### **Triple Higgs couplings**

### ECFA WG1-SRCH

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### Introduction

- Measuring h\*->hh appears as a high priority of our field
- A very low SM x-section, 30 fb, with very large backgrounds makes this a formidable task
- Much easier if there are **resonances H->hh**
- Direct evidence, 3.8 sd : A(420)->H(320)->hh->bbbb
   2210.05415
- BR(W+W+) ~10% using Haber et al. SR implies light charged Higgs H+(130) <u>2312.00420</u> and a dominant BR(H+H+)<sup>↑</sup>
- These results naturally fit into Georgi Machacek model
- This model associates to H+(130), seen in <u>2302.11739</u> a light CP-odd A with similar mass





# A(151)

- There is a candidate A(151)-> γγ at 4.8 s.d. when asking +b or Etmiss or leptons <u>2404.1492</u>
- CP odd suggested by non observation in ZZ
- GM predicts that A(420)->H(320)Z->A(151)A(151)Z
- Could easily be found using the same technique usec for h(125)h(125)
- Gives a cross section in bbbb 4 times larger than h(125)h(125)
- Should provide the most convincing (>>5 sd) BSM LH signal so far !
- Three discoveries at a time : A(420), H(320), A (151).



### e-GM summary

All but one among the 10 e-GM scalars have a candidate indicated by LHC data

GM	Isosinglet	h95	h125		
GM	Isotriplet	A151	H+	·130	
	Isofiveplet	H320	H+375	H++450	
E-GM	Extradoublet	A420	H650	H+ ?	

- Physical states differ substantially from the GM Isospin states (see below)
- There is a candidate H+->A(420)W+ -> ttW+

### Example of a matrix solution

- h(125)=0.58(\phi1+\phi2)+0.58H'1
- v1 =-30 v2=102 u=70 GeV v=174 GeV
- Type I Yukawa Yi/SM=xi2\*mt/v2
- Hi<sub>ww</sub>/SM=(xi1v1+xi2v2)/v+(2xi3+2v2xi4)u/v
- Neutral scalars do not coincide with GM isospin states H1, H3 and H5
- Coloured squares have unmeasured couplings which can be **predicted** by this method
- H125 has a large mixing with H<sup>0</sup>'1 as predicted by PM of <u>1807.10660</u>
- H650 dominated by **doublets** does not belong to fiveplet
- H320 belongs to fiveplet but differs from H05 therefore couples to h125h125
- H320->ZZ has a width ~5 GeV subdominant to  $\Gamma_{\rm H320->AA}$  ~ 100 GeV
- Predicts μ95γγ and μ125~1 while ATLAS+ CMS measure μ95γγ=0.27±0.1 2302.07276 and μ125~1 implying that charged scalar contributions act very differently

	1	2	3	4	htt/SM	ZZ/SM	WW/SM
	<b>φ</b> 1	<b>φ</b> 2	χ	٤			
H95	0.08	-0.56	0	0.82	- 0.96	- 0.34	0.59
H125	0.58	0.58	0.47	0.33	0.99	0.99	1.1
H320	0.31	0.30	-0.88	0.17	0.52	- 1.29	- 0.38
H650	0.74	-0.52	0	-0.43	- 0.90	- 0.43	- 0.91

### An extra H+?

- An e-GM scheme requires an extra H+ related to H(650)
- By analogy with H(650)->A(420)Z->ttZ, one expects that H+->A(420)W+->ttW+
- An inclusive search for heavy jet-jet masses associated to a high pT lepton provides such a candidate 2001.04770
- ATLAS and CMS observe an excess in the inclusive measurement of ttW+/- 2401.05299
- Seems to proceed through ZW fusion to explain the charge asymmetry (p->u->W+ : factor 2)
- One should therefore observe H+->ZW
- No such effect in ttZ, which is not yet understood





### e+e- collider reach



- Final states are complex modes (~ SM ttH) requiring the highest *L* and an almost ideal detector with forward coverage for b jet ID
- ILC would provide 8000 fb-1 at 1 TeV
- **H(650)** mainly produced through VBF (beam polarisation allows a factor ~2 gain, not included ) benefits from an increased energy
- A(420) and A(130) can be seen through cascades like H(650)->ZA(420), H+(375)->A(130)W+, H(320)->A(131)A(131)
- Using an e-e- collider one could also produce H<sup>--</sup>through VBF with polarized beams ~100 fb at 1 TeV
- Circular machine can access to h95, h151 and H+(130)

### Conclusions

- H(320)->h(125)h(125) should contribute to the h\*->hh SM measurements
- A global interpretation based on GM+SR predicts an immediate triple discovery for A(420), A(151), H(320)
- The table of **e-GM isospin states** can be filled with the various indications provided by LHC
- The **matrix method** shows that the neutral candidates, including h(125), strongly differ from the isospin pure states predicted by GM
- Evidence for a **third H+** in H+->ttW+ as expected in e-GM
- Read our papers : <u>2404.09827</u> the most recent
- <u>2211.11723</u> and <u>https://indico.cern.ch/event/1253605/</u>
- <u>2308.12180</u> constantly updated
- Stay tuned !



### Additional slides

### Sum Rule I

• W+W- ->W+W- Haber et al. in <u>P.R.D 43 (1991) 904-912</u>

$$g^{2}(4m_{W}^{2} - 3m_{Z}^{2}c_{W}^{2}) \stackrel{\rho \simeq 1}{\simeq} g^{2}m_{W}^{2} = \sum_{k} g^{2}_{W^{+}W^{-}H_{k}^{0}} - \sum_{l} g^{2}_{W^{+}W^{+}H_{l}^{-}}$$

- So-far we have been able to measure H(650)W+W- and (<u>2302.07276</u>) h(95)W+W-
- There are other candidates like h(151) and H(330) where these measurements are unavailable, but we have ideas on how to deal with them (2308.12180 and <u>https://indico.cern.ch/event/1253605/</u>
- H(650) alone forces to have a contribution of H++->W+W+ with a coupling ~ SM=gmW

### First hint for H++

- Recently at the Belgrade ATLAS meeting: H++(450)->W+W+
- LHC is ideally suited for this measurement:



• The reconstruction efficiency of CMS is a factor 2 below that of ATLAS 2312.00420





### Sum Rule II

• W+W- -> ZZ allows a similar SR

$$\frac{g^2 m_Z^4 c_W^2}{m_W^2} \stackrel{\rho \simeq 1}{\simeq} g^2 m_Z^2 = \sum_k g_{W^+ W^- H_k^0} g_{ZZH_k^0} - \sum_l g_{W^+ ZH_l^-}^2 g_{W^+ ZH_l^-}^2$$

- This forces a strong coupling for H+->ZW+ which should be observed at LHC
- Note that this result depends on the signs of the coupling constants which are not known from present measurements
- h95ZZ is known from LEP2 (but not its sign !)

### Evidence for H+ -> ZW+



• Coincident excesses at mH5+~375 GeV for ATLAS & CMS

- ATLAS claims 2.8 s.d. local
- In GM H5++ and H5+ are mass degenerate which is almost true (see for e-GM <u>2111.14195</u>)
- H(650) cannot fulfil the requirements of a neutral candidate of H5 but H(320) is more appropriate

### Model independent results

• From these and the SR, one can deduce the total cross section, the elastic BR and the total widths as given in the following table:

Channel	$\sigma_{\scriptscriptstyle VBF}$ fb	$\sigma_{\text{VBF}}$ VV fb	BR(VV) %	Γtot GeV
H++(450)	830	75	9±4	160
H+(375)	810	125	15±8	80

- These predictive results only rely on the validity of the sum rule approach, which seems legitimate given that VV final states at the LHC energy scale agree with the SM predictions
- They call for lighter charged scalers to provide VH and HH contributions

### **GM** interpretation

• Quantitatively, SR predicts  $\Gamma_{H++->W+W+}$  and the measured cross section allows to deduce the BR(W+W+) and the total width  $\Gamma_{H++->W+W+}$  /BR(W+W+)

Channel	u GeV	s <sub>H</sub>	BR(VV) %	BR(VH) %
H++	70±12	$0.80 \pm 0.1$	9	12.5
H+	80±13	$0.90 \pm 0.2$	15	17

- **u=70 GeV** comes as a surprise: usual lore is BR(W+W+)=1 and u<25 GeV
- This large value is inconsistent with models with only one triplet (<u>2312.17314</u>) requiring u much smaller to fulfill ρ~1
- BR(W+W+)~10% requires other modes like H'+W+ or even H'+H'+ (ZH'+ for H+)
- A light (or several) H'+ predicted

# A light H'+ ?

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- There are few indirect hints for this
- B decays into Dτ and Λτ are reduced by 1.6 and 1.4 s.d. <u>2305.00614</u> suggesting mH+~200 GeV
- ATLAS has searched for t->bH+->bbc and found a 3 s.d. local (2.5 global) excess around 130 GeV 2302.11739
- Not allowed in 2HD models for type II <u>1702.04571</u> but allowed for tan $\beta$ >2 in type I
- One predicts A mass degenerate which can feed into H+(375)->AW+ (could be A(151) seen into 2γ)
- Works quantitatively to explain the observed BR of H++ and H+(375) into H'+H'+ and H'+A
- Good news for circular colliders





## An extra H+?

- An e-GM scheme requires an extra H+ related to H(650)
- By analogy with H(650)->A(420)Z->ttZ, one expects that H+->A(420)W+->ttW+
- An inclusive search for heavy jet-jet masses associated to a high pt lepton provides such a candidate <u>2311.04033</u>
- This reaction could be indirectly observed by ATLAS and CMS as an excess in the inclusive measurement of ttW+ <u>2401.05299</u>
- However no sign of an excess in ttZ



### **Precision Measurements**

- u~70 GeV deduced from the sum rules seems incompatible with PM
- There is however a GM solution with large  $\alpha \sim 60^{\circ}$  and  $u=v_{\xi}=v_{\chi}=75$  GeV which satisfies PM for h(125)
- Implies that h can have a large triplet component still passing PM
- Not necessarily true for h->hh or Zγ
- μ95γγ~0.3 differs from the matrix prediction ~1, perhaps due to the charged Higgs sector while μ125γγ~1 could be due to an accidental cancellation



### The neutral sector in e-GM

- e-GM comprises two doublet fields φ1, φ2 with vev v1 and v2 and two triplet fields χ, ξ with the same vev u
- For the neutral sector one writes:

$$\begin{pmatrix} h_{95} \\ h_{125} \\ H_{320} \\ H_{650} \end{pmatrix} = \mathscr{X}_{4 \times 4} \begin{pmatrix} \phi_1^0 \\ \phi_2^0 \\ \chi^0 \\ \xi^0 \end{pmatrix}$$

- where the matrix is 4X4 unitary real (no CPV) with 16-4-6=6 free parameters requiring the unitary vectors to be orthogonal
- In total there are 6+3 (v1, v2, u) free parameters and 7 observables from LHC measurements, u from SR + constraint v1<sup>2</sup>+v2<sup>2</sup>+4u<sup>2</sup>=(174 GeV)<sup>2</sup>
- One needs to choose between various Yukawa coupling patterns and we find that type I (all
  fermions having the same coupling) gives a reasonable agreement with the data

## H(320) as a partner of H++?

- The **H5 multiplet** containing H++ needs to be completed by a neutral scalar, which cannot be H(650) which is doublet dominated
- Given its mass, H(320) seems appropriate and its dominant content in triplet fields (see matrix) reinforces this hypothesis
- However, its decay into bbbb interpreted as h(125)h(125) seems to violate GM
- Note that h(125) and h(95) also carry triplet components which allows H(320)->hh
- H(320) most probably decays into A(151)A(151) which feeds into bbbb, experimentally indistinguishable from hh

### Collider reach



- Final states are complex modes (~ SM ttH) requiring the highest *L* and an almost ideal detector with forward coverage for b jet ID
- ILC would provide 8000 fb-1 at 1 TeV
- H(650) mainly produced through VBF (beam polarisation allows a factor ~2 gain, not included ) benefits from an increased energy
- A(420) and A(130) can be seen through cascades like H(650)->ZA(420) and H+(375)->A(130)W+
- Using an e-e- collider one could also produce H<sup>--</sup>through VBF with polarized beams ~100 fb at 1 TeV

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• Circular machine can access to h95, h151 and H+(130)

# • Selecting a scalar solution in ZZ->4I , D<sub>bkg</sub>>0.6, CMS finds:



• A tensor resonance, fwd peaked, removed by this selection ?

### Bulk KK graviton ?

<u>2310.01643</u>
 k/Mplanck

#### <u>9909255</u>e+e- -> $G_{KK}(600)$ -> $\mu$ + $\mu$ - versus



### b->sγ constraint on mH+

• Light H+ excluded for 2HDM II, not for 2HDM I with  $\tan\beta>2$  <u>1702.04571</u>



### How to derive the missing couplings ?

- There are indications for several neutral scalars candidates on the market, with unknown couplings to WW/ZZ
- Can one derive them taking into account the present measurements ?
- The answer seems positive assuming there is no CP violation and using available measurements

Process	Channels	References	# s.d. glob. (local)	Michelin
H650	WW/ZZ ggF/VBF h95h125	1806.04429 2009.14791 2103.01918 CMS PAS HIG-20-016 2310.01643	6.1	**
A420	tt ZH320->Zh125h125	1908.01115 2210.05415	5	*
h95	γγ ττ bb (LEP)	0306033 1811.08159 1803.06553 CMS-PAS-HIG-20-002 ATLAS-CONF-2023-035	3.9	~*
h151	γγ +ETmiss	2109.02650	4.8	?
H+375	ZW	ATLAS-CONF-2022-005 2104.04762	(3.5)	
H++450	W+W+	ATLAS-CONF-2023-023 2104.04762	(3.9)	
H+160	bc	EPS-HEP2021, 631	(3)	
h146	μе	CMS-PAS-HIG-22-002	(3.8)	

### W+W- with b jet veto > 50 times larger W+W+ due to tt background

#### ggFW+W-

#### VBF W+W-



### Scalars for sum rules

Scalar	Channels	References	# s.d. glob.
H650	WW/ZZ ggFVBF h95h125	1806.04529 2009.14791 <u>2103.01918</u> CMS-PAS-HIG-20-016 CMS-PAS-HIG-21-011	6.1
h95	γγ ττ <b>bb (LEP2)</b>	0306033 1811.08159 1803.06553 CMS-PAS-HIG-20-002 ATLAS-CONF-2023-035	3.9
H++450	W+W+	ATLAS-CONF-2023-023 2104.04762	2.6
H+375	ZW	2207.03925 2104.04762	2.7
H++ & H+			4.3

### 1<sup>st</sup> indication : H->ZZ into 4 leptons

- The cleanest channel for discoveries
- From a combination of published histograms <u>1806.04529</u> with 113.5 fb<sup>-1</sup> from CMS (2/3) and ATLAS (1/3) one observes a peak with M<sub>H</sub>~660 GeV Γ<sub>H</sub>~100 GeV, σ~90±25 fb with s/b=46/20~3.8 s.d. local significance (5.8 Bayesian), 2.8 s.d. global
- With 139 fb-1, with sequential cuts, an excess is observed at the same mass, s/b=9/2 ~2.1 s.d., for VBFBR(ZZ)->H(660)->ZZ ~34±20 fb (~2 times smaller with a MVA analysis) 2009.14791 and 3 sd 150±60 fb for ggFBR(ZZ)
- The MVA analysis gives ggFBR(ZZ)<50 fb MVA + e+e-vv</li>
- CMS analyses into four leptons are not yet published
- These results call for a combination of both analyses before one can draw a valid conclusion
- Could stop here but...



### CAVEAT on H(650)->ZZ

- CBA with 4 leptons indicates an excess ~3.5s d combining ggF and VBF
- This translates (guesswork) into ggF(BR(ZZ)~150+-60 fb
- Adding *ℓ+ℓ-vv* one sets an upper limit ggF(BR(ZZ)<50fb assuming a 100 GeV width
- In "tension" with above result



### Historical progress of H(650)

Steps	Mode	Origin	Local sd	Remark	Global sd
0	ZZ->4ℓ	ATLAS+CMS	3.8	ATLAS+CMS 113.5 fb-1	2.8
		from [7]		Defines mass & width	
1	ZZ->4ℓ	From ATLAS	3.5	From histogram	3.5
2	WW->&v&v	From CMS	3.8	Official statement	5
3	h(95)h(125)->bbγγ	From CMS	3.8	Official statement	6.1



### Evidence for VBF->H(650)->W+W--> $\ell\ell\nu\nu$

- ggF has a large top background even after b-jet vetoing and using  $\mu e$  (against DY)
- Wide signal with  $\pm$  50% mass resolution
- VBF->H(650)-> $\ell\ell\nu\nu$  allows to see a signal
- This VBF cross section ~160±50 fb, close to SM, is ~3 times larger than VBF->ZZ, inconsistent with GM which predicts for the scalar H5 WW/ZZ=0.5
- 2 HD excluded (bue line) h(125)WW predicts  $sin^2(\alpha-\beta)^{\circ}0.97\pm0.09$  meaning that H(650)WW^cos^2(\alpha-\beta)^{\circ}(0.03\pm0.09)SM
- Both GM and 2HD excluded !
- An attempt from ATLAS does not reach the same sensitivity (only  $\mu e$ ) ATLAS-CONF-2022-066



Table 3: Summary of the signal hypotheses with highest local significance for each  $f_{VBF}$  scenario. For each signal hypothesis the resonance mass, production cross sections, and the local and global significances are given.

Scenario	Mass [GeV ]	ggF cross sec. [pb]	VBF cross sec. [pb]	Local signi. $[\sigma]$	Global signi. $[\sigma]$
$SM f_{VBF}$	800	0.16	0.057	3.2	$1.7 \pm 0.2$
$f_{VBF} = 1$	650	0.0	0.16	3.8	$2.6 \pm 0.2$
$f_{VBF} = 0$	950	0.19	0.0	2.6	$0.4 \pm 0.6$
floating $f_{VBF}$	650	$2.9 \times 10^{-6}$	0.16	3.8	$2.4 \pm 0.2$

### W+W- with b jet veto > 50 times larger than W+W+ due to tt and DY backgrounds



#### ggF->W+W-

#### VBF W+W-



### Evidence for gg+VBF->H(650)->Y(90)+h(125)->bb+γγ

- 3.8 s.d. for mH=650 GeV and mY~90 GeV shown at ICHEP22
- Mass resolution on Y does not allow to distinguish between Z and h(95) which is by now a "good old friend"
- CP says that bb cannot come from Z->bb but could be h(95) which is another scalar candidate seen in 3 channels <u>2203.13180</u> +<u>2302.07276</u>
- The cross section is dominant over all other indications ~190+90-70 fb but it includes ggF+VBF
- Also interpreted by CMS as a tensor particle



### Evidence for H(650)->A(450)Z

- ATLAS sees a 2.85 s.d. excess in ttZ in >H(450)Z->ttℓ+ℓ- <u>2311.04033</u>
- Also compatible with H(650)->A(450)Z->tte+e-
- Reinforces the case for H(650)
- The CP=-1 candidate A(420)->tt 1908.01115 is compatible given the poor mass resolution
- A third observation was in A(420)->H(320)Z->hhZ <u>ATLAS-CONF-2022-043</u>
- In this context, there is no need to invoke the LE criterion which would justify the word 'insignificant' for this new indication easily accommodated within GM



### Scalars for sum rules

Scalar	Channels	References	# s.d. glob.
H650	WW/ZZ ggFVBF h95h125	1806.04529 2009.14791 <u>2103.01918</u> CMS-PAS-HIG-20-016 CMS-PAS-HIG-21-011	6.1
h95	γγ ττ bb (LEP2)	0306033 1811.08159 1803.06553 CMS-PAS-HIG-20-002 ATLAS-CONF-2023-035	3.9
H++450	W+W+	ATLAS-CONF-2023-023 2104.04762	2.6
H+375	ZW	2207.03925 2104.04762	2.7
H++ & H+	E Pichard UCLab A	vril 2024	4.3

### LHC inputs for our work

- We choose to select \* combined searches with >
   4 s.d. global significance with the exception of
   h151 which results from an unofficial
   combination of CMS & ATLAS data
- This keeps 4 neutral scalars and one pseudo scalar
- No change of significance after a CMS update of h(95)->2γ with RUN1 and RUN2 after some cleaning against Z->e+e-
- ATLAS claims 1.7 s.d. on h95->2 $\gamma$
- Recent progress for H++ from ATLAS

Scalar	Channels	References	# s.d. glob.	Michelin
H(125)	WW/ZZ ggF/VBF γγ ττ bb		>6.9	***
H(650)	WW/ZZ ggF/VBF h95h125 H(650)->A(450)Z	2009.14791 2103.01918 CMS-PAS-HIG-20-016 CMS-PAS-HIG-21-011 2311.04033	6.1	**
A(420)	tt ZH320->Zh125h125 H(650)->A(450)Z	1908.01115 2210.05415 2311.04033	5	*
h(95)	γγ ττ bb (LEP)	0306033 1811.08159 1803.06553 CMS-PAS-HIG-20-002	4.3	*
h(151)	γγ +ETmiss	2109.02650	4.8	?
H++450	W+W+	ATLAS-CONF-2023-023 2104.04762	3.9	
H+375	ZW	2205.03925 2104.04762	3.5	
h146	μe	CMS-PAS-HIG-22-002	2.8 (3.8)	

# Evidence for H(320) and A(420)

- ATLAS has observed A(420)->ZH(320) with H(320)->h(125)h(125)->bbbb
- The bb mass resolution is too poor to exclude contributions from h(95) or A(130)
- The significance is 3.8 s.d. local <u>2210.05415</u>
- This decay sits close to the kinematical limit meaning that H(320) could be heavier and complete the GM H5 multiplet, together with H+(375), H++(450)
- Recall that H(320)->hh is forbidden only if h is a pussinglet and H pure triplet, which is not the case
- Note finally that this indication constitutes the 3d evidence for a CP odd A, together with A->tt and H(650)->AZ



### Evidence for $h/A(151) \rightarrow \gamma\gamma + tag$

- A second γγ+Zγ peak appears when requiring extra tag Etmiss or b jet
- 2109.02650 claims ~4 sd by combining ATLAS and CMS data
- GM predicts that ggF->H(320) has a cross cross section of 2000 fb, 2/3 going into A(151)A(151) with A->bb, ττ providing the tagging ingredient
- One predicts BR(A(151)->γγ)~1.310-3



### SUMMARY OF BSM CANDIDATES



### Georgi-Machacek for pedestrians

- Allows I=2, H++, without violating ρ=M<sup>2</sup>w/Mz<sup>2</sup>cos<sup>2</sup>θw=1 at tree level
- Is achieved by combining 1 isospin doublet  $(v_{\phi}) + 2$  triplets, one real the other imaginary, with the same vacuum expectations :

$$\rho = \frac{\tilde{v}_{\phi}^2 + 4\tilde{v}_{\chi}^2 + 4\tilde{v}_{\xi}^2}{\tilde{v}_{\phi}^2 + 8\tilde{v}_{\chi}^2} = \frac{v^2}{v^2 + 4(\tilde{v}_{\chi}^2 - \tilde{v}_{\xi}^2)}.$$
 =1 with  $v_{\chi} = v_{\xi} = u_{\xi}$ 

- Predicts a 5-plet of physical states H5++ H5+ H50 H5- H5- Fermiophobic only produced by VBF
- + 3-plet H3+ H30 (CP-odd) -> A(400)
- Mass degeneracy inside multiplets usually assumed but unnecessary for  $\rho{=}1$  see  $\underline{2111.14195}$
- + Singlets **h** and h' mixing angle  $\alpha$

ullet

### The GM model for advanced

H1 and H1' have following composition one complex  $\chi$  and one real  $\xi$ , with the same vacuum expectations to get  $\rho=1$  $H_1^0 = \phi^{0,r},$ 

$$\phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}, \quad \chi = \begin{pmatrix} \chi^{++} \\ \chi^+ \\ \chi^{0+} \end{pmatrix}, \quad \xi = \begin{pmatrix} \xi^+ \\ \xi^0 \\ \xi^- \end{pmatrix}$$

$$Y = 1/2 \text{ T} = 1/2 \text{ v}\phi \qquad Y = 1 \text{ T} = 1 \text{ v}\chi \qquad Y = 0 \quad \text{T} = 1 \text{ v}\xi = \text{v}\chi \qquad \rho = 1$$

$$\rho = \frac{\tilde{v}_{\phi}^2 + 4\tilde{v}_{\chi}^2 + 4\tilde{v}_{\xi}^2}{\tilde{v}_{\phi}^2 + 8\tilde{v}_{\chi}^2} = \frac{v^2}{v^2 + 4(\tilde{v}_{\chi}^2 - \tilde{v}_{\xi}^2)}.$$

- They form the following physical states, dominantly triplet r
- $s_{\mu} = 2\sqrt{2}v\chi/v$

$$\begin{split} H_5^{++} &= \chi^{++}, \\ H_5^+ &= \frac{(\chi^+ - \xi^+)}{\sqrt{2}}, \\ H_5^0 &= \sqrt{\frac{2}{3}} \xi^0 - \sqrt{\frac{1}{3}} \chi^{0,r}, \\ H_3^+ &= -s_H \phi^+ + c_H \frac{(\chi^+ + \xi^+)}{\sqrt{2}}, \\ H_3^0 &= -s_H \phi^{0,i} + c_H \chi^{0,i}. \end{split}$$

 $H_1^{0\prime} = \sqrt{\frac{1}{3}}\xi^0 + \sqrt{\frac{2}{3}}\chi^{0,r}.$ 

The physical states are

 $h = \cos \alpha H_1^0 - \sin \alpha H_1^{0\prime},$  $H = \sin \alpha H_1^0 + \cos \alpha H_1^{0'}.$ 

- Common wisdom: the mixing angle  $\alpha$ has to be small to avoid altering the doublet properties of the SM h(125)
- Also  $v\xi = v\chi$  are predicted small while SR says that  $v\xi = v\chi = 70$  GeV

## SGM: a SUSY version of GM

#### <u>1308.4025</u>

 GM does not necessarily mean compositeness

 $\Sigma_{-1} = \begin{pmatrix} \frac{\chi^{-}}{\sqrt{2}} & \chi^{0} \\ \chi^{--} & -\frac{\chi^{-}}{\sqrt{2}} \end{pmatrix}, \quad \Sigma_{0} = \begin{pmatrix} \frac{\phi^{0}}{\sqrt{2}} & \phi^{+} \\ \phi^{-} & -\frac{\phi^{0}}{\sqrt{2}} \end{pmatrix}, \quad \Sigma_{1} = \begin{pmatrix} \frac{\psi^{+}}{\sqrt{2}} & \psi^{++} \\ \psi^{0} & -\frac{\psi^{+}}{\sqrt{2}} \end{pmatrix}$ SGM provides all the "goodies" of SUSY:

Perturbativity, computability

- EWSB naturally triggered
- Mh predicted with less "tension" on stop masses with extra contributions to RC
- Two doublets as needed to interpret H320 and the ZZ/WW decays of H(650)
- DM candidate
- Complex/rich world with ~20 Higgs scalars

$$H_1 = \begin{pmatrix} H_1^0 \\ H_1^- \end{pmatrix}, \quad H_2 = \begin{pmatrix} H_2^+ \\ H_2^0 \end{pmatrix}$$

### **Expected HL-LHC accuracies**



### TeV projects

SNOWMASS

D. Schulte Higgs Hunting 23

+ CEPC-ee 0.24 TeV SPPC-pp 100 TeV

	CME [TeV]	Lumi per IP [10 <sup>34</sup> cm <sup>-2</sup> s <sup>-1</sup> ]	Years to physics	Cost range [B\$]	Power [MW]
FCC-ee	0.24	8.5	13-18	12-18	290
ILC	0.25	2.7	<12	7-12	140
CLIC	0.38	2.3	13-18	7-12	110
ILC	3	6.1	19-24	18-30	400
CLIC	3	5.9	19-24	18-30	550
MC	3	1.8	19-24	7-12	230
MC	10	20	>25	12-18	300
FCC-hh	100	30	>25	30-50	560

#### **Snowmass Paper**

arXiv:2203.07622

Quantity	Symbol	Unit	Initial	$\mathcal{L}$ Upgrade	Z pole		Jpgrades		tamational develo
Centre of mass energy	$\sqrt{s}$	${\rm GeV}$	250	250	91.2	500	250	1000	
Luminosity	${\cal L} = 10^{34}$	$\mathrm{cm}^{-2}\mathrm{s}^{-1}$	1.35	2.7	0.21/0.41	1.8/3.6	5.4	5.1	
Polarization for $e^{-}/e^{+}$	$P_{-}(P_{+})$	%	80(30)	80(30)	80(30)	80(30)	80(30)	80(20)	
Repetition frequency	$f_{\mathrm{rep}}$	Hz	5	5	3.7	5	10	4	
Bunches per pulse	$n_{\rm bunch}$	1	1312	2625	1312/2625	1312/262	2625	2450	
Bunch population	$N_{ m e}$	$10^{10}$	2	2	2	2	2	1.74	
Linac bunch interval	$\Delta t_{\rm b}$	ns	554	366	554/366	554/366	366	366	
Beam current in pulse	$I_{\rm pulse}$	$\mathbf{m}\mathbf{A}$	5.8	8.8	5.8/8.8	5.8/8.8	8.8	7.6	
Beam pulse duration	$t_{\rm pulse}$	$\mu { m s}$	727	961	727/961	727/961	961	897	
Average beam power	$P_{\rm ave}$	MW	5.3	10.5	$1.42/2.84^{*)}$	10.5/21	21	27.2	
RMS bunch length	$\sigma_z^*$	$\mathbf{m}\mathbf{m}$	0.3	0.3	0.41	0.3	0.3	0.225	
Norm. hor. emitt. at IP	$\gamma \tilde{\epsilon_{\mathrm{x}}}$	$\mu m$	5	5	5	5	5	5	
Norm. vert. emitt. at IP	$\gamma \epsilon_{ m y}$	nm	35	35	35	35	35	30	
RMS hor. beam size at IP	$\sigma^*_{\mathrm{x}}$	nm	516	516	1120	474	516	335	
RMS vert. beam size at IP	$\sigma_{\rm v}^*$	nm	7.7	7.7	14.6	5.9	7.7	2.7	
Luminosity in top 1%	$\mathcal{L}_{0.01}/\mathcal{L}$		73%	73%	99%	58.3%	73%	44.5%	
Beamstrahlung energy loss	$\delta_{\mathrm{BS}}$		2.6%	2.6%	0.16%	4.5%	2.6%	10.5%	
Site AC power	$P_{\rm site}$	MW	111	138	94/115	173/215	198	300	
Site length	$L_{ m site}$	$\mathbf{km}$	20.5	20.5	20.5	31	31	40	

Table 4.1: Summary table of the ILC accelerator parameters in the initial 250 GeV staged configuration and possible upgrades. A 500 GeV machine could also be operated at 250 GeV with 10 Hz repetition rate, bringing the maximum luminosity to  $5.4 \cdot 10^{34} \text{ cm}^{-2} \text{s}^{-1}$  [26]. \*): For operation at the Z-pole additional beam power of 1.94/3.88 MW is necessary for positron production.

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