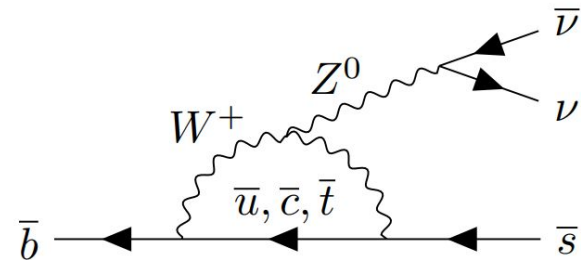
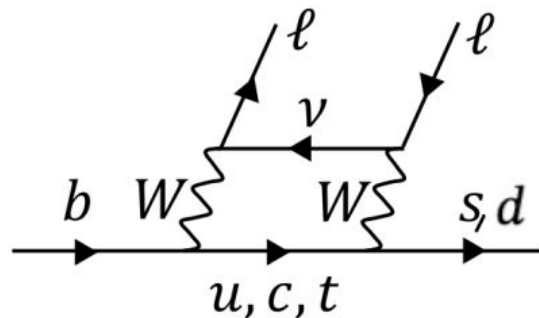
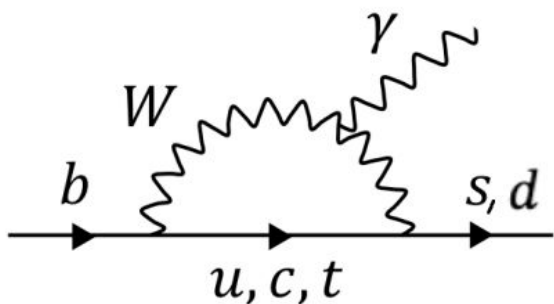
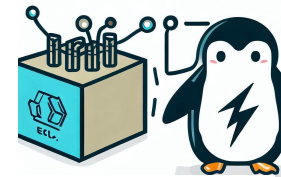


Studies of $b \rightarrow s$ transitions with Belle II

Discrete-2024, 2 Dec 2024
Sasha Glazov, on behalf of Belle II



Study of $b \rightarrow s$ transitions: motivation



- Flavor-changing neutral-current $b \rightarrow s(d)$ transitions are suppressed in SM, while many BSM theories predict significant contributions
- Several observables have clean theoretical predictions and show tensions between data and SM
- Channels involving 3rd generation interesting in particular due to e.g. connections to anomalies in semi-tauic decays (“ $R(D^{(*)})$ ”)

Belle II and SuperKEKB

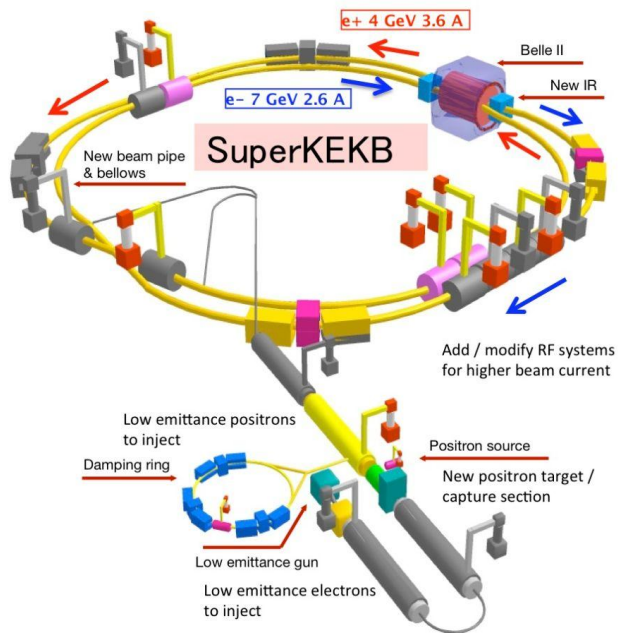
Collected in total:

551 fb⁻¹

Today's talk: Run I Belle II sample: 0.4×10^9 BB plus complete Belle sample.

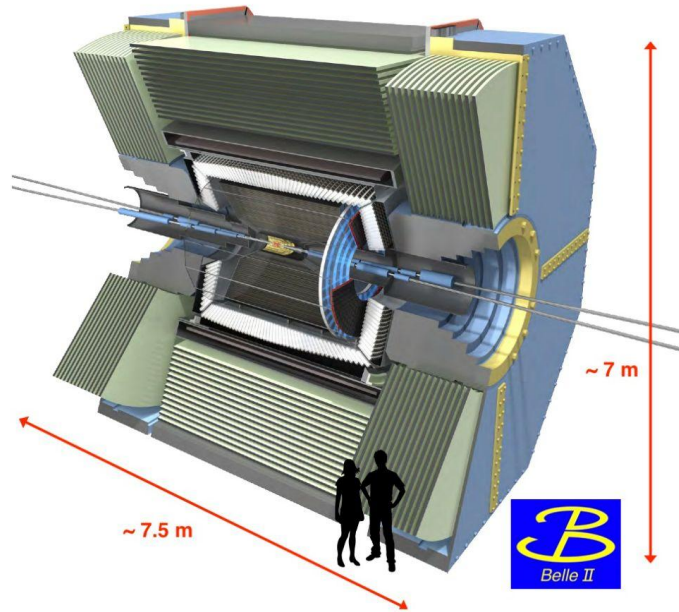
SuperKEKB:

- e^+e^- collider with energies 4 GeV and 7 GeV operating around $Y(4S)$ resonance
- Achieved world-record peak luminosity of $4.7 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$



Belle II:

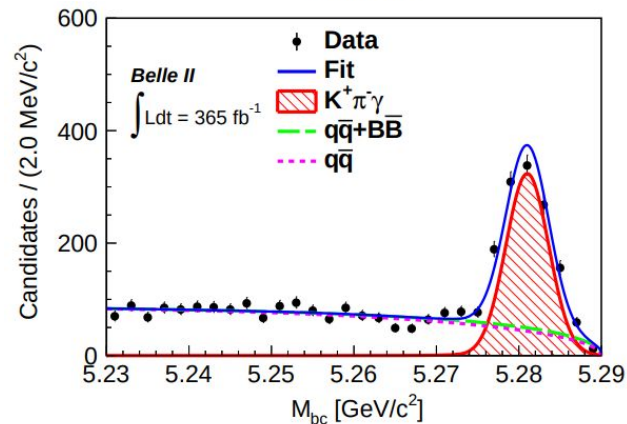
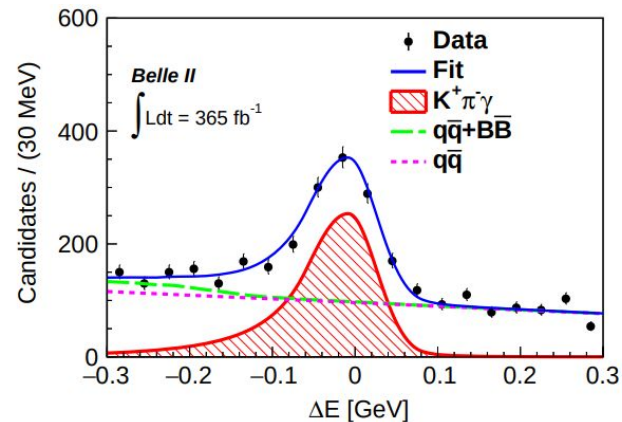
- Nearly 4π detector
- Tracking, PID, and photon reconstruction capabilities
- Similar performance for electrons and muons
- Well-suited to measure decays with **missing energy**, π^0 in the final state, inclusive measurements



Measurement of $B \rightarrow K^* \gamma$

- Measurement of $B^{+,0} \rightarrow K^{*+,0} \gamma$ using Run I Belle II data
- $K^{*0} \rightarrow K^+ \pi^-$, $K^{*0} \rightarrow K_S^0 \pi^0$, $K^{*+} \rightarrow K^+ \pi^0$, $K^{*+} \rightarrow K_S^+ \pi^+$ modes considered.
- Dominant background from continuum with $\pi^0(\eta) \rightarrow \gamma\gamma$ faking the prompt photon
- Dedicated MVA to suppress $\pi^0(\eta)$ background and continuum
- 2D unbinned fit in M_{bc} , ΔE
- Large signal, with moderate background \rightarrow precision measurement.

arXiv:2411.10127



Measurement of $B \rightarrow K^* \gamma$

- Comparable statistical and systematic uncertainties for the measured branching fractions
- Dominant systematics from π^0 reconstruction efficiency (3.9%)
- For CP and isospin asymmetry, statistical uncertainties dominate
- Isospin asymmetry is consistent with the SM expectations and previous measurements from Belle and BaBar.

$$\mathcal{B} = \frac{N_S/\epsilon_S + N_{\bar{S}}/\epsilon_{\bar{S}}}{2 \times N_{B\bar{B}} \times f_{+-}(f_{00})},$$

$$\mathcal{A}_{CP} = \frac{N_S/\epsilon_S - N_{\bar{S}}/\epsilon_{\bar{S}}}{N_S/\epsilon_S + N_{\bar{S}}/\epsilon_{\bar{S}}},$$

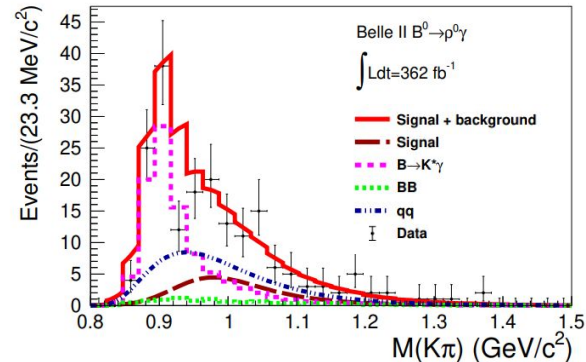
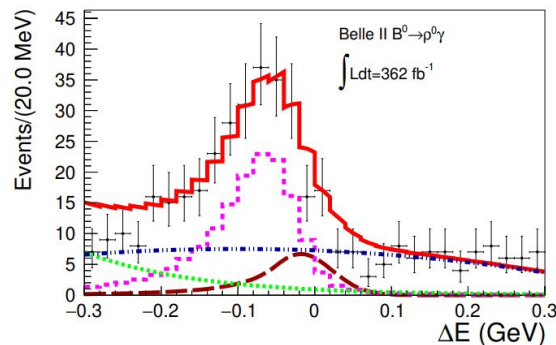
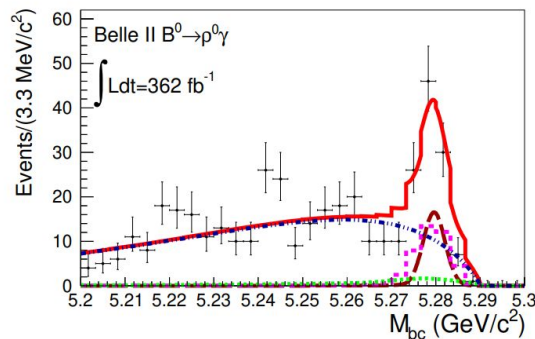
$$\Delta_{0+} = \frac{(\tau_+/\tau_0) \times \mathcal{B}(B^0 \rightarrow K^{*0} \gamma) - \mathcal{B}(B^+ \rightarrow K^{*+} \gamma)}{(\tau_+/\tau_0) \times \mathcal{B}(B^0 \rightarrow K^{*0} \gamma) + \mathcal{B}(B^+ \rightarrow K^{*+} \gamma)},$$

$$\Delta \mathcal{A}_{CP} = \mathcal{A}_{CP}(B^+ \rightarrow K^{*+} \gamma) - \mathcal{A}_{CP}(B^0 \rightarrow K^{*0} \gamma),$$

Channel	\mathcal{B} (10^{-5})	\mathcal{A}_{CP} (%)
$B^0 \rightarrow K^{*0}[K^+\pi^-]\gamma$	$4.14 \pm 0.10 \pm 0.11$	$-3.3 \pm 2.3 \pm 0.4$
$B^0 \rightarrow K^{*0}[K_S^0\pi^0]\gamma$	$4.07 \pm 0.33 \pm 0.23$	—
$B^0 \rightarrow K^{*0}\gamma$	$4.14 \pm 0.10 \pm 0.10$	$-3.3 \pm 2.3 \pm 0.4$
$B^+ \rightarrow K^{*+}[K^+\pi^0]\gamma$	$3.97 \pm 0.17 \pm 0.20$	$+1.7 \pm 4.0 \pm 0.9$
$B^+ \rightarrow K^{*+}[K_S^0\pi^+]\gamma$	$4.06 \pm 0.18 \pm 0.13$	$-3.5 \pm 4.3 \pm 0.7$
$B^+ \rightarrow K^{*+}\gamma$	$4.02 \pm 0.13 \pm 0.13$	$-0.7 \pm 2.9 \pm 0.6$
	Δ_{0+} (%)	$\Delta \mathcal{A}_{CP}$ (%)
$B \rightarrow K^* \gamma$	$+5.0 \pm 2.0 \pm 1.0 \pm 1.1$	$+2.6 \pm 3.8 \pm 0.7$

Measurement of $B \rightarrow \rho\gamma$

arXiv:2407.08984



- Measurement using combined Belle+Belle II (run I) data sample
- Dominant backgrounds from $B \rightarrow K^*\gamma$ and continuum
- 3D unbinned fit in M_{bc} , ΔE and $M(K\pi)$
- Isospin and CP asymmetries are consistent with zero.

$$\mathcal{B}(B^+ \rightarrow \rho^+ \gamma) = (13.1_{-1.9}^{+2.0+1.3}) \times 10^{-7}$$

$$\mathcal{B}(B^0 \rightarrow \rho^0 \gamma) = (7.5 \pm 1.3_{-0.8}^{+1.0}) \times 10^{-7}$$

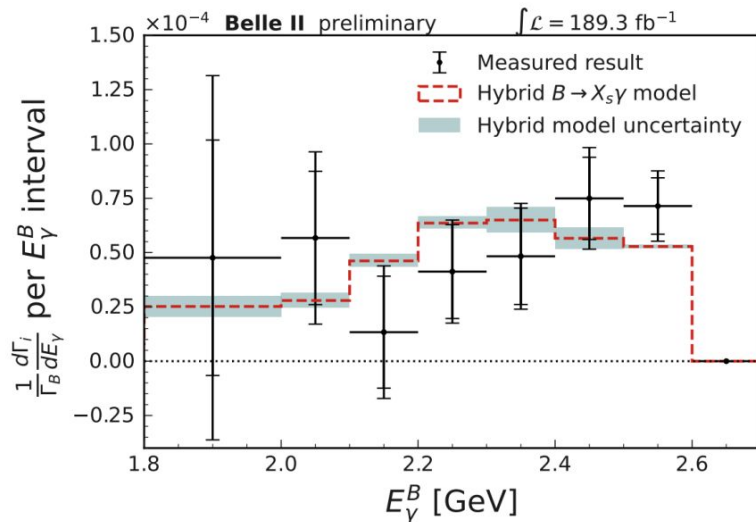
$$A_{CP}(B^+ \rightarrow \rho^+ \gamma) = (-8.2 \pm 15.2_{-1.2}^{+1.6}) \%$$

$$A_I(B \rightarrow \rho\gamma) = (10.9_{-11.7}^{+11.2+6.8+3.8} - 6.2 - 3.9) \%$$

Status of inclusive $b \rightarrow s\gamma$ analyses

ICHEP 2022

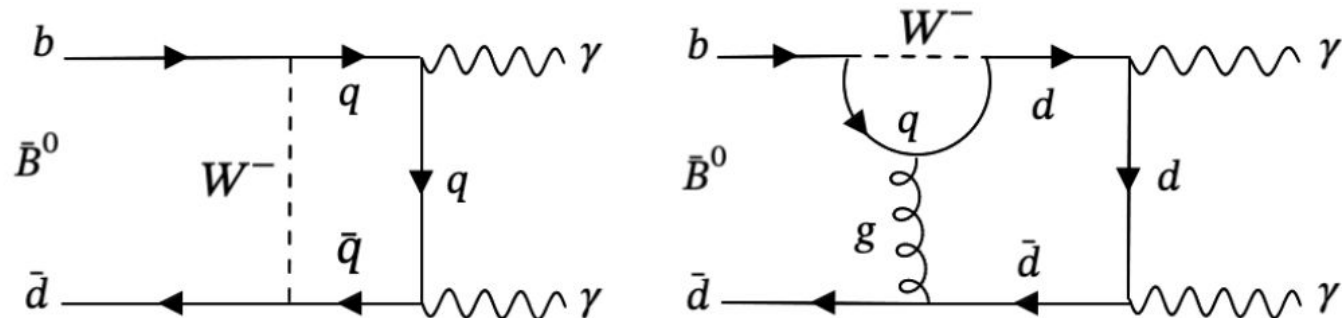
- Inclusive $b \rightarrow s\gamma$ measurement is theoretically clean, especially if performed with low E_γ threshold (large continuum background)
- First analysis performed sometime ago, using hadronic tagging, with promising sensitivity
- Interesting results expected with increased luminosity, a parity between statistical and systematic uncertainty is expected to be reached at about 5 ab^{-1}



Snowmass (arXiv:2207.06307) projections:

Lower E_γ^B threshold	Statistical uncertainty				Baseline (improved) syst. uncertainty
	1 ab^{-1}	5 ab^{-1}	10 ab^{-1}	50 ab^{-1}	
1.4 GeV	10.7%	6.4%	4.7%	2.2%	10.3% (5.2%)
1.6 GeV	9.9%	6.1%	4.5%	2.1%	8.5% (4.2%)
1.8 GeV	9.3%	5.7%	4.2%	2.0%	6.5% (3.2%)
2.0 GeV	8.3%	5.1%	3.8%	1.7%	3.7% (1.8%)

Search for $B^0 \rightarrow \gamma\gamma$

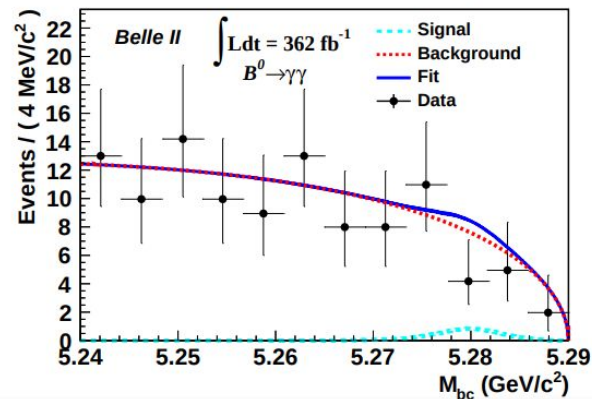
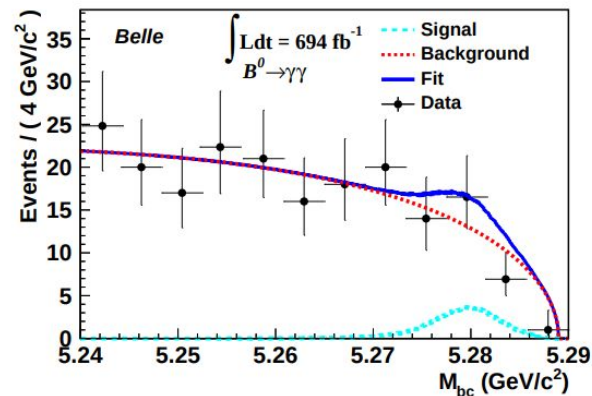


- Analysis based on Belle + Belle II data ($694 \text{ fb}^{-1} + 365 \text{ fb}^{-1}$)
- In SM, suppressed vs $B_s \rightarrow \gamma\gamma$ as $|V_{td}|/|V_{ts}| = 0.04$.
- Penguin diagram contains sizable long-distance contribution: large SM uncertainties
- $B_{SM} = (1.4^{+1.4}_{-0.8}) \times 10^{-8}$ (JHEP12(2020)169)

Search for $B^0 \rightarrow \gamma\gamma$

	$\mathcal{B}(B^0 \rightarrow \gamma\gamma)$	UL on $\mathcal{B}(B^0 \rightarrow \gamma\gamma)$
Belle	$(5.4_{-2.6}^{+3.3} \pm 0.5) \times 10^{-8}$	$< 9.9 \times 10^{-8}$
Belle II	$(1.7_{-2.4}^{+3.7} \pm 0.3) \times 10^{-8}$	$< 7.4 \times 10^{-8}$
Combined	$(3.7_{-1.8}^{+2.2} \pm 0.5) \times 10^{-8}$	$< 6.4 \times 10^{-8}$

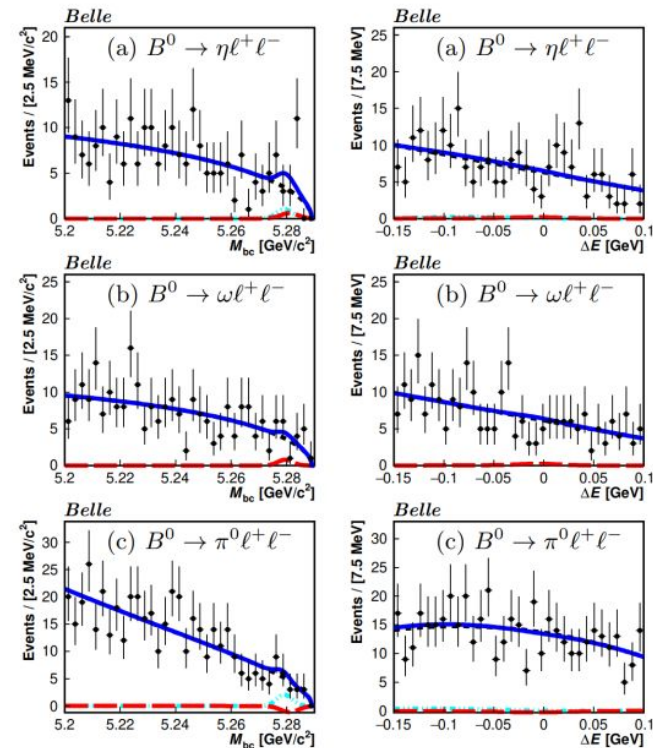
- Dominant background from continuum, suppressed by MVA classifier
- 3D unbinned fit to M_{bc} , ΔE and classifier output
- Comparable sensitivity for Belle and Belle II data
- Consistent with no signal at 2σ level, significantly better vs previous Belle and BaBar results
- Approaching SM sensitivity



Belle searches for $b \rightarrow d$ ll transitions

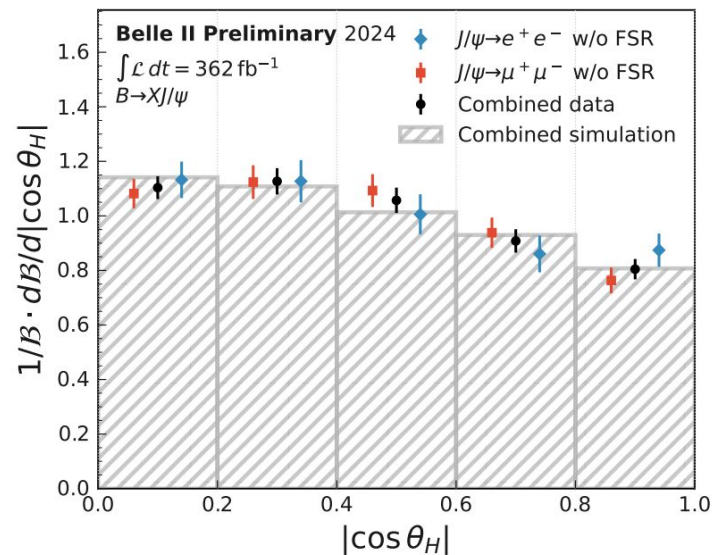
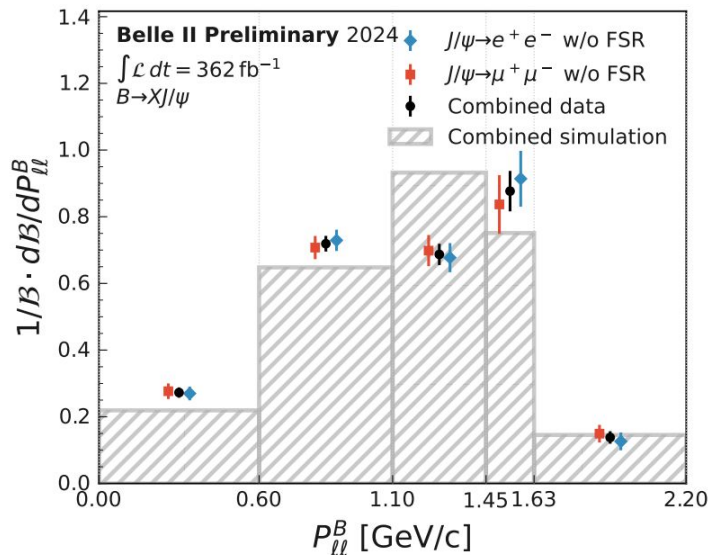
- Analysis using full Belle data sample (711 fb^{-1})
- Focusing on channels complementary to LHCb (with e, π^0 in final state)
- 2D unbinned fit to M_{bc} ΔE
- Best or first results for a number of channels.

Channel	$\mathcal{B}^{UL} (10^{-8})$
$B^0 \rightarrow \eta e^+ e^-$	< 10.5
$B^0 \rightarrow \eta \mu^+ \mu^-$	< 9.4
$B^0 \rightarrow \eta \ell^+ \ell^-$	< 4.8
$B^0 \rightarrow \omega e^+ e^-$	< 30.7
$B^0 \rightarrow \omega \mu^+ \mu^-$	< 24.9
$B^0 \rightarrow \omega \ell^+ \ell^-$	< 22.0
$B^0 \rightarrow \pi^0 e^+ e^-$	< 7.9
$B^0 \rightarrow \pi^0 \mu^+ \mu^-$	< 5.9
$B^0 \rightarrow \pi^0 \ell^+ \ell^-$	< 3.8
$B^+ \rightarrow \pi^+ e^+ e^-$	< 5.4
$B^0 \rightarrow \rho^0 e^+ e^-$	45.5
$B^+ \rightarrow \rho^+ e^+ e^-$	< 46.7
$B^+ \rightarrow \rho^+ \mu^+ \mu^-$	< 38.1
$B^+ \rightarrow \rho^+ \ell^+ \ell^-$	< 18.9



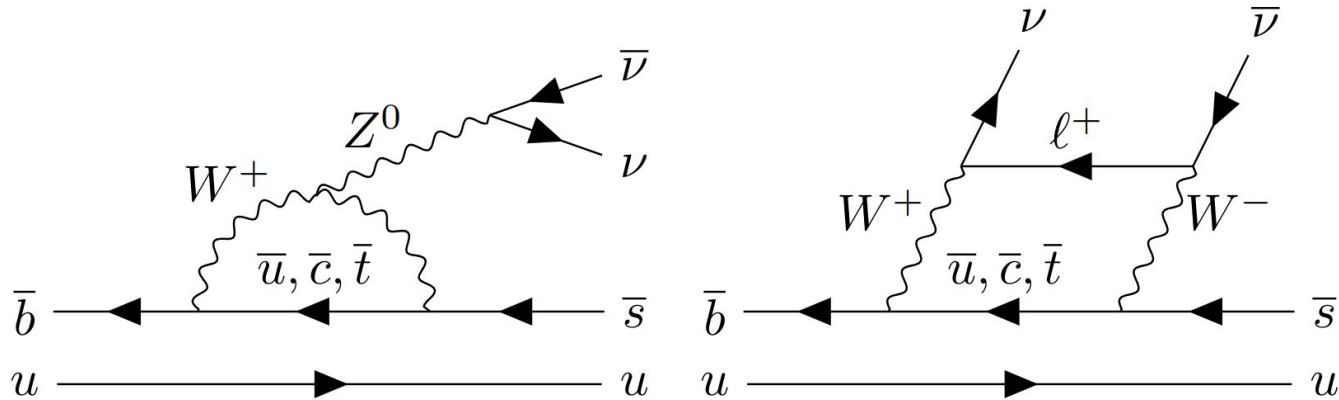
Measurement of inclusive $B \rightarrow J/\psi X$

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- Belle II analysis of inclusive $B \rightarrow J/\psi X$ production employing hadronic tag for companion B
- Differential measurement of the J/ψ momentum and polarization
- Useful as a control channel for (semi) inclusive $B \rightarrow X \ell \ell$ and $B \rightarrow X \nu \nu$ measurements.

Search for $B^+ \rightarrow K^+ \nu \nu$ motivation

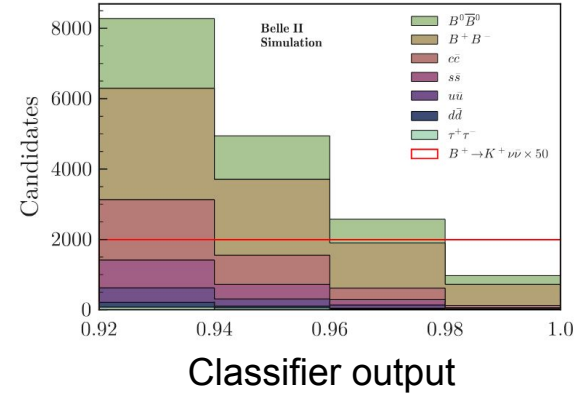
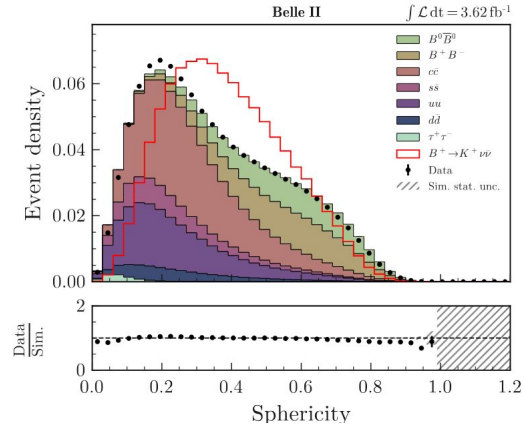
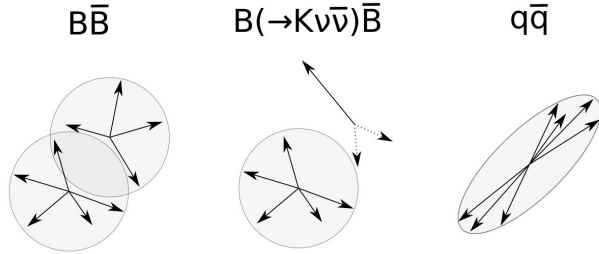


- The $B \rightarrow K^+ \nu \nu$ process is known with high accuracy in the SM:

$$B(B \rightarrow K^+ \nu \nu) = (5.6 \pm 0.4) \times 10^{-6} \quad (\text{arXiv:2207.13371})$$

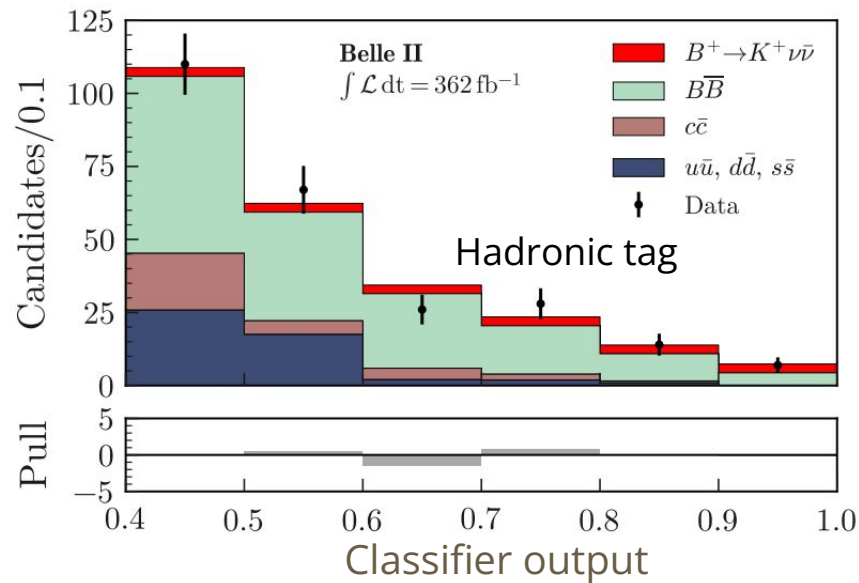
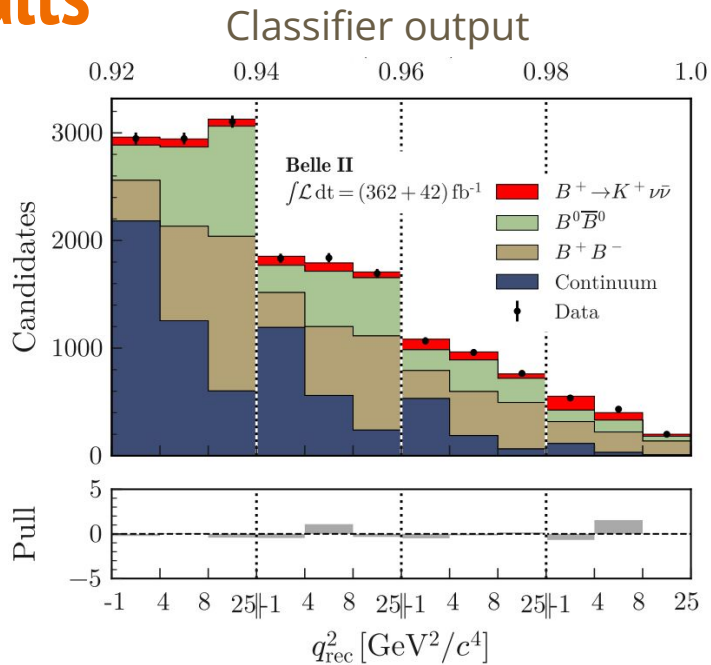
- Extensions **beyond SM** may lead to significant rate increase
- **Very challenging** experimentally, not yet observed
 - Low branching fraction, high background contributions
 - 3-body kinematics, no good kinematic variable to fit
- Unique for Belle II

Analysis strategy



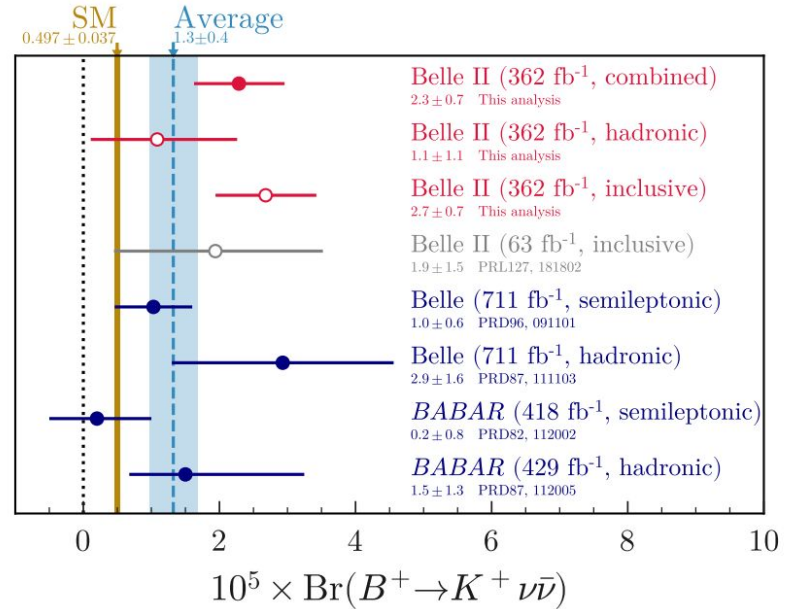
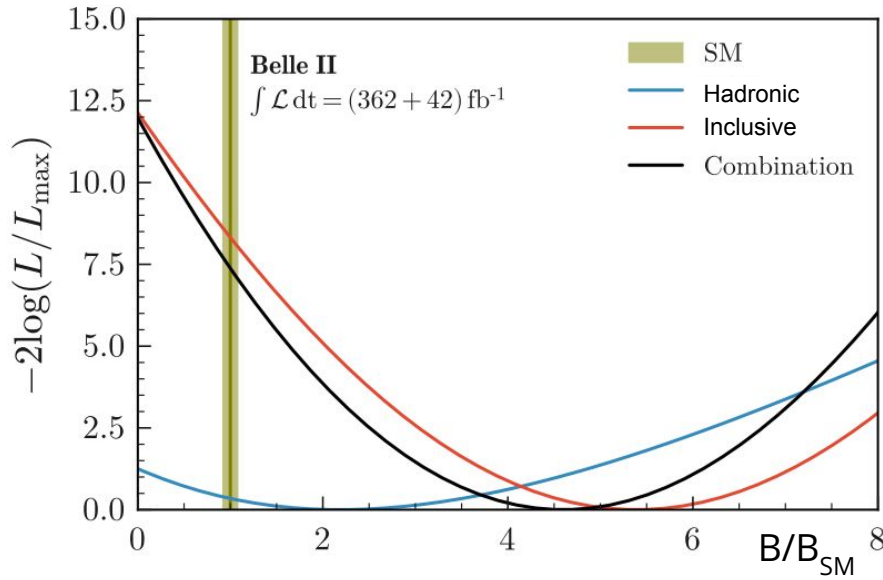
- Two analyses: more sensitive **inclusive** (total efficiency: 8%) and conventional **hadronic** tagging (total efficiency: 0.4%)
- Use event properties to suppress background with multiple variables combined
- Use classifier output as (one of) the fit variable(s), use **simulation** for signal and background templates
- Use multiple control channels to validate simulation with data

Results



- Maximum likelihood fit to data using signal and background templates
- Branching fractions: $B_{\text{incl.}} = (2.7 \pm 0.5(\text{stat}) \pm 0.5(\text{stat})) \times 10^{-5}$, $B_{\text{had.}} = (1.1^{+0.9}_{-0.8}(\text{stat})^{+0.8}_{-0.5}(\text{syst})) \times 10^{-5}$
- For inclusive analysis, **evidence for $B \rightarrow K \nu \nu$ at 3.5σ** , branching fraction within **2.9σ** of standard model (both considering total uncertainty)
- For hadronic tag, the result is consistent with null hypothesis and SM at 1.1σ and 0.6σ

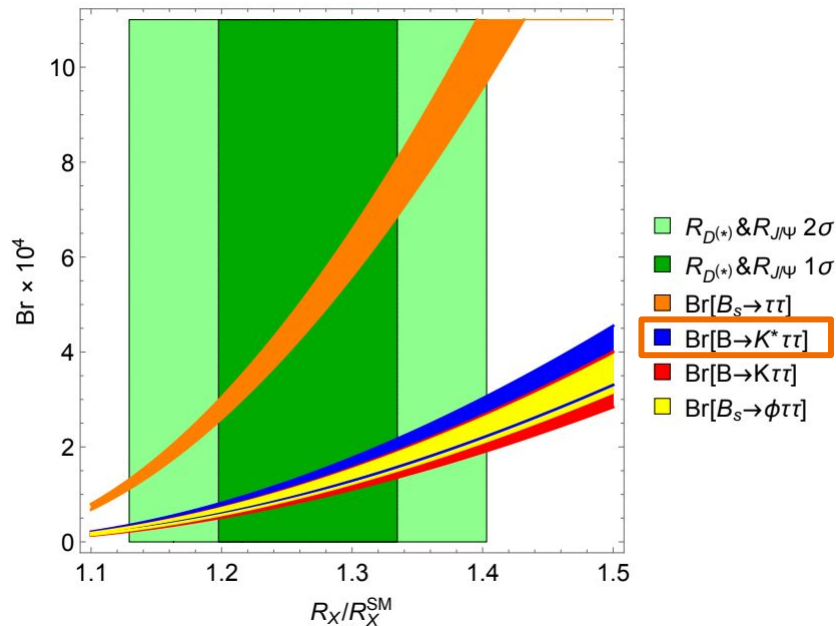
Combination and comparison with other measurements



- Inclusive and hadronic measurements are combined, taking into account common correlated uncertainties. The resulting branching fraction is $\mathbf{B_{comb}(B^+ \rightarrow K^+ \nu \bar{\nu}) = (2.3 \pm 0.7) \times 10^{-5} = [2.4 \pm 0.5(\text{stat})^{+0.5}_{-0.4}(\text{syst})] \times 10^{-5}}$ significance of **observation** is **3.5 σ** the result is within **2.7 σ** vs standard model
- Some tensions between inclusive and semileptonic results for Belle and BaBar, however overall compatibility of the results is good with $\chi^2/\text{dof} = 5.6/5$

Search for $B^0 \rightarrow K^{*0} \tau \tau$

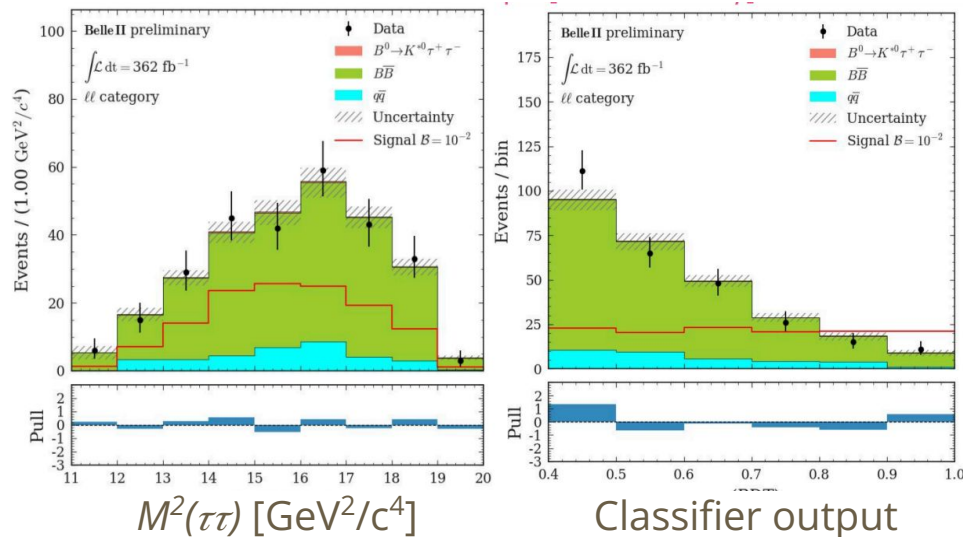
- Very small branching fraction in SM: 1×10^{-7}
- However, NP models that describe $b \rightarrow c \tau l$ anomalies (" R_X ") may generate $\times 10^4$ increase in the branching fraction
- Experimentally very challenging
 - Low efficiency
 - A lot of missing energy
 - Large backgrounds
 - Low K^{*0} momentum
- Last limit from Belle based on 711 fb^{-1} : $< 3.1 \times 10^{-3}$ @90% CL (PRD 108 011102 (2023))



Search for $B^0 \rightarrow K^{*0} \tau \tau$

- Analyses uses hadronic tagging for companion B, based on 365 fb^{-1} Belle II data.
 - Several τ decays considered: ll , $l\pi$, $\pi\pi$, $\rho\pi$. The best sensitivity for ll channel
 - Binned likelihood fit to MVA classifier output (BDT), that is trained using missing energy, extra energy in the calorimeter, etc.
 - Multiple validation channels
 - Main backgrounds from B decays
- Twice better limit vs Belle due to better tagging efficiency, more τ decay channels, MVA.

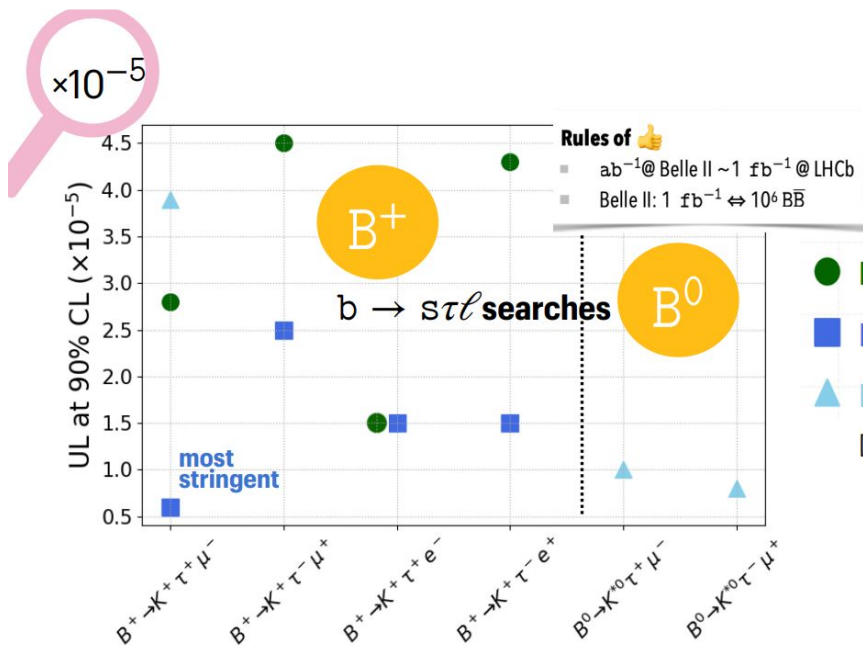
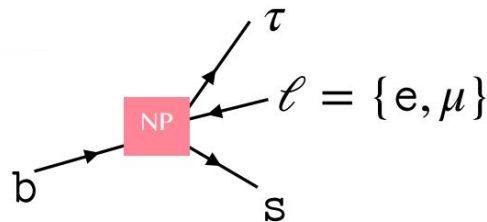
ICHEP 24



$$B(B \rightarrow K^{*0} \tau \tau) < 1.8 \times 10^{-3} \text{ at } 90\% \text{ CL}$$

Search for forbidden $B^0 \rightarrow K_S \tau \ell$

- $R(X)$ anomalies and $B(B^+ \rightarrow K^+ \nu \nu)$ excess can be explained by a new heavy particles coupled differently to 3rd generation leptons
- BSM Models can generate LFV decays with branching fractions $\sim 10^{-5}$
- Recent experimental limits approach their level



- **BaBar** (428 fb^{-1}) $B^+ \rightarrow K^+ \tau^\pm \ell^\mp$ [PRD86, 012004, 2012]
- **Belle** (711 fb^{-1}) $B^+ \rightarrow K^+ \tau^\pm \ell^\mp$ [PRL130, 261802, 2023]
- ▲ **LHCb** (9 fb^{-1}) $B^+ \rightarrow K^+ \tau^+ \mu^-$, $B^0 \rightarrow K^{*0} \tau^\pm \mu^\mp$ [JHEP06,129,2020] [JHEP06,143,2023]

No search yet in $B^0 \rightarrow K_S^0 \tau^\pm \ell^\mp$

Search for forbidden $B^0 \rightarrow K_S \tau l$

- Analysis based on Belle and Belle II data sample (711 and 365 fb⁻¹)
- Hadronic tagging employed for companion B^0 , its kinematics plus signal K_S and l are used to reconstruct τ mass, used as the fit variable
- Four channels considered, with e and μ leptons separated in different charges. τ one-prong decays into μ , e and π are used.
- Dedicated veto for semileptonic decays plus BDT for other backgrounds.

$$\mathcal{B}(B^0 \rightarrow K_S^0 \tau^+ \mu^-) < 1.1 \times 10^{-5}$$

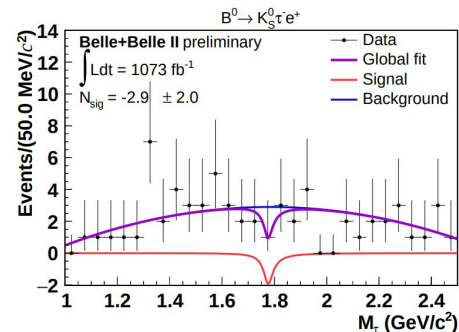
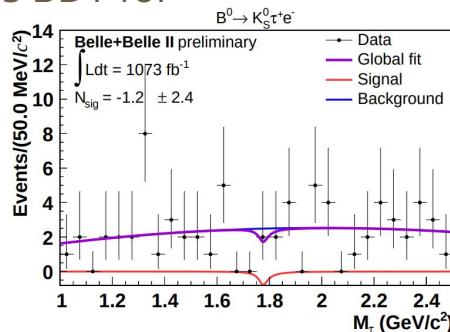
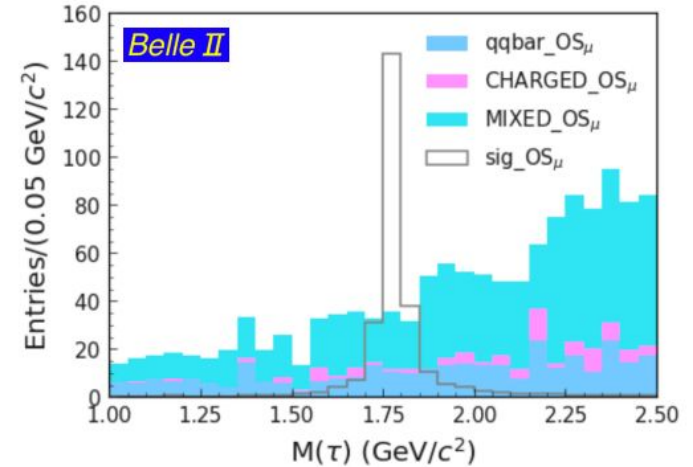
$$\mathcal{B}(B^0 \rightarrow K_S^0 \tau^- \mu^+) < 3.6 \times 10^{-5}$$

$$\mathcal{B}(B^0 \rightarrow K_S^0 \tau^+ e^-) < 1.5 \times 10^{-5}$$

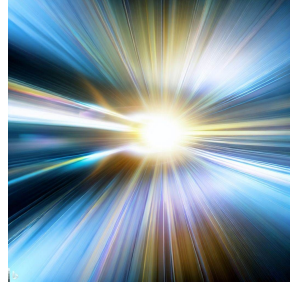
$$\mathcal{B}(B^0 \rightarrow K_S^0 \tau^- e^+) < 0.8 \times 10^{-5}$$

Comparable to the best existing limits

$$M_\tau = \left[m_{B_{\text{DVT}}}^2 + m_{K_\ell}^2 - 2 \left(E_B^* E_{K_\ell}^* + |\vec{p}_B^*| |\vec{p}_{K_\ell}^*| \cos \theta \right) \right]^{\frac{1}{2}}$$



Summary

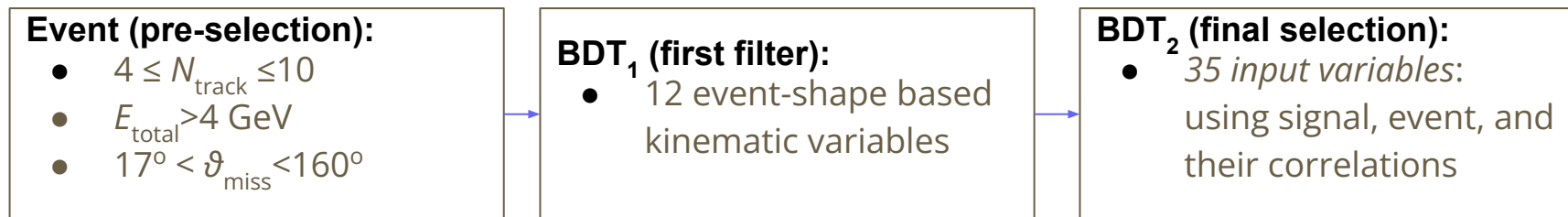


- SuperKEKB and Belle II provide unique opportunities for studies of $b \rightarrow s(d)$ transitions
- Many new results in the recent years, focused on the strengths of the detector: inclusive measurements, final states including photons, electrons and missing energy,
- Evidence for $B^+ \rightarrow K^+ \nu \nu$ decay with a branching fraction 2.7 standard deviations above the standard model
- Best limit for $B \rightarrow \gamma \gamma$, approaching SM sensitivity
- Precision measurements of radiative $B \rightarrow K^* \gamma$ decays
- First results on $b \rightarrow d ll$ transitions from Belle and combined analysis of $B \rightarrow \rho \gamma$
- Best limits for $B^0 \rightarrow K^{*0} \tau \tau$
- First search for $B^0 \rightarrow K_S^0 \tau l$, sensitivity similar to other similar channels with LFV

Backup

Reconstruction and background suppression

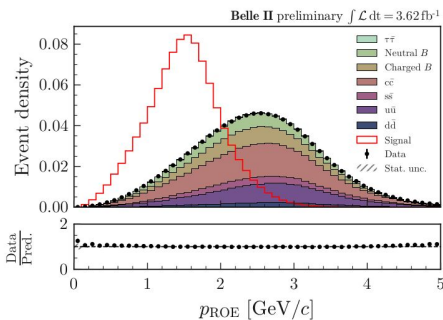
- Selection criteria for particles to ensure high and well-measured efficiency:
 - charged particle momenta and neutral particle energies greater than 100 MeV
 - only in central region
 - charged particles consistent with being from interaction point
- **Signal candidate:**
 - an identified charged kaon that gives the minimal mass of the neutrino pair q_{rec}^2 (computed as K^+ recoil)



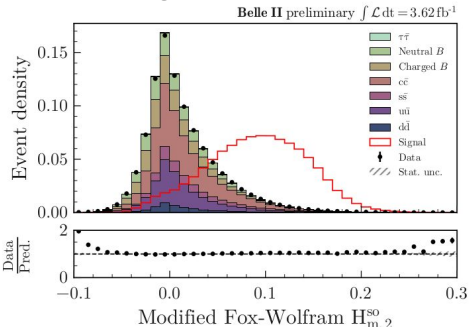
- **Three-step filter:** basic event cuts, BDT-based filter (BDT₁) and final selection (BDT₂). BDT₂ improves performance in terms of $s/\sqrt{s+b}$ by almost factor 3

Examples of input variables for BDT₁ and BDT₂

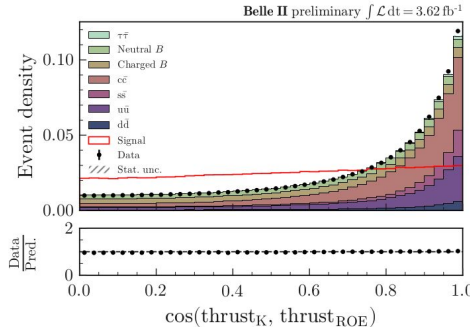
Recoil momentum



"Missing momentum"

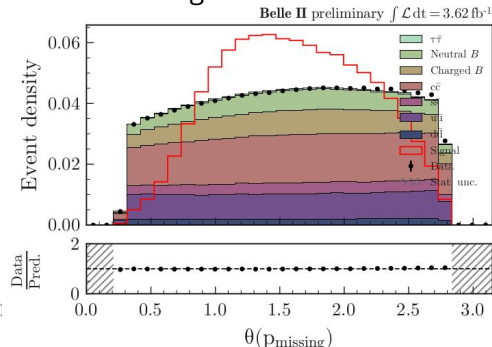


Spherical

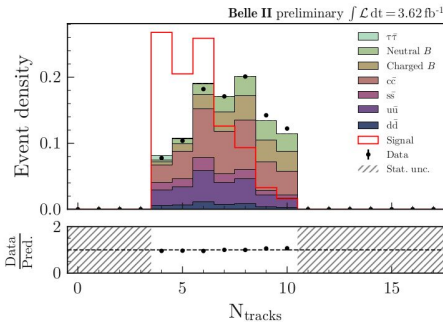


Jet-like

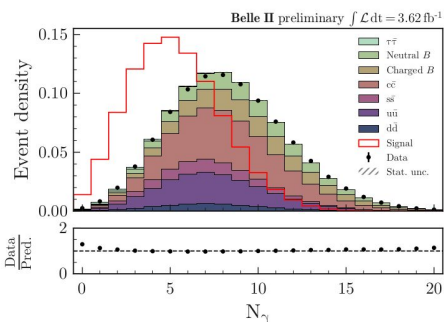
Missing momentum direction



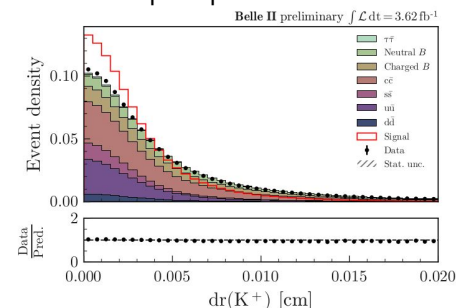
Number of tracks



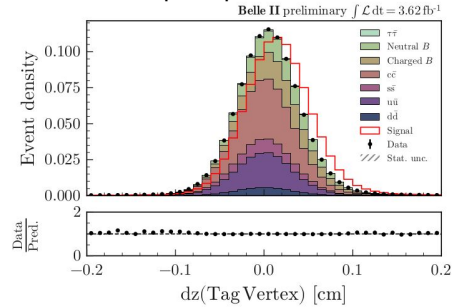
Number of neutrals



K⁺ impact parameter

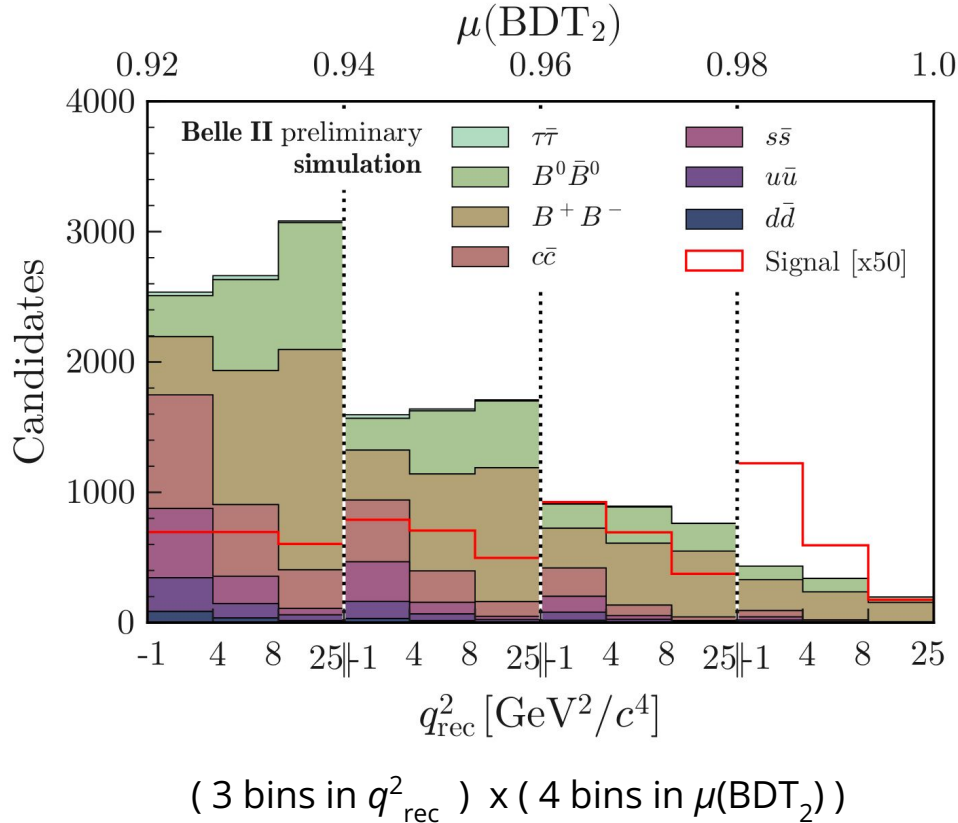


Recoil impact parameter



- Example of input distributions at pre-selection level, 1% of data, with detector-level corrections applied but no physics modeling corrections
- Each variable is examined to have reasonable description by simulation and significant separation power

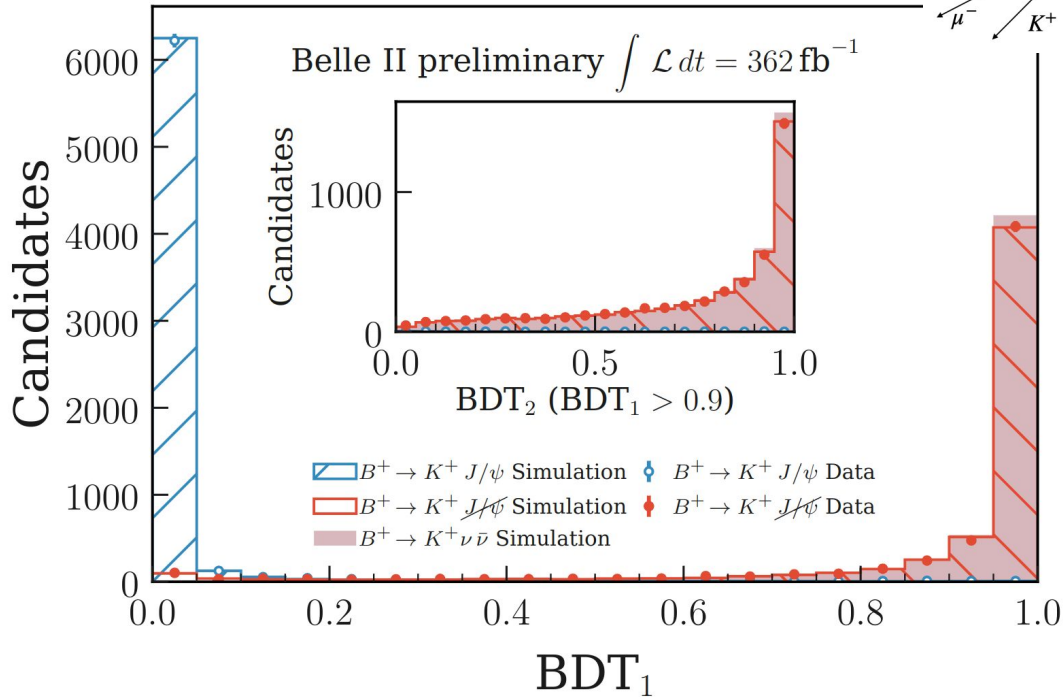
Signal extraction



- Define the signal region at the plateau of the classifier sensitivity which corresponds to signal efficiency of **8%**
- Further subdivide it in 4 bins of classifier output $\mu(\text{BDT}_2)$ and 3 bins in q_{rec}^2
- Binned profile maximum likelihood fit to data using **signal** and **7** background templates
- Systematic uncertainties varied in the fit

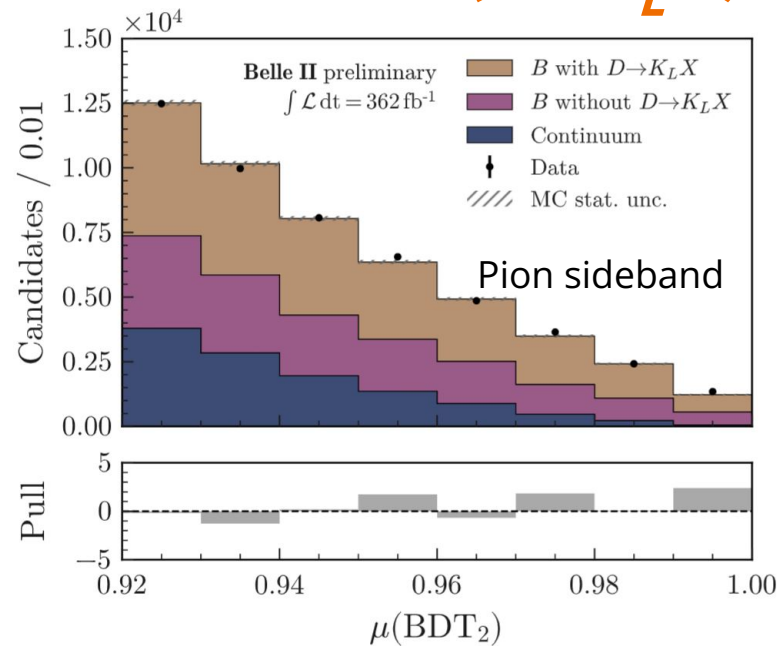
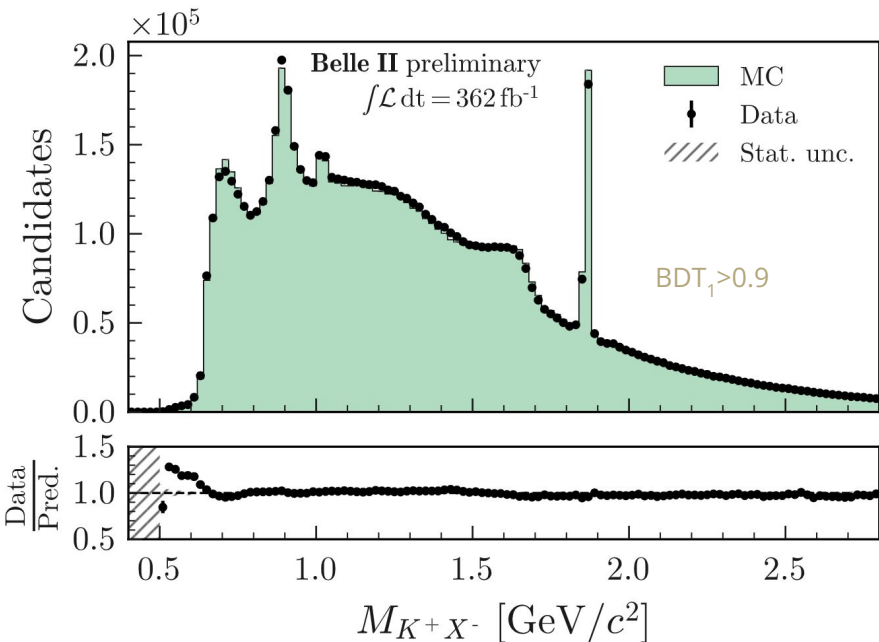
Main backgrounds are from neutral and charged B decays; continuum sources are checked/constraint using data taken below $Y(4S)$ resonance.

Signal efficiency validation



- Use cleanly reconstructed $B^+ \rightarrow K^+ J/\psi (\rightarrow \mu^+ \mu^-)$ decays with $\mu^+ \mu^-$ pair removed and K^+ kinematics adjusted to validate the **signal efficiency** in simulation. The ratio of data/simulation efficiency in the signal region is **1.00 ± 0.03**

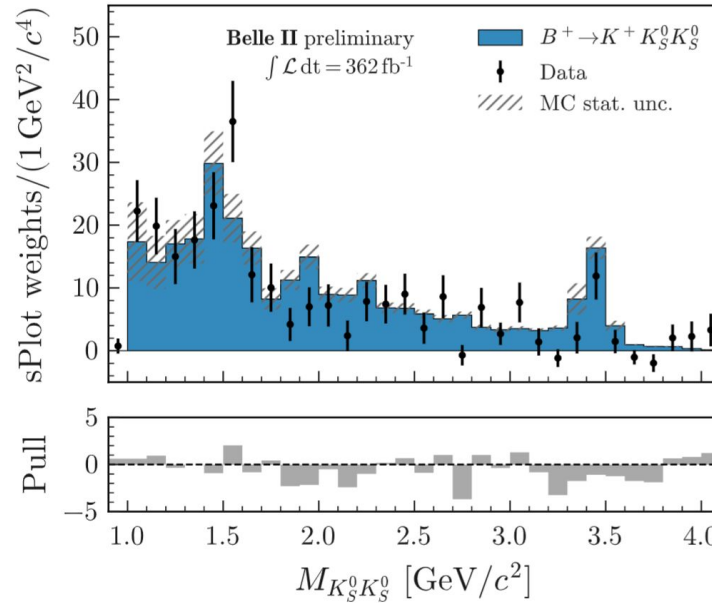
Background from $B \rightarrow D(\rightarrow K^+ X) l \nu$ and $B \rightarrow K^+ D(\rightarrow K_L X)$



- Main backgrounds: semileptonic $B \rightarrow D(\rightarrow K^+ X) l \nu$ decays and prompt $B \rightarrow K^+ X$ production (>90%)
- Semileptonic decays suppressed by several MVA variables, checked at each selection step
- Prompt K^+ production studied using prompt π^+ from $B^+ \rightarrow \pi^+ X$ (and l^+ from $B^+ \rightarrow l^+ X$) decays
- Systematic uncertainties on decay branching fractions, enlarged for $D(\rightarrow K_L X)$ and $B \rightarrow D^{**} l \nu$

Background from $B^+ \rightarrow K^+ K^0 K^0$

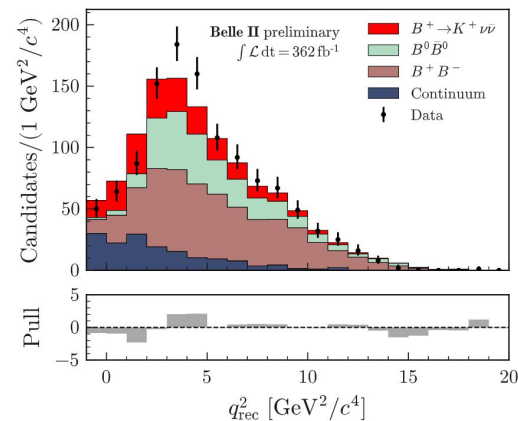
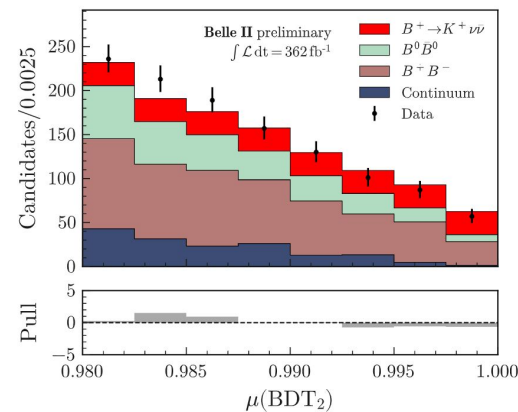
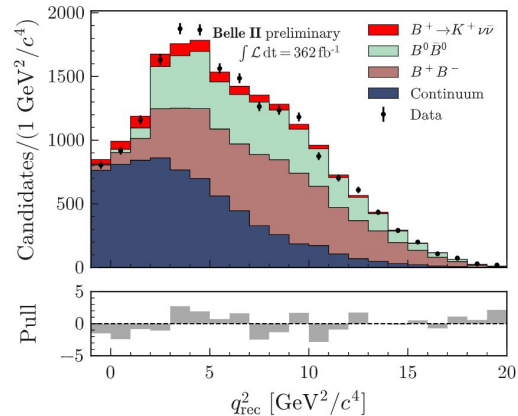
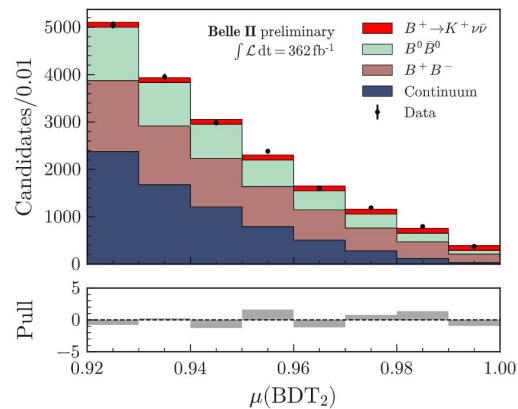
Most signal-like backgrounds



$\leftarrow B^+ \rightarrow K^+ K_S K_S$ decays

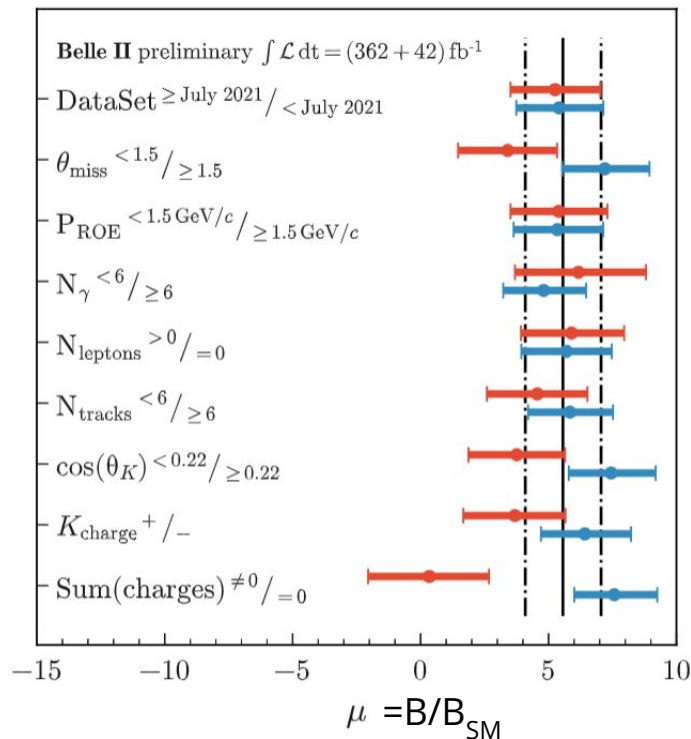
- Backgrounds from $B^+ \rightarrow K^+ nn$ and $B^+ \rightarrow K^+ K^0 K^0$ have branching fractions of few $\times 10^{-5}$, however K_L and neutrons can **escape** EM calorimeter
- $B^+ \rightarrow K^+ K^0 K^0$ modeled based on BaBar analysis ([arXiv:1201.5897](https://arxiv.org/abs/1201.5897))
- Dedicated checks of K_L 's **performance** in calorimeter using radiative φ production
- Dedicated checks using $B^+ \rightarrow K^+ K_S K_S$ and $B^0 \rightarrow K_S K^+ K^-$ control channels

Post-fit distributions for inclusive analysis

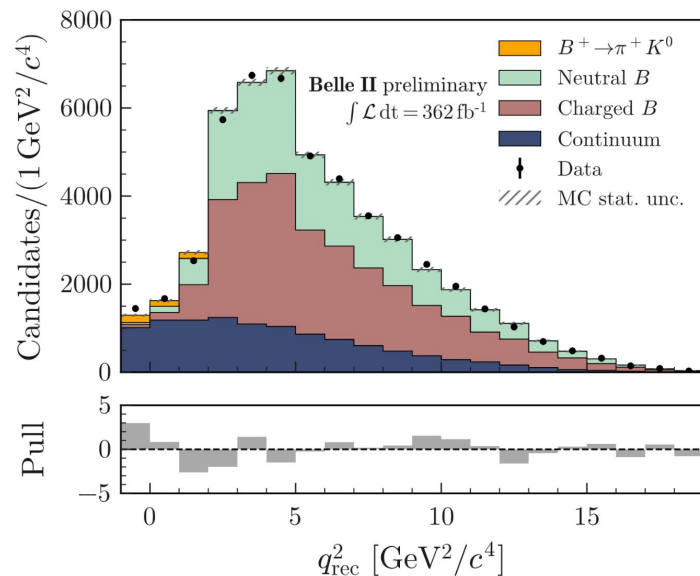


- Post-fit distributions for the inclusive analysis shown for the signal region and separately for the region with maximal sensitivity, $\mu(\text{BDT}_2) > 0.98$

Cross checks



- Multiple checks of the analyses stability, including tests dividing data into approximately equal sub-samples. Reported here as measured branching fraction divided by SM expectation, $\mu = B/B_{\text{SM}}$.
- Control measurement of $B^+ \rightarrow \pi^+ K^0$ decay



$$B(B^+ \rightarrow \pi^+ K^0) = (2.5 \pm 0.5) \times 10^{-5}$$

$$\text{PDG: } (2.38 \pm 0.08) \times 10^{-5}$$

Systematic uncertainties of the inclusive analysis

Source	Correction	Uncertainty type	Uncertainty size	Impact on σ_μ
Normalization of $B\bar{B}$ background	—	Global, 2 NP	50%	0.88
Normalization of continuum background	—	Global, 5 NP	50%	0.10
Leading B -decays branching fractions	—	Shape, 5 NP	$O(1\%)$	0.22
Branching fraction for $B^+ \rightarrow K^+ K_L^0 K_L^0$	q^2 dependent $O(100\%)$	Shape, 1 NP	20%	0.49
p -wave component for $B^+ \rightarrow K^+ K_S^0 K_L^0$	q^2 dependent $O(100\%)$	Shape, 1 NP	30%	0.02
Branching fraction for $B \rightarrow D^{(**)}$	—	Shape, 1 NP	50%	0.42
Branching fraction for $B^+ \rightarrow n\bar{n}K^+$	q^2 dependent $O(100\%)$	Shape, 1 NP	100%	0.20
Branching fraction for $D \rightarrow K_L X$	+30%	Shape, 1 NP	10%	0.14
Continuum background modeling, BDT_c	Multivariate $O(10\%)$	Shape, 1 NP	100% of correction	0.01
Integrated luminosity	—	Global, 1 NP	1%	< 0.01
Number of $B\bar{B}$	—	Global, 1 NP	1.5%	0.02
Off-resonance sample normalization	—	Global, 1 NP	5%	0.05
Track finding efficiency	—	Shape, 1 NP	0.3%	0.20
Signal kaon PID	p, θ dependent $O(10 - 100\%)$	Shape, 7 NP	$O(1\%)$	0.07
Photon energy scale	—	Shape, 1 NP	0.5%	0.08
Hadronic energy scale	-10%	Shape, 1 NP	10%	0.36
K_L^0 efficiency in ECL	-17%	Shape, 1 NP	8%	0.21
Signal SM form factors	q^2 dependent $O(1\%)$	Shape, 3 NP	$O(1\%)$	0.02
Global signal efficiency	—	Global, 1 NP	3%	0.03
MC statistics	—	Shape, 156 NP	$O(1\%)$	0.52