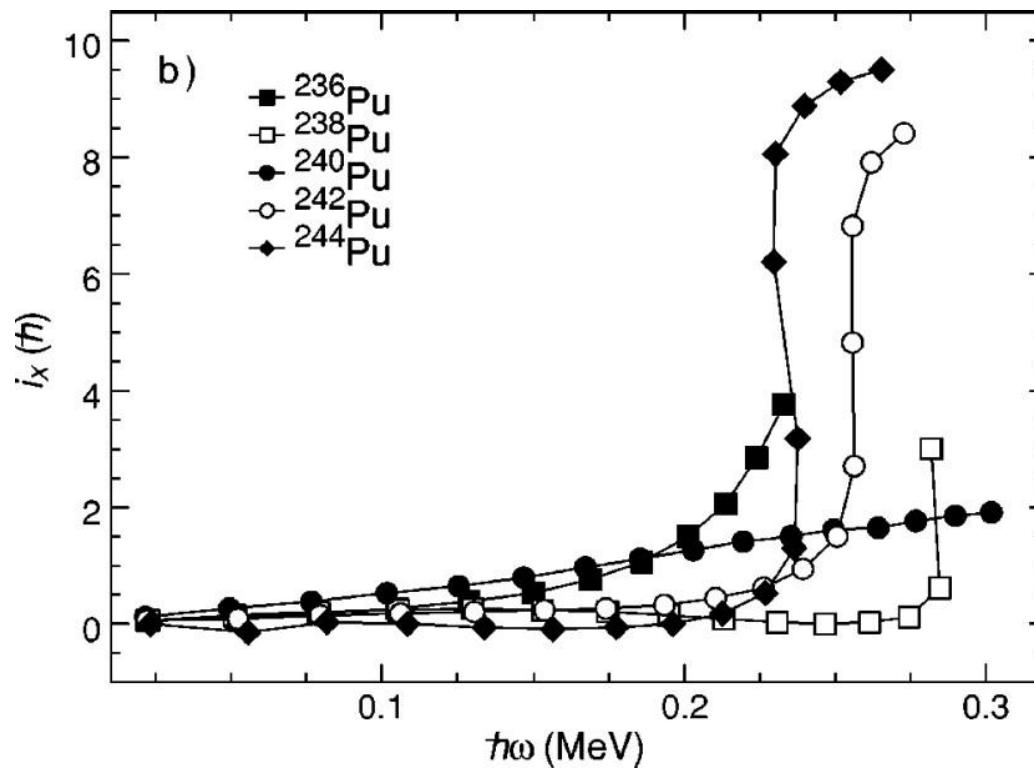
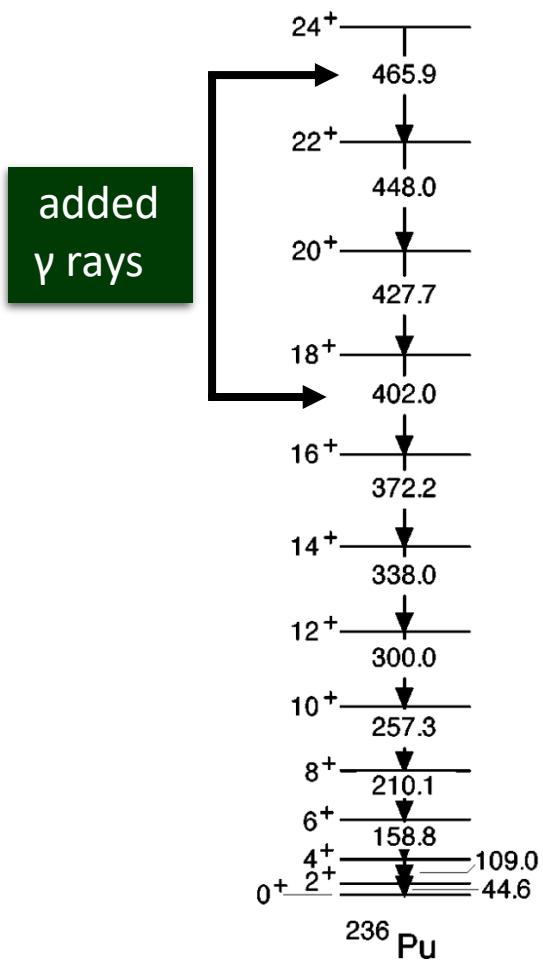


# Regional understanding



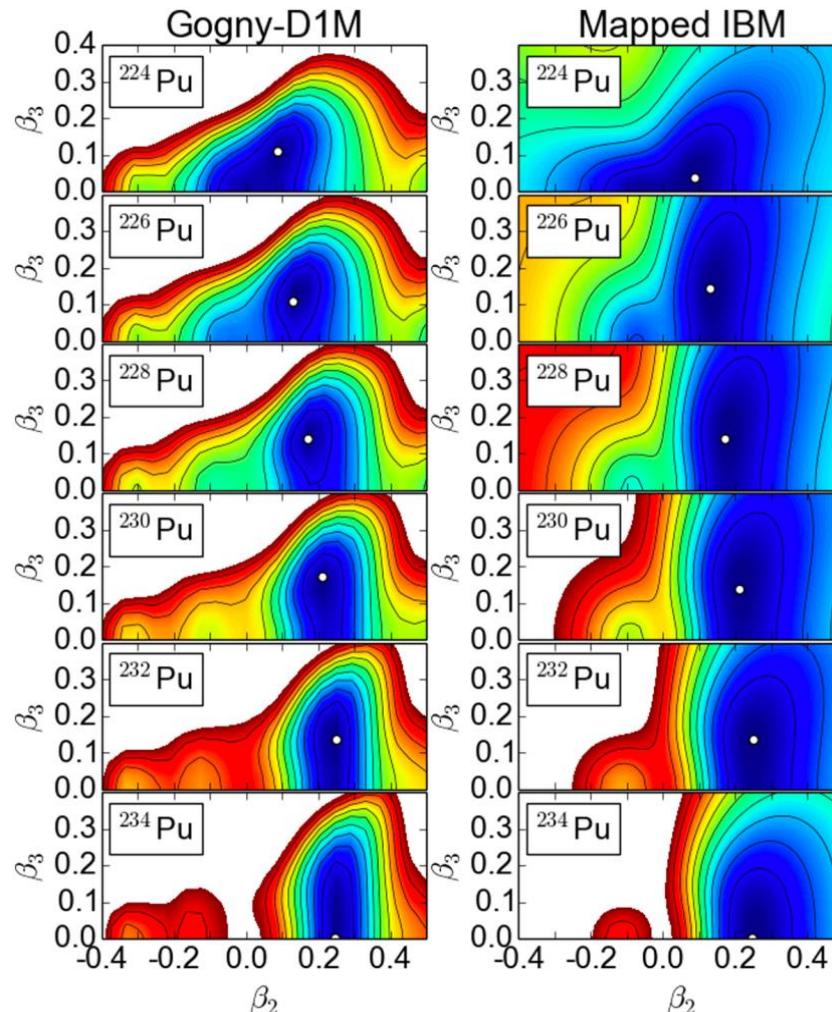
# Previous plutonium studies

- An experiment by K. Abu Saleem et al. studied the  $^{236}\text{Pu}$  isotope [K. Abu Saleem et al., Phys. Rev. C 70, 024310 (2004)] using the  $^{237}\text{Np}(^{209}\text{Bi}, ^{210}\text{Pb})$  transfer reaction.
- Additional four  $\gamma$ -ray transitions identified in  $^{236}\text{Pu}$  adding to established level scheme.



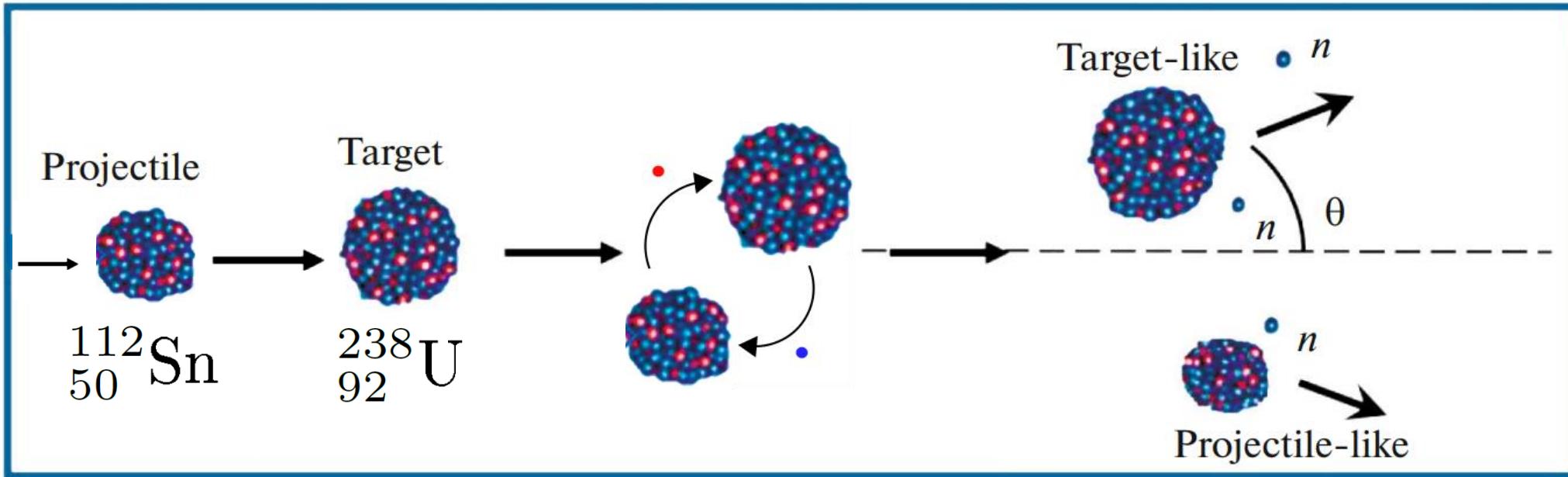
- Alignments show delayed backbending for plutonium isotopes with  $^{236}\text{Pu}$  and  $^{238}\text{Pu}$ .
- Only  $^{238-240}\text{Pu}$  show interleaving alternating parity states indicating stronger octupole effects.

# Theoretical predictions



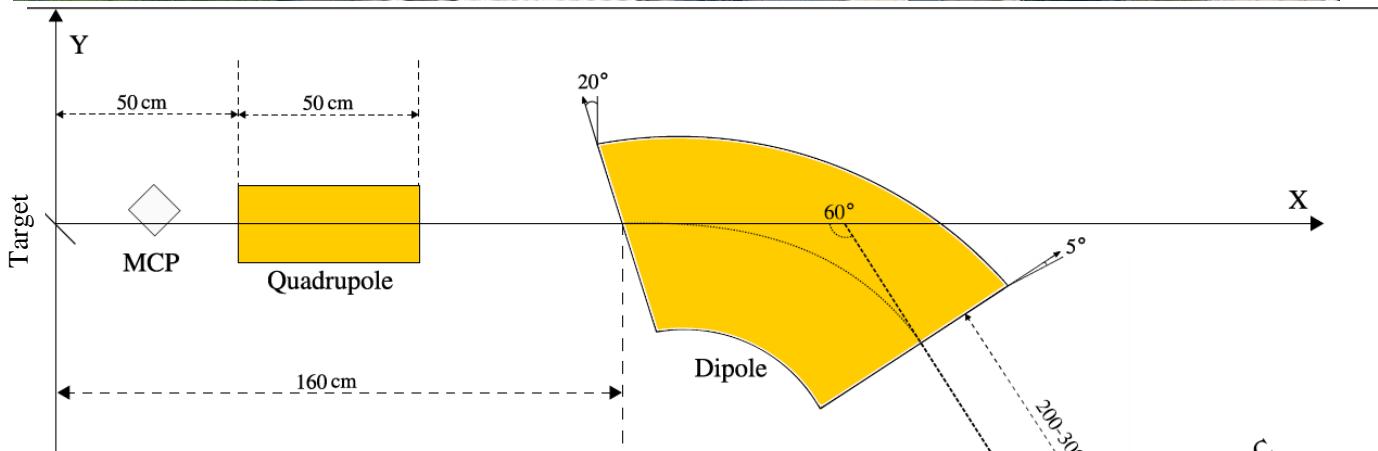
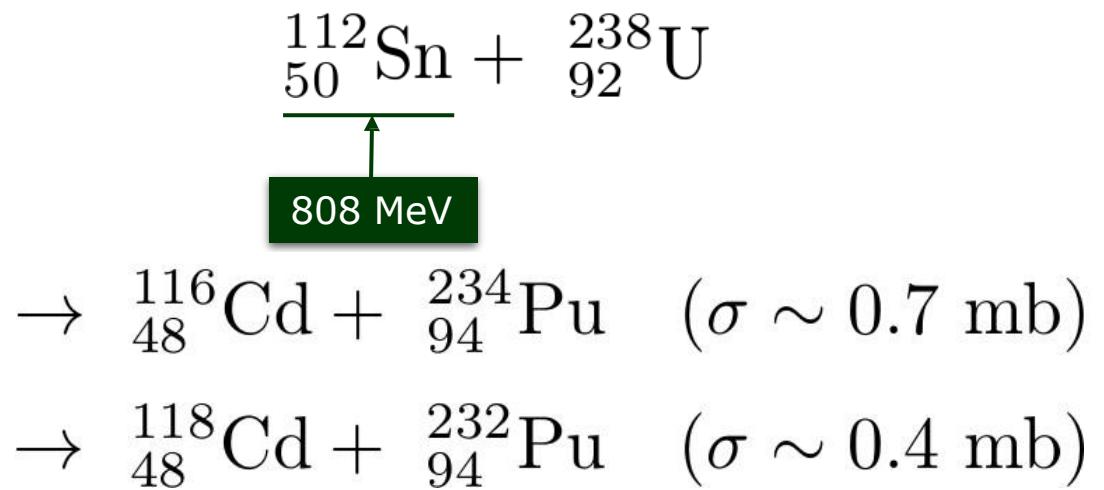
- Potential-energy surfaces by Nomura et al. (Phys. Rev. C **103**, 044311 (2021)) for  $^{234}\text{Pu}$  has  $\beta_3 \approx 0$  whereas for  $^{232}\text{Pu}$ ,  $\beta_3 \approx 0.22$ .

# Multi-nucleon transfer reactions



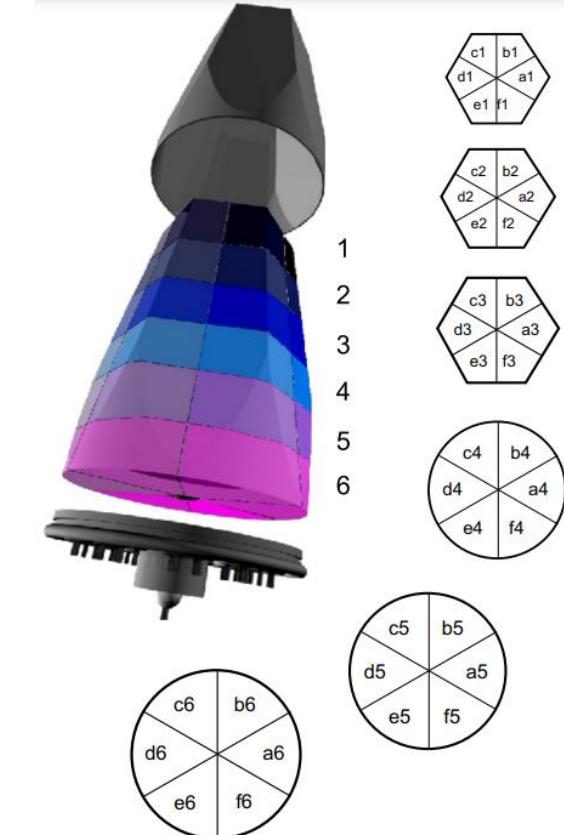
- Able to probe exotic nuclei past the current experimental limit when using fusion, fragmentation and other methods.
- Combination of MNT reactions with AGATA-PRISMA detector setup allows improved efficiency and selectivity.

# Experimental details



PRISMA Large Solid Angle  
Magnetic Spectrometer

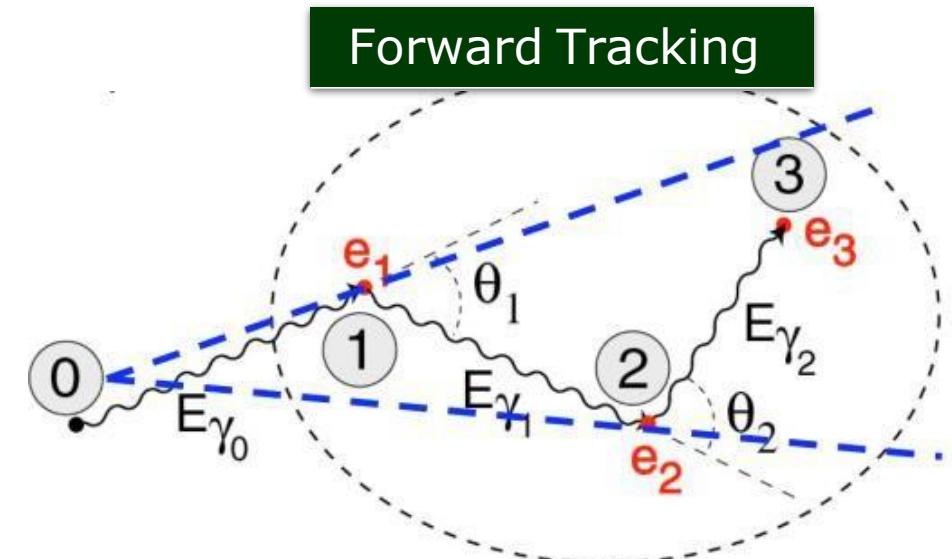
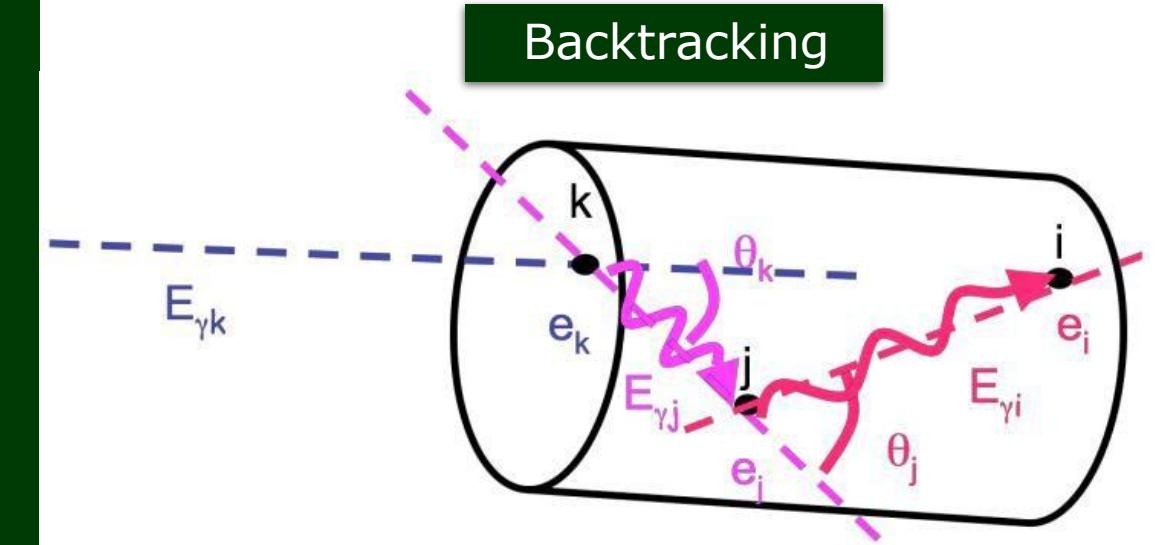
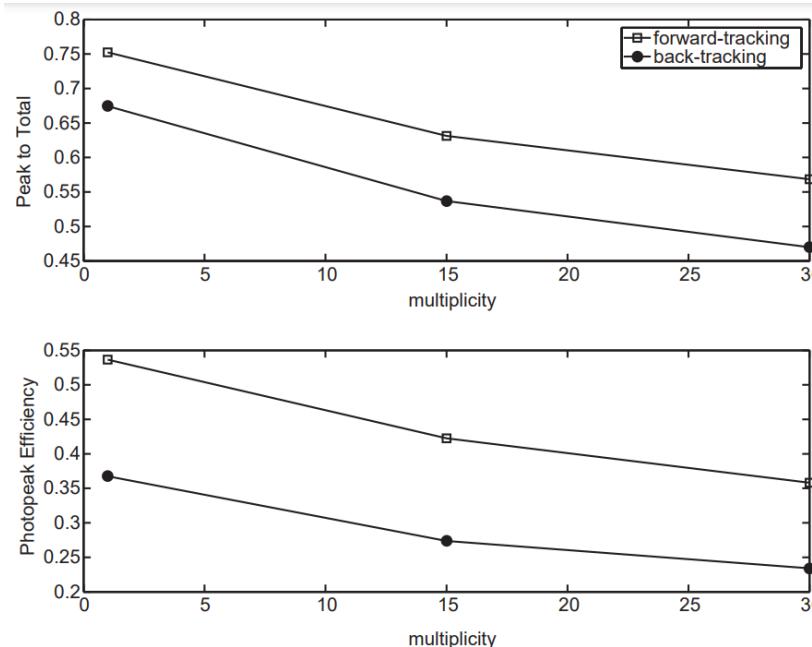
# AGATA- Advanced Gamma-ray Tracking Array



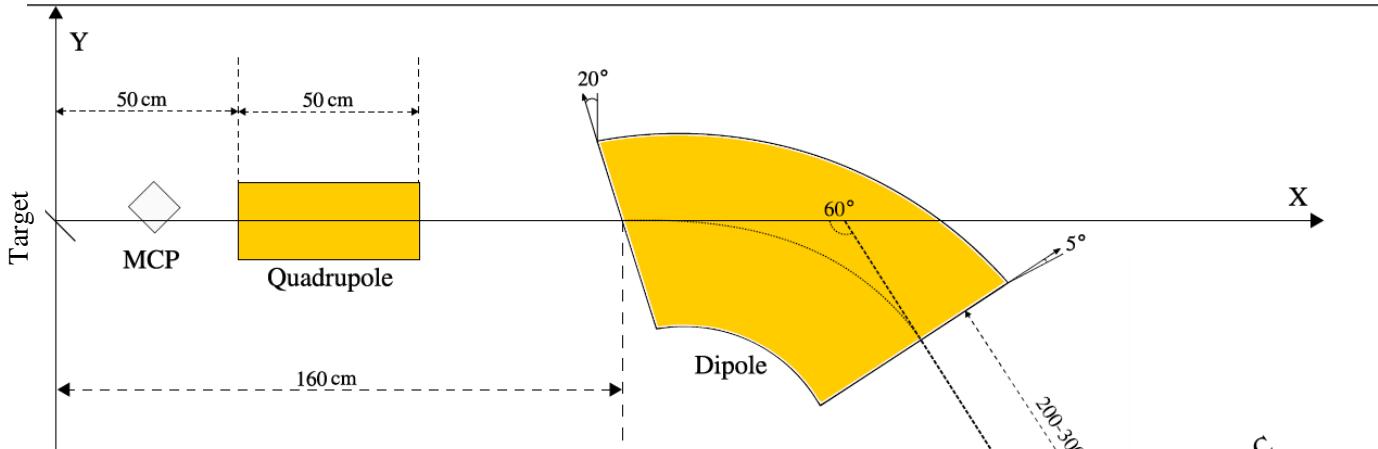
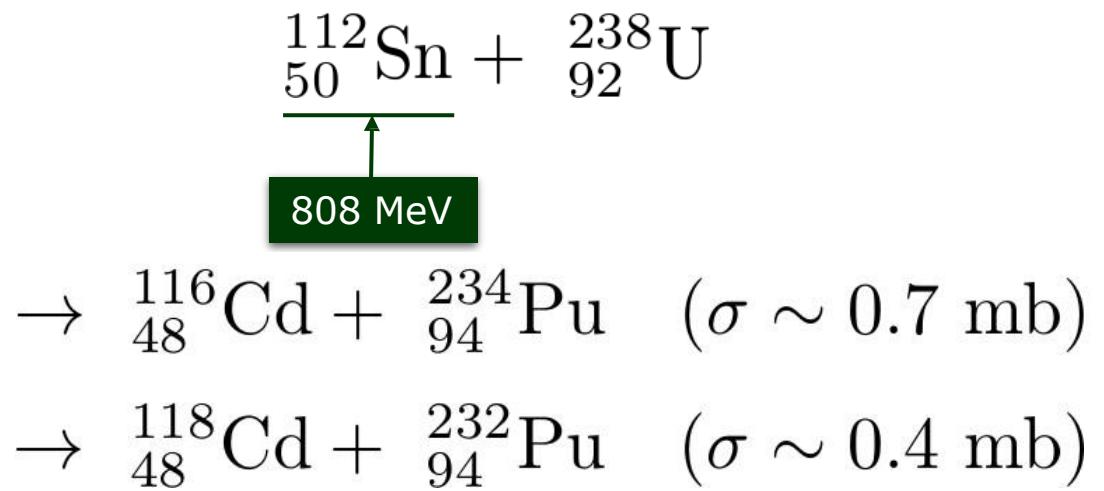
- New generation of gamma-ray spectrometers.
- Employs the novel technique of gamma-ray tracking to reconstruct events.
- 13 triple clusters.
- 36-fold segmentation.

# AGATA - Gamma-ray tracking

- Segmented germanium crystals allows reconstruction of gamma-ray energy.
- Two algorithms are employed to determine correct interaction sequence.
- Negates the requirement for Compton suppression and improves the overall detection efficiency of the apparatus.

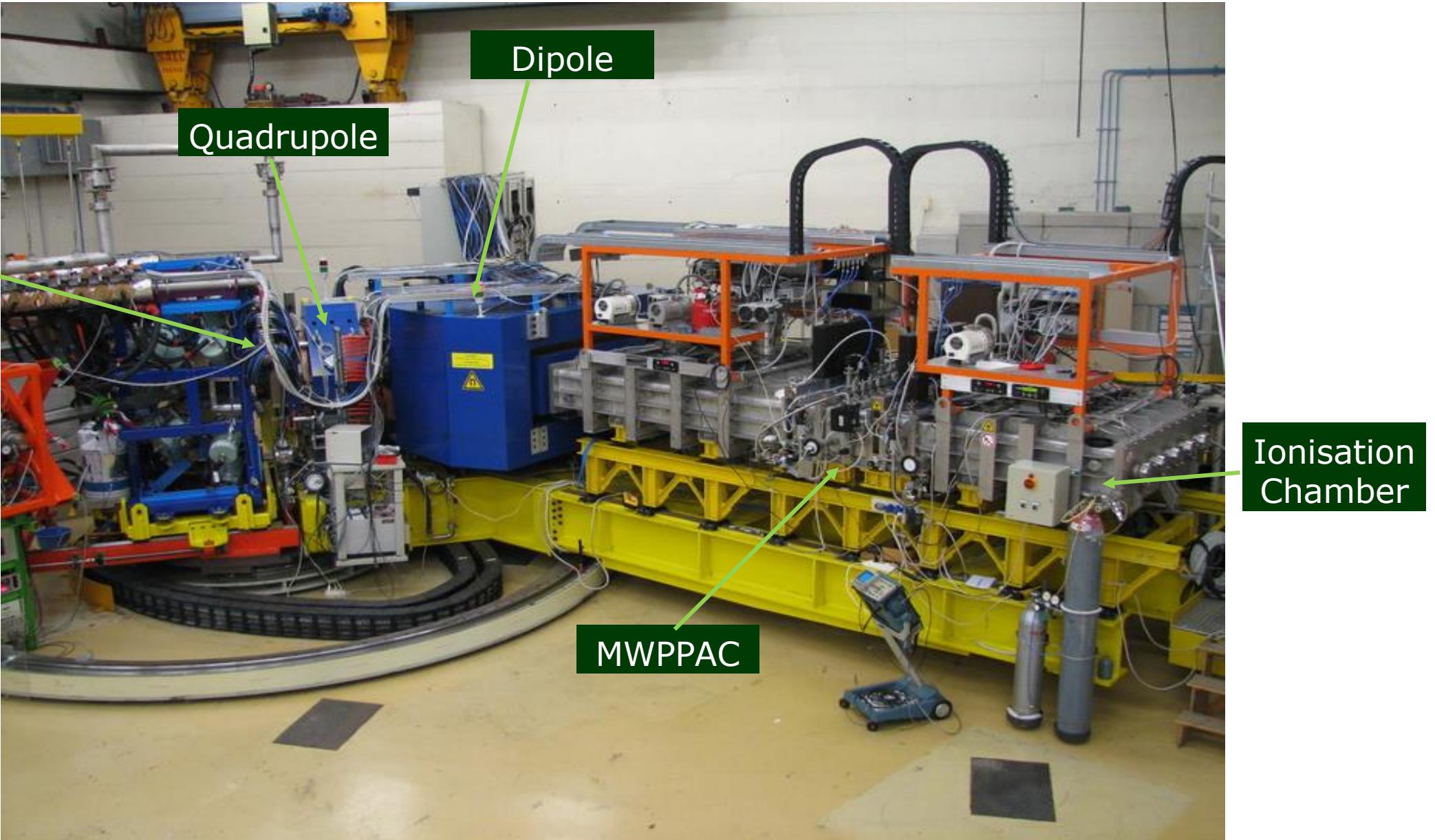


# Experimental details

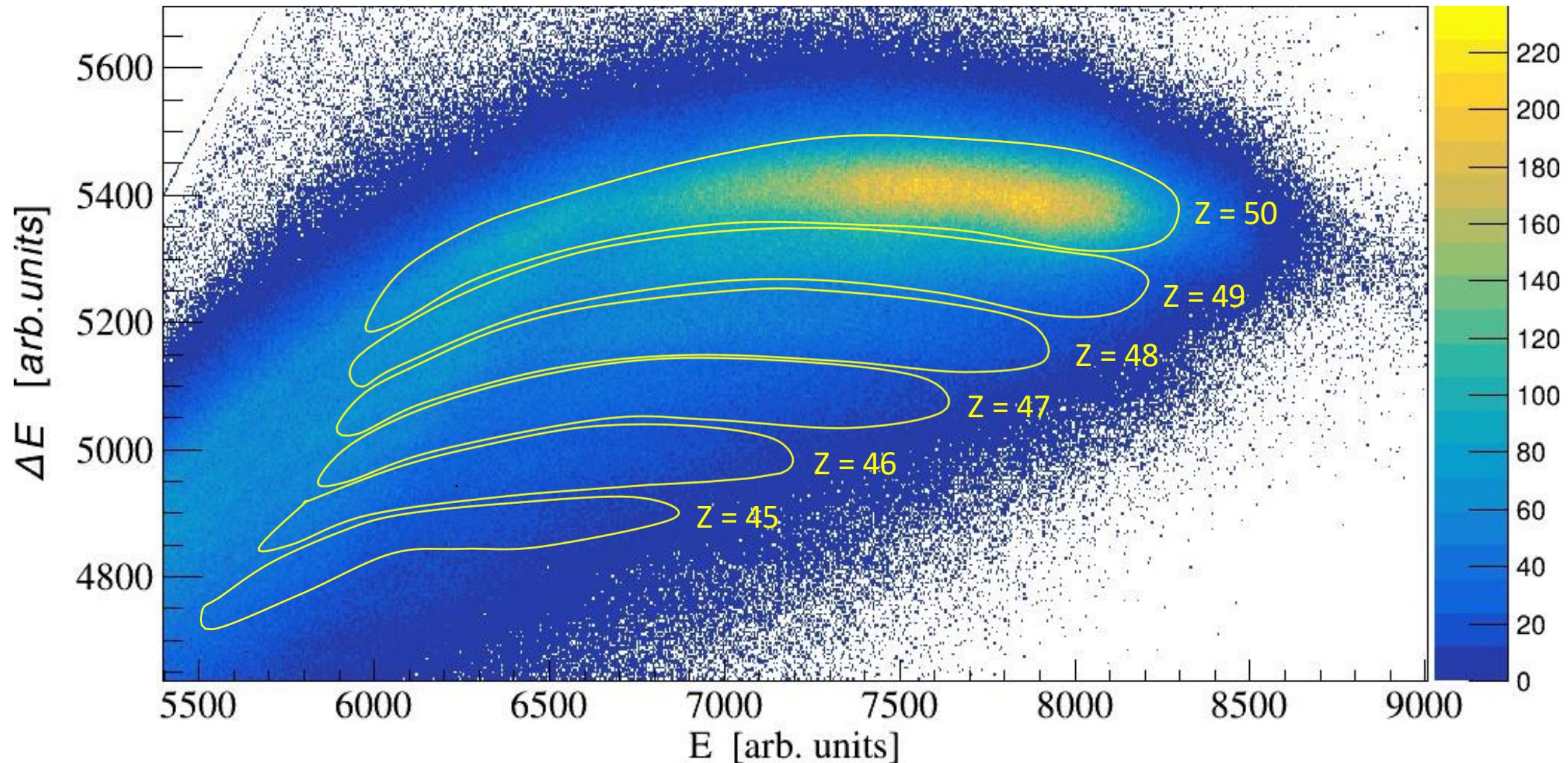


PRISMA Large Solid Angle  
Magnetic Spectrometer

# PRISMA Magnetic Spectrometer



# PRISMA - Z identification

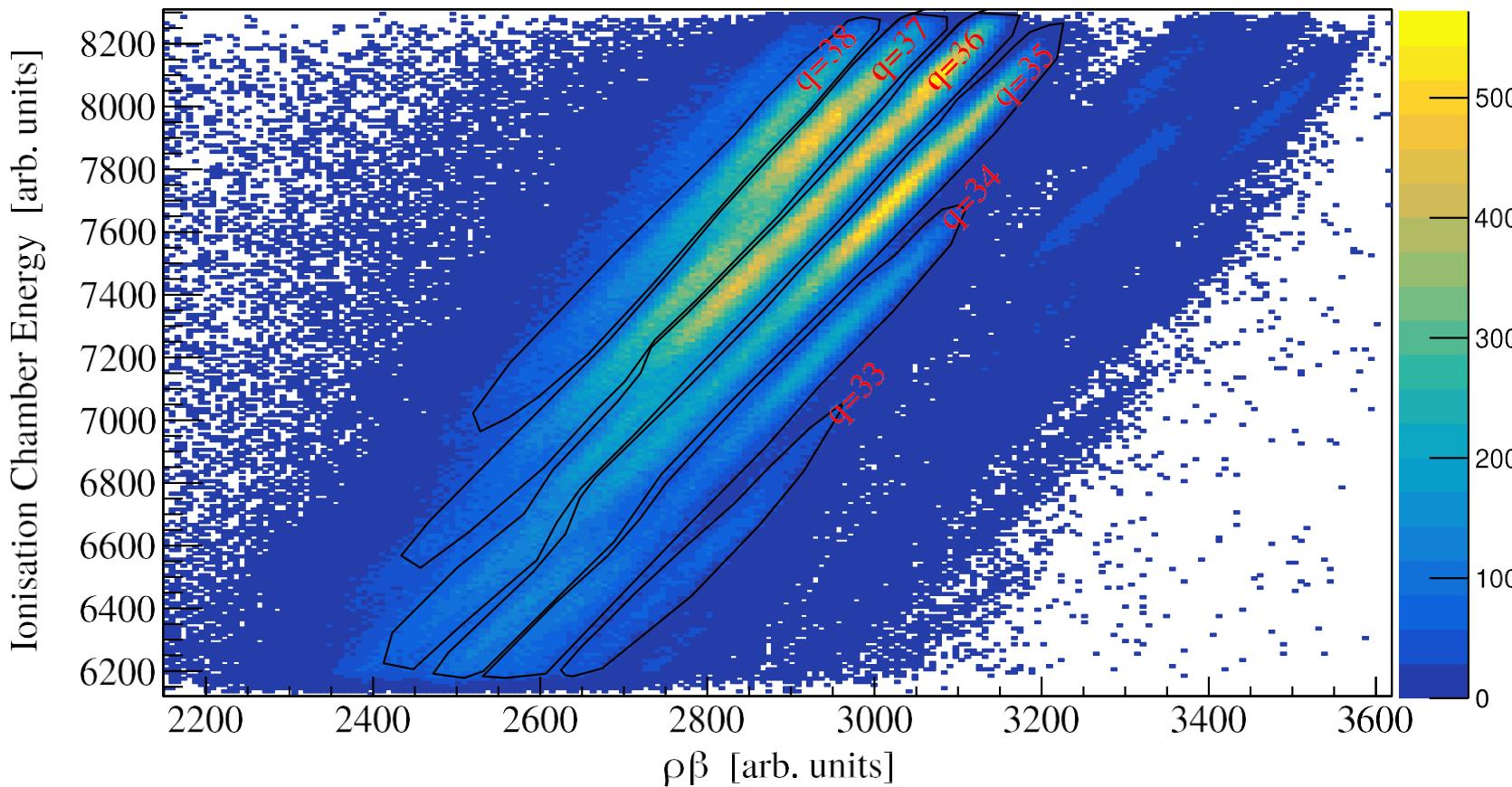


# PRISMA - q selection

$$B\rho = \frac{p}{q}$$

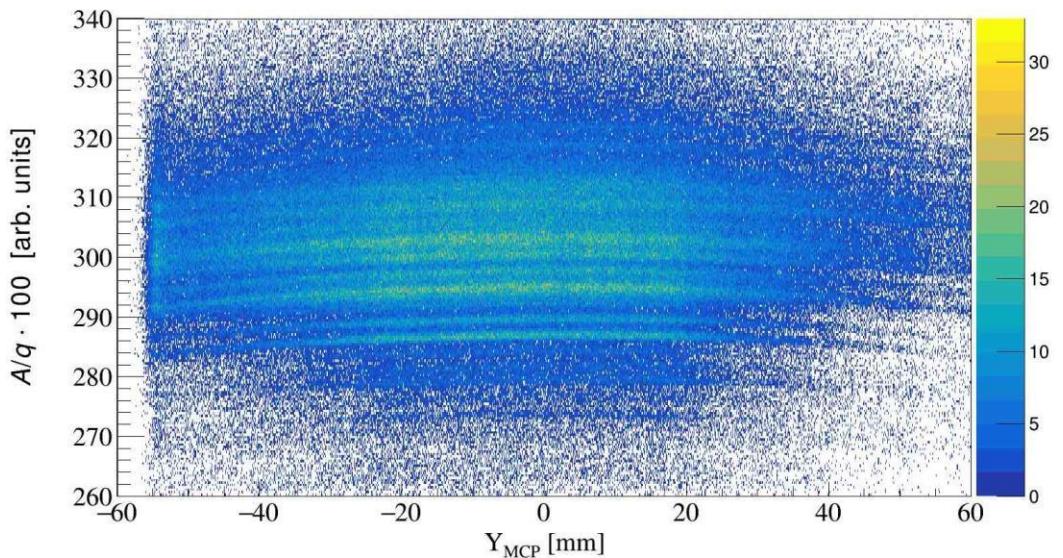
$$p = mv, \quad E_k = \frac{1}{2}mv^2, \quad v = \beta c$$

$$E_k \propto q \cdot \rho\beta$$

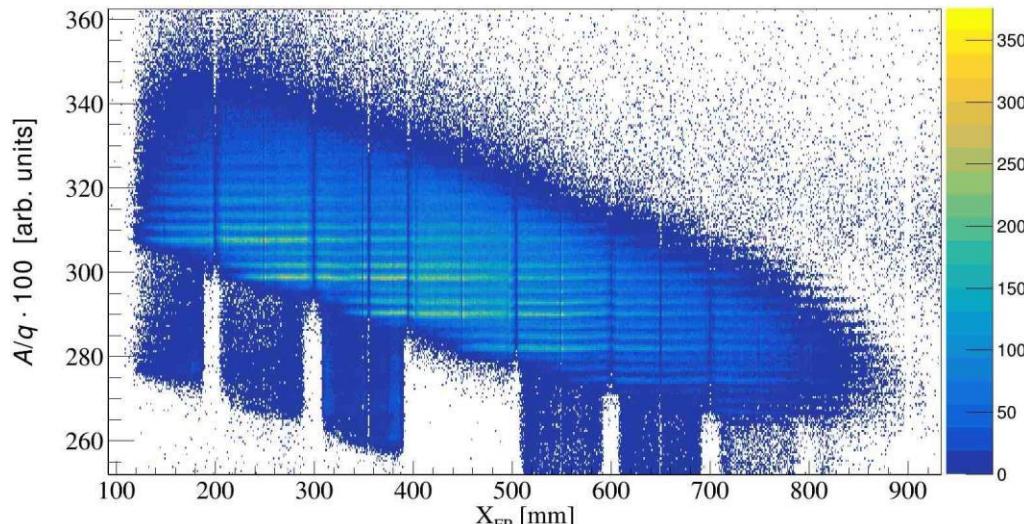
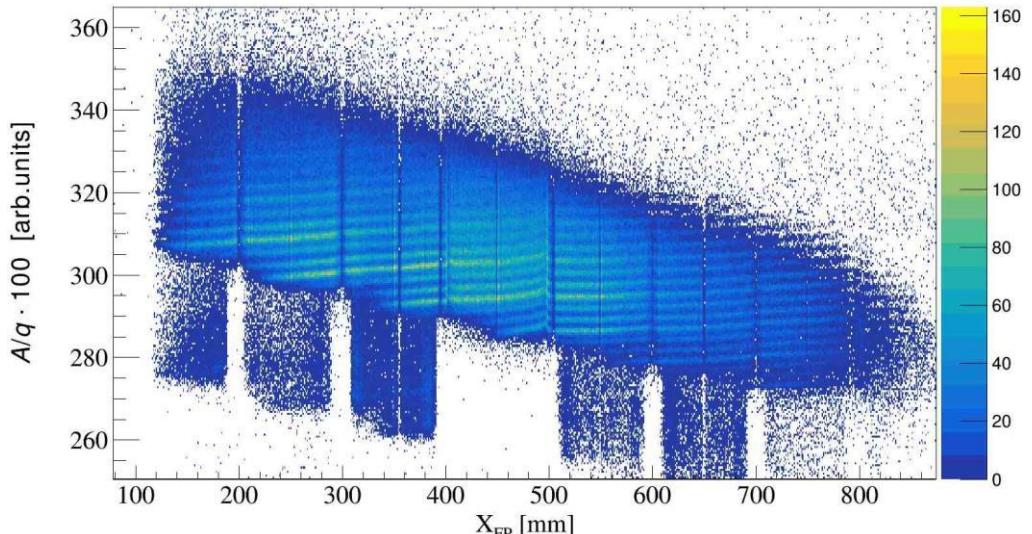
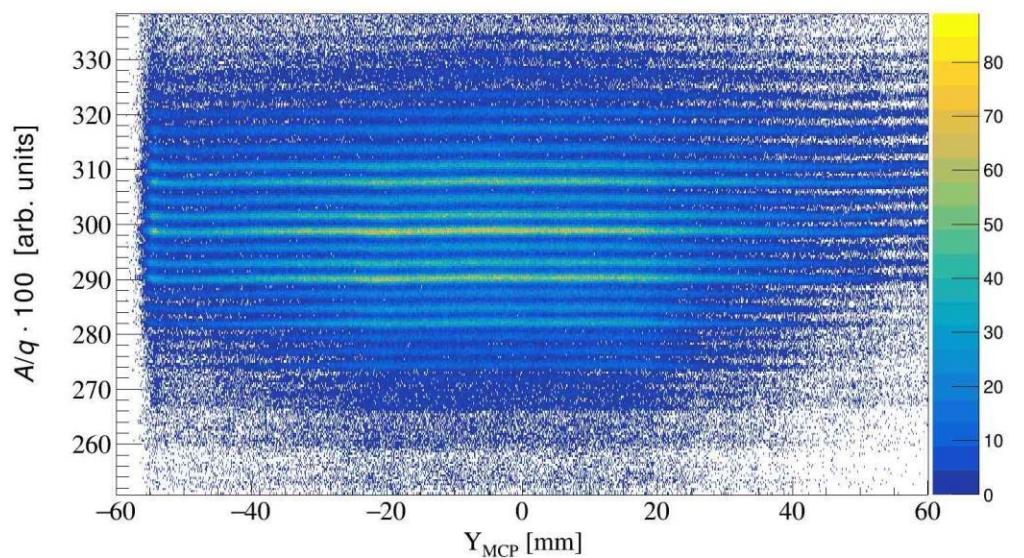


# PRISMA - A/q calibration

Before Aberrational corrections

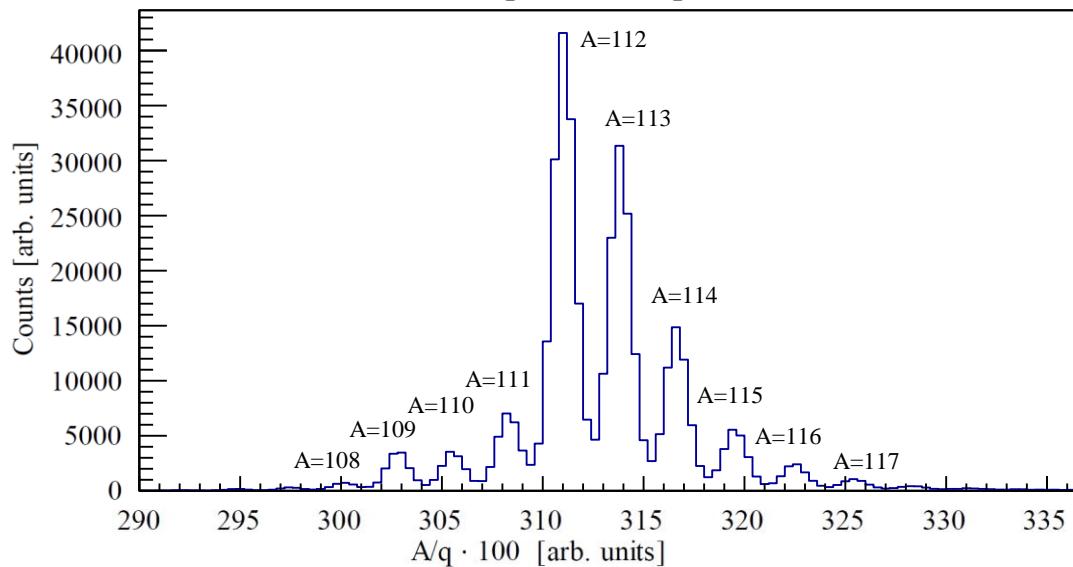


After aberrational corrections

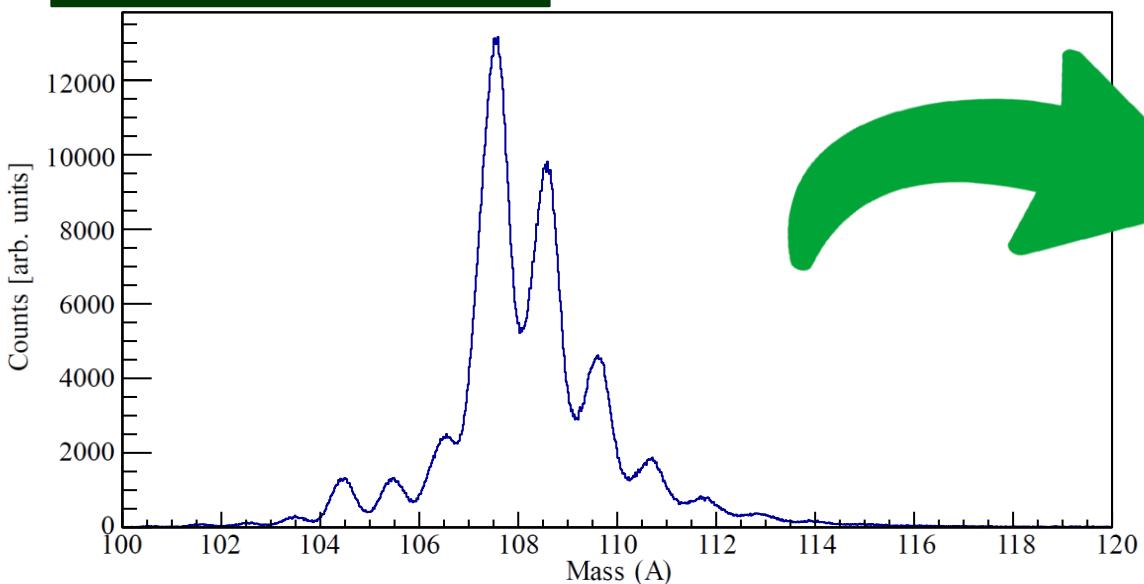


# PRISMA - Mass calibration

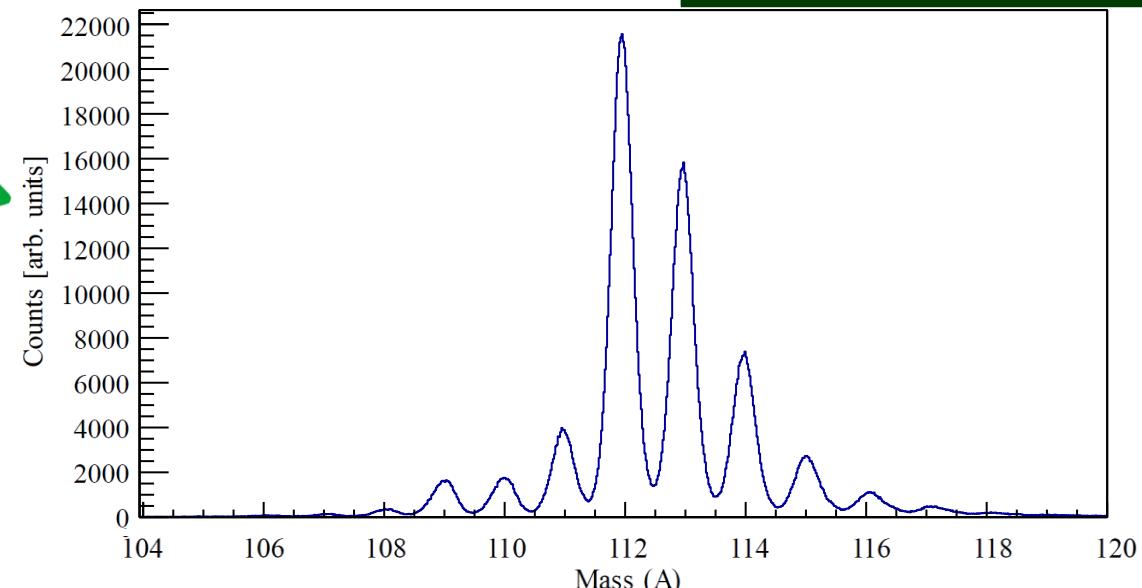
$A/q$  ( $Z = 50, q = 36$ )



Mass ( $Z = 50$ ) before linear calibration

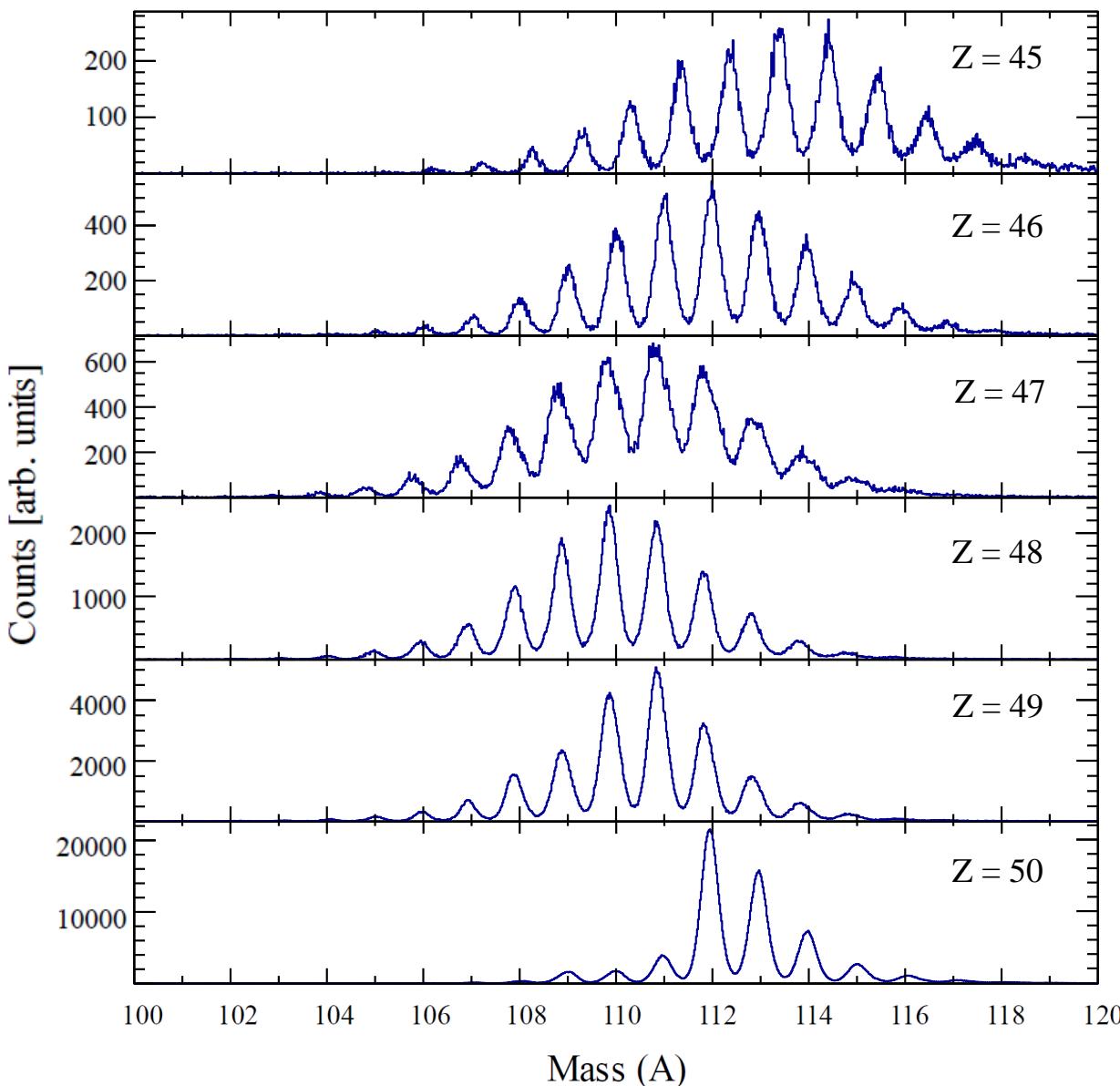


Mass ( $Z = 50$ ) after linear calibration



$A/q$  linear calibration applied by measuring centroid of  $ZQ$ -gated 1D  $A/q$  distributions and comparing observed with expected.

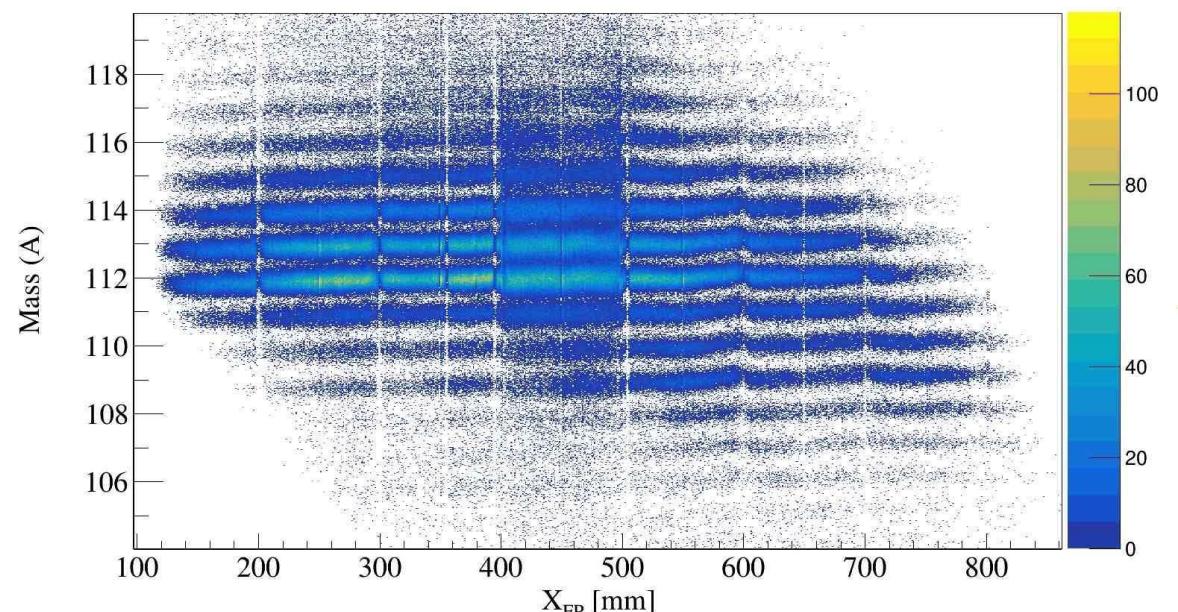
# PRISMA - Mass distributions



Mass  
resolutions

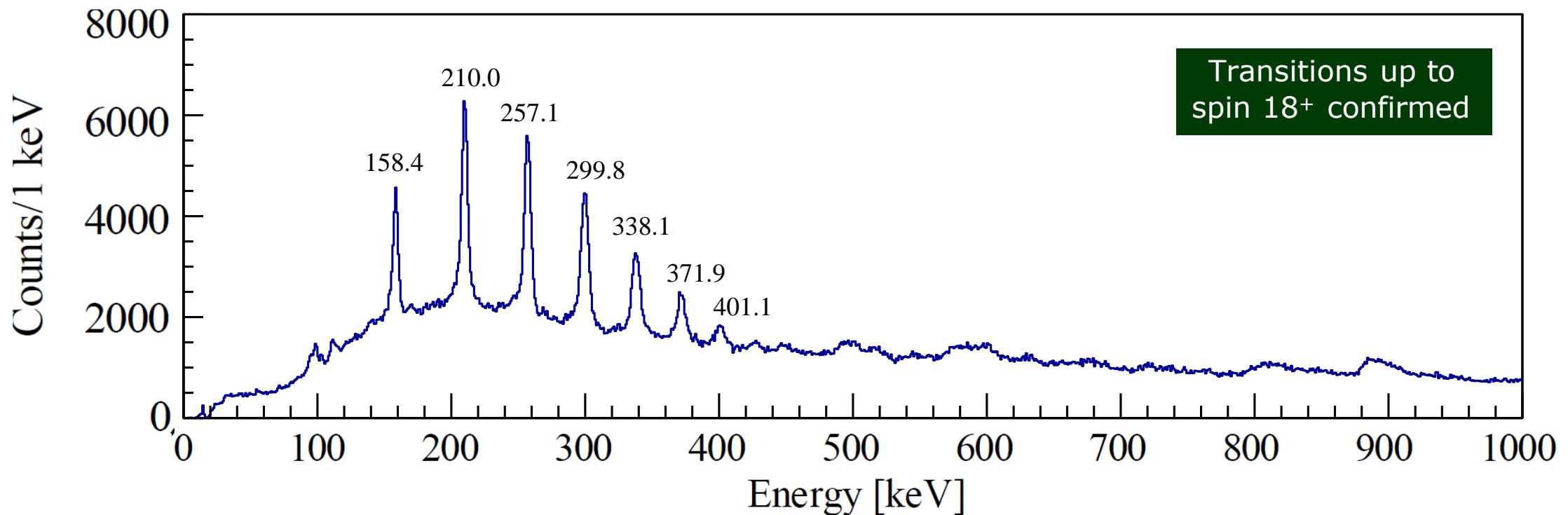
$$\begin{aligned}Z = 50 &\rightarrow \frac{1}{250} \\Z = 49 &\rightarrow \frac{1}{231} \\Z = 48 &\rightarrow \frac{1}{229}\end{aligned}$$

Mass assignments are gated on to look at coincidence gamma-ray spectra either using 2D gate or rounding to nearest integer.



# Preliminary Analysis results – AGATA

AGATA-PRISMA coincidence spectra Analysis ongoing



$^{238}\text{U}$  Doppler-corrected tracked  $\gamma$ -ray spectra gated on binary partner Sn ( $Z = 50$ ,  $A=112$ ).

# Summary

## With thanks to all collaborators:

H. Ayatollahzadeh <sup>1, 2</sup>, J. M. Keatings <sup>1, 2</sup>, J. F. Smith <sup>1, 2</sup>, D. Mengoni <sup>3</sup>, P. Aguilera <sup>3, 4</sup>, G. Andreetta <sup>3, 5</sup>, F. Angelini <sup>3, 4</sup>, M. Balogh <sup>4</sup>, J. Benito <sup>3, 4</sup>, M. A. Bentley <sup>6</sup>, A. J. Boston <sup>7</sup>, H. C. Boston <sup>7</sup>, S. Bottoni <sup>8, 9</sup>, M. Bowry <sup>1, 2</sup>, P. A. Butler <sup>7</sup>, D. Brugnara <sup>4</sup>, S. Carollo <sup>3</sup>, G. Corbari <sup>8</sup>, L. Corradi <sup>4</sup>, R. Escudeiro <sup>5</sup>, P. T. Greenlees <sup>10</sup>, R. Chapman <sup>1, 2</sup>, D. M. Cullen <sup>1, 2</sup>, G. de Angelis <sup>4</sup>, A. Ertoprak <sup>4</sup>, C. Everett <sup>7</sup>, L. P. Gaffney <sup>7</sup>, F. Galtarossa <sup>5</sup>, A. Goasduff <sup>4</sup>, B. Góngora Servián <sup>4, 11</sup>, A. Gottardo <sup>4</sup>, A. Gozzelino <sup>4</sup>, J. Hackett <sup>7</sup>, S. D. Hart <sup>12</sup>, F. Holloway <sup>7</sup>, P. M. Jones <sup>12</sup>, S. Jongile <sup>12</sup>, D. Judson <sup>7</sup>, M. Labiche <sup>13</sup>, M. S. R. Laskar <sup>9</sup>, K. L. Malatji <sup>12</sup>, A. McCarter <sup>7</sup>, G. Montagnoli <sup>3</sup>, N. Marchini <sup>14</sup>, B. S. Nara Singh <sup>1, 2</sup>, D. R. Napoli <sup>4</sup>, R. Nicolás del Álamo <sup>3, 5</sup>, D. O'Donnell <sup>1, 2</sup>, J. Pellumaj <sup>4</sup>, R. Pérez <sup>4</sup>, S. Pigliapoco <sup>3</sup>, E. Pilotto <sup>5</sup>, M. Polettini <sup>3</sup>, F. Recchia <sup>3</sup>, K. Rezynkina <sup>4</sup>, E. Rintoul <sup>7</sup>, M. Rocchini <sup>14</sup>, M. Sedlak <sup>4</sup>, M. Siciliano <sup>15</sup>, A. Stefanini <sup>4</sup>, D. Stramaccioni <sup>3, 4</sup>, C. Sullivan <sup>7</sup>, J. J. Valliente-Dobon <sup>4</sup>, F. van Niekerk <sup>12</sup>, L. Zago <sup>3, 4</sup>, and I. Zanon <sup>4</sup>.

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<sup>12</sup>iThemba LABS, National Research Foundation, PO Box 722, Somerset West 7129, South Africa

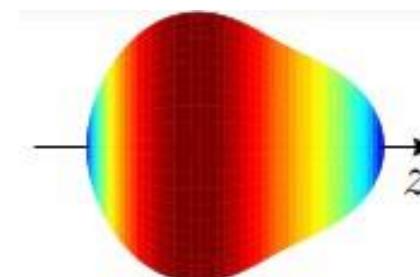
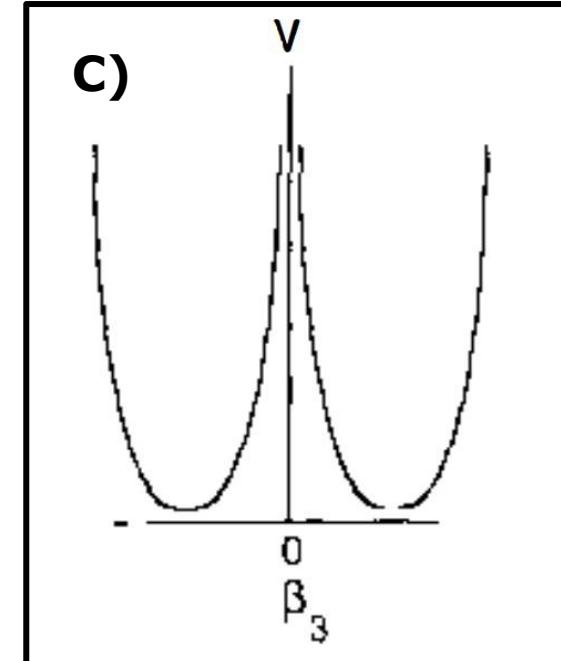
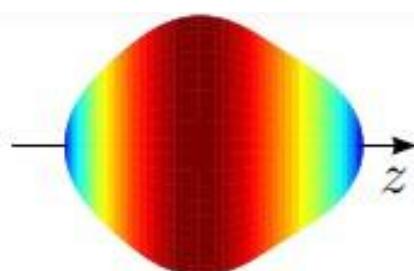
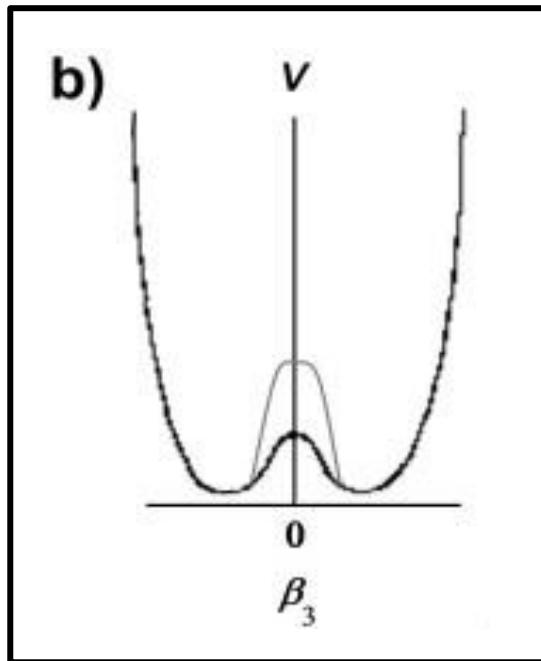
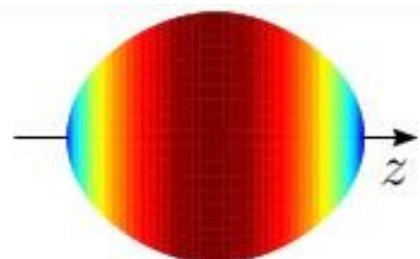
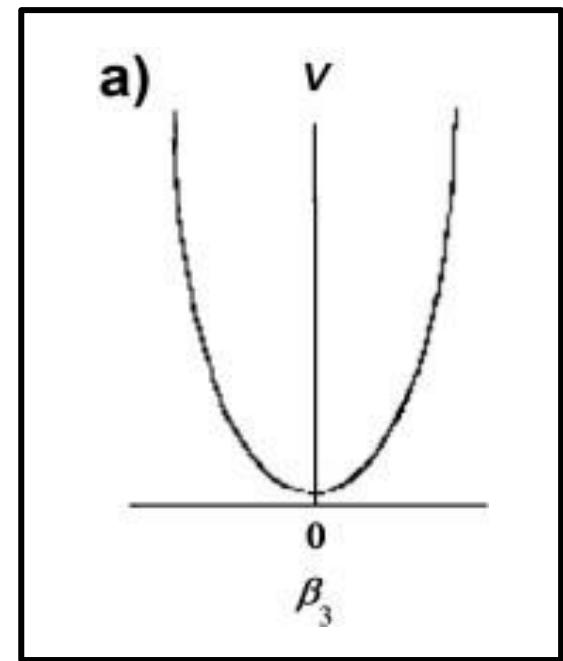
<sup>13</sup>STFC Daresbury Laboratory, Daresbury, Warrington WA44AD, United Kingdom

<sup>14</sup>INFN Sezione di Firenze, IT-50019 Firenze, Italy

<sup>15</sup>Physics Division, Argonne National Laboratory, Argonne, USA

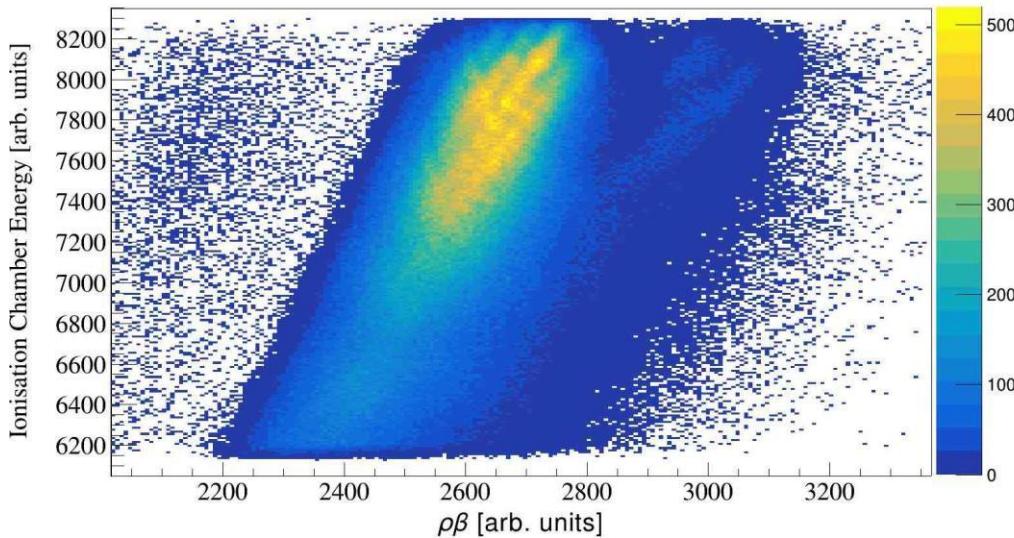
# Spectroscopic features of octupole deformation

Angular momentum increasing

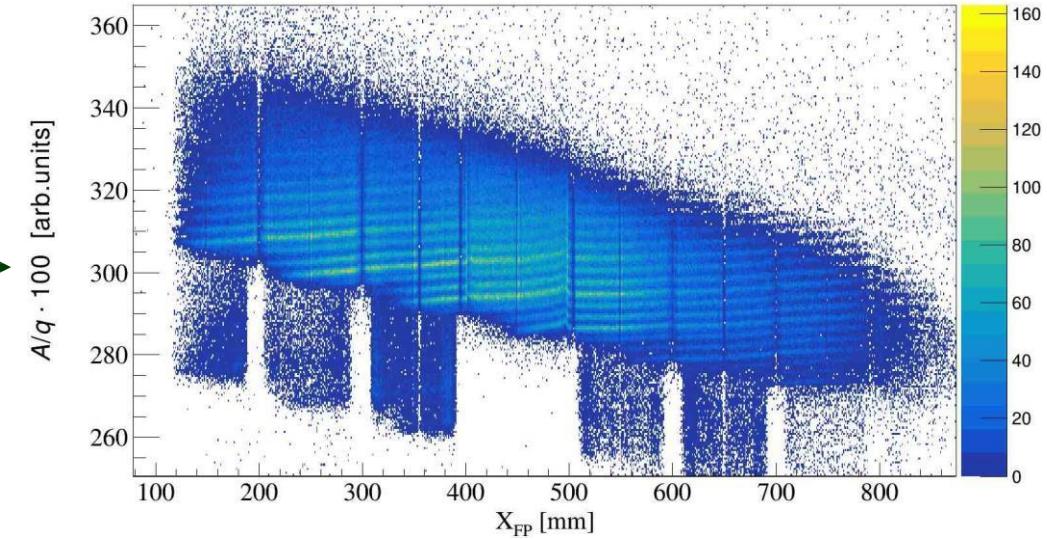
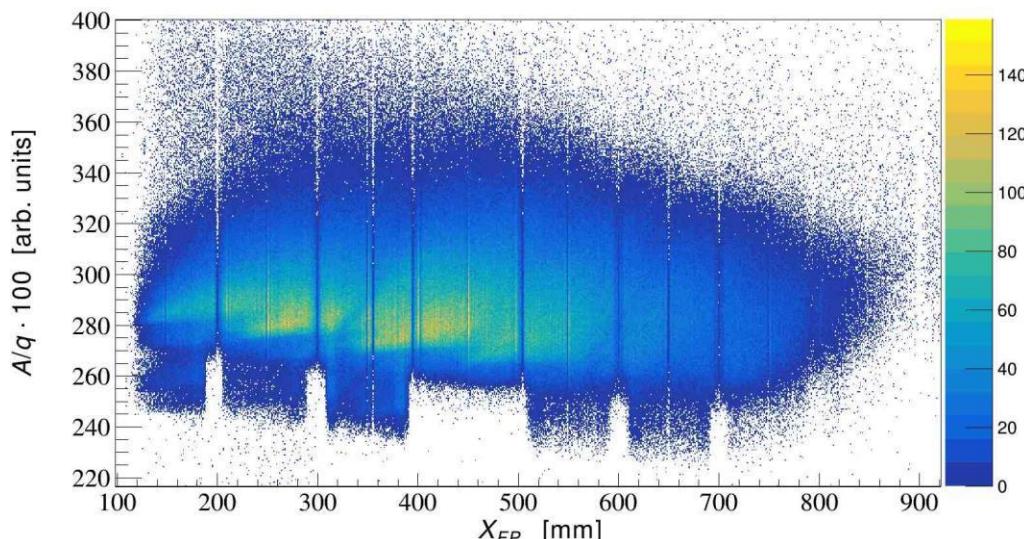
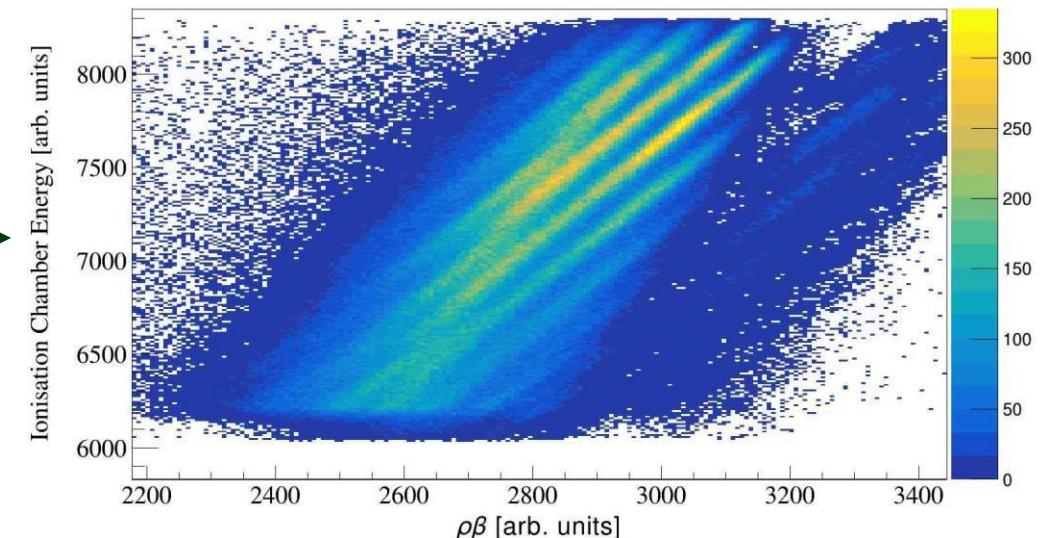


# PRISMA – Trajectory reconstruction

Bad optical parameters



Good optical parameters



# Forward tracking vs. backtracking

