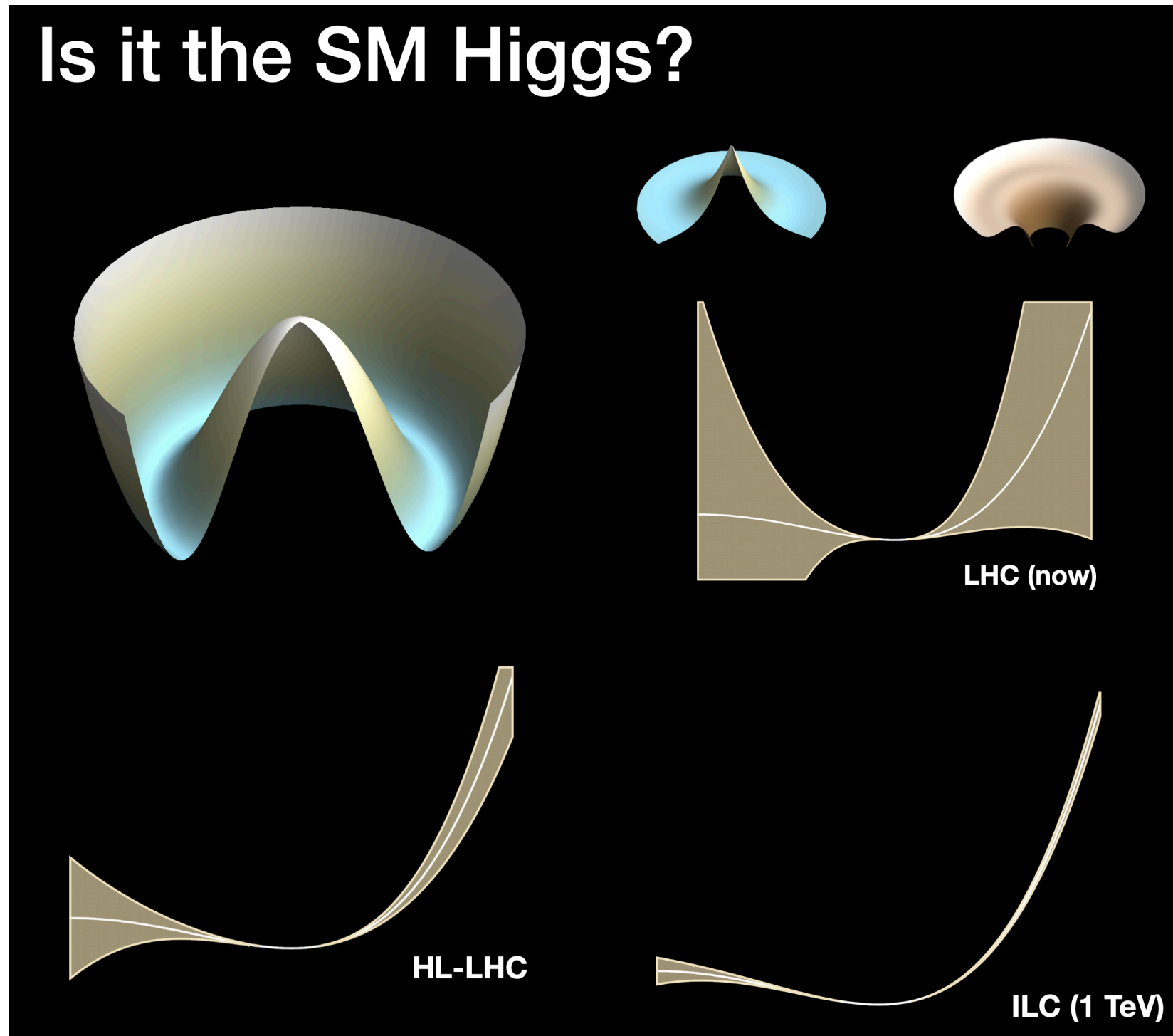


Higgs self-coupling @ Linear Collider



[courtesy: N. Craig @ LCWS 2023]

Higgs self-coupling @ Linear Collider



Junping Tian (U. Tokyo)

Higgs 2024 @ Uppsala U.
Nov. 4-8, 2024

Collaborators:

Bryan Bliewert, Jenny List,
Julie Torndal (DESY)

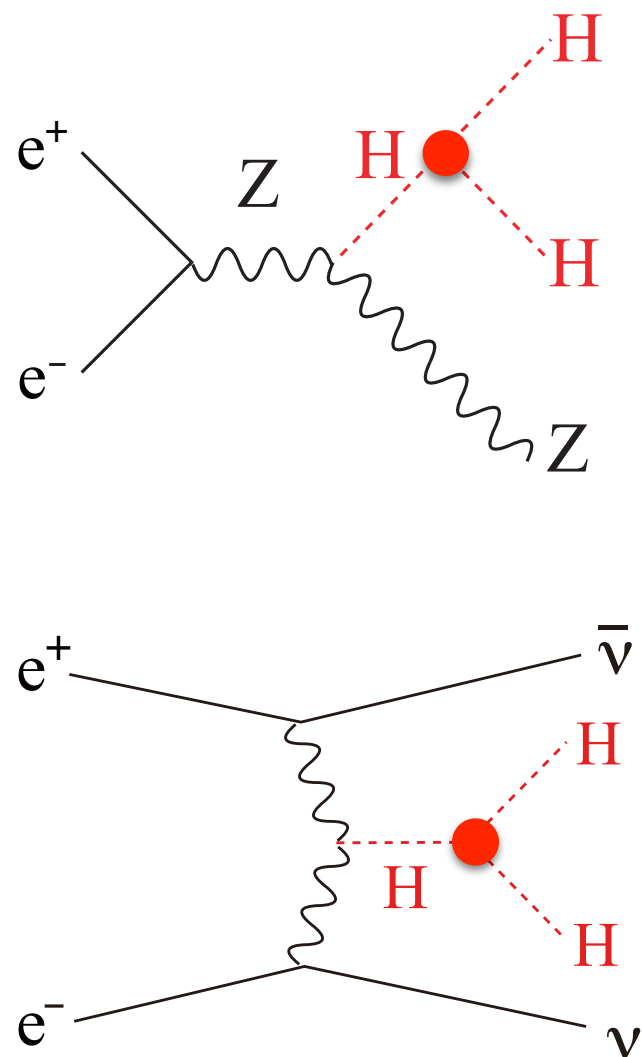
Dimitris Ntounis, Caterina
Vernieri (SLAC)

[arXiv:2410.15323](https://arxiv.org/abs/2410.15323)
[arXiv:2411.01507](https://arxiv.org/abs/2411.01507)
[arXiv:2307.16515](https://arxiv.org/abs/2307.16515)

[courtesy: [N. Craig @ LCWS 2023](#)]

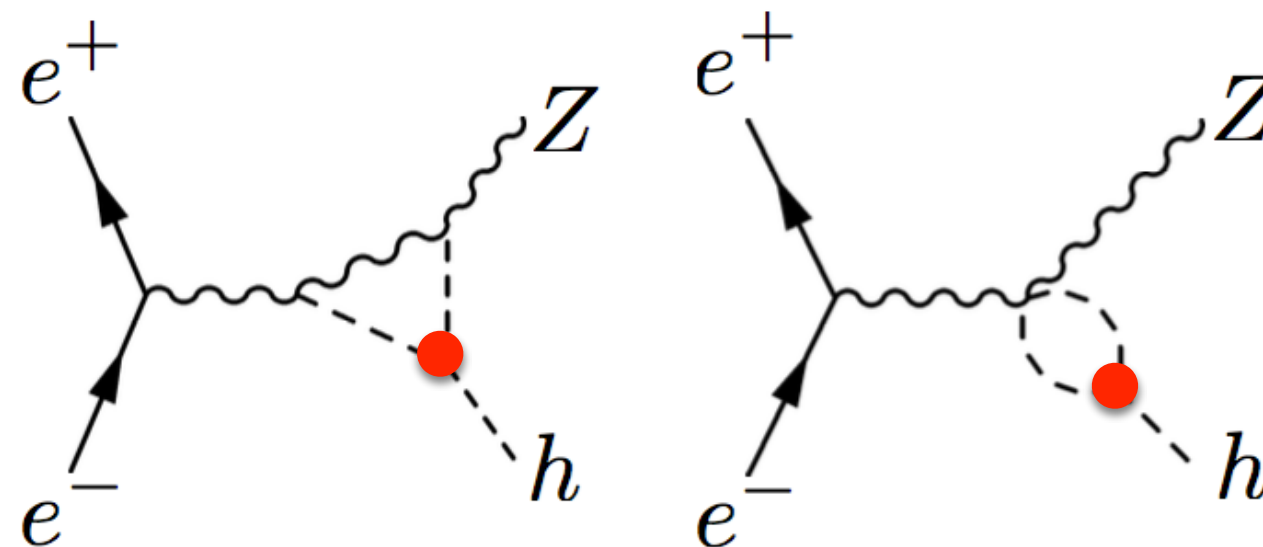
λ_{HHH} : di-Higgs & single-Higgs processes

$\sqrt{s} \gtrsim 500 \text{ GeV}$



$\sigma_{HH} \sim O(0.1) \text{ fb}$

$\sqrt{s} \gtrsim 240\text{--}250 \text{ GeV}$

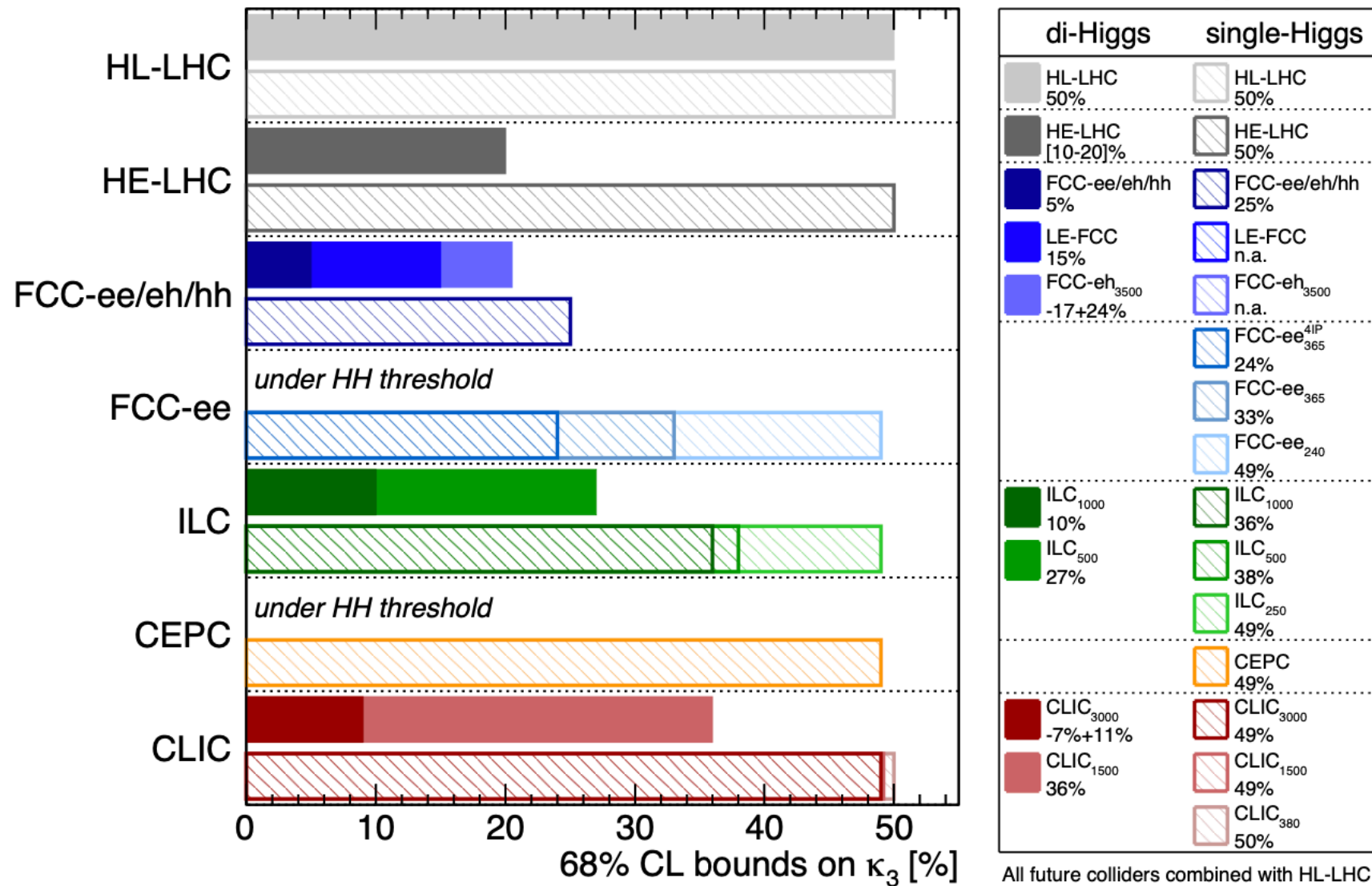


$\delta\sigma_{ZH} \sim O(1\%)$

Goal: update the projections in ESU 2020

[Physics Briefing Book, arXiv:1910.11775]

Higgs@FC WG September 2019

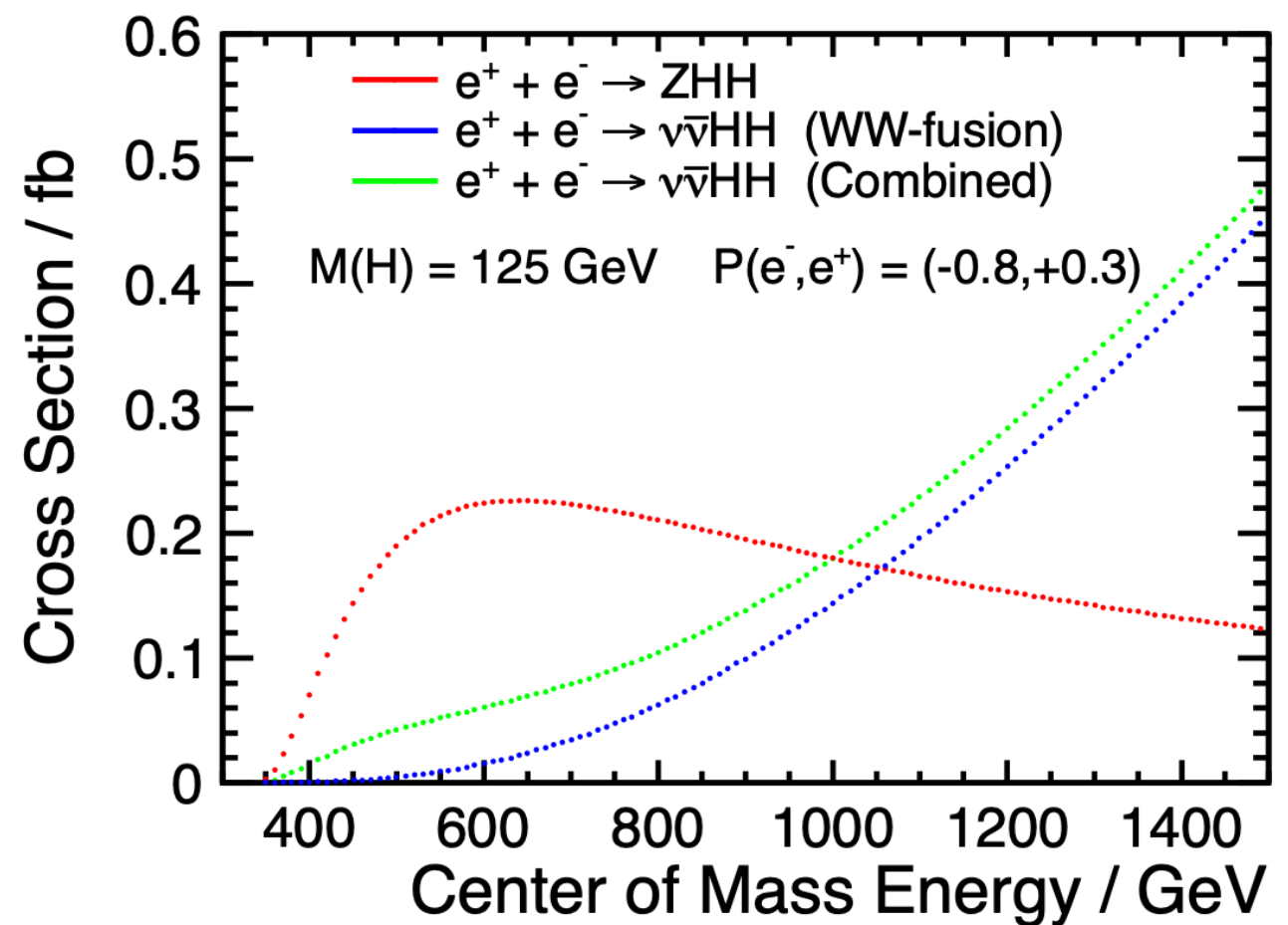
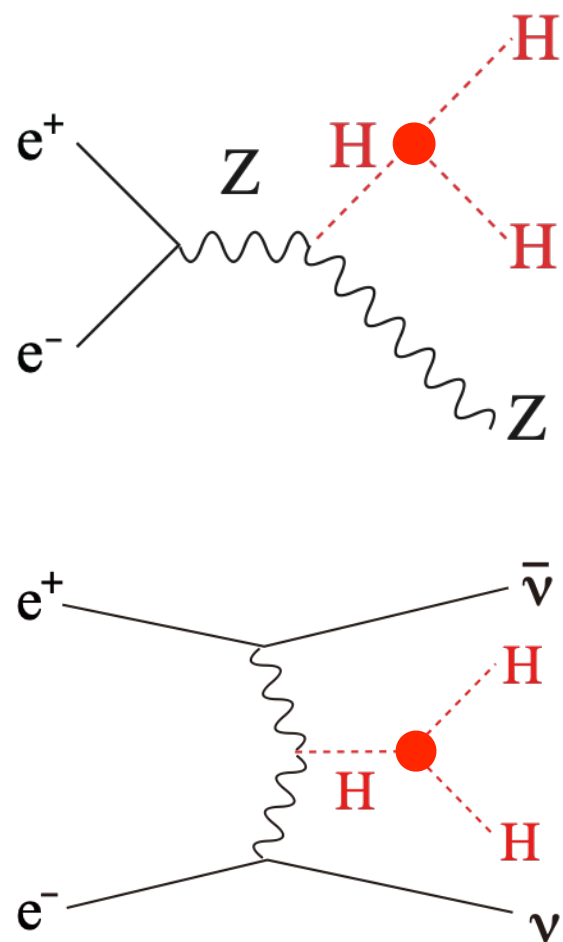


- based on global SMEFT fits
- HL-LHC di-Higgs contribution was always combined

- current focus: detailed look in Single-Higgs about other NLO effects; potential improvement in Di-Higgs analyses

Higgs self-coupling studies @ ILC

- $\sqrt{s} \sim 500$ GeV: $e^+e^- \rightarrow ZHH$
- $\sqrt{s} \sim 1$ TeV: $e^+e^- \rightarrow \nu_e \bar{\nu}_e HH$



full simulation studies @ ILC

- dominant channels covered

<50%

Z decay mode	HH decay mode	BranchingRatio
$Z \rightarrow e^+e^-$	$HH \rightarrow b\bar{b}b\bar{b}$	1.1%
$Z \rightarrow \mu^+\mu^-$	$HH \rightarrow b\bar{b}b\bar{b}$	1.1%
$Z \rightarrow \nu^+\bar{\nu}$	$HH \rightarrow b\bar{b}b\bar{b}$	6.7%
$Z \rightarrow b\bar{b}$	$HH \rightarrow b\bar{b}b\bar{b}$	5.0%
$Z \rightarrow q\bar{q}$	$HH \rightarrow b\bar{b}b\bar{b}$	17%
$Z \rightarrow b\bar{b}$	$HH \rightarrow b\bar{b}WW^*, WW^* \rightarrow 4q$	1.7%
$Z \rightarrow c\bar{c}$	$HH \rightarrow b\bar{b}WW^*, WW^* \rightarrow 4q$	1.4%
$Z \rightarrow b\bar{b}$	$HH \rightarrow b\bar{b}WW^*, WW^* \rightarrow l\nu 2q$	1.1%
$Z \rightarrow c\bar{c}$	$HH \rightarrow b\bar{b}WW^*, WW^* \rightarrow l\nu 2q$	0.92%
$Z \rightarrow l^+l^-$	$HH \rightarrow b\bar{b}WW^*, WW^* \rightarrow 4q$	0.76%
$Z \rightarrow l^+l^-$	$HH \rightarrow b\bar{b}WW^*, WW^* \rightarrow l\nu 2q$	0.50%

Table 1: signal channels analysed for $e^+e^- \rightarrow ZHH$ at $\sqrt{s} = 500$ GeV.

(for $e^+e^- \rightarrow \nu\nu HH$ @1TeV: $HH \rightarrow b\bar{b}b\bar{b}/b\bar{b}WW^*$ are covered)

full simulation studies @ ILC

[analysis ~10y ago]

- **generator:** *Whizard* 1.95, *Physsim* (realistic beamsstrahlung, ISR, pile-up)
- **parton shower & hadronization:** *Pythia* 6
- **detector model:** ILD (as realistic as possible material budget, blind areas)
- **simulation & reconstruction:** *Geant* 4, *iLCSoft* (realistic algorithms for tracking, particle flow (*PandoraPFA*), flavor tagging (*LCFI+*), jet-clustering, etc)
- **event selection:** full SM background, realistic cuts, careful categorization, kinematic fitting, multivariate method

full simulation studies @ ILC

- results (example individual channels) [analysis ~10y ago]

ZHH channel	s ($HH \rightarrow bbbb$)	b	σ_e	eff.
$eeHH$	3.9 ± 0.03 (2.6)	7 ± 0.6	1.29σ	59%
$\mu\mu HH$	5.1 ± 0.03 (2.8)	9 ± 0.5	1.48σ	55%
$\nu\nu HH$	5.6 ± 0.04 (5.5)	7 ± 1.0	1.78σ	19%
$bbHH$	8.5 ± 0.10 (8.0)	22 ± 1.3	1.75σ	29%
$qqHH$	12.6 ± 0.1 (10.9)	55 ± 2.0	1.65σ	15%

Table 2: Results of the event selection of ZHH with $HH \rightarrow bbbb$ corresponding to an integrated luminosity of $\mathcal{L} = 2 \text{ ab}^{-1}$ and a beam polarisation of $P(e^+e^-) = (0.3, -0.8)$.

major bkg.: tt , ZZ , ZZZ , ZZH

- results (combined)

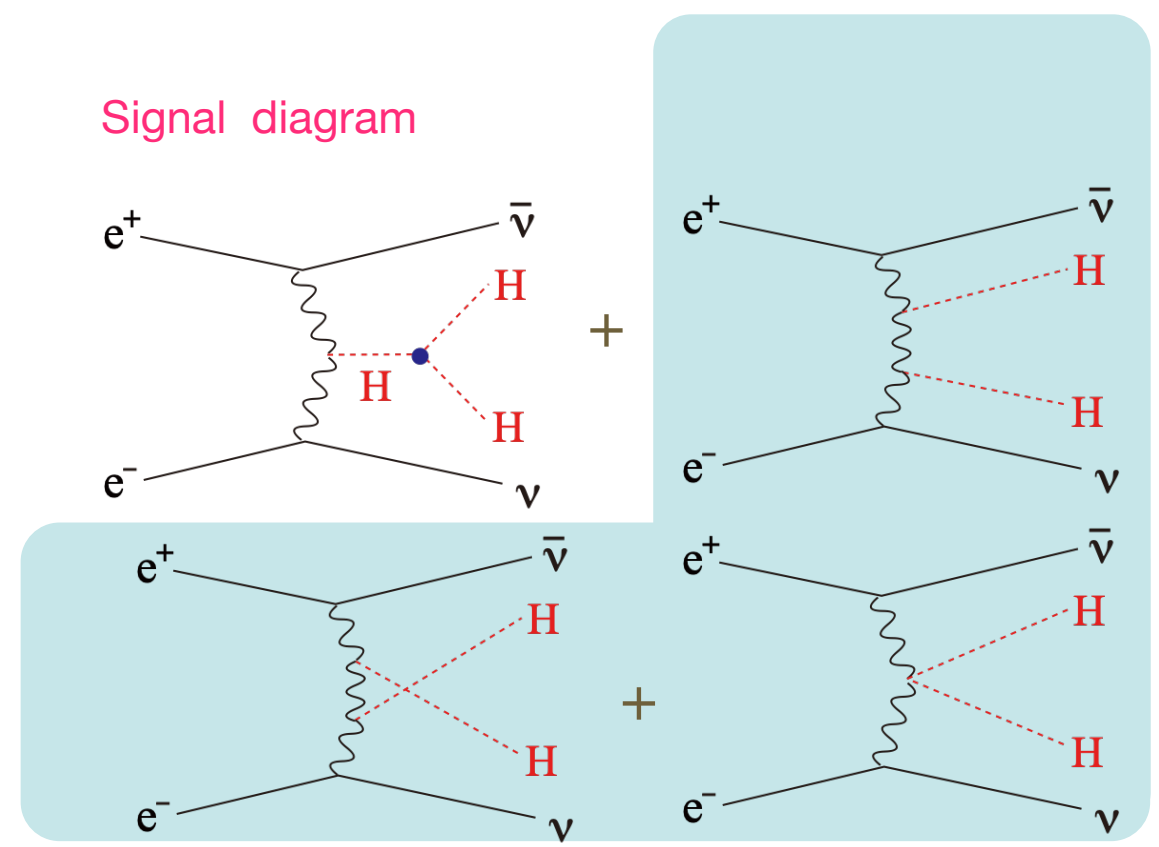
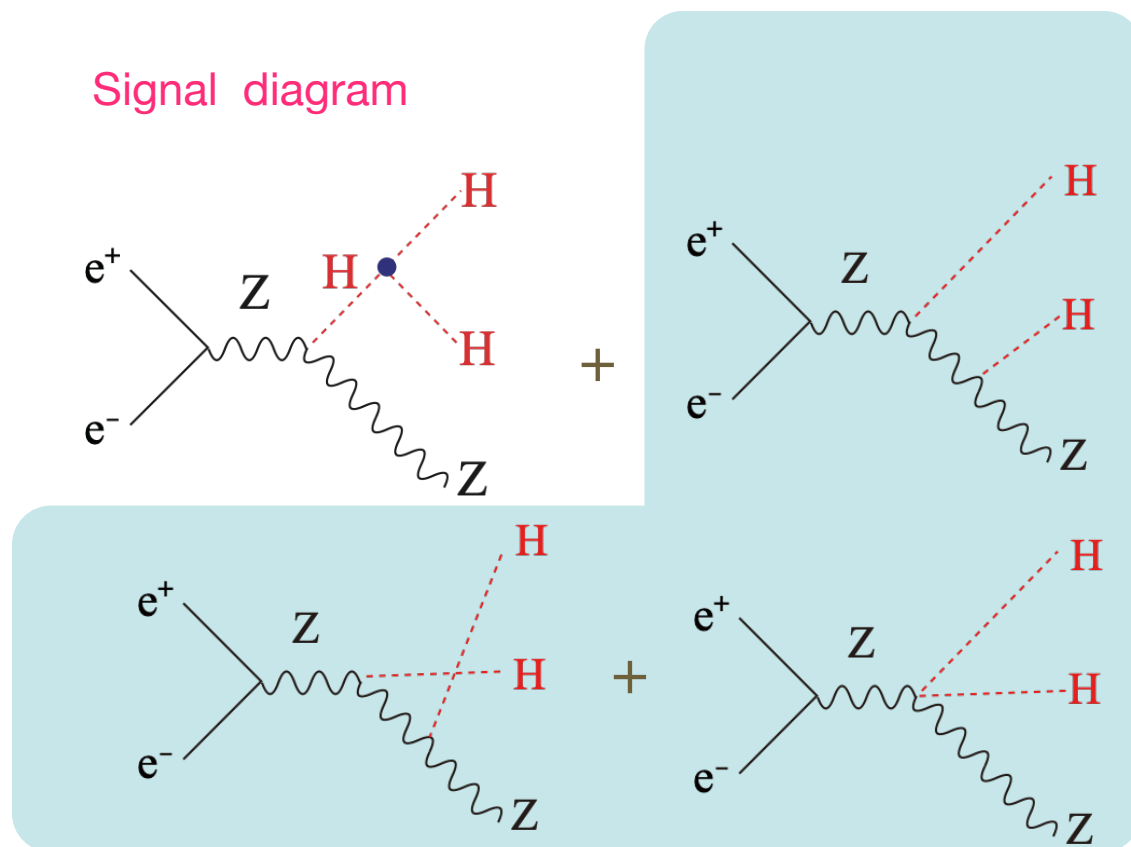
\sqrt{s}	$\int Ldt$	$\Delta\sigma/\sigma$	$\Delta\lambda_{HHH}/\lambda_{HHH}$
ZHH @ 500 GeV	4 ab^{-1} (*)	17%	27%
wHH @ 1 TeV	4 ab^{-1} (**)	15%	10%

$P(e^+, e^-) =$ *: equally shared by $(-0.8, +0.3)$ and $(+0.8, -0.3)$; **: $(-0.8, +0.2)$

from di-Higgs cross section to λ_{HHH}

$$\sigma = S\lambda^2 + I\lambda + B$$

(signal diagram) (interference) (background diagram)

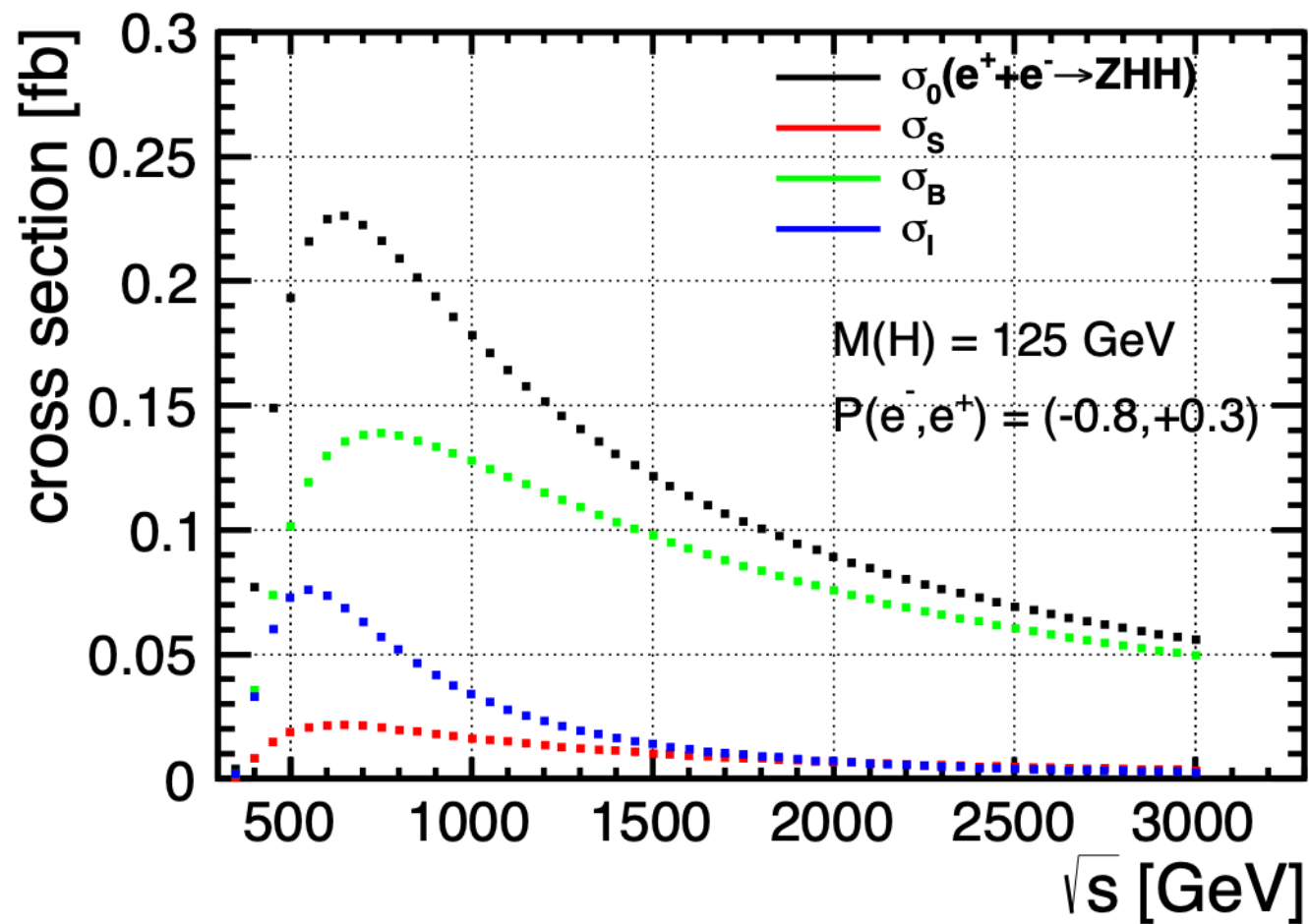


interference: constructive in ZHH, destructive in wHH

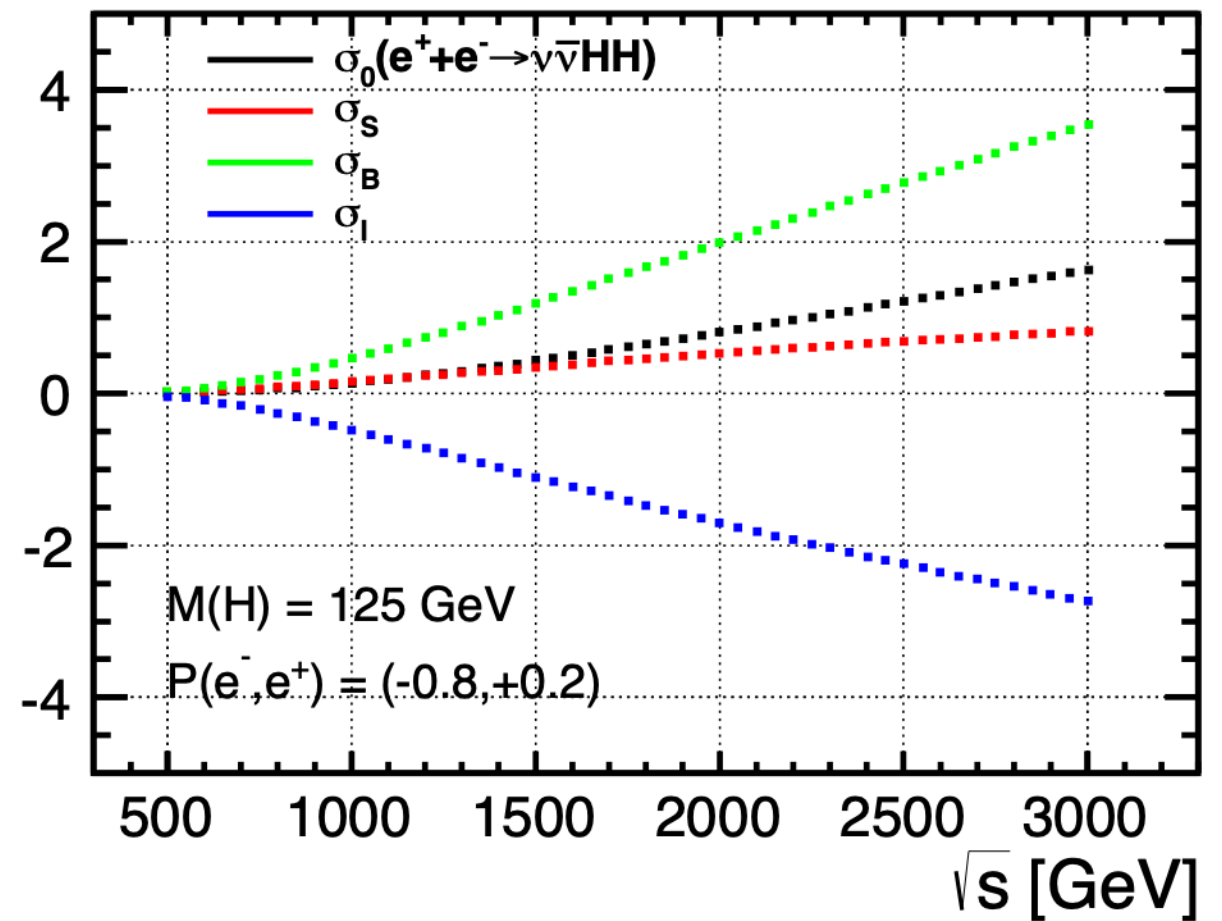
Di-Higgs cross section: break down & impact of \sqrt{s}

$$\sigma = S\lambda^2 + I\lambda + B$$

ZHH

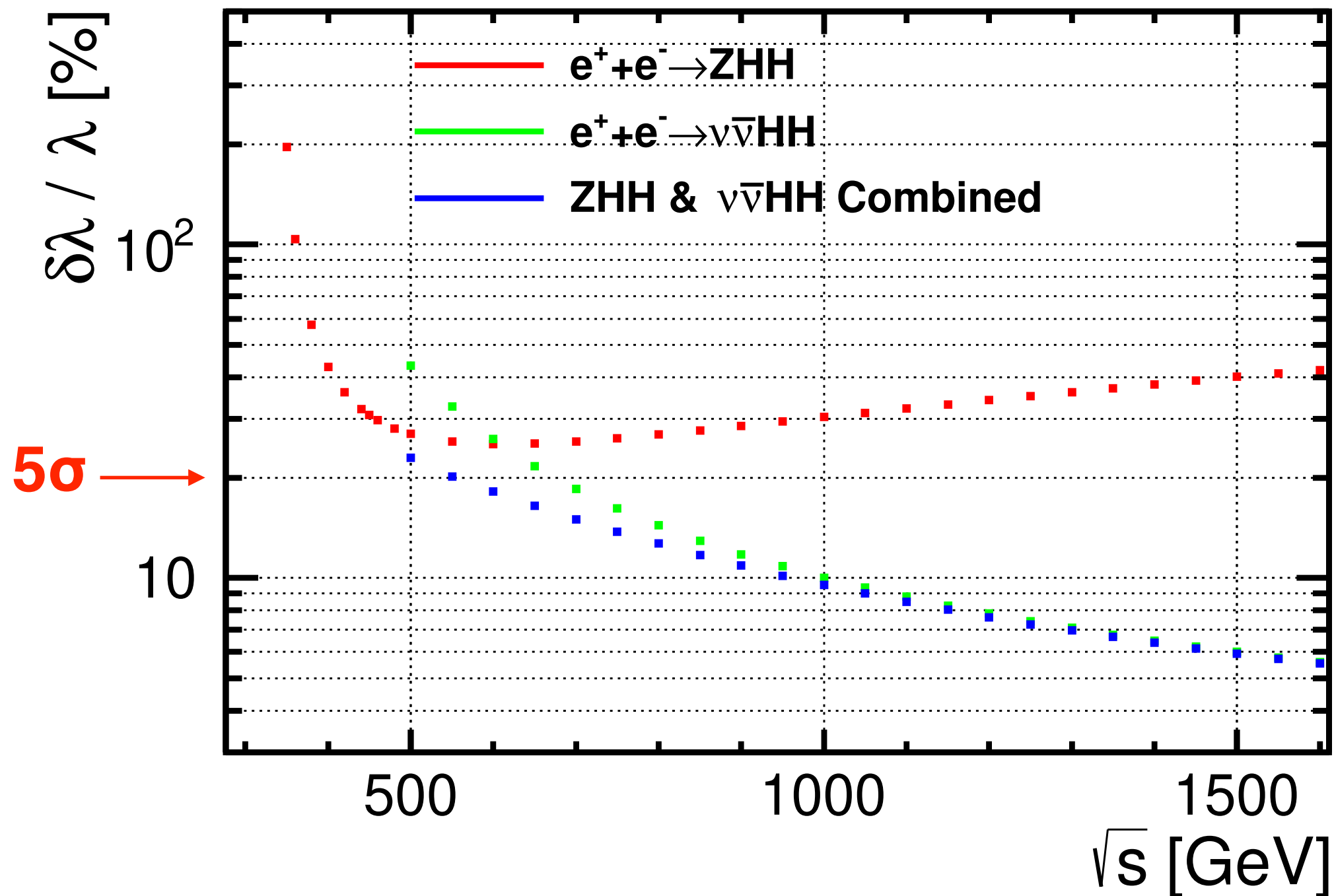


$\nu\nu HH$



updated projection $\Delta\lambda_{HHH}$

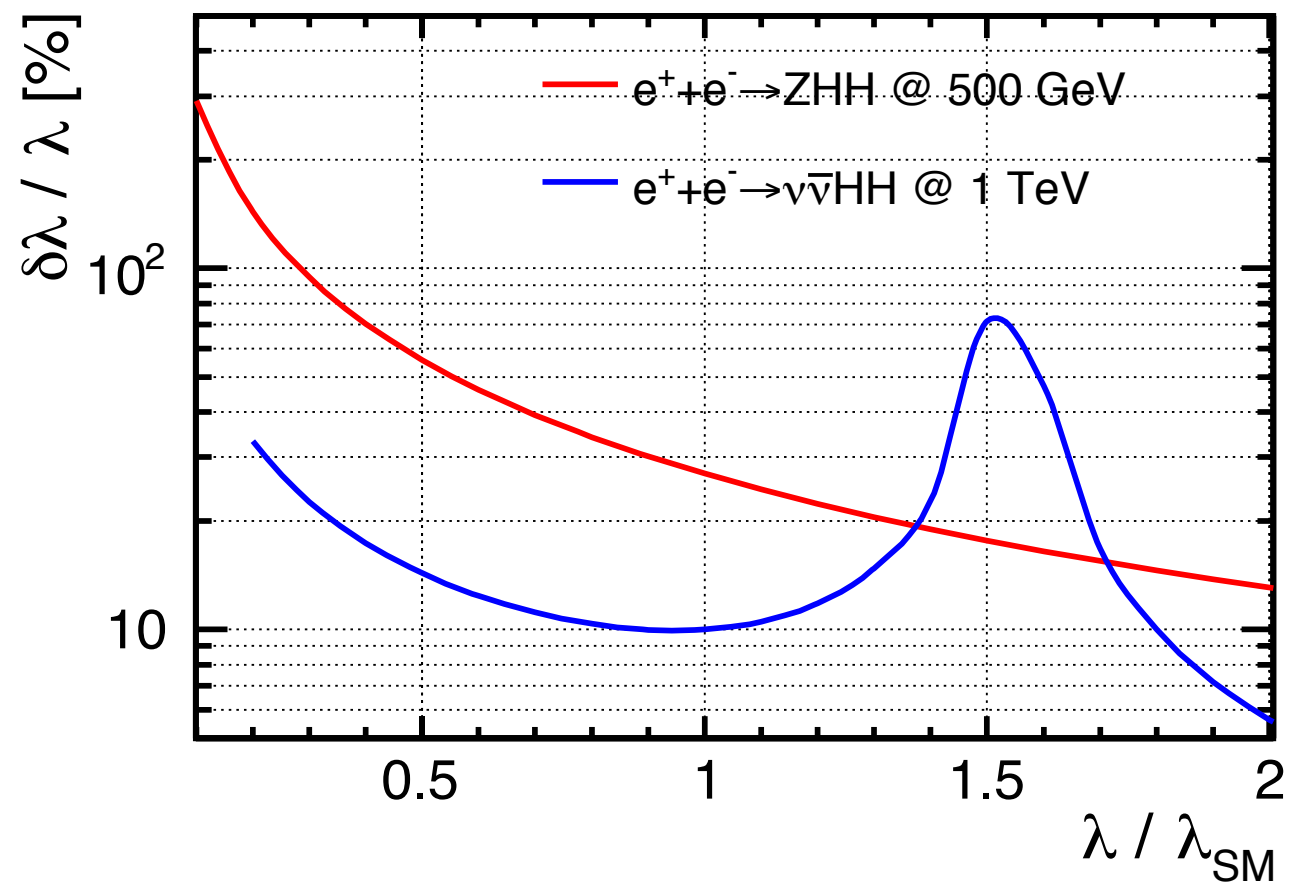
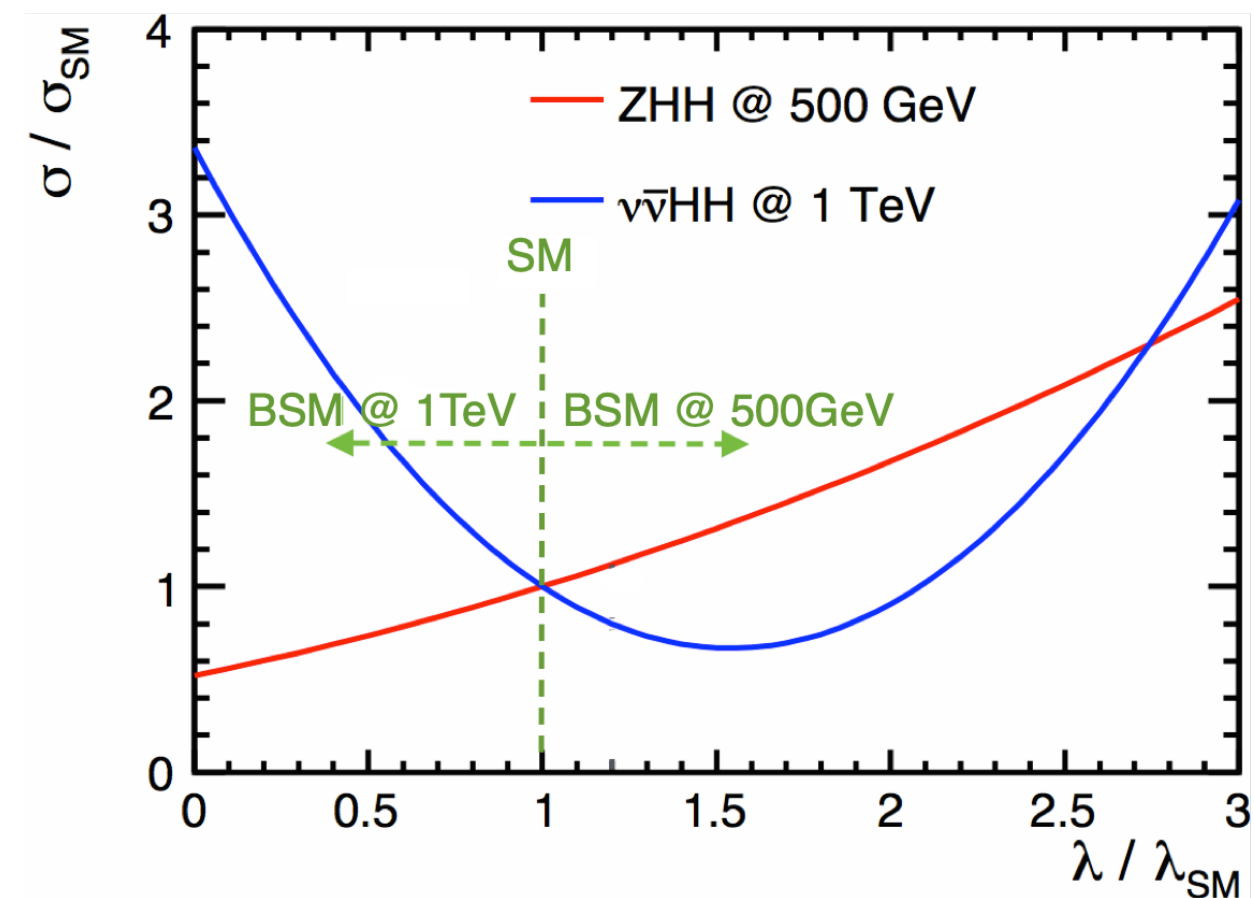
- two production channels **combined** at all \sqrt{s} : WW-fusion channel rapidly becomes useful just a little above 500 GeV
- luminosity now also scaled **proportionally** to \sqrt{s}



note: this is still based on old ILD DBD analysis

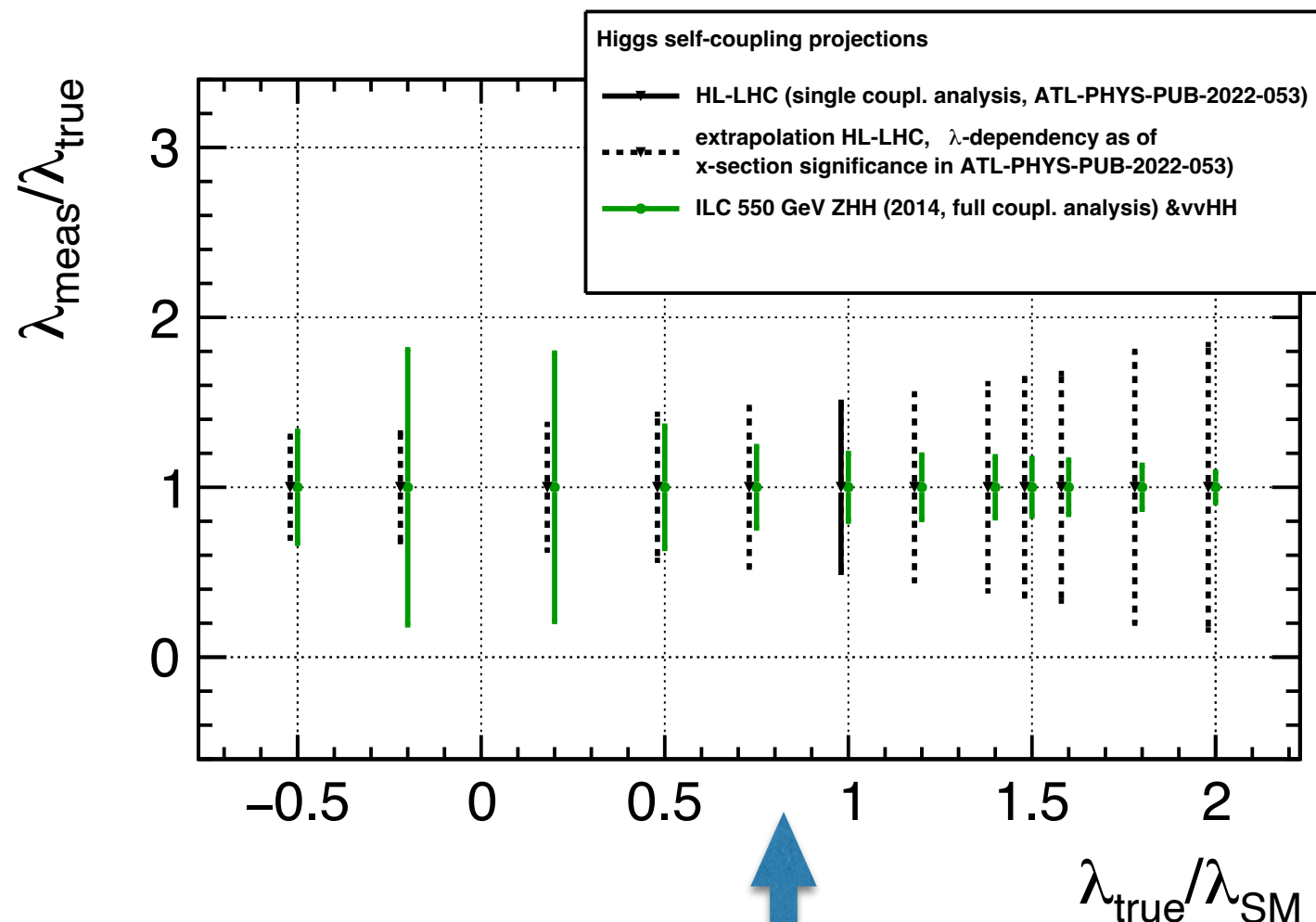
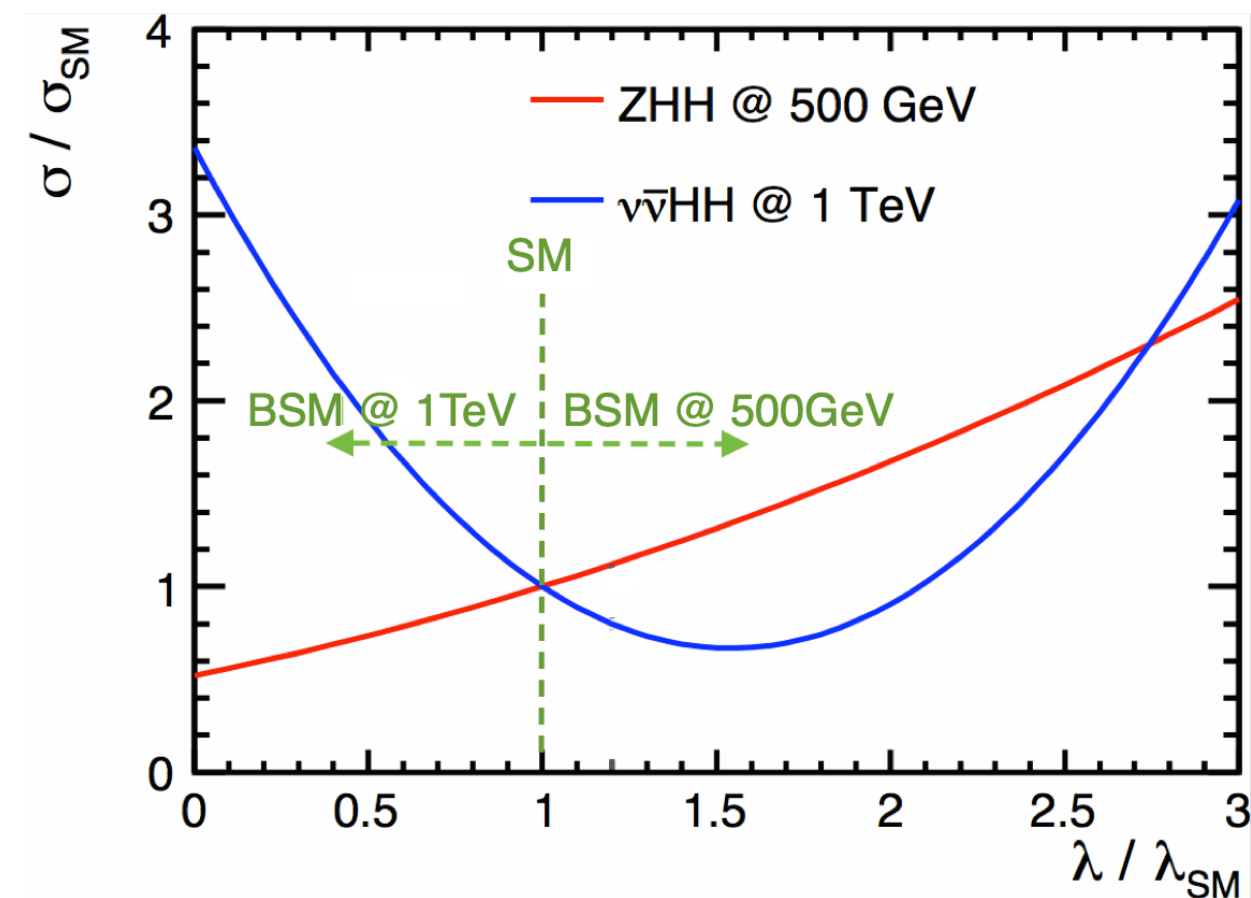
Higgs self-coupling: when $\lambda_{HHH} \neq \lambda_{SM}$?

- λ_{HHH} can be enhanced significantly $O(1)$ in BSM \longrightarrow [J. Braathen @ ECFA'24]
- complementarity between ZHH & $\nu\bar{\nu}HH$ (& LHC): interference nature
- if $\lambda_{HHH} / \lambda_{SM} = 2$, λ_{HHH} be measured to $\sim 10\%$ using ZHH @ ILC550 GeV



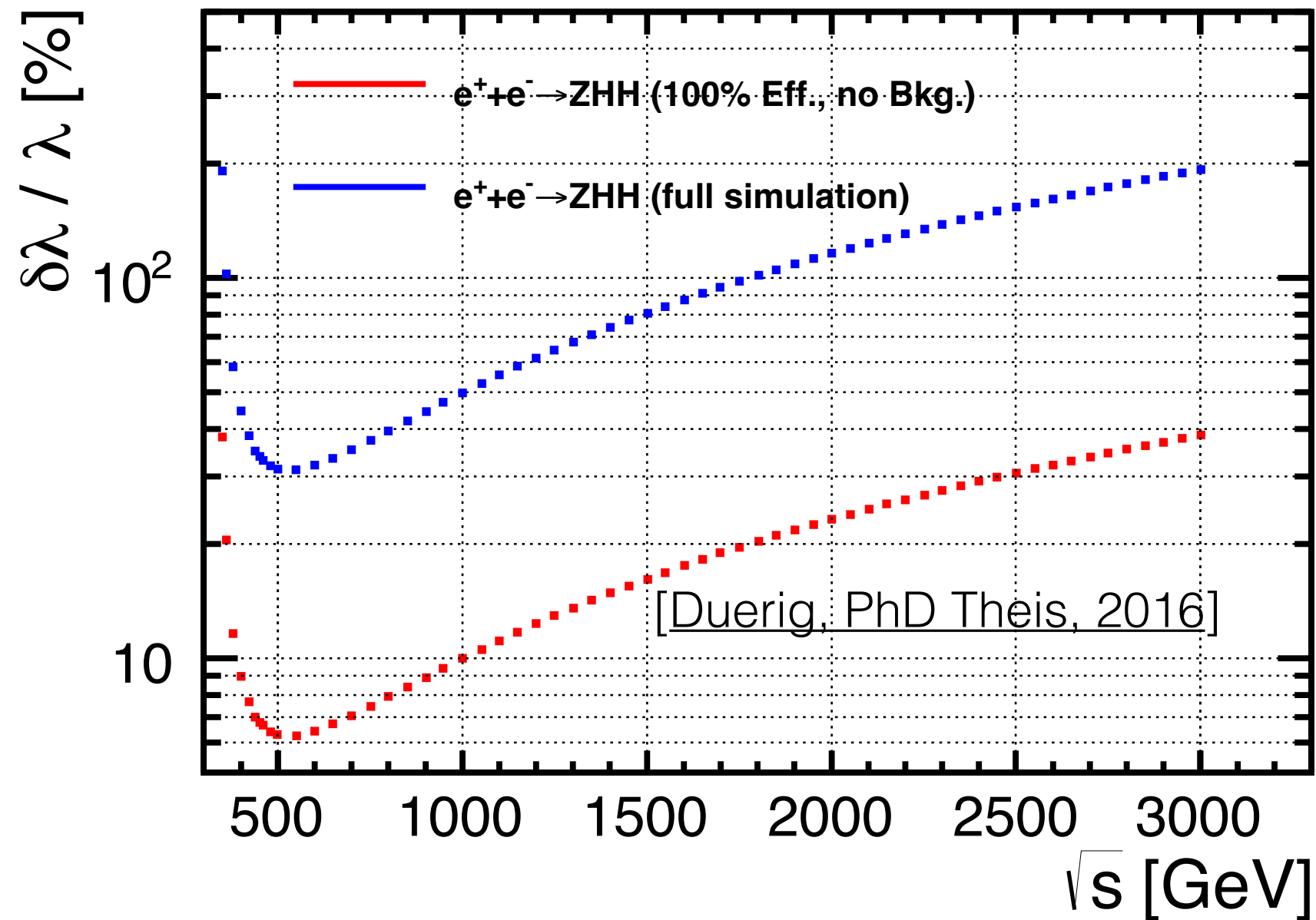
Higgs self-coupling: when $\lambda_{HHH} \neq \lambda_{SM}$?

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complementarity with LHC

prospect: $\Delta\lambda_{HHH}$ a factor of 5 from “perfect”

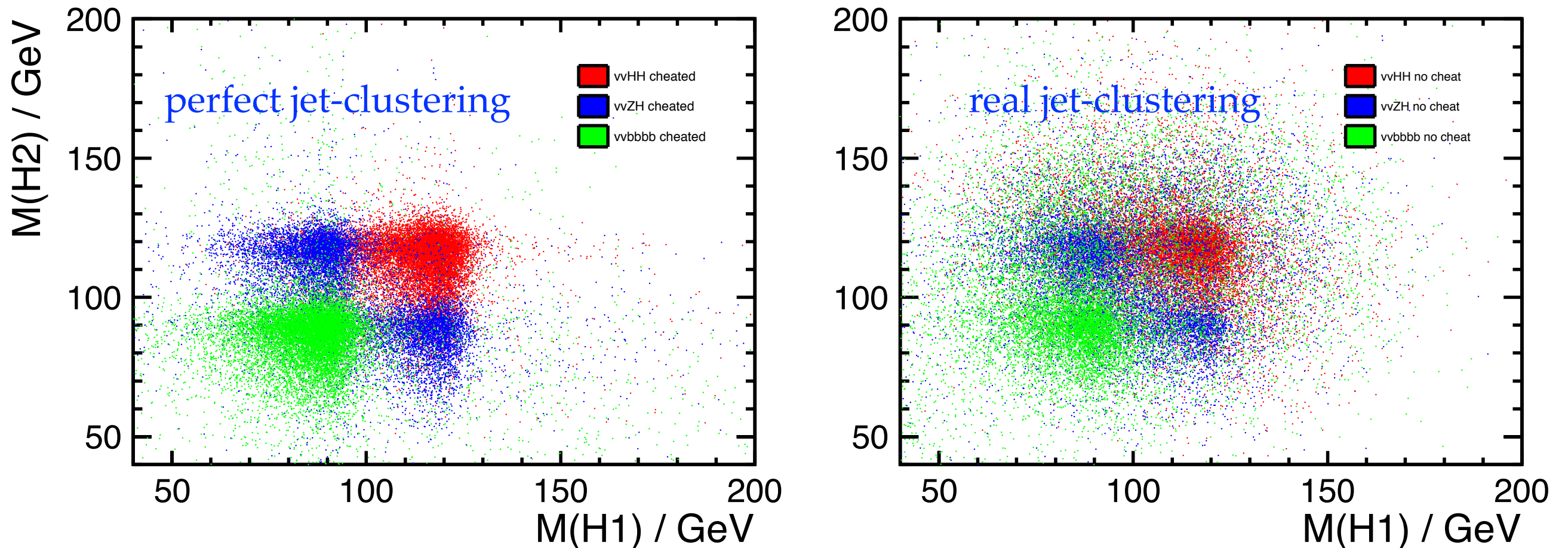


- how far can we go?

limiting factor: new jet-clustering algorithm?

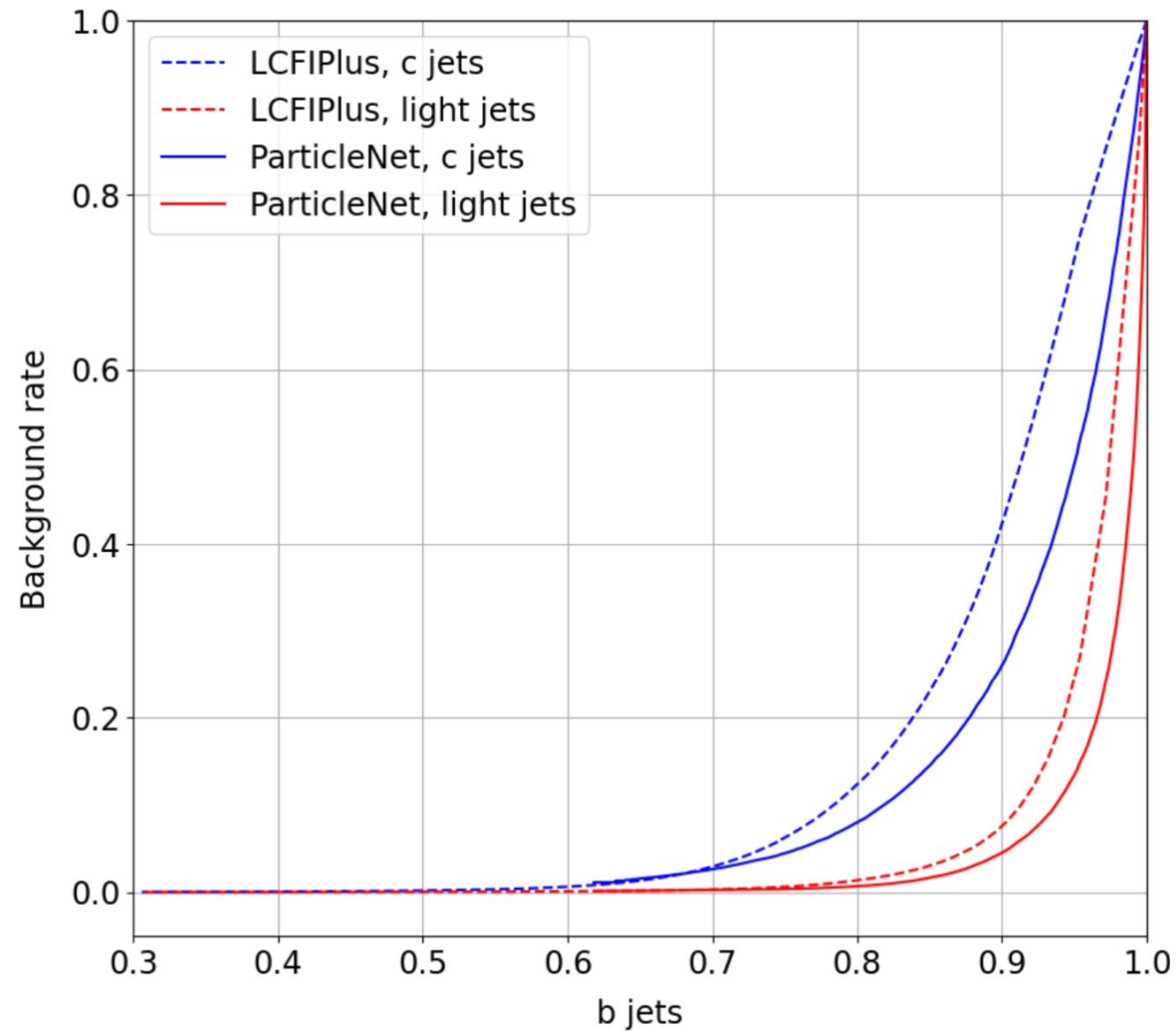
ZHH->vvbbbb (BG: ZZH and ZZZ)

scatter plot of two Higgs masses



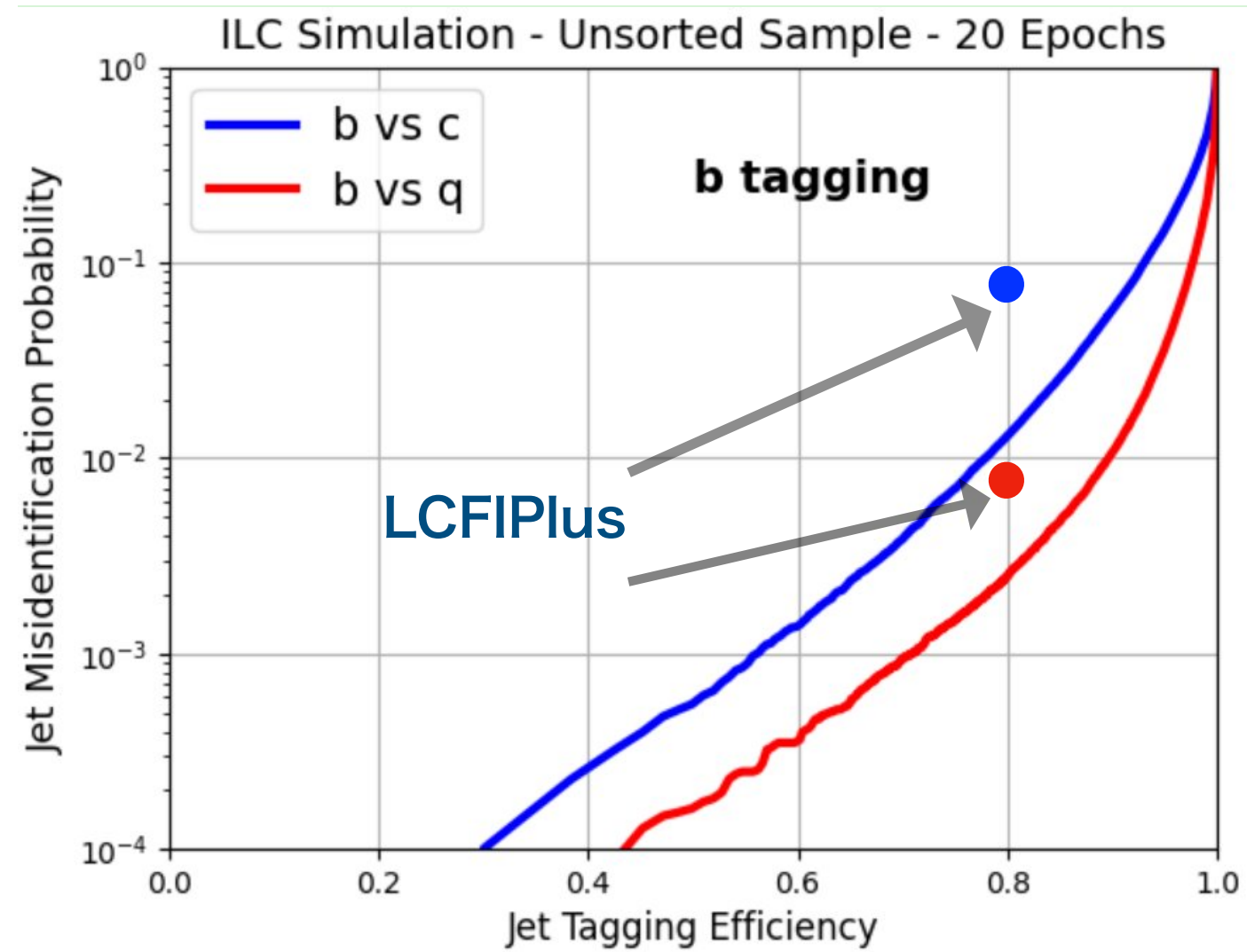
- ♦ the mis-clustering of particles degrades significantly the separation between signal and BG.
- ♦ it is studied that using perfect color-singlet-jet-clustering can improve $\delta\lambda/\lambda$ by 40%

new development on flavor tagging by ML



ParticleNet

[\[M. Meyer @ ECFA '23\]](#)



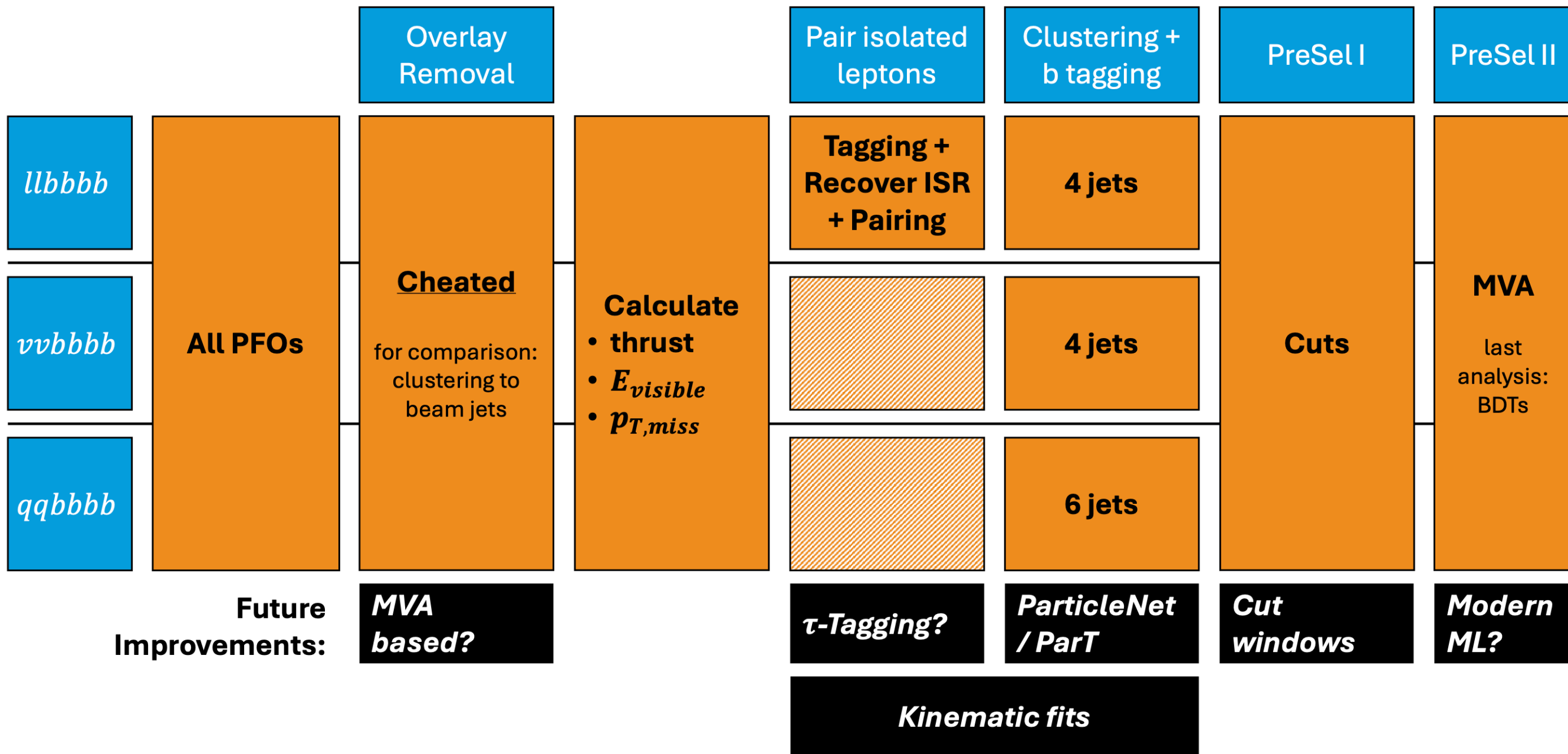
ParticleTransformer

[\[T. Suehara @ LCWS '24\]](#)

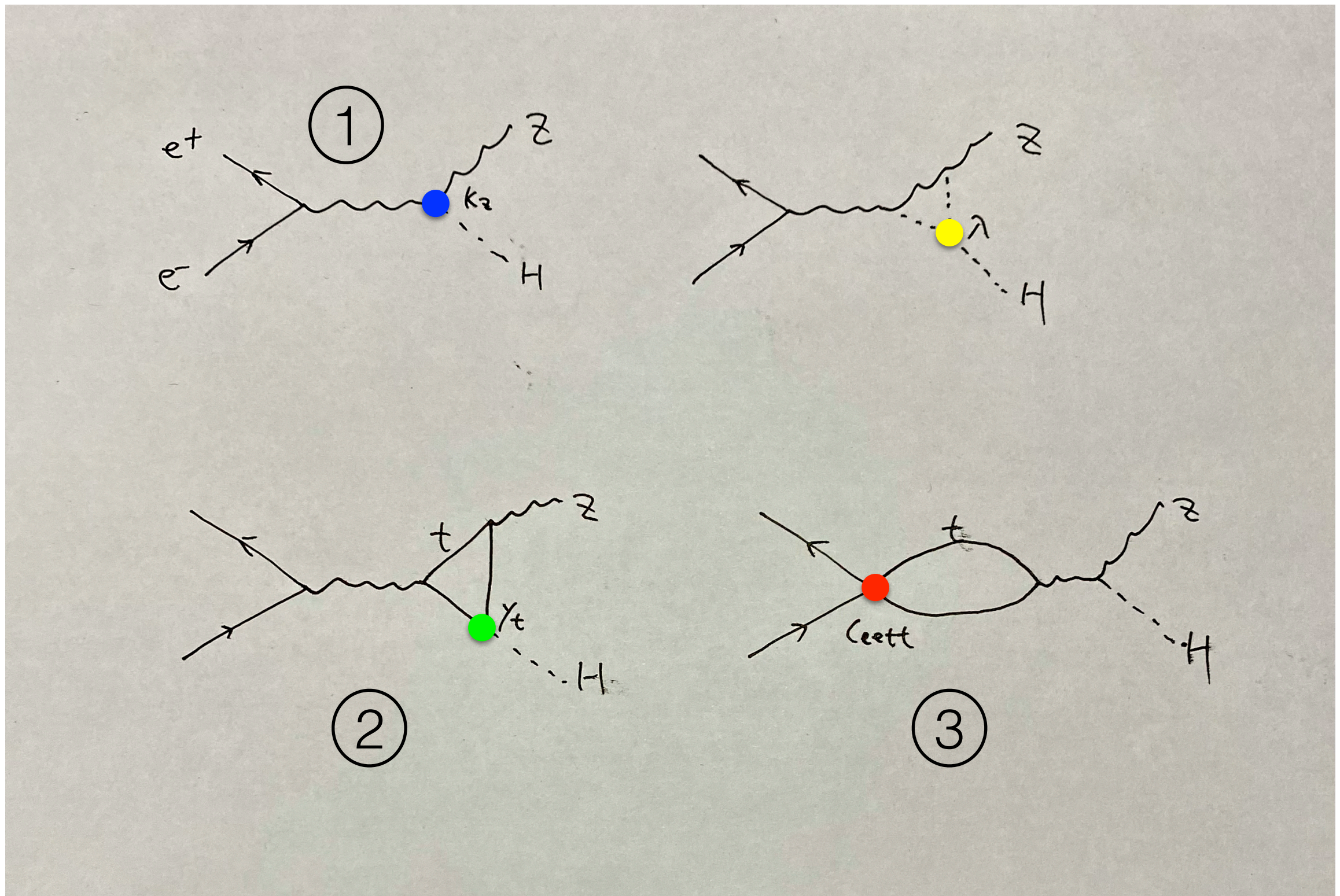
ongoing full ZHH analysis for next ESU

common ILC & C³

Analysis Flow

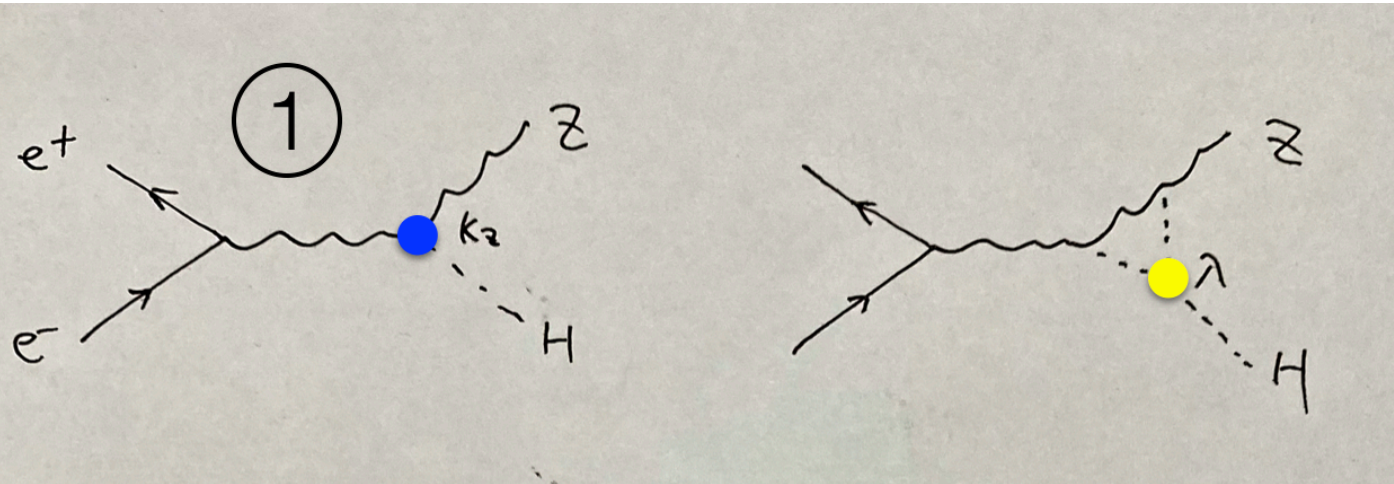


(ii) λ_{HHH} from Single-Higgs



+ many more operators in the same NLO order \longrightarrow [K. Asteriadis @ Higgs'24]

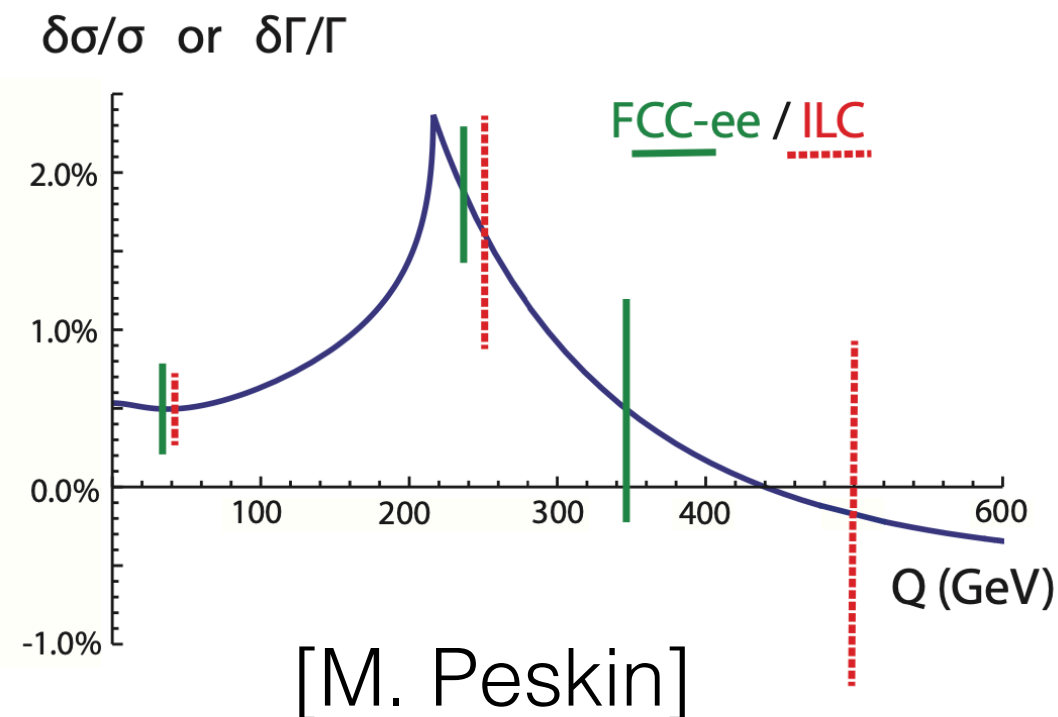
How to discriminate with HZZ coupling



[McCullough, '13]

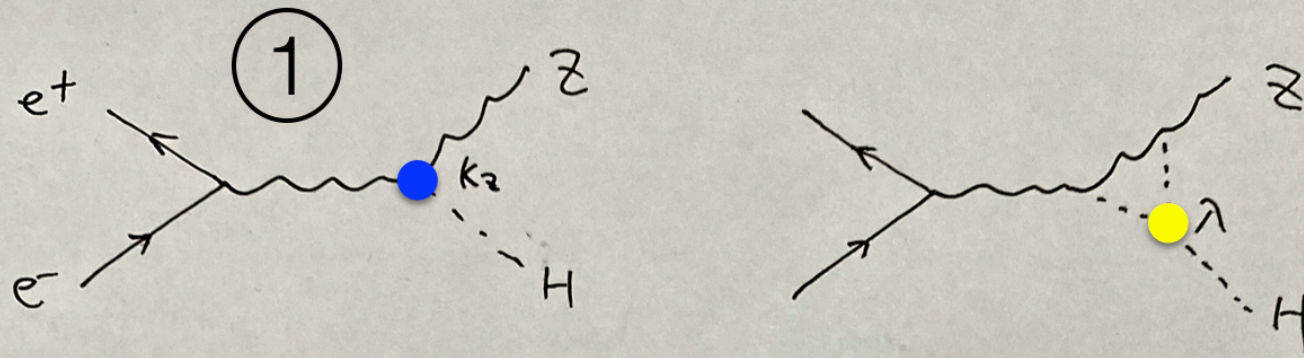
$$\delta_{\sigma}^{240} = 100 (2\delta_Z + 0.014\delta_h) \%$$

- $\delta\sigma_{ZH} < 1\%$ is a necessity; but not sufficient
- $\delta\sigma$ could receive contributions from many other sources
 —> $\delta h \sim \mathbf{O(500)\%}$ at 250GeV only; [Gu, et al, arXiv:1711.03978]



► “easy” solution: lift degeneracy by multiple \sqrt{s}


(iv) How to discriminate with HZZ coupling



[McCullough, '13]

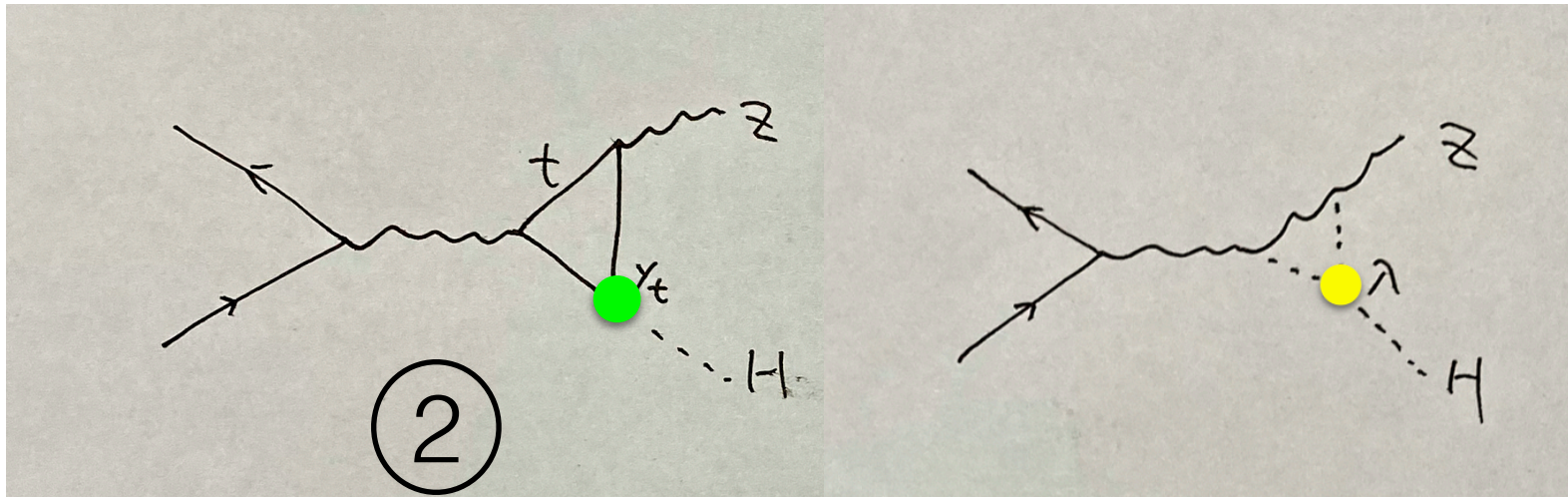
$$\delta_{\sigma}^{240} = 100 (2\delta_Z + 0.014\delta_h) \%$$

► difficult solution: using differential cross section

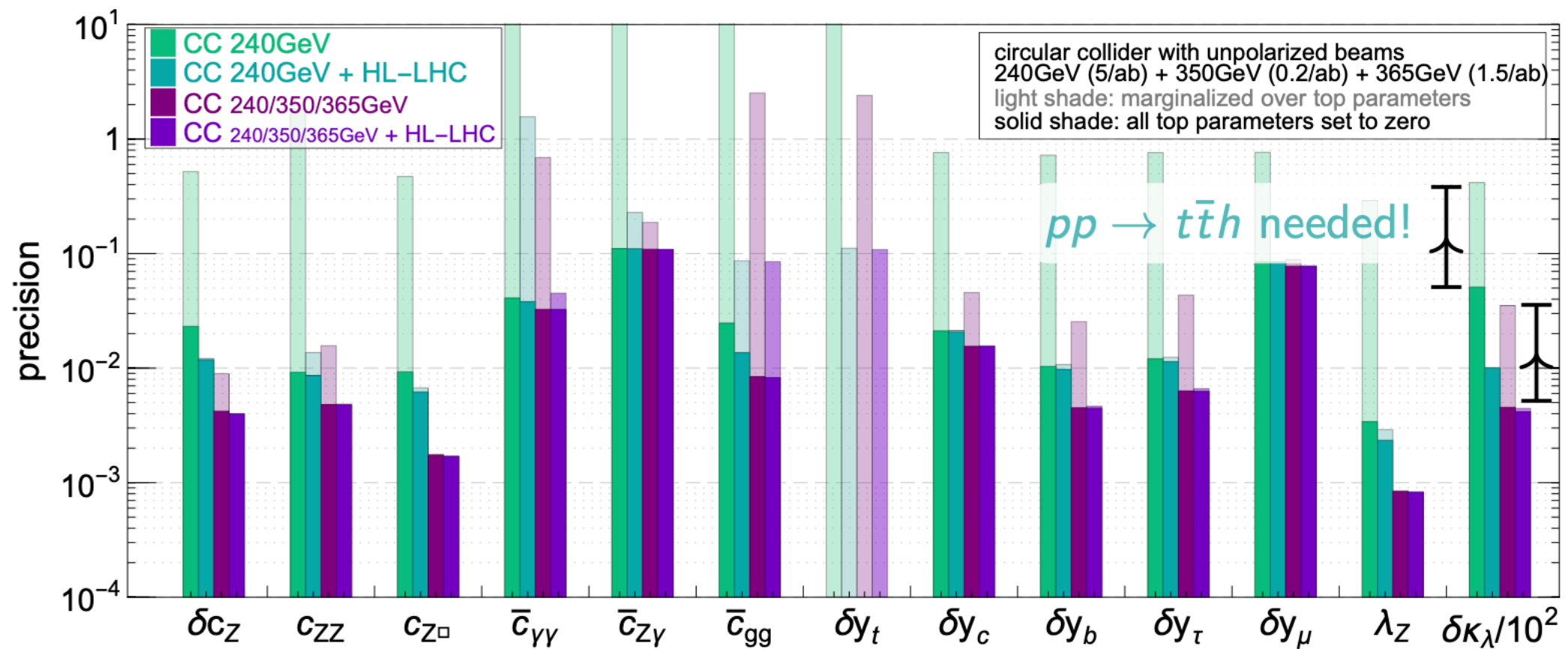
- angular meas.; radiative return  [G. Durieux @ ECFA mini-WS '23]
- effect of λ may connect to anomalous HZZ coupling

$$\mathcal{L} = m_Z^2 \left(\frac{1}{v} + \frac{a}{\Lambda} \right) H Z^\mu Z_\mu + \frac{b}{2\Lambda} H Z^{\mu\nu} Z_{\mu\nu} + \frac{\tilde{b}}{\Lambda} H Z^{\mu\nu} \tilde{Z}_{\mu\nu}$$

How to discriminate with top-Yukawa coupling



► mitigated by LHC top-Yukawa measurement

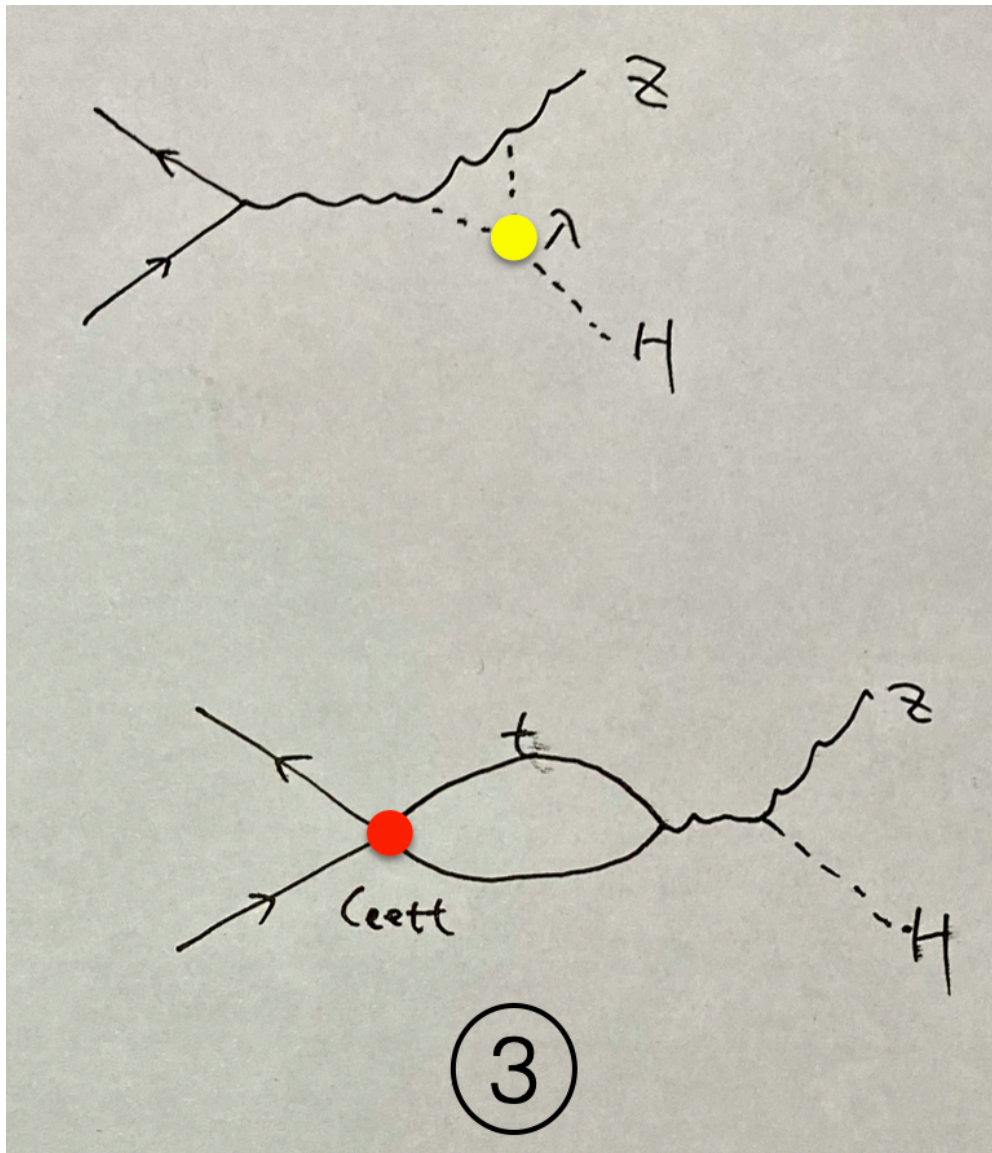


Top-quark uncertainties can impede Higgs precision!

[Durieux, Gu, Vyronidou, Zhang, '18]

How to discriminate with 4-fermion interaction

might be most pressing



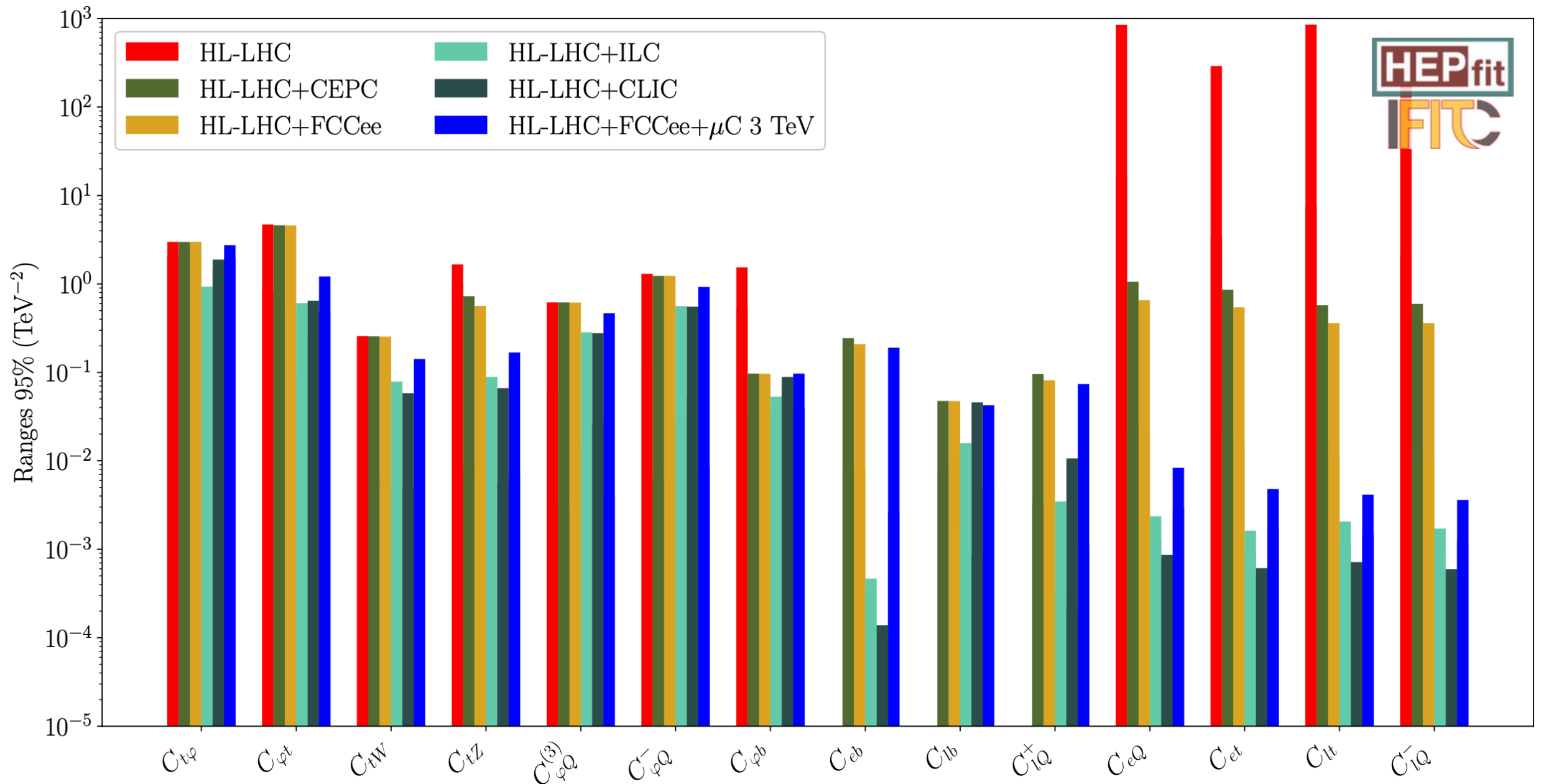
- the effects from (many) eett operators have just been calculated! [[Asteriadis, Dawson, Giardino, Szafron, arXiv:2406.03257](#)]

	$\sqrt{s} = 240 \text{ GeV}$		$\sqrt{s} = 365 \text{ GeV}$	
	Δ_i/Λ^2	$\bar{\Delta}_i/\Lambda^2$	Δ_i/Λ^2	$\bar{\Delta}_i/\Lambda^2$
C_ϕ	$-7.22 \cdot 10^{-3}$	0	$-1.00 \cdot 10^{-3}$	0
$C_{uW}[3, 3]$	$-1.63 \cdot 10^{-3}$	$4.01 \cdot 10^{-3}$	$3.36 \cdot 10^{-3}$	$6.25 \cdot 10^{-3}$
$C_{uB}[3, 3]$	$0.15 \cdot 10^{-3}$	$-2.22 \cdot 10^{-3}$	$-2.96 \cdot 10^{-3}$	$-3.20 \cdot 10^{-3}$
$C_{u\phi}[3, 3]$	$0.32 \cdot 10^{-3}$	0	$-1.09 \cdot 10^{-3}$	0
$C_{\phi q}^{(1)}[3, 3]$	$-1.34 \cdot 10^{-3}$	$-4.10 \cdot 10^{-3}$	$-4.39 \cdot 10^{-3}$	$-4.31 \cdot 10^{-3}$
$C_{\phi q}^{(3)}[3, 3]$	$0.51 \cdot 10^{-3}$	$4.12 \cdot 10^{-3}$	$4.15 \cdot 10^{-4}$	$7.58 \cdot 10^{-4}$
$C_{\phi u}[3, 3]$	$-0.54 \cdot 10^{-3}$	$3.49 \cdot 10^{-3}$	$5.37 \cdot 10^{-3}$	$3.11 \cdot 10^{-3}$
$C_{eu}[1, 1, 3, 3]$	$0.01 \cdot 10^{-3}$	$-1.39 \cdot 10^{-2}$	$-3.73 \cdot 10^{-2}$	$-3.23 \cdot 10^{-2}$
$C_{lu}[1, 1, 3, 3]$	$-0.02 \cdot 10^{-3}$	$1.73 \cdot 10^{-2}$	$4.64 \cdot 10^{-2}$	$4.01 \cdot 10^{-2}$
$C_{lq}^{(1)}[1, 1, 3, 3]$	$-0.37 \cdot 10^{-2}$	$-1.80 \cdot 10^{-2}$	$-6.09 \cdot 10^{-2}$	$-4.18 \cdot 10^{-2}$
$C_{lq}^{(3)}[1, 1, 3, 3]$	$-0.37 \cdot 10^{-2}$	$1.29 \cdot 10^{-2}$	$4.54 \cdot 10^{-2}$	$3.29 \cdot 10^{-2}$
$C_{qe}[3, 3, 1, 1]$	$0.30 \cdot 10^{-2}$	$1.45 \cdot 10^{-2}$	$4.90 \cdot 10^{-2}$	$3.36 \cdot 10^{-2}$

How to discriminate with 4-fermion interaction

[M. Vos @ ECFA '24]

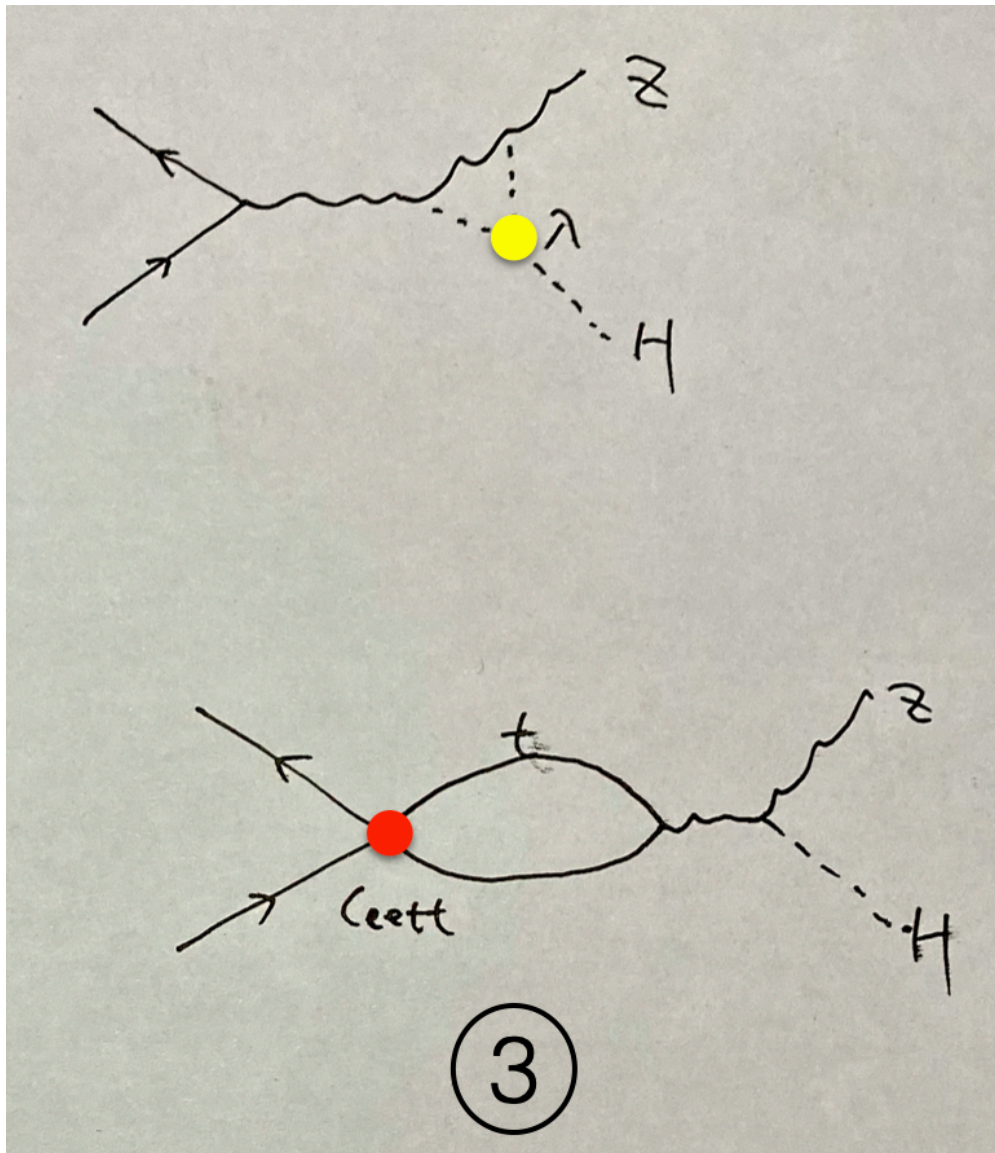
- need projection for eett at HL-LHC & e+e-



All e+e- colliders improve the bounds on the top sector dramatically
 High-energy operation is important to provide the strongest global bounds

first look at the global fit with NLO eett for $\Delta\lambda_{HHH}$

[ongoing work by: Yong Du, Jiayin Gu, JT]



- based on a fitting program for last ESU: 23 (Higgs + WW + EWPO) + 5 (eett) operators
- take directly covariance matrix as eett bounds (from Victor Miralles)
- reproduced (almost) the NLO calculation about eett in ZH

extra uncertainty induced by eett on σ_{ZH}

$$\delta\sigma_{ZH} \sim 0.3\% (1.5\%) \text{ for } 240 (365) \text{ GeV}$$

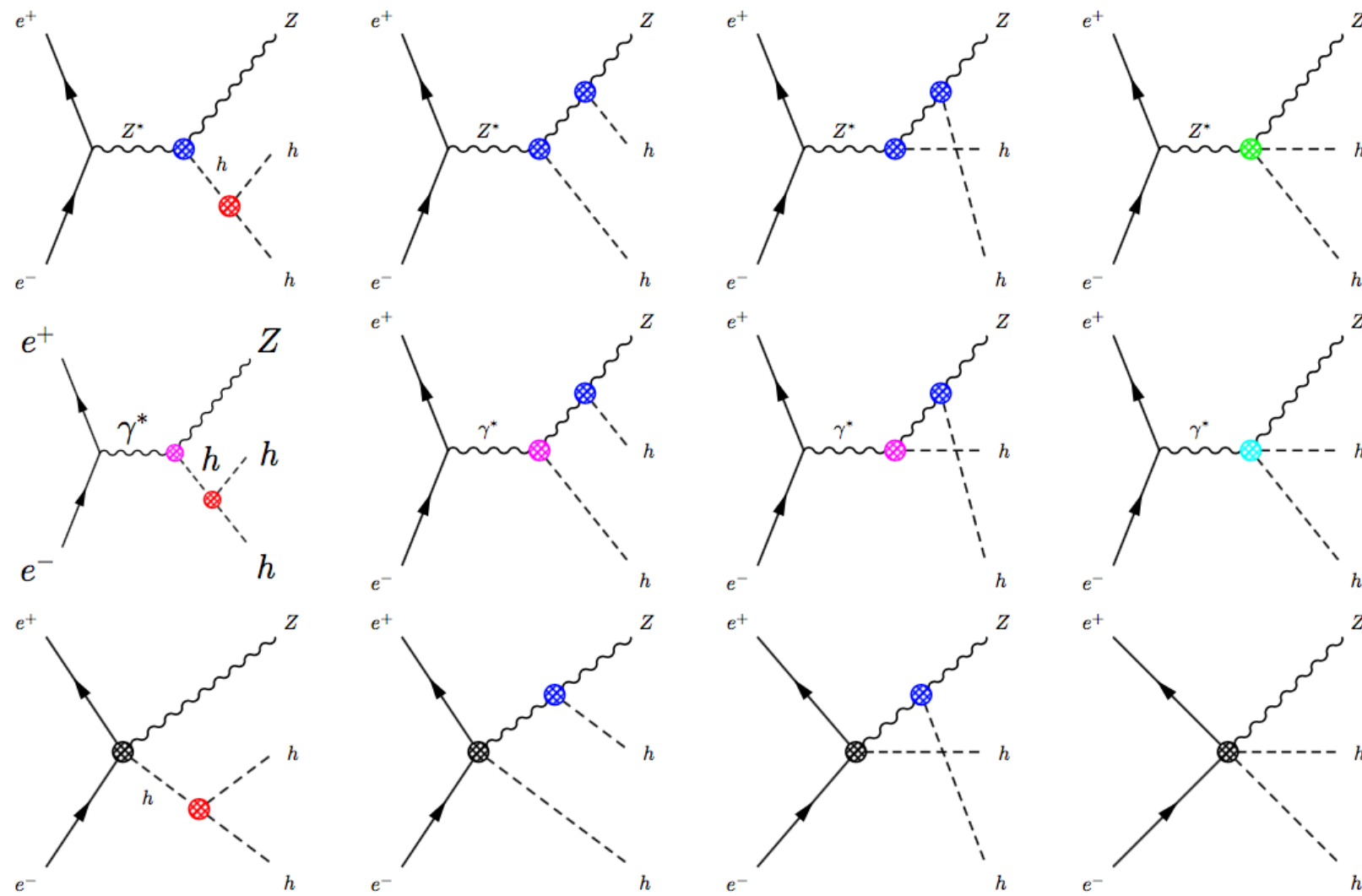
a test fit for $5000 \text{ fb}^{-1} (240) + 1500 \text{ fb}^{-1} (365)$

$\Delta\lambda_{HHH}$ mildly degraded from 57% to 77%

[warning: this is very preliminary, many things to be done, e.g. include NLO eett in other observables as well.]

similar issue in double-Higgs approach

[Barklow, Fujii, Jung, Peskin, JT, '17]



- degeneracies from same-order SMEFT resolved

summary

- Challenging task to measure Higgs self-coupling at future colliders
- Many progresses on theory, di-Higgs & single-Higgs approaches
- Ongoing di-Higgs analysis to update λ_{HHH} projection: huge room existing by new advanced analysis tools
- A new global SMEFT fit is being worked out to address the opportunity / challenges in probing λ_{HHH} using single-Higgs
 - welcome to join the adventure!

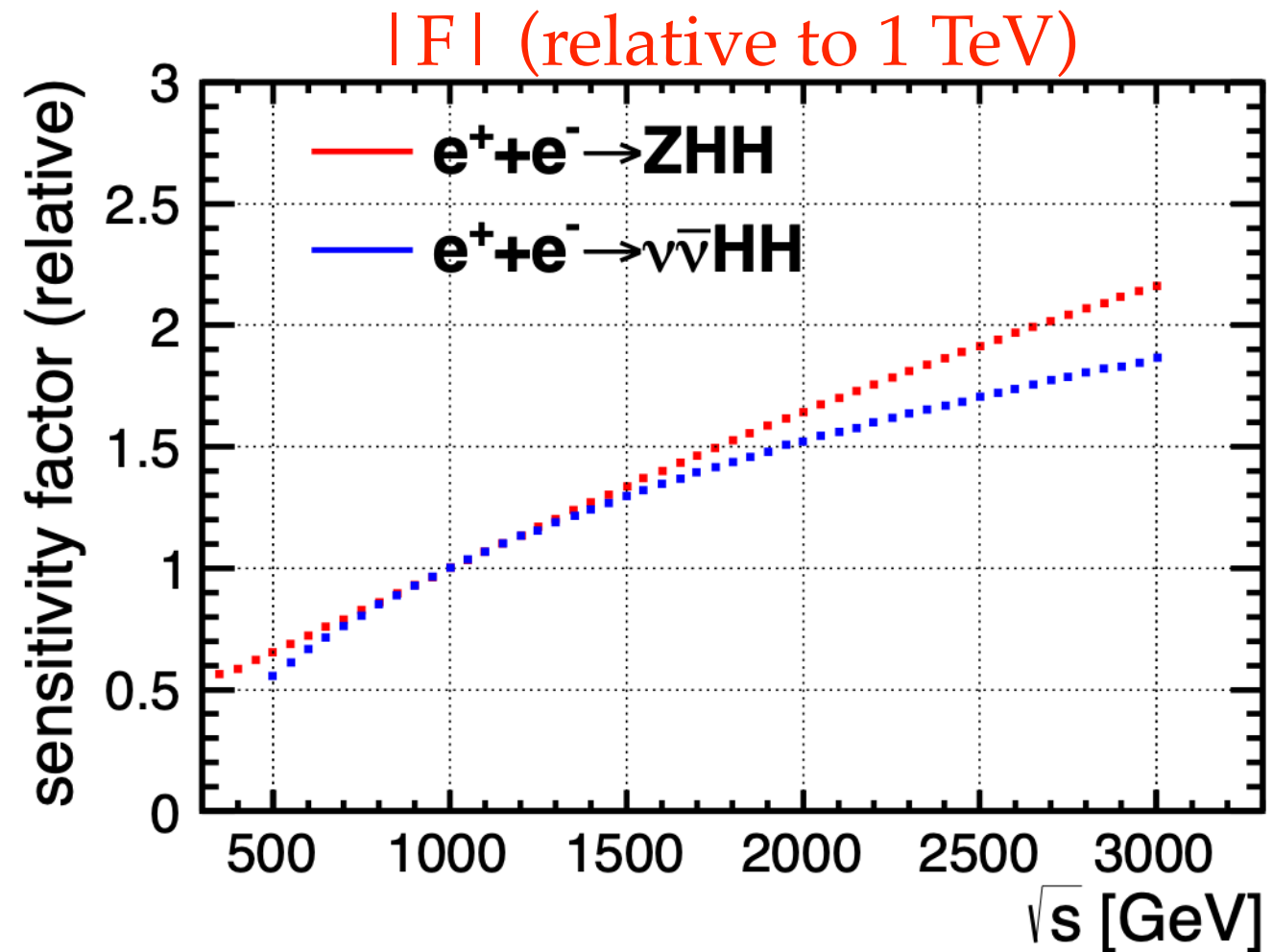
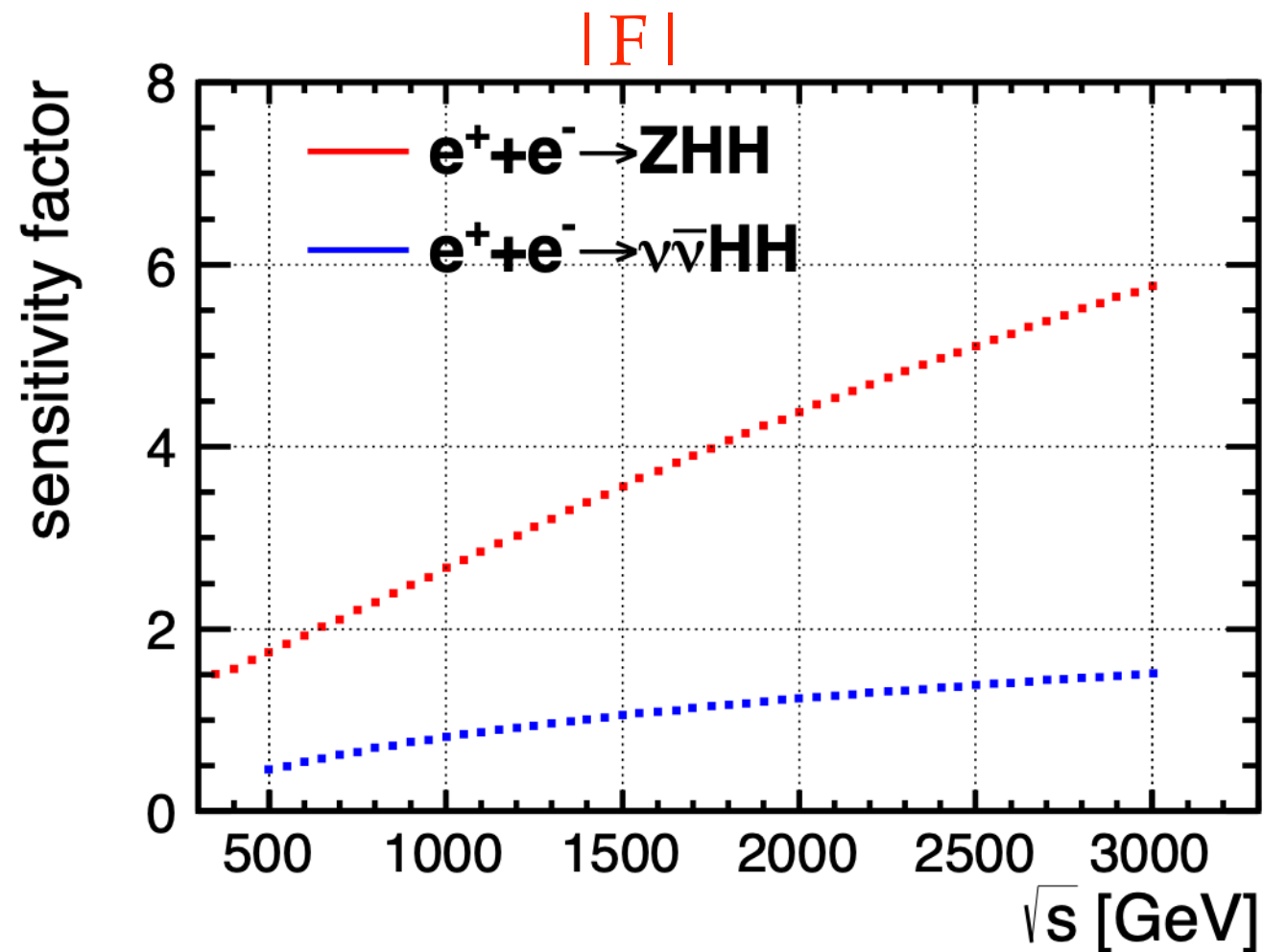
backup

Higgs self-coupling: impact of ECM

$$\frac{\delta\lambda}{\lambda} = F \cdot \frac{\delta\sigma}{\sigma}$$

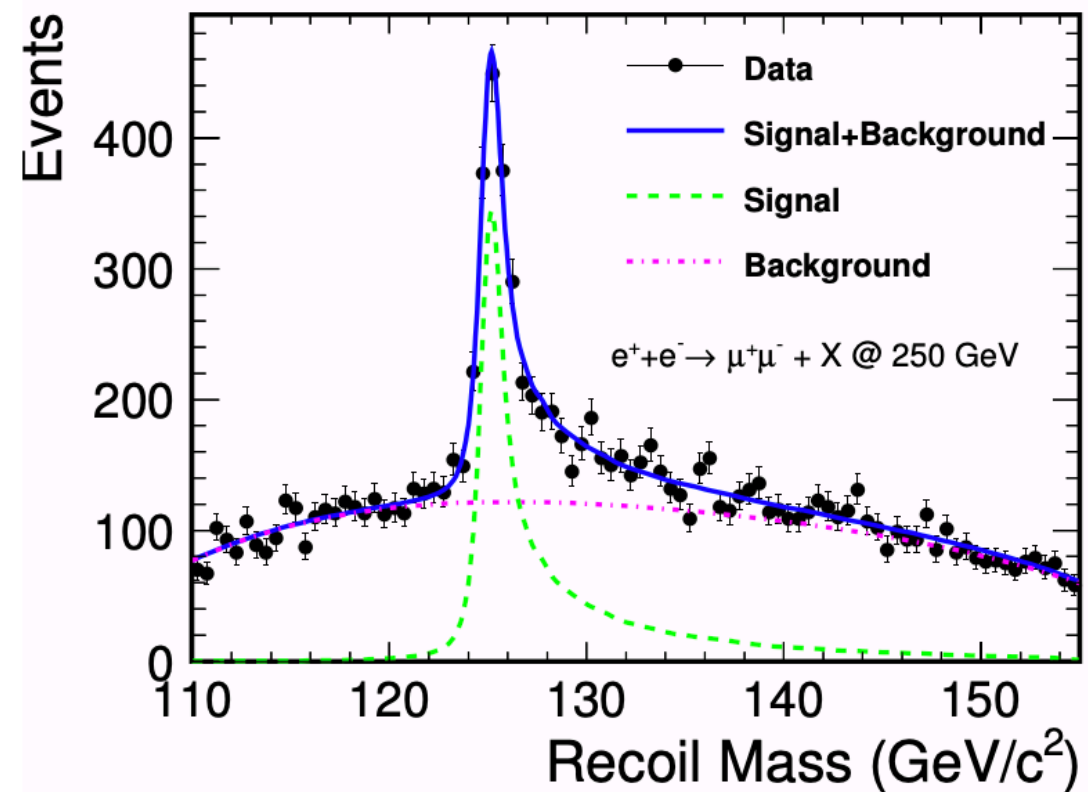
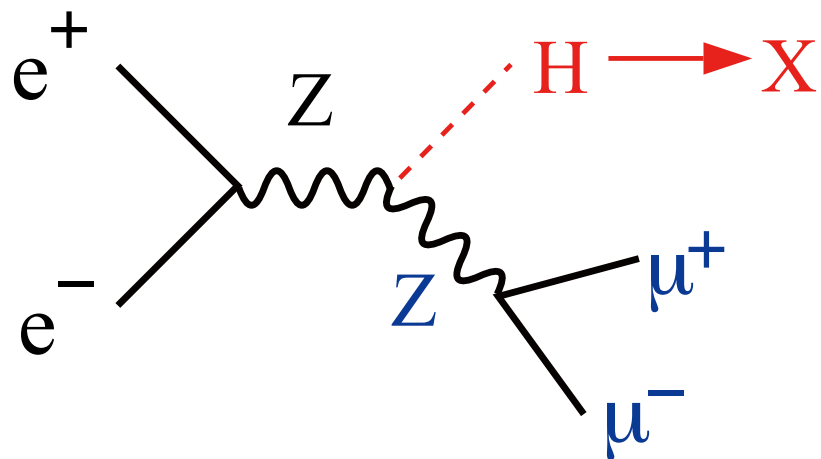
$$F = \frac{\sigma}{2S\lambda^2 + I\lambda}$$

sensitivity factor



Challenges: $\delta\sigma_{ZH} \ll 1\%$?

- **A: yes!** Just give me **1 million** recoil Higgs events $\rightarrow 0.1\%$
- **B: likely!** Assume only **1/4** of the 1M events useful $\rightarrow 0.2\%$
- **C: let's look at some systematics first**



[Yan et al, arXiv:1604.07524]

- a crucial requirement for measuring σ_{ZH} using recoil mass technique:
independent of how Higgs decay \rightarrow who not just test it!

Challenges: $\delta\sigma_{ZH} \ll 1\%$?

- $Z \rightarrow \mu\mu$: $\delta\text{Efficiency} \sim 1\%$

[Yan et al, arXiv:1604.07524]

$H \rightarrow XX$	bb	cc	gg	$\tau\tau$	WW*	ZZ*	$\gamma\gamma$	γZ
BR (SM)	57.8%	2.7%	8.6%	6.4%	21.6%	2.7%	0.23%	0.16%
BDT > -0.25	88.90%	89.04%	88.63%	89.12%	88.96%	89.11%	88.91%	88.28%
$M_{\text{rec}} \in [110, 155] \text{ GeV}$	88.25%	88.35%	87.98%	88.43%	88.33%	88.52%	88.21%	87.64%

- $Z \rightarrow qq$: $\delta\text{Efficiency} \sim 15\%$

[Thomson, arXiv:1509.02853]

[Tomita 2015; Miyamoto, arXiv:1311.2248]

Decay mode	$\epsilon_{\mathcal{L}>0.65}^{\text{vis.}}$	$\epsilon_{\mathcal{L}>0.60}^{\text{invis.}}$	$\epsilon^{\text{vis.}} + \epsilon^{\text{invis.}}$
$H \rightarrow \text{invis.}$	$<0.1\%$	23.5%	23.5%
$H \rightarrow q\bar{q}/gg$	22.6%	$<0.1\%$	22.6%
$H \rightarrow WW^*$	22.1%	0.1%	22.2%
$H \rightarrow ZZ^*$	20.6%	1.1%	21.7%
$H \rightarrow \tau^+\tau^-$	25.3%	0.2%	25.5%
$H \rightarrow \gamma\gamma$	25.7%	$<0.1\%$	25.7%
$H \rightarrow Z\gamma$	18.6%	0.3%	18.9%
$H \rightarrow WW^* \rightarrow q\bar{q}q\bar{q}$	20.8%	$<0.1\%$	20.8%
$H \rightarrow WW^* \rightarrow q\bar{q}l\nu$	23.3%	$<0.1\%$	23.3%
$H \rightarrow WW^* \rightarrow q\bar{q}\tau\nu$	23.1%	$<0.1\%$	23.1%
$H \rightarrow WW^* \rightarrow l\nu l\nu$	26.5%	0.1%	26.5%
$H \rightarrow WW^* \rightarrow l\nu\tau\nu$	21.1%	0.5%	21.6%
$H \rightarrow WW^* \rightarrow \tau\nu\tau\nu$	16.3%	2.3%	18.7%

► trash **99%** of those 1M events unless one can improve the bias

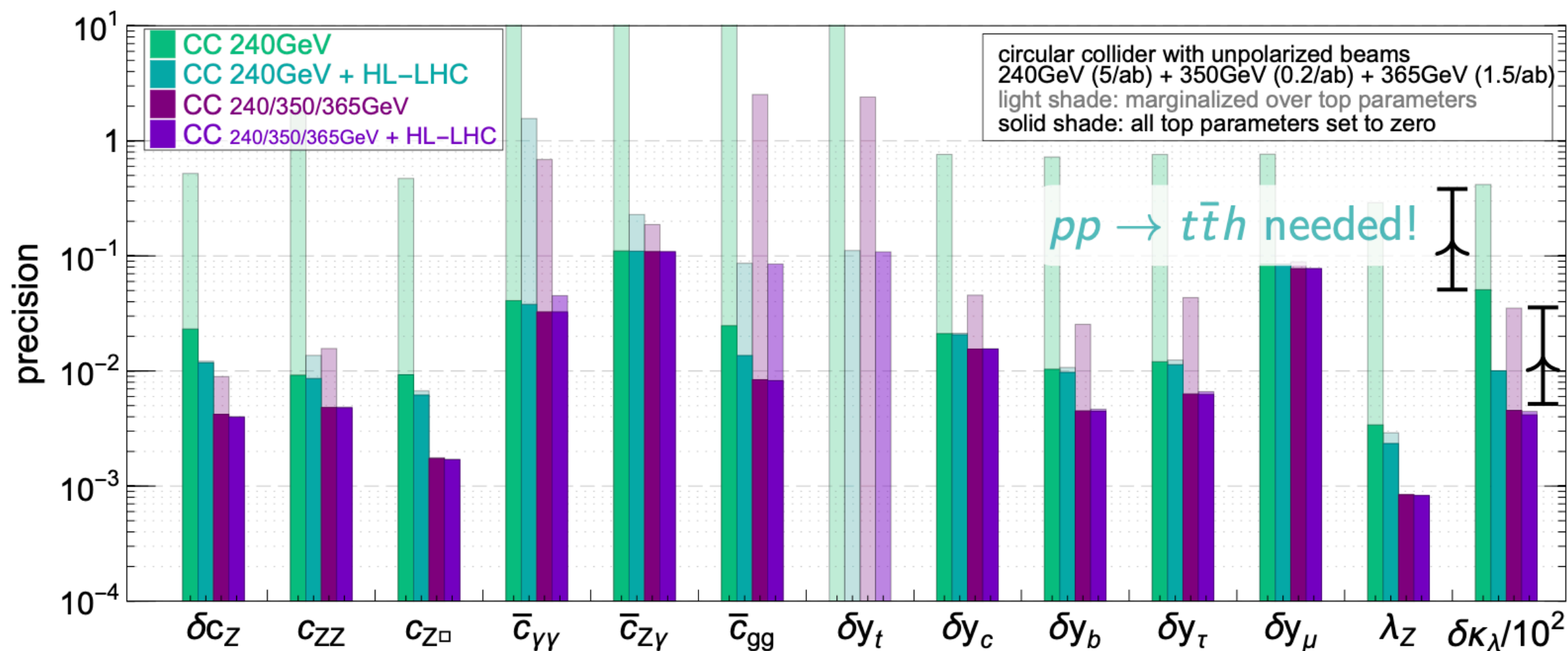
Top and trilinear

[GD, Gu, Vryonidou, Zhang '18]

[see also Jung, Lee, Perelló, Tian, Vos '20]

light shades: 12 Higgs op. floated + 6 top op. floated

dark shades: 12 Higgs op. floated + 6 top op. $\rightarrow 0$



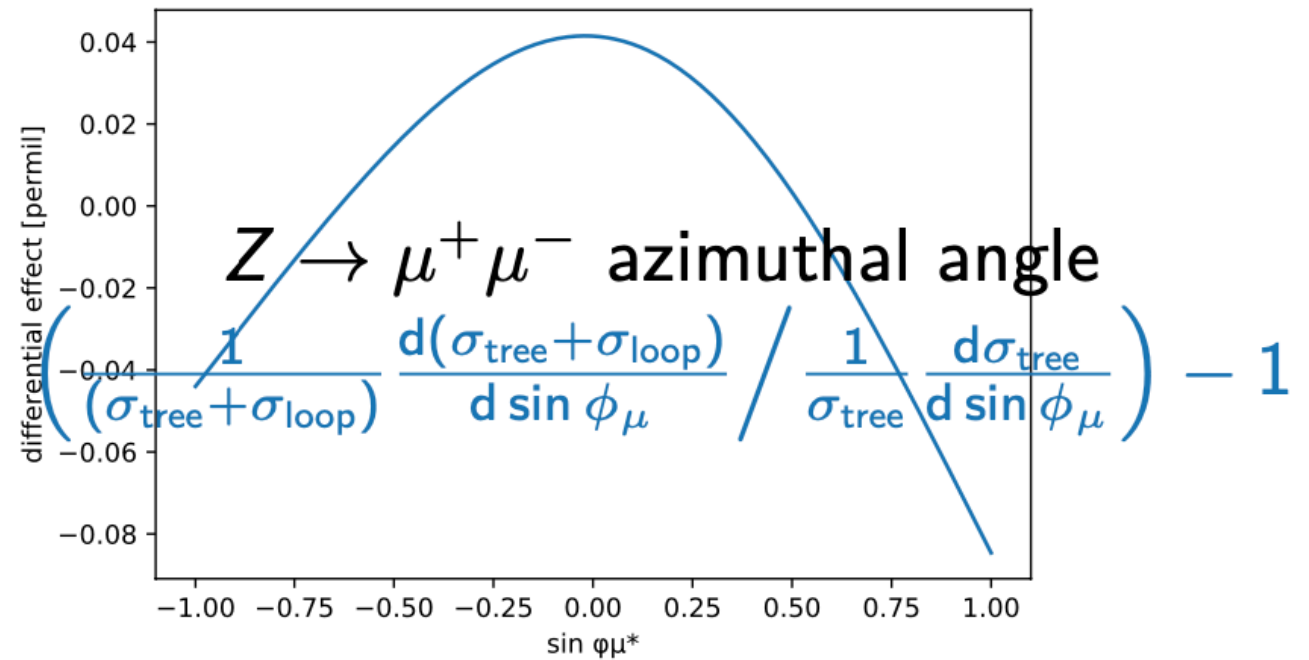
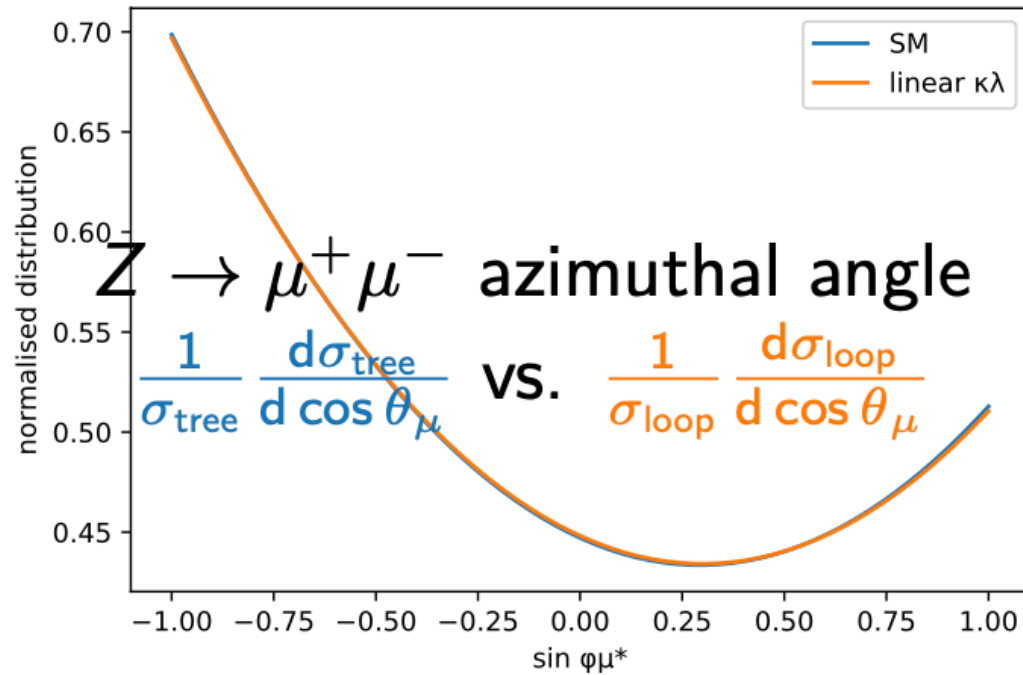
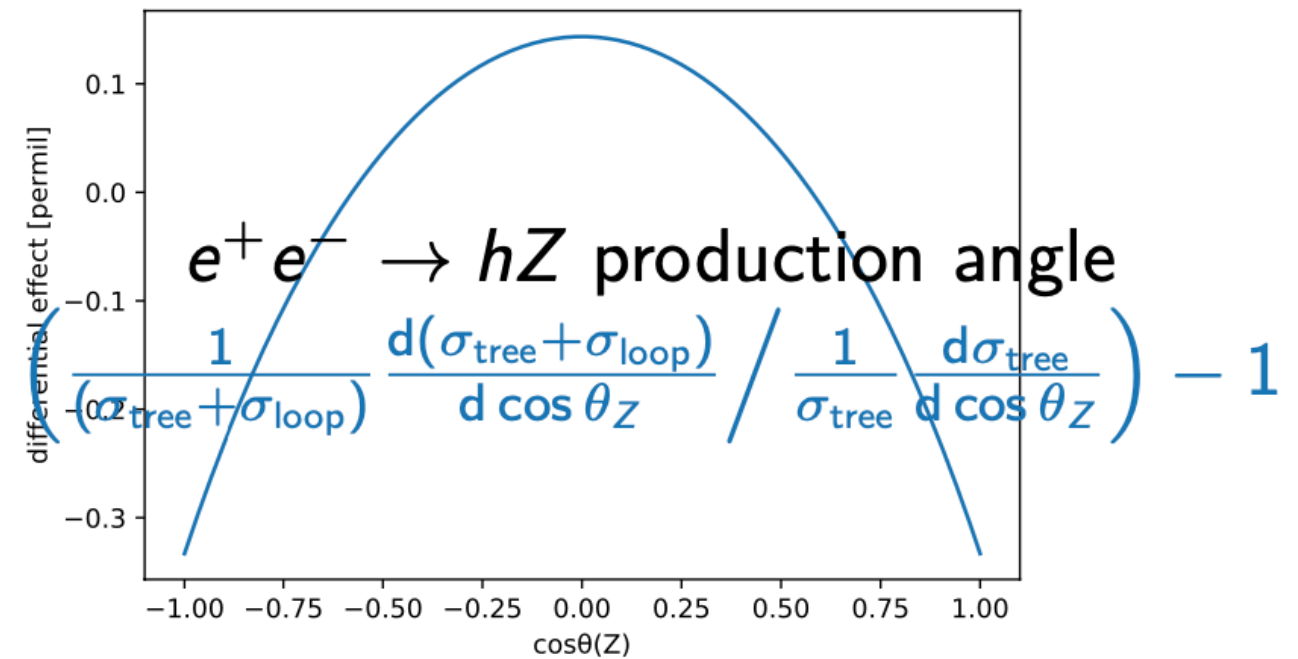
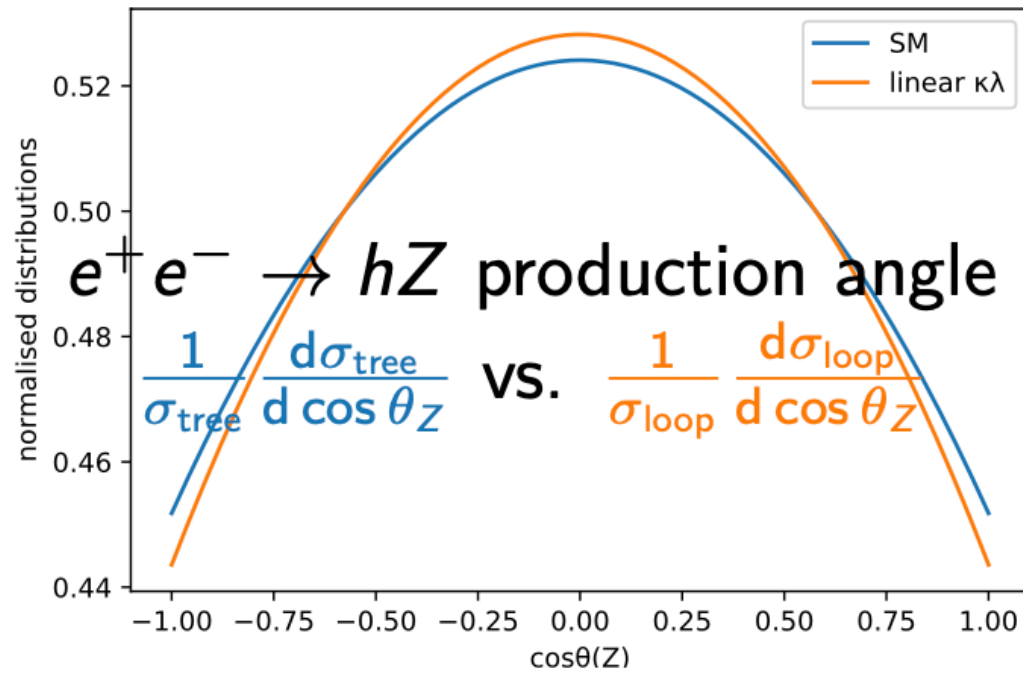
Uncertainties on the top have a big effect on the Higgs

- Higgsstr. run: insufficient
- Higgsstr. run \oplus top@HL-LHC: large top contaminations in $\bar{c}_{\gamma\gamma,gg,Z\gamma,ZZ}$
- Higgsstr. run \oplus $e^+e^- \rightarrow t\bar{t}$: large y_t contaminations in various coefficients
- Higgsstr. run \oplus $e^+e^- \rightarrow t\bar{t} \oplus$ top@HL-LHC: top contam. in \bar{c}_{gg} only

Differential hZ information

[Back-of-the-envelope calculations!!]
and discussions with Fabio Maltoni
& Xiaoran Zhao

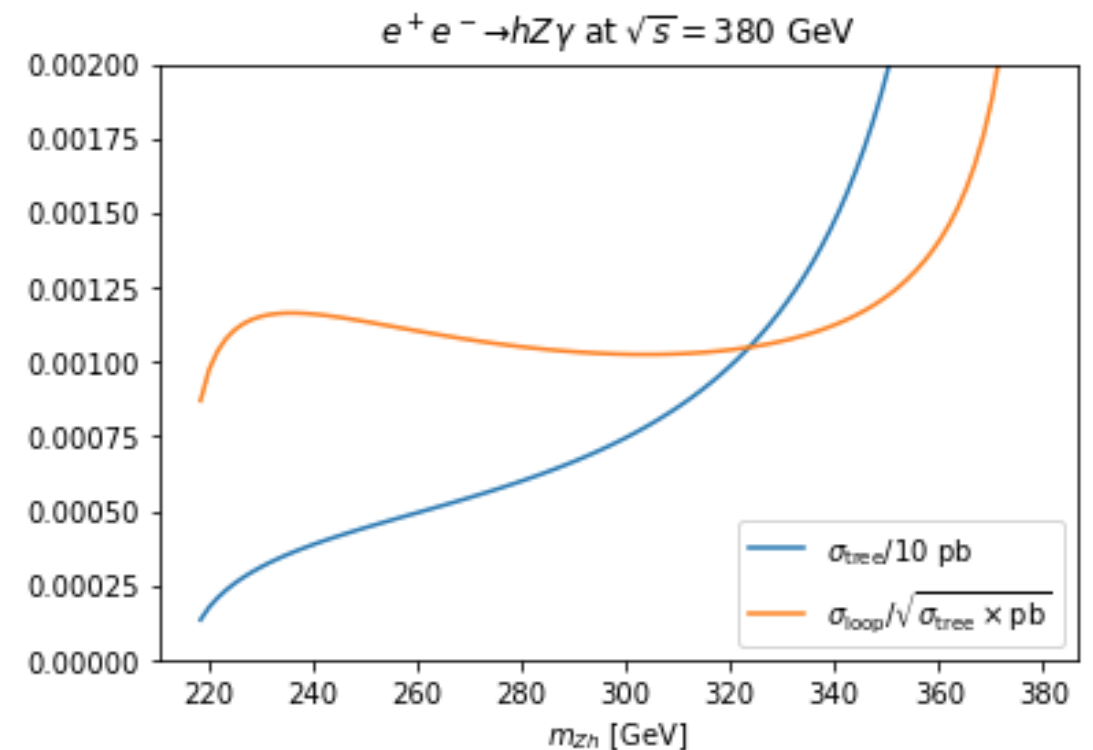
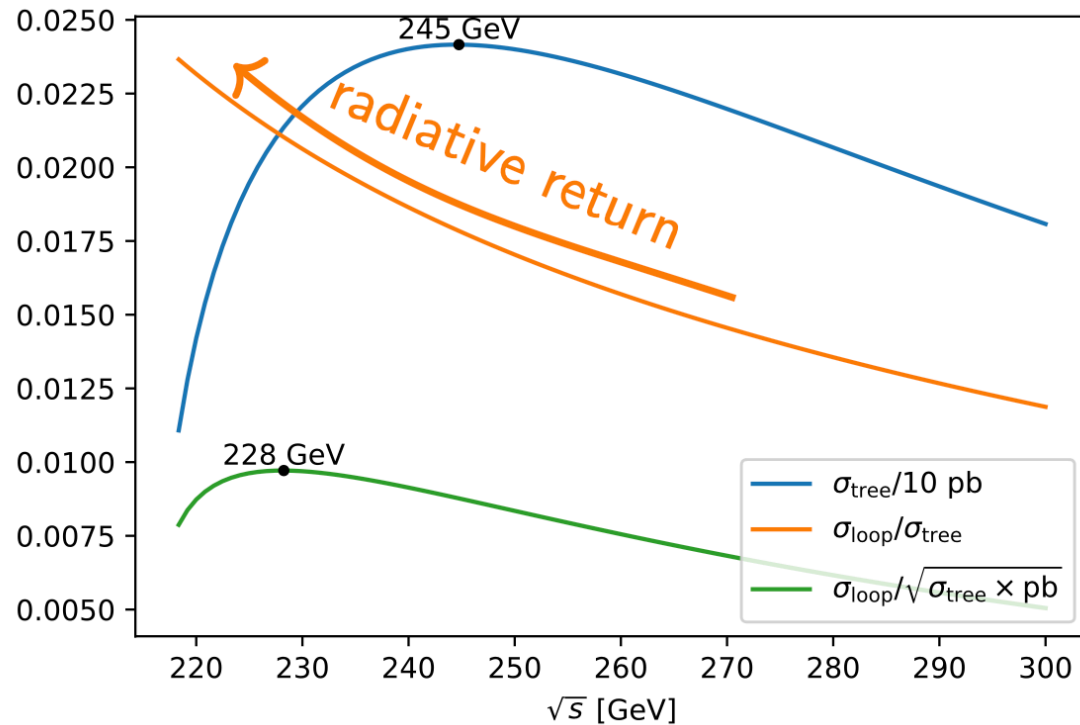
ZZh loop κ_λ vertex: $F_a(p_i^2) (\epsilon_1 \cdot \epsilon_2) + F_b(p_i^2) (p_1 \cdot \epsilon_2)(p_2 \cdot \epsilon_1)$
with $F_b/F_a \sim 10^{-2}$ so only $\lesssim 10^{-4}$ differential effect



¿exploitable with an optimal discriminant?

(ii) single-Higgs: lift degeneracies

- can energy scan around 240-250 help? or using radiative return from 365/380 GeV?

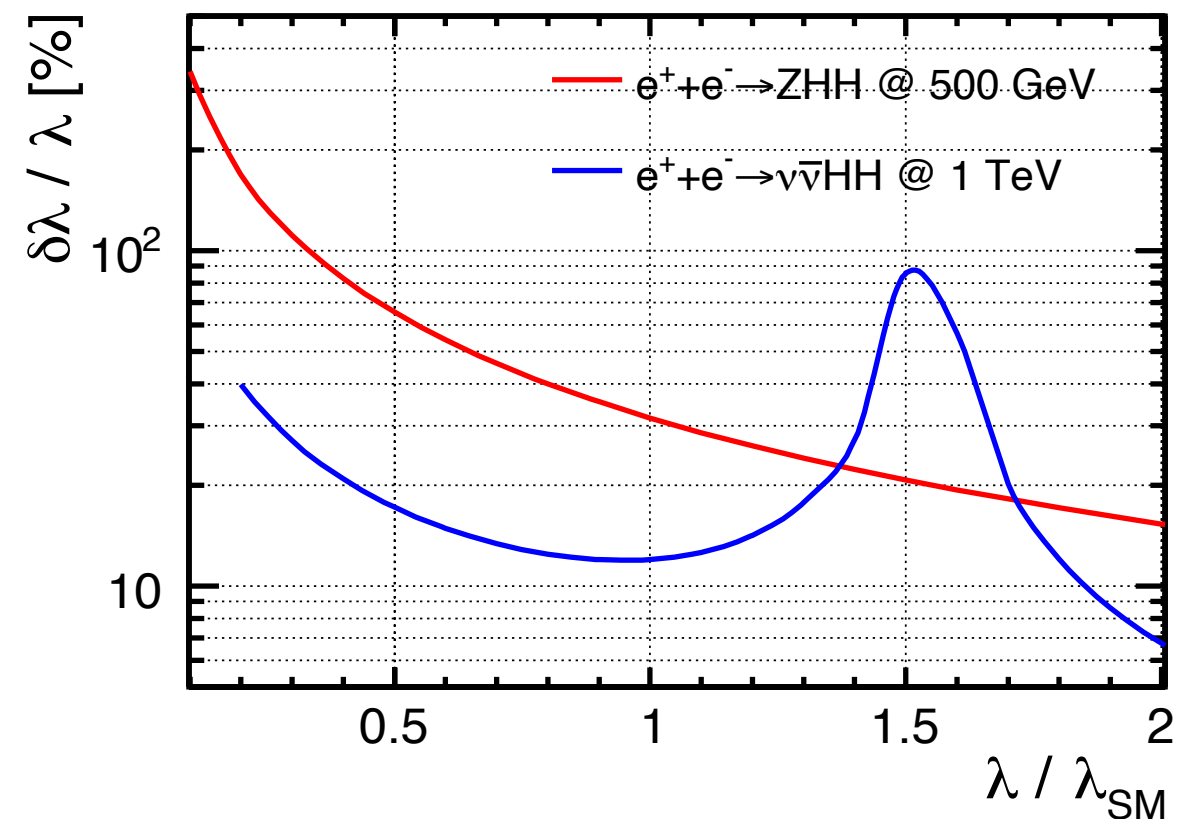
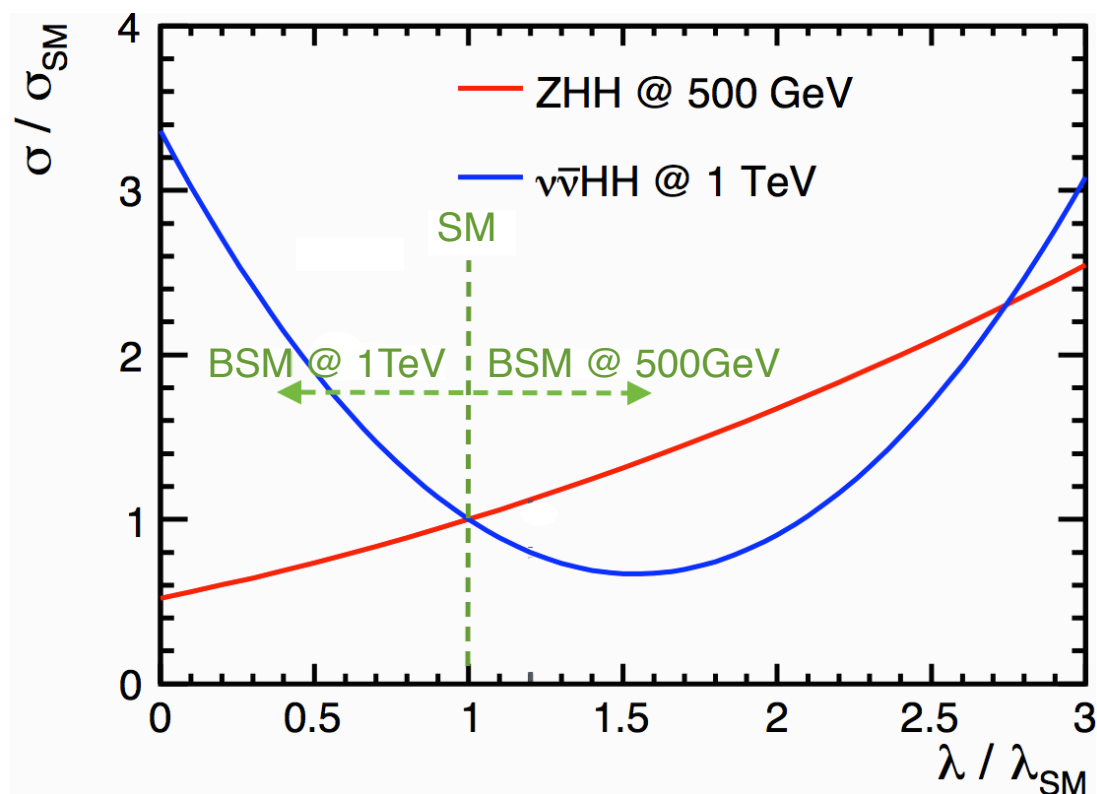


[Durieux, et al, preliminary]

(i) beyond SMEFT: large $\delta\lambda_{hhh}$; light scalars

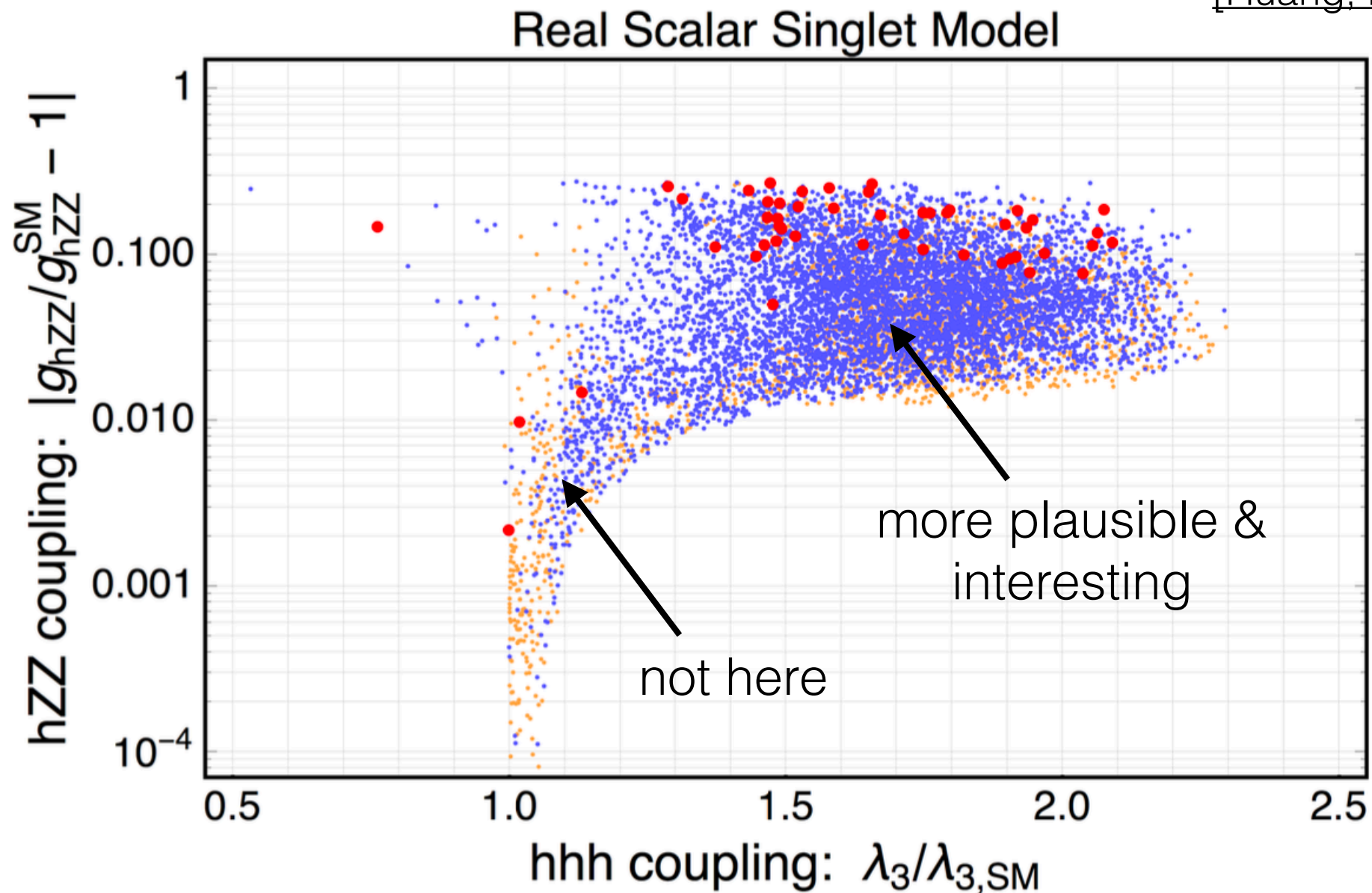
(examples)

- profound effect on di-Higgs processes
- complementarity between ZHH & $\nu\bar{\nu}HH$ (& LHC): different interference
- if $\lambda_{HHH} / \lambda_{SM} = 2$, λ_{HHH} be *discovered* ($\sim 13\%$) using ZHH at 500 GeV e^+e^-



(i) beyond SMEFT: large $\delta\lambda_{hhh}$; light scalars

[Huang, Long, Wang, '16]



orange: first-order phase transition

blue: strongly first-order phase transition ($v/T > 1.3$)

red: very strongly first-order phase transition (GW @ eLISA)

[recent models with even larger hierarchy $\delta_{hhh} / \delta_{hVV}$: [Durieux, McCullough, Salvioni, '22](#)]