## Triple Higgs couplings

## ECFA WG1-SRCH

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## Introduction

- Measuring $h^{*}$->hh appears as a high priority of our field
- A very low SM x-section, 30 fb , with very large backgrounds makes this a formidable task
- Much easier if there are resonances $\mathbf{H}->$ hh
- Direct evidence, 3.8 sd : A(420)->H(320)->hh->bbbb $\underline{2210.05415}$

- BR(W+W+) ~10\% using Haber et al. SR implies light charged Higgs $\mathrm{H}+(130) \underline{2312.00420}$ and a dominant $\mathrm{BR}(\mathrm{H}+\mathrm{H}+)$
- These results naturally fit into Georgi Machacek model
- This model associates to $\mathbf{H + ( 1 3 0 )}$, seen in 2302.11739 a light CP-odd A with similar mass



## A(151)

- There is a candidate $\mathrm{A}(151)->\gamma \gamma$ at 4.8 s.d. when asking +b or Etmiss or leptons $\underline{2404.1492}$
- CP odd suggested by non observation in ZZ
- GM predicts that A(420)->H(320)Z->A(151)A(151)Z
- Could easily be found using the same technique usec for $\mathrm{h}(125) \mathrm{h}(125)$
- Gives a cross section in bbbb 4 times larger than h(125)h(125)
- Should provide the most convincing (>>5 sd) BSM LH signal so far !
- Three discoveries at a time : $\mathrm{A}(420), \mathrm{H}(320), \mathrm{A}(151)$.



## e-GM summary

- All but one among the $\mathbf{1 0}$ e-GM scalars have a candidate indicated by LHC data

| GM | Isosinglet | h95 | h125 |  |
| :--- | :--- | :--- | :--- | :---: |
|  | Isotriplet | A151 | H+130 |  |
|  | Isofiveplet | H320 | H+375 H++450 |  |
| E-GM | Extradoublet | A420 | H650 $\quad$ H+ ? |  |

- Physical states differ substantially from the GM Isospin states (see below)
- There is a candidate $\mathbf{H + - > A ( 4 2 0 ) W + - > ~ t t W + ~}$


## Example of a matrix solution

| $\begin{aligned} & H_{1}^{0}=\phi^{0, r}, \\ & H_{1}^{0,}=\sqrt{\frac{1}{3}} \xi^{0}+\sqrt{\frac{2}{3}} \chi^{0, r} . \end{aligned}$ |  | 1 | 2 | 3 | 4 | htt/SM | ZZ/SM | WW/SM |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | ¢1 | \$2 | $\chi$ | $\xi$ |  |  |  |
|  | H95 | 0.08 | -0.56 | 0 | 0.82 | -0.96 | -0.34 | 0.59 |
| $25)=0.58(\phi 1+\phi 2)+0.58 \mathrm{H}^{\prime} 1$ | H125 | 0.58 | 0.58 | 0.47 | 0.33 | 0.99 | 0.99 | 1.1 |
| $=-30 \mathrm{v} 2=102 \mathrm{u}=70 \mathrm{GeV} \mathrm{v}=174 \mathrm{GeV}$ | H320 | 0.31 | 0.30 | -0.88 | 0.17 | 0.52 | -1.29 | -0.38 |
| ( Yukawa Yi/SM=xi2*mt/v2 | H650 | 0.74 | -0.52 | 0 | -0.43 | -0.90 | -0.43 | -0.91 |

- $\mathrm{h}(125)=0.58(\phi 1+\phi 2)+0.58 \mathrm{H}^{\prime} 1$
- v1 =-30 v2=102 u=70 GeV v=174 GeV
- Type I Yukawa Yi/SM=xi2*mt/v2
- $\mathrm{Hi}_{\mathrm{ww}} / \mathrm{SM}=(x i 1 v 1+x i 2 \mathrm{v} 2) / \mathrm{v}+(2 x i 3+2 \mathrm{~V} 2 x i 4) u / v$
- Neutral scalars do not coincide with GM isospin states H1, H3 and H5
- Coloured squares have unmeasured couplings which can be predicted by this method
- H125 has a large mixing with $\mathbf{H}^{01} \mathbf{1}$ as predicted by PM of $\underline{1807.10660}$
- H650 dominated by doublets does not belong to fiveplet
- H320 belongs to fiveplet but differs from H05 therefore couples to h125h125
- H320->ZZ has a width ~5 GeV subdominant to $\Gamma_{\text {H320->AA }} \sim 100 \mathrm{GeV}$
- Predicts $\mu 95 \gamma \gamma$ and $\mu 125^{\sim} 1$ while ATLAS+ CMS measure $\mu 95 \gamma \gamma=0.27 \pm 0.12302 .07276$ and $\mu 125^{\sim} 1$ implying that charged scalar contributions act very differently


## An extra $\mathrm{H}+$ ?

- An e-GM scheme requires an extra $\mathrm{H}+$ related to $\mathrm{H}(650)$
- By analogy with $\mathrm{H}(650)$->A(420)Z->ttZ, one expects that H+->A(420)W+->ttW+
- An inclusive search for heavy jet-jet masses associated to a high pT lepton provides such a candidate 2001.04770

- ATLAS and CMS observe an excess in the inclusive measurement of ttW+/- $\underline{2401.05299}$
- Seems to proceed through ZW fusion to explain the charge asymmetry ( $\mathrm{p}->\mathrm{u}->\mathrm{W}+$ : factor 2)
- One should therefore observe $\mathrm{H}+->$ ZW
- No such effect in ttZ, which is not yet understood



## e+e- collider reach






- Final states are complex modes ( $\sim \mathrm{SM} \mathrm{ttH}$ ) requiring the highest $\mathcal{L}$ and an almost ideal detector with forward coverage for $b$ jet ID


## - ILC would provide $\mathbf{8 0 0 0} \mathbf{f b}-\mathbf{1}$ at $\mathbf{1 ~ T e V}$

- H(650) mainly produced through VBF (beam polarisation allows a factor ~2 gain, not included ) benefits from an increased energy
- $A(420)$ and $A(130)$ can be seen through cascades like $H(650)->Z A(420), H+(375)->A(130) W+$, $H(320)->A(131) A(131)$
- Using an e-e- collider one could also produce $\mathrm{H}^{--}$through VBF with polarized beams $\sim 100 \mathrm{fb}$ at 1 TeV
- Circular machine can access to h95, h151 and $\mathrm{H}+(130)$


## Conclusions

- $\mathrm{H}(320)->h(125) \mathrm{h}(125)$ should contribute to the $\mathrm{h}^{*}->$ hh SM measurements
- A global interpretation based on GM+SR predicts an immediate triple discovery for $A(420)$, A(151), H(320)
- The table of e-GM isospin states can be filled with the various indications provided by LHC
- The matrix method shows that the neutral candidates, including $\mathrm{h}(125)$, strongly differ from the isospin pure states predicted by GM
- Evidence for a third $\mathrm{H}+$ in $\mathrm{H}+->t \mathrm{tW}+$ as expected in e-GM
- Read our papers : $\underline{2404.09827}$ the most recent
- 2211.11723 and https://indico.cern.ch/event/1253605/
- 2308.12180 constantly updated
- Stay tuned!


$$
0
$$

## Sum Rule I

- W+W- ->W+W- Haber et al. in P.R.D 43 (1991) 904-912

$$
g^{2}\left(4 m_{W}^{2}-3 m_{Z}^{2} c_{W}^{2}\right) \stackrel{\rho \widetilde{ }}{\sim} g^{2} m_{W}^{2}=\sum_{k} g_{W^{+} W^{-}-H_{k}^{0}}^{2}-\sum_{l} g_{W^{+} W^{+} H_{l}^{-}}^{2}
$$

- So-far we have been able to measure H(650)W+W- and (2302.07276) h(95)W+W-
- There are other candidates like $h(151)$ and $H(330)$ where these measurements are unavailable, but we have ideas on how to deal with them (2308.12180 and https://indico.cern.ch/event/1253605/
- $\mathrm{H}(650)$ alone forces to have a contribution of $\mathrm{H}++->\mathrm{W}+\mathrm{W}+$ with a coupling ~ SM $=\mathrm{gmW}$


## First hint for $\mathrm{H}++$

- Recently at the Belgrade ATLAS meeting: $\mathbf{H + + ( 4 5 0 ) - > W + W +}$
- LHC is ideally suited for this measurement:

- 3.2 s.d. local, 2.5 s.d. global
- The reconstruction efficiency of CMS is a factor 2 below that of ATLAS 2312.00420



## Sum Rule II

- W+W- -> ZZ allows a similar SR

$$
\frac{g^{2} m_{Z}^{4} c_{W}^{2}}{m_{W}^{2}} \stackrel{\rho \simeq 1}{\simeq} g^{2} m_{Z}^{2}=\sum_{k} g_{W^{+} W^{-} H_{k}^{0}} g_{Z Z H_{k}^{0}}-\sum_{l} g_{W+Z H_{l}^{-}}^{2}
$$

- This forces a strong coupling for $\mathbf{H}+->\mathbf{Z W}+$ which should be observed at LHC
- Note that this result depends on the signs of the coupling constants which are not known from present measurements
- h95ZZ is known from LEP2 (but not its sign !)


## Evidence for $\mathrm{H}+->\mathrm{ZW}+$




- Coincident excesses at mH5+~375 GeV for ATLAS \& CMS
- ATLAS claims 2.8 s.d. local
- In GM H5++ and H5+ are mass degenerate which is almost true (see for e-GM 2111.14195)
- $\mathrm{H}(650)$ cannot fulfil the requirements of a neutral candidate of H 5 but $\mathrm{H}(320)$ is more appropriate


## Model independent results

- From these and the SR, one can deduce the total cross section, the elastic BR and the total widths as given in the following table:

| Channel | $\sigma_{\text {VBF }} \mathrm{fb}$ | $\sigma_{\text {VBF }}$ VV fb | BR(VV) \% | $\Gamma$ tot GeV |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{H}++(450)$ | 830 | 75 | $9 \pm 4$ | 160 |
| $\mathrm{H}+(375)$ | 810 | 125 | $15 \pm 8$ | 80 |

- These predictive results only rely on the validity of the sum rule approach, which seems legitimate given that VV final states at the LHC energy scale agree with the SM predictions
- They call for lighter charged scalers to provide VH and HH contributions


## GM interpretation

- Quantitatively, SR predicts $\Gamma_{\mathrm{H}++-\mathrm{W}+\mathrm{W}_{+}}$and the measured cross section allows to deduce the $\mathrm{BR}(\mathrm{W}+\mathrm{W}+)$ and the total width $\Gamma_{\mathrm{H}++-\mathrm{W}+\mathrm{W}+} / \mathrm{BR}(\mathrm{W}+\mathrm{W}+)$

| Channel | $u \mathrm{GeV}$ | $s_{H}$ | BR(VV) $\%$ | $\mathrm{BR}(\mathrm{VH}) \%$ |
| :--- | :---: | :---: | :---: | :---: |
| $\mathrm{H}++$ | $70 \pm 12$ | $0.80 \pm 0.1$ | 9 | 12.5 |
| $\mathrm{H}+$ | $80 \pm 13$ | $0.90 \pm 0.2$ | 15 | 17 |

- $\mathbf{u}=\mathbf{7 0} \mathrm{GeV}$ comes as a surprise: $u$ usual lore is $B R(W+W+)=1$ and $u<25 \mathrm{GeV}$
- This large value is inconsistent with models with only one triplet (2312.17314) requiring u much smaller to fulfill $\rho^{\sim} 1$
- $\mathrm{BR}(\mathrm{W}+\mathrm{W}+)^{\sim} 10 \%$ requires other modes like $\mathrm{H}^{\prime}+\mathrm{W}+$ or even $\mathrm{H}^{\prime}+\mathrm{H}^{\prime}+\left(\mathrm{ZH}^{\prime}+\right.$ for $\mathrm{H}+$ )
- A light (or several) $\mathrm{H}^{\prime}+$ predicted


## A light H' + ?

- There are few indirect hints for this
- B decays into $D \tau$ and $\Lambda \tau$ are reduced by 1.6 and 1.4 s.d. 2305.00614 suggesting $\mathrm{mH}+{ }^{\sim} 200 \mathrm{GeV}$
- ATLAS has searched for t->bH+->bbc and found a 3 s.d. local ( 2.5 global) excess around 130 GeV $\underline{2302.11739}$
- Not allowed in 2HD models for type II 1702.04571 but allowed for $\tan \beta>2$ in type I
- One predicts A mass degenerate which can feed into $\mathrm{H}+(375)$->AW+ (could be $\mathrm{A}(151)$ seen into $2 \gamma$ )
- Works quantitatively to explain the observed BR of $\mathrm{H}++$ and $\mathrm{H}+(375)$ into $\mathrm{H}^{\prime}+\mathrm{H}^{\prime}+$ and $\mathrm{H}^{\prime}+\mathrm{A}$
- Good news for circular colliders



## An extra H+ ?

- An e-GM scheme requires an extra $\mathrm{H}+$ related to H(650)
- By analogy with H(650)->A(420)Z->ttZ, one expects that $\mathrm{H}+->\mathrm{A}(420) \mathrm{W}+->t t W+$
- An inclusive search for heavy jet-jet masses
 associated to a high pt lepton provides such a candidate $\underline{2311.04033}$
- This reaction could be indirectly observed by ATLAS and CMS as an excess in the inclusive measurement of ttW+ $\underline{2401.05299}$
- However no sign of an excess in ttZ



## Precision Measurements

- $\mathbf{u}^{\sim} \mathbf{7 0} \mathrm{GeV}$ deduced from the sum rules seems incompatible with PM
- There is however a GM solution with large $\alpha \sim 60^{\circ}$ and $u=v_{\xi}=v_{\chi}=75 \mathrm{GeV}$ which satisfies PM for h(125)
- Implies that h can have a large triplet component still passing PM
- Not necessarily true for $\mathbf{h}->\mathbf{h h}$ or $\mathbf{Z} \boldsymbol{\gamma}$
- $\mu 95 \gamma \gamma \sim 0.3$ differs from the matrix prediction $\sim 1$, perhaps due to the charged Higgs sector while $\mu 125 \gamma \gamma \sim 1$ could be due to an accidental cancellation

1807.10660


## The neutral sector in e-GM

- e-GM comprises two doublet fields $\phi 1, \phi 2$ with vev v1 and v2 and two triplet fields $\chi, \xi$ with the same vev u
- For the neutral sector one writes:

$$
\left(\begin{array}{c}
h_{95} \\
h_{125} \\
H_{320} \\
H_{650}
\end{array}\right)=\mathscr{X}_{4 \times 4}\left(\begin{array}{c}
\phi_{1}^{0} \\
\phi_{2}^{0} \\
\chi^{0} \\
\xi^{0}
\end{array}\right)
$$

- where the matrix is $4 X 4$ unitary real (no CPV) with 16-4-6=6 free parameters requiring the unitary vectors to be orthogonal
- In total there are $6+3(v 1, v 2, u)$ free parameters and 7 observables from LHC measurements, $u$ from SR + constraint $v 1^{2}+v^{2}+4 u^{2}=(174 \mathrm{GeV})^{2}$
- One needs to choose between various Yukawa coupling patterns and we find that type I (all fermions having the same coupling) gives a reasonable agreement with the data


## $\mathrm{H}(320)$ as a partner of $\mathrm{H}++$ ?

- The H 5 multiplet containing $\mathrm{H}++$ needs to be completed by a neutral scalar, which cannot be $\mathrm{H}(650)$ which is doublet dominated
- Given its mass, $\mathrm{H}(320)$ seems appropriate and its dominant content in triplet fields (see matrix) reinforces this hypothesis
- However, its decay into bbbb interpreted as $\mathrm{h}(125) \mathrm{h}(125)$ seems to violate GM
- Note that $\mathrm{h}(125)$ and $\mathrm{h}(95)$ also carry triplet components which allows H(320)->hh
- $\mathrm{H}(320)$ most probably decays into $\mathbf{A}(151) \mathbf{A}(151)$ which feeds into bbbb, experimentally indistinguishable from hh


## Collider reach






- Final states are complex modes ( $\sim \mathrm{SM} \mathrm{ttH}$ ) requiring the highest $\mathcal{L}$ and an almost ideal detector with forward coverage for b jet ID
- ILC would provide 8000 fb-1 at 1 TeV
- H(650) mainly produced through VBF (beam polarisation allows a factor $\sim 2$ gain, not included) benefits from an increased energy
- $A(420)$ and $A(130)$ can be seen through cascades like $H(650)->Z A(420)$ and $H+(375)->A(130) W+$
- Using an e-e- collider one could also produce $\mathrm{H}^{--}$through VBF with polarized beams ~100 fb at
- Circular machine can access to h95, h151 and H+(130)


## Results from CMS

- Selecting a scalar solution in $\mathrm{ZZ}->4 \mathrm{I}, \mathrm{D}_{\text {bkg }}>0.6, \mathrm{CMS}$ finds:








Tensor decay in ZZ

- Nu sigir Ui dir excess du סכט vev iri uris sunsarimple
- A tensor resonance, fwd peaked, removed by this selection?


## Bulk KK graviton?

- 2310.01643

9909255 e+e- -> $G_{\text {KK }}(600)$-> $\mu+\mu$ - versus
k/Mplanck


## b->s $\gamma$ constraint on $\mathrm{mH}+$

- Light $\mathrm{H}+$ excluded for 2 HDM II, not for 2 HDM I with $\tan \beta>2 \quad 1702.04571$


Figure 4: $95 \%$ C.L. lower bounds on $M_{H^{ \pm}}$as functions of $\tan \beta$.

## How to derive the missing couplings ?

- There are indications for several neutral scalars candidates on the market, with unknown couplings to WW/ZZ
- Can one derive them taking into account the present measurements ?
- The answer seems positive assuming there is no CP violation and using available measurements

| Process | Channels | References | \# s.d. glob. (local) | Michelin |
| :---: | :---: | :---: | :---: | :---: |
| H650 | WW/ZZ ggF/VBF h95h125 | 1806.04429 2090.1491 2103.01918 CMS PAS HIG-200-016 2310.01643 | 6.1 | ** |
| A420 | tt ZH320->Zh125h125 | 1908.01115 2210.05415 | 5 | * |
| h95 | $\gamma \gamma \tau \tau$ bb (LEP) | 0306033 1811.08159 1803.06553 CMS-PAS-HIG-20.002 ATLAS-CONF-2023-035 | 3.9 | ~* |
| h151 | $\gamma \gamma+$ ETmiss | 2109.02650 | 4.8 | ? |
| H+375 | zW | ATLAS-CONF-2022-005 2104.04762 | (3.5) |  |
| H++450 | W+W+ | ATLAS-CONF-2023-023 2104.04762 | (3.9) |  |
| H+160 | bc | EPS-HEP2021, 631 | (3) |  |
| h146 | $\mu \mathrm{e}$ | CMS-PAS-HIG-22-002 | (3.8) |  |

W+W- with b jet veto > 50 times larger $W+W+$ due to $t t$ background
ggF W+W-




CMS Preliminary

VBF W+W-

$$
\text { CMS Preliminary } \quad \mathrm{L}=59.7 \mathrm{fb}^{-1}(13 \mathrm{TeV})
$$

$\square$



VBF W+W+

## Scalars for sum rules

| Scalar | Channels | References | \# s.d. glob. |
| :---: | :---: | :---: | :---: |
| H650 | WW/ZZ ggFVBF h95h125 | 1806.04529 2009.14791 2103.01918 CMS-PAS-HIG-20.016 CMS-PAS-HIG-21-011 | 6.1 |
| h95 | $\gamma \gamma \tau \tau \mathrm{bb}$ (LEP2) | 0306033 1811.08159 1803.06553 CMS-PAS-HIG-20-002 ATLAS-CONF-2023-035 | 3.9 |
| H++450 | W+W+ | $\begin{gathered} \text { ATLAS-CONF-2023-023 } \\ 2104.04762 \end{gathered}$ | 2.6 |
| H+375 | ZW | $\begin{aligned} & 2207.03925 \\ & 2104.04762 \end{aligned}$ | 2.7 |
| H++ \& H+ |  |  | 4.3 |

## $1^{\text {st }}$ indication : H->ZZ into 4 leptons

- The cleanest channel for discoveries
- From a combination of published histograms 1806.04529 with 113.5 $\mathrm{fb}^{-1}$ from CMS (2/3) and ATLAS (1/3) one observes a peak with $\mathrm{M}_{\mathrm{H}}^{\sim}{ }^{\sim} 660 \mathrm{GeV} \Gamma_{\mathrm{H}}{ }^{\sim} 100 \mathrm{GeV}, \sigma^{\sim} 90 \pm 25 \mathrm{fb}$ with $\mathrm{s} / \mathrm{b}=46 / 20 \sim 3.8$ s.d. local significance (5.8 Bayesian), 2.8 s.d. global
- With $139 \mathrm{fb}-1$, with sequential cuts, an excess is observed at the same mass, $s / b=9 / 2 \sim 2.1$ s.d., for VBFBR(ZZ)->H(660)->ZZ ~34 20 fb ( $\sim 2$ times smaller with a MVA analysis) 2009.14791 and 3 sd $150 \pm 60 \mathrm{fb}$ for $\operatorname{ggFBR}(Z Z)$
- The MVA analysis gives ggFBR(ZZ)<50 fb MVA + $\ell+\ell-v v$ - CMS analyses into four leptons are not yet published
- These results call for a combination of both analyses before one can draw a valid conclusion
- Could stop here but...



## CAVEAT on H(650)->ZZ

- CBA with 4 leptons indicates an excess $\sim 3.5$ s d combining ggF and VBF
- This translates (guesswork) into ggF(BR(ZZ)~150+-60 fb
- Adding $\boldsymbol{\ell}+\boldsymbol{\ell}-v \nu$ one sets an upper limit $\operatorname{ggF}(B R(Z Z)<50 f b$ assuming a 100 GeV width
- In "tension" with above result



## Historical progress of $\mathrm{H}(650)$

| Steps | Mode | Origin | Local sd | Remark | Global sd |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | ZZ->4l | ATLAS+CMS <br> from [7] | 3.8 | ATLAS+CMS 113.5 fb-1 <br> Defines mass \& width | 2.8 |
| 1 | ZZ->4e | From ATLAS | 3.5 | From histogram | 3.5 |
| 2 | WW->evev | From CMS | 3.8 | Official statement | 5 |
| 3 | $\mathrm{~h}(95) \mathrm{h}(125)->$ bb $\gamma \gamma$ | From CMS | 3.8 | Official statement | 6.1 |



## Evidence for VBF->H(650)->W+W-->elvv

ggF has a large top background even after b-jet vetoing and using $\mu \mathrm{e}$ (against DY)
Wide signal with $\pm 50 \%$ mass resolution VBF->H(650)->EL $\nu \nu$ allows to see a signal This VBF cross section $\sim \mathbf{1 6 0} \mathbf{\pm} \mathbf{5 0} \mathbf{f b}$, close to $S M$, is $\sim 3$ times larger than VBF->ZZ, inconsistent with GM which predicts for the scalar H5 WW/ZZ=0.5
2 HD excluded (bue line) h(125)WW predicts $\sin ^{2}(\alpha-\beta) \sim 0.97 \pm 0.09$ meaning that $H(650) W W^{\sim} \cos ^{2}(\alpha-\beta)^{\sim}(0.03 \pm 0.09) S M$
Both GM and 2HD excluded!
An attempt from ATLAS does not reach the same sensitivity (only $\mu \mathrm{e}$ ) ATLAS-CONF-2022-066


CMS PAS HIG-20-016


Table 3: Summary of the signal hypotheses with highest local significance for each $f_{V B F}$ scenario. For each signal hypothesis the resonance mass, production cross sections, and the local and global significances are given.

| Scenario | Mass $[\mathrm{GeV}]$ | ggF cross sec. $[\mathrm{pb}]$ | VBF cross sec. $[\mathrm{pb}]$ | Local signi. $[\sigma]$ | Global signi. $[\sigma]$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | SM $f_{V B F}$ | 800 | 016 | 0057 | 32 |
|  | $f_{V B F}=1$ | 650 | 0.0 | 0.16 | 3.8 |
|  | $f_{V B F}=0$ | 950 | 0.19 | 0.0 | $2.6 \pm 0.2$ |
| floating $f_{V B F}$ | 650 | $2.9 \times 10^{-6}$ | 0.16 | 2.0 | $0.4 \pm 0.6$ |

## W+W- with b jet veto > 50

 times larger than $\mathrm{W}+\mathrm{W}+$ due to tt and DY backgrounds
W+W+ much easier


## Evidence for gg+VBF->H(650)->Y(90)+h(125)->bb+ $\gamma \gamma$

- 3.8 s.d. for $\mathrm{mH}=650 \mathrm{GeV}$ and $\mathrm{m} \mathrm{m}^{\sim} 90 \mathrm{GeV}$ shown at ICHEP22
- Mass resolution on Y does not allow to distinguish between Z and $\mathrm{h}(95)$ which is by now a "good old friend"
CP says that bb cannot come from Z->bb but could be $\mathrm{h}(95)$ which is another scalar candidate seen in 3 channels $\underline{2203.13180}$ +2302.07276
- The cross section is dominant over all other indications $\boldsymbol{\sim 1 9 0 + 9 0 - 7 0 ~ f b ~ b u t ~ i t ~ i n c l u d e s ~}$ ggF+VBF
- Also interpreted by CMS as a tensor particle


## Evidence for H(650)->A(450)Z

- ATLAS sees a 2.85 s.d. excess in ttZ in >H(450)Z->ttl+ $\ell$ - 2311.04033
- Also compatible with H(650)->A(450)Z->tt $\ell+\ell-$
- Reinforces the case for $\mathrm{H}(650)$
- The $C P=-1$ candidate $A(420)->t t 1908.01115$ is compatible given the poor mass resolution
- A third observation was in A(420)->H(320)Z->hhZ


## ATLAS-CONF-2022-043

- In this context, there is no need to invoke the LE criterion which would justify the word 'insignificant' for this new indication easily accommodated within GM

A(650)-


## Scalars for sum rules

| Scalar | Channels | References | \# s.d. glob. |
| :---: | :---: | :---: | :---: |
| H650 | WW/ZZ ggFVBF h95h125 | 1806.04529 2009.14791 2103.01918 CMS-PAS-HIG-20-016 CMS-PAS-HIG-21-011 | 6.1 |
| h95 | $\gamma \gamma \tau \tau \mathrm{bb}$ (LEP2) | 0306033 1811.08159 1803.06553 CMS-PAS-HIG-20-002 ATLAS-CONF-2023-035 | 3.9 |
| H++450 | W+W+ | $\begin{gathered} \text { ATLAS-CONF-2023-023 } \\ 2104.04762 \end{gathered}$ | 2.6 |
| H+375 | ZW | $\begin{aligned} & 2207.03925 \\ & 2104.04762 \end{aligned}$ | 2.7 |
| H++ \& H+ |  |  | 4.3 |

## LHC inputs for our work

We choose to select * combined searches with > 4 s.d. global significance with the exception of h151 which results from an unofficial combination of CMS \& ATLAS data

This keeps 4 neutral scalars and one pseudo scalar
No change of significance after a CMS update of $h(95)->2 \gamma$ with RUN1 and RUN2 after some cleaning against Z->e+e-

ATLAS claims 1.7 s.d. on h95->2 $\gamma$

| Scalar | Channels | References | \# s.d. glob. | Michelin |
| :---: | :---: | :---: | :---: | :---: |
| H(125) | WW/ZZ ggF/VBF $\gamma \gamma \tau \tau$ bb |  | >6.9 | *** |
| H(650) | WW/ZZ ggF/VBF h95h125 H(650)->A(450)Z | 2009.14791 2103.01918 CMS-PAS-HIG-20-016 CMS-PAS-HIG-21-011 2311.04033 | 6.1 | ** |
| A(420) | $\begin{gathered} \text { tt ZH320->Zh125h125 } \\ \text { H(650)->A(450)Z } \end{gathered}$ | $\begin{aligned} & 1908.01115 \\ & 2210.05415 \\ & 2311.04033 \end{aligned}$ | 5 | * |
| h(95) | $\gamma \gamma \tau \tau$ bb (LEP) | 0306033 1811.08159 180.06553 CMS-PAS-HIG-20-002 | 4.3 | * |
| h(151) | $\gamma \gamma+$ ETmiss | 2109.02650 | 4.8 | ? |
| H++450 | W+W+ | ATLAS-CONF-2023-023 2104.04762 | 3.9 |  |
| H+375 | zW | $\begin{aligned} & 2205.03925 \\ & 2104.04762 \end{aligned}$ | 3.5 |  |
| h146 | $\mu \mathrm{e}$ | CMS-PAS-HIG-22-002 | 2.8 (3.8) |  |

Recent progress for H++ from ATLAS

## Evidence for $\mathrm{H}(320)$ and $\mathrm{A}(420)$

- ATLAS has observed A(420)->ZH(320) with $\mathrm{H}(320)->h(125) \mathrm{h}(125)->b b b b$
- The bb mass resolution is too poor to exclude contributions from $\mathrm{h}(95)$ or $\mathrm{A}(130)$
- The significance is 3.8 s.d. local 2210.05415
- This decay sits close to the kinematical limit meanil that $H(320)$ could be heavier and complete the GM H5 multiplet, together with $\mathrm{H}+(375), \mathrm{H}++(450)$
- Recall that $\mathrm{H}(320)->h h$ is forbidden only if $h$ is a pu singlet and H pure triplet, which is not the case
- Note finally that this indication constitutes the 3d evidence for a CP odd $A$, together with $A->t t$ and
 H(650)->AZ


## Evidence for $h / A(151)->\gamma \gamma+$ tag

- A second $\gamma \gamma+Z \gamma$ peak appears when requiring extra tag Etmiss or b jet
- 2109.02650 claims $\sim 4$ sd by combining ATLAS and CMS data
- GM predicts that ggF->H(320) has a cross cross section of $2000 \mathrm{fb}, 2 / 3$ going into $A(151) A(151)$ with $\mathbf{A}->b b, \tau \tau$ providing the tagging ingredient
- One predicts BR(A(151)-> $\left.{ }^{\prime} \gamma\right)^{\sim} 1.310-3$






## SUMMARY OF BSM CANDIDATES



## Georgi-Machacek for pedestrians

- Allows $\mathrm{I}=2, \mathrm{H}++$, without violating $\rho=\mathrm{M}^{2} \mathbf{w} / \mathrm{Mz}^{2} \cos ^{2} \theta \mathrm{w}=1$ at tree level
- Is achieved by combining 1 isospin doublet $\left(v_{\phi}\right)+2$ triplets, one real the other imaginary, with the same vacuum expectations :
- Predicts a 5-plet of physical states H5++ H5+ H50 H5- H5- - Fermiophobic only produced by VBF
-     + 3-plet H3+ H3O (CP-odd) -> A(400)
- Mass degeneracy inside multiplets usually assumed but unnecessary for $\rho=1$ see 2111.14195
-     + Singlets $h$ and $h^{\prime}$ mixing angle $\boldsymbol{\alpha}$


## The GM model for advanced

GM is constituted by one doublet $\phi$ and two triplets,

- H1 and H1' have following composition one complex $\chi$ and one real $\xi$, with the same vacuum expectations to get $\rho=1$

$$
H_{1}^{0}=\phi^{0, r},
$$

$$
\begin{aligned}
& \phi=\binom{\phi^{+}}{\phi^{0}}, \quad \chi=\left(\begin{array}{c}
x^{++} \\
x^{+} \\
x^{0 *}
\end{array}\right), \quad \xi=\left(\begin{array}{c}
\xi^{+} \\
\xi^{0} \\
\xi^{-}
\end{array}\right) \\
& \mathrm{Y}=1 / 2 \mathrm{~T}=1 / 2 \mathrm{v} \phi \quad \mathrm{Y}=1 \mathrm{~T}=1 \mathrm{v} \chi \quad \mathrm{Y}=0 \quad \mathrm{~T}=1 \mathrm{v} \xi=\mathrm{v} \chi \quad \rho=1 \\
& \rho=\frac{\tilde{v}_{\phi}^{2}+4 \tilde{v}_{\chi}^{2}+4 \tilde{v}_{\xi}^{2}}{\tilde{v}_{\phi}^{2}+8 \tilde{v}_{\chi}^{2}}=\frac{v^{2}}{v^{2}+4\left(\tilde{v}_{\chi}^{2}-\tilde{v}_{\xi}^{2}\right)} .
\end{aligned}
$$

$$
H_{1}^{0_{1}^{\prime \prime}}=\sqrt{\frac{1}{3}} \xi^{0}+\sqrt{\frac{2}{3}} x^{0, r} .
$$

Only $\phi$

- They form the following physical states, dominantly triplet $r$

$$
\mathbf{S}_{\mathbf{H}}=2 \mathbf{V} 2 \mathbf{V} \chi / \mathbf{V} \quad \begin{aligned}
H_{5}^{++} & =\chi^{++}, \\
H_{5}^{+} & =\frac{\left(\chi^{+}-\xi^{+}\right)}{\sqrt{2}}, \\
H_{5}^{0} & =\sqrt{\frac{2}{3}} \xi^{0}-\sqrt{\frac{1}{3}} \chi^{0, r}, \\
H_{3}^{+} & =-s_{H} \phi^{+}+c_{H} \frac{\left(\chi^{+}+\xi^{+}\right)}{\sqrt{2}}, \\
H_{3}^{0} & =-s_{H} \phi^{0, i}+c_{H} \chi^{0, i} .
\end{aligned}
$$

- The physical states are

```
h=\operatorname{cos}\alpha\mp@subsup{H}{1}{0}-\operatorname{sin}\alpha\mp@subsup{H}{1}{0\prime},
H=\operatorname{sin}\alpha\mp@subsup{H}{1}{0}+\operatorname{cos}\alpha\mp@subsup{H}{1}{0\prime}.
```

- Common wisdom: the mixing angle $\alpha$ has to be small to avoid altering the doublet properties of the SM $\mathrm{h}(125)$
- Also $\mathrm{v} \xi=\mathrm{v} \chi$ are predicted small while SR says that $v \xi=v \chi=70 \mathrm{GeV}$


## SGM: a SUSY version of GM

### 1308.4025

- GM does not necessarily mean compositeness
$\Sigma_{-1}=\left(\begin{array}{cc}\frac{x^{-}}{\sqrt{2}} & x^{0} \\ x^{-} & -\frac{x^{-}}{\sqrt{2}}\end{array}\right), \quad \Sigma_{0}=\left(\begin{array}{cc}\frac{\phi}{}^{0} & \phi^{+} \\ \phi^{-} & -\frac{\delta^{0}}{\sqrt{2}}\end{array}\right), \quad \Sigma_{1}=\left(\begin{array}{cc}\frac{\nu^{+}}{\sqrt{2}} & \psi^{++} \\ \psi^{0} & -\frac{\nu^{+}}{\sqrt{2}}\end{array}\right)$ SGM provides all the "goodies" of SUSY:

Perturbativity, computability

- EWSB naturally triggered

$$
H_{1}=\binom{H_{1}^{0}}{H_{1}^{-}}, \quad H_{2}=\binom{H_{2}^{+}}{H_{2}^{0}}
$$

- Mh predicted with less "tension" on stop masses with extra contributions to RC
- Two doublets as needed to interpret H32C and the ZZ/WW decays of $H(650)$
- DM candidate
- Complex/rich world with ~20 Higgs scalars


## Expected HL-LHC accuracies



ATLAS and CMS HL-LHC prospects

$3 \mathrm{ab}^{-1}(14 \mathrm{TeV})$

- Combination
… bБ̄y
… bప̄т
$\cdots$ bб̄b̄
- ... b̄̄ZZ
… $\mathrm{b} \overline{\mathrm{b} V \mathrm{~V}}(\mathrm{lv} \mid \mathrm{v})$


## TeV projects

D. Schulte

Higgs Hunting 23

+ CEPC-ee 0.24 TeV
SPPC-pp 100 TeV

|  | CME <br> [TeV] | Lumi per IP [ $\left.10^{34} \mathrm{~cm}^{-2} \mathrm{~s}^{-1}\right]$ | Years to physics | Cost range <br> [B\$] | Power [MW] |
| :---: | :---: | :---: | :---: | :---: | :---: |
| FCC-ee | 0.24 | 8.5 | 13-18 | 12-18 | 290 |
| ILC | 0.25 | 2.7 | <12 | 7-12 | 140 |
| CLIC | 0.38 | 2.3 | 13-18 | 7-12 | 110 |
| ILC | 3 | 6.1 | 19-24 | 18-30 | 400 |
| CLIC | 3 | 5.9 | 19-24 | 18-30 | 550 |
| MC | 3 | 1.8 | 19-24 | 7-12 | 230 |
| MC | 10 | 20 | >25 | 12-18 | 300 |
| FCC-hh | 100 | 30 | >25 | 30-50 | 560 |


| Quantity | Symbol | Unit | Initial | $\mathcal{L}$ Upgrade | Z pole |  | Jpgrades |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Centre of mass energy | $\sqrt{s}$ | GeV | 250 | 250 | 91.2 | 500 | 250 | 1000 |
| Luminosity | $\mathcal{L} \quad 10$ | $\mathrm{m}^{-2} \mathrm{~s}^{-1}$ | 1.35 | 2.7 | 0.21/0.41 | 1.8/3.6 | 5.4 | 5.1 |
| Polarization for $e^{-} / e^{+}$ | $P_{-}\left(P_{+}\right)$ | \% | 80(30) | 80 (30) | 80(30) | $80(30)$ | 80(30) | $80(20)$ |
| Repetition frequency | $f_{\text {rep }}$ | Hz | 5 | 5 | 3.7 | 5 | 10 | 4 |
| Bunches per pulse | $n_{\text {bunch }}$ | 1 | 1312 | 2625 | 1312/2625 | 1312/262 | 2625 | 2450 |
| Bunch population | $N_{\text {e }}$ | $10^{10}$ | 2 | 2 | 2 | 2 | 2 | 1.74 |
| Linac bunch interval | $\Delta t_{\mathrm{b}}$ | ns | 554 | 366 | 554/366 | 554/366 | 366 | 366 |
| Beam current in pulse | $I_{\text {pulse }}$ | mA | 5.8 | 8.8 | 5.8/8.8 | 5.8/8.8 | 8.8 | 7.6 |
| Beam pulse duration | $t_{\text {pulse }}$ | $\mu \mathrm{s}$ | 727 | 961 | 727/961 | 727/961 | 961 | 897 |
| Average beam power | $P_{\text {ave }}$ | MW | 5.3 | 10.5 | 1.42/2.84*) | 10.5/21 | 21 | 27.2 |
| RMS bunch length | $\sigma_{2}^{*}$ | mm | 0.3 | 0.3 | 0.41 | 0.3 | 0.3 | 0.225 |
| Norm. hor. emitt. at IP | $\gamma \epsilon_{\mathrm{x}}$ | $\mu \mathrm{m}$ | 5 | 5 | 5 | 5 | 5 | 5 |
| Norm. vert. emitt. at IP | $\gamma \epsilon_{y}$ | nm | 35 | 35 | 35 | 35 | 35 | 30 |
| RMS hor. beam size at IP | $\sigma_{\mathrm{x}}^{*}$ | nm | 516 | 516 | 1120 | 474 | 516 | 335 |
| RMS vert. beam size at IP | $\sigma_{y}^{*}$ | nm | 7.7 | 7.7 | 14.6 | 5.9 | 7.7 | 2.7 |
| Luminosity in top 1\% | $\mathcal{L}_{0.01} / \mathcal{L}$ |  | $73 \%$ | 73\% | 99\% | 58.3\% | $73 \%$ | 44.5 \% |
| Beamstrahlung energy loss | $\delta_{\text {BS }}$ |  | 2.6\% | 2.6\% | 0.16\% | 4.5\% | $2.6 \%$ | 10.5\% |
| Site AC power | $P_{\text {site }}$ | MW | 111 | 138 | 94/115 | 173/215 | 198 | 300 |
| Site length | $L_{\text {site }}$ | km | 20.5 | 20.5 | 20.5 | 31 | 31 | 40 |

Table 4.1: Summary table of the ILC accelerator parameters in the initial 250 GeV staged configuration and possible upgrades. A 500 GeV machine could also be operated at 250 GeV with 10 Hz repetition rate, bringing the maximum luminosity to $\left.5.4 \cdot 10^{34} \mathrm{~cm}^{-2} \mathrm{~s}^{-1}[26] .^{*}\right)$ : For operation at the $Z$-pole additional beam power of $1.94 / 3.88 \mathrm{MW}$ is necessary for positron production.

