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Collaboration



Structural analysis of Final Cooling Solenoid Coil

C. Accettura,

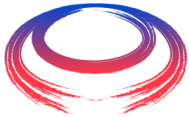
With several contributions from A. Bertarelli, B. Bordini, L. Bottura, A.
Dudarev, A. Kolehmainen, F. Sanda

[Final Cooling Solenoid Design and Fabrication \(19
September 2024\) · Indico \(cern.ch\)](#)

20/09/2024, CERN

Index

- Review of the model presented at the IMCC2024
- New model

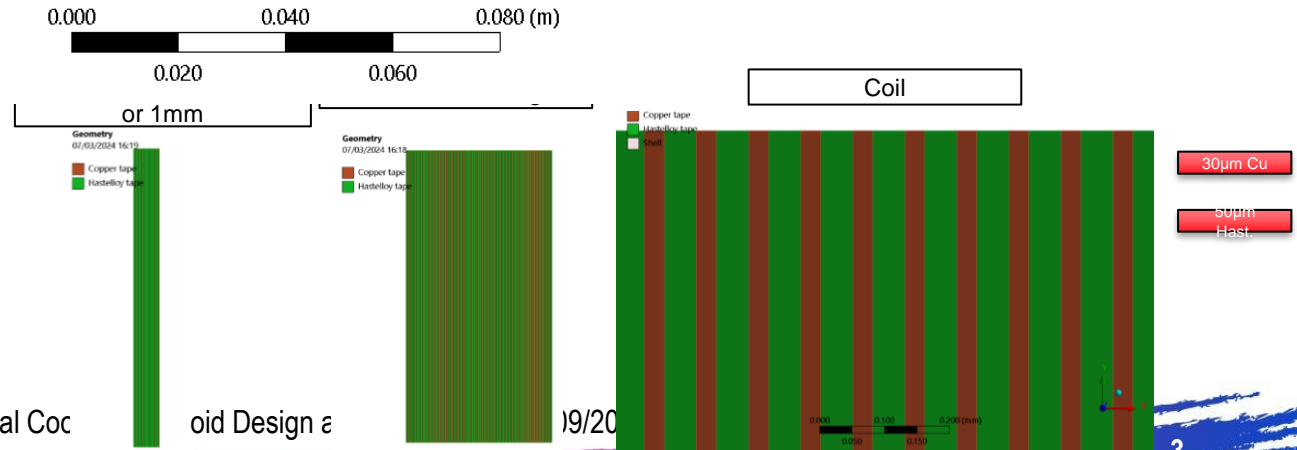


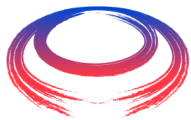
Stress and Strain in the coil

- Mechanical Simulation of a modular coil: all 750 windings are represented
- The model accounts for: Cu yielding and; the thermal contractions of the different materials
 - $P_M = B_0^2 / 2\mu_0 \sim 600\text{MPa}$
 - Hoop stress $\sim 1.4\text{-}2.2P_M$ (compact coil)



- To further reduce the stresses on the coils, a lower amount of Cu in the tape and a much larger outer-ring thickness





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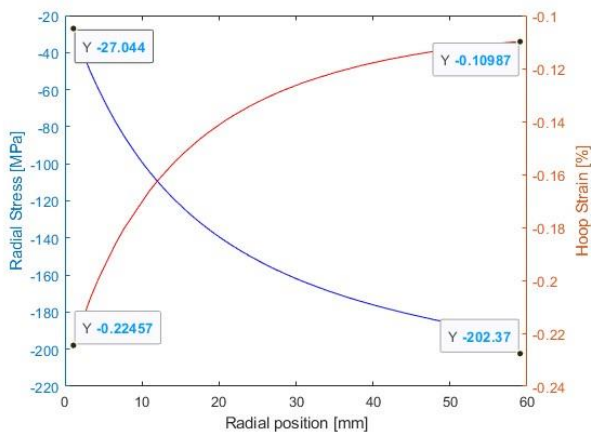
Stress and Strain in the coil



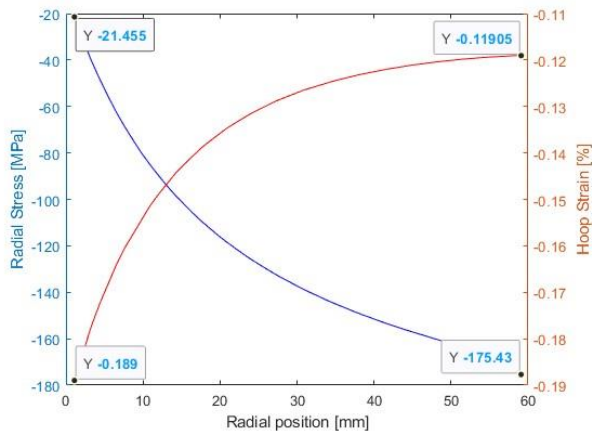
Pre-compression
170 MPa

Inner Joint ring
1 mm thick

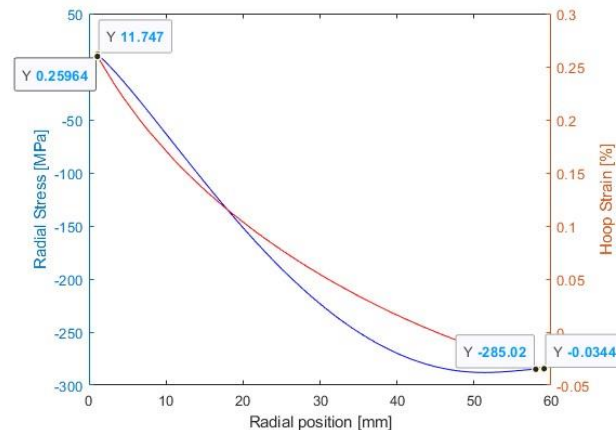
Step 1



Step 2



Step 3

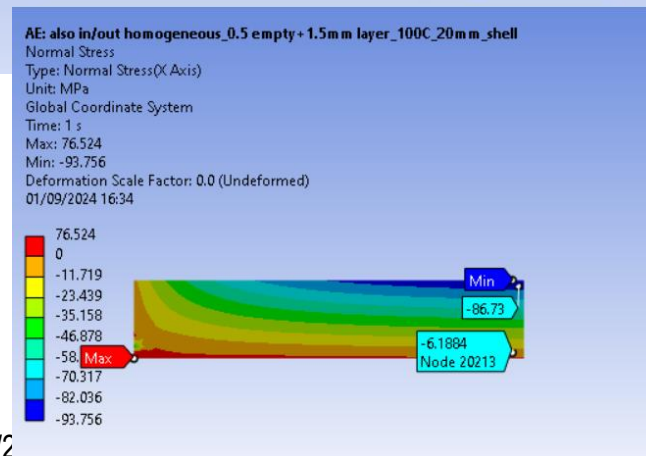
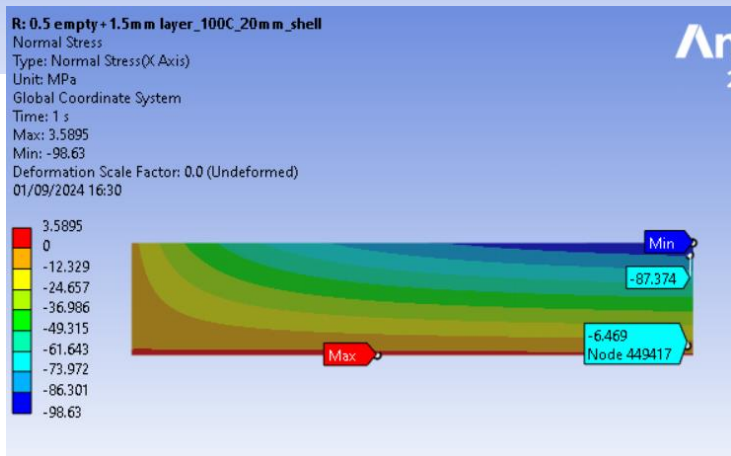
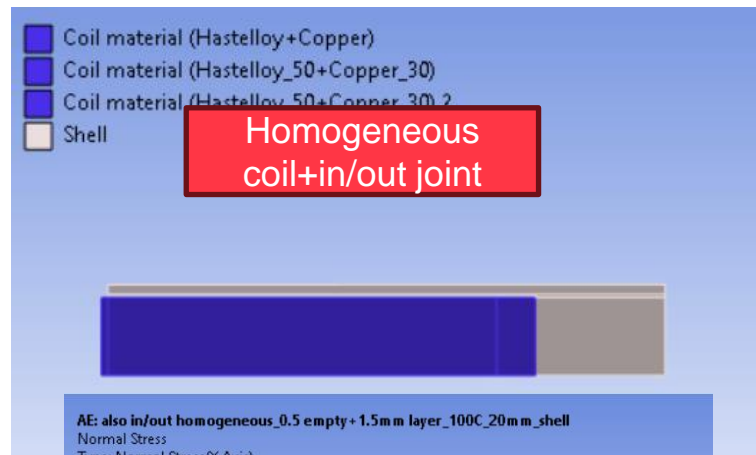
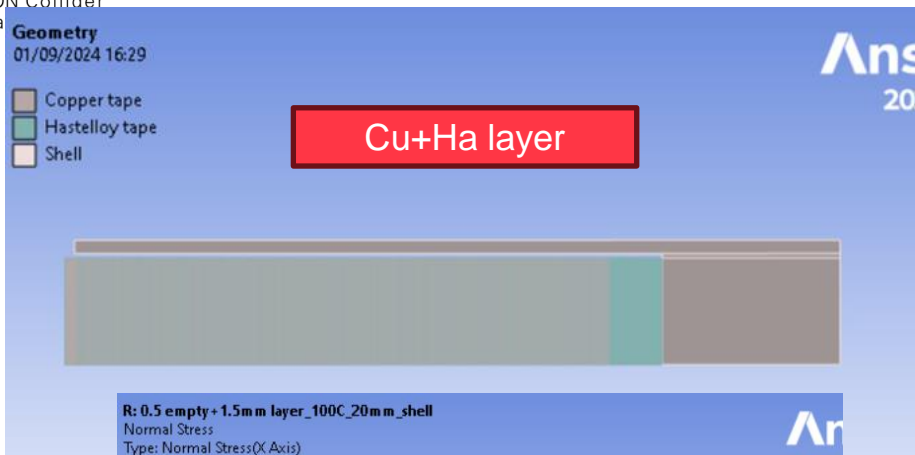


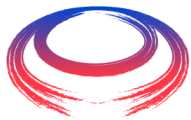
Inner joint optimization

Inner Joint ring thickness [mm]	Pre-compression at cold [MPa]	Radial stress [MPa]			Hoop Strain [%]			Shear Stress [MPa]		
		Step 1	Step 2	Step 3	Step 1	Step 2	Step 3	1	2	3
0.5	170	-205/-8	-190/-5	-290/10	-0.25/-0.10	-0.20/ -0.12	-0.04/ 0.28	6	4.5	4
	250	-318/-12	-258/-8	-367/7	-0.39/-0.17	-0.31/-0.16	-0.09/ 0.18	10	6	5
1	170	-205/-14	-190/-10	-288/19	-0.25/-0.10	-0.2/-0.12	-0.05/ 0.29	6	4	5
	250	-320/-21	-259/-15	-366/13	-0.39/-0.17	-0.3/-0.16	-0.09/ 0.18	10	6	5



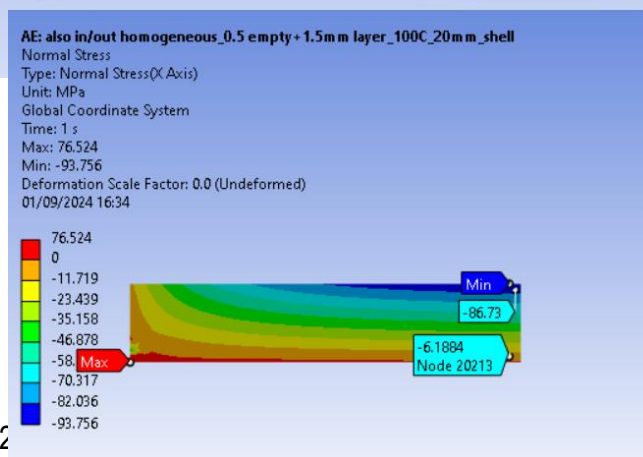
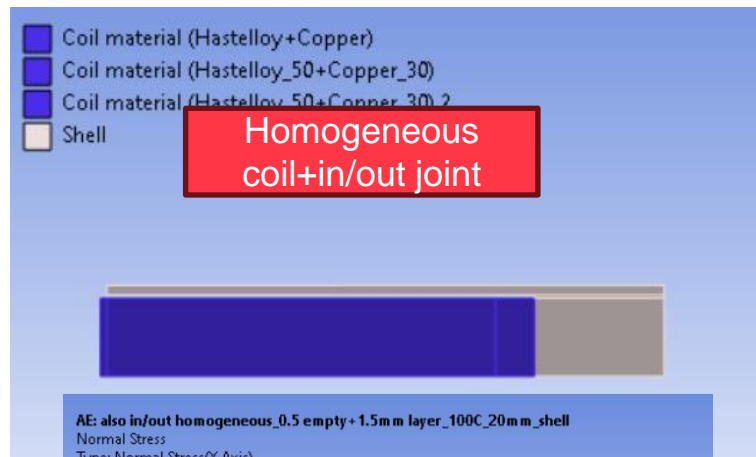
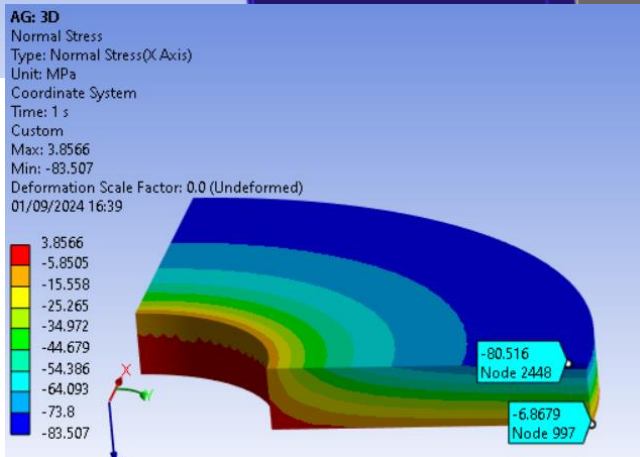
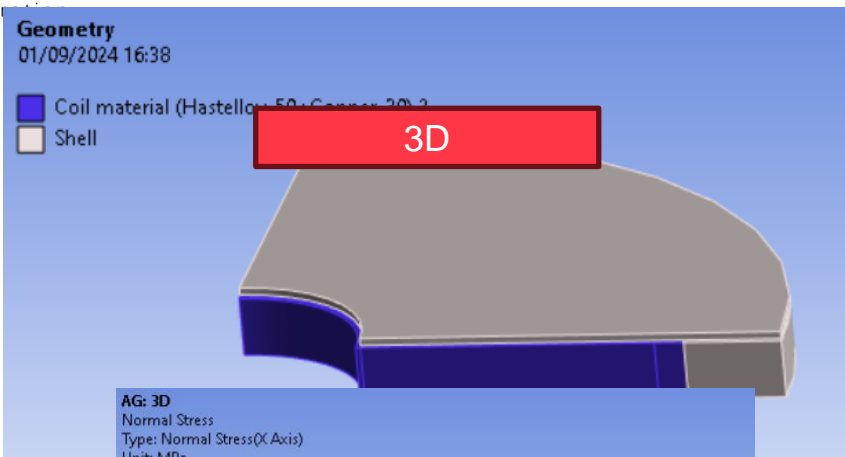
2D layered vs homogeneous



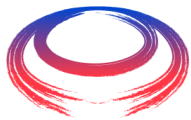


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3D vs 2D

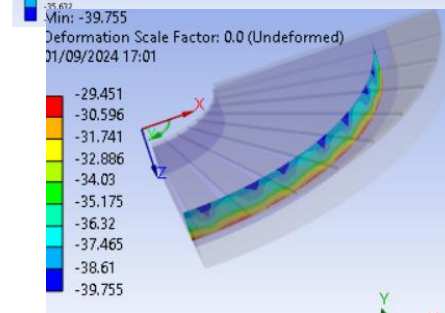
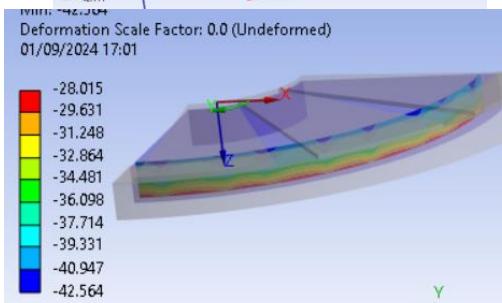
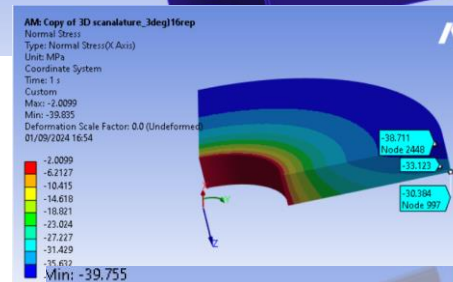
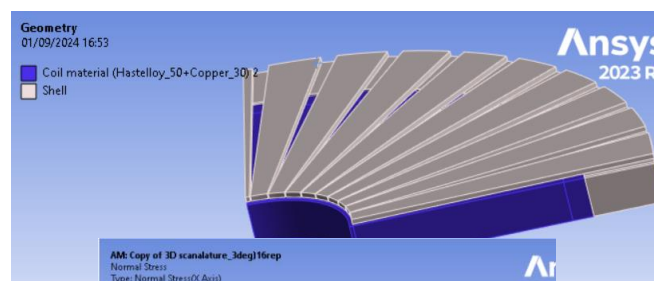
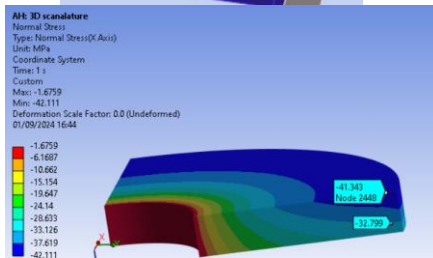
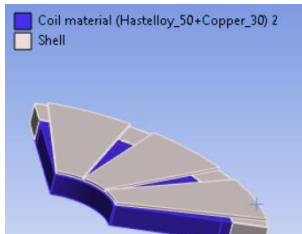
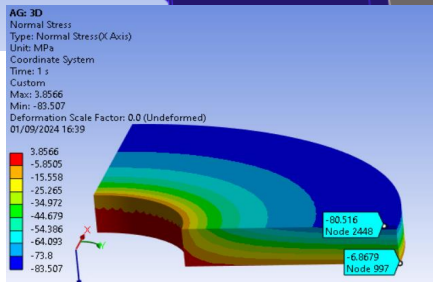
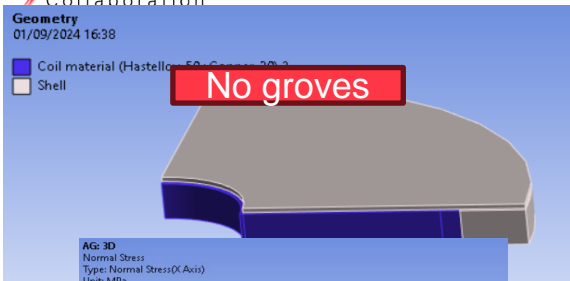


Fabrication, 20/09/2



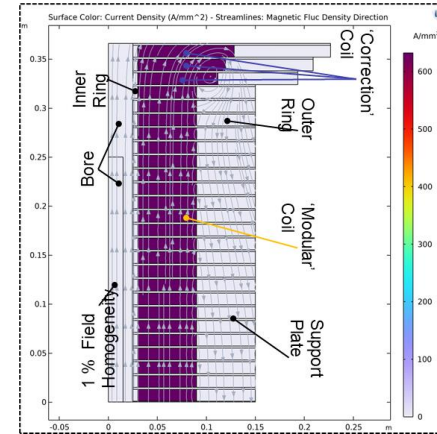
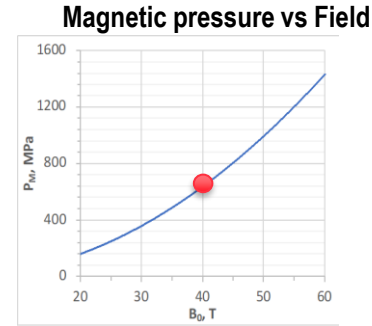
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Groves optimization



Introduction and Motivations

- Design proposed for the Final Cooling solenoid based on single and compact coil → critical stress management:
 - $P_M = B_0^2 / 2\mu_0 \sim 600 \text{ MPa}$
 - Hoop stress $\sim 1.4\text{-}2.2P_M$ (compact coil)

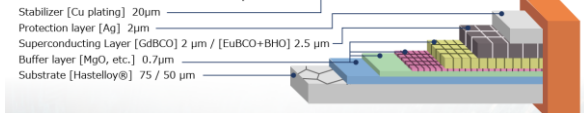


See [B. Bordini, Technology options for the final cooling solenoids, IMCC Annual Meeting 2023, Orsay](#)

Introduction and Motivations

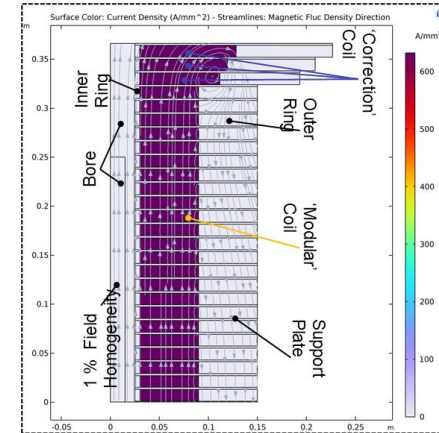
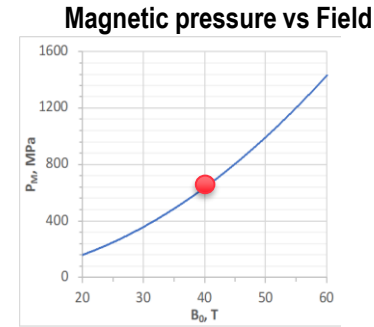
- Design proposed for the Final Cooling solenoid based on single and compact coil → critical stress management:
 - $P_M = B_0^2 / 2\mu_0 \sim 600\text{MPa}$
 - Hoop stress $\sim 1.4\text{-}2.2P_M$ (compact coil)
- Non-homogeneous and anisotropic material:
 - Maximum allowable stress very weak in certain direction
 - Scarce literature
 - Reduced safety margin

<Schematic of RE-based HTS tape>



Reference Conductor Fujikura FESC-SH12.

<https://www.fujikura.co.jp/eng/products/newbusiness/superconductors/01/superconductor.pdf>



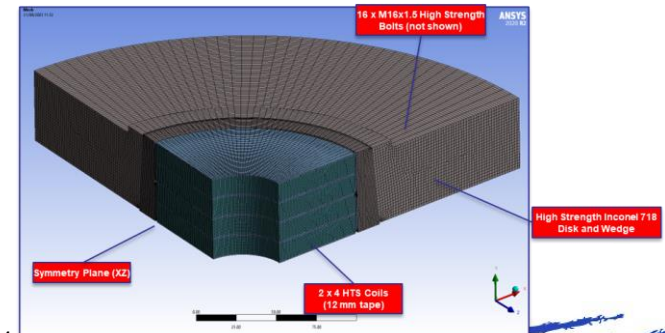
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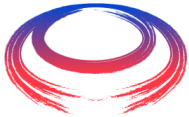
REBCO conductor	
Axial tensile stress	700MPa
Axial tensile strain	0.4%
Transverse compressive stress	>100MPa
Transverse tensile stress	10-100MPa
Max shear stress	>19MPa

- A pre-compression of $\sim 200\text{MPa}$ is needed to remain below this value

Pre-compression

- How to obtain the pre-compression?
- Mechanical concept is based on **encapsulating** HTS pancake coils in an **external structure**, generating high **radial compressive stresses**. **Three concepts analysed:**
 1. Thermally-induced shrink fitting
 2. Adjustable shrink-discs with conical surfaces
 3. Hybrid solution (1+2)





Shrink Fitting



- Coil surrounded by a cylindrical shell with $r_{in_shell} < r_{ext_coil}$
- Shell is pre-heated → fitting of the coil inside → cool-down of the shell and thermal contraction
- Simple analytical evaluation: $\sigma_{hoop} = 500\text{MPa} \rightarrow 200\text{MPa} \rightarrow \text{interference gap } \sim 220\mu\text{m} \rightarrow T_{shell} \sim 170^\circ\text{C}$

$$\sigma_{\theta} = -\frac{\rho^2 + \beta^2}{\rho^2} \frac{1}{1 - \beta^2} P_e$$

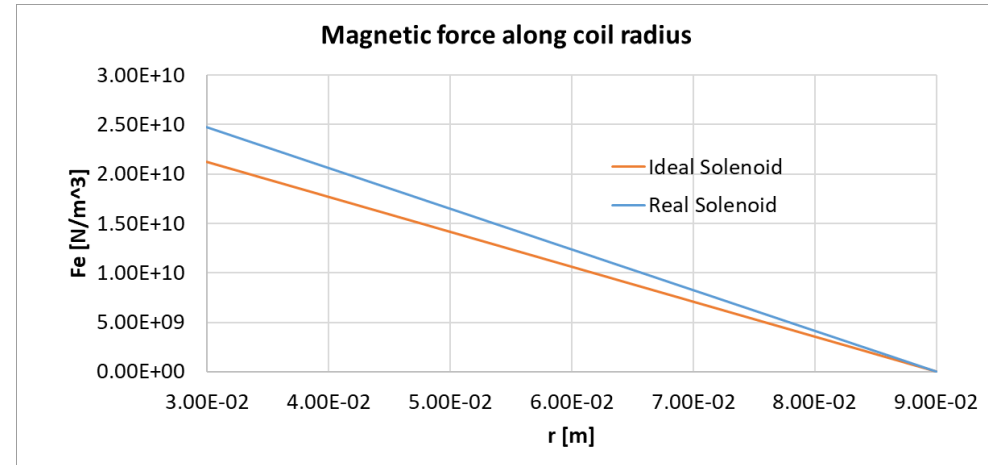
$$\delta = \delta_{i2} - \delta_{e1} = \left[\frac{1}{E_2} \left(\frac{1 + \beta_2^2}{1 - \beta_2^2} + \nu_2 \right) + \frac{1}{E_1} \left(\frac{1 + \beta_1^2}{1 - \beta_1^2} - \nu_1 \right) \right] r_{e1} P_f$$

- Some practical aspects must be considered:
 - Differential contraction during cooldown
 - Strength of the cylinder
 - Impact of the joints
 - Plasticity
 - Mechanical tolerances: 1MPa/μm lost
 - Buckling
- FEA simulations at different levels of complexity

Assumptions

- 2D axisymmetric
- Electromagnetic Forces

- Ideal Solenoid ($J_{ideal} = \frac{B_{MAX}}{\mu_0(r_{co} - r_{ci})} = 531 \text{ A/mm}^2$)
- Real Solenoid ($J_{real} = J_{ideal} \frac{t_{coil} + t_{supportplate}}{t_{coil}} = 620 \text{ A/mm}^2$)



All
Unit: N/mm³
Max: 22.343
Min: 0
06/12/2023 09:49

22.343
19.86
17.378
14.895
12.413
9.9302
7.4477
4.9651
2.4826
0



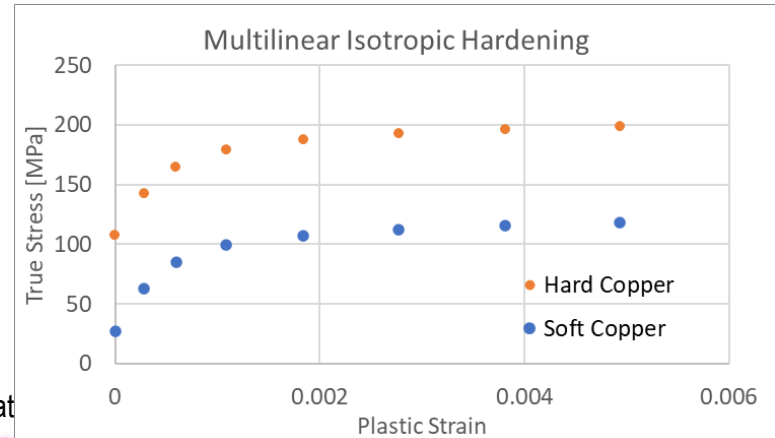
Reference model

- Coil material (Hastelloy_50+Copper_30)
- Copper hard
- Copper soft
- Hastello
- Shell

Homogeneous
tape properties

Needed to keep the pre-compression.
Soft copper was resulting in a lower
pre-compression

Ha to avoid radial tensile and
shear stress after cooldown



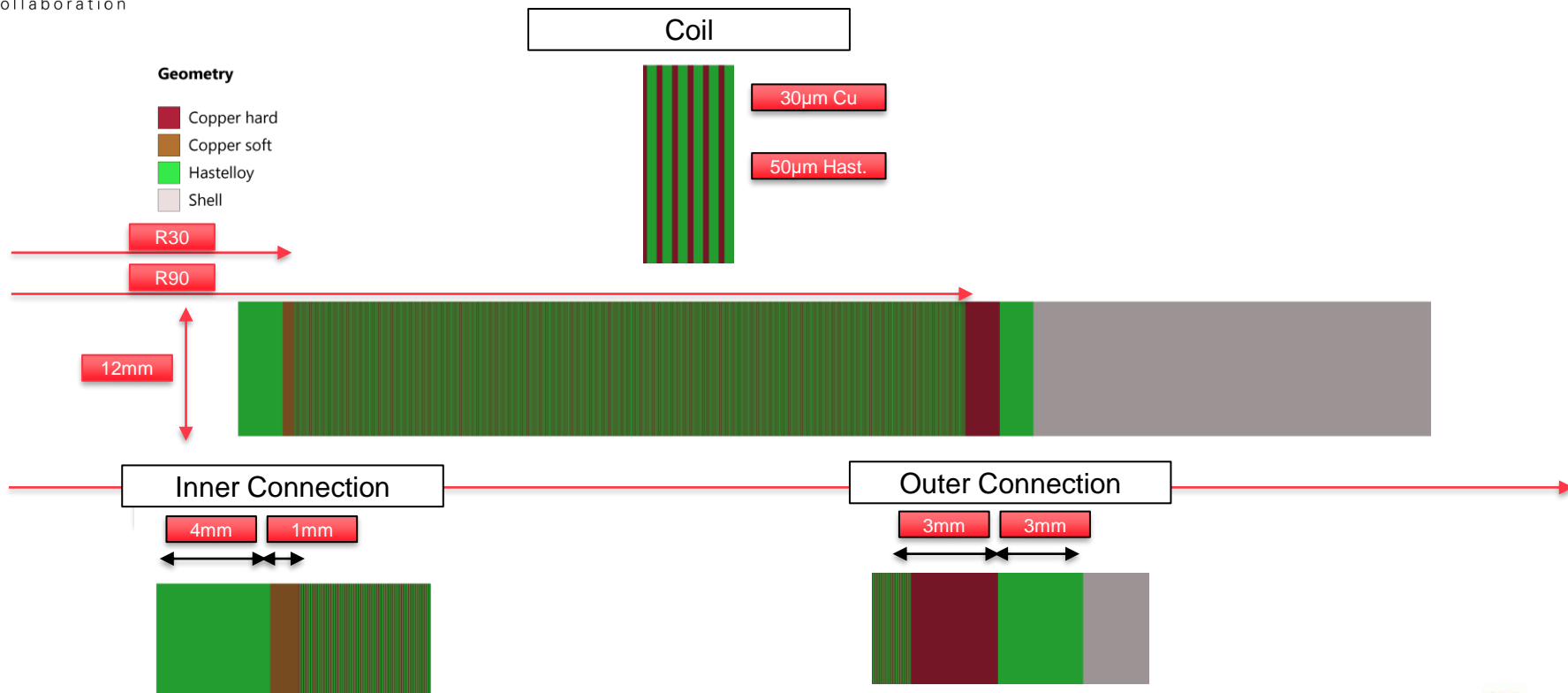
Layered model

Geometry

- Copper hard
- Copper soft
- Hastelloy
- Shell



Geometry and Materials



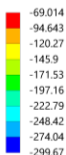
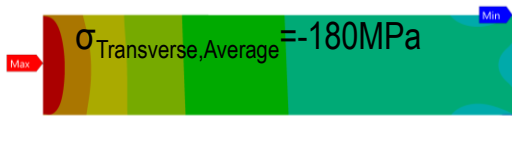
Validity of homogeneous model



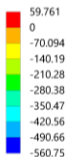
Step 1: Shrink fitting (T external shell =250°C)

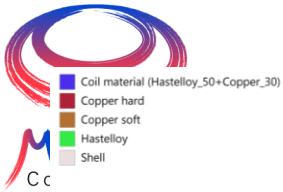
$$\sigma_{\text{Transverse,Average}} = -210\text{MPa}$$

Step 2: Cool-down



Step 3: Energization





Validity of homogeneous model

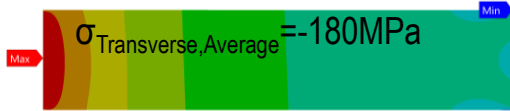
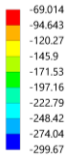


Step 1: Shrink fitting

$$\sigma_{\text{Transverse,Average}} = -210\text{MPa}$$

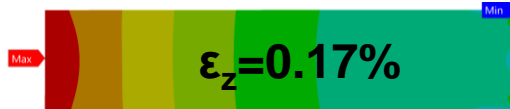
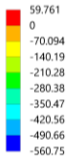
Step 2: Cool-down

$$\sigma_{\text{Transverse,Average}} = -180\text{MPa}$$



Step 3: Energization

$$\epsilon_z = 0.17\%$$



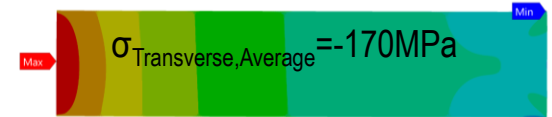
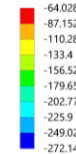
750 layers: 30μm+50 μm

Step 1: Shrink fitting

$$\sigma_{\text{Transverse,Average}} = -215\text{MPa}$$

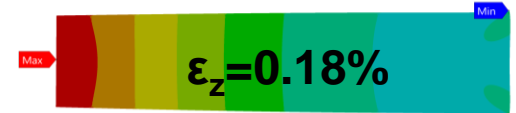
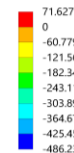
Step 2: Cool-down

$$\sigma_{\text{Transverse,Average}} = -170\text{MPa}$$

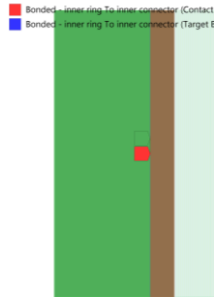


Step 3: Energization

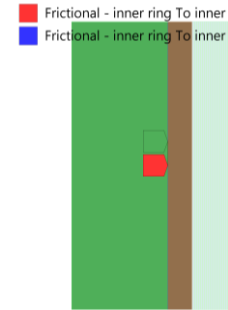
$$\epsilon_z = 0.18\%$$



Effect of the inner joint properties



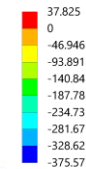
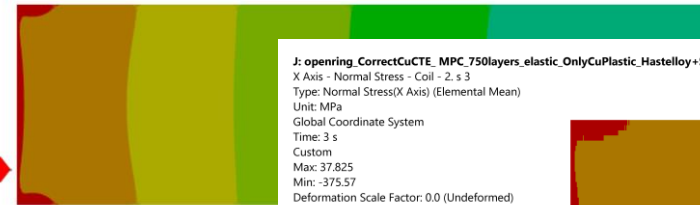
Let the ring detach to limit radial tensile stress



G: CorrectCuCTE_MPC_750layers_elastic_OnlyCuPlastic_Hastelloy+SoftCu INSIDE_HardCu+Hastelloy OUTSIDE_Orthotropic_1supportfrictionless_FRICTIONLESS_2D_axyal
 X Axis - Normal Stress - All layer + 1 - 3.s
 Type: Normal Stress(X Axis)
 Unit: MPa
 Global Coordinate System
 Time: 3 s
 Custom
 Max: 71.627
 Min: -486.23
 Deformation Scale Factor: 56 (5x Auto)
 06/12/2023 10:04



Max: 73.473
 Min: -502.27
 Deformation Scale Factor: 0.0 (Undeformed)
 06/12/2023 11:52



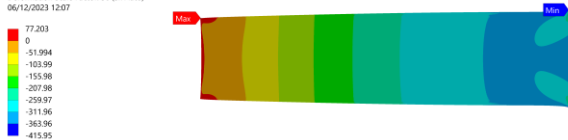
Effect of the tape plasticity

step	σ_x -radial[MPa]			ϵ_z -hoop
	min	max	ave	max
1	-289	-57	-210	
2	-224	-67	-164 (200*)	
3	-416	77	-213	0.30%
1	-308	-54	-214	
2	-272	-63	-171 (210*)	
3	-502	73	-224	0.22%

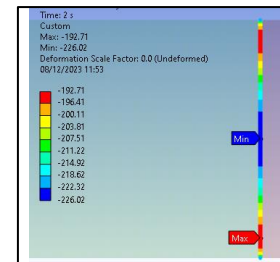
Plastic

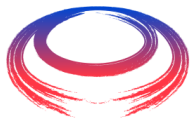
Elastic

L: opening_CorrectCuTE MPC_750layers_plastic_OnlyCuPlastic_Hastelloy+SoftCu INSIDE_HardCu+Hastelloy OUTSIDE_Orthotropic_1supportfrictionless_FRICTIONLESS_2D_axisym_1coil_cor
 X Axis - Normal Stress - All layer+1 - 3, s
 Type: Normal Stress(X Axis)
 Unit: MPa
 Global Coordinate System
 Time: 3 s
 Custom Obsolete
 Max: 77.203
 Min: -415.95
 Deformation Scale Factor: 56 (5x Auto)
 06/12/2023 12:07



*Average on the external edge





Effect of the tape properties



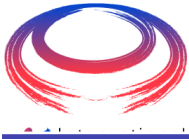
step	σ_x -radial[MPa]			ε_z -hoop
	min	max	ave	max
1	-291	-55	-208	
2	-264	-60	-171 (215*)	
3	-484	75	-218	0.24%
1	-289	-57	-210	
2	-224	-67	-164 (200*)	
3	-416	77	-213	0.30%

*Average on the external edge

Experiments and FE modeling of stress–strain state in ReBCO tape under tensile, torsional and transverse load

To cite this article: K Il'in et al 2015 *Supercond. Sci. Technol.* **28** 055006

Reference

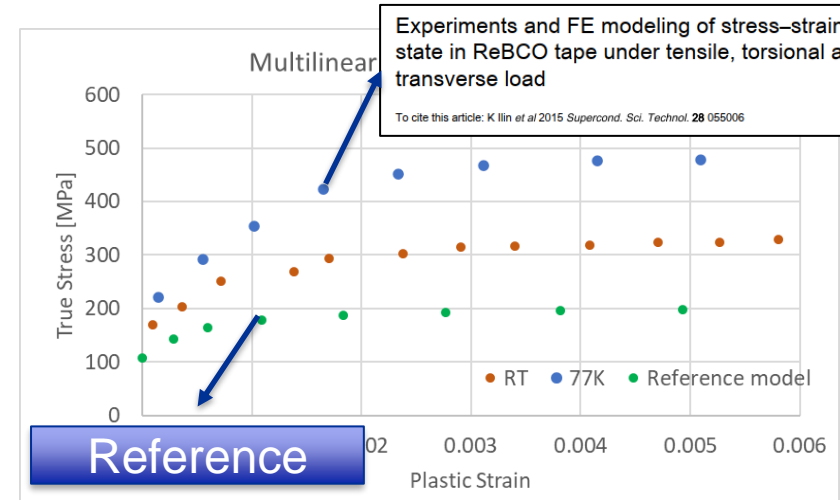


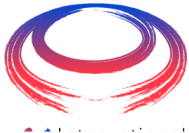
Effect of the tape properties



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Effect of the tape properties

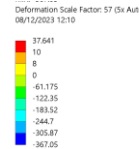
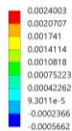


step	σ_x -radial[MPa]			ϵ_z -hoop
	min	max	ave	max
1	-291	-55	-208	
2	-264	-60	-171(215)	
3	-484	75*	-218	0.24%

*Localized effect

$\epsilon_z=0.24\%$ ✓

$\sigma_x \sim 10\text{MPa}$ ✓



Alternative Inner Joint-1

Reduced Hastelloy (1mm-Bonded to Cu)

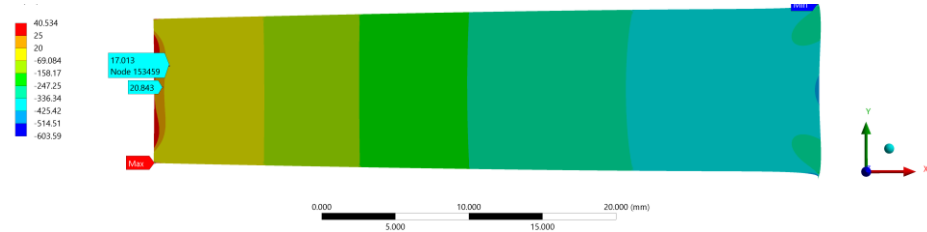
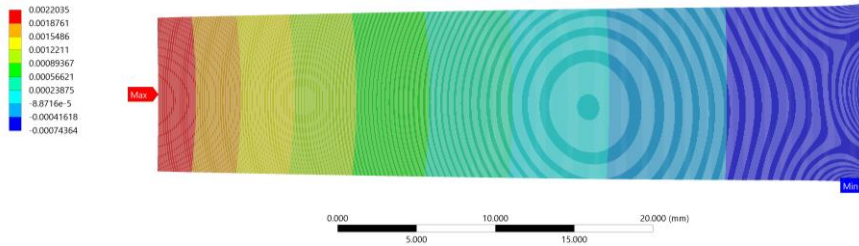
Geometry
01/02/2024 10:44

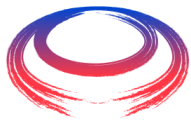
- Copper hard
- Copper soft
- Copper tape
- Hastelloy
- Hastelloy tape
- Shell



$\epsilon_z = 0.22\%$ ✓

$\sigma_x \sim 20\text{MPa}$
($p \sim 250\text{MPa}$)





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- Copper hard
- Copper tape
- Hastelloy
- Hastelloy ortho
- Hastelloy tape
- Shell

Alternative Inner Joint-2

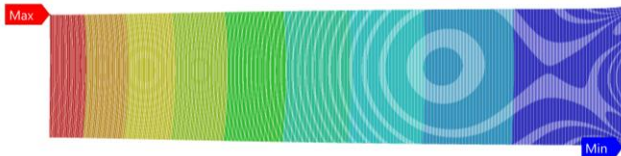
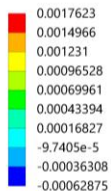


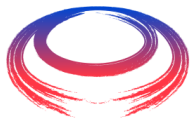
Hastelloy orthotropic	
Ex-radial[GPa]	Ey,z-hoop[GPa]
100	200



$\epsilon_z = 0.17\%$

$\sigma_x = 80\text{MPa}$



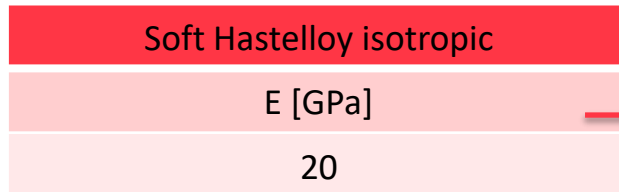


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Alternative Inner Joint-3

- Copper hard
- Copper tape
- Hastelloy
- Hastelloy tape
- Shell

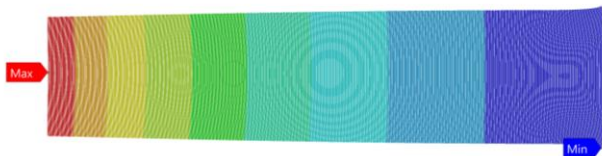
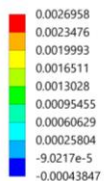


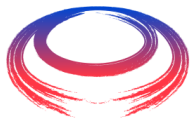
Model simplification, important to have a 3D design of the inner ring to take into account the real stiffness of the structure



$$\epsilon_z = 0.27\% \quad \checkmark$$

$$\sigma_x = 12\text{MPa} \quad \checkmark$$





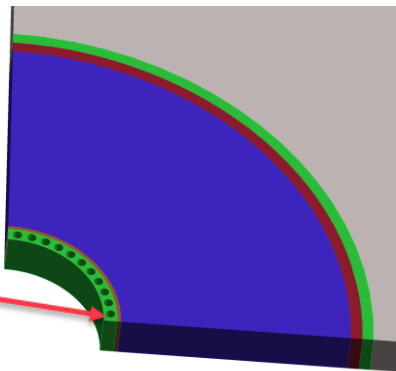
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Collaboration

Alternative Inner Joint-4



Geometry
01/02/2024 09:55

- Coil material (Hastelloy_50+Copper_30)
- Copper hard
- Copper soft
- Hastelloy
- Shell



3D model more time-consuming,
homogeneous material and mesh to be
refined → **INCREASE OF at least~50%**
expected

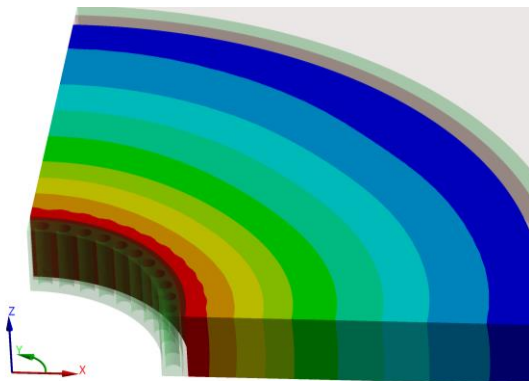
Cooling channel

$\epsilon_z = 0.18\%$

$\sigma_x < 20\text{MPa}$

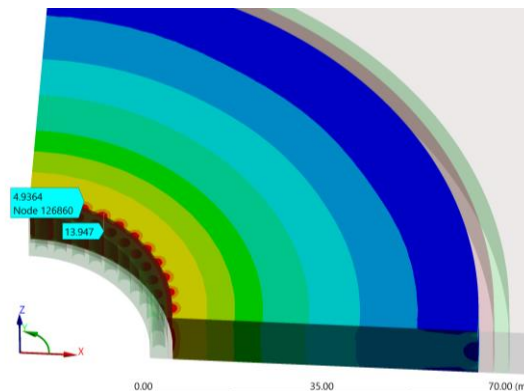
Type: Normal Elastic Strain(Y Axis)
Unit: mm/mm
Coordinate System 3
Time: 2 s
Max: 0.0018075
Min: -0.00038037
Deformation Scale Factor: 0.0 (Undeformed)
01/02/2024 10:00

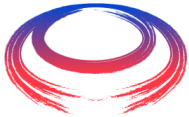
0.0018075
0.0015644
0.0013213
0.0010782
0.00083513
0.00059203
0.00034893
0.00010583
-0.00013727
-0.00038037



X Axis - Normal Stress - Coil - 3.s
Type: Normal Stress(X Axis)
Unit: MPa
Coordinate System 3
Time: 2 s
Custom
Max: 38.188
Min: -401.82
Deformation Scale Factor: 0.0 (Undeformed)
01/02/2024 09:56

38.188
10
0
-57.403
-114.81
-172.21
-229.61
-287.02
-344.42
-401.82





Shrink Fitting



- Coil surrounded by a cylindrical shell with $r_{in} < r_{ext_coil}$
- Shell is pre-heated → fitting of the coil inside → cool-down of the shell and thermal contraction
- Simple analytical evaluation: 600MPa → 200MPa → interference gap ~300μm → ~250°C

$$\sigma_{\theta} = -\frac{\rho^2 + \beta^2}{\rho^2} \frac{1}{1 - \beta^2} P_e$$

$$\delta = \delta_{i2} - \delta_{e1} = \left[\frac{1}{E_2} \left(\frac{1 + \beta_2^2}{1 - \beta_2^2} + \nu_2 \right) + \frac{1}{E_1} \left(\frac{1 + \beta_1^2}{1 - \beta_1^2} - \nu_1 \right) \right] r_{e1} P_f$$

- Some practical aspects must be considered:
 - Differential contraction during cooldown
 - Strength of the cylinder
 - Impact of the joints
 - Plasticity
 - Mechanical tolerances: 2MPa/μm lost**
 - Buckling**
- FEM simulations at different levels of complexity

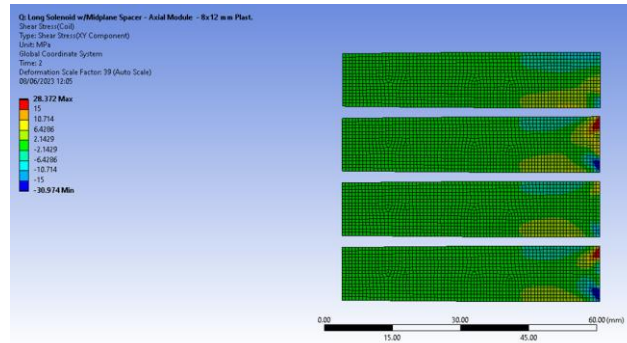
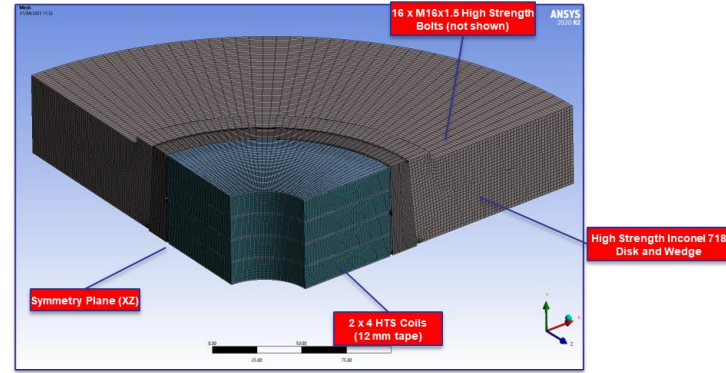


Mechanical considerations - Second concept



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- 2 Load Steps:
 - Shrink Disk displacement (5 mm)
 - Energization
- Max. Hoop Stress (after energization): 620.4 MPa
- Max. Hoop Strain (after energization): 0.344 %
- Shear Stresses globally lower than 15 MPa
- However, locally they can reach after energization $\sim |30|$ MPa

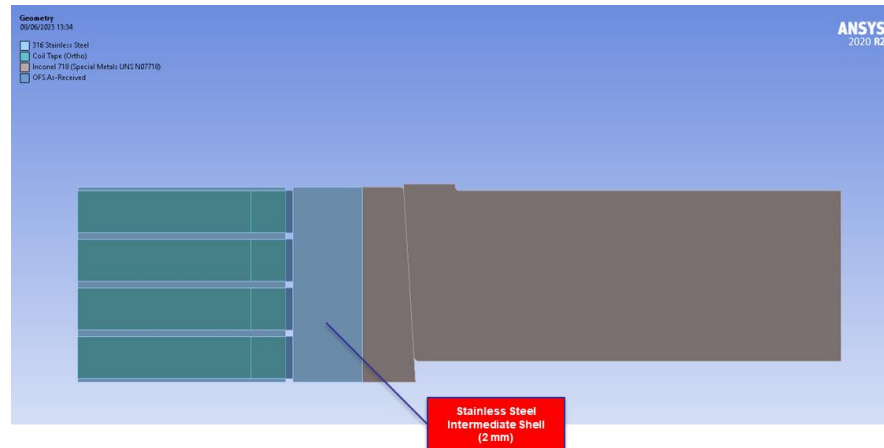


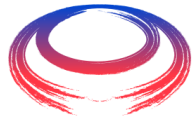


Mechanical considerations - Third concept



- To limit shear stresses, an intermediate steel shell is added (ID 184 mm; OD 224 mm)
- ~ 150 μm interference with coil pack created by differential heating
- 3 Load Steps: 1. Shell/Coil Interference; 2. Shrink Disk Displacement (2.2 mm); 3. Energization
- Min. Hoop Stress after shrinking: -426 MPa
- Max. Hoop Stress after energization: 598 MPa
- Max. Hoop Strain after energization: 0.332 %
- Local peak shear stress ~ 10 MPa
- Max Shear after energization |9.2| MPa





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Collaboration

Mechanical considerations - Third concept

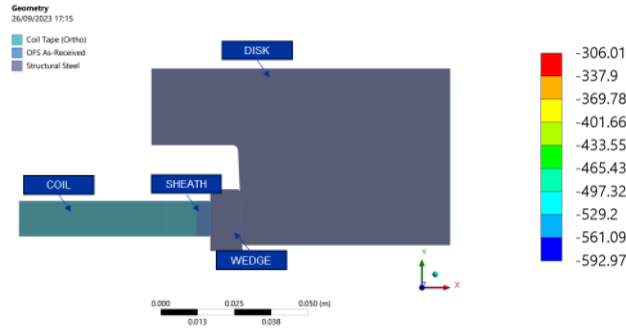
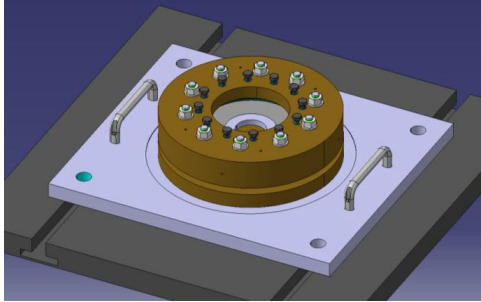


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- Max Shear after energization |9.2| MPa

REBCO conductor	
Axial tensile stress	700MPa
Axial tensile strain	0.4%
Transverse compressive stress	>100MPa
Transverse tensile stress	10-100MPa
Max shear stress	>19MPa

- Preliminary is ok, but **limited safety margins** → Fundamental to have a good understanding of the **material limits** and **failure mode**

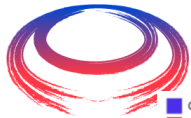
Testing



- $\sigma_{hoop} \sim -600\text{MPa}$ reached on the inner radius of the coil
- The required compression is achieved with 10 M16 bolts
- System equipped with strain gauges and digital image correlation to characterize the coil

Conclusion and next step

- The final cooling solenoid requires a pre-compression to operate at 40T:
 - Shrink fitting, mechanical jigs or a combined solution can provide the required pre-compressions
 - Tape properties impacting the results → important to benchmark them with experimental tests
 - The design of the inner and outer rings is critical: some possible solutions identified, more modelling work is needed to finalize the design
 - Different FEM models ready to investigate more options
 - Extensive work of design of the tooling for the experimental characterization of the tape



International Fusion Collaboration

- Coil material (Hastelloy_50+Copper_30)
- Copper hard
- Copper soft
- Hastelloy
- Shell

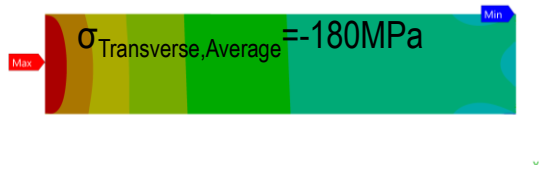
Validity of homogeneous model



Step 1: Shrink fitting (T external shell =250°C)

$$\sigma_{\text{Transverse,Average}} = -210\text{MPa}$$

Step 2: Cool-down

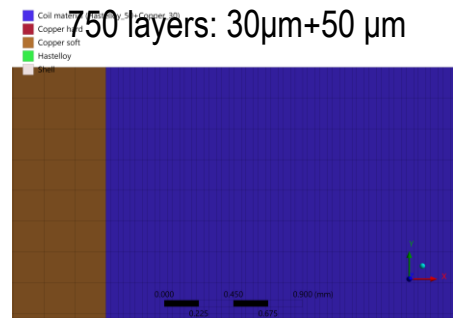


- 69.014
- 94.643
- 120.27
- 145.9
- 171.53
- 197.16
- 222.79
- 248.42
- 274.04
- 299.67

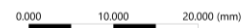
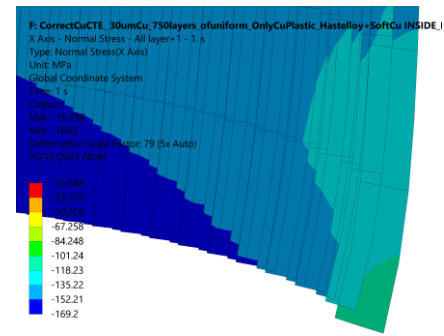
Step 3: Energization



- 59.761
- 0
- 70.094
- 140.19
- 210.28
- 280.38
- 350.47
- 420.56
- 490.66
- 560.75



$$\sigma_{\text{Transverse,Average}} = -85\text{MPa}$$

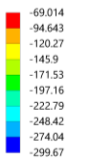
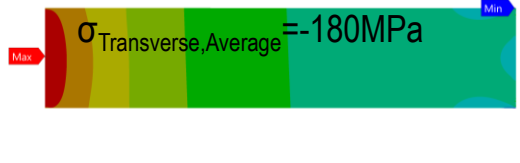


Validity of homogeneous model

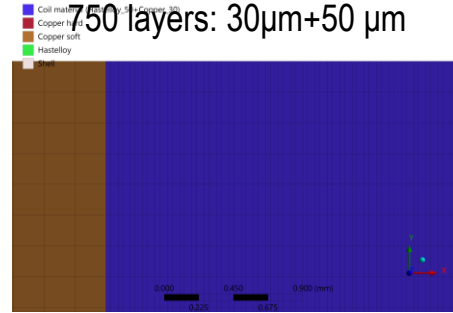
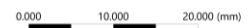
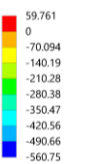
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Step 3: Energization

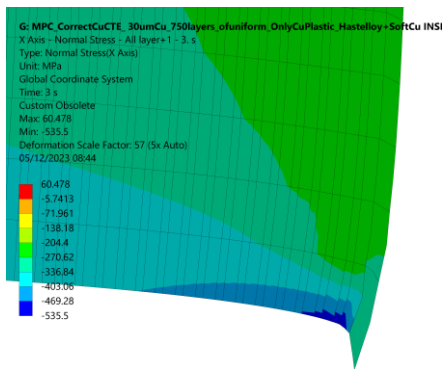
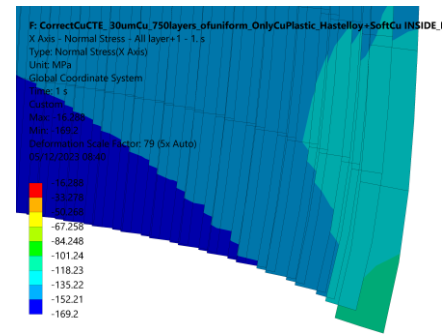


$$\sigma_{\text{Transverse,Average}} = -85\text{MPa}$$



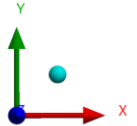
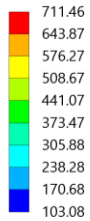
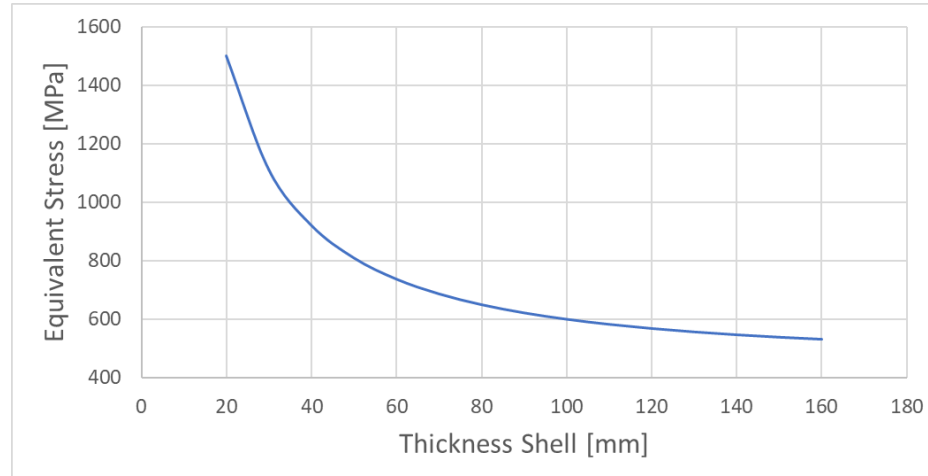
MPC CONTACT

$$\sigma_{\text{Transverse,Average}} = -215\text{MPa}$$



Why thick shell?

Before energization



Homogeneization

- Radial direction → springs in series
- Tangential direction → springs in parallel

$$E_{radial} = \frac{E_{Cu} \cdot t_{Cu} + E_{Ha} \cdot t_{Ha}}{t_{tot}}$$

$$E_{tangential} = t_{tot} \cdot \left(\frac{t_{Cu}}{E_{Cu}} + \frac{t_{Ha}}{E_{Ha}} \right)^{-1}$$

