

# Exotic Hadrons

## Experimental and Theoretical overview

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Hadronic physics and heavy quarks on the lattice

Hamilton Mathematics Institute, Ireland, 06/06/2024



# Introduction

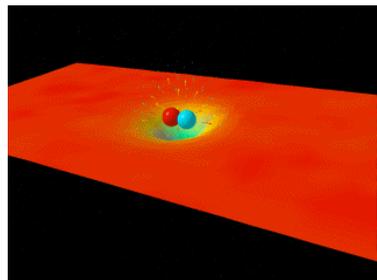
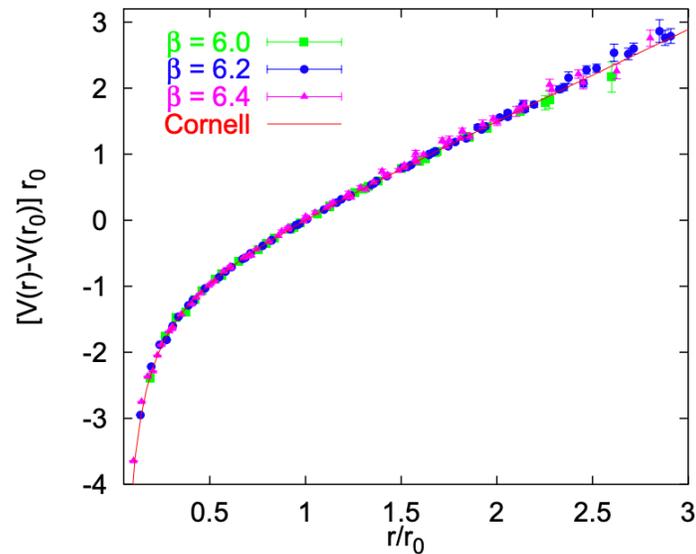
1. String breaking

2. Mixture with the threshold

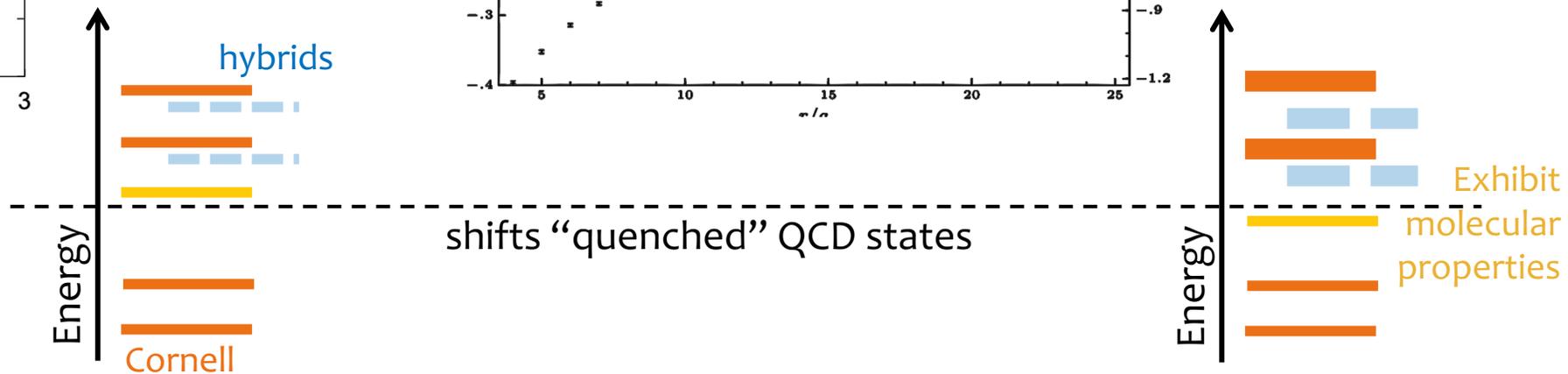
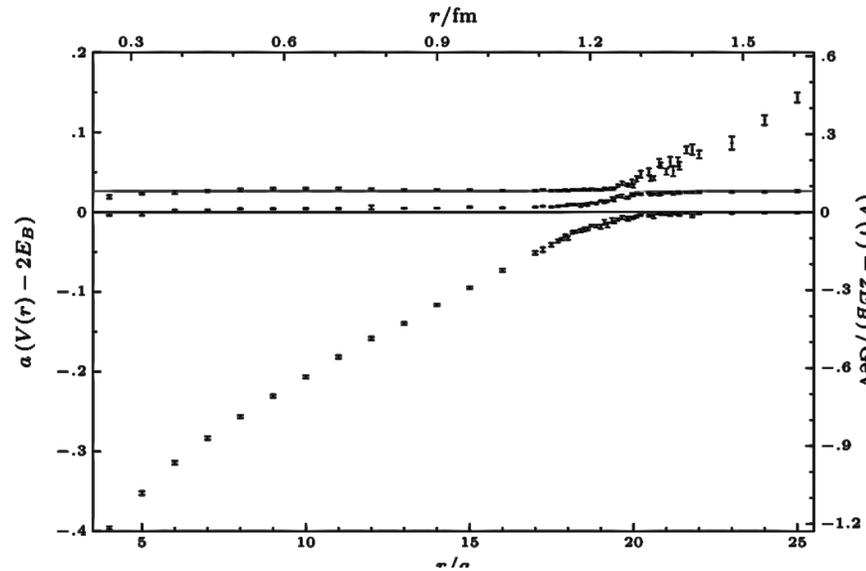
3. Different Hadrons and Nuclei

# Effect of string breaking

## The quenched potential (no breaking)

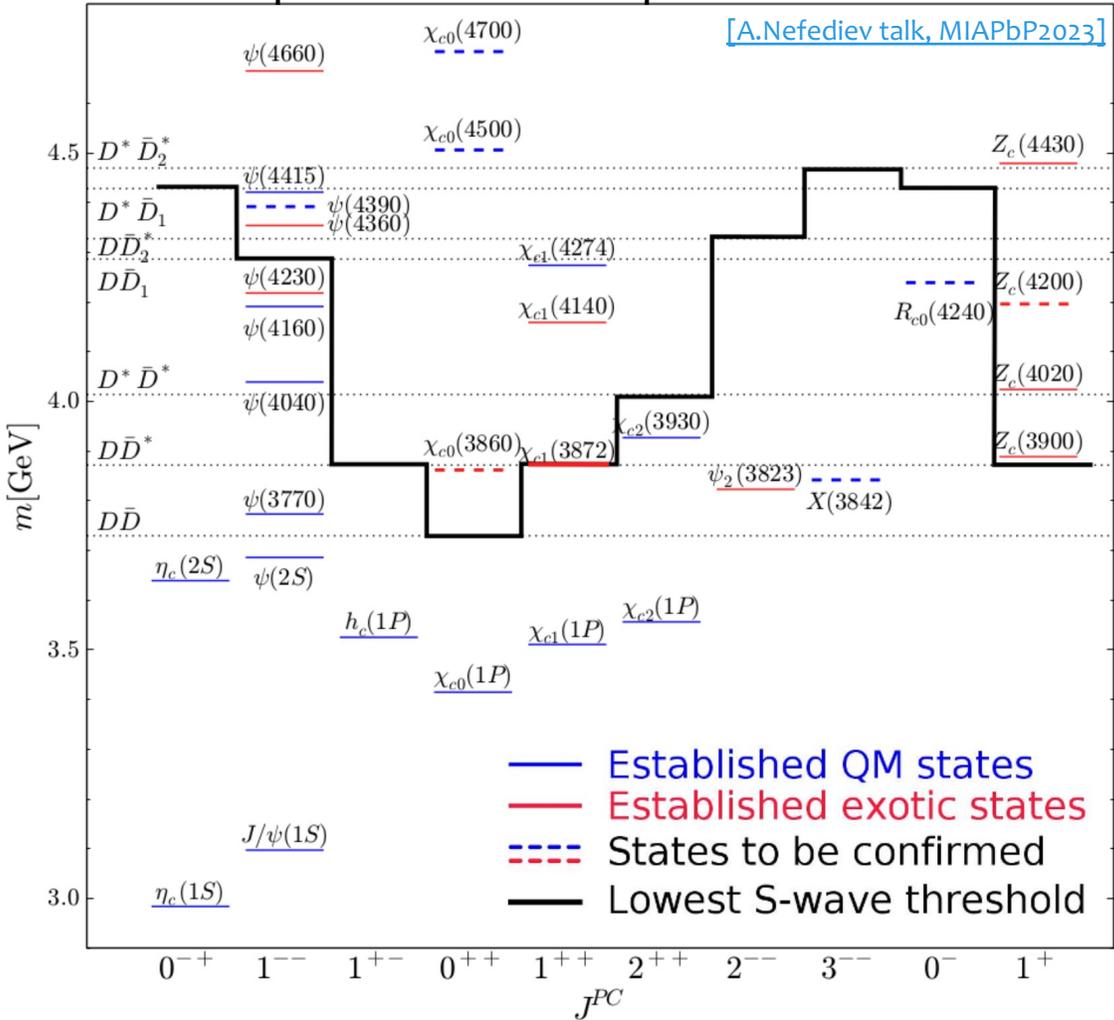


## The unquenched potential (breaking)



# QM states and thresholds

An example: charmonium spectrum



Most of hadrons are not isolated:  
near hadron-hadron threshold,

e.g.  $q\bar{q} \rightarrow (q\bar{q})(q\bar{q})$ ,

hadronic states are coupled to hadron-hadron continuum

Molecule component:  
a part of the state wave function is  $(q\bar{q})(q\bar{q})$

# Possible configurations of hadrons

Conventional Quark Model:  $(q\bar{q}, qqq)$

Bigger Quark Model  $(q\bar{q}q\bar{q}, qqqq\bar{q}, \dots)$

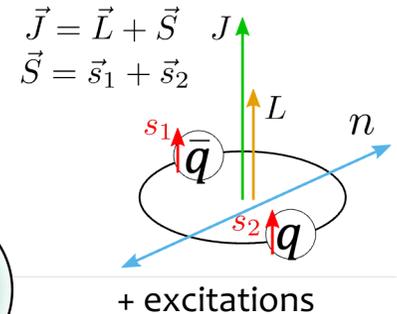
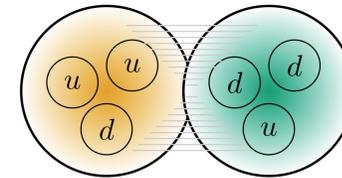
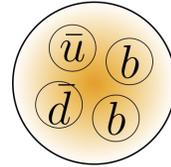
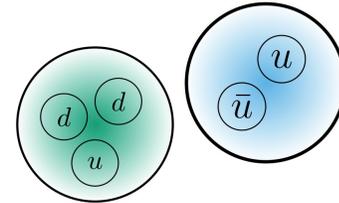
Conventional Hadronic Molecules = Nuclei:  $(qqq)(qqq)$

Heavy-Flavor Hadronic Molecules:  $(Qqq)(Qqq), (Q\bar{q})(Qqq), \dots$

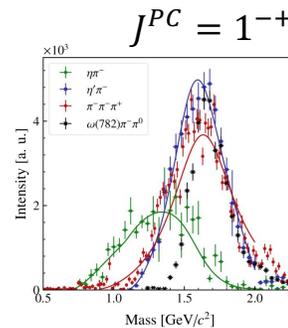
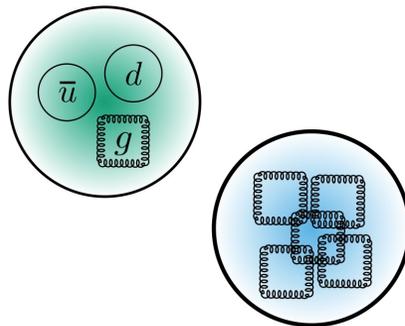
Admixed Molecules:  $q\bar{q} \rightarrow (q\bar{q})(q\bar{q})$

Hybrids:  $q\sim g\sim\bar{q}$

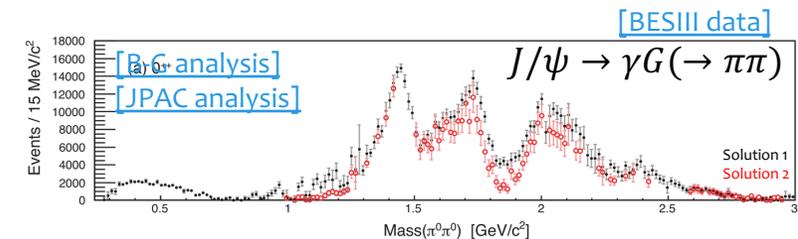
Glueballs:  $g\sim g$



+ nuclei chart



[P.Haas, HADRON2023]

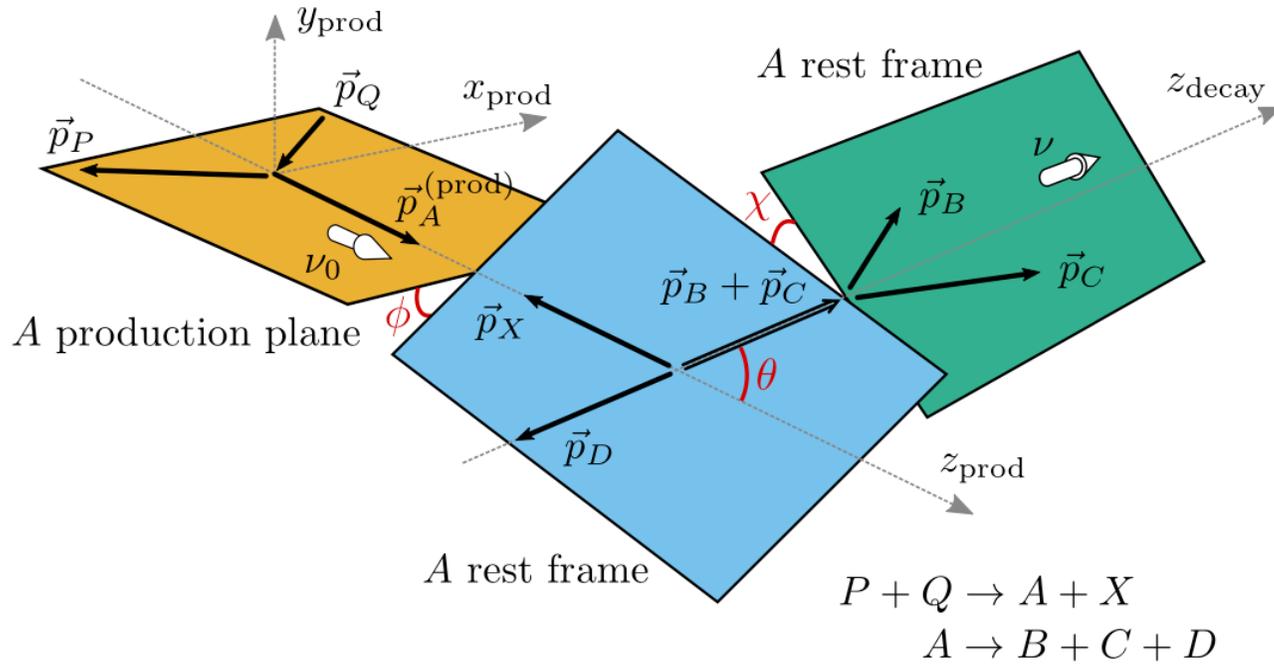


# Experimental techniques

$e^+e^-$  machines: Belle, BESIII, BaBar  
pp production: LHCb, ALICE, CMS, ATLAS  
b-decays: LHCb, BaBar  
pip and lepton production: COMPASS  
photoproduction: GlueX, Crystal Barrel  
 $p\bar{p}$  annihilation: Crystal Ball, (PANDA)

1. Select clean data sample
2. Identify hadronic resonances
  3. Pole mass and width  
(reaction-theory analysis)
  3. Spin and parity  
(angular analysis)

# Angular Analysis



Correlations in angular distributions give access to particle spins

- model-independent rotational properties

$$A_{\lambda_0, \lambda_1, \lambda_2}^{(23)} = \underbrace{\square(\phi_i, \theta_i)}_{0 \rightarrow X, 1} \times \underbrace{\square(\phi'_i, \theta'_i)}_{X \rightarrow 2, 3} \times \underbrace{\square(\phi''_i, \theta''_i)}_{\text{spin align.}}$$

- unphysical inhomogeneity
- spin 1/2:  $A(\pi) \neq A(-\pi)$
- range of  $\phi$  matters  $[-\pi, \pi]$  vs  $[0, 2\pi]$

Recent simplification of amplitude construction approach

[IPAC, PRD 101, 034033 (2020)]

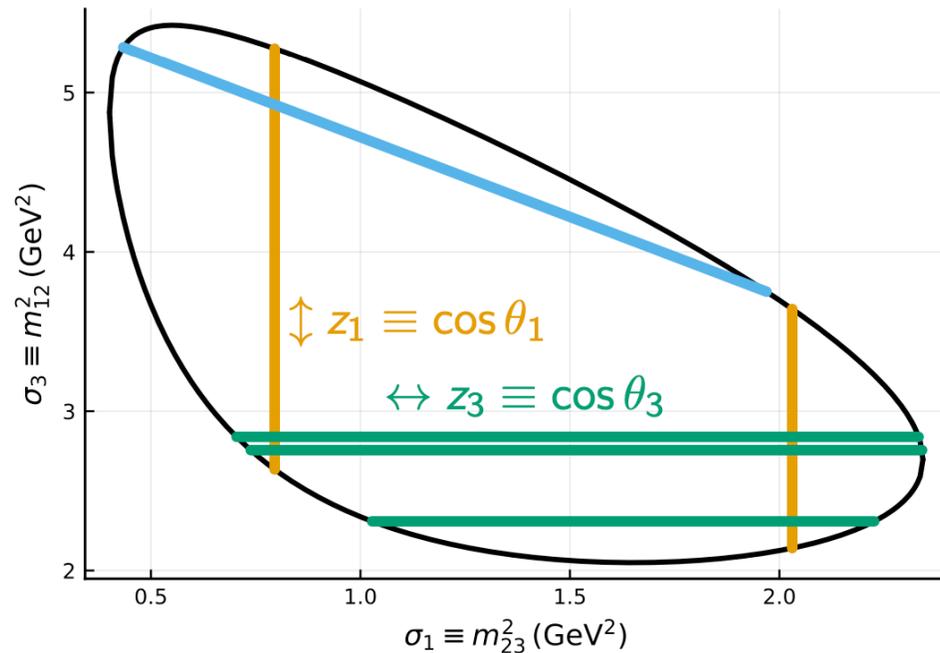
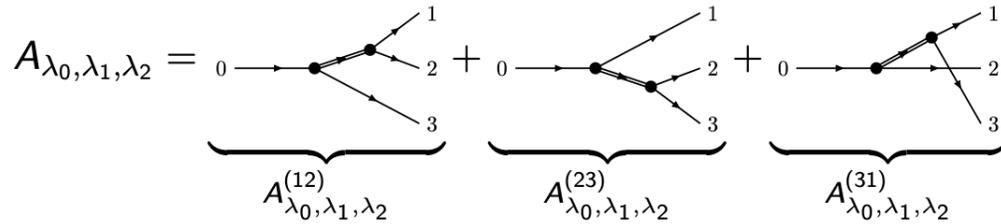
$$A_{\lambda_0, \lambda_1, \lambda_2} = \sum_{\nu} D_{\lambda_0, \nu}^{1/2*}(\alpha, \beta, \gamma) \underbrace{O_{\lambda_1, \lambda_2}^{\nu}(m_{12}^2, m_{23}^2)}_{O^{(12)} + O^{(23)} + O^{(31)}}$$

$$O_{\nu, \lambda_1, \lambda_2}^{(23)}(m_{12}^2, m_{23}^2) = \underbrace{\square}_{0 \rightarrow X, 1} \times \underbrace{\square}_{X \rightarrow 2, 3} \times \underbrace{\square}_{\text{spin align.}}$$

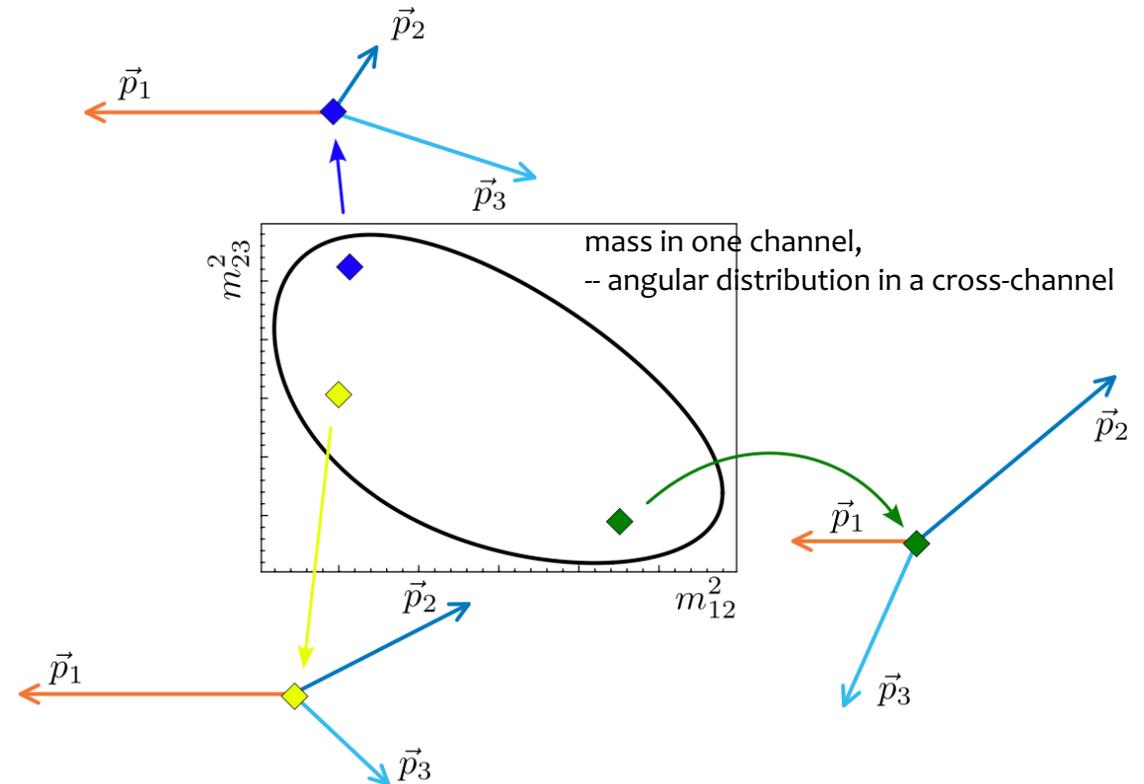
- correct  $\phi$  dependence by construction

# Dynamic modeling

## Cascade-reaction approach (“isobar model”)



Due to cross channels  
angular distributions and dynamic lineshapes  
are mixed



# Hadronic amplitude

Probability density function is a square of amplitude summed over spin projections

$$I(s) = \sum_{\text{spin}} |A(s)|^2$$

$A(s)$  is a complex function of energy,  $s = E^2$

Example of a resonance amplitude

$$A(s) = \frac{N(s)}{m^2 - s - ig^2\rho(s)}$$

$N(s)$  is reaction dependent (B-decays / e+e-),  
denominator is universal

Imaginary part is something we control well:

1. Decay threshold is far away / unknown

$$ig^2\rho(s) = m\Gamma \quad (\text{const})$$

2. The only relevant continuum to consider

$$ig^2\rho(s)$$

**=Breit-Wigner=**

3. there are multiple channels to consider

$$i(g_1^2\rho_1 + g_2^2\rho_2 + \dots)$$

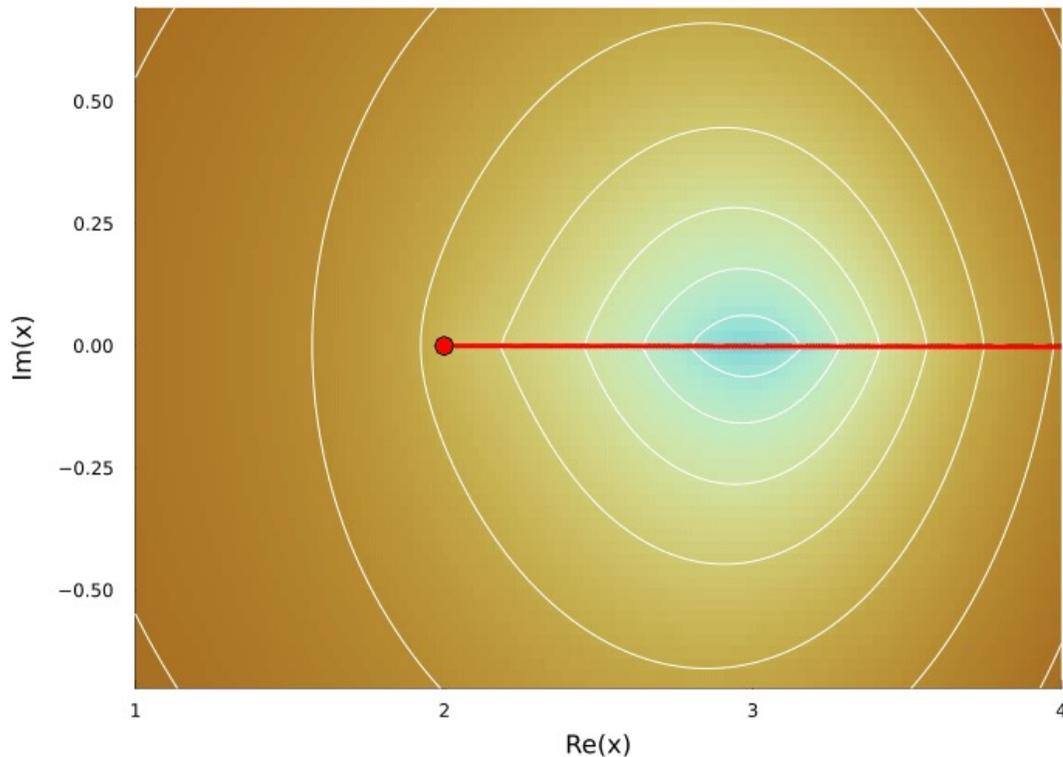
**=Flatte=**

4. Multiple channels, multiple resonances

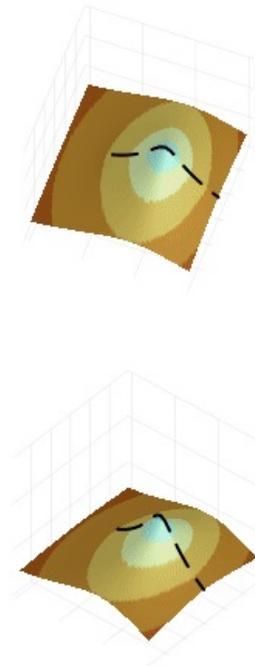
**=K-matrix=**

# Analytic continuation – resonance poles

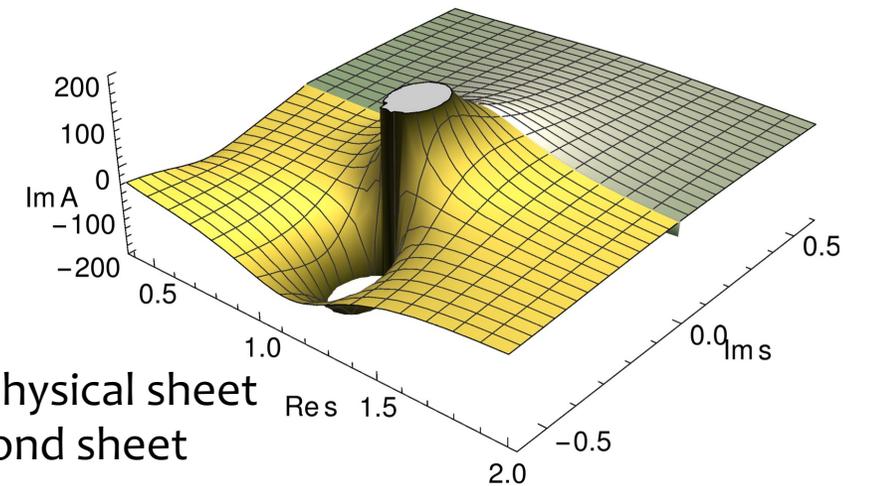
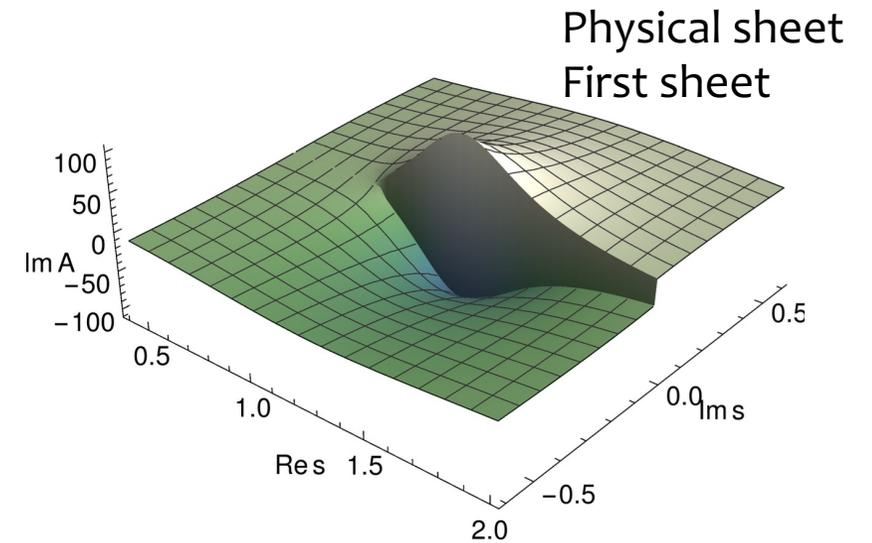
- Amplitude  $A$  is a complex function of  $E = x+iy$
- $\text{Im}(1/A) \sim \text{phase sp.} \sim \text{sqrt}(\text{kin. energy})$
- sqrt branch point – forms two sheets



$$|A(x + iy)|^2$$



$$\text{Im} A(x + iy)$$



# $\chi_{c1}(3872)$

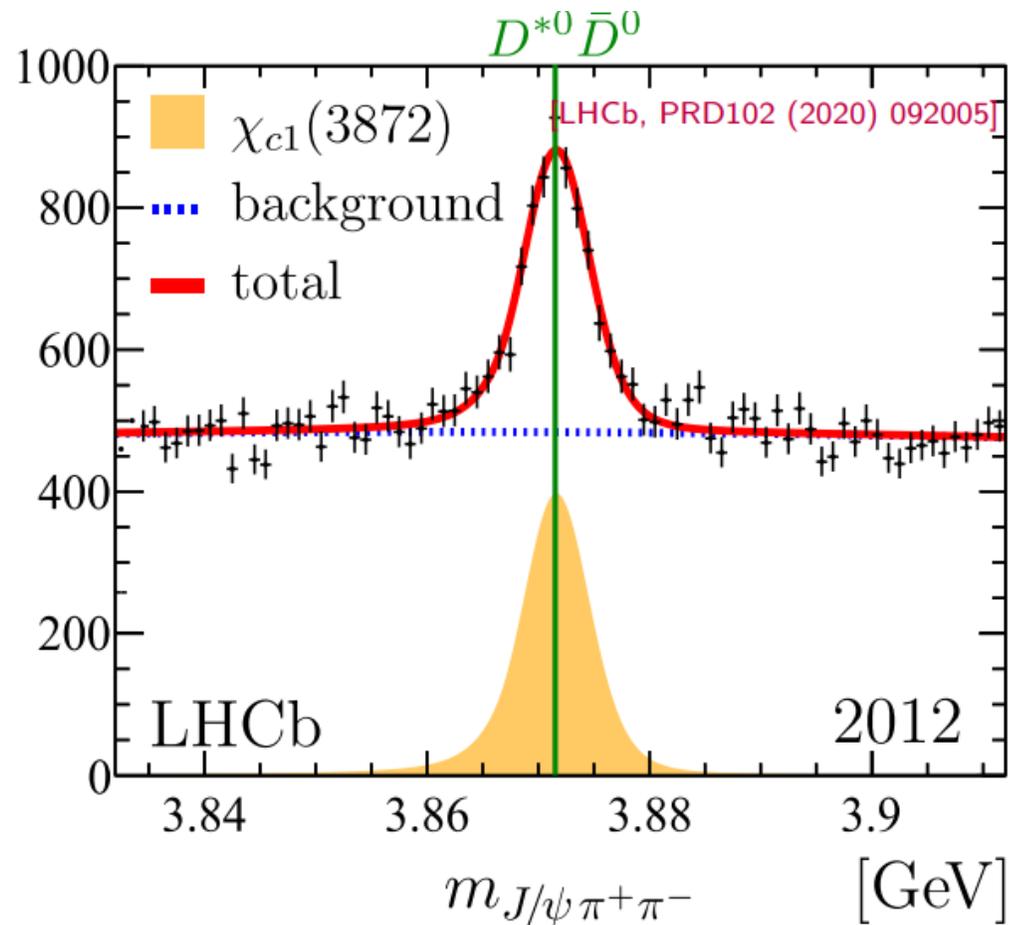
Consistent with the charmonium state that shows up next to **hadron-hadron threshold**  
exhibit molecular properties

QM core, molecular appearance

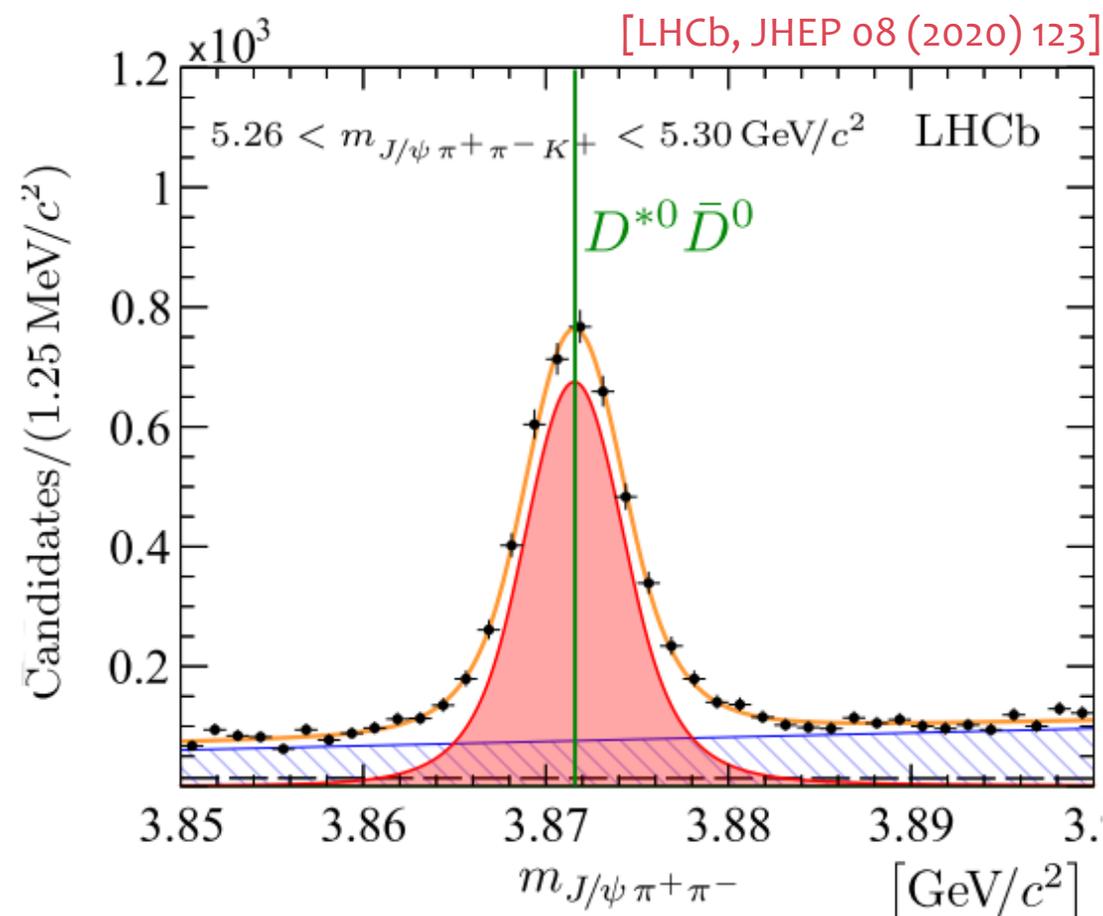
Seen in  $e+e^-$  by Belle, BESIII, BaBar  
Seen in  $pp$  by LHCb, CMS, ALICE.  
Seen in  $b$ -decays by LHCb, BaBar,  
Might be seen in lepton production by COMPASS

# $\chi_{c1}(3872)$ is right at the $D^0 D^{*0}$ threshold

Prompt production ( $pp \rightarrow \chi_{c1} X$ )



From B-decays ( $B^+ \rightarrow \chi_{c1} K^+$ )



# $\chi_{c1}(3872)$ lineshape and parameters

## Flatte lineshape

$$A(s) = \frac{1}{m^2 - s - ig^2 \rho_{D^* \bar{D}} - im\Gamma_0}$$

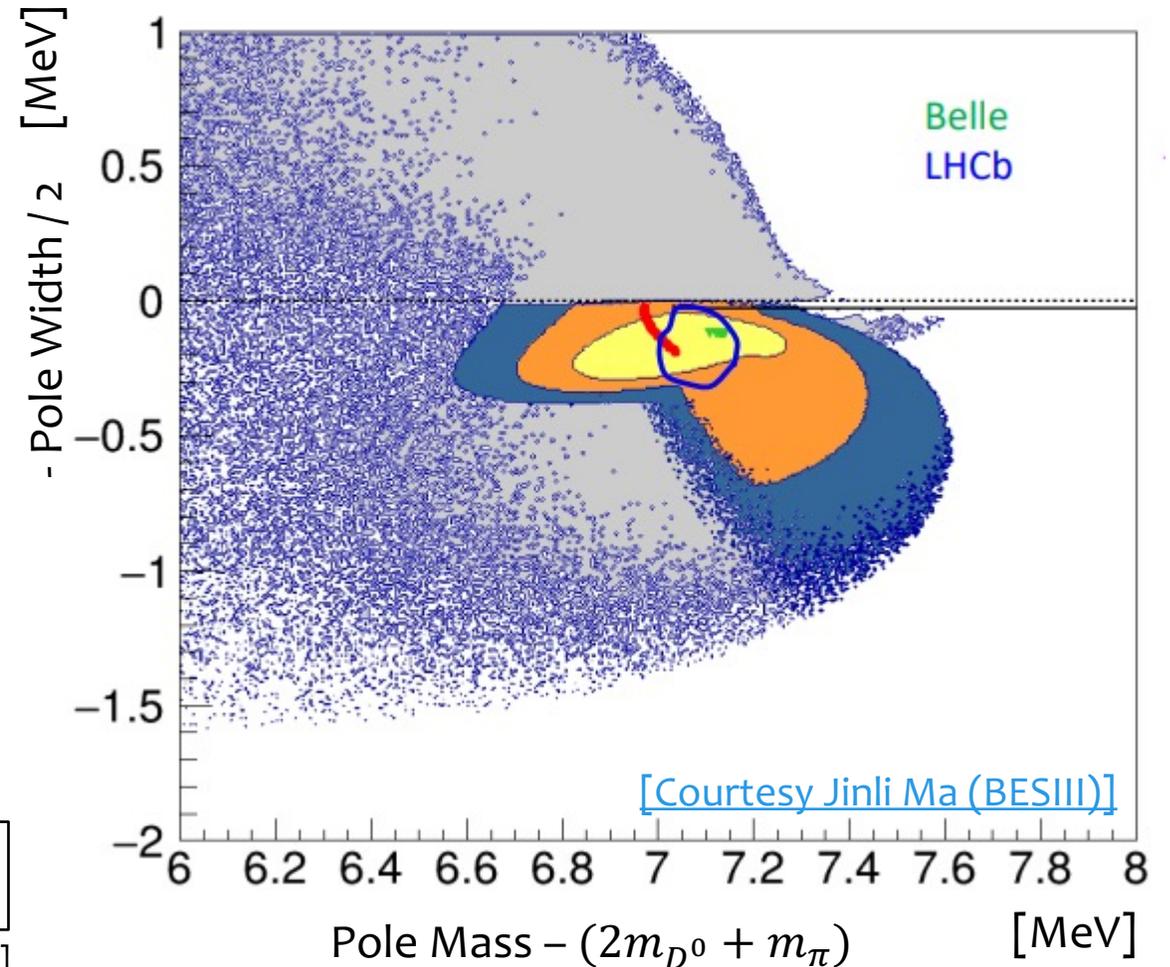
## General agreement on the pole parameters between BESIII, Belle, LHCb:

- Analysis of  $J/\psi \pi^+ \pi^-$  by LHCb  
[PRD102 (2020) 092005]

- BESIII combined analysis of  $J/\psi \pi^+ \pi^-$  &  $D^{0*} \bar{D}^0$   
[hep-ex: [2309.01502](https://arxiv.org/abs/2309.01502)]

$\Gamma_{\text{known}}/\Gamma_{\pi^+\pi^- J/\psi}$	$\beta$	2.8
$\Gamma_{\text{unknown}}/\Gamma_{\pi^+\pi^- J/\psi}$	$\alpha$	8

[C. Li and C.-Z. Yuan, PRD 100, 094003 (2019)]



# Doubly heavy tetraquark $T_{QQ}$

Look like regular QM-tetraquark state similar to  $\Lambda_b^0$  baryon

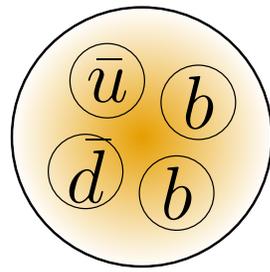
$T_{cc}^+$  : shows up next to hadron-hadron threshold  
exhibit molecular properties

$T_{bb}^-$  : decays weakly, can flies meters

Only seen in pp by LHCb

$T_{cb}^0$  : likely to exist

# Tetraquark $T_{bb}^-$



Firmly established in pheno, e.g.

[\[Ader, Richard, PRD 25, 2370 \(1982\)\]](#)

lattice calculations, e.g.

[\[Francis et al., PRL 118, 142001 \(2017\)\]](#)

Below open-flavor threshold

Stable wrt strong interaction

Similar to a “regular” QM hadron

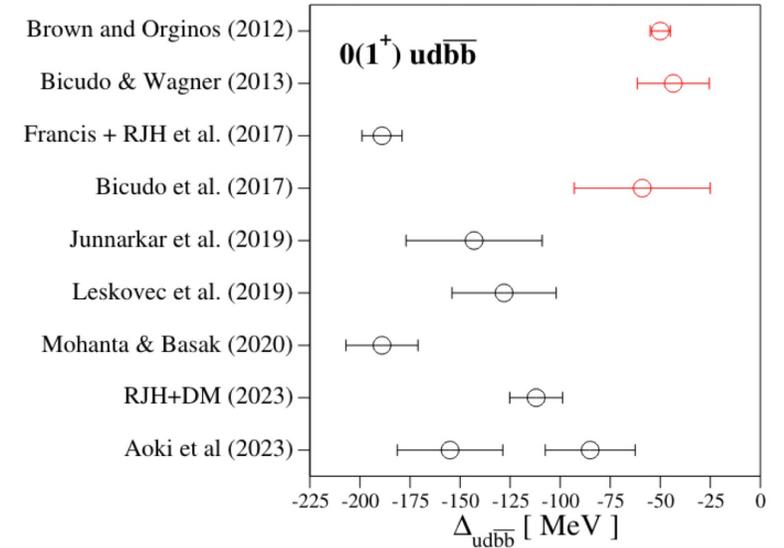
bb are close together, and

are in color-anti-triplet

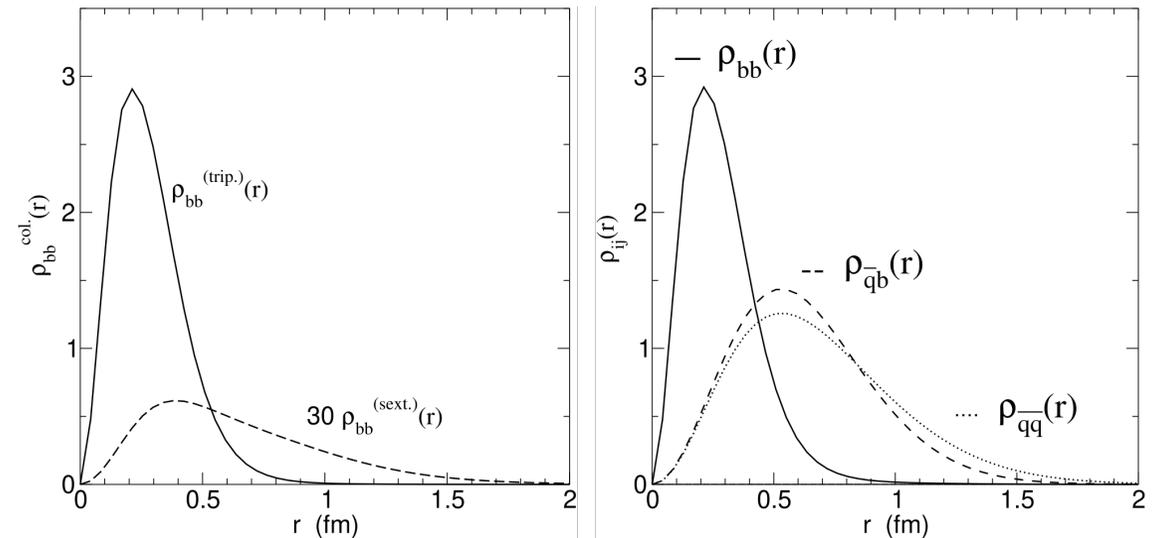
Not yet seen experimentally; won't be soon

Anticipated for 50y

[courtesy Renwick Hudspith]



[\[Janc, Rosina, FBS35 \(2004\) 175-196\]](#)



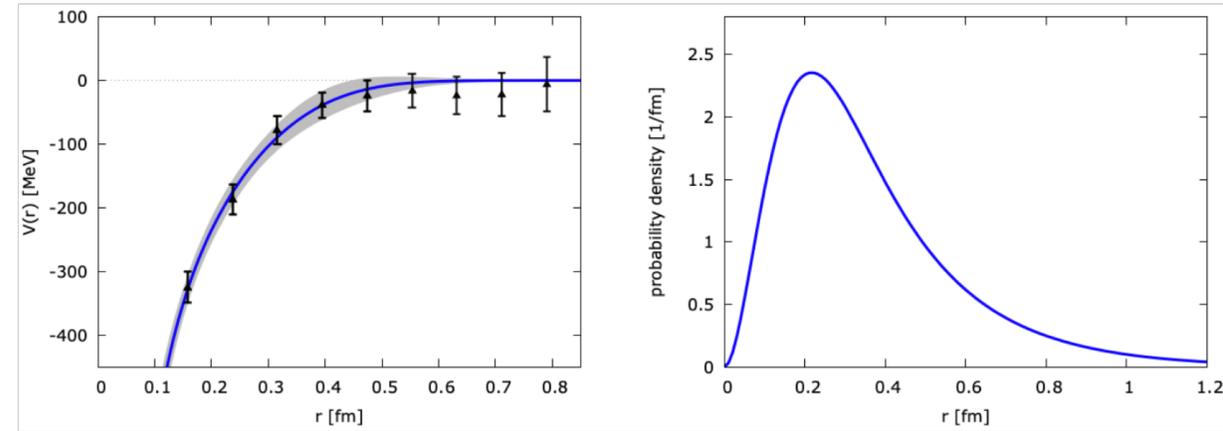
# Continuum for $T_{bb}^-$

Born-Oppenheimer approach with a lattice potential

Diquark-diquark configuration vs meson-meson configurations

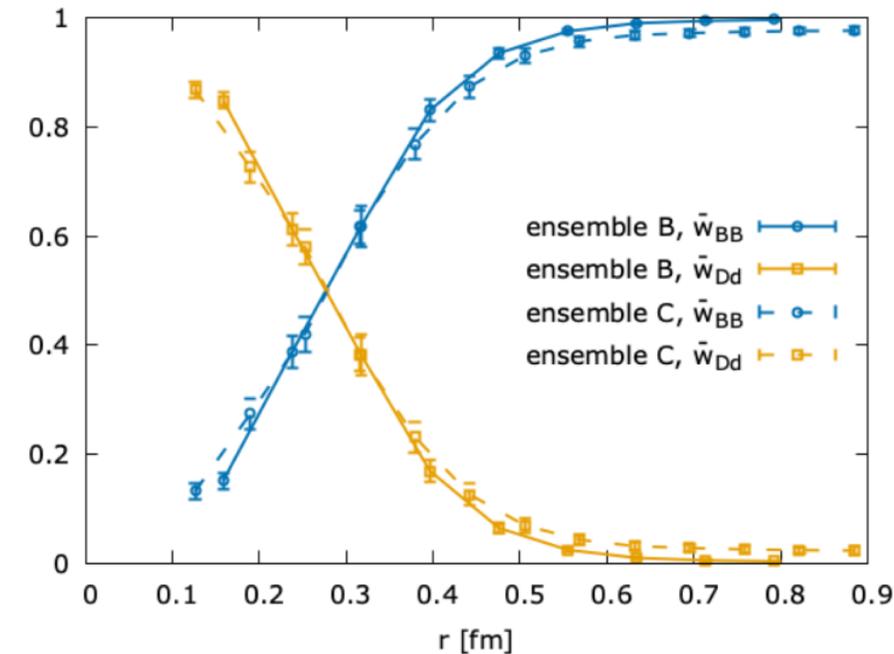
Tetraquark component dominants at smaller  $r$ , while at the high  $r$  tails, the molecular component is present.

meson-meson is surprisingly important

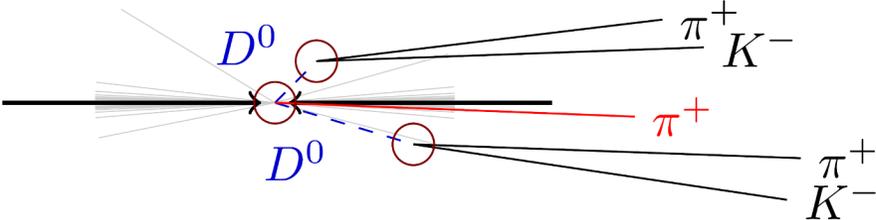


$$\mathcal{O}_{BB,\Gamma} = 2N_{BB}(C\Gamma)_{AB}(C\tilde{\Gamma})_{CD} \left( \bar{Q}_C^a(\mathbf{r}_1)\psi_A^{(f)a}(\mathbf{r}_1) \right) \left( \bar{Q}_D^b(\mathbf{r}_2)\psi_B^{(f')b}(\mathbf{r}_2) \right)$$

$$\mathcal{O}_{Dd,\Gamma} = -N_{Dd}\epsilon^{abc} \left( \psi_A^{(f)b}(\mathbf{z})(C\Gamma)_{AB}\psi_B^{(f')c}(\mathbf{z}) \right) \epsilon^{ade} \left( \bar{Q}_C^f(\mathbf{r}_1)U^{fd}(\mathbf{r}_1;\mathbf{z})(C\tilde{\Gamma})_{CD}\bar{Q}_D^g(\mathbf{r}_2)U^{ge}(\mathbf{r}_2;\mathbf{z}) \right)$$



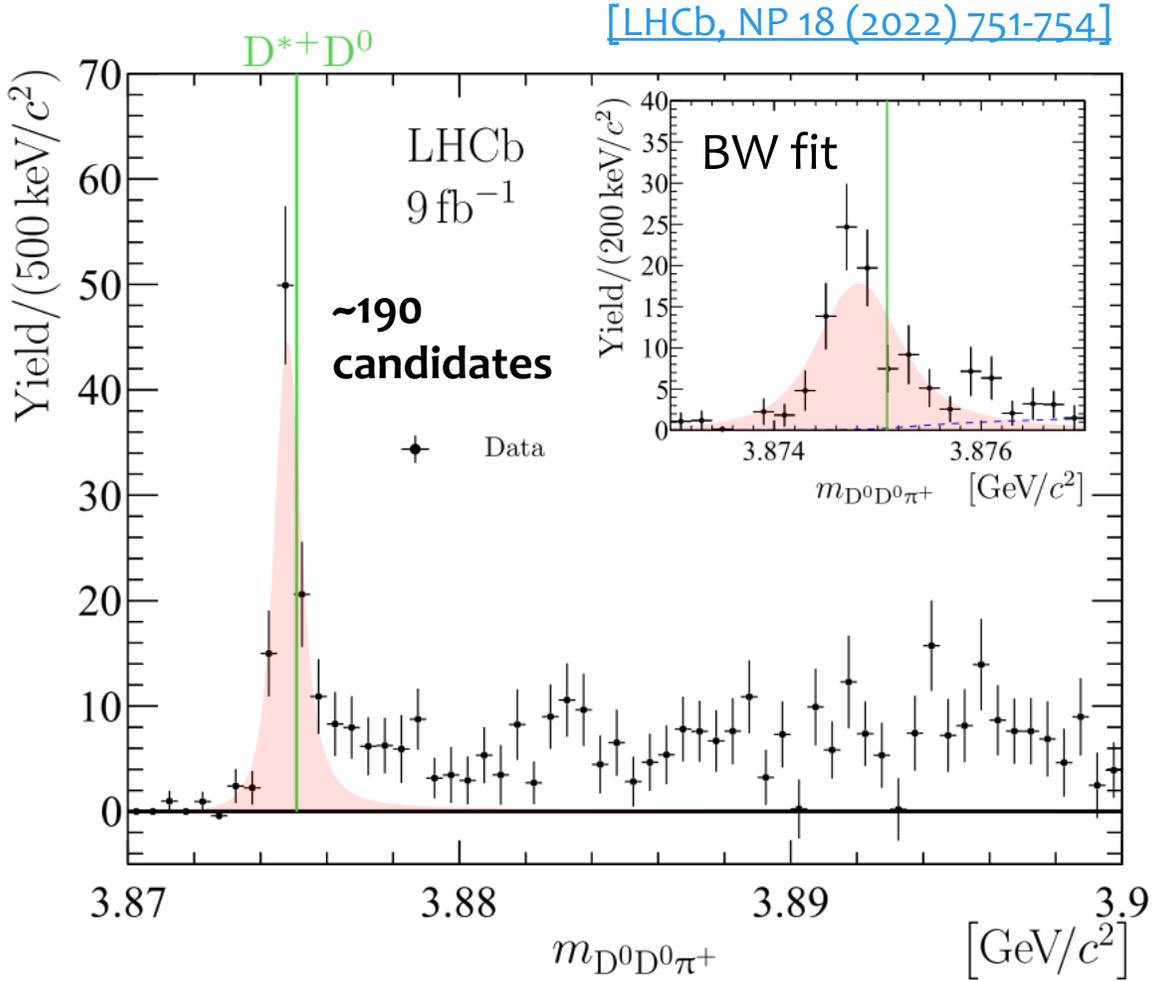
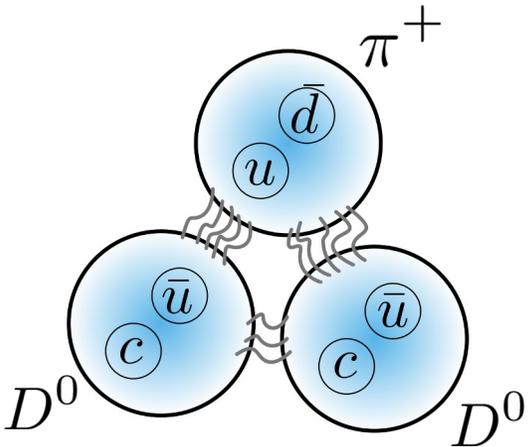
# Doubly-charm tetraquark $T_{cc}^+$ right at the $D^0 D^{*+}$ threshold



Peak in  $D^0 D^0 \pi^+$  just below  $D^{*+} D^0$  threshold

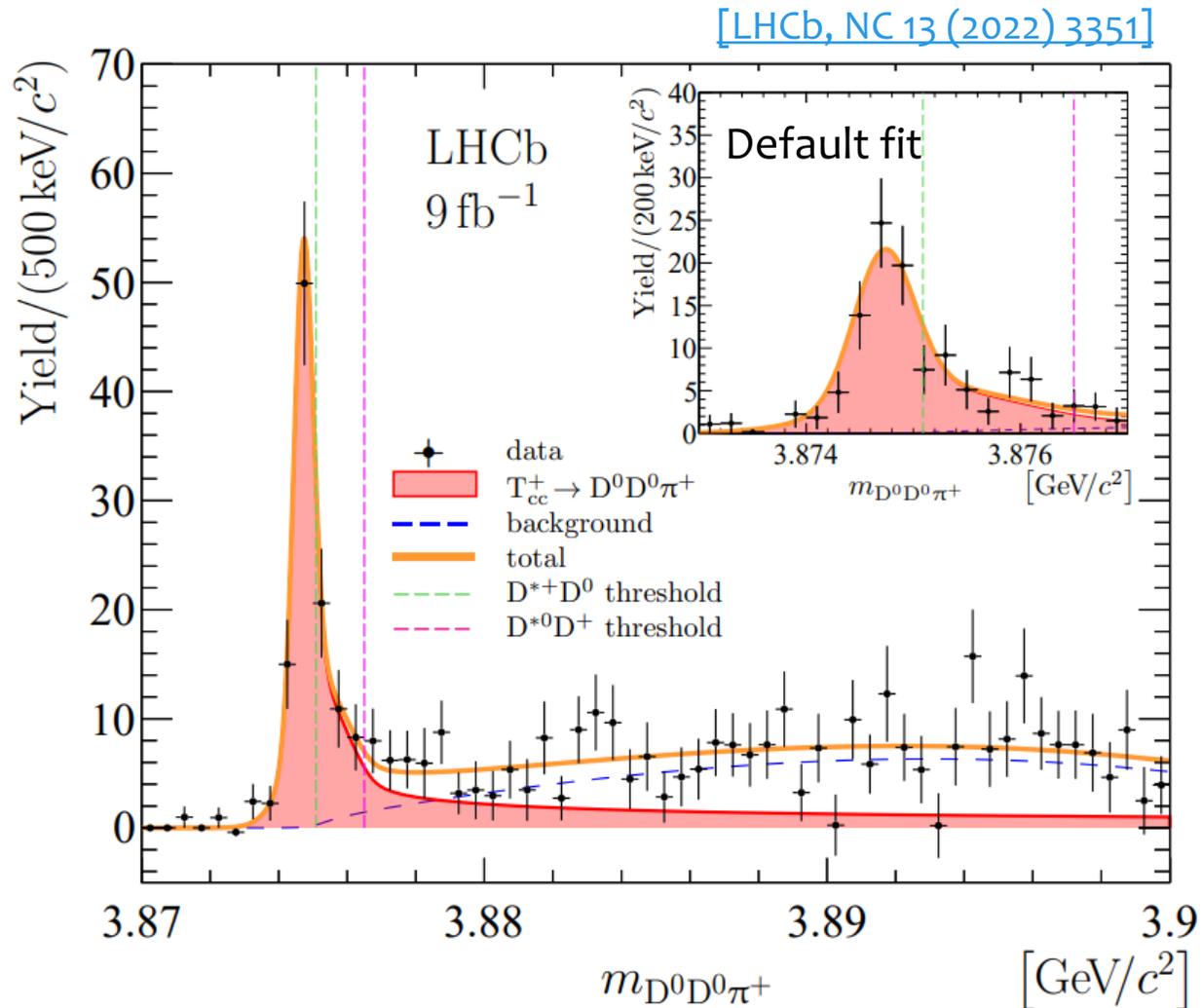
Extremely narrow,  $\sim 300\text{keV}$   
(resolution)

Needs to be treated as  
three-body effect



[LHCb, NP 18 (2022) 751-754]

# Studies of the doubly-charm tetraquark $T_{cc}^+$



QN: isoscalar ( $I = 0$ ), axial ( $J^{PC} = 1^{++}$ )

Coupled channel model

$$D^{*+} D^0 + D^{*0} D^+ \\ \rightarrow \{D^0 D^0 \pi^+, D^0 D^+ \pi^0, D^0 D^+ \gamma\}$$



Yields good agreement with the data

# Analytic continuation and $T_{cc}^+$ pole parameters

Yields pole parameters:

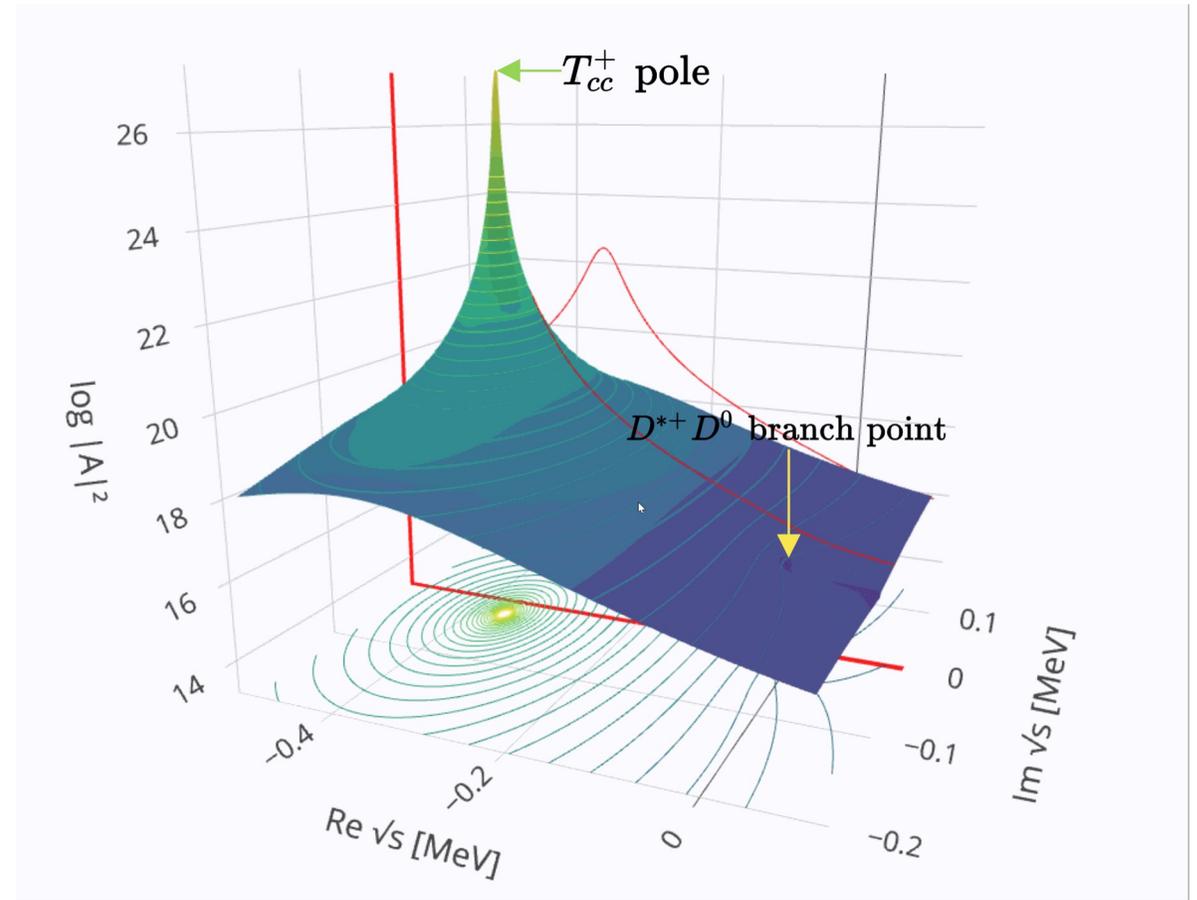
❖ Binding energy:  $-360 \pm 40_{-0}^{+4}$  keV

(well determined by the data)

❖ Width:  $48 \pm 2_{-14}^{+0}$  keV

(driven by the model:  $D^{*+}$  width, pion-exchange)

[Baru et al., ]  
[MM, Effective range, hep-ph:]  
[QWG talk, ]  
[Albaladejo,]



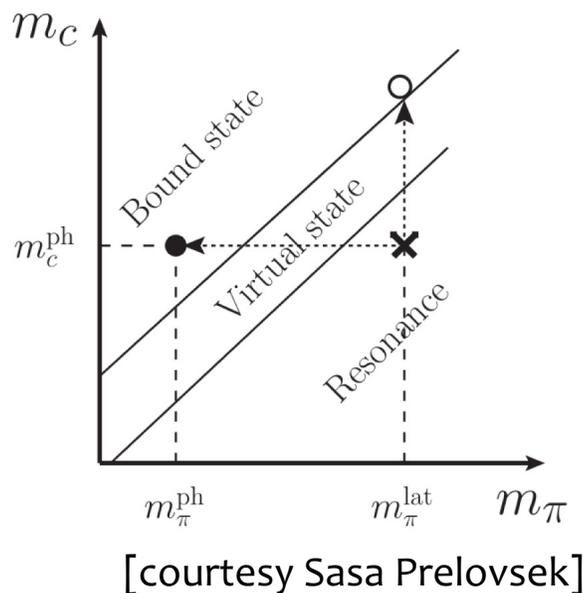
# $T_{CC}^+$ on lattice

Seen on lattice by several groups

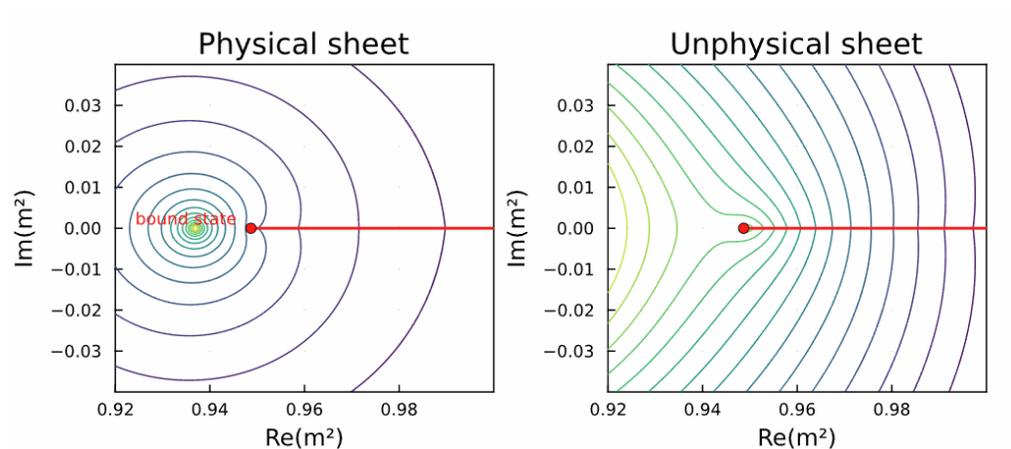
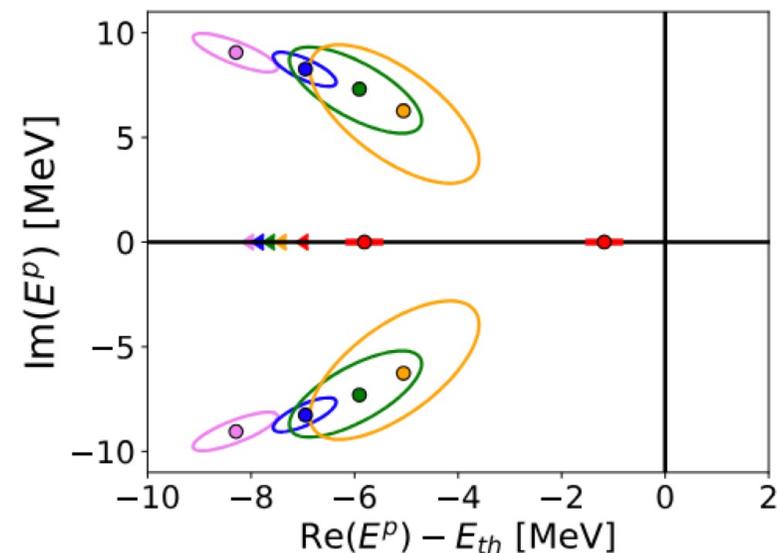
[Yan Lyu et al., PRL131, 161901 (2023)]

[Padmanath-Prelovsek, PRL129, 032002 (2022)]

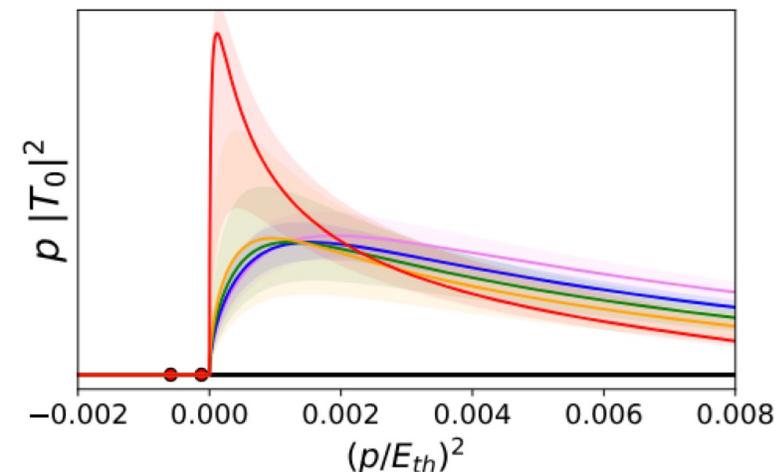
[S. Chen et al., PLB833, 137391 (2022)]



[Collins et al., PRD109 (2024) 9, 094509]



[mmikhasenko@github]



Transition: **bound state** → **virtual state** → **resonance**.

No fundamental difference. The state is mostly **molecular** in vicinity of the threshold

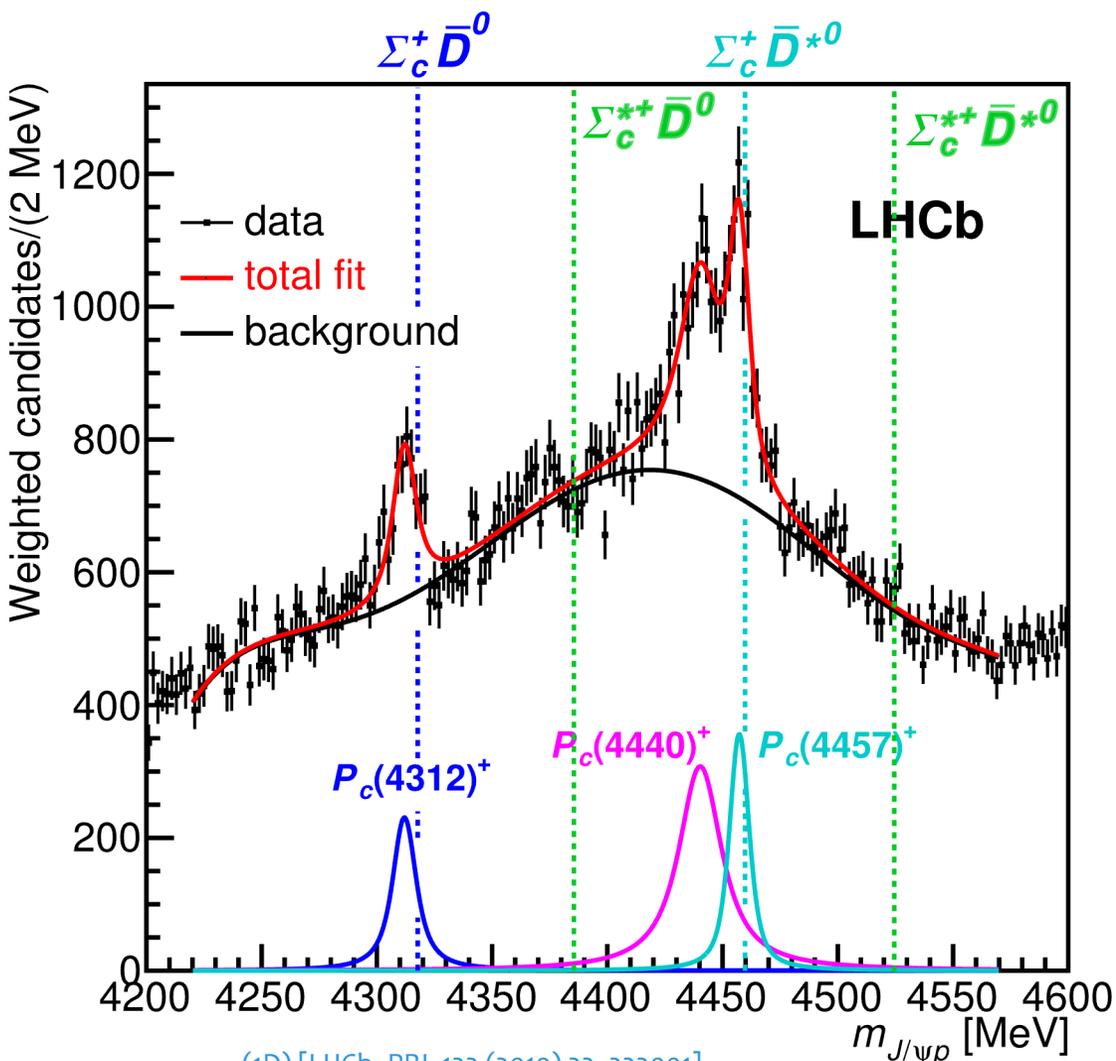
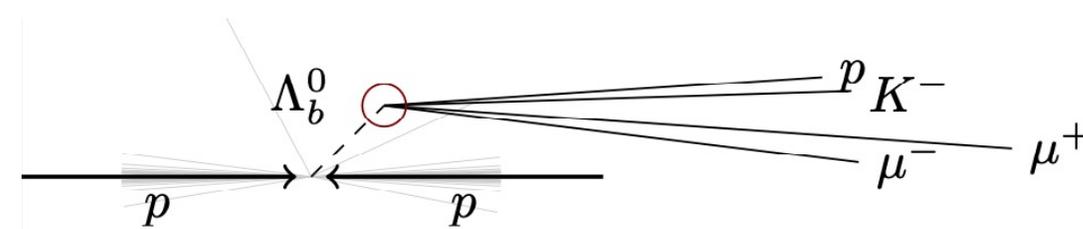
# Pentaquarks $P_{c\bar{c}}^+$

Show up next to hadron-hadron threshold  
unclear if consistent with the QM-tetraquark state that

QM core(?), molecular appearance(!)

Only seem in b-decays by LHCb

# Pentaquarks $P_{c\bar{c}}^+$



Narrow resonance states near threshold of  $\Sigma_c^{+(*)} \bar{D}^{0(*)}$

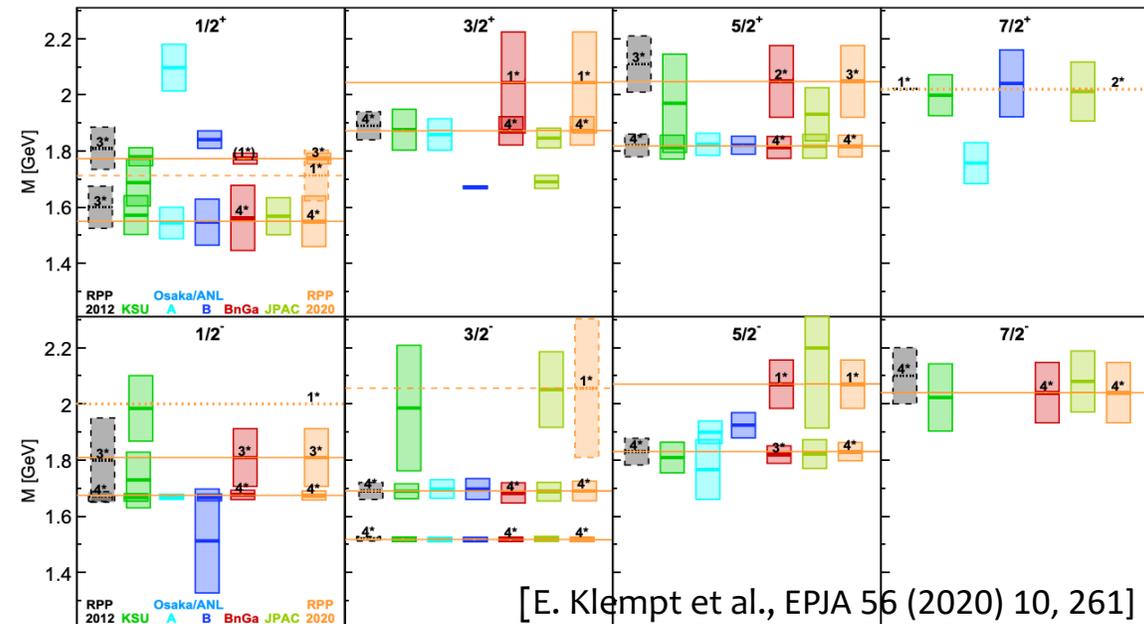
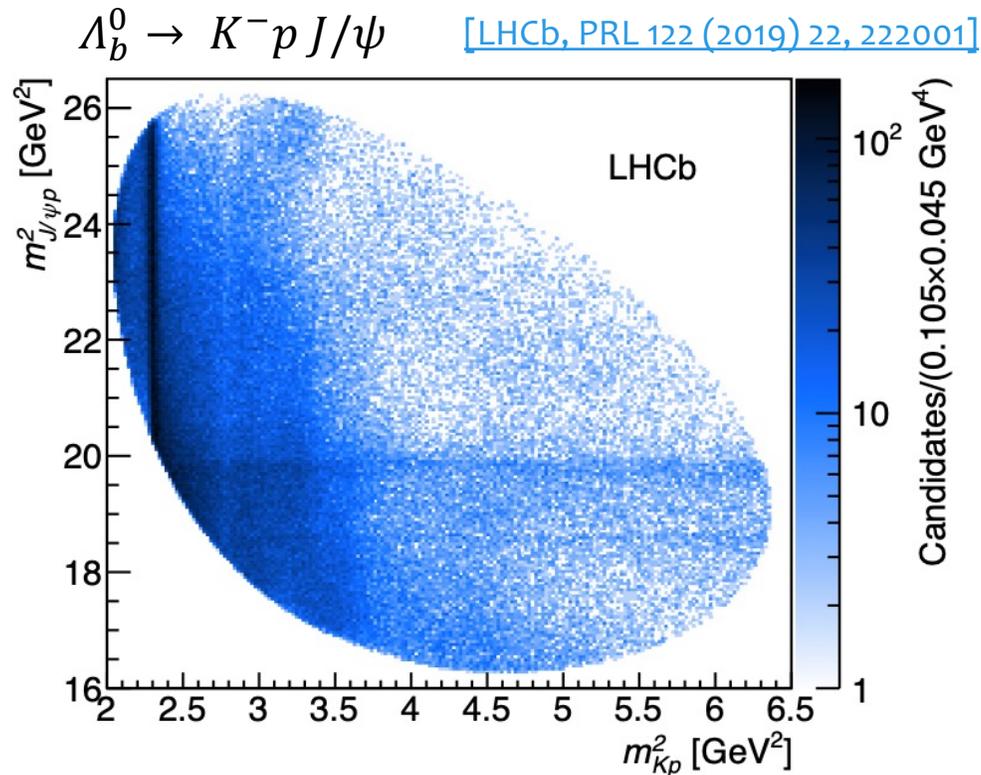
Large background from  $pK^-$  scattering –  $\Lambda$  resonances

[\(1D\) \[LHCb, PRL 122 \(2019\) 22, 222001\]](#)

[\(AmAn\) \[LHCb, PRL 115 \(2015\), 072001\]](#)

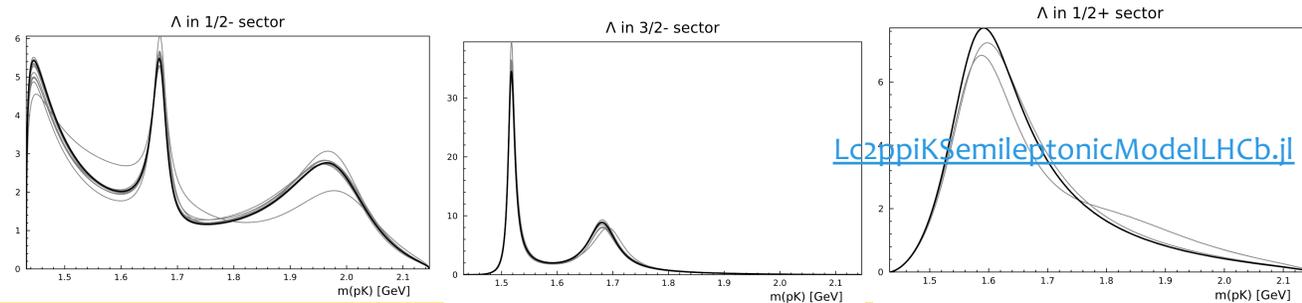
# Challenges for amplitude analysis (work in progress)

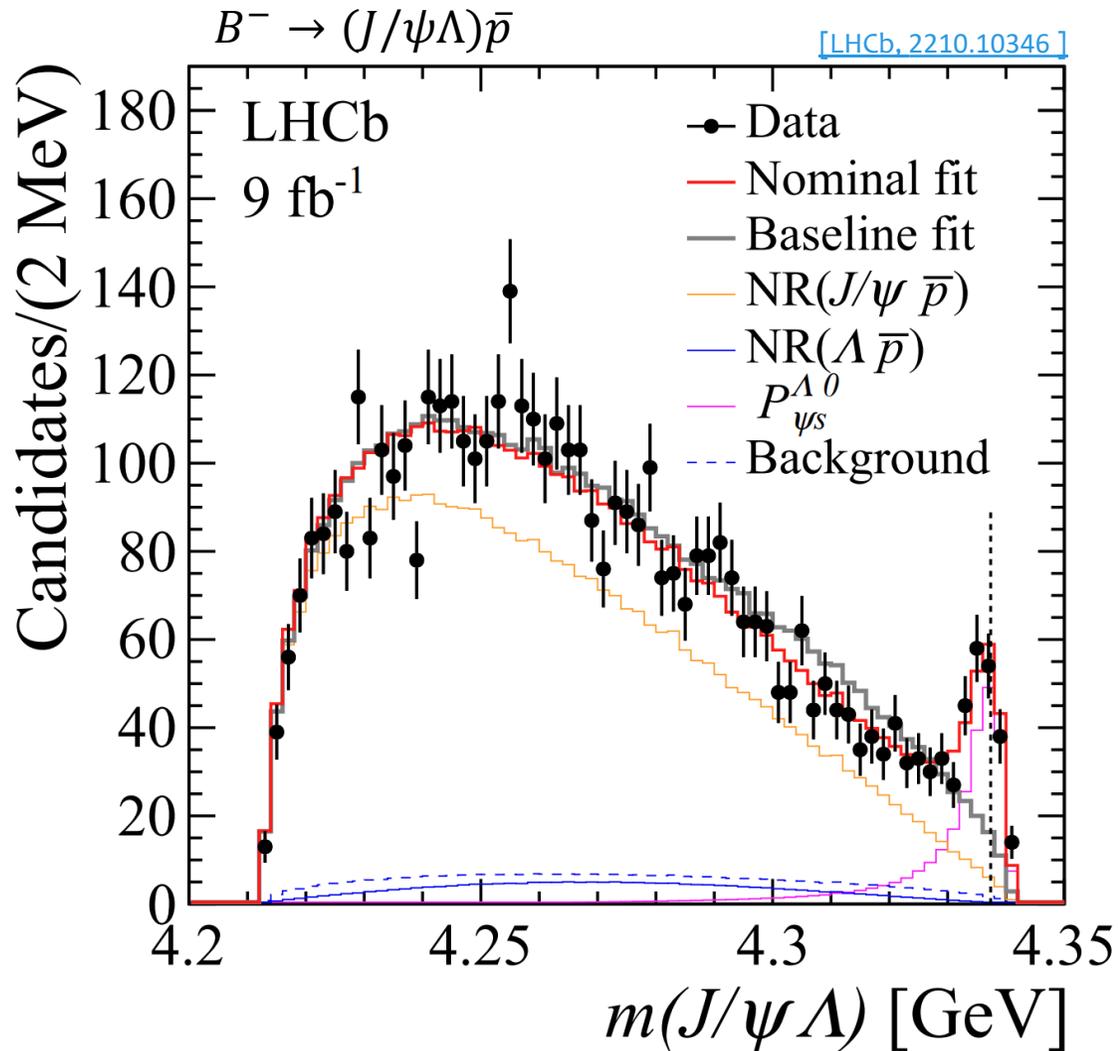
Might benefit from knowledge on  $\Lambda$  spectrum from  $p K^-$  scattering data is needed



Phase space is dominated by resonances in  $p K^-$

- Interfering background
- Largely unknown, now well constrained





## Strange Partner\*

Prominent peak near  $\Xi_c \bar{D}$  threshold

❖  $0.8 \pm 0.7$  MeV above  $\Xi_c^+ D^-$

❖  $2.9 \pm 0.7$  MeV above  $\Xi_c^0 \bar{D}^0$

$J^P = 1/2^-$  is preferred

Aligned with  $\Xi_c^+ D^-$  molecule

# Fully heavy tetraquarks, $QQ\bar{Q}\bar{Q}$

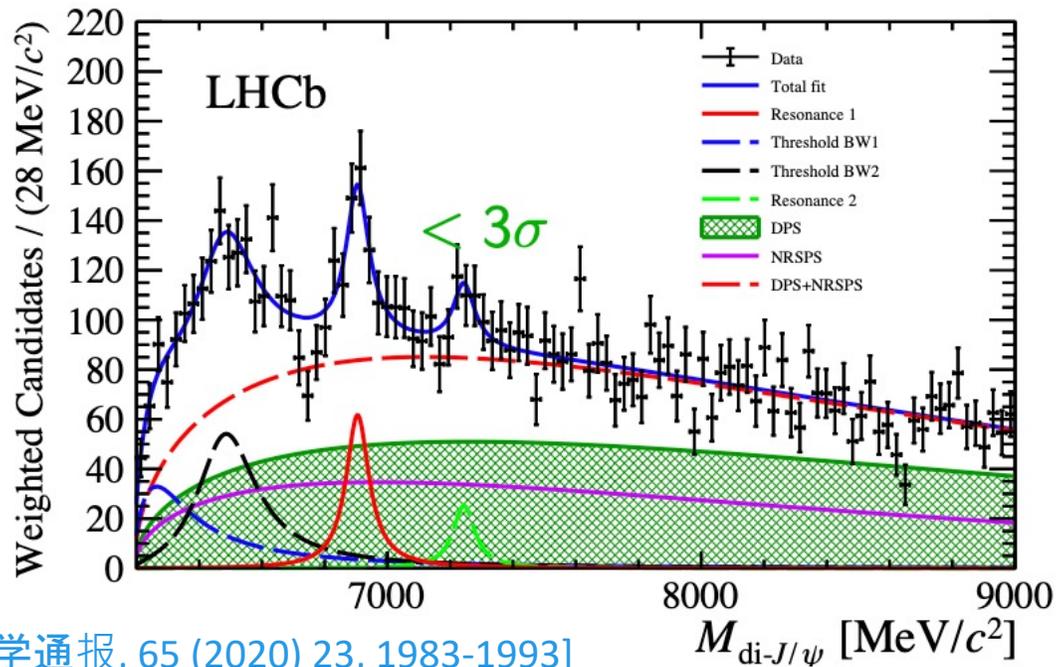
Unclear, many thresholds

Lattice QCD, pheno:  
no hints for binding for  $b\bar{b}b\bar{b}$

Seen in pp by LHCb, CMS, ATLAS

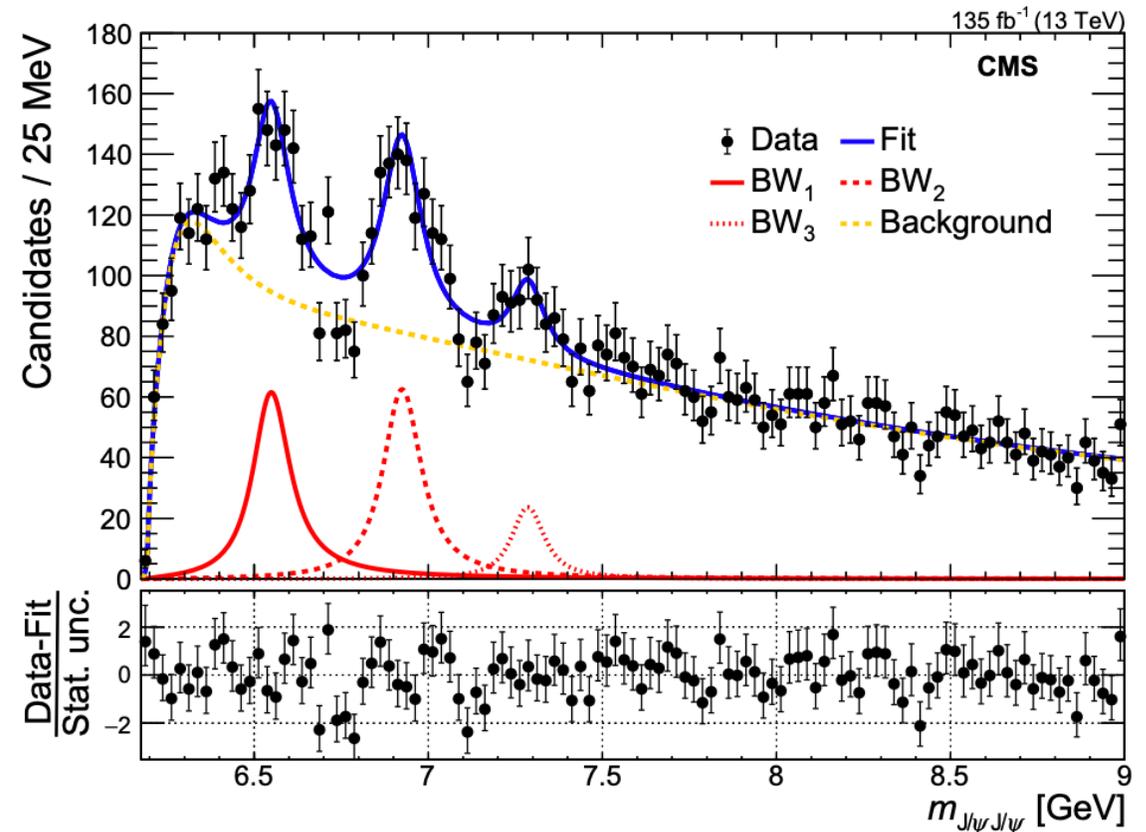
# $cc\bar{c}\bar{c}$ from double $J/\psi$ structures

[PRL 132 (2024) 11, 111901]



[科学通报, 65 (2020) 23, 1983-1993]

- Rapid **raise** at the threshold followed by the **three peaks**.
- Clear dips at 6.8 GeV, and 7.2 GeV
- Only simplistic modeling with unknown JP



# $bb\bar{b}\bar{b}$ from ATLAS

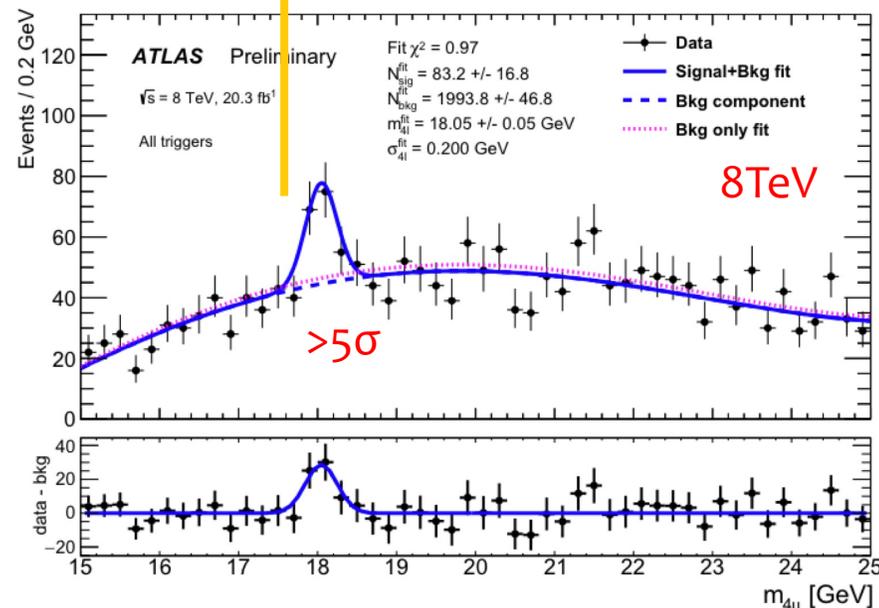
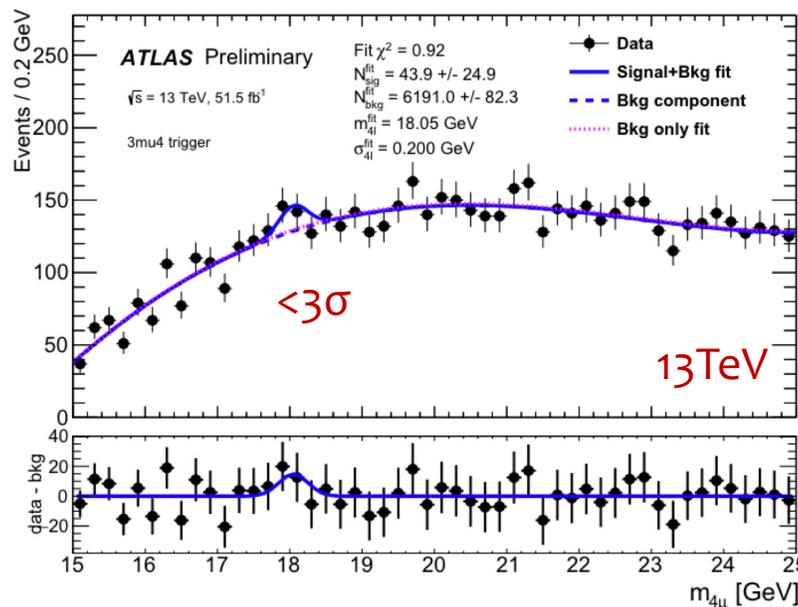
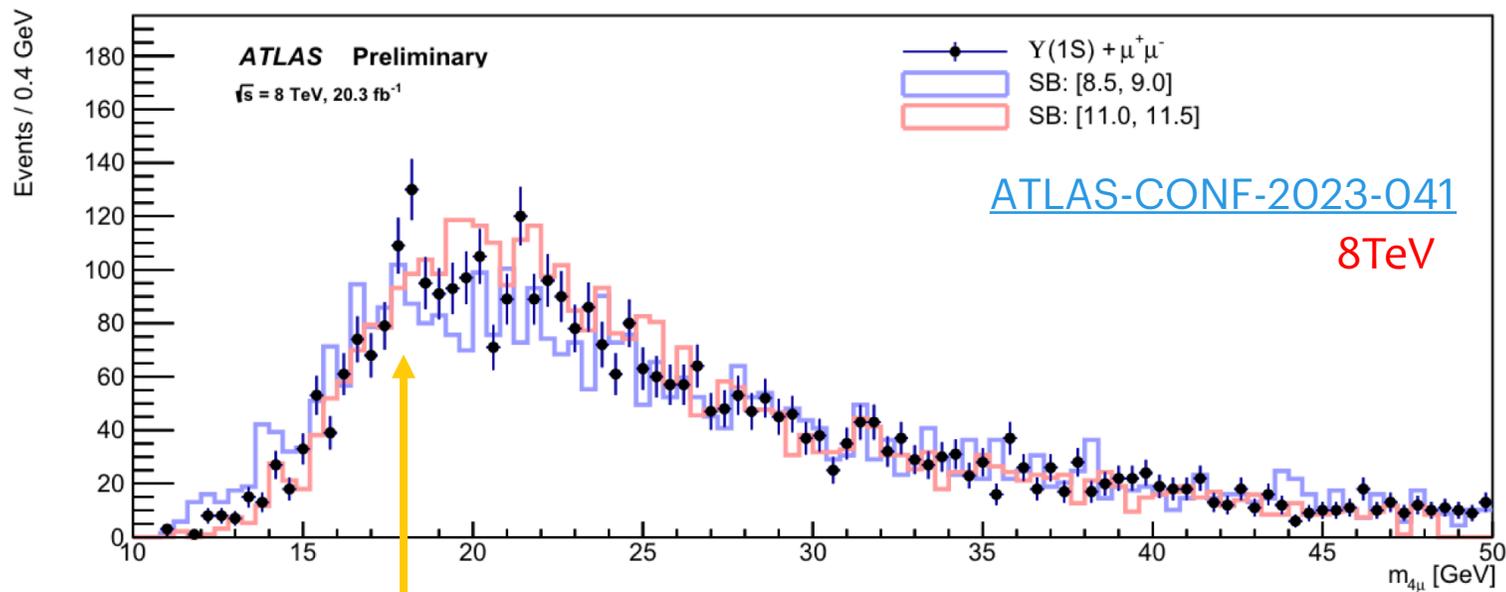
ATLAS observed a signal in  $\Upsilon\mu^+\mu^-$

Local significance  $>5\sigma$

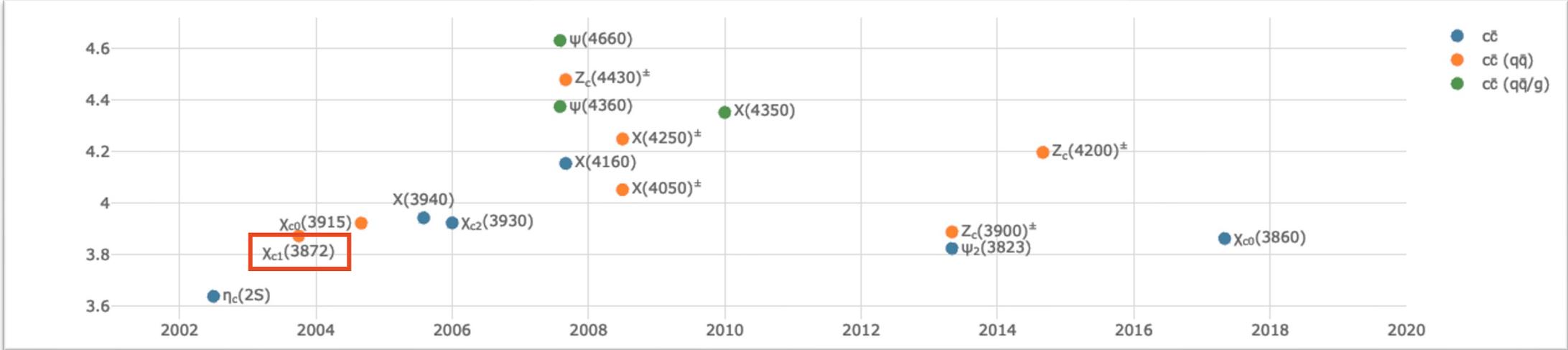
Mass is about 18 GeV

Stable with respect to modifications of cuts trigger conditions.

Disappears with 13TeV data (sadly)

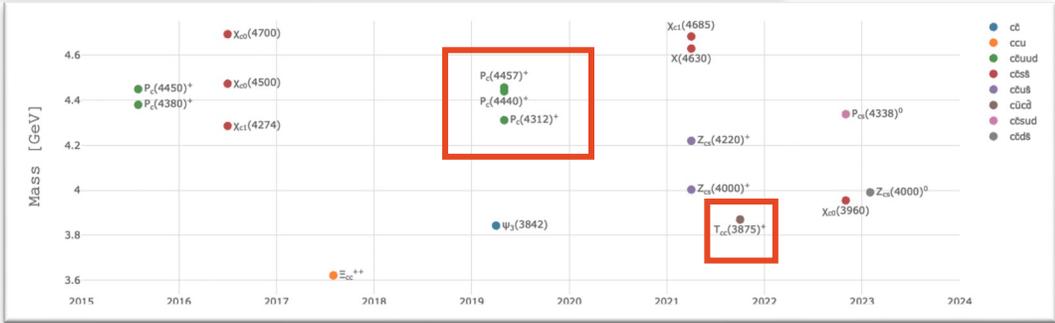


# Many exotic states. Particle zoo v2.0



Belle

LHCb



BESIII



[QWG Exotics hub]



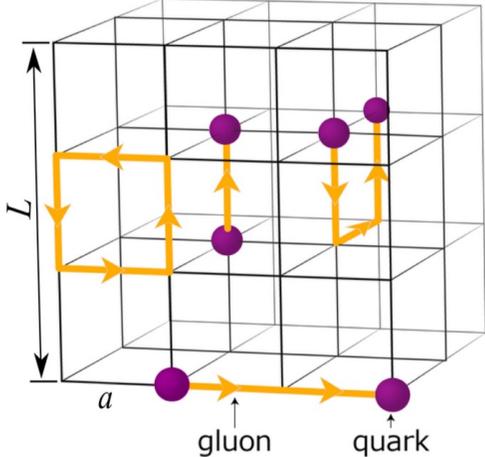
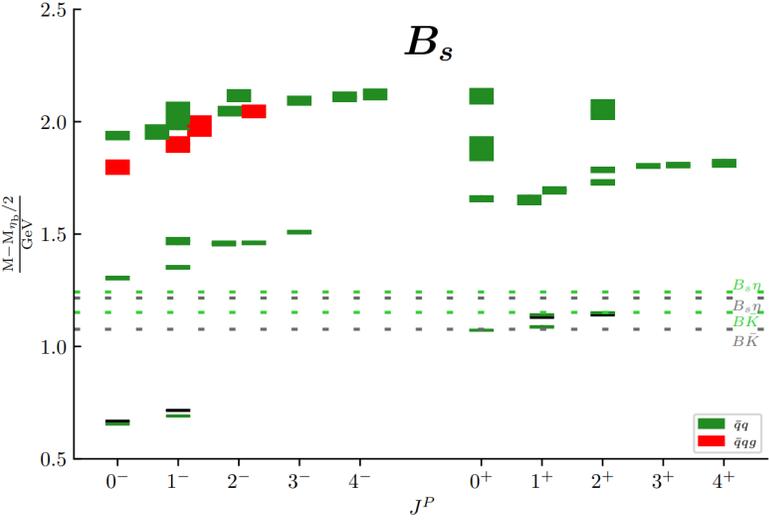
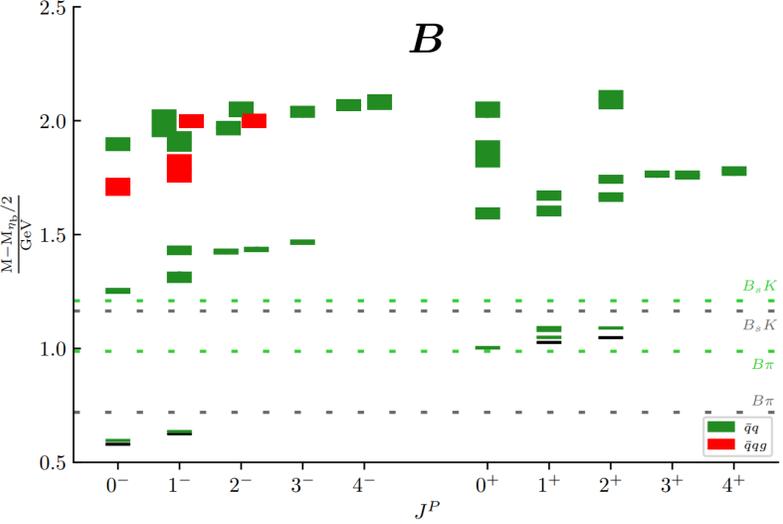
# Open questions on exotic hadrons

Having significant molecular contribution for hadronic state is fine.

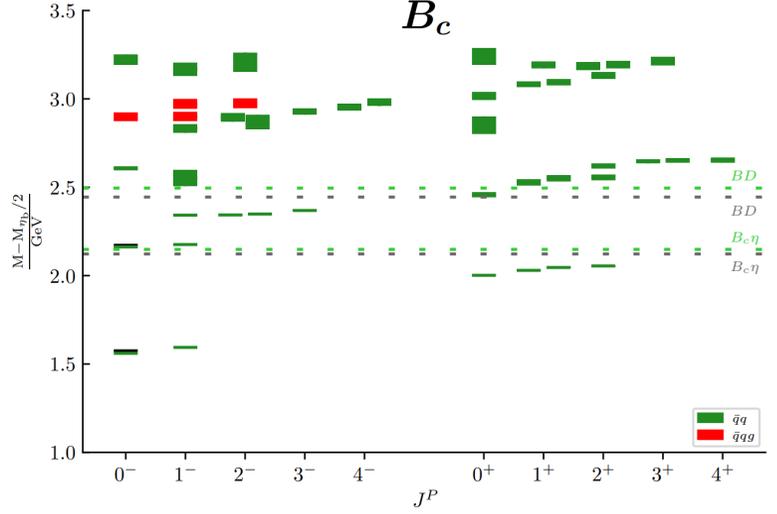
- We do not understand how the continuum acts.  
Why it sets some states **right** on the threshold? [ $\chi_{c1}(3872) \rightarrow D^0 D^{*0}, T_{cc}^+ \rightarrow D^0 D^{*0}$ ]
- Does one always need a genuine QCD seed? – (extra numerous states wrt QM)  
From nuclear physics – “No” (plenty of atoms and isotops)  
 $P_{c\bar{c}}^+, T_{cc\bar{c}\bar{c}}^0$  ?
- Extra-numerous states: hybrids, glueballs?

- Advanced amplitude analysis
- Collaboration of theory & experiment
- Synergy between different subfields  
**is critical to progress**

# Hybrids in meson spectrum



[S. Ryan et al., JHEP 02 (2021) 214]



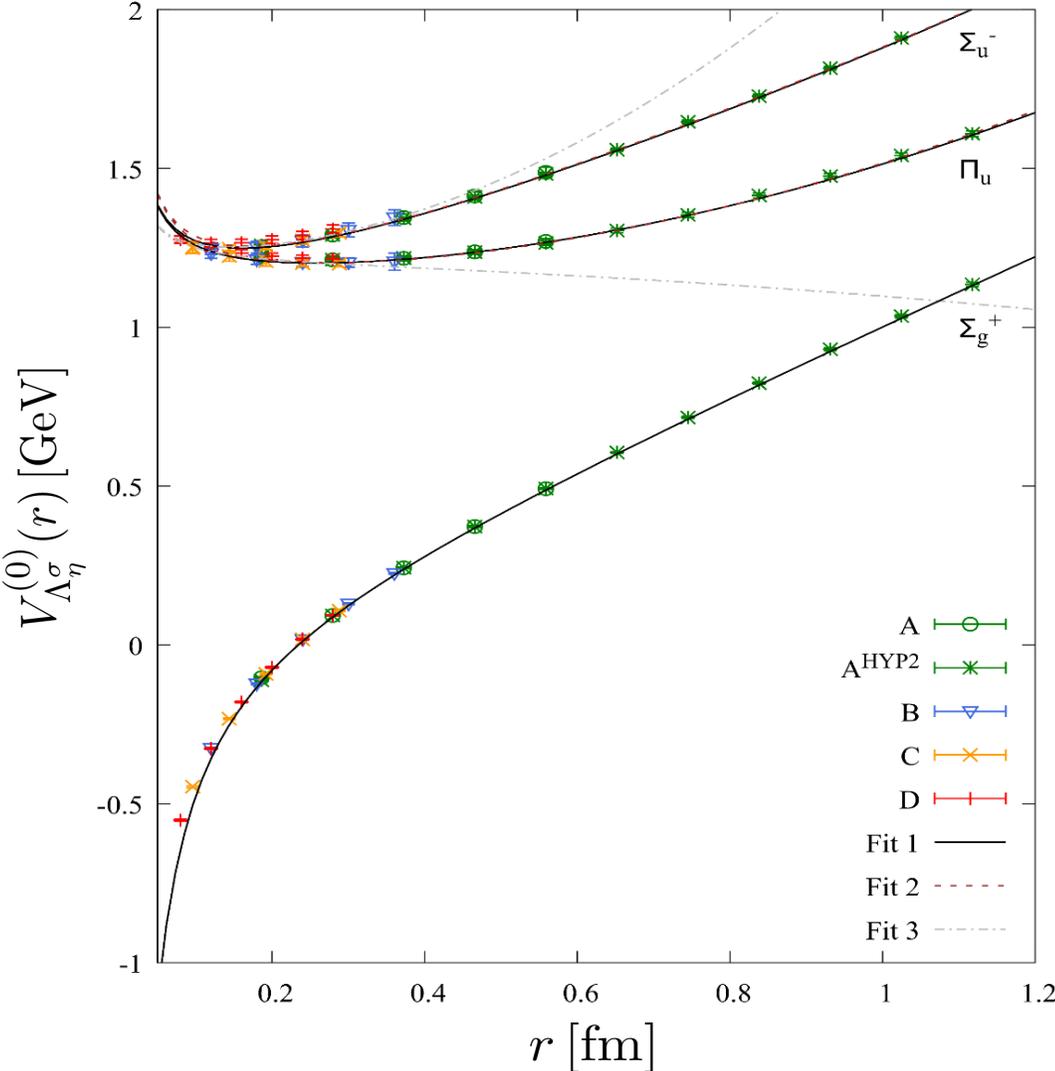
Hybrid states appear in all meson sectors consistently

# Hybrids

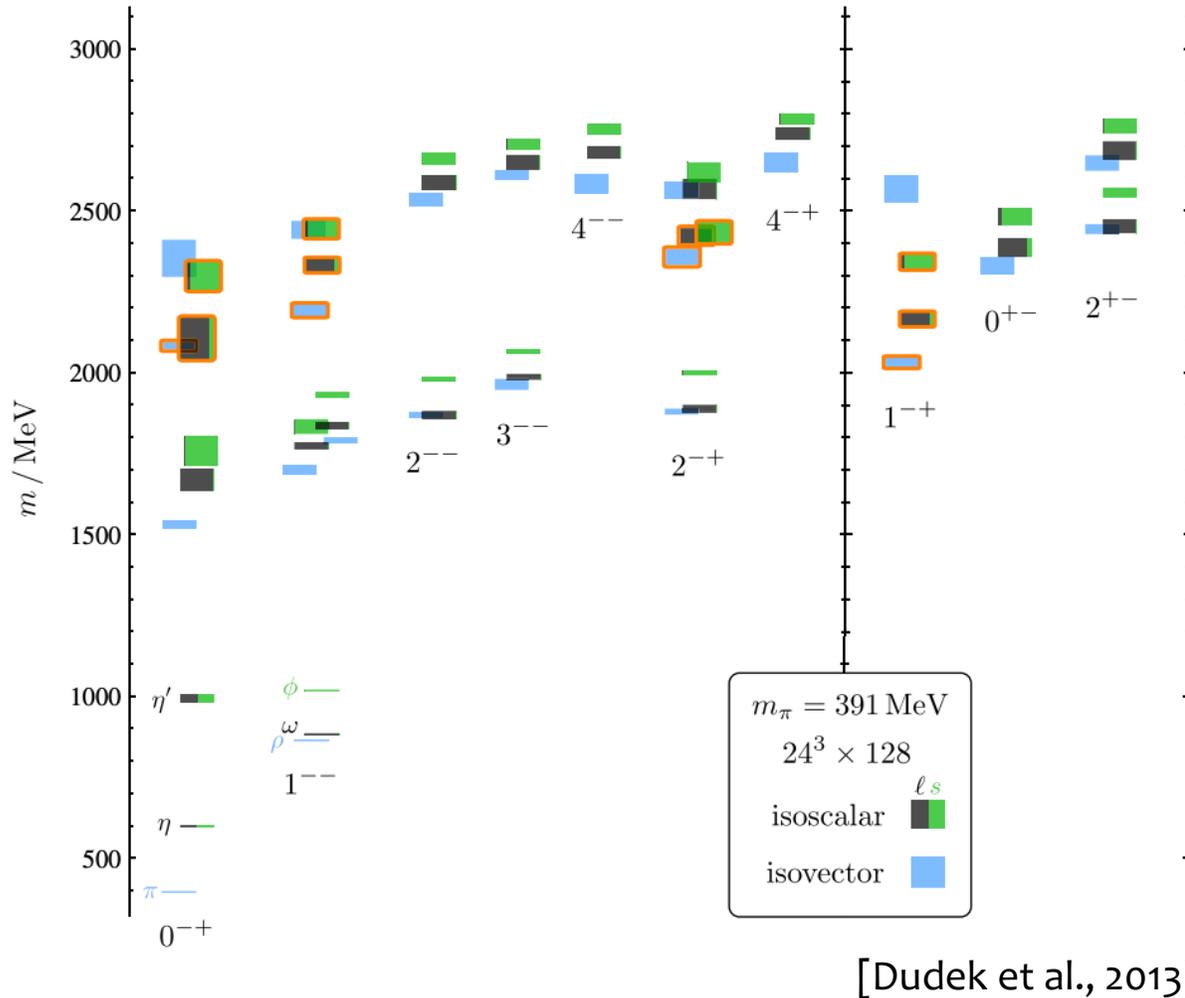
are extra numerous states in charmonium spectrum?

Multiplet	$J^{PC}$	$M_{c\bar{c}g}$	$M_{b\bar{b}g}$
$H_1$	$\{1^{--}, (0, 1, 2)^{-+}\}$	4155	10786
$H'_1$		4507	10976
$H''_1$		4812	11172
$H_2$	$\{1^{++}, (0, 1, 2)^{+-}\}$	4286	10846
$H'_2$		4667	11060
$H''_2$		5035	11270
$H_3$	$\{0^{++}, 1^{+-}\}$	4590	11065
$H'_3$		5054	11352
$H''_3$		5473	11616
$H_4$	$\{2^{++}, (1, 2, 3)^{+-}\}$	4367	10897
$H_5$	$\{2^{--}, (1, 2, 3)^{-+}\}$	4476	10948

[Courtesy to Abhishek Mohapatra]



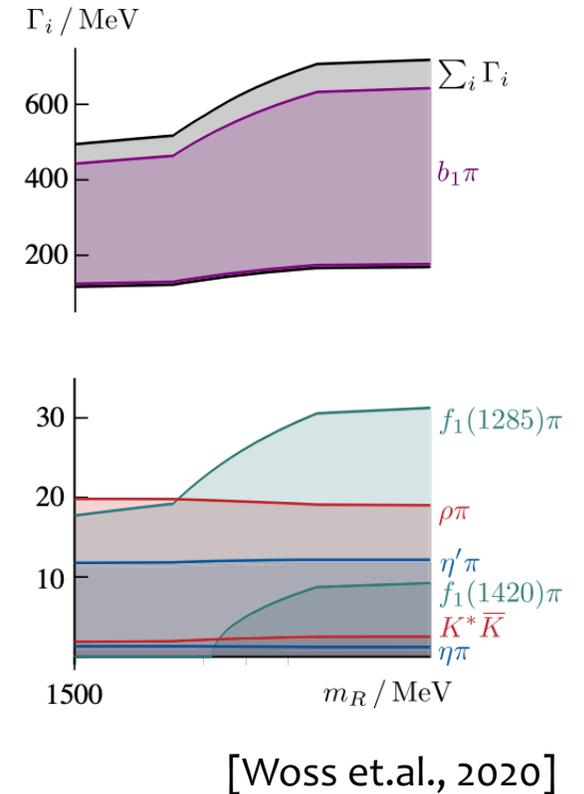
# Hybrids in the light meson spectrum



Lattice QCD calculations for light meson sector are the most advanced

- Hybrid multiplets in GEVP calculations

- properties of the lightest hybrid meson using scattering amplitudes



# Hybrid mesons from COMPASS

Exotic  $\pi_1(1600)$  with  $JPC = 1^{-+}$

- Established in  $\eta'\pi$
- Consistently described in  $\eta\pi$
- Found in  $\rho\pi$  [sophisticated  $3\pi$  PWA]
- is being discovered in  $b_1\pi$  [sophisticated  $2\pi\omega$  PWA]

