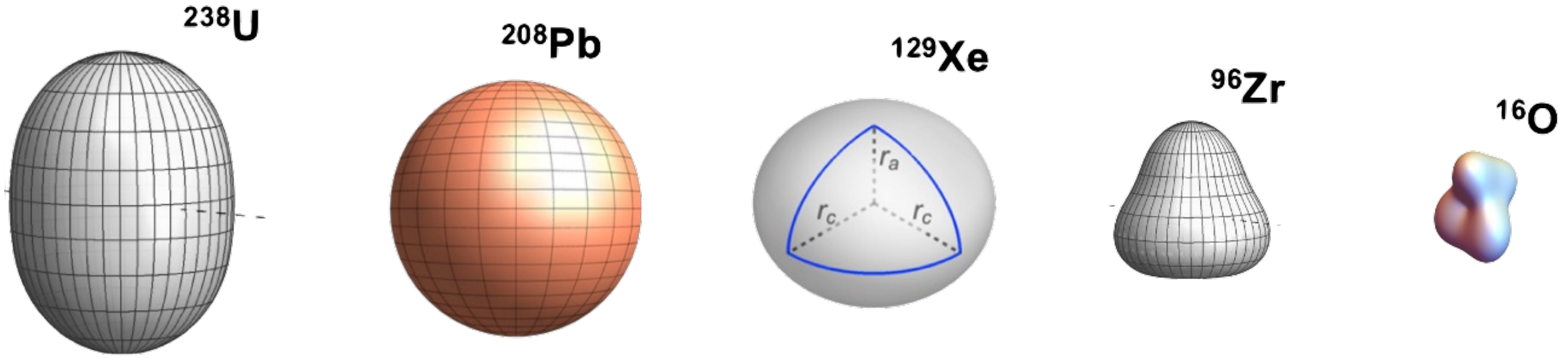
Brookhaven National Laboratory
Office of Science | U.S. Department of Energy

Stony Brook University

Outlook for fluctuations and correlations

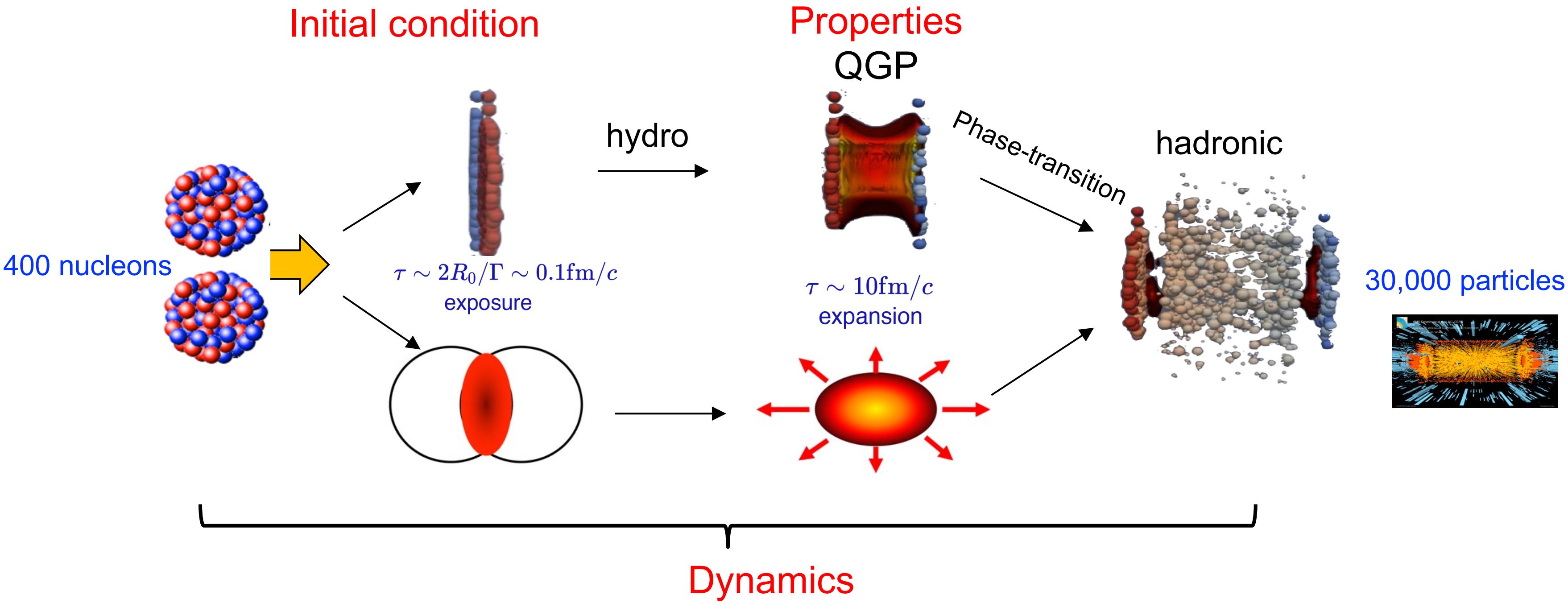
Jiangyong Jia

May 31, 2024



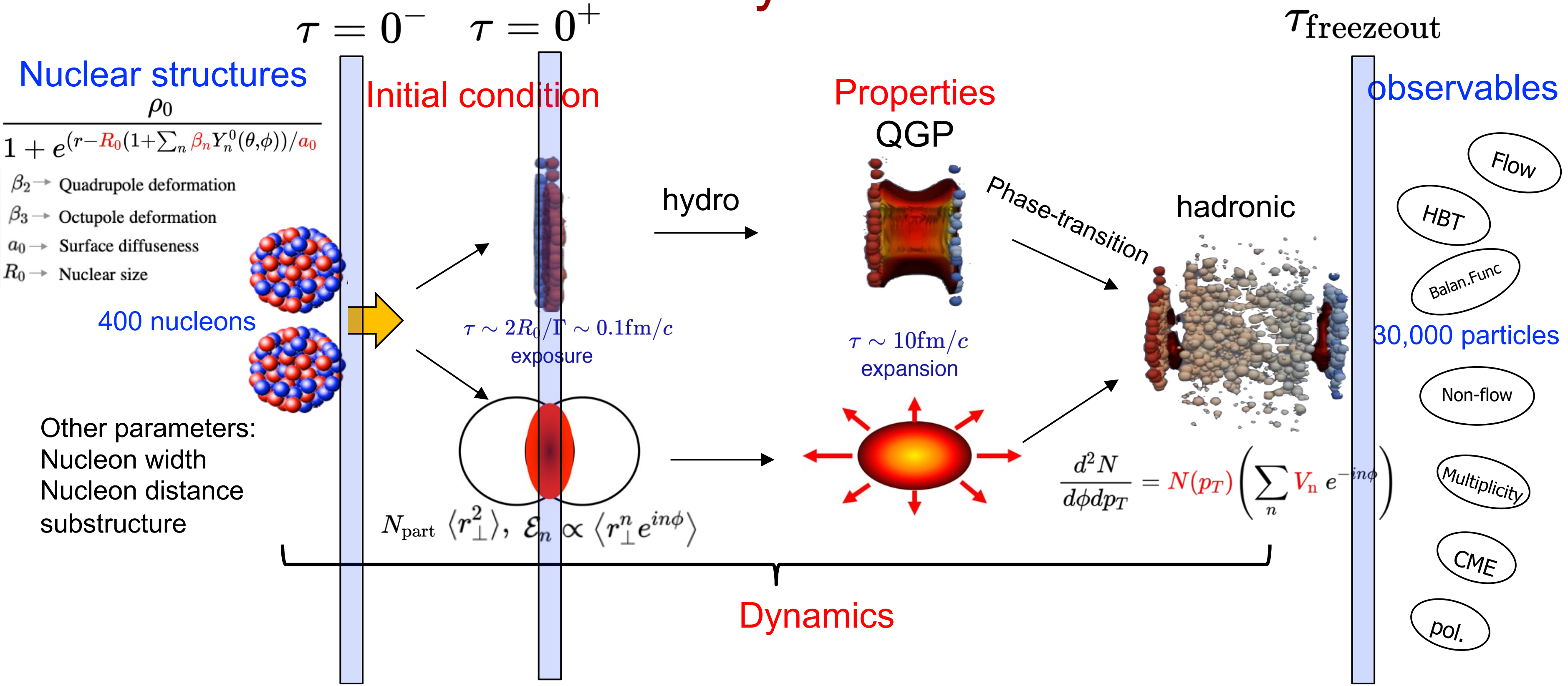
2024 ALICE USA meeting at Yale

Heavy ion collisions



Three pillars of understanding: Properties, Dynamics, Initial condition

Heavy ion collisions



Two snap-shots: Final state particles, Nuclear structures
→Measure more observables or collide more systems

A plethora of observables

- Single particle distribution

Flow vector: $\boldsymbol{V}_n = v_n e^{in\Psi_n}$

$$\frac{d^2N}{d\phi dp_{\mathrm{T}}} = N(p_T)\left[1+2\sum_n v_{\mathrm{n}}(p_T)\cos n(\phi-\Psi_n(p_T))\right]$$

$$= N(p_T)\left[\sum_{n=-\infty}^{\infty} V_{\mathrm{n}}(p_T)e^{in\phi}\right]$$

Radial flow ↗ Anisotropic flow ↖

- Two-particle correlation function

$$\left\langle \frac{d^2N_1}{d\phi dp_{\mathrm{T}}}\frac{d^2N_2}{d\phi dp_{\mathrm{T}}}\right\rangle \Rightarrow \langle \boldsymbol{V}_n(p_{T1})\boldsymbol{V}_n^*(p_{T2})\rangle \quad n-n=0$$

- Multi-particle correlation function

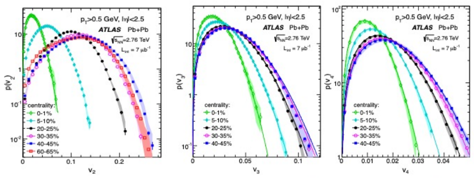
$$\left\langle [p_{\mathrm{T}}]^k \frac{d^2N_1}{d\phi dp_{\mathrm{T}}}\cdots\frac{d^2N_m}{d\phi dp_{\mathrm{T}}}\right\rangle \Rightarrow \langle [p_{\mathrm{T}}]^k \boldsymbol{V}_{n_1}\boldsymbol{V}_{n_2}\ldots\boldsymbol{V}_{n_m}\rangle \quad n_1+n_2+\ldots+n_m=0$$

$$\downarrow$$

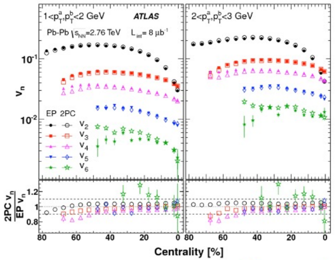
$$p([p_{\mathrm{T}}],\boldsymbol{V}_2,\boldsymbol{V}_3\ldots) = \frac{1}{N_{\mathrm{evts}}}\frac{dN_{\mathrm{evts}}}{d[p_{\mathrm{T}}]d\boldsymbol{V}_2 d\boldsymbol{V}_3\ldots}$$

EbyE fluctuations of initial volume, size and shape

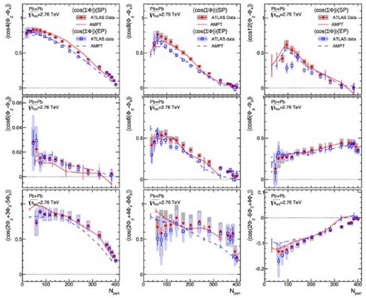
E-by-E flow amplitude distribution $p(v_n)$



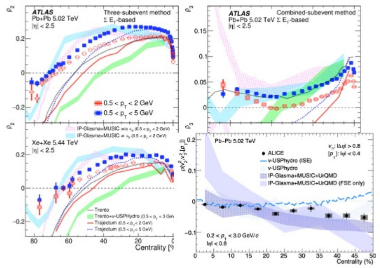
Higher-harmonics v_2-v_6



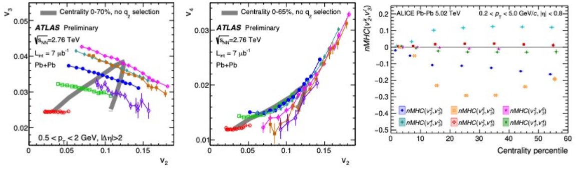
Event-plane correlation $p(\Psi_n,\Psi_m,\Psi_k)$



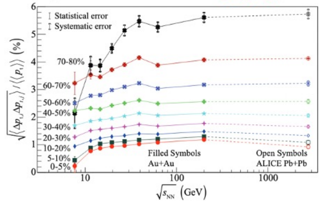
v_n-p_T correlation $p(v_n, p_T)$



v_n amplitude correlation $p(v_n,v_m)$



p_T fluctuations $p(p_T)$



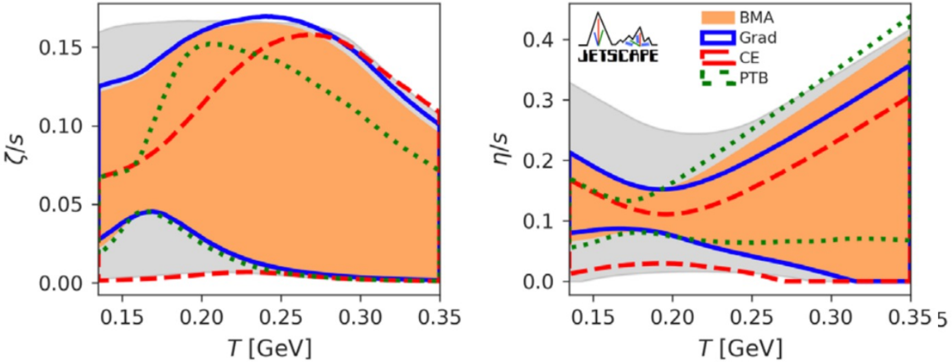
From Weiyao Ke, Jetscape

Uncertainty quantification

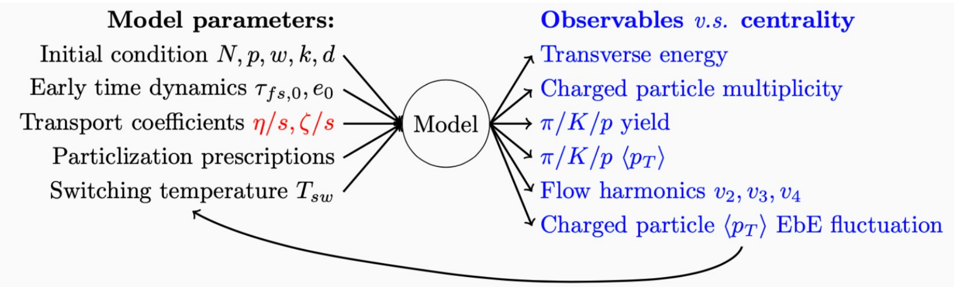
PRL.126.24230

Norm. Pb-Pb 2.76 TeV	N[2.76 TeV]	[10, 20]
Norm. Au-Au 200 GeV	N[0.2 TeV]	[3, 10]
generalized mean	p	[−0.7, 0.7]
nucleon width	w	[0.5, 1.5] fm
min. dist. btw. nucleons	$d^3_{\rm min}$	[0, 1.7^3] fm^3
multiplicity fluctuation	σ_k	[0.3, 2.0]
free-streaming time scale	τ_R	[0.3, 2.0] fm/c
free-streaming energy dep.	α	[−0.3, 0.3]
particlization temperature	$T_{\rm sw}$	[0.135, 0.165] GeV

temperature of (η/s) kink	T_η	[0.13, 0.3] GeV
(η/s) at kink	$(\eta/s)_{\rm kink}$	[0.01, 0.2]
low temp. slope of (η/s)	$a_{\rm low}$	[−2, 1] GeV^{-1}
high temp. slope of (η/s)	$a_{\rm high}$	[−1, 2] GeV^{-1}
shear relaxation time factor	b_π	[2, 8]
maximum of (ζ/s)	$(\zeta/s)_{\max}$	[0.01, 0.25]
temperature of (ζ/s) peak	T_ζ	[0.12, 0.3] GeV
width of (ζ/s) peak	w_ζ	[0.025, 0.15] GeV
asymmetry of (ζ/s) peak	λ_ζ	[−0.8, 0.8]



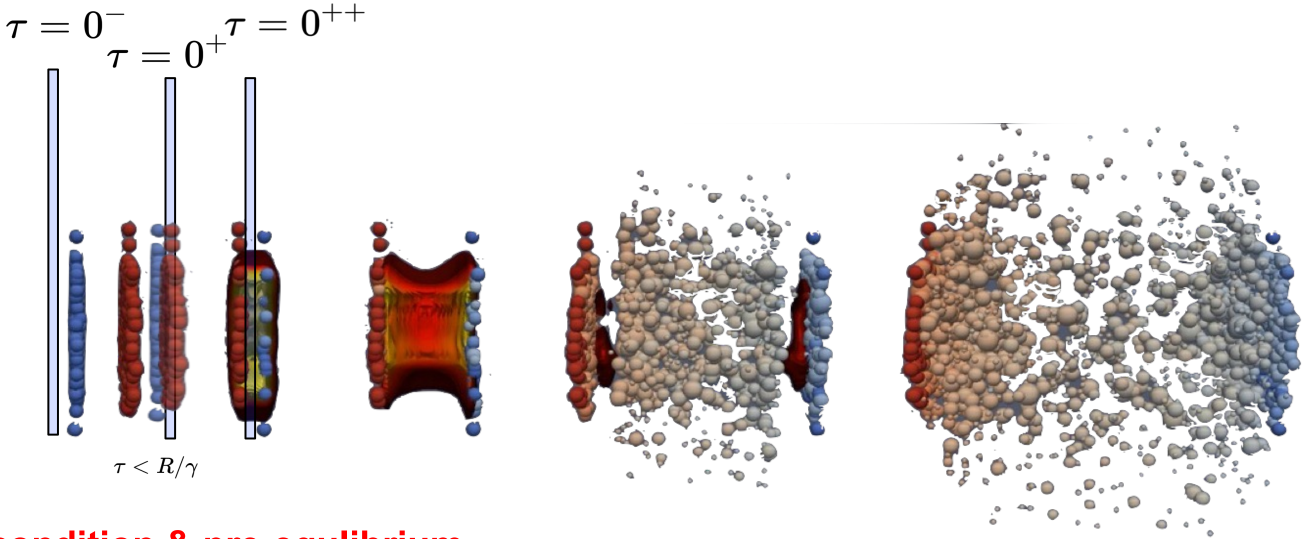
Only a subset of observables are used



- Extraction of QGP properties is limited by the initial condition
- At this moment, more observables do not necessarily improve the situation.

Isolating the impact of initial condition

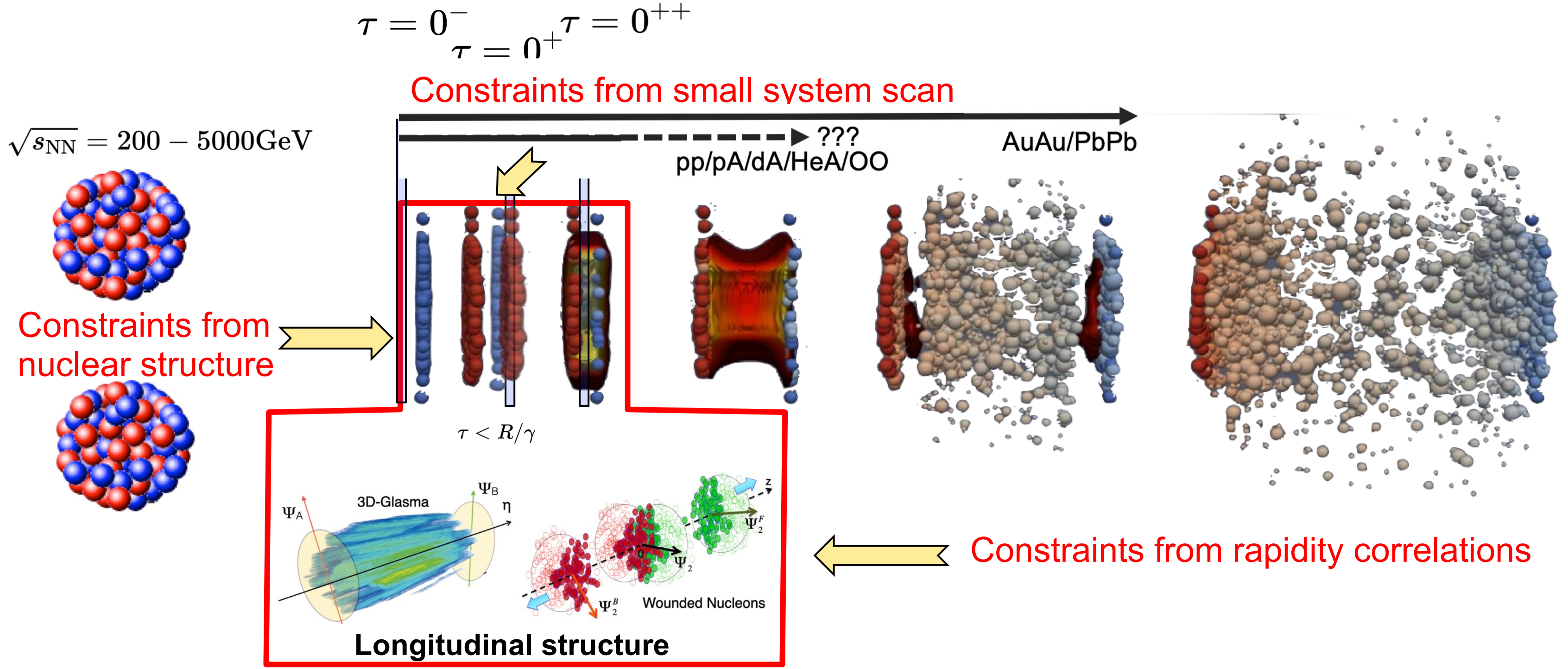
$\sqrt{s_{\rm NN}} = 200 - 5000 \mathrm{GeV}$



Initial condition & pre-equlibrium

What is the nature of quantum fluctuations?
How is the energy deposited?
What are the DoFs?
How does the system hydrodynamize/thermalize? timescales?

Isolating the impact of initial condition

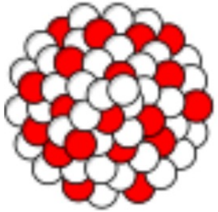


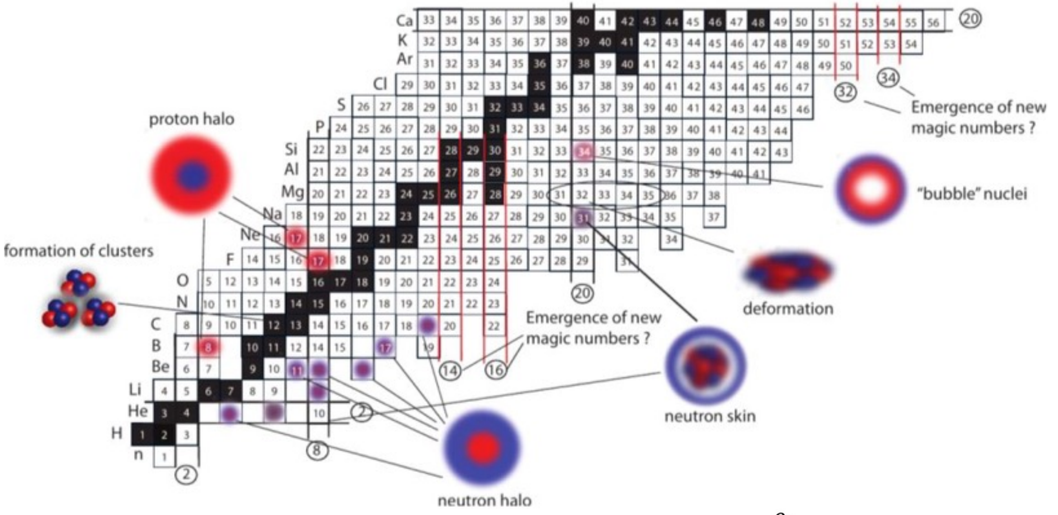
What is the nature of quantum fluctuations?
How is the energy deposited?
What are the DoFs?
How does the system hydrodynamize/thermalize? timescales?

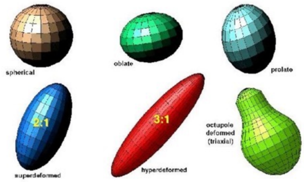
Three experimental approaches:

- Explore nuclear structure
- Longitudinal correlation
- Small system scan

Constraints from nuclear structure





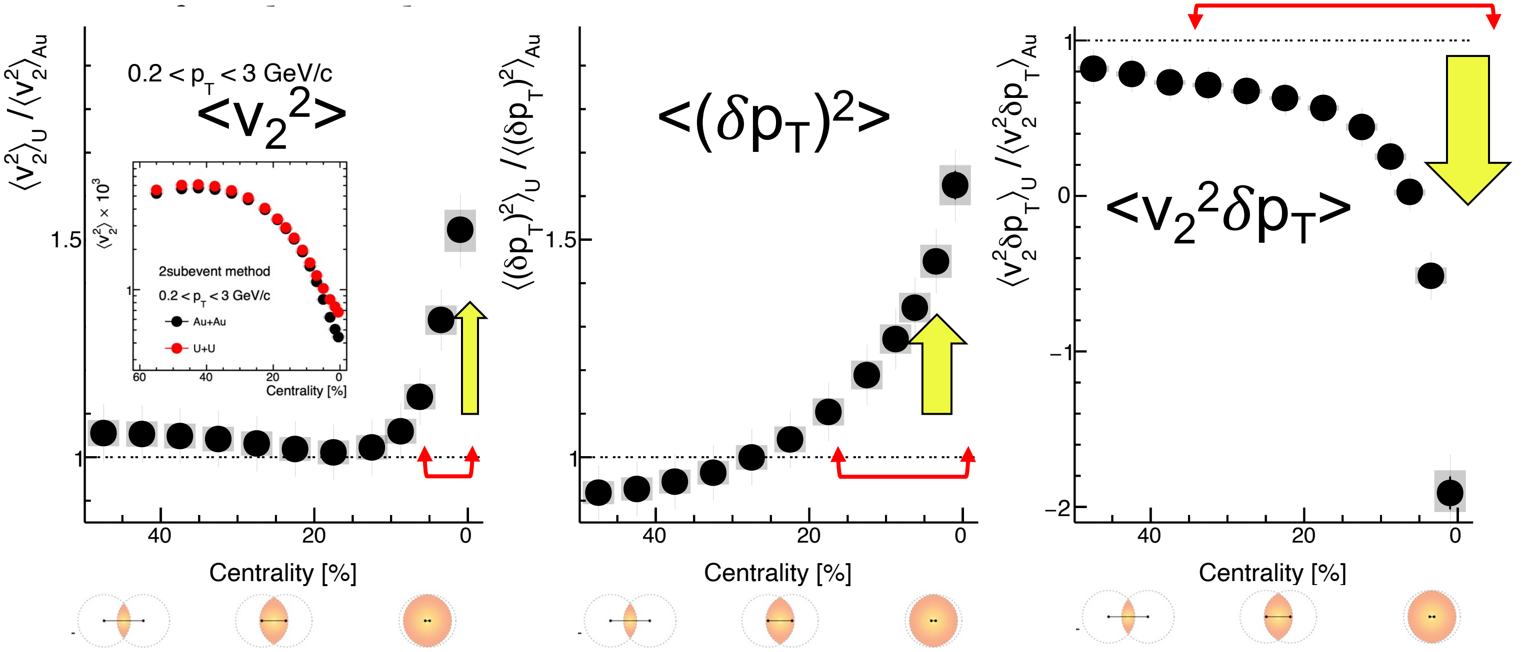


$$\rho(r,\theta,\phi) = \frac{\rho_0}{1 + e^{(r - R(\theta,\phi))/a_0}}$$

$$R(\theta,\phi) = R_0(1 + \beta_2[\cos\gamma Y_{2,0}(\theta,\phi) + \sin\gamma Y_{2,2}(\theta,\phi)] + \beta_3 Y_{3,0}(\theta,\phi) + \beta_4 Y_{4,0}(\theta,\phi))$$

Image U shape via Isobar-like U+U vs Au+Au collisions

$R_{\mathcal{O}} = \langle\mathcal{O}\rangle_{U+U} / \langle\mathcal{O}\rangle_{Au+Au}$ →Insensitive to final state parameters



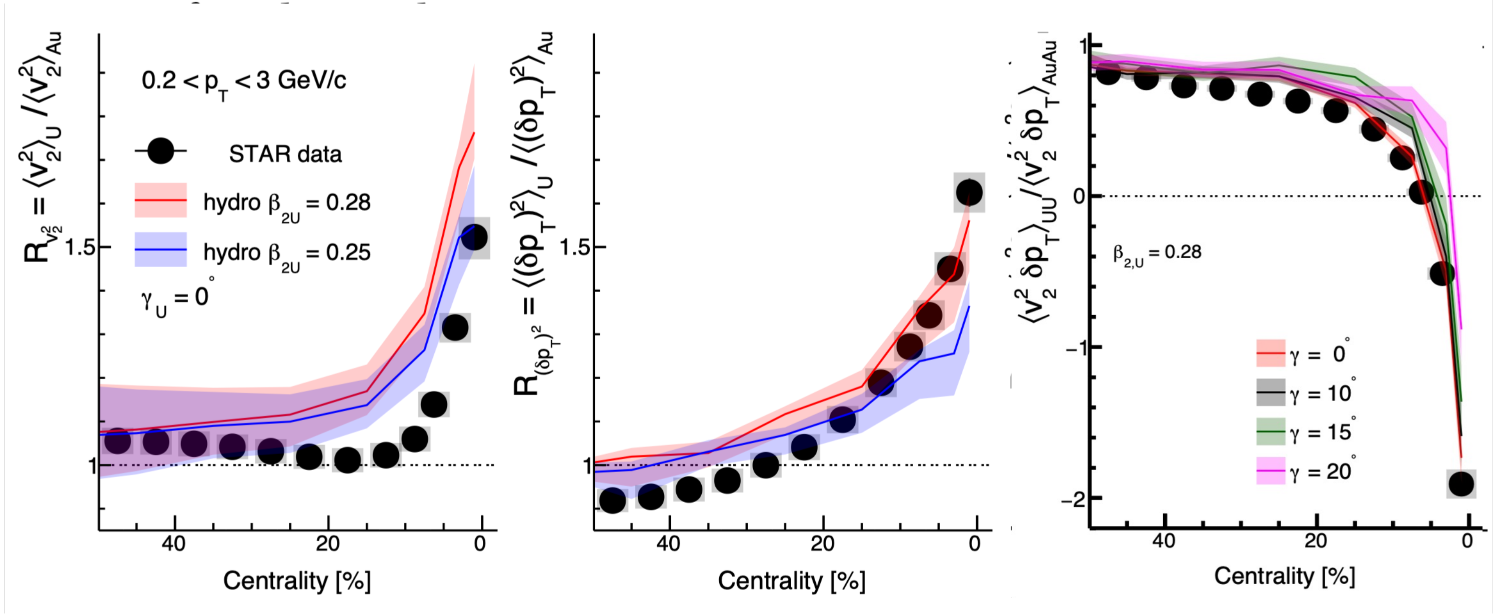
U deformation dominates the ultra-central collisions

→50%-70% modification on $<v_2^2>$ and $<(\delta p_T)^2>$, 300% for $<v_2^2\delta p_T>$

Image U shape via Isobar-like U+U vs Au+Au collisions

2401.06625,submitted to Nature

$R_{\mathcal{O}} = \langle \mathcal{O} \rangle_{U+U} / \langle \mathcal{O} \rangle_{Au+Au}$ →Insensitive to final state parameters



Reasonable agreement with IPGlasma+Music+UrQMD hydro model 2005.14682

Constraints from $\langle \delta p_T^2 \rangle$ and v_2-p_T : $\beta_{2U} = 0.297 \pm 0.013$ $\gamma_U = 8.6° \pm 4.8°$

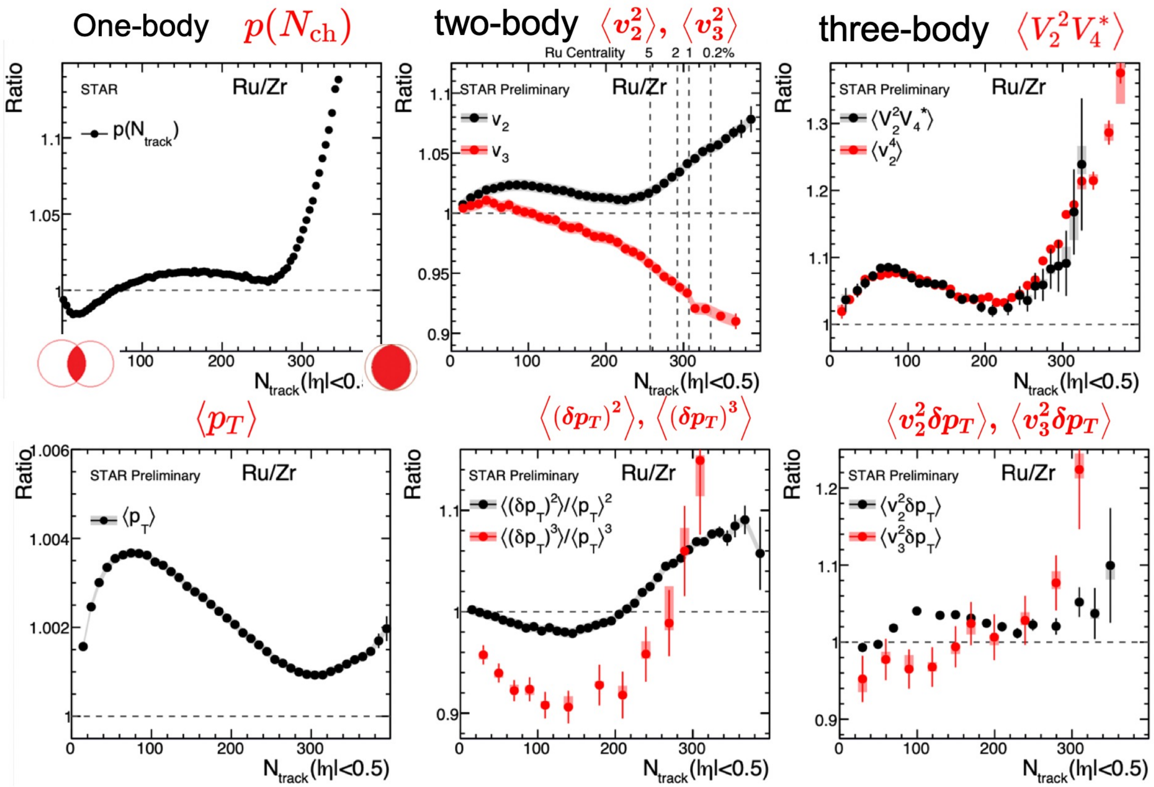
Isobar ^{96}Ru+^{96}Ru and ^{96}Zr+^{96}Zr collisions at RHIC 200 GeV

$$R_{\mathcal{O}} \equiv \frac{\mathcal{O}_{\mathrm{Ru}}}{\mathcal{O}_{\mathrm{Zr}}}$$

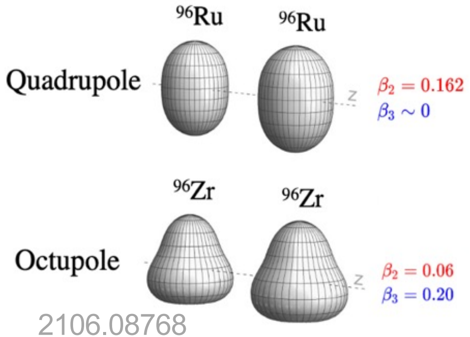
- Insensitive to parameters in the final state
- Deviation from one reflects differences in nuclear structure

Structure influences everywhere

Nuclear structure is inherently part of Heavy ion problem



Nuclear structure via v_2-ratio and v_3-ratio

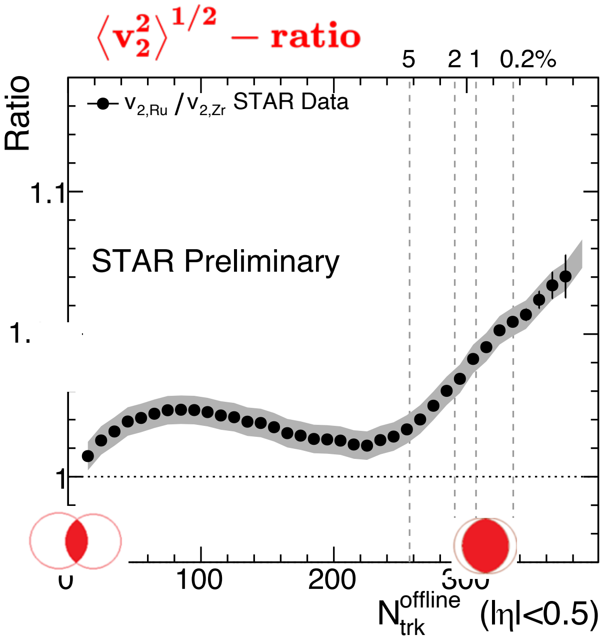


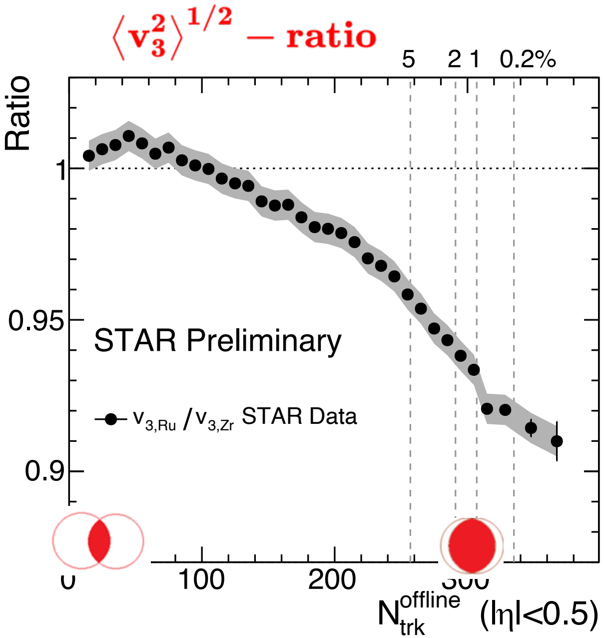
2106.08768

Species	β_2	β_3	a_0	R_0
Ru	0.162	0	0.46 fm	5.09 fm
Zr	0.06	0.20	0.52 fm	5.02 fm
difference	$\Delta\beta_2^2$	$\Delta\beta_3^2$	Δa_0	ΔR_0
	0.0226	-0.04	-0.06 fm	0.07 fm

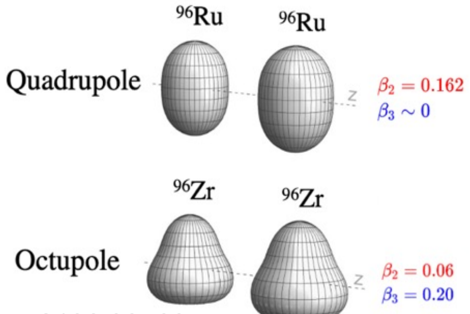
$$R_{\mathcal{O}} \equiv \frac{\mathcal{O}_{\mathrm{Ru}}}{\mathcal{O}_{\mathrm{Zr}}} \approx 1 + c_1 \Delta\beta_2^2 + c_2 \Delta\beta_3^2 + c_3 \Delta R_0 + c_4 \Delta a$$

Simultaneously constrain four structure parameters





Nuclear structure via v_2-ratio and v_3-ratio



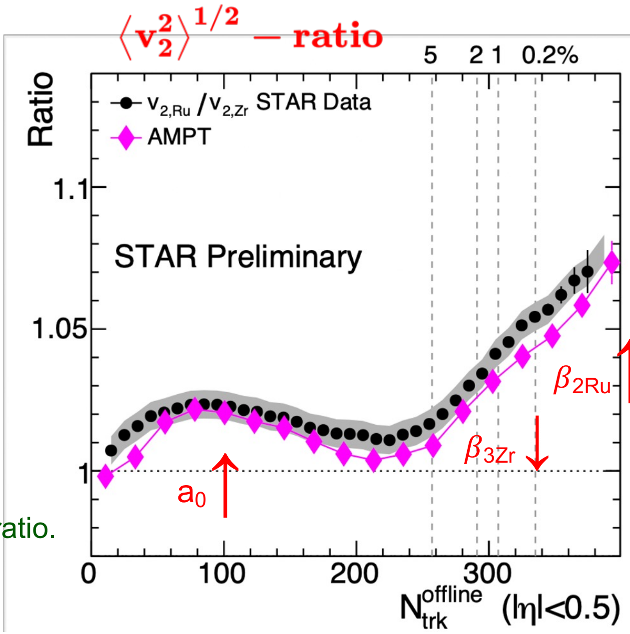
2106.08768

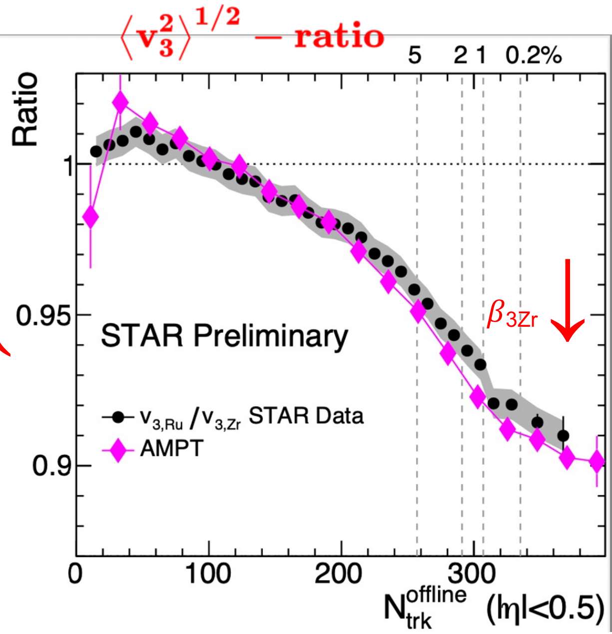
$$R_{\mathcal{O}} \equiv \frac{\mathcal{O}_{\mathrm{Ru}}}{\mathcal{O}_{\mathrm{Zr}}} \approx 1 + c_1 \Delta\beta_2^2 + c_2 \Delta\beta_3^2 + c_3 \Delta R_0 + c_4 \Delta a$$

Simultaneously constrain four structure parameters

Species	β_2	β_3	a_0	R_0
Ru	0.162	0	0.46 fm	5.09 fm
Zr	0.06	0.20	0.52 fm	5.02 fm
difference	$\Delta\beta_2^2$	$\Delta\beta_3^2$	Δa_0	ΔR_0
	0.0226	-0.04	-0.06 fm	0.07 fm

- $\beta_{2\mathrm{Ru}} \sim 0.16$ increase v_2, no influence on v_3 ratio
- $\beta_{3\mathrm{Zr}} \sim 0.2$ decrease v_2 and v_3 ratio
- $\Delta a_0 = -0.06$ fm increase v_2 mid-central,
- Radius $\Delta R_0 = 0.07$ fm slightly affects v_2 and v_3 ratio.





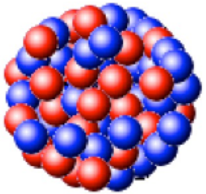
Isobar ratio constraints on the initial condition

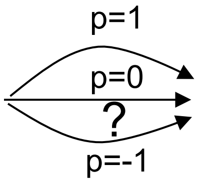
Nucleus

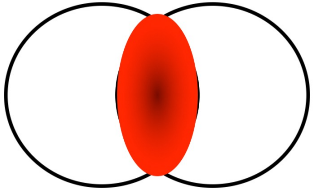
$$T \propto \left(\frac{T_A^p + T_B^p}{2}\right)^{1/p}$$

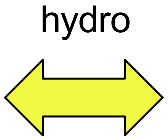
Initial condition

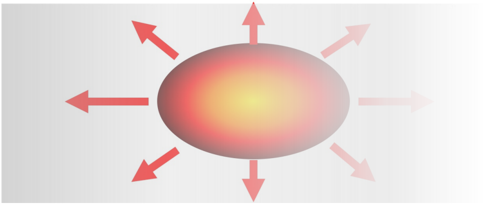
Final state



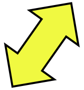






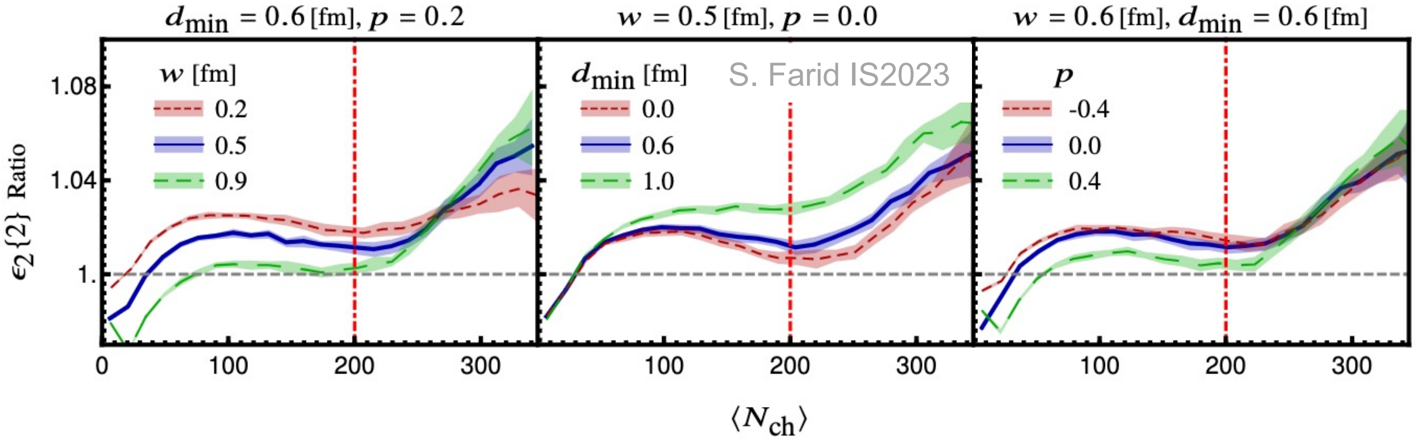


$$T_A(x,y) = \int \rho(x,y,z)dz$$



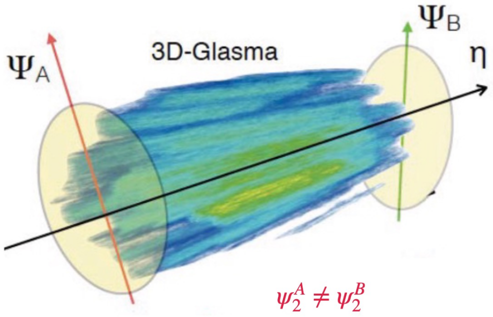
$$\frac{\mathcal{O}_{\mathrm{Ru}}}{\mathcal{O}_{\mathrm{Zr}}} \approx 1 + c_1\Delta\beta_2^2 + c_2\Delta\beta_3^2 + c_3\Delta R_0 + c_4\Delta a$$

c_n relates nuclear structure and initial condition

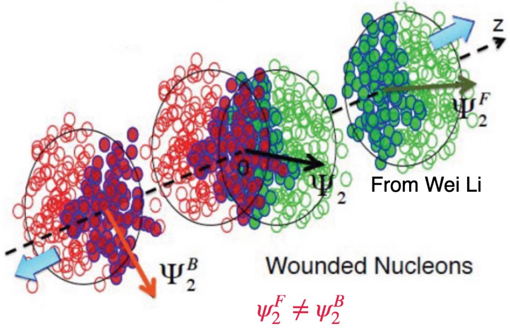


Longitudinal structure

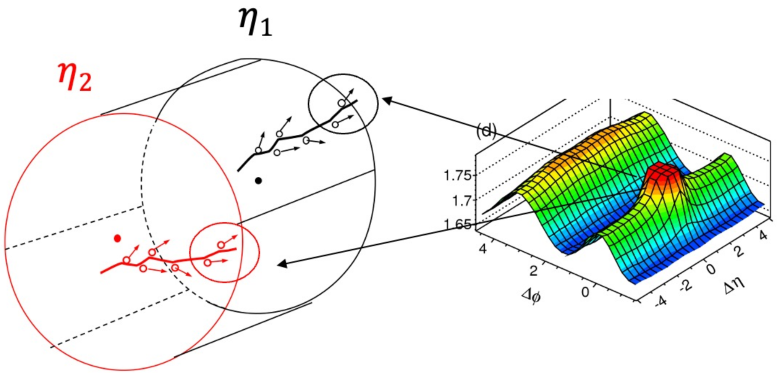
- Sensitive to stopping and entropy production mechanism
- Varying the timescales $\tau \sim e^{-\Delta\eta}$
- Short-range structure sensitive to hydrodynamization (also non-flow)



Bjorn Schenke, Soren Schlichting
Phys. Rev. C 94 (2016) 4, 044907

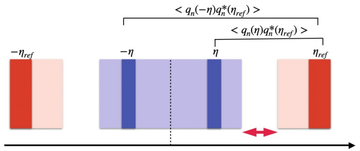


Jiangyong Jia, Peng Huo
Phys. Rev. C 90 (2014) 034905



Long-range sees geometry, short-range sees microscopic origin of collectivity

Traditional observables are insufficient, e.g.



$$r_2(\eta)_{\eta_{\rm ref}} = \frac{\langle V_2(-\eta) V_2^*(\eta_{\rm ref})\rangle}{\langle V_2(\eta) V_2^*(\eta_{\rm ref})\rangle} \equiv \frac{R(-\eta, \eta_{\rm ref})}{R(\eta, \eta_{\rm ref})}$$

Decorrelation is non-linear!!

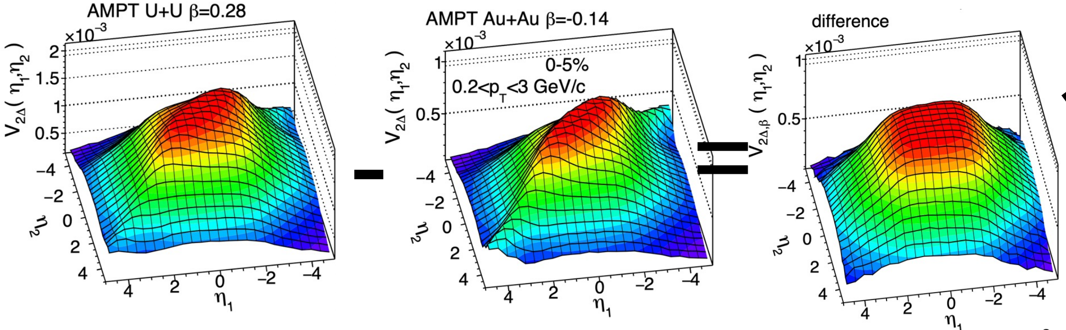
We want: $$R(\eta_1, \eta_2) = \frac{\langle V_2(\eta_1) V_2^*(\eta_2)\rangle}{\sqrt{\langle V_2(\eta_1) V_2^*(\eta_1)\rangle \langle V_2(\eta_2) V_2^*(\eta_2)\rangle}}$$

How to deal with non-flow?

Deformation-assisted study of longitudinal structure

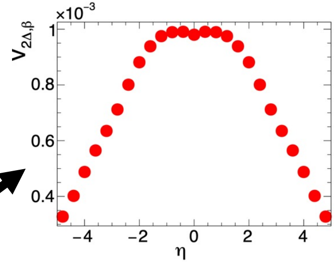
2405.08749

$$V_{2\Delta} = V_{2\Delta,\mathrm{sp}} + V_{2\Delta,\beta} + \delta_{\mathrm{nf}} \qquad V_{2\Delta}(\eta_1,\eta_2) = \langle V_2(\eta_1)V_2^*(\eta_2)\rangle$$



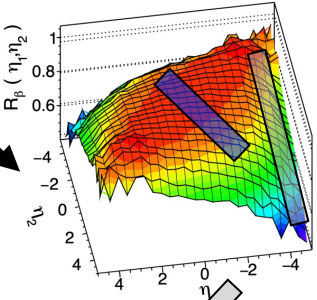
$V_{2\Delta,\mathrm{sp}} + V_{2\Delta,\beta} + \delta_{\mathrm{nf}}$ $\quad$ $V_{2\Delta,\mathrm{sp}} + \delta_{\mathrm{nf}}$ $\quad$ $V_{2\Delta,\beta} = b(\eta_1,\eta_2)\beta^2$

Isolate the decorrelation map of deformation-induced flow



η dependence of flow

$$V_{2\Delta,\beta}(\eta,\eta) = \langle v_{2,\beta}^2(\eta)\rangle$$

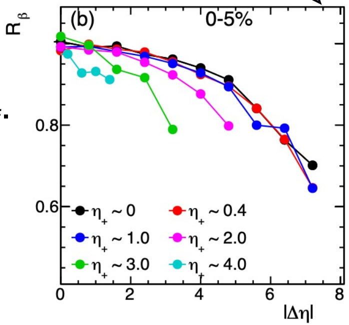


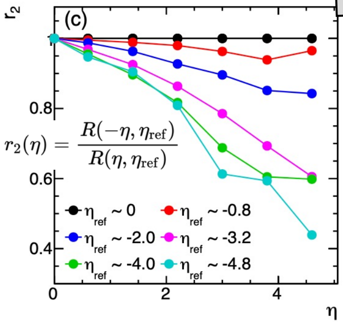
Decorrelation of flow

$$R_\beta(\eta_1,\eta_2)$$

Projection in off-diagonal direction
Decorrelation stronger in forward η_{ref}.

Longitudinal structure is non-linear and not factorizable





Projection in slices→normal r_2.
Decorrelation depends on η_{ref}.

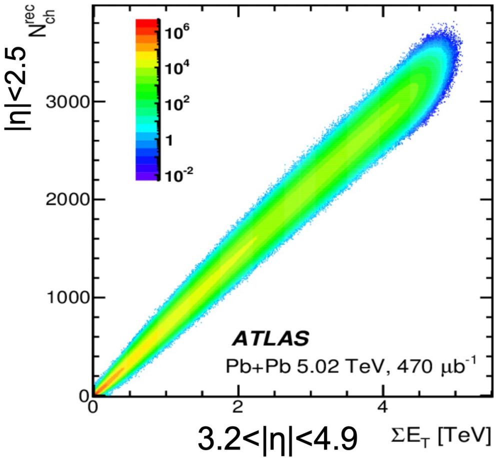
Can not be interpreted as decor between $-\eta$ and η

Observables for long-range collectivity

- n^{th}-order long-range correlations are azimuthal flow harmonics v_n.
  - Most studies of collectivity use this, in particular small system.

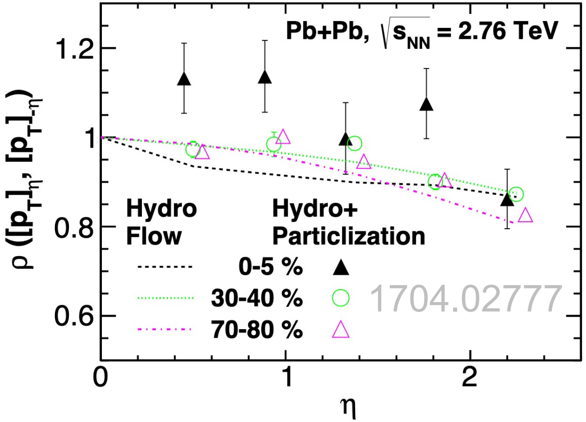
- 0^{th}-order long-range correlation is energy/multiplicity
  - Such correlation comes from boost invariance of initial condition. Does not require final state effects

- 1^{st}-order long-range correlation is $\langle p_T \rangle$ or radial flow.



$$\frac{\langle N(\eta_1)N(\eta_2)\rangle}{\langle N(\eta_1)\rangle\langle N(\eta_2)\rangle}$$

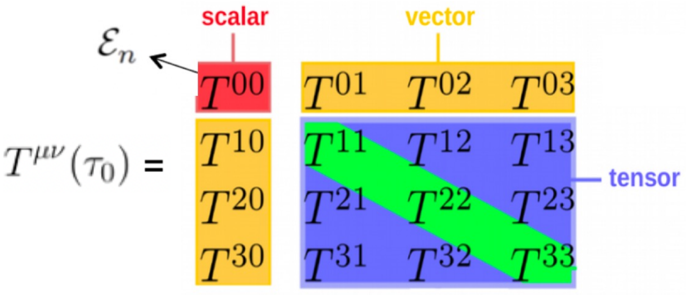
$$\frac{\langle \delta p_{\mathrm{T}}(\eta_1)\delta p_{\mathrm{T}}(\eta_2)\rangle}{\sqrt{\left\langle(\delta p_{\mathrm{T}})^2\right\rangle_{\eta_1}\left\langle(\delta p_{\mathrm{T}})^2\right\rangle_{\eta_2}}}$$



Small system scan

Why small systems

- Need to consider full energy-momentum tensor $T_{\mu\nu}(\tau = 0)$ for the initial condition



[Sousa, Luzum, Noronha, 2002.12735]

SCALAR

$$\mathcal{E}_2 = \frac{\langle x^2 - y^2\rangle + i\langle 2xy\rangle}{\langle x^2 + y^2\rangle}$$ ⟵ Initial eccentricity

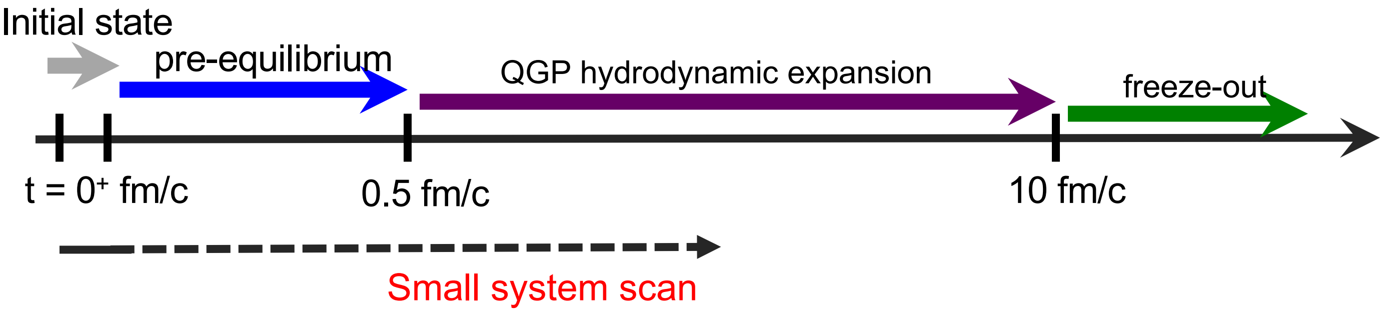
TENSOR

$$\mathcal{E}_p \equiv \frac{\langle T^{xx} - T^{yy}\rangle + i\langle 2T^{xy}\rangle}{\langle T^{xx} + T^{yy}\rangle}$$ ⟵ Initial momentum anisotropy

2405.13600

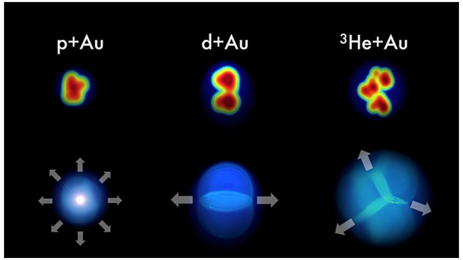
$$\mathcal{E}_n = -\frac{\int_{\vec{x}_\perp} \rho(\vec{x}_\perp)\vec{x}_\perp^{\,n}}{\int_{\vec{x}_\perp} \rho(\vec{x}_\perp)|\vec{x}_\perp|^n} \qquad \rho(\vec{x}_\perp) = T^{\tau\tau}(\vec{x}_\perp) - \alpha\partial_i T^{\tau i}(\vec{x}_\perp) + \beta\partial_i\partial_j T^{ij}(\vec{x}_\perp)$$

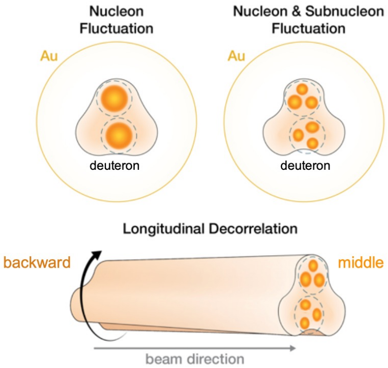
- Interplay of different sources holds key to hydrodynamization and its timescales

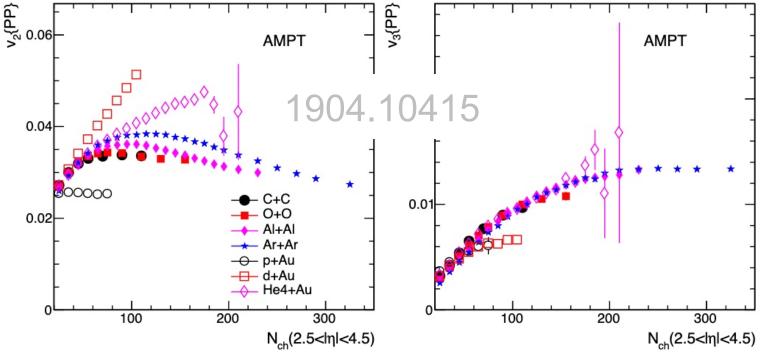


Disentangle sources of collectivities

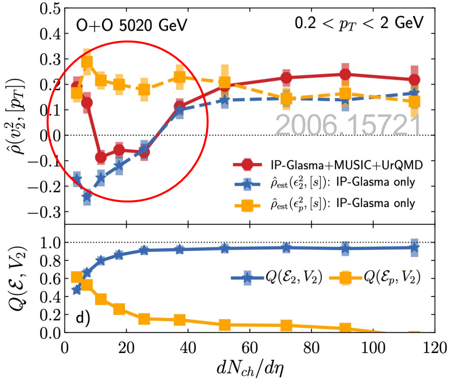
Identifying the geometry response via geometry scan

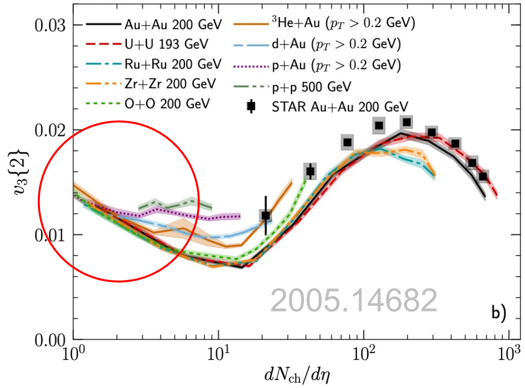






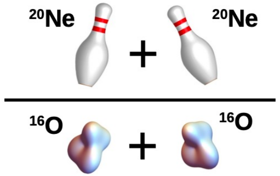
Quantify the fraction of each component



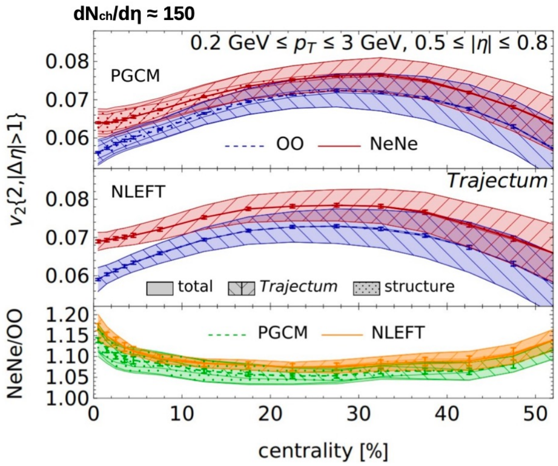


Small system scan

Design isobar collisions with drastically different geometry



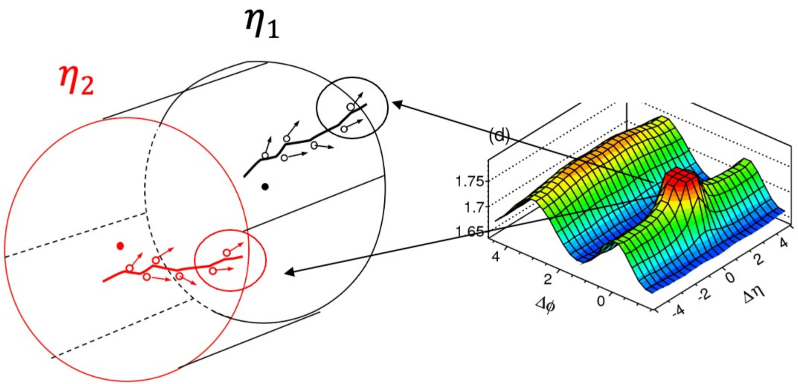
2402.05995



$$\frac{v_2\{2\}_{\mathrm{NeNe}}}{v_2\{2\}_{\mathrm{OO}}} = \begin{cases} 1.170(8)_{\mathrm{stat.}}(30)^{\mathrm{Traj.}}_{\mathrm{syst.}}(0)^{\mathrm{str.}}_{\mathrm{syst.}} & \mathrm{(NLEFT)} \\ 1.139(6)_{\mathrm{stat.}}(27)^{\mathrm{Traj.}}_{\mathrm{syst.}}(28)^{\mathrm{str.}}_{\mathrm{syst.}} & \mathrm{(PGCM)}, \end{cases}$$

QGP's rapidity structures by comparing symmetric vs asymmetric systems

Decorrelation should be different from large systems

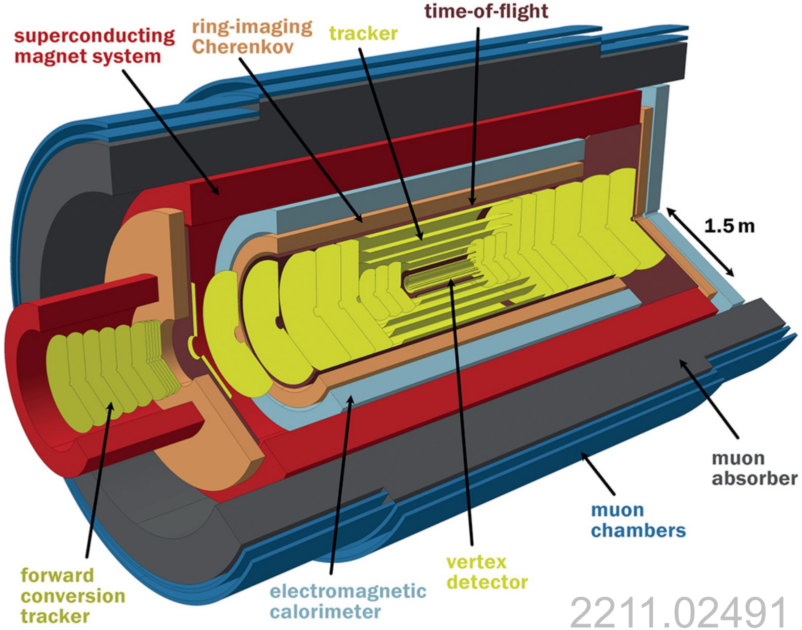


Precision requires a scan from small to medium-sized systems.

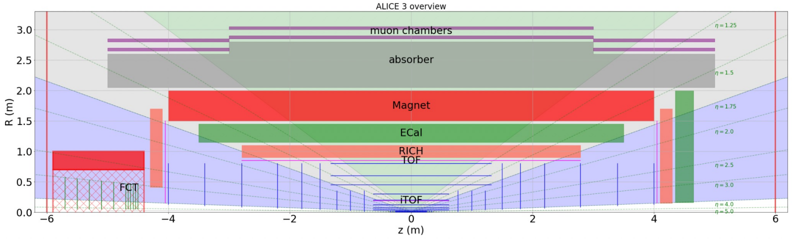
And understand the role of non-flow

Future

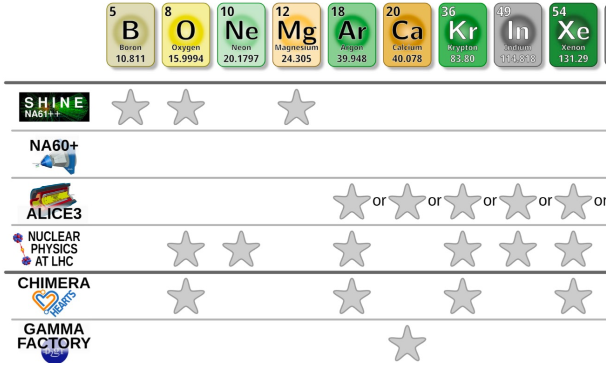
Require large acceptance detector and flexible collision species



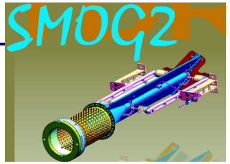
2211.02491



Collider mode



SMOG2 fixed target mode: $\sqrt{s_{NN}} = 65 - 110\text{GeV}$



Summary of possible gas targets

✌	H	validated for O(100) h/year
~✌	D	as above (not tested yet)
✌	He	
~✌	N	not tested yet, but ok from simulations
☞	O	to be validated, should be possible at least for short runs
✌	Ne	
✌	Ar	
☞	Kr	to be validated, should be possible for short runs at end of data-taking
☞	Xe	to be validated, should be possible for short runs at end of data-taking

any isotope for approved gas should be ok

Summary

- Precision understanding of QGP properties, its initial condition, and dynamics.
  - Can we reach within 10-20% uncertainties?

- Exploration of the full 3D structure
  →ALICE 3, ATLAS/CMS/LHCb

- Design collision species with different geometries: shape, size, and correlations
- System scan from small to medium species.
  → Enable by LHC and SMOG2

A	isobars	A	isobars	A	isobars	A	isobars	A	isobars	A	isobars
36	Ar, S	80	Se, Kr	106	Pd, Cd	124	Sn, Te, Xe	148	Nd, Sm	174	Yb, Hf
40	Ca, Ar	84	Kr, Sr, Mo	108	Pd, Cd	126	Te, Xe	150	Nd, Sm	176	Yb, Lu, Hf
46	Ca, Ti	86	Kr, Sr	110	Pd, Cd	128	Te, Xe	152	Sm, Gd	180	Hf, W
48	Ca, Ti	87	Rb, Sr	112	Cd, Sn	130	Te, Xe, Ba	154	Sm, Gd	184	W, Os
50	Ti, V, Cr	92	Zr, Nb, Mo	113	Cd, In	132	Xe, Ba	156	Gd,Dy	186	W, Os
54	Cr, Fe	94	Zr, Mo	114	Cd, Sn	134	Xe, Ba	158	Gd,Dy	187	Re, Os
64	Ni, Zn	96	Zr, Mo, Ru	115	In, Sn	136	Xe, Ba, Ce	160	Gd,Dy	190	Os, Pt
70	Zn, Ge	98	Mo, Ru	116	Cd, Sn	138	Ba, La, Ce	162	Dy,Er	192	Os, Pt
74	Ge, Se	100	Mo, Ru	120	Sn, Te	142	Ce, Nd	164	Dy,Er	196	Pt, Hg
76	Ge, Se	102	Ru, Pd	122	Sn, Te	144	Nd, Sm	168	Er,Yb	198	Pt, Hg
78	Se, Kr	104	Ru, Pd	123	Sb, Te	146	Nd, Sm	170	Er,Yb	204	Hg, Pb

Strategy for nuclear shape imaging

Flow observable = k ⊗ initial condition (structure)

QGP response,
a smooth function of N+Z

Structure of colliding nuclei,
non-monotonic function of N and Z

Compare two systems of similar size but different structure

$$R_{\mathcal{O}} \equiv \frac{\mathcal{O}_{\rm Ru}}{\mathcal{O}_{\rm Zr}} \approx 1 + c_1 \Delta\beta_2^2 + c_2 \Delta\beta_3^2 + c_3 \Delta R_0 + c_4 \Delta a$$

arXiv: 2111.15559

Deviation from unity depends only on their structure differences
c_1-c_4 are function of centrality