

International
UON Collider
Collaboration



Optimization of inner and outer joint for stress management

C. Accettura,

With several contributions from A. Bertarelli, B. Bordini, L. Bottura, A.
Dudarev, A. Kolehmainen, F. Sanda

Final Cooling Solenoid Progress Meeting

<https://indico.cern.ch/event/1390332/>

15/03/2024, CERN

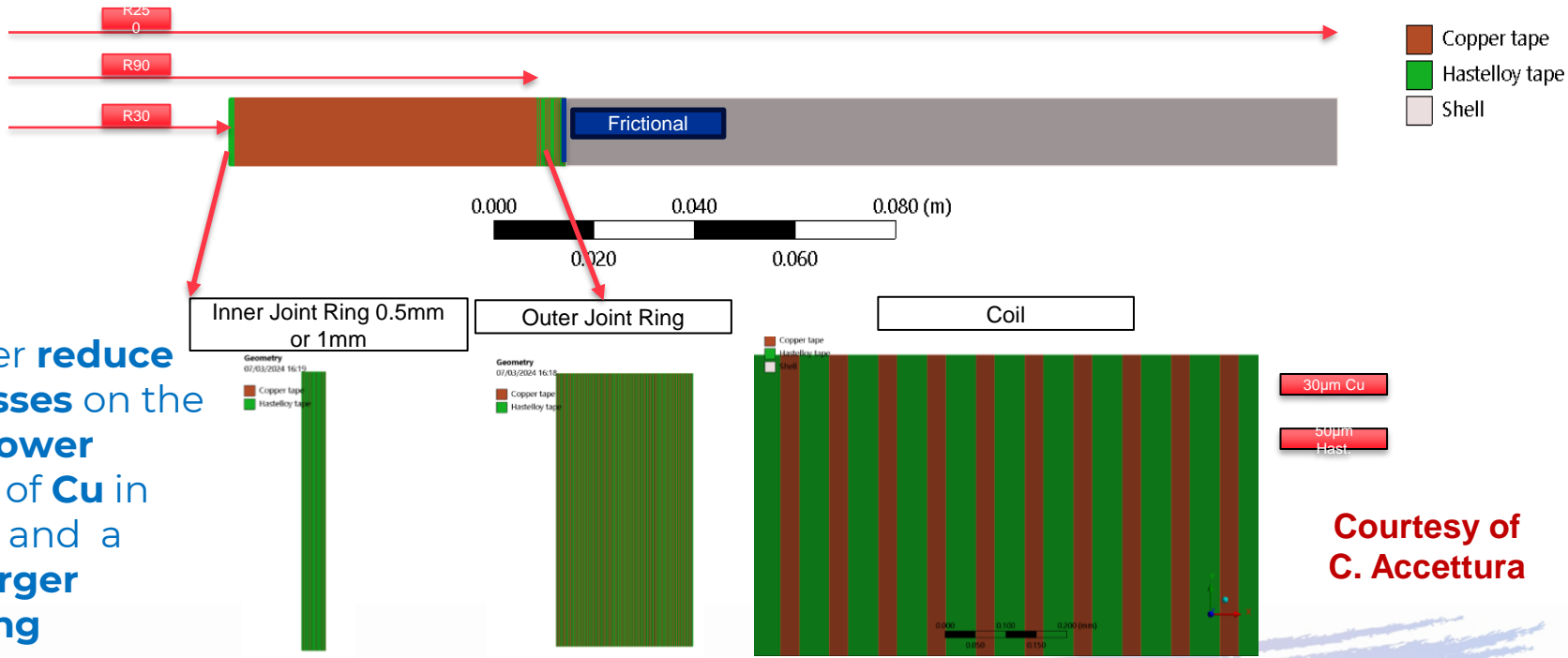
Index

- Review of the model presented at the IMCC2024
- Alternatives

From Annual Meeting
13.03.2024 B. Bordini et al.

2D FEM : geometry

- Mechanical **Simulation of a modular coil: all 750 windings are represented**
- The model **accounts for: Cu yielding** and; the **thermal contractions** of the different materials



- To further **reduce** the **stresses** on the coils, a **lower amount of Cu** in the tape and a much **larger outer-ring thickness**

Courtesy of
C. Accettura

From Annual Meeting
13.03.2024 B. Bordini et al.

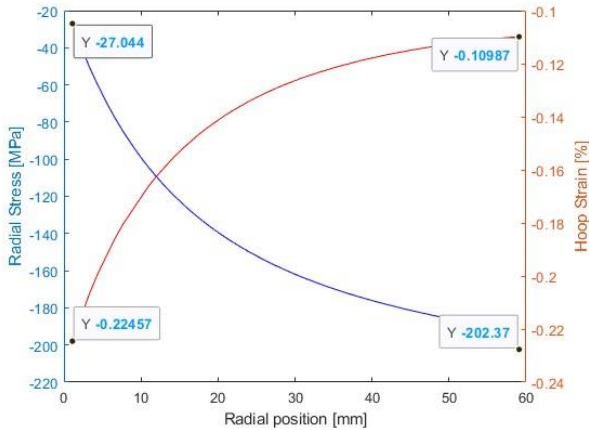
EM : Stress-Strain Profiles

Courtesy of C. Accettura

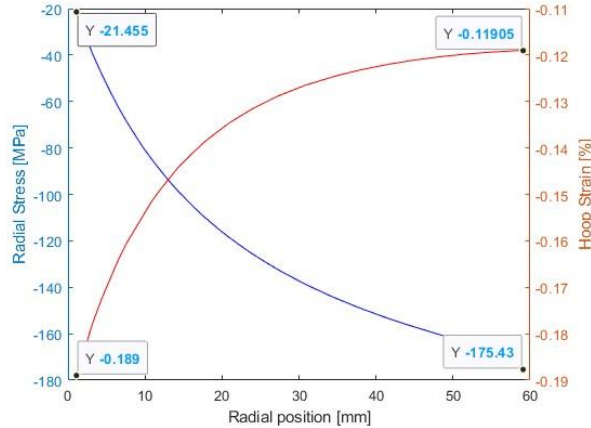
Pre-compression
170 MPa

Inner Joint ring
1 mm thick

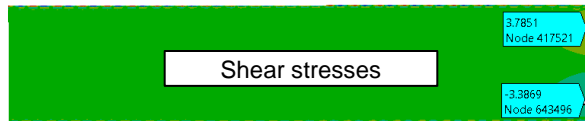
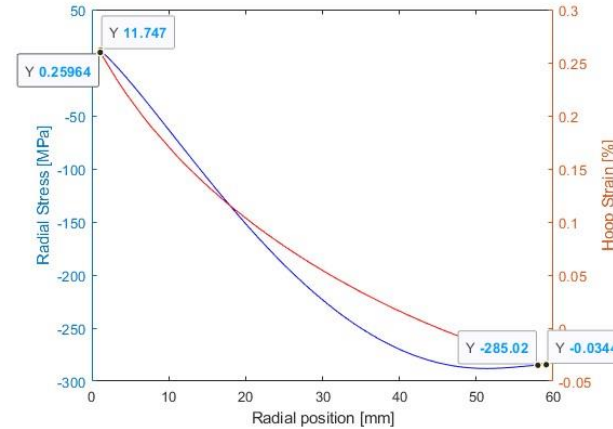
Step 1



Step 2



Step 3



Shear stresses



Mechanical Analysis

From Annual Meeting
13.03.2024 B. Bordini et al.

FEM : four Case Studies

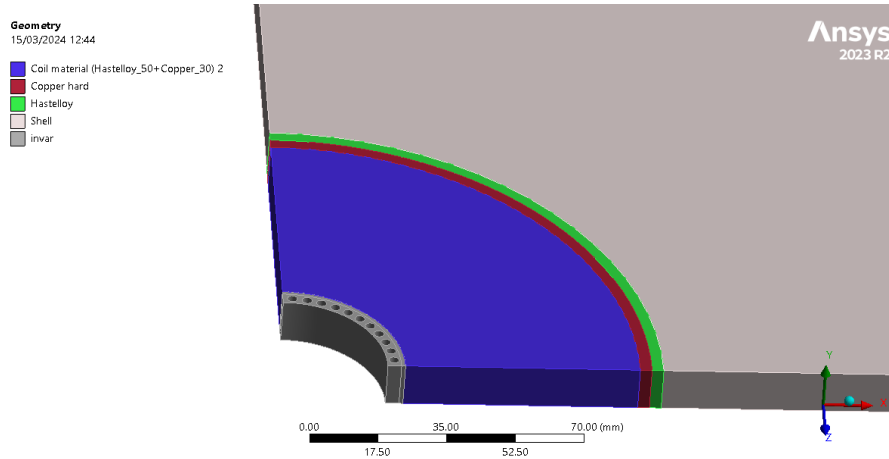


Inner Joint ring thickness [mm]	Pre-compression at cold [MPa]	Radial stress[MPa]			Hoop Strain [%]			Shear Stress [MPa]		
		Step 1	Step 2	Step 3	Step 1	Step 2	Step 3	1	2	3
0.5	170	-205/-8	-190/-5	-290/10	-0.25/-0.10	-0.20/ -0.12	-0.04/ 0.28	6	4.5	4
	250	-318/-12	-258/-8	-367/7	-0.39/-0.17	-0.31/-0.16	-0.09/ 0.18	10	6	5
1	170	-205/-14	-190/-10	-288/19	-0.25/-0.10	-0.2/-0.12	-0.05/ 0.29	6	4	5
	250	-320/-21	-259/-15	-366/13	-0.39/-0.17	-0.3/-0.16	-0.09/ 0.18	10	6	5

Courtesy of C. Accettura

Alternative model

■ Invar ring with channels for cooling



Alternative model

- Stresses → radial tensile ok, but high shear during the cool-down

Y: Copy of Copy of correct material_optimized_with_channels_axysym_1/4_sym_Homogeneous_30mCu

X Axis - Normal Stress - Coil - 3, s

Type: Normal Stress(X Axis)

Unit: MPa

Coordinate System: 3

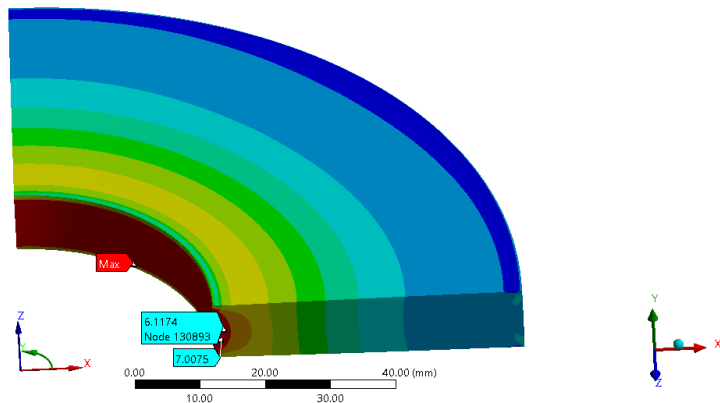
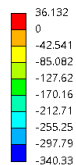
Time: 3 s

Custom

Max: 36.132

Min: -340.33

15/03/2024 13:49



Y: Copy of Copy of correct material_optimized_with_channels_axysym_1/4_sym_Homogeneous_30mCu

XY Component - Shear Stress - Coil - 1, s 3

Type: Shear Stress(XZ Component)

Unit: MPa

Coordinate System: 3

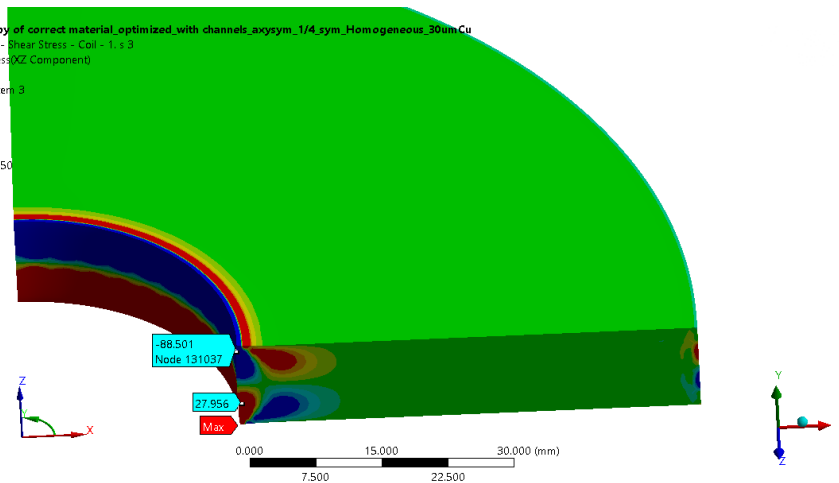
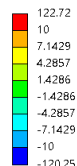
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Custom

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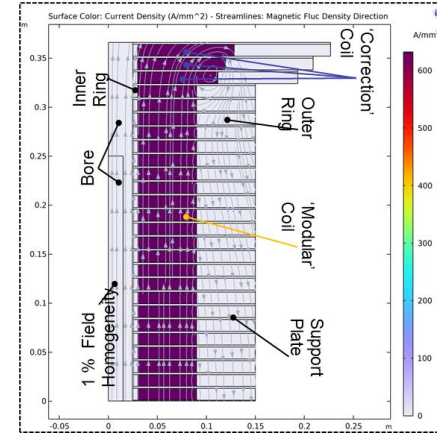
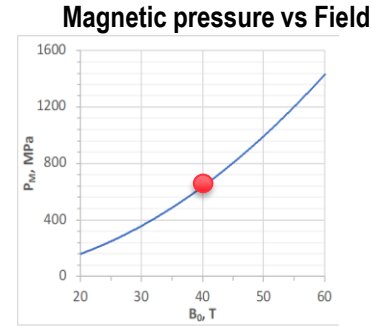
Min: -120.25

15/03/2024 13:50



Introduction and Motivations

- Design proposed for the Final Cooling solenoid based on single and compact coil → critical stress management:
 - $P_M = B_0^2 / 2\mu_0 \sim 600 \text{ MPa}$
 - Hoop stress $\sim 1.4\text{-}2.2P_M$ (compact coil)

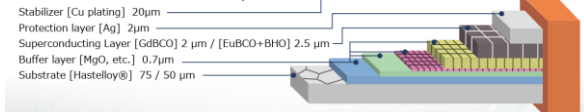


See [B. Bordini, Technology options for the final cooling solenoids, IMCC Annual Meeting 2023, Orsay](#)

Introduction and Motivations

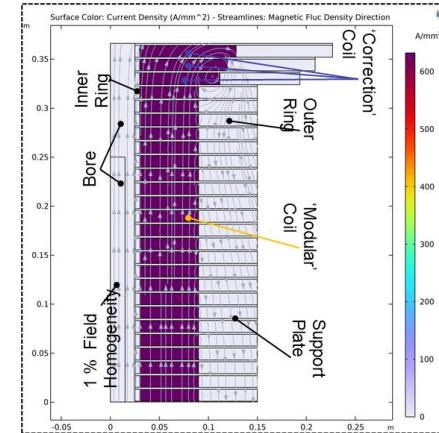
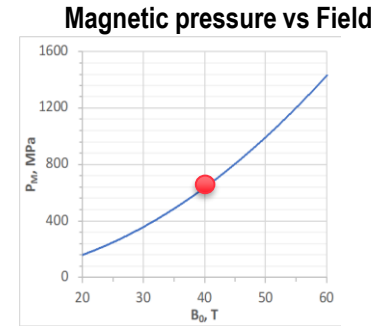
- Design proposed for the Final Cooling solenoid based on single and compact coil → critical stress management:
 - $P_M = B_0^2 / 2\mu_0 \sim 600\text{MPa}$
 - Hoop stress $\sim 1.4\text{-}2.2P_M$ (compact coil)
- Non-homogeneous and anisotropic material:
 - Maximum allowable stress very weak in certain direction
 - Scarce literature
 - Reduced safety margin

<Schematic of RE-based HTS tape>



Reference Conductor Fujikura FESC-SH12.

<https://www.fujikura.co.jp/eng/products/newbusiness/superconductors/01/superconductor.pdf>



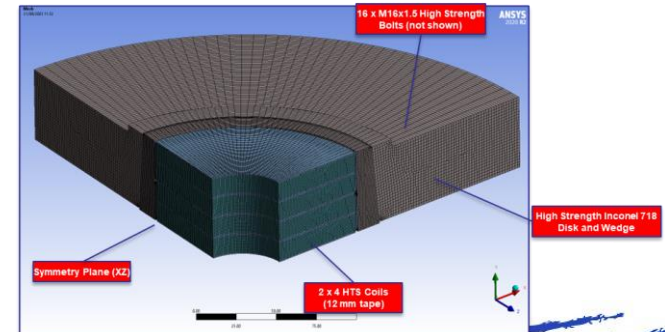
See [B. Bordini, Technology options for the final cooling solenoids, IMCC Annual Meeting 2023, Orsay](#)

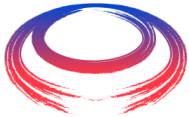
REBCO conductor	
Axial tensile stress	700MPa
Axial tensile strain	0.4%
Transverse compressive stress	>100MPa
Transverse tensile stress	10-100MPa
Max shear stress	>19MPa

- A pre-compression of $\sim 200\text{MPa}$ is needed to remain below this value

Pre-compression

- How to obtain the pre-compression?
- Mechanical concept is based on **encapsulating** HTS pancake coils in an **external structure**, generating high **radial compressive stresses**. **Three concepts analysed:**
 1. Thermally-induced shrink fitting
 2. Adjustable shrink-discs with conical surfaces
 3. Hybrid solution (1+2)





Shrink Fitting



- Coil surrounded by a cylindrical shell with $r_{in_shell} < r_{ext_coil}$
- Shell is pre-heated → fitting of the coil inside → cool-down of the shell and thermal contraction
- Simple analytical evaluation: $\sigma_{hoop} = 500\text{MPa} \rightarrow 200\text{MPa} \rightarrow \text{interference gap } \sim 220\mu\text{m} \rightarrow T_{shell} \sim 170^\circ\text{C}$

$$\sigma_{\theta} = -\frac{\rho^2 + \beta^2}{\rho^2} \frac{1}{1 - \beta^2} P_e$$

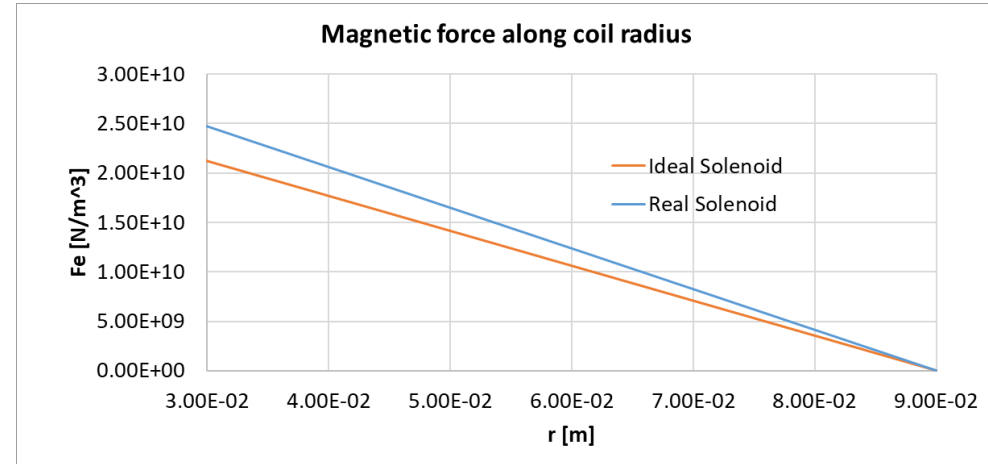
$$\delta = \delta_{i2} - \delta_{e1} = \left[\frac{1}{E_2} \left(\frac{1 + \beta_2^2}{1 - \beta_2^2} + \nu_2 \right) + \frac{1}{E_1} \left(\frac{1 + \beta_1^2}{1 - \beta_1^2} - \nu_1 \right) \right] r_{e1} P_f$$

- Some practical aspects must be considered:
 - Differential contraction during cooldown
 - Strength of the cylinder
 - Impact of the joints
 - Plasticity
 - Mechanical tolerances: 1MPa/μm lost
 - Buckling
- FEA simulations at different levels of complexity

Assumptions

- 2D axisymmetric
- Electromagnetic Forces

- Ideal Solenoid ($J_{ideal} = \frac{B_{MAX}}{\mu_0(r_{co} - r_{ci})} = 531 \text{ A/mm}^2$)
- Real Solenoid ($J_{real} = J_{ideal} \frac{t_{coil} + t_{supportplate}}{t_{coil}} = 620 \text{ A/mm}^2$)



All
Unit: N/mm³
Max: 22.343
Min: 0
06/12/2023 09:49

22.343
19.86
17.378
14.895
12.413
9.9302
7.4477
4.9651
2.4826
0

Force Density



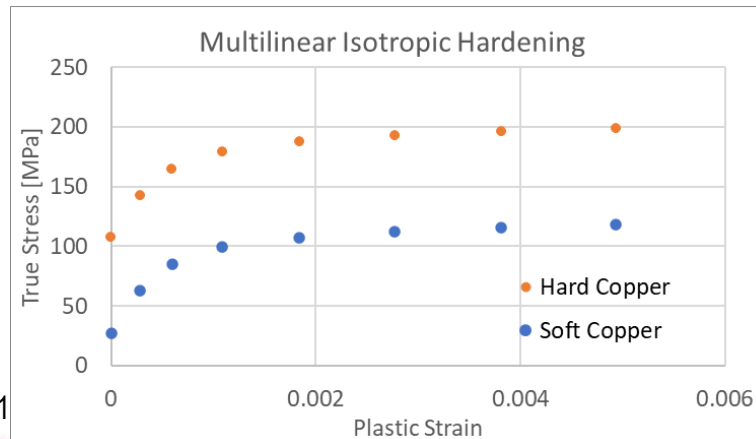
Reference model

- Coil material (Hastelloy_50+Copper_30)
- Copper hard
- Copper soft
- Hastello
- Shell

Homogeneous
tape properties


Needed to keep the pre-compression.
Soft copper was resulting in a lower
pre-compression

Ha to avoid radial tensile and
shear stress after cooldown



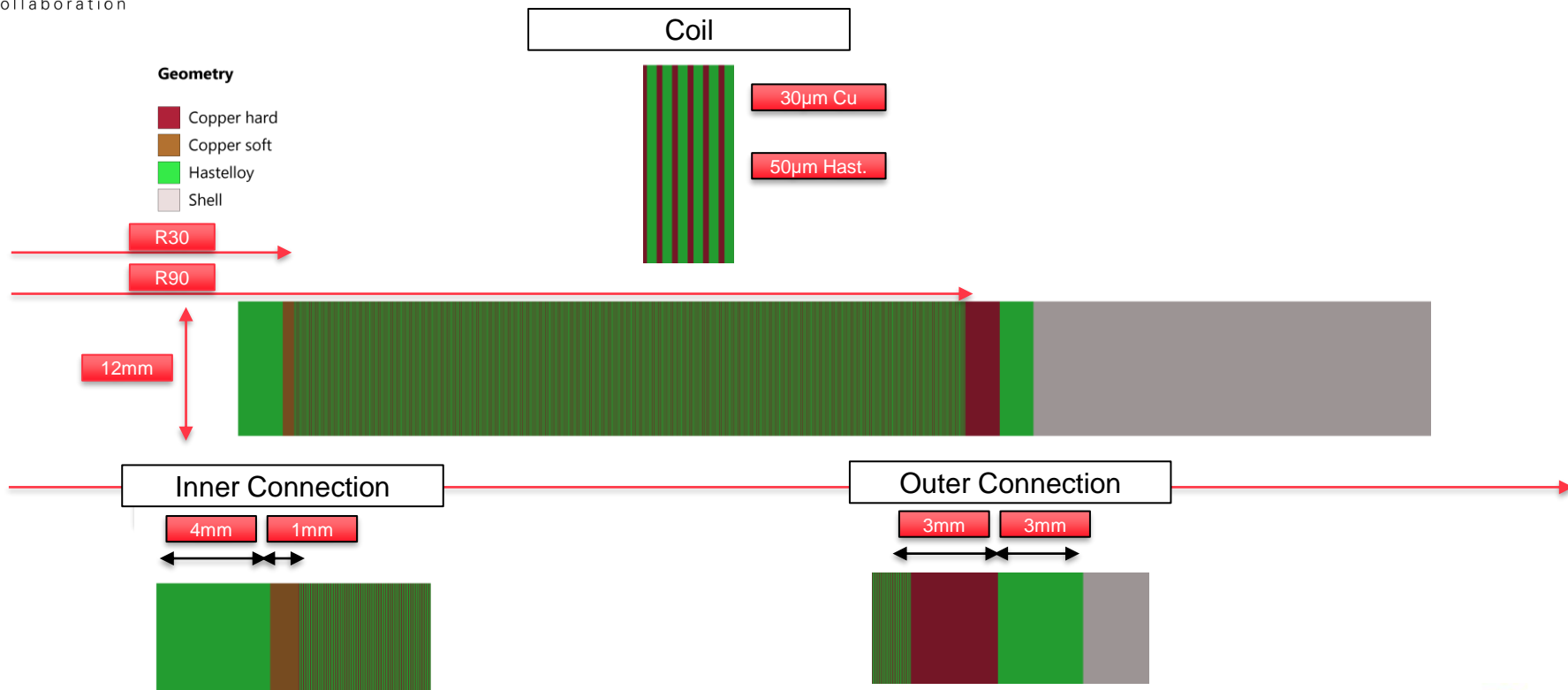
Layered model

Geometry

-  Copper hard
-  Copper soft
-  Hastelloy
-  Shell



Geometry and Materials



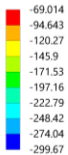
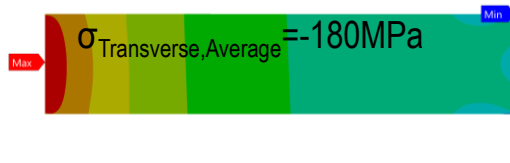
Validity of homogeneous model



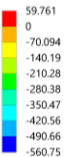
Step 1: Shrink fitting (T external shell =250°C)

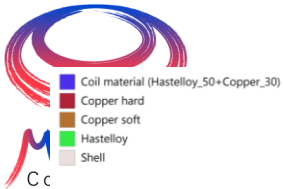
$$\sigma_{\text{Transverse,Average}} = -210\text{MPa}$$

Step 2: Cool-down



Step 3: Energization





Validity of homogeneous model

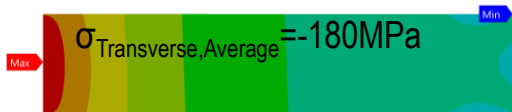
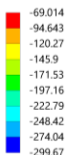


Step 1: Shrink fitting

$$\sigma_{\text{Transverse,Average}} = -210\text{MPa}$$

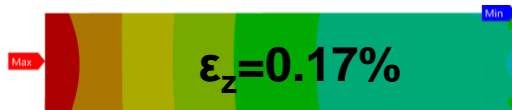
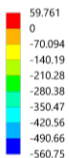
Step 2: Cool-down

$$\sigma_{\text{Transverse,Average}} = -180\text{MPa}$$



Step 3: Energization

$$\epsilon_z = 0.17\%$$



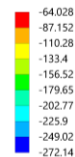
750 layers: 30μm+50 μm

Step 1: Shrink fitting

$$\sigma_{\text{Transverse,Average}} = -215\text{MPa}$$

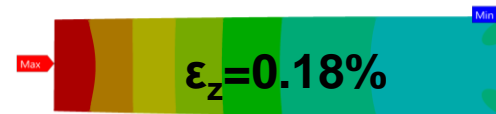
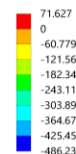
Step 2: Cool-down

$$\sigma_{\text{Transverse,Average}} = -170\text{MPa}$$



Step 3: Energization

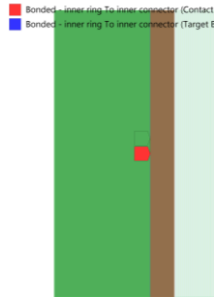
$$\epsilon_z = 0.18\%$$



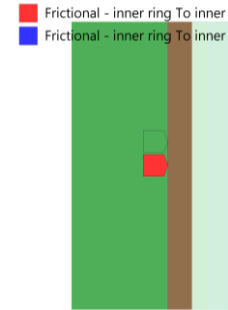
Press Meeting, 15/03/2024

0,000 10,000 20,000 (mm)

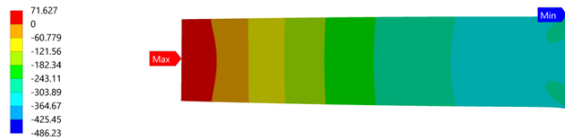
Effect of the inner joint properties



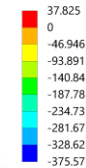
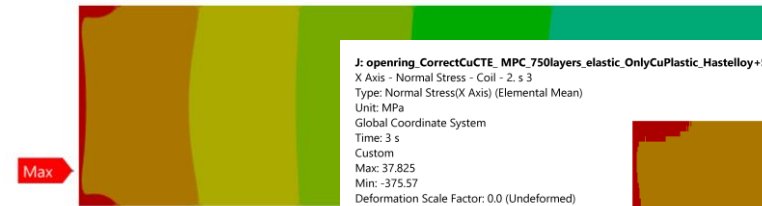
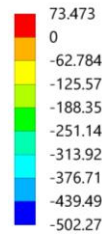
Let the ring detach to limit radial tensile stress



G: CorrectCuCTE_MPC_750layers_elastic_OnlyCuPlastic_Hastelloy+SoftCu INSIDE_HardCu+Hastelloy OUTSIDE_Orthotropic_1supportfrictionless_FRICTIONLESS_2D_axial
 X Axis - Normal Stress - All layer + 1 - 3.s
 Type: Normal Stress(X Axis)
 Unit: MPa
 Global Coordinate System
 Time: 3 s
 Custom
 Max: 71.627
 Min: -486.23
 Deformation Scale Factor: 56 (5x Auto)
 06/12/2023 10:04



Max: 73.473
 Min: -502.27
 Deformation Scale Factor: 0.0 (Undeformed)
 06/12/2023 11:52



Effect of the tape plasticity

step	σ_x -radial[MPa]			ϵ_z -hoop
	min	max	ave	max
1	-289	-57	-210	
2	-224	-67	-164 (200*)	
3	-416	77	-213	0.30%
1	-308	-54	-214	
2	-272	-63	-171 (210*)	
3	-502	73	-224	0.22%

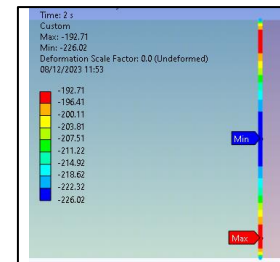
Plastic

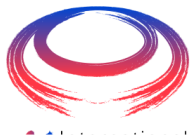
Elastic

L: opening_CorrectCuTE MPC_750layers_plastic_OnlyCuPlastic_Hastelloy+SoftCu INSIDE_HardCu+Hastelloy OUTSIDE_Orthotropic_1supportfrictionless_FRICTIONLESS_2D_axisym_1coil_cor
 X Axis - Normal Stress - All layer=1 - 3, s
 Type: Normal Stress(X Axis)
 Unit: MPa
 Global Coordinate System
 Time: 3 s
 Custom Obsolete
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 Min: -415.95
 Deformation Scale Factor: 56 (5x Auto)
 06/12/2023 12:07



*Average on the external edge





Effect of the tape properties



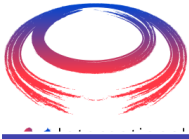
step	σ_x -radial[MPa]			ε_z -hoop
	min	max	ave	max
1	-291	-55	-208	
2	-264	-60	-171 (215*)	
3	-484	75	-218	0.24%
1	-289	-57	-210	
2	-224	-67	-164 (200*)	
3	-416	77	-213	0.30%

*Average on the external edge

Experiments and FE modeling of stress–strain state in ReBCO tape under tensile, torsional and transverse load

To cite this article: K Ilin et al 2015 *Supercond. Sci. Technol.* **28** 055006

Reference

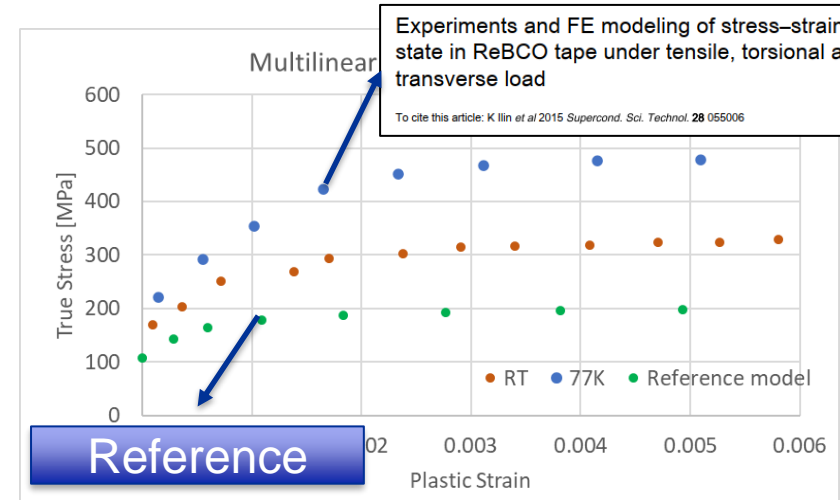


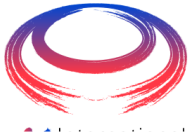
Effect of the tape properties



step	σ_x -radial[MPa]			ϵ_z -hoop
	min	max	ave	max
1	-291	-55	-208	
2	-264	-60	-171(215*)	
3	-484	75	-218	0.24%
1	-289	-57	-210	
2	-224	-67	-164 (200*)	
3	-416	77	-213	0.30%

*Average on the external edge





Effect of the tape properties

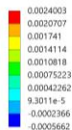


step	σ_x -radial[MPa]			ϵ_z -hoop
	min	max	ave	max
1	-291	-55	-208	
2	-264	-60	-171(215)	
3	-484	75*	-218	0.24%

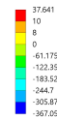
*Localized effect

$\epsilon_z=0.24\%$ ✓

$\sigma_x \sim 10\text{MPa}$ ✓



Deformation Scale Factor: 57 (St Auto)
08/12/2019 12:10



Alternative Inner Joint-1

Reduced Hastelloy (1mm-Bonded to Cu)

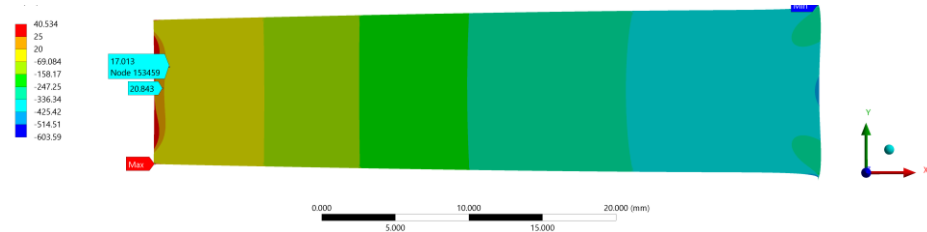
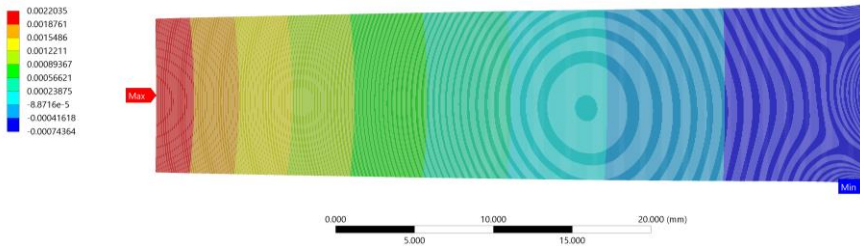
Geometry
01/02/2024 10:44

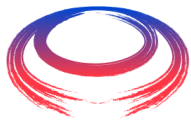
- Copper hard
- Copper soft
- Copper tape
- Hastelloy
- Hastelloy tape
- Shell



$\epsilon_z = 0.22\%$ ✓

$\sigma_x \sim 20\text{MPa}$
($p \sim 250\text{MPa}$)





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- Copper hard
- Copper tape
- Hastelloy
- Hastelloy ortho
- Hastelloy tape
- Shell

Alternative Inner Joint-2

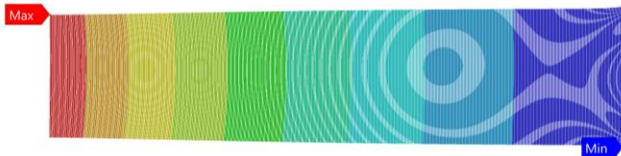
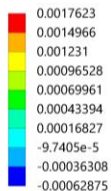


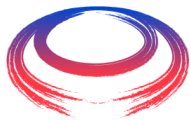
Hastelloy orthotropic	
Ex-radial[GPa]	Ey,z-hoop[GPa]
100	200



$\epsilon_z = 0.17\%$ ✔

$\sigma_x = 80\text{MPa}$ ✘



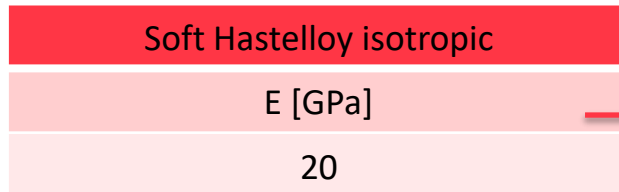


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Alternative Inner Joint-3

- Copper hard
- Copper tape
- Hastelloy
- Hastelloy tape
- Shell

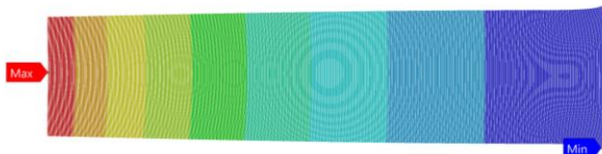
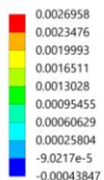


Model simplification, important to have a 3D design of the inner ring to take into account the real stiffness of the structure



$$\epsilon_z = 0.27\% \quad \checkmark$$

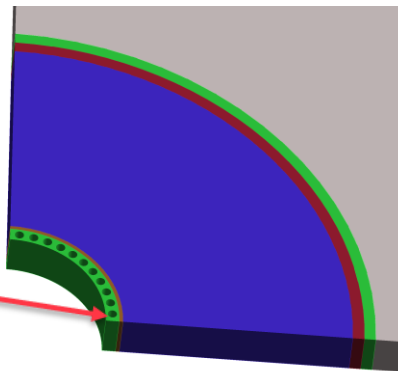
$$\sigma_x = 12\text{MPa} \quad \checkmark$$



Alternative Inner Joint-4

Geometry
01/02/2024 09:55

- Coil material (Hastelloy_50+Copper_30)
- Copper hard
- Copper soft
- Hastelloy
- Shell



3D model more time-consuming,
homogeneous material and mesh to be
refined → **INCREASE OF at least~50%**
expected

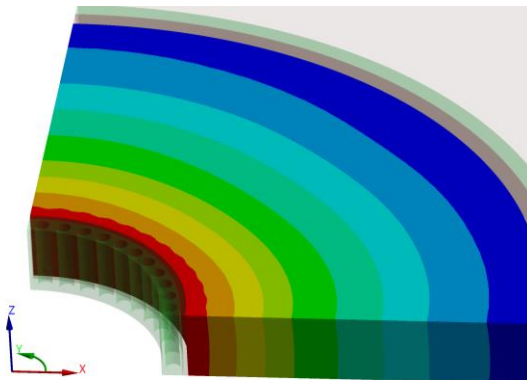
Cooling channel

$\epsilon_z = 0.18\%$

$\sigma_x < 20\text{MPa}$

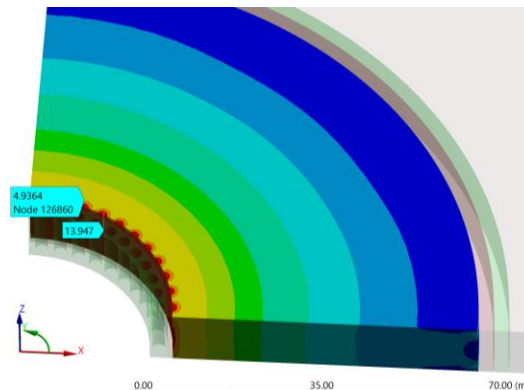
Type: Normal Elastic Strain(Y Axis)
Unit: mm/mm
Coordinate System 3
Time: 2 s
Max: 0.0018075
Min: -0.00038037
Deformation Scale Factor: 0.0 (Undeformed)
01/02/2024 10:00

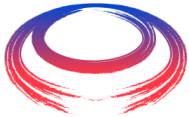
0.0018075
0.0015644
0.0013213
0.0010782
0.00083513
0.00059203
0.00034893
0.00010583
-0.00013727
-0.00038037



X Axis - Normal Stress - Coil - 3.s
Type: Normal Stress(X Axis)
Unit: MPa
Coordinate System 3
Time: 2 s
Custom
Max: 38.188
Min: -401.82
Deformation Scale Factor: 0.0 (Undeformed)
01/02/2024 09:56

38.188
10
0
-57.403
-114.81
-172.21
-229.61
-287.02
-344.42
-401.82





Shrink Fitting

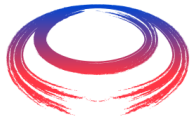


- Coil surrounded by a cylindrical shell with $r_{in} < r_{ext_coil}$
- Shell is pre-heated → fitting of the coil inside → cool-down of the shell and thermal contraction
- Simple analytical evaluation: 600MPa → 200MPa → interference gap $\sim 300\mu\text{m}$ → $\sim 250^\circ\text{C}$

$$\sigma_\theta = -\frac{\rho^2 + \beta^2}{\rho^2} \frac{1}{1 - \beta^2} P_e$$

$$\delta = \delta_{i2} - \delta_{e1} = \left[\frac{1}{E_2} \left(\frac{1 + \beta_2^2}{1 - \beta_2^2} + \nu_2 \right) + \frac{1}{E_1} \left(\frac{1 + \beta_1^2}{1 - \beta_1^2} - \nu_1 \right) \right] r_{e1} P_f$$

- Some practical aspects must be considered:
 - Differential contraction during cooldown
 - Strength of the cylinder
 - Impact of the joints
 - Plasticity
 - Mechanical tolerances: 2MPa/ μm lost**
 - Buckling**
- FEM simulations at different levels of complexity

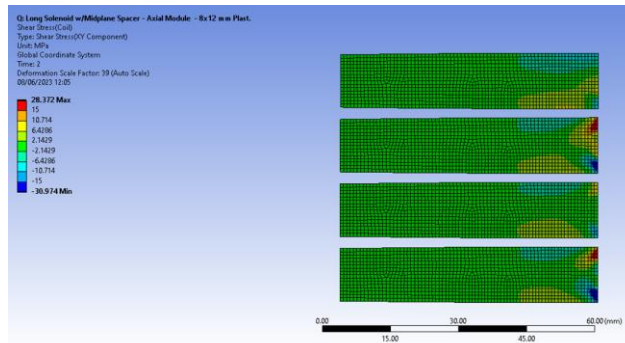
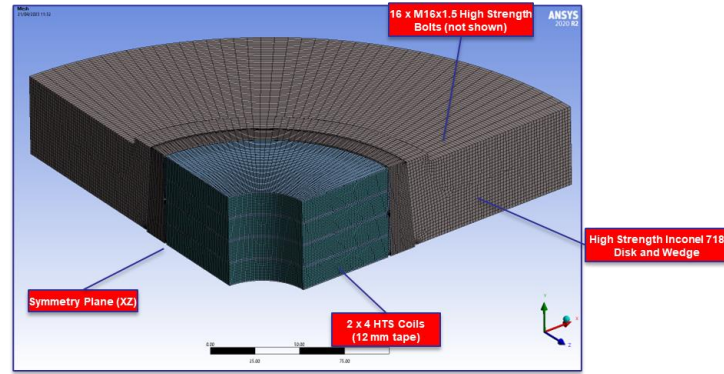


Mechanical considerations - Second concept



International
UON Collider
Collaboration

- 2 Load Steps:
 - Shrink Disk displacement (5 mm)
 - Energization
- Max. Hoop Stress (after energization): 620.4 MPa
- Max. Hoop Strain (after energization): 0.344 %
- Shear Stresses globally lower than 15 MPa
- However, locally they can reach after energization $\sim |30|$ MPa

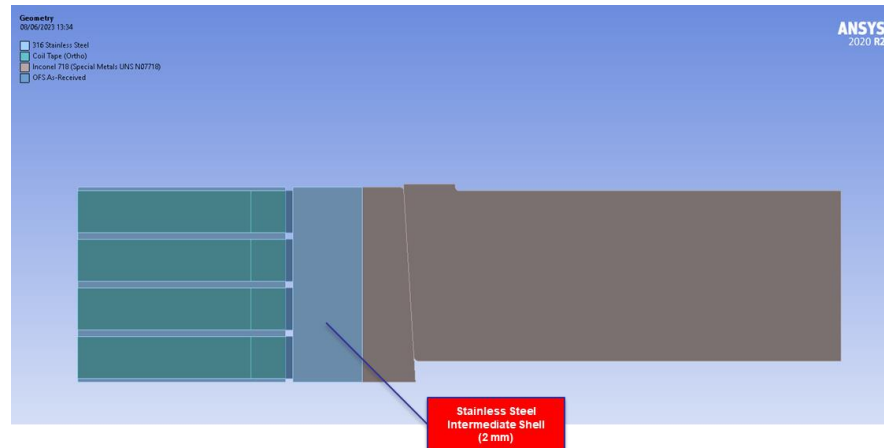




Mechanical considerations - Third concept



- To limit shear stresses, an intermediate steel shell is added (ID 184 mm; OD 224 mm)
- ~ 150 μm interference with coil pack created by differential heating
- 3 Load Steps: 1. Shell/Coil Interference; 2. Shrink Disk Displacement (2.2 mm); 3. Energization
- Min. Hoop Stress after shrinking: -426 MPa
- Max. Hoop Stress after energization: 598 MPa
- Max. Hoop Strain after energization: 0.332 %
- Local peak shear stress ~ 10 MPa
- Max Shear after energization |9.2| MPa





International
UON Collider
Collaboration

Mechanical considerations - Third concept

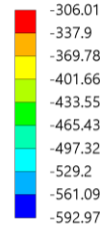
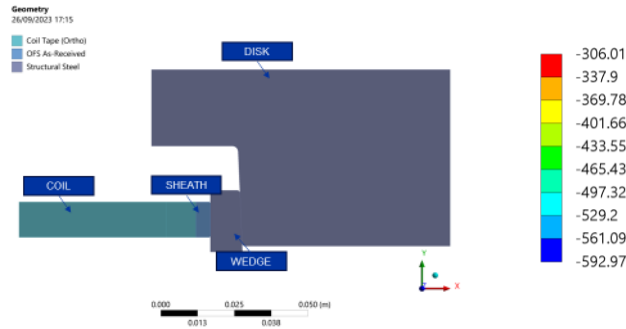
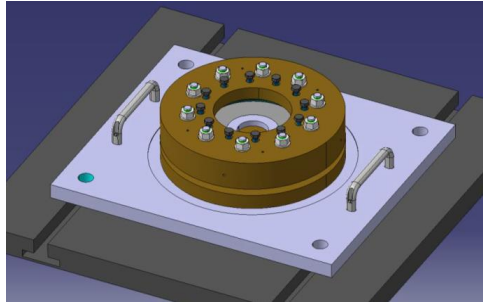


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REBCO conductor	
Axial tensile stress	700MPa
Axial tensile strain	0.4%
Transverse compressive stress	>100MPa
Transverse tensile stress	10-100MPa
Max shear stress	>19MPa

- Preliminary is ok, but **limited safety margins** → Fundamental to have a good understanding of the **material limits** and **failure mode**

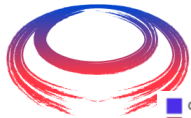
Testing



- $\sigma_{\text{hoop}} \sim -600\text{MPa}$ reached on the inner radius of the coil
- The required compression is achieved with 10 M16 bolts
- System equipped with strain gauges and digital image correlation to characterize the coil

Conclusion and next step

- The final cooling solenoid requires a pre-compression to operate at 40T:
 - Shrink fitting, mechanical jigs or a combined solution can provide the required pre-compressions
 - Tape properties impacting the results → important to benchmark them with experimental tests
 - The design of the inner and outer rings is critical: some possible solutions identified, more modelling work is needed to finalize the design
 - Different FEM models ready to investigate more options
 - Extensive work of design of the tooling for the experimental characterization of the tape



International Fusion Collaboration

- Coil material (Hastelloy_50+Copper_30)
- Copper hard
- Copper soft
- Hastelloy
- Shell

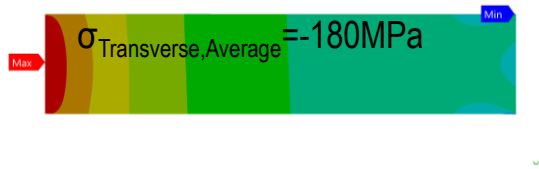
Validity of homogeneous model



Step 1: Shrink fitting (T external shell =250°C)

$$\sigma_{\text{Transverse,Average}} = -210\text{MPa}$$

Step 2: Cool-down

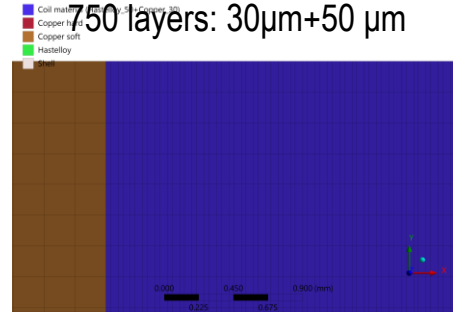


- 69.014
- 94.643
- 120.27
- 145.9
- 171.53
- 197.16
- 222.79
- 248.42
- 274.04
- 299.67

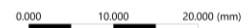
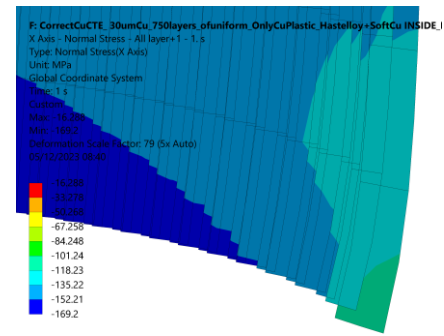
Step 3: Energization



- 59.761
- 0
- 70.094
- 140.19
- 210.28
- 280.38
- 350.47
- 420.56
- 490.66
- 560.75



$$\sigma_{\text{Transverse,Average}} = -85\text{MPa}$$



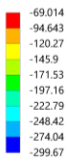
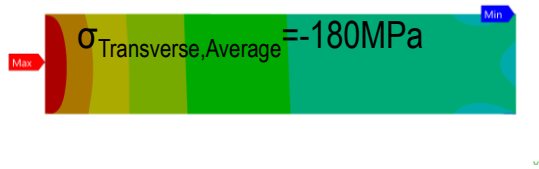
Validity of homogeneous model



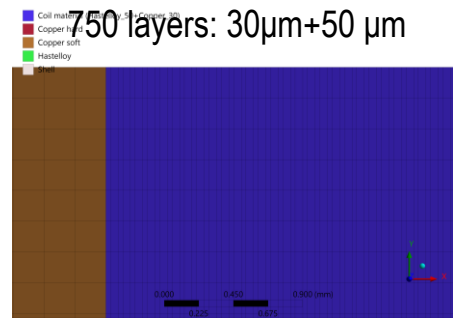
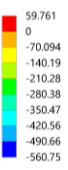
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$\sigma_{\text{Transverse,Average}} = -210\text{MPa}$

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Step 3: Energization

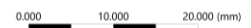
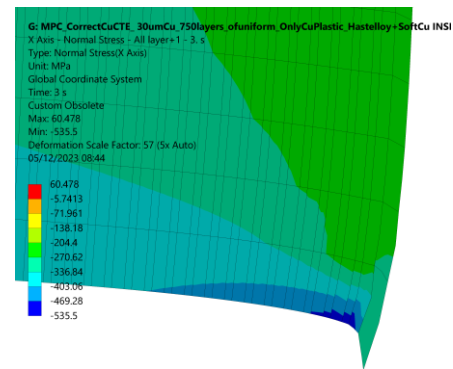
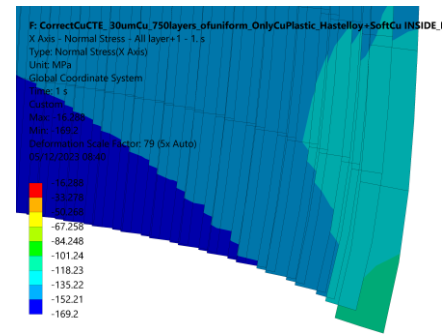


$\sigma_{\text{Transverse,Average}} = -85\text{MPa}$



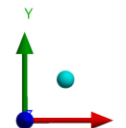
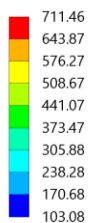
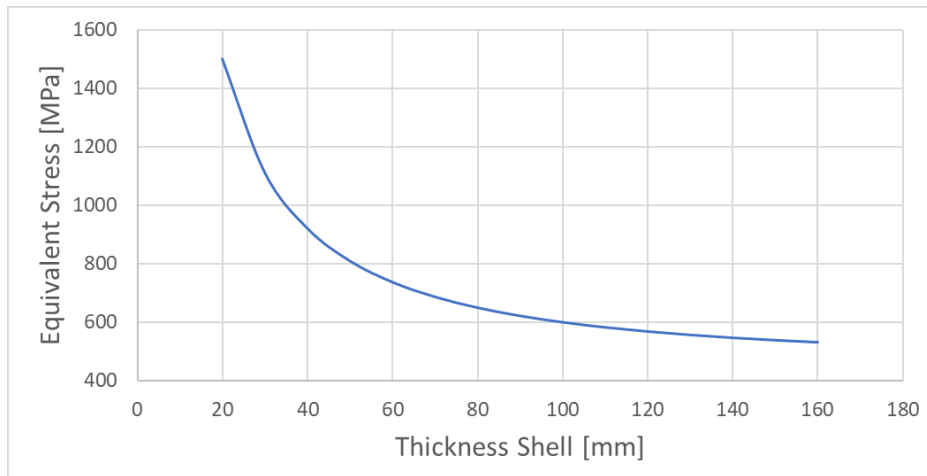
MPC CONTACT

$\sigma_{\text{Transverse,Average}} = -215\text{MPa}$



Why thick shell?

Before
energization



Homogeneization

- Radial direction → springs in series
- Tangential direction → springs in parallel

$$E_{radial} = \frac{E_{Cu} \cdot t_{Cu} + E_{Ha} \cdot t_{Ha}}{t_{tot}}$$

$$E_{tangential} = t_{tot} \cdot \left(\frac{t_{Cu}}{E_{Cu}} + \frac{t_{Ha}}{E_{Ha}} \right)^{-1}$$

