

Summary of precision Higgs calculations

Higgs 2024
Uppsala, Sweden
4 November 2024


Raoul Röntschi





Preamble

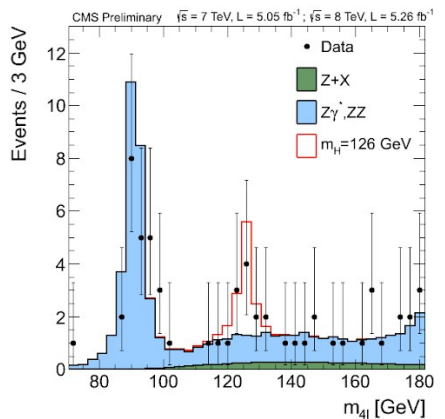
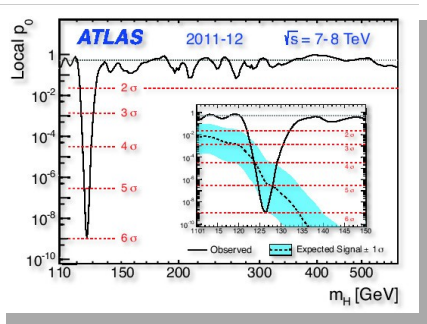
Summarizing ~ 12 months of hard work done by dozens of theorists in 20 minutes is an impossible task.

I have tried to highlight results that have appeared since ~ Higgs 2023 (and indicate these as ) and especially those that will be presented at this workshop.

My apologies if I've left something (or someone) out!

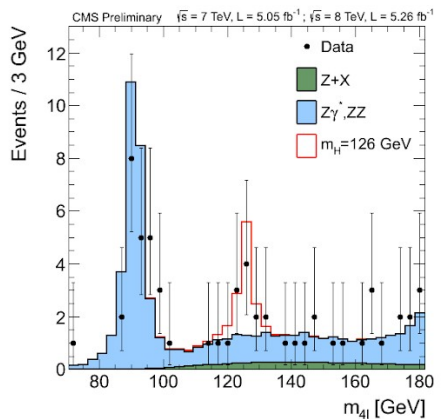
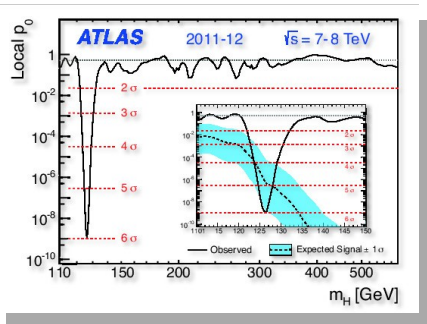
The Road to Precision Higgs Physics

The now-famous discovery in 2012...



The Road to Precision Higgs Physics

The now-famous discovery in 2012...



... was only the beginning!

The Higgs completes the SM, but that doesn't mean our work is complete!

The Road to Precision Higgs Physics

We have a new particle to explore:

- Source of EWSB
- First fundamental scalar (?)
- New coupling structure (Yukawa interactions)
- Deep connections to fate of the universe
- Bridge to New Physics?

We need to understand:

- Its **properties**
(mass, width, spin, CP properties, ...)
- Its **couplings** to other particles
- Its **self-couplings** (i.e. form of potential)
- ...

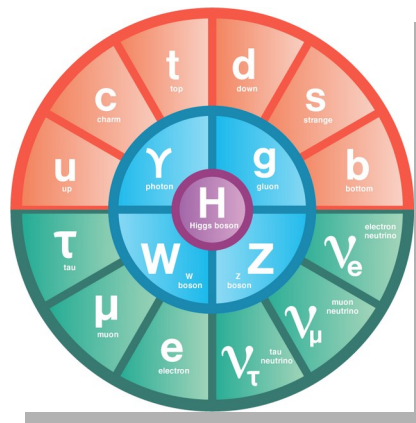
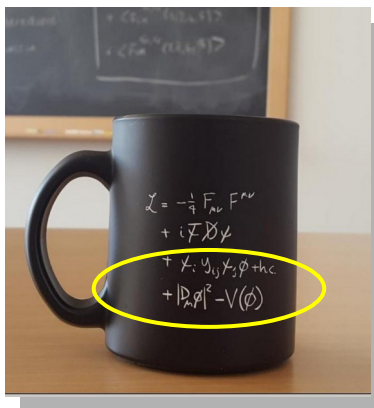
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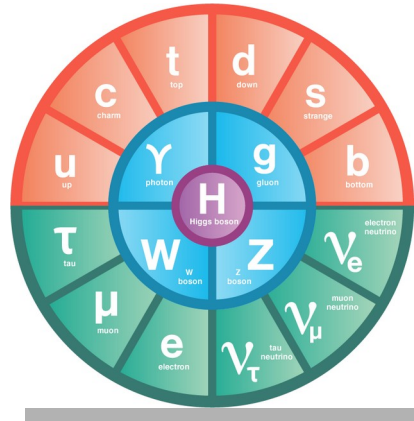
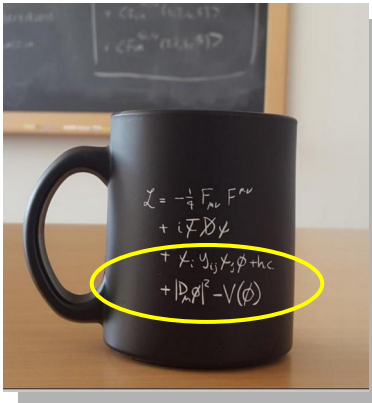
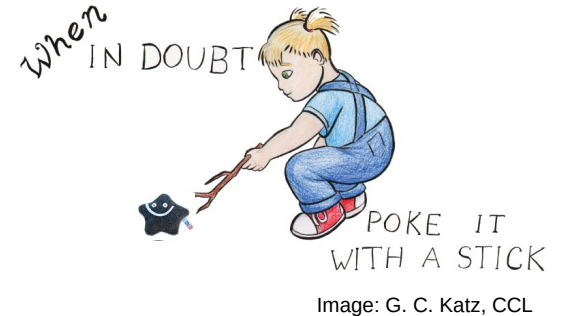
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The Road to Precision Higgs Physics

The LHC : a very powerful stick



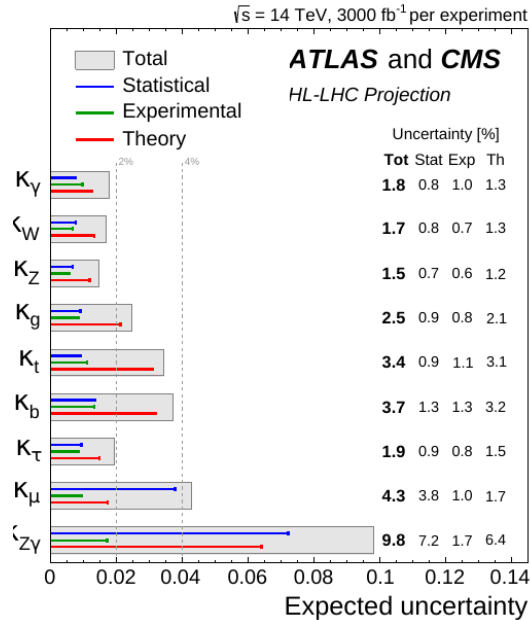
“Speak quietly and carry a big stick.”

- Theodore Roosevelt

The Road to Precision Higgs Physics

The LHC : a very powerful stick

... and a (surprisingly) sharp one!



Percent-level precision on Higgs couplings by the end of the HL-LHC

“Except for rare decays, the overall uncertainties will be dominated by the theoretical systematics, with a precision close to percent level.”

- Report on *Physics Potential of the HL-LHC*, submitted to CERN Council

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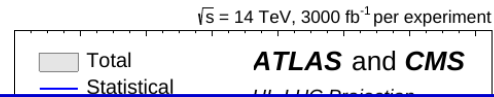
The Road to Precision Higgs Physics

The LHC : a very powerful stick

... and a (surprisingly) sharp one!



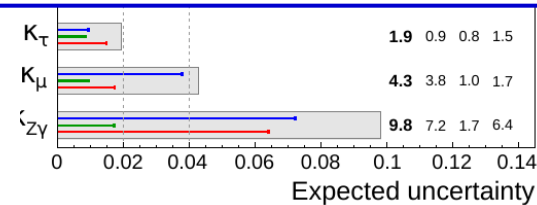
Precision measurements need to be confronted with precision predictions



Present-level precision Higgs couplings by end of the HL-LHC

For rare decays, the overall errors will be dominated by the systematic uncertainties, with a precision at the percent level.”

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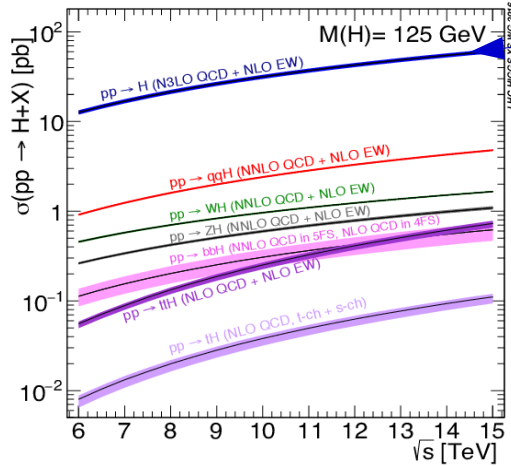
Outline

- Higgs production in gluon fusion
- Higgs + jet
- Electroweak Higgs production
- $t\bar{t}H$ production
- Di-Higgs Production

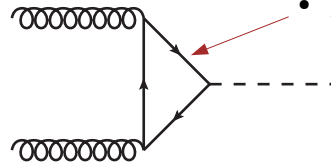


Gluon Fusion

Gluon fusion

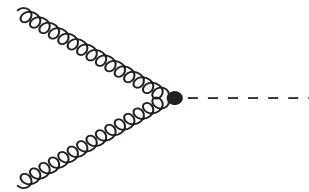
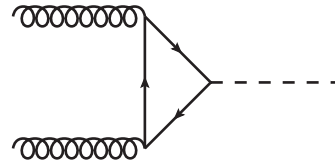


- Largest production cross section
(~ 87% of Higgs production at LHC come from GF)
- **Loop-induced** process



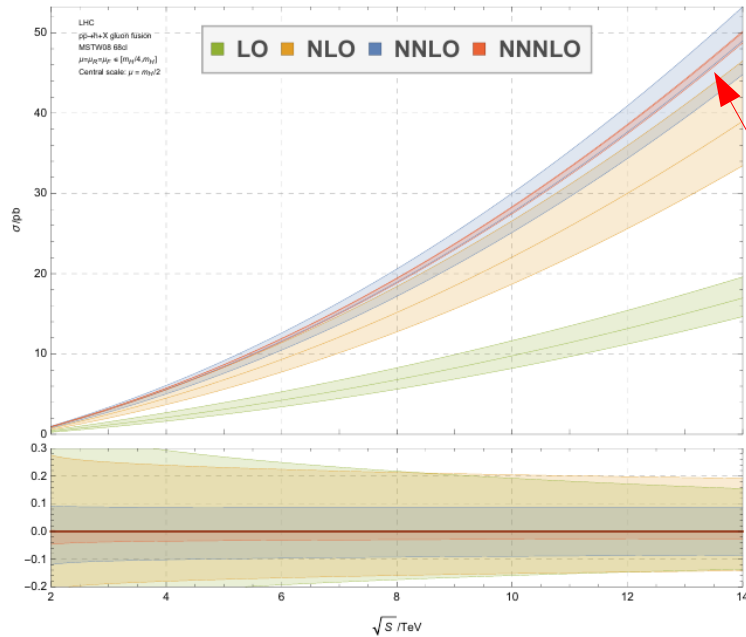
- Top quarks dominate in loop

- **Heavy Top Limit** $m_t \rightarrow \infty$



$$\sim HG_{\mu\nu,a}G^{\mu\nu,a}$$

Gluon fusion: Using the Heavy Top Limit



[Anastasiou et al, '15]

- Very large QCD corrections – **higher order calculations are essential.**

($K_{\text{NLO}} \sim 2$)

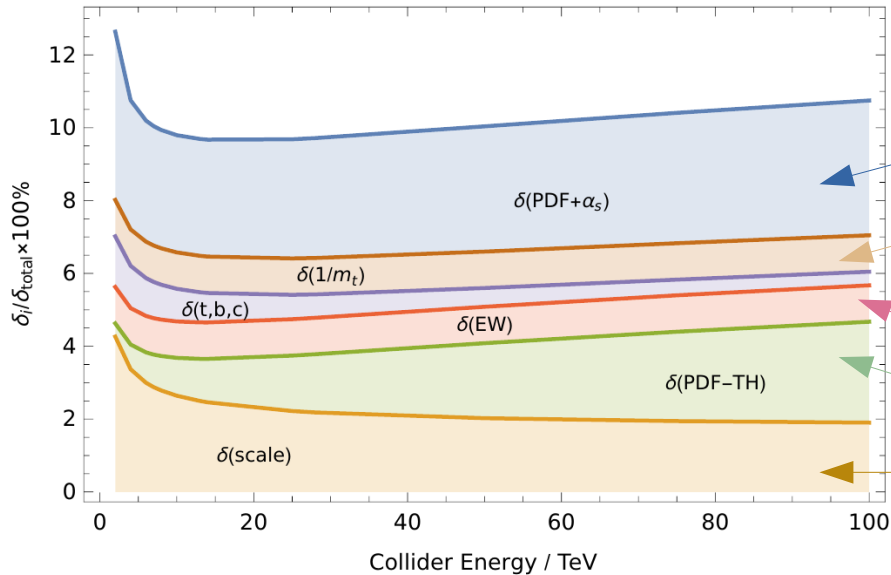
- **N3LO** result within scale uncertainty bands at **NNLO**:
➔ Perturbative expansion under control from NNLO.
- N3LO scale uncertainty \sim **few percent**

[NLO: Dawson '91; Graudenz, Spira, Zerwas '93; + Djouadi '95]

[NNLO: Anastasiou, Melnikov '02; Harlander, Kilgore '02; Ravindran, Smith, v. Neerven '03]

[N3LO: Anastasiou et al '15, '16; Mistlberger '18]

Gluon Fusion: Sources of Uncertainties



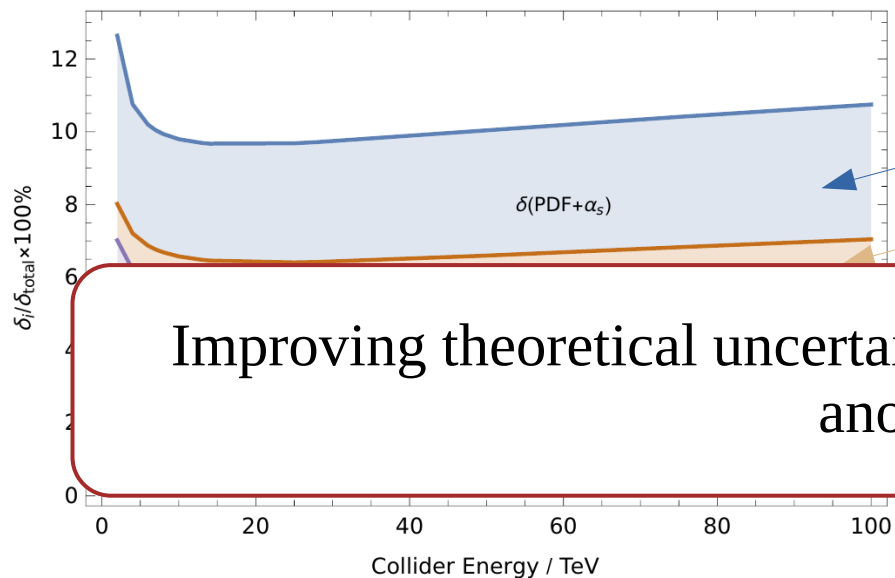
Sources of theoretical uncertainty:

- α_s determination
- Top mass effects
- Other quark mass effects
- EW corrections
- Pdf determination
- Missing higher-order QCD corrections

[Mistlberger, Dulat, Lazopoulos '18]

All roughly the same size

Gluon Fusion: Sources of Uncertainties



Sources of theoretical uncertainty:

- α_s determination
- Top mass effects

Improving theoretical uncertainty is no longer just a case of “add another N”

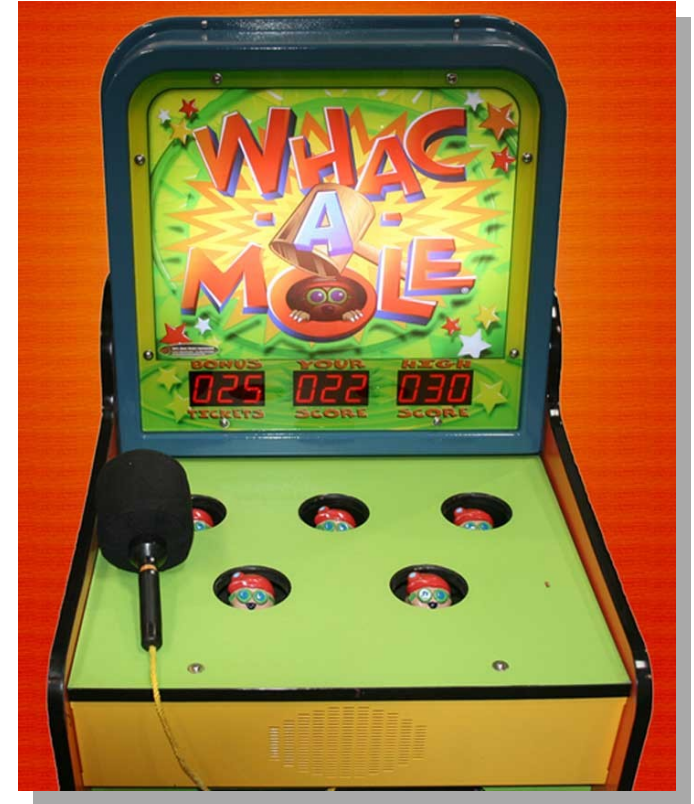
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[Mistlberger, Dulat, Lazopoulos '18]

Glueon fusion



Glueon fusion



With a small apology to Peter Skands for re-appropriating his metaphor.

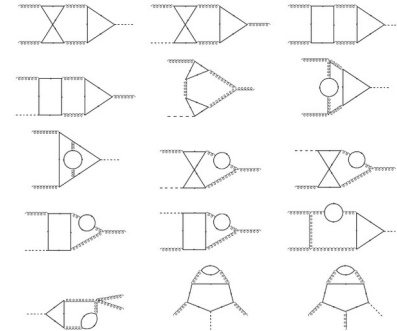
Beyond the Heavy Top Limit

- **Heavy Effective Field Theory:** QCD corrections are (approximately) independent of value of top mass
→ Include top mass effects by **rescaling** HTL results according to exact LO cross section.

$$d\sigma_{\text{HEFT}}^{(N^n LO)} = \frac{d\sigma_{\text{exact}}}{d\sigma_{\text{HTL}}} d\sigma_{\text{HTL}}^{(N^n LO)}$$

- Exact (finite top mass) results known to NNLO
- Requires 3-loop **H + 2 parton** and 2-loop **H + 3 parton** amplitudes.
- Reduce cross section by **-0.32%** relative to HEFT (at 13 TeV)

[Czakon, Niggetiedt '20;
Czakon, Harlander, Klappert, Niggetiedt '21]

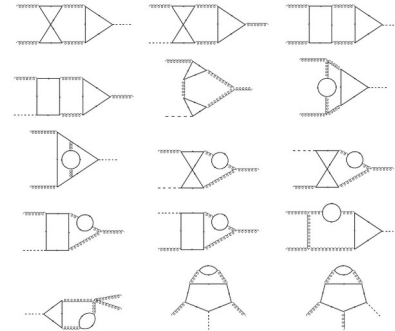


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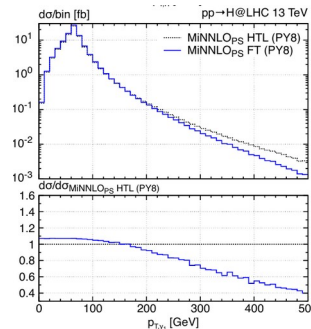
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 Matched to PS with MiNNLO_{PS}

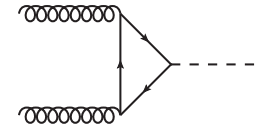
[Niggetiedt, Wiesemann '24]

Gluon Fusion: It's not all about tops

- Other quarks in the loop suppressed by m_q^2/m_H^2 but enhanced by $\log^2(m_q^2/m_H^2)$
- Biggest contribution is interference with top quark loops.

 Computed to NNLO QCD

[Czakon, Eschment, Niggetiedt, Poncelet, Schellenberger '23]



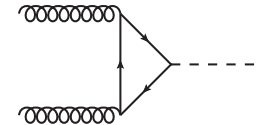
Order	σ_{HEFT} [pb]	$(\sigma_t - \sigma_{\text{HEFT}})$ [pb]	$\sigma_{t \times b}$ [pb]	$\sigma_{t \times b}(Y_{b, \overline{\text{MS}}})$ [pb]	$\sigma_{t \times b}/\sigma_{\text{HEFT}}$ [%]
$\sqrt{s} = 13.6 \text{ TeV}$					
$\mathcal{O}(\alpha_s^2)$	+17.47	–	–2.117	–1.311	
LO	$17.47^{+4.67}_{-3.32}$	–	$-2.12^{+0.40}_{-0.57}$	$-1.31^{+0.31}_{-0.47}$	–12
$\mathcal{O}(\alpha_s^3)$	+22.76	–0.338	–0.464(1)	–0.659(1)	
NLO	$40.23^{+9.07}_{-6.77}$	$-0.338^{+0.11}_{-0.18}$	$-2.58^{+0.20}_{-0.12}$	$-1.97^{+0.28}_{-0.28}$	$-6.4^{+0.9}_{-0.8}$
$\mathcal{O}(\alpha_s^4)$	+10.47	+0.162(1)	+0.464(9)	+0.022(6)	
NNLO	$50.70^{+4.53}_{-5.14}$	$-0.176(1)^{+0.14}_{-0.03}$	$-2.12(1)^{+0.33}_{-0.16}$	$-1.95(1)^{+0.09}_{-0.03}$	$-4.2^{+0.9}_{-0.8}$

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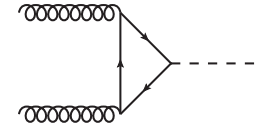
- Interference effect $\sim -12\%$
- QCD corrections $\sim 2\%$
- NLO and NNLO have opposite sign

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Computed to NNLO QCD

[Czakon, Eschment, Niggetiedt, Poncelet, Schellenberger '23]

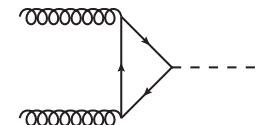


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- $\overline{\text{MS}}$ renormalization of Yukawa coupling gives **smaller** contribution...
- And **better behaved** perturbative expansion.

Gluon Fusion: It's not all about tops

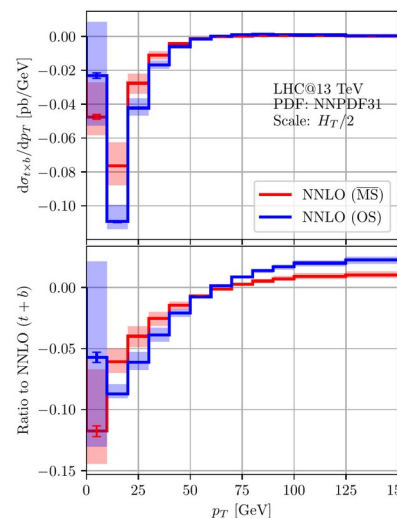
- Additional inconsistency: bottom quarks treated as **massive** inside loop, **massless** inside proton (5FS). **Better to use 4FS?**
- Impact of $\overline{\text{MS}}$ versus onshell renormalization for bottom mass? For top mass? Compared to impact of 5FS versus 4FS? Compared to impact of finite top masses?



🌟 Comprehensive study at NNLO QCD

[Czakon, Eschment, Niggetiedt, Poncelet, Schellenberger '23]

Order	$\sigma_{t \times b}$ [pb]			
	$\sqrt{s} = 13 \text{ TeV}$			
	5FS	5FS	5FS	4FS
	$m_t = 173.06 \text{ GeV}$ $\overline{m}_b(\overline{m}_b) = 4.18 \text{ GeV}$	$m_t = 173.06 \text{ GeV}$ $m_b = 4.78 \text{ GeV}$	$m_t(m_t) = 162.7 \text{ GeV}$ $\overline{m}_b(\overline{m}_b) = 4.18 \text{ GeV}$	$m_t = 173.06 \text{ GeV}$ $\overline{m}_b(\overline{m}_b) = 4.18 \text{ GeV}$
$\mathcal{O}(\alpha_s^2)$	-1.11	-1.98	-1.12	-1.15
LO	$-1.11^{+0.28}_{-0.43}$	$-1.98^{+0.38}_{-0.53}$	$-1.12^{+0.28}_{-0.42}$	$-1.15^{+0.29}_{-0.45}$
$\mathcal{O}(\alpha_s^3)$	-0.65	-0.44	-0.64	-0.66
NLO	$-1.76^{+0.27}_{-0.28}$	$-2.42^{+0.19}_{-0.12}$	$-1.76^{+0.27}_{-0.28}$	$-1.81^{+0.28}_{-0.30}$
$\mathcal{O}(\alpha_s^4)$	+0.02	+0.43	-0.02	-0.02
NNLO	$-1.74(2)^{+0.13}_{-0.03}$	$-1.99(2)^{+0.29}_{-0.15}$	$-1.78(1)^{+0.15}_{-0.03}$	$-1.83(2)^{+0.14}_{-0.03}$



→ Talk by Tom Schellenberger

Gluon Fusion: Offshell Production

Offshell production $p_H^2 \gg m_H^2$ allows us to probe **unitarizing behavior** of Higgs and constrain Higgs **width**

Need to account for **signal**, **background** and their **interference**.



Two-loop amplitudes for $gg \rightarrow ZZ$ known [Agarwal, Jones, v. Manteuffel '20; Brønnum-Hansen, Chen '20, '21]

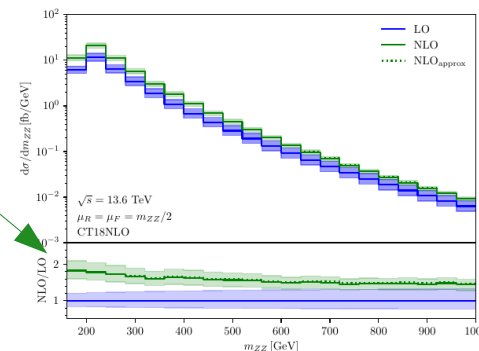
☀ NLO QCD corrections to $gg \rightarrow ZZ$

[Agarwal, Jones, Kerner, v. Manteuffel '24]

➡ **Reweighting of massless amplitudes** seems to work very well

☀ Soft-virtual NLO QCD corrections to interference in $gg \rightarrow Z\gamma$

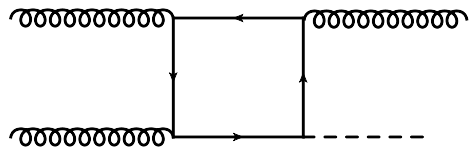
[Buccioni et al, '23]





Higgs + Jet

Higgs + Jet



Can probe what happens **inside** loop

- **Light quark** Yukawa couplings
- NP effects
- ...

[Bishara, Haisch, Monni, Re '16 ;
Soreq, Zhu, Zupan '16 ; ...]

- **NNLO** in HTL

➤ HTL not valid for $p_{T,H} \gtrsim m_t$

[Chen, Gehrmann, Glover, Jaquier, '14; + Cruz-Martinez '16;
Boughezal, Caola, Melnikov, Petriello, Schulze '15; Boughezal, Focke, Giele, Liu, Petriello '15;
Caola, Melnikov, Schulze '15; Campbell, Ellis, Seth '19]

- **Top-bottom** interference at NLO

[Lindert, Melnikov, Tancredi, Wever '17]

- NLO including **top mass effects**

[Jones, Kerner, Luisoni '18; Kudashkin, Lindert, Melnikov, Wever '18; Neumann '18]

- **Top** and **bottom mass effects**

[Bonciani et al, '22]

Higgs + Jet: Resummations

Jet vetos introduce **large logarithms** $\sim \log(p_T^{\text{veto}}/m_H)$ which spoil perturbative convergence and must be **resummed**

☀️ Jet veto resummation at (approximate)NNLL'+NLO computed for STXS bins

[Cal, Lim, Scott, Tackmann, Waalewijn '24]

Semi-hard regime (large rapidity gap) induces $\sim \log(s/Q^2)$

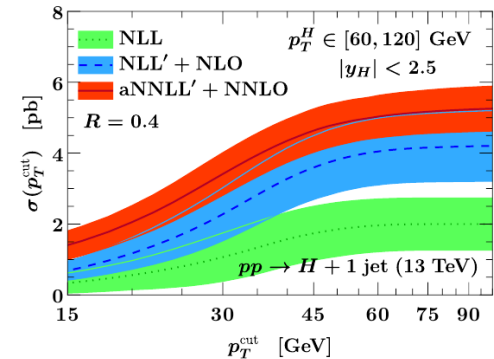
➤ Resummed using BFKL

☀️ Resummation to NLL/NLO+ in hybrid factorization approach

[Celiberto, Papa, '20; Celiberto, Delle Rose, Fucilla, Gatto, Papa '24]

$$\underbrace{d\sigma^{\text{NLL}/\text{NLO}^-}}_{\text{NLL}/\text{NLO}^- \text{ POWHEG+JETHAD}}(\Delta Y, \varphi, s) = \underbrace{d\sigma^{\text{NLO}}}_{\text{NLO POWHEG w/o PS}}(\Delta Y, \varphi, s) + \underbrace{d\sigma^{\text{NLL}^-}}_{\text{NLL}^- \text{ resum (HyF)}}(\Delta Y, \varphi, s) - \underbrace{\Delta d\sigma^{\text{NLL}/\text{NLO}^-}}_{\text{NLL}^- \text{ expanded at NLO}}(\Delta Y, \varphi, s).$$

NLL⁻ JETHAD w/o NLO⁻ double counting



→ Talk by Francesco
Celiberto

H+J: New Physics + QCD effects

Full NLO QCD corrections combined with NP parametrized in HEFT Lagrangian

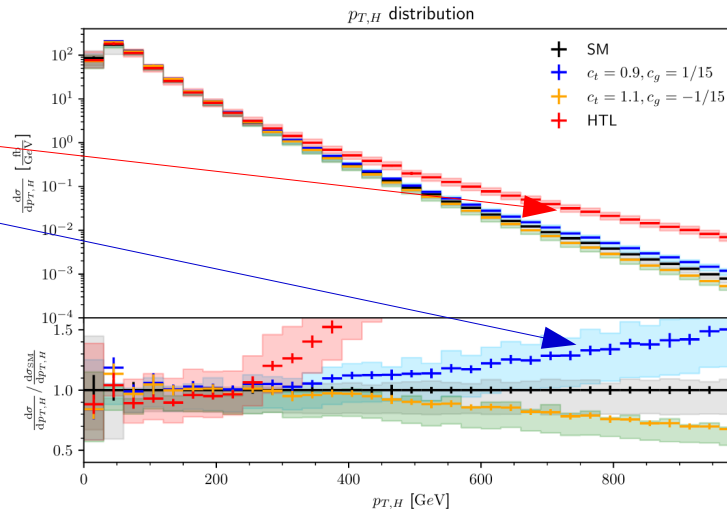
[Aveleira, Heinrich, Kerner, Kunz '24]

$$\mathcal{L} \supset -c_t m_t \frac{H}{v} \bar{t}t + \frac{\alpha_s}{8\pi} c_g \frac{H}{v} G_{\mu\nu}^a G^{a,\mu\nu} .$$

NP integrated out → effective vertex

Rescale top Yukawa

- HTL overshoots in tail
- NP effects can also enhance tail
- Delicate interplay between NP effects and higher-order corrections

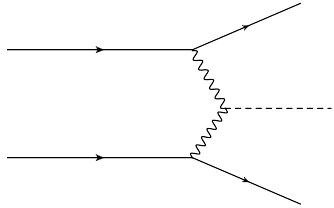


→ Talk by
Benjamin Aveleira



Vector Boson Fusion

Vector boson fusion



- Direct coupling to EW bosons
- Distinctive signature:
 - forward jets in opposite hemispheres
 - little hadronic activity at central rapidities

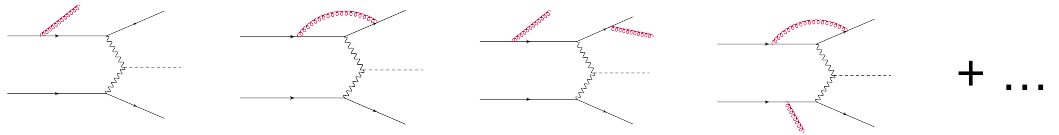
VBF cuts:

$$m_{j_1 j_2} > 600 \text{ GeV}, \Delta y_{j_1 j_2} > 4.5, y_{j_1} y_{j_2} < 0$$

[Cacciari, Dreyer, Karlberg, Salam, Zanderighi '15]

“Double-DIS approximation” for QCD corrections:

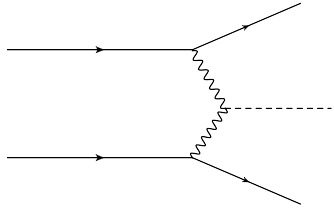
- Radiation connecting quark lines is zero at NLO, color-suppressed at NNLO.
- Fully differential at NNLO QCD (VBF cuts):
 - NNLO corrections at 1%-5% level
 - Residual scale uncertainties ~ 1%
- Inclusive cross section known to N3LO QCD
 - Corrections ~ 2%, within NNLO scale uncertainty bounds
 - Residual scale uncertainties ~ 1%-2%



[Cacciari, Dreyer, Karlberg, Salam, Zanderighi '15;
Cruz-Martinez, Gehrmann, Glover, Huss '18; Asteriadis, Caola, Melnikov, RR '21]

[Dreyer, Karlberg '16]

Vector boson fusion



- Direct coupling to EW bosons
- Distinctive signature:
 - **forward** jets in **opposite hemispheres**
 - **little hadronic activity** at central rapidities



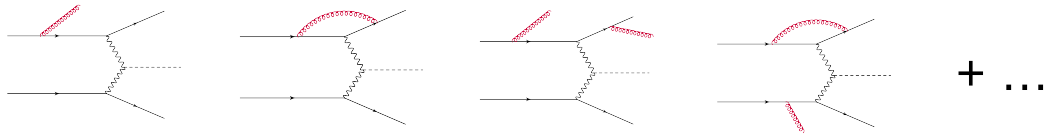
VBF cuts:

$$m_{j_1 j_2} > 600 \text{ GeV}, \Delta y_{j_1 j_2} > 4.5, y_{j_1} y_{j_2} < 0$$

[Cacciari, Dreyer, Karlberg, Salam, Zanderighi '15]

“**Double-DIS approximation**” for QCD corrections:

- Radiation connecting quark lines is **zero** at NLO, **color-suppressed** at NNLO.



- Fully differential at NNLO OGD (VBF cuts):

- NNLO corrections at **1%-5%**
- Residual scale uncertainties

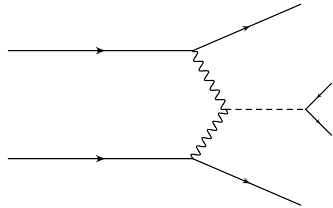
- Inclusive cross section known

- Corrections \sim **2%**, **within NNLO**
- Residual scale uncertainties \sim **1%-2%**

Perturbative QCD corrections
appear to be well-controlled

[Cacciari, Dreyer, Karlberg, Salam, Zanderighi '15;
Cacciari, Dreyer, Huss '18; Asteriadis, Caola, Melnikov, RR '21]

Vector boson fusion + Higgs decay

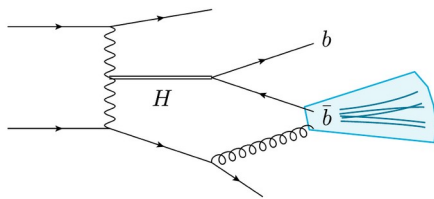


VBF + $H \rightarrow b\bar{b}$ decay:

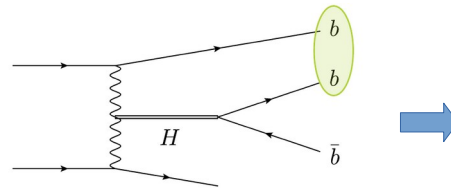
- B-tagged jets in **central region** – can access **bottom quark Yukawa**.
- Higgs is a narrow-width scalar \rightarrow production and decay factorize and can be treated **separately**:

VBF at NNLO, $H \rightarrow b\bar{b}$ at LO.

[Asteriadis, Caola, Melnikov, RR '21]



Jet-clustering breaks factorization



B-tagging breaks factorization



$$\begin{array}{ccc}
 \frac{\sigma_{\text{NLO}}^H}{\sigma_{\text{LO}}^H} = 0.917(1) & \xrightarrow{-3.2\%} & \frac{\sigma_{\text{NNLO}}^H}{\sigma_{\text{LO}}^H} = 0.885(1) \\
 \downarrow +1.7\% & & \downarrow +2.9\% \\
 \frac{\sigma_{\text{NLO}}^{b\bar{b}}}{\sigma_{\text{LO}}^{b\bar{b}}} = 0.934(1) & & \frac{\sigma_{\text{NNLO}}^{b\bar{b}}}{\sigma_{\text{LO}}^{b\bar{b}}} = 0.914(2)
 \end{array}$$

[From talk by K. Asteriadis at “Past, present, and future of VBF” workshop, 20/10/2022]

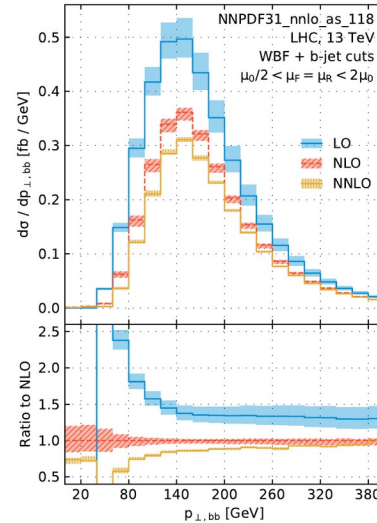
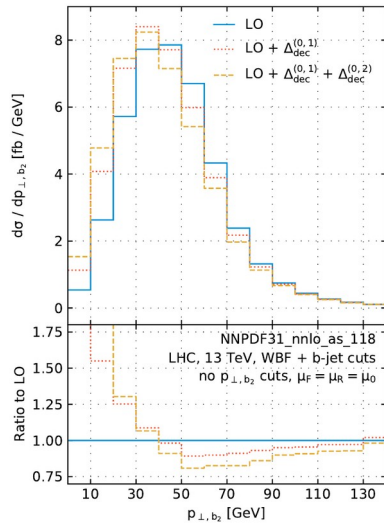
Impact of including decay **comparable to NNLO** corrections

Vector boson fusion + Higgs decay

☀ NNLO in production and decay:

- Large impact: corrections in decay reduce fiducial cross section by 7% at NLO and 7% at NNLO (poor perturbative convergence)
- Interplay of cuts on b-tagged jets and corrections to decay

[Asteriadis, Behring, Melnikov, Novikov, RR '24]



→ Talk by
Ivan Novikov

Vector boson fusion: non-factorizable effects

Two-loop non-factorizable corrections computed in eikonal expansion ($p_{T,j}/\sqrt{s}$)

- Color-suppressed but enhanced by Glauber phase → 0.5%-1% corrections

[Liu, Melnikov, Penin '19; Dreyer, Karlberg, Tancredi '20]

- Other non-factorizable contributions at NNLO (real-real and real-virtual) negligible
- Sub-leading eikonal effects $\sim 20\%$ of leading eikonal contribution
- $\mathcal{O}(\beta_0\alpha_s^3)$ corrections $\sim 20\%$ of leading eikonal and reduce scale uncertainty on eikonal to $\sim 5\%$



[Asteriadis, Brønnum-Hansen, Melnikov '23]

[Long, Melnikov, Quarroz '23]

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[Long, Melnikov, Quarroz '23]

[Brønnum-Hansen, Long, Melnikov '23]

Non-factorizable effects under control

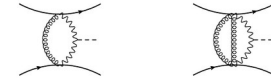
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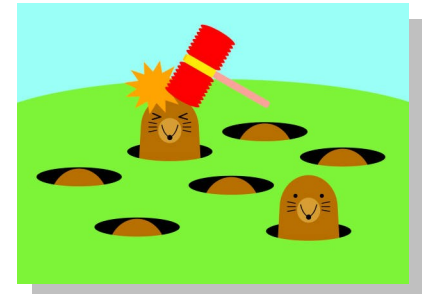


[Asteriadis, Brønnum-Hansen, Melnikov '23]

[Long, Melnikov, Quarroz '23]

[Brønnum-Hansen, Long, Melnikov '23]

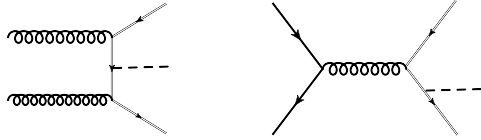
Non-factorizable effects under control





$t\bar{t}H$ production

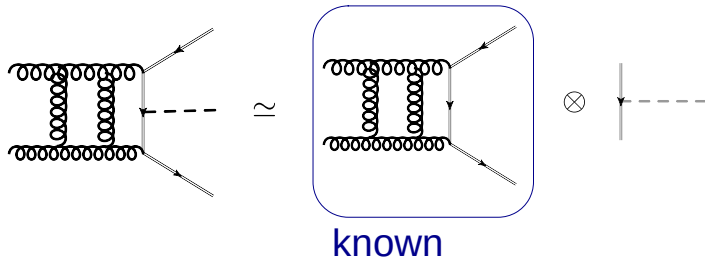
$t\bar{t}H$ production



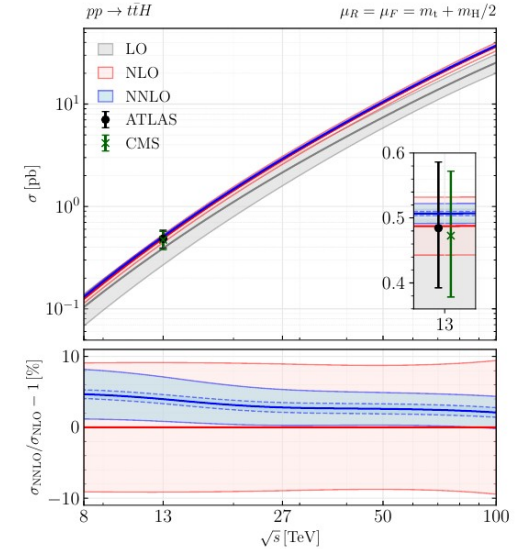
Direct access to **top Yukawa**

- NNLO two-loop amplitudes are extremely challenging (2 → 3 process with 7 scales)
- Soft-Higgs approximation

[Catani et al , '22]



- Rescale LO amplitude



- (Approximate) NNLO QCD corrections $\sim 4\%$
- Residual scale uncertainty $\sim 3\%$,
- Approximation uncertainty $\sim 0.5\%$

$t\bar{t}H$ production: Towards two-loop amplitudes

Amplitudes computed in boosted limit (top and Higgs approximately massless)

[Wang, Xia, Yang, Ye '24]

Recent progress towards full two-loop amplitude:

Master integrals for leading color amplitudes

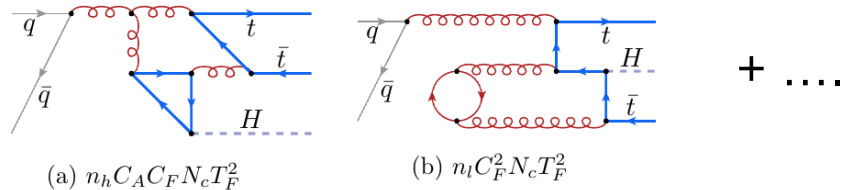
[Febres Cordero et al '23]

One-loop $gg \rightarrow t\bar{t}H$ amplitude at $\mathcal{O}(\epsilon^2)$

[Buccioni, Kreer, Liu, Tancredi '23]

Nf-dependent contributions computed numerically

[Agarwal et al '24]

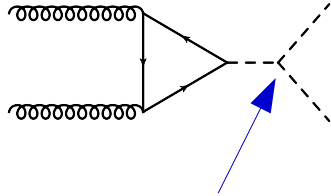
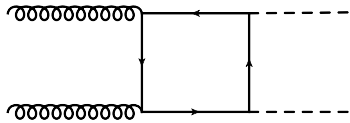


→ Talk by Anton Olsson



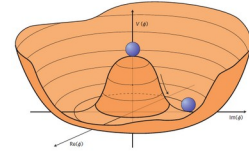
Di-Higgs Production

Di-Higgs Production



$$V(\phi) = -\mu^2 \phi^2 + \lambda \phi^4$$

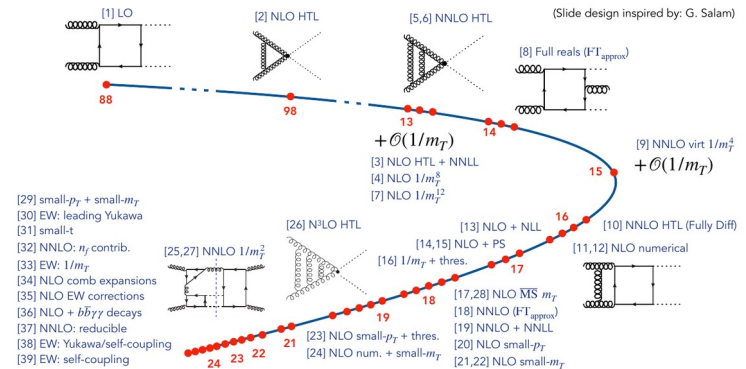
$$\lambda_{HHH} = 6\lambda v = 3 \frac{m_H^2}{v}$$



- Direct access to Higgs self-coupling → Higgs potential
- NLO QCD corrections increase cross section by ~ 60%-70%
- Residual scale uncertainty ~ 10%-15%
- Top mass definition uncertainty as high as 20%
- NNLO QCD results unavailable, but numerous approximations + matching to resummation/PS

[Borowka et al, '16, '16; Baglio et al '18; '20]

Including $HH \rightarrow b\bar{b}\gamma\gamma$ at NLO [Li, Si, Wang, Zhang, Zhao '24]



[1] Glover, van der Bij 88; [2] Dawson, Dittmaier, Spira 98; [3] Shao, Li, Wang 13; [4] Grigo, Hoff, Melnikov, Steinhäuser 13; [5] de Florian, Mazzitelli 13; [6] Grigo, Melnikov, Steinhäuser 14; [7] Grigo, Hoff 14; [8] Maltoni, Vayonidou, Zaro 14; [9] Grigo, Hoff, Steinhäuser 15; [10] de Florian, Grazzini, Hanga, Kallweit, Lindert, Maierhöfer, Mazzitelli, Rathlev 16; [11] Borowka, Greiner, Heinrich, SPJ, Kerner, Schlenk, Schubert, Zanke 16; [12] Borowka, Greiner, Heinrich, SPJ, Kerner, Schlenk, Zanke 16; [13] Ferrera, Pires 16; [14] Heinrich, SPJ, Kerner, Luisoni, Vayonidou 17; [15] SPJ, Kuttimali 17; [16] Gröber, Maier, Rauh 17; [17] Baglio, Campanario, Glaus, Mühlleitner, Spira, Stöcher 18; [18] Grazzini, Heinrich, SPJ, Kallweit, Kerner, Lindert, Mazzitelli 18; [19] de Florian, Mazzitelli 18; [20] Bonciani, Degrandi, Giardino, Gröber 18; [21] Davies, Mishima, Steinhäuser, Wellmann 18; [22] Mishima 18; [23] Gröber, Maier, Rauh 19; [24] Davies, Heinrich, SPJ, Kerner, Mishima, Steinhäuser, David Wellmann 19; [25] Davies, Steinhäuser 19; [26] Chen, Li, Shao, Wang 19; [27] Davies, Herren, Mishima, Steinhäuser 19; [28] Baglio, Campanario, Glaus, Mühlleitner, Ronca, Spira 21; [29] Bellafante, Degrandi, Giardino, Gröber, Vitti 22; [30] Davies, Mishima, Schönwald, Steinhäuser, Zhang 22; [31] Davies, Mishima, Schönwald, Steinhäuser 23; [32] Davies, Schönwald, Steinhäuser 23; [33] Davies, Schönwald, Steinhäuser, Zhang 23; [34] Bagdasarian, Degrandi, Gröber 23; [35] Bi, Huang, Huang, Ma Yu 23; [36] Li, Si, Wang, Zhang, Zhao 24; [37] Davies, Schönwald, Steinhäuser, Viti 24; [38] Heinrich, SPJ, Kerner, Stone, Vestner 19; Li, Si, Wang, Zhang, Zhao 24

[Slide from S. Jones, Higgs Hunting 2024]

Di-Higgs Production: EW corrections

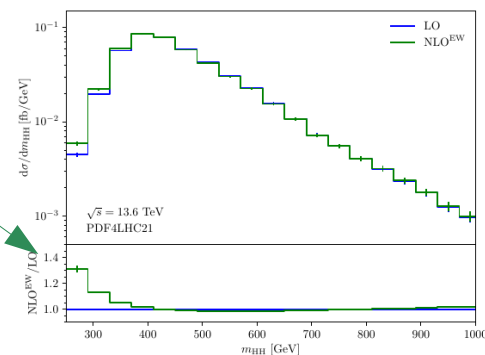
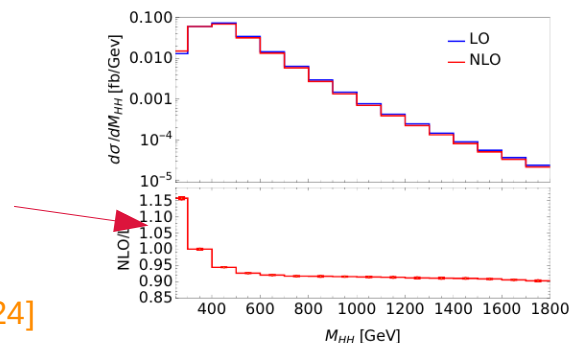
🌟 NLO EW corrections computed [Bi, Huang, Huang, Ma, Yu '23]

- Decrease cross section by $\sim 5\%$
- **Stronger shape change** in invariant mass and transverse momentum distributions

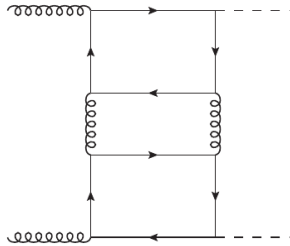
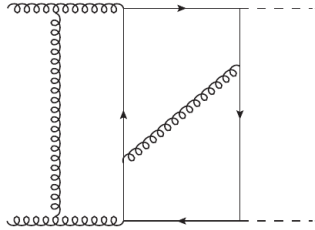
🌟 Partial NLO EW corrections [Heinrich, Jones, Kerner, Stone, Vestner '24]

- Corrections involving top Yukawa and Higgs self-interaction
- **Larger impact** on shapes of distributions compared to full EW corrections

→ See talk by Augustin Vestner

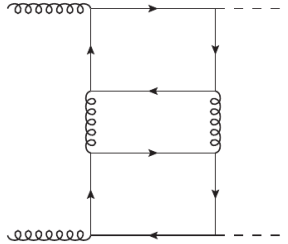
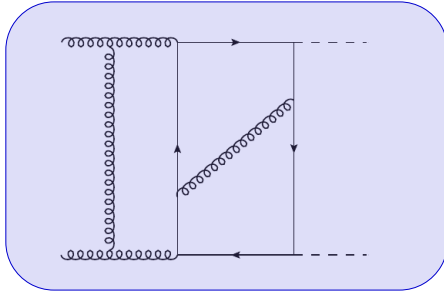


Di-Higgs: Towards full NNLO QCD



Higgs may couple to **same** quark loop or **different loops**

Di-Higgs: Towards full NNLO QCD

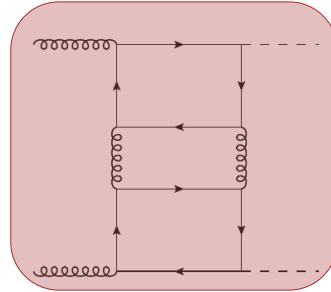
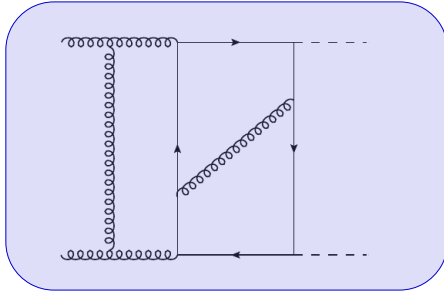


Known for $t = 0, m_H = 0$

[Davies, Schönwald, Steinhauser '23]

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Di-Higgs: Towards full NNLO QCD



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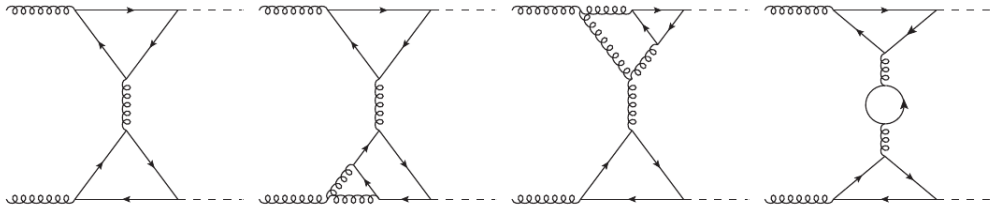
[Davies, Schönwald, Steinhauser '23]

Higgs may couple to **same** quark loop or **different** loops



Reducible contributions computed

[Davies, Schönwald, Steinhauser, Vitti '24]



→ Talk by Marco Vitti

Smörgåsbord

Many other interesting and important topics:

- Progress towards **N4LO** gluon fusion
- Impact of **aN3LO** pdfs on gluon fusion
- Progress towards **N3LO** in $H+j$ (HTL)
- Mixing between VH with hadronic Higgs decay and **VBF** at **NLO QCD+EW**
- Progress towards $t\bar{t}H$ fully differential at **NNLO**
- **Parton shower** uncertainties in **VBF**
- Interference effects in **diphoton** production and Higgs width
- Higgs **decays**
- ...



Conclusions

Precision theoretical predictions are one of the pillars on which the success of the Higgs programme has been built.



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Good luck!



THANK YOU FOR YOUR ATTENTION

QUESTIONS?